A MULTIBAND STUDY OF THE GALAXY POPULATIONS OF THE FIRST FOUR SUNYAEV–ZE’L’DOVICH EFFECT SELECTED GALAXY CLUSTERS

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1. INTRODUCTION

Galaxy clusters can be readily discovered or selected using optical or IR emission from their member galaxies, X-ray emission from the hot intracluster medium (ICM), and now even by the impact of this ICM on the cosmic microwave background temperature toward these systems. First, from optical observations, Abell (1958) identified, cataloged, and characterized clusters of galaxies using classification criteria such as compactness, distance, and richness. Later, new optical surveys added other optical properties to the clusters. Luminosity function (LF), radial profile, blue fraction, dwarf-to-giant ratio, among others, became tools for understanding different physical processes in the galaxy cluster environment.

With the advent of space-based astronomy new properties of clusters of galaxies were discovered. Strong X-ray emission made the galaxy clusters some of the most luminous objects in the universe, and their properties such as X-ray luminosity, temperature, and mass have been compiled in several X-ray-selected cluster surveys (see Giacconi et al. 1972; Voges et al. 1999, 2000; Boehringer et al. 2004, for example).

In the infrared regime, the properties of clusters have emerged from a single burst at redshift $z \approx 3$. The faint-end power-law slope of the LF is found to be on average $\alpha \approx -1.2$ in $griz$ bands, with the characteristic luminosities in $griz$ bands consistent with passively evolving populations emerging from a single burst at redshift $z \approx 3$. The faint-end power-law slope of the LF is found to be on average $\alpha \approx -1.2$ in $griz$. HONs to $m^* + 2$ for these systems appear to be consistent with those based on X-ray-selected clusters. The blue fraction estimated to $0.36 L^*$, for the three lower redshift systems, suggests an increase with redshift, although with the current sample the uncertainties are still large. Overall, this pilot study of the first four clusters provides no evidence that the galaxy populations in these systems differ significantly from those in previously studied cluster populations selected in the X-ray or the optical.

Key words: cosmology; observations – galaxies: clusters: general – galaxies: evolution – galaxies: formation

Online-only material: color figures
(Elston et al. 2006), UKIDSS (van Breukelen et al. 2006), FLS (Muzzin et al. 2008), and the Infrared Array Camera Shallow Survey (Eisenhardt et al. 2008) have delivered cluster catalogs, at high redshift, allowing initial systematic characterization of the galaxy populations of those systems.

In the millimeter regime, the use of the Sunyaev–Zel’dovich Effect (SZE; Sunyaev & Zel’dovich 1972) as a selection method for cluster of galaxies has recently produced the first results (Staniszewski et al. 2009; Vanderlinde et al. 2010; Williamson et al. 2011). The use of the SZE for cluster detection has several advantages. A catalog of SZE-selected clusters is approximately mass limited, nearly redshift independent and the observable signature is closely related to the cluster mass (Birkinshaw 1999; Carlstrom et al. 2002), making it less prone to be biased in the selection. In particular, an SZE-selected cluster sample provides an opportunity to systematically study the galaxy populations and their redshift evolution in clusters of the same mass range over a wide range of redshift.

In this paper, we use tools developed for optical studies to analyze the galaxy populations of the first four SZE-selected clusters published by the South Pole Telescope (SPT) collaboration (Staniszewski et al. 2009). As well as being among the first SZE-selected systems, these clusters are among the most well studied. This sample has been imaged deeply in the optical Blanco Cosmology Survey (BCS), studied in the X-ray (Andersson et al. 2010), targeted spectroscopically for redshifts (High et al. 2010), and the BCS data have been used to estimate weak lensing masses (McInnes et al. 2009). Also these four systems span a broad range in redshift and mass, much like the larger samples that have been published so far (Vanderlinde et al. 2010; Williamson et al. 2011). In this pilot study, we study the LF, the radial profile, the halo occupation number (HON) and the blue fraction, in an effort to answer a basic question: are the galaxy populations from these first SZE-selected clusters any different than the populations in clusters selected by other means?

The paper is organized as follows: Section 2 describes the observations and data reduction. In section Section 3, properties of the clusters, such as redshift and mass, are described. In Section 4 we study the galaxy populations in the clusters, presenting the main results. Conclusions of this study are presented in Section 5. Magnitudes are quoted in the AB system.

We assume a flat, $\Lambda$CDM cosmology with $H_0 = 100\ km\ s^{-1}\ Mpc^{-1}$, $h = 0.702$, and matter density $\Omega_m = 0.272$, according to WMAP7 + BAO + $H_0$ data (Komatsu et al. 2011).

2. OBSERVATIONS AND DATA REDUCTION

2.1. Blanco Cosmology Survey

The BCS$^{22}$ project was awarded 60 nights from the NOAO (National Optical Astronomy Observatory) survey program starting in semester 2005B. Data were gathered in 2005–2008 using the Blanco 4 m telescope located at Cerro Tololo Inter-American Observatory$^{23}$ in Chile. The telescope is equipped with a wide-field camera called the Mosaic2 imager, which consists of an array of eight $2k \times 4k$ CCDs. The pixel scale of the Mosaic2 imager is 0.27 arcsec pixel$^{-1}$, leading to a field of view of about 0.36 deg$^2$. The observations were carried out to obtain a deep, four band photometric survey ($g, r, i$, and $z$) of two 50 deg$^2$ patches of the southern sky centered at $23^h00^m, -55^\circ12^\prime$ and $05^h30^m, -55^\circ47^\prime$. These regions were chosen to enable observations by three millimeter-wavelength survey experiments (the SPT, the Atacama Pathfinder Experiment, and the Atacama Cosmology Telescope experiments). On photometric nights, we also observed several standard star fields that contain stars with known magnitudes. This approach allows the calibration of our data to the standard magnitude system. In addition, we obtained deep imaging of several fields overlapping published spectroscopic surveys to enable calibration of photo-$z$’s using samples of many thousands of spectroscopic redshifts. The data volume we collected for the BCS observation was about 20–30 gigabytes per night.

The first three seasons (2005–2007) of the BCS imaging data were processed in 2008 and 2009 using version 3 of the data management system developed for the upcoming Dark Energy Survey (DES). Details of the DES data management system can be found in Ngeow et al. (2006) and Mohr et al. (2008). A brief description is presented in this paper. Data parallel processing was carried out primarily on NCAS’s TeraGrid IA-64 Linux cluster. The pipeline processing middleware developed within the DES data management system provides the infrastructure for the automated and robust execution of our parallel pipeline processing on the TeraGrid cluster.

To remove the instrumental signatures, the raw BCS images were processed using the following corrections: crosstalk correction, overscan correction, bias subtraction, flat fielding, fringe, and illumination correction. Bad columns and pixels, saturated pixels and bright star halos, and bleed trails are masked automatically. Wide-field imagers have field distortions that generally deviate significantly from a simple tangent plane, and there are typically telescope pointing errors as well. The Astromatic code $\text{SCAMP}$ (Bertin 2006) was used to refine the astrometric solution by matching the detected stars in BCS images to the USNO-B catalog. We adopted the $PV$ distortion model that maps detector coordinates to sky coordinates using a third-order polynomial expansion of distortions, across each CCD, relative to a tangent plane. The DES data management system is using an experimental version of the Astrromatic tool $\text{SExtractor}$ (Bertin & Arnouts 1996). This experimental version includes model-fitting photometry and improved modes of star–galaxy classification to detect and catalog astronomical objects in the images. We harvested a wide range of photometric and astrometric measurements (and their uncertainties) for each object during this cataloging.

For the photometric nights that include observation of the standard star fields, we determined the band-dependent (atmospheric) extinction coefficients ($k$) together with CCD and band-dependent photometric zero points ($a$) and instrumental color terms ($b$). Specifically, the equation we constructed for each star in the standard star fields is $m_{\text{inst}} - m_{\text{std}} = \sum_i w_i \times [a_i + b_i(\Delta C)] + kX$, where $w_i = 1$ if the standard star is on CCD $i$ and $w_i = 0$ otherwise. In this equation, $m_{\text{inst}}$ and $m_{\text{std}}$ are the instrumental and the true magnitudes for the standard stars, respectively, $\Delta C$ is the color offset of the standard stars from a reference color, and $X$ is the air mass. The standard star fields include the Sloan Digital Sky Survey (SDSS) Stripe 82 fields and the Southern Standard Stars Network fields.$^{24}$ The resulting photometric solutions were then used to calibrate the magnitudes for other astronomical objects observed on the same night.

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$^{22}$ http://cosmology.illinois.edu/BCS/

$^{23}$ Cerro Tololo Inter-American Observatory (CTIO) is a division of the U.S. National Optical Astronomy Observatory (NOAO), which is operated by the Association of Universities for Research in Astronomy (AURA), under contract with the National Science Foundation.

$^{24}$ http://www-star.fnal.gov/Southern_ugriz/index.html
The nightly reduced and astrometric refined images were remapped and co-added to a pre-defined grid of tiles (which is a rectangular tangent plane projection, with ∼36 arcmin on a side, hereafter the BCS tiles) in the sky using another AstrOmatic tool, SWarp (Bertin et al. 2002). During this co-addition, we carry out a point-spread function (PSF) homogenization across each tile and within each band to match the PSF to median delivered seeing in that part of the sky. The zero points for the flux scales for these input remap images are determined using different sources of photometric information, including direct photometric zero points which are derived from the photometric solution on photometric nights, relative photometric zero points determined using all pairs of images that overlap on the sky, and the color behavior of the stellar locus (High et al. 2009). We determine the zero points for all images by doing a least-squares solution using the constraints described above. During co-addition, we use a weighted mean combine option in SWARP. The co-added images are built in each band for a given co-add tile, then a χ² image (Szalay et al. 1999) is created for detection and cataloging to ensure each object will have measurements in the griz bands extracted from the same portion of the object.

2.2. Completeness

For this work we estimate the completeness of the BCS tiles from the comparison of their griz source count histograms and those extracted from the deeper Canada–France–Hawaii–Telescope Legacy Survey (CFHTLS; Brimijoule et al. 2008, private communication). Specifically, we used count histograms from the D-11 deg² patch at high galactic latitude ($l = 172.0$; $b = -58.0$) from the CFHTLS Deep Field, whose magnitude limit is beyond $r = 27$ and the seeing is better than 1.0 and 0.9 for $g$ and $riz$, respectively. Dividing both count histograms (see Figure 1), we can estimate the level of completeness in the different tiles in each band. We can use this completeness estimate for each field to account for the missing objects as we approach the full depth of the photometry. Table 1 contains the magnitude limits in each band corresponding to 50% and 90% completeness for the tiles used in our analysis.

Table 1

| ID          | R.A. (deg) | Decl. (deg) | g (500 s) | r (600 s) | i (1350 s) | z (705 s) |
|-------------|------------|-------------|-----------|-----------|------------|-----------|
| SPT-CL J0516–5430 | 79.15569   | −54.50062   | 23.18/24.24 | 22.73/23.87 | 22.20/23.47 | 21.87/23.19 |
| SPT-CL J0509–5342 | 77.33908   | −53.70351   | 23.72/24.78 | 23.29/24.51 | 23.10/24.23 | 22.45/23.78 |
| SPT-CL J0528–5300 | 82.02212   | −52.99818   | 23.70/24.62 | 23.42/23.32 | 22.93/23.94 | 22.23/23.37 |
| SPT-CL J0546–5345 | 86.65700   | −53.75861   | 23.34/24.31 | 22.87/23.90 | 22.48/23.64 | 21.97/23.08 |

Figure 1. We estimate the completeness of our BCS co-adds by comparing objects counts from them with counts from deeper CFHT data. The resulting completeness curve is fitted by an error function, which later is used to correct for the missing galaxies and to define 90% and 50% completeness limits for analysis. Here is an example for the SPT-CL J0516–5430 field.

Figure 2. Masses and redshifts of the SPT cluster sample published to date. Open circles are from Williamson et al. (2011), open triangles are from Andersson et al. (2010) and Vanderlinde et al. (2010), and filled squares from Staniszewski et al. (2009), the sample here studied. The $M_{200, crit}$ mass estimations come from X-ray observations where that is possible, or from the SPT detection significance. In the latter case, masses have been converted from their native estimation $M_{200, mean}$ to $M_{200, crit}$ assuming a concentration parameter of $c = 5$ for the halo mass (see Table 2) under assumed cosmology. It can be seen that our sample spans on the redshift and mass space for the latest SPT sample. (A color version of this figure is available in the online journal.)

3. BASIC PROPERTIES OF THESE SPT CLUSTERS

The basic properties of these SPT-selected clusters, including the characteristics of the optical counterparts, are presented in Staniszewski et al. (2009) and are further discussed in follow-on papers (Menanteau et al. 2009; McInnes et al. 2009; High et al. 2010; Andersson et al. 2010). Several spectroscopic redshifts are now available as well as Chandra X-ray observations, providing dramatically improved mass information which enables the kind of galaxy population study we undertake here. Despite being a small sample, these four clusters are among the most well-studied SZE-selected systems and their range of mass and redshift distributions is similar to the whole SPT published cluster sample (see Figure 2). In particular, these masses and redshifts are used to estimate the projected cluster virial radius in which the optical properties are measured. These properties are presented below.

25 Details can be found at http://www.ast.obs-mip.fr/article212.html.
3.1. Redshifts

The spectroscopic redshifts of the four cluster are now available (Table 2). SPT-CL J0516—5430, a known cluster identified in the Abell supplementary southern catalog (AS0520; Abell et al. 1989) and in the REFLEX survey (RXC J0516.6—5430; Böhringer et al. 2004), had a redshift of 0.2952 (Guzzo et al. 2004), and a redshift of 0.2952 (Böhringer et al. 2004), values obtained using eight galaxy spectra from the ESO Key Programme.

For the other three clusters, spectroscopic data have recently been acquired. Using LDSS-3 on Magellan Clay telescope, High et al. (2010) reported redshifts of 0.7648 for SPT-CL J0509—5342 and 0.4626 for SPT-CL J0516—5340, and 0.7648 (Guzzo et al. 1997) and in the REFLEX survey (RXC J0516.6—5430; Böhringer et al. 2004), had a redshift of 0.2952 (Guzzo et al. 1999) and 0.2952 (Böhringer et al. 2004), values obtained using eight galaxy spectra from the ESO Key Programme.

For the other three clusters, spectroscopic data have recently been acquired. Using LDSS-3 on Magellan Clay telescope, High et al. (2010) reported redshifts of 0.7648 for SPT-CL J0509—5342 and 0.4626 for SPT-CL J0516—5340. For SPT-CL J0546—5345, Brodin et al. (2010) used IMACS on Baade Magellan telescope to measure a redshift of 1.0665.

3.2. Cluster Masses

As mentioned in Section 3, the optical analyses performed in this work require an estimate of the projected cluster virial radius. For this purpose, along with spectroscopic redshifts, X-ray mass estimations are used. We adopt mass estimates defined with respect to the critical density.

As has been previously mentioned, SPT-CL J0516—5430 is a previously known cluster, and its mass has also been estimated. With the name of RXC J0516.6—5430 in the REFLEX survey, Zhang et al. (2006) used XMM-Newton to find an $M_{500}$ of $(6.4 \pm 2.1) \times 10^{14} M_{\odot}$. Also, recent X-ray observations of the four clusters have been performed, and the mass estimation of SPT-CL J0517—5430 has been refined.

Using Chandra and XMM-Newton, Andersson et al. (2010) reported X-ray measurements of 15 of the 21 SZE-selected clusters presented in Vanderlinde et al. (2010). The observations of those clusters, which include the original four first clusters, have been designed to deliver around 1500 photons within 0.5 $r_{500}$ in order to enable measurement of the ICCM and ICCM temperature, allowing a mass estimation through an $M_{500}$—$Y_x$ scaling relation (Vikhlinin et al. 2009) with approximately 15% accuracy.

From X-ray $M_{500,Y_x}$ and spectroscopic redshifts Andersson et al. (2010) estimated the physical $r_{500,Y_x}$, both defined with respect to the critical density. Here, those $r_{500,Y_x}/M_{500,Y_x}$ are transformed to $r_{200,Y_x}/M_{200,Y_x}$ using the Navarro–Frenk–White (Navarro et al. 1997, hereafter “NFW” profile) radial mass profile with concentration of five for the dark matter halo, which implies $r_{200,Y_x} = 1.51 \times r_{500,Y_x}/M_{500,Y_x} = 1.38 \times M_{500,Y_x}$ conversion. The angular projection is calculated using the spectroscopic redshifts. $M_{200,Y_x}$ as well as $r_{200,Y_x}$ are listed in Table 2.

4. CLUSTER GALAXY POPULATIONS

The galaxy populations in clusters have been studied using several techniques and selection processes. Clusters of galaxies have been selected mainly from optical images (Abell 1958; Abell et al. 1989; Koester et al. 2007, for example) and through their X-ray emission (Ebeling et al. 1996; Vikhlinin et al. 1998; Böhringer et al. 2004, among others). A selection of clusters based on their SZE signature promises a less biased selection method, as it is likely to be less affected by projections or false clusters like optical surveys (Lucey 1983; Sutherland 1988; Collins et al. 1995; Cohn et al. 2007), and its mass selection function is nearly redshift independent, making the cluster sample more homogeneous than X-ray surveys in redshift space. Also, the SPT survey will be able to find the most massive clusters of galaxies in the universe (Carlstrom et al. 2002, 2009).

Once completed, the size, redshift extent, and the degree of completeness of the SZE-selected cluster sample will be ideal for statistical analysis of astrophysical properties in high-mass clusters. Here we focus on the first four SPT-selected clusters, which are all high-mass systems extending over a broad redshift range.

4.1. Radial Distribution of Galaxies

The radial distribution of galaxies in clusters can be used to further our understanding of the cluster environment physics. For example, from N-body and gas dynamical simulations, which include radiative cooling, star formation, signal-to-noise feedback, UV heating, etc., Nagai & Kravtsov (2005) produced radial distributions consistent with observations of X-ray-selected cluster samples from Carlberg et al. (1997) and Lin et al. (2004). Saro et al. (2006), using hydrodynamical simulations, also showed an agreement between the radial distribution of the simulated galaxies and X-ray and optically selected clusters from Popesso et al. (2007a).

For the following analysis we define the cluster center to be the position of the observed brightest cluster galaxy (BCG) member (coordinates are listed in Table 1), which agrees with its X-ray center (Andersson et al. 2010). In order to compare different studies, we estimate the concentration parameter from the NFW surface density profile. We obtain the NFW surface density by integrating the three-dimensional number density profile $n(x) = n_0 x^{-\gamma} (1 + x)^{-\gamma-2}$ along the line of sight (see Bartelmann 1996), where $x = c_x r/r_{200}$, $n_0$ is the normalization and $c_x$ is the concentration parameter. On stacked cluster data it is customary to fit both parameters, $n_0$ and $c_x$. In our case the NFW fit is done over single cluster data to a common magnitude limit, and this leads to considerable uncertainties.
in the parameters of the NFW profile. In order to minimize this problem, we introduce the observed number of galaxies in the equation. Integrating the NFW surface density over the projected area, we can derive \( n_0 / (n_{\text{obs}}, c_g) \) allowing us to fit the NFW density profile as a single parameter function. Also, after a statistical background correction, a background fitting is performed along with the NFW fit. Such background fit is limited within the Poisson uncertainty of the observed background.

The radial surface density profiles are constructed using both the red+blue and the red galaxy population defined from the color–magnitude diagram of the red sequence (see Section 4.4). The galaxy population is also selected by performing a cut in brightness, selecting galaxies which are fainter than the BCG and brighter than a common limit of \( 0 \) \( \text{mag} \) for \( r \)-band. The galaxy population is also selected by performing a cut in color–magnitude diagram of the red sequence (see Section 4.4).

The construction of the LF is done assuming that the observed LF in the cluster area is the superposition of the cluster LF and the background/foreground non-cluster LF. To recover the cluster LF we subtract the galaxy source count, rescaled by the area, from the observed LF. Given the wide range in redshift we present the LF in the four \( griz \) bands.

Some corrections are applied to these profiles. In the area calculation for each radial bin in Figure 3, the area covered by saturated stars was excluded in order to avoid an underestimation of the surface density. This is especially important in the case of SPT-CL J0509–5342 where several bright stars close to the BCG are blocking the detection of galaxy cluster members, covering about 50% of the area at a radius of 0.4 \( r_{200} \).

The concentration parameters found are shown in Table 2. With a concentration in the range of \( c \sim 3–6 \), the clusters agree at 1\( \sigma \) confidence. We note that the blue+red distribution tends to be less concentrated than the red population alone, which is consistent with previous analyses where a higher concentration is seen in the red population (e.g., Goto et al. 2004). The concentration we find is in agreement with concentrations drawn from X-ray-selected clusters of galaxies. For example, Carlberg et al. (1997) found a \( c_g \) of \( 3.70^{+0.39}_{-1.39} \) at 95% confidence, using 16 clusters from the CNOV survey with a median redshift of \( \sim 0.3 \) for a similar mass range (\( 2 \times 10^{15} M_\odot -6.6 \times 10^{15} M_\odot \); Carlberg et al. 1996). Lin et al. (2004), from stacked Two Micron All Sky Survey (2MASS) \( K \)-band data on 93 nearby X-ray-selected clusters, found a value of \( c_g = 2.90^{+0.21}_{-0.22} \) in a wider \( 3 \times 10^{13} M_\odot -2 \times 10^{15} M_\odot \) range. Both are consistent with our results.

We also found agreement between our concentration parameter and the concentration parameter found for optical-selected clusters. Biviano & Poggianti (2010) found, studying 19 intermediate redshift (0.4 \( \lesssim z \lesssim 0.8 \); 0.7 \( \lesssim M_{200} \lesssim 13.6 \times 10^{15} M_\odot \)) EDisCS+MORPHS clusters, a concentration parameter of \( c = 3.2^{+6.0}_{-2.0} \). Also, Johnston et al. (2007) found, using the SDSS sample, a concentration parameter of \( c_{200||14} = 4.1 \pm 0.2 \text{stat} \pm 1.2 \text{sys} \) for a cluster mass of \( M = 10^{14} h^{-1} M_\odot \). In summary, we find no evidence that SZE-selected clusters exhibit different galaxy radial distributions than in optical- and X-ray-selected clusters.

### 4.2. Luminosity Functions

The LF is an important tool for testing theories of galaxy formation and evolution. For example, ever more complex simulations can be tested against the LF, as an observational constraint, to probe our understanding of the evolution of galaxies in the cluster’s environment (Romeo et al. 2005; Saro et al. 2006). With clusters of similar masses we can study the LF as a function of redshift and with the LF parameters we can calculate the HON and test the \( N-M \) scaling relation (Lin et al. 2004, 2006).

The LF can be described by the three-parameter Schechter function (Schechter 1976),

\[
\phi(m) = 0.4 \ln(10) \Phi^* 10^{0.4(m^* - m)/(\alpha + 1)} \exp(-10^{0.4(m^* - m)}),
\]

where \( \Phi^* \) is the normalization, \( m^* \) is the characteristic magnitude, and \( \alpha \) accounts for the faint-end power-law behavior of the function.

The construction of the LF is done assuming that the observed LF in the cluster area is the superposition of the cluster LF and the background/foreground non-cluster LF. To recover the cluster LF we subtract the galaxy source count, rescaled by the area, from the observed LF. Given the wide range in redshift we present the LF in the four \( griz \) bands.

The area of the cluster is defined by our estimation of \( r_{200} \) (see Section 3.2 and Table 2), and the area of the background is the tile area \( (36' \times 36') \) minus the cluster area. The bright-end limit of the LF is defined by the cluster’s BCG while the faint-end limit is defined by its completeness at 90% or 50%, depending on the redshift, in each band. Below the 100% completeness, the 0.5 mag bins are corrected using the error function fitted to the BCS/CFHT comparison galaxy count histograms described in Section 2.2 and shown in Figure 1. Finally, the number of galaxies, background corrected, is divided by cluster volume (in Mpc\(^3\)) and the uncertainty is assumed Poissonian in the total number of galaxies (cluster plus background).

Below we extract \( m^* \) and \( \alpha \) from our cluster sample and compare them to previous results drawn from X-ray- and optical-selected clusters of galaxies.

#### 4.2.1. Evolution of \( m^* \)

Studies of \( m^* \) evolution in clusters have been done in different wavelengths and with different selection methods. These studies indicate that the stellar populations in many of the cluster galaxies have evolved passively after forming at high redshift (see, e.g., Gladders et al. 1998; De Lucia et al. 2004; Holden et al. 2004; Muzzin et al. 2008, and references therein). There are several indications that \( m^* \) evolution can be described from a single stellar populations (SSP) synthesis model as optical- and...
in our study show red sequences (see Figure 11), and their color
X-ray-selected clusters. All four of these SPT-selected clusters
in our study show red sequences (see Figure 11), and their color
evolution is consistent with colors derived from an SSP synthesis
model.

In order to perform a direct comparison of the brightness
and evolution of the characteristic magnitude, we let all the LF
variables vary, where possible, and compare $m^*$ in griz bands
derived from the LF fitting to that based on the SSP model. The
SSP model we use for the red galaxy population is constructed
using a Bruzual & Charlot synthesis model (BC03; Bruzual
& Charlot 2003) for the red galaxy populations, assuming a
single burst of star formation at $\alpha = 3$ from Bruzual & Charlot (2003). It is clear that these SPT-selected clusters have galaxy populations consistent with this simple evolution model.

4.2.2. Faint-end Slope

To learn about the $\alpha$ behavior, we take advantage of the
agreement shown in Section 4.2.1 between SSP model and the
data. We adopt $m^*$ from the model (see Table 3) and fit for $\Phi^*$ and
$\alpha$ for each cluster individually. The study of the faint-end slope $\alpha$
provides us with information about the faint galaxy populations
in the cluster with respect to the more evolved bright end, which
is dominated by luminous early-type galaxies. This relation
gives us insight into competing processes in the hierarchical
structure formation scenario, including the accretion of faint
galaxies by the cluster, causing a steep $\alpha$, and the evolution of
galaxies inside the cluster through galaxy merging, dynamical
friction, star formation quenching, and other processes.

Using the amoeba simplex minimization routine (Press et al.
1992), $\Phi^*$ and $\alpha$ are chi-square fitted, and their uncertainties
are determined by gridding in parameter space (see the LF
in Figures 5, 6, 7, 8, and their contour confidence regions in
Figure 9).

From the literature, we find that our average $\alpha \approx -1.2$ is
in agreement at the $1\sigma$ level with previous studies which
used samples constructed with different selection methods. For
example, from an optical work, De Propris et al. (2003) used
60 clusters at $z < 0.11$ from 2dF Galaxy Redshift Survey
(2dFGRS) in the $b_i$ band finding $\alpha = -1.28 \pm 0.03$. Paolillo
et al. (2001) found, on a composite LF of 39 Abell clusters, an
$\alpha$ of $-1.07^{+0.09}_{-0.07} -1.11^{+0.06}_{-0.05}$, and $-1.09^{+0.12}_{-0.11}$ for Gunn $g$, $r$, and
$i$, respectively.

From X-ray-selected samples Lin et al. (2004) created a
composite K-band LF of 93 clusters, finding that the faint-end
slope is well fitted by $-1.1 \leq \alpha \leq -0.84$ in agreement with our
findings within the errors. Popesso et al. (2005), using 97
X-ray-selected clusters with SDSS photometry, for a redshift $z < 0.25$, found that a better representation of the data is given by two Schechter functions, characterized by a bright-end and a faint-end slope. Comparing to the bright end of the double Schechter function with local background subtraction (which is the most similar case), the bright-end slope, in Mpc $h^{-1}$, has a slope $\alpha$ of $-1.23 \pm 0.11$, $-1.05 \pm 0.13$, $-1.17 \pm 0.13$, and $-1.06 \pm 0.12$ in $g$, $r$, $i$, and $z$, respectively, also agreeing with our findings at the $1\sigma$ level.

From IR-selected clusters Muzzin et al. (2008) detected 99 clusters and groups of galaxies and constructed the LF in $3.6 \mu m, 4.5 \mu m, 5.8 \mu m$, and $8.0 \mu m$. Although the $3.6 \mu m$ band is redward of our griz photometry, the LF constructed seems to be consistent with $\alpha \approx -1$.

The agreement found between the multiband LF parameters calculated for our SZE-selected clusters and previous studies of galaxy cluster LFs indicates that the galaxy populations in

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**Table 3**

| ID          | $\Phi^*_{\mu}$ (Mpc$^{-3}$) | $\alpha_{\phi}$ | $\mu_{\phi}$ | $\Phi^*_{\mu}$ (Mpc$^{-3}$) | $\alpha_{\phi}$ | $\mu_{\phi}$ | $\chi^2$ | $\Phi^*_{\mu}$ (Mpc$^{-3}$) | $\alpha_{\phi}$ | $\mu_{\phi}$ | $\chi^2$ |
|-------------|-----------------------------|-----------------|--------------|-----------------------------|-----------------|--------------|---------|-----------------------------|-----------------|--------------|---------|
| SPT-CL J0516–5430 | $3.95^{+0.98}_{-0.94}$ | $-1.29^{+0.16}_{-0.18}$ | 20.73 | $327^{+157}_{-112}$ | 0.44 | $3.78^{+0.81}_{-0.76}$ | $-1.27^{+0.10}_{-0.13}$ | 19.28 | $308^{+105}_{-83}$ | 0.81 |
| SPT-CL J0509–5342 | $7.07^{+1.11}_{-1.11}$ | $-1.1^{+0.0}$ | 22.27 | $191^{+30}_{-30}$ | 0.35 | $4.36^{+1.71}_{-1.59}$ | $-1.1^{+0.26}_{-0.28}$ | 20.74 | $199^{+57}_{-57}$ | 0.58 |
| SPT-CL J0528–5300 | ... | ... | 24.34 | ... | ... | $6.89^{+0.66}_{-0.64}$ | $-1.82^{+0.06}_{-0.09}$ | 22.52 | $149^{+61}_{-122}$ | 0.16 |
| SPT-CL J0546–5345 | ... | ... | 25.92 | ... | ... | ... | ... | ... | ... | ... |

**Note.** $\alpha$ set to fixed value. $\mu^*$ from model of passive evolution.
these SZE-selected clusters are not very different from those in clusters selected by other means.

### 4.3 Halo Occupation Number

Based on the Press & Schechter formalism (Press & Schechter 1974), the halo occupation distribution (HOD) is a powerful analytical tool for understanding the physical processes driving galaxy formation (Seljak 2000; Berlind et al. 2003). Also, the HOD can be used to constrain cosmological parameters (Zheng & Weinberg 2007).

One of the key ingredients in the HOD formalism is \( \langle N(M) \rangle \), the mean number of galaxies per halo or the HON. In the hierarchical scenario, the HON is expected to increase slower than the mass. While a fraction of the accreted galaxies merged, the galaxy production becomes less efficient as larger haloes are also hotter and less efficient in gas cooling (Cole et al. 2000). Observationally, several studies with cluster samples selected optically and through their X-ray emission have been performed, reinforcing that picture. For example, from samples of optically selected clusters and groups, Marinoni & Hudson (2002) found \( N \propto M^{0.83 \pm 0.15} \) for systems with \( M \gtrsim 10^{13} h^{-1} M_\odot \).

Muzzin et al. (2007c) found \( N \propto M_{200}^{0.71 \pm 0.11} \) in the ~\( 2 \times 10^{14} M_\odot \) mass range. In the X-ray selection method counterpart, Lin et al. (2004) found, from a sample of ~93 nearby clusters and groups, \( N \propto M^{0.87 \pm 0.04} \). Combining X-ray and optically selected clusters, Popesso et al. (2007a) found \( N \propto M_{200}^{0.92 \pm 0.03} \). A similar picture was found by Rines et al. (2004), who used nearby X-ray luminous Abell clusters of mass ~\( 3 \times 10^{14} h^{-1} M_\odot \) and found \( N \propto M_{200}^{0.74 \pm 0.15} \).

Here we test whether the HON of SZE-selected clusters exhibits an \( N \propto M^\beta \), with \( \beta < 1 \), behavior shown by other selection methods.

Due to the small sample presented here, our approach is to construct the HON and compare our results to the \( N-M \) scaling relation and evolution constraints obtained by Lin et al. (2004, 2006). That scaling relation is appropriate in this analysis as it covers the mass and redshift range of this SZE sample. The scaling relation was constructed using X-ray-selected clusters in the \( 3 \times 10^{13} M_\odot \) mass range using nearby clusters with 2MASS \( K \)-band photometry, and Lin et al. (2006), counting galaxies to the depth \( m^* + 2 \), expanded the study to the 0–0.9 redshift range showing that the relation does not strongly evolve.

The Lin et al. (2004) \( N-M \) relation is

\[
N_{200} = (36 \pm 3)(M_{200}/(10^{14} h^{-1} M_\odot))^{0.87 \pm 0.04}.
\]

To calculate \( N_{200} \) we integrate the cluster LF to \( L(m^*+2) \) using the parameters of the Schechter LF fit, \( \phi_s, L_s, \) and \( \alpha \) computed in Section 4.2. The total number of galaxies is

\[
N = 1 + N^* + \int_{y_{200}}^{\infty} y^\alpha e^{-y} dy,
\]

where the 1 comes from the BCG, which is not a part of the LF fitting, \( V \phi \) is the cluster volume, and \( y_{200} = L_{200}/L_s \). We use the derived \( M_{200,y} \) masses and uncertainties as explained in Section 3.2 from Andersson et al. (2010) Chandra and XMM-Newton observations. The uncertainty in \( N_{200} \) is estimated by propagating the 1σ uncertainty in \( \phi_s \) and \( \alpha \) through the integration of the LF to \( m^* + 2 \).

The \( N_{200} \) with their X-ray mass for the four clusters in the four observed bands, along with the HON relation found by Lin et al. (2004), are shown in Figure 10. Agreement between these SPT clusters and the published results on the X-ray-selected sample is good. With the concentration and the LF faint end, there is no significant evidence that the galaxy properties differ from those already extracted from previous X-ray-selected cluster samples.

### 4.4 Blue Fractions

Another property of the galaxy populations used to study their evolution in clusters of galaxies is the blue fraction \( f_b \). In their seminal work Butcher & Oemler (1984, BO hereafter), using a sample of 33 optically selected clusters of galaxies, estimated \( f_b \) and showed that it increased with look-back time (termed the Butcher–Oemler effect). Later studies, such as Rakos & Schomber (1995; \( 0 < z < 1 \)) and Marzio & de Carvalho (2000; 0.03 \( \lesssim z \lesssim 0.38 \)), using optically selected clusters, also have found a strong increase in \( f_b \) with redshift.

With the advent of new optical surveys with hundreds or thousands of clusters the analyses have been strengthened statistically. Using a sample of \( \approx 1000 \) clusters, in a wide redshift range \( 0 \lesssim z \lesssim 0.9 \), drawn from the Red-sequence Cluster Survey, Loh et al. (2008) found a mild correlation between the red fraction and redshift. Hansen et al. (2009), using thousands of clusters and groups from SDSS, found an evolving \( f_b \) in the two redshift bins studied (0.1–0.25 and 0.25–0.3), also noticing that \( f_b \) evolution was weaker for optical masses above \( 10^{14} h^{-1} M_\odot \).

Studies using samples of X-ray-selected clusters have been contradictory. Kodama & Bower (2001) used a sample of seven clusters, in the redshift range of 0.23–0.43, and found a blue fraction trend consistent with BO, while Fairley et al. (2002), using a sample of eight clusters in a 0.23–0.58 redshift range, found virtually no trend with redshift. More recently, Urguhart et al. (2010) used CFHT MegaCam \( g \) and \( r \) photometry on 34 X-ray-selected clusters in the redshift range 0.15–0.41 to study \( f_b \) correlation with other intrinsic cluster properties and found that \( f_b \) is correlated with mass \( (T_X) \) and redshift.

Also, there are environmental factors to be considered. Smail et al. (1998) used 10 X-ray-selected clusters at similar redshift...
(0.22−0.28) and found a low blue fraction of \( f_b = 0.04 \pm 0.02 \) with a variation of \( \Delta f_b = 0.06 \), explained by "small accretion events" which contribute blue members to the clusters without much increase of other parameters such as mass or X-ray luminosity. Such events could be a source of scatter in the galaxy populations of clusters selected by any selection method. To analyze \( f_b \) correlation with other cluster parameters, De Propris et al. (2004) used a sample of clusters from 2dFGRS at redshift \(<0.11\), finding a large variation \( (f_b \sim 0.1−0.5 \) for \( M^* + 1.5 \) at \( r_{200}^* \)) from cluster to cluster. 

The apparent contradiction between X-ray and optically selected samples, and the sensitivity to environmental effects, raises questions about how much of the observed \( f_b \) is due to a selection method, how much it is due to the intrinsic scatter, and if these two effects can conspire to produce an apparent trend where no trend exists.

What is needed is a sample of galaxy clusters which possess two main characteristics: (1) the selection of clusters is made in a way that is independent of the quantity whose evolution is being studied to avoid possible bias (Newberry et al. 1988; Andreon & Ettori 1999) and (2) the sample must contain the same class of clusters (i.e., same mass range) at different redshift to help in separating mass trends from redshift evolution (Andreon & Ettori 1999). A sample of SZE-selected clusters of galaxies fulfills these requirements. The selection of the SZE clusters is closely related to mass, and that mass selection is approximately independent of redshift, allowing a comparison of the same type of clusters at different epochs.

Historically, \( f_b \) has been measured in different ways. Initially the average color of the E/S0 galaxies, within a radius of \( R_{30} \) from the cluster center, which is the radius that contains 30% of all galaxies that belong to the cluster, and a concentration index were used to define \( f_b \) (see Butcher & Oemler 1984; Rakos & Schombert 1995; Marston & de Carvalho 2000; Fairley et al. 2002). Another approach is using the red sequence from the color–magnitude diagram of the clusters and \( r_{200} \) (Popesso et al. 2007b; Barkhouse et al. 2007) or a combination of both methods, that is using the color–magnitude diagram but \( R_{30} \) (Kodama & Bower 2001; Fairley et al. 2002).

Here we follow the approach of using the red sequence to define the red and blue populations, and \( r_{200} \) to define the radial extent. This ensures we are using the same portion of the cluster virial region, independent of redshift, and that we are exploring populations with colors defined with respect to a passively evolving SSP model.

The galaxies used for the \( f_b \) measurement are inside the \( r_{200} \) cluster radius and are fainter than the BCG and brighter than 0.36 \( L_{\text{MODEL}}^* \). They are classified as red if they are located within \( \pm 3 \) times the average dispersion of the Gaussian fit to the color–magnitude relation \( (\pm 0.22 \text{ mag}; \text{López-Cruz et al. 2004}) \) and blue if they are more than 0.22 mag bluer than the red sequence. We choose a limit of 0.36 \( L_{\text{MODEL}}^* \) to allow a meaningful comparison among three of our four clusters, as it is the deepest magnitude that we can detect with good completeness for the three of them. For the fourth cluster, SPT-CL J0546−5345, we currently do not have deep enough photometry for this analysis.

The color–magnitude diagram used for the clusters depends on the red-sequence identification: \( g − i/1 \) for SPT-CL J0516−5430, \( r − i/i \) for SPT-CL J0509−5342, and \( i − z/z \) for SPT-CL J0528−5300 and SPT-CL J0546−5345 (see Figure 11). The blue fraction is defined as the statistically background corrected number of blue galaxies \( n_b \), divided by the total number of statistically background corrected galaxies \( n_i \). The blue fraction and its Gaussian propagated uncertainty are

\[
\begin{align*}
\frac{f_b}{n_b} = \frac{n_b}{n_r + n_b}, \\
\sigma_{f_b}^2 = \sum_{i=r,b} \left( \frac{\partial f}{\partial n_i} \right)^2 \sigma_{n_i}^2.
\end{align*}
\]

Here, \( n_b \) and \( n_r \) are the blue and red statistically background subtracted number of galaxies:

\[
n_i = N_i - N_i^{\text{bg}}
\]

The uncertainties are expressed as

\[
\sigma_{n_i}^2 = \sigma_{N_i}^2 + \sigma_{N_i^{\text{bg}}}^2
\]

assuming \( \sigma_{N_i} \) Poissonian. The last term is calculated directly by measuring the rms of the Gaussian distribution observed on histograms constructed from the blue and red (or total) number of galaxies background corrected in a circle of radius \( r_{200} \) on \( n \) random positions outside the cluster radius (background \( r_{200} \)) in order to account for background variations on the observed \( 36' \times 36' \) patch of the sky.

A special mention for SPT-CL 0509−5342 is required. In the center of the cluster are three bright stars leaving only a few visible galaxies; we have corrected this effect by accounting for the area masked around these stars. Nevertheless, the statistical background subtraction leads to negative blue galaxy counts in the ~0.6 \( r_{200} \) inner part of the cluster area. The blue fraction of three of the four clusters, at redshifts 0.295, 0.463, and 0.763, is shown in Figure 12. The measurements suggest an increase with redshift, as shown for optically selected clusters, although the result could be consistent with a constant blue fraction over the range of redshift that we explored with our limited sample. Future optical follow-up of SPT–SZE-selected clusters using larger aperture telescopes on the high-redshift end will be necessary to understand the Butcher–Oemler effect in this cluster mass range within the SZE-selected sample.

5. CONCLUSIONS

We present the results of a careful examination of the multiband optical properties of the galaxy populations in the first
four SZE-selected galaxy clusters. This analysis builds upon the selection by the SPT survey, deep multiband optical data from the BCS, Chandra, and XMM-Newton mass estimates and published spectroscopic redshifts.

The radial distributions of galaxies in the four systems are consistent with NFW profiles with low concentration in the 2.2–3.6 range, although the constraints in our highest redshift clusters are weak due to the imaging depth. One system shows a clear secondary peak, which is evidence of multiple galaxy components. The observed galaxy concentrations in these SPT systems are consistent with X-ray- and optical selected cluster samples as well as simulations.

We showed that the characteristic luminosities in bands griz are consistent with passively evolving populations emerging from a single burst at redshift $z = 3$. This is observed by direct comparison of the griz $m^*$ measurements with the evolution of the red sequence expected from the SSP model.

The slope of the LF, $\alpha$, in all four bands showed an average of $-1.2$ consistent with previous studies and roughly independent of redshift, although in the high-redshift systems the constraints are weaker and the $\Phi-\alpha$ contours are much more extended (see Figure 9) due to the depth of the data.

HONs (to $m^* + 2$) for these systems appear to be consistent with the relation measured in X-ray-selected clusters. As shown previously (Lin et al. 2004), these well-behaved and simple galaxy populations are unfortunately not easy to use as a mass indicator with optical data alone, because the HON varies with the adopted virial radius of the cluster.

The blue fractions $f_b$ observed in these systems are consistent with those seen in clusters selected using other means. Although the measured $f_b$ suggest a redshift evolution (as optical studies show), it is within the errors also consistent with a constant $f_b$. It is clear that definitive conclusions should be drawn with a larger number of clusters for more robust statistics. A larger sample and deeper multiband data on the high-redshift end are needed.

The SPT selection provides a powerful means of choosing similar mass systems over a broad range of redshift, making the future larger cluster sample particularly interesting for this study.

In summary, our systematic analysis of the galaxy populations in the first SZE-selected galaxy clusters spanning the redshift range $0.3 < z < 1.1$ provides no clear evidence that the galaxy populations in these SPT-selected clusters differ from populations studied in other X-ray and optically selected samples. An extension of our analysis to the full SPT sample will enable a more precise test of the effects of selection. In addition, comparison of the observed properties of the SPT cluster galaxy populations and their evolution to numerical simulations of galaxy formation should allow for clean tests of the range of physical processes that are responsible in determining the formation and evolution of cluster galaxies.

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Figure 12. Blue fraction vs. redshift using the populations shown in Figure 11. The Butcher & Oemler (1984) relation is shown (dashed line). The blue fraction is calculated using statistical background correction within $r_{200}$ and to a depth of $0.36 L_{\text{MODEL}}$ for each system.
