Noise-Modulated Effects of Anisotropy and Position-Dependent Effective Mass on the Oscillator Strength of Impurity Doped Quantum Dots

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Abstract. We study the modulation of oscillator strength (OS) of impurity doped quantum dot (QD) under the influence of geometrical anisotropy and position-dependent effective mass (PDEM) in presence and absence of noise. The OS profiles are monitored as a function of anisotropy and dopant location considering PDEM and fixed effective mass (FEM). Noise considered here is Gaussian white noise which has been administered to the system additively and multiplicatively. Always a comparison has been attempted between FEM and PDEM to understand the role of the latter on OS profiles. Application of noise has been found to affect the OS profiles only over some particular domains of anisotropy and dopant location. And use of PDEM promotes greater contribution from noise than FEM in fabricating the OS profiles. The observations reveal sensitive interplay between noise and anisotropy/PDEM to tailor the features of OS profiles which bear substantial technological importance in the study of nonlinear optical properties of doped QD systems.

Keywords: Quantum dot, impurity, Gaussian white noise, oscillator strength, geometrical anisotropy, position-dependent effective mass

1 Introduction

Low-dimensional semiconductor systems (LDSS) such as quantum wells (QWLs), quantum wires (QWRs) and quantum dots (QDs) are widely appreciated for their noticeably large nonlinear optical (NLO) properties. The enhanced quantum confinement effect (in comparison with the bulk materials) existing in LDSS favors such magnified nonlinear effects [1]. Such strong confinement in LDSS causes small energy interval between the subband levels and large value of electric dipole matrix elements. These two factors promote achievement of resonance conditions. Such enhanced NLO properties of LDSS turn out to be immensely significant in view of probing the electronic structure of mesoscopic media [2], application of electronic and optoelectronic devices in the infra-red region of the electromagnetic spectrum [3, 4], exploring the area of integrated optics and optical communications [5, 6], fabricating many optoelectronic devices such as far-IR laser amplifiers, photo-detectors, and high-speed electro-optical modulators [7–9] and most significantly, understanding and realization of fundamental physics.

Oscillator strength (OS) is an extremely significant dimensionless quantity absolutely pertinent to the investigation of optical properties which are connected to the electronic dipole allowed transitions. It also delivers additional information regarding the fine structure and selection rules of optical absorption. In LDSS large value of OS is responsible for high dipole moment expectation values and consequent exhibition of large NLO response. These important features have led to some prominent theoretical researches on OS by Yilmaz and Şafak [10], Özmen et al. [11], Çakir et al. [12], Kumar et al. [13], Tiutiumnyk et al. [14], Xie [15], Sadeghi [16], and He and Xie [17], to mention a few.
Ingression of impurity (dopant) into LDSS initiates delicate interplay between the dopant potential with the confinement potential of LDSS and eventually modifies the energy level distribution. Such modification severely affects the electronic and optical properties of LDSS. Thus, a well-controlled inclusion of dopant favors achievement of desirable optical transitions. Such desirable optical transition has become an essential part of fabricating optoelectronic devices with tunable emission or transmission properties and ultra narrow spectral line widths. This has largely opened up new vista of technological applications of LDSS. Moreover, the proximity of optical transition energy and the confinement strength (or the quantum size) can effectively design the resonance frequency. In what follows, optical properties of doped LDSS have envisaged rigorous research activities [18–49].

Of late, we have come across a few important studies concerned with the influence of geometrical anisotropy on the optical properties of LDSS. Among them the important contributions were made by Niculescu et al. [39], Xie and his coworkers [50-52] and Safarpour et al. [53, 54]. In reality, in most cases LDSS are not at all isotropic which justifies the need of realizing how anisotropy governs their optical properties. In practice anisotropic QDs can be manufactured by chemically controlling the nanostructure aspect ratio [50]. Thus, study of anisotropic systems has produced substantial interest in view of obtaining novel as well as useful devices.

In recent times we also envisage a considerable number of investigations which involve position-dependent effective mass (PDEM) of LDSS. PDEM gives rise to perceptible change in the binding energy of the doped system and thus alters the optical properties. Such change in the optical properties has induced lots of studies on LDSS with spatially varying effective mass. With reference to above the works of Rajashabala and Navaneethakrishnan [55-57], Peter and Navaneethakrishnan [58], Khordad [59, 60], Qi et al. [61], Peter [62], Li et al. [63], and Naimi et al. [64] deserve attention.

Presence of noise invariably affects the NLO properties of mesoscopic devices. Motivated by this fact recently we have made thorough investigations on how Gaussian white noise affects the oscillator strength of doped QD [65]. We have also explored the role played by geometrical anisotropy [66] and PDEM [67, 68] on various NLO properties of doped QD in presence of noise. However, despite a thorough literature survey we have not found any study that deals with influence of noise on OS under the purview of anisotropy and/or PDEM. Realizing the fact that OS forms the backbone of emergence of many NLO properties, in the present work we explore the influence of geometrical anisotropy and PDEM on OS of doped QD in presence of Gaussian white noise. The OS profiles are monitored for different extents of geometrical anisotropy (to understand the anisotropy effect) and simultaneously with fixed effective mass (FEM) and dopant position-dependent effective mass (PDEM) (to understand the role of PDEM). Moreover, the influence of pathway of application of noise (additive/multiplicative) has also been explored for a comprehensive analysis.

2   Method

The impurity doped QD Hamiltonian, subject to external static electric field (F) applied along x and y-directions and noise (additive/multiplicative) can be written as

$$H_0 = H_0 + V_{imp} + \int [F(x+y) + V_{noise}]$$  

Under effective mass approximation, $H_0$ represents the impurity-free 2-d quantum dot containing single carrier electron under lateral parabolic confinement in the $x-y$ plane and in presence of a perpendicular magnetic field. $V_{imp}$ is the impurity (dopant) potential and $V_{noise}$ stands for white noise applied to the system. $H_0$ is therefore given by [69, 70].

$$H_0 = \frac{\hbar^2}{2m^*} \left[ -i\hbar \nabla + \frac{e}{c} A \right]^2 + \frac{1}{2} m^* \omega_0^2 (x^2 + y^2)$$

$m^*$ represents the effective mass of the electron inside the QD material. $e$ and $c$ are charge of electron and velocity of light, respectively. $V(x,y) = \frac{1}{2} m^* \omega_0^2 (x^2 + y^2)$ is the confinement potential with $\omega_0$ as the harmonic confinement frequency. Using Landau gauge [A= (B_y, 0, 0), where A is the vector potential and B is the magnetic field strength], $H_0$ reads.
\[ H_0 = -\frac{\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) + \frac{1}{2} m^* \omega_0^2 x^2 + \frac{1}{2} m^* \left( \omega_y^2 + \omega_x^2 \right) y^2 - i\hbar \omega_0 y \frac{\partial}{\partial x} \]  

\[ \omega_0 = \frac{eB}{mc} \]  

being the cyclotron frequency. \( \Omega = \sqrt{\omega_y^2 + \omega_x^2} \) can be viewed as the effective confinement frequency in the \( y \)-direction. Following the notable works of Xie the ratio \( \eta = \frac{\Omega}{\omega_0} \) could be defined as the anisotropy parameter [50-52].

\[ V_{\text{imp}} \]  
is represented by a Gaussian function \([65]\),

\[ V_{\text{imp}} = V_0 e^{-\gamma(x-x_0)^2 + (y-y_0)^2} \]

\( x_0, y_0 \) are the site of dopant incorporation, strength of the dopant potential, and the spatial spread of impurity potential, respectively. \( \gamma \) can be written as \( \gamma = k\varepsilon \), where \( k \) is a constant and \( \varepsilon \) is the dielectric constant of the medium.

The dopant location-dependent effective mass \( m^* \) is given by \([55, 58]\)

\[ \frac{1}{m^*} \left( r_0 \right) = \frac{1}{m} + \left( 1 - \frac{1}{m} \right) \exp \left( -\beta r_0 \right) \]  

where \( \beta \) is a constant chosen to be 0.01 a.u. The choice of above form of PDEM indicates that the dopant is strongly bound to the dot confinement center as \( r_0 \rightarrow 0 \) i.e. for on-center dopants whereas \( m^* \left( r_0 \right) \) becomes highly significant as \( r_0 \rightarrow \infty \) i.e. for far off center dopants.

\( V_{\text{noise}} \) stands for white noise \([f(x,y)]\) which follows a Gaussian distribution (generated by Box-Muller algorithm), has a strength \( \zeta \) and is characterized by zero-average and spatial \( \delta \)-correlation conditions \([65-67]\). Such white noise can be introduced to the system via two different modes (pathways) i.e. additive and multiplicative \([65-67]\). These two different modes can be discriminated on the basis of extent of system-noise interaction.

The time-independent Schrödinger equation has been solved by generating the sparse Hamiltonian matrix \( H_0 \). The relevant matrix elements involve the function \( \psi(x,y) \) which is a superposition of the products of harmonic oscillator eigenfunctions. In this context a sufficient number of basis functions have been included after performing the convergence test. \( H_0 \) is diagonalized afterwards in the direct product basis of harmonic oscillator eigenfunctions to obtain the energy levels and wave functions.

OS is given by \([10-17]\)

\[ P_y = \frac{2m^*}{\hbar^2} \Delta E_y \left| M_0 \right| \]  

where \( \Delta E_y = E_j - E_i \) is the energy difference between states \( \left| j \right> \) and \( \left| i \right> \) and \( M_0 = \left< \psi_i \left| \hat{y} + \hat{\delta} \right| \psi_j \right> \) is the electric dipole transition moment. The matrix elements are usually small whereas \( \Delta E_y \) is very high in small QDs.

3 Results and Discussion

The calculations are performed using the following parameters: \( \varepsilon = 12.4 \), \( m^* = 0.067m_0 \), where \( m_0 \) is the free electron mass, \( \hbar \omega_0 = 2.72 \text{ meV} \), \( F = 100 \text{ KV/cm} \), \( B = 1.0 \text{ T} \), \( \zeta = 1.0 \times 10^{-13} \), \( V_0 = 272.0 \text{ meV} \). The parameters are suitable for GaAs QDs.

Role of anisotropy (\( \eta \)): Fig. 1 shows the variations of OS with anisotropy parameter \( \eta \) in absence of noise [fig. 1(i)] and in presence of additive [fig. 1(ii)] and multiplicative [fig. 1(iii)] noise, respectively. Up to \( \eta \sim 25 \) OS remains nearly unobservable. However, as soon as \( \eta \geq 25 \), OS exhibits pronounced enhancement with increase in \( \eta \) and culminates into saturation beyond \( \eta \sim 175 \). The profiles have been found to be nearly identical both in presence and absence of noise throughout the entire range of variation of \( \eta \) with minor fluctuations. However, only in the neighborhood of a typical
anisotropy regime i.e. $\eta \sim 28$ a somewhat observable noise induced departure of the OS profiles has been found from that of noise-free situation [66]. The mode of application of noise (additive/multiplicative) comes out to be quite inactive in modulating the OS profile.

![Figure](image)

**Figure.** Plots of OS vs $\eta$: (i) under noise-free condition, (ii) in presence of additive noise and (iii) in presence of multiplicative noise.

The observations indicate that a fruitful overlap between concerned eigenstates can only be realized if and only if $\eta \geq 25$ both in presence and absence of noise. As soon as anisotropy exceeds the threshold value of $\eta \sim 25$ the said overlap comes into play and begins to increase profoundly with increase in $\eta$. And within very large anisotropy domain of $\eta \geq 175$ the overlap settles to some steady value. Moreover, application of noise happens to moderately enhance the said overlap only through a small anisotropy window (in the vicinity of $\eta \geq 25$) and fails to make any impact on the entire remaining anisotropy domain.

**Role of PDEM:** Fig. 2 evinces the variation of OS with dopant location ($r_0$) using PDEM [$m'(r_0)$] in absence of noise [fig. 2(i)] and in presence of additive [fig. 2(ii)] and multiplicative [fig. 2(iii)] noise, respectively. In absence of noise the OS profile exhibits successive maximization and minimization at $r_0 = 0.1$ nm and $r_0 = 0.3$ nm, respectively. After minimization OS increases with $r_0$ and shows some sort of steady value beyond $r_0 = 0.6$ nm.

![Figure 2](image)

**Figure 2.** Plots of OS vs $r_0$ using PDEM: (i) under noise-free condition, (ii) in presence of additive noise and (iii) in presence of multiplicative noise.

The profile suggests that, in absence of noise, PDEM of dopant causes maximum and minimum overlap between the relevant eigenfunctions at some typical dopant locations and the extent of overlap
attains some stability for the off-center dopants. Application of noise does not much alter the overall OS profile from that of noise-free condition qualitatively. However, it is the magnitude of OS which is affected most. The plot reveals noise-induced suppression and amplification of OS (in comparison with noise-free case) nearly at the same dopant locations where maximization and minimization have been found previously. And beyond $r_0 = 0.6$ nm the noise effect nearly subsides and the OS value approaches the noise-free one. It can therefore be inferred that presence of noise simply modulates the size of overlap between the pertinent wave functions from that of noise-free condition. Noise, however, does not grossly affect the pattern of said overlap as a function of dopant location in case of PDEM. The mode of application of noise, as before, does not exhibit any noticeable contribution.

Role of FEM: Fig. 3 displays the variation of OS with dopant location ($r_0$) using FEM ($m^* = 0.067m_0$) in absence of noise [fig. 3(i)] and in presence of additive [fig. 3(ii)] and multiplicative [fig. 3(iii)] noise, respectively. Both in presence and absence of noise the OS profiles exhibit maximization around a dopant location of $r_0 = 0.3$ nm indicating maximum overlap between the eigenstates concerned. It needs to be noted that the difference between OS profiles in absence and presence of noise decreases further using FEM than using PDEM. In the present case of FEM, only for on-center ($r_0 = 0.0$ nm) and very near off-center ($r_0 \leq 0.1$ nm) dopants, presence of noise causes prominent amplification of OS over that of noise-free condition. At all other dopant locations noise remains insignificant.

![Figure 3](image)

**Figure 3.** Plots of OS vs $r_0$ using FEM: (i) under noise-free condition, (ii) in presence of additive noise and (iii) in presence of multiplicative noise.

4 Conclusion

The modulation of oscillator strength (OS) of impurity doped QD has been investigated under the influence of geometrical anisotropy and position-dependent effective mass (PDEM) in presence and absence of noise. The findings can be summarized as follows:

1. OS becomes noticeable only if the anisotropy parameter $\eta$ exceeds a threshold value of $\sim 25$ both in presence and absence of noise. Effect of noise on OS profile can be manifested only around a narrow anisotropy domain of $\eta \sim 28$ when a moderate enhancement of OS takes place.

2. In case of PDEM, OS undergoes maximization and minimization depending upon the dopant location both in presence and absence of noise. Presence of noise does not qualitatively alter the OS profiles but only affects the extent of maximization and minimization causing suppression and amplification of OS.

3. In case of FEM, OS displays prominent maximization around $r_0 \sim 0.3$ nm both in presence and absence of noise. Difference between the OS profiles in absence and presence of noise becomes perceptible only for on-center ($r_0 = 0.0$ nm) and very near off-center ($r_0 \leq 0.1$ nm) dopants where OS gets amplified in presence of noise. On the whole, it is PDEM that invites greater difference between OS profiles in presence and absence of noise than FEM.
Above features can highlight important aspects of NLO properties of doped QD systems in presence of noise.

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