BOAT: a cross-platform software for data analysis and numerical computing with arbitrary-precision

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Abstract

BOAT is a free cross-platform software for statistical data analysis and numerical computing. Thanks to its multiple-precision floating point engine, it allows arbitrary-precision calculations, whose digits of precision are only limited by the amount of memory of the host machine. At the core of the software is a simple and efficient expression language, whose use is facilitated by the assisted typing, the automatic engine and the built-in help for the syntax. In this paper a quick overview of the software is given. Detailed information, together with its applications to some case studies, is available at the BOAT web page [1].

1 Introduction

At present, several tools for statistical data analysis and numeric computing, including free and commercial software, are available on the market. Some of them have become industry standards, like SAS [2] and SPSS [3], while others like R [4], MATLAB [5] and ROOT [6] are widely used among scientists.

In this paper a new software, called BOAT, is presented. Obviously, it has not been thought and developed as a replacement of the previously mentioned software, which have benefited (feature-wise) from decades of development. Instead, the idea was to create a framework where to perform
frequently used statistical analyses (t-test, z-test, ANOVA, normality tests, etc...) and numerical computing with ease (thanks to a very simple and efficient syntax) and with arbitrary precision. The latter feature, in particular, makes BOAT more suitable, than many other available tools, in those scenarios where many digits of precision are requested. This is briefly explained in the following.

At present most of the floating-point computations are performed in double precision. The IEEE 754 standard [7] specifies the binary64 format (corresponding to the double data-types in the ISO C language) as having a significand precision of 53 bits, which corresponds to about 16 decimal digits of precision. Although this precision is more than enough in most of the practical cases, several applications in fields like Physics, Mathematics or Engineering require a higher precision.

Such applications include [8] studies on planetary orbit dynamics, zeroes of the Riemann Zeta function, Ising-class integrals or electromagnetic scattering theory to name a few. Another notable field of application is data security and in particular cryptography algorithms, like for example the RSA [9]. Its security is based on the very challenging problem of the decomposition of an integer into two prime numbers, when very large primes are involved. High level of security requires to handles prime numbers with many hundreds of digits [10].

In order to handle these scenarios, in the last decades, some libraries for arbitrary precision arithmetic have been developed, like the GNU Multiple Precision Arithmetic Library [11]. The general idea is to split large significands over several machine words of 64 bits or 32 bits, depending on the system architecture. This allows to reach a number of precision digits which is only limited by the available memory of the host machine. Notwithstanding the availability of these libraries, the number of software for statistical data analysis with full support of arbitrary precision arithmetic is quite limited [12].

BOAT allows arbitrary-precision calculations, not only for integer and float numbers, but also for complex numbers, vectors and matrices. Since high precision calculations can (sensibly) impact the performance, BOAT allows the user to choose the precision before each operation. In this way, many digits of precision can be reserved just for those calculations, which could really benefit from them. In addition to that, an automatic downcast...
to \textit{double} is performed for all those cases where arbitrary precision is not required, like for charts. A more extensive explanation about the arbitrary precision in BOAT is given in Section 5.

The support for arbitrary-precision calculations is only one of the key features in BOAT. Others include:

- compatibility with OSX, Windows and Linux (in beta);
- a modern graphical user interface with retina display support on OSX;
- a simple and effective expression language;
- an input console with assisted typing, syntax highlight and auto-complete functions;
- the support for several statistical analyses;
- a built-in help system.

In the following section an overview of the graphical user interface is given.
2 The Graphical User Interface

The main graphical user interface in BOAT is shown in Figure 1. It consists of three main elements: the info panel on the left, the input console on top-right of the window, and the output console which is placed just below the input console. Both input and output consoles are fully resizable.

2.1 The info panel

The info panel, organized into expandable tabs, provides an overview of all the objects which are temporarily or permanently stored in memory or on disk. BOAT defines four types of objects:

- *dataset*: a collection of data organized as a table of observations (rows) and variables (columns);
• variable: an identifier associated to a value of any supported data type (see Section 4);

• chart: an identifier associated to a graphical representation of data;

• report: any non BOAT-specific object (images, HTML pages, etc...).

The info panel also facilitates to manage objects, like delete or recall variables, exporting charts, edit datasets, etc...

2.2 The input console

The input console is the interface between the user and the BOAT expression language, and it has been designed to help writing the code. The list of features includes: syntax highlight, auto-complete, parentheses matching and assisted typing. The input console also supports editing multiple files, which are arranged into different tabs. Projects in different tabs will share all the objects listed in the info panel.

2.3 The output console

Most of the operations performed in BOAT result in a text output, which is shown in the output console. The content of the output console, being related to the code execution, is always temporary but it could be converted to a report object (plain text and HTML) to store it on disk permanently.

3 Syntax Overview

In this section a quick overview of the syntax is given. More detailed information is available on the online user guide [1]. BOAT is built around a user-friendly expression language by which every construction is an expression that returns an object (number, matrix, chart, etc...).

Expressions are separated by a newline and basic statements in BOAT consist of either an expression evaluation or a variable assignment. In the first case the result of the evaluation is printed on the output console and it is not saved, whereas, in an assignment statement, the result is passed to a variable and it is not displayed. This is clarified in the next example.
In Example 1 three statements are defined. The first line is a numerical calculation with integer numbers: BOAT evaluates the expression and displays the result in the output console (as shown Example 1: output). The second line is a variable assignment, which stores the result (of the same calculation as before) into a variable named \texttt{myvar}, and does not produce any output on screen. Finally, the third statement is again an expression evaluation, where the value associated to the previously defined variable is accessed. The corresponding result is again sent to the output console.

| Example 1: code | Example 1: output |
|-----------------|-------------------|
| $2^*(3 + 1)/4$  | 4                 |
| $\texttt{myvar} = 2^*(3 + 1)/4$ | 12 |
| $\texttt{MyVar} \times 3$ | \textbf{} |

Example 1 also shows two other important features of the expression language in BOAT:

- variables are identified by the prefix \$ and their data type does not have to be specified, as it is automatically determined;
- BOAT is case insensitive, so variables like $\texttt{myvar}$ and $\texttt{MyVar}$ are equivalent, and so are functions like \texttt{sqrt} and \texttt{sQRt}.

As previously stated, expressions are separated by a newline. However, in some practical cases, it could be preferable to handle a single long expression by splitting it over few lines. This can be done by placing the special char \% at the begin and end of the expression, as shown in Example 2.

| Example 2: code |
|-----------------|
| \% plot( [1, 2, 3],[3, -2, 1], \texttt{title = "test plot"}, \texttt{Xtitle = "x axis"}, \texttt{Ytitle = "y axis"}) \% |
Expressions can also be composed by one or more functions or one command. Functions in BOAT are operations which act on one or more of the supported data classes (see Section 4) and always return an object. On the other hand commands do not work on data and do not always return an object (for example those commands which only set software options). Another distinctive feature of functions is that they are usually (if they include CPU-intensive operations) processed in separate threads, so that the interface remains responsive. In Example 3, the use of some functions (returning different data classes) and commands is shown.

Example 3: code

| Code                | Description                  |
|---------------------|------------------------------|
| \texttt{log( 2 )}  | \texttt{\textbackslash \ function \ -> \ number} |
| \texttt{append([1, -2], 5)} | \texttt{\textbackslash \ function \ -> \ vector} |
| \texttt{invert([[1, 3, -1, 4], 2, 2])} | \texttt{\textbackslash \ function \ -> \ matrix} |
| \texttt{output\_precision \ 8} | \texttt{\textbackslash \ command \ -> \ no \ output} |
| \texttt{help invert} | \texttt{\textbackslash \ command \ -> \ output} |

4 Data types

BOAT handles four data classes: numbers, complex numbers, vectors, and matrices. The memory allocation for each data class is automatically determined on the basis of the provided data and the chosen precision. This means that, for example, BOAT will automatically decide whether to define a vector of integers or floats. Examples of different data class definitions (and assignments to variables) is shown in Example 4.

Example 4: code

| Code                                | Description             |
|-------------------------------------|-------------------------|
| $\texttt{int\_var = 54987}$          | $\texttt{\textbackslash \ integer \ number}$ |
| $\texttt{real\_var = \exp(1)}$     | $\texttt{\textbackslash \ real \ number}$ |
| $\texttt{com\_var = \{1, -3\}}$   | $\texttt{\textbackslash \ complex \ number}$ |
| $\texttt{vec\_var = [1, 3.1415, \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbackslash \textbacklash}|
| $\texttt{mat\_var = \{[4, 12, -1, 0], 2, 2\}}$ | $\texttt{\textbackslash \ matrix}$ |
In the following an overview of the supported data classes is provided. Detailed information and the full list of supported operations and functions is available at online user guide [1].

4.1 Numbers

As it will be discussed in more detail in Section 5, BOAT supports numbers with arbitrary precision. By default numbers are internally handled with 256 bit precision and displayed with 8 digits of precision (compatible with 32 bit precision). The precision of 256 bit is very optimized in BOAT and it is the recommended value to use. Operations involving integer numbers are automatically identified and a proper cast to integer in internally performed.

4.2 Complex Numbers

A complex number is defined by enclosing its real and imaginary parts, separated by a comma, in curly brackets, as shown in the following example.

| Example 5: code          | Example 5: output                      |
|-------------------------|----------------------------------------|
| {2, -3}                 | 2 - i 3                                |
| $x = {2, -1}$           |                                        |
| $y = {-1, 3}$           |                                        |
| \(\text{im} (x*y)\)    | 7                                      |

The fourth expression in Example 4 uses the function \(\text{im}\) to get the imaginary part of a complex number.

4.3 Vectors

A vector is a sequence of data elements of the same data type. It is defined by enclosing its components, separated by a comma, within square brackets. The data type of the vector components is automatically determined by BOAT. The following example shows the syntax to define a vector, the assignment to a variable, and few simple operations with vectors and numbers.
Example 6: code

\[
[1, 2, 3] \\
\$x = [ -1, \log(2)] \\
\$x \\
\$x + [1, 2] - 10 \\
\text{dotprod}([1, -2], [-3, 4])
\]

Example 5: output

\[
[1, 2, 3] \\
[-1, 0.69314718] \\
[-10, -7.3068528] \\
-11
\]

Example 4 also shows that \textit{functions} returning numbers (\texttt{log} in the example) can also be used in the vector definition.

4.4 Matrices

Matrices are defined by curly brackets, including a vector of data and two integers, \(r\) and \(c\), specifying the number of rows and columns of the matrix respectively. As for vectors, the data type of the matrix elements (and the consequent memory allocation for the matrix data class) is automatically determined by BOAT. In the following example a \(2 \times 3\) and a \(3 \times 3\) matrix is defined.

Example 7: code

\[
\{ [1, 3.4, 21.6, 19, -0.1, 10], 2, 3 \} \\
\{ [1, 3.4, 21.6, 19, -0.1, 10], 3, 3 \}
\]

Example 7: output

\[
\begin{array}{ccc}
1 & 3.4 & 21.6 \\
19 & -0.1 & 10 \\
\end{array} \\
\begin{array}{ccc}
1 & 3.4 & 21.6 \\
19 & -0.1 & 10 \\
0 & 0 & 0 \\
\end{array}
\]
As shown in Example 6, if the declared size of the matrix is bigger than the size of the vector data, the remaining elements are set to 0. BOAT has full support for matrix arithmetic and provides a set of functions for the most common operations (determinant, inverse, trace, etc...). The full list is available in the user guide [1].

4.5 Dataset

In addition to the four data classes described before, the dataset is a convenient object to handle input data. As already introduced in Section 2.4, a dataset is a collection of data which are organized as a table of observations (rows) and variables (columns). BOAT provides a handy graphical interface to import and edit datasets, which is shown in Figure 2.

Figure 2: The graphical interface to import and edit datasets in BOAT.

Datasets can be imported from few formats: CSV files, tabulated text files
Variables from a dataset can be accessed by specifying the corresponding column index (0-based) in the dataset table. For instance, given the dataset shown in Figure 2 called mydataset, the statement in Example 7 accesses the variable $X$.

Example 8: code

```bash
$mydataset[0]
```

Example 8: output

```
[0.6439767, 0.0746277, 0.79...]
```

5 Arbitrary Precision

As already introduced in Section 1, BOAT supports arbitrary precision arithmetic, which means that calculations can be performed with a precision which is only limited by the amount of the available memory of the host system. Unlike other available solutions, BOAT not only supports arbitrary precision for integer and float numbers, but for all data classes defined in Section 4. This means that also vector and matrix calculations can benefit from high precision.

Handling numbers with many digits of precision comes at the price of CPU time, which for most of the calculations is not justified. For this reason, BOAT allows to set the precision before each calculation. The `command precision` sets the internal precision to handle float numbers. The precision is specified by passing the number of 32 bit words used to store the number. If no value is specified, a summary of the current precision scheme is returned to the output console.

Example 9: code

```
precision 2
precision
```
In the following example, the same calculation is performed with two different levels of precision. In the first case the number $\pi$ ($\text{pi()}$) is computed with 64 bit precision (\texttt{precision 2}), while, in the second case, a 192 bit precision (\texttt{precision 6}) is used. The function \texttt{pi()} uses the Bailey-Borwein-Plouffe formula for calculating $\pi$ \cite{13}.

\begin{verbatim}
Example 9: output

Internal precision is set to 2 (memory blocks)
Actual precision: 64 bits
Number of printed digits: 16
\end{verbatim}

\begin{verbatim}
Example 10: code

\texttt{precision 2}
\texttt{pi()}
\texttt{precision 6}
\texttt{pi()}
\texttt{precision}
\end{verbatim}

\begin{verbatim}
Example 10: output

3.141592653589793
3.14159265358979323846264338327950288419716939938

Internal precision is set to 6 (memory blocks)
Actual precision: 192 bits
Number of printed digits: 48
\end{verbatim}

In some cases, it could be preferable to work with many digits of precision but to reduce the number of digits displayed on screen or stored into a report. The command \texttt{(output\_precision)} specifies the number of digits to
be printed. In the following example the calculation of $\log(2)$ is performed with 192 bit precision but the result is printed with just two significant figures.

Example 11: code

```boat
precision 6
output_precision 2
precision
pi()
```

Example 11: output

```
Internal precision is set to 6 (memory blocks)
Actual precision: 192 bits
Number of printed digits: 2

0.69
```

6 Charts

BOAT comes with a chart suite for data visualization. The list of supported charts is available at the online user guide [1]. The function `plot` provides a general template to plot data, starting from vectors or datasets. The following example shows the creation of a plot starting from two same-size vectors.

Example 12: code

```boat
$x = sequence(-1, 1, 0.1)
$y = cos($x) * sin($x)
plot($x, $y, xtitle="x [rad]", ytitle="cos(x)*sin(x)")
```
The first assignment statement uses the function \texttt{sequence} to create a vector with values from \(-1\) to \(1\) with a step of \(0.1\). In the second statement functions \texttt{cos} and \texttt{sin} act on each component of the vector \(x\) to create a new vector \(y\). The output of Example 12 is shown in Figure 3.

Figure 3: Chart windows in BOAT. The chart inspector on the left allows to change the appearance of a chart.

The layout of a chart can be customized either by specifying the options in the corresponding statement (as it was done with \texttt{xtitle} and \texttt{ytitle} in Example 12) or by using the chart inspector panel. The chart inspector panel (the left panel in Figure 3), can be optionally shown from each chart to edit its appearance.

Although \texttt{plot} is the general template to produce plots, some other functions (like \texttt{frequency} for example) automatically produce a chart as output.

7 Reports

Some functions and commands can optionally produce printable reports, which usually contain charts, tables and text. All the reports, produced
by a project, are accessible from the corresponding tab in the info panel. At present the supported formats are: images, RTF (for compatibility with almost all word processors), and HTML.

The following example performs a one-sample z-test on the vector ($x$). The option report=true enables the creation of the HTML report shown in Figure 7, which summarizes all the relevant information from the test.

Example 12: code

```r
x = [9, 3, -1, -2, 4, 5]
ztest(x, 2, 3, report=true)
```

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Figure 4: HTML report from a one-sample $z$-test (two-sided).

|                |        |
|----------------|--------|
| **One Sample $z$-test** |        |
| mean           | 3      |
| $z$            | 0.74535599 |
| $p$-value      | 0.45605654 |

**Alternative hypothesis:**

true mean is not equal to 2

95% CL interval: $[-0.62956764, \ 4.6295676 ]$

8 Conclusions

BOAT is a cross-platform software for data analysis and numerical computing, which can be freely downloaded from the official web page [I]. It has been designed and developed with the goal of providing an easy-to-use tool for statistical data analysis, with support for arbitrary precision. The very first release of the software basically laid the foundation, but expansion of features and optimization are expected for the next versions.
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