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File list (2)

- Embedded_Microbubble_Manuscript.pdf (7.90 MiB) [view on ChemRxiv] [download file]
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Embedded Microbubbles for Acoustic Manipulation of Single Cells and Microfluidic Applications

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Abstract

Acoustically excited microstructures have demonstrated significant potential for small scale biomedical applications by overcoming major microfluidic limitations. Recently, the application of oscillating microbubbles has demonstrated their superiority over acoustically excited solid structures due to their enhanced acoustic streaming
at low input power. However, their limited temporal stability hinders their direct applicability for industrial or clinical purposes. Here, we introduce the embedded micробubble, a novel acoustofluidic design based on the combination of solid structures (polydimethylsiloxane) and microbubbles (air-filled cavity) to combine benefits of both approaches while minimizing their drawbacks. We investigate the influence of various design parameters and geometrical features through numerical simulations and experimentally evaluate their manipulation capabilities. Finally, we demonstrate the capabilities of our design for microfluidic applications by investigating its mixing performance as well as through the controlled rotational manipulation of individual HeLa cells.

**Introduction**

Precise manipulation capabilities at small scales are of increasing importance for a wide variety of research fields such as biomedicine or biology, e.g., for the investigation of morphogenesis through single-cell analysis or detailed 3D reconstruction of complex model organisms.\(^1,2\) Therefore, it is not surprising that a large number of techniques have been introduced to facilitate the controlled rotation of small particles based on mechanical, magnetic, electrical, hydrodynamic, and optical forces.\(^3\) Unfortunately, many of these techniques rely on specific properties of the specimen, which significantly reduces their applicability for biological samples. The controlled particle manipulation using acoustic forces, acoustophoresis, has been widely applied due to its advantages of being label-free, contactless, and flexible in design while exposing biocompatible behaviour.\(^4\)

Recent publications have illustrated a large variety of microstructures suitable for the controlled manipulation of single cells and particles through acoustic forces. Solid features such as polydimethylsiloxane (PDMS) or silicon sharp-edges are acoustically excited *via* an external piezoelectric transducer, leading to the formation of acoustic streaming patterns in the nearby liquid.\(^5-8\) Unfortunately, the majority of these acoustofluidic setups require a
high input power to generate acoustic fields that are strong enough to manipulate the specimens, which might damage biological samples. Additionally, depending on their design and arrangement, hydrophilic surface coatings are required to prevent the unintended formation of air bubbles which otherwise significantly alter the anticipated streaming patterns. Furthermore, most solid-feature-based designs are limited to the generation of in-plane vortices and are, therefore, unable to provide additional visual insights through the re-orientation of the specimen.

To overcome these challenges, microstreaming induced by an oscillating microbubble can be utilized. The streaming patterns of the microbubble can be switched from in-plane to out-of-plane streaming via altering the excitation frequency, allowing for controlled three-dimensional rotations of cells and organisms, as well as microfluidic applications including pumping or mixing. Due to its high compressibility and the corresponding strong oscillations, the microvortices produced by acoustically-activated microbubbles are significantly enhanced compared to the ones caused through the vibration of solid structures. However, the major drawback of microbubbles is their limited temporal stability. If acoustically excited, rectified diffusion leads to the bubble’s growth, which alters its resonance frequency and by that the strength and shape of the vortices. This process can be decelerated using commercially available encapsulated bubbles; however, the instability of the thin polymer membrane of encapsulated bubbles complicates their application for long-term investigations. Lastly, as microbubbles are prone to be trapped in cavities due to hydrophilic/hydrophobic interactions, their dimensions show slight variations between multiple experiments, making it difficult to predict their precise response to acoustic excitation and preventing their use for clinical applications.

In this work, we introduce the embedded microbubble, a novel PDMS-based microstructure combining the low power advantage of bubble-based acoustic streaming with the temporal stability of acoustically-excited solid features. We perform in-depth numerical investigations and quantify the influence of geometrical parameters, such as the PDMS wall
thickness or the microbubble’s length, on the acoustic streaming inside the fluid channel and utilise these findings to optimise our device design. The manipulation capabilities of our acoustofluidic lab-on-chip are analysed through experimental characterisations and the revealed insights are discussed in further detail with respect to the numerical results. Finally, we highlight our device through the controlled and reliable out-of-plane rotation of single HeLa cells; a task beneficial to improve our understanding of biological processes on the cellular and sub-cellular level, and demonstrate the relevance of our approach for additional microfluidic applications through its use for mixing; a key step required for a wide variety of biomedical as well as chemical research.

**Materials and Methods**

**Governing Equations**

The force responsible for moving small (relative to the acoustic wavelength) particles in an acoustic field is called acoustic radiation force (ARF). For an inviscid fluid, it is given by the negative gradient of the Gor’kov potential\(^{22}\)

\[
F_{rad} = -\nabla U, \tag{1}
\]

which can be expressed as:

\[
U = \frac{4}{3} \pi r^3 \left( \frac{1}{2} \langle p^2 \rangle \frac{f_0}{c^2 \rho} - \frac{3}{4} \rho \langle f_1 \rangle \langle v^2 \rangle \right), \tag{2}
\]

with the particle radius \(r\), the incident acoustic pressure field \(p\), the acoustic velocity field \(v\), the fluid speed of sound \(c\), the density of the fluid \(\rho\), the monopole \(f_0\) and the dipole \(f_1\) scattering coefficients. \(\langle . \rangle\) denotes time averaging

\[
\langle x \rangle = \frac{1}{\tau} \int_{t_1}^{t_1+\tau} x \, dt, \tag{3}
\]
where \( \tau = \frac{2\pi}{\omega} \) is the period of oscillation, with angular frequency \( \omega \). The Gor'kov potential is derived under the assumption that boundaries are far away from the region of interest, which is not the case here. However, experimental studies revealed, that the theory should be valid up to close proximity of the embedded microbubble.\textsuperscript{23}

In acoustofluidics, the acoustic energy density is often used as a benchmark for the device’s performance and, therefore, used in our numerical analysis. The average acoustic energy density \( \langle E_{ac} \rangle \) is given as\textsuperscript{24}

\[
\langle E_{ac} \rangle = \frac{1}{V} \int_V \left( \frac{1}{2} \rho \langle v^2 \rangle + \frac{1}{2} \kappa \langle p^2 \rangle \right) dV,
\]

(4)

with compressibility \( \kappa \) and volume \( V \).

Another force that needs to be considered in our acoustofluidic chip is acoustic streaming, which affects a particle through a drag force:

\[
F_s = 6\pi \eta r (v_{str} - v_{prt}),
\]

(5)

with the fluid dynamic viscosity \( \eta \), particle radius \( r \), streaming velocity \( v_{str} \) and particle velocity \( v_{prt} \). The magnitude of the streaming velocity can be estimated as\textsuperscript{25}

\[
|v_{str}| = \psi \frac{v_a^2}{c},
\]

(6)

with the first order acoustic velocity \( v_a \), the fluid speed of sound \( c \), and the geometry dependant factor \( \psi = \frac{3}{8} \) for a standing wave parallel to a planar wall.

**Numerical Model**

We built a 2D numerical model of the chip and evaluated it in COMSOL Multiphysics (version 5.4). We specifically studied the frequency response of the device. At resonance frequencies, we looked at the wall displacement as well as the Gor'kov potential and streaming
velocity. First, a mesh study was conducted, to determine the converged mesh parameters (see Figure S-1). After the initial frequency domain study of the Thermoviscous Acoustics and Solid Mechanics interface, a stationary study of the Creeping Flow interface at the resonance frequency was carried out by taking the solutions from the first study into account. With this study, we were able to investigate the streaming velocity. Please refer to the Supporting Information SI-1 for a more detailed description of the numerical model.

Device Fabrication

The polydimethylsiloxane (PDMS) device was fabricated using photolithography techniques (see Figure S-2) as well as a Bosch process with an inductively-coupled plasma deep reactive ion etching (ICP-DRIE) tool (PlasmaPro 100 Estrelas, Oxford Instruments). The etching mask consisted of a 7 μm thick AZ nLOF 2070 layer. The effect of prominent reactive ion etching (RIE) lag was reduced through iterative parameter optimisations following an approach introduced by Lai et al.\textsuperscript{26} (see Supporting Information SI-2 and Figure S-3). The etch depth was 47.8 ± 0.7 μm. The processed silicon wafer was coated with silane (1H, 1H, 2H, 2H-Perfluorooctyltriethoxysilane, abcr GmbH) to ensure successful PDMS casting and prevent damage to the fragile polymer features. Subsequently, the designed structures were transferred into PDMS through moulding and chemically bonded to a microscope glass slide (AA00000102E01, VWR International) via oxygen plasma treatment. Finally, the transducer (KPEG-126, Kingstate) was fixed onto the glass slide using epoxy glue (UHU plus schnellfest, UHU).

Experimental Evaluation

Preliminary experiments to find the best excitation frequencies via attraction forces were performed with 10.29 ± 1.01 μm fluorescence polystyrene particles (FSEG008, Bangs Laboratories). When strong resonances were found, yeast cells, i.e., \textit{Saccharomyces cerevisiae}, bought from a local supermarket, were submerged in de-ionised water and injected into
the microfluidic channel to be used as tracer particles for the acoustic streaming. Given the limited visual accessibility of the out-of-plane vortices, experimental evaluation relied on secondary in-plane streaming visualized by the yeast cell circulation near the embedded microbubbles.

The piezoelectric transducer has been excited via an arbitrary function generator (AFG3011C, Tektronix). The motion of the yeast cells has been captured at 12 – 17 frames/s using an inverted microscope (IX81, Olympus). To account for the varying size of yeast cells, multiple frames of the recordings were averaged. All data required for individual qualitative evaluations of design or process parameters has been collected in single experimental sessions to ensure comparability and to prevent inter-device discrepancies such as in the distance between the transducer and the PDMS device.

Our device’s mixing capabilities have been evaluated using normalised grey-scale analysis, with a standard deviation threshold of 10% denoting sufficient mixing. Mixing has been performed using a constant excitation frequency of 69kHz. Steady volume flows of 0.3µl min⁻¹ and 0.66µl min⁻¹ for de-ionised water and black ink (4001, Pelikan) were achieved by syringe pumps (neMESYS, Cetoni).

**Biological Model**

HeLa S3 cells were cultured in RPMI 1640 (R5886, Sigma Aldrich) with 1x GlutaMAX (35050061, Invitrogen), supplemented with 10% (v/v) Foetal Calf Serum (CVFSVF0001, Eurobio Scientific), 100µg ml⁻¹ penicillin/streptomycin (30-002-CI, Corning) and MEM non-essential amino acids solution (100x) (11140050, Gibco). The cells were grown at 37°C with 5% CO₂ in a humidified incubator. Prior to their insertion into the chip, cells were detached via the addition of 0.05% Trypsin-EDTA (1x) (25300096, Gibco).
Results & Discussion

Design Optimisation and Geometric Analysis

Accurate investigations and optimisations of design parameters are essential to ensure efficient and reliable manipulation capabilities in lab-on-chip applications. Figure 1 introduces our acoustofluidic device through the side (a) as well as the top (b) view. The main component consists of a polydimethylsiloxane (PDMS) feature that contains a microfluidic channel with dimension $D = 300 \, \mu m$ as well as the embedded microbubbles. The microbubbles have a constant width of $W = 100 \, \mu m$ but varying lengths $L$ and are separated from the nearby liquid channel through thin PDMS walls with different thicknesses $T = 5 - 20 \, \mu m$. The PDMS device is excited via a piezoelectric transducer. By driving the transducer at specific frequencies, the thin PDMS wall between the microfluidic channel and the embedded microbubble can be brought to resonate in its eigenmodes, which subsequently allows for the attraction and rotation of small specimens in the nearby liquid.

To investigate the influence of the various geometrical design parameters onto the manipulation capabilities of the embedded microbubbles, features with different wall thicknesses $T = 5 - 20 \, \mu m$ and air chamber lengths $L = 500 - 1000 \, \mu m$ have been fabricated and the strength of the resulting acoustic effects has been evaluated qualitatively. For a device height $H$ of $50 \, \mu m$, a smallest wall thickness of $T = 5 \, \mu m$ was chosen, which leads to an aspect ratio $H/T = 10$. Figure 1 c) shows two embedded microbubbles aligned along a microchannel with wall thicknesses $T$ of $5 \, \mu m$ (B1) and $10 \, \mu m$ (B2). The initial analysis of our device revealed only minor changes in resonance frequencies between the different designs, a factor crucial for the subsequent in-depth experimental and numerical investigations.

Figure 1 d) shows polystyrene (PS) particles trapped near the acoustically excited microstructure. The wall thickness $T$ of the embedded microbubble is $15 \, \mu m$ and the excitation parameters are $67.1 \, kHz$ and $10 \, V_{pp}$. The $10 \, \mu m$ PS particles remained in their stable positions while slowly rotating out-of-plane. The particles in the microchannel are only trapped...
Figure 1: Device layout and microscope pictures of particle attraction and rotation. (a) Side view of a single embedded microbubble. The air trapped in a cavity is separated from the microchannel by a thin wall with thickness $T$. Four designs with different wall thicknesses $T = 5 - 20 \mu$m have been fabricated. Additionally, the air chamber length $L$ has been varied from $L = 500 - 1000 \mu$m. The height $H$ of all features is approximately $50 \mu$m. (b) Top view of a single embedded microbubble with the numerically investigated wall thickness $T$, air chamber length $L$, and channel dimension $D$. The width $W$ of the embedded microbubble was kept at $100 \mu$m. (c) Two embedded microbubbles B1 and B2 next to each other along the microchannel. B1 and B2 have a wall thickness $T$ of $5 \mu$m and $10 \mu$m, respectively. (d) Seven $10 \mu$m PS particles trapped near an embedded bubble with $T = 15 \mu$m. The particles are slowly rotating out-of-plane. Particles were only trapped close to an embedded microbubble and not by the channel walls in general. (e) Fluorescent microparticles following an out-of-plane vortex in front of an embedded microbubble. A single particle is highlighted in red as it follows the streaming for two rotations. The white dashed lines indicate the location of the thin PDMS wall and the dashed grey line indicates the centre of rotation. Scale bars: $c = 100 \mu$m, $d = 25 \mu$m, $e = 25 \mu$m.
near the embedded microbubbles while not attracted by the regular walls of the microchannel, indicating that the effect is not induced through the general PDMS-liquid interface. Furthermore, Figure 1 e) presents an image sequence of out-of-plane rotating PS particles close to an embedded microbubble with a wall thickness $T$ of 15 µm (white dashed lines in the first image). The excitation frequency and voltage are 68 kHz and $10 \text{ V}_{PP}$, respectively.

The demonstrated motion of the microparticles is further presented in Supporting Information SV-1, which highlights our feature’s capability to generate stable out-of-plane vortices reliably; a crucial task for single-cell analysis as well as the investigation of small model organisms.

Following our preliminary experimental analysis, we performed numerical investigations of the various designs to optimise the device’s performance. Figure 2 a) shows the simulated wall displacements for varying wall thicknesses $T$. As our investigations focused on the region near the embedded microbubble, the streaming velocity (Eq. 6) and the acoustic energy density (Eq. 4) have been integrated and averaged over the hatched area of 50x50 µm. The simulation results suggest that the wall thickness and wall displacement are inversely proportional with thinner walls demonstrating higher displacement amplitudes than thicker walls for the same excitation voltage. The simulations have been performed at each structure’s corresponding mode with the largest displacement, which correlates nicely to the highest acoustic energy density. The modes have been chosen based on preliminary experimental observations that suggested strong acoustic interactions for excitations around a frequency of 69 kHz. Surprisingly, the numerical investigations revealed only minor variations of the frequency (69.05±0.02 kHz) with the strongest displacement for the various wall thicknesses. The minor variations of the frequency indicate that the amplitude of the wall’s displacement is not solely dependant on the wall thickness but further significantly influenced by the geometry of the air, water, and PDMS components. This assumption was further verified by an extended frequency sweep for all wall thicknesses. Supporting Figures S-4, S-5, and S-6
Figure 2: Design optimization with numerical and experimental investigations.

(a) Numerical model of the device’s yz-plane zoomed in to highlight the embedded microbubble and water channel. The region of interest, containing the thin PDMS wall, is highlighted with a red square. The green hatched area near the PDMS wall inside the fluid channel denotes the area used for the numerical evaluation of the average acoustic energy density $E_{ac}$ as well as the average streaming velocity $v_{str}$. The wall displacement for varying wall thicknesses $T = 5 – 20 \mu m$ have been derived through numerical simulations. While thinner walls lead to stronger displacements, similar resonance frequencies of the thicker walls have been observed, indicating that the resonance of the bubble dominates. (b) Experimentally determined in-plane streaming sizes (in y-direction) for different wall thicknesses $T$ with a constant air chamber length $L = 500 \mu m$. The largest streaming pattern has been observed for a wall thickness of $T = 5 \mu m$. (c) Numerical results for the average streaming velocity $v_{str}$ at the resonance frequency for air chamber lengths $L = 250 – 1000 \mu m$ with a constant wall thickness $T = 5 \mu m$. The maximum average streaming velocity in the area close to the vibrating wall is achieved for an air chamber length of $L = 500 \mu m$. (d) Experimental results of the in-plane streaming size for different air chamber lengths $L$ and a constant wall thickness $T = 5 \mu m$. The experimental results nicely fit the findings of the numerical investigations, indicating that $L = 500 \mu m$ leads to the largest streaming vortices.
display the typical S-shaped resonances of the different geometries. It is important to note
that, despite being in resonance, the amplitudes of their vibrations decrease for increasing
excitation frequency. Since the decrease in displacement is mainly independent of the wall’s
geometry, the investigated vibrations are likely dominated by the resonances of the embedded
microbubbles.

Subsequently, we performed experimental characterisations of the strong dependence be-
tween wall thickness and wall displacement highlighted by the numerical simulations. As a
measure for comparison between the different geometries, yeast cells have been introduced
into the microchannel as tracer particles. The sizes of the resulting in-plane streaming
vortices were taken as a measure for comparison. A channel dimension $D = 300 \mu m$ has
been chosen to avoid interference between the local acoustic streaming at the embedded
microbubble and the opposing wall. As can be seen in Figure 2 b), significantly larger
streaming patterns have been achieved for embedded microbubbles with 5 $\mu m$ walls than for
designs with thicker features. It is important to highlight that all embedded microbubbles
were located on the same device and arranged next to each other along the microchannel,
as shown in Figure 1 c), to prevent possible inaccuracies in the results due to variations in
the setup. Additionally, all features have been evaluated around an excitation frequency of
66 kHz and voltage of $20 V_{PP}$ with only minor distinctions between resonance peaks being
possible through visual observations. Excitation of the device at significantly higher or lower
frequencies did lead to none or only minor acoustic streaming, indicating that the wall has a
limited activity at other frequencies as expected by our numerical analysis (see Supporting
Figure S-4, S-5, and S-6). While no clear differences in the streaming patterns have been
observed for the wall thicknesses of $T = 10 - 20 \mu m$, higher input power might be required
to allow for a clear distinction of the influence of this geometrical parameter.

Following the quantification of the wall thickness’ effect on the acoustic capabilities of
our device, we proceeded with the investigation of the influence of the air chamber length $L$. 
In numerical simulations, the air chamber length $L$ has been increased from 250 to 1000 µm with steps of 50 µm. Figure 2 c) indicates that the strongest average streaming velocity can be expected for $L = 500$ µm. At this air chamber length, the surrounding PDMS seems to compress the embedded air in a way that supports the vibrational mode of the resonating thin wall. However, further investigations are needed to evaluate the influence of the air chamber length properly. Additionally, we cannot fully exclude other factors such as large scale deformations of the PDMS device due to overall changes in the stability of the features. Subsequently, the influence of the air chamber length $L$ has been quantified experimentally (Figure 2 d) ). All microstructures have been excited using the same parameters, i.e., frequency and voltage, and the sizes of the generated in-plane vortices have been measured. While the experimentally obtained results expose a similar trend as predicted by the numerical simulations, the superiority regarding streaming size of $L = 500$ µm is less pronounced in experiments, therefore further investigations might be necessary to allow for the appropriate interpretation of these results. A non-negligible reason for the variation observed between the numerically determined results and the experimental quantifications might also be based on differences in the evaluated quantity. While the numerical simulations allow for a direct investigation of the streaming velocity of the produced out-of-plane streaming near the embedded microbubble, due to limited accessibility to this streaming during experimental evaluations, the latter has to rely on the generated in-plane vortices. Therefore, the comparison of the results obtained through the different techniques, i.e., numerical and experimental evaluations, might be restricted by the complex and possibly non-linear relationship between the out-of-plane and the in-plane streaming vortices.

**Investigation of Acoustofluidic Capabilities**

Based on the results presented in the device optimisation, we opted for a design with wall thickness $T = 5$ µm and air chamber length $L = 500$ µm and performed more specific numerical analyses to gain further insights regarding the underlying mechanisms and the acoustic
phenomena. Figure 3 a) shows the average wall displacement and the average acoustic energy density for frequencies from 40 to 90 kHz with 100 Hz steps. The maximal energy density correlates with the highest displacement of the wall and reveals two strong resonances (41.89 kHz and 69.03 kHz). Experimental investigations showed that frequencies around 69 kHz lead to much stronger particle attraction and streaming velocities than frequencies around 40 kHz. The deviation from observed and simulated resonance frequency can be attributed to idealised material parameters and the limited significance of the displacement boundary condition, e.g., through lower amplitudes of the piezoelectric element at this frequency range. However, the aim of the numerical investigations is not to attain exact amplitudes but to show trends and get insight into the physical phenomena of the device.

At the resonance frequency of 69.03 kHz, a strong fluid vortex is generated close to the thin wall that drives the fluid in a counter-clockwise fashion, which is ranging up to 50 µm into the channel (see Figure 3 b) ) and could be utilised for controlled particle rotation. However, the particle needs to be positioned close to the thin wall to be influenced by the streaming vortex, which can be achieved by the acoustic radiation force. For particle attraction towards the thin wall, the Gor’kov potential minimum needs to be close to the embedded microbubble (see Equation 1). As can be seen in Figure 3 c), at the resonance frequency of 69.03 kHz a Gor’kov potential minimum is generated at half of the height of the thin wall; thus, particles are attracted to the displacement node of the thin PDMS wall. It is important to highlight, that the generated node is not based on a standing wave formation inside the channel and, thereby, does not rely on the geometrical dimensions of the PDMS as a whole.\textsuperscript{28}

Figure 3 d) shows the experimentally evaluated relation between the out-of-plane rotational speed of a specimen and the applied excitation voltage. The embedded microbubble has been excited at a constant frequency of 69.2 kHz, which is in great accordance with the numerically detected maximal wall displacements around that frequency. The rotational
Figure 3: **Detailed investigation of a device with wall thickness $T = 5 \, \mu m$ and embedded microbubble length $L = 500 \, \mu m$.** (a) Frequency sweep from 40 to 90 kHz with steps of 0.1 kHz. The displacement of the thin PDMS wall and the average acoustic energy density $E_{ac}$ show prominent resonances at 41.89 kHz and 69.03 kHz. (b) Streaming velocity field near the thin PDMS wall. The velocity of the acoustic streaming is strongest close to the wall and drives the fluid in a counter-clockwise fashion. (c) Gor’kov potential as well as the acoustic radiation force (white arrows). The minimum of the Gor’kov potential can be found at half the height of the thin wall. Therefore, the acoustic radiation force is pointing towards this position, which, in experiments, leads to a particle attraction from the channel towards the embedded microbubble. Both (b) and (c) were simulated with an excitation frequency of 69.03 kHz, which is corresponding to the strongest resonance. (d) The experimentally determined relationship between the excitation voltage and the out-of-plane rotational speed of a specimen (rotation around x-axis). While the excitation frequency is kept constant at 69.2 kHz, an increase of the input power leads to stronger streaming velocities (Eq. 6) and subsequently to faster rotations of the specimen. The dashed line denotes a fitted quadratic curve with a coefficient of determination $R^2 = 0.98$.

speed follows the input voltage in a quadratic dependency ($R^2 = 0.98$), demonstrating our approach’s high controllability of the specimens orientation which is crucial for biomedical applications such as single-cell analysis. It is important to note that the increasing error at high voltages might be induced through uncertainties based on frame rate limitations of the experimental setup. However, additional sources, including possible cell membrane instabilities or the motion of intracellular features during fast rotational manipulations, can
Figure 4: **Microfluidic applications for embedded microbubbles.** (a) The controlled out-of-plane rotation of a single HeLa cell. The microstructure is excited at a constant frequency and voltage of 69.2 kHz and 5 V<sub>PP</sub>, respectively. The white arrow denotes the direction of the specimen’s rotation while the red arrow highlights a spot on the specimen’s surface. (b) Microfluidic mixing of two liquids in a 150 µm wide microchannel based on acoustically activated embedded microbubbles. The top image shows the laminar flow of the liquid where mixing is limited to diffusion. The red dots show the positions along the microchannel used for the evaluation of the efficiency. The yellow rectangle indicates the area used for the calculation of the mixing index at position 2. The bottom image demonstrates the mixing procedure for an excitation voltage of 20 V<sub>PP</sub> and a flow velocity of $v_{avg} = 2.13$ mm s<sup>-1</sup>. (c) Experimental evaluation of the mixing index for different input voltages. The mixing index corresponds to the standard deviation of the normalised grey-scale image at the corresponding positions of the microchannel. The horizontal line at 10 % denotes sufficient mixing. Scale bars: (a) = 10 µm, (b) = 150 µm.

**Single-Cell Manipulation and Microfluidic Mixing**

We expand the investigation of our device by demonstrating its application for two diverse applications, *i.e.*, single-cell manipulation as well as microfluidic mixing. HeLa cells are a prominent model organism for biomedical as well as genetic research<sup>29,30</sup> and their controlled
manipulation exposes great potential to allow for further insights on a single cell level.

The image sequence in Figure 4 a) presents the slow and stable out-of-plane rotation of a single HeLa cell near an embedded microbubble with a wall thickness $T = 5 \mu m$, while the piezoelectric transducer is excited with a constant frequency of 69.2 kHz and voltage of $5 V_{PP}$. The HeLa cell’s motion is further presented in Supporting Information SV-2. Please note that, in contrast to many solid microstructures used for acoustic manipulation, the demonstrated rotational motion has been achieved at a low excitation voltage of $6 V_{PP}$, thereby preventing possible damage to the sample due to high power pressure fields. The successful manipulation of the HeLa cell is based on the combination of the acoustic radiation force and acoustic streaming. As demonstrated through the numerical simulations, the Gor’kov potential (see Figure 3 c) leads to a force which pushes biological specimens towards the embedded microbubble. Once trapped, the single cell is rotated via the viscosity-related acoustic streaming, which allows for the visual investigation of the specimens intracellular components as well as individual features of the cell membrane. Please note that the wall thickness appears larger in the image sequence due to the plane of focus being set on the specimen.

Due to the flow limitations at the low Reynolds regime, reliable mixing is essential for a variety of lab-on-chip applications in chemical as well as biomedical analysis. Our acoustic-based mixer consists of a series of alternating embedded microbubbles with wall thickness $T = 5 \mu m$ arranged along a single microchannel. The channel dimension $D$ has been set to $150 \mu m$ based on numerical investigations to ensure strong and local streaming near the microstructures. Two liquids, i.e., de-ionised water and blue ink, are introduced through separated channels while their volume flow is controlled via a high-precision microfluidic pumping system to achieve an average flow velocity $v_{avg}$. The inlet channels meet at an angle of $90^\circ$ to minimise diffusion-based mixing while avoiding possible acoustic streaming near sharp-edge features.
Figure 4 b) shows the PDMS device with the two laminar flows prior to acoustic excitation, \textit{i.e.}, the piezoelectric transducer is off, as well as during mixing of two fluids using an input voltage of 20 V\textsubscript{PP} (see Supporting Information SV-3). The average flow velocity inside the microchannel is $v_{\text{avg}} = 2.13 \text{ mm s}^{-1}$, which, despite requiring significantly lower input power and not relying on surface treatments, is comparable to results presented for solid-structure-based acoustic mixers.\textsuperscript{27,37,38} Additionally, as our design allows to prevent geometrical constrictions, unintended trapping of microbubbles inside the mixing channel can be avoided. While bubble-based acoustic mixers allow for increased handling of fluid volumes, our approach circumvents their limitations in temporal stability and re-usability.\textsuperscript{14,39,40}

The graph in Figure 4 c) demonstrates the experimentally determined relationship between the applied input power and the acoustic manipulation capabilities of our device. To allow for the evaluation of device performance, we calculated the mixing indices at different positions of the microchannel, starting with position 1 in front of the mixer (see red labels in Figure 4 b)). For each position, a mixing index has been derived as the standard deviation of the normalised grey-scale image (area highlighted with yellow lines). A threshold of 10\% has been defined as sufficient mixing based on previous literature.\textsuperscript{27} The graph demonstrates that, for our design with 20 alternating embedded microbubbles and for average flow velocities $v_{\text{avg}} = 2.13 \text{ mm s}^{-1}$, successful mixing can be achieved for excitation voltages as low as 16 V\textsubscript{PP} (blue squares) while, for 20 V\textsubscript{PP} (orange triangle), the threshold is already reached after 8 features.

To allow for direct comparison between various designs and techniques applied in microfluidic mixing, the average mixing time can be derived as

$$\tau_S = L_{\text{mix}} / v_{\text{avg}} \approx 376 \text{ ms}$$ \hfill (7)

where $L_{\text{mix}} = 800 \mu\text{m}$ is the mixing distance required to achieve sufficient mixing for an excitation voltage of 20 V\textsubscript{PP}. However, it is important to note that the device’s efficiency
might be further improved through design optimisations, such as by arranging the embedded bubbles in an opposite instead of an alternating manner. Additionally, as active streaming has only been observed directly in front of the embedded microbubbles, the distance between the features could be reduced without leading to unintended and possibly unfavorable interactions between the generated vortices. Furthermore, through the simple application of an external amplifier, the strength of the acoustic streaming could be further increased, which would allow to reduce the derived mixing distance.

**Conclusion & Outlook**

In this work, we introduced a novel acoustofluidic device combining the advantages of solid and bubble-based features and demonstrated its use for particle and single-cell manipulation as well as microfluidic applications. We numerically investigated different geometrical design parameters and derived their complex relationship to the acoustically generated streaming pattern. Then, following noticeable fabrication improvements, we successfully confirmed our observations through experimental characterisations. Optimum device performance with regards to its out-of-plane rotation capabilities has been numerically determined for a microbubble length of 500 µm, wall width of 5 µm, and fluid channel width of 150 µm.

We explored the applicability of our device for biomedical research through the controlled out-of-plane rotation of single HeLa cells and quantified the near quadratic dependency between the applied voltage and the specimen’s rotational speed, which allows for the high controllability necessary to achieve slow yet stable motions crucial for future biological investigations, *e.g.*, through fluorescence imaging. Finally, we illustrated our lab-on-chip sub-second mixing performance and discussed potential design improvements for increased efficiency. Nevertheless, it is worth highlighting that the current achievements are comparable to previous publications while relying on significantly lower input power and maintaining the microbubble’s temporal stability.
Future work may include mixing-based gradient generation important for various chemical applications and the extension of our approach for manipulating multi-cellular organisms, such as Caenorhabditis elegans.

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Supporting Information Available

Supplementary Material Available: Details on the the numerical model and its mesh study, the fabrication procedure and optimisation, and videos on the manipulation capabilities.

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Graphical TOC Entry
Supporting Information for "Embedded Microbubbles for Acoustic Manipulation of Single Cells and Microfluidic Applications"

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Supporting Figures

Figure S-1: Mesh study of the numerical simulation.
We introduced three mesh parameters reflecting different aspects of the mesh. On the top left, we show the numerical model and two magnifications that show the channels and the upper part of the thin wall in between the two channels with mesh, respectively. (a) Maximal triangular element size throughout the whole model given as size per wavelength ($\lambda/n$). (b) Width of the elements in the mesh refinement layer as multiples of the viscous boundary layer thickness ($\delta/n$). (c) The number of rows within the mesh refinement layer. The width of the mesh refinement layer ($x$) was found to be of negligible importance and thus set to the viscous boundary layer thickness $x = \delta$. With $E_{ac}$ as the average energy density in the water channel, wall disp as the average wall displacement of the thin PDMS wall, streaming the average streaming velocity, and DOF the number of degrees of freedom. We chose the following mesh parameters for all simulations in this work, corresponding to an error below 1% with respect to the finest mesh: maximum triang. element size = $\lambda/500 = 5\mu m$ (air), 11\mu m (water), 162\mu m (glass); element width of mesh refinement layer = $\delta/2.5 = 0.86\mu m$; number of rows in the mesh refinement layer =15.
Figure S-2: **Fabrication process for embedded microbubbles.**

(a) The design of the embedded microbubble is transferred onto a silicon wafer using photolithography. (b) An optimized DRIE etching process is applied to etch the designed into the silicon wafer and produce a mold containing narrow trenches at the locations of the required thin PDMS walls. (c) The wafer is vapour-coated with silane to ensure successful device replication in PDMS casting. The PDMS structures as peeled off the silicon mold and chemically bonded to glass slides using oxygen plasma.
Figure S-3: Aspect ratio dependent etching (ARDE) lag improvement.
(a) ARDE lag as typically observed for silicon processing. Wide microstructures expose a higher etching rate which subsequently leads to deeper trenches than for narrow channels. (b) The red squares denote the relative etch depths, i.e., the features etch depth in relation to depths achieved in non-constricted areas, for a standard Bosch process. According to this graph, if open spaces of a wafer are etched to a depth of 50 µm, the depth of 5 µm thin trenches will only reach approximately 40 µm, resulting in insufficient bonding for embedded microbubbles with thin walls. The blue triangles present the resulting relative etch depths for a process with significantly reduced ARDE lag. The feature depths have been evaluated using white light interferometry.
Figure S-4: **Extended frequency study of a device with wall thickness $T = 10 \mu m$ and embedded microbubble length $L = 500 \mu m$.**

(a) Frequency sweep from 65 to 160 kHz with steps of 0.1 kHz. The displacement of the thin PDMS wall and the average acoustic energy density $E_{ac}$ show resonances at frequencies above 69.04 kHz depicted in Figure 2. (b) Displacement of the wall at selected resonance frequencies. To achieve the same mode shape of the wall as for a wall thickness of $T = 5 \mu m$ (see Figure 2), one has to excite the wall with $T = 10 \mu m$ at 123.6 kHz. Slightly lower and higher frequencies lead to a different mode shape.
Figure S-5: **Extended frequency study of a device with wall thickness** $T = 15 \, \mu\text{m}$ **and embedded microbubble length** $L = 500 \, \mu\text{m}$.

(a) Frequency sweep from 110 to 210 kHz with steps of 0.1 kHz. The displacement of the thin PDMS wall and the average acoustic energy density $E_{ac}$ show resonances at frequencies above 69.05 kHz depicted in Figure 2. (b) Displacement of the wall at selected resonance frequencies. To achieve the same mode shape of the wall as for a wall thickness of $T = 5 \, \mu\text{m}$ (see Figure 2), one has to excite the wall with $T = 15 \, \mu\text{m}$ at 178.3 kHz. Slightly lower and higher frequencies lead to a different mode shape.
Figure S-6: **Extended frequency study of a device with wall thickness** $T = 15 \, \mu m$ **and embedded microbubble length** $L = 500 \, \mu m$.

(a) Frequency sweep from 200 to 260 kHz with steps of 0.1 kHz. The displacement of the thin PDMS wall and the average acoustic energy density $E_{ac}$ show resonances at frequencies above $69.07 \, kHz$ depicted in Figure 2. (b) Displacement of the wall at selected resonance frequencies. To achieve the same mode shape of the wall as for a wall thickness of $T = 5 \, \mu m$ (see Figure 2), one has to excite the wall with $T = 20 \, \mu m$ at $233.1 \, kHz$. Slightly lower and higher frequencies lead to a different mode shape.
Supporting Information

Supporting Information SI-1: Numerical Model

We used the Solid Mechanics interface to model the solid components of the model (glass, PDMS). To account for damping, we chose to model the glass as a linear elastic material with complex Lamé parameters. The PDMS was modeled as a linear elastic material with poisson’s ratio and complex Young’s modulus to account for damping in our system. Please refer to table 1 for all material parameters.

Table 1: Table of the material properties and damping factors.\textsuperscript{1,2}

| Parameter                  | Symbol and value                        | Unit       |
|----------------------------|-----------------------------------------|------------|
| Glass density              | $\rho_{gl} = 2240$                      | [kg/m$^3$] |
| Lamé parameters            | $\lambda = 23.1 \cdot 10^3 \cdot (1 + i/2420)$ | [MPa]      |
|                           | $\mu = 24.1 \cdot 10^3 \cdot (1 + i/2420)$ | [MPa]      |
| PDMS density               | $\rho_{PDMS} = 970$                     | [kg/m$^3$] |
| Poisson ratio              | $\nu = 0.49$                            |            |
| quality factor             | $Q_{PDMS} = 1000$                       |            |
| complex Young’s modulus    | $E_{PDMS} = 0.75 \cdot (1 + i/Q_{PDMS})$ | [MPa]      |

The mechanical vibrations were implemented in the model by means of a prescribed displacement boundary condition within the solid mechanics interface. The displacement was applied over the whole length of the bottom of the glass plate and its amplitude was set to 10 nm.

The Thermoviscous Acoustics interface was applied to both channels within the PDMS. The materials inside both channels were modeled with the standard material parameters provided by the software.

The Thermoviscous Acoustic-Structure Boundary interface was implemented to couple the Solid Mechanics interface and the Thermoviscous Acoustics interface at the Water-PDMS and the Air-PDMS interfaces.

To incorporate acoustic streaming in our simulations we followed the procedure described in.\textsuperscript{3,4} We assigned the Creeping Flow interface to the water domain. Volume Forces were set...
on the whole domain. Finally, a Pressure Point Constraint was set to an arbitrary point of the domain boundary \( (p_0 = 0[Pa]) \).

**Supporting Information SI-2: ARDE lag reduction**

Aspect ratio dependent etching (ARDE) lag has been reduced through iterative parameter optimisations. Figure S-3a) shows ARDE lag as typically observed in deep reactive ion etching, where wider trenches are etched deeper than narrow structures. This observation is further represented by the red squares in Figure S-3b) denoting the etch depth for trenches with varying widths \( T \) in relation to the depth \( D \) achieved in unconfined areas of the processed wafer. Following an approach introduced by Lai et al.,\(^5\) we adjusted the durations of the two process steps, \( i.e. \), of \( t_D \) for the deposition or passivation and \( t_E \) for the etching, to allow for equal etch rates between trenches with varying widths and, subsequently, the reduction of ARDE lag (see blue triangles in Figure S-3b) ). It is important to highlight that the derived durations are closely related to the aspect ratio dependency of the individual steps, with the polymer deposition and silicon etching being mostly chemically induced while the initial polymer etching at the bottom of the trench relies on physical processes.
Supporting Videos

Supporting Information SV-1: Stable out-of-plane motion of 10 µm polystyrene particles. The particles are trapped via radiation forces in front of an embedded microbubble with a wall thickness \( T = 10 \mu m \) and follow the developed out-of-plane streaming. The excitation frequency and voltage are 68 kHz and 10 V\(_{PP}\), respectively. Scale bar = 50 µm.

Supporting Information SV-2: Stable out-of-plane rotation of a single HeLa cells. The single cell is trapped in the pressure node near an embedded microbubble with a 5 µm thin wall and slowly rotated using the generated out-of-plane vortices. The embedded microbubble is excited at frequency of 67 kHz with 6 V\(_{PP}\). The video offers an additional view onto the manipulated specimen with focus on the PDMS wall. Scale bar = 25 µm.

Supporting Information SV-3: Mixing capabilities of the acoustic device. Black dye and de-ionised water are mixed using a series of embedded microbubbles. The microstructures are excited at a frequency of 69 kHz. The videos demonstrate the mixing for excitation voltages of 14 V\(_{PP}\) and 20 V\(_{PP}\), respectively. For demonstration purposes, the acoustic activation is switched on and off. Scale bar = 500 µm.

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