Homeostasis: Design and Implementation of a Self-Stabilizing Compiler

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Mainstream compilers perform a multitude of analyses and optimizations on the given input program. Each analysis (such as points-to analysis) may generate a program-abstraction (such as points-to graph). Each optimization is typically composed of multiple alternating phases of inspection of such program-abstractions and transformations of the program. Upon transformation of a program, the program-abstractions generated by various analyses may become inconsistent with the modified program. Consequently, the correctness of the downstream inspection (and consequent transformation) phases cannot be ensured until the relevant program-abstractions are stabilized; that is, the program-abstractions are either invalidated or made consistent with the modified program. In general, the existing compiler frameworks do not perform automated stabilization of the program-abstractions and instead leave it to the compiler pass writers to deal with the complex task of identifying the relevant program-abstractions to be stabilized, the points where the stabilization is to be performed, and the exact procedure of stabilization. In this article, we address these challenges by providing the design and implementation of a novel compiler-design framework called \textit{Homeostasis}.

\textit{Homeostasis} automatically captures all the program changes performed by each transformation phase, and later, triggers the required stabilization using the captured information, if needed. We also provide a formal description of \textit{Homeostasis} and a correctness proof thereof. To assess the feasibility of using \textit{Homeostasis} in compilers of parallel programs, we have implemented our proposed idea in IMOP, a compiler framework for OpenMP C programs. Furthermore, to illustrate the benefits of using \textit{Homeostasis}, we have implemented a set of standard data-flow passes, and a set of involved optimizations that are used to remove redundant barriers in OpenMP C programs. Implementations of none of these optimizations in IMOP required any additional lines of code for stabilization of the program-abstractions. We present an evaluation in the context of these optimizations and analyses, which demonstrates that \textit{Homeostasis} is efficient and easy to use.

CCS Concepts: • Software and its engineering → Compilers; Frameworks; Development frameworks and environments; Design patterns; Incremental compilers;

Additional Key Words and Phrases: Compiler design, multi-pass compilation, self-stabilization

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1 INTRODUCTION

Modern compilers often span millions of lines of code, and perform a multitude of analyses and optimizations on the given input program. Each analysis (such as points-to analysis, call-graph construction, and so on) derives some meaningful information about the program, in the form of a program-abstraction (such as points-to graph, call-graph, and so on). An optimization typically involves multiple alternating phases of inspections of such program-abstractions, and transformations of the program. In the inspection phase, the optimization invokes the required analyses, if needed, and inspects various program-abstractions to discover opportunities of optimization in the program. In the transformation phase, the optimization pass may use the results of the inspection phase to modify the program. Consequently, the transformation phase may render various existing program-abstractions inconsistent with the modified program. As a result, the existing program-abstractions must be stabilized before their next use; that is, the program-abstractions must be regenerated or updated such that they correspond to the modified program. Otherwise, the correctness of the future inspection phases of the current or downstream optimizations cannot be ensured. This, in turn, can negatively impact the optimality and even the correctness of the overall compilation. We illustrate these problems using an example.

Example 1.1. In Figure 1(a), we show the pseudocode of a standard compiler optimization that utilizes points-to information to remove dead branches from a program. For simplicity, we assume that the predicates do not contain any side-effects, and that there are no arbitrary goto-statements in the input program. The isNeverZero method returns true when it can be statically determined that the given expression can never evaluate to zero; similarly, the isAlwaysZero method returns true only when the expression would always evaluate to zero. Further, assume that both these methods use the points-to information to statically evaluate the given expression. Hence, in the inspection phase, the optimization pass invokes a flow-sensitive points-to analysis pass to obtain the required points-to map (a program-abstraction), if not already available. Furthermore, in this phase, the optimization utilizes the methods isNeverZero and isAlwaysZero to determine whether an if-statement can be replaced with either of its branches. Accordingly, the transformation phase may be triggered to perform the replacement using the replace method (Lines 7 and 9). Note that these transformation and inspection phases may alternate in the presence of multiple if-statements in the program.

This simple and intuitive code of dead-branch remover may not work as expected: Consider a sample input program $P_1$ shown in Figure 1(b), and a part of its points-to map in Figure 1(c). Say the optimization processes the if-statement at label L1 first, and relying on the points-to map at the predicate, replaces the if-statement with its else-branch (i.e., an empty body), transforming program $P_1$ to $P_2$ (Figure 1(d)). This transformation renders the points-to map stale: at the predicate ($p == \&a$), the pointer $p$ continues to point to {$a$, b}, instead of {$a$}, the more precise points-to set. In the absence of stabilization of the points-to map, the optimizer pass in its next iteration cannot determine that the predicate at L2 will never be zero. As a result, the optimizer will not generate the optimal program $P_3$; instead, $P_2$ will be the final output of the optimizer. Note that such issues of sub-optimality (and even correctness) may also be observed in the downstream optimization passes, until the points-to map is stabilized.

To perform the correct stabilization manually and efficiently, we need to identify all the places in the dead-branch remover where the points-to map may require stabilization. Furthermore, we also need to be concerned about the stabilization of all the other program-abstractions as well: (i) We need to identify the program-abstractions (for example, use-def information [Muchnick 1998]) that may become stale because of the current optimization, and may be required by other downstream optimizations and analyses. (ii) For each of these
Fig. 1. An example optimizer pass, and a program-abstraction. After removing the if-statement at L1 from the input program $P_1$ to obtain $P_2$, the optimizer will not be able to remove the else-branch of L2, thereby not producing the expected optimal code $P_3$: In the absence of stabilization, the points-to map from Figure 1(c) does not get updated after removal of the statement at L1. Consequently, with the stale points-to information, the optimizer cannot infer that pointer $p$ may point only to $a$ at the predicate at L2 in $P_2$.

Upon adding a new optimization $O_n$

| Q1 | Which existing program-abstractions need to be stabilized by $O_n$? |
| Q2 | Where to invoke the stabilization code in $O_n$, for the existing program-abstractions? |
| Q3 | How to stabilize each of the existing program-abstractions, in $O_n$? |

Upon adding a new program analysis $A_n$

| Q1 | Which existing optimizations need to stabilize the program-abstraction of $A_n$? |
| Q2 | Where to invoke the stabilization code for $A_n$, in each of the existing optimizations? |
| Q3 | How to stabilize the program-abstraction of $A_n$, in each of the existing optimizations? |

Fig. 2. Key stabilization-related question to be addressed while adding new compiler passes.

program-abstractions, we need to identify the places in the dead-branch remover where the program-abstraction needs to be stabilized. In practice, in the presence of multiple optimizations and analyses (hereafter, collectively referred to as compiler passes), this problem compounds as we need to be concerned about stabilization of all the program-abstractions in all the optimizations.

In summary, we observe that to avoid the generation of such sub-optimal and/or incorrect programs upon compilation, three key stabilization-related questions shown in Figure 2 need to be addressed while adding/modifying an optimization or analysis. In conventional compilers, such as LLVM [Lattner and Adve 2004], GCC [Stallman and GCC-Developer-Community 2009], Soot [Vallée-Rai et al. 2010], Rose [Quinlan et al. 2013], JIT compilers (OpenJ9 [IBM 2017], HotSpot [Oracle 1999], V8 [Google 2001]), and so on, the onus of addressing these key questions lies mostly on the compiler pass writers. Some such instances are shown in Figure 3. This manual process often leads to complex and error-prone codes. Further, as the number and complexity of compiler passes increase (for example, LLVM has more than 347 passes), addressing these questions precisely and efficiently becomes progressively more difficult. This may lead to correctness/efficiency bugs (see bug-fixing commits on GitHub [LLVM-Developer-Community 2019a, b, c, 2020a, b, c, d, e, f, g, h, i, 2021a, b, c]). With the compiler development effort spanning multiple decades involving (sometimes) hundreds of developers, it becomes extremely challenging to manually solve these problems, as no developer of a compiler pass might possess a clear understanding of the semantics of all the hundreds of other passes already present in the compiler.
To mitigate these issues, the focus of this article is to perform automatic stabilization of all the relevant program-abstractions, when needed, in response to any program modification. We term a compiler that provides this guarantee as a self-stabilizing compiler.

There have been various attempts [Blume et al. 1995; Brewster and Abdelrahman 2001; Carle and Pollock 1989; Carroll and Polychronopoulos 2003; Nilsson-Nyman et al. 2009; Reps et al. 1983] towards enabling automated stabilization of specific program-abstractions, in response to program transformations in serial programs. However, these works suffer from different drawbacks. For example, Carle and Pollock [1989], Nilsson-Nyman et al. [2009], and Reps et al. [1983] require that program-abstractions have to be expressed as context-dependent attributes of the language constructs; this is too restrictive. Similarly, besides the non-object-oriented nature of the approach of Carroll and Polychronopoulos [2003], it is unclear how their restrictive techniques can (i) be applied to compilers that use non-hierarchical IRs, which is a common practice in modern compilers (such as LLVM, Soot, OpenJ9, IMOP [Nougrahiya and Nandivada 2019], and so on), (ii) be used for data-flow analyses that are not based on structural analysis [Muchnick 1998], and (iii) automate the resolution of pass dependencies, or handle manually-defined dependencies. Blume et al. [1995] and Brewster and Abdelrahman [2001] handle only a small set of specific program-abstractions (such as symbol and scope information); this is insufficient. To the best of our knowledge, there are no compiler designs or implementations\(^1\) that address the challenges discussed above for any arbitrary IR, optimization and analysis.

**Proposed solution.** In this article, we propose a novel and efficient compiler-design framework called Homeostasis that addresses the above discussed issues related to stabilization, in the context of object-oriented compilers. Homeostasis efficiently captures a summary of all the program changes performed by each transformation phase. Later, if/when an attempt is made to read the possibly stale program-abstraction of a program analysis, Homeostasis triggers the required

\(^1\)Our observation is based on our manual inspection of more than 50 mainstream and experimental compilers [Nougrahiya and Nandivada 2023].
stabilization using the captured information, before returning the correct value of the program-abstract. With Homeostasis, no additional coding effort is required by the optimization writers to guarantee self-stabilization of the existing (or future) program-abstractations. For example, in an implementation of the dead-branch remover (Figure 1(a)) in a Homeostasis-enabled compiler, Homeostasis would ensure self-stabilization of the points-to map, without requiring any additional code in the optimization; this will lead to generation of the expected optimal program P3.

In Homeostasis, for ensuring self-stabilization, analysis writers need to spend minimal effort to only conform to the design of Homeostasis, while being oblivious to all the (existing/future) optimizations. As part of this conformance, if the analysis writer decides to use an incremental update algorithm for stabilization (instead of full recomputation), the writer has to clearly demarcate the code to incrementally update the program-abstract. Note that such a code is needed even when the stabilization is performed manually; hence this is not an additional overhead. In essence, while working with a Homeostasis-enabled compiler, a compiler pass writer need not manually address any of the key questions listed in Figure 2, and hence incurs no additional overhead.

For the ease of exposition, we have discussed Homeostasis using IMOP [Nougrahya and Nandivada 2019] a Java-based compiler in the context of a C-like language. We believe that the underlying principles of the Homeostasis are quite generic in nature, and that they can be extended to any object-oriented compilers for any serial/parallel languages.

Note that the goal of this article is not to propose any new incremental analysis technique (or any new analysis technique or optimization for that matter). The key goal of this article is to present a scheme which ensures that correct values of various program-abstractations are obtained efficiently by all the compiler passes, without needing any additional manual effort in these passes.

Contributions:

— We present Homeostasis, a generalized compiler-design framework for self-stabilization, which can be added to any object-oriented compiler infrastructure to ensure that all program-abstractations are automatically kept consistent with the modified program during the compilation process. The underlying concepts of Homeostasis can be used in any object-oriented compiler for serial/parallel languages to realize self-stabilization.

— To overcome the possible overheads resulting from the naive tracking of the program changes, we present a novel compression algorithm that reduces the memory requirements significantly.

— We give a formal description of Homeostasis and a correctness proof thereof, which guarantees that in a Homeostasis-enabled compiler, any compiler pass attempting to access the program-abstractation of an analysis will see only the stable value of that program-abstractation.

— We have implemented all the key components of Homeostasis in IMOP, a source-to-source Java-based compiler infrastructure for OpenMP C programs, as a successful proof-of-concept. Further, to demonstrate the benefits of using Homeostasis, we have implemented (i) HIDFA, a generic, self-stable, inter-thread, flow-sensitive, context-insensitive iterative data-flow analysis (IDFA) and six instantiations thereof, (ii) a set of optimization passes, collectively termed as BarrElim, that removes redundant barriers from OpenMP C programs; BarrElim uses a set of nine optimization passes, each of which may involve multiple alternating phases of inspection and transformation. As expected, the implementation of the set of BarrElim optimization passes required zero additional lines of code for stabilization, and the stabilization of the analyses required minimal effort.

— We present an evaluation over a set of twenty-four benchmarks from four benchmark suites NPB [Van der Wijngaart and Wong 2002], SPEC OMP [Aslot et al. 2001], Sequoia [Seager 2008] and IMSuite [Gupta and Nandivada 2015], performed over two different platforms.

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We show that *Homeostasis* makes it easy to write optimization and analysis passes, and it leads to faster compilation times compared with the possible alternative of typical manual stabilization performed by experts. We also show that our proposed optimizations lead to significant memory savings.

The rest of the manuscript is organized as follows: We give a brief background of the relevant concepts used in the manuscript in Section 2. We present our design of *Homeostasis* in Section 3. We give a formal description of *Homeostasis*, along with a correctness argument in Section 4. We discuss some salient features of *Homeostasis* in Section 5. In Section 6, we discuss an instantiation of *Homeostasis* in a real-world compiler. In Section 7, we briefly describe our implementation and present a detailed evaluation of *Homeostasis*. In Section 8, we discuss some of the relevant prior work, before concluding in Section 9.

## 2 BACKGROUND AND TERMINOLOGY

We now give a brief description of certain relevant concepts and terminologies used in this article.

**Representation of program IR.** Without loss of generality, in this article, we assume each program’s intermediate representation (IR) is represented as a graph. For instance, when the control flow graph (CFG) is the IR, nodes in the graph represent the basic-blocks, and the edges model the flow of control. Similarly, if three-address code (TAC) is the IR, then the TAC instructions are the nodes, and the edges may be of many types, such as control-flow edges, SSA edges [Muchnick 1998], and so on.

**Analysis, Analysis-instances, and Program-abstractions.** In the context of compilers written in an object-oriented language, we assume that each analysis (for example, Andersen’s points-to analysis [Andersen 1994]) is implemented as a class. During compilation, one or more of these classes are instantiated to provide analysis-instances. Each such analysis-instance, say $A_i$, can be seen as a function from the set of programs to a set of program-abstractions. A program-abstraction may refer to any data-structure that denotes some meaningful information generated by an analysis-pass, about the input program at compile time. In this manuscript, we use $A_i(P)$ to denote the program-abstraction generated by running the underlying analysis of $A_i$ on a program $P$. For example, Figure 1(c) shows a part of the points-to map, the program-abstraction of the corresponding points-to analysis.

**Stable program-abstraction.** At any point during compilation, if the current program IR is $P$, and the stored program-abstraction for an analysis-instance $A_i$ is $v$, then we term $v$ as the stable program-abstraction of $A_i$, iff $A_i(P) = v$.

**Elementary transformations.** Based on the grammar of the language under consideration, corresponding to each type of program node with a body (such as a block in LLVM IR, or a while-statement construct), we identify a fixed set of primitive transformations which can add/delete/modify the logical components of the program node (such as an instruction of a block, or the predicate of a while-statement); we term such transformations as elementary transformations.

## 3 HOMEOSTASIS: DESIGNING SELF-STABILIZING COMPILERS

Considering the stabilization challenges inherent in the design of conventional compilers, we now present a novel solution in the form of a new object-oriented compiler-design framework named *Homeostasis* (in Sections 3.1–3.3). In order to access/maintain stable program-abstractions in a *Homeostasis*-enabled compiler, while the analysis pass writers have to spend minimal effort, the optimization pass writers need not spend any effort (elaborated in Section 3.4). We formalize the design of *Homeostasis* and present a correctness argument in Section 4.
3.1 Overview of Homeostasis

Homeostasis realizes self-stabilization by tracking the program modifications resulting from different transformations. These program modifications are then used by Homeostasis to perform the stabilization of relevant program-abstractions if/when required.

3.1.1 Design Pattern Employed by Homeostasis. To track program modifications resulting from different transformations, Homeostasis uses an extension of the popular Observer pattern [Gamma et al. 1995]. The Observer pattern defines a one-to-many dependency between multiple entities, where an update in one entity (termed subject), is notified to all the other registered entities (termed observers). Figure 4 shows a class diagram (in Object Modeling Technique, or OMT, notation [Rumbaugh et al. 1991]) which gives an overview of the key design elements of Homeostasis: (i) Node class and its subtypes (such as WhileStmt) correspond to the subject(s), (ii) all the program analyses (such as CallGraphGenerator) along with their base class (BasePA) correspond to the observers, and (iii) program modifications (such as WhileStmt::elemTransformReplaceBody) correspond to the various updates to the subject(s). The use of the Observer pattern ensures that these updates (program modifications) are correctly notified to all the observers (program analysis passes).

Homeostasis goes beyond the standard design of the Observer pattern in two key ways. First, instead of triggering updates of the values (i.e., program-abstractions) maintained by various program analyses immediately upon a program modification, Homeostasis simply marks the program-abstractions as stale (or UNSTABLE). The actual update of each program-abstraction is performed lazily, by deferring the update to a later stage where an attempt is made to read from the program-abstraction, using its getters (such as CallGraphGenerator::getCallGraph). Second, instead of storing a copy of the program changes corresponding to such pending updates individually with each program analysis (each of which may need to handle a different list of pending updates), Homeostasis maintains a central copy of these program changes in an efficient data-structure (discussed in Section 3.3).

3.1.2 Nodes of Intermediate Representation (IR). In Figure 4, the Node class represents the super class of all the types of nodes in the program’s IR. Each such class may define a fixed set of elementary transformation methods that may be invoked to add/modify/delete any of the logical
component(s) of the node. For example, in Figure 4, elemTransformReplaceBody is an elementary transformation method defined on the node WhileStmt; this transformation replaces a component (the loop body) of the associated while-statement with the given argument. Homeostasis requires that (i) all program modifications are performed via a sequence of invocations of elementary transformations, (ii) each elementary transformation marks each program-abstraction in the system as stale by resetting the corresponding stableStatus flag, and (iii) each elementary transformation stores the details of the resulting IR changes in the global sequence of program-changes, chSequence, maintained by BasePA, to be read by the individual program analyses as and when required. Note that the first requirement does not restrict the availability of high-level transformation APIs to the optimization-pass writers; each such API may be adapted by the compiler-writers such that it invokes one or more elementary transformations directly and/or via invocation of other similar high-level APIs. For example, a high-level transformation API to delete a block of statements can be implemented as a sequence of invocations of an elementary transformation that deletes individual statements. Note that updating the high-level APIs is a one-time effort on the part of compiler-writers; no additional effort is needed from the optimization-pass writers.

3.1.3 Program Analysis Pass Classes. In Homeostasis, each program analysis is implemented as a class that inherits from the abstract class BasePA, as shown in Figure 4; this class contains various key data structures and methods that are required to enable self-stabilization of the associated program-abstractions. BasePA maintains a global set, allAnalyses, of all instances of the analysis classes (henceforth, referred to as analysis-instances). Furthermore, a sequence of all changes to the IR, resulting from various elementary transformations, is maintained in a global list, named chSequence. During stabilization trigger for any analysis-instance, if needed, the exact set of IR changes whose impact needs to be incorporated in its program-abstraction, is obtained using chIndex, an index to some location in the list chSequence. Note that both allAnalyses and chSequence are initialized to empty set/list. Homeostasis may periodically employ the compress method to reduce the space requirements of chSequence, depending upon the chIndex value of various analysis-instances in allAnalyses (details in Section 3.2).

Figure 4 shows CallGraphGenerator as a concrete class of BasePA, which implements the call-graph generation routines and maintains the program-abstraction denoting the call-graph information of the program. In Homeostasis, each program-abstraction can only be queried through its corresponding getter methods (such as getCallGraph in CallGraphGenerator). Before returning the requested information, each getter method should check if the program-abstraction is stable (by inspecting the value of stableStatus flag) and trigger stabilization if needed (by invoking the method stabilize). Depending upon the mode of stabilization, discussed next, the stabilize method provided by Homeostasis internally invokes either the compute or the handleUpdate method, passing them the correct arguments, if any.

3.1.4 Modes of Stabilization. An important defining characteristic of self-stabilization is the time and manner in which a program-abstraction is stabilized under program modifications. Accordingly, the stabilization mode can vary along the following two dimensions: eager versus lazy, and invalidate versus update.

Eager versus lazy. After an elementary transformation, the stabilization of an abstraction may either get triggered (i) immediately (eager stabilization), or (ii) only in response to the first read request made on the program-abstraction after the transformation (lazy stabilization). Note that in practice, not every program-abstraction is read after each program modification. Hence, to avoid the overheads due to the redundant invocation of the stabilization routines in case of eager stabilization, Homeostasis advocates the use of lazy modes of stabilization.
**Invalidate versus update.** In response to one or more program modifications, the resulting stabilization of a program-abstraction may either (i) involve the complete invalidation of the program-abstraction (leads to regenerating the program-abstraction from scratch), or (ii) be able to incrementally update the program-abstraction based on the modifications. *Homeostasis* attains the fully-automated stabilization for invalidate modes without requiring any stabilization-specific code from the analysis-pass writers. In invalidate modes, the stabilize method reinitializes the program-abstraction, and invokes the compute method to regenerate the program-abstraction from scratch; note that the code for this method would exist even in the absence of *Homeostasis*. In contrast, to realize the update modes of stabilization, *Homeostasis* provides a well-defined method, handleUpdate, to be implemented by the analysis-pass writers, which it later uses during automated stabilization triggers, by passing the correct set of program changes to be handled. Though the update modes may seem much more efficient than the invalidate modes, in practice the difference in their performance depends on a number of factors, such as the number of program modifications, the complexity of the associated incremental update, and so on. Further, note that enabling the update modes of stabilization for certain program-abstractions can be a challenging task. Considering such issues, *Homeostasis* supports both invalidate as well as update modes of (lazy) stabilization.

On the basis of these two dimensions, *Homeostasis* supports the following two modes of stabilization for any program-abstraction: (i) Lazy-Invalid (LZINV), and (ii) Lazy-Update (LZUPD).

### 3.2 Components of *Homeostasis*

In this section, we expand on the design details of different components of *Homeostasis* (in Sections 3.2.1–3.2.3). In Section 3.2.4, we discuss the details of how effective changes to the IR, resulting from a sequence of elementary transformations, are obtained during stabilization in *Homeostasis*. Finally, in Section 3.2.5, we demonstrate how stabilization is performed in the presence of *Homeostasis*, using the example from Figure 1(a).

#### 3.2.1 Structure of Node and its Subclasses.

Stabilization of program-abstractions in response to the modifications performed by an optimization pass, can intuitively be done in two ways: (i) the optimization pass directly modifies the program-abstraction, or (ii) the program analysis pass performs the stabilization internally, possibly based on the exact modifications that have been performed on the program. The first option can be complicated, and goes against the spirit/design principles of object-oriented programming. Hence, we use the latter option in *Homeostasis*.

**Elementary transformations.** *Homeostasis* uses elementary transformations to communicate the program modifications performed by different optimization passes to the program analyses. As mentioned in Section 3.1, in *Homeostasis*, all program modifications happen only via elementary transformations. Each elementary transformation in *Homeostasis* (i) collects the information about addition/deletion of IR nodes and edges, and (ii) makes the collected information visible to every program analysis object. We elaborate this using an example template of a generic elementary transformation method that replaces a component C with a new node, as shown in Figure 5. The templates for the elementary transformation methods that add (or remove) components can be trivially derived from the above template. The template method in Figure 5 has four main steps.

**Step A:** This step applies to all those elementary transformations that may remove a node from the IR. Besides storing the removed node in removedNodes, this step records all the edges that have been removed (in removedEdges) or added (in addedEdges) as a result of removal of the node oldX.

**Step B:** This step performs the actual modification to the IR. For example, in Figure 5, the component X of a program node is replaced with the provided new node. This step contains the code that would comprise the body of an elementary transformation in the absence of *Homeostasis*. 
Function replaceX(newNode) // Method to replace the component X with newNode
oldX = getComponentX();
// Step A: Save nodes and edges affected by the removal of old node.
Set removedNodes = {oldX};
Set removedEdges = {outgoing edges from, and incoming edges to, oldX};
Set addedEdges = {new edges formed due to the removal of oldX};
// Step B: Perform the actual program update by invoking appropriate writer(s).
Replace the component X with newNode;
// Step C: Save nodes and edges affected by the addition of new node.
removedEdges = removedEdges ∪ {old edges removed due to the addition of newNode};
addedEdges = addedEdges ∪ {outgoing edges from, and incoming edges to, newNode};
// Step D: Communicate relevant information to each analysis.
for anl ∈ BasePA.allAnalyses do anl.stableStatus = UNSTABLE;
BasePA.chSequence.addFourTupled(addedNodes, removedNodes, addedEdges, removedEdges);

Fig. 5. Template of an elementary transformation in Homeostasis that replaces the component X of a program node with newNode.

**Step C:** This step applies to only those elementary transformations that add a node to the IR. Besides storing the added node in addedNodes, this step records all the edges that have been removed (in removedEdges) or added (in addedEdges) as a result of addition of the node newNode.

**Step D:** In this step, Homeostasis first marks the status of each program analysis as UNSTABLE, so that the corresponding stabilization routine is invoked whenever its program-abstraction is read next (using the getter methods). As discussed in Section 3.1.4, for using the LZUPD mode of stabilization a program analysis requires information about all the added/removed nodes and edges. Instead of maintaining a copy of this information with each program analysis, for efficiency, Homeostasis maintains it globally in the list chSequence, in the BasePA class. This list is 0-indexed. Each element of chSequence is a four-tuple composed up of four sets: nodes added, nodes removed, edges added, and edges removed. At the end of each elementary transformation, the method addFourTuple appends the collected list of IR changes to the end of chSequence.

We now highlight three important points related to these four steps. (1) The exact definitions of Steps A–C depend on (i) the exact type of the node being transformed, (ii) the specific component being added/removed/replaced, and (iii) the semantics of the underlying language. For instance, in case of OpenMP compilers, addition/removal of a node containing flush-directives, would necessitate changes to the inter-task edges (or their equivalents) in the IR; these edges are used to denote inter-task communication via shared variables. The exact set of edges added/removed depend on the underlying semantics of OpenMP constructs. (2) An elementary transformation may also result in addition or removal of edges without any changes in the nodes. In such cases, Steps A and C capture the impacted edges accordingly. Further, if an elementary transformation changes only the type, label, or annotation of an edge, then this can be represented as the replacement of the old edge with a distinct new edge; the former is added to the set removedEdges in Step A, and the latter is added to the set addedEdges in Step C. (3) In Step D, the list chSequence may grow prohibitively large with increasing number of invocations of elementary transformations; this list is maintained efficiently by Homeostasis using a compression optimization, explained later in Section 3.3.

**Example 3.1 (Concrete elementary transformation).** Figure 6 shows the values for the various sets used in Figure 5, for an elementary transformation method that replaces the body component

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Fig. 6. Values for the various sets used in Figure 5, for a concrete elementary transformation that replaces the body of a while-statement in the IMOP compiler framework (WhileStatementCFGInfo.java: 81–146).

```java
Elementary transformation : WhileStmt::setBody(Statement newBody);
oldBody = this.body
Set removedEdges = {(this.predicate, oldBody), (oldBody, this.predicate), ...}
Set addedEdges = {(this.predicate, newBody), (newBody, this.predicate), ...}
Set removedNodes = {oldBody}
Set addedNodes = {newBody}
```

Fig. 7. Constructor and stabilizer methods of BasePA, and a template getter of a program-abstraction.

of a while-statement with a given argument (newBody). This example has been taken from our implementation of Homeostasis in the IMOP [Nougriahyia and Nandivada 2019] compiler framework for OpenMP C programs. Note that in addition to the elements shown, the sets removedEdges and addedEdges also include all the jump edges (due to jump statements, such as continue, break, etc.) that will be removed/added from the IR as a result of this elementary transformation. Furthermore, these sets also contain inter-task edges\(^2\) that are used as a part of the IR to model the parallel semantics of OpenMP C.

3.2.2 Structure of BasePA and its Subclasses. Homeostasis maintains a global set allAnalyses of program analysis instances, by adding the reference of each program analysis instance (at the

\(^2\)IMOP uses the concept of inter-task edges between flush operations of a parallel region to statically model the communication that may happen using shared variables between different threads.
Fig. 8. Algorithms to obtain the net IR changes for those elements in chSequence whose impact needs to be taken into account by the handleUpdate method to obtain the stable program-abstraction.

```plaintext
Function getNetChanges(chIndex) // Obtain the net IR changes to be handled for a given chIndex
    netChanges = <>;
    foreach ind from (chIndex + 1) to (BasePA.chSequence.size() - 1) do
        netChanges = mergeChanges(netChanges, BasePA.chSequence.get(ind));
    return netChanges;

Function mergeChanges(ch1, ch2) // Obtain the net IR changes for the given changes
    mergedChanges = <>;
    mergedChanges.addNodes = (ch1.addNodes\ch2.removeNodes) \cup (ch2.removeNodes\ch1.addNodes);
    mergedChanges.remNodes = (ch1.removeNodes\ch2.addNodes) \cup (ch2.addNodes\ch1.removeNodes);
    mergedChanges.addEdges = (ch1.addEdges\ch2.removeEdges) \cup (ch2.removeEdges\ch1.addEdges);
    mergedChanges.removeEdges = (ch1.removeEdges\ch2.addEdges) \cup (ch2.addEdges\ch1.removeEdges);
    return mergedChanges;
```

3.2.4 Obtaining Net IR Changes. In order to obtain the net IR changes to be taken into account by the handleUpdate method during a stabilization trigger, Homeostasis provides getNetChanges function, whose algorithm is shown in Figure 8. The net IR change is obtained by merging the IR changes denoted by all the elements (if any) that lie to the right of the location indexed by chIndex in the global list chSequence. The exact merge operation is specified in the function mergeChanges in Figure 8. We demonstrate the working of these functions using a concrete example.
**Fig. 9.** A concrete example demonstrating how the net IR changes are obtained in the LZUPD mode of stabilization for some analysis-instance with value of chIndex as $m$. Size of the global list chSequence is $(m + 4)$. Each element of chSequence shows a four-tuple, corresponding to the following sets, in order: nodes added, nodes removed, edges added, and edges removed. The $\oplus$ operator denotes the application of mergeChanges function from Figure 8.

**Example 3.2 (Net IR changes).** Figure 9 illustrates a concrete example of how the net IR changes are obtained by Homeostasis, when required by the handleUpdate method during stabilization trigger of some analysis-instance. The value of chIndex for the analysis-instance is $m$, and the size of chSequence list is $(m + 4)$. Assume, the last three elementary transformations are:

(i) Addition of node $n_1$, resulting in addition of edges $\{e_1, e_2\}$.

(ii) Replacement of node $n_3$ with node $n_2$, resulting in addition of edges $\{e_3, e_4\}$, and removal of edges $\{e_5, e_6\}$.

(iii) Replacement of the previously-added node $n_1$ with node $n_4$, resulting in addition of edges $\{e_7, e_8\}$, and removal of the previously-added edges $\{e_1, e_2\}$.

The figure shows the corresponding set of IR changes, whose impact needs to be taken into account during the next stabilization trigger. The net IR changes are obtained by merging all the three IR changes using the mergeChanges function from Figure 8 (represented using $\oplus$ binary operator).

Now, we demonstrate how self-stabilization achieved by Homeostasis, as discussed in this section, fixes the issues in compilation of the example shown in Figure 1(a), without requiring any changes to the code written by the optimization-pass writer.

**3.2.5 Example Compilation with Homeostasis.** Let us revisit the example of the dead-branch remover optimization pass given in Figure 1(a), implemented in a Homeostasis-enabled compiler. Here, the replace method would invoke a sequence of elementary transformations, directly or indirectly through other high-level transformation APIs. These elementary transformations will capture the information about the resulting program modifications (say, from $P_1$ to $P_2$), and notify it to BasePA, thereby making the information available to all program analysis passes, including the points-to analysis pass. Later, when an attempt is made to read the points-to map using a getter of the analysis pass, say from within the methods isNeverZero and isAlwaysZero, the getter would automatically trigger stabilization of the points-to map internally such that the map correctly corresponds to $P_2$. Hence, the compiler will be able to precisely deduce that the pointer $p$ at L2 will now point only to variable $a$; this would trigger the removal of the false branch of the if-statement at L2, thereby generating the expected program, $P_3$. 

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3.3 Compression Optimization: Efficient Tracking of Program Changes

The number of elementary transformations that a program undergoes during compilation can be substantial—compilation of large programs may easily involve several hundreds of elementary transformations. Hence, storing the individual IR-changes resulting from each elementary transformation separately in the global list chSequence can be prohibitively expensive in terms of space requirements. In order to address this challenge, Homeostasis employs a compression optimization that reduces the size of chSequence, relying on the following two key observations on the value of chIndex of analysis-instances that employ the LZUPD mode of stabilization.

**Observation 1.** If the IR-changes corresponding to an elementary transformation have been taken into account by all the analysis-instances in the compiler, then the IR-changes need not be saved in chSequence. In other words, if no analysis-instance has chIndex less than 0, then the first element (at index 0) in chSequence can be safely removed (while adjusting the chIndex of all the analysis-instances by decrementing 1 from their values).

**Correctness argument.** Recall that chSequence is a 0-indexed list. Furthermore, as per the definition of getNetChanges from Figure 8, the net IR changes to be used in the next stabilization trigger of an analysis-instance are obtained by merging the IR changes denoted by all the elements that lie beyond the index chIndex (of the analysis-instance) in chSequence. Hence, if there is no analysis-instance with chIndex less than 0, then the first element of chSequence (at index 0) will not be used to obtain the net IR changes during the stabilization trigger of any analysis-instance.

**Observation 2.** If no analysis-instance has a chIndex that indexes into the location of an IR-change element in the chSequence list, then it is safe to merge the IR-change element to its successor, if any, in the list (while also adjusting the chIndex of various analysis-instances appropriately).

**Correctness argument.** Consider an index i in chSequence, such that no analysis-instance has its chIndex as i. In this case, those analysis-instances whose chIndex is greater than i, will not consider the element at index i while obtaining their net IR changes during future stabilization triggers (see Figure 8). Whereas, those analysis-instances whose chIndex is less than i, will anyway merge the elements at index i and (i + 1) (if the element exists) to obtain the net IR changes for their next stabilization trigger. Hence, merging the elements at i and (i + 1) in chSequence, will not affect the net IR changes for any analysis-instance during any of their future stabilization triggers.

The compression optimization employed by Homeostasis compresses the global chSequence list by repeated application of these two observations, until fixed-point. Note that Homeostasis does not dictate how often the compression optimization is invoked during the compilation. The exact details of the compression optimization, including details on how various corner cases are handled, are discussed formally in Section 4.2. In this section, we demonstrate the application of these two observations using a concrete example.

**Example 3.3 (Compression Optimization).** In Figure 10, we demonstrate the working of compression optimization on a concrete example. Consider only two analysis-instances in the compiler, namely a1 and a2. Their chIndex values are 1 and 3, respectively. Upon repeated applications of Observation 1, we find that IR-changes A and B both can be safely removed from chSequence. Accordingly, both the chIndex values are decremented by 2. Furthermore, the IR-changes C and D (and later E and F), can be merged, by repeated applications of Observation 2. Due to the merging of C and D, the chIndex of a2 is further decremented by 1, to obtain 0.

**Impact of compression optimization on space complexity of tracking IR-changes.** In the absence of compression, the list chSequence would contain as many elements as the number of
elementary transformations employed (say $k$). The size of each element can be $O(s)$, in terms of
the size $s$ of the input program (calculated as some function of the number of nodes and edges
in the IR). Hence, the total space complexity of an uncompressed chSequence can be $O(k \times s)$. In
contrast, from Observations 1 and 2, we note that the number of elements in the fixed-point
compressed state of chSequence cannot be greater than $\min(k, p)$, where $p$ is the number of
analysis-instances in the compiler. Since $p$ is usually significantly smaller than $k$, the worst-case
space complexity of chSequence with compression optimization, drops to $O(p \times s)$.

**Time complexity of the compression algorithm.** When the compression algorithm is invoked,
the fixed-point state obtained upon repeated applications of Observations 1 and 2 may compress
chSequence to a single-element, in the worst-case. Hence, if the total number of elementary
transformations performed is $k$, then the compression algorithm may perform at most $k$ merge
operations (using function mergeChanges, Figure 8). If the program size is given by $s$, then the
worst-case time complexity of each merge operation will be $O(s)$. Hence, the worst-case time
complexity for the compression algorithm is $O(k \times s)$.

### 3.4 Working in a Homeostasis-Enabled Compiler

We now describe the additional effort that is needed to enable and use Homeostasis, and the
impact of using it on the key questions from Figure 2. For this discussion, let us assume a
hypothetical compiler $C$ and its Homeostasis-enabled counterpart $C_{HS}$. We present
this discussion with respect to three key kinds of compiler developers: (i) Compiler-base writers
obtain $C_{HS}$ from $C$ by implementing those core components of Homeostasis which are common
across all the analysis/optimization passes. (ii) Analysis-pass writers write analysis passes in $C_{HS}$.
(iii) Optimization-pass writers write optimization passes in $C_{HS}$. Figure 11 summarizes the impact
of enabling and using Homeostasis, on these key developers.

**Impact on compiler-base writer.** To obtain $C_{HS}$ from $C$, the compiler-base writer will have
to additionally perform the following tasks: (i) identify the elementary transformations and
develop them in accordance with the design discussed in Section 3.2.1, (ii) ensure that all
high-level transformation APIs in the compiler internally rely on the identified set of elementary
transformations to perform any program modifications, and (iii) create a base class for all analysis

![Fig. 10. Concrete example of compression optimization, demonstrating application of Observations 1 and 2. Those indices in chSequence, which are indexed to by chIndex of any analysis-instance in the compiler, are shown encircled.](image-url)
passes, equivalent to BasePA from Sections 3.2.2 and 3.2.3. Note that these tasks are one-time efforts and involve modifying only some of the IR-related classes.

**Impact on analysis-pass writer.** Given any analysis class AC in C, the analysis writer would have to additionally ensure the following, for adapting AC to \( C_{HS} \): (i) AC is a subtype of BasePA, (ii) the code of AC needed to generate the corresponding program-abstraction is written in the compute method, (iii) the corresponding program-abstraction for AC can be accessed only through a getter as defined in Section 3.2.2, and (iv) optionally, if the analysis writer wants to support the LZUPD mode of stabilization, the method handleUpdate has to be defined as per Section 3.2.3.

In terms of additional coding effort, ensuring point (i) is trivial; so is ensuring points (ii) and (iv), since the relevant code would be common to both \( C \) and \( C_{HS} \), and would only possibly differ in their method names. We argue that point (iii) would be automatically ensured in an object-oriented compiler, and hence requires no additional effort. Consequently, we claim that the amount of additional coding effort required to write an analysis in \( C_{HS} \) is minimal. In terms of the key questions shown in Figure 2, in a Homeostasis-enabled compiler, an analysis-pass writer does not need to address questions \( Q_{1-3}^{T} \), while adding any new program analysis in the LZINV mode of stabilization; for the LZUPD mode of stabilization, the analysis writer needs to address only \( Q_{3}^{T} \), by providing the definition of the method handleUpdate. Note that this is not an additional overhead when using Homeostasis—such a code is needed even in the case of manual stabilization in incremental update modes.

**Impact on optimization-pass writer.** An optimization-pass writer need not write any additional code to adapt an optimization in \( C \) to \( C_{HS} \). In terms of the key questions shown in Figure 2, in a Homeostasis-enabled compiler, an optimization pass writer need not address the key questions \( Q_{1-3} \), while adding any new optimization in a Homeostasis-enabled compiler. For instance, in Figure 1, a Homeostasis-enabled compiler can generate the expected program \( P_{3} \) without requiring any changes to the code of the optimization (DeadBranchRemover) shown in Figure 1(a). Note that the compiler-base writer would have updated the code for high-level transformation APIs (including the replace method), such that all program-changes are expressed directly or indirectly using elementary transformations; a one-time effort.

**Overall Summary:** Once a Homeostasis-enabled compiler has been designed (requires one-time moderate effort on the part of the compiler-base writers), designing and implementing program analyses and optimizations require minimal/zero additional coding effort to maintain stable program-abstractions.

## 4 FORMAL DESCRIPTION AND CORRECTNESS OF HOMEOSTASIS

We now present a formal description of various components of Homeostasis. In Section 4.1, we formally define an abstract Homeostasis-enabled compiler, and argue the correctness guarantee provided by Homeostasis: in a Homeostasis-enabled compiler, any compiler pass accessing the program-abstraction of an analysis will only read the stable value of that program-abstraction.
| Set | Description | Typical Element Symbol |
|-----|-------------|-----------------------|
| $N$ | set of all possible IR nodes | $n$ |
| $E$ | set of all possible IR edges | $e$ |
| $L$ | set of all valid IR programs $\subseteq \mathcal{P}(N) \times \mathcal{P}(E)$ | $P_i$ |
| $\Gamma$ | set of all the elementary transformations, where each element is of the form $L \to L$ | $\tau_i$ |
| $C$ | set of all program-changes $\subseteq \mathcal{P}(N) \times \mathcal{P}(N) \times \mathcal{P}(E) \times \mathcal{P}(E)$; if program $P_i = (N_i, E_i)$ and program $P_j = (N_j, E_j)$, then program-change $\Delta(P_i, P_j) = c = (N_j \setminus N_i, N_i \setminus N_j, E_j \setminus E_i, E_i \setminus E_j)$ | $c$ |
| $C^*$ | set of all change-sequences of elements in $C$, of any size | $\bar{c}$ |
| $\mathcal{A}$ | set of all analysis-instances in the compiler $= \{A_1, A_2, \ldots\}$, where each element is of the form $L \to R_i$ | $A_i$ |
| $R_i$ | set of all program-abstraction values for analysis-instance $A_i$ | $v$ |
| $\mathcal{R}$ | set of all the program-abstraction values $= R_1 \cup R_2 \cup \ldots$ | $-$ |
| $\text{StBST}$ | set of stabilization-status values $= \{\text{STABLE}, \text{UNSTABLE}\}$ | $\text{st}$ |
| $\text{StBMd}$ | set of lazy modes of stabilization $= \{\text{LZINV, LZUPD}\}$ | $m$ |
| $D_i$ | set of all analysis-states for the analysis-instance $A_i$ | $d$ |
| $= R_i \times \text{StBST} \times \text{StBMd} \times \mathbb{N}_1$ | $-$ |
| $\mathcal{D}$ | set of all the analysis-states $= D_1 \cup D_2 \cup \ldots$ | $-$ |
| $\mathcal{S}$ | set of compiler states $= L \times \mathcal{P}(\mathcal{D}) \times C^*$ | $S$ |

Fig. 12. Sets and maps used in the formalism. $\mathbb{N}_{-1}$ is the set of natural numbers $\cup \{0, -1\}$. $\mathcal{P}(X)$ denotes the power set of $X$.

(see Theorem 4.12). Later, in Section 4.2, we first formally describe how Homeostasis maintains the compressed list of program-changes, and then we prove that the compression is semantics-preserving.

### 4.1 An Abstract Homeostasis-Enabled Compiler

Consider a Homeostasis-enabled compiler for an IR language $\mathbb{L} = \{P_1, P_2, \ldots\}$, where each $P_i$ is a valid (syntactically and semantically correct) IR program. Without loss of generality, we assume each program IR to be in the form of a graph. Let the fixed set of elementary transformations in the compiler be represented as $\Gamma = \{\tau_1, \tau_2, \ldots, \tau_m\}$, where each transformation $\tau_i$ is a map $\mathbb{L} \to \mathbb{L}$. Note that each elementary transformation updates an IR program by adding/removing a set of nodes and/or edges in the graph to obtain the modified IR program. Figure 12 summarizes the sets and maps used in the formalism.

**Definition 4.1 (Program-change).** Given two programs, $P_i$ and $P_j \in \mathbb{L}$, the program-change between $P_i$ and $P_j$ (denoted by $\Delta(P_i, P_j)$) is defined as a 4-tuple of the form $(\delta_{na}, \delta_{nr}, \delta_{ea}, \delta_{er})$, where to obtain $P_j$ from $P_i$, $\delta_{na}$ is the minimal set of program nodes to be added to $P_i$, $\delta_{nr}$ is the minimal set of nodes to be removed from $P_i$, $\delta_{ea}$ is the minimal set of edges to be added to $P_i$, and $\delta_{er}$ is the minimal set of edges to be removed from $P_i$. Specifically, for $P_i = (N_i, E_i)$ and $P_j = (N_j, E_j)$, the following holds: $\delta_{na} = N_j \setminus N_i$, $\delta_{nr} = N_i \setminus N_j$, $\delta_{ea} = E_j \setminus E_i$, and $\delta_{er} = E_i \setminus E_j$. We denote the set of all possible program-changes in $\mathbb{L}$ by $C$. Further, we term a sequence of program-changes, of any
length, as a change-sequence. Without loss of generality, for the ease of exposition, we assume that all such sequences are 0-indexed.

**Definition 4.2 (Merge Operator).** If $\Delta(P_a, P_b) = c_p$ and $\Delta(P_b, P_c) = c_q$, then we use $c_p \oplus c_q$ to provide the net program-change between $P_a$ and $P_c$. The set $C$ is closed under the binary operator $\oplus$ ($C \times C \rightarrow C$). This operator corresponds to the function mergeChanges from Figure 8.

In a compiler written in OO-style, we assume that each analysis is implemented as a class, extending BasePA. During the invocations of the compiler, one or more analysis classes get instantiated (one or more times). Let $\mathcal{A} = \{A_1, A_2, \ldots\}$ be the set of all analysis-instances (such as an instance of points-to analysis, an instance of alias analysis, and so on) in the compiler, where each analysis-instance is of the form $A_i : L \rightarrow R_i$, where $R_i$ denotes the set of meaningful program-abstraction values for $A_i$. We term $A_i(P)$ as the stable program-abstraction of the analysis-instance $A_i$ for program $P$.

**Definition 4.3 (Analysis State).** While compiling a program $P$, at any point during the compilation process, for an analysis-instance $A_i$, we define its analysis state as a 4-tuple of the form $d_i = (\nu, st, m, r)$, where $\nu \in R_i$ is the value currently maintained by the compiler for the program-abstraction corresponding to $A_i$, $st \in \text{StbSt} = \{\text{STABLE}, \text{UNSTABLE}\}$ denotes the current stabilization status of $A_i$, $m \in \text{StbMd} = \{\text{LZINV}, \text{LZUPD}\}$ determines the selected lazy mode of stabilization for $A_i$, and $r$ is either $-1$ (for LZINV mode of stabilization) or an integer that refers to an index in the global change-sequence (for LZUPD mode of stabilization); $r$ is termed as the change-index of $A_i$. For the LZUPD mode of stabilization, intuitively, the non-negative change-index of an analysis-instance $A_i$ denotes that position in the global change-sequence list until and including which the impact of all elementary transformations have been taken into account, to arrive at the program-abstraction value $\nu$ for analysis-instance $A_i$.

Let the set $R = R_1 \cup R_2 \cup \ldots$ be the set of all possible values for all program-abstractions. Further, let $D$ be the set of all analysis states, for all the analyses-instances.

**Definition 4.4 (Compiler State).** Consider a compilation process, where $k$ elementary transformations have been performed on the input program $P$. We define a compiler state as a 3-tuple of the form $S_i = (P_i, D_i, \overline{c}_i)$, where $P_i$ represents the current program (obtained upon applying the $k$ transformations on $P$), $D_i = \{d_1, d_2, \ldots\}$ represents the current set of analysis states for different analysis-instances (each a 4-tuple as defined above), and $\overline{c}_i = \{c_0, c_1, c_2, \ldots c_{k-1}\}$, denotes the sequence of $k$ program-changes obtained upon application of each of the $k$ elementary transformations (in order) on the input program $P$. We denote the set of all compiler states by $S$. Note that for an input program $P$, the initial compiler state when compilation starts is $(P, \emptyset, \emptyset)$.

Now, we state two axioms that are derived from the assumption that the analysis writer has provided the correct implementations of compute and handleUpdate methods; the latter is required only for the LZUPD mode of stabilization. Axiom 4.5 formally states that the exhaustive algorithm of an analysis-instance has been correctly implemented by the analysis writer in a method named compute. Axiom 4.6 formally states that in order to realize the incremental-update mode of stabilization, the analysis writer has provided a correct definition of the handleUpdate method, specifying how an abstraction would get updated in response to the given program-changes (between the current program and the one to which the stale program-abstraction corresponds). For the ease of presenting our formal argument, we assume that compute and handleUpdate methods also return the set of abstractions that were stabilized during the evaluation of these methods. This set is used to only facilitate the formal treatment of our proposed design, and is not required otherwise to perform the actual stabilization.
Axiom 4.5. In a Homeostasis-enabled compiler, consider an analysis-instance \( A_k \) with LZINV stabilization mode. The analysis writer of \( A_k \) provides a correct implementation of the method \( \text{compute} \), such that when \( \text{compute} \) is invoked at any compilation point, \( \text{compute} \) returns a two-tuple \( (v, L) \), where \( v = A_k(P_i) \), and \( L \subseteq \overline{A} \), is the set of abstractions which were stabilized during the evaluation of the compute method.

Axiom 4.6. Consider an analysis \( A_k \) with LZUPD mode of stabilization. Consider any compiler state \( S_i = (P_i, D_i, \overline{c}_i) \), where the corresponding analysis state for \( A_k \) in \( D_i \) is denoted by \( d_k = (v_k, \text{LKUPD}, r_k) \). Further, let, \( \overline{c}_i = (c_0, c_1, \ldots, c_n) \). In a Homeostasis-enabled compiler, the analysis writer of \( A_k \) provides the correct implementation of method \( \text{handleUpdate} \), such that if there exists a program \( P_j \in L \), such that \( v_k = A_k(P_j) \) and \( \Delta(P_j, P_i) = c_{r_k+1} \oplus c_{r_k+2} \oplus \ldots \oplus c_n \), then, when \( \text{handleUpdate} \) is invoked on the compiler state \( S_i \), it returns a pair \( (v, L) \), where (i) \( v = A_k(P_i) \), and (ii) \( L \subseteq \overline{A} \), the set of abstractions which were stabilized during the evaluation of the handleUpdate method.

In Figure 13, we provide the definition of stabilization-function, \( \sigma : S \times D \rightarrow D \times \mathbb{P}(A) \), which, given a compiler state and a (possibly stale) analysis state for some analysis-instance (in that compiler state), utilizes the definitions of compute and handleUpdate methods, to provide a two-tuple: (i) the stabilized analysis state of the analysis-instance, and (ii) the set of other analysis-instances on which the stabilization-function was invoked internally during the evaluation of compute or handleUpdate method. Given such a two-tuple \( \Theta \), we use \( \Theta.\text{fst} \) and \( \Theta.\text{snd} \) to refer to the first and second elements, respectively, of the tuple.

If the given analysis state is already \textbf{Stable}, the stabilization-function returns the analysis state as it is, along with an empty set of analysis-instances (rule [Stb]). Otherwise, when the stabilization mode of the analysis state is LZINV, the method compute is invoked in order to obtain the correct abstraction value \( (v') \) by re-running the corresponding analysis from scratch on the current program (rule [Stb-Inv]). In contrast, as per rule [Stb-Upd], when the stabilization mode is LZUPD, the method handleUpdate is invoked to obtain the correct abstraction value \( (v') \), given the following arguments: (i) a reference to the analysis-instance \( (A_k) \), (ii) the current program, (iii) the unstable/stale abstraction value \( (v) \), and (iv) the net program-changes obtained by using the merge operator on the appropriate elements from the change-sequence. Note that the change-index for the returned analysis state is set to \( n \) (index of the last element in the global change-sequence).
Definition 4.7 (Compiler Action). Recall that Homeostasis allows changes to the IR program only through elementary transformations. Similarly, the program-abstraction of an analysis can be accessed only through its appropriate getters. Accordingly, we define three kinds of compiler actions that can be issued by an optimization or analysis pass, and may alter the current compiler state, \(S = \langle P, D, \tau \rangle\).

(i) Given an analysis class \(AC\), the compiler action \(\text{construct}(AC, m)\) creates an instance of \(AC\), invokes the \(\text{compute}\) method to populate the program-abstraction, and sets the stabilization mode of the constructed analysis-instance to \(m \in \text{STBMD}\).

(ii) The compiler action \(\text{get}(A_k)\) returns the value \(A_k(P)\).

(iii) The compiler action \(\text{transform}(\tau_i)\) transforms the current program \(P\) to \(\tau_i(P)\).

We represent the set of all possible compiler actions with \(W\). \(\Box\)

Note that in object-oriented compilers, the \(\text{construct}\) compiler action for an analysis will always be invoked before the first invocation of the corresponding \(\text{get}\) compiler action.

Definition 4.8 (\(\text{apply}\) Function). We define a compilation step using the function \(\text{apply}: S \times W \rightarrow S \times (\mathcal{R} \cup \{\epsilon\})\), which applies a given compiler action \(w\) on the compiler state \(s\), to generate (i) a possibly-modified compiler state \(s'\), and (ii) a program-abstraction value or \(\epsilon\).

For a Homeostasis-enabled compiler, the definition for function \(\text{apply}\) is shown in Figure 14(a)–14(c), for the design templates of various components shown in Figure 7(a) (constructor), Figure 7(b)–7(c) (getters and stabilizers), and Figure 5 (elementary transformations), respectively.

- When a \(\text{construct}\) compiler action is issued for an analysis-instance \(A\), an initial analysis state for \(A\) is generated and added to the set of analysis states in the current compiler state (rule [C-\(\text{Apply}\)]). Note that in the case of LZUPD mode, the change-index of \(A\) is set to the index of the last element in the global change-sequence; it is set to \(-1\) if the list is empty.

- When a \(\text{get}\) compiler action is issued for \(A_k\), the design of Homeostasis ensures that the analysis state of \(A_k\) is changed as per the mapping rules shown in Figure 14(b) and 13. Using Axioms 4.5 and 4.6, rules [STB-1\(\text{New}\)] and [STB-UPD] set the stabilization status of \(A_k\) to STABLE, as can be inferred from the design of an abstraction getter, and stabilizer.

- When a \(\text{transform}\) compiler action with elementary transformation \(\tau_i\) is issued on a compiler state \(S = \langle P, D, \tau \rangle\), then as per rule [T-\(\text{Apply}\)] in Figure 5, the design of Homeostasis changes the compiler state to a tuple where, (i) the current program \(P\) is modified to \(\tau_i(P)\), (ii) the stabilization status of all analyses is set to UNSTABLE, and (iii) \(\Delta(P, \tau_i(P))\) is added to the sequence of program-changes.

Definition 4.9 (Valid Compiler State). We term a compiler state of the form \(S_i = \langle P_i, D_i = \{d_1, d_2, \ldots\}, \tau_i = \langle c_0, c_1, \ldots, c_n\rangle\rangle\) as a valid compiler state, if and only if the following condition, termed as stability-condition, holds for the state \(d_j = \langle v_j, s_{jt}, m_j, r_j \rangle \in D_i\) of each analysis-instance \(A_j\):

(i) if \(s_{jt} = \text{STABLE}\), then \(r_j = n\) and \(v_j = A_j(P_i)\), else
(ii) if \(s_{jt} = \text{UNSTABLE}\), then \(n \geq 0\), \(r_j < n\), and \(\exists P_0 \in \mathbb{L}\), such that \(v_j = A_j(P_0)\) and \(\Delta(P_0, P_i) = c_{r_{j+1}} \oplus c_{r_{j+2}} \ldots \oplus c_n\).

Intuitively, a compiler state is considered valid when each program-abstraction is either stable, or has access to the complete information that can be used to make it stable. \(\Box\)

The following Lemma gives the correctness guarantee for the value returned by a \(\text{get}\) compiler action.
Fig. 14. Definition for the \texttt{apply} function, derived from the design of \textit{Homeostasis} explained in Section 3.2.

**Lemma 4.10.** If a compiler state $S_i = \langle P_i, D_i, \overline{c} \rangle$ is valid, then for each analysis-instance $A_k$ with corresponding analysis state $d_k \in D_i$, the value obtained upon invocation of get compiler action for $A_k$ (i.e., get($A_k$)) on $S_i$, will always be same as $A_k(P_i)$ (i.e., the stable program-abstraction value). Formally, for each analysis $A_k$ and valid compiler state $S_i$, there exists a program $P_j$ such that $A_k(P_j)$ and $\Delta(P_j, P_i) = c_{r_k+1} \oplus c_{r_k+2} \ldots \oplus c_U$. Using Axiom 4.6, we obtain $v'_k = A_k(P_i)$. Hence proved. □
The following Lemma gives the correctness guarantee that the invocation of any compiler action (construct, get, or transform) on a valid compiler state will result in a valid compiler state.

**Lemma 4.11.** For every sequence \( W = (\langle w_1, w_2, \ldots \rangle) \) of compiler actions, the compiler state, starting with the initial compiler state \( \langle P, \phi, \phi \rangle \), remains valid after application of each action from the sequence.

**Proof.** (Proof by natural induction on the number of elements in \( W \).)

**Base Case:** \( |W| = 0 \). For an input program \( P \), the initial compiler state is always \( \langle P, \emptyset, \emptyset \rangle \), which is trivially valid.

**Inductive hypothesis:** The compiler state, say \( S_i = \langle P_i, D_i, c_i \rangle \), obtained after application of all compiler actions from the string \( W_m \), of length \( m \), is valid. Let \( D_i = \{ d_1, d_2, \ldots, d_k \} \), then \( S' \) is a valid compiler state. Three cases occur for possible form of compiler action \( w_{m+1} \):

**Case A:** \( w_{m+1} \) is \( \text{construct}(AC, m_s) \) for some analysis class \( AC \). Say the created analysis-instance is \( A_s \) and the initial analysis state for \( A_s \) is \( d_s = \langle v_s, s_{st}, m_s, r_s \rangle \). As per rule \([\text{C-APPLY}]\), \( S' = (P_i, D_i \cup \{ d_s \} = (A_s(P_i), \text{STABLE}, m_s, U), c_i) \). \( S' \) is trivially valid as \( d_s \) satisfies the stability-condition from Definition 4.9. Hence proved.

**Case B:** \( w_{m+1} \) is \( \text{get}(A_s) \) for some \( d_x \in D_i \). As \( S \) is a valid compiler state, \( \forall d_j \in D_i \) satisfies the stability-condition. Let \( \text{get}(A_s) \) change a subset of analysis states \( D_y \subseteq D_i \). Let \( d_y (\in D_y) \) be given by \( \langle v_y, s_{st}, m_y, r_y \rangle \). Assume, for each \( d_y \), the changed analysis state \( d_y' \) is given by \( \langle v_y', s_{st}', m_y, r_y' \rangle \). To prove that \( S' \) is a valid compiler state, it is sufficient to prove that each such \( d_y' \) satisfies the stability-condition. Let us consider any such \( d_y' \). Two sub-cases arise based on the values of \( s_{st} \):

**Case B.1:** \( s_{st} = \text{STABLE} \). As \( d_y' \) satisfies the stability-condition, we derive the following from rule \([\text{STB}]\): \( s_{st}' = \text{STABLE}, r_y' = r_y = U \), and \( v_y' = v_y = A_x(P_i) \). Hence, \( d_y' \) satisfies the stability-condition. Hence proved.

**Case B.2:** \( s_{st} = \text{UNSTABLE} \). From rules \([\text{STB-INV}]\) and \([\text{STB-UPD}]\), we derive \( s_{st}' = \text{STABLE} \). Similarly, we derive \( r_y' = -1 \) or \( r_y' = U \), from rules \([\text{STB-INV}]\) and \([\text{STB-UPD}]\), respectively. Depending upon value of \( m_y \), two sub-cases arise:

**Case B.2.i:** \( m_y = \text{LZINV} \). From rule \([\text{STB-INV}]\), \( v_y' = \text{compute}(A_y, P_i) \). From Axiom 4.5, \( v_y' = A_y(P_i) \). Hence, \( d_y' \) satisfies the stability-condition, and \( S' \) is a valid compiler state.

**Case B.2.ii:** \( m_y = \text{LZUPD} \). From rule \([\text{STB-UPD}]\), \( v_y' = \text{handleUpdate}(A_y, P_i, v_y, c_{r+y+1} \oplus c_{r+y+2} \oplus \ldots \oplus c_U) \). From Axiom 4.6, \( v_y' = A_y(P_i) \), if there exists a program \( P_k \in \mathbb{L} \), such that (i) \( v_y = A_y(P_k) \), and (ii) the net program-change (i.e., last argument of \( \text{handleUpdate} \)) is same as \( \Delta(P_k, P_i) \). Since \( d_y \) satisfies the stability-condition, such a program \( P_k \) exists. (Note that the \( \Delta(P_k, P_i) \) is the same as the last argument of \( \text{handleUpdate} \).) Hence, \( v_y' = A_y(P_i) \), and \( S' \) is a valid compiler state.

**Case C:** \( w_{m+1} \) is \( \text{transform}(\tau_i) \) for some \( \tau_i \in \Gamma \). Let \( S' = (P_i', D_i', c_i') \). From rule \([\text{T-APPLY}]\), we have: \( P_i' = \tau_i(P_i) \), and \( c_i' = (c_o, c_1, \ldots, c_U, \Delta(P_i, \tau_i(P_i))) \). Furthermore, for each \( d \in D_i \), there exists a modified analysis state \( d' \in D_i' \). To prove that \( S' \) is a valid compiler state, we need to prove that each analysis state \( d' \in D_i' \) satisfies the stability-condition. Consider any analysis-state \( d_x \in D_i \), and its corresponding modified analysis-state \( d_x' \in D_i' \). Let \( d_x = \langle v_x, s_{st}, m_x, r_x \rangle \), and \( d_x' = \langle v_x', s_{st}', m_x', r_x' \rangle \). Now, two sub-cases arise based on the value of \( s_{st} \):

**Case C.1:** \( s_{st} = \text{STABLE} \). Since \( d_x \) satisfies the stability-condition, we have: \( r_x = U \) (if \( m_x = \text{LZUPD} \) or \( r_x = -1 \) (if \( m_x = \text{LZINV} \)), and \( v_x = A_x(P_i) \). From rule \([\text{T-APPLY}]\), we have: \( v_x' = v_x, m_x' = m_x, r_x' = r_x, \) and \( s_{st}' = \text{UNSTABLE} \). From Definition 4.9, \( d_x' \) satisfies the stability-condition, and \( S' \) is a valid compiler state.
Case C.2: $st_x = \text{UNSTABLE}$. Since $d_x$ satisfies the stability-condition, we know that: $U \geq 0$, $r_x < U$, and that a program, say $P_j$, exists such that $v_x = A_x(P_j)$ and $\Delta(P_j, P_i) = c_{r_x+1} \oplus c_{r_x+2} \ldots \oplus c_U$.

From rule $\text{T-Apply}$, we have:  $v_x' = v_x$, $m_x = m_x'$, $r_x' = r_x$, and $st_x' = \text{UNSTABLE}$. Hence, $r_x' < U + 1$.

Further from the definition of $\oplus$, $\Delta(P_j, P_i') = \Delta(P_j, P_i) \oplus \Delta(P_i, P_i')$. Hence, $\Delta(P_j, P_i') = \Delta(P_j, P_i) \oplus c_{r_x+1} \oplus c_{r_x+2} \ldots \oplus c_U \oplus c_{U+1}$. By Definition 4.9, $S'$ is a valid compiler state.

Now, we first state the correctness theorem for Homeostasis. Intuitively, Theorem 4.12 states that at any point of time during compilation, the analysis results given by Homeostasis match those obtained by rerunning the complete analyses, provided the methods compute and $\text{handleUpdate}$ provided by the analysis writer are correct (i.e., Axioms 4.5 and 4.6 hold).

**Theorem 4.12 (Correctness of Homeostasis).** At any compilation point of a Homeostasis-enabled compiler with compiler state $S_i = (P_i, D_i, \vec{c_i})$, for each analysis $A_k$ with corresponding analysis state $d_k \in D_i$, the value obtained upon invocation of get compiler action for $A_k$ (i.e., $\text{get}(A_k)$) on $S_i$, will always be same as $A_k(P_i)$. Formally, for each analysis $A_k$ and compiler state $S_i$, $\exists S_j \in \mathbb{S}$, such that $\text{apply}(S_i, \text{get}(A_k)) \Rightarrow (S_j, A_k(P_i))$.

**Proof.** Follows directly from Lemma 4.10 and Lemma 4.11. □

### 4.2 Compression of Change-Sequence in Homeostasis

Homeostasis keeps the global change-sequence compact by internally performing the compression operation on it, as discussed in Section 3.3. In this section, we formalize this functionality, and argue that the correctness of Homeostasis continues to hold when we use the proposed idea of change-sequence compression.

Figure 15 presents the formal definition of the compress function. This function takes a two-tuple of the form $(D, \vec{c})$, where $D$ is a set of analysis-states, and $\vec{c}$ is a change-sequence. The compress function returns another two-tuple, say $(D', \vec{c'})$, such that (i) the change-sequence $\vec{c'}$ is obtained by optionally compressing a single element of the input change-sequence $\vec{c}$, and (ii) the set $D'$ contains all the analysis-states from $D$, with required modifications in case if the input change-sequence was compressed.

Recall that the key intuition behind compression is as follows: If no analysis-state in the compiler has a change-index equal to some index in the change-sequence, then the element at that index in the change-sequence can be safely merged (using the $\oplus$ operator) to its successor (if any) in the change-sequence. Furthermore, if no analysis-state in the compiler has a change-index less than zero, then the first element (at index 0) of change-sequence can be safely removed. Following are the cases that may arise when performing compression of the input change-sequence one element at a time:

- When the change-sequence $\vec{c}$ is empty, it is already in its compressed form. Hence, as per rule [CS-BASE], $D$ and $\vec{c}$ are returned without any changes.
- Similarly, if corresponding to each element in the change-sequence (except, optionally, the last) if there exists at least one analysis-state that has its change-index same as the index of that element, and if there exists at least one analysis-state that has its change-index as $-1$, then the change-sequence is already in its compressed form ([CS-COMPRESSED]).
- Otherwise, if no analysis-state has a change-index of $-1$, then we purge the first element from the change-sequence, and update all the analysis-states by decrementing their change-index by one (rule [CS-DELFIRST]).
- Otherwise, the element at the least index number that is not present as the change-index of any analysis-state is merged to its successor element (if any) in the change-sequence.
Fig. 15. Definition for the function \( \text{compress} : \mathcal{P}(\mathcal{D}) \times C^* \rightarrow \mathcal{P}(\mathcal{D}) \times C^* \).

Further, the change-index of all those analysis-states whose change-index is greater than the compressed index number, is decremented by one (rule [CS-MergeMid]). Note that no action is performed during compression when only the last element in the change-index is not indexed to by any of the analysis-states; this case falls under the rule [CS-Compressed], once the fixed-point application of the \( \text{compress} \) is complete. Further note that for efficiency purposes, in practice, in a change-sequence, all those \( k \) consecutive elements that are not indexed by any change-index are compressed together and change-indices of the affected analysis-instances are decremented by \( k \), in one go.

In Homeostasis, the \( \text{compress} \) function can be called during any compilation point, such as, immediately after a stabilization trigger, after an elementary transformation, and so on. Regardless of the number and places of invocations for this function, the following lemma holds.

**Lemma 4.13.** Consider a valid compiler state, say \( S = (\mathcal{P}, \mathcal{D}, \overline{c}) \), and another state obtained after a single application of the \( \text{compress} \) function, say \( S' = (\mathcal{P}, \mathcal{D}', \overline{c}') \), such that \( \text{compress}((\mathcal{D}, \overline{c})) = (\mathcal{D}', \overline{c}') \). Assume, \( \overline{c} = \{c_0, c_1, \ldots, c_{|\overline{c}|-1}\} \), and \( \overline{c}' = \{c_0', c_1', \ldots, c'_{|\overline{c}|-1}\} \). For each analysis-state in LZUPD mode, say \( d = (v, s, \text{LZUPD}, r) \in \mathcal{D} \), and the corresponding modified analysis-state, say \( d' = (v, s, \text{LZUPD}, r') \in \mathcal{D}' \), the following equality holds.

\[
\sum_{i=1}^{k} c_r \oplus c_{r+1} + \cdots + c_{|c|-1} = c'_{r+1} \oplus c'_{r+2} + \cdots + c'_{|c'|-1}.
\]  

**Proof.** Let \( k \) be the smallest integer in the set \( \{-1, 0, 1, \ldots, |\overline{c}|-1\} \) such that there does not exist any analysis-state in \( \mathcal{D} \) whose change-index is same as \( k \). That is, \( \nexists d \in \mathcal{D}, d = (\ast, \ast, \ast, i) \). Following three cases arise:
**Case I:** No such $k$ exists. This case refers to the fixed-point state for the compress function, as described by Rules [CS-BASE] and [CS-COMPRESSED]. As per these rules, note that $\overline{c'} = \overline{c}$, and $D' = D$. Hence, Equation (1) trivially holds.

**Case II:** $k = -1$. Following two sub-cases arise based on the size of $\overline{c}$.

Case II.a.: $|\overline{c}| = 0$. In this case, Rule [CS-BASE] is applicable. Since $\overline{c'} = \overline{c}$, and $D' = D$, Equation (1) trivially holds.

Case II.b.: $|\overline{c}| \geq 1$. In this case, Rule [CS-DELFIRST] is applicable. As per this rule, $|\overline{c'}| = |\overline{c}| - 1$,

$$r' = r - 1 \quad \text{and} \quad \frac{|\overline{c'}| - 1}{i=0} c'_i = c_{i+1}$$

Under these equalities we infer that, (i) the number of terms on the LHS and RHS of Equation (1) is same, and (ii) each term on the LHS is same as the corresponding term on the RHS. Hence, Equation (1) holds.

**Case III:** $k \geq 0$. When $k = |\overline{c}| - 1$, Rule [CS-COMPRESSED] is applicable. As before, Equation (1) will hold in that case. Otherwise, when $0 \leq k \neq |\overline{c}| - 1$, Rule [CS-MERGE MID] is applicable. In this case, $|\overline{c'}| = |\overline{c}| - 1$. Further, as per this rule, the following holds:

$$\forall_{i=0}^{k-1}, c'_i = c_i \quad \text{and} \quad \frac{|\overline{c'}| - 1}{i=k+1} c'_i = c_{i+1}$$

The following two sub-cases arise based on the different values of $r$:

Case III.a. $r < k$. As per Rule [CS-MERGE MID], $r' = r$. In this case, the number of elements on the LHS of Equation (1) is one more than the number of elements of its RHS. Clearly, $c_k$ and $c_{k+1}$ are present in the LHS, whereas in the RHS, $c_k$ and $c_{k+1}$ have been replaced with another element $c'_k$. Using Equation (2), we derive that all terms on the left of $c_k$ are same as the corresponding terms on the left of $c'_k$. Similarly, all terms on the right of $c_k$ are same as the corresponding terms on the right of $c'_k$. Additionally, since $c'_k = c_k \oplus c_{k+1}$, we infer that Equation (1) holds.

Case III.b. $r > k$. As per Rule [CS-MERGE MID], $r' = r - 1$. In this case, the number of elements on the LHS of Equation (1) is same as the number of elements of its RHS. Clearly, $c_k$ does not appear in the LHS. As per Equation (2), each term on the LHS is same as the corresponding term on the RHS. Hence Equation (1) holds.

**Corollary 4.14.** Consider a valid compiler state, say $S = (P, D, \overline{c})$. If the fixed-point application of the compress function on the input $(D, \overline{c})$ is $(D', \overline{c'})$, that is, $\text{compress}((D, \overline{c}))^* = (D', \overline{c'})$, then the compiler state $S' = (P, D', \overline{c'})$ is valid.

**Proof.** The proof follows directly from Definition 4.9 and Lemma 4.13.

Note that as a direct implication of Corollary 4.14, Lemma 4.10, and Lemma 4.11, the correctness guarantee of Homeostasis, stated in Theorem 4.12, will hold regardless of the number of compilation points where the compress function is invoked by Homeostasis.

### 5 DISCUSSION

We now present some salient characteristics of Homeostasis, followed by an account of how we estimate the amount of stabilization-effort required in the absence of Homeostasis. Then, we briefly discuss a generic incremental iterative data-flow analysis pass, which we have implemented and instantiated in Homeostasis to aid our evaluation.
5.1 Salient Characteristics of Homeostasis

Merging program changes across transformations. To stabilize a program-abstraction in update (UPD) mode, the handleUpdate method of the corresponding analysis requires net changes performed on the program (in terms of added and removed nodes/edges) since the last stabilization of that program-abstraction. A simple union of all such changes performed across multiple transformations, would not suffice. For instance, if a program node \( n \) (or edge \( e \)), is added by a transformation, and then deleted by another transformation before the stabilization gets triggered, the node \( n \) (or edge \( e \)) should not be considered as an added/removed node (or edge). In Homeostasis, BasePA internally merges the changes saved across all transformations to provide the relevant information when requested. In Section 5.5, we give an example of how the provided information is used in the handleUpdate method of a specific analysis.

Resolving pass-dependencies. Homeostasis automatically resolves the pass-dependencies of all compiler passes on program analysis passes by internally stabilizing the program-abstractions in the topological order of their dependencies. This is achieved through the design of getters and stabilizers in Homeostasis (see Figure 7). For example, the getter method of an UNSTABLE analysis, say \( A \), does not return until its stabilizer has been run. If analysis \( A \) is dependent upon some other analysis \( B \) (that is, if the computation of the program-abstraction of \( A \) requires the program-abstraction of \( B \)), then the compute or handleUpdate methods of \( A \) invoked from the stabilizer of \( A \) would, in turn, invoke the getter of \( B \). This will ensure that the stabilizer of \( B \) is run before the completion of \( A \), regardless of the order in which the stabilizations of both analyses were triggered.

5.2 Using Homeostasis in Compilers with Multi-Level IRs

A majority of the real-world compilers employ multiple levels of IR, and invoke a host of IR-level-specific analyses and optimizations on the program at each IR level. For such compilers, we can easily see that Homeostasis can be used for stabilizing the program-abstractions of the analyses within each such IR level, in response to the optimizations performed at that level. During compilation when the program is lowered from a higher-level IR (HIR) to a lower-level IR (LIR), (i) the program-abstractions of HIR are no longer relevant for the compiler passes of LIR (and hence need not be stabilized), and (ii) all the necessary program-abstractions for LIR are computed on the current state of the program, when needed. Thus, program-abstractions need not be stabilized across different levels of IR. Consequently, compilers supporting multi-level IRs can realize self-stabilization by using Homeostasis at each level of the IR independently.

5.3 Using Homeostasis in Non-Object-Oriented Compilers

While this article presents the design of Homeostasis in the context of object-oriented compilers, we believe that the proposed design can be adapted to allow self-stabilization in compilers that are written even in procedural languages. For example, in languages like C, the information about each analysis pass can be represented as a structure containing six members: (i) a program-abstraction of type "void*", (ii) an enum field stabilizationMode, (iii) an integer field chIndex, (iv) a function pointer named compute pointing to the function that populates the corresponding program-abstraction, and (v) a function pointer named handleUpdate pointing to the function that incrementally stabilizes the corresponding program-abstraction, (vi) a function pointer named get pointing to a method that returns a stable program-abstraction (by invoking the corresponding compute or handleUpdate functions, as needed). The first five members correspond to the instance fields and methods of the class BasePA, and the last member corresponds to the get method shown in Figure 7. All instances of this six-member structure are maintained in a global
list. We have to identify the set of elementary transformations and modify them to conform to the code is shown in Figure 5.

Since procedural languages do not support the Observer pattern naturally, we would need that the compiler writer follows a disciplined approach in modifying the IR, and accessing the program-abstractions. To use Homeostasis in compilers written in such a language, (i) the compiler writer must perform all IR modifications (directly/indirectly) only via the fixed set of elementary transformations, (ii) perform the initialization of the analysis instance via a generic method (akin to the constructor of BasePA, Figure 7(a)), and (iii) access the program-abstraction of an analysis, only via the invocation of its get function. We believe that a similar exercise can be carried out for compilers written in functional programming languages. We leave it as a future work to actually instantiate Homeostasis in such non-OO compilers.

5.4 Estimating Manual Stabilization Effort in the Absence of Homeostasis

To contrast the savings in effort due to the self-stabilization scheme of Homeostasis, we now present a scheme to estimate the effort required for manual stabilization in the absence of Homeostasis.

**Critical program-abstractions, and change-points.** Note that in order to perform manual stabilization in the context of an optimization $O$, the pass writer needs to inspect the following two parameters in relation to questions $Q_1$ and $Q_2$ (see Figure 2): (i) critical program-abstractions: those program-abstractions which may be rendered stale by $O$, and may be read later by an existing or future optimizing pass (and hence may need to be stabilized); we use $S_a$ to denote the set of critical program-abstractions, and (ii) change-points: those program points in the code of the optimization $O$ which may directly or indirectly trigger an elementary transformation (and hence may necessitate stabilization); we use $S_p$ to denote the set of change-points. We demonstrate these parameters using an example.

### Example 5.1

Figure 16 shows a snippet of a concrete optimization pass that performs loop unrolling in the IMOP compiler framework. We have added the calls to the dumpPointsTo method to simply print the points-to information corresponding to the specified node, symbolising the clients that may need points-to information, before and after unrolling. Method setBody is an elementary transformation method that replaces the current body of the receiver while-statement with the provided body. Method removeExtraScopes is used to remove unnecessary wrapping of statements within blocks (for example, $\{S\} \rightarrow \{S\}$). For this snippet, $S_p = \{L2, L3\}$, and $S_a$ is the set of those program-abstractions that may be impacted by the statements in $S_p$; for example, CFG, call-graph, use-def chains, and so on. Note that there may be other change-points within the implementation of the common utility removeExtraScopes; we do not consider them here as they are not present in the code written as a part of this pass.

**Relevant change-Points (RP).** An inexperienced programmer may perform manual stabilization naively by re-computing each of the program-abstractions (or a likely superset of $S_a$, for correctness), after each change-point in $S_p$ – a highly inefficient scheme, both in terms of its effect on...
performance, and the number of program points where the stabilization code needs to be invoked. An experienced programmer, on the other hand, is more likely to insert stabilization code only at a subset of change-points present in the code of the optimization pass. This reduction stems from two key insights: (i) Stabilization is required only after the last change-point in a series of transformations, after which one or more critical program-abstractions may be read. (ii) Furthermore, a program-abstraction need not be stabilized at such a last change-point, if the net program-changes at that change-point is guaranteed to not alter the existing values of the program-abstraction. For example, consider the addition/deletion of a node for an assignment statement (of the form $x = y$). If the variable $x$ is a pointer-type variable, then such an addition/deletion does not change the points-to map of the variable $x$, if both $x$ and $y$ point to the same set of ‘may points-to’ locations, even in the absence of this statement. Similarly, if the variable $x$ is of integer type, then the addition/deletion of such a node will not impact the points-to information of any variable (if the expert can assert that the value of the variable $x$ is not used as an offset for any pointer dereference).

The second key insight leads to cases where even if the program-abstraction is marked as UNSTABLE, in reality no stabilization is required. Considering the challenges in obtaining an expert-based study in a large compiler framework, and the difficulty in automatically identifying the cases related to the second key insight, for the purpose of our evaluation, we approximate the set of expert-marked change-points by the set of relevant change-points that is based on the first key insight. A relevant change-point is a program point in the optimization pass that corresponds to the last change-point in a series of transformations, after which one or more critical program-abstractions may be read; hence, one or more program-abstractions may require manual stabilization at a relevant change-point. For example, in Figure 16, the set of relevant change-points, from among the change-points \{L2, L3\}, is a singleton set \{L3\} – L3 is the last change-point in the series of transformations (L2;L3) after which a program-abstraction, the points-to map, will be read (at L4).

**Modes of manual stabilization.** Besides the lazy modes of stabilization preferred by *Homeostasis*, a few other modes of stabilization are easily conceivable. For example, the stabilization of all program-abstractions can be triggered during each elementary transformation of the program eagerly (see Section 3.1.4). Like the two modes of lazy stabilization, this eager scheme leads to two modes of stabilization: eager-invalidate (EGINV) and (EGUPD). An efficient alternative to the eager modes of stabilization is to invoke stabilization at only the set of relevant change-points. Like before, two modes of stabilization are possible—RPINV and RPUPD, corresponding to the invalidate and incremental update options, respectively.

These stabilization modes are very similar to the custom codes manually written by the compiler pass writers in conventional compilers: (i) UPD modes in the presence of incremental update, whereas INV modes otherwise, and (ii) EG-modes during naïve (and inefficient) but easy manual stabilization, whereas RP-modes during relatively efficient stabilizations performed by an experienced compiler writer. For the purpose of evaluation (see Section 7), along with the two lazy-modes of self-stabilization advocated by *Homeostasis*, we have implemented these four modes of stabilization (EGINV, EGUPD, RPINV, and RPUPD) to approximate different modes of manual stabilization. Figure 17 summarizes all the implemented modes of stabilization.

### 5.5 Implementing Iterative Data-Flow Analyses in *Homeostasis*

To conveniently implement multiple analyses that can use LZUPD mode of stabilization, we implemented a generic pass of an analysis that can be used to implement any incremental, inter-thread, flow-sensitive, IDFA for OpenMP parallel programs. We term this generic analysis as HIDFA and implemented it as a class that extends BasePA.
| Stabilization triggers eagerly at each elementary transformation | Full recomputation of the analysis from scratch | Incremental update of the program-abstraction using the stored changes to the program |
|---------------------------------------------------------------|-----------------------------------------------|--------------------------------------------------------------------------------|
|                                                               | EGINV                                         | EGUPD                                                                         |
| Stabilization triggers at relevant change-points in the optimization pass | RPINV                                         | RPUPD                                                                         |
| Stabilization triggers lazily upon an attempt to read from the stale program-abstractions | LZINV                                         | LZUPD                                                                         |

Fig. 17. Summary of various modes of stabilization used in the evaluation of our implementation of *Homeostasis* in IMOP.

```plaintext
1 Function handleUpdate()
2    | Set seeds = an empty set.;
3    | IRChanges = getNetChanges(this.chIndex);
4    | foreach e in netIRChanges.removedEdges do Add the destination node of the removed edge e to seeds;
5    | foreach n in netIRChanges.removedNodes do Add the (old) successors of the removed node n to seeds;
6    | foreach e in netIRChanges.addedNodes do Add the added node n itself, as well as its successors to seeds;
7    | foreach e in netIRChanges.addedEdges do Add the destination node of the added edge e to seeds;
8    | incrementalIDFA(seeds);
```

Fig. 18. Definition of the handleUpdate function for forward iterative data-flow analysis.

Figure 18 shows the steps used by the handleUpdate method of the HIDFA class in the context of forward data-flow analyses; the steps in the context of backward analysis are similarly derived (not shown). To realize self-stabilization, it populates a set (seeds) of nodes, starting which the flow maps may need an update as a result of program transformations. These seed nodes are passed to the `incrementalIDFA` method for performing the stabilization (Line 8). The implementation of `incrementalIDFA` is inspired from the work by Marlowe and Ryder [1989] and Ryder et al. [1988], and is a simple extension of the two-phase incremental update algorithms for iterative versions of data-flow analysis given by Pollock and Soffa [1989], adapted to handle the parallel semantics of the OpenMP parallel programs.

For completeness, we now give brief details of our implementation of `incrementalIDFA`. This method starts with the reconstruction of the SCC Decomposition Graph (SDG) of the updated CFG of the program. Each SCC-node in the SDG that contains any of the seed nodes is marked for processing. All the marked SCC-nodes are processed one-by-one, as per their topological-sort order in the SDG. Within each SCC-node, the processing continues using a worklist-based approach in two-phases: (i) exaggerate phase: in this phase, the flow-maps of various program-nodes in the SCC-node are initialized to an under-approximated value (such as $\top$), starting which the precise flow-map can be eventually obtained, and (ii) adjust phase: in this phase, the program-nodes are processed until fixed-point, using the data-flow equations similar to the exhaustive iterative data-flow algorithm. At the end of the second phase, the flow-maps of all program-nodes within the SCC-node correspond to the maximum fixed-point (MFP) solution. During the processing of an
SCC-node, if it is found that the program-nodes of any successor SCC-nodes need to be added to the worklist, then such successor SCC-nodes are marked for processing. This method continues till there are no more marked SCC-nodes left for processing. We refer the reader to the work by Pollock and Soffa [1989] for more details on the underlying two-phase incremental update algorithm.

6 Instantiation of Homeostasis

In order to assess the feasibility and generality of Homeostasis, we have retrofitted Homeostasis to a research compiler, and have implemented/adapted a number of analysis passes and optimization passes in the compiler, to conform to the design of Homeostasis. In this section, we discuss the relevant instantiation details.

6.1 Retrofitting Homeostasis to a Real-World Compiler

The design of Homeostasis is applicable to all the object-oriented compilers. Retrofitting Homeostasis in mainstream real-world compilers, like LLVM, OpenJ9, IMOP, and so on, will require rewriting all the existing program transformations using the identified fixed set of elementary transformations, and modifying all the existing analysis passes to conform to the structure prescribed by Homeostasis (see Figure 11). We have implemented our prototype in IMOP. We believe that a similar exercise can be undertaken for other object-oriented compiler frameworks as well. To further strengthen this belief, in Appendix B, we briefly discuss the guidelines on how the LLVM compiler framework can be extended with Homeostasis. The one-time effort required to retrofit Homeostasis to IMOP is discussed next.

Identifying elementary transformations. The IMOP IR comprises two kinds of nodes—leaf nodes and non-leaf nodes. All OpenMP or C constructs with “body”, such as while-loop, if-statement, and OpenMP parallel-region, are represented as non-leaf nodes. Similarly, nodes such as simple statements of C, and OpenMP directives such as barriers and flushes, are considered as leaf nodes. Each non-leaf node defines a nested flow of control, using edges among its components, which can themselves be non-leaf nodes. We identified the pre-existing fundamental transformations in IMOP that are used to add, replace, or delete various components of a non-leaf node, as the set of elementary transformations. In total, we identified and modified 47 elementary transformations spread across 17 non-leaf nodes to make them conform to the design shown in Figure 5.

We observe that the modification of these elementary transformations did not necessitate any changes at their call-sites. From Figure 5, note that Step B, which corresponds to the pre-existing code of an elementary transformation (in the absence of Homeostasis) does not undergo any changes while retrofitting the compiler with Homeostasis – the IR transformations are performed as before. Steps A, C, and D, interact only with stabilization-specific data structures to capture the program-changes resulting from Step B; they do not alter the meaning of the elementary transformation. Consequently, the compiler-pass writers can continue to use the elementary transformation as before, without having to consider their impact on self-stabilization.

Modifying higher-level transformation APIs. In order to allow for easier expression of transformation passes, IMOP provides four basic CFG transformations: (i) insertion of a successor node, (ii) insertion of a predecessor node, (iii) insertion of a node on an edge, and (iv) removal of a node. To retrofit Homeostasis to IMOP, we have modified the implementation of all these four transformations such that they express all IR changes directly or indirectly in terms of the identified set of elementary transformations. IMOP provides many higher-level transformation APIs such as duplicating a block of statements, renaming of free variables, and so on. All these transformation APIs employ elementary transformations, the above-mentioned CFG transformations, or other higher-level transformations to express any changes to the IR. Since all the transformations APIs...
Fig. 19. List of program-abstractions corresponding to key analysis passes in IMOP that were made conforming to Homeostasis. The bracketed text in the first column, gives the name of the IMOP class modified. Classes annotated with ∗ are the analyses that are implemented as subclasses of HIDFA in IMOP.

deployed in IMOP directly or indirectly express all the program changes via elementary transformations, the implementation of none of the existing optimization passes in IMOP required any specific modifications to adapt them to use Homeostasis.

Creating/identifying the super-class BasePA. IMOP already contains a class named BasePA, which serves as the super-class of all the analysis passes. We modified BasePA as per Figure 7 to conform to the design of Homeostasis. This mainly involved (i) modifying the constructor as shown in Figure 7(a), (ii) adding the stabilize method from Figure 7(c), (iii) adding an abstract method compute to be implemented by each concrete subclass of BasePA, and (iv) adding a dummy method for handleUpdate to be overridden by each concrete subclass of BasePA that seeks to employ LZUPD stabilization-mode. Further, to allow efficient maintenance of the centralized list of program-changes, as detailed in Figure 15, we added the appropriate data structures and methods.

6.2 Adapting Analysis Passes to Use Homeostasis

In order to assess the applicability of Homeostasis to various kinds of program-abstractions, we have (i) extended existing analysis passes of IMOP to conform to the design of Homeostasis, and (ii) implemented HIDFA and its various instantiations in IMOP.

Figure 19 provides a brief description of the program-abstractions for some of the key analysis passes in IMOP that now use Homeostasis. In particular, we have implemented a set of six standard flow-sensitive context-insensitive inter-thread iterative data-flow analyses as subclasses of the HIDFA class: (i) points-to analysis, (ii) reaching-definitions analysis, (iii) liveness analysis (a backward IDFA), (iv) copy propagation analysis, (v) lockset analysis, and (vi) dominance analysis.
### Optimization Passes in the Context of Homeostasis

Recall that in a Homeostasis-enabled compiler framework, the optimization-pass writers can efficiently design and implement new optimizations without having to write any stabilization-specific code (see Figure 11). Figure 20 lists some key optimization passes (including existing, as well as new ones implemented by us) in IMOP; none of them required any stabilization-specific code. Two common characteristics of these passes are: (i) Each of them expresses the required program

| Optimization Pass                                             | (Relevant class/method in IMOP)                                                                 | Description                                                                 |
|---------------------------------------------------------------|-----------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------|
| 1. Redundant barrier remover†                                 | (RedundantSynchronizationRemoval)                                                              | removes those barriers that do not preserve any inter-thread dependences across them |
| 2. OmpPar expander†                                           | (ParallelConstructExpander.expandParRegion)                                                   | expands the scope of parallel-regions upwards and downwards                 |
| 3. OmpPar merger†                                             | (ParallelConstructExpander.mergeParRegions)                                                   | merges two consecutive parallel-regions, if safe                            |
| 4. OmpPar-loop interchange†                                    | (ParallelConstructExpander.interchangeUp)                                                     | interchanges a parallel-region with its enclosing loop, if safe             |
| 5. OmpPar unswitching†                                         | (ParallelConstructExpander.interchangeUp)                                                     | interchanges a parallel-region with its enclosing if-statement, if safe      |
| 6. Variable privatization†                                     | (ParallelConstructExpander.expandUpward)                                                      | privatizes OpenMP shared variables, if safe                                 |
| 7. Function inliner†                                           | (FunctionInliner)                                                                              | selectively inlines those monomorphic calls that contain at least one barrier |
| 8. Scope remover†                                              | (CompoundStatementNormalizer)                                                                 | removes redundant encapsulations of compound-statements within the given node |
| 9. Unused-elements remover†                                    | (NodeInfo::removeUnusedElements)                                                               | removes unused functions, types, typedefs, and symbol declarations           |
| 10. Expression simplification (ExpressionSimplifier)           |                                                                                               | simplifies complex C expressions as per IMOP’s normalization rules           |
| 11. OmpConstruct simplification (ExpressionSimplifier)         |                                                                                               | simplifies combined OpenMP constructs as per IMOP’s normalization rules      |
| 12. Loop unroller (IterationStatementInfo::unrollLoop)         |                                                                                               | unrolls a serial loop                                                       |
| 13. Inter-phase code percolator (BarrierDirectiveInfo::percolateCodeUpwards) |                                                                                               | moves instructions across an OpenMP barrier, if safe                       |
| 14. Copy eliminator (CopyElimination)                          |                                                                                               | removes redundant variables, relying on copy-propagation analysis            |
| 15. Loop barrier extractor (LoopInstRescheduler::peelFirstBarrier) |                                                                                               | peels out a barrier from within a serial loop, if safe                      |

Fig. 20. List of key optimization passes inspected in IMOP; none of these passes required any stabilization-specific code in the context of Homeostasis. The bracketed text in the first column, gives the name of the IMOP class modified. Passes annotated with a † indicate that they belong to, or are used by, the BarrElim set of optimization passes.

None of these IDFA passes required any stabilization-specific code in order to support LZUPD stabilization-mode. For their super-class HIDFA, as well as for other analyses listed in the figure, we had to (1) modify their corresponding getter methods, as per the design from Figure 7, (2) ensure that the code to generate the program-abstraction from scratch is invoked from the overridden method compute, and (3) wherever applicable, ensure that the code to perform an incremental update of the program-abstraction is invoked from the overridden method handleUpdate.

### 6.3 Optimization Passes in the Context of Homeostasis

Recall that in a Homeostasis-enabled compiler framework, the optimization-pass writers can efficiently design and implement new optimizations without having to write any stabilization-specific code (see Figure 11). Figure 20 lists some key optimization passes (including existing, as well as new ones implemented by us) in IMOP; none of them required any stabilization-specific code. Two common characteristics of these passes are: (i) Each of them expresses the required program
transformations using either the elementary transformations and/or other transformation APIs provided by IMOP. (ii) Each of them uses/impacts one or more Homeostasis-enabled program-abstractions described in Figure 19. Now, we briefly describe a subset of these optimization passes (that we implemented for evaluating Homeostasis), which we collectively term as BarrElim.

**BarrElim: a set of optimization passes to aid barrier elimination.** In order to develop a real-world client for evaluating Homeostasis, we have implemented a set of three optimization passes that aim to reduce redundant barriers in OpenMP C programs: redundant-barrier-remover, parallel-construct-expander, and selective-function-inliner. The parallel-construct-expander in turn uses five pre-existing optimizations: (i) privatisation of shared variables, (ii) parallel-region scope expander, (iii) merging of consecutive parallel-regions, (iv) parallel-region and enclosing serial-loop interchange, and (v) parallel-region unswitching. Further, the selective-function-inliner uses two pre-existing cleanup-optimizations: extra-scope-remover, and unused-elements-remover. Collectively, we term the three implemented optimization passes as BarrElim.

The optimization passes in BarrElim extend prior work by Gupta and Schonberg [1996] and Tseng [1995] on parallel-region expansion and barrier removal with function inlining to realize an efficient barrier removal algorithm. These optimization passes perform the following steps, as shown in the block diagram in Figure 21: (1) Remove redundant barriers (within a parallel-region), whose removal do not violate any data dependence among the statements across them. The remaining two passes help improve the opportunities for barrier removal within each function. (2) Expand and merge the parallel-regions, while possibly expanding their scope to the call-sites of their enclosing functions, wherever possible. This helps in bringing more barriers (including the implicit ones) within the resulting parallel-region, thereby creating new opportunities for barrier removal. (3) Inline those monomorphic calls whose target function (i) is not recursive, and (ii) contains at least one barrier. These three optimization passes are repeated until fixed-point (no change).

Like many similar optimizations [Aloor and Nandivada 2015; Barik et al. 2013; Gupta et al. 2017; Nandivada et al. 2013], the optimization passes in BarrElim involve multiple alternating phases of inspections and transformations, which in turn lead to a number of interleaved accesses (reads and writes) to various program-abstractions, such as phase information, points-to information, super-graph (involving CFGs, call-graphs, and inter-task edges), AST, and so on—this interaction is depicted in Figure 21 using the dotted edge.

We have found that BarrElim is an impactful set of optimization passes for OpenMP codes. For example, on the NPB benchmarks [Van der Wijngaart and Wong 2002], the BarrElim optimized code yielded up to 5% improvement in execution time; the input benchmarks, as well as the BarrElim optimized codes were compiled using the -O3 switch of gcc. Considering that the obtained gains are on top of the many optimizations enabled by the -O3 switch, it can be seen that the gains are significant. Consequently, from among the various optimization passes present in IMOP, we select the BarrElim set of optimization passes (involving nine optimization passes...
and numerous program-abstractions) to evaluate the ease-of-use and performance of Homeostasis (see Section 7).

7 IMPLEMENTATION AND EVALUATION

We have implemented all the key components of Homeostasis (see Figure 4, and Section 3.2) in the IMOP compiler framework [Nougrahiya and Nandivada 2019]. IMOP is a new open-source compiler framework for conveniently writing program analyses, source-to-source optimizations, and profiling tools for OpenMP C programs; it spans more than 170k lines of code (LOC) in Java. IMOP has been used successfully in various published works (such as Viswakaran Sreelatha and Balachandran [2016], Viswakaran Sreelatha et al. [2018], Viswakaran Sreelatha and Nasre [2018], and Krishnakumar et al. [2019]), and is under active development. Our implementation of Homeostasis in IMOP involved coding of \( \sim 4500 \) LOC for adding self-stabilization to the elementary-transformation methods, and \( \sim 2500 \) LOC for supporting self-stabilization for existing program-abstractions of IMOP.

We have also implemented HIDFA, our generic inter-thread IDFA pass with incremental update in Homeostasis (\( \sim 3300 \) LOC; discussed in Section 5.5). We instantiated HIDFA to realize the implementation of following six standard flow-sensitive context-insensitive inter-thread iterative data-flow analyses: (i) points-to analysis (\( \sim 870 \) LOC), (ii) reaching-definitions analysis (\( \sim 190 \) LOC), (iii) liveness analysis (\( \sim 140 \) LOC), (iv) copy-propagation analysis (\( \sim 200 \) LOC), (v) lock-set analysis (\( \sim 240 \) LOC), and (vi) dominance analysis (\( \sim 116 \) LOC). Further, in order to assess the usability of Homeostasis, we have implemented a set of optimization passes, collectively termed as BarrElim, for barrier removal (\( \sim 2500 \) LOC; see Section 6.3). As expected, in the set of optimization passes in BarrElim no stabilization-specific code was needed. This underscores the ease-of-use facilitated by the design of Homeostasis. We have made our implementation of Homeostasis in IMOP open-source and publicly available [Nougrahiya and Nandivada 2021].

7.1 Experimental Setup

We present our evaluation on a set of twenty-four real-world benchmark programs taken from four popular benchmark suites (listed in Figure 22): (i) all eight benchmark programs of NPB-OMP 3.0 suite [Van der Wijngaart and Wong 2002], (ii) quake, and art-m, the two (out of 3) OpenMP-C benchmark programs from SPEC OMP 2001 [Aslot et al. 2001] that can be handled by IMOP, (iii) all three OpenMP C benchmark programs – amgmk, clomp, and stream – from Sequoia benchmark suite [Seager 2008], and (iv) all the eleven benchmark programs from IMSuite benchmark suite [Gupta and Nandivada 2015]. Note that these comprise some of the largest standard open-source benchmark programs for OpenMP C. Since IMOP accepts only OpenMP C programs, we did not consider any other benchmarks from SPEC OMP 2001, or from Sequoia, as they contain a mix of C/C++/MPI code. For IS from NPB, the set of client optimization passes, BarrElim, could not find any opportunity for optimization; as no program transformation was performed by the pass, no stabilization of data-flow analyses was triggered in any mode of self-stabilization – hence, we omit IS from our discussion. In Figure 22, we list a few static characteristics of the benchmarks, such as the size of each selected benchmark, the number of parallel constructs, and the number of static barriers.

In order to study the impact of different hardware on the performance improvements obtained with Homeostasis, we used two multicore platforms to perform our empirical evaluation: (i) Nanda, a 64-thread (dual socket, 16 cores per socket, 2 threads per core) 2.3 GHz Intel Xeon Gold 5218 system with 64 GB of memory, running Ubuntu 22.04.1 LTS and Java HotSpot 64-Bit Server VM 14.0; and (ii) K2, a 64-thread (quad-socket, 8 cores per socket, 2 threads per core) 2.3 GHz AMD Abu Dhabi system with 512 GB of memory, running CentOS 6.4 and Java HotSpot 64-Bit Server VM...
Fig. 22. Benchmark characteristics. Abbreviations: \#LOC=number of lines of code, \#Node=number of executable nodes in the CFG, \#Edge=number of edges in the CFG, \#PC=number of static parallel constructs, and \#Barr=number of static barriers (implicit + explicit).

9.0. The multi-core aspect of these systems is relevant for the part of the evaluation that executes the generated OpenMP code. The OpenMP codes were compiled using the GCC 11.3.0 compiler. Taking inspiration from the insightful paper of Georges et al. [2007], we report the compilation- and execution-time numbers by taking a geometric mean over 30 runs. We present the evaluation in four directions: (i) Ease-of-use of Homeostasis (in Section 7.2), (ii) Performance evaluation of the proposed lazy modes of stabilization (in Section 7.3), (iii) Impact of using the compression optimization on the data-structures employed by Homeostasis to keep track of the program-changes (in Section 7.4), and (iv) Correctness of the lazy modes of stabilization (in Section 7.5).

7.2 Ease of Use: Self-Stabilization vs. Manual Stabilization

We now present an empirical study for assessing the impact of Homeostasis on writing different compiler passes, by comparing the coding effort required to realize self-stabilization in a Homeostasis-enabled compiler, against those required to perform manual stabilization (in the absence of Homeostasis). We perform this evaluation in the context of the various component optimization passes of BarrElim.

Based on the discussion in Section 5.4, we designed a simple scheme to estimate the additional coding effort that may be required to perform manual stabilization. We profiled the IMOP compiler

| 1 | Benchmark | 2 | #LOC | 3 | #Nodes | 4 | #Edges | 5 | #PC | 6 | #Barr |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | BT (NPB) | 2615 | 4748 | 5016 | 9 | 47 |
| 2 | CG (NPB) | 642 | 1403 | 1485 | 14 | 31 |
| 3 | EP (NPB) | 352 | 775 | 813 | 2 | 4 |
| 4 | FT (NPB) | 899 | 2033 | 2151 | 7 | 14 |
| 5 | IS (NPB) | 333 | 711 | 762 | 2 | 4 |
| 6 | LU (NPB) | 2355 | 4687 | 4974 | 8 | 35 |
| 7 | MG (NPB) | 1278 | 2784 | 2918 | 10 | 19 |
| 8 | SP (NPB) | 2543 | 5364 | 5744 | 7 | 72 |
| 9 | quake (SPEC) | 1489 | 3333 | 3491 | 11 | 22 |
| 10 | art-m (SPEC) | 1691 | 1710 | 1791 | 4 | 4 |
| 11 | amgmk (Sequoia) | 895 | 1867 | 1949 | 2 | 5 |
| 12 | clomp (Sequoia) | 1605 | 4162 | 4289 | 28 | 73 |
| 13 | stream (Sequoia) | 331 | 735 | 762 | 6 | 12 |
| 14 | bellman-ford (IMSuite) | 143 | 546 | 564 | 3 | 6 |
| 15 | bfs-dijkstra (IMSuite) | 104 | 295 | 305 | 2 | 4 |
| 16 | byzantine (IMSuite) | 135 | 444 | 467 | 3 | 6 |
| 17 | dominating-set (IMSuite) | 321 | 1223 | 1277 | 12 | 24 |
| 18 | kcommittee (IMSuite) | 220 | 889 | 925 | 6 | 12 |
| 19 | leader-elect-dp (IMSuite) | 122 | 442 | 460 | 2 | 4 |
| 20 | leader-elect-hs (IMSuite) | 184 | 528 | 553 | 3 | 6 |
| 21 | leader-elect-lcr (IMSuite) | 89 | 301 | 314 | 3 | 6 |
| 22 | mis (IMSuite) | 161 | 549 | 574 | 4 | 8 |
| 23 | mst (IMSuite) | 299 | 1226 | 1279 | 9 | 18 |
| 24 | vertex-coloring (IMSuite) | 172 | 609 | 636 | 3 | 6 |
Fig. 23. Stabilization-related information for the set of optimization passes constituting BarrElim, obtained upon profiling/inspecting the code.

| Component Pass of BarrElim | LOC | #CP |
|---------------------------|-----|-----|
| Parallel-construct expansion | 1675 | 66  |
| Function inlining          | 463  | 15  |
| Redundant-barrier deletion | 313  | 2   |
| Driver                    | 10   | 1   |
| **Total**                 | 2461 | 84  |

(a) Maximum number of change-points obtained within the component optimization passes of BarrElim upon running them on the benchmarks under study. Abbr.: LOC=number of lines of code; #CP=number of change-points.

| Program-Abs.       | Mode | #RP |
|--------------------|------|-----|
| Points-to graphs   | UPD  | 17  |
| Control-flow graphs| UPD  | 70  |
| Call graphs        | UPD  | 60  |
| Phase information  | INV  | 61  |
| Inter-task edges   | INV  | 31  |
| Symbol-/type-tables| UPD  | 37  |
| Label-lookups      | UPD  | 60  |

(b) Program-abstractions read by the BarrElim passes. Abbr.: Mode=stabilization-mode; #RP=number of relevant change-points in the BarrElim passes after which the abstraction was read from.

by instrumenting the implementations of the various optimization passes of BarrElim, as well as of various program analyses and elementary transformations. By running this profiled compiler on each benchmark program, we obtained (i) the set of change-points for the BarrElim passes, and (ii) the set of program-abstractions that may be impacted by the BarrElim passes (see Section 6.3). In this section, we use this data to estimate the manual coding effort that may be required to answer the key questions from Figure 2.

**Which program-abstractions to stabilize?** As discussed in Section 5.4, since it is difficult to obtain the exact set of critical program-abstractions (to be stabilized manually), we manually analyzed the code of various optimization passes of BarrElim and estimated that there are seven program-abstractions (listed in Figure 23(b)) that may be impacted by the BarrElim passes. Thus, in the case of manual-stabilization, on writing each of the BarrElim passes, the pass writer needs to identify these seven program-abstractions, from the plethora of available program-abstractions—a daunting task. Note that the BarrElim optimization passes may also impact other program-abstractions that may be added to the compiler in future; hence, for each newly added analysis-pass, the analysis-pass writer would have to manually assess whether the corresponding program-abstraction may be rendered stale due to the transformations performed by any of the BarrElim optimization passes (and, in fact, by any of the other optimization passes in the compiler).

In contrast, in a Homeostasis-enabled compiler, all these tasks are automated—the optimization-pass (or even analysis-pass) writer needs to put no effort into identifying the program-abstractions (existing or new) that may be impacted by an optimization pass.

**Where to invoke stabilization?** In Figure 23(a), we enumerate the number of change-points discovered in the major components of BarrElim. In the absence of Homeostasis, the pass writer would have to correctly identify these 84 change-points (i.e., on average, almost 1 for every 28 lines of code) across various optimization passes of BarrElim, and insert code for ensuring stabilization of the affected program-abstractions. At each change-point, the pass writer may need to handle stabilization of the impacted program-abstractions, irrespective of the chosen mode of stabilization. To identify a more aggressive baseline, we note that not all change-points (referred to in Figure 23(a)) may warrant stabilization, and a pass writer may need to invoke the stabilization code only at the relevant change-points (see Section 5.4), for only those set of abstractions that may be modified at that point.

Figure 23(b), column 4, lists the number of relevant change-points for each program-abstraction impacted by the optimization passes of BarrElim; this data too was obtained by profiling the IMOP.
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The figure shows that there are a significant number of places in the components of BarrElim where this stabilization code needs to be manually invoked, in the absence of Homeostasis. For example, CFG stabilization needs to be performed at 70 places, and call-graphs at 60 places – which can lead to cumbersome and error-prone code. Further, upon addition of any new program analysis to the compiler (or any modification to the existing analysis), the pass writer would have to revisit all the change-points of pre-existing optimizations (for example, 84 change-points across all optimization passes of BarrElim) to check if the change-point may have necessitated stabilization of the newly added/modified program-abstraction.

In contrast, in a Homeostasis-enabled compiler, all the above tasks are automated—the pass writer needs to spend no effort in identifying the places of stabilization, as she needs to add no additional code as part of the optimization in order to stabilize the program-abstractions.

How to stabilize? We use the same stabilization code for both manual stabilization and Homeostasis, and hence there is no difference between them, with respect to this key question.

Summary. In contrast to the traditional compilers, it is much easier to ensure stabilization of program-abstractions when writing optimizations or analyses in Homeostasis.

7.3 Performance Evaluation

We conduct the performance evaluation of the proposed lazy modes of stabilization, by studying the parameters related to stabilization time, total compilation time, and memory consumption, in the context of the prior discussed set of optimization passes, BarrElim. We do so by presenting a comparison to the RP-modes of stabilization, which correspond to manual stabilizations performed by experienced compiler-pass writers (see Section 5.4). In Figure 24, we present various parameters related to compilation of the benchmark programs under study, when compiled with the RPINV mode of stabilization; these numbers serve as the baseline for the evaluations discussed in this section.

We have also done an elaborate evaluation compared with the weaker baseline of the eager EG-modes of stabilization, which correspond to naïve (that is, easy but inefficient) manual stabilizations; the details can be found in Appendix A.

(A) Stabilization time. In Figure 24, columns 4 and 5 show the stabilization time for IDFA flow-maps in the context of RPINV mode of stabilization, while performing the set of optimization passes of BarrElim on the benchmark programs under study, for Nanda and K2, respectively. The zero (0) entries for the STB-times of IS are due to the fact that no optimization opportunities were found by the BarrElim passes for IS.

In Figure 25, we illustrate the impact of using LZINV, RPUPD, and LZUPD modes of stabilization, by showing their relative speedups with respect to RPINV, in terms of speedups in the IDFA stabilization-time. We exclude SP from this discussion on stabilization time, since there were no stabilization triggers for SP under lazy modes of stabilizations (that is, the stabilization time for lazy modes of stabilization was zero). As expected, the LZUPD mode incurs the least cost for stabilization among all the cases across both the platforms; consequently, it results in the maximum speedup with respect to RPINV – with speedups varying between 2.6× and 30.64× (geomean 8.84×) for Nanda; between 3.22× and 29.68× (geomean 9.58×) for K2.

We have noted that the gains in IDFA stabilization time using a particular mode of stabilization depend on multiple stabilization-mode-specific factors, such as (i) number of triggers of stabilization, (ii) number of times transfer-functions are applied on various program nodes during IDFA stabilization, (iii) cost incurred to process each program node per stabilization, and so on. For our baseline mode of stabilization, RPINV, we show the first two factors in columns 2 and 3 of Figure 24,
Table 1: Evaluation numbers for performing the BarrElim optimization passes on various benchmark programs, in the context of RPINV mode of stabilization. These numbers serve as the baseline for Section 7.3.

| Benchmark       | #Trig | #T-Func | STB-Time (s) | Total Time (s) | Memory (MB) | Ch-Size |
|-----------------|-------|---------|--------------|----------------|-------------|---------|
|                 |       |         | Nanda        | K2             | Nanda       | K2      | Nanda | K2 |
| 1. BT (NBP)     | 17    | 214327  | 3.62         | 5.93           | 8.29        | 14.25   | 2862.24 | 8550.41 | 15170 |
| 2. CG (NBP)     | 89    | 242019  | 2.14         | 3.46           | 3.65        | 6.11    | 1675.41 | 3850.55 | 115070 |
| 3. EP (NBP)     | 2     | 1983    | 0.04         | 0.07           | 0.56        | 1.17    | 421.32  | 1784.43 | 0    |
| 4. FT (NBP)     | 61    | 443820  | 4.42         | 7.16           | 7.81        | 13.03   | 2771.97 | 10060.87 | 49871 |
| 5. IS (NBP)     | 0     | 806     | 0            | 0              | 0.33        | 0.82    | 330.51  | 1430.90 | 0    |
| 6. LU (NBP)     | 33    | 507444  | 8.43         | 14.63          | 11.92       | 21.13   | 2856.21 | 8894.1 | 41361 |
| 7. MG (NBP)     | 230   | 2372204 | 24.95        | 58.17          | 34.47       | 74.12   | 2788.71 | 13969.44 | 571691 |
| 8. SP (NBP)     | 35    | 672958  | 8.31         | 14.36          | 11.66       | 20.43   | 2828.68 | 16217.09 | 38102 |
| 9. quake (SPEC)| 35    | 457217  | 6.74         | 10.44          | 8.92        | 14.29   | 3220.78 | 13348.05 | 16727 |
| 10. art-m (SPEC)| 5     | 88347   | 1.03         | 2.01           | 2.33        | 4.56    | 610.15  | 3050.15 | 134  |
| 11. amgmk (Sequioa)| 56  | 239940  | 3.2          | 6.54           | 6.15        | 11.36   | 2715.4  | 7760.55 | 52486 |
| 12. clomp (Sequioa)| 63 | 397078  | 6.76         | 11.56          | 13.72       | 23.19   | 2779.42 | 14921.1 | 146511 |
| 13. stream (Sequioa)| 45   | 51020   | 0.55         | 1.03           | 1.4         | 2.79    | 548.6   | 2154.01 | 36426 |
| 14. bellman-ford (IMS)| 23 | 15038   | 0.44         | 0.86           | 0.96        | 1.71    | 488.84  | 2008.73 | 6051 |
| 15. bfs-dijkstra (IMS)| 17 | 4695   | 0.13         | 0.29           | 0.73        | 1.49    | 480.23  | 1965.33 | 3237 |
| 16. byzantine (IMS)| 19 | 7979   | 0.19         | 0.32           | 0.59        | 1.25    | 405.9   | 1768.1 | 4563 |
| 17. dominating-set (IMS)| 75 | 186360  | 1.88         | 3.09           | 3.19        | 5.32    | 1255.84 | 4298.49 | 64687 |
| 18. kcommittee (IMS)| 43 | 44272   | 0.56         | 1.01           | 1.57        | 2.93    | 535.33  | 2147.7 | 30767 |
| 19. leader-elect-dp (IMS)| 5   | 2325    | 0.07         | 0.12           | 0.39        | 0.84    | 340.87  | 1407.41 | 282  |
| 20. leader-elect-hs (IMS)| 11 | 9978   | 0.18         | 0.35           | 0.84        | 1.67    | 500.83  | 1977.11 | 2624 |
| 21. leader-elect-lcr (IMS)| 6   | 1844    | 0.05         | 0.1            | 0.52        | 1.11    | 407.03  | 1698.05 | 402  |
| 22. mis (IMS)| 7     | 6033    | 0.13         | 0.24           | 0.51        | 1.08    | 380.34  | 1650.04 | 540 |
| 23. mst (IMS)| 53    | 217334  | 2            | 3.21           | 3.28        | 5.57    | 899.43  | 3184.65 | 48387 |
| 24. vertex-coloring (IMS)| 13 | 13370   | 0.26         | 0.46           | 0.91        | 1.82    | 504.2   | 2017.47 | 1954 |

Fig. 24. Evaluation numbers for performing the BarrElim optimization passes on various benchmark programs, in the context of RPINV mode of stabilization. These numbers serve as the baseline for Section 7.3. Abbreviations: #Trig = number of stabilization triggers, #T-Func = number of transfer-function applications, and Ch-Size = total size of the change-sequence across all stabilization triggers (as a sum of the number of nodes and twice the number of edges in each trigger). STB-Time and Total Time refer to the IDFA-stabilization time, and overall compilation time, respectively. Memory refers to the maximum resident set size of the compilation process when running the BarrElim optimization passes. Note that Ch-Size is calculated through a special run of the RPINV mode, where we force retention of the change-sequence, even though the mode does not require it.

respectively. We do not report the numbers for the third factor as it varies significantly based on the different types of statements in the benchmark, and hence is difficult to summarize per benchmark. In Figure 26, we show the number of stabilization triggers when using the lazy modes of stabilization normalized with respect to the RP-modes. Similarly, in Figure 27, for various modes of stabilization we show the number of transfer-function applications across all stabilization triggers normalized with respect to those numbers in the case of RPINV mode. We observe that for each benchmark, the speedup obtained across different modes of stabilization closely correlates to these numbers. Across different benchmarks, the relative impact of these factors may vary, depending upon, for instance, the fraction of time spent in applying transfer-function when processing a program node during IDFA stabilization. We now illustrate our observations by comparing the performance of different modes of stabilization.
Fig. 25. Speedup in IDFA stabilization-time under various modes of stabilization with respect to the RPINV mode, when applying the client optimization passes of BarrElim. Higher is better.

**LZUPD vs. RPINV.** The LZUPD mode consistently outperforms the RPINV mode across all benchmarks, for both the platforms, as shown in Figure 25. This can be attributed to the significant reductions in the number of transfer-function applications, as well as in the number of stabilization triggers, when using the LZUPD mode as compared to the RPINV mode, as shown
The maximum speedup in IDFA stabilization-time for LZUPD was observed in quake for Nanda (30.64×), and in MG for K2 (29.68×), consequent upon the fact that for quake and MG, compared to RPINV, LZUPD re-processes a significantly small fraction of the nodes (1.18% and 0.25%, respectively), over a reduced number of stabilization triggers (82.86% and 75.22%, respectively). In contrast, for bfs-dijkstra, LZUPD attains the least (though still quite significant) speedups of 2.6× in Nanda, and 3.22× in K2, as it results in reprocessing one of the highest fractions of nodes (9.03%), along with a higher count of stabilization triggers (76.47%), as compared to the RPINV mode, across all the benchmarks.

**LZUPD vs. RPUPD.** It is clear from Figure 25 that though the RPUPD mode consistently performs better than RPINV, and compared to LZUPD it performs either worse or similarly, across all the benchmarks.
benchmarks, for both the platforms. This is because, as shown in Figures 26 and 27, LZUPD results in significantly fewer stabilization triggers (geomean 36.52% lower) than the RPUPD mode, while also reprocessing considerably fewer nodes (geomean 8.41% lower).

**LZUPD vs. LZINV.** As shown in Figure 25, we see that in the context of IDFA stabilization-time, LZUPD performs better than LZINV for all the benchmarks (geomean 6.18× better for Nanda; geomean 6.51× better for K2). This observation can be attributed to the fact that the cost of invalidating and recomputing a program-abstraction (such as the results of any instantiation of HIDFA) is, in general, higher than the cost of incrementally updating the program-abstraction. This is evident from Figure 27, which shows that the LZUPD mode reprocesses only a small fraction of the program nodes reprocessed in the case of LZINV mode (geomean 91.19% fewer).

**LZINV vs. RPINV.** Across all the benchmarks, and both the platforms, we notice a performance improvement with LZINV mode, as compared to the RPINV mode, with geomean speedup as 1.43×, for Nanda, and 1.47×, for K2. The maximum speedup was observed in the case of stream (2.29× in Nanda, and 2.94× for K2), consequent upon the fact that among the benchmarks shown in Figure 25, stream corresponds to the largest reduction in the number of stabilization triggers (see Figure 26) with the lazy modes of stabilization. In contrast, clomp and mst correspond to some of the lowest reductions in number of stabilization triggers, thereby resulting in some of the lowest speedups with the LZINV mode.

**LZINV vs. RPUPD.** From Figure 25, note that the RPUPD mode consistently outperforms the LZINV mode in the context of IDFA-stabilization time, across all the benchmarks, for both the platforms (except for EP in K2, where the performance is the same). This trend can be explained as follows. From Figure 26, it is clear that the LZINV mode consistently results in fewer stabilization triggers than the RPUPD mode. However, it is also expected that the incremental update of IDFA flow-maps in UPD-modes will result in fewer applications of the transfer-functions per trigger, as compared to the same in the case of INV-modes which involve invalidation and full recomputation of the IDFA flow-maps. This is evident in Figure 26, where we notice that RPUPD mode consistently applies significantly fewer transfer-functions (geomean 90.38% fewer) as compared to the LZINV mode. As a result, RPUPD mode outperforms the LZINV mode. For the case of EP on K2, where we observe similar performance for both these modes, we believe that the performance gains expected due to 47.53% reduction in the number of transfer-function applications in case of RPUPD as compared with the LZINV mode (which is also the least of such reductions across all the benchmarks), are negated by the other overheads resulting from double the number of stabilization triggers in case of RPUPD as compared to that in LZINV.

**Summary.** Overall, we found that the LZUPD mode leads to the maximum benefits in stabilization time, across all the four modes of stabilization. Further, we also observed that if the UPD-mode is unavailable for a program-abstraction due to the absence of its incremental-update algorithm, the fully-automated stabilization provided by Homeostasis in the form of LZINV mode can still provide good performance improvements over the manual stabilization attained using the RPINV mode. These observations underline the performance benefits in stabilization time when using Homeostasis. This may in turn improve the overall compilation speed, as discussed next.

**(B) Total compilation time.** In Figure 24, columns 6 and 7 show the overall compilation time incurred in the context of RPINV mode of stabilization, for Nanda and K2, respectively. These numbers correspond to an end-to-end compilation that starts with parsing of the input program file, followed by the application of various default simplification/normalization passes employed by IMOP, and ends with the application of the Barr Elim set of optimization passes until fixed-point, before the final (optimized) program is written to the disk.
In Figure 28, we demonstrate the impact of using the lazy modes of stabilization, as compared to the RPINV mode of manual stabilization, in terms of speedup obtained in the total compilation time. Both LZINV and LZUPD perform consistently better than the baseline across all the benchmarks, with maximum and geomean speedups of: 5.58× and 1.25× for Nanda with LZINV; 5.06× and 1.23× for K2 with LZINV; 8.95× and 2.36× for Nanda with LZUPD; and 11.32× and 2.21× for K2 with LZUPD mode of stabilization. We have also observed that LZUPD is never slower than RPUPD mode of stabilization—we skip the plot for RPUPD and the detailed analysis for brevity.

We observe that the speedups obtained in total compilation time using different modes of stabilization, with respect to a baseline mode, depends on the following key factors: (i) fraction of the total compilation time spent in performing the stabilization using the baseline mode (see Figure 24: columns 4 and 6 for Nanda; columns 5 and 7 for K2); (ii) overall speedup obtained in the stabilization process (shown in Figure 25); and (iii) changes in memory footprint and available heap size for the VM across the compilation process, both of which may non-deterministically affect the GC overheads. We now illustrate these observations by comparing the relative performances of various modes of stabilization.

**LZUPD vs. RPINV.** In Figure 28, we observe that LZUPD consistently outperforms RPINV, as expected. The greatest speedups in total compilation time are obtained for MG (8.95× in Nanda, and 11.32× in K2), owing to the facts that MG has (i) one of the highest fractions of total compilation time spent in stabilization (72.38% in Nanda; 78.48% in K2; see Figure 24), and (ii) one of the highest speedups in stabilization-time (17.33× in Nanda; 29.68× in K2), across all the benchmarks.
benchmarks. In contrast, since EP corresponds to the least fraction of total compilation time spent in stabilization (7.14% in Nanda; 5.98% in K2), across all the benchmarks, as well as (comparatively) only moderate speedup in stabilization-time (8× in Nanda; 7× in K2), it obtains the least speedup in total compilation time (1.10× in Nanda; 1.09× in K2).

**LZINV vs. RPINV.** Across all the benchmarks, and for both the platforms, LZINV results in better total-compilation time than RPINV (geomean 2.36× in Nanda; 2.21× in K2). In Figure 26, note that the number of stabilization-triggers is reduced to zero in the case of SP, when using the lazy modes of stabilization; this results in SP attaining the highest gains in total compilation time with LZINV (5.58× in Nanda; 5.06× in K2), among all the benchmarks. In contrast, for similar reasons as in the case of LZUPD, EP corresponds to the least speedup in total compilation time when using LZINV, for both the platforms (1.04× in Nanda; 1.03× in K2).

**LZUPD vs. LZINV.** In Figure 28, LZUPD consistently performs better than LZINV (except for SP, where the performance difference is negligible), across both the platforms – maximum and geomean values are 6.98× and 1.88× in Nanda, respectively; 8.98× and 1.79× in K2, respectively. We attribute this observation to the fact that, as shown in Figure 27, the number of applications of the transfer-functions in the case of LZUPD is smaller than that with LZINV for all the benchmarks (except for SP, where the difference is zero); note that the number of stabilization triggers remain the same between both the modes. The maximum speedups in both the platforms are obtained for MG, consequent upon the fact that MG corresponds to the largest drop in the number of stabilization-triggers (138.72×, in Figure 27) from LZINV to LZUPD, across all the benchmarks.

An interesting observation from our study was that across both the lazy modes of stabilization, the actual benefits obtained in the total compilation time, with respect to the RPINV mode of stabilization, were far higher than the speedups expected in the total compilation time (based on the fraction of the total compilation time spent in the stabilization process, and the speedup within the stabilization process). For instance, in the case of MG in K2, when using the RPINV mode of stabilization (i) around 78% of the total compilation time was spent in performing the IDFA-stabilization (as shown in Figure 24), and (ii) this fraction of the time spent in IDFA-stabilization process benefitted from the LZUPD mode with an approximate speedup of 30× (shown in Figure 25) over the RPINV mode. This should result in a speedup of 4.14× (= 1/(1 – 0.78) + (0.78/30)) in the total compilation time. However, as shown in Figure 28, the actual speedup observed in MG for K2 was 11.32×! We believe that this behavior can be attributed to the latent benefits obtained in other parts of the compilation (that is, outside the stabilization process itself), owing to a significant reduction in the memory usage across most of the benchmarks, as discussed in part (C) of this section.

**Summary.** In conclusion, the lazy modes of stabilization used in *Homeostasis* may result in significant gains in the overall compilation time, as compared to the manual stabilization (RPINV mode). Furthermore, the UPD-mode consistently outperforms the INV-mode, between both the lazy modes of stabilization facilitated by *Homeostasis*. These gains in lazy modes are on top of the benefits obtained in terms of ease-of-use (see Section 7.2) due to the nearly-automated nature of *Homeostasis*, requiring minimum (in case of LZUPD) or zero (in case of LZINV) additional effort from the compiler developers.

**C) Memory consumption.** In Figure 24 (columns 8 and 9) we show the maximum memory footprint (in MB), in terms of the maximum resident set size, while running the BarrElim optimization passes in the context of RPINV mode, for Nanda and K2, respectively. The values shown are calculated with the help of `/usr/bin/time` GNU utility (version: 1.7). While this tool is quite effective in drawing a broad picture of the peak memory requirements of a process, there are two main limitations to using this tool. First, the resident set size is not measured continuously, but rather at some indeterminate intervals. This means that the tool might not calculate the actual

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peak memory usage of the process. Second, the maximum resident set size does not include the size of pages that have been swapped out, which may not accurately reflect the true memory requirements of the process. In addition, the non-deterministic nature of the garbage collector (GC) implemented by the Java Virtual Machine (JVM) can also affect the accuracy of these measurements. For example, a process with higher memory demands may result in the triggering of a full GC, in which the JVM is paused to clean up the garbage from all memory regions of the JVM heap. This can result in a much smaller heap size compared to a process with lower memory demands that does not trigger a full GC. Considering these sources of imprecision in such a measurement, we believe that very small improvements or deteriorations (< 5%) should be ignored.

In Figure 29, we illustrate the percentage savings in the memory footprint by LZINV, RPUPD, and LZUPD modes, as compared with the RPINV mode, for both Nanda and K2. All these three modes of stabilization perform better (or are more or less comparable), in terms of memory requirements, than the RPINV mode, except for the case of mst with LZINV in Nanda. The geometric improvements in memory consumption for LZINV, RPUPD, and LZUPD modes, as compared with the RPINV mode, are 10.67%, 34.29%, and 36.35%, respectively, for Nanda; 10.69%, 34.25%, and 35.97%, respectively, for K2.

One key factor that determines the impact of various modes of stabilization on the percentage reduction in memory footprint with respect to RPINV is the relative count of the number of times various transfer-functions were applied (see Figure 27). As discussed above, both lazy and update options minimize the number of times different transfer functions are applied during stabilization of the data-flow analyses. Consequently, LZUPD requires the least amount of memory (within the margin of error), with maximum percentage savings over the RPINV mode – 81.78% for quake in Nanda, and 85.8% for SP in K2. In SP, the lazy modes (LZINV and LZUPD) do not trigger any stabilization of the data-flow analyses (i.e., zero transfer functions are applied during stabilization), attributing to high savings in memory consumption – 78.41% and 78.45%, respectively, for Nanda; 85.96% and 85.80%, respectively, for K2. In contrast, since for both the UPD-modes (RPUPD and LZUPD), EP corresponds to the least reduction in the number of transfer-function applications as compared to the RPINV mode (see Figure 27), it witnesses some of the least savings in its memory footprint with the UPD-modes. For the case of mst with LZINV mode, we observe an anomalous behaviour, where the memory footprint reduces by 5.09% in K2, but increases by 21.05% in Nanda. Since all the steps involved in compilation remain the same across both the platforms, we believe that such behavior is due to the differences in the underlying architectures and operating systems, as well as in the JVMs and the GCs.

Summary. Overall, we see that the proposed lazy modes of stabilization lead to significant memory savings compared to the naive RPINV scheme. This in turn can improve the memory traffic and overall gains in performance.

7.4 Impact of Compression Optimization

In this section, we empirically study the memory requirements of the change-set, which represents the program changes that need to be maintained in order to allow UPD-modes of stabilization at a later stage during compilation. Furthermore, we also assess the efficacy of compression optimization employed by Homeostasis in order to keep the change-set compact.

Memory requirements of maintaining change-set. In Figure 22, columns 3 and 4 show the size of each benchmark program in terms of the number of program nodes and program edges, respectively. In order to obtain the memory requirements of maintaining the change-set throughout the compilation process, we calculate its size in terms of two parameters at each stabilization-trigger: (i) fraction of the program nodes that are present in the change-set, and (ii) fraction of
Fig. 29. Percentage savings in memory footprint (in terms of maximum resident set size) under various modes of self-stabilization, with respect to the RPINV mode, while running the client analysis. Higher is better.

the program edges that are present in the change-set. Note that the size of the program itself may differ across each stabilization trigger. In Figure 30, we show the average of these two parameters taken individually across all the stabilization triggers that occurred during the compilation. We observe that the memory requirements for maintaining the change-set are negligible in terms of the
Fig. 30. Size of the compressed change-set in terms of the program nodes and edges, averaged across various stabilization triggers, when applying the set of client optimization passes from BarrElim. Lower is better.

Impact of compression on change-set. In order to study the impact of compression optimization employed by Homeostasis in order to keep the change-set compact, we ran a set of experiments where we disabled the compression optimization altogether. For the ease of comparison, we consider the size of a change-set to be equal to the summation of (i) its number of program nodes, and (ii) twice the number of its program edges. In Figure 24, column 10 shows the sum of the size of the uncompressed change-set across all the stabilization triggers, when compilation was performed with compression-optimization disabled.

Recall that Homeostasis allows the compression routine to be invoked at any point of compilation, any number of times. For the purpose of our evaluation, we invoked the compression routine at the end of each stabilization trigger (a natural choice for performing compression, as the change-index gets updated there). The total number of stabilization triggers, and hence, the total number of invocations of the compression routine, for each benchmark program when applying the BarrElim set of optimization passes is shown in Column 2 of Figure 24. In Figure 31, we show the percentage reduction in the sum of the total size of the change-set across all the stabilization triggers, when we ran the experiments with compression-optimization enabled, as compared to the runs where the optimization was disabled. We observe that the overall reduction in memory requirements with the help of compression-optimization are significant – maximum and geomean values are 99.7% and 93.18%, respectively. The overall impact of the compression-optimization on the change-set depends on the exact transformations being performed by the client optimization pass on the program under compilation. For the case of art-m, we observe that the
compression-optimization yielded the least benefits (39.55%). This observation is attributed to the fact that the absolute size of the uncompressed change-set itself is quite small to begin with (only 134, which is the least among all the programs).

**Impact of compression on compilation time.** We also studied the impact of compression optimization on the compilation time, and found no observable difference resulting from the optimization.

**Summary.** In conclusion, we observe that (i) the compression-optimization is quite efficient at keeping the change-set compact, and as a result, (ii) the memory requirements of the change-set are negligible in terms of the program size under compilation, thereby making the UPD-modes feasible for even large programs which may undergo aggressive optimizations.

### 7.5 Empirical Correctness

In order to empirically validate the correctness of our design/implementation of HIDFA and its six instantiations (see Section 5), we have verified the generated flow-facts under each mode of stabilization, in the context of various optimization passes provided by IMOP [Nougrahiya and Nandivada 2019]. We found that the final flow-facts across all the stabilization-modes match.

Further, to empirically validate correct stabilization in the context of the BarrElim optimization passes, we have also verified that for each benchmark the generated optimized code (i) does not differ across the modes of self-stabilization, and (ii) produces the same execution output as that of the unoptimized code.

**Overall evaluation summary.** Our evaluation shows that (i) Homeostasis makes it easy to write optimizations and program analysis passes, (ii) the lazy stabilization choices lead to faster compilation times with lesser memory requirements, (iii) the proposed compression optimization employed by Homeostasis is effective and leads to negligible space requirements for keeping track of the program-changes, and (iv) our implementation leads to correct analysis and optimized code.

### 7.6 Threats to Validity

In this section, we discuss various external and internal threats to the validity of our evaluation results, and how we mitigate the same.

**Threats to external validity.** (1) The evaluation results obtained for any one client-optimization pass may not depict the nature of results for other optimization passes. To mitigate the impact of this threat to validity, we have performed the evaluation with a large set of optimization
passes – involving nine diverse optimization passes and numerous program-abstractions – which we collectively term as BarrElim (see Section 6.3). (2) The evaluation results on selected benchmark programs may not be generalizable to other kinds of input programs. To mitigate this issue, we have performed our evaluation on a set of 24 real-world programs from four popular benchmark suites (see Section 7.1). Some of these are among the largest open-source standard benchmark programs available in OpenMP C. For better coverage, the selected set also contains some medium-/small-sized standard programs. (3) The performance results obtained on one compiler framework may not be applicable to other compiler frameworks. In Section 7.3, we notice a strong correlation between the performance of a stabilization-mode (in terms of compilation time and memory requirement) and the number of times transfer-functions are applied when using that mode. Usage of a different underlying compiler framework is not expected to have any considerable impact on the number of transfer-function applications: this number depends on the incremental algorithm, the current program, and the change-set. Consequently, we expect similar relative-performance behavior across various compilers.

**Threats to internal validity. (4)** For any program-abstraction, the set of relevant change-points in an optimization pass may be an over-approximation of the program-points where an expert compiler writer would manually trigger stabilization (with no redundant stabilization operations). Thus, the RPINV stabilization-mode may not exactly represent an expert-written stabilization (see Section 5.4). Such a threat-to-validity is unavoidable, as it would require manual analysis of large unfamiliar code of the selected set of client optimization passes as well as the numerous program-abstractions that these passes may potentially impact – these could span many tens of thousands of lines of code, making it nearly infeasible for independent experts to carry out such an exercise, owing to their busy schedules. To investigate the impact of this threat-to-validity on our evaluation, we manually compared the set of relevant change-points obtained via profiling, and the set of change-points where we (the implementers of BarrElim passes) would have inserted stabilization triggers for manual stabilization. We found that these two sets matched. We have made the complete codebase for our client optimization passes and related program-abstractions as open-source [Nougrahiya and Nandivada 2021] for the purpose of cross-checking and reproducing the experiments. (5) The measurement of memory consumption can be unreliable due to the non-deterministic behaviour of the GC of Java VM. In order to mitigate the impact of GC, we report the numbers by taking a geometric mean over 30 runs of each experiment, taking inspiration from the findings of Georges et al. [2007].

8 RELATED WORK

We divide the related work into two different subsections: one on the efficient recomputation of programs under development, and another on incremental analyses.

8.1 Efficient Recompilation

When a program undergoes edits across its multiple versions, or during the process of its development in IDEs, the full recomputation of the modified program including re-computation of all the analyses and application of optimizations from scratch can be cost-prohibitive. Various approaches have been given to reuse different program-abstractions (including object code, and IR obtained before/after applying optimizations) to minimize the cost of recomputation. Smith et al. [1990] have developed mechanisms to perform incremental update of dependence information during interactive parallelization of Fortran programs. During the recomputation of programs, Pollock and Soffa [1992] incrementally incorporate the changes into globally optimized code in an attempt to reduce redundant analysis that is performed for the purpose of optimizations. For
enabling incremental symbolic executions, Person et al. [2011] have provided methods to detect and characterize the effects of program changes, using static analyses. Incrementalization of static analyses that are expressed using logic programming languages, such as Prolog and Datalog, is facilitated by Eichberg et al. [2007], Szabó et al. [2018], Szabó et al. [2021], and Garcia-Contreras et al. [2021], among others. Various approaches, such as those by Szabó et al. [2018, 2016], exist to enable incremental update of static analyses in response to program edits in the context of Integrated Development Environments (IDEs). Eichberg and Bockisch [2005] provide a constraint-solving based approach for resolving dependencies (explicitly specified) among the analyses, in Eclipse. Kloppenburg [2009] discusses the notion of incremental update for static analyses, in the context of IDEs. To the best of our knowledge, there are no generic object-oriented compiler designs or implementations that address the challenges related to stabilization requirements, and guarantee self-stabilization during the process of compilation, especially in the context of parallel programs.

8.2 Incremental Analyses

There is a vast literature on the topic of incremental update of program-abstractions of various kinds of program analyses ([Arzt and Bodden 2014; Carroll and Ryder 1987, 1988; Chen et al. 2015; Liu and Huang 2022; Liu et al. 2019; Lu and Xue 2019; Marlowe and Ryder 1989; Nichols et al. 2019; Pollock and Soffa 1989; Ryder 1983; Ryder et al. 1988; Sathyanathan et al. 2017; Sreedhar et al. 1996; Yur et al. 1997]). Though these incremental approaches provide algorithms that take a set of program changes as their argument, and stabilize the stale program-abstraction accordingly, they only address $Q_3$ out of the six key questions raised in Figure 2. Further, these approaches do not provide any mechanism for efficiently maintaining the program changes either. Homeostasis closes this gap by providing automated techniques to address the remaining five key questions. Thus, different incremental analyses can be used along with Homeostasis. Under Homeostasis, such algorithms can be directly implemented in the handleUpdate method. The pass writers need not specify where to invoke the incremental stabilization and with what arguments—these tasks are conveniently automated by Homeostasis, for all the existing and future optimizations.

9 CONCLUSION

In this article, we have presented a novel, efficient, and reliable compiler-design framework called Homeostasis, for enabling generic self-stabilization of the relevant program-abstractions in response to every possible transformation of the program, in the context of object-oriented compilers. Homeostasis decouples the program analysis and optimization passes in a compiler: using Homeostasis, neither the optimization writers need to write any code to stabilize the (existing or future) program-abstractions, nor do the writers of a program analysis need to know about the set of optimization passes in the compiler in order to ensure correct stabilization of the corresponding program-abstraction. We added Homeostasis to the IMOP compiler framework for OpenMP C programs. To illustrate the benefits of Homeostasis, we implemented a generic inter-thread data-flow analysis pass HIDFA, and a set of six standard IDFAs as its instantiations. We also implemented a set of optimization passes, collectively termed as BarrElim, which includes a set of four standard optimizations, and is used to remove redundant barriers in OpenMP programs; we did not have to add any stabilization-specific code for any of the optimization passes of BarrElim. Our evaluation of these passes on a set of real-world benchmarks has given us encouraging results concerning the performance and feasibility of using Homeostasis. While Homeostasis has been discussed using a Java-based compiler, we believe that the design of Homeostasis is generic enough to be applicable to other object-oriented compilers (including JIT compilers), for serial as well as parallel programs.

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APPENDICES

A PERFORMANCE COMPARISON WITH EAGER MODES OF STABILIZATION (EGINV AND EGUPD)

We now present an evaluation describing the impact of the lazy modes of self-stabilization on compilation while running the BarrElim set of optimizations, taking the weaker baseline of EGINV mode, where the stabilization is performed eagerly at the end of each elementary transformation. Note that such a scheme of EGINV stabilization is easy to automate, but can be quite inefficient, as we show in this section. We present our evaluation in the context of parameters related to stabilization time, and total compilation time. In Figure 32, we present various parameters related to compilation of the benchmark programs under study, when compiled with EGINV mode of stabilization; these numbers serve as the baseline for the evaluations discussed in this section.

In Figure 32, columns 4 and 5 show the stabilization time for IDFA flow-maps in the context of EGINV mode of stabilization, while performing the BarrElim set of optimization passes on the benchmark programs under study, for Nanda and K2, respectively. The zero (0) entries for the

| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---|---|---|---|---|---|---|
| Benchmark | #Trig | #T-Func | STB-Time (s) | Total Time (s) |
| | | | Nanda | K2 | Nanda | K2 |
| 1. BT (NPB) | 77 | 842396 | 12.3 | 22.56 | 18.92 | 34.45 |
| 2. CG (NPB) | 226 | 601627 | 4.89 | 8.16 | 6.76 | 11.2 |
| 3. EP (NPB) | 4 | 3304 | 0.07 | 0.15 | 0.6 | 1.28 |
| 4. FT (NPB) | 153 | 1108996 | 9.54 | 16.8 | 14.98 | 26.28 |
| 5. IS (NPB) | 0 | 806 | 0 | 0 | 0.33 | 0.8 |
| 6. LU (NPB) | 139 | 1998450 | 29.65 | 58 | 35.07 | 67.68 |
| 7. MG (NPB) | 540 | 5097722 | 52.46 | 129.09 | 70.44 | 158.95 |
| 8. SP (NPB) | 122 | 2252994 | 24.86 | 46.52 | 30.18 | 55.67 |
| 9. quake (SPEC) | 91 | 1115729 | 15.11 | 25.98 | 17.81 | 30.56 |
| 10. art-m (SPEC) | 10 | 161550 | 1.92 | 3.63 | 3.39 | 6.51 |
| 11. amgnk (Sequoia) | 161 | 714256 | 7.69 | 16.17 | 12.73 | 24.53 |
| 12. clomp (Sequoia) | 330 | 2048957 | 30.57 | 54.78 | 54.14 | 95.16 |
| 13. stream (Sequoia) | 141 | 158386 | 1.41 | 2.57 | 2.27 | 4.22 |
| 14. bellman-ford (IMS) | 55 | 34775 | 0.63 | 1.17 | 1.27 | 2.44 |
| 15. bfs-dijkstra (IMS) | 37 | 10037 | 0.42 | 0.71 | 0.89 | 1.76 |
| 16. byzantine (IMS) | 47 | 19061 | 0.51 | 0.91 | 0.98 | 1.96 |
| 17. dominating-set (IMS) | 180 | 442560 | 3.97 | 6.34 | 5.74 | 9.04 |
| 18. kcommittee (IMS) | 131 | 134113 | 1.38 | 2.3 | 2.8 | 4.68 |
| 19. leader-elect-dp (IMS) | 10 | 4260 | 0.29 | 0.5 | 0.61 | 1.3 |
| 20. leader-elect-hs (IMS) | 40 | 32761 | 0.41 | 0.7 | 1.15 | 2.26 |
| 21. leader-elect-lcr (IMS) | 12 | 3422 | 0.08 | 0.16 | 0.58 | 1.2 |
| 22. mis (IMS) | 14 | 11315 | 0.38 | 0.68 | 0.8 | 1.58 |
| 23. dst (IMS) | 169 | 687945 | 5.82 | 8.75 | 7.54 | 11.57 |
| 24. vertex-coloring (IMS) | 29 | 28527 | 0.44 | 0.81 | 1.17 | 2.27 |

Fig. 32. Evaluation numbers for performing the BarrElim set of optimizations on various benchmark programs, in the context of EGINV mode of stabilization. These numbers serve as the baseline for Section A. Abbreviations: #Trig = number of stabilization triggers, #T-Func = number of transfer-function applications, and STB-Time and Total Time refer to the IDFA-stabilization time, and overall compilation time, respectively.
Fig. 33. Speedup in IDFA stabilization-time under various modes of stabilization with respect to the EGINV mode, when applying the set of client optimizations, BarrElim. Higher is better.

STB-times of IS are due to the fact that no optimization opportunities were found by BarrElim passes for IS.

In Figure 33, we illustrate the impact of using LZINV, EGUPD, and LZUPD modes of stabilization, by showing their relative speedups with respect to EGINV, in terms of speedups in the IDFA.
stabilization-time. We exclude SP from this discussion on stabilization time, since there were no stabilization triggers for SP under lazy modes of stabilizations (that is, the stabilization time for lazy modes of stabilization was zero). As expected, the LZUPD mode incurs the least cost for stabilization among all the cases across both the platforms; consequently, it results in the maximum speedup with respect to EGINV — with speedups varying between 8.00× and 82.36× (geomean 22.39×) for Nanda; between 7.89× and 87.88× (geomean 24.42×) for K2.

We have noted that the gains in IDFA stabilization time using a particular mode of stabilization depend on multiple stabilization-mode-specific factors, such as (i) number of triggers of stabilization, (ii) number of times transfer-functions are applied on various program nodes during IDFA stabilization, (iii) cost incurred to process each program node per stabilization, and so on. For our baseline mode of stabilization, EGINV, we show the first two factors in columns 2 and 3 of Figure 32, respectively. In Figure 34, we show the number of stabilization triggers when using the lazy modes of stabilization normalized with respect to the EG-modes. Similarly, in Figure 35, for various modes of stabilization we show the number of transfer-function applications across all stabilization triggers normalized with respect to those numbers in case of EGINV mode. We observe that for each benchmark, the speedup obtained across different modes of stabilization closely correlates to these numbers. Across different benchmarks, the relative impact of these factors may vary, depending upon, for instance, the fraction of time spent in applying transfer-function when processing a program node during IDFA stabilization. We now illustrate our observations by comparing the performance of different modes of stabilization.

**LZUPD vs. EGINV.** The LZUPD mode consistently outperforms the RPINV mode across all benchmarks, for both the platforms, as shown in Figure 33. This can be attributed to the significant reductions in the number of transfer-function applications, as well as in the number of stabilization triggers, when using the LZUPD mode as compared to the EGINV mode, as shown in Figures 35 and 34, respectively. The maximum speedup in IDFA stabilization-time for LZUPD was observed in LU (82.36× in Nanda, and 29.68× in K2), consequent upon the fact that for LU, compared to EGINV, LZUPD re-processes significantly small fraction of the nodes (3.93%) over a reduced number of stabilization triggers (13.67%). In contrast, for leader-elect-lcr and bfs-dijkstra, LZUPD leads to some of the least (though still quite significant) speedups, as it results in reprocessing high fractions of nodes (15.24% and 19.30%, respectively), along with a high count of stabilization triggers (25% and 35.14%, respectively), as compared to the EGINV mode.

**LZUPD vs. EGUPD.** It is clear from Figure 33 that though the EGUPD mode consistently performs better than EGINV, compared to LZUPD it performs consistently worse, across all the benchmarks,
for both the platforms. This is because, as shown in Figures 34 and 35, LZUPD results in significantly fewer stabilization triggers (geomean 76.36% lower) than the EGUPD mode, thereby also resulting in a considerably fewer number of applications of the transfer-functions (geomean 14.6% fewer).

**LZINV vs. EGINV.** Across all the benchmarks, and both the platforms, we notice a performance improvement with LZINV mode, as compared to the EGINV mode, with geomean speedup as 3.62×, for Nanda, and 3.75×, for K2. The maximum speedup was observed in case of stream (5.88×) in Nanda, and leader-elect-dp (8.33×) in K2, consequent upon the fact that among the benchmarks shown in Figure 33, stream and leader-elect-dp correspond to quite large reductions in the number of stabilization triggers (see Figure 34) with the lazy modes of stabilization.

**LZINV vs. EGUPD.** From Figure 33, note that the EGUPD mode outperforms the LZINV mode in the context of IDFA-stabilization time, for most of the cases across both the platforms. This trend can be explained as follows. From Figure 34, it is clear that the LZINV mode consistently results in fewer stabilization triggers than the EGUPD mode. However, it is also expected that the incremental update of IDFA flow-maps in UPD-modes will result in fewer applications of the transfer-functions per trigger, as compared to the same in case of INV-modes which involve invalidation and full re-computation of the IDFA flow-maps. This is evident in Figure 34, where we notice that EGUPD mode consistently applies significantly fewer transfer-functions (geomean 90.38% fewer) as compared to the LZINV mode. As a result, EGUPD mode outperforms the LZINV mode, for most of the scenarios.

**Summary.** Overall, we found that the LZUPD mode leads to the maximum benefits in stabilization time, across all the four modes of stabilization. Furthermore, we also observed that if the UPD-mode is unavailable for a program-abstraction due to absence of its incremental-update algorithm, the fully-automated stabilization provided by Homeostasis in the form of LZINV mode can still provide good performance improvements over the naive automated stabilization attained using the EGINV.
mode. These observations underline the performance benefits in stabilization time when using Homeostasis. This may in turn improve the overall compilation speed, as shown in Figure 36 (with geomean improvements of 4.09× and 3.80× in Nanda and K2, respectively).

B GUIDELINES TO RETROFIT HOMEOSTASIS IN LLVM

Given the popularity of the LLVM compiler framework, in this section we provide brief guidelines on how LLVM can be retrofitted with Homeostasis. This further helps us argue about the generality and applicability of Homeostasis to arbitrary IRs. The key components of Homeostasis (from Section 3.2) are mapped in LLVM as follows:

– The LLVM IR corresponds to the IR which can be used as the base program-abstraction. The basic blocks (BasicBlock), functions (Function), and modules (Module) of the LLVM IR can be treated as the three specific nodes on which elementary transformations can be specified. Each element (Instruction) of the basic-block needs to be made immutable.

– Various fundamental transformations on BasicBlock of LLVM IR that can serve as the elementary transformations need to be identified. A key requirement here is that one should be able to represent all possible transformations of the basic blocks using these elementary transformations. One such possible set comprises of two fundamental transformations: (i) insertion of an IR instruction at a given index, and (ii) removal of an IR instruction. Note that the updates to an immutable IR instruction can be achieved by creating a new instruction,
and replacing the old instruction with the new one. The structure of these elementary transformations should be made conforming to the design shown in Figure 5. Similar elementary transformations can be identified for the classes Function and Module.

— For ease of use, various higher-level transformation APIs (such as those that support copying a block, renaming a variable, etc.) can be created using these elementary transformations. Further, the code for existing transformation APIs should be updated such that all translations of the IR are expressed directly or indirectly using the identified set of elementary transformations.

— In Homeostasis, all program-abstractions must inherit from a base class, BasePA. LLVM already has a Pass super-class, which can serve the purpose of BasePA. The Pass class can be modified to adhere to the design given in Figure 7. The definition of stabilize method from Homeostasis can be used as it is in the Pass class.

— LLVM already identifies a set of analysis passes, and a set of transformation passes; former corresponds to the analysis passes discussed in this text, whereas latter to the optimization passes. For each of the identified analysis passes, one needs to ensure that all accesses to the related program-abstractions are done through the appropriate getters that follow the simple structure shown in Figure 7. As discussed in Section 6.2, one needs to ensure that (1) the existing code to generate the program-abstraction from scratch is invoked from the overridden method compute, and (2) the existing code to perform incremental update of the program-abstraction, wherever applicable, is invoked from the overridden method handleUpdate.

Note that the core library of LLVM is larger than one million lines of code written in C++, spanning across more than 3k files. Consequently, the development effort required to retrofit Homeostasis to LLVM is not trivial. However, the proven benefits of attaining self-stabilization in a compiler clearly make this one-time effort worthwhile, more so considering the large size of the code base involving numerous interacting passes of analysis and transformation passes. We leave this as a future work.

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