Indications of stellar prominence oscillations on fast rotating stars: the cases of HK Aqr and PZ Tel

M. Leitzinger1†, P. Odert2,1, T.V. Zaqarashvili1,2,3, R. Greimel1, A. Hanslmeier1, H. Lammer2

1Institute of Physics, Department for Geophysics, Astrophysics, and Meteorology, NAWI Graz, Universitätsplatz 5, 8010 Graz, Austria
2Space Research Institute, Austrian Academy of Sciences, Schmiedlstraße 6, 8042, Graz, Austria
3Abastumani Astrophysical Observatory, Ilia State University, Tbilisi, Georgia

Accepted 2016 August 1. Received 2016 July 8; in original form 2015 December 2

ABSTRACT

We present the analysis of six nights of spectroscopic monitoring of two young and fast rotating late-type stars, namely the dMe star HK Aqr and the dG/dK star PZ Tel. On both stars we detect absorption features reminiscent of signatures of co-rotating cool clouds or prominences visible in Hα. Several prominences on HK Aqr show periodic variability in the prominence tracks which follow a sinusoidal motion (indication of prominence oscillations). On PZ Tel we could not find any periodic variability in the prominence tracks. By fitting sinusoidal functions to the prominence tracks we derive amplitudes and periods which are similar to those of large amplitude oscillations seen in solar prominences. In one specific event we also derive a periodic variation of the prominence track in the Hβ spectral line which shows an anti-phase variation with the one derived for the Hα spectral line. Using these parameters and estimated mass density of a prominence on HK Aqr we derive a minimum magnetic field strength of ∼2 G. The relatively low strength of the magnetic field is explained by the large height of this stellar prominence (>0.67 stellar radii above the surface).

Key words: stars: late-type – stars: activity – stars: individual: HK Aqr – stars: individual: PZ Tel

1 INTRODUCTION

Prominences are manifestations of solar/stellar coronal magnetic fields. Coronal magnetic field supports cool dense prominence plasma against gravity, which may be kept for several rotations (quiescent prominences) or may be ejected because of disturbances in the stellar plasma causing the plasma to accelerate very fast (eruptive prominences). Prominences and filaments refer to the same phenomenon with the difference that prominences are seen against the dark background at the solar/stellar limb in emission and filaments are seen against the solar/stellar disk in absorption. We will use the term “prominence” throughout the paper. Eruptive prominences often lead to Coronal Mass Ejections (CMEs) which propagate through the solar/stellar corona and interplanetary space where they normally decelerate and dissolve into the solar/stellar wind.

There exists a good correlation of solar CMEs and eruptive prominences (Hori & Culhane 2002; Gopalswamy et al. 2003) which seems to be not surprising as the erupting filament represents the CME core. On the Sun, prominences/filaments and CMEs have been studied since decades and data covering a complete solar cycle allow statistical analyses (Gopalswamy et al. 2003). Solar quiescent prominences have lifetimes between 1 and 300 days and a mean height of 2.6×10⁴ km (Wang et al. 2010). The masses of solar prominences are not easily determined from observations, therefore only a few measurements of selected prominences exist. Using typical values for hydrogen column density and volume of solar prominences, masses in the range of 5×10¹²-10¹⁵ g are derived (Labrosse et al. 2010).

On the Sun, we know that prominences show oscillations, both longitudinal and transverse. Oscillating prominences may lead to eruptions sometimes. Large amplitude oscillations are oscillations which are triggered by Moreton or EIT waves, flares, or are related to the eruptive phase of filaments. The prominence oscillations are divided
into small-amplitude (2–3 km s$^{-1}$) and large-amplitude (>20 km s$^{-1}$) oscillations (see Arregui et al. 2012). Periods of large amplitude oscillations are in the range of 6–150 min (Tripathi et al. 2009) while small amplitude oscillations have periods up to 90 minutes. But even periods below one minute and above several hours are reported for small amplitude oscillations (Arregui et al. 2012). The so-called winkings are manifestations of large-amplitude oscillations. Solar H$\alpha$ filters have a certain narrow bandpass. The large-amplitude oscillation periodically shifts the H$\alpha$ line outside of the filter bandpass making the filament “invisible”. Therefore they were named “winking”.

Stellar prominences have been detected for the first time by Collier Cameron & Robinson (1989a) on the rapidly (0.52 d Innis et al. 1988) rotating K-star AB Doradus as transient absorption features in H$\alpha$. Prominences can only be detected in rotationally broadened H$\alpha$ line profiles while the absorption transients travel over the H$\alpha$ line profile. In a rotationally unBroadened H$\alpha$ line profile such absorption transients cannot be detected. Up to now, prominences have been detected on a number of fast rotators such as AB Doradus (Collier Cameron & Robinson 1989a), BO Mic (Jeffries 1993; Dunstone et al. 2006), HK Aqr (Byrne et al. 1994), PZ Tel (Barnes et al. 2000), G dwarf stars in the Persei cluster (Collier Cameron & Woods 1992), the post T Tauri star RX J1508.6-4423 (Donati et al. 2000) and EY Dra (Jeffries 1993; Dunstone et al. 2006), HK Aqr (Byrne et al. 1994), PZ Tel (Barnes et al. 2000), G dwarf stars in the Persei cluster (Collier Cameron & Woods 1992), the post T Tauri star RX J1508.6-4423 (Donati et al. 2000) and EY Dra (Eibl 1998). The prominences of the stars reach heights of several stellar radii, even above the co-rotation radius. Masses have been determined for AB Dor in the range of 2–6×10$^{17}$ g (Collier Cameron et al. 1990) and for Speedy Mic in the range of 0.5–2×10$^{17}$ g (Dunstone et al. 2006). Moreover, prominences have also been detected on binary systems as absorptions in optical spectra (Parsons et al. 2011) and dips in light-curves lasting for several rotation periods (Irawati et al. 2015). Oscillations in stellar prominences derived from absorption transients have so far not been detected.

Within this study we aim for the detection of prominence oscillations which can be used to estimate the magnetic field strength in stellar prominences. This method is a further development of solar coronal seismology, which uses observed oscillations to determine plasma parameters (Nakariakov & Ofman 2001). Moreover, stars hosting prominences should also be potential candidates for the detection of prominence eruptions as we know from the Sun that the core of a CME is the prominence/filament. As targets for observations observed oscillations to determine plasma parameters (Nakariakov & Ofman 2001). Moreover, stars hosting prominences should also be potential candidates for the detection of prominence eruptions as we know from the Sun that the core of a CME is the prominence/filament. As targets for

### Table 1. Observational details of the ESO FEROS data used in the study. The S/N values refer to mean values for each night calculated around H$\alpha$.

| date     | no. of spectra | S/N |
|----------|----------------|-----|
| HK/PZ    |                |     |
| 07/08/2012 | 10/49          | 46/74 |
| 08/08/2012 | 17/60          | 38/98 |
| 09/08/2012 | 14/50          | 77/91 |
| 10/08/2012 | -/30           | -/109 |
| 11/08/2012 | 38/30          | 61/90 |
| 12/08/2012 | 31/10          | 55/106 |

### 2.1 Data reduction and preparation

The FEROS Echelle spectra have been reduced with the Image Reduction and Analysis Facility (IRAF) V2.16. The standard reduction steps were BIAS and Flat Field correction, cosmic ray removal, and wavelength calibration (ThArNe frames). The data have been normalized for analysis. To make prominence structures in H$\alpha$ visible we apply a common method, which is the subtraction of individual spectra by an average spectrum generated from the whole time series. The residual spectra are then plotted as a dynamic spectrum (wavelength vs. time) which is shown in Fig. 4 for HK Aqr and PZ Tel.

To determine the center positions of the prominence tracks we fitted the residual spectra, which we build using total and daily averages, with single and double gaussians (see section 4.3.1). In this way we can deduce the central position of each absorption feature as it moves across the H$\alpha$ profile.

Dunstone et al. (2006) investigated prominence systems on the ultra-fast rotator Speedy Mic. By generating dynamic spectra of their time series it was obvious that many absorption structures were visible already from the spectral time series without dividing or subtracting a mean profile. These authors avoided the above described simple method to obtain residual spectra because of the many strong and variable absorption signatures in H$\alpha$. Therefore these authors...
Indications of stellar prominence oscillations

Figure 1. Hα dynamic residual spectra of HK Aqr (left panel) and PZ Tel (right panel) starting from 07-08-2012 lowest panel to 12-08-2012 top panel (night of 10-08-2012 is missing as no observations of HK Aqr were possible due to technical problems). The intensity in the images is grey scaled (black refers to minimum values whereas white corresponds to maximum values). One can clearly see drifting structures over the Hα profile, both black and white. The prominences are named according to Table 2. The solid vertical lines mark the center of Hα and the vertical dashed lines mark the vsini value of the corresponding star.

© 2002 RAS, MNRAS 000, 1–20
applied a gaussian weighted running mean in the temporal direction to obtain residual spectra. The dynamic spectra of HK Aqr show only subtle absorption features, therefore it is possible to find a reference level which is not influenced by the absorptions.

The same is true for PZ Tel. Moreover, the application of a gaussian weighted running mean requires a longer spectral time series to achieve good results. As our observation strategy was directed to the observation of two stars during the same night the number of continuous spectra is therefore small. The application of an average spectrum as a reference strategy was directed to the observation of two stars during the same night the number of continuous spectra is therefore small. The application of an average spectrum as a reference level to allow a detection of prominences in emission when they rotate off the disk.

We detect in total 8 prominence structures on HK Aqr and 6 on PZ Tel, all of them seen in absorption. In the spectroscopic time series of HK Aqr of the first night there is one drifting structure seen in emission which clearly shows an enhancement during the first few spectra indicating a flare. In Table 2 we present the prominence parameters of the detected structures. Those are height and projected area of the prominences, as well as prominence oscillation parameters, amplitude and period (see sections 3.3.1, 3.4, and 3.3.2).

3 RESULTS

3.1 Prominences on HK Aqr and PZ Tel

Fig. 1 shows dynamic residual spectra obtained from Hα spectroscopic observations of HK Aqr (left panel) and PZ Tel (right panel) for each night of observation. Prominence tracks caused by co-rotating prominences can be identified as drifting structures from blue to red. One can see structures of different slopes, indicating different heights and/or occurrence on different stellar latitudes, as well as structures seen in absorption and emission. The majority of the structures is seen in absorption. The nature of the tracks seen in emission might be related to stellar activity such as plage regions. Prominences, seen off-disk in emission are visible as subtle emission features beyond the stellar vsini value. Dunstone et al. (2006) nicely show prominences seen in emission above the stellar limb on the ultra-fast rotator Speedy Mic. Our data have a S/N too low to allow a detection of prominences in emission when they rotate off the disk.

As the FEROS spectra cover a wavelength range from 3500-9200Å we are able to look for signatures of prominences also in other spectral lines. FEROS covers several Balmer lines but the S/N decreases towards shorter wavelengths due to reduced emission of the star and the fact that the sensitivity of the detector is lower at blue wavelengths. Because Hβ is the second strongest line of the Balmer sequence we have chosen it as a second spectral line to look for signatures of prominences and neglect Hγ, Hδ, and further Balmer lines. Prominences are also visible in the CaII H+K lines but the S/N is much lower than at Hα in our observations. Not all prominences which we have detected on HK Aqr in Hα can be seen in Hβ. Especially two events can be reproduced very well in Hβ, which are HK_{11}P2 and HK_{12}P1. When detecting prominence signatures in Hβ we can deduce the residual Hβ flux and can compare it to the residual Hα flux. By building a Hα/Hβ flux ratio we are able to infer, if the prominence material is optically thick. If it is optically thick, then we may derive the area on the star which is obscured by the prominence (cf. section 3.3.2) as well as its mass. The analysis of the Hβ prominences has revealed that the linear fits to the prominences tracks deviate from the Hα fits which is surprising, as we would have expected a similar slope because the signatures detected in both spectral lines originate from the same prominence.
no. 1-2 indicate absorptions. Taking a look at Fig. 1 shows that there is indeed a weak absorption event visible, but it seems to be a separate prominence appearing before prominence HK_08_P0. Moreover, the quality of the spectra of this night is not as good as in the other nights, therefore a distinct identification becomes difficult. Spectrum no. 9 shows a sudden increase in flux which is related to a very low S/N.

The night of the 11th of August shows three prominences, namely HK_11_P1, HK_11_P2, and HK_11_P4, all of them are consistent with dips in the light-curve, the most pronounced event is HK_11_P2. The Hβ light-curve of the same night shows several dips, the most pronounced event is also prominence HK_11_P2.

In the following night (12/08/2012) three prominences are visible (HK_12_P0, HK_12_P1, and HK_12_P2) which coincide with the dips in the light-curves. Spectrum no. 2 of that light-curve shows a peak which is related to the fact that guiding was lost at that time. As one can see from the light-curve, one would assign also spectra no. 3 to prominence HK_12_P0 but we do not see absorptions as signatures of prominences in the corresponding spectrum. From Fig. A6 (see Appendix) on can see that spectrum no. 3 is very noisy. As one can see, no typical flare light-curve is seen in Fig. 3 except the event which was detected during the first night (see upper panel of Fig. 3). Even there are enhancements in the light-curves of HK Aqr in the night of the 11th of August (spectra no. 0-6 and spectra no. 29-33) and in the night of the 12th of August (spectra no. 28-30), we do not detect activity indicators such as the HeI line at 5876Å (e.g. Montes et al. 1997), during those enhancements, which typically rises during flares.

### 3.3 Prominence parameters

#### 3.3.1 Prominence height

As in previous studies we assume that the prominence clouds are located at a distance $R_c$ from the stars center and rotate rigidly with the star. For simplicity we assume an inclination of $i = 90^\circ$ which is likely considering the parameters of both stars (see Eibe 1998, Maire et al. 2015). For HK Aqr we adopt a radius of $0.59R_\odot$ (Barnes & Collier Cameron 2001) and for PZ Tel a radius of $1.23R_\odot$ (Jenkins et al. 2012). The cloud motion is then given by $V = \omega R_c \cos \theta$ where $\omega = 2\pi/P$ is the stellar rotation rate and $\theta$ is the latitude of the cloud (see Fig. 4). The product $R_c \cos \theta$ gives the distance of the cloud from the rotational axis. In the spectra we observe only the line-of-sight component of $V$ which is given by $V_c = V \sin \phi$ where $\phi = \omega (t - t_0)$ is the longitude, which is zero at $t = t_0$ when the cloud crosses the observer’s meridian. Hence, the cloud’s velocity evolution, as determined from the absorption features crossing the Ha line, is described by (Collier Cameron & Robinson 1989a)

$$V_c = \frac{R_c}{R_\star} v \sin(i) \cos(\theta) \sin(\phi),$$

(1)

where we assume that $v \sin(i) \approx \upsilon_\infty = \omega R_\star$. If $t \sim t_0$, then $\sin(\phi) \approx \phi$ and Eq. (1) describes the linear part of the radial velocity curve. To obtain the projected height $R_c \cos \theta$ we fit the linear part of the prominence tracks. For large-height prominences the prominence track lies completely in this linear part. Results are given in Table 2 and shown in Fig. 4.
(see also Fig. A1 and Fig. A2 in the Appendix). In Eq. [4] there are two unknown variables, which is the true height of the prominence \( R_e \) and its latitude \( \theta \), but only the combined quantity \( R_e \cos \theta \) can be measured. However, one can deduce a range of possible \( R_e \). Apparently, the minimum value of \( R_e \) occurs if the clouds orbit in the equatorial plane where \( \theta = 0^\circ \) and is thus equal to the measured value \( R_e \cos \theta \). The maximum of \( R_e \) can be deduced from visibility arguments. For any true height \( R_e \) there is a maximum possible latitude \( \theta_{\text{max}} \) which the prominence can have and can still be seen in projection onto the stellar disk. Since all prominences we observe are seen in absorption it is obvious that their latitudes must be smaller than \( \theta_{\text{max}} \). This maximum latitude of the clouds can be derived by the requirement that their heights from the equatorial plane must be smaller than \( R_e \), i.e. \( \sin \theta < R_e/R_e \) or \( \tan \theta < R_e/(R_e \cos \theta) \). From the latter relation one can obtain the maximum \( \theta \) for which a given prominence can still be seen against the stellar disk. Thus one can calculate the maximum possible height as \( \theta_{\text{max}} = (R_e \cos \theta)/\cos \theta_{\text{max}} \) (see Fig. 4). Since we obtained minimum values of \( R_e \), for several prominences it is possible to also estimate a minimum latitude for these cases through the requirement that \( R_e \geq R_e \) and thus \( \cos \theta_{\text{min}} \geq R_e \cos \theta/R_e \). From the results given in Table 2 one can see that the obtained range of true heights is rather narrow. We find two types of prominences, large ones with \( R_e \geq R_e \) and small ones with \( R_e \approx R_e \). We find only large prominences for PZ Tel, but both large and small ones for HK Aqr. Large prominences must have latitudes smaller than about 40°, whereas the small prominences are located at high latitudes between 60 – 70°. To see whether the large prominences are stable structures with respect to gravity we calculate the co-rotation radii. For HK Aqr we find a co-rotation radius of 3.16 R_\star, and for PZ Tel a co-rotation radius of 3.42 R_\star. As one can see, except prominence HK_08 P0, all other prominences are well below the co-rotation radius and are therefore expected to be stable. This finding is in agreement with Byrne et al. (1996) who found prominences with heights ranging from 0.3–0.4 R_\star above the stellar surface. For the calculation of the co-rotation radius we adopted a mass of 0.4 M_\odot for HK Aqr (Byrne et al. 1996) and a mass of 1.1 M_\odot for PZ Tel (Jenkins et al. 2012).

### 3.3.2 Prominence area

If the prominence material is optically thick we may estimate the projected area of the prominences. We follow the method in Dunstone et al. (2006) to see if the prominences on HK Aqr are optical thick or thin. We compare the Hβ/Hα ratio of the prominence residuals to the theoretical curve of growth calculated in Dunstone et al. (2006) for the Balmer lines. We see that our calculated values lie on the saturated part of the theoretical curve and are therefore assumed to be optical thick. Now we can estimate the projected area. The equation which describes the flux density determined from the spectra closest to the line of sight crossing (based on Collier Cameron et al. 1990) is

\[
f_{\lambda} = f_{\text{backgr,}\lambda}(1 - \frac{A_C}{A_{\text{star}}}[1 - \exp(-\tau_{\lambda})]).
\]

If the prominences are optical thick then one can neglect \( \exp(-\tau_{\lambda}) \) and Eq. 2 gives

\[
\frac{A_C}{A_{\star}} = 1 - \frac{f_{\lambda}}{f_{\text{backgr,}\lambda}}.
\]

According to this equation we can infer the projected area of the prominences. In Table 2 we list the derived projected areas. The values range from ~7% ... 24% for HK Aqr and ~4% ... 8% for PZ Tel. From Fig. 5 one can see that the area derived from Hα and Hβ data are roughly consistent, but the errors for the area derived from Hβ data are large, with respect to the errors for the area derived from Hα data.
3.4 Indications of prominence oscillations

From the variation of the center positions of the prominence tracks we detect periodic variability in two prominences on HK Aqr (HK\text{11P2} and HK\text{12P1}). The oscillatory motion is already visible when looking at the left panels of Fig. 7. To remove the stellar rotation we fitted the prominence track with a line and subtracted it (see section 3.4.1 for details). Interestingly, we detect residual sinusoidal motion on HK Aqr only, and none on PZ Tel. In Fig. A1 and Fig. A2 (Appendix) we show sinusoidal motion of the prominence tracks of prominences HK\text{112} (in H\text{β}) and HK\text{121} (in H\text{α}) which are the same prominence seen in different nights. We also searched for variability of the center-positions in intensity but none could be found. The prominence tracks showing oscillatory motion have been fitted with a sinusoidal function of the form

\[ d(t) = x_0 \sin \left( \frac{2\pi t}{P} + \phi \right) + d_0, \quad (4) \]

where \(x_0\) is the amplitude, \(P\) the period, \(\phi\) the phase, and \(d_0\) a displacement in the y-axis. As the tracks of prominences HK\text{112} and HK\text{121} consist of 8 and 6 data points, respectively, we do not include damping, as the number of free parameters of a damped sine function is close to the number of data points of prominences HK\text{112}, and HK\text{121}. To exclude that the detected variations might come from instrumental effects we perform the following test. Photospheric lines are assumed to stay stable during the time series with respect to their line center. We choose the CaI line at 6439Å which we fitted in the same way as the spectral residuals. The test showed that the center positions show deviations within one wavelength resolution element. As the spectra are oversampled this corresponds to \(\sim 2\) km s\(^{-1}\). Therefore we exclude the possibility that the periodic variability of the center-positions is influenced by instrumental effects. In Table 2 we show the parameters of the sinusoidal motions of the H\text{α} prominence tracks.

The derived periods of periodic variability of prominences HK\text{11P2} and HK\text{12P1} lie within the range of solar large amplitude oscillations, whereas the derived amplitudes are lower and lie between solar small- and large-amplitude oscillations. The derived amplitudes are close to the spectral resolution of FEROS (\(\sim 6\) km s\(^{-1}\)). As we have detected prominences HK\text{11P2} and HK\text{12P1} also in H\text{β} we are able to infer if both show also periodic variability in H\text{β}. By comparing the H\text{α} and H\text{β} tracks for prominence HK\text{11P2} we see that H\text{β} shows the H\text{α} oscillation in anti-phase (see Fig. 8), at least for prominence tracks derived from single gaussian fitting from residuals obtained from total average subtraction (we find the same results for residuals obtained from daily average subtraction). For prominence tracks derived from double gaussian fitting, for both residuals determined from daily and total average subtraction, we find a phase shift between H\text{α} and H\text{β} rather than an anti-phase behaviour. For the HK\text{12P1} event we can not reproduce the sinusoidal motion in H\text{β}, as seen in H\text{α}. The H\text{α} and H\text{β} discrepancy seen in HK\text{11P2} is possibly related to the different quality of the data around H\text{α} and H\text{β} or is a sign of a prominence oscillation seen in different regions in the same prominence (see section 3.4.1).

![Figure 6. Hα (blue square symbols) and Hβ (red square symbols) prominence tracks for prominence HK\text{11P2} determined from single gaussian fitting (upper panel) and double gaussian fitting (lower panel). Overplotted is a sinusoidal function (Eq. 4). For the prominence track derived from single gaussian fitting we clearly see an anti-phase behaviour of Hα and Hβ. For the prominence track derived from double gaussian fitting we see a phase shift rather than an anti-phase behaviour.](image)

3.4.1 Stability of the periodic variability, errors, and significance

As we deduce sinusoidal motion of the center positions of the residuals, the generation of the residuals might have an influence on the parameters of periodic variability of the center positions of the prominence tracks. To check what the influence of different built residuals is, we build total and daily averages. To check what the influence of different fitting functions is we use single and double gaussian functions to fit the residuals. This results in four cases, (a) single gaussian fitting of the residual built from total average subtraction, (b) single gaussian fitting of the residual built from daily average subtraction, (c) double gaussian fitting of the residual built from total average subtraction, and (d) double gaussian fitting of the residual built from daily average subtraction. The influence of daily and total averaging is smaller with respect to variations in the center positions compared to the influence of single and double gaussian fitting, respectively. Therefore we plot in Fig. 7 the H\text{α} prominence tracks determined for cases (a) and (c) for prominence HK\text{11P2} in the left panels. The prominence tracks are over-plotted with the line fits from which we determine the prominence height and which is subtracted to remove the cloud velocity. The prominence tracks with removed cloud velocity are shown in the panels in the right column of Fig 7. Over-plotted is the sinusoidal function (see Eq. 4). One can see that case (a), which originates from single gaussian fitting, shows a sinusoidal motion. Case (c), which originates from double gaussian fitting, can be fitted with a sine function, showing phase shift and a difference in amplitude, with respect to case (a).

Going back to Fig. 8 one can see that single and double gaussian fitting applied to residuals derived from daily and total average subtraction yield different center positions. Both fit-
ting functions introduce systematic errors, as some residuals are better fitted by single gaussians and some are better fitted by double gaussians. In the analysis we introduced a weighted mean to include all four cases ((a)-(d)), but this representation includes also all systematic errors, therefore we believe that a representation of the prominence tracks by a weighted mean is not appropriate.

To evaluate the goodness of fit of the sine function we calculate its reduced $\chi^2$. In addition we fit a line to the data and calculate its reduced $\chi^2$ for comparison. Especially as the amplitudes are rather small and the data errors are not negligible the choice of a straight line as comparison fit function is reasonable. In table 3 we list the reduced $\chi^2$ values for prominences HK11 P2 and HK12 P1 for residual cases (a) and (c). The reduced $\chi^2$ depends on the number of observations (i.e. data points) and free parameters of the fitting function. For prominence HK11 P2 there are only 8 data points and for prominence HK12 P1 only 6. Therefore the usage of a damped sine function is not applicable especially for prominence HK12 P1, which has 6 data points only.

The different reduced $\chi^2$ values of prominence HK12 P1 clearly show that fitting with a sine function is reasonable as the reduced $\chi^2$ values are in all cases smaller than for line fitting.

The different reduced $\chi^2$ values of prominence HK11 P2 (both Hα and Hβ) show that fitting with a sine function is reasonable. All reduced $\chi^2$ values for prominence HK11 P2 show that the sine function matches the observed values better than a line. The differences of deriving center positions using single and double Gauss fitting can be inferred from Fig. 2 where we show the residual spectral sequences of prominences HK11 P2 and HK12 P1 over-plotted with single- and double-gaussian fits. The double Gauss functions follow the absorptions in the residuals in more detail than

Table 2. Parameters of prominences detected on HK Aqr and PZ Tel during the 07-12$^{th}$ of August 2012. For each detected prominence we list the phase, the event type (if we see the full prominence transit or only a part of it), the $R_{c,\cos(\theta)}$ value which corresponds also to $R_{c,\text{max}}$ (for $\theta=0^\circ$), the maximum height (as $R_c$ and $R_{c,\text{max}}$ are counted from the center of the star one has to subtract the stellar radius to obtain the height of the prominences above the stellar surface), and the projected area. For the detected periodic variability of center-positions we list amplitude and period. We list amplitudes and periods for solutions (a) and (c). For information see text. For some of the partially observed events we could not derive their height as there were too few data points to be fitted.

| struct | date       | phase | event type | $R_{c,\cos(\theta)}$ | $R_{c,\text{max}}$ | area (%) | oscillation | amplitude (km s$^{-1}$) | period (min) |
|--------|------------|-------|------------|-----------------------|---------------------|----------|-------------|------------------------|-------------|
| HK 08 P0 | 08-08-2012 | 0.45-0.60 | full        | 3.75                  | 3.88                | 13.3     | no          | -                      | -           |
| HK 08 P2 | 08-08-2012 | 0.64-0.74 | partial     | 0.32                  | 1.05                | 19.7     | no          | -                      | -           |
| HK 09 P1 | 09-08-2012 | 0.17-0.22 | partial     | -                     | -                   | -        | no          | -                      | -           |
| HK 11 P1 | 11-08-2012 | 0.40-0.62 | full        | 0.49                  | 1.11                | 9.4      | no          | -                      | -           |
| HK 11 P2 | 11-08-2012 | 0.64-0.74 | full        | 1.67                  | 1.95                | 24.1     | yes         | 6.26±0.92(a)           | 50.83±3.02(a) |
| HK 11 P4 | 11-08-2012 | 0.87-0.93 | partial     | -                     | -                   | -        | no          | -                      | -           |
| HK 12 P0 | 12-08-2012 | 0.53-0.62 | full        | 2.41                  | 2.61                | 7.4      | no          | -                      | -           |
| HK 12 P1 | 12-08-2012 | 0.66-0.78 | full        | 0.54                  | 1.14                | 16.8     | yes         | 5.44±1.40(a)           | 46.25±4.35(a) |
| HK 12 P2 | 12-08-2012 | 0.84-0.94 | full        | 1.35                  | 1.68                | 15.9     | no          | -                      | -           |
| PZ 07 P1 | 07-08-2012 | 0.9-0.17 | partial     | -                     | -                   | -        | no          | -                      | -           |
| PZ 08 P1 | 08-08-2012 | 0.20-0.085 | full       | 1.44                  | 1.75                | 4.1      | no          | -                      | -           |
| PZ 09 P1 | 09-08-2012 | 0.150-0.252 | full       | 1.05                  | 1.45                | 7.8      | no          | -                      | -           |
| PZ 10 P0 | 10-08-2012 | 0.14-0.248 | full        | -                     | -                   | -        | no          | -                      | -           |
| PZ 11 P0 | 11-08-2012 | 0.31-0.33 | partial     | -                     | -                   | -        | no          | -                      | -           |
| PZ 12 P0 | 12-08-2012 | 0.299-0.328 | partial     | -                     | -                   | -        | no          | -                      | -           |

Table 3. Reduced $\chi^2$ calculated for prominences HK11 P2 (Hα and Hβ) and HK12 P1 (Hα). In each column we list the reduced $\chi^2$ value derived from fitting with a sine function and separated by a slash from fitting with a line.

| struct | event type | $R_{c,\cos(\theta)}$ | $R_{c,\text{max}}$ | amplitude (km s$^{-1}$) | period (min) |
|--------|------------|-----------------------|---------------------|------------------------|-------------|
| HK11 P2 Hα | sine/line | 3.59/5.09 | 2.21/10.4 | 16.16/18.02 | 2.86/6.26 |
| HK11 P2 Hβ | sine/line | 3.99/4.45 | 1.38/24.30 | 9.36/10.18 |

3.5 Estimation of magnetic field strength in stellar prominences: stellar coronal seismology

Observed oscillations can be used to estimate plasma parameters in the prominences. The periodic variability of the center-positions is only found in line-of-sight velocity but not in intensity, which indicates their transverse character. Then the periodic variability of the center positions of the prominences can be interpreted in terms of Alfvén or magneto-hydrodynamic kink waves. Their dispersion relation depends on magnetic field strength and plasma density. The wavelength can be assumed from the spatial extent of prominences. Then the magnetic field strength can be estimated if one assumes a plasma density in the prominences. [Dunstone et al. 2006] used the curve of growth method to obtain the column density of Hα and CaII atoms. Both are necessary to estimate the column density of hydrogen atoms in the ground state. By assuming that at
Indications of stellar prominence oscillations

Table 4. Comparison of solar and stellar prominence parameters. The stellar prominence parameters are estimated from HK_{11}P2 and the solar parameters are taken from Schwartz et al. (2004).

|          | HK Aqr | Sun |
|----------|--------|-----|
| mass density [g cm^{-3}] | 2.9×10^{-15} | 10^{-15} |
| mass [g] | 5.7×10^{16} | 10^{14}-10^{15} |
| volume [cm^3] | 2.0×10^{31} | 10^{29} |
| area [cm^2] | 7.4×10^{20} | 9.9×10^{19} |
| thickness [cm] | 2.7×10^{10} | 7×10^9 |

prominence temperatures of 10^4 K the Ca atoms are single ionized, these authors used the hydrogen to calcium ratio for solar prominences. By doing so they obtain the column density for hydrogen atoms in the ground state. The data Dunstone et al. (2006) used have a much higher S/N as our data and therefore we can not repeat their method to obtain the column density of hydrogen in the ground state. But as an approximation we use our determined ratio of EW(Hβ)/EW(Hα) (0.37) and determine the logarithmic hydrogen column density for state N_2 from the curve of growth given in Dunstone et al. (2006) which gives logN_2 ∼ 18 m^{-2}. As we have no CaII H&K measurements we adopt the N_1 to N_2 ratio of Speedy Mic, which we assume to be comparable to the ratio of HK Aqr and find a log(N_1) value of 23.7 m^{-2}. As we have estimated the area of the prominences we are able to calculate the mass according to M=μH_N A. For the only prominence on HK Aqr for which we have Hα and Hβ measurements and which shows sinusoidal motion in both lines, which is HK_{11}P2, we calculate a mass of 5.7×10^{16}g. To obtain the density of the prominence plasma we have to assume the extension in the third dimension of the prominence. We assume that the thickness is comparable to the length scale which we estimate as √A_β/√A_α. Applying this geometrical thickness to the prominence area gives a volume of ∼ 2×10^{31} cm^3. The hydrogen density of the prominence plasma results finally to 2.9×10^{-15} g cm^{-3}. In Table 4 we list derived parameters for HK_{11}P2 and for a solar prominence analysed in Schwartz et al. (2004) as comparison. One can see that the solar and stellar values differ within one or two orders of magnitude. Of course, the scaling of the prominence thickness is the most uncertain parameter and influences the results significantly.

To assess the magnetic field of prominence HK_{11}P2 we assume kink oscillations of a cylindrical fluxtube with length L. We assume that the density is much higher in prominences than in the surrounding coronal plasma as it is the case on the Sun. Then the phase speed of the kink oscillation is defined by (Edwin & Roberts 1983) as

\[ c_k = \frac{\sqrt{\frac{7}{5} B_0}}{\mu_0 \rho_0} = \frac{2L}{T}. \]  

(5)

\( B_0 \) is the magnetic field of the prominence plasma, \( \rho_0 \) the mass density of the prominence plasma, L denotes the length of the prominence and T is the period of the first harmonic of the prominence oscillation. For the calculation of the magnetic field strength of HK_{11}P2 we take the values given in Table 4. The only missing parameter is the length of the prominence, which we have deduced assuming that the prominences area has a quadratic shape. The average area of prominence HK_{11}P2 is 7.4×10^{20} cm^2 and the length of a corresponding square with the same area is 2.7×10^{10} cm. Using these values we get a B_0 of ∼ 2 G. Since the prominence length is underestimated because prominences are known to be elongated, B_0 is a lower limit. Prominence HK_{11}P2 is located at almost 1 R_s from the stellar surface. This means that the magnetic field strength is estimated approximately at this height, which is quite high in comparison with solar prominence heights. Recently, Zaqarashvili et al. (2013) estimated solar coronal magnetic field strengths through coronal seismology using radio observations and found ∼ 1 G at the height of 1 R_S. Therefore, our estimations are in good coincidence with those of the solar corona. This similarity is surprising as surface magnetic fields of dM stars are much higher than on the Sun (Mullar 1973).

4 DISCUSSION

In this section we will discuss the periodic variability of the center-positions of two prominences detected on HK Aqr, especially the anti-phase detection in Hβ of prominence HK_{11}P2. Moreover we will discuss the roughly estimated magnetic field strength of the prominence.

4.1 Indications of prominence oscillations

On the Sun one distinguishes between small amplitude oscillations which are mainly related to quiescent prominences with amplitudes of a few km s^{-1} and large amplitude oscillations mainly related to flares with amplitudes of > 20 km s^{-1}. On stars there is so far no detection of prominence oscillations of this kind found here. Houdebine et al. (1993) found during a flare on the dMe star AD Leo that the CaII K line revealed periodic Doppler shifts (of the whole line) with a period of a few minutes and a maximum amplitude of 53 km s^{-1}. Jeffries (1993) analyse Speedy Mic spectra and find prominences co-rotating with the star. Looking at their Fig. 3 one can see variations of the absorption transients around the radial velocity fit, which the authors mention as “...there is marginal evidence for a sinusoidal velocity for transient B.” Probably we see here the first manifestation of prominence oscillations on Speedy Mic.

With respect to spectrographs with moderately high resolving power, such as FEROS, one will be able to resolve the stellar analogue of solar large amplitude oscillations only. As we detected amplitudes with velocities lying between solar small- and large amplitude oscillations on HK Aqr a higher resolving power would have been desirable. As mentioned above, if we indeed detected the stellar analogue of the solar large amplitude oscillations then one would expect a flare and/or CME occurring as the exciter for the oscillation, as the oscillation of huge masses requires much energy (e.g. Liu et al. 2012). No optical signature of a flare and/or a CME was detected before prominence HK_{11}P2. As mentioned in section 4.1 prominence HK_{11}P2 shows an anti-phase behaviour of periodic variability of the center-positions in Hβ. From the upper panel of Fig. 6 which
Figure 7. Panels in the left column from top to bottom: Prominence Hα tracks of prominence HK$_{11}$P2 derived from residuals generated from (a1) total average subtraction and single Gauss fitting and (c1) total average subtraction and double Gauss fitting. In panels a1 and c1 the linefits representing the cloud velocity are over plotted as black solid lines. Panel (e) shows an overplot of prominence tracks a1 and c1. Panels in the right column from top to bottom: Prominence Hα tracks of prominence HK$_{11}$P2 corrected for cloud velocity derived from residuals generated in the same order as for the panels (a1-c1) in the left row. Overplotted is a sinusoidal function from which we determine period and amplitude of the periodic variability. In the last panel in the right column (f) we show the spread of the line fits (a1-c 1) used for removing the cloud velocity.
shows the Hα and Hβ prominence tracks derived from single gaussian fitting, one can see that the Hβ oscillation is indeed in anti-phase to the Hα oscillation. The Hα and Hβ prominence tracks derived from double gaussian fitting (lower panel of Fig. 3) show a reduced phase shift. We already introduced the problem of systematic errors in section 3.4.1 for single and double gaussian fitting. Probably this might become an issue also here. However, in the following we discuss this finding with a special emphasis to solar observations of prominence oscillations.

The neutral prominence matter is mainly comprised of hydrogen atoms of different excitation levels, Hα and Hβ are generated from the same atomic level (n=2) and from similar temperatures. If we see in Hα and Hβ different regions of the prominence then it could be possible that we see oscillations out of phase. On the Sun it is possible to spatially resolve filaments and make the fine structure, the so-called fibrils, visible (Schmidt & Mein 1989). Regarding small-amplitude oscillations it is known that individual fibrils, or even groups of fibrils of the filament oscillate independently (Díaz et al. 2003). Terradas et al. (2002) found anti-phase oscillations in a sub-region of a quiescent prominence, detected in Hβ filtergrams with a period of 75 minutes and a mean amplitude of 2 km s⁻¹. The anti-phase was found in different regions of the prominence but not in different wavelengths, as for HK Aqr. Ning et al. (2003) report on a solar filament, observed with Hα and CaII filters, consisting of two spines which oscillated in anti-phase. The oscillation amplitude was measured to be on average 3 km s⁻¹ which is in the range of small amplitude oscillations but the period of 98 minutes classifies it as a long-period oscillation. Luna et al. (2008) numerically investigated transverse oscillations in two parallel cylindrical slabs to understand the collective oscillatory behaviour of the system. Different modes were found with oscillations in and out of phase. With this model several solar findings with respect to prominence oscillations can be explained. Zapiór et al. (2015) simultaneously observed solar quiescent prominences in several spectral lines, including Hα and Hβ. These authors detected small amplitude oscillations of quiescent prominences showing the same phase in Hα and Hβ. Again, there are no simultaneous observations of Hα and Hβ solar prominence large amplitude oscillations. However, stellar prominences are, compared to solar ones, huge structures. They are detectable in several spectral lines including Hα and Hβ. It is likely that the fine-structure of stellar prominences is also comprised of solar analogues of fibrils. Possibly those are also able to oscillate out of phase. Furthermore, it could be possible that not only the whole loop containing the prominence oscillates, but also the prominence Hα and Hβ plasma itself, producing a superimposed motion.

The Hβ anti-phase oscillation was detected in one event only and only for case (a), case (c) showed a reduced phase shift only. Additional observations with higher spectral resolution of the Hα and Hβ oscillatory signatures are needed to draw conclusions on this behaviour.

On PZ Tel we did not detect sinusoidal motion in the prominence tracks, only non-periodic variability. Possibly PZ Tel has oscillations with amplitudes not detectable with our spectral resolution. In section 3.4.1 we have shown the influence of different built residuals and different fitting functions on the variation of the center-positions. One source of uncertainty for the variation of the center-positions of the prominences is the finding of a reference profile, which is subtracted to receive the residual spectra from which the center-positions are determined. Ideally one would need a spectrum which is not influenced by any prominence signature and/or signature of stellar activity at the same time. From Fig. 3 one can see that for HK Aqr no “quiescent” spectrum is available, either it is affected by absorptions and/or emission features in the residuals.

Young main-sequence stars have high activity levels and frequent flaring is often observed, especially for dMe stars. A source of uncertainty which possibly influences the center-positions of the residuals is the activity of the star. In the first night of the observations we have detected a flare on HK Aqr which is seen as distinct enhancement of the Hα profile. Such an enhancement has not been detected again in the remaining nights (see Fig. 3). A flare event leads to an increase of the flux of an Hα profile, even if a prominence is projected onto the disk a pronounced flare event (like the one seen during the first night) can be still identified from the corresponding light-curve, therefore we are confident that the only pronounced flare detected in the data is that from the first night. The identification of less pronounced flares is problematic as they cause changes in the light-curves at a flux level comparable to prominences or even weaker. If such less pronounced flares have occurred and are superimposed on the prominence signatures then their contribution is hard to estimate, because the amount of residual flux varies with longitude and latitude of prominence occurrence. Moreover, if a plage region is also visible at the time of prominence occurrence then this is also seen superimposed onto the residual, as it is the case for prominence HK_11_P2 where we see an emission emerging in residual no. 27 in Fig. 3.

We do not expect that a superimposed plage region causes periodic variability, but a deviation from the linear prominence track.

For the superposition of a flare it is nearly impossible to disentangle flare and prominence contribution. A flare causes the Hα core to symmetrically rise and line asymmetries related to a flare are known to occur in the wings (both blue and red) of Hα. Prominences can be seen on HK Aqr in absorption with a wavelength range of ±1.5Å from line center which corresponds to the resi of HK Aqr of ~70 km s⁻¹. From the Sun, it is known that asymmetries during flares related to up- and down-ward flows can reach several tens of km s⁻¹ (Ichimoto & Kurokawa 1984). We can not determine the influence of frequent less energetic flares, compared to the event during the first night, on the determination of the center-positions derived from the residuals, as we can not identify them from the light-curves. The determination of underlying stellar activity would require spectroscopic data of HK Aqr without prominence signatures or spectroscopic data of a stellar twin of HK Aqr showing no prominences.
4.2 Magnetic field of stellar prominences

In section 3.5 we derived under several assumptions for the prominence geometry the magnetic field strength of prominence HK$_{11}$P2. We derived a lower limit of $B_0 \sim 2$ G which is comparable to magnetic fields in solar prominences which are in the range of a few G (Parenti 2014) but are located at lower heights compared to the height of prominence HK$_{11}$P2. Therefore the centrifugal forces acting on the prominence material is smaller.

Collier Cameron & Robinson (1989a) found prominences on AB Dor extending beyond the co-rotation radius therefore they argued for an additional force (magnetic tension) acting against the centrifugal force. The prominences detected on HK Aqr are below the co-rotation radius, which is in agreement with [Byrne et al.] and should be therefore stable.

Wang et al. (2014) performed an automated statistical analysis of solar prominences and found that the majority reaches a height of $2.6 \times 10^4$ km. Heights of stellar prominences are much bigger than solar ones. From literature (see section 1) and the height determination from this study stellar prominences reach heights of a few stellar radii. E.g. for prominence HK$_{11}$P2 we find a maximum height above the stellar surface of 0.67 R$_*$ which corresponds to $2.8 \times 10^5$ km which is a factor $\sim 11$ higher than for average solar prominences. Collier Cameron & Robinson (1989a) used an approximation to estimate the magnetic field strength inside the prominences on the fast rotating K dwarf AB Dor. Saying that magnetic pressure must be bigger than the gas pressure,

$$\frac{B^2}{8\pi} > nkT$$

these authors estimated a magnetic field strength of the AB Dor prominences of $\sim 1$ G assuming a neutral particle density $n$ of $10^9$ cm$^{-3}$ which is in agreement with our estimate of particle density $(3.9 \times 10^8$ cm$^{-3}$) and magnetic field strength (as estimated from Eq. 6). If we calculate the magnetic field strength of the prominence using Eq. 6 and assuming a temperature of $10^5$ K we get a lower limit for the magnetic field strength of 0.12 G. We also consider the contribution from ions and electrons, assuming that both are equal in number, to obtain the final magnetic field strength.

Therefore we multiply the obtained magnetic field strength by a factor of 3 assuming the same number densities of ions and neutral hydrogen atoms. This gives 0.36 G which is similar to the $B_0$ derived for prominence HK$_{11}$P2.

Vrsnak (1984) investigated vertical prominence oscillations and argued that the magnetic field of the prominence must satisfy the relation of kinetic energy density and magnetic pressure

$$\frac{B^2}{8\pi} > \rho v^2$$

Here $v$ is the amplitude of the oscillation. From this equation we calculate a lower limit of the magnetic field strength of 0.12 G. Houdebine et al. (1993) estimated for their CaII K Doppler-shifts a minimum magnetic field strength of $\sim 20$ G assuming an electron density of $5 \times 10^{10}$ cm$^{-3}$.

The above estimations have shown that the determined magnetic field strength in the prominence deduced from the oscillations agrees with magnetic field strengths estimated by Collier Cameron & Robinson (1989a) for prominences on AB Dor. Moreover the deduced magnetic field strength fulfills the requirements expressed in Eq. 6 and 7 and agrees with the solar coronal magnetic field strength at similar heights (Zaqarashvili et al. 2013).

5 CONCLUSIONS

We have analysed 6 nights of spectroscopic observations of the fast rotating, young, and active stars HK Aqr and PZ Tel. We detected in total 14 prominences on both stars. Two prominences detected on HK Aqr show periodic variability of the center-positions of prominence tracks with periods in the range of solar large amplitude oscillations. The amplitudes are smaller than found for large-amplitude oscillations in solar prominences. In one of the prominences of HK Aqr we detect an anti-phase oscillation in H${\beta}$ which probably is a sign of fine structure of stellar prominences.

Using several assumptions we estimated the magnetic field strength of a prominence detected on HK Aqr which is in the order of so far reported magnetic field strengths in stellar prominences.

ACKNOWLEDGEMENTS

ML, PO, and AH acknowledge the support from the FWF project P22950-N16. AH acknowledges the support from the FWF project P27765-N27. PO and HL acknowledge the support by the FWF project P 27256-N27. HL acknowledges the support by the FWF NFN project S116 “Pathways to Habitability: From Disks to Active Stars, Planets and Life”, and the related FWF NFN subproject S116607-N16. The work of TZ was supported by the Austrian Fonds zur Förderung der Wissenschaftlichen Forschung under project P26181-N27 and by FP7-PEOPLE-2010-IRSES-269299 project- SOLSPANET.

REFERENCES

Arregui I., Oliver R., Ballester J. L., 2012, Living Reviews in Solar Physics, 9, 2
Barnes J. R., Collier Cameron A., 2001, MNRAS, 326, 950
Barnes J. R., Collier Cameron A., James D. J., Donati J.-F., 2000, MNRAS, 314, 162
Barnes J. R., James D. J., Collier Cameron A., 2004, MNRAS, 352, 589
Byrne P. B., Eibe M. T., Rolleston W. R. J., 1996, A&A, 311, 651
Collier Cameron A., Duncan D. K., Ehrenfreund P., Foing B. H., Kuntz K. D., Penston M. V., Robinson R. D., Soderblom D. R., 1990, MNRAS, 247, 415
Collier Cameron A., Robinson R. D., 1989a, MNRAS, 236, 57
Collier Cameron A., Robinson R. D., 1989b, MNRAS, 238, 657
Collier Cameron A., Woods J. A., 1992, MNRAS, 258, 360
Díaz A. J., Oliver R., Ballester J. L., 2003, A&A, 402, 781
Donati J.-F., Mengel M., Carter B. D., Marsden S., Collier Cameron A., Wichmann R., 2000, MNRAS, 316, 699
Indications of stellar prominence oscillations

Dunstone N. J., Barnes J. R., Collier Cameron A., Jardine M., 2006, MNRAS, 365, 530
Dunstone N. J., Collier Cameron A., Barnes J. R., Jardine M., 2006, MNRAS, 373, 1308
Edwin P. M., Roberts B., 1983, Sol. Phys., 88, 179
Elie M. T., 1998, A&A, 337, 757
Gopalswamy N., Shimojo M., Lu W., Yashiro S., Shibasaki K., Howard R. A., 2003, ApJ, 586, 562
Hori K., Culhane J. L., 2002, A&A, 382, 666
Houdebine E. R., Foung B. H., Doyle J. G., Rodono M., 1993, A&A, 274, 245
Ichimoto K., Kurokawa H., 1984, Sol. Phys., 93, 105
Innis J. L., Coates D. W., Thompson K., Lloyd Evans T., 1990, MNRAS, 242, 306
Innis J. L., Thompson K., Coates D. W., Evans T. L., 1988, MNRAS, 235, 1411
Irawati P. et al., 2015, ArXiv e-prints
Jeffries R. D., 1993, MNRAS, 262, 369
Jenkins J. S. et al., 2012, MNRAS, 420, 3587
Labrosse N., Heinzl P., Vial J.-C., Kucera T., Parenti S., Gunár S., Schmieder B., Kilper G., 2010, Space Sci. Rev., 151, 243
Liu W., Ofman L., Nitta N. V., Aschwanden M. J., Schrijver C. J., Title A. M., Tarbell T. D., 2012, ApJ, 753, 52
Luna M., Terradas J., Oliver R., Ballester J. L., 2008, ApJ, 676, 717
Maire A.-L. et al., 2015, ArXiv e-prints
Messina S., Desidera S., Turatto M., Lanzafame A. C., Guinan E. F., 2010, A&A, 520, A15
Montes D., Fernández-Figueiroa M. J., de Castro E., Sanz-Forcada J., 1997, A&AS, 125
Montes D., López-Santiago J., Gálvez M. C., Fernández-Figueiroa M. J., De Castro E., Cornide M., 2001, MNRAS, 328, 45
Mullan D. J., 1975, A&A, 40, 41
Nakariakov V. M., Ofman L., 2001, A&A, 372, L53
Ning Z., Cao W., Goode P. R., 2009, ApJ, 707, 1124
Parenti S., 2014, Living Reviews in Solar Physics, 11, 1
Parsons S. G., Marsh T. R., Gänscicke B. T., Tappert C., 2011, MNRAS, 412, 2563
Schmidt T. O. B., Mugrauer M., Neuhausen R., Vogt N., Witte S., Hauschildt P. H., Helling C., Seifahrt A., 2014, A&A, 566, A85
Schmieder B., Mein P., 1989, Ivar Observatory Bulletin, 13, 31
Schwartz P., Heinzel P., Anzer U., Schmieder B., 2004, A&A, 421, 323
Terradas J., Molowny-Horáková R., Wiehr E., Balthasar H., Oliver R., Ballester J. L., 2002, A&A, 393, 637
Tripathi D., Isobe H., Jain R., 2009, Space Sci. Rev., 149, 283
Vrsnak B., 1984, Sol. Phys., 94, 289
Wang Y. et al., 2010, ApJ, 717, 973
Young A., Skumanich A., MacGregor K. B., Temple S., 1990, ApJ, 349, 608
Zapiór M., Kotró P., Rudawy P., Oliver R., 2015, Sol. Phys., 290, 1647
Zaqarashvili T. V., Melnik V. N., Brazhkenko A. I., Panchenko M., Konovařenko A. A., Franzuzenko A. V., Dorovsky V. V., Rucker H. O., 2013, A&A, 555, A55
Zuckerman B., Song I., Bessell M. S., Webb R. A., 2001, ApJ, 562, L87

APPENDIX A:
Figure A1. Same description as for Fig. 7 but for Hβ.
Figure A2. Same description as for Fig. 7 but for prominence HK12P1.
Figure A3. Left panel: Spectral Hα time series of night 08/08/2012 of HK Aqr. Right panel: Residual Hα time series of night 08/08/2012 of HK Aqr. Grey shaded area indicate the prominence spectra or residuals for that night.
Figure A4. Left panel: Spectral Hα time series of night 11/08/2012 of HK Aqr. Right panel: Residual Hα time series of night 11/08/2012 of HK Aqr. Grey shaded area indicate the prominence spectra or residuals for that night.
Figure A5. Left panel: Spectral Hβ time series of night 11/08/2012 of HK Aqr. Right panel: Residual Hβ time series of night 11/08/2012 of HK Aqr. Grey shaded area indicate the prominence spectra or residuals for that night.
Figure A6. Left panel: Spectral Hα time series of night 12/08/2012 of HK Aqr. Right panel: Residual Hα time series of night 12/08/2012 of HK Aqr. Grey shaded area indicate the prominence spectra or residuals for that night.
This paper has been typeset from a \TeX/I\TeX file prepared by the author.