Enhancing advance encryption standard security based on dual dynamic XOR table and mixcolumns transformation

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ABSTRACT
An efficient approach to secure information is critically needed at present. Cryptography remains the best approach to achieve security. On this basis, the National Institute of Standards and Technology (NIST) selected Rijndael, which is a symmetric block cipher, as the advanced encryption standard (AES). The MixColumns transformation of this cipher is the most important function within the linear unit and the major source of diffusion. Dynamic MixColumns transformation can be used to enhance the AES security. In this study, a method to enhance the AES security is developed on the basis of two methods. The first method is an extension of a previous study entitled “A novel Approach for Enhancing Security of Advance Encryption Standard using Private XOR Table and 3D chaotic regarding to Software quality Factor.” In the current study, the fixed XOR operation in AES rounds is replaced with a dual dynamic XOR table by using a 3D chaotic map. The dual dynamic XOR tables are based on 4 bits; one of the xor tables is used for even rounds, and the other is used for odd rounds. The second method is dynamic MixColumns transformation, where the maximum distance separable (MDS) matrix of the MixColumns transformation, which is fixed static and public in every round, is replaced with a private dynamic MDS matrix utilizing 3D chaotic map. A 3D chaotic map is used to generate secret keys. These replacements enhance the AES security, particularly the resistance against attacks. Diehard and NIST tests, entropy, correlation coefficient, and histogram are used for security analysis of the proposed method. C++ is used to implement the proposed and original algorithms. MATLAB and LINX are used for the security analysis. Results show that the proposed method is better than the original AES.

Keywords: 3D chaotic map, AES, Dynamic XOR, Mixcolumns, NIST

1. INTRODUCTION
Safekeeping of information has been a trouble of concern over the past several decades. Nowadays, people exchange large amounts of data over unconfident channels, where any private data can be unprotected [1, 2]. Cryptography is probably the most important data protection technology. Numerous encryption algorithms have been developed to ensure data security. To establish an advanced encryption standard (AES), the National Institute of Standards and Technology (NIST) has selected Rijndael, a widely used symmetric key encryption standard, particularly when data confidentiality is a critical issue. This highly efficient cipher is particularly appropriate for encrypting relatively long plain data [1-3]. Three versions of AES based on key
length are conducted: AES-128, AES-192, and AES-256. The keys are represented in arrays with sizes of $4 \times 4$, $4 \times 6$, and $4 \times 8$, respectively. Among these arrays, a state is when 128-bit block data are arranged in a $4 \times 4$ array. Originally, four successive transforms are conducted on a state in 10, 12, or 14 rounds based on key length [4, 5].

The MixColumns transformation of the AES is one of the critical components and the responsible for diffusion. It plays an important role with respect to the wide trail strategy of the cipher. Each column is treated as a polynomial using Galois Field (GF) of $2^8$. Modulo $x^4 + 1$ is multiplied by a fixed polynomial $c(x)=3x^3+x^2+x+2$. The inverse of this polynomial is $C^{-1}(x) = 11x^3+13x^2+9x+14$. The MixColumns transformation can be performed by multiplying a coordinate vector of the four numbers within the Rijndael's Galois field with the circulated maximum distance separable (MDS) matrix as following.

\[
\begin{bmatrix}
  b_0 \\
  b_1 \\
  b_2 \\
  b_3 \\
\end{bmatrix} = \begin{bmatrix}
  2 & 3 & 1 & 1 \\
  1 & 2 & 3 & 1 \\
  1 & 1 & 2 & 3 \\
  3 & 1 & 1 & 2 \\
\end{bmatrix} \begin{bmatrix}
  a_0 \\
  a_1 \\
  a_2 \\
  a_3 \\
\end{bmatrix}
\]

The math operation is conducted within the median Rijndael’s Galois field, thus resulting in a complicated multiplication operation, whereas the addition operation is simple [5-7]. Figure 1 shows the AES MixColumns transformation.

![AES MixColumns transformation](image)

The analysis of AES resistance to differential and linear cryptanalyses shows that random, unknown, and key-dependent permutations can enhance the resistance of block ciphers against differential and linear cryptanalyses and that block ciphers can be completely dynamic and unknown to such cryptanalyses. Therefore, dynamic MixColumns transformation can be applied to improve the AES security [7-9]. The fixed XOR table can be replaced with a dynamic XOR table during rounds in the AES factor for improving the AES security as well [1]. Chaos has competitive advantages, such as high sensitivity to initial values, ergodicity, mixing property, deterministic dynamics, and structure complexity. Consequently, chaos theory has attracted extensive attention from the field of cryptography [2, 9, 10]. On this basis, secret keys are in this study to enhance the AES security.

Many related studies proposed different techniques for enhancing the security of AES. The predefined XOR operation is replaced with a novel private XOR table during rounds in AES by using a 3D chaotic map as a private key [1]. The MixColumns transformation in the AES is replaced with dynamic MixColumns transformation on the basis of DNA processes and structure, which rely on keys [7]. MixColumns transformation in the AES is replaced by an alike dynamic MixColumns transformation. A dynamic MixColumns transformation includes dynamic MDS matrices, which are based on the default MDS matrix of AES and m-bit additional key. Here, m is a variable length that does not exceed the product of 31.97 and one less the number of encryption rounds [6]. S-boxes bank as a rotor mechanism and dynamic key MDS matrix is used in AES algorithm. However, in this manner, the AES becomes key dependent to enhance its resistance to frequency attacks [11]. The conservation of various good cryptographic assets of MDS matrices direct exponent transformation is reported. This report has important applications in constructing dynamic diffusion layers for block ciphers. The strength of ciphers against developing cryptanalyses can be enhanced by dynamic MDS diffusion layers [12]. Dynamic MDS matrices are generated.
from direct exponent and scalar multiplication transformations on the basis of the original MDS matrices. Then, they calculated the outputs and inputs of these matrices when they are available. They reported that encryption and decryption by the dynamic MDS matrices is performed fastly by salvaging the original MDS matrices. An easy calculation for the direct exponent of MDS matrices based on a lookup table is presented [13]. The MixColumns Transformation in AES is replaced by used Bit Permutation since bit permutation is easy to implement and it does not have any complex mathematical computation [14]. In this study, the AES security is enhanced by two approaches. In the first approach, the fixed XOR is replaced with a dual dynamic XOR; one is used for odd rounds, whereas the other is used for even rounds. In the second approach, the fixed MDS matrix of the MixColumns transformation is replaced with a dynamic MDS matrix for all rounds. In both approaches, 3D Chebyshev is used to generate secret keys.

The remainder of the paper is organized as follows: In the second section, the properties of the chaotic map are explained. In the third section, the proposed algorithm is detailed. In the fourth section, the security of the proposed algorithm is analyzed and compared with that of the original AES. Finally, in the fifth section, future work and conclusions are presented.

2. CHAOTIC MAP

In the past two decades, chaos theory has been extensively applied in scientific fields such as mathematics, physics, computer science, and engineering. Cryptography, which is a branch of mathematics and computer science, has attracted considerable attention. The intrinsic features of chaotic maps support the use of such maps in the design of such algorithms. These properties comprise highly sensitive dependence on initial condition and control parameter, ergodicity, unpredictability, mixing, and random-like behavior. These properties are comparable with the confusion and diffusion assets of Shannon entropy. Therefore, chaotic dynamic is expected to provide a fast and easy way for building cryptography systems. Recently, researchers have studied high-dimensional chaotic systems to enlarge key space and address the issue of weak security; as a result of such intensive study, 2D chaotic maps have been generalized to 3D chaotic maps, such as 3D baker’s map, 3D Cat map, 3D logistic map, and 3D Chebyshev, for designing a secure symmetric scheme that enhances cryptosystem security [1, 9, 10, 15-17, 18].

a) 3D CHEBYSHEV

The private keys which are necessary in the encryption are generated by the chebyshev polynomials. The Chebyshev polynomial \( F_n(x) \) of the first type, which is a polynomial in \( x \) of degree \( n \), is a prototype of a chaotic map and is defined as follows:

\[
\begin{align*}
F_2(x) &= 2 \times x^2 - 1 \\
F_3(y) &= 4y^3 - 3y \\
F_4(z) &= 8z^4 - 8z^2 + 1
\end{align*}
\]

Chebyshev polynomial map \( F_p: [-1,1] \rightarrow [-1,1] \) of degree \( p \), when \( p \geq 1 \) [9, 10, 19, 20]

3. PROPOSED ALGORITHM

The proposed algorithm is executed as follows:

a) Three starting parameters of the 3D Chebyshev are initialized to obtain the sequences that will be used as secret keys.

b) Secret keys are generated from a 3D Chebyshev map by using (1)–(3).

c) The generated secret keys are converted from the above point to the decimal by using the following equations:

\[
\begin{align*}
x_{i,j} &= (x_{i,j} \times 10^{10} \mod 16), (4) \\
y_{i,j} &= (y_{i,j} \times 10^{10} \mod 16), (5) \\
z_{i,j} &= (z_{i,j} \times 10^{10} \mod 4), (6)
\end{align*}
\]

d) The secret keys are stored in three arrays: two \( 16 \times 16 \) arrays for \( x \) and \( y \) sequences and \( 4 \times 4 \) for \( Z \) sequences.

e) Steps are taken to ensure that the arrays of the \( X \) and \( Y \) sequences follow the features reported in a previous paper [1].

f) The array of the \( X \) and \( Y \) sequences is used for odd and even rounds, respectively.

g) The numbers in the arrays of the \( Z \) sequences are ensured to be between 0–3 without any repeat value in each row. These values will represent the new positions of values in the MDS matrix of the
Enhancing advance encryption standard security based on dual dynamic XOR

Adnan Ibrahem Salih

MixColumns transformation.

Figures 2 and 3 present the dynamic XOR tables for the even and odd rounds, respectively.

| Original MDS | Secret keys | Dynamic MDS |
|--------------|-------------|-------------|
| 2 3 1 1 3 2 0 1 1 1 2 3 | 1 2 3 1 2 3 1 0 3 1 2 1 |
| 1 1 2 3 1 0 3 2 1 1 3 2 | 3 1 1 2 1 2 0 1 2 3 1 3 1 2 |

As shown in the above figure, the first row of the original MDS is permuted on the basis of the values of the secret keys. The first row of the secret keys comprises 3, 2, 0, and 1. The fourth value of the original MDS will be the first value in the dynamic MDS. This action is repeated for the third value, then the first value, and finally the second. The same process is performed for the second, third, and fourth rows.

4. EXPERIMENTAL RESULTS

The proposed algorithm is implemented in C++ on 128 different sequences, where every sequence is $10^6$ bits. Some criteria of the security analysis, such as the NIST test, are applied by using LINUX. Other criteria are used with MATLAB R2018a (Mathworks) on a computer with Windows 7 64-bit, Intel Core i5-4500U processor, 4 GB RAM, and 1600 MHz CPU clock speed. The following initial values of the 3D Chebyshev maps are used in all experiments:

For the 3D Chebyshev map, $x_0 = 0.234$, $y_0 = -0.398$, and $z_0 = -0.88$.

5. SECURITY ANALYSIS

In this section, the security of the proposed algorithm is analyzed using different criteria and compare with the original algorithm.

5.1. Nist Test

Randomness is a necessary property for a suitable encryption algorithm and is one of the important factors used to amount the confusion and diffusion assets of a novel cryptography system. The NIST test is
a statistical test suite used to test the randomness of any cryptographic algorithm. This test suite judges whether the outputs of the algorithms under assured test settings show assets that can be deemed to be arbitrarily produced outputs. The NIST test develops a statistical package that comprises of 15 tests. The proposed algorithm generates 128 different sequences with 128 different 16-byte keys, each with \( 10^6 \) bits. The \( P \) value is calculated in accordance with each corresponding sequence across all the 15 tests. The results are presented in Tables 1 and 2 for the proposed and the original algorithms respectively. The sequences pass all the 15 tests for the proposed algorithm while fail in FFT test for the original algorithm. Therefore, the proposed algorithm has good randomness and better than from the original algorithm. The symbol \( \checkmark \) in the below tables indicates a passing result while the symbol \( \times \) in Table 2 indicated a failing result [11, 15, 21-23].

| No | Test | Success sequence \( P \) value | Proportion successful | Assessment |
|----|------|---------------------------------|-----------------------|------------|
| 1  | Frequency | 0.949602 | 0.984375 | \( \checkmark \) |
| 2  | Block frequency | 0.026648 | 0.9921875 | \( \checkmark \) |
| 3  | Accumulative sums (forward) | 0.509934 | 0.984375 | \( \checkmark \) |
|    | Accumulative sums (reverse) | 0.082177 | 0.984375 | \( \checkmark \) |
| 4  | Run | 0.517442 | 0.984375 | \( \checkmark \) |
| 5  | FFT | 0.534146 | 1 | \( \checkmark \) |
| 6  | Non-overlapping template | 0.116519 | 0.9921875 | \( \checkmark \) |
| 7  | Overlapping template | 0.100508 | 0.96875 | \( \checkmark \) |
| 8  | Universal | 0.404758243 | 0.990234375 | \( \checkmark \) |
| 9  | Approximate entropy | 0.452799 | 0.984375 | \( \checkmark \) |
| 10 | Long run | 0.023812 | 0.9765625 | \( \checkmark \) |
| 11 | Rank | 0.299251 | 0.9921875 | \( \checkmark \) |
| 12 | Random excursions | 0.554822125 | 0.993421053 | \( \checkmark \) |
| 13 | Random excursions variants | 0.466392 | 0.989473684 | \( \checkmark \) |
| 14 | Serial 1 | 0.000316 | 1 | \( \checkmark \) |
|    | Serial 2 | 0.110952 | 0.984375 | \( \checkmark \) |
| 15 | Linear complexity | 0.756476 | 1 | \( \checkmark \) |

Table 1 Results of NIST test for proposed algorithm

| No | Test | Success sequence \( P \) value | Proportion successful | Assessment |
|----|------|---------------------------------|-----------------------|------------|
| 1  | Frequency | 0.550148 | 0.9921875 | \( \checkmark \) |
| 2  | Block frequency | 0.481243 | 0.9765625 | \( \checkmark \) |
| 3  | Accumulative sums (forward) | 0.538846 | 0.9921875 | \( \checkmark \) |
|    | Accumulative sums (reverse) | 0.538846 | 0.9921875 | \( \checkmark \) |
| 4  | Run | 0.432788352 | 0.96875 | \( \checkmark \) |
| 5  | FFT | 0.522352 | 0.9765625 | \( \checkmark \) |
| 6  | Non-overlapping template | 0.513129813 | 1 | \( \checkmark \) |
| 7  | Overlapping template | 0.148899 | 0.640625 | \( X \) |
| 8  | Universal | 0.500141138 | 0.991026182 | \( \checkmark \) |
| 9  | Approximate entropy | 0.557094391 | 0.9921875 | \( \checkmark \) |
| 10 | Long run | 0.461856563 | 1 | \( \checkmark \) |
| 11 | Rank | 0.568625938 | 1 | \( \checkmark \) |
| 12 | Random excursions | 0.315794968 | 0.9921875 | \( \checkmark \) |
| 13 | Random excursions variants | 0.317097578 | 0.99375 | \( \checkmark \) |
| 14 | Serial 1 | 0.687015 | 0.9921875 | \( \checkmark \) |
|    | Serial 2 | 0.575824 | 0.9921875 | \( \checkmark \) |
| 15 | Linear complexity | 0.48313281 | 1 | \( \checkmark \) |

Table 2 Results of NIST test for original AES

5.2. Diehard Test
The diehard test, which consists of 12 tests, is used to test the randomness of random number generators (RNGs) and to evaluate how well a pseudo-RNG produces values. The results are categorized in a way that clearly indicates the randomness of cipher texts produced by the tested block ciphers. The diehard test was originally developed by George Marsaglia and published in 1995. This test comprises several standard tests that operate by using the \( P \)-value method. The diehard test results are presented in Tables 3 and 4 respectively. From the results it can be seen the proposed algorithm passed all tests while the original algorithm fails in overlapping sums test [1, 24, 25].
5.3. Correlation Coefficient

The correlation coefficient is calculated from the correlation between two random variables. It is considered one of the significant features of the security of block ciphers that handle the dependency of individual output bits on input bits. Moreover, it is a measure of how two variables affect each other, i.e., the degree of dependency of two variables on each other. In this study, it is used to measure the dependency between plaintexts and ciphertexts. The correlation values can determine the confusion effect of the block ciphers. Correlation coefficient is a number between (−1) and (1) and is the amount of the unit of linear relationship between two variables. If the correlation coefficient is (1), then the relationship is linear. If the correlation coefficient is (−1), then the relationship is decreasingly linear. In the case of independent variables, the correlation is 0. The test is run on 128 different sequences of 10^6 bits with 128 different 16-byte keys of both algorithms the proposed and the original algorithms. The average correlation coefficient is 0.008109 and 0.023021 correspondingly. Hence, the relation between plaintexts and ciphertexts is near zero. Figures 4 and 5 illustrate the correlation between plaintexts and ciphertexts for the proposed and original algorithms respectively. However, the correlation between the plaintext and cipher text in the proposed algorithm is better than the original algorithm. This means the security of the proposed algorithm is better than the original [21, 26-28].

![Figure 4. Correlation coefficient of the proposed algorithm](image1)

![Figure 5. Correlation coefficient of the original AES algorithm](image2)

5.4. ENTROPY

The idea of entropy comes from information theory and ergodic theory. Shannon entropy is a metric associated with the information content of an input signal. Entropy analysis measures the complexity of encrypted data. The optimum entropy value is 8. Thus, a value that is close to 8 corresponds to the high complexity of encrypted data. The information entropy H(s) of a source s with 2^N symbols si is clear as follows:

\[ H(s) = \sum_{i=0}^{2^N-1} P(s_i) \log_2 s_i, \]  \hspace{1cm} (4)

where P(s_i) means the likelihood of the symbol si being emitted from s. If s is a truly random source, that is, if P(s_i)= 2^-N for all i, then H(s)=2^N\log_2 2^N = N.

| Test               | P-value | Assessment |
|--------------------|---------|------------|
| Birthdays          | 0.531082 | √          |
| OPERMS             | 0.294862 | √          |
| Rank 31x31         | 0.342524 | √          |
| Rank 32x33         | 0.641602 | √          |
| Rank 6x8           | 0.452536 | √          |
| BITSTREAM          | 0.999992 | √          |
| OPSSO              | 1       | √          |
| OQSSO              | 0.884964 | √          |
| DNA                | 0.610985 | √          |
| Count-1s-star      | 0.643509 | √          |
| PARKING LOT        | 0.57112 | √          |
| Minimum Distance   | 0.999753 | √          |
| 3D SPHERES TEST    | 0.884159 | √          |
| Squeeze            | 0.741109 | √          |
| OVERLAPPING SUMS   | 0.534791 | √          |
| Run                | 0.698266 | √          |
| Craps              | 0.333134 | √          |

| Test               | P-value | Assessment |
|--------------------|---------|------------|
| Birthdays          | 0.742062 | √          |
| OPERMS             | 0.237064 | √          |
| Rank 31x31         | 0.765169 | √          |
| Rank 32x33         | 0.621038 | √          |
| Rank 6x8           | 0.149836 | √          |
| BITSTREAM          | 0.533555 | √          |
| OPSSO              | 0.561696 | √          |
| OQSSO              | 0.465943 | √          |
| DNA                | 0.552726 | √          |
| Count-1s-star      | 0.542229 | √          |
| PARKING LOT        | 0.274812 | √          |
| Minimum Distance   | 0.599324 | √          |
| 3D SPHERES TEST    | 0.670784 | √          |
| Squeeze            | 0.794714 | √          |
| OVERLAPPING SUMS   | 0.08783  | x          |
| Run                | 0.693404 | √          |
| Craps              | 0.267394 | √          |
This test is run on the original AES and the proposed algorithm with 128 sequences of $10^6$ bits with 128 different random keys. The results are presented in Figures 6 and 7. The average entropy of the original AES and the proposed algorithm are 7.9998299 and 7.9998319, respectively. Therefore, the entropy value of both algorithms is close to 8 [5, 15, 21].

![Figure 6. Entropy of the original AES algorithm](image)

![Figure 7. Entropy of the proposed algorithm](image)

5.5. Histogram

Histograms present the number of occurrences (frequency) of every component, i.e., how many times each and every component appears in a sequence, in the form of a graph. The histogram of a text shows the frequency distribution of the characters in a text in graphical formula in a corresponding window. A good RNG should present a uniform histogram with any secret key to avoid detection by opponents, especially statistical attackers. This test is run on the proposed algorithm and the original algorithm on $10^4$ with 8-bit number. The results are presented in Figures 8 and 9. The results show that both algorithms have a uniform histogram [21, 29, 30].

![Figure 8. Histogram of the original AES algorithm](image)

![Figure 9. Histogram of the original AES algorithm](image)

6. CONCLUSION AND FUTURE WORKS

According to numerous studies, the dynamic component of block cipher algorithms is more secure than their fixed component. Thus, this study aims to increase the AES security by proposing dual dynamic XOR table and MixColumns transformation based on 3D Chebyshev instead of fixed XOR table and MixColumns transformation. The experiments show that the proposed algorithm can provide high-level security. In future works, this proposed algorithm will be developed for use in bioinformatics.

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