Returning radiation in strong gravity around black holes: reverberation from the accretion disc

D. R. Wilkins, J. A. García, T. Dauser and A. C. Fabian

1Kavli Institute for Particle Astrophysics and Cosmology, Stanford University, 452 Lomita Mall, Stanford, CA 94305, USA
2Cahill Center for Astronomy and Astrophysics, California Institute of Technology, Pasadena, CA 91125, USA
3Dr. Karl Remeis-Observatory and Erlangen Centre for Astroparticle Physics, Sternwartstr. 7, D-96049 Bamberg, Germany
4Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK

ABSTRACT

We study reflected X-ray emission that returns to the accretion disc in the strong gravitational fields around black holes using General Relativistic ray-tracing and radiative transfer calculations. Reflected X-rays that are produced when the inner regions of the disc are illuminated by the corona are subject to strong gravitational light bending, causing up to 47 per cent of the reflected emission to be returned to the disc around a rapidly spinning black hole, depending upon the scale height of the corona. The iron Kα line is enhanced relative to the continuum by 25 per cent, and the Compton hump by up to a factor of 3. Additional light traveltime between primary and secondary reflections increases the reverberation time lag measured in the iron K band by 49 per cent, while the soft X-ray lag is increased by 25 per cent and the Compton hump response time is increased by 60 per cent. Measured samples of X-ray reverberation lags are shown to be consistent with X-rays returning to the accretion disc in strong gravity. Understanding the effects of returning radiation is important in interpreting reverberation observations to probe black holes. Reflected X-rays returning to the disc can be uniquely identified by blueshifted returning iron K line photons that are Compton scattered from the inner disc, producing excess, delayed emission in the 3.5–4.5 keV energy range that will be detectable with forthcoming X-ray observatories, representing a unique test of General Relativity in the strong field limit.

Key words: accretion, accretion discs – black hole physics – relativistic processes – galaxies: active – X-rays: binaries – X-rays: galaxies.

1 INTRODUCTION

The reflection of X-rays from the accretion disc provides a unique insight into the extreme environments just outside the event horizons of astrophysical black holes; supermassive black holes accreting in active galactic nuclei (AGN) and stellar mass black holes accreting in Galactic X-ray binaries. Continuum X-rays emitted from a compact corona, composed of energetic particles that are accelerated either from the inner regions of the accretion disc or within the black hole magnetosphere (Haardt & Maraschi 1991) propagate through the strong gravitationa field. A significant fraction of the X-rays emitted close to the black hole will be focused towards the event horizon and the inner parts of the accretion disc by strong gravitational light bending.

Those rays incident on the geometrically thin but optically thick accretion disc are reprocessed. A ‘reflection spectrum’ is formed by the combination of Compton scattering, photoelectric absorption, fluorescent line emission, and bremsstrahlung emission by the heated plasma (Ross & Fabian 2005). The observed reflection from the inner accretion disc is subject to gravitational redshifts as rays propagate out of the deep gravitational potential, and Doppler shifts, owing to the orbital motion of the reflecting material in the disc. This causes ‘relativistic blurring’ of the reflection spectrum, most easily seen in the profile of emission lines, narrow in the frame of the emitter, that become broadened to display a blueshifted peak and an extended redshifted wing arising form the innermost regions (Fabian et al. 1989). Broadening is most easily seen in the iron Kα fluorescence line at 6.4 keV (in the rest frame), owing to the high fluorescent yield of this line (George & Fabian 1991) and the fact that it sits relatively isolated in the spectrum such that the broadening can be seen. The broadening of the iron L line along with lines of oxygen, nitrogen, and other elements below 1 keV blends the lines together, contributing to a soft excess of emission seen above the power-law continuum spectrum at these energies.

In accreting black hole systems where there is little absorption, either due to outflowing winds or more distant obscuration, measurements of the reflected X-rays have begun to reveal a wealth of information about the accretion process. The extremal redshift detected in the redshifted wing of the iron Kα fluorescence line reveals the innermost extent of the accretion disc, from which the spin of the black hole can be inferred (Brenneman & Reynolds 2006). Measurement of the profile of the broadened wing of the line reveals the pattern of illumination of the accretion disc by the primary X-ray source, or the emissivity profile of the disc (Wilkins & Fabian 2011), in turn probing the extent of the corona over the surface of the accretion disc (Wilkins & Fabian 2012) and also the geometry of the accretion flow (Taylor & Reynolds 2018).
Extreme variability is observed in the coronal X-ray emission, in particular in a class of AGN, the narrow-line Seyfert 1 galaxies, noted for their variability and complex X-ray spectra (Gallo 2006). The reflected X-rays are seen to respond to changes in the continuum luminosity, though after a time delay, the reverberation time lag, corresponding to the additional light traveltime between the corona and the reflecting accretion disc (Fabian et al. 2009; Uttley et al. 2014). Observations of this X-ray reverberation add a further dimension to the study of accreting black holes. The observed lag times are short (De Marco et al. 2013; Kara et al. 2016), indicating the compactness of the corona, lying within 2−3\,r_g of the disc plane (Wilkins & Fabian 2013). The gravitational radius, \( r_g = G M/c^2 \), is the characteristic scale length in the gravitational field and is approximately the radius of the event horizon of a maximally spinning black hole. Measurement of length in the gravitational field and is approximately the radius of the event horizon as the primary rays emitted from the corona. It is therefore expected not only that a significant fraction of the X-rays reflected from the inner disc will be lost within the event horizon, but also that some fraction of these reflected rays will be returned to the disc to be reflected a second time (and indeed further times), which we shall henceforth refer to as returning radiation. Returning radiation will impact not just the emissivity profile of the disc, but also the measured reverberation lags as higher order reflections impart additional light traveltime delays. Therefore, understanding the effects of returning radiation on X-ray reflection and reverberation observations is an important component of using these as probes of black holes and accretion physics, while direct detection of the relativistic effects of returning radiation will validate the prediction of General Relativity that strong light bending should operate in the vicinity of a black hole.

The first studies of returning radiation, conducted by Cunningham (1976), considered its effect on the thermal emission from the accretion disc. It was found that while the effects of returning radiation are negligible when the spin parameter, \( a/M \ll 0.9 \), the returning flux can be comparable to or greater than the locally generated flux at small radii (\( r < 1.5 r_g \)) when \( a/M > 0.99 \), altering not only the thermal emission spectrum but also the dynamics of the disc as returning photons impart a torque. Agol & Krolik (2000) incorporated returning radiation into calculations of disc dynamics and found that returning thermal emission becomes more significant when the zero-torque condition is relaxed at the innermost stable orbit (i.e. magnetic connections between the plunging region and inner edge of the disc can exert stresses). They find that up to 58 per cent of the thermal emission can return to the disc as returning photons. Connors et al. (2020) find that the X-ray reflection spectrum detected in the black hole X-ray binary XTEJ1550−564 during the soft, disc-dominated accretion state is best described by a disc illuminated by a thermal blackbody spectrum rather than by a power-law spectrum from the corona, suggesting that returning radiation is indeed significant and that it is the reflection of returning thermal emission that is detected.

The reflection of returning X-rays was first studied in the context of multiple local reflections on a corrugated accretion disc surface by Ross, Fabian & Ballantyne (2002). It was found that when the reflected X-ray emission impacts the disc surface multiple times before being able to escape that the effective ionization potential is increased, enhancing the observed soft excess, while the iron Kα emission line is sharpened and increased by around 20 per cent relative to the continuum.

We extend these studies of returning radiation, considering not just local multiple reflections, but returning radiation in General Relativity between different patches of the disc. Returning rays between distinct patches of the disc undergo gravitational redshift or blueshift and Doppler shifts owing to the relative motion of the disc material at the start and end points of the ray coupled with the direction of the ray. We follow returning rays in the Kerr space–time using ray-tracing simulations and employ radiative transfer calculations to compute the response of the disc to the returning primary reflection. We assess the impact of returning radiation on X-ray reflection spectroscopy and reverberation measurements and assess the detectability of direct signatures of returning radiation in strong gravitational fields.

2 TRACING THE RETURNING RADIATION

The passage of photons in the curved space–time around the black hole was followed using General Relativistic ray-tracing simulations. Rays were traced by integrating the null geodesics in the Kerr space–time, until they reach locations (\( r, \varphi \)) the accretion disc in the equatorial plane, where they are reflected. The primary reflection may be observed directly, or reflected rays may return to the disc (the returning radiation) to produce the secondary reflection component.

### 2.1 Primary irradiation

For simplicity, the primary source of the X-ray continuum was taken to be an isotropically emitting point source located at some co-ordinate height \( h \) above the singularity on the spin axis of the black hole, illustrated in Fig. 1. Rays were started at equal intervals in solid angle (starting at equal steps in \( \cos \alpha \) and \( \beta \), the polar angles) as measured in the source frame. The initial four-momentum vectors describing each ray were transformed to the global Boyer–Lindquist co-ordinate system (given the four velocity of the source) and the constants of motion \( h \) and \( Q \), corresponding to angular momenta in the \( \varphi \) and \( \theta \) directions and identifying each ray, were computed. The rays were traced by numerically integrating the first-order geodesic equations, evolving each of the co-ordinates (\( t, r, \vartheta, \varphi \)) as the affine parameter was advanced.
Rays from the primary source were traced until they reached the equatorial plane, in which the geometrically thin, optically thick accretion disc was taken to lie. Upon hitting the disc plane, the time co-ordinate, $t$, of each ray was recorded and the redshift, $g$, of each ray between the source and an observer in a (relativistic) circular orbit at the receiving radius in the disc was calculated following the standard procedure, calculating the ratio of the scalar products of the photon four momentum with, respectively, the receiver and emitter’s four velocity. By assuming the disc is flat, we consider only radiation that returns to the disc by light bending around the black hole. If the disc has a finite aspect ratio, there will be an additional geometric contribution to returning radiation from one side of the disc to the other that we do not consider here.

The equatorial plane was divided into 500 logarithmically spaced radial bins between the innermost stable circular orbit, representing the inner extent of the accretion disc, at $r = 1.235r_g$ for a maximally rotating black hole with spin parameter $a = 0.998 GMc^{-2}$ (where the spin parameter in the Kerr metric is related to the angular momentum of the black hole by $J = Mac$), and $r = 500r_g$.

The photon arrival rate into the bin at the end of each ray is given simply by the redshift between the source and the corotating observer at the intercept point on the disc, representing the relative rates at which proper time elapses (since the photon count is conserved along the ray). The flux along each ray is obtained by multiplying by a second factor of the redshift to account for the energy shift of each photon for a monochromatic source, or by $g^3$ for a source emitting a power-law spectrum with the count rate following $E^{-\gamma}$ (see Dauser et al. 2012). The aberration in solid angle between the emitter and receiver is accounted for by counting the relative numbers of rays landing in different bins and does not require additional factors of $g$ in this instance. The total photon count rate and flux incident upon each bin was computed by summing, respectively, the redshift $g$ and $g^2$ for all of the rays landing in the bin, dividing by the total number of rays emitted from the primary source. We average the redshift and arrival time over all of the rays arriving in each bin.

The primary reflection spectrum generated when a power-law continuum spectrum irradiates the disc was calculated for each radial bin using the XILLVER model (García & Kallman 2010; García, Kallman & Mushotzky 2011; García et al. 2013), describing the reprocessed X-ray spectrum as emitted in the rest frame of the irradiated material. The ionization parameter, $\xi = 4\pi F/n$, where $F$ is the ionizing flux integrated between 0.1 and 1000 keV, and the density, $n$, were assumed to be constant over the entire disc. For simplicity, these ‘reflected’ photons are assumed to be emitted isotropically in the disc frame. The combination of frame dragging and light bending in the Kerr space–time brings much of the radiation to the inner disc at glancing angles, leading to limb darkening that is offset against limb darkening in the disc atmosphere (Svoboda et al. 2010; García et al. 2014). This, however, is only simply calculated when each patch of the disc is illuminated by just one ray path from a point source. Here, we consider illumination of the disc by rays coming from a range of angles, both from the corona and returning from the disc.

X-rays reflected by the accretion disc are subject to Doppler shifts, due to the orbital motion of the disc material, and gravitational redshifts in the strong field close to the black hole, the combination of which is a function of the position $(r, \phi)$ on the disc. The energy shift seen from each location on the disc was computed by tracing a regular grid of rays backwards from an image plane a large distance ($r = 10,000r_g$) from the singularity centred on the line of sight at angle $\beta$ to polar axis, representing the inclination at which the accretion disc is observed. The parallel rays passing through perpendicular to the image plane represent the patch of sky observed by a telescope some large distance away (see Wilkins et al. 2016; Reynolds et al. 1999). The disc is divided into radial and azimuthal bins and the ray arrival time and redshift between each bin and the (stationary) image plane was recorded in a lookup table.

When treated separately, the observed primary reflection is computed for each of the radial bins on the disc by integrating through each of the azimuthal bins in the disc-to-observer table. For each radial and azimuthal bin, the rest-frame reflection spectrum described by XILLVER (Fig. 2) is shifted in energy according to the bin’s redshift and normalized in photon count according to the primary photon count recorded in each bin, and then multiplied by $g^3$.

Figure 2. The XILLVER model of the primary X-ray reflection spectrum from an accretion disc with iron abundance $A_{Fe} = 8$ and ionization parameter $\xi = 50$ erg cm s$^{-1}$ illuminated by a continuum with photon index $\Gamma = 3$. Returning radiation possesses this spectrum, shifted in energy. The XILLVERRR model predicts the secondary reflection spectrum emergent from plasma in the accretion disc illuminated by this spectrum.

The returning radiation possesses this spectrum, shifted in energy. The XILLVER model of the primary X-ray reflection spectrum from an accretion disc with iron abundance $A_{Fe} = 8$ and ionization parameter $\xi = 50$ erg cm s$^{-1}$ illuminated by a continuum with photon index $\Gamma = 3$. Returning radiation possesses this spectrum, shifted in energy. The XILLVERRR model predicts the secondary reflection spectrum emergent from plasma in the accretion disc illuminated by this spectrum.

In order to compute the reflected radiation that returns to the accretion disc, a secondary source was placed in the equatorial plane in each radial bin. Due to the axisymmetry of the Kerr metric and illumination of the disc by the primary source, emission from each radial bin can be represented by just a single-point source at one azimuthal location.

The disc sources were taken to be elements of an isotropically emitting plane, with $dI/d\Omega = \cos \alpha d\Omega = \cos \alpha d(\cos \alpha) d\beta$, where $\alpha$ is the angle from the normal to the disc and $\beta$ is the azimuthal direction of emission (in contrast to the spherically emitting primary source for which $dI/d\Omega = d(\cos \alpha) d\beta$). Disc elements were assumed to be in a stable circular orbit with angular velocity $\Omega = \frac{a}{r^2} = (a^2 + r^2)^{-1}$.

Rays were traced from the point source at each radius, integrating the geodesic equations, until they returned to the equatorial plane. Upon returning to the disc, rays were once again counted into radial bins, recording the total returning count rate and flux in each bin as well as the redshift, $g$, and co-ordinate traveltime, $t$, of the rays. While the source at each radius emitted the same number of rays to maintain resolution, the count rate and weighting of rays from each source were scaled according to the primary flux that was incident in the

2.2 The returning radiation

In order to compute the reflected radiation that returns to the accretion disc, a secondary source was placed in the equatorial plane in each radial bin. Due to the axisymmetry of the Kerr metric and illumination of the disc by the primary source, emission from each radial bin can be represented by just a single-point source at one azimuthal location.

The disc sources were taken to be elements of an isotropically emitting plane, with $dI/d\Omega = \cos \alpha d\Omega = \cos \alpha d(\cos \alpha) d\beta$, where $\alpha$ is the angle from the normal to the disc and $\beta$ is the azimuthal direction of emission (in contrast to the spherically emitting primary source for which $dI/d\Omega = d(\cos \alpha) d\beta$). Disc elements were assumed to be in a stable circular orbit with angular velocity $\Omega = \frac{a}{r^2} = (a^2 + r^2)^{-1}$.

Rays were traced from the point source at each radius, integrating the geodesic equations, until they returned to the equatorial plane. Upon returning to the disc, rays were once again counted into radial bins, recording the total returning count rate and flux in each bin as well as the redshift, $g$, and co-ordinate traveltime, $t$, of the rays. While the source at each radius emitted the same number of rays to maintain resolution, the count rate and weighting of rays from each source were scaled according to the primary flux that was incident in the
corresponding bin to accurately represent the relative contributions of the primary and returning radiation.

The secondary reflection produced by each of the returning rays was modelled using XILLVERRR, a modification of the XILLVER model that computes the emergent spectrum when the disc is irradiated using a XILLVER primary reflection spectrum rather than a power-law continuum. The primary reflection spectrum received at each point on the disc, from each other point of the disc, is subject to a different shift in energy, depending upon the relative locations (and hence velocities) of the emitting and receiving positions and the direction of the ray relative to the emitter and receiver. As such, the XILLVERRR spectrum is computed as a function of the energy shift of the incoming spectrum. Each ray path has only a single energy shift so it is only necessary to shift the energy of the incident spectrum. No blurring kernel needs to be applied at this stage. For each radial bin, the secondary reflection spectrum is computed based upon the average energy shift of all returning rays.

The specific reprocessed spectrum depends upon the total incident spectrum at a given point in time, thus, strictly, the primary and secondary reflections cannot be treated separately. Hence, when considering the time-averaged spectrum that is observed when the primary illuminating flux is constant, the reprocessed spectrum from each position on the disc is computed from the sum of the primary continuum and the primary reflection, meaning that XILLVERRR has two parameters, the energy shift and the flux ratio between the returning primary reflection and the primary continuum. We here only consider the first-order effect of the primary reflection returning to the disc and do not consider the higher orders of returning radiation that will further impact the illuminating and the observed spectrum, but with reducing magnitude.

The observed secondary reflection, or the observed combined reflection spectrum, is calculated in the same manner as the observed primary reflection, exploiting the fact that for illumination by an axisymmetric source, axisymmetry is not broken until the disc is observed from a specific line of sight. Each radial bin is again divided up into azimuthal bins and the lookup table is employed to obtain the energy shift and traveltime between each bin and the observer.

3 PROPERTIES OF THE RETURNING RADIATION

General relativistic ray tracing in the Kerr space–time around the black hole reveals the destinations of reprocessed X-rays that are emitted from the disc; the fraction that return to the disc, to where on the disc they return and the energy shifts and time delays of returning rays when they arrive back at the disc.

Fig. 3 shows the fraction of rays that are emitted from each radius on the disc around a maximally spinning (a = 0.998) black hole that escape (and can be observed as part of the reflection spectrum or reverberation response), defined as rays being able to reach r = 100rg without returning to the equatorial plane; the fraction that return to the disc; and the fraction lost within the event horizon of the black hole. The disc is illuminated by a point source at h = 5rg above the singularity. A greater fraction of rays emitted from the inner parts of the disc pass closer to the black hole, thus are strongly bent in the gravitational field, resulting in a larger fraction of rays from the inner disc returning to the disc.

Up to 50 per cent of the rays emitted from the innermost stable orbit (ISCO) return to the disc, while only 6 per cent are able to escape to be observed. Due to the large solid angle subtended by the event horizon to an observer at the ISCO, up to 43 per cent of the rays emitted will be lost into the black hole. The returning fraction drops substantially to just 12 per cent at 6rg, the innermost stable orbit for a non-spinning black hole, consistent with the findings of Agol & Krolik (2000). The majority of rays from beyond 10rg are able to escape to be observed in the primary reflection component without being returned to the disc. Returning radiation is, hence, much less significant around more slowly spinning black hole, as shown in Table 1, showing the total fraction of rays (emitted from all radii on the disc) that return to the disc and escape from the whole disc as a function of black hole spin. We will therefore only consider the maximal spin, a = 0.998 for the remainder of this work.

Fig. 4 shows the properties of the returning rays received as a function of radius on the disc. Fig. 4(a) shows the illumination pattern as a function of radius of the returning rays compared to the primary illumination by a point source at h = 5rg above the singularity. Shown is the photon count rate received per unit proper area, measured by an observer corotating with the disc and including the effect of length contraction of the orbiting frame (Wilkins & Fabian 2012). The primary illumination pattern shows the typical broken power law, flattening from $r^{-3}$ over the outer parts of the disc to a flattened profile at radii $r \ll h$. There is a slight steepening on the inner disc due to gravitational light bending focusing the primary emission and the time dilation to observers on the inner disc enhancing the photon arrival rate (Wilkins & Fabian 2012). Shown is the photon arrival rate per unit area, measured in a rest-frame corotating with the disc, rather than the emissivity profile, which is defined as the energy flux and is thus enhanced to a steeper power law at small radius.
Figure 4. The properties of the returning radiation received at different radii upon the disc. (a) The returning photon flux, that is, the count rate received per unit area (from the primary reflection) compared to the primary incident photon flux, as measured in the rest frame of the disc. (b) The ratio of the returning to primary flux. (c) The average energy shift of returning photons between when they are emitted at the primary reflection site and when they are received upon returning to the disc.

The returning fraction increases and tends to a constant value at large radius because the rays returning here largely originate from the inner disc. While the returning flux falls off at large radius, so too does the primary flux. At large radii, the majority of the returning radiation, which comes from the inner disc, appears to originate from a point source that adds to the photon count from the primary source. Since the ratio between the returning flux and primary continuum flux at most radii on the disc is less than around 20 per cent, returning radiation does not significantly affect the radial emissivity profile of the accretion disc.

Fig. 4(c) shows the energy shift of the returning radiation. Plotted is the average energy shift of all rays landing in each bin, between their emission measured in the orbiting frame of their source on the disc and their reception, as measured in the receiving frame. The returning energy shifts are weighted by the flux the disc observes returning along each ray. Any individual returning ray could have a range in energy shift due to the varying gravitational redshifts between the points of emission and reception, and the Doppler shift due to the direction of the specific ray relative to the disc. A significant number of the rays returning to the innermost radii on the disc are blueshifted. These rays, in general, originate from larger radius. Rays that are emitted from the disc counter to the direction of motion around a spinning black hole are more likely to be directed towards the event horizon and inner regions of the disc (Thorne 1974), an effect that is most pronounced for emission radii within $\sim 10r_g$. These rays will be bent around the black hole to encounter orbiting material head-on when they return to the disc, meaning they are Doppler shifted to higher energies, coupled with the blueshift experienced as they travel inwards through the gravitational potential from larger to smaller radii.

On the other hand, rays returning to the outer disc must climb out of the gravitational potential from smaller radii. They are not strongly redshifted, however, because the rays from the inner disc that are able to travel outwards are predominantly those emitted in the forward direction of motion of the emitting material. They are Doppler shifted to higher energy by the orbital motion of the disc before they propagate out of the potential, thus only moderate redshifts are seen in the radiation returning to the outer disc.
3.1 The reflection fraction

Enumerating rays emitted from all radii reveals that only 33 per cent of rays that are emitted from the disc around a maximally spinning black hole (i.e. 33 per cent of the reprocessed or reflected primary rays) are able to escape to infinity to be observed. This is the primary irradiation escape fraction, \( E_p \). 39 per cent of the reprocessed rays return to the disc to be reflected a second time, the primary return fraction, \( R_p \).

The total escaping and returning fractions, integrated over the whole disc, are functions of the illumination pattern or emissivity profile of the accretion disc. Greater flux emitted at small radius where the local return fraction is greater will lead to an overall increase in the returning flux. Secondary illumination of the disc follows approximately a constant \( r^{-3} \) power-law profile (with a slight steepening over the innermost radii), in contrast to the broken power-law emissivity profile that is typical of the primary illumination. For this single power-law illumination pattern, the escape fraction \( E_p \) is 0.29, while the return fraction \( R_p \) is 0.41. For comparison, Agol & Krolik (2000) find that up to 58 per cent of the thermal emission returns to the disc, although this is calculated based upon the emissivity profile of the thermal emission from the disc, including a significant flux emitted from the plunging region, inside the ISCO, deep within the gravitational potential. Here, we consider the emissivity profile of just the stably orbiting disc due to external irradiation by the corona.

The reflection fraction, here defined as the ratio of the total observed reflected flux to the continuum flux, can be used as a measure of the compactness of the corona around the black hole. Emission from a more compact corona, closer to the black hole, is subject to strong light bending, enhancing the flux that irradiates the disc and, hence, enhancing the observed reflected flux at the expense of the directly observed continuum flux (Miniutti & Fabian 2004; Wilkins & Gallo 2015; Wilkins 2016). For a given coronal geometry, the reflection fraction can be estimated from ray-tracing calculations by measuring the fraction of rays that reach the disc versus that able to escape to be observed as part of the continuum. The fraction of reflected rays, however, should be adjusted by the fraction of the reflected emission that is able to escape versus that returning to the disc. It should be noted that this definition of the reflection fraction; the ratio of the total number of rays that reaches the disc to that which escapes, differs from the definition of the reflection fraction in, for example, Dauser et al. (2016), where the reflection fraction is the ratio of reflected to continuum flux received by an observer at a given inclination.

A fraction \( E_p \) of the primary reflection directly escapes to be observed as the reflection component. A fraction \( R_p \) return to the disc. In addition to the \( E_p \) observed primary reflection, a fraction \( E_r \) of the \( R_p \) rays will escape in the secondary reflection component. A fraction \( R_r \) of the secondary return to the disc again and will form higher order returning radiation components.

Ray-tracing calculations show that the while the illumination profile changes from a broken power law to approximately a single \( r^{-3} \) power law between the primary and secondary reflections, illumination of the disc by higher order returning components where the disc source flux follows \( r^{-3} \) is not substantially altered from this power law, thus the same fractions \( E_r \) and \( R_r \) may be used for all higher order reflection components.

The total observed reflected flux is obtained by multiplying the primary flux incident upon the disc by the total escape fraction

\[
E = E_p + R_p \left( E_r + R_p E_r + R_p^2 E_r + \ldots \right)
\]

\[
E = E_p + R_p E_r \sum_{N=0}^{\infty} R_p^N
\]

Summing this geometric progression to infinity yields

\[
E = E_p + R_p \frac{E_r}{1 - R_r}
\]

Hence, for a point source located at, for example, \( h = 5r_g \) above the singularity, the intrinsic reflection fraction of 2.1 (Wilkins 2016) is reduced to 0.52 times that value due to reflected radiation returning to the disc in the strong gravitational field around the black hole.

The returning fraction varies with the geometry and location of the primary X-ray source. For a more compact source, closer to the black hole, a greater fraction of the emission will fall on to the inner regions of the accretion disc. From these inner regions regions of the disc, photons pass closer to the black hole and so a greater fraction return to the disc. Fig. 5 shows the escaping and returning fraction of the reflected photons as a function of the height of a point source above the singularity (which may be considered a proxy for the extent of the corona). The returning fraction increases from 35 per cent when the disc is illuminated by a source at \( h = 10r_g \) to 47 per cent when the source is at \( h = 1.5r_g \). The total escape fraction by which the observed reflection fraction is reduced (equation 2), shown by the solid line in Fig. 5, reduces from 57 per cent for \( h = 10r_g \) to 39 per cent for \( h = 1.5r_g \).

X-ray reverberation time-scales in Seyfert galaxies typically indicate distances between the corona and accretion disc between 2 and 9\( r_g \) (Kara et al. 2016), hence, in the following analysis, we shall consider a simplified model of a point source at \( h = 5r_g \).

4 THE REPROCESSED SPECTRUM

XILLVERRR predicts the spectrum that is emitted from the accretion disc when it is illuminated by the returning primary reflection. It is based upon the XILLVER model of García & Kallman (2010) and García et al. (2011, 2013), which solves the radiative transfer, energy balance, and ionization equilibrium of a Compton thick plasma to calculate the emergent reflection spectrum. While in XILLVER, the...
incident spectrum takes the form of a cut-off power law to predict the primary reflection spectrum, in XILLVERRR, the incident spectrum is the sum of the primary power law and the primary reflection spectrum described by XILLVER, and the reflection spectrum is computed for the total illumination.

XILLVERRR has two variable parameters; the energy shift of the returning primary reflection to account for Doppler shift and gravitational redshift between the primary and secondary reflections, and the flux ratio between the returning and primary continuum radiation. Illumination is assumed to be constant in time, thus the ionization parameter, \( \xi = 4\pi F n_{\infty} \), is fixed (the ionization is assumed to not change between the arrival of the primary and returning radiation). The reflection spectrum is also varied by the iron abundance in the disc, \( A_{Fe} \), relative to the Solar abundance, and the photon index, \( \Gamma \), of the primary continuum.

In this study, we assume values in line with those measured in narrow-line Seyfert 1 galaxies in which strong X-ray reflection, indicated by a relativistically broadened iron Kα line, is seen from the inner regions of the accretion disc, such as 1H0707−495 or IRAS 13224−3809. We take \( \xi = 50 \text{ erg cm}^{-2} \text{s}^{-1}, A_{Fe} = 8, \) and \( \Gamma = 3 \).

In order to illustrate the reprocessing of returning radiation by the accretion disc, Fig. 6 shows the secondary reflection spectrum as measured in the rest frame of emission, as predicted by XILLVERRR. The reprocessing of just the primary reflection is shown, with no incident continuum. Shown are the reprocessed spectra for three different energy shifts between the emission of the primary reflection spectrum and its return to the disc. In each case, the reprocessed spectrum is compared to the primary XILLVER reflection spectrum.

When there is no energy shift (\( E_{\text{return}}/E_{\text{emit}} = 1 \)), the features of the reflection spectrum, notably the iron Kα and \( \beta \) lines around 6.4 keV and the Compton hump around 30 keV are sharpened, as discussed by Ross et al. (2002). The secondary reflection spectrum above 1 keV is suppressed, with greater relative suppression above the iron K absorption edge at 7.1 keV and less relative suppression of the core of the iron Kα line. This results in the iron K absorption edge and fluorescence line being enhanced with respect to the rest of the spectrum, while sharpening the low-energy side of the Compton hump.

Some of the most striking alterations to the spectrum occur when the returning radiation is blueshifted. Shown for illustration is an extreme case where \( E_{\text{return}}/E_{\text{emit}} = 2 \). In this case, the iron K line photons returning to the disc are shifted to 12.8 keV. At such high energies, there is little photoelectric absorption. As such, the majority of these blueshifted iron K line photons are simply scattered, producing a blueshifted iron K line at around 12 keV in the secondary reflection spectrum. This is slightly broadened as some of the scattered photons gain or lose energy by Compton scattering. This is produced in addition to the 6.4 keV fluorescence line that is produced after the photoelectric absorption of photons in the returning radiation field.

The returning radiation changes the effective ionization balance in the upper layers of the disc in which the reflection spectrum is produced. The effective ionization potential is increased by the increased incident flux from the returning radiation (Ross et al. 2002). In the case of no energy shift, the slightly increased effective ionization in the surface layers enhances the soft X-ray emission lines around 1 keV relative to the primary reflection spectrum.

When the returning radiation is blueshifted, the enhancement in the effective ionization has a more significant effect that is particularly important with a steep, soft continuum spectrum (i.e. when \( \Gamma \gtrsim 2.5 \)). In this case, the hard X-ray spectrum is photon-starved, but blueshifting the primary reflection significantly increases the number of photons at high energies. This results in an increased temperature

![Figure 6](https://academic.oup.com/mnras/article/498/3/3302/5896458)
in the upper layers of the disc and a high effective ionization parameter. In addition to increasing the Compton broadening of the 12 keV blueshifted iron K line, this results in the smearing of the soft X-ray lines into a clearly defined soft excess.

When the returning primary radiation is redshifted, as in the case $E_{\text{return}}/E_{\text{emitted}} = 0.6$, the alteration of the spectrum during the secondary reflection is more subtle. In this case, the redshift results in the hard X-ray spectrum being further photon-starved, meaning the upper layers of the disc do not experience an increase in temperature and the effective ionization potential is reduced. Therefore, when the returning radiation is strongly redshifted, the soft X-ray lines are not enhanced to the same degree. Some Compton scattering of the returning radiation does still occur, however, leading to a redshifted reflection of the primary iron K lines around 3.8 keV in the secondary reflection spectrum, in addition to the soft X-ray lines in this part of the spectrum and the 6.4 keV iron Kα fluorescence line. Similar behaviour is seen with more extreme redshifts of the returning radiation, though the redshifted, scattered iron K lines then sit among the soft lines and are not so intuitively identified as in this illustrative case.

5 THE OBSERVED SPECTRUM

The total observed spectrum was calculated from ray-tracing simulations including both the primary illumination of the accretion disc by the corona and the illumination of the disc by the returning primary reflection. Higher order returning radiation would have added considerable computational expense and was not included in this study. From equation (1), each successive order is approximately 59 per cent weaker.

We consider the time-average spectrum, so therefore assume that the primary irradiation remains constant in time. The total reprocessed spectrum was computed for each radius on the disc for irradiation by the sum of the primary continuum and the returning primary reflection. For the emergent secondary reflection spectrum from each radial bin, we compute the average spectrum based upon the distribution of the energy shifts of the returning photons, weighted by the observed fluxes in the receiving frame of reference on the disc. Gravitational redshifts and Doppler shifts between each point on the disc and the observer producing the relativistic broadening have been applied.

The observed spectrum is shown in Fig. 7 and is compared, for reference, to the relativistically broadened primary reflection spectrum, and to the total secondary reflection that would be produced if the disc were illuminated by only the returning primary reflection. The lower panel displays the ratio of the total observed reflection to just the primary reflection.

While returning radiation has a pronounced effect on the rest-frame reflection spectra emitted from individual annuli on the disc, the effects are much more subtle when the integrated spectrum from the whole disc is considered and the emission is subject to gravitational redshifts as it climbs out of the potential of the black hole. The most notable effect of returning radiation on the observed, time-averaged spectrum is an enhancement in the relativistically broadened iron Kα line, slightly redward of the peak of the line. The strength of the line above the continuum is enhanced by 25 per cent.

Much of the returning radiation is Compton scattered, enhancing the amplitude of the Compton hump (relative to the best-fitting underlying continuum) by a factor of 3. This is particularly pronounced when the accretion disc is illuminated by a steep continuum spectrum, as in the case of the narrow-line Seyfert 1 galaxies in which the strongest reflection is seen. When the photon index $\Gamma = 3$, as shown here, the hard X-ray spectrum is photon-starved and few photons are available at high energy to Compton scatter. The blueshifting of the returning radiation to higher energy significantly increases the population of photons that form the Compton hump.

When the continuum spectrum is harder, the enhancement of the Compton hump by returning radiation is less. For $\Gamma = 2.4$, the level of the Compton hump above the best-fitting power-law spectrum is enhanced by a factor of 2, and only below 30 keV, as shown in Fig. 8 (the high-energy part of the Compton hump is not enhanced when the primary X-ray continuum is harder). For $\Gamma = 2$, the Compton hump is enhanced by only a factor of just 1.35 below 20 keV and is, in fact, slightly weakened at high energy, which may mimic a lower coronal temperature. In each case, the iron K absorption edge is deepened, sharpening the low-energy side of the Compton hump.

Because a significant fraction of the returning radiation is blueshifted, the ionization balance is changed in the layers of the disc in which the reflection spectrum is produced. The increase in the effective ionization produces additional soft X-ray emission, particularly in the 1–2 keV band. Such additional soft X-ray emission has been seen in the spectra of a number of AGN (Jiang et al. 2018) and has often been modelled by including additional reflection components (attributed to a clumpy structure in the disc with varying ionization parameter across the surface) or by an increase in the disc density. Returning radiation may explain some of this excess emission and reduce the need for such a severe increase in disc density.

The secondary reflection spectrum that is observed from different radii, after the effects of the Doppler shift and gravitational redshift between the disc and the observer, is shown in Fig. 9. Even though a strong blueshifted iron K line is produced when the returning radiation is blueshifted, the returning radiation most strongly blueshifted only within the innermost 2$r_g$ around a maximally spinning black hole. The photons emitted from such small radii are all strongly redshifted as they climb out of the gravitational potential, which
means that the blueshifted iron K line is seen not at 12 keV but between 2.5 and 5 keV. This broadened, blueshifted, Compton-scattered returning line can be seen separated from the iron Kα fluorescence line in the emission from 1.24rg on the disc, while at 2rg the blueshifted line blends into the blue wing of the fluorescence line. At 6rg, the returning radiation is no longer blueshifted and the additional scattered line emission can no longer be seen. A subtle peak corresponding to the scattered, blueshifted, returning iron K photons can be seen in the total reflection spectrum, forming a peak between 2.5 and 3.4 keV, though the peak is only 30 per cent above the emission features that surround it, which means it is likely difficult to detect in the time-averaged spectrum.

The shape of the reflection spectrum depends upon the inclination at which the accretion disc is viewed. Most notably, increasing the inclination angle of the disc normal to the line of sight (i.e. viewing the disc closer to edge-on) increases the range of radial velocities that are observed which hence broadens the profile of the iron Kα line. The enhancements in the reflection spectrum due to returning radiation are not strongly dependent on the inclination angle. Decreasing the inclination angle from the pictured 60° to returning radiation are not strongly dependent on the inclination observed in the absence of returning radiation.

The variation in the reflection spectrum as the photon index of the primary continuum, $\Gamma$, is varied. In each case, the total reflection spectrum, including both the primary and the secondary reflections due to returning radiation is compared to the primary reflection spectrum that would be observed in the absence of returning radiation.

The X-ray continuum emitted from the corona is highly variable. Variability in the continuum luminosity will be mirrored in the intensity of reflection signatures after a time lag corresponding to the additional light traveltime between the corona and the accretion disc (Uttley et al. 2014). Signatures of returning radiation will be further delayed due to the additional light traveltime between the sites of the primary and secondary reflections.

Reverberation signatures of returning radiation were explored by considering the response of the accretion disc to a single flash of X-rays emitted from the corona. In this case, the primary illumination will arrive at each point on the disc before any returning radiation, hence the reprocessed spectrum in response to each can be considered separately, rather than having to account for a time-variable primary to returning flux ratio.

When the accretion disc is irradiated by the continuum, species will become ionized and the reprocessed spectrum will vary accordingly on the order of the ionization time-scale, $t_{\text{ion}} \sim (h\nu) / F_X \sigma_{\text{ion}} \sim 10^{-7} (F/10^{16} \text{erg cm}^{-2} \text{s}^{-1})^{-1} \text{s}$ (Collin et al. 2003). Approximating Euclidean geometry, the flux received at radius $r$ on the disc is $L_X/4\pi (r^2 + h^2)$. Thus, assuming a 10$^7$M$\odot$ black hole about which the X-ray luminosity is 2 per cent of the Eddington luminosity (about 10 per cent of the bolometric luminosity where $L_{\text{bol}} \sim 0.2$ to maintain a thin accretion disc), that is, $L_X \sim 0.02L_{\text{bol}}$, the ionization time-scale at $r = 10rg$ in a disc illuminated by a point source at $h = 5rg$ is $t_{\text{ion}} \sim 10^{-7} \text{s}$.

Following the flash of continuum emission, ions and electrons in the disc will recombine and the reprocessed emission from the disc
will ‘reset’ to its initial state before the flash on the recombination time-scale:

\[ t_{\text{rec}} \sim \frac{1}{n_{\text{rec}}} \sim 10^5 (\frac{n}{10^{12} \text{ cm}^{-3}})^{-1} \text{ s.} \]

When the number density of the plasma in the accretion disc is taken to be \( n = 10^{15} \text{ cm}^{-3} \), as is typically assumed in reflection models applicable the accretion discs around supermassive black holes (e.g. García et al. 2013), the recombination time \( t_{\text{rec}} \sim 0.01 \text{ s.} \) If the density is increased to \( n = 10^{19} \text{ cm}^{-3} \), as suggested by recent spectral analysis of the reflected X-rays from the accretion disc in the narrow-line Seyfert 1 galaxy IRAS 13224−3809 (Jiang et al. 2018), the recombination time shortens to \( t_{\text{rec}} \sim 10^{-6} \text{ s.} \)

The interval between the arrival of the primary continuum and the mean arrival time of the returning radiation (from all parts of the disc) is minimum on the inner disc. Here, the delay between the mean arrival time of the primary and secondary reflection is

\[ 22 \frac{GMc}{r_g^3} \]

where the natural time unit \( GMc^{-3} \) is the light traveltime over one gravitational radius, and can be readily scaled by the mass of the black hole to evaluate light traveltimes for any black hole mass. For a \( 10^7 M_{\odot} \) black hole, \( GMc^{-3} = 50 \text{ s,} \) much longer than either the ionization or the recombination time-scale. The disc can be assumed to have reset between the arrival of the primary continuum and the returning radiation and these can be treated separately in the simulation when just a single flash of emission from the corona is considered.

### 6.1 The response of the disc

Fig. 10 shows the energy- and time-resolved response functions of the reverberation seen from the accretion disc after a single flash of X-rays from the corona. The total response is shown alongside the primary and secondary responses. Though each shows the characteristic response of relativistically broadened emission lines; the iron K lines around 6.4 keV and the lines that comprise the soft X-ray emission, discussed in detail by Reynolds et al. (1999) and Wilkins et al. (2016), the additional time delay between the arrival of the majority of the primary and the secondary emission is immediately apparent.

Following the flash of continuum emission, a single response is seen in each emission line in the primary reverberation component. The earliest arriving line photons are seen slightly redshifted from the rest-frame energy, originating just beyond the inner parts of the disc (around \( 5r_g \)) where the integrated light path from the corona to the disc to the observer is minimized, including the effects of light traveltime delays through the strong gravitational field. The most red- and blueshifted line emission comes from the innermost parts of the disc, where the orbital velocity is the greatest. Light traveltime delays mean the response function broadens to reach the most extreme red- and blueshifts some time after the first response is seen. The blueshifted side of the line response is seen to loop round to low, redshifted energies as gravitationally lensed (hence magnified) emission from the back side of the disc re-emerges from behind the black hole. Finally, the latest response is seen in a double-peaked line profile from the approaching and receding sides of the outer disc, furthest from the primary X-ray source. The reflected continuum provides emission over all energies over a range in time, while the Compton hump produces broad, delayed emission feature around 30 keV.

While the primary reverberation shows just a single response in each emission line, the returning radiation produces multiple line responses superimposed upon one another at later times, becoming broader in their range of redshift. In addition, the returning, blueshifted iron K photons that are scattered from the innermost parts of the disc add an additional line-like feature starting at 3 keV.
The change in the lag profile from that caused by variation in either the red wing of the line relative to the core of the line distinguishes radiation arriving at late times. The average arrival time of photons radiation increases the reverberation time lag across the broad iron singularity, the inclusion of the secondary response from returning reverberation.

The response of the total continuum, primary and secondary response is compared to just the primary response. For X-rays originating from a point source at $h = 5r_g$ above the singularity, the inclusion of the secondary response from returning radiation increases the reverberation time lag across the broad iron K line, due to the additional iron K line emission from returning radiation arriving at late times. The average arrival time of photons in the core of the iron K line at 6.4 keV is increased by just under 30 per cent, while the average arrival time of photons in the redshifted wing is increased by 60 per cent. This increase in the arrival time of the red wing of the line relative to the core of the line distinguishes the change in the lag profile from that caused by variation in either the black hole mass or the scale height of the primary X-ray source which would cause a rescaling of the entire iron K line lag profile (Cackett et al. 2014).

Between 0.5 and 1 keV, the soft X-ray reverberation lag is, on average, not affected by the presence of returning radiation. This is not to say that the secondary soft X-ray reflection is not delayed, rather that the lag is shorter relative to the 1–2 keV band. When returning radiation is included, additional reprocessed emission between 1 and 2 keV from the ionized top layers of the disc delays the average response time of this reference band.

The response time of the Compton hump is more than doubled at energies between 10 and 30 keV as the returning radiation contributes significantly to this band. The strong iron K absorption edge in the secondary reflection spectrum, however, means that emission between 7 and 9 keV is strongly dominated by the continuum and primary reverberation components (a significant number of these photons are absorbed in the secondary reverberation), producing a sharp dip in the lag profile between these energies, between the iron K emission line and the rise of the response time into the Compton hump.

The scattered blueshifted iron K line photons that return to the inner disc are manifested in the lag-energy spectrum as a steepening in the rise of the iron K line between 3.5 and 4.5 keV. These photons are scattered within the innermost 2$r_g$ of the disc. They are redshifted before they reach the observer, and their passage is significantly delayed as they travel through the strong gravitational field (Shapiro 1964).

6.2.2 Time-domain response functions

In order to verify that any additional lag seen in the redshifted wing of the iron K line is due to the reverberation of returning radiation, rather than differences in the primary spectrum or the geometry of the corona or accretion disc that may also change the line profile, we examine the specific shape of the response in this energy band. Fig. 12 shows the time-domain response functions to a flash of continuum emission at $t = 0$, showing the total response and the contributions from the primary and secondary reverberations. The response is shown in energy bands corresponding to the soft excess, below 1 keV, the continuum, the core of the iron K line, and the blueshifted returning iron K photons scattered from the inner disc, superimposed upon the redshifted wing of the line.

The delayed response due to returning radiation can be clearly seen in energy bands dominated by the reflected iron K line complex, in Figs 12(b) and (d). The primary response of the 5–7 keV iron K band initially peaks at time $6 GMc^{-3}$ after the flash of primary continuum emission from a source at $h = 5r_g$ is received and is relatively narrow. Following this, there is a sharp second peak, consisting of the magnified, lensed emission re-emerging from the back side of the disc, which would classically be hidden behind the black hole. In strong gravity, these rays are bent around the black hole (Reynolds et al. 1999; Wilkins & Fabian 2013; Cackett et al. 2014). Following this re-emergence peak, the response decays at late times as the parts of the disc furthest from the primary source respond.

While the first primary response is seen at $t = 6 GMc^{-3}$ after the continuum flash, the secondary reverberation is not seen until $t = 23 GMc^{-3}$, creating a secondary peak at $t = 35 GMc^{-3}$, reaching 25 per cent of the first part of the primary response (not including the sharp narrow peak of X-rays re-emerging from the back side of the disc). The secondary response is broad due to the multiple light paths by which reflected emission can return to/from across the disc.

The width of the response may be quantified by the ‘half-flux interval,’ the interquartile time interval between the times at which 25 and 75 per cent of the total cumulative flux have been received. The half-flux interval of the primary iron K response in the 5–7 keV band is $9 GMc^{-3}$ when the point source is located at $h = 5r_g$. The inclusion of returning radiation increases the width of the response function to a half-flux interval of $15 GMc^{-3}$.

The blueshifted iron K line photons returning to the inner regions of the disc and scattered before being redshifted on their passage to the observer are seen in the 3.5–4.5 keV band. These scattered
Figure 12. The impulse response function of the accretion disc in response to a single flash of emission from a point source at $h = 5r_g$ as a function of time after the primary continuum emission is observed in energy bands corresponding to (a) the soft excess emission between 0.3 and 1 keV, (b) the core of the broadened iron K line between 5 and 7 keV, (c) the Compton hump, and (d) the 3.5–4.5 keV energy band containing redshifted iron K line emission and scattered, blueshifted iron K emission returning to the inner disc that is observed redshifted. In each band, the primary and secondary responses are shown in addition to the total response. The response functions are normalized according to the width of each band and the normalization is consistent between each panel.

Returning photons form a broad secondary response that extends the decaying tail of the primary response (in this energy band, the primary response consists of the most strongly redshifted line photons from the inner disc in addition to a contribution from the reflected continuum). The half-flux interval is increased from 9 to $12 \, G M c^{-3}$, increased by slightly less than the width of the response in the 5–7 keV band since a narrower range of ray paths are able to produce this blueshifted emission returning to the inner disc, though the relative flux fraction is greater since the primary reflected flux in this energy band is lower.

Returning radiation has a much smaller impact on the soft excess, shown in Fig. 12(a), where the half-flux interval is increased from 8 to just $10 \, G M c^{-3}$ and the secondary response peaks at just 2 per cent of the primary peak. On the other hand the effect on the low-energy side of the Compton hump, shown in Fig. 12(c), is much greater, with not just the average response time increasing by a factor of 2, but the half-flux interval increasing from 8 to $21 \, G M c^{-3}$, though with a strong secondary peak comprising the secondary reverberation. In the absence of returning radiation, the Compton hump responds 35 per cent sooner than the core of the iron K line, but when returning radiation is included, the response times of the core of the iron K line and of the iron K line core are comparable. The effect on the continuum-dominated 1–2 keV band is minimal and the half-flux interval in this band is unchanged.

6.2.3 Lag-frequency spectra

The time-domain impulse response functions represent the count rate as a function of time following a single flash of emission from the corona. Rather than observing a single flash of continuum emission, the accretion disc is observed responding to stochastic variability in the X-ray continuum. In this case, the observed light curve in each energy band is given by the time-series describing the variability in the primary continuum convolved with the response in that energy band.
The inclusion of returning radiation increases the average arrival time of photons, which represent the Fourier components. The characteristic black hole mass and frequencies scale as the inverse of $\tau^2$ and of a reference band (in fact the response functions of both energy bands are encoded). This is expressed as the lag-frequency spectrum; the phase of the complex cross-spectrum, that is, the time lag as a function of the low and high Fourier frequency components that make up the observed variability (Zoghbi et al. 2010; Uttley et al. 2014).

The lag-frequency spectra that are typically used to make X-ray reverberation measurements are shown in Fig. 13. Fig. 13(a) shows the time lag between the reverberating 0.3–1 keV soft X-ray band relative to the continuum-dominated 1–4 keV band. Fig. 13(b) shows the time lag between the 1–4 keV continuum band and the 4–7 keV iron K band. Fig. 13(c) shows the time lag between the 3.5–4.5 keV band in which scattered blueshifted iron K photons that return to the inner disc are expected to be observed, and the core of the iron K line in the 5–7 keV band. In each case, the full response, including both the primary and secondary reverberation response, is compared to the lag-frequency spectrum that would be produced with just the primary response.

By convention, a positive lag indicates that variability in the harder X-ray band is lagging behind that in the softer band. In the iron K bands, a positive lag indicates reverberation from the disc, while in the soft X-ray band, a negative lag indicates reverberation. Lags are expressed in units of $GMc^{-3}$, the light crossing time over $1r_g$, and frequencies are expressed in $c^3(GM)^{-1}$, one wave cycle per light crossing time over $1r_g$. These natural units can readily be converted to the measured lag times and frequencies for black holes of any mass. The characteristic light traveltime scales proportional to the black hole mass and characteristic frequencies scale as the inverse of the mass.

The effect on the measured soft lag is small over the observable frequency range. The time lag measured in the lowest frequency Fourier components represents the average arrival time of photons, integrated through the response function at all times (Wilkins & Fabian 2013). The inclusion of returning radiation increases the measured soft lag by between 12 and 25 percent at the lowest frequencies.

Typically reverberation lags are observed between $10^{-4}$ and $10^{-3}$ Hz (Kara et al. 2016), corresponding to characteristic frequencies between $5 \times 10^{-2}$ and $5 \times 10^{-3}$ $c^3(GM)^{-1}$ for a $10^6M_\odot$ black hole and 10 times lower frequencies for a $10^7M_\odot$ black hole. In observed accreting black holes, the lag spectra at low frequencies become dominated by the so-called hard lags, rather than reverberation, where variability in higher energy X-ray bands systematically lags behind that in lower energy bands, likely due to the propagation of luminosity fluctuations through the extent of the corona (Miyamoto & Kitamoto 1989; Arévalo & Uttley 2006). At high frequencies, the measured lag wraps from negative to positive once the phase of a given Fourier component is shifted by more than half a wavelength. For a lag time $\tau$, at frequency $f = 1/2\tau$ it is not possible to tell whether the sinusoidal component has been shifted forward or backward. At higher frequencies still the measured lag decays to zero. In reality, such sharp phase wrapping is not seen as coronae with finite spatial extent will not have the sharp edges in the response function that lead to this effect, and the increasing contribution of Poisson noise in the high frequency components.

In the iron K band, the inclusion of returning radiation and the secondary iron K line emission increases the average time lag between the 1–4 keV continuum-dominated band and the 4–7 keV band by 49 percent. The secondary reverberation peak in the response function is manifested in the time lag in the highest frequency components. While the time lag is increased at low frequency, the profile of the lag-frequency spectrum steepens as the lag decreases up to the phase-wrapping frequency of $0.03c^3(GM)^{-1}$. If the increased lag at low frequency were caused by an increased black hole mass or increased scale height of the primary X-ray source, it would be accompanied by a shift in the phase-wrapping frequency, which scales as $1/2\tau$. The increase in the width of the response function relative to its average response time means that the profile steepens and while the average lag shown in the low-frequency components increases by 49 percent, the phase-wrap frequency (or in realistic systems the frequency at which the lag begins to decay to zero) is unchanged.

In order to detect the delayed, the scattered blueshifted iron K emission that returns to the inner disc (seen at $3.5–4.5$ keV), we compute the time lag as a function of Fourier frequency between this band and the core of the iron K line in the 5–7 keV band, shown in Fig. 13(c). This lag-frequency spectrum shows the additional, delayed emission between these bands by 60 percent. At low frequencies, the inclusion of secondary reverberation increases the average time lag between these bands by 60 percent. This is due to the delayed iron K line emission in the secondary reverberation component and is...
also seen in the lag-energy spectrum through the steepening of the redshifted wing of the line.

The extension of the decaying tail of the response function, however, is encoded in the higher frequency Fourier components (Wilkins et al. 2020). The delayed, scattered photons from the inner disc lead to a steepening of the decay of the time lag at high frequencies. With and without the inclusion of returning radiation, the lag drops to $2GMc^{-3}$ at a frequency of $0.01c^3(GM)^{-1}$, but it declines from a lag of $11GMc^{-3}$ compared to just $7GMc^{-3}$ when only the primary reverberation is considered. It will be possible to identify this signature of returning radiation in X-ray reverberation measurements if sufficient signal-to-noise ratio is available in the $3.5–4.5$ keV band to measure the slope, requiring 30 per cent accuracy in the time lag in separate frequency bins at $10^{-3}$ and $10^{-2}c^3(GM)^{-1}$ to infer the presence of the secondary response. This secondary response in the redshifted part of the iron K line will be detected alongside an increase in the response of the iron K line with respect to the reverberating soft X-ray band and in the response time of the Compton hump.

If the accretion disc is observed closer to edge on, at a lower inclination, both the primary and secondary response functions in each energy band become narrower (at high inclination, there is a greater range of light paths between the disc and observer), though the time delay between the onset of the primary and secondary responses remains the same, since this is governed by the light traveltime as it returns from one part of the disc to another. This means that at lower inclination, the secondary response of the scattered, blueshifted iron K photons in the $3.5–4.5$ keV band is more pronounced as a secondary peak in the tail of the response function, rather than blending into the decaying tail of the primary response. This signature of returning radiation is marginally more detectable from accretion discs observed at lower inclination; the gradient of the decrease in lag with Fourier frequency increases by 60 per cent when the disc is observed at $30^\circ$ rather than $60^\circ$.

7 DISCUSSION

The reflection and reverberation of the X-ray continuum from the inner regions of the accretion disc has been observed in a number of AGN, most notably the narrow-line Seyfert 1 galaxies, as well as in accreting stellar mass black holes and neutron stars in X-ray binaries. Reflection from the inner disc is identified by the broadening of the iron K fluorescence line, with the combination of Doppler shifts and gravitational redshifts from the innermost radii on the disc producing an extended redshifted wing to the line, from the $6.4$ keV rest-frame energy of the line down to around $3$ keV (Fabian et al. 1989). Reflection from the inner parts of the disc is further identified by the detection of reverberation time lags; the time delay between variability in the primary continuum emission and the response of the reflected emission from the disc due to the additional light traveltime between the primary source and the disc (Fabian et al. 2009; Uttley et al. 2014). Time delays correspond to the light traveltime over a few gravitational radii (De Marco et al. 2013; Kara et al. 2016), indicating reflection from close to the primary X-ray source.

X-ray reflection from the inner parts of the disc provides a unique probe of the accretion flow and the strong gravity environment just outside the event horizon of a black hole. Strong light bending in the gravitational field around the black hole plays a significant role in shaping the appearance of the reflected X-ray emission. When the corona is compact and close to the black hole, a significant fraction of the continuum rays are focused towards the black hole and, hence, on to the inner regions of the accretion disc. The reflection of X-rays from regions of the disc close to the black hole means that a significant fraction of the reflected or reverberating emission will be focused back towards the black hole. The strong bending of the reflected rays in the gravitational field returns a significant fraction of the primary reflection to the disc to be reflected again; the returning radiation. When illuminated by the primary reflected emission, the plasma in the accretion disc produces a different spectrum to that produced when illuminated by the power-law continuum spectrum, while time delays between higher order reflections delay the average arrival time of the reverberating emission. It is thus important to understand the consequences of returning radiation on the appearance of X-ray reverberation around black holes.

7.1 Implications for X-ray reverberation

General relativistic ray-tracing simulations show that up to 40 per cent of the reflected X-ray emission can return to the accretion disc, depending on the primary illumination pattern and hence the height or extent of the corona.

The fraction of reflected photons that return to the disc and that are lost inside the black hole event horizon reduce the reflected flux that is able to escape to infinity to be observed. Measuring the reflection fraction, that is the ratio of the total reflected X-ray flux to the continuum flux, can indicate the compactness of the corona. When the corona is compact and confined to a small region of space close to the black hole, the number of continuum photons focused on to the inner parts of the accretion disc relative to the number able to escape to be observed as part of the X-ray continuum, increases (Fabian et al. 2012; Wilkins 2016). An isotropic point source above an infinite accretion disc in the absence of gravity, the limit of a corona far from the black hole, would produce a reflection fraction of unity, as half of the continuum is emitted into the upper hemisphere, where it can escape, and half reaches the disc. When a point source is located at $h = 2r_g$ above the black hole, strong light bending increases the reflection fraction to $R \sim 8$. Reflection fractions below unity can be explained by relativistic motion of the continuum source upwards, away from the disc (such as in a jet), beaming emission away from the disc (Beloborodov 1999).

When returning radiation and the fraction of reflected rays that are lost into the event horizon are taken into account, the observed reflection fraction can be reduced to between 39 and 57 per cent of the ‘intrinsic’ ratio between the number of rays that reach the disc and escape to infinity from the source, depending upon the scale height of the primary X-ray source. If a reflection fraction greater than unity is measured, the intrinsic value will be greater still, meaning the corona would be more compact than previously inferred. Conversely, however, if a reflection fraction less than unity is measured, relativistic beaming of emission away from the disc may be overestimated. Only if the measured reflection fraction is below around 0.6 (assuming the intrinsic fraction is always greater than unity, approaching unity for higher sources) or is inconsistent with other measurements of the corona such as those made from the emissivity profile of the disc, it is necessary to invoke beaming to explain the reflection fraction, such as in X-ray flares observed from Markarian 335 where the reflection fraction was measured to be 0.34 (Wilkins et al. 2015).

Returning radiation does not significantly alter the emissivity profile of the accretion disc; that is the radial dependence of the reflected X-ray flux. It will therefore not affect interpretation of true, intrinsic emissivity profile in terms of the height and spatial extent of the corona over the surface of the accretion disc that is inferred (Wilkins & Fabian 2012). The time-averaged spectrum, however, is
altered. Returning radiation enhances the observed flux in the iron Kα line above the continuum by 25 per cent (see also Ross et al. 2002), and in the Compton hump, between 10 and 30 keV, by a factor of 3. The enhancement of the Compton hump depends upon the slope of the primary continuum spectrum and is greatest when the disc is illuminated by a steeply falling continuum. Enhancement in the observed iron Kα line flux may go part way to explaining the supersolar abundance of iron required to fit the observed spectra of AGN, which is difficult to fully explain. It is unlikely however that an enhancement of only 25 per cent in the line will fully account for iron abundances more than 10 times solar that have been reported (e.g. Jiang et al. 2018).

The most significant impact of returning radiation is an increase in reverberation time-scales of the continuum from the accretion disc. The additional light traveltime between the primary and secondary reflection points on the disc delays the average arrival time of the reverberating emission in regions of the spectrum where returning radiation contributes most significantly. Time lags measured between the 1–4 keV continuum band and 4–7 keV iron K band are increased by 49 per cent.

The reverberation time between the primary continuum and the reflection from the accretion disc indicates the scale height of the corona above the plane of the disc. This represents the height of a compact point-like source above the black hole, or the vertical extent of an extended corona above the disc. Lag times are relatively insensitive to the radial extent of the corona over the surface of the disc (Wilkins & Fabian 2013). Measuring the reverberation time lag between the continuum and iron K line can cause the scale height of the corona to be overestimated by up to 39 per cent if the effect of returning radiation is not taken into account. From iron line reverberation time-scales, coronae are found to be compact, typically lying between 2 and 9rg above the accretion (Kara et al. 2016). Accounting for the effect of returning radiation reinforces the conclusion that coronae are compact, potentially reducing the scale height of the corona to be overestimated by up to 39 per cent from the measured value. Dilution of the measured lag by the contribution of the continuum emission to the reflection-dominated band, and vice versa, has the opposite effect and must also be accounted for, however. Dilution can reduce the measured lag from the intrinsic value by up to 50 per cent (Wilkins & Fabian 2013a; Kara et al. 2013a; Cackett et al. 2014), depending on specific details of the spectrum of the system in question. An accurate estimate of the corona scale height requires simultaneous analysis of the reverberation time-scales and the spectrum.

While the reverberation time-scale in the iron K band is increased by 49 per cent when returning radiation is included, the measured time lag between the continuum-dominated band and the 0.3–1 keV band dominated by the reverberating soft excess from the disc (where Fabian et al. 2009 first reported the detection of X-ray reverberation) is increased to a much lesser extent. This is because returning radiation contributes significantly to the 1–2 keV band.

The effects of returning radiation were calculated in detail for a disc illuminated by a point source located at $h = 5r_g$ above the singularity, corresponding to the average scale height of corone indicated by measured samples of X-ray reverberation lags. For sources closer to the black hole, the inner disc is more strongly illuminated, in turn increasing the returning fraction from 39 per cent to 47 percent as the source is moved from $h = 5$ to $1.5r_g$. A compact corona, located closer to the black hole, would lead to a stronger relative contribution of returning radiation, further enhancing the spectral features and corresponding reverberation time lags. Conversely, a corona located further from the black hole would weaken the impact of returning radiation. We find that the impact of returning radiation on the reflection spectrum and reverberation

![Figure 14](https://academic.oup.com/mnras/article/498/3/3302/5896458)

### Figure 14

The relationship between the soft X-ray lag (measured between the 0.3–1 and 1–5 keV bands) from De Marco et al. (2013) and the iron K lag (measured between the the 1–4 and 4–7 keV bands) from Kara et al. (2016) in a sample of Seyfert galaxies. The dashed line shows the predicted ratio between the soft X-ray lag and iron K lag if only the primary reverberation is included in the model (a factor of 1.4 between the soft X-ray and iron K lag). The vast majority of the observed AGN show longer than predicted iron K lags. A linear fit to the sample is shown by the solid line, consistent with the prediction of the reverberation model including returning radiation.

The time-scales are not strongly affected by the inclination angle at which the accretion disc is viewed, although observing the disc closer to face on sharpens the response function of the blueshifted iron K photons returning to the inner disc, marginally increasing their detectability in lag versus Fourier frequency measurements.

#### 7.1.1 Returning radiation in measured reverberation lags

Returning radiation may offer an explanation to the offset in the sample of reverberation lags that are measured by De Marco et al. (2013) in the soft X-ray band and by Kara et al. (2016) in the iron K band. We note that the soft X-ray lags are defined between the 0.3–1 keV and 1–5 keV band, rather than the more commonly used 1.2–4 keV band. The median lag, normalized by black hole mass, in the iron K sample corresponds to the light traveltime over $5.2r_g$ (with the 25th and 75th percentiles at 2.6 and 10.4 $GMc^{-1}$). In the soft lag sample, the median lag corresponds to $2.3r_g$ (with 25th and 75th percentiles at 1.6 and 2.8 $GMc^{-1}$). The median lag between the continuum and iron K band is longer than that in the soft X-ray band by a factor of 2.

The model of only the primary reverberation from the disc (with continuum photon index $\Gamma = 3$, ionization parameter $\xi = 50$ erg cm s$^{-1}$, iron abundance $A_{Fe} = 8$, and reflection fraction $R = 1.5$) predicts a ratio of just 1.4 between the iron K and soft lags. The difference in reverberation lag between the two bands is due to different relative contributions of the primary continuum to the two bands, producing different dilution factors. When returning radiation is included, the predicted ratio between the iron K and soft reverberation lags is 2.1, in closer agreement to the measured sample, illustrated in Fig. 14. The predicted ratio of 2.1 will vary depending upon the height of the corona in each AGN, as well as the ionization and iron abundance in the accretion disc, producing the observed scatter scatter around the linear relation, and indeed it is largely those AGN showing longer reverberation lags (with a larger coronal scale height, and thus a lesser influence of returning radiation) that exhibit a smaller ratio, closer to 1.4.
This simple calculation demonstrates that reflected emission returning to the accretion disc in the strong gravitational field around the black hole can, in part, explain the offset between measured X-ray reverberation lags in the iron K and soft X-ray bands, that are not explained by simple reverberation models. Reverberation measurements in Seyfert galaxies show some evidence of returning radiation around the black hole. Furthermore, returning radiation is only expected to have a significant impact when the black hole is rapidly spinning and the inner radius of the disc is close to the event horizon, reinforcing the conclusion that many astrophysical black holes in AGN are rapidly spinning.

This calculation does not, however, account for the specific spectral shape in each member of the sample, which can vary due to different coronal heights or extents or different ionization states of the reflecting accretion disc, which may alter the specific ratio of the lags in each source, or variation in black hole spin across the sample, which will change the contribution of returning radiation. Accounting for this effect would require spectral analysis of each individual source. Moreover, the propagation of luminosity fluctuations through the corona (Wilkins et al. 2016) or additional emission processes that contribute to the soft X-ray emission (Gardner & Done 2014) will further alter the profile of the lag-energy spectrum. Detailed modelling of X-ray reverberation around black holes should include the additional time delays imparted by reflected radiation returning to the disc.

In addition to the ratio between measured X-ray reverberation lags in the iron K line and in the soft X-ray band, we may examine lags that have been measured in the Compton hump emission with NuSTAR. The lag at the peak of the Compton humps in MCG–5–23–16 (Zoghbi et al. 2014), Swift J2127.4 + 5654, and NGC 1365 (Kara et al. 2015) are observed to be between 1 and 3 times the lag at the peak of the iron K line, relative to the 2 keV continuum, given uncertainties in the data. The simple point source reverberation model predicts that the Compton hump lag is 0.6 times the lag at the peak of the iron K lag. When returning radiation is included, the Compton hump lag is expected to be 1.1 times that in the iron K band, in agreement with the observations.

7.2 Direct detection of strong light bending

General Relativity predicts that the trajectories of light rays passing close to a black hole should be strongly bent by the gravitational field. This includes photons that are emitted or scattered from the innermost regions of the accretion disc, a significant fraction of which should be brought back to the accretion disc to be reflected again. If a direct signature of this returning radiation can be detected in X-ray reverberation observations, it would constitute a direct test of strong light bending around the black hole, as predicted by General Relativity. Because returning radiation is only significant around rapidly spinning black holes, the detection of returning radiation would confirm the rapid spin of a black hole.

Relativistic effects and strong light bending are manifested in multiple aspects of the X-ray reflection and reverberation that is detected. The combination of Doppler shifts and gravitational redshifts determines the energy shift observed in emission-line photons, while light bending towards the black hole and hence on to the inner regions of the disc in part explains the brightness of the redshifted wing of the observed iron Kα line, with the emissivity profile falling off steeply from the most strongly irradiated inner radii of the disc. This steepening is also in part explained by time dilation, blueshifting emission that lands on the inner parts of the disc closest to the black hole (Wilkins & Fabian 2012). A direct detection of returning radiation would identify a further impact of strong light bending in General Relativity.

Returning radiation needs to be factored into models of X-ray reverberation to explain the observed time lags and the relative lag in different energy bands. Indeed, while the observed ratios between the soft X-ray reverberation lag and the iron K lag, and the iron K and Compton hump lags are not consistent with simple reverberation models from X-ray point sources, they are consistent with models that include the secondary reflection from returning radiation.

The enhancement of the iron K lag with respect to the soft X-ray lag and shifts in the profile of the lag-energy spectrum are, however, likely degenerate with other parameters of the system. The height or extent of the X-ray source above the disc varies the amplitude of the reverberation lag, while variations in the ionization parameter and iron abundance alter the relative contributions of the soft excess, the line emission and the continuum to each energy band. Combinations of parameters could be found that explain the lag amplitude and the variation in lag as a function of energy that do not invoke returning radiation, although detecting a systematic offset in the soft X-ray and iron K lags in a sample of objects limits the degree to which parameters can be fine-tuned to mimic returning radiation. Moreover, it is difficult to explain such a significant increase in the Compton hump lag with respect to the iron K lag without significantly altering the underlying rest-frame reflection model.

The detection of returning radiation in X-ray reverberation measurements would be validated through the detection of specific features of the secondary reflection spectrum. Detection of the bright secondary peak in the response function of the Compton hump, or of the blueshifted iron K photons that return to the inner disc would confirm the presence of returning radiation in strong gravity around the black hole. These photons are blueshifted as they return under strong gravity to the inner parts of the disc, having originated further out. Upon hitting the disc, the majority of these photons are Compton scattered, so re-emitted at their blueshifted energy, producing a line-like feature at around 12 keV in the local rest frame. The photons are then redshifted between the inner disc and the observer. These photons can be separated from other features in the spectrum by their response time, most notably in the 3.5–4.5 keV energy band.

These delayed photons produce a broad response function that extends the decay tail of the primary response in this energy band. This is encoded in the time lags of the response in this band as a function of the Fourier frequency components that make up the slow and fast components of the variability. Measuring the time lags between this 3.5–4.5 and the 5–7 keV bands (the core of the iron K line) brings out the additional response from the inner disc. The average lag between these bands in the lowest frequency components is increased, and the slope with which the lag decays towards high frequencies is steepened. X-ray spectral timing measurements will be sensitive to this additional response due to radiation returning to the inner disc if the time lag can be measured to 30 per cent accuracy in separate frequency bins at frequencies of $10^{-3}$ and $10^{-5}c^2/(GM)$. For a $10^8M_\odot$ black hole, this corresponds to the lag dropping from 35 to 10 s over the frequency range 0.2 to $2 \times 10^{-3}$ Hz. For a $10^7M_\odot$ black hole, the lag increases from 350 to 100 s between 0.2 and $2 \times 10^{-4}$ Hz.

7.2.1 Prospects with future missions

Observing bright Seyfert galaxies, such as Ark564 (Kara et al. 2013b), using XMM–Newton, it is possible to measure the lag in the 3.5–4.5 keV energy band in two frequency bins between 0.2
and $2 \times 10^{-3}$Hz with 1σ uncertainty of 50 per cent. At these high frequencies, the limited count rate means that the variability becomes dominated by Poisson noise. In order to detect signatures of returning radiation, it is necessary to reduce this uncertainty by a factor of 6 (for a 3σ feature).

When time lags are measured in the low frequency (i.e. mHz) Fourier components, as for supermassive black holes, many photons are collected per wave cycle but few wave cycles are recorded per observation. The uncertainty for count rate $N$ scales as $\sqrt{N}$ (Uttley et al. 2014). The next-generation X-ray observatory, Athena (Barcons et al. 2017), will provide 1.4 m$^2$ collecting area between 1 and 2 keV, and 2500 cm$^2$ at 6 keV, providing increased sensitivity over XMM–Newton by factors of 16 and 3 in these bands. The proposed, specialized X-ray timing mission, STROBE-X (Ray et al. 2018) is planned to carry two non-imaging instruments with large collecting areas. Due to its lower background, the X-ray Concentrator Array will be better suited to observations of AGN, providing six times the effective area of Athena at 6 keV, while the Large Area Detector, with 5–10 m$^2$ effective area at 6 keV, will enable timing between 2 and 30 keV. This will enable delays due to returning radiation to be detected in the Compton hump around stellar mass black holes in bright X-ray binaries.

Reducing the uncertainty in the high-frequency Fourier components by a factor of 4 with Athena or STROBE-X holds the potential to observe direct signatures of returning radiation and strong light bending. In particular, observations of AGN that have dropped into low flux states in which the corona has contracted to a confined region close to the black hole (Fabian et al. 2012; Parker et al. 2014; Wilkins & Gallo 2015) exhibit X-ray spectra strongly dominated by reflection from the inner accretion disc. Observations of such states with large collecting area observatories will be powerful in detecting signatures of strong light bending close to black holes.

8 CONCLUSIONS

Reflected X-ray emission from accretion discs that returns to the disc in the strong gravitational field around a black hole to produce higher order reflections alters the observed spectrum of the reflected X-ray emission, as well as the reverberation time lags that are measured between variability in the X-ray continuum and in its reflection.

When the accretion disc is illuminated by a simplified model of point source, located a height $h = 5r_g$ above the singularity, up to 40 per cent of the reflected emission is returned to the disc by light bending in the strong gravitational field. As the X-ray emitting corona becomes more compact, the returning fraction increases to up to 47 per cent when the source is within $1.5r_g$ of the singularity.

The reduction in the fraction of photons reflected from the inner disc that are able to escape to be observed reduces the measured reflection fraction, which can be used to estimate the extent of the corona, to between 39 and 57 per cent of its intrinsic value.

Returning radiation modifies the observed spectrum of the reflected emission, enhancing the iron Ka line flux by 25 per cent. The Compton hump is enhanced by up to a factor of three when the accretion disc is illuminated by a steep power-law continuum spectrum with photon index $\Gamma = 3$. The enhancement in the Compton hump is reduced to a factor of 2 when $\Gamma = 2.4$ and when $\Gamma = 2$, only the low-energy side of the Compton hump is enhanced, by a factor of 1.35.

The additional light traveltime between primary and secondary reflections increases the reverberation time lag that is measured between the continuum-dominated 1–4 and the 4–7 keV bands in which the reverberating iron K line is observed, by 49 per cent, while time lags between the continuum and the 0.3–1 keV band, dominated by the reverberating soft excess, are increased by only 25 per cent. The corresponding overestimate of the distance between the corona and the accretion disc measured from reverberation in the iron K line reinforces the conclusion that the X-ray emitting corona around black holes are compact.

Returning radiation increases the ratio between the measured reverberation lag times in the iron K band and the soft X-ray excess. Including secondary reverberation, the ratio between the iron K and soft X-ray lags, each relative to the continuum, is increased to 2.1 (compared to a ratio of 1.4 expected from a simple point source reverberation model). The reverberation lag time of the Compton hump is increased significantly to be comparable to the iron K lag. Measured samples of soft X-ray, iron K and Compton hump reverberation lags, while being inconsistent with simple point source reverberation models, can be explained by the effects of returning radiation in strong gravity around the black hole.

Reflected X-rays returning to the accretion disc in strong gravity are uniquely identified by iron K line photons that are blueshifted as they return to the innermost regions of the disc. These photons are predominantly Compton scattered, producing a blueshifted feature around 12 keV in the rest-frame spectrum. This is redshifted to the 3.5–4.5 keV band when it is observed, significantly delayed with respect to the primary reflection. Returning, blueshifted iron K line photons in the 3.5–4.5 keV band and a strong secondary peak in the response of the Compton hump represent a signatures of strong light bending as predicted by General Relativity, that will be detectable through X-ray spectral timing observations that can be conducted with the next-generation X-ray observatories.

ACKNOWLEDGEMENTS

DRW was supported by NASA for this work, through Einstein Postdoctoral Fellowship grant number PF6-170160, awarded by the Chandra X-ray Center, operated by the Smithsonian Astrophysical Observatory for NASA under contract NAS8-03060. JAG acknowledges support from NASA grant 80NSSC17K0345, from the Alexander von Humboldt Foundation, and from the International Space Science Institute (ISSI), Bern, Switzerland, as a member of the International Teams 458 and 486. Computing for this project was performed on the Sherlock cluster. DRW thanks Stanford University and the Stanford Research Computing Center for providing computational resources and support. We thank the anonymous referee for their feedback on the original version of this manuscript.

DATA AVAILABILITY

Simulation codes and resulting data sets are available on request to the corresponding author. X-ray reverberation measurements are published in De Marco et al. (2013) and Kara et al. (2016) and the raw data may be obtained from the XMM–Newton Science Archive (http://nxsa.esac.esa.int/nxsa-web).

REFERENCES

Agol E., Krolik J. H., 2000, ApJ, 528, 161
Arévalo P., Uttley P., 2006, MNRAS, 367, 801
Barcons X. et al., 2017, Astron. Nachr., 338, 153
Beloborodov A. M., 1999, ApJ, 510, L123
Brenneman L. W., Reynolds C. S., 2006, ApJ, 652, 1028

MNRAS 498, 3302–3319 (2020)
Returning radiation around black holes

Cackett E. M., Zoghbi A., Reynolds C., Fabian A. C., Kara E., Uttley P., Wilkins D. R., 2014, MNRAS, 438, 2980
Collin S., Coupé S., Dumont A. M., Petrucci P. O., Rózańska A., 2003, A&A, 400, 437
Connors R. M. T. et al., 2020, ApJ, 892, 47
Cunningham C., 1976, ApJ, 208, 534
Dabrowski Y., Lasenby A. N., 2001, MNRAS, 321, 605
Dabrowski Y., Fabian A. C., Iwasawa K., Lasenby A. N., Reynolds C. S., 1997, MNRAS, 288, L11
Dauser T. et al., 2012, MNRAS, 422, 1914
Dauser T., García J., Walton D. J., Eikmann W., Kallman T., McClintock J., Wilms J., 2016, A&A, 590, A76
De Marco B., Ponti G., Cappi M., Dadina M., Uttley P., Cackett E. M., Fabian A. C., Miniutti G., 2013, MNRAS, 431, 2441
Fabian A. C. et al., 2009, Nature, 459, 540
Fabian A. C. et al., 2012, MNRAS, 419, 116
Fabian A. C., Rees M. J., Stella L., White N. E., 1989, MNRAS, 238, 729
Gallo L. C., 2006, MNRAS, 368, 479
García J. et al., 2014, ApJ, 782, 76
García J., Kallman T. R., 2010, ApJ, 718, 695
García J., Kallman T. R., Mushotzky R. F., 2011, ApJ, 731, 131
García J., Dauser T., Reynolds C. S., Kallman T. R., McClintock J. E., Wilms J., Eikmann W., 2013, ApJ, 768, 146
Gardner E., Done C., 2014, MNRAS, 442, 2456
George I. M., Fabian A. C., 1991, MNRAS, 249, 352
Haardt F., Maraschi L., 1991, ApJ, 380, L51
Jiang J. et al., 2018, MNRAS, 477, 3711
Kara E. et al., 2015, MNRAS, 446, 737
Kara E., Fabian A. C., Cackett E. M., Steiner J. F., Uttley P., Wilkins D. R., Zoghbi A., 2013a, MNRAS, 428, 2795
Kara E., Fabian A. C., Cackett E. M., Uttley P., Wilkins D. R., Zoghbi A., 2013b, MNRAS, 434, 1129
Kara E., Alston W. N., Fabian A. C., Cackett E. M., Uttley P., Reynolds C. S., Zoghbi A., 2016, MNRAS, 462, 511
Miniutti G., Fabian A. C., 2004, MNRAS, 349, 1435
Miyamoto S., Kitamoto S., 1989, Nature, 342, 773
Parker M. L., Wilkins D. R., Fabian A. C., Grupe D., Dauser T., Matt G., Harrison F. A., 2014, MNRAS, 443, 1723
Ray P. S. et al., 2018, Proc. SPIE, Vol. 10699, Astronomical Telescopes and Instrumentation, p. 1069919
Reynolds C. S., Young A. J., Begelman M. C., Fabian A. C., 1999, ApJ, 514, 164
Ross R. R., Fabian A. C., 2005, MNRAS, 358, 211
Ross R. R., Fabian A. C., Ballantyne D. R., 2002, MNRAS, 336, 315
Shapiro I. I., 1964, Phys. Rev. Lett., 13, 789
Suebsuwong T., Malzac J., Jourdain E., Marcowith A., 2006, A&A, 453, 773
Svoboda J., Dovcik M., Goosmann R. W., Karas V., 2010, in Comastri A., Angelini L., Cappi M., eds, AIP Conference Proceedings, Vol. 1248, Proceedings of the International Conference. p. 515
Taylor C., Reynolds C. S., 2018, ApJ, 855, 120
Thorne K. S., 1974, ApJ, 191, 507
Uttley P., Cackett E. M., Fabian A. C., Kara E., Wilkins D. R., 2014, A&ARv, 22, 72
Wilkins D. R., 2016, Astron. Nachr., 337, 557
Wilkins D. R., Fabian A. C., 2011, MNRAS, 414, 1269
Wilkins D. R., Fabian A. C., 2012, MNRAS, 424, 1284
Wilkins D. R., Fabian A. C., 2013, MNRAS, 430, 247
Wilkins D. R., Gallo L. C., 2015, MNRAS, 449, 129
Wilkins D. R., Gallo L. C., Grupe D., Bonson K., Komossa S., Fabian A. C., 2015, MNRAS, 454, 4440
Wilkins D. R., Cackett E. M., Fabian A. C., Reynolds C. S., 2016, MNRAS, 458, 200
Wilkins D. R., Reynolds C. S., Fabian A. C., 2020, MNRAS, 493, 5532
Zoghbi A. et al., 2014, ApJ, 789, 56
Zoghbi A., Fabian A. C., Uttley P., Miniutti G., Gallo L. C., Reynolds C. S., Miller J. M., Ponti G., 2010, MNRAS, 401, 2419
Zoghbi A., Fabian A. C., Reynolds C. S., Cackett E. M., 2012, MNRAS, 422, 129
Zoghbi A., Reynolds C., Cackett E. M., Miniutti G., Kara E., Fabian A. C., 2013, ApJ, 767, 121

This paper has been typeset from a \TeX/\LaTeX file prepared by the author.