EXTENT AND STRUCTURE OF INTERVENING ABSORBERS FROM ABSORPTION LINES REDSHIFTED ON QUASAR EMISSION LINES* 

J. Bergeron¹ and P. Boissé¹

¹ Institut d’Astrophysique de Paris, UPMC - CNRS, UMR 7095, 98 bis Bd Arago, F-75014, Paris, France

e-mail: bergeron@iap.fr

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ABSTRACT

Aims. We wish to study the extent and sub-parsec spatial structure of intervening quasar absorbers, mainly those involving cold neutral and molecular gas.

Methods. We have selected quasar absorption systems with high spectral resolution and a good signal-to-noise ratio data, with some of their lines falling on quasar emission features. By investigating the consistency of absorption profiles seen for lines formed either against the quasar continuum source or on the much more extended (Lyα-Nv, C iv or Lyβ-O vi) emission line region (ELR), we can probe the extent and structure of the foreground absorber over the extent of the ELR (>0.3 – 1 pc). The spatial covering analysis provides constraints on the transverse size of the absorber and thus is complementary to variability or photoionisation modelling studies, which yield information on the absorber size along the line of sight. The methods we used to identify spatial covering or structure effects involve line profile fitting and curve-of-growth analysis.

Results. We have detected three absorbers with unambiguous non-uniformity effects in neutral gas. For the extreme case of the Fe ii absorber at \( z_{abs} = 0.45206 \) towards HE 0001–2340, we derive a coverage factor of the ELR of at most 0.10 and possibly very close to zero; this implies an overall absorber size no larger than 0.06 pc. For the \( z_{abs} = 2.41837 \) C i absorber towards QSO J1439+1117, absorption is significantly stronger towards the ELR than towards the continuum source in several C i and C iv velocity components, pointing to spatial variations of their column densities of about a factor of two and to structures at the 0.1 - 0.01 pc scale. The other systems with firm or possible effects can be described in terms of a partial covering of the ELR, with coverage factors in the range 0.7 - 1. The overall results for cold neutral absorbers imply a transverse extent of about five times the ELR size or smaller, which is consistent with other known constraints. Although not our primary goal, we also checked when possible that singly-ionised absorbers are uniform at the parsec scale, in agreement with previous studies. In Tol 0453–423, we have discovered a very unusual case with a small but clearly significant residual flux for a saturated Fe ii 2600 line at \( z_{abs} = 0.72604 \) seen on Lyα emission, thus with an absorber size comparable to or larger than that of the ELR.

Key words. Quasars: absorption lines – ISM: structure

1. Introduction

Some of the absorption systems detected in distant quasar spectra that are commonly used to investigate the properties of diffuse gas in various environments throughout the universe have been noted to display unexpected properties in the relative strength of absorption lines that are associated with distinct transitions from a given species. In fact, in some systems with broad absorption lines (BAL) or in intrinsic systems, the observed resolved profiles of multiplet lines are clearly inconsistent with models in which the absorber uniformly covers the background source (Barlow & Sargent 1997; Ganguly et al. 1999). This is especially evident when resolved line profiles display a flat core, which indicates saturation together with a non-zero residual flux at the line centre. In BAL systems, such effects can be easily explained by invoking small clumdeits within the disc wind that only partially cover the quasar accretion disc.

A variant of this situation is found when the profile of intervening absorption lines that fall on top of quasar emission features appears to be inconsistent with the profile of lines from the same species that formed against the continuum source alone. One good example is the C i and H2 system at \( z_{abs} = 2.3377 \) towards LBQS 1232+082 (Balashev et al. 2011). The C i 1656 feature arises on the C iv quasar emission line; thus, the background flux at the corresponding wavelength is provided by both the accretion disc that is responsible for the continuum emission and by the C iv emission line region (hereafter ELR), while the C i 1560 line is seen against the continuum source alone. While the accretion disc is no larger than about 100 au (Dai et al. 2010), the ELR is much more extended, with a size in the range 0.1 - 1 pc for luminous quasars (Bentz et al. 2009). Since the C i 1656 feature is weaker than C i 1560, whereas the opposite is expected on the basis of oscillator strength values, one cannot escape the conclusion that the C i absorber is not uniform over the whole background source and covers the extended ELR only partially. A few other systems that display effects of this type have been reported (see, e.g., Krogager et al. 2016; Fathivavsari et al. 2017); we note, however, that the interpretation for some of them remains ambiguous because the presence of unresolved optically thick velocity components might be sufficient to explain the observed line ratio.

When present, these effects imply a lower apparent opacity for the lines that are affected by partial covering. This biases the determination of column densities, \( N \), and Doppler parameters, \( b \). Thus, an immediate objective is to properly take these effects into account in order to obtain correct \( N \) and \( b \) values. A further more essential motivation is related to our knowledge of the

* Based on observations with VLT-UVES and Keck-HIRES
size and internal structure of the associated gaseous clouds. In the intervening systems mentioned above, the peculiar relative strength of absorption lines is related to the finite extent of the background source and more specifically to its composite nature, involving two widely different scale lengths (∼ 100 au and 1 pc). By modelling the profile of absorption lines that fall on or away from quasar emission features, one should then be able to compare the absorber size to these scale lengths.

This approach is especially relevant for molecular or neutral gas (as probed, e.g., by C i lines for high-redshift systems) since cloud sizes in the range 0.1 - 10 pc have been inferred (see Jenkins & Tripp 2011 for Galactic gas and Jorgenson et al. 2010 for high-redshift systems), which is comparable to the ELR size. These scales have been derived from the analysis of C i fine-structure transitions, which provides an estimate of the volume density; the inferred extent is therefore along the line of sight. In contrast, the analysis of partial covering effects yields constraints on the transverse size. Thus, both methods provide independent complementary estimates, and their comparison should lead to a robust estimate of the absorber extent, which is a key parameter for modelling.

The absorption lines induced by an absorber located in front of an extended background source is governed not only by their relative extent, but also by the small-scale structure within the intervening gas. In the interstellar medium of our own Galaxy, small-scale structure in the neutral medium (as traced by C i or Na i) is observed at all scales above about 10 au (Welty 2007; Watson & Meyer 1996). If structure over such small scales is also present in high-redshift galaxies, it should manifest itself through time changes in absorption lines, as argued recently by Boissé et al. (2015). Transverse peculiar velocities of a few 100 km s\(^{-1}\) are expected for the observer, quasars, and intervening galaxies. This implies drifts of the line of sight through the absorber of tens to hundreds of au over a time interval of about 10 years. To date, only tentative variations (3σ significance level) have been observed for neutral (C i) and molecular (H\(_2\)) gas in a damped Ly\(_\alpha\) (DLA) absorber at \(z_{\text{abs}} = 2.05454\) towards FBQS J2340−0053 over a two-year time interval (Boissé et al. 2015, and references therein for other approaches involving quasar pairs or lensed quasars). If internal structure were present in the intermediate 100 au - 1 pc range within distant neutral or molecular absorbers, this would potentially affect the behaviour of absorption lines that are detected on quasar emission features. Thus, a detailed analysis of such absorption lines can provide useful information that complements the information provided by time variation studies.

While these effects have been investigated in many quasar intrinsic systems (see, e.g., Hamann et al. 2011), to our knowledge no systematic study has been performed for intervening systems. Only a few cases have been identified, suggesting that these effects are rare, while given the similarity between the size inferred for the C i absorbers and the ELR extent (Jorgenson et al. 2010), one might expect them to be common. In order to clarify this question and derive useful constraints on the extent and small-scale structure of distant neutral absorbers, we have assembled a sample of C i, Fe i, and H\(_2\) systems detected in quasar spectra with a good signal-to-noise ratio (S/N) and high resolution, and we investigate their properties in a systematic manner.

This paper is organised as follows. In Sect. 2 we describe the various effects that can be expected when an absorber is not uniform over the whole extent of the ELR together with the simplest models that can be used to account for them. We also discuss under which conditions the non-uniformity can be established unambiguously. Section 3 presents the sample we studied and the analysis we performed in order to search for partial covering or structure effects. Our results on the transverse extent of the absorbers are presented in Sect. 4. A discussion together with future prospects are given in Sect. 5.

### 2. Effects due to non-uniform absorbers

#### 2.1. Expected effects

When an absorber is not uniform over the extent of the background source, two alternatives are possible. First, the absorption towards the ELR (that is, seen in a quasar emission line) can be weaker than what is expected on the basis of absorption lines that are detected against the continuum source alone. This corresponds to the classical partial covering effect (Fig. 1ab). In the most extreme situation, the fraction of the ELR that is covered by the continuum emission is small, and the absorption line flux remains essentially unabsorbed (we recall that the size of the ELR is at least two orders of magnitude larger than that of the accretion disc).

Second, the absorption seen against the ELR can be stronger than that detected on the continuum; in Figs. 1c and 1d, we show two configurations corresponding to this alternative. The absorber in Fig. 1c does not absorb the continuum source flux at all and that in Fig. 1d is inhomogeneous, with an average absorption of the emission line flux larger than that of the continuum flux.
2.2. Models

2.2.1. Partial covering model

Several authors have proposed models that can be used to describe absorption by a non-uniform gas layer. The most popular is the partial covering model (Barlow & Sargent 1997; Hamann et al. 1997, Ganguly et al. 1999), in which the absorber is assumed to uniformly cover some fraction of the source with an opacity \(\tau_\lambda\), the remaining fraction being unabsorbed. In this picture, the observed flux writes

\[ F_{\text{obs}}(\lambda) = C_f F_b \exp(-\tau_\lambda) + (1 - C_f) F_b, \]

(1)

where \(F_b\) is the total background flux \((F_b = F_c + F_{\text{elr}},\) with \(F_c\) and \(F_{\text{elr}}\) referring to the continuum and ELR sources, respectively), \(\tau\) is the line opacity and \(C_f\) the covering factor, that is, the fraction of the background flux that is covered by the absorber. In this equation, \(F_b\) varies smoothly with wavelength over the interval covered by the absorption line. The term \(\exp(-\tau_\lambda)\) describes the absorption line profile. The corresponding normalised spectrum is

\[ F_{\text{obs,}\text{norm}}(\lambda) = C_f \exp(-\tau_\lambda) + (1 - C_f). \]

(2)

An immediate consequence of partial covering is that saturated lines do not reach the zero level, but display a non-zero line flux residual (LFR, after Balashev et al. 2011) at their core. For \(\exp(-\tau) \ll 1\), the above relation gives

\[ F_{\text{obs,}\text{norm}}(\text{core}) = \text{LFR} = 1 - C_f. \]

(3)

For resolved doublet lines of this type, the apparent opacity ratio is no longer equal to the atomic physics value, but reaches unity when both lines are optically thick and a convolution by the instrumental line spread function is taken into account. If lines are not resolved, profile fitting or curve-of-growth analysis of at least two transitions must be used to derive the LFR and \(C_f\) values.

\(C_f\) is determined by the fraction of the ELR and of the continuum flux that is occulted, \(C_{\text{elr}}\) and \(C_{\text{c}}\), respectively, and by the ratio of the emission line to the continuum flux, \(x = F_{\text{elr}}/F_c\), at the wavelength of the absorption feature considered (we follow the notations introduced by Ganguly et al. 1999, except for \(W\), which is commonly used for equivalent widths, for which we adopt \(x\)). From the relation \(C_f F_b = C_{\text{elr}} F_{\text{elr}} + C_{\text{c}} F_c\), we obtain

\[ C_f = \frac{C_{\text{c}} + x C_{\text{elr}}}{1 + x} \quad \text{or, equivalently,} \quad C_{\text{elr}} = \frac{C_f (1 + x) - C_{\text{c}}}{x}. \]

(4)

The configurations shown in Fig. 1ab correspond to \(C_{\text{c}} = 1\) and \(C_{\text{elr}} < 1\), while \(C_{\text{c}} = 0\) and \(C_{\text{elr}} < 1\) correspond to the configuration sketched in Fig. 1c. In practise, the \(x\) value can be estimated by interpolating the continuum measured on the blue and red side of the emission feature at the location of the absorption line (this is performed more accurately if a flux-calibrated spectrum is available). We stress that in this model the absorber is uniform (with the advantage of introducing a minimum number of free parameters) but the covering of the source is not.

2.2.2. Two-value model

The above picture would not be appropriate to describe absorbers in which the opacity towards the continuum source is lower than the value averaged over the entire background source, as in Fig. 1d. In this case, one could instead consider a two-value model involving distinct opacities for the gas in front of the continuum source, \(\tau_c(\lambda)\), and in front of the ELR, \(\tau_{\text{elr}}(\lambda)\) (note that

Ganguly et al. (1999) considered a sort of mixed model in their Appendix A2, involving two opacity values \(\tau_{\text{elr}}\) and \(\tau_c\) together with two covering factors \(C_c\) and \(C_{\text{elr}}\). With the notations introduced above, the observed profile writes

\[ F_{\text{obs}}(\lambda) = F_c \exp(-\tau_c(\lambda)) + F_{\text{elr}} \exp(-\tau_{\text{elr}}(\lambda)), \]

(5)

corresponding to the normalised profile,

\[ F_{\text{obs,}\text{norm}}(\lambda) = \frac{\exp(-\tau_c(\lambda)) + x \exp(-\tau_{\text{elr}}(\lambda))}{1 + x}. \]

(6)

This model, with only two discrete opacity values, \(\tau_c\) in front of the continuum source and \(\tau_{\text{elr}}\) elsewhere may look academic (we note that the partial covering model also assumes two discrete values, \(\tau\) and \(0\), but their spatial distributions are different in the two models). A more realistic picture is that of an absorber displaying spatial fluctuations of the opacity that are due to internal structure within the region probed by the ELR. If the fluctuations remain moderate enough, one may adequately represent the inhomogeneous gas layer by the two parameters \(\tau_c\) and \(\tau_{\text{elr}}\), where \(\tau_{\text{elr}}\) characterises the “effective” (i.e., “equivalent uniform”) absorber intercepted by the ELR. If in this picture the continuum source is located behind a region of low (respectively large) column density, this will result in \(\tau_{\text{elr}} > \tau_c\) (respectively \(\tau_{\text{elr}} < \tau_c\)), and the \(\tau_{\text{elr}}/\tau_c\) ratio can be used as a measure of the deviation from a uniform covering. This two-value model is more flexible than the partial covering picture and can potentially describe a wider range of physical situations. Since the underlying assumptions about the geometry are distinct in these types of models, there is no rigorous correspondence between them. In the optically thin limit, however, one can obtain the \(\tau_c\) and \(\tau_{\text{elr}}\) values corresponding to a given partial covering model (characterised by \(\tau_c\) and \(C_c\)) by using Eqs. (2) and (5) and by setting \(C_{\text{c}} = 1\) as well as \(\tau_{\text{elr}} = \tau_c\) (Eqs. (2) and (5), which do not have the same functional form in general, become equivalent in the \(\tau \ll 1\) limit). As expected, we obtain \(\tau_{\text{elr}} = C_{\text{elr}} \tau_c\), which is the average opacity value over the ELR extent.

If appropriate absorption lines formed against the continuum source can be used to derive \(\exp(-\tau_c(\lambda))\), then in the frame of this model, Eq. (6) provides the absorption profile that one would obtain against the ELR alone,

\[ \exp(-\tau_{\text{elr}}(\lambda)) = \frac{(1 + x) F_{\text{obs,}\text{norm}} - \exp(-\tau_c(\lambda))}{x}, \]

(7)

which potentially allows us to derive \(\tau_{\text{elr}}\) and next to compare it to \(\tau_c\). We note that the above relations are still valid if the convolution by the instrumental line spread function is taken into account.

We finally mention that some other non-uniform models such as the power-law model have been introduced by Arav et al. (2005) in the context of intrinsic absorbers.

2.3. Analysis of absorption lines on quasar emission features

In practise, most of the absorption lines from the systems considered in this paper are only partially spectroscopically resolved or unresolved. Furthermore, they often involve blends of adjacent velocity components for a given transition or blends of various transitions (e.g., those from \(\text{C} \text{I}\) and \(\text{C} \text{I} \star\)). Thus, we need to rely on a line fitting procedure; we used VPFFT10.2 for this purpose, and we adopted the oscillator strength \(f\) values of Morton (2003). If for a given system there is more than one transition

1 http://www.ast.cam.ac.uk/~rhc/vpfft.html
seen against the quasar continuum, they were analysed together to obtain a fit of the normalised spectrum under the assumption of a uniform covering of the background source. This fit ($F_{\text{fit}}(\lambda)$) was then compared to the profile that is observed for the transitions that fall on emission lines. If the latter appear weaker than the prediction drawn from the fit, the partial covering model (with $C_f < 1$) can be used for these transitions. The associated corrected synthetic profile writes

$$F_{\text{fit,corr}}(\lambda) = C_f F_{\text{fit}}(\lambda) + (1 - C_f).$$

(8)

The optimum $C_f$ value, or a lower bound when no evidence of $C_f < 1$ is found, can be obtained by minimizing the $\chi^2$ computed from the difference between the observed and corrected synthetic profiles.

Often, too few lines arising on the continuum alone are available; we therefore simultaneously fit the profile of all transitions that are observed, against both the continuum source and the ELR. We first assume $C_f = 1$ for all lines; if the fit is not satisfactory with, for instance, absorption lines seen on an emission feature that are overfitted, we consider $C_f < 1$ values for those transitions. In this case, the simultaneous fit must be performed after rescaling the observed spectrum near the corresponding lines to account for the fact that only a fraction $C_f$ of the flux is affected by absorption:

$$F_{\text{corr}}(\lambda) = \frac{F_{\text{obs}}(\lambda) - (1 - C_f)}{C_f}.$$

(9)

Again, the optimum $C_f$ value can be obtained by $\chi^2$ minimization (in this case, all transitions are used to compute $\chi^2$).

If the opposite applies and absorption lines detected on quasar emission features appear to be underfitted, the two-value model must be adopted. Once the absorption profiles towards the ELR have been derived from Eq. (6), they can be directly fitted, provided at least two distinct transitions occurring on emission lines are available. This leads to a separate determination of $N$ and $b$ parameters for the gas toward the continuum source and ELR (this case is illustrated in Sect. 3.2.8 by the C1 system at $z_{\text{abs}} = 2.41837$ in QSO J1439+1117).

The curve-of-growth approach can also be used if the absorption involves well-detached velocity components and if no blending of distinct transitions is present. The usual curve-of-growth method implicitly assumes uniform covering of the source. In the presence of partial covering, it follows directly from Eq. (2) that the equivalent width $W'$ becomes

$$W' = \int \left[ 1 - F_{\text{obs}}(\lambda) \right] d\lambda = C_f \int \left[ 1 - e^{-\tau(\lambda)} \right] d\lambda = C_f W,$$

(10)

where $W$ is the value that one would obtain if the source were fully covered. Alternatively, in the framework of the two-value model, Eq. (6) leads to

$$W' = W_0 + x W_{\text{elr}},$$

(11)

where $W_0$ and $W_{\text{elr}}$ are the equivalent widths that one would measure separately towards the continuum and ELR sources, respectively ($W'$ is just the flux-weighted average, as expected).

If enough transitions are available to define a curve of growth for the absorber situated in front of the continuum source (i.e., $W_c$ values), the location of observed $W'$ values for transitions that fall on quasar emission lines relative to this curve will indicate whether the absorption formed against the ELR is weaker or stronger than that against the continuum source ($W' < W_c$, thus $W_{\text{elr}} < W_c$ in the former case and $W' > W_c$, thus $W_{\text{elr}} > W_c$ in the latter).

### 2.4. Reliable identification of non-uniformity effects

We now discuss in which conditions it is possible to unambiguously establish the reality of non-uniformity effects in a quasar absorption system. An obvious difficulty comes from the fact that partial covering of the background source and components with unresolved saturated features can both affect line profiles or equivalent width ratios in the same way.

We first consider two lines from the same species detected on a quasar emission feature and examine whether their relative strength can be used to assess non-uniform covering. If the lines are close to each other in the spectrum (as in the case of a Mg II doublet, for instance) and remain unresolved, both equivalent widths will be affected in a similar way (the two lines are characterised by the same $x$ and hence $C_f$ values) and their ratio unchanged. The situation is more favorable when lines are fully resolved, especially if some display a flat-bottom profile, leading to a direct determination of the LFR and then of $C_f$ (cf. Eq. (3)). Using at least two lines is important to check that the flat bottom is not due to a blend of several unresolved velocity components, even though this is unlikely when the flat core is extended enough because an unrealistic combination of widths, opacities, and component separations would be required to produce a flat profile. There are cases of intervening systems for which the LFR is close to, but different from, zero: this was first reported for H₂ lines (Balashev et al. 2011; see also Sect. 3.3), and we have discovered this effect for Fe II lines (see Sect. 3.2.4).

Systems in which one line (line 1) is seen against the continuum source and the other line (2) over an emission feature provide much better constraints, especially for systems involving (generally unresolved) lines from neutral or molecular gas, which are the main motivation for this paper. In the partial covering model, the equivalent widths are $W'_1 = W_1$ (we assume $C_f = 1$) and $W'_2 = C_f W_2$, where $W_1$ and $W_2$ are the equivalent width values expected for a fully covered source, and their ratio is

$$r' = \frac{W'_2}{W'_1} = C_f \frac{W_2}{W_1}.$$

(12)

If instead line 1 were falling on the emission line, these relations would write $W'_1 = C_f W_1$, $W'_2 = W_2$, and $r' = \frac{W_1}{C_f W'_2}$. To illustrate the behaviour of $r'$, we consider the C115600 and C11656 transitions; depending on $z_{\text{obs}}$ and $z_m$, these lines can be seen with either C115600 or C11656 appearing on the quasar C IV emission line (see Sect. 3.2.10 for such a case). Assuming an emission line to continuum flux ratio, $x = 0.5$, we plot in Fig. 2 the variation of $r'$ with $C_f$ for Gaussian velocity components with various opacity values, $\tau(\text{C115600})$. The useful part of the diagram corresponds to $C_f > \frac{1}{\tau_{\text{C115600}}}$, the minimum value reached when $C_f \rightarrow 0$. For full covering, the ratio $r' = W'(\text{C115600})/W'(\text{C115600})$ ratio must lie in the range $r'_{\text{min}} < r' < r'_{\text{max}}$ with $r'_{\text{min}} = 1.061$ (the optically thick limit, for which $W$ scales as $\lambda$) and $r'_{\text{max}} = 2.169$ (the thin limit; $W \propto \lambda^2$), which remains true even if unresolved components are present. Thus, if $r'$ values that fall outside this interval are measured, this is necessarily a signature of non-uniform covering. As can be seen in Fig. 2, $r' < r'_{\text{min}}$ can be observed for relatively opaque lines when C11656 appears on the emission line (thick blue lines), whereas $r' > r'_{\text{max}}$ is found for moderate opacities when C115600 coincides with the emission. A similar plot could be made in the two-value model, using $\tau_{\text{elr}}/\tau$, to quantify the non-uniformity of the absorber in front of the quasar source. For each
transition \( i (i = 1 \text{ or } 2) \), one can define the equivalent widths \( W_{c,i} \) and \( W_{elr,i} \); the \( r' \) ratio takes the form
\[
r' = \frac{W_{2}'}{W_{1}'} = \frac{W_{c,2}}{W_{c,1}} \frac{1 + x}{1 + x}, \tag{13}
\]
assuming that line 2 falls on the quasar emission line. \( W_{c,2} / W_{c,1} \) can be inferred from the \( \tau_{elr}/\tau_{c} \) value, provided some assumption is made about the respective \( b \) values for the gas lying in front of the ELR and continuum source (e.g., \( b_{elr} = b_{c} \)).

Still better constraints can be obtained when several transitions are available to model the absorption profile towards the continuum source. An ideal - but rare - situation occurs when two distinct transitions from the same species are seen on quasar emission lines, allowing us to check the consistency of the analysis, especially if \( C_{f} < 1 \) or \( \tau_{elr} \neq \tau_{c} \).

3. Absorber sample and analysis
3.1. Sample of quasars and their absorption systems

The UVES and HIRES data for the quasars we selected to investigate spatial covering of intervening absorbers are all public and have high S/N spectra: UVES (Bergeron et al. 2004; Molaro et al. 2013) and HIRES (Prochaska et al. 2007).

First, we selected quasar absorption systems that trace molecular and cold neutral gas; the species we considered are mainly H\(_{2}\), C, and Fe\(_{i}\). The systems of greatest interest are those where some absorption lines fall on the background quasar emission lines and for species with enough transitions to provide good constraints for line profile fitting.

We then extended our study to a few systems involving moderately ionised gas, mainly C\(_{i}\), Fe\(_{ii}\), Ni\(_{ii}\), and Si\(_{ii}\), for which we wish to check for the absence of substructure at pc scales. Finally, we included the few cases for which the interstellar medium, local or at low redshift, could be studied by its Ca\(_{ii}\) absorption falling on Ly\(\alpha\) or C\(_{iv}\) quasar emission lines.

The quasars under investigation are listed in Table 1. Hereafter, the concordance cosmological model is adopted.

### Table 1. The sample.

| target name\(^a\) | \( z_{em} \) | spectrograph | \( \Delta t \) hr | date     |
|------------------|------------|-------------|----------------|---------|
| HE 0001–2340     | 2.280      | UVES        | 12.0           | 06-08/2001 |
|                  |            | UVES        | 15.0           | 09/2009  |
| PKS 0237–23      | 2.225      | UVES        | 25.3           | 2001-2002 |
|                  |            | UVES        | 18.8           | 2011-2013 |
| Tol 0453–423     | 2.261      | UVES        | 16.2           | 01/2002  |
|                  |            | UVES        | 16.8           | 03-11/2011|
| TXS 1331+170     | 2.089      | UVES        | 8.5            | 03-04/2011|
|                  |            | HIRES(>4220Å) | 10.0          | 04-06/1994|
| QSO J1439+1117   | 2.583      | UVES        | 8.2            | 03/2007  |
| PKS 1448–232     | 2.208      | UVES        | 13.5           | 06-07/2001|
| FBQS J2340–0053  | 2.085      | UVES        | 7.5            | 10/2008  |
|                  |            | HIRES       | 4.2            | 08/2006  |

\( ^{a} \) : Resolved by SIMBAD.

### Fig. 3. Intervening Fe\(_{i}\)2719 absorption at \( z_{abs} = 0.45206 \) (as marked) towards the quasar HE0001–2340. This line falls on the blue wing of the quasar Ly\(\alpha\) emission line. The spectrum (black curve) is shown together with a fit (see Sect. 3.2.3) of three blended Ly\(\alpha\) absorptions, and bluewards, one Si\(_{ii}\) absorption at \( z_{abs} = 1.58643 \) (red curve). The Fe\(_{i}\)2719 absorption is unexpectedly very weak (see Fig. 4).

3.2. Metal systems with absorption line(s) on the quasar Ly\(\alpha\) or C\(_{iv}\) emission lines

In this subsection, we successively describe metal systems involving either neutral gas (as traced by C, Fe, and Ca) or moderately ionised gas. Systems involving diffuse molecular gas are considered in Sect. 3.3.
3.2.1. HE 0001–2340: the Ca \textsc{ii} system at $z_{\text{abs}} = 0.2705$

The Ca\textsc{ii} $\lambda 3934,3969$ doublet falls on the blue wing of the C\textsc{iv} emission line. A differential covering effect is thus possible since the ratios of the emission line to the quasar continuum flux differ for the two transitions: $x($Ca\textsc{ii}$\lambda 3934) = 0.36$ and $x($Ca\textsc{ii}$\lambda 3969) = 0.86$. This is a simple system, with a main component of moderate strength at $z_{\text{abs}} = 0.270515$, partly resolved, and a very weak component blueshifted by $-19.4$ km s$^{-1}$. The fit is good and there is no suggestion of any spatial covering effect; for the main component we obtain $N($Ca\textsc{ii}$) = (3.71 \pm 0.12) \times 10^{11}$ cm$^{-2}$ and $b = 3.38 \pm 0.35$ km s$^{-1}$.

In the red part of the spectrum, the associated Na\textsc{i}$\lambda 5891,5897$ doublet is not detected. In the Ly$\alpha$ forest, there is an associated strong multiple component Mg\textsc{ii} absorption doublet as well as a Fe\textsc{i}$\lambda 2586,2600$ doublet (partly blended).

3.2.2. HE 0001–2340: the Fe\textsc{i} system at $z_{\text{abs}} = 0.45206$

This very peculiar absorber has been studied by D’Odorico (2007) and Jones et al. (2010), with extensive photoionisation modelling. There are associated absorptions by rare neutral species, Si\textsc{i} and Ca\textsc{i}, and these authors concluded that this neutral gas system traces a cold medium ($T \lesssim 100$ K) of high density ($n_H \sim 30 - 1000$ cm$^{-3}$). There are two available UVES spectra, taken about eight years apart (see Table 1); they both have very good S/N, with a higher S/N redwards of Ly$\alpha$ emission for the 2001 spectrum. Our analysis is based on the latter, which was also the spectrum used by D’Odorico and Jones et al. in their studies of this system.

To estimate the column density $N$ and line width $b$ of the $z_{\text{abs}} = 0.45206$ Fe\textsc{i} absorber, we have selected the three stronger well-detected transitions that fall on the quasar continuum in the UVES 2001 spectrum: Fe\textsc{i}$\lambda 3021,3720$ redwards of Ly$\alpha$ emission, and Fe\textsc{i}$\lambda 12484$ (unblended line) in the Ly$\alpha$ forest. A good fit is achieved with a single, unresolved component together with full coverage $C_f = C_z = 1$, and we get $N($Fe\textsc{i}$) = (1.95 \pm 0.25) \times 10^{12}$ cm$^{-2}$ and $b = 0.55 \pm 0.05$ km s$^{-1}$.

There is a very weak Fe\textsc{i}$\lambda 2719$ absorption that falls on the blue side of Ly$\alpha$ emission, in a region where a blend of three Ly$\alpha$ absorptions ($z_{\text{abs}} = 2.24825,2.24876$ and $2.24924$) is present together with, bluewards, one Si\textsc{ii}$\lambda 1526$ ($z_{\text{abs}} = 1.58643$) absorption. A plot of the normalised spectrum of this region is shown in Fig. 3, with a fit of the three Ly$\alpha$ and the Si\textsc{ii} absorptions. The Fe$\textsc{i}$ absorption is unexpectedly very weak, although its oscillator strength $f$ is similar to that of Fe$\textsc{i}$\textsc{ii} (see Fig. 4). This points towards a strong spatial covering effect for this Fe\textsc{i} absorber.

To estimate the spatial coverage factor $C_f$, we renormalised the spectrum around the Fe$\textsc{i}$\textsc{ii}$\lambda 2719$ line, taking the Ly$\alpha$ and Si\textsc{ii} absorptions mentioned above into account to derive the local continuum in this region. This procedure is legitimate because Ly$\alpha$ forest clouds are known to be very large and to display no internal structure at scales comparable to the ELR extent (Rauch et al. 2001). We then used the values of $N$ and $b$ as determined with the three transitions falling on the quasar continuum to fit the renormalised spectrum around the Fe$\textsc{i}$\textsc{ii}$\lambda 2719$ line for different values of $C_f$; the best values of $C_f$ correspond to the minimum of $\chi^2$. It should be noted that the $\chi^2$ of the fit is sensitive to values of $b$. Fig. 5. Curve of growth for the Fe$\textsc{i}$ transitions detected in the $z_{\text{abs}} = 0.45206$ system towards HE 0001–2340. For each point we indicate the rest wavelength of the Fe$\textsc{i}$ transition involved. The smooth curve corresponds to $b = 0.55$ km s$^{-1}$ and log $N($Fe$\textsc{i}) = 12.289$ (see text). The Fe$\textsc{i}$\textsc{ii}$\lambda 2719$ line falls near the top of the quasar Ly$\alpha$ emission and is characterised by a high value of the ELR to continuum flux ratio ($x = 2.31$). We note that the corresponding $W$ measurement lies well below the curve-of-growth expectation because of partial covering of the ELR. The Fe$\textsc{i}$\textsc{ii}$\lambda 3441$ is also characterised by a low $x$ value, and a barely significant shift is seen.
the continuum rms, the latter being inversely proportional to \( C_f \) (cf. Eq. (9)). To minimize the effect of the continuum noise on the \( x^2 \) of the fit around the Fe\( \text{I} \)2719 absorption, we therefore limited the selected wavelength range around this line since the \( C_f \) values are low. We then obtained \( C_f = 0.32 \) and estimate that the uncertainty on this value is about 0.05.

The determination of the coverage factor of the emission line region \( C_{elr} \) requires an estimate of the quasar continuum flux \( F_c \) underlying the Ly\( \alpha \) emission line. There is no low-resolution spectrum of this quasar available at any epoch. Since variability of the Ly\( \alpha \) emission flux is detected even in high-redshift quasars (see, e.g., Woo et al. 2013: SDSS data), we used the 2001 UVES spectrum itself, which was taken in good seeing and clear sky conditions, to measure \( F_c \) and accordingly the flux ratio \( x \). We obtained \( x = 2.31 \), which implies \( C_{f, \text{min}} = 0.30 \) when assuming full coverage of the quasar continuum (\( C_r = 1 \) in Eq. 4). Thus the coverage factor of the ELR is very small: it is consistent with zero, while the coverage factor of the quasar continuum is fully compatible with \( C_r = 1 \). The maximum possible value of \( C_{elr} \) is determined by \( C_{f, \text{max}} = 0.37 \) and equals \( C_{elr, \text{max}} = 0.10 \).

The Fe\( \text{I} \) curve of growth is shown in Fig. 5, adopting the \( b \) and log \( N \) values derived from the three transitions seen on the continuum alone. Some weak lines have been included in addition to those used to obtain the fit displayed in Fig. 4 (Fe\( \text{I} \)2984 and Fe\( \text{I} \)3841 together with Fe\( \text{I} \)3441) in order to better sample the low-opacity end of the curve. The Fe\( \text{I} \)2719 line clearly falls below the curve of growth: the inferred \( C_f \) value, \( C_f = 0.33 \), is fully consistent with the value obtained from the fit of the Fe\( \text{I} \)2719 absorption profile. The Fe\( \text{I} \)3441 line arises on the blue wing of the C\( \text{IV} \) emission line. For this feature, the ELR to continuum flux ratio is low, \( x = 0.22 \), which implies a \( C_f \) value of 0.82 (assuming \( C_{elr} = 0 \) and \( C_r = 1 \) as for the Ly\( \alpha \) ELR). This is close enough to 1 to account for the absence of a significant departure from the curve of growth. In Fig. 6 we show the equivalent width ratio \( r' \) versus \( C_f \) in the partial covering models for the two Fe\( \text{I} \)2719 and Fe\( \text{I} \)3021 transitions. The latter have very similar \( Jf \) values, implying that i) the allowed (\( r'_{\text{min}}, r'_{\text{max}} \)) range for \( C_f = 1 \) is very small, and that ii) \( r' \) depends very little on line opacities (all the curves are nearly coincident, regardless of the value of \( \tau_0(\text{Fe}\text{I}3021) \)). The observed ratio, \( r' = 0.32 \pm 0.05 \), lies well below the possible range for \( C_f = 1 \), showing unambiguously that \( C_f < 1 \) for this system; the inferred \( C_f \) value (corresponding to the blue cross in Fig. 6, where the line \( r' = 0.32 \) intersects theoretical curves) is close to the minimum covering factor associated with \( C_{elr} = 0 \), in agreement with the optimal value derived from line fitting. This figure illustrates that detecting two transitions with similar opacities, one over a quasar emission line and the other against the continuum alone, is a powerful way to establish the reality of partial covering effects.

The Fe\( \text{I} \)3441 transition, which is on the C\( \text{IV} \) emission line, is intrinsically too weak to detect a significant partial covering effect. As mentioned above, its W measurement lies barely below the curve of growth expectation for full spatial covering. In addition, nearly equally good fits were obtained when we added this transition to the three that fall on the quasar continuum assuming either \( C_f = 1 \) or 0.88 (i.e., \( C_{elr} = 0.10 \)); these fits have very similar values of \( N(\text{Fe} \text{I}) \) and \( b \) (the difference is about 5%).

The Mg\( \text{II} \) doublet associated with the Fe\( \text{I} \) system at \( \lambda_{abs} = 0.45206 \) falls on the red wing of the N\( \text{V} \) emission line. Jones et al. (2010) found evidence of partial covering in this Mg\( \text{II} \) system and estimated \( C_f \approx 0.6 \). As discussed in Sect. 2, spatial covering effects are difficult to ascertain in such an unsaturated system because both transitions fall in a small wavelength range and thus have nearly the same associated \( x \) values (we estimate \( x = 0.92 \) at Mg\( \text{II} \)\lambda2796). Furthermore, since the LFR and W ratio lie in the allowed range for \( C_f = 1 \), it should be possible to obtain an acceptable fit that is consistent with \( C_f = 1 \). Using the procedure described above, we obtain a good fit of this doublet assuming full coverage: \( N(\text{Mg} \text{II}) = (1.41 \pm 0.03) \times 10^{12} \text{cm}^{-2} \) and \( b = 2.50 \pm 0.10 \text{ km s}^{-1} \) (which corresponds to \( \tau_0(\text{Mg}\text{II}2796) = 1.5 \)). Equally good fits are achieved down to \( C_f = 0.75 \), which leads to a possible range of the ELR coverage factor, \( 0.48 \leq C_{elr} \leq 1.0 \).

3.2.3. PKS 0237-23: the C\( \text{I} \) system at \( \lambda_{abs} = 1.3650 \)

Srianand et al. (2007) analysed UV (IUE) and 21 cm (GMRT) data to derive \( N(\text{H}\text{I}) \) for this absorber and concluded that this system is a sub-DLA. They also derived abundances by simultaneously analysing (same \( \lambda_{abs} \) and \( b \)) neutral and singly-ionised species; very many components were included in their fit, and the \( b \) values they derived for the C\( \text{I} \) components are in the range 2.5-6.8 km s\(^{-1}\). This is a case for which there are only two available C\( \text{I} \) transitions, each with multiple absorption components: C\( \text{I} \)\lambda1565, which falls at the top of Ly\( \alpha \) emission, and C\( \text{I} \)\lambda1560, which is in a fairly clean region with high S/N of the Ly\( \alpha \) forest. Our fit of the regions around these two transitions includes a C\( \text{IV} \)\lambda1550 absorption at \( \lambda_{abs} = 1.52580 \) bluewards of C\( \text{I} \)\lambda1656, and a weak somewhat broad Ly\( \alpha \) absorption at \( \lambda_{abs} = 2.22263 \) (this Ly\( \alpha \) absorption accounts for some of the C\( \text{I} \) components included in the Srianand et al. paper mentioned above) as well as another weak somewhat broad Ly\( \alpha \) absorption at \( \lambda_{abs} = 2.03427 \) bluewards of C\( \text{I} \)\lambda1560. For the UVES 2001–2002 data, the fit for the main isolated component at \( \lambda = 1.364695 \) and full spatial covering yields \( N(\text{C} \text{I}) = (9.0 \pm 0.2) \times 10^{12} \text{ cm}^{-2} \) and \( b = 4.27 \pm 0.17 \text{ km s}^{-1} \), which

![Fig. 6. Same as in Fig. 2, but for the two Fe\( \text{I} \)2719 and Fe\( \text{I} \)3021 lines seen at \( \lambda_{abs} = 0.4521 \) towards HE 0001–2340. For \( C_f = 1 \), the range allowed for \( r' \) is very small (red horizontal lines). The behaviour of \( r' \) is shown for \( \tau_0(\text{Fe}\text{I}3021) = 1, << 1 \) and \( >> 1 \) (thin blue lines); \( r' \) depends very little on line opacities. The observed ratio, \( r' = 0.32 \pm 0.07 \) (plain black horizontal line, with 1\( \sigma \) uncertainties shown as dotted lines) is clearly outside the allowed range. It implies a value \( C_f \approx 0.33 \) (thick blue cross), compatible with \( C_f = C_{f, \text{min}} \) thus \( C_{elr} = 0 \) (thick black vertical line), irrespective of \( \tau_0(\text{Fe}\text{I}3021) \).](image-url)
Table 2. Systems with absorption line(s) on the quasar Lyα or C iv emission.

| target name   | $z_{em}$ | $z_{abs}$ | element | number transitions | number components | structure effects | $C_f$  | $C_{elr}$ |
|---------------|----------|-----------|---------|--------------------|-------------------|------------------|--------|----------|
| HE 0001−2340 | 2.280    | 0.27052   | Ca ii   | 2                  | 2                 | no               | 1.0    | 1.0      |
|               |          |           | Fe iii  | 5                  | $1 + 1^{b,c}$    | yes              | 0.30–0.37 | 0.0–0.10 |
|               |          |           | Mg ii   | 2                  | 1                 | possible         | 0.75–1.0 | 0.48–1.0 |
| PKS 0237−23  | 2.225    | 1.36469   | C i     | 2                  | 5                 | possible         | 0.80–0.90 | 0.71–0.85 |
|               |          |           | Fe ii   | 5                  | 13                | no               | 1.0    | 1.0      |
| Tol 0453−423 | 2.261    | 0.72604   | Fe ii   | 2                  | $5 + 4$           | yes              | 0.98   | 0.96     |
|               |          |           | Mn ii   | 3                  | 5                 | no               | 1.0    | 1.0      |
| TXS 1331+170 | 2.089    | 0.74461   | Fe iii  | 5                  | 1                 | possible         | 0.80–1.0 | 0.56–1.0 |
|               |          |           | C i     | 6                  | 9                 | no               | 1.0    | 1.0      |
|               |          |           | C i     | 3                  | $2 + 1^{c}$       | possible         | 0.90–1.0 | 0.66–1.0 |
| QSO J1439+1117 | 2.583   | 2.41837   | C i     | 5                  | 7                 | yes              | see text |          |
| PKS 1448−232 | 2.208  | −0.00002  | Ca ii   | 2                  | 10                | no               | 1.0    | 1.0      |
| FBQS J2340−0053 | 2.085 | 2.05454   | C i     | 5                  | 8                 | yes              | 0.85–0.90 | 0.63–0.75 |

$^b$: Blended components.
$c$: Additional component either very weak or noisy.

Fig. 7. Intervening C i absorption towards the quasar PKS 0237−23: spectrum (black curve) and simultaneous fit to the two transitions (red curve). The green curves correspond to a fit with a spatial coverage factor $C_f = 0.85$ of the Lyα emission line. In the bottom panel, bluewards of C i 1560 line (which falls at the top of Lyα emission) C iv 1550 absorption at $z_{abs} = 1.52580$ is present as well as a weak, somewhat broad Lyα absorption. At $v_{b Harvard}$ = 0 km s$^{-1}$, the redshift is $z = 1.364695$.

means that the line is partly resolved. This fit is shown in Fig. 7 (red curve). It is not entirely satisfactory at least for the main isolated component: the transition on the Lyα emission line is overfitted and the transition on the quasar continuum is underfitted, which suggests partial covering. For the other C i, C iv components (weak and mostly blended), the discrepancy between the observation and the fit is not as conspicuous.

We then examined the possibility of a partial covering effect and applied a $C_f$ correction factor to the normalised flux of the Lyα emission region. The best fit, obtained for the minimum $\chi^2$ value, yields $C_f = 0.85(\pm 0.05)$. For the isolated component at $z_{abs} = 1.364695$, we obtain $N(C i) = (1.05 \pm 0.02) \times 10^{13}$ cm$^{-2}$ and $b = 4.09 \pm 0.15$ km s$^{-1}$. The difference in the N values between $C_f = 1$ and 0.85 is significant at the 5σ level. This fit with partial covering is also good for all the other weaker C i, C iv components. The $C_f$ value is consistent with the value obtained for the more recent UVES data (2011-2013), although this spectrum has a lower S/N ratio. The ratio of ELR to quasar continuum flux at C i 1656 equals $x = 2.16$, which implies a coverage factor of the ELR of about $C_{elr} \sim 0.78$.

An alternative model, which assumes full spatial covering of the ELR, involves a narrow additional component that is fully blended with the strong isolated component at $z_{abs} = 1.364695$. The fit of this blend is poorly constrained, especially since the additional component has to be very narrow. A possible fit is $N(C i) = (1.71$ and 0.54) $\times 10^{13}$ cm$^{-2}$ and $b = (0.5$ and 6.4) km s$^{-1}$. Although such a narrow component is not unrealistic, as indeed outlined below for the C i absorber towards TXS 1331+170, this alternative model is not favoured considering the fairly high temperature ($T \gtrsim 1000$ K) inferred from the detailed analysis of Srianand et al. (2007: the discussion of the velocity range B).

The associated Fe ii absorption is highly multiple (13 components). The Fe ii 11608 line is in the Lyα forest, the Fe ii triplet on the continuum redwards of the C iv emission, and the Fe ii 12586,2600 doublet falls on the blue wing of the C iv emission line (the Fe ii 12600 absorption is at the top of the emission line). The component associated with the C i absorber is of moderate strength. For the component at $z_{abs} = 1.364994$, the Fe ii 12382,2600 lines are just about saturated. The fit obtained for the five transitions redwards of the Lyα emission with full spatial covering is very good for all the components.

3.2.4. Tol 0453–423: the Fe ii system at $z_{abs} = 0.7261$

This bright quasar has been extensively used to study its numerous absorption systems at $z_{abs} > 1$ (e.g., Sargent et al. 1979; Kim et al. 2013), but a detailed study of the $z_{abs} = 0.7261$ system has
Fig. 8. Intervening Fe\textsc{ii} absorption towards the quasar Tol 0453−423: spectrum (black curve) and simultaneous fit to the two transitions (red curve), both falling on the quasar Ly\textalpha emission line. The bottom black curve in each panel corresponds to the noise level. The upper panel is a zoom of the lower to clearly show the good fit of the observed spectrum as obtained with a spatial coverage factor $C_f = 0.98$ (green curve). At $v_{\text{helio}} = 0$ km s$^{-1}$, the redshift is $z = 0.72604$.

For our analysis we used the 2002 UVES spectrum, which has high S/N. The Fe\textsc{ii} 2586,2600 doublet of the $z_{\text{abs}} = 0.7261$ system falls on the quasar Ly\textalpha-N\textalpha emission. The profile of the Fe\textsc{ii} 2600 absorption is extremely unusual for a singly-ionised species: as clearly seen in Fig. 8 (top panel), it has a flat bottom, covering about 60 km s$^{-1}$, which does not reach the zero flux level. The flux residual is at the 2.0% level; with an rms of 0.003, this yields a detection at a 7$\sigma$ significance level. The fit obtained with nine components and full spatial covering is inconsistent with the data since the bottom of the Fe\textsc{ii} 2600 absorption should then reach the zero flux level (red curve in Fig. 8). Although the 2011 UVES spectrum has a lower S/N, a similar residual is observed for the Fe\textsc{ii} 2600 absorption (clearer after some smoothing of the data). This effect is very rarely detected for singly-ionised species; another clear example involving Si\textsc{ii} towards LBQS 1232+082 is discussed by Balashev et al. (2011). The derived value of the spatial coverage factor for this Fe\textsc{ii} absorber is $C_f = 0.98$, which for a flux ratio $x = 1.22$ gives a coverage factor of $C_{\text{eff}} = 0.96$. The absorber fully covers the quasar continuum since the Fe\textsc{ii} 2382 absorption line, which is in a clean part of the Ly\textalpha forest, reaches the zero flux level over 100 km s$^{-1}$.

The Mn\textsc{ii} absorption lines associated with this Fe\textsc{ii} system are weak with blended components. The Mn\textsc{ii} 2576 absorption line is at the top of the Ly\textalpha emission line and Mn\textsc{ii} 2606 is at the knee of the Ly\alpha-N\textalpha emission. Only the five components that trace the saturated part of the Fe\textsc{ii} 2600 absorption line have Mn\textsc{ii} counterparts. A good fit of the three Mn\textsc{ii} transitions is obtained with $C_f = 1.0$. Assuming that Mn\textsc{ii} transitions trace the same region as those of Fe\textsc{ii}, that is, adopting the same value of $C_f$, we can estimate the values of $C_f$ for Mn\textsc{ii} 2576 and 2606. Despite the large difference in the values of the flux ratios, $x(2576, 2606) = 3.92$, 1.03, the derived values of $C_f$ are nearly identical $C_f(2576, 2606) = 0.97, 0.98$. This was expected since $C_f$(Fe\textsc{ii}) is very close to unity.

3.2.5. TXS 1331+170: the Fe\textsc{i} system at $z_{\text{abs}} = 0.74461$

Carswell et al. (2011) studied this quasar, but did not discuss this system. The 2011 UVES spectrum has high S/N and high spectral resolution (FWHM = 5.5 Å). There are four well-detected Fe\textsc{i} transitions on the quasar continuum as well as the Fe\textsc{i} 2167 absorption (S/N $\approx$ 50), which falls on the knee of the quasar Ly\alpha-N\textalpha emission. The HIRES spectrum does not cover the Ly\alpha emission region, but the other four transitions on the quasar continuum (Fe\textsc{i} 2484, 2523, 2719, 3021) are well detected. The fit of these transitions involves only one component, and within the uncertainties, the results are identical for the two spectra; for UVES we obtain $N$(Fe\textsc{i}) = $(1.13 \pm 0.03) \times 10^{12}$ cm$^{-2}$ and $b = 1.18 \pm 0.08$ km s$^{-1}$, and for HIRES $N$(Fe\textsc{i}) = $(1.12 \pm 0.05) \times 10^{12}$ cm$^{-2}$ and $b = 1.06 \pm 0.12$ km s$^{-1}$.

The Fe\textsc{i} 2167 absorption is weak (see Fig. 9) and somewhat overfit with the $N$, $b$ values derived for the four transitions on the quasar UVES continuum. Its normalised minimum flux is
also equal to that of the Fe \(\lambda 2719\) absorption, whereas its oscillator strength is greater than that of Fe \(\lambda 2719\) by 23\%. This suggests some spatial covering effect. From the minimum \(\chi^2\) value of the fit we obtain \(C_F \approx 0.8\); this fit is also shown in Fig. 9 (green curve). The flux ratio \(x\) is determined from the UVES data and equals \(x = 0.83\) at the position of the Fe \(\lambda 2167\) absorption, implying a coverage factor of the ELR \(C_{elr} \approx 0.56\). However, this is uncertain since for a full covering of the ELR, the difference between the data and the fit is only about 1.8 times the value of the spectrum rms. A full covering of the ELR therefore cannot be ruled out.

### 3.2.7. TXS 1331+170: the C\(\text{I}\) system at \(z_{abs} = 1.7764\)

The neutral and singly-ionised species of this system were analysed in detail by Carswell et al. (2011), including H\(\text{I}\) (optical and 21 cm data), H\(\text{II}\), and C\(\text{I}\). Old UVES (2002 and 2003) and HIRES data taken at different epochs were combined for this purpose. One of the three detected C\(\text{I}\) components (at \(z_{abs} = 1.77653\)) is very narrow, with \(b = 0.55 \pm 0.13\) km s\(^{-1}\); thus of low kinetic temperature, as confirmed by a curve-of-growth analysis. These authors discussed the possibility that this C\(\text{I}\) cold absorber only partially covers the background source; they concluded that it is most unlikely since the corresponding saturated H\(\text{II}\) transitions have flat cores with zero residual intensities. We note that this is also the case for O\(\text{I}\)\(\lambda 1302\) in the Ly\(\alpha\) forest and C\(\text{II}\)\(\lambda 1334\) on the blue side of the Ly\(\alpha\) emission line.

Only three transitions are well detected in the 2011 UVES spectrum: C\(\text{I}\)\(\lambda 1277\) is in a clean region of the Ly\(\alpha\) forest, C\(\text{I}\)\(\lambda 1328\) is on the blue wing of Ly\(\alpha\) emission, and C\(\text{I}\)\(\lambda 1560\) is on the weak Si\(\text{II}\) emission. The 1994 HIRES spectrum only covers the C\(\text{I}\)\(\lambda 1560,1656\) transitions. It has a somewhat lower resolution (FWHM= 6.25 km s\(^{-1}\)) than the 2011 UVES spectrum (FWHM= 5.5 km s\(^{-1}\)); we therefore did not combine these spectra for data analysis. For a full spatial covering of the background source, we find a low \(b\) value for the \(z_{abs} = 1.77653\) component: \(b = 0.68 \pm 0.18\) and \(0.82 \pm 0.49\) km s\(^{-1}\) for the UVES and HIRES spectra, respectively, both with about the same column density \(N(C) = (1.10 \pm 0.18) \times 10^{13}\) cm\(^{-2}\). This is consistent with the results of Carswell et al. The UVES data and their fit are shown in Fig. 10; the fit includes Al\(\text{II}\)\(\lambda 1862\) absorption at \(z_{abs} = 1.325342\) blueswards of C\(\text{I}\)\(\lambda 1560\).

Constraints on the spatial covering of the ELR by the cold component can only be obtained from the UVES data; we note that the spatial coverage factor should be close to unity since the dif-
Fig. 12. Intervening C\textsc{i} absorption towards the quasar J1439+1117: spectrum (black curve) and simultaneous fit to the four transitions (red curve). The bottom black curve in each panel corresponds to the low noise level (rms=1.7\%). At $v_{\text{helio}} = 0$ km s$^{-1}$, the redshift is $z = 2.418372$: the corresponding C\textsc{i} component has the highest column density. The blue tick marks in the C\textsc{i}1656 panel (lower one) correspond to the stronger seven components. In the C\textsc{i}1560 panel, the two tick marks correspond to weaker components at $-104$ and $-118$ km s$^{-1}$. In the upper panel, the absorption seen in the 50-90 km s$^{-1}$ velocity range is a blend of C\textsc{ii}$\lambda$1276 and C\textsc{i}$\lambda$1277 from the two weak components with the bluest velocity.

The difference between the observations and the fit ($\sim 1.7$ times the rms) for the C\textsc{i}$\lambda$1328 absorption only indicates a slight overfitting. Acceptable fits can also be obtained with a coverage factor for the Ly$\alpha$ emission region $C_{f} \neq 1$ provided that $C_{f} \gtrsim 0.9$ for the C\textsc{i} component at $z_{\text{abs}} = 1.77653$. The flux ratio at the position of the C\textsc{i}$\lambda$1328 transition equals $x = 0.41$, which implies a minimum coverage factor of the ELR $C_{\text{elr}} \gtrsim 0.66$.

Four Ni\textsc{ii} transitions associated with the C\textsc{i} system are detected at $z_{\text{abs}} = 1.7764$. The Ni\textsc{ii}$\lambda$1170 absorption falls on the quasar Ly$\alpha$-N\textsc{v} emission line and Ni\textsc{ii}$\lambda$11709 on the blue wing of the C\textsc{iv} emission. One medium-weak component is located at $z_{\text{abs}} = 1.77640$ and three weak components redwards of this. A good fit is obtained for full spatial covering.

3.2.8. QSO J1439+1117: the C\textsc{i} system at $z_{\text{abs}} = 2.41837$

The UVES spectrum of this quasar has been discussed by Srianand et al. (2008), who detected CO, H$_{2}$, and HD molecules at $z_{\text{abs}} = 2.4184$. Several C\textsc{i} and C\textsc{ii} transitions (around 1276, 1277, and 1280 Å) fall on the red part of the Ly$\alpha$ emission line while the stronger multiplets around 1560 and 1656 Å are seen against the continuum source alone (unfortunately, transitions at $\lambda = 1328$ Å fall in a gap of the spectrum). We first examine whether a model in which the absorber uniformly covers the whole source is consistent with all absorption line profiles. When we attempted to fit the C\textsc{i} and C\textsc{ii} transitions near 1276, 1277, 1280, 1560, and 1656 Å, it clearly appeared that additional absorption is present, blended with the 1277 multiplet (it is presumably Ly$\alpha$ at $z_{\text{abs}} = 2.59213$; when we adopt the emission redshift $z_{\text{em}} = 2.5853 \pm 0.0001$ inferred from SDSS data, this corresponds to a relative velocity of $V = -570$ km s$^{-1}$). We therefore retain only the 1276, 1280, 1560, and 1656 Å multiplets. The simultaneous fit of these four transitions involves seven main velocity components (indicated by blue tick marks in the bottom panel of Fig. 11) that cover a range of 70 km s$^{-1}$. In addition, two weak detached components are also present at $v = -104$ and $-118$ km s$^{-1}$ (these can be seen in the C\textsc{i} 1560 panel and to a lesser extent, in the C\textsc{i} 1280 panel); the corresponding C\textsc{i}$\lambda$1277 features are blended with C\textsc{ii}$\lambda$1276 absorption (upper panel of Fig. 11). Some discrepancies between the observed spectrum and the fit are seen especially near C\textsc{ii} transitions (they are most apparent for the 1280 Å multiplet), and to investigate the possibility of spatial variations over the ELR extent in more detail, we separately fit the 1560 and 1656 Å multiplets (formed against the continuum source) and those at 1276, 1277, and 1280 Å (formed against the ELR and continuum source; the Ly$\alpha$ absorption line mentioned above was included). Comparison of the two fits confirms that C\textsc{ii} absorption tends to be stronger on average towards the ELR than towards the continuum source. The total C\textsc{ii} column density derived from the 1276, 1277, and 1280 Å multiplets, $N$(C\textsc{ii}) = $2.10 \pm 0.11 \times 10^{14}$ cm$^{-2}$, is significantly higher than the value derived from the 1560-1656 multiplets, $N$(C\textsc{ii}) = $1.50 \pm 0.04 \times 10^{14}$ cm$^{-2}$ (the corresponding values for C\textsc{i} are nearly identical, $N$(C\textsc{i}) = $4.1 \times 10^{14}$ cm$^{-2}$). Since the two fits involve velocity components with nearly identical redshifts, it is possible to compare the absorption toward the continuum and that towards the ELR separately. To this purpose, we used Eq. (7) to extract the absorption profile toward the ELR alone for the 1276 and 1280 Å transitions and adopted $x = 3.1$ and 2.0, respectively, as measured on the spectrum.

The result is shown in Fig. 12, where both the ELR absorption computed from Eq. (7) (red curve) and the continuum source absorption derived from fitting the 1560 and 1656 Å transitions are shown (green curve). Absorption clearly tends to be weaker towards the continuum source, especially for C\textsc{ii}. By fitting the 1276 and 1280 Å ELR profiles, we can compare the values of $N$(C\textsc{i}) and $N$(C\textsc{ii}) towards the continuum source and ELR for each component. For C\textsc{i}, only the $v = -10$ km s$^{-1}$ component shows a significant difference, with N(C\textsc{i}) larger towards the ELR by a factor 2.1 $\pm$ 0.15. For C\textsc{ii}, the three central components at $v = -10$, 0, and $+12$ km s$^{-1}$ display a higher column density towards the ELR by factors of 3.0 $\pm$ 0.3, 1.4 $\pm$ 0.1, and 2.1 $\pm$ 0.2, respectively. We conclude that this system shows significant spatial structure at scales in the range of 100 au - 0.1 pc.

3.2.9. PKS 1448–232: the Ca\textsc{ii} system at $z_{\text{abs}} = -0.00002$

The quasar PKS 1448–232 shows strong multicomponent absorption in Galactic Ca\textsc{ii} and Na\textsc{i} (Ben Bekhti et al. 2008). The Ca\textsc{ii} absorption coincides with Ly$\alpha$ and N\textsc{v} emission. The two doublet lines have distinct $x$ values (0.66 and 0.60 for the Ca\textsc{i}$\lambda$3934 and 3969 lines, respectively), which offers the opportunity of investigating non-uniformity effects. Assuming that
Fig. 13. Normalized profile of the C\textsc{i}, C\textsc{i}\,*, and C\textsc{i}\,** lines near 1276 (top panel) and 1280 Å (bottom) at $z_{\text{abs}} = 2.4184$ towards J1439+1117, seen on the Ly\textsc{o} emission line of this quasar. Observed profiles are shown in black, while the profiles derived from fitting of the 1560 and 1656 Å transitions observed against the continuum source are displayed in green and the profiles computed towards the ELR alone (see text) in red. C\textsc{i} lines are presented in green and the profiles from fitting of the 1560 and 1656 Å transitions observed against observed profiles are shown in black, while the profiles derived towards J1439+1117 at $z \approx 1276$ (top panel) and 1280 Å (bottom) at $v = -10,0$ and +12 km s\(^{-1}\)) as well as the C\textsc{i} absorption in the $v = -10$ km s\(^{-1}\) component. The velocity scale is the same as in Fig. 11.

The Ly\textsc{a} ELR has an extent of about 1 pc, it delineates an angle $\theta \approx 10^{-5}$ rad or 0.20 mas, given the quasar emission redshift, $z_{\text{em}} = 2.208$. This corresponds to a very small linear extent of 0.02 au in a galactic cloud located at a distance of about 100 pc. Since significant structure is detected in Galactic Ca\textsc{ii} gas only at scales on the order of 10 au or higher (Smith et al. 2013; McEvoy et al. 2015), the absorber is expected to be uniform and provides a test case for our fitting procedure. An excellent fit is obtained for the whole Ca\textsc{ii} doublet line profiles with $C_f = 1$, which confirms the absence of any departure from uniformity for all pieces of the Galactic gas associated with the five main velocity components.

3.2.10. FBQS J2340–0053: the C\textsc{i} system at $z_{\text{abs}} = 2.05454$

There are two available spectra taken about two years apart (see Table 1). The C\textsc{iv}1560 multiple absorption falls on the top of the C\textsc{iv} quasar emission line; this region is only covered by the HIRES spectrum. A good fit of the C\textsc{i} lines that fall on the quasar continuum (C\textsc{ii}1277,1280,1328 just redwards of the Ly\textsc{a}-N \textsc{v} quasar emission line, and C\textsc{ii}1656) is obtained separately for the HIRES and UVES spectra using eight components and assuming full coverage of the quasar continuum, $C_c = 1$. The estimated values of $N$ and $b$ are consistent between the two epochs, except for the C\textsc{i} component at $z_{\text{abs}} = 2.05472$, for which tentative variation has been reported by Boissé et al. (2015). The physical properties (density and temperature) of this multiple-component absorption system have been thoroughly investigated by Jorgenson et al. (2010) using the C\textsc{i} fine-structure lines and H\textsc{ii} absorption. Their C\textsc{i} fit is solely based on the HIRES data; it includes an unidentified line blended with C\textsc{ii}1328 (Jorgenson: private communication) and does not consider spatial covering effects of the C\textsc{iv} ELR.

Our fit of the HIRES data obtained for the four transitions that fall on the quasar continuum is shown in Fig. 13 for two transitions (C\textsc{ii}1328 and 1656) as well as for C\textsc{ii}1560, which is on the C\textsc{iv} quasar emission line. The C\textsc{ii}1560 and C\textsc{i}\,*1560 multiple-component profiles are both overfitted (Fig. 13 red curve), which points towards partial covering of the C\textsc{iv} emission line region. We then applied a spatial coverage factor to these absorption lines; the best fit is obtained for $C_f = 0.85$ (with an uncertainty of $\pm 0.05$), which is also plotted in Fig. 13 (green curve).

The determination of the coverage factor of the emission line region $C_{\text{elr}}$ requires an estimate of the quasar continuum flux $F_c$, that underlies the C\textsc{iv} emission line. There is a 2004 SDSS low-resolution spectrum of this quasar that we use to derive a flux ratio $\lambda = 0.68$. This yields $C_{\text{elr}} = 0.63$ with a possible range of $0.50 < C_{\text{elr}} < 0.75$.

3.3. Absorption systems with H\textsc{ii} lines on Ly\textsc{a}–O \textsc{vi} emission

- **FBQS J2340–0053**, the H\textsc{ii} absorber at $z_{\text{abs}} = 2.05473$

In this system, numerous transitions from H\textsc{ii} are seen from levels $J = 0$ up to $J = 5$ (Jorgenson et al. 2010). We examined...
the spectrum in detail in the range containing the quasar Lyβ-O vi emission line and found several features from $J = 0$ (at 1049.37 Å), $J = 1$ (at 1049.96 Å), $J = 2$ (1050.37 Å), and $J = 3$ (1041.16 and 1043.51 Å) that reach the zero level at the core of absorption lines associated with the main velocity components (we estimate that the residual flux is lower than about 3% at the 3σ level). This unambiguously indicates that the Lyβ-O vi ELR is fully covered ($C_{\text{elr}} \approx 1$) by both the cold molecular material ($J = 0$ and $J = 1$) and the higher excitation gas ($J \geq 3$) in these velocity components.

Other intervening systems have been studied in the literature for which some constraints can be derived. To our knowledge, the only marked partial covering effect of an ELR by an H₂ absorber has been found at $z_{\text{abs}} = 2.338$ towards LBQS 1232+082 (Ivanchik et al. 2010; Balashev et al. 2011). The covering factor for which some constraints can be derived. To our knowledge, extend beyond the Ct estimate the ELR size, (Trevese et al. 2014, and references therein) can be used to estimate the ELR size, $l_{\text{elr}}$. For instance, applying this relation to HE 0001–2340 obtains an ELR overall size of about 0.3 pc. This value should be appropriate for other quasars as well since all targets in our sample have about the same luminosity and redshift, and since its dependence on luminosity $L$ is moderate (roughly $L^{0.5}$). We note that some fraction of Lyα emission can extend beyond the C iv ELR (Balashev et al. 2011; Fathivavari et al. 2016; Fathivavari et al. 2017).

In the following, when we discuss the constraints derived on the absorber extent, we assume for simplicity that the ELR displays a uniform brightness with the same extent at all relative velocities.

4.2. Extent and structure of neutral absorbers

4.2.1. Unambiguous detections of non-uniform absorbers

We outline the three cases with marked structure effects in neutral gas traced either by Fe i or C i.

- HE 0001–2340, the Fe i absorber at $z_{\text{abs}} = 0.45206$
  
  This is our only clear case of small (<50%) spatial covering of the ELR, corresponding to the configuration shown in Fig. 1a. The analysis of line profiles and the curve-of-growth method both yield a spatial coverage factor $C_\gamma \approx 0.32$ of the Lyα ELR (see Sect. 3.2.2). This value is fully compatible with $C_\gamma$ being at its minimum, $C_{\text{f,min}} \approx 0.30$ (as derived from the measured flux ratio $r_\gamma$; see Figs. 5 and 6), that is, with a spatial coverage of the ELR $C_{\text{elr}} \approx 0$, together with full coverage of the continuum source. An estimate of the maximum value allowed by the data is $C_\gamma \approx 0.37$, implying $C_{\text{elr,max}} \approx 0.10$. The overall extent, $l_{\text{abs}}$, of the absorber must then be quite small. When we take the different redshifts of the absorber and quasar into account (0.3 pc at $z_{\text{em}} = 2.28$ defines the same angle as 0.21 pc at $z_{\text{abs}} = 0.45$), $C_{\text{elr,max}}$ scales as $(l_{\text{abs}}/l_\gamma^2)$, we obtain a maximum absorber overall size $l_{\text{abs}} \approx 0.06$ pc, which is well consistent with the range 0.01 - 0.06pc inferred from modelling by Jones et al. (2010).

The spectroscopic characteristics of this absorber are similar to those of the so-called CaFe clouds (Bondar et al. 2007). The estimate of their physical properties depends on the assumed depletion level: either insignificant, which results in a high gas temperature $T \sim 5000-10000$ K (Gnaciński & Krogulec 2008), or strong, with an assumed high H₂ fraction and low temperature $T < 100$ K (Jones et al. 2010). We did not detect any absorption from CH and CH⁺, although this does not exclude the presence of dust and moderate depletion, as cautioned by Welty et al. (2008).

- QBQS J2340–0053, the C i absorber at $z_{\text{abs}} = 2.41837$
  
  For this system, one C i and three C i⁺ components are found to display higher column density values towards the ELR than to the continuum source, with ratios ranging from 1.4 to 3.0. This means that significant spatial structure must be present at scales in the 100 au - 0.1 pc range, with the continuum source seen through more tenuous and less dense gas at the velocities of these three components. However, since the strongest components nearly reach the zero level in C i, the associated gaseous clouds should cover the whole ELR.

- FBQS J2340–0053, the C i absorber at $z_{\text{abs}} = 2.05473$
  
  This C i multiple absorption system has five well-detected transitions, one of which is on the C iv quasar emission line. The constraints obtained from the analysis of line profiles imply partial covering of the ELR with $C_{\text{elr}} \approx 0.63$ for the C i and C i⁺ components (see Fig. 13). This case corresponds to the configuration shown in Fig. 1b. The minimum size of the absorber, $l_{\text{abs,min}}$, is obtained when the whole absorber covers the ELR, for which we obtain $l_{\text{abs,min}} = 0.79 l_\gamma$. All values above $l_{\text{abs,min}}$ are possible for $l_{\text{abs}}$. This direct constraint on the transverse size can be compared to the indirect estimate derived by Jorgenson et al. (2010) from an analysis of the physical properties of the gas (density in particular). For each main C i component (velocity range 0 - 25 km
sizes, the gas associated with the 1.5 pc, which is quite consistent with our results. For such large sizes, the gas associated with the velocity scale adopted in Fig. 3 from Boissé et al. is different from that in this paper.

4.2.2. Possible detections of non-uniformity effects

We summarize the three cases with possible spatial covering effects for neutral gas traced either by Fe i or C i.

- PKS 0237−23, the C i absorber at \( z_{\text{abs}} = 1.36469 \)

This C i multiple component absorption system has only two detected transitions: one on Ly\( \alpha \) emission, and the other in the Ly\( \alpha \) forest. The narrowest component at \( z_{\text{abs}} = 1.36469 \) is partly resolved (\( b = 4.3 \) km s\(^{-1}\)). The line profile analysis with partial covering of the ELR implies \( C_f = 0.85 \) and \( C_{elr} = 0.78 \), thus a size \( \frac{d_R}{a} \) of about 0.23 pc.

An alternative model involves a ‘hidden’ very narrow component together with full spatial covering of the ELR. The line profile analysis for this narrow component yields a width \( b = 0.5 \) km s\(^{-1}\); this model is not favoured considering the fairly high temperature (\( T \geq 10^4 \) K) inferred for the C i phase.

- TXS 1331+170, the Fe i absorber at \( z_{\text{abs}} = 0.74461 \)

This Fe i single-component absorption system has five well-detected transitions, one of which is on the Ly\( \alpha \)-N\( \nu \) quasar emission line, the latter is weak and somewhat overlit with full spatial covering. A better fit is obtained with \( C_f \approx 0.8 \), thus \( C_{elr} = 0.56 \) for \( x = 0.83 \). However, this is not highly significant considering the small differences in the fits relative to the rms of the spectrum.

- TXS 1331+170, the C i absorber at \( z_{\text{abs}} = 1.77653 \)

Three well-detected transitions are present, one of which is on the blue wing of Ly\( \alpha \) emission: we obtain \( C_f \geq 0.9 \), which for \( x = 0.41 \) yields \( C_{elr} \geq 0.66 \); however, \( C_f = 1.0 \) is fully acceptable. Consequently, this cold C i absorber does not show an unambiguous spatial covering effect, which is consistent with the presence of associated H\( _2 \) saturated absorptions with flat cores and zero residual intensities.

4.2.3. Statistical analysis

We now attempt to extract quantitative information on the neutral absorber extent from results obtained for the whole sample. Clearly, the population is not homogeneous since the Fe i absorber at \( z_{\text{abs}} = 0.452 \) towards HE 0001–2340 covers a negligible fraction of the ELR, while the others cover all or most of it. We therefore exclude the former from our overall analysis. Although the remaining six systems provide poor statistics (we include the Ca ii system towards HE 0001–2340 at \( z_{\text{abs}} = 0.270 \) since Ca ii traces regions containing gas that is mainly neutral), the fact that only one of them shows unambiguous non-uniformity effects tells us that generally, when these absorbers cover the continuum source, they also cover most of the ELR. Their extent must then be notably larger than that of the ELR. In the following, we therefore consider that of the six absorbers that cover the continuum source, at least one displays partial covering with \( C_{elr} \leq 0.75 \), which leads to a probability \( P(C_{elr} \leq 0.75) \geq 0.17. \)

To analyse the implication of this rough estimate in terms of relative size, we assume for simplicity i) that all these six absorbers display a spherical shape with the same radius, \( R_e \), and ii) that the effect of ELR and absorber redshift differences can be ignored (we proceed as if the ELR and absorber had the same redshift). We summarize the three cases with possible spatial covering effects for neutral gas traced either by Fe i or C i.

\[
A = R_e^2 \arccos(y_a) + R_a^2 \arccos(y_e) - H, \tag{14}
\]

with
\[
y_a = \frac{d^2 + R_e^2 - R_a^2}{2dR_a}, \quad y_e = \frac{d^2 + R_e^2 - R_a^2}{2dR_e}, \tag{15}
\]

and
\[
H = \frac{\sqrt{(d(R_e + R_a)^2 - d^2)(d^2 - (R_a - R_e)^2)}}{2}. \tag{16}
\]

Consider for instance a model in which \( R_a = R_e \) and compute the expected probability of obtaining \( P(C_{elr} \leq 0.75) \). Of the absorbers that cover the continuum source (i.e., those that satisfy \( d \leq R_a \)), Eq. (14) implies that only those with \( d \geq 0.40 R_e \) have \( C_{elr} \leq 0.75 \). Then, for \( R_e = R_e \),
\[
P(C_{elr} \leq 0.75) = \frac{\pi R_a^2 - (0.40 R_e)^2}{\pi R_e^2} = 0.84. \tag{17}
\]

The latter value would imply too many absorbers with marked partial covering effects as compared to what we observe. Proceeding in the same way for higher \( R_a/R_e \) values, we find that \( P(C_{elr} \leq 0.75) = 0.17 \), for \( R_a \approx 5 R_e \). The latter value is to be considered as an upper limit for \( R_e \) since some of the systems noted “possible” might show real partial covering. We conclude that a neutral absorber radius of about 0.2 \( \pm 0.75 \) pc or smaller is consistent with the data. Interestingly, these values are in the range (0.2 - 4.7 pc) derived by Jenkins & Tripp (2011) for Galactic C i clouds.

4.2.4. Diffuse molecular gas

C i is known to be nearly cospatial to H\( _2 \) (Srianand et al. 2005), and it is therefore relevant to compare the extent derived for these two species. As discussed above (Sect. 3.3), constraints are available for very few H\( _2 \) absorbers. For the only case in which a marked partial covering effect is found, the absorber towards LBQS 1232+082, the estimated \( C_{elr} \) value (\( > 0.7 \)) is comparable to those obtained for C i absorbers, leading to a lower limit of a few 0.1 pc size.

It is noticeable that for the FBQS J2340–0053 absorber, the excited H\( _2 \) (J = 3) lines display no residual flux. This provides useful constraints for models invoking intermittent turbulent vortices to account for this warmer gas (Godard et al. 2014): although these localized regions are supposed to fill a tiny volumic fraction, their number density and extent must be such that their surface coverage factor is very close to unity.

4.3. Singly-ionised gas

When possible, we searched for structure effects in moderately ionised gas, as traced by species such as Mg ii, Fe ii, and Mn ii. Two such absorbers have been detected in FBQS J2340–0053 absorber, the excited H\( _2 \) (J = 3) lines display no residual flux. This provides useful constraints for models invoking intermittent turbulent vortices to account for this warmer gas (Godard et al. 2014): although these localized regions are supposed to fill a tiny volumic fraction, their number density and extent must be such that their surface coverage factor is very close to unity.
for a singly-ionised species is that of Fe\textsc{ii} at $z_{\text{abs}} = 0.72609$ towards Tol 0453–423. The effect is small, but very unusual: the Fe\textsc{ii}2600 saturated components have a flat core with a clear flux residual of 2\% (7σ significance level). We obtain from the fit of this Fe\textsc{ii} doublet, which falls on the quasar Lyα-N v emission, $C_f = 0.98$ and $C_p = 0.96$, that is, an absorber size comparable to or larger than the ELR.

For two cases, either full or partial covering of the ELR are equally acceptable or inconclusive due to the weakness of the absorption lines: the Mg\textsc{ii} absorber at $z_{\text{abs}} = 0.452$ towards HE 0001–2340, with $0.75 < C_f < 1.0$, and the very weak Mn\textsc{ii} absorber at $z_{\text{abs}} = 0.726$ towards Tol 0453–423.

Finally, two cases are well consistent with full covering of the ELR: the multiple Fe\textsc{ii} system at $z_{\text{abs}} = 1.365$ towards PKS 0237–23 and the multiple Fe\textsc{ii} system at $z_{\text{abs}} = 1.328$ towards TXS 1331+170; in total 22 distinct velocity components are detected in these Fe\textsc{ii} absorbers. The absence of structure effects in these Fe\textsc{ii} absorbers appears to be in good agreement with constraints obtained previously concerning the extent - about 200 pc from uniformity as seen towards HE 0001.

Finally, two cases are well consistent with full covering of the ELR: the multiple Fe\textsc{ii} system at $z_{\text{abs}} = 1.365$ towards PKS 0237–23 and the multiple Fe\textsc{ii} system at $z_{\text{abs}} = 1.328$ towards TXS 1331+170; in total 22 distinct velocity components are detected in these Fe\textsc{ii} absorbers. The absence of structure effects in these Fe\textsc{ii} absorbers appears to be in good agreement with constraints obtained previously concerning the extent - about 200 pc from uniformity as seen towards HE 0001.

5. Discussion and prospects

5.1. Detection of non-uniformity effects

The analysis of the systems in our sample illustrates well the difficulties encountered in establishing the reality of non-uniformity effects in foreground absorbers. Large departures from uniformity as seen towards HE 0001–2340 for Fe\textsc{i} at $z_{\text{abs}} = 0.45206$ are very rare, and the observed effects are generally too small to bring equivalent width or apparent opacity ratios clearly out of the range expected for a point-like background source. When the values of these ratios remain within the optically thin and thick bounds, the apparent inconsistencies between the various line profiles can potentially be removed by introducing “hidden” additional velocity components (see the $z_{\text{abs}} = 1.364$ absorber towards PKS 0237–23; we note, however, that for this system, additional arguments do not favour the presence of a low $b$ component). In the interstellar medium of our own Galaxy, ultra-high resolution observations have directly shown that $b$ parameters in some neutral velocity components can be lower than $b = 1$ km s$^{-1}$ (Andersson et al. 2002); our line fitting or curve-of-growth analysis also require similarly narrow lines, but for severe blending, our resolution of about 6 km s$^{-1}$ might be insufficient to reach reliable conclusions.

It is noteworthy, however, that when two transitions with about equal $J$/$f$ values (e.g., to within 10\%) are detected, one against the continuum and the other one on an emission line, robust results can be obtained; indeed, the opacities being then nearly equal, line profiles are expected to be identical in the velocity scale (corresponding to $W \propto \lambda$), regardless of any assumption on the velocity distribution (Fe\textsc{i}13021 and Fe\textsc{i}12719 seen towards HE 0001–2340 nearly fulfill this condition), which results in a very narrow range expected for the $W$ ratio (Fig. 6). For the main C\textsc{i} and Fe\textsc{i} transitions, we note that the $J$/$f$ ratio of the C\textsc{i}1277 to C\textsc{i}1328 lines is 1.075, while the $J$/$f$ ratios of the Fe\textsc{i}12719 to Fe\textsc{i}12167 lines and the Fe\textsc{i}12719 to Fe\textsc{i}13021 lines are 1.018 and 1.054, respectively, which is very close to unity. This means that for a C\textsc{i} or Fe\textsc{i} system that displays one of these transitions on an emission line, it would be easier to investigate structure effects.

One obviously important parameter in detecting structure effects is the emission line over continuum contrast, that is the $x$ value. If the latter is high (as with absorption detected on top of Lyα emission), small departures from full covering can be revealed more easily. In practise, for the high z quasars considered in this study, Lyα-N v or C iv emission, and to a lesser extent Lyβ-O vi, are the only emission lines providing reasonably high $x$ values. Another key parameter is the absorption line opacity: when optically thick flat-bottom features are seen on emission lines, departures from full covering of only a few percent can be established reliably, as illustrated by the $z_{\text{abs}} = 0.726$ system towards Tol 0453–423. For low- or intermediate-opacity lines, the detection of several transitions with various $f$ values formed against either the continuum source or ELR is important to achieve well-constrained fits for absorption line profiles and to assess the uniformity of the absorber. Species such as Fe\textsc{i} and C\textsc{i} are well suited owing to the large number of relatively strong transitions they provide.

Finally, we pinpoint a few values of the $r = (1+z_{\text{em}})/(1+z_{\text{abs}})$ ratio that provide especially favourable distributions of Fe\textsc{i} and C\textsc{i} absorption lines with respect to quasar emission lines. We first consider the main C\textsc{i} transitions and we find that $r = 1.072$ brings the 1260, 1276, 1277, and 1280 Å transitions on Lyα-N v together with C\textsc{i}11656 on C iv emission (this corresponds to the system observed by Balashev et al. 2011 with $z_{\text{em}} = 2.57$ and $z_{\text{abs}} = 2.338$, thus $r = 1.070$). For $r = 1.035$, the 1260, 1276, 1277, and 1280 Å transitions lie on Lyα-N v, while all other transitions are seen against the continuum source alone. For Fe\textsc{i}, we find that $r = 2.512$ (Fe\textsc{i}3201 on Lyα and Fe\textsc{i}3720 on C iv), 2.239 (Fe\textsc{i}12719 on Lyα and Fe\textsc{i}13441 on C iv, as towards HE 0001–2340) and 1.928 (Fe\textsc{i}3201 on C iv and Fe\textsc{i}13720 on C ml) provide valuable configurations.

5.2. Incomplete absorption systems

The discussion in Sect. 4.2 and our conclusion that the extent of cold neutral absorbers is about five times that of the ELR raises the possibility of detecting absorption lines induced by cloudlets that cover part of the ELR, but not the continuum source (Fig. 1c). This would correspond to velocity components seen only on emission lines, with no corresponding feature detected in transitions seen against the continuum. Such small clouds are expected to be embedded in a more extended HI region and in an even larger ionised gaseous envelope. Thus, one does not expect to miss the identification of systems that would present absorption lines exclusively on emission lines, but instead to occasionally encounter some additional velocity components on the emission line.

The simple model described in Sect. 4.2.3 can be used to estimate the incidence of such components. The associated absorbers are characterised by $R_a < d < R_a + R_e$; then, their number ($N_e$) relative to the number of those covering the continuum source ($N_c$) is given by

$$N_e = \frac{\pi(R_a + R_e)^2 - \pi R_a^2}{\pi R_a^2} = \frac{1 + \frac{R_e}{R_a}}{1} - 1. \quad (18)$$

For $R_a \approx 5 R_e$, we obtain $N_e/N_c = 0.44$. A significant fraction of incomplete systems is therefore expected, but the latter should on average exhibit much weaker features since the absorbed flux is low. $C_e = 0$, and furthermore, for $R_e = 5 R_a$, we find that 50\% of these systems have $0 < C_{\text{abs}} < 0.17$ (with $d$ lying in the range 5.52 $R_a < d < 6 R_a$); the remaining 50\% have 0.17 $< C_{\text{abs}} < 0.48$ and 5 $R_a < d < 5.52 R_a$. We searched for such additional components within the C\textsc{i} and Fe\textsc{i} systems investigated in this
paper and could not find any. To our knowledge, no absorption feature of this type has been reported.

5.3. Structure effects and $f$ values

Some oscillator strength values for UV transitions that are commonly detected in quasar absorption systems are still not accurately determined. In particular, there has been some debate on the $f$ values for C$\text{I}$ transitions as derived by Jenkins & Tripp (2001 & 2011) from interstellar absorption lines using high spectral resolution HST-STIS data, and those given by Morton (2003). When precise laboratory measurements or computations are not available, astrophysical data can be used to constrain the ratio of $f$ values for several transitions from a given species (see, e.g., Federman & Zsargo 2001). The excellent S/N quasar spectra considered in this paper could help to determine which of the two sets of C$\text{I}$ $f$ values is the most consistent with the observed line profiles.

In doing this, transitions that occur on emission lines must of course be dismissed because a change in $f$ and partial covering of the ELR might be confused. Equation (2) indicates that for low opacities, $F_\text{abs}$ reduces to $F_\text{obs} = 1 - \tau C_f$ where $\tau \ll f$; thus both effects are indistinguishable in the $\tau \ll 1$ limit. All our measurements are consistent with full covering of the continuum source, as indeed expected given the small size of the latter. Then, for transitions seen against the continuum, quasar spectra can provide reliable constraints on the ratio of $f$ values, exactly as stellar spectra do for interstellar lines.

We therefore selected pairs of C$\text{I}$ transitions seen on the quasar continuum, when possible in regions of similar S/N, and with Morton’s $f$ ratios differing substantially from those of Jenkins & Tripp. This is clear for the $f$(C$\text{I}$1560)/$f$(C$\text{I}$1656) ratio: using Jenkins & Tripp, it is 1.74 times that obtained with Morton’s $f$ values (there is a similar difference for C$^+$ transitions). It is also the case, but to a lesser extent, for the $f$(C$\text{I}$1560)/$f$(C$\text{I}$1277) ratio, which is 1.13 times higher when adopting the values of Jenkins & Tripp instead of those of Morton. Two systems with C$\text{I}$1560 and C$\text{I}$1656 transitions are detected against the continuum: at $z_{\text{abs}} = 1.7765$ towards TXS 1331+170 (HIRES spectrum), and at $z_{\text{abs}} = 2.4183$ towards QSO J1439+1117 (UVES spectrum). The simultaneous fit of these lines in both cases results in a much poorer fit when using the $f$ values of Jenkins & Tripp instead of those of Morton. For TXS 1331+170, the $\chi^2$ statistic for the fit is 33% higher, with the C$\text{I}$1560 transition of the moderate-opacity component at $-17$ km s$^{-1}$ (see Fig. 10) clearly overfit, whereas it is underfit for the C$\text{I}$1656 transition. The system at $z_{\text{abs}} = 2.4183$ toward QSO J1439+1117 has multiple components with strong C$^+$ absorptions of intermediate opacity. The $\chi^2$ statistics for the fit is 95% higher with Jenkins & Tripp’s $f$ values, corresponding to a clear overfit of the C$\text{I}$1560 transitions and significant underfit for the C$^+$1656 lines. In contrast, satisfactory fits are obtained for both systems using Morton’s values.

The distances of intervening absorbers

The C$\text{I}$1560 and C$\text{I}$1277 transitions are present at $z_{\text{abs}} = 1.7765$ in the UVES spectrum of TXS 1331+170. Since the $f$ ratios for these transitions only differ by 13% between Jenkins & Tripp’s and Morton’s values, we do not expect a strong difference in the fits. The $\chi^2$ statistics for the fit is only 9% higher with Jenkins & Tripp’s $f$ values instead of Morton’s values. In both cases, the fit of C$\text{I}$1560 absorptions is good (the S/N ratio is better near the C$\text{I}$1560 lines, which drive the fit), whereas the C$\text{I}$1277 absorption of the component at $-17$ km s$^{-1}$ (see above) is slightly underfitted when using Jenkins & Tripp’s $f$ values.

Therefore, the $f$ values adopted for C$\text{I}$ in our study (from Morton 2003) appear to be more consistent with the data for the three systems mentioned above.

Another species with transitions for which $f$ values are still uncertain is Ni$\text{II}$ (see Cassidy et al. 2016 for a comparison between calculations, experimental determinations, and observations). In the course of our study, we identified a few systems that we believe to be free of partial covering or structure effects; we plan to investigate them in a future paper in order to improve the determination of $f$ values for this ion.

5.4. Prospects

The conclusions drawn from our analysis are limited by the small number of systems we investigated, and it is clearly desirable to extend the C$\text{I}$ and Fe$\text{II}$ samples. Additional C$\text{I}$ absorbers can be selected with an appropriate $(1 + z_{\text{abs}})/(1 + z_{\text{em}})$ ratio from the C$\text{I}$ survey performed by Ledoux et al. (2015) on the basis of SDSS-II DR9 spectroscopic data. This could be complemented by a similar C$\text{I}$ search in the public SDSS-III DR12 spectroscopic database. For Fe$\text{II}$ systems involving this species are much rarer and weaker than C$\text{I}$ systems, and it would be very difficult to build a sample of reasonable size. We note that some multi-object spectrographs such as MOONS at the VLT and 4MOST at VISTA, which are still under construction, will help in the near future to increase the number of high-redshift quasar identifications and will provide additional C$\text{I}$ and Fe$\text{II}$ systems of interest for studies of cold neutral absorber extent and structure.

Another promising approach would consist of using observations with higher spectral resolution. As illustrated by our study, at a resolution of about 6 km/s, some velocity components in neutral gas remain unresolved, and furthermore, line blending of adjacent components is often a problem in establishing the reality of structure effects. The upcoming ESO instrument ESPRESSO, with its higher resolution (R=120000 and up to 220000) and full wavelength coverage from 3800 to 7800 Å (Pepe et al. 2013), would clearly allow us to perform a much more detailed study of the few systems for which we have identified partial covering or non-uniformity effects. This is especially true for the complex system at $z_{\text{abs}} = 2.4183$ towards QSO J1439+1117, which involves many closely spaced velocity components.

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