Raising Dielectric Permittivity Mitigates Dopant-Induced Disorder in Conjugated Polymers

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Conjugated polymers need to be doped to increase charge carrier density and reach the electrical conductivity necessary for electronic and energy applications. While doping increases carrier density, Coulomb interactions between the dopant molecules and the localized carriers are poorly screened, causing broadening and a heavy tail in the electronic density-of-states (DOS). The authors examine the effects of dopant-induced disorder on two complimentary charge transport properties of semiconducting polymers, the Seebeck coefficient and electrical conductivity, and demonstrate a way to mitigate them. Their simulations, based on a modified Gaussian disorder model with Miller-Abraham hopping rates, show that dopant-induced broadening of the DOS negatively impacts the Seebeck coefficient versus electrical conductivity trade-off curve. Increasing the dielectric permittivity of the polymer mitigates dopant-carrier Coulomb interactions and improves charge transport, evidenced by simultaneous increases in conductivity and the Seebeck coefficient. They verified this increase experimentally in iodine-doped P3HT and P3HT blended with barium titanate (BaTiO₃) nanoparticles. The addition of 2% w/w BaTiO₃ nanoparticles increased conductivity and Seebeck across a broad range of doping, resulting in a fourfold increase in power factor. Thus, these results show a promising path forward to reduce the dopant-charge carrier Coulomb interactions and mitigate their adverse impact on charge transport.

1. Introduction

Organic electronics have attracted intense research attention as they are environmentally friendly and solution-processable, which makes them cost-efficient. They are also lightweight and flexible, which allows for facile integration for wearables, medical monitoring, and internet-of-things electronics.[1] Conjugated polymers are poor electronic conductors for two principal reasons: their morphology has a significant disorder and they do not have intrinsic free charge carriers. Therefore, conjugated polymers need to be doped, that is, oxidized or reduced, to increase the density of free carriers. These free carriers in the oxidized or reduced polymer impart electronic and optoelectronic properties of conjugated polymers that form the basis of organic electronics. The simple process of doping introduces complexities in the electronic structure because of the charge–charge Coulomb interactions between the dopant and the polymer. This long-range interaction is much more pronounced in polymers than in inorganic semiconductors because of their low dielectric permittivity (<3).[2] Inadequate screening of the dopant-polymer interactions increases energetic disorder as it increases the width and alters the shape of the distribution of density of states (DOS).[3–5] These factors suppress the density of free charge carriers by electrostatically binding the charge carriers to their conjugate dopant counterions, making doping less efficient. They also create deep traps, which adversely affect charge transport and thus the electronic and optoelectronic properties of the polymer.

The intrinsic DOS, which denotes the number of available states in a given energy range, typically follows a Gaussian
distribution \( g(E) \propto \exp(-E^2/2\Gamma^2_E) \), as prescribed in the Gaussian disorder model (GDM). The width of DOS (\( \Gamma_E \)) is the “energetic disorder” arising from structural and morphological randomness.\(^{[7,8]}\) When ionized dopants interact with carriers through long-range Coulomb forces, it increases \( \Gamma_E \) and introduces a heavy tail in the DOS,\(^{[4]}\) which is particularly pronounced when dopants cluster together.\(^{[3]}\) A direct consequence of the changes in DOS is seen in the two principal measures of charge transport: conductivity (\( \sigma \)) and Seebeck coefficient (\( \alpha \)), which is a measure of the open-circuit voltage produced by a temperature gradient and is related to the average energy transported by each carrier. There is a dramatic flattening in the shape and a downward-left shift of the entire \( \alpha-\sigma \) curve.\(^{[3]}\) This directly impacts the electronic and optoelectronic properties of the polymer. For example, in thermoelectric materials a flattened \( \alpha-\sigma \) curve limits the maximum power factor and thus the thermoelectric conversion efficiency.\(^{[5]}\) In organic photovoltaics, energetic disorder limits the maximum power factor and thus the thermoelectric performance of organic electronic materials.\(^{[6]}\) 

Our simulations, which are based on the GDM, capture the impact of dopants to extract the effective energetic disorder from each DOS curve. Energetic disorder is the standard deviation of the DOS \( g(E) \): \( \Gamma_E^2 = \int E^2 g(E) dE / \int g(E) dE \), which can be determined regardless of the shape of the DOS. The additional energetic disorder is caused by doping as it closely follows the Coulomb interaction energy with the nearest dopant (Figure 1c). Here \( N_2 = N_1 \) for all cases. Raising the dielectric permittivity lowered this additional dopant-induced energetic disorder even at high doping concentrations, nearly restoring the intrinsic Gaussian DOS.

To capture the impact of doping and dielectric constant on the shape of the DOS, we liken it to a generalized Gaussian distribution (GGD), a parametric classification of symmetric distributions given by\(^{[12]}\)

\[
G(E) = \frac{p A (p, \Gamma_E)}{2 \Gamma_E^p} \exp\left\{ \left[ \frac{E}{\Gamma_E} \right]^p \right\}
\]

where \( A(p) = \sqrt{\Gamma/\pi} / \Gamma(1/p) \), \( \Gamma \) denotes the gamma function, \( \Gamma_E \) is the standard deviation, and \( p \) is the shape parameter. For a given distribution, \( p \) can be estimated by finding the root of \( M_2 \Gamma^2 = (1 + p) = 0 \) using a secant method, where \( M_2 \) is the rth absolute moment of the GGD.\(^{[12]}\) We find that at low doping the shape parameter \( p \) is \( \approx 2 \), indicating the DOS is more Gaussian and as we increase doping \( p \) decreases indicating that the tail gets heavier, with \( p \) reaching as low as \( 0.8 \) at very high doping values (Figure 1d). However, increasing the dielectric constant shifts the \( p \) values closer to \( 2 \) even at high doping concentrations, keeping the DOS more Gaussian.

Since doping affects both the width (\( \Gamma_E \)) and shape (\( p \)) of the DOS distribution, we studied their individual impact on the \( \alpha \) versus \( \sigma \) curve. First, we used a fixed Gaussian DOS (\( p = 2 \) in Equation (1)), keeping its width \( \Gamma_E \) constant across doping concentrations, and obtained the \( \alpha \) and \( \sigma \) at various carrier densities by moving \( E_\text{F} \) closer to the center. In this case, larger \( \Gamma_E \) shifted the \( \alpha \) versus \( \sigma \) curve down (lower \( \alpha \)) and left (lower \( \sigma \)), with minimal changes to its slope (grey lines in Figure 2a and Figure S2a, Supporting Information). However, if we let the \( \Gamma_E \) increase with doping concentration by extracting it from the DOS (Equation (5)) but keep the shape Gaussian (\( p = 2 \)), the resulting \( \alpha \) versus \( \sigma \) exhibited a much higher slope (\( \alpha \sigma^{-1.25} \)), indicating that the doping-induced \( \Gamma_E \), while detrimental to transport in general, had a net effect of lowering \( \alpha \) at higher doping concentrations. This can be understood from the Mott formula\(^{[13,14]}\)

\[
\sigma(T, E) = \frac{T^{3/2}}{\pi^2} \frac{1}{\gamma} \ln\left[ \sigma(T, E) \right] = \frac{\mu(E)}{E_{\text{F}}} \sim E_{\text{F}} \exp\left\{ \int \frac{E}{\Gamma(E)} dE \right\}
\]

where \( \mu(E) \) is only weakly varying, the second term is small, resulting in \( \alpha \sigma \sim (E_\text{F}/\Gamma_E)^p - 1 \). A broader Gaussian DOS results in a smaller Seebeck coefficient.

### 2. Results and Discussion

#### 2.1. Impact of Dopants on DOS and Transport

We calculated the DOS for doping concentration \( N_2 \) in clusters having size \( C_p \), according to procedure in the Experimental Section and found that doping resulted in a heavy-tailed distribution with a Gaussian core and a wide quasi-exponential tail (Figure 1a). Increasing dopant concentration lifted the long quasi-exponential tail at the expense of the central Gaussian DOS; clustering of dopants further amplified this effect, as seen from the similarity between the DOS curves with cluster size \( C_p = 3 \) at 2% and \( C_p = 1 \) at 20% doping. Here \( C_p \) refers to the number of charges in each cluster while the percentage refers to the portion of simulated sites, on average spaced by 0.6 nm, that are occupied by carriers. Thermoelectric power factors are typically found to peak near 20% doping.\(^{[3]}\) Increasing the effective dielectric permittivity dramatically reduced the Coulomb interactions and minimized the tail (Figure 1b). A more general way to capture the impact of dopants is to extract the effective energetic disorder from each DOS curve. Energetic disorder is the standard deviation of the DOS \( g(E) \): \( \Gamma_E^2 = \int E^2 g(E) dE / \int g(E) dE \), which can be determined regardless of the shape of the DOS. The additional energetic disorder is caused by doping as it closely follows the Coulomb interaction energy with the nearest dopant (Figure 1c).

Here \( N_2 = N_1 \) as \( C_p = 1 \) for all cases. Raising the dielectric permittivity lowered this additional dopant-induced energetic disorder even at high doping concentrations, nearly restoring the intrinsic Gaussian DOS.

To capture the impact of doping and dielectric constant on the shape of the DOS, we liken it to a generalized Gaussian distribution (GGD), a parametric classification of symmetric distributions given by\(^{[12]}\)

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\]
Figure 1. Increasing the dielectric permittivity counteracts the broadening of the DOS. a) The effect of doping and clustering on the DOS distribution with intrinsic Gaussian width of 100 meV. b) Increasing the dielectric constant counters the broadening of the DOS by mitigating the Coulomb carrier-dopant interactions. c) Additional energetic disorder caused by doping as a function of Coulomb energy for the standard ($\epsilon_r = 3$) and elevated dielectric constants. The grey dashed lines are linear fits showing that the amount of energetic disorder closely follows the Coulomb interaction energy. d) Generalized Gaussian shape parameter $p$ versus doping concentration showing that increasing the dielectric constant keeps the shape parameter more Gaussian ($p \approx 2$) even at higher doping concentrations.

Figure 2. Effect of the width ($\Gamma_E$) and shape parameter $p$ of the DOS on the trend of the $\alpha$ versus $\sigma$ curve. a) The $\alpha$ versus $\sigma$ curves for GGD with fixed $\Gamma_E$ (gray lines) and the $\alpha$ versus $\sigma$ curve with $\Gamma_E$ increasing with doping (pink and cyan lines), $p$ is fixed to 2 for all the cases. b) The $\alpha$ versus $\sigma$ curve for a DOS with shape parameter fixed to 0.8, 1.2, 1.6, and 2, and $\Gamma_E$ increasing with doping (black lines). The blue and red lines show the standard case with DOS computed from Equation (5), where $\Gamma_E$ and shape parameter $p$ are both changing for $\Gamma_i$ values of 100 and 200 meV, respectively.

while a value of $p$ closer to 1 produces a flatter $\alpha$ curve. The point $E_F = 0$ where $\alpha$ vanishes coincides with 50% doping. Intrinsic disorder plays a complementary role and dictates an upper bound on the trade-off curve—larger $\Gamma_i$ depresses the $\alpha$ even at low doping and flattens the curve, typically from $\alpha \alpha \sigma^{-1/2.5}$ to $\sigma^{-1/4}$.

Taking the dopant-induced $\Gamma_E$ while fixing the shape parameter to different values, however, produced a significant difference in the $\alpha$ versus $\sigma$ curve, whose slope decreased with $p$ (black lines in Figure 2b and Figure S2b, Supporting Information). The difference is largest at low-to-moderate doping when carriers are predominantly in the tail of the DOS. In the presence of the heavy tail, doping moved $E_F$ closer to the center of the DOS while the transport energy $E_T = \langle E_i \rangle$ initially decreased as the trap-like states in the tail, which do not contribute significantly to transport, are filled first. This results in a lower $\alpha \alpha E_F - E_T$, decreasing the Seebeck along with the conductivity. The $\alpha$ versus $\sigma$ curve with the DOS computed from Equation (5), where both $\Gamma_E$ and $p$ are varying with doping (solid line in
polymers that encounter significant long-range Coulomb inter- 
casements (SEM-EDS). As seen in Figure 3c, a BaTiO$_3$ image 
composites films by drop casting of a solution containing 
rative polymer composite films by drop casting of a solution 
masking nanocrystals do not interfere with crystalline packing and 
aural domains of the polymer. However, we did observe a shift in 
$\alpha$) to counteract the coulombic broadening of the DOS and keep it 
ideal DOS for TE applications would be a sharp narrow Gaussian 
ability with the shape of the DOS as it evolves in the presence 
put material property. Here we have connected the transport pa- 
polymer of interest by simply using a different dielectric additive. 
ntally may be present in the amorphous domain of the polymer. 
other data, we concluded that at and below 2% (wt./wt.), the nano- 
ver the thermoelectric properties and obtain the $\alpha$–$\sigma$ trade-off curve experimentally, we used a dedoping method with 
verse the DOS that arise from modulation doping using field-effect 
rness over existing methods: 1) it avoids any interfacial effects 
are concentrated at high dopant concentrations. To explore the effect of 
composites in comparison to the pristine polymer, indicating a si-
ly made up of lamellar (100) and $\pi$–$\pi$ stacking (020) of P3HT. We 
hydrogen (020) peak at 10% (wt./wt.) SrTiO$_3$–P3HT. This result es-
tidence wide angle X-ray scattering (WAXS) and show the 
WAXS pattern shows the disappearance of the (020) peak at 10% (wt./wt.) SrTiO$_3$–P3HT. This result estab-
the crystalline regions of P3HT. We also evaluated the out-of-plane scattering pattern with grazing-incidence wide angle X-ray scattering (GIWAXS) and show the 
 Diane K. Ming, supporting information, 2013. 
first step forward is by mitigating the dopant-induced disorder. 
production, as shown in Figure 1f, the log–log plot shows an 
almost Gaussian distribution of dopants, exhibit the $\alpha$–$\sigma$ behaviour with $\alpha$ between 2.5 and 4, while polymers that encounter significant long-range Coulomb inter-
t to the shape of the DOS as it evolves in the presence of 
found that nanocrystals that remain a more Gaussian DOS, stemming from a higher $\epsilon$, larger on-site energy, or a more homogenous distribution of dopants, exhibit the $\alpha$–$\sigma$ behaviour with $\alpha$ between 2.5 and 4, while polymers that encounter significant long-range Coulomb inter-
unity dispersion of the nanocrystals across the polymer film. 
We used X-ray scattering to understand the impact of incorpo-
rating polymer morphology. We used peaks associated with lamellar (100) and $\pi$–$\pi$ stacking (020) of P3HT. We observed no significant change in the scattering patterns and 
ake positions of these peaks in P3HT composites containing 0.1% to 2% of SrTiO$_3$ and BaTiO$_3$ nanocrystals. These results indicate that the nanocrystal additives do not interfere with crystal-
we used X-rays scattering to understand the impact of incorpo-
imated long-range Coulomb interactions have $\alpha$ ranging from 6 to 8 (Figure S2c,d, Supporting Information). For films with higher nanocrystal 
recorded, indicating that the path forward is by mitigating the dopant-induced disorder.

2.2. Experimental Validation

We hypothesized that the detrimental effect of dopant-induced disorder on charge transport and the $\alpha$ versus $\sigma$ curve can be mitigated by increasing the dielectric constant, which we have shown to counteract the coulombic broadening of the DOS and keep it nearly Gaussian (Figure 1). To test our hypothesis, we studied the impact of dielectric constant on the thermoelectric properties of P3HT, a well-studied conjugated polymer for thermoelectric applications. The dielectric constant of a polymer can be changed by two methods: 1) without altering the chemical structure of the polymer by blending the polymer with additives (or “fillers”) or 2) by altering the chemical structure of the polymer by appending polar groups to the side chains\(^{17,18}\) or the backbone\(^{18-20}\) For our study, we chose to prepare composites of conjugated polymers with colloidal nanocrystals of dielectric perovskite oxides with different dielectric constants. This method is straightforward and can be deployed to vary the dielectric constant of the conjugated polymer of interest by simply using a different dielectric additive.

We synthesized colloidal nanocrystals of TiO$_2$, SrTiO$_3$, and BaTiO$_3$ using established protocols. These nanocrystals were $\approx$10 nm in size and have a narrow size distribution, as characterized with transmission electron microscopy (TEM) and X-ray diffraction. Figure 3b shows a TEM image of BaTiO$_3$ nanocrystals showing almost identical cubic shape and size. The nanocrystals are capped with oleic acid as ligands, which increases the miscibility between the additive and the polymer. We then fabricated polymer composite films by drop casting of a solution of nanocrystals and the polymer. The thicknesses of the composite films are about 4 $\mu$m, as characterized with profilometry. To ensure an adequate dispersion of the nanocrystals within the polymer films, we image the elemental composition of the films with scanning electron microscopy with energy dispersive spectroscopy (SEM-EDS). As seen in Figure 3c, a BaTiO$_3$ image exhibits a uniform distribution of Ti and O signals, indicating an adequate dispersion of the nanocrystals across the polymer film.

We measured the dielectric permittivity of the polymer-nanocrystal composite films with electrochemical impedance spectroscopy (EIS), which obtains the bulk dielectric permittivity...
Figure 3. Fabricating polymer-nanocrystal composites for enhancing thermoelectric performance and its morphological characterization. a) Scheme of components used to fabricate the polymer composites. b) TEM image of BaTiO$_3$ nanocrystals shows consistent size and cubic shape. c) SEM-EDS image shows a uniform distribution of BaTiO$_3$ nanoparticles in the polymer composite film. The signal is weak due to the low concentration and smaller size of the nanoparticles. See also Figure S4c, Supporting Information. d) In-plane X-ray scattering pattern of SrTiO$_3$-P3HT composites with different ratio of SrTiO$_3$ nanocrystals to P3HT. The disappearance of the (020) peak at SrTiO$_3$-P3HT composition ratios of 10% (wt./wt.) delineates a concentration limit for adding nanocrystals without affecting the polymer nanostructure. e) In-plane X-ray scattering pattern of SrTiO$_3$ and BaTiO$_3$ composites shows no change in the signature peaks of P3HT. TiO$_2$ composite shows the formation of polymer morph form II of P3HT. f) Plot of $\alpha$ versus $\sigma$ experimental values of BaTiO$_3$, SrTiO$_3$, and TiO$_2$-P3HT composite and pristine P3HT. SrTiO$_3$ and TiO$_2$ composites showed no change in the $\alpha$ and $\sigma$ interplay in comparison to pristine P3HT. The error horizontal bars represent the error in the electrical conductivity due to the variation in film thicknesses of thick films.

(\epsilon_{\text{bulk}}) of a composite material across a frequency range. As can be seen in the Figure S6, Supporting Information, at 1 kHz, BaTiO$_3$ composites exhibits a significant increase in $\epsilon_{\text{bulk}}$ from 3.5(±0.1) to 84.6(±1.4) when compared to the pristine polymer, whereas SrTiO$_3$ nanocrystals showed a $\epsilon_{\text{bulk}}$ of 14.0(±3.6). This dramatic enhancement arises from the polarization induced by BaTiO$_3$, which is consistent with previous work on similar polymer-nanocrystal composites.[23] The measured $\epsilon_{\text{bulk}}$ value for P3HT matches very well with the value obtained with the numerical simulations' fit.

2.3. Analysis of Experimental Results and the Role of Energetic Disorder

To understand the experimental trends, we fit the experimental data with our simulations and found that the $\alpha$ versus $\sigma$ curve for pristine P3HT can be fit with $\epsilon_r = 3.7$ whereas BaTiO$_3$-P3HT composite with $\epsilon_r = 5$, shown in Figure 4a. This is consistent with our expectation that a higher dielectric permittivity will counteract the effect of dopant-induced Coulomb interactions on the polymer DOS, leading to better charge transport properties. The simultaneous increase in the Seebeck coefficient and conductivity results in a tremendous increase in the thermoelectric power factor (PF), given by $PF = a^2\sigma$, as shown in Figure 4b. With $\epsilon_r=3.7$, we observed a peak PF of 4.8 $\mu$Wm$^{-1}$ K$^{-1}$ in pristine P3HT, which increased to 16.2 $\mu$Wm$^{-1}$ K$^{-1}$ with the addition of BaTiO$_3$. However, we recognize that there is a discrepancy between the measured $\epsilon_{\text{bulk}}$ and the value needed to fit the curve for the BaTiO$_3$ composites. We posit that the value needed to fit the curve may be an effective dielectric permittivity ($\epsilon_{\text{eff}}$) experienced by the electric fields between charge carriers and dopant ions, which depends on their average distance from the nanocrystal. The dopant-induced energetic disorder is primarily caused by the Coulomb interaction with the nearest dopant, whose average distance can be estimated from $N_0^{-1/3}$ to span 1–10 nm in our experiments and calculations and is therefore smaller than the average size of the nanocrystals (10 nm). We surmise that, to increase the dielectric permittivity experienced by the electric field between charge-carriers and dopant ions, we need to use nanocrystals with a higher $\epsilon_r$ or to tailor the ligands on the nanocrystals so that they place closer to the radical cation on the polymer or its counterion. Nonetheless, applying such a strategy could compromise the polymer morphology, which can affect charge transport.

We examine conductivity and Seebeck versus doping in Figure 5a. Increasing $\epsilon_r$ mitigates dopant-induced disorder and produces a more sharply peaked DOS, boosting Seebeck at high
Figure 4. Higher dielectric permittivity leads to a higher power factor in OSCs. a) Plot of simulated $\alpha$ versus $\sigma$ values and experimental values of BaTiO3-P3HT composite and pristine P3HT. BaTiO3-P3HT composite shows a fit to $\epsilon_r = 5$ while pristine P3HT fits $\epsilon_r = 3.7$. The simulations were iterated 25 times; the solid lines represent averaged values and the shaded region represents the minimum and maximum values. The horizontal error bars represent the error in the experimental electrical conductivity due to the variation in film thicknesses. b) Power factor as a function of carrier density. There is an approximately fourfold increase in power factor from 4.8 to 16.2 as $\epsilon_r$ is increased.

Figure 5. Power factor enhancement and the role of energetic disorder. a) $\alpha$ and $\sigma$ as a function of carrier density showing the respective increase with increasing $\epsilon$ at medium to high doping concentrations. b) Power factor versus energetic disorder showing that increasing the dielectric constant reduces the energetic disorder at all doping concentrations and leads to higher power factor. c) Maximum power factor and the energetic disorder versus $\epsilon_r$, showing that gains in the power factor saturate beyond $\epsilon_r > 12$, when they are limited by intrinsic disorder. d) Conductivity $\sigma$ and shape parameter $p$ as a function of $\epsilon_r$, plotted at the doping concentration corresponding to maximum power factor, showing increasing conductivity with decreasing intrinsic disorder, particularly when low intrinsic disorder and small $p$ value produce a narrow main DOS with a heavy tail.

doping due to the increased separation between the transport energy and the Fermi level (Figure S7a, Supporting Information). The impact of dielectric screening on conductivity is even more dramatic—carriers in a heavy-tailed DOS get “stuck” in the trap-like states deep in the tail. Transport improves at higher doping concentrations when the tail states are filled, discerned by the steeper conductivity curves in Figure 5a. Conductivity increases super-linearly with doping$^{[24]}$, following a power-law$^{[25]}$ trend $\sigma \propto N_f^\zeta$, with the average exponent related to disorder $\zeta \propto \Gamma_E$ (see Figure S7b, Supporting Information). A narrower DOS reduces the difference $\Delta E_{ij}$ between energies of neighboring sites, which increases the probability of favorable hopping pathways by alleviating the required thermal assistance by absorption of phonons, resulting in a much higher conductivity for the higher $\epsilon_r$ case. While both Seebeck and conductivity depend on the complex interplay between doping and energetic disorder,
the peaks in the PF exhibit an inverse trend with energetic disorder, shown in Figure 5b. Increasing the $e_\text{f}$ from 3 to 12 mitigates dopant-induced energetic disorder, pushing the curves to lower $\Gamma_\text{T}$ while increasing the height of the peak in the PF. Doping is more effective at higher $e_\text{f}$ as carriers contribute more readily to transport in the absence of the deep coulombic tail. Consequently, we achieve higher power factors at lower doping concentrations (Figure S8, Supporting Information). While there is a modest increase in Seebeck with higher $e_\text{f}$ at a fixed doping concentration, reaching the peak PF requires less doping, which effectively raises the Seebeck at the peak (Figure S9a, Supporting Information). We note that a recent paper observed a quadratic relationship between power factor and dielectric constant in crystalline inorganic thermoelectrics.[26]

However, the maximum attainable PF saturates for $e_\text{f}>12$. Beyond this value, the polymer’s intrinsic energetic disorder acts as a limiting factor in the highest attainable PF. Dielectric screening can only mitigate the broadening of the DOS by carrier-dopant Coulomb interactions but not the intrinsic disorder within the polymer, which is related to structural disorder and depends on the polymer’s morphology.[27] In Figure 5c, we plot the peak PF reached2170 were observed (Figure S9b, Supporting Information) and the PF parameters in the simulation to values within the range encountered mitigates dopant-induced energetic disorder, pushing the curves to a RT $zT$ of 3.2. However, increasing the effective dielectric constant in organic semiconductors is a fertile new avenue of research in organic TEs and a path forward to obtain $zT$ values well over the highest reported 0.4 so far.[29] Beyond improving TE performance, we note that most of the improvement we observed in the PF comes from increases in the conductivity, particularly at low to medium doping concentrations, which is broadly useful in organic electronics. Long-range Coulomb interactions also impact other systems such as photogenerated carriers in organic photovoltaics. Raising the dielectric permittivity of the active layer could increase exciton dissociation, enhancing photovoltaic performance, and improve carrier mobility in field effect transistors.

3. Conclusion

We conclude that increasing dielectric screening can mitigate dopant-induced traps and have a positive impact on the transport properties of doped polymers with an intrinsically low $e_\text{f}$. At the same time, we develop an experimental framework that can alter the permittivity of the material without affecting its intrinsic properties, BaTiO$_3$-induced dielectric screening can decrease Coulomb interactions and thus the magnitude of the heavy-tailed DOS. This synergetic computational and experimental study opens avenues towards developing more effective strategies to use dielectric screening for mitigating the effect of dopants in the DOS. Our results indicate that polymers with high dielectric permittivity are a fertile new avenue of research in organic electronics. A path forward to obtain $zT$ values well over the highest reported 0.4 so far.[29] Beyond improving TE performance, we note that most of the improvement we observed in the PF comes from increases in the conductivity, particularly at low to medium doping concentrations, which is broadly useful in organic electronics. Long-range Coulomb interactions also impact other systems such as photogenerated carriers in organic photovoltaics. Raising the dielectric permittivity of the active layer could increase exciton dissociation, enhancing photovoltaic performance, and improve carrier mobility in field effect transistors.

4. Experimental Section

Hopping Transport Simulation: We compute the average-occupation probabilities of the sites using a non-linear iterative solver and the initial site occupation probability is given by the Fermi–Dirac distribution. In steady-state, $\frac{dS_i}{dt} = \sum_j [W_{ij}(1-p_j) - W_{ji}(1-p_i)]$, where $p_i$ is the occupation probability of a site $i$ and $W_{ij}$ is the hopping transition rate, and the whole term is summed over the neighbor sites $j$.[31] The current density $j$ is found by a summation over all the carriers in the direction of the applied field, $j = \frac{1}{e} \sum_{i,j} W_{ij}(1-p_i) R_{ij}$ and the Seebeck coefficient is calculated as $S = \frac{j}{T E}$ where $E$ is the average transport energy, calculated from $E_i = (E_i) = \sum_j W_{ij}(1−p_j) R_{ij}$.[32] We simulate a 35 × 35 × 50 lattice of sites with an average distance between adjacent sites $a = 0.6$ nm, and consider up to the fifth-nearest neighbor.

Solving the Non-linear PME: We solve the non-linear PME using a standard iterative non-linear solver. First, we cast the PME as zero-finding for some cases. Hence, we follow a fixed-point iteration for the unknown $p_i$.

We arrange the 35 × 35 × 50 × 35 × 50 array of $\Delta \rho$ in a column vector $p$ and compute the Jacobian matrix of derivatives of $F_i$ with respect to $p_i$ as $J_i = df_i/dp_i = -W_i(1-p_i)$. Then we apply the Levenberg–Marquardt algorithm,[33] as implemented in MATLAB’s fsolve function, with the known Jacobian matrix, which requires a linear solve at each iteration but
typically converges in a few iterations due to its high rate of convergence. The linear solver is a preconditioned conjugate gradients algorithm with a banded preconditioner based on an incomplete Cholesky factorization.

Density-of-States Model Including Carrier-Dopant Electrostatic Interactions: Arkhipov et al. have shown that Coulomb interactions between carriers and ionized dopants result in a heavy-tailed DOS given by \( g(E) = \frac{4\pi N_d q^2}{(4\pi\varepsilon_0)^3} \int_0^\infty \frac{dE}{E^4} \exp\left(\frac{4\pi N_d q^2}{3(4\pi\varepsilon_0)^3 E^3}\right) g(E - E_c) \), where \( N_d \) is the dopant concentration, \( E_c \) is the potential energy of the Coulomb interaction, and \( g \) is the intrinsic Gaussian DOS centered at 0 energy and given by \( g(E) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{E^2}{2}\right) \) where \( E \) is the intrinsic concentration. However, \( r < a \) the presence of dopant clustering, the probability density \( w(r) \) of the minimum distance at which the nearest dopant cluster is present is given by a Poisson distribution \( w(r) = 4\pi r^2 N_c \exp(-4\pi N_c r^2) \), where \( N_c = N_c/C_e \) is the density of clusters and \( C_e \) is the number of dopants in each cluster. The potential energy of the Coulomb interaction between the localized carrier and dopant cluster is now \( E_c(r) = -C_0 q^2/(4\pi\varepsilon_0 r) \). Combining these equations to obtain the energy distribution of localized states over the intrinsic distribution \( g \) and energy \( E \) we have:\(^{[4,5]}\)

\[
g(E) = \frac{4\pi N_d N_c^3}{(4\pi\varepsilon_0)^3} \int_0^\infty \frac{dE}{E^4} \exp\left(\frac{4\pi N_d q^2}{3(4\pi\varepsilon_0)^3 E^3}\right) g(E - E_c) \tag{2}\]

For the contributions arising from energies satisfying \( E_c > \Gamma \), which correspond to instances where carriers are close to the ionized dopants, the integral in Equation (2) can be further simplified. This condition is primarily satisfied by states in the heavy tail of the DOS, representing deep traps. The intrinsic DOS can then be approximated by a delta function \( g(E - E_c) \approx N_c \delta(E - E_c) \) so that the whole integral can be evaluated analytically.

\[
g_{\text{tail}}(E) = \frac{4\pi N_c^3}{(4\pi\varepsilon_0 E_c^4)} \int_0^\infty \frac{dE}{E^4} \exp\left(\frac{4\pi N_d q^2}{3(4\pi\varepsilon_0)^3 E^3}\right) g(E - E_c) \tag{3}\]

where the pre-factor groups together all the constants into:

\[
E_{\text{Coulomb}} = \frac{q^2 C_e}{4\pi\varepsilon_0 N_c} \tag{4}\]

which is the average Coulomb energy of interaction between two dopants. This heavy tail of the DOS exhibits a combination of exponential and power-law dependence on energy, departing from the intrinsic Gaussian shape. The \( E^4 \) term in the denominator of the DOS gives the tail a polynomial shape when doping is low and the exponential term is close to 1.

However, the model in Equation (2) produces a tail with very deep traps because it allows \( E_c(r) \) to diverge to \(-\infty\) as \( r \to 0 \), equivalent to treating dopants as point charges. Such infinitely deep traps have a dramatic impact on conductivity which has been noted in the literature\(^{[4,34]}\), and solved by limiting the most negative value of \( E_c(r) \) to \(-1eV\).\(^{[4]}\) Doing so is equivalent to limiting the distance to the nearest dopant to be no smaller than a dopant radius \( R_d \) obtained by setting \( E_c(R_d) = 0 \) which is the on-site energy of \(-0.5 \text{ to } -1 \text{ eV}\)^{[4]} Doing so is equivalent to limiting the distance to the nearest dopant to be no smaller than a dopant radius \( R_d \) obtained by setting \( E_c(R_d) = 0 \) which is the on-site energy of \(-0.5 \text{ to } -1 \text{ eV}\). More generally, a finite-sized dopant can be modelled by a charge distribution instead of a point charge. For a Gaussian charge distribution, the potential energy becomes \( E_c(r) = -\frac{C_0 q^2}{4\pi\varepsilon_0 r} \exp\left(-\frac{r^2}{R_d^2}\right) \). Then the integral for the DOS must be performed with respect to nearest dopant distance \( r \) rather than energy because \( E_c(r) \) is no longer invertible, resulting in:

\[
g(E) = \frac{4\pi N_c}{\pi} \int_0^\infty r^2 \exp\left(\frac{4\pi N_c q^2}{3(4\pi\varepsilon_0)^3 r^3}\right) g(E - E_c) \, dr \tag{5}\]

This approach is also useful in capturing the finite size of dopant clusters, which can be assigned a radius \( R_d \) instead of being treated as being point charges. Other formulations are possible, such as treating the ionized dopant’s charge distribution as a shell of radius \( R_e \) in which case the Coulomb potential inside \( r < R_e \) becomes constant \( E_c(r) = -\frac{C_0 q^2}{4\pi\varepsilon_0 r} \). Coincidentally, this is also the maximum value reached by the potential from a Gaussian charge distribution.

We have implemented the above and found the Gaussian distribution to produce the smoothest DOS tail, while the choice of dopant size/radius has far more impact on the DOS than how the dopant distribution is modelled. We compute the DOS for a given doping concentration and cluster size by numerical quadrature of Equation (5), after breaking it up into two intervals, \( r < a \) and \( r > a \), and normalizing as described by Zuo et al.\(^{[34]}\) We use \( E_l = 100 \text{ meV} \) and \( E_c = 3.7 \), unless noted otherwise, and \( r = 2 \text{ Å} \) in our simulations which would correspond to on-site energy of \(-1.9 \text{ eV}\). Next, we use the rejection sampling technique to generate an energy distribution that follows from the calculated DOS, and an energy value is randomly assigned to each site from the resulting distribution. We then use the bisection method to iteratively find the corresponding Fermi level \( E_F \) for the given carrier density. The iteration typically converges to sufficient precision within 20 iterations. We iterate the entire simulation at each dopant concentration 25 times, to reduce the sampling error from the randomly assigned site energies.

Polymers: P3HT (MW: 36 kg/mol, regioregularity: 96% HT) was purchased from Rieke Metals. Iodine crystals were purchased from Sigma Aldrich. All solvents were purchased from commercial vendors.

Film Preparation: P3HT was dissolved in chloroform to prepare 10 mg mL\(^{-1}\) solutions by stirring and heating at 45 °C for at least 2 h. 1.1 × 2.2 cm glass slides were hand cut for dielectric measurements, and 1.5 × 1.5 cm ITO-covered glass slides used for dielectric measurements, and 1.5 × 1.5 cm p-doped silicon substrates for SEM-EDS imaging.

All substrates were sonicated with soap/water, water, acetone, and isopropanol for 20 min each and dried in an oven at 130 °C. The substrates were cleaned under ozone (UVO Cleaner, Model 342, Jelight Company, Inc.) for 10 min. All films were prepared by drop casting the solutions in preheated slides at 45 °C. The films were left under vacuum (-10 \text{ to } -2 \text{ mbar}) for at least 24 h to evaporate residual solvents. The thickness of the films (≈4 μm) was measured with a profilometer at three different points across the film.

Strontium Titanate Nanocrystals: Synthesis of strontium titanate nanocrystals was carried out using a hydrothermal method. In a typical synthesis, 1.25 mmol of each of bis(ammonium lactate) titanium dihydroxide (TALH) and strontium hydroxide (Sr(OH)\(_2\)) were dissolved with 30 mL of distilled water in a 45 mL Teflon-lined autoclave. The pH of the solution was then adjusted to 11 with 10 m L \text{ of } 1 M \text{ tetramethylammonium hydroxide (} NM{e}_2OH) \text{ solution followed by the addition of oleic acid (2.5 mmol)} \text{. The reaction vessel was then sealed and heated to } 200 \text{ °C in oven for 24 h. The resulting nanocrystals were collected, washed with ethanol three times, and suspended in non-polar solvents.}

Barium Titanate Nanocrystals: Synthesis of barium titanate colloidal nanocrystals was also carried out by a similar hydrothermal method. In a typical preparation, 1.5 mmol of each TALH and Ba(OH)\(_2\) were dissolved in 24 mL distilled water followed by addition of 6 mL of sodium hydroxide (NaOH, 5 M) \text{. The reaction solution was then transferred} to a 45 mL Teflon-lined autoclave and oleylamine (6 mmol) and oleic acid (6 mmol) were added. The sealed autoclave was placed in custom-made aluminum block housing that was heated to 215 °C and stirred constantly for 24 h using a stirring hotplate. After the synthesis, autoclave was cooled to room temperature and the solid product was collected, washed with ethanol several times, and then dissolved in nonpolar solvents.

Titanium Dioxide Nanocrystals: Synthesis of TiO\(_2\) nanocrystals was carried out by a solvothermal method. In a typical preparation, 1.5 mmol of titanium butoxide were mixed with 7.5 mmol of oleic acid and 7.5 mmol of oleylamine in 1.1 mL of ethanol. The obtained mixture was then transferred to a 45 mL Teflon-lined autoclave containing 5.1 mL of 96% ethanol in water (v/v) and heated to 200 °C for 18 h. After the synthesis, the autoclave was cooled down to room temperature and the solid product was collected, washed with ethanol several times, and then dissolved in nonpolar solvents.
was collected, washed with ethanol several times and resuspended in non-polar solvents to produce colloidal solutions.

**Nanocrystal Characterization:** The solution concentration of nanocrystals was calculated with ICP-OES. The size of the nanocrystals was determined by TEM and powder x-ray diffraction patterns. To prepare the polymer composites, weight ratios of nanocrystal solutions to polymer solutions were used. The solution blends were drop casted by following the same procedure as for the pristine polymer.

**I₂ Doping and Thermoelectric Properties:** The I₂ method was adapted from a previous work.[3,5] The method consisted of transferring 50 mg of I₂ into a 1 mL vial and placing this vial inside a larger glass container with the film inside. The films were doped at 75 °C for 2 h in sealed chamber with 50 mg of I₂. After removing the film from the doping system, the instability of iodine caused the polymer film to dedope over time. Immediately, the polymer film was transferred into a custom-built thermodilectric box to measure the electrical conductivity and the Seebeck coefficient as the doping progressed. This electrically grounded box was equipped with two copper blocks: the temperature of the hot block was maintained with a heating element and the cold block was cooled with a water chiller. To create a temperature gradient, the films were placed on top of an insulating glass slide that was bridged between the two blocks. A PTFE block was used to hold four platinum probes in a four-point probe arrangement and two k-type thermocouples. To measure the electrical conductivity, a Keithley 2400 SA sourcemeter was used to source a bias of −0.1 to 0.1 V and generate an I-V curve. The conductance was calculated with the slope of this curve and normalized with the geometry of the film. A Keithley 2182A nanovoltmeter was used to measure the temperature-induced voltage difference (ΔV), and the thermocouple cables were used to monitor the temperature difference (ΔT) in both sides of the film. The Seebeck coefficient was calculated by the empirical relationship

\[ \alpha = \frac{\Delta V}{\Delta T} \]

**Dielectric Properties:** To measure the dielectric properties, polymer-nanocrystal solutions were dropcast onto an ITO slide. Aluminum electrodes were deposited on the film in an open-circuit correction configuration. The AC frequency was 100 Hz. The dielectric constant was determined by

\[ \varepsilon' = -\frac{d}{2\varepsilon_0 \omega \tan(d/2\varepsilon_0 \varepsilon' \varepsilon_0 \omega t)} \]

and the dielectric loss was determined by

\[ \varepsilon'' = \frac{2}{\tan(d/2 \varepsilon_0 \varepsilon_0 \omega t)} \]

where \( \varepsilon' \) is the real impedance, \( \varepsilon'' \) is the imaginary impedance, \( f \) is the frequency, \( d \) is the thickness of the film, \( \varepsilon_0 \) is the vacuum dielectric constant, and \( A \) is the overlapping area between the electrodes.

**X-Ray Scattering:** WAXS measurements were performed in a SAXS-LAB Ganesha 300XL X-ray Scattering instrument. The instrument was equipped with a Xenocs GenIX 3D Cu Ka source (\( \lambda = 0.15418 \) nm) and a Dectris Pilatus 30 K photon-counting detector. The sample-detector distance was \( d = 100 \) mm, and ultra-high vacuum was applied to reduce background scattering. The films were peeled off from their substrates to prepare free-standing thick films and perform in-plane WAXS measurements.

**Scanning Electron Microscopy (SEM-EDS):** Scanning electron microscopy (SEM) images were captured in a FEI (Thermo Fischer Scientific) Magellan 400 XHR-SEM equipped with an Oxford X-MAX 80 mm² energy dispersive x-ray spectrometer (EDS).

**Supporting Information**

Supporting Information is available from the Wiley Online Library or from the author.

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**Conflict of Interest**

The authors declare no conflict of interest.

**Author Contributions**

Z.A. and D.V. conceived the project and supervised the work. M.L.-D. and S.S. carried out the experiments. Z.A. and M.U. developed the simulation code and M.U. ran the simulations. K.R.K. and M.A. synthesized the nanoparticles. M.U. and M.L.-D. contributed equally to this work. All authors contributed to writing the manuscript.

**Data Availability Statement**

The data that support the findings of this study are available from the corresponding author upon reasonable request.

**Keywords**

conjugated polymer, dielectric, energetic disorder, P3HT, thermoelectric

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