SYNTHETIC OBSERVATIONS OF THE EVOLUTION OF STARLESS CORES IN A MOLECULAR CLOUD SIMULATION: COMPARISONS WITH JCMT DATA AND PREDICTIONS FOR ALMA

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ABSTRACT

Interpreting the nature of starless cores has been a prominent goal in star formation for many years. In order to characterize the evolutionary stages of these objects, we perform synthetic observations of a numerical simulation of a turbulent molecular cloud. We find that nearly all cores that we detect are associated with filaments and eventually form protostars. We conclude that observed starless cores that appear Jeans unstable are only marginally larger than their respective Jeans masses (within a factor of three). We note single dish observations such as those performed with the James Clerk Maxwell Telescope appear to miss significant core structure on small scales because of beam averaging. Finally, we predict that interferometric observations with Atacama Large Millimeter Array Cycle 1 will resolve the important small-scale structure, which has so far been missed by millimeter wavelength observations.

Key words: instabilities – ISM: clouds – ISM: structure – stars: pre-main sequence – stars: protostars

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1. INTRODUCTION

The coldest and densest regions of the interstellar medium are the places in which dust and gas form stars (see, e.g., Benson & Myers 1989). Although the time a star spends on the main sequence as well as its subsequent evolution is one of the most well-understood problems in astrophysics today, the same statement cannot be made about the dense, dusty “cores” that are the progenitors of these objects. The opaque envelopes that have not yet formed protostars are of particular interest because they reside at the intersection between the properties of the surrounding molecular cloud and its nascent Sun.

A core, as defined in this work, is an object that has a relatively small mass and will form at most a few stars. Distinguishing “starless” cores from “protostellar” cores is the first step to answering several open questions in the field of star formation. For example, many starless cores have been measured to have masses several times that of their “Jeans mass” (Sadavoy et al. 2010b), the limit at which thermal pressure alone can provide adequate support against the self-gravity of the object (Jeans 1902). One possibility is that there are poorly understood nonthermal support mechanisms, such as magnetic fields or turbulence, preventing the collapse of these cores. Another likely possibility, however, is that the cores have been misclassified as starless when in fact they are collapsing and dim protostars lie hidden within their dusty envelopes. In fact, there is strong evidence from recent interferometric observations (Schnee et al. 2012a; Enoch et al. 2010; Dunham et al. 2011; Pineda et al. 2011) that many cores classified as “starless” actually harbor very low luminosity objects (objects with luminosities ≤0.1 L⊙; see Young et al. 2004; Kauffmann et al. 2005; Di Francesco et al. 2007; Dunham et al. 2008).

Another avenue of study that relies on an accurate classification of starless and protostellar cores is the effort to link the prestellar core mass function (CMF) to the stellar initial mass function (IMF; e.g., Nutter & Ward-Thompson 2007; Enoch et al. 2008; Könyves et al. 2010; Alves et al. 2007). It appears that more massive cores are typically found to harbor protostars (see, e.g., Sadavoy et al. 2010a and Ragan et al. 2012). As a result, if protostellar cores have been misclassified as starless and if the misclassification is more likely for particular masses, then any attempt to compare the observed starless CMF with the IMF is problematic.

Finally, as Kirk et al. (2005) describe, the lifetime of the subset of starless cores that will go on to form stars can be determined by comparing the relative number of starless cores and protostellar cores. Similarly, the number of protostars relative to more evolved young stars is proportional to the protostellar lifetime (Evans et al. 2009).

The most common method to classify cores as starless or protostellar is to identify cores via their dust continuum emission by using catalogs such as the “Sub-millimeter Common-User Bolometer Array (SCUBA) Legacy Survey” (Di Francesco et al. 2008) and then attempt to identify embedded sources by using infrared data (e.g., Jørgensen et al. 2007; Sadavoy et al. 2010a), such as the “Molecular Cores to Planet Forming Disks Catalog” (c2d; Evans et al. 2003, Evans et al. 2009). Because of the high optical depth of these dusty envelopes, however, extinction can obscure and even completely hide dim protostars in the center of these structures, leading to errors in the core classification. In an attempt to explore the veracity of the nondetections of embedded infrared objects, recent studies have utilized interferometric spectroscopy of a variety of protostellar and outflow tracers such as CO, SiO (2–1), HCO+, and N2H+ (Pineda et al. 2011; Schnee et al. 2012a, 2012b).

In order to gain further insight into the misclassification of starless cores while investigating the effectiveness of observational techniques, we compare starless and protostellar cores observed in the controlled environment of a simulated turbulent molecular cloud. We analyze the formation and evolving properties of dense structures in the same manner as real observations taken with SCUBA at the James Clerk Maxwell Telescope (JCMT), with the added benefit of knowing the precise locations and masses of forming protostars. This analysis concentrates on
the observed stability of a given object, as defined by the Jeans mass, near the time in which collapsing regions begin to form.

This paper is organized as follows: Section 2 describes the numerical simulation. Section 3 outlines the methods we use to simulate observations and describes our method to identify objects and derive their stability. We present the bulk properties of the observed objects and their general evolution, including stabilities, densities, and protostar–envelope relationships as “observed” by SCUBA in Section 4. Section 5 gives the results of the simulated interferometric observations. In Section 6, we discuss the results. Section 7 presents concluding remarks.

2. SIMULATIONS

In this paper, we analyze a series of snapshots from a hydrodynamic simulation of a turbulent molecular cloud that is forming stars. This simulation was previously presented in Offner et al. (2013, simulation Rm6), in which it was used to study the chemical distribution in molecular clouds. We briefly summarize the numerical procedure and parameters below.

The simulation was performed with the orion adaptive mesh refinement (AMR) code (Truelove et al. 1998; Klein 1999), and it includes large-scale driven turbulence, self-gravity, and sink particles (Kruijssen et al. 2004). The simulation was first driven for two crossing times without gravity and then evolved for a global free-fall time with gravity. Sink particles were inserted at the finest AMR level when the local density violated the Truelove criterion for $J = 0.25$ (Truelove et al. 1997). This corresponds to a mass density of $4.6 \times 10^{-16} \text{ g cm}^{-3} (n_H = 1.2 \times 10^5 \text{ cm}^{-3})$. Throughout this work, the terms “sink particle” and “protostar” will be used interchangeably when discussing the simulation. The basegrid is 256$^3$ cells, and the run has four AMR levels.

The bulk properties of the simulation were chosen to represent a typical Galactic low-mass, star-forming region. The simulation domain has a length of 2 pc and contains $\sim 600 M_\odot$, which corresponds to an average number density of $n_H = 1300 \text{ cm}^{-3}$. The Mach number, $M_{\text{MF}} = 6.6$, was set so that the simulated cloud is approximately virialized and satisfies the linewidth–size relation (e.g., McKee & Ostriker 2007).

The simulation was run for one global free-fall time of 0.95 Myr. At the final time, the cloud contains 88 protostars and has a star formation rate per free-fall time of 0.18. Since the collapse has not been followed down to the sizes of individual protostars and feedback such as outflows is not included, the sink particles likely overestimate the stellar mass by a factor of $\sim 3$ (Matzner & McKee 2000; Enoch et al. 2007; Alves et al. 2007). The most massive sink particle formed throughout the simulation is $8.5 M_\odot$.

3. SYNTHETIC OBSERVATION METHODS

3.1. Single Dish Synthetic Observations

The simulation was placed at a distance of 250 pc to represent the Perseus molecular cloud as this region has been well studied by c2d (Evans et al. 2003, 2009) and other surveys (Kirk et al. 2006; Hatchell et al. 2005; Sadavoy et al. 2010a). At this distance, 2 pc corresponds to 1650″. We analyze column density maps integrated along each of the $x$, $y$, and $z$ directions. Each integrated image was gridded to 512 × 512 square pixels 3′′22 on a side.

For the optically thin case, as we have here, it is simple to convert column density, $N$, to flux, $S_{\nu}$: $S_{\nu} = N \kappa_{\nu} B_\nu$, where $B_\nu$ is the Planck function and $\kappa_{\nu}$ is the opacity calculated at frequency $\nu$. The flux can then be related to the core mass via Equation (2) in Sadavoy et al. (2010b, modified for a typical core temperature of 10 K):

$$S_{345} \text{Jy} = 0.48 \left( \frac{M_*}{M_\odot} \right) \left( \frac{d}{250 \text{ pc}} \right)^{-2} \left( \frac{\kappa_{345}}{0.01 \text{ cm}^2 \text{ g}^{-1}} \right) \times \left\{ \frac{\exp \left[ 1.7 \left( \frac{10 \kappa_{345}}{T_d} \right) \right] - 1}{\exp(1.7) - 1} \right\}^{-1} (1)$$

Here $S_{345}$ represents the flux received at 345 GHz (850 μm), $M_*$ is the core mass, $d = 250 \text{ pc}$ is the distance to the source, $\kappa_{345}$ is the opacity at 345 GHz (see below), and $T_d = 10 \text{ K}$ is the isothermal dust temperature.

We adopt an opacity value appropriate for a dusty protostellar core at 230 GHz, $\kappa_{230} = 0.009 \text{ cm}^2 \text{ g}^{-1}$ (Ossenkopf & Henning 1994), in accordance with previous observations (e.g., Schnee et al. 2012a). This value assumes MRN grains with a thin ice mantle for a core with a density of $10^6 \text{ cm}^{-3}$, which is typical in nearby star-forming regions (see Johnstone et al. 2000; Schnee et al. 2012a; Sadavoy et al. 2010a). By assuming a spectral index, $\beta$, where $\kappa_\nu \propto \nu^\beta$, one can extrapolate to other frequency values. For $\beta = 2.0$, which we adopt here, $\kappa_{345} = 0.0202 \text{ cm}^2 \text{ g}^{-1}$.

The flux maps are smoothed to 20″ to compare against the smoothed SCUBA catalogs. Then, to further match the observations, we remove large-scale structure by smoothing the same images by 120″ and subtracting this smoothed map from the former 20″ maps (see also Kirk et al. 2006). In total, we analyze 68 simulation outputs distributed between $t = 0 − 1 t_{\text{ff}}$. For each of these outputs, we consider each projection separately. Note that the mass of each core changes depending on the projection (see Section 3.2 below), but if detected multiple times, each detection will be considered as an individual core. The sink particle masses remain unchanged over each projection.

3.2. Core Definition

To extract the bulk properties of the core population and analyze their time evolution, we use the automated routine CLFIND2D (Williams et al. 1994).

The lowest flux level that defines the boundary of an observed core is 0.09 Jy beam$^{-1}$, set by comparison with the observations. This threshold is defined by the opacity, and assuming the material is isothermal, it is equivalent to the mass depth to which we are sensitive (see Equation (1)). Thus, the choice in our opacity value sets our scaling between the observations and the simulation.

Each core’s radius is then compared to the FWHM of the smoothed 850 μm SCUBA observations, 20″. If the core is smaller than this, it is deemed spurious and removed from the analysis (since it might be noise). For the nonspurious cores, we average their time evolution, we use the automated routine CLFIND2D (Williams et al. 1994).

Once the mass is attained, an object’s stability can be analyzed using simple assumptions. We estimate the Jeans mass, $M_{\text{Jeans}}$.

\[ M_{\text{Jeans}} = \left( \frac{\kappa_{345}}{0.01 \text{ cm}^2 \text{ g}^{-1}} \right) \frac{S_{345} \text{Jy}}{0.48 \left( \frac{M_*}{M_\odot} \right) \left( \frac{d}{250 \text{ pc}} \right)^{-2} \times \left\{ \frac{\exp \left[ 1.7 \left( \frac{10 \kappa_{345}}{T_d} \right) \right] - 1}{\exp(1.7) - 1} \right\}^{-1} (1) \]
Figure 1. Four snapshots ranging from “early” times to “late” times ($t = 0.15t_{ff}$ to $t = t_{ff}$; see labels). Protostellar masses have been included in the stability calculations. The $Y$-dimension integrated images are shown. Circles represent unstable cores, squares show the locations of stable cores, and plus signs display the locations of protostar formation sites. Three cores that we study in greater detail are highlighted in the top right panel. (A color version of this figure is available in the online journal.)

of an identified core by applying the simple scaling relation presented by Sadavoy et al. (2010b):

$$M_{J,c} = 1.9 \left( \frac{T_d}{10 \, \text{K}} \right) \left( \frac{R_c}{0.07 \, \text{pc}} \right) M_\odot.$$  

Here $T_d = 10 \, \text{K}$ is the (assumed) isothermal dust temperature and $R_c$ is the radius of the core.

To determine the stability of each core, we compare the mass attained from inverting Equation (1) to the Jeans mass calculated by Equation (2). If $M_c \geq M_{J,c}$, the object is defined as “super-Jeans,” an unstable configuration that should show signs of gravitational collapse if thermal pressure alone were counteracting the force of gravity; $M_c < M_{J,c}$ represents a stable, “sub-Jeans” object that would not be expected to collapse since the thermal pressure within the assumed spherical object would be more than enough to balance the gravitational forces.

Once we determined the stability parameter by using only the envelope mass, we correlated the positions of protostars (sink particles) with the CLFINDD2D objects. If a protostar lies within 75% of the circular radius (see below) of the center of a core, we define the core to be protostellar. Therefore, a comparison can be made, for example, between the cores that are observed to be stable (cores without protostars) and the cores with evidence of collapse (due to the fact that they have embedded protostars). We tracked the growth of protostellar and starless core masses through time along with density, stability, and position.

To visually display the cores on the flux maps, the images include circles and squares corresponding to the size of each core at the location of each of the core centroids (see Figure 1). Circles represent cores that are Jeans unstable ($M \geq M_{J,c}$), and squares denote cores with masses less than the calculated Jeans mass. Plus signs show the location of protostars.
We constructed movies by stitching together images of sequential outputs (labeled at the top of each frame; see Figure 1).

Since protostellar masses cannot be directly measured, adding the protostellar mass to the core mass does not make observational sense but allows us to track the stability of an object. When more than one protostar is associated with a given core, the protostellar masses are simply added. Without sufficient feedback, however, the available material will continue to accrete onto a given protostar. Without outflows, protostellar masses may be overestimated by up to a factor of 0.3 (Matzner & McKee 2000; Enoch et al. 2007; Alves et al. 2007).

Once a protostar is formed, the inner envelope will be heated. Observationally this makes it harder to convert from observed 850 μm flux to mass and thus makes Jeans stability investigations difficult for protostellar cores. For the simulations investigated here, however, the lack of included heating makes the mass determination and stability analysis straightforward.

Note that the mass, size, and density scales of the objects we extract are dependent on the large-scale structure in the image. To investigate, we performed structure identification for maps that had not undergone the 120″ scale removal. In these cases we find large reservoirs of mass, which are strongly associated with filamentary structure (see Section 4.1), surrounding each core. These extended zones are approximately twice the size of cores identified when the large-scale structure is removed. It is useful to consider that it has been previously determined that CLFIND2D works reasonably well when a field is sparsely populated with discrete objects, but it struggles to sensibly pick out important structures when the field is “crowded” (see, e.g., Pineda et al. 2009).

3.3. Interferometric Synthetic Observations

The Common Astronomy Software Applications (CASA) package is used to simulate 100 GHz Atacama Large Millimetre Array (ALMA) Cycle 1 interferometric observations of several individual cores in order to compare with the single dish results. We choose a 5 s “snapshot” integration time to match real observations; 90 s in total is required to create a mosaic for each core.

Beginning with the simulated column density maps, we again generate flux maps as described above. For a given core, we use a square 2 arcmin on a side centered on the object’s coordinates as the input sky model (the simulated flux map). Then, we construct the UV visibilities for the most compact arrangement of antennas using the CASA package simobserve. We employ simanalyze to Fourier transform these visibilities into the image plane.

In this study, the simulation has similar densities and temperatures to the Perseus cloud. Therefore, the declination of the observation is set to a reasonable approximation of the cloud’s position: J2000 +30d00m00. We use a hexagonal stitching pattern for each mosaic.

All observations include thermal noise. In CASA, a robust atmospheric profile exists for the ALMA site, including the altitude, ground pressure, relative humidity, sky brightness temperature, and receiver temperatures. In simobserve, the user need only define the precipitable water vapor, which had a chosen value of 1.262 mm. With these assumptions, the noise for the ALMA Cycle 1 image is ~0.1 mJy beam^{-1}.

Since these simulated observations are only meant to note whether the source was detected, the maps are not “cleaned”; we simply convolve them with the point spread function of the instrument to produce a “dirty” map for analysis. This will not significantly alter the mass of the objects detected; however, a cleaned map would reveal more structure over a potentially larger area.

Simulated observations using the Submillimeter Array (SMA) and the Combined Array for Research in Millimeter-Wave Astronomy (CARMA) were also performed, but we did not detect any cores in the resulting maps.

4. RESULTS FROM SINGLE DISH “OBSERVATIONS”

Over the course of one free-fall time, we traced several core properties both qualitatively and quantitatively. The following sections describe our main results.

4.1. Filamentary Structure

The idea that filaments play a role in the formation of dense cores has been entertained for several decades (see, e.g., Schneider & Elmegreen 1979). The growth of instabilities in filaments and subsequent fragmentation have been numerically analyzed in both the linear (e.g., Inutsuka & Miyama 1992) and nonlinear regimes (e.g., Inutsuka & Miyama 1997). Robust simulations of isothermal, self-gravitating cylinders have revealed several properties of filaments such as characteristic temperatures, external pressures, densities, and radii that are consistent with Herschel observations (Fischera & Martin 2012a, 2012b). The Herschel observations show that filaments are present throughout many star-forming regions (Andrè et al. 2010). Additionally, Hacar et al. (2013) performed observations of $^{12}$CO(1–0), $^{13}$CO(1–0), and SO(1–0) in the Taurus star-forming region with the 14 m FCRAO Telescope (and supplemented the data with APEX 870 μm and IRAM 30 m 1200 μm) where they found that cores appear to form in a two-step process. First, velocity-coherent filament forms. Then, these large structures fragment into cores. Kirk et al. (2013) and Friesen et al. (2013) have found evidence of filamentary accretion flows in the Serpens star-forming region using a variety of spectral lines observed with the ATNF Mopra 22 m telescope and the K-band focal plane array at the Robert C. Byrd Green Bank Telescope, respectively. Hennemann et al. (2012) suggest that gravitationally unstable filaments are the driving factor for star formation in the Cygnus X region with a specific emphasis on the DR21 ridge. Furthermore, Myers (2009) shows that young, embedded star clusters are associated with multiple filaments. It has also been shown that filamentary geometry is ideal for the growth of small-scale perturbations that lead to large-scale collapse in a preferential dimension (the length of the filament) and that filaments containing only a few Jeans masses can easily fragment (for a thorough description, see Pon et al. 2011).

Of course, some detections of filaments may be attributed to multiple beam-diluted objects, so careful investigation of properties such as velocity coherence from spectral fitting are necessary to characterize a structure with certainty. As suggested by the authors above and references therein, a typical filament within a molecular cloud has a width of ~0.1 pc. We removed scales of 0.15 pc (120″ at the distance of the Perseus star-forming region) from the analysis of the simulation presented here, however, to focus on the cores themselves and not their parent structures.

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5 Movies and plots are available at http://www.astro.uvic.ca/~smairs/research/starless/movies/movies.html
6 See http://www.casa.nrao.edu.
With this in mind, the convolved simulation hosts cores that are forming almost exclusively along what appear to be dense filamentary structures. As the simulation evolves in time, the objects appear to travel along these striations, fragmenting and coalescing into a variety of morphologies (see movies).

Figure 1 shows images of 4 of the 68 snapshots. The top left panel represents an early time in which no protostars have formed; the bottom right panel represents one free-fall time, $t_{ff}$. The filaments stand out clearly, and their qualitative association with the identified cores is obvious.

### 4.2. Bulk Properties of the Ensemble

In this section we present the mass and density distribution of the identified cores, where we analyze cores identified from three orthogonal views. Figure 2 shows the distributions of core masses and densities at different times throughout the simulation. We calculate the density of each core by assuming the mass is uniformly distributed over the object as if it were a sphere with a radius determined by its projected area.

The top row of Figure 2 presents the data set in which no protostellar masses were included in the mass determination in order to compare directly with observations. We note that the range in core masses and densities found in the simulation are consistent with real observations of Perseus (Sadavoy et al. 2010a; Enoch et al. 2008). The bottom row illustrates the core mass distribution including the protostellar masses in order to analyze the “true” stability of a given core. As time progresses, the core masses increase as gas accretes and collapses to higher densities. This is more evident in the bottom row than the top. New cores are identified throughout the simulation; therefore, an approximately constant low mass population of objects is present throughout the later stages of the simulation.

At the end of the simulation when protostars are not taken into account in the mass estimate, the median core mass and the mean core mass are both found to be 0.89 $M_\odot$. Including
the mass of protostars yields nearly equivalent median and mean masses of approximately 1.9 $M_\odot$. The median and mean number densities of the data set without protostellar masses are both $n_H = 1.3 \times 10^6$ cm$^{-3}$. The data set including protostellar masses has a median number density of $n_H = 1.8 \times 10^5$ cm$^{-3}$ and a mean number density of $n_H = 2.7 \times 10^5$ cm$^{-3}$.

The density of a core can be compared with three reference values: the average density of the box, $n_0$, the density of a typical shocked region, $n_s$, and the “modal density,” $n_c$.

Here $n_0 = 1.3 \times 10^5$ cm$^{-3}$. This is an order of magnitude lower than the density of any identified object. To estimate the compressed density, we consider a one-dimensional (1D), isothermal shock at the typical density: $n_s = \frac{M_{1D}^2}{\pi H^2} n_0 = 1.9 \times 10^4$ cm$^{-3}$ (see Section 6.1 for more details). This value is shown by the vertical line in Figure 2, which is close to the lowest densities of the cores.

The “modal density” is an empirically derived density noted by the vertical dashed line in Figure 2. Whether or not the masses of the sink particles are taken into account in the analysis, there appears to be a peak in the density distribution at a number density of $n_H \sim 1.0 \times 10^5$ cm$^3$. Note that the tail of the distribution in Figure 2 is quite different depending upon whether we include the protostellar masses in the estimates, especially at later times.

### 4.3. Core Stability

Over time, cores become visible because gravity produces densities that exceed the threshold of observability. Thus, more cores are identified as the simulation proceeds (see Figure 3). At $t = 0.5 t_{ff}$ there are 78 identified cores over all three projections; 80 cores are identified by $t = 0.8 t_{ff}$, and the simulation ends with 86 identified cores at $t = t_{ff}$.

As expected, the simulation begins with few identified cores, then mass accumulates and observationally stable starless cores begin to form in what appears to be a bottom-up fashion. As the simulation proceeds, many of these cores become unstable and begin to form protostars (see right-hand panel of Figure 3).

Figure 4 shows the number of cores in different stability states throughout the observed portion of the simulation for cases in which the dust envelope alone is taken into consideration (left panel) and when protostars are added to the flux maps (right panel). Together, the two panels show the evolution of cores defined as sub-Jeans (observationally stable), super-Jeans (observationally unstable to collapse), protostellar (contain a sink particle), and starless (contain no sink particles).

It is important to note that when the protostellar masses are not taken into account, the true masses of the identified objects are underestimated and there is a population of cores that are deemed “stable” even though they are collapsing and forming protostars. This suggests that when the embedded protostar is unobservable, the Jeans stability argument used by Sadavoy et al. (2010b) may not be sufficient to identify super-Jeans cores.

Although we find super-Jeans cores without any protostars inside, it appears these objects are only marginally unstable. All but one of these cores have masses that are less than a factor of two greater than their respective Jeans masses (see Figure 5). As noted by Sadavoy et al. (2010b), starless cores that satisfy $M > 4.5 M_{Je}$ are those that are deemed “unusual relative to the protostellar cores.” We find no such cores throughout this simulation.

When protostellar masses are included, the observed core stability changes significantly. We see that practically all of the previously sub-Jeans cores that had protostars are now classified as super-Jeans, as expected.

### 4.4. Evolution

We selected several cores to study in greater detail. These cores are taken from isolated positions in the flux maps so other objects and protostars will not significantly affect the measurements (three are highlighted in Figure 1). We track one of these cores through the entire simulation and choose specific time steps for the others on the basis of the protostar formation time. Figure 6 shows the mass and density of three example cores tracked over a number of times.
In Figure 6, the solid horizontal line shows the density associated with the shocked material (see Section 6.1). The dashed horizontal line highlights the “modal density” as defined in Section 4.2. The diagonal line indicates the minimum density for a core to be considered observationally unstable (Equation (2)).

It is evident that there are a few discontinuous jumps (annotated by “D”) in Figure 6. These are due to CLFIND2D itself and how it defines multiple objects.

Although a core is initially isolated, it fragments and coalesces with its pieces as it evolves. When an extended object becomes large enough to exceed the flux threshold between two regions, CLFIND2D draws a boundary between the regions and labels each as a separate object. Sometimes, this bifurcation lasts only for a brief period of time and the object reassembles into its previous configuration in the next time step. Of course, a sudden decrease in radius becomes a sudden increase in density and vice versa. Both in the synthetic observation and in actual observations, there are occasionally multiple objects and filaments that have been “smeared” into one identified core because of the 20″ smoothing.

Both panels in Figure 6 highlight specific regions of interest. In the left panel, which is directly comparable with real observations, stage 1 shows the beginning of the core evolution when a protostar has not yet formed. There is a short period (stage 2) in which the mass increases but the density remains constant. A brief subdivision and merging takes place before the core splits into two distinct objects, losing mass and becoming far more dense as it enters stage 3. Another CLFIND2D identified bifurcation and amalgamation takes place when the defined flux threshold is briefly achieved before the object settles into its final evolutionary state (stage 4). From this point until the end of the simulation, the mass and the density both increase as in stage 1 but to a much larger degree. When considering the envelope mass alone, the evolution is less monotonic but still exhibits periods of collapse.

The right panel of Figure 6 shows density versus mass including the protostellar mass. There are two obvious regions marked with “D” in which CLFIND2D subdivided and then merged this object. Beginning in stage 1, there is a very steady mass and density increase as this object forms a protostar and becomes observationally Jeans unstable shortly thereafter. After the early collapse, the density begins to level off for a short period of time. Meanwhile, the mass continues to increase, indicating that the radius must also be increasing before a large upward jump in density. Here again, the core bifurcates, causing an abrupt density spike. During this period, the mass is essentially constant for the rest of the simulation, which suggests the core is simultaneously decreasing in size.

The bottom left panel of Figure 6 shows the evolution of a core that is recognizably Jeans unstable before a protostar forms. The right panel shows an isolated core that we select at random in the simulation to highlight the diversity in the core population. When only the envelope masses are taken into account, each core resembles the left panel of Figure 6. When protostellar masses are included as shown, there is a rapid evolution in the core properties. Both the mass and the density increase substantially over time, such that the cores appear observationally unstable.
4.5. Protostar and Envelope Relationship

In this section, we explore the relationship between the mass of a protostar and its parent core. Figure 7 shows the fraction of core mass in sink particles. The points that lie at exactly 1.0 on the ordinate axis are protostars that did not have an associated envelope. These protostars lie outside 75% of their nearest core’s radius (measured from the core center). Thus, with no apparent envelope, the sink mass is 100% of the object’s mass. Note that because of the background subtraction, some of the core mass may be lost in this analysis.

As expected, many young objects have not formed protostars and lie along the bottom of the plot. As time progresses, the sink particles begin to dominate the core masses quickly. The bottom right quadrant of Figure 7 is empty. This means that the more massive cores observed in the simulation are dominated by the protostars present. Stepping through time, it is clear that this is a rapid process. Once sink particles form, they quickly accrete a large amount of mass. Therefore, observations ignoring the embedded protostars could miss a significant portion of mass. This will lead to errors in stability classification using noninterferometric observational techniques.

When each of the time steps are analyzed in a sequential fashion, the points travel from the bottom left through an “S” shape to the top right of the plot. Since the total mass of a given object substantially increases throughout the formation and growth of a protostar, it is clear that the protostar mass cannot come from the initial material detected in the envelope alone. One possibility is that cores extend below our flux limit and are collapsing to higher densities such that they enter the observable regime. Another likely possibility is the accretion of mass due to bulk flows in the simulation in conjunction with gravity. The obvious filamentary structures in the map are the most likely sources of mass. In fact, mass flow along filaments...
associated with protostars have been observed in many star-forming regions (e.g., Kirk et al. 2013; Friesen et al. 2013; Hacar & Tafalla 2011; Schneider et al. 2010).

Since the final mass of the protostars is sometimes larger than the initial observed core mass, this suggests that either the observed cores are initially more massive than observed or they continue to accrete. In either case, this undermines the comparison of a single time snapshot of the core mass distribution with the IMF.

5. INTERFEROMETRIC ANALYSIS

In this section, we assess the conditions for which the detection of an embedded protostar is possible. Employing the high resolution and sensitivity offered by interferometers is the logical next step in characterizing the dynamic nature of cores.

As described in Section 3.3, we performed synthetic ALMA Cycle 1, SMA, and CARMA simulated interferometric observations. It was found, however, that a 90 s observation performed at 100 GHz with ALMA Cycle 1 is comparable to an 8 hr observation taken by SMA at 230 GHz and achieves a far better signal-to-noise ratio than an 8 hr observation taken with CARMA at 100 GHz. Offner et al. (2012) found a similar result. The SMA and CARMA observations produced only nondetections; evidently, to identify any substructure present in faint cores or to even detect the objects with $3\sigma$ confidence, greater sensitivity is required. This null result is compatible with recent interferometric observations (see Schnee et al. 2012b).

Thus, we focus primarily on ALMA. We analyze each interferometric image down to the same flux threshold ($6\sigma = 0.6 \text{ mJy beam}^{-1}$, defined by eye) for a consistent analysis. Purely investigating the results of CLFIND2D, we see that in most cases there is no significant build up of mass before a protostar forms. In two of the cases, the core is identified very briefly after the formation of the protostar. In one case, the core is identified concurrently with the formation of a sink particle and continues to grow in time. In the last case, CLFIND2D does not identify a core at any time output.

Figure 8 shows the observations of the object in the bottom left panel of Figure 6 (labeled “Core 1” in Figure 1) at three different time steps: two approaching the formation of the first protostar and one at the time the first protostar appears. The core begins in an undetected state. By the time a protostar forms, a clear detection is possible.

Table 1 shows the properties of the three identified objects at the point of their first detection. In all three cases, the objects already contained sink particles. Cores 1 and 2 are the same as in Figure 6 (left and right panels, respectively); note the increase in density in the center of the core compared with the core average (compare with Section 4.4).

CASA simulations such as these provide a strong prediction for real interferometric observations. Currently, ALMA Cycle 1 telescope time has been awarded with the highest priority to observe the 3 mm continuum emission from all 60 starless cores and 13 protostellar cores in the Chamaeleon I molecular cloud, as identified in Belloche et al. (2011). These observations will be sensitive to point sources with masses $\gtrsim 0.01 M_\odot$, with less than 2 minutes of on-source integration time per object (see Table 1). Once these data are collected, we will be able to perform robust comparisons between simulated core properties and their observed counterparts.

6. DISCUSSION

6.1. Shocked Densities and Structure

In this section we consider some simple estimates of the role of turbulence and gravity to place our results in context.

The characteristic size scale at which gravity dominates over thermal pressure is given by

$$L_3 = \sqrt{\frac{\pi c_s^2}{G\rho_0}},$$

where $c_s = (k_B T/\mu m_H)^{1/2}$ is the sound speed, $\mu = 2.33$ is the mean molecular weight, $k_B = 1.38 \times 10^{-16} \text{ erg K}^{-1}$, $G$ is the gravitational constant, $m_H$ is the mass of hydrogen, $T$ is the isothermal gas temperature, and $\rho_0$ is the average mass density in the simulation.

In a typical shocked region in the simulation, the density and hence the Jeans length will be higher. The shocked density

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Table 1

| Core Identifier | Radius (AU) | Envelope Mass ($M_\odot$) | Sink Particle Mass ($M_\odot$) | Envelope Mass/$M_\odot$ | Density ($\text{cm}^{-3}$) |
|----------------|-------------|---------------------------|--------------------------------|------------------------|-------------------------|
| 1              | 829.30      | 0.27                      | 0.619                          | 2.44                   | $1.70 \times 10^7$     |
| 2              | 579.48      | 0.09                      | 0.090                          | 1.17                   | $1.66 \times 10^7$     |
| 3              | 645.38      | 0.13                      | 0.078                          | 1.57                   | $1.81 \times 10^7$     |

Figure 7. Fraction of a total core’s mass (protostar and envelope) found in the protostars contained within the object’s boundaries plotted against total core mass for all objects in all three projections observed at three time steps. Only the Y-dimension integrated images are shown here for clarity. Red represents 50% of the box free-fall time, green represents 80% of the box free-fall time, and blue represents one free-fall time. The solid vertical line is drawn at the 50% mark (i.e., where the collapsing regions dominate the core mass).

(A color version of this figure is available in the online journal.)
of a 1D isothermal shock is given by $\rho_s = M_{1D}^2 \rho_0$, where $M_{1D} = M_{3D}/\sqrt{3} = 3.8$ is the 1D simulation Mach number. Plugging this into Equation (3), we can express the compressed Jeans length as

$$L_{1m} = \sqrt{\frac{\pi c_s^2}{G M_{1D}^2 \rho_0}}$$

or

$$L_{1m} = M_{1D}^{-1} L_1.$$

Values of $T = 10$ K and $\rho_0 = 5.1 \times 10^{-21} \text{ g cm}^{-3}$ give a compressed Jeans length of $L_{1m} = 4.7 \times 10^{17} \text{ cm}$ or $126.42$, assuming a distance of 250 pc. For the 2 pc box, the low-resolution (512 $\times$ 512) grid used in this analysis had $3''.2 \times 3''.2$ pixels. So, a typical shock forces material together on scales of $\sim 40$ pixels in the low-resolution grid.

The Jeans mass, $M_J$, associated with the Jeans length is given by Equation (2), replacing $R_c$ with the Jeans radius, $R_J = L_1/2$. Thus, the Jeans mass corresponding to the average density in the simulation is $M_{J,0} = 7.92 M_\odot$, and the Jeans mass corresponding to shocked densities is $M_{Jam} = 2.08 M_\odot$. The average CLFIND2D core mass is much closer to the shocked Jeans mass than the Jeans mass corresponding to the average density of the box.

This is, of course, a very simple estimate. The actual processes at play are more complicated and can involve a number of oblique shocks and shears. Note that the “modal density” is approximately a factor of five greater than the shocked density calculated here; this corresponds to a higher characteristic velocity than that associated with $M_{1D}$.

To gain a better understanding of the true densities attained in the center of an individual object, we analyzed one of the cores tracked in Sections 4.3 and 4.4 in more depth at a higher resolution (level 2 in the AMR simulation). The core we selected was the first object to achieve a super-Jeans state in the $Y$-dimension flux maps.

Figure 9 shows number density maps for Core 1 at four different time steps centered on the formation of the first sink. The outer contours show the expected number density achieved using the $M_{1D}$ coefficient ($n_H = 1.9 \times 10^4 \text{ cm}^{-3}$). The inner contours show the “modal density” ($n_H = 1.0 \times 10^5 \text{ cm}^{-3}$)—approximately a factor of five larger. Clearly, both these values are significant in tracing the structure present in the map.
Figure 9. Density map for one individual core observed at a resolution of 1.6 pixel$^{-1}$. The top row shows the core before it forms a protostar (Left to right: 0.15$t_{\text{ff}}$ and 0.24$t_{\text{ff}}$); the bottom row shows two time steps shortly after a protostar forms (Left to right: 0.34$t_{\text{ff}}$ and 0.41$t_{\text{ff}}$). The plus signs indicate the locations of the protostar. The outer contour indicates a density of $1.9 \times 10^4$ cm$^{-3}$ and the inner contour a density $1.0 \times 10^5$ cm$^{-3}$ (see text).

(A color version of this figure is available in the online journal.)

Evidently, much higher densities are achieved than those expected by the simple argument presented above. Throughout the observed frames, both before and after the protostar has formed within the core, gravity quickly creates regions of high density on scales much smaller than the beam. Thus, important structures will remain unobserved without deep interferometric maps.

Analyzing the simulation itself, a typical number density value within Figure 9’s inner contour was found to be $n_{\text{H}_2} = 5 \times 10^5$ cm$^{-3}$ by averaging over the projection. The highest inferred average density of a region exceeds $n_{\text{H}_2} = 10^6$ cm$^{-3}$ (see Table 1). This typical density corresponds to a dynamical collapse time of approximately 5% of the total box free-fall time. Near the beginning of the simulation, this is close to the time resolution in which observations were performed. Therefore, for densities significantly greater than $5 \times 10^5$ cm$^{-3}$, the collapse will not be resolved temporally with the chosen, observed simulation snapshots in the earlier stages of core evolution.

6.2. Single Dish Results

The CLFIND2D objects span a range of masses and morphologies. The objects are initially detected when they are starless; quickly, a subset undergoes mass accretion, gravitational collapse, and protostar formation. In fact, the majority of the cores detected go on to form protostars. This indicates that the objects observed are not transient but are “real” star formation sites. In the earliest time steps, before gravity has had a chance to significantly affect localized regions, there are very few cores identified. As time progresses, the number of observationally defined super-Jeans cores as well as the number of protostars increases.

It is interesting to note that the majority of the mass in cores accretes onto the protostars and the protostar mass rapidly dominates the mass budget. In fact, in this simulation the most massive envelope including at least one protostar was approximately 10 $M_\odot$. The cumulative mass of the protostars present within the largest core, however, totaled more than 60 $M_\odot$. Recall, however, that without removing the 120$''$ scale structure from the flux maps, we find these cores reside within much larger mass envelopes (Section 3.2). These extended regions predominantly trace the filamentary structure in the simulation and act as reservoirs for the smaller scale cores.

When the mass of the protostars is not included (to resemble observations of cores, wherein the dense central object is unobservable), there exists a small population of cores forming stars that are deemed stable from an observational perspective. When the protostellar mass is added, however, these cores are found to be unstable to collapse, as expected. Observationally detecting collapse proves to be quite difficult. For example, if the protostar is deeply embedded and undetectable, its mass cannot be accounted for in the gravitational analysis. The problem of detecting embedded protostars is generally expected to be more severe when the protostars are small and dim. Consequently, the results presented here are most applicable to the transition between the starless and protostellar stages. In many cases, the core, the protostar, or both may be too faint to detect in the first
place, and detection is especially difficult at early times (Schnee et al. 2012b; Pineda et al. 2011; Dunham et al. 2008; Bourke et al. 2006; Young et al. 2004).

Smith et al. (2012) show that the problem of detecting protostars extends to observations of molecular lines. They performed radiative transfer calculations for cores embedded in filaments in a turbulent hydrodynamic simulation. They find that in over 50% of viewing angles, there is no “blue asymmetry,” which is a classic sign of material infall in an isolated spherical core. In a continuation of this work, Smith et al. (2013) highlight the need for high-resolution observations with ALMA in order to test how line profiles and results change with beam size.

Note that a few significantly super-Jeans starless objects (core mass >4.5\(M_\odot\)) were identified by Sadavoy et al. (2010b); little evidence of objects fitting this classification is found in this simulation.

Of course, the detection and analysis of cores relies on many assumptions. We adopted typical values for the dust properties (Johnstone et al. 2000; Kirk et al. 2006; Schnee et al. 2012a; Sadavoy et al. 2010a). We neglected internal heating due to protostars. In actual observations, the warmed dust grains cause an increase in flux that can easily be misconstrued as a core with a larger mass.

One can clearly see a low mass core population that is maintained throughout the simulation in Figure 2. It appears that once a core is identified, it continues to collapse and gain mass. Most of this mass is accreted onto embedded protostars. A sufficient amount of the mass flow, however, replenishes the dust envelope, leaving it detectable.

This distribution of mass within an evolving protostellar core can be best illustrated by Figures 2 and 7. The top right-hand panel of Figure 2, which takes into account only what is observable in the submillimeter regime, shows the total remains approximately constant over time. If the mass of the protostar is included, the total mass within the core increases over time. Even when the embedded protostars become quite massive, the core masses remain comparatively low. When considering only the material in the envelope, the density increases only slightly over time. In general, when the protostellar masses are added, the peak of the mass and density distributions stay approximately constant while more higher mass objects are observed. This is also shown in Figure 7, where the protostars dominate the mass by a significant factor.

These distributions were also analyzed assuming each protostar was a factor of three less massive in order to compensate for the overestimate inherent in the simulation (see Section 2). We found a less prominent but still significant increase in higher mass objects, as expected. A modified version of Figure 7 did not undergo any substantial changes. The protostar masses still greatly dominate the envelope masses.

6.3. Interferometric Results

To truly determine the nature of a given core, one needs to look more closely at the internal structure. The large JCMT beam size “washes out” the more compact structure, causing the object to appear less dense. In order to investigate the details of protostar formation at the scales, sensitivity, image fidelity, and resolution necessary, an interferometer such as ALMA is required.

The bottom right panel of Figure 8 shows the difference between the JCMT and the ALMA beams for a simulated ALMA Cycle 1 observation (100 GHz). It is clear that the JCMT beam blends much smaller structures that can be detected with an interferometer.

Comparing the Table 1 values with the same cores as in the single dish data, we highlight several interesting points. Beginning with Core 1, the mass inferred using interferometry is an order of magnitude less than found by the JCMT. This is to be expected as the envelope observed by ALMA is much smaller than that observed by the JCMT. The reduction in mass indicates that there is a structure present that is on larger angular scales that cannot be recovered by ALMA’s 12 m array in its most compact configuration at 100 GHz. The object was detected concurrently with the snapshot in which the protostar formed.

Core 2 appears more unstable when synthetically observed by ALMA. Removing the noise from the observations and redefining the clump boundaries at a lower flux threshold that is discernible by eye, the object is found to be up to 1.5 times more massive. This indicates that the signal-to-noise ratio significantly influences the core classification and stability calculation. The object was detected shortly after the sink particle first appeared. The third isolated core in which a detection was made with ALMA is similar to the second. The core mass to Jeans mass ratio indicates more instability in the case of ALMA. Probing the central densities of these cores is important for understanding the single dish data.

Our interferometric analysis of core stability also assumes isothermal dust and spherical cores. It is clear, however, that the morphologies of these objects could indicate collapse along preferred axes (see Pon et al. 2011 for a thorough description of collapse modes). This type of analysis is vital to perform at small scales near the center of identified objects in order to truly observe how stars are forming.

7. CONCLUSION

In this study, we performed synthetic single dish and interferometric observations of a simulated star-forming region. Assuming the gas and dust were optically thin, we inferred masses and densities by assuming the objects were spheres. We calculated the gravitational stability using the density of each core and correlated protostars with the objects. The single dish analysis was performed with and without including protostellar masses; the former was to emulate real observations while the latter was to compute the core’s “true” stability. We investigated the relationship between the protostar and its parent envelope in terms of their mass, and we considered the significance of the core densities with respect to turbulence and gravity.

There are several key results.

1. Our analysis is consistent with various observations. Namely, the masses and densities of the simulated cores we detect are very similar to “real” cores in Perseus (see Section 4.2). We find many more sub-Jeans cores than super-Jeans, in terms of their mass and size, which is consistent with Sadavoy et al. (2010a). The fact that we do not detect substructure with simulated CARMA observations is consistent with Schnee et al. (2012b).

2. Nearly all cores that we detect eventually form protostars. This suggests that observed cores detected in this manner (assuming the physical conditions and distance of Perseus) are probably “real,” that is, they will likely go on to form protostars in the future (see Section 6.2). The mass of the observed envelope, however, does not appear to be a good tracer of the eventual protostellar mass. This has implications for comparing the CMF with the stellar IMF.
(see Section 4.5). Note, however, that the simulation does not include magnetic fields, which could provide additional support that may inhibit a core from collapsing.

3. Nearly all cores we identify are associated with filaments. This is consistent with the ubiquity of filaments recently observed by Herschel and suggests that if observations had better resolution and sensitivity they would also see a similar correspondence between cores and filaments (see Section 4.1).

4. Single dish observations such as those with the JCMT as well as previous-generation interferometers appear to miss significant core structure on small scales because of flux averaging. Interferometric observations with ALMA are necessary to recover this information (see Sections 5 and 6.3).

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