The **Pristine** survey – XVIII.
C-19: Tidal debris of a dark matter-dominated globular cluster?

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**ABSTRACT**

The recently discovered C-19 stellar stream is a collection of kinematically associated metal-poor stars in the halo of the Milky Way lacking an obvious progenitor. The stream spans an arc of \(\sim 15^\circ\) in the sky, and orbit-fitting suggests an apocentric distance of \(\sim 20\) kpc and a pericentre of \(\sim 10\) kpc. The narrow metallicity dispersion of stars with available spectra, together with light element abundance variations, suggests a globular cluster (GC) origin. The observed metallicity ([Fe/H] \(\approx -3.4\)), however, is much lower than that of any known GC. In addition, the width and velocity dispersion of the stream are similar to those expected from disrupting dwarf galaxies, and substantially larger than the tidal debris of GCs able to disrupt on C-19’s orbit. We propose here an unconventional model where the C-19 progenitor is a dark matter-dominated stellar system with GC-like abundance patterns. We use N-body simulations to show that the tidal disruption of a \(\sim 100\) pc King-model stellar component embedded in a \(\sim 20\) km/s cuspy cold dark matter halo yields debris consistent with C-19’s observed width and velocity dispersion. The stellar component of the progenitor is fully disrupted, and is spread over two distinct streams; one corresponding to C-19 and another possibly hiding behind the Galactic plane. If such companion stream were found, it would suggest that dark matter-dominated dwarfs may also develop GC-like enrichment patterns, a finding that would inform our theoretical understanding of the formation of multiple populations in GCs and dwarf galaxies alike.

**Key words:** dark matter; globular clusters: general; Galaxy: kinematics and dynamics; galaxies: evolution; galaxies: dwarf; galaxies: evolution

1 INTRODUCTION

The number of known stellar streams in the Milky Way (MW) has increased dramatically over the last few decades thanks to discoveries made by the Sloan Digital Sky Survey (e.g. Odenkirchen et al. 2001; Belokurov et al. 2006; Koposov et al. 2012), the Dark Energy Survey (e.g. Shipp et al. 2018), and the Gaia satellite (e.g. Malhan et al. 2018; Ibata et al. 2019, 2021), among others.

Stellar streams form through tidal stripping of globular clusters (GCs) or dwarf galaxies (DGs) as they orbit in the gravitational potential of the Milky Way. Since globular clusters are in general denser and physically smaller than dwarfs, they produce narrow, kinematically cold stellar streams (like, e.g., the Pal-5 stream, Odenkirchen et al. 2001). Dwarfs, on the other hand, are expected to
produce thicker and kinematically hotter streams (like, e.g., the massive Sagittarius stream, Ibata et al. 2001; Newberg et al. 2002). Stream kinematic properties are particularly useful when inferring the progenitor properties of “orphan” streams, where no bound remnant of the original system can be identified.

Kinematic signatures, however, are inconclusive on their own. One reason is the recent discovery of “ultra-faint dwarfs” (UFDs, usually defined as DGs with $L < 10^3 L_\odot$), whose structural properties (size, velocity dispersion, luminosity) overlap those of some GCs (Simon 2019). Indeed, often it isn’t clear whether a system is a GC or a UFD unless a fairly precise estimate of its dynamical mass can be made: objects dominated by dark matter are considered UFDs whereas self-gravitating ones are regarded as GCs.

This litmus test, however, cannot be applied to “orphan” streams, as they are not self-gravitating systems, so other diagnostics need to be considered. A popular one makes use of the ubiquitous presence of “multiple populations” (MPs) in massive, old GCs. These MPs show a narrow dispersion in metallicity (as measured by [Fe/H]), but wide variations in the light-element abundances of individual stars (Gratton et al. 2004, 2019). These variations are also often correlated (or anti-correlated) between elements such as C, N, O, Na, Mg, and Al, signalling a complex nucleosynthetic process which operated during GC formation and whose origin has not yet been fully elucidated (Bastian & Lardo 2018).

UFDs, on the other hand, appear to have formed their stars differently, with available data indicating a fairly broad dispersion in $\text{[Fe/H]}$ ($\sigma_{\text{[Fe/H]}}$) (Willman & Strader 2012; Leaman 2012), and no GC-like correlations between light-element abundances (Tolstoy et al. 2009; Simon 2019). It is therefore common practice to associate narrow $\sigma_{\text{[Fe/H]}}$ and wide variations in light-element abundances with GCs, although even here important exceptions apply: for example, the well-studied $\omega$-Cen GC has a fairly broad $\sigma_{\text{[Fe/H]}}$ (Norris & Da Costa 1995), and younger, more metal-rich GCs appear to lack MPs (Milone et al. 2020), and some UFDs, like Grus-1, have unresolved dispersion in the metallicity (and velocity) of the stars measured so far (Walker et al. 2016; Ji et al. 2019).

Stream kinematic properties are also inconclusive as progenitor diagnostics because thin, cold streams originating from GCs may be thickened and “heated” if formed in Galactic subhaloes prior to accretion into the Milky Way (Carlibor 2018, 2020; Malhan et al. 2021). Such heating may also occur because of the gravitational effect of dark matter substructures in the MW halo (Ibata et al. 2002; Johnston et al. 2002; Peñarrubia 2019), or because of the dispersal of stream stars in axisymmetric (Erkal et al. 2016) as well as non-axisymmetric or time-evolving potentials (Price-Whelan et al. 2016).

The recent detection of C-19, a stream of metal-poor stars recently discovered in the MW halo by combining the power of Gaia proper motions with the photometric metallicities of the Pristine survey, has renewed interest in this topic (Martin et al. 2022). Interestingly, C-19 has kinematic properties that suggest a dwarf galaxy origin (i.e., a width and velocity dispersion of $\approx 180$ pc (for a heliocentric distance of 20kpc) and $\approx 6$ km s$^{-1}$, respectively, see Yuan et al. 2022), but the element abundances of the few stars measured so far indicate a narrow spread in metallicity ($\sigma_{\text{[Fe/H]}} < 0.18$, Martin et al. 2022) and light-element abundance variations akin to those in GCs. At the same time, at $\text{[Fe/H]} \approx -3.4$, C-19 is more metal-poor than any other dwarf galaxy (Chiti et al. 2021) or known globular cluster (Beasley et al. 2019), so elucidating the properties of its progenitor is particularly intriguing.

We explore here an unconventional model, where C-19’s progenitor is envisioned as a dark matter-dominated dwarf galaxy with GC-like enrichment patterns. As we show below, this model circumvents a major difficulty afflicting GC progenitor models: no known GC can disrupt fully on C-19’s orbit and leave a stream as thick and as kinematically hot as observed. Either the stream has been heated after formation by some of the external effects mentioned earlier, or C-19’s progenitor was unlike any GC or dwarf system that has survived to the present.

This contribution is meant to explore the consequences of assuming that C-19’s progenitor was a dark matter-dominated dwarf, and to identify features of this scenario that may falsify it. Our intention is not to deny the possibility that the C-19 stream may have indeed originated from a conventional GC (with an unconventional dynamical heating history), nor to survey the full range of possible origins for C-19, but rather to explore the possibility that the most metal-poor stellar systems to form in the early Universe might have differed systematically from the examples (GCs or UFDs) that have survived to the present day. Should C-19’s progenitor be actually a dark matter-dominated low-surface-brightness UFD, as proposed here, this would be extremely useful for theoretical models of the origins of MPs in globular clusters, many of which assume that the high density environment of present-day GCs is critical for the existence of MPs.

The paper is structured as follows. We introduce the numerical modelling of the stream in Sec. 2, and discuss our main results in Sec. 3. In particular, we explore the evolution of systems modelled after three well-known GCs (NGC 2419, Pal-5 and Pal-14) placed on C-19’s current orbit, and discuss whether it is possible to match the properties of C-19 without leaving behind at the same time a luminous bound remnant (Sec. 3.1). We then explore the stripping of a cold dark matter-dominated dwarf galaxy model in Sec. 3.2. We end with a brief summary of our main conclusions in Sec. 4.

2 C-19 MODELLING

2.1 Observational summary
The extreme metallicity of C-19 stars ([Fe/H] = $-3.38 \pm 0.06$ (stat.) $\pm 0.20$ (syst.); Martin et al. 2022) is well below the metallicity of the second most metal-poor stream discovered so far, the Phoenix stream ([Fe/H] $\approx -2.7$; Wan et al. 2020), and well below the most metal-poor dwarf galaxy, Tucana 2 ([Fe/H] $\approx -2.8$; Chiti et al. 2021). It is also more metal-poor than all known globular clusters, implying that its progenitor was a unique system by any account.

As mentioned above, its width$^2$ and velocity dispersion$^3$ ($177 \pm 25$ pc and $6.2^{+2.0}_{-1.4}$ km s$^{-1}$, respectively, see Yuan et al. 2022) suggest a dwarf galaxy origin rather than a globular cluster one. We show this in Figure 1, where we compare the width and velocity dispersion of C-19.

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1 Ji et al. (2019) identify Grus-1 as a UFD based on its member stars being deficient in neutron-capture elements (indicative for dwarf galaxies, see, e.g., Frebel & Norris 2015), while Walker et al. (2016) refer to Grus-1 more astrophysically as an “ultrafaint stellar system”.

2 The width of the stream is defined as one standard deviation in right ascension $\alpha$ at fixed declination $\delta$ for a heliocentric distance of 20 kpc, multiplied by $\cos(\delta)$.

3 The transverse velocity dispersion is estimated as the dispersion in line-of-sight velocity with respect to the fitted orbit at fixed declination $\delta$. 
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Figure 1. Half-light radii $R_h$ and line-of-sight velocity dispersions $\sigma_{los}$ of dwarf galaxies (blue, filled circles) and globular clusters (grey, filled triangles) with luminosities $L < 10^4 L_\odot$, compared against the characteristic width and velocity dispersion (see footnotes 2, 3) of the C-19 stream (red errorbars). Indicative values of width and velocity dispersion are also shown for other stellar streams (crosses, in blue for streams with dwarf galaxy progenitors, and in grey for those with globular cluster progenitors). N-body models explored in this work are marked in red. References for the data shown are given in footnote 4. A line of constant crossing time $T_{\text{cross}} = 2\pi R_h/\sigma_{los}$ that equals the circular orbital time at pericentre $T_{\text{peri}} = 2\pi R_h/(240 \text{ km s}^{-1})$, is shown in grey. Systems that fall to the right of this line are likely to experience significant tidal stripping on the C-19 orbit. The two dashed diagonal lines correspond to self-gravitating Plummer models (Eq. 3) with fixed total masses of $M_* = 6 \times 10^5 M_\odot$ (the minimum stellar mass of C-19, see text), and of $10^7 M_\odot$. The characteristic width and velocity dispersion of the C-19 stream place it closer to the regime of dwarf galaxies than to the regime of globular clusters.

Figure 2. Metallicity [Fe/H] and luminosity $L$ of the dwarf galaxies (blue, filled circles) and globular clusters (grey, filled triangles) shown in Fig. 1. The C-19 progenitor (shown in red, with errorbars in [Fe/H] corresponding to $\pm 0.2$ dex systemtic uncertainty) appears unique in its properties when compared against known dwarf galaxies and globular clusters.

C-19 (red symbols with errorbars) with a compilation4 of half-light radii, $R_h$, and line-of-sight velocity dispersions, $\sigma_{los}$, of globular clusters (filled grey triangles) and dwarf galaxies (filled blue circles) with $L < 10^4 L_\odot$. The same figure also includes data for other streams in the halo of the Milky Way (blue crosses for dwarf galaxy streams, and grey crosses for GC streams). The globular cluster stream closest in width and velocity dispersion to C-19 is the “Atlas and Aliqa Uma” stream (AUA), which is likely perturbed from interaction with the Sagittarius dwarf (Li et al. 2021).

Fig. 2, on the other hand, compares the metallicity of C-19 and its inferred luminosity $\sim 3 \times 10^4 L_\odot$ (more appropriately, its lower limit, as derived by Martin et al. 2022) with dwarf galaxies and GCs. Clearly, regardless of its luminosity, the progenitor of C-19 has no known parallel in our Local Group.

Aside from its width and velocity dispersion, another C-19 property useful for comparison with our models is its angular extent. This is estimated to be $\sim 15^\circ$ in the sky, with only one star candidate beyond that region (Yuan et al., 2022), and no identifiable bound remnant. We shall take this to imply that the detected stream contains the bulk of the stars in the disrupted progenitor (assumed fully disrupted). Since streams grow longer and sparser as they orbit the Galactic halo, this, in turn, suggests that the stream is relatively “young”, in the sense that its disruption happened relatively recently (i.e., in the most recent past few orbital periods).

Because the stream’s pericentric distance of $r_{\text{peri}} \sim 10$ kpc and apocentric distance $r_{\text{apo}} \sim 20$ kpc indicate an orbital period of just $T_{\text{orb}} \sim 300$ Myr, this implies that either (i) the progenitor has been recently accreted into the MW halo, or that (ii) the stellar component of C-19 was deeply embedded in a more massive (dark) halo that has only recently been sufficiently stripped to affect its stars. Since (i) is disfavoured by the relatively short orbital time and small apocentric distance, we take this observation to support, at least in principle, the premise that C-19’s progenitor could have been more massive and extended in the past.

2.2 Numerical methods

We summarize in this section the N-body models and numerical tools used in this work.

2.2.1 Host galaxy model

We model the Milky Way using a static, axisymmetric, analytical potential with a circular velocity of $V_c(R_\odot) = 240$ km s$^{-1}$ at the solar circle, $R_\odot = 8.3$ kpc. We use the parametrisation of Errani & Peñarrubia (2020), which in turn is derived from the McMillan (2011) model.

In this parametrization, the dark matter halo is modelled using a spherical NFW profile with virial5 mass $M_{200} = 1.15 \times 10^{12} M_\odot$, virial radius $r_{200} = 192$ kpc and concentration parameter $c = 9.5$.

(1996) version December 2010, and updated half-light radii and velocity dispersions for Pal-5 from Kazma et al. 2015; Gieles et al. 2021; for NGC 2419 from Baumgardt et al. 2009, and for Pal-14 from Hilker 2006; Jordi et al. 2009). Width and velocity dispersions for stellar streams are from the $S^3$ survey (Li et al. 2022, table 1), with stream width defined as one standard deviation of a Gaussian profile. In addition, data is shown for the Sagittarius stream (width and velocity dispersion from Ibata et al. 2020 and Gibbons et al. 2017, respectively), the Palomar-5 stream (Bonaca et al. 2020, Kazma et al. 2015), the GD-1 stream (Koposov et al. 2010, Giallucio et al. 2021), and the C-19 stream (both width and dispersion from Yuan et al. 2022, for a heliocentric distance of 20 kpc).

4 Data for dwarf galaxies is as compiled in McConnellie (2012) (version January 2021, width updated data for Antlia 2, Crater 2 (Ji et al. 2021), Tucana (Taibi et al. 2020), Tucana 2 (Chiti et al. 2021), And 19 (Collins et al. 2020) and And 21 (Collins et al. 2021), and for globular clusters as in Harris (1996) version December 2010, and updated half-light radii and velocity dispersions for Pal-5 from Kazma et al. 2015; Gieles et al. 2021; for NGC 2419 from Baumgardt et al. 2009, and for Pal-14 from Hilker 2006; Jordi et al. 2009). Width and velocity dispersions for stellar streams are from the $S^3$ survey (Li et al. 2022, table 1), with stream width defined as one standard deviation of a Gaussian profile. In addition, data is shown for the Sagittarius stream (width and velocity dispersion from Ibata et al. 2020 and Gibbons et al. 2017, respectively), the Palomar-5 stream (Bonaca et al. 2020, Kazma et al. 2015), the GD-1 stream (Koposov et al. 2010, Giallucio et al. 2021), and the C-19 stream (both width and dispersion from Yuan et al. 2022, for a heliocentric distance of 20 kpc).

5 Virial quantities are computed within spheres of mean density equal to 200
We use the potential described above to fit an orbit that matches with masses (2010). The bulge is modelled using a Hernquist (1990) sphere with total vectors in Cartesian coordinates. 2.2.2 Orbit

We use the potential described above to fit an orbit that matches approximately the sky location \((\alpha, \delta)\), proper motions \((\mu_\alpha\ast, \mu_\delta)\), and radial velocities \(v_{\mathrm{rad}}\) (if available), of C-19 member candidates identified by Yuan et al. (2022). Our orbit fitting assumes a solar motion relative to the local standard of rest as in Schönrich et al. (2010).

The fitted orbit has a pericentre of \(r_{\mathrm{peri}} \approx 11\) kpc, an apocentre of \(r_{\mathrm{apo}} \approx 23\) kpc, and an orbital period of \(T_{\mathrm{orb}} \approx 0.34\) Gyrs. The orbit is shown in Fig. 3 in heliocentric Galactic coordinates \([l, b]\). Fig. 4 shows the orbit in Galacticentric Cartesian coordinates, with the Sun at \((x_\odot, y_\odot, z_\odot) = (-R_\odot, 0, 0)\).

The bottom right-hand panel of Fig. 4 shows a zoom-in on the main stream segment, with velocity vectors shown as arrows. For member stars without measured radial velocities (shown in blue), the radial velocity of the orbit at their location is used to obtain the velocity vectors in Cartesian coordinates.

2.3 Globular cluster models

We model globular clusters as self-gravitating Plummer spheres with isotropic velocity dispersion,

\[ \rho_\ast(r) = \frac{3M_\ast}{4\pi a^3} \left[ 1 + (r/a)^2 \right]^{-3/2} \]

with total mass \(M_\ast\), and scale radius \(a\). For spherical Plummer models, the projected half-light radius coincides with scale radius, \(R_\mathrm{h} = a\).

The line-of-sight velocity dispersion profile equals (see, e.g.,

\[ \sigma_{\mathrm{los}}^2(R) = \frac{G M_\ast}{a} \frac{3\pi}{64} \left[ 1 + (R/a)^2 \right]^{-1/2}, \]

which implies that the total mass, \(M_\ast\), may be estimated from the projected half-light radius, \(R_\mathrm{h}\), and the central line-of-sight velocity dispersion, \(\sigma_{\mathrm{los}}(0)\).

\[ M_\ast \approx 6.8 R_\odot \sigma_{\mathrm{los}}^2(0)/G. \]

The importance of Galactic tides on the evolution of a cluster may be gauged by comparing its inner crossing time, \(T_{\mathrm{cross}} \approx 2\pi R_\odot/\sigma_{\mathrm{los}}(0)\), with the circular orbital time at pericentre, \(T_{\mathrm{peri}} \approx 2\pi r_{\mathrm{peri}}/(240 \ \text{km} \ \text{s}^{-1})\). The latter is shown in Fig. 1 as a solid grey line. Systems on or to the right of this line are expected to be severely affected by tides on such orbit; systems well to the left should be able to survive relatively unscathed for many orbital periods.

As may be seen from Fig. 1, most GCs are too dense to disrupt on an orbit like that of C-19, with \(r_{\mathrm{peri}} \approx 11\) kpc; only Pal-14, the least dense known MW GC, is likely to disrupt fully on such orbit. With this caveat, we explore three different self-gravitating GC models, with parameters chosen as GC-1, GC-2, and GC-3 in Fig. 1. These models span a fairly wide range of velocity dispersions and radii, and hence also of stellar mass, as listed in Table 1. Model GC-1 is a fairly dense and massive \((M_\ast \approx 5.1 \times 10^5 M_\odot)\) GC, with parameters resembling those of NGC 2419. Model GC-3, on the other hand is a fluffly, low mass \((M_\ast \approx 6 \times 10^5 M_\odot)\) cluster resembling Pal-14. Model GC-2 has intermediate properties, resembling those of Pal-5.

The \(N\)-body realizations have \(N = 10^6\) particles each and are

Dejonghe 1987, eqn. 43)

\[ \sigma_{\mathrm{los}}^2(R) = \frac{G M_\ast}{a} \frac{3\pi}{64} \left[ 1 + (R/a)^2 \right]^{-1/2}, \]

which implies that the total mass, \(M_\ast\), may be estimated from the projected half-light radius, \(R_\mathrm{h}\), and the central line-of-sight velocity dispersion, \(\sigma_{\mathrm{los}}(0)\).

\[ M_\ast \approx 6.8 R_\odot \sigma_{\mathrm{los}}^2(0)/G. \]
Table 1. Projected half-light radii $R_h$, line-of-sight velocity dispersions $\sigma_{\text{los}}$ and total masses $M_*$ of the globular cluster models used in this work. Masses are estimated using Equation 3.

| Model | Equivalent GC | $R_h$/pc | $\sigma_{\text{los}}$/km s$^{-1}$ | $M_*$/$M_\odot$ |
|-------|---------------|-----------|----------------------------------|-----------------|
| GC-1  | NGC 2419      | 19.0$^1$  | 4.14 ± 0.48$^1$                 | 5.1 $\times$ 10$^5$ |
| GC-2  | Pal-5         | 18.7$^2$  | 1.2 ± 0.3$^3$                   | 4.2 $\times$ 10$^6$ |
| GC-3  | Pal-14        | 27.8$^4$  | 0.38 ± 0.12$^5$                 | 6.3 $\times$ 10$^3$ |

1 Baumgardt et al. (2009) 2 Gieles et al. (2021) 3 Kuzma et al. (2015) 4 Hilker (2006) 5 Jordi et al. (2009)

Figure 5. Initial conditions of the dwarf galaxy-like model. Dark matter properties are shown in blue, those of stars in red. The total stellar luminosity is scaled to $3 \times 10^3 L_\odot$. The top panel shows the initial energy distributions of dark matter and stars, as well as the energy distribution of those particles which remain bound after 0.8 Gyr, 1.8 Gyr and 2.7 Gyr, corresponding to the snapshots shown in Fig. 8. The initial (2D) surface brightness profile is shown in the bottom left, together with the projected initial dark matter density (arbitrary normalisation). The stellar profile is cored, with a projected half-light radius of $R_h = 85$ pc. A King (1962) surface brightness profile with concentration parameter $c_{\text{K}} = 1$ and King core radius $R_C = 210$ pc is shown, for reference, as a black dotted curve. The stellar line-of-sight velocity dispersion profile is shown in the bottom right, with a central line-of-sight velocity of $\sigma_{\text{los}} = 8.1$ km s$^{-1}$.

generated using the code of Errani & Peñarrubia (2020), available online$^6$.

2.4 Dark matter-dominated dwarf galaxy-like model

Our dwarf galaxy-like model assumes that the stellar component of C-19’s progenitor may be modelled as spherical King-like models (King 1962) embedded in a Navarro-Frenk-White (hereafter, NFW, Navarro et al. 1996, 1997) halo. Stars are assumed to be subdominant gravitationally, and can therefore be modelled as massless tracers of the NFW halo, as detailed below.

The NFW dark matter subhalo model is given by

$$\rho_{\text{NFW}} = \rho_s (r/r_s)^{-1} (1 + r/r_s)^{-2}$$

where $\rho_s$ and $r_s$ denote the scale density- and radius, respectively. The corresponding circular velocity curve $V_c = \sqrt{GM(<r)/r}$ reaches its maximum of $V_{\text{max}} \approx 1.65 r_s \sqrt{G \rho_s}$ at a radius $r_{\text{max}} \approx 2.16 r_s$. The N-body realization consists of $10^7$ particles. The NFW density profile is exponentially tapered beyond $10 r_s$ to prevent the divergence of the total mass.

We choose the virial mass of the subhalo to approximately correspond to the minimum halo mass able to form stars imposed by the hydrogen cooling limit (HCL) at an early redshift, chosen here to be $z = 5$ (Benítez-Llambay et al. 2019). The motivation for this choice is mainly one of simplicity: given C-19’s extreme metallicity, its progenitor is likely one of the oldest systems to form in the Universe, and therefore, if dark matter dominated, it should populate some of the lowest mass systems where efficient energy dissipation of the collapse energy may occur. More specifically, we chose a maximum circular velocity of $V_{\text{max}} = 20$ km s$^{-1}$, and a radius of maximum circular velocity $r_{\text{max}} = 1.7$ kpc in order to match the $z = 5$ mean mass-concentration relation (Ludlow et al. 2016). The mass enclosed within $r_{\text{max}}$ equals $M_{\text{NFW}} \approx 1.6 \times 10^7$ $M_\odot$ and the virial mass of the subhalo is $M_{200} \approx 3 \times 10^8$ $M_\odot$.

Stars are embedded in this subhalo as massless tracers, and can therefore be modelled by attaching to each dark matter particle a “stellar probability” that depends on their initial binding energy. We express the binding energy in dimensionless units,

$$E = 1 - E/\Phi_0,$$

where $\Phi_0 \equiv \Phi(r = 0)$ corresponds to the potential minimum of the dark matter halo. In these units, the most-bound state is $E = 0$, and $E = 1$ corresponds to the boundary between bound and unbound. For NFW profiles, the potential minimum is directly related to the maximum circular velocity, $\Phi_{0,\text{NFW}} = -4\pi G \rho_s r_s^2 \approx -4.64 V_{\text{max}}^2$ (for details, see, e.g., Errani et al. 2022). For the tapered NFW models used in this work, we have $\Phi_0 \approx -4.32 V_{\text{max}}^2$.

We select the stellar energies so that the stars form a deeply embedded cored profile within the NFW halo dark matter cusp, with a (2D) half-light radius of $R_h \approx 85$ pc, and a central line-of-sight velocity dispersion of $\sigma_{\text{los}} \approx 8.1$ km s$^{-1}$. We accomplish this by simply assigning a uniform “stellar probability” to all dark matter particles between a specified minimum, $E_{\text{min}}$, and maximum, $E_{\text{max}}$, initial binding energy (see top panel of Fig. 5). Probabilities are set to zero for dark matter particles outside that range.

This choice results in a stellar profile well described by a sharply truncated King (1962) surface brightness profile with concentration parameter $c_{\text{K}} = 1$ and King tidal radius $R_K = 210$ pc. (See Table 2 for a summary of the model parameters.)

Figure 5 shows the resulting stellar density and velocity dispersion profiles (shown in red) compared with the dark matter (in blue). Note that because the stars are assumed to be subdominant, the stellar mass of the galaxy can be rescaled arbitrarily. Our dwarf galaxy-like model for the C-19 progenitor assumes a total stellar luminosity consistent with the minimum inferred from the minimum integrated luminosity of C-19, i.e., $3 \times 10^5 L_\odot$ (Martin et al. 2022). Using a mass-to-light ratio for old stellar populations of $\sim 2$ (Maraston 2005; Woo et al. 2008), this corresponds to a stellar mass of $\sim 6 \times 10^5 M_\odot$.

https://github.com/errani/nbopy
2.5 N-body code

We use the particle-mesh code SUPERBOX (Fellhauer et al. 2000) to evolve the N-body particles of the GC and DG models in the specified Milky Way potential. The code uses two comoving grids, centred on the N-body model, with 128^3 grid cells each. The sizes of the co-moving grids are chosen relative to the size of the N-body model, resulting for Plummer (NFW) models in cell spacings of Δ ≈ 10 r_{max}/128 (∆ ≈ 0.8 r_{max}/128) for the medium resolution grid and Δ ≈ 0.8 r_{max}/128 (∆ ≈ 0.6 r_{max}/128) for the high resolution grid.

The equations of motions are solved using a leap-frog-scheme with a time step ∆t = T_{bin}/200 for Plummer models, where T_{bin} denotes the period of a circular orbit at radius a, and with a time step ∆t = T_{mx}/400 for NFW models, where T_{mx} denotes the period of a circular orbit at r_{max}. Using these choices, a circular orbit with a radius equal to the grid resolution r = Δx is resolved, in the case of Plummer models, with ≈ 120 time steps, and in the case of NFW models, with ≈ 16 steps.

3 RESULTS

We begin by analysing the streams produced by the C-19 globular cluster progenitors described in Section 2.3, before considering dark matter-dominated progenitors in the following subsection.

3.1 Self-gravitating GC model progenitors

3.1.1 NGC 2419-like progenitor (GC-1)

The GC-1 model represents a globular cluster with structural properties similar to that of NGC 2419. It has an initial velocity dispersion (∼ 4 km s$^{-1}$) slightly below that measured for the C-19 stream (∼ 6 km s$^{-1}$), but it is much more massive (M$_{\star}$ ∼ 5 × 10^5 M$_{\odot}$) than the lower limit on the stellar mass inferred for C-19 (M$_{\star}$ ≥ 6 × 10^5 M$_{\odot}$). More importantly, NGC 2419 has a half-light radius of only ∼ 19 pc, implying a relatively high density compared to the inner mean density of the host Galaxy model at its pericentric radius (i.e., it lies well to the left of the grey line in Fig. 1).

Because of this, GC-1 is barely affected by Galactic tides, losing only 15% of its stars over 10 Gyrs of evolution. This model would predict a massive bound remnant on the same orbit as C-19, at odds with observations, where no known cluster has been found to share C-19’s orbit. We show this in Fig. 6, which shows in grey stars from the GC-1 progenitor in heliocentric Galactic coordinates l, b. The location of the bound luminous remnant (with stellar mass ∼ 4 × 10^5 M$_{\odot}$) is indicated by an arrow.

The figure also shows the positions of all known Milky Way GCs with apocentric and pericentric distances in a fairly wide range around the corresponding C-19 values (i.e., 10 kpc < r$_{apo}$ < 30 kpc and pericentric distances 5 kpc < r$_{peri}$ < 20 kpc), taken from Baumgardt et al. 2019). No GC shown in Fig. 6 lies closer than 4º from C-19’s current orbital path. In addition, as mentioned earlier, the metallicity of all known GCs is far in excess of that measure for C-19 members, making them incompatible with being potential progenitors to the C-19 stream. We conclude that GC-1 is not viable as a possible progenitor of the C-19 stream.

3.1.2 Pal 5-like progenitor (GC-2)

The GC-2 model has properties similar to those of Pal-5, a relatively fluffy Milky Way globular cluster, substantially less dense and less massive than NGC 2419. As may be seen from Fig. 1, this cluster model still has a characteristic crossing time $T_{cross} \sim 2\pi R_0/\sigma_{los}$ shorter than the circular orbital time $T_{peri} \sim 2\pi R_0/\sigma_{los}$ at pericentre, and, as a result, we would not expect GC-2 to be fully disrupted by tides.

Indeed, our results show that GC-2 loses ∼ 65 per cent of its initial mass after completing ∼ 30 orbits in about 10 Gyrs. This implies that GC-2 would predict that a bound remnant with total luminosity ∼ 10^4 L$_{\odot}$ should remain visible at present, also at odds with observations. We hence conclude that, just like for GC-1, the GC-2 model is not a viable progenitor of C-19.

3.1.3 Pal 14-like progenitor (GC-3)

Finally, we consider a much lower density GC model (GC-3), inspired by Pal-14, the least dense GC known in the Galaxy. When placed on C-19’s orbit, this system is tidally destroyed after about a dozen of orbits. In order to match C-19’s observed length and width, we are forced to study the remnant after just ∼ 5 Gyrs of evolution. The comparison with C-19, shown in Fig. 7, shows that GC-3 is able to approximately match the width (and length) of the observed stream without leaving behind a bound luminous remnant. However, the velocity dispersion of this stream (∼ 1.4 km s$^{-1}$) is much lower than observed for C-19 (∼ 6 km s$^{-1}$), even if analysed just after disruption. Since streams generally lengthen and become kinematically colder as they evolve (see; e.g., Helm & White 1999) it is unlikely that...
of a halo at the HCL boundary (see Sec. 2.4), a fact that motivates the choice of stellar component parameters described in Sec. 2.4, which are shown by the red symbol labelled “DG” in Fig. 1. Dark matter-dominated models have an advantage over self-gravitating GC models, for they allow us to construct systems where the stellar component may fully disrupt, leaving behind no self-bound stellar remnant, even if a small dark matter clump may remain. We explore these issues in more detail below.

As an illustration, we choose here to simulate the tidal evolution of the dwarf-like model for roughly eight pericentric passages, or 3 Gyrs. Tides strip mass gradually and “outside-in” in terms of initial binding energy (Errani et al. 2022). This is shown in the top panel of Fig. 5, where thin dashed lines outline the sharp energy truncation experienced by the halo at various stages of evolution (i.e., after 0.8, 1.8, and 2.7 Gyr, respectively). Note that after 2.7 Gyr of evolution there is no bound stellar remnant left, although a dense clump of dark matter (consisting of the innermost initial dark matter cusp) remains bound (see, also, Errani & Navarro 2021).

Figure 8 shows projections of the dwarf-like system at those stages of the evolution. The dark matter surface density \( \rho_{2D} \) is shown in grey, and stellar surface brightness \( \Sigma \) in colour. At \( t = 0.8 \) Gyr (or after 2 pericentric passages, left-hand panel), some dark matter has been stripped, but the stellar component is still largely unaffected by tides. At \( t = 1.8 \) Gyr (second panel from left), a stellar stream has formed, and a bound stellar remnant remains centred on the dark matter subhalo (marked by the arrows in each panel). At \( t = 2.6 \) Gyr and \( t = 2.7 \) Gyr (third panel from left, and right-hand panel), the stellar component has been completely dispersed, and no bound stellar progenitor is detectable, consistent with observations.

This scenario leads to the formation of two fairly symmetric streams, each of which, at \( t = 2.6 \) Gyr and \( t = 2.7 \) Gyr, respectively, matches fairly well the width and velocity dispersion of the C-19 stream. This is illustrated in Fig. 9 for the trailing stream at \( t = 2.7 \) Gyr, the top panel compares line-of-sight velocities of the simulation model against C-19 member stars, while the bottom panel shows the positions in the sky. Adjacent histograms sum over the main stream segment, defined as all stars with \( 15^\circ < \delta < 40^\circ \).

What about the other stream? In the case where C-19 is identified with the trailing stream (i.e., \( t = 2.7 \) Gyr in Fig. 8) this would predict the presence of a second, nearly symmetric stream segment that is currently not observed. However, if C-19 were identified with the leading stream (i.e., \( t = 2.6 \) Gyr), then the bulk of the trailing stream would be at very low Galactic latitudes, and could have easily escaped detection. At least from the kinematic perspective, this scenario provides an attractive explanation for the unexpected width and velocity dispersion of C-19.

The times quoted here are for illustrative purpose only: matching models with earlier (or later) accretion time may be constructed through small modifications to the initial stellar binding energies. As the angular separation between leading and trailing stream increases over time, the discovery of a second companion stream to C-19, sharing its orbital pole \( \approx \) \( -140^\circ, b \approx -6^\circ \), see Fig. 3, might allow to constrain the time of accretion of the C-19 progenitor onto the Milky Way. If the C-19 progenitor is still in the process of disrupting, leading and trailing stream may appear as a single, connected structure.

7 Eq. 3 was derived for self-gravitating Plummer spheres. Here, we apply it tentatively to the width and velocity dispersion of the C-19 stream, assuming that these values are a rough proxy for size and velocity dispersion of the C-19 progenitor at the time when the stream formed.

8 While the pole of the C-19 orbit precesses over time, the angular separation between the orbital poles of leading and trailing stream grows at a much lower pace.
Figure 8. Distribution of dark matter (grey) and stars (colour) for the dwarf galaxy-like model at different times after accretion, in galactocentric Cartesian coordinates. At \( T = 0.8 \) Gyrs (left-hand panel), some dark matter has been stripped, but the stellar component is largely unaffected by tides. At \( T = 1.8 \) Gyrs (second panel from left), a stellar stream has formed, but a bound stellar cluster remains centred on the remnant dark matter subhalo. At \( T = 2.6 \) Gyrs (third panel from left), the stellar cluster has been completely dispersed, and no bound stars remain within the dark matter subhalo. This scenario is a possible model for the formation of the C-19 stream, with the leading stream corresponding to C-19. Observed stream members are shown using red and blue points (with distances adjusted), in good agreement with the leading stream of the disrupted dwarf galaxy-like model. Note that while no bound stellar remnant remains, the dark matter subhalo does not fully disrupt. The right-hand panel \( (T = 2.7 \) Gyrs) shows a similar situation, but here, the trailing tidal stream matches the C-19 data. The centre of mass of the bound dark matter remnant is shown using an arrow in all panels. A video of this simulation is available on the journal website.

Figure 9. Comparison of the dwarf galaxy-like model against velocities (top panel) and positions (bottom panel) of C-19 member stars (as in Fig. 7). The width and dispersion of the \( N \)-body model match that of the C-19 stream members. The arrow shows the position of the centre of mass of the bound dark matter remnant.

4 SUMMARY AND CONCLUSIONS

The C-19 stellar stream is the most metal-poor stream known to date, with a mean metallicity of \([\text{Fe}/\text{H}] \approx -3.4\). As only a very small spread in metallicity \((\sigma_{[\text{Fe}/\text{H}]} \lesssim 0.18)\) is observed, it is tempting to associate C-19 with a tidally disrupted globular cluster. However, the unusual width and velocity dispersion of the stream suggest a possible dwarf galaxy origin for the stream. We have explored here scenarios where the progenitor of C-19 is either a self-gravitating globular cluster, or a dark matter dominated stellar system similar in structure to dwarf spheroidal galaxies.

Our main conclusions may be summarised as follows.

i) The C-19 stellar stream has a width and a velocity dispersion exceeding those of known globular cluster streams, and structurally place C-19 closer to the regime of dwarf galaxies than that of globular cluster streams.

ii) Self-gravitating globular cluster progenitors similar in structure to NGC 2419 and Pal-5 are too dense to be fully disrupted on C-19’s orbit over a period of 10 Gyrs. These may be ruled out by the lack of a bound luminous remnant associated with C-19.

iii) A self-gravitating progenitor similar to the Pal-14 globular cluster matches the integrated luminosity of C-19 and disrupts fully, but yields a stream too kinematically cold to match C-19’s observed velocity dispersion.

iv) A dark matter-dominated dwarf galaxy-like progenitor, where stars follow a King-like profile embedded in a low-mass cuspy cold dark matter model near the hydrogen cooling limit, is able to reproduce the width and velocity dispersion of C-19, leaving behind no bound stellar remnant.

v) The dwarf galaxy progenitor model predicts the existence of a second tidal stream, similar to C-19 but at Galactic latitudes likely coinciding with the Galactic plane, hindering its discovery. The discovery of such a stream, symmetric in structure and luminosity to C-19, would strongly favour the dwarf-like progenitor model.

Although the dynamical evidence seems to favour a DG-like progenitor for C-19, it is difficult to completely rule out GC-like progenitors. Indeed, different dynamical processes have been discussed in the literature that could increase the width and velocity dispersion of globular cluster streams beyond the values expected from stripping in smooth tidal fields such as the one considered here. These include the gravitational effect of (dark) matter clumps in the MW halo (Ibata et al. 2002; Johnston et al. 2002; Penarrubia 2019), the dispersal of stream stars in non-axisymmetric or time-evolving potentials (Price-Whelan et al. 2016), tidal evolution of the GC within a subhalo prior to accretion onto the MW (Carlberg 2018, 2020; Malhan et al. 2021), as well as collisional processes within the GC that might facilitate tidal disruption (Gieles et al. 2021). What observations could help us distinguish a globular cluster stream that has been thickened and “heated” from the dwarf galaxy-like progenitor we explored here? A non-exhaustive list of diagnostics include the following:

i) Signs of collisional processes in the progenitor, like mass-
segregation of C-19 member stars along the orbit, might give dynamical hints on the progenitor dynamics and allow to distinguish a (collisional) GC from a (collision-less) dwarf-like system.

ii) Our dwarf galaxy-progenitor model predicts two rather symmetric tidal streams. The detection of a second stream segment, with a luminosity and structure similar to that of the current C-19 segment, would be an indicator in favour of the dwarf-like model, in contrast to the more irregular streams of pre-accretion stripped globular clusters (see, e.g., Malhan et al. 2021).

iii) A better understanding of the origin of light-element abundance patterns in GCs and in low-metallicity UFDs, together with improved observational constraints on a larger number of C-19 stars, might allow to use them as discriminating diagnostics of C-19’s progenitor. Is it actually possible for dwarf galaxies to develop GC-like light-element enrichment patterns while keeping a narrow spread in metallicity?

If the hypothesis of a dark matter-dominated progenitor holds, then C-19 is allowing a glimpse at galaxy evolution at the faintest end of the galaxy luminosity function, and would suggest that the earliest, most metal-poor stellar systems formed may differ substantially from the more metal-rich globulars and dwarfs that have survived to the present day.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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