Keywords: gearbox, wind turbine, condition monitoring, thermal modelling

Abstract

This paper details the development of a mathematical thermal model of a small wind turbine gearbox for use in condition monitoring. The model was optimised and partially validated using experimental data from a wind turbine drivetrain test rig. The model was then used to mimic bearing faults, by simulating additional heat losses at respective faulty components. The extent to which the thermal behaviour changed as a result of a fault was studied, with a view to use such an approach to detect and locate faults.

1 Introduction

In this work, the authors propose creating a mathematical model of a wind turbine gearbox so that when a fault occurs, the failure can be diagnosed, located and a prognosis can be developed. Through this modelling, a better understanding of the physics of failure will be obtained allowing failure prediction and in turn, reduce downtime when a failure occurs. This is especially useful when historical operational data is unavailable and/or diagnostic/prognostic models are transferred from other gearbox types. Thermal modelling based on the principles of heat transfer theory is used to develop this understanding, exploiting temperature measurements to understand a ‘healthy’ gearbox and then use it to detect and locate abnormal gearbox operating conditions.

2 Nomenclature

| Symbol | Description |
|--------|-------------|
| $P_a$  | Power in (W) |
| $n$    | Rotational speed (rpm) |
| $c$    | Specific heat capacity (J kg$^{-1}$ K$^{-1}$) |
| $T$    | Temperature (K) |
| $m$    | Mass (kg) |
| $b$    | Tooth width (mm) |
| $b_0$  | Reference width (10mm) |
| $Q$    | Heat flow (W) |
| $v_t$  | Peripheral speed at pitch circle (m/s) |
| $v_{r0}$ | Reference speed (10 m/s) |
| $d_m$  | Mean bearing diameter (mm) |
| $d_{sh}$ | Shaft diameter (m) |
| $\nu_{oil}$ | Kinematic viscosity of oil (mm$^2$/s) |
| $F_a$  | Bearing thrust load (N) |

3 Background

Wind turbine gearboxes operate under conditions subject to a broad spectrum of load and speed variations creating difficulties in predicting reliability and preventing failures [1]. Gearbox failure incurs high costs for repair in addition to lost revenue from high downtime per failure. The lengthy lead time and time typically cause an increase in the cost of energy [2].

Condition monitoring refers to processes that focus on early detection of faults, failures and wear of machinery with the intention of minimising downtime, operation and maintenance costs while maximising production [3]. Different techniques have been applied to diagnose gearbox failures in the main looking at vibration, oil quality and temperature with thresholds on sensor outputs used as fault indicators. State of the art remaining useful life methodologies predominately use data-driven machine learning techniques to predict failure, these so-called ‘black box’ approaches rely on large amounts of operational data and failure histories. The variable speed nature of modern wind turbine operation can be challenging for a conventional spectral-based method of fault diagnosis [4].

Exploiting temperature measurements to detect abnormal gearbox operating conditions is based on the theory that gearboxes generate power losses in the form of heat. It can be assumed that any degradation on the contact surface will generate more losses and thus a different thermal distribution will occur [5]. Most modern wind turbines (which use gearboxes) measure the gearbox temperature as a proxy of gearbox health.

4 Method

The gearbox used in the study is from an 11kW wind turbine. Relevant technical details of the gearbox are listed in Table 1.

| Description | Value |
|-------------|-------|
| Rated Power | 17.7 kW |
| Gearbox ratio | 18 |
| Type | 2 stage, parallel axis |
| Lubrication | Oil Splash |
| Orientation | Vertical |

Table 1: Gearbox Specifications
4.1 Thermal Modelling

The gearbox is modelled in MATLAB Simulink using the Simscape package. Thermal network modelling can be equated to electrical circuit theory by analogy where resistance to heat transfer is equivalent to electrical resistance, heat flow equates to current, temperature difference is equivalent to potential difference and thermal mass to capacitance [6].

To create the thermal model, the gearbox components are split into a number of lumped mass isothermal nodes. The heat transfer between nodes are shown in Figure 1, where the black lines represent the component nodes, labelled at the top of the figure. Linking these nodes are thermal resistances, representing heat transfer by conduction, convection and radiation. Losses are introduced at the respective nodes. Heat flows between nodes can be calculated, as temperature differences.

![Figure 1: Thermal Model Network Diagram](image)

4.1.1 Heat Transfer

The heat propagation through the gearbox is made up of different modes of heat transfer which are used in the thermal model as thermal resistances $R_{th}$, as shown by (1). The heat flow is via conduction, convection or radiation.

$$R_{th} = \frac{dT}{Q}$$ (1)

Each component in the gearbox acts as a thermal mass, retaining heat. The change in flow is dictated by (2).

$$Q = c\, m \frac{dT}{dt}$$ (2)

4.1.2 Power Losses in a “Healthy” Gearbox

To measure the heat propagation of the gearbox, heat needs to be inputted into the model. The model assumes that any power loss in the gearbox eventually appears in the form of heat. The losses are generated by rotating parts; the interaction between the shaft, gears and bearings and their interaction with the air and lubrication. The total losses from different component parts are a mixture of load dependent and load independent losses as shown in (3). Each loss type can be estimated numerically, for the difference gearbox stages.

$$\sum P_T = \sum P_{GD} + \sum P_{GI} + \sum P_{BD} + \sum P_{BI} + \sum P_S$$ (3)

$P_{GD}$ Load dependent gear losses
$P_{GI}$ Load independent gear losses
$P_{BD}$ Load-dependent bearing losses
$P_{BI}$ Load independent bearing losses
$P_S$ Seal losses

Load Dependant Gear Losses

Gear contact losses occur when gear teeth are in contact. The standard ISO/TR 14179-2:2001 [7] for calculating thermal losses uses equation (4). It uses a gear loss factor ($H_g$) which accounts for gear geometry and a mean coefficient of friction ($\mu$). This method is widely used in other literature relating to gearbox efficiency [8] [6] [9] [10] [11].

$$P_{GD} = P_a \, \mu \, H_g$$ (4)

Load Independent Gear Losses

Load independent gear losses are made up of air windage and oil churning. For splash lubricated gears, oil churning is considered a major source of power loss [12]. Churning is dependent on rotational speed, immersion depth in the sump and lubricant viscosity [8]. A simple approach to calculating churning losses in [7] is used, with equations (5)-(9).

$$P_{GI} = \sum_{i=1}^{n} T_{HI} \frac{\eta_{hi}}{30}$$ (5)

$$T_H = C_{Sp} C_{Te} \left( \frac{v_e}{v_m} \right)$$ (6)

$$C_{Sp} = \left( \frac{2h_{c, max}}{3h_c} \right)^{1.5} \frac{2h_c}{l_h}$$ (7)

$$C_1 = 0.063 \left( \frac{h_{c1} + h_{c2}}{h_{c0}} \right) + 0.0128 \left( \frac{b}{b_o} \right)^3$$ (8)

$$C_2 = \frac{h_{c1} + h_{c2}}{800 h_{c0}} + 0.2$$ (9)

where $h_{c1}, h_{c2}, h_{c0}, h_{c, max}, h_c$ and $b_o$ are all related to the geometry of the gearbox and oil sump. This approach was used based on the gearbox information available from design drawings; there are other more detailed approximations of churning losses [12] [10] [9] [13] that could be used for future thermal model development.

Load Dependant and Load Independent Bearing Losses

An experimental approach to bearing losses is used by [14]. Experimental data is used to estimate coefficients of friction that contribute to the total frictional torque which is split into rolling, sliding, seals and drag losses. This approach includes a number of numerical factors, unknown for this gearbox so the approach, described in [7] was used, as listed in equations (10)-(14).

$$T_B = T_{BLO} + T_{BLP1} + T_{BLP2}$$ (10)
Load Independent:

If \( v_{oil} n < 2000 \frac{mm^2}{s} \cdot min \)
\[
T_{BLO} = 1.6 \times 10^{-8} f_0 d_m^3
\]  
(11)

If \( v_{oil} n \geq 2000 \frac{mm^2}{s} \cdot min \)
\[
T_{BLO} = 10^{-10} f_0(v_{oil}n)^{2/3} d_m^3
\]  
(12)

Load-Dependent:

for radial loading
\[
T_{BLP1} = f_1 P_1^2 d_m^6 10^{-3}
\]  
(13)

for cylindrical roller bearing additional thrust loading \( (F_a) \)
\[
T_{BLP2} = f_2 F_a d_m^6 10^{-3}
\]  
(14)

where:
\( f_1, P_1, f_2 \) and \( a \) and \( b \) are from look up tables in [7].

Seal Losses
Equation (15) is used widely for calculating contacting, radial shaft seals [7][13].
\[
P_s = 7.69 \times 10^{-6} d_m^2 n
\]  
(15)

4.3 Experimental Validation

Once the mathematical model was created, it was partially validated by experimental data using a wind turbine drive train test rig located at the University of Strathclyde. For operational wind turbine gearboxes, there are usually at least three temperature sensors installed: the main bearing, high-speed shaft bearing and gearbox oil [15]. As this gearbox is in the University lab, sensors can be added in more locations. Allowing for restrictions in the geometry of the gearbox, a sensor system was designed and installed to correspond to the individual gears and shafts. This configuration is shown in Figure 2. These are held in very close proximity to the shafts and gears.

![Figure 2: Temperature Sensor Set-up](image)

The test rig is made up of two identical gearboxes back to back, driven by a motor, controlled by a torque and speed control unit. One of the gearboxes is set up with the temperature sensors and a torque meter is fitted to the output shaft. The data acquisition instrumentation was made up of TMP35/6/7 temperature sensors connected to an Arduino Mega. The operating conditions were set at 968 Nm and 57 rpm, giving an output power of 5.8kW, approximately half the rated power of the small wind turbine it is designed for.

5 Results

5.1 Verification of Model using a “Healthy” Gearbox

To compare the experimental data with the thermal model, the data was filtered to remove the noise for a clearer comparison. Figure 3 shows the temperature measurements as the difference from ambient temperature, from experimental data (solid lines) and thermal model (dashed lines). The temperature results from the thermal model at the gear nodes are in general agreement with the experimental model. In some cases, they were lower than those of the experimental data, suggesting that the calculated losses at the gear meshes were underestimated in the model, that there are differences in the thermal resistance network or that the measurements are not accurate (e.g. due to indirect temperature measurement).

![Figure 3: Experimental & Numerical Temperature Measurements](image)

The experimental data shows all components increasing in temperature at a similar rate of change. There is a significant difference between the low speed and intermediate speed gears which is explained by the larger effective thermal resistance between the intermediate speed gears and ambient temperature as well as their different thermal capacities. It can be noticed that there is an inflection point in the experimental data between 1000 and 2000 seconds. It is postulated that this because as the temperature of the oil increases the viscosity reduces and the losses also drop. This feedback is not present in the model.

5.2. Further Results from “Healthy” Gearbox model

The thermal model can give temperature measurements for parts of the gearbox that would be difficult to access. Figure 4 and 5 show the temperature of the gearbox bearings and the oil sump and casing, respectively. The model running time was increased from 6000 seconds to 60000 seconds to clearly see when thermal equilibrium is reached. It should be highlighted
that due to the variable nature of wind turbine operation, a wind
turbine gearbox would rarely be in thermal equilibrium.

4.2 Use of Thermal Model to Investigate Gearbox “Fault”

The hypothesis that the model can be used to monitor a fault at the
component level was tested. To do this, extra heat losses were introduced into the model at the high-speed (HS) bearing
nodes to mimic fault heat. The bearing was selected in the first
instance as it is a common gearbox failure mode. Bearing failure
cause around 70% of gearbox downtime [3]. The top failure modes for bearings from a case study [16] found most common root causes is cracking, abrasion and adhesion/scuffing. To a
certain degree, these faults will all affect the friction within the
bearing and thus heat generated. However, the magnitude of this additional heat input in real gearboxes is unknown, it does not appear to be covered in available literature.

To model a fault in the high-speed bearing, an estimated
approach has been taken, where a step increase in heat flow is
added at the HS bearing node at 1/3 way into the total
simulation when it has reached thermal equilibrium. The temperature increase of different levels of fault are shown in
Figure 6. An important outcome of the thermal model is to
determine if a fault in a component can be detected elsewhere,
for example, the oil sump. A location commonly used to
monitor temperature for SCADA Figure 7 shows oil sump
temperature as a result of a “fault” at the HS bearing
temperature. These fault heat levels (10, 20 and 30W) represent
a 12.5, 25 and 37.5% increase in heat that is already present in
the healthy gearbox.

The same “Fault” process has been applied to the low-speed
(LS) bearing in the model to compare Figure 8. This gives a
similar result but with a lower equilibrium temperature due to its slower rotational speed and lower equivalent thermal resistance. The thermal behaviour of the oil sump (Figure 9) is
almost identical to a fault in the high-speed bearing.

Figures 8 and 9 show that using a single temperature
measurement, such as the oil sump temperature doesn’t give
much information about a fault location. However, if the
difference in temperature between two components is used, it yields more useful information.

Figures 10 and 11 show the difference in temperature between nodes, illustrating that faults in different locations produce different thermal behaviour. This suggests that multi-locational measurements alongside a thermal model should be able to locate faults.

It is suggested by [3] that an effective way to reduce the effects of the load is to monitor the difference between temperatures of components since both temperatures would increase with load and, their difference should be less dependent on load variation. This idea can be used to develop the thermal model further, especially when considering a range of operating conditions.

5 Discussion
The preliminary nature of this stage of research means there are a number of simplifications and uncertainties.

5.1 Uncertainties
Thermal network models rely on simplifying the gearbox components but it can be argued that isothermal approaches that rely on oil sump temperature may underestimate gearbox efficiency because the contributions of local temperature rises are ignored. Reference [6] suggests dividing the gearbox into a number of isothermal parts to account for these variations.

5.1.1 Heat Transfer Modes
Using a simplified model ignores more complex heat transfer interaction, for example, [6] introduced an additional heat transfer method, heat removal by centrifugal fling-off. Moreover, [12] added an additional thermal resistance to their model; strain, which is where a constriction of the thermal current from the surface to the gear centre occurs.

The temperature probes in the gearbox could provide a source of error. They add an additional thermal mass and heat propagation channel which wasn’t included in the thermal model.

5.1.2 Lubrication
The splash lubrication system relies on the rotation of the gears moving oil around the gearbox; the high-speed gears rely on the submerged low-speed shaft to distribute oil. From witnessing the gearbox during experimentation, it is effective in doing so. However, this means the chaotic nature of the lubrication system makes it difficult to model, especially the high-speed components as they aren’t in direct contact with the oil sump.

5.1.3 Data Acquisition
The data acquisition system for this research used simple thermocouple sensors with an accuracy of ±2°C in terms of uncertainty, as given in the specifications.

The design of the system had to account for the compact nature of the gearbox. Literature has found temperature measurement methods influence diagnostic capabilities, for example, data from thermography was found to be different from data from contact sensor [5]. Therefore, subsequent research will consider a more sophisticated data acquisition system. With the aim of improving precision by repeating experiments and using sensors with increased sensitivity.
5.2 Future Work

In addition to addressing the uncertainties previously discussed. Future work will involve validating gearbox faults experimentally by injecting known quantities of heat and inducing faults on test rig components. Also gathering data from a number of different operating conditions as changes to load will affect the thermal behaviour.

Using this thermal model in the context of condition monitoring will be an important further step. By posing the thermal model in a matrix format, it can then be inverted in a way so that temperature measurements can be used as an input to estimate losses at nodes. With a combination of temperature measurements, this could identify and locate a gearbox fault. Sensitivity analysis is required to determine how significant the uncertainties are in thermal modelling. Reference [17] identified 4 input parameters for sensitivity analysis using a Monte Carlo method. They found radiation and air velocity impacted oil sump temperature most. This is something that can be explored in future work.

6 Conclusions

This paper demonstrates the potential for thermal modelling to be used as a wind turbine gearbox condition monitoring tool by understanding changes in thermal behaviour. A “healthy” gearbox thermal model has been developed, modelling losses and heat transfer. The model was optimised and validated using experimental data and then used to mimic a component fault. It was found that single temperature measurements can’t necessarily detect or locate faults, but potentially a combination of temperature measurements could be used together to identify a gearbox fault. The method used in this paper allows further investigation into thermal behaviour of gearboxes as a result of a fault.

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