Two-dimensional Vortices in Superconductors

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Superconductors have two key characteristics. They expel magnetic field and they conduct electrical current with zero resistance. However, both properties are compromised in high magnetic fields which can penetrate the material and create a mixed state of quantized vortices. The vortices move in response to an electrical current dissipating energy which destroys the zero resistance state. One of the central problems for applications of high temperature superconductivity is the stabilization of vortices to ensure zero electrical resistance. We find that vortices in the anisotropic superconductor Bi$_2$Sr$_2$CaCu$_2$O$_{8+\delta}$ (Bi-2212) have a phase transition from a liquid state, which is inherently unstable, to a two-dimensional vortex solid. We show that at high field the transition temperature is independent of magnetic field, as was predicted theoretically for the melting of an ideal two-dimensional vortex lattice. Our results indicate that the stable solid phase can be reached at any field as may be necessary for applications involving superconducting magnets. The vortex solid is disordered, as suggested by previous studies at lower fields. But its evolution with increasing magnetic field displays unexpected threshold behavior that needs further investigation.

Shortly after the discovery of cuprate superconductivity it was recognized that their high transition temperature would mean that thermal fluctuations can produce a liquid vortex state. In fact the thermodynamic transition to superconductivity in a magnetic field occurs between a thermally fluctuating liquid vortex phase to one or more solid phases. The liquid vortex state is inherently unstable with non-zero electrical resistance. For extremely anisotropic materials, like Bi-2212, the liquid phase covers a wide range of temperature; but it is not known exactly how wide this is in high magnetic fields. For fields perpendicular to the conducting planes, $H||c$-axis, the transition temperature between liquid and solid vortex phases, $T_m(H)$, is principally controlled by vortex-vortex interactions which get stronger as the density of vortices increases, proportional to the field. The supercurrents that form each vortex are mainly confined to the conducting planes and, in high field, they lose their coherence from one plane to the next so that vortices are expected to become two-dimensional. It is remarkable that the theory for the two-dimensional vortex melting transition has only one parameter, the magnetic field penetration depth, and that this simple picture has not yet been experimentally confirmed.

We use nuclear magnetic resonance (NMR) of $^{17}$O to detect the melting transition of vortices as a function of temperature and magnetic field. NMR can be performed on selected elements in site specific locations in the structure as we see in the $^{17}$O spectra in Fig. 1. There are three stoichiometric positions for oxygen in Bi-2212, in atomic planes containing Cu, the O(1) site; Sr planes, the O(2) site; and Bi planes. The last oxygen atoms are unobserved owing to disorder in this plane. In addition there is a small amount of non-stoichiometric oxygen, $\delta$-oxygen, too small to be observed directly by NMR and whose location in the structure is not yet established. The parts of the NMR spectra in the middle range of field in Fig. 1 are the central transitions from the O(1) (broad) and O(2) (narrow) sites. The electronic coupling to $^{17}$O is much stronger for O(1) compared with O(2) as is apparent from the temperature dependences in Fig. 1. This is confirmed by measurements of the spin-lattice relaxation rate which are one order of magnitude larger for O(1) as compared to O(2). The narrowness of
The central transition, the NMR spectrum to the left. At high temperatures two oxygen sites can be distinguished. The optimally doped $T_{c}$, with $T_{c} = 75$ K, with $\approx 60\%$ of $^{16}$O exchanged for $^{17}$O. The spectroscopy can be understood in terms of defects in the copper-oxygen plane. This curve is given by, $\Delta \nu = \Delta \nu_0 + KHD/T$, where $\Delta \nu_0$ is a background magnetic contribution to the linewidth possibly associated with regions of the sample where superconductivity is suppressed, $K(T)$ is the measured Knight shift, $H/T$ is the field-to-temperature ratio and $D$ is a Curie constant. The key feature of the data is the systematic break from this curve that we identify with the transition from a liquid to a solid vortex state.

Decreasing the temperature below the superconducting transition temperature we find the $^{17}$O(1) resonance peaks move to the left, i.e. to a higher field at a fixed NMR frequency, (lower frequency at fixed field) approaching the zero spin-shift position. Simultaneously, the central NMR line narrows. The decrease of the Knight shift to zero in the superconducting state is a characteristic signature for spin-singlet pairing. The line broadening with decreasing temperature in the normal state, Fig. 1 and 2, can be associated with a Knight shift distribution introduced by the $\delta$-oxygen. Similar behavior has been observed for chemical impurities, like Ni, Zn, or Li, substituted for Cu in the CuO$_2$ plane in YBCO, and which form a local moment. Their contribution to the $^{17}$O NMR linewidth is given by a Curie law, proportional to the ratio of applied magnetic field to temperature. Additionally, we find that below $T_c$ their associated local magnetic fields.

the O(2) resonance indicates a homogeneous electronic environment with negligible spin-shift (Knight-shift) and uniform electric field gradient. For fast pulse repetition, as is the case for our measurements in Fig.1, O(2) is partially saturated and comprises less than 6% of the spectrum at 60 K, decreasing with decreasing temperature to 2% at 40 K. We remove it numerically in this range of temperature and below this, it has negligible contribution to the spectrum. The critical temperature of the oxygen in the strontium-oxygen plane, O(2), is the narrow peak at 13.49 T at 100 K. The central transition for the oxygen in the copper-oxygen plane, O(1), is the wide line near 13.49 T at 100 K. The central transition for the oxygen in the strontium-oxygen plane, O(2), is the narrow line near the zero Knight shift position at 13.51 T. The other two peaks are quadrupolar satellites of the O(1) resonance. For $T = 4$ and 12 K we show the Fourier transform of the echo at fixed field, having a smaller spectral bandwidth so that satellites are not observed here. Our separate measurement of the satellite intensity at $T/T_m = 0.67$ compared to the central transition is the same as that at $T/T_m = 1.33$, confirming this picture. The spectra at different temperatures are normalized to have the same peak intensity of the O(1) central transition.

FIG. 1: Spectra of $^{17}$O NMR in Bi-2212 for magnetic field parallel to the $c$-axis at fixed frequency. The sample is an overdoped, 28 mg, single crystal of Bi$_2$Sr$_2$CaCu$_2$O$_{8+\delta}$ (Bi-2212), with $T_c = 75$ K, with $\approx 60\%$ of $^{16}$O exchanged for $^{17}$O. The optimally doped $T_c = 93$ K. In field-sweep experiments ($T = 20, 40, 60, 100$ K), a decreasing Knight shift moves the NMR spectrum to the left. At high temperatures two oxygen sites can be distinguished. The central transition, the NMR spectrum to the left. At high temperatures two oxygen sites can be distinguished.
On further cooling in the superconducting state there is a sharp onset for a new contribution to the linewidth which is not proportional to applied magnetic field. The well-defined temperature at which this line broadening appears is plotted in Fig. 3, decreasing, but progressively more slowly, with increasing magnetic field in our range between 3 and 29 Tesla. We identify this behavior with the formation of a solid vortex structure. More precisely, the extra linewidth corresponds to an inhomogeneous magnetic field distribution that is static on the NMR time scale, precisely the extra linewidth corresponds to an inhomogeneous magnetic field distribution from vortex supercurrents. Specifically, NMR is complementary to these methods with definite advantages for detecting the absolute value of the penetration depth at low temperature and SANS show that at low temperature and vortex structure is somewhat disordered. In fact, we have observed. From a fit to the data, dotted line, we use the framework of Eq. 1-3. to analyze the freezing temperature, \( T_m(H) \), of vortex melting transition temperatures, \( T_m(H) \), identified from the data, as shown in Fig. 2. The two-dimensional vortex melting transition temperature, \( T_m^{2D} \), (vertical dashed line), is determined from a fit to the data. Deviations of the fit from the data are expected for \( H \approx H_{cr} \).

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FIG. 3: The magnetic field-temperature phase diagram for vortex melting in Bi-2212 for \( H \parallel c \). The transition temperatures, \( T_m(H) \), are identified from the data, as shown in Fig. 2. The two-dimensional vortex melting transition temperature, \( T_m^{2D} \), (vertical dashed line), is determined from a fit to the data. Deviations of the fit from the data are expected for \( H \approx H_{cr} \).

The immediate critical field \( H_{cr} \) for vortex melting in Bi-2212 for \( H \parallel c \) is \( \approx 2 \) T, determined by Hall probe measurements and transport measurements. Khaykovich et al. explore this behavior as a function of oxygen doping (anisotropy). NMR is complementary to these methods with definite advantages for detecting vortex melting at very high magnetic fields. The NMR or \( \mu \)SR spectrum is a direct map of the magnetic field distribution from vortex supercurrents. Specifically, NMR with \(^{17}\)O affords excellent resolution as a magnetometer on the atomic scale and has been exploited in previous work to spatially resolve and study excitations in the vortex core.

The NMR vortex lineshape is asymmetric but less so than for a perfect line-vortex lattice suggesting that the vortex structure is somewhat disordered. In fact, we have observed. From a fit to the data, dotted line, we use the framework of Eq. 1-3. to analyze the freezing temperature, \( T_m(H) \), of vortex melting transition temperatures, \( T_m(H) \), identified from the data, as shown in Fig. 2. The two-dimensional vortex melting transition temperature, \( T_m^{2D} \), (vertical dashed line), is determined from a fit to the data. Deviations of the fit from the data are expected for \( H \approx H_{cr} \).

The limiting two-dimensional melting temperature in Eq. 1, is,

\[
T_m^{2D} = A \frac{\phi_0^2d}{8\pi\sqrt{3}k_B(4\pi\lambda_{ab})^2}.
\]

where \( 0.605 \leq A \leq 0.615 \), comes from numerical calculations (Koshelev, A.E., private communication). This spread in \( A \) reflects the existence of an intermediate phase since the ideal two-dimensional melting scenario proceeds in two steps with an intervening hexatic phase bounded by continuous transitions. The limiting two-dimensional melting temperature in Eq. 1, is,

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The strong upward curvature of the phase diagram in Fig 3, has been anticipated theoretically. Torque magnetometry in fields \( H \leq 5 \) T gave similar indications. For highly anisotropic superconductors the electromagnetic interaction between vortices dominates the Josephson coupling between planes. In this high field limit the simplest picture for vortex melting is a first order thermodynamic transition given by

\[
T_m(H) = T_m^{2D} \left[ 1 + \frac{b^{1/\nu}}{ln^{1/\nu}(H/H_{cr})} \right],
\]

for \( H \) larger than a crossover field,

\[
H_{cr} \approx \frac{2\pi\phi_0}{\gamma^2d^2} \ln \left( \frac{\gamma d}{\xi_{ab}} \frac{1 + (4\pi\lambda_{ab})^2d^2}{2(\phi_0\xi_{ab})^2k_B^2T} \right).
\]

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At low magnetic fields, $H << H_{cr}$, it is well-established that there is a complex phase diagram for Bi-2212 with transitions on cooling from liquid vortex matter to a solid. At low temperature an increasing magnetic field drives a transition at $H^* \approx 0.1$ T from Bragg glass to vortex glass, indicated by an abrupt increase in the symmetry of the $\mu$SR spectrum,$^{2}$ a decrease in its second moment,$^{4} \gamma$ and disappearance of Bragg peaks in SANS. At this transition vortices lose coherence between planes. The resulting destructive interference between vortices on adjacent planes averages out the magnetic field distribution$^{26,27,28}$ that one might expect for straightline vortices such as are seen in the Bragg glass phase$^{2}$. This interference reduces both symmetry and linewidth in the $\mu$SR spectrum. With even larger fields the second moment of the $^{17}$O NMR spectrum, $\sigma(H)$, ($\approx$ linewidth squared) progressively increases and asymmetry is restored, until the spectrum linewidth collapses at 5 T. There are two possibilities for this anomalous behavior at 5 T. Either the transition is field-induced-ordering (ordering in-plane) or field-induced-disordering (further disorder between planes). The significant asymmetry in the spectrum in the high field phase compared to that at our lowest fields favors vortex ordering with increasing field. This scenario might follow if interplanar coupling is weakened with increasing field compared to intraplanar interactions, reducing frustration that originated from vortices in adjacent planes. As a consequence vortices order two-dimensionally and we observe the second moment decrease abruptly. At much larger fields, we can see that the two-dimensional vortex solid becomes progressively more disordered.

Experiments consistent with the two-dimensional melting theory have basic significance. But they are also relevant to applications of superconductivity at very high magnetic field. One of the most promising materials for magnet wires is Bi-2212. To achieve this goal there will be an upper limit on the operational temperature of the magnet determined by critical currents that are more easily stabilized in the vortex solid phase.

To make a comparison with straight line vortices we have performed a Ginzburg-Landau calculation$^{30}$ of the corresponding magnetic field distribution, Fig. 4. Our measurement is of a similar magnitude as expected from this calculation, although the GL approximation does not capture the details of the observed field dependence. In fact the transition from liquid to a solid in high magnetic fields is predicted to occur first to a supersolid phase and then at lower temperatures to a decoupled solid phase where defects in the vortex lattice become zero-dimensional$^{10,31}$. NMR techniques may be helpful in exploring these fascinating aspects of vortex behavior in strongly anisotropic superconductors.

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