Model Predictive Virtual Synchronous Control of Permanent Magnet Synchronous Generator-Based Wind Power System

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Abstract: As much wind power is integrated into the power grid through power electronic equipment, the use of wind power is increased rapidly. Wind power system makes the power grid lack inertia and damping, thereby reducing power grid stability; in severe cases, it may even be disconnected. Virtual synchronous generator (VSG) has been put forward to enhance the anti-disturbance performance of power grid. However, conventional VSG adopts an outer power loop and inner-current loop control. The inner-current loop control needs a pulse width modulation (PWM) module and proportion integration (PI) parameter settings. In order to reduce the parameter settings and simplify control structures, in this study, model predictive control (MPC) is used instead of inner-current loop control. At the same time—for the overall stability and control flexibility of the back-to-back system—we further propose to use outer-voltage loop control (OVLC) and MPC to stabilize direct current (DC) voltage on the machine-side and to employ model predictive virtual synchronous controls to provide inertia and damping for the power grid. The proposed control method was simulated in Matlab/Simulink (MathWorks, Massachusetts, MA, 2016) and verified by experimental results.

Keywords: model predictive control; virtual synchronous generator; wind power; cost function

1. Introduction

Since the 21st century, renewable energy sources (RES) has emerged globally as a new energy reform [1–3]. Distributed generation (DG) is dominated by solar energy and wind power [4–6]. Wind energy has received extensive attention in terms of economy and system stability [7,8]. However, wind energy is fed to the grid through a power electronics system, which usually cannot provide the necessary inertia and damping for the grid [9–12]. When the power grid is disturbed, it cannot recover by itself, which is extremely unfavorable for building a strong smart grid.

In order to make power electronic equipment show the mechanical characteristics of motors, the first concept virtual synchronous machine (VSM) was proposed in 2007 by Dr. Beck [13]. By simulating the mathematical model of traditional generators, inertia and damping are provided to the power grid, making the grid-connected inverter work as a controlled current source. In 2009, Q. Zhong proposed the VSG, which works as a controlled voltage source by simulating the synchronous generator voltage model [14,15]. The VSG can simulate the characteristics of the synchronous generator, such as electromagnetic characteristics, rotor inertia, frequency modulation and voltage regulation. Therefore, the VSG shows the same characteristics as the traditional synchronous generator, which can support the grid connection of wind power and achieve a large-scale grid connection of wind power.
VSG research primarily focuses on power-fluctuation reduction, parameter adaptive, power distribution and power grid imbalance management [16–19]. Concerning VSG research into power-fluctuation reduction, hybrid energy storage systems (HESS) were introduced in [16], composed of a battery and a supercapacitor. The supercapacitor stabilizes high-frequency power fluctuation by simulating the inertia of VS; a battery compensates for the long-term and slow power fluctuations by simulating the sag control of VSG. A parameter adaptive control strategy was suggested in [17]. The influence of inertia and damping on power and frequency are determined by deducing small-signal model, and an optimal damping ratio is maintained throughout the operation to suppress power and frequency oscillations. In [18], a new low voltage ride through (LVRT) control strategy based on a smooth switching algorithm was raised, the control strategy converts a voltage source into a current source and provides reactive power support through proportional resonance limited current control. An improved VSG control was proposed under the condition of an unbalanced grid voltage in [19]. The added positive sequence current regulator in traditional VSG control allows the reference current to track the positive sequence current. At the same time, it suppresses the negative sequence current component. Besides in [20], a generalized optimal wind energy conversion system with a VSG strategy was suggested, which could improve the frequency support capability. However, the VSG strategy mentioned connects to the power grid through a PWM control, which requires PWM modulation and PI control. Although the PWM control could improve the efficiency of power conversion, the control structure is complicated, and the parameter adjustment is difficult.

MPC has the advantages of good adaptability, strong robustness and multiple constraint variables and without using PI control and PWM modulation [21,22]. MPC has been extensively studied to improve power and frequency stability [23–25]. According to the Lyapunov criterion, the MPC method based on constraint dichotomy was proposed in [23] to improve the stability of the cascade system. In [24], a disturbance observer-based offset-free MPC was introduced for the controlled converter, which selects the weighted matrix of the correct value function to accelerate the error attenuation. Under this control strategy, power tracking performance was improved. The system stability problems caused by RES has also been studied using MPC. In [25], an active frequency response (AFR) method based on MPC was proposed. The MPC–AFR control strategy could effectively improve the frequency stability of the system under large disturbances.

Based on the above analysis, the traditional VSG adopts the outer power loop and inner-current loop control, the inner-current loop control needs a PWM module and PI parameter settings, for which the control structure is complex and the dynamic response is slow. The method MPC does not need PI control and PWM modulation, which simplifies the control structure and has a faster dynamic response. Thus, in this paper, MPC is used instead of the inner-current loop control. At the same time—for the overall stability and control flexibility of the back-to-back system—it is further suggested to employ OVLC and MPC to stabilize DC voltage on the side of the machine and to use model predictive virtual synchronous control to provide inertia and damping for the power grid. First, the reference voltage and DC-link voltage generate the reference current by PI control and MPC samples the stator current of Permanent Magnet Synchronous Generator (PMSG) to generate the prediction current. The cost function is defined as the error absolute value of the reference current and the predicted current. Moreover, a group of switching states with the minimum error is selected and applied to the next sampling period. Second, VSG is used to simulate the mathematical model of the traditional synchronous generator on the grid-side, which provides inertia and damping for the power grid and improving its reliability and disturbance resistance.
2. Outer-Voltage Loop Control and Model Predictive Control in Generator-Side

2.1. Wind Power System

The structure of the PMSG system applied to wind power generation is shown in Figure 1. The PMSG is connected to the power grid by a back-to-back power electronic converter. It composes a rectifier alternating current to direct current (AC–DC), DC-link capacitors and a DC–AC inverter.

The wind energy captured by a wind turbine is expressed as $P_{\text{wind}}$ and the formula as follows:

$$P_{\text{wind}} = \frac{1}{2} mv^2 = \frac{1}{2} \rho Vr^2 = \frac{1}{2} \rho Sv^3$$  \hspace{1cm} (1)

where $P_{\text{wind}}$ is the wind power, $v$ is the wind speed, $m$ is the air mass flow, $S$ is the swept area, $\rho$ is the air density, $V$ is airflow volume.

The wind turbine output power depends on the power coefficient $C_p$, thus the wind turbine output power can be expressed as:

$$P_{\text{tur}} = C_pP_{\text{wind}} = \frac{1}{2} \rho Sv^3C_p = \frac{1}{2} \rho \pi R^2 v^3 C_p(\lambda, \beta)$$  \hspace{1cm} (2)

where $\beta$ is pitch angle, $\lambda$ is the tip-speed ratio, $R$ is the turbine rotor radius.

The power coefficient $C_p$ is usually tracked by maximum power point tracking (MPPT), in [26] the maximum value of $C_p$ is 0.593, which means that the output power of wind power generation is always less than 59.3%. From the above formula, when the effect of $C_p$ on the wind generator is ignored, the wind speed and the output power are directly proportional. When the wind speed changes, the output power of the generator changes, and the power of the DC-link voltage capacitor also changes.

The DC-link voltage acts as an energy store and which can decouple the active and reactive power. When the DC-link voltage is constant, the active power can be transferred from the PMSG to the grid side, but the reactive power cannot pass through the intermediate DC-link voltage. Therefore, when the wind turbine generates active power to the grid through the PMSG, the stability of the DC-link voltage is crucial. In this section, OVLC is used to stabilize the DC-link voltage and MPC is used to control the current in the inner ring.

2.2. Establish Permanent Magnet Synchronous Generator Current Model

The stator voltage equation of PMSG can be expressed as:

$$U_d = L_d \frac{dl_d}{dt} - \omega_L L_qi_q + R_si_d$$  \hspace{1cm} (3)

$$U_q = L_q \frac{dl_q}{dt} + \omega_L L_qi_q + \omega_li_q + R_si_q$$  \hspace{1cm} (4)
where $U_d$ is the stator voltage direct axis component, $U_q$ is the stator voltage quadrature axis component, $i_d$ is the stator current direct axis component, $i_q$ is the stator current direct axis component, $L_d$ is the stator inductance direct axis component, $L_q$ is the stator inductance quadrature axis component, $R_s$ is stator resistance, $\omega_s$ is rotor speed and $\varphi_f$ is the synthetic rotor flux.

Therefore, the stator current equation of PMSG can be obtained as follows:

$$\frac{di_d}{dt} = \frac{1}{L_d}(u_d - R_s i_d + \omega_s L_q i_q)$$  \hspace{1cm} (5)

$$\frac{di_q}{dt} = \frac{1}{L_q}(u_q - R_s i_q - \omega_s L_d i_d - \omega_s \varphi_f)$$  \hspace{1cm} (6)

In order to calculate the predicted current at $t_{k+1}$ instant, ignore the interaction of stator, Euler’s formula can be used to approximate the discrete current prediction formulas of $dq$ axes as follows:

$$i_d(k + 1) = i_d(k) + \frac{T_s}{L_d}(u_d(k) - R_s i_d(k))$$  \hspace{1cm} (7)

$$i_q(k + 1) = i_q(k) + \frac{T_s}{L_q}(u_q(k) - R_s i_q(k))$$  \hspace{1cm} (8)

where $i_d(k)$, $i_q(k)$, $u_d(k)$ and $u_q(k)$ are the $dq$ components of output current and voltage at $t_k$ instant, $i_d(k + 1)$ and $i_q(k + 1)$ are the $dq$ components of the predictive current value at $t_{k+1}$ instant.

Predicted current $i_d(k + 1)$, $i_q(k + 1)$ is calculated by using Equations (7) and (8). The reference voltage $V_{ref}$ and DC-link voltage $V_{dc}$ generate the reference current signal by PI control. When the rectifier operates at unity power factor, the reactive current component $i_{dref} = 0$, and the output reference current is the active current component $i_{qref}$. The error absolute value of the reference current and the prediction current is defined as the cost function $g$ in Equation (9).

$$g = |i_{dref} - i_d(k + 1)| + |i_{qref} - i_q(k + 1)|$$  \hspace{1cm} (9)

Among the eight switch vectors generated by the three-phase, six-switch inverter, $g$ is chosen to be the minimum, and the corresponding switching state is applied to the inverter. Then a voltage outer loop control and MPC inner loop control are formed. Compared with the traditional voltage and current double closed-loop control, the proposed control strategy not only stabilizes the DC-link voltage, but also reduces the PI controller and the modulation method is simple. The control block diagram is shown in Figure 2.

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**Figure 2.** Generator-side converter control block diagram.
3. Virtual Synchronous Inverter in Grid-Side

3.1. Virtual Synchronous Generator Mathematical Model in Grid-Side

Causing the traditional inverter cannot provide damping and inertia to the power grid, the stability and anti-interference ability of the power grid are reduced. Proposed by Q. Zhong and other scholars, the VSG controls the inverter by simulating the mechanical and electromagnetic equations of the synchronous generator, which makes the inverter has the same performance as the synchronous generator, so that the inverter can provide damping and inertia for the power grid. The VSG can also modulate the active power frequency modulation and reactive power voltage. The control block diagram of the VSG is shown in Figure 3.

The VSG simulates the mechanical of the synchronous generator. The core formula is the swing Equation (10).

\[ J \dot{\theta} = T_m - T_e - D \dot{\theta} \]  

(10)

\( J \) provides inertia for the power grid and \( D \) provides damping. These two variables make up for the low rotational inertia and low overload capacity of power electronic devices when they are connected to the grid. Adding \( J \) and \( D \) is a great significance to improve the microgrid performance.

\( T_m \) is regulating the mechanical power of the VSG, while \( T_e \) is adjusting the electromagnetic power. The formula is as follows:

\[ \frac{P_{\text{ref}}}{\theta_n} = T_m \]  

(11)

\[ T_e = M_f i_f (i, \sin \theta) \]  

(12)

In the part of reactive power–voltage control, set the reference value of reactive power is \( Q_{\text{ref}} \), the grid actual reactive power \( Q \) is calculated based on the excitation current and mutual inductance (13).

\[ Q = -\theta M_f i_f (i, \cos \theta) \]  

(13)

The error between the terminal voltage \( V_m \) and the rated voltage \( V_r \) is adjusted by the voltage droop coefficient \( D_qr \) and the error value is fed back to the reference reactive power \( Q_{\text{ref}} \). Therefore, the grid voltage is regulated by voltage droop control, which is composed of the reference reactive power \( Q_{\text{ref}} \), grid reactive power \( Q \) and voltage deviation.

There is an error voltage between the virtual potential \( E \) of VSG and the terminal voltage \( V_m \), generating a reference current, so VSG is represented as a controlled current source. According to the
control block diagram in Figure 2 and the relationship between voltage and current, Equation (14) is obtained:

\[
I = \frac{E - V_m}{R + juL} \tag{14}
\]

where \(R\) is the grid resistance and \(L\) is the filter inductance.

3.2. Establish Virtual Synchronous Generator Prediction Control Model

From the structure of the three-phase, six-switch inverter and Kirchhoff’s voltage law, the voltage expression is shown as follows:

\[
L \frac{di_w}{dt} + R i_w = V_{wm} - e_w, \ w = a, b, c \tag{15}
\]

where \(L\) is filtering inductance, \(R\) is equivalent resistance, \(i_w, V_{wm}\) and \(e_w\) are, respectively \(w\) phase current, phase voltage and grid voltage.

The state equation of the \(\alpha\beta\) two-phase stationary coordinates is obtained, after a coordinate transformation of (15) as

\[
L \frac{d i_j}{dt} = V_j - e_j - R i_j, \ j = \alpha, \beta \tag{16}
\]

Simplify (16), the predictive current at \(t_{k+1}\) instant is given as follows:

\[
i_j(k+1) = \frac{T_s}{L} [V_j(k) - e_j(k)] + \left(1 - \frac{RT_s}{L}\right) i_j(k), \ (j = \alpha, \beta) \tag{17}
\]

where \(T_s\) represents the sampling period, \(i_j(k), V_j(k)\) and \(e_j(k)\) are the output current value, voltage vector and grid voltage of the sampling inverter side, respectively.

Eight voltage vectors are obtained from different switching states of the inverter, every voltage vector outputs a current value. In order to have the least error between the output current at \(t_k\) instant and \(t_{k+1}\) instant, it is necessary to predict the current value in different switching states from Equation (17) and select the optimal switching vector by the cost function.

The relationship between VSG and MPC is shown in Figure 4. Three-phase current \(i_a, i_b, i_c\) are sampled by VSG and MPC and VSG output reference current \(i_{ref}\) for MPC, the MPC selects the optimal voltage vector control inverter to track the reference current and forms the current closed-loop control.

![Figure 4. Connection between virtual synchronous generator and model predictive control.](image)

Model predictive virtual synchronous control is shown in Figure 5. First, the three-phase current \(i_a, i_b, i_c\) and the grid voltages \(e_a, e_b, e_c\) are sampled. The current values \(i_a, i_b\) and voltage values \(e_a, e_b\) are obtained in the \(\alpha\beta\) stationary coordinate system with Clark transform. The output voltages of inverter \(u_a, u_b\) are obtained by \(V_{dc}\). Predictive current values \(i_k(k+1)\) and \(i_{\beta}(k+1)\) at \(t_{k+1}\) instant are calculated by the predictive current Equation (17). Second, three-phase current \(i_a, i_b, i_c\) voltage \(u_a, u_b, u_c\) and reference power \(P_{ref}, Q_{ref}\) are sampled. Reference current values \(i_a^*\) and \(i_{\beta}^*\) are output by virtual
synchronization control. Last, the cost function is defined as the error absolute value of the reference current and the predicted current Equation (18).

\[ g = |i_{a}^* - i_a(k + 1)| + |i_{b}^* - i_b(k + 1)| \] (18)

Figure 5. Model predictive virtual synchronous control diagram.

4. Simulation Verification

In order to verify the effectiveness of the DC-link voltage stabilization control and model predictive virtual synchronous control, MATLAB/Simulink simulation model is built with system parameters showing in Table 1.

| System Parameters       | Symbol | Value |
|-------------------------|--------|-------|
| Reference DC voltage    | \( V_{ref} \) | 400 V |
| Filter inductance       | \( L \) | 10 mH |
| Line resistance         | \( R \) | 0.01 \( \Omega \) |
| Power line voltage      | \( U \) | 190 V |
| Power line frequency    | \( f \) | 50 Hz |
| Sampling frequency      | \( f_s \) | 10 kHz |
| Voltage sag coefficient | \( D_f \) | 5 |
| Inertia                 | \( J \) | 0.0122 |
| Damping coefficient     | \( D_p \) | 50 |

4.1. Simulation Waveform of Wind Speed Variations

Figure 6a shows the wind speed, electromagnetic torque of the generator, angular velocity of the wind turbine and DC-link voltage, respectively. Figure 6b shows output three-phase current and current local amplification in the generator-side. The simulation results are carried out under the condition of wind speed variation. When \( 1 \ s < t < 2 \ s \), the wind speed is 8 m/s, the electromagnetic torque \( T_e = 0 \ N \times m \), the wind turbine angular velocity \( W_m = 42 \ rad/s \) and the DC-link voltage \( U_{dc} = 400 \ V \). The generator outputs three-phase current is 1 A. When \( 2 \ s < t < 4 \ s \), the wind speed is 16 m/s, \( T_e = -13 \ N \times m \), \( W_m = 54 \ rad/s \), DC-link voltage is 400 V, and the three-phase current increases to 7 A. When \( 4 \ s < t < 6 \ s \), the wind speed is 24 m/s, \( T_e = -26 \ N \times m \), \( W_m = 66 \ rad/s \), the DC-link voltage remains unchanged at 400 V, and the three-phase current increases to 14 A.
When the wind speed is constant, the grid-side frequency is changing. Figure 7a shows the simulation waveform of active and reactive power on the grid-side. Figure 7b shows the output of the three-phase current and local amplification current of the inverter. The active power and three-phase current increases with changes in wind speed. When a 1–2 s wind speed is 42 m/s, the active power $P$ is 0 W and the three-phase current is 1 A. When a 2–4 s the wind speed is increased to 54 m/s, $P$ is increased to 800 W, and the current is increased to 4 A. When a 4–6 s the wind speed increases to 66 m/s, $P$ increases to 2200 W and the current also rise to 11 A. The reactive power remains constant at 0 var. In order to verify the influence of grid-side frequency changes on DC-link voltage and active power, $f$ was set to decrease to 0.05 Hz at $t = 3$ s and return to normal at $t = 4$ s. The grid-side frequency fluctuation has no effect on the torque, turbine speed and DC-link voltage in the generator-side. The reactive power is kept at 0 var and active power rises from 1000 W to 1500 W in 3 s and falls from 1500 W to 1000 W in 4 s. The grid-side current rises from 5 A to 7 A in 3 s and drops from 7 A to 5 A in 4 s. Simulation results show that model predictive virtual synchronous control adjusts active power–frequency variations automatically, then the power grid self-recover when it suffers disturbance and keep DC-link voltage stable.

**Figure 6.** Wind-speed influence on generator-side and grid-side parameters. (a) Wind speed, torque, turbine speed and DC-link voltage; (b) Generator-side three-phase current, current local magnification.

Figure 7a shows the simulation waveform of active and reactive power on the grid-side. Figure 7b shows the output of the three-phase current and local amplification current of the inverter. The active power and three-phase current increases with changes in wind speed. When a 1–2 s wind speed is 42 m/s, the active power $P$ is 0 W and the three-phase current is 1 A. When a 2–4 s the wind speed is increased to 54 m/s, $P$ is increased to 800 W, and the current is increased to 4 A. When a 4–6 s the wind speed increases to 66 m/s, $P$ increases to 2200 W and the current also rise to 11 A. The reactive power remains constant at 0 var. In order to verify the influence of grid-side frequency changes on DC-link voltage and active power, $f$ was set to decrease to 0.05 Hz at $t = 3$ s and return to normal at $t = 4$ s. The grid-side frequency fluctuation has no effect on the torque, turbine speed and DC-link voltage in the generator-side. The reactive power is kept at 0 var and active power rises from 1000 W to 1500 W in 3 s and falls from 1500 W to 1000 W in 4 s. The grid-side current rises from 5 A to 7 A in 3 s and drops from 7 A to 5 A in 4 s. Simulation results show that model predictive virtual synchronous control adjusts active power–frequency variations automatically, then the power grid self-recover when it suffers disturbance and keep DC-link voltage stable.
Figure 7. Wind-speed influence on generator-side and grid-side parameters. (a) Active and reactive power; (b) grid-side three-phase current, current local magnification.

Figure 8. Cont.
predictive virtual synchronous control adjusts reactive power–voltage variations automatically, then the grid-side three-phase current, current local magnification simulation waveform. Figure 9c is the output three-phase current, active and reactive power simulation waveform. Figure 9d shows the output three-phase current in the grid-side and current local magnification simulation waveform. Given the initial value $v = 16 \text{ m/s}$, $T_e = -13 \text{ N} \times \text{m}$, $W_m = 78 \text{ rad/s}$, $U_{dc} = 400 \text{ V}$, $U = 190 \text{ V}$, $P = 1000 \text{ W}$, $Q = 0 \text{ var}$. In order to verify the influence of grid-side voltage changes on DC-link voltage and reactive power. Set $U$ reduces $15 \text{ V}$ at $t = 3 \text{ s}$ and return to normal at $t = 4 \text{ s}$. The grid-side voltage fluctuation has no effect on the torque, turbine speed and DC-link voltage in the generator-side. The active power is kept at $1000 \text{ W}$ and reactive power rises from $0 \text{ var}$ to $1500 \text{ var}$ in $3 \text{ s}$ and falls from $1500 \text{ var}$ to $0 \text{ var}$ in $4 \text{ s}$. The grid-side current rises from $5 \text{ A}$ to $7 \text{ A}$ in $3 \text{ s}$ and drops from $7 \text{ A}$ to $5 \text{ A}$ in $4 \text{ s}$. Simulation results show that model predictive virtual synchronous control adjusts reactive power–voltage variations automatically, then the power grid self-recovers when it suffers disturbance and keeps the DC-link voltage stable.

**Figure 8.** Frequency-variation influence on parameters when wind speed is constant. (a) Wind speed, torque, turbine speed and DC-link voltage; (b) generator-side three-phase current, current local magnification; (c) frequency, active and reactive power; (d) grid-side three-phase current, current local magnification.

**4.3. Simulation Waveform of Voltage Variation**

When the wind speed is constant, the grid-side voltage is changing. Figure 9a shows wind speed, torque, turbine speed and DC-link voltage simulation waveform. Figure 9b is the output three-phase current in the generator-side and current local magnification simulation waveform. Figure 9c is the grid-side voltage, active and reactive power simulation waveform. Figure 9d shows the output three-phase current in the grid-side and current local magnification simulation waveform. Given the initial value $v = 16 \text{ m/s}$, $W_m = 78 \text{ rad/s}$, $U_{dc} = 400 \text{ V}$, $U = 190 \text{ V}$, $P = 1000 \text{ W}$, $Q = 0 \text{ var}$. In order to verify the influence of grid-side voltage changes on DC-link voltage and reactive power. Set $U$ reduces $15 \text{ V}$ at $t = 3 \text{ s}$ and return to normal at $t = 4 \text{ s}$. The grid-side voltage fluctuation has no effect on the torque, turbine speed and DC-link voltage in the generator-side. The active power is kept at $1000 \text{ W}$ and reactive power rises from $0 \text{ var}$ to $1500 \text{ var}$ in $3 \text{ s}$ and falls from $1500 \text{ var}$ to $0 \text{ var}$ in $4 \text{ s}$. The grid-side current rises from $5 \text{ A}$ to $7 \text{ A}$ in $3 \text{ s}$ and drops from $7 \text{ A}$ to $5 \text{ A}$ in $4 \text{ s}$. Simulation results show that model predictive virtual synchronous control adjusts reactive power–voltage variations automatically, then the power grid self-recovers when it suffers disturbance and keeps the DC-link voltage stable.

**Figure 9.** Cont.
The experimental parameters are shown in Table 1.

Grid Side Experimental Verification

In order to further verify the grid side effectiveness of the proposed strategy, an experimental setup based on PE-PRO was built as shown in Figure 10. The control system was implemented by TI TMS320F28335 and IGBT 7MBP50RJ120. The test instrument was composed of YOKOGAWA DLM4000 series mixed-signal oscilloscope, FLUKE 435B power quality analyzer and APL-II DC power supply. The experimental parameters are shown in Table 1.

The experimental waveforms in Figures 11 and 12 reflect the influence of frequency changes in the power grid. In Figure 11, the active power is 500 W when the frequency is 50 Hz. When \( t = 2.5 \) s, the frequency drops from 50 Hz to 49.95 Hz. With a change of 0.05 Hz, active power rises from 500 W to 1000 W and stabilized rapidly after 1 s. The reactive power keeps at 0 var. Moreover, the three-phase current increases from 3 A to 5 A. Figure 11 shows that the frequency increases from 50 Hz to 50.05 Hz when \( t = 2.5 \) s, the active power decreases from 500 W to 0 W in response to the change in frequency. The reactive power still keeps at 0 var and the three-phase current drops from 3 A to 1 A to keep the grid voltage constant. The above parameters are set to verify the active power frequency modulation.
From Figures 11 and 12, the model predictive virtual synchronous control can provide active power support to the grid when the frequency changes.

![Figure 11. Experimental waveform of power and current when frequency decreases.](image)

**Figure 11.** Experimental waveform of power and current when frequency decreases.

![Figure 12. Experimental waveform of power and current when frequency increases.](image)

**Figure 12.** Experimental waveform of power and current when frequency increases.

Figures 13 and 14 testify the reactive power–voltage variations. Figure 13 shows the voltage drop of 5 V, the changing trend of power and current. It is clear that reactive power rises from 500 var to 1000 var and stabilized rapidly after 1 s and the active power keeps at 0 W. At the same time, the three-phase current increases from 3 A to 5 A. Figure 14 shows that the voltage increases from 120 V to 125 V when \( t = 2.5 \) s, the reactive power decreases from 500 var to 0 var in response to the change in voltage. The active power still keeps at 0 W and the three-phase current drops from 3 A to 1 A in order to keep the active power constant. Figures 13 and 14 successfully testify the effectiveness of the model predictive virtual synchronous control for reactive power voltage regulation.

![Figure 13.](image)

**Figure 13.** Experimental waveform of power and current when the voltage decreases. (a) Power mutation waveform when voltage decreases; (b) current mutation waveform when voltage decreases.
Figure 14. Experimental waveform of power and current when the voltage increases. (a) Power mutation waveform when voltage increases; (b) current mutation waveform when voltage increases.

6. Conclusions

To reduce the PMSG parameter settings and simplify the control structure, this paper proposes MPC instead of inner-current loop control. On the machine side, OVLC and MPC are used to stabilize the DC voltage. OVLC uses PI control to stabilize the outer voltage loop, while MPC controls the inner-current loop stability by predicting and correcting the current at the next moment. On the power grid, model predictive virtual synchronous control is used to provide inertia and damping for the grid. VSG simulates the synchronous generator mathematical model to provide inertia and damping for the power grid, MPC stabilizes grid current with VSG output current as the reference target. Simulation and experimental results show that the proposed control strategy not only reduces parameter setting and optimizes control structure, but also plays an important role in stabilizing DC voltage and providing power support for power grid.

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