Fermi-Surface Topological Phase Transition and Horizontal Order-Parameter Nodes in CaFe$_2$As$_2$ Under Pressure

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Iron-based compounds (IBS) display a surprising variety of superconducting properties that seems to arise from the strong sensitivity of these systems to tiny details of the lattice structure. In this respect, systems that become superconducting under pressure, like CaFe$_2$As$_2$, are of particular interest. Here we report on the first directional point-contact Andreev-reflection spectroscopy (PCARS) measurements on CaFe$_2$As$_2$ crystals under quasi-hydrostatic pressure, and on the interpretation of the results using a 3D model for Andreev reflection combined with ab-initio calculations of the Fermi surface (within the density functional theory) and of the order parameter symmetry (within a random-phase-approximation approach in a ten-orbital model). The almost perfect agreement between PCARS results at different pressures and theoretical predictions highlights the intimate connection between the changes in the lattice structure, a topological transition in the holelike Fermi surface sheet, and the emergence on the same sheet of an order parameter with a horizontal node line.

The picture of a superconducting pairing mediated by spin fluctuations (SF) in iron-based compounds (IBS) is justified by the proximity of superconductivity to an antiferromagnetic (AFM) state$^1$ characterized by a $\left(\pi, \pi\right)$ ordering wavevector that connects holelike and electronlike sheets of the Fermi surface (FS). This mechanism, which would lead to the so-called $s^{\pm}$ symmetry of the OP$^2$, has been questioned by the discovery of superconducting compounds with only electronlike or holelike FS, such as FeSe monolayers on SrTiO$_3$$^3$, KFe$_2$As$_2$$^4$$^5$, K$_{0.8}$Fe$_{1.7}$Se$_2$$^6$.

The disappearance of a FS sheet (Lifshitz transition) was also found in CaFe$_2$As$_2$. When cooled at ambient pressure, CaFe$_2$As$_2$ shows a tetragonal (T) to orthorhombic (OR) structural transition, accompanied by the paramagnetic (PM) to AFM transition. Under moderate pressure, a tetragonal (T) to collapsed tetragonal (cT) transition occurs on cooling$^7$$^8$. In the cT phase, stable at low temperature under hydrostatic pressure, the out-of-plane lattice constant is shorter by 10% than in the T phase; angle-resolved photoemission spectroscopy (ARPES)$^9$, transport and Seebeck measurements$^{10}$ as well as Density Functional Theory (DFT) calculations$^{11}$ concur to indicate the absence of holelike FS around $\Gamma$. Inelastic neutron scattering experiments show no spin fluctuations$^{12$$^13}$, and indeed this phase is not superconducting$^{14}$. However, superconductivity was observed in CaFe$_2$As$_2$ under pressure$^{15}$ and ascribed to a paramagnetic "non-collapsed" tetragonal phase close to a magnetic instability$^{16}$. Such a tetragonal phase was indeed observed experimentally and stabilized by non-hydrostatic pressure$^{17}$. Pressure can thus drive CaFe$_2$As$_2$ across a structural and electronic transition that makes it bridge the gap between "usual" multiband IBS and "anomalous" single-band ones, and is associated with the emergence of a superconducting phase with a relatively high $T_c$.

To investigate the importance of the Lifshitz transition in the superconductivity of IBS and its effects on the symmetry of the OP, we designed a dedicated experimental study of the superconducting OP of CaFe$_2$As$_2$.

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as a function of the cell deformation induced by non-hydrostatic pressure. To determine the amplitude and structure of the OP, we used an energy-resolved, directional spectroscopic technique such as point-contact Andreev-reflection spectroscopy (PCARS) and interpreted the experimental results with the aid of first-principles Density Functional Theory (DFT) and Random Phase Approximation (RPA) calculations. This combined experimental/theoretical approach shows that the pressure-induced OR-cT transition is accompanied by a topological 2D-3D transition in the holelike FS, the emergence of a horizontal node line in the relevant OP, an increase in \( T_c \) and an even greater increase in the OP amplitude that suggests a considerable enhancement of the electron-boson coupling.

**Results**

**Point-contact Andreev-reflection spectroscopy.** In a PCARS experiment the differential conductance \( \frac{dI}{dV} \) of a nanometric contact between a normal metal (N) and a superconductor (S) is measured as a function of \( V \) (and \( V \) being the probe current through the contact and the voltage at the contact's ends, respectively). Under suitable conditions (in particular, if the contact diameter is smaller than the electron mean free path)\(^\text{17}\) the point contact is ballistic and hence spectroscopic, i.e. its differential conductance contains energy-resolved information about the amplitude and the symmetry of the superconducting gap thanks to the quantum phenomenon called Andreev reflection (see ref. 18 and references therein).

In the present case, the superconducting samples were CaFe\(_2\)As\(_2\) crystals (of about 2.0 × 1.5 × 0.1 mm\(^3\)) grown in Sn flux as described in ref. 19 (see Methods for details). The point contacts were made by putting a small drop of Ag paste (\( \varnothing \approx 50 \mu \text{m} \))\(^\text{19}\) on the top surface or on the side of the crystals (see Fig. 1a) – which means injecting the current preferentially along the \( c \) axis or the \( ab \) planes, respectively. Within this “soft” PCARS technique\(^\text{18}\) the contact is a parallel of nanometric junctions that can be destroyed and/or created by short current or voltage pulses\(^\text{18}\). Its resistance can thus be tuned without external mechanical action, so that we could close the crystal in a CuBe clamp cell filled with silicone oil and then pressurized (see Fig. 1c). To determine the value of the pressure \( P \) (at low \( T \)) we inductively measured the critical temperature \( T_c^{\text{crit}} \) of a small Pb rod (mounted on the sample holder, see Fig. 1b) and used the well-known \( T_c^{\text{crit}}(P) \) dependence. A uniaxial pressure component \( P_{un} \) (essential for superconductivity in CaFe\(_2\)As\(_2\))\(^\text{14,16}\) appears when the oil freezes; comparing the pressure dependence of the \( T_c \) of our crystals to the analogous curve obtained under uniaxial pressure\(^\text{17}\) leads to estimate \( P_{un} \approx 1/4 \text{ } P \).

Figure 2 reports the resistance as a function of temperature (in the region of the superconducting transition) of a CaFe\(_2\)As\(_2\) crystal under a pressure of 0.51 GPa and in the presence of a magnetic field up to 11 T. The inset to the same figure reports a subset of \( R \) vs. \( T \) curves recorded at different pressures from 0 up to 0.51 GPa, zoomed in the region of the superconducting transition. In general, the shape of the \( R(T) \) curves up to room temperature is practically identical to that reported by Torikachvili et al.\(^\text{7}\) apart from the fact that the pressures there are slightly different (indeed, they used a different pressure-transmitting medium, and the uniaxial pressure component was different).

Figures 3(a) and 3(b) show some raw PCARS spectra (\( dI/dV \) vs. \( V \) curves) measured in “\( ab \)-plane contacts” (i.e. with \( I \parallel ab \)) at different temperatures and at \( P = 0.40 \text{ GPa} \) (a) and \( P = 0.61 \text{ GPa} \) (b). The spectra in Fig. 3(c) were measured in a \( c \)-axis contact at \( P = 0.53 \text{ GPa} \). The temperature at which the spectra lose any structure and become temperature independent is the “Andreev critical temperature” \( T_c^{\text{A}} \). Its uncertainty is always of the order of ±0.5 K. As shown in Fig. 2, \( T_c^{\text{A}} \) always agrees with the critical temperature determined by transport measurements (i.e. it falls on the top of the resistive transition). The PCARS spectrum measured just above \( T_c^{\text{A}} \) (i.e. when both banks are in the normal state) will be referred to as \( (dI/dV)_{\text{NOX}} \). The insets to Fig. 3(a–c) show the low-\( T \) spectra normalized to \( (dI/dV)_{\text{NOX}} \) in such a way, only the structures associated to superconductivity in the sample are displayed.

Looking at the unnormalized curves, there are various arguments that strongly indicate the contact to be in the ballistic regime and to possess a spectroscopic character\(^\text{17}\). First of all, the spectra show no “dips” at finite energy\(^\text{22}\) that are associated to the quenching of superconductivity in the sample due to overcritical current. The slightly concave shape of the high-voltage tails (even above \( T_c^{\text{A}} \)) and the good agreement between \( T_c^{\text{A}} \) and the bulk \( T_c \) determined from resistivity measurements at the same pressure indicate that there is no heating in the contact (i.e. the contact is ballistic). The superposition of the tails on increasing temperature indicates that there is no “spreading resistance” in series to the contact\(^\text{18,21,24}\), so that the measured voltage exactly corresponds to the energy of electrons injected in the S bank.

**Figure 1.** (a) Scheme of the “soft” point-contact technique, with the electric connections for PCARS measurements: A probe current \( I \) is injected into the crystal through the point contact and the voltage drop \( V \) across the contact is measured. (b) Drawing of the fiberglass board used as a sample holder. (c) Drawing of the Cu-Be pressure cell in which the sample is enclosed.
All the low-T spectra in Fig. 3(a–c) display a zero-bias conductance peak (ZBCP) and shoulders at 3–5 mV. The same holds for all the spectra we measured, at different pressures and with either $I \parallel ab$ or $I \parallel c$. In general, the ZBCP in PCARS can have various origins: it can be associated to OP anisotropies, in particular involving lines of nodes or zeros, or to spurious effects (contact heating, impurity scattering, etc). It can also arise from Josephson currents if a SIS junction is fortuitously obtained, which is practically impossible in our case due to the “soft” PCARS technique we used.

Heating effects can be ruled out since, as previously shown, the contact is ballistic. To see whether the ZBCP could be due to scattering from impurities, we performed model calculations by solving a three-band $s\pm$ version of the Eliashberg equations, and we found that: a) the impurity level should be extremely high and incompatible with the very high quality of our crystals; b) even in case of such a large amount of impurities, the shape of the
ZBCPs would be quite different from the experimental findings. Further indications about the intrinsic nature of the ZBCP come from the magnetic-field dependence of the PCARS spectra. Figure 3d shows the magnetic-field dependence of the low-temperature (\( T = 1.27 \text{ K} \)) conductance curve of an \( ab \)-plane contact at a pressure \( P = 0.61 \pm 0.01 \text{ GPa} \). The ZBCP is progressively suppressed by the field at approximately the same rate as the shoulders, and this means that both these features are likely to arise from the same mechanism. The ZBCP (and the shoulders) clearly persist up to \( B = 6 \text{ T} \). This is evident if the curve at \( T = 1.27 \text{ K} \) and \( B = 6 \text{ T} (\text{pink}) \) is compared to the normal-state conductance just above \( T^* \) (red). The comparison also shows that a field of 6 T is by far smaller than the upper critical field at this temperature and pressure.

Therefore, the shape of the spectra in Fig. 3, as well as their temperature and magnetic-field dependence, strongly suggest the existence of lines of nodes (or zeros) in the OP, as well as the upper critical field at this temperature and pressure.

\[ T \]

and leaving the in-plane one fixed to its equilibrium value at \( P \).

The two-gap version of the same model instead allows fitting rather well the \( ab \)-plane spectra if a large isotropic gap and a small nodal gap are used; unfortunately, in the same conditions it completely fails to fit the \( c \)-axis spectra. The main reason is that the 2D BTK model is based on the assumption of spherical or cylindrical FS, which is unreasonable for CaFe\(_2\)As\(_2\). We thus need to use a more refined 3D version of the BTK model\(^ {18,29} \) that can account for any shape of the FS and any \( k \)-dependence of the OP. In this model, the normalized conductance at \( T = 0 \) for current injected along the direction \( n \) is expressed as:

\[
\langle G(E) \rangle_{\parallel n} = \frac{\sum_i \langle \sigma_{\parallel n}(E) \rangle_{\parallel n}}{\sum_i \langle \tau_{\parallel n} \rangle_{\parallel n}} \frac{\sigma_{\parallel n}(E) \tau_{\parallel n}}{\tau_{\parallel n}}.
\]

Here \( \{ \rangle_{\parallel n} \) represents the integral over the \( i \)-th FS sheet; \( \sigma_{\parallel n} \) is the magnitude of the Fermi velocity at \( k \); \( \sigma_{\parallel n} = v_{\parallel n} \) \( \cdot \) \( n \); and \( \tau_{\parallel n} \) is the normal-state barrier transparency which depends on the Fermi velocities and on the potential barrier at the NS interface (represented by a dimensionless parameter \( Z \)). Finally, \( \sigma_{\parallel n}(E) \) is the relative barrier transparency in the superconducting state, that contains the information about the \( k \)-dependence of the OP on the \( i \)-th FS sheet\(^ {18,29} \). The normalized conductance at any \( T \neq 0 \) can be calculated by convolution of \( \langle G(E) \rangle_{\parallel n} \) with the Fermi function.

**Calculation of the Fermi surface.** Since the 3D BTK model requires knowing the shape of the FS, we calculated the band structure of CaFe\(_2\)As\(_2\), by DFT using both pseudopotential\(^ {20} \) and all-electron full-potential\(^ {19,32} \) codes, within the generalized gradient approximation (GGA) for the exchange-correlation functional, using the PBE approach\(^ {31} \) (see Methods for details). Uniaxial pressure was simulated by reducing the lattice parameter \( c \) and leaving the in-plane one \( a \) fixed to its equilibrium value at \( P = 0 \) \( (a = 3.925079 \text{ Å}) \). This is justified by the fact that, up to 6 GPa, \( a \) decreases by about 1%, while \( b \) by about 10%\(^ {34} \). For any \( c/a \) value, the equilibrium structure corresponds to the value of \( h_{\text{AS}} \) (the height of the As atoms above the Fe layer) that minimizes the total energy – determined considering the AFM (PM) phase for the orthorhombic (tetragonal) structure\(^ {15} \). Figure 4a reports the total energy and the magnetic moment \( \mu \) in the AFM and PM phases, versus the \( c/a \) ratio. The structure at \( P = 0 \) \( (c/a = 1.4466, \mu = 1.5 \mu_B) \) corresponds to the minimum energy in the AFM OR phase. On decreasing \( c/a \) the energy of this phase increases and, for \( c/a < 1.3826 \), the system undergoes a sharp first-order transition towards a non-magnetic phase. We associate the narrow region around this \( c/a \) value to the non-collapsed tetragonal phase \( (T^*) \) where superconductivity is thought to exist\(^ {45} \). Note that at the onset of the phase transition \( h_{\text{AS}} \) and the As-Fe-As bond angle jump to values close to the “optimal” ones observed at the maximum \( T \) for various Fe-based compounds\(^ {35} \). On further increasing pressure, the total energy exhibits a second minimum at \( c/a = 1.3570 \), related to the cT phase – this \( c/a \) value being in excellent agreement with that calculated under hydrostatic conditions\(^ {34} \).

Figure 4 also shows the electronic structure and the FS of CaFe\(_2\)As\(_2\) in the equilibrium structure at \( P = 0 \) (b), in the \( T^* \) phase at the edge of the phase transition (c), and in the equilibrium cT structure (d). The FS at \( P = 0 \) consists of three holelike sheets (two almost cylindrical, one largely warped in the Brillouin zone (BZ) and two 2D electronlike sheets centered at the X point. In the \( T^* \) phase \( (c/a = 1.3826) \) the two inner hole bands are completely filled at \( \Gamma \) and give rise to two 3D Fermi pockets centered at the \( Z \) points.

The outer holelike FS further expands at \( c/a = 1.3570, \mu = 1.5 \mu_B \) (red). The comparison also shows that a field of 6 T is by far smaller than the upper critical field at this temperature and pressure.

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Here \( \{ \rangle_{\parallel n} \) represents the integral over the \( i \)-th FS sheet; \( \sigma_{\parallel n} \) is the magnitude of the Fermi velocity at \( k \); \( \sigma_{\parallel n} = v_{\parallel n} \) \( \cdot \) \( n \); and \( \tau_{\parallel n} \) is the normal-state barrier transparency which depends on the Fermi velocities and on the potential barrier at the NS interface (represented by a dimensionless parameter \( Z \)). Finally, \( \sigma_{\parallel n}(E) \) is the relative barrier transparency in the superconducting state, that contains the information about the \( k \)-dependence of the OP on the \( i \)-th FS sheet\(^ {18,29} \). The normalized conductance at any \( T \neq 0 \) can be calculated by convolution of \( \langle G(E) \rangle_{\parallel n} \) with the Fermi function.

**Calculation of the order parameter structure.** In addition to the shape of the FS, the 3D BTK model also requires the knowledge of the \( k \) dependence of the OP. Even in the absence of any specific information about this point, some simulations with the 3D BTK model allow drawing some qualitative conclusions. Indeed, to reproduce the existence of a zero-bias maximum in both \( ab \)-plane and \( c \)-axis spectra, i) the shoulders must be associated to a “large” gap, possibly isotropic, and the zero-bias maximum to a smaller gap, featuring lines of nodes or zeros; ii) this small gap must reside on a FS with a pronounced 3D character (i.e. not on a hyperboloid-like FS sheet, as shown elsewhere\(^ {28} \)); iii) the lines of nodes (or zeros) can be either vertical or horizontal (for further
details see Supplementary Information). These conclusions actually agree with what we found in 6% Co-doped CaFe$_2$As$_2$;36,37 (that, by the way, has a Fermi surface similar to that of the T* structure shown in Fig. 4c); theoretical predictions for the OP structure in the 122 family of IBS;38–40 indicate that the lines of nodes on the holelike FS may be horizontal rather than vertical.

To get some more specific hints about the $k$ dependence of the OP in the T* structure of CaFe$_2$As$_2$, we followed the method adopted for BaFe$_2$(As, P)$_2$;38: Starting from the band structure in the T* phase we constructed a ten-orbital model (five 3d orbitals $\times$ two Fe atoms per unit cell) exploiting the maximally localized Wannier functions;41,42. We then applied a Random Phase Approximation (RPA) approach to obtain the spin susceptibility, and we solved the linearized Eliashberg equations using a pairing interaction proportional to this spin susceptibility (see Methods for details). The superconducting gaps for the quasi-2D outer electron sheet and the quasi-3D outer hole sheet are depicted in Fig. 5 at different $k_z$ values. The OP on the electron FS, $\Delta_e$, is relatively isotropic (except at $k_z = \pi$), while the OP on the hole FS, $\Delta_h$, is smaller and strongly anisotropic in the $ab$ plane. Moreover, the latter decreases on decreasing $k_z$ until it changes sign at $k_z \approx \pi/4$, forming a horizontal node line. These calculations thus confirm the qualitative conclusions about the OP structure drawn on the sole basis of the shape of the PCARS spectra, and give them a robust foundation; however, they do not provide reliable values of the gap amplitudes $\Delta_e$ and $\Delta_h$. These quantities can be obtained by fitting the PCARS spectra with the 3D BTK model (eq. 1).

**Fit of the PCARS spectra.** For ease of calculation, we schematize the outer electronlike FS in the upper half of the BZ by a one-sheeted hyperboloid of revolution and the outer holelike FS by an oblate spheroid centered at $Z$ (see Fig. 6(a)). This simplification preserves all the important characteristics of the FS from the point of view of eq. 1. For example, the cylindrical neck along $\Gamma-Z$ (see Fig. 4(c)) gives a small (for $I \parallel ab$) or null (for $I \parallel c$) contribution to the conductance and can be neglected, leaving a small hole in the spheroid. According to the results of RPA calculations, the gap on the electronlike FS ($\Delta_e$) is isotropic, but that on the holelike FS has a horizontal node line at $k_z = 3\pi/4$ and a fourfold in-plane anisotropy (see Fig. 6(a)). $\Delta_h$ is defined so that at $k_z = \pi$ the holelike gap varies between 0.5 $\Delta_h$ and 1.5 $\Delta_h$.

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**Figure 4.** (a) Fe magnetic moment (solid circles) and total energy in the AFM (black circles) and PM (red circles) phases, as a function of $c/a$. The $c/a$ values corresponding to the OR, cT and T* structures are indicated by arrows. (b–d) Electronic band structure and Fermi surface in the OR AFM (b), T* (c) and cT structure (d).
The adjustable parameters of the 3D BTK model are thus the gap amplitudes $\Delta_e$ and $\Delta_h$, the barrier parameters $Z_e$ and $Z_h$, and the broadening parameters $\Gamma_e$ and $\Gamma_h$ that account for the small amplitude of the Andreev signal. The weight of each band is fixed by the FS geometry and the direction of current injection. The results of the best fits—always obtained by minimizing the sum of squared residuals—are shown in Fig. 6(b–d) for ab-plane contacts (at $P = 0.40, 0.61$ and $0.85$ GPa) and in Fig. 6(e) for a c-axis contact (at $0.53$ GPa). The fit is very good for both the injected-current directions, and similar results have been obtained for all the contacts at different pressures. Note that the OP structure indicated by RPA calculations allows the best fit of the spectra, if compared to other configurations (e.g. vertical node lines on the holelike FS). Further details on this point as well as on the error bars and the robustness of the fits can be found in Supplementary Information.

Once the spectra measured at different temperatures are normalized, it is possible to fit them with the 3D BTK model to determine how the amplitude of the OPs depends on temperature. Figure 7 reports, as an example, a set of conductance curves of the same ab-plane contact at $P = 0.61 \pm 0.01$ GPa measured at different temperatures between 1.27 and 12.01 K (symbols). The 3D BTK fits (solid lines) of the curves are shown as well. The fit allowed us to extract the temperature dependence of the gap amplitudes $\Delta_h$ and $\Delta_e$ that is reported in the inset.

Similar results are obtained from the temperature dependencies of the normalized PCARS spectra at the other pressures.

**Pressure dependence of the gap amplitudes.** Figure 8(a) reports $T_{c1}^c$, $\Delta_h$ and $\Delta_e$ vs. pressure. The error bars on the gaps represent the range of values that give an acceptable fit (within a fixed confidence level) when all the other parameters are changed as well (see Supplementary Information for the procedure). $T_{c1}^c$ follows very well the bulk $T_c$ reported elsewhere, showing a broad maximum between 0.6 and 0.75 GPa. The gaps remain almost constant.
constant between 0.4 and 0.55 GPa, but between 0.55 and 0.6 GPa they increase so much that even the gap ratios \(2\Delta_e/k_BT_c\) and \(2\Delta_e/k_BT_c\) grow (see Fig. 8(b)) becoming both greater than the BCS value 3.52; \(2\Delta_e/k_BT_c\) even reaches values of about 8. Note that similar gap ratios were obtained in 6% Co-doped CaFe\(_2\)As\(_2\), which is close to an analogous Lifshitz transition induced by chemical doping\(^\text{37}\). In KFe\(_2\)As\(_2\) (that shows no electrolike FS) gap ratios equal to 7.58\(\pm\)0.34, 2.80\(\pm\)0.34 and 1.02\(\pm\)0.41 were measured by ARPES on the FS sheets around \(\Gamma\)\(^\text{43}\).

Even larger values were found in (Ba\(_{0.1}\)K\(_{0.9}\))Fe\(_2\)As\(_2\)\(^\text{44}\).

**Discussion**

The enhancement of the critical temperature and of the gap amplitudes in a narrow pressure range, and even more the steep increase in the gap ratios, suggest an enhancement in the electron-boson coupling in concomitance with the 2D-3D topological transition, which can still be explained within a spin-fluctuation mediated pairing (even though alternative strong-coupling explanations\(^\text{44}\) cannot be excluded): When the holelike FS shrinks, the set of “nesting wavevectors” that connect it to portions of the electronlike FS widens, and the integral of the susceptibility increases – until the holelike FS completely vanishes at \(\Gamma\) and superconductivity disappears. The occurrence of a maximum in \(T_c\) and in the gap amplitudes in correspondence of a 2D-3D Lifshitz transition has been recently predicted – within a BCS approach, with the inclusion of the density equation – in multiband superconductors when the chemical potential is tuned near a band edge\(^\text{45}\). This picture holds for 3D superlattices of quantum wells, of which IBS, among other layered superconductors, can be considered a practical realization, and is based on the concept of shape resonance. In similar conditions, a peak in the isotope coefficient has also been predicted\(^\text{46}\).

To summarize the results obtained by the unique combination of directional PCARS on CaFe\(_2\)As\(_2\) under quasi-hydrostatic pressure and state-of-the-art ab-initio calculations proposed in the present paper, it can be said that: i) the electron-boson coupling largely increases in the narrow pressure range where a topological 2D-3D transition of the holelike FS occurs; ii) this transition drives the emergence of a horizontal node line in the OP on the holelike FS sheet, which leaves its fingerprints in the zero-bias Andreev-reflection conductance. It is intriguing to notice that the same phase transition with disappearance of the holelike FS at \(\Gamma\) that here produces a
dramatic increase of the coupling in both bands seems to be responsible for the high-\( T_c \) phase at 47 K observed in rare-earth doped CaFe\(_2\)As\(_2\)\(^{47}\), and for the second, higher-\( T_c \) superconducting dome in LaFeAsO\(_1-x\)H\(_x\)\(^{48}\). Recently, a study of KFe\(_2\)As\(_2\) in an extended pressure range (up to 30 GPa) has shown two superconducting phases in the phase diagram\(^{49}\). A first superconducting dome (with a maximum \( T_c \approx 7 \) K around 2.5 GPa) occurs in the T structure, and is extended up to about 7 GPa. Note that, as previously reported, no electronlike FS sheets exist in this structure. A second superconducting phase with a greatly enhanced critical temperature (about 11 K) appears abruptly when the system undergoes the transition to the cT phase at \( P = 13 \) GPa; \( T_c \) then decreases on further increasing the pressure. The sudden jump in \( T_c \) around 13 GPa is ascribed to the fact that the holelike FS sheet at...
Γ shrinks, the hololike FS at X disappears and is replaced by an electronlike pocket, thus restoring the usual conditions of imperfect nesting associated to the spin-fluctuation pairing mechanism. In this case, as in ours, the maximum \( T_c \) occurs exactly at the T-c transition.

**Methods**

**Crystal growth.** The CaFe_{2}As_{2} single crystals were grown in a Sn flux, starting from atomic ratios \( \text{Ca:Fe:As:Sn = 1.1:2.2:1:4} \). The components, contained in alumina crucibles, were placed in sealed quartz ampoules previously filled with Ar gas under a pressure of 0.3 bar. The ampoules were then slowly heated (~4 h) to 600 °C, held at this temperature for 1 h, then further heated (~5 h) to 1050 °C, and kept at this temperature for 5 h so that all the components dissolved in the Sn flux. Crystals were grown by slow cooling the melt at a rate of 2 K/h to 600 °C, followed by furnace cooling to room temperature. The flux was finally removed by etching in diluted hydrochloric acid. The resulting single crystals were platelike, with the c-axis perpendicular to the plate. Phase purity was checked by powder x-ray diffraction (XRD). The details of the characterization can be found in ref. 19.

**Experimental setup for point-contact measurements under pressure.** The most usual way for making the point contact in PCARS is the so-called needle-anvil technique, in which a sharp normal-metal tip is pressed against the surface of the superconductor\(^{17}\). The resistance of the contact is generally controlled by moving the tip forward/backward through a rigid shaft connected to a suitable device (i.e. a stepper motor). This setup is obviously not applicable if the sample has to be closed in a high-pressure cell, as in our case. We thus adopted an alternative setup (the “soft” point-contact technique we introduced some years ago\(^{14}\)) wherein the contact tip is substituted by a tiny silver paste contact whose resistance can be tuned via short current or voltage pulses. This method can be easily adapted to work in a pressure cell since it allows the whole setup to be mounted on a small support, and does not require any mechanical action from external moving parts. Moreover, it ensures a greater mechanical, thermal and electrical stability of the contacts.

In this specific case, the small drop of Ag paste (\( \phi \approx 50 \mu \text{m} \)) was put on the freshly cleaved surface of the crystal. A varying probe current \( I \) was then injected from the Ag spot into the superconductor and the voltage \( V \) across the contact was measured, thus determining the \( I-V \) characteristics of the contact (see Fig. 1(a)) and then the differential conductance \( dI/dV \text{ vs.} V \). Note that if the contact is put on the topmost surface, the current is mainly injected along the c axis; if it is placed on the side surface, the current is preferentially injected along the a/b planes.

The sample holder was made from a small (\( \approx 7 \times 3 \text{ mm}^2 \)) fiberglass board, with a small 50-turn coil wrapped around a piece of high-purity Pb (99.9999%) placed on the reverse side (see Fig. 1(b)). The sample holder was mounted in a Cu-Be pressure cell and immersed in silicone oil used as the pressure-transmitting medium. This ensures hydrostatic pressure conditions above the freezing point of the oil, but when the oil freezes a uniaxial pressure component sets in. The pressure was applied at room temperature, then the cell was cooled in a \( \text{He} \) variable temperature cryostat. To determine the pressure at low temperature, we measured the temperature of the superconductor transition of Pb by an ac mutual inductance technique; then we used the well-known \( T_c(P) \) dependence for Pb to extract the pressure value. This technique allows determining the pressure at low temperature, but does not allow separating the uniaxial component from the hydrostatic one; therefore, a scaling factor might be necessary when comparing our results with those obtained by using different pressure-transmitting media.

**DFT and RPA ab-initio calculations.** The ab-initio DFT calculations were performed by using both the pseudopotential method (Vienna ab-initio Simulation Package, Quantum Espresso\(^{30}\)) and all-electron full-potential codes (Wien2K\(^{31}\), Elk\(^{32}\)) in order to compare the results and confirm the findings. For the structural optimization (always done in the antiferromagnetic phase) the charge density was integrated with \( \Delta_{\text{shift}} = 2 \Delta_{g} \left[ \sin \left( \phi + \frac{\pi}{3} \right) \Theta \left( -\phi + \frac{2\pi}{3} \right) \cos^2 \left( 2\theta \right) + \frac{1}{2} \right] + \sin \left( \phi + \frac{\pi}{3} \right) \Theta \left( \phi - \frac{2\pi}{3} \right) \),

where \( \Theta \) is the Heaviside step function. In the \( k_x = \pi \) plane (\( \phi = \pi/2 \)), the gap amplitude varies (depending on \( \theta \)) between 0.5 \( \Delta_{g} \) and 1.5 \( \Delta_{g} \) (note that \( \phi = \pi \) corresponds to the \( Z - \Gamma \) direction). The \( \Delta_{\text{shift}} \) function, together with the constant order parameter on the electronlike FS \( \Delta_{e} \), is plotted in Fig. 4(a) of the main text (grid surfaces) and is used in the 3D BTK fit of the experimental data.
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**Acknowledgements**

This work was supported by the Collaborative EU-Japan Project ”IRON SEA” (NMP3-SL-2011-283141). R.S.G. wishes to thank the Max-Planck Institute for Solid State Research in Stuttgart where the measurements were carried out. The authors acknowledge the OpenAIRE FP7 post-grant Open Access Pilot project of the European Commission for the specific funding of the publication costs.

**Author Contributions**

R.S.G. designed the PCARS measurements under pressure and performed them with the collaboration of P.G.R. and R.K.K. Z.B. and J.K. grew and characterized the CaFe$_2$As$_2$ single crystals. R.S.G., M.T., D.D. and G.A.U. developed the 3D BTK model for fitting the experimental PCARS data and made all the data analysis. G.P. made *ab-initio* DFT calculations. K.S. and K.K. made the 10-orbital RPA calculations. R.S.G. and D.D. wrote the paper.

**Additional Information**

**Supplementary information**

accompanies this paper at http://www.nature.com/srep

**Competing financial interests:** The authors declare no competing financial interests.

**How to cite this article:** Gonnelli, R. S. et al. Fermi-Surface Topological Phase Transition and Horizontal Order-Parameter Nodes in CaFe$_2$As$_2$ Under Pressure. *Sci. Rep.* **6**, 26394; doi: 10.1038/srep26394 (2016).

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