Effects of Fock term, tensor coupling and baryon structure variation on a neutron star

Tsuyoshi Miyatsu, Tetsuya Katayama and Koichi Saito

Department of Physics, Faculty of Science and Technology,
Tokyo University of Science, Noda 278-8510, Japan

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Abstract

The equation of state for neutron matter is calculated within relativistic Hartree-Fock approximation. The tensor couplings of vector mesons to baryons are included, and the change of baryon internal structure in matter is also considered using the quark-meson coupling model. We obtain the maximum neutron-star mass of $\sim 2.0M_\odot$, which is consistent with the recently observed, precise mass, $1.97\pm 0.04M_\odot$. The Fock contribution is very important and, in particular, the inclusion of tensor coupling is vital to obtain such large mass. The baryon structure variation in matter also enhances the mass of a neutron star.

Keywords: neutron stars, equation of state, quark-meson coupling model, relativistic Hartree-Fock calculation, tensor interaction

*Electronic address: koichi.saito@rs.tus.ac.jp
Because the internal structure and the mass of a neutron star significantly depend on the equation of state (EOS) for neutron matter, the observation of pulsars provides important information to understand the properties of dense matter \[1\]. At sufficiently high density, nuclear or neutron matter would be composed of not only nucleons \((N)\) and leptons \((\ell)\) but also hyperons \((Y)\) \[1–5\] and, possibly, meson condensates \[2, 6\]. Since it is important to calculate the EOS relativistically, many studies on neutron matter have been performed within relativistic Hartree approximation.

Recently, the precise observation finds the pulsar with the mass of \(1.97 \pm 0.04 \text{M}_\odot\) (solar mass) \[7\]. It is, however, difficult to explain the observed mass by the EOS calculated in relativistic Hartree approximation, because the inclusion of hyperons makes the EOS soft and thus reduces the maximum mass of a neutron star \[3–5\]. Thus, it seems very urgent to consider how this discrepancy can be reconciled. It may be necessary to first study the effects of the Fock term, the tensor couplings of vector mesons and the baryon structure change in matter, and see how those effects contribute to the EOS or the maximum mass of a neutron star.

In fact, the relativistic Hartree-Fock calculation of the EOS for neutron matter has already been performed in Quantum Hadrodynamics (QHD) \[8\] or in the quark-meson coupling (QMC) model \[9\], and it is pointed out that the Fock term is significant to enhance the maximum mass. However, in Ref. \[8\], the effect of the baryon structure change in matter is ignored. In Ref. \[9\], although the maximum mass of about \(2\text{M}_\odot\) is obtained, their calculation misses the tensor coupling and the space component of baryon self-energy.

In this paper, we study the properties of nuclear and neutron matter within relativistic Hartree-Fock approximation \[10, 11\], where the pion exchange and the tensor couplings of vector mesons to baryons are included in the Fock term. Furthermore, using the QMC model \[12\], we consider the variation of the quark substructure of baryon in matter. In the past few decades, the QMC model has been extensively developed and applied to various nuclear phenomena with tremendous success \[12\]. We also apply the chiral QMC (CQMC) model \[13, 14\], which is recently extended to include the quark-quark hyperfine interaction due to the gluon \[15\] and pion exchanges based on chiral symmetry, to the EOS for neutron matter.
The Lagrangian density for dense matter is given by

\[ \mathcal{L} = \mathcal{L}_B + \mathcal{L}_\ell + \mathcal{L}_M + \mathcal{L}_{\text{int}}, \]  

(1)

where

\[ \mathcal{L}_B = \sum_B \bar{\psi}_B (i \gamma_\mu \partial^\mu - M_B) \psi_B, \quad \mathcal{L}_\ell = \sum_\ell \bar{\psi}_\ell (i \gamma_\mu \partial^\mu - m_\ell) \psi_\ell, \]

(2)

with \( \psi_B(\ell) \) the baryon (lepton) field and \( M_B(m_\ell) \) the free baryon (lepton) mass. The sum \( B \) runs over the octet baryons, \( p, n, \Lambda, \Sigma^{0-} \) and \( \Xi^0- \), and the sum \( \ell \) is for the leptons, \( e^- \) and \( \mu^- \). For the baryon masses, we take \( M_N = 939 \text{ MeV}, M_\Lambda = 1116 \text{ MeV}, M_\Sigma = 1193 \text{ MeV} \) and \( M_\Xi = 1313 \text{ MeV} \), respectively.

The meson term reads

\[ \mathcal{L}_M = \frac{1}{2} \left( \partial_\mu \sigma \partial^\mu \sigma - m_\sigma^2 \sigma^2 \right) + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu - \frac{1}{4} W_{\mu\nu} W^{\mu\nu} \]

\[ + \frac{1}{2} m_\rho^2 \rho_\mu \rho^\mu - \frac{1}{4} \vec{R}_{\mu\nu} \cdot \vec{R}^{\mu\nu} + \frac{1}{2} \left( \partial_\mu \vec{\pi} \cdot \partial^\mu \vec{\pi} - m_\pi^2 \vec{\pi}^2 \right), \]

(3)

with

\[ W_{\mu\nu} = \partial_\mu \omega_\nu - \partial_\nu \omega_\mu, \quad \vec{R}_{\mu\nu} = \partial_\mu \vec{\rho}_\nu - \partial_\nu \vec{\rho}_\mu, \]

(4)

where we consider the isoscalar (\( \sigma \) and \( \omega \)) mesons and the isovector (\( \vec{\pi} \) and \( \vec{\rho} \)) mesons, and the meson masses are respectively chosen as \( m_\sigma = 550 \text{ MeV}, m_\omega = 783 \text{ MeV}, m_\pi = 138 \text{ MeV} \) and \( m_\rho = 770 \text{ MeV} \).

The interaction Lagrangian is given by

\[ \mathcal{L}_{\text{int}} = \sum_B \bar{\psi}_B \left[ g_{\sigma B}(\sigma) \sigma - g_{\omega B} \gamma_\mu \omega^\mu + \frac{f_{\omega B}}{2 \mathcal{M}} \sigma_\mu \partial^\mu \omega^\mu \right. \]

\[ \left. - g_{\rho B} \gamma_\mu \vec{\rho}_\mu \cdot \vec{I}_B + \frac{f_{\rho B}}{2 \mathcal{M}} \sigma_\mu \partial^\mu \vec{\rho}_\mu \cdot \vec{I}_B - \frac{f_{\pi B}}{m_\pi} \gamma_\mu \gamma_\nu \vec{\pi}_\mu \vec{\pi}_\nu \cdot \vec{I}_B \right] \psi_B, \]

(5)

where \( \vec{I}_B \) is the isospin matrix for baryon \( B \) (we set \( \vec{I}_B = 0 \) when \( B \) is iso-singlet) and the common, scale mass \( \mathcal{M} \) is taken to be the free proton mass \([16] \). The \( \sigma-, \omega-, \rho-, \pi-B \) coupling constants are respectively denoted by \( g_{\sigma B}(\sigma), g_{\omega B}, g_{\rho B} \) and \( f_{\pi B} \), while \( f_{\omega B} \) and \( f_{\rho B} \) are the isoscalar- and isovector-tensor coupling constants.

In QHD, \( g_{\sigma B}(\sigma) \) is constant at any density because the baryons are assumed to be structureless. In contrast, in the QMC and CQMC models, the \( g_{\sigma B}(\sigma) \) has the \( \sigma \)-field dependence, which reflects the baryon structure variation in matter \([12] \). In relativistic Hartree-Fock approximation, the \( \sigma \)-field is replaced by the constant mean-field value, \( \bar{\sigma} \). Furthermore, for
TABLE I: Values of $a_B$ and $b_B$ for various baryons in the QMC or CQMC model.

|       | QMC   |       | CQMC  |
|-------|-------|-------|-------|
|       | $a_B$ (fm) | $b_B$ | $a_B$ (fm) | $b_B$ |
| $N$   | 0.179 | 1.00  | 0.118 | 1.04 |
| $\Lambda$ | 0.172 | 1.00  | 0.122 | 1.09 |
| $\Sigma$ | 0.177 | 1.00  | 0.184 | 1.02 |
| $\Xi$  | 0.166 | 1.00  | 0.181 | 1.15 |

For simplicity, we here use the parameterization of the quark scalar-density ratio, $C_B(\bar{\sigma})$, in the linear form \[12, 17\]

\[
C_B(\bar{\sigma}) = 1 - a_B \times \left( g_{\sigma N} \bar{\sigma} \right), \tag{6}
\]

where $g_{\sigma N}$ is the $\sigma$-$N$ coupling constant at zero density and $a_B$ is a parameter. Using this parameterization, the $\sigma$-$B$ coupling constant in Eq. (5) is given by \[12, 17\]

\[
g_{\sigma B}(\bar{\sigma}) = g_{\sigma B} b_B \left[ 1 - \frac{a_B}{2} (g_{\sigma N} \bar{\sigma}) \right], \tag{7}
\]

where we introduce a parameter $b_B$ to use Eq. (7) in both the QMC and CQMC models. The values of $a_B$ and $b_B$ are listed in Table I. If we set $a_B = 0$ and $b_B = 1$, $g_{\sigma B}(\bar{\sigma})$ is identical to the $\sigma$-$B$ coupling constant in QHD.

In the present calculation, we add a non-linear (NL) term of the $\bar{\sigma}$,

\[
U(\bar{\sigma}) = \frac{g_2}{3} \bar{\sigma}^3 + \frac{g_3}{4} \bar{\sigma}^4, \tag{8}
\]

to only the QHD Lagrangian, because the EOS given by the naive QHD is too hard \[10\]. We call this QHD+NL.

To sum up all orders of the tadpole and exchange diagrams in the baryon Green’s function, $G_B$, we use the Dyson’s equation

\[
G_B(k) = G^0_B(k) + G^0_B(k) \Sigma_B(k) G_B(k), \tag{9}
\]

where $\Sigma_B$ is the baryon self-energy and $G^0_B$ is the Green’s function for the free baryon. In nuclear or neutron matter, the baryon self-energy is generally written as

\[
\Sigma_B(k) = \Sigma_B^s(k) - \gamma_0 \Sigma_B^0(k) + (\vec{\gamma} \cdot \vec{k}) \Sigma_B^v(k), \tag{10}
\]
TABLE II: Functions $A_i$, $B_i$, $C_i$, and $D_i$. The index $i$ is specified in the left column, where $V(T)$ stands for the vector (tensor) coupling at each meson-$BB'$ vertex. The last row is for the (pseudovector) pion contribution.

| $i$   | $A_i$          | $B_i$          | $C_i$          | $D_i$      |
|-------|----------------|----------------|----------------|------------|
| $\sigma$ | $g_{\sigma B}^2(\vec{\sigma})\Theta_\sigma$ | $g_{\sigma B}^2(\vec{\sigma})\Phi_\sigma$ | $-2g_{\sigma B}^2(\vec{\sigma})\Phi_\sigma$ | $-$ |
| $\omega_{VV}$ | $2g_{\omega B}^2\Theta_\omega$ | $-4g_{\omega B}^2\Phi_\omega$ | $-4g_{\omega B}^2\Phi_\omega$ | $-$ |
| $\omega_{TT}$ | $-\left(\frac{f_\omega}{2M}\right)^2m_\omega^2\Theta_\omega$ | $-3\left(\frac{f_\omega}{2M}\right)^2m_\omega^2\Theta_\omega$ | $4\left(\frac{f_\omega}{2M}\right)^2\Psi_\omega$ | $-$ |
| $\omega_{VT}$ | $-$ | $-$ | $-$ | $12\frac{f_{\omega B}g_{\rho B}}{2M}\Gamma_\omega$ |
| $\rho_{VV}$ | $2g_{\rho B}^2\Theta_\rho$ | $-4g_{\rho B}^2\Phi_\rho$ | $-4g_{\rho B}^2\Phi_\rho$ | $-$ |
| $\rho_{TT}$ | $-\left(\frac{f_\rho}{2M}\right)^2m_\rho^2\Theta_\rho$ | $-3\left(\frac{f_\rho}{2M}\right)^2m_\rho^2\Theta_\rho$ | $4\left(\frac{f_\rho}{2M}\right)^2\Psi_\rho$ | $-$ |
| $\rho_{VT}$ | $-$ | $-$ | $-$ | $12\frac{f_{\rho B}g_{\rho B}}{2M}\Gamma_\rho$ |
| $\pi_{pv}$ | $-f_{\pi B}^2\Theta_\pi$ | $-f_{\pi B}^2\Theta_\pi$ | $2\left(\frac{f_{\pi B}}{m_\pi}\right)^2\Pi_\pi$ | $-$ |

with $\hat{k}$ the unit vector along the momentum $\vec{k}$ and $\Sigma_B^{s(0)i}$ the scalar part (time component) [space component] of the self-energy. Furthermore, the effective baryon mass, momentum and energy in matter are respectively defined by [11]

\[
M_B^*(k) = M_B + \Sigma_B^s(k),
\]

\[
k_B^{\mu} = (k_B^{s0}, k_B^s) = (k^0 + \Sigma_B^0(k), \vec{k} + \hat{k}\Sigma_B^s(k)),
\]

\[
E_B^*(k) = \left[\vec{k}_B^2 + M_B^2(k)\right]^{1/2}.
\]

The baryon self-energies in Eq. (10) are then calculated by [11]

\[
\Sigma_B^s(k) = -g_{\sigma B}(\vec{\sigma})\Theta_\sigma + \sum_{B',i} \frac{I_{BB'}^s}{(4\pi)^2k} \int_0^{k_{F_B}} dq q \left[ \frac{M_B^*(q)}{E_{B'}^*(q)}B_i(k,q) + \frac{q_{B'}^s}{2E_{B'}^*(q)}D_i(k,q) \right],
\]

\[
\Sigma_B^0(k) = -g_{\omega B}\vec{\omega} - g_{\rho B}(\vec{I}_{B})\vec{\rho} - \sum_{B',3} \frac{I_{BB'}^0}{(4\pi)^2k} \int_0^{k_{F_B}} dq q A_i(k,q),
\]

\[
\Sigma_B^\pi(k) = \sum_{B',i} \frac{I_{BB'}^\pi}{(4\pi)^2k} \int_0^{k_{F_B}} dq q \left[ \frac{q_{B'}^\pi}{E_{B'}^*(q)}C_i(k,q) + \frac{M_B^*(q)}{2E_{B'}^*(q)}D_i(k,q) \right],
\]

where $\vec{\omega}$ and $\vec{\rho}$ are respectively the mean-field values of $\omega$ and $\rho$ mesons in matter, $k_{F_B}$ is the Fermi momentum for baryon $B$ and the factor, $(I_{BB'}^i)^{1/2}$, is the isospin weight at the meson-$BB'$ vertex in the Fock diagram. The index $i$ in the sum and the functions $A_i$, $B_i$, $C_i$,
\[ C_1 \text{ and } D_1 \text{ in Eqs. (14)-(16) are explicitly given in Table I } \]

Table II in which the following functions are used \([11]\):

\[ \Theta_i(k, q) = \ln \left[ \frac{m_i^2 + (k + q)^2}{m_i^2 + (k - q)^2} \right], \]

(17)

\[ \Phi_i(k, q) = \frac{1}{4kq} (k^2 + q^2 + m_i^2) \Theta_i(k, q) - 1, \]

(18)

\[ \Psi_i(k, q) = \left[ \left( k^2 + q^2 - m_i^2 / 2 \right) \Phi_i(k, q) - kq \Theta_i(k, q) \right], \]

(19)

\[ \Pi_i(k, q) = \left[ \left( k^2 + q^2 \right) \Phi_i(k, q) - kq \Theta_i(k, q) \right], \]

(20)

\[ \Gamma_i(k, q) = [k \Theta_i(k, q) - 2q \Phi_i(k, q)]. \]

(21)

The mean-field values of \( \bar{\omega} \) and \( \bar{\rho} \) are respectively given by the usual forms

\[ \bar{\omega} = \sum B \frac{g_{\omega B}}{m^2_\omega} \rho_B, \quad \bar{\rho} = \sum B \frac{g_{\omega B} (I_B)_3}{m^2_\omega} \rho_B, \]

(22)

where the density of baryon \( B \) is \( \rho_B = \frac{(2J_B + 1)}{6\pi^2} k_{FB}^3 \) with \( J_B \) the spin of \( B \).

On the other hand, combining with Eqs. (14)-(16), the value of \( \bar{\sigma} \) is self-consistently calculated by \([8]\)

\[ \bar{\sigma} = \sum B \frac{g_{\sigma B} b_B C_B(\bar{\sigma}) \rho^s_B}{m^2_\sigma} - \frac{1}{m^2_\sigma} (g_2 \sigma^2 + g_3 \sigma^3), \]

(23)

where the scalar density of baryon \( B \) reads

\[ \rho^s_B = \frac{2J_B + 1}{2\pi^2} \int_0^{k_{FB}} dk \frac{k^2 M^*_B(k)}{E^*_B(k)}. \]

(24)

In Eq. (23), \( g_2 \) and \( g_3 \) vanish in the QMC or CQMC model, while, in QHD+NL, \( b_B C_B(\bar{\sigma}) \) is taken to be unity.

The total energy density (pressure) for matter can be divided into the baryon and lepton contributions, namely \( \epsilon = \epsilon_B + \epsilon_\ell \) \( (P = P_B + P_\ell) \), where the baryon energy density, \( \epsilon_B \), and pressure, \( P_B \), are expressed by

\[ \epsilon_B = \sum B \frac{2J_B + 1}{(2\pi)^3} \int_0^{k_{FB}} dk \left[ T_B(k) + \frac{1}{2} V_B(k) \right] - \frac{\sigma^3}{2} \left( \frac{g_2}{3} + \frac{g_3}{2} \sigma^2 \right), \]

(25)

with

\[ T_B(k) = \frac{M_B M^*_B(k) + kk^*_B}{E^*_B(k)}, \quad V_B(k) = \frac{M^*_B(k) \Sigma^*_B(k) + k^* \Sigma^*_B(k)}{E^*_B(k)} - \Sigma^*_B(k), \]

(26)

and

\[ P_B = n_B^2 \frac{\partial}{\partial n_B} \left( \frac{\epsilon_B}{n_B} \right). \]

(27)
TABLE III: Coupling constants and calculated properties of symmetric nuclear matter at $n_B^0$. In the left column, H (HF) stands for the Hartree (Hartree-Fock) calculation. The incompressibility, $K_v$, and the symmetry energy, $a_4$, are in MeV. The coupling constants, $g_2$ (in fm$^{-1}$) and $g_3$, in QHD+NL are chosen so as to adjust $K_v$ and $M_N^*$ to the values given by the QMC model.

| Model          | $g_{\sigma N}^2/4\pi$ | $g_{\omega N}^2/4\pi$ | $g_{\rho N}^2/4\pi$ | $g_2$   | $g_3$ | $K_v$  | $M_N^*/M_N$ | $a_4$ |
|----------------|------------------------|------------------------|----------------------|---------|-------|--------|-------------|-------|
| QHD+NL(H)      | 5.34                   | 5.41                   | 1.88                 | 11.07   | 95.59 | 280    | 0.80       | 36.9  |
| QMC(H)         | 5.45                   | 5.41                   | 1.88                 | −       | −     | 280    | 0.80       | 36.9  |
| CQMC(H)        | 5.75                   | 7.11                   | 1.82                 | −       | −     | 302    | 0.76       | 36.9  |
| QHD+NL(HF)     | 3.63                   | 6.66                   | 0.48                 | 16.27   | 48.52 | 280    | 0.73       | 38.6  |
| QMC(HF)        | 3.50                   | 6.41                   | 0.48                 | −       | −     | 280    | 0.73       | 36.9  |
| CQMC(HF)       | 3.59                   | 7.34                   | 0.48                 | −       | −     | 300    | 0.70       | 37.4  |

In Eq. (27), the total baryon density, $n_B$, is given by $n_B = \sum B \rho_B$.

The numerical result for the properties of symmetric nuclear matter is presented in Table III. In the present calculation, the $\sigma$-$N$ and $\omega$-$N$ coupling constants are determined so as to reproduce the saturation energy ($-15.7$ MeV) at normal nuclear density ($n_B^0 = 0.15$ fm$^{-3}$).

In the Hartree calculation, the $\rho$-$N$ coupling constant, $g_{\rho N}$, is determined so as to fit the symmetry energy, $a_4 = 36.9$ MeV [4, 5, 18], and the meson-hyperon coupling constants, $g_{\sigma Y}$, $g_{\omega Y}$ and $g_{\rho Y}$, are taken to be the values derived from the quark model [3, 4].

In the Hartree-Fock calculation, we use the more reliable set of the coupling constants (except $g_{\sigma B}$ and $g_{\omega N}$) determined in the Nijmegen extended-soft-core (ESC) model (see Table VII in Ref. [16]). Furthermore, from the recent analyses of hypernuclei and hyperon production reactions, it is inferred that the $\Lambda (\Sigma) [\Xi]$ feels the potential, $U_{\Lambda (\Sigma) [\Xi]} \simeq -30 (+30) [-15]$ MeV, in nuclear matter [3, 14]. Therefore, we adjust the coupling constants, $g_{\sigma \Lambda}$, $g_{\sigma \Sigma}$ and $g_{\sigma \Xi}$, so as to reproduce the suggested potential values at $n_B^0$. In the case of QHD+NL (QMC) [CQMC], we take $g_{\sigma \Lambda}/\sqrt{4\pi} = 2.88 (2.78) [2.44]$, $g_{\sigma \Sigma}/\sqrt{4\pi} = 2.05 (1.97) [1.94]$ and $g_{\sigma \Xi}/\sqrt{4\pi} = 2.06 (1.98) [1.70]$.

In Table IV, the contents of the nucleon self-energies in the QMC model are presented. The Fock term contributes to the self-energy significantly. In symmetric nuclear matter, the effect of the tensor coupling of $\omega$ meson is small, while that of the $\rho$ meson is considerable;
TABLE IV: Nucleon self-energies, $\Sigma^{s,0,v}_N$, at $n_B^0$ in symmetric nuclear matter. The values of the self-energy are in MeV.

|         | $\Sigma^s_N$ | $\Sigma^0_N$ | $\Sigma^v_N$ |
|---------|--------------|--------------|--------------|
| Hartree | -186         | -128         | 0            |
| Hartree-Fock |
| Direct  | -131         | -151         | 0            |
| Exchange |              |              |              |
| $\sigma$ | 13           | -14          | 0            |
| $\omega$ | -63          | -32          | -3           |
| $\pi$    | -4           | 4            | -4           |
| $\rho$   | -69          | 13           | 14           |
| total    | -255         | -180         | 6            |

FIG. 1: Nucleon self-energies, $\Sigma^{s,0,v}_N$, in symmetric nuclear matter.

for example, the $\rho$-meson contributions of the vector ($VV$), tensor ($TT$) and vector-tensor ($VT$) mixing to the scalar part, $\Sigma^s_N$, are respectively $-14$ MeV, $-58$ MeV and 4 MeV. The space component, $\Sigma^v_N$, at $n_B^0$ is relatively small.

In Fig. 1 we show the nucleon self-energies calculated by the QMC model as functions of the total baryon density, $n_B$. The scalar and time components, $\Sigma^{s,0}_N$, in the Hartree-Fock
TABLE V: Neutron-star radius, $R_{\text{max}}$ (in km), the central density, $n_c$ (in fm$^{-3}$), and the ratio of the maximum neutron-star mass to the solar mass, $M_{\text{max}}/M_\odot$. The Hartree and the Hartree-Fock calculation with (without) hyperons are denoted by npY (np).

|                | np  | npY    |
|----------------|-----|--------|
|                | $R_{\text{max}}$ | $n_c$ | $M_{\text{max}}/M_\odot$ | $R_{\text{max}}$ | $n_c$ | $M_{\text{max}}/M_\odot$ |
| QHD+NL(H)      | 11.3 | 1.04   | 2.00       | 12.5  | 0.86   | 1.56       |
| QMC(H)         | 11.5 | 1.01   | 2.05       | 12.5  | 0.86   | 1.60       |
| CQMC(H)        | 11.8 | 0.92   | 2.20       | 12.5  | 0.88   | 1.66       |
| QHD+NL(HF)     | 11.7 | 0.95   | 2.15       | 11.9  | 0.95   | 1.92       |
| QMC(HF)        | 11.5 | 0.97   | 2.11       | 12.0  | 0.92   | 1.95       |
| CQMC(HF)       | 11.9 | 0.90   | 2.23       | 12.3  | 0.87   | 2.02       |

calculation are much deeper than those in the Hartree calculation. It is noticeable that the space component also becomes deep at high densities and thus it is not negligible in dense matter.

In a neutron star, the charge neutrality and the $\beta$ equilibrium under weak processes are realized. Under these conditions, we calculate the EOS for neutron matter and solve
FIG. 3: Neutron-star mass as a function of the radius. The left (right) panel is for the Hartree (Hartree-Fock) calculation. In solving the TOV equation, we use the EOS of BBP [20] and BPS [21] at very low densities.

the Tolman-Oppenheimer-Volkoff (TOV) equation. In Fig. 2 we show the QMC result of particle fractions in relativistic Hartree-Fock approximation. With respect to hyperons, only the $\Xi^-$ appears around $0.49 \text{ fm}^{-3}$ and the other hyperons are not produced at densities below $1.2 \text{ fm}^{-3}$. We note that, in the case of QHD+NL, the $\Xi^-$ first appears around $0.43 \text{ fm}^{-3}$, and that the $\Lambda$ and $\Xi^0$ are produced at densities beyond $0.69 \text{ fm}^{-3}$. This tendency is similar to the result of Ref. [9]. It may be interesting to compare the present result with the Hartree result given in Ref. [19].

We summarize the properties of neutron star in Table V and show the mass as a function of the neutron-star radius in Fig. 3. As known well, the inclusion of hyperons generally reduces the mass of a neutron star. However, because the Fock contribution makes the EOS hard, the maximum mass in the present calculation can reach the recently observed value, $1.97 \pm 0.04 M_\odot$. If we ignore the tensor coupling in the Fock term, the difference between the maximum masses in the Hartree and the Hartree-Fock calculations is not large. Therefore, the tensor coupling (especially, in the high density region) is very vital to obtain the large neutron-star mass. The variation of the quark substructure of baryon in matter also enhances the mass, because the QMC model includes the (repulsive) many-body interaction given...
through the scalar polarizability in the coupling constant, $g_{\sigma B}(\bar{\sigma})$ [14, 22]. Furthermore, the quark-quark hyperfine interaction due to the gluon and pion exchanges increases the mass of a neutron star. We should note that the inclusion of the meson-baryon form factor at the interaction vertex in the Fock term does not change the present result much.

In summary, we have studied the effects of the Fock term, the tensor couplings of vector mesons and the baryon structure variation on the properties of a neutron star. The present calculation can produce the maximum neutron-star mass of $\sim 2.0M_\odot$, which is consistent with the recently observed mass, $1.97 \pm 0.04M_\odot$. The Fock contribution is very important and, particularly, the inclusion of tensor coupling is necessary to obtain such large mass. The in-medium variation of baryon structure also makes the EOS hard and thus it enhances the mass of a neutron star. In the future, it may be desirable to consider the degrees of freedom of $\Delta$ isobar [1, 8], the $K$-meson exchange and the baryon mixing in the Fock diagram. It is also interesting to study the possibility of meson condensates [1, 2, 6] and/or quark matter [1].

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