Review of a Decade of Research on Disordered Anderson Localizing Optical Fibers

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Nearly a decade ago, transverse Anderson localization was observed for the first time in an optical fiber with a random transverse refractive index profile. This started the development of a whole new class of optical fibers that guide light, not in a conventional core-cladding setting based on total internal reflection, but utilizing Anderson localization, where light can guide at any location across the transverse profile of the fiber. These fibers have since been used successfully in high-quality endoscopic image transport. They also show interesting nonlinear and active (lasing) properties with promising applications. This review will cover a brief history of these fibers with personal accounts of the events that led to their development in our research groups. It will then follow with recent progress and future perspectives on science and applications of these fibers.

Keywords: Anderson localization, optical fibers, transverse Anderson localization, disorder, imaging fiber, nonlinear optics, fiber lasers

1 INTRODUCTION

Nearly a decade ago, transverse Anderson localizing optical fiber (TALOF) was introduced as a novel class of optical fibers with intriguing unconventional properties [1, 2]. There has since been a rapidly growing interest in these fibers in academia and industry with their realization covering a broad range of applications including beam multiplexing [3], ultra-bend performance [3], image transport [4–8], nonlocal nonlinear behavior [9, 10], sharp focusing and wave-front shaping [11, 12], data packing using single photons [13], and random lasing [14]. In this article, we review the current progress and challenges in the development and application of TALOFs and speculate on their future potential.

TALOFs are not typical core-cladding optical fiber structures. Their refractive index profile is random (disordered) in the transverse cross-section of the fiber but, ideally, does not change along the fiber length. TALOFs guide light, not by total internal reflection as in conventional fibers but via a mechanism referred to as transverse Anderson localization (TAL). TAL is Anderson localization (AL) in a longitudinally invariant and transversely disordered optical structure. AL is the absence of diffusive wave transport in highly disordered scattering media [15–21]. Although our focus here is on optical structures, AL has been observed in various physical systems that are described by waves, including the quantum wave function of an electron governed by the Schrödinger equation (15, 22–24), matter waves and Bose-Einstein condensates [25–27], quantum fields such as photons [28–31], as well as classical waves such as acoustics/elastics [32–34], and electromagnetics [35–38].

Many research papers and review articles have discussed optical realizations of AL over the years [39–43]. Optics has access to a broad range of materials and characterization tools without requiring...
prohibitively complicated or expensive infrastructure and is a unique platform to study AL phenomena [44–49], including its interaction with nonlinearity [9, 10, 50–52]. Over the years, many attempts have been made to observe AL of light in a three-dimensional (3D) optical setting, including some recent demonstrations [53–55]. To observe 3D Anderson localization, a large refractive index contrast is typically required. Unfortunately, such large refractive index contrasts are generally accompanied by considerable losses in materials such as in metals. Because it is difficult to differentiate between the exponential decay of the optical field due to AL and that associated with loss, 3D AL of light remains a subject of active on-going research.

The possibility of TAL in optics was first explored in a pair of visionary theoretical papers independently by Abdullaev et al. [56] in 1980 and De Raedt et al. [57] in 1989. They argued that if a finite beam of light is coupled to the (transverse) cross-section of a dielectric that is transversely disordered and longitudinally invariant, it can remain spatially localized in the cross-section while propagating freely along the dielectric. The extent of the transverse localization depends on the strength of the randomness—weak randomness results in weak localization (large localization radius) and strong randomness results in strong localization (small localization radius). TAL is ubiquitous in transversely disordered lossless dielectrics with an infinitely large cross-section, regardless of the amount of disorder. However, for structures with a finite cross-section such as optical fibers, the transverse scattering must be sufficiently strong such that the localization radius stays smaller than the transverse dimensions of the dielectric to avoid boundary-induced complications [50, 58–61].

The TAL structure proposed by Abdullaev et al. and De Raedt et al. are conceptually close but different in implementation. Abdullaev et al. [56] proposed the structure sketched in Figure 1, which is a two-dimensional (2D) array of coupled optical fibers. The design parameters of the optical fibers are slightly different (random); therefore, they support optical modes with different propagation constants [62]. As such, the modes cannot couple to one another efficiently and the amplitude of optical field injected into one fiber decreases exponentially as it is coupled into the neighboring fibers. The tunneling efficiency decreases in the presence of larger randomness. In the language of supermodes, which are the collective modes of the entire structure, one observes localized modes with their radius representing the disordered waveguide’s localization radius.

The structure proposed by De Raedt et al. [57] takes a different form from that proposed by Abdullaev et al. In Figure 2 we show a waveguide similar to an optical fiber but without the core and cladding structure. The refractive index across the waveguide is pixelated into small squares of nearly wavelength-size side-widths. Each pixel is assigned a refractive index of $n_1$ or $n_2$ with a 50–50 chance. Therefore, the transverse refractive index profile of the waveguide is randomized, while the index remains invariant in the longitudinal direction. In the absence of such randomization, for example, when the entire waveguide is made from the same glass, an optical field that is launched into the facet rapidly diffracts as it propagates along the waveguide and fills the entire cross-section of the waveguide. However, for the disordered structure, the optical field scatters strongly in the transverse direction from the pixelated structure and remains localized, after a brief expansion (diffusion), as it freely propagates along the fiber. The localization radius can be generally reduced by increasing the scattering cross-section, which can be achieved, for example, by increasing the refractive index contrast $\Delta n = |n_2 - n_1|$ of the two constituent materials. The original TALOF structures developed in our groups and most of the other practical structures follow the
The design proposed by De Raedt et al. [57], which will be discussed in the rest of the review article.

2 PERSONAL ACCOUNTS ON THE DEVELOPMENT OF THE FIRST TALOFs

This Section offers personal accounts of the events that led to the development of the first TALOFs and is written as a first-person narrative by the Authors. In Figure 3, we present a chronology of selected TALOF “firsts,” which will be discussed in more detail throughout the text.

2.1 Arash Mafi

It has been quite a while, and I have to rely on my fading memory to reconstruct the events, so I may not get the exact dates right but will do my best to capture the sequence of events. Sometime in late 2008, I recall having a discussion with Karl W. Koch of Corning Incorporated, who introduced me to a couple of interesting papers on the observation of TAL [50, 63]. We briefly discussed that it would be nice to observe TAL in optical fibers. After that discussion, I asked Krishna Mohan Gundu, who was a postdoctoral researcher in my group at the University of Wisconsin-Milwaukee (UWM), to write a scalar beam propagation code and reproduce the results of De Raedt et al. [57]. After this exercise, we gained some confidence, came up with a few ideas on how to make the fiber, and decided to look for funding to support the research. We chose the Grant Opportunities for Academic Liaison with Industry (GOALI) program at the National Science Foundation (NSF). NSF-GOALI allowed us to forge a university-industry alliance. The officials at UWM and Corning were quite accommodating in letting us work on this topic and quickly came to an agreement on intellectual property rights and freedom to publish the results. We submitted the grant application in February 2010 and received the funding to start the research in August of the same year.

When we received the funding, I asked Salman Karbasi, who was a relatively new graduate student in my research group to focus his efforts on this research. Over the next few months, we brainstormed on various ways to fabricate the disordered fiber to observe TAL, while Salman was also developing his own beam propagation code. For a while, we were stalled and did not know how to approach the fiber fabrication problem. Finally, in our hopeless attempts, we decided to shift the work to microwave frequencies, essentially scaling up the structure by three orders of magnitude. Figure 4 shows one of the structures we built by filling a large pipe with candle and drilling air-holes into the structure using long drill bits in the Civil Engineering Laboratory at UWM.

While we were working on the candle waveguide, we came up with the idea of assembling the structure from polymer fibers. I looked on the web and found Paradigm Optics Incorporated that was specialized in polymer fiber drawing. I contacted the President and CEO David Welker, and mentioned what we were looking for, and he helped us select the right polymer fibers. Of course, we did not disclose much about our intentions at the time due to intellectual property restrictions. David Welker agreed to draw the fiber for a fee, and we received 80,000 strands of polyester (PS) and polymethyl methacrylate (PMMA) fibers from Paradigm Optics. We randomized and assembled the fibers into a square holder as shown in Figure 5. We shipped the randomized fibers back to Paradigm Optic, where they made it into a preform, drew the fiber, and sent it back to us. The first attempt was a total failure. However, we decided not to give up and thought that perhaps the randomization process was flawed. When we received the second set, several students worked together for 3 weeks to mix the fibers randomly. The biggest challenge, I recall, was the static charge build-up that prevented us from separating and mixing the fibers easily. After we felt comfortable with the extent of randomization, we shipped the assembled fibers back to Paradigm Optics, and they sent us the newly drawn fibers a few weeks later, in July 2011.

After we received the fibers, Salman went to the laboratory, spent a day or two aligning the optics, and observed TAL by coupling a He-Ne laser into the fiber in late July 2011. It was a joyful event for all of us, and of course, we decided to abandon the microwave project and the candles and focused on the newly developed Anderson localizing optical fiber. We decided to run many tests on our fibers and ensuring that our results were robust. It took us a while before we were fully convinced that we
had observed transverse Anderson localization for the first time in an optical fiber. The manuscript was submitted to Optics Letters on April 11, 2012, revised and accepted on April 26, 2012, and was posted online the next day.

2.2 John Ballato

While the polyester/PMMA fibers provided a necessary proof-of-principle, the transition to an all-glass TALOF was well-appreciated as being a critical step towards greater utility and practicality. Arash was aware that our Group at Clemson University had a long history of fabricating a variety of unusual fibers from unusual combinations of materials and a general willingness to try almost anything once. He contacted me around the end of 2011 to talk through an all-glass TALOF and solicit our collaboration.

Intrigued by the physics and opportunity, we set out thinking about how to best achieve a glass TALOF. Admittedly, the idea of drawing lengths from two different glasses and then stacking them into random arrays by the tens-of-thousands was not appealing. Further, and in equal candor, we were not sure it would work and did not want to spend significant time or money on the effort. We decided to try satin quartz, which is comprised of silica with small air bubbles entrained in it. Satin quartz is used by artisans because the small bubbles provide a white iridescence. Most importantly, it is cheap, and we happened already to have some for an unrelated project.

The satin quartz rod was drawn on 16 April 2012. After trying several settings to achieve reasonable draw tension and diameter control, 150 m of fiber was drawn at a temperature of about 1850°C. We did not hear anything back for several months until Arash mentioned, somewhat in passing, that the fiber had worked and that a manuscript was being drafted. We were as pleased that the satin quartz fiber worked as we were surprised, and I remember unfortunately thinking those famous last words “well that was easy.” The manuscript was submitted for consideration on 16 August 2012, published on 1 October 2012 [64], and subsequently highlighted in Spotlight on Optics [64].

3 EARLY DEMONSTRATIONS OF TAL IN DISORDERED OPTICAL FIBERS

The first two early demonstrations of TALOFs were reported in a polymer design in Ref. [1] and a silica structure in Ref. [64]. In the following, we discuss these developments.

3.1 First Polymer TALOF

The first demonstration of TALOF was reported in 2012 by Karbasi et al. [1] in a polymer structure. The design followed the structure proposed by De Raedt et al. [57] in their 1989 paper. We briefly discussed this in Section 2.1. To fabricate the first TALOF, Karbasi et al. used the stack-and-draw method to create a disordered transverse profile with the low-index component, polymethyl methacrylate (PMMA) with a refractive index of 1.49, and a high-index component, polystyrene (PS) with a refractive index of 1.59. As shown in Figure 5, 40,000 pieces of PS and 40,000 pieces of PMMA fibers were randomly mixed [65], fused together in a square container, and redrawn to a fiber with a nearly square profile and approximate side-width of 250 µm, as shown in the left panel in Figure 6. The right panel shows the zoomed-in scanning electron microscope (SEM) image of an approximately 24 µm-wide region on the tip of the fiber. To enhance the contrast between the PS and PMMA regions, the fiber tip was exposed to an ethanol solvent to
The less-than-clean assembly process with exposure of the assembly on an of strands to room dust over the 3 weeks of randomizing and observed TAL was a 60 cm segment. The visibly large variations 1 m prevented the observation of TAL in longer segments. This was performed with the scalar approximation, which is generally valid when index contrasts are small. The jury is still out for larger values of the index contrast, especially if ∆n becomes so large that the vectorial nature of the optical field must be taken into account [66]. As for the optical fill-fraction, our current understanding is that the 50–50 percent mixture of the high and low index constituent materials results in the strongest transverse scattering. However, this hypothesis has been tested only numerically and for transverse index variations on the order of a wavelength. It is possible that if the air-holes are much smaller than a wavelength, the 50–50 percent would not be the ideal ratio. As for embedding the optimal 50% ratio of the low index (possibly air) material in a higher index network, the 50% value is below the percolation threshold (59.27%) of a square lattice; therefore, the host material with the higher refractive index remains generally connected in the long-range, making the TAL non-trivial, i.e., light localization is not merely due to the disconnected clusters of the higher index material.

Another important observation made in Ref. [2] is that the statistical distribution of the mode field diameters follows a nearly Poisson-like distribution. It is observed that in the presence of a stronger transverse scattering, not only does the localization radius decrease due to a stronger TAL, but the mode-to-mode variations in the localization radius also decrease. In other words, a stronger localization is always accompanied by more uniformity of the localized modes. This is a critical observation because it sets the stage for making a practical TALOF for real-life applications. These observations led the team to look for mechanisms to increase the scattering strength by creating a larger index contrast, which eventually led to a glass-air disordered fiber structure. Another issue that was explored was the impact of the random site size on the localization radius. We will discuss this issue in some detail in Subsection 4.1.

3.2 First Silica TALOF

The first observation of the TAL in a silica fiber was reported by Karbasi et al. [64] in 2012. As already elaborated in Section 2.2, this glass-air disordered fiber was fabricated in Ballato’s group at Clemson University. The preform was made from “satin quartz” (Heraeus Quartz), which is a porous artisan glass. The air-holes in the porous glass structure became elongated air channels in the fiber drawing process. The final structure resembled the design
proposed by De Raedt et al. [57], with \( n_1 = 1.0 \) and \( n_2 = 1.46 \). In Figure 7, we show SEM images of the cross-section of this fiber, with the right panel showing a zoomed-in image. The black dots are air-holes embedded in the light-gray background matrix of silica. The diameter of the fiber shown in the left panel of Figure 7 is around 250 µm. The diameters of the air-holes vary between 0.2 and 5.5 µm. At the center of the fiber, the air-hole fill-fraction was reported to be nearly 2%, while increasing to around 7% near the edges; therefore, TAL was only observed near the periphery of the fiber. The observation of TAL near the boundary rather than the center was an issue that caused a bit of concern, considering the perceived delocalizing impact of the boundaries in disordered TAL systems [58, 67–69], which was subsequently addressed in some detail in Ref. [61].

3.3 Stack-and-Draw Method

In 2014, Chen and Li [70] at Corning Incorporated reported another successful attempt in observing TAL in an air-glass TALOF. They observed TAL in structures with significantly lower air-fill-fraction than those reported by Karbasi et al. [64]. While this requires further investigation, it is quite possible that this can be attributed to the far-subwavelength size of the transverse scattering centers and the much higher scattering center density (air-line density) compared with the structure in Figure 7.

There have since been other successful attempts in observing TAL in glass-based fibers. Starting in 2017, Axel Schülzgen’s group at CREOL, University of Central Florida, have reported various TALOF structures using the stack-and-draw technique [6, 71]. The stack-and-draw process consists of randomly mixing thousands of silica capillaries with different diameters and air-hole diameters and assembling them in a jacket tube to make the preforms. The preforms are subsequently drawn to desired diameters. For example, they reported drawing a fiber with the inner diameter of the randomly disordered region at 278 µm, and the outer diameter of 414 µm. For this particular fiber, they reported an air-filling fraction of about 28.5% where the air-hole areas ranged from 0.64 µm² to over 100 µm², with 2.5 µm² being the peak of the statistical distribution. They have since refined the fiber fabrication process and have reported excellent image transport properties that will be discussed in Section 4.

Another more recent successful development of glass TALOF, as early as 2019, is by Yasutake Ohishi’s research group at the Toyota Technological Institute in Japan [72]. They reported the fabrication of all-solid all-glass disordered fiber structures using tellurite optical glasses that can be used for near-infrared image transport. The two-glass drawing process can potentially result in undesirable stresses and cracks. To avoid this issue, they managed to develop two tellurite glasses with high compatibility in thermal and mechanical properties. The two tellurite glasses were made of TeO₂, Li₂O, WO₃, MoO₃, Nb₂O₅ (TLWMN) and TeO₂, ZnO, Na₂O, La₂O₃ (TZNL) with the adequately large refractive index contrast of \( \Delta n = 0.095 \). TLWMN and TZNl glass rods were drawn down at 440°C to fibers whose diameters were 100 µm using a home-designed fiber drawing tower. They followed a stack-and-draw process, similar to that of the polymer fiber reported in Ref. [1]. They reported the transport of optical images through the all-solid tellurite-glass TALOF, 10 cm long, in the wavelength range of 1.44–1.60 µm.

3.4 Other TALOF Materials

The basis for much of the TALOF materials development, at least as relates to all-glass versions, stems from the original work on phase-separated glasses [73]. Here, microscopic secondary phase regions were formed throughout the volume, which subsequently were elongated under strain leading to the observation of localization [74]. The intervening 35 years before this seminal work in glasses and the eventual realization of Anderson localization in (glass) optical fibers was, presumably, due largely to the lack of an obvious application, particularly as telecommunications pulled all attention for glass optical fiber materials and manufacturing. However, over the past decade, numerous innovations with respect to TALOFs, and the materials from which they are made, has been achieved. From a materials perspective, silica remains the dominant material, unsurprising given its prevalence, strength, and low optical losses. Silica-based TALOFs are routinely fabricated using both Chemical Vapor Deposition (CVD) [70] and stack-and-draw fabrication methods [6]. That said, important advancements have been made using tellurite glasses, which extends the utility of TALOFs into the
infrared spectral region [75–77] and offers the potential for infrared nonlinear fibers.

Publications do, of course, focus attention on what is deemed successful. That which is not often remains in the dark. Provided here is a brief discussion of what did not work, at least to-date, some of which is highlighted in Ref. [78]. It is useful to remember first the general design considerations: 1) large index difference between the two materials comprising the TALOF, 2) a fill-factor of approximately 50%, 3) the size of the phases being about the wavelength of the light being employed, and 4) these idealized constraints in a structure that possesses transverse randomness but longitudinal invariance. The latter suggests the stack-and-draw of a random ensemble of canes into fiber where the canes possess a high index cores of reasonably large diameter relative to the cane outer diameter. The highest index core phase made, to the Author’s best knowledge, into a glass-clad (index ~ 1.44) optical fiber is that of crystalline semiconductors, specifically Ge [79] and Si [80], with refractive indices of 4 and 3.5, respectively. Several attempts at a Si/SiO2 TALOF were ultimately unsuccessful since the drawing down to smaller dimensions either led to oxidation of the Si or dimensional instabilities due to Plateau-Rayleigh phenomena. Efforts at less extreme index contrasts were successful, particularly those employing a “hybrid” approach of using the molten core method to create novel core material canes followed by stack-and-draw to fabricate longitudinally invariant TALOFs from random stacks of said canes. In particular, core glasses in the strontium aluminosilicate system, with index of about 1.53, provided to be effective.

4 IMAGE TRANSPORT AND ILLUMINATION USING TALOFs

Perhaps the most successful application of TALOFs has been so far in imaging. This possibility was highlighted first in a paper by Karbasi et al. in Ref. [3], which showed that multiple beams can propagate simultaneously in TALOF with minimal distortion even when the fiber is bent. In a subsequent paper, Karbasi et al. [4] used simulation in a 1D structure to show that the introduction of disorder in an originally periodic structure significantly improves the image transport capabilities. Motivated by these findings, in Ref. [5], Karbasi et al. explored image propagation in the TAL polymer fiber of Ref. [1] (see Figure 5). They butt-coupled a 1951 USAF resolution test chart to the input end of the fiber—the test chart can be briefly described as a stencil into which small numbers and bars are carved. They illuminated the test chart from the input tip and images the output of the fiber on a CCD camera. The polymer TALOF provided high quality image transportation as highlighted in Figure 8 and Karbasi et al. showed that the image transport quality was comparable with or better than some of the best commercial multicore imaging fibers, with less pixelation and higher contrast. The approximate width of the point-spread function was calculated to be smaller than 10 μm at 405 nm wavelength for this TALOF in Ref. [2].

Some of the most intriguing imaging results using TALOFs have been obtained in Axel Schülzgen’s group at CREOL, University of Central Florida, since 2017 [6–8, 71, 81–90]. Over the years, they have continuously improved the quality of the stack-and-draw TALOFs, lowered the attenuation, and have improved the image quality transport. Most notably, they have applied deep-learning techniques to improve the quality of the image transport in these fibers. In a recent publication, they utilized a deep convolutional neural network and trained it to classify the output images and tested on images never seen, namely, images collected when the fiber is bent or when the fiber facet is placed several millimeters away from the object without any distal optics. Their work is a considerable advancement compared with previous reports of image transport in multimode fibers, which are susceptible to bending distortions [91].

There has been a series of exciting papers from Yasutake Ohishi’s research group at the Toyota Technological Institute in Japan on near-infrared (NIR) optical image transport in TALOFs. Their work started in 2016 focused on the fabrication of the first all-solid tellurite optical glass rod for NIR imaging [72, 75–77, 92–94]. In Ref. [72], they reported a refractive index contrast of Δn = 0.095 and observed TAL and image transport at the NIR optical wavelength of 1.55 μm. Most recently, they reported the fabrication and analysis of chalcogenide TALOFs (AsSe2/As2S3 and AsSe2/As2S5) for mid-IR image transport [95, 96]. So far, they have reported the observation of TAL in the chalcogenide TALOF and actual image transport is yet to be demonstrated in these fibers.

In addition to these reported works on optical image transport using TALOFs, Leonetti et al. [13] propagated reconfigurable localized optical patterns in the polymer TALOF of Ref. [1] and encoded up to six bits of information in the localized channels, even with a low photon count. The results they reported are interesting for the potential application of TALOFs in spatially multiplexed configurations for quantum information processing.
4.1 Wavelength Dependence of the Localization Radius and Optimal Pixel Size

The issue of the wavelength dependence of the localization radius and optimal pixel size was initially explored in Ref. [2]. In this paper, Karbasi et al. claimed that a shorter wavelength decreases the localization radius, using both simulations and experiments, and that a larger pixel size at a given wavelength decreases the localization radius. They argued that these two claims are interdependent due to the scale invariance in Maxwell’s equations. However, by carrying out extensive numerical simulations in 1D [97], they observed that the optimum value of the pixel size is around half the free-space wavelength. A more recent experiment along with simulations presented in Ref. [98] cast doubt on the results of Ref. [2] and Ref. [97] on wavelength dependence of the localization radius. Schirmacher et al. [98] observed that the mean localization radius, over a reasonable range, shows no dependence on the wavelength. Schirmacher et al. argued that the experiments conducted in Ref. [2] had large error-bars, so their results were not conclusive. Moreover, the simulations conducted in Ref. [2] ignored a term proportional to the transverse gradient of the refractive index, as is common in fiber optic simulations. Apparently, this term is responsible for making the localization radius wavelength independent. However, detailed simulations performed in Ref. [97] correctly took the transverse gradient of the refractive index into account and still showed some wavelength dependence. Therefore, this issue is inconclusive, and the matter has yet to be settled.

To address these issues, detailed numerical simulations are essential. However, the size of the numerical problem is often extremely large. A TALOF has a typical transverse dimension of a couple of hundred microns or more, with index fluctuations that are subwavelength. Therefore, such a large structure may have to be discretized into an enormous mesh in typical numerical schemes such as the Finite Element Method. The extremely large number of modes adds to this complexity, and the fact that TALOFs are random fibers and must be studied statistically. Therefore, many simulations must be performed and the results must be averaged. Fortunately, Nature has been somewhat kind and accommodating. In many cases, results obtained by fully analyzing a TALOF allow us to make broad conclusions due to the self-averaging behavior of the large number of modes supported by TALOFs. In many cases, it may also be possible to get by with simulating a much smaller structure, using the scaling properties of TAL structures [16, 19, 20, 23, 99–103].

In addition to the problems stated above, the traditional study of TAL is based on launching a beam and analyzing its propagation along the waveguide. It is hard to ensure that the results are not biased by the choice of the initial launch condition. One way to address such issues is to analyze the TALOF using the modal method and calculate the mode-area (MA) probability density function (PDF) for these structures [104, 105]. The MA-PDF encompasses all the relevant statistical information on TAL; it is independent of the launch condition and relies only the physical parameters of the TALOF. An important observation in Refs. [104, 105] is that as the transverse dimensions of TALOF increase, the MA-PDF eventually converges to a final form, especially for the localized modes. It turns out that for many practical structures and designs, the MA-PDF converges for TALOF dimensions much smaller than the sizes used in practical applications. Therefore, one can potentially find all relevant statistical information of a TALOF by simulating a much smaller structure.

4.2 Nonlinearity and Lasing in TALOFs

The interaction between nonlinearity and Anderson localization has been explored over the years with somewhat inconclusive results [51, 52, 63, 106–108]. There is evidence, at least in certain systems of interest, that a focusing Kerr-type nonlinearity may enhance the localization [63]. Other types of nonlinearity, such as thermally-induced ones, have also been observed to affect TAL [9]. An interesting recent development is the observation of nonlinear four-wave mixing (FWM) in an all-solid TALOF, which was fabricated by using a novel combination of the stack-and-draw and molten core methods [109]. This is potentially interesting in light of the fact that a TALOF is a highly multimode fiber and can provide ample multimodal phase-matching opportunities to observe FWM at many different wavelengths. The main advantage of a TALOF compared with a conventional highly multimode fiber is that it provides localized modes [110] with smaller effective areas and larger relative nonlinear coefficients, so the FWM process can be more efficient [52].

Regarding the progress on TALOF lasers, we point out that there is a large body of literature on random lasers, which is beyond the scope of this article but is covered in several review articles, including by D. S. Wiersma [111]. A notable work on TALOF-based random lasers is by Abaie et al. [14] who filled the air-holes of a glass-air TALOF with an active dye using capillary action to make a transversely disordered active medium. They pumped the TALOF-based dye laser and observed that the active TALOF results in a spectrally broad, and a stable highly directional laser beam. More research on TALOF lasers is presently conducted in Mafi’s and Ballato’s research groups.

4.3 Future Opportunities

TALOFs demonstrate many interesting linear and nonlinear properties, and we anticipate that we will see an expanded role for these fibers in photonics applications. Much of the novel properties of these fibers are driven by the multiplicity of modes that are highly localized. Therefore, future development activities will focus on making the localization radii as small as possible. For device applications, uniformity and reproducibility can also be important. Fortunately, it appears that these issues are intimately tied to one another, and reducing the localization radius is accompanied by a smaller variation in localization radii. At present, several companies are keenly interested in commercializing TALOFs for imaging. We anticipate that endoscopic imaging in visible and near-IR would be the first real-life device application for TALOFs.
Future improvements in nonlinear applications may include the simultaneous generation of many wavelengths using FWM or even making a broadband source of light comparable to light-emitting diodes or supercontinuum sources, centered around any visible or infrared wavelength. We also expect notable results in making relatively broadband and spatially incoherent (highly multimode) lasers for application in imaging and illumination.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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