Fracture analysis of fisheye failures in the tooth root fillet of high-strength gears made out of ultra-clean gear steels

D. Fuchs · S. Rommel · T. Tobie · K. Stahl

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Abstract

In shot-peened components, failures can be caused by a crack initiation below the surface at a non-metallic inclusion in the steel matrix. This fracture mechanism is called “fisheye failure”. In addition, this failure type can lead to a decreased endurance fatigue limit for the component. By preventing this crack mechanism, higher bending strength is expected to be achievable. Various research by universities and research institutes has taken place in this field using standard specimen and sometimes special alloy systems. However, in the tooth root of a gear, a complex multiaxial stress condition is present. Furthermore, the most commonly gears used in transmissions are made out of case-hardened wrought steels. Therefore, in the gear industry, there is only limited knowledge available about this failure type and the failure characteristics, so far. The first step to gain more knowledge requires extended and proper characterization of the crack area. Furthermore, in standardized gear calculation methods a consideration of a crack initiation below the surface at non-metallic inclusions is not possible, yet. Therefore, extended model approaches are still necessary. However, the reliability of such model approaches depends strongly on the quality of the input data, which can only be ensured by a proper fracture surface analysis. As a starting point, the aim of this paper is to characterize systematically the fracture area characteristics in the tooth root fillet of case-hardened, shot-peened gears in detail according to a presented approach to further extend a presented extended model approach in the medium term.
Bruchflächenanalyse von Zahnfußbrüchen von unterhalb der Oberfläche an nicht-metallischen Einschlüssen bei hochtragfähigen Zahnrädern aus hochreinen Zahnradstählen

Zusammenfassung
Bei kugelgestrahlten Bauteilen kann eine Rissinitierung unterhalb der Oberfläche an einem nicht-metallischen Einschluss in der Stahlmatrix stattfinden. Dieser Ausfallmechanismus wird im Deutschen als Bruchlinsenversagen und im Englischen als “fisheye failure” bezeichnet. Darüber hinaus kann dieser Ausfallmechanismus zu einer verminderten Dauerfestigkeit des Bauteils führen. Es wird erwartet, dass durch die Hemmung dieses Rissmechanismus eine höhere Dauerfestigkeit erreicht werden kann. Auf diesem Forschungsgebiet wurden bereits verschiedene Untersuchungen an Universitäten und Forschungsinstituten durchgeführt, wobei im Rahmen der Untersuchungen einfache Standardproben und zuweilen spezielle Legierungssysteme verwendet wurden. Im Zahnfuß eines Zahnrads liegt jedoch ein komplexer, multiaxialer Spannungsza stand vor und die meisten Zahnräder in Getrieben werden aus einsatzgehärteten Zahnradstählen hergestellt. Daher gibt es in der Getriebeindustrie bisher nur begrenzte Kenntnisse über das Bruchlinsenversagen und dessen Versagenscharakteristik. Eine erste Maßnahme zur Generierung weiteren Wissens erfordert eine vollumfängliche und angepasste Charakterisierung des Rissausgangsortes. Darüber hinaus ist in standardisierten Zahnradberechnungsverfahren eine Berücksichtigung einer Rissinitierung von unterhalb der Oberfläche an nicht-metallischen Einschlüssen bisher nicht möglich. Daher sind weiterhin höherwertige Modellansätze notwendig. Die Zuverlässigkeit solcher höherwertiger Modellansätze hängt jedoch stark von der Qualität der Eingangsdaten ab, die nur durch eine geeignete Bruchflächenanalyse sichergestellt werden kann. Ziel dieser Arbeit ist es, die Bruchflächencharakteristik im Zahnfuß einzugsgehärteter, kugelgestrahlter Zahnräder nach einer vorgestellten Vorgehensweise systematisch und detailliert zu charakterisieren, um mittelfristig den vorgestellten, höherwertigen Modellansatz weiterzuentwickeln.

Abbreviations
NMI Non-metallic inclusion
ODA Optically dark area
FVA German Drive Technology Research Association (registered association)
SEP Steel test specification
Eq Equation
EDX Energy-dispersive X-ray
c.f. Abbreviation for compare

1 Introduction
Nowadays, gearboxes must meet steadily increasing as well as completely new requirements, be it due to the trend towards green energy or to the electrification of the powertrain. In the wind power industry, long operating durations are required. In powertrains for e-mobility applications, high-speed approaches are being investigated and fewer gear stages are needed. In both examples, the number of load cycles for the gears is much higher than in the past. Therefore, a higher gear load carrying capacity in relation to endurance fatigue is needed.

A shot-peening process can strengthen the tooth root fillet of a gear and will most likely raise the tooth root bending strength. However, research shows that for shot-peened tooth root fillets, there can be a change in the crack mechanism. Due to the induced compressive residual stresses, a so-called fisheye failure can initiate at a non-metallic inclusion below the surface. Various research was performed to investigate fisheye failures at research institutes using standard specimen (tension-compression and rotating bending specimen) and sometimes special alloy systems. However, in the tooth root of a gear, a complex multiaxial
stress condition is present. Furthermore, the most commonly gears used in transmissions are made out of case-hardened wrought steels. Therefore, in the world of gears, there is only limited knowledge available in this field about this failure type and the failure characteristics, so far. A first step to gain more knowledge requires extended and proper characterization of the fracture area.

Furthermore, in standardized gear calculation methods, like AGMA 2001-D04 [1] or ISO 6336 [2], a consideration of a crack initiation from below the surface at non-metallic inclusion (fisheye fracture) is not possible, yet. Therefore, extended model approaches are still necessary. However, the reliability of such model approaches depends strongly on the quality of the input data, which can only be ensured with a proper fracture surface analysis. As a starting point, the aim of this paper is to characterize systematically the crack area characteristics in the tooth root fillet of case-hardened, shot-peened gears in detail according to a presented approach to further extend a presented model approach in the medium term.

2 Overview of the state of knowledge

A fisheye failure is characterized by an optically brighter area in the fractured surface; see Fig. 1. Typically, in the center is a non-metallic inclusion, which is responsible for the crack initiation. Usually, a darker-appearing area is visible around the non-metallic inclusion. In Fig. 1 the darker area is named “GBF” acc. to the nomenclature of Shiozawa et al. [3]. When the fisheye expansion reaches a certain area, the crack will propagate through the rest of the material.

In the past, extensive experimental investigations with tension-compression or rotating bending fatigue specimens have been conducted on this type of crack mechanism, for example in [4–6]. In the course of the aforementioned research projects, the fisheye was usually characterized by its area and the non-metallic inclusion was characterized by its size and resulting area and chemical composition. In the following, the common characteristics of fisheye failures will be presented.

2.1 Characteristics of fisheye failures

Within the literature, generally, two geometrical shapes and positions for fisheyes are shown. In tension-compression specimens the shape of the fisheye is circular, and it is located in the center of the specimen (see Fig. 2a). In rotating bending specimens, the form of the fisheye is usually
slightly oval and is located at the edge of the specimen (see Fig. 2b).

In [8], heat-treated and unpeened gear specimens displayed a circular fisheye, whereas heat-treated and shot-peened specimens had an ellipsoidal form, c.f. Fig. 3. The difference can be attributed to the different stress conditions during the tests and the material properties in the center and at the edge of the specimen. There is no proper documentation in the literature on how the area of the fisheye is to be determined exactly. It is assumed that the area of the fisheye is derived from its circumference.

Non-metallic inclusions and their morphology are classified into five groups according to ISO 4967 [9]; see Table 1. In typical gear steels, like MnCr or CrNiMo-alloyed steels, the most common inclusion types found are aluminum oxides (Al₂O₃), manganese sulfides (MnS), and titanium nitrides (TiN). Furthermore, mixed inclusions and minor elements, like calcium (Ca), can be found. The morphology of non-metallic inclusions can be elongated, spherical, or the shape of stringers; c.f. Fig. 4.

Non-metallic inclusions are spatial defects in a steel matrix. However, when stressed in the direction of the maximum tensile stress, the non-metallic inclusion can be seen as a two-dimensional void according to the model approach of Murakami [6]. According to Murakami the non-metallic

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**Fig. 5** Globular inclusion and dark area “ODA” [10]

**Fig. 6** a SEM observation of a fisheye type fracture surface; b Surface roughness plot along a cutting plane line (A to B) at a fisheye [14] (key: (1) Inclusion (2) GBF zone (3) Fisheye (4) Outside the fisheye)

**Fig. 7** Schematic diagram of a model approach for the evaluation of the tooth root bending strength of gears [21]
inclusion can be seen as an actual void. No stress step-up is assumed due to the non-metallic inclusion, even when the non-metallic inclusion de-bonds from the steel matrix. According to Murakami [6], the area of a non-metallic inclusion can be determined approximately as a circular area. This approach applies very well to globular oxide inclusions. However, aluminum oxides and manganese sulfides in gear steels can also be found as elongated or stringer inclusions; c.f. Fig. 4. In these cases, this approximation does not fit.

There is no proper documentation in the literature on how the area of the inclusion is to be determined exactly. It is assumed that either the area is derived from the circumference or an approximation using a basic geometric shape is made.

Often, a darker-appearing area around the non-metallic inclusion can be detected [10, 11]; c.f. Fig. 5. The theory is that the formation of the dark area starts at the non-metallic inclusion. It then grows non-uniformly until it reaches a certain threshold, where the rest of the fisheye starts to form.

There are several theories on how the dark area is formed and therefore different nomenclatures:

- ODA: Optically dark area acc. to Murakami [10, 11]
- GBF: Granular-bright facet acc. to Shiozawa et al. [3]
- FGA: Fine granular area acc. to Sakai [5, 12]
- RSA: Rough surface area acc. to Ochi et al. [13]

In the course of this publication, the nomenclature “ODA” acc. to Murakami is used. Shiozawa et al. present at a fisheye fracture a surface roughness plot along a cutting plane line [3, 14]. It can be seen that the granular-bright facet (GBF) zone has a different roughness to the rest of the fisheye. The ODA and its properties are also discussed in [15–18]. (Fig. 6).

There is no proper documentation in the literature on how the area of the dark area is to be determined exactly. Murakami [11] summarizes the area of the NMI and the dark area to determine the area of the ODA; see Eq. 1. It is assumed that the area of the dark area $A_1$ is derived from the circumference.

$$\sqrt{A_{ODA}} = \sqrt{A_0} + A_1$$

2.2 Model approach for considering the influence of non-metallic inclusions on the tooth root load carrying capacity of gears

In standardized gear calculation methods a consideration of a crack initiation from below the surface at non-metallic inclusions is not possible, yet, and extended model approaches are still necessary. The area of the non-metallic inclusion is usually one of the main parameters for local calculation approaches for predicting the tooth root bending strength. However, the reliability of such an extended model approach is very much dependent on the quality of the input data.

An extended model approach for the evaluation of the tooth root bending strength of gears, which is based on the model approach of Murakami [19, 20], was presented in
Fig. 9 Stacked bar diagram of the degree of cleanliness according to ISO 4967 Method A [9] of the steel batches investigated.

[21]. This model approach allows a consideration of the effects of non-metallic inclusions in the matrix of gear steels on the tooth root bending strength. Fig. 7 illustrates this model approach for gears. As main input data, the characteristics of the non-metallic inclusions are used, like the area and the distance from the surface of the non-metallic inclusion. However, the influence of the ODA, for example, is not yet taken into account.

2.3 Summary

Various aspects have to be taken in account when characterizing fisheye failures. For example, the size respectively area of the fisheye, the form and chemical composition of the non-metallic inclusions and the characteristics of the ODA. However, no extensive studies on fisheye failure characteristics in the tooth root fillet of case-hardened, shot-peened gears can be found in the literature so far.

Extended model approaches are still necessary, to consider the influence of non-metallic inclusions on the tooth root bending strength of shot-peened gears. However, the reliability of such extended model approaches is strongly dependent on the data quality. However, in the literature different and sometimes not fully documented assumptions and approaches have been used so far to document fisheye characteristics. It can be summarized that still a deeper understanding of the characteristics of fisheye fractures in shot-peened gears is necessary and the input data quality for model approaches has to be ensured to get reliable results.

3 Aim of the investigation

Extensive experimental investigations on case-hardened, shot-peened gears in the high cycle fatigue range, which had failed mostly due to fisheye failures, have been conducted by Schurer [22], Bretl [23] and Stenico [24] in the past. The tests were done with FZG back-to-back as well as pulsator test rigs. The test rigs are shown in Fig. 8. The experimental investigations were done up to 15, 30 respectively 50 million load cycles and it was shown that even up to a higher number of load cycles the load carrying capacity still decreases. Some of the experimental results have already been internationally published in [25] and [26]. First investigations into crack area characteristics of these fisheye fractures were also already presented in [27]. The investigations in [27] show, for example, that in the fisheye fracture surface of gears also an ODA is present.

In the course of FVA research project 293 IV [30], which builds on the results and conclusions of [22–24] and especially on [27], extensive experimental investigations with the focus on the very high cycle fatigue range of gears made out of ultra-clean gear steels were performed. Ultra-clean gear steels were used to examine, if by using such gear steels a crack initiation below the surface at non-metallic inclusions can be prevented and higher load carrying capacities are possible. Gear sizes with a normal module of $m_n = 1.5$ and $5$ mm were used for the investigations on the FZG back-to-back test rig and on the Pulsator test rig.

The alloy systems of these ultra-clean gear steels were MnCr, CrNiMo, NiCr and NiMo. Table 2 presents an overview of the steel batches, alloy systems, diameters of the steel bars and area reduction ratios. All area reduction ratios are above the specification value of 5:1 for continuous casting according to ISO 6336-5 [31].

### Table 3: Chemical analysis of ultra-clean steel batches

| Variant | Alloy system                  | Chemical composition in mass-% |
|---------|-------------------------------|--------------------------------|
|         |                               | C  | Mn  | Cr  | Ni  | Mo  | S   | Al  | Cu  | P   | Si  |
| OW1     | EN20MnCr5                     | 0.20 | 1.17 | 1.15 | 0.12 | 0.05 | 0.019 | 0.026 | 0.18 | 0.018 | 0.23 |
| S4      |                               | 0.21 | 1.20 | 1.14 | 0.15 | 0.04 | 0.028 | 0.030 | 0.14 | 0.009 | 0.15 |
| S6      |                               | 0.18 | 1.25 | 1.07 | 0.22 | 0.06 | 0.012 | 0.023 | 0.09 | 0.012 | 0.26 |
| S8      |                               | 0.18 | 1.12 | 1.15 | 0.19 | 0.05 | 0.006 | 0.019 | 0.12 | 0.016 | 0.16 |
| OW4     |                               | 0.21 | 1.31 | 1.25 | 0.16 | 0.02 | 0.006 | 0.031 | 0.12 | 0.010 | 0.17 |
| OW3     | EN18CrNiMo7-6                 | 0.20 | 0.54 | 1.74 | 1.56 | 0.29 | 0.011 | 0.025 | 0.20 | 0.011 | 0.26 |
| OW5     |                               | 0.19 | 0.54 | 1.65 | 1.42 | 0.27 | 0.001 | 0.009 | 0.10 | 0.007 | 0.27 |
| OW7     | EN20NiMo9-7                   | 0.20 | 0.23 | 0.38 | 2.24 | 0.67 | 0.001 | 0.082 | 0.16 | 0.004 | 0.08 |
| S9      | EN18NiCr5-4                   | 0.18 | 0.78 | 1.15 | 1.41 | 0.09 | 0.001 | 0.033 | 0.13 | 0.008 | 0.31 |
Table 4  Limits according to DIN EN ISO 683-3 [32] and for steel batch EN20NiMo9-7 according to the material inspection document of the steel manufacturer

| Limits in mass-% | C | Mn | Cr | Ni | Mo | S | Al | Cu | P | Si |
|-----------------|---|----|----|----|----|---|----|----|---|----|
| EN20MnCr5       | Max | 0.22 | 1.40 | 1.30 | – | – | 0.035 | – | – | 0.025 | 0.40 |
|                 | Min | 0.17 | 1.10 | 1.00 | – | – | – | – | – | – | – |
| EN18CrNiMo7-6   | Max | 0.21 | 0.90 | 1.80 | 1.70 | 0.35 | 0.035 | – | – | 0.025 | 0.40 |
|                 | Min | 0.15 | 0.50 | 1.50 | 1.40 | 0.25 | – | – | – | – | – |
| EN20NiMo9-7     | Max | 0.21 | 0.30 | 0.40 | 2.35 | 0.70 | 0.002 | – | – | 0.025 | 0.10 |
|                 | Min | 0.18 | 0.22 | 0.35 | 2.25 | 0.67 | – | – | – | – | – |
| EN18NiCr5-4     | Max | 0.21 | 0.90 | 1.20 | 1.50 | – | 0.035 | – | – | 0.025 | 0.40 |
|                 | Min | 0.16 | 0.60 | 0.90 | 1.20 | – | – | – | – | – | – |

Fig. 9 provides a first impression of the degree of cleanliness of the steel batches. The values were determined according to ISO 4967, Method A [9]. The steel batches OW7 und S9 show the lowest cleanliness index and therefore the highest degree of cleanliness. Steel batches OW1, S4 and OW3 show values above five, while the values for the other steel batches are in between.

The chemical compositions of all variants were in accordance with the specifications in [32]. Table 3, 4 and 5 provide a brief overview.

Fig. 10 gives a first impression of the crack area characteristics of tooth root failures due to a crack initiation below the surface at a non-metallic inclusion in case-hardened, shot-peened gears made out of these ultra-clean gear steels. The fisheye (encircled red) is clearly visible. The general crack area characteristics are similar to these of case-hardened, shot-peened gears made out of common and clean gear steel grades (c.f. [25]).

However, the crack area characteristics of these fisheye failures were not analyzed in detail or published so far. Therefore, in the course of this publication, the fisheye failures, which have occurred, were examined thoroughly in Sect. 5 following the approach in Sect. 4. For the characterization, a scanning electron microscope “CamScan4” with an “Oxford” EDX detector and an optical high-resolution 3D measurement system (Alicona InfiniteFocus [33]) were used. Table 6 shows an overview of the database of fisheye failures for this publication.

In industrial applications, mainly the size and the chemical composition of the non-metallic inclusion are characterized. It is also possible that the fracture surface is damaged, or the failed tooth cannot be found in a broken gearbox. Therefore, in addition, a damage assessment of fisheye failures on the fracture surface on the broken tooth and on the gear is done in Sect. 6 to investigate if differences are present between both fracture surfaces.

4 Analytical approach for fisheye fracture characterization

In the following, an analytical approach for the fisheye fracture characterization is given. It is shown, which chemical elements and geometrical parameters of the non-metallic inclusion are determined. The determined geometrical parameters of the fisheye is displayed, as well. Furthermore, an approach for the determination of the area of the non-metallic inclusion and a definition of the area of the fisheye in this publication are presented.

The chemical composition of the non-metallic inclusions in gear steels was determined using an energy-dispersive X-ray (EDX). The following chemical elements were determined: carbon (C), oxygen (O), magnesium (Mg), aluminum (Al), silicon (Si), sulfur (S), calcium (Ca), chromium (Cr), manganese (Mn), iron (Fe), nickel (Ni) and molybdenum (Mo).

Fig. 11 shows an overview of the determined geometrical parameters of the fisheye fractures in the case that the non-metallic inclusion consists of one or more than one particle:

- Length of the fisheye \( l_{\text{fisheye}} \)
- Width of the fisheye \( w_{\text{fisheye}} \)
- Length of the NMI \( l_{\text{NMI}} \)
- Width of the NMI \( w_{\text{NMI}} \)
- Distance from the surface of the NMI \( d_{\text{NMI}} \)

Table 5  Total oxygen content of the ultra-clean steel batches

| Alloy system | MnCr | CrNiMo | NiMo | NiCr |
|--------------|------|--------|------|------|
| Variant      | OW1  | S4     | S6   | S8   |
|              | OW4  | OW3    | OW5  | OW7  |
|              | S9   |
| \( O_{\text{total}} \) in ppm | 14   | Not determined | 9    | 14   |
|              | 18   | 6      | 13   |      |
In the case that the non-metallic inclusion consists of one particle, the geometrical center of the particle is used to determine the distance from the surface. If the non-metallic inclusion consists of two or more particle, an assumed geometrical center of all particles is used. In the case of two or more particles, to determine the length and width of the non-metallic inclusion, an overall length and width is used that includes all particles (see Fig. 11b).

In a previous publication [27] the area of the non-metallic inclusion is determined as presented in Fig. 12. According to this method, not only the area of the non-metallic inclusion but also part of the area between the inclusion particles is measured as well. This results in an overestimation of the inclusion area. Furthermore, a proper determination of the area of the ODA is not possible.

According to steel test specification (SEP) 1571 parts 1 to 3 [34], a non-metallic inclusion consists of one or more particles. To determine the area of the NMI, the area of each particle is considered. Within this publication, this approach is used; see Fig. 13 and Eq. 2. The particle area was hereby derived from the measured circumference of the particle.

Inclusion particles, which are not directly involved in the crack initiation, can be found in the fisheye, especially for stringers; c.f. Fig. 14. Such particles should not be considered in the determination of the inclusion area; see Eq. 3 As a decision criterion, the surface structure around the inclusion can be chosen. Usually, the surface structure around the non-relevant particle is slightly different from the surface structure around the inclusions involved in the crack initiation. The crack initiation is typically in the region of a finer microstructure around the NMI; c.f. Fig. 6. Furthermore, if the particle is near the boundary of the fisheye it should be non-relevant for the crack initiation.

\[ A_{\text{NMI}} = \sum_{i=1}^{l} A_{\text{particle},i} \]  
\[ A_{\text{Particle},\text{non}} \notin \sum_{i=1}^{l} A_{\text{particle},i} \]  

A few non-metallic inclusions were longer than the fisheye itself; c.f. Fig. 15 and 16. In this case, the following assumption for the area of the NMI was made: the areas at the border and outside of the fisheye should not be relevant for the crack initiation. Therefore, only the area of the NMI assumed to be relevant for crack initiation was determined.

| Alloy system | Number of fisheye failures |
|--------------|---------------------------|
| MnCr         | 75                        |
| NiCr         | 8                         |
| CrNiMo       | 21                        |
| NiMo         | 3                         |
| **In total** | **107**                   |
If an ODA is present, the relevant area of the NMI is in the region of the ODA. The length of the ODA could be either longer (see Fig. 15a) or shorter (see Fig. 15b) than the length of the NMI. The crack initiation is in the region of a finer surface structure around the NMI. An assumption of the relevant area can be made based on the finer surface structure around the NMI, which is exemplarily shown in Fig. 6 in detail.

If no ODA is present, determining the relevant area of the NMI relevant for crack initiation may be more difficult; c.f. Fig. 16. The differences in the surface structure between the crack initiation area and the crack growth area in the fisheye are slightly more similar and not as pronounced when there is an ODA present. However, a subjective distinction is sometimes not possible. Therefore, often an assumption must be made based on professional experience.

The area of the ODA is the sum of the area of the dark area and the NMI; see Eq. 4. This follows the approach according to Murakami [11] (c.f. Eq. 1). Fig. 17 shows two examples, where the dark area completely includes the NMI and where the dark area partly includes the NMI.

\[ A_{\text{ODA}} = A_{\text{NMI}} + A_{\text{Dark area}} \]  

(4)

The area of the total fisheye consists of the areas of the NMI, the ODA, and the rest of the area inside the fisheye itself; see Eq. 5.

\[ A_{\text{Fisheye}} = A_{\text{ODA}} + A_{\text{NMI}} + A_{\text{Fisheye, rest}} \]  

(5)

5 Fracture analysis of fisheye failures in the tooth root fillet of shot-peened gears

In the following a fracture analysis of fisheye failures in the tooth root fillet of shot-peened gears is made. The analysis follows the approach in Sect. 4.

In MnCr-alloyed steels, fisheye failures are caused mainly by manganese sulfides (MnS), and in CrNiMo-alloyed steels mainly by aluminum oxides (Al₂O₃). For

\[ A_{\text{Fisheye}} = A_{\text{ODA}} + A_{\text{NMI}} + A_{\text{Fisheye, rest}} \]  

(5)
Area of the non-metallic inclusion
Area of the ODA
Relevant area for crack initiation
Area of the fisheye
Fig. 15 Relevant area for crack initiation of the non-metallic inclusion a the length of the ODA is longer than the length of the NMI and b the length of the ODA is shorter than the length of the NMI.

Area of particle 1
Area of particle 2
Area of particle 3
Area of the ODA
Fisheye
Fig. 17 Area of the ODA a dark area completely includes the NMI b dark area partly includes the NMI.

In the investigated alloy systems, Table 7 shows the chemical composition and the percentage of the non-metallic inclusion, which was mainly responsible for the crack initiation. In Fig. 18 an example of a manganese sulfide inclusion is shown.

The crack initiations in MnCr alloyed steels, which were not at a manganese sulfide inclusions, were at aluminum oxide inclusions (9.5%) and mixed inclusions (3.2%). In CrNiMo alloyed steels 20% of the crack initiations were at manganese sulfide inclusions and 26.7% at mixed inclusions. 12.5% of the remaining crack initiations in the NiCr alloyed steel were at mixed inclusions. In the NiMo alloyed steel all three failures were due to an aluminum oxide inclusion.

None of the analyzed non-metallic inclusions were manganese sulfide or aluminum oxide inclusions only. In every non-metallic inclusion, minor elements were detected, such as silicon (Si), copper (Cu), molybdenum (Mo), and calcium (Ca). Furthermore, the analytical investigation regard-
Table 7 Chemical composition of the NMI, which was mainly responsible for crack initiation, and percentage

| Alloy system | Chemical composition of NMI (percentage) |
|--------------|----------------------------------------|
| MnCr         | Manganese sulfide (MnS) (87.3%)         |
| CrNiMo       | Aluminum oxide (Al₂O₃) (53.3%)         |
| NiCr         | Aluminum oxide (Al₂O₃) (87.5%)         |
| NiMo         | Aluminum oxide (Al₂O₃) (100%)          |

The chemical composition showed mixed inclusions. These consisted of manganese, sulfur, aluminum, oxygen, and further minor elements. In the MnCr alloyed steels, the most present minor element was molybdenum (Mo). Calcium (Ca) was the most present minor element in the CrNiMo alloyed steel. In the NiCr and NiMo alloyed steels the most present minor elements were calcium (Ca) and manganese (Mn).

In Fig. 19 the measured area of the fisheye is plotted against the calculated ellipsoidal area of the fisheye according to Eq. 6. It can be seen that the area of a fisheye can be described by an ellipsoidal area using the length and the width of the fisheye. This approach should not only be applicable on gears but also on fisheye failures in general components and specimens, too. If the fisheye is circularly formed, the diameter can be used to derive a circular area; c.f. Fig. 2.

$$A_{\text{Fisheye,calc}} = \pi \cdot \frac{l_{\text{Fisheye}} \cdot w_{\text{Fisheye}}}{4}$$

(6)

In [27], a correlation between the area of the fisheye and the distance from the surface of the NMI was published. This correlation can be confirmed by the extended available database of this publication; see Fig. 20. The greater the distance of the NMI from the surface, the larger the area of the fisheye.

In Fig. 21, the width of the NMI is plotted against its length. No clear correlation is observable. Therefore, the width and length of the NMI cannot be used to properly describe the area of the NMI. The approach based on a particle-based determination, which is used in this publication, is more appropriate when defining the area of non-metallic inclusions. In Fig. 22 the distance from the surface is plotted against the measured area of the NMI. There is no clear correlation.

Not all of the inspected fracture surfaces showed an ODA. An ODA was present in 82% of the fisheye fractures. Therefore, in the following, only the fisheye failures with an ODA are looked at in detail. In Fig. 23, the area of the NMI is plotted against the area of the ODA. It can be seen that there is a correlation between the area of the NMI and the ODA. The ratio decreases with an increasing area of the NMI. However, no correlation between the area of the ODA and the distance from the surface of the NMI can be found; see Fig. 24.

6 Damage assessment of fisheye failures on the fracture surface on the broken tooth and on the gear

In the following, further investigations into possible differences on the fracture surfaces of the broken teeth and the corresponding gears were performed. Fig. 25 shows the fisheye characteristic on a broken tooth and the corresponding gear. The fisheye structures are inverse and therefore the length, width, and area can be determined on each fracture surface.

In Fig. 26, a comparison of the determined areas of a non-metallic inclusion on the fracture surface on a broken tooth and the corresponding gear are shown. It can be seen that the determined areas differ from each other. The area of the NMI on the broken tooth is 1271 μm², whereas it is 1088 μm² on the corresponding gear, which is approximately a difference of 15%. The available database shows that in 20% of the cases, the area on the broken tooth can be up to 20% larger than the area on the corresponding gear. In the other cases, the difference is approximately 2 to 10% and is almost equally divided between broken tooth and corresponding gear. Therefore, the area of the non-metallic inclusion should be determined on both fracture surfaces and the biggest area (worst-case) should be used for further analysis and local calculation approaches.

Fig. 27 shows EDX images of the fracture surfaces of a manganese sulfide and an aluminum oxide inclusion. A manganese sulfide inclusion is softer than the steel ma-
matrix and has strong bonding to the steel matrix, whereas an aluminum oxide is harder and merely has weak bonding. Some of these characteristics can be seen in Fig. 27. The manganese sulfide inclusion is almost equally divided between the fracture surfaces. It can be assumed that the separation of the NMI was at an internal crack. On the other hand, the aluminum oxide inclusion is mainly on the fracture surface of the gear. Here, it can be assumed that the main separation was between the inclusion and the steel matrix. The conclusion is that for a proper determination of the chemical composition of an NMI, both fracture surfaces should be considered.

7 Discussion of the results

So far, no systematic extensive studies on failure characteristics in the tooth root fillet of case-hardened, shot-peened gears made out of case-hardened wrought steels, where the cracks have been initiated from non-metallic inclusions below the surface, can be found in the literature. Therefore, in this publication an extended fracture analysis was performed to ensure the quality of the input data for a presented model approach and to further extend the model approach in the medium term.

All of the shot-peened, case-hardened gears made out of ultra-clean gear steels failed in the range of the endurance limit mainly due to fisheye failures in the tooth root. Even the steel grades OW7 and S9, which show the highest degree of cleanliness, failed mainly due to a crack initiation at a non-metallic inclusion. It can be concluded, that even with ultra-clean gear steels a crack initiation at a non-metallic inclusion cannot be prevented in the range of the endurance limit of shot-peened, case-hardened gears.

The different alloy systems failed due to different types of non-metallic inclusions. In MnCr alloyed steels the non-metallic inclusion, which was mainly responsible for crack initiation, was a manganese sulfide, whereas in the other three steel grades aluminum oxide inclusions were mainly responsible. However, the proportion of failures at aluminum oxide inclusions is also different for these three steel grades. In every non-metallic inclusion different minor elements were present. In addition, in the MnCr, CrNiMo and NiCr alloyed steels some mixed inclusions were responsible for the crack initiation. Only in the NiMo alloyed steel all three failures were due to an aluminum oxide inclusion.

The area of a fisheye in these shot-peened, case-hardened gears can be described by an ellipsoidal area using the length and the width of the fish eye. This is in accordance to Fig. 3, where the fisheyes of heat-treated and shot-peened specimens had an ellipsoidal form.

One correlation found is that the greater the distance of the non-metallic inclusion from the surface, the larger the area of the fisheye. However, no clear correlation is observable between the width and the length of the non-metallic inclusions. This can be attributed to the fact that in the available database, a large number of the non-metallic inclusions are stringer inclusions. These stringer inclusions consists of two or more particles and are counted as one
non-metallic inclusion, because the distance between these particles is very small. Each particle has its own length and width. However, no correlation between the absolute length and absolute width of the non-metallic inclusion is possible, due to the stringer characteristic; c.f. Fig. 10b. The distance from the surface and the measured area of the non-metallic inclusion do not correlate, as well. Therefore, the area of the NMI cannot be derived from the distance of the NMI from the surface.

An ODA was present in 82% of the fisheye fractures. There is a correlation between the area of the NMI and the ODA. The ratio decreases with an increasing area of the NMI. Employing this correlation, the area of the ODA can be estimated based on the area of the NMI. Murakami derived in [11] a master-curve of the ODA, which correlates the increase of the ODA area in comparison to the NMI area as a function of the load cycles. These two correlations of the ODA should be analyzed in more detail in further work. However, no correlation between the area of the ODA and the distance from the surface of the NMI can be found.

The investigations regarding possible differences on the fracture surfaces of the broken teeth and the corresponding gears showed that the length, width, and area of the fisheye can be determined on each fracture surface. However, the area of the non-metallic inclusion and the chemical composition of an NMI should be determined on both fracture surfaces. In industrial practice, it is possible that one of the fracture surfaces cannot be characterized after a tooth root failure, be it for reasons of a damaged fracture surface or a missing tooth. In the course of this publication, it has been shown that the area of the NMI on both fracture surfaces can differ by up to 20%.

8 Conclusions

The summarized conclusions are:

- None of the analyzed non-metallic inclusions were manganese sulfide or aluminum oxide inclusions only. In
Fig. 25 Fisheye characteristic on both fracture surfaces. a broken tooth, b corresponding gear.

Fig. 26 Comparison of the areas of a non-metallic inclusion on both fracture surfaces. a broken tooth, b corresponding gear.

Fig. 27 EDX analysis of a, b manganese sulfide and an, c, d aluminum oxide inclusion on both fracture surfaces. a broken tooth, b corresponding gear, c broken tooth, d corresponding gear.

every non-metallic inclusion, minor elements were detected.

- The area of a fisheye can be described by an ellipsoidal area using the length and the width of the fisheye.
- The greater the distance from the surface of the non-metallic inclusion, the larger the area of the fisheye.
- No clear correlation is observable between the width and the length of non-metallic inclusions. This can be attributed to the fact that in the available database, a large number of the non-metallic inclusions are stringer inclusions.
- An approach based on a particle-based determination, which is used in this publication, is more appropriate as the approach from a previous publication [27] when defining the area of non-metallic inclusions.
- Using the applied approach a proper characterization of the area of the ODA is possible.
- An ODA was present in 82% of the fisheye fractures.
- No clear correlation is observable between the distance from the surface and the measured area of the non-metallic inclusion.
- A correlation between the area of the NMI and the ODA is apparent. Employing this correlation, the area of the ODA can be estimated based on the area of the NMI.
- No correlation between the area of the ODA and the distance from the surface of the NMI can be found.

Further investigations into possible differences on the fracture surfaces of the broken teeth and the corresponding gears were performed. The summarized conclusions are:

- The length, width, and area of the fisheye can be determined on each fracture surface.
- The area of the non-metallic inclusion should be determined on both fracture surfaces.

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Table 8 Nomenclature

| Symbol       | Unit     | Description                                      |
|--------------|----------|--------------------------------------------------|
| $A_{\text{Dark area}}$ | $\mu m^2$ | Area of the dark area                            |
| $A_{\text{Fisheye,rest}}$ | $\mu m^2$ | Rest of the area inside the fisheye, which is not the ODA or NMI |
| $A_{\text{Fisheye,calc}}$ | $\mu m^2$ | Calculated ellipsoidal area of the fisheye       |
| $A_{\text{NMI}}$ | $\mu m^2$ | Area of the non-metallic inclusion               |
| $A_{\text{ODA}}$ | $\mu m^2$ | Area of the optically dark area (ODA)            |
| $A_{\text{particle,i}}$ | $\mu m^2$ | Area of particle i                                |
| $A_{\text{Particle,non}}$ | $\mu m^2$ | Area of a non-relevant inclusion particle        |
| $d_{\text{NMI}}$ | $\mu m$  | Distance of the NMI from the surface             |
| $l_{\text{Fisheye}}$ | $\mu m$  | Length of the fisheye                            |
| $l_{\text{NMI}}$ | $\mu m$  | Length of the NMI                                |
| $W_{\text{Fisheye}}$ | $\mu m$  | Width of the fisheye                             |
| $W_{\text{NMI}}$ | $\mu m$  | Width of the NMI                                 |
For a proper determination of the chemical composition of an NMI, both fracture surfaces should be considered.

9 Summary and subsequent steps

In shot-peened, case-hardened gears, fisheye failures can occur. However, in standardized gear calculation methods a consideration of a crack initiation below the surface at non-metallic inclusions is not possible, yet. Therefore, extended model approaches are still necessary. However, the reliability of such model approaches depends on the quality of the input data, which can be ensured with a proper fracture surface analysis. As a result, the aim of this paper was to characterize the crack area characteristics in the tooth root fillet of case-hardened, shot-peened gears in detail according to a presented approach to further extend the presented extended model approach in the medium term.

It was shown that various aspects have to be taken into account when characterizing fisheye failures. In the literature different and sometimes not fully documented assumptions and approaches have been used so far to document fisheye characteristics. Therefore, the applied approach for fracture analysis was documented in detail in this publication. In addition, so far, no systematic extensive studies on fisheye failure characteristics in the tooth root fillet of case-hardened, shot-peened gears can be found in the literature. Therefore, in this publication an extended fracture analysis was performed following the presented approach and several conclusions could be drawn.

The main findings of this paper with regard to the crack area characteristics of fisheye failures are:

- The applied approach based on a particle-based determination is more appropriate, when defining the area of non-metallic inclusions.
- Using the applied approach a proper characterization of the area of the ODA is possible.
- Some characteristics can be determined on one fracture surface and others should be determined on both fracture surfaces.

The area of the non-metallic inclusion is usually the main parameter for local calculation approaches for predicting the tooth root bending strength (c.f. [6, 21]). It would be a great benefit, if in all future publications the chosen approach for the characterization of fisheye failures would be documented. This will allow a comparison and holistic use of the databases in the future and therefore contributes to an advanced understanding of the fisheye failure mechanism in gears.

In Fig. 25 several lines respectively steps at the non-metallic inclusion can be seen, which were not looked at in detail in the framework of this publication. Both steps start at the non-metallic inclusion, which lies here horizontally, and then run almost vertically to the boundary of the fisheye in this example. Therefore, in subsequent work, an extended fracture analysis of fisheye failures will be performed regarding the presented steps at the non-metallic inclusion and possible further characteristics. In addition, the chemical composition and morphology of non-metallic inclusions in ultra-clean gear steels are also considered in more detail in subsequent work. The aim is to further understand the formation and propagation of cracks at non-metallic inclusions and in fisheyes. Moreover, based on the results of the publication, the presented extended model approach will be further developed in subsequent work. In particular, the ODA will be taken into account.

In the long term, the aim is to provide a basis for countermeasures in steelmaking and gear manufacturing that can be applied to avoid the initiation of subsurface cracks at non-metallic inclusions and to achieve higher load carrying capacities.

10 Nomenclature

The nomenclature is shown in Table 8.

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