Logical Inferences with Comparatives and Generalized Quantifiers

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Abstract

Comparative constructions pose a challenge in Natural Language Inference (NLI), which is the task of determining whether a text entails a hypothesis. Comparatives are structurally complex in that they interact with other linguistic phenomena such as quantifiers, numerals, and lexical antonyms. In formal semantics, there is a rich body of work on comparatives and gradable expressions using the notion of degree. However, a logical inference system for comparatives has not been sufficiently developed for use in the NLI task. In this paper, we present a compositional semantics that maps various comparative constructions in English to semantic representations via Combinatory Categorial Grammar (CCG) parsers and combine it with an inference system based on automated theorem proving. We evaluate our system on three NLI datasets that contain complex logical inferences with comparatives, generalized quantifiers, and numerals. We show that the system outperforms previous logic-based systems as well as recent deep learning-based models.

1 Introduction

Natural Language Inference (NLI), or Recognizing Textual Entailment (RTE), is the task of determining whether a text entails a hypothesis and has been actively studied as one of the crucial tasks in natural language understanding. In recent years, systems based on deep learning (DL) have been developed by crowdsourcing large datasets such as Stanford Natural Language Inference (SNLI) (Bowman et al., 2015) and Multi-Genre Natural Language Inference (MultiNLI) (Williams et al., 2018) and have achieved high accuracy. NLI datasets focusing on complex linguistic phenomena, such as negation, antonyms, and numerals, have also been developed (Naik et al., 2018).

However, it has been pointed out that these datasets contain various biases that can be exploited by DL models (Dasgupta et al., 2018; McCoy et al., 2019), including easily classifying numerical expressions in inference (Liu et al., 2019) and answering by only looking at a hypothesis (Gururangan et al., 2018). This suggests that the success of NLI models to date has been overestimated and that tasks remain unresolved.

To handle inferences involving various linguistic phenomena, there are also studies to probe the effects of additional training using artificially constructed data (Dasgupta et al., 2018; Richardson et al., 2020). However, in the case of structurally complex inferences involving comparisons and numerical expressions, there is a myriad of ways to combine possible inference patterns. For example, consider the following inference.

\[
\begin{align*}
P_1: & \text{ John is taller than 6 feet.} \\
P_2: & \text{ Bob is shorter than 5 feet.} \\
H: & \text{ Bob is not taller than John. (Yes)}
\end{align*}
\]

To correctly derive \( H \) from \( P_1 \) and \( P_2 \), it is necessary to capture the predicate-argument structures of the sentences, antonyms (tall, short), numerical expressions, and negation. Note that if the hypothesis sentence \( H \) is changed to \textit{John is not taller than Bob}, the correct answer is not an entailment (Yes) but rather a contradiction (No); even if numerical expressions are excluded, the number of combinations of sentence patterns that produces this kind of reasonable inference is enormous.

In another approach, unsupervised NLI systems based on various logics have been studied (Bos, 2008; MacCartney and Manning, 2008; Mineshima et al., 2015; Abzianidze, 2016). However, the accuracies of these systems on comparative constructions are relatively low (see Section 3). Although there have been detailed discussions in formal semantics taking into account the
complexity associated with adjectives and comparative expressions (Cresswell, 1976; Kennedy, 1997; Heim, 2000; Lassiter, 2017), such theories have not yet been implemented in NLI systems. Also, some logic-based NLI systems handle comparatives (Chatzikyriakidis and Bernardy, 2019; Haruta et al., 2019), but these systems do not implement a parser and/or a prover.

The goal of this study is to fill this gap by implementing a formal compositional semantics based on the so-called A-not-A analysis (Seuren, 1973; Klein, 1980, 1982; Schwarzschild, 2008), which maps various comparative constructions in English to logical forms (LFs) via CCG (Steedman, 2000) derivation trees. Based on this, we present an inference system that computes complex logical inference over comparatives, generalized quantifiers, and numerals. For evaluation, we use the FraCaS test set (Cooper et al., 1994), which contains various linguistically challenging inferences, and the Monotonicity Entailment Dataset (MED) (Yanaka et al., 2019), which contains inferences with generalized quantifiers. We also construct a new test set, the Comparative and Adjective Dataset (CAD), which extends FraCaS and collects both single-premise and multi-premise inferences with comparatives. The experiments show that our system outperforms previous logic-based systems as well as recent DL models.

2 System overview

Figure 1 shows the pipeline of the proposed system. First, the input sentences are a set of premises \( P_1, \ldots, P_n \) and a hypothesis \( H \). Next, the CCG derivation trees are obtained using CCG parsers.

![Figure 1: Overview of the proposed method. The premises and hypothesis are mapped to logical forms based on A-not-A analysis via CCG parsing and tree transformation; then a theorem prover judges yes, no, or unknown with the axioms for comparatives.](https://github.com/izumi-h/ccgcomp)

Derivation trees are modified to derive appropriate LFs based on A-not-A analysis. We use the semantic parsing system ccg2lambda (Martínez-Gómez et al., 2016) based on \( \lambda \)-calculus to obtain LFs, which are then converted to the Typed First-order Form (TFF) of the Thousands of Problems for Theorem Provers (TPTP) format (Sutcliffe, 2017), that is, a formal expression in first-order logic with equality and arithmetic operations. Finally, together with the axiom system Comp (Haruta et al., 2019) for comparatives and numerical expressions, a theorem prover checks whether \( P_1 \land \cdots \land P_n \rightarrow H \) holds or not. The system output is yes (entailment), no (contradiction), or unknown (neutral).

2.1 Degree semantics: A-not-A analysis

In formal semantics, comparative and other gradable expressions are usually analyzed using the notion of degree (Cresswell, 1976).

\[
\text{(2) a. Ann is taller than Bob.} \\
\text{b. John is 5 feet tall.} \\
\text{c. John is tall.}
\]

For example, the sentence (2a), in which the comparative form taller of the gradable adjective tall is used, compares the degree of height between two persons. (2b) is an expression that includes a specific height, which is the numerical expression 5 feet. (2c) is a sentence using the positive form of the adjective, which can be regarded as representing a comparison with some implicit standard value. In degree-based semantics, such gradable adjectives are treated as two-place predicates that have entity and degree (Cresswell, 1976). For instance, (2b) is analyzed as tall(John, 5 feet),...
where \( \text{tall}(x, \delta) \) is read as “\( x \) is at least as tall as degree \( \delta \)” (Klein, 1991).

We use A-not-A analysis of comparatives, which analyzes (3a) as (3b).

(3)  
\[
\begin{array}{c}
a. \ Ann \text{ is taller than Bob is.} \\
b. \exists \delta ( \text{tall}(ann, \delta) \land \neg \text{tall}(bob, \delta)) \\
\end{array}
\]

According to this analysis, (3a) is interpreted as saying that there exists a degree \( \delta \) of height that Ann satisfies, but Bob does not. As shown in the
figure in (3), this guarantees that Ann’s height is greater than Bob’s height. A-not-A analysis makes it possible to derive entailment relations between various comparative constructions in a simple way using first-order logic theorem provers.

Table 1 shows LFs for some example sentences using A-not-A analysis. Here, LFs can be divided into two patterns. The examples in (i) in Figure 1 belong to the first type, where the degree of an individual exceeds a certain degree. For example, the sentence (i-2) means that the height of John is greater than the height of Bob. The sentence (i-3) means that the number of Ann’s children exceeds the number of Bob’s children. Under our analysis, this type of sentence is mapped to formulas of the form \( \exists \delta (\cdots \land \cdots) \).

The second type includes the examples in (ii), which say that the degree of an individual is greater than or equal to a certain degree. For example, (ii-1) means that John’s height is greater than or equal to Bob’s height (Klein, 1982). The sentence (ii-3) means that the number of cookies John ate is 3 or more greater than the number of cookies that Bob ate; in other words, if Bob ate \( n \) cookies, then John ate at least \( n + 3 \) cookies. Sentences of type (ii) are mapped to formulas of the form \( \forall \delta (\cdots \rightarrow \cdots) \), as in Table 1.

### 2.2 Compositional semantics in CCG

In CCG, the mapping from syntax to semantics is defined by assigning syntactic categories to words (Steedman, 2000); the LF of a sentence is then compositionally derived using \( \lambda \)-calculus. However, there is a gap between the syntactic structures assumed in formal semantics and the output derivation trees of existing CCG parsers, i.e., statistical parsers trained on CCG-Bank (Hockenmaier and Steedman, 2007). For this reason, we modify the derivation trees provided by CCG parsers in post-processing. There are several types of modifications.

#### Syntactic features

The first modification is to add syntactic features to CCG categories. For example, in the default CCG trees, a nominal adjective (a tall, boy) has the category \( N/N \), while a predicate adjective (John is tall) has the category \( S_{adj} \setminus NP \). To provide a uniform degree semantics to both constructions, we rewrite \( N/N \) as \( N_{adj}/N \) for the category of nominal adjectives.

#### Multiword expressions

Compound expressions for comparatives and quantifiers are combined as one word, such as a few, a lot of, and at most.

#### Empty categories

We insert an empty category to systematically derive the LFs of the two patterns described in Table 1. The distinction between patterns (i) and (ii) can be controlled by an expression appearing in the adjunct position of an adjective phrase, for example, a degree modifier such as very or a numerical expression such as 2 cm.

| Pattern | Example                                                                 | Type               | LF                                                                 |
|---------|-------------------------------------------------------------------------|--------------------|----------------------------------------------------------------------|
| (i)     | 1. John is tall.                                                        | Positive           | \( \exists \delta (\text{tall}(\text{john}, \delta) \land (\delta > \theta_{\text{tall}}(U))) \) |
|         | 2. John is taller than Bob.                                             | Increasing         | \( \exists \delta (\text{tall}(\text{john}, \delta) \land \neg \text{tall}(\text{bob}, \delta)) \) |
|         | 3. Ann has more children than Bob.                                      | Numerical          | \( \exists \x (\text{child}(x) \land \text{have}(\text{ann}, x) \land \text{many}(x, \delta)) \)          |
|         |                                                                          |                    | \( \neg \exists \x (\text{child}(x) \land \text{have}(\text{bob}, x) \land \text{many}(x, \delta)) \) |
| (ii)    | 1. John is as tall as Bob.                                              | Equatives          | \( \forall \delta (\text{tall}(\text{bob}, \delta) \rightarrow \text{tall}(\text{john}, \delta)) \)   |
|         | 2. Mary is 2 inches taller than Harry.                                   | Differential       | \( \forall \delta (\text{tall}(\text{harry}, \delta - 2^\circ) \rightarrow \text{tall}(\text{mary}, \delta)) \) |
|         | 3. John ate 3 more cookies than Bob.                                     | Measure            | \( \forall \delta (\exists \x (\text{cookie}(x) \land \text{eat}(\text{bob}, x) \land \text{many}(x, \delta - 3))) \) |
|         |                                                                          |                    | \( \rightarrow \exists \x (\text{cookie}(x) \land \text{eat}(\text{john}, x) \land \text{many}(x, \delta)) \) |

Table 1: Semantic representation of comparative constructions based on A-not-A analysis
When such an adjunct expression does not appear, we insert an empty category \( \text{dgr} \) into the adjunct position, which is used to derive the desired LF compositionally. Figure 2 shows an example of a modified derivation tree containing an empty element \( \text{dgr} \) for increasing comparatives. Similarly, we use two other types of empty categories for quantifiers (e.g., as tall as) and the positive form.

### 2.3 Generalized quantifiers

The analysis of comparatives by the degree-based semantics described above can naturally be extended to generalized quantifiers. In the traditional analysis (Barwise and Cooper, 1981), generalized quantifiers such as many, few, more than, and most are analyzed as denoting a relation between sets. Alternatively, an analysis based on degree semantics has been developed, which represents expressions such as many and few as adjectives (Partee, 1988; Rett, 2018) and most as the superlative form of many (Hackl, 2000; Szabolcsi, 2010). We recast this alternative analysis in our degree-based semantics. Table 2 shows the LFs for some examples. We use the binary predicate \( \text{many}(x, n) \), which reads “\( x \) is composed of (at least) \( n \) entities”. Most \( A \) are \( B \) is analyzed as meaning “More than half of \( A \) is \( B \)”, following the standard truth-condition (Hackl, 2000).

### 3 Experiments

#### 3.1 Experimental settings

For CCG parsing, we use two CCG parsers, namely, C&C (Clark and Curran, 2007) and depcg (Yoshikawa et al., 2017), to mitigate parsing errors. If two parsers output a different answer, we choose the system answer in the following way: if one answer is yes (resp. no) and the other is unknown, the system answer is yes (resp. no); if one answer is yes and the other is no, then the system answer is unknown. For POS tagging, we use the C&C POS tagger for C&C and spaCy\(^4\) for depccg.

To implement compositional semantics, we use ccg2lambda\(^4\). We extend the semantic templates proposed in Mineshima et al. (2015) to handle linguistic phenomena based on degree-based semantics. The total number of lexical entries assigned to CCG categories is 106, and the number of entries directly assigned to particular words (e.g., than and as for comparatives and items for quantifiers) is 214. For tree transformation, we use Tsurgeon (Levy and Andrew, 2006). We use 74 entries (rewriting clauses) in the Tsurgeon script. For theorem proving, we use Vampire\(^5\), which accepts TFF forms with arithmetic operations.

For evaluation, we use three datasets. First, FraCaS (Cooper et al., 1994) is a dataset comprising nine sections, each of which contains semantically challenging inferences related to various linguistic phenomena. In this study, we use three sections: Generalized Quantifiers (GQ; 73 problems), Adjectives (ADJ; 22 problems), and Comparatives (COM; 31 problems). The distribution of gold answer labels for the three sections is \( (yes|no|unknown) = (36/5/32), (9/6/7), (19/9/3) \), respectively.

Second, MED\(^6\) is a dataset that contains:

\(^4\)https://github.com/explosion/spaCy
\(^5\)https://github.com/mynlp/ccg2lambda
\(^6\)https://github.com/vprover/vampire
ferences with quantifiers (so-called monotonicity inferences). We use a subset (498 problems) of MED that does not require world knowledge and commonsense reasoning; these problems were collected from various linguistics papers. The distribution of the gold answer is (yes/unknown) = (215/283).

Because there are only 31 problems for comparatives in FraCaS, we created the CAD test set consisting of 105 problems, which focuses on comparatives and numerical constructions not covered by FraCaS. We collected a set of inferences (9 problems) from a linguistics paper (Klein, 1982) and created more problems by adding negation, using degree modifiers (e.g., very), changing numerical expressions, replacing positive and negative adjectives (e.g., large to small), and swapping the premise and hypothesis of an inference. Of the 105 problems 50 are single-premise problems, and 55 are multi-premise problems. The distribution of gold answer labels is (yes/unknown/unknown) = (50/17/38). All of the gold labels were checked by an expert in linguistics. Table 3 shows some example problems.

### 3.2 Results and discussion

#### FraCaS test suite

Table 4 shows the experimental results on FraCaS. *Majority* is the accuracy of the majority baseline and *Ours* the accuracy of our system. Some errors were caused by failing to assign correct POS tags and lemmas to comparatives; for example, cleverer is wrongly assigned NN rather than JJR (FraCaS-217). To estimate the upper bound of the accuracy of our system by reducing error propagation, we added hand-coded rules to assign correct POS tags and lemmas (14 words). We also added two rules to join multi-word expressions to derive correct logical forms (law lecturer and legal authority) for FraCaS-214, 215. In Table 4, +rule shows the improvement in accuracy realized by adding these rules.

We compare our system with previous logic-based NLI systems as well as three popular DL models. For logic-based systems, we use MN (Mi-neshima et al., 2015) and LP (Abzianidze, 2016) based on CCG parsers and theorem proving and NL (MacCartney and Manning, 2008) based on Natural Logic. NL is evaluated on single-premise problems only (indicated by *). Our system accepts both single-premise and multiple-premise problems and outperforms the previous logic-based systems on the comparatives sections. Our system solves complex reasoning problems with multiple premises involving comparatives and numerical expressions, such as FraCaS-235 in Table 3, for which the previous systems were unable to give a correct answer.

For DL models, LSTM is the performance of a long short-term memory model trained on SNLI, which is reported in Bowman (2016) (only evaluated on single-premise problems). We also tested the Decomposable Attention (DA) model (Parikh et al., 2016), a simple attention-based model trained on SNLI. We used the implementation provided in AllenNLP (Gardner et al., 2018). Finally, BERT is the performance of a BERT model (Devlin et al., 2019). We used the bert-base-cased model fine-tuned with MultiNLI. We used the code available at the orig-

| Table 3: Examples of entailment problems from the FraCaS, MED, and CAD test sets |
|---------------------------------|---------------------------------|---------------------------------|
| **Premise 1** | **Premise 2** | **Hypothesis** |
| ITEL won ten orders. | ITEL won more orders than APCOM. | ITEL won at least eleven orders. |
| **Premise 1** | **Hypothesis** |
| No more than fifty campers have caught a cold. | Chris is taller than Alex is. |
| **Premise 1** | **Hypothesis** |
| Alex is not as tall as Chris is. | Chris is taller than Alex is. |
| **Premise 1** | **Premise 2** | **Hypothesis** |
| John is taller than Bob. | John is taller than Bob. | John is taller than Bob. |

| Table 4: Accuracy on the FraCaS test suite: ‘#All’ shows the number of all problems and ‘#Single’ the number of single-premise problems |
|---------------------------------|-----------------|-----------------|-----------------|
| **Section** | **GQ** | **ADJ** | **COM** |
| **#All** | 73 | 22 | 31 |
| **#Single** | 44 | 15 | 16 |
| **Majority** | .48 | .39 | .61 |
| **Logic** | | | |
| MN | .77 | .68 | .48 |
| LP | .93 | .73 | - |
| NL | .98* | .80* | .81* |
| Ours | .92 | .86 | .77 |
| +rule | .95 | .95 | .84 |
| **DL** | | | |
| LSTM | .64* | .47* | .56* |
| DA | .59 | .45 | .61 |
| BERT | .64 | .45 | .58 |
Our system outperforms the three DL models by large margins.8

MED and CAD datasets Table 5 shows the results on MED and CAD. For MED, we compared our system with a BERT model fine-tuned with MultiNLI (BERT) and a BERT model with data augmentation (approximately 36K) in addition to MultiNLI (BERT+), both being tested in Yanaka et al. (2019). For CAD, we evaluated DA and BERT. The results show that our system achieved high accuracy on the logical inferences with adjectives, comparatives, and generalized quantifiers.

Table 6 shows examples that were solved by our system but not by DA and BERT. The DL models were particularly difficult to handle inferences related to antonyms (e.g., FraCaS-209) and numerical expressions (e.g., CAD-001). Indeed, the results on the DL models were predictable because these models were trained on datasets (SNLI and MultiNLI) that do not target the logical and numerical inferences we are concerned with in this study. However, it is fair to say that it is very challenging to generate effective training data to handle various complex inferences with comparatives, numerals, and generalized quantifiers.

There were some problems that our system could not solve. For FraCaS, the accuracy for the comparative section (COM) was relatively low (.84). This is because this section contains linguistically challenging phenomena such as clausal comparatives (FraCaS-239, 240, 241) and attributive comparatives (FraCaS-244, 245). For MED, the present system does not handle downward monotonic quantifiers (e.g., less than), non-monotonic quantifiers (e.g., exactly), and negative polarity items (e.g., any). Furthermore, the system needs to be extended to deal with linguistic phenomena such as comparative subdeletion and quantified comparatives that appear in CAD. To address these problems, further improvement of the CCG parsers will be needed.

4 Conclusion

In this study, we presented an end-to-end logic-based inference system for handling complex inferences with comparatives, quantifiers, and numerals. The entire system is transparently composed of several modules and can solve complex inferences for the right reason. In future work, we will extend our analysis to cover the more complex constructions mentioned in Section 3. We are also considering combining our system with an abduction mechanism that uses large knowledge bases (Yoshikawa et al., 2019) for handling commonsense reasoning with external knowledge.

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