Quantitative Analysis of the Processes and Signaling Events Involved in Early HIV-1 Infection of T Cells

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Abstract

Lymphocyte invasion by HIV-1 is a complex, highly regulated process involving many different types of molecules that is prompted by the virus's association with viral receptors located at the cell-surface membrane that culminates in the formation of a fusion pore through which the virus enters the cell. A great deal of work has been done to identify the key actors in the process and determine the regulatory interactions; however, there have been no reports to date of attempts being made to fully understand the system dynamics through a systemic, quantitative modeling approach. In this paper, we introduce a dynamic mathematical model that integrates the available information on the molecular events involved in lymphocyte invasion. Our model shows that moesin activation is induced by virus signaling, while filamin-A is mobilized by the receptor capping. Actin disaggregation from the cap is facilitated by cofillin. Cofillin is inactivated by HIV-1 signaling in activated lymphocytes, while in resting lymphocytes another signal is required to activate cofillin in the later stages in order to accelerate the decay of the aggregated actin as a restriction factor for the viral entry. Furthermore, stopping the activation signaling of moesin is sufficient to liberate the actin filaments from the cap. The model also shows the positive effect of gelsolin on actin capping by means of the nucleation effect. These findings allow us to propose novel approaches in the search for new therapeutic strategies. In particular, gelsolin inhibition is seen as a promising target for preventing HIV-1 entry into lymphocytes, due to its role in facilitating the capping needed for the invasion. Also it is shown that HIV-1 should overcome the cortical actin barrier during early infection and predicts the different susceptibility of CD4+ T cells to be infected in terms of actin cytoskeleton dynamics driven by associated cellular factors.

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Introduction

The invasion and infection of CD4+ T lymphocytes by human immunodeficiency virus type 1 (HIV-1) is a complex process involving many cellular events that have been the subject of many studies [1]. The accumulated evidence indicates that the actin mobilization that occurs before the formation of the fusion pore plays a central role in this process. In fact, the actin cytoskeleton is deeply involved in the capping of cell-surface receptors for viral infection, which facilitates the interaction with the viral envelope (Env) complex and the subsequent fusion pore formation. However, this is not the only cellular component of importance in the viral infection process. Another main character in this plot is the HIV-1 Env-gp120 viral-surface protein. This element, located in the virus’s outer coat, docks with high affinity at the lymphocyte’s surface CD4 receptor. As a consequence of this interaction, HIV-1 Env-gp120 changes its conformation, exposing other regions of the viral protein responsible for its binding to a second co-receptor, either CCR5 or CXCR4. These bindings trigger a signaling pathway inside the lymphocyte that culminates with the formation of an actin cap in a pole of the cell (hereinafter ‘cap’), driving CD4 and co-receptor co-localization and direct interaction, in an actin-dependent manner. These HIV-1 Env-gp120/CD4-mediated actin and receptor reorganization and capping events have been shown to correlate with the infectivity of the virus [2]. This fact will be a central issue the present study, since we will choose a cap indicator as a measure of HIV-1 infectivity.

Another observed fact is that activated CD4+ T lymphocytes, due to its active cell cycling, are continuously remodeling their actin cytoskeleton. There is ample evidence that the inhibition of the signal transduction or the removal of the intracellular signaling domain of CXCR4/CCR5, did not affect HIV infection [3–6]. However, in resting CD4+ T lymphocytes such inhibition...
diminishes HIV infection [7]. In the same vein it has been shown that resting T cells are more sensitive to actin inhibitors than transformed T cells [8]. All these evidences point out to the fact that while the viral requirement for actin dynamics are universal, the HIV-mediated signaling pathways to the actin activity are cell-line dependent. These facts have been taken into account in this modeling exercise.

The actin mobilization required for cap formation is in turn influenced by other elements. This is the case of moesin, for example, an HIV-1-activated protein that acts as a reversible link between the lymphocyte membrane and the actin filaments [9]. HIV-1-triggered moesin activation promotes the reorganization of cortical F-actin and its subsequent anchoring to the membrane at HIV-1-cell contact points [10]; through this interaction, it facilitates the receptor/co-receptor direct interaction and co-localization. Furthermore, moesin also promotes the polymerization of actin filaments as a nucleation factor [10–12]. Moreover, experimental results show that increasing the total moesin available at the lymphocyte enhances HIV-1 infectivity, while a decrease in the activity of moesin negatively affects the invasion process [10]. During fusion pore formation, moesin has to be deactivated to allow F-actin depolymerization and viral entry [13].

Other key players in these processes are gelsolin, filamin-A and cofilin. Gelsolin is an actin-binding protein with a severing activity on actin filaments, which thus also has an effect on actin mobilization. It is assumed that this severing activity is what underlies the protein’s observed influence on virus infectivity, by driving HIV-1-mediated cortical actin reorganization [14]. Gelsolin acts as a basal restrictive barrier for HIV-1 infection by severing actin to control the appropriate amount of cortical actin to be reorganized together with CD4-CXCR4/CCR5 redistribution to one pole of the cell. Both events are required for limiting early viral infection [14]. In the case of filamin-A, this protein participates in the invasion by linking membrane receptors to the actin cytoskeleton [15]. It has been shown too, that changes in filamin-A activity affects the invasion process of HIV-1 [15].

Finally, the last element to be considered is the actin-severing factor cofilin. This protein is regulated by virus signaling through the CXCR4 co-receptor and LIMK activation that leads to cofilin phosphorylation and inactivation [7,16], thus assuring an intact actin cortex before fusion pore formation. However, the mechanism involved in the activation of cofilin, just at the instant where the fusion pore is formed to allow cortical actin destruction and viral capsid entry, is not well understood. It has been observed that increasing the activity of cofilin enhances the infectivity of HIV-1 on resting lymphocytes, but that this does not have any effect on active lymphocytes [7]. In order to explain these observations, it has been hypothesized that cofilin facilitates cortical actin remodeling after fusion pore formation in resting lymphocytes only; this effect is caused by the impairment of the viral restriction factor at the static cortical actin in resting cells at later stages of the invasion [7,17].

Furthermore, the complexity of this scenario is growing, as recently other actin-associated factors appear to alter early HIV-1 infection. Hence, RNA silencing of debrin decreases F-actin polymerization allowing HIV-1 infection [18], while syntenin-1 polymerises F-actin in a post-fusion step [19]. Although the HIV-1 Env-mediated signaling that activates LIMK-cofilin appears to be more clear after the involvement of PAK1/2 and the role of LIMK in viral-induced actin capping, the factors that lies upstream the RhoA/Rac1-PAK1/2-LIMK-cofilin and syntenin-1 pathways remain poorly understood [19–23]. Similarly, the identity of the kinase that phosphorylates moesin in the ERM-F-actin/receptor complex is unknown [10]. The cap itself, together with the processes described above that lead to its formation, emerges in many studies [1,2,7,10,14,15,24] as one of the main system responses prompted by the HIV-1 signaling.

From this observation it can naturally be derived that any insight into this fairly complex dynamic phenomenon is of foremost interest. Consequently, a great deal of information has been accumulated on the factors influencing the cap formation [7,10,14,15]. The approach followed when gathering the bulk of this information has been determined by the need to isolate the influence of each element considered relevant from that of the others participating in the process. In our view, these attempts to understand cap formation can be complemented by taking an integrated approach, where the activities of most of the key factors already described are simultaneously considered in a quantitative and dynamic framework. This integrated approach is not new in the field, since it has been used to unravel different aspects of HIV-1 infection [25–28]. However, to our knowledge, the present work is the first integrated exercise on the invasion of lymphocytes by HIV-1 during the first stages of the viral cycle.

Following this line of reasoning, the aim of this work is to integrate all available information on the molecules, mechanisms and regulatory features involved in the early lymphocyte invasion process into a dynamic mathematical model. By means of this approach, we aim to achieve a better understanding of the dynamics of the process and the role played by the various molecular components. The model is based on a plethora of experimental observations already made on the functional role of a number of cytoskeleton elements (receptors, enzymes, proteins, etc.) that participate in cytoskeleton reorganization and plasma membrane dynamics. It is this systemic approach that will allow us to model and evaluate the dynamics of the plasma membrane, as well as the role and relative importance of the different cortical structures and signal transduction through the CD4 receptor and CXCR4 or CCR5 co-receptors, which are the viral receptors involved in the generation of the membrane fluidity to promote fusion pore formation, entry and infection.

**Results and Discussion**

The signaling structure involved in the actin mobilization observed throughout the first stages of lymphocyte invasion by HIV-1 has recently been elucidated in great detail (see Liu et al. 2009, [1]). Key actors in these series of events are the CD4 and CXCR4 (or CCR5) membrane receptors, filamin-A and the ERM protein moesin, actin and the severing factor cofilin, as well as gelsolin, another actin-severing factor. In order to unravel the role of each one of these molecules in the process, they have been studied separately [7,10,14,15]. As a result, we have a considerable body of information offering a great deal of insight into the series of coordinated events involved in lymphocyte invasion by HIV-1.

However, the existing descriptions and interpretations are in many cases “element biased”, since there is currently no integrated picture of the process where all the system components are simultaneously considered in a dynamic and quantitative way. In this work, we have tried to fill this gap by proposing a mathematical model where a great deal of the available information about the elements and the interactions among them is organized and integrated in a dynamic fashion (Figure 1).

The model thus obtained has been shown to be a robust and reliable representation of the system under consideration (see Material and Methods). Based on this model and on its subsequent analysis, we have been able to quantify the relative importance of each component for the system.
Relevant processes

Valuable information can be obtained from the values of the processes’ rate constants ($K_n$). Their values tell us about the relative velocity of the processes. In Figure 2 it can be seen that the values of the constants for processes 3, 5, 8, 9, and 13 are almost negligible. This implies that the system dynamics is virtually independent of them.

Processes 3 and 5 represent the spontaneous aggregation and disaggregation, respectively, of filamin to the cap. It thus seems that the dynamics of filamin comes mostly from the induced effect of the receptor capping (process 4).

Process 8 represents the spontaneous disaggregation of actin from the cap. We must therefore conclude that the disaggregation of the cap is due only to the positive signaling from the HIV-1-induced molecules. This model prediction is supported by the observations of Yoder et al. 2008 [7], where they established the influence of cofilin as being determinant of subsequent stages of the invasion process.

Another process which would appear to be of little, if any, relevance is process 9, which describes the activation of moesin by causes other than the HIV-1 induction. Instead, it is the HIV-1-induced activation of moesin which is of foremost importance, as stated by Barrero-Villar et al. 2009 [10].

The last of the processes that would appear to bear little relevance to the system dynamics is the activation of cofilin (process 13). The conclusion to be drawn here is that HIV-1 infection is not due to the activation of cofilin, but rather to the induced inactivation of cofilin (process 12). It should be noted that this is the situation observed in the active lymphocytes. The importance of this process in resting lymphocytes will be analyzed below.

The value of the rate constant of process 11 (the inactivation of moesin) deserves some attention. This constant has the larger
the low values (see Figure 2) of the rate constant. Some authors have claimed that the inactivation of moesin is necessary for the relaxation of the tension in the cap, which allows the virus to enter [10]. Our result shows that intense moesin inactivation is not a requisite for virus entry. Instead, stopping the moesin activation signaling is enough to lead to the disassembling of the actin cap (see Figure 3).

Moesin

The actin mobilization that occurs after activation is mediated by moesin, which activates the association of actin filaments to the lymphocyte membrane at the point of the HIV-1 infection. It has been shown that this process is of foremost importance [10].

Our model was able to reproduce the observation made by Barrero-Villar et al. 2009 [10] regarding the role of moesin during the invasion. This work evaluates the effect of changing the total amount of functional moesin (or overexpressing a dominant negative mutant of moesin) on the peak of activated moesin. As stated above [see the Mathematical Model section], these experiments can be simulated in our model by proportionally modifying the corresponding rate parameter $K_6$, which gives the

Figure 2. Rate constant values of the model processes. Rate constants from 1 to 13 correspond to the processes named from 1 to 13 in Figure 1. Mean values for the 12 selected solutions (see Material and Methods) are represented by the bars; standard deviation measures are included.

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Figure 3. Model fitting and parameter estimation. These panels represent the 12 solutions - one for each of the predicted dynamics - which best predict the experimental ratio between total actin and total moesin as measured by Barrero-Villar et al. 2009 [10] (black solid circles). RECRatio: receptor ratio inside the cap; FILAMINratio: filamin-A ratio inside the cap; MOESINratio + ACTINratio: ratio of moesin within the cap over the total amount of actin and moesin; COFILINi: inactive cofilin ratio with respect to the total amount of cofilin; COFILIna: proportion of active cofilin over the total amount of cofilin; HIV: virus units per lymphocyte. The HIV variable correlates with the intensity of the signal inside the lymphocyte triggered by the virus.

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Figure 4. Model verification of the moesin role on the HIV-1 viral entry process. Panel A shows the total amount of functional moesin on the peak of activated moesin (at 90 minutes after infection) as determined by Barrero-Villar et al. 2009 [10]. Panel B shows the result of the MOESINratio value obtained from the model by modifying the parameter rate $K_6$ (related with the total amount of moesin). The red color refers to N-Moe (a dominant negative N-terminal fragment of the protein which impedes the physiological function of the intact moesin); the black refers to the control conditions and the green to the FL-Moe (an intact form of the protein which increases the total amount of moesin inside the lymphocyte).

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Figure 5. Comparison of the model predictions for two alternative roles of gelsolin in the cap formation. Red bars represent the experimental measurements of actin capping in a control situation or after over-expressing gelsolin. Blue bars represent the model prediction with the standard deviation of all solutions selected (see Material and Methods). A. A set of scenarios is evaluated in the model assuming different actin capping influences of gelsolin. In “a” K7 was increased by 50%, assuming that gelsolin has a negative effect on actin capping. In “b”, K6 was increased to mimic a gelsolin activation on the actin capping by increasing the actin remodeling dynamics. B. Model verification of scenario “b” shown in panel A. The measured and the predicted maximum peak of the capping of receptors on the gelsolin over-expressed cell lines are shown. C. In “a” K6, the parameter that models gelsolin stimulation of actin capping, takes the value of 0.75 times the value in Control; in “b” this figure is 0.5 times.

Gelsolin

Gelsolin, an actin-severing protein related to actin cytoskeleton reorganization, plays a role in the cortical actin reorganization during HIV-1 invasion of lymphocytes.

Although gelsolin is not explicitly represented in the model, it is possible to use the model to predict how changes in gelsolin activity will affect the dynamics of the system. This can be achieved by translating the modified values of gelsolin into the kinetic rate parameter values and observing the predicted system behavior.

To do so, two types of changes should be made simultaneously in the model. First, we should increase the amount of gelsolin. It has been proposed that gelsolin has an actin-severing activity [29], and so this increase can be mimicked in our model by increasing the kinetic rate parameter of the actin disaggregation process 7 (K7; see Figure 1). As an alternative to this proposed role of gelsolin, we also explored another mechanism proposed by García-Expósito et al. [14], which attributes to gelsolin a positive influence on the aggregation rate of actin to the cap. This was represented by an increase in K6.

At the same time, based on the observations by García-Expósito et al. [14], where it is shown that the over-expression of gelsolin decreases the total actin expression by 30%, we changed the total actin activity in the model by reducing by 30% the rate constants of processes 4 and 10, which are the processes activated by actin (see the Mathematical Model section).

In Figure 5, the red bars show the actin capping measurements [14], while the blue bars correspond to the model predictions. Figure 5A shows the results obtained in K7, K6, K4 and K10 following the changes described above.

The “control” condition shows that the model prediction is well within the observed range of values. In scenario “a” the values of K4 and K10 have been lowered by 30% and at the same time K7 has been raised by 50%. In scenario “b” K6 and K10 have been lowered by 30% as before, but in this case, instead of K7, the other simultaneous change was in K6, which was increased by 27%. What can easily be observed is that there is a poor correlation between the experimental data and the data predicted by the model in scenario “a”, but that both sets of results match in scenario “b”. From these observations it can be concluded that our model supports the proposed role of gelsolin as an activator of the actin capping [14,29]. Accordingly, it also supports the actin-severing activity of gelsolin as instrumental in facilitating the aggregation of actin by producing actin filaments of optimum sizes and the appropriate amount of these filaments to be co-localized at virus-cell contact and entry regions.

In the same vein, other evidence provided in García-Expósito et al [14] offers additional support for the model’s insights into the proposed role for gelsolin. It measures the maximum peak of the capping of receptors on the gelsolin over-expressed cell lines. The experimental data (Figure 5B) are compared with the model predictions as described above (scenario “b” of Figure 5A), a good correlation between the experimental and model results can be observed. This model verification lends additional support to the proposed effect of gelsolin on the actin capping. As a whole, we can conclude from our model that gelsolin has two direct effects on actin: one by decreasing the total amount of actin in the lymphocyte and another through promoting the aggregation of actin in the cap.
In the same work [14], it is reported that the inhibition of gelsolin negatively affects the efficiency of the virus-lymphocyte contact, and consequently impedes viral invasion. At the same time, it has been established that the amount of actin present in the cap correlates positively with infectivity [2]. In the following, we will use the actin in the cap as an indicator of the infectivity of the virus to evaluate the effect of inhibiting gelsolin in the model. As in the previous analysis, we will translate a decrease in gelsolin onto the parameters of the model in order to predict the impact of these changes on the actin capping.

Based in our previous conclusion, we can assume that a decrease in gelsolin activity will increase total actin expression (parameters $K_4$ and $K_{10}$) and reduce the rate of aggregation of actin filaments to the cap (process 6; Figure 1). In García-Expósito et al. 2013 [14], it is shown that specific knockdown of endogenous gelsolin (represented in our model as an inhibition of gelsolin function) increases the total actin expression by about 30%. Accordingly, we increased parameters $K_4$ and $K_{10}$ by 30%. Figure 5C shows the actin capping prediction after these changes. The “control” bar is the predicted actin capping level before parameter changes. In scenario “a” we see the actin capping prediction when $K_4$ and $K_{10}$ are raised by 30% and $K_6$ is lowered by 25%, while in scenario “b” $K_4$ and $K_{10}$ remain the same as in “a” but $K_6$ is lowered by 30%. It can be interpreted that when the effect of gelsolin inhibition on the velocity of aggregation of actin (process 6) is above 25%, the infectivity is lower than in the physiological reference conditions, a finding that correlates well with observations [14].

**Filamin-A**

Filamin-A is an actin-crosslinking protein that binds to the CD4 and CXCR4 receptors after being induced by the signaling triggered by the association of the virus [15]. Interestingly for the objectives of this study is the observation that the down-regulation of filamin impairs the infectivity of the virus [Jiménez-Baranda et al. 2007 [15]]. Our model provides us with a tool to explore and explain this observation; for this purpose we will use, as before, the actin capping as an indicator of the infectivity. It is straightforward to simulate a decrease of the total amount of filamin-A ($FILAMIN_a$) in our model. This can be done through a simultaneous decrease in the rate constants of processes 1 and 6 ($K_1$ and $K_6$, respectively), which are regulated by $FILAMIN_a$ (see Figure 1).

**Figure 6. Model evaluation of the role of filamin on virus infectivity.** Red curves and bars refer to the control situation, while the blue ones represent the predicted response after a decrease in the total amount of filamin-A. A. Virus-induced actin aggregation time course. B. Virus infectivity in control and filamin down-regulated conditions according to Jiménez-Baranda et al. 2007 [15].

![](image1)

Figure 6 shows the model prediction after simultaneous reduction in the values of $K_1$ and $K_6$. Figure 6A shows a decrease in the actin capping that correlates fairly well with the experimental observations (Figure 6B). These facts constitute a mechanistic explanation, through the regulatory interactions measured by $K_1$ and $K_6$, of the observed reduction in the infectivity. This observation points to these regulatory interactions as potential therapeutic targets.

**Cofilin**

Cofilin is another of the key players in the HIV-1 infection process. This protein initially appears in its active form ($COFILIN_a$). $COFILIN_a$ stimulates the disaggregation of the actin from the cap through process 7 [see Figure 1] [7,16], thus contributing to the clearance of the cortical actin cap [7,16]. It is only after the pore formation that the inactive [dephosphorylated] form is activated (dephosphorylated) ($COFILIN_p$) [7]. The inactivation of cofilin by the LIMK1 signaling pathway is represented in our model by a signal coming from HIV (process 12; Figure 1), but since this interaction has a limited temporal span, cofilin will be back in its active form at the later stages of the invasion (see panel G in Figure 3).

The model prediction on the behavior of the cofilin during the virus invasion can give us some insight into the role of this protein in the pore formation and the enhancement of HIV-1 infectivity. Vorster et al. 2011 [22] have studied the LIMK1 signaling pathway leading to an early inactivation of cofilin, which promotes actin polymerization (see Figure 1). In the Figure 3G is represented the model predicted dynamics of the active cofilin. It can be seen the early inactivation of cofilin that rapidly falls from 1 to close to zero; behavior that tightly correlates with the sudden increase of the inactive of cofilin (Figure 3F).

Another work showed that knockdown of this LIMK1 signaling pathway decreased actin cap [23]. Again our model was able to reproduce this effect. Figure 7A and 7B displays the dynamics of the active cofilin and actin, respectively, before (black line) and after (red line) a 50% decrease in the strength of the LIMK1 signaling pathway. The model predicts a very slight decrease in the inactivation of cofilin, which, however, is enough to cause a decrease the actin cap to a third of the previous value. This prediction correlates very well with the results of Xu et al. 2012 [23] since it reproduces not only the observed fall in the peak of
The predicted effect of actin polymerization and/or the co-receptor signaling on the activation of cofilin. We included in the model the activation signal on the cofilin in the case of resting lymphocytes and subsequently evaluated the effects on the dynamics of the cap of increasing values of the rate constant $K_{13}$ (rate constant of the activation of cofilin; see Figure 1). It was observed (Figure 7C) that the delay in the actin capping decay becomes less pronounced, thus making the virus invasion more effective (dark blue lines in Figure 7C).

This observation supports the hypothesis presented by different authors [7,22] about the role of co-receptor signaling and serves to clarify and quantify the role and importance of this signal. Also these model results correlate well with the above commented observations about the different actin dynamics and cortical F-actin amounts between non-cycling resting and cycling cell lines [8,14,30,31]. In this concern, chemokine-induced actin cytoskeleton reorganization has been associated to the establishment of HIV-1 latency in infected resting CD4+ T cells [32]. An observation reinforced by the fact that inhibition of chemokine receptor-associated ability to promote intracellular signals diminishes HIV-1 infection of resting CD4+ T cells [7].

The predicted effect of actin polymerization and/or the co-receptor signals on HIV-1 infection could be verified experimentally using related published data. For example, analyzing the effect of the actin-severing activity factor latrunculin A (Lat-A) on the virus infectivity. These results, which are shown in Figure 7D
and thus makes the virus infection less effective. curves in Figure 7C), which negatively affects the invasion process predicts a steeper decay of the actin in the cap (see light blue However, when the signaling intensity increases further, the model increases after a later decay. This trend is in agreement with that implemented in the model correlates with the increasing dosages of Lat-A factor, the infectivity of the virus (taken from Yoder et al. 2008, [7]), indicate that, in conditions of increasing dosages of the Lat-A factor, the infectivity of the virus increases after a later decay. This trend is in agreement with that predicted by our model (Figure 7C), since the increasing signal implemented in the model correlates with the increasing dosages of Lat-A; the initial increase in infectivity after a slight increase of the signal strength corresponds to a lesser delay of the actin cap. However, when the signaling intensity increases further, the model predicts a steeper decay of the actin in the cap (see light blue curves in Figure 7C), which negatively affects the invasion process and thus makes the virus infection less effective.

Considering the role of actin cytoskeleton, later after viral fusion and entry, it has been recently described that HIV-1 anchoring to CD4/CXCR4 or/CCR5 promotes transient actin polymerization in a WAVE2-Arp2/3-dependent manner, thereby favoring intracellular viral migration to the nucleus and therefore HIV-1 infection [33–35]. Hence, RNA interference of endogenous Arp2/3 perturbs actin nucleation and filament branching thereby diminishing viral intracellular trafficking to the nucleus and HIV-1 infection [21,35]. These events related to Arp2/3-mediated actin dynamics on HIV-1 infection occurs later after viral entry, and merit to be analyzed in a different piece of work that could be of relevance to engage with a recently reported work that highlights the importance of the intracellular trafficking of intact viral capsides for HIV-1 infection and immune escape [36]. However, it is possible with the current modelling approach, to simulate the effect on the HIV infection of the inhibition of the WAVE2 signaling. As previously indicated process 12 represents the LIMK signaling that inactivates cofilin. In fact, the WAVE2 signal bifurcates from the LIMK one, although the WAVE2 signaling activates Arp2/3 instead [35]. Process 10 is activated from the same inputs as process 12 but can also be independently activated without inactivating cofilin. On the other hand, this same process 10 activates moesin and thus, induces the aggregation of actin filaments. Since this is a similar effect that the caused by Arp2/3 we could assume that the WAVE2 signaling is represented by this process. Figure 7F shows the model prediction of the effect of reducing the WAVE2 signaling by a 50%. It can be seen that this inhibition causes a reduction of the actin aggregation, an indicator in our model of the HIV infectivity.

Figure 8. Model verification of the cofilin activity decay. Red dots and line represent the dynamics of the active cofilin during the invasion of HIV-1 as determined by Yoder et al. 2008 [7]. These observations are compared with the predicted dynamics (blue line) of the same model variable (Cofα).

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Future modeling exercises on this field through the use of new data not currently available will provide further insight of the role and importance of the WAVE2 signaling.

Finally, we compared the model predictions regarding the dynamics of the inactive cofilin with the experimental observations provided by Yoder et al. 2000 [7]. In Figure 8 it can be seen that there is a decay of this protein as the invasion progresses. Here, the model prediction is close to the experimental data only in the very first moments, after which it deviates significantly. Soon after the first 10 hours the predicted cofilin is above the experimental measurements. But it turns out that, in the light of the model hypothesis, these discrepancies help us gain a better comprehension of the role of the cellular factors that are operating in the invasion process. In our simplified model, it was assumed that cofilin is the only actin-severing factor which is regulated by HIV. However, it has been proposed that another actin-severing factor such as gelsolin might play a significant role in this process [14]. It is thus suggested that the observed discrepancies could be attributed to the role that these, somewhat neglected, actin-severing HIV-1 regulated factors play during invasion.

Our results and model integrate, and also appear to predict some reported evidences that indicate that the virus infection is less effective in resting lymphocytes than in active ones [7,8,17]. Moreover and considering resting lymphocytes, memory CD4+ T cells appear to be more susceptible to be infected by HIV-1 compared to naı ve cells [19,37–41]. Resting CD4+ T cells represent a major reservoir of HIV-1 [39,40], being responsible for viremia when antiretroviral therapy is stopped [40]. All these data could be explained in terms of actin dynamics and cortical F-actin amount, which is different between non-cycling resting and active primary cells or cycling cell lines, with a less or a highly dynamic actin cytoskeleton, respectively [14,30,31]. Therefore, HIV-1-triggered actin signaling seems critical for the infection of primary CD4+ T cells.

Altogether these data and our results prompted us to propose that the our model integrates and quantifies the processes and signaling events involved in early HIV-1 infection of T cells, and supports the role and importance of HIV-1 to overcome the cortical actin barrier for efficiently fuse and infect target cells. The model also predicts the observed different susceptibility of CD4+ T cells to be infected by HIV-1 in terms of their actin cytoskeleton dynamics and the amount of cortical actin reorganized.

Materials and Methods

Model Design

We used the findings and observations on the processes involved in early viral entry referred to above to construct a mathematical model of these processes. This representation integrates most of the available information on the components, pathways and regulatory interactions involved in the actin rearrangements and movements during lymphocyte infection by HIV-1. Figure 1 shows, in a schematic form, the selection of variables, processes and signaling features used. Regarding the variables, we distinguish between those components that are integrated within the cap (denoted with subscript c) and those that are outside the cap (subscript n). The data for the HIV variable (from now HIV without the number 1 refers to the variable of the model) have been taken from cultures of lymphocytes [10]; accordingly, this variable is expressed in units of multiplicity of infection (MOI). It should be noted that the HIV is measured as the decay of the effective virus density; thus, this variable represents the intensity of the virus signaling in a lymphocyte culture. Accordingly, the model represents the
invasion at population level. Another relevant observation refers to cofilin. This protein, present in either its active or inactive form (COFILIN\textsubscript{a} and COFILIN\textsubscript{i}, respectively), is measured in our model as the ratio of each form with respect to the total amount of cofilin present (COFILIN\textsubscript{a} and COFILIN\textsubscript{i}).

In Figure 1, the wide arrows (numbered from 1 to 13) represent processes, while the black dashed arrows represent the referenced interactions, all of which are positive, among variables and processes.

The aggregation and disaggregation of the different forms of receptors and co-receptors (REC\textsubscript{nc} and REC\textsubscript{c}) during the HIV-1 junction is represented by processes 1 and 2, respectively. Aggregation process 1 is activated by the cap-aggregated filamin-A (FILAMIN\textsubscript{c}) [15]. Processes 3 and 4 represent two different mobilization mechanisms of filamin-A to the cap. The former represents the non-regulated aggregation of filamin-A into the receptors assumed to be important, while the latter represents the aggregation of filamin-A influenced by the clustered receptors [15]. It has been shown [2,15] that the actin form (ACTIN\textsubscript{c}) enhances aggregation process 4, through the interaction of filamin-A with the actin filaments. Process 5 represents the disaggregation of filamin-A from the cap.

The actin aggregation in the cap (process 6) is stimulated by filamin-A (FILAMIN\textsubscript{c}) [13] and moesin [10]. We assume that the inverse process, the disaggregation of the actin from the cap, can occur either spontaneously (process 8) or be promoted by active cofilin (cofilina) through process 7 [7]. The spontaneous processes of association/disassociation of moesin with actin [10] are represented by processes 9 and 11. The activation of moesin by HIV-1 allows the actin to reorganize into the cell pole where the virus-cell contacts occur. This is where moesin anchors actin to the plasma membrane (this process is referred to as aggregation of moesin). In doing so, it facilitates the reorganization of CD4/CXCR4 or CCR5 receptors and the generation of the membrane tension needed for the virus-cell contacts and the fusion pore formation. During the formation of the fusion pore, moesin is inactivated, which relaxes the interaction of actin with the membrane and allows for the entry of the viral capsid. Process 10 represents the induced activation of moesin (MOESIN\textsubscript{a}) with actin to become MOESIN\textsubscript{nc}. This process is subject to two influences. One is the well-known effect of the virus on the activation process of the moesin to the cap [10]. This is represented through the interaction originating from the variable COFILIN\textsubscript{nc}, which in turn is activated by the HIV signaling. Although this interaction has not been reported at the intracellular level, it has been observed [7,10] that the accumulation of inactive cofilin in a culture occurs earlier than the accumulation of activated moesin. In addition, through this interaction the model is able to represent the observed time delay from the inactivation of cofilin to the activation of moesin.

On the other hand, it has been observed that, as the aggregated actin accumulates, its interaction with MOESIN\textsubscript{i} intensifies, thus exerting a positive influence on the moesin association [2,10]. Process 12 has a more complex meaning. It serves to represent the changes in the virus signaling (measured as a decay of the HIV) as well as the inactivation of COFILIN\textsubscript{a} by the LIMK signaling pathway. We have chosen this form of representation since we want to illustrate the transmission of the signaling from the HIV-1 to the lymphocyte, represented as the inactivation of cofilin. Finally, process 13 represents the spontaneous transformation of the inactive cofilin (COFILIN\textsubscript{i}) into its active form (COFILIN\textsubscript{a}) [7].

The Mathematical Model

The dynamics of the invasion process of lymphocytes by HIV-1 was represented as a set of General Mass Action [42] ordinary differential equations in a mathematical model developed within the Power Law formalism [43]. This formalism allows for non-integer kinetic orders [42,43], but all rates were assumed to be linear. This assumption gives the formulation a mass action shape. A description of how the model equation was derived can be found in the Supporting Information (see equations S1 and S2 in Text S1).

Each of the processes described above (Figure 1; 1 to 13) has a rate kinetic constant parameter; these have been named $K_1$ to $K_{13}$. Figure 3 shows the corresponding values of the selected solutions for the model equations (mean value and standard deviation).

The regulatory interactions of a given variable on a given process (the red, dashed lines in Figure 1) are implemented in the model as having a linear effect on the corresponding rate process (see Text S1); that is, any change in the variable’s value will translate proportionately to the rate of the regulated process. Accordingly, the effect of a change in the total amount of a given component in the model will be simulated in the model by changing the corresponding rate constants of the processes involved.

Experimental Data

The modeling task refers to the initial stages of the infection dynamics just before the virus capsid is introduced inside the lymphocyte. In a culture of lymphocytes this process lasts, on average, 90 minutes [10]. However, it should be noted that the entire process can be completed in just a few seconds in an isolated lymphocyte [10]; thus the rates here have to be interpreted as population rates.

The experimental data were drawn from the work done by Barrero-Villar et al. 2009 [10]. These authors used human activated CD4+/CXCR4 or CCR5 receptors and the generation of the membrane tension needed for the virus-cell contacts and the fusion pore formation. During the formation of the fusion pore, moesin is inactivated, which relaxes the interaction of actin with the membrane and allows for the entry of the viral capsid. Process 10 represents the induced activation of moesin (MOESIN\textsubscript{a}) with actin to become MOESIN\textsubscript{nc}. This process is subject to two influences. One is the well-known effect of the virus on the activation process of the moesin to the cap [10]. This is represented through the interaction originating from the variable COFILIN\textsubscript{nc}, which in turn is activated by the HIV signaling. Although this interaction has not been reported at the intracellular level, it has been observed [7,10] that the accumulation of inactive cofilin in a culture occurs earlier than the accumulation of activated moesin. In addition, through this interaction the model is able to represent the observed time delay from the inactivation of cofilin to the activation of moesin.

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perturbations from the environment, well-adapted systems should be able to conserve homeostasis. Accordingly, any useful biological model has to exhibit this property. A rule of thumb is that any sensitivity value under 1 means that the response of the system to perturbations is adequately controlled and biologically acceptable.

**Conclusions**

The present work is, to our knowledge, the first attempt to model and quantify the complex molecular mechanisms and the dynamics of the key variables involved in early HIV-1 infection of lymphocytes. The model, based on recent findings about these mechanisms, integrates different experimental measurements into a mathematical framework that is able to compress all considered processes simultaneously. The model’s reliability was tested against new sets of experimental data not used for its calibration and parameter estimation and was submitted to sensitivity analysis for assessment of its robustness.

In spite of the data limitations, the verifications carried out on some of the model’s predictions allow us to answer some key questions about the infection process and the role of the interactions involved. The results of the model confirm the important role of moesin in mobilizing and concentrating actin filaments to the contact region of the virus, by linking them to the membrane in response to virus signaling. This means that stopping moesin activation signaling is sufficient for the release of the actin filaments from the cap. Moreover, the model confirms the hypothesis proposed by García-Expósito et al. 2013 [14] by which gelsolin, as an actin-severing factor, can improve the colocalization of actin during the invasion process, thus identifying gelsolin as a promising target to impede the invasion. We also confirmed the role of filament-A in the actin capping by linking it to the receptors influenced by the receptor capping. It is also proposed that later cofilin activation by virus signaling facilitates the entry of the virus in resting lymphocytes by accelerating the decay of the aggregated actin as a restriction factor.

Finally, the works of Barrero-Villar et al. 2009 [10], García-Expósito et al. 2013 [14] and Yoder et al. 2008 [7] put forth the idea of active cortical actin being a factor in restricting the entry of the virus. Our model supports this hypothesis, and at the same time contributes to its understanding by specifying the phenomena by which the cortical actin impedes entry. The model also predicts that there could be actin-severing factors other than cofilin induced by the virus with importance in the entry mechanism, as recently proposed for the PDZ-adaptor protein syntenin-1 that seems to similarly regulate HIV-1 entry at a post-fusion stage [50].

**Supporting Information**

**Figure S1 Dynamic sensitivities respecting the initial conditions of the variables. (TIF)**

**Figure S2 Dynamic sensitivities respecting the parameters of the model.**

(TIF)

**Text S1**

(DOCX)

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**Author Contributions**

Conceived and designed the experiments: GS AV-F NVT. Performed the experiments: GS. Analyzed the data: GS AV-F NVT. Contributed reagents/materials/analysis tools: GS AV-F NVT. Wrote the paper: GS NVT AV-F.

**References**

1. Liu Y, Belkina NV, Shaw S (2009) HIV infection of T cells: Actin-in and actin-out. Sci Signal 2: pe23.

2. Iyengar S (1998) Actin-dependent receptor colocalization required for human immunodeficiency virus entry into host cells. J Virol 72: 5251–5255.

3. Alkhatib G, Locati M, Kennedy PE, Murphy PM, Berger EA (1997) HIV-1 coreceptor activity of CCR5 and its inhibition by chemokines: independence from G protein signaling and importance of coreceptor downmodulation. Virology 241(2): 340–348.

4. Doranz BJ, Orsini MJ, Turner JD, Hoffman TL, Berson JF, et al. (1999) Identification of CXCR4 coreceptors that support CCR5 and chemokine receptor functions. J Virol 73(4): 2732–2741.

5. Gooing J, Montecarlo FS, Ashison RE, Arai H, Tous CL, et al. (1997) Molecular uncoupling of C-C chemokine receptor 5-induced chemotaxis and signal transmission from HIV-1 coreceptor activity PNAS 94(10): 5061–5066.

6. Aramori I, Ferguson SS, Bieniasz PD, Zhang J, Cullen B, et al. (1997) Identification of virally targeted, G protein-coupled receptors as novel coreceptors for HIV-1. Virology 234(2): 352–360.

7. Mangeat P (1999) ERM proteins in cell adhesion and membrane dynamics. J Cell Sci 122: 103–113.

8. Cofilin Activity That Facilitates HIV-1 Infection of Transformed and Resting cells. Cell 134: 782–792.

9. Moesin + filamin-A in the actin capping by linking it to the receptors influenced by the receptor capping. It is also proposed that later cofilin activation by virus signaling facilitates the entry of the virus in resting lymphocytes by accelerating the decay of the aggregated actin as a restriction factor.

10. Barrero-Villar M, Cabrero JR, Gordon-Alonso M, Barroso-Gonzalez J, Alvarez-Losada S, et al. (2009) Moesin is required for HIV-1-induced CD4+CXCR4 interaction, -F-actin redistribution, membrane fusion and viral infection in lymphocytes. J Cell Sci 122: 103–113.

11. Maríck BM, San Miguel-Ruiz JE, Letourneau PC (2012) Activation of Erk/Nadhim/Mosedin mediates active growth cone guidance through regulation of growth cone actin and adhesion receptors. The Journal of Neuroscience: 32: 292–296.

12. Mebger P (2000) Signal-regulated ADP/cofilin activity and growth cone motility. Mol Neurobiol 21: 97–107.

13. Syntenin-1 that seems to similarly regulate HIV-1 entry at a post-fusion stage [50].

14. García-Expósito L, Ziglio S, Barroso González J, de Armas-Rillo L, Valera MS, et al. (2013) Gelsolin activity controls efficient early HIV-1 infection. Retrovirology 10: 39.

15. Jiménez-Baranda S, Gómez-Moutón C, Rosas J, Martínez-Prats L, Mira E, et al. (2007) Filamin-A regulates actin-dependent clustering of HIV receptors. Nat Cell Biol 9: 383–386.

16. Melberg P (2000) Signal-regulated ADP/cofilin activity and growth cone motility. Mol Neurobiol 21: 97–107.

17. Syntenin-1 that seems to similarly regulate HIV-1 entry at a post-fusion stage [50].

18. Gordon-Alonso M, Rocha-Peregrino V, Álvarez S, Ursa A, Izquierdo-Usos A, et al. Actin-binding protein Cdc42 regulates HIV-1 triggered actin polymerization and viral infection. J Biol Chem 2013 Sep 27;288(39):28382–97.

19. Gordon-Alonso M, Rocha-Peregrino V, Álvarez S, Moreno-Gonzalo O, Ursa A, et al. (2012) The PDZ-adaptor protein syntenin-1 regulates HIV-1 entry. Mol Cell 23(12):2253–63.

20. Pontov SE, Heyden NV, Wei S, Ratner L (2004) Actin cytokoskeletal reorganizations and coreceptor-mediated activation of rac during human immunodeficiency virus-induced cell fusion. J Virol 78:7138–7147.

21. Komano J, Miyazaki K, Matsuda Z, Yamamoto N (2004) Inhibiting the Arp2/3 complex limits infection of both intracellular mature vaccinia virus and primate lentiviruses. Mol Biol Cell 15:5197–5207

22. NVT AV-F.
Early HIV-1 Infection Signaling of T Cells

22. Vorster PJ, Guo J, Yoder A, Wang W, Zheng Y, et al. (2011) LIM Kinase 1 Modulated Cortical Actin and CXCR4 Cycling and Is Activated by HIV-1 Viral Infection. J Biol Chem 286(14): 12554–12564.

23. Xu X, Guo J, Vorster PJ, Wu Y (2012) Involvement of LIM kinase 1 in actin polarization in human CD4 T cells. Communicative & Integrative Biology 5(3): 381–383.

24. Mark S, Guo J, Wu Y (2012) The trinity of the cortical actin in the initiation of HIV-1 infection. Retrovirology 9: 45.

25. Dunia R (2013) Mathematical modeling of viral infection dynamics in spherical organs. J Math Biol 67: 1425–1455.

26. Nampala H, Luboobi LS, Mugisha JY, Obua C (2013) Mathematical modeling of liver enzyme elevation in HIV mono-infection. Math Biosci 242: 77–85.

27. Kounyri B, Sadiq SK, Turányi T, Hírmondo R, Müller B, et al. (2013) Gag-pol processing during HIV-1 virion maturation: A systems biology approach. PLoS Computational Biology 9: e1003103.

28. Phillips A (1996) Reduction of HIV concentration during acute infection: Independence from a specific immune response. Science 271: 497–499.

29. Cayota A, Vuillier F, Scott-Algara D, Dighiero G (1990) Preferential replication of HIV-1 in memory CD4+ subpopulation. Lancet 336:941

30. Wang W, Guo J, Yu D, Vorster PJ, Chen W, et al. (2012) A dichotomy in cortical actin and chemotactic actin activity between human memory and naive T cells contributes to their differential susceptibility to HIV-1 infection. J Biol Chem 287: 35455–35469

31. Permanyer M, Pauls E, Badia R, Esté JA, Ballana E (2013) The cortical actin determines different susceptibility of naive and memory CD4+ T cells to HIV-1 cell-to-cell transmission and infection. PLoS One 8(11):e79221.

32. Cameron PU, Saleh S, Sallmann G, Solomon A, Wightman F, et al. (2010) Establishment of HIV-1 latency in resting CD4+ T cells depends on chemokine-induced changes in the actin cytoskeleton. Proc Natl Acad Sci USA 107:16934–16939

33. Spear M, Guo J, Turner A, Weilburg W, Yu D, et al. (2012) Arp2/3-Dependent Nuclear Migration in HIV-1 Infection of CD4 T Cells. Cold Spring Harbor, NY: The 2012 Retroviruses Meeting

34. Spear M, Guo J, Wu Y (2013) Novel anti-HIV therapeutics targeting chemokine receptors and actin regulatory pathways. ImmunoL Rev 250(1): 300–12.

35. Spear M, Guo J, Turner A, Yu D, Wang W, et al. (2014) HIV-1 Triggers WAVE2 Phosphorylation in Primary CD4+ T Cells and Macrophages, Mediating Arp2/3-dependent Nuclear Migration. J Biol Chem 289(10): 6949-6959.

36. Rasaiyaah J, Ping-Tan C, Fletcher AJ, Price AJ, Blondeau C, et al. (2013) HIV-1 evades innate immune recognition through specific cofactor recruitment. Nature 21;503(7476):402–5.

37. Roederer M, Raju PA, Mitra DK, Herzenberg LA, Herzenberg LA (1997) HIV does not replicate in naive CD4 T cells stimulated with CD3/CD28. J Clin Invest 99: 1555–1564.

38. Spina CA, Prince HE, Richman DD (1997) Preferential replication of HIV-1 in the CD45RO memory cell subset of primary CD4 lymphocytes in vitro. J Clin Invest 99: 1774–1785.

39. Schmittman SM, Lane HC, Greenhouse J, Justement JS, Baseler M, et al. (1990) Preferential infection of CD4+ memory T cells by human immunodeficiency virus type 1: evidence for a role in the selective T-cell functional defects observed in infected individuals. Proc Natl Acad Sci USA 87:6058–6062.

40. Chomont N, El-Far M, Ancuta P, Trautmann I, Procopio FA (2009) HIV reservoir size and persistence are driven by T cell survival and homeostatic proliferation. Nat Med;15:893–900

41. Helbert MR, Walter J, L’Age J, Beverley PC (1997) HIV infection of CD45RA+ and CD45RO+ CD4+ T cells. Clin Exp Immunol 107:300–305.

42. Voit E (2000) Computational analysis of biochemical systems. A practical guide for biochemists and molecular biologists. Cambridge, UK: Cambridge University Press. 530 p.

43. Savageau MA (1976) Biochemical systems analysis: A study of function and design in molecular biology. USA: Addison-Wesley, Reading, Mass. 379 p.

44. Vera J, Bachmann J, Pfeifer AC, Becker V, Hormiga JA, et al. (2011) A systems biology approach to analyse amplification in the JAK2-STAT5 signalling pathway-6.

45. Hormiga J, González-Alcón C, Sevilla Á, Cánovas M, Torres N (2010) Quantitative analysis of the dynamic signaling pathway involved in the cAMP mediated induction of l-carnitine biosynthesis in E. coli cultures. Mol Biosyst 6: 690–710.

46. Santos GS, José Hormiga, Paula Arencé, Manuel Cánovas, Néstor Torres (2012) Modelling and analysis of central metabolism operating regulatory interactions in salt stress conditions in a L-carnitine overproducing E. coli strain. PLoS One 7: e34533.

47. Santos GS, Torres NV (2013) New targets for drug discovery against malaria. PLoS One 8: e59968.

48. Frank PM (1978) Introduction to system sensitivity theory. New York: Academic Press.

49. Siljak DD (1969) Nonlinear system. The parameter analysis and design. New York: Wiley.

50. Burnnick L (1997) The crystal structure of plasma gelsolin: Implications for actin severing, capping, and nucleation. Cell 90: 661–670.