Dynamic charge Kondo effect and a slave fermion approach to the Mott transition

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The Mott transition plays a key role in strongly correlated physics but its nature is not yet fully understood. Motivated by recent development of Schwinger boson approach for the Kondo lattice, we propose in this work a novel slave fermion algorithm to study the Mott transition. Upon local approximation, our method yields a phase diagram with a zero-temperature continuous (Mott) metal-insulator transition at finite Coulomb interaction $U$ for the half-filled one-band Hubbard model on a square lattice, and the resistivity exhibits a critical scaling around the quantum Widom line. We argue that the Mott transition may be associated with a dynamic charge Kondo effect of local degenerate doublon and holon states, causing sharp resonances on the doublon/holon and electron spectra. The transition is pushed to $U = 0$ once intersite antiferromagnetic correlations are included, in agreement with exact numerical calculations. Our approach captures some essential features of the Mott transition and offers an alternative angle to view this important problem. It can be extended to study other correlated electron models with more complicated local interactions.

I. INTRODUCTION

The Mott transition is a metal-insulator transition driven by local Coulomb interactions. Its nature remains obscure for over half a century, due to the lack of an obvious order parameter. Experimentally, it has been observed in a wide spectrum of materials such as transition metal oxides, organic compounds, and transition-metal dichalcogenides (TMDs). There are two major features in the electron spectra associated with the Mott transition: the high-energy lower and upper Hubbard bands and the low-energy quasiparticle peak which is suppressed as the system turns from a metal to an insulator. Near the transition, a quantum critical scaling has also been reported in resistivity. Theoretically, the Mott transition has been extensively explored using various analytical and numerical methods, including studies based on parton theories, doublet-holon binding scenarios, charge-2e boson theories, Hatsugai-Kohmoto (HK) model, dynamical mean-field theory (DMFT) and its extensions, comparison of different numerical approaches, and many others. Among them, DMFT can yield both features as well as the resistivity scaling, but predicted a first-order Mott transition at finite Coulomb interaction for the half-filled one-band Hubbard model. On the other hand, exact determinant quantum Monte Carlo (DQMC) simulation on a square lattice predicted a continuous transition at $U = 0$, possibly due to intersite antiferromagnetic (AFM) correlations. Since many effects are involved in these calculations, it is difficult to clarify the role of each factor and establish a clear picture of the Mott transition.

Slave particle approaches have also been applied to understand the Mott transition, which describe the electrons by fractionalized spin and charge degrees of freedom such as spinons, holons, doublons, or rotors. These approaches are less rigorous compared to exact numerical methods, but may provide more intuitive pictures of the transition. To date, most of these works adopted a fermionic representation of the spinons and treated the charge degrees of freedom as bosons. As a result, the Mott transition may be naturally characterized as boson condensation. By contrast, a fermionic representation is seldom used for the charge degrees of freedom, although doublon and holon excitations created by $c^\dagger_{i\sigma} n_{i,-\sigma}$ and $c_{i\sigma}(1 - n_{i,-\sigma})$ have a fermion-like form. Here $c_{i\sigma}$ and $c^\dagger_{i\sigma}$ are the annihilation and creation operators of electrons and $n_{i\sigma}$ is its density operator. In fact, a fermionic representation with self-consistent Born approximation (SCBA) has recently been applied to analyze the doublon-holon binding and found good agreement with exact DQMC simulation.

In this work, we propose an alternative approach based on the fermionic representation. Our method is motivated by the recent development of Schwinger boson approach to heavy fermion systems. Instead of using Born approximation, we introduce a fermionic auxiliary field to decouple the kinetic term and use self-consistent one-loop approximation to calculate the quasiparticle spectra. As an example, we apply this method to the one-band Hubbard model at half filling and derive successfully a $T-U$ phase diagram with a continuous metal-insulator transition at zero temperature. Near the transition, the resistivity exhibits a critical scaling around the quantum Widom line. We find that the transition may be understood as a dynamic charge Kondo effect of the local degenerate doublon and holon states, with bosonic spinons playing the role of fluctuating hybridization fields. Comparison with DMFT indicates that the DMFT first-order transition may originate from vertex corrections beyond one-loop approximation.
cluding intersite AFM correlations drives the transition to \( U = 0 \), in good agreement with DQMC prediction.

Hence, our approach captures the essential aspects of the Mott transition and is a useful tool to explore the roles of different ingredients during the transition. It can be easily extended to other more complicated models and offer novel perspective on their correlated electron physics.

II. METHOD

We start with the half-filled one-band Hubbard model on a square lattice:

\[
H = - \sum_{ij\sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i (n_{i\uparrow} - \frac{1}{2})(n_{i\downarrow} - \frac{1}{2}),
\]

which contains a kinetic term and a Hubbard \( U \)-term. In the slave fermion representation, the physical electron operator is rewritten as \( c_{i\sigma} = \epsilon_i^c s_{i\sigma}^c + \sigma s_{i\sigma}^d d_i \), where \( d_i \) and \( \epsilon_i \) are fermionic operators denoting the doubly occupied (doublon) and empty (holon) states, respectively, and \( s_{i\sigma} \) describe bosonic spinons for the singly occupied states. The physical Hilbert space is constrained by requiring \( Q_i \equiv \epsilon_i^c + d_i^\dagger \sum_i s_{i\sigma}^d s_{i\sigma} = 1 \). In this way, the Hubbard-\( U \) term becomes quadratic, but the kinetic term turns into a more complicated quartic form, which may be decoupled via a Hubbard–Stratonovich transformation by introducing a fermionic auxiliary field \( \chi_{i\sigma} \). The final effective action reads

\[
\mathcal{L} = \mathcal{L}_0 + \frac{U}{2} \sum_i (d_i^\dagger d_i + \bar{e}_i e_i) + \sum_i \lambda_i (Q_i - 1)
\]

\[- \sum_{ij\sigma} g_{ij}^{-1} \chi_{i\sigma} \chi_{j\sigma} + \sum_{i\sigma} [\chi_{i\sigma}(\bar{e}_i s_{i\sigma}^d + \sigma \bar{s}_{i\sigma}^d d_i) + \text{H.c.}],
\]

where \( \mathcal{L}_0 = \sum_i \{ \bar{d}_i \partial_t d_i + \bar{e}_i \partial_t e_i + \sum_{\sigma} \bar{s}_{i\sigma} \partial_{\tau} s_{i\sigma} \}, \lambda_i \) is the Lagrange multiplier, and \( g_{ij}^{-1} = -(t^{-1})_{ij} \) with \( t \) being the hopping matrix with site indices. As illustrated in Fig. III(a), only the auxiliary \( \chi \) field carries spatial correlation information in this model, while the local slave particles \( d_i, e_i, \) and \( s_{i\sigma} \) can only hop on the lattice by coupling to the field through a three-particle vertex. Such a form actually covers a large family of strongly correlated models, similar to that in the dual fermion approach\cite{105-110}. The above procedure can be readily extended to other models with more complex local interactions. By requiring \( G^{-1}(k, \omega_n) = (\omega_n - \epsilon_k) \), we may also obtain the periodic Anderson model with local degrees of freedom represented by slave particles.

There are different ways to solve the above action. We may use DMFT by approximating \( \mathcal{G} \) with a self-consistent local Weiss field\cite{106-110}. But DMFT is a black box incorporating many effects that are hard to extract. Here, motivated by the recent development of Schwinger boson approach for studying heavy fermion quantum phase transitions\cite{97-104}, we adopt one-loop approximation and solve the following self-energy equations:

\[
\Sigma_{\chi}(\omega_n) = \frac{1}{\beta} \sum_m G_{s}(\nu_{m}) G_{c}(\omega_{m-n}) - G_{d}(\omega_{m+n}),
\]

\[
\Sigma_{s}(\nu_{m}) = \frac{1}{\beta} \sum_n G_{\chi}(\nu_{n}) [G_{d}(\nu_{m+n}) - G_{c}(\nu_{m-n})],
\]

\[
\Sigma_{d/e}(\omega_{n}) = - \frac{2}{\beta} \sum_m G_s(\nu_{m}) G_{\chi}(\nu_{m-n}),
\]

where \( \nu (\nu') \) are the fermionic (bosonic) Matsubara frequencies, \( \Sigma \) are the local self-energies of all slave particles and auxiliary fields, and \( G \) are their full local Green’s functions to be determined self-consistently. The holon and doublon self-energies are the same due to the particle-hole symmetry. For simplicity, we have adopted a local approximation and ignore the moment dependence in the self-energies. The Lagrange multipliers are also approximated by their mean-field value, \( \lambda_i = \lambda \).

The one-loop approximation is numerically more efficient than DMFT. In this form, we may have a more intuitive picture on physics, in the cost of numerical exactness. Below we will focus on the square lattice model with only nearest-neighbor hopping \( t \), and set the half bandwidth \( D \) of the free electrons to unity so that \( t = 1/4 \). Note that all calculations were performed in real frequency.

![Figure 1](image-url)
As shown in Fig. (b), the doublon (holon) spectra contains a broad peak around $\omega = U/2 + \lambda$, which is the bare energy of the local doublon (holon) state. The spectra are, however, greatly broadened due to the coupling with the spinon and $\chi$ fields. The slight spectral weight below the Fermi energy contributes a small doublon occupation number. For large $U$ above $U_c \approx 2.1$, we see a finite excitation gap, which gradually diminishes with decreasing $U$ as the whole spectra move leftwards and touch the Fermi energy. For $U < U_c$, a sharp resonance peak appears around $\omega \sim \eta T$ ($\eta \approx 1 - 2$) for $U < U_c$. Hence $U_c$ marks the Mott metal-insulator transition point below which the charge excitation gap closes. The sharp resonance on the doublon (holon) spectra reflects the emergent electron quasiparticles in the metallic state.

To clarify its origin, we note that a similar peak also appears in the spinon spectra as shown in Fig. (c). Its location scales linearly with the temperature, $\omega_s \approx 1.1T$ (inset). This may be easily understood from the constraint $\langle Q_i \rangle = 1$. Because both doublon and holon occupations are small, the spinon energy must satisfy $n_B(\omega_s) \approx 0.5$ if we ignore its broadening. Here $n_B(\omega)$ is the Bose-Einstein distribution function. We immediately find $\omega_s \approx 1.1T$. Hence, the resonance peak in the doublon (holon) spectra comes from the coupling with spinons and the auxiliary $\chi$ field through the three-particle vertex. Since the spinon is a bosonic field, we may also compare it to the Kondo effect, where the Kondo resonance appears when two degenerate local (spin) states couple to conduction electrons through a finite hybridization field. This suggests a possible Kondo-like mechanism in the Hubbard model, albeit for the degenerate doulon and holon states.

In fact, if we integrate out the bosonic spinons and define $f_i \equiv (\alpha_i, e_i)^T$ and $\psi_i \equiv (\chi_i, \chi_{i\uparrow})^T$, the vertex term in the effective action Eq. (3) becomes $g^{\alpha}_{i\uparrow} \tau_1 - \tau_2 \left[ (f_i \sigma_{\uparrow\downarrow} \pi_i \pi_i)(\psi_i \pi_{i\uparrow} f_i \pi_{i\uparrow}) - (f_i \sigma_{\downarrow\uparrow} \pi_i \pi_i)(\psi_i \pi_{i\uparrow} f_i \pi_{i\uparrow}) \right]$, where $g^{\alpha}_{i\uparrow}$ is the bare spinon Green’s function in imaginary time. This looks quite complicated. However, at $\tau_1 = \tau_2$, it reduces to a familiar form, $-4g^{\alpha}_i S^\alpha_i \cdot S^\alpha_i$, where $S^\alpha_i = f_i \frac{\pi_{i\downarrow}}{2} f_i$ and $S^\alpha_i = \psi_i \frac{\pi_{i\uparrow}}{2} \psi_i$. In deriving this, we have used the equality, $\sigma_{\alpha\beta} \cdot \sigma_{\mu\nu} = \delta_{\alpha\mu} \delta_{\beta\nu} - (i\sigma^y)_{\alpha\mu} (i\sigma^y)_{\beta\nu}$. It can be shown that $g^{\alpha}_i = n_B(-\lambda)$, which is always negative for $\lambda > 0$, indicating an effective antiferromagnetic coupling. Hence, the three-particle vertex contains some Kondo-like physics, where the doublon/holon are local degenerate states, the $\chi$ field plays the role of conduction electrons, and the spinon contributes the hybridization. This analogy underlies the Mott transition at $U_c$ and the emergence of electron quasiparticles for $U < U_c$.

However, there are two important differences from the usual Kondo effect. First, it happens in the charge degree of freedom, the effective “spin” can have a time dependence for $\tau_1 \neq \tau_2$, and the bosonic “hybridization” (spinon) field has a peak at finite frequency. Hence, we may better call it a dynamic charge Kondo effect. Second, most of the holon and doublon spectra are above the Fermi energy, so these states are only slightly occupied. As a result, the Kondo-like resonance only appears when their spectra are close to the Fermi energy, and the interaction-driven Mott transition must be associated with some singular variation in the doublon (holon) occupation. We will see that this is indeed the case.

For completeness, we also show in Fig. (d) the spectra of the auxiliary $\chi$ field. Similarly, it contains two broad peaks at high energies representing the processes of creating a doublon and annihilating a holon, respectively. Around the Fermi energy, the spectra are gapped for $U > U_c$ but develop a finite weight for $U < U_c$. The gap for $U > U_c$ separates the peaks at positive and negative energies and implies that the doublon and holon processes are independent and do not cooperate to form electron quasiparticles. For $U < U_c$, the finite spectra at
\( \omega = 0 \) imply that the \( \chi \) field becomes itinerant, through which all low-energy slave particle excitations become moveable on the lattice. In addition, the gapped doublon/holon and \( \chi \) spectra also prohibit spinon decay, so the spinon peak at \( \omega_s \) is sharp for large \( U \) but damped for small \( U \), as is seen in Fig. 1c.

As in the usual spin Kondo effect, the dynamic charge Kondo effect for \( U < U_c \) leads to a superposition of the holon and doublon states through coupling to the \( \chi \) field. Such a superposition is necessary for the emergence of electron-like quasiparticles because \( c_{i\sigma} = c_{i\sigma} + \sigma s_{i\sigma} d_i \) involves both holons and doublons. To see this, we calculate the spectra of physical electrons using the self-energy of the \( \chi \) field, \( G_\epsilon(k, i\omega_n) = \Sigma_{\epsilon} (i\omega_n) / [1 - \epsilon_k \Sigma_{\epsilon} (i\omega_n)] \), where \( \epsilon_k \) is the bare dispersion of electrons. This formula can be derived by making derivative of the action with respect to the hopping parameter \( t_{ij} \). The resulting local DOS \( \rho_\epsilon (\omega) \) is plotted in Fig. 2a. We find the same features as in the slave particles with two broad peaks near \( \pm (U/2 + \lambda) \), which can be identified as the upper and lower Hubbard bands. For \( U > U_c \), the spectra are also gapped, while for \( U < U_c \), we find a sharp quasiparticle peak at \( \omega = 0 \). Obviously, all these features are related to those on the doublon and holon spectra. To see the Mott transition clearly, we plot the electron DOS at zero energy \( \rho_\epsilon (0) \) in Fig. 2b. For all temperatures, \( \rho_\epsilon (0) \) decreases as \( U \) grows. At low temperatures, \( \rho_\epsilon (0) \) drops rapidly to nearly zero at \( U_c \), signaling the occurrence of a Mott transition. Our results are supported by the comparison of the Mott gap above \( U_c \) with those derived by DMFT using different impurity solvers. As plotted in the inset of Fig. 2b, the overall agreement is quite good, except that DMFT predicts a first-order Mott transition instead of a finite temperature first-order transition predicted by DMFT. To determine the order of the transition, we further calculate the double occupancy \( n_d \equiv \sum_i \langle n_{i\uparrow} n_{i\downarrow} \rangle / N = \sum_i \langle d_i^\dagger d_i \rangle / N \), where \( N \) is the number of lattice sites. \( n_d \) is therefore also the doublon occupation. The results are shown in Fig. 2d. We see it also varies continuously with \( U \) for all temperatures (inset), but its second derivative \( \partial^2 n_d / \partial U^2 \) exhibits a sharp peak near \( U_c \) as \( T \) decreases, implying a jump in \( \partial n_d / \partial U \) or a slope change in \( n_d (U) \) at \( U_c \), as \( T \to 0 \). Since \( n_d \) is proportional to the first derivative of the free energy \( F \) with respect to \( U \), our method successfully captures the Mott transition and identifies it as a continuous (second-order) quantum phase transition at zero temperature.

Next we consider thermodynamic and transport properties within our method. Figures 3a and 3b plot the spin and charge susceptibility calculated using a bubble diagram of the slave particles:

\[
\chi_s = 4 \int_{-\infty}^{\infty} \frac{d\omega}{\pi} n_B(\omega) \text{Re} G_\sigma(\omega) \text{Im} G_\sigma(\omega),
\]

\[
\chi_c = 4 \int_{-\infty}^{\infty} \frac{d\omega}{\pi} n_F(\omega) \text{Re} G_d(\omega) \text{Im} G_d(\omega),
\]

FIG. 3: Temperature dependence of (a) the spin susceptibility \( T \chi_s \) and (b) the charge susceptibility \( \chi_c \) for different values of \( U \). The black circles in (b) marks the temperature \( T_d \) where the doublon (holon) occupation is lowest for each \( U < U_c \). (c) Intensity plot of the temperature derivative of the resistivity, \( \beta R(U, T) \equiv d \log R(U, T) / d \log T \) on the \( T \) vs. \( U \) plane, showing all four temperature scales \( T_d, T_g, T_0, T_0 \). A quantum Widom line (QWL) can be identified from \( \beta R(U, T) = 0 \). (d) Quantum critical scaling of the resistivity, \( R(U, T) / R_c(T) = f(T)/|U - U_c(T)|^{\nu z} \), where \( R_c(T) \equiv R(U_c(T), T) \), with the exponent \( \nu z \approx 1.0 \). The inset of (d) shows the original data of the resistivity.
where $n_F(\omega)$ is the Fermi-Dirac distribution. For large $U$, $T\chi_s(T)$ approaches a constant at low temperatures, indicating that the spinons form well-defined local moments in the insulating phase. Its decrease at small $U$ suggests that the moments are partially screened in the metallic phase, consistent with the expectation that the spinons are damped for small $U$. The behavior of the charge susceptibility $\chi_c(T)$ in the metallic phase is similar to that of DMFT. As $T$ decreases, $\chi_c$ first increases due to the development of quasiparticle coherence, then decreases due to the formation of local moments, and finally increases again due to the screening of local moments. As expected, the onset temperature of the final increase in $\chi_c$ is close to $T_d$ (black circles), where $n_d(T)$ has a local minimum but starts to grow at lower temperatures.

The resistivity $R = 1/\sigma$ is calculated using the following equation:

$$\sigma = -\frac{4\pi^2}{N} \sum_{\mathbf{k},\mu} \sin^2(k_\mu) \int_{-\infty}^{\infty} \frac{d\omega}{\pi} \frac{\partial n_F(\omega)}{\partial \omega} |\text{Im} G_c(\mathbf{k}, \omega)|^2.$$ (5)

The data are presented in the inset of Fig. 3(d) for the same $U$ values as in Fig. 3(a). For $U < U_c$, $R$ displays a small maximum and then drops as $T$ goes down, while for $U > U_c$, it diverges at low temperatures in accordance with experimental observations in both organic compounds and TMDs. Figure 3(c) gives the intensity plot of $\beta_R(U,T) \equiv d \log R(U,T)/d \log T$ on the $T-U$ phase diagram. Besides the three temperature scales $T_d$, $T_0$, $T_g$ already shown in Fig. 2(c), we also include $T_d$ in the metallic phase. Interestingly, we can identify a clear quantum Widom line (QWL) for $U_c(T)$ from $\beta_R(U,T) = 0$, which has the same shape as that reported in organic compounds, and partly coincides with $T_d$ identified from the lower boundary of the pseudogap region. Around the QWL, as shown in Fig. 3(d), our calculated resistivity data all collapse onto two separate curves for the insulating and metallic phases, respectively. We find a critical scaling $R(U,T)/R(U_c(T),T) = f[T/U − U_c(T)]^{-\nu}$ around the QWL. A similar scaling has been reported previously in both experiment and DMFT calculations. However, the critical exponent is found to be $\nu z \approx 1.0$ here, in contrast to $\nu z = 0.67$ from DMFT and $0.5 \sim 0.7$ from organic compounds and TMDs. Compared to DMFT, we suspect that vertex correction, which is ignored in the one-loop approximation, might be responsible for this difference.

So far we have adopted a local approximation and ignored spatial correlation. To see its potential effects on the Mott transition, we include in the Hamiltonian an additional spinon-correlation term, $H_{\text{spin}} = J \sum_{\mathbf{k}} \xi_k(s_{\mathbf{k},\uparrow} + \xi^\dagger_{\mathbf{k},\downarrow} + \text{H.c.})$, which can be derived from the Heisenberg interaction, $J_H \sum_{(ij)} \mathbf{S}_i \cdot \mathbf{S}_j \rightarrow -(J_H/2) \sum_{(ij)} (A_{ij} s_{i,\uparrow} s_{j,\uparrow}^\dagger + \text{H.c.})$, with $A_{ij} \equiv \sum_\sigma \langle \sigma s_i \sigma s_j \rangle$ under Schwinger boson mean-field approximation. For simplicity, we will not solve $A_{ij}$ self-consistently, but give by hand a dispersion $\xi_k = 2t[\sin(k_x) + \sin(k_y)]$. Again, we can solve the one-loop self-consistent equations for the local self-energies. The resulting spinon spectra are plotted in Fig. 4(a) for different values of $J$ at a fixed $T$ and $U = 1.0$. We see two major features. First, the spinon peak shifts to higher energy linearly with increasing $J$, namely $\omega_s \sim J$. Second, for finite $J$, a sharp change occurs near $\omega = 0$ at sufficiently low temperatures, which is a precursor of spinon condensation and implies an AFM ground state at zero temperature. Meanwhile, as shown in Fig. 4(b), the doublon (holon) peak near $\omega = 0$ gradually moves to higher energy, and a charge gap opens at low temperature even for small $U$. Correspondingly, the physical electron spectra in Fig. 4(c) also exhibit a gap near the Fermi energy. Figure 4(d) shows the electron spectra $\rho_e(\omega)$ for different $U$ at $J = 0.1$. For all $U$, $\rho_e(\omega)$ always shows a gap and additional narrow peak structures on the inner side of the Hubbard bands at sufficiently low temperatures. These inner peaks were also captured in former QMC and slave fermion SCBA calculations.
give the intensity plots of $\rho_c(0)$ in Fig. 4(e) and the resistivity $R$ in Fig. 4(f) on the T-U plane. We see quite similar behaviors on both plots, where $\rho_c(0)$ always decreases and $R$ diverges as the temperature approaches zero. These confirm an insulating ground state for all $U > 0$, although we cannot perform calculations at sufficiently low temperature to confirm the gap opening for very small $U$. Thus, intersite AFM correlations drive the metal-insulator transition to $U = 0$, as predicted in exact DQMC calculations. However, a better estimate of $J$ will be needed in order to obtain good prediction of the gap size compared to the exact QMC results.

The above spectral features have also been discussed previously in the literature and ascribed to doublon-holon binding or doublon-spinon interaction. In our method, their origins are quite transparent since these features only appear after we introduce the spinon correlation term, so they must be associated with the interaction of doublons (holons) with a correlated spinon background. In fact, if we again integrate out the spinon fields, the new spinon-correlation term will induce an effective pairing of the form $d_i e_j$, which causes the doublon-holon binding, produces an additional contribution to the charge gap in the doublon (holon) excitation spectra even for small $U$, and drives the metal-insulator transition to $U = 0$. On the other hand, for large $U$ or $J$, we find the inner peak appears only at very low temperatures when the spinon gap approaches zero, which confirms its “polaronic” origin as the doublons (holons) move on a magnetically correlated background. Interestingly, we also find that the Mott gap in the electron spectra is always smaller than the charge gap in the doublon/holon spectra at finite temperatures and they only become equal at zero temperature. This feature has also been observed in previous SCBA calculations and may be attributed to the convolution of the doublon/holon and spinon spectra in calculating the electron spectra. It reflects an intrinsic spin-charge separation nature of the Mott physics, while the electron quasiparticle can only be excited as a composite object of holon/doublon and spinon. For small $U$ and $J$, the hybridization effect still plays a role and is of primary responsibility for the peak, which is different from the situation at large $U$.

**IV. CONCLUSION**

To summarize, we develop a novel approach to study the mechanism of Mott metal-insulator transition. Our method combines the slave fermion representation of the electrons and the fermionic auxiliary field to decouple the kinetic term in the Hamiltonian. This results in a three-particle vertex that may be solved by a self-consistent one-loop approximation. Our calculations reproduce the Mott transition as a continuous quantum phase transition at zero temperature and associate the quasiparticle emergence with a dynamic charge Kondo effect. We also derive a phase diagram containing a pseudogap region above the metallic phase and obtain a resistivity scaling around the quantum Widom line. Including AFM spin correlation drives the Mott transition to $U = 0$ and induces some special spectral features, confirming the importance of intersite magnetic correlations. Hence, our theory captures the essential features of the Mott physics and provides an alternative angle for clarifying this longstanding problem. Our method may be easily extended to cover a large family of correlated models with more complex local interactions.

It may be helpful to compare our method with other slave particle approaches such as the Kotliar-Ruckenstein slave boson and the slave rotor approaches. There are three major differences. First, in the slave boson approaches, doublons and holons are treated as bosons and the metallic phase is realized when they condense. Under mean-field approximation, it is equivalent to the Gutzwiller approach and can only account for the quasiparticle bands near the Fermi energy. To obtain the Hubbard bands, additional Gaussian fluctuations or a more complicated approximation are needed. Similarly, in the slave rotor approach, the charge degree of freedom is described as a rotor and the metallic phase is obtained by the condensation of a constrained bosonic field. In our slave fermion approach, the Hubbard bands come naturally from the fermionic doublon/holon states, and the Mott transition is associated with a dynamic charge Kondo effect tuned by the doublon/holon levels. While it seems less intuitive, the Kondo effect does not involve any symmetry breaking and the transition takes place likely between two orthogonal ground states at zero temperature. Second, in slave boson and slave rotor approaches, the spins are described by fermions. Because the mean-field approximation replaces the local constraint by lattice average, the fermionic representation of spins is more appropriate for describing a fermionic spin liquid with a spinon Fermi surface rather than long-range magnetic orders of localized moments. By contrast, the bosonic representation of the spin degree of freedom can describe well the magnetic long-range order of local moments by the condensation of bosonic spinons. Third, in all above approaches, the kinetic term in the Hamiltonian becomes quite complicated under the slave particle representation, so a mean-field approximation has often been applied to decouple the kinetic term. By contrast, our work introduces an additional fermionic auxiliary field to describe the kinetic term, and thereby successfully applies the one-loop self-consistent calculations of the Green’s functions. This naturally takes into account some dynamic fluctuations of the slave particles beyond the mean-field approximation. It will be interesting to see if our idea can also be applied to the bosonic representations and yield improved description of the Mott transition there.

**Note added:** After completing this work, we were informed of a simultaneous study by DMFT, which reported some similar results as in Fig. 3 including the
coincidence of the QWL and $T_q$ at low temperatures. The agreement again confirms the validity of our slave fermion approach.

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