RESEARCH ARTICLE

Development of a Multiple Coil Magneto-Rheological Smart Damper to Improve the Seismic Resilience of Building Structures

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Abstract:
Introduction: The incremental research progress on Magneto-Rheological (MR) damper and its response motivated many researchers and engineers to focus on this topic in the last decade.

Methods: MR damper is classified as a semi-active vibration controlling device owing to its mechanical simplicity, low power usage, large response reduction, perfect damping mechanism, good stability, quick reaction time and robust interface.

Results: In the current investigation, experimental studies were performed for the design, development, and testing of a new type of MR damper. A proposed approach was adopted for the magnetic generation using multi-coils to produce more shear force in the flow gap. The study investigates time history responses of the proposed system under an array of strong ground motions at both element and structure levels. Numerical hybrid simulation using OpenSees has also been carried out on a building structure to show the effectiveness of the new device.

Conclusion: The performance of the investigated structure equipped with the proposed system indicates a large reduction in displacement and an increase in damping force under major seismic events.

Keywords: MR damper, Nonlinear control, Semi-active, OpenSees, RC frame, Seismic resilience, Response control, Numerical hybrid simulation.

1. INTRODUCTION

In recent years, many researchers have focused on adding control systems in structures/infrastructure to monitor and minimize earthquake vibrations. Particularly, it has been proved by researchers that Magneto-Rheological (MR) dampers have more advantages over conventional vibration control devices. Notably, simple mechanical design, less power, more damping force, and better stability are added advantages. Most of the MR dampers are working based on the Bouc-Wen hysteretic model which controls vibration in buildings and bridges. In the last couple of years, researchers were implementing various mathematical models and algorithms to prove the superior performance of MR dampers for seismic application. However, the implementation of these devices in building structures was not attained to date due to the high cost of MR Dampers and MR Fluid [1 - 9]. MR fluids also called controllable fluids are classified as smart materials category composed of nano to micron size magnetic particles disseminated in a liquid carrier of hydrocarbon oils. MR fluids respond in a unique manner to the applied magnetic field, by changing their rheology under various magnetic fields [10 - 14]. In detail, particularly in the absence of a magnetic field, these MR fluids normally act as conventional oil, while in the presence of the magnetic field, magnetic iron particles present...
in the fluid align themselves along magnetic flux lines. The reaction time of the fluid is in milliseconds. Furthermore, the MR fluids possess a steady hysteretic characteristic, high yield stress, and variations in viscosity and temperature range [15 - 21]. However, the cost of MR fluids is very high [22 - 24]. The semi-active eddy current pendulum tuned mass damper with variable frequency and damping using a Linear-Quadratic-Gaussian (LQG)-based control algorithm can be used as a vibration resistance of structures for both seismic and wind forces [25, 26]. MR damper works in three modes of operation: namely squeeze, shear and valve modes. In the design aspects of MR Dampers, many novel ideas were contributed by researchers. Notably, the variation in the outer cylinder, piston diameter, annular gap, and magnetic circuit geometry makes such dampers to perform in a superior way. Therefore, a well-detailed investigation should be performed before fabricating these devices [27 - 31]. Conventional vibration control devices have many limitations as they are compromising the application as passive dampers. Whereas the MR devices are belonging to active and semi-active categories. Therefore, the control system has less power requirement and change its response when needed, depending on the design and demand [32].

In the current study, an innovative MR damper with 9 multiple coils is designed, fabricated and tested under several strong ground motions. The advantage of using the toothing system in the piston configuration is the alternate polarities in the magnetic field which strengthen the fluid through two adjacent cores in the piston. Additionally, numerical investigations using OpenSees software were carried out for seismic mitigation of the building structures. OpenSees is well recognized as one of the best nonlinear platforms for earthquake engineering simulation applications. Various researches on the performance assessment of RC frames with various control devices under seismic excitations have been done using this software [33, 34].

2. THE PROPOSED DEVICE

2.1. MR Fluid

The Lord MRF-132 DG is a commercially available

| Parameter                      | Value     |
|--------------------------------|-----------|
| Inductance                     | 83100 microH |
| Former Diameter                | 60 mm     |
| Winding Length                 | 100 mm    |
| Wire Diameter                  | 0.61 mm   |
| Coils turns                    | 1638      |
| Coil Thickness                 | 20 mm     |
| Coil Resistance                | 20.727 Ohm|
| Length of wire without leads   | 346.142 m |
| Weight of wire                 | 900.313 g |
| Number of layers               | 9         |
| Wire Diameter with insulation  | 0.6649 mm |

Magneto-Rheological fluid generally used for controlling devices. It is a dark gray liquid with high density. It is composed of a suspension of magnetic iron particles in hydrocarbon-based oil. Additionally, it is mixed with additives to reduce sedimentation. The viscosity of the fluid is about 0.112 Pa/s and varies in the presence and absence of a magnetic field. The rheological behavior of the fluid is instant and reversible. The fast reaction time is an added advantage of the fluid. The flashpoint of the fluid is above 150-degree Celsius. The technical data such as yield stress, shear stress and shear rate of the fluid are given in the material safety data sheet (MSDS) of the fluid [35].

2.2. MR Damper

In general, the damping force generated in the MR damper is due to the result of viscous friction when the magnetic field is applied. MR fluid is endorsed inside the cylinder with an annular gap of 1mm. The viscosity of the fluid varies according to the magnetic field created by the coil [36 - 38]. Conventional MR damper has a maximum of 3 piston poles and 3 coils, whereas in the proposed MR damper 9 coils and 10 piston poles with a uniform distance of 10 mm and a depth of 20 mm were fabricated to produce more shear forces. The thickness of the cylinder was 5 mm. Generally, increasing the number of flow gaps by having more piston poles results in more shear forces in the sides of the piston which is depicted in Fig. (1). A maximum damping force of 15 kN can be generated by the proposed MR damper. As per the design, the electromagnetic circuit can provide more flux lines in the flow gaps within milliseconds as shown in Fig. (2). For producing 15kN damping force, 9 multiple coils should be modeled. The wires from the coils were connected to the DC power supply, and as a result, the magnetic field was generated and yield stress in the MR fluid appeared. The advantage of using the toothing system in the piston configuration is the alternate polarities in the magnetic field strengthen the fluid through two adjacent cores in the piston. Whereas in the conventional single coil it is absent. The proposed damper has a payload of 13.2 kg. The coil properties are given in Table 1. As per the design, the proposed damper was fabricated and shown in Fig. (3). The electromagnetic coil is wounded on a light-duty lathe.
Fig. (1). Schematic representation of the proposed MR Damper.

Fig. (2). Flux direction and magnetic circuit in the proposed MR Damper.
2.3. Principle and Magnetic Circuit of the Proposed MR Damper

The scheme of flux direction and magnetic circuit of the proposed damper is depicted in Fig. (2). The chambers in the device are filled with MR fluid. The accumulator is not provided at the bottom end of the chamber. When the piston moves, MR fluid flows through the annular gaps between chambers. The 9 coils are heat-resistant and electrically insulated. When the magnetic field applied, the field created around the piston head. Due to the effect of the current supply, the magnetic field direction in multiple coils creates maximum damping force. The magnetic flux lines are perpendicular to the flow direction and provide resistance to the flow. The proposed design can control a wide range through varying values and directions of current. The active volume of MR fluid is defined as the magnetic field passes the volume of fluid. Magnetic field and power required by coils should maintain the balance to optimize the circuit. Currents $I_1, I_2, I_3, I_4, ..., I_9$ were applied in the 1$^{st}$, 2$^{nd}$, 3$^{rd}$, 4$^{th}$, ..., and 9$^{th}$-coil, respectively. When the magnetic flux density increases, the viscosity of the fluid resistance in the gaps also increases and will produce damping force as a result. The damper geometry is characterized by the length of piston head $L$, the thickness of outer housing $R_h$, the width of coil $W_c$, the radius of the cylinder $R$, the length of coil $L_c$, the radius of piston $R_c$, the magnetic field dependent force $F_\tau$, the friction force $F_f$, and the viscous force $F_\eta$. The total force is calculated as follows (Eq. 1):

$$F = F_\tau + F_\eta + F_f$$  \hspace{1cm} (1)

The coils properties and the configuration of the new device are presented in Table 1 and Fig. (3).

3. EXPERIMENTAL INVESTIGATIONS

3.1. Magnetic Flux Density Test

To measure the magnetic flux density of the coil, a unique test setup was built in our lab as shown in Fig. (4). The #. 23 standard wire gauge with a diameter of 0.61mm was used in the experiment. Magnetic flux density was evaluated using the hall probe, at the current interval of 0.25A. A voltage of 8.5V was set as a constant throughout the test. At the maximum current of 3A, 2.15 Tesla was observed in the coil as shown in Fig. (5).

3.2. Time History Loading Test

Damper assessment was carried out by time history loading approach under four different strong ground motions, (namely El Centro 1940, Northridge 1994, Petrolia 1992, and Loma Preita 1989) in the MTS 100 T UTM machine in Karunya Institute of Technology and Sciences, Coimbatore as shown in Fig. (6). 0A and 3A currents were kept in the power supply for the entire test. Top of the piston and the end cover were fixed with threaded fixtures. The earthquake event details are tabulated in Table 2. The resulted damping forces of the proposed MR damper are also obtained and presented in Table 3. The input of the MTS Machine was taken as a displacement response. Therefore, as shown in Figs. (7 and 8), acceleration time-histories were converted to displacement time-histories to perform the experiments. The PGA values used in this study were in the range of 0.276 g- 0.662 g.
Fig. (4). Magnetic flux density test setup.

Fig. (5). Current vs. Magnetic flux density for the proposed damper.
Fig. (6). The proposed MR damper in the MTS machine.

Fig. (7). Response spectra of the selected ground motions.
Fig. (8). Input displacement vs. time for the considered earthquakes.

Table 2. Details of the used earthquake events.

| Earthquake Event | Date and Year       | Station                          | Magnitude (Mw) | PGA (g) | Epicenter              | Maximum Input Displacement (mm) |
|------------------|---------------------|----------------------------------|----------------|---------|------------------------|---------------------------------|
| El Centro        | May 18, 1940        | Imperial Valley - Southern California | 6.9            | 0.321  | 32.733°N 115.5°W       | 11.628                          |
| Northridge       | January 17, 1994    | Newhall - LA County Fire Station  | 6.7            | 0.583  | 34.213°N 118.537°W     | 22.251                          |
| Petrolia         | April 25, 1992      | Cape Mendocino                   | 7.2            | 0.662  | 40.33°N 124.23°W       | 25.289                          |
| Loma Prieta      | October 17, 1989    | Oakland Outer Harbor Wharf       | 6.9            | 0.276  | 37.04°N 121.88°W       | 10.734                          |

Table 3. Experimental results (Element level).

| No. | Earthquake | Damping Force (kN) | Damper Displacement (mm) | % Increase in Damping Force | % Reduction in Displacement |
|-----|------------|--------------------|----------------------------|-----------------------------|-----------------------------|
| 1   | El Centro  | 1.18               | 13.08                      | 11.59                       | 9.17                        |
| 2   | Northridge | 1.36               | 13.37                      | 21.36                       | 19.72                       |
| 3   | Petrolia   | 1.43               | 12.86                      | 19.85                       | 17.085                      |
| 4   | Loma       | 1.08               | 12.08                      | 10.76                       | 9.25                        |
|    | Average    | 1.26               | 12.85                      | 15.89                       | 13.81                       |
|     |            |                    |                            | 919.84                      | 14.15                       |

3.3. Hysteretic Responses

To proceed with the hybrid simulations, experimental time step results produce stiffness of the MR Damper for different earthquakes under 0A and 3A currents. In the next step, these results are used as inputs for numerical simulation in OpenSees. Damping force for 0A and 3A for four earthquakes are shown in Fig. (9 a-d). The damping force vs. time for 0A and 3A are plotted in Fig. (10).

4. NUMERICAL INVESTIGATION (HYBRID SIMULATION)

Using OpenSees (Open System for Earthquake Engineering Simulation) software, a single-story RC frame equipped with the proposed system was considered to study the
effectiveness of the new device at the structure’s level [39 - 43]. The basic geometry of the model is shown in Fig. (11). Beam and columns were modeled using a non linear beam-column element. To define the geometry of the proposed MR damper, two node-link elements were created diagonally and were used to link two nodes with an element. The element has n length and 6 degrees of freedom.
The input parameters are based on the Bouc-Wen material properties. This model has a nonlinear basis and the backbone differential equation has some mathematical parameters which should be defined and calibrated appropriately to give accurate results. These parameters are defined as; Alpha which is the ratio of post-yield stiffness to the initial elastic stiffness, K which is the stiffness at each time interval, and γ and β defined as the softening, hardening or quasi-linearity of hysteretic loop characteristics.

The single-story RC frame shown in Fig. (12) equipped with MR damper was subjected to four earthquakes time history records. The detailing of a frame was added to the material properties of the beam-column elements. The boundary conditions were numbered according to the behavior of elements. Kyrlov-Newton-Newmark integrator was used for time history analysis for various time steps. As a logical assumption, MR damper was kept diagonal throughout the analysis. The dimension and reinforcement details of the model are tabulated in Tables 4 and 5.
Fig. (11). Model geometry [39].

Fig. (12). Bare RC frame model [41].
Table 4. Dimensions of the numerical model.

| No. | Scale Factor | Member                  | Prototype (mm) | Our Model (mm) |
|-----|--------------|-------------------------|----------------|---------------|
| 1   | 1/3          | Length of beam          | 4500           | 1500           |
| 2   | 1/3          | Depth of beam           | 200            | 77            |
| 3   | 1/3          | Width of beam           | 200            | 77            |
| 4   | 1/3          | Height of column        | 4500           | 1500           |
| 5   | 1/3          | Depth of column         | 300            | 77            |
| 6   | 1/3          | Width of column         | 200            | 77            |

Table 5. Reinforcement details of the prototype.

| Element Type | Reinforcement Details                  | Details          |
|--------------|----------------------------------------|------------------|
| Beam         | Tension Rebar                          | 3 Φ 12           |
|              | Compression Rebar                      | 3 Φ 12           |
|              | Shear Reinforcement                    | Φ 8 @120mm c/c   |
| Column       | Longitudinal Reinforcement             | 4 Φ 12           |
|              | Transverse Reinforcement               | Φ 8 @200mm c/c   |

4.1. Results of the Numerical Simulation

The force vs. displacement hysteresis curves for 0A and 3A currents under different earthquake motions are plotted in Fig. (13 a-d). The responses of damper force vs. time and damper displacement vs. time are plotted in Figs. (14 and 15), respectively. The Frame displacement response histories without MR damper, with 0A and 3A currents under four different earthquakes motions, are illustrated in Fig. (16). The numerical simulation summary is given in Table 6.

The numerical simulation results indicated that the proposed device has a superior performance in dissipating the seismic vibrations. Based on the results depicted in Figs. (14-16) and Table 6, the proposed MR damper has a good capability in reducing the structure’s deformations. It will lead to a better vibration control mechanism. The average percentage of reduction in lateral deformations is more than 90% compared to the reference bare model without any damping devices. On the other hand, a significant increase in damping force is observed when the proposed device is under 3A current condition. The average increment at the device level is around 900%, while at the structure’s level it is around 250%, which proves that the new semi-active device has improved performance as compared to those of passive and constant control devices.

![Fig. 13 contd.....]
Fig. (13). Numerical simulation results of damping force vs. displacement a) El Centro b) Northridge c) Petrolia d) Loma Prieta.
Fig. (14). Damper force vs. time (Numerical simulation results).

Fig. (15). Damper displacement vs. time (Numerical simulation results).

Fig. 16 contd....
**Fig. (16).** Frame displacement response histories under the considered earthquakes (Numerical simulation results).

**Table 6. Numerical results (Structure level).**

| Earthquake      | Maximum Displacement (mm) | Maximum Damping Force (kN) | % Reduction in Displacement | % Increase in Damping Force |
|-----------------|---------------------------|---------------------------|-----------------------------|----------------------------|
|                 | Without MR Damper | 0A | 3A | 0A | 3A | 0A to 3A | 0A to 3A |
| El Centro       |               | 85.13 | 66.30 | 6.58 | 2.21 | 10.1 | 90.07 | 357.01 |
| Northridge      |               | 306.27 | 190.43 | 51.95 | 5.3 | 9.9 | 72.71 | 86.79 |
| Petrolia        |               | 267.17 | 236.38 | 9.56 | 2.05 | 10.1 | 95.95 | 392.68 |
| Loma Prieta     |               | 143.87 | 113.48 | 0.1302 | 2.2 | 5.3 | 99.88 | 140.9 |
| Average         |               | 200.61 | 151.64 | 17.06 | 2.94 | 8.85 | 89.65 | 244.34 |

**CONCLUSION**

In the current study, a smart semi-active control strategy was proposed and evaluated through both experimental and numerical simulations. The proposed device is an MR damper fabricated using mild steel consists of 9 electromagnetic coils and 10 piston poles which produces more shear forces in the flow of the MR fluid. The magnetic flux density of the coil is 2.15 Tesla at 3A current and 8.5 Volts. Investigations have been carried out at both local and global levels. The local investigation has been done through a real scale experiment in the laboratory. The results indicated that the proposed semi-active device has a broad adjustable damping force range under a magnetic field. It was shown that the damping coefficient increases significantly as the electric current increases, while decreases with seismic excitation amplitude. To monitor the performance of the proposed device on a global level, a 1/3 scale RC frame was simulated in the OpenSees nonlinear platform. The behavior of the proposed device under electric current cannot be treated as a viscous damper, hence a more sophisticated model should be used. To this aim, the Bouc-Wen model has been implemented in numerical simulations. The response of the scaled-down single-story RC frame has an average lateral displacement reduction of 90% under four major seismic events, whilst the damping force has increased up to 244% on average.

As a conclusion, it is demonstrated through experimental and analytical investigations that the proposed semi-active damping device is superior over conventional control devices and can be considered as an economical and smart alternative to improve the seismic resilience of building structures in earthquake-prone areas. A more detailed investigation using a shake table is recommended to be carried out for future studies.

**CONSENT FOR PUBLICATION**

Not applicable

**AVAILABILITY OF DATA AND MATERIALS**

Implementation of the numerical part of this study was undertaken using OpenSees. All developed codes and models supporting the findings of this study are available from the corresponding author upon reasonable request.

**FUNDING**

The study is financially supported by the Department of Science and Technology, Karunya Institute of Technology and Sciences, India (Grant No: DST/TSG/STS/2015/30-G).

**CONFLICT OF INTEREST**

The authors declare no conflict of interest, financial or otherwise.
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