Formation of Wide-orbit Gas Giants Near the Stability Limit in Multi-stellar Systems

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Abstract

We have investigated the formation of a circumstellar wide-orbit gas giant planet in a multiple stellar system. We consider a model of orbital circularization for the core of a giant planet after it is scattered from an inner disk region by a more massive planet, which was proposed by Kikuchi et al. We extend their model for single star systems to binary (multiple) star systems, by taking into account tidal truncation of the protoplanetary gas disk by a binary companion. As an example, we consider a wide-orbit gas giant in a hierarchical triple system, HD131399Ab. The best-fit orbit of the planet is that with semimajor axis \( \sim 80 \) au and eccentricity \( \sim 0.35 \). As the binary separation is \( \sim 350 \) au, it is very close to the stability limit, which is puzzling. With the original core location \( \sim 20–30 \) au, the core (planet) mass \( \sim 50 M_E \) and the disk truncation radius \( \sim 150 \) au, our model reproduces the best-fit orbit of HD131399Ab. We find that the orbit after the circularization is usually close to the stability limit against the perturbations from the binary companion, because the scattered core accretes gas from the truncated disk. Our conclusion can also be applied to wider or more compact binary systems if the separation is not too large and another planet with \( \geq 20–30 \) Earth masses that scattered the core existed in inner region of the system.

Key words: accretion, accretion disks – planetary systems – planets and satellites: formation

1. Introduction

Most of the stars in our Galaxy are members of binary or triple star systems. Many exoplanets have been discovered in circumstellar orbits in multiple star systems by transit and radial velocity surveys. Although the circumstellar orbits of planets can be destabilized by secular perturbations from a binary companion, they are stable if their orbital radii are less than a critical value. Holman & Wiegert \( (1999) \) derived a fitting formula for the critical separation for stability as

\[
a_c \simeq (0.46 - 0.38 \mu - 0.63 e_b + 0.59 \mu e_b) a_b,
\]

where \( \mu \) is the binary companion mass scaled by the sum of the host and companion stars, \( e_b \) and \( a_b \) are the eccentricity and semimajor axis, respectively, of the binary companion orbit, and circular orbits are assumed for the planets. For an equal-mass binary pair (\( \mu = 0.5 \)) with a circular binary orbit, \( a_c \simeq 0.27 a_b \).

Wide-orbit extrasolar gaseous giant planets in nearly circular orbits have been detected by direct imaging observations for several systems \( \text{e.g.}, \) Kalas et al. \( (2008) \); Marois et al. \( (2008) \); Kuzuhara et al. \( (2013) \). One of the latest announcements is a \( (4 \pm 1) \) \( M_{\text{Jup}} \) planet in the HD131399 triple star system \( \text{(Wagner et al. \( 2016) \).} \) The primary star, HD131399A, is an A-type star with mass \( \sim 1.82 M_\odot \), which the discovered planet (HD131399Ab) orbits. The close binary of a G-type star with mass \( \sim 0.96 M_\odot \) (HD131399B) and a K-type star with mass \( \sim 0.6 M_\odot \) (HD131399C) is orbiting HD131399A with semimajor axis of \( \sim 350 \) au and eccentricity of \( \sim 0.13 \) \( \text{(Wagner et al. \( 2016) \).} \) With these values, Equation (1) shows \( a_c \sim 0.24 a_b \simeq 84 \) au. The estimated semimajor axis and eccentricity of the planet HD131399Ab are \( 82^{+42}_{-29} \) au and \( 0.35 \pm 0.25 \) \( \text{(Wagner et al. \( 2016) \).} \) Although Equation (1) is for planets in circular orbits, the estimated planetary semimajor axis is close to \( a_c \) and the planet’s orbit would be marginally stable or possibly unstable on long timescales \( \text{(Wagner et al. \( 2016) \); Veras et al. \( 2017) \).} \) Although the planet could be a background star \( \text{(Nielsen et al. \( 2017) \), if it is a planet, how to form such a} \)

marginally stable world in a multiple planetary system is a challenge for planet formation theory.

Because in situ formation of gas giant planets is difficult at \( \sim 80 \) au with the conventional core accretion scenario \( \text{(e.g., Ida & Lin \( 2004 \))}, \) Wagner et al. \( (2016) \) discussed the following three possibilities: (i) planet–planet scattering in the star A system, (ii) formation of a circumbinary planet around the B/C pair followed by transfer to the A system, and (iii) formation of the planet around either of the stars and evolution in the course of stellar orbital evolution of the triple stellar system before settling down to the current stellar configuration. For model (i), an additional unseen massive planet is required in the inner region. Because the eccentricity after the scattering must be closed to unity, an eccentricity damping mechanism for the scattered planet is also required. Although models (ii) and (iii) are not ruled out, it is not clear what evolutionary path leads to the current planetary and stellar orbital configurations.

Here, we are focused on the scattering model and discuss how a gas planet with baffling features (a wide-separation moderate-eccentric orbit close to the stability limit by perturbations from a companion(s)) such as HD131399Ab can be reproduced. Planet scattering by a more massive planet can significantly increase the apoastron distance, but not the periastron distance. To explain a wide-orbit gas giant with moderate orbit eccentricity, a mechanism to lift the periastron distance, equivalently, to damp the eccentricity without significant semimajor axis damping is required.

The Lidov–Kozai mechanism \( \text{(Kozai \( 1962 \); Lidov \( 1962 \)) is one of the possible eccentricity variation mechanisms. The secular perturbation from the binary companions orbiting around HD131399A can induce large amplitude oscillations of the eccentricity \( e \) and inclination \( i \) of HD131399Ab without changing the semimajor axis due to conservation of the vertical component of the orbital angular momentum \( (\sim \sqrt{1 - e^2 \cos i}) \) around A, if the initial argument of periastron is proper. In this case, however, the proper range of the initial argument of
periastron is narrow. Furthermore, even if the narrow range of initial conditions is satisfied, the periastron distance repeatedly becomes smaller according to the oscillation, and HD131399Ab’s orbit can also be repeatedly perturbed by the massive planet in the inner region that scattered HD131399Ab. It is not clear if HD131399Ab’s orbit can be stable during the age of the host star.

Another possibility is dynamical friction from the protoplanetary disk gas if exists after the scattering. Bromley & Kenyon (2014) investigated the orbital evolution of eccentric planets by dynamical friction. They found that the periastron distance is increased by a factor of at most four times in the case of uniform disk gas depletion. In the case of inside-out depletion, dynamical friction from the outer part of the disk contributes to significant lift-up of the periastron distance, but it is unlikely that the inside-out disk gas depletion continues up to the ∼50 au that is required to reproduce the orbit of HD131399Ab.

The model proposed by Kikuchi et al. (2014) is also based on planet–planet scattering, but considers scattering of a solid core and the eccentricity damping during gas accretion onto the core to form a gas giant. The gas accretion is most efficient when the core is near the apostron in the highly eccentric orbit after the scattering. Even if the disk gas surface density of ∝r^{−3/2} − r^{−1}, the periastron distance is significantly increased. This model does not require a gas giant in an inner region more massive than the wide-orbit gas giant in the final state. This model is a promising option to reproduce the current orbital configuration of HD131399Ab.

The model also naturally explains why the orbit is close to the stability limit. Kikuchi et al. (2014) considered the formation of a wide-orbit gas giant around a single star and found that the final orbit is regulated by the radius of the disk’s outer edge, because gas accretion onto the planet does not occur beyond the disk’s outer edge. When a stellar companion exists, the circumstellar disk is truncated at ∼1/3 of the binary separation by the perturbations from the companion with e_b ∼ 0.1, and the truncation radius becomes larger for a smaller-mass companion and for smaller e_b (e.g., Artymowicz & Lubow 1994). If the model by Kikuchi et al. (2014) is adopted, the final semimajor axis of the planet settles down to the location just inside the disk truncation radius, which is close to the stability limit. This result is not specific to the HD131399 system, but can be applied generally to circumstellar gas giants in multiple stellar systems. We use the HD131399 system as a reference system. Note that circumstellar gas giant planets, γ Cephei Ab, HD196885Ab, and HD41004Ab, in closer binary systems (a_b ∼ 20 au) also have orbits close to the stability limit (e.g., Thebault & Haghighipour 2015). Because these gas giants are at ∼2 au, they can be in principle formed by the standard core accretion model. However, it is not clear if planet formation proceeds in such highly perturbed environments (Thebault & Haghighipour 2015). These planets could also be formed by the model here, if another planet with ≥20–30 Earth masses existed at ≤1 au, as discussed later.

We briefly summarize the model of Kikuchi et al. (2014) in Section 2.1 and describe the assumptions and initial conditions for the discussions on HD131399 system in Section 2.2. We present the results of numerical simulations in Section 3. Section 4 is devoted to the summary and discussion.

### 2. Model

#### 2.1. The Model by Kikuchi et al. (2014)

The scenario proposed by Kikuchi et al. (2014) is based on the conventional core accretion model as follows: (i) an icy core (or a core with some amount of gaseous envelope) accretes from planetesimals in inner regions at semimajor axis ≲30 au, (ii) it is scattered outward by a nearby gas giant or more massive core to acquire a highly eccentric orbit with a periastron distance close to the original semimajor axis, (iii) it is circularized with significant lift-up of the periastron distance through accretion of local protoplanetary disk gas along the eccentric orbit, and (iv) through the local gas accretion, the planet becomes a gas giant. For a given initial high eccentricity and semimajor axis, Kikuchi et al. (2014) investigated the details of the process in step (iii), assuming that the gas disk motion is Keplerian, the motions of the planet and the gas disk are coplanar (they found that if the inclination is smaller than 30°, the final values of eccentricity and semimajor axis change by less than 5%), the gas accretion rate onto the planet from local disk regions is regulated by its envelope contraction rather than supply from the disk and accordingly, it is independent of a radial distribution of disk gas surface density except that it vanishes beyond the disk’s outer edge.

Here, we summarize their results (for detailed derivations of formulas, refer to Kikuchi et al. 2014). The changes of the energy and angular momentum are derived analytically, although it must be solved numerically. The damping rates of eccentricity e and semimajor axis a as a function of the planetary mass M are given by

\[
\frac{de}{d \log M} = - \frac{1 - e^2}{e} \left( f_e(e, u_d) + \frac{1}{2} f_r(e, u_d) \right),
\]

\[
\frac{d \log a}{d \log M} = - f_r(e, u_d),
\]

where \(u_d\) is the maximum eccentric anomaly (0 < \(u_d\) < \(\pi\)) within the gas disk of the outer edge at \(r_\text{d}\), which is given by

\[
u_d \equiv \begin{cases} 
\cos^{-1} \left[ \frac{1}{e} \left( 1 - \frac{2}{\pi} \right) \right] & \text{for } [Q > r_\text{d}], \\
\pi & \text{for } [Q < r_\text{d}],
\end{cases}
\]

where \(Q\) is the apostron distance of the planet. The functions \(f_e\) and \(f_r\) are the change rates of the specific angular momentum and orbital energy over one orbital period expressed as

\[
f_e = \int_{-\tilde{t}_d/2}^{\tilde{t}_d/2} s \left( \frac{\epsilon_{\text{gas}}}{\tilde{t}_p} - 1 \right) dt,
\]

\[
f_r = \int_{-\tilde{t}_d/2}^{\tilde{t}_d/2} s \left( \frac{\epsilon_{\text{gas}}}{\tilde{t}_p} - \frac{\epsilon_{\text{coll}}}{\tilde{t}_p} - 1 \right) dt,
\]

where \(\tilde{t}_d\) is a duration at \(r < r_\text{d}\), \(r\) is the instantaneous distance of the planet from the central star, \(\tilde{t}_p\) and \(\epsilon_p\) are the specific angular momentum and orbital energy of the planet, \(\epsilon_{\text{gas}}\) and \(\epsilon_{\text{coll}}\) are those of accreting gas at instantaneous locations along the orbit, and \(\epsilon_{\text{coll}}\) is energy dissipation by collision between the planet and accreting gas. The factor \(s\) is given as follows. The relative velocity between the planet and the unperturbed gas
flow (circular Keplerian flow), is readily derived by
\[ v_{\text{rel}}(r)^2 = \frac{GM_*}{r} \left( 3 - \frac{r}{a} - 2 \sqrt{\frac{a}{r}(1 - e^2)} \right), \]  
(7)
where \( M_* \) is the host star mass and \( a \) and \( e \) are the semimajor axis and the eccentricity of the instantaneous planetary orbits. However, because we are concerned with damping of initially highly eccentric orbits, the reduction of the relative velocity due to bow shock that occurs in front of the planet must be taken into account. Kikuchi et al. (2014) derived the reduction factor \( s \) for post-shock relative velocity \((v_{\text{rel}})\) with a 1D plane-parallel approximation as
\[ s = \frac{(\gamma - 1)M_*^2 + 2}{(\gamma + 1)M_*^2} \approx \frac{1}{4} \left( 1 + \frac{3}{M_*^2} \right), \]  
(8)
where \( \gamma \) is the specific heat ratio \((\gamma = 7/5 \text{ for H}_2 \text{ molecules})\) and \( M \) is Mach number of pre-shock.
\[ M = \frac{v_{\text{rel}}}{c_s} = \frac{30}{1 \text{ au}} \left( \frac{r}{1 \text{ au}} \right)^{-1/4} \left( 3 - \frac{r}{a} - 2 \sqrt{\frac{a}{r}(1 - e^2)} \right)^{1/2}, \]  
(9)
where we used an optically thin disk temperature, \( T = 280(r/1 \text{ au})^{-1/2} \text{ K} \), for evaluation of sound velocity \( c_s \). Note that Equations (2) and (3) are independent of a disk model except the estimation of Mach number.

### 2.2. Initial Conditions or Settings

We apply Kikuchi et al.’s model to a reference planet, HD131399Ab. We first evaluate the initial orbital elements and mass of a precursor body for HD131399Ab and the gas disk that are substituted into Kikuchi et al.’s model, where “initial” means the moment just after the scattering by an unseen planet. We do not simulate the scattering process itself, but evaluate a reasonable range of the “initial” parameters after the scattering.

The initial periastron distance \( q_i \) must be around the unseen massive planet. In the conventional core accretion model, \( q_i \) may be \( \lesssim 40 \text{ au} \). The upper limit of the initial apoastron distance \( Q_i \) may be limited by the existence of the binary companions. The best-fit of the orbit of the binary by Wagner et al. (2016) is \( a_b = 349 \pm 28 \text{ au} \) and \( e_b = 0.13 \pm 0.05 \) where \( a_b \) and \( e_b \) are the semimajor axis and eccentricity of the binary with respect to HD131399A. We assume \( a_b = 350 \text{ au} \) and \( e_b = 0.13 \) and consider the cases of \( Q_i \lesssim 300 \text{ au} \). The initial semimajor axis \( a_i \) and eccentricity \( e_i \) of the planet are calculated by \( q_i \) and \( Q_i \) as
\[ a_i = \frac{Q_i + q_i}{2}, \]  
(10)
\[ e_i = \frac{Q_i - q_i}{Q_i + q_i}. \]  
(11)

The inclination to the gas disk is assumed to be zero for simplicity. The initial mass of the planet \((M_i)\) must be larger than the critical core mass for the onset of gas accretion. We use \( M_i = 20 M_\oplus \) and \( 50 M_\oplus \), where \( M_\oplus \) is an Earth mass. The final mass of the planet is given by the observational best-fit value, \( 4 M_j \) (Wagner et al. 2016). We stop the calculation when the mass of the planet reaches the final mass. In Kikuchi et al.’s model, orbital evolution is described by the planetary mass evolution but not by time evolution. We do not need to assume gas accretion rate onto the planet.

We use 100 au and 150 au for the gas disk radius—because the circumstellar disk is tidally truncated by the perturbations from the binary companions—at \( \sim 1/3 \) of the distance between the primary star HD131399A and the binary (e.g., Artymowicz & Lubow 1994). The disk truncation radius is comparable to or slightly larger than the long-term orbital stability limit radius. We assume the gas disk exists until the end of the calculation.

### 3. Results

Using the initial semimajor axis and eccentricity, we calculate the final semimajor axis and eccentricity for different values of disk size \( r_d \) and the initial core mass \( M_i \), integrating Equations (2) and (3) up to \( M = 4 M_j \). Figure 1 shows some examples of orbital evolution as a function of the planetary mass growth. According to the mass growth of the planet, its eccentricity and semimajor axis are damped and periastron \( q \) and apoastron \( Q \) converge. Periastrons are lifted up quickly and the scattered planet becomes isolated from the perturber, the more massive planet. Apoastrons \( Q \) settle down to \( f_q \) with \( f \sim 0.7–1.0 \). Kikuchi et al. (2014) showed that the final \( Q \) is smaller for smaller \( q_i/r_d \) and smaller final \( e \). Because the final \( e \) is similar in each panel of Figure 1, the difference of the final values of \( Q \) reflects the different values of \( q_i/r_d \).

The damping of \( Q \) is associated with the planetary mass increase. This figure shows that the mass increase by 10 times from the initial value is enough to damp the apoastrons \( Q \) to \( \lesssim r_d \). The mass increase factor to the “final” state is \( 4 M_j/M_i = 25 \) or 64. Thus, the planets’ final orbits are inevitably close to the disk truncation radius. Orbital eccentricities are damped significantly from the initial values \( \sim 1 \), but have not been completely damped in this case. The semimajor axes are slightly smaller than \( Q \) in the final state, corresponding to the retained \( e \). Because the orbital stability limit is slightly closer to the primary star than the disk outer edge is, the final semimajor axes are comparable to the orbital stability limit. With \( Q \sim f_q \), the final \( a \) would be
\[ a = \frac{(1 - e)Q \sim (1 - e)f_q \sim (1 - e)(f/3)\left(\frac{r_d}{a_b/3}\right)a_b}. \]  
(12)

For \( e \sim 0.35, f \sim 0.7–1.0, \) and \( r_d \sim a_b/3, a \sim (0.15–0.22) a \). Figure 2 shows the values of the semimajor axis \( a \) and eccentricity \( e \) of the planet when the planetary mass reaches \( 4 M_j \), on the \( Q-q_i \) plane with available ranges of \( 50 \text{ au} < Q_i < 300 \text{ au} \) and \( q_i < 40 \text{ au} \) for disk sizes, \( r_d = 100 \text{ au} \) and 150 au, and the initial planetary masses, \( M_i = 20 M_\oplus \) and \( 50 M_\oplus \). The parameter \( f \) is controlled by \( q_i/r_d \), so that \( q_i/r_d \) and \( r_d/a_b \) (the binary separation is fixed to be \( a_b = 350 \text{ au} \)) determine the final \( a_0 \), as shown in Equation (12). Because the mass increase factor determines the final \( e \) and the final mass is fixed to \( 4 M_j \), \( M \) determines the final \( e \) in this case. Each square on the map corresponds to one calculation that we have performed. The observationally estimated semimajor axis and eccentricity of HD131399Ab are \( 82^{+22}_{-27} \text{ au} \) and \( 0.35 \pm 0.25 \), respectively (Wagner et al. 2016). Different colors for the squares represent how the calculated final values of \( a \) and \( e \) are consistent with the observational estimates, from yellow, light blue, orange, and black. The yellow squares show the best ones, where \( 77 \text{ au} < a < 87 \text{ au} \) and \( 0.3 < e < 0.4 \).
Figure 2 shows that the current orbit of HD131399Ab is reproduced from the initial conditions with $q_i \sim 20–30$ au, a relatively large initial mass ($M_i = 50 M_E$), and relatively large disk truncation radius ($r_d = 150$ au).

If $Q_i$ is close to the separation of the binary companion, there is a risk that the planet is again scattered by the binary companion pair until $Q$ is sufficiently damped. For $M_i = 50 M_E$ and $r_d = 150$ au, the yellow squares exist down to $Q_i \sim 150$ au, where the risk may be low. The relatively massive initial mass, $M_i = 50 M_E$, corresponds to a planet on its way to becoming a gas giant. In this case, a gas giant more massive than Saturn must have existed at 20–30 au to scatter the planet.

4. Summary and Discussion

We have investigated the formation of circumstellar wide-orbit gas giants in multiple star systems, motivated by the announcement of the discovery of planet HD131399Ab by direct imaging (Wagner et al. 2016). This planet is a circumstellar gas giant in a hierarchical triple star system and has perplexing orbital features. The semimajor axis is about 1/4 of the separation between A and the B/C binary pair, which means that the planet’s orbit would be marginally stable or possibly unstable on long timescales. We have applied the formation model for wide-orbit gas giants by Kikuchi et al. (2014) and found that the orbit close to the stability limit is not a fortunate accident, but rather an inevitable result.

The suggested scenario is as follows: (i) a core with or without a gaseous envelope is scattered by a nearby more massive planet at 20–30 au so that it develops a highly eccentric orbit with the periastron at 20–30 au, (ii) the scattered planet spends most of its time near the apoastron on a highly eccentric orbit after the scattering, where the planetesimal accretion rate must be very small, (iii) rapid gas accretion starts because of the low planetesimal accretion rate, and the gas accretion is most efficient near the apoastron, (iv) through gas
accretion onto the planet, the orbit is circularized such that the periastron distance is significantly increased and the apoastron distance is adjusted to the tidal truncation radius of the disk by the binary companion \( r_d \), which is comparable to the orbital stability limit. Therefore, this model is a promising option for reproducing the current orbital configuration of HD131399Ab.

The best-fit results are obtained by the initial scattering location \( q_i \approx 20-30 \text{ au} \), the initial planet mass \( M_i \approx 50 \text{ } M_\oplus \) and the disk truncation radius \( r_d \approx 150 \text{ au} \).

If the orbital data of HD131399Ab is improved, the predicted initial conditions are better constrained. Even if HD131399Ab turns out to be a background star, our model can be generally applied to circumstellar gas giants in multiple stellar systems, and it predicts that the planets would often be located close to the stability limit against the perturbations of a companion(s). The results depend on the scaled parameters, \( q_i / r_d \) and \( r_d / a_b \), where \( a_b \) is the binary separation and \( q_i \) corresponds to the original semimajor axis of the planet before scattering. The parameter \( r_d / a_b \) is usually \( \sim 1/3 \), except for cases with high \( e_b \) or a very different mass companion from the host star, and the final \( Q \) does not change sensitively for \( q_i / r_d \lesssim 0.1 \) (Kikuchi et al. 2014).

Other circumstellar gas giant planets close to the stability limit have already been discovered in more compact binary systems \( (a_b \sim 20 \text{ au}) \): \( \gamma \) Cephei Ab, HD196885Ab, and HD41004Ab, all of which are located at \( \sim 2 \text{ au} \). The parameter \( r_d / a_b \) for these systems should be similar to HD131399Ab. Our model can reproduce their orbits close to the stability limit with reasonable ranges of values of \( q_i \) and \( M_i \) (see Equation (12)), while these planets could also be formed by the standard in situ accretion model. Note that our model needs another planet with \( q_i > \gamma \text{Cephei A}, \text{HD196885A, and HD41004A systems. Furthermore, in compact binary systems, there is a greater risk that the scattered core will be perturbed by the binary companion before the scattered orbit shrinks. For very wide binary systems, our model may not work well either. In our model, } Q_i \text{ must be between } r_d \sim a_b/3 \text{ and } a_b \text{, while it is likely that } q_i \lesssim 30 \text{ au. From Equation (11), } 1 > e_i \gtrsim (a_b - 90)/(a_b + 90). \text{ The range of } e_i \text{ that satisfies this condition becomes narrower as } a_b \text{ increases. Furthermore, the disk size cannot become infinitely large when } a_b \text{ is very large. In this case, } r_d \text{ is independent of the stability limit. Thus, our model is better applied to binary systems with}

![Figure 2.](image-url) Compatibility of the final semimajor axis \( a \) and eccentricity \( e \) of the planet (when the planetary mass \( M \) reaches \( 4 \text{ } M_\oplus \)) to observationally estimated values of HD131399Ab as a function of initial \( Q_i \) and \( q_i \), for \( r_d = 100 \text{ au} \) and 150 au, and \( M_i = 20 \text{ } M_\oplus \) and \( 50 \text{ } M_\oplus \). The yellow color points represent the best-fit: 77 au < \( a \) < 87 au and 0.3 < \( e \) < 0.4. The other colors represent more deviated values. Light blue: 72 au < \( a \) < 102 au and 0.2 < \( e \) < 0.5, black: 55 au < \( a \) < 105 au and 0.2 < \( e \) < 0.5, respectively.
separations of, say, 100–1000 au, while it could also be applied to more compact or more extended binary systems.

It is also pointed out that circumbinary gas giant planets tend to be located near the inner limit of the stable region around binary systems because the circumbinary disks are truncated by an inner binary pair and planetary migrations stop at the inner edge (Kley & Haghighipour 2014, 2015). Here, we predict that circumplanetary wide-orbit gas giant planets tend to be located near the outer limit of the stable region around the host star. These predictions should be tested by more samples of direct imaging observations for wide-orbit gas giants in multiple stellar systems.

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