Real time simulation of sensorless control based on back-EMF of PMSM on RT-Lab/ARTEMIS real-time digital simulator

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Article Info

ABSTRACT

Real-time simulation (RT) is very useful for rapid prototyping of complex and expensive systems using the high performance of a multiprocessor system. It has many applications in the field of testing controllers and protection systems under real conditions. In this article, Real-time simulations results of sensorless control of permanent magnet synchronous motor (PMSM) are presented. This simulator consists of two major subsystems, software with a Matlab / Simulink and hardware including FPGA boards for data acquisition, control boards and sensors. The two subsystems were coordinated together to achieve the simulation RT. To estimate the rotor position, a sliding mode observer (SMO) based on back emfs of the motor was implemented. The stability of the proposed method was verified using the concept of Lyapunov. A real-time system based on FPGA, is used for implementing and testing the algorithm for rotor position estimation based on back-emf tracking.

Keywords:
PMSM
Real time simulation
RT-Lab
Sensorless control
Sliding mode observer

1. INTRODUCTION

The Permanent-Magnet Synchronous Motor (PMSM) controlled by a converter of power electronics is a nonlinear system usually present complex. The main research areas in electrical drives include high-level integrated motor drive, new topologies of converter-inverter, new adjustable speed drives (ASD), optimization of performance, control algorithms, and fault tolerant controllers design. Therefore, to perform tests at system level which is one of the principle subsystems in the development of a complex product and to maintain this development and prototyping costs at reasonable level, we need real-time (RT) simulations [1-5]. In addition, trying to reach technology and cost at optimum point, it pushes us to use a device that can be able of doing many parallel execution at the same time. DSPs are fast but it is necessary to do sequential calculation. If someone wants to build simulation in real time it is possible with DSP but it needs a DSP with very fast clock. Since the 1970s, Programmable logic arrays (PLAs) have been available but their applications were limited. Field-Programmable Gate Array offers more possibilities by the (FPGA) concept [6-8], introduced by Xilinx' cofounder Freeman in 1984 [9]. RT-Lab simulator consists of two major subsystems, software with a Matlab / Simulink and hardware including FPGA boards for data acquisition, control boards and sensors. The two subsystems were coordinated together to achieve the simulation RT.

Recently, there has been a lot of interest in the development of sensorless algorithms in which the motor was controlled using the rotor angular speed estimated values [10, 11]. Several methods have been developed in order to estimate speed or position of the rotor, and among them are Extended Kalman Filter
(EKF), Sliding Mode Observer (SMO) and Flux Linkage Observer (FLO) [12]. The latter has a fast response, good robustness against themachine parameter variations and external disturbances [13, 14]. In sensorless control [15-21], some variables of machines are often not directly measurable, but their accurate knowledge is more than necessary for high-performance electrical drives control. Sensorless vector control scheme is successfully implemented if the the accuracy of the estimation of the rotor position is good. This algorithm is implemented by fundamental excitation method and the position of the rotor is detected from the back electromotive force (back EMF) [22, 23].

In this paper, a fully digital real-time simulation of a high performance of sensorless control of Permanent Magnet Synchronous Motor based on back-EMF estimator was presented. The validation and implementation of the proposed algorithm was reached through Opal RT’s RT-Lab real-time simulation platform; able to perform calculations at time steps up to 10μs. This real-time simulation tool is now extensively employed by a great number of high-tech industries as a real-time laboratory package for rapid prototyping of complex control systems and for hardware-in-the-loop (HIL) applications. By the use of HIL simulations in the design process, overall cost can be reduced, development cycles reduced, costly breakdowns avoided, and interaction between different subsystems tested.

2. PMSM MATHEMATICAL MODEL

The field-based control framework presented in this paper is presented on a low voltage permanent magnet synchronous motor. To simplify the motor equations, the following hypotheses have been formulated [1, 19]: Magnetic flux distribution in the air gap is sinusoidal, Inductivity and resistivity are constant and equivalent in all phases, Hysteresis losses and Eddy currents are neglected and Lead of star point is not connected. Model of synchronous motor in (d − q) rotating frame can be described by (1)

\[
\begin{align*}
\frac{d}{dt} [_{d}i_{d}] &= -\frac{R_s}{L_s} i_{d} - \frac{e_{a}}{L_s} + \frac{1}{L_s} u_{sa} \\
\frac{d}{dt} [_{d}i_{q}] &= -\frac{R_s}{L_s} i_{q} - \frac{e_{a}}{L_s} + \frac{1}{L_s} u_{sb} \\
\frac{d}{dt} \omega &= \frac{p}{J} (i_{d} \cos \theta_e - i_{q} \sin \theta_e) - \frac{f}{J} - \frac{C_e}{J}
\end{align*}
\]

Where \(u_{sa}, u_{sb}, i_{d}, i_{q}\) are the (\(\alpha, \beta\)) components of stator voltage and current vectors, and \(\Omega = \omega \theta_e\) are the mechanical angular speed and rotor position, \(R_s, L_s\) are stator resistance and inductance, \(\phi_f\) is the flux generated by PMs, \(J\) is moment of inertia, \(C_e\) is electromagnetic torque and \(p\) is the number of motor pole pairs. \(e_{a}\) and \(e_{b}\) are the stator back EMF components on (\(\alpha, \beta\)) frame defined by (2)

\[
\begin{align*}
e_{a} &= -\phi_f \omega_e \sin \theta_e \\
e_{b} &= \phi_f \omega_e \cos \theta_e
\end{align*}
\]

3. SLIDING MODE OBSERVER

3.1. Observer based on back EMF

For the estimation of the unmeasured mechanical quantities, we will develop an electromotive force (EMF)-based sliding mode observer defined in (2). Assuming that the speed varies slowly [24, 25].

\[
\omega_e \approx 0
\]

The EMF dynamics can be written as follows

\[
\begin{align*}
\frac{de_{a}}{dt} &= -\omega_e e_{b} \\
\frac{de_{b}}{dt} &= -\omega_e e_{a}
\end{align*}
\]

The SMO can be designed from the electrical equations in the fixed reference (\(\alpha, \beta\)) (1) and the back EMF dynamics (4)
\[
\begin{align*}
\left\{ \begin{array}{l}
    i_{sa, \text{est}} = -\frac{R_s}{L_s} i_{sa} - \frac{e_{a, \text{est}}}{L_s} + \frac{1}{L_s} u_{sa} + K_s \text{sign}(i_{sa} - i_{sa, \text{est}}) \\
    i_{sb, \text{est}} = -\frac{R_s}{L_s} i_{sb} - \frac{e_{b, \text{est}}}{L_s} + \frac{1}{L_s} u_{sb} + K_s \text{sign}(i_{sb} - i_{sb, \text{est}})
\end{array} \right.
\tag{5}
\]

The EMF is given as follows
\[
\begin{align*}
\left\{ \begin{array}{l}
    \dot{e}_{a, \text{est}} = -e_{\beta, \text{est}} \omega_{e, \text{est}} + k_2 \text{sign}(i_{sa} - i_{sa, \text{est}}) \\
    e_{\beta, \text{est}} = -e_{a, \text{est}} \omega_{e, \text{est}} + k_2 \text{sign}(i_{sb} - i_{sb, \text{est}})
\end{array} \right.
\tag{6}
\end{align*}
\]

Where, \(i_{sa, \text{est}}, i_{sb, \text{est}}\) are estimated currents and \(k_1, k_2\) are observer gains.

The estimated speed can be calculated from (2)
\[
\omega_{e, \text{est}} = \frac{1}{\phi_f} \sqrt{\frac{e_{a, \text{est}}^2}{e_{a, \text{est}}^2} + e_{\beta, \text{est}}^2} \text{sign}(E_q)
\tag{7}
\]

\[
\Omega_{e, \text{est}} = \frac{1}{p} \omega_{e, \text{est}} \text{ and } E_q \text{ is the back EMF on the axis (q)}
\]

Finally, the rotor position can be estimated as follow
\[
\theta_{e, \text{est}} = \arctan \left( \frac{-e_{a, \text{est}}}{e_{\beta, \text{est}}} \right)
\tag{8}
\]

### 3.2. Stability analysis

A fast and accurate current regulator is essential to reach a good dynamic and static performance of sensorless control of the PMSM. The structure of the proposed control uses two sliding surfaces to regulate the stator current according to the fixed reference \((\alpha, \beta)\)

\[
i_{sa} S_a = i_{sa} - i_{sa, \text{est}}
\tag{9}
\]

\[
i_{sb} S_\beta = i_{sb} - i_{sb, \text{est}}
\tag{10}
\]

When the variable structure control system operates in sliding mode, the switching control law ensures the condition \(S_a = S_\beta = 0\). AN yapunov function is used to analysis the stability of the sliding mode observer

\[
V = \frac{1}{2} S^T S = \frac{1}{2} (S_a^2 + S_\beta^2) = \frac{1}{2} \left( (i_{sa} - i_{sa, \text{est}})^2 + (i_{sb} - i_{sb, \text{est}})^2 \right)
\tag{11}
\]

Requisite condition for sliding mode observer stability is obtained as follows

\[
\dot{V} = S_a \dot{S}_a + S_\beta \dot{S}_\beta \leq 0
\tag{12}
\]

By subtracting (10) from (5) and (6), the estimation error equation is concluded

\[
\begin{align*}
\left\{ \begin{array}{l}
    i_{sa, \text{est}} = -\frac{R_s}{L_s} (i_{sa} - i_{sa, \text{est}}) - \frac{e_{a, \text{est}}}{L_s} - K_s \text{sign}(i_{sa} - i_{sa, \text{est}}) \\
    i_{sb, \text{est}} = -\frac{R_s}{L_s} (i_{sb} - i_{sb, \text{est}}) - \frac{e_{\beta, \text{est}}}{L_s} - K_s \text{sign}(i_{sb} - i_{sb, \text{est}})
\end{array} \right.
\tag{13}
\end{align*}
\]

Then

\[
\begin{align*}
V &= -\frac{R_s}{L_s} (i_{sa} - i_{sa, \text{est}})^2 - \frac{1}{L_s} e_{a, \text{est}} (i_{sa} - i_{sa, \text{est}}) - K_s (i_{sa} - i_{sa, \text{est}}) \text{sign}(i_{sa} - i_{sa, \text{est}}) - \\
& \frac{R_s}{L_s} (i_{sb} - i_{sb, \text{est}})^2 - \frac{1}{L_s} e_{\beta, \text{est}} (i_{sb} - i_{sb, \text{est}}) - K_s (i_{sb} - i_{sb, \text{est}}) \text{sign}(i_{sb} - i_{sb, \text{est}})
\tag{14}
\end{align*}
\]

From (14) we have

\[
-\frac{R_s}{L_s} (i_{sa} - i_{sa, \text{est}})^2 - \frac{R_s}{L_s} (i_{sb} - i_{sb, \text{est}})^2 \leq 0
\tag{15}
\]
\[ V < 0, \text{ if} \]
\[ \frac{1}{L_s} e_{a,\text{est}} (i_s - i_{sa,\text{est}}) - K_1 \left| i_s - i_{sa,\text{est}} \right| - \frac{1}{L_s} e_{\beta,\text{est}} \Rightarrow \left| i_s - i_{s\beta,\text{est}} \right| - K_1 \left| i_s - i_{s\beta,\text{est}} \right| < 0 \] (16)

Therefore, to keep the observer sliding modes stable, the observer gain should satisfy the following inequality

\[ K_1 > \max \left( \frac{e_{a,\text{est}}}{L_s}, \frac{e_{\beta,\text{est}}}{L_s} \right) \] (17)

According to (17), the observer gain must be greater than the induced back EMF.

4. PLATFORM OF RT-LAB REAL TIME

The RT-LAB Simulator Architecture is shown in Figure 1. RT-LAB simulator includes:

- One or more target PC’s; one of the PCs (Master) operates the communication between the hosts and the targets and between all other target PC’s. The targets use the Quick unix (QNX) operating system in real time.
- One or more host PC’s permitting multiple users to access the targets; one of the hosts PC’s has simulator control fully, while other hosts, in read-only mode, can display and receive simulator signals in real time.
- Various Types of Inputs/Outputs (I/O’s); Input & Output (Digital & Analog), Pulse Width Modulation (PWM) in & out, timers, encoders, etc. I/O’s can be managed by dedicated processors distributed [26] over several nodes.

![Figure 1. RT-Lab simulator architecture](image)

5. REAL TIME HYBRID SIMULATION PRINCIPLE

A PC-Cluster is a parallel multiprocessor computer system capable of meeting the real-time simulation performance requirements [1, 27]. Figure 2 shows the design of the real-time digital simulation of PMSM sensorless control. The real-time simulation is performed by running on separate processors (targets) and in parallel the speed and decoupling control module, the static converter module and the PMSM module. These three modules are actually C code (digital modules) obtained by an automatic code generator for real-time execution.

![Figure 2. Real-time simulation of PMSM](image)
6. IMPLEMENTATION USING RT-LAB SIMULATOR

6.1. Organization of software development

Figure 3 shows the proposed sensorless control of PMSM as implemented in Real time RT-Lab environment. The model is distributed over three target processor motherboards. The first two target processors operate at 2.4 GHz. The third, connected to others through a fast real-time Fire Wire link. The first CPU of the dual CPU unit calculates in real time the sliding mode observer and the decoupling unit of the rotor flux. The second calculates in real time the permanent magnet synchronous motor, the PWM signal generator and the voltage source inverter. The third processor is dedicated to data acquisition. The host PC is the console used for the control signals, the input reference, and the signal visualization.

Figure 3. Real-time model configuration of the PMSM

Figure 4 shows the steps of control algorithm for real-time execution. In RT-Lab real time simulation, the first step is to group the model into sub-systems; the second step is the addition of the OpComm communication blocks which allow the activation and the saving of communication between host PC and target PC as well as between the different calculation nodes of a distributed simulation. The last step is to execute the model under RT-Lab according to the following steps (see Figure 4): open the model already created under Matlab/Simulink, then divide the global system into subsystems (model separation) and convert the Simulink model in real time via Real-Time Workshop (RTW) (specify exactly on which node of target will be executed each subsystem) and finally run the model on one or more QNX (Quick Unix) target. The C code is generated automatically for each subsystem for real-time execution [3]. Figure 5 shows the experimental setup of RT-Lab platform. The distributed configuration (multiple targets) allows complex models to be distributed on a parallel PC cluster. The real-time cluster is connected to the host PC through a TCP/IP Protocol.

Figure 4. Steps of control algorithm for real-time execution
7. REAL TIME SIMULATION RESULTS

Using sim power systems (SPS) toolbox, the sensorless control induction motor drive system has been modeled and built offline in Simulink environment. The offline Simulink model uses a variable step solver. For the improvement simulation speed, RT-Lab real-time platform uses a discretized fixed step time solver with a step size of 100µs which is much smaller than what could be achieved by the most advanced DSPs. The workstation is connected to the real-time simulation platform via the Ethernet (TCP/IP) protocol. The target runs the model and the results are viewed and saved on the workstation, which is the front end interface.

Figures 6 to Figure 8 show real-time simulation results of the sensorless control of the PMSM. The results of the sliding mode observer based on the estimation of back EMF show a good performance with small error estimation.

![Figure 5. Experimental setup of LAA/UMBB Lab](image)

![Figure 6. Real time simulation: (a) Real and reference speed, (b) Real and estimated position](image)

![Figure 7. Real time simulation of estimated back EMF](image)
The curves of real and estimated speed, position and currents respectively show the good responses. The results obtained from real time simulation show the efficiency of this powerful tool, wish is now widely used for Rapid Control Prototyping and Hardware in the Loop applications. RT-Lab/ARTEMIS simulation and model separation have significantly improved the simulation speed compared to Power System Blockset (PSB). Figure 9 shows the real time simulation of real and estimated currents. As shown in Figure 9 the estimated stator current components converge to the real stator current components, it’s clear that the waveforms of currents are sinusoid.

From the experimental results, we concluded that that the sensorless control scheme associated with sliding mode observer has a fast response time and good estimation accuracy over a wide speed range. Table 1 shows the simulation time with PSB and RT-Lab / ARTEMIS. The article [24] shows the simulation conditions and processors used for the simulation of the separate model on the multiprocessor platform.
Table 1. Simulation performance

| Simulation Mode  | Sampling Time | Acceleration | Real time report |
|-----------------|---------------|--------------|------------------|
| Simulink/PSB    | $T_s = 2 \mu s$ | 500 $\mu$s  | 1                | 250              |
| RT-Lab/ARTEMIS  | $T_s = 2 \mu s$ | 34 $\mu$s   | 14               | 15               |

8. CONCLUSION

A real-time simulation of the sensorless control using a sliding mode observer based on the back EMF estimation has been presented in this paper. The stability of the proposed scheme has been demonstrated using Lyapunov concept. The feasibility of the whole algorithm has been verified by real time simulation results using RT-Lab/ARTEMIS real time digital simulator. Hardware applications in loops need real-time simulations and their use allows rapid prototyping of high-performance electrical machine controllers. A multi-processor system, parallel processing and FPGA-based computing support make this platform a very interesting tool for research, innovation and testing. High speed PMSM implementation, especially in technology of electrical vehicle is very expensive and risky. Real time simulator helps us to evaluate simulation results. As future work, once the controller is designed in MATLAB/SIMULINK, it will be physically implemented using the rapid control prototyping of the real time RT-Lab platform. FPGA based digital platform is good enough for real time control of electrical machines.

NOMENCLATURE

RT LAB Real Time Laboratory
ARTEMIS Advanced Real-Time Electro Mechanical Simulator
PMSM Permanent Magnet Synchronous Motor
FPGA Field-Programmable Gate Array
FTP File Transfer Protocol
HIL Hardware-in-the-Loop
QNX Quick unix
RCP Rapid Control Prototyping
RTW Real-Time Workshop
SMO Sliding Mode Observer
EMF Electromotive force

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APPENDIX PMSM MOTOR PARAMETERS

Three-phase induction motor parameters, used for real-time implementation, in SI units are:

\[ R_s = 2.5 \Omega, L_s = 3.42 \text{mH}, p = 4, I_{\text{max}} A, J = 0.00025 \text{ Kg.m}^2, \phi_f = 0.47 \text{ Wb}, f = 0.05 \text{ Nm/rad.s}^{-1} \]

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Abdelhakim Idir was born in Bejaia, Algeria. He received his B.S and M.S degrees in Control from the Bejaia University and Setif University in 2003 and 2006 respectively. He received his doctorate and HDR degrees in Electrical Engineering from the University M’Hamed Bougara of Boumerdes, Algeria, in 2015 and 2018, respectively. He currently works as an associate professor in the Department of Electrical Engineering, Boumerdes University, Algeria. He is the author and co-author of numerous research publications in international conferences and journals. In 2019, he joined the Department of Electrical Engineering at the Mohamed Boudiaf University of M’sila, where he is currently working as an associate professor. His current research interests include the modeling, simulation and control of fractional systems, fractional PID control, AC drives and renewable energy.

Real time simulation of sensorless control based on back-EMF of PMSM on RT-Lab/ARTEMIS ... (A. Idir)
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