Resolving the Planetesimal Belt of HR 8799 with ALMA

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ABSTRACT

The star HR 8799 hosts one of the largest known debris discs and at least four giant planets. Previous observations have found evidence for a warm belt within the orbits of the planets, a cold planetesimal belt beyond their orbits and a halo of small grains. With the infrared data, it is hard to distinguish the planetesimal belt emission from that of the grains in the halo. With this in mind, the system has been observed with ALMA in band 6 (1.34 mm) using a compact array format. These observations allow the inner edge of the planetesimal belt to be resolved for the first time. A radial distribution of dust grains is fitted to the data using an MCMC method. The disc is best fit by a broad ring between 145\,+12\,-12\,AU and 429\,+37\,-32\,AU at an inclination of 40\,+5\,-6\,° and a position angle of 51\,+8\,-8\,°. A disc edge at \sim\,145\,AU is too far out to be explained simply by interactions with planet b, requiring either a more complicated dynamical history or an extra planet beyond the orbit of planet b.

Key words: circumstellar matter – planetary systems – submillimetre: planetary systems – submillimetre: stars – stars: individual: HR 8799

1 INTRODUCTION

As we build up our census of nearby stars, we find many systems that are host to both a debris disc and planets. These systems provide interesting test cases for understanding how planets and discs interact, the most useful of which are the cases where the disc has been resolved, allowing us to determine the geometry of the system and look for asymmetries in the disc (see Moro-Martín 2013 for a review). Unfortunately, resolved images to date have only probed the outer reaches of planetary systems (the Kuiper belt analogues), whereas the majority of detected planets (detected through radial velocity and transit observations) are very close to their host stars. This discrepancy in the measured scales of detection of host planets and host disc has limited our understanding of their interaction. The advent of direct imaging of planets is changing this paradigm as this method is much more sensitive to planets at tens of AU. So far HR 8799 is the only star around which multiple planets have been detected through direct imaging (Marois et al. 2008, 2010), making it a key system for detailed investigations.

Observations of the debris disc around HR 8799 go back to IRAS (Sadakane & Nishida 1986). Detailed study of this disc did not happen until it was observed by Spitzer (Su et al. 2009). This resulted in a detailed SED but also a resolved image at 24\,\mu m. The Spitzer observations imply that the dust must be going out to very large radii. This lead Su et al. (2009) to propose a model of the debris disc that consists of an inner asteroid belt analogue, a planetesimal belt between 100 and 310 AU and a blowout grain halo going out to at least 1500 AU. Deep observations using Herschel are also fit well by this model and have a high enough resolution that it is possible to constrain the inclination of the system to 26\,+3\,-2\,° (Matthews et al. 2014). This agrees with some measures of the inclination of the star (Reidemeister et al. 2009) and the likely inclination of the planets’ orbits.
2 OBSERVATIONS

HR 8799 was observed with ALMA in band 6 (1.34 mm) for the cycle 1 project 2012.1.00482.S. The observations were taken with a compact array format with baselines between 15-349 m. Given the distance to the star of 39.4 pc (van Leeuwen 2007), these correspond to spatial scales of 32 and 430 AU respectively. The data are comprised of 5 separate observations taken between 3rd and 18th January 2015. Details are shown in table 1. The correlator was configured to optimise continuum sensitivity, processing two polarizations in four, 2 GHz-wide baselines centred at 216, 218, 231 and 233 GHz, each with 128 spectral channels of width 16 MHz (20 km/s).

The data was calibrated using standard observatory calibration in CASA version 4.3.1, which includes water vapour radiometry correction, system temperature, complex gain calibration and flagging. Uranus was used as a flux calibrator for observations 1-4 and Neptune was used for observation 5. J2253+1608 was used to calibrate the phase. Calibration of observation 2 was worse than the rest due to large water vapour fluctuations so this data was discarded from the analysis. The total on source time is 2.8 hours. Figure 1 shows the dirty image (the inverse Fourier transform of the observed visibilities) of the continuum emission along with the dirty beam. These were created using CLEAN with zero iterations and a natural weighting, taking advantage of the multi-frequency synthesis. The resulting synthesised beam has a size 1.7″×1.3″. The RMS noise is best measured using a large region far from the source so as not to be affected by any of the artefacts of the Fourier transform. In this case, the diameter of the source (see section 3) is comparable to the FWHM of the primary beam (26″); therefore the RMS was measured by creating a dirty image pointing slightly away from the target (+90″ in declination) with a field of view that does not include the target. Using this method, the RMS is measured to be σ = 16 μJy/beam. A ring is detected at ~5.5″. This ring is surrounded by negative emission and an outer ‘ring’ is also present at ~20″, both of which are artefacts of the dirty beam.

As well as continuum, we detected CO J=2-1 emission at a barycentric velocity consistent with that of the star (-12.6±1.4 km/s). The emission is spectrally unresolved at our resolution of 40.6 km/s, in line with previous CO measurements showing much narrower line widths (Williams & Andrews 2006; Su et al. 2009; Hughes et al. 2011). Spatially, the dirty map shows complicated structure, with striping along the NE-SW direction analogous to that reported from previous SMA observations and indicative of line-of-sight contamination by the molecular cloud HLCG 92-35 (Yamamoto et al. 2003). The CO emission is seen as a clump ~12″ SW of the star (near the continuum ansa), which appears to be consistent with that detected in previous JCMT observations (Williams & Andrews 2006; Su et al. 2009). Our ALMA observations therefore confirm the presence of CO emission along the line of sight to HR8799 originating from the HLCG 92-35 cloud.

3 MODELLING

Interferometric observations measure complex visibilities in the u-v plane – the Fourier transform of the image plane. Whilst it is common practice to model interferometric observations in the Fourier plane, it is more efficient, whilst still retaining accuracy, to work in the image plane as the dirty image is simply the Fourier transform of the gridded visibilities (see Clark 1999 for the basics of interferometry).

To find the best fit parameters of the disc and their uncertainties an MCMC routine is run making use of emcee (Foreman-Mackey et al. 2013). The disc is modelled with 6 free parameters using a line of sight integrator method (Wyatt et al. 1999). We assume a wide ring of dust grains between $R_{in}$ and $R_{out}$ with an optical depth that varies as $R^2$. The ring is inclined from face on by an angle $I$ and given a position angle, $\Omega$, measured anti-clockwise from North. The total flux density of the disc at this wavelength is set by $F_{\nu}$. Since the stellar emission is not significantly detected (see figure 1) we extrapolate the PHOENIX model (Brott & Hauschildt 2005) fit of Matthews et al. (2014) to give a stellar flux density at this wavelength of $F_{\nu} = 17 \mu$Jy. Although the star is not significantly detected, there is a clear peak near the phasecentre but offset by approximately +0.4″ in right ascension and −0.2″ in declination. This lies within the pointing accuracy of ALMA and so we assume that this is the location of the star. For the radial temperature profile we treat the grains as blackbodies.

To accurately replicate the observation process, the model image is first attenuated by the primary beam – particularly important for this disc as the outer edge is potentially a significant fraction of the primary beam size and so we are likely to lose flux far from the phase centre. It is then convolved with the dirty beam (the Fourier transform of the sampling function) and the likelihood (−χ^2/2) is then calculated by comparison with the dirty image. The high resolution of the image compared to the beam size has the side effect of introducing correlated noise. To account for this, the value of $\sigma$ used in the $\chi^2$ is modified by a noise correlation ratio given by the square root of the beam area $\sim 1.5″$ given the resolution and signal-to-noise ratio of 1.1. See https://help.almascience.org/index.php?knowledgebase/article/View/319/alma/ what-is-the-astrometric-accuracy-of-alma for the equation.

Table 1. Details of the observations. PWV stands for precipitable water vapour.

| ID | Observation Start | Antennas | PWV (mm) |
|----|-------------------|----------|----------|
| 1  | 2015-01-03 20:23:49 | 38       | 1.2      |
| 2  | 2015-01-13 22:03:07 | 37       | 3.6      |
| 3  | 2015-01-14 21:47:52 | 38       | 4.2      |
| 4  | 2015-01-16 21:44:55 | 35       | 3.5      |
| 5  | 2015-01-18 18:35:04 | 34       | 4.0      |

(Goździewski & Migaszewski 2014). The disc has previously been observed in the sub-mm using the James Clerk Maxwell Telescope (Williams & Andrews 2006). Caltech Submillimeter Observatory (Patience et al. 2011) and the Submillimeter Array (Hughes et al. 2011), although none of these had the resolution and/or sensitivity required to accurately determine the geometry of the cold belt.
in pixels. The likelihood is then passed to emcee, which is run with 120 walkers and for 2500 timesteps. Uninformative priors have been assumed for all the parameters, i.e. they are uniform in $R_{in}$, $R_{out}$, $\gamma$, $\ln(F_\nu)$, $\cos(I)$ and $\Omega$. The best fit parameters and their uncertainties are shown in table 2. All parameters are fit to an accuracy or around 10%. This may seem surprising for the outer edge as it extends to a region where the signal-to-noise ratio is low, but the strong interaction between the parameters helps constrain the outer region where the signal-to-noise ratio is low, but the strong interaction between the parameters helps constrain the outer edge as strongly as the other parameters. The best fit model, convolved model and residuals are shown in figure 2. Three residuals at $\sim$3$\sigma$ are seen in or near the disc at locations relative to the star of (5.7,-8.2), (-0.9,2.2) and (-4.9,1.3). Deeper observations are necessary to determine whether these are real and comoving with the star. The residuals are otherwise smooth and the RMS in the residual image is equivalent to the noise measured in section 2. A restored image of the disc is shown in figure 3 showing how the disc should look to a single dish telescope i.e. removing the artefacts of the Fourier transform.

### Table 2. Best fit parameters and uncertainties from the MCMC modelling (see section 2)

| Parameter | Value |
|-----------|-------|
| $R_{in}$ (AU) | $145^{+12}_{-12}$ |
| $R_{out}$ (AU) | $429^{+37}_{-32}$ |
| $\gamma$ | $-1.0^{+0.4}_{-0.4}$ |
| $\ln(F_\nu)$ (mJy) | $2.8^{+0.5}_{-0.4}$ |
| $I$ (°) | $4.0^{+5.5}_{-6}$ |
| $\Omega$ (°) | $51^{+8}_{-8}$ |

Figure 1. Dirty image (left) of the continuum emission and the dirty beam (right). The dirty image is the inverse Fourier transform of the observed complex visibilities and has been created using natural weighting and multi-frequency synthesis. Contours show $\pm 2$, $3$ and $4\sigma$ significance levels. Negative ‘emission’ is seen surrounding the ring, which is due to the sidelobes of the beam that need to be removed by the modelling process (see section 3).

### 4 DISCUSSION

#### 4.1 Comparison with previous observations

The modelling of far-IR data by Matthews et al. (2014) predicts a planetesimal belt between roughly 100 and 310 AU whereas prior sub-mm interferometric observations using the SMA by Hughes et al. (2011) found an inner edge at $\sim$150 AU. Our inner edge of $145^{+12}_{-12}$ clearly reinforces the SMA result and is discrepant with the far-IR modelling. This discrepancy in inner edge at different wavelengths could potentially be real. The shorter wavelength observations are more sensitive to smaller grains. These grains are potentially susceptible to Poynting-Robertson drag, which will cause them to spiral in towards the star from the planetesimal belt as is seen in other discs such as Vega (Müller et al. 2010). The discrepancy in outer edge is significant and is likely due to the assumption by Matthews et al. (2014) of modelling the planetesimal belt and outer halo as two distinct components. In reality, there is likely some overlap between these components and the ALMA observations are better representing the actual outer edge of the planetesimal belt since the smaller grains in the halo are too faint at mm wavelengths to contribute significantly to the emission.

Matthews et al. (2014) find the disc to be oriented such that $I = 26 \pm 3^\circ$ and $\Omega = 64 \pm 3^\circ$ as opposed to our values of $I = 40^{+4}_{-3}$ and $\Omega = 51^{+8}_{-8}$. Whilst these parameters are consistent at the 95% level, there is a possibility that there is a real difference between the orientation of the planetesimal belt and the small grain population similar to the warp seen in the $\beta$ Pic disc (see Millar-Blanchaer et al. 2015, and references therein). Alternatively, it could be that emission from the background cloud (see section 2) or asymmetries in the disc (that have been assumed to be insignificant) are biasing the model fits in different ways. Given our knowledge of planetary system formation and evidence from our own Solar System (Brown & Pan 2004), it is expected that most planetary systems will be roughly coplanar unless they have undergone an instability. The latest astrometric fit to the observations of the planets from Zurlo et al. (2016) finds an inclination of $30\pm5^\circ$. A large difference in inclination could potentially tell us something about the dynamical history of the system but a $10^\circ$ difference, especially given the uncertainties, is not much larger than the inclination variations in the Solar System’s planets and disc (around $2^\circ$. Brown & Pan 2004).

An extrapolation of the total disc flux density based on the SCUBA and Herschel flux densities (Matthews et al. 2014) predicts a value of $3.5$ mJy at 1.3 mm. At $F_{\nu,3mm} = 2.8^{+0.5}_{-0.4}$ mJy, the result found here is somewhat lower than the extrapolated value and may mean that the sub-mm slope is slightly steeper than previously thought.
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Figure 2. The modelling process is conducted by taking the sky plane image of the model (left), multiplying by the primary beam and convolving with the dirty beam to produce a convolved image (middle), then subtracting this from the dirty image to produce a map of residuals (right). The images shown here are for the best fitting model and contours are at significance levels of ±2 and 3σ.

Figure 3. Restored image using the best fitting model (i.e the primary beam attenuated model convolved with a beam of size 1.7′′×1.3′′ – shown by the black ellipse – added to the residuals and primary beam corrected). Contours start at 2σ and increase in increments of 1σ. This also shows the planets as seen in the K2 band with SPHERE-IRDIS on the VLT (Zurlo et al. 2016).

4.2 Interaction between planets and the disc

The ability of planets to open gaps in circumstellar disks and to carve the inner edges of outer debris belts has been widely studied both analytically and numerically. This phenomenon is caused by the chaotic zone a planet possesses and within which mean motion resonances overlap. Therefore particles in the chaotic zone are unstable and will be removed on short dynamical timescales. The width of a planet’s chaotic zone mainly depends on the mass and location of the planet (Wisdom 1980; Duncan et al. 1989), but also on its eccentricity (Pearce & Wyatt 2014). Consequently, it is possible to link the location of a debris belt’s inner edge to the mass and orbital characteristics of the belt shaping planet.

In the case of the HR 8799 system, it is expected that planet b (the outermost planet) is responsible for shaping the debris ring inner edge. The latest astrometric fit to all the observations of the planets is given in Zurlo et al. (2016). Based on their orbital fit and using equations (9) and (10) of Pearce & Wyatt (2014), which gives the highest estimate of the width of the chaotic zone of all the methods mentioned previously, we expect an inner edge between 100-110 AU (for masses between 4-9 M_J). An alternative method for finding the orbits of the planets is to run simulations of the dynamical stability of the planetary system as done by Gozdiewski & Migaszewski (2014). They find that the planets must be in Laplace resonance to keep such a packed system of very massive planets stable. In contrast with the fit of Zurlo et al. (2016), who assumed planets on circular and non coplanar orbits, their models involve planets on coplanar and eccentric orbits, which will produce a more distant inner edge for the disc. Although the nominal eccentricity of planet b in their fit creates an inner edge further out, it is not predicted to go beyond 106-116 AU with the largest estimates.

In practice, the inner edge of the disc can be further out than this as the analytical equations assume a fixed orbit whereas perturbations from the other planets on planet b can vary its orbit, thereby varying the chaotic zone. If planet b can reach an eccentricity of at least 0.3 (higher if the planet mass is less than 9 M_J) for a prolonged period of time, then it could clear planetesimals out to 145 AU. In order to capture these effects, n-body simulations are necessary. Moro-Martín et al. (2010) ran such simulations and they did find that it is possible to have an inner edge as far out as 150 AU. This may be due to variations in the orbital eccentricity of planet b coupled with the effect of the Laplace resonance, however, it may result from the low resolution of their simulations (one particle every 0.5 AU).

All this opens up the possibility for another planet beyond the orbit of planet b. Such a planet would need to be beyond the chaotic zone of planet b to have any possibility of being stable. Using the equations of Pearce & Wyatt (2014), a planet at the edge of planet b’s chaotic zone (110 AU) on a circular orbit would need to be ∼1.25 M_J to create an inner edge at 145 AU. If it was further out or on an eccentric orbit, the required mass of the extra planet would be lower. This is lower than the limits from current observations, which can only reach multiple Jupiter masses (Zurlo et al. 2016).

The modelling in this paper assumes that the disc has sharp edges and is described by a single power law. In reality there are likely particles within the inner edge and the radial distribution may be better described by a rising then falling power law or a Gaussian-like distribution. The low level of signal-to-noise in the data does not warrant exploration of more detailed radial distributions, but they would be un-
likely to affect our conclusions as the clearing of the chaotic zone is not 100% efficient and so the inner edge referred to in the analytical and dynamical models is also not a sharp edge.

5 CONCLUSIONS

This paper presents the ALMA observations of the debris disc around the star HR 8799. The observations were conducted in band 6 using a compact configuration. Using MCMC techniques, a parametric disc model is fit to the data. Assuming a single power law radial distribution, the inner edge is found to be 145\pm12 AU and the outer edge is 429\pm37 AU, whilst the inclination is found to be 40\pm6 at a position angle of 51\pm8\textdegree. The inner edge found here agrees with that found by previous modelling of sub-mm data (Hughes et al. 2011) but not with the models of the far-infrared data (Su et al. 2009; Matthews et al. 2014). It is also inconsistent with the edge of planet b’s chaotic zone given its current orbit. This likely means that either planet b’s orbit has varied over time or a smaller planet exists beyond its orbit. The outer edge is clearly much further out than the models that fit to the infrared data (Su et al. 2009; Matthews et al. 2014). This shows the benefit of sub-mm observations, which only detect dust in the planetesimal belt, whereas with infrared observations it is difficult to distinguish between the planetesimal belt and the halo of small grains being pushed out by radiation pressure. Finally, the CO detected in these observations confirms the prior observations that the CO in the cloud has the same radial velocity as that of the star and the clump in CO is found to overlap with the disc.

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