Quantum control of $^{88}\text{Sr}^+$ in a miniature linear Paul trap

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Abstract We report on the construction and characterization of an apparatus for quantum information experiments using $^{88}\text{Sr}^+$ ions. A miniature linear radio-frequency (rf) Paul trap was designed and built. Trap frequencies above 1 MHz in all directions are obtained with 50 V on the trap end-caps and less than 1 W of rf power. We encode a quantum bit (qubit) in the two spin states of the $S_{1/2}$ electronic ground-state of the ion. We constructed all the necessary laser sources for laser cooling and full coherent manipulation of the ions’ external and internal states. Oscillating magnetic fields are used for coherent spin rotations. High-fidelity readout as well as a coherence time of 2.5 ms are demonstrated. Following resolved sideband cooling the average axial vibrational quanta of a single trapped ion is $\bar{n} = 0.05$ and a heating rate of $\dot{\bar{n}} = 0.016 \text{ ms}^{-1}$ is measured.

1 Introduction

Trapped ions have proven to be a valuable resource in the field of experimental quantum information and precision measurements. Their tight spatial localization, isolation from external perturbations and the ability of experimenters to coherently manipulate their internal and external degrees of freedom with high fidelity, place trapped ions among the leading technologies of quantum information research [1, 2].

The realization of scalable quantum computation and simulation requires the design and fabrication of small trap arrays. The smallest traps demonstrated to date were built using modern micro-fabrication techniques [3–10]. Due to the technical complexity of micro-fabrication, most of the current research in this field is still conducted using manually assembled traps. While sub-mm traps are constructed using gold on alumina [11, 12], traps which are assembled from individual electrodes [13–15] have usually minimal ion-electrode distance not smaller than 0.5 mm. Here we report on a manually assembled miniature trap having individual electrodes with a minimal ion-electrode distance of 0.27 mm. Our trap has dimensions that approach those of micro-fabricated traps but with simplicity similar to Ref. [15]. Its construction required only commercial parts, conventional workshop capabilities, and laser machining which is also commercially available.

Various internal states can be used to encode a qubit; examples include optical, hyperfine, and Zeeman splitted levels [16–19]. Here, we focus on a Zeeman qubit in a $^{88}\text{Sr}^+$ ion [20, 21]. We have implemented all frequency stabilized lasers that drive the various transitions required for laser-cooling, state-selective fluorescence detection, and coherent control. One convenient property of the Strontium ion is that all its relevant optical transition wavelengths are available using diode lasers.

Using a narrow line-width laser, we perform electron shelving on a narrow quadrupole transition, and are thus able to demonstrate high fidelity qubit readout. With the same laser, we performed resolved sideband cooling and demonstrated 95% ground state occupation of the axial vibrational mode. A heating rate of $\dot{\bar{n}} = 0.016 \text{ ms}^{-1}$ for this mode is measured.

Although a ground-state Zeeman qubit has practically an infinite life time, a coherent superposition is hard to maintain in the presence of ambient magnetic field noise. We constructed a servo system that reduces magnetic field noise and...
which leads to the extension of the qubit coherence time by an order of magnitude to 2.5 ms. In this paper, we give an overview of the apparatus we built and discuss various aspects of its performance.

2 Experimental apparatus

2.1 Trap and vacuum system

Our trap has the generic linear Paul trap configuration of four parallel rods positioned at the corners of a square, and two additional “end-cap” rods that are aligned along the square center, symmetrically from each side of the trap; see Fig. 1(a). The four parallel rods carry the rf and dc voltages necessary for radial confinement, whereas the dc voltages on the end-caps provide confinement in the axial direction. The square sides length is 0.6 mm and the distance between the two end-caps is 1.3 mm. The four rods and two end-caps are made of tungsten with diameters of 0.3 and 0.2 mm, respectively. Tungsten has several advantages over stainless steel which is the more commonly used material in ultra high vacuum. Most importantly, it is non-magnetic even after machining. Tungsten is also more rigid; an important property when working with small diameter rods. Moreover, Tungsten is superior in its electrical and thermal conductivity. The distances of the ion from the rf/dc electrodes and end-caps is 0.27 and 0.65 mm, respectively.

Structural integrity and electric insulation are provided by four laser machined alumina wafers with adequate holes for holding the electrodes. These alumina wafers are aligned and held together by two, 5 mm diameter, stainless steel rods that provide a skeleton for the trap structure. The wafers are separated by three titanium spacers of 3, 4, 3 mm thickness. Here, Titanium is used because it is non-magnetic. The wafers thus define four straight support points for each electrode. Small naturally occurring misalignment causes mechanical friction that keeps the electrodes in place once they have been threaded through the four alumina wafers.

Two additional electrodes are placed below the trap, at a distance of 1.66 mm from the ion. One electrode is used to drive current that produces the oscillating magnetic field needed for magnetic-dipole coupling between the qubit levels. The second electrode is used for compensation of stray electric fields in the direction of the rf electrodes. The trap is driven at \( \Omega_{\text{rf}}/2\pi = 21 \text{ MHz} \) with 0.5 W of power. A helical resonator with a Q-factor of 70 produces a voltage gain to 200 V on the rf electrodes. The resulting radial trap frequencies are \( \omega_{\text{rad}}^{1,2}/2\pi = (2.5, 2.35) \text{ MHz} \). The degeneracy between the two radial directions is lifted by a 0.5 V bias on the dc electrodes. The trap axial frequency is \( \omega_{\text{ax}}/2\pi = 1 \text{ MHz} \) with a voltage of 50 V applied to the end-cap electrodes. The deviation of the trapping potential from a pure harmonic potential has been characterized as well. The next term beyond linear in the force along the axial direction is cubic, \( F_{\text{nl}} = ax^3 \). This term is measured by the study of the ion non-linear response to a strong, near resonance, drive. The cubic force term coefficient is found to be \( a/(2\pi)^2 = 1.74 \pm 0.03 \times 10^{-7} \text{ kg Hz}^2/\text{m}^2 \) [22].

The trap is mounted inside an octagon-shaped vacuum chamber (Kimball physics MCF600-SphOct-F2C8) with eight 2.75 in. view-ports on the octagon faces and two 6 in. ports at the top and the bottom of the chamber. The side ports are used for laser access, electrical feedthrough and connection to the vacuum pumps whereas the top port is designated for imaging. Three types of vacuum pumps are combined to achieve ultra-high vacuum. A 20 l/s ion getter pump and a Titanium sublimation pump are connected to the main chamber through a 2.75 in. port. Inside the main chamber we placed two non-evaporable getter strips (SAES St707) which are thermally (300°C) activated during bake-out. After bake-out, the vacuum ion-gauge was indicating a pressure below its baseline reading of \( 4 \times 10^{-12} \) mbar. During the last 2 years, ions were regularly trapped for periods of up to a week. We never observed chemistry of trapped-ions with residual background molecules or loss of ions from the trap, as long as they were laser-cooled.

A thermal jet of neutral Strontium atoms is directed into the trap center from either one of two Sr ovens that are positioned approximately 2 cm from the trap center. The ovens
are made of 1 mm diameter stainless-steel tubes with one end crimped. Small grains of Strontium metal are placed inside the tubes in a dry nitrogen atmosphere since it is highly reactive to moisture. We seal the ovens with a thin layer of Indium before we expose them to room atmosphere. The Indium seal melts once the ovens are heated in vacuum. Resistance heating the oven with a current of 2 A, results in the jet of neutral Strontium atoms necessary for trap loading.

2.2 The $^{88}$Sr$^+$ energy levels and laser sources

A single or few ions are loaded into the trap by photo-ionization. Photo-ionization is performed using a resonant two-photon process [23, 24]. A Sr atom is initially excited to the $5s5p^1P_1$ level and then, by a second photon, to the auto-ionizing $5p^21D_2$ level, at transition wavelengths of 461 nm and 405 nm, respectively. The first is generated by doubling a 922 nm external-cavity diode laser (ECDL) in a single pass through a PPKTP crystal (Raicol Crystals Ltd.). The crystal is mounted in a thermally stabilized housing. A 100 mW of 922 nm light generates an output power of 100 μW at 461 nm. The second beam of 20 mW at 405 nm, is produced using a free running laser diode (InGaN). The 461 nm (405 nm) beam is focused, at the trap center, to a waist of 50 μm with a typical power of 15 μW (3 mW).

Doppler-cooling and florescence detection are performed on the $S_{1/2} \rightarrow P_{1/2}$ electric-dipole transition at 422 nm. See Fig. 2(a) for an energy-level diagram. Since Sr$^+$ has low lying 4D levels, the cooling cycle has to be closed with additional light at 1092 nm which repumps population from the long-lived (0.37 s) $D_{3/2}$ level. The cooling light is generated by a 844 nm ECDL which is frequency doubled, producing 15 mW of light at 422 nm (Toptica SHG110). The fundamental diode laser at 844 nm is locked, using a Pound–Drever–Hall (PDH) error signal, to a hemispherical Fabry–Perot cavity. The cavity is built using an Zerodur spacer and has one of its mirrors mounted on a piezo-electric stack. The cavity maintains long-term stability by locking it to the $5s2S_{1/2} \rightarrow 6p^2P_{1/2}$ transition in $^{88}$Rb which is 400 MHz red detuned from the cooling transition [25]. The error signal is generated by passing 422 nm light through a heated (120°C) Rb vapor cell and recording the derivative of a saturation absorption signal. The repump light at 1092 nm is generated by a distributed feedback (DFB) diode laser (Toptica DL100 DFB) producing 15 mW. Another ECDL (Toptica DL100) at 1033 nm with 30 mW is needed to repump the $D_{3/2}$ level. Both the 1092 nm and the 1033 nm lasers are simultaneously locked to an in-vacuum Zerodur cavity with a finesse of 100 using PDH and lock-in techniques, respectively. Typical frequency drifts of the lasers due to thermal fluctuations of the cavity are of the order of 1 MHz in few hours.

The narrow $S_{1/2} \rightarrow D_{3/2}$ quadrupole transition is driven by another ECDL (Toptica DL100) emitting 10 mW at 674 nm. The cavity of this laser is 10 cm long leading to a fast line-width of approximately 100 kHz in 10 μs, significantly above the expected Schawlow–Townes limit. The ECDL is then locked to in-vacuum (10$^{-8}$ mbar) Ultra Low Expansion glass (ULE) cavity with a finesse of 100,000 (AT-Films, [26]) using a PDH technique. A laser line-width of less than 80 Hz is measured by performing Ramsey experiments on the ion. Thermal fluctuations cause the cavity resonance to drift on a time scale of few hours with peak to peak amplitude of 1 MHz (the lab temperature is stabilized to within 0.3°C), with a typical slope of 10 Hz/s. These slow drifts are automatically compensated for by scanning the atomic transition every few minutes and continuously updating the laser frequency by linear extrapolation. Using this technique, the laser detuning from any desired transition can be smaller than 300 Hz at all times.

All light sources pass through acousto-optical modulators (AOM’s), in a double-pass configuration, before they are brought to the trap by polarization maintaining single mode fibers. The AOMs have two roles. First, they bridge the frequency difference between the frequency references and the atomic transitions. Second, they allow for switching and control of the light intensity by controlling their driving rf power. The frequency sources for the AOMs are based on either voltage controlled oscillators (VCOs) or direct digital synthesizers (DDSs) which are controlled by a field programmable gate array (FPGA). The use of DDSs allows for phase and frequency control during a single experimental sequence.

The beams are focused at the trap center to a waist of 50 μm. The schematic drawing of the laser beams configuration is presented in Fig. 2b. A magnetic field of 1–20 G defines a quantization axis. The cooling and detection beams at 422 nm are combined with the two repumping beams at 1092 and 1033 nm on a dichroic beam combiner before being focused on the ion. The beams are oriented at 45° to the trap axis and perpendicular to the quantization axis while having a projection on both of the trap radial principal directions as well. A circularly polarized beam at 422 nm, aligned parallel to the magnetic field, is used for optical pumping. The 674 nm beam that drives the $S_{1/2} \rightarrow D_{3/2}$ quadrupole transition is also parallel the quantization axis. For this configuration, quadrupole transitions with $\Delta m = \pm 1$ are allowed [27] with a Lamb–Dicke parameter of $\eta_{674} = 0.05$.

2.3 Imaging system and photons counting

Ion fluorescence at 422 nm is collected with an N.A. 0.31 objective lens (LENS-Optics). This lens was custom designed, based on [28], to correct for the view-port spherical aberrations. A flipping mirror switches between forming an image of the trapped-ions onto a electron multiplying CCD (EMCCD) camera (Andor Luca), with magnification of 42.
and a diffraction limited resolution (0.8 μm), or single photon counting by two photomultiplier tubes (PMT) each on a different side of a polarizing beam splitter (PBS) cube. Computer-controlled quarter and half wavelength retardation plates are positioned in front of the PBS to allow for full polarization analysis of fluorescence photons.

We measured the total photon detection efficiency by counting detection events in the process of single photon scattering. Single photon scattering is achieved by first applying a cooling pulse on the $S_{1/2} \rightarrow P_{1/2}$ transition. After an average of 14 scattering events, the electron decays to the meta-stable $D_{3/2}$ level. Then a short pulse of 1092 nm light pumps the electron back to the $P_{1/2}$ state, from which it decays back to the $S_{1/2}$ state via single photon emission. The total photon detection efficiency was thus found to be $2.5 \times 10^{-3}$. When both the 422 and 1092 nm beams are applied to the ion, the maximal photon detection rate is 70 kHz. In the absence of an ion, we measure a 1 kHz photon detection rate due to scattering of laser light from trap surfaces.

Figure 3(a) shows an EMCCD image of a three ion crystal with inter-ion separation of 5.5 μm. Figure 3(b) shows fluorescence spectroscopy of the $S_{1/2} \rightarrow P_{1/2}$ transition based on PMT photons counting. The dip on the left side of the spectrum is a dark resonance resulting from transition amplitude interference in the presence of both the 422 nm and the 1092 nm light. The dependence of the spectrum on the magnetic field is shown in the inset. As the magnetic field is increased, the dark resonances due to different Zeeman sub-levels separate and can be resolved.

3 Micro-motion compensation

Displacement of the ion from the rf potential minimum due to stray electric fields or structural deformations causes excess micro-motion, i.e. oscillation of the ion at the rf trap frequency, which deteriorates cooling and detection efficiency. Once the excess micro-motion is probed, it can be eliminated by proper voltage biasing of different trap electrodes in order to bring the ion to the rf minimum. There are various methods for probing micro-motion [30]. We implement a method that was recently demonstrated by the NIST ion storage group [31, 32]. We inject a small additional rf voltage at a frequency $\Omega_{\text{drive}} = \Omega_{\text{rf}} + \omega_{ax}$ to the trap rf resonator. Due to pseudo potential nonlinearity in the electric field ($\propto E^2$),
4 Single qubit manipulation

There are several ways to encode a qubit using the electronic states of a trapped-ion. In the $^{88}\text{Sr}^+$ ion, which lacks a nuclear spin but has a low lying meta-stable $D$ level, two options can be used. One is encoding the qubit in the $S_{1/2}$ and $D_{5/2}$ levels which are separated by an optical transition. The second, which is discussed here, is encoding the qubit in the two Zeeman sub-levels of the $S_{1/2}$ ground state.

4.1 Qubit initialization and detection

Initialization of the Zeeman qubit is performed by optical pumping, in which a circularly polarized laser beam parallel to the magnetic field ($\sigma^+/-$) and in resonance with the $S_{1/2} \rightarrow P_{1/2}$ transition, excites only one of the Zeeman states. A 3 µs, $\sigma^+$ polarized, pulse initializes the qubit to the $m = +1/2$ spin state with probability greater than 0.99. The initialization fidelity in this case depends on the polarization purity which at low magnetic field is limited by magnetic field fluctuations and at a high magnetic field by stress-induced birefringence in the vacuum chamber viewport. To improve on the initialization fidelity, we further perform optical pumping using the narrow quadrupole transition, $S_{1/2} \rightarrow D_{5/2}$, in which spectral selectivity rather than polarization allows for the excitation of only one of the Zeeman states. Here, errors as small as $10^{-4}$ were obtained [33].

In contrast to initialization, state detection presents a much harder challenge. Since the two qubit levels are typically separated by an energy difference which is smaller than the $P_{1/2}$ excited state linewidth, direct state selective fluorescence is impossible. To discriminate between them, one of the qubit states is shelved to the meta-stable $D_{5/2}$ level prior to detection by resonance fluorescence. The selective shelving of only one spin state is done using the narrow linewidth 674 nm laser. High fidelity state detection, therefore, imposes stringent requirements on the laser performance. Robust shelving can be achieved by applying several consecutive excitation pulses to different Zeeman levels in the $D_{5/2}$ state manifold. We have demonstrated a total initialization and detection fidelity of 0.9989(1) [33] which is compatible with recent estimates for the fault-tolerance error threshold.

4.2 Qubit rotations and coherence

The transition between the two $S_{1/2}$ Zeeman states is driven by resonant oscillating magnetic field. It is produced by a current flowing in one of the rod electrodes that are positioned 1.66 mm away from the ion; see Fig. 1(a). The electric current source is an amplified DDS which is impedance matched to a few Ohms by a Balun transformer. The oscillating current has an amplitude of 100 mA at a frequency range

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1 When the 405 nm beam directly hits the alumina surface, a clear charging effect is observed.
of 1–30 MHz, and gives rise to a Rabi frequency around 50 kHz. Rabi oscillations between the two qubit levels are shown in Fig. 5.

The coherence of a Zeeman superposition is quickly lost in the presence of magnetic field noise. To protect our qubit from decoherence due to magnetic field noise, we have designed and built a servo system that stabilized the magnetic field on the ion and reduced noise components, mainly at the power line frequency (50 Hz) and its harmonics. We were thus able to reduce these magnetic field noise amplitudes to the few μG level. The coherence time of the qubit, as was measured in a Ramsey experiment, is 2.5 ms. Coherence oscillations in a typical Ramsey spectroscopy experiment are shown in Fig. 6. Here, the coherence time was limited by low frequency (<1 Hz) and large amplitude (>100 μG) magnetic field noise, as suggested by the un-smooth appearance of the fringes at Ramsey times longer than ~500 μs. By further using dynamic decoupling methods, our qubit coherence time was extended up to 1.4 s [34].

5 Cooling and heating rate

Cooling the ion to a low mean vibrational quantum number, \( \bar{n} \), is useful for both quantum information and precision measurement applications. Doppler laser cooling is a simple and efficient mechanism for cooling but typically yields \( \bar{n} > 1 \). A multi-level cooling cycle, such as in Sr+, raises additional complications on reaching the Doppler limit. The atomic line profile on which we preform Doppler cooling is shown in Fig. 3(b). We slightly detune the 1092 nm repump laser red of resonance to create a pronounced dark resonance (seen as a deep in the graph). This results in a steeper slope on which we detune the cooling laser to reach a lower final temperature.

The ion temperature can be measured in several ways [35–37]. The spectrum of the narrow \( S_{1/2} \rightarrow D_{5/2} \) transition has resolved sidebands. The ratio of red to blue sideband excitation probability can be used for thermometry, when \( \bar{n} \leq 1 \). However, after only Doppler cooling \( \bar{n} \gg 1 \). Instead, a simple way to estimate the ions’ temperature is to measure the decay of the carrier Rabi oscillation due to the ion motion. The carrier Rabi frequency depends on the occupation of the vibrational mode as \( \Omega_0 \propto 1 - \eta^2 \bar{n} \) up to second order in \( \eta \). Hence, a thermal distribution leads to different Rabi frequencies which result in oscillation with a decaying envelope. Figure 7 shows Rabi oscillations on the carrier transition with an average Rabi frequency of \( \Omega_0/2\pi = 180 \) kHz. Fitting the data to a thermal distribution model, shown by the red solid line, yields \( \bar{n} = 12 \), consistent with the Doppler cooling limit.

High fidelity qubit operations require \( \bar{n} \) below the Doppler limit and close to the ground state. This is achieved by applying sideband cooling on the narrow \( S_{1/2} \rightarrow D_{5/2} \)
transition. Since the meta-stable $D_{5/2}$ level is long lived, it needs to be quenched by the 1033 nm repump laser. By properly choosing the saturation parameter of the quenching laser, continuous sideband cooling can be performed on the, effectively broadened, $S_{1/2} \rightarrow D_{5/2}$ transition. For optimal performance, the repump laser intensity has to be modified as the ion is cooled, or the cooling time has to be increased [38]. In order to shorten the total cooling time, we perform such continuous cooling for only 2 ms, after which the ion is cooled to $\tilde{n} \lesssim 1$. Since most of the population that is not in the ground state is in $n = 1$, we then apply two discrete population transfer pulses on the red sideband followed by a 1033 nm repump pulse. Figure 8 shows spectroscopy of the axial red sideband (RSB) and blue sideband (BSB) after (a) Doppler cooling only. Here, the sideband excitation pulse duration is 15 $\mu$s, (b) resolved sidebands cooling and a pulse duration of 100 $\mu$s. Without sideband cooling, the population transfer on the two sidebands is similar, while after sideband cooling, the RSB almost completely disappears. For a thermal distribution model, the probabilities to excite the RSB and BSB are given by

$$P_{ex}^{(r,b)} = \sum_n P_{th}(n) \sin^2(\Omega_n^{(r,b)} t).$$

Here, $P_{th}(n) = \frac{1}{\pi+1}(\frac{n}{n+1})^\eta$ is the thermal distribution and $\Omega_n^{(r,b)} = \hbar \omega_0 \sqrt{n} \sqrt{n+1}$ are the sideband Rabi frequencies. A fit to the measured data, shown by the blue and red solid lines in Fig. 8, indicates an average occupation number of $\tilde{n} = 0.05$. The small background in the measurement is mainly due to carrier excitation resulting from fast frequency noise in the laser spectrum [39]. We find this combined protocol of continuous and pulsed cooling to be efficient and robust without the need to dynamically optimize the quenching laser intensity.

We determined the trap heating rate by varying the time between resolved sideband cooling and the measurement of $\dot{\tilde{n}}$. Figure 9 shows the excitation probability of the RSB and BSB as function of this delay time. Assuming a thermal distribution and a constant heating rate, we fit our data. The fit, shown by the red and blue solid lines, indicates a heating rate of $\dot{\tilde{n}} = 0.016$ ms$^{-1}$. Using this measurement, we calculate the electric field noise spectral density, $S_E = 4m_{Sr} \hbar \omega_0 \hbar \dot{\tilde{n}}/e^2$ [40]. Assuming, $1/f$ noise, a good quantity to compare between traps of similar dimensions is $\omega S_E$. We measure $\omega S_E = 1.3 \times 10^{-6}$ (V/m)$^2$. This value is consistent with heating rate measurements in traps of similar size [9]. During more than 2 years of operation, we did not observe a significant change in the heating rate.

6 Summary

In conclusion, we have constructed various basic building blocks necessary for quantum information related experiments with trapped ions. A, sub-mm scale, trap was manually assembled using conventional and laser machining and commercially available parts. The trap harmonic frequencies are in the MHz range, allowing for operation in the Lamb–Dicke regime. All the necessary laser sources were constructed and frequency locked to stable references. A qubit was encoded into the Zeeman splitting of the electronic ground-state of a single $^{88}$Sr$^+$ ion. A narrow linewidth laser enables electron shelving on the $S_{1/2} \rightarrow D_{5/2}$ transition prior to state selective fluorescence detection. Using the red sideband of this transition, we have also demonstrated ground-state cooling. Coherent transitions between the qubit states are performed by oscillating a current through an additional electrode which is integrated in the trap structure. By
servo stabilization of magnetic field noise, we demonstrate a long qubit coherence time.

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