Prediction of vitrinite reflectance values using machine learning techniques: a new approach

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Abstract
Vitrinite reflectance (VR) is considered the most used maturity indicator of source rocks. Although vitrinite reflectance is an acceptable parameter for maturity and is widely used, it is sometimes difficult to measure. Furthermore, Rock-Eval pyrolysis is a current technique for geochemical investigations and evaluating source rock by their quality and quantity of organic matter, which provide low cost, quick, and valid information. Predicting vitrinite reflectance by using a quick and straightforward method like Rock-Eval pyrolysis results in determining accurate and reliable values of VR with consuming low cost and time. Previous studies used empirical equations for vitrinite reflectance prediction by the $T_{\text{max}}$ data, which was accompanied by poor results. Therefore, finding a way for precise vitrinite reflectance prediction by Rock-Eval data seems useful. For this aim, vitrinite reflectance values are predicted by 15 distinct machine learning models of the decision tree, random forest, support vector machine, group method of data handling, radial basis function, multilayer perceptron, adaptive neuro-fuzzy inference system, and multilayer perceptron and adaptive neuro-fuzzy inference system, which are coupled with evolutionary optimization methods such as grasshopper optimization algorithm, bat algorithm, particle swarm optimization, and genetic algorithm, with four inputs of Rock-Eval pyrolysis parameters of $T_{\text{max}}$, $S_1$/TOC, HI, and depth for the first time. Statistical evaluations indicate that the decision tree is the most precise model for VR prediction, which can estimate vitrinite reflectance precisely. The comparison between the decision tree and previous proposed empirical equations indicates that the machine learning method performs much more accurately.

Keywords Vitrinite reflectance · Rock-eval pyrolysis · Maturity · Depth · Decision tree

Introduction

Rock-Eval pyrolysis is considered one of the most powerful and influential geochemical techniques which can provide valuable information about organic matter sediments promptly (Espitalié et al. 1977; Behar et al. 2001). This technique is also used extensively in petroleum source rock evaluation through the determination of organic matter types, generation potential, and level of maturity (Dembicki 2016). $S_1$ (formerly generated hydrocarbon), $S_2$ (remain potential of hydrocarbon generation), TOC (total organic carbon), $T_{\text{max}}$ (temperature of $S_2$ maximum), HI (hydrogen index), and OI (oxygen index) are some parameters which are obtained by Rock-Eval pyrolysis. Despite all Rock-Eval advantages, this method is associated with some obstacles for maturity interpretations as well as the determination of organic matter type (Katz 1983). $T_{\text{max}}$ is a parameter which varies with depth and is used for thermal maturity determination (Espitalié et al. 1977). Changing of Rock-Eval apparatus condition, the matrix of analyzed sample, and heavy components of bitumen are factors which influence on $T_{\text{max}}$ determination. As a consequence, this parameter can sometimes result in inverted and fallacious conclusions toward the actual level of maturity (Espitalié 1986). Furthermore, in situations in which the $S_2$ peak has more than one maximum, or suffers weak intensity, $T_{\text{max}}$ determination will be complicated (Peters 1986). It should also be noted that maturity determination through the $T_{\text{max}}$ parameter is changed by some other factors such as bitumen or kerogen in adjacent units (Snowdon 1995). Therefore, $T_{\text{max}}$ can’t be considered as a dependable indicator for thermal maturity interpretation. In the cases that the $T_{\text{max}}$ is affected by the facies effects,
vitrinite reflectance can provide more reliable results (Peters and Cassa 1994).

In addition to the Rock-Eval parameters, time alteration index (TAI), conodont alteration index (CAI), and vitrinite reflectance (VR) are considered as other maturity indicators. TAI is defined based on color variations of kerogen. The color range of spore and pollen from yellow to black (immature to mature) is then converted to a numerical scale. Since spore and pollen belong to terrigenous plants that are absent before the middle Paleozoic, this parameter has some problems (Staplin 1961). Also, CAI is defined similarly. The color of conodonts is studied by binocular microscopes. These types of fossils are found in carbonate rocks so this index is improper for maturity assessment of shale rocks. Moreover, CAI cannot be used in cases earlier than Jurassic (Epstein et al. 1976). Zooclast and solid bitumen reflectivities are 2 other known petrographic methods for this aim. It should be noted that these methods are not free of problems. The identification of the correct Zooclast is always difficult. Also, different sources cause this problem in solid bitumen assessment (Bertrand 1990; Cole 1994; Petersen et al. 2013; Curiale 1986).

Vitrinite particle as a diagenetic product of higher plant remnants is one of the most significant macerals of petroleum source rock that can be found dispersed in other clastic sedimentary rocks and majorly in coals (Suggate 1959; Taylor et al. 1998). The light reflection phenomenon from a polished vitrinite surface is known as vitrinite reflectance (Mukhopadhyay 1994). Vitrinite reflectance (Ro%) is sensitive to temperature variations. In 1982, for the first time, it was discovered that vitrinite reflectance increases with time and temperature (Teichmüller and Teichmüller 1982). Thus, vitrinite reflectance varies based on maturity and is assumed to be the traditional and most robust diagnostic tool for maturity investigation, which can be applicable in a wide range of maturity levels (Mählmann and Le Bayon 2016). Data of this parameter can be applied for source rock evaluation or coal rank assessment (Kadkhodaie and Rezaee 2017; Jiang et al. 2019).

Vitrinite reflectance (VR) is the most applied factor for maturity determination (Cheshire et al. 2017; Peters et al. 2018). In addition to geological evaluation of petroleum source rocks as well as the coal rank assessment, VR possesses a significant role in basin modeling. Vitrinite reflectance data are the most known calibration parameters in the modeling procedure. Kinetic maturation of source rocks modeling also requires maturation data (Mukhopadhyay 1994). Vitrinite reflectance data are commonly used in three forms of empirical, single reaction kinetic, and parallel reactions kinetic (Barker and Elders 1981; Waples 1984; Welte and Yalcin 1988; Sweeney and Burnham 1990). The VR values of hydrocarbon generation in different types of kerogen can be helpful for source rock potential evaluation. For instance, type II-S kerogen starts generating earlier than other types (Dembicki 2009). Moreover, the method of EASY %Ro as the most famous and reputable concept of maturation in basin modeling considers a defined range for activation energy distribution (Sweeney and Burnham 1990) and tectonic history determination (Middleton 1982) and seeking hidden pluton in sedimentary rocks (Chen et al. 2017).

According to the aforementioned issue, finding a way to relate \( T_{\text{max}} \) to vitrinite reflectance can cover deficits of imperfect maturity interpretations based on the \( T_{\text{max}} \) parameter and results in more precise outcomes. In other words, there are several associated problems with measuring vitrinite reflectance such as time-consuming, lack of vitrinite particles in some cases, and the anisotropy of vitrinite (Wust et al. 2013; Dembicki 2016). Also, the vitrinite maceral belongs to after Devonian plants, and samples that are older than this time don’t have any vitrinite. In addition to problems with the age of source rock samples, low amounts of incoming plants result in low quantities of vitrinite values (Peters and Cassa 1994), and oxidation of this maceral also results in high values (Liu et al. 2020). In other words, two maturity indicators of VR and \( T_{\text{max}} \) have some problems, but the shortcoming of the first one is in measuring and the second one in the final result. Therefore, finding a way of predicting vitrinite reflectance through the simple procedure of Rock-Eval pyrolysis can be considered as a novel and efficient method that can dispel the problem of VR measuring by using several Rock-Eval parameters. Because of challenges in VR determination, finding a way for maturity estimation had been an interesting subject for researchers. Some of them have studied the relationship between \( T_{\text{max}} \) and VR parameters and proposed equations that can calculate vitrinite reflectance based on \( T_{\text{max}} \) data (Galimov and Rabbani 2001; Jarvie et al. 2001; Wust et al. 2013; Peters 1986; Jarvie 2012). It must be emphasized that all these equations suffer from some deficits, such as a low coefficient of determination or incorrect predictions in some cases. Also, these types of VR calculations are simple correlations just on the basis of one parameter (\( T_{\text{max}} \)), and this issue increases uncertainties. Some efforts have been made to determine vitrinite reflectance values by spectroscopic techniques which are also based on equations (Cheshmeh Sefidi and Ajorkaran 2019; Wilkins et al. 2015, 2018; Kibria et al. 2020). Moreover, Lupoi et al. (2019) and Hou et al. (2020) used the partial least squares model by Raman spectra of shale samples and modified the EASY% Ro model for vitrinite reflectance prediction, respectively.

The main objective of this paper is the precise prediction of vitrinite reflectance based on Rock-Eval parameters, not just \( T_{\text{max}} \) data or equation-based methods. Contrary to limited previous researches that have merely used the \( T_{\text{max}} \) parameter for vitrinite reflectance predictions or some simple
equations, this paper, for the first time, uses machine learning methods by using depth, $T_{\text{max}}$, $S_1$/TOC, and HI. Also, using machine learning for determining vitrinite reflectance values has been unprecedented. Previous researches for predicting geochemical parameters using machine learning methods were done to predict rock eval data such as TOC (Khoshnoodkia et al. 2011; Shalaby et al. 2019; Ge et al. 2015), $S_1$, and $S_2$ (Johnson et al. 2018; Wang et al. 2019). None of the earlier studies were about vitrinite reflectance prediction. Also, all machine learning methods in this article are assessed, which is unprecedented.

Artificial intelligence methods can learn the pattern of data and use multiple inputs, but previous attempts were merely based on one input without any learning (just simple regression). Also, this paper applies not only one way but also 15 distinct methods for this purpose. Moreover, the results of these methods are compared to finding the most proper model. The final result of the best machine learning method is then compared with the previously presented equations. The depth, $T_{\text{max}}$, $S_1$/TOC, and HI parameters are applied as inputs of constructed models by 15 machine learning methods of decision tree (DT), random forest (RF), support vector machine (SVM), group method of data handling (GMDH), radial basis function (RBF), multilayer perceptron (MLP), multilayer perceptron couple with grasshopper optimization algorithm (MLP + GOA), bat algorithm (MLP + BAT), particle swarm optimization algorithm (MLP + PSO), and genetic algorithm (MLP + GA) as well as adaptive neuro-fuzzy inference system (ANFIS), ANFIS + GOA, ANFIS + BAT, ANFIS + PSO and ANFIS + GA for VR determination. Then, the accuracy of all methods was compared through four statistical parameters of average absolute relative deviation (AARD), coefficient of determination (R2), root mean square error (RMSE), and standard deviation (SD). Eventually, the most accurate model was selected. The final results of this paper were then compared with the results of previous efforts. A schematic form of the methodology of this paper is shown in Fig. 1.

### Materials and methods

#### Data gathering and preparation

As mentioned in this paper, the required data for predicting VR are depth, $T_{\text{max}}$, $S_1$/TOC, and HI. To that end, 54 data sets of these aforementioned data are extracted from a broad area of the Persian Gulf as can be seen in Fig. 2. The Persian Gulf, as the most significant foreland basin
of hydrocarbon resources in the world, is located at the confluence of Arabian and Eurasian plates. This contains more than two-thirds of the proven oil reserves of the world (Rabbani 2007; Haghi et al. 2013). Pabdeh (Paleocene), Gurpi (Campanian–Paleocene), Ahmadi member of Sarvak (Cenomanian), and Kazhdumi (Albian) are considered as the most probable source rocks of the Middle Cretaceous–Early Miocene petroleum system of the studied area (Mashhadi et al. 2015). These formations are illustrated in Fig. 3 in the form of a simple stratigraphic column. Pabdeh Formation consists mainly of shale, argillaceous limestone, and marls, which overlies Gurpi Formation. Gurpi is another probable source rock of this area that can also act as cap rock of lower reserves and includes marl and marly limestone. Ahmadi Member contains shaly facies, especially in northern parts of the Persian Gulf, and can be considered as one of the probable intervals for hydrocarbon generation. Eventually, Kazhdumi, as the most crucial source layer, generally consists of calcareous shale as well as dark bituminous limestone (Ghazban 2009; Homke et al. 2009; Soleimani et al. 2013).

After selecting proper and complete data, 54 Rock-Eval pyrolysis data (depth, \( T_{\text{max}} \), \( S_1/\text{TOC} \), and HI) belong to ten oil fields in the Iranian sector of the Persian Gulf (Fig. 2) were extracted (Mashhadi et al. 2015). Minimum, maximum, and average values of selected data are summarized in Table 1. Twenty-one samples belong to Pabdeh Formation, whereas contributions of Gurpi Formation, Ahmadi member, and Kazhdumi Formation are 6, 4, and 23 samples, respectively. In this paper, data of depth, \( T_{\text{max}} \), \( S_1/\text{TOC} \), and HI are considered as inputs of constructed models, and VR is the output. Data normalizing, which improves the performance of constructed models, has been done through the below equation:

\[
n_{z_i} = 2 \times \frac{z_i - z_{\text{min}}}{z_{\text{max}} - z_{\text{min}}} - 1,
\]

where \( n_{z_i} \) refers to the normalized value, \( i \) is the number of parameters, \( z_{\text{min}} \) is the minimum value of \( z \) series, and \( z_{\text{max}} \) refers to the maximum value of them.

**Table 1** Minimum, maximum, and average values of selected inputs and output data

| Parameter | Minimum | Maximum | Average |
|-----------|---------|---------|---------|
| \( X_1 \) Depth (m) | 1159 | 3603 | 2290.16 |
| \( X_2 \) \( T_{\text{max}} \) (°C) | 410 | 464 | 430.51 |
| \( X_3 \) \( S_1/\text{TOC} \) | 0.07 | 1.26 | 0.48 |
| \( X_4 \) HI | 84 | 786 | 237.74 |
| Y Ro (%) | 0.35 | 0.82 | 0.57 |

**Machine learning systems methodology**

Machine learning methods are currently excessively used in various fields of science and industry. They are straightforward and flexible tools for accurate prediction. Also, they don’t consume so much time for modeling (Lary et al. 2015; Mohaghegh 2017; Al-Fatlawi 2018). These aforementioned factors result in their complete application, especially in oil industries (Anifowose et al. 2017; Kahani et al. 2018; Sabah et al. 2019; Ghaffarkhah et al. 2019; Amin et al. 2019; Cheshmeh Sefidi and Ajorkaran 2019; Esfandiarian et al. 2019). Despite abundant researches based on soft computing methods, no studies have been done in VR prediction through Rock-Eval data, and this article is considered as the first attempt for this purpose which applies 15 distinct intelligent methods of decision tree (DT), support vector machine (SVM), group method of data handling (GMDH), radial basis function (RBF), random forest (RF), multilayer perceptron (MLP), as well as MLP + GOA, MLP + BAT, MLP + PSO, and MLP + GA as well as adaptive neuro-fuzzy inference system (ANFIS), ANFIS + GOA, ANFIS + BAT, ANFIS + PSO, and ANFIS + GA.

Decision tree as supervised learning with a technique of classification and regression tree or CART consists of branches and nodes in a graphical form that is considered as a predictive model in data mining (JiaWei and Micheline 2001; Taylor 2019). The flowchart of the decision tree is illustrated in Fig. 4.

The support vector machine is one of the artificial neural network branches that can be applied for regression and classification purposes through a theory of statistical learning. This approach is also considered as an efficient tool in machine learning as well as data mining (Vapnik 2013; Abbas et al. 2019). In this paper, the kernel function and
A simple schematic form of SVM is shown in Fig. 5.

Group method of data handling as one of the other applied approaches is a robust connecting algorithm between inputs and outputs, which is proper for settling down nonlinear situations as a self-organized system (Hwang 2006; Loni et al. 2018). Detail information on GMDH belongs to this study, and the flowchart is presented in Table 2 and Fig. 6, respectively.

Radial basis functions are types of artificial neural networks with a structure that employs RBF instead of prevalent activation functions (Amedi et al. 2016). The properties of the operated RBF network are summarized in Table 3.

Moreover, the simplified structure of the RBF network for prediction vitrinite reflectance values as well as its flowchart is illustrated in Figs. 7 and 8, respectively.

One of the significant statistical methods is the random forest, which operates based on the variance concept and can be applied for prediction and sensitivity analysis goals. Moreover, the great advantage of a random forest statistical learning tool is its rapidity (Bosch et al. 2007; Genuer et al. 2010; Aulia et al. 2019). The flowchart of this method is shown in Fig. 9.

Feedforward networks of multilayer perceptions are well-known artificial neural networks with at least three main layers in their structure. In this paper, the MLP network with...
2 hidden layers was selected. As is evident, the efficiency of these types of networks depends on the number of neurons in each layer. To that end, several MLP networks with different numbers of neurons were constructed, and then their performances were analyzed by mean square error. This procedure is illustrated in Fig. 10. As shown, the structure with three neurons in the first hidden layer and four neurons in the second hidden layer can be considered as the best situation. Since determining the optimum values of MLP parameters requires several calculations, which takes a lot of time, for increasing efficiency, other parameters are derived from the previous study (Sabah et al. 2019a). Also, the MLP flowchart is presented in Fig. 11. The characteristics of the used MLP network with two hidden layers are presented in Table 4.

The smart hybrid system of ANFIS is the conflation of fuzzy logic and artificial neural network, and this feature makes ANFIS an effective tool and powerful strategy with high accuracy and less time for goals of systems recognition, time series prediction, function approximation, simulation of nonlinear systems, etc. (Jang 1993; Mir et al. 2018). Additional information on ANFIS parameters is listed in Table 5. It must be noted that ANFIS parameters have been determined through previous research (Sabah et al. 2019a) and trial and error approach. Furthermore, the algorithm and the flowchart’s architecture are shown in Figs. 12 and 13, respectively.

In addition to the aforementioned methods and to improve the precision of VR prediction, GOA, BAT, GA, and PSO algorithms were used for training MLP neural networks and coupled with ANFIS. Their flowcharts are illustrated in Figs. 14, 15, 16, and 17, respectively. As the name of the grasshopper optimization algorithm implies, this algorithm is derived from the cumulative life of grasshopper in nature. The location of grasshoppers among their swarm can represent a solution for the current issue. Saremi et al. (2017) were the first one who proposed its algorithm relationships, which simulate grasshopper motions. Optimum GOA parameters had been determined by both previous
research (Ghaffarkhah et al. 2020) and the trial and error approach. BAT is another algorithm that is inspired by nature. Yang (2010) proposed this optimization algorithm based on bats features for finding bait or way by sending audio pulses. It must be emphasized that this algorithm is quite capable of solving complicated problems (Yang 2010, 2012; Yang and Hossein Gandomi 2012). A particle swarm optimization algorithm as an appropriate tool for searching in a multidimensional space is extremely applied as an optimizer (Atashnezhad et al. 2014). Also, the genetic algorithm is a proper technique for stochastic searching that can find the optimum value of the function by its various processes (Joshi et al. 2006). The control parameters of these four algorithms are completely presented in Table 6.

### Results and discussion

As mentioned before, four input values (depth, $T_{\text{max}}$, $S_I$/TOC, and HI) were used for constructing models to predict vitrinite reflectance values. Pair plot of inputs and output, which provides an appropriate insight into the relationship between all implemented inputs and output values, is illustrated in Fig. 18. This plot reveals that there is a positive correlation between vitrinite reflectance and applied inputs. Moreover, it can be comprehended that VR values are strongly dependent on depth and $T_{\text{max}}$.

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**Table 3** Properties of RBF network

| Network type          | Radial basis network |
|-----------------------|----------------------|
| Training function code| newrb                |
| Max neuron number     | 10                   |
| Performance function  | MSE                  |
| Spread                | 1                    |
| Goal                  | 0                    |
Fig. 7  Schematic form of RBF network structure

Fig. 8  Schematic of RBF workflow
Fig. 9  Schematic of RF workflow

Fig. 10  Values of MSE for various numbers of neurons in hidden layers of MLP network
Table 4  Architecture parameters of MLP network

| Network type       | Multilayer perceptron |
|--------------------|-----------------------|
| Training function  | Levenberg–Marquardt backpropagation |
| Number of layers   | 3                     |
| Nodes in 1st hidden layer | 3                 |
| Transfer function of 1st hidden layer | TANSIG |
| Nodes in 2nd hidden layer | 4                 |
| Transfer function of 2nd hidden layer | TANSIG |
| Neurons in output layer | 1                  |
| Transfer function of output layer | PURELIN |
| Performance objective function | MSE |

Table 5  Values of ANFIS parameters

| ANFIS Parameters         | Value |
|--------------------------|-------|
| Number of MFs            | 5     |
| Radius of influence      | 0.5   |
| Squash factor            | 0.5   |
| Accept ratio             | 0.15  |
| And method               | Prod  |
| Or method                | Probor|
| Implication              | Min   |
| Aggregation              | Max   |
| Defuzzification          | Wtaver|

Fig. 11  Schematic of MLP workflow

Fig. 12  Simplified structure of the ANFIS algorithm
As a general procedure, constructed models by different aforementioned methods must be compared. To that end, statistical parameters are considered as appropriate tools for appraising the performance of defined models. In this paper, four parameters of average absolute relative deviation (AARD), coefficient of determination ($R^2$), root mean square error (RMSE), and standard deviation ($SD$) have been employed for a complete comparison of 15 distinct developed models and selection of the most precise methods for vitrinite reflectance prediction. Equations of these statistical parameters are expressed as follows:

$$AARD = \frac{1}{N} \sum_{i=1}^{N} \left| \frac{O_{\text{exp}} - O_{\text{pred}}}{O_{\text{exp}}} \right| \times 100$$

$$R^2 = 1 - \frac{\sum_{i=1}^{N} \left( O_{\text{exp}} - O_{\text{pred}} \right)^2}{\sum_{i=1}^{N} \left( O_{\text{exp}} - O_{\text{exp}} \right)^2}$$  \hspace{1cm} (3)$$

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left( O_{\text{exp}} - O_{\text{pred}} \right)^2}$$  \hspace{1cm} (4)$$

$$SD = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} \left( \frac{O_{\text{exp}} - O_{\text{pred}}}{O_{\text{exp}}} \right)^2}.$$  \hspace{1cm} (5)$$

Four above indicators are calculated for all implemented models, and graphical results for three categories of train data, test data, and total data are illustrated in Figs. 19, 20,
Figure 19 shows the AARD values of all applied models. As seen, the lowest amount of AARD belongs to the DT model in train and total sets of data, whereas the MLP possesses the lowest AARD in test data. In test data, after MLP, the lowest value belongs to the DT model. The next figure illustrates the $R^2$ values of the three sets of data. As shown, the highest amount of $R^2$ is for the decision tree model in all 3 groups of the train, test, and total data (Fig. 20). The variation of RMSE values is shown in Fig. 21. The DT model has the lowest amounts of RMSE. Also, Fig. 22 shows the DT model has the lowest SD values. For better understanding, all these aforementioned data are summarized in Table 7. As can be seen, almost all models are acting correctly, and the prediction of vitrinite reflectance has been made with high accuracy. However, with a little more precision, it can be realized that among all methods, the decision tree has the best performance, and hence, diagrams of this method merely are presented in the following. The constructed tree for vitrinite reflectance prediction associated with statistical information is shown in Fig. 23. DTs split predictors and form subgroups of separate observations. This process is binary recursive partitioning that divides parent nodes into child nodes (binary splitting). This process is continued to reach terminal nodes that do not have any splitting (Singh 2017). Figure 23 shows the best tree for predicting vitrinite reflectance after running the decision tree model. As illustrated, this tree consists of nodes and leaves.
This tree takes the inputs and gives vitrinite reflectance values in leaves. The first input is $T_{\text{max}}$. If the $T_{\text{max}}$ value is less than 432.5 °C, the tree chooses the left side to continue the route, and if $T_{\text{max}}$ is more than this amount, the right path will be selected. In the next steps, depth, $T_{\text{max}}$, and S1/TOC are determinant factors to continue. Final results of predicted vitrinite reflectance values are presented in the leaves of the tree.

Furthermore, the relative deviation plot of the decision tree method is depicted in Fig. 24. This figure indicates that there is a small deviation between experimental data of vitrinite reflectance and predicted values by the DT method. Obviously, this slight difference suggests the accuracy of this method. To provide a complete sense of the precision of the decision tree model for vitrinite reflectance prediction, the plot of experimental and predicted data is presented in Fig. 25. As it is obvious, DT has been able to predict Ro values with high accuracy, and measured and predicted data are close to each other. The correlation of experimental and predicted data for both train and test data is illustrated in Fig. 26. This figure depicts the DT method as very precise in training data and the test dataset.

In the next step, the achievement of this paper should be compared with previous experimental equations. As mentioned, four equations had been presented for vitrinite reflectance prediction based on $T_{\text{max}}$ data. These formulas are as follows:

$$R_o = (1/30)T_{\text{max}} - 13.5 \quad \text{(Galimov and Rabbani 2001)} \quad (6)$$

$$R_o = (0.0180)T_{\text{max}} - 7.16 \quad \text{(Jarvie et al. 2001)} \quad (7)$$

$$R_o = (0.0085)T_{\text{max}} - 2.7914 \quad \text{(Wust et al. 2013)} \quad (8)$$

$$R_o = (0.0149)T_{\text{max}} - 5.8593 \quad \text{(Wust et al. 2013).} \quad (9)$$

### Table 6 Parameters of GOA, BAT, GA, and PSO

| Method | GOA | BAT | GA | PSO |
|--------|-----|-----|----|-----|
| GOA property | | | | |
| Population size | 50 | | | |
| Max iteration | 100 | | | |
| BAT property | | | | |
| Swarm size | 50 | | | |
| Max generation | 100 | | | |
| Loudness | 0.5 | | | |
| Pulse rate | 0.5 | | | |
| GA property | | | | |
| Population size | 150 | | | |
| Max generation | 100 | | | |
| Selection mode | Tournament | | | |
| Recommendation percent | 40 | | | |
| Crossover percent | 50 | | | |
| Mutation percent | 10 | | | |
| PSO property | | | | |
| Swarm size | 150 | | | |
| Max iteration | 100 | | | |
| Cognition coefficient | 2 | | | |
| Social coefficient | 2 | | | |

![Fig. 17 Schematic of PSO workflow](image)
To better understand the performance of methods based on experimental equations and artificial intelligence methods, the vitrinite reflectance values have been calculated by Eqs. 6–9 based on this paper’s presented $T_{\text{max}}$ data. The statistical parameters (AARD, $R^2$, RMSE, SD) are computed for these experimental equations and summarized in Table 8. For better understanding, the statistical parameters of the decision tree are also listed in this table. As seen, the DT method with the lowest amounts of AARD, RMSE, SD, and the highest value of $R^2$ is the most...
precise method for vitrinite reflectance prediction. The results of Table 8 show the poor performance of experimental equations. These results indicate the high accuracy of machine learning approaches compared to experimental methods. The variations of predicted vitrinite reflectance quantities by empirical equations and the decision tree approach (as the most precise machine learning method) with depth are illustrated in Fig. 27. Empirical equations perform weakly for vitrinite reflectance prediction.
Conclusions

Vitrinite reflectance values have been predicted by using machine learning approaches for the first time in this paper. For this purpose, several Rock-Eval parameters were used to construct machine learning models. For this purpose, in addition to depth, \(T_{\text{max}}\), \(S_1/\text{TOC}\), and HI values were selected for vitrinite reflectance prediction. Decision tree (DT), support vector machine (SVM), group method of data handling (GMDH), radial basis function (RBF), random forest (RF), multilayer perceptron (MLP), MLP + GOA, MLP + BAT, MLP + PSO and MLP + GA, adaptive neuro-fuzzy inference system (ANFIS), ANFIS + GOA, ANFIS + BAT, ANFIS + PSO, and ANFIS + GA.
and ANFIS + GA are 15 implemented methods for vitrinite reflectance prediction. After normalizing data, constructed models were compared via four statistical parameters of average absolute relative deviation (AARD), coefficient of determination ($R^2$), root mean square error (RMSE), and standard deviation (SD). Results of the comparison indicate that all methods are precise, and their outputs are

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**Fig. 23** An implemented tree for vitrinite reflectance prediction. Statistical information and vitrinite reflectance values are shown in blue rectangles and orange ellipsoids, respectively

**Fig. 24** Relative deviation plot of the decision tree model

**Fig. 25** Experimental data of vitrinite reflectance and prediction values by DT
acceptable, whereas the decision tree can be considered as the most accurate method, which possesses the lowest relative deviation between measured and predicted vitrinite reflectance values. A comparison between the decision tree and previously proposed equations for vitrinite reflectance prediction indicates that the machine learning approach performs more accurately than empirical equations.

Fig. 26 Predicted values of Ro by DT versus experimental values for both train and test datasets

Fig. 27 The variation of vitrinite reflectance quantities with depth for decision tree and 4 empirical equations. Note that 1st eqn and 2nd eqn are Eqs. 8 and 9, respectively

Table 8 The calculated statistical parameters for DT method and empirical equations of 6–9

|          | DT      | Equation 6 | Equation 7 | Equation 8 | Equation 9 |
|----------|---------|------------|------------|------------|------------|
| AARD     | 3.683   | 50.014     | 13.307     | 53.535     | 12.482     |
| $R^2$    | 0.933   | −10.757    | −0.102     | −7.420     | 0.199      |
| RMSE     | 0.027   | 0.353      | 0.108      | 0.298      | 0.092      |
| SD       | 0.052   | 0.585      | 0.196      | 0.587      | 0.170      |
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