TRAO Survey of the Nearby Filamentary Molecular Clouds, the Universal Nursery of Stars (TRAO FUNS). II. Filaments and Dense Cores in IC 5146

Eun Jung Chung1,2, Chang Won Lee2,3, Shinyoung Kim2,3, Maheswar Gopinathan4, Mario Tafalla5, Paola Caselli6, Philip C. Myers7, Tie Liu8, Hyunjoo Yoo2, Kyoung Hee Kim2, Mi-Ryang Kim2, Jungyoon Cho1, Wooin Kwon10,11, Changhoon Lee2, and Hyunwoo Kang2

1 Department of Astronomy and Space Science, Chonnam National University, 99 Daehe-ro, Yeosu-gu, Daejeon 34154, Republic of Korea
2 Korea Astronomy and Space Science Institute, 776 Daehe-dong, Yeosu-gu, Daejeon 54055, Republic of Korea
3 University of Science and Technology, Korea (UST), 217 Gajeong-ro, Yeosu-gu, Daejeon 34113, Republic of Korea
4 Indian Institute of Astrophysics, Koramangala (IIA), Bangalore 560034, India
5 Observatorio Astronómico Nacional (IGN), Alfonso XII 3, E-28014 Madrid, Spain
6 Max-Planck-Institut für Extraterrestrische Physik, Giessenbachstrasse 1, 85748 Garching bei München, Germany
7 Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA
8 Key Laboratory for Research in Galaxies and Cosmology, Shanghai Astronomical Observatory, Chinese Academy of Sciences, 80 Nandan Road, Shanghai 200030, People’s Republic of China
9 SOFIA Science Centre, USRA, NASA Ames Research Centre, MS-12, N232, Moffett Field, CA 94035, USA
10 Department of Earth Science Education, Seoul National University, 1 Gwanak-ro, Gwanak-gu, Seoul 08826, Republic of Korea
11 SNU Astronomy Research Center, Seoul National University, 1 Gwanak-ro, Gwanak-gu, Seoul 08826, Republic of Korea

Received 2021 April 6; revised 2021 June 3; accepted 2021 June 4; published 2021 September 16

Abstract

We present the results on the physical properties of filaments and dense cores in IC 5146, as a part of the TRAO FUNS project. We carried out on-the-fly mapping observations using the Taeduk Radio Astronomy Observatory (TRAO) 14 m telescope covering about 1 square degree of the area of IC 5146 using various molecular lines. We identified 14 filaments (24 in total, including sub-filaments) from the C18O (1–0) data cube and 22 dense cores from the N2H+ (1–0) data. We examined the filaments’ gravitational criticality, turbulence properties, accretion rate from filaments to dense cores, and relative evolutionary stages of cores. Most filaments in IC 5146 are gravitationally supercritical within the uncertainty, and most dense cores are formed in them. We found that dense cores in the hubs show a systemic velocity shift of ≃0.3 km s⁻¹ between the N2H+ and C18O gas. Besides, these cores are subsonic or transonic, while the surrounding filament gas is transonic or supersonic, indicating that the cores in the hubs are likely formed by the dissipation of turbulence in the colliding turbulent filaments and the merging is still ongoing. We estimated a mass accretion rate of 15–35 M⊙ yr⁻¹ from the filaments to the dense cores, and the required timescales to collect the current core mass are consistent with the lifetime of the dense cores. The structures of filaments and dense cores in the hub can form from a collision of turbulent converging flows, and mass flow along the filaments to the dense cores may play an important role in forming dense cores.

Unified Astronomy Thesaurus concepts: Interstellar filaments (842); Molecular clouds (1072); Interstellar medium (847); Star formation (1569)

1. Introduction

It has been noticed that many star-forming regions are associated with elongated filamentary structures of parsec scales in observations at optical, infrared, and submillimeter wavelengths (e.g., Lynds 1962; Lada & Lada 2003; Goldsmith et al. 2008). The Herschel Space Observatory has made significant progress in the study of these filamentary molecular clouds and early star-forming conditions, showing that filamentary structures pervade the molecular clouds, from the low- to high-mass star-forming clouds, and the non-star-forming clouds (e.g., André et al. 2010; Arzoumanian et al. 2019). Over 75% of the prestellar cores are found to reside in filaments with supercritical mass per unit length in the Aquila molecular cloud complex (Könnyves et al. 2015). A similar result was reported for L1641 molecular clouds in Orion A, where ≃71% of the prestellar cores are found to be located on the filaments and they are usually more massive than the prestellar cores off the filaments (Polychroni et al. 2013).

Although the Herschel observations have made great progress with its extraordinarily high spatial resolution, it does not provide any velocity information on the structures it identifies, which poses a serious limitation. Possible overlaps of filaments with different velocities into the plane of the sky are expected, and submillimeter radio observations, mainly with carbon monoxide and its isotopologues, were carried out to obtain crucial dynamical information on the filaments (e.g., Nagahama et al. 1998; Hacar et al. 2013; Panopoulou et al. 2014). It was found that some filaments have multiple velocity substructures (e.g., Hacar et al. 2013, 2016, 2017, 2018; Henshaw et al. 2013; Maureira et al. 2017; Clarke et al. 2018; Dhabal et al. 2018). One of the interesting things that is revealed by the observations of molecular lines is the mass flow along filaments toward the star clusters in hub-filament structures (HFSs; Myers 2009). Velocity gradients along the filaments are observed and mass flow along these filaments is considered to be responsible for the formation of the star clusters in the hubs (e.g., Kirk et al. 2013; Peretto et al. 2014; Limara et al. 2017; Baug et al. 2018; Yuan et al. 2018; Treviño-Morales et al. 2019). Hence, the filaments and their related structures are supposed to be a prerequisite stage of star formation and closely linked to the formation of prestellar cores and stars. However, a detailed understanding of how they form is still unclear.
Numerical simulations of the interstellar medium (ISM) show that filaments can be generated by gravitational instability of a sheet, global gravitational collapse of a cloud, and collisions of large-scale turbulence (e.g., Nagai et al. 1998; Padoan et al. 2001; Hennebelle 2013; Gómez & Vázquez-Semadeni 2014). In addition, recent magnetohydrodynamics (MHD) and hydrodynamical turbulent simulations show that clumps in a magnetic field tend to have more elongated filamentary shapes (see Hennebelle & Inutsuka 2019, and references therein). For the formation of dense cores in filaments, it is suggested that cores form in filaments by collapse and fragmentation due to the gravitational instability (Inutsuka & Miyama 1997). With the observational results obtained from Herschel, a two-step formation scenario has been proposed in which the filaments first form by the dissipation of large-scale turbulence, and then the cores are generated in the gravitationally supercritical filaments via fragmentation (e.g., André et al. 2014; Arzoumanian et al. 2019). Another model proposed for the formation of the filaments and the dense cores is by the collision of turbulent flows that form dense cores by the compression and dissipation of turbulence at the stagnation point between two flows (e.g., Ballesteros-Paredes et al. 1999; Padoan & Nordlund 2002).

“TRAO FUNS,” which is an acronym of the “TRAO survey of the nearby Filamentary molecular clouds, the Universal Nursery of Stars,” is a project to survey the clouds belonging to the Gould Belt in molecular lines using the Taeduk Radio Astronomy Observatory (TRAO)12 14 m antenna. We have made observations of nine molecular clouds under the TRAO FUNS project in eight molecular lines. These clouds are found to have diverse physical conditions and range from being quiescent non-star-forming clouds like Polaris to low-mass star-forming clouds such as L1478 of California cloud, and to active high-mass star-forming clouds such as the Orion B molecular complex. This project mainly aims to obtain the kinematic and chemical structures of the filaments and the associated dense cores to understand the processes involved in their formation.

This is the second paper presenting the results obtained from the TRAO FUNS project, especially on IC 5146 located in the constellation Cygnus. IC 5146 is a nearby star-forming molecular cloud consisting of a reflection nebula in the east, the Cocoon Nebula, and a dark cloud with multiple filaments in the west, the Streamer (Lada et al. 1994). Spitzer Space Telescope observations of the IC 5146 region made using the Infrared Array Camera (IRAC) and the Multiband Imaging Photometer for Spitzer (MIPS) resulted in the identification of ~200 candidate young stellar objects (YSOs; Harvey et al. 2008). Based on the Herschel data, Arzoumanian et al. (2011) identified 71 YSOs and 45 candidate bound prestellar cores in IC 5146. Observations at 450 and 850 μm with the James Clerk Maxwell Telescope (JCMT) have been carried out in this cloud, and 15 Class 0/I, 4 Flat, 14 Class II, and 6 Class III YSOs have been found (Johnstone et al. 2017). The complex filamentary structure of IC 5146 was revealed in the Herschel Gould Belt Survey (Arzoumanian et al. 2011). The main results from the Herschel observations are that the filaments in IC 5146 have a narrow characteristic width of ~0.1 pc and the most bound prestellar cores are located on the gravitationally supercritical filaments, similar to the results obtained for other regions by the Herschel observations (e.g., André et al. 2014).

The distance to IC 5146 is still uncertain, and ranges from 460 to 1400 pc (e.g., Harvey et al. 2008; Nunes et al. 2016). Nunes et al. (2016) measured the distance to the embedded clusters in the Streamer and quoted a distance of ~1.2 ± 0.1 kpc. Recently, using the newly released Gaia data (Gaia DR2, Bailer-Jones et al. 2018), Dzib et al. (2018) estimated the distances to the star-forming clouds in the Gould Belt, and estimated a distance of 813 ± 106 pc for the Cocoon Nebula. Meanwhile, Wang et al. (2020) estimated the distance to IC 5146 including the Streamer using Gaia DR2, and argued that the Streamer is nearer than the Cocoon Nebula. In this work for the analysis, we adopted the most recent distance estimations of 800 ± 100 pc and 600 ± 100 pc for the Cocoon and the Streamer, respectively, made using the Gaia measurements by Wang et al. (2020). Recently the third Gaia Data Release (Gaia EDR3; Bailer-Jones et al. 2021) was also made available, and the distances of these two regions from the Gaia EDR3 are found to be consistent (within the uncertainties) with the distances adopted here.

The paper is organized in the following manner. Section 2 describes the observations and data reduction. Section 3 shows the spatial distributions of the detected molecular lines. Sections 4 and 5 explain the identification and the estimations of physical quantities of filaments and dense cores, respectively. Section 6 discusses the formation mechanisms of filaments and dense cores in IC 5146 with their physical and chemical properties. Section 7 gives a summary and conclusions.

2. Observations and Data Reduction

2.1. Observations

IC 5146 was observed with the TRAO 14 m telescope. TRAO provides spatial resolution of ~49″ at 110 GHz, corresponding to 0.14 pc at the distance of 600 pc (0.19 pc at 800 pc). TRAO has the frontend of Second Quabbin Optical Image Array focal plane array receiver (SEQUOIA-TRAO) consisting of 16 horns, configured in a 4 × 4 array with a spatial separation of 89″. The backend system used is the fast Fourier transform (FFT) spectrometer, which has 4096 × 2 channels at 15 kHz resolution (~0.04 km s⁻¹ at 110 GHz) and covers a total bandwidth of 62.5 MHz, corresponding to ~170 km s⁻¹ at 110 GHz. Simultaneous observations of two molecular lines at frequencies of 85 and 100 GHz or 100 and 115 GHz are allowed. The beam efficiency of the telescope is 0.48 at 98 GHz, and 0.46 at 110 GHz (Jeong et al. 2019).

We choose eight molecular lines to investigate the physical properties of filaments and dense cores. C^18O (1–0) and N_2H^+ (1–0) molecular lines are chosen as tracers of relatively less dense filaments and denser cores, respectively. HCO^+ (1–0) and CS (2–1) molecular lines were chosen because they are known to be good tracers of infall motions in prestellar cores (e.g., Lee et al. 2001). SO and NH_2D are known to be respectively the most and least sensitive molecules to gas freeze-out (e.g., Tafalla et al. 2006). Hence, we selected SO (3−2−1) and NH_2D (1_1−1_0) lines to investigate the chemical evolution of dense cores. We made the simultaneous observations in two molecular lines with sets of C^18O (1–0) and ^13CO (1–0), N_2H^+ (1–0) and HCO^+ (1–0), CS (2−1) and SO (3−2−1), and NH_2D (1_1−1_0) and H^13CO^+ (1–0), respectively.

12 http://radio.kasi.re.kr/trao/main_trao.php
The observations were carried out from 2018 May to 2019 November. These data are obtained in on-the-fly mapping mode. To cover the whole IC 5146 region including the Cocoon Nebula and the Streamer, we divided it into four subregions having box shapes (referred as “tiles” hereafter) with a size of $28' \times 30'$. Five tiles were made for the N$_2$H$^+$ (1–0) and HCO$^+$ (1–0) line set, of which three were of $20' \times 20'$ size and two of $20' \times 24'$ size. For the third molecular line set of CS (2–1) and SO (3–2), three tiles (one $28' \times 22'$ and two $29' \times 20'$) are made. For the last molecular line set of NH$_2$D (1$_1$–0$_0$) and H$_2$CO$^+$ (1–0), five tiles with various sizes from $6' \times 6'$ to $17' \times 18'$ were made to cover the dense core regions detected in N$_2$H$^+$ (1–0). The scanning rate was $55''$ per second and the recording time is 0.2 s. We chose scan steps of $5''$ to $11''$ along the scan direction and separations of $5''$ to $33''$ between the rows to increase the observation efficiency according to the sizes of tiles. The scan steps used are smaller than the recommended Nyquist spacing to avoid undersampling. We made several maps alternately along the R.A. and decl. directions to obtain uniform target sensitivity. Figure 1 shows the observed regions for each set of molecular lines over the Herschel 250 $\mu$m continuum image.

2.2. Data Reduction

The data were reduced as follows. First, the raw on-the-fly data for each map of each tile were read and converted into a CLASS$^{13}$ format map after the subtraction of baseline (with first order) in OTFTOOL. A resulting cell size of $10''$ was chosen and noise-weighting was applied. Further reductions and inspection of the data were done using the otfpro CLASS script. The baseline subtractions were done iteratively. Both ends of the raw spectra were cut off and baselines of the spectra were subtracted with a second-order polynomial. After that, the spectra were resampled with a channel width of $0.06$ km s$^{-1}$, and both ends were cut off again, giving the spectra a velocity range of $60$ km s$^{-1}$; the baselines of the spectra were again subtracted but with a first-order polynomial. Finally, the maps were merged into a final fits cube with $20''$ cell size and $0.1$ km s$^{-1}$ velocity channel width for C$^{18}$O (1–0), $^{13}$CO (1–0), SO (3–2), and NH$_2$D (1$_1$–0$_0$) data, and $20''$ cell size and $0.06$ km s$^{-1}$ velocity channel width for the N$_2$H$^+$ (1–0), HCO$^+$ (1–0), CS (2–1), and H$_2$CO$^+$ (1–0) data. The basic information on the observations and the final data is given in Table 1. The final rms levels achieved were $\lesssim 0.1$ K[T$_A^*$] for the C$^{18}$O and $^{13}$CO lines and $\sim 0.07$ K[T$_A^*$] for other molecular lines.

3. Results

3.1. $^{13}$CO and C$^{18}$O Emissions

Figure 2 shows the integrated intensity maps of $^{13}$CO (1–0) and C$^{18}$O (1–0) lines, which are found to nicely delineate the large-scale structure of IC 5146. The line intensity maps are integrated over the velocity range from $-0.8$ to $10.7$ km s$^{-1}$ for $^{13}$CO (1–0), and $0.7$ to $9.4$ km s$^{-1}$ for C$^{18}$O (1–0). The distribution of $^{13}$CO (1–0) emission is well matched with that of the Herschel 250 $\mu$m emission, while C$^{18}$O (1–0) lines are only detected in relatively compact regions of high continuum flux. In the eastern region of IC 5146, the ball shape of the Cocoon Nebula is shown in the 250 $\mu$m emission as well as H$_2$O image (e.g., Arzoumanian et al. 2011). However, the CO isotopologues have a different distribution from those of the dust and ionized gas. They have the shape of three-leafed clover instead of a roundish structure. In the Streamer, hub–filament structures and filament shapes can be seen in the $^{13}$CO and C$^{18}$O (1–0) maps. The molecular gases $^{13}$CO and C$^{18}$O have relatively higher LSR velocity toward the southeast than toward the northwest (see the spectra in Figure 2 and Figure 15 in the Appendix).

In Figure 2, the right panels present the $^{13}$CO and C$^{18}$O (1–0) spectra at four positions indicated in the maps with crosses,
showing that overlapping of the multiple velocity components seems common. Shown here are the various shapes of $^{13}$CO and C$^{18}$O (1–0) spectra found toward IC 5146. In position (a), $^{13}$CO and C$^{18}$O (1–0) lines trace the same multiple velocity components at 7.6 and 8.8 km s$^{-1}$. These two components are shown to be clearly separated in the $^{13}$CO (1–0) spectrum as well as in the

**Table 1**

| Molecule       | $\nu_{\text{ref}}$ (GHz) | $\theta_{\text{FWHM}}$ (arcsec) | Area (arcmin$^2$) | $\theta_{\text{pixel}}$ (arcsec) | $\delta v$ (km s$^{-1}$) | rms (K) | rms of mom0 (K km s$^{-1}$) | $n_{\text{crit}}$ (cm$^{-3}$) |
|----------------|--------------------------|---------------------------------|------------------|---------------------------------|--------------------------|----------|-------------------------------|-------------------------------|
| C$^{18}$O (1–0)| 109.782173 (1)           | 49                              | 3360             | 20                              | 0.1                      | 0.096    | 0.090                         | $1.9 \times 10^5$            |
| $^{13}$CO (1–0)| 110.201353 (2)           | 49                              | 3360             | 20                              | 0.1                      | 0.096    | 0.103                         | $1.9 \times 10^5$            |
| N$_2$H$^+$ (1–0)| 93.176258 (1)            | 52                              | 2160             | 20                              | 0.06                     | 0.066    | 0.071                         | $5.7 \times 10^5$            |
| HCO$^+$ (1–0)| 89.188525 (3)            | 57                              | 2160             | 20                              | 0.06                     | 0.066    | 0.050                         | $1.6 \times 10^5$            |
| CS (2–1)      | 97.980953 (1)            | 52                              | 1780             | 20                              | 0.06                     | 0.069    | 0.056                         | $3.3 \times 10^5$            |
| SO (3$\text{_{2-1}}$)| 99.299870 (4)         | 52                              | 1780             | 20                              | 0.1                      | 0.056    | 0.052                         | $3.5 \times 10^5$            |
| NH$_2$D (1$\text{_{11-10}}$)| 85.926278 (3)       | 57                              | 864              | 20                              | 0.1                      | 0.058    | 0.078                         | $3.8 \times 10^6$            |
| H$^{13}$CO$^+$ (1–0)| 86.754248 (3)    | 57                              | 864              | 20                              | 0.06                     | 0.068    | 0.067                         | $1.5 \times 10^7$            |

**Notes.**

a Rest frequency of each molecular line. The references are: (1) Lee et al. (2001), (2) Lovas (2004), (3) Cologne Database for Molecular Spectroscopy (CDMS: Müller et al. 2001, https://cdms.ph1.uni-koeln.de/cdms/portal/), and (4) Submillimeter, Millimeter, and Microwave Spectral Line Catalog provided by Jet Propulsion Laboratory (Pickett et al. 1998).

b FWHM of the telescope beam (Jeong et al. 2019).

c Total observed area.

d The pixel size of the final data cube.

e The channel width of the final data cube.

f Noise level in $T_A^*$ of the final data cube.

gh Noise level of integrated intensity moment 0 map.

Critical density, which is estimated from $A/\gamma$ where $A$ is the Einstein $A$ coefficient and $\gamma$ is the collisional rate coefficient at 10 K from LAMDA (Schöier et al. 2005). $n_{\text{crit}}$ of SO (3$\text{_{2-1}}$) is calculated with $\gamma$ at 60 K, which is the lowest temperature provided by LAMDA.
C$^{18}$O (1–0) spectrum, though the former shows much larger line width than the latter. However, in positions (b) and (c), the \(^{13}\)CO (1–0) spectra show different peaks when compared with the \(^{15}\)O (1–0) spectra. In (b), the \(^{18}\)O (1–0) line has only one peak at \(\sim 4.5\) km s\(^{-1}\), but the \(^{13}\)CO (1–0) line shows an additional peak at \(\sim 2\) km s\(^{-1}\), suggesting that \(^{13}\)CO covers less dense and larger bulk structures where \(^{18}\)O is not detected. However, toward brighter regions, \(^{13}\)CO can be self-absorbed as shown in position (c). Looking at the \(^{13}\)CO (1–0) spectrum alone, it appears that there are two different velocity components. However, it can be seen that the dip between the two peaks of \(^{13}\)CO (1–0) exactly matches with the peak position of the \(^{15}\)O (1–0) spectrum which has a relatively smaller optical depth than \(^{13}\)CO (1–0), indicating that the double components of the \(^{13}\)CO (1–0) line are caused by the self-absorption of the \(^{13}\)CO (1–0) spectrum due to its high optical depth. The \(^{13}\)CO (1–0) spectrum at position (d) shows a larger line width (\(\Delta V_{\text{FWHM}} \sim 4\) km s\(^{-1}\)) and appears to be composed of multiple Gaussian components while the \(^{15}\)O (1–0) shows only a single component. The \(^{13}\)CO (1–0) line is useful to trace the less dense filament material and covers a large area, but has limitations due to its large optical depth in the area of high column density. After visual inspections of all the spectra, we chose the \(^{18}\)O (1–0) line to trace the velocity structure of the dense filament material, which is thought to be more closely related to the star formation (e.g., Nishimura et al. 2015).

3.2. HCO\(^+\), CS, N\(_2\)H\(^+\), and SO Emission

We present the distributions of HCO\(^+\) (1–0), CS (2–1), N\(_2\)H\(^+\) (1–0), and SO (3\(_2\)–2\(_1\)) emission in Figure 3. The HCO\(^+\) (1–0), CS (2–1), and SO (3\(_2\)–2\(_1\)) intensities are integrated over the velocity ranges from 0.62 to 9.98 km s\(^{-1}\), \(\sim 1.66\) to 9.2 km s\(^{-1}\), and 0.86 to 9.2 km s\(^{-1}\), respectively. The N\(_2\)H\(^+\) (1–0) intensity is integrated from \(-5.9\) to 13.6 km s\(^{-1}\) including all hyperfine components.

The distribution of HCO\(^+\) (1–0) emission matches well with the region of overall high H\(_2\) column density derived from the 70–500 \(\mu\)m Herschel data (Arzoumanian et al. 2011). In the Cocoon Nebula, HCO\(^+\) (1–0) emission shows a shell-like structure. The abundance of HCO\(^+\) is maintained by the balance between its formation from the reactions between H\(_3^+\) and CO and its destruction from dissociative recombination with electrons. Besides, it is reported that in far-ultraviolet irradiated environments HCO\(^+\) can more easily recombine with free electrons, leading to a decrease in its abundance (e.g., Pety et al. 2017). Hence, the central hole in HCO\(^+\) (1–0) emission may be due to the dominance of its destruction processes through electronic recombination in an environment that contains abundant free electrons produced by the central B-type star. In the Streamer, the HCO\(^+\) (1–0) emission appears to be well matched with the H\(_2\) column density distribution as well as with \(^{18}\)O (1–0).

CS (2–1) emission (shown with contours in the second panel from the top of Figure 3) is in good agreement with the \(^{18}\)O (1–0) emission (the bottom panel in Figure 2) in the Cocoon Nebula as well as in the Streamer. For the N\(_2\)H\(^+\) and SO species (presented with contours in the third and bottom panels of Figure 3, respectively), the emission shows a clumpy distribution in the bright \(^{18}\)O (1–0) and/or dense H\(_2\) regions. It is noticeable that N\(_2\)H\(^+\) (1–0) is hardly detected in the Cocoon Nebula at the rms level of \(\sim 0.07\) K km s\(^{-1}\) while other species are detected above the 3\(\sigma\) level. The lack of N\(_2\)H\(^+\) (1–0) emission in the Cocoon Nebula may have something to do with the presence of the central B-type star, which may increase the dust temperature enough for CO to be evaporated rather than depleted. CO freezes out at low temperature (\(< 20\) K) but starts to evaporate back into the gas phase at \(\sim 25\) K (e.g., Hocuk et al. 2014). Indeed, the mean dust temperature of the Cocoon Nebula is 23 K and it goes up to \(\sim 30\) K. The abundant CO can play a role in destroying N\(_2\)H\(^+\), making the N\(_2\)H\(^+\) abundance lower (Caselli et al. 1999, 2002; Bergin et al. 2002). In the Streamer, some distinct features can be noticed based on the distribution of various molecular species. One representative example is the N\(_2\)H\(^+\) (1–0) bright region in the very northern part (F1 region in Figure 4), where there is weak \(^{18}\)O (1–0), relatively bright CS (2–1), but no SO (3\(_2\)–2\(_1\)) emission. The spatial differentiation between molecules may be due to the different evolutionary stages as well as distinct physical conditions. The chemical differentiation is studied in more detail in Section 5.3.

4. Filament Properties

4.1. Filament Identification

We identified velocity coherent filaments using the three-dimensional information of the C\(^{18}\)O (1–0) data cube. There are several algorithms available that can be used to identify the structures of clumps and filaments (e.g., Rosolowsky et al. 2008; Soubbie 2011; Soubbie et al. 2011; Men’shchikov et al. 2012; Hacar et al. 2013; Koch & Rosolowsky 2015; Ossenkopf-Okada & Stepanov 2019). Consequently, it is important to make a comparison between the results obtained by them. However, this is definitely beyond the scope of the paper. Thus, in this paper, we simply introduce the various algorithms developed for filament identification and describe in detail the one that we used in this work.

The algorithms astrodendro (Rosolowsky et al. 2008), DISPERSE (Soubbie et al. 2011), FIVE (Hacar et al. 2013), and FILFINDER (Koch & Rosolowsky 2015) have been used for finding filamentary structures in the astronomical data. FILFINDER uses two-dimensional image data and is not suitable for the identification of the filaments in a three-dimensional data cube. The other algorithms, namely DISPERSE, astrodendro, and FIVE, can be used with the three-dimensional data cube, but the methodology used to identify the filaments in each of them is quite different. DISPERSE finds critical points where the intensity gradient equals zero in a map and examines the persistence, which is the absolute difference between the pair of critical points. If the persistence is larger than the persistence threshold given as a free parameter, it connects the critical points to make arcs of integral shapes, producing the skeletons of the filaments as their ridges. However, with only the information on the ridges of the filaments, this algorithm is not able to give any detailed information on the physical quantities of the whole velocity coherent three-dimensional structure. Meanwhile, astrodendro, a PYTHON package utilizing DENDROGRAMS, is designed to find hierarchical structures in the molecular line data cube and provide three-dimensional isosurface hierarchical structures. astrodendro finds structures, called leaves, from local maxima and appends the surrounding regions with lower flux densities, increasing the volume of the structures. When they meet neighboring structures, they continue to merge into larger structures, the so-called branches and trunks. This process is found to be useful
Figure 3. Integrated intensity contour maps of HCO$^+$ (1–0), CS (2–1), N$_2$H$^+$ (1–0), and SO (3$_2$–2$_1$) on an H$_2$ column density map (Arzoumanian et al. 2011). The contours are drawn every 5$\sigma$ from the 3$\sigma$ level for HCO$^+$, N$_2$H$^+$, and CS emissions, and every 3$\sigma$ for SO emission. 1$\sigma$ values for the integrated intensity maps for each line are given in Table 1.
to identify the isosurface hierarchical structures and thus the filamentary structures in the molecular clouds with a simple hierarchical structure like L1478 (Chung et al. 2019). However, in a complex molecular cloud where multiple velocity components are mixed up in a complicated way with their significant intensity variance, e.g., F4 of IC 5146 (see Figures 4 and 5), the use of isosurface structures is found to be not effective for identifying velocity coherent filamentary structures in detail.

Above all, we aim to find velocity coherent structures in the position–position–velocity (PPV) space regardless of the intensity. The FIVE algorithm is found to be a well-designed algorithm for identifying coherent structures in the PPV cube by applying the friends-of-friends (FoF) technique to the central velocity information of the molecular line (Hacar et al. 2013). Its concept is very simple, and it is straightforward to find velocity coherent structures in the PPV space, making the FIVE algorithm more suited to our aim.

Hence we take the concept of the FIVE algorithm to find continuously connected structures in the PPV space and to segregate structures having different velocity components that appear to be connected owing to overlap in the line of sight. We first decomposed the multiple velocity components of C$^{18}$O (1–0) spectra using the tool FUNStools.Decompose$^{14}$ (S. Kim et al. 2021, in preparation). We then identified filaments with an FoF-like algorithm, FindingFilaments (FF).

FUNStools.Decompose is a tool that automatically decomposes multiple Gaussian components from the C$^{18}$O (1–0) data cube. The algorithm primarily decides the number of components and their velocity positions in the smoothed spectrum using the first, second, and third derivatives based on a conceptual idea that the velocity component in a filament is continuous with the surroundings. Then, the fitting results are given as the initial guess, and a Gaussian fitting is performed again.

The parameters that we used for C$^{18}$O (1–0) data of the IC 5146 are 3σ level for the lower limit of intensity, smoothing parameters of two pixels ($40'' \times 1\theta_{\text{beam}}$) and three velocity channels (0.3 km s$^{-1}$) in the initial fitting stage and one pixel and one velocity channel in the final fitting stage. We gave low and high limits of fitted velocity dispersion of 0.1 and 2.0 km s$^{-1}$ to avoid creating pseudostructures such as spikes or baseline-like structure with a wide velocity line width. We found $\sim$3700 velocity components for 3236 pixels, and pixels having double and triple velocity components are $\sim$15% and <1%, respectively. The velocity structures appear to be somewhat complicated, especially in the western region, and the results of decomposition are significantly uncertain in the pixels with low signal-to-noise ratio (S/N).

FindingFilaments is an algorithm designed for identifying filamentary structures that uses a similar concept to the FoF. FoF is the algorithm originally used to find a group of galaxies in an external galaxy survey, and to create groups of adjacent galaxies within a certain range in three-dimensional space of R.A., decl., and redshift (e.g., Huchra & Geller 1982). The FF algorithm is similar to the FoF in that it collects adjacent points in three-dimensional space of R.A., decl., and velocity, but differs from the FoF in that it treats overlapping components in the line-of-sight direction, i.e., components at the same R.A. and decl. but having different velocities, as different ones. The data set used in the FF algorithm is the pixel number, the emission amplitude, the central velocity, and the velocity dispersion for the Gaussian components that are decomposed from the spectra.

The FF algorithm works in an iterative manner based on the steps mentioned below. First, it selects a decomposed Gaussian seed component with the maximum amplitude and gives the structure a number. Second, it selects the other Gaussian components in the neighboring pixels whose pixel distance is less than $\sqrt{2}$ from the seed component, and checks the velocity differences of the seed and other components in the neighboring pixels. At this stage, if the velocity difference between the seed and other components in the neighboring pixel is less than the velocity dispersion of the seed ($\sigma_{\gamma}^{\text{seed}}$), the neighboring

---

$^{14}$ https://github.com/radioshiny/funstools
component is assigned as a friend of the seed and given the same structure number. If more than one velocity component in a neighboring pixel is within the range of velocity dispersion from the velocity of the seed, then only the closest one becomes the friend of the seed. Third, after every neighboring component has been checked, the assigned friends of the seed become the seeds of the structure for the next turn, and the same second and third steps are repeated until there are no more friends to assign.

We do not use any criterion of intensity gradient or initial assumption of filament direction but use the distance in the PPV space. Hence, the result changes only with the given criterion of velocity difference between the seed and the neighboring component for which we use $\sigma_v^{seed}$ in our study.

**Figure 5.** Integrated intensity map (top), velocity field map (middle), and line width map (bottom) of each filament. Peak velocity ($V_{\text{peak}}$) and line width ($\Delta V$) are quantities derived by the Gaussian fitting method. Locations of the filament’s ridges (skelets) are drawn on top of the maps and the notations of sub-filaments are given in the middle panel. A small offset is given to the original position of each filament to avoid spatial overlaps and distinguish them from each other. The small clumps in the left and right dotted square boxes are shifted by (0, $+18^\prime$) and (0, $-29^\prime$) from their original positions (dashed square boxes), respectively.
However, it turned out that the result does not change with an even smaller criterion value (∼0.1 km s$^{-1}$) than $\sigma_{\text{int}}$. Hence, the algorithm applying to the decomposed Gaussian components firmly identifies the velocity coherent structures in the PPV space.

We found 44 structures that are larger than one beam size ($\theta_{\text{FWHM}} \sim 49\arcsec$). Of these, 30 structures have sizes $\lesssim 4 \times \theta_{\text{beam}}$ and aspect ratios ($d_{\text{max}}/d_{\text{min}}$ where $d_{\text{max}}$ and $d_{\text{min}}$ are the largest and smallest diameters of the structure, respectively) less than 3, i.e., they can be considered roundish clumps rather than elongated filaments. The other 14 structures have sizes larger than $6 \times \theta_{\text{beam}}$ and elongated shapes. Hence, we mainly analyzed the largest 14 structures, and assigned numbers to the filaments as F1 to F14 from west to east. For the other 30 smaller structures ($\lesssim 4 \times \theta_{\text{beam}}$), we assigned numbers as Clump1 to Clump30 (CL1 to CL30), again from west to east in our analysis.

The distribution of the filaments and the clumps is presented in Figure 4. The 14 filaments are identified with their numbers, but the small clumps are presented as unnumbered thin white and black lines. Filament4 (F4) is the largest filament of IC 5146 that is continuously connected in the plane of the sky and also in velocity space. Four filaments (F2, F3, F5, and F6) and a large number of small clumps are found to overlap F4 in the plane of the sky.

To estimate the length of the filaments, the skeleton is determined with FILFINDER (Koch & Rosolowsky 2015) using the integrated intensity map of each filament. FILFINDER uses the medial axis transform method, which gives the skeleton of the set of central pixels of inscribed circles having a maximum radius. We already identified filaments with the three-dimensional data cube, and the resulting filaments are continuous and coherent in the PPV three-dimensional space; the skeletons are used to calculate the length and width of each filament. Hence, we used the major skeleton only and excluded small minor skeletons in each filament. However, some filaments show multiple structures in the integrated intensity map of the filaments (F1, F4, F6, and F9, see Figure 5(a)). Hence, we used multiple skeletons to estimate physical quantities of each subfilament (e.g., F1a, F1b).

### 4.2. Physical Properties of the Identified Filaments

Physical properties of the 14 filaments, such as H$_2$ column density, H$_2$ mass, length, width, mass per unit length, and nonthermal velocity dispersion, are derived. The results are listed in Table 2. For the 30 clumps, H$_2$ column densities, H$_2$ masses, effective radii, and virial masses are calculated and given in Table 6 in the Appendix.

#### 4.2.1. H$_2$ Column Density and Mass

H$_2$ column densities ($N_{\text{H}_2}$) in the filaments were estimated from C$^{18}$O (1–0) data using the formula derived under the assumption of local thermodynamic equilibrium (see Section A.1.
in the Appendix for more details), and ranged between \(\sim 6 \times 10^{20}\) and \(2 \times 10^{22}\) cm\(^{-2}\). H\(_2\) masses of the filaments are from \(\sim 4\) to \(400\) \(M_\odot\). The masses of the 30 clumps that are given in Table 6 range from \(\sim 1\) to \(7\) \(M_\odot\). The given uncertainty of mass is assigned by propagating the observational rms error.

4.2.2. Length, Width, and Mass per Unit Length

The lengths of the filaments are estimated along the skeleton without any correction for inclination. The widths of the filaments are measured from the radial profile of H\(_2\) column density along the distance from the skeleton, where the FWHM of a Gaussian fit is the width of the filament.

The lengths of the main filaments are about 0.3–4.2 pc and the widths are about 0.2–0.7 pc assuming distances of 800 pc and 600 pc for the Cocoon (F10 to F14) and the Streamer (F1 to F9), respectively. The width is significantly larger than the filament width of 0.1 pc derived from the Herschel continuum data (e.g., Arzoumanian et al. 2019). These large widths of the filaments in our study are probably due to the limited spatial resolution (0.14–0.2 pc) of our observations and/or a relatively flat distribution of CO, which may be due to the possible depletion of CO molecules in the region of the filament with high column density and/or the lower dynamic range of the distribution of CO emission in comparison with the continuum emission.

The mean masses per unit length (\(M_{\text{line}}\)) of the filaments were calculated by simply dividing the mass by the length obtained above, and given in Table 2 with the errors propagated from the observational uncertainties. \(M_{\text{line}}\) is found to be between \(\sim 20\) and \(120\) \(M_\odot\) pc\(^{-1}\). We derived the virial mass and the virial parameter, \(\alpha_{\text{vir}} = M_{\text{vir}}/M_\odot\), for 30 clumps with a low aspect ratio (\(\lesssim 3\)) using Equation (A5), instead of deriving the mass per unit length. Their estimated values are found in the ranges \(\sim 0.5–5\) \(M_\odot\) and \(\sim 0.4–1.2\), respectively.

4.2.3. Global Velocity Field

Global velocity fields of the filaments are presented in the middle panel of Figure 5 and in Figure 6. It is shown that the filaments have coherent and continuously changing velocity fields. Overall IC 5146 has filaments with LSR velocities from 1.2 to 8.8 km s\(^{-1}\) and the velocity in each filament changes by \(\sim 1–2\) km s\(^{-1}\).

Figure 6 presents in detail the velocity fields of the filaments along the skeletons. \(L_{\text{fil}}\) is the distance of a position in the filament measured along the skeleton from its easternmost point. There are several positions that are not on the skeleton. \(L_{\text{fil}}\) for those were assigned as \(L_{\text{fil}}\) of the locations on the skeleton nearest to such positions. The velocities monotonically increase or decrease along the skeletons in the majority of the filaments. However, oscillatory behavior as seen in the Taurus L1495/B213 complex and California L1478 (e.g., Tafalla & Hacar 2015; Chung et al. 2019) can be also seen in filament F4a. It was suggested that the increment of the velocity from the center to both edges in F4a can be a signature of edge-driven collapse and fragmentations (Wang et al. 2019).

We measured velocity gradients employing the gradient numpy PYTHON code.\(^{15}\) We used the Gaussian-decomposed velocity field of each filament, and the gradient algorithm computes the gradient at every position using second-order central differences. The right panel of Figure 6 shows the normalized histogram of the derived velocity gradient. This is an upper limit, because we have not corrected the inclination. Most of the filaments have velocity gradients between 0 and 2 km s\(^{-1}\) pc\(^{-1}\), and about 46% of the velocity gradients are larger than 1 km s\(^{-1}\) pc\(^{-1}\). F4, which is the largest filament in IC 5146, appears to have distinguishably larger velocity

\(^{15}\) https://numpy.org/doc/stable/reference/generated/numpy.gradient.html
4.2.4. Nonthermal Velocity Dispersion

Nonthermal velocity dispersion (σNT) is calculated with the following equation:

$$\sigma_{NT} = \sqrt{\frac{\sigma_{obs}^2 - k_B T}{m_{obs}}},$$

where σobs is the total velocity dispersion estimated from the FWHM of the observed molecular line, $k_B$ is the Boltzmann constant, $T$ is the gas temperature, and $m_{obs}$ is the mass of the observed molecule of C18O. Dust temperature from the Herschel data (André et al. 2010; Arzoumanian et al. 2011) is used for the gas temperature after the data have been convolved to the resolution of TRAO and resampled to the pixel grid of TRAO data. The uncertainty of $\sigma_{NT}/c_s$ is measured from that of the velocity dispersion and that of the dust temperature caused by the different resolution of Herschel and TRAO, and $\sigma_{NT}/c_s$ varies within about ±5%.

Figure 7 shows the distribution of nonthermal velocity dispersion along the filament skeleton and the normalized histogram of $\sigma_{NT}/c_s$ of the filament. Filaments in IC 5146 appear to be mostly transonic ($1 < \sigma_{NT}/c_s < 2$). However, some filaments (e.g., F4) show supersonic motions within a somewhat limited area. We found some correlation between the presence of dense cores in the filaments and the nonthermal velocity dispersion in the filaments. Most of all, dense cores tend to exist in the filaments with large nonthermal velocity dispersion mostly in the transonic regime. Furthermore, all the filaments that are dominant with subsonic motions ($\sigma_{NT}/c_s \sim 1$) are found to have no dense core except for one, filament F12.

4.3. Comparison of C18O Filaments with the Herschel Continuum Filaments

Arzoumanian et al. (2011) investigated the filament properties of IC 5146 using Herschel dust continuum data. They produced dust temperature ($T_{dust}$) and H2 column density ($N_H$) maps of IC 5146 based on the 70 to 500 μm data, and applied the DISPERSE algorithm (Sousbie 2011) to the curvelet image to find 27 filaments. In this section, we examine and compare the filaments of IC 5146 identified using C18O (1-0) emission with those identified by Arzoumanian et al. (2011). We will refer to these two types of filaments as C18O filaments and Herschel continuum filaments, respectively.

Figure 8 compares the skeletons of the Herschel continuum filaments and the outlines of the C18O filaments. The main features of the filaments found with these two different tracers appear to be similar in the bright regions, but are different in the less bright region and the regions where there are multiple C18O filaments with different velocity components overlapped in the line-of-sight direction.
Due to the superior sensitivity, the filaments identified using the Herschel continuum data are also found in areas where C$^{18}$O (1–0) emission is absent. These Herschel continuum filaments are well connected to the filaments where the C$^{18}$O (1–0) line is bright, so that one C$^{18}$O filament consists of several Herschel continuum filaments. For example, in the case of F9 in region A, three different Herschel continuum filaments depicted in bright green, red, and blue meet, but only one C$^{18}$O filament, F9, is identified. In contrast, the filaments identified using the dust continuum emission from Herschel can be separated into two or more structures in the analyses done with the C$^{18}$O (1–0) emission since the Herschel dust emission is detected in relatively less bright regions than C$^{18}$O (1–0). For example, the Herschel continuum filament shown in bright green in region A includes the C$^{18}$O filaments F8 and F9. The nearest points of F8 and F9 have similar velocities of \( \sim 4.4 \) km s\(^{-1}\), but they are slightly off (about one FWHM beam size) in the plane of the sky.

Identification of the continuum filaments cannot be consistent with that of the C$^{18}$O filaments if there are multiple filaments with different velocities along the line of sight. The Herschel continuum filament illustrated with a red line in region C is overlaid on the C$^{18}$O filaments F2 and F4. As indicated by white arrows in the \( p-v \) diagram (Figure 15 in the Appendix), F2 and F4 have totally different velocities in the C$^{18}$O (1–0) observations even though they appear to be continuously connected in the continuum emission. Another inconsistency in the identification of the filaments in line and continuum emission can be seen around the C$^{18}$O filament F5 in region B. F5 overlaps with F4 but has a different velocity to it. In the dust continuum emission, the overlapping region appears brighter and the ridges found in the Herschel continuum filament are separated into two (skeletons with black and lime colors).

5. Dense Core Properties

5.1. Dense Core Identification

The N$_2$H$^+$ line is usually optically thin (except toward the central regions of prestellar cores; e.g., Keto & Caselli 2010), and is an appropriate tracer of dense cores in nearby star-forming regions. We identified dense cores by applying the FELLWALKER clump-finding algorithm (Berry 2015) to the N$_2$H$^+$ (1–0) integrated intensity images. In running this algorithm, an object with a peak intensity higher than 3\( \sigma \) and size larger than \( 2.5 \times \) the beam size of 52\( '' \) is identified as a real dense core. Pixels with intensities \( >0.5\sigma \) are allowed to be associated with a peak. Two neighboring peaks are considered as separate if the difference between the peak values and the minimum value (dip value) between the peaks is larger than 1\( \sigma \).

In total, we found 22 dense cores: one core in the Cocoon Nebula and 21 in the Streamer. Information about the identified dense cores is in Table 3. The position, size, and position angle (PA) of the dense cores are the results that the applied FELLWALKER algorithm gives. \( V_{\text{peak}} \) and \( \Delta V(N_2H^+) \) are estimated by simultaneously fitting seven Gaussian functions for the seven hyperfine components of N$_2$H$^+$ (1–0) using the line parameters given by Caselli et al. (1995). Filament ID that shares the PPV space with the dense core is provided. It is noticeable that C18 is not related with the filament F7, but with the clump CL22, while every other dense core shares the PPV space with various filaments and not with the clumps. There are 14 stared cores that are well matched with the positions of the YSO candidates from Spitzer (Harvey et al. 2008) and 70 \( \mu \)m point sources from Herschel/PACS Point Source Catalogue (HPSC; Poglitsch et al. 2010) and eight starless cores where no YSOs are found. The positions and averaged spectra of the dense cores are presented in Figures 9 and 10.

5.2. Mass and Virial Mass

We derive masses of dense cores with the integrated intensity of N$_2$H$^+$ (1–0) and the virial masses as described in Section A.2 in the Appendix and tabulate the quantities in Table 3. The virial parameters, \( \alpha_{\text{vir}} = M_{\text{vir}}/M \), of the dense cores range between \( \sim 0.3 \) and 2.6. A significant number of dense cores (10 among the 22) are virialized (\( \alpha \leq 1 \)), and three dense cores have \( 1 < \alpha < 2 \) and are likely close to gravitationally bound considering the large uncertainty in \( \alpha \) (a factor of \( \sim 2 \)). We found three most massive dense cores C3, C7, and C17. Their masses are estimated to be \( \geq 15 M_\odot \) and their virial parameters are found to be quite small (\( \alpha_{\text{vir}} \approx 0.5 \), giving a

Figure 8. Comparison between C$^{18}$O filaments and Herschel continuum filaments. C$^{18}$O filament outlines are drawn and tagged with their numbers. The skeletons of the Herschel continuum filaments are shown as colored lines. The dashed circles A, B, and C show representative regions where the C$^{18}$O filaments and Herschel continuum filaments are differently identified. See the text.
hint that there must be active star formation. In fact, they are found to contain multiple YSOs.

5.3. Chemical and Dynamical Properties of Starless Cores

SO and CO molecules are known to easily deplete in cold dense cores while the N$_2$H$^+$ molecule can survive well at very evolved stage of the dense core (e.g., Caselli et al. 1999; Tafalla et al. 2006). In addition, NH$_2$D, deuterated ammonia, can survive in the gas phase in the interior of highly evolved prestellar cores, and comparison of the distributions of these molecules around dense cores would be very useful to infer how the cores are chemically evolved (e.g., Crapsi et al. 2007). Here we explain how the distribution of these molecules is different from core to core, especially for starless cores (C2, C5, C6, C8, C10, C12, C13, and C16).

Table 3

| Core ID | Position | Size | PA | $V_{\text{N}_2\text{H}^+}$ | $\Delta V_{\text{N}_2\text{H}^+}$ | $M_{\text{obs}}$ | $\alpha_{\text{corr}}$ | Fil. ID | YSOs |
|--------|----------|------|----|----------------|-----------------|----------------|----------------|--------|------|
| C1     | 21:44:42.5 | +47:45:18.5 | 0.33 | 0.14 | 101 | 4.50 | 0.49 ± 0.05 | 4.2 ± 3.0 | 0.5 ± 0.4 | F1a | 3 |
| C2     | 21:44:51.4 | +47:36:42.3 | 0.17 | 0.10 | 8   | 3.80 | 1.20 ± 0.20 | 1.8 ± 1.2 | ... | F4h | 4 |
| C3     | 21:44:56.1 | +47:39:51.7 | 0.57 | 0.26 | 126 | 4.20 | 1.04 ± 0.04 | 23.7 ± 16.7 | 0.5 ± 0.3 | ... | F4g | 2 |
| C4     | 21:44:59.6 | +47:42:09.0 | 0.11 | ≤0.15 | 104 | 1.70 | 0.59 ± 0.05 | 0.5 ± 0.4 | ... | F2  | 2 |
| C5     | 21:44:59.1 | +47:36:11.2 | ≤0.15 | ≤0.15 | 172 | 4.29 | 0.47 ± 0.06 | 0.8 ± 0.6 | ... | F4e | 2 |
| C6     | 21:45:04.3 | +47:43:59.5 | 0.23 | 0.09 | 20  | 1.40 | 0.54 ± 0.06 | 1.0 ± 0.7 | 1.7 ± 1.5 | F2  | 2 |
| C7     | 21:45:07.7 | +47:33:28.2 | 0.54 | 0.27 | 121 | 3.98 | 0.57 ± 0.02 | 16.5 ± 11.6 | 0.3 ± 0.2 | ... | F4e | 2 |
| C8     | 21:45:26.8 | +47:33:20.8 | 0.02 | ≤0.15 | 131 | 3.70 | 0.38 ± 0.07 | 0.9 ± 0.6 | ... | F4e | 2 |
| C9     | 21:45:31.2 | +47:36:09.5 | 0.32 | 0.29 | 71  | 4.00 | 0.89 ± 0.06 | 7.3 ± 5.2 | 0.9 ± 0.7 | F4a | 2 |
| C10    | 21:45:46.0 | +47:36:28.2 | 0.18 | ≤0.15 | 22  | 4.00 | 0.87 ± 0.17 | 1.4 ± 1.0 | ... | F4a | 1 |
| C11    | 21:45:57.7 | +47:35:45.4 | 0.27 | 0.24 | 126 | 3.80 | 0.68 ± 0.05 | 6.4 ± 4.5 | 0.5 ± 0.4 | ... | F4a | 8 |
| C12    | 21:46:28.6 | +47:34:42.8 | 0.14 | 0.11 | 116 | 3.40 | 1.13 ± 0.41 | 1.0 ± 0.7 | ... | F4a | 2 |
| C13    | 21:46:52.0 | +47:40:03.7 | 0.09 | ≤0.15 | 169 | 3.90 | 0.49 ± 0.08 | 0.6 ± 0.5 | ... | F4b | 1 |
| C14    | 21:47:04.5 | +47:39:49.1 | 0.16 | 0.08 | 95  | 4.30 | 0.47 ± 0.10 | 1.7 ± 1.2 | ... | F4b | 1 |
| C15    | 21:47:05.8 | +47:33:02.3 | 0.33 | 0.11 | 174 | 4.10 | 0.49 ± 0.04 | 3.8 ± 2.7 | 0.5 ± 0.4 | F4a | 2 |
| C16    | 21:47:22.0 | +47:34:06.4 | 0.21 | 0.13 | 128 | 3.67 | 0.54 ± 0.03 | 3.8 ± 2.7 | 0.4 ± 0.3 | F4a | 8 |
| C17    | 21:47:23.0 | +47:31:55.9 | 0.35 | 0.22 | 113 | 3.90 | 0.94 ± 0.06 | 17.0 ± 12.0 | 0.4 ± 0.3 | ... | F4a | 2 |
| C18    | 21:47:56.5 | +47:37:01.3 | 0.27 | 0.09 | 150 | 5.00 | 0.52 ± 0.04 | 2.9 ± 2.1 | 0.6 ± 0.5 | ... | F4a | 8 |
| C19    | 21:48:52.6 | +47:31:10.5 | 0.42 | 0.24 | 151 | 3.90 | 1.04 ± 0.10 | 5.4 ± 3.8 | 1.6 ± 1.4 | F8  | 2 |
| C20    | 21:49:23.4 | +47:29:02.0 | 0.27 | 0.06 | 37  | 5.00 | 0.59 ± 0.06 | 3.0 ± 2.1 | 0.6 ± 0.5 | F9a | 2 |
| C21    | 21:49:30.9 | +47:27:20.4 | 0.30 | 0.20 | 122 | 4.90 | 0.45 ± 0.40 | 4.4 ± 3.1 | ... | F9a | 2 |
| C22    | 21:52:36.7 | +47:14:33.4 | 0.20 | ≤0.20 | 60  | 4.60 | 0.64 ± 0.12 | 1.6 ± 1.2 | ... | F12 | 7 |

Notes.

a The core size is corrected for the beam smearing effect with the equation $x_{\text{corr}} = \sqrt{x_{\text{obs}}^2 - \theta^2}$ where $x_{\text{corr}}$ is the corrected size, $x_{\text{obs}}$ is the observed size, and $\theta$ is the standard deviation of the Gaussian beam profile (Berry 2015). For the cores with smaller observed size than $\theta$, the beam size is given as the upper limit of the core size.

b The uncertainty of $M_{\text{obs}}$ is estimated from the observational rms error and that of $\alpha_{\text{corr}}$ is propagated from those observational uncertainties.

c Filament ID given in Table 2.

d Number of YSO candidates from Spitzer (Harvey et al. 2008) and HPPSC (Poglitsch et al. 2010).

e Dense core C18 is located in the overlapped region of filament F7 and clump CL22, but its velocity is the same as that of CL22.
Figures 16–20 in the Appendix present the integrated intensity maps of N$_2$H$^+$ (1–0), SO (3$_2$–2$_1$), and C$^{18}$O (1–0) of dense cores. The N$_2$H$^+$ (1–0) emission in our sample of starless cores found in IC 5146 is mostly weak but centrally concentrated, and its peak positions are approximately coincident with those of the 250 μm continuum emission. The SO (3$_2$–2$_1$) line seems also to trace the dense region of the cores. But its emission is as weak as N$_2$H$^+$ (1–0) in most starless cores. On the other hand, the C$^{18}$O (1–0) emission appears much brighter than the other two molecular lines, tracing wide regions of the clouds. Looking at the distribution of the C$^{18}$O (1–0) emission toward the N$_2$H$^+$ starless cores, we do not see any significant hint of CO freeze-out in those cores. The differences among the spatial distributions of our tracers are probably from a combination of the critical densities and the chemical properties of the tracers. The C$^{18}$O (1–0) line with relatively low critical density (∼1.9 × 10$^3$ cm$^{-3}$) would be easily detected over the wide area of the less dense clouds.
while tracers such as SO and N$_2$H$^+$ with higher critical densities ($>10^5$ cm$^{-3}$) are detected only in the very dense core regions (see $n_{\text{crit}}$ in Table 1). However, all those distributions would be modified with their chemical properties such as freeze-out or enhancement in the cold dense regions of the cores. In the case of starless cores in IC 5146, weak emission in N$_2$H$^+$ and SO, and no significant depletion in CO, give a hint that most starless cores may not be highly evolved.

NH$_2$D ($J = 11 - 10$) is not detected at the rms level of 0.06 K[$T^*_A$] with 0.1 km s$^{-1}$ channel resolution. We estimated a 3σ upper limit of the NH$_2$D abundance using the column density obtained from Equation (4) in Wienen et al. (2021) as $\sim 5 \times 10^{-10}$. This upper limit can be compared with the abundance of NH$_2$D as a function of time from the NAUTILUS chemical model by Majumdar et al. (2017), giving an upper limit for the age of the starless cores in our study as a few million years, which is consistent with the range of the statistical timescale of starless dense cores (e.g., Lee & Myers 1999). This indicates that our dense cores may have a wide range of ages. However, many dense cores found in IC 5146 may not be fully evolved to have detectable NH$_2$D emission. This is also consistent with the idea that most dense starless cores are chemically young from their characteristic distribution of N$_2$H$^+$, SO, and C$^{18}$O. On the other hand there are several other starless cores showing a signature of highly evolved status such as gas infalling motions as mentioned below. Thus we cannot rule out another possibility that some of the starless cores are highly evolved, but NH$_2$D may be present only in the limited small area of the central region of the core and thus be beam-diluted within our large beam of the TRAO.
6. Discussion

6.1. Nonthermal Motion and Systemic Velocity of Filaments and Dense Cores

A colliding model has been proposed where filaments can form by the collision of turbulent flows, and the dissipation of turbulence creates the dense cores (e.g., Ballesteros-Paredes et al. 1999; Padoan & Nordlund 2002). It is expected that if the cores form from the collision between turbulent filaments, the initially turbulent filaments would remain supersonic while the cores formed in them would be in subsonic motion. Hence, diagnosing the kinematic properties of the filaments and dense cores would examine this collision mechanism for the formation of filaments and dense cores.

Figure 11 displays the nonthermal velocity dispersions and systemic velocities for the C$^{18}$O and N$_2$H$^+$ gas to compare the line width and systemic velocity properties between the filaments and the dense cores. The velocity dispersion and systemic velocity of the C$^{18}$O gas are derived from the Gaussian fitting of the C$^{18}$O (1–0) spectrum averaged over the area of the dense core, and thus would represent the kinematic properties of the filament material in the line-of-sight direction of the dense core. The velocity dispersion and systemic velocity of N$_2$H$^+$ (1–0) were obtained in the same manner as those of C$^{18}$O (1–0).

In the left panel of Figure 11, the nonthermal velocity dispersions of C$^{18}$O and N$_2$H$^+$ (1–0) are compared. All the dense cores have smaller $\sigma_{\text{NT}}^{\text{CIO}}/c_s$ than $\sigma_{\text{NT}}^{\text{NHO}}/c_s$ except C12, C18, C19, and C22, where $\sigma_{\text{NT}}^{\text{NHO}}/c_s$ is almost the same as $\sigma_{\text{NT}}^{\text{CIO}}/c_s$ within their uncertainties. The ratios of $\sigma_{\text{NT}}^{\text{NHO}}/c_s$ to $\sigma_{\text{NT}}^{\text{CIO}}/c_s$ for most of the dense cores range between $\sim$0.4 and $\sim$0.7.

Similar kinetic features between dense cores and the surrounding filaments have also been found in a previous study of L1478 in the California cloud by Chung et al. (2019). In that study, the dense cores are divided into two groups according to their nonthermal velocity dispersions. One group contains cores where the nonthermal velocity dispersions are similar to those of their surrounding filaments, and the other contains cores where the nonthermal velocity dispersions are smaller than those of their surrounding filaments. The cores in the former group are found to be in a single-shaped filament but the cores in the latter group are located in the hub–filament structures.

Likewise, this study also shows that all the dense cores (except C1, C6, and C21) have $\sigma_{\text{NT}}^{\text{NHO}}/c_s$ smaller than $\sigma_{\text{NT}}^{\text{CIO}}/c_s$ by about the sound speed ($c_s$) are located in the filament F4 showing hub–filament structures in the easternmost (near C17) and also westernmost (near C3) regions. In addition, the central region of F4, near C11, appears to be a hub where the sub-filaments F4a, F4e, and F4f meet. C15 is also located at the intersection of F4a and F4d (see Figure 22 in the Appendix). These nonthermal motions of dense cores, i.e., $\sigma_{\text{NT}}^{\text{NHO}}/c_s$ smaller than $\sigma_{\text{NT}}^{\text{CIO}}/c_s$, are consistent with the expectations of the collision scenario.

One thing we should notice here is that the nonthermal velocity dispersion may arise from turbulence and/or any bulk motions such as gas infall or bipolar outflow. Infall motions are found in three starless cores, C2, C6, and C16 (Section 5.3), and CO outflows have been observed in five starless cores, C3, C7, C11, C17, and C18 (Dobashi et al. 2001). However, such motions can be hardly traced with N$_2$H$^+$ and C$^{18}$O (1–0) because these lines are usually optically thin and poorly sensitive to those gas motions (e.g., Lee et al. 2001; Fuente et al. 2012; Lo et al. 2015). Most of all, the infall speeds found in starless cores are quite low, of the order of 0.1 km s$^{-1}$, making it hard for them to play a major role in broadening of the lines. Moreover, these lines likely trace the gas at the centers of the outflows in the starless cores, i.e., the outflow motions can be partially traced by these lines only at the position of the driving source (e.g., Su et al. 2004; Lee et al. 2018). Thus in our case where the line profiles under discussion were obtained from averaging profiles over the area of the dense cores, it is unlikely that infall or outflow motions would significantly affect the broadening of the lines and both $\sigma_{\text{NT}}^{\text{CIO}}$ and $\sigma_{\text{NT}}^{\text{NHO}}$. Hence, the main origin of the nonthermal velocity dispersions obtained from the C$^{18}$O and N$_2$H$^+$ (1–0) lines is thought to be from the turbulence. Therefore, the different nonthermal velocity dispersions of C$^{18}$O and N$_2$H$^+$ (1–0) of the cores can be interpreted with the dissipation of turbulence after the collisions of turbulent filaments.

Hence, F4 and most of the dense cores in it, at least the cores in the
Figure 14. Dense cores in the filaments. The integrated intensity of C$^{18}$O (1–0) emission is drawn with contours at the 3σ level, and skeletons of filaments are overlaid with solid lines. The 14 cores with YSOs are drawn in red, and the eight starless cores are color-coded based on the total points for grading their evolutionary status in Table 5, i.e., black, gray, blue, purple, and pink for cores with total points from 1 to 5, respectively; a larger total means that the core is more evolved. The thick red ellipses indicate cores with YSOs located in the hubs.

The systemic velocity shift between the C$^{18}$O and N$_2$H$^+$ gas also supports the collision scenario for the formation of dense cores in the hubs. In the right panel of Figure 11, the systemic velocities of the dense cores and the filament material correlate well with each other, and in the majority of them, the differences are smaller than or similar to the sound speed ($\sim$0.20 km s$^{-1}$ at 13 K, which is the mean dust temperatures of the dense cores measured from the Herschel data). However, C3, C5, C14, C15, and C17 have a larger offset than the sound speed between the systemic velocities of the dense cores and the filamentary gas. The systemic velocity shift between the N$_2$H$^+$ and C$^{18}$O gas of the five cores is 0.32 ± 0.06 km s$^{-1}$. This discrepancy is first attributed to the uncertain $V_{N_2H^+}^{sys}$ due to the low S/N. However, the N$_2$H$^+$ (1–0) spectra of C3 and C17 show high S/N, and the velocity difference between the C$^{18}$O and N$_2$H$^+$ (1–0) emission can be caused by the merging of filaments with different velocities.

The relative core-to-envelope motions have been studied to investigate the core formation mechanism, but no displacement in the systemic velocities between the dense gas and the surrounding gas has been found in the low-mass star-forming regions (e.g., Kirk et al. 2007; Harc& Tafalla 2011; Punanova et al. 2018; Chung et al. 2019). However, recently, a velocity difference of $\sim$0.3 km s$^{-1}$ between C$^{18}$O and N$_2$H$^+$ (1–0) lines was observed in the infrared dark clouds (IRDCs) G035.39–00.33 and G030.43+00.24 (Henshaw et al. 2013; Barnes et al. 2018). These clouds are proposed to be formed by the collision of filaments, and the velocity difference indicates that the merging of filaments is still ongoing.

In fact, filaments and clumps overlapped on the line of sight can be easily found around most of the dense cores (see Figure 9). C3 and C17, in particular, are located at the hubs where the largest filaments merge. Inspecting the C$^{18}$O (1–0) spectra in the regions, multiple velocity components are presented in the cores (Figure 21 in the Appendix). The offset value of $V_{C^{18}O_{sys}}-V_{N_2H^+_{sys}}$ is similar to the velocity shift between C$^{18}$O and N$_2$H$^+$ gas in the IRDCs G035.39–00.33 and G030.43+00.24. Hence, the velocity difference of the five cores with respect to the systemic velocities of their parent filaments can imply that the dense cores are forming via the merging of the filaments.

6.2. Are the Filaments and Clumps in IC 5146 Gravitationally Bound?

Under the assumption that a filament is an infinitely long, self-gravitating, isothermal cylinder with only thermal support, the equilibrium mass per unit length is given by

$$M_{\text{line}}^{\text{th, crit}} = \frac{2c_s^2}{\mu G},$$

(2)

where $c_s$ and $G$ are the isothermal sound speed and gravitational constant, respectively (Inutsuka & Miyama 1992, 1997). The median value of the dust temperature in IC 5146 is about 23 K in the Cocoon Nebula and about 15 K in the Streamer (Arzoumanian et al. 2011). The corresponding $M_{\text{line}}^{\text{th, crit}}$ is $\sim$32 $M_{\odot}$ pc$^{-1}$ at 23 K and $\sim$20 $M_{\odot}$ pc$^{-1}$ at 15 K. On the other hand, the effective critical mass per unit length that includes the nonthermal components of turbulent motions is calculated as

$$M_{\text{line}}^{\text{crit}} = \frac{2\sigma_{\text{tot}}^2}{\mu G},$$

(3)

where $\sigma_{\text{tot}}$ is the average total velocity dispersion of the mean free particle of molecular weight $\mu = 2.8$ within a filament (e.g., Arzoumanian et al. 2013; Peretto et al. 2014). The effective critical mass per unit length of each filament is calculated using the average total velocity dispersion, and these values are tabulated in Table 2.

Figure 12 gives the mass per unit length of filaments with the critical mass per unit length, indicating that the majority of those in IC 5146 are supercritical or marginally critical ($\gtrsim M_{\text{line}}^{\text{crit}}$ or $M_{\text{line}}^{\text{th, crit}}$) within uncertainties of a factor of 2. Meanwhile, the filaments F2 and F8, which harbour dense cores, have $M_{\text{line}}^{\text{crit}}/M_{\text{line}}^{\text{th, crit}} \lesssim 1$ and are subcritical even with the uncertainties of a factor of 2. One of the possible explanations for the subcritical filaments with dense cores is that the CO depletion via freeze-out onto dust grains as the core evolves results in an understimation of the filament mass. Filaments with N$_2$H$^+$ cores clearly must have CO freeze-out, since otherwise N$_2$H$^+$ emission would not have been seen. This implies that the C$^{18}$O-based masses are probably an underestimate of the true value. In Figure 23 in the Appendix, H$_2$ column densities derived from our C$^{18}$O (1–0) and from the Herschel data...
are compared. F2 and F8 are shown to have a shallower slope of $N_{C^{18}}^{\mathrm{HC}}$ to $N_{C^{18}}^{\mathrm{Herschel}}$ than that in total, especially where $N_{C^{18}}^{\mathrm{Herschel}} \gtrsim 5 \times 10^{21}$ cm$^{-2}$. The presence of cores in the filament may reflect fragmentation that occurred in the past history of the filament, but the current criticality of a filament indicates its ability to make cores in the future. If filament velocity dispersions and other properties have changed over time, their criticality may have changed as well. Hence, we speculate that F2 and F8 formed dense cores in supercritical, or at least transcritical, conditions, but they appear to be subcritical subsequently due to the depletion of CO as a result of core evolution inside the filament.

We also test gravitational instability for the 30 clumps that show a smaller aspect ratio than the filaments by deriving their virial parameters. Figure 13 shows masses of the 30 clumps as a function of their virial mass ($M_{\mathrm{vir}}$). Most of the clumps are virialized ($M_{\mathrm{obs}} > M_{\mathrm{vir}}$). The clump CL22, which is found to be consistent in the velocity field as well as in the plane of the sky with the dense core C18, has $\alpha_{\mathrm{vir}} \sim 0.5$, indicating that CL22 is virialized and gravitationally contracting.

We conclude that most of the filaments and clumps in IC 5146 are gravitationally bound systems that can form prestellar cores and stars by contraction and fragmentation.

6.3. Velocity Field and Gradient: Filaments as Passages of Mass Flow?

Several previous observations of molecular lines toward filaments have found that filaments have velocity gradients (e.g., Hacar et al. 2016; Barnes et al. 2018; Chung et al. 2019). One explanation for the velocity gradients in the filaments is gravitational accretion onto the filaments. The most representative example is the Taurus B211/3 filament, in which striations parallel to the B-field but perpendicular to the main filament ridge are observed (Palmeirim et al. 2013). The velocity difference between the filament and the striations is $\sim 1$ km s$^{-1}$, being well matched with what is expected from gravitational freefall motions. Another example of a velocity gradient, which is now along the filament, is presented by Kirk et al. (2013) in the Serpens South filament. The reported velocity gradient in Serpens South is $1.4 \pm 0.2$ km s$^{-1}$ pc$^{-1}$ with an assumption for the inclination angle of $20^\circ$. Their study suggested that mass flow along the filaments into the central star clusters plays an important role in their ongoing star formation. Treviso-Morales et al. (2019) investigated Monoceros R2, a representative hub-filament system forming high-mass stars. They found increasing velocity gradients along the filaments toward the hub, claiming that the gas accelerates near the gravitational potential well of the hub and makes the formation of high-mass stars possible in the hub region. All of these findings indicate that the flow of material along the filaments will possibly directly affect the formation of dense cores and stars.

It is interesting to note that F4, which harbors the largest number of dense cores and YSOs, has the largest velocity gradient ($\nabla V$) in IC 5146. The mean $\nabla V$ of F4 is $1.7 \pm 1.2$ km s$^{-1}$ pc$^{-1}$, and the portion of the filament with $\nabla V$ larger than 2 km s$^{-1}$ pc$^{-1}$ is close to 30%. However, the other filaments have mean $\nabla V$ of $1.3 \pm 0.9$ km s$^{-1}$ pc$^{-1}$, and the portion with $\nabla V$ larger than 2 km s$^{-1}$ pc$^{-1}$ is less than 15%. Since we derived the velocity gradient without correcting for the inclination ($\alpha$), projection effects should be considered. The observed velocity gradient is identical to the true velocity gradient multiplied by $\tan(\alpha)$. If the inclination changes from $20^\circ$ to $70^\circ$, the true velocity gradient can vary by a factor of 2.7 to 0.4 of the observed velocity gradient. Therefore it is possible that the relatively large velocity gradient inferred in F4 may not be true in reality but appears to be so as a result of the projection effect.

Kirk et al. (2013) have estimated the accretion mass of the filament to the stellar cluster in Serpens South with the following equation by assuming that the filament would have a simple cylindrical shape with mass $M$, length $L$, radius $r$, and velocity $V_l$, along the filament long axis:

$$M_l = V_l \times (M / \pi r^2 L) \times (\pi r^2)$$

(4)

$$= V_l \times (M / L).$$

With the inclination angle $\alpha$ of the filament to the plane of the sky, $L_{\text{obs}} = L \cos(\alpha)$ and $V_{l,\text{obs}} = V_l \sin(\alpha)$, and $V_{l,\text{obs}} = \nabla V_{l,\text{obs}} \times L_{\text{obs}}$. Then the mass accretion rate becomes

$$M_l = \nabla V_{l,\text{obs}} \times M \times \tan^{-1}(\alpha).$$

(5)

Using this equation, we attempted to estimate the mass accretion rate from the filament to the cores C3, C11, C15, and C17, located in the hubs of HFSs where converging flows can be seen. However, a direct application of Equation (5) using the total mass and global velocity gradient of the filament is not straightforward, as there are multiple dense cores in filament F4. For example, a large velocity gradient can be seen along F4h to core C3. However, there is a core, C2, in the middle of F4h, and the global velocity gradient, mass, and length of F4h are not appropriate to measure the mass accretion rate from F4h to C3. Therefore, we carefully examined the systemic motions along with the filament’s skeleton. We selected a local area of filament at which filament gas material possibly flows to the cores. For C3, the accretion rates are calculated along F4g, F4e, and F4h. For C11, although it is not large, the velocity gradients are found along F4a and F4e, and the mass accretion rates are derived for both directions. Accretion rates for C15 are estimated from the areas of F4a and F4d. C16 and C17 are located quite close to each other, and the mass accretion rate is measured from F4b and F4a, respectively. We have limited the filament area to an area where the velocity gradient is visible but seemingly related to the cores only in the hub-like region. The filament areas that we use are shown by arrows in the top panel of Figure 22 in the Appendix.

We applied the mean gas density of the local area for $M / \pi r^2 L$ in Equation (4) to estimate the local accretion rates for cores. Assuming that the thickness of a filament along the line of sight is equal to its width, the mean gas density of the ith filament area becomes $\bar{\rho} = N_{\text{H}_2,i}/W_i$ where $N_{\text{H}_2,i}$ and $W_i$ are the mean H$_2$ column density and the width of the ith filament. Then, the mass accretion rate from the ith filament area to the core can be estimated from the equation

$$M_{l,i} = \frac{\pi}{4} \nabla V_{l,\text{obs},i} \times \bar{\rho}_i \times L_i / W_i^2 \tan(\alpha),$$

(6)

where $\nabla V_{l,\text{obs},i}$ and $L_i$ are the observed velocity gradient and length of the ith filament area. $\nabla V_{l,\text{obs},i}$ is derived from a linear least-squares fit for the systemic velocities along with the filament skeleton. The region where the velocity gradient is estimated with this fit is drawn with a green line in the bottom panel of Figure 22 in the Appendix. The accretion time, $t_{\text{acc}} = M_{\text{core}} / \Sigma M_{l,i}$, is calculated to compare with the freefall time $t_{\text{ff}} = \sqrt{3\pi/32G\rho_0}$. The results are given in Table 4.
similar to those found for the Serpens South filament (28 $M_{\odot}$ Myr$^{-1}$; Kirk et al. 2013) and smaller than that of the Monoceros R2 filaments (70 $M_{\odot}$ Myr$^{-1}$; Treviño-Morales et al. 2019). C3 is placed at the hub of the western-HFS, and the mass accretion rate of $35 M_{\odot}$ Myr$^{-1}$ is comparable to that of Serpens South. The timescales to collect the current core mass via accretion flows from filaments are found to be 0.2 to 0.8 Myr. Though longer than the freefall time of $\sim$0.3 Myr, this is consistent with the lifetime of YSOs within the uncertainty. It is reported that the global lifetime of the prestellar core phase is $1.2 \pm 0.3$ Myr (Könnyves et al. 2015). The lifetimes of Class I and Class II are known to be around 0.5 Myr and 1 Myr, respectively (see Evans et al. 2009, and references therein). Hence, the accretion time of the cores is roughly in agreement with the time for the formation of YSOs and prestellar cores in the filaments. In conclusion, it is likely that the accretion flow from the filaments to the cores in IC 5146 plays a significant role in the star-forming processes in IC 5146.

6.4. Filaments in the Cocoon Nebula

The Cocoon Nebula and the Streamer have been investigated together due to their proximity in the plane of the sky (e.g., Lada et al. 1994; Johnstone et al. 2017; Wang et al. 2017). However, the distances of the Cocoon and the Streamer are known to be quite different. Our observations of the C$^{18}$O (1–0) line indicate that the velocity range of the Cocoon Nebula (6–9 km s$^{-1}$) also differs from that of the Streamer (1–7 km s$^{-1}$). Besides, the Cocoon and the Streamer have significantly different star formation environments. The Cocoon Nebula has $\sim$100 YSOs, while the Streamer has $\sim$20 (Harvey et al. 2008). Also, there is a massive B-type star BD+46$^\circ$ 3474 at the center of the Cocoon Nebula (Herbig & Reipurth 2008). Hence, comparing the physical properties of filaments in the Cocoon and in the Streamer would be meaningful. In this section, we compare the physical properties of filaments in the Cocoon Nebula with those in the Streamer, focusing on the more evolved Cocoon Nebula.

In the Cocoon Nebula region, five filaments are identified (F10–F14). Only one dense core is detected in the Cocoon Nebula, while a few tens of dense cores are found in the filaments associated with the Streamer. There is no significant difference found between the filaments identified with the Cocoon Nebula and those with the Streamer in terms of their physical properties such as H$_2$ column density and mass per unit length ($M_{\text{line}}$). The H$_2$ column density ranges between 2.5 and $6.1 \times 10^{21}$ cm$^{-2}$ in the Cocoon filaments and between 2.2 and $8.8 \times 10^{21}$ cm$^{-2}$ in the Streamer filaments. The Cocoon filaments have $M_{\text{line}}$ of $\sim$25–68 $M_{\odot}$ pc$^{-1}$, and the Streamer filaments have $M_{\text{line}}$ of $\sim$19–115 $M_{\odot}$ pc$^{-1}$. The critical value of mass per unit length at which thermal pressure can support the gravitational contraction is $\sim$32 $M_{\odot}$ pc$^{-1}$ at 23 K for the Cocoon’s filaments and $\sim$20 $M_{\odot}$ pc$^{-1}$ at 15 K for the Streamer’s filaments (Ostriker 1964).

F10, F11, and F14 in the Cocoon have smaller $M_{\text{line}}$ than $M_{\text{crit}}$, and thus they are seemingly thermally supported and no dense cores form. The filament F12 where a small N$_2$H$^+$ dense core is detected has $M_{\text{line}}$ of $\sim$36 $M_{\odot}$ pc$^{-1}$, similar to the critical $M_{\text{line}}$ within the uncertainty. F13 has an effective critical $M_{\text{line}}$ of $71 \pm 24$ $M_{\odot}$ pc$^{-1}$. The observed mass per unit length of F13 is $\sim$68 $M_{\odot}$ pc$^{-1}$, hence, F13 is gravitationally supercritical but devoid of any dense cores. One possible explanation for F13 not forming dense cores despite being physically supercritical is that its dynamical state may be controlled by other means of support such as turbulence and/or magnetic field that are not considered here. However, the nonthermal velocity dispersions show that the filaments associated with the Cocoon Nebula have subsonic or transonic turbulent motions, while those associated with the Streamer are transonic or supersonic. Hence, we tentatively conclude that the thermal pressure and magnetic field rather than the turbulence may be more important in filaments of the Cocoon Nebula than in filaments of the Streamer.

The roles of gravity, turbulence, and magnetic field may change along with the formation and evolution of filaments and cores. The models of clouds and star formation suggest that the magnetic field and turbulence may play different roles at different stages of evolution (e.g., Crutcher 2012). Besides, the types of clumps that evolve can be affected by the balance of the three factors. It has recently been suggested that the subtle difference in the relative significance between gravity, turbulence, and magnetic field can produce different fragmentation from the clump to the core scale.

| C3-F4g | 1.5 ± 0.1 | 26 ± 10 | 35 ± 11 | 0.7 ± 0.2 | 0.3 |
|--------|----------|--------|--------|----------|---|
| C3-F4e | 0.5 ± 0.1 | 4 ± 1 | 0.2 ± 0.1 | 0.3 |
| C3-F4h | 0.9 ± 0.1 | 6 ± 3 | 0.3 ± 0.1 | 0.3 |
| C11-F4a | 0.6 ± 0.1 | 12 ± 5 | 15 ± 5 | 0.4 ± 0.1 | 0.3 |
| C11-F4e | 0.3 ± 0.1 | 3 ± 1 | 19 ± 6 | 0.2 ± 0.1 | 0.3 |
| C15-F4a | 1.0 ± 0.1 | 10 ± 5 | 5 ± 2 | 0.2 ± 0.1 | 0.3 |
| C15-F4d | 0.2 ± 0.1 | 5 ± 2 | 26 ± 14 | 0.8 ± 0.4 | 0.2 |
| C16-F4b | 0.7 ± 0.1 | 5 ± 2 | 26 ± 14 | 0.8 ± 0.4 | 0.2 |
| C17-F4a | 0.7 ± 0.1 | 20 ± 14 | 26 ± 14 | 0.8 ± 0.4 | 0.2 |

Notes.

$^a$ The mass accretion rates and the total mass accretion rates from filaments to the cores are given assuming $\tan(\alpha) = 1$ (i.e., the inclination angle $\alpha = 45^\circ$) for all filaments. The real accretion rate should be divided by $\tan(\alpha)$, and the accretion rate can vary by a factor of 2.7–0.4 between inclination angles of 20$^\circ$ and 70$^\circ$.

$^b$ The accretion time is the time taken to gather the current core mass through the accretion flow from the filaments, i.e., $t_{\text{acc}} = M_{\text{core}}/\sum M_{\text{fil}}$.

$^c$ The freefall time, $t_{ff} = \sqrt{3 \pi / 32 G M_{\odot}}$.

$^d$ F4aE and F4aW refer to the eastern and western filament regions of C15.

$^e$ The accretion time is measured for the total mass of C16 and C17.

Table 4

| $\nabla V_{\text{obs}}$ (km s$^{-1}$ pc$^{-1}$) | $M_{\odot}$ (Myr$^{-1}$) | $\sum M_{\text{fil}}$ (Myr$^{-1}$) | $t_{\text{acc}}$ (Myr) | $t_{\text{ff}}$ (Myr) |
|-----------------|----------------|-----------------|----------------|----------------|
| C3-F4g          | 1.5 ± 0.1      | 26 ± 10         | 35 ± 11        | 0.7 ± 0.2      | 0.3 |
| C3-F4e          | 0.5 ± 0.1      | 4 ± 1           | 0.2 ± 0.1      | 0.3 |
| C3-F4h          | 0.9 ± 0.1      | 6 ± 3           | 0.2 ± 0.1      | 0.3 |
| C11-F4a         | 0.6 ± 0.1      | 12 ± 5          | 15 ± 5         | 0.4 ± 0.1      | 0.3 |
| C11-F4e         | 0.3 ± 0.1      | 3 ± 1           | 19 ± 6         | 0.2 ± 0.1      | 0.3 |
| C15-F4aE$^d$    | 1.0 ± 0.1      | 10 ± 5          | 5 ± 2          | 0.2 ± 0.1      | 0.3 |
| C15-F4aW$^d$    | 0.3 ± 0.1      | 5 ± 2           | 26 ± 14        | 0.8 ± 0.4      | 0.2 |
| C15-F4d         | 0.2 ± 0.1      | 5 ± 2           | 26 ± 14        | 0.8 ± 0.4      | 0.2 |

19
Table 5
Evolution Indicators of Starless Dense Cores

| Core ID | \(N(N_2H^+)\) \((10^{12}\text{ cm}^{-2})\) | \(\Delta V(N_2H^+)\) \((\text{km s}^{-1})\) | \(f_{\text{de}}(\text{CO})\) | \(N(\text{H}_2)\) \((10^{20}\text{ cm}^{-2})\) | Det(SO) | Infall Asy. | Total |  
|--------|-----------------|-----------------|---------------|------------------------|---------|-------------|-------|
| C2     | 0.97 (1)        | 0.49 (1)        | 1.1 (1)       | 108.1 (1)              | Y (0)   | Y (1)       | 5     |
| C5     | 0.95 (1)        | 0.31 (0)        | 0.9 (0)       | 65.5 (0)               | N (1)   | N (0)       | 2     |
| C6     | 0.68 (0)        | 0.47 (0)        | 1.1 (1)       | 73.9 (1)               | Y (0)   | Y (1)       | 3     |
| C8     | 1.01 (1)        | 0.47 (0)        | 1.0 (0)       | 56.0 (0)               | N (1)   | N (0)       | 2     |
| C10    | 0.82 (0)        | 0.45 (0)        | 0.5 (0)       | 55.7 (0)               | N (1)   | N (0)       | 1     |
| C12    | 0.88 (0)        | 1.62 (1)        | 0.7 (0)       | 86.3 (1)               | Y (0)   | N (0)       | 2     |
| C13    | 0.75 (0)        | 0.78 (1)        | 1.0 (0)       | 64.9 (0)               | Y (0)   | N (0)       | 1     |
| C16    | 2.29 (1)        | 0.57 (1)        | 1.3 (1)       | 166.2 (1)              | Y (0)   | Y (1)       | 5     |

Notes. These physical parameters provide the evolutionary status of starless dense cores (Crapsi et al. 2005). Columns numbered (1)–(6) show \(N(N_2H^+)\) column density \((N(N_2H^+))\), \(N_2H^+\) line width \((\Delta V(N_2H^+))\), CO depletion factor \((f_{\text{de}}(\text{CO}))\), \(\text{H}_2\) column density at the peak position \((N(\text{H}_2))\), the detection of SO emission \((\text{Det(SO)})\), and infall asymmetry of the HCO\(^+\) spectrum (Infall Asy.). Det(SO) indicates whether the SO line was detected above its 3\(\sigma\) level. Each number in parentheses is the point given for each parameter of each core if its property is ranked to mean that it is more evolved than the average for that property among the cores.

The total is sum of points, and a larger total means that the core is more evolved.

(Tang et al. 2019). To investigate the precise roles of gravity, turbulence, and magnetic field in forming stars, more observational constraints, particularly observations of polarization, are required. The filaments in Cocoon are interesting targets in which to investigate the precise roles played by gravity, turbulence, and magnetic field in their formation and evolution. Further investigations on the importance of magnetic field relative to gravity and turbulence will be given in our next paper (E. J. Chung et al. 2021, in preparation).

6.5. Formation of Filaments and Dense Cores in the Streamer

This section discusses possible roles of the filamentary structures in the formation and evolution of filaments and dense cores. Most of the filaments in the Streamer are gravitationally supercritical, and the kinematic properties of filaments and dense cores imply that the mechanisms forming filaments and dense cores can differ depending on the environment of each filament. We have found 21 dense cores with the \(N(\text{H}_2)\) \((1–0)\) line in the Streamer, and investigating the relative evolutionary stages of the cores may help in understanding the possible formation history of the Streamer.

Observations toward the starless cores found that dynamical and chemical properties such as line width, inward motion, and depletion of C-bearing molecules, yet enhancement of deuterated species in the dense cores, can be used as indicators of the evolution of cores. In particular, Crapsi et al. (2005) examined dynamical and chemical properties of several tens of starless cores, and found that the most evolved cores have higher \(N(\text{H}_2)\), \(N_2\text{D}^+\), and \(\text{H}_2\) column densities, a higher ratio of \(N(N_2\text{D}^+)\) to \(N(N_2\text{H}^+)\), higher CO depletion factor \((f_{\text{de}}(\text{CO}))\), the ratio of the canonical CO abundance to the observed CO abundance, larger \(N_2\text{H}^+\) line width with infall signature, and more compact density distribution than the others.

Adopting the indicators provided by Crapsi et al. (2005), we investigated the relative evolutionary status of eight starless cores in IC 5146. Table 5 shows the available quantities of \(N(\text{H}_2)\) column density, \(N_2\text{H}^+\) \((1–0)\) line width, CO depletion factor, and \(\text{H}_2\) column density at the peak position of \(N_2\text{H}^+\) \((1–0)\) emission for the eight starless cores. We used the canonical CO abundance \((N_{\text{CO}}/N(\text{H}_2))\) of \(9.1 \times 10^{-5}\) from Pineda et al. (2010), and derived the observed CO abundance from the CO column density and \(\text{H}_2\) column density obtained in Section 4.2. We included one more factor, i.e., the detection of SO \((3_2–2_1)\) over 3\(\sigma\), as an evolution indicator for the cores in our discussion. We gave one point for each parameter of each of the cores and summed the points to get a total. A larger sum of points implies that that core is relatively more evolved. Among the eight starless cores, C2 and C16 secured the highest sums, implying that they are the most evolved starless cores, while C10 and C13 appear to be the least evolved cores.

Figure 14 shows the distribution of dense cores that are color-coded based on their relative evolutionary stage. The cores with YSOs are located in the supersonic filaments and hubs of HFSs while most of the starless cores are found in single-shaped, transonic filaments. This indicates that the filamentary accretion flow as well as turbulent gas motions in the filament may play an important role in the formation of dense cores and stars.

Seo et al. (2019) investigated the kinematics and chemistry of star-forming regions in the Taurus molecular cloud, and proposed three star formation types, i.e., fast, slow, and isolated modes, depending on the filamentary structures involved in the star formation. The fast mode may apply for star formation at the hub where the column density is high. The converging flow from filaments to the hub and ram pressure may promote mass accretion and the formation of the cores and stars. The slow mode would work for the formation of stars at a gravitationally supercritical filament as well as the formation of pressure-confined cores at a gravitationally subcritical filament. The isolated mode is the classical mode of star formation where cores and stars form in isolated clumps by gravitational contraction.

We note that the cores with YSOs and starless cores in IC 5146 can be explained well by these modes. The formation of dense cores and YSOs in C3, C11, C15, and C17 in hubs of IC 5146 seems consistent with the suggested fast mode. On the other hand, the starless core C6 seems to be controlled by a slow mode because it is located in a single-shaped filament (F2). C18, the dense core linked with a clump, but not with a filament, seems to be a case of the isolated mode.

Meanwhile, sub-filaments not located in hubs of F4 harbor both cores with YSOs and cores without. The starless cores C2, C5, C8, C10, C12, C13, and C16 are embedded between or next to the dense cores with YSOs. This seems to be because when a chain of cores forms in a filament, a core having a deeper gravitational potential well grows first, and then the adjacent less massive core gains mass slowly.
7. Summary and Conclusion

We carried out mapping observations of the clouds and dense cores in IC 5146 in molecular lines with the TRAO 14 m antenna to investigate how stars form in relation to filamentary structures in IC 5146. The main results of our observations are as follows.

1. From C$^{18}$O (1–0) data, 14 filaments (size $\geq 6 \times \theta_{\text{FWHM}}$) and 30 clumps (size $\leq 4 \times \theta_{\text{FWHM}}$ and aspect ratio $\leq$3) are identified by performing a Gaussian decomposition for the observed spectra and a friends-of-friends algorithm for the decomposed Gaussian components. The basic physical quantities of the filaments such as $H_2$ column density, length, width, mass, mass per unit length, and mean velocity gradient are estimated.

2. From N$_2$H$^+$ (1–0) data, 22 dense cores (21 in the Streamer and 1 in the Cocoon Nebula) are found. Among the 22 dense cores, 14 are found to have YSOs while the other cores that are identified for the first time in this study are starless. Their positions, sizes, peak velocities, line widths, masses, and virial parameters are derived.

3. We compared the identified C$^{18}$O filaments with the Herschel continuum filaments found in the dust continuum emission (Arzoumanian et al. 2011). In some cases, filaments seen as a single entity in the continuum observations are found to consist of multiple filaments of different systemic velocities in our C$^{18}$O (1–0) map. This indicates that our observations of molecular lines are useful for extracting velocity coherent structures from those having multiple velocities that are spatially overlapped and hence would have been treated as a single filament based on the continuum maps alone.

4. Based on the comparison of nonthermal velocity dispersions derived from C$^{18}$O and N$_2$H$^+$ (1–0), we divided the dense cores into two groups: one where the nonthermal velocity dispersions of the filaments and dense cores are nearly the same, and the other where the nonthermal velocity dispersions of the dense cores are smaller than those of the filaments. Among the dense cores in the latter group, three located in hubs show a different systemic velocity from that of filament material. This agrees with what the collision model of turbulent flows predicts in the formation of the filaments and the dense cores. Hence, we propose that the hubs and dense cores in them may have been formed through the collision of turbulent flows.

5. Most of the filaments in IC 5146 have a larger mass per unit length ($M_{\text{line}}$) than the critical $M_{\text{line}}$ within the uncertainty, and hence they are gravitationally supercritical. Most of the dense cores are found on the supercritical filaments, but four are found in the subcritical filaments. Only one dense core is found to be in a virialized small clump.

6. Every filament shows a continuously coherent velocity field, and its velocity gradient is on average $\leq 1.1$ km s$^{-1}$ pc$^{-1}$. F4, the largest filament with most of the dense cores in IC 5146, shows the largest velocity gradient, up to about $2-3$ km s$^{-1}$ pc$^{-1}$. We estimate accretion rates of $\sim 15-35 M_\odot$ Myr$^{-1}$ from filaments onto the cores in the filaments where the velocity gradients were measured. The timescales to gain current core masses via the accretion flow are $\sim 0.2-0.8$ Myr, which is consistent with the timescales of the YSOs formed in IC 5146. This suggests that the accretion flows along the filaments may have played a significant role in the formation of stars in IC 5146.

7. The formation processes of dense cores and stars found in the filaments of IC 5146 appear to be well explained based on the three modes suggested by Seo et al. (2019)—the fast, slow, and isolated modes. The cores with YSOs tend to be located in the turbulent hubs, and hence might have been formed in the fast mode, while starless cores located on the transonic single-shaped filaments might be currently forming in a slow mode. One dense core embedded in the clump CL22 is likely to have formed by the isolated mode.

We appreciate the referee and the editor for the valuable comments and suggestions. This work was supported by the National Research Foundation of Korea (NRF) grant funded by the Korea government (MSIT) (No. NRF-2019R1I1A1A01042480) and the Basic Science Research Program through the NRF funded by the Ministry of Education, Science and Technology (NRF-2019R1A2C1010851). K.H.K. is supported by the center for Women In Science, Engineering and Technology (WISET) grant funded by the Ministry of Science and ICT (MSIT) under the program for returners into R&D (WISET-2019-288; WISET-2020-247; WISET-2021-080). A.S. acknowledge the support from the NSF through grant AST-1715876.

Appendix

We present the moment 0 maps and position–velocity diagrams of $^{13}$CO and C$^{18}$O (Figure 15), derivation of $H_2$ column density from C$^{18}$O emission and N$_2$H$^+$ core mass (Sections A.1 and A.2, respectively), the integrated intensity maps of N$_2$H$^+$, SO, and C$^{18}$O and the averaged spectra of SO, CS, HCO$^+$, and N$_2$H$^+$ isolated component of each N$_2$H$^+$ core (Figures 16–20), C$^{18}$O spectra and the Gaussian decomposition results around C17 (Figure 21), the systemic velocity map of filament F4 (Figure 22), and the physical properties of C$^{18}$O clumps (Table 6).
Figure 15. The integrated intensity maps (top) and the position–velocity cuts along the white solid line in the integrated intensity maps (bottom) of $^{13}$CO and C$^{18}$O (1–0) emissions, respectively. The $p$–$v$ diagrams are averaged within the regions of white dotted lines in the integrated intensity maps. The yellow dashed lines indicate R.A. (J2000) of $21^h50^m 31.5^s$, which separates the Cocoon Nebula and the Streamer as in Figure 1. The white arrow in the C$^{18}$O $p$–$v$ diagram indicates the F2 emission, which has quite a different velocity from F4’s velocity.
Figure 16. Images: integrated intensity contour maps of N$_2$H$^+$ (1–0) (left), SO (3$_2$–2$_1$) (second column), and C$^{18}$O (1–0) (third column) on the Herschel 250 μm image toward the dense cores C1 to C4. The contour levels are $3n \times \sigma$ ($n = 1, 2, 3, \ldots$). The red cross and ellipse indicate the peak position and the size of the N$_2$H$^+$ dense core. The black crosses represent the positions of YSO candidates (Harvey et al. 2008; Poglitsch et al. 2010). The FWHM beam sizes at the N$_2$H$^+$, SO, and HCO$^+$ frequencies are shown with white circles in the upper right corner. Spectra: the averaged SO (3$_2$–2$_1$), CS (2–1), HCO$^+$ (1–0), and N$_2$H$^+$ isolated component (1$_{0,2}$–0$_{1,2}$) spectra of each dense core are presented in magenta, green, navy, and red, respectively. N$_2$H$^+$ spectra are presented with hyperfine fitting results (maroon lines). The spectrum drawn with the sky-blue line is representative of the blue asymmetric HCO$^+$ spectrum at the offset position from the core center (in the parenthesis).
Figure 17. Same as Figure 16 for C5 to C9.
Figure 18. Same as Figure 16 for C10 to C14.
Figure 19. Same as Figure 16 for C15 to C19.
Figure 20. Same as Figure 16 for C20 to C22.
Figure 21. $^{18}$O (1–0) spectra around C17. The ranges of the velocity and intensity are given by the lower left box in km s$^{-1}$ and in K[T$_A^*$/], respectively. The red polygon indicates C3. The yellow and red lines are the decomposed Gaussian components of F4 and F6, respectively.
Figure 22. Top: systemic velocity map of filament F4. The skeleton is drawn with the dotted line and dense cores with triangles. Large triangles indicate dense cores (C3, C11, C15, and C17), which seem to form in a hub-like structure. The possible mass flows near the cores are depicted with the arrows. Bottom: systemic velocities along the filament F4. To emphasize the velocity gradient along filaments to cores, velocity distributions of several sub-filaments are plotted together. The offset of \( \pm 1.2 \) km s\(^{-1}\), indicated with the dotted red lines, is given for \( V_{\text{sys}} \) of F4b, F4d, and F4e to avoid overlaps of data points. The green lines indicate the linear least-squares fit of filament components from which the velocity gradient along the filament to the dense cores is estimated.
\[ N = \frac{3k_B}{8\pi^2B\mu^2} \frac{e^{hBJ(J+1)/k_BT_\text{ex}}}{J+1} \frac{T_\text{ex} + \frac{hB}{3k_B}}{1 - e^{-hB/T_\text{ex}}} \int \tau dv, \tag{A1} \]

where \( B \) is the rotational constant, \( \mu \) is the permanent dipole moment of the molecule, \( J \) is the lower rotational level, and \( T_\text{ex} = h/\mu k_B \) is the excitation temperature.

The rightmost integration of \( \tau \), the optical depth of the line, can be calculated following (Pattle et al. 2015)

\[ \int \tau(v) dv = \frac{1}{J(T_\text{ex}) - J(T_\text{bg})} \int \frac{\tau(v)}{1 - e^{-\tau(v)}} T_\text{mb} dv \approx \frac{1}{J(T_\text{ex}) - J(T_\text{bg})} \int \frac{\tau(v_0)}{1 - e^{-\tau(v_0)}} T_\text{mb} dv, \tag{A2} \]

where \( J(T) \) is the equivalent Rayleigh–Jeans temperature function, \( J(T) = T_0/(e^{J(v)/T_0} - 1) \), and \( T_\text{ex} \) and \( T_\text{bg} \) are the excitation temperature, for which we used dust temperature obtained from Herschel dust continuum emission, and the cosmic microwave background temperature, respectively. \( v_0 \) is the central velocity, and the optical depth at the central velocity

is derived with the abundance ratio of \( [^{13}\text{CO}/^{18}\text{O}] = 5.5 \) (Freking et al. 1982) and the relation

\[ \frac{T_{\text{CO}^{18}\text{O},\text{max}}}{T_{\text{CO},\text{max}}} = \frac{1 - e^{-\tau_{^{13}\text{CO}}}}{1 - e^{-\tau_{^{18}\text{O}}}}, \tag{A3} \]

where \( T_{\text{CO}^{18}\text{O},\text{max}} \) and \( T_{\text{CO},\text{max}} \) are the maximum intensities of \(^{18}\text{O}\) and \(^{13}\text{CO} \) (1−0), respectively. \( T_\text{mb} \) is the observed main beam temperature of the line. The area under the fitted Gaussian function is used for \( \int T_{\text{mb}}dv \), because multiple velocity components in the line of sight are slightly overlapped along the velocity directions.

H\(_2\) column density \( (N_{\text{H}_2}) \) is derived from \(^{18}\text{O}\) column density \( (N_{\text{CO}^{18}\text{O}}) \) with the abundance ratios of \( [^{13}\text{CO}/^{18}\text{O}] = 5.5 \) (Freking et al. 1982) and \( [^{12}\text{CO}/^{13}\text{CO}] = 69 \) (Wilson 1999) and the conversion factor of \( N_{\text{H}_2}/N_{\text{CO}^{13}\text{CO}} = 1.1 \times 10^4 \) (Pineda et al. 2010).

We compare the derived \( N_{\text{H}_2} \) with that of the Herschel data (André et al. 2010; Arzoumanian et al. 2011) in Figure 23. They are linearly correlated, and \( N_{\text{H}_2}^{\text{CO}^{13}\text{CO}} \) appears slightly smaller than \( N_{\text{H}_2}^{\text{Herschel}} \) on average but matches well within the range of uncertainty. The abundance for \( N_{\text{H}_2}^{\text{CO}^{13}\text{CO}} \) to be best matched with \( N_{\text{H}_2}^{\text{Herschel}} \) for IC 5146 would be 0.8 \pm 0.2 for the Cocoon region and 0.7 \pm 0.3 for the Streamer region. This is mostly due to the use of standard conversion factors of \( [^{12}\text{CO}/^{13}\text{CO}] \) and \( N_{\text{H}_2}/N_{\text{CO}^{13}\text{CO}} \). We corrected the \( \text{H}_2 \) column density by factors
of 0.8 and 0.7 for the Cocoon and the Streamer, respectively, and estimated the masses of filaments and clumps.

A.2. Mass and Virial Mass of Dense Cores

The masses of dense cores are calculated with N$_2$H$^+$ (1–0) molecular line data. First, total column density of N$_2$H$^+$ is derived using the equation of Caselli et al. (2002):

$$ N = \frac{8\pi W g_l}{\Lambda A} \frac{1}{g_u J(T_{ex}) - J(T_{bg})} \times \frac{Q_{rot}}{1 - \exp(-h\nu/kT_{ex}) g_l \exp(-E_l/kT_{ex})}, $$

(A4)

where $W$ is the integrated intensity of N$_2$H$^+$ (1–0) emission, $A$ is the Einstein coefficient, $g_l$ and $g_u$ are the statistical weights of the lower and upper levels, and $Q_{rot}$ is the partition function. H$_2$ column density is estimated from the N$_2$H$^+$ column density with the average abundance of N$_2$H$^+$ of 6.8 (± 4.8) × 10$^{-10}$ (Johnstone et al. 2010; Lee & Myers 2011). The most uncertain factors for dense core mass are the excitation temperature and the conversion factor between the column densities of N$_2$H$^+$ and H$_2$, but the uncertainty caused by these factors is claimed to be less than a factor of 2 (Johnstone et al. 2010).

The virial mass ($M_{vir}$) for a spherical dense core is estimated as

$$ M_{vir} = kR\sigma_{tot}^2/G, $$

(A5)

where $R$ is the radius of the core and $\sigma_{tot}$ is the total velocity dispersion of the mean molecular weight ($\mu = 2.8$) averaged over the core. Assuming the density profile of $\rho \propto R^{-2}, k = 1$ is applied. For the virial mass of clumps, the effective radius, the radius of a circle that has the same area as the clump, is applied (Table 6). With the assumption of the density profile of $\rho \propto R^{-2}$ where $R$ is the radius, $k = 1$ is used.

**ORCID iDs**

Eun Jung Chung © https://orcid.org/0000-0003-0014-1527
Chang Won Lee © https://orcid.org/0000-0002-3179-6334
Shinyoung Kim © https://orcid.org/0000-0001-9333-5608

Mario Tafalla © https://orcid.org/0000-0002-2569-1253
Paola Caselli © https://orcid.org/0000-0003-1481-7911
Philip C. Myers © https://orcid.org/0000-0002-2885-1806
Tie Liu © https://orcid.org/0000-0002-5286-2564
Hyunjoo Yoo © https://orcid.org/0000-0002-8578-1728
Kyoung Hee Kim © https://orcid.org/0000-0001-9597-7196
Mi-Ryang Kim © https://orcid.org/0000-0002-1408-7747
Archana Soam © https://orcid.org/0000-0002-6386-2906
Jungyeon Cho © https://orcid.org/0000-0003-1725-4376
Woojin Kwon © https://orcid.org/0000-0003-4022-4132
Hyunwoo Kang © https://orcid.org/0000-0001-9317-7646

References

André, P., Di Francesco, J., Ward-Thompson, D., et al. 2014, in Protostars and Planets VI, ed. H. Beuther et al. (Tucson, AZ: Univ. Arizona Press), 27
André, P., Men’shchikov, A., Bontemps, S., et al. 2010, A&A, 518, L102
Arzoumanian, D., André, P., Didelon, P., et al. 2011, A&A, 529, L6
Arzoumanian, D., André, P., Könyves, V., et al. 2019, A&A, 621, A42
André, P., Peretto, N., & Könyves, V. 2013, A&A, 553, A119
Bailer-Jones, C. A. L., Rybizki, J., Fouesneau, M., Demleite, M., & André, R. 2021, AJ, 161, 147
Bailer-Jones, C. A. L., Rybizki, J., Fouesneau, M., Mantelet, G., & André, R. 2018, AJ, 156, 58
Ballesteros-Paredes, J., Hartmann, L., & Vázquez-Semadeni, E. 1999, ApJ, 527, 285
Barnes, A. T., Henshaw, J. D., Caselli, P., et al. 2018, MNRAS, 475, 5268
Baugh, T., Dewangan, L. K., Ohja, D. K., et al. 2018, ApJ, 852, 119
Bergin, E. A., Alves, J., Huard, T., & Lada, C. J. 2002, ApJL, 570, L101
Berry, D. S. 2015, A&C, 10, 22
Caselli, P., Myers, P. C., & Thaddeus, P. 1995, ApJL, 455, L77
Caselli, P., Walmsley, C. M., Tafalla, M., Dore, L., & Myers, P. C. 1999, ApJL, 523, L165
Caselli, P., Walmsley, C. M., Zucconi, A., et al. 2002, ApJ, 565, 344
Chung, E. J., Lee, C. W., Kim, S., et al. 2019, ApJ, 877, 114
Clarke, S. D., Whitworth, A. P., Spowage, R. L., et al. 2018, MNRAS, 479, 1722
Crapsi, A., Caselli, P., Walmsley, C. M., et al. 2005, ApJ, 619, 379
Crapsi, A., Caselli, P., Walmsley, M. C., & Tafalla, M. 2007, A&A, 460, 221
Crutcher, R. M. 2012, ARA&A, 50, 29
Dhabal, A., Mundy, L. G., Rizzo, M. J., Storm, S., & Teuben, P. 2018, ApJ, 853, 169
Dobashi, K., Yonekura, Y., & Hayashi, Y. 2001, PASJ, 53, 811
Dzib, S. A., Loinard, L., Ortiz-León, G. N., Rodríguez, L. F., & Galli, P. A. B. 2018, ApJ, 867, 151

Figure 23. Comparison of $N_{H_2}$ derived from C$^{18}$O (1–0) with that from the Herschel data (André et al. 2010; Arzoumanian et al. 2011). The cyan and red dots are for F2 and F8, respectively. The thin solid gray line shows where $N_{H_2}^{C^{18}O}$ and $N_{H_2}^{Herschel}$ are identical, and the two dashed lines indicate where the ratio of $N_{H_2}^{C^{18}O} / N_{H_2}^{Herschel}$ is 10 and 0.1. The least-squares fit result is shown as a thick solid line.
