Rearrangement of uncorrelated valence bonds evidenced by low-energy spin excitations in YbMgGaO$_4$

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dc-magnetization data measured down to 40 mK speak against conventional freezing and reinstate YbMgGaO$_4$ as a triangular spin-liquid candidate. Magnetic susceptibility measured parallel and perpendicular to the c-axis reaches constant values below 0.1 and 0.2 K, respectively, thus indicating the presence of gapless low-energy spin excitations. We elucidate their nature in the triple-axis inelastic neutron scattering experiment that pinpoints the low-energy ($E \leq J_0 \sim 0.2$ meV) part of the excitation continuum present at low temperatures ($T < J_0/k_B$), but completely disappearing upon warming the system above $T \gg J_0/k_B$. In contrast to the high-energy part at $E > J_0$ that is rooted in the breaking of nearest-neighbor valence bonds and persists to temperatures well above $J_0/k_B$, the low-energy one originates from the rearrangement of the valence bonds and thus from the propagation of unpaired spins. We further extend this picture to herbertsmithite, the spin-liquid candidate on the kagome lattice, and argue that such a hierarchy of magnetic excitations may be a universal feature of quantum spin liquids.

Introduction.—Quantum spin liquids (QSLs) have a special place in condensed-matter physics as states with unconventional excitations solely driven by spin degrees of freedom in the absence of charge and orbital fluctuations. The QSL physics may be behind many intriguing phenomena studied over the last decades, including the high-temperature superconductivity [1,2]. Exotic properties of the QSLs are also central to new technologies, such as topological quantum computing [3]. The prototype of a QSL was proposed by Anderson back in 1973 as a resonating-valence-bond (RVB) state, a superposition of many different partitions of the triangular spin network into valence bonds (VBs, spin-0 singlets), $\frac{1}{\sqrt{2}}(|\uparrow\uparrow\rangle - |\downarrow\downarrow\rangle)$ [1,2]. In a two-dimensional QSL, unpaired spins constitute fermionic excitations with exotic properties, the quantum number fractionalization and intrinsic topological order [4,7]. They propagate through the lattice by locally rearranging the uncorrelated VBs, an effect well established theoretically but never observed in any real material.

YbMgGaO$_4$, the triangular antiferromagnet proposed by one of us in 2015 [8], may be a window into this interesting physics. It features a triangular lattice of the Yb$^{3+}$ ions with the antiferromagnetic coupling of $J_0 \sim 0.2$ meV [9], which is equivalent to the temperature of $\sim 2$ K [8,10]. No signatures of spin freezing could be seen in the heat capacity [8], thermal conductivity [11], and muon spin relaxation ($\mu$SR) [12] measurements down to 48 mK. Although zero residual entropy ($S_m$) has been reported based on the magnetic heat capacity data down to 60 mK [8], the zero-field $\mu$SR rate only slightly increases from $\sim 0.2$ $\mu$s$^{-1}$ at 50 K to $\sim 0.3$ $\mu$s$^{-1}$ below $\sim 0.4$ K suggesting very strong quantum fluctuations [12]. A broad excitation continuum can be interpreted within the framework of a spinon Fermi surface [13], although several experimental observations have challenged this optimistic scenario. In particular, absent magnetic contribution to the thermal conductivity [11] implies the localization of fermionic excitations, possibly caused by the random distribution of Mg$^{2+}$ and Ga$^{3+}$ that has strong impact on the crystal-field levels of Yb$^{3+}$ [14,15], although its eventual effect on the magnetic parameters and spin-liquid physics remains debated [16]. Signatures of spin freezing observed in the ac-susceptibility around 0.1 K [17] seem to corroborate the importance of structural disorder, as do some of the recent theory studies suggesting the possibility of the spin-liquid mimicry [18] or the formation of a VB glass [19].

In this Letter, we critically test these scenarios by probing the low-temperature magnetization and low-energy spin excitations of YbMgGaO$_4$. We argue that the slowing down of spin fluctuations at 0.1 K affects only few spin degrees of freedom while having no serious influence on spin dynamics. This unusual dynamics can be well understood within the uncorrelated VB formalism. The high-energy excitations at $E > J_0$ are due to the breaking of nearest-neighbor (NN) VBs [20], whereas the low-energy ones at $E \leq J_0$ arise from the re-arrangement of VBs and propagation of unpaired spins. This renders YbMgGaO$_4$ different from the VB glass proposed in Ref. [19] and can’t be well captured by any theoretical model reported to date. Interestingly, similar formalism can be applied to another QSL candidate, herbertsmithite [21]. We then argue that such low-energy exci-
tions due to the re-arrangement of VBs may be generic for QSLs.

Experimental techniques.—Large-size high-quality single crystals of YbMgGaO$_4$ ($\sim$ 1 cm) were grown by the floating zone technique [10]. Two properly sized (10–20 mg) single crystals were selected for the magnetization measurements using the Faraday force magnetometer [22, 23] down to 40 mK and up to 1 T applied both parallel and perpendicular to the $c$-axis, respectively. dc and ac magnetization above 1.8 K were measured in a magnetic property measurement system (MPMS, Quantum Design) using single crystals of $\sim$ 60 mg. Eleven best-quality single crystals (total mass of $\sim$ 10 g) were selected for the cold triple-axis inelastic neutron scattering (INS) measurements on PANDA at the Heinz Maier-Leibnitz Zentrum (MLZ) [24, 25]. The international system of units is used throughout this Letter.

Absence of a conventional spin freezing.—Whereas the absence of long-range magnetic order in YbMgGaO$_4$ is well established, it remains ambiguous whether spins are static (frozen in a conventional spin glass) or dynamic at low temperatures.

Our dc magnetization measurements speak against the conventional freezing scenario. In fact, we do observe a weak anomaly (kink) at 0.1–0.2 K depending on the field direction. This anomaly could be paralleled to the broad peak in the ac-susceptibility at 0.1 K reported earlier [17], but several additional observations suggest that the low-temperature behavior of YbMgGaO$_4$ is different from simple freezing into a spin glass, where all or at least most of the spins would be static.

(i) In low fields of 0.01 and 0.02 T, the anomaly appears at $T_s^\perp \sim 0.1$ K when the field is applied along the $c$-axis [see Fig. 1(a)] and at $T_s^\parallel \sim 0.2$ K $\sim 2T_s^\perp$ when the field is applied in the ab-plane [see Fig. 1(b)]. Such a direction dependence is not expected in a conventional freezing scenario, where the transition temperature should remain the same for all field directions [26, 27], especially in the applied field as low as 0.01 T, two orders of magnitude smaller than $J_0$ [$J_0/(g\mu_B) \sim 1$ T]. We recognize that $T_s^\perp/T_s^\parallel \sim J_{xx}/J_{zz}$, where $J_{xx} = 2J_\perp \sim 2$ K and $J_{zz} \sim 1$ K [10], and the direction dependence of $T_s$ merely reflects the anisotropy of magnetic couplings, whereas the difference between $\chi_\parallel$ and $\chi_\perp$ is mostly due to the $g$-tensor anisotropy [25]. (ii) No splitting between the ZFC and FC data is observed down to 40 mK, $|\chi^{ZFC}-\chi^{FC}|/(\chi^{ZFC}+\chi^{FC}) < 2\%$ (Fig. 1). (iii) Below $T_s^\parallel$ and $T_s^\perp$, the susceptibility remains constant with $|\Delta \chi/\chi| < 2\%$ (Fig. 1), while in a conventional spin glass the ZFC susceptibility should significantly decrease below the freezing point. We note in passing that even in the ac-data the decrease is relatively small, less than 8\% upon going from $\sim 0.1$ K down to 50 mK [17]. (iv) Phenomenologically, there is no $T_c \sim 0.1$ K scaling behavior of the magnetization upon approaching the anomaly from above [23, 28]. Both the magnetic susceptibility and heat capacity show power-law behavior [29–31], $\chi \sim (T-T_c)^{-\gamma}$ and $C_m \sim (T-T_c)^{\alpha}$, where $\gamma \sim 1/3$ [25], $\alpha \sim 2/3$ [8], and $T_c$ = 0 K. (v) The anomaly in the dc-data shifts to higher temperatures upon increasing the magnetic field and follows the Zeeman energies in the zero-field limit [25], similar to paramagnets [32]. In contrast, magnetic field will generally suppress the transition in a conventional spin glass, so that the opposite trend would be observed [33, 34].

Should the low-$T$ state of YbMgGaO$_4$ be a spin glass, it must be highly unconventional. However, it seems more plausible that a small amount of frozen spin degrees of freedom [$S_m(0.1 \text{ K}) \leq 3\%$] [8] coexists with the majority remaining dynamic. Moreover, finite zero-temperature susceptibility reveals the presence of gapless low-energy excitations that may be central to the physics of YbMgGaO$_4$. We elucidate their nature below.

High-energy spin excitations.—Before turning to the low-energy part of the spectrum, let’s briefly discuss its high-energy part. Previous time-of-flight LET data suggested that excitations above 0.5 meV can be naturally ascribed to the breaking of NN VBs [20]. Such a high-energy excitation continuum centered at 3–6 J$_0$ is also clearly observed in the triple-axis measurement on PANDA up to 20 K [see Fig. 2(a)–2(c)]. The wave-vector dependence of the spectral weight is well described by the $S_{q1}$ model that includes the breaking of uncorrelated NN VBs, for both the LET data integrated over 0.5 $\leq E \leq 1.5$ meV [20] and the PANDA data collected at $E = 0.7$ meV [25]. Because a finite energy of $J_0$ is needed to break a singlet, the high-energy continuum clearly shows a gap at $E \leq J_0$ [see Fig. 2(c)], confirming the scenario of NN VB excitations [20]. The temperature dependence of the dynamical spin susceptibilities roughly follows that of the bulk susceptibilities [25], suggesting that our INS
signal is predominantly magnetic.

Recently, the signal observed at high temperatures (10 K) was attributed to the anisotropy of the magnetic form-factor (MFF) of Yb$^{3+}$ [35]. As MFF is independent of the transfer energy $E$ [36], and high temperature smears the low-energy excitations out, we expect that any $Q$-dependence observed at high temperatures and low energies should be due to the MFF. However, we find that the INS signal measured at 20 K is almost $Q$-independent, and shows no anisotropy at $E \leq J_0$ [see Fig. 2(c) and 2(f)]. Therefore, the $Q$-dependent INS signal observed at $E > J_0$ and 20 or 35 K [see Fig. 2(c)] predominantly originates from the spin-spin correlations, and not from the anisotropy of MFF. This anisotropy is negligible, and the dipole approximation for the MFF is good enough for YbMgGaO$_4$ at $|Q| \leq 4\pi/\sqrt{3a} \sim 2.2$ Å$^{-1}$ [30].

**Low-energy spin excitations.—**The temperature-independent spin susceptibility below $T_0$ and $T_1$ (Fig. 1) and the power-law behavior of the magnetic heat capacity [8] suggest the presence of distinct gapless low-energy excitations in YbMgGaO$_4$. Unfortunately, these excitations were not well resolved in our previous time-of-flight data [20], where contamination by the background signal from the magnet posed a serious problem [25] that we were able to remedy in the triple-axis experiment performed without the magnet.

The high-energy excitations are fully gapped, and the INS signal becomes wave-vector independent at 20 K below $\sim J_0$ [see Fig. 2(c) and 2(f)]. Conversely, the INS signal at low temperatures (70 and 750 mK) shows a pronounced $Q$-dependence at $E \leq J_0$ [see Fig. 2(a), 2(b), 2(d), and 2(e)], which is now characteristic of the low-energy part of the excitation continuum. These excitations are very different from their high-energy counterparts [Fig. 2(d)]. Indeed, fitting with the same $S_{M}$ model leads to the least-$R_{p}$ = 1.44 at 70 mK and least-$R_{p}$ = 1.37 at 750 mK [Fig. 2(e)] [25]. The most conspicuous differences at low energies are the significantly narrowed peaks in the $Q$-dependence (along $[0, \xi, 0]$ for example) and the higher intensity around the $\Gamma$ points [Fig. 2(d) and 2(e)]. We notice that the INS signal of the kagome-lattice QSL candidate, ZnCu$_3$(OD)$_6$Cl$_2$, shows very similar features in the low-energy part of the spectrum (i.e., at energies below $J$) [21].

Qualitatively, the narrowing of the $Q$-dependence in-
in a RVB/QSL state, the low-energy excitations arise from several processes that involve VBs and unpaired spins \[25\]. One example would be the recent phenomenological model by Kimchi \textit{et al.} who proposed \(f_1:f_2 = 4:1\) and \(f_3 = 0\) \((j \geq 3)\) [see Eq. (1)] for the low-energy excitations \[19\]. This model successfully explains the relative increase in the INS intensity around the M points below \(J_0\) [see Fig. 2(a) and 2(b)], but does not account for the narrowing of the Q-dependence and for the increased intensity around the \(\Gamma\) points \[24\].

Therefore, the processes of the second type should be taken into account. The constant susceptibility in the zero-temperature limit would suggest the presence of unpaired spins not bound into VBs, so we focus on those processes that combine the re-arrangement of the VBs with the propagation of unpaired spins. They are exemplified in Fig. 3 that shows the \(S^\parallel_{\ell\geq1}\) model with \(f_2 = -1/4, f_3 = -1/8,\) and \(f_1 = 0\) \((j \geq 4,\) here we fix \(f_1 = 1)\) [see Eq. (1)] \[23\]. This model describes the experimental low-energy INS data much better than the \(S_3^1\) model, with the least-\(R_p = 1.00\) at 70 mK and least-\(R_p = 1.03\) at 750 mK [Fig. 2(e)], respectively.

The best description of the experimental data is achieved by treating \(f_j (j \geq 2)\) as free parameters while fixing \(f_1 = 1\). We find that two such parameters, \(f_2\) and \(f_3\), are sufficient to fit the spectra. The addition of \(f_4\) does not improve the fits significantly \[27\], indicating a relatively short correlation length, \(\xi_{\ell\geq1} \sim 2a = 6.8\) \(\AA\) \[25\]. Through the \(S_{1\ell}+f_2S_{2\ell}+f_3S_{3\ell}\) fits, we get \(f_2 = -0.18, f_3 = -0.21\) with the least-\(R_p = 0.89\) at 70 mK [Fig. 2(d)] and \(f_2 = -0.18, f_3 = -0.24\) with the least-\(R_p = 0.87\) at 750 mK [Fig. 2(e)]. For the quasielastic neutron scattering at 0.07 meV, the very similar results are obtained \[25\]. The fitted values of \(f_2\) and \(f_3\) are relatively close to those expected for the scattering process depicted in Fig. 3(a), suggesting that the re-arrangement of VBs and the propagation of unpaired spins, not bound into VBs, between second and higher neighbors should be considered.
agitation of unpaired spins make a significant contribution to the low-energy excitations.

Discussion.—In Ref. [20], we conjectured that the high-energy part of the excitation continuum arising from the breaking of NN VBs should be preceded by the distinct low-energy part driven by excitations of different nature. We are now able to confirm directly that the Q-dependence of the spectral weight changes indeed. At low energies, spin-spin correlations extend beyond nearest neighbors and can be represented by the re-arrangement of VBs that facilitates the propagation of unpaired spins. This is reminiscent of the original concept of fermionic excitations [13], although the propagation of unpaired spins in YbMgGaO$_4$ must be limited, as no magnetic contribution to the thermal conductivity has been observed [11]. We suggest that random magnetic couplings caused by the mixing of Mg$^{2+}$ and Ga$^{3+}$ may restrict the propagation of unpaired spins. We also note that unpaired spins are integral to the ground state of YbMgGaO$_4$, and their concentration estimated from the size of the INS background [23] is significantly larger than the fraction of spins that may become frozen around 0.1 K.

On a related note, we mention that a similar description of low-energy excitations holds for the QSL candidate herbertsmithite (ZnCu$_3$(OH)$_6$Cl$_2$) that features spins on the kagome lattice [21, 22]. Moreover, the similar narrowing of the excitation continuum at low energies was also reported in the one-dimensional K$_2$CuF$_3$ [38, 39] and honeycomb Kitaev system α-RuCl$_3$ [40, 41] and honeycomb Kitaev system α-RuCl$_3$ [40, 41].

Conclusions.—The low-T magnetization data and low-energy neutron spectroscopy help us to resolve several open issues in the putative spin-liquid physics of YbMgGaO$_4$. Our observations suggest that only an insignificant fraction of spin degrees of freedom may become static, whereas dynamics of the majority gives rise to the broad excitation continuum. We interpret this continuum as consisting of two parts, the breaking of nearest-neighbor VBs at high energies and the re-arrangement of VBs at low energies. Although the low-energy excitations we observed are rather similar to the anticipated fermionic excitations, the propagation of unpaired spins must be curtailed. More generally, we argue that a similar formalism of the low-energy rearrangement of VBs is applicable to herbertsmithite and may be a universal feature of spin-liquid states with unusual spin dynamics, a problem that clearly warrants further theoretical investigation.

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