Robust site-resolvable quantum gates in an optical lattice via inhomogeneous control

J.H. Lee¹, E. Montano¹, I.H. Deutsch² & P.S. Jessen¹

The power of optical lattices for quantum simulation and computation is greatly enhanced when atoms at individual lattice sites can be accessed for measurement and control. Experiments routinely use high-resolution microscopy to obtain site-resolved images in real time, and site-resolved spin flips have been implemented using microwaves resonant with frequency-shifted target atoms in focused light fields. Here we show that methods adapted from inhomogeneous control can greatly increase the performance of such resonance addressing, allowing the targeting of arbitrary single-qubit quantum gates on selected sites with minimal cross-talk to neighbouring sites and significant robustness against uncertainty in the atom position. We further demonstrate the simultaneous implementation of different gates at adjacent sites with a single global microwave pulse. Coherence is verified through two-pulse experiments, and the average gate fidelity is measured to be $95 \pm 3\%$. Our approach may be useful in other contexts such as ion traps and nitrogen-vacancy centres in diamond.

¹ Center for Quantum Information and Control, College of Optical Sciences and Department of Physics, University of Arizona, Tucson, Arizona 85721, USA.
² Center for Quantum Information and Control, Department of Physics and Astronomy, University of New Mexico, Albuquerque, New Mexico 87131, USA.

Correspondence and requests for materials should be addressed to P.S.J. (email: poul.jessen@optics.arizona.edu).
ultracold atoms in optical lattices are an important platform for quantum information science, lending itself naturally to quantum simulation of many-body physics and providing a possible path towards a scalable quantum computer. Quantum simulations with the atom-lattice system generally explore many-body physics of condensed matter systems described by simple model Hamiltonians, for example, the families of Hubbard and Ising models, and similar physics is typically relevant when exploring optical lattice-based architectures for universal quantum computing. Thus, although optical lattices in principle can have spatial periods from one-quarter to many times the optical wavelength, the need for site-to-site tunnelling in such experiments tends to limit the workable lattice period to \( < 1 \) \( \mu \)m. That in turn poses a significant obstacle to the implementation of reliable, high-fidelity quantum control of atoms at individual lattice sites, which will ultimately be required to reach the full potential of this system.

Atoms in two-dimensional (2D) lattices with periods near the optical wavelength have been successfully imaged using high numerical aperture optics with resolution close to the lattice spacing.\(^{9,10}\) Other demonstrations include cavity-aided magnetic resonance imaging\(^{11}\), optical microscopy in conjunction with numerical deconvolution\(^{12}\) and imaging in a three-dimensional (3D) lattice with \( \approx 5 \) \( \mu \)m period.\(^{13}\) Coherent quantum control of atoms at targeted lattice sites requires even higher resolution than imaging if adjacent atoms are to remain unperturbed. Subwavelength resolution can in principle be achieved with a tightly focused optical field that shifts the transition frequency of an atomic qubit relative to its neighbours, in combination with a frequency-selective microwave pulse that implements the desired rotation of the targeted qubit.\(^{34}\) In practice, such a resonance-addressing scheme involves a tradeoff—for a sharply focused addressing field, the frequency shift becomes overly sensitive to its alignment relative to the target site, whereas a softer focus leads to unwanted perturbations at adjacent sites. Faced with these difficulties, experiments have so far demonstrated only adiabatic spin flips,\(^{15}\) which are robust to small variations in the frequency shift but cannot manipulate coherence between the spin-up and spin-down states in the manner of universal quantum gates. Misalignment between the trapping and addressing fields can be avoided by incorporating a spatially varying qubit frequency shift into the lattice itself. This approach has been used to target quantum gates on sub-ensembles of qubits located on one or the other side of the barrier in a lattice consisting of double wells, but does not lend itself to more general forms of addressing.\(^{16}\)

In this article, we explore the use of advanced quantum control to dramatically improve and extend the capabilities of resonance addressing. It is known from the theory of inhomogeneous control in nuclear magnetic resonance that composite pulses can be designed to achieve any desired qubit response as a function of one or more parameters.\(^{17-19}\) Applying this idea to resonance addressing, we first map position onto frequency shift and then design a single phase-modulated microwave pulse to implement a unitary transformation that is a chosen function of that frequency shift. An example might be a pulse that executes a quantum gate across a desired frequency and spatial interval, while at the same time doing nothing (the identity transformation) outside it. We show that such a ‘top-hat’ response can greatly improve the robustness against misalignment between trapping and addressing fields, while at the same time suppressing perturbation of the adjacent sites. We further show that it is possible to simultaneously perform different gates at adjacent sites with a single global control waveform. In both cases, we verify coherent gate operation through two-pulse Ramsey interrogation, and use randomized benchmarking\(^{20}\) to measure an average gate fidelity of 95 \( \pm \) 3\%. This control-based approach to reduce cross-talk and increase robustness is broadly applicable in optical lattices irrespective of geometry, and may be useful also on other platforms for quantum information processing, such as ion traps\(^{21}\) and nitrogen-vacancy centres in diamond.\(^{22}\)

Results
Preparing and imaging the atom sample. To test the basic idea in the laboratory, we have implemented spatially resolved resonance addressing along one dimension of a 3D optical lattice with a \( \Lambda = 426 \) \( \mu \)m period, using a superimposed optical standing wave—the ‘addressing lattice’—as illustrated in Fig. 1a. The trap lattice is loaded with caesium atoms at a density of one atom per \( \sim 100 \) sites, each representing a qubit encoded in two spin states, \(|\uparrow\rangle\) and \(|\downarrow\rangle\). The addressing lattice is formed by two laser beams intersecting at a shallow angle, producing a frequency shift that varies sinusoidally along the \( x \)-axis of the trap lattice as shown in Fig. 1b. Because the frequency shift is uniform in the \( y-z \) plane, this geometry addresses \( \sim 35 \) planes of \( \sim 10^3 \) atoms simultaneously, rather than individual sites in the 3D trap lattice.

The addressing lattice is translated with nanometre accuracy along \( x \) by changing the relative optical phase between the addressing beams. Passive stability keeps jitter in the relative position of the trap and addressing lattices \( < 15 \) \( \mu \)m on a timescale of several seconds, sufficient that it can be regarded as constant during a single run of the experiment, whereas on timescales from minutes to hours, the lattice positions may drift by several microns. For the purposes of our experiments here, the effects of this slow drift can be eliminated using a preparation and resonance imaging protocol described in the following.

To prepare a well-defined starting point, we select a subset of atoms in the trap lattice, by flipping their spins from \(|\uparrow\rangle\) to \(|\downarrow\rangle\) with a narrow-band microwave pulse and removing the remaining atoms in \(|\uparrow\rangle\). In this situation, the spin-flip probability depends on the qubit transition frequency and thus on the position of the atoms relative to the addressing lattice (Fig. 1b). By introducing a slight tilt between the planes of the trap and addressing lattices, we ensure that there will always be a subset of sites in the trap lattice whose resonance frequencies lie within the bandwidth of the ‘preparation pulse’, no matter the relative position of the lattice (Fig. 1c). The result is an ensemble of atoms prepared in the \(|\downarrow\rangle\) state at sites in the trap lattice that have a precisely controllable distribution of spatial offsets relative to the nominal target plane.

We can construct a high-resolution resonance image of an atom distribution thus prepared, through repetitions of the experiment wherein the preparation step is followed by a translation of the addressing lattice, a second ‘imaging pulse’, and a measurement of the number of atoms returned to the \(|\uparrow\rangle\) state. Figure 2a shows such an image, together with a Gaussian fit with s.d. \( \sigma = 80 \) \( \mu \)m. The image width is given by the convolution of the (identical) preparation and imaging pulses, and indicates a spatial resolution of \( \sim 56 \) \( \mu \)m, well below the lattice period. It is also possible to prepare and image atom distributions in planes that are separated by, for example, one trap lattice period along \( x \) by applying a sequence of preparation pulses with identical frequency and separated by appropriate translations of the addressing lattice (Fig. 1c). A resonance image of an atom distribution corresponding to triplets of adjacent sites along \( x \) is shown in Fig. 2c.

Spin flips and quantum gates. Robust control in the presence of broad distributions of qubit positions and frequencies requires the use of more advanced techniques such as phase-modulated microwave pulses. These composite pulses consist of a train of \( N \) square pulses with variable phases \( \phi \) that have been computer
optimized, so that the overall transformation accomplishes a desired objective.\textsuperscript{17,18} This can be either a spin rotation on a fixed input state, $|\downarrow\rangle \rightarrow \alpha|\downarrow\rangle + \beta|\uparrow\rangle$, or a full unitary transformation (quantum gate) $W(\delta)$ that varies in a prescribed way with the frequency shift $\delta$ of the qubit resonance relative to the microwave frequency (see Methods). Figure 2b shows the response to a composite pulse designed to flip spins uniformly across a targeted frequency region and leave them unaffected elsewhere. We can test the performance of a similar top-hat pulse whose three regions have been optimized to overlap with an atom distribution corresponding to triplets of adjacent sites. Figure 2d shows the distribution after the pulse, indicating a complete, robust absence of spin flips at the adjacent sites. For comparison, Fig. 2e shows the result of applying a single Gaussian pulse (identical to the preparation pulses) resonant at the centre of the distribution. In this case, some spins at the centre sites are unaffected, whereas some spins at the adjacent sites have been flipped. Adjusting the width of the pulse allows a tradeoff between the two types of error, but performance never approaches that of Fig. 2d.

The performance of unitary quantum gates can be evaluated with a two-pulse version of the approach above. We begin by applying a composite pulse that implements a $\pi/2$ rotation around the $i$ axis of the Bloch sphere in the central frequency region and the identity elsewhere. Shifting the overall phase of the pulse by $\phi$ changes the axis of rotation to $\cos(\phi)|i\rangle + \sin(\phi)|j\rangle$, and two pulses in sequence lead to a spin-flip probability $\cos^2(\phi/2)$, similar to the $\phi$-dependent interference in a two-path interferometer. Figure 3a–d shows a sequence of resonance images and corresponding populations remaining in $|\downarrow\rangle$ as a function of the phase $\phi$. The clear interference for atoms in the central region and the lack of $\phi$ dependence for atoms in the adjacent regions demonstrate that the pulse functions as intended and coherence is preserved.

A second example of a two-pulse experiment is shown in Fig. 3e–h. In this case, for frequency regions that correspond to triplets of adjacent sites as in Fig. 2c. Here the first pulse implements a Hadamard gate (rotation about $i$ around the $(i+k)/\sqrt{2}$ axis) on the centre sites and $\pi/2$ rotations on the adjacent sites. The second pulse implements identical $\pi/2$ rotations at every site, leading to interference patterns similar to Fig. 3c but with a $90^\circ$ shift at the centre sites. This data set shows explicitly that the gate operations are coherent on every site, and also demonstrates the freedom to perform independent gates simultaneously at adjacent sites with a single composite pulse. The contrast of the interference patterns in Fig. 3f–h provides information about the fidelity of the various transformations. We can estimate the overall fidelity of a two-gate sequence as $F_{\text{pair}} = S_{\text{max}}/(S_{\text{min}} + S_{\text{max}})$, where $S_{\text{min}}$ and $S_{\text{max}}$ are the minimum and maximum values of the interference signal. Assuming that gate errors are small, $e = 1 - F \ll 1$, uncorrelated, and independent of $\phi$, the gate fidelity can then be estimated as $F \approx \sqrt{F_{\text{pair}}}$. For the data in Fig. 3f–h, this yields an average gate fidelity of $F = 0.96$.

**Randomized benchmarking.** A more comprehensive test of gate fidelity is best performed using randomized benchmarking\textsuperscript{20}. This approach separates gate errors from errors in the preparation of input states and measurement of output states,
to the interference pattern, and error bars are estimated as 1 s.d. of the residuals from the fit.

Figure 2 | Resonance imaging and addressing of single and multiple planes. (a) Resonance image showing a distribution of atoms prepared in a single plane as indicated in Fig. 1c. (b) Spin-flip probability for a composite microwave pulse with a ‘top-hat’ response as function of frequency. The frequency and position axes are matched between a and b. (c) Preparation of atoms in three adjacent planes as in Fig. 1c. (d) Selective spin flip of atoms at the centre sites, performed using a composite pulse with a top-hat response similar to, but narrower than, b. (e) Imperfect spin flip of atoms at the centre sites, performed using a Gaussian pulse. Solid dots represent data and lines represent fits. In a and c-e, the shaded areas show the separate Gaussians fits associated with atoms at adjacent sites.

Figure 3 | Unitary quantum gates. (a) Sequence of colour-coded resonance images (similar to Fig. 2c), showing the coherent action of a pair of composite pulses. Each pulse implements a π/2 rotation on the central atom distribution, with full spin flips occurring at ϕ = 0° and 360°, and the identity at ϕ = 180°. Both the individual pulses and the pair always implement the identity on the adjacent atom distributions. (b-d) Population remaining in the initial |↑⟩ state as function of relative pulse phase, for each distribution. The populations (dots) are determined from the areas of Gaussian fits as in Fig. 2c. Solid lines are fits to the interference pattern, and error bars are estimated as 1 s.d. of the residuals from the fit. (e-h) Sequence of resonance images and interference patterns similar to a-d, but with atom distributions chosen to coincide with adjacent sites along x. The first composite pulse here implements a Hadamard pulse at the centre sites and a π/2 rotation at the adjacent sites, and the second pulse implements π/2 rotations at every site. Solid lines are fits to the interference pattern, and error bars are estimated as 1 s.d. of the residuals from the fit.

and provides a meaningful measure of the average fidelity of gates when they are combined into long random sequences. For the 4 ms pulses used in Fig. 3, the total duration of the necessary pulse sequences exceeds the time available in our experiment, but useful information can still be obtained by benchmarking a set of pulses that have been rescaled and shortened to 1 ms duration in such a way that the intrinsic control fidelity remains unchanged (see Methods). Figure 4 shows the fidelity for sequences of rescaled pulses that were originally designed to implement computational gates (CGs) on the target lattice sites and the identity at neighbouring sites. Fits yield an average fidelity $\mathcal{F}_{\text{CG}} = 0.98$ for the central region, and a fidelity per identity of $\mathcal{F}_1 = 0.96$ for the adjacent regions. In the absence of external perturbations, for example, magnetic fields and light scattering, one would expect similar fidelities for the site-resolvable gates implemented by the original pulse. On the other hand, if gate errors were entirely due to external factors, one might expect four times the error for the original pulses. This implies a fidelity in the range $\mathcal{F}_{\text{CG}} = 0.92 – 0.98$ for the site-resolvable quantum gates in Fig. 3. This is consistent with the $\mathcal{F} \sim 0.96$ obtained from the two-pulse interference patterns, especially because the latter estimate includes a non-negligible contribution from initialization and readout errors.

Discussion

Our laboratory realization of robust, site-resolvable quantum gates through quantum control points to further experiments...
**Addressing lattice.** The addressing lattice is formed by two plane waves with orthogonal linear polarizations, intersecting at an angle of 1.74°. This configuration creates a lattice of constant intensity and spatially varying polarizations. The corresponding light shift is equivalent to a fictitious magnetic field, with the steepest gradient where its value is near zero (Fig. 1b), the most favourable situation for resonance imaging and addressing. The addressing lattice period is 28 μm, corresponding to 65.9 periods of the trapping lattice. For perfectly aligned trap and addressing lattices, such incomplete periods would slightly shift the relative position of the trap sites from period to period of the addressing lattice, but this becomes irrelevant for misaligned lattices as discussed in the main text.

**Calibrating translations and frequency shifts.** The addressing lattice is translated by a shift in the relative phase between its plane wave components with an electro-optic modulator (EOM) in the beam path (Fig. 1a). To prepare atoms in adjacent planes (Fig. 1c), an accurate calibration of translation as a function of the EOM control voltage is required. This calibration is performed by preparing atoms in a single y-z plane at position x₀, displacing them a known distance Δx along x, constructing a resonance image and noting the EOM voltage V at the image centre where the addressing lattice has been translated by the same Δx. As illustrated in Supplementary Fig. S1a, atoms are moved by changing the angle θ between the linear polarizations of the beams making up the trap lattice along x, with angles θ = (−360°, −180°, 0°, 180°, 360°) resulting in displacements Δx = [−Δ, −Δ/2, 0, Δ/2, Δ], where Δ = 426 nm is the trap lattice period. Supplementary Figure S1b shows resonance images for various polarization angles θ. A fit to the EOM voltages at the image centres (Supplementary Fig. S1c) shows an addressing lattice translation of one trap lattice period per 164 V, consistent with independent measurements of the EOM phase shift and the intersection angle of 1.74° between the addressing and trapping lattice beams. Once the translation is determined, the gradient where its value is near zero (Fig. 1b), the most favourable situation for resonance imaging and addressing can be calibrated.

**Figure 4 | Randomized benchmarking.** Overall fidelities achieved by sequences of composite pulses that apply computational gates (CGs) and Pauli randomizing gates (PGs) to the central atom distribution (red), and repeated identities to the adjacent ones (blue). Dots and squares are experimental data and lines are fits. Error bars are ±1 s.d., estimated from the spread of fidelities seen in different sequences.

**Methods**

**Atom trapping and manipulation.** Our trap lattice is formed by three pairs of counter-propagating laser beams with parallel linear polarizations, tuned 140 GHz above the 6S_{1/2}(F = 4) → 6P_{3/2}(F = 5) hyperfine transition at 852 nm. The depth of the optical potential is ~40 μK, corresponding to a trap vibrational frequency of 20 kHz. We load the trap lattice with 10^6 atoms from a magneto-optic trap and optical molasses, with a density of one atom per 100 sites in a volume with a diameter of ~35 addressing lattice periods. Qubits are encoded in states |↓⟩ = |F = 3, m = −3⟩ and |↑⟩ = |F = 4, m = −4⟩ in the hyperfine ground state. We use sideband cooling to prepare atoms in the |↑⟩ state, with mean vibrational excitation n ≈ 0.01 along x (excitation along y and z is unimportant). A bias magnetic field separates the qubit transition frequency from others in the ground manifold, and the combined bias, DC and AC background magnetic fields are stabilized to better than 20 μG using an approach similar to Smith et al. The resulting frequency variation in the qubit transition frequency is ~50 Hz. The atomic qubits are driven with 9.2 GHz microwaves from two horn antennae adjusted to improve the field homogeneity across the atom cloud. Selective removal of atoms in the |↓⟩ state is accomplished with radiation pressure from a resonant laser beam. Populations of the |↑⟩ and |↓⟩ states are obtained via Stern–Gerlach measurement.

**Microwave pulse design.** Atom preparation and resonance imaging are performed with microwave pulses having fixed frequency and phase, and a Gaussian envelope with a s.d. of 0.5 ms in the time domain. The corresponding power spectrum is also Gaussian with a root mean square width of 225 Hz. More advanced control is performed with composite microwave pulses consisting of a train of N square pulses having common amplitude A, duration T and frequency ω_mn fixed and with phases φ_n that vary between each pulse in the train. We keep ω_mn fixed and use the set of phases {φ_n}, along with A, T and the detuning δ = ω_qubit − ω_mn from qubit resonance, as our control parameters. Each of the square pulses has Rabi frequency Ω_m, a duration T, detuning δ and a phase φ, and will implement a unitary transformation $U(φ, A, T, δ) = \exp(-i(Ω_m T) \sigma_z)$. This corresponds to a rotation of the qubit Bloch vector by an angle $\theta = \Omega_m T/\Omega$ around an axis $\sigma_z = (Ω_m/Ω)(\cos(φ) + i(Ω_m/Ω)(\sin(φ)+i(δ/Ω)))$, where $Ω = \sqrt{Ω_m^2 + δ^2}$ is the generalized Rabi frequency, and $\sigma_z = \sin(φ) \sigma_x + \cos(φ) \sigma_y$ is the vector of Pauli operators. In that case, the composite rotation implemented by all N pulses is an overall transformation $U_N(φ, A, T, δ) = U_N(φ, A, T, δ)$.

** адресующий латтеч.** Однородный латтеч адаптирован к полю градиента, при этом направление поля градиента получается из компьютерного алгоритма GRAPE. Настройка частоты градиента позволяет получить надежную работу системы.
running a number of independent searches in parallel on different processors in a cluster.

**Microwave source.** We use an inexpensive microwave source as depicted in Supplementary Fig. S3a, combining an HP8672A Synthesized Signal Generator, which supplies a carrier at 9.2 GHz, and a Tabor-WW2572-2 Direct Digital Synthesis Arbitrary Waveform Generator, which supplies a signal at 30 MHz. The two are mixed in a single-sideband mixer whose output is preamplified, split in two, passed through a pair of 2 W power amplifiers and radiated by a pair of horn antennae with 15 dB gain. A low-power microwave switch between the HP8672A and the mixer is used for digital on/off control, whereas amplitude, frequency and phase modulation of the WW2572A under internal arbitrary waveform control is used to correspondingly modulate the sideband used to drive the atomic qubits. The overall system delivers microwave fields with amplitude sufficient to drive the qubit transition with Rabi frequencies up to 40 kHz. The amplitude-modulation capability is used when we generate preparation and imaging pulses with Gaussian envelope in the time domain, whereas the phase-modulation capability is used when we generate composite pulses for more advanced inhomogeneous control. An example of the time-dependent Rabi frequency (proportional to the square of amplitude) and phase of one of these composite pulses is shown in Supplementary Fig. S3b,c.

**Pulse rescaling.** As stated above, the jth square pulse in a pulse train rotates the qubit Bloch vector by an angle $\theta = \Omega T$ around an axis $\mathbf{q}$. It follows that replacing $\Omega_{j} \rightarrow \Omega_{j} T^{-1/2}$ and $\theta \rightarrow \theta T^{-1/2}$ leaves the angle and axis of rotation unchanged. Extending this to an entire pulse train, we see that $\Omega_{j} = \Omega_{j} T^{-1/2}$, $A_{j} T^{-1}$, $\delta = \delta T^{-1/2}$, $\mathbf{q}_{j} = \mathbf{q}_{j} T^{-1}$, with the same value of the cost function when averaged over a bandwidth $\Omega T$. As a result, a composite pulse can be rescaled to stretch or compress it in the time domain while preserving the bandwidth in the frequency domain, without otherwise changing the fidelity with which it implements the desired objective (the intrinsic control fidelity).

**Randomized benchmarking.** Following Knill et al.20, we perform randomized benchmarking by initializing atoms in the $|\uparrow\rangle$ state, applying $t$ successive pairs of $\pi/2$ CEs and PGs, and reading out the overall fidelity with which the qubit is returned to the $|\uparrow\rangle$ state. The sequence is repeated with random choices of CEs and PGs to obtain average overall fidelities as function of $t$. This data is then fitted with a function $F(t) = 1 - (1 - \alpha) (1 - 2 \epsilon)/2$, where $\alpha$ is the combined initialization and readout error, and $\epsilon$ is the average error per CE. To fit a sufficient number of composite pulses into the time window available in the experiment, we shorten them to 1 ms (rescaling by $1/2$). Provided that errors are dominated by imperfections in the control fields, and that the pulses are tested on a broadened version of the distribution in Fig. 2c, benchmarking will then provide a valid measure of the experimental gate fidelity.

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**Author contributions**

J.H.L. and E.M. performed the experiment and data analysis. I.H.D. and P.S.J. provided ideas and advice. P.S.J. supervised the work.

**Additional information**

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