In voltage-gated cation channels, a recurrent pattern for mutations is the neutralization of positively charged residues in the voltage-sensing S4 transmembrane segments. These mutations cause dominant ion channelopathies affecting many tissues such as brain, heart, and skeletal muscle. Recent studies suggest that the pathogenesis of associated phenotypes is not limited to alterations in the gating of the ion-conducting alpha pore. Instead, aberrant so-called omega currents, facilitated by the movement of mutated S4 segments, also appear to contribute to symptoms. Surprisingly, these omega currents conduct cations with varying ion selectivity and are activated in either a hyperpolarized or depolarized voltage range. This review gives an overview of voltage sensor channelopathies in general and focuses on pathogenesis of skeletal muscle S4 disorders for which current knowledge is most advanced.

Keywords: epilepsy and neuromyotonia, long QT syndrome, familial hemiplegic migraine, myotonia and paramyotonia, hyperkalemic and hypokalemic periodic paralysis, sodium overload, cytotoxic edema, degeneration

INTRODUCTION

The basic motif of the alpha subunit of voltage-gated cation channels is a tetrameric association of four domains I–IV, each consisting of six transmembrane helical segments S1–S6, connected by intracellular and extracellular loops. At the resting potential, open probability is low. Activation results from a depolarization-induced conformational change leading to the opening of the alpha pore. When the pore is pharmacologically blocked, charge movements in the electrical membrane field are measurable as so-called gating currents. These gating currents are a result of the outward movement of highly conserved voltage-sensitive S4 segments which display an arginine or lysine residue at every third amino acid position, almost vertically aligned (denoted as R1, R2, R3, etc.). At resting potential, the outermost S4 charge separates the extracellular fluid from the cytoplasm. With membrane depolarization, each S4 moves outwardly shifting deeper situated arginines to the critical position of extra-intracellular separation. During their outward movement, the S4 segments move in a spiral path through canaliculi of the channel protein made up of segments S1–S3 (Figures 1 and 2). Likewise, during recovery from channel inactivation, the S4 segments are thought to move back to their original position. Because of the narrow constriction separating extracellular from intracellular compartments, mutations of the S4 charges may cause either a hyperpolarization-activated or a depolarization-activated non-specific cation leak called the omega current (Figure 2).

An omega current was first described in the voltage-gated potassium channel of drosophila Shaker. In this channel the mutation R1H in S4 generates an inward-directed hyperpolarization-induced proton current that becomes increasingly prominent as the proton reversal potential $E_H$ is shifted to more positive values (Starace and Bezanilla, 2004). R1 substitutions to residues other than histidine result in a hyperpolarization-induced inward current carried by alkali metal cations rather than protons (Tombola et al., 2005) indicating that this mutation creates a short-circuit connection of intracellular and extracellular compartments in the canaliculus. This current varies with the identity of the substituted residue: $R_1S > R_1C > R_1V > R_1A$, has the selectivity $Cs^+ > K^+ > Li^+$, and is not affected by alpha pore blockers. Shaker mutants R2H and R3H conduct protons at potentials corresponding to the voltage-dependent movement of S4 charges, as the current is maximal at potentials close to midpoint of the $Q_{ON}$-voltage relation (Starace et al., 1997; Starace and Bezanilla, 2001). Further depolarization blocks the omega pore, consistent with the model that outward S4 movement shifts the short-circuiting mutant residues out of the canaliculus.

Studies on Shaker potassium channel and domain II of rat brain sodium channel Na$_{1.2}$ suggest that substitution of a single S4 arginine may be insufficient to produce a non-proton omega current, but that two adjacent mutations (i.e., R2/R3 or II-R1/R2) are required (Sokolov et al., 2005; Gamal El-Din et al., 2010). In this respect, the presence of alanine at the position equivalent to R0 in Shaker may therefore enhance the omega current of R1S. The motif of adjacent arginine replacements recurs in some of the potassium channel disorders and may be explained by the degree of accessibility of arginines to the extracellular or intracellular compartments. However, this does not hold true for all channels suggesting that position and orientation of the S4 segment and its environment play an important role as well. Based on current knowledge of S4 position, in this review R0 designates charge positions of S4 outside of the canaliculus and R1 the first charge inside of it.

For human diseases, the channelopathies result from mutations in voltage-gated ion channels. In several of these disorders,
mutations of specific charges of S4 segments are known, such as in epilepsy, hemiplegic migraine, long QT (LQT) syndrome, paramyotonia congenita, and periodic paralyses (Table 1). The underlying mutations generally modify voltage sensitivity of gating and maximal amplitude of alpha current. Additionally, some of these mutations have been reported to produce an omega current. Most of these are inward currents that result in enhanced membrane depolarization, contributing to the symptoms of the channelopathy. Depending on the position of the S4 mutation and the voltage threshold of activation of the channel, the omega current can appear in very different voltage ranges.

This review briefly outlines the clinical features and pathogenesis of the S4 channelopathies with a focus on mutation-dependent changes of alpha and omega currents as well as their contributions to the phenotype. It also introduces the concept of membrane bistability in general and in computer simulations incorporating omega current. Also discussed are the consequences of intracellular sodium overload and tissue degeneration to explain the non-episodic features of the channelopathies and the ideas behind best practice treatment. For further reading, there are reviews with more emphasis on S4 structure and function (Catterall, 2010), S4 mutations in channels of skeletal muscle (Cannon, 2010; Jurkat-Rott et al., 2010), or drug action in periodic paralyses and related channelopathies (Matthews and Hanna, 2010; Tricarico and Camerino, 2011).

**EPILEPSY AND NEUROMYOTONIA**

Epilepsy is characterized by recurring episodes of synchronized electrical discharges of neurons caused by their facilitated depolarization within the central nervous system. The symptoms of a seizure depend on age of the patient, the underlying cause, and the brain region involved.

Generalized epilepsy with febrile seizures plus (GEFS+) is a childhood-onset syndrome featuring febrile seizures (FS) and afebrile epileptic convulsions within the same pedigree. The penetrance is ~60%. In two-thirds of affected individuals either FS persist after the sixth year of life or afebrile generalized tonic-clonic seizures additionally occur (FS+). GEFS+ type II is caused among others by missense mutations in the alpha subunit of the neuronal sodium channel Na_1.1, encoded by SCN1A. Mutations frequently destabilize the fast-inactivated state, resulting in a persistent inward sodium current that depolarizes the membrane potential to a value closer to the Na_1.1 threshold (facilitated spike generation). Additionally, a few mutations result in loss-of-function by trafficking defects (Catterall et al., 2010; Escayg and Goldin, 2010). S4 mutations II-R1C, IV-R4H, and IV-R7C (Figure 3) result in additional loss-of-function effects such as decreased current amplitude and stabilization of the inactivated state (Alekov et al., 2000; Spampanato et al., 2001; Lossin et al., 2003; Barela et al., 2006; Vanoye et al., 2006). Apparently, loss-of-function in inhibitory neurons produces overexcitability (Martin et al., 2010).
similar to gain-of-function effects in excitatory neurons (Kahlig et al., 2006, 2010).

Severe myoclonic epilepsy of infancy (SMEI), or Dravet syndrome, is characterized by clonic or tonic-clonic seizures that occur in the first year of life, are often prolonged, and are typically associated with fever. During the course of the disease, patients develop additional afebrile generalized and partial seizures. Cognitive deterioration appears in early childhood. In contrast to GEFS+, the syndrome is resistant to pharmacotherapy, although stiripentol seems to have a positive effect by enhancing GABAergic neurotransmission. Cranial magnetic resonance (MR) imaging in patients reveals focal and generalized atrophy. Because some patients with SMEI have a family history of febrile or afebrile seizures, and in some families GEFS+ and SMEI overlap, SMEI may therefore be regarded as the most severe phenotype of the GEFS+ spectrum (Mullen and Scheffer, 2009). SMEI is caused by mutations in SCN1A encoding Na\textsubscript{v}1.1. Most SMEI mutations cause loss-of-function due to nonsense mutations demonstrating that haploinsufficiency of SCN1A is pathogenic (Oakley et al., 2011). The loss-of-function of Na\textsubscript{v}1.1 channels results in reduced action potential (AP) firing in hippocampal inhibitory neurons, thus generating overexcitability. IV-R4C causes gain-of-function

FIGURE 2 | Omega pores and currents dependent on the R position. (A) Replacement of the outermost arginine (red) by a neutral amino acid (gray) such as glycine (R1G) opens a conductive pathway through the polarized membrane, resulting in an omega current (red). At depolarized potentials at which the S4 segment moves outward, the conductive pathway is closed by a deeper arginine and the omega current ceases. In contrast the replacement of a deeper arginine (R3G) only opens the omega pore if the membrane is depolarized. (B) Homology model of domain I in hNa\textsubscript{v}1.4 based on crystal structure of NaVAb (activated-closed; crystal structure at 0 mV), using Modeller. Positions of arginine and lysine residues of DIS4 are shown, relative to the putative gating pore constriction (arrow). Modified from Groome and Winston (2012). (C) Comparison of current-voltage (I/V) traces for wild type hNa\textsubscript{v}1.4 and R222G, with plots of raw I/V, linear leak, and normalized current (linear leak subtracted from I/V and normalized to gating current at +40 mV). The mutation R222G causes HypoPP type 2. External solution contained 120 mM K\textsuperscript{+} and 1 \mu M TTX. Modified from Holzherr et al. (2010).
| Channel Gene | Disease | Mutation | Location | Reference genetics |
|-------------|---------|----------|----------|-------------------|
| Kv7.1       | LQT-1   | R231C    | S4       | Lupoglazoff et al. (2004), Fodstad et al. (2004) |
|             |         | R243H/C  | R5       | Mohammad-Panah et al. (1999), Franqueza et al. (1999), Dodek et al. (2001), Wurts et al. (2007) |
| Kv7.2       | BFNS-PNH| R207W/Q  | S4       | Dedek et al. (2001), Wuttke et al. (2007) |
|             |         | R259G    | R3       | Dedek et al. (2001), Wuttke et al. (2007) |
| Kv11.1      | LQTS-2  | K525N-R528P | R0-R1 | Millat et al. (2006) |
|             |         | R534C    | R3       | Nakajima et al. (1999) |
| Nav1.1      | GEFS+   | R859C    | S4       | Barela et al. (2006) |
|             |         | R1648H   | R4       | Escayg et al. (2000), Alekov et al. (2000), Spampanato et al. (2000), Kahlig et al. (2010) |
|             |         | R1657C   | R7       | Lossin et al. (2003) |
|             |         | SMEI     | R2       | Matthews et al. (2009) |
|             |         | HypoPP-2 | R2       | Bulman et al. (1999), Struyk et al. (2000), Sokolov et al. (2001), Kuzmenkin et al. (2002), Sandoval et al. (2007), Strom and Cannon (2007), Wu et al. (2008) |
|             |         | HypoPP-2 | R3       | Carle et al. (2009), Cook et al. (2009) |
|             |         | NormoPP  | R1       | Hong et al. (2010) |
|             |         | R129Q    | R2       | Carle et al. (2009) |
|             |         | R135Q    | R3       | Carle et al. (2009) |
|             |         | R135H    | R3       | Carle et al. (2009) |

Table 1 | Voltage sensor mutations in K⁺, Na⁺, and Ca²⁺ channelopathies.

| Channel | Gene | Disease | Mutation | Location | Reference | Reference function |
|---------|------|---------|----------|----------|-----------|--------------------|
| K⁺      | KCNQ1| LQT-1   | R231C    | S4       | Lupoglazoff et al. (2004), Fodstad et al. (2004) |               |
|         |      |         | R243H/C  | R5       | Mohammad-Panah et al. (1999), Franqueza et al. (1999), Dodek et al. (2001), Wurts et al. (2007) |               |
| Na⁺     | KCNQ2| BFNS-PNH| R207W/Q  | S4       | Dedek et al. (2001), Wuttke et al. (2007) |               |
|         |      |         | R259G    | R3       | Dedek et al. (2001), Wuttke et al. (2007) |               |
| Na⁺,1,4 | SCN4A| HypoPP-2| R222W    | R2       | Matthews et al. (2009) |               |
|         |      |         | R672H    | R4       | Bulman et al. (1999), Struyk et al. (2000), Sokolov et al. (2001), Kuzmenkin et al. (2002), Sandoval et al. (2007), Strom and Cannon (2007), Wu et al. (2008) |               |
| Ca²⁺    | SCN1A| GEFS+   | R1200C   | R3       | Matthews et al. (2009) |               |
|         |      |         | R1200C   | R3       | Matthews et al. (2009) |               |
| Channel  | Subunit  | Mutation  | Location  | Reference                                                                 |
|----------|----------|-----------|-----------|---------------------------------------------------------------------------|
| Na\textsubscript{1.5} | SCN5A    | R1448H/C/SA/L/P | IVS4      | Ptacek et al. (1992), Lerche et al. (1996), Matthews et al. (2008)       |
| Na\textsubscript{1.5} | SCN5A    | R225Q/W   | IS4       | Bezzina et al. (2003), Millat et al. (2006)                               |
| Na\textsubscript{1.5} | SCN5A    | R814Q     | IS4       | Frigo et al. (2007)                                                      |
| Na\textsubscript{1.5} | SCN5A    | R1623U/Q  | IVS4      | Makita et al. (1998), Yamagishi et al. (1998), Splawski et al. (2000)   |
| Na\textsubscript{1.5} | SCN5A    | R1626P    | R1        | Ruan et al. (2007)                                                       |
| Na\textsubscript{1.5} | SCN5A    | R1644Q/H  | R7        | Splawski et al. (2000)                                                   |
| Ca\textsubscript{2.1} | CACNA1S  | R528H/G   | IS4       | Jurkat-Rott et al. (1994), Matthews et al. (2009)                        |
| Ca\textsubscript{2.1} | CACNA1S  | R897S     | IIIS4     | Chabrier et al. (2008)                                                   |
| Ca\textsubscript{2.1} | CACNA1S  | R900S     | IIIS4     | Matthews et al. (2009)                                                   |
| Ca\textsubscript{2.1} | CACNA1S  | R1239H/G  | IVS4      | Ptacek et al. (1994), Lehmann-Horn et al. (1995)                         |
| Ca\textsubscript{2.1} | CACNA1A  | R19Q      | IS4       | Ophoff et al. (1996)                                                     |
| Ca\textsubscript{2.1} | CACNA1A  | R195Q     | R1        | Ducros et al. (2001)                                                     |
| Ca\textsubscript{2.1} | CACNA1A  | R883Q     | R1        | Battistini et al. (1999)                                                 |
| Ca\textsubscript{2.1} | CACNA1A  | R1346Q    | IIIS4     | Alonso et al. (2004)                                                     |
| Ca\textsubscript{2.1} | CACNA1A  | R1681H    | IVS4      | Friend et al. (1993)                                                     |
| Ca\textsubscript{2.1} | CACNA1A  | R1664Q    | R2        | Tonelli et al. (2006)                                                    |
| Ca\textsubscript{2.1} | CACNA1A  | R1667W    | R3        | Ducros et al. (2001)                                                     |

**Bold print:** proof of omega currents or omega-analogous leaks in native tissue.
by destabilizing fast inactivation and producing persistent currents (Rhodes et al., 2004) that may be inhibited by the sodium channel blocker ranolazine (Kahlig et al., 2010; Figure 3).

Benign familial neonatal seizures (BFNS) are dominantly inherited with a penetrance of 85%. The seizures manifest within the first weeks of life and typically disappear spontaneously after weeks to months. Seizures may have a partial onset or may appear as generalized. Accordingly, ictal EEGs show focal and generalized discharges. Intercital EEGs are mostly normal. The risk of seizures recurring in adulthood is ~15%, but psychomotor development is usually normal. Causative mutations have been identified in Kv7.2 and Kv7.3 potassium channels encoded by KCNQ2 and KCNQ3 respectively that interact with each other and constitute the so-called M-current, an important regulator of membrane potential near the AP threshold. Co-expression of heteromeric wild type and mutant Kv7.2/Kv7.3 channels usually reveals a potassium current reduction of ~20–30% in the setting of haploinsufficiency. This causes BFNS by depolarizing the membrane and facilitating AP firing (Maljevic et al., 2008). In contrast, S4 mutations of the pattern R3W/Q (Figure 3) produce a dominant negative effect on co-expressed wild type brought about by a drastic depolarizing shift of the activation curve and slowing of the activation time course (Dedek et al., 2001; Wutke et al., 2007; Miceli et al., 2012). This suppression of inhibitory neurons explains the hyperexcitability that affects central as well as peripheral neurons. The latter locus of hyperexcitability leads to additional neuromyotonia also termed peripheral nerve hyperexcitability (PNH). This disorder is characterized by short spells of spontaneous skeletal muscle overactivity resulting in twitching, undulation, or rippling of the muscles and painful cramps, so that the phenotype for these S4 mutation carriers is BFNS-PNH. Omega currents have been implicated in BFNS for the analogous Kv7.4 channel. There, corresponding R3W/Q mutations generate non-specific depolarization-induced cation outward currents of ~1% of the pore current amplitude, at the +40 mV voltage step (Miceli et al., 2012). In Kv7 channels, single mutations of R1 and R3 fulfill the concept of adjacent arginine replacements because there is a glutamine at position R2.

LONG QT SYNDROME

Long QT syndrome is named for an elongated QT interval in the electrocardiogram. It is caused by lengthening of the repolarization phase of the cardiac ventricular AP. Because duration of the cardiac AP is dispersed in different regions of the ventricle depending on regional channel expression, any disproportionate

![FIGURE 3 | S4 sequences of channels with an R0 to R6 mutation.](image)

Positively charged residues in R0 to R6 positions are delineated with a shaded background (gray). The constriction of the omega pore lies between R2 and R3. Therefore an inward movement of S4 due to hyperpolarization opens the omega pore if R1 or R2 is replaced by a neutral amino acid. An outward movement of S4 due to depolarization opens the omega pore if R3 or R4 is replaced by a neutral amino acid. These gray-background arginines are boxed. The Shaker K+ channel serves as reference. Neutral replacements of its arginines R2 and R3 have been described as proton transporters.
prolongation of the AP increases the probability for re-entry of the depolarization wave, early after-depolarizations and thus, arrhythmia. Associated ECG findings may be ventricular bigemini and torsade de pointes in which the QRS complex twists around the isoelectric axis in the electrocardiogram. By this, syncope and sudden death may result in young and otherwise healthy individuals. LQT syndrome (LQTS) is caused among others by loss-of-function of potassium channels $K_v$7.1 encoded by $KCNQ1$ or $KCNH2$ and by gain-of-function of the $Na_v$1.5 sodium channel encoded by $SCN5A$.

$K_v$7.1 currents deactivate very slowly allowing adaptive shortening of the AP during tachycardia by incomplete deactivation. Therefore, loss-of-function in $K_v$7.1 leads to arrhythmia especially at elevated heart rate due to physical or emotional stress. R1C decreases current amplitude which explains the LQT in the electrocardiogram, but also produces a hyperpolarizing shift of the voltage dependence of activation and tail currents, thereby explaining the additional atrial fibrillation in these patients (Bartos et al., 2011). RSH/C produce a slowed rate of activation, a positive voltage shift of activation and/or dominant suppression of co-expressed wild type (Franqueza et al., 1999; Mohammad-Panah et al., 1999; Chouabe et al., 2000). R1, R3, and R5 mutants all fulfill the concept of adjacent arginine replacements because there is a glutamine at R2 and a histidine at R4 (Figure 3).

$K_v$11.1 activates and deactivates relatively slowly in comparison to a rapid inactivation. LQT mutations suppress repolarization of the myocardial AP and lengthen the QT interval by either loss-of-function or haploinsufficiency. A dominant negative effect may be achieved by current reduction of the tetrameric channel complex. For the LQT double mutation of R0/R1, there is no functional data but there are two adjacent arginines are changed (Figure 3). The point mutation R3C reduces current amplitude and accelerates deactivation thereby slowing repolarization of the cardiac AP in its final phase (Nakajima et al., 1999).

$Na_v$1.5 initiate the cardiac AP. LQT mutants frequently conduct a persistent inward current during membrane depolarization and single channel recordings show fluctuation between normal and non-inactivating gating modes. I-R3Q/W shift the steady-state inactivation curve to the right (Bezzina et al., 2003), IV-R0L/Q delay inactivation (Makita et al., 1998), IV-R1P impairs inactivation or shifts the steady-state inactivation curve to the left (Ruan et al., 2007) and decreases inactivation upon stretch modulation (Banderali et al., 2010). Mutations IV-R7C/H show dispersed re-openings (Dumaine et al., 1996; Figure 3). It has yet to be established that omega currents play a role in the pathogenesis of $K_v$ or $Na_v$ LQTS channelopathies, but the finding of mutations in these cardiac disorders in R1–R3 residues of S4 raises that possibility (Table 1; Sokolov et al., 2007).

HEMIPLEGIC MIGRAINE

Familial hemiplegic migraine (FHM) presents with characteristic unilateral migraine headaches accompanied by nausea, phonophobia, and photophobia. Episodes are typically precipitated by an aura with symptoms of both hyper- and hypo-excitability such as aphasis, dysarthria, vertigo, homonymous hemianopsia, cheiro-oral paresthesias, and some degree of (primarily) unilateral paresis. Additionally, ataxia and cerebellar degeneration are frequently part of the FHM phenotype. Up to 50% of cases are caused by mutations in $Ca_{v}$.2.1 encoded by $CACNA1A$. Current pathogenesis models of migraine with aura suggests cortical spreading depression which consists of an initial brief spike of increased neuronal activity followed by long-lasting suppression of excitability spreading across the cortex at 1–3 mm/min. The depression wave is associated with long-lasting depolarization associated with elevation of extracellular potassium and intracellular sodium. The progress of FHM correlates to the succession of symptoms during the aura initiating the migraine attacks. FHM1 includes sporadic hemiplegic migraine with progressive cerebellar ataxia. The aura may be prolonged and confusion and loss of consciousness may occur. In the interval, some families additionally present with epilepsy, retinal degeneration, hypacusis, and persistent cerebellar dysfunction with Parkinje cell atrophy. While migraine is mainly caused by gain-of-function, loss-of-function may lead to additional ataxia. Of the seven known S4 mutations in $Ca_{v}$.2.1, there is functional data for only two. I-R0Q increases open probability and channel density in vitro (Kraus et al., 1998; Hans et al., 1999). In a knock-in mouse this mutation generates increased current density in cerebellar neurons, enhanced transmission at the neuromuscular junction, and reduced threshold and increased velocity of cortical spreading depression, effects that are compatible with an omega current (van den Maagdenberg et al., 2004; Figure 3). II-R1Q shifts activation to the left but decreases peak current (Kraus et al., 2000). Omega currents produced by either of these mutations have yet to be demonstrated.

SODIUM CHANNEL MYOTONIA AND PARAMYOTONIA

Myotonia is an involuntary slowed relaxation after a forceful voluntary muscle contraction, experienced by the patient as muscle stiffness. After making a forceful fist or eyelid closure, the patient cannot reopen their hand or eye. Repetition decreases the myotonia, a phenomenon called warm-up. Electrical hyperexcitability of the muscle fiber membrane is the basis for myotonia, apparent in the form of repetitive APs in the EMG. Needle insertions into the resting muscle elicit myotonic bursts, i.e., runs of APs with amplitude and frequency modulation that sound like dive bombers. Autosomal dominantly inherited myotonia can be caused among others by mutations in $SCN4A$, the gene encoding the alpha subunit of the voltage-gated sodium channel of skeletal muscle, $Na_v$.1.4 (Heine et al., 1993), essential for generation of the muscle fiber AP. Most mutations destabilize the fast-inactivated state so that the channel inactivates slower and incompletely (Lerche et al., 1993). The resulting subthreshold membrane potential facilitates AP generation. I-R3W causes typical myotonia with warm-up phenomenon and transient weakness (Lee et al., 2009). However, no functional data are available.

Paramyotonia (PC) is also caused by dominant $SCN4A$ mis-sense mutations. The cardinal symptom is cold-induced muscle stiffness that increases with continued activity called paradoxical myotonia, or paramyotonia for short. In most families, on intensive cooling the stiffness gives way to flaccid weakness or even to paralysis which is caused by severe membrane depolarization (Lehmann-Horn et al., 1987; Lerche et al., 1996). Families with IV-R0/H/C/S/L/P also have episodes of generalized periodic paralysis (Lehmann-Horn and Jurkat-Rott, 1999). Such attacks occur...
Autosomal dominant hypokalemic periodic paralysis (HypoPP) is characterized by episodes of flaccid generalized muscle weakness accompanied by low serum potassium levels. Triggers for the weakness are carbohydrates and insulin with subsequent hypokalemia, rest after exercise, and cooling. Oral potassium administration accelerates the recovery of muscle strength. Native patient muscle fibers show long-lasting membrane depolarization paradoxically triggered by lowering of extracellular potassium, resulting in an inactivation of sodium channels necessary for AP generation (Jurkat-Rott et al., 2000). This effect is exacerbated in the presence of insulin (Bond and Gordon, 1993; Ruff, 1999). Permanent progressive weakness is additionally found in ~60% of patients whereby muscle degenerates and is increasingly replaced by fatty tissue. The causative mutations are located in the skeletal muscle calcium channel Ca,1.1 encoded by CACNA1S (HypoPP-1) and the skeletal muscle sodium channel Na,1.4 encoded by SCN4A. Given the finding that all but one of these mutations neutralize a positively charged S4 residue, it is not surprising that a role for omega currents as a causal factor in the pathogenesis of the channelopathies has been most clearly demonstrated for the periodic paralysis.

Functional studies of the alpha currents of either of these channels do not satisfactorily explain the phenotype. In Ca,1.1, II-R1H/G and IV-R2H/G (Figure 3) lead to loss-of-function in the sense of current amplitude reduction, slowing of activation, reduced open probability, left shift of steady-state inactivation, reduced amplitude and broadening of APs (Lehmann-Horn et al., 1995; Lapie et al., 1996; Jurkat-Rott et al., 1998; Morrill et al., 1998; Morrill and Cannon, 1999; Kuzmenkin et al., 2007). None of these gating defects are expected to lead to increased depolarization. Similarly, in Na,1.4, II-R1H, II-R2H/G/S/C, and II-R3G/W/Q show reduced current amplitude, left shift of steady-state fast inactivation, enhanced fast and slow inactivation, slowed recovery after long depolarizations, and reduced AP amplitudes (Bulman et al., 1998; Jurkat-Rott et al., 2000; Struyk et al., 2000; Bendahhou et al., 2001; Kuzmenkin et al., 2002; Carle et al., 2006; Wu et al., 2008, 2011). These defects would not contribute to depolarization either.

In Na,1.4, II-R1H, II-R2H/G/C/S, and III-R2Q mutations generate omega currents that are activated by hyperpolarization, are still active at the usual resting potential, but are closed by depolarizations large enough to activate and thus, move S4 (Figure 3). Their amplitude is about 1% of the alpha pore current. Substitution of these arginines by the bulky histidine residue enables proton transport only; other cations do not seem to have enough space to pass (Sokolov et al., 2007; Struyk and Cannon, 2007; Francis et al., 2011). Substitution of these arginines with uncharged residues such as glycine allow an inwardly rectifying flow of small monovalent cations whereby potassium and cesium are preferred over sodium or lithium (Sokolov et al., 2007; Struyk et al., 2008). Figure 2C shows current-voltage relationships for R222G/hNaV1.4 channels from experiments performed in our lab as an example (Holzherr et al., 2010). Omega pores conduct currents that show an above-linear increase in amplitude with hyper- or depolarization although the electrical field is focused to a single amino acid (Ohm resistor) and not constantly increasing within the membrane (constant field theory). The non-linearity of the omega current reflects the stochastic process of a voltage-dependent open probability and follows a Boltzmann distribution.

Guanidinium, a derivative of arginine, has greater than 10 times the conductance through the omega pore than monovalent cations, while divalent and trivalent cations block the omega pore at mM concentrations (Sokolov et al., 2010). In that study, a screen of guanidine derivatives as potential blockers of the pathogenic omega current in HypoPP yielded one compound, 1-(2-4 xylyl) guanine that exhibited similar potency for block compared to the divalent cations tested. In addition, there is an inward cation leak current at hyperpolarized potentials in native muscle of R1H knock-in mice with omega features (Wu et al., 2011). The conclusion from these alternative approaches to study omega currents is that they contribute to the depolarization leading to inexcitability and weakness. Nevertheless, despite similarities of sodium channel omega currents with those in Shaker produced by R1H mutations, their blockade is quite different, suggesting differences in shape, size, and exact cation pathway along the canaliculi of these channels. Perhaps this phenomenon is related to the postulation that two adjacent mutated charges promote omega currents in voltage-gated potassium channels, a requisite that does not hold true for sodium channels.

In contrast to the hyperpolarization-induced omega currents from substitutions of II-R1 and II-R2, II-R3G/Q/W mutations generate Na,1.4 cation currents that are activated by depolarization (Figure 3). This means that the omega currents are conducted when S4 is in the activated or inactivated state, but not in the resting state. This omega current is deactivated at hyperpolarized membrane potentials (Sokolov et al., 2008). The associated phenotype differs slightly in the ictal serum potassium levels which can be low or normal (normokalemic periodic paralysis, NormoPP). Also, the reaction to oral potassium administration may be different for HypoPP – anything from amelioration to worsening of the weakness.

For II-R1H/Q and IV-R2H/G Ca,1.1 channel mutations (Figure 3), no direct omega currents have been shown. However, in native patient muscle there is an inward cation leak current at hyperpolarized potentials with omega features (Jurkat-Rott et al., 2009). Also, based on these measurements, the periodic paralysis

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**PERIODIC PARALYSIS**

Autosomal dominant hypokalemic periodic paralysis (HypoPP) is characterized by episodes of flaccid generalized muscle weakness accompanied by low serum potassium levels. Triggers for the weakness are carbohydrates and insulin with subsequent hypokalemia, rest after exercise, and cooling. Oral potassium administration accelerates the recovery of muscle strength. Native patient muscle fibers show long-lasting membrane depolarization paradoxically triggered by lowering of extracellular potassium, resulting in an inactivation of sodium channels necessary for AP generation (Jurkat-Rott et al., 2000). This effect is exacerbated in the presence of insulin (Bond and Gordon, 1993; Ruff, 1999). Permanent progressive weakness is additionally found in ~60% of patients whereby muscle degenerates and is increasingly replaced by fatty tissue. The causative mutations are located in the skeletal muscle calcium channel Ca,1.1 encoded by CACNA1S (HypoPP-1) and the skeletal muscle sodium channel Na,1.4 encoded by SCN4A.

Given the finding that all but one of these mutations neutralize a positively charged S4 residue, it is not surprising that a role for omega currents as a causal factor in the pathogenesis of the channelopathies has been most clearly demonstrated for the periodic paralysis.

Functional studies of the alpha currents of either of these channels do not satisfactorily explain the phenotype. In Ca,1.1, II-R1H/G and IV-R2H/G (Figure 3) lead to loss-of-function in the sense of current amplitude reduction, slowing of activation, reduced open probability, left shift of steady-state inactivation, reduced amplitude and broadening of APs (Lehmann-Horn et al., 1995; Lapie et al., 1996; Jurkat-Rott et al., 1998; Morrill et al., 1998; Morrill and Cannon, 1999; Kuzmenkin et al., 2007). None of these gating defects are expected to lead to increased depolarization. Similarly, in Na,1.4, II-R1H, II-R2H/G/S/C, and II-R3G/W/Q show reduced current amplitude, left shift of steady-state fast inactivation, enhanced fast and slow inactivation, slowed recovery after long depolarizations, and reduced AP amplitudes (Bulman et al., 1998; Jurkat-Rott et al., 2000; Struyk et al., 2000; Bendahhou et al., 2001; Kuzmenkin et al., 2002; Carle et al., 2006; Wu et al., 2008, 2011). These defects would not contribute to depolarization either.

In Na,1.4, II-R1H, II-R2H/G/C/S, and III-R2Q mutations generate omega currents that are activated by hyperpolarization, are still active at the usual resting potential, but are closed by depolarizations large enough to activate and thus, move S4 (Figure 3). Their amplitude is about 1% of the alpha pore current. Substitution of these arginines by the bulky histidine residue enables proton transport only; other cations do not seem to have enough space to pass (Sokolov et al., 2007; Struyk and Cannon, 2007; Francis et al., 2011). Substitution of these arginines with uncharged residues such as glycine allow an inwardly rectifying flow of small monovalent cations whereby potassium and cesium are preferred over sodium or lithium (Sokolov et al., 2007; Struyk et al., 2008). Figure 2C shows current-voltage relationships for R222G/hNaV1.4 channels from experiments performed in our lab as an example (Holzherr et al., 2010). Omega pores conduct currents that show an above-linear increase in amplitude with hyper- or depolarization although the electrical field is focused to a single amino acid (Ohm resistor) and not constantly increasing within the membrane (constant field theory). The non-linearity of the omega current reflects the stochastic process of a voltage-dependent open probability and follows a Boltzmann distribution.

Guanidinium, a derivative of arginine, has greater than 10 times the conductance through the omega pore than monovalent cations, while divalent and trivalent cations block the omega pore at mM concentrations (Sokolov et al., 2010). In that study, a screen of guanidine derivatives as potential blockers of the pathogenic omega current in HypoPP yielded one compound, 1-(2-4 xylyl) guanine that exhibited similar potency for block compared to the divalent cations tested. In addition, there is an inward cation leak current at hyperpolarized potentials in native muscle of R1H knock-in mice with omega features (Wu et al., 2011). The conclusion from these alternative approaches to study omega currents is that they contribute to the depolarization leading to inexcitability and weakness. Nevertheless, despite similarities of sodium channel omega currents with those in Shaker produced by R1H mutations, their blockade is quite different, suggesting differences in shape, size, and exact cation pathway along the canaliculi of these channels. Perhaps this phenomenon is related to the postulation that two adjacent mutated charges promote omega currents in voltage-gated potassium channels, a requisite that does not hold true for sodium channels.

In contrast to the hyperpolarization-induced omega currents from substitutions of II-R1 and II-R2, II-R3G/Q/W mutations generate Na,1.4 cation currents that are activated by depolarization (Figure 3). This means that the omega currents are conducted when S4 is in the activated or inactivated state, but not in the resting state. This omega current is deactivated at hyperpolarized membrane potentials (Sokolov et al., 2008). The associated phenotype differs slightly in the ictal serum potassium levels which can be low or normal (normokalemic periodic paralysis, NormoPP). Also, the reaction to oral potassium administration may be different for HypoPP – anything from amelioration to worsening of the weakness.

For II-R1H/Q and IV-R2H/G Ca,1.1 channel mutations (Figure 3), no direct omega currents have been shown. However, in native patient muscle there is an inward cation leak current at hyperpolarized potentials with omega features (Jurkat-Rott et al., 2009). Also, based on these measurements, the periodic paralysis
episodes can be successfully modeled. The underlying idea is that depolarized muscle fibers will be paralyzed, and that polarized fibers will be fully functional. If transitions between these two situations are reversible, the membrane potential is bi-stable.

**BI-STABILITY OF MEMBRANE POTENTIAL**

*P-states* are the electrically stable resting membrane potentials of a cell in the nomenclature of Jurkat-Rott et al. (2009). Normal cells reveal a bimodal distribution around the stable membrane potentials P1 and P2. At physiological conditions, most fibers are highly negative polarized and in the excitable P1-state which follows the predictions of the Goldman–Hodgkin–Katz equation. Upon an increased sodium conductance, e.g., by omega pores, the fraction of cells in the (depolarized) P2-state is increased. With slow depolarization, voltage-gated sodium channels might inactivate via closed-state inactivation and render the cells inexitable. In contrast, cells that remain in the P1-state are only slightly depolarized and thus still excitable. This bi-stability is the result of inwardly rectifying potassium channels ($K_{ir}$), which open with hyperpolarization and close with depolarization (Figure 4A). The bi-stability is the reason that only a small increase in sodium conductance, e.g., by an omega pore, is required to shift cells from the P1- to the P2-state (Figure 4B). Vice versa, a repolarizing conductance can shift the membrane back to the P1-state (Figure 4).

Transitions between the P1- and P2-states can occur when any trigger drives the system closer to a limit point or shifts a limit point. If the limit points of both states (LP1 and LP2) are situated at different $K^+$ values, the system shows hysteresis (Figure 4C). If external $K^+$ is considered as a control parameter, it is shown to play an important role in driving the system to its limits, and set the stage during “physiological” hypokalemia, for the paradoxical depolarization triggered by a slight increase in sodium conductance provided by an omega current. A significant role for the activated omega pore as a causal factor in the pathogenesis of HypoPP is supported by the computer model whose details are given in the Appendix and whose parameters are given in Table 2.

A drop of serum $K^+$ will decrease $K_{ir}$ conductance. Although the Nernst equation predicts hyperpolarization when external $K^+$ is reduced, the hypokalemia-induced reduction of $K_{ir}$ conductance may shift the cells from the P1- to the P2-state (Figure 4C). Therefore, cells show a bimodal distribution of membrane potentials especially at low $K^+$. This phenomenon is called paradoxical depolarization (Jurkat-Rott and Lehmann-Horn, 2007; Struyk and Cannon, 2008; Jurkat-Rott et al., 2009). Not surprisingly, decreased conductance in mutant $K_{ir}$ channels contributes to the pathogenesis of episodic paralysis associated with thyrotoxicosis ($K_{ir}$ 2.6; Ryan et al., 2010; Cheng et al., 2011), periodic paralysis and cardiac arrhythmia in Tawil–Anderson’s syndrome ($K_{ir}$ 2.1; Plaster

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**Figure 4** Effects of omega currents schematically (A) and in a computer simulation (B). (A) The current-voltage relationship of $K_{ir}$, potassium channels shows a voltage range characterized by a “negative” resistance. This negativity leads to membrane bi-stability. Whereas small instantaneous changes of P1 will be compensated for (P1 is therefore a stable membrane potential), larger depolarizing artifacts will cause a jump of P1 to the limit point LP2. P1 can be regained by substantial repolarizing influences like the Na/K pump. (B) The curve is downwardly shifted by an omega Na$^+$ current. Limit point LP1 is a very instable membrane potential that will be shifted to P2 by even smallest instantaneous changes. In the P2-state the cell membrane will be electrically stable. (C) Membrane potentials P for various $K^+$, values and for various omega pore conductances (in $\mu$S/cm²). Reducing $K^+$ first leads to hyperpolarization until the limit point (LP1) is reached at which the membrane potential becomes instable and jumps to the depolarized state of about −58 mV. From there, increasing $K^+$, takes the potential along the curve until LP2 is reached. LP2 is the starting point for the repolarization. The curves of LP1 and LP2 meet in the cusp point, CP. The region inside the cusp (bounded by LP1, LP2, and CP) is bi-stable. In contrast omega pore conductances larger than 18 $\mu$S/cm² result in gradual depolarization without bi-stability. The model reveals that an omega pore shifts LP1 and LP2 (the cusp) to the right, i.e., less severe hypokalemia is required to shift cells from the P1- to the P2-state. The membrane potentials yielded by the computer simulation were compared with values measured for muscle fibers by use of microelectrodes: open symbols stand for human controls (−83 ± 5 mV in 95% of fibers at 4 mM K$^+$, −99 ± 3 mV for 87% at 1.5 mM K$^+$, and −58 mV for 91% at 1 mM K$^+$); filled symbols for HypoPP patients with either Ca1.1-R1239H (circle: −74 ± 5 mV in 76% of fibers at 4 mM K$^+$) or Ca1.1-R528H (triangle: −75 ± 5 mV in 91% of fibers at 4 mM K$^+$); at 1.5 mM K$^+$, 95% of the patients’ fibers −56 mV (square; n = 127). Modified after Jurkat-Rott et al. (2010).
Table 2 | Parameters of the catastrophe model.

| Parameter | Value | Unit |
|-----------|-------|------|
| **GATING PARAMETERS OF NaV, Kv, AND CLC** | | |
| \(E_{\text{omega}}\) | –110 | mV |
| \(A_{\text{omega}}\) | 34 | mV |
| \(g_{\text{NaV}}\) | 268 | mS/cm² |
| \(g_{\text{Kv}}\) | 2.75 | μS/cm² |
| \(g_{\text{DC}}\) | 2.16 | mS/cm² |
| \(g_{\text{IR}}\) | 0.5 | mS/cm² |
| \(g_{\text{IR}}\) | 0.0485 | mS/cm² |
| \(k_{s}\) | 0.0475 | mS/cm² |
| \(k_{i}\) | 5 | mV² |
| \(d\) | 0.2 | – |
| \(V_{p}\) | 8 | Nm mol cm⁻² s⁻¹ |
| \(K_{\text{IM}}\) | 1 | mM |
| \(K_{\text{IRNa}}\) | 8 | mM |
| \(L_{\text{IR}}\) | 1.25 × 10⁻¹⁰ | cm⁻² N⁻¹ s⁻¹ |
| **EXTRA AND INITIAL INTRACELLULAR CONCENTRATIONS** | | |
| \(c_{\text{Na}^{+}}\) | 141.5 | mM |
| \(c_{\text{K}^{+}}\) | 25.8 | mM |
| \(c_{\text{K}\text{Neutral}}\) | 10 | mM |
| \(c_{\text{K}^{+}}\) | 15.6 | mM |
| \(c_{\text{Na}^{+}}\) | 132.3 | mM |
| \(c_{\text{Na}^{+}}\) | 8.9 | mM |
| \(c_{\text{Cl}^{-}}\) | 4.3 | mM |
| \(c_{\text{Cl}^{-}}\) | 124.1 | mM |
| \(E_{\text{K}^{+}}\) | –18.5 | mV |
| \(V_{i}\) | 3.38 | μV |
| \(\delta_{\text{H}_2\text{O}}\) | 555.55 | mM |
| **PARAMETERS FOR ION AND WATER FLUXES** | | |
| \(a_{\text{m}}\) | 0.288 | ms⁻¹ |
| \(\beta_{\text{m}}\) | 1.38 | ms⁻¹ |
| \(E_{\text{m}}\) | –42 | mV |
| \(K_{\text{m}}\) | 10 | mV |
| \(K_{\beta m}\) | 18 | mV |
| \(a_{\text{f}}\) | 0.0081 | ms⁻¹ |
| \(\beta_{\text{f}}\) | 4.38 | ms⁻¹ |
| \(E_{\text{f}}\) | –45 | mV |
| \(K_{\text{un}}\) | 14.7 | mV |
| \(K_{\beta n}\) | 9 | mV |
| \(E_{\text{un}}\) | –85 | mV |
| \(A_{\text{f}}\) | 6 | mV |
| \(a_{\text{f}}\) | 0.0131 | ms⁻¹ |
| \(\beta_{\text{f}}\) | 0.067 | ms⁻¹ |
| \(E_{\text{f}}\) | –37 | mV |
| \(K_{\text{n}}\) | 7 | mV |
| \(K_{\beta n}\) | 40 | mV |
| \(E_{\text{n}}\) | –30 | mV |
| \(K_{\text{NK}}\) | 25.75 | mV |
| \(A_{\text{n}}\) | 75 | mV |
| \(E_{\text{a}}\) | 70 | mV |
| \(A_{\text{a}}\) | 150 | mV |

(Continued)

| Parameter | Value | Unit |
|-----------|-------|------|
| **PHYSICAL AND STRUCTURAL PARAMETERS** | | |
| \(D_{\text{l}}\) | 70 | μm |
| \(\eta\) | 2 | – |
| \(\sigma_{\text{m}}\) | 1 | μF/cm² |
| \(z_{\text{Fix}}\) | –1.3 | – |
| \(R\) | 8.3145 | J mol⁻¹ K⁻¹ |
| \(T\) | 311.15 | K |
| \(F\) | 96485 | C/mol |

et al., 2001) and underlies barium-induced augmentation of paradoxical depolarization of skeletal muscle fibers in low external \(K^+\) (\(K_{\text{IR}} 2.1\); Struyk and Cannon, 2008). Decreased conductance of the ATP-sensitive K channel in skeletal muscle may also be a causative factor in hypokalemic-induced depolarization, at least in response to insulin (Tricarico et al., 1998). It has been proposed that part of the therapeutic effect of acetazolamide in HypoPP is its action to promote the activation of several different types of skeletal muscle potassium channels, which may offset the decreased conductance of \(K_{\text{IR}}\) (for review see Matthews and Hanna, 2010).

If the omega pore conductance is >18 μS/cm² (for the conditions in Figure 4C), the bi-stability is replaced by a single stable resting potential. The value depends on the conductance ratio \(g_{K}/g_{\omega}\) with \(g_{K}\) carried by additional (e.g., delayed rectifying) \(K_{v}\) channels which are less dependent on extracellular \(K^+\) than are \(K_{\text{IR}}\) channels. In this monostable system, the membrane potential can vary between –74 and –58 mV (Figure 4C).

Usually the majority of normal cells do not become inexcitable in response to decreased serum \(K^+\), because the limit points are located at very low \(K^+\) that do not occur physiologically. However in the presence of an omega current, the limit points are shifted to higher \(K^+\), and transitions between the states are possible under physiological conditions. HypoPP seems to be caused by such a shift. For instance, computer simulation of the effect of R669H on \(V_{\text{rest}}\) in response to low external \(K^+\) predicts a decrease in the threshold for paradoxical depolarization of muscle fibers, similar to that observed experimentally with barium poisoning (Struyk and Cannon, 2008). Cation ionophores like amphotericin B and gramicidin can mimic the omega pore current and serve as a successful, pharmacological in vitro model for HypoPP (Jurkat-Rott et al., 2009). Based on the ionophore experiments, the fraction of fibers in the P2-state may correspond to the chronic weakness in HypoPP patients. Typical triggers such as glucose and insulin causing hypokalemia will further increase this fraction and precipitate a paralytic attack. The pharmacological computer model predicts that smaller omega currents require a more severe hypokalemia of the patients to shift cells into the P2-state than larger omega currents.

**SODIUM OVERLOAD, CYTOTOXIC EDEMA, AND TISSUE DEGENERATION**

By tackling the question as to whether sodium influx (e.g., through omega pores) increases the cytoplasmic sodium concentration, a \(^{23}\)Na MR sequence was developed (Nielles-Vallespin et al., 2007).
that indeed revealed a muscle sodium overload in HypoPP patients (Figure 5). In addition, 1H-MR images (MRI) with a short-tau inversion recovery (STIR) sequence displayed an edema in the muscles of these HypoPP patients (Figures 5A–F). Therefore the question arose as to whether the edema was caused by a cytoplasmic sodium accumulation and osmotic imbalance, or by an interstitial edema, e.g., by an inflammation. To answer this question the MRI technique was further improved to a 23Na MRI inversion recovery sequence (Na-IR) which partially suppresses the signal raised by free sodium in the extracellular fluid and thus mainly represents cytoplasmic sodium (Nagel et al., 2011). In the HypoPP patients the nature of the edema was cytoplasmic. It seemed to be cytotoxic as all patients who showed the edema presented with a chronic weakness and muscle degeneration with age (Figures 5G–I).

In parallel with the concept of degeneration caused by sodium overload, ictal cytotoxic edema during the long-lasting depolarization (spreading depression) has been frequently reported in FHM (for example Chabriat et al., 2000; Butteriss et al., 2003) and has been suggested to sustain the long-lasting aura (Iizuka et al., 2006) and contribute to neurodegeneration (Carreño et al., 2011). Likewise, ictal edema is associated with neuronal degeneration and sclerosis of the hippocampus in FSs (Scott et al., 2003, 2006; Sokol et al., 2003). Therefore, it is possible that intracellular sodium overload may contribute to neuronal as well as muscle channelopathies.

**REPOLARIZATION AND RELIEF OF THE CYTOTOXIC EDEMA**

Guided by the experience that acetazolamide has favorable effects on the episodic weakness in the periodic paralyses (Resnick et al., 1968), this agent was administered to HypoPP patients and reduced the chronic weakness of the patients as well as the sodium overload and edema in the MRI (Figure 5). In the pharmacological in vitro model of HypoPP using an ionophore, acetazolamide shifted many fibers from the P2- to the P1-state. This in vitro effect was considered to be responsible for the positive, in vivo effects (Jurkat-Rott et al., 2009). Thus, drugs that repolarize the fiber membrane may prevent progression of the cell degeneration by reducing the cytotoxic edema. Supporting the idea that FHM and epilepsy share similar pathomechanisms to HypoPP, it is not surprising that acetazolamide is standard treatment option for both epilepsy (Wolf, 2011) and FHM (Russell and Ducros, 2011).
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APPENDIX
PATHOGENESIS MODEL – CATASTROPHE ON THE CUSP

Using catastrophe theory, the effects of an omega current were simulated in a one-compartment computer model of skeletal muscle fibers. Both sizes of ion concentrations and consecutive water shifts were considered. The size of the T-tubular system was accounted for by a specific factor. It was not considered a separate compartment since the low-resistance T-tubular openings justified the assumption of an equilibrium. Parameters of the catastrophe model are given in Table 2; notations and abbreviations at the end of the Appendix.

The membrane was equipped with the following conductances: a background Na⁺ leak conductance (g_{NaL}), the omega pore conductance (g_{om}), a voltage-gated Na⁺ (g_{Nav}) and K⁺ (g_{Kv}) conductance, an inward-rectifying K⁺ (g_{IR}) and a voltage-dependent Cl⁻ (g_{Cl}) conductance, a hydraulic conductivity (L_{H}), and a Na⁺/K⁺ pump flux (J_{p}). The model was based on the charge-difference approach (3) in which the membrane potential E is calculated from the amount of charges in the intracellular compartment $Q_i$ and the membrane area $A_m$:

$$E = \frac{Q_i}{\epsilon_m \cdot A_m} \text{ with } A_m = 4 \cdot \eta \cdot \frac{V_i}{D_f}$$

$Q_i = F \cdot \sum_{\text{ion}} n_{\text{ion}} \cdot z_{\text{ion}} \text{ ion} \in \{\text{Na}, \text{K}, \text{Cl}, \text{Fix}, S\}$

$V_i$ was the cell volume, $D_f$ the fiber diameter and $\eta$ a factor correcting the size of the T-tubular membrane. The cell was only permeable for Na, K, Cl, and H₂O. Fix are intracellular anions (e.g., proteins, phosphates), which – in this model – cannot pass through the membrane. Their overall charge valence $z_{\text{Fix}}$ is set to $-1.3$. This was necessary to avoid very negative membrane potentials at low potassium concentrations. S are the positive charged ions, that block inward-rectifying K⁺ channels from inside upon depolarization. Its valence $z_S$ is set to $+2$, so they represent Mg²⁺. Multiple positively charged polyamines that increase the strength of rectification were not considered.

The amounts of ions and water in the cell $n$ are state variables in this model. They are integrated over time by numerically solving the differential equations that describe their fluxes $J$:

$$n_i = \dot{n}_i + \int_{0}^{t} J_i \cdot dt \ s \in \{\text{Na}, \text{K}, \text{Cl}, \text{H}_2\text{O}\}$$

$$J_i = \frac{d n_i}{d t} = \sum_{c} J^c_i + \sum_{p} J^p_i \ c \in \{\text{Nav}, \text{Kv}, \text{K}_{ir}, \text{ClC}, \text{Aqua}\} \ p \in \{\text{Na/K - pump}\}$$

The fluxes of ions through channels $J^c_i$ and water through an aquaporin $J^\text{Aqua}_{H_2O}$ (modeled by a simple hydraulic conductivity) are computed by the following equations:

$$J^c_i = -F^{-1} \cdot g^c_{\text{ion}} \cdot (E - E_{ion}) \ c \in \{\text{Na}^+, \text{K}^+, \text{Cl}^-\}$$

$$J^\text{Aqua}_{H_2O} = L_{H} \cdot \dot{H}_{H_2O} \cdot \Delta \Pi$$

The driving forces for the fluxes were the electrochemical gradients $(E - E_{ion})$ for ions or the osmotic pressure difference $\Delta \Pi$ for water:

$$E_{ion} = \frac{R \cdot T}{z_{ion} \cdot F} \cdot \ln \left( \frac{c_{ion}^i}{c_{ion}^o} \right)$$

$$\Delta \Pi = R \cdot T \cdot \sum_{\text{sol}} (c_{sol}^i - c_{sol}^o) \ sol \in \{\text{Na, K, Cl, Fix, S}\}$$

The Na/K pump was modeled by

$$J_p = J_p \cdot \left(1 + K_{mK} / c_{K}^{K^+}\right)^{-2} \cdot \left(1 + K_{mNa} / c_{i}^{Na}\right)^{-3}$$

$J_{pNa} = -3 \cdot J_p$ and $J_{pK} = 2 \cdot J_p$
The parameters $K_{mK}$ and $K_{mNa}$ were taken from Wallinga et al. (1999). The maximum pump flux $\dot{J}_p$ was chosen to get an intracellular $Na^+$ concentration $c_{iNa}^+$ of 15 mM at control conditions. Intracellular ion concentrations were calculated from the cell volume $V_i$ and the amount of ions:

$$V_i = \sum_{s} \frac{n_s}{\Omega_{H_2O}}, \ s \in \{Na, K, Cl, Fix, H_2O\}$$

$$c_{i\text{ion}} = \frac{n_{i\text{ion}}}{V_i}, \ i\text{on} \in \{Na, K, Cl, Fix\}$$

The voltage-gated $Na^+$ ($NaV$), $K^+$ ($K_V$), and $Cl^-$ (ClC1) conductances were based on the Hodgkin–Huxley type formalism; identifiers had their classical meaning. The equations taken from Wallinga et al. (1999) are given here for completeness:

$$g_{Na}^+ = \hat{g}_{Na}^+ \cdot \beta_m^3 \cdot h \cdot S, \ g_{K}^+ = \hat{g}_{K}^+ \cdot n^4 \cdot hK$$

The gating variables $m$, $h$, $S$ ($NaV$ slow inactivation), $n$, and $hK$ (inactivation of $K_V$) were state variables and defined by the following differential equations:

$$\frac{dy}{dt} = \alpha_y \cdot (1 - y) - \beta_y \cdot y, \ y \in \{m, n, h\}$$

$$\alpha_m = \hat{\alpha}_m \cdot \left( E - \hat{E}_m \right) / \kappa_{alpha}$$

$$\beta_m = \frac{\hat{\beta}_m \cdot e^{-\left( E - \hat{E}_m \right) / \kappa_{beta}}}{1 + e^{-\left( E - \hat{E}_m \right) / \kappa_{beta}}}$$

$$\alpha_n = \hat{\alpha}_n \cdot \left( E - \hat{E}_n \right) / \kappa_{alpha}$$

$$\beta_n = \frac{\hat{\beta}_n \cdot e^{-\left( E - \hat{E}_n \right) / \kappa_{beta}}}{1 + e^{-\left( E - \hat{E}_n \right) / \kappa_{beta}}}$$

$$\frac{dS}{dt} = \frac{S_\infty - S}{\tau_S}, \ \tau_S = \frac{60}{0.2 + 5.65 \cdot \left( (E + 90) / 100 \right)} \text{ and } S_\infty = \frac{1}{1 + e^{(E - \hat{E}_S) / \kappa_S}}$$

$$\frac{dhK}{dt} = \frac{hK_\infty - hK}{\tau_{hK}}, \ \tau_{hK} = e^{-\left( E - \hat{E}_{hK} \right) / \kappa_{hK}} \text{ and } hK_\infty = \frac{1}{1 + e^{\left( E - \hat{E}_{hK} \right) / \kappa_{hK}}}$$

The gating variable of ClC1 was assumed to reach the steady-state instantaneously:

$$a = \frac{1}{1 + e^{(E - \hat{E}_a) / \kappa_a}}$$

For the inward-rectifying potassium channels the same model as in Wallinga et al. (1999) was used, parameters were chosen to get appropriate values for the limit points at control conditions and a resting conductivity at $c_e^{K^+} = 3.5$ mM of 41 $\mu$S/cm$^2$. The equations were:

$$\xi_{IR}^K = \xi'_{IR} \cdot y, \ \xi'_{IR} = \frac{\hat{\xi}_{IR} \cdot \left( \xi_{IR} \right)^2}{K_{IR}^K + \left( \xi_{IR} \right)^2}, \ \xi_{IR}^K = \xi_e^{K^+} \cdot e^{-\delta E_{K^+} F / RT}$$
The constant background sodium leak conductance was then adapted to reach a K$^+$ to Na$^+$ permeability ratio between 0.01 and 0.02 and a membrane potential of approximately –86 mV (at c$^K_\infty$ = 3.5 mM).

For modeling the H$^+$ leak conductance, it was assumed – based on the $^{31}$P MR spectroscopy measurements (Jurkat-Rott et al., 2009) – that the H$^+$ equilibrium potential was constant and further, that every H$^+$ was exchanged by one Na$^+$ ion, presumably by a Na$^+$/H$^+$ exchanger. Thus the omega current was treated as a sodium current (indirectly) driven by the electrochemical gradient for protons. Its conductance was modeled as a pore with a voltage-dependent open probability that follows a Boltzmann distribution. The equation

$$g_{\text{omega}} = \hat{g}_{\text{omega}} \cdot \left(1 + e^{\frac{E - E_{\text{leak}}}{A_{\text{leak}}}}\right)^{-1}$$

was fitted to the HypoPP muscle fiber results. The Na$^+$ flux (indirectly) mediated by the omega pore was calculated by

$$j_{\text{Na}^+} = -F^{-1} \cdot g_{\text{omega}} \cdot (E - E_{\text{H}^+}) \text{ with } E_{\text{H}^+} = \frac{R \cdot T \cdot \ln(10pH_{\text{i}}/10pH_{\text{e}})}{F}$$

The model was implemented in MatLab Version 7.3 (The Mathworks, Inc.). Initial-value problems were solved with ODE15s, a solver for sets of stiff ordinary differential equations. Then bifurcation analysis was done by using the continuation routines of the toolbox CL_MATCONT Version 2.4.

**NOTATIONS AND ABBREVIATIONS**

**Indices**

| Symbol | Description |
|--------|-------------|
| Aqua   | water channel |
| c      | channel like voltage-gated Na$^+$ channel, voltage-gated K$^+$ channel |
| ClC1   | voltage-dependent Cl$^-$ channel |
| e      | extracellular |
| f      | fiber |
| i      | intracellular |
| ion    | Ion: Na$^+$, K$^+$, Cl$^-$ |
| IR     | inwardly rectifying K$^+$ channel |
| Kv     | voltage-gated K$^+$ channel |
| Omega  | omega pore conductance |
| NaL    | background Na$^+$ channels |
| NaV    | voltage-gated Na$^+$ channel |
| p      | Na$^+$/K$^+$-pump |
| s      | substance: sodium, potassium, chloride, fixed anion, water |
| $\infty$ | steady-state |

**Identifiers**

| Symbol | Description |
|--------|-------------|
| a      | gating variable of the Cl$^-$ channel |
| $A_m$  | membrane area |
| c      | concentration |
| Cl$^-$ | chloride ion |
| $c_m$  | specific membrane capacity |
| Symbol | Description |
|--------|-------------|
| $D_t$  | fiber diameter |
| $\delta$ | electrical distance from outside where binding site for $K^+$ and $S^{2+}$ is localized in $K_r$ |
| $E$ | membrane potential |
| $E_{ion}$ | equilibrium potential (Nernst) |
| $F$ | Faraday constant |
| $F_{ix}$ | intracellular fixed anions (e.g., proteinates, phosphates) |
| $g$ | conductance |
| $H^+$ | protons |
| $\eta$ | scaling factor relating the size of T-tubular membrane to sarcolemma |
| $J$ | flux |
| $K^+$ | potassium ion |
| $K_{mK}$ | sensitivity of the $Na^+/K^+$-pump for extracellular potassium |
| $K_{mNa}$ | sensitivity of the $Na^+/K^+$-pump for intracellular sodium |
| $K_K$ | dissociation constant of $K^+$ on $K_r$ channels |
| $K_S$ | dissociation constant of $S^{2+}$ on $K_r$ channels |
| $L_H$ | hydraulic conductivity |
| $m, h, S$ | gating variables of the voltage-gated $Na^+$ channel (activation, fast, slow inactivation) |
| $n, h_K$ | gating variables of the voltage-gated $K^+$ channel (activation, inactivation) |
| $n$ | amount of substance |
| $Na^+$ | sodium ion |
| $\Pi$ | osmotic pressure |
| $Q$ | charge |
| $R$ | gas constant |
| $S^{2+}$ | intracellular fixed cation (cytoplasmic blocker of $K_r$ channels) |
| $T$ | absolute temperature |
| $t$ | time |
| $V_i$ | cell volume |