Realistic modeling of wind and supernovae shocks in star clusters: addressing $^{22}\text{Ne}/^{20}\text{Ne}$ and other problems in Galactic cosmic rays

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ABSTRACT
Cosmic ray (CR) sources leave signatures in the isotopic abundances of CRs. Current models of Galactic CRs that consider supernovae (SNe) shocks as the main sites of particle acceleration cannot satisfactorily explain the higher $^{22}\text{Ne}/^{20}\text{Ne}$ ratio in CRs compared to the interstellar medium. Although stellar winds from massive stars have been invoked, their contribution relative to SNe ejecta has been taken as a free parameter. Here we present a theoretical calculation of the relative contributions of wind termination shocks (WTSs) and SNe shocks in superbubbles, based on the hydrodynamics of winds in clusters, the standard stellar mass function, and stellar evolution theory. We find that the contribution of WTSs towards the total CR production is at least $25\%$, which rises to $\gtrsim 50\%$ for young ($\lesssim 10$ Myr) clusters, and explains the observed $^{22}\text{Ne}/^{20}\text{Ne}$ ratio. We argue that since the progenitors of apparently isolated supernovae remnants (SNRs) are born in massive star clusters, both WTSs and SNe shocks can be integrated into a combined scenario of CRs being accelerated in massive clusters. This scenario is consistent with the observed ratio of SNRs to $\gamma$-ray bright ($L_\gamma \gtrsim 10^{35}$ erg s$^{-1}$) star clusters, as predicted by star cluster mass function. Moreover, WTSs can accelerate CRs to PeV energies, and solve other longstanding problems of the standard supernova paradigm of CR acceleration.

Key words: shock waves – ISM: bubbles – cosmic rays – hydrodynamics – methods:numerical – galaxies: star clusters: general

1 INTRODUCTION
CRs have been thought to be mostly accelerated by SNe through shocks running into the ISM (Grenier et al. 2015). One of the main arguments for this is the energy requirement of Galactic CRs to maintain a steady CR luminosity. This scenario demands $2 \pm 1$ SNe explosions per century in our Galaxy, given that $\sim 10\%$ of SNe energy goes to CRs (Diehl et al. 2006). However, this standard scenario is known to bear several ailing problems (e.g., Gabici et al. 2019) and additional/complementary sources of CRs have been sought in the literature. One such problem concerns the abundance ratios of certain isotopes which are different from solar abundances and yet not secondary products. For example, the observed ratio of $^{22}\text{Ne}$ to $^{20}\text{Ne}$ in Galactic CRs (GCRs) is $5.3 \pm 0.3$ times the solar value (Wiedenbeck & Greiner 1981; Binns et al. 2008), and it cannot be satisfactorily explained by SNe shocks in the ISM.

It has been suggested that this observed anomalous ratio in GCRs can be explained if SN shocks in superbubbles (SBs) played a major role in accelerating CRs because the gas inside a SB is rich in $^{22}\text{Ne}$, ejected in the winds of massive stars (Higdon & Lingenfelter 2003; Binns et al. 2008). This fits in with the mounting evidence of CRs being accelerated in star clusters, as predicted by Cesarsky & Montmerle (1983). A signature of CRs in the form of $\gamma$-radiation has been detected in massive star clusters such as Cyg OB2, which are too young ($\lesssim 3$ Myr) to have had SN (Ackermann et al. 2011). Moreover, $\gamma$-ray luminosities of these clusters is $\sim 0.1\%$ of the wind mechanical power ($L_w$) feeding the cluster (Ackermann et al. 2011; Yang et al. 2018), and there-
fore, it raises the possibility of a significant contribution from young star clusters in CR acceleration, even in the absence of SNe shocks.

However, shifting the arena of CR acceleration from SNe shocks in the ISM to star clusters have not quite yielded a better estimate of the Neon isotope ratio. For this, one needs to estimate the relative contribution of shocks due to stellar winds and SNe shocks towards CR acceleration. This ratio has so far been treated as a free parameter, empirically chosen to fit the observed Neon isotopic ratio (e.g., Murphy et al. 2016) in the absence of a rigorous theoretical calculation. In order to understand observed anomalous \(^{22}\text{Ne}/^{20}\text{Ne}\) in CRs, several empirical models have been proposed (e.g., Higdon & Lienerfelt 2003; Binns et al. 2008; Prantzos 2012). However none of these models have discussed the shock energetics and corresponding source of upstream particles (stellar wind and SNe ejecta), which goes into the acceleration process. It has also been pointed out that the \(^{22}\text{Ne}\) yield used in previous studies to explain the observed ratio from SB scenario is likely an overestimate (Prantzos 2012).

As an alternative scenario, some studies proposed CR acceleration by SNe shocks in the wind of massive progenitor star. However, these models need some fine tuning, such as the requirement that SN shocks should be effective only when the shock speed \(\geq 1600\) km s\(^{-1}\) (which excludes the possibilities of CR acceleration by SNe shock beyond free-wind region of the progenitor star, for detail see e.g., Prantzos 2012). Therefore, although the basic premise of solving the Neon isotope problem by invoking stellar winds in star clusters seems appealing, detailed estimates have not been available, and in addition, other avenues also appear bleak.

In this paper, we take a fresh look at the Neon isotope problem, using hydrodynamics of winds in star clusters, the latest stellar evolutionary yields (Limongi & Chiuffe 2018), with the standard stellar mass function. Recently using numerical simulations, we have shown that termination shocks of stellar winds from massive stars can accelerate CRs to produce \(\gamma\)-ray luminosity of a similar magnitude, as well as explain the observed X-ray and synchrotron luminosities (Gupta et al. 2018b). In this paper, we investigate the implications of our model to explain Neon isotope ratio. We show that the observed \(^{22}\text{Ne}/^{20}\text{Ne}\) ratio can be achieved if CRs are produced in massive star clusters by the combined effects of WTS and SN shocks. With 1-D numerical simulation we estimate the fraction of shock energy processed in wind and SNe ejecta for various acceleration scenarios. We find that for compact clusters, WTS can accelerate particles from the wind material before the onset of SNe. We also show that, in the case of SN shock in wind of progenitor star (Prantzos 2012), the reverse shock is as efficient as the forward shock, thereby accelerating both wind material and SN ejecta. We demonstrate that in this case both the forward and reverse shocks are energetically comparable. Therefore the acceleration of the ejecta material (rich in \(^{20}\text{Ne}\)) cannot be neglected as is usually done in the literature, and this poses a problem for the \(^{22}\text{Ne}/^{20}\text{Ne}\) abundance ratio.

The implications of this calculation goes beyond the Neon isotope problem. We show that our results imply more than a quarter of the Galactic CRs being accelerated in WTSs of star clusters. The extent of the shocked wind region also allows us to draw important conclusions about the maximum energy of accelerated CRs. We further argue that SNRs and stellar winds in clusters are both linked to massive stars, and therefore the two sites of CR acceleration, namely, WTS and SNe shocks may be put together on a common platform, of CR acceleration in SBs. Isolated SNe remnants would merely represent the lower end of the star cluster mass function, where OB stars number less than two. These lines of argument paint an integrated scenario of CR acceleration that not only solves Neon isotope and other problems, but also rids the standard paradigm of acceleration in SNRs of its generic problems.

The paper is structured as follows. We first characterise and discuss the WTS in §2. The numerical set-up is described in §3. In §4, we present our main results on the relative contribution of WTS and SNe shocks and estimate the Neon isotope ratio. In §5, we draw attention to a few important implications of our calculations for Galactic CRs. Our findings are summarized in section §6.

## 2 WIND TERMINATION SHOCK (WTS)

### 2.1 Formation of the WTSs

Consider a star cluster in which the massive stars (\(M_\ast > 8\) \(M_\odot\)) are mostly located within a radius \(R_c\). The total mechanical power launched by massive stars from this spherical region of radius \(R_c\) can be written as \(L_w = M_c^2/2\), where \(L_w\) is the wind velocity and \(M_c\) is the total out-flowing wind mass per unit time. Interaction of the collective wind with the parent cloud forms an interstellar bubble. Near the core of this bubble, the wind expands adiabatically and its mass density is \(\rho_w = M/(4\pi v_w^2 r_c)\). A WTS forms at the location where the wind ram pressure \(P_{\text{ram}} = \rho_w v_w^2\) balances the hot gas pressure \(P_{\text{h}}\) in the bubble. Thus, the radius of the WTS w.r.t. the center of the star cluster is

\[
R_{w} \approx \left( \frac{L_w}{2\pi v_w P_{\text{ram}}} \right)^{1/2}.
\]

This suggests that if a cluster is compact (i.e., \(R_c \ll R_{w}\)) then a WTS can form. We have confirmed this by performing two 3D simulations of star cluster of twelve massive stars (i.e., \(N_{\text{OB}} = 12\)) with two different core radius \(R_c = 0.5\) pc and \(5.0\) pc respectively. The results are shown in Fig. 1 and for numerical set-up, see Appendix A.

Left and right panels of Fig. 1 show density snapshots in the \(z = 0\) plane at 2.9 Myr for compact (left) and loosely bound (right) star clusters. The left panel shows that a compact cluster has formed a coherent WTS as shown by grey points (the shock Mach numbers are shown by grey/black points displayed in the horizontal colour palette). This can be understood as follows.

For this set-up, the total wind power of both clusters is \(L_w \approx N_{\text{OB}} \times 10^{50}\) erg s\(^{-1} \approx 1.2 \times 10^{55}\) erg s\(^{-1}\) and wind velocity is \(v_w = (2L_w/M)^{1/2} \approx 2000\) km s\(^{-1}\). Taking the hot gas pressure \(P_{\text{h}} \approx 10^{-10}\) dyne cm\(^{-2}\) (as observed in SBs, see e.g., Table 7 in Lopez et al. 2014), from Eq. 1 we obtain \(R_{w} = 3.2\) pc. In the left panel, since the stars are distributed in a region smaller than 3.2 pc (see the zoomed-in sub-plot), a WTS has formed\(^1\). In contrast, the right panel shows that the stars are

\[1\] In this calculation, we have assumed that wind mechanical power of each star remains steady. In case of episodic winds, there will
Acceleration of wind vs SNe ejecta in star clusters

2.2 Mach number of WTSs

In the case of compact clusters, the physical properties of the wind (e.g., density, velocity, and pressure profiles) in the region \( r < R_{ts} \) are similar to the model of Chevalier & Clegg (1985). For \( r \geq R_{ts} \), there is a shocked wind region, which is separated from the ambient medium via a contact discontinuity (for details, see Weaver et al. 1977). In order to determine the Mach number of the WTS, we need to know the shock velocity and the upstream wind (free-wind) profile. In the lab frame, the WTS slowly moves outward (see e.g., Eq. 9 in Gupta et al. 2018a), the upstream velocity is the same as the wind velocity. The upstream sound speed can be obtained by using Table 1 in Chevalier & Clegg (1985). This gives the Mach number of WTS as

\[
M = \frac{V_w}{c_s} = \sqrt{0.56 M^{-1/2} L_w^{1/2} (R_{ts}/R_c)^{-2/3}} \approx 2.5 \left( \frac{R_{ts}}{R_c} \right)^{2/3}.
\]

(2)

This implies that a large separation between WTS and the cluster core leads to a large Mach number which increases with time as the termination shock moves out.

For a typical cluster of mass \( 10^5 M_\odot \) (\( N_{OB} \approx 12 \)) Eq. (1) gives \( R_{ts} \approx 3.2 \text{pc} P_{in}^{-1/2} L_w^{1/2}. \) The corresponding Mach number of WTS is

\[
M \approx 6 \left( \frac{R_c}{pc} \right)^{-2/3} \left( \frac{P_{in}}{10^{-10} \text{ dyn cm}^{-2}} \right)^{-1/3} \left( \frac{L_w}{10^{37} \text{ erg s}^{-1}} \right)^{1/3}.
\]

(3)

This suggests that compact clusters can have high Mach number WTS. In contrast, the outer shock Mach number is small as seen in Fig. 1.

Although these calculations refer to star clusters, Eq. (3) is also valid for the wind from a single star. In this case, \( R_c \) can be taken as the radius beyond which the wind becomes supersonic. This scenario is also applicable for bigger star clusters (i.e., core radius \( > R_{ts} \)) in which a global WTS may not form (as shown in the right panel of Fig. 1). In this case, individual stars can accelerate CRs in their WTS. We discuss these cases separately in section 4.1.4.

3 NUMERICAL SET-UP

The central result of the present work is to compare the energy efficiency in accelerating wind material, SNe ejecta, and ambient matter by the WTS and SNe shocks. For this purpose, we need to quantify the fraction of upstream energy that is encountered by wind material, SNe ejecta, and ambient matter. In order to estimate the energy processed at different shocks, we consider four different acceleration scenarios, which can be broadly classified into two categories: (1) isolated SN (sections 4.1.1 and 4.1.2) and (2) star cluster (sections 4.1.4 and 4.1.3). In the first case, SN shock expands

Figure 1. Various diagnostics from 3D star cluster simulations for a compact (left) and a loosely-bound cluster (right). Snapshots of density (top colour palette) and shock Mach numbers (bottom colour palette) in the \( z = 0 \) plane at 2.9 Myr are shown. Sub-plots show the zoomed-in view of the central few pc of the star cluster where magenta circles denote the locations of the stars after projecting them in the \( z = 0 \) plane. Left and right panels show two different simulations that have identical set-up except for the core radius \( R_c \) of the cluster. For both left and right panels, the ambient shocks are weak and appear dark according to the bottom colour palette. The figure shows that a compact star cluster forms a WTS (left panel), and its Mach number is \( \sim 5 \)–\( 10 \), as shown by bright points.

distributed much beyond 3.2 pc, and there is no coherent WTS. We have also confirmed this for the clusters of mass \( \gtrsim 10^5 M_\odot \). Therefore, compact star clusters can form WTS.
either in the parent cloud or in the wind of the progenitor star. In the second case, the star cluster may be compact or loosely bound. We have labeled these four acceleration scenarios as Case I to Case IV (for a brief overview see Fig. 2). For each of these cases, we discuss the energetics of various shocks with the help of 1-D simulations.

We solve the standard Euler equations in 1-D spherical geometry. We use uniformly distributed grids with spatial resolutions $\Delta r = 0.01$ pc for the Case I, II and $\Delta r = 0.04$ pc for the Case III, IV respectively. In order to include the effect of stellar winds/SNe, we consider a spherical region of radius $r_{\text{inj}}$ within which we inject mass and energy uniformly. Depending on the acceleration scenario that we wish to study, $r_{\text{inj}}$ ranges from 0.05 to 15 pc. The SN shock is launched by injecting thermal energy $E_{\text{SN}} = 10^{51}$ erg and mass $M_{\text{ej}} = 10 M_\odot$ in a region of radius 0.05 pc (0.25 pc) for cases I and II (cases III and IV). For cases II, III, and IV, the first SN occurs at $3.5 \times 10^5$ Myr, which corresponds to the main sequence life time of $\sim 100 M_\odot$ star. The cases III and IV represent clusters of mass $10^4 M_\odot$ with two different core radii: 1 pc and 15 pc respectively. For these two cases, the time between two consecutive SN explosions is $\Delta t_{\text{SN}} = \tau_{\text{cluster}} / N_{\text{OB}}$, where $N_{\text{OB}} \approx 109$ and $\tau_{\text{cluster}} \approx 30$ Myr is typical cluster lifetime. For all cases, we assume the initial ambient density $\rho = 10 m_{\text{H}}$ cm$^{-3}$, and pressure $10^{-12}$ dyne cm$^{-2}$. Radiative cooling has been included using a tabulated cooling function (Sutherland & Dopita 1993). We have used three passive scalars to distinguish wind, SN ejecta, and ambient matter. These passive scalars help us to identify the material(s) available in the upstream/downstream region of a shock. This is required to find the energy that goes into different types of material: wind, SN ejecta, and ambient matter.

### 3.1 Shock energetics

Various steps in the analysis are described in sections below.

- **Step 1 - Simulation output**: Directly obtained from our hydro runs.
- **Step 2 - Shock detection**: The following three conditions are used to identify the shocked zones.
  \[ \nabla \cdot \mathbf{v} < 0, \quad \nabla \rho \cdot \Delta r / \rho > \delta_{\text{threshold}}, \quad \text{and} \quad \nabla T \cdot \nabla \rho > 0. \]

Here $\rho$, $p$, and $T$ are the density, pressure and temperature of the fluid. The first condition selects compressed zones. The second condition sets a threshold in pressure jump ($\delta_{\text{threshold}} \approx 0.5$), and the third conditions helps to avoid contact discontinuity. We have confirmed that these conditions robustly identify shocked zones.

- **Step 3 - Identifying upstream/downstream parameters**: For each shocked zone, the program compares density, pressure, and sound speed of 4 to 8 neighbouring zones on both sides.
Figure 3. Four different CR acceleration scenarios: in all panels, blue curve represents density profiles, where time $t = 0$ denotes the epoch of SN explosion. Red and green curves display tracer of wind material and SN ejecta respectively. Four different acceleration scenarios, which are labeled by Case I to Case IV, are described as follows. Case I: explosion of an isolated star in a uniform medium ($t = 0 \Rightarrow t_{\text{dyn}} = 0$), Case II: explosion of an isolated star in wind of the progenitor star ($t = 0 \Rightarrow t_{\text{dyn}} = 3.5$ Myr), Case III: SN explosion in a compact star cluster ($t = 0 \Rightarrow t_{\text{dyn}} = 3.5$ Myr). Case IV: SN explosion in a medium made by a loosely bound star cluster ($t = 0 \Rightarrow t_{\text{dyn}} = 3.5$ Myr).

- Step 4 - Next we determine the following entities.

(i) Density compression ratio: $\rho_2/\rho_1$.
(ii) Pressure jump: $p_2/p_1$
(iii) Upstream sound speed: $c_1 = (\gamma p_1/\rho_1)^{1/2}$, where $\gamma = 5/3$.
(iv) Upstream Mach number: $M_1 = 1/((2\gamma)/\gamma + 1)^{1/2}$
(v) Mass flux: $\dot{m}_m = p_1 v_1 = \rho_1 c_1 M_1 = p_2 v_2$.  
(vi) Energy flux: $\dot{\epsilon}_e = [(5/2)p_2/p_1 + v_2^2/2]\rho_1 v_1 = [(5/2)p_2/p_2 + v_2^2/2]\rho_2 v_2$

Finally, we obtain the total mass/energy flux that crosses the shock surface. This is estimated by multiplying the flux with the shock surface area. In numerical simulations, since the shock surface is made of more than one zone, we have calculated the shock-zone averaged entities by using the following equations:

\[
\hat{m}_T = \frac{\sum_i \dot{m}_m A_i}{\sum_i Z_i}, \quad \hat{\epsilon}_T = \frac{\sum_i \dot{\epsilon}_e A_i}{\sum_i Z_i}
\]

where $i$ denotes the effective shocked zones where the analysis is performed, $A_i = 4\pi r_i^2$ is the shock area, and $\sum_i Z_i$ is the total number of zones in a shock surface (typically $\sum_i Z_i = 4 - 8$). The net flow of mass/energy through the

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**Density (cm$^{-3}$)**

| $t$ (yr) | Density (cm$^{-3}$) |
|----------|---------------------|
| $t = 0.00 \times 10^3$ | 10
| $t = 1.96 \times 10^3$ | 10
| $t = 3.91 \times 10^3$ | 10
| $t = 68.45 \times 10^3$ | 10
| $t = 216.12 \times 10^3$ | 10

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**Energy Flux (m$^{-2}$s$^{-1}$)**

| $t$ (yr) | Energy Flux (m$^{-2}$s$^{-1}$) |
|----------|-------------------------------|
| $t = 0.00 \times 10^3$ | 10
| $t = 1.96 \times 10^3$ | 10
| $t = 3.91 \times 10^3$ | 10
| $t = 68.45 \times 10^3$ | 10
| $t = 216.12 \times 10^3$ | 10

---

**Mass Flux (m$^{-2}$s$^{-1}$)**

| $t$ (yr) | Mass Flux (m$^{-2}$s$^{-1}$) |
|----------|-----------------------------|
| $t = 0.00 \times 10^3$ | 10
| $t = 1.96 \times 10^3$ | 10
| $t = 3.91 \times 10^3$ | 10
| $t = 68.45 \times 10^3$ | 10
| $t = 216.12 \times 10^3$ | 10
shock surface are calculated using

\[ m_{\text{T}} = \int dt \, \dot{m}_{\text{T}}, \quad \text{and} \quad e_{\text{T}} = \int dt \, \dot{e}_{\text{T}}. \]

Note that, the computational domain may contain more than one shock surface encountered by the same material at different locations. In this case, we have to find zone averaged entities for each shock surface separately (e.g., \( \Sigma_{\text{shock}} \dot{m}_{\text{T}} \)). In order to do this, we define a critical distance \( r_{\text{cri}} = 8 \Delta r \) (i.e., the length of shock analysis domain), to specify the minimum distance between two shock surfaces. When the separation between two neighbouring shocked zones is smaller than \( r_{\text{cri}} \), they are considered as the part of the same shock surface.

4 RESULTS

The results of our shock analysis program for the cases I, II, III, and IV are discussed below. For a brief overview of different cases, see Fig. 2.

Fig. 3 shows the density profiles at five different epoch for four different cases. Panel I shows the classical results of SN in a uniform medium (Case I). The magenta dots show the position of forward and reverse shocks of the blast wave. The red curves show that the SN ejecta reaches up to the contact discontinuity (hereafter, CD). For Case II, the first panel shows the density profile just before the SN, where position of the WTS is marked by an arrow. The green curves show that wind material reaches up to the CD. When the SN shock reaches WTS and collides with it, the WTS disappears. In contrast, in Case III, the WTS appears again due to the winds from remaining stars. For Case IV, although we see shocked zones at WTS, it is weak compared to that of case III because the separation between WTS and core radius is small (see e.g., Eq. 2). Note that, in the rightmost panel of Case I, II (\( t = 216.12 \times 10^3 \) yr), the interior of the bubble contains SN ejecta. In contrast, in the Case III and Case IV, SN ejecta is accumulated near the swept up ISM (shell) and the interior of the bubble is filled with wind material.

4.1 Shock energetics

We have described each of these cases in detail in the following sections. Note that, each section contains two figures. The first figure shows zoomed-in shock profiles (i.e., Figs. 4, 6, 8, and 10), where the blue curves stand for density and yellow curves for pressure. The second figure in each section shows the time evolution of mass/energy of the material that is swept up by the shock (i.e., Figs. 5, 7, 9, and 11), where green/cyan stands for wind material, red/light-red denotes SN ejecta and dark-blue/light-steel-blue stands for ambient matter.

4.1.1 Case - I: SN in a uniform medium

For a SN in a uniform medium, we have used the blast wave solution (e.g., Truelove & McKee 1999) to check our analysis program. For our set-up (i.e., \( E_{\text{SN}} = 10^{51} \) erg, \( M_{\text{ej}} = 10 M_{\odot} \), and \( \rho = 10 n_{\odot} \text{cm}^{-3} \)), at \( t = 1.96 \times 10^3 \text{yr} \), \( R = 4.2 \text{ pc} \) and \( \dot{R} \approx 840 \text{ km s}^{-1} \). Therefore, we expect the shock Mach number \( M_{\text{sh}} \approx 840/3 \approx 280 \), pressure jump \( p_2/p_1 = (5/4) M_{\text{sh}}^2 \approx 10^5 \), and compression ratio \( p_2/p_1 \approx 4 \). Our shock analysis program confirms this, as shown in Fig. 4.
Figure 5. Various diagnostics from an isolated SN simulation (Case I). Left panels display the net mass/energy that passes through the shock surface per unit time. Right panels display the time integrated entities corresponding to the left panels. In the bottom right panel, the vertical axis is normalized w.r.t. the input energy (i.e., $E_{in} = 10^{51}$ erg). Sky-blue solid curves display analytic predictions (representing forward shock), and blue (ambient)/red (SN ejecta) curves show the results from our analysis. Top right panel shows that the mass swept-up by the reverse shock is equal to ejecta mass $M_{ej} = 10 M_{\odot}$ as expected. Right bottom panel shows that the reverse shock is energetically sub-dominant compared to the forward (ambient) shock of the blast wave. In this case, acceleration of the ambient matter is energetically dominant, with only 5% of the total shock energy processed by the SN ejecta. Note that, the energy swept up in the ambient medium is larger than unity because our calculation does not include the loss of upstream energy due to deceleration of the shell (see e.g., Eq. 5 in Dermer & Powale 2013).

Fig. 4 shows the zoomed-in density (sky-blue) and pressure (yellow) profiles of a blast wave near the reverse shock (left) and the forward shock (right). The magenta points show the shocked zones. Two background colours, i.e., light-red and light-steel-blue, represent the tracers of SN ejecta and ambient matter respectively. In the left panel, the transition between these two colours represent the location of the contact discontinuity.

Top/bottom panels of Fig. 5 show various diagnostics of mass/energy that passes through the shock surfaces calculated using Eqs 7 and 8. Blue and red curves stand for ambient matter and SN ejecta respectively. Sky-blue solid curves represent the analytical predictions. The bottom right panel shows that the reverse shock energy is smaller than the forward shock by a factor of ten. Therefore, the acceleration of SN ejecta is energetically not preferred in this scenario. In this case, the shock energy is mainly encountered by the ambient matter.

4.1.2 Case - II: SN in wind of the progenitor star

In this case, the stellar wind of the progenitor star has been included. Before the SN explosion, interaction of the wind with the ambient medium forms a wind bubble. This wind bubble has four distinct regions: (i) free wind, (ii) wind termination shock, (iii) shocked wind region, and (iv) swept up ambient shell (Weaver et al. 1977). In this case, the WTS can accelerate the wind material even before the SN. When SN occurs, the blast wave moves through these four regions mentioned above. We show the shock profiles in Fig. 6.

In the WTS rest frame the upstream fluid moves with velocity $v_w$, and therefore, the mass and energy flux that pass through the WTS are roughly equal to the stellar wind mass-loss rate (i.e., $M_\ast = M = 8 \times 10^{-7} M_{\odot} \text{yr}^{-1}$) and wind power ($\dot{E}_w = L_w = 10^{36} \text{erg s}^{-1}$), as shown in the left of Fig 7. The shock evolution at different epochs are described below.

- The WTS sweeps up stellar wind material until 3.5 Myr (green curves in the left panel). It also confirms the analytic prediction (yellow curve).
- After SN explosion, the forward shock of the blast wave moves in the free wind region. In this phase, the wind material (green) is swept up by both WTS and SN forward shock.
- This can be seen from the sudden rise in the green curve at 3.5 Myr. However, this phase lasts for a short time, typically $\approx 900$ yr from the epoch of explosion. The Galactic CR acceleration paradigm that considers SN blast wave in the wind of massive stars mostly focuses on this phase (e.g., Prantzos 2002; Biermann & Cassinelli 1993). However, there are phases described below, which are also important and should not be neglected.
- When the SN forward shock reaches the WTS, it collides with WTS and the WTS disappears. At this moment, a reflected shock and a transmitted shock are formed.
Figure 6. Left and right panels display the zoomed-in view of density (blue) and pressure (yellow) profiles near the WTS at two different times separated by a time interval of ≈ 300 yr. The left panel shows a phase when SN shock is propagating in free wind region and the right panel shows just after SN shock hits the WTS. The right axes represent upstream Mach number $M_1$ (red squares), density jump $\rho_2/\rho_1$ (dark-blue circles), and pressure jump $p_2/p_1$ (brown diamond symbols) obtained from the analysis program. The tracer of wind material and SN ejecta are shown by background colours (light-cyan for wind and light-red for SN ejecta as in Fig. 4). Left panel contains three distinct shock surfaces: (starting from left) (a) SN reverse shock (sweeping up SN ejecta), (b) SN forward shock (wind material), (c) wind termination shock (wind material). In this case the wind material encounters two different shock surfaces (i.e., shock - b, c) whereas the SN ejecta encounters a single shock surface (shock - a). As soon as the blast wave forward shock collides with the WTS (i.e., collision between shock b with shock c), the WTS disappears (see the right panel, shock - c is absent). Comparison of Mach numbers (red squares) between left and right panels near the shock (a) shows that the SN reverse shock becomes stronger after the SN forward shock and WTS collide.

Figure 7. Shock diagnostics from an isolated SN in wind of progenitor star (top/bottom panel: mass/energy). Unlike Case-I, in this model, we have included stellar wind until 3.5 Myr when the star has exploded. Left panels shows the zoomed-in view of 3.46–3.56 Myr, during the epoch of SN explosion. They display the net mass/energy that passes through the shocked surface per unit time (i.e., $m_T e_T$ using Eq. 7). Right panels display the time-integrated mass (top) and energy (bottom) i.e., $m_T$ and $e_T$ (using Eq. 8). In the bottom right panel, the vertical axis is normalized w.r.t. the total input energy until that epoch. In all panels, green, red, and blue curves denote wind, SN ejecta, and ambient matter respectively. Yellow/sky-blue solid curves display the expected results from analytic calculation (shown only for WTS and ambient shock).
shocked-wind region where it sweeps up the wind material. During this time, the shock energy processed by the wind material is larger than that by the SN ejecta (in the bottom left panel, the green curve is above the red curve). This phase continues as long as the SN forward shock does not reach the CD of wind bubble (until \( \approx 7500 \) yr from the epoch of the SN explosion).

- When (transmitted) SN forward shock reaches the CD, the wind material accumulates near the CD. Acceleration of wind material stops when the SN shock collides with CD. This occurs after \( \approx 7500 \) yr from the epoch of SN explosion (see green curves in left panels disappear after \( \approx 3.5 \) Myr + 7500 yr).

- The collision between the SN forward shock with shocked ambient medium again forms a transmitted shock and a reflected shock. The transmitted shock moves through the ambient medium. This can be noticed in the left panels where dark-blue curves suddenly appear after 3.5 Myr + 7500 yr.

- The reflected shock and SN reverse shock moves towards the center of the explosion and continues to sweep up the SN ejecta (see the sudden rise in red curves at \( \approx 3.5 \) Myr). They reach the point of explosion at \( \approx 3.5 \times 10^6 + 2 \times 10^4 \) yr and both shocks disappear.

Therefore, in this scenario, the strong shocks remain in bubble for \( \approx 3.5 \times 10^6 + 2 \times 10^4 \) yr, much longer than in an isolated SN. The top right panel shows that the swept up ejecta mass \( \approx 10 M_\odot \) (red), as expected. Comparison of red and green curves in the bottom right panel shows that the shock energy encountered by SN ejecta is larger than the wind/ambient material, a point usually missed in discussions of CR acceleration by SN shocks in massive stellar wind.

4.1.3 Case - III: Compact star clusters

In this case, the stars are close to each other and the wind bubbles of individual stars overlap and generate a collective wind which forms a WTS. This WTS can accelerate the wind material, similar to Case II. When the first SN occurs in the cluster, the forward shock of the blast wave moves outward by sweeping up the wind material. In this case, the free wind is denser than that of a single star (i.e., Case II), and therefore, the forward shock of the blast wave spends a longer time in the free wind region.

The shock profiles at 3.5 Myr + 4 \( \times 10^5 \) yr are shown in Fig. 8. Left and right panels represent the zoomed-in shock profiles near the WTS and ambient shock respectively. The profiles look similar to Fig 6; however, in this case the SN reverse shock (labeled shock - a) also sweeps up the wind of remaining stars. This can be noticed from the background colour in the left panel of Fig. 8 where the mixing between light-red (SN ejecta) and cyan (wind material) has produced a mixed colour (light-grey).

Fig. 9 shows the shock energetics of wind material, SN ejecta, and ambient matter as described below.

- The peak in the green curves at 3.505 Myr represents the epoch of collision between the SN forward shock and WTS. This collision produces a transmitted shock and a reflected shock, similar to Case II. However, unlike Case II, the transmitted shock that moves in the shocked-wind region may not reach the CD of the SB. This is because of the fact that the size of the bubble is bigger than Case II, the SN forward shock becomes subsonic. Therefore, the shocked ISM shell can remain unaffected. This is shown by dark-blue curves in the left panels of Fig 9.

- The SN reverse shock keeps moving toward the center of the bubble. However, due to the winds of remaining stars, it cannot reach the central region. Instead, the winds of other stars push the SN reverse shock outwards. In this phase, the shock energy is equally shared by the wind material and SN ejecta (red curves fall on the top of green curves). This phase ends when the SN ejecta accumulate near the CD of the SB (red curves disappear at \( \approx 3.5 \) Myr + 2.5 \( \times 10^4 \) yr). By this time, the WTS forms again and the acceleration of wind material continues.

- This chain of events repeats as long as the energy deposited by the wind is larger than that of SNe. When the number of SN events in the cluster becomes large, the WTS becomes weak. After that, SNe shocks accelerate both wind material and SNe ejecta.

Right bottom panel of Fig. 9 shows that the fraction of the input energy encountered by the wind material is larger than the SN ejecta by a factor of \( \gtrsim 6 \). Therefore, in this scenario, the acceleration of wind material is energetically dominant.

4.1.4 Case - IV: Loosely bound star clusters

For loosely bound star clusters, a global WTS may not form. However, the individual stars can have their own WTSs. For a detailed investigation, we need to focus on two different length scales: (i) a global length scale (SB; \( \gtrsim 10 \) pc), and (ii) a local length scale that focuses on the individual stars ( \( \lesssim 1 \) pc).

In the global length scale, strong shocks appear only when SNe occur in the cluster. The zoomed-in density profiles near the SN forward/reverse shock and ambient shock are shown in Fig. 10. From the epoch of a given SN explosion, since the blast wave moves in a hot bubble, the shock Mach number is small compared to the case of compact star cluster (Case III). This can be seen by comparing the red squares of Figs. 8 and 10.

The shock energetics are shown in Fig. 11 and described below:

- In the left panels of Fig. 11, green curves are absent until 3.5 Myr because WTS is absent. The wind material gets accelerated (green curves appear after 3.5 Myr) after the first SN.

- The wind material is swept up by both the forward and reverse shocks of the SN blast wave, similar to Case III. In this phase, the shock energy mostly goes into wind material (the green curves are above the red curves until 3.5Myr+5000 yr).

- Since the bubble is made of hot plasma, the SN forward shock disappears before it can reach the CD of the SB. The
Figure 8. The zoomed-in view of density (sky-blue) and pressure (light yellow) profiles of a SB near the WTS (left) and ambient shock (right) respectively at \( t = 3.504 \) Myr (i.e., immediately after the first SN). The used colour codes are identical with Figs 4 and 6. The figure contains four shocked regions: (starting from left) (a) SN reverse shock \((M_1 \approx 7; \text{sweeps up wind + SN})\), (b) SN forward shock \((M_1 \approx 20; \text{sweeps up wind})\), (c) WTS \((M_1 \approx 18; \text{sweeps up wind})\), and (d) ambient shock \((M_1 \approx 5; \text{sweeps up ambient material})\). The figure shows that wind material is swept up at three locations: (a), (b), and (c), whereas the SN ejecta is swept up only at (a). Therefore, in the global energy budget, one can expect the acceleration of SN ejecta to be energetically sub-dominant compared to the wind material.

Figure 9. Shock diagnostics of a compact star cluster (top panel: mass and bottom panel: energy), similar to Figs 5 and 7. In the bottom right panel, comparison of red and green curves (dashed/solid) shows that the net shock energy going into SN ejecta is smaller than that of the wind material by a factor of \( \sim 10 \) at \( \gtrsim 10 \) Myr.
**Figure 10.** The zoomed-in view of density (sky-blue) and pressure (light yellow) profiles of a SB near the SN forward/reverse shocks (left) and ambient shock (right) respectively at $t \approx 3.504$ Myr (the same epoch as in Fig 8). Unlike Case III (Fig. 8), this figure contains only three shock surfaces: (starting from left) (a) SN reverse shock ($M_1 \approx 4$; sweeping up wind+SN), (b) SN forward shock ($M_1 \approx 3$; sweeping up the wind material), and (d) ambient shock ($M_1 \approx 5$; sweeping up ambient matter), i.e., a global WTS (shock - c) is missing. The figure shows that wind material is swept up at the shocks (a) and (b), whereas the SN ejecta is swept up only at (a). Therefore, the shock energy encountered by wind material can be larger than the SN ejecta.

**Figure 11.** Shock diagnostics of a loosely bound star cluster. In this case, the strong shocks appear after the first SN. The description of this figure is similar to Fig. 11. Comparison of red and green curves in the right bottom panel shows that the shock energy going into SN ejecta is smaller than that into wind material by a factor of $\sim 2$. 

$\rho \sim m_H \text{cm}^{-3}$, $p_{th} \sim 10^{-10}$ dyne cm$^{-2}$

$r \sim \text{pc}$

$\rho_{\text{Shocked}}$, $\rho_{\text{Wind}}$, $\rho_{\text{SN}}$, $\rho_{\text{Amb}}$

$M_1$, $\rho_{\text{Wind}}/\rho_{\text{SN}}$, $\rho_{\text{Amb}}/\rho_{\text{SN}}$

$\text{Swept-up mass (M}_\odot\text{s)}$

$\text{Swept-up energy (E}_\text{in}\text{)}$

$t_{\text{dyn}} \sim \text{Myr}$

$\text{Cooling}$

$\text{Wind} > \text{ambient} > \text{SNj}$

$\text{SN explosion}$
SN reverse shock remains active and moves toward the central region of the cluster. The wind of remaining stars push the SN ejecta and accumulate them near the CD of the SB. In this phase, the SN reverse shock energy equally goes to the wind material and SN ejecta (the red curves fall on the top of green curves until \(3.5 \text{ Myr } +4 \times 10^4 \text{ yr}\), similar to Case III.

- When the SN reverse shock completely sweeps up the SN ejecta, the red curves disappear \(3.5 \text{ Myr } +4 \times 10^4 \text{ yr}\). However, the SN reverse shock continues to sweep up the wind material till \(3.5 \text{ Myr } +6 \times 10^4 \text{ yr}\) and then it disappears (green curves disappear).
- The above scenario repeats itself whenever a star explodes in the cluster.

The bottom right panel of Fig. 11 shows that the shock energy going into SN ejecta is smaller than that into wind material by a factor of \(\sim 2\) (unlike the factor of \(\gtrsim 6\) for compact clusters).

There are some additional physical processes at local length scale of a loosely bound star cluster. In this case, a star is located in a hot medium made by the winds of other stars. Here, the ambient gas (inside the hot bubble) is mostly dominated by the wind material. This can be seen from Case IV of Fig. 3, which shows that the interior of the bubble is covered by green curve (a tracer of wind material). In this case, the shock evolution is similar to Case II, although the shock energetics are different. For example, the stellar wind of a star can form a wind bubble. However, the outer shock of the bubble is weak because the ambient medium is hot. It also makes the bubble size smaller than in Case II. In contrast, the WTS can be as strong as in Case II. We have calculated the shock energetics and found that the shock energy is mostly encountered by the wind material, similar to Case III.

### 4.2 Shock energetics

Let us summarise our findings here regarding the shock energetics, before moving on to the estimate of Neon isotope ratio:

- **Isolated SN:**

  In Case I, i.e., SN explosion in a uniform medium, the SN ejecta is confined inside a blast wave, and therefore can be accelerated by the reverse shock. We have shown that the reverse shock energy is \(~ ten times smaller than that of the forward shock (see bottom right panel of Fig. 5). Therefore, acceleration of SN ejecta is energetically not preferred in this case. We expect ISM nuclei to be accelerated more efficiently compared to SN nuclei by a ratio of \(10 : 1\).

In Case II (SN in the wind of a progenitor star), WTS can accelerate the wind material before the SN. When SN occurs, a blast wave moves through the free wind region for a few 100 yr. Eventually, the forward shock of the blast wave collides with the WTS. During this phase, the reverse shock of the blast wave becomes strong (see left panel of Fig. 6) and finally reaches the center. In contrast, the forward shock of the blast wave moves through the hot bubble and hits the wind-driven shocked ISM shell. As the temperature of the bubble is \(~ 10^7 \text{ K}\), the SN forward shock is weak compared to the reverse shock (see right panel of Fig. 6). We have estimated the shock energy encountered by the wind material and SN ejecta, and found that both are comparable. Therefore, in realistic calculations, acceleration of SN ejecta should also be considered in addition to the acceleration of the wind material.

- **Star cluster:**

  In this case, depending on the compactness of the star cluster, stellar winds from the stars can form a coherent WTS. This WTS can accelerate wind material for \(~ 3 \text{ Myr} \) before any SN. When the first SN occurs in the cluster, the forward shock of the blast wave moves outward by sweeping up the wind material. A reverse shock develops and sweeps up SN ejecta as well as the winds of remaining stars. When the SN forward shock collides with the WTS, it becomes weak. After that, it travels through the hot interior and the shock may disappear depending on the size of the bubble. Unlike Case - II, the SN reverse shock cannot reach to the center because the remaining stars continuously push it outward. This process brings the SN ejecta near the CD of the SB.

Next we define two parameters to represent the fraction of shock energy processed in the wind material and SN ejecta.
where \( E_w \) and \( E_{sn} \) denote the total shock energy processed by wind material and SN ejecta respectively. These factors are shown in Fig. 12 as a function of dynamical time\(^2\).

This figure shows that \( f_w \approx 2/3 - 6/7 \) and \( f_{sn} \approx 1/3 - 1/7 \). At early times (\( \lesssim 10 \) Myr), the difference is larger than a factor of 10 in case of a compact star cluster. Therefore, in star clusters, the acceleration of the wind material is energetically preferred than the SN ejecta.\(^3\)

### 4.3 \( ^{22}\text{Ne} / ^{20}\text{Ne} \) in CRs

Next we use our results of shock energetics to determine the isotope ratios in CRs, using the stellar evolutionary model of Limongi & Chieffi (2018). The yields of various elements in these models depend on initial metallicities, rotational velocities, and black hole cut off masses. Our estimates are robust to the variations within the uncertainties of these models. The abundances of \(^{20}\text{Ne} \) and \(^{22}\text{Ne} \) in wind and SN ejecta are shown in Fig. 13. In the rightmost panel, the curves indicate that \(^{22}\text{Ne} / ^{20}\text{Ne} \) ratio is large in the winds of massive stars (and to some extent, the SN ejecta of \( \lesssim 20M_\odot \) progenitors). The green line shows the corresponding ratio in Galactic CRs. Note that there are some differences in the ratio of \(^{22}\text{Ne} / ^{20}\text{Ne} \) between rotating and non-rotating models.

Denoting the masses of elements \(^{22}\text{Ne} \) and \(^{20}\text{Ne} \) by \( m^{22}\text{Ne} \) and \( m^{20}\text{Ne} \) respectively, we estimate the isotopic ratio of \(^{22}\text{Ne} / ^{20}\text{Ne} \) as follows. Various steps of the calculation are summarised in Fig. 14. Since the number of CRs accelerated is expected to be proportional to the energy crossing the shock, we calculate energy weighted wind and SN yields making use of shock energy deposited in wind material and SN ejecta, as calculated in §4.2. The instantaneous isotopic ratio of \(^{22}\text{Ne} / ^{20}\text{Ne} \) in SB is

\[
\frac{\left( \frac{m^{22}\text{Ne}}{m^{20}\text{Ne}} \right)_{SN}}{\left( \frac{m^{22}\text{Ne}}{m^{20}\text{Ne}} \right)_{wind}} = \frac{f_w \left\{ \int_{t=0}^{t_f} dt \left( \sum_{i=1}^{N_{SN}} m_{w}^{22}\text{Ne} \left( t' \right) \right) \right\} + f_{sn} \left\{ \sum_{i=1}^{SN} m_{sn}^{22}\text{Ne} \right\}}{f_w \left\{ \int_{t=0}^{t_f} dt \left( \sum_{i=1}^{N_{SN}} m_{w}^{20}\text{Ne} \left( t' \right) \right) \right\} + f_{sn} \left\{ \sum_{i=1}^{SN} m_{sn}^{20}\text{Ne} \right\}}
\]

\((10)\)
The time average ratio of $^{22}\text{Ne}/^{20}\text{Ne}$ that is accelerated up to time $t$ in SB (Prantzos 2012) is obtained using

$$
\left(\frac{^{22}\text{Ne}}{^{20}\text{Ne}}\right)_{\text{CR}} = \frac{1}{t} \int_{t' = 0}^{t} dt' \left( \frac{m}{m^{22}\text{Ne}} \right)
$$

(11)

These ratios for different stellar parameters are shown in Fig. 15.

Figure 15 shows that the ratio of $^{22}\text{Ne}/^{20}\text{Ne}$ is dominated by the abundance ratio in the stellar wind material. Initially the ratio is small because the wind of massive stars is dominated by $^{20}\text{Ne}$ except in the supernova wind of stars with mass $\gtrsim 20-60 \, M_\odot$, which begin to appear only after $\sim 3$ Myr. Therefore, $^{20}\text{Ne}$ produced in SN ejecta and winds of lower mass stars remain sub-dominant in CRs. After $\sim 10$ Myr, the cluster is left with stars ($\lesssim 20 \, M_\odot$) that contribute little to $^{22}\text{Ne}$ and $^{20}\text{Ne}$, and the isotope ratio remains practically frozen at the value attained by this time. Although there is a clear enhancement of $^{22}\text{Ne}/^{20}\text{Ne}$ has been observed in our analysis, it is worth mentioning that the stellar yields depend on the assumption of rotational speed of massive stars. We also note that since the acceleration of ejecta material is energetically less efficient, other isotope ratios such as $^{59}\text{Ni}/^{56}\text{Co}$ are likely to be small in GCR, as observed (Wiedenbeck et al. 1999).

5.1 Common platform for WTS and SNe shocks

To begin with, our calculations make use of both SNe shocks and WTS in star clusters. It may appear that isolated SNRs, which are considered as the standard sites of CR acceleration, have no relation with star clusters. However, star clusters provide the necessary ingredients for an integrated picture of both sources (SN shocks and wind termination shocks), considering the fact that massive OB stars form in dense, compact (of pc scale) clusters (Portegies Zwart et al. 2010; Pfalzner 2009). Although massive stars are sometimes found outside clusters, as in LMC (Sana 2013), they can be considered to be ‘slow runaways’ from massive clusters (Banerjee et al. 2012; Lucas et al. 2018). Although diffuse or ‘leaky’ clusters (Pfalzner 2009) have sizes of about an order of magnitude larger than compact clusters (e.g., Cyg OB2), they can be thought of as assemblies of compact clusters, given that they have substantial substructures (Wright et al. 2014). Finally, if the initial cluster is small enough, it can be dissolved (or nearly dissolved) due to gas dispersion and mass loss during SNe (Brinkmann et al. 2017, Shakirgaliyev et al. 2017).

Observations therefore indicate that all OB stars, including the progenitor isolated SNRs, can be considered to have formed in massive compact clusters.

5.2 Number statistics of SNe and massive clusters

Based on above discussions, we can therefore argue that the massive progenitors of apparently isolated SNRs can be considered as belonging to clusters in which the number of massive (OB) stars is $\lesssim 2$. The cluster luminosity function (Williams & McKee 1997) is observed to be $dN/dM_{\odot} \propto N_{\odot}^{-0.5}$, where $N_{\odot}$ is the number of OB stars in a cluster. This implies that roughly half the clusters would produce an apparently isolated (core collapse) SNR, since (for a lower limit of
a massive star cluster being that with a single OB star
\[
\frac{\int_{0}^{2} N_{OB}^{-2} dN_{OB}}{\int_{50-100} N_{OB}^{-2} dN_{OB}} \approx \frac{1}{2} \tag{12}
\]

which is almost independent of the upper limit of total number of OB stars in a cluster which is roughly $\sim 7000$ (McKee & Williams 1997).

In comparison, $\gamma$-ray bright clusters ($\gamma$-ray luminosity $\gtrsim 10^{35}$ erg s$^{-1}$) have typically $\sim 50-100$ OB stars (Gupta et al. 2018b). This mass function implies a ratio of core collapse SNRs to WTS gamma-ray sources is
\[
\frac{\int_{0}^{2} N_{-2}^{-2} dN_{OB}}{\int_{50-100} N_{OB}^{-2} dN_{OB}} \approx \frac{1}{2} (50-100) = (25-50). \tag{13}
\]

Observations show that in Sbc galaxies (Milky-Way-type) the ratio of thermonuclear to core collapse SNe is $\sim 1/3$ (Mannucci et al. 2005). Adding thermonuclear SNRs, this indicates a ratio of SNRs to WTS $\gamma$-ray sources in our Galaxy of order $33-65$.

We can check this argument by counting the SNRs and $\gamma$-ray bright clusters in a given volume. The size of the sampling volume is hard to decide, since $\gamma$-ray bright clusters are rare: there are only 3 $\gamma$-ray bright clusters near us, Cygnus at $\approx 1.4$ kpc, Westerlund 1 at $\approx 4$ kpc (Aharonian et al. 2019), and Westerlund 2 at $\approx 5$ kpc (Yang et al. 2018). Therefore, it makes sense to use all these three and use a sphere of radius 5 kpc around us. Counting the number of SNRs from the available catalogue, we find 124 of them within a distance of 5 kpc (listed in Table C1 of Appendix C), so that the ratio 124:3 falls in the ballpark of the above estimate.

This match can be regarded as a consistency check for our proposed scenario, and this implies that isolated SNRs can indeed be considered as part of the phenomena of star clusters. Therefore, the two types of CR acceleration sites can indeed be put on a common platform.

5.3 Contributions of WTS and SN shocks in total energy budget of GCRs

The next issue to consider is the energy budget of Galactic CRs from these two sites. It can be shown that these two classes of sources are energetically comparable (as pointed out in 1980s, see e.g., Abbott et al. 1981), WTS being dominant in young phase of clusters. Figure 16 plots the evolution of the contribution of stellar winds to the total mechanical energy of a star cluster, using Starburst99 (Leitherer et al. 1999), and Kroupa initial mass function (Kroupa 2002), for different assumptions of black hole mass cutoff. All curves are obtained using the Starburst99 stellar synthesis code (Leitherer et al. 1999) for the Kroupa Initial Mass Function (Kroupa 2002). Each curve represents a model with different black hole mass, $M_{BHcut}$ (blue - $25 M_{\odot}$, red - $30 M_{\odot}$, yellow - $40 M_{\odot}$, and green - $120 M_{\odot}$). The figure shows that wind mechanical energy dominates over SN energy before $\gtrsim 11 \pm 3$ Myr.

which in turn corresponds to a SN rate of $\sim 2$ per century, consistent with the observed rate of 2 per century (Diehl et al. 2006). Incidentally, with a typical efficiency of CR acceleration $\sim 0.1$, the total mechanical luminosity of $8 \times 10^{34}$ erg s$^{-1}$ is comparable to the inferred Galactic CR (GCR) luminosity (Strong et al. 2010) of $\sim 8 \times 10^{34}$ erg s$^{-1}$.

Therefore, the scenario of CR acceleration in WTS and SNSs is consistent with respect to the energy budget.

5.4 Maximum energy of CRs

The importance of WTS as CR sources becomes crucial at high energies (Csargsky & Montmerle 1983), since the observed $\gamma$-ray spectra of clusters are flatter than that of SNRs (Aharonian et al. 2019). The maximum CR energy depends on the extent of the accelerating region, in this case, the width of the shocked wind region, which separates the contact discontinuity and WTS. The distance of the WTS is roughly given by
\[
R_{TS} \approx 25 \, \text{pc} \, n_1^{-3/10} \, \eta^{-1/5} \, L_{w38}^{-5/12} \, L_{w,2000}^{2/5}, \tag{14}
\]
where $n_1$ is the ambient particle density in units of 10 cm$^{-3}$, $\eta$ is mass loss rate in units of $10^{-4} M_{\odot}$ yr$^{-1}$, $v_{w,2000}$ is wind speed in units of 2000 km s$^{-1}$, $L_{w38}$ is wind mechanical power in units of $10^{38}$ erg s$^{-1}$, $t_{1M}$ is time in 3 Myr unit. The distance of the contact discontinuity is $(q L_{w38}/\rho)^{1/3}$, where $q \approx 0.2$ takes into account energy lost in radiative cooling (see e.g., Sharma et al. 2014). For the same fiducial parameters, this distance is given by $\sim 62$ pc. Therefore, for a $10^4 M_{\odot}$ cluster, the extent of the shocked wind region at
\[ E \leq \frac{1}{2} \times 10^{15} \epsilon L_{\text{pc}} B_{\mu G} Z \beta, \tag{15} \]

where \( \beta \) is the ratio of shock speed to that of light, and \( L_{\text{pc}} \) is the extent of the accelerating region in parsec.\(^4\) With a 10\( \mu G \) field, and wind velocity \( \sim 2000 \text{km s}^{-1} \), this implies a maximum energy \( E \) of \( \sim 1.5 \text{Z PeV} \), much larger than in isolated SNR. We note that Volk & Biermann (1988) had argued that SNe shocks expanding in a wind bubble could circumvent the problems with isolated SNRs, but our prediction is independent of SNe event in a star cluster. We also note that LOFAR observations show PeV CRs to be enriched in low-Z nuclei (Buttink et al. 2016), consistent with their being accelerated from CNO enriched wind material in SBs (Thoudam et al. 2016). It is also possible that the hard component of CRs due to WTS is the one inferred to be present in molecular clouds (de Boer et al. 2017). Therefore WTSs are potential PeVatrons and they should be studied in detail in this regard.

### 5.5 Decoupling of grammage from ISM

Our proposed scenario can also provide the astrophysical framework for the phenomenologically motivated models of CR propagation in which the grammage traversed by CRs are mostly near the source (Cowsik & Madziwa-Nussinov 2016; Eichler 2017; Blasi & Serpico 2009; Biermann et al. 2018). In these models the diffusion property of CR particles is assumed to be different inside the ‘cocoons’ surrounding the CR acceleration sites than elsewhere in the ISM in order to alleviate problems associated with secondary production.

The scenario of CR acceleration in SBs satisfies the basic premises of these models, since most of the CR collisions occur in the outer shell of shocked ISM, whereas CRs are advected by the wind in the inner regions. The grammage suffered by CRs in the shocked ISM region is \( \sim 10 \text{ g cm}^{-2} \), comparable to the total grammage of Galactic CR (Gabici et al. 2019), since the typical residence time is \( t_r \sim 1 \text{Myr} \) (\( \sim \kappa/v^2 \), for a diffusion coefficient \( \kappa \sim 10^{27} \text{cm}^2 \text{ s}^{-1} \) and \( v \sim 50 \text{ km s}^{-1} \), the typical outer shock speed), and typical density in this region is \( \sim 10 \text{ cm}^{-3} \).

Therefore, CR grammage can be decoupled from Galactic residence time, alleviating a number of outstanding problems (Butt 2009; Gabici et al. 2019). Instead of listing them all, we mention one of the problems here, that of the observed scaling of light elements with metallicity in halo stars (Parizot & Drury 1999). In the case of isolated SNRs (which accelerates ISM particles), the Li/Be/B abundance is expected to scale as \( Z^2 \), since both CR and the target gas share the same metallicity. In the case of WTS, the metallicity of CRs is independent of that of the ambient ISM,

\[ \sim 3 \text{ Myr} \text{ (when WTS dominates)} \text{ is } \sim 40 \text{ pc}. \text{ This estimate is also borne out with our 1-D simulation (see e.g., Figure 3 for compact star cluster, i.e., Case III).} \]

According to the Hillas criterion (Hillas 1984), the accelerating region should be larger than \( 2r_L/\beta \) where \( r_L \) is the Larmor radius of a particle, which leads to a maximum energy

\[ E \leq \frac{1}{2} \times 10^{15} \epsilon L_{\text{pc}} B_{\mu G} Z \beta, \tag{15} \]

\[ \text{where } \beta \text{ is the ratio of shock speed to that of light, and } L_{\text{pc}} \text{ is the extent of the accelerating region in parsec.} \]

\[ \text{With a } 10\mu G \text{ field, and wind velocity } \sim 2000 \text{km s}^{-1}, \text{ this implies a maximum energy } E \text{ of } \sim 1.5 \text{Z PeV}, \text{ much larger than in isolated SNR.} \]

\[ \text{We note that Volk & Biermann (1988) had argued that SNe shocks expanding in a wind bubble could circumvent the problems with isolated SNRs, but our prediction is independent of SNe event in a star cluster.} \]

\[ \text{We also note that LOFAR observations show PeV CRs to be enriched in low-Z nuclei (Buttink et al. 2016), consistent with their being accelerated from CNO enriched wind material in SBs (Thoudam et al. 2016).} \]

\[ \text{It is also possible that the hard component of CRs due to WTS is the one inferred to be present in molecular clouds (de Boer et al. 2017).} \]

\[ \text{Therefore WTSs are potential PeVatrons and they should be studied in detail in this regard.} \]

### 6 CONCLUSIONS

With 1-D numerical hydrodynamical simulation of stellar winds in star clusters, we have studied the relative importance of SNe shocks and wind termination shocks (WTSs) in clusters, both compact and massive, and also in the case of SNe shocks running into stellar winds of the progenitor star. Our findings are as follows:

\[ \text{(i) WTSs process more than } 1/4 \text{ of the total mechanical power in a star cluster, and this fraction rises to } \gtrsim 0.5 \text{ for young (} \lesssim 10 \text{ Myr) clusters (Figure 16).} \text{ Therefore a significant fraction of Galactic CRs are accelerated in these shocks in massive compact star clusters.} \]

\[ \text{(ii) A large fraction (} \sim 2/3-6/7) \text{ of the total energy processed by WTS and SNe shocks goes to accelerate the stellar wind material, enriched in } ^{22}\text{Ne (Figure 12).} \text{ Using this ratio as an energy weightage for the stellar wind and SN ejecta, we show that the time averaged ratio of } ^{22}\text{Ne}/^{20}\text{Ne} \text{ matches the observed value.} \]

\[ \text{(iii) We also show that the scenario often quoted in literature for explaining the Neon ratio, namely, by SNe shocks in a stellar wind of progenitor star, is problematic because we find that the reverse shock in this case is as efficient as the forward shock, and it would accelerate SN ejects (rich in } ^{20}\text{Ne}) \text{ posing a problem for the isotope ratio.} \]

\[ \text{(iv) The combined effect of WTSs and SNe shocks in star clusters can explain the observed Neon isotope ratio (Figure 15), unlike previous approaches of either SNe shocks (in stellar winds) or only stellar winds (e.g., Binns et al. 2008).} \]

\[ \text{(v) We take this approach forward to suggest that these two sources can be brought under a same umbrella of CR acceleration in SBs, since SNe and stellar wind are both related to massive stars and they form in clusters. Isolated SNRs can be considered as representing the lower end of the star cluster mass function.} \]

\[ \text{(vi) Using the luminosity function of OB associations, we show that the expected ratio of isolated SNRs to } \gamma\text{-ray bright star clusters matches observed numbers (section 5.2).} \]

\[ \text{(vii) We argue that the accelerating region in the case of WTSs is large enough to explain CRs in PeV range (section 5.4), thus making WTSs an important complementary source of CRs.} \]

\[ \text{(viii) The fact that most of the CR interactions occur in the SB, with a grammage that corresponds to the observed grammage of GCRs (section 5.5), decouples the CR grammage from the Galactic residence time and helps solve other long standing problems with the standard paradigm of SNRs as CR acceleration sites.} \]

The integrated picture of CR acceleration in SBs inflated by clustered WTS and SN presented here can solve these problems as well as explain \(^{22}\text{Ne}/^{20}\text{Ne}\) ratio, while being consistent with the number statistics of SNRs and WTS sources.
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REFERENCES

Abbott D. C., Bieging J. H., Churchwell E., 1981, ApJ, 250, 645
Ackermann M., et al., 2011, Science, 334, 1103
Aharonian F., Yang R., de Oña Wilhelmi E., 2019, Nature Astronomy, 3, 561
Banerjee S., Kroupa P., Oh S., 2012, ApJ, 746, 15
Biermann P. L., Cassinelli J. P., 1993, A&A, 277, 691
Biermann P. L., et al., 2018, Advances in Space Research, 62, 2773
Binns W. R., et al., 2008, New Astron. Rev., 52, 427
Blasi P., Serpico P. D., 2009, Phys. Rev. Lett., 103, 081103
Brinkmann N., Banerjee S., Motwani B., Kroupa P., 2017, A&A, 600, A49
Buitink S., et al., 2016, Nature, 531, 70
Butt Y., 2009, Nature, 460, 701
Cesarsky C. J., Montmerle T., 1983, Space Sci. Rev., 36, 173
Chevalier R. A., Clegg A. W., 1985, Nature, 317, 44
Cowsik R., Madziwa-Nussinov T., 2016, ApJ, 827, 119
Dermer C. D., Powale G., 2013, A&A, 553, A34
Diehl R., et al., 2006, Nature, 439, 45
Eichler D., 2017, ApJ, 842, 50
Gabici S., Evoli C., Gaggero D., Lipari P., Mertsch P., Orlando E., Strong A., Vittino A., 2019, arXiv e-prints, p. arXiv:1903.11584
Grenier I. A., Black J. H., Strong A. W., 2015, ARA&A, 53, 199
Gupta S., Nath B. B., Sharma P., Eichler D., 2018a, MNRAS, 473, 1537
Gupta S., Nath B. B., Sharma P., 2018b, MNRAS, 479, 5220
Higdon J. C., Lingenfelter R. E., 2003, ApJ, 590, 822
Hillas A. M., 1984, ARA&A, 22, 425
Jokipii J. R., 1987, ApJ, 313, 842
Kroupa P., 2002, Science, 295, 82
Leitherer C., et al., 1999, ApJS, 123, 3
Limongi M., Chieffi A., 2018, ApJS, 237, 13
Lopez L. A., Krumholz M. R., Bolatto A. D., Prochaska J. X., Ramirez-Ruiz E., Castro D., 2014, ApJ, 795, 121
Lucas W. E., Rybak M., Boullin I. A., Gieles M., 2018, MNRAS, 474, 3582
Mannucci F., Della Valle M., Panagia N., Cappellaro E., Cresci G., Maiolino R., Petrosian A., Turatto M., 2005, A&A, 433, 807
McKee C. F., Williams J. P., 1997, ApJ, 476, 144
Mignone A., Bodo G., Massaglia S., Matsakos T., Tesileanu O., Zanni C., Ferrari A., 2007, ApJS, 170, 298
Murphy R. P., et al., 2016, ApJ, 831, 148
Parizot E., Drury L., 1999, A&A, 349, 673
Pfalzner S., 2009, A&A, 498, L37
Portegies Zwart S. F., McMillan S. L. W., Gieles M., 2010, ARA&A, 48, 431
Prantzos N., 2012, A&A, 538, A80
Reed B. C., 2005, AJ, 130, 1652
Sana H., 2013, in Pavlovski K., Tkachenko A., Torres G., eds, EAS Publications Series Vol. 64, EAS Publications Series. pp 147–154 (arXiv:1311.0009), doi:10.1051/eas/1364021
Seo J., Kang H., Ryu D., 2018, Journal of Korean Astronomical Society, 51, 37
Sharma P., Roy A., Nath B. B., Shchekinov Y., 2014, MNRAS, 443, 3463
Shukirgaliev B., Parmentier G., Berczik P., Just A., 2017, A&A, 605, A119
Strong A. W., Porter T. A., Digel S. W., Jóhannesson G., Martin P., Moskalenko I. V., Murphy E. J., Orlando E., 2010, ApJ, 722, L58
Sutherland R. S., Dopita M. A., 1993, ApJS, 88, 253
Thoudam S., Rachen J. P., van Vliet A., Achterberg A., Buitink S., Falcke H., Hörandel J. R., 2016, A&A, 595, A33
Truelove J. K., McKee C. F., 1999, ApJS, 120, 299
Völk H. J., Biermann P. L., 1988, ApJ, 333, L65
Weaver R., McCray R., Castor J., Shapiro P., Moore R., 1977, ApJ, 218, 377
Wiedenbeck M. E., Greiner D. E., 1981, Phys. Rev. Lett., 46, 682
Wiedenbeck M. E., et al., 1999, ApJ, 523, L61
Williams J. P., McKee C. F., 1997, ApJ, 476, 166
Wright N. J., Parker R. J., Goodwin S. P., Drake J. J., 2014, MNRAS, 438, 639
Yang R.-z., de Oña Wilhelmi E., Aharonian F., 2018, A&A, 611, A77
de Boer W., Bosse L., Gebauer I., Neumann A., Biermann P. L., 2017, Phys. Rev. D, 96, 043012
Figure B1. Time dependent wind model. [Left panel] Time evolution of stellar wind luminosity and mass-loss rate of a cluster of mass $10^4 M_{\odot}$ obtained using the Starburst99 stellar synthesis code (Leitherer et al. 1999). Each curve represents a model with different black hole cut-off mass. $M_{\text{BHcut}}$ (blue - $25 M_{\odot}$, red - $30 M_{\odot}$, yellow - $40 M_{\odot}$, and green - $120 M_{\odot}$). The figure shows that stellar wind luminosity decreases and becomes almost negligible after $\gtrsim 15$ Myr. [Right panel] Comparison between wind mechanical energy and SN energy in a cluster. Different colours show that the time when SN energy dominates over wind energy depends on $M_{\text{BHcut}}$ and it occurs after $\approx 11 \pm 3$ Myr. In both panels, the black curves represent an injection model used to show the effect of time-dependent wind model in our calculation.

APPENDIX A: 3-D SET-UP

Here we present the set-up of our 3-D simulations discussed in section 2.1. We simulate two star clusters with two different core radii $R_c$. Both clusters have twelve massive stars (i.e., $N_{\text{OB}} = 12$), which corresponds to a cluster of stellar mass $10^3 M_{\odot}$ (for a standard Kroupa initial mass function (IMF) with lower- and upper- cutoff masses $0.1 M_{\odot}$ and $120 M_{\odot}$; Kroupa 2002). We have solved the standard Euler equations in 3-D Cartesian geometry using the PLUTO code (Mignone et al. 2007), where the HLLC Riemann solver is used (CFL number 0.3) and the computational box extends from $-60$ pc to $+60$ pc along x, y, and z directions. At $t = 0$, we assume that ambient density is uniform with $\rho = 50 \, \text{m}_1 \, \text{cm}^{-3}$, and pressure is $10^{-12} \, \text{dyne cm}^{-2}$. Radiative cooling has been included both runs. Locations of the stars are randomly chosen by making use of a Gaussian random number generator, where we have used two sets of mean deviations, $\sigma_{x,y,z} = 0.5$ pc and $\sigma_{x,y,z} = 5$ pc, to represent compact and loosely bound star clusters respectively. For each star, we have assumed $M = 8 \times 10^{-7} M_{\odot} \, \text{yr}^{-1}$ and $L_w = 10^{36} \, \text{erg s}^{-1}$, which are injected in small spherical regions of radius $\delta r_{\text{inj}} = 0.2$ pc (for details see section 4.2 in Gupta et al. 2018b).

APPENDIX B: TIME DEPENDENT LUMINOSITY MODEL

To estimate the fraction of shock energy encountered by wind material and SNe ejecta, in the previous sections we have considered a time-independent wind model, where it has been assumed the wind mechanical luminosity of each star in a cluster is $10^{36} \, \text{erg s}^{-1}$ until it explodes as SN. Here we investigate the effect of the time-dependent wind luminosity in our calculation.

We use a stellar synthesis code Starburst99 (Leitherer et al. 1999) to obtain the time evolution of wind luminosity, stellar mass-loss rate, and SNe energy of a cluster of mass $10^4 M_{\odot}$ for four different black hole cut-off masses: 25, 30, 40, and $120 M_{\odot}$. The wind mechanical power and mass-loss rates are shown in the left panel of Fig. B1. Figure shows that the wind mechanical power and mass-loss rates do not depend on the black hole cut-off mass, as expected. The right panel shows the total energy deposited by SNe and by winds in the cluster until a given epoch. The black curves represent fitted curves used in our model to inject stellar wind and SN energy. The fraction of shock energy processed in wind material and SNe ejecta is shown in Fig. B2. The figure shows that the fraction of shock energy processed in wind is larger than that in SN ejecta.

APPENDIX C: SNRS

Table C1 shows a list of 124 SNRs that has been used in section 5.2 to discuss number statistics of SNe and massive clusters.

This paper has been typeset from a $\LaTeX$ file prepared by the author.
### Table C1

This table provides a list of SNRs which are located within 5 kpc. [1] and [2] refer to [1] https://arxiv.org/abs/1409.0637; https://www.mrao.cam.ac.uk/surveys/snr/ and [2] https://hea-www.cfa.harvard.edu/ChandraSNR/sncat_gal.html.

| Galactic coordinates  | Distance (kpc) | Ref. |
|-----------------------|----------------|------|
| (l, b)                | (kpc)          |      |
| 1. 4.5, +0.8          | 3.3 ± 5.1      | [1]  |
| 2. 5.2, +2.6          | 4.3 ± 5.2      | [1]  |
| 3. 5.7, +0.1          | 2.9 ± 3.2      | [2]  |
| 4. 6.4, +0.1          | 2.2 ± 1        | [1]  |
| 5. 7.5, +3.7          | 3.2 ± 6        | [1]  |
| 6. 8.7, +0.1          | 4.0 ± 1        | [1]  |
| 7. 11.0, +0.0         | 5.0 ± 1        | [1]  |
| 8. 11.1, +0.1         | 4.4 ± 1        | [1]  |
| 9. 13.5, +1.3         | 2 ± 4          | [1]  |
| 10. 5.7, +0.1         | 3.2 ± 1        | [1]  |
| 11. 7.5, +1.7         | 1.7 ± 2.0      | [2]  |
| 12. 15.1, -1.6        | 2.1 ± 1        | [1]  |
| 13. 15.4, +0.1        | 4.8 ± 1        | [1]  |
| 14. 18.6, -0.2        | 4.2 ± 4.6      | [1]  |
| 15. 18.9, -1.1        | 4.2 ± 4.6      | [1]  |
| 16. 19.1, +0.2        | 1 ± 2          | [1]  |
| 17. 21.5, +0.9        | 4.7 ± 1        | [1]  |
| 18. 22.7, -0.2        | 4.5 ± 4.9      | [1]  |
| 19. 23.3, -0.3        | 4.6 ± 5.0      | [1]  |
| 20. 24.7, -0.6        | 4 ± 1          | [1]  |
| 21. 24.7, +0.6        | 2 ± 3.7        | [1]  |
| 22. 28.8, +1.5        | 3.8 ± 4.0      | [1]  |
| 23. 29.6, +0.1        | 4.4 ± 5.0      | [1]  |
| 24. 29.7, -0.3        | 5 ± 1          | [1]  |
| 25. 32.0, -0.9        | 1.8 ± 1        | [1]  |
| 26. 32.1, -0.9        | 4.6 ± 1        | [1]  |
| 27. 32.8, -0.1        | 4.5 ± 5.1      | [1]  |
| 28. 34.7, -0.4        | 2.1 ± 3        | [1]  |
| 29. 40.5, -0.5        | 3.2 ± 1        | [1]  |
| 30. 42.0, -0.1        | 3.1 ± 3.9      | [1]  |
| 31. 49.2, -0.7        | 4.3 ± 1        | [1]  |
| 32. 53.6, -2.2        | 2.8 ± 1        | [1]  |
| 33. 55.7, +3.4        | 0.56 ± 1       | [1]  |
| 34. 57.2, +0.8        | 3.5 ± 1        | [1]  |
| 35. 21.5, -0.9        | 4.7 ± 2        | [1]  |
| 36. 21.9, -0.1        | 4.3 ± 2        | [2]  |
| 37. 23.5, +0.1        | 5 ± 2          | [1]  |
| 38. 26.6, -0.5        | 1.3 ± 1        | [1]  |
| 39. 34.8, +20.3       | 1.4 ± 1        | [1]  |
| 40. 59.2, +0.7        | 2.5 ± 1        | [1]  |
| 41. 65.3, +5.7        | 0.8 ± 1        | [1]  |
| 42. 65.7, +1.2        | 1.5 ± 1        | [1]  |
| 43. 65.8, -0.5        | 1.9 ± 2.7      | [1]  |
| 44. 66.0, -0.0        | 2.0 ± 2.6      | [1]  |
| 45. 67.6, +0.9        | 1.8 ± 2.2      | [1]  |
| 46. 70.6, -21.5       | 3 ± 1          | [1]  |
| 47. 73.9, +0.9        | 0.5 ± 4.0      | [1]  |
| 48. 74.0, -8.5        | 0.44 ± 1       | [1]  |
| 49. 78.2, +2.1        | 1.7 ± 2.6      | [1]  |
| 50. 82.2, +5.3        | 1.3 ± 3.2      | [1]  |
| 51. 85.4, +0.7        | 3.5 ± 1        | [1]  |
| 52. 85.9, -0.6        | 4.8 ± 1        | [1]  |
| 53. 89.0, +4.7        | 0.8 ± 1        | [1]  |
| 54. 93.3, +4.9        | 2.2 ± 1        | [1]  |
| 55. 93.7, -0.2        | 1.5 ± 1        | [1]  |
| 56. 10.9, -45.4       | 0.25 ± 2       | [2]  |
| 57. 25.1, -2.3        | 2.9 ± 1        | [1]  |
| 58. 33.6, +0.1        | 3.5 ± 7.1      | [1]  |
| 59. 39.7, -2.0        | 3.5 ± 6.5      | [1]  |
| 60. 42.8, +0.6        | 2.8 ± 7.7      | [1]  |
| 61. 69.0, +2.7        | 1.5 ± 1        | [1]  |
| 62. 106.3, -4.7       | 0.8 ± 3.0      | [1]  |
| 63. 126.2, -1.6       | 4.5 ± 1        | [1]  |