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Reactive mission and motion planning with deadlock resolution avoiding dynamic obstacles

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Abstract In the near future mobile robots, such as personal robots or mobile manipulators, will share the workspace with other robots and humans. We present a method for mission and motion planning that applies to small teams of robots performing a task in an environment with moving obstacles, such as humans. Given a mission specification written in linear temporal logic, such as patrolling a set of rooms, we synthesize an automaton from which the robots can extract valid strategies. This centralized automaton is executed by the robots in the team at runtime, and in conjunction with a distributed motion planner that guarantees avoidance of moving obstacles. Our contribution is a correct-by-construction synthesis approach to multi-robot mission planning that guarantees collision avoidance with respect to moving obstacles, guarantees satisfaction of the mission specification and resolves encountered deadlocks, where a moving obstacle blocks the robot temporally. Our method provides conditions under which deadlock will be avoided by identifying environment behaviors that, when encountered at runtime, may prevent the robot team from achieving its goals. In particular, (1) it identifies deadlock conditions; (2) it is able to check whether they can be resolved; and (3) the robots implement the deadlock resolution policy locally in a distributed manner. The approach is capable of synthesizing and executing plans even with a high density of dynamic obstacles. In contrast to many existing approaches to mission and motion planning, it is scalable with the number of moving obstacles. We demonstrate the approach in physical experiments with walking humanoids moving in 2D environments and in simulation with aerial vehicles (quadrotors) navigating in 2D and 3D environments.

Keywords Multi-robot systems · Formal methods · Mission specification · Motion planning · Deadlock resolution · Dynamic environments

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1 Introduction

Mobile robots, such as package delivery robots, personal assistants, surveillance robots, cleaning robots, mobile manipulators or autonomous cars, execute possibly complex tasks and must share their workspace with other robots and humans. For example, consider the case shown in Fig. 1 in which two mobile robots are tasked with patrolling and cleaning the rooms of a museum. What makes this task challenging is that the environment in which the robots operate could be filled with static obstacles, as well as dynamic obstacles, such as people or doors, that could lead to collisions or block the robot. To guarantee the task of continuously monitoring all the rooms, each robot must react to the environment at runtime in a way that does not prevent making progress toward fulfilling the overall mission. In particular, we describe an approach for navigation in dynamic environments that is able to satisfy a mission by resolving deadlocks, i.e. situations where a robot is temporally blocked by a dynamic obstacle and can not make progress towards achieving its mission, at runtime.

Planning for multi-agent systems has been explored extensively in the past. Many have focused on approaches for local motion planning (van den Berg et al. 2009; Alonso-Mora et al. 2010) that offer collision avoidance in cluttered, dynamic environments. While these approaches are effective for point-to-point navigation, the planning is myopic and could fail when applied to complex tasks in complex workspaces. On the other hand, it has been demonstrated that correct-by-construction synthesis from linear temporal logic (LTL) specifications has utility for composing basic (atomic) actions to guarantee the task in response to sensor events (Kress-Gazit et al. 2009; Ehlers et al. 2015; Liu et al. 2013; Wongpiromsarn et al. 2012). Such approaches are naturally conducive to mission specifications written in structured English (Kress-Gazit et al. 2008), which are translatable into LTL formulas over variables representing the atomic actions and sensor events associated with the task.

In the surveillance-cleaning scenario of Fig. 1, the motion (moving between rooms), atomic actions (e.g., “remove garbage”, “identify a subject”), and binary sensors (e.g. “intruder sensing”, “garbage sensing”) are assumed to be perfect: they are treated as black boxes that always return the correct result and hence admit a discrete abstraction that is appropriate for the task and workspace. A major challenge underpinning this approach is in creating atomic elements holding guarantees for correct execution of the discrete abstraction. To guarantee motion fulfillment, researchers have explored combining LTL-based planners with grid planners (Bhatia et al. 2010), sampling-based planners (Karaman and Frazzoli 2009), or planners for multiple robots predicated on motion primitives (Saha et al. 2016). Such approaches are able to guarantee motion in cluttered environments but do not readily extend these guarantees to cases where the environment is dynamic in nature. Solutions have been sought that, in a computationally expensive manner, partition the workspace finely (Livingston et al. 2013; Wongpiromsarn et al. 2012) or re-compute the motion plan (Bhatia et al. 2010), or else apply conservative constraints forbidding the robot to occupy the same region as an adversarial agent (Kress-Gazit et al. 2008).

1.1 Approach

In the approach introduced in this paper, we alleviate such difficulties by considering an integration of a high-level mission planner with a local planner that guarantees collision-free motion in three dimensional workspaces when faced with both static and dynamic obstacles, under the assumption that the dynamic obstacles are not intentionally adversarial. In this context, “intentionally adversarial” means that the dynamic obstacles may behave in a way that may temporarily prevent the robot from achieving a goal, but cannot move in a way that actively always prevents the robot from achieving its goals, for instance by blocking the robot forever. Our integration involves two components: an offline algorithm for plan synthesis adopting the benefit of an LTL formalism, and an online local planning algorithm for executing the plan. Our approach is centralized for the robots in the team, which execute the high-level specification, and decentralized with respect to moving obstacles, i.e. we do not control the moving
obstacles yet perform decentralized avoidance and deadlock resolution strategies. While the robots are able to measure the position and velocity of moving obstacles, they only need to do so within a local range of the robot—the key assumption in this paper is that the robots are not required to have global knowledge of their environment.

The basis of the offline synthesis is a novel discrete abstraction of the problem that applies simple rules to resolve physical deadlocks, between two or more robots in a team or between a robot and a dynamic obstacle. This abstraction is composed with a specification of a multi-agent task to synthesize a strategy automaton encoding the mission plan. In contrast to approaches that would require on-the-fly re-planning upon encountering a physical deadlock (Bhatia et al. 2010; Maly et al. 2013; Karaman and Frazzoli 2009), the approach we propose automatically generates alternative plans within the synthesized automaton. As with any reactive task, there may exist no mission plan that guarantees the task, due to the conservative requirement that a mission plan must execute under all possible environment behaviors. To address this conservatism, our approach automatically identifies for which environment behaviors the mission is guaranteed to hold. These additional assumptions are transformed succinctly into a certificate of task infeasibility that is explained to the user.

The online execution component is based on a local planner that can optimally avoid dynamic obstacles in two- or three-dimensions, executed as a service called during execution of the strategy automaton. Given a dynamic model of the robots and a coarse description of the moving agents (e.g. their maximum velocities) our local planner computes a plan that guarantees collision-free motion between the robot and static and dynamic obstacles. The collision-avoidance feature obviates the need for collision avoidance to be taken care of by the discrete abstraction. It furthermore allows our local planner to preserve the behaviors of the strategy automaton, by preventing a robot from entering unintended regions as it carries out its task. To the authors’ knowledge, this is the first end-to-end system that has been devised to guarantee multi-agent mission-level tasks in dynamic environments using optimization-based local planners.

The proposed deadlock resolution approach is motivated by works in event-driven planning (e.g. Dimarogonas et al. 2012), but yields a strategy that scales well with the number of dynamic obstacles without incurring conservatism that would prevent mission plans from being synthesized. In particular,

- Our approach establishes proof for task success without requiring a costly re-planning step or fine workspace discretization, as long as the environment that causes deadlocks behaves according to the generated assumptions.

- Our approach comes with proof that admissible deadlocks are always resolved and livelocks (the situation where a robot is free to move but unable to reach a goal) never occur.

- The fully automated nature of our approach has practical utility, since the user does not need to intervene to debug specifications. In fact, our approach explains, in an intelligible way, any additional environment assumptions it has added.

- Another practical feature of our approach is that, unlike related planners (Livingston et al. 2013; Kress-Gazitt et al. 2008), we do not require global knowledge of the obstacles. As we show, this allows our approach to scale to an arbitrary number of dynamic obstacles, as long as the aggregate behavior of the obstacles adhere to all specified assumptions.

Our approach is well-suited for any dynamic environment, but we emphasize its particular value to human environments. Specifically, our automatically-generated environment assumptions are transformed into human-readable certificates such as:

The synthesized controller is certified for this task, if any encountered deadlock between the robot and a dynamic obstacle in the hallway resolves eventually.

The certificates provide, at synthesis time, a set of rules defining situations which could make it impossible for the robot to achieve its goals, with the purpose of creating a layer of cooperation between the user (i.e. the human that performs the controller synthesis and deploys the system) and the robots. This frees a user from having to come up with assumptions that characterize the environment’s behavior, a difficult proposition in practice. If these assumptions are broken at runtime, then this signifies that the task is no longer strictly guaranteed. Our approach also aims to reduce situations where members of the robot team become deadlocked with one another, by adopting a coordination strategy in the specification preventing actions that may induce deadlocks.

A more detailed overview of the approach is given in Sect. 4, right after formalizing the problem in Sect. 3.

1.2 Contribution

This paper presents two main contributions toward reactive mission and motion planning with deadlock resolution among dynamic obstacles.

- A holistic synthesis approach to provably achieve collision-free behaviors in dynamic environments with an arbitrary number of moving obstacles that does not require mutual exclusion. The approach leverages (a) reactive mission planning to globally resolve deadlocks
and achieve the specified task, and (b) online local motion planning to guarantee collision-free motion and respect the robot kinodynamics.

- An automatic means for encoding tasks that resolve deadlock based on automatically-generated revisions to a specification. Our approach automatically generates human-comprehensible assumptions in LTL that, if satisfied by the controlled robots and the dynamic obstacles, would ensure correct behavior. We show that our revision approach is sufficient in making the original specification realizable.

We also contribute an optimization-based method for local motion planning that guarantees real-time collision avoidance with static and dynamic obstacles in 3D environments while remaining faithful to the robot’s dynamics. The method extends (Alonso-Mora et al. 2015) by efficiently computing the robot’s local free-space in cluttered environments. Yet, the reader may opt for a different local planner and maintain the synthesis approach, as long as the local planner provides avoidance guarantees. The method is evaluated in experiments with ground robots and in simulations with aerial vehicles.

In a preliminary version of this work (DeCastro et al. 2015), a strategy was developed for synthesizing controllers for guaranteed collision-free motion of a robot team. In this paper, we extend those results by presenting a complete description of the proposed abstraction method and offline controller synthesis procedure, solidify details on the mathematical derivation for the constraints of the local motion planner, and provide in-depth evaluation of our proposed synthesis techniques aided by both simulation and physical experiments. Additionally, we enhance the approach in two ways. First, our approach reasons about the geometry of workspace regions in order to avoid preventable deadlock. For instance, if a corridor is only wide enough for one robot, we offer an approach that coordinates the actions of two robots so that they do not head in opposite directions in the corridor. Second, we present a general approach that allows a richer set of deadlock resolution rules to be chosen at synthesis time.

1.3 Related work

1.3.1 Reactive synthesis for mission planning

A number of approaches are suited to automatic synthesis of correct-by-construction controllers from mission specifications written as temporal logic formulas (Bhatia et al. 2010; Karaman and Frazzoli 2009; Loizou and Kryiakopoulos 2004). Reactive synthesis (Kress-Gazit et al. 2009; Wongpiromsarn et al. 2012) extends these capabilities to tasks in which the desired outcome depends on uncontrolled events in the environment and changing sensor inputs, and is especially compelling given the complex nature of multi-agent scenarios. For instance, Ulusoy et al. (2013) synthesized control and communication for producing optimal multi-robot trajectories, Chen et al. (2012) distributed a specification among a robot team, and Raman and Kress-Gazit (2014), Raman (2014) synthesized centralized reactive controllers based on analytically constructed multi-robot motion controllers. Distributed and decomposition-based planning approaches tackle the complexity problem when scaling to a large number of robots. For instance, Tumova and Dimarogonas (2015) construct distributed controllers from specifications already separated into coordinating and non-coordinating tasks, while Schillinger et al. (2016) automatically decompose a specification into independent, distributed task specifications. In most approaches, moving obstacles are modeled in a discrete manner as part of the abstraction, leading to over-conservative restrictions like requiring robots to be at least one region apart. In contrast, our method only requires local awareness of the robot’s surroundings, and guarantees collision-avoidance via a local planner.

Reactive synthesis in dynamically-changing environments presents a crucial dilemma: explicitly modeling the state of all other agents can be computationally prohibitive, but incomplete models of the environment destroy task satisfaction guarantees. To address the state-explosion problem while tracking the state of uncontrollable agents, Wongpiromsarn et al. (2013) formulated an incremental synthesis procedure that started with a set number of agents assumed observable, and added more agents to this set depending on available computational resources; however, unlike our approach, they still required global knowledge of the external agents. The authors in Livingston et al. (2013), on the other hand, made local modifications to the synthesized strategy when new elements of the environment were discovered that violated the original assumptions. While we also update our specification, we differ from Livingston et al. (2013) in that no re-synthesis step is needed at runtime, thereby preserving guarantees before runtime.

Our goal is different in that we assume a centralized high-level controller that guarantees the specification through deadlock resolution by choosing environment assumptions to avoid both deadlock and livelock.

1.3.2 Specification revisions

Recent efforts in reactive synthesis have focused on automatically identifying certain environment assumptions that may prevent the existence of a controller that satisfies the task. Approaches to assumption-mining have provided techniques that enable automatic specification debugging for specifi-
cations of any structure (Alur et al. 2013; Li et al. 2011). While providing the ability to automate the debugging process, they still require input from the user, for instance the variables the user desires and a final selection of candidate assumptions generated by the algorithm, which has drawbacks for realizing a fully-automated robotic mission planner. An assumption-mining approach to certify the necessary environment assumptions for a given task and robot dynamics was introduced in DeCastro et al. (2016), however, the dynamics-based abstraction do not extend naturally to multi-agent scenarios. This proposed approach obviates the need for the user to intervene during the planning process.

We propose a novel approach in which assumptions on the environment are generated to identify likely deadlock situations. These added assumptions may be interpreted as restricting the mobility of the uncontrolled agents and are relaxed, when possible, by identifying when they may be violated, if only on a temporary basis. In this regard, our approach is inspired by works on error resilience (Ehlers and Topcu 2014) and recovery (Wong et al. 2014) in reactive synthesis.

1.3.3 Motion planning in dynamic environments

Collision-free (and deadlock-free) motion planning for multirobot teams has been successfully demonstrated via non-convex optimization, as proposed in Bento et al. (2013) and Mellinger et al. (2012), but these approaches did not account for dynamic obstacles, nor could be computed in real-time. On the other hand, convex optimization approaches for collision avoidance, such as van den Berg et al. (2009) and Alonso-Mora et al. (2010), are online and account for dynamic obstacles, but cannot reason globally to resolve deadlocks. In this work, we extend these works to enforce collision avoidance and motion constraints over a short time horizon, where the global execution is given by a discrete controller synthesized from a mission specification.

Also relevant to our efforts are the works in deadlock resolution. The authors of Knepper and Rus (2012) applied pedestrian-avoidance principles to deadlock resolution in narrow passageways. While our approach is similarly reactive to the environment, we additionally reason about situations that cannot be locally resolved (e.g. a blocked corridor). Along similar lines, Cirillo et al. (2014) described a centralized graph search technique for motion planning, but did not consider dynamic obstacles, and required a rich underlying graph to represent multi-robot motions with kinematic constraints. In contrast, our proposed local planning approach presents a more concise discrete abstraction and also applies to 3D environments. Traditional motion planning approaches such as RRT (LaValle and Kuffner 2001), PRM (Hsu et al. 2007) and lattice based planners (Pivtoraiko et al. 2009) can also be applied to compute collision—and deadlock—free motions for a single robot. But, in contrast to our synthesis approach, they do not typically reason about the mission strategy of multiple robots, or encode logical constraints representing mission specifications.

1.4 Organization

The remainder of this paper is structured as follows. The required concepts for offline synthesis and online motion planning are described in Sect. 2. We formalize the problem in Sect. 3 and give an overview of the method in Sect. 4. In Sect. 5, we introduce a strategy for mission planning for resolving deadlock at runtime, while, in Sect. 6, we introduce an automated approach for generating runtime certificates and a coordination scheme for mission planning. In Sect. 7, we describe the online motion planner. We provide theoretical guarantees of the integrated approach in Sect. 8. In Sect. 9, we present extensive simulation and experimental results. Conclusions and future work are provided in Sect. 10.

2 Preliminaries

Throughout this paper scalars are denoted in italics, $x$, and vectors in bold, $x \in \mathbb{R}^n$, with $n$ denoting the dimension of the workspace. The robot’s current position is denoted by $p \in \mathbb{R}^n$ and its current velocity by $v = \dot{p}$. A map of the workspace $W \subset \mathbb{R}^n$ is considered, and formed by a set of static obstacles, given by a list of polytopes, $O \subset \mathbb{R}^n$. For mission synthesis the map is abstracted by a set of discrete regions $R = \{R_1, \ldots, R_p\}$, and their topological connections, covering the obstacle-free workspace $F = \mathbb{R}^n \setminus O$, where the open sets $R_a \subseteq W$.

We consider robots moving in $\mathbb{R}^3$ and approximate them by their smallest enclosing cylinder of radius $r$ and height $2h$, denoted by $V$. Its $\epsilon$-additive dilation of radius $\tilde{r} = r + \epsilon$ and height $\tilde{h} = h + \epsilon$ is denoted by $V_\epsilon$. For a set $X \subset \mathbb{R}^n$ we denote the collision set by $X + V = \{p \in \mathbb{R}^n \mid X \cap V(p) \neq \emptyset\}$, with $V(p)$ a volume $V$ at position $p$. Throughout, the notation $\| \cdot \|$ is used to denote the Euclidean norm.

We consider a set of dynamic obstacles $DO$ and denote the volume occupied by a dynamic obstacle $i \in DO$, at position $p_i$, by $V_i(p_i)$. To be able to prove safety in dynamic environments, we assume that all moving obstacles either maintain a constant velocity during the planning horizon (a couple of seconds), or that they employ an identical algorithm for collision avoidance as our robots, as introduced in the Reciprocal Velocity Obstacles literature (Alonso-Mora et al. 2015). In this work we do not treat the case where moving obstacles seek collisions and are capable of overtaking the robots. Instead, we assume a fair environment—one where it is always possible for the robots to avoid collisions—such as
the case when operating with humans or other risk-adverse agents.

2.1 Linear temporal logic

LTL formulas are defined over the set $AP$ of atomic (Boolean) propositions by the recursive grammar $\varphi ::= \pi \in AP | \varphi_1 \land \varphi_2 | \neg \varphi | \varphi_1 \lor \varphi_2$. From the Boolean operators $\land$ “conjunction” and $\lor$ “disjunction”, and the temporal operators $\circ$ “next” and $\square$ “until”, the following operators are derived: “disjunction” $\lor$, “implication” $\Rightarrow$, “equivalence” $\Leftrightarrow$, “always” $\square$, and “eventually” $\diamond$. We refer the reader to Vardi (1996) for a description of the semantics of LTL. Let $AP$ represent the set of atomic propositions, consisting of environment propositions ($X$) corresponding to thresholded sensor values, and system propositions ($Y$) corresponding to the robot’s actions and location with respect to a partitioning of the workspace. The value of each $\pi \in X \cup Y$ is the abstracted binary state of a low-level component. These might correspond to, for instance, thresholded sensor values, discrete actions that a robot can take, or a discrete region (e.g. room in a house).

**Definition 1** (Reactive mission specification) A reactive mission specification is a LTL formula of the form $\varphi = \varphi^s_i \land \varphi^e_i \land \varphi^g_i \Rightarrow \varphi^t_i \land \varphi^e_i \land \varphi^g_i$, with $s$ and $e$ standing for ‘system’ and ‘environment’, such that

- $\varphi^s_i$, $\varphi^e_i$ are formulas for the initial conditions free of temporal operators.
- $\varphi^s_i$, $\varphi^r_i$ are the safety conditions (transitions) to be satisfied always, and are of the form $\square \psi$, where $\psi$ is a Boolean formula constructed from subformulas in $AP \cup \square AP$.
- $\varphi^r_i$, $\varphi^g_i$ are the liveness conditions (goals) to be satisfied infinitely often, with each taking the form $\square \diamond \psi$, with $\psi$ a Boolean formula constructed from subformulas in $AP \cup \square AP$.

A strategy automaton that realizes a reactive mission specification $\varphi$ is a deterministic strategy that, given a finite sequence of truth assignments to the variables in $X$ and $Y$, and the next truth assignment to variables in $X$, provides a truth assignment to variables in $Y$ such that the resulting infinite sequence satisfies $\varphi$. If such a strategy can be found, $\varphi$ is realizable. Otherwise, it is unrealizable. Using a fragment of LTL known as generalized reactivity(1), a strategy automata for $\varphi$ of the form above can be efficiently synthesized (Bloem et al. 2012), and converted into hybrid controllers for robotic systems by invoking atomic controllers (Kress-Gazit et al. 2009). These controllers are reactive: they respond to sensor events at runtime.

2.2 LTL encoding for multi-robot tasks

We adopt a LTL encoding of a centralized multi-robot mission that is robust to the inherent variability in the duration of inter-region robot motion in continuous environments (Raman et al. 2013). Let $AP_R = \{\pi^i_\alpha \mid \alpha \in R\}$ be the set of Boolean propositions representing the workspace regions, such that $\pi^i_\alpha \in AP_R$ is true when robot $i$ is physically in $\alpha$, for $\alpha \in [1, \ldots, p]$. We call $\pi^i_\alpha$ in $AP_R \subseteq X$ a completion proposition, signaling when robot $i$ is physically inside $\alpha$. We also define the set $AP^{act}_R \subseteq Y$ that captures robot commands that initiate movement between regions. We call $\pi^{i,act}_\alpha$ in $AP^{act}_R$ an activation variable for moving to $\alpha$ (but has not necessarily completed motion to $\alpha$). Non-motion actions are handled similarly. Observe that $\pi^i_\alpha$ and $\pi^{i,act}_\alpha$ may be true at the same time if robot $i$ is in $\alpha$ and is moving toward $\alpha$, where $\alpha$ and $\alpha'$ are adjacent regions. Also note that this is sufficient for the special case $\pi^i_\alpha$ and $\pi^{i,act}_\alpha$ (the robot stays put). We assume reasonably that non-motion actions are independent of motion, so that actions themselves do not involve moving within any particular region and, if it is possible to execute a particular action within a region, it can be performed anywhere within that region.

We now solidify the semantics of the LTL formulas in the context of robot mission and motion planning. Let $T$ denote a particular fixed time step at which the strategy automaton is updated with sensory information and supplies a new input to the local planner (as described in Sect. 4.3). A proposition $\pi \in AP$ is true at time $t > 0$ iff $\square \pi \in \square AP$ is true at $t + T$.

**Definition 2** [LTL encoding of motion (Raman et al. 2013)]

A task encoding that admits arbitrary controller execution durations is

$$
\varphi^s_i : \bigwedge_{\pi^i_\alpha \in AP_R, \ i \in [1, n_{robots}]} \left( \square \pi^i_\alpha \Rightarrow \bigvee_{R_\beta \in Adj(R_\alpha)} \square \pi^{i,act}_\beta \right),
$$

$$
\varphi^e_i : \bigwedge_{\pi^i_\alpha \in AP_R, \ i \in [1, n_{robots}]} \left( \pi^i_\alpha \land \pi^{i,act}_\beta \Rightarrow \square \pi^i_\alpha \lor \square \pi^{i,act}_\beta \right),
$$

$$
\varphi^r_i : \square \diamond \bigvee_{\pi^{i,act}_\alpha \in AP^{act}_R, \ i \in [1, n_{robots}]} \left( \left( \pi^{i,act}_\alpha \land \bigcirc (\pi^{i,act}_\alpha \lor \neg \pi^{i,act}_\alpha) \right) \lor \left( \neg \pi^{i,act}_\alpha \land \bigcirc (\neg \pi^{i,act}_\alpha \lor \pi^{i,act}_\alpha) \right) \right),
$$

where $Adj : R \rightarrow 2^R$ is an adjacency relation on regions in $R$ and $n_{robots}$ is the number of robots. The $\varphi^r_i$-formula is a system safety condition describing which actions can occur ($\bigcirc \pi^{i,act}_\beta$) given the observed completion variables...
Formula $\phi^e_i$ captures the allowed transitions ($\bigcirc \pi^e_i$) given past completion ($\pi^t_i$) and activation ($\pi^l_{act,i}$) variables. Formula $\phi^g_i$ enforces that every motion and every action eventually completes (first disjunct) as long as the activation variable is held fixed (second disjunct). Specifically, the second disjunct in this formula allows the system to change its mind for a given action, absolving the environment from having to complete motion for that action. Both $\phi^e_i$ and $\phi^g_i$ are included as conjuncts to the antecedent of $\varphi$.

Take, for example, two regions $R_1$ and $R_2$, arranged as shown in Fig. 2, with a robot positioned in $R_1$ and heading toward $R_2$. The system can only take a subset of actions; in this case, it is free to stay in $R_1$ or move to $R_2$:

$\Box (\bigcirc \pi^t_1 \implies \bigcirc \pi^l_{act,1} \lor \bigcirc \pi^l_{act,2})$.

Upon taking an action, for instance move to $R_2$ (activate $\pi^l_{act,2}$), the system is allowed to be in either of the two regions

$\Box \bigcirc (\pi^l_{act,1} \land \pi^l_{act,2} \implies \bigcirc \pi^l_{act,1} \lor \bigcirc \pi^l_{act,2})$, 

and the environment must eventually allow the system to either arrive at this region or change course

$\Box \bigcirc (\bigcirc \pi^t_2 \lor \bigcirc (\pi^t_2 \lor \neg \pi^l_{act,2})) \lor (\neg \pi^l_{act,1} \land \pi^l_{act,2})$.

To complete the motion encoding, mutual exclusion is also enforced to express the fact that the robot can only be in one region at a time and must decide on one motion at a time. That is, $\Box (\pi^l_{act,1} \lor \pi^l_{act,2})$ and $\Box (\pi^l_{act,1} \lor \pi^l_{act,2})$.

We note that it is shown in Ehlers (2013) that complexity of synthesis under the generalized reactivity(1) fragment is polynomial in the size of the state space of the game structure that is, in turn, at most exponential in the total number of propositions. Considering motion alone, the formulas effectively impose restrictions to the allowed state transitions to only consider those that are physically adjacent, effectively reducing the size of the synthesis problem.

### 3 Problem formulation

This work combines global planning with local motion planning to produce a correct-by-construction synthesis method that avoids collisions locally yet is able to resolve deadlocks. Synthesis is carried out in a fully-automated way; when modifications to the original specification are necessary, these are explained to the user in an intelligible manner. We provide an example to motivate our correct-by-construction synthesis method.

**Example 1** Consider the workspace in Fig. 3b, where two robots are tasked with visiting regions Goal1 and Goal2 infinitely often; that is,

$$\phi^g_i = \bigwedge_{i \in \{1,2\}} \Box \bigcirc (\pi^l_{Goal1}) \land \Box \bigcirc (\pi^l_{Goal2}).$$

Figure 3 illustrates two approaches for solving this task. Figure 3a, b show the result of applying a local motion planning scheme to locally avoid collisions with other robots or dynamic obstacles. In certain instances, such as the case shown in Fig. 3b, deadlocks can lead to the execution failing to satisfy the task.

Our approach, shown in Fig. 3c, relies on a local motion planner to allow several agents per region and avoid dynamic obstacles, as in Fig. 3a. Furthermore, it is able to resolve encountered deadlocks that may arise. In this example, when one of the robots encounters deadlock, it reverses its motion to allow the other one to pass into Goal 1, ultimately taking another route to Goal 2.

**Definition 3** (Collision) A robot at position $p$ is in collision with a static obstacle if $V(p) \cap \mathcal{O} \neq \emptyset$. The robot is in collision with a dynamic obstacle $i$ at position $p_i$ and of volume $V_i(p_i)$ if $V(p) \cap V_i(p_i) \neq \emptyset$.

Denote by $p(t)$ the position of a robot at time $t$ and by $p_i(t)$ the position of a dynamic obstacle $i$ at time $t$. The trajectory of the dynamic obstacles is estimated between the current time $t_k$ and a time horizon $\tau$. In our model we consider constant velocity.

**Definition 4** (Collision free local motion) A trajectory is said to be collision free if for all times between $t_k$ and the time horizon there is no collision between the robot and any static or dynamic obstacle,

$$V(p(t)) \cap \bigcup_{i \in \mathcal{O}} V_i(p_i(t)) = \emptyset \quad \forall t \in [t_k, t_k + \tau]. \quad (1)$$
Examples of integrated mission and motion planning. The blue robot starts in the region Goal 1 (top) and is tasked to visit Goal 2 (bottom right) and return to Goal 1. The red robot is placed in the region Goal 2 and is tasked to visit Goal 1 and return. The shortest path for both robots, given by solving a specification $\phi$ is to go through the corridor on the right. In (a), an execution of a specification $\phi$ using a local planner that locally avoids the collision between both robots and succeeds in executing the mission, b employs the same specification as (a), but the workspace is shrunk, resulting in a deadlock at location *. c shows an execution of a controller synthesized from the modified specification $\phi''$ using the deadlock resolution strategy and local planner developed in this work. With our approach, dynamic obstacles can be avoided locally, as in (a), and deadlocks can also be resolved (Color figure online).

Which is equivalent to

$$V(p(t)) \subseteq F \quad \text{and} \quad V(p(t)) \cap V_i(p_i(t)) = \emptyset \quad \forall t \in [t_k, t_k + \tau], \forall i \in DO.$$ (2)

**Definition 5 (Deadlock)** In this work we consider motion related deadlocks. A robot at position $p$ is said to be in a deadlock if it is not in a collision, it has not achieved the target given by the automaton and it can not make progress towards the goal, i.e. it is not moving, for a prespecified amount of time.

The goal of this work is to solve a set of problems as follows.

**Problem 1 (Local collision avoidance)** Given the dynamics for each robot in the team, construct an online local planner that guarantees collision avoidance with static and dynamic (moving) obstacles.

**Problem 2 (Synthesis of strategy automaton with deadlock resolution)** Given a topological map, a local motion planner that solves Problem 1 and a realizable mission specification $\phi$ that ignores collisions, automatically construct a specification $\phi'$ that includes both $\phi$ and a model of deadlock between robots and unmodeled dynamic obstacles. Use $\phi'$ to synthesize a controller that satisfies $\phi'$.

This synthesized controller will re-route the robots to resolve deadlocks (should they occur), while satisfying the reactive mission specification and remaining livelock free. For mission specifications that consider the presence of possible deadlocks, there may be no satisfying controller. We therefore synthesize environment assumption revisions as additional LTL formulas to identify cases where dynamic obstacles may trigger deadlock and trap the system from achieving its goals. These formulas are significant because they offer certificates explaining the required behaviors of the environment that, if followed, guarantee that the robot team will carry out the task. Such certificates must be conveyed to the user in a clear, understandable manner. An example of such a condition is: “the environment will never cause deadlock if robot 1 is in the kitchen and moving to the door”. This leads to the following Problem.

**Problem 3 (Revising environment assumptions)** Given an unrealizable reactive mission specification $\phi'$, synthesize environment assumption revisions $[\phi^e \mid \text{rev}]$ such that the specification $\phi''$ formed by replacing $\phi^e$ with $[\phi^e \mid \text{rev}]$ is realizable, and provide the user with a human-readable description of these revisions as certificates for guaranteeing the task.

### 4 Approach

This work solves Problems 1, 2 and 3 via a combined offline and online approach, which (a) synthesizes a strategy automaton that realizes the mission and (b) computes a local motion planner that executes the automaton in a collision-free manner. Figure 4 highlights the offline and online components and their interconnections, which we now introduce.

#### 4.1 Offline

The inputs for the offline part of the method are: (a) a user given mission specification, (b) a discrete topological map...
4.1.1 Mission planning

In this step we synthesize a centralized controller, or finite state machine, that will guide the robots in the team through the topological map. This controller considers possible physical deadlocks between robots in the team as well as with moving obstacles. Since the position of the moving obstacles is not known at synthesis time, environment assumptions are iteratively revised as necessary. The resulting strategy automaton with the revisions included accommodate deadlocks wherever they may occur at runtime, and fulfillment of the specification is guaranteed as long as the environment behaves according to the assumptions explained to the user in the revisions generation step. We also adopt a recovery scheme (Wong et al. 2014) that synthesizes a strategy that allows violations of environment safety assumptions to be tolerated, retaining satisfaction guarantees as long as the violation is transient.

The mission planning part of the offline synthesis approach is described in detail in Sects. 5 and 6.

4.1.2 Motion planning

The automaton is agnostic to the robot’s dynamics, which are instead accounted for by the local planner. For a given robot model and controller a set of motion constraints, or tracking errors, are precomputed at synthesis time. This part is described in Sect. 7.2.

During execution, the local planner is fed, at runtime, a set of constraints that are then solved for in an efficient manner. These constraints include region boundaries, static and dynamic obstacles and kinodynamic model of the robot.

4.2 Online

At each time step of the execution, the synthesized strategy automaton provides a desired goal for each controlled robot in the team. Then, each robot independently computes a local trajectory that achieves its goal while avoiding other agents.

If a physical deadlock is sensed, an alternative goal is extracted for the robot from the synthesized strategy automaton. The existence of such an alternative in the automaton is guaranteed by construction if the environment assumptions are satisfied. The local planner builds on Alonso-Mora et al. (2015) by adopting a convex optimization approach as described in Sect. 7.

4.3 Integration of mission and motion planning

The proposed method consists of two interconnected parts, the mission planner and the motion planner. Figure 4 highlights the components and their interconnections.

The mission planner is computed offline, prior to execution. It requires a topological map of the environment given by a description of the regions, such as rooms, and their connections. It creates a finite state machine or automaton that achieve the high-level specification and from which the robots in the team can extract a strategy at runtime. Note that we do not optimize the mission planner in this work, but our framework allows us to readily adopt techniques for optimal execution such as Jing et al. (2013) to extract an optimal strategy automaton.

At each time instance in the execution, a target motion is extracted from the automaton. The motion planner computes a collision-free motion to make progress towards the target. If a physical deadlock is sensed, an alternative strategy is extracted from the automaton.

The motion planner requires a local map of the environment $W$, containing all the static and moving obstacles. The regions in the free space $F$ of the local map—used at
run-time—must be labeled to match the regions $R$ of the topological map—used for offline synthesis.

If the automaton commands a robot to transition between two connected regions, a path is computed from the current position of the robot to the border of the destination region and then is followed by the local planner. If the automaton commands a robot to remain in a region, the local planner moves the robot towards the middle point of the region.

5 Offline synthesis: resolving deadlock

In this section, we discuss how to synthesize a strategy automaton given a mission specification and a topological map of the environment, provided that, at runtime, a low-level control strategy is applied that guarantees collision-free motion. We assume that the task specification $\varphi$ ignores collisions, but we allow the possibility that deadlocks can occur at any time during the robot’s execution. Deadlocks can trap the robot from achieving its goals, rendering the specification unrealizable. The crux of this work is an approach that systematically modifies the specification with additional behaviors that redirect the robot team in order to resolve deadlocks, whenever possible. If a satisfying mission plan does not exist, the approach iteratively adds assumptions on the deadlock behavior to the specification until a satisfying strategy can be found for the robot team. By focusing on deadlock rather than the positioning of dynamic obstacles, it allows our approach to be valid for any number of dynamic obstacles, as long as they fulfill the stated assumptions returned by our synthesis approach. It also removes the need to globally track the positions of every obstacle at runtime.

An outline of the general approach is shown in Fig. 5. Such a strategy was chosen to disable any blocked routes to the goal and thereby enable the strategy automaton to seek alternate routes once deadlock has been encountered. In this section, we detail the steps involved to implement the overall approach.

5.1 Deadlock resolution

We declare a robot to be physically in deadlock with another agent if it has not reached its goal but cannot move. This can happen when an agent becomes blocked either by another agent or by a dynamic obstacle. To keep track of which robot is in deadlock, we introduce Boolean input signals $x^i_j \in X$, where $i = 1, \ldots, n_{\text{robots}}$ and $j = 0, \ldots, n_{\text{robots}}$ (the index $j = 0$ representing a dynamic obstacle). Without loss of generality, we consider only deadlock between pairs of agents at a time. For the case where a robot is in deadlock while in proximity to a dynamic obstacle, we let $j = 0$ and refer to this case as singleton deadlock. Otherwise, the robot is in deadlock with another robot on its team, $j \neq 0$, and is considered to be in a state of pairwise deadlock. The proposition $x^i_j$ is True iff robot $i$ is in singleton deadlock and $x^i_j$ is True iff robots $i$ and $j$ are in pairwise deadlock.

To simplify the notation in what follows, we introduce the following shorthand:

\[
\begin{align*}
\delta_P^i &= \neg x^i_j \land \bigcirc x^i_j & \text{rising edge–pairwise deadlock between robots } i \text{ and } j \\
\delta_S^i &= \neg x^{i0} \land \bigcirc x^{i0} & \text{rising edge–singleton deadlock for robot } i \\
\psi_{\alpha\beta}^i &= \pi^i_{\alpha} \land \bigcirc \pi^i_{\alpha} \land \pi^i_{\text{act,}\beta} & \text{incomplete transition } (\alpha \neq \beta); \\
\text{remain in region } (\alpha = \beta)
\end{align*}
\]

The definition for singleton deadlock is abstract enough to capture the case where deadlock occurs between the robot and any number of dynamic obstacles—singleton deadlock will be set if the robot stops moving when encountering one or more dynamic obstacles blocking its path. On the other hand, since the members of the team are controlled by the same mission planner, pairwise deadlock can be resolved separately. For instance, if three robots on a team converge on the same point, then three pairwise deadlock propositions will be set.

Resolving deadlock by redirecting the robot’s motion based on the instantaneous value of $x^i_j$ alone may result in livelock, where the robot may be trapped from achieving its goals as a result of repeated deadlock status changes. For this reason, our scheme automatically introduces additional memory propositions that are set when deadlock is sensed, and reset once the robot moves a predefined discrete
radius, denoted $m$, defining the a deadlock resolution horizon (i.e., it traverses $m$ regions away from the region where deadlock occurred in order for the deadlock to be considered “resolved”).

**Definition 6 (Discrete radius)** Let $\pi^i_{\text{curr}(k_i)} \in AP_R$ and $\pi^i_{\text{act,curr}(k_i-1)} \in AP_{\text{act}}$ be, respectively, the configuration and action taken by robot $i$, where $k_i = 1, 2, \ldots$ represents an event that is incremented when robot $i$ enters a new region, i.e., $k_i$ is incremented at the time instant when $\text{curr}(k_i - 1) \leftarrow \text{curr}(k_i)$. The current region index $\text{curr}(\cdot) \in [1, p]$ is defined recursively, initialized such that $\pi^i_{\text{curr}(1)}$ is the robot’s completion when deadlock was recorded and $\pi^i_{\text{act,curr}(0)}$ is the robot’s action when deadlock was recorded. Then, the discrete radius $m$ is the number of successive steps $k_i \in [1, m]$ for which we impose the restriction $\pi^i_{\text{act,curr}(k_i)} \in AP_{\text{act}} \setminus \{\pi^i_{\text{act,curr}(k_i-1)}\}$ on the robot’s actions. This ensures that the robot makes a move that does not re-enter the region just visited.

The concept behind the proposed deadlock resolution approach is to force the robot to actively alter its strategy to overcome a deadlock by imposing a small number of constraints without directly prescribing the path the robot is required to take. The path is derived once a strategy algorithm is synthesized from the specification augmented with these revisions. For instance, as illustrated in Fig. 5, for the case $m = 1$ (resp. $m = 3$), if a deadlock is sensed at point (2), the revisions forbid the robot from crossing the red line until it reaches the green line (resp. cyan line). As a result, different choices of $m$ will lead to the synthesis of strategies that give rise to different subsequent paths to goal region $R^8$ and decisions whether or not to revisit the location where deadlock had occurred.

We first introduce an approach where resolution occurs when the robot leaves its current region, then generalize this approach to allow the user to choose any number of discrete steps, $m \geq 0$, to be taken by the robot before deadlock is declared as resolved. In this work, we assume $m$ to be chosen ahead of time.

### 5.2 Resolving deadlock when $m = 0$

Our deadlock resolution approach for the case $m = 0$ amounts to the situation where robot $i$ is forced to move in another direction whenever $x^{ij}$ becomes True for $j = 0, \ldots, n_{\text{robots}}$. As long as $x^{ij}$ remains True when robot $i$ is in region $R_a$, we disallow motion to $R_b$ as follows:

$$\bigwedge_{\pi^i_\alpha \in AP_R, R_b \in Ad_{\{R_a\}}} \left( x^{ij} \land \pi^i_\alpha \Rightarrow \bigcirc \left( -\pi^i_{\text{act},a} \land -\pi^i_{\text{act},b} \right) \right) \ .$$  \ (3)

It is easily observed that, as soon as the robot’s motion is nonzero when it begins to move in a direction opposite to its previous motion, $x^{ij}$ becomes False again and the robot is free to resume its motion to $R_b$. This can lead to unwanted behaviors, such as chattering. To avoid chattering behaviors, we enrich the deadlock resolution approach to allow for any choice of $m > 0$.

### 5.3 Resolving deadlock when $m = 1$

For each robot, we introduce into $\mathcal{Y}$ the system propositions $\{y^i_\beta \mid R_\beta \in \mathcal{R} \} \subset \mathcal{Y}$ representing the deadlock flag occurring when activating a transition from a given region $R_a$ to region $R_b$. When the flag is set, the following formula restricts the robot’s motion:

$$\bigwedge_{\pi^i_\alpha \in AP_R, R_b \in Ad_{\{R_a\}}} \left( y^i_\beta \land \pi^i_\alpha \Rightarrow \bigcirc \left( -\pi^i_{\text{act},a} \land -\pi^i_{\text{act},b} \right) \right) \ .$$  \ (4)

The role of $y^i_\beta$ is to disallow the current transition (from $R_a$ to $R_b$), as well as the self-transition from $R_a$ to $R_a$. The self-transition is disallowed to force the robot to leave the region where the deadlock occurred ($R_a$), instead of waiting for it to resolve; $R_b$ is disallowed since the robot cannot make that transition.

Next, we encode conditions for detecting singleton deadlock at runtime, and storing these as propositions $y^i_\beta$ that memorize that singleton deadlock had occurred:

$$\bigwedge_{\pi^i_\alpha \in AP_R, R_b \in Ad_{\{R_a\}}} \left( \neg y^i_\beta \Rightarrow \left( \psi^i_\beta \Rightarrow \bigcirc y^i_\beta \right) \right) \ .$$  \ (5)

$$\bigwedge_{\pi^i_\alpha \in AP_R, R_b \in Ad_{\{R_a\}}} \left( y^i_\beta \Rightarrow \left( \pi^i_\alpha \land \pi^i_\beta \Rightarrow \bigcirc y^i_\beta \right) \right) \ .$$  \ (6)

The first formula sets the deadlock flag $y^i_\beta$ if the robot is activating transition from $R_a$ to $R_b$. The second formula keeps the flag set until a transition has been made out of $R_a$ (to a region different from $R_b$). Notice that, in our construction, singleton deadlock considers deadlock between one robot and any number of dynamic obstacles, alleviating the need to globally track or identify obstacles at runtime. While this construction could introduce cycling, we prefer it over an approach that stores the entire path because we can limit the number of propositions added to $\mathcal{Y}$ in order to manage complexity. For instance, if we are aware that deadlock does not occur when the robot is trying to reach a given region $R$, we can eliminate the variable $y^i_\beta$.

For pairwise deadlock, we add the following formulas encoding the conditions for declaring that pairwise deadlock has been detected. Note that the disjunction in the formula...
allows the synthesis tool to decide which one of the two robots should react to the deadlock:

$$\square \left( \theta^{ij}_p \Rightarrow \left( \bigvee_{\ell \in \{i,j\}, \pi^\ell \in \text{AP}_R} \bigwedge_{R_\ell \in \text{Adj}(R_a)} (-y^{j?}_f \land \psi^{\ell}_o \beta) \Rightarrow \bigcirc y^{i?}_f \right) \right).$$

(7)

We also add the following to ensure that the memory propositions are only set when the rising edge of deadlock (singleton or pairwise) is sensed.

$$\square \left( \bigwedge_{\ell \in \{1,...,\text{ntrobots}\}} \bigwedge_{R_\ell \in R} (-y^{j?}_f \land \neg \theta^{\ell?}_S \land \bigwedge_{j \in \{1,...,\text{ntrobots}\}, j \not= i} \neg \theta^{j?}_p) \Rightarrow \bigcirc \neg y^{i?}_f \right).$$

(8)

In practice, we do not need a proposition $y^{i?}_f$ for every $R_\ell \in R$, but only $d = \max_{R_\ell \in R}(|\text{Adj}(R_a)|)$ such propositions for each robot in order to remember all of the deadlocks around each region of the workspace. Here $\cdot\cdot\cdot$ denotes the set cardinality. The number of conjuncts required for condition (7) is $\binom{n\text{robots}}{2}$, but, since the number of formulas contributes at worst linear complexity (due to parsing of each formula), the conjuncts contribute only a small amount to the overall complexity. Note that the complexity of the synthesis algorithm is a function of the number of propositions and not the size of the specification.

Conjuncting the conditions (4)–(8) with $\psi^i_s$ yields a modified formula $[\psi^i_s]'$ over the set $\text{AP}$, and the new abstracted specification $\varphi^{\text{abstr}} = \psi^i_s \land \psi^i_t \land \psi^i_c \Rightarrow [\psi^i_s]' \land [\psi^i_t]' \land \psi^i_c$. The initial conditions are modified by setting the additional propositions $x^{ij}, y^i_a$ to False.

### 5.4 Resolving deadlock when $m > 1$

In some cases, having a deadlock resolution strategy in which multiple discrete steps must be made away from any encountered deadlock may result in different behavior than a strategy in which deadlock is resolved when moving away just one step. Considering Fig. 5, the case $m = 3$ results in greater exploration of the workspace, whereas the case $m = 1$ results in confinement to a smaller portion of the workspace.

We generalize the strategy presented in Sect. 5.3 by considering the case where deadlock is resolved once $m > 1$ discrete moves have been taken away from the last encountered deadlock. In what follows, the same formulas as in Sect. 5.3 apply; here, we only describe modifications to this setup. To ensure each robot moves away from deadlock a discrete radius, we require $m - 1$ propositions (for robot $i$, $y^{i?}_{\text{out},1}, \ldots, y^{i?}_{\text{out},m-1}$) that are set and reset in a chain in order to memorize the robot’s position from the encountered deadlock. $y^{i?}_{\text{out},k}$ are initially False for all $i, k$.

In order to set the first such memory proposition in the chain, the terms $\bigcirc y^{j?}_f$ in (5) and $\bigcirc y^{i?}_f$ in (7) are replaced with $\bigcirc y^{j?}_f \land \bigcirc y^{i?}_{\text{out},1}$ and $\bigcirc y^{i?}_f \land \bigcirc y^{i?}_{\text{out},1}$, respectively, and the abstracted specification $\varphi^{\text{abstr}}$ is constructed based on these formulas. For each subsequent discrete step away from deadlock, we require the remaining propositions to be set when the one with next lowest index has been reset. This behavior occurs through the formula:

$$\square \bigwedge_{k=2,...,m-1} \left( (-y^{i?}_{\text{out},k} \Rightarrow \left( (y^{i?}_{\text{out},k-1} \land \neg y^{i?}_{\text{out},k-1}) \Rightarrow \bigcirc y^{i?}_{\text{out},k} \right) \right).$$

(9)

Additionally, for each $k = 1, \ldots, m-1$, we require that each $y^{i?}_{\text{out},k}$ be reset only when the robot has left the current region; specifically,

$$\bigwedge_{k=1,...,m-1} \left( y^{i?}_{\text{out},k} \Rightarrow \left( \left( \bigwedge_{i=1}^{m} \pi^i_a \land \bigcirc \pi^i_a \right) \Leftrightarrow \bigcirc y^{i?}_{\text{out},k} \right) \right).$$

(10)

Finally, as long as some $y^{i?}_{\text{out},k}$ is set, we also set the deadlock flag memory proposition $y^i_a$ corresponding to the region $R_a$ that the robot had immediately departed. That is,

$$\bigwedge_{k=1,...,m-1} \left( \left( \bigwedge_{i=1}^{m} \pi^i_a \land \bigcirc y^{i?}_{\text{out},k} \right) \Rightarrow \bigcirc y^i_a \right).$$

(11)

This prevents the robot from re-entering the region from which it just departed.

The safety revisions restrict the system’s moves in the execution sequence be ones that actively take it $m$ away from the location where the deadlock flag was raised. Since waiting in a region is disabled in (4), and reentering a region is disabled in (11), these safety revisions will cause the system to move $m$ steps away from deadlock in finite time.

In general, setting $m$ large, could lead to behavior that “explores” more of the workspace, but also could result in unrealizability. Consider again the scenario in Fig. 5, but with R2 always blocked. In this case, $m = 3$ would result in an unrealizable specification because the robot cannot make three discrete steps away from R6 without entering R2. Such design tradeoffs therefore depend on the workspace and its partitioning. Automatic selection of $m$ for a given specification and collection of regions is the subject of future work, as is the use of $\square \lozenge$ liveness formulas to resolve livelock in a more direct manner similarly to DeCastro et al. (2016) and
Alur et al. (2013) while remaining scalable to the number of robots on the team.

6 Offline synthesis: environment assumptions and coordination

If the specification $\varphi_{\text{abstr}}$ is synthesizable, then Problem 2 has been solved and no further modifications to the abstracted specification are necessary. But, the possible presence of humans or other uncontrollable agents in some parts of the environment may cause the abstracted specification to be unrealizable. Then, it becomes necessary to solve Problem 3 to find a minimal set of environment assumptions that restores the guarantees.

We automatically generate assumptions on the environment’s behavior in cases where the modified specification is unrealizable. To prevent any unreasonable assumptions (assumptions that the robot can overcome deadlock when it is impossible to do so), we provide a means for coordinating robot actions to prevent such assumptions from being given to the user. Combining the encoding and revisions approach, we formally show that the synthesized automaton is guaranteed to fulfill the task under these assumptions, showing that our approach also removes the possibility of deadlock and livelock from occurring.

6.1 Runtime certificates for the environment

We note that the dynamic obstacles are uncontrollable agents, and lacking behavioral information, so altering environment assumptions does nothing to characterize their behavior. Rather, we may still provide the user with a certificate under which the environment’s behavior will guarantee that the team can achieve all its goals without being trapped permanently in a state of deadlock or livelock. Such assumptions can be given to the user to allow him/her to be mindful of any condemning situations when co-inhabiting the robots’ environment. As such, we call these added assumptions runtime certificates.

When a specification is unrealizable, there exist environment behaviors (called environment counterstrategies) that prevent the system from achieving its goals safely. Here we build upon the work of Alur et al. (2013), DeCastro et al. (2016) and Li et al. (2011), processing synthesized counterstrategies to mine the necessary assumptions. Rather than synthesize assumptions from the counterstrategy as in Alur et al. (2013), which requires specification revision templates to be specified by hand, we automate the counterstrategy search by searching for all deadlock occurrences, then store the corresponding conditions as assumptions.

We denote $C_{\text{abstr}}$ as an automaton representing the counterstrategy for $\varphi_{\text{abstr}}$. Specifically, a counterstrategy is the tuple $C_{\text{abstr}} = (Q, Q_0, \mathcal{X}, \mathcal{Y}, \delta, \gamma_X, \gamma_Y)$, where $Q$ is the set of counterstrategy states; $Q_0 \subseteq Q$ is the set of initial counterstrategy states; $\mathcal{X}$, $\mathcal{Y}$ are sets of propositions in $AP$; $\delta: Q \times 2^\mathcal{Y} \rightarrow 2^Q$ is a labelling function mapping states to the set of environment propositions that are $\text{True}$ for incoming transitions to that state; and $\gamma_X: Q \rightarrow 2^\mathcal{X}$ is a labelling function mapping states to the set of system propositions that are $\text{True}$ in that state. We compute $C_{\text{abstr}}$ using the slugs synthesis tool (Ehlers and Raman 2016).

To find the graph cuts in the counterstrategy graph that prevent the environment from impeding the system, we first define the following propositional representation of state $q \in Q$ as $\psi(q) = \psi_X(q) \wedge \psi_Y(q)$, where

$$
\psi_Y(q) = \bigwedge_{p \in \gamma_Y(q)} \pi \wedge \bigwedge_{\pi \in \gamma_Y \setminus \{q\}} \neg \pi,
$$

$$
\psi_X(q) = \bigwedge_{p \in \gamma_X(q)} \pi \wedge \bigwedge_{\pi \in \gamma_X \setminus \{q\}} \neg \pi.
$$

Next, letting $\delta_Y(p) = \{q \in Q \mid \exists \pi \in \gamma_Y; q \in \delta(p, \pi)\}$, the set of cut transitions $S_{\text{cuts}}$ is computed as $S_{\text{cuts}} = \{(p, q) \in Q^2 \mid q \in \delta_Y(p), \psi(p) \wedge \psi(q) \models \bigwedge_{i \in \{1, \ldots, n_{\text{robots}}\}} \delta_Y_i\}$. $S_{\text{cuts}}$ collects those transitions on which the environment has intervened (by setting deadlock) to prevent the system from reaching its goals.

Finally, the following safety assumptions are found:

$$
\varphi_{\text{rev}}^e = \Box \bigwedge_{(p, q) \in S_{\text{cuts}}} (\psi_Y(p) \wedge \psi_X(p) \implies \neg \Box \psi_X(q))
$$

If any of the conjuncts in (12) falsify the antecedent of $\varphi$ (the environment assumptions), they are discarded. Then, set $[\varphi]^e_{\text{rev}} = \varphi^e \wedge \varphi_{\text{rev}}$ and construct the final revised specification $\varphi_{\text{rev}} = \varphi^f_{\text{rev}} \wedge \varphi_{\text{rev}}^e \implies [\varphi^f_{\text{rev}}] \wedge [\varphi^f_{\text{rev}}] \wedge \varphi_{\text{rev}}^e$.

Algorithm 1 expresses our proposed approach for resolving deadlock. The automatically generated assumptions act to restrict the behavior of the dynamic obstacles. Each revision of the high-level specification excludes at least one environment move in a given state. Letting $| \cdot |$ denote set cardinality, with $2^{|\mathcal{X}|}$ environment actions and $2^{|\mathcal{Y}|}$ states, at most $2(|\mathcal{Y}| + |\mathcal{X}|)$ iterations occur, though in our experience far fewer are needed. The generated assumptions are minimally restrictive—omitting even one allows the environment to cause deadlock, resulting in unrealizability. Note that the parsing step in line 8 creates statements that are displayed to the user. The user display step is explained in detail in the implementation in Sect. 9.
Algorithm 1 Find realizable $\varphi^\text{rev}$ fulfilling task $\varphi$ and resolving deadlock.

1: $\varphi^\text{whit}$ $\leftarrow \varphi_1^r \land \varphi_2^r \land \varphi_3^r \Rightarrow [\varphi_4^r]' \land [\varphi_5^r]' \land \varphi_6^r$
2: $[\varphi_1^r]' \land \varphi_2^r$
3: $\varphi_1^r \land [\varphi_1^r]' \land \varphi_2^r \Rightarrow [\varphi_1^r]' \land [\varphi_1^r]' \land \varphi_6^r$
4: while $\varphi^\text{rev}$ is unrealizable do
5: Extract $C_{\text{rev}}$ from $\varphi^\text{rev}$
6: $\varphi^\text{rev} \leftarrow \text{Eq. (12)}$
7: for each $i$th conjunct of $\varphi^\text{rev}$ s.t. $\varphi^\text{rev} \land [\varphi_i^r]' \neq \text{false}$ do
8: Parse $\varphi^\text{rev}$ into human-readable statements and display to user.
9: $[\varphi_i^r]' \land [\varphi_i^r]' \land \varphi^\text{rev}$
10: end for
11: $\varphi^\text{rev} \leftarrow \varphi_1^r \land [\varphi_1^r]' \land \varphi_2^r \Rightarrow [\varphi_1^r]' \land [\varphi_1^r]' \land \varphi_6^r$
12: end while

In practice, many of the added environment safety statements can be violated by dynamic obstacles at runtime without consequence, if these violations can be assumed to be temporary. For this reason, we introduce a recovery scheme that synthesizes a strategy that allows environment safety assumption violations to be tolerated. We refer the reader to Wong et al. (2014) for these technical details of the details of this strategy. Note that we modify the approach to attempt a recovery only for violations of the newly added assumption $\varphi^\text{rev}$, rather than for the entire formula $[\varphi_i^r]'$, since our goal is to only make assertions on the environment’s behavior with respect to deadlock and not all behaviors in general.

The requirement for temporary deadlock is less restrictive than the requirement that deadlocks should never occur, but it nonetheless places additional requirements on the environment’s behaviors, i.e. that the dynamic obstacles cannot infinitely often cause deadlock. Hence such conditions are displayed to the user in an easily-interpretable form.

Runtime certificates are displayed to the user in a format such as: The task is guaranteed as long as for robot 1 any singleton deadlock in the kitchen while heading to the door is eventually resolved on its own. In this specific case, dynamic obstacles may enter deadlock with robot 1, but the obstacles are obligated to eventually resolve deadlock. If the dynamic obstacle is a person, the certificate may have no impact on the true behavior of the environment, as social norms deem it natural for people to resolve deadlocks on their own. If the dynamic obstacle is a door, then the certificate could alert that the door should eventually be opened to allow the robot to pass through. On the other hand, if the door never opens, then the certificate could help to explain that the door being closed as the reason the task remains unfulfilled.

It is possible that many such certificates are required, which may overwhelm the user. We address this in two ways. First, we project the found certificates onto the set of propositions relating to motion only, eliminating any propositions that do not relate to motion. Second, we use a graphical visualization of the certificates overlaid on a map of the physical workspace. In addition to the above provisions, the work in DeCastro et al. (2016) offers an approach that can be adopted to further reduce the number of revisions fed to the user. There, a method is introduced for grouping regions that share the same properties for the revisions, and convey to the user metric information that is necessary for fulfilling the added revisions. Such an integration is left for future work.

We refer the reader to Sect. 9 for implementation details.

We point out that (12) gives revisions that are possibly conservative. The formula is created from a counterstrategy that is extracted from a game structure capturing the environment’s behaviors for every possible behavior of the system (DeCastro et al. 2016). In the current implementation, the counterstrategy is computed without regard to the number of revisions that could be generated. Future iterations of the approach could make use of an optimality criterion to extract a counterstrategy with a minimal number of revisions. Another cause for conservatism is due to the fact that the approach abstracts away the actual behavior of the dynamic obstacles, neglecting the physical behavior of the dynamic obstacles. This can be improved by enhancing the existing approach with LTL formulas that impose physical constraints on the environment, for instance mutual exclusion conditions on deadlocks.

6.2 Coordination between robots

Since the strategy for the robots’ motion is completely determined at synthesis time, the controllers we synthesize should not lead to deadlocks if they can be safely avoided. For instance, two robots on the team should not enter a narrow doorway from opposite ends, only to become deadlocked there. This motivates the creation of a method for automatically inserting dimension-related information into the specification based on the workspace geometry and the volume of the robot so that the robots can pre-coordinate, at synthesis time, to avoid unneeded deadlock. This pre-coordination serves two purposes: (1) it allows to eliminate any environment assumptions between two robots in a region where there is high likelihood of deadlock if both are occupying that region, and (2) it changes the behavior of the agents to actively avoid potential deadlock in such high-risk regions, such as one-way corridors.

The modification considers the restrictions on what robots are allowed to do in certain regions, based on the dimension of the region and the size of the robot. We introduce an encoding of LTL formulas that eliminate the actions of robots that would result in deadlock. Specifically, we consider two cases: (1) a robot will not enter a region if the move will exceed the region’s capacity and, (2) it will be prevented that two or more robots enter through opposite sides a one-way.
7 Online local motion planning

In this section we describe the local planner that links the mission plan with the physical robot (recall Fig. 4). The offline synthesis and generated state machine are agnostic to the local planner, which can be substituted as long as avoidance of unmodeled moving obstacles is guaranteed. Our online local planner does account for the robot dynamics, which were abstracted for high-level synthesis.

At each step of the online execution, the synthesized strategy automaton provides a desired goal position for each robot and a preferred velocity \( \tilde{\mathbf{u}} \in \mathbb{R}^n \) towards it. An overview of the algorithm is given in Algorithm 3 and each step is described in detail in the following sections. We note that the reader may choose any other method for online planning as long as it preserves the avoidance guarantees with the kinematic model of the robots.

## Algorithm 3 Execution of the local planner using the synthesized strategy automaton.

1. **Input:** Current state of the robot, a local map, position and velocity of neighbors and a synthesized strategy automaton (FSM).
2. At each time instance (\( \sim 10 \) Hz) do the following:
3. If the robot is in deadlock with any other agent then
4. Send a deadlock flag to the FSM.
5. **end if**
6. Obtain command from the FSM (e.g. “stay in the current room” or “move to the next room”), based on current state and deadlock flag.
7. Convert command into a goal position and preferred velocity \( \tilde{\mathbf{u}} \).
8. Compute constraints to satisfy the dynamic model of the robot.
9. For each neighboring agent do
10. Compute pairwise collision avoidance constraint.
11. **end for**
12. Compute largest obstacle-free convex region wrt static obstacles.
13. Solve constrained optimization to obtain collision-free motion
14. **Output:** A collision-free motion for the robot and the time horizon

### 7.1 Overview

We build on the work on distributed Reciprocal Velocity Obstacles with motion constraints (Alonso-Mora et al. 2014), and its recent extension to aerial vehicles (Alonso-Mora et al. 2015).

As described by Alonso-Mora et al. (2014), the method follows two ideas. (a) The radius of the robot is enlarged by a pre-defined and typically fixed value \( \varepsilon > 0 \) for collision avoidance. This value depends on the kinodynamic model of the robot and can be reduced in real time without having to recompute the stored maximum tracking errors. And, (b) in run time, the local trajectories are limited to those with a tracking error below \( \varepsilon \) with respect to their reference trajectory. Recall that the tracking errors were precomputed in the offline process.

At each time-step an optimal reference velocity \( \mathbf{u}^* \in \mathbb{R}^n \) is obtained by solving a convex optimization in reference velocity space. The associated local trajectory is guaranteed to be collision-free, satisfies the motion constraints and minimizes a cost function. The cost function minimizes the deviation to a preferred velocity \( \bar{\mathbf{u}} \), corrected by a small repulsive velocity \( \mathbf{u} \) inversely proportional to the distance to the neighboring obstacles when in close proximity. As described by Alonso-Mora et al. (2015) this additional term introduces a desired separation between robots and obstacles. Note that the avoidance guarantees arise from the constrained optimization and not from the repulsive velocity.

### 7.2 Robot dynamics

Letting \( t \in \mathbb{R}_+ \) denote time and \( t_k \) the current time instant, we define the relative time \( \bar{t} = t - t_k \in [0, \ldots, \infty) \) and the time horizon of the local planner \( \tau > 0 \), greater than the required time to stop if moving at maximum speed. Note that different robots may present different dynamic models.

---

**Algorithm 2** Augmenting a specification with agent coordination with respect to region geometry.

```plaintext
1: \( D \leftarrow \max \) dimension of the enclosing hull of the robots on the team
2: for each \( R_i \in \mathbb{R} \) do
3: \( A \leftarrow \text{area of region } R_i \)
4: if \( \frac{A}{D^2} < 1 \) then
5: Region capacity is too small
6: \( \varphi_i^t \leftarrow \varphi_i^t \land (\bigcirc \pi_i^t) \land (\bigcirc \pi_i^t) \land (\bigcirc \pi_i^t) \)
7: end if
8: for each \( R_j \in \text{Adj}(R_i) \) do
9: if \( \|R_j \cap R_i\| < 2D \) then
10: /\ Boundary between \( R_j \) and \( R_i \) is too narrow
11: \( \varphi_i^t \leftarrow \varphi_i^t \land (\bigcirc \pi_i^t) \land (\bigcirc \pi_i^t) \land (\bigcirc \pi_i^t) \)
12: end if
13: end for
14: end for
```

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narrow region. We then create a new specification \( \varphi_{abstr.coord} \) with pre-coordination of robots, and apply Algorithm 1 on \( \varphi_{abstr.coord} \) by swapping out \( \varphi_{abstr} \) in line 1.

To create the LTL encoding, we introduce Algorithm 2 to enforce pairwise coordination amongst robots in the controlled team. If the region is too small to contain a pair of robots, any robot outside of the region is prevented from entering (line 6). If the boundary between two regions \( R_a \) and \( R_b \) is too small for two robots to pass through at once, and one robot is approaching the boundary from \( R_a \) (resp. \( R_b \)), then no other robot may approach that boundary if in \( R_b \) (resp. \( R_a \)). This requirement is encoded in lines 11–12. Note that Algorithm 2 is general to any workspace with convex regions.
We denote the state of a robot by \( z = \{ p, \dot{p}, \ddot{p}, \ldots \} \), which includes its position and velocity and may include additional terms such as acceleration and orientation. Given a control input \( u(\cdot) \) the dynamical model is \( \dot{z} = g(z, v) \).

In our local planner, we consider a set of candidate local trajectories, each defined by a straight-line reference \( p_{\text{ref}}(\cdot) = p + u(t) \) of constant velocity \( u \in \mathbb{R}^n \) and starting at the current position \( p \) of the robot. Each motion primitive is then given by an appropriate approximating tracking controller \( p_{\text{robot}}(\cdot) = f(z, u, \cdot) \) that is continuous in the initial state \( z \) of the robot, respects its dynamical model and converges to the straight-line reference trajectory. Local trajectories are now parametrized by \( u \), see Fig. 6 for an example. Suitable controllers defining the function \( f(z, u, \cdot) \) include LQR control and second order exponential curves, for ground robots (Alonso-Mora et al. 2014) and quadrotors (Alonso-Mora et al. 2015).

For fixed robotic platform, controller, initial state \( z \) and reference velocity \( u \), the maximum deviation (initial position independent) between the reference and the simulated trajectory is given by

\[
\gamma(z, u) = \max_{i > 0} ||(p + iu) - f(z, u, i)||_2. \tag{13}
\]

In an offline procedure, we precompute the maximal tracking errors \( \gamma(z, u) \) via forward simulation of the robot dynamics and controller \( f(z, u, \cdot) \) for a discretization of reference velocities \( u \) and initial states \( z \)—we only discretize in initial velocity since the error is independent of the initial position of the robot. They are stored for online use in a look-up table.

### 7.3 Constraints

To define the motion and inter-agent avoidance constraints we build on the approach in Alonso-Mora et al. (2015). We additionally introduce constraints for avoiding static obstacles. For completeness, we give an overview of each of the constraints.

![Fig. 6 Schema local and reference trajectories for an aerial vehicle, generated from the reference velocity u. The tracking error is limited by \( \varepsilon \) and the robot volume dilated by \( \varepsilon \).](Image)

**7.3.1 Robot dynamics**

Recalling Eq. (13) the motion constraint is given by the reference velocities for which the tracking error is below \( \varepsilon \),

\[
R(z, \varepsilon) = \{ u \mid \gamma(z, u) \leq \varepsilon \}. \tag{14}
\]

approximately by the largest inscribed convex polytope/ellipsoid \( \hat{R}(z, \varepsilon) \subset R(z, \varepsilon) \).

**7.3.2 Avoidance of other agents**

Denote by \( p_j, v_j, \bar{r}_j \) and \( \bar{h}_j \) the position, velocity, dilated radius and height of a neighboring agent \( j \). Assume that it keeps its velocity constant for \( \bar{r}_j(t) \leq \bar{r}_j(t_0) \). Reciprocity (i.e. the other agent follows the same algorithm) can as well be assumed and is discussed in Alonso-Mora et al. (2015). For every neighboring agent \( j \), the constraint is given by the reference velocities \( u \) for which the agents’ enveloping shape do not intersect within the time horizon. For cylindrically-shaped agents moving in 3D the velocity obstacle of colliding velocities is a truncated cone

\[
VO_j^T = \left\{ u \mid \exists \bar{r} \in [0, \tau]: \|p_j^H - p_j^H + (u^H - v_j^H)\bar{r}\| \leq \bar{r} + \bar{r}_j \right\}
\]

and \( |p^V - p_j^V| \leq h \). Assume that \( \bar{h} = \bar{h}_j \), where \( n_j \in \mathbb{R}^3 \) and \( b_j \in \mathbb{R}^3 \) subject to \( A_j(p, \varepsilon) = \{ u \mid n_j^T u \leq b_j \} \), where \( A_j \) is the set of steps in the linear search, typically between 2 and 4.

**7.3.3 Avoidance of static obstacles**

We extend a recent fast iterative method to compute the largest convex polytope in free space (Deits and Tedrake 2014), by directing the growth of the region in the preferred direction of motion and enforcing that both the current position of the robot and a look ahead point in the preferred direction of motion are within the region. The convex polytope is computed in position space (\( \mathbb{R}^3 \) for aerial vehicles) and then converted to an equivalent region in reference velocity space. See Algorithm 4, where directedEllipsoid \( (p, q) \) is the ellipsoid with one axis given by the segment \( p - q \) and the remaining axis infinitesimally small, and \( K \) the number of steps in the linear search.

**7.3.4 Avoiding incorrect region transitions**

The local planner prevents incorrect region transitions (for instance, avoiding entering another region if the robot’s local goal is within the current one) by introducing “virtual” doors...
at borders between workspace regions. These virtual doors may be closed or opened depending on the desired transition. A closed door is introduced as an obstacle in trajectories.

The local trajectory up to time \( \tau \) with the assumption that all interacting agents maintain a constant velocity.

Avoidance of dynamic obstacles was shown in our previous work (Alonso-Mora et al. 2015). Here we reproduce it for the case of a dynamic obstacle maintaining a constant velocity, and it extends to the case where all agents do reciprocal collision avoidance.

Recall that \( t_k \) represents the current time instant and \( \tilde{t} = t - t_k \in [0, \infty) \) the relative time. Let \( \mathbf{p}(\tilde{t}) \) denote the position at time \( t \geq t_k \), and if not specified, variables are evaluated at \( t_k \). The idea is that the optimal reference trajectory is collision-free for an agent whose volume is enlarged by \( \varepsilon \) and the robot stays within \( \varepsilon \) of it. Formally,
(p + w) − (p_j + v_j t) 
\text{Avoidance constraint, } u \in A_j(p, \epsilon). V \epsilon + \epsilon \Rightarrow p(t) − p_j(t) = f(z, u, \tilde{t}) − (p_j + v_j t) \not\in V + \epsilon 

For the case of planar disk robots, this is equivalent to showing the relative distance is greater than the sum of radii,

||p(t) − p_j(t)|| = ||f(z, u, \tilde{t}) − (p_j + v_j t)|| \geq \epsilon \Rightarrow r + e + r_j − \epsilon = r + r_j.

For avoidance of static obstacles, u \in F(p, \epsilon) implies

If the assumptions are violated, e.g. the moving obstacles quickly change their velocity, the constrained optimization of Eq. (15) can be infeasible. In that case, no collision-free solution exists that respects all of the constraints and a collision may arise. In this case the robot decelerates at its maximum deceleration rate until full stop or a feasible collision-free trajectory is found. In practice, since this computation is performed at a high frequency, each individual robot is able to adapt to changing situations, and the resulting motion is collision-free if the moving obstacles behave fairly (i.e. never cause collisions).

8.3 Correctness with respect to the task specification

Since the local planner is myopic, it provides guarantees up to a time horizon \tau and consequently may result in deadlock and livelock. However, as we have shown, the planner’s local guarantees allow a discrete abstraction that the strategy automaton can use to resolve deadlocks and avoid livelocks. Here we formally prove the guarantees on the execution provided by our synergistic online and offline synthesis.

Proposition 1 Given a task specification \varphi that ignores collisions, if the resulting specification \varphi^{\text{abstr}} defined in Sect. 5 is realizable, then the corresponding strategy automaton also realizes \varphi.

Proof Assume given \varphi = \varphi^e_r \land \varphi^e_i \land \varphi^e_s \Rightarrow \varphi^e_r \land \varphi^e_i \land \varphi^e_s. Recall that \varphi^{\text{abstr}} = \varphi^e_r \land \varphi^e_i \land \varphi^e_s \Rightarrow [\varphi^e_r'] \land [\varphi^e_i'] \land \varphi^e_s$, where $[\varphi^e_r']$ and $[\varphi^e_i']$ contain $\varphi^e_r$ and $\varphi^e_i$ as subformulas, respectively. Suppose that strategy automaton $A_{\varphi^{\text{abstr}}}$ realizes $\varphi^{\text{abstr}}$. This means that the resulting controller is guaranteed to fulfill the requirement $[\varphi^e_r'] \land [\varphi^e_i'] \land \varphi^e_s$ as long as the environment fulfills the assumption $\varphi^e_r \land \varphi^e_i \land \varphi^e_s$. This implies that $A_{\varphi^{\text{abstr}}}$ fulfills $\varphi^e_r \land \varphi^e_i \land \varphi^e_s$ as long as the environment fulfills the assumption $\varphi^e_r \land \varphi^e_i \land \varphi^e_s$. \hfill \blacksquare

Proposition 2 Given a task specification \varphi that ignores collisions, if \varphi is realizable but the resulting specification \varphi^{\text{abstr}} is not realizable, then the revision procedure in Sect. 6.1 will find an assumption $\psi^{\text{rev}}$ to add to $\varphi^{\text{abstr}}$ that renders the resulting specification $\varphi^{\text{rev}}$ realizable and the resulting strategy $A_{\varphi^{\text{rev}}}$ free of deadlock and livelock.

Proof Suppose \varphi is realizable by strategy $A_{\varphi}$, but $\varphi^{\text{abstr}}$ is not realizable, admitting counterstrategy $C_{\varphi^{\text{abstr}}} = (Q, \ldots)$. It suffices to show that the set $S_{\text{cuts}}$ is nonempty. Assume by way of contradiction that $S_{\text{cuts}}$ is empty. Then the rising edge of deadlock $\phi_i$ never occurs for any i, so no robot transitions are ever disabled. Since we assume that deadlock does not occur in the initial state, this means that $x^i$ is always False for every $i, j$. Therefore $[\varphi^e_r] \land [\varphi^e_i] \land \varphi^e_s$ defined in Sect. 5 reduces to $\varphi^e_r \land \varphi^e_i \land \varphi^e_s$. The lack of deadlock means that any region transition contained in $A_{\varphi}$ is still admissible, and therefore $A_{\varphi}$ can be used as a strategy to realize $\varphi^{\text{abstr}}$, a contradiction. Therefore, there must be deadlock and $S_{\text{cuts}}$ is not empty. Now, upon addition of the assumptions $\varphi^{\text{abstr}}$, existence of $A_{\varphi^{\text{rev}}}$ that satisfies $\varphi^{\text{abstr}}$ implies, by construction, that $A_{\varphi^{\text{rev}}}$ is deadlock-free. \hfill \blacksquare

Note that it may be the case that $S_{\text{cuts}}$ is nonempty, but for every $(p, q) \in S_{\text{cuts}}$, the resulting revision

$(\psi \land \psi \chi(p) \Rightarrow \neg \bigcirc \psi \chi(q))$

contradicts $\psi^e_s$. This indicates that $\varphi$ is only realizable because it makes unreasonable assumptions on the environment. Our approach identifies this fact as a by-product of the revision process.

8.4 Computational complexity

For a given choice of $m$, the offline reactive synthesis algorithm used in this work is exponential in the number of propositions (Bloem et al. 2012; Ehlers and Raman 2016). Using our encoding, the problem scales linearly with $n_{\text{robots}}$—no worse than existing approaches (e.g. Ulusoy et al. 2013). When one or more dynamic obstacles are considered, the number of propositions does not change. As stated in Sect. 6, $2|\Sigma|^{|X|}$ iterations of the main loop in Algorithm 1 are needed in the worst case, yielding a theoretical complexity that is doubly exponential in the number of propositions.

For the online component, a convex program is solved independently for each robot, with the number of constraints linear in the number of neighboring robots. The runtime of the iterative computation of the convex volume in free space

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barely changes with the number of obstacles, up to tens of thousands (Deits and Tedrake 2014), and a timeout can be set, with the algorithm returning the best solution found.

9 Experiments and simulations

We present results of our end-to-end approach both in simulation and on hardware. Our evaluation is meant to illustrate the various parts of the synthesis and execution process, and provide a statistically-grounded evaluation of the approach when placed in a difficult environment that does not necessarily behave according to the automatically-generated environment assumptions. In this context, our results reveal that our approach has merit in dealing with such environments to execute the task successfully. We furthermore show that our approach is scalable to any number of dynamic obstacles, and that the local planner applies to 3-D workspaces. Lastly, we show that our approach may be executed in real time on actual hardware.

The synthesis procedure described in Sect. 5 was implemented with the slugs synthesis tool (Ehlers and Raman 2016), and executed with the LTLMoP toolkit (Finucane et al. 2010). The local motion planner (Sect. 7), was implemented with the IRIS toolbox (Deits and Tedrake 2014) and an off-the-shelf convex optimizer. We assume the dynamic obstacles are cooperative in avoiding collisions, therefore, each one is controlled by a local planner. Many of the experiments presented in this section are available in the accompanying video.

In what follows, we consider a “garbage collection” scenario, upon which we synthesize a strategy automaton.

Example 2 (Garbage collection) A robot team is required to patrol the Living Room (R_LR) and Bedroom (R_BR) of the workspace in Fig. 7. For two robots, the specification is:

$$
\Box (\pi_{LR}^{1}) \land \Box (\pi_{BR}^{1}) \land \Box (\pi_{LR}^{2}) \land \Box (\pi_{BR}^{2})
$$

and if garbage is observed, pick it up

$$
\Box (\pi_{garb} \implies \pi_{act, pickup}^{1}) \land \Box (\pi_{garb} \implies \pi_{act, pickup}^{2}).
$$

Additionally, the robots must always avoid other moving agents.

The system propositions are actions to move between regions ($\pi_{act,LR}^{1}, \ldots, \pi_{act, BR}^{1}$) and to pick up ($\pi_{act, pickup}$). The environment propositions are sensed garbage ($\pi_{garb}$), region completions ($\pi_{LR}^{1}, \ldots, \pi_{BR}^{1}$), and pick up completion ($\pi_{pickup}^{1}$).

We omit the complete encoding of Definition 2, however, for illustration we supply the transition formulas for the case where robot 1 is in Hall:

$$
\varphi_1^{x}:
\begin{align*}
&\Box (\pi_{Hall}^{1} \lor \pi_{LR}^{1} \lor \pi_{BR}^{1} \lor \pi_{Kitchen}^{1} \lor \pi_{Door}^{1}) \\
&\Box (\Box \pi_{Hall}^{1} \implies \Box \pi_{act, Hall}^{1} \lor \Box \pi_{act, BR}^{1} \lor \Box \pi_{act, LR}^{1}) \\
&\Box (\pi_{act, Hall}^{1} \lor \pi_{act, BR}^{1} \lor \pi_{act, LR}^{1} \lor \pi_{act, Kitchen}^{1} \lor \pi_{act, Door}^{1}) \\
&\Box (\pi_{Hall}^{1} \land \pi_{act, Hall}^{1} \implies \Box \pi_{Hall}^{1}) \\
&\Box (\pi_{Hall}^{1} \land \pi_{act, LR}^{1} \implies \Box \pi_{Hall}^{1} \lor \Box \pi_{LR}^{1}) \\
&\Box (\pi_{Hall}^{1} \land \pi_{act, BR}^{1} \implies \Box \pi_{Hall}^{1} \lor \Box \pi_{BR}^{1})
\end{align*}
$$

The initial conditions $\varphi_1^{y}$ and $\varphi_1^{z}$ are True.

We implement the above example using humanoid robots (able to rotate in place, move forward and along a curve) and simulated quadrotor UAVs.

9.1 Synthesis and revisions

Upon synthesizing a controller for single robot, we obtain 16 revisions to the environment assumptions. These are displayed to the user as runtime certificates. One example is: Deadlock should not occur when the robot is in the Hall moving toward the Living Room and had already been blocked from entering the Bedroom. Note that, with each robot added to the team, the number of revisions grows combinatorially. In contrast to the single-robot case, there are a total of 1306 statements given to the user in the case of two robots. In these cases, we display the revisions graphically, by projecting over the variables of interest: the current region and action for each robot. Rather than displaying all 1306 statements, we show the projection consisting of 45 statements projected onto the set of each robot’s motion and activation propositions. Satisfying these 45 statements implies that we also satisfy the 1306 statements. To further aid the user, we display them graphically on the workspace as shown in Fig. 7.

For instance, a red arrow on the boundary of the Hall indicates that the automaton cannot guarantee the task if the robot experiences deadlock when it is in the Hall and while activating a motion to the Living Room. The certificates displayed in Fig. 7 are projections onto a subset of the complete set of propositions (i.e. deadlocks, memory propositions, robot positions, and robot actions for each of the robots in the team), by abstracting those variables away. That is, if there exist restrictions on deadlock for any of the propositions that have been abstracted away, then the revision displayed will be a conservative overapproximation to the true revision and the dot will be labeled red.
9.2 Scalability with respect to dynamic obstacles

Considering Example 2, the specification for the single-robot case consists of 14 propositions, while that for the two-robot case consists of 29 propositions. The specification is invariant to the number of dynamic obstacles in either case.

One could also consider a two-robot team controlled by a baseline strategy that relies on mutual exclusion (one robot per region) to be kept with other robots and dynamic obstacles (DO). That strategy required 20 propositions for the case without DOs. One additional proposition is added for each region for each DO (producing 25 for one DO, 35 for three DO, 60 propositions for eight DO, etc.). Because the obstacles are assumed to behave in an adversarial manner, they can violate mutual exclusion if they enter a neighboring region of the robot. Hence, the baseline synthesis procedure is not realizable for one or more dynamic obstacles.

In contrast, our approach is realizable independently of the number of dynamic obstacles and requires fewer propositions than the case with two or more DO.

9.3 Performance evaluation

We directly compare the proposed approach with a baseline approach where the robots execute a local planner, but there is no deadlock resolution in the strategy. Recall that there is no guarantee of mission satisfaction in that case. Figures 8, 9 and 10 display results for various problem scenarios. In each experiment, we use the model described in Alonso-Mora et al. (2015) to model the robots and dynamic obstacles as quadrotors. The “counter-flow” cases follow a pre-defined set of waypoints that allow DOs to circulate within the workspace in one direction (counter to the flow of the robots), while, in the “random waypoints” cases, DOs randomly select a neighboring waypoint once a waypoint has been achieved. To detect deadlock, we use the criteria in (16) with the choice of parameters $k_1 = \frac{1}{3}$, $k_2 = \frac{1}{4}$, and $k_3 = 1.5$.

Each test case consisted of 133 min of data obtained over multiple simulation runs lasting 200 s each. The simulation was terminated before 200 s if none of the controlled robots reached their goal, but none had been moving (their velocity falls below a threshold) for 100 s or longer. Any such runs were flagged as unresolved deadlock, at which point the robots are deemed unable to continue their task. The robots in the team were initialized randomly at different regions in the workspace.

Fig. 7 Workspace showing specification revisions for each region completion/activation pairs where singleton or pairwise deadlock may occur. An arrow’s color indicates the type of assumption that has been made. The number (or pair of numbers) indicates the robot (or robot pairs) concerned with the assumption. The placement of the arrow indicates the region that the robot is headed (i.e. its action commands $AP^{R}$) when the given assumption holds true true (Color figure online).

Fig. 8 Example of the approach in a scenario with six dynamic obstacles (dark red) and one controlled quadrotor (light green/yellow). The path of the controlled quadrotor is shown with a dashed green line. a The original approach without deadlock resolution avoids collisions but can get into unresolved deadlocks. The path leading to the deadlock is shown, b the proposed approach successfully resolves deadlocks, like the one shown here. The path leading to and resolving the deadlock are shown, c path of the controlled quadrotor using the proposed approach during a 10 min simulation. The quadrotor successfully avoids collisions and reverts the motion when it encounters a deadlock. a Without deadlock resolution, b with deadlock resolution, c path with deadlock resolution (Color figure online).
In the “counter-flow” example of Fig. 10, 100% of the simulation runs without the proposed deadlock resolution approach eventually enter unresolved deadlock at some point during the run. In contrast, when the proposed approach is used, deadlock is able to be resolved, resulting in more goals being visited. In the single-robot case, only 5% of the runs lead to unresolved deadlock. In all such runs, the DOs had violated a runtime certificate (note that the DOs were not programmed to satisfy any such certificates); in some cases the DOs surrounded the robot. In the two-robot case, nearly 20% of the runs lead to unresolved deadlock. This number is higher than in the one-robot case because there is more than one robot whose motion could be blocked by the DOs, leading to more encountered deadlocks. Additionally, when one robot has already become deadlocked, the objects in the environment effectively act as static obstacles to the remaining robot, increasing the chance it will become deadlocked as compared with moving, dynamic obstacles. The combined effect of these two factors is the reason why there is a four-fold increase in the number of encountered deadlocks.

The “random waypoints” cases are included to evaluate the performance of the proposed approach where the DOs do not all move in the same direction, but instead move randomly in the workspace. In the case of a single robot, deadlock resolution allows the robots to find alternate routes around deadlocks, and thus the robot is able to visit 40% more goals than the case without deadlock resolution. In the case of two robots, the team is able to achieve 136% more goals than without resolution. As may be observed in the supplementary videos, deadlock resolution gives the robots an ability to exploit areas of the workspace containing a lower density of dynamic obstacles to achieve their goals. The cases where deadlock resolution is included results in greater likelihood of task achievement over a 200-s interval. As compared with the counter-flow cases, there are fewer cases of unresolved deadlock because the random nature of the DOs allows the robots to move more freely in some cases than in others.

9.4 3D problem domain

We next demonstrate the effectiveness of the approach in a 3D scenario where, in the $5 \times 5 \times 5$ m$^3$ two-floor workspace of Fig. 11, robots move between floors through a vertical opening at the left corner or the stairs at the right side. The two robots on the team as well as the dynamic obstacle are simulated quadrotors. The task is to infinitely often visit the top and bottom floors while avoiding collisions and resolving deadlock. The strategy automaton is synthesized as described in Sect. 5. A local planner for the 3D environment is constructed following Sect. 7. A representative experiment is shown in the snapshots in Fig. 11. The green robot enters
deadlock when moving towards the upwards corridor; however, deadlock is resolved by taking the alternative route up the stairs.

9.5 Physical experiments

To demonstrate effectiveness in a physical setting, we employ two Aldebaran Nao robots to carry out the planar garbage collection scenario, with a teleoperated KUKA youBot serving as the dynamic obstacle. The model for the Nao robots is one where the robots are able to rotate in place, move forward, and move along a curve at a constant velocity. The size of the field is 5 m by 3 m, and the sensing range for the local planner is 1 m. The size is such that only one Nao robot may fit through the Hall and Door at a time. The positions of each robot are measured through a motion capture system. The local planner is implemented on a laptop computer communicating via a WiFi connection to the robots. In the local planner, the Nao robots are taken to have a circular footprint with effective radius of 0.2 m.

We carried out experiments using two robots on the team, using the workspace shown in Fig. 7. The revisions for these two robots are pictured in the figure for the synthesized mission plan. As demonstrated in the snapshots in Fig. 12, the Nao can execute the task, by avoiding collisions and resolving deadlocks with one another and with the dynamic obstacle (the KUKA youBot). At the particular deadlock event shown in Fig. 12b, the youBot must eventually move away from the Door region, as the assumption pictured in Fig. 7 states that ‘only temporary deadlock is allowed’ when either of the robots are trying to enter it from the Kitchen. The experiments demonstrate that the approach is effective at deadlock resolution and at achieving collision free motion, thereby satisfying the mission specification.

10 Conclusion

We present a framework for synthesizing a strategy automation and collision-free local planner that guarantees completion of a task specified in linear temporal logic, where we consider reactive mission specifications abstracted with respect to basic locomotion, sensing and actuation capabilities. Our approach is less conservative than current approaches that impose a separation between agents, and is computationally cheaper than explicitly modeling all possible obstacles in the environment. If no controller is found that satisfies the specification, the approach automatically generates the needed assumptions on deadlock to render the specification realizable and communicates these to the user. The approach generates controllers that accommodate deadlock between robots or with dynamic obstacles independently of the precise number of obstacles present, and we have shown that the generated controllers are correct with respect to the original specification. Experiments with ground and aerial robots demonstrate collision avoidance with other agents and obstacles, satisfaction of a task, deadlock resolution and livelock-free motion. Future work includes optimizing the set of revisions and decentralizing the synthesis.

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