Graphene-Integrated Metamaterial Device for All-Electrical Polarization Control of Terahertz Quantum Cascade Lasers

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Supporting Information

ABSTRACT: Optoelectronic modulators that operate by the electrical tuning of plasmonic resonator structures have demonstrated fast (>MHz) manipulation of terahertz (THz) radiation for communications, imaging, and spectroscopy applications. Among this class of THz device, chiral metamaterial-based polarization modulators have attracted increasing attention due to the importance of THz polarization control for chemistry, biology, and spectroscopy applications, as well as for THz communication protocols. In this paper, active polarization modulation of a THz quantum cascade laser is demonstrated by the electrical tuning of a 2D chiral metamaterial array. The operating principle of this device is based on an electromagnetically induced transparency analogue, produced by the coupling between a bright resonator and two dark resonators. The orientation of these resonators is such that a radiating electric dipole orthogonal to the incident electric field polarization is induced, causing a rotation of the polarization angle of the transmitted radiation. By variably dampening the dark resonators using graphene, the coupling condition is electrically modulated such that continuous tuning of the transmitted polarization angle is achieved. This device, operating at room temperature, can be readily implemented as a fast, optoelectronic, polarization modulator with a maximum tuning range of 20 degrees at 1.75 THz, with demonstrated reconfiguration speeds of >5 MHz.

KEYWORDS: terahertz, graphene, chiral metamaterials, coupled plasmonic resonators, optoelectronics, polarization modulation, quantum cascade laser

The motivation for building electrically controllable polarization devices lies in the myriad of applications where active control of THz radiation polarization is essential. THz communications is an emerging application, with protocols such as polarization shift keying and polarization division multiplexing expected to be important parts of this technology where speed of modulation is paramount. A device that could actively control the polarization condition of THz radiation would be an important tool in several fields of research. This would address fundamental challenges in material characterization, for instance, characterization of topological insulators, as well as probing the birefringence of materials, which has applications, for example, in the pharmaceutical industry. Finally, an active control of THz light polarization enables the probing and characterization of inherently chiral biomolecules, such as DNA, RNA, and proteins. Despite the breadth and importance of all the aforementioned applications, there is a distinct shortage of available modular devices capable of controlling THz polarization electrically.

Various THz sources with variable output polarization conditions have been demonstrated; however these approaches have integrated the THz source with the polarization element. A more versatile approach would be to design a polarization modulator device that can be integrated with any THz source such as a standard quantum cascade laser (QCL), which is a narrow-bandwidth, powerful, and ultrastable THz source. In order to modify the polarization state of the QCL-emitted radiation, which is transverse-magnetic linearly polarized because of the intersubband transition rules, broadband grating-based devices could be used; however, chiral metamaterial arrays represent an optimal solution, as they display dramatic frequency-dependent characteristics such as optical activity and circular dichroism.

There is a wealth of static chiral metamaterial structures that have been shown to possess these properties however, realizing actively tunable chiral metamaterial devices is fundamentally more complex. Several approaches have been reported. For example, Kan et al. demonstrated effective polarization rotation by using microelectromechanical systems (MEMS). Alternatively, the introduction of photoactive materials, such as silicon, proved to be an effective method in combination with chiral complex structures to induce
polarization modulation. Single-layer chiral metamaterial devices, as well as a double-layer devices, have incorporated photoactive silicon to actively tune the polarization angle and handedness, respectively.

The aforementioned modulation approaches proved to be effective, although MEMS devices suffer from intrinsically low maximum modulation speeds (100 kHz), and photoactive schemes require complex optical systems. Graphene instead represents an ideal tunable material, as its conductivity can be modulated via electrostatic backgating, with carrier concentrations of $10^{14}$ cm$^{-2}$ achievable, and has been successfully integrated with metamaterial structures to produce a range of modulators working in the THz and infrared. These devices have shown to be effective when integrated with THz QCLs, providing 100% amplitude modulation depths, as well as modulation speeds of greater than 100 MHz. This paper will look to integrate a single layer, chiral metamaterial array with graphene to realize an electrically tunable polarization modulator that demonstrates polarization control of a THz QCL.

### RESULTS AND DISCUSSION

**Outline.** Active polarization modulation was achieved by integrating a single-layer chiral metamaterial structure with electrostatically gated graphene to variably dampen the resonance condition and hence modify the transmitted polarization through the device. This device makes use of a coupled bright and dark resonator structure that has a built-in 2D chirality with the device exhibiting electrically tunable optical activity. As a consequence, the polarization angle of transmitted radiation through the device can be actively controlled. A graphene tuning mechanism similar to the approach in ref 44 was used, which involves variably dampening one of the coupled resonators with graphene. An illustration of the metamaterial structure is shown in Figure 1, with the central dipole resonator acting as a bright resonator when excited with incident radiation polarized in the y direction ($E_y$). The two C-shaped resonators on either side represent dark resonators, which are not excited directly by the incident radiation. These dark resonators are indirectly excited from capacitive coupling with the central bright resonator, resulting in resonating electric dipoles in the x direction, $P_x$, illustrated in Figure 1(a). These resonating $P_x$ dipoles re-emit THz radiation which is plane polarized in the x direction ($E_x$), causing a rotation effect on the polarization of the transmitted radiation. This effect can be modulated by tuning the graphene conductivity via electrostatic backgating, using the thin metal lines to electrically contact the graphene. This results in a transmitted polarization angle that is dependent on the applied backgate voltage across the device.

**Device Fabrication.** The device was fabricated on a boron p-doped silicon substrate with a 300 nm insulating layer of SiO$_2$ to realize the electrostatic backgate. The total metamaterial area was 1.7 mm $\times$ 1.7 mm, containing 27 $\times$ 27 individual unit cells. Standard photolithography techniques were first used to define the bond pads, followed by the deposition of 10/100 nm of Ti/Au via thermal evaporation. The coupled metal resonator arrays were then fabricated using electron beam (e-beam) lithography, thermal evaporation of 10/70 nm of Ti/Au, and liftoff. The specific lithographic tuning parameters are shown in SI.1 (Supporting Information).

Graphene was grown via chemical vapor deposition (CVD) on a Cu catalyst and subsequently transferred on top of the gold resonator arrays using a sacrificial polymer layer. It was then patterned into 6 $\mu$m $\times$ 4 $\mu$m patches using e-beam lithography with oxygen plasma etching. A scanning electron microscope (SEM) image of the fabricated device surface is shown in Figure 1(b). The sample was mounted and wire-bonded for electrical biasing on a chip carrier configured for transmission measurements, with silver paste electrically contacting the p-doped silicon substrate for backgate biasing purposes. A 1.2 mm $\times$ 1 mm continuous, uniform graphene area was included next to the device array on the same substrate for the electrical characterization of the graphene conductivity as a function of the backgate voltage. The same conductivity range measured from the uniform area was assigned to the graphene patches in the metamaterial devices, since the graphene growth and transfer, as well as the processing, had been carried out at the same time. A diagram of the full device illustrating the backgating method is shown in Figure 1(c). The working principle of the device is also illustrated in this figure, with the device displaying an electrically controllable optical activity. When incident $E_y$ radiation passes through the device, the polarization angle, $\theta(V)$, of the transmitted radiation is rotated by an angle that is dependent on the applied backgate voltage.

**Simulation: Finite Element Method.** A set of simulations were performed with the finite element method (FEM) software COMSOL Multiphysics V 5.3a, in order to gain insight into the polarization rotation phenomenon and to inform optimal device parameters. A base unit cell was defined, as shown in Figure 2, with Floquet boundary conditions used to simulate a continuous metamaterial array. The incoming THz radiation was simulated with a top port emitting $E_x$-polarized plane waves toward the device structure. The Drude model was employed to describe the complex conductivity of both graphene and gold; however, for simplicity, only the DC sheet conductivity for graphene was quoted in the following...
figures when describing different graphene conductivities. The specific Drude parameters are reported in more detail in Section SI.2.

The polarization plane angle of transmitted radiation depends on the relative weight of the $E_x$ component re-emitted by the C-shaped resonators, and the transmitted $E_y$ component, which is not reflected by the central dipole resonator. Figure 2(a) and (b) show these simulated components as a function of frequency for graphene DC sheet conductivity values of 0.1 and 1.9 mS, respectively. When the graphene sheet conductivity is 0.1 mS, the dampening of the dark resonators is low; hence the metamaterial is in a coupled resonator regime, with a bonding resonance and antibonding resonance visible at 1.65 and 2.07 THz, respectively, which are identified by dips in $|E_y|$ shown in Figure 2(a). Figure 2(b) shows the response of the metamaterial when the graphene sheet conductivity is increased to 1.9 mS, with only one resonance visible at 1.75 THz and with a clear overall reduction in $|E_y|$. In this case the dampening of the dark resonators is much greater due to the increased graphene conductivity, effectively switching the dark resonators on and converting the metamaterial from a coupled resonator regime to a single dipole resonator regime.

The peak charge carrier concentration and polarity on the surface of the metal resonators are probed by simulating the electric field in the z direction at a height of 20 nm above the metal surface produced by incident plane wave excitation of $E_y$-polarized radiation with a nominal power of 1 W across the unit cell. (c and e) Indication of carrier concentration due to excitation of bonding mode with incident radiation at 1.65 THz for graphene conductivities of 0.1 and 1.9 mS, respectively. (d and f) Indication of carrier concentration due to excitation of the antibonding mode with incident radiation at 2.07 THz for graphene conductivities of 0.1 and 1.9 mS, respectively.

Simulation: Equivalent Circuit Model. An LCR equivalent electric circuit model was developed to further understand the working principle of the metamaterial design building on similar reported models. The individual resonators in isolation are modeled as antennas that have a frequency-dependent impedance described by a standard LCR electrical circuit. The coupling between the resonators was taken into account using parallel coupling capacitors between the different resonators.
the bright resonator circuit and the two dark resonator circuits, as shown in Figure 3. The quantitative values for the circuit model parameters are derived from the FEM Comsol simulations and discussed in more detail in Section SI.3. The AC voltage source labeled \( V_{\text{bright}} \) describes the electromotive force arising from the incident THz radiation in the central dipole resonator. The C-shaped resonator circuits on either side have no driving voltage source associated with them, as they are acting as dark resonators. The capacitors take into account the energy stored in the electric field due to the buildup of charges in the resonators, and the inductors reflect the magnetic energy stored from the induced current in each resonator. \( R_{\text{Total}} \) describes the combined energy lost due to ohmic losses and radiation losses in the bright resonator. The loss in the dark resonators are divided into their constituent parts with the ohmic losses, labeled \( R_{\text{Ohm}} \), and the radiative losses in the reverse and forward direction, \( R_{\text{Rev}} \) and \( R_{\text{Fwd}} \), respectively. To account for the power lost due to dissipation in graphene, a variable resistor in series, \( R_{\text{Grap}} \) was included. For simplicity, due to the low scattering time of the graphene, only the real part of the conductivity was considered. The graphene patch dissipates power and hence dampens the dark resonator according to the following equation:\(^{45}\)

\[
P_{\text{Diss}} = \sigma_{\text{Graph}} \| E_{\text{Gap}} \|^2
\]

(1)

The power dissipated, \( P_{\text{Diss}} \), in the graphene is dependent on the time-averaged electric field magnitude across the capacitive gap of the dark resonators, \( \| E_{\text{Gap}} \| \), and the real conductivity of the graphene patch, \( \sigma_{\text{Graph}} \). To determine the transmitted \( E_y \) power through the device, \( T \), the power drawn from the voltage source as a function of incident power was determined, which is equal to \( |1 - T| \).\(^{44}\) The \( E_x \) power reradiated in the forward direction was determined by simulating the power dissipated by the resistor, \( R_{\text{Fwd}} \), as a function of incident power. The resultant \( |E_y| \) and \( |E_x| \) terms emitted through the sample as a function of frequency and backgate voltage are shown in Figure 4(b) and compared with the equivalent Comsol simulation values reported in Figure 4(a). The two waveforms obtained from Comsol simulations and the equivalent model are in very good agreement, thus reinforcing the validity of the circuital analysis. Both simulations have a bonding resonance at 1.65 THz, as characterized by a minimum in transmitted \( |E_y| \)
There is a weaker dip in |Ey| radiation. There is a weaker dip in |Ey| at 2.07 THz, indicating the antibonding resonance. The lithographic tuning of the bright and dark resonators was chosen to create this lopsided coupled resonance condition, as described in ref 44, to demonstrate a larger polarization modulation depth at 1.65 THz. As the graphene conductivity increases, the coupled resonator regime is converted into a single-resonator regime, with an |Ey| transmission dip at 1.8 THz and a reduction in the overall value of |Ey|. Accordingly, the polarization plane angle of transmitted radiation, with a frequency around the bonding or antibonding resonance, is rotated as the graphene conductivity is changed.

Measurements: Broadband THz Time Domain Spectroscopy. The broadband THz transmission response of the fabricated device was measured in a polarization-sensitive time domain spectroscopy (TDS) system from Menlo Systems, model k15, operated in transmission mode as described in Section SI.4. |Ey(f)| and |Ex(f)| as a function of backgate voltage were measured in the TDS setup, normalized to |Ey(f)| measured with no sample present, with the results shown in Figure 4(c). Electrical characterization of the large graphene area fabricated on chip was used to obtain the graphene conductivity at different backgate voltages. Two Keithly 2400 source−drain units were used, with one supplying 5 μA of current across the source and drain while measuring the required voltage and the other used to apply a variable DC voltage across the backgate. The resultant graphene DC conductivity as a function of backgate voltage is shown in Figure 4(d) with the Dirac point visible at around +30 V. The overall emitted |Ey(f)| amplitude is maximum when the backgate voltage is set to +25 V, in very good agreement with the Dirac point retrieved from the large graphene area. The |Ex(f)| amplitude reduces as the backgate voltage, V_{BG}, is lowered from the Dirac point due to the increased conductivity of the graphene, which is shunting the capacitive gap, dissipating more power, and dampening the resonance. The coupled resonator bonding and antibonding resonances are clearly visible at +25 V, with |Ey| transmission dips at 1.75 and 2.15 THz, respectively. For V_{BG} = −100 V, there is only one visible resonance given by a transmission dip at around 1.85 THz. Therefore, at the fixed frequency of 1.72 THz, |Ey| increases by approximately 60% while E_y reduces by approximately 40%, leading to a change in the |Ey|/|Ex| ratio from 1.2 to 2.3, which corresponds to a change in polarization angle of around 20°. There is very good qualitative agreement between the measured E-field components and the simulation curves obtained with the FEM simulation and the theoretical circuit model shown in Figure 4(a) and (b), respectively. The resonance frequencies of the TDS results are blue-shifted by around 75 GHz when compared to simulation, due to the discrepancy in material permittivity values in the simulation when compared to the TDS results. For the FEM simulation, there is a larger tuning range for |Ey| and |Ex|, with a change in the |Ey|/|Ex| ratio from 1.1 to 3 shown in Figure 4(a), using conductivities of 0.1 and 1.9 mS shown by the dotted curves. These values are beyond the achievable range for the device, with the tuning range measured to be between 0.3 and 1.3 mS. The larger simulation range was implemented to gain insight into the potential tuning capabilities for the device if graphene with a different conductivity range was used. By implementing the measured graphene conductivity tuning range into the FEM simulation, the ratio |Ey|/|Ex| is modulated between 1.2 and 2.5, thus yielding a remarkable agreement (within 10%) with the measurements acquired using the THz-TDS.

In order to fully analyze the results of the polarization tuning, the relative phase between the E_x and E_y terms must be considered along with the relative magnitudes. The angle and

**Figure 5.** (a) TDS results of polarization angle of emitted radiation through the device as a function of frequency and backgate voltage. (b) Corresponding ellipticity of radiation through the device. (c and d) Polar plots of radiation measured after the device at 1.75 and 2.24 THz, respectively, for different backgate voltages. (e) Polarization angle as a function of backgate voltage at 1.75 and 2.24 THz.
ellipticity of the transmitted radiation can be determined from these two components using the relations described in Section SI.5. The transmitted polarization condition can be characterized generally as elliptical polarization, with an ellipticity value ranging from 0 (perfectly linear polarization) to ±1 (circular-polarized radiation). For many applications where a polarization modulation is required, ideally the ellipticity would remain as close to 0 as possible as the plane polarization angle is rotated. Plots of the resultant transmitted polarization angle and ellipticity are shown in Figure 5 (a) and (b), respectively.

The measured rotation angle presents positive values at low frequencies, peaking at around 40° as the frequency reaches 1.75 THz, with the backgate voltage set to +25 V. At this frequency, the corresponding ellipticity is close to 0, since the Ex and Ey components are almost in phase. As the frequency is increased beyond this point, the polarization angle reduces until it crosses zero at 2.0 THz. In this case the polarization is highly elliptical, with the Ey and Ex components being out of phase by around π/2. As the frequency is increased further, the polarization angle becomes negative, peaking at 2.2 THz, corresponding to a phase difference of π, representing completely linear polarization once again. According to Figure S(a), the maximum modulation of the polarization plane angle is achieved at 1.75 THz with the polarization angle increasing from 20° to 40° and the ellipticity magnitude remaining below 0.1 as the backgate voltage is decreased from +25 V to −125 V. The polarization at 2.24 THz is modulated from −13° to −22°, with the ellipticity remaining stable at around 0.15. Polar plots illustrating the polarization condition at these two frequencies are shown in Figure S(c) and (d), and the resultant polarization angles as a function of the backgate voltage are plotted in Figure 5(e). The polarization angle trends match the graphene conductivity measurements shown in Figure 4(d), with the angle magnitude increasing in a nearly linear fashion between −75 and 0 V, before reaching a maximum at the Dirac point around +30 V, and then decreasing in magnitude as the voltage is increased beyond this point. The polarization modulation in the 2.24 THz frequency region, although presenting a reduced modulation depth because of the aforementioned lopsided lithographic mismatch, intercepts the spectral range where terahertz QCLs emit strongly. This frequency overlap allowed the integration of this polarization modulator device with a THz QCL, thus paving the way for its implementation in polarization spectroscopy or for the fundamental investigation of topological insulator materials to aid the development of novel spintronic devices.46

QCL Polarization Control. The polarization modulator was integrated with a THz QCL fabricated into a single plasmon waveguide from a bound-to-continuum design and emitting in single-mode frequency throughout the dynamic range at 2.24 THz. The frequency spectrum for this laser is shown in Section SI.6. The experimental setup used to tune the polarization of QCL emission is schematically reported in Figure 6(a).

The QCL was mounted on a liquid-He flow cryostat with the emitted radiation collimated using a 7 cm long focal length parabolic mirror. A second mirror with a focal length of 5 cm was inserted to focus the radiation onto the metamaterial polarization device. Two 10 cm long focal length parabolic mirrors were then used to collect the transmitted output and focus the radiation onto a Tydex Golay cell for detection. Two
grid wire polarizers, identified here as the polarizer and analyzer, were inserted before and after the sample, to allow for precise control of the incoming radiation and to probe the transmitted E-field polarization component. The analyzer was mounted onto an active rotational stage to probe the electric field emitted by the device at various polarization angles. Typically the QCL was operated with a 10 kHz repetition rate with a duty cycle of 15%, and a further 5 Hz gate frequency was applied for lock-in detection of the Golay-measured power.

The normalized electric field as a function of the analyzer angle is shown by the black curve in Figure 6(b) taken before inserting the sample. The same operation was performed with the device in the optical path for backgate voltages of +25 V (Dirac point) and −100 V, as shown in Figure 6(b). The rotation angle changes from about −9° to −16° when the backgate voltage is swept from −100 V to +25 V, respectively, thus yielding a 7° modulation range, in good agreement with the THz-TDS measurements at 2.24 THz. Similar measurements were performed by setting the analyzer to 0° and 90° to measure the emitted |Ex| and |Ey| terms, respectively, as a function of backgate voltage. These results are reported in Figure 6(c), with the corresponding plane polarization angle plotted in Figure 6(d) alongside the graphene conductivity measurements, reporting a consistent trend. When the graphene conductivity is minimum, the polarization angle is maximum to within ±10 V, commensurate to Dirac point variation of exposed graphene. Further to this, the polarization angle trend follows an inverse relation with respect to the conductivity, with high conductivities corresponding to low angle rotations, as predicted in Figure 5. The modulation speed of the QCL polarization was also tested, with the modulation depth as a function of modulation frequency shown in Section SI.7. Modulation speeds of up to 5 ± 1 MHz are demonstrated for this device; however, modifications to the device size and substrate resistivity could increase this modulation speed to >100 MHz, as demonstrated in ref 36.

# CONCLUSION

Active polarization modulation has been demonstrated using a 2D chiral metamaterial device integrated with electrically tunable graphene. The device was fully characterized with a THz-TDS spectrometer, yielding remarkable agreement with the finite element simulations and equivalent circuit model predictions. A continuous polarization angle tuning of 20° was achieved at 1.75 THz by tuning the applied backgate voltage. This device has also been successfully integrated with a THz QCL operating at 2.24 THz, demonstrating active polarization modulation of 7° with modulation speeds of up to 5 ± 1 MHz. The integrated polarization modulation of QCL emission opens new scenarios for the all-electrical fast control of THz radiation. This device represents an important demonstration of how standard THz sources can be actively polarization controlled at electronic speeds, for a plethora of applications in THz polarization spectroscopy, real time material characterization, and THz communication systems of the future.

## ASSOCIATED CONTENT

Supporting Information
The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphoto-000411.

Lithographic tuning parameters for the device design, the frequency-dependent material parameters used in the Comsol simulation, the parameters used in the equivalent circuit model, TDS polarization setup, including the polarization angle and ellipticity mathematical definitions, a section of the QCL spectrum of the laser, and measurement of the modulation speed of the polarization device coupled with the QCL (PDF).

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Notes
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