Radio Variability from a Quiescent Stellar-mass Black Hole Jet

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Abstract

Relativistic outflows are believed to be a common feature of black hole X-ray binaries (BHXBs) at the lowest accretion rates, when they are in their “quiescent” spectral state. However, we still lack a detailed understanding of how quiescent jet emission varies with time. Here we present 24 yr of archival radio observations (from the Very Large Array and the Very Long Baseline Array) of the BHXB V404 Cygni in quiescence (totaling 150 observations from 1.4 to 22 GHz). The observed flux densities follow lognormal distributions with means and standard deviations of \( \langle \log f_r \rangle, \sigma_{\log f_r} = (0.53, 0.19) \) and \( (0.53, 0.30) \) at 4.9 and 8.4 GHz, respectively (where \( f_r \) is the flux density in units of mJy). As expected, the average radio spectrum is flat with a mean and standard deviation of \( \langle \alpha \rangle, \sigma_{\alpha} = (0.02, 0.65) \), where \( f_r \propto \nu^\alpha \). We find that radio flares that increase the flux density by factors of 2–4 over timescales as short as \(<10 \text{ minutes} \) are commonplace, and that long-term variations (over 10–4000 day timescales) are consistent with shot-noise impulses that decay to stochastic variations on timescales \(<10 \text{ days} \) (and perhaps as short as tens of minutes to several hr). We briefly compare the variability characteristics of V404 Cygni to jetted active galactic nuclei, and we conclude with recommendations on how to account for variability when placing quiescent BHXB candidates with radio luminosities comparable to V404 Cygni \( (L_R \approx 10^{28} \text{ erg s}^{-1}) \) onto the radio/X-ray luminosity plane.

Key words: accretion, accretion disks – stars: black holes – stars: individual (V404 Cygni) – X-rays: binaries

Supporting material: machine-readable table

1. Introduction

Black hole X-ray binaries (BHXBs) that accrete at low Eddington ratios \( \langle \lesssim 0.01 \rangle \) are associated with compact radio emission from partially self-absorbed synchrotron jets (Blandford & Königl 1979; Fender 2001; Remillard & McClintock 2006). These relativistic outflows provide channels for accretion flows to shed angular momentum and transport energy out to large distances (e.g., Meier 2001; Fender & Muñoz-Darias 2016; Romero et al. 2017; Douna et al. 2018). Radio observations of relativistic jets are therefore crucial for understanding how matter is transported through and away from accretion flows with low-mass accretion rates.

The most weakly accreting black holes reside in the “quiescent” spectral state, which we define here by a soft X-ray spectrum that can be characterized by a power-law photon index \( \Gamma \sim 2.1 \) (e.g., Tomsick et al. 2001; Kong et al. 2002; Corbel et al. 2006; Plotkin et al. 2013; Reynolds et al. 2014). Most BHXBs spend the majority of their time in quiescence, which usually corresponds to \( (0.5–10 \text{ keV}) \) X-ray luminosities \( L_X \lesssim 10^{26}–10^{27} \) \( L_\text{Edd} \) (Plotkin et al. 2013, 2017). In quiescence, a large fraction of the radiative power emitted by the accretion flow/jet system appears to be emitted in the radio waveband (e.g., Fender et al. 2003; Corbel et al. 2013; Gallo et al. 2018; although see Yuan & Cui 2005 for a prediction otherwise). This increased dominance of radio emission implies that the radio domain can be effective for discovering quiescent BHXBs (Maccarone 2005; Fender et al. 2013), which would produce less-biased samples of BHXBs in the Milky Way compared to the traditional method of discovering BHXBs through X-ray emission during an outburst.

Coordinated radio and X-ray surveys are indeed starting to reveal candidate BHXBs in Milky Way globular clusters (Strader et al. 2012; Chomiuk et al. 2013; Miller-Jones et al. 2015; Shishkovsky et al. 2018) and in the field (Tetarenko et al. 2016). Such an approach is highly complementary to other strategies for discovering quiescent BHXBs through, e.g., Hα surveys (Casares 2018), X-ray surveys (e.g., Agol & Kamionkowski 2002; Jonker et al. 2014), and optical spectroscopic searches capable of discovering nonaccreting black hole candidates in detached binary systems (Giesers et al. 2018; Thompson et al. 2018).

At the moment, even our most sensitive radio facilities are only capable of probing the tip of the quiescent BHXB population. We have currently detected radio emission from only four nearby quiescent BHXBs \( (\lesssim 4 \text{ kpc}) \), including one of the most luminous known quiescent systems, V404 Cygni \( (L_R \approx 10^{28} \text{ erg s}^{-1} \) at 5 GHz; Hynes et al. 2004; Gallo et al. 2005; Rana et al. 2016) and three of the least luminous known systems \( (A0620–00, \text{ XTE J1118+480}, \text{ and \ MWC 656}; L_R \approx 10^{26} \text{ erg s}^{-1}); \text{ Gallo et al. 2006, 2014}; \text{ Dzib et al. 2015}; \text{ Ribó et al. 2017}; \text{ Dinger et al. 2018}) \). Thus, we are still establishing the empirical properties of quiescent BHXB radio jets, which is an essential step for eventually defining reliable radio-based selection criteria.

To help inform future radio surveys, this paper focuses on quantifying the radio variability characteristics of quiescent

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\(^5\) The photon index \( \Gamma \) is defined by \( N_E \propto E^{-\Gamma} \), where \( N_E \) is the photon number density per unit energy, \( E \).
jets. Understanding that variability level is important, as (i) it would establish whether radio variability can discriminate quiescent BHXBs from other classes of radio-emitting objects, and (ii) it would help determine how close in time radio observations must be coordinated with other multiwavelength data.

To open the quiescent radio time domain, we focus on V404 Cygni, which represents the luminous end of the quiescent BHXB population. Containing a dynamically confirmed black hole \((9.0^{+0.6}_{-0.5} \, M_\odot)\) orbiting a K3 III companion (Kharghoria et al. 2010) in a long \(6.473 \pm 0.001\) day orbit (Casares et al. 1992), V404 Cygni was the first transient BHXB to have an unambiguous X-ray detection in quiescence \((4 \times 10^{33} \text{ erg s}^{-1}\) from 0.2 to 2.4 keV with the ROSAT satellite; Wagner et al. 1994). It also has a well-established distance \((2.39 \pm 0.14\) kpc) from radio parallax measurements (Miller-Jones et al. 2009) that has also been measured in the optical (albeit with poorer precision) by Gaia (Gaia Collaboration et al. 2018). Crucially, there already exist \(\approx 10^3\) radio observations of V404 Cygni in the Very Large Array (VLA) archive dating back to the 1990s. It is the only quiescent BHXB with such a rich radio data set (the next best-sampled quiescent BHXBs are AO620–00 and MWC 656, each of which have two to three published radio detections; Gallo et al. 2006; Dzib et al. 2015; Ribó et al. 2017; Díncer et al. 2018). However, the full VLA archive has yet to be synthesized into a single variability study. The quiescent X-ray variability characteristics of V404 Cygni have already been well quantified from minute through month timescales (e.g., Wagner et al. 1994; Hynes et al. 2004; Bradley et al. 2007; Bernardini & Cackett 2014; Rana et al. 2016), making V404 Cygni ripe for radio–to–X-ray comparisons.

In this paper, we reanalyze all observations of V404 Cygni in quiescence with the VLA through 2015, and we also consider 14 observations with the Very Long Baseline Array (VLBA). We describe our data reduction in Section 2. In Section 3, we describe the flux density variability characteristics on long (days to decades) and short (minutes to hours) timescales, and we explore radio spectra on long and short timescales. We discuss the radio jet properties in Section 4, and in Section 5, we provide recommendations on how to combat radio variability when coordinating multiwavelength observing campaigns on quiescent BHXBs and on BHXB candidates at luminosities comparable to V404 Cygni.

2. Archival Observations and Data Analysis

During the VLA era, V404 Cygni has undergone two major outbursts, the first discovered on 1989 May 22 (Makino 1989) and the second on 2015 June 15 (Barthelmy et al. 2015; Kuulkers et al. 2015; Negoro et al. 2015; Younes 2015). After the main 2015 outburst ended in July (see next paragraph), renewed X-ray activity was observed on 2015 December 21 (Malyshev et al. 2015), and V404 Cygni went through a mini-outburst that lasted \(\sim 30\) days (see, e.g., Kimura et al. 2017; Muñoz-Darias et al. 2017; Tetarenko et al. 2019).

For the 2015 outburst, from Plotkin et al. (2017), we consider that V404 Cygni reentered quiescence around 2015 July 23, based on when the X-ray spectrum finished softening from \(\Gamma \sim 1.6\) to 2.0–2.1 (see their Figure 1 and Table 3). We therefore exclude VLA observations on or before July 23 in this study, but we include VLA observations after July 23 (four total). Since the X-ray characteristics after July 23 appear similar to those before the outburst, we infer that the physical properties of the underlying accretion flow are no different during these 2015 observations compared to pre-outburst (and, by extension, we do not expect physical differences in the radio jet pre- and post-outburst). We therefore include these four observations from 2015 for completeness. However, out of caution, we generally use different symbols/colors to mark the post-outburst observations in figures within this manuscript, and we often remove the post-outburst observations from statistical tests. We do not include any data during or after the 2015 mini-outburst.

The 1989 outburst lasted much longer than the 2015 outburst (e.g., Tetarenko et al. 2019). Similar-quality X-ray spectral coverage of the transition into quiescence is not available from 1989, making it difficult to pinpoint when V404 Cygni reentered quiescence. Han & Hjellming (1992) monitored the 1989 outburst and decay with the VLA for 2 yr, and from their Table 1, the 4.9 and 8.4 GHz flux densities remained brighter than 1 mJy even as late as 1990 September, perhaps indicating elevated accretion (for reference, typical flux densities between outbursts were 0.2–0.4 mJy; e.g., Gallo et al. 2005; Hynes et al. 2009; Rana et al. 2016). We suspect that only the final two epochs in Han & Hjellming (1992) might represent the source in quiescence (taken on 1991 January 31 and May 31), but we cannot be certain. We therefore conservatively exclude all epochs already reported by Han & Hjellming (1992) from our study, and we begin our data set with a VLA epoch taken on 1991 September 25. However, we stress that none of our results are (qualitatively) affected if we include the final two epochs from Han & Hjellming (1992).

We found a total of 129 observations over five observing frequencies from 1.4 to 22.5 GHz taken with the historical VLA, i.e., before the VLA was upgraded and rededicated as the Karl G. Jansky VLA in 2012. The majority of these data are at 8.4 GHz (86 observations). We also found five observations with the upgraded VLA from 4 to 8 GHz and four taken from 8 to 12 GHz. We also include 14 observations with the VLBA at 5.0 GHz (13 observations in 2014) and 8.4 GHz (1 observation in 2008). A summary of observations is provided in Table 1, and a catalog of flux densities is given in Table 2. Note that there are two observations at 8.4 GHz for which we could not obtain good calibration solutions. We include entries for those observations in our catalog (Table 2) for completeness, but we have omitted them from the tally of observations in Table 1. In total, we measure flux densities (or limits) for 150 observations.

2.1. Historical VLA

The vast majority of data from the historical VLA were obtained through campaigns led by either Robert Hjellming or Michael Rupen. All observations were taken in continuum mode using two 50 MHz wide spectral windows. We reduced historical VLA observations following standard procedures within the Astronomical Image Processing System (AIPS) version 31DEC14 (Greisen 2003). We set the flux scale (using either 3C 48 or 3C 286) with the task SETJY and (time-dependent) Perley & Butler (2013) coefficients. The complex gain solutions were then solved using scans of a secondary point-source calibrator (usually J2025+337, although see Table 2 for exceptions), and the flux scale was bootstrapped from the primary calibrator using the task GETJY. Primary flux calibrator scans were not included for 24 observations. For those epochs, we manually set the flux scale to the expected value of the secondary phase calibrator by interpolating the flux densities.
Table 1  
Number of Observations per Frequency

| Observing Band (1) | Telescope          | N_{obs} (2) | N_{det} (3) | N_{det} (4) |
|--------------------|--------------------|-------------|-------------|-------------|
| L/1.4 GHz          | Historical VLA     | 4           | 1           |             |
| C/4.9 GHz          | Historical VLA     | 24          | 14          |             |
| ...                | Upgraded VLA       | 5           | 5           |             |
| ...                | VLBA               | 13          | 13          |             |
| X/8.4 GHz          | Historical VLA     | 84          | 59          |             |
| ...                | Upgraded VLA       | 4          | 4           |             |
| ...                | VLBA               | 1          | 1           |             |
| K_{\nu}/14.9 GHz   | Historical VLA     | 11          | 5           |             |
| K/22.5 GHz         | Historical VLA     | 4           | 0           |             |

Notes. Column (1): observing band and frequency. Column (2): telescope. Column (3): number of observations. Column (4): number of detections.

* Four observations with the upgraded VLA post-2015 outburst were taken in subarray mode, with half of the antennas observing at the C band and the other half at the X band, which we count as separate C- and X-band observations in this table. The fifth upgraded VLA observation was taken at the C band (4–8 GHz) in 2013. We often add a 7.7 GHz flux density measurement from this C-band observation into our analysis of the X-band sample (which is not reflected within this table).

** There are two additional observations in the archive at this frequency for which we could not obtain a calibration solution.

reported by GETJY of time-adjacent observations of the same calibrator at the same frequency. In these cases, we add a systematic uncertainty based on the level of variability of the secondary calibrator in nearby epochs, typically ≈5%. Finally, we add 5% and 10% systematic uncertainties to the flux scale for observations below and above 10 GHz, respectively.

The data were imaged using the task IMAGR, using Briggs weighting with a robust value of zero to help minimize sidelobes from nearby sources in the field. Of particular note is that a bright Jansky-level source lies 16.6° southeast of V404 Cygni (J2025+337, which was often used as the phase calibrator). This source is difficult to deconvolve during the imaging process because of bandwidth smearing (given the 50 MHz spectral windows of the historical VLA). We visually inspected a random subset of images of V404 Cygni over a range of frequencies and array configurations. We find that sidelobe artifacts from J2025+337 do not reach V404 Cygni at observing frequencies >8 GHz. At frequencies <8 GHz, there are multiple instances where artifacts from J2025+337 appear to increase the noise level near the location of V404 Cygni, but there are no cases where those artifacts obviously bias the measured flux densities.

Flux densities were measured using the task JMFIT by fitting a two-dimensional Gaussian (fixed to the width of the synthesized beam) at the known location of V404 Cygni. Given potential systematics raised by J2025+337 at lower frequencies, we require detections to display peak flux densities at >5σ_{rms}, where σ_{rms} is the rms noise measured in a blank region of the sky (with upper limits for nondetections calculated as 5σ_{rms}).

2.2. Karl G. Jansky VLA

Our sample also includes five epochs with the upgraded VLA. The first was taken in 2013 (Rana et al. 2016), and the other four were taken at the end of the 2015 outburst after the system reentered quiescence (Plotkin et al. 2017).

2.2.1. 2013 Quiescence

The 2013 observation lasted ≈9 hr in the C band (4–8 GHz) in the B configuration (maximum baseline ≈11 km) under program code 13B-016 (PI: Corbel). Two basebands of bandwidth 1024 MHz were placed at 5.25 and 7.45 GHz. The sources 3C 286 and J2025+337 were used as the primary and secondary calibrators, respectively.

Similar data reduction steps were performed as described in Section 2.1, except for the following: we used the Common Astronomy Software Application (CASA) v5.1.1 (McMullin et al. 2007) to allow us to account for the larger fractional bandwidth, we Hanning smoothed the data to avoid radio frequency interference from bleeding into nearby frequency channels, we used the primary flux calibrator to solve for delay and complex bandpass solutions, and we imaged the field using the task CLEAN, using Briggs weighting (robust=1.0) and two Taylor terms to model the frequency dependence over the 2 GHz bandwidth. In these observations, the effects of bandwidth smearing on J2025+337 were not significant, on account of the smaller frequency channels (2 versus 50 MHz), so we were able to adequately deconvolve J2025+337. Flux densities were measured by fitting a two-dimensional Gaussian with the CASA task IMFIT, forcing a point source (fixed to the width of the synthesized beam) at the known location of V404 Cygni.

2.2.2. 2015 Post-outburst

Four observations from the end of the 2015 decay are included in this study (from July 28–August 5) under program code SG0196 (PI: Plotkin). As noted at the beginning of Section 2, V404 Cygni reentered quiescence by the time these observations were taken, according to its X-ray spectral behavior (Plotkin et al. 2017). All four observations were taken in the most extended A configuration (maximum baseline ≈30 km) using the VLA in subarray mode, where about half of the antennas observed from 4 to 8 GHz and the other half observed from 8 to 12 GHz, yielding strictly simultaneous multifrequency coverage over four frequencies centered at 5.2, 7.5, 8.6, and 11.0 GHz (with 1024 MHz bandwidth at each frequency). These data were reduced using the same procedures as described in Section 2.2.1 (see Plotkin et al. 2017 for details).

2.3. VLBA

We monitored V404 Cygni with the VLBA over 13 (approximately) fortnightly observations between 2014 February 3 and August 22 under program code BM399 (PI: Miller-Jones). Each observation lasted 2 hr, yielding ≈56 minutes on source. We observed with all available antennas, using 256 MHz of bandwidth centered on a frequency of 4.98 GHz. We used J2025+337 (Ma et al. 1998; 16.6′′ from V404 Cygni) as both the fringe finder and phase reference calibrator and the somewhat more distant J2023+3153 (Ma et al. 1998; 1′′99 from V404 Cygni) as an astrometric check source. We also identified an additional VLBA observation at 8.4 GHz reported by Miller-Jones et al. (2009) taken on 2008 November 17 under program code BM290.
in dual circular polarization with 64 MHz bandwidth per polarization (133 minutes on source), which we rederived.\(^7\)

We calibrated the data using AIPS (version 31DEC15) following standard procedures. For the 8.4 GHz observation, we used geodetic blocks at the start and end of the observation to correct for unmodeled clock errors and tropospheric delays.

For all observations, we updated applied Earth orientation parameters, and we corrected for ionospheric dispersive delays using total electron content maps. We used system temperature parameters, and we corrected for ionospheric dispersive delays with respect to the sky, and iteratively imaged and self-calibrated the phase reference source J2025+337 to derive a model for calibrating the phase, delay, and rate solutions, which were then applied to the target. Here V404 Cygni was too weak for self-calibration. After imaging with natural weighting (for maximum sensitivity), we determined the source flux density by fitting a point source in the image plane. V404 Cygni remains point-like at VLBA resolutions in quiescence (Miller-Jones et al. 2008). Therefore, we do not expect to resolve out any jetted radio emission, allowing a fair flux density comparison between the VLA and VLBA epochs.

3. Results

3.1. Long-term Variability

Light curves are shown in Figure 1 at 4.9, 8.4, and 14.9 GHz (we omit our other two frequencies, 1.4 and 22.5 GHz, as they each contain only four observations). To quantify the distribution of flux densities at each frequency in the presence of nondetections, we perform a survival analysis. Using survfit in R (within the survival package\(^8\)), we calculate the survival function, \(S(\log f_\nu)\), via the Kaplan–Meier estimator (see, e.g., Feigelson & Nelson 1985 for a description of the Kaplan–Meier estimator and examples of astrophysical applications). We then estimate the cumulative distribution function as \(P(\log f_\nu) = 1 - S(\log f_\nu)\), which we display in Figure 2 at 4.9 and 8.4 GHz (omitting the four observations from 2015). In Section 3.3, we image the 2013 observation with the upgraded VLA at four separate frequencies centered at 5.0, 5.5, 7.2, and 7.7 GHz (each using 512 MHz bandwidth) to measure a spectral index. We therefore include the 5.0 GHz flux density from 2013 in the 4.9 GHz distribution here and the 7.7 GHz flux density in the 8.4 GHz distribution. In total, our 4.9 and 8.4 GHz distributions include 38 and 86 data points, respectively (of which 10 and 25 are upper limits, respectively). Detections (at the >5\(\sigma_{\text{rms}}\) level) range between 0.14 and 1.35 mJy bm\(^{-1}\).

We compare the cumulative distribution functions in Figure 2 to lognormal distributions using the Peto & Peto modification of the Gehan–Wilcoxon test, as implemented by cendiff in the R package Nondetects and Data Analysis for Environmental Data (NADA\(^9\)). The distributions of flux densities from V404 Cygni are not statistically different from lognormal distributions (\(p = 0.81\) and 0.93 at 4.9 and 8.4 GHz, respectively) with \(\log f_\nu/\text{mJy} = -0.53 \pm 0.19\) and \(\log f_\nu/\text{mJy} = -0.53 \pm 0.30\), where \(f_\nu\) are flux densities at 4.9 and 8.4 GHz, respectively, in units of mJy. The quoted errors represent standard deviations on the lognormal distribution (i.e., they are not errors on the mean).\(^10\)

We find that V404 Cygni shows significant flux density variations that are in excess of statistical fluctuations from measurement errors (which are typically ±0.04 mJy bm\(^{-1}\) with the historical VLA). Taking 8.4 GHz as an example, among 61 detections, we find a reduced \(\chi^2\) of 46 (for 60 degrees of freedom, as compared to a model with constant flux density). We note that \(\chi^2\) is slightly biased by one observation from

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\(^7\) Program BM290 contained four other observations at 8.4 GHz, which were already included in our sample because they used the phased VLA with the VLBA. We used the phased VLA observations in preference to the VLBA because the phased VLA uses a standard flux calibrator, while the VLBA observations rely on system temperatures for amplitude calibration.

\(^8\) https://CRAN.R-project.org/package=survival

\(^9\) https://CRAN.R-project.org/package=NADA

\(^10\) The quoted numbers for the lognormal distributions are not biased by a small number of individual observations in the small or large flux density tails of the distributions. We show this by bootstrapping the flux density distributions 100 times at each frequency, selecting subsamples of 30 and 50 at 4.9 and 8.4 GHz, respectively, with replacement. After running the same survival analysis on each bootstrapped distribution, we find the average values from the 100 distributions to be \(\log f_\nu/\text{mJy} = -0.54 \pm 0.19\) and \(\log f_\nu/\text{mJy} = -0.54 \pm 0.28\), where errors represent standard deviations.
with a higher signal-to-noise ratio (S/N) using the upgraded VLA. Removing that observation still suggests significant intrinsic variability ($\chi^2 = 33$ for 59 degrees of freedom). The fractional rms variability for all 61 observations at 8.4 GHz is $F_{\text{var}} = 54\% \pm 6\%$ (Vaughan et al. 2003), which is not biased by the higher S/N observations (i.e., we also calculate $F_{\text{var}} = 54\% \pm 6\%$ if we exclude the 2013 observation). If we consider the statistical fluctuations induced by variability to have a standard deviation of $\sigma_{f_{\text{var}}} = \pm f_{\text{var}}$, then propagating errors would yield $\sigma_{\log f_{\text{var}}} = \pm F_{\text{var}}/\ln 10$, such that a 54% fractional rms variability translates to 0.23 dex in logarithmic space.

To further quantify the flux variability, we produce the first-order structure function $V(\tau)$, which characterizes the amount of variability power as a function of timescale in the case of irregularly sampled data,

$$V(\tau) = \left\langle \left[ f(t + \tau) - f(t) \right]^2 \right\rangle,$$

where $f(t)$ is a flux density measurement at time $t$, and $\tau$ is a time delay. In the following analysis, we include only the 61 detections at 8.4 GHz. For every pair of data points $(t_i, t_j)$ in our light curve, we calculate $V_f(\tau_{ij}) = [f(t_j) - f(t_i)]^2$, where $\tau_{ij} = t_j - t_i$. We then bin our set of $V_f$ measures by time difference ($\tau_{ij}$) so that each bin contains 50 data points, and we take the average of those 50 measurements to calculate $V(\tau)$ (where we adopt the midpoint of all time differences within each bin as the value for the time delay $\tau$). The structure function is shown in Figure 3, where we probe long-term variability over timescales of $\sim 10$–4000 days.

The slope of the structure function provides information on the power distribution of flux variations (see, e.g., Hughes et al. 1992 for details, which we summarize below). For example, if variability
We characterize the level of variability on each epoch by calculating the reduced $\chi^2$ of the flux densities in each light curve. For this calculation, we ignore upper limits (which causes us to underestimate $\chi^2$ in some cases). Our measured $\chi^2$ values are listed in Table 3. Treating $\chi^2 > 3$ as a crude diagnostic for significant intrinsic variations, we find obvious variability on 8/11 epochs. However, we cannot determine from $\chi^2$ alone if we should consider the other three epochs as nonvariable. Rather, lower $\chi^2$ values imply that variability on those epochs is less extreme relative to fluctuations from statistical noise, and further tests are required (see next paragraph).

The three epochs with the upgraded VLA each display different short-term variability characteristics (i.e., the flux density is slowly decreasing with time on 2013 December 2, there are no obvious flares on $>3$ minute timescales on 2015 August 1, and we observe the beginning of a flare on 2015 August 5). These three epochs therefore provide useful illustrative examples, and as such, we display their structure functions in Figure 5. We fit a power law to each structure function, and we find power-law indices of $\beta = 0.29 \pm 0.05$, 0.10 $\pm$ 0.11, and 1.08 $\pm$ 0.08 on 2013 December 2, 2015 August 1, and 2015 August 5, respectively ($V(\tau) \propto \tau^\beta$). Note that the structure function on 2015 August 1 is flat, plateauing at $2\sigma^2_{\text{err}}$, indicating that V404 Cygni indeed shows (uncorrelated) variability in excess of statistical measurement noise fluctuations on 2015 August 1, even though $\chi^2_{\tau} = 2.8$.

3.2.1. Quiescent Flares

In this subsection, we summarize some of the flaring behavior of V404 Cygni in quiescence. We note that factor of $>2$ changes in flux density appear to be common. However, we do not attempt to define a duty cycle, on account of the limited number of observations (11) with short-term light curves for which we do not have uniform time resolution.

The 2007 December 2 observation (first reported by Miller-Jones et al. 2008) provides an extreme example of rapid short-term variability, where the 8.4 GHz flux density increased by a factor of 3–4 in $<10$ minutes, reaching 1.4 mJy, followed by a slower decay that lasted at least 30 minutes. (The beginning of that light curve also shows a series of three alternating detections and nondetections, suggesting a factor of $>2.5$ flux variability over 10 minutes.) However, not all short-term variability follows a pattern of a fast rise followed by a slower decay. For example, on 1998 May 4, a factor of 2–3 flare rose over $\approx 20$ minutes; on 2009 April 26, a rise and decay of a factor of $\approx 3$ in flux density occurred over $\approx 60$–90 minutes in each direction; and on 2015 August 5, V404 Cygni displayed an increase in flux density by a factor of $>2$ over $>60$ minutes.

We also see a potential variety in decay timescales. For example, the 2007 December 2 flare that quickly rose in $<5$–10 minutes took at least 30 minutes to decay. At the other extreme, the $\approx 9$ hr 2013 December 2 observation appears to be decreasing in flux the entire time (with some smaller-scale variations superposed). If a flare preceded the beginning of that observation, it implies that some flares decay on timescales of at least several hr. From the above, we conclude that tens of minutes to hours represent reasonable minimum characteristic timescales for the damping of radio flares. Although flares appear common, V404 Cygni also undergoes quieter periods of

![Figure 3. First-order structure function, including observations taken between 7.7 and 8.4 GHz (61 measurements, omitting upper limits). We bin the structure function to contain 50 data points per time delay. Horizontal dashed and dotted lines illustrate, respectively, twice the average measurement error squared ($2\sigma^2_{\text{err}}$) and twice the variance ($2\sigma^2_{\text{var}}$) of the 61 data points. The flat slope indicates either flicker-noise variations (i.e., a power function $P(F) \propto F^{-1}$) or shot-noise disturbances that resemble (uncorrelated) white noise when probed on timescales longer than a characteristic damping timescale of $\lesssim 10$ days.](image-url)
time, where either flares are absent or low-amplitude flares occur on short timescales of <3 minutes (e.g., 2015 August 1).

3.3. Radio Spectra

For 24 epochs, there are observations at multiple frequencies within ±30 minutes from which we measure spectral indices \( f(\nu) \propto \nu^{-\alpha_r} \), as shown in Figure 6. For epochs with exactly two frequencies, we calculate \( \alpha_r \) (or place a limit) analytically as \( \alpha_r = \ln(f_2/f_1)/(\nu_2/\nu_1) \), where \( f_1 \) and \( f_2 \) refer to flux densities at frequencies \( \nu_1 \) and \( \nu_2 \), respectively. We assign an error on \( \alpha_r \) by propagating through statistical errors (we ignore errors on frequency for the historical VLA given the relatively small bandwidth at each frequency, and we also ignore systematic errors from short-term variability, since we generally do not know if the

spectra were taken during flaring activity). If >2 observing frequencies, then we measure \( \alpha_r \) through a least-squares fit to the spectrum (in log space). We estimate error bars through Monte Carlo simulations, where we randomly add noise to each flux density measurement (assuming Gaussian noise with a standard deviation equal to the measurement error on each data point) and then refit the spectral index. We repeat 1000 times and estimate \( \sigma_{\alpha_r} \) as the standard deviation on the resulting \( \alpha_r \) distribution.

For the 2013 epoch from Rana et al. (2016) with the upgraded VLA, we create four (strictly simultaneous) images by splitting the bandwidth into four sub-bands with 512 MHz bandwidth (centered at 5.0, 5.5, 7.2, and 7.7 GHz), and we allow the frequency to randomly vary across each 512 MHz when running our Monte Carlo simulations to estimate error
We measure a large range of spectral indices, $-1.5 < \alpha_r < +1.6$, with the spread of $\alpha_r$ being larger at lower flux densities (Figure 7). However, we argue in Section 4.1 that this spread in $\alpha_r$ is likely attributed largely to statistical and systematic errors (i.e., large error bars on most $\alpha_r$ measurements, especially at lower flux densities, combined with only five epochs having strictly simultaneous multifrequency data).

To quantify the dispersion in radio spectral indices, we fit a Gaussian distribution to the $\alpha_r$ measurements (using a Bayesian framework that allows for both upper and lower limits). We find a mean $\langle \alpha_r \rangle = 0.02 \pm 0.17$ and a standard deviation $\sigma_{\alpha_r} = 0.65 \pm 0.15$, where the errors represent 68% confidence intervals of the posterior distributions. If we exclude the five spectra obtained from the upgraded VLA (which have significantly smaller error bars on $\alpha_r$), we find consistent results: $\langle \alpha_r \rangle = -0.07 \pm 0.25$ and $\sigma_{\alpha_r} = 0.78 \pm 0.21$. Throughout, we adopt $\langle \alpha_r \rangle = 0.02 \pm 0.65$, which is consistent with a flat radio spectral index, on average, as expected for a partially self-absorbed compact synchrotron jet.

### 3.3.2. Short-term Spectral Variations

Among the 11 observations from which we produce sub-hour light curves in Section 3.2, four contain multifrequency data allowing us to explore variations in $\alpha_r$ over sub-hour timescales. These epochs include 2013 December 2 with the upgraded VLA (Rana et al. 2016; 4–8 GHz), two epochs at the end of the 2015 outburst on August 1 and 5 (Plotkin et al. 2017; 4–12 GHz), and a historical VLA observation on 2003 July 29 that interleaved observations at 4.9 and 8.4 GHz every $\approx 15$ minutes (Hynes et al. 2004, 2009).

The radio spectra from these four epochs are displayed in Figure 8, where we also display the corresponding light curves for reference. The spectral constraints during the 2003 epoch are not very meaningful, but we include that epoch in the figure for completeness. For the other three epochs, we do not see any obvious changes of $\alpha_r$ with time; variations of $\alpha_r$ are consistent with statistical noise, with reduced $\chi^2_{\text{reduced}}$ values of 1.5, 2.5, and 1.5 (for 52, 32, and 32 degrees of freedom) on 2013 December 2, 2015 August 1, and 2015 August 5, respectively. We note that Rana et al. (2016) reported that the radio spectrum of V404 Cygni switched from optically thick to optically thin over $\approx 10$ minute periods on 2013 December 2. While we also see some variations in $\alpha_r$ over 10–30 minute timescales, they tend to be at the $1\sigma$–$2\sigma$ level, such that we do not consider these variations to be highly significant relative to the measurement error. We tentatively see marginal indications for a long-term evolution of the spectrum over the $\approx 9$ hr observation. Imaging the first 100 minutes of the observation yields $\alpha_r = -0.39 \pm 0.10$, while a less steep (and potentially flat)
Figure 6. Epochs with multifrequency information taken within 30 minutes, with each panel showing detections as filled symbols (error bars are smaller than the size of each symbol) and 5σ_{rms} upper limits as open symbols. The radio spectral index \( \alpha_r \) (or limit) is provided in the top right corner of each panel, with the gray shaded regions representing 68% confidence intervals on \( \alpha_r \) (and dashed lines representing limits). Note that we observe a range of steep, flat, and inverted spectra, but nonsimultaneity could be exaggerating the true spread in \( \alpha_r \) (except for the final five epochs, where the multifrequency information from the upgraded VLA is strictly simultaneous). The average spectral index is consistent with a flat radio spectrum, \( \langle \alpha_r \rangle = 0.02 \pm 0.05 \). However, the 2013 December 2 observation highlights that the strictly simultaneous spectral index can be negative on some epochs \( \alpha_r = -0.26 \pm 0.05 \).
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Figure 7. Radio spectral index $\alpha$ vs. 8.4 GHz flux density. The cyan stars represent the four epochs from 2015. The five data points with the smallest error bars were taken with the upgraded VLA, and the other 19 data points were taken with the historical VLA. The dashed horizontal line marks $\alpha = 0$ for reference. The spectral index tends to become negative only at low flux densities, which may be related to observational effects, such as nonsimultaneity and/or most low flux density observations having larger measurement errors. However, some negative spectral indices at low flux densities are likely reflecting intrinsic changes within the jet (e.g., the 2013 December 2 epoch with a well-measured $\alpha = -0.26 \pm 0.05$ from strictly simultaneous multi-frequency data).

The spectral index of $\alpha = -0.14 \pm 0.14$ is measured from images during the last 100 minutes. The steeper spectral index during the first 100 minutes appears to be driven by variations at 7.45 GHz that are not mimicked at 5.25 GHz.

4. Discussion

We have presented radio light curves of V404 Cygni in quiescence from 150 VLA and VLBA observations spanning 1991–2015, and we find that factor of 2–4 variations are common on timescales ranging from minutes to decades. Eleven observations are long enough to produce light curves on sub-hour timescales, from which we conclude that radio flares that last from tens of minutes to hours are common. However, there is no simple template to describe quiescent radio variability, either in flare profile, amplitude, or timescale. The observed variety in flare properties could imply that multiple mechanisms control the radio variability or that a single type of process yields a range of subtly different radiative signatures (e.g., a shock traveling through a steady jet, where the dissipation of energy is highly sensitive to the local conditions at the location of the shock).

For a single large flare (2015 August 5) do we have sufficient time resolution to attempt to statistically characterize its properties during the rise. Its structure function displays a slope $\beta \approx 1$, which means that at least some flares are consistent with red noise (i.e., $P(F) \propto F^{-2}$, although we note that we do not have coverage of the entire flare, which could bias our slope measurement). Considering that the structure function of long-term variations is flat (over $\approx 10$–4000 day timescales; Figure 3), we suggest that the quiescent jet of V404 Cygni (sometimes) displays flares with “random walk” noise characteristics that dampen to uncorrelated variations on longer timescales. We suspect that the damping time can be as short as tens of minutes to hours, as observed during some flares in Figure 4, but from Figure 3, we can only constrain the damping timescale to $\lesssim 10$ days.

We do not assert that all flares have red-noise characteristics, since there is only one (large) flare for which we have sufficient time resolution to calculate a structure function, and that observation was taken very shortly after the system returned to quiescence following the 2015 outburst. Nevertheless, the behavior of red-noise flares that dampen to uncorrelated variations on long timescales is reminiscent of decade-long radio light curves of BL Lac objects, i.e., low-luminosity active galactic nuclei (AGNs) with a jet pointed toward Earth. Hughes et al. (1992) found that BL Lac objects typically show first-order structure functions with slopes $\beta \sim 1$ that become flat at long timescales (i.e., consistent with a damped random walk). They find a broad distribution of characteristic damping timescales from $\approx 1$ to 10 yr for BL Lac objects.\(^\text{13}\)

To first order, after correcting for beaming effects related to BL Lac orientation, we expect BL Lac objects to be analogous to hard-state BHXBs (e.g., Falcke et al. 2004; Kording et al. 2006), and, despite their higher Eddington ratios, we believe that BL Lac objects also make reasonable analogs for comparison to a luminous quiescent BHXB like V404 Cygni (i.e., both types of systems launch compact radio jets from a black hole fed by inefficient accretion). However, to compare BL Lac timescales to V404 Cygni requires correction for the effects of relativistic beaming from the BL Lac jets, which is difficult given the unknown Doppler factors and redshifts for most of the BH Lac objects in Hughes et al. (1992). As an extreme example, we consider a BL Lac object with a Doppler factor $\delta \approx 60$, which would correspond to a very fast jet with a bulk Lorentz factor $\Gamma \approx 50$ (e.g., Lister et al. 2009) aligned within only 1° to our line of sight. In that case, the intrinsic (i.e., rest-frame) characteristic timescales from Hughes et al. (1992) would be $\lesssim 600$ yr (BL Lac objects tend to have low redshifts, e.g., a median $z \approx 0.33$ in Shaw et al. 2013, such that cosmological corrections will be smaller than beaming corrections).

If one were to associate the above timescale with a timescale that scales linearly with black hole mass (e.g., the light travel time across an emitting region that is comparable in size to the radio photosphere of a conical jet), then $\lesssim 600$ yr would scale down to $\approx 10$ minutes for V404 Cygni (comparing the $9 M_\odot$ mass of V404 Cygni to a typical $3 \times 10^8 M_\odot$ mass for a BL Lac object; Plotkin et al. 2011). We suspect that most flares from V404 Cygni decay on timescales of at least several tens of minutes to hours, longer than expectations from the above mass scaling. Therefore, we are either probing physical variations in V404 Cygni that are inaccessible for individual supermassive black holes, or it is possible for some AGN phenomenology to occur on much faster timescales than expected from (simplistic) mass-scaling arguments. We view the latter as a plausible explanation, particularly in light of the existence of changing-look AGNs, which have accretion disks that appear to operate on much quicker timescales than expected from mass-scaling arguments (e.g., Dexter & Begelman 2019; Noda & Done 2018).

Finally, we note that the radio photosphere of the quiescent jet from V404 Cygni (at GHz frequencies) is empirically

\(^{13}\) This phenomenology is also common for jet-dominated emission in the optical waveband, where BL Lac object light curves can be well characterized by a damped random walk (Ruan et al. 2012), and in some cases also in the gamma-ray (where sporadic flaring over a steady flicker-/red-noise power spectrum is often observed; e.g., Abdollahi et al. 2010).
constrained to be located at a distance $\lesssim 3.4$ au from the black hole (Miller-Jones et al. 2008; Plotkin et al. 2017). The size of the radio-emitting region would be even smaller (e.g., by a factor of $\tan \phi$ for a conical jet, where $\phi$ is the jet opening angle; Miller-Jones et al. 2006), such that one should not expect radio variations on timescales longer than $\approx$ tens of minutes to be causally connected unless the jet is very slow. Thus, long-term variations likely reflect the jet responding to separate disturbances, like changes in the mass accretion rate through the inner flow or changing intrinsic properties of the jet (e.g., how internal energy in the jet is partitioned between the particles and magnetic field). That both the radio and X-ray display similar long-term variability characteristics (i.e., flat structure functions; see Bernardini & Cackett 2014) might support that both wavebands release radiative power by tapping into the same energy reservoir, as suggested by, e.g., Malzac et al. (2004).\footnote{We note that we are probing longer timescales than considered by Malzac et al. (2004), who considered X-ray variations associated with dynamical timescales at 10–100 Schwarzschild ($\approx 0.1$ s), while in our case, the X-ray and radio variations are over timescales longer than several days. However, the general idea that both the radio and X-ray emission regions are responding to a common physical driver seems to be a reasonable interpretation.}

4.1. Spectral Variations

As noted in Section 3.3.1, we measure radio spectral indices in the range $-1.5 < \alpha_r < +1.6$, with a mean $\alpha_r = 0.02$ and a standard deviation $\sigma_{\alpha_r} = 0.65$. We suspect that the large range in $\alpha_r$ can be attributed to the poorer sensitivity of the historical VLA and multifrequency data that can be offset by $\pm 30$ minutes. For example, a factor of 2 variability within 30 minutes would adjust $\alpha_r$ by $\pm 1.3$. We are therefore cautious not to overinterpret the apparently large range of measured $\alpha_r$, which might not require a physical explanation.

The above variability-related concerns, however, do not preclude the possibility of less extreme spectral variations. The upgraded VLA provides strictly simultaneous multifrequency observations, and the 2013 December 2 epoch ($\alpha_r = -0.26 \pm 0.05$) provides evidence that the spectral index can indeed stray negative at times (as originally pointed out by Rana et al. 2016). We stress that $\alpha_r = -0.26 \pm 0.05$ is inconsistent with a purely optically thin spectrum, as expected from transient ejecta (e.g., Fender et al. 1999; Corbel et al. 2004). Possible explanations for a mildly negative spectral index, as observed on 2013 December 2, could include the combination of optically thick and thin emission (e.g., the

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\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig8}
\caption{Four observations for which we can extract spectral information over sub-hour timescales, including 2003 July 29 (60 minute time bins; also see Hynes et al. 2009), 2013 December 2 (10 minute time bins; also see Rana et al. 2016), and 2015 August 1 and 5 (3 minute time bins; also see Plotkin et al. 2017). Note that the multifrequency information is strictly simultaneous for the final three observations, but not for the 2003 observation. We do not observe meaningful fluctuations in $\alpha_r$ on these short timescales.}
\end{figure}
fading optically thin stage of a flare superposed over a steady, flat-spectrum jet, a jet that expands more slowly than a conical jet, or a decelerating jet. Also contributing could be that low-
frequency variations are “smeared,” since they are emitted over a larger volume (farther from the black hole) compared to higher-frequency emission. Indeed, the 2013 December 2 light curve (Figure 8) displays dips at 7.45 GHz approximately 50 and 150 minutes after the start of the observation that are not mimicked at 5.25 GHz, which likely contributes to the overall negative spectral index.

To our knowledge, the 2013 December 2 observation of V404 Cygni is the only observation of a quiescent BHXB to show a (well-measured) negative spectral index. However, comparable negative spectral indices have been measured from compact jets in the hard state (see, e.g., Espinasse & Fender 2018 and references therein, although we note that many of those observations also suffer from low sensitivity). Reasonable explanations for different spectral indices in the hard state include intrinsic differences in jet properties (Espinasse & Fender 2018), differences in inclination (Motta et al. 2018), or both. One difference in our work, however, is that we are seeing both positive and negative spectral indices from the same source. Therefore, we cannot explain a varying radio spectral index from V404 Cygni in quiescence as an inclination effect.

5. Coordinating Multiwavelength Observations

Part of our motivation for this work is to quantify the level to which variability-related systematic uncertainties can influence the location of quiescent BHXBs in the radio/X-ray luminosity plane (L_R − L_X). Understanding these uncertainties is important for studies of disk/jet couplings (e.g., fitting L_R − L_X correlation slopes for individual objects), as well as studies that appeal to L_R − L_X to identify new BHXB candidates. Below, we compare the radio variability of V404 Cygni to its X-ray variability (taken from the literature), and we recommend some guidelines for reducing variability-induced systematics when coordinating and interpreting radio/X-ray observations of quiescent BHXB (candidates) with luminosities comparable to V404 Cygni.

5.1. X-Ray Variability in Quiescence

Bernardini & Cackett (2014) obtained dense X-ray monitoring of V404 Cygni with the Neil Gehrels Swift Observatory, taking 33 observations over 75 days. Their study provides the most appropriate comparison to our long-term radio light curve (s) in Figure 1. They find a fractional rms variability in the X-ray of F_{var}.X-ray = 57% ± 3% (~0.25 dex), and they obtain a flat structure function over timescales of ~5–80 days. These X-ray results are similar to our radio results, where we find F_{var}.radio = 54% ± 6% (~0.23 dex) and a flat structure function (although our study extends to longer timescales of of ~10–4000 days).

While the level of long-term X-ray variability is comparable to that in the radio, short-term X-ray variability can be larger in amplitude. For example, on hour timescales, factor of 4–8 X-ray variations are typical (e.g., Bradley et al. 2007; Bernardini & Cackett 2014; Rana et al. 2016); at the extreme end, Hynes et al. (2004) observed a flare that increased the Chandra count rate by a factor of ~20 (also see Wagner et al. 1994 for a factor of 10 variation in <0.5 days). For comparison, in our work, we commonly observe flares that change the flux density by factors of 2–4 in the radio.

Whether or not one should expect correlated variations between the radio and X-ray bands on short timescales is an open question. To our knowledge, there have been no multiwavelength campaigns that simultaneously take radio and X-ray observations in quiescence over multiple epochs separated by only 1–2 days, thereby making it impossible to empirically test if radio/X-ray variations are correlated on sub-week timescales. On minute-through-hour timescales, only two attempts have been published so far that searched for coordinated radio/X-ray variability over observations lasting several hr (2003 July 29 and 2013 December 2), and neither attempt has shown obvious radio/X-ray correlations with light curves on 30–100 minute time bins (Hynes et al. 2009; Rana et al. 2016). However, detecting correlated variations may require finer time resolution.

5.2. Recommendations for Coordinating Radio and X-Ray Observations

Considering the above X-ray characteristics, and that correlated (short-term) radio and X-ray variability might only be detectable with minute time resolution, we suggest the following strategies when coordinating multiwavelength campaigns on quiescent X-ray binaries.

1. Radio and X-ray observations should be scheduled as simultaneously as possible. If the source is bright enough to provide sufficient S/N on <10 minute time bins in both the radio and X-ray, then (some) individual flares should be resolvable, and one can directly control for multiwavelength variability. Ideally, the observations would be long enough to observe the entire flare rise and decay (which can last several hr).

2. If data are nonsimultaneous, or if one does not have sufficient time resolution to resolve individual flares, then inflate the error bars by ~0.25 dex in both the radio and the X-ray. However, one should still bear in mind that variations as large as factors of 2–4 in the radio and 4–8 in the X-ray are common.

3. Radio observations should be taken as close as possible to the frequency required to achieve one’s science goals. If spectral constraints from strictly simultaneous multi-frequency data are lacking, then we support the standard assumption of a flat radio spectrum when extrapolating radio observations to other frequencies. However, we find evidence that α_r is not always strictly zero, and we recommend propagating errors on flux densities by assuming that the radio spectrum could vary by α_r ≈ ±0.6 (see Section 3.3.1).

5.3. A Comparison to the Transitional Millisecond Pulsar PSR J1023+0038

While quiescent BHXBs tend to have higher L_R/L_X ratios than other classes of Galactic compact accreting objects (e.g., Migliari & Fender 2006; Tudor et al. 2017; Gallo et al. 2018), the transitional millisecond pulsar (tMSP) PSR J1023+0038 (hereafter J1023) was recently shown to sometimes be an exception to that trend (Bogdanov et al. 2018). Considering periods when J1023 does not show radio pulsations as accretion-powered states, J1023 exhibits aperiodic and rapid switching between two distinct
X-ray flux levels, a low mode ($L_X \approx 5 \times 10^{32}$ erg s$^{-1}$) and a high mode ($L_X \approx 3 \times 10^{33}$ erg s$^{-1}$; e.g., Patruno et al. 2014; Stappers et al. 2014; Bogdanov et al. 2015; Jaodand et al. 2016). Bogdanov et al. (2018) discovered that the low modes are nearly always accompanied by radio flares that both rise and decay on minute timescales. The radio flux density appears anticorrelated with the X-ray flux, although some radio flaring is also observed when the X-ray flux remains in a high mode. During these low X-ray mode states, the increased radio flaring tends to reach $L_R \approx 2 \times 10^{27}$ erg s$^{-1}$.

In Figure 9, we highlight the location of J1023 in the $L_R - L_X$ plane (large green triangles) compared to V404 Cygni in quiescence and the hard state (large blue circles). We also shade in a region that represents the minimum and maximum luminosities displayed by V404 Cygni within our radio data set ($\approx 5 \times 10^{27} - 5 \times 10^{28}$ erg s$^{-1}$, which corresponds to flux densities ranging from 0.14 to 1.35 mJy if one assumes a flat radio spectrum) and the minimum and maximum X-ray luminosities displayed during the Swift campaign from Bernardini & Cackett (2014). We estimate 1–10 keV X-ray luminosities assuming a photon index of 2.1 and a column density of $9 \times 10^{21}$ cm$^{-2}$ (Bernardini & Cackett 2014) using X-ray count rates extracted from the online Swift-XRT product generator tool (Evans et al. 2007, 2009). The shaded region in Figure 9 assumes that radio and X-ray luminosities are not correlated in quiescence and therefore represents a conservative range for where one might find V404 Cygni in the $L_R - L_X$ plane if considering nonsimultaneous data. The mean radio flux density from our study ($\log f_r$/mJy $= -0.53$) corresponds to $\log L_R$/erg s$^{-1} \approx 28$, such that V404 Cygni likely spends most of its time toward the bottom left of the shaded region (with the top right region representing periods of flaring activity).

After accounting for the range of flux density variations exhibited by V404 Cygni, we expect its radio luminosity to always be $\gtrsim 2.5$ times larger than the radio luminosity of J1023, even when J1023 is in a low X-ray flux (i.e., radio-flaring) state. Still, J1023 ventures very close to the parameter space expected for quiescent BHXBs, and it is easy to envision that it could overlap with a BHXB that has similar variability characteristics as V404 Cygni but at a slightly lower Eddington ratio. Although J1023 only ventures toward the BHXB parameter space on short timescales, $\lesssim 500$ s (i.e., over longer time-averaged observations, J1023 will generally appear radio fainter), other tMSPs could venture toward the BHXB parameter space for longer periods of time (e.g., the tMSP IGR J18245–2452 has displayed at least one low mode that lasted for nearly 10 hr; e.g., Linares et al. 2014). We therefore reiterate the conclusion from Bogdanov et al. (2018) that radio and X-ray luminosities alone are not always sufficient to confidently assert that a quiescent X-ray binary contains a black

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15 Data taken from Bahramian et al. (2018); see https://github.com/bersavosh/XRB-LxX_pub.

16 http://www.swift.ac.uk/user_objects
hole instead of a neutron star.\textsuperscript{17} Other multiwavelength data should naturally also be consulted, e.g., to search for an orbital period, emission lines, or other properties to give clues on the nature of the companion star and accreting compact object (e.g., Bahramian et al. 2017; Shishkovsky et al. 2018; Tudor et al. 2018).

Lacking detailed multiwavelength data, we assert that radio light curves could have some diagnostic power to determine if one is observing a black hole or a neutron star.

1. Frequent and relatively short radio flares that both rise and decay on rapid (minute) timescales may favor a neutron star. Bogdanov et al. (2018) found radio flares that last \( \lesssim 500 \) s, and they rise and decay rapidly (see their Figures 1, 4, and 5). These flares can occur quite frequently at times (e.g., Bogdanov et al. 2018 observed as many as three to four radio flares per hour during some portions of their observation). For V404 Cygni, we observe less frequent flaring, and we only observe rapid flare rises. The decays tend to proceed on longer timescales of tens of minutes to hours.

2. An order-of-magnitude change in the quiescent radio flux density over minute-to-hour timescales might argue for a neutron star. Deller et al. (2015) showed light curves of J1023 from 13 different epochs (see their Figure 5), and they found a case where the radio flux density steadily increases by an order of magnitude over \( \approx 30 \) minutes. While V404 Cygni has also been observed to show flares with comparably slow rise times, none of those \( > 30 \) -minute flares have increased in flux density by an order of magnitude.

We stress that the above assertions are predicated on observing a system that is close enough to produce radio light curves on minute timescales (e.g., V404 Cygni is at 2.39 \( \pm \) 0.14 kpc, Miller-Jones et al. 2009; and J1023 is at 1.368\( ^{+0.042}_{-0.036} \) kpc, Deller et al. 2012). Also, in some cases, radio light curves will not hold any diagnostic power, since, particularly with shorter observations, J1023 and V404 Cygni can both show time periods of low activity. Furthermore, the variability observed so far from J1023 and V404 Cygni is unlikely to represent the full range of variability that can be displayed by either class of systems (e.g., as evidenced by the nearly 10 hr X-ray low mode displayed by the tMSP IGR J18245 – 2452).

If one does not have access to radio light curves with minute time resolution, then taking a radio flux density integrated over long observations could provide a less ambiguous interpretation: over long time intervals, nonflaring time periods will dilute the radio flux density, thereby moving the tMSP farther away from the quiescent BHXBs in space \( L_r - L_x \). Finally, in some cases, the X-ray spectrum can provide additional diagnostic power: J1023 has an X-ray photon index of \( \Gamma \approx 1.7 \) in both low and high X-ray modes (Bogdanov et al. 2018), while quiescent BHXBs are well established to have a softer \( \Gamma \approx 2.1 \) in quiescence (Plotkin et al. 2013; Reynolds et al. 2014). The radio spectral index, however, is a poor discriminant, given that both V404 Cygni and J1023 exhibit a range of mildly positive and negative spectral indices (Bogdanov et al. 2018 reported a range of \( -0.5 \lesssim \alpha_r \lesssim 0.4 \)) and that \( \alpha_r \) is usually not well measured in low-luminosity sources.

\textsuperscript{17} Although in some cases, e.g., a system being very radio bright or radio faint, one could reasonably disfavor or favor a neutron star from radio and X-ray luminosities.

\section{6. Summary}

We present archival radio observations of V404 Cygni spanning 24 yr (1991 – 2015), providing the most stringent long-term constraints to date on the radio variability of a synchrotron jet from a quiescent BHXB. We find flux densities that follow a lognormal distribution, with mean and standard deviation (in \( \log f_r / \mu Jy \)) of \( -0.53 \pm 0.19 \) and \( -0.53 \pm 0.30 \) at 4.9 and 8.4 GHz, respectively. Factor of \( > 2 \) – 4 variations are common on every observable timescale from minutes to decades. As expected, the radio spectrum of V404 Cygni is flat on average \( \langle \alpha_r \rangle = 0.02 \pm 0.65 \), where the error represents the standard deviation, but we also find that \( \alpha_r \) becomes significantly negative on at least one epoch.

Over two decades of observations, V404 Cygni displays a flat structure function, such that the long-term flux density variations (days – years) are consistent with either flicker noise \( (P(F) \propto F^{-1}) \) or white noise. On epochs when we have sufficient-quality data, we observe individual flares that appear to decay within minutes to hours. These results are consistent with an interpretation of shot noise probed over a timescale that is longer than the characteristic damping time of each disturbance. We suspect that typical flare decay timescales are on the order of tens of minutes to hours, but we are formally only capable of constraining that timescale to \( < 10 \) days (with tens of minutes a reasonable lower bound). These properties may be expected from shock instabilities traveling through a steady, compact jet. Given similar characteristics observed in the X-ray band (Bernardini & Cackett 2014), the radio variability appears consistent with scenarios where the X-ray and radio radiative processes are powered by a common energy source (e.g., Malzac et al. 2004).

Finally, we provide recommendations for combating variability-induced systematics when attempting to place accreting compact objects onto the radio/X-ray luminosity plane, as is commonly done in surveys for quiescent BHXBs. We recommend that radio and X-ray observations be taken as simultaneously as possible to allow direct detections of flares during each observation. If the data are not of sufficient quality to detect individual flares or are not simultaneous, then we recommend inflating the error bars on radio and X-ray luminosities by 0.25 dex. If one must extrapolate radio observations to different frequencies, then ideally, one would be able to measure a radio spectrum from strictly simultaneous multifrequency observations. Otherwise, a flat radio spectrum is a reasonable approximation, except that the error bars should also be adjusted according to expectations that the radio spectrum can vary \( \langle \alpha_n \rangle = \pm 0.6 \) is a reasonable uncertainty. Finally, we repeat warnings by Bogdanov et al. (2018) that some accreting neutron stars (i.e., tMSPs) can obtain radio and X-ray luminosities comparable to those achieved by quiescent BHXBs, such that other types of multiwavelength data (e.g., optical, ultraviolet, and X-ray spectra and timing) should be considered when attempting to identify the nature of accreting compact objects when mass functions are not available.

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