Correlation in transport coefficients of hole-doped CuRhO$_2$ single crystals

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To clarify the origin of the nontrivial thermoelectric properties observed in the delafossite oxide CuRhO$_2$ polycrystals, we have performed the systematic transport measurements on the single-crystalline CuRhO$_2$ samples. In the parent compound, we find a pronounced peak structure due to a phonon-drag effect in the temperature dependence of the Seebeck coefficient, which is also confirmed by the size effect experiments. In the Mg-substituted crystals, in contrast to the results of the polycrystals, both the resistivity and the Seebeck coefficient decrease with increasing Mg content $y$. In particular, the coefficient $A$ for the $T^2$ term of the resistivity and the $T$-linear coefficient for the Seebeck coefficient at low temperatures are well described within a simple relationship expected for metals, which is also applicable to the correlated materials with low carrier densities.

I. INTRODUCTION

The search for the guiding principles toward the efficient thermoelectric materials is of great importance both in fundamental and applied physics. The oxides have attracted a keen attention as a key class of thermoelectric materials with certain merit of their high stability at high temperature in air [1–4]. In particular, since the discovery of the good thermoelectric properties in Na$_x$CoO$_2$ [5], various cobalt oxides are investigated, and interesting mechanisms to enhance the Seebeck coefficient, $S$, including the spin-orbital entropy of correlated $d$ electrons [6,7] and the peculiar shape of the electronic band structure [8], are proposed and examined.

The rhodium oxides are the isovalent 4$d$ counterpart for the cobalt oxides, essential to the thorough understanding of the origin of the thermoelectric transport properties in this system [9–13]. In this respect, the delafossite CuRhO$_2$ is a suitable material [14–22], since the two-dimensional (2D) RhO$_6$ layer is consisting of the edge-shared RhO$_6$ octahedra to form a triangular lattice as is similar to the 2D triangular lattice of Co ions in Na$_x$CoO$_2$. The parent compound is insulating and becomes conducting with the hole doping by the Mg$^{2+}$ substitution to the Rh sites. Indeed, polycrystalline CuRh$_{0.6}$Mg$_{0.4}$O$_2$ exhibits a large Seebeck coefficient with a metallic resistivity [18,19], which may originate from a “pudding mold” type band structure suggested by Usui et al. [23], as is similar to the case of Na$_x$CoO$_2$. Although there exists a contribution of the Cu layer [20], combined spectroscopic experiments have shown that the Rh 4$d$ electron is dominant for the conduction phenomena [21], as is similar to other hole-doped delafossite compounds [24].

The low-temperature transport nature of CuRh$_{1-y}$Mg$_y$O$_2$ is, on the other hand, still controversial: while the resistivity certainly varies from insulating to conducting behavior with the hole doping, the temperature variations of the Seebeck coefficient for $0 \leq y \leq 0.2$ fall into a single curve below 150 K [17], highly incompatible with the conventional behavior where the Seebeck coefficient decreases in magnitude with increasing carrier density [3]. Since the Seebeck coefficient measures the temperature derivative of the chemical potential, $\partial \mu / \partial T$ [25,26], the $y$-independent Seebeck coefficient indicates that the compressibility, $\partial \rho / \partial \mu$ ( $\rho$ being the carrier density), is divergently large [17]. This implies an occurrence of a phase separation, in which a percolation network for the doped holes is away from the substituted Mg ions. Thus it represents an intriguing doping effect to be further addressed where the substituted ions act as the carrier donors/acceptors with weak scattering, although the earlier studies are performed by using polycrystalline samples.

The aim of this paper is to clarify the low-temperature thermoelectric properties of CuRh$_{1-y}$Mg$_y$O$_2$ by using single-crystalline samples. We find that the parent compound shows a peak structure in the temperature dependence of the Seebeck coefficient at around 120 K. We also observe a size effect of the peak structure, indicating an existence of the phonon-drag effect. In the Mg-substituted crystals, the Seebeck coefficient systematically varies with the hole doping unlike the polycrystalline data. Moreover, we show that the relation between the $T$-linear coefficient for the Seebeck coefficient, $S/T$, and the coefficient $A$ for the $T^2$ term in the Fermi-liquid resistivity is described within a simple model for metals. In contrast to other universal relations, such as the Kadowaki-Woods ratio $A/\gamma^2$ ($\gamma$ being the electronic specific heat coefficient) [27] and $S/T$ ratio suggested by Behnia et al. [28], the present relation among the transport coefficients is widely applicable to the correlated materials even with low carrier density.

II. EXPERIMENTS

The experiments were performed using CuRh$_{1-y}$Mg$_y$O$_2$ single crystals ($y = 0, 0.03, 0.06, 0.1$). Powders of Rh$_2$O$_3$ (99.9%), MgO (99.99%), and CuO (99.9%) were mixed in a stoichiometric ratio and calcined in air at 1203 K for 36 h. The powders were then ground and calcined again in air at 1203 K for 72 h [17]. The single crystals were then grown by a self-flux method as is similar to the crystal growth of CuAlO$_2$ [29]. CuO (99.9%) powder was added with the calcined powder as a flux. The concentration of CuRh$_{1-y}$Mg$_y$O$_2$ powder was set to be 10% in molar ratio. The mixture was put in a platinum crucible and heated up to 1423 K in air with a heating rate of 200 K/h. After keeping 1423 K for 10 h, it was slowly cooled down with a rate of 0.5 K/h, and at 1323 K, the power of the furnace was switched off. As-grown samples were rinsed in 1 M HNO$_3$ to remove the flux, and then annealed at 673 K for 20 h in air to obtain the homogeneous samples. Typical crystal dimension was $1 \times 0.3 \times 0.01$ mm$^3$

X-ray diffraction (XRD) measurements were performed at...
FIG. 1. X-ray diffraction patterns of (a) CuRh₁₋ₓMgₓO₂ powders and (b) single-crystalline samples. The powders are obtained by grinding the single crystals. The vertical bars show the Bragg positions. (c) The a-axis (left) and the c-axis (right) length as a function of the Mg content y.

room temperature by using an x-ray diffractometer (Rigaku UltimaIV) with Cu Kα radiation in a θ-2θ scan mode. For the powder XRD experiments, we ground the single crystals grown by the self-flux method. In the case of the single-crystalline experiments, the scattering vector was normal to the surface of the sample. The in-plane resistivity was measured with a conventional dc four-probe method. The excitation current of I = 20 μA was provided by a Keithley 6221 current source and the sample voltage was measured with a synchronized Keithley 2182 nanovoltmeter. These two instruments were operated in a built-in Delta mode to cancel unwanted thermoelectric voltage. The Seebeck coefficient was measured by using a steady-state method with a typical temperature gradient of 0.5 K/mm made by a resistive heater. The thermoelectric voltage of the sample was measured with Keithley 2182A nanovoltmeter. The temperature gradient was measured with a differential thermocouple made of copper and constantan in a liquid He cryostat. The thermoelectric voltage from the wire leads was subtracted.

III. RESULTS AND DISCUSSION

A. Structural and transport properties

Figures 1(a) and 1(b) represent the x-ray diffraction patterns of CuRh₁₋ₓMgₓO₂ powders and single-crystalline samples, respectively. No impurity phase is detected in the powder data, and only (00l) reflections are observed in the single-crystalline samples, showing that the measured crystal surface is the ab plane. Figure 1(c) depicts the Mg content y dependence of the lattice parameters. The a-axis length decreases with increasing y, while the c-axis length is almost constant for y, as is consistent with the previous reports [17]. The volume reduction with increasing y is explained by the comparison of the ionic radii for Mg²⁺ (0.72 Å), Rh³⁺ (0.665 Å), and Rh⁴⁺ (0.60 Å) [30]: if we simply express the valence state of CuRh₁₋ₓMgₓO₂ as CuRh⁺ₓRh⁺⁴⁺MgₓO₂ from the charge neutrality, the average ionic radius of the Rh site Ravg is calculated as Ravg = 0.665 × (1 − 2y) + 0.66 × 2y. The reduction of Ravg at y = 0.1 is then calculated as 0.15%. On the other hand, experimental reduction of the a-axis length at y = 0.1 is 0.13%, which well agrees with the theoretical calculation.

Figure 2(a) shows the temperature variations of the in-plane resistivity, ρ(T), for CuRh₁₋₀.₅Mg₀.₅O₂ crystals (0 ≤ y ≤ 0.1). The resistivity systematically decreases with the Mg substitution, indicating the successful hole doping. Figure 2(b) depicts lnρ as a function of T⁻¹ for the parent compound, and the dotted line represents a thermal activation fitting ρ ∝ exp(Δ/2kBT), where Δ = 0.17 eV is the activation energy. Now this value is smaller than the energy gap value of 0.8 eV estimated from the band calculations [19–23], indicating a thermal excitation from the valence band to an ac-
ceptor level. Below 100 K, the resistivity deviates from the activation formula since an impurity band conduction sets in. In the metallic samples for $y \geq 0.06$, as shown in Fig. 2(c), the low-temperature resistivity shows a Fermi-liquid behavior $\rho(T) = \rho_0 + AT^2$ with a small upturn below 20 K, as is similar to the polycrystalline study [19] and to the results of other layered oxides [31–34]. The doping dependence of $A$ will be mentioned later.

The temperature variations of the Seebeck coefficient are displayed in Fig. 3. In sharp contrast to the polycrystalline results [17], the Seebeck coefficient systematically varies with the Mg content $y$. In the parent compound, it exhibits a relatively large value of $S \sim 200 \mu V/K$ at room temperature and shows a peak structure at $T \approx 120$ K. Such a structure may originate from a phonon-drag effect, because it is not resolved in the polycrystalline sample with a considerable phonon scattering effect at the grain boundaries [35]. Also note that the observation of the phonon-drag effect supports the thermal activation transport in the resistivity as mention above, rather than the variable range hopping conduction. For $y \geq 0.03$, the Seebeck coefficient shows a metallic behavior, and the overall temperature dependence of $S$ qualitatively agrees with the theoretical calculations [23]. The low-temperature $T$-linear coefficient decreases with the doping, which will be argued with the results of the resistivity.

**B. Phonon-drag effect**

To discuss the phonon-drag effect in the CuRhO$_2$ crystal in more details, we have examined the size effect on the Seebeck coefficient. It is well known that the phonon-drag contribution to the Seebeck effect can be enhanced by sizing up the crystal owing to the enhancement of the mean free path of the ballistic phonon. Figure 4 represents the temperature variations of the Seebeck coefficient of several CuRhO$_2$ crystals with different dimensions. Here, a mean free path dominated by the crystal boundary scattering, $l_b$, can be estimated by using the sample dimensions as [36]

$$l_b = \left( \frac{1}{4} D x \right)^{1/2} \left\{ 3 x^{1/2} \ln \left( x^{-1} + \left( x^{-2} + 1 \right)^{1/2} \right) + 3 x^{-1/2} \ln \left( x + \left( x^2 + 1 \right)^{1/2} \right) - \left( x + x^3 \right)^{1/2} + x^{3/2} - \left( x^{-1} + x^{-3} \right)^{1/2} + x^{-3/2} \right\},$$

(1)

where $D \times x D$ is the cross section of the crystal with a rectangular shape. As seen in Fig. 4, the peak structure in $S(T)$ is enhanced with increasing $l_b$, implying the phonon-drag effect.

It should be noted that, however, other scattering processes such as the phonon-phonon scattering should be dominant in the present temperature range, in contrast to the phonon-drag effect at low temperature [37]. Let $l_T$ be a temperature-dependent mean free path, which is determined by the other scatterings, and then the phonon mean free path, $l_{ph}$, is generally given as

$$l_{ph}^{-1} = l_T^{-1} + l_b^{-1}.$$  

(2)

Here, $l_T \ll l_b$ holds around $T = 120$ K, since the phonon transport should be diffusive. Now, the phonon-drag contribution to the Seebeck coefficient, $S_{ph}$, is given as [38]

$$S_{ph} = \frac{\beta \nu l_{ph}}{\mu_e T},$$  

(3)

where $\beta$, $\nu$, and $\mu_e$ are an electron-phonon coupling constant ($0 < \beta < 1$), the phonon velocity, and the carrier mobility, respectively. Then the total Seebeck coefficient is approximately expressed as

$$S \approx S_d + \frac{\beta \nu l_T}{\mu_e T} \left( 1 - \frac{l_T}{l_b} \right),$$  

(4)
where $S_d$ is the diffusive term of the Seebeck coefficient. The inset of Fig. 4 depicts the maximum Seebeck coefficient at the peak structure, $S_{\text{peak}}$, as a function of $1/l_b$. According to Eq. 4, the experimental data are roughly fitted by a linear function of $1/l_b$ as shown by the dashed line, supporting the present phonon-drag model.

C. Relation in the transport coefficients

Now let us discuss the doping dependence of the resistivity and the Seebeck coefficient. As shown in Fig. 2(c) and Fig. 5, both the coefficient $A$ for the $T^2$ term of the resistivity and the $T$-linear coefficient for the Seebeck coefficient at low temperatures are reduced with increasing Mg content $y$, which is readily understood with the increase in the carrier density $n$ [99].

Here, let us compare the present results with other systems. It is well known that both $A$ and $S/T$ values are correlated with the electronic specific heat coefficient, $\gamma$, as is represented by Kadowaki-Woods [27] and Behnia plots [28]. Figures 5(a) and 5(b) represent the $A$ vs. $\gamma^2$ and $S/T$ vs. $\gamma$ plots, respectively, for various materials [40–88]. Note that we refer the literature data, but the analysis for the Fermi-liquid behavior is a remaining issue [89, 90]. Here, although the Kadowaki-Woods plot can be corrected by involving the degeneracies [91–93], both plots well explain the universal relations among those quantities for the correlated materials with a metallic carrier density. On the other hand, since both $A/\gamma^2$ and $S/\gamma T$ ratios include the carrier density $n$ [28, 94–95], the data of correlated materials with low carrier density, such as a Kondo insulator CeNiSn [50] and slightly doped SrTiO$_3$ [79], significantly deviate from the universal relation in these plots. Note that there are several attempts to correct this deviation due to the carrier density [96, 97].

In Fig. 6, we instead plot $A$ as a function of $(S/T)^2$ for the materials shown in Figs. 5(a) and 5(b), in addition to the present data for CuRh$_1$–MgO$_2$ ($y = 0.06, 0.1$). All the data, including the low-density materials mentioned above, seem to fall into a single line. Now, the $A$ term in the resistivity is expressed as [98, 99]

$$A = \frac{\hbar}{e^2} \left( \frac{k_B}{\epsilon_F} \right)^2 l_{\text{quad}},$$

(5)

where $\hbar$ is the reduced Planck constant, $e$ the elementary charge, and $\epsilon_F$ the Fermi energy. Here $l_{\text{quad}}$ is a characteristic length for the scattering events, which is given as $l_{\text{quad}} = k_F \sigma_{cs}$ ($k_F$ and $\sigma_{cs}$ are the Fermi wavenumber and the collision cross section between two electrons, respectively). On the other hand, in a free-electron model, the Seebeck coefficient divided by temperature is given as

$$\frac{S}{T} = \frac{\pi^2}{2} \frac{k_B}{e} \frac{k_B}{\epsilon_F}.$$  (6)

Therefore, we express the ratio as

$$\frac{A}{(S/T)^2} = \frac{4}{\pi^2} \frac{\hbar}{k_B} l_{\text{quad}},$$

(7)
in which the Fermi energy is cancelled out. The present ratio \( A/(S/T)^2 \) is, in other words, a direct measure for \( l_{\text{quad}} \). This ratio can also be expressed as \((2/3\pi^2)(l_{\text{quad}}/G_{\text{en}})\), using the thermal conductance quantum, \( G_{\text{th}} \), divided by temperature, \( G_{\text{th}}/T = G_{\text{en}} = (\pi/6)(k_B^2/\hbar) \). Since \( G_{\text{en}} = (G_{\text{th}}/T) \) may be related to an entropy conductance, \( A/(S/T)^2 \approx l_{\text{quad}}/G_{\text{en}} \) may imply a resistivity for an entropy flow, in analogy to the Fermi-liquid resistivity \( A^2 \approx (l_{\text{quad}}/G_{\text{th}})(k_B^2T/\varepsilon_F)^2 \) \((G_{\text{th}} \text{ being the conductance quantum)}\), which expresses a resistivity for the charge flow. Here, in Eq. \( l_{\text{quad}} \) is indeed material-dependent but mostly lies in a narrow range between 1 and 40 nm \([99]\), consistent with the plot shown in Fig. 6, in which various experimental data are on a single line calculated with a constant \( l_{\text{quad}} \) of 4 nm. It is an interesting issue to clarify the origin of the weak material dependence of \( l_{\text{quad}} \) for various compounds with very different size and shape of Fermi surfaces.

Noted that, in the present compound CuRh\(_{1-y}\)Mg\(_2\)O\(_2\), a pudding-mold type band structure is suggested to enhance the charge flow. Here, in Eq. 7, \( l_{\text{quad}} \) conductance quantum, which expresses a resistivity for the Seebeck coefficient \( A \), divided by temperature, which can be described within a simple relationship expected for metals. This relation may also be applicable to the correlated materials with low carrier densities.

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