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Robust Optimization and Kriging Metamodeling of Deep-Drawing Process to Obtain a Regulation Curve of Blank Holder Force

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Abstract: In recent decades, the automotive industry has had a constant evolution with consequent enhancement of products quality. In industrial applications, quality may be defined as conformance to product specifications and repeatability of manufacturing process. Moreover, in the modern era of Industry 4.0, research on technological innovation has made the real-time control of manufacturing process possible. Moving from the above context, a method is proposed to perform real-time control of a deep-drawing process, using the stamping of the upper front cross member of a car chassis as industrial case study. In particular, it is proposed to calibrate the force acting on the blank holder, defining a regulation curve that considers the material yield stress and the friction coefficient as the main noise variables of the process. Firstly, deep-drawing process was modeled by using commercial Finite Element (FE) software AutoForm. By means of AutoForm Sigma tool, the stability and capability of deep-drawing process were analyzed. Numerical results were then exploited to create metamodels, by using the kriging technique, which shows the relationships between the process parameters and appropriate quality indices. Multi-objective optimization with a desirability function was carried out to identify the optimal values of input parameters for deep-drawing process. Finally, the desired regulation curve was obtained by maximizing total desirability. The resulting regulation curve can be exploited as a useful tool for real-time control of the force acting on the blank holder.

Keywords: sheet metal forming; deep-drawing; kriging metamodeling; multi-objective optimization; FE (Finite Element) AutoForm Robust Analysis; defect prediction

1. Introduction

Sheet metal cold forming processes, or deep-drawing processes, play an important role in modern industry, since components of complex geometry can be produced. However, there are some aspects that must be taken into consideration such as: (i) the influence of sheet anisotropy; (ii) the formability limits; and (iii) the spring-back phenomenon that is not negligible. The cold forming process involves plastic deformation, and it should not involve alterations in the thickness of the starting sheet. Actually, the thickness of the blank may have considerable variations during stamping. Cold forming consists of pressing the blank on a punch, by means of a die. The correct execution of the process is ensured by the blank holder, which, by exerting a force on the blank edges, allows the correct material draw-in in the die, avoiding part defects such as wrinkles, thickening, thinning and cracks. It is possible to identify the following main phases of the process: (i) gravity, during which the sheet, resting on the tool, undergoes a first deformation due to its weight; (ii) holding, during which the sheet metal is closed between the die and the blank holder; (iii) stamping, during which die-blank-blank holder system moves towards the
punch for the plastic deformation; and (iv) trimming, during which the excess metal is removed while spring-back occurs in the finished part.

Deep-drawing process is very effective especially for symmetrical pieces, but, if the component is non-axisymmetric, it is important to have a uniform material flux in the die; in fact, in sheet metal forming, it is fundamental to control the rate of material flow into the die cavity [1]. To control material flow during drawing operation in order to achieve the optimal forming of a part without cracks and wrinkles, it is generally necessary to slow down the sliding of the blank regions that flow more easily. This can be achieved by calibrating the blank holder force and eventually by drawbeads, which are rib-like projections mounted on the binder and designed with the aim of improving the metal flow control [2]. For better effectiveness, during the stamping phase, the action of the drawbeads and the force on the blank holder can be differentiated in the different regions of the sheet. This means having active drawbeads and active blank holder control system (different forces on the different segments of the blank holder). A good optimization leads to a better distribution of thickness on the formed part reducing the occurrence of defects such as fracture and wrinkling [3].

In general, defects on stamped components can be multiple:

- **Wrinkles** are generally caused by insufficient force on blank holder.
- **Cracks** occur when the applied load exceeds the maximum resistance of the material.
- **Spring-back** is due to the deformations of the component in the elastic–plastic field. Spring-back is a critical aspect of drawing processes especially in the automotive industry, where high-dimensional accuracy is often required. Many parameters influence this phenomenon such as Young modulus, yield stress, punch radius and sheet thickness.

The good performances of the deep-drawing process depend on the correct setting of the process parameters that govern the phenomenon such as pressure on the blank holder, gap between die and punch, radius of the tools, lubrication and initial geometry of the blank. In the literature, in fact, several studies evaluate the effects of different process parameters on the quality of the final product [4,5].

In this perspective, to support and facilitate the analysis of the criticalities of the process, there is various simulation software such as AutoForm and PamStamp, which is becoming increasingly widespread. The success of these software packages is due to the ability to conduct a preliminary analysis of the process to identify critical parameters, thus reducing the costs of the experimentation (in terms of time, material, energy resources, etc.).

In the present work, the cold forming process for the production of an upper cross member was modeled using the finite element (FE) commercial software AutoForm. Once the process was modeled, it was decided to investigate how some input parameters affect the quality of the final product. The input parameters considered are the blank holder force, friction coefficient and yield stress of blank material. The first was considered a design parameter, while the other two were considered noise parameters. Instead, the quality of the final product was assessed by optimizing at the end of drawing phase the output responses: thickening, insufficient stretch, safe zone, potential splits and thinning.

It is important to consider the noise variables in addition to design variables, because in everyday production it is possible for parts to be produced safely one day, and the next day problems arise even though production condition have apparently not changed. This is probably due to noise and variation during forming process. Therefore, the robustness analysis was indispensable. It can be verified whether a forming process provides stable results under the influence of the noise parameters. Therefore, in this work, after robustness analysis, thanks to the numerical results, metamodels were built with the kriging technique for each quality criterion considered. The combination of finite element analysis with metamodeling techniques is a consolidated methodology in the literature [6–8]. Metamodeling is a powerful tool that allows deriving the mathematical relationship between
inputs and outputs even when the analysis is based on a deterministic computer experiments.

In the present work, after the metamodeling phase, a multi-objective optimization with a desirability approach was carried out. The innovative aspect of this work is linked to the need to find a regulation curve of the force to be imparted to the blank holder as a function of the yield stress of the material in order to control the process online from the perspective of Industry 4.0.

2. Materials and Methods

The component studied in this work is the upper front cross member of a car currently being produced at Tiberina company (Sangro – Atessa (CH), Italy); Figure 1 shows the image of this component realized in HR 440Y580T-FB-UC steel (2 mm thick) that is common in the automotive field for cold forming of structural components. It is a hot-rolled steel strip; in particular, it belongs to the family of ferritic-bainitic steel. This microstructure offers a particularly attractive combination of high strength and good cold workability.

![Figure 1. Upper cross member B-Suv.](image)

Table 1 shows chemical composition of investigated steel and Figure 2 shows the mechanical characteristics of the material considered for the studied component.

| C max | Si max | Mn max | P max | S max | Al max | Ti+Nb max | Cr+Mo max | B max | Cu max |
|-------|--------|--------|-------|-------|--------|-----------|-----------|-------|--------|
| 0.18  | 0.50   | 2      | 0.05  | 0.010 | 0.015-2| 0.15      | 1         | 0.01  | 0.2    |

Specifically, Figure 2a shows the hardening curve. AutoForm requires the true stress as a function of true plastic strain measured in the direction of rolling. In this image, the values of the uniform elongation ($A_g$), yield stress ($\sigma_0$), tensile strength ($R_m$) and strain hardening exponent ($n$) are highlighted.

Figure 2b shows the yield surface defined with the BBC criterion (Banabic et al.) in order to take into account material anisotropy [9]. The main values of this model are illustrated in this figure: $r_m$ is the average of plastic strain ratio at 0°, 45° and 90° of rolling direction; $r$ is plastic strain ratio at biaxial stress, which is defined as the ratio of strains $\varepsilon_2$ and $\varepsilon_1$; $\sigma_b/\sigma_0$ is the ratio between onset of yielding at equi-biaxial stress and yield stress; $\sigma_{pol}/\sigma_0$ is the ratio between plane strain stress at 0° of rolling direction and yield stress;
σ_p90/σ_0 is the ratio between plane strain stress at 90° of rolling direction and yield stress; and σ_shear/σ_0 is the ratio between shear stress and yield stress.

Figure 2c shows the Formability Limit Curve (FLC). The curve represents the maximum values of the principal strains ε_1 and ε_2 measured at the onset of material failure.

![Formability Limit Curve (FLC)](image)

Figure 2. (a) Hardening curve; (b) yield surface with BBC criterion; and (c) Formability Limit Curve (FLC).

The goal of industrial digitization is to increase production efficiency and improve the quality of the final product. In fact, aiming at zero defect production, the number of scrap products is reduced and consequently the production costs are reduced. Therefore, it is necessary to optimize and design the process correctly. However, it must be taken into account that unwanted system changes may occur during a production process. In
this work, for the examined deep-drawing process, possible fluctuations of the material in a coil (yield stress) and a variation of the lubrication conditions (friction coefficient) were considered. These two parameters are called noise factors; this means that they cannot be controlled. A possible controllable design parameter is the force on the blank holder, which can be adjusted in the production line.

The objective of this work, in fact, is the robust optimization of the process investigated. Moreover, once the process has been optimized, the goal is to find a regulation curve that allows, once it is implemented in the process through an algorithm, to identify how to adjust the force on the blank holder as the yield stress varies for different values of the friction coefficient. In the article by P. Fischer et al. [10], the control based on the feed-forward algorithm for the force on the blank holder is studied considering the fluctuations of the yield stress measured through the eddy currents.

The methodology adopted to derive the regulation curves is shown in Figure 3.

![Figure 3. Scheme of adopted methodology.](image)

In particular: (1) The component and the process phases were modeled in the AutoForm (R8, GmbH, Zurich, Switzerland) environment. (2) Thanks to the AutoForm Sigma module, the process was simulated and studied as the process parameters changed. In particular, the parameters that were changed are the force on the blank holder, the friction coefficient and the yield stress. These last two parameters were considered noise parameters. The target value and a standard deviation to all parameters considered were assigned. The software, then, proceeded to a sampling according to the Latin Hypercube statistical method (Latin Hypercube Sampling, LHS), generating a near-random samples of parameter values. In total, 81 numerical simulations were performed. Once the results of the numerical simulations were obtained, a robust analysis was carried out to analyze the influence of the noise variables on the forming process. The quality indices taken into
consideration for this study were thickening, insufficient stretch, safe zone, potential splits and thinning. The results of robust analysis were used to predict the stability and capability of the process. (3) Given the dataset obtained with the numerical simulations of AutoForm Sigma, thanks to the Matlab DACE toolbox (2.0, Technical University of Denmark DK-2800 Kgs, Lyngby, Denmark), the metamodels were obtained. These metamodels allow predicting a new (untried) site [11]. These sites on which to evaluate the predictor were generated thanks to a definition of a grid points. We chose a 39 × 39 mesh of points distributed equidistantly in the area [0, 100]^2 covered by the design sites. After kriging meta-modeling phase, there was the multi-objective optimization phase. The approach used for optimization is that of desirability. With the optimization phase, the combination of input parameters (force on the blank holder, friction coefficient and yield stress) which guarantees a stamped component without defects (wrinkles, thinning, thickening and breakage) was identified. (4) Considering combination of input parameters that give high desirability, force regulation curves on the blank holder were obtained as a function of the yield stress of the material for three different values of friction coefficient. Finally, by comparing an optimized solution with a non-optimized one, the draw-in of metal sheet was evaluated, and it was observed that the sheet has different sliding in the two conditions.

3. Results

3.1. Design of Stamping Process Using Finite Element Model (FEM)

The process was first numerically modeled using commercial Finite Element (FE) software AutoForm. The numerical model provides for the definition of tools geometries (die, punch and blank holder), the initial blank and their reference systems and material characteristics and production plan (defining the individual operations of the production process). Figure 4 shows the tools modeled in AutoForm.

![Figure 4. Tools geometry (die, punch and binder or blank holder).](image)

The die and the punch were defined as rigid tools. The blank holder was defined as a force-controlled tool, which means that the assigned force is automatically increased; if the reaction force acting on the binder exceeds the defined force, the binder always remains closed [12].

For model construction, a membrane element, extended by an approximate bending stiffness (Bending Enhanced Membrane, BEM) is chosen. AutoForm software uses an adaptive mesh and an implicit solver.

Once the component and the process were modeled, robust analysis was carried out by means of AutoForm-Sigma, an AutoForm module. This tool allows analyzing and im-
proving the robustness of sheet metal products and processes; in fact, it enables identifying which design and noise parameters influence part quality and to what extent. It also supports in determining appropriate correction measures during tryout and production. In addition, it identifies the correction measures that have no effect at all, as well as those that offer a real chance of resolving the particular problem at hand. By analyzing process performance and, in particular, process capability, it is possible to validate the stamping process, minimize part rejects and maximize production efficiency.

The friction coefficient and the yield stress, as well as the force on the blank holder, are the considered input parameters. The force on the blank holder was considered as a design variable and a variability of 25% was imposed with respect to the nominal value of 1470.5 kN; instead, the friction coefficient and the yield stress were considered noise variables. Variabilities of 10% and 15% were set for the friction coefficient (0.15 as nominal value) and for the yield stress (509.6 MPa as nominal value), respectively. The value of the force on the blank holder was chosen thanks to the design data of the press present in Tiberina Sangro company and the value of yield stress was set according to material datasheet. Instead, the software default value was chosen for the friction coefficient, specifying a mill oil for the lubrication condition. The Coulomb lubrication model was selected for the numerical simulation of deep-drawing process. However, the Coulomb model is only an approximation of the real friction behavior. In fact, the friction coefficient is not a constant in reality, but is dependent on multiple factors such as contact pressure.

The need to distinguish the parameters into two categories (controllable or design variables and non-controllable or noise variables) arises from the need to evaluate the process robustness before production phase. The variability of noise and controllable parameters, in fact, will lead to a response variation, thus causing changes in the product characteristics. If the response differs too much from the expected characteristics, the product may be unacceptable. However, while controllable variables can be corrected in the design phase, or even in-process, the noise variables must be carefully defined and studied; therefore, the process must be developed so as that these variations do not lead to worsening product quality.

The qualities of the final product were assessed on the basis of the percentage of thickened area, the percentage of the area with insufficient elongation, the percentage of safe zones, the percentage of area with potential cracks and the thinning at the two Critical Points A and B indicated in Figure 5. These two points are critical because at Point A the minimum global thinning value of 25.2% is reached, while at Point B a value of 23.6% is reached. The different maximum thinning values at Points A and B are justified by the lack of symmetry of the part.

The output variables were evaluated at the end of the drawing phase, before the trimming operation in order to optimize the drawing phase.

![Figure 5. Critical Points A and B for the evaluation of thinning.](image-url)
These issues can be determined by means of the Formability Limit Diagram (FLD). Thanks to the FLC imported during the material definition phase, the software is able to represent the FLD showing the strain state of all elements for each time step.

As an example, Figure 6 shows the formability limit diagram at the end of drawing phase for the nominal case (process parameters set at the nominal values); the different colored areas represent the behavior of the material during the deformation process. Figure 7 shows the formability map on the component.

The red region, above the formability limit curve, represents the area of points subject to splits. The area of the points subject to risk of splits is shown in yellow. The regions in which the deformation occurs in an optimal way are highlighted in green. When the material is not sufficiently deformed, it is called insufficient stretch, and this region is colored in gray. The other two regions in blue and purple represent, respectively, the compression zone and the thickening zone, where there may be a greater tendency to wrinkle.

These areas are calculated as the ratio between the area of the finite elements that present critical issues and total area of the component.

![Formability limit diagram (FLD).](image)

**Figure 6.** Formability limit diagram (FLD).

![Formability map on component at the end of drawing phase.](image)

**Figure 7.** Formability map on component at the end of drawing phase.

The thinning issue shows the thickness variation of the blank during the process. It is important to predict which areas are subjected to excessive thinning because it is more likely that the ruptures occur there.

### 3.2. Robust Analysis

Fluctuations of lubrication conditions are noise factors in forming process, and yield strength, which can vary from coil to coil and supplier to supplier, is a noise in material properties. These are some of important but unavoidable and uncontrollable variations during deep-drawing process under real production conditions. In this work, the friction
coefficient and the yield stress were taken into account to verify whether the process provides stable results under the influence of these most common noise parameters.

The robustness was analyzed with index process capability ($cp_k$), which indicates controllability of the process around the defined specification limits. This index is calculated as:

$$cp_k = \min \left( \frac{USL - \mu}{3\sigma}, \frac{\mu - LSL}{3\sigma} \right)$$  \hspace{1cm} (1)

where $USL$ is the Upper Specification Limit, $LSL$ is the Lower Specification Limit, $\mu$ is the mean value and $\sigma$ is the standard deviation.

Upper and lower specification limits are defined thanks to an evaluation standard present in AutoForm that, being a commercial software, ensures to industrial companies that results are always evaluated in the same way. However, these standards can be modified by the user.

The discrete representation provided by the FE software AutoForm reports the following results [12]:

- $cp_k < 0.67$: The process is not acceptable, as more than 2.25% of the results do not meet the specification limits.
- $cp_k \in [0.67; 1)$: The process is unreliable, as 0.14–2.25% of results do not meet the specification limits.
- $cp_k \in [1; 1.33)$: The process may be acceptable because the results fall within limit imposed. However, a check is required.
- $cp_k \geq 1.33$: The process is reliable, as less than 0.004% of the results exceed the limits.

For splitting and wrinkling, parameters to evaluate the quality of the final product, typically specification limits, are defined as: (i) thinning, for which only the lower $cp_k$ is relevant; (ii) maximum failure (defined as the ratio between the maximum major strain computed at an element and the major strain of the strain-based FLC for the same minor strain), for which only the upper $cp_k$ is relevant; and (iii) potential wrinkles, for which only the upper $cp_k$ is relevant [13].

By evaluating the lower $cp_k$ for thinning and the upper $cp_k$ for maximum failure after drawing phase, a value of $cp_k$ greater than 1.33 was obtained. The upper $cp_k$ for potential wrinkles is shown in Figure 8.

**Figure 8.** (a) Upper $cp_k$ for potential wrinkles after drawing phase; and (b) upper $cp_k$ for potential wrinkles at the end of the process.
Figure 8a shows that the variable potential wrinkles produces unacceptable results if the end of drawing phase is considered. However, with the subsequent trimming step and thanks to the spring-back phenomenon, the regions with defects are eliminated (Figure 8b). Therefore, it can be assumed that the process is reliable.

3.3. Metamodeling with Kriging Methodology

To study the relationship of the process parameters and material parameters with forming quality indices, a kriging method was used. For this purpose, a Matlab toolbox called DACE (Design and Analysis of Computer Experiments) was employed. This software allows constructing a kriging approximation model based on data from computer experiments and using this approximation model as a surrogate for the computer model [11]. The advantage of using this technique is that kriging models are accurate because they interpolate the sampled points and they are not limited by the type of function chosen, unlike other polynomial regression models. Moreover, kriging models are chosen to interpolate the data and are fit using maximum likelihood estimation [14]; for this reason, the surfaces may not be perfectly smooth, unlike the surfaces that could be obtained with response surface modeling that typically employs least squares regression to fit a polynomial model to the sampled data.

Figures 9–13 show the metamodels obtained in correspondence with the nominal force value (1470.5 kN). These metamodels represent, respectively, how the percentage of thickened zone, the percentage of area with insufficient stretching, the percentage of the safe zone, the percentage of zone with potential splits and the percentage of thinning at Critical Points A and B vary as the two noise variables (friction coefficient and yield stress) vary.

Figure 9. Metamodel of the percentage of thickened zone as friction coefficient and yield stress vary.
Figure 10. Metamodel of the percentage of area with insufficient stretching as friction coefficient and yield stress vary.

Figure 11. Metamodel of the percentage of safe zone as friction coefficient and yield stress vary.

Figure 12. Metamodel of the percentage of area with potential splits as friction coefficient and yield stress vary.
In these graphs, it is possible to observe that the noise variables greatly influence the quality indices of the final product. In particular, the figures show that an increase in the yield stress involves an increase in the percentage of thickened areas, areas with insufficient stretch, areas with potential splits (only for low friction coefficient) and an increase in thinning at Critical Points A and B. Consequently, increasing this parameter, there is a reduction in the percentage of the safe zone. Furthermore, if the blank lubrication conditions have a reduction in the friction coefficient, there is an increase in the percentage of the thickened area, a reduction in the safe area, a reduction in areas with potential splits and a reduction in thinning of the part region near Point B.

In the part region near Point A, there is a minimum value for the friction coefficient beyond which the percentage of thinning in this region begins to increase. The percentage of the zone with insufficient stretch increases as the friction coefficient decreases up to a maximum value, beyond which it begins to decrease.

3.4. Multi-Objective Optimization and Regulation Curve

To obtain an upper cross member free of defects, it is necessary to minimize the percentage of thickening, the percentage of areas with insufficient stretch, the percentage of areas with risk of splits and the percentage of thinning. Moreover, it is necessary to maximize the percentage of safe zones as well. It is clear that these characteristics cannot simultaneously assume the best possible values; therefore, the need to identify a compromise solution arises. This explains the multi-objective nature of optimization.

In this study, the Desirability Function Approach (DFA) was chosen. This approach is one of the most common methods for the optimization of multiple response processes in the industry field. According to this method, when the quality of a product or a process depends on several characteristics, if even one of them exceeds the imposed limits, the product or process is not acceptable. The DFA identifies the operating conditions that return the “most desirable” response values [15].

For each output variable, the criterion to be followed for optimization was chosen. In particular for the response relating to the percentage of safe zone, the criterion “the larger the better” was chosen, and, for all the other responses, the criterion was “the smaller the better”.

If a “the larger the better” response is desired, i.e., if the response is to be maximized, the desirability function is of the type:

\[
D = \begin{cases} 
1 & \text{if the response is less than the lower limit or greater than the upper limit;} \\
\frac{y - L}{U - L} & \text{if the response is within the range of limits;} \\
0 & \text{if the response is the target value.}
\end{cases}
\]
If a "the smaller the better" response is desired, instead, i.e., if the response is to be minimized, the desirability function is defined as follows:

\[
d_i(Y_i) = \begin{cases} 
0 & \text{if } Y_i(x) < L_i \\
\left(\frac{Y_i(x) - L_i}{T_i - L_i}\right)^s & \text{if } L_i \leq Y_i(x) \leq T_i \\
1 & \text{if } Y_i(x) > T_i 
\end{cases} 
\] (2)

According to this approach, total desirability is defined as:

\[
D = \prod_{i=1}^{k} \left[d_i(Y_i)\right]^{1/k} 
\] (4)

Table 2 presents the notation related to the equations.

| Symbol   | Definition                                                                 |
|----------|---------------------------------------------------------------------------|
| \(Y_i(x)\) | \(i\)th response as a function of \(x\) parameter                       |
| \(d_i(Y_i)\) | \(i\)th desirability function correlated to the response parameter \(Y_i\) |
| \(L_i\) | Minimum \(i\)th value                                                   |
| \(U_i\) | Maximum \(i\)th value                                                   |
| \(T_i\) | Target \(i\)th value                                                   |
| \(s\) | Exponent that defines the shape of the function \((s = 0.1\; \text{convex function})\) |
| \(D\) | Total desirability                                                        |
| \(k\) | Number of responses                                                      |

This optimization was a useful tool to obtain the regulation curves shown in Figure 14. These curves, in fact, were obtained considering the points of maximum desirability \((D > 0.9)\). In this figure, the desirability curves for each value of the friction coefficient are also shown. In particular, regulation curves of the force on the blank holder as a function of yield stress for all friction coefficient \((f)\) considered are highlighted with solid lines. The curves of the total desirability as a function of the yield stress for all values of the friction coefficient are highlighted with dashed lines.
Figure 14 shows that, at low values of the friction coefficient, the process requires higher force values, while, for the other levels of friction considered, the force initially increases, and then it stabilizes at a constant value. In particular, for a blank with a yield stress lower than 500 MPa and high friction (>0.135), it is necessary to reduce the force on the blank holder. Moreover, at low friction coefficient values, the process is insensitive and the maximum desirability curve is horizontal.

The regulation curves identified provide the control of the deep-drawing process in the case of random variations of the material mechanical characteristics (yield stress and friction coefficient). These noise parameters affect the sheet draw-in. In fact, in Figure 15, taking some reference points, the draw-in is compared as a function of the punch stroke for one of the conditions with maximum desirability (safe) and for a generic non-optimized condition (cracks).

![Figure 15. Draw-in as a function of the punch stroke at Points D, F and I of the sheet in the optimized condition (safe) and in the non-optimal condition (cracks).](image)

From the comparison, the different sliding of the sheet is observed in the non-optimized case compared to the optimal case; this leads to excessive thinning or rupture. The comparison in-process of draw-in with the safe condition proves to be a promising strategy for online monitoring of the stamping process. In fact, through laser sensors placed on the most critical points, it is possible to evaluate sliding of the sheet by comparing it with the optimal case. Thus, if there is no correspondence, a signal is sent to the piezoelectric actuators on the blank holder which acts on the force, modifying it. Neugebauer [16] used piezoelectric actuators for manipulating the blank holder force. The used state variable was the edge draw-in, which was measured by a laser displacement sensor developed in the work of Bräunlich [17].

4. Conclusions

The results of the numerical simulations show that the factors considered for the evaluation of the quality of the final product (thickening, insufficient stretch, safe zone, potential splits and thinning in the part region near Points A and B) are strongly influenced by the causal variation of the yield stress and the coefficient of friction. Therefore, these disturbing factors should be taken into consideration when designing the process.

The main result of this work shows that numerical simulation using AutoForm FE software, meta-modeling using kriging technique and multi-objective optimization with a desirability approach are support tools for obtaining regulation curves that can be implemented by means of some control algorithms in the stamping process investigated. In this work, the regulation curve of the force on the blank holder was obtained as a function of the yield stress for different lubrication conditions.
These curves could allow regulating in process the force on the blank holder, in view of Industry 4.0, avoiding defects at the end of the process, when there are random variations in the yield stress of the material coil or in the lubrication conditions.

From the results of the draw-in as a function of the punch stroke for some points, it emerges that, to have a safe stamped component, it is possible to monitoring the sheet sliding online by correcting the force on the blank holder in process if the draw-in differs from that in the optimal case.

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