Formation of Complex Organic Molecules in Cold Interstellar Environments through Nondiffusive Grain-surface and Ice-mantle Chemistry

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Abstract

A prevailing theory for the interstellar production of complex organic molecules (COMs) involves formation on warm dust-grain surfaces, via the diffusion and reaction of radicals produced through grain-surface photodissociation of stable molecules. However, some gas-phase O-bearing COMs, notably acetaldehyde (CH3CHO), methyl formate (CH3OCHO), and dimethyl ether (CH3OCH3), are now observed at very low temperatures, challenging the warm scenario. Here, we introduce a selection of new nondiffusive mechanisms into an astrochemical model to account for the failure of the standard diffusive picture and to provide a more generalized scenario of COM formation on interstellar grains. New generic rate formulations are provided for cases where (i) radicals are formed by reactions occurring close to another reactant, producing an immediate follow-on reaction; (ii) radicals are formed in an excited state, allowing them to overcome activation barriers to react with nearby stable molecules; and (iii) radicals are formed through photodissociation close to a reaction partner, followed by immediate reaction. Each process occurs without thermal diffusion of large radicals. The new mechanisms significantly enhance cold COM abundances, successfully reproducing key observational results for prestellar core L1544. H abstraction from grain-surface COMs, followed by recombination, plays a crucial role in amplifying chemical desorption into the gas phase. The ultraviolet-induced chemistry produces significant COM abundances in the bulk ices, which are retained on the grains and may persist to later stages. O2 is also formed strongly in the mantle though photolysis, suggesting cometary O2 could indeed be interstellar.

Unified Astronomy Thesaurus concepts: Astrochemistry (75); Interstellar dust processes (838); Star formation (1569); Molecule formation (2076)

Supporting material: machine-readable table

1. Introduction

Complex organic molecules (COMs), usually defined as carbon-bearing molecules with six or more atoms, have been detected within the interstellar medium and in various protoplanetary environments (Blake et al. 1987; Arce et al. 2008; Bottinelli et al. 2010; Öberg et al. 2010; Bacmann et al. 2012; Fuyolle et al. 2015). COMs synthesized at the early stages of star formation are suggested to have been a starting point for the organic materials that went on to seed the nascent solar system (Herbst & van Dishoeck 2009). While the degree to which the interstellar synthesis of COMs may contribute to prebiotic/biotic chemistry on Earth is still a matter of debate, many recent studies have shed light on the possible interstellar/protostellar origins of chemical complexity. For instance, the sugar-like molecule glycolaldehyde (CH2(OH)CHO) has been detected toward the class 0 protostellar binary source IRAS 16293-2422 (Jørgensen et al. 2012), as well as the Galactic Centre source Sgr B2(N) and other hot cores (Hollis et al. 2000; Beltrán et al. 2009). A related molecule, ethylene glycol (HOCH2CH2OH), has also been found toward low-mass protostars (Maury et al. 2014; Jørgensen et al. 2016), having first been detected in Sgr B2(N) (Hollis et al. 2002). The simplest amino acid, glycine (NH2CH2COOH), has not been detected in the interstellar medium, but numerous amino acids have been found in meteorites (Kvenvolden et al. 1970), and glycine has been detected in two comets: Wild 2 (Elsila et al. 2009) and Churyumov–Gerasimenko (Altweig et al. 2016). In the laboratory, Meinert et al. (2016) observed the generation of numerous sugar molecules, including the aldopentose ribose, through photochemical and thermal processing of interstellar ice analogs initially composed of H2O, CH3OH, and NH3. One of the prevailing theories explaining the formation of interstellar COMs is based on radical chemistry occurring on dust-grain particles, following the formation of ice mantles on their surfaces. In dark clouds and prestellar cores, where temperatures may be as low as around 10 K, hydrogen atoms are the most mobile species on the grain. Their high mobility allows them to find reaction partners on the surface easily. Thus, the accretion of other atoms and simple molecules, such as O, C, N, and CO, onto the grain surfaces often leads to reactions with atomic H, producing an ice mantle composed of commonly observed stable hydrides like water, methane, and ammonia, through repetitive hydrogenation. In dense regions, almost all of the CO produced in the gas phase may ultimately freeze out onto the dust grains (e.g., Caselli et al. 1999), producing an outer ice surface that is rich in CO. Atomic H may also react with CO to produce methanol (CH3OH); although there are activation-energy barriers that prevent all of this CO from being hydrogenated, a substantial fraction of the ice—up to as much as around 30% with respect to water—toward some protostars, but generally of the order of 5% (Boogert et al. 2015)—is found observationally to be composed of CH3OH.

Grain-surface methanol, and indeed other molecules, may be broken down into radicals through ultraviolet (UV)-induced photolysis, caused either by external photons or by the secondary UV field induced by cosmic-ray collisions with gas-phase H2; however, in the standard picture used in most
astrochemical models, these radicals are still immobile on the
grain surfaces at low temperatures, hindering their ability to
react with anything other than mobile H atoms. As a star-
forming core evolves to be heated to temperatures greater than
∼20 K, radicals such as CH₃ and HCO become more mobile,
allowing them to meet via diffusion and quickly react to form
larger COMs (Garrod & Herbst 2006; Garrod et al. 2008). At
this stage, most of the COMs produced in this way are unable
to desorb effectively into the gas phase where they may be
directly detected; only nonthermal mechanisms such as
chemical desorption (Garrod et al. 2007) and photodesorption
(Öberg et al. 2009a, 2009b) are active, with the former
expected to yield only around 1% of reaction products to the
gas phase, while the latter would be weaker still in such regions
where visual extinction is high. Only when the dust grains in
the core reach a high-enough temperature (typically on the
order of ∼100 K), through protostellar heating, can large
COMs sublime efficiently from the grains. This process is
reviewed in more detail by Öberg et al. (2010).

According to this scenario, it would be unlikely that COMs
other than methanol would be effectively synthesized under the
low-temperature conditions of dark clouds and prestellar cores,
due to the immobility of heavy species on the grains, while
methanol would still be formed as the result of the diffusion
and reaction of H alone. The detection of COMs in these cold
environments therefore presents a significant challenge to
current astrochemical models based on diffusive grain-surface
chemistry. In particular, three O-bearing COMs, acetaldehyde
(AA; CH₃CHO), methyl formate (MF; CH₃OCHO), and
dimethyl ether (DME; CH₂OCH₂), have been detected in
prestellar cores such as L1689B, L1544, and B1-b (Bacmann
et al. 2012; Cernicharo et al. 2012; Vastel et al. 2014) as well as
in the cold outer envelopes of protostars (Öberg et al. 2010;
Bergner et al. 2017).

Many chemical mechanisms have been proposed to explain
the presence of COMs in cold cores: the Eley–Rideal (E-R)
process combined with complex-induced reactions on the
grains (Ruaud et al. 2015), nondiffusive reactions (Chang &
Herbst 2016), oxygen insertion reactions (Bergner et al. 2017),
cosmic-ray-induced chemistry (Shingledecker et al. 2018), and
gas-phase formation through radical reactions (Balucani et al.
2015). In particular, the latter gas-phase formation scheme is
noteworthy in that it suggests a chemical link between gas-
phase methyl formate and dimethyl ether via the radical
CH₃OCH₂, which would be formed through the abstraction of a
hydrogen atom from DME by atoms such as F and Cl. The
dimethyl ether itself would form through the efficient radiative
association of the radicals CH₃ and CH₂O in the gas phase.

Although many of the above-mentioned studies provide
plausible routes to one or more complex molecules, some
suffer from poorly constrained parameters due to the lack of
experimental data or detailed computational chemistry studies
(e.g., the radiative association reaction to produce DME), or
require somewhat extreme chemical conditions. For example,
the fractional abundance of methoxy in the model of Balucani
et al. (2015) is more than one order of magnitude larger than
the observed value, making it unclear whether dimethyl ether
can be formed solely in the gas phase in cold cores (Vasyunin
& Herbst 2013; Chang & Herbst 2016). Also, the chemical
networks for F and Cl are relatively sparse, introducing further
uncertainties; the models of Vasyunin et al. (2017) suggest that
OH is instead a more important agent of H abstraction from
dimethyl ether.

Cosmic-ray-induced radiolysis models by Shingledecker
et al. (2018) appear promising, although it is unclear whether
they can account for large abundances of COMs on their own,
or whether they require radicals also to be produced by UV
photons. For example, those authors suggest an average rate of
solid-phase water dissociation by cosmic rays of around
6 × 10⁻¹⁶ s⁻¹ at the canonical cosmic-ray ionization rate.
However, the typically assumed rate used in astrochemical
models for the separate process of UV photodissociation of
gas-phase water by cosmic-ray-induced photons is around
1.3 × 10⁻¹⁴ s⁻¹. Even if the rates of UV photodissociation in
the solid phase are around three times lower than those of gas-
phase molecules (Kalvåns 2018), the influence of cosmic-ray-
induced photons in producing radicals in ice mantles would,
on average, appear to be greater than that of direct cosmic-ray
impingement by close to an order of magnitude. Other
calculations for cosmic-ray-induced water dissociation
(Garrod 2019) would suggest an even greater discrepancy.
The formation of COMs through direct cosmic-ray impacts into
icy grains may therefore rely on the presence of preexisting
radicals produced by cosmic-ray-induced UV.

In order for chemical modeling studies to be directly
comparable with observations, they should ideally seek to
reproduce the spatio-physical conditions of the target source. In
prestellar cores such as L1544, strong gradients in physical
parameters such as dust temperature, density, and visual
extinction may sample a range of chemical regimes. The recent
detection of a chemically active outer shell around the core
center of L1544 sheds light on the complexity of its chemical
structure (Bizzocchi et al. 2014). Methanol column density in
this source appears to peak at a radius around 4000 au distant
from the source center. Abundances of other COMs seem to be
enhanced at this position also (Jiménez-Serra et al. 2016).

The modeling study by Vasyunin et al. (2017) is notable in
its use of an explicit spatio-physical model to perform chemical
modeling of L1544, successfully reproducing a similar feature
to the observed methanol peak. Those authors used a surface-
specific treatment of chemical desorption from grains in which
a pure water-ice surface would allow only minimal desorption
of newly formed molecules, while a more CO-rich surface
would allow molecules including methanol to desorb more
easily. However, the peak fractional abundances of methanol
produced in this model appear high (∼10⁻⁷ with respect to
total hydrogen) compared with the usual values observed in
cold sources (∼10⁻⁸). The efficiency of the chemical
desorption of methanol (which is responsible for its gas-phase
abundance) and many other species on water ice is poorly
constrained by experiment, with an upper limit of 8% for
methanol formed through H addition (Minissale et al. 2016);
thus, there is room for the efficiency of this mechanism to be
varied in models to produce the correct observed quantity.
However, the Vasyunin et al. (2017) models rely on gas-phase
methanol as the feedstock for the production of other, larger
COMs. Lower peak abundances of gas-phase methanol would
almost certainly render the gas-phase routes investigated by
those authors too weak to account for the abundances of DME,
MF, and AA. Furthermore, using gas-phase reactions between
CH and CH₂OH as a mechanism to form CH₃CHO, they
erroneously extrapolated experimental reaction rates deter-
mined at room temperature (Johnson et al. 2000) down to
10 K; this produces impossibly large rate values that are around three orders of magnitude greater than the collisional rates for neutrals at such temperatures. It is unclear how much influence their alternative route for AA production, the radiative association of CH₃ and HCO radicals, would have on that molecule’s peak gas-phase abundance; however, in their network, they assume a rate that is on the order of the collisional rate (i.e., high efficiency), based on high-pressure experiments that would in fact be more representative of collisional (rather than radiative) deexcitation, and which therefore say nothing certain about radiative association. Until detailed calculations for this, or indeed for the radiative association of CH₂O with CH₃, are available, those rates may be considered to be somewhat optimistic.

Recent laboratory results have added new impetus to understanding the behavior of grain-surface chemistry at very low temperatures. Fedoseev et al. (2015, 2017) considered the co-deposition of CO and H at low temperatures, resulting in significant production of complex organics such as glycolaldehyde, ethylene glycol, and glycerol. They postulate that reactions between adjacent HCO radicals, and/or HCO and CO, may produce such species with minimal thermal diffusion required—a result not predicted by standard gas-grain chemical models, due to the lack of diffusion involved. So-called microscopic Monte Carlo models, unlike the more usual rate-equation models, are capable of simulating the relative positions of all atoms and molecules on a grain surface at each moment, allowing them automatically to account for this nondiffusive process. Such models seem to indicate that COM production through nondiffusive mechanisms is plausible (Fedoseev et al. 2015; Chang & Herbst 2016; Dulieu et al. 2019; R. T. Garrod et al. 2020, in preparation; Ioppolo et al. 2020, submitted).

It would appear, therefore, that—regardless of other mechanisms such as gas-phase processes or radiolysis—the standard rate description of grain-surface reactions is insufficient to treat all temperature regimes; there are situations in which reactants may be produced and rapidly meet (and react), either without diffusion of radicals or with some minimal amount of diffusion that does not obey the more general rate treatment.

In this study, we present a relatively simple formulation for nondiffusive chemistry, for use in standard gas-grain chemical models, that allows a newly formed reaction product to react further with some other chemical species that happens to be in close proximity to the product(s) of the first reaction. Due to the instantaneous nature of this process, we refer to it here as a “three-body reaction mechanism” (3-B). We also consider a similar, related mechanism in which the new product has sufficient excitation energy to allow it to overcome the activation-energy barrier to its reaction with some nearby species—here, specifically with CO or H₂CO. This mechanism is referred to here as the “three-body excited-formation mechanism” (3-BEF).

A functionally similar mechanism was included in the recent model of the solid-phase chemistry of cometary nuclei by Garrod (2019), but rather with the initiating process being the production of radicals by UV-induced photodissociation. In preliminary versions of that model that did not include that mechanism, it was found that the photodissociation of bulk-ice molecules at temperatures 5–10 K was capable of producing implausibly high abundances of reactive radicals, which were unable to react due to the lack of bulk thermal diffusion at those temperatures. The Garrod (2019) model includes a new reaction process whereby a newly formed photoproduct may react immediately with a nearby reaction partner in the ice. This mechanism is included in the present model also, which we label as the “photodissociation-induced reaction mechanism” (PDI).

Garrod & Pauly (2011) used a similar mechanism to the three-body mechanisms to explain the formation of CO₂ ice at low temperatures. In their treatment, the production of an OH radical via the reaction of H and O atoms in proximity to a CO molecule could allow the immediate formation of CO₂ (overcoming a modest activation-energy barrier). Their models successfully reproduced the observed behavior of CO, CO₂, and water ice in dense clouds, and showed that such nondiffusive processes could be handled within a standard gas-grain chemical model. More recently, Chang & Herbst (2016) implemented a similar process, which they called a “chain reaction mechanism” in their microscopic Monte Carlo simulation, achieving abundances of gas-phase COMs high enough to reproduce the observational values toward cold cores (at a temperature of ~10 K), using a chemical desorption efficiency of 10% per reaction. Dulieu et al. (2019), seeking to explain the surface production of NH₂CHO in laboratory experiments involving H₂CO, NO, and H deposition, introduced a nondiffusive reaction treatment for a single reaction (see also Section 2.4).

Finally, a simple treatment for the E-R process is included in the present model, in which an atom or molecule from the gas phase is accreted directly onto a grain-surface reaction partner, resulting in immediate reaction (mediated by an activation-energy barrier, where appropriate). Such processes have been included in similar models before (e.g.,Ruaud et al. 2015), but are included here for completeness in the consideration of all mechanisms by which reactants may instantly be brought together without a mediating diffusion mechanism.

The formulations presented here for the above processes also allow, through a repetitive application of the main nondiffusive reaction process (i.e., the three-body mechanism), for the products of each of those processes themselves to be involved in further nondiffusive reaction events (in cases where such processes are allowed by the reaction network). Thus, for example, an E-R reaction may be followed by an immediate secondary nondiffusive reaction. The importance of such repetitive processes will diminish with each iteration.

All of the above nondiffusive reaction mechanisms are considered in the model, with a particular emphasis on the production of the O-bearing COMs that are now detected in the gas phase in cold prestellar cores. The formulations corresponding to each of the new mechanisms presented here are functionally similar to each other, but quite different from the standard diffusive reaction formula used in typical astrochemical models. However, they are fully compatible with the usual treatment and may be used in tandem with it.

With the introduction of the new mechanisms, we run multipoint chemical models of prestellar core L1544 to test their effectiveness in an appropriate environment. A spectroscopic radiative-transfer model is implemented here as a means to evaluate the observable column densities of molecules of interest, allowing the direct comparison of the model results with observations.

This paper is structured as follows. The chemical model and the newly implemented mechanisms are described in Section 2.
The results of the models are explored in Section 3, with discussion in Section 4. Conclusions are summarized in Section 5.

2. Chemical Model

We use the astrochemical kinetic code MAGICKAL to study new grain-surface/ice-mantle mechanisms that may effectively form COMs in cold environments. The model uses a three-phase approach, based on that described by Garrod & Pauly (2011) and Garrod (2013), in which the coupled gas-phase, grain/ice-surface and bulk-ice chemistry are simulated through the solution of a set of rate equations. Initial chemical abundances used in the model are shown in Table 1, with elemental values based on those used by Garrod (2013). The initial H/H\textsubscript{2} abundances are chosen to agree approximately with the steady-state values appropriate to our initial physical conditions, as determined by the chemical model. Bulk diffusion is treated as described by Garrod et al. (2017). Although the bulk ice is technologically chemically active in this model, at the low temperatures employed in this work, diffusive reactions in general are negligibly slow, excluding processes involving H or H\textsubscript{2} diffusion. However, the addition of nondiffusive reactions to the model increases significantly the degree of chemical activity within the bulk.

The model uses the modified-rate treatment for grain-surface chemistry presented by Garrod (2008), which allows the stochastic behavior of the surface chemistry to be approximated; the back-diffusion treatment of Willis & Garrod (2017) is also used. Surface-diffusion barriers (\(E_{\text{diff}}\)) are related to desorption (i.e., binding) energies (\(E_{\text{des}}\)) such that \(E_{\text{diff}} = 0.35E_{\text{des}}\) for all molecular species, with bulk diffusion barriers taking values twice as high (Garrod 2013). However, the recent study by Minissale et al. (2016) estimated surface-diffusion barriers for atomic species such as N and O to be \(E_{\text{diff}} = 0.55E_{\text{des}}\). We adopt a similar value \(E_{\text{diff}}/E_{\text{des}} = 0.6\) for all atomic species; the impact of this parameter is discussed in Section 4.3. These basic surface-diffusion and desorption parameters are also adjusted according to the time-dependent abundance of H\textsubscript{2} in the surface layer, following the method of Garrod & Pauly (2011). All diffusion is assumed to be thermal, with no tunneling component (see also Section 4.3).

Chemical desorption, whereby grain-surface reactions allow some fraction of their products to desorb into the gas phase, is treated using the RRK formulation of Garrod et al. (2007) with an efficiency factor \(a_{\text{RRK}} = 0.01\).

The grain-surface/ice-mantle photodissociation rates used in MAGICKAL are based on the equivalent gas-phase rates, in the absence of other evidence (e.g., Garrod et al. 2008), and they likewise assume the same product branching ratios. Following the work of Kalvåns (2018), we adopt photodissociation rates on the grain surfaces and in the ice mantles that are a factor of 3 smaller than those used for the gas phase. Photodissociation may be caused either by external UV, or by the induced UV field caused by cosmic-ray collisions with H\textsubscript{2} molecules, and both sources of dissociation are included in the model.

Methanol in cold clouds is mainly formed on the grain surfaces through ongoing hydrogenation of CO (Fuchs et al. 2009). The methanol production network used in the present network follows from that implemented by Garrod (2013) and includes not only forward conversion of CO to methanol but also the backward reactions of each intermediate species with H atoms.

The overall chemical network used here is based on that of Garrod et al. (2017), with a few exceptions. In particular, a new chemical species, CH\textsubscript{3}OCH\textsubscript{3}, has been added along with a set of associated gas-phase and grain-surface reactions/processes listed in Tables A1 (gas phase) and A2 (solid phase). This radical is a key precursor of DME in our new treatments (see Section 2.5). Its inclusion also allows the addition of a grain-surface H-abstraction reaction from DME, making this species consistent with methyl formate and acetaldehyde.

An additional reaction was included in the surface network, corresponding to H abstraction from methane (CH\textsubscript{4}) by an O atom (\(E_A = 4380\) K; Herron & Huie 1973), as a means to ensure the fullest treatment for the CH\textsubscript{3} radical in the network.

The final change to the network is the adjustment of the products of CH\textsubscript{3}OH photodesorption to be CH\textsubscript{3} + OH rather than CH\textsubscript{2}OH, roughly in line with the recent experimental study by Bertin et al. (2016).

Each of the generic nondiffusive mechanisms that we include in the model (as described below) is allowed to operate on the full network of grain-surface and ice-mantle reactions that is already applied to the regular diffusive mechanism; reactive desorption, where appropriate, is also allowed to follow on from each of these, in the case of surface reactions. The full model therefore includes around 1600 surface and 1100 bulk-ice reaction processes for each new generic mechanism included in the model (excluding 3-BEF; see Section 2.5). All grain-surface and bulk-ice reactions allowed in the network are presented in machine-readable format in Table A2. The rate formulations for diffusive and nondiffusive reaction mechanisms used in the model are described below.

2.1. New Chemical Mechanisms

The standard formulation, as per, e.g., Hasegawa et al. (1992), for the treatment of a diffusive grain-surface chemical reaction (also known as the Langmuir–Hinshelwood or L-H mechanism) between species A and B is based on the hopping rates of the two reactants, \(k_{\text{hop}}(A)\) and \(k_{\text{hop}}(B)\); the abundances of both species on the grains, \(N(A)\) and \(N(B)\), which here are expressed as the average number of atoms or molecules of that species present on an individual grain; the total number of binding sites on the grain surface, \(N_G\), often assumed to be on the order of 1 million for canonically sized grains; and an
efficiency related to the activation-energy barrier (if any), \( f_{\text{act}}(AB) \), which takes a value between zero and unity. Thus, the total rate of production (s\(^{-1}\)) may be expressed in the following form (which is arranged in such a way as to demonstrate its correspondence with the nondiffusive mechanisms discussed later):

\[
R_{AB} = f_{\text{act}}(AB)[k_{\text{hop}}(A) N(A)] \frac{N(B)}{N_S} + f_{\text{act}}(AB)[k_{\text{hop}}(B) N(B)] \frac{N(A)}{N_S},
\]

(1)

In the first term, the expression within square brackets corresponds to the total rate at which particles of species \( A \) may hop to an adjacent surface binding site. The ratio \( N(B)/N_S \) gives the probability for each such hop to result in a meeting with a particle of species \( B \). Multiplying these by the reaction efficiency gives the reaction rate associated solely with the diffusion of species \( A \). The reaction rate associated with diffusion solely of species \( B \) is given by the second term. The total reaction rate is commonly expressed more succinctly thus

\[
R_{AB} = k_{AB} N(A) N(B),
\]

(2)

\[
k_{AB} = f_{\text{act}}(AB) (k_{\text{hop}}(A) + k_{\text{hop}}(B))/N_S,
\]

(3)

which provides a more standard-looking second-order reaction rate. The rate coefficient, \( k_{AB} \), may be further adjusted to take account of random walk, in which a reactant that has yet to meet a reaction partner may revisit previous, unsuccessful sites. This effect typically reduces the overall reaction rate by no more than a factor of a few (e.g., Charnley 2005; Lohmar & Krug 2006; Lohmar et al. 2009; Willis & Garrod 2017).

The individual hopping rate for some species \( i \) is assumed in this model to be a purely thermal mechanism, given by

\[
k_{\text{hop}}(i) = \nu(i) \exp \left( \frac{-E_{\text{act}}(i)}{T} \right).
\]

(4)

where \( \nu(i) \) is the characteristic vibrational frequency of species \( i \), and \( E_{\text{act}}(i) \) is the barrier against diffusion in units of Kelvin.

The reaction efficiency factor for a reaction between species \( A \) and \( B \) considers the case where, if there is an activation-energy barrier, the diffusion of either species away from the other may compete with the reaction process itself (see e.g., Garrod & Pauly 2011), thus

\[
f_{\text{act}}(AB) = \frac{\nu_{AB} \kappa_{AB}}{\nu_{AB} \kappa_{AB} + k_{\text{hop}}(A) + k_{\text{hop}}(B)},
\]

(5)

where \( \nu_{AB} \) is taken as the faster of either \( \nu(A) \) or \( \nu(B) \), and \( \kappa_{AB} \) is a Boltzmann factor or tunneling efficiency for the reaction (see Hasegawa et al. 1992). The denominator represents the total rate at which an event may occur when species \( A \) and \( B \) are in a position to react.

In order to formulate rates for nondiffusive reaction processes of whatever kind, the total rate must again be decomposed into its constituent parts, which, unlike in Equations (2) and (3), cannot generally be recombined.

The generic form that we adopt for such processes is

\[
R_{AB} = f_{\text{act}}(AB) R_{\text{comp}}(A) \frac{N(B)}{N_S} + f_{\text{act}}(AB) R_{\text{comp}}(B) \frac{N(A)}{N_S},
\]

(6)

where \( R_{\text{comp}}(i) \) is labeled the “completion rate” for the reaction, corresponding specifically to the “appearance” of species \( i \). The determination of \( R_{\text{comp}}(i) \) values is explained in more detail in the following subsections for each of the specific reaction mechanisms considered. The above form is essentially the same as that given by Garrod (2019) for photodissociation-induced reactions. The correspondence of Equation (1) (for diffusive reactions) with Equation (6) is clear; the latter may be considered a more general description of a surface reaction rate, which can be applied to both diffusive and nondiffusive processes, according to the chosen form of \( R_{\text{comp}}(i) \). The regular diffusive mechanism would use \( R_{\text{comp}}(i) = k_{\text{hop}}(i) N(i) \).

While the general form given in Equation (6) is set up to describe grain-surface processes, it may easily be adapted for bulk-ice processes by substituting \( N_S \) for \( N_{\text{grain}} \), the total number of particles in the ice mantle, with \( N(i) \) now representing the number of atoms/molecules of species \( i \) present in the mantle. In this case, mantle-specific diffusion rates should be used.

The several nondiffusive processes incorporated into the chemical model, based on Equation (6), are described below. Table 2 indicates which specific new mechanisms are included in each of the model setups tested in the present study.

### 2.2. E-R Reactions

The E-R reaction process occurs when some atom or molecule that is adsorbing/accreting from the gas phase onto the grain surface immediately encounters its grain-surface reaction partner as it adsorbs. Ruaud et al. (2015) considered a more intricate treatment than we use here, in which an adsorbing carbon atom could enter into a bound complex with a surface molecule. Here we adopt a more generalized treatment in which we do not differentiate between the binding properties of local surface species.

The rates for the E-R process can easily be represented using Equation (6). For reactions that have no activation-energy barrier (and for which \( f_{\text{act}}(AB) \) is therefore close to unity), this is achieved by setting \( R_{\text{comp}}(i) = R_{\text{acc}}(i) \), the total accretion rate of species \( i \) from the gas phase.

In the interests of completeness, it is necessary also to consider how to treat the kinetics of E-R reactions that have at least some modest activation-energy barrier. To this end, one may consider a hypothetical case where oxygen atoms are slowly accreting onto an otherwise pure CO surface. For purposes of illustration, it is initially assumed here that the surface-diffusion rates of both O and CO are negligible, with the result that \( f_{\text{act}}(O + CO) \) is 1.

The reaction \( O + CO \rightarrow CO_2 \) has an activation energy on the order of 1000 K, although the reaction will not be instant, in the absence of all other competing processes it should nevertheless occur on some finite timescale. Thus, the total timescale for the complete E-R process for an individual accreting O atom encountering and reacting with a surface CO molecule would be the sum of (i) the accretion timescale of the oxygen atom onto the surface and (ii) the lifetime against its subsequent reaction with CO, i.e., \( 1/R_{\text{acc}}(O) + 1/(\nu_{O+CO} \kappa_{O+CO}) \). This would provide a total completion rate associated with O accretion (to be employed in Equation (6)) of

\[
R_{\text{comp}}(O) = \frac{1}{1/R_{\text{acc}}(O) + 1/(\nu_{O+CO} \kappa_{O+CO})}.
\]
The completion rate $R_{\text{comp}}(O)$ should be viewed as the rate at which the reaction process occurs successfully from the point of view of an individual accreting O atom, taking into account all sequential steps in the completion of the reaction process. Note that, in the full description, the probability of encountering a CO molecule on the surface, $N(\text{CO})/N_S$, and the reaction efficiency, $f_{\text{acc}}(\text{O} + \text{CO})$, should both remain outside of the formula for $R_{\text{comp}}(O)$, as per Equation (6). Neither of these values affects the actual timescale over which an individual O atom successfully accretes and reacts with a surface CO molecule; rather, they affect the probability that a single such event is successful.

This expression for $R_{\text{comp}}(O)$ could result in one of two important outcomes, depending on the relative rates of accretion and reaction. If accretion of O is very slow, and therefore reaction is comparatively fast, then $R_{\text{comp}}(O) \approx R_{\text{acc}}(O)$. Because $N(\text{CO})/N_S \approx 1$, this means that the total E-R production rate would initially be $R_{\text{O}+\text{CO}} \approx R_{\text{acc}}(O)$. In other words, the overall production rate of CO$_2$ is only limited by the rate of O accretion onto the surface, which is as one would expect for this case.

However, if reaction is slower than or comparable to the initiating accretion process, each accretion of O would be followed by some significant lag time between accretion and reaction, which must be accounted for in the overall rate; the incorporation of the above expression for $R_{\text{comp}}(O)$ into Equation (6) indeed does this. Without this expression and instead using the value $R_{\text{comp}}(O) = R_{\text{acc}}(O)$, the rate of conversion of O and CO into CO$_2$ would incorrectly be set to the accretion rate of O. The correct formulation gives a total E-R reaction rate that is less than the total accretion rate, allowing the build up of O on the surface.

The final adjustment to the barrier-mediated E-R treatment comes into play when one or other surface-diffusion rate is non-negligible. If diffusion of (say) O is indeed fast compared to reaction, then the reaction efficiency, $f_{\text{acc}}(\text{O} + \text{CO})$, becomes small, which reduces the total rate of the reaction per Equation (6). However, the completion rate $R_{\text{comp}}(O)$ must also be adjusted to correspond only to the instances in which the O + CO reaction is actually successful. Successful reactions would have to occur before the diffusive separation of the two reactants could render the process unsuccessful, so the reaction timescale would become shorter, even though the reaction probability (i.e., $f_{\text{acc}}$) were reduced. For this reason, diffusion rates must also be considered when formulating $R_{\text{comp}}(O)$. Using a more general description for reactants A and B, the average lifetime against some event occurring (including reaction itself), once the reactants are in a position to react, may be described more fully by the expression:

$$t_{AB} = \frac{1}{(v_{AB} \kappa_{AB} + k_{\text{hop}}(A) + k_{\text{hop}}(B))},$$

which can then be used in the general definitions:

$$R_{\text{comp}}(A) = \frac{1}{1/R_{\text{app}}(A) + t_{AB}},$$

$$R_{\text{comp}}(B) = \frac{1}{1/R_{\text{app}}(B) + t_{AB}},$$

where $R_{\text{app}}(i)$ is the “appearance rate” of species $i$, which in the case of the E-R mechanism is simply $R_{\text{acc}}(i)$.

It should be noted that once diffusion becomes significant, a model even as simple as the one used above to describe pure E-R reaction processes would be incomplete; the standard diffusive reactions described by Equation (1) must also be considered (as an entirely separate process) in such a model to handle the occasions where accreting atoms (e.g., O) do not immediately react with their reaction partners (e.g., CO) before they diffuse away to another binding site, where they may also have the ability to react. In this case, the E-R expressions would depend much less strongly on the time-lag effect described above, meaning that $R_{\text{comp}}$ and $R_{\text{acc}}$ would be similar in cases where diffusion of either reactant were relatively fast.

In practical application to astrochemical models, for nondiffusive reactions whose reactants have slow or negligible diffusion rates, other processes could also act to interfere with the reaction; for example, the UV-induced dissociation of one or the other reactant might occur on a shorter timescale than a very slow reaction, or a hydrogen atom might arrive to react with one or the other reactant, before the reaction in question could occur. Competition from processes such as these would prevent very slow reactions (i.e., those with large activation barriers) from becoming important, even where diffusion of the reactants were negligible. A yet more complete treatment of reaction competition would include rates for these processes in Equations (5) and (7).

In our chemical model MAGICKAL, Equations (6)–(9) are used to set up E-R versions of all allowed grain-surface reactions in the network. Because the E-R process is exclusively a surface process, no such processes in the ice mantle are included. Note that when incorporating the E-R mechanism into a model, no modification of the accretion (adsorption) rates themselves is required, because the E-R mechanism does not replace any part of the adsorption rate. Rather, the E-R mechanism occurs immediately after adsorption and therefore acts as a sink on the surface populations of the reactants, even though its rate is driven by the rate of arrival from the gas phase of one reactant or another.

Equations with the general form of Equations (6)–(9) are used also to formalize the remaining nondiffusive reaction mechanisms described below, where $R_{\text{app}}(i)$ is the only quantity to vary between processes. These formulations can be used equally well for processes with or without activation-energy barriers.
While Equation (6) is still valid for the regular diffusive reaction mechanism with completion rates of $R_{\text{comp}}(i) = k_{\text{hop}}(i) N(i)$, no adjustment following Equations (7)–(9) should be used nor would be needed. The formulation required to model any lag time for diffusive reactions is different from that of nondiffusive processes (because $N(i)/N_S$ and $f_{\text{rad}}(AB)$ cannot remain outside the $R_{\text{comp}}(i)$ expression), but there are no circumstances in which such a lag time would be significant.

2.3. Photodissociation-induced Reactions

Garrod (2019) suggested that the omission of nondiffusive, photodissociation-induced reactions from models of interstellar ice chemistry may result in the photolytic production of COMs being severely underestimated. Past models of chemistry in star-forming regions (e.g., Garrod et al. 2008, 2017) have allowed photodissociation to contribute to the production of COMs in the surface and bulk-ice phases in only an indirect way, mediated by thermal diffusion. That is, photodissociation of various molecules produces radicals, which are separately allowed to react through the standard diffusive mechanism. Thus, at very low temperatures, no significant COM production is seen via radical–radical recombination, as diffusion of radicals is minimal. However, the presence of radicals in or upon the ice means that in some fraction of photodissociation events, the products may sometimes be formed with other reactive radicals already present nearby. In this case, the immediate products of photodissociation could react with the preexisting radicals either without diffusion, or following some short-ranged, nonthermal diffusion process (possibly enabled by the excitation of the dissociation products).

Equations (6)–(9) can again be used to describe this process, with an appropriate choice for $R_{\text{app}}(i)$, which is simply the total rate of production of the photoproduct $i$ caused by all possible photodissociation processes:

$$R_{\text{app}}(i) = \sum_{\text{all } j} R_j(i),$$  

(10)

where $R_j(i)$ is the production rate of $i$ via an individual photodissociation process $j$. For the radical CH$_3$, for example, this would include the photodissociation of CH$_3$OH, CH$_4$, and various larger molecules containing a methyl group.

If one were to consider, for example, the production of dimethyl ether through this mechanism, an important reaction would be CH$_3$ + CH$_3$O $\rightarrow$ CH$_2$OCH$_3$, which is usually assumed to be barrierless. For this reaction, in Equation (6), species $A$ = CH$_3$ and species $B$ = CH$_3$O; the appearance rate of CH$_3$ would be as described above. The main contribution to the appearance rate of CH$_2$O would likely be the photodissociation process CH$_3$OH $\rightarrow$ CH$_2$O + H. The formulation used for the dimethyl ether-producing reaction simply states that some fraction of CH$_3$ produced by the photodissociation of various molecules in the ice will immediately meet a CH$_3$O radical that it can react with, and vice versa.

Reactions affected by this PD-induced mechanism need not only be radical–radical recombination reactions; the production, via photodissociation, of atomic H in close proximity to CO, for example, could enhance the rate of the reaction H + CO $\rightarrow$ HCO, which has an activation-energy barrier. The treatment of barrier-mediated reactions in the generic Equations (7)–(9) is used again for this purpose.

This treatment does not take into account any explicit consideration of excitation of the photoproducts, which could also enhance reaction rates (as per e.g., Shingledecker et al. 2018, in the case of cosmic-ray-induced dissociation). It is also implicitly assumed that the rates of photodissociation used in the network represent the rates at which dissociation occurs without immediate recombination of those same photoproducts.

It is trivial to adapt the equations used for surface reactions to deal instead with ice-mantle-related processes, and this is indeed implemented in the simulations presented here.

2.4. Three-body Reactions

The laboratory results of authors such as Fedoseev et al. (2015, 2017), in which H, CO, and/or other species are deposited onto a cold surface, indicate that surface reactions between radicals of low mobility may produce COMs, even at low temperatures and without any energetic processing. The suggested explanation is that pairs of radical species such as HCO may, on occasion, be formed in close proximity to each other, allowing them to react either immediately or after a very small number of surface hops. The HCO radicals themselves would initially be formed through a more typical diffusive (L-H) process or through an E-R process, via the barrier-mediated reaction of H and CO. Fedoseev et al. (2015) suggest that reactions of HCO with CO may also be active, which would require no diffusion of HCO at all, if the HCO itself is formed through the reaction of atomic H and CO on top of a CO-rich surface.

In a similar vein, Garrod & Pauly (2011) found, using chemical kinetics modeling, that the interstellar abundance of solid-phase CO$_2$ could be explained by the reaction H + O $\rightarrow$ OH occurring on a CO-rich dust-grain ice surface. This allows the newly produced OH to react rapidly with the CO without any intervening thermal diffusion. They introduced into their models a new reaction rate specifically for this process that was functionally similar to Equation (6).

Here, we use Equations (6)–(9) to calculate rates for what may be termed three-body reactions, which include the above examples. This approach is extended to all grain-surface reactions in the network, with a similar treatment for bulk-ice processes. To do this, another dedicated expression for the appearance rate $R_{\text{app}}(i)$ to be used in Equations (8) and (9) must be constructed specifically for three-body reactions. Equation (10) can again be used, this time where $R_j(i)$ is the production rate of $i$ (as determined using Equation (1)) resulting from any diffusive (L-H) reaction, or for any nondiffusive E-R or photodissociation-induced reaction, whose rates are described above. Thus, $R_{\text{app}}(i)$ includes the production rates of $i$ for all reactive mechanisms $j$ that could lead to a subsequent reaction. From a technical point of view, the rates of all such reaction processes must therefore be calculated in advance of the calculations for any three-body reactions.

Using the example of the process considered by Garrod & Pauly (2011), the reaction under consideration as a three-body process would be OH + CO $\rightarrow$ HCO$_2$; thus, in Equation (6), $A$ = OH and $B$ = CO. There are several reactions in our network that could produce OH, but the main one is indeed H + O $\rightarrow$ OH. The sum of the production rates of OH from all of these reactions would comprise $R_{\text{app}}$(OH). The appearance rate for CO would also be constructed from the CO production rates of all reactions leading to its formation.

In this way, CO$_2$ could be formed via a three-body reaction process in which, for example, a H and an O atom diffuse on a
Three-body reactions was recently employed by Dulieu et al. simulations presented here.

usually be lower than those used in the 

H2 of all species in the bulk ice

exclusively a surface mechanism, while the thermal diffusion

photodissociation-induced reactions, as the E-R process is

important for certain species if they have no other dominant

production mechanism. In the present models, we allow a total

reactions, the second three-body reaction could be the most

Note that the new treatment does not explicitly differentiate

between the case where the newly formed reactant is immediately

in contact with the next reaction partner, and the case where it has

sufficient excess energy to allow it to undergo a thermal hop in

order to find its next reaction partner. It is in fact highly probable

that the products of exothermic reactions (which include virtually

every surface reaction included in the network) would have

sufficient energy to allow some degree of nonthermal hopping

immediately following formation. The possibility of such energy

also allowing barrier-mediated three-body reactions to occur more

rapidly is considered in the next subsection.

To go yet a stage further, one may imagine a scenario in which

the products of three-body reactions themselves could also be involved in subsequent nondiffusive three-body

reactions. This possibility is also included in our model, using

the same equations as before, with appearance rates defined by

\[ R_{\text{app}}(i) = \sum_{j} R_{3B}(i,j), \]

where \( R_{3B}(i,j) \) is the production rate of \( i \) caused by the three-

body reaction labeled \( j \). Although these appearance rates will

usually be lower than those used in the first round of three-body

reactions, the second three-body reaction could be the most

important for certain species if they have no other dominant

production mechanism. In the present models, we allow a total

of three rounds of three-body reactions to take place. Although

this could in theory be increased to any arbitrary number of

rounds, the influence of those processes rapidly diminishes

beyond the second round.

As with the photodissociation-induced reactions, a similar

method is employed also for reactions in the bulk ice. In this

case, the appearance rates of reactants in the first round of

three-body reactions would generally all be products of

photodissociation-induced reactions, as the E-R process is

exclusively a surface mechanism, while the thermal diffusion

of all species in the bulk ice—excluding arguably H and

H2—would be very slow at the temperatures considered in the

simulations presented here.

Finally, we note that a method for treating what we label

three-body reactions was recently employed by Dulieu et al.

(2019) for a single reaction between H2CO and newly formed

H2NO. Those authors constructed a separate chemical species

to represent the H2NO that is formed in contact with H2CO on

a surface, then included a special reaction in their network that

occurs at a rate equal to the vibrational collision frequency of

the two contiguous species. Although apparently different from

our approach, such a treatment should also provide the correct

result; this is because, assuming that there are no competing

processes with the reaction in question, the abundance of the

special H2NO species is determined solely by its formation rate

and its one destruction rate. In that case, both the specific

abundance of the special H2NO species and its reaction rate

coefficient are canceled out in the overall rate calculation,
giving a total production rate for the reaction that is equal to the

rate that we employ in the present work. In such a case, therefore,

the chosen rate coefficient becomes immaterial to the result.

It is presumably possible to set up a large network of such reactions for newly formed species; however, the

requirement to include a new chemical species for each

reactant pair would likely make this method prohibitive for

large networks.

2.4.1. Specific Reactions

Although the full model includes a range of 3-B processes

capable of producing acetaldehyde (CH3CHO), methyl formate

(CH3OCHO) and dimethyl ether (CH3OCH3), the dominant

mechanisms for each (based on model results) are presented

below.

For acetaldehyde, the most important three-body mechanism

is made up of a pair of sequential two-body processes as follows:

\[ H + CH_2 \rightarrow CH_3 \] (12)

\[ CH_3 + HCO \rightarrow CH_3CHO. \] (13)

The most important sequential mechanisms for the other two

COMs are

\[ H + CH_2 \rightarrow CH_3 \] (14)

\[ CH_3 + CH_2O \rightarrow CH_3OCH_3 \] (15)

\[ H + CO \rightarrow HCO \] (16)

\[ HCO + CH_3O \rightarrow CH_3OCHO. \] (17)

Each of these reaction pairs involves the addition of radicals

in the second step, and two of them involve the addition of

atomic H to a radical in the first step. The production of the

COMs through these mechanisms should therefore have a

strong dependence on the instantaneous abundances of short-

lived reactive radicals.

The full network used in the models includes three-body

versions of all the reactions used for regular diffusive

chemistry, for all surface and mantle species.

2.5. Excited Three-body Reactions

Besides the three-body reaction process described in

Section 2.4, we also consider a mechanism whereby the

initiating reaction produces a product that is sufficiently excited

that it is able to overcome the activation-energy barrier to a

subsequent reaction. This is of particular interest if it may allow

a reaction with either CO or H2CO—both abundant surface

species—that would result in the production of a precursor to

an important O-bearing COM. In this picture, the energy of

formation released by a reaction is held in the vibrational
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excitation of the product species. That excited species can then immediately react with a contiguous reaction partner.

Figure 1 shows the formation of CH₃CHO via this three-body excited-formation (3-BEF) mechanism as an example. The original reaction network included the direct association of CH₃ and HCO, mediated by radical diffusion, as the main formation process for surface CH₃CHO. The chance of forming CH₃CHO in that purely diffusive model is small, because it would require immobile heavy radicals to meet at low temperature. The new three-body process described above, as well as the photodissociation-induced and E-R processes, would allow this reaction to occur nondiffusively. However, the excited production of CH₃ could also allow reaction with abundant surface CO. In the first step, an H atom meets and then reacts with a CH₂ radical that is adjacent to a CO molecule. This reaction is exothermic by 4.80 eV (∼55,700 K), sufficient to overcome the barrier to the CH₃ + CO reaction (nominally 2870 K; see below). Once this follow-up reaction has occurred, the product CH₃CO, which is a precursor to acetaldehyde, can easily be converted into a stable species via hydrogenation by another H atom. The entire process is described as follows:

\[
\begin{align*}
    H + CH₂ &\rightarrow CH₃^* \\
    CH₃^* + CO &\rightarrow CH₃CO \\
    H + CH₃CO &\rightarrow CH₃CHO,
\end{align*}
\]

where an asterisk indicates an excited species. Similar reactions for the production of CH₃OCH₃ and CH₃OCHO through the 3-BEF process are as follows:

\[
\begin{align*}
    H + CH₂ &\rightarrow CH₃^* \\
    CH₃^* + H₂CO &\rightarrow CH₃OCH₂ \\
    H + CH₃OCH₂ &\rightarrow CH₃OCHO.
\end{align*}
\]

The 3-BEF process technically concerns only the first two reactions out of the three, in each case; the final hydrogen-addition step most typically occurs through the usual L-H mechanism that is already included in the model, although nondiffusive mechanisms may also act to add the final H atom.

Due to the more complicated requirement to consider the energy of formation in each case, the three new 3-BEF processes shown above were individually coded into the model, rather than constructing a generic mechanism. For this reason, the 3-BEF mechanism is included only in the first round of three-body processes. The production rate of the standard diffusive process for the initiating reaction in each case is responsible for the entire energy barrier of 2500 K, based on the approximate value for \( R_{app} \), and only one term is required in Equation (6). Crucially, the reaction efficiency for the second reaction in the process (i.e., the reaction whose rate is actually being calculated with the 3-BEF method) is initially set to unity to signify that the activation-energy barrier is immediately overcome.

Unfortunately, the activation energies of the above reactions between the radicals and CO or H₂CO are not well constrained. The chemical network of Garrod (2013) included the CH₃ + CO and CH₃O + CO reactions, adopting a generic activation-energy barrier of 2500 K, based on the approximate value for the equivalent reactions of atomic H with CO and H₂CO. A reaction between CH₃ and H₂CO was also present in that network, with products CH₄ and HCO, and \( E_A = 4440 \) K; this reaction is retained here in addition to the new pathway. For the present network, we calculate an approximate activation energy of 2870 K for the CH₃ + CO reaction using the Evans–Polanyi (E-P) relation (e.g., Dean & Bozzelli 2000); this would be well below the energy produced by the initiating reaction (∼55,700 K). Due to the lack of comparable reactions for a similar E-P estimate for the activation energy of the CH₃ + H₂CO reaction, the same value of 2870 K might be
assumed, placing it also comfortably less than the energy produced by the $H + CH_2 \rightarrow CH_3$ reaction. Few determinations exist for the activation energy of the $CH_3O + CO$ reaction, although an experiment places it at 3967 K (for temperatures of 300–2500 K; see Huynh &Violi 2008). This also is less than the energy produced by the initiating reaction, $H + H_2CO \rightarrow CH_3O$ ($\sim$10,200 K). In any case, the activation energies involved in each of the three reactions mentioned here are sufficiently large that they should be of no importance without the inclusion of the 3-BEF mechanism to provide the energy required, while the 3-BEF mechanism itself is assumed to go at maximum efficiency. However, the latter assumption may not necessarily be accurate, depending on the form of the energy released by the reaction, and whether there is any substantial loss prior to reaction actually occurring (see Section 3.3).

2.6. Physical Conditions

MAGICKAL is a single-point model, but a spatially dependent picture of the chemistry of L1544 can be achieved by running a set of models with different physical conditions at specific positions within the prestellar core. Recently, Chacón-Tanarro et al. (2019) determined the parameterized density and temperature structure of L1544 as follows, considering the optical properties of dust grains as a function of radius:

\[
T(r) (K) = 12 - \frac{12 - 6.9}{1 + \left(\frac{r}{28.7 \, \text{au}}\right)^{1.7}},
\]

\[
nH_2(r) (\text{cm}^{-3}) = \frac{1.6 \times 10^6}{1 + \left(\frac{r}{17.3 \, \text{au}}\right)^{2.6}},
\]

where $r$ is measured in arcseconds. Based on this density structure, we determine 15 densities at which the chemical models are to be run, ranging logarithmically from the minimum of $n_H = 4.4 \times 10^4 \text{cm}^{-3}$ ($\sim$11,000 au) to the maximum of $n_H = 3.2 \times 10^6 \text{cm}^{-3}$ (core center). An additional eight density points are then placed to achieve better spatial resolution toward the core center (where the density profile is relatively flat). The appropriate temperature for each point is then chosen from the profile, based on density/radius.

In order to take account of the gradual collapse of the gas into this final density profile, the density used for each chemical model in the set is independently evolved using a simple modified freefall collapse treatment. (The radial position of each model point is thus not explicitly considered during this evolution.) Each point begins with a gas density of $n_{H_2} = 3 \times 10^4 \text{cm}^{-3}$, with an initial $H_2/H$ ratio of $5 \times 10^{-4}$. The density evolution stops once each model reaches its specified final density, resulting in a marginally different evolutionary time for each density point. The collapse treatment is based on that used by Rawlings et al. (1992). Magnetic fields can play an important role in the equilibrium of dense cores, significantly slowing down the collapse process. Estimating an accurate collapse timescale is challenging, although the ratio of the ambipolar diffusion time ($\tau_{ap}$) to the freefall time ($\tau_{ff}$) is typically assumed to be $\tau_{ap}/\tau_{ff} \sim 10$ (see, e.g., Hennebelle & Inutsuka 2019). Thus, the magnetic retardation factor for collapse, $B$, is adopted here to control the collapse timescale. This parameter takes a value between 0 (static) and 1 (freefall) and is technically density dependent. In our model, this value is set for simplicity to 0.3 for all density points, which results in a collapse timescale approximately three times longer than the freefall timescale. A time of a little over $3 \times 10^6$ yr is therefore required to reach the final density at each point, although much of this time is spent under relatively low-density conditions as the collapse gradually ramps up.

The density evolution for each model is accompanied by increasing visual extinction, which evolves according to the expression $A_V = A_{V,0}(n_H/n_{H_2})^{2/3}$ (Garrod & Pauly 2011). The initial extinction values are set such that the values at the end of the chemical model runs correspond to the linear integration of the density profile, converted to visual extinction using the relationship $N_H = 1.6 \times 10^{22} A_V$. An additional background visual extinction of 2 is added for all positions and times, under the assumption that L1544 is embedded in a molecular cloud (e.g., Vasyunin et al. 2017). In contrast to density and visual extinction, the temperature is held steady throughout the chemical evolution for each density point, with the same value adopted for both the gas and the dust. Temperatures range from approximately 8 to 14 K depending on radius, which is consistent with the observational features (Crapsi et al. 2007).

3. Results

The time evolution of the fractional abundances at the core-center position is presented in Figures 2 (gas phase) and 3 (solid phase) for each of the main chemical model setups. In the control model, no new mechanisms are added. In each of the other model setups, a single new mechanism is added to the control-model setup, except for model 3-B+3-BEF, in which it is assumed that the 3-BEF mechanism could not occur without the 3-B mechanism also being active.

As seen in Figure 2, every new mechanism introduced here, excluding E-R, significantly increases the abundances of CH$_3$OCH$_3$ and CH$_3$OCHO in the gas phase during core evolution, while CH$_3$CHO is only substantially increased via 3-BEF. However, it should be noted that the increased fractional abundances rapidly drop as density increases toward the end time of all the models, mostly converging to the control-model values. This indicates that the new mechanisms may hardly affect the gas-phase COMs at the core center, but may be more effective at more distant radii (i.e., lower-density regions); this would nevertheless result in higher abundances toward the core-center position when averaged over the line of sight to include lower-density gas.

The presence of the COMs in the gas phase following their formation on grain surfaces is the result of chemical desorption. All surface reactions that form a single product have a small possibility of returning that product to the gas phase. The upper limit on the ejection probability per reaction is 1%.

Similar to the gas phase, every mechanism excluding E-R significantly increases the solid-phase populations of the COMs (Figure 3). Note that the solid-phase population of CH$_3$CHO, whose gas-phase abundance is only strongly increased by the 3-BEF mechanism, increases even in the 3-B (only) and PD-induced models. The 3-B and 3-B+3-BEF models converge to essentially the same value at the end time. Dimethyl ether in the mantle is produced in similar quantities by each of the three effective mechanisms, while 3-BEF and then 3-B are more important than PD-induced formation in the case of methyl formate. The E-R mechanism produces only marginal increases in mantle abundances of acetaldehyde and methyl formate. The increase in dimethyl ether production caused by E-R is around...
an order of magnitude throughout most of the evolution, although this is dwarfed by the effects of the other mechanisms.

Figure 4 shows the radial distribution of gas-phase COM abundances using the full radius–density–temperature profile model results; abundances shown correspond to the end-time abundances, at which the final density profile is achieved. The observational values that are also indicated in the figure are for the core-center position; however, those observations correspond to a beam of radius \( \sim 1900 \) au and would also sample a range of physical conditions along the line of sight—some caution should therefore be taken in directly comparing them with the local fractional abundance values.

It may be seen that the general trend, even for the control model, is for COM abundances to increase toward greater radii. The 3-B+3-BEF model produces maximum molecular abundances for acetaldehyde and methyl formate similar to the observational values. For the latter molecule, the modeled fractional abundance exceeds the observational values at radii greater than around 2500 au, although the absolute gas density begins to fall off at these positions, so that they should contribute less to the total column density of the molecule. At the largest radii modeled, the 3-B (only) model produces methyl formate sufficient to match the observed abundance (although, again, perhaps with little contribution to total column density). Acetaldehyde also reaches its peak abundance at large radii, although it reaches a similar abundance at smaller radii.

For each of the new models, the local fractional abundance of CH$_3$OCH$_3$ is greatest at positions away from the core center, but a significant increase in abundance is achieved at almost all positions for every model, versus the control. However, the maximum value achieved (for the 3-B model) is still at least two orders of magnitude lower than the observations, both in the inner regions and at the outer edge. Curiously, for dimethyl ether, the most effective model is the 3-B (only) model, whereas the 3-B+3-BEF model is the most productive for the other two COMs.

In each of the 3-B, 3-B+3-BEF, and PD-induced models, acetaldehyde and dimethyl ether abundances show a prominent peak feature at around 2000 au. This feature is also present for methyl formate in the PD-induced and 3-B (only) models. Observations of L1544 by Jiménez-Serra et al. (2016) show higher fractional abundances of CH$_3$CHO and CH$_3$OCH$_3$ toward an off-center position at \( r \approx 4000 \) au versus those at the core center, with CH$_3$OCHO arguably showing similar behavior. Our 3-B, 3-B+3-BEF, and PD-induced models all show this general behavior (methyl formate in the 3-B+3-BEF model notwithstanding), albeit at a somewhat different radius.

Figure 2. Time evolution of the gas-phase abundances of the three O-bearing COMs, at the core center, for models using each of the new mechanisms. The abundance from the control model is denoted by the black dashed line. Diamonds indicate the abundances at the end of each model run. The black dotted lines and the gray shaded regions indicate the observational abundances and their uncertainties, obtained from Jiménez-Serra et al. (2016) for L1544. The gas density is indicated by the right-hand vertical axis and the similarly colored line.
from the observations. The origin of this peak and its similarity to the observations are discussed in more detail in Section 4.2.

Figure 5 shows the radial distribution of the ice-mantle abundances at the end time of each model, plotted as a function of the water abundance in the ice at each position. In contrast with the gas phase, all of the new mechanisms but E-R significantly increase the solid-phase abundances of COMs at all radii. This is partly because the ice mantle preserves the earlier surface layers during the evolution of the prestellar core, when significant enhancement of the COM abundances in the gas phase is found (see Figure 2), which is itself caused by the increased efficiency of the production of COMs on the grain surfaces. However, the PD-induced model permits substantial ongoing processing of mantle material itself.

While COM production is not especially important in the control or E-R models, the others attain substantial COM abundances in the ices, comparable with gas-phase values observed in hot molecular cores. The maximum abundance achieved by methyl formate in the 3-B+3-BEF model is close to 1% of the water abundance at the core center, i.e., around $10^{-6}$ with respect to total hydrogen. This value may thus be too high to agree with observations of hot cores/corinos, if the abundances achieved in the prestellar stage should be preserved intact to the later, warmer stages of evolution.

It is also noteworthy that the COM fraction in the ices is in general somewhat greater at larger radii, although the dimethyl ether abundance is fairly stable through the core in the 3-B and 3-B+3-BEF models, and methyl formate is also stable throughout in the 3-B+3-BEF model.

Figure 6 shows the final radial distribution of the main ice constituents as a fraction of the local water-ice abundance for the control model and for the 3-B+3-BEF model. The absolute abundance of water ice is fairly constant across the profiles. The latter is taken as representative of all new models, due to their similarity, except for the E-R model, which is rather similar to the control. Based on the absolute abundance profiles, column densities for each ice species are derived by integrating along the line of sight (without beam convolution); the resulting abundances with respect to the H$_2$O ice column density are summarized in Table 3. Comparable observational ice abundances are also shown; these are taken from Boogert et al. (2015), who provided median values with respect to H$_2$O, along with the full range of the observed abundances (from subscript to superscript value). Both of our model setups produce a centrally peaked distribution of CH$_3$OH ice, while CO ice is approximately as abundant as H$_2$O ice, especially toward inner radii where the most extreme depletion occurs. With the new mechanisms, a more gently sloped distribution appears, and a better match with observational abundances of CO and CO$_2$ is achieved. The other ice components in the 3-B+3-BEF model are within the observational range as well.
3.1. Column Density Analysis

Observational abundances may not accurately represent the true local abundances within a source. This is because the observational intensities are not only averaged over the line of sight, but are also affected by the excitation characteristics of each observed species and by the response of the telescope beam. Considering this, it is indispensable to perform spectral simulations for better comparison with the observations. The spectral model used here simulates molecular lines (of COMs) that are expected to be observable and uses the chemical abundances shown in Figure 4 as the underlying distribution.

The 1D chemical/physical model is treated as spherically symmetric, so that molecular emission can be simulated along lines of sight passing through the core at various offsets (including directly on source), assuming local thermodynamic equilibrium. Each line of sight passes through a range of gas densities, temperatures, and chemical abundances. The resulting 2D simulated intensity maps for each frequency channel are then convolved with a Gaussian telescope beam of appropriate size, dependent on frequency and the telescope in question.

The FWHM of the molecular lines is assumed here to be 1 km s$^{-1}$, with a spectral resolution of 250 kHz, although the simulations are quite insensitive to the precise choice of parameters.

The integrated intensities of the ensemble of molecular lines is used in a rotational diagram (RD) analysis (Goldsmith & Langer 1999) to obtain column densities ($N_{\text{tot}}$) and rotational temperatures ($T_{\text{rot}}$) for each molecule. These quantities can then be compared directly with those obtained from observations.

Beam sizes were assumed to be $\sim28''$-$31''$ between 79 and 87 GHz and $\sim24''$-$26''$ between 94 and 103 GHz, based on the size of the observing beam of the IRAM 30 m telescope. The distance to the model prestellar core is assumed to be 140 pc (Elias 1978).

The radiative transfer and RD analysis is performed toward the on-source position and toward two offset positions: (i) the peak of the COM abundances (2000 au) and (ii) the low-density outer shell (9000 au). By considering these three positions, we may compare the modeled COM peaks with the observational ones and determine the dependence of the chemical reactions on the local physical conditions in the prestellar core.

One strategy to apply this radiative transfer and RD technique would be to simulate precisely the same molecular lines used in individual observational data sets for L1544. However, because the present aim is to determine a well-defined column density (and rotational temperature) based on the models, with which observed column densities may be directly compared, we instead choose a selection of lines that may plausibly be (or indeed have been) detected toward cold...
sources and which include a range of upper energy levels. Emission lines of CH$_3$CHO and CH$_3$OCHO recently detected toward the cold dark cloud B5 (Taquet et al. 2017) are chosen for this analysis. While Taquet et al. (2017) detected a relatively large number of molecular lines for CH$_3$CHO and CH$_3$OCHO, only four transitions of CH$_3$OCH$_3$ with a limited range of $E_{\text{up}}$ (10–11 K) were detected by those authors. Our adoption of only those lines could therefore cause substantial uncertainty in the determination of $N_{\text{tot}}$(CH$_3$OCH$_3$). For this reason, we choose eight bright (i.e., high $A_{ij}$) AA transitions of CH$_3$OCH$_3$ with $E_{\text{up}}$ ranging from 8 to 19 K, using the Splatalogue web tool. The spectroscopic data originate from the JPL line list$^4$ (Bauder et al. 1976; Lovas et al. 1979; Taquet et al. 2017).

\footnotesize
\textsuperscript{3} http://www.cv.nrao.edu/php/splat
\textsuperscript{4} https://spec.jpl.nasa.gov

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure5}
\caption{Radial distribution of the solid-phase abundances of the three O-bearing COMs depending on the mechanisms. The black dotted line and gray shaded region indicate the abundance from the observation and error, respectively. The observational data and its error are taken from Jiménez-Serra et al. (2016). The observational error of CH$_3$CHO is not provided in the reference. The abundance from the control model is denoted by a black dashed line and a black dotted line, respectively. While the result from the 3-B combined with the 3-BEF is denoted by a black solid line, a green line represents the 3-B only model. The red and blue solid lines indicate the abundances from the E-R model and PD-induced model, respectively.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure6}
\caption{Radial distribution of the ice abundances of the main ice constituents. The abundance of CO and CO$_2$ is denoted by a black solid and a black dashed line, respectively. The blue, green, and red solid lines represent the abundances of CH$_4$, NH$_3$, and CH$_3$OH, respectively.}
\end{figure}
Table 3
Abundances Relative to the H2O Ice Column Density

| Model          | CO    | CO2   | CH4   | NH3   | CH3OH |
|----------------|-------|-------|-------|-------|-------|
| Observation*   | 0.21±0.03 | 0.29±0.01 | 0.05±0.01 | 0.06±0.01 | 0.00±0.01 |
| Control        | 0.83  | 0.07  | 0.19  | 0.09  | 0.07  |
| 3-B+3-BEF      | 0.57  | 0.12  | 0.11  | 0.08  | 0.01  |

Note. * Boogert et al. (2015); values correspond to low-mass young stellar objects.

Table 4
List of Targeted Transitions with Their Spectroscopic Properties

| Molecule          | Transition | Frequency (GHz) | $E_{up} \ (K)$ | $A_{g} \ (s^{-1})$ |
|-------------------|------------|-----------------|---------------|------------------|
| A-CH3CHO          | 2_{1,2}−1_{0,1} | 84.21976       | 4.96          | 2.4 \times 10^{-6} |
| E-CH3CHO          | 5_{0,5}−4_{1,4} | 95.94744       | 13.9          | 3.0 \times 10^{-5} |
| A-CH3CHO          | 5_{0,5}−4_{1,4} | 95.96346       | 13.8          | 3.0 \times 10^{-5} |
| E-CH3CHO          | 8_{1,7}−7_{1,6} | 90.15647       | 19.7          | 9.8 \times 10^{-6} |
| A-CH3CHO          | 5_{1,4}−4_{1,3} | 98.86331       | 16.6          | 3.0 \times 10^{-5} |
| AA-CH3OCH3        | 3_{2}−2_{1,2} | 84.63680       | 11.0          | 4.4 \times 10^{-6} |
| AA-CH3OCH3        | 2_{0,2}−2_{1,1} | 86.22872       | 8.36          | 3.5 \times 10^{-6} |
| AA-CH3OCH3        | 2_{1,2}−1_{2,1} | 89.70281       | 8.36          | 3.8 \times 10^{-6} |
| AA-CH3OCH3        | 6_{0,6}−5_{1,5} | 90.93754       | 19.0          | 5.7 \times 10^{-6} |
| AA-CH3OCH3        | 3_{2,2}−3_{1,3} | 91.47931       | 11.1          | 4.9 \times 10^{-6} |
| AA-CH3OCH3        | 4_{2,3}−4_{1,4} | 93.85964       | 14.7          | 5.6 \times 10^{-6} |
| AA-CH3OCH3        | 5_{2,5}−5_{1,5} | 96.85246       | 19.3          | 6.2 \times 10^{-6} |
| AA-CH3OCH3        | 4_{1,4}−3_{1,3} | 99.32600       | 10.2          | 8.8 \times 10^{-6} |
| AA-CH3OCH3        | 7_{2,6}−6_{1,5} | 84.45475       | 19.0          | 8.0 \times 10^{-6} |
| A-CH3OCHO         | 7_{3,4}−6_{2,3} | 87.16129       | 22.6          | 7.8 \times 10^{-6} |
| A-CH3OCHO         | 8_{1,8}−7_{1,7} | 89.31664       | 20.1          | 1.0 \times 10^{-5} |
| A-CH3OCHO         | 7_{2,6}−6_{1,5} | 90.15647       | 19.7          | 9.8 \times 10^{-6} |
| A-CH3OCHO         | 9_{1,8}−8_{1,7} | 100.0805       | 24.9          | 1.5 \times 10^{-5} |
| A-CH3OCHO         | 8_{1,7}−7_{1,6} | 100.4907       | 22.8          | 1.5 \times 10^{-5} |
| A-CH3OCHO         | 9_{0,9}−8_{1,8} | 100.6834       | 24.9          | 1.5 \times 10^{-5} |
| A-CH3OCHO         | 8_{2,6}−7_{2,5} | 103.47787      | 24.6          | 1.5 \times 10^{-5} |

Note. Acetaldehyde line data from the JPL catalog based on the data set of Bauder et al. (1976). Dimethyl ether line data from the JPL catalog based on the data set of Lovas et al. (1979) and Neustock et al. (1990). Methyl formate line data from the JPL catalog based on the data set of Ilyushin et al. (2009) and Plummer et al. (2014). The representative molecular transition used for the normalized convolved intensity analysis in Section 3.4 is denoted with an asterisk.

Plummer et al. 1984; Neustock et al. 1990; Ilyushin et al. 2009; the COM transitions considered in this analysis are listed in Table 4.

3.2. Column Densities of O-bearing COMs toward the Core Center

Tables 5–7 (core center, 2000, 9000 au) compare the molecular column densities obtained from the RD analysis of different chemical models with observational values from the literature; observational errors and RD line-fitting error estimates are given in parentheses. Figure 7 shows the molecular column densities for each model at three different positions as histograms. The observed value (a solid horizontal line) and its error bounds (dashed horizontal lines) are presented together for comparison. While every chemical model introduced here significantly underproduces CH3OCH3, both the 3-B and 3-B+3-BEF models result in meaningful differences from the control model for the other two COMs at the core center (Table 5). One thing to note is that the COMs are more actively formed via 3-BEF than solely via the 3-B mechanism. For example, while 3-B+3-BEF significantly increases the column density of CH3CHO as well as CH3OCHO, 3-B substantially increases CH3OCHO only. Furthermore, even though both the 3-B and 3-B+3-BEF mechanisms enhance the CH3OCHO population significantly, the increment is much higher in the 3-B+3-BEF model (3-B+3-BEF even substantially overproduces CH3OCHO—see also Section 3.3).

In either the 3-B or 3-BEF models, the key quantities through which the production rates of COMs (on the grains or in the gas phase) may be understood are the surface abundance of reactants, and the production (i.e., appearance) rates of their reaction partners. The latter quantity is an explicit component of the new expressions for nondiffusive processes, whereas in the regular L-H formulation it does not appear. The higher formation rates in the 3-BEF model can be explained by the fact that this mechanism involves the addition of radicals to stable compounds (which are thus more abundant on the grain surface) in the second step of the consecutive reaction chain (Equations (18)–(20), while the 3-B process involves the addition of sparse radicals (Equations (13), (15), and (17)).

The greater rate of formation of CH3OCHO over that of CH3CHO in either the 3-B or 3-BEF model can also be understood in the same context. In the 3-B model, the reactants CH3 and CH3O are technically competing with each other to form either CH3CHO or CH3OCHO by reacting with HCO radicals on the grain surface. As seen in Figure 8, the fractional grain-surface abundance of CH3O (shown for the core-center position) is much higher than that of CH3. The production rate of CH3O is also much greater than that of CH3, which is partly why its surface abundance is higher. Similarly, in the 3-BEF model, CH3 and CH3O* are competing with each other to react with CO on the grain surface to form either CH3CHO or CH3OCHO; CO is abundant, and the appearance rates of CH3* and CH3O* directly determine the formation rates of CH3CHO and CH3OCHO.

Note that only a fraction of newly formed methyl radicals can take part in the formation of the COMs through the 3-BEF mechanism, because only the excited methyl radicals formed via hydrogenation of CH2 have this mechanism available; abstraction of H from CH4 by other H atoms is slightly endothermic, so it should not produce CH3+.

Thus, the radical CH3 acts as a bottleneck to the formation of the COMs in the nondiffusive models. Also, the gradual depletion of C and related hydrocarbons from the gas phase, while CO remains abundant, means that production of CH3 cannot keep up with the production of CO-related radicals. The reaction of CH3 with H or H2 from the gas phase to re-form CH4 also keeps the average grain-surface CH3 abundance low. The production of HCO and CH3O radicals continues to be endothermic, so it should not produce CH3*.
are competing to form either CH$_3$CHO or CH$_3$OCH$_3$ by reacting with the excited methyl radicals on the grain surface, but CO is much more abundant than H$_2$CO (Figure 8). The small amount of excited methyl radicals on the surface is thus preferentially consumed to form CH$_3$CHO.

The E-R mechanism does not make a substantial difference to the gas-phase abundances versus the control (see Figure 4 and Table 5). This is because the E-R process requires high surface coverage of the reactive species on the grains to be effective. This result is not exactly consistent with the results from Ruaud et al. (2015). They find that the combination of E-R and their complex-induced reaction mechanisms is efficient enough to reproduce the observed COM abundances at temperatures as low as 10 K. Beyond the uncertainty in the level of contribution of either mechanism, the different model parameters of both studies should be noted: Ruaud et al. (2015) mainly focus on the accretion of carbon atoms and assume a much higher binding energy (3600–8400 K) than ours (800 K).

This may cause a higher concentration of reactive species on the grain surface, allowing the E-R process to be efficient.

The PD-induced reaction process is ineffective in increasing the population of COMs in the gas phase at the core center. However, the PD-induced model significantly increases (more than two orders of magnitude) the amount of COMs in the ice mantles throughout the core’s evolution (see Figure 5). Other studies suggest indeed that the bulk ice is where the majority of physico-chemical changes caused by radiation chemistry are likely to occur (Johnson 1990; Spinks & Woods 1990; Shingledecker et al. 2017). The enhanced population of the COMs in the ice mantle does not actively affect the population in the gas phase, because the COM products are preserved in the mantle rather than diffusing to the grain surface, which is directly coupled to the gas phase. Even though this process does not make a prominent difference in the gas-phase abundance for the prestellar core, it would significantly affect the chemistry during the warm-up period of a protostellar core.

**Table 5**

| Model         | CH$_3$CHO (cm$^{-2}$) | CH$_3$OCH$_3$ (cm$^{-2}$) | CH$_3$OCHO (cm$^{-2}$) |
|---------------|------------------------|---------------------------|-------------------------|
| Observation   | 1.2 × 10$^{12}$        | 1.5 × 10$^{10}$ (4.0 × 10$^{11}$) | 4.4 × 10$^{10}$ (8.0 × 10$^{12}$) |
| Control       | 2.6 × 10$^{10}$ (4.3 × 10$^{7}$) | 1.2 × 10$^{10}$ (9.9 × 10$^{7}$) | 1.1 × 10$^{10}$ (9.9 × 10$^{7}$) |
| 3-B           | 3.8 × 10$^{10}$ (1.1 × 10$^{6}$) | 2.6 × 10$^{10}$ (4.4 × 10$^{6}$) | 4.7 × 10$^{10}$ (4.4 × 10$^{6}$) |
| 3-B+3-BEF     | 1.2 × 10$^{12}$ (4.1 × 10$^{5}$) | 2.6 × 10$^{10}$ (7.0 × 10$^{5}$) | 1.1 × 10$^{10}$ (1.3 × 10$^{5}$) |
| E-R           | 2.7 × 10$^{10}$ (4.5 × 10$^{6}$) | 1.3 × 10$^{10}$ (9.8 × 10$^{6}$) | 1.1 × 10$^{10}$ (9.8 × 10$^{6}$) |
| PD-induced    | 4.0 × 10$^{10}$ (1.2 × 10$^{6}$) | 1.4 × 10$^{10}$ (6.0 × 10$^{6}$) | 1.3 × 10$^{10}$ (9.6 × 10$^{6}$) |

**Notes.** Values in parentheses indicate observational or RD line-fitting (model) errors.

*a* Jiménez-Serra et al. (2016).

**Table 6**

| Model         | CH$_3$CHO (cm$^{-2}$) | CH$_3$OCH$_3$ (cm$^{-2}$) | CH$_3$OCHO (cm$^{-2}$) |
|---------------|------------------------|---------------------------|-------------------------|
| Observation   | 3.2 × 10$^{12}$        | 7.7 × 10$^{10}$ (3.2 × 10$^{11}$) | 2.3 × 10$^{10}$ (2.8 × 10$^{10}$) |
| Control       | 3.3 × 10$^{10}$ (3.7 × 10$^{8}$) | 2.8 × 10$^{10}$ (3.6 × 10$^{8}$) | 1.4 × 10$^{10}$ (6.9 × 10$^{8}$) |
| 3-B           | 3.6 × 10$^{10}$ (4.2 × 10$^{8}$) | 4.2 × 10$^{10}$ (5.7 × 10$^{8}$) | 5.3 × 10$^{10}$ (2.1 × 10$^{8}$) |
| 3-B+3-BEF     | 1.1 × 10$^{12}$ (4.6 × 10$^{7}$) | 1.8 × 10$^{10}$ (1.2 × 10$^{7}$) | 1.3 × 10$^{10}$ (1.3 × 10$^{7}$) |
| E-R           | 3.3 × 10$^{10}$ (3.9 × 10$^{8}$) | 2.9 × 10$^{10}$ (2.9 × 10$^{8}$) | 1.4 × 10$^{10}$ (6.8 × 10$^{8}$) |
| PD-induced    | 3.3 × 10$^{10}$ (3.7 × 10$^{8}$) | 2.8 × 10$^{10}$ (3.6 × 10$^{8}$) | 1.5 × 10$^{10}$ (7.3 × 10$^{8}$) |

**Notes.** The off-center position for the observations is 4000 au, corresponding to the observational methanol peak of L1544 (Jiménez-Serra et al. 2016). In the models, the fractional abundance peak occurs around 2000 au. Values in parentheses indicate observational or RD line-fitting (model) errors.

*a* Jiménez-Serra et al. (2016).

**Table 7**

| Model         | CH$_3$CHO (cm$^{-2}$) | CH$_3$OCH$_3$ (cm$^{-2}$) | CH$_3$OCHO (cm$^{-2}$) |
|---------------|------------------------|---------------------------|-------------------------|
| Control       | 2.5 × 10$^{10}$ (3.8 × 10$^{6}$) | 3.9 × 10$^{10}$ (8.8 × 10$^{6}$) | 1.3 × 10$^{10}$ (1.4 × 10$^{6}$) |
| 3-B           | 3.0 × 10$^{10}$ (3.1 × 10$^{7}$) | 5.7 × 10$^{10}$ (4.4 × 10$^{7}$) | 3.7 × 10$^{10}$ (3.5 × 10$^{7}$) |
| 3-B+3-BEF     | 7.5 × 10$^{11}$ (2.0 × 10$^{8}$) | 1.5 × 10$^{10}$ (2.2 × 10$^{8}$) | 9.5 × 10$^{11}$ (6.0 × 10$^{8}$) |
| E-R           | 2.6 × 10$^{10}$ (3.8 × 10$^{7}$) | 4.0 × 10$^{10}$ (8.7 × 10$^{7}$) | 1.3 × 10$^{10}$ (1.4 × 10$^{7}$) |
| PD-induced    | 2.5 × 10$^{10}$ (3.7 × 10$^{6}$) | 3.9 × 10$^{10}$ (8.8 × 10$^{6}$) | 1.5 × 10$^{10}$ (1.5 × 10$^{6}$) |

**Note.** Values in parentheses indicate RD line-fitting errors.
in which accumulated mantle material is ejected from the grains.

### 3.3. Optimization of the 3-BEF Model

As discussed in Section 3.2, the formation of methyl formate (CH$_3$OCHO) through the 3-BEF mechanism is so efficient that CH$_3$OCHO is significantly overproduced, while this is not the case for acetaldehyde (CH$_3$CHO). The 3-BEF mechanism as described in Section 2.5 is assumed to proceed with 100% efficiency; however, the appropriate value in individual cases could be lower if the exothermic energy available from the initiating reaction ($E_{\text{reac}}$) is similar in magnitude to the activation-energy barrier ($E_A$) of the subsequent reaction. Assuming the energy is initially released into the vibrational modes of the excited species, it may not be available in the required mode for reaction with an adjacent species to occur before that energy is lost to the surface, or indeed that the excited species diffuses away entirely from its reaction partner. If the excited product has $s$ internal vibrational modes, the 3-BEF process would be expected to have substantially suboptimal efficiency in the case where $E_A > E_{\text{reac}}/s$, while it would not occur at all in the case where $E_A > E_{\text{reac}}$. The former condition would appear to hold for the reactions shown in Equations (20), in which methyl formate is produced; here, $s$(CH$_3$O) = 9, $E_{\text{reac}}$ ≈ 10,200 K, and $E_A$ = 3967 K for the CH$_3$O + CO $\rightarrow$ CH$_3$OCO reaction (Huynh & Violi 2008).

The Rice–Ramsperger–Kassel (RRK) theory may be introduced to obtain a statistical estimate of the efficiency. Using the same formulation that is employed to determine the probability of chemical desorption in the model (Garrod et al. 2007), the probability of a successful 3-BEF process would be

$$P = \left[1 - \frac{E_A}{E_{\text{reac}}}\right]^{-1},$$

where $s$ now includes an additional vibrational mode representing the reaction coordinate (i.e., $s$(CH$_3$O) = 10). For the reactions forming CH$_3$OCHO, the values provided above give a probability of 1.2%, while for the reactions producing CH$_3$CHO and CH$_3$OCH$_3$ the probability would be 73%. This shows that the $P$(CH$_3$OCHO) of 1 originally introduced in our 3-B+3-BEF model was too high, explaining the overproduction of that species.

For the present models, in which only three 3-BEF processes are explicitly considered, we empirically test a selection of efficiencies for the reaction to form CH$_3$OCHO, ranging incrementally from 100% to 0.1% in factors of 10; the other two 3-BEF reactions are assumed to operate at maximum
efficiency. It is found that a probability of 0.1% best reproduces the molecular column densities from the observations.

The empirically determined optimal efficiency is clearly lower than the simple RRK treatment above would suggest. However, the latter does not include competition between reaction and diffusion of the excited species, which could account for at least a factor of a few, representing several diffusion directions. Likewise, additional translational degrees of freedom of the excited species could be considered in Equation (23), rather than just one reaction coordinate. We note also that these modifications would reduce the efficiency of the other two 3-BEF reactions considered here, perhaps bringing them closer to around 10%. The molecular dynamics study by Fredon et al. (2017) of reaction-induced nonthermal diffusion would indeed suggest that translational motion would be a necessary factor to consider in a detailed treatment of the 3-BEF process (although it should be noted that those authors assumed all of the energy to be immediately released into translational modes, rather than distributed also into internal vibration and/or rotation).

Figure 9 shows RDs obtained from LTE radiative-transfer calculations based on the 3-BEF Best model molecular profiles, with the beam directed toward the core center. Table 8 compares the molecular column densities toward the core center from this model with the observational literature values. The errors (in parentheses) for the modeled column densities are derived from the standard deviation of the linear regression fitting in the rotation diagrams. The three-body mechanisms introduced here are efficient enough to reproduce the amount of CH₃OCHO and CH₃CHO in the prestellar core when an appropriate efficiency for the 3-BEF mechanism is adopted.

Figure 10 compares the chemical distribution of the 3-BEF Best results (solid lines) with those of the control (dotted lines) and the normal 3-BEF (dashed lines) models. While the amount of CH₃OCHO is significantly reduced in the 3-BEF Best model compared to the normal 3-BEF in both gas and solid phases,
the population of CH$_3$OCH$_3$ increases (by roughly an order of magnitude in the gas); the weakening of the 3-BEF mechanism for methyl formate production leaves more of the CH$_3$O radical available to participate in other reactions, including the regular 3-B mechanism (CH$_3$ + CH$_3$O) that produces dimethyl ether. A commensurate increase is seen in the column density values. The adjustment to the efficiency of MF production through the 3-BEF process also reduces the solid-phase abundance of that molecule with respect to water back to more plausible values that are in line with the maximum typical values observed in hotter sources (i.e., around 10$^{-8}$ with respect to H$_2$). The fraction is higher beyond around 5000 au, but the total ice abundance at these positions would also be somewhat lower.

### 3.4. CO Hydrogenation and CH$_3$OH Abundances

The CH$_3$OH map of Bizzocchi et al. (2014) shows a highly asymmetric nonuniform ring surrounding the dust peak of L1544. This morphology is consistent with central depletion...
and preferential release of methanol in the region where CO starts to freeze out significantly. Jiménez-Serra et al. (2016) shows that COMs are actively formed and already present in this methanol peak.

The upper panel of Figure 11 shows the radial distribution of CH₃OH fractional abundance for each of the chemical models; abundances are very similar for all models at all positions. Methanol in the gas is mainly formed as the result of the hydrogenation of grain-surface CO all the way to CH₃OH, followed by chemical desorption. The radial distribution of the fractional abundance of gas-phase methanol has its peak well beyond where the observations would suggest. However, it should be noted that the gas density in these more distant regions drops off significantly, according to the physical profile. The location of the peak in absolute abundance would provide a better comparison directly with observations, although the best method is to consider the column density structure of methanol explicitly.

The lower panel of Figure 11 shows the normalized convolved intensity of a representative emission line of methanol as a function of the beam offset from the center, using the radiative-transfer model already described with the 3-BEF Best model data. Because the lines are optically thin and are well represented by an LTE treatment (see Figure 12 and Table 9), the line intensity profile scales well with the column density profile along each line of sight. The modeled methanol emission shows a peak near 4000 au as reported in the observations, even though this feature is not so obvious, as the slope is quite gentle. The same treatment is shown for the other three COMs of interest. Methyl formate shows a fairly similar distribution of emission to that of methanol, while the other two COMs show peaks at 2000 au as seen in the fractional abundances. The representative molecular transition used for this analysis is denoted by an asterisk in Tables 4 and 9.

The full RD analysis is performed for methanol as for the other COMs. The seven E-transition lines of CH₃OH that were detected by Taquet et al. (2017) are chosen for this (Table 9). A single fit to all lines provides a column density of $8.6 \times 10^{13}$ cm⁻² at the core center. This value is roughly consistent with the observation ($2.6 \times 10^{13}$ cm⁻²; Bizzocchi et al. 2014). The precise value, as with those of the other COMs, will be dependent on the fidelity of the chemical desorption treatment used here.
4. Discussion

Of the several new nondiffusive processes tested here, the E-R mechanism appears to have the least effect, due largely to the low surface coverage of reactive species. Those reactive species that might benefit from the spontaneous arrival of a reaction partner from the gas phase always maintain low fractional surface coverage due to their reactivity with highly diffusive surface species, e.g., atomic H. Species that do build up a large surface coverage, like CO, tend to have large barriers to reaction, so that incoming species are more likely to diffuse away than to react spontaneously. The importance of the E-R process to typical surface reactions is unlikely to be substantial under any physical conditions as long as atomic H remains mobile.

Photodissociation-induced reactions, in which the PD process acts spontaneously to bring a reactive radical into contact with some other species, has no significant influence on the gas-phase abundances of complex organics, but has a strong effect on the COM content of the ice mantles. The basic three-body process provides substantial improvement in the gas-phase abundances of COMs, notably methyl formate and dimethyl ether, by allowing the products of diffusive reactions (in some fraction of cases) to find a reaction partner themselves without requiring further diffusion. However, the excited-formation mechanism, which allows the reaction of excited, newly formed radicals with stable species (in spite of activation-energy barriers) has the strongest effect, and is again most important for methyl formate and acetaldehyde. An adjustment to the efficiency of these processes, based on the available energy from the initiating reaction, appears to provide the best match with observational column densities of those molecules.

It is important that the process that seems to reproduce most effectively the gas-phase abundances of the COMs (3-BEF) is one that occurs on the grain/ice surface itself, rather than deep within the mantle, allowing chemical desorption to return some fraction of the product to the gas phase. The details of the various mechanisms and their implications are discussed in more detail below.

4.1. H Abstraction/Recombination as an Amplifier of Chemical Desorption

The models show substantial success in reproducing observed gas-phase column densities through molecular production mechanisms operating on the surfaces of the icy dust grains. Consideration should therefore be given to the efficiency of the desorption mechanism that releases surface molecules into the gas phase. Although photodesorption is included in all of the models presented here (with the explicit assumption of fragmentation of methanol as the result of this process), the most important ejection mechanism for grain-surface COMs is chemical desorption. In these models, this occurs with a maximum efficiency per reaction of 1%; this efficiency is further lowered according to the RRK-based treatment described by Garrod et al. (2007).

Thus, the formation of, for example, acetaldehyde, through Equation (18), culminating in the addition of a H atom to the CH_3CO radical, may sometimes produce gas-phase CH_3CHO. However, the immediate desorption following its formation is not the only factor in ejecting those molecules into the gas. The chemical desorption effect is considerably amplified by the abstraction of H atoms from existing surface COMs, followed rapidly by recombination of the resulting radical with another H atom, inducing the ejection into the gas of some fraction of the product molecules. In the case of methanol, for instance, once it is formed on the grain surface through the repetitive addition of H to CO, the abstraction of H from CH_3OH by another H atom allows it to be transformed back to its precursor (CH_3O/CH_3OH), providing additional chances for chemical desorption—indeed, this process of addition and abstraction was suggested by Minissale et al. (2016) as a mechanism by which the depletion of CO from the gas phase could be slowed and its grain-surface conversion to methanol delayed. Similar H-abstraction/addition processes are present for each of the larger COMs of interest in our models.

To understand how significantly this process takes part in the overall chemical desorption scheme, four additional test models were run for conditions appropriate to the core center, turning off the H-abstraction reaction for each molecule (the three larger COMs plus methanol). The local fractional abundances of COMs from each test model are compared with the control in Table 10. When the H-abstraction reaction of a specific COM is turned off, the gas-phase abundance of that molecule decreases by ~1 order of magnitude. Furthermore, when H abstraction from methanol is switched off, it reduces the fractional abundance of other COMs such as CH_3OCHO and CH_3OCH_3, whose surface production is closely related to the CH_3O radical. The abstraction of H from methanol by other H atoms in fact strongly favors the production of the CH_2OH radical; the network employed here uses surface reaction rates for these processes calculated by F. Goumans and S. Andersson (see Garrod 2013) based on harmonic quantum transition-state theory. However, as per the network of Garrod (2013), the recombination of CH_3OH with H is assumed to produce either methanol or H_2CO+H_2 with a branching ratio of 1:1. The production of formaldehyde in this way can then lead to reaction with H atoms again; this forward process strongly favors production of the CH_3O radical, thus influencing the production of DME and MF.

4.2. COM Distribution and COM Peaks

As seen in Figure 10 for the 3-BEF Best model, the COMs in the gas phase have their lowest fractional abundances at the core center, gradually increasing toward the outer shell of the prestellar core. This general feature is observed regardless of model type (Figure 4). Interestingly, a local fractional abundance peak for COMs is found at around 2000 au, especially for CH_3CHO and CH_3OCH_3. This result suggests at least qualitative agreement with the observational result of Jiménez-Serra et al. (2016); those authors performed deep observations of the COMs toward the low-density outer shell (4000 au) as well as the core center of L1544. While they observed higher abundances for all three COMs at the outer position, the level of enhancement for CH_3OCHO was ambiguous, due to its large observational error.

The behavior seen in the models indicates that there are two possible peak features (or two plausible causes for observed peaks) that could become apparent in column densities or line intensities (e.g., lower panel of Figure 11) as opposed to fractional abundances. The first of these relates simply to the increased fractional abundances of COMs at large radii, combined with the drop off in overall gas density at the greatest extents, producing a peak in the absolute molecular
Table 10
Local Fractional Abundances of COMs at the Core Center, Using the 3-BEF Best Model with Selected Reactions Switched Off

|                  | All on CH₃OH=H | CH₃CHO=H | CH₃OCHO=H | CH₃OCH₂=H |
|------------------|----------------|----------|-----------|-----------|
| CH₃OH            | 2.9 × 10⁻¹³   | 2.9 × 10⁻¹¹| 2.9 × 10⁻¹¹| 2.9 × 10⁻¹¹|
| CH₃CHO           | 4.5 × 10⁻¹³   | 3.8 × 10⁻¹⁴| 4.5 × 10⁻¹³| 4.5 × 10⁻¹³|
| CH₃OCHO          | 1.4 × 10⁻¹²   | 1.4 × 10⁻¹⁴| 7.2 × 10⁻¹⁴| 1.4 × 10⁻¹²|
| CH₃OCH₂          | 2.6 × 10⁻¹⁴   | 2.6 × 10⁻¹⁴| 2.6 × 10⁻¹⁴| 1.4 × 10⁻¹⁵|

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abundances that manifests in the resulting column density or line intensity profiles. This behavior is especially apparent for methyl formate (which does not show the bump-like feature at around 2000 au). This peak seems to be in reasonably good agreement with the observational peak position; Figure 11 indicates peak line intensities around 4000–6000 au. A major cause of the lack of COMs in the gas phase at small radii in terms of fractional abundance, e.g., Figure 10) is that most of the gas-phase material at those locations has already accreted onto the grains and become locked into the ice mantles by the end time of the models; little CO exists in the gas phase (on the order of 10⁻⁷ with respect to total H), thus grain-surface chemistry involving CO-related products is limited. At the greatest radii, freeze-out is incomplete and CO chemistry is still active with the accretion of new CO. Somewhat greater gas-phase abundances of atomic H at large radii, caused by the density slope, also encourage H abstraction from COMs on the surfaces, followed by recombination and chemical desorption.

The local peak at 2000 au in the fractional abundances of acetaldehyde and dimethyl ether occurs particularly in models that use the 3-B and 3-BEF processes and also manifests in the resultant column density profiles of those molecules (lower panel of Figure 11). The gas density at the 2000 au position is at least three times higher than at the outer-peak region (4000–6000 au), so the inner peak tends to dominate over the outer in its contribution to column densities, for the models/molecules in which that inner peak occurs.

What is the origin of the inner peak at 2000 au? It is related to the freeze-out of gas-phase material through the core. It traces a position at which the net rate of accretion of gas-phase material onto the grains is close to zero, caused by the high degree of depletion that has already occurred for most major gas-phase species other than hydrogen. For example, the gas-phase abundance of CO reaches a local minimum at this position. At radii internal and external to the 2000 au peak region, there is slightly more gas-phase material remaining to be accreted onto dust grains at the end of the model runs, thus the ice mantles still continue (slowly) to grow. This local peak in freeze-out is due to the combined density and temperature profiles used in the models. The adsorption rates of neutrals scale with gas density, which is greatest at the core center, but they also scale with the square root of the gas temperature, which is greater at larger radii. The 2000 au position is the point where the two profiles combine to give the largest total adsorption rate. The position of the maximum freeze-out position is thus strongly dependent on the density and temperature profiles. Furthermore, given a slightly longer model run time, the freeze-out peak would likely widen, as other positions reached a state of near-zero net accretion onto grains.

The stronger production of COMs (acetaldehyde and dimethyl ether) around this 2000 au position peak is a consequence of the changing freeze-out conditions described above. Once the net rate of freeze-out reaches zero, it indeed undergoes a reversal in which there is a small, net rate of loss of material from the grains. This loss is caused by the desorption of molecular hydrogen from the grain surface, which is slowly replenished by the gradual outward diffusion of H₂ molecules embedded deep in the ice mantles. This H₂-loss process occurs throughout all model runs, but is of little importance until the adsorption of nonvolatile species diminishes, when gas-phase species become depleted. Once this net loss of material from the grains starts to occur, some molecules embedded in the upper layer of the ice mantles are “uncovered,” becoming available for surface chemical processing. Most importantly, this includes CH₃, from which a H atom may be chemically abstracted through several mechanisms, increasing both the production rate of CH₃ and its surface abundance. This drives up the three-body production of acetaldehyde and dimethyl ether (Equations (12)–(15)), which are chemically desorbed into the gas phase—either directly, or as the result of H abstraction and recombination on the surface.

The behavior of the inner peak in certain COMs should therefore be treated with a degree of skepticism. Not only does its position depend on the interplay of the observationally determined physical profiles, but its strength must be time dependent. Furthermore, the ability of the chemical model to treat accurately the return (“uncovering”) of mantle material to the ice surface is limited by the use of only a single mantle phase, rather than the consideration of distinct layers within the ice (cf. Taquet et al. 2014). If most of the methane residing in the mantles is present mainly in the deepest layers, the inner-peak effect described above would be overestimated here. It is also the case that, even with this mechanism in play, the gas-phase abundance of dimethyl ether is insufficient to reproduce observed column densities in L1544 (although see Section 4.6). If such a mechanism is active, considering the uncertainty in its precise position (based on models), it may not be easily distinguished from the outer peak at 4000+ au.

The peak in methanol column density occurs at the outer-peak position, caused again by a peak in absolute abundance of that molecule. It is noteworthy that in the present models, the local fractional abundance of methanol does not need to exceed a value of a few 10⁻⁹ to be able to reproduce the observed column density. Again, the strength of the methanol peak will be dependent on the efficiency of chemical desorption for that molecule, which is not well constrained through purely experimental means.

4.3. The Effect of Diffusion Barriers

In many astrochemical models including MAGICKAL, chemistry on the grains is governed by the diffusion of surface species via thermal hopping (any nondiffusive processes notwithstanding). The energy required for a particular species to hop from one surface binding site to another is given by the diffusion barrier \(E_{\text{diff}}\); this value is parameterized in the chemical model as some fraction of the desorption energy,
i.e., $E_{\text{diff}}/E_{\text{des}}$. Even though this is a key parameter to describe the mobility of species on grain surfaces, the exact value has not historically been well constrained, broadly ranging from 0.3 to 0.8. In the present models, this parameter was set to $E_{\text{diff}}/E_{\text{des}} = 0.6$ for all atomic species, which leans toward a high value based on recent experimental estimates by Minissale et al. (2016), who suggested 0.55 for atoms. In our past models (e.g., Garrod 2013), atoms and molecules were assigned the same fractional barrier value of 0.35, based on the optimum value for CO. All molecular species in the present models retain the 0.35 value.

At the very low surface temperatures that are found in prestellar cores, the diffusion of atoms in particular is of great importance. For this reason, test models were also run using the previous fractional diffusion barrier of 0.35 for atoms. Figure 13 shows a comparison of COM abundances for the two cases, shown for the end time of the 3-BEF Best model run using the L1544 physical profiles as before. Using the higher $E_{\text{diff}}/E_{\text{des}}$ ratio, the COMs typically show much higher abundances at positions near the core center. This result is somewhat contradictory to the expectations of Vasyunin et al. (2017), who suggest that the $E_{\text{diff}}/E_{\text{des}}$ ratio would not play a crucial role in cold environments, as diffusion of H and H$_2$ via tunneling is dominant. In our model, while tunneling through chemical barriers is included, surface diffusion via tunneling is not, as the barriers are assumed to be too broad for tunneling to be effective. In this case, the higher diffusion barrier for the atomic species means that the time taken for H atoms to reach and react with surface radicals is increased. This consequently raises the lifetimes of those radicals on the surface (see Figure 14), which in turn renders the nonthermal mechanisms explored here more effective, increasing the production of COMs.

It should be noted that the higher $E_{\text{diff}}/E_{\text{des}}$ ratio does not always result in a larger amount of COMs (or radicals) on the grain surface. For example, the discrepancy in the COM abundances between the two models decreases at large radii, and methyl formate and acetaldehyde here are even a little more abundant in the case where atomic diffusion barriers are lower, due to slightly more effective H abstraction from methane to produce CH$_3$. 

Figure 13. Comparison of chemical distribution of the COMs in the 3-BEF Best models with different values of $E_{\text{diff}}/E_{\text{des}}$ for atoms.

Figure 14. Comparison of chemical distribution of the reactants in the 3-BEF Best models with different values of $E_{\text{diff}}/E_{\text{des}}$ for atoms.
The variation of the \( E_{\text{dif}}/E_{\text{des}} \) ratios thus has an important effect on the chemical model results; the higher value for atomic species, and for \( H \) in particular, reproduces COM abundances more effectively, through the increase in radical lifetimes. Senevirathne et al. (2017) calculated the distribution of binding energies and diffusion barriers for \( H \) on an amorphous water surface, suggesting representative values for each; although their hydrogen-atom binding energy (661 K) is higher than the value used in our models (450 K), their diffusion barrier (243 K) is close to the value we use here (270 K) for the \( E_{\text{dif}}/E_{\text{des}} = 0.6 \) models. We note also that Senevirathne et al. (2017), based on their calculations of diffusion rates using quantum transition-state theory, aver that tunneling (as opposed to the thermal mechanism) is likely of limited importance under most temperature conditions in dark clouds; our use of purely thermal diffusion rates in MAGICKAL is thus broadly consistent with that work.

In other models, in which nondiffusive chemical processes were not included, the variation of the \( H \) diffusion barrier might have less of an effect, as most of the active chemistry in that case would involve only atomic \( H \). The lifetime of the radicals would therefore be of less relevance, because \( H \) would still be the dominant reaction partner. In the present models, the mobility of atomic hydrogen is a major determinant of the effectiveness of nonthermal processes in producing complex species.

### 4.4. Gas-phase Processes

Due perhaps to the generally low abundances of DME that our chemical models provide, they do not appear to reproduce the correlation between \( CH_3OCHO \) and \( CH_3OCH_3 \) sometimes observed in various evolutionary stages of star-forming regions (Jørgensen et al. 2011; Brouillet et al. 2013; Jaber et al. 2014). As a means by which such a relationship might arise, Brouillet et al. (2013) suggested protonated methanol \( CH_3OH_2^+ \) in the gas phase as the common precursor to \( CH_3OCHO \) and \( CH_3OCH_3 \) via reactions with \( HCOOH \) and \( CH_3OH \). As a test, the proposed reactions were incorporated into our chemical network; however, they were too slow to be effective in producing \( CH_3OCHO \) and \( CH_3OCH_3 \) in our model, due to the low abundance of protonated methanol in the gas.

Recently, potentially influential gas-phase reactions were proposed by Shannon et al. (2013, 2014), who found that reactions of either \( OH \) or \( C_3(\text{P}) \) with methanol are efficient at low temperatures, due to quantum tunneling:

\[
\text{OH} + \text{CH}_3\text{OH} \rightarrow \text{CH}_3\text{O} + \text{H}_2\text{O} \\
C_3(\text{P}) + \text{CH}_3\text{OH} \rightarrow \text{CH}_3 + \text{HCO}.
\]

The gas-phase methanol reactions could act not only as an efficient loss process for gas-phase methanol, but also produce more radicals that would be available as reactants to form other COMs when they accrete onto grain surfaces, or directly in the gas phase if such processes are efficient. Vasyunin & Herbst (2013) suggested a gas-phase radiative association reaction between the radicals that are produced by the above mechanisms, to form DME:

\[
\text{CH}_3\text{O} + \text{CH}_3 \rightarrow \text{CH}_3\text{OCH}_3 + h\nu.
\]

To understand how significantly these reactions would affect the overall formation of COMs in our chemical model, we ran a test model that included all three (with rate coefficients on the order of \( 10^{-10} \text{ cm}^{-3} \)). However, gas-phase methanol was still predominantly destroyed by ion–molecule reactions at the core center. The contribution of the above neutral–neutral reactions to the loss of gas-phase methanol was minor (\( \sim 2\% \)), hardly changing the abundances of methanol and the three COMs, while the radiative association reaction also showed minimal influence.

Balucani et al. (2015) proposed a gas-phase mechanism that would form methyl formate from dimethyl ether through the radical \( CH_3OCH_2 \). The dimethyl ether itself would form through the efficient radiative association of the radicals \( CH_3 \) and \( CH_3O \):

\[
\text{CH}_3OH_3 + (\text{F, Cl}) \rightarrow \text{CH}_3OCH_2 + (\text{HF, HCl}) \quad \text{CH}_3OCH_2 + O \rightarrow \text{HCOOCH}_3 + H.
\]

Although our network does not include fluoride, the incorporation of the other reactions into our model did not make a meaningful difference to the results, because they involve a one-way process where \( CH_3OCH_3 \) is converted into \( CH_3OCHO \). In our chemical model, neither the radiative association of the radicals \( CH_3 \) and \( CH_3O \) nor any other processes were efficient enough to form abundant \( CH_3OCH_3 \). As such, several key reactions concerning gas-phase chemistry of COMs do not affect our chemical model significantly.

Thus, at least under the conditions tested in our physical model, we found no efficient gas-phase mechanisms that could produce either DME or MF.

### 4.5. Other Surface Processes

The three-body excited-formation mechanism included here is especially efficient for the initiating reaction \( H + \text{CH}_2 \rightarrow \text{CH}_3 \), which is highly exothermic, but which also results in a small product, \( CH_3 \), that has only a limited number of vibrational modes in which the resulting energy may be stored. The models suggest that when this is coupled with highly abundant CO on the grain surface, the subsequent reaction between the two proceeds at a sufficient pace to produce enough \( CH_4CO \) (and hence \( CH_3CHO \)) to be able to explain the gas-phase abundance of the latter molecule (given an adequate desorption mechanism). The production of \( CH_3O \) via the hydrogenation of formaldehyde is also exothermic, but not sufficiently so to allow the subsequent reaction with abundant CO to proceed at high efficiency. Nevertheless, this low-efficiency mechanism is capable of producing enough \( CH_3OCO \) (and hence \( CH_3OCHO \)) to account for the presence of methyl formate in the gas phase.

As noted in Section 3.3, a more detailed treatment of the 3-BEF mechanism should include not only the energy partition between bonds, but also translational degrees of freedom of the excited species. This would impact the RRK calculation, but could also provide an alternative outcome to the process. The RRK treatment as formulated in Section 3.3 assumes that the efficiency of the process is determined solely by the competition between energy going into the “reaction mode” and energy being lost to the surface. However, if diffusion spontaneously occurred, moving the two reactants apart, then the process would automatically end (unless another reactant were present in this new site), regardless of the energy status of
the excited species. We would expect this effect to reduce efficiency by a factor of, say, 4 (on the basis of there being four available diffusion directions), even for the otherwise efficient 3-BEF mechanism that produces CH$_3$CO/CH$_2$CHO. The production of CH$_3$CHO may therefore be somewhat less efficient than the simple 100% approximation used in the treatment presented here.

It is also of interest to consider specifically the possible effects of reaction-induced diffusion, such as that studied by Fredon et al. (2017) for stable molecules including methane. If reactive species like CH$_3$ were able to undergo some nonthermal diffusion as the result of excitation caused by their formation, they could react with other radicals that they could not otherwise reach under low-temperature (i.e., nondiffusive) conditions. In fact, as we allude to in Section 2.4, the standard (nonexcited) 3-B mechanism that we already implement in the models will automatically include such processes to a first approximation. The treatment that we construct for 3-B processes does not explicitly require the reactants to be immediately contiguous, but rather to become so immediately following the initiating reaction. If one were to consider a newly formed radical species, A, taking some finite and approximately straight-line trajectory across an ice surface, the probability of it encountering some reaction partner, B, along its path would still be given, to first order, by $N(B)/N_A$, as already included in Equation (6). The simple 3-B mechanism is therefore broad enough to cover this specific case also.

While the 3-BEF mechanism for the production of the dimethyl ether precursor, CH$_3$OCH$_3$, should be highly efficient based on the statistical calculations in Section 3.3, the lower abundance of H$_2$CO on the grain surfaces appears to be too low to allow this mechanism to account for gas-phase DME. It should also be noted that in this work, it was assumed that DME is the only product of this reaction. It is possible, and perhaps favorable, for ethanol (C$_2$H$_5$OH) also ultimately to be formed, if the methyl radical attaches to the carbon atom in formaldehyde, producing a radical C$_2$H$_5$O. This would naturally limit the yield of DME through the suggested excited-formation mechanism.

Are there alternative surface processes that might produce sufficient dimethyl ether if the reactants could be brought together through some nondiffusive process? One possibility might be the reactions of the carbene CH$_2$ with methanol (CH$_3$OH). Methylene, CH$_2$, is a diradical in its ground (triplet) state. Reactions of triplet CH$_2$ with methanol could involve the abstraction of hydrogen from CH$_3$OH, followed by the immediate radical–radical addition of the resultant CH$_3$ to the remaining CH$_3$O or CH$_2$OH. The review of Tsang (1987) suggests gas-phase rate coefficients for the abstraction processes (without the subsequent recombination); the activation barrier for the CH$_3$O branch is marginally lower than that for CH$_2$OH, indicating that CH$_2$O (and thence DME) might be the preferred product. On a dust-grain/ice surface, the production of CH$_3$, either by H addition to CH or by the barrier-mediated reaction of H$_2$ with atomic C, would likely be exothermic enough to allow the subsequent abstraction barriers to be overcome. However, abstraction might be fast in any case, even without (vibrationally) excited CH$_2$, due to hydrogen tunneling through the activation-energy barrier.

Another possibility is that the higher-energy singlet CH$_2$ could undergo a direct, barrierless insertion into the methanol molecule, producing either dimethyl ether or ethanol. Bergantini et al. (2018) investigated the action of singlet CH$_2$, produced through the irradiation of a mixed CH$_4$/CH$_3$OH ice, to produce DME and ethanol in this way; they found essentially equal production of the two branches. If, instead of the dissociation of methane, the hydrogenation of carbon on the grain surfaces were the means by which singlet CH$_2$ were produced, then this mechanism could occur effectively as a nondiffusive (i.e., three-body) process, although the short lifetime of the singlet methylene might make a diffusive meeting of the reactants unlikely. Although the dissociation of methane, as per those experiments, is an entirely plausible starting point for the production of COMs within ice mantles, it is an unlikely explanation for the gas-phase detection of COMs.

A further consideration, relating to the production of CH$_3$CHO via the 3-BEF mechanism, is the possible production of ketene, CH$_2$CO, through the reaction CH$_2$ + CO → CH$_2$CO. This process could also occur through the 3-BEF mechanism, following production of methylene through exothermic surface reactions. The more complex nature of the coding of the 3-BEF mechanism required us to include only the three 3-BEF mechanisms directly related to MF, DME, and AA in the present work, but the application of this mechanism to the full chemical network might impact ketene production. An immediate question would be whether ketene production might also preclude the production of acetaldehyde, as the CH$_2$ used to produce ketene would otherwise be required to produce the CH$_3$ needed for AA production. Furthermore, one could argue that the production of CH$_3$ in the presence of CO, as needed for our 3-BEF route to AA, would first require contiguous CH$_2$ and CO, and that this CH$_2$ would also have to be formed in the presence of CO, making ketene the preferred product instead of AA. Such a view implicitly assumes that there is no reaction-induced diffusion occurring, when in fact, due to the large exothermicities of the reactions in question, it is highly likely that there is some form of diffusion following each reaction. As mentioned above, this diffusion does not make either the 3-B nor the 3-BEF treatments any less accurate, as we do not explicitly rule out such occurrences. Rather, it might be better to assume that, on a surface at least, such reaction-induced diffusion is the rule, rather than the exception, and thus that there is no expectation nor requirement that any newly formed reaction product considered in the 3-B mechanisms necessarily meets its own reaction partner within its immediate surroundings. In that case, any conditionality in the production of one species from another, based on location, would be lost. On the topic of ketene in particular, it is also possible that it may be hydrogenated to acetaldehyde anyway; the reaction H + CH$_2$CO → CH$_3$CO is assumed in our network to have a barrier of 1320 K (Senosiaian et al. 2006), which is lower than, for example, the typically assumed barrier to hydrogenation of CO. In future work, we will apply the 3-BEF process to the entire surface network, allowing the relationship between acetaldehyde and ketene to be explored more deeply.

Fedoseev et al. (2015) conducted experiments investigating the production of COMs, specifically glycolaldehyde and ethylene glycol, through nondiffusive surface reactions of HCO radicals produced through H and CO co-deposition. Those experiments did not detect any methyl formate production, but follow-up work by Chuang et al. (2016), who co-deposited various combinations of CO, H$_2$CO, CH$_3$OH, and H, demonstrated methyl formate production in the setups that
involved direct deposition of formaldehyde ($\text{H}_2\text{CO}$). Thus, under the conditions of their experiments, the HCO and $\text{CH}_4$ radicals required for the radical–radical reactions to produce $\text{CH}_3\text{OCHO}$ derived mainly or uniquely from $\text{H}_2\text{CO}$ reactions with atomic H (either H addition or H abstraction by H atoms). In the case of CO and H deposition alone, they suggested that the reaction between two HCO radicals dominates, producing glyoxal ($\text{HOCOOK}$) that can be further hydrogenated to glycolaldehyde ($\text{CH}_2(\text{OH})\text{CHO}$) and ethylene glycol ($\text{HOCH}_2\text{CH}_2\text{OH}$).

The reaction network we use here includes HCO–HCO reaction routes (Garrod et al. 2008), with one branch producing glyoxal and an equal branch producing CO and $\text{H}_2\text{CO}$ through a barrierless H-abstraction process. Our network does not include the further hydrogenation of glyoxal, but the removal of HCO radicals should be treated well enough.

In our astrochemical models (in which the overall system is much more complicated than the laboratory setups, with many more species and processes), grain-surface formaldehyde and methanol are produced through CO hydrogenation by H atoms; in the experiments, the CO + H system does not produce enough formaldehyde to allow substantial production of $\text{CH}_2\text{O}$ and thence methyl formate. The outcomes of the models, which are run over astronomical timescales, should not therefore be expected to correspond directly with the experimental outcomes. However, the mechanism of non-diffusive radical chemistry that seems to produce methyl formate in the experiments (via HCO + $\text{CH}_2\text{O}$) is present in our models (the basic three-body mechanism).

The key comparison with the experiment concerns our implementation of the excited three-body formation mechanism for the reaction of $\text{CH}_2\text{O}$ with CO (the other 3-BEF mechanisms tested in this work involve $\text{CH}_3$ and are therefore not tested in the laboratory experiments). The very low efficiency that we require (0.1%) for immediate reaction is likely to be too small to have an important effect in a laboratory regime where the regular three-body process is presumably efficient (unlike in our prestellar core models). In this sense, it seems superficially consistent with the experiments, as there are no experimental setups in which methyl formate was not found in which our excited-formation mechanism would predict it to be highly abundant. Indeed, our mechanism should only become important if other means of production (such as the regular three-body process) are already weak. Thus, it may be difficult to test the excited-formation mechanism for methyl formate through experimental means.

Another possibility exists for the production of all three COMs considered here: that is, that they are produced in the ice mantles, through UV processing (or some other means). The ice-mantle material would then have to be removed by some violent process such as sputtering by cosmic rays. (Such a process would also result in some degree of complex molecule production, e.g., Shingledecker et al. 2018.) However, it is unclear whether such mechanisms would be capable of maintaining gas-phase abundances of COMs at the required levels.

A separate point of discussion concerns the experimental evidence surrounding the interaction of H atoms specifically with solid-phase acetaldehyde. Bisschop et al. (2007) studied the deposition of H onto a predeposited surface of pure $\text{CH}_3\text{CHO}$ at temperatures ranging from 12.4 to 19.3 K. They found reaction products $\text{C}_2\text{H}_5\text{OH}$, $\text{H}_2\text{CO}$, $\text{CH}_3\text{OH}$, and $\text{CH}_4$, which they posited to be formed either through repetitive hydrogenation (ethanol), or fragmentation into a stable molecule and a radical, which may be further hydrogenated to a stable species. In our model, it is assumed that H atoms interact with $\text{CH}_3\text{CHO}$ by abstracting another hydrogen atom from the aldehyde end of the molecule. If the alternative mechanisms measured in the laboratory should compete strongly with this process, then the mechanism described in Section 4.1, in which H abstraction and re-hydrogenation work together to enhance reactive desorption, could become less effective, and the acetaldehyde produced on the surface could be converted to entirely different species.

The Bisschop et al. (2007) data suggest production yields for ethanol of ~20%, with other products also on the order of 10%. However, these yields are provided as a fraction of the acetaldehyde initially available in the surface layer of the ice; they do not indicate yields per hydrogen atom or per H–$\text{CH}_3\text{CHO}$ interaction. Furthermore, the experiments would not appear to be sensitive to processes in which acetaldehyde were converted to $\text{CH}_4\text{CO}$, then re-hydrogenated to $\text{CH}_3\text{CHO}$. As a result, it is not possible to determine how strongly H abstraction may dominate over hydrogenation or fragmenta-

tion, or vice versa. However, each of these processes would involve an activation-energy barrier, and it is found that abstraction from aldehyde groups occurs more readily than H addition. Hippler & Viskolcz (2002) calculated barriers to such processes, including the H + $\text{CH}_3\text{CHO}$ → $\text{H}_2\text{O}$ addition reaction, finding an activation energy of 22.4 kJ mol$^{-1}$ (2690 K), versus the literature value for abstraction of 17.6 kJ mol$^{-1}$ (2120 K Warnatz 1984). Assuming the simple rectangular-barrier tunneling treatment used in our models and assuming a 1 Å barrier width, the abstraction process should go around 350 times faster than hydrogenation. The preferred gas-phase value in the more recent review by Curran (2006) suggests an even higher barrier to hydrogenation of 26.8 kJ mol$^{-1}$ (3220 K), which would provide an abstraction/hydrogenation ratio closer to $10^5$. Fragmentation is more sparsely studied in the literature, but based on the Bisschop et al. study we presume those mechanisms to occur at similar rates to the hydrogenation mechanism. Because chemical desorption in our model is calculated to proceed in a little less than 1% of cases, we would not expect our results for acetaldehyde to be strongly affected by the inclusion of alternative reaction branches, either on the grains or in the gas phase.

4.6. $\text{O}_2$ Production

Aside from its effect on COM abundances in the ice mantles, the PD-induced reaction mechanism also produces a significant increase in $\text{O}_2$ ice abundance; this effect is noteworthy, as it may provide a clue to the origin of $\text{O}_2$ in comets. Gas-phase $\text{O}_2$ was recently observed toward comet 67P/C-G, as part of the Rosetta mission (Bieler et al. 2015). It was found that $\text{O}_2$ achieves a fractional abundance as high as ~4% with respect to water, indicating this compound as one of the most dominant species in cometary material. While the origin of molecular oxygen is still controversial because of its difficulty in observation, the strong correlation with H$_2$O implies a connection to dust-grain ice chemistry rather than gas-phase chemistry in the coma.

Many studies directly or indirectly suggest a primordial nature for $\text{O}_2$ in comets. For example, Rubin et al. (2015) confirmed the presence of $\text{O}_2$ in the Oort cloud comet 1P/
Halley at a level similar to that seen in the Jupiter-family comet 67P/C-G. This suggests that O\textsubscript{2} may be common, regardless of dynamical history, indicating a primordial origin. Mousis et al. (2016) proposed that the radiolysis of water-containing interstellar ices in low-density environments such as molecular clouds could produce O\textsubscript{2} in high abundance. Meanwhile, Taquet et al. (2016) conducted a range of astrochemical models based on diffusive grain-surface chemistry, to investigate three possible origins for O\textsubscript{2} in comets: (i) dark cloud chemistry, (ii) formation in protostellar disks, and (iii) luminosity outbursts in disks. They concluded that dark clouds are the most plausible regime in which to form the O\textsubscript{2} through diffusive O atom addition on grain/ice surfaces at temperatures around 20 K. However, as they noted, the temperature required in their models is rather higher than typical dark cloud values. Garrod (2009) suggested that the upper layers of cold-storage comets could be processed to increase their O\textsubscript{2} content, as the result of photolysis and radiolysis by the galactic UV and cosmic-ray fields. The chemical models presented by Garrod included the same PD-induced mechanism used in the present study.

Here, we propose nondiffusive, photodissociation-induced processing of interstellar ice mantles as the possible origin of the abundant O\textsubscript{2} in comets; this avoids the requirement for higher-temperature diffusive chemistry on dust-grain surfaces.

Figure 15 shows the radial distribution of the O\textsubscript{2} ice (solid lines) in our model of L1544 with the PD-induced process activated. The fractional abundance of O\textsubscript{2} ice in this model is as high as 0.6% with respect to water ice toward the core center, which is one to two orders of magnitude higher than in the other models. The abundance of O\textsubscript{2} ice has been suggested to be low in prestellar core material, because O\textsubscript{2} is efficiently hydrogenated to form H\textsubscript{2}O and H\textsubscript{2}O\textsubscript{2} ices at low temperature (Ioppolo et al. 2008). However, the PD-induced process induces the association of O atoms in the icy mantle (sourced from water molecules), resulting in the production of large amounts of O\textsubscript{2}. The other models (without PD-induced reactions) accumulate the O\textsubscript{2} ice on the grain surface over time rather than directly synthesizing it within the ice mantles. If interstellar O\textsubscript{2} ice formed via the PD-induced process were locked in until such ices were incorporated into comets, it could remain there to contribute to the O\textsubscript{2} population observed in 67P/C-G. It should be noted that H\textsubscript{2}O\textsubscript{2} ice in the PD-induced model is more abundant than O\textsubscript{2} ice (dashed line; Figure 15), in contrast to observations. The H\textsubscript{2}O\textsubscript{2}/O\textsubscript{2} ratio found in 67P/C-G by ROSINA was as low as 6.0 ± 0.7 × 10\textsuperscript{-3} (Bieler et al. 2015). The same discrepancy was found by Garrod (2019) and is related to the relative formation rates of other compounds in the ice as well as O\textsubscript{2}. Photodissociation of water leads first to OH; two such radicals may recombine through the PD-induced processes to form H\textsubscript{2}O\textsubscript{2} in high abundance. The present chemical network may be missing some chemical reactions related to the destruction of H\textsubscript{2}O\textsubscript{2} or may overestimate the efficiency to form H\textsubscript{2}O\textsubscript{2} via the PD-induced process. The efficiency of H-atom diffusion within the bulk ice to abstract another H atom from H\textsubscript{2}O\textsubscript{2} may also be an important factor; Figure 15 shows that the H\textsubscript{2}O\textsubscript{2} abundance strongly dominates O\textsubscript{2} in the coldest (inner) regions of the core. The sum of the O\textsubscript{2} and H\textsubscript{2}O\textsubscript{2} abundances collectively reach a value on the order of 1% in total at the core center. Inclusion of O\textsubscript{3} and O\textsubscript{2}H boosts this total further. The photodissociation that leads to O\textsubscript{2}, H\textsubscript{2}O\textsubscript{2}, and other species’ production from H\textsubscript{2}O in these models is the result of the secondary, cosmic-ray-induced UV field. Thus, the abundances of each would likely be enhanced by the adoption of a somewhat larger cosmic-ray ionization rate. A longer evolutionary timescale, or further processing of the ices during the later disk stage, could also lead to enhancement. Radiolysis, i.e., direct cosmic-ray impingement on the ice mantles, could also act in concert with the photodissociation effect.

Figure 15. Radial distribution of the solid-phase abundances of O\textsubscript{2} (solid lines) and H\textsubscript{2}O\textsubscript{2} (dashed lines) in the PD-induced model.
Further modeling to reproduce the amount of O$_2$ and H$_2$O$_2$ seen in 67P/C-G is outside the scope of this work, but may be a fruitful means to elucidate the origins of cometary O$_2$. The vast majority of this O$_2$ could indeed be interstellar, produced by photolysis.

5. Conclusions

Here we have introduced new rate formulations that allow astrochemical models to simulate a number of new, nondiffusive chemical mechanisms on interstellar dust-grain surfaces and within bulk ices. These formulations are fully compatible with existing model treatments for diffusive chemistry. Some of the nondiffusive mechanisms considered here, such as the E-R process and three-body reactions, are automatically taken into account in microscopic Monte Carlo kinetics models of the same systems, but must be explicitly added in rate-based treatments such as the one used here. Others, such as the three-body excited-formation mechanism and photodissociation-induced reactions, are entirely new.

Crucially, it is shown that nondiffusive processes can affect the bulk-ice, the ice-surface, and—indirectly—the gas-phase composition, through a cyclic H-abstraction and addition process that amplifies the efficiency of chemical desorption. E-R reaction processes appear not to have a strong effect in our implementation.

To place the new nondiffusive mechanisms into a context in which they could be directly tested, a physical model approximating the prestellar core L1544 was adopted, with a focus on reproducing the observed gas-phase abundances of the recently produced by other surface or bulk reactions) appear to be influential in producing COMs, although their influence is likely limited to reactions involving the highly abundant CO molecule on the grain surfaces, and/or the excited radical CH$_3$, whose production through the addition of H to CH$_2$ is especially exothermic. In the three-body excited-formation model, the efficiency of the 3-BEF mechanism for methyl formate production must indeed be optimized, as this mechanism is otherwise more efficient than is required to agree with observations. Although the gas-phase dimethyl ether abundance in particular remains difficult to reproduce, the models presented here tested only three plausible excited-formation mechanisms; alternative surface-formation processes for this molecule could be active.

Further application of the new mechanisms and formulations presented here in astrochemical models of the later stages of star formation, such as the hot core/corino stage, is currently underway.

The main conclusions of our study are enumerated below:

1. Nondiffusive reactions between newly formed radicals and nearby species on dust grains, which we label three-body reactions, appear to influence strongly the production of complex organics and other species on interstellar dust grains and in their ice mantles, producing abundances similar to those detected in the gas phase toward hot star-forming sources.

2. We propose a new surface/bulk mechanism in which the energy of formation of a newly formed radical allows it to overcome an activation-energy barrier against reaction with a nearby, stable species (the three-body excited-

formation process, 3-BEF). For key molecules/processes, especially reactions between excited radicals and abundant grain-surface CO, this mechanism appears to influence production strongly, beyond the effects of the regular three-body mechanism. Except for these key processes, the 3-BEF process is expected to be inefficient in most cases.

3. Grain-surface molecule production is enhanced by the three-body excited-formation mechanism sufficiently to explain observed gas-phase abundances of methyl formate and acetaldehyde in prestellar core L1544. Chemical desorption allows these grain-surface-formed molecules to enter the gas phase.

4. Dimethyl ether is still underproduced in the model, when compared with observations of L1544. Other plausible gas-surface production mechanisms, such as reactions between CH$_3$ and methanol, remain to be tested in the models.

5. Repetitive H abstraction by H atoms from COMs on grain surfaces, followed by recombination with another H atom and the possible desorption of the product into the gas phase, gives chemical desorption a greater influence than its basic efficiency of around 1% would otherwise suggest. This cyclic amplification effect brings the required surface-formed COMs into the gas phase effectively enough to reproduce abundances as described above. The effect should be especially important in regions where gas-phase H abundances remain relatively high.

6. Specific to the L1544 models, the position of the methanol peak is located farther outward than observation, but it is still associated with the region where CO starts to freeze out significantly. The off-center peaks in COM column densities toward L1544 are most likely related to the interplay between rising COM fractional abundances at larger radii and rising gas density at smaller radii.

7. The surface-diffusion rate of atomic H is important to radical lifetimes, which affects the efficiency of nondiffusive mechanisms that rely on reactive radicals being available on the grain surfaces. Thus, the choice of diffusion barrier for H has a strong effect on the production of COMs in chemical models that consider nondiffusive chemistry.

8. PD-induced nondiffusive chemistry within the bulk ices produces abundances of O$_2$ and related species on the order of 1% of water. This suggests that interstellar (and perhaps later) UV processing of grain-surface ices may be sufficient to reproduce observed cometary values, regardless of the precise temperature of the dust grains.

9. The broader inclusion of various nondiffusive grain-surface/ice chemical reactions in interstellar chemical models now seems imperative.

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Appendix

We list here, in Tables A1 and A2, important or newly-added gas-phase reactions and grain-surface/ice mantle reactions used in the model.
Table A1
Gas-phase Reactions Newly Included in the Chemical Network

| Reaction | Rate Coefficient | References | Type |
|----------|------------------|------------|------|
| CH₃OCH₂ + H⁺ → CH₃OCH₃ + H₂ | 3.21 × 10⁻⁹ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + H₂O⁺ → CH₃OCH₃ + H₂O | 1.48 × 10⁻⁹ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + CO⁺ → CH₃OCH₃ + CO | 1.29 × 10⁻⁹ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + Cs⁺ → CH₃OCH₃ + C + He | 1.76 × 10⁻⁹ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + He⁺ → CH₃ = CH₂ + CO + He | 7.06 × 10⁻¹⁰ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + He⁺ → CH₃OCH₃ + He | 7.06 × 10⁻¹⁰ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + H⁺ → CH₃ = CH₂ + H₂O + He | 7.06 × 10⁻¹⁰ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + Ne⁺ → CH₃ = CH₂ + H₂O + He | 7.06 × 10⁻¹⁰ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + Ne⁺ → CH₃OCH₃ + Ne | 7.06 × 10⁻¹⁰ (T/300 K)⁻⁰·⁵ cm³ s⁻¹ | a | ion-neutral |
| CH₃OCH₂ + CH₂OH → CH₃OCH₃ + H₂CO | 1.00 × 10⁻¹¹ cm³ s⁻¹ | b | neutral-neutral |
| CH₃OCH₂ + CH₂O → CH₃OCH₃ + H₂CO | 1.00 × 10⁻¹¹ cm³ s⁻¹ | b | neutral-neutral |
| CH₃OCH₂ + H₂O → CH₃OCH₃ + CO | 1.00 × 10⁻¹¹ cm³ s⁻¹ | b | neutral-neutral |
| CH₃OCH₂ + CH₂CO → CH₃OCH₃ + CO₂ | 1.00 × 10⁻¹¹ cm³ s⁻¹ | b | neutral-neutral |
| CH₃OCH₂ CRUV → CH₃ + H₂CO | 5.00 × 10⁵ × ζ₂ s⁻¹ | c,d | cosmic-ray-induced photodissociation |
| CH₃OCH₂ CRUV → CH₃ + CH₄ | 5.00 × 10⁵ × ζ₂ s⁻¹ | c,d | cosmic-ray-induced photodissociation |
| CH₃OCH₂ UV → CH₃ + H₂CO | 5.00 × 10⁻¹⁰ exp(-1.7 A₀) s⁻¹ | d,e | external UV photodissociation |
| CH₃OCH₂ UV → CH₃ + CH₂O | 5.00 × 10⁻¹⁰ exp(-1.7 A₀) s⁻¹ | d,e | external UV photodissociation |

Notes.
* Ion-molecule rates calculated using the method of Herbst & Leung (1986).
* Neutral-neutral reactions are assumed as per Garrod (2013).
* The cosmic-ray-ionization rate, ζ, is set to 1.3 × 10⁻¹⁷ s⁻¹; generic prefactors are assumed based on like processes.
* Same processes are assumed for grain-surface/ice species with a factor of 3 smaller rate.
* Neutral-neutral reactions are assumed based on like processes.

Table A2
Important and/or Newly Included Grain-surface and Ice-mantle Reactions

| Reaction | EA (K) | Width (Å) | Notes |
|----------|--------|----------|-------|
| CH₃ + CO → CH₂CO | 2870 | 1.0 | a,b |
| CH₃ + H₂CO → CH₃CH₂O | 2870 | 1.0 | a,b,c |
| CH₃O + CO → CH₂OOCO | 3967 | 1.0 | a,d |
| CH₃ + H₂ → CH₃H₂ | 0 | 1.0 | a,e |
| H + CH₂OCH₂ → CH₃OCH₂ | 4450 | 1.0 | e |
| H + CH₂OCH₃ → CH₂OCH₃ + H₂ | 3050 | 1.0 | f |
| H + CH₂O → CH₂O | 1320 | 1.0 | f |
| H + CH₂O → CH₂CHO | 0 | 1.0 | f |
| O + CH₃ → CH₄ + OH | 4380 | 1.0 | g |

Notes. The full set of the bulk-ice reactions is available in machine-readable format. This version only shows important and/or newly included reactions.
* Also treated using the 3-BEF scheme; see Section 2.5.
* Estimate using Evans–Polanyi relation.
* Estimate based on CH₃ + CO reaction.
* Huynh & Violi (2008).
* Takahashi et al. (2007).
* Senosiain et al. (2006).
* Westenberg & DeHaas (1967).

(This table is available in its entirety in machine-readable form.)
