First–Principles Investigation of the Structural, Elastic, Electronic, and Optical Properties of \( \alpha \)– and \( \beta \)–SrZrS\(_3\): Implications for Photovoltaic Applications

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Abstract: Transition metal perovskite chalcogenides are attractive solar absorber materials for renewable energy applications. Herein, we present the first–principles screened hybrid density functional theory analyses of the structural, elastic, electronic and optical properties of the two structure modifications of strontium zirconium sulfide (needle–like \( \alpha \)–SrZrS\(_3\) and distorted \( \beta \)–SrZrS\(_3\) phases). Through the analysis of the predicted electronic structures, we show that both \( \alpha \)– and \( \beta \)–SrZrS\(_3\) materials are direct band gaps absorbers, with calculated band gaps of 1.38, and 1.95 eV, respectively, in close agreement with estimates from diffuse–reflectance measurements. A strong light absorption in the visible region is predicted for the \( \alpha \)– and \( \beta \)–SrZrS\(_3\), as reflected in their high optical absorbance (in the order of \( 10^5 \) cm\(^{-1}\)), with the \( \beta \)–SrZrS\(_3\) phase showing stronger absorption than the \( \alpha \)–SrZrS\(_3\) phase. We also report the first theoretical prediction of effective masses of photo-generated charge carriers in \( \alpha \)– and \( \beta \)–SrZrS\(_3\) materials. Predicted small effective masses of holes and electrons at the valence, and conduction bands, respectively, point to high mobility (high conductivity) and low recombination rate of photo-generated charge carriers in \( \alpha \)– and \( \beta \)–SrZrS\(_3\) materials, which are necessary for efficient photovoltaic conversion.

Keywords: earth–abundant materials; chalcogenide perovskites; Solar cell; Density Functional Theory; Optoelectronic properties

1. Introduction

Perovskite materials have attracted significant attention from researchers due to their potential in various applications. In photovoltaic applications, inorganic–organic halide perovskite materials represent a great breakthrough in the development of solar cell materials with the power conversion efficiency rising from 3.6 to about 24%, since the first application in 2009 by Kojima et al. [1]. The recently reported efficiencies are comparable to the most advanced thin film solar cells, such as CdTe, GaAs, as well as the silicon-based solar cells. In addition to this unprecedented improvement in power conversion efficiency are the ease and low-cost of synthesis of the materials, as well as the fabrication of the solar cell device. Notwithstanding the rapid increase in their efficiencies, the toxicity of the lead content and the intrinsic instability of the bulk lead–halide perovskite materials and their interface heterostructures remain significant drawbacks to their large–scale applications and commercialization [2–5]. These concerns have motivated the search for new absorber materials, that are lead–free but with similar electronic and optical properties as lead–halide perovskite materials. Efforts to replace the Pb in lead halide perovskites with low toxic cations including Sn (II) [6], Ag (I) [7],
Bi (III) [8,9], Ti (IV) [10] and Sb (III) [10] have, therefore, received significant attention. These materials yielded non–toxic but low efficiency devices, a maximum of 9% power conversion efficiency (PCE) for the Sn based perovskite. Oxide perovskites on the other hand have proven to have higher stability, due to their resistance to moisture, and have been reported to be promising solar absorbers if engineered to have the band gap matched with the solar spectrum [11,12].

Chalcogenide perovskites having the structure ABX₃ (X = S, Se; A, B = metals with combined valence of 6), have recently been proposed for photovoltaic application [13]. Compared to lead halide perovskites, chalcogenide perovskites materials are more environmentally friendly (component elements are earth–abundant and non–toxic) and possess superior electronic and optical properties, suggesting their potential ideal for low–cost tandem solar cell application. So far, a number of transition metal chalcogenide perovskites have been successfully synthesized experimentally and investigated theoretically [3,13–17]. Sun et al. [3] in their theoretical studies, predicted that the band gaps of CaTiS₃ (1.0 eV), BaZrS₃ (1.75 eV), CaZrSe₃ (1.3 eV), and CaHfSe₃ (1.2 eV) having the distorted perovskite structure are suitable for making single–junction solar cells. They are generally n–type semiconductors, with thin–films of BaZrS₃ recently to have carrier densities in the range of 10¹⁸–10²⁰ cm⁻³ [18]. Chalcogenide perovskites also display high optical absorption properties, making them promising materials used in addressing the instability and toxicity issues associated with halide perovskites. A number of chalcogenide perovskites including CaZrS₃, SrTiS₃, SrZrS₃ and BaZrS₃ have been successfully synthesized by Perera et al. [17] using high temperature sulfurization of their oxide counterparts. A widely tunable bandgap range of 1.73–2.87 eV was reported for these materials. Ju et al. [14] predicted a series of chalcogenide perovskites such as SrSnSe₃, CaSnS₃ and SrSnS₃ with tunable direct bandgaps within the optimal range of 0.9–1.6 eV for single junction solar cell applications. Peng et al. [19] demonstrated, from first–principles density functional theory (DFT) calculations, that the optical transitions near the band edges of chalcogenide perovskites differ from those of their halide counterparts.

Single crystal X–ray diffraction analysis of strontium zirconium sulfide (SrZrS₃) samples show two structure modifications (needle–like α–SrZrS₃ and distorted β–SrZrS₃ phases (Figure 1). The α–and β–SrZrS₃ phases both crystallize in the orthorhombic crystal structure with space group Pnma. The optical band gaps were estimated to be 1.52 and 2.05 eV for the α–SrZrS₃, and β–SrZrS₃ phases, respectively, from diffuse–reflectance measurements [16]. Thermal stability investigations by Niu et al. [20] on synthesized α–SrZrS₃, β–SrZrS₃, BaZrS₃, Ba₂ZrS₄ and Ba₃Zr₂S₇ show that these chalcogenide perovskites possess excellent thermal stability in air for a temperature range up to 550 °C [16]. The fundamental atomic–level insights into the mechanical and structural characteristics, as well as the electronic and optical features of SrZrS₃ materials, albeit, poorly understood and inconclusive. Previous theoretical studies by Oumertem et al. have characterized the electronic and thermodynamic properties of the cubic and orthorhombic XZrS₃ (X = Ba, Sr, Ca) compounds, predicting their band gap in the range of 1.151–1.617 eV [15]. There is, however, no systematic theoretical investigation dedicated to elucidating the structural, elastic, and optoelectronic properties of the α–SrZrS₃ and β–SrZrS₃ chalcogenide perovskites, which makes this investigation timely.

In the present study, we do not only report the structural, mechanical, and electronic properties of α–SrZrS₃ and β–SrZrS₃ by means of screened hybrid (HSE06) density functional theory methods, but also comprehensively characterized the optical properties and discussed their implications for photovoltaic applications. Based on the calculated optical absorbance, reflectivity, and refractive index, we demonstrate that α– and β–SrZrS₃ are suitable solar absorber materials for solar cell and other optoelectronic applications.
Figure 1. Crystal structure of (a) α–SrZrS$_3$ and (b) β–SrZrS$_3$. Color code: Sr = Green, Zr = Blue, and S = yellow.

2. Computational Details

The density functional theory (DFT) were performed within periodic boundary conditions as implemented in the Vienna Ab initio Simulation Package (VASP) \cite{21,22}. The Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation (GGA) functional \cite{23} was used for geometry optimizations, while for electronic structures and optical calculations, the screened hybrid functional HSE06 with 25% Hartree–Fock exchange and screening parameter of $\omega = 0.11$ bohr$^{-1}$ was employed \cite{24}. The projected augmented wave (PAW) method was used to describe the interactions between the valence electrons and the cores \cite{25}. Long–range van der Waals (vdW) were accounted for using the Grimme (DFT–D3) method \cite{26}. A plane–wave basis, set with a kinetic energy cut–off of 600 eV, was tested to be sufficient to converge the total energy of the α–SrZrS$_3$ and β–SrZrS$_3$ phases to within $10^{-6}$ eV and the residual Hellmann–Feynman forces on all relaxed atoms reached $10^{-3}$ eV Å$^{-1}$. The Brillouin zone of the α–SrZrS$_3$ and β–SrZrS$_3$ phases was sampled using $5 \times 7 \times 3$, and $5 \times 3 \times 5$ Monkhorst–Pack \cite{27} K–points mesh, respectively.

The optical properties of α–SrZrS$_3$ and β–SrZrS$_3$ were determined from the complex dielectric function, $\varepsilon(\omega) = \varepsilon_1(\omega) + i \varepsilon_2(\omega)$ within the independent–particle formalism \cite{28}, where the the imaginary part of the dielectric function is calculated in the long wavelength $q \to 0$ limit as,

$$\varepsilon_2(\omega) = \varepsilon_2^{(2)}(\omega) = \frac{4\pi e^2}{\Omega} \lim_{q \to 0} \sum_{c,v,k} 2w_k \delta(\epsilon_{ck} - \epsilon_{vk} - \omega)$$

$$\times \langle u_{ck+e_\alpha q} | u_{vk} \rangle \langle u_{ck+e_\beta q} | u_{vk} \rangle^*$$

(1)

where, $\Omega$ and $w_k$ are the volume of the primitive cell and k–point weights, respectively. The $\epsilon_{ck}(\epsilon_{vk})$ are $k$–dependent conduction (valence) band energies, $u_{ck}, u_{vk}$ are the cell periodic part of the pseudo–wave function and $e_{\alpha,\beta}$ are the unit vectors along the Cartesian directions. From Kramers–Kronig transformations, the real part of dielectric function can be determined from the relation,

$$\varepsilon_1(\omega) = \varepsilon_1^{(1)}(\omega) = 1 + \frac{2}{\pi} \int_0^{\infty} \frac{\varepsilon_2^{(2)}(\omega')\omega'}{\omega'^2 - \omega^2 + i\eta} d\omega'$$

(2)

where $P$ denotes the principle value. A small value of 0.1, which is acceptable for most calculations was used for the complex shift ($\eta$) to smoothen the real part of the dielectric function. The optical
parameters, such as absorption coefficient, are based on \( \varepsilon_1 \) and \( \varepsilon_2 \). The absorption coefficient \( (\alpha_{abs}) \) is calculated using the following relation:

\[
\alpha_{abs} = \sqrt{2\alpha}\left(\sqrt{\varepsilon_2^2(\alpha) + \varepsilon_3^2(\alpha)} - \varepsilon_1(\alpha)\right)^{1/2}.
\]

Local field and excitonic effects have been neglected in the present study as they are not accurately treated in the independent-particle formalism. These effects may be accounted for by using expensive methods, such as Bethe–Salpeter equation (BSE) and time–dependent DFT with proper exchange–correlation kernels [29].

The elastic stiffness constants were calculated using the stress–strain method [30]. The strain \( (\sigma) \) and stress \( (\varepsilon) \) are related according to Hook’s law by \( \sigma_{ij} = C_{ij}\varepsilon_{ij} \), where \( C_{ij} \) are the elastic stiffness constants. For an orthorhombic system, there are nine independent elastic constants viz; \( C_{11}, C_{22}, C_{33}, C_{12}, C_{13}, C_{23}, C_{44}, C_{55} \), and \( C_{66} \). These elastic constants are used to predict the bulk modulus \( (B_V) \) and the shear modulus \( (G_V) \). Whereas, Young’s modulus \( (E) \) and the Poisson’s ratio \( (\nu) \) are in turn predicted from the calculated bulk and shear moduli. The bulk and shear moduli measure the material’s resistance to uniform compression, and shearing strains, respectively. The bulk and shear moduli were calculated using the Voigt approximation [31] which for orthorhombic structures, can be simplified as follows:

\[
B_V = \frac{1}{9}(C_{11} + C_{22} + C_{33}) + \frac{2}{9}(C_{12} + C_{13} + C_{23})
\]

\[
G_V = \frac{1}{15}(C_{11} + C_{22} + C_{33} - C_{12} - C_{13} - C_{23}) + \frac{1}{5}(C_{44} + C_{55} + C_{66})
\]

The Young’s modulus \( (E) \) and Poisson’s ratio \( (\nu) \), which are characteristic stiffness properties of a material were obtained using the relations: \( E = \frac{9BG}{3(B+G)} \) and \( \nu = \frac{(3B-2G)}{2(3B+G)} \).

3. Results and Discussion

3.1. Structural Properties

\( \text{SrZrS}_3 \) crystallizes in two structure modifications; \( \alpha \) and \( \beta \)–phases, both in the orthorhombic crystal system with space group \( Pnma \) (Figure 1). The \( \alpha \)-\( \text{SrZrS}_3 \) has five independent lattice sites; one \( \text{Sr} \), one \( \text{Zr} \), and three \( S \) sites, whereas in the \( \beta \)–phase, there exist only four positions (one \( \text{Sr} \), one \( \text{Zr} \), and two \( S \) sites) [32]. The \( \alpha \)-\( \text{SrZrS}_3 \) structure consists of one–dimensional double chains of edge–sharing \( \text{ZrS}_6 \) octahedra along the \( b \) axis, with \( \text{Sr} \) atoms in nine–fold coordination with \( S \) atoms, forming tri–capped trigonal prisms (Figure 1a) that are interconnected via common triangular faces [32]. Based on powder neutron diffraction analysis, the \( \beta \)-\( \text{SrZrS}_3 \) is said to have a distorted perovskite structure [33]. Unlike the \( \alpha \)–phase, the structure of \( \beta \)-\( \text{SrZrS}_3 \) is constituted by three–dimensionally connected corner–sharing \( \text{Zr} \) octahedra, and \( S \) atoms which are eightfold coordinated in a bi-capped trigonal prism (Figure 1b).

Summarized in Table 1 are the calculated lattice parameters obtained from a full structure optimization at the using PBE and HSE06 functionals, which show good agreement with known experimental data.\(^{32}\) In the \( \alpha \)-phase, each of the \( \text{ZrS}_6 \) octahedra shares two opposite edges with one another, forming a linear chain which in turn, interconnect in pairs through additional edge–sharing. The \( \text{Zr–S} \) bonds form the shortest, having a length of 2.45 Å, whereas the longest bond having a length of 2.65 Å, which involves an \( S \) atom bonding to three \( \text{Zr} \) atoms, occurs opposite to the shortest bond. The \( \text{Sr–S} \) bonds in the \( \alpha \)-\( \text{SrZrS}_3 \) phase ranges from 3.06–3.09 Å. Conversely, the \( \text{ZrS}_6 \) octahedra of the \( \beta \)–phase have all their corners interconnected forming a three–dimensional network, with \( \text{Zr–S} \) bonds ranging from 2.54 to 2.57 Å, in close agreement with experimental values (Table 1).
Table 1. Lattice constant (Å) and bond lengths (Å) of for α–SrZrS₃ and β–SrZrS₃.

| Parameter | α–SrZrS₃ | β–SrZrS₃ | Experiment [32] | α–SrZrS₃ | β–SrZrS₃ | Experiment [32] |
|-----------|-----------|-----------|-----------------|-----------|-----------|-----------------|
| a (Å)     | 8.551     | 8.540     | 8.525           | 7.133     | 7.125     | 7.109           |
| b (Å)     | 3.814     | 3.810     | 3.826           | 9.783     | 9.772     | 9.766           |
| c (Å)     | 13.930    | 13.908    | 13.925          | 6.752     | 6.748     | 6.735           |
| d(Sr–S)   | 3.06–3.09 | 3.05–3.09 | 3.06–3.08       | 2.99–3.16 | 2.98–3.21 | 2.96–3.37       |
| d(Zr–S)   | 2.45–2.65 | 2.44–2.63 | 2.44–2.64       | 2.54–2.57 | 2.54–2.56 | 2.53–2.56       |

Based on the optimized structures, we have simulated X-ray diffraction (XRD) spectrum of α–SrZrS₃ and β–SrZrS₃ using the VESTA Crystallographic Software as shown in Figure 2a. We can see that clear differences between the assigned peaks of α–SrZrS₃ and β–SrZrS₃, which is consistent with the difference in their lattice parameters. All the peaks in the simulated DFT spectrum match very closely with the experimental XRD measurement from the work of Niu et al. [34], as shown (Figure 2b). We consider that the assigned reflection peaks in the DFT XRD spectrum may become useful in clarifying future experiments, for instance to distinguish between the α–SrZrS₃ and β–SrZrS₃ phases.

Figure 2. (a) DFT-simulated X–ray diffraction pattern of α–SrZrS₃ and β–SrZrS₃ compared with (b) experimental XRD measurement [34].

3.2. Mechanical Properties

The elastic properties of materials give the data necessary in understanding the bonding property between adjacent atomic planes, stiffness, bonding anisotropic and structural stability of the material [35,36]. Shown in Table 2 are the calculated single crystal elastic constants of the α– and β–SrZrS₃ materials, all of which satisfy the Born’s mechanical stability criteria for orthorhombic structures [37], indicating that both materials are mechanically stable under ambient conditions. The predicted trend of C₁₁ > C₂₂ > C₃₃ for the α–SrZrS₃ phase, indicates greater stiffness in the [100] direction than in the [010] and [001] directions. For the β–SrZrS₃ phase, C₂₂ > C₃₃ > C₁₁ which implies that β–SrZrS₃ is stiffest in the [101] direction and least stiff in the [100] direction. The high elastic stiffness of the α– and β–SrZrS₃ could be attributed to strong Sr–S and Zr–S chemical bonding [35]. Summarized in Table 2 are the calculated Bulk (B), shear (G) and Young’s (E) moduli. A higher
bulk modulus is predicted for the $\beta$–SrZrS$_3$ phase (79.9 GPa), similar to the value of 77.35 predicted by Oumertem et al.$^{15}$, compared to the $\alpha$–SrZrS$_3$ (61.7 GPa) phase. Similar bulk modulus values were obtained by fitting a third–order Birch–Murnaghan (3$^{rd}$ BM) equation of state (EOS) $^{[38,39]}$ to the DFT–PBE obtained total electronic energy (E) vs unit cell volume (V) data (Figure 3) based on the equation,

\[
E(V) = E_0 + \frac{9V_0B_0}{16} \left\{ \left( \frac{V_0}{V} \right)^{\frac{3}{2}} - 1 \right\}^3 B'_0 + \left[ \left( \frac{V_0}{V} \right)^{\frac{3}{2}} - 1 \right]^2 \left[ 6 - 4 \left( \frac{V_0}{V} \right)^{\frac{3}{2}} \right]
\]  

where $E_0$ and $V_0$ are the equilibrium energy and volume, $B_0$ is hydrostatic bulk modulus and $B'$ is the pressure derivative of the bulk modulus at $T = 0$ K and $P = 0$ GPa. The bulk modulus and its pressure derivative are calculated at 66.73 GPa and 2.33 for $\alpha$–SrZrS$_3$ and 83.75 GPa and 2.93 for $\beta$–SrZrS$_3$, respectively. This result suggests that the $\beta$–SrZrS$_3$ phase is more rigid and less prone to compressive deformation than the $\alpha$–SrZrS$_3$ phase. Conversely, the $\alpha$–phase has higher shear and Young’s moduli than the $\beta$–phase implying more resistance to shear and tensile deformation. The Poisson’s ratios ($\nu$) are predicted at 0.244 and 0.436 for the $\alpha$, and $\beta$–phases, respectively. The Poisson’s ratio allows us to test the ductility/brittleness of material. A material is characterized as ductile if $\nu < 0.5$, otherwise it is classified as brittle $^{[40]}$. Based on this criterion, we conclude that both $\alpha$– and $\beta$–SrZrS$_3$ are ductile materials, which implies that any strain-induced defects at the interface, when these materials are deposited on substrates may relax over a relatively short distance.

Table 2. Elastic constants ($C_{ij}$), bulk modulus (B), shear modulus (G), Young’s modulus (E), and Poisson’s ratio ($\nu$) of $\alpha$–SrZrS$_3$ and $\beta$–SrZrS$_3$.

| Parameter | $\alpha$–SrZrS$_3$ | $\beta$–SrZrS$_3$ |
|-----------|------------------|------------------|
| $C_{11}$  | 137.3            | 50.3             |
| $C_{22}$  | 107.4            | 242.3            |
| $C_{33}$  | 74.3             | 118.5            |
| $C_{44}$  | 32.0             | 50.9             |
| $C_{55}$  | 35.4             | 29.3             |
| $C_{66}$  | 56.3             | 8.9              |
| $C_{12}$  | 44.4             | 53.1             |
| $C_{13}$  | 63.6             | 34.9             |
| $C_{23}$  | 10.3             | 66.0             |
| B (GPa)   | 61.73            | 79.9             |
| G (GPa)   | 38.12            | 34.96            |
| E (GPa)   | 95.36            | 91.53            |
| $\nu$     | 0.244            | 0.436            |

Figure 3. The third–order Birch–Murnaghan equation of state (EOS) fitting to the calculated E–V data of (a) $\alpha$–SrZrS$_3$ and (b) $\beta$–SrZrS$_3$. 
3.3. Electronic Properties

Shown in Figure 4a,b are the electronic band structures of the α-SrZrS₃ and β-SrZrS₃ phases, respectively, with the corresponding density of states projected on the Sr–d, Zr–d and S–p states in Figure 5a,b. Analysis of the band structures reveal that both α– and β–SrZrS₃ are direct band gaps absorbers seeing the bottom of the conduction band and the top of the valence band are located at the same crystal momentum (Γ) points on the Brillouin zone. The band gap energies of α– and β–SrZrS₃ are predicted at 1.38, and 1.95 eV, respectively. The predicted values are in close agreement with the estimated optical band gaps from diffuse–reflectance measurements: α-SrZrS₃ (1.52 eV) and β-SrZrS₃ (2.05 eV) [16]. It is evident from the projected density of states (Figure 5a,b) that the conduction band edge, in both phases, is dominated by Zr–d states. Whereas, the contribution from S–p orbital dominates the valence band edge.

![Figure 4. Band structure along the high–symmetry directions of the Brillouin zone of (a) α–SrZrS₃ and (b) β–SrZrS₃.](image)

![Figure 5. The partial density of states for (a) α–SrZrS₃ and (b) β–SrZrS₃.](image)
The charge carrier effective masses \((m^*)\) which is intricately linked to the diffusion coefficient \((D)\) and mobility \((\mu)\) of charge carrier in a semiconductor via the relations \(D = \frac{k_B T}{e m^*} \mu\) and \(\mu = e \frac{1}{m^*}\), were also calculated for the \(\alpha-\) and \(\beta-\text{SrZrS}_3\) materials. Small photo-carrier effective masses result in increased \(\mu\) and \(D\). The conductivity of charge carrier effective mass dictates the electrical resistivity and optical response of solar devices; hence their calculation is important [41]. Whiles effective masses can be quite difficult to obtain experimentally, accurate DFT calculations [42,43] can complement experiments by computing these properties. The effective masses can be obtained by fitting the energy of the valence band maximum (holes) and conduction band minimum (electrons) to a quadratic polynomial in the reciprocal lattice vector \(k\) based on the equation \(m^*_{\alpha(h)}(k) = \pm \hbar^2 \left(\frac{\partial^2 E}{\partial k^2}\right)^{-1}\). In Table 3 the calculated electron and hole effective masses for the \(\alpha-\) and \(\beta-\text{SrZrS}_3\) materials are summarized in some selective directions of the Brillouin zone. The predicted smaller, and therefore, the light mass charge carriers correspond to a high mobility of the electrons and holes at the conduction, and valence bands, respectively, and consequently point to high conductivity. The high conductivity also demonstrates the efficient separation of photo-generated charge carriers, which give rise to high-efficiency fabricated solar cell devices. In general, we found that the holes have higher effective masses than electrons in both the \(\alpha-\) and \(\beta-\text{SrZrS}_3\) materials, suggesting that the electrons do tunnel much readily than the holes. The large effective mass difference between the electrons and holes is an important factor in minimizing their recombination rate [44]. By computing the ratio of the hole to electron effective masses \((D = m^*_{\alpha}/m^*_{\beta})\), the recombination rate of photo-generated charge carriers can be assessed [45]. Higher \(D\) values generally signify higher mobility and a lower recombination rate of the photo-generated charges [46,47]. As shown in Table 3, the highest \(D\) values for the \(\alpha-\text{SrZrS}_3\) phase were calculated along the \(Y-\Gamma\) (26.67), \(T-\Gamma\) (5.25), \(Z-U\) (5.00), \(U-R\) (3.20), and \(\Gamma-X\) (2.75) directions. For the \(\beta-\text{SrZrS}_3\) phase, the highest \(D\) values were obtained along the \(\Gamma-X\) (13.50), \(Z-U\) (7.40), \(X-S\) (4.67), \(\Gamma-Z\) (3.40), \(Y-\Gamma\) (2.36), and \(U-R\) (2.33). The higher \(D\) values along various directions on the Brillouin zone points to efficient separation and low recombination of photo-generated charge carriers in the \(\alpha-\) and \(\beta-\text{SrZrS}_3\) materials, which is necessary for the fabrication of highly efficient solar device.

| Material   | Direction | \(m^*_{\alpha}(m_e)\) | \(m^*_{\beta}(m_e)\) | \(D = m^*_{\alpha}/m^*_{\beta}\) |
|------------|-----------|------------------------|------------------------|----------------------------------|
| \(\alpha-\text{SrZrS}_3\) | \(\Gamma-X\) | 0.011 | 0.004 | 2.75 |
|            | \(X-S\) | 0.010 | 0.007 | 1.43 |
|            | \(S-Y\) | 0.015 | 0.013 | 1.15 |
|            | \(Y-\Gamma\) | 0.080 | 0.003 | 26.67 |
|            | \(\Gamma-Z\) | 0.007 | 0.005 | 1.40 |
|            | \(Z-U\) | 0.020 | 0.004 | 5.00 |
|            | \(U-R\) | 0.016 | 0.005 | 3.20 |
|            | \(R-\Gamma\) | 0.023 | 0.049 | 0.47 |
|            | \(\Gamma-\Gamma\) | 0.021 | 0.004 | 5.25 |
| \(\beta-\text{SrZrS}_3\) | \(\Gamma-X\) | 0.054 | 0.004 | 13.50 |
|            | \(X-S\) | 0.014 | 0.003 | 4.67 |
|            | \(S-Y\) | 0.017 | 0.067 | 0.25 |
|            | \(Y-\Gamma\) | 0.026 | 0.011 | 2.36 |
|            | \(\Gamma-Z\) | 0.017 | 0.005 | 3.40 |
|            | \(Z-U\) | 0.037 | 0.005 | 7.40 |
|            | \(U-R\) | 0.007 | 0.003 | 2.33 |
|            | \(R-\Gamma\) | 0.012 | 0.015 | 0.80 |
|            | \(\Gamma-\Gamma\) | 0.009 | 0.008 | 1.13 |

3.4. Optical Properties

The calculated real (dispersive, \(\varepsilon_1\)) and imaginary (absorptive, \(\varepsilon_2\)) parts of the dielectric function for \(\alpha-\text{SrZrS}_3\) and \(\beta-\text{SrZrS}_3\) are shown in Figures 6 and 7, respectively. The dielectric constant is
predicted at 9.36 for $\alpha$-SrZrS$_3$ (Figure 6a) and 15.75 $\beta$-SrZrS$_3$ (Figure 7a). The predicted high dielectric constants are desired properties for photovoltaics applications as a dielectric constant value of 10 or more is good enough to obtain exciton binding energy ($E_b$) value lower than 25 meV at room temperature [48]. The absorbance of $\alpha$-SrZrS$_3$ (Figure 6b) starts at around 1.5 eV, close to its band gap, but with negligible absorption until after 2 eV. The absorption of $\beta$-SrZrS$_3$ (Figure 7b) starts at around 2.0 eV, which corresponds to its fundamental band gap. Owing the orthorhombic crystal symmetry of $\alpha$- and $\beta$-SrZrS$_3$, the absorption coefficient, reflectivity and refractive index plotted along the three the crystallographic directions: x, y, and z directions ([100], [010], and [001]) are found to be anisotropic. The absorption coefficient of a material represents its light harvesting ability, which is very necessary as it has great effects on the power conversion efficiency of the resulting solar cells. The high absorption coefficient is desired in solar cell applications. The calculated absorption coefficient, reflectivity and refractive index are shown in Figures 6 and 7. A high absorption coefficient in the order of $10^5$ cm$^{-1}$ is predicted for both $\alpha$- and $\beta$-SrZrS$_3$ in the visible light region, which make them suitable for the photovoltaic application. The $\beta$-SrZrS$_3$ phase shows stronger absorption around 2 eV than $\alpha$-SrZrS$_3$ phase.

Figure 6. Calculated (a) dielectric function, (b) absorbance, (c) reflectivity and (d) refractive index of $\alpha$-SrZrS$_3$.

The reflectivity and refractive index are two important parameters necessary for solar applications. The reflectivity gives a measure of reflecting light or radiation. When it comes to solar cells, the less the material surfaces reflect a sun’s rays, the more energy can be generated. The refractive index of a material, on the other hand, shows its transparency. The optical reflectivity of $\alpha$-SrZrS$_3$ (Figure 6c) shows a high reflectivity in the y–direction, starts at about 30.2% and reaches a maximum value of about 68.2% at an energy of about 3.8 eV. The static reflectivity in the x, y, and z directions are predicted at about 23%, 30%, and 26%, respectively. This indicate that the least reflection occurs in the z direction. The calculated static reflectivity of $\beta$-SrZrS$_3$ (Figure 7c) is predicted to be about 30%, 34% and 38% in the y, z, and x directions, respectively. The reflectivity reaches a maximum (82.2%) at an energy of about 3.5 eV. The high reflectivity in the visible region could cause a significant loss in solar cell efficiency of devices fabricated. Optical losses from reflected light from the front surface can be reduces through surface texturing and anti–reflection coatings. The refractive index is predicted in the range of
2.8–3.5 for $\alpha$–SrZrS$_3$ (Figure 6d) and 3.5–4.0 for $\beta$–SrZrS$_3$ (Figure 7d). The calculated refractive indexes for $\alpha$– and $\beta$–SrZrS$_3$ are similar to the refractive index of Si ($\eta = 3.4$ at 550 nm) [49].

![Figure 7](image_url). Calculated (a) dielectric function, (b) absorbance, (c) reflectivity and (d) refractive index of $\beta$–SrZrS$_3$.

4. Summary and Conclusions

We performed comprehensive first–principles GGA and hybrid DFT investigations the structures and properties $\alpha$–SrZrS$_3$ and $\beta$–SrZrS$_3$ transition metal chalcogenide perovskites. Both $\alpha$– and $\beta$–SrZrS$_3$ materials demonstrated to be mechanically stable at ambient conditions, based on their calculated single–crystal elastic constants. The predicted electronic structures show that both $\alpha$– and $\beta$–SrZrS$_3$ are direct band gaps absorbers with band gap of calculated at 1.38, and 1.95 eV, respectively, in close agreement with estimates from diffuse–reflectance measurements. Based on the dielectric functions obtained, we show that $\alpha$– and $\beta$–SrZrS$_3$ have strong light absorption in the visible region, as reflected in their high optical absorbance (in the order $10^5$ cm$^{-1}$). The $\beta$–SrZrS$_3$ shows a stronger absorption around 2 eV than $\alpha$–SrZrS$_3$. The first theoretical prediction of effective masses of photo-generated charge carriers, in $\alpha$– and $\beta$–SrZrS$_3$ materials, suggest high-mobility (high-conductivity) and low recombination rate of photo-carriers in these materials, making them attractive for solar cell and other optoelectronic applications.

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