Multi attribute decision making parametric optimization in weld bead by gas metal arc welding through grey relation analysis: A case study

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Abstract

The basic purpose of this study was to identify the effect of gas metal arc (GMA) welding process parameters on the weld bead geometry of IS2062 structural steel of A grade. L16 Taguchi orthogonal array (OA) design with the idea of S/N (signal to noise) ratio was applied to obtain objective function to be optimized within the experimental field. In this research work the Taguchi technique was joined with grey relational analysis to solve the multi-response optimization problem. ANOVA (Analysis of Variance) was applied to estimate the most significant input parameters which contribute toward the output parameters. Arc voltage, gas flow rate, and wire feed speed were carefully selected as input parameters, whereas weld bead, depth of penetration, and reinforcement were output respectively. The optimal GMA welding process parameters were identified in order to enhance the productivity and curtail the overall functional cost of weld.

Keywords: grey-relational analysis (GRA), Taguchi technique, optimization, GMAW, ANOVA.

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1. Introduction

In today’s era GMA welding process is extensively used to weld a lot of variety materials. GMA welding is adopted due to the excellent quality of weld and the weld quality basically depends upon the mechanical properties of weldments. Weld bead geometry generally depends upon the different welding parameters. IS 2062 structural steel of grade A is a very common engineering material which is extensively used in various industries such as fabrication, building, pharmaceutical, chemical, nuclear and many more industries due to its excellent ductility, good heat resistance, and fair weldability (Rizvi and Ali, 2009). A very excellent good quality of weld can be fabricated by using the gas metal arc welding (GMAW) process. GMA welding is a semi-automatic process and appropriate to weld typically all types of engineering material (Sharma et al., 2014). Grey relational analysis coupled with the Taguchi method was applied to optimize the submerged arc welding process parameters for weld bead of mild steel plate (Datta et al., 2008) and it informed the user that grey based Taguchi technique is suitable to continuous improvement in product quality of component. Another researcher used the grey relational analysis (GRA) with Taguchi technique to determine the multi-response optimization of TIG welding process for most favorable parametric mixture to yield favorable weld bead geometry of weldments by clubbing (Esme et al., 2009). Weld bead geometry parameters were also optimized by grey relational analysis during the plasma arc welding of AISI 304L and it was observed that the optimal weld bead geometry was obtained at a 8A peak current, 5A back current, 20 pulse/sec rate, and pulse width of 50% (Prasad et al., 2015).

Grey relational analysis was used with Taguchi technique in order to optimise the laser welding process for weld bead of AISI 904L material and on the basis of it was concluded that calculation of grey relational grade (GRG) assisted to quantify the integrated performance of weld bead in laser welding process (Satishya and Jaleel, 2010). Many researchers applied grey relational method to optimize the process parameters in the drilling process of Al/ SiC metal matrix composite and it was concluded that the process was greatly improved (Haq et al., 2008). Dongxia et al. (2012) used Taguchi technique to optimize the laser welding
parameters and they reported in their result that the effect of welding parameters on weld quality decreased in order of welding speed, wire feed speed followed by laser power. Ravikumar and Vijian (2014) coupled Taguchi method with GRA to solve multi-response optimization problem and the authors was informed that the best welding process parameters are 140A, welding speed of 4mm/sec, and wind velocity at 7m/sec.

Lin (2012) integrated Taguchi technique with GRA (grey relational analysis) and ANN to minimize the gas metal arc welding process parameters and the authors mentioned in their result that the attribute, quality of gas metal arc welding process, is enhanced together by applying the planned approach. Xiong et al. (2014) used an ANN (artificial neural network) technique and a regression analysis of second order to predict the weld bead geometry by robotic GMA welding process and they informed that ANN performed better than regression analysis of the second order. Kshirsagar et al. (2020) tried to optimize the TIG welding parameters by applying a hybrid Nelder Mead-evolutionary algorithms technique and it was revealed from their result that this hybrid technique were better than that obtained from individual algorithms and also indicate significant reduction in the computation efforts. Yadav and Paswan (2019) predicted and optimized the weld bead geometry during the GMA welding process and they concluded that welding parameters such polarity, welding speed, welding current, and arc voltage influence weld bead geometry.

2. Experimental procedure

In this experimental work IS 2062 Structural steel is used as a base metal with the dimension of 75mm X 55mm X 10mm. The filler wire used to weld was ER 30S6. The chemical composition of the parent metal and filler wire is listed in Table 1, while the welding process parameters and their levels used in this study is listed in Table 2 respectively.

Table 1. Chemical composition (Wt%) of base metal and filler wire

| Material   | % of C | % of Si | % of Mn | % of P | % of S | Fe  |
|------------|--------|---------|---------|--------|--------|-----|
| IS 2062    | 0.079  | 0.45    | 1.65    | 0.012  | 0.03   | balance |
| ER 70S6    | 0.19   | 0.98    | 1.62    | 0.025  | 0.028  | balance |
| Filler wire|        |         |         |        |        |      |

Table 2. Welding process variable and their level

| Factor | Parameters          | Level-I | Level-II | Level-III | Level-IV |
|--------|---------------------|---------|----------|-----------|----------|
| A      | Arc Voltage (V)     | 24      | 26       | 28        | 30       |
| B      | Gas flow rate (l/min) | 10      | 15       | 20        | 25       |
| C      | Wire feed speed (m/min) | 300     | 350      | 400       | 450      |

Figure 1 shows the schematic diagram of gas metal arc (GMA) welding process, which consists a nozzle thought to which the copper coated mild steel wire is fed and an inert gas i.e. 75% Ar+25% CO₂ is passed as shielding gas through the nozzle to avoid any atmospheric contamination of weld pool from the atmosphere. Figure 2 shows the detailed cross section of a weld bead while Figure 3 shows the macrograph of weld bead.
Figure 2. Detailed cross-section of a weld

Figure 3. Macrograph of weld bead

Figure 4 shows the different weld beads produced in this experimental work.

In this study, weld bead, reinforcement, and penetration were measured at each run as response parameters. Experiments were planned as per Taguchi’s (Patil and Naik, 2015) L₁₆ orthogonal array technique (Table 3). Three parameters such as arc voltage, gas flow rate, and wire feed speed selected at four levels were selected as process parameters.

Table 3. L₁₆ orthogonal array and experimental results corresponding to the input parameters.

| Trial No. | Arc voltage (V) | Gas flow rate (l/h) | Wire feed speed (IPM) | Weld bead width (mm) | Reinforcement (mm) | Penetration (mm) |
|-----------|----------------|---------------------|-----------------------|----------------------|-------------------|-----------------|
| 1         | 24             | 10                  | 300                   | 13.15                | 3.85              | 9.10            |
| 2         | 24             | 15                  | 350                   | 14.29                | 3.15              | 9.61            |
| 3         | 24             | 20                  | 400                   | 14.39                | 2.87              | 9.28            |
| 4         | 24             | 25                  | 450                   | 15.13                | 4.51              | 9.95            |
| 5         | 26             | 10                  | 350                   | 16.11                | 4.35              | 9.30            |
| 6         | 26             | 15                  | 300                   | 13.29                | 2.87              | 9.23            |
| 7         | 26             | 20                  | 450                   | 14.95                | 2.41              | 9.38            |
| 8         | 26             | 25                  | 400                   | 17.08                | 2.71              | 9.92            |
Table 3 (cont’d), listed the L_{16} orthogonal array and experimental results corresponding to the input parameters.

| Trial No. | Arc voltage (V) | Gas flow rate (l/h) | Wire feed speed (IPM) | Weld bead width (mm) | Reinforcement (mm) | Penetration (mm) |
|-----------|-----------------|---------------------|-----------------------|----------------------|--------------------|------------------|
| 9         | 28              | 10                  | 400                   | 18.19                | 3.43               | 10.08            |
| 10        | 28              | 15                  | 450                   | 13.89                | 1.39               | 10.00            |
| 11        | 28              | 20                  | 300                   | 14.83                | 1.81               | 9.00             |
| 12        | 28              | 25                  | 350                   | 17.06                | 2.97               | 9.98             |
| 13        | 30              | 10                  | 450                   | 18.25                | 3.78               | 9.24             |
| 14        | 30              | 15                  | 400                   | 15.35                | 4.26               | 8.54             |
| 15        | 30              | 20                  | 350                   | 13.21                | 2.81               | 8.89             |
| 16        | 30              | 25                  | 300                   | 12.54                | 1.95               | 8.75             |

3. Results and Discussions

3.1 Grey relation analysis

The grey relation analysis was proposed by Deng (1982). The grey means the ancient data with poor, incomplete and uncertain information in the grey relation theory. The steps followed in the optimization process are:

Step 1: Calculation of grey relational generation

Let us assume that the sequence of original reference and sequence for comparison be denoted as \( x_0(k) \) and \( x_i(k) \), \( i=1, 2, \ldots, m; k=1, 2, \ldots, n \), correspondingly, where \( m \) is the experimental numbers to be considered, and \( n \) is the total number of observation data. Optimization of multiple responses can be simultaneously performed with Grey Relation Analysis (GRA) to determine the best levels that consist of many outputs (Deng, 1989) with the meager information available; grey relation analysis can evaluate or judge the performances of intricate process which consist more than one output. In grey relation analysis, the raw data have to be pre-processed into a quantitative index for further investigation.

In grey-relation generation, the normalized bead width, reinforcement, and penetration, corresponding the lower-the-better condition is shown as

\[
x_i(k) = \frac{\max x_i(k) - x_i(k)}{x_i(k) - \min x_i(k)}
\]

Bead penetration should follow for Higher-the-better order which can be shown as

\[
x_i(k) = \frac{x_i(k) - \min x_i(k)}{x_i(k) - \max x_i(k)}
\]

Where \( X_i(k) \) denotes the data sequence after pre-processing, \( x_i(k) \) denotes the original sequence, highest value of \( x_i(k) \) is \( \max x_i(k) \), lowest value of \( x_i(k) \) is \( \min x_i(k) \) imply normalizing the data for lower-the-better condition is shown as

A Grey relational coefficient (GRC) can be determined, as expressed in Eq. (3):

\[
\xi_j(k) = \frac{\Delta \min + p\Delta \max}{\Delta x_j(k) + p\Delta \max}
\]

\( \Delta x_j(k) \) denotes the deviation sequence, which is calculated by

\[
\Delta x_j(k) = \| X_j^*(k) - X_j(k) \| \Delta \max. (k) = \max_{\forall j} \max_{\forall k} \| X_0^*(k) - X_j^*(k) \|
\]

\( \Delta \min. (k) = \max_{\forall j} \max_{\forall k} \| X_0^*(k) - X_j^*(k) \| \), where \( \zeta \) is the distinguishing coefficient and in current study \( p = 0.5 \) is used.

The second standardized formula is suitable for defect – type factor.

\[
x_j(k) = \frac{|x_j(k) - x_0(k)|}{\max x_j(k) - x_0(k)}
\]

The third standardized formula is suitable for the medium – type factor.

The grey relation (GR) degree can be estimated by steps as given by:

The absolute difference of the compared series and the referential series should be obtained by using the following formula:
\[ \Delta x_i(k) = |x_{0i}(k) - x_i(k)| \] (5)

**Step 2: Estimation of grey relational coefficient (GRC)**

After pre-processing, a grey relation coefficient (GRC) can be calculated with the pre-processed sequence. It expresses the relationship between ideal normalized value and actual normalized values results.

**Step 3: Estimation of grey relational grade (GRG)**

The weighted sum of grey relational coefficients is known as grey relational grade (GRC), and is referred to as follows and determined by Equation (6). It shows the relation between the normalization value and ideal normalization values of the performance characteristics.

\[ \gamma_i = \frac{1}{n} \sum_{k=1}^{n} \xi(k) \] (6)

where \( n \) = number of process responses. The higher value of grey relational grade corresponds to the intense relational degree between the interface sequence \( x_{0i}(k) \) and the comparability sequences \( x_i(k) \).

### Table 4. Data processing of each performance characteristics (Normalized values)

| Experiment No | WB   | Reinforcement | Penetration |
|---------------|------|---------------|------------|
| 1             | 0.893| 0.212         | 0.364      |
| 2             | 0.694| 0.436         | 0.695      |
| 3             | 0.676| 0.526         | 0.481      |
| 4             | 0.546| 0.000         | 0.916      |
| 5             | 0.375| 0.051         | 0.494      |
| 6             | 0.869| 0.526         | 0.448      |
| 7             | 0.578| 0.673         | 0.545      |
| 8             | 0.205| 0.577         | 0.896      |
| 9             | 0.011| 0.346         | 1.000      |
| 10            | 0.764| 1.000         | 0.948      |
| 11            | 0.599| 0.865         | 0.299      |
| 12            | 0.208| 0.494         | 0.935      |
| 13            | 0.000| 0.234         | 0.455      |
| 14            | 0.508| 0.080         | 0.000      |
| 15            | 0.883| 0.545         | 0.227      |
| 16            | 1.000| 0.821         | 0.136      |

To determine the optimum process parameters and their effect on selected output parameters such as weld bead, reinforcement, and penetration have been measured. Data related to weld bead (WB), reinforcement, and penetration have been furnished in Table 4.

### Table 5. Data processing of each performance characteristics (grey relation analysis) and grey relation grade

| Experiment No | WB   | Reinforcement | Penetration | GRG  | Rank |
|---------------|------|---------------|------------|------|------|
| 1             | 0.824| 0.388         | 0.440      | 0.551| 12   |
| 2             | 0.620| 0.470         | 0.621      | 0.570| 10   |
| 3             | 0.607| 0.513         | 0.490      | 0.537| 13   |
| 4             | 0.524| 0.333         | 0.856      | 0.571| 9    |
| 5             | 0.444| 0.345         | 0.497      | 0.429| 14   |
| 6             | 0.792| 0.513         | 0.475      | 0.593| 3    |
| 7             | 0.542| 0.605         | 0.524      | 0.557| 11   |
| 8             | 0.386| 0.542         | 0.828      | 0.585| 7    |
| 9             | 0.336| 0.433         | 1.000      | 0.590| 4    |
| 10            | 0.679| 1.000         | 0.906      | 0.862| 1    |
Table 5 (cont’d). Data processing of each performance characteristics (grey relation analysis) and grey relation grade

| Experiment No. | WB   | Reinforcement | Penetration | GRG | Rank |
|----------------|------|---------------|-------------|-----|------|
| 11             | 0.555| 0.788         | 0.416       | 0.586| 6    |
| 12             | 0.387| 0.497         | 0.885       | 0.590| 5    |
| 13             | 0.333| 0.395         | 0.478       | 0.402| 15   |
| 14             | 0.504| 0.352         | 0.333       | 0.396| 16   |
| 15             | 0.810| 0.523         | 0.393       | 0.575| 8    |
| 16             | 1.000| 0.736         | 0.367       | 0.701| 2    |

Figure 5 shows the S/N ratio (signal to noise) for overall Grey relational grade calculated using HB (Higher-the-better) criterion is calculated as:

\[
S /N (\text{Higher the better}) = -10\log \left[ \frac{1}{n} \sum_{i=1}^{n} \frac{1}{y_i^2} \right]
\]

(7)

The higher values of mean grey relational grade (GRG) as shown in Figure 5, gives the minimum value of weld bead, reinforcement, and maximum value of penetration. From Figure 5 it is very clear that optimal settings for multi-responses becomes V3-G4-W1 i.e. arc voltage is 28 V, gas flow rate 25 l/m, and wire feed speed is 300 IPM.

3.2 Analysis of Variance (ANOVA)
ANOVA is a statistical tool, which is used to reveal the level of significance of influence of factors. Result of ANOVA for overall grey relation grade (GRG) has been listed in Table 6. From Table 6, it is very clear that arc voltage having the most significant effect on weld bead (Reddy et al., 2020) followed by gas flow rate and wire feed speed respectively and it is validated by previous research work (Kant et al., 2020).

| Source        | DF | Seq SS  | Adj SS | Adj MS | F    | P    | % Contribution |
|---------------|----|---------|--------|--------|------|------|----------------|
| Arc Voltage   | 3  | 0.04486 | 0.04486| 0.01495| 1.07 | 0.430| 24.35          |
| Gas flow rate | 3  | 0.03578 | 0.03578| 0.01193| 0.85 | 0.515| 19.42          |
| Wire feed speed| 3  | 0.01956 | 0.01956| 0.00652| 0.47 | 0.717| 10.62          |
| Error         | 6  | 0.08403 | 0.08403| 0.01400|      |      | 45.61          |
| Total         | 15 | 0.18422 |        |        |      |      | 100            |
Figure 6 shows grey relation grade values from Table 5, for all 16 experiments run as per L_{16} orthogonal arrays and it was observed from Figure 6 that change in the response when factors go from one level to other. Figure 4 also reveals that trial No. 10 has the highest grey relation grade value.

![Figure 6. Grey relation grade for multi response](image)

4. Conclusion

In this research article, the Taguchi technique was integrated with GRA (Grey relational analysis) and used to determine the best optimal GMA welding process parameters to get the acceptable depth of penetration (DOP) and lowest weld bead height, and weld bead width.

The following main outcomes of this study can be highlighted by the following:

1. Weld bead width, reinforcement, were measured to identify the optimal welding parameter combination.
2. The multiple responses performance characteristic was converted to an optimization of a single performance characteristic from the stance of the correlations between arc voltage, gas flow rate, and wire feed speed to obtain enhanced outcomes for weld bead, reinforcement, and penetration.
3. From result it was observed that the optimal welding process parameters were arc voltage 28V, gas flow rate 25 l/m, and wire feed speed 300 IPM. Further it has been noticed that ANOVA shows that arc voltage having the most important effect followed by gas flow rate and wire feed speed respectively.
4. The optimum result assists the manpower to getting the preferred performance measure which curtail the manpower’s time, expenditure and assist in enhancing the yield.

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