Drive-Tolerant Current Residual Variance (DTCRV) for Fault Detection of a Permanent Magnet Synchronous Motor Under Operational Speed and Load Torque Conditions

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ABSTRACT This paper proposes a novel method that uses stator current signals to detect motor faults under operational speed and load torque conditions. Previous studies on motor current signature analysis (MCSA) have been devoted to developing methods to detect faults in non-stationary conditions; however, they have limitations. Conventional methods require much domain knowledge or parameter selection for signal decomposition, and are applicable under limited variable conditions. Thus, this paper proposes a new feature, drive-tolerant current residual variance (DTCRV), for fault detection. This new approach requires no domain knowledge and is applicable under varying speed and load torque conditions. In the proposed method, first, the envelope of the current signal is calculated to extract its modulation. Second, the drive-related signal, which greatly varies based on speed and load torque conditions, is extracted from the enveloped current signal. Third, the drive-tolerant current residual (DTCR) is calculated; the DTCR is defined as the subtraction of the drive-related signal from the enveloped current signal. Finally, the new health feature is calculated as the variance of the DTCR. To demonstrate the proposed method, experimental studies were conducted under several operating conditions (i.e., different speed profiles and load torque levels) with two fault modes: 1) a stator inter-turn short and 2) misalignment. Results confirm the ability of DTCRV to promptly and accurately detect faults in a variety of conditions; in contrast, conventional methods are greatly affected by the operating conditions.

INDEX TERMS Current analysis, fault detection, permanent magnet motors, time-varying condition, variable speed.

I. INTRODUCTION

Industrial motors are widely used in lots of manufacturing processes and permanent magnet synchronous motors (PMSMs), which are one type of industrial motors, are usually integrated into many types industrial equipment that perform precise control, such as industrial robots, cooperative robots, and CNC machines [1]–[3]. Since a trivial fault in any of the numerous PMSMs in a manufacturing line can cause huge economic loss due to downtime and defective items, many studies have been conducted to develop a robust fault-detection method for PMSMs [4], [5]. Many studies on fault detection can be categorized as model-based approach and signal processing-based approach in general [6]–[10]. Among several signals that have been used for the signal processing-based fault detection, the stator current signal has emerged as the most generally analyzed signal for monitoring the health condition of PMSMs and
the load components in rotating systems; this analysis is called motor current signature analysis (MCSA) [11], [12]. Despite continuous development of MCSA, practical application of the approach is difficult in modern industrial systems, where non-stationary operating conditions (i.e., various speeds and load torques) are prevalent [13]–[17]. The signal deformation that results from these variable drive-related conditions makes it difficult to identify the fault-related fluctuations because the drive-related current signals are dominant in the non-stationary conditions of normal operation.

To address this issue, several previous studies have tried to detect motor faults by examining transient current signals. Time-frequency analysis (TFA) represents signals in the time-frequency domain; therefore, the spectral properties of signals can be shown in time-series. Most previous research using TFA has investigated the trend of coefficients according to the particular fault frequency [18]. In [19]–[22], the energy around fault characteristic frequency was computed in Wigner-Ville distribution (WD), and its behavior on speed and load variations were investigated. Similarly, the harmonic order tracking method was developed to identify rotor faults using Garbor transformed current signals [23]. The TFA-based approaches, however, require motor-specific domain knowledge (e.g., fault frequencies, the number of poles, rotating frequencies) and usually time-consuming. The signal decomposition-based approaches can be one of the ways to avoid the challenge of TFA-based approaches. The discrete wavelet transform (DWT), which decomposes a signal using high- and low-pass filters with particular mother wavelets, was applied to detect a motor fault by utilizing the detail signals in DWT that revealed the fault patterns [24]–[27]. In [28], DWT decomposed the current signal of which the fundamental component was removed by the adaptive filter to detect faults under variable driving conditions. Also, the intrinsic mode function (IMF) calculated by empirical mode decomposition (EMD) was investigated to extract the information related to faults in the current signals. Several fault indicators were developed to detect faults under non-stationary condition, such as the degree of fluctuations of IMFs [29], [30], the energy of IMFs [31], and the instantaneous amplitude of IMFs computed by the Hilbert-Huang transform (HHT) [32], [33]. The signal decomposition-based approaches, however, demand the selection of the particular bandwidth or decomposition level that is sensitive to the fault. Furthermore, the aforementioned TFA-based and signal decomposition-based approaches have not been validated to detect faults with one criterion under various speed profiles. In Section IV, the effectiveness of the proposed DTCRV method is confirmed through two experimental studies: 1) a stator inter-turn short and 2) misalignment. Section V summarizes the conclusions of the paper.

II. BACKGROUNDS

This section briefly explains the background of the stator current signal from the perspective of operating conditions and for fault diagnosis. Next, several previous studies that have used the stator current signals for fault diagnosis are summarized; further, we outline the challenges of the prior methods when applied in various speed and load torque conditions.

A. THE RELATION OF THE STATOR CURRENT AND DRIVING CONDITIONS

The electromagnetic torque $T_e$ is a torque produced by the interaction between the magnetic field and the stator current in a motor. For a PMSM, $T_e$ can be expressed as [34]

$$T_e = \frac{3p}{2} [\phi_i q + (L_d - L_q)i_d i_q]$$  \hspace{1cm} (1)

where $p$ is the number of poles, $\phi$ is the flux linkage generated by the permanent-magnet poles of the rotor, $i_d$, $i_q$ and $L_d$, $L_q$ are the stator currents and inductances of the $d$- and $q$-axis, respectively. $i_d$ and $i_q$ are the values converted from the three-phase stator currents using dq-transform for pursuing convenience in control. In the case of field-oriented control systems, which are generally used for servo-systems, $i_d$ is
TABLE 1. Fault characteristic features in the current spectrum.

| Fault mode                          | Fault characteristic frequencies in the current spectrum $f_c$ |
|-------------------------------------|---------------------------------------------------------------|
| Stator inter-turn short             | $f_c = 3f_r$ [16], [38], [39], $f_c \pm nf_r$ [40], [41]    |
| Mechanical faults caused by load torque oscillation (e.g., unbalance, misalignment, bearing faults) | $f_c = f_r \pm nf_r$ [19]–[23]                                    |

interpreted to be proportional to $T_e$, because the flux of the $d$-axis is controlled to be continuously aligned with $i_d$ [35]. Considering the surface-mounted PMSM, which has the same $L_q$ and $L_d$ value, $T_e$ and the electromechanical torque equation can be expressed as

$$T_e(t) = k_i i_d(t) = J \frac{d}{dt} \omega_r(t) + B \omega_r(t) + T_L(t)$$  \hspace{1cm} (2)

where $k$ is the torque constant, $J$ is the inertia of the rotating system, $B$ is the friction coefficient, $\omega_r(t)$ is the rotating speed, and $T_L(t)$ is the load torque. From (2), the driving conditions (i.e., load component, velocity, and acceleration) are confirmed to affect not only $T_e(t)$, but also $i_d(t)$, which is the converted value of the stator current signals.

B. STATOR CURRENT SIGNATURE DUE TO FAULTS

Several mechanical faults, (e.g., misalignment, unbalance and bearing wear) make the airgap non-uniform [20]. This state is called eccentricity. The non-uniform airgap affects the permeance, which is inversely related to the airgap length as

$$\Lambda(t, \theta) = \frac{\mu_0}{g} (1 + \delta_s \cos(\theta - \varphi_s) + \delta_d \cos(\omega_r t - \theta))$$  \hspace{1cm} (3)

where $\mu_0$ is the permeability of air, $g$ is the nominal airgap length, $\varphi_s$ is the angle of the minimum airgap position due to the static eccentricity, and $\theta$ is the circumference angle. $\delta_s$ and $\delta_d$ are the normalized degree of static and dynamic eccentricity [36], [37]. Considering the fundamental harmonic term, the magnetomotive force (MMF) can be approximated as

$$F(t, \theta) = F_1(t) \cos(\omega t - \rho \theta)$$  \hspace{1cm} (4)

where $F_1(t)$ denotes the major amplitude of MMF, and $\omega$ is the electric rotating speed. Then, the airgap flux density $B$ is defined as the product of MMF and the permeance as

$$B(t, \theta) = F(t, \theta) \cdot \Lambda(t, \theta)$$

$$= K_B(t)[B_c + B_m \cos(\omega_r t - \theta)] \cos(\omega t - \rho \theta)$$  \hspace{1cm} (5)

$$V(t) = Ri(t) + \frac{d}{dt} \Phi(t)$$  \hspace{1cm} (6)

where $K_B(t)$ is $F_1(t) \mu_0/g$, $B_c$ is $1 + \delta_s \cos(\theta - \varphi_s)$, $B_m$ is $\delta_d$, $R$ is stator resistance, and $V(t)$ is power supply voltage. As $B$ is the derivative of the flux $\Phi(t)$, the stator voltage equation (as in (6)) implies that the major component of the stator current can be expressed as

$$I(t) = K_i i_d(t) + I_m \cos(\omega_r t - \varphi_m) \cos(\omega t - \rho \theta)$$

$$= I_1(t) \cos(\omega t - \rho \theta) + \alpha_1 I_1(t) \cos((\omega + \omega_r) t - \varphi)$$  \hspace{1cm} (7)

where $K_i$, $I_c$, and $I_m$ are the corresponding terms of $K_B(t)$, $B_c$, and $B_m$, respectively. $I_1(t)$, $\varphi$, $\varphi_m$, and $\alpha$ are the coefficients and phases of the stator current’s major components, including the terms related to the static and dynamic eccentricity, and $\varphi$ is the modulation index. Based on (7), the faults can be confirmed by investigating the amplitude modulation (AM) in the stator current signals. Also, the electrical faults represented by stator turn shorts affect the stator current by showing odd multiples of the supply frequency’s third harmonics [16], [38], [39], or AM of the rotating frequency [40], [41]. Therefore, the AM of the stator current can be observed in both the mechanical and electrical fault states of a rotating system.

C. BRIEF REVIEW OF FAULT DIAGNOSIS USING THE STATOR CURRENT IN TIME-VARYING CONDITIONS

TABLE 1 summarizes the fault characteristic frequencies $f_c$ in the current spectrum, which were used in previous studies, where $f_c$, $f_r$ are the supply and rotating frequency, respectively, and $n = 1, 2, 3, \ldots$ Since $f_c$ cannot be applied to non-stationary conditions directly due to the time-varying $f_c$ and $f_r$, several studies have conducted TFA to track the magnitude of $f_c$ in the time-frequency domain [19], [22], [23]. In particular, WD has been widely used to calculate the features in the time-frequency domain [19], [22], and pseudo-WVD (PWD) often replaces WD to compensate for interference terms in practical applications [20]. For example, the energy of $3f_c$ could be extracted for investigating stator inter-turn shorts; the energy around $f_c \pm f_r/2$ could be calculated to investigate mechanical faults using PWD. These TFA-based approaches require several motor-specific information and the speed profile to compute the time-varying characteristic frequencies. Therefore, signal decomposition techniques (e.g., DWT [24]–[28], EMD [29]–[31], HHT [32], [33]) have been adopted to readily extract the fault-related components. When DWT was used, the energy of the specific detail signals could be calculated for the health feature [26], [27]. The specific detail signals were selected based on an observation of the fault-pattern. When EMD [29]–[31] or HHT [32], [33] was used, the IMFs that reveal the fault-related components were investigated after decomposing the drive-related components in the preceding IMFs. However, the observation of the appropriate decomposed signals containing fault information is difficult for the signal decomposition based approach. In addition, most of the aforementioned studies were validated under only

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variable-speed profiles. Therefore, the application of these conventional methods for real driving conditions – in which the speed varies under several load torque conditions – is uncertain.

III. THE PROPOSED DTCRV METHOD
This section presents the proposed DTCRV method to detect faults under operational speed and load torque conditions. Fig. 1 offers a flowchart of the proposed method. The details of each step are described in Sections A and B, focusing on the principle of the proposed method. In Section C, the contribution and advantages of the proposed method are explained with the comparison of the conventional methods.

A. EXTRACTION OF THE DRIVE-RELATED SIGNAL
Since the raw stator current signal consists of a fundamental driving sinusoidal wave and other harmonics that can be generated by the controller, faults, or other factors, the envelope of the raw stator current signal is firstly extracted. Based on (7), the major component of the raw stator current signal can be expressed as

\[ x(t) = I_1(t) \cos(2\pi f_1 t) + \alpha I_1(t) \cos(2\pi (f_s \pm f_k) t + \varphi_k) \]  

(8)

where \( I_1(t) \) is the modulation index; \( f_k \) and \( \varphi_k \) are the frequency and phase angle of the fault, respectively. Then, the analytic signal of \( x(t) \) using HT can be related to the amplitude of the enveloped current signal as

\[ x_a(t) = x(t) + j\tilde{x}(t) = x_m(t)e^{j\varphi(t)} \]  

(9)

where \( x_a(t) \) is the analytic signal of \( x(t) \), \( \tilde{x}(t) \) is the HT result of \( x(t) \) that is \( \pi/2 \) phase-shifted, \( x_m(t) \) is the amplitude of \( x_a(t) \), and \( \psi(t) \) is the instantaneous phase. Based on Section II-B, the information about the fault-related AM is expected to be carried in \( x_m(t) \). \( x_m(t) \) conserves the magnitudes of \( x(t) \), while it reduces the effect of high-frequency noises that are usually induced from a variable frequency drive. In this study, the upper signal of \( x_m(t) \), denoted as \( \text{ENV}(t) \), is used.

Next, the drive-related signal is extracted from \( \text{ENV}(t) \). In a balanced three-phase system, the magnitude of \( x_m(t) \) is proportional to \( T_c(t) \); therefore, \( \text{ENV}(t) \) can be expressed from (2) as

\[ \text{ENV}(t) \propto ki_q(t) \]  

(10)

Based on the fact that \( i_{q}(t) \) is the result of \( dq \)-transformation of the three-phase \( x(t) \), \( i_{q}(t) \) can be written from (8) as

\[ i_q(t) = I_1(t) \cos(2\pi f_1 t - \theta_0) + \alpha I_1(t) \cos(2\pi (f_s \pm f_k) t + \varphi_k - \theta_0) \]  

\[ = I_1(t) \cos(\theta_p) + \alpha I_1(t) \cos(\pm 2\pi f_k t + \varphi') \]  

(11)

where \( \theta_0 \) is set to \( 2\pi f_k t + \theta_p \); \( \theta_p \) is the constant phase angle, and \( \varphi' \) is \( \varphi_k - \theta_p \). Also, the right-hand side of (2) can be rewritten to include the torque oscillations and spatial harmonics as

\[ (J \frac{d}{dt} \omega_r(t) + B\omega_r(t) + T_c) + \sum_{n=1}^{\infty} T_n(t) \cos(2\pi f_{n} t + \varphi_n) \]  

(12)

where \( T_c \) is the constant load torque, \( T_n \), \( f_n \), and \( \varphi_n \) are the amplitude, frequency, and phase angle for torque oscillations and spatial harmonics.
oscillations respectively. When (11) and (12) are incorporated into (2), the torque-current mechanism can be described as

\[ kI_1(t) \cos(\theta_\rho) + k\alpha I_1(t) \cos(\pm 2\pi f_k t + \varphi') = (J \frac{d}{dt} \omega_r(t) + B\omega_r(t) + T_r) + \sum_{n=1}^{\infty} T_n(t) \cos(2\pi f_n t + \varphi_n) \]

(13)

Sequentially the first term in the left-hand side corresponds to the first term in the right-hand side, which is related to the driving condition. Also, \(ENV(t)\) is proportional to (13) based on (10) as

\[ ENV(t) \propto (J \frac{d}{dt} \omega_r(t) + B\omega_r(t) + T_r) + \sum_{n=1}^{\infty} T_n(t) \cos(2\pi f_n t + \varphi_n) \]

(14)

The first term in the right-hand side of (14) can be matched to the dominant linear trend of \(ENV(t)\) in the case of constant acceleration. Although the motion of manufacturing machines is complicated, the speed profile of a servo motor usually consists of constant acceleration, short or no constant speed, and deceleration.

Fig. 2 shows the procedure of extracting the dominant trend from \(ENV(t)\) in the driving condition, which consists of constant acceleration, constant speed, and constant deceleration. The dominant trend of \(ENV(t)\) changes linearly as the speed changes linearly in a uniform acceleration region. When the driving condition changes from acceleration to stationary, \(ENV(t)\) changes rapidly as \(Jd\omega_r(t)/dt\) in (14) disappears and becomes proportional to the level of load torque. Based on the association of the dominant trend of \(ENV(t)\) and the driving condition, the linear trend of \(ENV(t)\) is determined to be the drive-related signal \(D(t)\). Before extracting \(D(t)\), the gradient of \(ENV(t)\), which is denoted as \(G(t)\), is computed for subdivision. When the driving condition is switched, \(ENV(t)\) changes drastically; thus, the transition time can be captured at the large gradient points. After subdividing \(ENV(t)\) into several sections, linear regressions of \(ENV(t)\) in each section are calculated. Then, \(D(t)\) is defined as the union of linear estimation. In Fig. 2., \(G(t)\) has two peak points at the transition time, and \(D(t)\) can be determined as the combination of the linear estimations in three subsections that \(G(t)\) divides.

Unlike the previous approaches that decomposed the non-stationary current signal empirically or removed the fundamental current signal using specific filters, the proposed DTCRV method readily extracts the drive-related components which are induced from the torque-current mechanism. The linear regressed \(D(t)\) is a strict equation-based extraction; however, several filters (e.g., moving average or low-pass) can be substituted for the linear regression and applied to various driving conditions.

B. DRIVE-TOLERANT CURRENT RESIDUAL

Using \(D(t)\) which is determined in advance, the drive-tolerant current residual \(DTCR(t)\) can be calculated by the subtraction of \(D(t)\) from \(ENV(t)\) as

\[ DTCR(t) = ENV(t) - D(t) \]

(15)

After \(D(t)\) is subtracted, the dependence of \(DTCR\) on the driving condition becomes small; therefore, the influences that are not related to the driving conditions are prominent in the DTCR. Also, the fluctuations caused by faults receive more attention. Then, the variance is calculated to arrive at a representation of \(DTCR\), which is defined as

\[ DTCRV = E[(DTCR(t) - \mu)^2] \]

(16)

where \(\mu\) is the average of \(DTCR(t)\). \(DTCRV\) can be interpreted as the energy of the \(DTCR\), since the energy of the time-series signal is usually defined as a summation of the squared signal and the mean of the \(DTCR\) would be zero in the ideal case. When \(D(t)\) does not include all time-varying effects, the \(DTCR\) could have a bias induced by a complicated driving condition; thus, the variance can compensate for the bias error of the \(DTCR\).

C. THE CONTRIBUTION AND ADVANTAGES OF DTCRV

Through the proposed DTCRV method, the stator current signals under operational driving conditions can be readily utilized to evaluate the health condition of a motor. It is beneficial that the DTCRV method, which is developed on the basis of physical relations between the torque and current
TABLE 2. Comparison of the proposed DTCRV and two conventional approaches.

|                                | Proposed (DTCRV) | TFA-based approach (e.g. PWD) | Signal decomposition-based approach (e.g. DWT, EMD, HHT) |
|--------------------------------|------------------|-------------------------------|--------------------------------------------------------|
| Required information about the fault | None             | Fault characteristic frequency | Decomposition level that fault patterns reveal |
| Required information about the driving conditions | None | Speed profile | Load torque (optional) |
| Parameter dependency           | Low              | Low                           | High                                                   |
| Time-cost                      | Low              | High                          | Low                                                    |

of a motor, can be applied with less expertise. To precisely describe the contribution and advantages of the DTCRV, it is compared with two conventional approaches (i.e., TFA-based and signal decomposition-based). TABLE 2 summarizes the comparisons described below. The proposed DTCRV method does not require any information about the fault. In contrast, the two conventional approaches are based on the extraction of fault-related components. Therefore, the two conventional methods are limited to situations where the fault-related information is pre-assigned, such as fault characteristic frequency over time and the decomposition level that the fault patterns reveal. The DTCRV method also does not require any information about the driving condition; instead, it adaptively decreases the effect of speed and load torque conditions by subtracting the linear components in the current envelope. For the TFA-based approach, the speed profile is essential for calculating the characteristic frequency. The load torque condition is optionally used to attempt to compensate for its influence. Furthermore, the DTCRV is less susceptible to the parameter settings and its time-cost is low because the entire process of DTCRV is automatically handled in the time-domain. In contrast, the time-cost for the TFA-based approach is high due to the computation of many convolutions. The signal decomposition-based approach is highly affected by several parameters, such as the type of wavelet function and the appropriate band using the DWT method, or the selection of proper IMFs using the EMD and HHT methods. Finally, the DTCRV method can highlight the current fluctuations through the automatic reduction of drive-related signals.

IV. EXPERIMENTAL STUDIES

To validate the effectiveness of the proposed method, two experimental studies were explored: 1) a stator inter-turn short (SIS) and 2) misalignment (MSGN). This section first describes the experimental settings used to acquire the datasets and then discusses the results of the proposed method. Both cases also include a comparative analysis with other previously published health features, which were described in Section II-C, to confirm the superiority of the proposed method.

A. DESCRIPTION OF THE EXPERIMENTAL SETUP

For the target motor, a 200W-5.5Nm, 20-pole, surface-mounted PMSM embedded in 4th axis of a cooperative robot was used (See Fig. 3 (a), (c)). Fig. 3(b) shows the test rig setup used in the experiment. The target PMSM was position-controlled using an incremental encoder, of which the resolution was 4000 pulses per revolution. A hysteresis brake (Magtrol, BHB-3BA) was connected to the motor shaft via couplings; a torque meter (Unipulse, UTM-II) was installed between two couplings to measure torque and speed. The three-phase stator current signals were measured by current probes (Tektroniks, A622), which were mounted between the servo drive and the motor. All signals were collected with a sampling rate of 12.8 kSa/s using an NI-system (C-RIO9066). All driving conditions that were used in the experiment are summarized in TABLE 3; two speed profiles (named trapezoidal and triangle) with five load torque conditions (0%, 30%, 50%, 70%, 100% of the rated load torque),
respectively, were studied. The trapezoidal profile was configured by controlling a motor with 100 revolutions in 3 seconds, and the triangle profile was configured by controlling a motor with 50 revolutions in 2 seconds. Among all experimental conditions, the three load torque conditions (0%, 50%, 100%) of each speed profile in normal (NOR) and fault level 2 are described in the figures for representative comparison.

### B. EXPERIMENT 1: STATOR INTER-TURN SHORT (SIS)

First, an SIS was emulated by coiling the uncovered windings in the production stage. Fig. 4 shows a faulty stator, in which a portion of the windings were chemically uncovered. Two motors with different fault levels, where the degrees of uncovered windings were different, were used in the experiment. TABLE 4 describes the measured impedance (resistance, inductance) of the two SIS and NOR motors; the uncovered windings were coiled up only in the a-phase.

![Inter-turn short windings of SIS2](image-url)

Fig. 5 shows the procedure for calculating DTCR from the raw current signal in several driving conditions of NOR; Fig. 6 shows calculation for SIS2. Comparing the raw current of Fig. 5 and 6, the modulation caused by SIS can be confirmed; the enlarged parts of Fig. 5(b) and Fig. 6(b) obviously show the severity of modulation due to SIS at the constant speed region. From all $\text{ENV}(t)$ of each driving condition in Fig. 5 and Fig. 6, it can be seen that $\text{ENV}(t)$ was highly influenced by the speed variation and load torque level. The amplitude trend of $\text{ENV}(t)$ was largely dominated by the speed variation and was simultaneously proportional to the load torque level. So DTCRs were obtained according to the procedure as described in Fig. 1. $G(t)$, which was calculated to set the criteria for subdividing $\text{ENV}(t)$, had peak points when the speed profile was drastically changed, regardless of the health state of the motor. There appeared two peak points in Fig. 5(a-c) and Fig. 6(a-c), while only one appeared in Fig. 5(d-f) and Fig. 6(d-f). Next, $D(t)$ was regressed in each section that the peaks of $G(t)$ divide. Then DTCRs were obtained by subtracting $D(t)$ from $\text{ENV}(t)$. The small difference of DTCRs under variable speed and load torque levels indicated the tolerance of DTCR to driving conditions, as shown in DTCRs in Fig. 5. While the difference of DTCRs depending on driving conditions was small in Fig. 6, DTCRs of Fig. 6 highly fluctuated compared to those of Fig. 5. Therefore, we can confirm that the influence of SIS on DTCR was larger than that of the driving conditions. Furthermore, DTCRs were occasionally amplified at the transient regions in the case of SIS. Not only the instantaneous irregularities that occur right after the speed transition but the deterioration of the stator windings where the current flows could aggravate the fluctuation of DTCR, as shown in the transient sections of DTCRs in Fig. 6.

Fig. 7 shows the results of each feature (i.e. $E_{\text{PWD}}$, $E_{\text{DWT}}$, $E_{\text{HHT}}$, and DTCRV), as determined using the PWD, DWT, HHT, and the proposed DTCRV methods, respectively. Each feature was normalized with an average feature value of NOR. $E_{\text{PWD}}$, $E_{\text{DWT}}$, $E_{\text{HHT}}$ were calculated based on the conventional methods described in Section II-C. For $E_{\text{PWD}}$, the magnitudes of the coefficients of PWD around $3f_s$ were mean-squared over time. For $E_{\text{DWT}}$, the fifth detail signal, $d_5$ was selected and calculated as the sum of squares based on the fact that the frequency band of $d_5$ was from 1 kHz to 2 kHz, which contains the characteristic frequency in the constant-speed region, of which the fundamental frequency was 500 Hz. For $E_{\text{HHT}}$, the third IMF of the raw current signal was extracted, and the variance of its instantaneous amplitude was computed. As can be seen in Fig. 7, DTCRV outperformed the other methods by detecting SIS with one criterion. $E_{\text{PWD}}$ and $E_{\text{DWT}}$ had the similar values between two speed profiles, but highly dependent on the load torque...
TABLE 4. The impedance of the motors used in the SIS experiment.

| Phase | Nor | SIS1 | SIS2 |
|-------|-----|------|------|
| Resistance (Ω) |     |      |      |
| a     | 0.37| 0.36 | 0.35 |
| b     | 0.37| 0.37 | 0.38 |
| c     | 0.37| 0.37 | 0.38 |

| Inductance (mH) | 250 Hz | 500 Hz |
|-----------------|--------|--------|
| a               | 0.33   | 0.33   |
| b               | 0.33   | 0.33   |
| c               | 0.32   | 0.32   |

FIGURE 5. The procedure for calculating DTCR in NOR: [speed profile, load torque] (a) [Trapezoidal, 0%], (b) [Trapezoidal, 50%], (c) [Trapezoidal, 100%], (d) [Triangle, 0%], (e) [Triangle, 50%], and (f) [Triangle, 100%].

TABLE 5. Performance of SIS detection and average time-cost for calculating one feature.

| Features | DTCRV (Proposed) | E_{PWD} [19] | E_{DWT} [26] | E_{HHT} [32] |
|----------|------------------|--------------|--------------|--------------|
| Performance measure | FDR | 4.919 | 0.034 | 0.027 | 0.002 |
|                  | PoS  | 0.959 | 0.091 | 0.082 | 0.019 |
| Time-cost        | 0.007±0.002 sec | 46.664±4.317 sec | 0.004±0.004 sec | 0.028±0.005 sec |

level as shown in Fig. 7(b, c). Since $E_{PWD}$ and $E_{DWT}$ of SIS in low load torque condition were smaller than those of NOR in high load torque condition, only SIS2 under 100% load torque level was detectable. Through the result, we can determine that the effect of load torque condition was difficult to be suppressed or separated using PWD or DWT. $E_{HHT}$ showed the deficient performance with widespread values in all driving conditions (See Fig. 7(d)). The inferior performance of $E_{HHT}$ might be due to the unstable extraction of IMF which is conducted empirically.
The procedure for calculating DTCR in SIS2: (a) [Trapezoidal, 0%], (b) [Trapezoidal, 50%], (c) [Trapezoidal, 100%], (d) [Triangle, 0%], (e) [Triangle, 50%], and (f) [Triangle, 100%].

Results of the proposed and the conventional methods under SIS: (a) DTCRV, (b) PWD, (c) DWT, (d) HHT.

TABLE 5 quantitatively shows the performance of SIS detection using two measures for class separation: 1) the Fisher discriminant ratio (FDR) [42] and 2) the probability of separation (PoS) [43]. DTCRV had an overwhelmingly better separation capacity in both measures. The outstanding performance of DTCRV was possible because its techniques,
which suppress the drive-related components, enhanced its sensitivity to the fault. Further, it is noticeable that the unit computing time of DTCRV was significantly faster than that of \( \text{E}_{\text{PWD}} \) and \( \text{E}_{\text{HHT}} \), as can be seen in TABLE 5. All the time-costs were measured under i7-6700K CPU with 32GB RAM. The faster computing time of DTCRV than \( \text{E}_{\text{PWD}} \) was attributed to its calculation in the time-domain only. The repeated convolutions to convert signals in the time-domain to the time-frequency domain are not required for DTCRV. Also the reason for the fast computing time of DTCRV than \( \text{E}_{\text{HHT}} \) was that the procedure of determining the drive-related signal of DTCRV was much simpler than calculating local maxima and local minima. The results of DTCRV in 50% load torque conditions were sometimes low, as shown in Fig. 7(a). These results could be explained based on the influence of the control system in deceleration. The motors were forced to stop in the commanded time in different load torque levels and the load torques were also used in deceleration. When the load torque was low, the output torque had to be replenished for the on-time stop; when the load torque was high, the output torque for hindering fast deceleration was required. This explanation was supported by checking the deceleration regions of Fig. 5 and 6. However, it is important to note that DTCRV showed remarkable performance when subjected to both speed profile and load torque variations, although it was affected by the control in deceleration.

### C. EXPERIMENT 2: MISALIGNMENT (MSGN)

To investigate a mechanical fault, MSGN was emulated by rearranging the vertical height of the motor, as shown in Fig. 8. Two fault levels (2 mm and 4 mm) were used in the experiment.

Fig. 9 shows the procedure for calculating DTCR from the raw current signal in several driving conditions of MSGN2. Comparing the raw current signals in Fig. 9 with those of the corresponding operating conditions in NOR (shown in Fig. 5), the amplitude became larger. This was because much output torque was required to compensate for the interference, which MSGN induced to normal output torque. Also, \( \text{ENV}(t) \)'s of MSGN showed more peak shapes, while those of SIS had the form of modulation, as shown in the enlarged parts of Fig. 6(b) and Fig. 9(b), respectively. The large fluctuation of \( \text{ENV}(t) \) sometimes caused the oscillated \( G(t) \), as can be seen in Fig. 9 (a, b). Nevertheless, it was not hard to divide sections because the peak points of \( G(t) \) were determined relatively. Comparing DTCRs in Fig. 9 with those of Fig. 6, DTCRs in MSGN more fluctuated than those of SIS.
Through this large fluctuation, we can suggest that DTCR is more sensitive to mechanical faults.

Fig. 10 shows the results of each feature (i.e. $E_{PWD}$, $E_{DWT}$, $E_{HHT}$, and DTCRV), as determined using the PWD, DWT, HHT, and the proposed DTCRV methods, respectively. The normalization of each feature and the calculation of the conventional features were conducted in the same way described in Section IV-B. For $E_{PWD}$, the magnitudes of the coefficients of PWD around $f_s \pm f_r/2$ were mean-squared over time. For $E_{DWT}$, the seventh detail signal $d_7$ was selected and calculated as the sum of squares because the frequency band of $d_7$ was from 250 Hz to 500 Hz, which was able to contain the time-varying characteristic frequency $f_s \pm f_r$. For $E_{HHT}$, the second IMF of the raw current signal was extracted, and the variance of its instantaneous amplitude was computed. Like the results in Section IV-B, the behaviors of DTCRV were robust to variable speed profile and load torque conditions. From the results that $E_{PWD}$ and $E_{DWT}$ were proportional to the load torque level as shown in Fig. 10(b, c), the influence of the load torque levels on $E_{PWD}$ and $E_{DWT}$ seemed to be higher than that of MSGN. $E_{PWD}$ could detect MSGN at 70% and 100% load torque levels; however, MSGNs under 50% or less load torque levels were not distinguishable from NOR at 100% load torque level (See Fig. 10(b)). $E_{DWT}$ had a significant variance in each operating condition due to the insufficient signal decomposition; the characteristics of MSGN were concealed in the load torque conditions (See Fig. 10(c)). As shown in Fig. 10(d), $E_{HHT}$ was able to detect MSGN2 because the drive-related components were separated in the first IMF; however, $E_{HHT}$ could not detect MSGN1. While HHT was not able to detect SIS, it showed decent performance in MSGN detection. Through these irregular result of HHT, the effect of instability that the empirical procedure of HHT causes could be confirmed.

TABLE 6 quantitatively describes the performance and unit computing time of all the features, which were measured in the same state as in Section VI-B. The result of high FDR and PoS values with the small time-cost in DTCRV confirmed its outstanding performance compared to the other three features. Though both MSGNs showed the higher DTCRV values, as compared to those of NOR, the DTCRVs of MSGN1 and MSGN2 did not linearly increase, and DTCRVs of MSGN2 were spread in the trapezoidal speed profile case (see Fig. 10(a)). It seems possible that these results were due to the slight misalignment that resulted from the repeated experimental disturbances. However, it is noticeable that the proposed DTCRV approach can promptly detect the incipient MSGN without any information about the fault or driving conditions.

D. REMARKS OF DTCRV RESULTS
Through the results of two experimental studies, the DTCRV method have shown the noticeable performance as below:

| Speed profile | A – Trapezoidal | B – Triangle |
|---------------|-----------------|--------------|
| Load torque   | NOR 0% 30% 50% 70% 100% | MSGN 0% 30% 50% 70% 100% |

FIGURE 10. Results of the proposed and the conventional methods under MSGN: (a) DTCRV, (b) PWD, (c) DWT, (d) HHT.
TABLE 6. Performance of MSGN detection and average time-cost for calculating one feature.

| Features       | DTCRV (Proposed) | $F_{PWD}$ [19] | $F_{DWT}$ [26] | $F_{HHT}$ [32] |
|----------------|------------------|----------------|----------------|----------------|
| Performance   |                  |                |                |                |
| measure       | FDR              | 2.986          | 0.258          | 0.001          | 0.222          |
|                | PoS              | 0.873          | 0.433          | 0.016          | 0.254          |
| Time-cost     | 0.007±0.002 sec  | 44.113±3.396 sec | 0.004±0.007 sec | 0.027±0.007 sec |

1) DTCRV was able to detect a fault without being affected by the driving condition (i.e., speed profiles and load torque levels), while the conventional methods were dominated by the driving conditions.

2) Neither motor-specific information nor parameter settings for signal decomposition were required to calculate DTCRV.

3) The computational cost of DTCRV was low.

V. CONCLUSION

This paper proposed a new, drive-tolerant current residual variance (DTCRV) method for detecting faults under operational speed and load torque conditions. The proposed method extracted the envelope of the raw current signal to emphasize its modulation, which contains both drive-related and fault properties. Then, drive-related components were estimated using gradient-based linear regression. The DTCR, which was taken by subtracting drive-related components from the envelope signal, highlighted the unexpected oscillations from the abnormal state. Finally, the variance was computed to quantify the variation of the DTCR. Two case studies that investigated the different fault modes (i.e., SIS and MSGN) were demonstrated to validate the performance of the proposed approach. These case studies showed that the DTCRV method detected each fault under several driving conditions, while the conventional methods using PWD, DWT, and HHT suffered from the effect of driving conditions. The primary benefits of the proposed method are that it can detect an incipient abnormal state without requiring information about the fault or the driving condition. Moreover, the computational time of DTCRV is far less than that of the TFA-based approach, motor domain knowledge is not required, and the number of parameters that DTCRV demands is also less than that of both TFA-based and signal decomposition-based approaches. Future work can be conducted to identify fault modes considering control constraints under a wider range of driving conditions. Further, DTCRV will be investigated and applied to other motors embedded in industrial robots or electric vehicles.

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