Desalination of Agricultural Wastewater by Solar Adsorption System: A Numerical Study

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Abstract. There are still areas around the world suffer from severe shortage of freshwater supplies. Desalination technologies are not widely used due to their high energy usage, cost, and environmental damaging effects. In this study, a mathematical model of single-bed adsorption desalination system using silica gel-water as working pair is developed and validated via earlier experiments. A very good match between the model predictions and the experimental results is recorded. The objective is to reveal the factors affecting the productivity of fresh water and cooling effect in the solar adsorption system. The proposed model is setup for solving within the commercially-available software (Engineering Equation Solver). It is implemented to solve the mass and heat balance equations for the adsorbent bed, condenser and evaporator components. At a typical temperature of 89 °C and flow rate of 30 m³/sec for the hot water entering the bed, the following results are reported: (a) the specific daily water production of 1.89 m³/ton of silica gel/day, (b) coefficient of performance of 0.32, and (c) specific cooling power of 40.82 W/kg of silica gel. The concentration of salt (X) in the product (desalinated water) has been set with value of 0.5 gm/kg to be suitable for drinking and irrigation. The salt concentration in the evaporator is estimated to be 4.611 gm/kg during the overall adsorption process. The results from this study should be of wide interest for the field of solar water desalination and air-conditioning.

Keywords: Solar desalination, Agricultural wastewater, Adsorption, Single bed, numerical modelling

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1. Introduction

Water and energy are two of the most important elements to human life, which largely influence the growth and development of human societies. Nowadays, the quest for abundant energy and freshwater witnesses a dramatic increase in demand due to the growth in urban population and industrialization. However, the resources of freshwater on Earth remain very limited and they are estimated to be no more than 3% against to 97% as seawater resources. Furthermore, there is only a marginal portion of seawater resources available to humans to turn them into freshwater. In recent decades, rising energy demand has resulted in significant increases in fossil fuel usage (Jahannoosh et al., 2021). Estimates indicate that utilizing renewable sources of energy for seawater desalination account for a small percentage of all freshwater generated in the world. Reasons include the high equipment costs and the growing environmental negative impacts due to the harsh fossil-fuel usage which is in favor of lowering carbon emissions (Naderipour et al., 2021). In several areas around the world, availability of great amounts of solar energy being usually associated with scarcity of freshwater especially in the middle east (Alnajdi et al., 2020). Also, in some rural and isolated areas, the grid electricity is not accessible and the access to freshwater resources is virtually absent. Therefore, the move to utilizing of renewable energy sources like solar seems very practical solution to mitigate the reliance on fossil fuels, reduce the consequences of fossil-fuel usage like the harmful CO₂ emissions, and save the high costs of supplying freshwater. In this regards, solar-powered desalination appears as a very dependable technology that has the potential to resolve the shortage of sufficient freshwater supplies at rural and isolated parts of the world.

There are various methods to produce freshwater using the desalination technologies. These technologies are divided according to the kind of the energy source driving the process as thermally-driven techniques such as multi-stage flash (MSF), multi-effect distillation and mechanical-and-thermal vapor compression and pressure-driven techniques such as Reverse osmosis (RO). There are some disadvantages associated with applying these traditional desalination technologies like scaling, fouling, corrosion, and the need for pre- and post-treatment
chemicals for seawater. To compensate for these disadvantages, the adsorption desalination is adopted as environment-friendly, highly efficient, and sustainable technology for water desalination. It also considered as an attractive and potentially competitive method compared to other thermal methods due to its ability to generate freshwater and cooling effect simultaneously (Raj & Baiju, 2019). Furthermore, it could be operated by a low-temperature heat source like solar energy thus the high operating costs and the risky CO₂ emissions associated with the traditional desalination methods could be substantially reduced. Other advantages include the chilled water which is produced as by-product can be employed for cooling or refrigeration purposes. Also, there is ability to work at relatively low temperature and pressure compared to traditional methods which minimizes the undesirable fouling and scaling. More important, the absence of moving parts makes the maintenance cost to be very low compared to the other methods (Woo et al., 2019).

Sakoda & Suzuki, (1984) presented an experiment on a solar-powered adsorption cooling system which simulated a functional unit by using a mixture of silica-gel and water vapor as adsorbent-adsorbate mixture. The transitional behaviour of heat and mass transfer was interpreted successfully by the model. Chua et al., (2002) studied experimentally the adsorption characteristics of pure water vapor onto two different types of silica gel. The Toth isotherm model is used to match all of the experimental results within the bounds of the experimental errors. The model is found to be able to accurately explain the efficiency of type A and RD silica gels. Ng et al., (2009) investigated the performance of a two-bed adsorption cycle that uses solar hot water to generate cooling and desalination effects. They showed that with SCC range of 25–35 Rton/tonne of silica gel, the AD cycle generates chilled water at temperatures ranging from 7 to 108°C and provides SDWP of 3–5 m³ per tonne of silica gel per day. Thu et al., (2013a) investigated three types of silica gels (Type-A5BW, Type-A++ and Type- RD 2560). They observed that the Type-A++ silica gel (granular type) has the largest surface area of 863.6 m² per gram, followed by type-A5BW and Type-RD 2560, respectively. They investigated the pore size of the silica gels, and found that their pore diameters range from 10 to 30 microns. (Rezk et al., 2019) proposed a silica gel-based on mathematical model for the SADC method (solar adsorption desalination cycle) based on result from experimental study. They optimized the performance of (SADC) system by employing a modern optimizer to evaluate the optimal cooling, heating, cycle time, and heating water flow rate.

Li et al., (2003) introduced simulation results for a solar refrigerator in which zeolite is put within the solar collector's evacuated tubes. It is found that the overall device efficiency is superior to previous solar adsorption refrigerators, with potential solar COP values exceeding 0.25. Zejli et al., (2004) presented a multi-effect desalination system that uses zeolite as the solid vapor adsorbent and runs on an adsorption heat pump with an open cycle. They showed that the regeneration efficiency decreased with increasing of time. Ullah et al., (2013) presented a review of various solar thermal refrigeration systems, with various working fluids. They reported that zeolite–water pair is better suited for air-conditioning applications. Ali & Chakraborty, (2016) investigated an adsorption desalination system using two adsorbents (zeolite and silica gel). They discovered that the silica gel is suitable for water production system, zeolite is a viable choice for cooling system. Alsaman et al., (2017) evaluated the adsorption characteristics for two-bed adsorption desalination system using 13.5 percent silica gel. They reported a specific cooling power of 112 W/kg and a specific daily water production of 4 m³ per ton silica gel with COP of 0.45. Kowsari et al., (2018) developed A three dimensional numerical scheme to investigate the impact of geometrical structure on the performance of a trapezoidal aluminium finned flat-tube heat exchanger in a single bed adsorption chiller. They found that the heat transfer resistance is primarily influenced by both the fin pitch and height in this form of Hex, while the inter-grain mass transfer resistance is regulated independently by the bed length. The fin height has a greater impact on the COP than the fin pitch, and the bed length has only small effects at a given fin height and pitch. (Raj & Baiju, 2019) studied adsorption desalination of single-bed system and their theoretical analysis was based on the performance parameters such as fresh water production, coefficient of performance and energy consumption per kg of water produced. (Amirfakhrakazi et al., 2020) implemented a new operation cycle for two-bed adsorption desalination cycle with heat and mass recovery between the adsorption beds, the condenser and the evaporator. They found that at a hot water temperature of 95 °C and cold water of 30 °C, the specific daily water output (SDWP) is 9.58 m³/ton of silica gel/day. (Naemi et al., 2020) provided theoretical framework focused on a modern advanced adsorption desalination and cooling system with internal heat recovery and double-cycle multi-bed dual-evaporator. They showed that contrary to the single-cycle multi-bed dual evaporator design, SDWP in the proposed configuration increases by 20%. Zhang et al., (2020) presented a 100 kg/h water production pilot-scale adsorption desalination system. The results showed that when the temperature of the hot water entering the desorber is 55°C and the flow rate is 28 m³/h, the rate of water production exceeds 100 kg/h. Bai et al., (2020) developed a mathematical model taking into account the influence of salinity on the physical properties of saltwater. They found that the specific cooling power and specific daily water production are 490 W/kg and 18 m³/ton adsorbent/day for seawater under the operating conditions of desorption temperature at 85 °C and evaporation temperature at 14°C. Ali et al., (2021) proposed a new combination of ADS with liquid-vapor ejector to boost freshwater productivity. It is found the proposed system using a desorption temperature of 95 °C can produce specific daily freshwater higher by a factor of 5.0.

In this paper, the mathematical modelling of solar adsorption desalination system with a new design under Iraq climate conditions is conducted and experimentally validated. An effective design with lower cost has been developed in this system since the high cost of installing solar modules is seen as an obstacle to their widespread usage. Domestic evacuated-tube solar collectors which are mainly mounted over homes and buildings roofs have been used in this research. The use of this type of solar collector helps in reducing the installing cost of the solar adsorption desalination system. It is designed to test the system
performance in terms of specific daily water production (SDWP), cooling performance assessment indicators such as the specific cooling power (SCP) and coefficient of performance (COP) at different working-fluid temperatures. In addition, the effects of various operating parameters on desalination and cooling performance, such as saltwater salinity, hot water, cold water, chilled water inlet temperature, are all investigated in this modelling study.

2. System description

The adsorption cooling system (AC) of (Lattieff et al., 2019) has been modified to match the new proposed configuration with water desalination strategies as shown in Fig. (1). In this configuration, the system modification includes separating the connecting line between the condenser and the evaporator in order to collect the distilled water in a tank. Also, the amount of salt water is added to the evaporator during the operation through a line for entering and exiting the saltwater stream from the evaporator. Thus the system can be described as a continuous desalination system with this new configuration. Fig. (1) shows the single bed ADS’s schematic plan. Desalination occurs during the desorption process, while the cooling effect occurs during the cycle’s adsorption process. After degassing the entire system and charging the evaporator with salt water, the evaporation is accomplished by the adsorbent substance up taking water vapor. The unsaturated silica gel type (A) which packed into a tube heat exchanger located within a reactor bed adsorbs water vapor. Table 1 shows the properties of the silica gel used in this work. A continuous vapor adsorption is achieved when the valve between the adsorption bed and the evaporator is opened. The heat of adsorption is released during the adsorption process. The saturated silica gel can be regenerated by introducing hot water at a low temperature from a heat source, which is known as the desorption process. The connecting vapor valves are set to open position after the switching time, and the regenerated water vapor flows to the condenser to provide distilled water. The heat of condensation is rejected into cooling water flowing through the condenser, and the condensate is stored as desalinated water. The heating water valve is opened to begin the preheating phase, and the adsorbent pressure and temperature are increased. The condenser-bed valve opens when the pressure inside the bed reaches that of the condenser. During the precooling process, cooling water valve is opened to lower the temperature of the adsorbent, which rises due to the physical contact between the vapor and the adsorbent. Then valve between the evaporator and bed is opened during adsorption process. After cycle time, the previous phases are rebated with desorption and adsorption processes.

Table 2 shows the timetable used in this research for the single-bed adsorption desalination system in use. The time for preheating and precooling processes is given by switching time. It can be observed from the table that the switching time for preheating process is 20 minutes and for precooling process is 10 minutes, while the time for desorption and adsorption process are 20 and10 minutes, respectively. So, the complete cycle time for all process is being 60 minutes.

![Fig.1 Schematic of the single-bed adsorption desalination system.](image-url)

**Table 1** Properties of silica gel type A.

| Property                  | Value       |
|---------------------------|-------------|
| Apparent density          | 750 kg/m³   |
| Average particle diameter | 6 mm        |
| Surface area              | 650-700 m²/g|
| Thermal conductivity      | 0.198 W/m.K |
| Specific heat capacity    | 921 J/kg.K  |
3. Mathematical modeling

A single bed adsorption desalination system is simulated to assess its ability to produce fresh water. Energy equations for the evaporator, condenser, and adsorption bed, as well as mass and salt balance equations for the evaporator, are solved in order to analyze the cycle. The mathematical model presented here is implemented to numerically simulate the real working conditions of the solar adsorption desalination system. The following assumptions are made to make the mathematical analysis easier to understand:

1. Pressure, temperature, and the amount of adsorbate in the adsorption bed are uniform.
2. Adsorbate vapor, metal tube, and fluid properties are all constant.
3. The evaporator is well insulated.
4. The flow resistance caused by pipeline water flow is neglected.

3.1 Isotherms of adsorption and adsorbate uptake

The adsorption/desorption rate is a main parameter for determining the silica gel's performance. This is one of the most important parameters to consider, since it is related to the adsorbent's temperature, which is increased by the solar collector. The transient uptake is expressed as follows using the linear driving force (LDF) model, (Alsaman et al., 2017)

\[
\frac{dx}{dt} = k_m \cdot (x_{eq} - x)
\]

where:

\[
k_m = \frac{15 + D_0}{n_p} \exp \left( -\frac{E_a}{RT_{bed}} \right)
\]

\[K_m\] known as overall mass transfer coefficient, \(D_0\) is the adsorbent's diffusion factor in the adsorbent that equals \(2.54 \times 10^{-4}\) \(m^2/s\), \(E_a\) is the surface diffusion activation energy, which is \(4.20 \times 10^4\) \(J/mole\), the universal gas constant \(R\) is given as \(8.314\) \(J/mole.K\), \(R_p\) is the radius of particle.

Adsorption isotherms must be determined in order to measure the amount of vapor adsorbed by the silica gel at various pressure ratios. Dubinin-Astakhov equation as stated in (Wang et al., 2005) was used for calculation of adsorption equilibrium uptake by the silica gel:

\[x_{eq} = x_0 \cdot \exp \left[-K \cdot \left(\frac{P_{bed}}{P_{sat}} \right)^{n} \right]
\]

Here \(x_{eq}\) is the amount adsorbed in equilibrium with \(P_b\) is the pressure of bed, \(P_{sat}\) is the saturation vapor pressure, \(n = 1.6\).

The Antoine equation is used to measure the saturation pressure which can be expressed in the following way:

\[P_b = 133.31 \cdot \left(1 - 10^{\frac{3820}{T_b+273.3-46.1}}\right)
\]

\[x = x_{eq} \cdot (1 - e^{-k_m \cdot t})
\]

\[\Delta x = (x^*_{eq} - x^*(T_{i-1} \cdot 1) \cdot (1 - e^{(-K_m \cdot t)})
\]

3.2 Equations of energy balance

3.2.1 Energy balance of the adsorption bed

The single bed adsorption desalination operates in two modes: adsorption and desorption when it is attached to the evaporator and condenser, respectively. In the adsorption/desorption mode, the energy balance can be written as follows:

\[(M_{SG} \cdot C_P_{PS} + M_{SG} \cdot C_P_{PS} \cdot x + M_{ML} \cdot C_P_{ML}) \frac{dT_P}{dt} = m_{iw} \cdot C_P_{IW} \left(T_{HWI} - T_{HWO}\right) + \left(H_a - C_P_{PS} T_P\right) M_{SG} \frac{dx_{des}}{dt}
\]

\[(M_{SG} \cdot C_P_{PS} + M_{SG} \cdot C_P_{PS} \cdot x + M_{ML} \cdot C_P_{ML}) \frac{dT_P}{dt} = m_{cw} \cdot C_P_{CW} \left(T_{CWI} - T_{CWO}\right) + \left(H_a - C_P_{PS} T_P\right) M_{SG} \frac{dx_{ads}}{dt}
\]

Here \(H_a\) represent the heat of adsorption.

3.2.2 Energy balance for condenser

In the condenser, the desorbed water vapor has been condensed and delivered to the collecting tank. The condenser's energy balance can be expressed as follows:

\[(M_{W, cond} \cdot C_P \left(T_{cond}\right) + M_{ML} \cdot C_P_{ML}) \frac{dT_{cond}}{dt} = \frac{dT_{cond}}{dt}\]

\[
\frac{dM_d}{dt} = h_f(T_{cond}) + \frac{dx_{des}}{dt} \cdot h_f(T_{cond}) + m_{cw, cond} \cdot C_P \left(T_{cond}\right)
\]

\[
\left(T_{cw, in} - T_{cw, out}\right)_{cond}
\]

Where \(M_{W, cond} \cdot C_P\) and \(M_{ML} \cdot C_P\) refer to condensed water capacity and condenser heat capacity, respectively. \(M_d\) Is the mass of the desalinated water.

3.2.3 Energy balance for evaporator

\[\left[M_{e, evaporator} \cdot C_P \left(T_{evaporator}\right) + M_{ML} \cdot C_P_{ML}\right] \frac{dT_{evaporator}}{dt} = h_f(T_{evaporator}) m_{in} - h_f(T_{evaporator}) \frac{dx_{des}}{dt} \cdot M_{SG} + m_{ch} \cdot C_P_M \left(T_{ch, in} - T_{ch, out}\right) - h_f(T_{evaporator}) m_b
\]

Where \(M_s\) and \(M_{ML}\) are seawater and evaporator metal heat capacities, respectively. The right-hand side of the equation has four terms: inlet heat of feed salt water, latent heat of evaporation, sensible heat transfer of chilled water and heat of discharge concentrated brine.

3.3 Mass balance equation

In an evaporator, the mass balance of seawater is written as:

\[
\frac{dM_{e, evaporator}}{dt} = M_{s, in} - M_p - M_b
\]

Where \(M_{e, evaporator}\) is the amount of seawater in evaporator, \(M_{s, in}\) is the rate at which seawater enters the evaporator,
The amount of pure water, $m_p$, is the mass of concentrated brine discharged, $M_{sg}$ the mass of silica gel
\[
\frac{dM_{sg}}{dt} = m_{s,in} - \frac{dx_a}{dt} * M_{sg} - m_b
\]
(12)

The temperature of the bed, condenser, and evaporator heat exchanger's outlet water was determined by using the formula for the log mean temperature difference (LMTD) as follows:
\[
T_{hw0} = T_{bed} + (T_{hw1} - T_{bed}) \exp \left(-\frac{U_{bed}A_{bed}}{m_{hw}C_{p_{hw}}} \right)
\]
(14)
\[
T_{cwo} = T_{bed} + (T_{cwi} - T_{bed}) \exp \left(-\frac{U_{bed}A_{bed}}{m_{cwi}C_{p_{cwi}}} \right)
\]
(15)
\[
T_{cwe} = T_{cond} + (T_{cwi} - T_{cond}) \exp \left(-\frac{U_{cond}A_{cond}}{m_{cwi}C_{p_{cwi}}} \right)
\]
(16)
\[
T_{cho} = T_{evap} + (T_{chi} - T_{evap}) \exp \left(-\frac{U_{evap}A_{evap}}{m_{cha}C_{p_{cha}}} \right)
\]
(17)

Here $X_{s,in}$ is the concentration of the salt water inter the evaporator, $X_p$ is the concentration of the product (desalinated water).

Finally, the efficiency of the system is measured using the $Q_c$ (heat of evaporation), SCP (specific cooling power), coefficient of performance (COP) and SDWP (specific daily water production).

\[
Q_C = \frac{(Msg \Delta x \Delta H_{ads})}{t}
\]
(18)
\[
SCP = \frac{Q_C}{M_{sg}}
\]
(19)
\[
COP = \frac{Q_C}{(m_hC_p(T_{hw1} - T_{hw0}))}
\]
(20)
\[
SDWP = \frac{N_{cycle} \int_{t_{cycle}}^{} \left(\frac{dx_{ads}}{dt}\right) dt}{M_{tot}}
\]
(21)

The equations of the mathematical modeling of adsorption desalination system are solved using EES (Engineering Equation Solver) is a modern computer tool. The parameters used in the simulation program are listed in Table 3.

### 3.4 Model validation

In this study, the present adsorption cooling system without water desalination model is validated using (Lattieff et al., 2019)'s experimental work. The performance parameters including SCP, COP are adopted in the validation. The following step is to suggest a new adsorption cooling system with water desalination capabilities. The effects of different parameters on the efficiency of the new adsorption-cooling (ADC) system are then investigated. Fig 2 shows a comparison between the present model with water desalination and the experimental temperature profile for adsorption bed. It shows that the present model can predict the experimental findings with good degree of precision.

| Parameter          | Value         |
|--------------------|---------------|
| $m_{hw}$           | 0.5 (kg/s)    |
| $m_{cwi}$          | 0.2 (kg/s)    |
| $m_{salt \ water}$| 0.0004 (kg/s) |
| $X_p$              | 0.5 gm/kg     |
| $T_{hw1}$          | 89 ºC         |
| $T_{chw}$          | 26 ºC         |
| $T_{chi}$          | 14.5 ºC       |
| $M_{sg}$           | 10 kg         |
| $M_{shell}$        | 80 kg         |
| $M_{coil}$, $M_{screen}$ | 2 kg     |
| $C_p$ screen (aluminium) | 900 J/kg.K    |
| $C_p$ coil (copper) | 385 J/kg.K    |
| $C_p$ shell        | 479 J/kg.K    |
| $C_p$ bed         | 4188 J/kg.K   |
| $A_{bed}$          | 0.351 m²      |
| $A_{evap}$         | 0.5 m²        |
| $A_{cond}$         | 0.1 m        |
In order to be more confident, Fig. (3) Which displays the evaporator temperature profile is adopted to make another comparison of the present model prediction with the experimental data of (Lattieff et al., 2019). It also shows a good agreement between the two studies. Hence, the present model is considered a reliable enough to be adopted to study the proposed ADC system.

4 Results and Discussion

After model validation, a new adsorption cooling system has been proposed with water desalination capability. Fig.4 illustrates the measured adsorption bed temperature at different inlet hot water temperatures at 70, 80, 90 °C. As indicated, the peak bed temperature $T_b = 74.6°C$ is achieved when the hot water inlet temperature is 90 °C. During the desorption period, a higher bed temperature would cause a large amount of adsorbed vapor to be released. As a result, higher adsorption capacity is obtained. This is very important because it lowers the evaporator temperature, which contributes to increasing of cooling power.

Fig (5) demonstrate the evaporator temperature profiles for the adsorption system with and without water desalination. It is observed that the temperature of evaporator for the proposed system with water desalination is steady at 25°C before adsorption time phase is started. When the valve between evaporator and adsorber is first opened at the beginning of the adsorption time the evaporator temperature decreases to 21.6°C. When the adsorption time exceeds one minute, the evaporator temperature drops to 17.9 °C, then rises to 22.4 °C at the end of the adsorption time. The cause for this rise is the flow of salt water within the evaporator. Comparably, in an adsorption cooling system without desalination, the evaporator temperature rises gradually between 8.9°C and 14°C before the adsorption phase begins. The insufficient isolation of the evaporator during this period causes heat transfer through the system’s valves resulting in a progressive rise in temperature. Also, the temperature reaches 6.7°C at the start of the adsorption time and remains fairly constant until the end of adsorption phase.
Effect of hot water inlet temperature on COP is shown in Fig.6 which illustrates that COP has the optimum value at T=70 °C. As shown in Fig.6 at T= 80 °C and 90 °C COP begins to decrease above this temperature. It can be deduced that when the regeneration temperature rises, the COP increases until it reaches 70 °C. The explanation for this is up to 70 °C, all of the adsorbate is desorbed, and afterwards the amount of desorbed adsorbate rapidly decreases. Furthermore, as compared to Qc (heat of evaporation), COP drops due to the high increase in heat input. This is related to the design of the adsorption bed heat exchanger, which results in insufficient heat transfer, lowering adsorption capacity and Qc, as well as lowering the COP.

Fig.7 shows specific cooling power (SCP) with cycle time at different hot water inlet temperatures. This figure indicates an improvement in SCP with an increase in hot water inlet temperature, and the peak value of SCP = 40.82 is obtained at Thwi =90 °C. Typically, SCP is zero before the adsorption process started. However, the cooling effect substantially rises when the valve between the evaporator and the adsorber is opened at the start of the adsorption time. Because the initial adsorption rate and the equilibrium adsorption rate are so dissimilar, SCP reaches its peak value of dry adsorbent. This implies that a 10-minute adsorption period is adequate to complete the hydration of silica gel.

The concentration of the feed salt water in the shell side of the evaporator is shown in Fig.8. Accordingly, when the valve between the evaporator and the bed was opened at the start of the adsorption phase, the salt water concentration (Xs) was 4 gm/kg and quickly grew to 4.61 gm/kg which is caused by the fact that during the adsorption process, the vapor is drawn from the evaporator into the adsorber which leading increasing in the salt concentration. Moreover, it is noticeable that a decrease in salt water concentration occurs after it reaches its maximum value of 4.61 gm/kg. The reason of that is the salt water enter and exits from evaporator which is in continuous flow rate causing in decreasing of salt concentration.

Fig.9 illustrates effect of hot water inlet temperature (HWIT) with time on the SDWP (specific daily water production). SDWP is presented for (HWI) temperatures ranging from 70 to 90 °C. The figure indicates that at T=90 °C, SDWP has the optimum value of 1.896 m³/ton silica gel/day. This attributed to the fact that when a higher regeneration temperature is used the amount of vapor regenerated in the adsorption bed increases resulting in an increase in the SDWP. In addition as HWIT rises, the rate of adsorption desalination system increases. This is because the regeneration process gets improved when higher hot water temperatures are used.
Table 4: Results of this work compared with those of (Alsaman et al., 2017) and (Thu et al., 2013b)

| No. of beds | Hot water inlet temperature °C | Adsorbent type | SDWP m³/ton | SCP w/kg |
|-------------|--------------------------------|----------------|-------------|---------|
| This work   |                                | Silica gel type | 1.89        | 40.82   |
| Alsaman, 2017 |                                | Silica-gel     | 4          | 112     |
| Thu, 2013   |                                | A++ Silica-gel | 26         | 0       |

Table 4 compares the results of this work with those of earlier studies on ADS systems. It can be seen that, when an integrated evaporator-condenser design and silica-gel A++ type are used, the maximum SDWP is 26 m³/ton silica gel/day (Thu et al., 2013b). The evaporator temperature of this system is around 42 °C, which is not appropriate for cooling thus SCP ~ 0. To make both the cooling effect and freshwater production possible, (Alsaman et al., 2017) decreases SDWP to 4 m³/ton silica gel/day so that the obtained SCP with value 126W/kg. In this work, the obtained values of SDWP and SCP are 1.89 m³/ton silica gel/day and 40.82 W/kg, respectively. This difference is due to the type of adsorber’s heat exchanger that used by Alsaman et al., (2017). They used finned tube heat exchanger, which improves the heat transfer rate thus leads to higher adsorption power and greater cooling capacity as well.

5. Conclusions

In this research, the mass and heat balance equations are used to model a single-bed adsorption desalination system powered by solar energy. The system uses the silica gel-water pair as working fluid. A computational code has been developed and implemented for solving the proposed mathematical model. The results revealed that the model has good potential to precisely predict the continuous water desalination via the proposed system design at different operating conditions. The effects of Various operational parameters on the performance of solar adsorption desalination are revealed. These parameters include the inlet hot water temperature, cooling water temperature, inlet chilled water temperature, adsorption/desorption phase time and saltwater salinity. The concentration of saltwater (X) is estimated to be 4.61 gm/kg in the evaporator as a result of adsorption process over a cycle period of 60 minutes. Meanwhile, the specific daily water production of seawater (SDWP), specific cooling power (SCP) and coefficient of performance (COP) are estimated as 1.89 m³/ton silica gel/ day, 40.82 W/kg and 0.32 respectively. Based on the results obtained, the following conclusions can be drawn: (1) saltwater with higher salinities can result in decreased cooling and desalination performance under the same conditions, (2) increasing the hot water temperature while decreasing the cooling-water temperature can boost better adsorbent's equilibrium adsorption capacity and leads to higher freshwater production and cooling impact, and (3) the optimal time for desorption/adsorption phase is dependent on the equilibrium adsorption rate that the silica gel is reached.

Nomenclature

- **ADS**: Adsorption desalination system
- **x**: Refrigerant concentration at any time, (kg water/kg silica gel)
- **x_e**: Refrigerant concentration at the equilibrium, (kg water/kg silica gel)
- **k_m**: Overall mass transfer coefficient, m/s
- **x_o**: Maximum adsorption capacity (kg/kg)
- **D_o**: Constant (m/s)
- **R_p**: Particle radius, (m)
- **R**: Gas constant (J/mol K)
- **T**: Temperature (°C)
- **P**: Pressure (Pa)
- **Δx**: variation of refrigerant concentration (kg water/kg silica gel)
- **X**: Concentration of salt (ppm)
- **M**: Mass (kg)
- **m**: Mass flow rate kg/s
- **t**: Time (s)
- **A**: Area (m²)
- **COP**: Coefficient of performance
- **SCP**: Specific cooling power, (W/kg)
- **SDWP**: Specific daily water production m³/ton silica gel
- **CP**: Specific heat (J/kg K)

Subscripts/Superscript

- **sg**: Silica gel
- **hwi**: Hot water inlet
- **hwo**: Hot water outlet
- **wr**: Water refrigerant
- **des**: Desorption
- **ml**: Metal
- **cwi**: Cold water inlet
- **cwo**: Cold water outlet
- **d**: Desalinated water
- **ch**: Chilled water
- **s**: Salt
- **w**: Water
- **p**: Product
- **cond**: Condenser
- **evap**: Evaporator
- **bed**: Adsorption bed
- **ads**: Adsorption

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