Pressure Observer Based Adaptive Dynamic Surface Control of Pneumatic Actuator with Long Transmission Lines

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Featured Application: This research dedicates to develop a pressure observer based nonlinear controller for precise position control of the MRI-compatible pneumatic servo system with long transmission lines.

Abstract: In this paper, the needle insertion motion control of a magnetic resonance imaging (MRI) compatible robot, which is actuated by a pneumatic cylinder with long transmission lines, is considered and a pressure observer based adaptive dynamic surface controller is proposed. The long transmission line is assumed to be an intermediate chamber connected between the control valve and the actuator in series, and a nonlinear first order system model is constructed to characterize the pressure losses and time delay brought by it. Due to the fact that MRI-compatible pressure sensors are not commercially available, a globally stable pressure observer is employed to estimate the chamber pressure. Based on the model of the long transmission line and the pressure observer, an adaptive dynamic surface controller is further designed by using the dynamic surface control technique. Compared to the traditional backstepping design method, the proposed controller can avoid the problem of “explosion of complexity” since the repeated differentiation of virtual controls is no longer required. The stability of the closed-loop system is analytically proven by employing the Lyapunov theory. Extensive experimental results are presented to demonstrate the effectiveness and the performance robustness of the proposed controller.

Keywords: pneumatic servo system; long transmission line; pressure observer; dynamic surface control; position tracking

1. Introduction

The magnetic resonance imaging (MRI) technique is widely used in clinical diagnosis due to its ability to image without the use of ionizing x-rays and superior soft tissue contrast as compared to computed tomography (CT) scanning. Recently, pneumatically actuated MRI-compatible robots, which enable real-time magnetic resonance (MR) image-guided needle placement, are designed for brachytherapy and biopsy by several researchers [1–15]. To fulfill the requirements for MR compatibility of the robotic systems, pneumatic valves are commonly placed outside the scanner room in the aforementioned works. Therefore, long transmission lines between the actuators and valves are used. Since long transmission lines have a significant influence on the pressure dynamics of the pneumatic system and MRI-compatible pressure sensors are not commercially available, precise position control is one of the main technical challenges in robot development.

Indeed, considerable research effort has been devoted to addressing the issue related to long transmission lines. Richer et al. [16] suggested a formula for the time delay and amplitude attenuation...
between the mass flows at the outlet and inlet of the line, as well as a formula for the pressure drop along the tube. Although this approach was later employed in many other studies (Jiang et al. [14]; Richer et al. [17]), it has been proven improper for long transmission lines (>2 m) [18]. Yang et al. [8] adopted a first order transfer function with time delay to describe the 9-m transmission line dynamics. However, for some unknown reason, the authors omitted the transmission line dynamics in the subsequent controller design. Based on the discretization of a general set of equations from fluid mechanics, two similar distributed models of long pneumatic transmission lines were derived by Li et al. [19] and Krichel et al. [20]. However, this type of model is not suitable for controller design for their high order and low computational speed. Turkseven et al. [21] developed a simplified distributed model to characterize the additional dynamics brought by the long transmission lines.

As previously mentioned, direct pressure measurement is unavailable for the lack of MRI-compatible pressure sensors. However, pressure states are commonly used in controller design for precise position control of a pneumatic actuator. To solve this problem, pressure observers were used in place of a pressure sensor in many studies. Pandian et al. [22] investigated two design methods of an observer to estimate the chamber pressures in a pneumatic cylinder. While a continuous gain observer was used to estimate one of the chamber pressures with the assumption that the other one is measured in the first method, a sliding mode observer was utilized to estimate both chamber pressures in the second method. In this study, the mass flow rate was assumed to be exactly known, which is apparently too restrictive in practice. Wu et al. [23] conducted an analysis on observability and concluded that the pressure states in the pneumatic servo system are not locally observable from the measurement of the output motion within several regions in the state space. Based on the actuator pressure dynamics, various observers are developed, such as the sliding-mode observer (Bigras [24]), energy-based Lyapunov observer (Gulati et al. [25]), and adaptive nonlinear observer (Langjord et al. [26]). It should be noted that the performance of these observers relies on the accuracy of the valve model. Driver et al. [27] developed a pressure estimation algorithm by utilizing the measured actuation force and the hypothesized average air pressure in the actuator. Turkseven et al. [18] presented a pressure observation method by using the measured force and piston displacement. However, the requirement for force sensing in the MRI environment is particularly burdensome because the MRI-compatible force sensor is not available commercially and its development cost is high.

Recently, the backstepping design method has been proven to be a very effective way to develop nonlinear robust controllers for pneumatic servo systems. However, this method has the problem of “explosion of complexity” since the requirement of repeated differentiation of virtual controls. Thus, a practical implementation is difficult. To solve this problem, Swaroop et al. [28] proposed the dynamic surface control (DSC) method, in which the calculation of the virtual control variable’s derivative was prevented by introducing a filter at each design step. Since then, the DSC method has been the topic of significant research efforts and a number of excellent theoretical contributions have been made. The applications of DSC can be found in many engineering fields, for example, hydraulic servo systems [29], underwater/autonomous surface vehicles [30], mobile wheeled inverted pendulum [31], pneumatic artificial muscle [32], and servo motor [33].

In this study, the needle insertion motion control of the MRI compatible robot developed in our lab is considered. The robot is actuated by a pneumatic cylinder with long transmission lines. The focus of this paper is dealing with the issue of long transmission lines and realizing a high accuracy control of a pneumatic actuator with a pressure observer. Therefore, the long transmission line is assumed to be an intermediate chamber connected between the control valve and the actuator in series, and a pressure observer based adaptive dynamic surface control is proposed. The main contributions are: (1) The long transmission line dynamic is approximated as a nonlinear first order system, which can estimate the pressure losses and time delay through the long transmission line precisely in real time. (2) A pressure observer, which is proven to be globally stable, is developed to estimate the chamber pressure in a pneumatic actuator with a long transmission line. (3) In contrast to most of the existing nonlinear robust controllers synthesized by the backstepping method, by using the dynamic surface control
(DSC) technique, the proposed controller can cope with the problem of “explosion of complexity”, since the repeated differentiation of virtual controls is no longer required. The rest of this paper is organized as follows: Section 2 presents the dynamic models and problem statement; Section 3 gives the design and stability proof of the pressure observer based adaptive dynamic surface controller; Section 4 presents the experimental results to demonstrate the performance of the proposed controller; and Section 5 draws the conclusions.

2. Dynamic Models and Problem Formulation

As shown in Figure 1, a 5-DOF (degree of freedom) MRI compatible robot for abdominal and thoracic punctures was built in our laboratory. The robot’s mechanism design was developed such that all motions were decoupled and actuated by pneumatic cylinders. With the help of the robot, the physician could manipulate the needle remotely without moving the patient out of the MRI scanners. A schematic of the pneumatic servo system driving the needle insertion motion is depicted in Figure 2. The pneumatic cylinder (customized product from XMC Corp., Ningbo, China), which had a 150 mm stroke and 10 mm diameter bore, was made of nonmagnetic material to ensure MRI compatibility. While Chamber A was controlled by a proportional directional control valve (FESTO MPYE-5-M5-010-B), a tank was used to maintain the pressure of Chamber B at a specified constant level for safety reasons. The control valve was connected to the cylinder via a 10 m transmission line since it had to be placed away from the MRI scanner. A pressure observer was needed to estimate the pressure of Chamber A, since direct measurement was expensive for the lack of MRI-compatible pressure sensors. The main purpose of this paper was to find a way to deal with the issue of the long transmission line and realize high accuracy control of a pneumatic cylinder with pressure observation. For the purpose of comparison, the pressures at the two ends of the long transmission line, as well as the supply pressure were measured by three pressure sensors (FESTO SDET-22T-D10-G14-I-M12). The piston position was obtained with an optical position sensor (Micronor MR328). The controller was programmed in Simulink on a dSPACE DS1103 control system with a 1 ms sampling period.

Figure 1. Virtual prototype of a 5-DOF (degree of freedom) magnetic resonance imaging (MRI) compatible robot for abdominal and thoracic punctures.
As shown in [34], the motion of the piston–rod–needle assembly can be expressed as:

$$m\ddot{x} = p_a A_a - p_b A_b - p_0 A_s - b\dot{x} - F_I S_f(x) - d_I,$$  

(1)

where $x$, $\dot{x}$, and $\ddot{x}$ are the piston position, velocity, and acceleration, respectively, $m$ is the normal mass of the piston–rod–needle assembly, $p_a$ and $p_b$ denotes the absolute pressures of actuator chambers, $p_0$ is the ambience pressure, $A_a$ and $A_b$ are the cross section areas of piston chambers, $A_s$ is the cross section area of the rod, $b$ is the total load and cylinder viscous friction coefficient, $F_I$ is the unknown friction coefficient, $S_f(x)$ is a continuous function, which is always chosen as $S_f(x) = \frac{r}{2}\arctan(900x)$, $F_I S_f(x)$ is utilized as the smooth approximation for the usual static discontinuous Coulomb friction force, and $d_I$ represents the unmodeled dynamics and external disturbances.

With the assumption that the discharging and charging processes are both isothermal, the pressure dynamic in the actuator chamber can be modeled as [16,35]:

$$p_a = \frac{RT_a}{V_a} \dot{m}_a - \frac{A_a p_a}{V_a} \dot{x}, \quad V_a = V_{a0} + A_a \left(\frac{L_c}{2} + x\right),$$  

(2)

where $R$ is the gas constant, $T_a$ is the ambient temperature, $V_a$ is the volume of the cylinder chamber $A$, $\dot{m}_a$ is the mass flow entering or exiting the chamber $A$, $V_{a0}$ is the dead volume of the cylinder chamber $A$, and $L_c$ is stroke of the actuator. $\dot{m}_a$ can be calculated by [16]:

$$\dot{m}_a = (p_l - p_a) \frac{p_v A_l D_l}{32 R T_s L_s \mu},$$  

(3)

where $p_l$ is the average air pressure in the transmission line, $p_v$ is the measured air pressure at the work port of the control valve, $L_s$, $A_l$, and $D_l$ denote the length, cross section area, and inner diameter of the transmission line, respectively, and $\mu$ is the dynamic viscosity of air.

As shown in Figure 2, the long transmission line is assumed to be an intermediate chamber connected between the control valve and the actuator in series, thus, the following equation is formulated to represent the pressure dynamic of the line [16,35]:

$$\dot{p}_l = \frac{RT_s}{V_l} (m_v - \dot{m}_a),$$  

(4)

Figure 2. Schematic of the pneumatic servo system used to drive the needle insertion motion.
Then, there exists a compact set \( \Omega \) will be given later.

\[
\hat{\pi} = A(u)K_\pi p_u, p_d, T_u)
\]

where \( A(u) \) is the effective valve orifice area, \( u \) is the control valve’s control input, \( C_d \) is the discharge coefficient, \( C_1 \) is a constant with a value of 0.0404, \( p_u \) and \( p_d \) are the upstream pressure and the downstream pressure, respectively, \( T_u \) is the upstream temperature of air, and \( p_r \) is the critical pressure ratio. Therefore, \( \hat{m}_v = A(u)K_q(p_u, p_d, T_u) \) when the line is charging, and \( \hat{m}_v = A(u)K_q(p_v, p_d, T_u) \) when the line is discharging.

Choose the state vectors
\[
x = [x_1, x_2, x_3, x_4]^T \text{ as } x_1 = x, x_2 = \dot{x}, x_3 = p_a \text{ and } x_4 = p_i \text{, thus the system dynamics can be expressed in a state-space form as:}
\]

\[
\begin{align*}
\dot{x}_1 &= x_2 \\
mx_2 &= A_x x_3 - A_b p_b - p_0 A_r - b x_2 - A_i S_i(x_2) - d_i \\
x_3 &= \frac{RT_a}{V_a} m_a - \frac{A_x^2 x_3}{V_a} \\
x_4 &= \frac{RT_a}{V_a} (\hat{m}_v - m_a)
\end{align*}
\]

The control objective is to synthesize a control input \( u \) for the system Equation (6) such that \( x \) tracks the desired trajectory \( x_d \) with a guaranteed transient and final tracking accuracy. Instead of using the pressure sensor, a globally stable pressure observer is developed to estimate the pressure in chamber A. The parametric uncertainties due to unknown \( b \) and \( A_i \) and unknown external disturbances will be explicitly considered in this paper.

**Assumption 1:** The desired trajectory \( x_d \) is at least second-order differentiable, and \( x_d, \dot{x}_d, \ddot{x}_d \) and \( \dddot{x}_d \) are bounded. Then, there exists a compact set \( \Omega_0 = \left\{ [x_d, \dot{x}_d, \ddot{x}_d]^T : x_d^2 + \dot{x}_d^2 + \ddot{x}_d^2 \leq B_0 \right\} \) such that \( [x_d, \dot{x}_d, \ddot{x}_d]^T \in \Omega_0 \), where \( B_0 \) is a positive constant.

**Assumption 2:** The extent of parametric uncertainties and external disturbances can be predicted and given by \( b_{\text{min}} \leq b \leq b_{\text{max}}, F_{\text{min}} \leq F \leq F_{\text{max}}, \text{ and } d_{\text{min}} \leq d \leq d_{\text{max}} \).

3. Controller Design

3.1. Pressure Observer

The following observer is proposed to estimate the pressure of the actuator chamber A and the average air pressure in the transmission line:

\[
\begin{align*}
\dot{\hat{p}_a} &= \frac{RT_a}{V_a} \hat{m}_a - \frac{A_x}{V_a} \hat{p}_a \\
\dot{\hat{p}_i} &= \frac{RT_a}{V_a} (\hat{m}_v - \hat{m}_a)
\end{align*}
\]

where \( \hat{p}_a \) and \( \hat{p}_i \) represent the estimates of \( p_a \) and \( p_i \), \( \hat{m}_a \) and \( \hat{m}_v \) denote the estimated mass flow rates according to Equation (3) and Equation (5) based on \( \hat{p}_a \) and \( \hat{p}_i \). It should be noted that the proposed observers are closed loop because of the relationship between the estimated mass flow rates and the estimated pressures. Proof of the convergence between the actual pressures and the estimated ones will be given later.
To verify the convergence between the actual pressures and the estimated pressures, the following Lyapunov function candidate was considered:

\[ V_o = V_{o1} + V_{o2}, \]

\[ V_{o1} = \frac{1}{2} \left( p_a - p_a \right)^2, \]

\[ V_{o2} = \frac{1}{2} \left( \hat{p}_a - V_a \right)^2, \]

where \( \hat{p}_a = p_a - \hat{p}_a \), and \( \hat{p}_1 = p_1 - \hat{p}_1 \).

The time derivative of \( V_{o1} \) is:

\[ \dot{V}_{o1} = \left( p_a V_a - \hat{p}_a V_a \right) \frac{d}{dt} \left( \hat{p}_a V_a - \hat{p}_a V_a \right) \]

\[ = RT_s V_a (p_a - \hat{p}_a)(\hat{m}_a - \hat{m}_a) \]

(9)

According to the Equation (3), one can obtain:

1. \( p_a > \hat{p}_a \) implies that \( \hat{m}_a < \hat{m}_a \), resulting in \( \hat{p}_a V_a - \hat{p}_a V_a > 0 \).
2. \( p_a < \hat{p}_a \) implies that \( \hat{m}_a > \hat{m}_a \), resulting in \( \hat{p}_a V_a - \hat{p}_a V_a < 0 \).
3. \( p_a = \hat{p}_a \) implies that \( \hat{m}_a < \hat{m}_a \), resulting in \( \hat{p}_a V_a - \hat{p}_a V_a = 0 \).

Therefore, \( \dot{V}_{o1} \) is negative semi-definite.

The time derivative of \( V_{o2} \) is:

\[ \dot{V}_{o2} = (p_1 V_1 - \hat{p}_1 V_1)(p_1 V_1 - \hat{p}_1 V_1) \]

\[ = RT_s V_1 (p_1 - \hat{p}_1)(\hat{m}_c - \hat{m}_c) - RT_s V_1 (p_1 - \hat{p}_1)(\hat{m}_a - \hat{m}_a) \]

(10)

According to the Equation (3), one can obtain:

1. \( p_1 > \hat{p}_1 \) implies that \( \hat{m}_a > \hat{m}_a \), resulting in \( p_1 V_1 - \hat{p}_1 V_1 > 0 \).
2. \( p_1 < \hat{p}_1 \) implies that \( \hat{m}_a < \hat{m}_a \), resulting in \( p_1 V_1 - \hat{p}_1 V_1 < 0 \).
3. \( p_1 = \hat{p}_1 \) implies that \( \hat{m}_a = \hat{m}_a \), resulting in \( p_1 V_1 - \hat{p}_1 V_1 = 0 \).

For the mass flow rate relationship given by Equation (5), it has been proven in [25] that the term \( (p_1 - \hat{p}_1)(\hat{m}_c - \hat{m}_c) \) is always non-positive. Thus, \( \dot{V}_{o2} \) and \( V_o \) are negative semi-definite, one can conclude that the proposed pressure observers are globally Lyapunov stable with regard to the errors in the estimated pressures.

3.2. Adaptive Dynamic Surface Controller

Step 1: Differentiate the trajectory tracking error \( e_1 = x_1 - x_d \) with respect to time leads to:

\[ \dot{e}_1 = x_2 - \dot{x}_d. \]

(11)

Consider \( x_2 \) as the first virtual control input, the virtual control law is designed as follows:

\[ \bar{x}_{2d} = \dot{x}_d - k_1 e_1, \quad k_1 > 0, \]

(12)

where \( k_1 \) is a positive control gain. Following the dynamic surface control theory [28], the signal \( \bar{x}_{2d} \) is fed to a low pass filter to obtain a new one \( x_{2d} \) for the next design step:

\[ \tau_1 \dot{x}_{2d} + x_{2d} = \bar{x}_{2d}, \quad x_{2d}(0) = \bar{x}_{2d}(0), \quad \tau_1 > 0, \]

(13)

where \( \tau_1 \) is the filter parameter.

Step 2: Define the first surface error as \( s_1 = x_2 - x_{2d} \), its time derivative can be derived as:

\[ \dot{s}_1 = \dot{x}_2 - \dot{x}_{2d} = A_3 x_3 - \frac{1}{m} \left[ p_b A_b + p_0 A_r + b x_2 + F_i S_i(\dot{x}) + d_i \right] - \frac{1}{\tau_1} (\bar{x}_{2d} - x_{2d}), \]

(14)
where $\bar{A}_a = A_a/m$.

Define $\dot{x}_3 = x_3 - \dot{x}_3$, and let $\zeta = \dot{x}_3$ be the second virtual control input, the virtual control law is designed as follows:

$$\ddot{z}_d = \frac{1}{A_a} \left( \frac{1}{m} [p_A A_b + p_B A_t + \dot{b} x_2 + \dot{F}_t S_t(x) + \dot{d}_t] + \frac{1}{\tau_1} (\ddot{x}_{2d} - x_{2d}) - k_2 s_1 - \frac{h^2}{4\eta_1} s_1 \right),$$  \hspace{1cm} (15)

where $k_2 > 0$ is a positive control gain, $\eta_1 > 0$ is a controller parameter, and $h_1$ is a known function that will be determined later, $\ddot{b}, \dot{F}_t,$ and $\dot{d}_t$ are the estimates of $b, F_t,$ and $d_t$, respectively. $\ddot{b}, \dot{F}_t,$ and $\dot{d}_t$ are updated by:

$$\dot{\hat{b}} = \text{Proj}_{\hat{b}} \left( -\frac{\gamma_1}{m} x_{2s_1} \right),$$  \hspace{1cm} (16)

$$\dot{\hat{F}}_t = \text{Proj}_{\hat{F}_t} \left( -\frac{\gamma_2}{m} S_t(x_2) s_1 \right),$$  \hspace{1cm} (17)

$$\dot{\hat{d}}_t = \text{Proj}_{\hat{d}_t} \left( -\frac{\gamma_3}{m} s_1 \right),$$  \hspace{1cm} (18)

where $\gamma_1 > 0, \gamma_2 > 0, \text{and } \gamma_3 > 0$ are the observer gains, and the projection mapping is defined as:

$$\text{Proj}_{\hat{x}}(\cdot) = \begin{cases} 0, & \text{if } \dot{\hat{x}} = \xi_{\text{max}} \text{ and } \cdot > 0 \\ 0, & \text{if } \dot{\hat{x}} = \xi_{\text{min}} \text{ and } \cdot < 0 \\ \cdot, & \text{otherwise} \end{cases}$$  \hspace{1cm} (19)

where $\xi$ is a symbol that can be replaced by $\hat{b}, \hat{F}_t,$ and $\hat{d}_t$.

Similarly, the signal $\ddot{z}_d$ is fed to a low pass filter to obtain a new one $\zeta_d$ for the next design step:

$$\tau_2 \ddot{\zeta}_d + \zeta_d = \ddot{z}_d, \zeta_d(0) = \ddot{z}_d(0), \tau_2 > 0,$$  \hspace{1cm} (20)

where $\tau_2$ is the filter parameter.

**Step 3:** Define the second surface error as $s_2 = \zeta - \zeta_d$, its time derivative can be derived as:

$$\dot{s}_2 = \dot{\zeta} - \dot{\zeta}_d = \dot{x}_3 - \ddot{x}_3 = \frac{RT}{v_a} \dot{m}_a - \frac{A_d x_2}{v_a} \ddot{x}_3 - \frac{1}{\tau_2} (\ddot{z}_d - \zeta_d)$$  \hspace{1cm} (21)

where $a = \frac{p_c A_d D_t}{2 \rho T_{s1} l_0 b}$.

Let $\chi = -\dot{x}_4$ be the third virtual control input, the virtual control law is designed as follows:

$$\ddot{\chi}_d = \frac{V_a}{RT_{s1}} \left[ \left( \frac{A_d x_2}{V_a} - \frac{RT_{s1}}{V_a} \right) \dot{x}_3 + \frac{1}{\tau_2} (\ddot{z}_d - \zeta_d) - k_3 s_2 \right],$$  \hspace{1cm} (22)

where $k_3 > 0$ is a positive control gain. Similarly, the signal $\ddot{\chi}_d$ is fed to a low pass filter to obtain a new one $\zeta_d$ for the next design step:

$$\tau_3 \ddot{\zeta}_d + \zeta_d = \ddot{\chi}_d, \zeta_d(0) = \ddot{\chi}_d(0), \tau_3 > 0,$$  \hspace{1cm} (23)

where $\tau_3$ is the filter parameter.

**Step 4:** Define the second surface error as $s_3 = \chi - \zeta_d$, its time derivative can be derived as:

$$\dot{s}_3 = \dot{\chi} - \dot{\zeta}_d = -\dot{x}_4 - \ddot{x}_3 = -\frac{RT}{v_a} (\ddot{m}_v - \ddot{m}_n) - \frac{1}{\tau_3} (\ddot{z}_d - \zeta_d).$$  \hspace{1cm} (24)
Similarly, the following control law $q_d$ for $\hat{m}_v$ is proposed:

$$
q_d = \hat{m}_v - \frac{RT_s}{V_f} \left[ \frac{1}{\tau_3} (\dot{\zeta}_d - \zeta_d) - k_4 \delta_3 \right],
$$

(25)

where $k_4 > 0$ is a positive control gain.

Once the $q_d$ is calculated, the desired effective valve orifice area $A(u)$ can be calculated by:

$$
A(u) = \begin{cases} 
\frac{q_d}{k_4(p_q,p_v,I_s)} & q_d > 0 \\
\frac{q_d}{k_4(p_q,p_0,I_s)} & q_d \leq 0 
\end{cases}.
$$

(26)

Thus, the input signal $u$ for the proportional-directional control valve could be obtained according to the relation between the input signal and effective valve orifice area.

The proposed pressure observer based adaptive dynamic surface control is illustrated in Figure 3.

![Figure 3. Block diagram of the control system.](image)

### 3.3. Proof of Stability

**Theorem 1.** Consider the closed loop pneumatic servo system consisting of the plant Equation (6), the nonlinear control law Equation (25), the pressure observers Equation (7), and the parameter and disturbance estimation algorithm Equations (16)–(18) under the Assumption 1–2. If there exists a set of the feedback gains and the filter constants satisfying $\gamma = \min \left\{ k_1 - 1, k_2 - \frac{1}{2} - \bar{A}_a, k_3 - \frac{1}{5} \bar{A}_a, k_4 - \frac{1}{2} \bar{A}_a, 1 - \frac{1}{2} \bar{A}_a \right\} > 0$, then the closed loop system is uniformly and ultimately bounded.

**Proof.** Consider the following Lyapunov function candidate:

$$
V_c = V_{es} + V_{ez} + V_{\theta}, \quad V_{es} = \frac{1}{2} z_1^2 + \frac{1}{2} z_2^2 + \frac{1}{2} z_3^2, \quad V_{ez} = \frac{1}{2} \bar{z}_1^2 + \frac{1}{2} \bar{z}_2^2 + \frac{1}{2} \bar{z}_3^2,
$$

$$
V_{\theta} = \frac{1}{2} \gamma_1 \dot{\gamma}_1 \ddot{\theta}_1^2 + \frac{1}{2} \gamma_2 \dot{\gamma}_2 \ddot{\theta}_2^2 + \frac{1}{2} \gamma_3 \dot{\gamma}_3 \ddot{\theta}_3^2.
$$

(27)

where $z_1 = x_{2d} - \bar{x}_{2d}$, $z_2 = \zeta_d - \bar{\zeta}_d$, $z_3 = \zeta_d - \bar{\zeta}_d$. Substituting Equation (12) into Equation (11) gives:

$$
\dot{\zeta}_1 = s_1 + z_1 - k_1 \zeta_1.
$$

(28)

Substituting Equation (15) into Equation (14) and noting $\dot{s}_3 = s_2 + \zeta_d = s_2 + \bar{\zeta}_d + \bar{\zeta}_d$ yields:

$$
\dot{s}_1 = \bar{A}_a (s_2 + \bar{\zeta}_d) - \frac{1}{m} \left[ \ddot{b} x_2 + \bar{F}_x \dot{S}_1(x) + \dot{d}_f \right] + \bar{A}_a \dot{s}_3 - k_2 \dot{s}_1 - \frac{\bar{b}^2}{4 \eta_1} s_1.
$$

(29)

where $\bar{b} = b - \bar{b}$, $\bar{F}_x = F_x - \bar{F}_x, \dot{d}_f = d_f - \dot{d}_f$. 

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Therefore, the time derivative of $V_1$ is:

$$\dot{V}_1 = -k_1e_1^2 - k_2s_1^2 - k_3s_2^2 - k_4s_3^2 + e_1s_1 + e_1z_1 + \overline{A}_a(s_1s_2 + s_1z_2) + \frac{RT_d}{V_a}(s_3 + z_3)$$

Substituting Equation (32) into Equation (25) gives:

$$\dot{s}_3 = -k_4s_3.$$  

(31)

Substituting Equation (22) into Equation (21) and noting $\dot{x}_4 = s_3 + \zeta_d = s_3 + z_3 + \zeta_d$ yields:

$$\dot{s}_2 = \frac{RT_d}{V_a}(s_3 + z_3) - k_3s_2.$$  

(30)

It has been proved in [36] that with the projection mapping, the following properties hold:

$$\tag{33a} \tilde{b}\left[\text{Proj}_b\left(-\frac{\gamma_1}{m}x_2s_1\right) - \left(-\frac{\gamma_1}{m}x_2s_1\right)\right] \leq 0,$$

$$\tag{34b} \tilde{F}_1\left[\text{Proj}_{F_1}\left(-\frac{\gamma_2}{m}s_1s_2\right) - \left(-\frac{\gamma_2}{m}s_1s_2\right)\right] \leq 0,$$

$$\tag{33c} \tilde{d}_1\left[\text{Proj}_{d_1}\left(-\frac{\gamma_3}{m}s_1\right) - \left(-\frac{\gamma_3}{m}s_1\right)\right] \leq 0.$$  

According to Assumption 1–2, there exists a known function $h_1(t)$ satisfies:

$$\tag{34} h_1(t) \geq \frac{1}{m}\left[b_{\text{max}} - b_{\text{min}}\right] + \left[F_{\text{max}} - F_{\text{min}}\right] + \left[d_{\text{max}} - d_{\text{min}}\right] + \overline{A}_a|\rho_1|,$$

where $\rho_1$ is the bound of $\overline{x}_3$ as proven in the above step. From the smoothed sliding mode control theory, the following inequality holds:

$$s_1\left(-\frac{h_1^2}{4\eta_1}s_1 - \frac{1}{m}\left[bx_2 + \tilde{F}_1S_t(x) + \tilde{d}_1\right] + \overline{A}_a\overline{x}_3\right) \leq \eta_1.$$  

(35)

Substituting Equation (34) into Equation (32) yields:

$$\dot{V}_1 \leq -k_1e_1^2 - k_2s_1^2 - k_3s_2^2 - k_4s_3^2 + e_1s_1 + e_1z_1 + \overline{A}_a(s_1s_2 + s_1z_2) + \frac{RT_d}{V_a}(s_3 + z_3) + \eta_1.$$  

(36)

The following inequalities can be obtained by using Young’s inequality.

$$e_1s_1 \leq \frac{e_1^2}{2} + \frac{s_1^2}{2}, \quad e_1z_1 \leq \frac{e_1^2}{2} + \frac{z_1^2}{2}, \quad s_1s_2 \leq \frac{s_1^2}{2} + \frac{s_2^2}{2}, \quad s_1z_2 \leq \frac{s_1^2}{2} + \frac{z_2^2}{2}, \quad s_1s_3 \leq \frac{s_1^2}{2} + \frac{s_3^2}{2}, \quad s_1z_3 \leq \frac{s_1^2}{2} + \frac{z_3^2}{2}, \quad s_3z_2 \leq \frac{s_3^2}{2} + \frac{z_2^2}{2}, \quad s_3z_3 \leq \frac{s_3^2}{2} + \frac{z_3^2}{2}, \quad s_3z_1 \leq \frac{s_3^2}{2} + \frac{z_1^2}{2}, \quad s_3z_1 \leq \frac{s_3^2}{2} + \frac{z_1^2}{2}, \quad s_3z_1 \leq \frac{s_3^2}{2} + \frac{z_1^2}{2}, \quad s_3z_1 \leq \frac{s_3^2}{2} + \frac{z_1^2}{2}.$$  

(37)

Substituting Equation (37) into Equation (36) gives:

$$\dot{V}_1 \leq -\left(k_1 - \frac{1}{2}\right)e_1^2 - \left(k_2 - \frac{1}{2}\right)s_1^2 - \left(k_3 - \frac{1}{2}\right)s_2^2 - \left(k_4 - \frac{RT_d}{V_a}\right)s_3^2 - \left(k_3 - \frac{RT_d}{V_a}\right)s_3^2 - \left(k_3 - \frac{RT_d}{V_a}\right)s_3^2 + \frac{RT_d}{V_a}s_3^2 + \frac{RT_d}{V_a}s_3^2 + \frac{RT_d}{V_a}s_3^2 + \eta_1.$$  

(38)

Following the similar analysis as done in [28], the following inequalities hold.

$$\frac{\dot{z}_1}{\tau_1} + \frac{\dot{z}_1}{\tau_1} \leq \dot{z}_1 + \frac{\dot{z}_1}{\tau_1} \leq \xi_1, \quad \frac{\dot{z}_2}{\tau_2} + \frac{\dot{z}_2}{\tau_2} \leq \dot{z}_2 + \frac{\dot{z}_2}{\tau_2} \leq \xi_2, \quad \frac{\dot{z}_3}{\tau_3} + \frac{\dot{z}_3}{\tau_3} \leq \dot{z}_3 + \frac{\dot{z}_3}{\tau_3} \leq \xi_3.$$  

(39)
where $\xi_1(e_1, s_1, z_1, x_d, \dot{x}_d, \ddot{x}_d), \xi_2(e_1, s_1, s_2, z_1, z_2, x_d, \dot{x}_d, \ddot{x}_d)$, and $\xi_3(e_1, s_1, s_2, s_3, z_1, z_2, z_3, x_d, \dot{x}_d, \ddot{x}_d)$ are three continuous functions. Due to the fact that the set $\Omega_0$ is compact in $R^3$ and the set $\Omega_1 = \{[e_1, s_1, s_2, s_3, z_1, z_2, z_3]^T : c_1^2 + s_1^2 + s_2^2 + s_3^2 + z_1^2 + z_2^2 + z_3^2 \leq 2B_1 \}$ (where $B_1 > 0$) is compact in $R^7$, $\Omega_0 \times \Omega_1$ is thus compact in $R^{10}$. Therefore, $\xi_1, \xi_2,$ and $\xi_3$ have maximums on $\Omega_0 \times \Omega_1$. Let $M_1, M_2,$ and $M_3$ be the maximums of $\xi_1, \xi_2,$ and $\xi_3$ on $\Omega_0 \times \Omega_1$, respectively, one can obtain that:

$$z_1 \dot{z}_1 + \frac{z_1^2}{t_1} \leq M_1|z_1|, \quad z_2 \dot{z}_2 + \frac{z_2^2}{t_2} \leq M_2|z_2|, \quad z_3 \dot{z}_3 + \frac{z_3^2}{t_3} \leq M_3|z_3|. \quad (40)$$

With the use of Young’s inequality, one can obtain that:

$$z_1 \dot{z}_1 \leq \frac{z_1^2}{t_1} + \frac{M_1^2}{2}, \quad z_2 \dot{z}_2 \leq \frac{z_2^2}{t_2} + \frac{M_2^2}{2}, \quad z_3 \dot{z}_3 \leq \frac{z_3^2}{t_3} + \frac{M_3^2}{2}. \quad (41)$$

Thus, the following inequalities can be obtained.

$$\dot{V}_{e2} \leq -\frac{1}{t_1}z_1^2 - \frac{1}{t_2}z_2^2 - \frac{1}{t_3}z_3^2 + \frac{1}{2}M_1^2 + \frac{1}{2}M_2^2 + \frac{1}{2}M_3^2. \quad (42)$$

Thus, the following inequalities can be obtained.

$$\dot{V}_1 \leq -(k_1 - 1)c_1^2 - (k_2 - 1 - \overline{A}_a)s_1^2 - (k_3 - \overline{A}_a - \frac{RT_a d}{V_a}s_2^2 - (k_4 - \frac{RT_a d}{V_a})s_3^2 - \left(\frac{1}{t_1} - 1\right)c_1^2 - \left(\frac{1}{t_2} - 1 - \frac{\overline{A}_a}{2}\right)s_2^2 - \left(\frac{1}{t_3} - 1 - \frac{\frac{RT_a d}{V_a}}{2}\right)s_3^2 + \frac{1}{2}M_1^2 + \frac{1}{2}M_2^2 + \frac{1}{2}M_3^2 + \eta_1. \quad (43)$$

By choosing $k_1 > 1, k_2 > \frac{1}{2} + \overline{A}_a, k_3 > \frac{\overline{A}_a}{2} + \frac{RT_a d}{V_a}, k_4 > \frac{RT_a d}{2V_a}, \tau_1 < 1, \tau_2 < \frac{2}{\overline{A}_a + 1},$ and $\tau_3 < \frac{2V_a}{RT_a d + V_a}$, one has:

$$\gamma = \min \left\{ k_1 - 1, k_2 - \frac{1}{2} - \overline{A}_a, k_3 - \frac{\overline{A}_a}{2} - \frac{RT_a d}{V_a}, k_4 - \frac{RT_a d}{2V_a}, \frac{1}{\tau_1} - 1, \frac{1}{\tau_2} - 1 - \frac{\overline{A}_a}{2}, \frac{1}{\tau_3} - \frac{1}{2} - \frac{RT_a d}{2V_a} \right\} > 0 \quad (44)$$

Then, it can be readily obtained that the following inequality holds.

$$\dot{V} \leq -2\gamma V + \eta. \quad (45)$$

where $\eta = \frac{1}{2}M_1^2 + \frac{1}{2}M_2^2 + \frac{1}{2}M_3^2 + \eta_1. \quad \Box$

Clearly, if $\gamma > \eta/2B_1$, then $\dot{V} \leq 0$ on set $\Omega$, thus $V$ will remain $V(t) \leq B_1$ for all $t$, provided that the initial conditions satisfy $V(0) \leq B_1$. Therefore, the errors $e_1, s_1, s_2, z_1, z_2, z_3$ are bounded. Hence, one can conclude that the closed loop system is uniformly and ultimately bounded.

4. Experimental Results

In this section, the proposed controller was implemented for the servo control of the pneumatic servo system as shown in Figure 2. The cylinder forward chamber was controlled by the valve through a 10 m long transmission line with 4 mm inside diameter, while the pressure in the return chamber was maintained at about 3 bar by utilizing a tank. A gel phantom was used to perform the following needle insertion experiments. The system physical parameters and the parameters of the controller are given in Table 1.
Table 1. Parameters of the system and the proposed controller.

| Symbol | Value          | Unit        |
|--------|----------------|-------------|
| \( m \) | 0.32           | kg          |
| \( A_a \) | \( 7.854 \times 10^{-5} \) | m\(^2\)  |
| \( A_b \) | \( 6.597 \times 10^{-4} \) | m\(^2\)  |
| \( A_r \) | \( 1.257 \times 10^{-5} \) | m\(^2\)  |
| \( R \) | 287            | N m/(kg K)  |
| \( T_s \) | 300            | K           |
| \( p_s \) | \( 6 \times 10^5 \) | Pa          |
| \( V_{a0} \) | \( 6 \times 10^{-7} \) | m\(^3\)  |
| \( L_c \) | 0.125           | m           |
| \( V_l \) | \( 1.257 \times 10^{-4} \) | m\(^3\)  |
| \( C_d \) | \( 1.099 - 0.1075 \times \frac{p}{p_0} \) |          |
| \( p_r \) | 0.29           |             |
| \( A_l \) | \( 1.257 \times 10^{-5} \) | m\(^2\)  |
| \( D_l \) | 0.004           | m           |
| \( L_l \) | 10              | m           |
| \( \mu \) | \( 1.79 \times 10^{-5} \) | N s/m\(^2\) |
| \( P_0 \) | \( 1 \times 10^5 \) | Pa          |
| \( \hat{b}(0),b_{\text{min}},b_{\text{max}} \) | 9, 0, 15 | N/s/m  |
| \( \hat{F}_l(0),\hat{F}_{\text{min}},\hat{F}_{\text{max}} \) | 6, 0, 20 | N       |
| \( \hat{d}_l(0),d_{\text{min}},d_{\text{max}} \) | 0, –10, 10 | N       |
| \( k_1,\tau_1 \) | 40, 0.5 |             |
| \( k_2, h_1, \eta_1, \tau_2 \) | 50, 40, 0.4, 0.75 |       |
| \( k_3,\tau_3 \) | 50, 1.2 |             |
| \( k_4 \) | 90              |             |
| \( \gamma_1,\gamma_2,\gamma_3 \) | 100, 10, 10 |         |

The same control algorithm as the proposed controller, but in which the long transmission line was characterized as a part of the cylinder’s dead volume and the chamber pressure was directly measured, was first tested for tracking a sinusoidal trajectory and a smooth square trajectory. As shown in Figure 4, the performance was poor for practical application, which indicates the need for an advanced method to address the issue of long transmission line. The performance of the proposed controller was tested on three types of reference trajectories: A 0.5 Hz sinusoidal signal, a smooth square signal, and a 4 s periodic signal. Figure 5 shows the response of the system, and the tracking errors are presented in Figure 6. The maximum absolute tracking errors (\( \max_{t \geq 5} \| e_1(t) \| \)) were about 2.51 mm, 2.68 mm, and 1.81 mm, while the final steady-state tracking errors (\( \max_{t \geq 5} \| e_1(t) \| \)) were about 0.96 mm, 1.05 mm, and 1.39 mm. As seen, the proposed controller could significantly improve the system performance, which indicates the effectiveness of the proposed long transmission line compensation method. However, it should be noted that these needle insertion experiments were performed in a gel phantom, whose resisting force behavior was simpler than real soft tissue. The interaction between needle and soft tissue is very complex and may decrease the needle insertion precision in practical. Since the current research focused on addressing the issue of long transmission line and realizing high accuracy control of a pneumatic actuator with a pressure observer, modeling of needle-tissue interaction and further improving needle insertion precision would be the subject of the next phase of this research.

The process of parameter and disturbance estimations is shown in Figure 7. It can be seen that the estimates converged quickly, and the tracking error improvement could be achieved within several seconds. Comparisons between the observed chamber pressure and the measured one are shown in Figure 8. As can be seen, the estimated chamber pressure was close to its actual value, which indicates the effectiveness of the proposed pressure observer. However, the estimation error during the charging process was slightly bigger than the one during the discharging process. This might be due to the fact that charging process was close to adiabatic and the discharging process was close to isothermal.
Figure 4. Tracking response of the same control algorithm as the proposed controller but without using long transmission line compensation.

Figure 5. Tracking response of the proposed controller for three different types of trajectories.
Figure 6. Tracking errors of the proposed controller for three different types of trajectories.

Figure 7. Parameter and disturbance estimations of the proposed controller when the reference is a 0.5 Hz sinusoidal trajectory.
Experiments were also conducted to verify the performance robustness of the proposed controller. To simulate a sudden disturbance acting on the system, a big step signal was added to the output of the position sensor at $t = 22$ s, and removed 10 s later. Figure 9 shows the control accuracy of the proposed controller in this scenario for tracking a sinusoidal trajectory with a frequency of 0.5 Hz and amplitude of 62.5 mm. It can be seen that the system performance did not deteriorate except the transient spikes when the sudden disturbance was added or removed.

5. Conclusions

In this paper, the precise motion control of a MRI compatible 1-DOF pneumatic servo system was considered. The long transmission line was characterized as an intermediate chamber connected between the valve and the cylinder in series, and a nonlinear first order system was used to approximate its dynamics. Simultaneously, a globally stable pressure observer was developed to estimate the chamber pressure. Based on the model of the long transmission line and the pressure observer, a pressure observer based adaptive dynamic surface controller was developed and the stability of the closed-loop system was proved via the Lyapunov method. In contrast to most of the existing nonlinear
controllers synthesized with the backstepping method, by employing the dynamic surface control technique, the proposed controller could cope with the problem of “explosion of complexity”, since the repeated differentiation of virtual controls was no longer required. The experimental results confirmed that the proposed controller was effective and had good performance robustness to sudden disturbances, thus enabling future application in pneumatically actuated MRI-compatible robots. However, precise motion control of pneumatic actuator did not necessarily lead to precise position control needle tip. Modeling of the interaction between needle and soft tissue, and incorporating a more accurate needle insertion force model in the controller design is an essential requirement for practical robot-assisted needle insertion. Thus, these issues will be explored further in the next phase of this research.

**Author Contributions:** D.M. and B.L. proposed the pressure observe based dynamic surface controller for precise position tracking control of the MRI-compatible pneumatic servo system. A.L. designed the experiments. J.Y. and Q.L. performed the experiments and analyzed the data. D.M. and A.L. wrote the paper.

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