High Fill-Factor Imagers for Neuromorphic Processing Enabled by Floating-Gate Circuits

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In neuromorphic modeling of the retina, it would be very nice to have processing capabilities at the focal plane while retaining the density of typical active pixel sensor (APS) imager designs. Unfortunately, these two goals have been mostly incompatible. We introduce our transform imager technology and basic architecture that uses analog floating-gate devices to make it possible to have computational imagers with high pixel densities. This imager approach allows programmable focal-plane processing that can perform retinal and higher-level bioinspired computation. The processing is performed continuously on the image via programmable matrix operations that can operate on the entire image or blocks within the image. The resulting dataflow architecture can directly perform computation of spatial transforms, motion computations, and stereo computations. The core imager performs computations at the pixel plane, but still holds a fill factor greater than 40 percent—comparable to the high fill factors of APS imagers. Each pixel is composed of a photodiode sensor element and a multiplier. We present experimental results from several imager arrays built in 0.5 micrometer process (up to $128 \times 128$ in an area of 4 millimeter squared).

Keywords and phrases: floating-gate circuits, CMOS imagers, real-time image processing, analog signal processing, transform imagers, matrix image transforms.

1. INTRODUCTION

In neuromorphic modeling of retinal and cortical signal processing, we see a trade-off between large-scale focal-plane processing and typical active pixel sensor (APS) imager designs in which significant processing is performed elsewhere. The APS imager designs result in high-resolution imagers with dense pixels [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]. In current neuromorphic imaging systems, the focal-plane processing usually limits the number of pixels [12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26]. Since both imager approaches use photodiode (or photo BJT) devices as the element to convert light into electrical signals, what is needed is an architecture/system that combines the advantages of both types of imagers. In this paper, we present an imager approach and resulting architecture that performs computation at the pixel plane, keeps the large number of pixels typical in APS imagers, and allows for retinal-like and cortical-like signal processing. This imager architecture, shown in Figure 1, is capable of programmable matrix operations for 2D transforms or filter operations on the entire image, or block-matrix operations on subimages. The resulting architecture is a dataflow structure that allows for continuous computation of these matrix transform operations.

Our new imaging architecture is made possible largely by advancements in analog floating-gate circuit technology and its application [27, 28, 29]. Floating-gate devices in imaging can be used to eliminate fixed pattern noise [11, 30] and to enable programmable and adaptive signal processing applied toward the images. These circuits have the added advantage that they can be built in standard CMOS or double-poly CMOS processes.

This paper addresses the following three areas:

1. floating-gate circuits and their use in this imager,
2. the context for and applications of our transform imager,
3. the image architecture and related details.
The paper is organized into five sections. In Section 2, we present an overview of floating-gate devices, circuits, and systems. We also discuss two key systems: floating-gate circuits for arbitrary parallel waveform generation and floating-gate circuits for matrix multiplication. In Section 3, we present the basic architecture design (single imager and computational system) and highlight the aspects of programmability that will be enabled by using floating-gate circuits. We also present an overview of our concept of cooperative analog-digital signal processing (CADSP) and its relationship to neuromorphic image processing. In Section 4, we present the basic pixel elements and their characterization as well as the mathematics needed to predict performance for a given application based on experimental measurements, including estimates on noise, speed, and so forth. In Section 5, we present system examples and measurements, and we conclude in Section 6.

2. ENABLING TECHNOLOGY: FLOATING-GATE CIRCUITS

From their early beginning, floating-gate devices have held promise for use in analog signal processing circuits and biologically motivated computation [29, 31, 32, 33]. Since these beginnings, this technology has begun to fulfill some of the early expectations; for a good review see [27]. One can imagine many straightforward approaches to using floating-gate circuits in imagers. For example, one could eliminate circuit offsets and dark current errors in the pixel circuits as well as in sensing circuits [11, 30]. These approaches often decrease the fill factor of the pixel. With the signal processing potential of floating-gate circuits already shown in auditory applications, one might imagine the possibility of a wider set of applications.

Our transform imager and architecture is enabled by floating-gate circuits in three ways. First, we can store arbitrary analog waveforms enabling arbitrary matrix image transforms or block image transforms. Second, we can program these waveforms to account for average device mismatch along a column, thereby getting significantly higher image transform quality. Third, we can use floating-gate circuits to compute additional vector-matrix computations. As a result, we can use a single, simple pixel element to perform a wide range of possible computations.

In the following sections, we will explore the issues of using floating-gate elements for the transform imager approaches. In Section 2.1, we present an overview of floating-gate circuits focusing on imager applications. In Section 2.2,
we address the issues of programming a large number of floating-gate elements. In Section 2.3, we discuss the two important floating-gate circuits/systems used in the transform imager architecture:

(i) generation of arbitrary on-chip waveforms,
(ii) analog vector-matrix multiplication.

One could imagine straightforward applications of the entire spectrum of floating-gate technologies and signal processing algorithms applied to this architecture [34].

2.1. Floating-gate circuits for imager applications

Floating-gate devices are not just for digital memories anymore, but they are used as circuit elements with analog memory and important time-domain dynamics [27]. We define floating-gate circuits as the field where floating-gate devices are used as circuit elements and not simply as digital memory elements. Floating-gate devices and circuits typically are divided into three major functions: analog memory elements, part of capacitive-based circuits, and adaptive circuit elements.

Figure 2 shows the layout, cross-section, and circuit symbol for our floating-gate pFET device. A floating gate is a polysilicon gate surrounded by silicon-dioxide. Charge on the floating gate is stored permanently, providing a long-term memory, because it is completely surrounded by a high-quality insulator. From the layout, we see that the floating gate is a polysilicon layer that has no contacts to other layers. This floating gate can be the gate of an MOSFET and can be capacitively connected to other layers. In circuit terms, a floating gate occurs when we have no DC path to a fixed potential. No DC path implies only capacitive connections to the floating node, as seen in Figure 2.

The floating-gate voltage, determined by the charge stored on the floating gate, can modulate a channel between a source and drain, and therefore, can be used in computation. Floating-gate circuits provide IC designers with a practical, capacitor-based technology; since capacitors, rather than resistors, are a natural result of an MOS process. Floating-gate devices can compute a wide range of static and dynamic translinear functions by the particular choice of capacitive couplings into floating-gate devices [35].

We modify the floating-gate charge by applying large voltages across a silicon-oxide capacitor to tunnel electrons through the oxide or by adding electrons using hot-electron injection. The physical effects of hot-electron injection and electron tunnelling become more pronounced as the line widths of existing processes are further scaled down [36], improving our floating-gate circuits. Floating-gate circuits based upon programmable (short periods of charge modification) and adaptive (continuous charge modification) techniques have found uses in applications from programmable on-chip biasing voltages and sensor circuits [37], to removing offsets in differential pairs and mixers [38], and to programmable filters and adaptive networks [33, 38].

These floating-gate transistors provide nonvolatile storage, compute a product between this stored weight and the inputs, allow for programming that does not affect the computation, and adapt due to correlations of input signals. These single transistor learning synapses [29], named because of the similarities to synapses, lead to a technology called analog computing arrays. Figure 3 shows a general block diagram of our floating-gate computing array. We have built analog computing arrays for auditory signal processing [28, 34, 39], as well as for image signal processing. The memory cells may be accessed individually (for readout or programming), or they may be used for full parallel computation within the array (as in matrix-vector multiplication or adaptation). Therefore, we have full parallel computation with the same circuit complexity and power dissipation as the digital memory needed to store a 4-bit digital coefficient. This technology can be integrated in a standard digital CMOS process or in standard double-poly CMOS processes. Furthermore, we only need to operate this system with effectively one memory access per incoming sample, or in other words, the system only needs to operate at the incoming data speed (maximum input frequency), thereby reducing requirements on our overall system design.

2.2. Programming arrays for floating-gate elements

Routinely programming thousands to millions of floating-gate elements requires systematic, automated methods for
programming. We have developed such a method as a critical part of this single-chip system. We take a similar approach as we described elsewhere [27, 28, 29, 40]. Our programming scheme minimizes interaction between floating-gate devices in an array during the programming operation. This scheme also measures results at the circuit’s operating condition for optimal tuning of the operating circuit (no compensation circuitry needed). Once programmed, the floating-gate devices retain their channel current in a nonvolatile manner.

Figure 3b shows that it is possible to isolate individual elements (access to an individual gate and drain line) in a large matrix using peripheral control circuitry. We program a device by increasing the output current using hot-electron injection, and erase a device by decreasing the output current using electron tunnelling. Because of the poorer selectivity, we use tunnelling primarily for erasing and for rough programming steps. Our programming scheme performs injection over a fixed time window using drain-to-source voltage based on the actual and target currents. The time used
for injection was 10 milliseconds. We have successfully used 100 microseconds, and we see no technological limitation to using one microsecond as injection time. These fast values are critical to programming mass production or large arrays of floating gates.

Programming a floating-gate element involves being able to adjust multiple control voltages for a single element. The isolation circuitry is made of multiplexors that switch the drain and gate voltages of the desired element onto a common bus for each signal. Other elements are switched to a separate voltage to ensure that those devices will not inject. Any circuit containing programmable floating-gate elements must also have various switching circuitry to access each floating-gate element in a standard array.

We designed a custom programming board to program large floating-gate arrays. The board, shown in Figure 3, allows for flexible floating-gate array programming over a wide range of IC processes and allows for nearly transparent operation to the user. Using custom circuits to program the floating gates allows for a self-contained programmer at a lower cost than a rack of testing equipment. This programming board is connected to the chip via a standard header that allows the option of additional logic when used as part of a larger testing approach. Figure 3 shows the output from a row of floating-gate multipliers that have been programmed to perform a differential cosine scale multiplication on the input signals.

2.3. Transform imager floating-gate systems

The transform imager architecture requires using fundamental floating-gate circuits/systems for the generation of arbitrary on-chip waveforms and for analog matrix-vector multiplication. Other floating-gate circuits are used to further enhance the circuit and signal processing performance of these systems.

Floating-gate basis generator

We use floating-gate circuit elements to store and to generate the arbitrary basis functions needed for the matrix-vector multiplication on the imager. This approach computes a similar function to ISD’s audio recording ICs [41], but uses floating-gate circuits in a standard process rather than analog EEPROM cells in a special process. Figure 4 shows the top-level view of our basis generation circuitry. This system operates in both operation (basis generation) mode and programming mode. In operation mode, we have an array of stored values that are output in sequence. Lowpass filtering on the output results in a continuous-time analog result. In programming mode, we can easily reconfigure this circuitry on the outside edges for programming. As a result, we achieve very high circuit density. In operation mode, the digital logic is a shift register or a counter behind the decoder; in programming mode, the digital logic is a decoder to conform to current standards. The capacitors can be either double-poly capacitors or MOS capacitors (single-poly process); both approaches work equally well. In single-poly, the coupling capacitor is built using an MOS capacitor.

Floating-gate vector-matrix multiplication

We use the floating-gate circuit elements to compute analog multiplications of a signal vector with a stored, programmable matrix. We can perform vector matrix computations using our existing analog computing array (ACA) technology based upon floating-gate circuits [28]. Using the output image stream, this system will compute a transposed matrix transform.

This system operates both in operation (basis generation) mode and programming mode. In operation mode, we have an array of four-quadrant multipliers with stored values at each multiplier. The inputs can be either currents or voltages depending upon the particular system interfacing and linearity requirements. For current inputs, the circuit is a set of programmable-gain current mirrors, resulting in minimal
distortion. We also use current inputs, because the outputs from previous stages are usually currents. Temperature dependence is based upon the difference in floating-gate charge [32]. The programmed currents remain within 10 percent for a factor of four range of currents over 0–40 °C, and change in similar directions throughout the array (gains will scale).

3. TRANSFORM IMAGER SYSTEM

3.1. Cooperative analog-digital signal processing framework

Neither analog signal processing nor digital signal processing can exist in current technologies without the other; that is, real-world signals are analog while much of the modern control and communication is digital. Typically, one does not think of analog and programmability together—analog circuits are primarily for preamplifiers, and programmability has been exclusively in the domain of digital processing. However, new advances in analog VLSI circuits have made it possible to perform operations that more closely reflect those done in DSP applications. Furthermore, analog circuits and systems can be programmable, reconfigurable, adaptive, and at a density comparable to digital memories [27, 28, 29, 42].

We define CADSP as looking at the issues of using combinations of programmable analog signal processing and digital signal processing techniques for real-world processing [43]. Our goal in CADSP is to build systems that benefit from the advantages of both types of signal processing to make something better than the sum of its parts and to enhance the overall functionality of a system by utilizing analog/digital computations in mutually beneficial way. Therefore, one might wonder if we have both digital and analog signal processing available, how does one choose a particular solution for a given application. The question of where to partition the analog-digital boundary is still an open research question.

3.2. Transform imager system overview

Figure 1 shows the block diagram of our transform imager technology. This approach allows for retina and higher-level bioinspired computation in a programmable architecture that still possesses similar high fill-factor pixels of APS imagers. If the incoming voltages represent functions in time, particularly transform bases like sine and cosine, then we are performing computations analogous to matrix image transforms. The output is a continuous stream of each row of the transformed image, repeated at a desired frame rate. This approach is enabled by floating-gate circuits in storing arbitrary analog waveforms for image transforms, in programming waveforms to account for average device mismatch, and in performing additional matrix-vector computations.

This transform imager can compute arbitrary separable 2D linear operations. These operations are expressed as two matrix multiplications on the image

\[ Y = A^T PB, \tag{1} \]

where \( P \) is the image array of pixels, \( Y \) is the computed output image array, and \( A \) and \( B \) are the transform matrices corresponding, respectively, to the transform on the image plane by the basis functions and the transform matrix corresponding to the floating-gate-enabled transform after the image plane. The values of \( A \) and \( B \) are stored in an analog floating-gate array typically on the imager IC and applied to the pixel columns. Furthermore, if the input waveforms are continuous, then the result is a continuous waveform, resulting in added computational options. For example, the choice of output signal sampling will result in different discrete-time inspired computations with an identical setup.

3.3. Application of the transform imagers

The transform imager architecture is both modular and programmable making it ideal for image dataflow computations. This architecture’s scalability makes it feasible to compute image operations at large-scale resolutions comparable to those in digital cameras. Furthermore, the image processing architecture computes on the image plane, thus allowing for data reduction that is compatible with machine vision and biological modeling. The image sensor can be used to subsample the incoming data if desired, or if the resulting system can handle the data rate, the full image can be passed on so that easier refinement can occur farther up the processing chain. The additional processing may be in analog circuitry or a digital system.

This architecture is modular because the output dataflow is a sequence of columns from an image. This image is either from a set of sensors or the output of some signal processing. We can have multiple image processing steps, where each intermediate result can be acquired by the controlling digital system for higher levels of processing. Furthermore, the outputs are continuous waveforms, allowing time-domain filters to be used to obtain spatial responses and image interpolation.

One must also consider the interface between computational blocks. A 1024 × 1024 imager computing at a 60 Hz image rate requires a parallel data rate (1024 signals) of 60 kHz. If two blocks are adjacent on the same IC, then this data rate is trivial to accommodate. However, if these signals are being passed between chips over 100 mega analog samples per second are required, which is a more challenging specification. This rate is similar to reading out pixels from any standard CMOS array. Each pixel could be directly read out in a transform imager, since a column scan is equivalent to multiplication by a digital value moving by one position for each step. In general, this issue is significant when interfacing to a digital system, since multiple “images” could be transmitted to the controlling digital system.

Separable matrix image transforms

Separable systems play an important part in image processing because of their simplified design and implementation. A 2D system is said to be separable if it (i.e., the impulse response) can be expressed as a product of two functions of one
variable each:
\[ h[n_1, n_2] = h_1[n_1]h_2[n_2]. \] (2)

A separable system can operate on the columns and rows of an image independently. As a result, a separable system can be written as a pair of matrix operations as in (1). The left-hand side matrix \( A^T \) operates on the columns of the image \( P \) and the right-hand side matrix \( B \) operates on the rows of the image.

In image processing, the most common linear operations consist of FIR filtering and real transforms such as the discrete cosine transform (DCT) or wavelet transforms. Examples of the left-hand side matrices, \( A^T \), for these operations are shown in Figure 5.

The range of operations possible within the architecture and expressed in (1) is significant. For example, it is possible to use differentiating FIR filters to do better edge detection or lapped orthogonal transforms for image compression without blocking artifacts. Smoothing filters combined with a decimation scheme could provide simple data reduction. Arbitrary transforms can be considered, because computational complexity and efficient algorithms are not a concern. Additionally, cascaded operations can be performed by collapsing the matrices describing the multiple operations:

\[ Y = C^T[A^T PB]D = \hat{A}^T PB, \] (3)

where \( \hat{A} = AC \) and \( \hat{B} = BD \).

Note that even though arbitrary matrices can be used without considering traditional computational complexity, the connectivity complexity should be considered. For example, a full image transform requires the instantiation and routing of the full transform matrices while a block transform can be implemented using only enough elements and interconnects for the nonzero transform matrix elements.

Temporal filtering

One interesting question with this flow model is how to perform temporal filtering. We can either build the filters directly into the pixel, which would result in much larger pixels and greatly increase the system cost for a given resolution, or we can store a delayed version of the transformed image. This approach requires a temporary storage array for currents or voltages for each delay thus limiting the number of temporal delays that can be built in practice (Figure 6). Our approach is to build a set of current mode sample-and-hold elements into an array that can be used for temporal filters. Dynamic current sources can be built that store their currents at reasonable accuracy for seconds, particularly with on-chip compensation of leakage through MOS-FET switches.

Applications of temporal filtering include subtraction of constant background images, temporal differencing, motion estimation, and, by using an array of floating-gate elements instead of the sample-and-hold elements, fixed images such as offset errors from dark currents may be subtracted out. In general, however, temporal filters should be used sparingly or after spatial compression due to the number of required sample-and-hold elements.

One could imagine combining these temporal filters as well as the spatial filters of the transform imager approach to be a front-end processor to compute optical flow.

### 3.4. Comparison of transform imagers with existing technologies

Focal-plane processing is characterized by significant amounts of signal processing occurring at the image plane, but usually at the cost of a small fill factor. Early retina model systems used focal-plane processing to mimic the edge enhancement properties in the early retina processing based on photodiodes and phototransistors that naturally occur in a silicon CMOS process [12, 13, 14]. Later designs improved so as to be usable in systems at high density levels [14, 15, 16] and for high performance [44]. From these retina chips, several higher level processing ICs have been built to investigate stereo processing [17, 18], communication architectures for action potentials [19], attention computations, and motion [20, 21, 22, 23, 24, 25, 26]. Typically, because of the large pixel size associated with the large number of transistors in each pixel, image sensors with retinal computation typically only have a fairly small number of pixels on a given IC. In only a very few cases, one will see more than 50,000 image elements on a fairly large IC [14]. Therefore, retinal processing imagers and research are focused primarily on machine vision tasks where the required pixel count can be smaller; for example, flies accomplish amazing things with the resolution from a small number of pixels [25, 26]. Although much can be explored in vision problems at the level of flies, many neuromorphic visual signal processing systems aim toward modeling much larger organisms.

APS imagers took a related route to the silicon retina models. These approaches, typically credited to Fossum, et al., [1, 2, 3, 4, 5, 6, 7, 8, 9, 11, 45] worked with photodiode-based arrays with minimal circuitry in the pixel, resulting in large imaging arrays, and therefore, a technology viable for digital cameras and more sophisticated computations. To characterize the spatial efficiency of a pixel, the concept of fill factor, which equals the ratio of image sensor area over the pixel area, is defined. The larger fill factor implies better spatial resolution per unit area. Typical APS imagers have fill factors from 30–50%, while typical focal-plane imagers have fill factors around 1–4%.

The question is whether one can combine the high fill factor advantages of APS imagers with the computational capabilities of retinal processing imagers. A few approaches try to bridge this gap [7, 8, 10, 19, 46, 47, 48], but they only begin to unlock the potential of these approaches. For example, the introduction of floating-gate circuits can enhance the performance of imager elements, but often straightforward application of these circuits results in larger pixels, and therefore, a decreased fill factor. Furthermore, these retina approaches have not been elegantly merged into a single circuit architecture; therefore, even in the design of retina ICs, several hard trade-offs remain.
The transform imager can perform many types of operations of the type $Y = A^TPB$, where $A^T$ operates on the columns of the image $P$ and $B$ operates on the rows. Examples of $A^T$ are shown here for different types of operations. (a) A transform of the entire image where $h_{ij}$ represent the windowed transform basis elements. (b) Block transform of the type more likely to be used in image compression. (c) FIR filter applied to the image, note that the corner coefficients are denoted with ’s because they are often normalized to account for the shorter length of the filter at that point; or they may be changed to accomplish filtering of a symmetrically extended image with $h'_0 = h_0$ and $h'_1 = 2h_1$, and so forth. (d) Wavelet transform of the image, note that a block wavelet transform could be also applied.

![Image Transform Matrix Examples](image)

### 4. Basic Transform Imager Pixel Element(s)

This section describes the first block of this architecture, the basic transform imager. We discuss the basic processor structure of the computation (multiplication) of the sensor signal in each pixel. This approach could include more advanced image sensor elements/circuits with a corresponding modification to the resulting fill factor. We present experimental data from an instrumented $14 \times 14$ image block, requiring roughly $150 \times 200 \mu m$ for the array in a $0.5 \mu m$ CMOS process. We present results from a signal pixel, the resulting computation, and effect of mismatch and offsets throughout this circuit.

These experimental results become the starting point to build large pixel arrays with the resulting floating-gate circuits. As a result, we need to have an analytic foundation for scaling these systems and for estimating system performance. The goal for the analytical discussions of these circuits is 1-million pixel arrays, which we configure as a $1024 \times 1024$ array of pixels, that operate at 60 frames a second. We have already built arrays up to $512 \times 512$ in size, and have plans to reach the $1024 \times 1024$ size in the near future.

![Imager Architecture](image)
we can express the difference (which should always be the case due to the low-level input sensitivities). For sufficiently small differential input voltages, we get a linear multiplication, as illustrated in the resulting experimental data. The simplicity of the pixel circuit results in fill factors competitive with APS imagers. (b) Floating-gate transistor. This circuit can store a current based upon the charge at the floating-gate node. Therefore, we use this element to store the basis functions for the transform imagers. This circuit can also be used as a transistor, and when operating with subthreshold currents, this transistor computes a product of the input voltage with the stored current. Therefore, we use this element in the matrix-vector multiplication memory arrays.

4.1. Basic pixel element

Each pixel is composed of a photodiode sensor element and an analog multiplier. Figure 7a shows that the circuit element for this multiplication is an nFET differential pair. For the differential pair operating with subthreshold bias currents (which should always be the case due to the low-level image sensor currents), we can express the differential output current as [12]

$$I_1 - I_2 = I_{\text{sensor}} \tanh \left( \frac{\kappa (V_1 - V_2)}{U_T} \right).$$

where $\kappa$ is the gate coupling efficiency into the transistor surface potential (typically 0.6–0.8), and $U_T = kT/q$. If $V_1 - V_2$ inputs are such that the circuit is in its linear range, then we get

$$I_1 - I_2 = I_{\text{sensor}} \frac{\kappa (V_1 - V_2)}{U_T}$$

or the product of the sensor output and the differential input voltage.

The experimental data in Figure 8 shows that we get a linear multiplication within the linear range, as expected. A single pixel would result in 300-pA current levels from typical room fluorescent lights at roughly 2 m from the imager without a lens to focus the light. A single pixel could include more advanced image sensor elements/circuits with a corresponding modification to the resulting fill factor. Additionally, each pixel could be directly read out by this technique, since a column scan is equivalent to multiplication by a digital value moving by one position for each step ($\tanh(x) \approx 1$ or $-1$ for large $x$ magnitudes).

Offsets in differential pairs are important for most analog design problems and are not exception for this imager. Small input offset voltages result primarily in a DC output current and have a small effect on the resulting algorithm. Because each pixel value is modulated by the incoming basis waveform, we have no signal at DC, and therefore, we filter out the DC signal. On the other hand, large input offset voltages result in no output signal, since one transistor of the differential pair pulls all of the sensor current. Pixels with these large offsets will result in significant image distortion at these points. Figure 9 shows the measured input voltage offsets for
our pixel array. We found that most of the offsets were within 10 mV of the other elements along the column. We can account for average column offsets by appropriately programming the input basis functions. These offsets can be further reduced by improving the matching of the two devices. We used (W/L) of 1.8 μm/1.8 μm in a noncommon centroid layout geometry. With a slight reduction in fill factor, the mismatch could be significantly reduced. In applications where very high performance (and therefore nearly zero offsets) is required, one can use floating-gate tuning techniques for pixel elements [11] or differential pairs [38], with the accompanying decrease in fill factor.

Our measurements show that a single pixel element exhibits little change from DC to 100 Hz for typical fluorescent lights. This frequency response will be dependent upon the incoming light levels. We observe a corner frequency at 30 Hz for four orders of magnitude of light intensity lower than average room light. From these measurements, we expect sufficient bandwidth for a 1024 × 1024 imager performing full-matrix operations at a 60 Hz image rate.

4.2. Modeling computation errors in transform imager computations

In practice, the elements will not be perfect multipliers and will not be exactly identical to the other elements. If we assume that one linearly encodes the broadcast gate voltages as the sensor modulation signal (by programming), then the errors encountered in this architecture can be divided into three categories.

1. **Gain error**—primarily due to κ mismatch in the differential pair transistors. Typically κ matches fairly well for transistors with similar currents and for source voltages at similar voltages.
2. **Offset error**—primarily due to offsets in the differential pair transistors. As long as the modulation signal is roughly within the linear range of the differential amplifier, we can eliminate offsets by eliminating the low frequency signal (less than the frame rate) from the result, because there is no signal at these low frequencies (we are modulating the pixels) except for the effect of offsets.
3. **Harmonic distortion**—primarily due to harmonic distortion in the differential pair transistors: Harmonic distortion effectively results in spreading modulation energy to other pixels. This spreading is independent of the sensor signals since the modulation signal stays at the same amplitude. We show below that one can modify the modulation signals to account for this spreading such that the transform is effectively free of this signal spreading.

We focus on multiplication errors because addition of currents by KCL is an ideal computation. Another source of error comes from the dark currents, which are typically in the fA range and therefore, are important for pixels operating in low-light levels. We can use floating-gate elements to eliminate them, as shown in Figure 6.

One can modify the modulation signals to account for this spreading such that the transform is effectively free of this signal spreading. To analyze this problem, we decompose all modulated signals, x(t), into a finite Fourier series because the signals repeat for each frame, and the signals have a maximum frequency by the clock rate of the basis generator. We write the Fourier series as

\[ x_k(t) = \sum_{\ell=-N}^{N} a_{k \ell} e^{j\omega_{\text{frame}} \ell}, \]  

where \( a_{k \ell} \) is the \( \ell \)th coefficient for the \( k \)th signal, and \( \omega_{\text{frame}} \) is \( 2\pi \) times the frequency of the frame rate. Note that \( a_{k0} = 0 \) because there is no DC signal component. In matrix form, \( x(t) = Af(t) \) where \( f(t) = e^{j\omega_{\text{frame}} t}. \) The output from the imager is

\[ y = Px = PAf(t), \]  

where \( P \) is the matrix of sensor values. If the multiplication distorts the computation (i.e., from the differential transistor pairs), we can reformulate the result of second, third, and higher-order harmonics by modifying \( A \) by \( A_1 \), which takes these terms into account. Furthermore, we can invert this process to modify the starting matrix \( A \) to get a matrix \( A_1 \), which gives the desired transform of interest. The correction will depend on the desired transform.
4.3. Bandwidth of the transform imager

Since we are modulating the input pixel currents, one should consider the highest modulation frequency that a particular pixel can support. We define the bandwidth as the highest frequency (i.e., the fastest generated signal) minus the lowest frequency (i.e., the frame rate or block rate); typically assuming that the bandwidth as related to the highest frequency is sufficient. This maximum frequency/bandwidth defines a trade-off between the resulting frame rate and the number of available pixel elements. We are looking at the frequency response for a differential signal, therefore, the source node of the differential pair is nearly fixed. Sensor capacitance and any capacitance in parallel with the phototransduction sensor have negligible effect on the frequency response.

For example, for a 1-million pixel imager \((1k \times 1k\)-pixel array), we need 60 kHz modulation for a 60 Hz frame rate. If the current output lines use one-stage active feedback (as used in the adaptive photoreceptor [44]) to reduce capacitive effects, then we could approach these frequencies for 10 pA of sensor current. A limit of 10 pA significantly limits the range of input illumination, for lower currents either the image size must decrease or the frame rate must slow down accordingly.

We can reduce this minimum current level by using stronger active feedback or by changing the phototransduction method in the pixel cell. Stronger active feedback will improve the frequency response at a given current, and therefore reduce the minimum current that can be modulated. The stronger, active feedback requires more gain, and therefore more power consumed and increased stability issues. One can change the phototransduction element to a vertical BJT to amplify the current, but this approach results in a more than proportional increase in the element noise, as well as decreases in pixel-circuit fill factor. Experimental measurements have qualitatively verified these results.

Often, early levels of image processing are based upon block transforms rather than full image transforms, and the bandwidth behaves similarly. For block processing, we often turn on a basis block when being used, and turn it off when not being used. The frequency response of turning on or turning off a block is fairly quick for both operations. Turning on the block, which means we are bringing up the resulting output voltage, looks like a source follower, using nFETs on the upswing. That is, we are working on the fast transition region of this circuit. Turning off the block, which means we are pulling down the resulting output voltage, looks like we quickly drop the gate voltage below the source voltage, and therefore, the current through the differential pair FETs is very small.

4.4. Signal-to-noise issues in transform imagers

Since we are using fairly low subthreshold currents, thermal noise contributes to most of the transistor noise. Thermal noise is modeled as [49]

\[
\frac{\Delta f^2}{I^2} = \frac{2q}{\Delta f} \Delta f,
\]

where \(I\) is the current level. The bandwidth \((\Delta f)\) is approximately the highest frequency (i.e., the fastest generated signal) of the basis generator. For the 1-million pixel example in Section 4.3, \(\Delta f = 60 \text{kHz}\), resulting in a relative noise level of 0.14 for a 1 pA bias current through a single transistor.

Due to the low currents (subthreshold), \(1/f\) noise only becomes noticeable at low frequencies (e.g., 10 Hz). Furthermore, noise generated at frequencies less than the frame rate will be eliminated from the final computation, so the low \(1/f\) noise will not affect these circuits. This property is similar to the computation in correlated double-sampling techniques. Therefore, we only need to address thermal noise generated from the sensor circuits.

The noise comes from two sources. First, we get one differential pair worth of noise due to the differential pair transistors on the photodiode. Second, we get two differential pairs worth of noise at the sensor’s bias current due to the basis generation structures. For very small signals, the system looks like a current mirror for small signals with different transconductances (the gain = \(g_{m2}/g_{m1}\)), resulting in two differential pairs worth of noise (two because of no common-mode rejection for this circuit component). Since each noise source is independent of the other noise sources, the noise power of each source increases linearly with the number of sources (\(N\)). Therefore, the noise relative to the signal from a single pixel is

\[
\frac{\Delta f^2}{I^2} = \frac{2qN}{I} \Delta f
\]

for the 1-million pixel example above, the relative noise level for the entire pixel sensor is 6.73 (−16.6 dB) for a 1 pA bias current in a single sensor and 0.673 (3.43 dB) for 100 pA bias current. For a completely correlated feature, which means all 1-k elements contribute to a large output signal, we get a relative noise level of 0.0066 (43.6 dB) for 1-pA bias current level. Therefore, for this imager setup, either higher illumination or more coherent features (features selected by the basis generator) result in increased higher SNR. This SNR value is better than the SNR if we acquired each pixel at the 60 Hz frame rate; therefore, correlated features have the higher SNR as reading the pixel array, but uncorrelated pixels will have lower SNR.

5. Imager System Results

We will discuss the overall computation using a 14 × 14-pixel array in the context of DST and DCT transforms. The results can be extended to arbitrary matrix transforms. For this paper, we will concentrate on computing a DST/DCT-like transforms of the image as a representative of possible matrix computations. To characterize this imager, we will compute these transforms for uniform illumination. The ideal DST would be all zeros, and the ideal DCT would be an impulse at position (1, 1).

We present experimental data from a small 14 × 14 image block, requiring roughly 150 × 200 µm for the array in a 0.5 µm CMOS process. Figure 10 shows the results of
DST/DCT-type transforms on a uniformly illuminated image. We input sine waves of integer frequencies and obtained the first image result by sampling at $\pi/2$ phase of the primary harmonic. This transform is symmetric, so we show only the first half of the output waveform. From the resulting waveforms (not sampled waveforms), we computed the second matrix transform using DST coefficients and then for DCT coefficients. We see some distortion in the transformed images, which correlates well to harmonic distortion from the differential pairs. Since the input patterns are fixed, the effect of harmonic distortion is fixed and appears as an additional spatial (smoothing) filter. In practice, we can account for this additional linear spatial filter by modifying the matrix transform coefficients to account for it. In the same process, we can scale to a $128 \times 128$ imager with matrix processing for $16 \times 16$ block transforms in an area of $4 \text{ mm}^2$.

We have built several functional imagers in 0.5 $\mu$m CMOS technology of sizes $16 \times 16$, $48 \times 48$, and $128 \times 128$. The $128 \times 128$-size imager uses a block transform window of sixteen, therefore requires an array of $252 \times 16$ floating gates, to store the required basis functions. All of these systems contain the necessary control circuits that allow for programming of individual floating gates. We program the floating-gate elements to arbitrary values using an external programming board that only requires an external power supply and standard RS-232 computer interface. We describe this board elsewhere [28]. We test our imagers by projecting a directed light source on our imager through a complex lens system. During our experiments, we have seen little noticeable movement of the floating-gate elements from their respective programmed values. Figure 11 shows an output image from one of our $128 \times 128$ transform imagers.

6. CONCLUSION
We introduced our transform imager technology and architecture. Transform imagers borrow both from focal-plane imagers like retinas as well as standard APS and random-access imagers to create this unique architecture. Our transform imager cell performs computation at the pixel plane, has a fill factor greater than 40%, and allows for retinal and advanced biological-type processing in a programmable architecture. Therefore, we have the best of both worlds in a single architecture.

Our new imaging architecture is enabled by programmable floating-gate circuits built in standard CMOS (single or double-poly) processes. The floating-gate circuits allow for arbitrary pattern generation as well as analog matrix-vector multiplication of images. This imager is capable of programmable matrix operations on the image, where we can represent the image as either a full matrix or using
block matrix operations. The resulting dataflow architecture directly allows computation of spatial transforms, motion computations, and stereo computations, in a straightforward on-chip or multi-chip architecture.

Each pixel is composed of a photodiode sensor element and a multiplier. We have presented experimental data from several transform imagers (14 × 14, 16 × 16, and 128 × 128 arrays) showing the performance of the pixel, mismatch between pixels, and basic transform results. We are currently in the process of further testing this imager architecture for various applications.

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