Results from the BABAR Fully Inclusive Measurement of $B \rightarrow X_s \gamma$

The BABAR Collaboration

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Abstract

We present preliminary results from a lepton-tagged fully-inclusive measurement of $B \rightarrow X_s \gamma$ decays, where $X_s$ is any strange hadronic state. Results are based on a BABAR data set of 88.5 million $B\bar{B}$ pairs at the $\Upsilon(4S)$ resonance. We present a reconstructed photon energy spectrum in the $\Upsilon(4S)$ frame, and partial branching fractions above minimum reconstructed photon energies of 1.9, 2.0, 2.1 and 2.2 GeV. We then convert these to measurements of partial branching fractions and truncated first and second moments of the true photon energy distribution in the $B$ rest frame, above the same minimum photon energy values. The full correlation matrices between the first and second moments are included to allow fitting to any parameterized theoretical calculation. We also measure the direct $CP$ asymmetry $A_{CP}(B \rightarrow X_{s+d}\gamma)$ (based on the charge of the tagging lepton) above a reconstructed photon energy of 2.2 GeV.

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1 Introduction

In the Standard Model the radiative decay $b \rightarrow s\gamma$ proceeds via a loop diagram, and is sensitive to possible new physics, with new heavy particles participating in the loop \cite{1}. Next-to-leading-order calculations for the branching fraction give $B(B \rightarrow X_s\gamma) = (3.57 \pm 0.30) \times 10^{-4}$ \cite{2}, where $E_\gamma$ is the photon energy in the $B$ rest frame; calculations to higher order are currently underway \cite{3}. Measurement of the $E_\gamma$ spectrum from $B \rightarrow X_s\gamma$ decays, and in particular of its moments above various minimum energies, allows the determination of the heavy quark effective field theory parameters $m_b$ and $\mu_b^2$, related to the $b$-quark mass and momentum within the $B$ meson, respectively \cite{4,5,6,7}.

This note reports on a fully inclusive analysis of data collected from $\Upsilon(4S) \rightarrow BB$, where the photon from the decay of one $B$ meson is detected, but the $X_s$ system is not reconstructed. Previous fully-inclusive measurements of $B \rightarrow X_s\gamma$ have been presented by the CLEO \cite{8} and BELLE \cite{9} collaborations. The alternative approach of summing a number of exclusive decays \cite{10} is more dependent on the $X$ fragmentation model, and in particular on assumptions made as to the fraction of unmeasured final states. In the fully-inclusive measurement we largely avoid such uncertainties, but at the cost of higher backgrounds, which need to be strongly suppressed. Much of the non-$BB$ (continuum) background is removed by requiring a high-momentum lepton tag; this selects $BB$ events in which the non-signal $B$ meson decays semileptonically. Continuum background is further suppressed by topological cuts. Remaining continuum background is subtracted using off-resonance data recorded at an $e^+e^-$ center-of-mass (c.m.) energy just below that of the $\Upsilon(4S)$. Backgrounds from $BB$ events are estimated from a Monte Carlo simulation; for the most important backgrounds the simulation is checked and corrected using data control samples.

We present preliminary results of this analysis, in particular the partial branching fraction and the first and centralized second moments of the photon energy distribution $\langle E_\gamma \rangle$ and $\langle E_\gamma^2 \rangle - \langle E_\gamma \rangle^2$, respectively) for each of four minimum-$E_\gamma$ cuts in the $B$ rest frame: 1.9, 2.0, 2.1 and 2.2 GeV. Hereafter we refer to the centralized second moment as the “second moment”. These are obtained from the corresponding quantities for reconstructed photon energy $E_\gamma^\ast$ in the $e^+e^-$ c.m. frame (an asterisk denotes a a c.m. quantity) by applying corrections for resolution smearing and the effect of imposing an experimental cut on $E_\gamma^\ast$ rather than $E_\gamma$. The full correlation matrix between the first and second moments is given to facilitate fitting to any parameterized theoretical calculation. The measurement does not distinguish $B \rightarrow X_d\gamma$ events from $B \rightarrow X_s\gamma$ events. We assume the ratio of $B \rightarrow X_d\gamma$ to $B \rightarrow X_s\gamma$ is $|V_{td}/V_{ts}|^2$, so that it constitutes $(4.0 \pm 1.6)\%$ of the rate \cite{9}, and correct for this at the end. This assumption is supported by newer theoretical calculations \cite{11,12}. We also present a measurement of the $CP$ asymmetry in the sum of $B \rightarrow X_s\gamma$ plus $B \rightarrow X_d\gamma$, based on the charge of the tagging lepton. Pending a more detailed study of the energy spectrum, we do not yet perform the model-dependent extrapolation to the entire photon spectrum.

The results presented are based on data recorded with the $BABAR$ detector \cite{13} at the PEP-II asymmetric-energy $e^+e^-$ collider located at the Stanford Linear Accelerator Center. The on-resonance data integrated luminosity is 81.5 fb$^{-1}$, corresponding to 88.5 million $BB$ events. Additionally, 9.6 fb$^{-1}$ of off-resonance data are used in the continuum background subtraction. The $BABAR$ Monte Carlo simulation program, based on GEANT 4 \cite{14} and JETSET \cite{15}, is used to generate samples of signal events, $B^+B^-$ and $B^0\overline{B}^0$ (excluding signal channels), $q\overline{q}$ (udsc continuum) and $\tau^+\tau^-$. In order to minimize any possible experimenter’s bias, the spectrum of reconstructed photon energy $E_\gamma^\ast$ from 1.9 to 2.9 GeV in the on-resonance data was “blinded”, i.e., not looked at until all selection cuts were set and dominant $BB$ corrections determined.
2 Signal Model and Backgrounds

In order to compute signal \((B \rightarrow X_s \gamma)\) efficiency, we use the \(m_{X_s}\) spectrum computed by Kagan and Neubert (KN) \[4\]. This quantity has a one-to-one correspondence with the photon energy in the \(B\)-meson rest frame via the kinematic relation

\[
E_\gamma = \frac{m_B^2 - m_{X_s}^2}{2m_B}.
\]

The KN spectrum is a smooth function of \(m_{X_s}\), i.e., it does not explicitly model strange resonances in the mass spectrum. This assumption is not valid for the decay \(B \rightarrow K^*(892)\gamma\), so the spectrum needs to be modified to describe it. Higher-mass resonances are broad and spaced closely enough, such that the smooth approximation of the KN treatment is justified. In practice, a relativistic Breit-Wigner distribution modeling the \(B \rightarrow K^*\gamma\) decay is used for \(m_{X_s} < 1.1 \text{ GeV}/c^2\) \((E_\gamma > 2.525 \text{ GeV})\) and the KN spectrum is used above the cutoff. The \(K^*\gamma\) part is normalized to the fraction of the KN spectrum below the \(m_{X_s}\) cutoff. The KN model is parameterized in terms of two quantities, \(m_b\) (the \(b\)-quark mass) and \(\mu_\pi^2\) (a measure of the quark’s Fermi momentum inside the \(B\) meson). We chose a KN480 model, with \(m_b = 4.80 \text{ GeV}/c^2\) and \(\mu_\pi^2 = 0.3 \text{ GeV}^2\), for studying systematic effects on signal efficiency and for optimizing selection criteria. For the latter purpose, an overall normalization was applied such that the \(B \rightarrow K^*\gamma\) component matches the previous \(B\bar{B}\) measurement \[16\]. In order to assess possible model-dependence of our results we use additional KN models with \(m_b\) between 4.55 and 4.80 \(\text{ GeV}/c^2\), along with a set of models based on the theory of ref. \[5\].

Backgrounds arise from continuum \((e^+e^- \rightarrow q\bar{q}, \text{ where } q = uds c, \text{ and } \tau^+\tau^-)\) and \(B\bar{B}\) events. There are additional contributions from QED and hadronic two-photon processes, which are not simulated. In \(B\bar{B}\) events, the main backgrounds come from decays of \(\pi^0\) and \(\eta\) mesons, with a smaller contribution from hadrons (mostly antineutrons) that are misidentified as photons. In continuum events, these backgrounds also contribute, along with initial state radiation (ISR), where a high-energy photon is radiated from one of the colliding \(e^\pm\).

3 Event Selection

The \(B\bar{B}\) detector \[13\] tracks charged particles with a five-layer double-sided silicon-strip detector and a forty-layer drift chamber placed inside a 1.5 T solenoidal magnet. Electromagnetic showers are detected in a total-absorption calorimeter consisting of 6580 CsI(Tl) scintillating crystals arranged hermetically in a projective geometry. Muons are indentified by resistive-plate chambers interleaved in the flux-return yoke of the magnet, outside of the calorimeter.

The distinctive feature of the signal decays is an isolated photon with c.m. energy from about 1.6 GeV to 2.8 GeV. Our starting point is finding in the event at least one isolated photon candidate, i.e., a localized calorimeter energy deposit, with \(1.5 < E_\gamma^c < 3.5 \text{ GeV}\) (“photon acceptance”). We then apply several categories of selection cuts, described in the next few paragraphs: hadronic event selection, photon quality criteria, event shape cuts and tagging requirements. Table \[11\] shows the efficiencies of the different categories of cuts for signal and background event samples. In order to avoid regions where the expected signal would still be overwhelmed by background (especially \(B\bar{B}\) background at low \(E_\gamma^c\)), our results will be quoted for several minimum-\(E_\gamma^c\) cuts of 1.9 GeV or above. The table illustrates the efficiencies for one particular choice.

Hadronic events are selected by requiring at least three reconstructed charged tracks and the second Fox-Wolfram moment \(R_2^* < 0.9\), calculated in the c.m. frame using all detected particles.
To reduce QED and two-photon backgrounds, we use a cut on “effective multiplicity,” defined as the number of charged tracks plus half the number of photons with energy above 0.08 GeV. We require $n_{\text{eff}} \geq 4.5$, a value that has essentially no impact on signal efficiency.

Photon quality cuts are designed to suppress high-energy photon candidates which arise from backgrounds. We require that the polar angle of the photon satisfy $-0.74 < \cos \theta_\gamma < 0.93$, to ensure that the photon shower is well contained in the calorimeter. We suppress hadronic showers and $\pi^0$s with merged photon showers by requiring that the shower has a lateral profile consistent with a single photon. Photons that are consistent with originating from an identifiable $\pi^0$ or $\eta$ decay are explicitly vetoed. The optimal $\pi^0(\eta)$ veto requirements are energy-dependent, with a more open selection for $E^*_\gamma > 2.3$ GeV. Finally, isolated photons are selected by requiring that no energy (neutral or charged) be within 25 cm (approximately seven times the Molière radius for CsI) of the photon, as measured at on the calorimeter’s inside surface.

Event shape variables are employed to exploit the difference in topology of $B\bar{B}$ events and continuum events. The former tend to be spherical in shape, since the $B$ mesons are produced nearly at rest in the $\Upsilon(4S)$ rest frame, while continuum events tend to have a more jet-like structure. We combine 19 different variables into a single Fisher discriminant. Eighteen of the quantities are the sum of charged and neutral energy found in 10-degree cones (from 0 to 180 degrees) centered on the photon candidate direction. The photon energy is not included in any of the cones. The nineteenth variable is the quantity $R_2/R_2^{\prime}$, where $R_2$ is the second Fox-Wolfram moment calculated in the frame recoiling against the photon (which for ISR events is the $q\bar{q}$ rest frame), using all particles except the photon. The Fisher coefficients were determined by maximizing the separation power between simulated signal and continuum events. Cuts on the Fisher variable and $R_2^{\prime} (< 0.55)$ remove 84% of the remaining continuum background at this stage.

Lepton tagging is used to further reduce the backgrounds from continuum events. About 20% of $B$ mesons decay semileptonically to either $e$ or $\mu$, and the large mass of the $B$ meson tends to impart large momentum to its lepton daughter. Leptons from fragmentation in continuum events tend to be at lower momentum. Since the tag lepton comes from the recoil $B$ meson, it does not compromise the inclusiveness of the $B \to X_s \gamma$ selection. Electrons are identified by requiring a well-measured track matched to an energy deposit in the calorimeter consistent with an electromagnetic shower. Muons are identified by matching a well-measured track to hits in the muon detector, with no more than a minimum-ionizing energy deposit in the calorimeter. The tag lepton is required to have c.m. momentum greater than 1.25 GeV/c for electrons and 1.5 GeV/c for muons. Furthermore, making a cut on the angle between the photon and the lepton, $\cos \theta_{\gamma\ell} > -0.7$, removes more continuum background, in which the lepton and photon candidates tend to be back-to-back. Finally, we exploit the presence of a relatively high-energy neutrino in semileptonic $B$ decays and place a cut on the missing energy in the event in the c.m. frame, $E_{\text{miss}}^* > 0.8$ GeV.

Virtually all of the tagging leptons arise from the decay $B \to X_\ell \ell \nu$. We correct the rate of such events in our simulation based on the studies presented in Ref. [17]. The overall rate of $B \to X_\ell \ell \nu$ is comprised of four decay modes, where the hadronic system is $D$, $D^*$, $D^{**}$ (higher mass resonances), and non-resonant $D^{(*)}\pi$, respectively. A scale factor was determined for each mode and we have weighted our simulated semileptonic decays accordingly. We also reweight the simulated form factors of the $D^*\ell\nu$ decay to those measured by BABAR[13].

The values for many of the cuts described above, along with the Fisher coefficients, were optimized with all other cuts applied, using an iterative technique. In each case, the quantity maximized was $S^2/(S + B + \alpha C)$, where $S$ is the expected signal from the KN480 model described above, $B$ is the simulated $B\bar{B}$ background, and $C$ is the simulated continuum background, each being the
Table 1: Selection efficiencies for signal and background events, broken down into different cut categories, as described in the text. The total selection efficiency is relative to the photon acceptance. The signal model used is KN480 including $K^*\gamma$, as defined in the text. The error on the total signal efficiency from Monte Carlo statistics is 1.1%.

|                      | $B \rightarrow X_s\gamma$ | $\bar{B}$ | udsc |
|----------------------|-----------------------------|-----------|------|
| Photon acceptance    | 0.782                       | 0.023     | 0.124|
| Hadronic             | 0.937                       | 0.979     | 0.826|
| Photon quality       | 0.753                       | 0.175     | 0.196|
| $2.0 < E_\gamma^* < 2.7$ GeV | 0.910                    | 0.114     | 0.326|
| Event shape          | 0.601                       | 0.401     | 0.167|
| Tagging              | 0.052                       | 0.041     | 7.4 $\times$ 10$^{-4}$|
| Total selection      | $2.0 \times 10^{-2}$       | $3.2 \times 10^{-4}$ | $6.5 \times 10^{-6}$|

number of events expected for the on-resonance data luminosity, and $\alpha$ is the ratio of total to off-resonance luminosity. The factor $\alpha$ takes into account the fact that we later use off-resonance data to subtract the residual continuum background.

Figure 1 shows the overall signal efficiency in bins of $E_\gamma^*$. The $E_\gamma^*$ dependence is a result of the optimization procedure, in particular the training of the Fisher discriminant. The sum of the 18 energy-flow variables combined in the Fisher discriminant is correlated with the energy of the photon in the $B$ rest frame. Without the Fisher selection the continuum background decreases by a factor of two over the 2.0 to 2.7 GeV range of $E_\gamma^*$ used for optimization, while the expected signal increases rapidly between 2.0 and about 2.4 GeV. Therefore, the optimization suppresses background more strongly with decreasing $E_\gamma^*$, leading to a corresponding reduction of the efficiency. The more stringent $\pi^0(\eta)$ vetoes applied in events with $E_\gamma^* < 2.3$ GeV also contribute to the energy dependence. The variation of the efficiency with $E_\gamma^*$ does not introduce a significant dependence on the multiplicity of the $X_s$ system, which would lead to uncertainties related to fragmentation modeling. However, the variation of the efficiency with $E_\gamma^*$ does lead to a dependence on the modeling of the photon energy spectrum. The dominant effect is that reducing the assumed value of $m_b$ in a particular model leads to reduction in the mean $E_\gamma^*$, which in turn yields a smaller selection efficiency. We improve the estimation of the signal efficiency and reduce the model-dependent uncertainty with a bootstrapping procedure described in section 5.1.

The simulated $E_\gamma^*$ distribution of signal, continuum and $\bar{B}B$ background events after all selection criteria is shown in Fig. 1. Note that the continuum Monte-Carlo does not include QED backgrounds present in the data. The actual continuum background is subtracted using the off-resonance data and is the dominant source of statistical uncertainty on the measurements.

## 4 $\bar{B}B$ Backgrounds

As can be seen in Figure 2 the $\bar{B}B$ background dominates for $E_\gamma^* < 2.4$ GeV. We present in Table 2 the various sources of background coming from $B\bar{B}$ events, as predicted by our Monte Carlo simulation.

About 80% of the background comes from photons from $\pi^0(\eta)$ decays, for both the nominal
signal region ($2.0 < E^*_\gamma < 2.7 \text{ GeV}$) and a control region ($1.6 < E^*_\gamma < 1.9 \text{ GeV}$). Other significant sources are hadrons in the signal region ($\sim 8\%$) and electrons in the control region ($\sim 9\%$). We have performed dedicated studies of data control samples for these sources, to verify and/or correct the Monte Carlo predictions.

The level of the largest $B\bar{B}$ background component, $\pi^0(\eta)$ decays, has been measured directly from the data. We explicitly measure the yield of $\pi^0$ and $\eta$ decays in bins of $E_{\pi^0}^*$ or $E_{\eta}^*$ in on-resonance data, off-resonance data and $B\bar{B}$ simulation samples, by fitting the $\gamma\gamma$ mass distributions. This allows us to derive correction factors versus $\pi^0(\eta)$ energy for the $\pi^0(\eta)$ rates predicted by the simulation. These corrections are then applied to our $B\bar{B}$ simulation when estimating the $B\bar{B}$ background passing the $B \rightarrow X_s\gamma$ selection. The $\pi^0(\eta)$ analysis uses the same selection criteria as for the $B \rightarrow X_s\gamma$ analysis, with three exceptions: 1) the $\pi^0(\eta)$ vetoes are not applied, 2) the requirement on the photon energy is reduced to $E^*_\gamma > 1.0 \text{ GeV}$ to increase statistics, and 3) the tagging momentum cuts are loosened to 1.0 GeV$/c$ for electrons and 1.1 GeV$/c$ for muons, again to increase the available statistics. We apply an additional small correction to account for differences in the performance of the $\pi^0(\eta)$ veto in data and $B\bar{B}$ simulation.

The background from hadrons faking photons in $B\bar{B}$ events consists primarily of $\pi$s with a small contribution from $\bar{p}$s. We have corrected the $B\bar{B}$ simulation for both the $\pi(\bar{p})$ production and $\pi(\bar{p})$ response in the calorimeter. First, an inclusive measurement of $p$ and $\bar{p}$ production, is used to correct the simulation prediction for both $\bar{p}$ and $\pi$ production. A conservative 50% systematic uncertainty is assigned to account for the fact that we are using a $\bar{p}$ measurement to correct $\pi$ production. Additionally, $\Lambda \rightarrow \bar{p}\pi^+$ decays are studied both in real data and simulation to compare the response of the calorimeter to $\bar{p}$s. We find a significantly smaller number passing

Figure 1: The overall signal efficiency in bins of $E^*_\gamma$ (computed using the KN480 model as defined in the text).
the $E^*_\gamma$ and lateral-shower-profile cuts in the data than that expected from the simulation. The total correction factor, then, is a product of the production correction and the efficiency correction, determined in bins of $E^*_\gamma$.

Electrons can cause a background to the photon sample if the charged track is not reconstructed or matched to the electromagnetic shower. (Bremsstrahlung photons are an additional source of background from $e^\pm$, which is well modeled in the simulation.) The electron tracking efficiency was measured in data by selecting one track of a Bhabha event and then measuring the probability of reconstructing the other electron track. A further correction is made to account for the fact that the environment of the control sample (Bhabha events) has significantly lower multiplicity on average than the actual data sample (hadronic events).

We have also derived corrections for the very small number of background photons from $\omega$ and $\eta'$ decays. The corrections to the modeling of $B \rightarrow X_s\gamma$ described in section 3 are applied to the $B\bar{B}$ simulation. After all corrections, we check our estimate of the $B\bar{B}$ background by considering the low energy control region $1.6 < E^*_\gamma < 1.9$ GeV, where we expect few photons from $B \rightarrow X_s\gamma$ decays. In this region we observe $1790 \pm 64$ events after continuum subtraction compared to an expectation of $1667 \pm 54$ events, i.e.

$$\text{Observed} - \text{Expected} = 123 \pm 64(\text{stat.}) \pm 54(\text{syst.})$$

The significance of the deviation is $1.5\sigma$. Note that for this check we have not subtracted any signal contribution, which for the KN480 and KN465 models defined above would be approximately 17 and 39 events, respectively. These would reduce the significance of the deviation to $1.3\sigma$ and $1.0\sigma$, respectively.
Table 2: Breakdown of Monte Carlo simulated $B\bar{B}$ backgrounds by high-energy photon origin for $2.0 < E^*_\gamma < 2.7$ GeV. These fractions are for the combined $B^0\bar{B}^0$ and $B^+\bar{B}^-$ Monte Carlo samples before tagging cuts.

| Truth-match     | Parentage | Fraction of $B\bar{B}$ background $(2.0 < E^*_\gamma < 2.7$ GeV) |
|-----------------|------------|---------------------------------------------------------------|
| Photon          | $\pi^0$    | 0.640                                                         |
|                 | $\eta$     | 0.174                                                         |
|                 | $\omega$   | 0.024                                                         |
|                 | $\eta'$    | 0.011                                                         |
|                 | FSR        | 0.007                                                         |
|                 | $J/\psi$   | 0.008                                                         |
|                 | Other      | 0.001                                                         |
|                 | Total      | 0.865                                                         |
| $\pi^0$ (merged)| Any        | 0.001                                                         |
| Electron        | Any        | 0.036                                                         |
| $\pi$ ($n$)     | Any        | 0.077                                                         |
| $\bar{\pi}$ ($p$)| Any      | 0.005                                                         |
| $K^0_L$         | Any        | 0.001                                                         |
| $\pi^\pm$ or $K^\pm$ | Any    | 0.001                                                         |
| Unidentified    |            | 0.015                                                         |

Table 3: Extracted tagged signal yields in various ranges of $E^*_\gamma$, uncorrected for efficiency. The first error is statistical, the second is from $B\bar{B}$ systematics.

| $E^*_\gamma$ (GeV) | Tagged Signal Yield (events) |
Figure 3: Photon energy spectrum after background subtraction, uncorrected for efficiency. Error bars include statistical (dominant) and $B\bar{B}$ systematic uncertainties, added in quadrature.

Efficiency and mean energy is approximately linear, with a best match close to a KN460 model (with $\mu^2_\pi = 0.603$). We have carried out the same studies for twelve different parameterizations of the Benson, Bigi and Uraltsev (BBU) calculation, using the same prescription to include a $K^*$ component as for KN. We varied $m_b$ between 4.45 and 4.75 GeV and $\mu^2_\pi$ between 0.25 and 0.65 GeV$^2$. (Note that these two parameters are defined differently than their KN counterparts.) We set $\mu^2_G$ (the matrix element of the chromomagnetic operator, responsible for the hyperfine splitting between $B$ and $B^*$ mesons) to either 0.35 or 0.27 GeV$^2$. All the BBU results for the signal efficiency versus mean energy lie on the same line as for the KN model, confirming the model-independence of the bootstrapping procedure. Thus the KN460 efficiency is used to determine the partial branching fractions (PBFs) according to:

$$B(B \to X_s \gamma, E^*_\gamma \text{ in range}) = \frac{\text{Events in range}}{2 \times N_{BB} \times \epsilon_{\text{KN460}}}. \quad (3)$$

Figure 4 shows the efficiency-corrected spectrum using the KN460 model. We have taken a conservative approach of assigning to each bin a model-dependence uncertainty corresponding to the maximum efficiency deviation, among KN455 to KN480 models and the 12 BBU models, from the KN460 value. Note that these models span a range of mean energy up to 2$\sigma$ away from our measured value.

To make the results directly comparable to theoretical predictions, we correct for the fact that the cut in photon energy is made on reconstructed $E^*_\gamma$ in the $\Upsilon(4S)$ (c.m.) frame rather than on true $E_\gamma$ in the $B$ rest frame. The latter energy has been smeared by a Doppler shift and by the (asymmetric) calorimeter resolution. (Doppler smearing arises from the Lorentz transformation

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Figure 4: Efficiency-corrected photon energy spectrum for the extracted signal, shown only for the originally-blinded range of reconstructed energy (note the range 2.7-2.9 GeV is not used to measure the branching fractions or moments). The small error bar is statistical only. The larger error bar also includes $B\bar{B}$ and other systematic uncertainties and a model-dependence uncertainty, all in quadrature. There are significant correlations among non-statistical uncertainties for different bins.

from the $B$ rest frame to the $\Upsilon(4S)$ frame, given our ignorance of the direction of the $B$.) We compute the correction factor $\alpha_{\text{cut}}$ for the KN and BBU models and find that it has minimal model-dependence. Table 4 shows PBFs with corrections applied, along with the statistical, systematic and model-dependent errors. For the corrected PBFs the latter includes two correlated contributions: the model-dependent efficiency uncertainty noted above, already applied to the measured PBFs, and the uncertainty on $\alpha_{\text{cut}}$.

We studied many sources of systematic uncertainty, and here note the more significant. The uncertainty on the $B\bar{B}$ background subtraction is shown in Table 3 and amounts to 5.5% for 2.0 to 2.7 GeV. It comes mostly from the statistical uncertainties on the correction factors derived from the $\pi^0(\eta)$ control sample. Other systematic effects total 6.4% in quadrature. Of this, 3.3% is the uncertainty on photon selection, dominated by a 2.5% uncertainty on photon efficiency (determined from $\pi^0$s in $\tau$ decays) and 2% for the photon isolation cut. It also includes allowance for uncertainties in photon energy scale and resolution, and in the photon lateral shape cut efficiency, derived mainly from data from the $\text{BABAR} \ B \rightarrow K^*\gamma$ analysis and photons from virtual Compton scattering. The efficiency of the event shape cuts was studied using a $\pi^0$ control sample to compare distributions of the Fisher discriminant between data and simulation, resulting in an uncertainty of 3.0%. A small sensitivity to details of $X_s$ fragmentation implies, for the adjustments determined in the $\text{BABAR}$ semi-inclusive analysis, an additional uncertainty of only 1.4%. A 2.2% uncertainty is assigned for lepton identification, and 3.0% for the uncertainties on the semileptonic corrections.
Table 4: Partial branching fractions (PBFs, preliminary) corrected to the $B$ rest frame for four different reconstructed-$E_\gamma^*$ ranges. The uncertainties shown for the PBFs are statistical, systematic and model-dependent. The “Measured” values are in terms of $E_\gamma^*$ in the c.m. frame. The correction factor $\alpha_{cut}$ converts the measured branching fraction for an $E_\gamma^*$ cut to a result in the $B$ rest frame with an equal $E_\gamma$ cut, while the factor $\alpha_{d/s}$ removes the (4.0 \pm 1.6)%) $B \rightarrow X_d\gamma$ component. For the last column, the error on $\alpha_{cut}$ is added linearly to the fractional model-dependence error, while the error on $\alpha_{d/s}$ is added in quadrature to the systematic error.

### 5.2 Truncated Moments

As noted above, the truncated moments of the photon energy spectrum are of interest because they can be related to parameters of heavy quark theory. The measured first moment $\langle E_\gamma^* \rangle$ and second moment $(\langle E_\gamma^* \rangle^2 - \langle E_\gamma^* \rangle^2)$ are computed by averaging over the efficiency-corrected photon energy spectrum in 100 MeV bins. We do this for four different energy ranges, extending from 1.9, 2.0, 2.1 or 2.2 GeV to 2.7 GeV. The bin-by-bin efficiencies derived from the KN460 model are used to correct the yields.

The observed moments are derived from the measured $E_\gamma^*$ spectrum but the moments computed in theoretical calculations involve the true $E_\gamma$. Thus we need to correct the former for Doppler and calorimeter-resolution smearing. For a spectrum without energy cuts, the total shift of the first (second) moment is the sum of the first (second) moments of the smearing functions, about $+0.005$ GeV ($+0.007$ GeV$^2$) for Doppler smearing plus $-0.040$ GeV ($+0.014$ GeV$^2$) for the calorimeter. The latter corrections are reduced when the spectrum is truncated by a minimum energy cut, e.g., to $-0.027$ GeV ($-0.007$ GeV$^2$) for a typical BBU model ($m_b = 4.6$ GeV, $\mu^2 = 0.45$ GeV$^2$) with a cut of 2.0 GeV. An additional small shift accounts for cutting on the reconstructed $E_\gamma^*$ in the $Y(4S)$ frame instead of on the true $E_\gamma$ in the $B$ rest frame. For a given signal model, Monte Carlo simulation provides the total shift $\Delta_{total}$ needed to obtain the first moment $\langle E_\gamma \rangle$ from the measured first moment $\langle E_\gamma^* \rangle$ for the same numerical cut value; likewise for the second moment.

Tables 5 and 6 show the observed and corrected first and second moment values for four different minimum photon energy cuts. Using 50 MeV bins instead of 100 MeV bins changes the first moment by less than 0.003 GeV (0.001 GeV) and the second moment by less than 0.001 GeV$^2$ (0.0004 GeV$^2$) for the 1.9 GeV cut (other cuts). The dominant systematic uncertainty arises from the $B\overline{B}$ background subtraction. In addition the uncertainty in the photon energy scale and the modeling of photon energy resolution cause smaller systematic errors in the first and second moments, respectively. The model-dependent uncertainty on the first moment is based on redoing the computation using the efficiency for each KN or BBU model that matches the nominal first moment within its uncertainties. The second moment is sensitive to the modeling of the low-energy tail of the photon energy resolution but not to the efficiency model or to the uncertainty in the photon en-
Table 5: Measured first moments (preliminary) for various energy ranges, then corrected for resolution smearing and for cutting on the $B$ rest frame $E_\gamma$. The systematic errors have two sources: $B\bar{B}$ background uncertainties, with their full covariance matrix taken into account, and the uncertainty in the photon energy scale. The model-dependence error on $\langle E_\gamma^2 \rangle$ is correlated with that on $\Delta_{\text{total}}$, so these are combined linearly for the last column. The $\langle E_\gamma \rangle$ values in that column can be compared to theoretical predictions. Note that $\approx 4\%$ of $B \to X_s \gamma$ is included, but its first moments are not expected to differ significantly from those for $B \to X_s \gamma$.

| $E$ range GeV | $\langle E_\gamma^2 \rangle + (\text{stat}) + (\text{sys}) + (\text{model})$ GeV (with cut on $E_\gamma^2$) | $\Delta_{\text{total}}$ GeV | $\langle E_\gamma \rangle + (\text{stat}) + (\text{sys}) + (\text{model})$ GeV (with cut on $E_\gamma$) |
|---------------|-------------------------------------------------|-----------------|-------------------------------------------------|
| 1.9 to 2.7    | $2.270 \pm 0.025 \pm 0.017 \pm 0.005$          | $0.018 \pm 0.007$ | $2.288 \pm 0.025 \pm 0.017 \pm 0.012$          |
| 2.0 to 2.7    | $2.304 \pm 0.016 \pm 0.010 \pm 0.005$          | $0.012 \pm 0.007$ | $2.316 \pm 0.016 \pm 0.010 \pm 0.012$          |
| 2.1 to 2.7    | $2.350 \pm 0.014 \pm 0.007 \pm 0.003$          | $0.005 \pm 0.007$ | $2.355 \pm 0.014 \pm 0.007 \pm 0.010$          |
| 2.2 to 2.7    | $2.412 \pm 0.012 \pm 0.005 \pm 0.002$          | $-0.005 \pm 0.006$ | $2.407 \pm 0.012 \pm 0.005 \pm 0.008$          |

Table 6: Measured second moments (preliminary) for various energy ranges, then corrected for resolution smearing and for cutting on the $B$ rest frame $E_\gamma$. The errors listed with $\Delta_{\text{total}}$ represent model-dependence. The systematic errors have two sources: $B\bar{B}$ background uncertainties, with their full covariance matrix taken into account, and (after the correction) the uncertainty in the modeling of the photon energy resolution. The final corrected value for an $E_\gamma$ cut can be compared to theoretical predictions.

| $E$ range GeV | $\langle E_\gamma^2 \rangle - \langle E_\gamma \rangle^2 \pm \text{stat} \pm \text{sys}$ GeV$^2$ (with cut on $E_\gamma^2$) | $\Delta_{\text{total}}$ GeV$^2$ | $\langle E_\gamma^2 \rangle - \langle E_\gamma \rangle^2 \pm \text{stat} \pm \text{sys} \pm \text{model}$ GeV$^2$ (with cut on $E_\gamma$) |
|---------------|-------------------------------------------------|-----------------|-------------------------------------------------|
| 1.9 to 2.7    | $0.0403 \pm 0.0049 \pm 0.0022$                  | $-0.0075 \pm 0.0025$ | $0.0328 \pm 0.0049 \pm 0.0023 \pm 0.0025$      |
| 2.0 to 2.7    | $0.0326 \pm 0.0026 \pm 0.0009$                  | $-0.0060 \pm 0.0020$ | $0.0266 \pm 0.0026 \pm 0.0010 \pm 0.0020$      |
| 2.1 to 2.7    | $0.0246 \pm 0.0019 \pm 0.0005$                  | $-0.0055 \pm 0.0015$ | $0.0191 \pm 0.0019 \pm 0.0006 \pm 0.0015$      |
| 2.2 to 2.7    | $0.0161 \pm 0.0014 \pm 0.0003$                  | $-0.0045 \pm 0.0005$ | $0.0116 \pm 0.0014 \pm 0.0004 \pm 0.0005$      |

Energy scale. A systematic uncertainty for the photon energy resolution is determined by comparing the asymmetric photon resolution function measured using a sample of events from virtual Compton scattering (in which the true photon energy can be determined by a kinematic constraint) with the corresponding function for simulated events. The uncertainty varies from 0.0005 GeV$^2$ for $E_\gamma^2 > 1.9$ GeV to 0.0002 GeV$^2$ for $E_\gamma^2 > 2.2$ GeV and is added in quadrature to the systematic uncertainty arising from the $B\bar{B}$ background systematic. We compute the corrections applied to the moments for the full range of KN and BBU models considered, in order to better represent possible model-dependence. The tabulated $\Delta_{\text{total}}$ is the average value of the maximum and minimum corrections for these models, and its uncertainty is taken to be half the value of the difference between the maximum and minimum. The model-dependent uncertainties on $\langle E_\gamma^2 \rangle$ and $\Delta_{\text{total}}$ are correlated, and hence added linearly.

Finally Tables 7 through 9 show the full correlation matrices between the eight measured moments for statistical, systematic, and model dependence errors, respectively. Statistical and systematic covariance matrices are computed using standard error propagation, starting from the measured spectrum in energy bins. For systematics, this incorporates the bin-to-bin covariance matrix that arises from the $B\bar{B}$ subtraction, with the fully-correlated covariance matrices arising from the energy-scale uncertainty (first moments only) and calorimeter resolution (second moments.
only) added at the end.

The model correlations take into account the variation of both the efficiency and the $\Delta_{total}$ corrections among different models. For each of the models (indexed $k$) and each of the eight measured first and second moments $M_j$ for $j=1,8$ we define $\Delta_k^{res/cut}(M_j)$ as the actual correction for that model. We also define $\Delta_k^{eff}(M_j)$ as the computed value of the first or second moment using a particular model minus its value using efficiencies from the nominal KN460 model. Letting

$$\Delta_k^{total}(M_j) \equiv \Delta_k^{cut/res}(M_j) + \Delta_k^{eff}(M_j),$$

we compute the covariance of $\Delta_k^{total}(M_j)$ between each pair of moments by averaging over the models, and then derive the correlation matrix. Note that this approach, which treats the predictions of the different models as a statistical distribution, would yield smaller model-dependence errors than the ones we quote in Tables 5 and 6; but we use this result solely for the correlation matrix, not for the errors themselves.

| Quantity | Min. $E_\gamma$ | 1.9 | 2.0 | 2.1 | 2.2 | 1.9 | 2.0 | 2.1 | 2.2 |
|----------|-----------------|-----|-----|-----|-----|-----|-----|-----|-----|
| Mean 1.9 GeV | 1.0000 | 0.5172 | 0.3548 | 0.2265 | -0.6110 | 0.0077 | 0.0821 | 0.1008 |
| Mean 2.0 GeV | 1.0000 | 0.6838 | 0.4326 | 0.2285 | -0.0008 | 0.1375 | 0.1645 |
| Mean 2.1 GeV | 1.0000 | 0.6260 | 0.4220 | 0.5660 | 0.1650 | 0.1884 |
| Mean 2.2 GeV | 1.0000 | 0.4528 | 0.7568 | 0.7383 | 0.2113 |
| Variance 1.9 GeV | 1.0000 | 0.4626 | 0.3486 | 0.2520 |
| Variance 2.0 GeV | 1.0000 | 0.6966 | 0.4887 |
| Variance 2.1 GeV | 1.0000 | 0.6709 |
| Variance 2.2 GeV | 1.0000 |

Table 7: Correlation matrix (preliminary) for statistical errors on the truncated first and second moments (four each, for different minimum $E_\gamma$ cuts). This matrix is symmetric, so redundant entries are not shown. Column labels are shorthand for the identical row labels.

| Quantity | Min. $E_\gamma$ | 1.9 | 2.0 | 2.1 | 2.2 | 1.9 | 2.0 | 2.1 | 2.2 |
|----------|-----------------|-----|-----|-----|-----|-----|-----|-----|-----|
| Mean 1.9 GeV | 1.0000 | 0.7841 | 0.6076 | 0.4622 | -0.7552 | -0.3862 | -0.1723 | -0.0942 |
| Mean 2.0 GeV | 1.0000 | 0.8007 | 0.6311 | -0.2515 | -0.4753 | -0.2298 | -0.1451 |
| Mean 2.1 GeV | 1.0000 | 0.7886 | 0.0320 | 0.0202 | -0.2903 | -0.2115 |
| Mean 2.2 GeV | 1.0000 | 0.0489 | 0.1850 | 0.2061 |
| Variance 1.9 GeV | 1.0000 | 0.4473 | 0.2219 | 0.1436 |
| Variance 2.0 GeV | 1.0000 | 0.5003 | 0.3342 |
| Variance 2.1 GeV | 1.0000 | 0.6592 |
| Variance 2.2 GeV | 1.0000 |

Table 8: Correlation matrix (preliminary) for systematic errors on the truncated first and second moments (four each, for different minimum $E_\gamma$ cuts). This matrix is symmetric, so redundant entries are not shown. Column labels are shorthand for the identical row labels. Systematic uncertainties included are those on the $B\bar{B}$ subtraction, the energy scale (first moments only) and calorimeter resolution (second moments only).
Table 9: Correlation matrix (preliminary) for model-dependent errors on the truncated first and second moments (four each, for different minimum $E_\gamma$ cuts). This matrix is symmetric, so redundant entries are not shown. Column labels are shorthand for the identical row labels. Uncertainties are included for the model-dependence of the signal efficiency and of the correction for resolution, Lorentz boost and cutoff. Sixteen models are averaged, as described in the text.

| Quantity | Min. $E_\gamma$ | M | M | M | V | V | V | V |
|----------|----------------|---|---|---|---|---|---|---|
| Mean 1.9 GeV | 1.0000 | 0.9267 | 0.9486 | 0.8252 | -0.9057 | -0.9223 | -0.9234 | -0.7983 |
| Mean 2.0 GeV | 1.0000 | 0.9576 | 0.8669 | -0.7452 | -0.8183 | -0.8087 | -0.8960 |
| Mean 2.1 GeV | 1.0000 | 0.9540 | -0.7390 | -0.7889 | -0.7843 | -0.7752 |
| Mean 2.2 GeV | 1.0000 | -0.5378 | -0.5857 | -0.5788 | -0.6023 |
| Variance 1.9 GeV | 1.0000 | 0.9650 | 0.9824 | 0.6983 |
| Variance 2.0 GeV | 1.0000 | 0.9810 | 0.8035 |
| Variance 2.1 GeV | 1.0000 | 0.8057 |
| Variance 2.2 GeV | 1.0000 |

The correlation matrices allow a fit of the moments to any parameterized theoretical calculation. However we note that of the eight moments only five are independent. One way to see this is by considering that there are two moments for the highest energy cut ($E_\gamma^* > 2.2$ GeV) and all the other moments can be derived by adding the three lower energy bins. Thus in fitting one must choose no more than five of the moments and check that the associated covariance matrices are positive definite.

5.3 CP Asymmetry

Within the Standard Model the combined direct $CP$ asymmetry for $b \to s\gamma$ and $b \to d\gamma$ decays,

$$A_{CP} = \frac{\Gamma(b \to s\gamma + b \to d\gamma) - \Gamma(\bar{b} \to \bar{s}\gamma + \bar{b} \to \bar{d}\gamma)}{\Gamma(b \to s\gamma + b \to d\gamma) + \Gamma(\bar{b} \to \bar{s}\gamma + \bar{b} \to \bar{d}\gamma)},$$

is zero to a very good approximation [19]. New physics models with additional flavour violation can significantly enhance $A_{CP}$ to a few percent [11]. Furthermore, measurements of the combined $A_{CP}$ in $b \to s\gamma$ and $b \to d\gamma$ processes complement those of $A_{CP}$ in only $b \to s\gamma$ [20, 16, 21] to constrain new physics models.

The use of lepton tagging on the non-signal $B$ for continuum suppression allows a straightforward determination of $A_{CP}$. The lepton’s positive (negative) charge tags the signal side to contain a $b$ ($\bar{b}$) quark. Therefore

$$A_{CP} = \frac{N^+ - N^-}{N^+ + N^-} \frac{1}{1 - 2\omega},$$

where $N^+$ ($N^-$) are the positive (negative) tagged signal yields and $1/(1 - 2\omega)$ is the dilution factor due to the mistag rate, $\omega$.

The systematic uncertainty on the $B\bar{B}$ background subtraction only contributes a multiplicative uncertainty to the measured $A_{CP}$. Therefore, the statistical uncertainty dominates and we find the optimal $E_\gamma^*$ range for the $A_{CP}$ measurement to be $2.2 < E_\gamma^* < 2.7$ GeV. The tagged signal yields are $N^+ = 349 \pm 48$ and $N^- = 409 \pm 45$ where the uncertainties are statistical. We use control samples
of $e^+e^- \rightarrow X\gamma$ and $B \rightarrow X\pi^0, \eta$ to estimate the bias on $A_{CP}$ from any charge asymmetry in the detector or in the $B\bar{B}$ background. The bias is $-0.005 \pm 0.013$, which is applied to the measured asymmetry. The uncertainty on the measurement of the bias is taken as an additive systematic uncertainty on the measured asymmetry. The measured asymmetry, uncorrected for dilution, is $-0.084 \pm 0.088 \pm 0.013$, where the first uncertainty is statistical and the second systematic.

The mistag rate is $(11.9 \pm 0.4)\%$. It is dominated by mixing in $B^0\bar{B}^0$ events, which when averaged over $B^0\bar{B}^0$ and $B^+B^-$ events is equal to half the time-averaged mixing rate $\chi_d/2 = (9.3 \pm 0.2)\%$. The remaining $(2.6 \pm 0.3)\%$ is estimated from simulation; these mistags are due to leptons from $D$ decay, $\pi^\pm$ faking $\mu^\pm, \gamma$ conversions, $\pi^0$ Dalitz decay, and charmonium decay. The error is dominated by uncertainties in the modeling of $D$ decay and fakes. The dilution factor of $1/(1-2\omega) = 1.31 \pm 0.01$ scales the measured $A_{CP}$ and its additive uncertainties to give

$$A_{CP} = -0.110 \pm 0.115(\text{stat.}) \pm 0.017(\text{syst.}) .$$

The systematic uncertainty includes a 5.4\% multiplicative uncertainty from the $B\bar{B}$ background subtraction and 1.0\% multiplicative uncertainty from the dilution factor. We have estimated that any model dependent uncertainty, due to differences in the $B \rightarrow X_s\gamma$ and $B \rightarrow X_d\gamma$ spectra, is much smaller than the systematic uncertainty.

6 Conclusions

We have performed a lepton-tagged fully-inclusive measurement of $B \rightarrow X_s\gamma$ decays. We present a reconstructed photon energy spectrum in the $\Upsilon(4S)$ frame, and partial branching fractions above minimum reconstructed energies of 1.9, 2.0, 2.1 and 2.2 GeV (Table 4). We also present the partial branching fractions, the first and second moments of the true photon energy distribution in the $B$ rest frame and the correlations between the first and second moments, above the same minimum photon energies (tables 4, 5, 6, 7, 8 and 9). Finally, we have used the charge of the tagging leptons to obtain the $CP$ asymmetry of the sum of $B \rightarrow X_s\gamma$ plus $B \rightarrow X_d\gamma$ with reconstructed photon energy above 2.2 GeV.

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We present preliminary results from a lepton-tagged fully-inclusive measurement of $B \to X_s \gamma$ decays, where $X_s$ is any strange hadronic state. Results are based on a BaBar data set of 88.5 million $B \overline{B}$ pairs at the $\Upsilon(4S)$ resonance. We present a reconstructed photon energy spectrum in the $\Upsilon(4S)$ frame, and partial branching fractions above minimum reconstructed photon energies of 1.9, 2.0, 2.1 and 2.2 GeV. We then convert these to measurements of partial branching fractions and truncated first and second moments of the true photon energy distribution in the B rest frame, above the same minimum photon energy values. The full correlation matrices between the first and second moments are included to allow fitting to any parameterized theoretical calculation. We also measure the direct CP asymmetry $A_{\text{cp}}(B \to X_{s+d} \gamma)$ (based on the charge of the tagging lepton) above a reconstructed photon energy of 2.2 GeV.