Hadronic versus Leptonic Models for $\gamma$-Ray Emission from VER J2227+608

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Abstract

Recent observations of VER J2227+608 reveal a broken power $\gamma$-ray spectrum with the spectral index increasing from $\sim 1.8$ in the GeV energy range to $\sim 2.3$ in the TeV range. Such a spectral break can be attributed to radiative energy loss of energetic electrons in the leptonic scenario for the $\gamma$-ray emission, which, in combination with the characteristic age of the nearby pulsar, can be used to constrain the magnetic field in the emission region. We show that the radio and X-ray observations can also be explained in such a scenario. In the hadronic scenario, the spectral break can be attributed to diffusion of energetic ions in a turbulent medium and detailed spectral measurement can be used to constrain the diffusion coefficient. These two models, however, predict drastically different spectra above 100 TeV, which will be uncovered with future high-resolution observations, such as Large High Altitude Air Shower Observatory (LHAASO) and/or Cherenkov Telescope Array (CTA).

Unified Astronomy Thesaurus concepts: Galactic cosmic rays (567); Gamma-ray sources (633); Non-thermal radiation sources (1119); Gamma-ray astronomy (628); Extended radiation sources (504); Supernova remnants (1667); Diffuse nebulae (382); Rotation powered pulsars (1408); Cosmic ray sources (328); Cosmic ray astronomy (324); Astrophysical processes (104); Ultra-high-energy cosmic radiation (1733)

1. Introduction

Identifying PeVatron plays an essential role in addressing the origin of cosmic rays (Albert et al. 2020). Although it is generally accepted that cosmic rays in the GeV and TeV energy ranges should be associated with particle acceleration by shocks in old and young supernova remnants (SNRs), respectively (Zhang et al. 2017), the $\gamma$-ray spectra of SNRs never extend beyond 100 TeV (Zeng et al. 2019), implying that alternative high-energy sources are needed to account for cosmic rays in the PeV energy range (HESS Collaboration et al. 2016). Recently, HAWC discovered several sources beyond 50 TeV and four of their spectra extend beyond 100 TeV (HAWC Collaboration et al. 2019). However, all these sources appear to be associated with powerful pulsars with evidence of spectral softening toward high energies.

VER J2227+608 was discovered by the VERITAS collaboration (Acciari et al. 2009), confirming earlier detection of TeV emission from this direction by the Milagro experiment (Abdo et al. 2007). Fermi observations revealed a GeV counterpart with a hard spectrum with the best-fit spectral index of $1.81 \pm 0.16$ (Xin et al. 2019). Recent HAWC observations of this source, in combination with VERITAS measurement, uncovered a single power-law spectrum in the TeV energy range with a spectral index of $\sim 2.3$ (Albert et al. 2020). In the hadronic scenario for the $\gamma$-ray emission, the authors obtained a lower limit of 800 TeV for the cutoff energy of the parent proton distribution, making it a promising PeVatron. Their observations, however, do not exclude the possibility of spectral softening beyond 100 TeV. A leptonic scenario may also fit their data.

In this Letter, we carry out detailed modeling of multi-wavelength emission from VER J2227+608 and the associated pulsar wind nebula PSR J2229+6114 and SNR G106.3+2.7 (Pineau & Joncas 2000; Halpern et al. 2001b; Kothes et al. 2001). The related observations are summarized in Section 2. In Section 3, we present the key results of our spectral modeling. Conclusions are drawn in Section 4.

2. Observations

G106.3+2.7 was discovered by a 408 MHz radio survey as having an elongated shape with a bright head to the northeast (Joncas & Higgs 1990). It was later interpreted as an SNR with an unusual central bright head–tail morphology (Pineau & Joncas 2000; see also the bottom left panel of Figure 1). A radio and X-ray pulsar PSR J2229+6114 was identified at the north edge of the bright radio head with a spin-down luminosity of $2.2 \times 10^{37}$ erg s$^{-1}$ and a characteristic age of $\sim 10$ kiloyears (Halpern et al. 2001a). Pulsed $\gamma$-ray emission was also revealed with Fermi observations with a luminosity of $1.8 \times 10^{34}$ erg s$^{-1}$ (Abdo et al. 2009a) at a distance of 0.8 kpc determined via analyses of atomic hydrogen and molecular cloud distribution in that direction (Kothes et al. 2001). This pulsar produces a prominent wind nebula, the so-called “Boomerang” PWN with strongly polarized radio emission surrounding an extended diffuse X-ray source (Halpern et al. 2001b; see also the top middle panel of Figure 1). With observations by ROSAT and ASCA, the total 2–10 keV flux of the extended diffuse X-ray source and the pulsar is found to be $1.56 \times 10^{-12}$ erg cm$^{-2}$ s$^{-1}$, with a power-law photon index of 1.51 $\pm$ 0.14 (Halpern et al. 2001b). With Chandra observations, Li et al. (2008) found that the flux from the pulsar is comparable to that of a compact X-ray PWN (Kargaltsev & Pavlov 2008). The X-ray flux adopted here therefore is dominated by the extended source.

$^{\dagger}$ Throughout this Letter, we will not draw distinctions between SNR G106.3+2.7 and VER J2227+608 unless specified otherwise.
Radio observations show that the overall spectral index of the whole SNR is $\sim -0.57$, and the tail region has a slightly steeper spectrum than the head region (Pineault & Joncas 2000). Gao et al. (2011) made the first observation of the entire SNR at \( \lambda = 6 \) cm and obtained an integrated spectral index of $\sim -0.64$ with flux densities at \( \lambda = 11 \) and 21 cm. In combination with the flux density at 408 MHz (Kothes et al. 2006a), there appears to be a spectral break near 500 MHz (Figure 2). For the “Boomerang” PWN, Kothes et al. (2006b) performed a multi-frequency analysis using observations at
high radio frequencies by Effelsberg 100 m radio telescope and low radio frequencies from the Canadian Galactic Plane Survey, and found that its radio continuum spectrum has a break between 4 and 5 GHz, with the spectral index varying from −0.11 to −0.59 (Kothes et al. 2006b). We reanalyzed these radio data and extracted flux densities from the bright regions indicated by green lines in the top row of Figure 1. The data points are shown as lower radio points in Figure 2.

Very high-energy emission from the direction of G106.3 +2.7, which was later named VER J2227+608 by the VERITAS collaboration (Acciari et al. 2009), was first reported by the Milagro experiment (Abdo et al. 2007). Xin et al. (2019) found prominent extended GeV emission with a spectral index of 1.81 ± 0.16 from the tail region of G106.3+2.7. Here, in addition a point source at PSR J2229+6114 and a uniform disk with a radius of 0′25 centered at (R.A., decl.) = (336°68, 60°88) for the Fermi source, we adopted a uniform disk with a radius of 0′2 centered at (R.A., decl.) = (337°30, 61°12) to calculate the upper limits of GeV γ-ray emission from the head region. The results are shown as green arrows in Figure 2. Recently, HAWC found that the TeV spectrum of VER J2227+608 can be fitted with a power-law with a spectral index of 2.29 ± 0.17, and all this high-energy emission appears to be from the tail region of the SNR.

3. Modeling

Based on the detection of a radio spectral break near ~5 GHz from the PWN, Kothes et al. (2006b) argued that the break is caused by synchrotron radiative energy loss of emitting electrons in a magnetic field of ~3 mG. We find several caveats for this scenario. (1) In the relative compact region of ~0.4 pc, the magnetic field has a total energy of ~10^{40} erg. The volume of the whole SNR is at least 1000 times larger than that of the PWN. For a comparable magnetic field in the SNR, the magnetic field would require an energy greater than 10^{41} erg, which is too high for a typical SNR (Chevalier & Reynolds 2011). Since the overall radio spectrum of G106.3 +2.7 shows evidence of softening toward high frequencies (Gao et al. 2011), its spectrum may also have a break near 500 MHz. If these spectral breaks have a common origin, the magnetic field in the SNR is then at most 10 times weaker than that in the PWN and is still too high for typical SNRs and PWNe. (2) For relativistic electrons accelerating in a magnetic field $B$, the synchrotron emission has a characteristic frequency of $\sim 4B^2 \gamma^2$ MHz, where $\gamma$ is the electron Lorentz factor. Electrons producing the 5 GHz radio emission therefore have a Lorentz factor of $\sim 700$, which appears to be too low for particle acceleration in PWNe. Given the hard spectrum below the break, this spectral feature is likely associated with the injection process (Olmi & Bucciantini 2019). It is interesting to note that based on modeling of the structure of PWNe affected by reverse shocks of SNRs, Chevalier & Reynolds (2011) reached similar conclusions for the magnetic field and origin of the radio spectral break.

Here we explore the possibility that magnetic fields in the γ-ray emission region are so weak that we may attribute the γ-ray spectral break to energy loss of energetic electrons in the leptonic scenario for the γ-ray emission. Given the relatively weak X-ray emission, there is increasing evidence that the magnetic fields in many extended TeV sources are less than 100 µG. In some extreme cases, the magnetic fields derived from multiwavelength observations are within 10 µG (Matsumoto et al. 2008; Fujinaga et al. 2011; H. E. S. S. Collaboration et al. 2019; Liu et al. 2019).

The processes of particle acceleration and transport in PWNe cover a large-scale range and are complicated in general (Olmi & Bucciantini 2019). We are mostly interested in large-scale features, and acceleration processes at small scales may be described with stochastic particle acceleration in a turbulent medium (Schlickeiser 1984). In this context, we will adopt a quantitative model first proposed for hotspots in radio galaxies (Fan et al. 2008). The model has two distinct zones. A steady acceleration region (Ac) is characterized by a particle injection rate, energy-independent particle acceleration, and escape times, whose ratio determines the index of particles escaping from the acceleration site, and a magnetic field, which in combination with the acceleration time determines the cutoff energy of the electron distribution for the synchrotron radiative energy loss. Electrons escaping from the Ac are injected into a uniform cooling zone. In the absence of observational evidence for spectral hardening below the spectral cutoff, we will ignore the expansion of the Ac implying that the cooling zone has the same magnetic field as the Ac. There are therefore six model parameters: the injection rate and injection energy in the Ac, the acceleration and escape times, and the magnetic field and age of the system.

The left panel of Figure 2 shows our fit to the multiband spectral energy distribution of G106.3+2.7 in the leptonic scenario for the γ-ray emission. For the IC emission, in addition to the cosmic microwave background radiation, we assume a near-infrared background with a temperature of 20 K and an energy density of 0.3 eV cm^{-3} (Abeysekara et al. 2017). The model parameters are indicated in the figure. The magnetic field $B = 4 \mu$G and the age of the system $T$ is fixed at 10 ky. The electron distribution cuts off at $\gamma_c = 10^{10}$. The acceleration time is given by the energy loss time at the cutoff energy $\gamma_c m_e c^2$: $\tau_{ac} \approx 25 \gamma_c^{-1} B^{-2}/2$ yr $\approx 150$ yr, which is longer than the gyropertime of ~28 yr for electrons with $\gamma_c = 10^{10}$ moving in a magnetic field of 4 $\mu$G. We note that $\gamma_c$ is not well constrained by our spectral fit and the value of $10^{10}$ can be considered a lower limit to fit the HAWC spectral measurement. Theoretically, $\gamma_c$ can be a factor of 5 larger for the case of maximum acceleration in magnetic reconnection (Tavani et al. 2011).

The spectral index of electrons escaping the Ac is $\alpha = 2.5$. The escape time is then $\tau_{esc} = 4\tau_{ac}/27 \approx 22$ yr. The injection energy at the Ac is $\gamma_{inj} = 5 \times 10^3$, which is constrained by the radio spectral break near 500 MHz. The injection rate is proportional to the total energy of emitting electrons. Here we give the total energy of electrons above 1 GeV $W_e = 1.4 \times 10^{57}$ erg. For comparison, the total energy of uniformly distributed magnetic field in the SNR is about $7.4 \times 10^{54}$ erg. These values are compatible with the leptonic model proposed by Xin et al. (2019). Since we have a softer electron distribution, implying more electrons with relatively lower energies, the overall magnetic field is weaker than the $8 \mu$G field they found and the total energy of electrons above 1 GeV is higher than their value of $4 \times 10^{46}$ erg.

The electron distribution in the cooling region has a broken power-law form with a break Lorentz factor $\gamma_b \approx 1.5 \times 10^8$,
where the radiative energy loss time is about 10 kyr for the age of the SNR. Via the IC, such a distribution leads to a $\gamma$-ray spectral softening above a few TeVs due to the KN effect. Although the $\gamma$-ray spectrum is soft near 100 TeV, it is still compatible with HAWC observations. Better spectral measurement beyond 100 TeV will be able to test this model.

The blue lines in the left panel of Figure 2 show emission from the Ac, which should be associated with an X-ray bright region near the pulsar (Kargaltsev & Pavlov 2008). However, the magnetic field at small scales should be high. At the surface of the neutron star, the magnetic field can be as high as $2 \times 10^{12}$ G (Halpern et al. 2001a). As mentioned above, the particle acceleration and transport near the pulsar are complicated, electrons with a small pitch angle to the magnetic field are expected to escape from the acceleration region more easily (Olmi & Bucciantini 2019). The magnetic field we derived from the spectral fit therefore should be interpreted as an effective magnetic field for electrons with small pitch angles moving in a much stronger magnetic field.

The model can also explain the diffuse X-ray emission at the PWN with electrons escaping from the Ac during the past 800 yr, as indicated by the purple lines in the left-panel of Figure 2. There are two sets of radio data. The upper one is for the overall emission and the lower one is for bright regions at the PWN and the head. The X-ray emission region of the PWN only covers part of the radio-bright regions and should have lower radio fluxes. The solid red line is for the overall emission from the SNR. We therefore expect soft diffuse X-ray emission from the head and tail regions with the X-ray spectral index to increase with increasing distance from the pulsar. Similarly, higher-energy $\gamma$-rays should originate from regions closer to the pulsar. The lack of GeV $\gamma$-ray emission from the head may be attributed to its stronger magnetic field or softer electron distribution, as suggested by its relatively softer radio spectrum shown in Figure 2.

The hadronic scenario is relatively simple. We assume instantaneous injection of protons into a uniform emission zone with a density of $n$ and a radius of $R$ at $T = 10$ kyr ago. The injected protons have a power-law energy distribution with an exponential cutoff $E_{cut}$:

$$Q(E) = Q_0 E^{-\Gamma} \exp(-E/E_{cut}),$$

where $\Gamma$ is the spectral index. We also assume a constant diffusion coefficient within $R$:

$$D(E) = D_0 \left( \frac{E}{10 \text{GeV}} \right) ^{\delta}.$$

Then the proton distribution within the emission zone is given by

$$N_p(E, T) = Q(E) 4 \pi \int_{0}^{R} r^2 dr \frac{1}{(4 \pi D(E) T)^{1/2}} \exp \left[ -\frac{r^2}{4D(E)T} \right].$$

It is evident that $N_p$ only depends on $Q(E)$ and $R^2/D(E)T$. We consider two values of $\delta$ for the diffusion coefficient. In a Kolmogorov turbulence, $\delta = 1/3$, while in the Kraichnan turbulence, $\delta = 1/2$. The right panel of Figure 2 shows our fit to the $\gamma$-ray spectrum with $\Gamma = 1.8$, $E_{cut} = 10$ PeV, and $R^2/D_0 T = 500$, and 63 for $\delta = 1/2$, and 1/3, respectively. At low energies with $R^2 \gg D(E) T$, $N_p$ approximately equals $Q(E)$. $N_p$ will deviate significantly (by a factor of $\sim 5$) from the power-law extension from low energies at $E_d$ where $R^2 = 4D(E_d)T$. Then we have $E_d = 160$, and 39 TeV for $\delta = 1/2$, and 1/3, respectively. We note that the diffusion coefficients we have here are about one order of magnitude lower than mean values around TeV PWNe (Di Mauro et al. 2020) but are comparable to that derived for the Vela X (Bao et al. 2019). To increase the diffusion coefficient, one needs to increase the size of the emission zone or decrease the age $T$ of the system so that the $\gamma$-ray spectrum does not change significantly. The total energy of protons above 1 GeV is about $4 \times 10^{48} (n/1 \text{ cm}^{-3})^{-1} \text{ erg}$ in the emission zone, which is consistent with that obtained by Xin et al. (2019). The averaged energy density is about tens of $eV \text{ cm}^{-3}$, which is typical for TeV halos (Giacinti et al. 2020). The corresponding total energy of injected protons is 8.5 and $11 \times 10^{48} (n/1 \text{ cm}^{-3})^{-1} \text{ erg}$ for $\delta = 1/2$, and 1/3, respectively. Compared with the leptonic scenario, the hadronic models predict much harder spectra at 100 TeV and beyond and an increase of the source extension with energy, which can be uncovered with future observations. Better $\gamma$-ray spectral measurement can also be used to constrain the diffusion coefficient.

The model here assumes spherical symmetry and efficient particle acceleration at the birth of the pulsar (Ohira et al. 2018), while the source is highly asymmetric. Since the pulsar was likely born at its current location (Kothes et al. 2001), there is a convective flow from the pulsar to the $\gamma$-ray-emitting tail region. Such a convection will lead to an increase of distance between the pulsar and $\gamma$-ray emission region with the decrease of energy for the energy-dependent diffusion, reminiscent of the leptonic scenario. The overall $\gamma$-ray spectrum, however, will not be affected, as the emission zone is more or less uniform.

4. Conclusions

We have shown that the broken power-law $\gamma$-ray spectrum of VER J2227+608 can be explained with both the leptonic and hadronic scenarios for the $\gamma$-ray emission with reasonable parameters. These two models, however, predict distinct spectra above 100 TeV. High-resolution observations such as Large High Altitude Air Shower Observatory (LHAASO) and Cherenkov Telescope Array (CTA) should be able to test these models.

The hadronic model attributes the spectral break to an energy-dependent diffusion process. To account for the observed $\gamma$-ray flux, the total energy of relativistic protons injected into the emission region is about $10^{50} (n/1 \text{ cm}^{-3})^{-1} \text{ erg}$. Although it is tempting to attribute such a population of protons to shock acceleration in the early stage of SNR evolution, as the only SNR with emission above 100 TeV, its pulsar may also play an important role in the proton acceleration (Ohira et al. 2018). Other powerful young PWNe then should have a similar emission component if there are sufficient background materials to support efficient hadronic emission. The model also requires a very low diffusion coefficient, commonly revealed in extended TeV sources (Di Mauro et al. 2020).

The leptonic scenario is very interesting in light of extensive multiwavelength studies of Vela X PWN and its pulsar, which has a similar characteristic age and a four times lower spin-down luminosity (Chevalier & Reynolds 2011). The center of the TeV source is also displaced from the pulsar. The TeV spectrum of Vela X cuts off a bit above 10 TeV, a cutoff that...
has been attributed to radiative energy loss of TeV electrons displaced by reverse shocks of the SNR a few thousand years ago (Bao et al. 2019). In our model, we have a constant injection rate of high-energy electrons into the cooling region, implying a very long spin-down age for PSR J2229+6114. It is possible that the spin-down age of Vela pulsar is within a few thousand years so that injections over the past few thousand years are negligible (Liu et al. 2019). Nevertheless, we expect some flux of γ-rays beyond 100 TeV from Vela X due to recent injection of high-energy electrons into the nebula. Detailed modeling of such PWNe is warranted (Chevalier & Reynolds 2011).

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**References**

Abdo, A. A., Ackermann, M., Ajello, M., et al. 2009a, *ApJ*, 706, 1331

Abdo, A. A., Allen, B., Berley, D., et al. 2007, *ApJL*, 664, L91

Abdo, A. A., Allen, B. T., Aune, T., et al. 2009b, *ApJL*, 700, L127

Abeysekara, A. U., Albert, A., Alfaro, R., et al. 2017, *Sci*, 358, 911

Acciari, V. A., Aliu, E., Arlen, T., et al. 2009, *ApJL*, 703, L6

Albert, A., Alfaro, R., Alvarez, C., et al. 2020, *ApJL*, 896, L29

Bao, Y., Liu, S., & Chen, Y. 2019, *ApJ*, 877, 54

Chevalier, R. A., & Reynolds, S. P. 2011, *ApJL*, 740, L26

Di Mauro, M., Manconi, S., & Donato, F. 2020, *PhRvD*, 101, 103035

Fan, Z.-H., Liu, S., Wang, J.-M., Fryer, C. L., & Li, H. 2008, *ApJL*, 673, L139

Fujinaga, T., Bamba, A., Dotani, T., et al. 2011, *PASJ*, 63, S857

Gao, X. Y., Han, J. L., Reich, W., et al. 2011, *A&A*, 529, A159

Giachinti, G., Mitchell, A. M. W., López-Coto, R., et al. 2020, *A&A*, 636, A113

H. E. S. S. Collaboration, Abdalla, H., Aharonian, F., et al. 2019, *A&A*, 627, A100

Halpern, J. P., Camilo, F., Gotthelf, E. V., et al. 2001a, *ApJL*, 552, L125

Halpern, J. P., Gotthelf, E. V., Leighly, K. M., & Helfand, D. J. 2001b, *ApJ*, 547, 323

HAWC Collaboration, Abeysekara, A. U., Albert, A., et al. 2019, *PhRvL*, 124, 021102

HESS Collaboration, Abramowski, A., Aharonian, F., et al. 2016, *Natur*, 531, 476

Joncas, G., & Higgs, L. A. 1990, *A&AS*, 82, 113

Kargaltsev, O., & Pavlov, G. G. 2008, in AIP Conf. Ser. 983, 40 Years of Pulsars: Millisecond Pulsars, Magnetars and More, ed. C. Bassa et al. (Melville, NY: AIP), 171

Kothes, R., Fedotov, K., Foster, T. J., & Uyaniker, B. 2006a, *A&A*, 457, 1081

Kothes, R., Reich, W., & Uyaniker, B. 2006b, *ApJ*, 638, 225

Kothes, R., Uyaniker, B., & Pineault, S. 2001, *ApJ*, 560, S6

Li, X.-H., Lu, F.-J., & Li, Z. 2008, *ApJ*, 682, 1166

Liu, R.-Y., Ge, C., Sun, X.-N., & Wang, X.-Y. 2019, *ApJ*, 875, 149

Matsumoto, H., Uchiyama, H., Sawada, M., et al. 2008, *PASJ*, 60, S163

Ohira, Y., Kisaka, S., & Yamazaki, R. 2018, *MNras*, 478, 926

Olmi, B., & Bucciantini, N. 2019, *MNras*, 490, 3608

Pineault, S., & Joncas, G. 2000, *AJ*, 120, 3218

Schlickeiser, R. 1984, *A&A*, 136, 227

Tavani, M., Bulgarelli, A., Vittorini, V., et al. 2011, *Sci*, 331, 736

Xin, Y., Zeng, H., Liu, S., Fan, Y., & Wei, D. 2019, *ApJ*, 885, 162

Zeng, H., Xin, Y., & Liu, S. 2019, *ApJL*, 874, 50

Zhang, Y., Liu, S., & Yuan, Q. 2017, *ApJL*, 844, L3