ANN Prediction of Performance and Emissions of CI Engine Using Biogas Flow Variation

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Abstract: Compression ignition (CI) engines are popular in the transport sector because of their high compression ratio. However, in recent years, it has become a major concern from an environmental point of view because of the emission and depleting fossil fuel. The advanced combustion concept has been a popular research topic in the CI engine. Low-temperature combustion with alternate fuel has helped in reducing the oxides of nitrogen (NO\textsubscript{x}) and soot emission of the engine. Biogas is a popular substitute of energy especially deduced from biomass because of its clean combustion properties, as well it being a renewable energy source compared to non-renewable diesel resources. In experiments with dual fuel, i.e., conventional diesel and alternate fuel (biogas) were carried out through them. In the present study, an artificial neural network model was used to estimate emissions and check the attributes of performance. Different algorithms and training functions were used to train the models. However, the best training algorithm was Levenberge Marquardt and the training function was Tansig (Hyperbolic tangent sigmoid) and Logsig (logarithmic sigmoid), which showed the best result with regression coefficient (R > 0.98) and Mean square error (MSE < 0.001). The best model was trained by evaluating MSE and regression coefficient. Experimental results and artificial neural network (ANN) prediction showed that the experimental results were similar to each other and lie at the same intervals. The ANN model helped in predicting experimental data that were earlier difficult to experimentally perform using interpolation and extrapolations. It was observed that there was an increase in Brake Specific Energy Consumption (BSEC) and a decrease in Brake thermal efficiency (BTE) with improved biogas flow rate and reduced NO\textsubscript{x} emission in the combustion chamber. Carbon monoxide (CO) and hydrocarbon (HC) emissions increase linearly with the increase in biogas flow rate, whereas smoke opacity decreases. It could be concluded that this study helps in understanding the effect of dual fuel (diesel-biogas) combustion under different load conditions of the engine with the help of ANN, which could be a substitute fuel and help to protect the environment.

Keywords: biogas; dual fuel; emissions; diesel; ANN modeling; biomass

1. Introduction

In recent years, the interest in alternate fuels and renewable energy [1] has increased because of an increase in energy demand [2] and stringent environmental policies [3], which are because of the depleting fossil fuels, and an increase in the price of fossil fuels for the internal combustion engine [4]. A compression ignition engine is being used by the transportation sector and holds a major share [5]. It was also observed that conventional compression ignition (CI) engines had higher NO\textsubscript{x} and soot. To control the emissions, exhaust gas recirculation and an after-treatment method (diesel particulate filter, diesel oxidation catalyst, and selective catalytic reduction), or both, were incorporated together. Incorporating these systems in the engine increases the complexity and cost of the engine. Advance combustion concepts and specific fuels were the topics of interest for many
researchers [6]. Energy demand has been increasing [7] and demand for decarbonization is important for the environment [8]. Therefore, an urgent need for alternate fuels is required for the CI engine [9], both liquid as well as gases [10,11]. In the case of IC engines, gaseous alternate fuel can be considered because of their high compression ratio [12] and good mixing characteristics, which in turn would decrease the emission and increase brake thermal efficiency [13].

For the CI engine, advanced combustion strategies such as:

• Reactivity controlled compression ignition (RCCI)
• Homogeneous charge compression ignition (HCCI)
• Partially premixed combustion (PPC) were used

NOx and soot emissions were reduced by partial premix combustion when applied to the IC engine. PPC helped in reducing heat transfer losses and shortened the combustion duration compared to conventional diesel engines. Other researchers mixed low-temperature combustion with alternate fuels (ethanol, butanol, natural gas, butanol, bio-methane, etc.) [14,15]. Bio-methane has been a popular alternate fuel in Poland and Italy. It could be developed from animal slurry, biodegradable waste, and from maize grown on agricultural land [16,17]. This combination showed improvement in NOx, soot emissions and efficiency. Generally, in dual-fuel combustion, one of the fuels is of high reactivity and the other is of low reactivity [18]. Biomethanol, as an alternative fuel in the transport and industrial sector, needs to be investigated [19].

A potential renewable energy is biogas, which could be produced from organic material under natural degradation by micro-organisms without the use of oxygen. Organic substances are converted to biogas by anaerobic digestion, which is used as fuel for vehicles and to generate heat and electricity. Biogas mainly constitutes of methane and carbon dioxide [20]. Biogas for industrial purposes is developed at (1) landfills, (2) agricultural organic waste digestion plants, (3) sewage treatment plants, and (4) sites with industrial processing units [21].

Biogas is environment friendly [22] and is available abundantly [23,24]. The use of biogas in the CI engine is difficult, as there is no spark plug for combustion and ignition. Biogas is also low in cetane number and has a high self-ignition temperature [25]. CO2 composition of biogas helps in combustion at low temperature, which reduces the chance of NOx emission formation at elevated temperature during combustion in dual fuel mode [26,27]. BTE remains unchanged for intermittent loads, whereas, at reduced loads, it decreases and increases at maximum loads [28,29]. Thus, by using biogas as a dual fuel mode [30], smoke and NOx emission were reduced and controlled [31,32].

Karthic et al. used an artificial neural network to foreshow the performance and emission of a diesel engine. The ANN model has input parameters such as the load on the engine, the injection pressure of fuel, fuel flow rate and injection timing of fuel; and the output parameters of the model were brake thermal efficiency and emission. It was evident that the experimental results and the ANN prediction were similar for the dual-fuel engine in terms of emission and performance [33]. Gul et al. obtained the optimum combination of engine speed, operating load and fuel nature by Taguchi DOE in a diesel engine that was run by 100% waste cooking oil and B20 (i.e., 20% biodiesel and 80% diesel). Experimental results and ANN simulation computed the best combination by guaranteeing refinement of the output response factors, thus ratifying the Gray–Taguchi method in curtailing emissions and enhancing combustion and performance simultaneously [34]. To conduct the experiment, Kumar used RSM based on box-Behnken experimental design. For the production of jatropha-algae oil, parameters such as the molar ratio, reaction time, catalyst concentration, and reaction temperature were optimized. The predicted results showed a correlation with the RSM outcomes [35]. Samuel et al. modeled the production of coconut oil ethyl ester by RSM and ANN. It was observed that the predicted yield by ANN agreed with the output of the experiment [36]. Calik et al. (2018) used corn, sunflower and canola biodiesel blends in a diesel engine, injected hydrogen through a manifold inlet and predicted the emission, noise and vibration level with the help of a support vector machine
and artificial neural network. It was concluded that ANN predicted better results than SVM [37]. Najafi et al. (2019) experimented on a CI engine, which was simultaneously run by pilot fuel (oxygenated additive) and main fuel (natural gas). Artificial Neural Network and genetic algorithm modeling were used to reduce emission by establishing the ratio of pilot fuel in respect to biodiesel, gaseous fuel, and additive [38]. Javed et al. used hydrogen fuel with ZnO nano additives biodiesel in a diesel engine. An artificial neural network was utilized to forebode noise with different engine criteria. ANN was also used so that extensive experimentation could be avoided.

This paper examined the performance and emission features under the influence of diesel and biogas used together at varying engine loads at different gas flow rates. The prediction of performance and emission was carried out by an artificial neural network [39]. Biogas was introduced into the combustion chamber through an artificial neural network. The comparative analysis of the prediction and the actual data are presented in this paper.

2. Experimental Setup

DAF8 Kirloskar make, single cylinder engine, four stroke-naturally aspirated, with a power of 6 kW was employed in the experiment. The experimental setup is shown in Figure 1. In India, such single-cylinder CI engines are mostly used in agriculture and for commercially generating electricity applications in rural areas. Table 1 depicts the specification of the CI engine employed for the experiment. Properties of different fuels used for the experiment are enlisted in Table 2 as per the American society for testing and materials (ASTM) standards. Table 3 describes biogas and its composition that was produced locally from vegetable and fruit waste along with animal leftovers. After a 45 to 60 day cycle, biogas was formed by anaerobic fermentation of the waste materials. The introduction of the gas mixture at the time of suction stroke takes place through the inlet air manifold. Flowmeter was used to evaluate the discharge of biogas, attached at inlet manifold pipe through a venturi meter. The fuel control mechanism regulated the fuel flow in the engine.

![Figure 1. Experimental setup block diagram.](image-url)
Table 1. Engine specification for experimentation.

| Company                              | Kirloskar Oil India Ltd. |
|--------------------------------------|--------------------------|
| Model                                | DAF8                     |
| Bore × stroke                        | 95 × 110 mm              |
| Power                                | 8 BHP                    |
| Speed (RPM)                          | 1500                     |
| Inlet valve opening (degree)         | 4.5°                     |
| Inlet valve closed (degree)          | 35.5°                    |
| Exhaust valve opening (degree)       | 35.5°                    |
| Exhaust valve closed (degree)        | 4.5°                     |
| Injection type                       | Direct Injection         |
| Nozzle opening pressure              | 200 bar                  |
| No. of holes (diesel injector)       | 4                        |
| Cylinder’s                           | 1                        |
| Compression ratio                    | 17.5:1                   |
| Cylinder volume                      | 780 cc                   |
| Static injection timing              | 26° bTDC                 |

Alternator Specifications

| Company                              | Kirloskar Private Limited |
|--------------------------------------|---------------------------|
| Dynamometer                          | AC alternator, 50 Hz, single phase |
| Current rating                       | 21.7 A                    |
| Rated output                         | 5 kVA                     |
| Voltage rating                       | 230 V                     |
| Rated speed                          | 1500 rpm                  |

Boundary Conditions

| Intake temperature                   | Room temperature          |
|--------------------------------------|---------------------------|
| Boost pressure                       | 205–210 bar               |
| Injection quantity                   | 0–10 kg/h                 |
| Injection strategy                   | Single Point              |

Table 2. Fuel attributes.

| Attributes                      | Biogas                          | Diesel                         |
|---------------------------------|---------------------------------|--------------------------------|
| Chemical Composition           | CH₄ (60%), CO₂ (40%) (volume)   | C₁₂H₂₅                          |
| Cetane Number                   | -                               | 45–55                          |
| Density (kg/m³)                 | 1.1                             | 840                            |
| Auto-ignition temperature (K)   | 1086                            | 553                            |
| Lower Calorific Value (MJ/kg)   | 20.67                           | 42                             |
| Stoichiometric air-fuel ratio   | 10                              | 14.92                          |

Table 3. Constitution of biogas.

| Name                | Formula | Amount (%) |
|---------------------|---------|------------|
| Methane             | CH₄     | 50–70      |
| Hydrogen            | H₂      | 5–10       |
| Water Vapor         | H₂O     | 0.3        |
| Carbon Dioxide      | CO₂     | 30–40      |
| Nitrogen            | N₂      | 1–2        |
| Hydrogen Sulfide    | H₂S     | Traces     |

Injection pressure and timing had been kept constant for engine operation under dual-fuel mode because of recommendation by the manufacturer. The experiment was conducted at a steady-state condition and a determined angular speed of 1500 rpm was attained. Standard data were generated with the help of conventional diesel fuel at various engine loads. Engine load was increased by 20% step by step, up to 100% for both the fuel operations. The parameters that were recorded at different engine operations were:
• fuel flow;
• air consumption;
• biogas flow rate;
• temperatures;
• power output;
• exhaust tailpipe emissions.

3. Performance Analysis

In the previous literature, performance characteristics were calculated [40,41] with the help Equations (1)–(3), shown below:

\[
\text{Brake Power} = \frac{\text{Voltage} \times \text{Current}}{\eta \times 1000} \text{KW},
\]

where \( \eta \) = Efficiency.

\[
\text{Brake Thermal Efficiency} = \frac{B.P \times 3600 \times 100}{(n_{\text{bio}} \times C_{\text{bio}} + n_d + C_d)},
\]

where \( n_{\text{bio}} \) and \( n_d \) are mass of biogas (kg/h) and diesel fuel. \( C_{\text{bio}} \) and \( C_d \) are the lower calorific value of biogas (kJ/kg) and diesel fuel (kJ/kg).

\[
\text{Brake Specific Energy Consumption} = \left\{ \frac{\sum (m_{\text{total fuel}} \times CV_{\text{total fuel}})}{\text{Brake Power}(B.P)} \right\} \text{KW},
\]

where \( m_{\text{total fuel}} \) and \( C_{\text{total fuel}} \) are the mass and lower calorific value of the total amount of fuel.

3.1. Exhaust Gas Emissions Analysis

Data recording of the exhaust gas emission was carried out by AVL Digas 444N, connected at the tailpipe. \( \text{O}_2, \text{CO}_2 \) and CO were measured in % vol., NO\textsubscript{x} and HC were measured in gm/kW hr. Equipment AVL 437C evaluated the smoke opacity. ASTM-D6522 protocol was used for the measurement of gas emission.

3.2. Uncertainty Analysis

Table 4 shows the uncertainty percentage that is associated with the measuring equipment. The uncertainty percentage in Table 4 has been enlisted from the equipment specifications as provided by the equipment make after a quality check. During the experiment, different parameters were measured and the error associated with them was calculated with the help of uncertainty analysis equations. Experimental data recording was repeated thrice for an average value and to maintain high accuracy. Uncertainty was calculated as shown by the below Equations (4) and (5) [2,42]:

\[
\text{Overall uncertainty} = \sqrt{\frac{(\text{Fuel flow rate})^2 + (\text{Flow properties})^2 + (\text{CO})^2 + (\text{CO}_2)^2 + (\text{NO}_x)^2 + \text{(HC)}^2 + (\text{Smoke opacity})^2 + (\text{Engine load})^2 + (\text{Temperature indicator})^2}{}}.
\]

\[
= \sqrt{(1.0)^2 + (1.0)^2 + (0.2)^2 + (0.2)^2 + (0.5)^2 + (0.1)^2 + (1.0)^2 + (0.5)^2 + (0.15)^2} = \pm 2.
\]
4. Artificial Neural Network

Artificial neural network was extensively employed for predicting the different thermal applications in this research. ANN can help in the prediction of different characteristics of the engine.

ANN model has many processing elements known as “neurons”, which are similar to the human brain. They are interlinked to each other and data is fed into the neurons and processing is carried out. Weights are defined to the neurons, based on which learning is carried out by the network (i.e., for learning, testing and validation). Mean square error is the performance function on which the ANN model is evaluated. Refinement of the activation level is carried out by determining the error weights [34]. This method of determining the error weights is called feed forward back propagation network. Hidden layers had to be included in the input and output layer because of the non-linear experimental data, therefore, a multilayer neural network was created [43]. The model was trained using Gradient descent with adaptive learning rate (TRAINDA) [44]. Hyperbolic tangent sigmoid (TANSIG), Logarithmic sigmoid (LOGSIG), and Linear (PURELIN) were the transfer functions for the model’s output [45].

5. Data Normalization

The performance of the ANN model depends on the presentation of the input layer data. Input and output data have to be graded to maximize the performance. The model used in this study is a back propagation model. The performance was tremendously affected by scaling of input and output data. The logistic sigmoid transfer function was used to generate data between 0 and 1 [46].

\[
\eta v_i = 2 \times \left( \frac{v_{\text{min}} - v_i}{v_{\text{min}} - v_{\text{max}}} \right) - 1, \quad (6)
\]

\[
\eta v_i = 0.8 \times \left( \frac{v_{\text{min}} - v_i}{v_{\text{min}} - v_{\text{max}}} \right) - 0.1. \quad (7)
\]

Normalization of both the data in the range 0.1–0.9 were carried out using a simple method [47]. Normalization formula used by different literature are shown by Equations (6) and (7), and input and output values were normalized by Equation (7). Before training the model, randomization of data was carried out and 70% of data was selected for model learning. After training the model, authentication was carried by 15% data and the remaining 15% was used for efficacy testing of the model [45,48].

6. Modelling and Simulation

Artificial neural network model was developed by using Matlab R2018. Biogas flow rate and the load were the input for all the experimental trials used in the ANN model. Emission and performance data acquired during the experimental process was used as an output parameter in the model. ANN configuration diagram is shown in Figure 2.
Artificial neural network model was trained in MATLAB R2018 by employing different training algorithms, functions, and changing the neurons in different layers. Tansig (Hyperbolic tangent sigmoid) and Logsig (logarithmic sigmoid) transfer functions were used in the layers of the model. Weights and bias were randomly chosen by MATLAB and initially the network executed 100 iterations. The minimum gradient was $10^{-7}$ and the stopping criteria for the network were 10,000 epochs [45].

To understand the output of the model, a simulation of all input data matching was carried out. The ANN model was evaluated by regression coefficient Equation (8), Mean square error Equation (9) by employing targets and outputs of the model:

\[
\text{Regression Coefficient} = \sqrt{1 - \left( \frac{\sum_{i=1}^{n}(T_i - O_i)^2}{\sum_{i=1}^{n}O_i^2} \right)}, \quad (8)
\]

\[
\text{Mean Squared Error} = \frac{1}{n} \left( \sum_{i=1}^{n}(T_i - O_i)^2 \right). \quad (9)
\]

The two statistical expressions value ($R > 0.98$ and MSE < 0.001) were used together to evaluate the model. After satisfying the iterations, it would be terminated. Figure 3 represents the developed ANN algorithm in MATLAB and the predicted data from the ANN model is given in Table 5.
Table 5. Predicted data from the ANN model.

| S.No | Bio Gas (kg/h) | BSEC (MJ/kWh) Predict | Brake Thermal Efficiency (Predicted) | NOx (g/kWh) Predict |
|------|----------------|------------------------|--------------------------------------|--------------------|
|      |                | 20% Engine Load | 40% Engine Load | 60% Engine Load | 80% Engine Load | 100% Engine Load | 20% Engine Load | 40% Engine Load | 60% Engine Load | 80% Engine Load | 100% Engine Load | 20% Engine Load | 40% Engine Load | 60% Engine Load | 80% Engine Load | 100% Engine Load |
| 1    | 1              | 38.51                | 27.53                | 22.28                | 20.00                | 18.27                | 8.57%                 | 14.92%                 | 18.79%                 | 19.93%                 | 21.99%                |
| 2    | 2              | 41.44                | 29.17                | 22.77                | 20.97                | 18.48                | 8.02%                 | 14.59%                 | 18.50%                 | 19.95%                 | 21.91%                |
| 3    | 3              | 44.81                | 30.79                | 23.06                | 21.93                | 18.97                | 7.49%                 | 14.14%                 | 17.52%                 | 18.99%                 | 21.49%                |
| 4    | 4              | 47.74                | 32.95                | 23.56                | 22.49                | 19.56                | 6.96%                 | 13.68%                 | 17.52%                 | 18.37%                 | 20.86%                |
| 5    | 5              | 50.50                | 35.03                | 24.73                | 23.04                | 20.17                | 5.98%                 | 13.06%                 | 16.05%                 | 17.70%                 | 20.46%                |
| 6    | 6              | 53.51                | 37.04                | 26.10                | 23.84                | 20.86                | 5.54%                 | 12.52%                 | 15.47%                 | 17.59%                 | 20.12%                |
| 7    | 7              | 56.50                | 38.95                | 27.60                | 24.54                | 21.61                | 5.16%                 | 11.86%                 | 14.99%                 | 17.25%                 | 19.79%                |
| 8    | 8              | 61.10                | 40.91                | 29.02                | 25.28                | 22.20                | 4.92%                 | 11.51%                 | 14.43%                 | 16.81%                 | 19.51%                |
| 9    | 9              | 65.25                | 43.07                | 30.19                | 26.02                | 22.71                | 4.75%                 | 11.29%                 | 13.87%                 | 16.38%                 | 19.18%                |
| 10   | 10             | 69.51                | 45.10                | 31.08                | 26.75                | 23.11                | 4.65%                 | 11.06%                 | 12.89%                 | 15.52%                 | 18.50%                |
| 11   | 11             | 72.56                | 46.62                | 33.55                | 27.44                | 23.36                | 4.54%                 | 10.55%                 | 12.33%                 | 15.08%                 | 18.22%                |
| 12   | 12             | 75.49                | 48.78                | 35.32                | 28.54                | 24.56                | 4.36%                 | 9.85%                  | 11.77%                 | 14.65%                 | 17.89%                |
| 13   | 13             | 78.25                | 50.87                | 36.59                | 29.34                | 25.26                | 4.16%                 | 9.48%                  | 11.27%                 | 14.12%                 | 17.54%                |


| S.No | Bio Gas (kg/h) | CO (% Vol) Predicted | Smoke Opacity (% HSU) Predicted |
|------|----------------|----------------------|-------------------------------|
|      |                | 20% Engine Load      | 40% Engine Load               | 60% Engine Load | 80% Engine Load | 100% Engine Load | 20% Engine Load | 40% Engine Load | 60% Engine Load | 80% Engine Load | 100% Engine Load | 20% Engine Load | 40% Engine Load | 60% Engine Load | 80% Engine Load | 100% Engine Load |
| 1    | 1              | 0.312                | 0.119                         | 0.061           | 0.090           | 0.170           | 15.75%          | 23.87%          | 29.89%          | 36.12%          | 44.93%          | 15.75%          | 23.87%          | 29.89%          | 36.12%          | 44.93%          |
| 2    | 2              | 0.320                | 0.128                         | 0.066           | 0.093           | 0.175           | 15.14%          | 23.41%          | 29.03%          | 34.25%          | 42.12%          | 15.14%          | 23.41%          | 29.03%          | 34.25%          | 42.12%          |
| 3    | 3              | 0.320                | 0.127                         | 0.066           | 0.094           | 0.180           | 14.54%          | 22.97%          | 26.97%          | 32.01%          | 41.98%          | 14.54%          | 22.97%          | 26.97%          | 32.01%          | 41.98%          |
| 4    | 4              | 0.324                | 0.135                         | 0.067           | 0.096           | 0.182           | 13.86%          | 22.36%          | 25.78%          | 30.00%          | 38.70%          | 13.86%          | 22.36%          | 25.78%          | 30.00%          | 38.70%          |
| 5    | 5              | 0.330                | 0.137                         | 0.070           | 0.098           | 0.185           | 13.03%          | 21.38%          | 24.09%          | 29.89%          | 40.78%          | 13.03%          | 21.38%          | 24.09%          | 29.89%          | 40.78%          |
| 6    | 6              | 0.331                | 0.140                         | 0.071           | 0.100           | 0.190           | 11.98%          | 20.00%          | 22.03%          | 28.00%          | 37.90%          | 11.98%          | 20.00%          | 22.03%          | 28.00%          | 37.90%          |
| 7    | 7              | 0.337                | 0.142                         | 0.073           | 0.101           | 0.193           | 10.77%          | 18.50%          | 20.46%          | 27.00%          | 36.40%          | 10.77%          | 18.50%          | 20.46%          | 27.00%          | 36.40%          |
| 8    | 8              | 0.340                | 0.147                         | 0.075           | 0.103           | 0.196           | 9.77%           | 16.84%          | 19.91%          | 25.85%          | 34.86%          | 9.77%           | 16.84%          | 19.91%          | 25.85%          | 34.86%          |
| 9    | 9              | 0.345                | 0.150                         | 0.076           | 0.106           | 0.199           | 9.30%           | 15.85%          | 19.19%          | 24.90%          | 33.34%          | 9.30%           | 15.85%          | 19.19%          | 24.90%          | 33.34%          |
| 10   | 10             | 0.346                | 0.155                         | 0.078           | 0.107           | 0.205           | 9.13%           | 14.55%          | 16.90%          | 23.91%          | 31.80%          | 9.13%           | 14.55%          | 16.90%          | 23.91%          | 31.80%          |
| 11   | 11             | 0.350                | 0.159                         | 0.081           | 0.110           | 0.211           | 8.11%           | 13.99%          | 15.75%          | 21.90%          | 30.10%          | 8.11%           | 13.99%          | 15.75%          | 21.90%          | 30.10%          |
| 12   | 12             | 0.353                | 0.162                         | 0.086           | 0.112           | 0.212           | 7.55%           | 12.87%          | 14.47%          | 20.15%          | 27.40%          | 7.55%           | 12.87%          | 14.47%          | 20.15%          | 27.40%          |
| 13   | 13             | 0.357                | 0.167                         | 0.087           | 0.113           | 0.217           | 6.99%           | 12.31%          | 13.92%          | 19.06%          | 25.85%          | 6.99%           | 12.31%          | 13.92%          | 19.06%          | 25.85%          |
| 14   | 14             | 0.362                | 0.176                         | 0.090           | 0.115           | 0.221           | 5.78%           | 11.73%          | 12.77%          | 18.11%          | 24.33%          | 5.78%           | 11.73%          | 12.77%          | 18.11%          | 24.33%          |
| 15   | 15             | 0.367                | 0.184                         | 0.092           | 0.117           | 0.226           | 5.78%           | 11.73%          | 12.77%          | 18.11%          | 24.33%          | 5.78%           | 11.73%          | 12.77%          | 18.11%          | 24.33%          |
7. Results and Discussion

The model was trained with different algorithms and training functions, but the best training algorithm was Levenberge Marquardt and the training function was Tansig (Hyperbolic tangent sigmoid). The Logsig (logarithmic sigmoid) showed the best result with \( R > 0.98 \) and \( \text{MSE} < 0.001 \). The best model was trained by evaluating the mean square error and regression coefficient.

ANN predictions were used for the experimental values with regression coefficient and predictions. ANN predictions were matched with the actual data. Regression coefficient for emission for BSEC, BTE, NO\(_x\), CO, HC and smoke opacity were 0.99939, 0.99866, 0.99699, 0.99942, 0.99706, and 0.99865 respectively.

Figure 4 shows the accuracy of the training data, validation of the data, and test data. The closeness of data points with the Fit line shows that the accuracy of the predicted data and the regression coefficient \( R = 0.99939 \) will be higher. The variation of BSEC at different engine loads is given in Figure 5. From the study, it is clear that BSEC was the highest and as we increase the flow of biogas from 1 kg/h to 15 kg/h, the BSEC increases linearly. At 100% engine load, BSEC was the lowest. The predicted values of BSEC at 20% load 1 kg/h biogas was 38.51 MJ/kWh, whereas at 15 kg/h BSEC was 84.26 MJ/kWh. As the engine load was increased, the BSEC decreased. BSEC at 100% engine load at 1 kg/h was 18.27 MJ/kWh. By increasing the biogas to 15 kg/h, the BSEC increased to 26.00 MJ/kWh. It can be concluded that the increase of biogas flow rate resulted in an overall lower heating value. From the figure, the maximum value was obtained for 20% engine load at 15 kg/h biogas mass flow rate. Figure 6 shows the regression coefficient \( R = 0.99866 \) for BTE predictions for the accuracy of the training data, validation of the data, and test data. A variation of BTE with the variation of the mass flow rate of biogas at different engine loads is given in Figure 7. From the figure, it is clear that BTE is lower at 20% engine load,
whereas at higher engine load BTE also increases. At 20% engine load at 1 kg/h biogas mass flow rate, the value of BTE was 8.57% and on increasing the gas flow rate, the BTE reduced to 3.38%. The highest BTE was at 100% engine load at 1 kg/h biogas flow rate with 21.99% BTE. On increasing the flow rate, the BTE was reduced to 17.54% at 15 kg/h. It could be observed that upon increasing the engine load, BTE increased. It was because poor utilization of gaseous fuel mixture resulted in reduced BTE under dual fuel mode. Figure 8 shows the regression coefficient ($R = 0.99966$) for NO$_x$ prediction. This shows how closely the training data and test data match closely with each other. Variation of NO$_x$ with the variation in the mass flow rate of biogas at different engine loads is given in Figure 9. From the figure, it is clear that at a lower engine load, NO$_x$ emission is higher. At 20% engine load and 1 kg/h biogas flow rate, the value of NO$_x$ was 42.78 g/kWh and on increasing the gas flow rate, it reduced to 19.40 g/kWh. At 100% engine load and 1 kg/h biogas flow rate, NO$_x$ was 14.40 g/kWh and on increasing the flow rate further, it reduces to 1.23 g/kWh. Increasing the engine load reduces the NO$_x$. It further reduces on increasing the biogas flow rate in the engine. It could be justified as the use of biogas diminishes the harmful emissions.

![Figure 4](image-url) **Figure 4.** Accuracy of the target and output data of BSEC using a Regression Coefficient metric.

![Figure 5](image-url) **Figure 5.** Effect on BSEC by change in engine load.
Figure 4. Accuracy of the target and output data of BSEC using a Regression Coefficient metric.

Figure 5. Effect on BSEC by change in engine load.

Figure 6. Accuracy of the target and output data of BTE using a Regression Coefficient metric.

Figure 7. Effect on BTE with change in engine load.

Figure 8. Accuracy of the target and output data of NOx using a Regression Coefficient metric.

Figure 10 shows the regression coefficient of CO emission, i.e., $R = 0.99942$. CO emission increases with an increase in engine load and biogas flow rate. CO emission increases with a decrease in load and increase in biogas flow into the engine, as shown in Figure 11.

At 20% engine load and 1 kg/h biogas flow rate, CO emission was 0.312% Vol, increasing the biogas flow rate to 15 kg/h increases the CO to 0.367% Vol. On increasing the engine load at 1 kg/h biogas flow rate, CO emission were 0.119% Vol, 0.061% Vol, 0.090% Vol, and 0.170% Vol, respectively for 40%, 60%, 80%, and 100% engine load. Increasing the mass...
Figure 7. Effect on BTE with change in engine load.

Figure 8. Accuracy of the target and output data of NO\textsubscript{x} using a Regression Coefficient metric.

Figure 9. Effect on NO\textsubscript{x} with change in engine load.

Figure 10 shows the regression coefficient of CO emission, i.e., $R = 0.99942$. CO emission increases with an increase in engine load and biogas flow rate. CO emission increases with a decrease in load and increase in biogas flow into the engine, as shown in Figure 11. At 20% engine load and 1 kg/h biogas flow rate, CO emission was 0.312% Vol, increasing the biogas flow rate to 15 kg/h increases the CO to 0.367% Vol. On increasing the engine load at 1 kg/h biogas flow rate, CO emission were 0.119% Vol, 0.061% Vol, 0.090% Vol, and 0.170% Vol, respectively for 40%, 60%, 80%, and 100% engine load. Increasing the mass flow rate of biogas in the engine decreases the oxygen supply in the engine, which leads to higher CO emissions.

Figure 11. Effect on CO with change in engine load.

Figure 12 shows the regression coefficient ($R = 0.99706$) for HC prediction. Variation of HC with the variation of the mass flow rate of biogas at different engine loads is given in Figure 13. From the figure, it is clear that HC emissions are lower at lower engine loads. At 20% engine load and 1 kg/h biogas flow rate, the value of HC was 1.18 g/kWh and on increasing the gas flow rate it increases to 2.59 g/kWh. At 100% engine load and 1 kg/h biogas flow rate, the HC was 0.28 g/kWh and on increasing the flow rate further, it increases to 0.47 g/kWh. Increasing the engine load reduces the HC. It increases by increasing the biogas flow rate in the engine. At 15 kg/h biogas flow rate, HC was 2.59, 1.66, 1.18, 1.08, and 0.47 g/kWh for 20%, 40%, 60%, 80%, and 100% engine load, respectively. An increase in HC with an increase in biogas flow rate could be justified by the lower flame velocity of biogas. The regression coefficient for smoke opacity was 0.099865, as shown in Figure 14. Variation of smoke opacity with the variation of the mass flow rate of biogas at different engine loads is given in Figure 15. From the figure, it is clear that smoke opacity increases the engine load. At 20% engine load and 1 kg/h biogas flow rate, smoke opacity was 15.75%. Increasing the biogas flow rate to 15 kg/h reduces the smoke opacity to 5.78%. At 100% engine load, 1 kg/h biogas flow rate smoke opacity was 44.93% and increasing the biogas flow reduced the smoke opacity to 24.33%. A decrease in smoke opacity with
flow rate of biogas in the engine decreases the oxygen supply in the engine, which leads to higher CO emissions.

Figure 10. Accuracy of the target and output data of CO using a Regression Coefficient metric.

Figure 11. Effect on CO with change in engine load.

Figure 12 shows the regression coefficient (R = 0.99706) for HC prediction. Variation of HC with the variation of the mass flow rate of biogas at different engine loads is given in Figure 13. From the figure, it is clear that HC emissions are lower at lower engine loads. At 20% engine load and 1 kg/h biogas flow rate, the value of HC was 1.18 g/kWh and on increasing the gas flow rate it increases to 2.59 g/kWh. At 100% engine load and 1 kg/h biogas flow rate, the HC was 0.28 g/kWh and on increasing the flow rate further, it increases to 0.47 g/kWh. Increasing the engine load reduces the HC. It increases by increasing the biogas flow rate in the engine. At 15 kg/h biogas flow rate, HC was 2.59, 1.66, 1.18, 1.08, and 0.47 g/kWh for 20%, 40%, 60%, 80%, and 100% engine load, respectively. An increase in HC with an increase in biogas flow rate could be justified by the lower flame velocity of biogas. The regression coefficient for smoke opacity was 0.099865, as shown in Figure 14. Variation of smoke opacity with the variation of the mass flow rate of biogas at different engine loads is given in Figure 15. From the figure, it is clear that smoke opacity increases with engine load. At 20% engine load and 1 kg/h biogas flow rate, smoke opacity was 15.75%. Increasing the biogas flow rate to 15 kg/h reduces the smoke opacity to 5.78%. At 100% engine load, 1 kg/h biogas flow rate smoke opacity was 44.93% and increasing the biogas flow reduced the smoke opacity to 24.33%. A decrease in smoke opacity with an increase in biogas is because of the absence of aromatic compounds in the biogas composition.

Figure 12. Accuracy of the target and output data of HC using a Regression Coefficient metric.
8. Conclusions

Performance and emission characteristics of a dual-fueled compression ignition engine were predicted using an artificial neural network, by varying the mass flow rate of biogas. Biogas is a clean fuel (obtained by anaerobic digestion from agricultural wastes) and a better alternative to conventional fuels, which reduces the NOx emissions gases without a major change in the existing diesel engine. ANN helped in predicting the performance and emission characteristics of the CI engine at different biogas mass flow rates. The comparative study shows that the experimental results are clearly identical to the ANN results. Based on the study it was noted that:

- The ANN model was trained using the Levenberg Marquardt algorithm and training function was Tansig (Hyperbolic tangent sigmoid) and Logsig (logarithmic sigmoid).
- The ANN model was evaluated on the basis of the regression coefficient ($R > 0.98$) and Mean squared error ($MSE < 0.0001$).
- BSEC was highest at 20% engine load and as we increase the flow of biogas from 1 kg/h to 15 kg/h BSEC increases linearly. At 20% engine load and 1 kg/h biogas flowrate, BSEC was 38.51 MJ/kWh, whereas at 100% load it was 18.27 MJ/kWh. Increasing the biogas flow rate increases the BSEC to 84.26 MJ/kWh and 26.00 MJ/kWh for 20% engine load and 100% engine load, respectively. It could be justified as an increase in biogas resulted in a lower heating value.
- BTE at 20% and 100% engine load and 1 kg/h biogas flow rate was 8.57% and 21.99%. On increasing the gas flow rate to 15 kg/h, BTE was reduced to 3.38% and 17.54%. Poor utilization of gaseous fuel may be blamed for lower BTE under dual fuel mode.
- NOx prediction showed that at 20% engine load and 1 kg/h biogas flow rate, the value of NOx was 42.78 g/kWh and on increasing the gas flow rate, it reduced to 19.40 g/kWh. At 100% engine load and 1 kg/h biogas flow rate, NOx was 14.40 g/kWh and on increasing the flow rate further, it reduces to 1.23 g/kWh.
- CO emission increases with a decrease in load and an increase in biogas flow into the engine. Biogas decreases the oxygen supply in the engine, which leads to higher CO emissions.
- Prediction showed that the trend of HC was similar to that of the experimental value. Increasing the engine load reduces the HC and it increases on increasing the biogas flow rate in the engine. The lower flame velocity of biogas was the reason for the increase in HC.
- The absence of aromatic compounds in the biogas decreased the smoke opacity with an increase in biogas mass flow rate.

It could be concluded that this study helps in understanding the effect of dual fuel (diesel-biogas) combustion under different load conditions of the engine with the help of ANN, which could be a substitute fuel and help to protect the environment.
a major change in the existing diesel engine. ANN helped in predicting the performance and emission characteristics of the CI engine at different biogas mass flow rates. The comparative study shows that the experimental results are clearly identical to the ANN results. Based on the study it was noted that:

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- BTE at 20% and 100% engine load and 1 kg/h biogas flow rate was 8.57% and 21.99%. On increasing the gas flow rate to 15 kg/h, BTE was reduced to 3.38% and 17.54%. Poor utilization of gaseous fuel may be blamed for lower BTE under dual fuel mode.
- NO\textsubscript{x} prediction showed that at 20% engine load and 1 kg/h biogas flow rate, the value of NO\textsubscript{x} was 42.78 g/kWh and on increasing the gas flow rate, it reduced to 19.40 g/kWh. At 100% engine load and 1 kg/h biogas flow rate, NO\textsubscript{x} was 14.40 g/kWh and on increasing the flow rate further, it reduces to 1.23 g/kWh.
- CO emission increases with a decrease in load and an increase in biogas flow into the engine. Biogas decreases the oxygen supply in the engine, which leads to higher CO emissions.
- Prediction showed that the trend of HC was similar to that of the experimental value. Increasing the engine load reduces the HC and it increases on increasing the biogas flow rate in the engine. The lower flame velocity of biogas was the reason for the increase in HC.
- The absence of aromatic compounds in the biogas decreased the smoke opacity with an increase in biogas mass flow rate.

It could be concluded that this study helps in understanding the effect of dual fuel (diesel-biogas) combustion under different load conditions of the engine with the help of ANN, which could be a substitute fuel and help to protect the environment.

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Nomenclature

ANN  Artificial Neural Network
ASTM  American Society for Testing and Materials
BSEC  Brake Specific Energy Consumption
BTE  Brake Thermal Efficiency
CI  Compression Ignition
CO  Carbon Monoxide
DOE  Design of Experiments
HC  Hydrocarbon
MSE  Mean Squared Error
NOx  Nitrogen Oxides
RSM  Response Surface Methodology
SVM  Support Vector Machines

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