Reconfigurable Adaptive Channel Sensing

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Abstract—This paper proposes an energy-efficient detection scheme, referred to as AdaSense, that is particularly suitable in the sparse regime when events to be detected happen rarely. To minimize energy consumption, AdaSense exploits the dependency between the receiver noise figure (i.e., the receiver added noise) and the receiver power consumption; less noisy channel observations typically imply higher power consumption. AdaSense is duty-cycled and begins each cycle with a few channel observations in a low-power-low-reliability mode. Based on these observations, it makes a first tentative decision on whether or not a message is present. If no message is declared, AdaSense waits till the beginning of the next cycle and starts afresh. If a message is tentatively declared, AdaSense enters a confirmation second phase, takes more samples, but now in a high-power-high-reliability mode. If these observations confirm the tentative decision, AdaSense stops, else AdaSense waits till the beginning of the next cycle and starts afresh in the low-power-low-reliability mode. Compared to prominent detection schemes such as the clear channel assessment algorithm of the Berkeley Media Access Control (BMAC) protocol, AdaSense provides relative energy gains that grow unbounded in the small probability of false-alarm regime, as communication gets sparser. In the non-asymptotic regime, energy gains are 30% to 75% for communication scenarios typically found in the context of wake-up receivers.

Index Terms—Channel sensing, detection, adaptive sampling, low-energy communication, wake-up receiver.

I. INTRODUCTION

EVENT-TRIGGERED communication scenarios, such as alarms and monitoring systems [1], [2], [3], or distributed detection in wireless sensor networks [4], [5], [6], often arise in the context of device-to-device communication. Predominantly, these devices possess limited battery [7]. Consequently, keeping these devices constantly switched-on is infeasible, especially if the event triggering the communication is low-probability, such as fire alarms [8].

To minimize energy consumption modern receivers are typically duty cycled [9], [10], [11], [12], [13], [14], [15], [16], [17], i.e., they listen only at predetermined time periods, and sleep otherwise. To alert the receiver of an incoming message, the transmitter sends a preamble either at the beginning of a listening period (e.g., [9], [17], [18], [19]), or immediately in which case the preamble is long enough to cover at least one listening period (e.g., [12], [15]). In both cases (as seen in [9], [12], [15], [17], [18], [19]) the receiver performs a binary hypothesis test, referred to as channel sensing, during the listening periods, to decide whether or not a preamble is present.

How to minimize the energy consumption of a channel sensing scheme given a desired reliability specified in terms of the probabilities of false-alarm and miss-detection? In this paper we address this question through a simple scheme referred to as AdaSense (for adaptive sensing). In a nutshell, AdaSense reconfigures its noise level in an adaptive manner in order to strike a balance between reliability and energy consumption. In more detail, the significant contributor to the noise in a machine-to-machine communication channel is the receiver noise, which is typically a non-increasing function of the power consumption at the receiver (see, e.g., [20, Ch. 12]); therefore, higher reliability requires greater power consumption. AdaSense exploits this dependency to adaptively choose the noise level of the observed samples in order to minimize the overall energy consumed in channel sensing.

AdaSense has two phases. In the first phase, AdaSense observes a small batch of samples at low power and makes a tentative decision on whether or not a preamble is present. If no preamble is detected, AdaSense stops, declares that there is no preamble, and moves to the next listening phase. If a preamble is detected, AdaSense enters a second confirmation phase and observes a fresh batch of samples at a higher power. At the end of this second phase, AdaSense decides whether or not the preamble is present. An overview of AdaSense’s operation is available in Figure 1.

We compared AdaSense against two well-known schemes, the “single-phase” scheme and the clear channel assessment algorithm of the Berkeley Media Access Control (BMAC) protocol [12], henceforth referred to as the BMAC scheme. The single-phase scheme refers to the standard binary hypothesis test based on the observations at constant power of a fixed number of n samples, where n denotes the length of the preamble. Upon observation, either a preamble is declared, or otherwise the receiver stops and waits for the next listening period. The BMAC scheme instead is sequential. The receiver observes samples at a constant power and declares that the preamble is present only if all n sample values exceed a given threshold. As soon as one sample value is below the threshold, it stops, declares that no preamble is present, and waits for the next listening period.

We show that the relative energy gain of AdaSense, compared to the BMAC and the single-phase schemes, grow
unbounded in the small probability of false alarm regime. In the non-asymptotic setting, our comparisons demonstrate that AdaSense achieves the targeted sensing performance with a reduced detection time, while consuming 30%-75% less energy than the single-phase and the BMAC schemes, across communication scenarios typically encountered in the context of event-triggered communication.

A. Related Works

AdaSense is inspired by the adaptive detection schemes proposed in [21], [22], [23], [24] which aim at minimizing the number of samples needed to efficiently detect a message. While the number of samples can be taken as a proxy for energy consumption, the present paper goes further by considering the actual energy spent in the observation of a sample through its dependency with the receiver noise figure. In particular, leveraging upon this dependency AdaSense adaptively varies the power consumption, in addition to the number of samples.

Two-stage detection schemes have also been proposed in the context of cognitive radios, where a binary hypothesis test is performed to determine whether a channel is busy or free [25], [26], [27]. These schemes however are weaker than AdaSense, since they only vary detection thresholds across the two phases, while keeping the power consumption constant. Moreover, the number of samples observed in the different phases are fixed beforehand, irrespective of the targeted levels of reliability. In contrast, AdaSense saves energy by choosing a different power consumption and a different number of samples for the two phases according to the desired reliability level.

B. Organization

The rest of the paper is organized as follows. In Section II, we give a precise description of the channel sensing problem. In Section III, we describe AdaSense and compare it with the single-phase scheme and the BMAC scheme. We first make analytical comparisons in the small probability of false-alarm regime as communication gets sparser, then make comparisons in non-asymptotic regimes through numerical performance evaluations. In Section IV, we discuss a possible practical implementation of AdaSense. Finally, in Section V, we draw a few concluding remarks.

II. CHANNEL SENSING: RELIABILITY AND ENERGY CONSUMPTION

Channel sensing at the physical layer amounts to a binary hypothesis test. Let $Y_1, Y_2, \ldots, Y_N$ denote the outputs of a coherent receiver that observes a modulated binary message $M \in \{0, 1\}$, repeated $N$ times, and corrupted by additive noise, that is

$$Y_i = M \cdot \sqrt{P} + Z_i, \quad 1 \leq i \leq N,$$  

where $Z_i \sim \mathcal{N}(0, \sigma_i^2)$ denotes the noise of the $i$-th sample, and where $P$ denotes the received power.\footnote{Authors note: The observed statistic on which they perform the hypothesis test is the signal energy. This is in contrast to our setting which involve coherent receivers (see Section II), and hence we observe the signal directly. However, adapting the detection schemes of [25], [26], [27] to our setting is straightforward.}

The two possible values of $M$ are interpreted as the hypothesis $H_0 = \{M = 0\}$, corresponding to no preamble, and $H_1 = \{M = 1\}$, corresponding to a preamble being present. These hypothesis are supposed to have a known prior which reflects the level of communication sparsity

$$p_1 = \Pr(H_1) = 1 - \Pr(H_0).$$

Based on $Y_1, Y_2, \ldots, Y_N$ the receiver provides a message estimate $\hat{M} \in \{0, 1\}$. The reliability of the estimator $\mathcal{N}(\mu, \sigma^2)$ refers to the Gaussian distribution with mean $\mu$ and variance $\sigma^2$. 

Fig. 1. An overview of AdaSense.
is quantified in terms of the probabilities of false-alarm and miss-detection
\[
P_{\text{FA}} = \Pr(\hat{M} = 1 | H_0) \quad \quad P_{\text{Miss}} = \Pr(\hat{M} = 0 | H_1).
\]

(2)

In addition to reliability, we are interested in the average energy \(E\) spent by the receiver in observing \(Y_1, \ldots, Y_N\). To quantify this energy, observe that the noise variance \(\sigma^2_r\) may be decomposed as
\[
\sigma^2_r = \sigma^2_t + \sigma^2_{r,i},
\]
where \(\sigma^2_t\) denotes the contribution due to thermal noise, and where \(\sigma^2_{r,i}\) denotes the contribution of the receiver. In many practical setups (see Section III-C), the thermal noise \(\sigma^2_t\) is negligible with respect to the receiver noise and is thus ignored. Therefore, we assume that
\[
\sigma^2_r = \sigma^2_{r,i}.
Our results (next section) immediately extend to the case where \(\sigma^2_t\) is no longer negligible, but yield slightly more cumbersome analytical results—this is briefly alluded to in Section V.

The receiver noise variance \(\sigma^2_{r,i}\) is typically a function of the receiver power consumption \(P_{r,i}\); the lower \(\sigma^2_{r,i}\) the larger \(P_{r,i}\). This function depends on the receiver circuit itself, and particularly on the low noise amplifier used in the receiver circuit (see, e.g., [20, Ch. 12]). We model this dependency by letting
\[
\sigma^2_{r,i} = f(P_{r,i})
\]
where \(f(\cdot)\) denotes a non-negative and non-increasing function, which we shall refer to as the noise profile of the receiver—in practice this function can be determined by means of electrical simulations on the low noise amplifier.3 Based on [28], throughout the paper we assume that the noise profile is given by
\[
\sigma^2_{r,i} = kP^{-\gamma}_r
\]
for some known \(k > 0\) and \(\gamma \geq 1\)—the case \(\gamma < 1\) is arguably less natural and shall be omitted.

Without loss of generality, we assume that the number of observed samples, \(N\), is no larger than the length \(n\) of the preamble. Moreover, both the number of observed samples and the power at which the samples are observed can be chosen adaptively. In more detail, the decision to stop at the \(i\)-th observation may depend on \(Y_1, \ldots, Y_i\). Similarly, the power \(P_{r,i}\) at which symbol \(Y_i\) is observed may depend on past observed samples \(Y_1, Y_2, \ldots, Y_{i-1}\). In probability language, \(N\) is a stopping time [29, Ch. 9] defined on the natural filtration induced by the process \(Y_1, Y_2, \ldots\) and the process \(P_{r,1}, P_{r,2}, \ldots\) is predictable with respect to this filtration.

3We emphasize the distinction between \(P\), the power of the received signal, and \(P_r\) the power consumed by the receiver to observe the signal.

The average energy consumption till a decision is made is then given by
\[
E = \mathbb{E}\left(\sum_{i=1}^{N} P_{r,i}\right)
\]
where \(\mathbb{E}\) denotes expectation over the channel noise and over the two hypothesis \(H_1\) and \(H_0\), assumed to have prior \(p_1\) and \(1 - p_1\), respectively. Here, we assume that each symbol has unit duration, without loss of generality.4

III. RESULTS

We first describe AdaSense in Section III-A, a scheme which aims at minimizing \(E\) for fixed \(P_{\text{FA}}\) and \(P_{\text{Miss}}\). We then compare AdaSense against two well-known detection schemes, namely the single-phase scheme and the BMAC scheme. In Section III-B, we provide analytical comparisons in the regime of small probability of false-alarm and sparse communication, which is relevant for IoT type of applications. In Section III-C, we numerically compare these schemes for a variety of relevant non-asymptotic parameters.

A. AdaSense

AdaSense is a two-phase scheme as illustrated in Fig. 2. It starts by observing a first batch of samples and makes a tentative decision. If \(H_0\) is declared AdaSense stops, and if \(H_1\) is declared AdaSense performs a second “highly reliable” confirmation test based on a second batch of samples. If hypothesis \(H_1\) is confirmed, AdaSense outputs \(H_1\), else it outputs \(H_0\).

In more detail, let \(\ell_1\) and \(\ell_2\) be two nonnegative integers such that \(\ell_1 + \ell_2 \leq n\), and let \(P_{r,1}, P_{r,2}\) be the receiver power consumptions for the two phases. The receiver starts by observing \(\ell_1\) samples \(Y_1, Y_2, \ldots, Y_{\ell_1}\) at a constant power \(P_{r,1}\) per sample. It then performs a standard log-likelihood ratio (LLR) test to discriminate between the hypothesis \(H_0\) and \(H_1\) (see Case III.B.2 of [30]), i.e., the receiver checks whether
\[
T_1 = \frac{\sqrt{P}}{\sigma^2_{r,1}} \sum_{i=1}^{\ell_1} Y_i - \frac{\ell_1 P}{2\sigma^2_{r,1}} \leq \eta_1,
\]

\[\]for an arbitrary symbol duration \(T_s\), just multiply \(E\) by \(T_s\) in equation (3).
for some given threshold $\eta_1$, and where $\sigma_{\ell_1}^2 = f(P_{r,1})$. If this inequality is satisfied, the receiver stops and declares $\bar{M} = 0$. Otherwise, it enters a second confirmation phase, observes the next $\ell_2$ samples $Y_{\ell_1+1}, \ldots, Y_{\ell_1+\ell_2}$ at a constant power $P_{r,2}$ per sample, typically greater than $P_{r,1}$, and performs a second LLR test on this second batch of samples, i.e., it checks whether

$$T_2 = \frac{\sqrt{2}}{\sigma_{\ell_2}^2} \sum_{i=\ell_1+1}^{\ell_1+\ell_2} Y_i - \frac{\ell_2 P_{r,2}}{2\sigma_{\ell_2}^2} > \eta_2$$

(5)

for some given threshold $\eta_2$, and where $\sigma_{\ell_2}^2 = f(P_{r,2})$. If this second inequality is satisfied, the receiver declares $\bar{M} = 1$, and otherwise $\bar{M} = 0$.

For this scheme, $P_{FA}, P_{Miss}$ and $E$ are explicitly given by (see Appendix A)\(^5\)

$$P_{FA} = Q\left(\frac{\sigma_{\ell_1} \eta_1}{\sqrt{2} P_{r,1}} + \frac{1}{2} \frac{\ell_1 P_{r,1}}{\sigma_{\ell_1}^2}\right) Q\left(\frac{\sigma_{\ell_2} \eta_2}{\sqrt{2} P_{r,2}} + \frac{1}{2} \frac{\ell_2 P_{r,2}}{\sigma_{\ell_2}^2}\right),$$

(6)

$$P_{Miss} = Q\left(\frac{-\sigma_{\ell_1} \eta_1}{\sqrt{2} P_{r,1}} + \frac{1}{2} \frac{\ell_1 P_{r,1}}{\sigma_{\ell_1}^2}\right) + \left(1 - Q\left(\frac{-\sigma_{\ell_1} \eta_1}{\sqrt{2} P_{r,1}} + \frac{1}{2} \frac{\ell_1 P_{r,1}}{\sigma_{\ell_1}^2}\right)\right) \times Q\left(\frac{-\sigma_{\ell_2} \eta_2}{\sqrt{2} P_{r,2}} + \frac{1}{2} \frac{\ell_2 P_{r,2}}{\sigma_{\ell_2}^2}\right),$$

(7)

and

$$E = \ell_1 P_{r,1} + p_c \ell_2 P_{r,2},$$

(8)

where $p_c$ denotes the probability of having a second phase and is given by

$$p_c = (1 - p_1) Q\left(\frac{\sigma_{\ell_1} \eta_1}{\sqrt{2} P_{r,1}} + \frac{1}{2} \frac{\ell_1 P_{r,1}}{\sigma_{\ell_1}^2}\right) + p_1 \left(1 - Q\left(\frac{-\sigma_{\ell_1} \eta_1}{\sqrt{2} P_{r,1}} + \frac{1}{2} \frac{\ell_1 P_{r,1}}{\sigma_{\ell_1}^2}\right)\right).$$

Given the received power $P$, the preamble length $n$, the sparsity level $p_1$, and the reliability targets $P_{FA} \leq \alpha$, $P_{Miss} \leq \beta$, the set of parameters $\{\ell_1, P_{r,1}, \eta_1, \ell_2, P_{r,2}, \eta_2\}$ are chosen so that to minimize the average energy:

$$\left\{\ell_1, P_{r,1}, \eta_1, \ell_2, P_{r,2}, \eta_2\right\} = \arg \min \left\{\ell_1, P_{r,1}, \eta_1, \ell_2, P_{r,2}, \eta_2\right\} \quad E \quad \text{s.t.} \quad \ell_1 + \ell_2 \leq n, \quad P_{FA} \leq \alpha, \quad P_{Miss} \leq \beta.$$  \hspace{1cm} (9)

Note that $N$ takes value $\ell_1$ or $\ell_1 + \ell_2$ and that the constraint $\ell_1 + \ell_2 \leq n$ refers to the constraint $N \leq n$—see Section II.

The optimization problem in (9) is non-convex. A quick way to see this is as follows. Consider the constraint $P_{Miss} \leq \beta$. Note that the expression for $P_{Miss}$ given in (7) involves $Q$-functions which are non-convex. Furthermore, observe that the variable $\ell_1$ appears within the argument to $Q$-functions present in the constraint in the following way, $Q\left(\frac{\sigma_{\ell_1}}{\sqrt{2} P_{r,1}} + b \sqrt{\ell_1}\right)$. Again, it is not difficult to see that functions of the form $f(x) = \frac{\sigma_1}{\sqrt{2} P_{r,1}} + b \sqrt{\ell_1}$ are not convex in general. As a result the constraint $P_{Miss} \leq \beta$ is clearly a non-convex constraint. One can similarly argue using (6) and (8) respectively that the constraint $P_{FA} \leq \alpha$ and the objective function $E$ (due to the presence of the quantity $p_c$) are non-convex.

It is well-known that non-convex optimization admits no analytical solution in general (see for example [31, Sec. 1.4]). Fortunately, for our purpose, the optimization problem (9) can easily be numerically evaluated as described in Section III-C. It should also be noted that this optimization needs to be carried out only once per target values $\alpha, \beta, n, p_1$ and $P$. Depending on $(\alpha, \beta)$ there might be no solution\(^6\) in which case we set $E = \infty$. However, if only $(\alpha, \beta)$ are fixed and $n$ can be optimized over then the above optimization problem always admits a feasible solution (see, e.g., [30, Example II.D.1]).

\begin{figure}[t]
\centering
\includegraphics[width=0.5\textwidth]{Fig3.pdf}
\caption{Single-phase scheme.}
\end{figure}

\subsection*{B. Performance: Small Probability of False-Alarm and Sparse Communication Regime}

The next result explicits a tradeoff between $E$ and $P_{FA}$ at fixed $P_{Miss}$ for AdaSense, when $P_{FA}$ tends to zero (the proof is deferred to Appendix C)\(^7\):

Theorem 1 (AdaSense, Asymptotics): Suppose $f(P_{r}) = kP_{r}^{-\gamma}$ for some fixed $\gamma \geq 1$ and $k > 0$. For any fixed $p_1, P > 0, 0 < \beta \leq 1$ and $0 < \varepsilon < 1$ AdaSense achieves $P_{Miss} \leq \beta$ and

$$E \leq \frac{2k^{1}}{P^{(1-\varepsilon - \alpha(1))}} \ln\left(\frac{1}{P_{FA}}\right)$$

(10)

where $o(1) \rightarrow 0$ as $P_{FA} \rightarrow 0$. Moreover, this tradeoff between $P_{Miss}$, $P_{FA}$, and $E$ is achievable with $n = O(\ln(1/P_{FA}))$.

The important thing to notice here is that the sparser the communication, that is the smaller $p_1$, the lower $E$. To put this result into perspective we now consider two other widely known detection schemes, namely the basic “single-phase” scheme and the BMAC scheme.

The single-phase scheme is described in Fig. 3. The receiver performs an (optimal) LLR test on a fixed number of $n$ samples $Y_1, \ldots, Y_n$, each observed at a constant receiver power $P_{r}$. The test consists in declaring $\bar{M} = 1$ whenever $T \geq \sqrt{2} P_{r} \sum_{i=1}^{n} Y_i - \frac{p_2 \sigma_{\ell_2}^2}{\sigma_{\ell_2}^2}$ is above a given threshold $\eta$ that depends

\footnote{That is no $\{\ell_1, P_{r,1}, \eta_1, \ell_2, P_{r,2}, \eta_2\}$ such that $\ell_1 + \ell_2 \leq n, P_{FA} \leq \alpha$, and $P_{Miss} \leq \beta$.}

\footnote{We make use of the Big O notation for limiting function behavior.}

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Similarly to the single-phase scheme, the energy spent by the BMAC scheme does not decrease as communication gets sparser. But note that the above lower bound has the preamble length \( n \) in the denominator. It turns out that this is inherent to the BMAC scheme and is not due to a loose lower bound—see proof of Theorem 3. A larger value of \( n \) allows to lower the receiver power for a given level of false-alarm. However, if we impose BMAC to operate with the same preamble length as for AdaSense, and require \( n = O(\ln(1/P_{\text{FA}})) \), AdaSense remains the most energy efficient in the sparse regime \( p_1 \rightarrow 0 \), at a fixed but small probability of false-alarm. In the next section, we will also see that for a wide range of parameter values AdaSense performs the best in terms of energy consumption.

### C. Performance: Nonasymptotic Parameters Regime

In this section we compare the performances of AdaSense, BMAC, and the single-phase scheme with parameters found in the context of wake-up receivers. Regarding preamble length we consider \( n \in \{20, 30, 40, 50\} \) which are consistent with the value in [14]. We fix the range of target \( P_{\text{FA}} \) and \( P_{\text{Miss}} \) to be respectively \([10^{-6}, 10^{-5}]\) and \([10^{-10}, 10^{-9}]\), as in [14], [33].

The probability \( p_1 \) varies with applications. For example, temperature sensors deployed in some cities are monitored every few minutes [34], which, considering a standard bit rate of 100 kbps and \( n = 50 \), corresponds to \( p_1 = 10^{-6} \). For other applications, for example fire alarms, \( p_1 \) can be much lower (see, e.g., [8]).

A survey published in 2017 [28] recommends a worst-case received power of \(-83 \) dBm, which corresponds to a line-of-sight communication over 1200 m using an antenna transmitting at 10 mW. Accordingly, we carry out the comparisons for values of received power in the range \( P \in [-60 \) dBm, \(-80 \) dBm].

The noise profile, i.e., the function that relates the power consumption to the receiver noise variance, is unique to each receiver, and is determined by electrical simulations performed on the low noise amplifier to be used at the input stage of the receiver. For demonstration purposes, we use the noise profile determined in [28, Sec. V-B] by stating the tradeoff between sensitivity and power consumption. Sensitivity is the defined as the received power needed to detect a single bit with a bit error rate of \(10^{-3} \) [35]. It is a textbook result that an SNR of 15 dB is needed to detect a single bit with a bit error rate of \(10^{-3} \) (see [30, Example II.B.2]), and hence, receiver noise power is simply sensitivity lowered by 15 dB. The sensitivity versus power consumption tradeoff mentioned in the survey can then be rephrased as follows: 1 \( \mu \)W of power consumption leads to a receiver noise of \(-55 \) dBm, and the noise power is decreased by 20 dB by increasing the power consumption ten times. This tradeoff corresponds to the noise profile \( f(\cdot) \) given by

\[
\sigma_r^2 = f(P_r) = \frac{10^{-20.5}}{P_r^{20}},
\]

where \( P_r \) is in Watts. The contribution of the thermal noise to the overall noise power is negligible, since the least value of

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Fig. 4. BMAC scheme.
Fig. 5. $E$ versus $P_{\text{Miss}}$ for the three different schemes with $p_1 = 10^{-10}$ and under two different regimes of $P$, $n$, and $P_{\text{FA}}$.

(a) $n = 30$, $P = -60$ dBm, $P_{\text{FA}} = 10^{-3}$, $P_{\text{Miss}} = 10^{-5}$. Energy savings 43%-67%.

(b) $n = 50$, $P = -80$ dBm, $P_{\text{FA}} = 10^{-5}$, $P_{\text{Miss}} = 10^{-5}$. Energy savings 39%-67%.

Fig. 6. $E$ versus $n$ for the three different schemes with $p_1 = 10^{-10}$ and $P_{\text{Miss}} = 10^{-5}$ under two different regimes of $P$ and $P_{\text{FA}}$.

(a) $P = -60$ dBm, $P_{\text{FA}} = 10^{-3}$, $P_{\text{Miss}} = 10^{-5}$. Energy savings 50%.

(b) $P = -80$ dBm, $P_{\text{FA}} = 10^{-5}$, $P_{\text{Miss}} = 10^{-5}$. Energy savings 45%-55%.

Fig. 7. $E$ versus $P$ for the three different schemes with $p_1 = 10^{-10}$ and $P_{\text{Miss}} = 10^{-5}$ under two different regimes of $n$ and $P_{\text{FA}}$.

(a) $n = 30$, $P_{\text{FA}} = 10^{-3}$, $P_{\text{Miss}} = 10^{-5}$. Energy savings 50%.

(b) $n = 50$, $P_{\text{FA}} = 10^{-5}$, $P_{\text{Miss}} = 10^{-5}$. Energy savings 60%.

As we see in Figures 5–8, AdaSense is always the most energy-efficient scheme, followed by the BMAC scheme and the single-phase scheme. Savings mostly vary around 30% to 70%, depending on the regimes of $P$, $n$, $P_{\text{FA}}$, and $P_{\text{Miss}}$, though outliers with savings as low as 13% and as high as 96% have been recorded (see Figure 8).

Finally, for AdaSense, the numerical optimization of (9) was obtained through the MATLAB fmincon optimizer, using multiple initial guesses. A detailed pseudocode is available in

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σ² used in our comparisons is −92.15 dBm, whereas standard values of thermal noise power lie below −113.83 dBm.  

AdaSense has the smallest detection delay—this follows from the fact that both BMAC and single-phase schemes require $n$ samples to detect a preamble, whereas AdaSense is constrained (see (9)) to take $\ell_1 + \ell_2 \leq n$ samples. Next, in Figures 5–8, we compare the exact energy consumption of the single-phase, the BMAC, and AdaSense (8)—after the optimization (9). The exact performance of these schemes are deferred to Appendix A, see Propositions 1-3. The graphs in Figures 5, 6, 7, and 8, plot the energy consumption $E$ versus $P_{\text{Miss}}$, $n$, $P$, and $P_{\text{FA}}$, respectively, while keeping the other parameters fixed. For example, Figure 6 plots $E$ versus $n$, for $P \in \{-60 \text{ dBm}, -80 \text{ dBm}\}$, $P_{\text{FA}} \in \{10^{-3}, 10^{-5}\}$, and $P_{\text{Miss}} = 10^{-5}$. The exact details of the fixed parameters appear in the captions below the figures. We further comment that these plots hold for any $p_1 < 10^{-4}$—in this range of $p_1$ plots remain unchanged.

As we see in Figures 5–8, AdaSense is always the most energy-efficient scheme, followed by the BMAC scheme and the single-phase scheme. Savings mostly vary around 30% to 70%, depending on the regimes of $P$, $n$, $P_{\text{FA}}$, and $P_{\text{Miss}}$, though outliers with savings as low as 13% and as high as 96% have been recorded (see Figure 8).

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8The thermal noise power is calculated using the formula $\sigma^2 = k_b T B$ in Watts [20, Ch. 11], where $k_b$ is the Boltzman constant, $T$ is the temperature, and $B$ is the bandwidth. We have used $T = 300K$ (see for example [35]) and $B = 1MHz$, which is the maximum bandwidth allocated to low power devices in the IEEE 802.15.4 standard for low-rate communication [36].
Algorithm 1 in Appendix B. Algorithm 1 was run on a simple desktop computer (Intel Core i5-10400 CPU @ 2.90GHz 16 GB of memory). The maximum wall-clock time needed to run the optimization was a couple of hours per set of target parameters. We remark that the time required is not an issue since the optimization in (9) needs to be run only once to set the parameters $\ell_1, \ell_2, \eta_1, \eta_2, P_{R,1}$, and $P_{R,2}$ for AdaSense.

IV. IMPLEMENTATION

In this section we briefly outline a possible implementation of AdaSense, see Fig. 9. The first few stages are standard for coherent receivers, which include a low noise amplifier (LNA) and a down-mixer followed by a rectifier or envelope detector and the integrator, which convert the incoming on-off keying (OOK) modulated signal to the required weighted sum $\frac{P}{\sigma_1^2} \sum_{i=1}^{\ell_1} Y_i$ (see Section III) [37, Ch. 2]. This is then compared against the threshold $\eta_1 + \frac{\ell_1 P}{2\sigma_1^2}$ (see Section III) using a comparator. The heart of the architecture then lies in switching the mode of the receiver or turning it off, which is taken care of by the digital controller block.

The overhead of AdaSense with respect to a classical non-adaptive receiver is the transition between the first and the second phase. This requires modification of the noise figure (in order to switch the noise variance from $\sigma_1^2$ to $\sigma_2^2$), the integration constant which controls the weighted sum, and the threshold. There are several efficient approaches to reconfigure the receiver noise figure. Firstly, note that the Friis formula (see [38]) says that the components at the beginning of the receiver chain (i.e., the radio frequency (RF) components) are the major sources of the receiver noise. The low noise amplifier (LNA) occurring at the start of the receiver chain is therefore the most suitable site to perform the noise figure reconfiguration. The simplest approach to perform this reconfiguration is to adjust the LNA’s bias current. A higher bias current leads to a higher transconductance of the LNA, and hence, a better noise figure [20], but at the cost of higher power consumption. Besides the bias current readjustment method, there exists other methods to reconfigure the noise figure of the LNA as well (see [39], [40], [41]). The choice of the exact reconfiguration method will depend on the application and the receiver architecture. It is worth mentioning that the narrow bandwidth of the modulated signals relaxes the speed constraints on the reconfiguration and makes it easy to implement. To modify the integration constant we need to modify passive elements (capacitors or resistors). This is achieved by implementing two different values of the considered elements (resistance or capacitance) and connecting or disconnecting them using switches depending on the phase. The comparison threshold is obtained through resistive bridge dividers. To generate different comparison voltages, it suffices to add an additional resistance in the resistive ladder, which allows us to generate two comparison voltages. Depending on the phase, the comparator is connected to one or the other using switches.

V. CONCLUDING REMARKS

In this paper we proposed a new channel sensing scheme, AdaSense, which is particularly energy efficient in the sparse communication regime. The main difference with existing schemes is that AdaSense adaptively chooses the number of observed samples as well as the power at which these samples are observed. We demonstrated that AdaSense provides higher energy savings than other existing channel sensing schemes, for an additive white Gaussian noise channel. Notice that the results immediately extend to the case where the thermal noise is no longer negligible—just add the thermal noise variance $\sigma_t^2$ to the receiver noise $\sigma_r^2 = f(P_r)$ throughout.

It should perhaps be emphasized that AdaSense operates only according to two power levels. In fact, one could envision a more gradual procedure where, after each observation, the receiver either stops or observes the next sample at a potentially lower noise level. Preliminary calculations reveal that the energy gains provided by such a general scheme would not be substantial compared to AdaSense. Moreover, potential energy gains would probably be offset by an increased complexity at the hardware level. Indeed, as suggested in Section IV, the implementation overhead of AdaSense with respect to a non-adaptive receiver appears to be negligible. This suggests that duty cycled receivers, including the duty-cycled wake-up receivers [14], [15], [16], [17], could benefit from AdaSense.

While in this paper we work with channels with fixed received power, our results and calculations can be extended to channels where the received power is a random variable,
such as fading channels. Extension of our results are also possible to channels with multiple antennas. Even in such scenarios, AdaSense, working with multiple receiver power consumption levels, and allowed to choose the number of samples it observes adaptively, will consume lower energy than schemes with fixed power levels. We leave the task of demonstrating the exact amount of energy savings provided by AdaSense for fading and multiple antenna channels as future work. Furthermore, noting that channel sensing is a hypothesis test, a comparison of AdaSense with active hypothesis testing merits attention in the future.

Finally, regarding the physical implementation, the chosen architecture should integrate the three needed reconfigurations to switch between the two phases, i.e., i) noise figure vs power consumption reconfiguration ii) integration constant adjustment and iii) comparison threshold adjustment. A possible implementation of the receiver and the reconfigurations have been introduced in the paper. Other families of receivers could be used such as mixer-first. The choice of the best architecture should be done as a compromise between the inherent power consumption of the architecture and its suitedness to Adasense, which we leave as future work.

**APPENDIX A**

**EXACT ANALYSIS**

According to the channel model (1), the distribution of the samples $Y_i$ under either of the hypothesis $H_0$ or $H_1$ is i.i.d., and is given by

$$Y_i \sim \begin{cases} 
\mathcal{N}(0, \sigma^2), & \text{given } H_0 \\
\mathcal{N}(\sqrt{P}, \sigma^2), & \text{given } H_1.
\end{cases}$$

Therefore, the log-likelihood ratio (LLR) of $m$ i.i.d. samples $Y_1, Y_2, \ldots, Y_m$ is given by

$$T = \log \left( \frac{\prod_{i=1}^{m} \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{1}{2\sigma^2} (Y_i - \sqrt{P})^2 \right)}{\prod_{i=1}^{m} \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{1}{2\sigma^2} (Y_i)^2 \right)} \right) = \frac{\sqrt{P}}{\sigma^2} \sum_{i=1}^{m} Y_i - \frac{mP}{2\sigma^2}.$$  \hspace{1cm} (12)

Hence,

$$T \sim \begin{cases} 
\mathcal{N}\left(-\frac{mP}{2\sigma^2}, \frac{mP}{\sigma^2}\right) & \text{given } H_0 \\
\mathcal{N}\left(\frac{mP}{2\sigma^2}, \frac{mP}{\sigma^2}\right) & \text{given } H_1.
\end{cases}$$

The next three propositions state the performance of the single-phase scheme, the BMAC scheme, and AdaSense, in the non-asymptotic regime.

**Proposition 1**: Given $n$, $P$, $\sigma_r^2 = f(P_r)$, the single-phase scheme achieves

$$P_{FA} = Q\left(\frac{\sigma_r \eta}{\sqrt{nP}} + \frac{1}{2} \sqrt{nP} \frac{1}{\sigma_r^2}\right),$$

and

$$P_{Miss} = Q\left(-\frac{\sigma_r \eta}{\sqrt{nP}} + \frac{1}{2} \sqrt{nP} \frac{1}{\sigma_r^2}\right).$$

The energy consumed by the receiver is

$$E = nP_r.$$  \hspace{1cm} (14)

**Proposition 2 (BMAC)**: Given $p_1$, $n$, $P$, $\sigma_r^2 = f(P_r)$, the BMAC scheme achieves

$$P_{FA} = P_{e,0}^n,$$

and

$$P_{Miss} = 1 - (1 - P_{e,1})^n,$$

where $P_{e,0} = Q\left(\frac{P_{e,0}}{\sigma_r^2}\right)$, $P_{e,1} = 1 - Q\left(\frac{\sqrt{P_{e,1}}}{\sigma_r^2}\right)$, with $\eta \in \mathbb{R}$. The average energy consumed by the BMAC scheme is

$$E = P_r \left[ \frac{p_1 P_{Miss}}{1 - (1 - P_{Miss})^{1/n}} + \frac{(1 - p_1)(1 - P_{FA})}{1 - P_{FA}^{1/n}} \right]$$

$$= P_r \left[ 1 - P_{FA}^{1/n} \right] + o(1)$$

where $o(1)$ tends to zero as $p_1 \to 0$.

Note that given $p_1$, $n$, and $P$, fixing any two values among $P_{FA}$, $P_{Miss}$, and $E$ specifies the third one.

**Proof of Proposition 2**: We have

$$P_{FA} = \Pr\left(\hat{M} = 1 | H_0\right).$$

\footnote{Recall that the transmitted symbols have unit duration.}
\[E = \prod_{i=1}^{n} \Pr(Y_i > \eta| H_0) = \prod_{i=1}^{n} \Pr(Y_i > \eta| H_1) = Q \left( \frac{\eta}{\sigma_r} \right)^n,\]

where (16) follows from the fact that the BMAC detection rule declares \( \hat{M} = 1 \) if and only if \( Y_i > \eta \) for \( i \in \{1, \ldots, n\} \) and (17) follows from (11). Similarly, we have

\[P_{\text{Miss}} = \Pr(\hat{M} = 0| H_1) = 1 - \prod_{i=1}^{n} \Pr(Y_i > \eta| H_1) = 1 - Q \left( \frac{\eta - \sqrt{P}}{\sigma_r} \right)^n.\]

For the average energy consumption \( E \) we have

\[E = \sum_{i=1}^{n} iP_r \Pr(N = i) = \sum_{i=1}^{n} iP_r[p_1 \Pr(N = i| H_1) + (1 - p_1) \Pr(N = i| H_0)].\]

We now calculate \( \Pr(N = i| H_0) \). For \( i < n \), note that \( N = i \) if and only if \( Y_j > \eta \) for all \( j < i \), and \( Y_i \leq \eta \). Thus, by (11), we have

\[\Pr(N = i| H_0) = Q \left( \frac{\eta}{\sigma_r} \right)^{i-1} \left( 1 - Q \left( \frac{\eta}{\sigma_r} \right) \right).\]

On the other hand, \( N = n \) occurs if and only if \( Y_j > \eta \) for all \( j < n \). Therefore, \( \Pr(N = n| H_0) = Q \left( \frac{\eta}{\sigma_r} \right)^{n-1} \). Similarly, we have

\[\Pr(N = i| H_1) = Q \left( \frac{\eta - \sqrt{P}}{\sigma_r} \right)^{i-1} \left( 1 - Q \left( \frac{\eta - \sqrt{P}}{\sigma_r} \right) \right),\]

for all \( i < n \), and

\[\Pr(N = n| H_1) = Q \left( \frac{\eta - \sqrt{P}}{\sigma_r} \right)^{n-1} \].

Define \( p \triangleq Q \left( \frac{\eta}{\sigma_r} \right) \) and \( q \triangleq Q \left( \frac{\eta - \sqrt{P}}{\sigma_r} \right) \). Then, using (20)

\[E = \sum_{i=1}^{n-1} iP_r \left[ p_1q^{i-1}(1-q) + (1-p_1)p^{i-1}(1-p) \right] + nP_r \left[ p_1q^{n-1} + (1-p_1)p^{n-1} \right] = P_r \left[ \sum_{i=0}^{n-1} q^{i} + (1-p_1) \sum_{i=0}^{n-1} p^{i} \right] = P_r \left[ p_1 \frac{1 - q^n}{1 - q} + (1-p_1) \frac{1 - p^n}{1 - p} \right] = P_r \left[ p_1 \frac{P_{\text{Miss}}}{1 - (1 - P_{\text{Miss}})^{1/n}} + (1 - p_1) \frac{1 - P_{\text{FA}}}{1 - P_{\text{FA}}^{1/n}} \right],\]

where (21) follows from the definitions of \( p \) and \( q \) together with (17) and (19).

**Proposition 3 (AdaSense):** Given \( p_1, n, P, \sigma^2_r = f(P_r) \), the first and second phase lengths \( \ell_1, \ell_2 \geq 0 \) such that \( \ell_1 + \ell_2 \leq n \), the powers in the first and second phases \( P_{r,1}, P_{r,2} \geq 0 \), and the thresholds of the hypothesis tests of the first and second phases \( \eta_1, \eta_2 \in \mathbb{R} \), AdaSense yields

\[P_{\text{FA}} = Q \left( \frac{\sigma_{r,1}\eta_1}{\sqrt{\ell_1}P} + \frac{1}{2} \sqrt{\frac{\ell_1}{\sigma^2_{r,1}}} \right) Q \left( \frac{\sigma_{r,2}\eta_2}{\sqrt{\ell_2}P} + \frac{1}{2} \sqrt{\frac{\ell_2}{\sigma^2_{r,2}}} \right),\]

and

\[P_{\text{Miss}} = Q \left( -\frac{\sigma_{r,1}\eta_1}{\sqrt{\ell_1}P} + \frac{1}{2} \sqrt{\frac{\ell_1}{\sigma^2_{r,1}}} \right) + \left( 1 - Q \left( -\frac{\sigma_{r,1}\eta_1}{\sqrt{\ell_1}P} + \frac{1}{2} \sqrt{\frac{\ell_1}{\sigma^2_{r,1}}} \right) \right) \times Q \left( \frac{\sigma_{r,2}\eta_2}{\sqrt{\ell_2}P} + \frac{1}{2} \sqrt{\frac{\ell_2}{\sigma^2_{r,2}}} \right),\]

The average energy consumed is given by

\[E = \ell_1 P_{r,1} + p_c \ell_2 P_{r,2},\]

where

\[p_c = (1 - p_1)Q \left( \frac{\sigma_{r,1}\eta_1}{\sqrt{\ell_1}P} + \frac{1}{2} \sqrt{\frac{\ell_1}{\sigma^2_{r,1}}} \right) + p_1 \left( 1 - Q \left( -\frac{\sigma_{r,1}\eta_1}{\sqrt{\ell_1}P} + \frac{1}{2} \sqrt{\frac{\ell_1}{\sigma^2_{r,1}}} \right) \right) = Q \left( \frac{\sigma_{r,1}\eta_1}{\sqrt{\ell_1}P} + \frac{1}{2} \sqrt{\frac{\ell_1}{\sigma^2_{r,1}}} \right) + o(1),\]

where \( o(1) \) tends to zero as \( p_1 \) tends to zero.

**Proof of Proposition 3:** We begin by evaluating the LLR for samples in the first and the second phases. Recall that the first batch of \( \ell_1 \) samples are received with noise variance \( \sigma^2_{r,1} = f(P_{r,1}) \), while the second batch of \( \ell_2 \) samples are received with noise variance \( \sigma^2_{r,2} = f(P_{r,2}) \). Let \( T_1 \) and \( T_2 \) denote the LLRs of the samples in the first and the second phases, respectively. By (12), we have

\[T_1 = \sqrt{\frac{P}{\sigma^2_{r,1}}} \sum_{i=1}^{\ell_1} Y_i - \frac{\ell_1 P}{2\sigma^2_{r,1}},\]

\[T_2 = \sqrt{\frac{P}{\sigma^2_{r,2}}} \sum_{i=\ell_1+1}^{\ell_1+\ell_2} Y_i - \frac{\ell_2 P}{2\sigma^2_{r,2}}.\]

From (13)

\[T_1 \sim \left\{ \begin{array}{ll} \mathcal{N} \left( \frac{-\ell_1 P}{2\sigma^2_{r,1}} \right) & \text{given } H_0, \\ \mathcal{N} \left( \frac{\ell_1 P}{2\sigma^2_{r,1}} \right) & \text{given } H_1, \end{array} \right. \]

and

\[T_2 \sim \left\{ \begin{array}{ll} \mathcal{N} \left( \frac{-\ell_2 P}{2\sigma^2_{r,2}} \right) & \text{given } H_0, \\ \mathcal{N} \left( \frac{\ell_2 P}{2\sigma^2_{r,2}} \right) & \text{given } H_1. \end{array} \right. \]
Note that $T_1$ and $T_2$ are independent since they are functions of different sets of samples.

We now proceed to evaluate $P_{FA}$ and $P_{Miss}$. Note that $\tilde{M} = 1$, if and only if $T_1 > \eta_1$ and $T_2 > \eta_2$. Therefore,

$$P_{FA} = \Pr(T_1 > \eta_1|H_0)\Pr(T_2 > \eta_2|H_0)$$

$$= Q\left(\frac{\sigma_r\eta_1}{\sqrt{\ell_1 P}} + \frac{1}{2} \sqrt{\frac{\ell_1 P}{\sigma_{r,1}^2}}\right) Q\left(\frac{\sigma_r\eta_2}{\sqrt{\ell_2 P}} + \frac{1}{2} \sqrt{\frac{\ell_2 P}{\sigma_{r,2}^2}}\right),$$

(26)

where the second equality follows from (24) and (25).

Similarly, we have

$$P_{Miss} = \Pr(T_1 \leq \eta_1|H_1) + \Pr(T_1 > \eta_1|H_1)\Pr(T_2 \leq \eta_2|H_1)$$

$$= Q\left(-\frac{\sigma_r\eta_1}{\sqrt{\ell_1 P}} + \frac{1}{2} \sqrt{\frac{\ell_1 P}{\sigma_{r,1}^2}}\right)\left(1 - Q\left(-\frac{\sigma_r\eta_1}{\sqrt{\ell_1 P}} + \frac{1}{2} \sqrt{\frac{\ell_1 P}{\sigma_{r,1}^2}}\right)\right)$$

$$\times Q\left(-\frac{\sigma_r^2\eta_2}{\sqrt{\ell_2 P}} + \frac{1}{2} \sqrt{\frac{\ell_2 P}{\sigma_{r,2}^2}}\right).$$

(27)

Next, we compute the average energy consumption $E$. We have

$$E = \ell_1 P_{r,1} + p_c \ell_2 P_{r,2}$$

where $p_c$ denotes the probability that the scheme continues after the first phase by $p_c$, that is $T_1 > \eta_1$. From (24), we have

$$p_c = (1 - p_1)\Pr(T_1 > \eta_1|H_0) + p_1\Pr(T_1 > \eta_1|H_1)$$

$$= (1 - p_1) Q\left(\frac{\sigma_r\eta_1}{\sqrt{\ell_1 P}} + \frac{1}{2} \sqrt{\frac{\ell_1 P}{\sigma_{r,1}^2}}\right)$$

$$+ p_1 \left(1 - Q\left(-\frac{\sigma_r\eta_1}{\sqrt{\ell_1 P}} + \frac{1}{2} \sqrt{\frac{\ell_1 P}{\sigma_{r,1}^2}}\right)\right).$$

(28)

(29)

which concludes the proof.

**APPENDIX B**

**Pseudocode to Obtain the Optimal Parameters for AdaSense Using fmincon**

In this section, we provide the pseudocode used to numerically solve the optimization in (9) needed to set the parameters $\ell_1, \ell_2, \eta_1, \eta_2, P_{r,1}, P_{r,2}$ of AdaSense, for a given $n$, $P$, $p_1$, $\alpha$, and $\beta$. As described in Section III, the optimization in (9) is non-convex, and hence we resort to obtain a ‘good-enough’ feasible point using MATLAB’s built-in fmincon optimizer. The fmincon module however performs local optimization starting with a single initial guess. Since the objective function and the constraints in (9) are highly non-convex, we run multiple instances of fmincon initiated at different points, and choose the best possible feasible choice, i.e., the one with the least energy consumption, across all possible instances.

In more detail, for the initialization, we chose two possible values for all parameters except $P_{r,1}$ and four possible values for $P_{r,2}$. In total, this gave us $2^2 \times 4 = 128$ different initial points. We initiated the fmincon solver at each of these initial points, and returned the results of the one which gave a feasible point with the least energy. The details are available in Algorithm 1.

**APPENDIX C**

**Asymptotics**

**Proof of Theorem 2 (Single-Phase):** From Stein’s Lemma [32, Th. 11.8.3], if the single-phase satisfies $P_{Miss} \leq \beta$, for some fixed $0 < \beta < 1$, then

$$P_{FA} = \exp\left(-\frac{P}{2 \sigma_r^2} n \pm o(n)\right)$$

$$= \exp\left(-\frac{P}{2k} P_r^\gamma n \pm o(n)\right)$$

$$= \exp\left(-\frac{P P_r^\gamma - 1}{2k} E \pm o(E)\right)$$

(30)

where for the first inequality we used the noise profile $\sigma_r^2 = kP_r^{-\gamma}$ and where the second inequality holds since $E = nP_r$ (see (14)). Therefore,

$$E = \frac{2k}{PP_r^{-\gamma}(1 \pm o(1))} \ln(1/P_{FA})$$

where $o(1)$ vanishes as $P_{FA} \to 0$—notice that as $P_{FA} \to 0$ we necessarily have $n$ and $E$ tend to infinity.

Notice that the proof of Theorem 2 also holds if $0 < \gamma < 1$. The same comment goes for the proof of Theorem 3 (see below). We nevertheless chose to state these theorems by restricting $\gamma \geq 1$ for the sake of uniformity with Theorem 1 and since the case $\gamma < 1$ is less natural as previously alluded to.

**Proof of Theorem 1 (AdaSense):** By Proposition 3

$$E = E_1 + E_2 p_c$$

(31)

where

$$E_i = \ell_i P_{r,i} \quad i = 1, 2$$

denotes the energy spent during the first and the second phase, and where $p_c$ denotes the probability that AdaSense performs the second phase, i.e., $p_c = \Pr(T_1 > \eta_1)$.

Now pick $0 < \varepsilon < 1$ and let us allocate the energy $E$ of the first and the second phase as

$$E_1 = \varepsilon E = \ell_1 P_{r,1}$$

and

$$E_2 = \frac{(1 - \varepsilon) E}{p_c} = \ell_2 P_{r,2}$$

(32)

Furthermore, pick

$$\ell_i = \delta_i n \quad i = 1, 2$$

(33)

such that $\delta_1 > 0$, $\min\{E_2/n, \varepsilon\} \leq \delta_2 \leq 1 - \varepsilon$, and $\delta_1 + \delta_2 \leq 1$. As we will see below, the tradeoff between $P_{FA}$ and $E$ is improved as $\varepsilon$ gets smaller, that is when the overwhelming energy is spent during the second phase.

$^{10}$We write $f(n) = g(n) \pm q(n)$ if $g(n) - q(n) \leq f(n) \leq g(n) + q(n).$
Algorithm 1 Optimization for AdaSense in (9)

Input: $n, P, \alpha, \beta, p_1$

1: $\ell_1^{(i)} \leftarrow [\ell_{1j}^{(i)} : 1 \leq j \leq k_1]$, $\ell_2^{(i)} \leftarrow [\ell_{2j}^{(i)} : 1 \leq j \leq k_2]$, $\eta_1^{(i)} \leftarrow [\eta_{1j}^{(i)} : 1 \leq j \leq k_3]$, $\eta_2^{(i)} \leftarrow [\eta_{2j}^{(i)} : 1 \leq j \leq k_4]$, $P_r, 1 \leftarrow [P_r, 1_j : 1 \leq j \leq k_5]$, $s^{(i)} \leftarrow [s_{ij}^{(i)} : 1 \leq j \leq k_6]$

$\triangleright$ Initial values of $\ell_1, \ell_2, \eta_1, \eta_2, P_r, 1, s \triangleq P_r, 2$ for starting fmincon.

2: flag$\leftarrow 0$;
3: val$\leftarrow 0$;

4: for $j_1 = 1 : k_1$
5: for $j_2 = 1 : k_2$
6: for $j_3 = 1 : k_3$
7: for $j_4 = 1 : k_4$
8: for $j_5 = 1 : k_5$
9: for $j_6 = 1 : k_6$
10: init$\leftarrow [\ell_{1,j_1}^{(i)}, \ell_{2,j_2}^{(i)}, \eta_{1,j_3}^{(i)}, \eta_{2,j_4}^{(i)}, P_r, 1_{,j_5}, s_{,j_6}]$; $\triangleright$ The initial guess for the optimization
11: $\ell_1, \ell_2, \eta_1, \eta_2, P_r, 1, \tilde{s} \leftarrow$ OPTIMIZE(init);
$\triangleright$ Optimization in (9) using fmincon. Returns the best possible argument as obtained by fmincon.
12: con1$\leftarrow 1\{\ell_1 + \ell_2 - n \leq 0\}$;
13: con2$\leftarrow 1\{P_{FA} \leq \alpha\}$;
14: con3$\leftarrow 1\{P_{Miss} \leq \beta\}$;
$\triangleright$ $P_{FA}$ is calculated according to (6) using $\ell_1, \ell_2, \eta_1, \eta_2, P_r, 1, \tilde{s}$
15: $E \leftarrow \tilde{\ell}_1 P_r, 1 + p_r P_r, 2$; $\triangleright$ Computing $E$ according to (8)
16: if con1$\Leftarrow 1$ && con2$\Leftarrow 1$ && con3$\Leftarrow 1$ then
17: if flag$\Leftarrow 0$ then
18: val$\leftarrow E$;
19: $\ell_1^*, \ell_2^*, \eta_1^*, \eta_2^*, P_r^*, s^* \leftarrow \ell_1, \ell_2, \eta_1, \eta_2, P_r, 1, \tilde{s}$;
20: flag$\leftarrow 1$;
21: end if
22: if $E < \text{val}$ then
23: val$\leftarrow E$;
24: $\ell_1^*, \ell_2^*, \eta_1^*, \eta_2^*, P_r^*, s^* \leftarrow \ell_1, \ell_2, \eta_1, \eta_2, P_r, 1, \tilde{s}$;
25: end if
26: end if
27: end if
28: end for
29: end for
30: end for
31: end for
32: end for
33: if flag$\Leftarrow 0$ then
34: return ‘No feasible point found’
35: else
36: return $\ell_1^*, \ell_2^*, \eta_1^*, \eta_2^*, P_r^*, s^*$
37: end if

From Stein’s Lemma [32, Th. 11.8.3] it follows that for any $\beta > 0$, the thresholds $\eta_1, \eta_2$ may be set such that $P_{Miss} \leq \beta$ and such that

$$\Pr(T_i > \eta_j | H_0) \leq \exp\left(-\frac{P}{2 \sigma_{r,i}^2} \ell_i + o(\ell_i)\right) \quad i = 1, 2.$$  (34)

Hence, from (26)

$$P_{FA} \leq \exp\left(-\frac{P}{2 \sigma_{r,2}^2} \ell_2 + o(\ell_2)\right) = \exp\left(-\frac{P}{2k} P_{r,2}^\gamma \delta_2 n + o(n)\right)$$  (35)

and distinguish the cases $\gamma = 1$ and $\gamma > 1$. $\gamma = 1$: In this case (36) is equal to $(1 - \varepsilon)E/np_c$ which together with (35) yields

$$\max_{(P_{r,2}, \delta_2)} \frac{P_{r,2}^\gamma \delta_2}{\min\{E_2/n, \varepsilon\}} \leq \delta_2 \leq 1 - \varepsilon \quad P_{r,2} \Delta = E_2/n$$  (36)
where \( \alpha(1) \) tends to zero as \( E \) tends to infinity. Hence, \( \gamma > 1 \): Here we obtain a tradeoff between energy and probability of false-alarm which is at least as good as for \( \gamma > 1 \). To see this suppose \( n \delta_2 P_{r, 2} = E_2 \) and pick \( \delta_2 > 0 \) small enough so that \( P_{r, 2} \geq 1 \) (this is possible since by assumption \( \delta_2 \) can be taken as small as \( \min(\varepsilon, E_2/n) \leq E_2/n \). Then \( P_{r, 2} \geq 1 \) and we deduce that (36) is greater or equal to \( E_2/n \). Hence (38) also holds if \( \gamma > 1 \).

We now upper bound \( p_c \) as

\[
\begin{align*}
p_c &= \Pr(T_1 > \eta_1 H_0)(1 - p_1) + \Pr(T_1 > \eta_1 H_0)p_1 \\
&\leq \Pr(T_1 > \eta_1 H_0) + p_1 \\
&\leq p_1 + o(1)
\end{align*}
\]

where \( o(1) \) tends to zero as \( n \) tends to infinity (or, equivalently, as \( P_{FA} \) tends to zero), and where for the last inequality we used (34) and the fact that \( \ell_1 \) increases with \( n \). The theorem then follows from (38) and (39).

**Proof of Theorem 3:** From Proposition 2, if BMAC satisfies \( P_{FA} = \alpha \) and \( P_{Miss} = \beta \), then

\[
\alpha = Q\left(\frac{\eta}{\sigma_r}\right)^n (1 - \beta) = Q\left(\frac{\eta - \sqrt{P}}{\sigma_r}\right)^n
\]

\[
E \geq P_r \frac{(1 - p_1)(1 - \alpha)}{1 - \alpha^{1/n}}.
\]

From (40), the noise profile \( \sigma_r^2 = kP_r^{-\gamma} \), and the Chernoff approximation on the Q-function \( Q(x) = \exp(-x^2/2(1 + o(1))) \) as \( x \to \infty \) we deduce that

\[
P_r = \left(\frac{\sqrt{\frac{Q^{-1}(\alpha^{1/n})}{\eta}}}{\eta}\right)^{2/\gamma} = \left(\frac{2}{n\eta^2(1 + o(1))}\ln(1/\alpha)\right)^{1/\gamma}
\]

where \( o(1) \to 0 \) as \( \alpha \to 0 \). Hence, from (42)

\[
E \geq \frac{(1 - p_1)(1 - \alpha)}{1 - \alpha^{1/n}} \left(\frac{2k}{n\eta^2(1 + o(1))}\ln(1/\alpha)\right)^{1/\gamma}
\]

Assuming \( \beta < 1/2 \) we necessarily have \( \eta \leq \sqrt{P} \) from (41) and we finally get

\[
E \geq (1 - p_1) \left(\frac{2k}{n\eta^2(1 + o(1))}\ln(1/\alpha)\right)^{1/\gamma}(1 - o(1)).
\]

as \( \alpha \to 0 \).

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