A review of the applications of ion floatation: wastewater treatment, mineral beneficiation and hydrometallurgy

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Ion floatation was originally used for pre-concentrating precious metals from dilute solutions. To date, it has attracted widespread attention in many fields due to its low energy requirements, simplicity, rapid operation, small space requirements, suitability for a variety of target ions at various levels, small volume of sludge, low residual concentration, and low operating cost. This review focuses on the applications of ion floatation in wastewater treatment, mineral beneficiation, such as rare precious metal recovery, and hydrometallurgy, such as pre-concentrating of rare earth elements and selective separation of multicomponent ions. The outlook of ion floatation is also discussed.

1 Introduction

As early as 1937, Langmuir and Schaefer observed an interesting and profound phenomenon where insoluble stearic acid on the surface of a solution can adsorb metal ions dissolved in the solution. It was not until 1959 that Sebba suggested using this phenomenon as a means of concentrating ions from solution, even very dilute solution, by a floatation method. This process is called ion floatation.

Ion floatation is a specific separation method that involves adding surfactants or collectors with opposite charges to those of the target ions to form a surfactant complex and then collecting the ions by passing gas bubbles through the solution. A small volume of a hydrophobic product that contains concentrated target ions is formed at the top of a floatation machine and recycled, as clearly depicted in Fig. 1. As a promising separation process, much attention has been paid to ion floatation due to its low energy requirements, simplicity, rapid operation, small space requirements, suitability for a variety of target ions at various levels, small volume of sludge, low residual concentration, relatively low cost, etc.

In the original studies, ion floatation was mostly used for pre-concentrating precious metals from dilute solutions. To date, the ion floatation method has also been applied for wastewater and water treatment, recovery of precious metals, pre-concentrating of rare earth elements and selective separation of multicomponent ions.
concentrating of rare earth elements,\textsuperscript{15,16} and selective separation of multicomponent ions.\textsuperscript{17,18}

The current state of the application of ion flotation is therefore reviewed in this paper. Basically, this review focuses on the application of ion flotation in wastewater treatment, mineral beneficiation, such as rare precious metal recovery, and hydrometallurgy, such as pre-concentrating of rare earth elements and selective separation of multicomponent ions; the intent of this review is to provide ideas and inspiration to spark rapid development of the application of ion flotation.

2 Wastewater treatment

The rapid development of industry and the increasing productivity of many industrial branches have resulted in the pollution of ground water sources; thus, people worldwide face the problems of lack of fresh water together with the spread of various diseases due to organic and inorganic contaminants.\textsuperscript{19} Sustainable development of wastewater is especially stressed because wastewater is a renewable resource from which water can be recovered for reuse.\textsuperscript{20–22} Numerous methods have been developed to remove contaminants from aqueous solutions, such as chemical precipitation, oxidation or reduction, adsorption, coagulation/floculation, filtration, ion-exchange, electrochemical treatment, reverse osmosis, membrane technology, evaporation and electroflotation.\textsuperscript{5,23–25} This may be due to the fact that metal ions can enter water bodies and soil, accumulate in animals and plants through the food chain, and eventually accumulate in the human body, seriously endangering human health and life due to their non-degradability, mobility and persistence.\textsuperscript{26} However, these removal methods have many disadvantages, such as high cost, generation of large amounts of sludge, high reagent or energy requirements, time consumption, incomplete removal of target ions, production of secondary wastes and difficulty of treatment of large volumes of wastewater.\textsuperscript{27–29} Accordingly, ion flotation has been evaluated as a good alternative treatment process for wastewater treatment due to its low energy requirements, simplicity, rapid operation, small space requirements, etc.

Lead is a persistent and toxic contaminant that emanates from acid batteries, painting, printing, ceramic and glass manufacturing, and production of lead additives for gasoline. Long-term exposure can lead to anaemia, cancer, kidney disease, metal retardation, etc.\textsuperscript{30–32} Craioveanu et al. conducted much research on Pb(II) removal; they noted that high removal efficiency (\(R\% = 99.93\)) could be obtained under optimum conditions using a naturally occurring compound (caffeic acid) as a collector. The removal mechanism is based on the fact that caffeic acid contains numerous complexing polar groups that

![Fig. 1 Schematic of the overall process of ion flotation.](image)

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can actively react with metallic ions. Similar studies were carried out by Peng et al.; they found that the removal of Pb(II) could be greater than 99% and the turbidity of the residual solution could decrease to 1.4 NTU by ion flotation under the optimum operation parameters when using graphene oxide (GO) as the collector (as shown in Fig. 2a). In addition, the GO could be reused after desorption, and the Pb(II) removal remained as high as 84.9% in the sixth regeneration (as shown in Fig. 2b). Additionally, they noted that GO was much more efficient than other collectors when used in Pb(II) removal experiments due to the fact that nanoscale GO possesses great numbers of hydroxyl and carboxyl groups that mainly participate in bonding with Pb(II) (as shown in Fig. 2c).

In addition, cadmium may cause destructive trauma to human organs, such as the kidneys, liver, and lungs, and to cardiovascular, immune and reproductive systems. Gratifyingly, in a study by Salmani et al., more than 92.1% of Cd(II) could be efficiently removed from simulated water via ion flotation under the optimum conditions.

Subsequently, more research on metal ion removal via ion flotation was undertaken by many researchers. They found that ion flotation could not only work on single metal ions but also on multicomponent metal ions. Mahmoud et al. carried out an investigation of the simultaneous removal of cationic iron(II) and anion ion chromium(vi) from simulated wastewaters and aqueous solutions. The results indicated that removals of more than 99.5% were obtained for both iron(II) and chromium(vi) in a single step via flotation even when the target ions were at high concentrations and the residual concentrations were all below their permissible limits in potable water. Ni(II) and Zn(II) ions could be removed simultaneously by ion flotation according to the research of Hoseinian et al. The removal rates of Ni(II) and Zn(II) ions were 88% and 92%, respectively, when SDS was used as the collector and Dowfroth 250 as the frother under the effective parameters investigated by experimental design performed by DX7 software and evaluated in a mechanical flotation cell (as shown in Fig. 3).

Almost 100% removal of Cd(II) and Zn(II) at pH 5 and 60% to 70% Sr(II) removal at pH 7 to 9 were achieved by Eivazihollah et al. via ion flotation when 2-dodecyldiethylenetriamine pentaacetic acid (C12-DTPA) served as the collector in combination with two foaming agents: dodecyl trimethyl
ammonium chloride (DoTAC) and dimethyl dodecyl amine-N-oxide (DDAO).\textsuperscript{19} Moreover, Yenidünya studied the removal of Zn(II), Mn(II) and Cu(II) from aqueous solution by ion flotation with sodium dodecyl sulphate in combination with some auxiliary ligands (malic acid, maleic acid and EDTA). He found that the maximum removal rates for Zn(n), Mn(n) and Cu(n) were 90.5\%, 99.8\% and 73.4\%, respectively, within 60 min when the molar ratio between the metal and sodium dodecyl sulphate was 1 : 5. Moreover, by adding auxiliary ligands (malic acid and maleic acid), the recovery efficiencies for all metal ions increased and the flotation times decreased to 40, 20 and 40 min for Zn(n), Mn(n) and Cu(n), respectively, when the molar ratio of metal : sodium dodecyl sulphate : auxiliary ligand was 1 : 5 : 5.\textsuperscript{21} It is evident that ion flotation has a high removal capacity for various metal ions and that the type and dosage of surfactant, solution pH, flotation time, etc. all play important roles in the process. The mechanisms for the removal of metal ions are mainly attributed to electrostatic attraction, ion exchange and surface complexation between the surfactant and target ions; these ions are then separated from the solution by attachment to gas bubbles passing through the solutions.

In addition to heavy metal ions, ion flotation is also commonly used for removing organic and biological pollutants such as oil, triazine herbicides, perfluorooctane sulfonate (PFOS) and perfluorooctanoate, Rhodamine 6G and sulfonyleurea herbicides from wastewater or aqueous solution.\textsuperscript{41–47} Lignin removal research was conducted by Wang et al. through ion flotation using cetyl dimethyl benzyl ammonium as the surfactant. They found that a fraction of more than 0.95 could be removed by continuous ion flotation under the optimum operational conditions.\textsuperscript{48} The residual concentration of Direct Red could be lowered to below 0.5 ppm after 3 minutes of treatment by ion flotation when Choi et al. used sodium lauryl sulfate as both collector and frother.\textsuperscript{49} Rhodamine B (RB) and thoron (TH) are widely used for analytical and biological staining purposes and may deleteriously affect water. Removals exceeding 99.5\% and 99.9\% could be achieved for RB and TH, respectively, when Shakir et al. adopted the anionic surfactant sodium lauryl sulfate (NaLS) and the cationic surfactant cetyltrimethylammonium bromide (CTAB) as collectors.\textsuperscript{50} More than 96\% of cationic dyes could be removed and the enrichment factors in the foam were about 6 under the optimum conditions when Groß et al. used two commercially available biopolymers as alternatives to classical surfactants for dye removal via ion flotation (as shown in Fig. 4). However, for anionic dyes, a further cationic surfactant, DTAB, should be added; the removal can thus be increased from 5\% to 70\%.\textsuperscript{51} Hu et al. also used ion flotation technology to remove methylene blue using commercial hydrophobic silica nanoparticles (SNP) (200.0 ± 10.0 nm average particle size) as a collector without using any surfactants. Removal efficiencies of methylene blue and SNPs and volume ratios of 91.1 ± 4.6\%, 93.9 ± 4.7\%, and 10.5 ± 0.5\% could be respectively obtained at pH 9.0, a SNP concentration of...
600 mg L\(^{-1}\), an anhydrous ethanol dosage of 8 ml and a flotation column height of 600 mm. In addition, methylene could be effectively separated from methylene blue-adsorbed SNPs with ethanol at pH 2.0 for reuse at least five times (as shown in Fig. 5 and Table 1).\(^{32}\) Tetracyclines are broad-spectrum antibiotics that are most commonly prescribed for human therapy; meanwhile, they are also commonly used in livestock farming. Therefore, they are one of the most commonly detected antibiotics in surface water resources discharged from agriculture wastewater and medical wastewater, and they should be removed as much as possible before discharge.\(^{25,24}\) Saitoh \textit{et al.} carried out a large number of experiments, and they noted that almost complete removal (>99%) of tetracycline antibiotics could be obtained with the combined use of 20 mg L\(^{-1}\) of an anionic surfactant, sodium dodecyl sulfate (SDS), 6.5 mg L\(^{-1}\) of a cationic polyelectrolyte, poly (allylamine hydrochloride) [PAH], and 1 mg L\(^{-1}\) Al(III). The remaining concentration of SDS was lower than that permitted by Japanese water regulations. Additionally, this process was used to remove other tetracycline and fluoroquinolone antibiotics as well as different acidic and basic pharmaceuticals, even in five minutes.\(^{25}\) Boron and its compounds are important materials in the fields of medicine, material science, the chemical industry, the nuclear industry and agriculture; additionally, boron is an essential micronutrient for humans, animals and some plants. However, it may generate deposits during the recycling of high quality magnesia products from Saline Lake resources because it can be readily absorbed by magnesium hydroxide; this decreases the efficiency of recycling of high quality magnesia products from brine and boron in waste water, which is also poisonous to the environment. 88.69% boron removal efficiency from Da Qaidam brine was obtained when Bai \textit{et al.} adopted sodium dodecyl benzene sulfonate (SDBS) and \(\nu\)-mannitol as collectors while applying optimized flotation conditions. The removal mechanism is clearly depicted in Fig. 6. Firstly, borate can be formed in alkaline solution by interacting with hydroxide ion:

\[
\text{B(OH)}_3 + \text{OH}^- \rightleftharpoons \text{B(OH)}_4^-
\]

Afterwards, due to its oxophilic character, B(OH)\(_4^-\) can form stable complexes with \(\nu\)-mannitol (as shown in Fig. 6a); then, the negatively charged complexes can be readily absorbed by SDBS due to its electron-acceptor sulfo groups (as shown in Fig. 6b). Finally, the hydrophobic boric complexes can attach to the rising bubbles and reach the top of the flotation cell (as shown in Fig. 6c).\(^{26}\) Briefly speaking, ion flotation can efficiently remove organic and biological pollutants using various types of surfactants as collectors, and the mechanisms of interaction between the target ions and used surfactants vary based on the surfactant and target ions.

Reprinted from M. Groß, M. Tupinamba Lima, M. Uhlig, A. Ebrahim, O. Roeber, B. Olszewski, R. von Klitzing, R. Schomäcker and M. Schwarze, Biopolymers for dye removal \textit{via} foam separation, \textit{Sep. Purif. Technol.}, 2017, \textbf{188}, 451–457, Copyright (2017), with permission from Elsevier.

In addition to the above studies, ion flotation has been applied to other target contaminants. However, considering the length of the present article, additional studies on wastewater treatment \textit{via} ion flotation are summarized in Table 2.

As a promising technology for wastewater treatment, ion flotation has attracted increasing attention due to its low energy requirements, rapid operation, small space requirements, low residual concentration, relatively low cost, \textit{etc}. However, it also has many disadvantages, such as secondary pollution caused by chemical synthetic surfactants, large consumption of biosurfactants, high cost of nanoparticle surfactants, \textit{etc}. However, to further promote the practical application of ion flotation in wastewater treatment, more work should be undertaken to develop eco-friendly and high-efficiency surfactants. Moreover, recycled surfactants will be very popular due to their low cost and environmental benignity.

### Table 1

|             | R\(_{\text{MB}}\) (%) | R\(_{\text{SNPs}}\) (%) | R\(_{\text{SNPs}}\) (%) | D (%) |
|-------------|---------------------|------------------------|------------------------|-------|
| 1 cycle     | 91.1 ± 4.6          | 93.9 ± 4.7             | 94.3 ± 4.7             | 97.5 ± 4.7 |
| 2 cycles    | 89.4 ± 4.5          | 93.6 ± 4.7             | 93.4 ± 4.7             | 93.1 ± 4.7 |
| 3 cycles    | 88.3 ± 4.4          | 93.3 ± 4.7             | 93.1 ± 4.7             | 92.5 ± 4.6 |
| 4 cycles    | 87.5 ± 4.4          | 93.4 ± 4.7             | 93.1 ± 4.7             | 92.5 ± 4.6 |
| 5 cycles    | 85.9 ± 4.3          | 93.4 ± 4.7             | 93.1 ± 4.7             | 92.5 ± 4.6 |

### 3 Recovery of precious metals

Precious metals mainly refer to 8 metal elements, such as gold, silver and platinum, which have beautiful colors and are not susceptible to chemical reactions under normal conditions. Precious metal resources are scarce and non-renewable; thus, arbitrary disposal not only causes waste of resources but also environmental pollution. Therefore, the recovery, purification
Fig. 6  The mechanism of boron removal. Adapted from ref. 56 with permission from Elsevier. Copyright 2018. Reprinted from C. Bai, M. Guo, Z. Liu, Z. Wu and Q. Li, A novel method for removal of boron from aqueous solution using sodium dodecyl benzene sulfonate and D-mannitol as the collector, *Desalination*, 2018, 431, 47–55, Copyright (2018), with permission from Elsevier. Reprinted with permission by Elsevier. 56
| Target contaminant | Collector | Experimental conditions | Removal (%) | Ref. |
|--------------------|-----------|-------------------------|-------------|-----|
| Cu(II)             | EHDABr    | pH 7, flow rate 60 ml min⁻¹, time 60 min, Cu(II) 0.066 mM, EHDABr 0.4 mM | 99          | 57  |
| Cu(II)             | Xanthates | pH 2.5 to 5.5, 10% excess of xanthate, airflow rate 100 cm³ min⁻¹ | 100%        | 58  |
| Cu(II)             | Anti and syn 2-hydroxy-3,5-di-tert-butyl-benzaldoxime | pH 8.5 to 9.5, Cu(II) 0.066 mM, EHDABr 0.4 mM | 100%        | 59  |
| Cu(II)             | Dry baker’s yeast and cetylpyridinium bromide (CPB) | pH 4.5, biosorbent 0.3% w/v, 10 min, CPB 0.01 M, molar ratio CPB/Cu(II) 1 : 2 | 97.09       | 60  |
| Cu(II)             | Sodium diethyldithiocarbamate (DEDTK) | pH 5, Cu(II) 50 mg L⁻¹, airflow rate 1.8 L min⁻¹, foaming agent 39.6 g m⁻³ | 96.4        | 61  |
| Cu(II)             | Silica nanoparticles (SNP) | pH 6.0, Cu(II) 15 mg L⁻¹, SNP 90 mg L⁻¹, CTAB 35 mg L⁻¹, flotation column height 750 mm | 94.5 ± 4.7% | 62  |
| Pb(II)             | SDS and barley husk | pH 8, Pb(II) 50 mg L⁻¹, barley husk 20 mg L⁻¹, SDS 25 mg L⁻¹, airflow rate 1 L min⁻¹ | 95          | 9   |
| Pb(II)             | SDS       | pH 8, Pb(II) 50 mg L⁻¹, SDS 25 mg L⁻¹, airflow rate 1 L min⁻¹ | 85          | 9   |
| Pb(II)             | Sodium lauryl sulfate | pH 8.2, molar ratio of surfactant/metal 2 | 97          | 63  |
| Cd(II)             | Sodium trideceth-4 carboxylate (AEC) | pH 7.5, AEC 7.5 mM, molar ratio of surfactant/metal 10 | 99.8        | 64  |
| Cd(II)             | Potassium ethyl xanthate (KEtX) | pH 6.2, Cd(II) 0.5 mM, KEtX/Cd(II) molar ratio 3, 30 min | 64          | 65  |
| Cd(II)             | KEX and SDS | pH 6.2, Cd(II) 0.5 mM, KEtX/Cd(II) molar ratio 3, collector 0.25 mM, 30 min | 99          | 65  |
| Zn(II)             | EHDABr    | Zn(II) 5 ppm, EHDABr 2.5 mM, flow rate 40 ml min⁻¹, 150 min | 95.98       | 66  |
| Co(u)              | EDTA and cetylpyridinium chloride (CPyCl) | Co(u) : EDTA : CPyCl 1 : 1 : 4 | 99          | 28  |
| U(vi)              | Cetyl trimethylammonium bromide | U(vi) 0.1 mM, carbonate 0.1 M, collector U 5, gas flow rate 52 ml min⁻¹ | 100         | 67  |
| Ge(iv)             | Pyrogallol and DA | pH 4, metal ions : pyrogallol : DA 1 : 3 : 3 | 100         | 14  |
| Cr₂O₇²⁻             | EHDABr    | pH 5.2, air rate 1600 ml min⁻¹, retention time 150 min | 90          | 68  |
| Cr₂O₇²⁻             | Rhamnolipid (RL) | Cr(vi) 40 ppm, pH 8, airflow rate 50 ml min⁻¹, RL/Cr molar ratio 0.01, Fe/Cr molar ratio 3 | 95          | 69  |
| Ni(u)              | R. opacus | pH 5, Ni(u) 5 mg L⁻¹, Al 50 mg L⁻¹, R. opacus 2 g L⁻¹, 15 min | 90          | 70  |
| Al(u)              |           | pH 5, Ni(u) 5 mg L⁻¹, Al 50 mg L⁻¹, R. opacus 2 g L⁻¹, 15 min | 93          |     |
| Pb(II)             | Sodium alginate and SDBS | pH 5.35, Pb(II) 0.4 mM, Cu(II) 1.5 mM, calcium chloride 4 wt%, flow rate 120 cm³ min⁻¹ | 99          | 71  |
| Cu(II)             |           | pH 5.35, Pb(II) 0.4 mM, Cu(II) 1.5 mM, calcium chloride 4 wt%, flow rate 120 cm³ min⁻¹ | 92          |     |
| Zn(II)             | SDBS      | Cd(II)/Zn(II) 0.01 mM, collector 0.1 mM, surfactant 0.2 mM, 60 min | 90          | 72  |
| Cd(II)             |           | Cd(II)/Zn(II) 0.01 mM, collector 0.1 mM, surfactant 0.2 mM, 60 min | 95.2        |     |
and reuse of precious metals is conducive to the construction of ecological civilizations and sustainable development.

A pilot scale field trial of recovering gold cyanide anions from heap leaching liquor via ion flotation was undertaken with the aid of cetyltrimethyl ammonium bromide (CTAB) as the collector. Almost 100% of the gold could be recycled, and the recyclability of the collector was about 80% after 13 reagent recycle stages.78 Reyes et al. investigated the recovery of silver in spent diluted fixer through ion flotation using a column. A recovery of 97% could be obtained using 0.06 g L\(^{-1}\) of sodium isopropyl xanthate (SIX) and 0.04 g L\(^{-1}\) of frother. Additionally, controlling the pH at 6 helped improve the silver recovery.79 Meanwhile, silver recovery from dilute aqueous solutions containing thioureas by ion flotation was also proved to be feasible. A high recovery of silver (almost 100%) could be obtained using dodecylamine as the collector together with ethanol (0.5%) as the frother (as shown in Fig. 7).80

As mentioned above, ion flotation can be used to recover multiple precious metal ions or their cyanide complexes. An experiment of ion flotation on an aqueous solution of gold and silver cyanide anions was conducted with cetyltrimethyl ammonium bromide as the collector. Almost 100% gold recovery could be obtained, and cetyltrimethylammonium bromide exhibited significant selectivity for gold over silver.81 The recovery of cationic complexes of rhodium and palladium via ion flotation was investigated using sodium dodecyl benzene sulfonate (SDBS) as the surfactant; it was noted that the cationic complexes of rhodium(III) and palladium(II) can be floated with SDBS. Otherwise, two ion flotation procedures were proposed which were rapid, simple and did not require expensive reagents or apparatus to obtain satisfactory separation of binary mixtures of Rh(III), Pd(II) and Pt(IV) (as shown in Fig. 8).13 Au(III), Ir(IV), Pd(II) and Pt(IV) could also be recovered by ion flotation when cationic collectors such as pentadecyl trimethyl ammonium bromide (PTMAB) and hexadecyl tripropyl ammonium bromide (HTPAB) were used. The recoveries of each metal were 99.9%, 99.8%, 99.45 and 99.7%, respectively, when floated under optimum conditions. The condensed foam volume was found to be less than 0.5 ml; thus, an enrichment of 200-fold could be obtained, which shows that ion flotation can be an effective method for precious metals recovery.82

In summary, ion flotation exhibits great advantages over other technologies in recovering precious metals due to its simplicity, ease of operation, low cost, etc. However, most surfactants used for recovering precious metals have low separation indices. Meanwhile, the surfactants used also bring great environmental hazards, which restrict their industrial application. Therefore, environmentally friendly surfactants with

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### Table 2 (Contd.)

| Target contaminant | Collector | Experimental conditions | Removal (%) | Ref. |
|--------------------|-----------|-------------------------|-------------|-----|
| As(III)            | SDS       | pH 4.0, SDS 54.13 mg L\(^{-1}\), Fe(III) 134.89 mg L\(^{-1}\), Mo(VI) 48 mg L\(^{-1}\), As(III) 60 mg L\(^{-1}\) | 99.4        | 73  |
| Cd(II)             | Calcium aluminat | pH above 11.5, CaO 0.75 g L\(^{-1}\), monocalcium aluminat (C70) 2 g L\(^{-1}\), reaction time 6 h | 80          | 74  |
| Cu(II)             | Xanthate and dialkylidithiocarbamate | pH 5, 10% excess of the stoichiometric amount of xanthate, stoichiometric amount of diethyl-dithiocarbamate | >95         | 75  |
| Fe(III)            | Tea saponin | pH 6, tea saponin to metal ratio 3 : 1 | 89.95       | 76  |
| Pb(II)             | Tea saponin | pH 8, metal ions 5 mg L\(^{-1}\), S-octanoyl-cysteine 0.01 M | 99.9        | 77  |
| Zn(II)             | S-Octanoyl-cysteine | pH 6, tea saponin to metal ratio 3 : 1 | 71.17       | 71  |

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Fig. 7 Effects of flotation time and air flow rate on \(R_{Ag}\). Reproduced from ref. 80 with permission from Elsevier. Copyright 1995. Reprinted from A. I. Zouboulis, Silver recovery from aqueous streams using ion flotation, Miner. Eng., 8, 1477–1488. Copyright (1995), with permission from Elsevier.
higher selectivity are urgently required to expand the practical application of ion flotation.

4 Pre-concentration of rare-earth elements

Rare-earth elements are widely used in semiconductors, electronic components, alloys, metallurgy, glass and ceramic manufacturing, special materials, and other industries; they have long been considered to be a strategic mineral resource. However, rare earth industries face the difficulty of separating certain elements from their sum. Ion flotation is a promising technology for ensuring production of concentrates containing 60% to 70% rare earth elements.

Rose et al. investigated conditions for concentrating yttrium from solution using 2-sulphonated fatty acids via ion flotation, and a maximum recovery of 99.5% was obtained under optimum conditions within 30 minutes; furthermore, they found that by increasing the pH to 8, the extraction rate was 3 times faster with a smaller loss in extraction compared with flotation at pH 2.75. Chirkst et al. found that as the pH increased, the distribution coefficients of yttrium(III), cerium(III) and europium(III) sharply increased to almost 100%. The pH values of initial extraction of 4.5 for yttrium(III), 5.5 for cerium(III) and 6.2 for europium(III) indicate that these ions can be recovered and separated from each other by adjusting the pH value via ion flotation with sodium dodecyl sulfate serving as the collector (as shown in Fig. 9). The experimental results fitted well with the calculation of the instability constants of hydroxo complexes, solubility products of hydroxides, and Gibbs energies of formation of the specified compounds.

Later, they found that cerium(III) and yttrium(III) could be concentrated individually from solutions of their salts at pH 4.5 to 6 when sodium dodecyl sulfate was used as the surfactant; the experimental results were consistent with the calculated dissociation constant of dodecyl sulfonic acid obtained from experimental potentiometric titration curves of the solutions. Additionally, they used sodium dodecyl sulfate as a collector to concentrate lanthanides; upon addition of chloride ions in concentrations of 0.01 to 0.1 M, a decreasing tendency of the distribution coefficients and shifts of the maximum recovery to the region of higher pH values were noted. A maximum distribution coefficient could be obtained at a chloride concentration of 0.01 M, which helped to improve the separation efficiency (as shown in Table 3).

The same phenomenon was also found when floating and concentrating La(III) from nitrate and nitrate-chloride solutions with dodecyl sulfate as the collector. However, the addition of chloride ions did not significantly improve the ion flotation of holmium(III); also, the distribution coefficient increased with the addition of chlorides and reached the maximum at a sodium chloride concentration of 0.01 M.

Lobacheva et al. used sodium dodecyl sulfate as a collector to concentrate yttrium(III) and ytterbium(III) cations from diluted aqueous solutions in the presence of chloride ions via ion flotation. A decreasing tendency of the distribution coefficient \( K_{\text{dissr.}} \) and a shift of the maximum recovery to the range of lower pH values was found for ytterbium ion flotation with the addition of chloride. The \( K_{\text{dissr.}} \) of yttrium also decreased, while the pH of maximum recovery shifted to a higher value region. The maximum yttrium recovery (in the form of Y(OH)\(_3\)) and separation coefficient could be obtained at a chloride concentration of 0.01 M and pH 7.8.

Maximum recoveries of yttrium and cerium ions could be obtained at pH 5.5 and 7.0, respectively, by ion flotation according to their other research. This allows recovery and separation of cerium and yttrium cations from their salts in the course of processing of lean technogenic raw materials at properly chosen pH values.

It can be concluded that ion flotation plays a critical role in concentrating and separating rare-earth elements due to its characteristics of low cost, small space requirement, energy saving, etc. Despite its numerous advantages, ion flotation also involves numerous difficulties; for example, when concentrating and separating multicomponent rare-earth elements, it is necessary to adjust the pH value more than once, which is
As mentioned above, ion flotation is a promising separation technology for recovering or removing target ions. However, the solution to be treated usually contains more than one ion that needs to be recovered. Separation of one colloid of interest from other ions that may also be collected is quite necessary, either for economic reasons or for compliance with environmental restrictions on waste composition. Therefore, information on the selectivity between different ions is important for designing new ion flotation processes to recover valuable components from solutions and waste treatment. Moreover, it is advantageous to acquire a mechanistic understanding of the selective separation of one ion over others to assist in selecting appropriate collectors and conditions for a specific application.

A great deal of research has been conducted on the selective separation of multicomponent ions by ion flotation, and satisfactory results have been acquired.

At the very beginning, the Gouy–Chapman diffuse layer theory was adopted to define the selective coefficient between two ions. According to this theory, a general discipline can be concluded that the selectivity of a colloid with a higher valence is usually greater than that of other ions with lower valence, which was verified by many studies.

The selective adsorption coefficient between two ions in the Gouy–Chapman model is defined as

$$\alpha_{AB} = \frac{\frac{(\Gamma/n)_A}{(\Gamma/n)_B}}{\frac{(\nu A - 1)}{\nu B}} \frac{\int_{\nu A}^{1} \frac{\sum_{i} n_i (\nu_i A - 1)^{1/2}}{\nu_i}}{\int_{\nu B}^{1} \frac{\sum_{i} n_i (\nu_i B - 1)^{1/2}}{\nu_i}}$$

where $(\Gamma/n)_i$ is the distribution factor, $\nu = \exp(-e\phi/kT)$, $\phi$ is the potential, $z_i$ is the valency of species $i$, and $n_i$ is the bulk concentration of ions of species $i$. 

### Table 3

| Separation coefficient $c_{NaCl}$ | $c_{NaCl} = 0$ | $c_{NaCl} = 0.01 M$ | $c_{NaCl} = 0.05 M$ |
|---------------------------------|---------------|---------------------|---------------------|
| $K_{Sm/Er}$ | 5.53 | 6.70 | 7.54 | 7.00 | 1.51 | 7.60 |
| $K_{Eu/Ce}$ | 13.78 | 6.70 | 41.52 | 7.00 | 1.39 | 7.65 |
| $K_{Eu/Er}$ | 40.92 | 6.70 | 6.77 | 6.50 | 2.32 | 6.00 |
| $K_{Ce/Yb}$ | 0.74 | 6.00 | 6.73 | 6.30 | 60.15 | 8.56 |
| $K_{Ce/Y}$ | 0.54 | 4.50 | 9.80 | 6.50 | 32.41 | 8.56 |
| $K_{Eu/Sm}$ | 1.10 | 6.00 | 14.60 | 6.30 | 0.92 | 7.40 |
| $K_{Sm/Er}$ | 3.89 | 4.00 | 54.13 | 7.52 | 17.08 | 8.70 |
| $K_{Sm/Yb}$ | 1.32 | 5.40 | 7.54 | 7.80 | 25.45 | 8.40 |
| $K_{Sm/Y}$ | 1.60 | 3.50 | 25.73 | 7.30 | 6.96 | 8.75 |
| $K_{Eu/Yb}$ | 1.48 | 5.55 | 25.16 | 7.30 | 6.96 | 8.75 |
| $K_{Eu/Y}$ | 1.21 | 6.10 | 20.69 | 6.30 | 7.57 | 8.90 |
| $K_{Eu/Yb}$ | 0.92 | 4.60 | 99.45 | 6.70 | 3.49 | 8.40 |
| $K_{Eu/Yb}$ | 5.94 | 6.40 | 110.03 | 7.80 | 4.28 | 7.40 |
| $K_{Eu/Yb}$ | 1.32 | 5.40 | 7.54 | 7.80 | 25.45 | 8.40 |
| $K_{Eu/Yb}$ | 1.10 | 6.00 | 14.60 | 6.30 | 0.92 | 7.40 |
| $K_{Eu/Yb}$ | 1.48 | 5.55 | 25.16 | 7.30 | 6.96 | 8.75 |
| $K_{Eu/Yb}$ | 1.21 | 6.10 | 20.69 | 6.30 | 7.57 | 8.90 |
| $K_{Eu/Yb}$ | 0.92 | 4.60 | 99.45 | 6.70 | 3.49 | 8.40 |
| $K_{Eu/Yb}$ | 5.94 | 6.40 | 110.03 | 7.80 | 4.28 | 7.40 |
There are two assumptions in the above theory; the first is that the dielectric constant is constant over the diffuse double layer and there is no polarization of ions, and the second is that the ions are points of charge with no radius so that there is no selectivity among ions with the same charge. Obviously, selectivity among ions of the same valency does in fact exist. Soon afterwards, Jorne and Rubin made some modifications on the basis of the Gouy–Chapman diffuse layer theory by introducing the difference in the distance of closest approach of ions with different sizes. The selective adsorption coefficient between two ions in the Jorne and Rubin model is defined as

\[
\alpha_{AB} = \frac{1}{\nu} \frac{\int_0^1 \left( r^\nu - 1 \right) dv}{\sum_i n_i \left( r_i^\nu - 1 \right)^{1/2} + 2(1/n_B)^{1/2} \left( v_B^{1/2} - v_i^{1/2} \right)}
\]

Soon afterwards, they noted that experimental data for the separation of \( \text{Sr}^{2+} \) and \( \text{UO}_2^{2+} \) ions in the presence of monobutyl biphenyl sodium sulfonate as a collector fitted well with the above theory, which indicates that the selectivity of ion flotation relies not only on the charge but also on the size of the hydrated ion.\(^a\)

Huang et al. experimentally studied the ion flotation of copper, cadmium and lead using sodium dodecylbenzene sulfonate on the basis of Jorne and Rubin’s model. They found that the order of ion removal was \( \text{Cu}^{2+} < \text{Cd}^{2+} < \text{Pb}^{2+} \), which supports the fact that the selectivity depends on the charge and effective radii of the hydrated ion.\(^b\)

An investigation of the ion flotation of the transition metal cations \( \text{In}^{3+}, \text{Cr}^{3+}, \text{Fe}^{2+}, \text{Cd}^{2+}, \text{Mn}^{2+}, \text{Co}^{2+}, \text{Zn}^{2+} \) and \( \text{Ag}^{+} \) with sodium dodecylbenzene sulfonate and sodium dodecyl sulfonate as the collectors was conducted by Walkowiak; the selectivity sequence of \( \text{Ag}^{+} \) over \( \text{Mn}^{2+} < \text{Zn}^{2+} < \text{Co}^{2+} < \text{Fe}^{2+} < \text{Cr}^{3+} < \text{In}^{3+} \) was established, which verified that the preferential removal of certain metal ions is closely related to the ratio of ionic charge to ionic radius and the solubility products of the metal-collector compounds. Additionally, the result confirmed the selective foam fractional model proposed by Jorne and Robin, which was based on the Gouy–Chapman diffused double layer theory with the restriction that the closest approach to the surface is determined by the size of the hydrated ions.\(^c\)

Liu et al. developed two thermodynamically based theoretical models to predict the selectivity coefficients for \( \text{Ca}^{2+} : \text{Cu}^{2+} \) and \( \text{Pb}^{2+} : \text{Cu}^{2+} \) in ion flotation with sodium dodecylsulfate (SDS) as the collector. Although the surface model predicted the right selectivity order, the selectivity coefficients did not match the experimentally measured selectivity. The selectivity coefficients estimated by the dehydration model were 1.55 and 2.07 for \( \text{Ca}^{2+} : \text{Cu}^{2+} \) and \( \text{Pb}^{2+} : \text{Cu}^{2+} \), respectively, which agreed well with the experimentally measured values.\(^d\)

Liu et al. removed \( \text{Cd}^{2+}, \text{Zn}^{2+} \) and \( \text{Cu}^{2+} \) from solution via ion flotation with rhamnolipid as a surfactant; they found that ions with larger crystalline radii preferentially reacted with the surfactant.\(^e\)–\(^g\) The ratios of the ionic radii for the competitive systems were 1.03, 1.28 and 1.32 for \( \text{Zn}^{2+} / \text{Cu}^{2+}, \text{Cd}^{2+} / \text{Zn}^{2+} \) and \( \text{Cd}^{2+} / \text{Cu}^{2+} \), respectively. As shown in Fig. 10, the selectivity coefficient of \( \text{Cd} \) over \( \text{Zn}, \text{Sc} \) \( \text{Zn} \), was determined to be 1.61, with \( R^2 = 0.9854 \) (as shown in Fig. 10a); the selectivity coefficient of \( \text{Cd} \) over \( \text{Cu}, \text{Sc} \) \( \text{Cd} \), was determined to be 3.05, with a coefficient of determination, \( R^2 \), of 0.9593 (as shown in Fig. 10b); and the selectivity coefficient of \( \text{Zn} \) over \( \text{Cu}, \text{Sc} \) \( \text{Cu} \), was determined to be 1.677, with \( R^2 = 0.9672 \) (as shown in Fig. 10c). The obtained selectivity coefficient values were in accordance with the ratios of the ionic radii, which suggests that the selectivity sequence of these metals in ion flotation with rhamnolipid as the collector is \( \text{Cd}^{2+} > \text{Zn}^{2+} > \text{Cu}^{2+} \).\(^h\)

![Fig. 10](View Article Online)
Furthermore, Chirkst et al. discovered that the distribution coefficients of yttrium(III) and cerium(III) sharply increased to almost 100% at pH 4.5 and 6, respectively; therefore, recovery of yttrium(III) began at pH 4.5 and recovery of cerium(III) began at pH 6. Thus, a general conclusion can be drawn that selective recovery of REMs can be obtained by varying the pH value. Additionally, they noted that the maximum yttrium recovery (in the hydrolysate form of Y(OH)3) and separation coefficient from ytterbium could be obtained at a chloride concentration of 0.01 M and pH 7.8. It can be concluded that pH and hydrolysis also contribute to the selectivity of multicomponent ions.

The above results indicate that the selectivity of multicomponent ions is closely related to the valence, crystalline radii, and hydrated radii of the metal ions, the ratio of ionic charge to ionic radius, pH, and hydrolysis together with the solubility products of the metal-collector compounds. Therefore, the selective separation of multicomponent ions can be easily accomplished with proper collectors, and accurate models should also be developed and established to predict the selectivity of different ions in future work.

Adapted with permission from A. Bodagh, H. Khoshdast, H. Sharafi, H. S. Zahiri and K. A. Noghabi, Removal of Cadmium(II) from Aqueous Solution by Ion Flotation Using Rhamnolipid Biosurfactant as an Ion Collector, Ind. Eng. Chem. Res., 52, 3910–3917. Copyright (2013) American Chemical Society.

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### 6 Summary and outlook

Currently, ion flotation, a promising separation technology, is widely used in the fields of wastewater treatment, mineral beneficiation, such as rare precious metal recovery, and hydrometallurgy, such as pre-concentrating of rare earth elements and selective separation of multicomponent ions. This technology has been widely recognized by the public due to its simplicity, rapidity, economy, good separation yields, and suitability for a variety of target ions at various levels. Much progress has been achieved in the application of ion flotation. Biosurfactants were developed to overcome secondary pollution due to chemical surfactants. Recently, in order to conquer the problem of large consumption of surfactants, nanoparticle collectors were introduced into ion flotation. Moreover, many novel flotation machines have been developed simultaneously, such as a cyclonic state micro-bubble flotation column and a modified Jameson cell. However, numerous challenges remain to be overcome. Among these, large consumption or high cost of collectors, secondary pollution from chemicals used in ion flotation and low selectivity among ions are the main factors that limit its practical application. In addition, more research should be pursued to develop new, efficient collectors which have the advantages of high efficiency, lower dosage, better selectivity, low cost and environmental friendliness.

### Conflicts of interest

There are no conflicts to declare.
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