Effect of rotor geometry on performance of 6/4 switched reluctance motors

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Abstract

This study investigates the effect of rotor geometry on performance in switched reluctance motors (SRM) using models analyzed by the 2-D Finite Element Method (FEM). All models have the same stator geometry, winding features, and air gap, but have different rotor geometries. The SRM model operates at nominal speed of 3000 rpm, with 6/4 pole and 150 W output power. Magnetic model analysis was undertaken for the 3 different rotor models. Electrical performance characteristics; speed, phase current, source current, efficiency, electromagnetic torque, and load torque were determined. Magnetic flux density and flux lines in the stator and rotor and the current densities in windings are presented. The optimal rotor model for SRM was determined by considering electrical and magnetic performance data.

Introduction

Switched Reluctance Motors (SRM) have become widely preferred in applications requiring high speed due to their superior characteristics including simple structure, low moment of inertia and high volume/power ratio. Their pole rotors do not contain structures such as collector, rings, magnets, brushes, or windings. In this way, the cost of the motor is decreased and the motor gains a robust and simple structure. In addition, the laminated rotor structure, which does not contain structures such as magnets or brushes, eliminates the decrease in efficiency caused by copper losses [1].

However, SRMs have disadvantages including vibration and noise due to the ripple in their torque [2]. Also, they require different driver circuits for different structures, and motion sensors for switch control [3,4].

In SRMs, the geometric structure of the motor directly affects the operating characteristics, and output parameters and the effect of factors, including pole arc width of rotor, air gap, skew angle of rotor and stator, stator/rotor pole number, pole embrace, and the truncation of pole corners, on SRM output performance have been investigated. In SRM, a change made to the rotor geometry leads to a change of rotor reluctance and inductance by affecting the flux path length and cross-section, which will affect torque and power in direct proportion to the square of the current [5].

The effect of the rotor pole angle on the electrical, mechanical and magnetic performance of the motor has been discussed in numerous studies [6-8]. The condition of the rotor pole arc being larger or smaller than the stator pole arc ($\beta_r > \beta_s$ and $\beta_s > \beta_r$) will change the reluctance of the magnetic circuit, which will lead to changes in inductance, input-output power, torque, and efficiency.
Other modifications have been made to improve performance. For example, Lee at al. [9] modified the rotor to include a 2 mm hole in each rotor pole of an SRM of 13.5 kW, which reduced torque ripple by 4.4%.

Other studies have found the ratio of the stator/rotor pole number to be important to the performance of the SRM and have determined that as the ratio, \( N_s/N_r \) (\( N_s/N_r = 6/4; 8/6; 12/8; 18/12 \)), is increased, radial forces cause stator vibrations and noise is increased. It is further concluded that current and moment characteristics affect the power and moment densities and decrease moment ripple [10,11].

In SRM design, it is known that pole embrace, which is proportional to the number of stator/rotor poles, affects efficiency due to average torque. In a study where stator pole width ratio was fixed at 0.35 and rotor width ratio varied over the range 0.3-0.5, the highest torque, highest efficiency and lowest torque ripple were achieved for a rotor pole width ratio of 0.5. This suggests that pole width should be increased in applications where high torque, high efficiency, and low torque ripple are desired. However, when pole width is increased, cost increases proportionally. Therefore, when high power is required or performance increased, pole width should be increased [12].

Most studies focus on the effect of rotor geometry on torque and torque ripple. This study also investigates electrical performance characteristics including shaft speed, phase current, source current, efficiency, electromagnetic torque, and load. The study also develops a visual presentation of the magnetic flux density in the stator and rotor, flux lines, and current density in windings. A 6/4-pole SRM was selected to investigate the effect of 3 rotor geometries on motor performance using analytic techniques and finite element analysis. Results from the 2-dimensional finite element analysis will allow the best rotor model to be determined for applications in an axial and radial fan.

### Materials and Methods

**Switched Reluctance Motor (SRM)**

When a current passes through a phase winding in an SRM, the torque in the motor will cause the rotor to move to the position of maximum inductance, resulting in rotation. If the rotor material is steel and there is no permanent magnetization, the direction of the current in the phase winding is not significant and the direction of torque is always towards the closest overlap position. In this way, the torque causes rotation in one direction, with movement occurring from the unaligned position to the aligned position, as shown in the sequence of the relative positions of rotor and stator in Figure 1 (a), (b), (c).

![Figure 1](image)

**Figure 1.** (a) Unaligned position, (b) Overlap position, (c) Aligned position

If the rotor and stator poles are symmetric, each phase can only generate torque in one direction according to the rotor pole arc angle. Therefore, at least two phases are needed to produce one-way torque in all rotor positions. If a current is passed through the winding while the rotor is rotating and it is in a position where the inductance is being reduced, a torque in an
opposing direction will be generated (known as braking or generator torque).

Torque ripple is high in SRMs. Smoother torque may be obtained by increasing the number of phases and including skew in the rotor. When the number of phases is increased, the electronic cost rises due to the greater number of switches in the driver. For low values of overall operating torque, the torque ripple in the three-phase motor can be reduced by the current profile. In practice, the phase current is reinforced in areas where there is torque descent [13-16].

**SRM Magnetic Model**

The SRM model investigated in this study has an output power of 150 W with a nominal maximum speed of 3000 rpm. The motor geometries that affect the performance of the SRM are shown in Figure 2 and defined in Table 1.

![Figure 2. SRM cross-section parameters and dimensions](image)

Table 1. Motor geometry parameters

| Symbol | Quantity | Size  |
|--------|----------|-------|
| $D_{so}$ | Stator outer diameter | 115 mm |
| $D_{si}$ | Stator inner diameter | 67 mm |
| $D_{ro}$ | Rotor outer diameter | 66.3 mm |
| $D_{ri}$ | Rotor inner diameter | 20 mm |
| $D_{sh}$ | Shaft diameter | 10 mm |
| $l_g$ | Air gap | 0.35 mm |
| $l_{sl}$ | Stack length | 30 mm |
| $\beta_s$ | Stator pole arc angle | 30 deg |
| $\beta_r$ | Rotor pole arc angle | 33 deg |
| $l_{sy}$ | Stator yoke length | 9.5 mm |
| $l_{ry}$ | Rotor yoke length | 15 mm |
| $h_{sp}$ | Stator pole height | 14.5 mm |
| $h_{rp}$ | Rotor pole height | 8.15 mm |

The stator pole arc angle ($\beta_s$) shown in Figure 2 is given by Equation 1, where $n_s$ is the number of stator poles [17]. The rotor pole arc angle ($\beta_r$) (Equation 2) was made to be 10% greater than the stator pole arc angle to avoid a zero torque position.

\[
\beta_s = \frac{\pi}{2n_s} \quad (1)
\]

\[
\beta_r = \beta_s \times 1.1 \quad (2)
\]

The flux path cross-section at the rotor pole ($A_r$) is given by Equation 3, and the flux path cross-section at the stator pole ($A_s$) is given by Equation 4 [17]. The ratio of the stator outer diameter to the stack length is taken as $(D_{so}/D_{sl}) = 3.83$. In this case, the stack length is calculated as 30 mm.

\[
A_r = D_{ro} \times \beta_r \times l_{sl} \quad (3)
\]

\[
A_s = (D_{ro} + l_g) \times \beta_s \times l_s \quad (4)
\]

The stator yoke flux path cross-section ($A_{sy}$) is given by Equation 5, and the rotor yoke flux path cross-section ($A_{ry}$) is given by Equation 6, where $l_{sy}$ and $l_{ry}$ are the stator and rotor yoke length, respectively [17].

\[
A_{sy} = l_{sy} \times l_{sl} \quad (5)
\]

\[
A_{ry} = l_{ry} \times l_{sl} \quad (6)
\]
The mean flux path length at the stator \((l_{fs})\) is given by Equation 7 and the mean flux path length at the rotor \((l_{fr})\) is given by Equation 8.

The stator pole length \((h_{sp})\) and rotor pole length \((h_{rp})\) in the related equations give the flux path length in the poles [17].

\[
l_{fs} = 2h_{sp} + \frac{(D_{so}+D_{si})\times \pi}{2}
\]  
(7)

\[
l_{fr} = 2h_{rp} + \frac{(D_{ro}+D_{rl})\times \pi}{2}
\]  
(8)

The SRM attempts to maximize the inductance in the active phase by triggering phase windings in an appropriate order to generate the moments of torque. The total reluctance \((R_t)\) of the magnetic circuit must be considered when calculating the inductance in the active phase. The magnetic flux path formed in the SRM when current is applied to the stator windings is shown in Figure 3(a), with the equivalent magnetic circuit shown in Figure 3(b), and consists of the entire rotor and stator yokes. In the aligned position, the flux path cross-section of the rotor and stator poles is symmetric and flux flows equally along the two alternate paths around the stator.

The total reluctance \((R_t)\) and air gap reluctance \((R_g)\), as shown in Equation 9 [17].

\[
R_t = 2\left(R_{sp} + R_{rp} + R_g\right) + R_{sy} + R_{ry}
\]  
(9)

The total reluctance may be expressed in terms of the permeability, \(\mu\), of the materials, where \(\mu_0\) is the permeability of vacuum, as given in Equation 10.

\[
\Sigma R = R_t = 2\left(\frac{h_{sp}}{\mu A_s} + \frac{h_{rp}}{\mu A_r} + \frac{l_g}{\mu_0 A_g}\right) + \frac{l_{fs}}{\mu A_{sy}} + \frac{l_{fr}}{\mu A_{ry}}
\]  
(10)

The phase inductance \((L)\) is determined from the total reluctance, as in Equation 11, where \(N\) is the number of turns of the winding [17].

\[
L = \frac{N^2}{\Sigma R}
\]  
(11)

The phase inductance of the SRM varies according to rotor position; with maximum phase inductance \((L_o)\) occurring when rotor and stator pole are aligned, as shown in Figure 1 (c), and minimum phase inductance \((L_u)\) occurring when rotor and stator poles begin to overlap, as shown in Figure 1 (b). In any unaligned position (Figure 1(a)) the inductance can be found for a given angle, \(\theta\), from Equation 12 [17].

\[
L(\theta, i) = a_0 - a_1 \cos (n_r, \theta)
\]  
(12)

where \(n_r\) refers to the number of the rotor poles. The coefficients \(a_0\) and \(a_1\) are from the maximum and minimum inductances as Equation 13.

\[
a_0 = \frac{l_{max} + l_{min}}{2}, a_1 = \frac{l_{max} - l_{min}}{2}
\]  
(13)

The electromagnetic torque \((T)\) for rotor position is given by Equation 14. This indicates SRMs are capable of generating a high starting moment as the moment changes with the square of the current.

\[
T(\theta, i) = \frac{1}{2} i^2 \frac{dL(\theta, i)}{d\theta}
\]  
(14)
Mean torque or electromagnetic torque ($T_e$) is given by Equation 15.

$$T_e = \frac{1}{2} i^2 L_a - L_u \beta_s \quad (15)$$

**Analysis Method**

The 2-dimensional analysis of the motor and driver circuit was undertaken using Finite Element Method (FEM), using the ANSYS/Maxwell FEM software. Transient and steady state analysis was performed for 3 different rotor geometries, named Type-1, Type-2 and Type-3. Analysis was performed at a sampling frequency of 2000 Hz for 1.5 s, during which the motor speed changed from 0 rpm to a nominal maximum speed of 3000 rpm.

**Model of the SRM**

The rotor geometry of the 3 motor models used in this study, Type-1, Type-2 and Type-3, is shown in Figure 4 (a), (b) and (c). All models had the same stator geometry and air gap. The motor power was 150 W, operating voltage 26 V DC and nominal maximum motor speed 3000 rpm.

![Figure 4. Rotor geometry types (a) Type-1, (b) Type-2, (c) Type-3](image)

A siliceous steel with a stacking factor of 0.95 with B-H curve as given in Figure 5 was used as rotor and stator material.
Driver Circuit

The 3-phase asymmetric bridge circuit given in Figure 6 was used to control the current in the 3 phases of the 6/4-pole SRM. Six (6) switching elements were used (two elements per phase), which ensured continuous rotation by switching the phases sequentially. The design of the rotor ensures that magnetic coupling between the phases is kept to a minimum, allowing independent control of each phase.

Finite Element Analysis (FEA)

Electrical and Mechanical Parameter

FEM was used for the 2-dimensional analysis of the SRM. Three (3) rotors having different shape, yoke length ($l_r$), rotor height ($h_{rp}$) and rotor area ($A_r$) were modeled (Figure 4 (a), (b), (c)). Stator geometry, number of turns, conductor size, and motor lamination material were maintained the same in all analyses.

Figure 7 shows the speed for the three rotor geometries during the start-up transient state and the average speed for steady-state conditions. This shows the Type-3 rotor geometry to have an average speed that is lower than Type-1 and Type-2.

Figure 8 shows the variation in electromagnetic torque and load torque for the three rotor geometries in steady state. It is seen that the Type-3 rotor geometry maintains a higher electromagnetic torque compared to the Type-1 and Type-2 rotor geometries, resulting in electromagnetic torque and load torque that are approximately 40% higher. Figure 8 also shows that at rated speed there is no occurrence of negative electromagnetic torque during a phase. However note that the Type-3 rotor geometry reaches a lower final speed compared to the Type-1 and Type-2 rotor geometries.
Table 2 presents the average and ripple values for electromagnetic and load torque in steady state for the 3 rotor geometries. This shows the Type-3 rotor geometry has higher average torque and lower ripple and should be preferred in applications where these are important.

Table 2. Average Torque and Torque Ripple depending on rotor geometry

|                | Electromagnetic Torque | Load Torque |
|----------------|------------------------|-------------|
|                | Avg. [Nm]   Ripple [SI] | Avg. [Nm]   Ripple [SI] |
| Type-1         | 0.5437      57.996     | 0.4996      0.167       |
| Type-2         | 0.5206      60.428     | 0.4739      0.226       |
| Type-3         | 0.7636      40.822     | 0.7347      0.145       |

Figure 9 shows how the stator phase current ($I$) varies depending on the rotor geometry. In models with Type-1 and Type-2 rotor geometry, the effective value of the phase current is approximately 3.5 A, whereas it is 5.16 A in Type-3, which would account for the higher torque.

Figure 10 shows the source current ($I_s$) for each rotor geometry. The Type-1 and Type-2 rotor geometries have an effective source current, $I_s$, of 6.9 A, whereas the Type-3 has $I_s$ of 7.55 A.
Figure 10. Source current depending on rotor geometry

Magnetic Parameters

The SRMs have been designed to operate with the core in saturation in order to achieve optimum performance. Figure 11 shows the distribution of flux lines with the rotor at an intermediate position, and how two poles occur.

Figure 11. SRM flux lines (Wb/mm) (a) Type-1, (b) Type-2, (c) Type-3

It is recommended that the magnetic flux density in the stator, rotor tooth and yoke regions of an SRM should be less than 1.8 T [18]. Figure 12 shows the distribution of the magnetic flux density in the stator and rotor in steady state for the Type-1, Type-2 and Type-3 rotor geometries.
Figure 12. SRM magnetic flux density distribution (T)
(a) Type-1, (b) Type-2, (c) Type-3

The maximum value for the magnetic flux density in the various regions of the stator and rotor for 3 geometries are given in Table 3 and shows that the magnetic flux density does not exceed the recommended maximum value in any location [18].

| Type   | Stator Yoke (T) | Stator Teeth (T) | Rotor Yoke (T) | Rotor Teeth (T) |
|--------|----------------|------------------|---------------|-----------------|
| Type-1 | 0.634          | 1.650            | 0.694         | 1.510           |
| Type-2 | 0.779          | 1.380            | 0.809         | 1.250           |
| Type-3 | 1.080          | 1.344            | 0.871         | 1.209           |

Current Density in Stator Windings

In enclosed and naturally cooled electrical machines, the current density in the phase windings should be in the range $1.5 < J_b < 5 \text{ A/mm}^2$ [19]. Figure 13 shows the distribution of the current density passing through the rotor bars at $t = 1 \text{ sec}$. The current density of the stator phase windings in each of the 3 geometries remains within the allowed range and indicates forced cooling is not needed.

(a) max 4.8 A/mm$^2$
thus the magnetic reluctance. This will change the inductance, which will result in a change in current, input power, and therefore efficiency.

In the Type-1 and Type-2 rotor geometries, the rotor pole and tooth geometry are arc-shaped, resulting in similar input power and efficiency. In the Type-3 rotor geometry, the edges of the rotor pole are flat and it has sharp points at the poles. This results in a higher input power and thus lower efficiency. This would compare with the findings of others; where the Type-2 rotor geometry with circular rotor pole and tooth geometry provide highest efficiency, but the Type-3 rotor geometry, with rotor pole and tooth geometry having rectangular shape and sharp points, gives the lowest efficiency.

A summary of the performance parameters is given in Table 4.

Table 4. Performance parameters of the rotor geometries

| Motor Parameters | Type-1 | Type-2 | Type-3 |
|------------------|--------|--------|--------|
| Source Current, $I_s (A)$ | 6.93 | 6.84 | 7.55 |
| Phase Current, $I_p (A)$ | 4.51 | 4.45 | 7.86 |
| Speed, $n$ (rpm) | 2861 | 3018 | 1943 |
| Load Torque, $T_l (Nm)$ | 0.50 | 0.47 | 0.73 |
| Shaft Torque, $T_m (Nm)$ | 0.54 | 0.52 | 0.76 |
| DC Feeding, $V (V)$ | 26.00 | 26.00 | 26.00 |
| Core Losses, $P_c (W)$ | 9.72 | 9.65 | 12.06 |
| Copper Losses, $P_{cu} (W)$ | 9.15 | 8.91 | 27.80 |
| Mechanical Losses, $P_m (W)$ | 10.00 | 10.00 | 7.00 |
| Leakage losses, $P_l (%1.5)$ | 2.24 | 2.24 | 2.24 |
| Output Power, $P_o (W)$ | 149.43 | 149.41 | 149.47 |
| Output Power, $P_i (W)$ | 180.54 | 177.97 | 196.34 |
| Efficiency, $\eta$ (%) | 82.77 | 83.95 | 76.13 |
| Current Density, $J (A/mm^2)$ | 4.801 | 4.161 | 3.531 |
| Flux linkage, $\lambda (Wb)$ | 0.01 | 0.0956 | 0.0147 |
| Phase resistance, $R_p (\Omega)$ | 0.15006 | 0.15006 | 0.15006 |

The Type-3 SRM has lower torque ripple than the other types due to having no-salient pole, therefore its mechanical losses are assumed as 7 W, as winding losses are low. Mechanical loss in the other types is assumed as 10 W.

Considering all electrical and mechanical performance parameters in Table 4, the Type-2...
rotor geometry is optimal for the 3 phase 6/4 SRM.

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