On the relative distance of Magellanic Clouds using Cepheid NIR and Optical-NIR PW relations

L. Inno\textsuperscript{1,2}, G. Bono\textsuperscript{1,3}, N. Matsunaga\textsuperscript{4}, M. Romaniello\textsuperscript{2}, F. Primas\textsuperscript{2}, R. Buonanno\textsuperscript{1,5}, F. Caputo\textsuperscript{3}, K. Genovali\textsuperscript{1}, C.D. Laney\textsuperscript{6,7}, M. Marconi\textsuperscript{8}, and A. Pietrinferni\textsuperscript{5}

\textsuperscript{1} Dipartimento di Fisica, Universit\`a di Roma Tor Vergata, via della Ricerca Scientifica 1, 00133 Rome, Italy; e-mail: laura.inno@roma2.infn.it
\textsuperscript{2} European Southern Observatory, Karl-Schwarzschild-Str. 2, 85748 Garching bei Munchen, Germany
\textsuperscript{3} INAF–OAR, via Frascati 33, Monte Porzio Catone, Rome, Italy
\textsuperscript{4} Kiso Observatory, Institute of Astronomy, School of Science, The University of Tokyo, 10762-30, Mitake, Kiso-machi, Kiso-gun,3 Nagano 97-0101, Japan
\textsuperscript{5} INAF-Osservatorio Astronomico di Collurania, via M. Maggini, 64100 Teramo, Italy
\textsuperscript{6} Dept. of Physics and Astronomy, N283 ESC, Brigham Young University, Provo, UT 84601, USA
\textsuperscript{7} South African Astronomical Observatory, P.O. Box 9, Observatory 7935, South Africa
\textsuperscript{8} INAF-Osservatorio Astronomico di Capodimonte, via Moiarello 16, 80131 Napoli, Italy

Abstract. We present new estimates of the relative distance of the Magellanic Clouds (MCs) by using NIR and Optical-NIR Cepheid Period Wesenheit (PW) relations. The relative distances are independent of uncertainties affecting the zero–point of the PW relations, but do depend on the adopted pivot periods. We estimated the pivot periods for fundamental (FU) and first overtone (FO) Cepheids on the basis of their period distributions. We found that log $P=0.5$ (FU) and log $P=0.3$ (FO) are solid choices, since they trace a main peak and a shoulder in LMC and SMC period distributions. By using the above pivot periods and ten PW relations, we found MC relative distances of 0.53$^{+0.06}_{-0.07}$ (FU) and 0.53$^{+0.07}_{-0.06}$ (FO) mag. Moreover, we investigated the possibility to use mixed-mode (FU/FO, FO/SO) Cepheids as distance indicators and we found that they follow quite well the PW relations defined by single mode MC Cepheids, with deviations typically smaller than 0.3$\sigma$.

Key words. Magellanic Clouds — stars: variables: Cepheids — stars: distances — stars: oscillations

1. Introduction

The cosmic distance ladder is a fundamental step not only for astrophysics, but also for observational cosmology \cite{Mould2011, Suyu2012}. The quest for precise and accurate cosmic distances involved a paramount observational and theoretical effort to constrain the systematics affecting distances based...
either on geometrical methods or on distance indicators (Freedman & Madore 2010; Storm et al. 2011; Matsunaga et al. 2011; Bono et al. 2013) In this context a relevant breakthrough has been the very accurate and precise measurement of the distance to the Large Magellanic Cloud (LMC) recently performed by Pietrzyński et al. (2013). They used eight double eclipsing binary systems including two red giants distributed across the LMC bar and found a true distance modulus of $18.493 \pm 0.008$ (statistical) $\pm 0.047$ (systematic) mag. The precision of the distance is at the 2% level and it is the most precise distance ever obtained of an extragalactic stellar system. The new measurement will have a substantial impact not only on the new estimation of the Hubble constant, but also to validate other standard candles.

The above issues are mainly dealing with absolute distance determinations. The absolute distances based on one of the variants of the Leavitt’s law –i.e. Period-Luminosity (PL), Period-Luminosity-Color (PLC), Period-Wesenheit (PW) relations– do require a detailed analysis of the dependence of both the zero-point and the slope on chemical composition and reddening (Romaniello et al. 2008; Bono et al. 2010; Ngeow 2012; Ripepi et al. 2012; Inno et al. 2013). The same applies to the many variants of the Baade-Wesselink method and their dependence on the parameter to transform radial velocities into pulsation velocities (Nardetto et al. 2004; Storm et al. 2011; Groenewegen 2013). The literature concerning pros and cons of the different distance scales is significant (Alves 2004; Feast et al. 2008; Bono et al. 2008; Walker 2012).

Relative distances have the indisputable advantage that they are independent of the absolute zero-point. These distances are quite useful not only for the cosmic distance scale, but also to constrain possible systematic uncertainties affecting different distance indicators.

2. Photometric data and theoretical models

The OGLE-III micro–lensing survey (Soszyński et al. 2008 2010) collected the most complete catalog of MC Cepheids in the Optical bands ($V,I$). The OGLE-III Catalog of variable stars (CVS) includes $V,I$ band light curves for $\sim 3300$ Cepheids in the LMC and $\sim 4500$ Cepheids in the SMC. The Fourier decomposition of these light curves allowed (Soszynski et al. 2000) to properly identify the different pulsation modes – LMC: 1848 fundamental-mode (FU), 1228 first-overtone (FO), 61 fundamental-first-overtone double-mode (FU/FO), 203 first-second overtone double-mode (FO/FO) pulsators; SMC: 2626 FU, 1644 FO, 59 FU/FO and 215 FO/FO. The single epoch measurements for $\sim 90\%$ of the OGLE-III Cepheids were extracted from the IRSF/SIRIUS Near-Infrared (NIR: $J,H,K_S$) Magellanic Clouds Survey Catalog (Kato et al. 2007) and transformed into the 2MASS photometric system (Carpenter 2001). We adopted the $V$ and $I$ mean magnitudes, the $V$-band amplitude, the period $P$, and the pulsation phase provided by the OGLE-III CVS to transform the FU Cepheids single-epoch NIR data to the NIR mean magnitudes by applying the template light curve, as described by Soszyński et al. (2005). We also included the NIR mean magnitudes by Persson et al. (2004) for 41 long-period FU Cepheids in the LMC. We ended up with a sample of $\sim 3300$ LMC and $\sim 4400$ SMC Cepheids with $VIJHK_S$ bands photometry, including double-mode pulsators (LMC: 1840 FU, 1202 FO, 60 FU/FO, 199 FO/FO; SMC: 2587 FU, 1579 FO, 55 FU/FO,195 FO/FO). In our analysis we focused on FU and FO Cepheids, in order to evaluate the PW relations (Inno et al. 2013).

To enlarge the statistics of our sample, we now include the double-mode pulsators. For these Cepheids, we decided to adopt the period of the dominant mode. The period distributions of FU, FU/FO and FO, FO/FO Cepheids for the LMC (top) and SMC (bottom) are shown in Fig. 1. The period distributions of FU (green dashed bars) and FU/FO (red filled bars) LMC Cepheids in the left–top panel cover the same period range and show similar shape. The same applies for the FU and FO panel FO Cepheids in the left-bottom panel of Fig. 1. Moreover, the period distributions of FO (blue dashed bars) and FO/FO (orange filled bars) LMC Cepheids in the left-bottom panel of Fig. 1. The period distributions of FU (green dashed bars) and FU/FO (red filled bars) LMC Cepheids in the left–top panel cover the same period range and show similar shape. The same applies for the FU and FO panel FO Cepheids in the left-bottom panel of Fig. 1. Moreover, the period distributions of FO (blue dashed bars) and FO/FO (orange filled bars) LMC Cepheids in the left-bottom panel of Fig. 1.
Inno: On the relative distance of Magellanic Clouds

Fig. 1. Left – Period distributions for FU (green), FU/FO (red) of the LMC (top) and SMC (bottom) Cepheids. Right – The same for FO (blue), FO/SO (orange) LMC (top) and SMC (bottom) Cepheids.

bars) MC Cepheids in the right–top (LMC) and right–bottom (SMC) panel of Fig. 1 also show similar shape. The period distribution of Cepheids plays a crucial role to constrain the recent Star Formation History (SFH) of their host galaxies (Becker et al. 1977, Alcock et al. 1999, Antonello et al. 2002). Cepheids are indeed good tracers of the young stellar populations, since their evolutionary status is well established. They are intermediate-mass stars evolving along the blue loop in the helium-core and hydrogen-shell burning stage. They obey to well known Period–Age and Period–Color–Age relations, which indicate that younger Cepheids have longer periods. Thus, the period distribution traces the underlying stellar population and several factors can affect its shape: the initial mass function, the metallicity, the star formation history, the mass loss rate and the topology of the instability strip. To further constrain the evolutionary status of MC Cepheids, Fig. 1 shows the NIR \((J, J - K_S)\) color–magnitude diagram (CMD) of the SMC Cepheids. The FO Cepheids (green circles), with longer periods, are brighter and bluer compared with FU Cepheids (blue circles). The gray lines show a set of isochrones with a scaled-solar chemical mixture and a chemical composition \((Z=0.004, Y=0.256)\) typical of SMC young population (Pietrinferni et al. 2004, 2006). The isochrones are based on evolutionary models that account for mild convective core overshooting during the central hydrogen-burning phase and for a canonical mass-loss rate \((\eta = 0.4)\). The comparison between theory and observations indicates that SMC Cepheids have ages ranging from a few tens to a couple of hundred Myr. The blue loops for the older \((t \approx 250 \text{ Myr})\) and the younger \((t \approx 30 \text{ Myr})\) isochrones do not extend over the whole color range of the Cepheids observed. This well known theoretical problem is related to the physical mechanisms and the input physics adopted in the evolutionary calculations (Bono et al. 2000, Neilson et al. 2011, Prada Moroni et al. 2012). The vertical blue and red lines show the predicted edges of the instability strip (IS) for the modal stability of both FU (red edge) and FO (blue edge) Cepheids with similar metallicity (Marconi et al. 2005). We also included the double-mode pulsators. The FU/FO Cepheids (red dots) are found in the same range of color of the FU Cepheids, but at lower luminosities, as expected. The FO/SO Cepheids (orange dots) are also fainter and older than the FO ones, as expected. Fig. 2 shows a quite good agreement between theory and observations. Moreover, we have to take into account that the theory predictions are obtained for a fixed mean chemical composition and are not corrected for differential reddening or geometrical effects.

3. MC Relative Distance

In order to address the problem concerning the linearity of the PW relations, in Inno et al. (2013) we devised a new empirical test based on the relative distance between SMC and LMC. In Fig. 3 we compare the MC relative distance modulus estimated with the ten...
Inno: On the relative distance of Magellanic Clouds

Fig. 2. NIR – J, J–Ks – Color-Magnitude Diagram (CMD) of FU (green dots), FO (blue dots), SO (purple dots) and double-mode (FU/FO, red dots; FO/SO, orange dots) SMC Cepheids. The grey lines display stellar isochrones with ages ranging from 30 Myr to 250 Myr (see labeled values), based on non-canonical evolutionary models (see Section 3). They are plotted by assuming a true distance modulus of $\mu = 18.93$ mag, a mean reddening of $A_V = 0.18$ mag and the reddening law by Cardelli et al. (1989) The cool (red) and the hot (blue) edge of the Cepheid IS are also shown (Marconi et al. 2005).

different PW relations for FU (left) and FO (right) Cepheids. We computed these distances according to the following equation: $\Delta \mu = a_{SMC} \mu_{SMC} - a_{LMC} \mu_{LMC} + \log P (b_{SMC} \log P_{SMC} - b_{LMC} \log P_{LMC})$; where $a, b$ are the coefficients of the FU and FO PW for the SMC and LMC and $P$ is the fixed pivot period. The choice of the pivot period is somewhat arbitrary in literature, ranging from $\log P = 0.5$ (Groenewegen 2000) or $\log P = 0.8$ (de Vaucouleurs 1978) to $\log P = 1.0$ (Udalski et al. 1999; Freedman et al. 2001) or $\log P = 1.3$ (Matsunaga et al. 1). However, with a glance to the period distribution in the left panels of Fig. 1 it is clear that the PW relations mainly depend on the bulk of the Cepheid distribution and the number of Cepheids that constrains the PW relation at $\log P = 1.0$ is quite poor compared with the number of Cepheids at the peak of the distribution (LMC: $\log P = 0.5$; SMC: $\log P = 0.3$). The peak of the period distribution of the FU LMC Cepheids, indicated by the black arrows in the left panels of Fig. 1 is a more suitable pivot period, since the SMC period distribution also shows a substantial number of Cepheids for the same period range. The choice of a new pivot period ($\log P = 0.5$) allow us to correctly sample the PW relation. The same applies for the LMC FO peak distribution at $\log P = 0.3$, indicated by the black arrows in the right panels of Fig. 1. By using the ten PW relations for FU and FO Cepheids, given in Inno et al. (2013), we evaluated ten different MC relative distance moduli, shown in Fig. 3. The error bars are drawn taking into account both the error on the coefficients $a, b$ of the PW relations and the statistical dispersion associated to the linear fit. In the case of the FO Cepheids, the error bars are larger, because of the larger dispersion in the FO PW relations. This is due to the lack of a template for these pulsators, as discussed in Inno et al. (2013). We also computed the weighted average of these ten values, to reduce the associated error, and we found $\Delta \mu = 0.53 \pm 0.06$ mag for the FU PW relations and $\Delta \mu = 0.53 \pm 0.07$ mag for the FO PW relations. The two results are in very good agreement, confirming the robustness of the relative distance estimation. Fig. 4 shows the comparison between the distribution of the double-mode pulsators in the PW($V, I$) diagram and the optical PW relations (solid lines) presented in Inno et al. (2013) for the single-mode FU (green dots) and FU (blue dots) Cepheids in the LMC (left) and SMC (right). Interestingly enough, the FU/FO (red dots) Cepheids follow the FU PW relation, with a deviation that is on average smaller than $0.3\sigma$ for the LMC and $0.1\sigma$ for the SMC Cepheids, where $\sigma$ is the statistical dispersion associated to the fit. The FO/FO (orange dots) Cepheids follow the FO PW relation with a deviation that is similar or smaller ($\sim 0.2\sigma$, LMC; $\sim 0.3\sigma$, SMC). We also tested the difference using the NIR and Optical-NIR PW relations and we found that the deviation is even smaller ($<0.05 \sigma$). The above findings indicate that the Optical and NIR PW relations can be adopted to estimate
In the relative distance of Magellanic Clouds

**Fig. 3.** Left – Comparison between the MC relative distances for the ten different PW relations for FU Cepheids, evaluated at the pivot period $\log P = 0.50$. The error bar for each point accounts for both the dispersion and the error on the coefficients of the PW relations. The red dashed lines is the weighted average of the ten values, that is also labeled in the top. Right – Same as the left, but for FO Cepheids. The relative distances are evaluated at the pivot period $\log P = 0.30$ (see Section 3).

**Fig. 4.** Left – ($V,I$) PW relations for LMC Cepheids: FU (green dots), FU/FO (red dots), FO (blue dots) and FO/SO (orange dots) Cepheids. The solid lines show the linear fits for FU and FO Cepheids. Right – Same as the left, but for the SMC. The relative distances were found relative distances of $0.53 \pm 0.06$ (FU) and $0.53 \pm 0.07$ (FO) mag.

Current findings indicate that both FU and FO Cepheids can be safely adopted to estimate relative distances. The above results further support the hypothesis that the difference in the absolute distance of MCs based on FU and FO Cepheids (Inno et al. 2013) is mainly caused by the limited accuracy of the absolute zero–point of FO PW relations. Indeed, the zero-point relies on a single object –Polaris (van Leeuwen et al. 2007)– since we still lack accurate trigonometric parallaxes for other nearby Galactic FO Cepheids.

We also investigated the possibility to use mixed-mode (FU/FO, FO/SO) Cepheids as distance indicators using both NIR and optical-NIR PW relations. We found that they follow quite well the PW relations defined by single mode MC Cepheids. Indeed, the deviations are typically smaller than $0.3\sigma$.

**Acknowledgements.** We are indebted to the editor, P. Bonifacio, for his constant support. Two of us
Inno: On the relative distance of Magellanic Clouds

(L.I. and K.G.) thank the SAIT for partial support to attend the EWASS conference. One of us (G.B.) thanks ESO for support as a science visitor. This work was partially supported by PRIN-INAF 2011 “Tracing the formation and evolution of the Galactic halo with VST” (P.I.: M. Marconi) and by PRIN-MIUR (2010LY5N2T) “Chemical and dynamical evolution of the Milky Way and Local Group galaxies” (P.I.: F. Matteucci).

References

Alcock, C., Allsman, R. A., Alves, D. R., et al. 1999, AJ, 117, 920
Alves, D. R. 2004, New Astronomy Reviews, 48, 659
Antonello, E., Fugazza, D., & Mantegazza, L. 2002, A&A, 388, 477
Becker, S. A., Iben, I., Jr., & Tuggle, R. S. 1977, ApJ, 218, 633
Bono, G., Caputo, F., Marconi, M., & Musella, I. 2010, ApJ, 715, 277
Bono, G., Stetson, P. B., Sanna, N., et al. 2008, ApJ, 686, L87
Bono, G., Castellani, V., & Marconi, M. 2000, ApJ, 529, 293
Bono,G., Matsunaga, N., Inno, L., Lagioia, E.P., & Genovali, K. 2013, in Cosmic-Ray in star-forming environments, ed. D.F. Torres, O. Reimer (Sant Cugat Forum in Astrophysics; Berlin: Springer), in press
Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245
Carpenter, J. M. 2001, AJ, 121, 2851
de Vaucouleurs, G. 1978, ApJ, 223, 730
Feast, M. W., Laney, C. D., Kinman, T. D., van Leeuwen, F., & Whitelock, P. A. 2008, MNRAS, 386, 2115
Freedman, W. L., & Madore, B. F. 2010a, ARA&A, 48, 673
Freedman, W. L., Madore, B. F., Gibson, B. K., et al. 2001, ApJ, 553, 47
Groenewegen, M. A. T. 2013, A&A, 550, A70
Groenewegen, M. A. T. 2000, A&A, 363, 901
Inno, L., Matsunaga, N., & Bono, G., et al. 2012, ApJ, 764, 84
Kato, D., Nagashima, C., Nagayama, T., et al. 2007, PASJ, 59, 615
Marconi, M., Musella, I., & Fiorentino, G. 2005, ApJ, 632, 590
Matsunaga, N., Feast, M. W., & Menzies, J. W. 2009, MNRAS, 397, 933
Matsunaga, N., Feast, M. W., & Soszyński, I. 2011, MNRAS, 413, 223
Mould, J. 2011, PASP, 123, 1030
Nardetto, N., Fokin, A., Mourard, D., et al. 2004, A&A, 428, 131
Neilson, H. R., Cantiello, M., & Langer, N. 2011, A&A, 529, L9
Ngeow, C.-C. 2012, ApJ, 747, 50 (N12)
Persson, S. E., Madore, B. F., Krzeminski, W., et al. 2004, AJ, 128, 2239
Pietrinferni, A., Cassisi, S., Salaris, M., et al. 2004, ApJ, 612, 168
Pietrinferni, A., Cassisi, S., Salaris, M., et al. 2006, ApJ, 642, 797
Pietrzyński, G., Graczyk, D., Gieren, W., et al. 2013, Nature, 495, 76
Prada Moroni, P.G., Gennaro, M., Bono, G., et al. 2012, ApJ, 749, 108
Ripepi, V., Moretti, M. I., Marconi, M., et al. 2012, MNRAS, 424, 1807
Romanienko, M., Primas, F., Mottini, M., et al. 2008, A&A, 488, 731
Soszyński, I., Gieren, W., & Pietrzyński, G. 2005, PASP, 117, 823
Soszyński, I., Udalski, A., Szymanski, M., et al. 2000, AcA, 50, 451
Soszyński, I., Poleski, R., Udalski, A., et al. 2008, AcA, 58, 163
Storm, J., Gieren, W., Fouqué, P., et al. 2011, A&A, 534, A94
Suyu, S. H., Treu, T., Blandford, R. D., et al. 2012, arXiv:1202.4459
Udalski, A., Szymanski, M., Kubiak, M., et al. 1999, AcA, 49, 201
van Leeuwen, F., Feast, M. W., Whitelock, P. A., & Laney, C. D. 2007, MNRAS, 379, 723
Walker, A. R. 2012, Ap&SS, 341, 43