Evidence of Long Two-Dimensional Folding Chain Structure Formation of Poly(vinylidene fluoride) in N-Methylpyrrolidone Solution: Total Form Factor Determination by Combining Multiscattering Data

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INTRODUCTION

Very recently, we carried out small- to wide-angle X-ray scattering (S-WAXS) and static light scattering (SLS) experiments in poly(vinylidene fluoride) (PVDF) solutions dissolved in N-methylpyrrolidone (NMP) to investigate the conformation and structure of PVDF depending on its weight average molar mass. Although many macromolecular scientists believe that a random coil like conformation of PVDF samples exists in NMP solution as usually observed in other ordinary synthetic polymer solutions, the obtained S-WAXS and SLS data strongly suggested the presence of long rigid rectangular columnar particles formed by the two-dimensionally developing planar particle structure describable in a high concentration range. The obtained ΔI(q) data were determined by using (d)NMP as a solvent. An increase in even under dilute conditions at concentrations less than the overlapping concentrations due to the quite high neutron scattering contrast obtained by using (d)NMP as a solvent. An increase in Mw from 100 to 1200 kg mol⁻¹ substantially increases the particle length and width from L = 80 to 350 nm and w₁ = 5.0 to 15 nm, respectively, while the thickness, w₂, is maintained at 0.3 nm. Since L is much longer than w₂ irrespective of Mw, the particles formed by PVDF molecules in NMP simply behave as long rigid rods in a scattering vector (q) range covered by SLS measurements. A combination study of S-WANS and S-WAXS experiments covering a higher q range with the SLS techniques could clearly reveal increases in both the L and w₂ values with increasing Mw.

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poorly scattered and the determined local particle size parameters from $\Delta I_0(q)$ data contain uncertainty. In particular, the spacing length existing in the formed two-dimensional folding chain structure estimated from the rather broad shoulder found in the $\Delta I_0(q)$ data of the S-WAXS experiments should be refined using other experimental techniques that possess high sensitivity even at concentrations lower than the overlapping concentrations roughly described by the reciprocal of the intrinsic viscosity $(\eta_p)^{-1}$.

It is well known that small- to wide-angle neutron scattering (S-WANS) techniques possess sufficient high sensitivity even under dilute conditions in combined systems between deuterated solutes and usual (protonated) solvents or those between ordinary solutes and deuterated solvents due to high scattering contrasts for neutrons because of a difference in scattering length densities between deuterium and proton atoms.4,5 Because fortunately deuterated NMP ((d)NMP) is commercially available, we decided to perform S-WANS measurements in (d)NMP solutions of PVDF samples, which were subjected to S-WAXS experiments in a previous study,1 to confirm the presence of two-dimensional planar particles formed by the folding chain structure in the (d)NMP solution. The substantial difference in scattering length densities between deuterium atoms in (d)NMP and proton atoms in PVDF would provide more obvious scattering signals due to the spacing present in the formed two-dimensional folding chain structure than the broad shoulder observed in the previous S-WAXS experiments.1 The overall particle structure formed by PVDF samples in NMP solution can be clarified in more detail by combining the results of SLS, S-WAXS, and viscometric experiments in a previous study and those of S-WANS experiments obtained in this study.

PVDF is one of the most important materials to make cathode binder parts contained in many commercial lithium ion secondary batteries, and NMP solutions of PVDF with various $M_w$ values have been practically used in the manufacturing process of cathode binder formation.6–9 PVDF has also been used as a useful polymeric material to develop mechanoelectrical devices due to its unique characteristics such as ferroelectricity, piezoelectricity, and pyroelectricity demonstrated in the solid state effectively caused by the presence of an all-trans zigzag conformation ($\beta$-phase or form I) of PVDF chains.9,10 Moreover, the content of the $\beta$-phase is effectively controllable in the solvent casting process from PVDF solutions.11–14 Therefore, a full understanding of the structure and conformation of PVDF in solution would lead to a breakthrough in processing procedures of new-type lithium ion secondary batteries and mechanoelectrical device manufacturing. Then, we complete a detailed discussion of the change in the structure and conformation of PVDF samples dissolved in NMP and (d)NMP depending on $M_w$ based on the newly obtained data from S-WANS techniques.

![Figure 1. Comparison between $\Delta I_0(q)c^{-1}$ data obtained from S-WANS experiments and $k\Delta I_0(q)c^{-1}$ data obtained from S-WAXS experiments in a previous study1 for PVDF100 (a) and PVDF1200 (b) solutions dissolved in (d)NMP (S-WANS) and NMP (S-WAXS), respectively. The numerical $k$ values used are identical to each other in both figures.](image)

### EXPERIMENTAL SECTION

**Materials.** Two PVDF samples with different $M_w$ values of 100 and 1200 kg mol$^{-1}$, coded PVDF100 and PVDF1200, were kindly supplied by Kureha Corporation (Tokyo) and used without any further purification processes. Precise molar mass distribution information for these samples is not provided by the company; however, the polydispersity indices ($M_w/M_n$) are reported to be approximately 2.0. (d)NMP (>98% in chemical purification and >99% in deuterium enrichment) was purchased from Cambridge Isotope Laboratories, Inc. (Tewksbury) and was used as a solvent to prepare PVDF solutions for S-WANS experiments. The concentrations ($c$) of PVDF solutions were set at $1.0 \times 10^{-2}$ and $5.0 \times 10^{-3}$ g mL$^{-1}$ for PVDF100 and at $3.0 \times 10^{-3}$ and $1.5 \times 10^{-3}$ g mL$^{-1}$ for PVDF1200 samples. To prevent molecular contacts or overlapping in the prepared solutions, such concentrations lower than the reciprocals of intrinsic viscosities $(\eta_p)^{-1}$, ca. $1.5 \times 10^{-2}$ g mL$^{-1}$ for PVDF100 and ca. $3.4 \times 10^{-3}$ g mL$^{-1}$ for PVDF1200, were chosen. Although extrapolation procedures of the concentration, $c \to 0$, for scattering intensities were necessary to determine form factors of dissolved PVDF molecules precisely, the permitted beam time was strictly limited. Thus, we chose the concentrations to obtain enough scattering intensities to be analyzed without PVDF molecule overlapping.

**Methods.** S-WANS experiments were performed using a small-angle neutron scattering instrument (TAIKAN)15 installed in the neutron beamline, BL15, at the Materials and Life Science Experimental Facility (MLF) in Japan Proton Accelerator Research Complex, J-PARC, (Tokai). The covered magnitude range of the scattering vector ($q$) ranged from $7.0 \times 10^{-3}$ to $1.0 \times 10^{0}$ nm$^{-1}$. A banjo-type quartz cell with a neutron path length of 2.0 mm was used as an exposure sample cell. The exposure time of a neutron beam was 2 h for each sample solution and 1 h for the solvent (d)NMP. The
measuring temperature was set at 25 °C for all the S-WANS experiments. The obtained scattering intensities were converted to absolute values using the standard material “glassy carbon”, for which absolute scattering values had been precisely determined.

## RESULTS AND DISCUSSION

### Comparison between the S-WANS & S-WAXS Data.

Excess neutron scattering intensities (\(\Delta I_N(q)\)) for each sample solution were evaluated as functions of \(q\) via the equation

\[
\Delta I_N(q) = I_S(q) - I_{Solv}^{\text{coh}}(q) - I_S^{\text{incoh}}(q),
\]

where \(I_S(q), I_S^{\text{coh}}(q),\) and \(I_S^{\text{incoh}}(q)\) are the scattering intensity of a tested sample solution, that of the solvent, \((d)\text{NMP},\) and the \((s)\) \(q\) independent incoherent component, respectively. The concentration normalized excess scattering intensity, \(\Delta I_N(q) q^{-1}\), for each tested sample was used for the consideration of the local structures in the particles formed by the PVDF samples in \((d)\text{NMP}\) solution.

The S-WANS experiments performed in this study covered almost the same \(q\) range as the S-WAXS experiments in a previous study.1 Figure 1 shows the comparison between the \(q\) dependence profiles of the determined \(\Delta I_N(q) q^{-1}\) data and those obtained by S-WAXS experiments, \(\Delta I_N(q) q^{-1}\), in a previous study.1 Although the \(\Delta I_N(q) q^{-1}\) data were converted into absolute values, the \(\Delta I_N(q) q^{-1}\) data obtained by S-WAXS were not converted. However, the \(q\) dependencies can be compared between the two data obtained by different methods for the same PVDF samples. Moreover, because the data were normalized by the concentration, \(c\), the intensities are also comparable with each other. A numerical constant \((k)\) was found, which can reasonably superpose \(k\Delta I_N(q) q^{-1}\) on the \(\Delta I_N(q) q^{-1}\) data in a \(q\) range lower than 1.0 nm\(^{-1}\). Then, Figure 1a was traced out employing the found \(k\) value. The same \(k\) value used in Figure 1a was also used to make Figure 1b. Because reasonable agreement between the \(k\Delta I_N(q) q^{-1}\) and \(\Delta I_N(q) q^{-1}\) data is also recognized in the \(q\) range less than 1.0 nm\(^{-1}\) in Figure 1b, we might conclude that both the S-WAXS and S-WANS behaviors are essentially identical to each other in the \(q\) range not only the dependence on \(q\), but also that on \(c\).

Because the \(q\) dependencies of the \(\Delta I_N(q) q^{-1}\) (and, of course, \(k\Delta I_N(q) q^{-1}\)) data for the PVDF100 sample are obviously different from those for the longer PVDF1200 sample, the local structures of the formed particles in these PVDF sample solutions are substantially different from each other, as discussed in a previous study.1 The \(q\) dependence in the PVDF100 system changes from \(\Delta I_N(q) q^{-1} \propto q^{-1}\) to \(\Delta I_N(q) q^{-1} \propto q^{-2}\) at \(q \approx 0.4\) nm\(^{-1}\) as seen in Figure 1a, while the \(q\) value where the \(q\) exponent alters from \(-2\) to \(-1\) seems to shift to a lower \(q\) value close to \(0.1\) nm\(^{-1}\) in the PVDF1200 system as recognized in Figure 1b.

According to theoretical predictions, the relationship \(\Delta I_N(q) q^{-1} \propto q^{-1}\) is the characteristic behavior of a rod-like structure, and \(\Delta I_N(q) q^{-1} \propto q^{-2}\) is the characteristic behavior of both random coil and plate-like structures.1,14,17 In the case of semiflexible chains such as polymeric samples, the former relationship is always observed in a \(q\) range higher than that in which the latter relationship is observed.1,14,15,19 The opposite \(q\) range order found in the PVDF systems to the behavior of semiflexible polymer chains strongly suggests that PVDF samples form flat plate particles responsible for the \(q\) exponent of \(-2\) in the higher \(q\) range, and one side length of the formed plates mainly elongates with increasing \(M_w\) values, maintaining its thickness at a constant value similar to long rigid rods, which show a \(q\) exponent of \(-1\) for \(\Delta I_N(q) q^{-1}\) in a lower \(q\) range. Such a \(q\) dependence is well described by the particle form factor \((P(q))\) of a rectangular column with length \((L)\), minor width \((w_1)\) corresponding to the particle thickness, and major width \((w_2 > w_1)\), as schematically depicted in Figure 2a.1

The presence of a broad interference peak at \(\delta^{***} \approx 4.5\) nm\(^{-1}\) is more clearly observed in the data of the S-WANS experiments than that of the S-WAXS experiments,1 showing much broader shoulders in a \(q\) range from 3 to 5 nm\(^{-1}\) as seen in Figure 1a,b. Although we roughly estimated the spacing distance \((d^{***})\) corresponding to the small shoulder to be ca. 2.0 nm in the previous study, the clearer peaks observed at ca. 4.5 nm\(^{-1}\) in the \(\Delta I_N(q) q^{-1}\) data permit one to determine the spacing to be \(d^{***} (= 2\pi/\delta^{***}) \approx 1.4\) nm. Considering the antiparallel alternating arrangement of extended PVDF chain parts in an all-trans conformation in NMP solution. The picture described in panel (b) corresponds to the expansion of a small portion enclosed with dotted lines in panel (a). Figure 2. (a) Schematic depiction of a possible particle shape, i.e., a rectangular column with length \((L)\), minor width \((w_1)\) corresponding to the particle thickness, and major width \((w_2 > w_1)\), responsible for the \(q\) dependence observed in both the S-WANS and S-WAXS experiments. (b) Two-dimensional folding chain structure constructed by the antiparallel alternating arrangement of extended PVDF chain parts in the all-trans conformation in NMP solution. The picture described in panel (b) corresponds to the expansion of a small portion enclosed with dotted lines in panel (a).

An interference peak found at \(\delta^{**} \approx 25\) nm\(^{-1}\) in the previous S-WAXS experiments1 as observed in Figure 1a,b, which corresponds to a spacing distance between adjacent vinylidene groups in the all-trans conformation, i.e., \(d^{**} (= 2\pi/\delta^{**}) \approx 0.25\) nm, was not as clearly observed in the S-WANS experiments as in the previous S-WAXS data.1 Weak excess scattering intensities due to low concentrations to reach the isolated polymer chain condition without contacts between PVDF particles employed in this study are one of the reasons for the difficulty in observing the peak at approximately 25 nm\(^{-1}\). It is possible that this interference peak is essentially more sensitively detectable by X-ray scattering than neutron scattering.

### Total Form Factors of PVDF Molecules.

The total form factors, \(P(q)\), for the tested PVDF molecules are now available, which can describe the \(q\) dependencies of the determined excess scattering intensities over the entire \(q\) range covered by SLS, S-WANS, and S-WAXS experiments from \(7 \times 10^{-2}\) to \(4 \times 10^{-1}\) nm\(^{-1}\) and are responsible for the overall structure and conformation of the PVDF molecules. According to the standard SLS theory,1,16,17,20 the intrinsic concentration-reduced
excess Rayleigh ratios determined at $c = 0$ g mL$^{-1}$ using the extrapolation procedures, $R_0$ ($Kc)^{-1}c=0$ where $K$ is an apparatus-dependent constant, are identical to $M_\infty P(q)$. On the other hand, a proportional constant connecting the $c$ independent $\Delta I_0(q)c^{-1}$ value as obtained in this study with $P(q)$, such as $M_w$ in the SLS theory, exists and must be proportional to $M_w^{-1}$. Then, the relationship $R_0$ ($Kc)^{-1}c=0 = m\Delta I_0(q)c^{-1}$ holds with a certain proportional constant $m$, which is independent of $M_w$ and can be determined under various experimental conditions.

Using the constant value of $m = 1.7 \times 10^4$ cm$^{-2}$ g$^{-2}$ mol$^{-1}$, the $\Delta I_0(q)c^{-1}$ data of PVDF100 ($c = 0.01$ g mL$^{-1}$) and PVDF1200 ($c = 0.003$ g mL$^{-1}$) were combined to the $R_0$ ($Kc)^{-1}c=0$ data obtained using SLS techniques in a previous study$^1$ and shown in Figure 3a. The solid and broken lines seen in Figure 3a represent $M_\infty P(q)$ curves for the PVDF samples determined previously assuming rectangular columns possessing $L = 80$, $w_2 = 5.0$, and $w_1 = 0.3$ nm for PVDF100 and $L = 350$, $w_2 = 15.0$, and $w_1 = 0.3$ nm for PVDF1200. The $q$ dependencies of these form factors, $P(q)$, for rectangular column particles$^{21}$ were precisely calculated via multipurpose open source software SasView,$^{22}$ which is useful for various kinds of scattering data analyses.$^4$ The $m\Delta I_0(q)c^{-1}$ data of both PVDF samples are smoothly linked to the $R_0$ ($Kc)^{-1}c=0$ data, and the $M_\infty P(q)$ lines reproduce the $q$ dependencies of both the $R_0$ ($Kc)^{-1}c=0$ and $m\Delta I_0(q)c^{-1}$ data over almost the entire $q$ range examined except for the interference signals observed at ca. 4.5 nm$^{-1}$ as seen in Figure 3a. These observations strongly suggest that the assumed rectangular columnar form factors, $P(q)$, obtained by combining scattering data obtained by using the S-WANS, S-WAXS, and SLS techniques, reasonably satisfy the essential characteristics of the particles formed by the PVDF samples with different $M_w$ values and reasonably behave as the total form factors.

Figure 3b shows the $q$ dependencies of $qR_0$ ($Kc)^{-1}c=0$ and $qm\Delta I_0(q)c^{-1}$ data, so called the Holzer plot,$^{23}$ for the PVDF solutions shown in Figure 3a. If the formed particles have the rigid rod structures, $qR_0$ ($Kc)^{-1}c=0$ and $qm\Delta I_0(q)c^{-1}$ data clearly show plateaus in the $q$ range of $R_g^{-1} < q < R_c^{-1}$, where $R_c$ is the cross-sectional radius of the formed rods. The height of the observed plateau theoretically means $\pi M_w/L$ corresponding to the weight average mass per unit length of the rods.$^2$ The plateau values observed in Figure 3b, 3.8 and 10 kg mol$^{-1}$nm$^{-1}$, respectively, in a $q$ range of $R_g < q < (0.5w_1)^{-1}$ (instead of $R_c^{-1}$ for rigid rods) reasonably agree with the $\pi M_w/L$ values, 3.9 and 11 kg mol$^{-1}$nm$^{-1}$, for each PVDF sample. Because the formed rectangular columnar particles of PVDF samples in NMP solutions have an $L$ much longer than the width $w_1$, such an argument based on the rigid rod particle structure seems to hold approximately.

The highly elongated rectangular columnar particle structure resulting from the determined form factor provides the $M_w$ dependence of the intrinsic viscosity, $[\eta]$, calculated via a widely accepted theoretical model for rigid rods$^{24,25}$ suspended in a liquid medium, which reasonably agrees with experimental results.$^1$ This strongly supports the validity of the form factor determined through combining multidata obtained from the S-WANS, S-WAXS, and SLS techniques in this study.

### CONCLUSIONS

Combining the data obtained by small- to wide-angle neutron scattering, S-WANS, small- to wide-angle X-ray scattering, S-WAXS, and static light scattering, SLS, experiments realized the total form factor determination for poly(vinylidene fluoride), PVDF, samples dissolved in N-methylpyrrolidone, NMP (and (d)NMP), which can reasonably describe the structure and conformation of particles formed by PVDF molecules in the solution. PVDF molecules form elongated rectangular columnar-shape particles in NMP solution. The elongated PVDF molecules approximately in the all-trans conformation are sequentially arrayed in the antiparallel manner of electric dipole moments due to the presence of fluoride atoms in the NMP solution. The two-dimensional folding structure formed by a PVDF chain resembles a long rectangular column possessing length $L$, major width $w_2 (< L)$, and minor width (thickness) $w_1 (< w_2)$. The values of $L$ and $w_2$ increase with increasing $M_w$, while $w_1$ remains at a constant value of approximately 0.3 nm irrespective of $M_w$.  

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**Figure 3.** $q$ dependencies of combined $R_0$ ($Kc)^{-1}c=0$ data previously obtained using SLS techniques$^1$ and $m\Delta I_0(q)c^{-1}$ data (a) and $qR_0$ ($Kc)^{-1}c=0$ and $qm\Delta I_0(q)c^{-1}$ data (b) for PVDF100 ($c = 0.01$ g mL$^{-1}$) and PVDF1200 ($c = 0.003$ g mL$^{-1}$) solutions dissolved in NMP (SLS) and (d)NMP (S-WANS). The same constant value of $m = 1.7 \times 10^4$ cm$^{-2}$ g$^{-2}$ mol$^{-1}$ was used to produce the combined data. The solid and broken lines represent the $q$ dependencies of the total form factors, $P(q)$, of rectangular columnar$^2$ proposed for particles formed by PVDF samples with different $M_w$ values examined in this study. The size parameters, $L$, $w_1$, and $w_2$ used to calculate $P(q)$ are listed in the figure.
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The authors declare no competing financial interest.

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