PULSAR TIMING CONSTRAINTS ON CUMULATIVE AND INDIVIDUAL MASS OF STARS IN THE GALACTIC CENTER

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ABSTRACT

We consider the time derivatives of the period $P$ of pulsars at the Galactic Center due to variations in their orbital Doppler shifts. We show that in conjunction with a measurement of a pulsar’s proper motion and its projected separation from the supermassive black hole, Sgr A*, measuring two of the three derivatives $\dot{P}$, $\ddot{P}$, or $\dddot{P}$ sets a constraint that allows for the recovery of the complete six phase space coordinates of the pulsar’s orbit, as well as the enclosed mass within the orbit. Thus, one can use multiple pulsars at different distances from Sgr A* to determine the radial mass distribution of stars and stellar remnants at the Galactic center. Furthermore, we consider the effect of passing stars on the pulsar’s period derivatives and show how it can be exploited to measure the characteristic stellar mass in the Galactic center.

Key words: Galaxy: center – pulsars: general

1. INTRODUCTION

The recent discovery of J1745-2900, a magnetar orbiting the supermassive black hole Sgr A* at a projected separation of 0.09 pc (Mori et al. 2013; Rea et al. 2013; Kennea et al. 2013) stimulated much interest in its timing and astrometry. Pulsars close to Sgr A* could allow for a precise measurement of the black hole’s mass and spin, in addition to a host of relativistic effects (Pfahl & Loeb 2004; Cordes et al. 2002; Kramer et al. 2004; Psaltis & Johannsen 2011; Liu et al. 2012).

Unfortunately, the timing of the magnetar J1745-2900 is not sufficiently stable for dynamical measurements (Kaspi et al. 2014). Furthermore, it is located too far from Sgr A* (with a Keplerian orbital period of $\sim$500 yr) for it to be useful as a probe of strong field gravity. Calculations imply that there could be $\sim$200 pulsars within a parsec from Sgr A* (Chennamangalam & Lorimer 2014), although perhaps only $\sim$20 of them being bright enough to be detected (Dexter & O’Leary 2014). Most of these pulsars might also be located too far from Sgr A* for testing strong field gravity.

Nevertheless, one can still use pulsars at these larger distances to probe the astrophysical environment of the Galactic center. In particular, the orbital dynamics of a pulsar is determined by the mass distribution within its orbit. Therefore, by measuring the imprint of the orbital Doppler effect on the pulsar’s period, $P$, one should be able to constrain the radial mass profile of stars and stellar remnants around Sgr A*. A previous study (Chaname & Gould 2002) considered this possibility, but neglected the contributions of closely passing stars. In this letter, we evaluate the limitations of this technique due to this extra source of uncertainty, and also show that one can constrain the characteristic stellar mass in this environment by measuring the third time derivative of the pulsar’s period, $\dddot{P}$.

This paper is organized as follows. In Section 2, we discuss the orbital contribution to the first, second, and third period derivatives $\dot{P}$, $\ddot{P}$, and $\dddot{P}$ by the mean field, and discuss how it can be used to measure the mass enclosed within the pulsar’s orbit. In Section 3, we calculate the effects of passing stars on the period derivatives, and how it could be used to constrain the characteristic stellar mass in the Galactic center.

2. MEASURING THE ENCLOSED MASS VIA THE MEAN FIELD CONTRIBUTION TO PERIOD DERIVATIVES

We begin with the equation for classical Doppler shift relating the observed period $P_O$ to the intrinsic (rest frame) period $P_i$:

$$P_O = P_i(1 - \beta \cdot \hat{n}) ,$$

where $\beta$ is the velocity of the pulsar in units of $c$, and $\hat{n}$ is the unit vector pointing from the pulsar to the observer (see Figure 1 for geometry). In general, pulsar timing measurements are done with respect to the solar system barycenter. However, since the motion of the solar system barycenter is well constrained (Reid et al. 1999), in writing Equation (1) we shifted to the frame where the observer is at rest with respect to the black hole. This could be done by the substitution $P \rightarrow P(1 - \beta_{ss} \cdot \hat{n})$, where $\beta_{ss}$ is the velocity of the solar system barycenter in units of $c$. Since both $\beta$ and $\hat{n}$ changes with time, the orbit of the pulsar induces nonzero time derivatives on $P_O$. Since the orbital time is much longer than the observation time, we can use a Taylor expansion in time $t$ to write

$$P_O(t) = P_O(0) + \dot{P}_O(0)t + \frac{1}{2} \ddot{P}_O(0)t^2 + \frac{1}{6} \dddot{P}_O(0)t^3 + \cdots \cdots .$$

The first two derivatives have been previously studied in the context of globular clusters (Phinney 1993). In this section we provide a treatment of $\dot{P}$, $\ddot{P}$, and $\dddot{P}$ for pulsars at the Galactic center. In general, these time derivatives depend on the pulsar’s six position and velocity phase space coordinates, as well as the enclosed mass. While throughout this paper we focus on the period derivatives themselves, we note that they are not the observables in pulsar timing measurements. Rather, timing measurements measure the frequency, $v = 1/P$, and its derivatives (Lorimer & Kramer 2005). The period derivatives depend not only on the frequency derivative of the same order, but on all successive frequency derivatives up to that order.

Direct imaging (e.g., Rea et al. 2013) yields the projected separation of the pulsar from Sgr A*. The proper motions of pulsars have been measured previously both in the context of quantifying the pulsar’s natal kick (e.g., Kaplan et al. 2008) and
for astrometric purposes (e.g., Du et al. 2014). In particular, the proper motion of J1745-2900 is currently being measured (Bower et al. 2014).

Line-of-sight distances to pulsars can be obtained via parallax (see Du et al. 2014 for an example of the technique applied to a millisecond pulsar not at the Galactic center), and progress has been made to measure the parallaxes of pulsars at large distances (up to 7.2 kpc) using very-long-baseline interferometers (Chattejee et al. 2009). The recently launched Gaia satellite\(^1\) is also expected to further improve the prospect of measuring pulsar parallaxes for pulsars with sufficiently bright optical companions. Further, for millisecond pulsars with high timing precision, timing analysis can also determine line-of-sight distances (Verbiest et al. 2008).

In addition, the distance to pulsars can be estimated from their pulse dispersion measure. The delay in pulse arrival time as a function of frequency, along with a model of the free electron distribution (e.g., the NE2001 model of Cordes & Lazio 2002, 2003), can be used to estimate distances. This method was recently applied to the Galactic center for the magnetar J1745-2900 (Eatough et al. 2013; Shannon & Johnston 2013). However, we note that the accuracy of the pulse dispersion measure distances depends strongly on knowledge of the free electron distribution. The electron distribution at the Galactic center is highly unconstrained, and thus the distance measured might not be reliable enough for our purposes.

Based on the above measurements, one can determine five out of six of the pulsar’s phase space coordinates. Another constraint can be placed via a measurement of one of the period derivatives, thereby constituting a full determination of its six phase space coordinates. Furthermore, we will show that with the measurement of another period derivative, one could directly measure the mass enclosed.

\[ 2.1. \text{The First Period Derivative} \]

The first time derivative of the pulsar’s period \( P \) is given by

\[
\dot{P}_O = -P_1 \frac{\partial \beta \cdot \hat{n}}{\partial t} = P_1 \left( \beta \sin \theta \frac{\partial \theta}{\partial t} - \hat{n} \cdot \frac{\partial \beta}{\partial t} \right),
\]

where \( \beta \equiv |\beta| \), and the subscript \( O \) denotes the orbital contribution to \( \dot{P}_O \), in difference from the \textit{intrinsic} pulsar spindown, \( \dot{P}_I \). The acceleration of the pulsar is given by

\[
\frac{\partial \beta}{\partial t} = \frac{GM}{r^2c} \hat{r},
\]

where \( M(r) \equiv M_{BH} + M_\star(r) \) is the total mass, namely, the mass of the supermassive black hole Sgr A*; \( M_{BH} = (4.31 \pm 0.36) \times 10^6 M_\odot \) (Gillessen et al. 2009; Ghez et al. 2008), plus the mass of the stars within the pulsar’s orbit. Substituting this into Equation (3) gives

\[
\frac{\dot{P}_O}{P_I} = \beta \sin \theta \frac{\partial \theta}{\partial t} + \frac{GM}{r^2c} \left( \hat{n} \cdot \hat{r} \right) = \beta \sin \theta \frac{\partial \theta}{\partial t} - \frac{GM}{r^2c} \cos \phi,
\]

where \( \phi \) is the angle between the pulsar’s radius vector \( \hat{r} \) and \( \hat{n} \). The negative sign arises from the direction of \( \hat{r} \). Noting that

\[
\frac{\partial \theta}{\partial t} = \frac{c}{\beta} \sin \theta,
\]

where \( d \) is the displacement of the solar system barycenter from the supermassive black hole Sgr A*, we obtain

\[
\frac{\dot{P}_O}{P_I} - \frac{c\beta_\perp^2}{d} - \frac{GM}{r^2c} \cos \phi = \frac{c\beta_\perp^2}{d} - \frac{GM}{r^2c} \sin^2 \phi \cos \phi,
\]

where \( \beta_\perp \) is the transverse component of \( \beta \) and we have used the definition of the projected distance: \( d_p \equiv r \cos \gamma \approx r \sin \phi \) in the second equality. Solving for \( \phi \), we obtain

\[
\sin^2 \phi \cos \phi = \frac{c}{GM} \left[ \frac{c\beta_\perp^2}{d} - \dot{P}_O/P_I \right].
\]

Defining \( r_i \) as the component of \( r \) in the line-of-sight direction:

\[
\frac{r_i}{r^3} = \frac{c}{GM} \left[ \frac{c\beta_\perp^2}{d} - \dot{P}_O/P_I \right].
\]

Note that in addition to the spindown rate due to the orbital Doppler effect, a portion of the observed \( \dot{P}_o \) is due to intrinsic radiative losses. The overall spindown rate is the sum of the \textit{intrinsic} \( \dot{P}_I \) and the orbital \( \dot{P}_O \) components. Given this perspective, we view Equation (9) as providing a new constraint to the orbital contribution to \( \dot{P} \) can account for at most \( \sim 17\% \) of the observed \( \dot{P} \) (assuming the observed \( \dot{P}_{obs} \) value of Mori et al. 2013). In this context, we can therefore be certain that measurements of the magnetar’s magnetic field strength is not contaminated significantly by the orbital component \( \dot{P}_O \).

If there is a way to measure \( \dot{P}_O \) on its own (e.g., if the magnetic field of the pulsar is small, and the orbital contribution dominates), or in the case of millisecond pulsars, where \( \dot{P}_O \) dominates \( \dot{P}_{obs} \), Equation (9) provides a new constraint to the pulsar’s phase space position. For example, if it is observed that

\[
\frac{\dot{P}_O}{P_I} = \frac{c\beta_\perp^2}{d},
\]

then

\[
r = d_p.
\]

Another case where the pulsar is orbiting in the Sgr A*-observer plane with \( P = 5 \times 10^{-15} \) and \( M \approx M_{BH} \) is presented in Figure 2.
2.2. The Second Period Derivative

If $\ddot{P}_O$ is measured, Equation (9) constitutes a new constraint on the pulsar’s phase space coordinates, allowing all six components to be determined. This last constraint is a function of the enclosed mass, $M$, which can be solved via a measurement of another period derivative. Taking the derivative of Equation (3) and noting that $\dot{r}_l$ is constant, we find

$$\frac{\ddot{P}_O}{P_i} = -\frac{GM}{c^2} \frac{\partial}{\partial t} \left[ \frac{\cos \phi}{r^2} \right],$$

$$= \frac{GM}{c} \left[ \frac{\sin \phi}{r^2} \frac{\partial \phi}{\partial t} + 2 \frac{\cos \phi}{r} \frac{\partial r}{\partial t} \right].$$

A pulsar on a purely circular orbit with an orbital frequency $\Omega = \beta c/r$ orbiting in the pulsar-Sgr A*-observer plane has

$$\frac{\partial r}{\partial t} = 0; \quad \frac{\partial \phi}{\partial t} = -\Omega = -\frac{\beta c}{r},$$

implying

$$\frac{\ddot{P}_O}{P_i} = -\frac{GM \sin \phi}{c r^2} \Omega = -GM \frac{d_r}{r^4} \beta,$$

which can be solved trivially for either $M(r)$ or $r(M)$ given $\beta$ (or limits of the quantity given the proper motion, $\beta_\perp \leq \beta$) and the projected separation $d_p$. For a pulsar with $P_O = 1$ s at the projected separation of J1745-2900 ($d_p = 0.09$ pc) that is currently at a phase of its orbit where $r \sim d_p$ and $\beta \sim 0.3 \times 10^{-3}$, we find that

$$|\ddot{P}| \approx 5 \times 10^{-23} \text{ s}^{-1}.$$ (16)

Within one year, the drift in $\dot{P}$ is

$$|\Delta \dot{P}| \approx 1.5 \times 10^{-15},$$ (17)

which is within the precision attainable in pulsar measurements (Taylor et al. 1993; Manchester et al. 2005). If a millisecond pulsar is found at the Galactic center, then $\ddot{P}$ could be measured to a precision of $10^{-20}$ (e.g., Champion et al. 2005). In general, $r^2 = (d_p^2 + r_i^2)$, therefore,

$$\frac{\partial r}{\partial t} = \frac{1}{2r} \frac{\partial r^2}{\partial t}$$ (18)
Considering $P \approx P_i \approx 1 \text{s}$, a magnetic field $B = 10^{12} \text{G}$, and the typical radius, $R = 10 \text{km}$, and mass, $M = 1.4 \, M_\odot$, for a neutron star, and adopting $\sin \alpha = 1$, we obtain the maximum $\dot{P}_i$ to be

$$\dot{P}_i \text{ max} = 7.6 \times 10^{-31} \text{s}^{-1}, \quad (27)$$

which is very small compared to the orbital contribution. This suggests that unlike $\dot{P}_i$, $\dot{P}$ is much less contaminated by the intrinsic contribution, allowing a clean measurement of $\dot{P}_0$. In general, the inclination angle $\alpha$ can be inferred by various methods (Taylor et al. 1993; Lyne & Manchester 1993; Rankin 1990; Miller & Hamilton 1993).

### 2.3. The Third Period Derivative

We now supply the third period derivative. This third timing constrain can be used in lieu of the $\dot{P}$ constraint in cases where $\dot{P}_{\text{obs}}$ is too contaminated by $P_i$. In addition, all three timing constraints can be used in cases where only 4 phase space coordinates are measured (e.g., for pulsars with no measured parallax). We also note that the third derivative $\dddot{P}$ is even less affected by its intrinsic contribution than $\dot{P}$, since $P_i \propto B^6/P_i^3$.

The derivative of Equation (13) is

$$\frac{\dddot{P}_O}{P_i} = \frac{GM}{c^3} \left[ \frac{2}{r^3} \cos \phi \frac{\partial^2 r}{\partial r^2} + \frac{1}{r^2} \sin \phi \frac{\partial^2 \phi}{\partial r^2} - \frac{6}{r^2} \cos \phi \left( \frac{\partial r}{\partial t} \right)^2 ight. $$

$$+ \left. \frac{1}{r^2} \cos \phi \left( \frac{\partial \phi}{\partial t} \right)^2 - \frac{4}{r^3} \sin \phi \frac{\partial r}{\partial t} \frac{\partial \phi}{\partial t} \right], \quad (28)$$

with the following equalities:

$$\frac{\partial^2 r}{\partial t^2} = -\frac{2}{r^2} (d_p \cdot v_{\perp} + r_i v_i) \frac{\partial r}{\partial t} $$

$$+ \frac{1}{r} \left[ v_{\perp}^2 + d_p \cdot a_{\perp} + v_i^2 + r_i a \cos \phi \right], $$

$$\frac{\partial^2 \phi}{\partial t^2} = \frac{\partial}{\partial t} \left( -\frac{v}{r} \cos i \right) = \cos i \left[ \frac{v}{r^2} \frac{\partial r}{\partial t} - \frac{1}{r} \frac{\partial v}{\partial t} \right], \quad (29)$$

and

$$\frac{\partial v}{\partial t} = \frac{1}{v} \left[ v_i a \cos \phi - a \sin \phi \frac{d_p \cdot v_{\perp}}{d_p} \right], \quad (31)$$

where $a = GM/r^2$ and $a_{\perp}$ is its components perpendicular to the line of sight. The magnitude of this orbital contribution can be estimated as (Phinney 1993)

$$\left| \frac{\dddot{P}_O}{P_i} \right| \approx 2 \left[ \frac{GM}{r^4} \right] v^2 \approx 3.1 \times 10^{-33} \text{s}^{-3}, \quad (32)$$

where for the second equality we plugged in numbers for a pulsar at 0.1 pc from the black hole moving at $v \approx 200 \text{ km s}^{-1}$. If the pulsar has period $P_O = 1 \text{s}$, in a year this induces a drift on $P_O$ of magnitude $P_O \times (1 \text{ yr}) \approx 9.4 \times 10^{-26} \text{s}^{-1}$, which is comparable in magnitude to the measured $\dot{P}$s of many observed pulsars (Manchester et al. 2005).

For a well studied pulsar with both a measured $\dddot{P}$ and $\dddot{P}_i$, we get two timing constraints on the phase space coordinates. If the pulsar has a low magnetic field strength or if $P_O$ dominates, there will be a third timing constraint. Treating $M(r)$ as an unknown function, these extra constraints can be used to directly measure the mass enclosed within the pulsar’s orbit. The method is analogous to that presented in Section 2.3.

### 3. Contributions by Stellar Kicks and Measuring the Characteristic Stellar Mass at the Galactic Center

As pointed out in Phinney (1993), stars passing close to the pulsar can gravitationally kick the pulsar, adding another contribution to the time derivatives of the pulsar’s period. In this section, we quantify the probability for these stochastic effects to significantly affect the mean field contribution. The probability of a star being a distance $< b$ away from the pulsar located a distance $r$ away from Sgr A* is

$$P(r) = 1 - \exp[-(4\pi/3) n_\ast \pi b^3], \quad (33)$$

where $n_\ast$ is the number density of stars. Using a density profile for stars around Sgr A* $n_\ast = n_0(r/r_0)^{-1.8}$, and the fact that the total stellar mass at 1 pc is measured to be $M_{\text{IPC}} \approx 2 \times 10^6 M_\odot$ (Genzel et al. 2010), the probability represented in Equation (33) becomes

$$P(r) = 1 - \exp \left[ -\frac{4\pi}{3} b^3 \left( \frac{1.2 M_{1\text{pc}}}{4\pi m_\ast (1 \text{ pc})^{1.2}} \right)^{-1.8} \right]. \quad (34)$$

The contribution of the nearest neighboring star to $\dddot{P}$ equals the mean field contribution at a distance that satisfies

$$b^2 = \frac{m_\ast}{M_\ast(r) + M_{\text{BH}}}, \quad (35)$$

where $M_\ast(r)$ is the total stellar mass within the orbit. The probability for this separation is

$$P(r) = 1 - \exp \left[ -\frac{1.2}{3}(M_{1\text{pc}}/r \text{ (1 pc)})^{1.2} + M_{\text{BH}}^{1.2} \left( \frac{r}{1 \text{ pc}} \right)^{1.2} \right]. \quad (36)$$

For all reasonable values for $m_\ast$, this probability is negligibly small at all radii, showing that the first derivative is uncontaminated by stellar kicks. We corroborated this analytical analysis...
with a numerical $N$-body simulation utilizing the Salpeter mass function for stars. The initial conditions for this simulation were generated using the star cluster integrator, $bhint$ (Lockmann & Baumgardt 2008) with density profile $\rho \propto r^{-1.8}$ and a supermassive black hole of mass $4.3 \times 10^6 M_\odot$ located at the center of the cluster.

However, the contributions of stellar kicks to the higher derivatives is larger. The nearest neighbor contribution to $\ddot{P}/P$ is (Phinney 1993)

$$\left[ \frac{\ddot{P}}{P} \right]_{nn} \approx \frac{G m_\star v_\star}{b^3} \frac{v_s}{c},$$

where $v_\star$ is the relative velocity between the star and the pulsar. Similarly, the mean field contribution is

$$\left[ \frac{\ddot{P}}{P} \right]_{mf} \approx \frac{G (M_\star(r) + M_{BH}) v}{r^3} \frac{v_s}{c},$$

where $v$ is the pulsar’s orbital speed relative to Sgr A$^*$. Equating the two contributions, we find that the nearest neighbor contribution equals the mean field at

$$b^3 = \frac{m_\star}{M_\star(r) + M_{BH}} \frac{v_\star}{v} r^3.$$  

The probability for this separation is again obtained from Equation (34):

$$Pr(r) = 1 - \exp \left[ -\frac{1.2 \frac{v_\star}{v}}{3} \frac{M_{1pc}}{M_\star(r/1 \text{ pc})^{1.2}} + M_{BH} \left( \frac{r}{1 \text{ pc}} \right)^{1.2} \right].$$

The probability decreases with $r$, so that pulsars closer to Sgr A$^*$ are less disturbed by perturbing stars. At a distance of 0.01 pc, the probability for the associated jerks is less than 0.1%. To corroborate this result, we performed a numerical simulation utilizing the Salpeter mass function as displayed in Figure 4.

This simulation shows that passing stars scatter $\dot{P}$ about its mean field value, and its contribution is large at distances larger than $\sim$0.03 pc.

While the analysis of Section 2 is largely unaffected at small $r$, the contribution of passing stars adds a significant source of uncertainty to the interpretation of measured period derivatives at large $r$. Due to the stochastic nature of this contribution, measuring $M(r)$ at large distances necessitates the use of multiple pulsars, whose average $\dot{P}$ should reveal the mean field.

### 3.1. Effect of Changing $m_\star$ on $\ddot{P}$

Although the probability for $\ddot{P}$ to be significantly contaminated by perturbing stars is independent of the characteristic stellar mass, $m_\star$, this is not true for all time derivatives. Here we show that the third period derivative is sensitive to changes in $m_\star$, and that this dependence can be used to probe the characteristic stellar mass at the Galactic center. The nearest neighbor contribution to $\ddot{P}/P$ is (Phinney 1993)

$$\left[ \frac{\ddot{P}}{P} \right]_{nn} \approx 2 \frac{G m_\star v_\star^2}{b^4} \frac{v_s}{c}.$$  

The mean field contribution is

$$\left[ \frac{\ddot{P}}{P} \right]_{mf} \approx 2 \frac{G (M_\star(r) + M_{BH}) v^2}{r^4}.$$  

The nearest neighbor and the mean field contributions are equal when

$$b^3 = \frac{m_\star}{M_\star(r) + M_{BH}} \left( \frac{v_\star}{v} \right)^2 r^4.$$  

In this case, the probability for a star to pass at distance $< b$ from the pulsar is

$$Pr(r) = 1 - \exp \left[ -\frac{1.2 \frac{v_\star}{v}}{3} \frac{M_{1pc}}{M_\star(r/1 \text{ pc})^{1.2}} + M_{BH} \left( \frac{r}{1 \text{ pc}} \right)^{1.2} \right].$$

Figure 5 shows this probability as a function of pulsar-Galactic center distance for $m_\star = 1, 5,$ and $10 M_\odot$. The differences between cases of different $m_\star$’s maxes out at around $r \approx 2$ pc, thus making this the optimal location to perform this study. We note that the difference between $Pr(0.2 \text{ pc})$ with $m_\star = 1 M_\odot$ and $m_\star = 10 M_\odot$ is $\sim 20\%$, and so with Poisson statistic one needs tens of pulsars to distinguish between the two cases.
4. SUMMARY AND IMPLICATIONS

If the pulsar’s projected separation from Sgr A∗, proper velocity, and line-of-sight distance are measured, then five of the six pulsar’s phase space coordinates are known. One of the period derivative constraints represented by Equations (9), (24), or (28) can then be used to derive a final constraint on the pulsar’s phase space coordinates. Another constraint can be used to limit the mass enclosed within the pulsar’s orbit. In this case, the line-of-sight velocity \( v_l \) to limit the mass enclosed within the pulsar’s orbit. In this case, the line-of-sight velocity \( v_l \) and the contribution is large for \( r \) greater than \( 0.03 \) pc. As such, measurements should be taken close to Sgr A∗, where they can constrain cumulative mass of stars and stellar remnants surrounding the black hole. Measuring \( M(r) \) further away from Sgr A∗ will require multiple pulsars, and thus be a challenging task.

Finally, we note that the scatter of \( P \) about the mean field value due to passing stars is affected by the characteristic stellar mass, \( m_\ast \). As such, measurements of \( P \) of multiple pulsars at the Galactic center will allow us to probe the characteristic mass of stars and remnants in this extreme environment. Such measurements can also place exquisite constraints on the existence of intermediate-mass black holes in the vicinity of Sgr A∗.

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