Cherenkov Telescopes as Optical Telescopes for Bright Sources: Today’s Specialised Thirty Metre Telescopes?

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Abstract

Imaging Atmospheric Cherenkov Telescopes (IACTs) use large-aperture (∼ 10 − 30 m) optical telescopes with arcminute angular resolution to detect TeV gamma-rays in the atmosphere. I show that IACTs are well-suited for optical observations of bright sources (V < ∼ 8 − 10), because these sources are brighter than the sky background. Their advantages are especially great on rapid time-scales. Thus, IACTs are ideal for studying many phenomena optically, including transiting exoplanets and the brightest gamma-ray bursts. In principle, an IACT could achieve millimagnitude photometry of these objects with second-long exposures. I also consider the potential for optical spectroscopy with IACTs, finding that their poor angular resolution limits their usefulness for high spectral resolutions, unless complex instruments are developed. The high photon collection rate of IACTs is potentially useful for precise polarimetry. Finally, I briefly discuss the broader possibilities of extremely large, low resolution telescopes, including a 10 arcsec resolution telescope and spaceborne telescopes.

Key words: telescopes – techniques: photometric – techniques: spectroscopic – techniques: polarimetric

1 INTRODUCTION

Extremely Large Telescopes (ELTs) with apertures of 30 m promise to open a new era in astronomy, but will be extremely costly and complex. It is less widely appreciated that we already have ELT-size telescopes of low optical resolution: the Imaging Atmospheric Cherenkov Telescopes (IACTs). IACTs are designed primarily to image TeV gamma-ray sources by detecting the Cherenkov radiation from the particle showers created when a TeV gamma-ray hits the atmosphere (for reviews of the uses of IACTs as TeV detectors, see for example Aharonian & Akerlof 1997; Ong 1998; Aharonian et al. 2008). Detecting the faint Cherenkov pulse requires high photon statistics, and reconstructing the structure and direction of the shower is aided by stereoscopic imaging. IACTs therefore typically consist of an array of multiple mirrors, each with large collecting areas (∼ 100 m²). Many IACTs have been built, including HESS (Bernlöhr et al. 2003; Cornils et al. 2003), VERITAS (Weekes et al. 2003; Humensky 2007), MAGIC (Lorenz 2004), CANGAROO (Kawachi et al. 2001), HEGRA (Akhperjanian et al. 1998), and Whipple (Lewis 1990; Kildea et al. 2007). Future IACT arrays like the Cherenkov Telescope Array (CTA) may have four 25 m mirrors and tens of 10 m mirrors, for an optical collection area equivalent to a ∼ 50 m telescope (Doro & CTA consortium 2009). The cost of the IACT mirrors is very low, only ∼ £2000/m² (2010), and may go down further in the future (CTA Consortium 2010). However, the lower quality IACTs have poor angular resolution by optical standards (∼ 1 − 2′; Bernlöhr et al. 2003; Cornils et al. 2003). The huge size of the mirrors still makes them ideal ‘light buckets’, and the primary science cannot occur on moonlit nights. IACTs have therefore been used for some optical studies, often when the sky glow is brighter: detecting the optical pulsations of the Crab pulsar (Öna-Wilhelmi et al. 2004; Hinton et al. 2006; Lucarelli et al. 2008), searches for microsecond optical transients (Deil et al. 2009), and even optical SETI (Eichler & Beskin 2001; Holder et al. 2003). IACTs have also been proposed as tools for stellar intensity interferometry (Le Bohec & Holder 2006) and detecting nanosecond optical transients (Borra 2010). However, the potential of

Conversely, the Narrabri Observatory intensity interferometer, which like an IACT array used several low angular resolution reflectors (Hanbury Brown, Davis, & Allen 1967), carried out one of the earliest Southern Hemisphere searches for TeV gamma-rays (Hanbury Brown, Davis, & Allen 1967; Grindlay et al. 1975).
IACTs to study bright, steady sources other than pulsars has not been studied in great detail.

The primary challenge to using IACTs as optical telescopes is that their low angular resolution blends sky background with a target source’s light. When the source is brighter than the sky background, the IACT will be at its most effective. On a moonlit night, the V-band sky brightness is $\mu V \approx 20$ mag arcsec$^{-2}$ (depending on the phase and Moon–source angle; [Krisicsin & Schaefer 1991; see also Fig. 4 of [Deil et al. 2009], and the sky brightness within the PSF is

$$V_{\text{sky}} \approx 8.36 - 5.0 \log_{10} \left( \frac{\theta_{\text{PSF}}}{2 \text{ arcmin}} \right)$$

(1)

where $\theta_{\text{PSF}} \approx 1 - 2\prime$ are typical radii of PSFs for IACTs. Similar values are found for B and I bands. On moonless nights, the V-band sky brightness at IACT sites is typically 22 mag arcsec$^{-2}$ to give $V_{\text{sky}} \approx 10.4$, at $|b| > 20^{\circ}$ and including all stars with $V \leq 6$ ([Preuss et al. 2002]). Confusion will also limit the usefulness of IACTs for stars with $V > 14 - 16$ ($|b| > 20^{\circ}$), as the images of the stars begin to overlap ([Bahcall & Soneira 1980]).

The point of this paper is to explore whether and how IACTs can exploit their huge photon collection rates for bright source optical astronomy. During a V-band ($\lambda = 5448$ Å; $\Delta \lambda = 840$ Å; [Bessell 2003] observation, IACTs collect

$$N_\ast \approx 2.7 \times 10^8 \times 10^{-0.4(V-8)} A_{100 \mu \text{m}} t_{\text{int}} \eta_{0.5}$$

(2)

photons, where $A_{100 \mu \text{m}}$ m$^2$ is the collecting area, 0.5$\eta_{0.5}$ is the photon detection efficiency, and $t_{\text{int}}$ is the integration time in seconds. IACTs are most suited for high speed measurements, where brighter objects will be the detectable ones in any telescope of a given aperture ([Deil et al. 2009]).

Fig. 1 shows that the integration times relative to a 1 metre diffraction-limited telescope. With bright sources, IACTs can achieve the same signal-to-noise with integration time $s$ times less than 10 ms, the spectral index of atmospheric turbulence changes and the scintillation noise becomes even greater, down to 0.3 ms when the inner scale of turbulence is reached ([Dravins et al. 1997a]). On the other hand, IACTs may be large enough to be affected by the outer scale of turbulence ([Dravins et al. 1997b]), which ranges somewhere between a few metres (e.g., [Nightingale & Buscher 1991] and several kilometres (e.g., [Colavita, Shao, & Staelin 1991]), in which case the scintillation noise may decrease ([Dravins et al. 1998]). The prospects for probing the outer scale are especially good if multiple telescopes in an array like HESS or VERITAS are used, since they are typically tens of metres apart.

Finally there is scintillation noise caused by turbulence in the atmosphere, which is given in [Young 1967] and [Southworth et al. 2009]:

$$\sigma_V^{\text{scint}} = 5.6 \times 10^{-4} A_{100}^{-1/3} t_{\text{int}}^{-1/2} X^{7/4} \sigma_{\text{int}}^{6-h/8 \text{ km}}$$

(5)

where $X$ is the airmass and $h$ is the altitude of the telescope, and is typically $\sim 2$ km ([Preuss et al. 2002]). For exposure times less than 10 ms, the spectral index of atmospheric turbulence changes and the scintillation noise becomes even greater, down to 0.3 ms when the inner scale of turbulence is reached ([Dravins et al. 1997a]). On the other hand, IACTs may be large enough to be affected by the outer scale of turbulence ([Dravins et al. 1997b]), which ranges somewhere between a few metres (e.g., [Nightingale & Buscher 1991] and several kilometres (e.g., [Colavita, Shao, & Staelin 1991]), in which case the scintillation noise may decrease ([Dravins et al. 1998]). The prospects for probing the outer scale are especially good if multiple telescopes in an array like HESS or VERITAS are used, since they are typically tens of metres apart.

In practice, the sky background noise may be greater if the image plane is not focused to infinity. IACTs are focused to the atmosphere, which spreads out the PSF of sources at infinity and dilutes their light with the sky background (e.g., [Lucarelli et al. 2008]). For a reflector of focal length $f$ with light from a distance $s$ in focus on the detector plane, the detector plane would have to be shifted by a length $\Delta s' \approx f^2/s \approx 1 \text{ cm}(f/10 \text{ m})^2 (s/10 \text{ km})^{-1}$ for sources at infinity to be in focus (e.g., [Schorr 1998]). Otherwise, the PSF radius will be broadened by an apparent angle $\theta_{\text{focus}} \approx D/(2s) \approx 1.7(D/10 \text{ m})(s/10 \text{ km})^{-1}$ for a telescope of aperture $D$. ([Deil et al. 2009] used a secondary

$\sigma_V^{\text{Poison}} \approx 6.7 \times 10^{-5} \times 10^{0.2(V-8)} \sqrt{A_{100} t_{\text{int}} \eta_{0.5}}$.

(3)

$$\sigma_V^{\text{Poison}} \approx 5.6 \times 10^{-5} \times 10^{-2(2V-16-V_{\text{sky}}+8.36)} \sqrt{A_{100} t_{\text{int}} \eta_{0.5}}.$$
mirror to put distant sources in focus on a custom detector, so focusing is not an insurmountable issue.

The total white noise in the magnitude is given by

\[ \sigma_V = \sqrt{\left(\sigma_{\text{snow}}\right)^2 + \left(\sigma_{\text{int}}\right)^2} \]

I show \(\sigma_V\) for IACTs as compared to diffraction-limited and 10 arcsec resolution telescopes in Fig. 2 as a function of V magnitude. We see that scintillation typically dominates \(\sigma_V\) except for faint sources (\(V \geq 10 - 14\)). A 10 metre IACT in principle achieves milli-magnitude photometry within a few seconds, for \(V \leq 12\). For sources with \(V \geq V_{\text{sky}}\), IACTs are less efficient than high resolution telescopes, because the S/N for IACTs goes as \(\sqrt{N_s \times \sqrt{N_s/N_{\text{sky}}}}\) while for high resolution telescopes the signal-to-noise goes as \(\sqrt{N_s}\).

2.1 Detectors

IACTs use photomultiplier tubes (PMTs) as their optical detectors, and it would be easiest to simply use these for optical observations. Such observations have been demonstrated with IACT observations of pulsars [Lucarelli et al. 2008]. The main advantage of PMTs, aside from already being installed, is that they can monitor photon flux on extremely short time scales, taking full advantage of the IACT’s ability to collect photons quickly. Automated Photoelectric Telescopes have for many years demonstrated the potential of milli-magnitude photometry with PMTs (e.g., Henry 1992; 1994), including one of the first detections of a transiting exoplanet [Henry et al. 2000]. Disadvantages of PMTs include lower quantum efficiency, and larger pixel sizes (typically \(\sim 0.1^\circ - 0.2^\circ\); Bernlohr et al. 2003; Lorenz 2004) with the currently installed PMTs. The low PMT angular resolution increases the sky background even further, reducing \(V_{\text{sky}}\) to \(\sim 6\) on moonlit nights and \(\sim 8\) on moonless nights for a pixel size of \(0.1^\circ\).

CCDs, by contrast, have higher quantum efficiency and much higher spatial resolution. However, using CCDs would require replacing the current PMT detectors of IACTs or the construction of new IACT-like telescopes designed to use CCDs. The image of a bright object will be spread over a very large area in an IACT; given a typical focal length of \(\sim 15\) m (image scale of 4.4 mm arcmin\(^{-1}\)), the image will have a diameter of 18 mm (\(\theta_{\text{PSF}}/2\) arcmin), roughly the size of a typical CCD detector. The large size essentially eliminates flat-fielding noise, but two issues may concern us when using CCDs: read noise and CCD saturation. For a typical pixel size of 15 \(\mu\)m, the image will be spread out over \(n_{\text{pix}}\) \(\approx 10^5(\theta_{\text{PSF}}/2\) arcmin\)\(^2\) pixels. From equation 1 we expect \(\sim 300\) photon/s\(^{-1}\) \(n_{\text{pix}}\) photons per pixel, far below saturation for most CCDs for 1 second exposures (note that for a given f-ratio, the image scale for a larger telescope will become proportionally bigger). Thus, whereas stopped apertures are used for photometry of bright stars with standard telescopes [Lopez-Morales 2006], IACTs evade the saturation problems precisely because they have such low angular resolution. Finally the read noise is \(N_{\text{RN}} = n_{\text{RN}}\sqrt{n_{\text{pix}}}\), where \(n_{\text{RN}}\approx 5\) is the read-out noise per pixel. The read-out noise is tiny except for the shortest of exposures: \(n_{\text{RN}}^2 \approx 1.0587(N_{\text{RN}}/N_s) \approx 2 \times 10^{-5} \times 10^{-0.4(V-8)}(\theta_{\text{PSF}}/2\) arcmin\)/\(A_{\text{FOV}}\times \theta_{0,5}\)^\(^{-1}\).

A major problem with typical CCDs is that they have readout times of \(\sim 10 - 100\) sec. Thus, exposure times are typically limited to at least about a minute, since low duty cycles would negate the light gathering power of the telescope. There are high speed CCD systems, but these typically work by using only a small part of the chip to image a target source, and shifting the image around on the CCD to get multiple exposures on one chip (e.g., O’Donoghue [1992]; Dhillon et al. 2007]. This will not be possible with IACTs, as the time of the source will be comparable to the size of the chip.

Geiger-mode Avalanche Photodiodes (G-APDs; also called silicon photomultipliers or SiPMs) are a relatively new detector system that are now being applied to Cherenkov telescopes (e.g., Buzhan et al. 2003; Renker 2007). G-APDs are \(\sim\)millimetre size detectors consisting of thousands of micro-pixels; the micro-pixels are connected by a substrate, which gives a signal for the detector. They are extremely good at timing photons (\(< 0.1\) ns timing precision), while being able to tolerate high sky backgrounds of GHz per detector (e.g., Anderhub et al. 2000) (compare eqn. 2). Be-
cause the individual detectors are smaller than the PMTs currently used in Cherenkov telescopes, G-APDs would not blend the source light with background light like PMTs would. G-APDs have already been used to detect Cherenkov photons using MAGIC (Biland et al. 2007), and the dedicated First G-APD Cherenkov Telescope (FACT) uses G-APDs (Braun et al. 2009; Anderhub et al. 2011).

A developing possibility is to use new cryogenic photon counting detector technologies, such as superconducting tunnel junction (STJ) detectors and Transition Edge Sensors (TES) (e.g., Verhoeve 2008). STJ detectors have small pixel sizes compared to PMTs (∼ 30 µm), high quantum efficiency, extremely high time resolution (∼ 1 µs), and even some low spectral resolution. On the other hand, the detectors must be cooled to sub-Kelvin temperatures. S-Cam at the William Herschel Telescope has demonstrated that STJs can be used for high time resolution astronomy (e.g., Perryman et al. 1997; Oosterbroek et al. 2008), however it only consists of a few pixels and has a very small field of view (e.g., Verhoeve et al. 2006). Much larger arrays are needed to fit the PSF of even one source imaged with an IACT, and differential photometry with STJs at IACTs is vastly more difficult still. Finally, STJs become saturated at count rates of ∼ 10^3 sec^-1 per pixel. Assuming a pixel size of 30 µm, there are n_pix ∼ 2 × 10^5(θ_{PSF}/2 arcmin)^2 pixels in the image of a source, and from eq. [2] we see saturation occurs at V ≈ 8.3. Thus, observations with current STJ technologies might require going to fainter sources on moonless nights. High time resolution photometry (and spectroscopy) has also been demonstrated with TES studies of the Crab pulsar, but again only for small detectors (e.g., Romani et al. 1999).

2.2 Systematics and Challenges

In practice, a number of systematic issues present the true challenge to attaining sub-millimagnitude photometry. These systematic effects add time-correlated red noise to the photometry, and decrease the precision.

Changes in the PSF as the telescope tracks a target may be one source of systematic noise. Gillon et al. (2009) attempted to use the defocused VLT to measure the light curves of WASP-4 and WASP-5. They found that systematic trends in the light curves of the target stars and field stars, probably due to the active optics being turned off. IACTs may experience similar effects; the PSFs of Whipple and HESS are changed by distortions in its support structure (Cornils et al. 2003; Kildea et al. 2007), although this seems to be insignificant for CANGAROO-II (Kawachi et al. 2001). To evade such problems, differential photometry with other stars in the field is probably necessary.

Photon-limited millimagnitude differential photometry is regularly achieved on the ground, but this requires monitoring multiple stars in the field (Everett & Howell 2001; Hartman et al. 2003). However, at V = 8, the population of stars is relatively sparse (∼ 0.3 − 2 deg^-2 at |b| ≥ 20°; Bahcall & Soneira 1980) with only a few in the entire ∼ 5° field of view (which would have to be covered with detectors). The situation improves somewhat at greater magnitudes (at V = 10, ∼ 2 − 10 deg^-2 spacing implies ∼ 20 − 50 arcmin between stars; at V = 12, ∼ 10 − 70 deg^-2 implies 8 − 20 arcmin spacing; Bahcall & Soneira 1980). Furthermore, the PSF of IACTs typically grows larger further from the centre of the field, which may hamper differential photometry. Image subtraction techniques have been invented for photometry when there are PSF variations in a field, however (Alard 2000; Kerins et al. 2010). A wide-field (15°) IACT using Schmidt optics has been proposed, which would have a stable PSF over its entire field; this kind of IACT may prove useful for differential photometry (Mirzoyan & Andersen 2004).

Another potential problem is that the comparison stars will appear on different CCDs than the target source. Since there will be gaps between the detectors (whether PMTs, G-APDs, or SJDs), the camera may have to be rotated during the night to avoid the comparison stars’ images from sliding into the gaps. Otherwise, as the fraction of a reference star’s PSF in a gap changes, there will be apparent changes in its brightness. On the other hand, Cherenkov telescopes typically use light concentrators like Winston cones to funnel light into detectors with little dead space, including HESS (Bernlörh et al. 2003), MAGIC (Lacarelli et al. 2008), and VERITAS (Weekes et al. 2002), and potentially, the future CTA (CTA Consortium 2010). Finally, the guiding will have to be sufficiently accurate that the image does not wander significantly during an observation.

Stray light in the telescope and detector can also introduce systematic errors in fine photometry (Deil 2011, private communication). For differential photometry, we are concerned with temporal and spatial variations of stray light, since we are interested in relative changes of the brightness of the source and stray light introduces much less shot noise than the night sky background itself. These variations can be caused by either (1) the amount of stray light varying as the telescope tracks a source over the course of a night and (2) different amounts of stray light between the comparison star and the source because they are at different angles. Winston cones, which reduces the solid angle visible to the detectors, can reduce the amount of light from the sky or the ground around the telescope; in HESS, they accept light roughly from the angle subtended by the primary reflector (acceptance angle is 27°), although small amounts of light come from larger angles (Bernlörh et al. 2003). In addition, there are gaps between the mirror facets in the reflector, through which the mount is visible. This is partly ameliorated in HESS because the mount is painted red while PMTs are mostly sensitive to blue light (Bernlörh et al. 2003). However, Preuß et al. (2002) find that ground light is about ∼ 15% of the night sky background for HESS, with the telescope mount contributing an additional ∼ 3%. Thus, in order to ensure that stray light is less than 10^-5 of the source light, the source may have to be ∼ 200 times brighter than the night sky, or V ≤ V_{sky} − 5.7 ≈ 2.7 − 4.7. On the other hand, there are techniques for doing photometry in the presence of variable backgrounds included stray light (e.g., Kerins et al. 2010), and the variations in the stray light over the course of an observation may a small fraction of the total amount of stray light, allowing photometry of fainter objects.

These systematics introduce red noise that is correlated on a time scale of a few hours, and make detections harder even for periodic phenomena. Pont et al. (2006) considered the effects of red noise specifically in the case of exoplanet...
transits, although their analysis should work similarly for other periodic phenomena. If a transit is observed \( N_{tr} \) times and has a depth \( d \), the threshold for detection is

\[
d^2 \gtrsim \frac{S^2}{\sum_{k=1}^{N_{tr}} n_k^2 (\sigma_w^2/n_k^2 + \sigma_r^2)}.
\]  

(6)

where \( S \approx 10 \) is a typical signal-to-noise required for detection, \( n_k \) is the number of observations within a transit, \( N_{tr} \) is the total number of observations in all the transits, \( \sigma_r \) is the time-uncorrelated white noise (including photon, scintillation, and detector noise), and \( \sigma_w \) is the red noise. When white noise dominates, \( \sigma_w \approx \sqrt{n_k \sigma_r} \), and when red noise dominates, \( d \approx S \sigma_w/\sqrt{N_{tr}} \). For most transit surveys, \( \sigma_r \approx 0.001 \), and since IACTs reach \( \sigma_w \approx 0.001 \) within seconds (eq. 3.4), they may be in the red noise regime, where only the number of transits observed matters:

\[
d \gtrsim 0.01 (\frac{\sigma_r}{0.001}) (\frac{S}{10}) \frac{1}{\sqrt{N_{tr}}}.
\]  

(7)

This negates most of the advantages of IACTs over smaller telescopes, but the remaining advantages from the shorter exposure times would be: (1) IACTs can do timing studies more accurately; (2) IACTs could move to the next target more quickly (though subject to slew times); (3) IACTs could easily conduct multiband photometry. Furthermore, photometry of individual transiting exoplanets have been able to reduce the red noise to \( \sim 10^{-4} \) (e.g., Winn, Holman, & Roussanova 2007, Winn et al. 2009). Note also that most IACTs come in arrays of multiple telescopes. It is unknown if the red noise between telescopes in an array is correlated, but if it is not, each telescope would contribute an independent observation, increasing \( N_{tr} \) by the number of IACTs. For CTA, which is planned to have \( \sim 50 \) IACTs, this effect may be very powerful.

Finally, absolute photometry over weeks or longer requires the monitoring the reflectance of the IACT. IACTs are built in the open, exposed to the elements, and suffer decreased reflectivity with time. IACTs are therefore occasionally washed or re-aluminised, which will affect performance (Kildea et al. 2007).

3 SPECTROSCOPY WITH IACTS

As light buckets, IACTs could also be useful for spectroscopy. If a proper spectrometer could be built, they can rapidly generate high S/N spectra:

\[
S/N \approx \begin{cases} 
416 \times 10^{-0.2(V-8)} \sqrt{\frac{A_{1000} \theta_{fib} \rho_{0.5}}{R_{10000}}} & (V \lesssim V_{sky}) \\
491 \times 10^{-0.2(2V-16)\Delta V_{sky}+8.36} & (V \gtrsim V_{sky})
\end{cases}
\]  

(8)

where \( R = 10^4 R_{10000} = \Delta \lambda/\lambda \) is the spectral resolution. Measurements of spectral line structure and depth are differential, thus there may not be as many systematics from the atmosphere.

The main challenge to designing a dispersive spectrograph for an IACT is that the low angular resolution smears out the image of the source. The resolving power of a spectroscopic grating is \( R \approx k d_{slit}/(\sigma_{slit} D_T) \), where \( d_{slit} \) is the size of the beam on the grating, \( \sigma \) is the grating spacing, \( \theta_{slit} \) is the slit width in terms of sky angular diameter, \( D_T \) is the telescope aperture, and \( k \approx 1 \) is a combination of other parameters relating to the optics of the spectrograph (e.g., Schroeder 2000). For typical parameters,

\[
R(\text{grating}) \approx 47k \left(\frac{d_{slit}}{1 \text{ m}}\right) \left(\frac{\sigma}{1000 \text{ mm}^{-1}}\right) \left(\frac{\theta_{slit}}{4 \text{ arcmin}}\right)^{-1} \left(\frac{D_T}{10 \text{ m}}\right)^{-1}.
\]  

(9)

Echelle spectrographs can do somewhat better by using higher orders, with a spectral resolution \( R \approx 2d_{slit} \tan \delta/\theta_{slit} D_T \), where \( \delta \) is the groove angle (e.g., Schroeder 2000). We find, with typical \( \delta \approx 63.5^\circ \),

\[
R(\text{echelle}) \approx 340 \left(\frac{d_{slit}}{1 \text{ m}}\right) \left(\frac{\theta_{slit}}{4 \text{ arcmin}}\right)^{-1} \left(\frac{D_T}{10 \text{ m}}\right)^{-1}.
\]  

(10)

Reducing the slit angular size below \( 2\theta_{PSF} \) sacrifices light from the target object, which negates the advantage of the large apertures of IACTs. In principle, this could be evaded by integral field spectroscopy, with the source image divided into many small pieces which are fed through narrow slits with fibre optics. This would require a large number of fibres to achieve high resolution; for the echelle case, \( N_{fib} \approx 870(R/10)^2(D_T/10 \text{ m})^2(\theta_{PSF}/2 \text{ arcmin})^2 \). Even higher \( R \) may be possible: VIRUS on the Hobby-Eberly Telescope demonstrates integral field spectroscopy with \( \sim 30000 \) fibres (Hill et al. 2006). However, such instruments may actually be more complicated and expensive than the Cherenkov telescope itself, and might require a dedicated IACT-like telescope. Given the extreme costs of ELTs and the applications of a high \( R \) spectrograph for even just bright sources, however, the possibility of massive integral field spectroscopy applied to source images in IACT-like telescopes warrants further investigation.
4 POLARIMETRY WITH IACTS

Polarimetry has now reached the $10^{-6}$ level with instruments like PlanetPol (Hough et al. 2006) and POLISH (Wiktorowicz & Matthews 2008). Polarimetry is typically limited by the number of photons, which IACTs excel at maximizing for bright objects.

Polarimeters work by measuring the changes in intensity as the polarization angle of transmitted light is varied (for example, by rotating a polarizer). As a model of a linear polarimeter, suppose it measures the intensity of a source parallel and perpendicular to its angle of polarization over an integration time $t_{\text{obs}}$. In practice, since we do not know the direction of linear polarization of a source (that is, we have to fit two Stokes parameters), we have to observe it at two polarizations tilted $45^\circ$ from parallel, so that the total number of photons collected is

$$N = N_\parallel + N_\perp + N_\chi + N_\gamma.$$  

The total number of photons observed for each polarization $i \in \{\parallel, \perp, \chi, \gamma\}$ is $N_{\text{obs}} = N_\parallel + N_{\text{back}}$ where $N_\parallel$ is the number of photons from the source and $N_{\text{back}}$ is the number of photons from the (sky) background. Since the sky polarization is typically large ($\sim 50$ per cent), it must be subtracted off by taking another measurement of the sky itself.

The polarimeter observes the sky background for some time $t_{\text{sky}}$, measuring $N_{\parallel\text{sky}}$ and $N_{\perp\text{sky}}$ photons from the sky; the background is then estimated as

$$N_{\text{back}} = (t_{\text{obs}}/t_{\text{sky}})N_{\parallel\text{sky}}.$$  

After sky subtraction, the degree of polarization is then

$$p_* = (N_\parallel - N_\perp)/(N_\parallel + N_\perp),$$  

or

$$p_* = \frac{[N_\parallel - \frac{t_{\text{obs}}}{t_{\text{sky}}} N_{\parallel\text{sky}}]}{[N_\parallel - \frac{t_{\text{obs}}}{t_{\text{sky}}} N_{\parallel\text{sky}}] + [N_\perp - \frac{t_{\text{obs}}}{t_{\text{sky}}} N_{\perp\text{sky}}]}.$$  

(11)

The Poisson noise in each of the measured photon numbers contributes to the noise of the measured $p_*$: $\sigma_{p_*}^2 = \sum_{j \in \{\parallel, \perp\}} \left( \frac{\partial p_*}{\partial N_{\text{obs}}^j} \sigma_{N_{\text{obs}}^j} \right)^2 + \left( \frac{\partial p_*}{\partial N_{\text{sky}}^j} \sigma_{N_{\text{sky}}^j} \right)^2$. This gives us:

$$\sigma_{p_*} = \sqrt{\sum_{j \in \{\parallel, \perp\}} 4 \frac{(N_j^2)}{(N_\parallel + N_\perp)^2} \left[ \frac{t_{\text{obs}}}{t_{\text{sky}}} \right]^2 \frac{N_j^2}{N_{\text{sky}}^2}},$$  

(12)

defining $j$ as $\perp$ when $j = \parallel$ and $\parallel$ when $j = \perp$. When both the sky and source are weakly polarized ($N \approx 4N_\parallel \approx 4N_\perp \approx 4N_\chi \approx 4N_\gamma$), $\sigma_{p_*} \approx \sqrt{2N_{\text{obs}} + (t_{\text{obs}}/t_{\text{sky}})^2 N_{\text{sky}}}/N_\parallel$. The noise can be understood to mainly arise from either sky subtraction or the observation itself:

$$\sigma_{p_*} \approx \left\{ \begin{array}{ll} \frac{t_{\text{obs}} \sqrt{2N_{\text{sky}}}}{t_{\text{sky}} N_\parallel} & (t_{\text{sky}} \lesssim t_{\text{obs}}/\sqrt{1 + N_\parallel/N_{\text{sky}}}) \\ \frac{\sqrt{2N_{\text{obs}}}}{N_\parallel} & (t_{\text{sky}} \gtrsim t_{\text{obs}}/\sqrt{1 + N_\parallel/N_{\text{sky}}}) \end{array} \right\}.$$  

(13)

Essentially, when the sky subtraction measurement is long enough, the degree of polarization of the combined source and sky can be measured to an accuracy $\sqrt{2}/N_{\text{obs}}$. If the source dominates, this is the accuracy of the source polarization measurement; if the sky dominates then the source polarization is diluted by a factor $N_{\text{sky}}/N_\parallel$, and the accuracy in the measurement is reduced. While measurements of optical circular polarization are relatively rare, they would be conceptually similar: we would simply take the difference of left-handed and right-handed photons, and with only one Stokes parameter, the noise would be $\sqrt{2}$ times smaller for the same total observation time.

Using equation (2) we can now evaluate how accurately IACTs can measure polarization, based on the photon noise and assuming the sky subtraction is sufficiently long ($t_{\text{sky}} \gtrsim t_{\text{obs}}/\sqrt{1 + N_\parallel/N_{\text{sky}}}$):

$$\sigma_{p_*} \approx \left\{ \begin{array}{ll} 8.7 \times 10^{-5} \times 10^{0.2(V-8)/\sqrt{A_{100\text{fof}}V_{\theta,5}}} & (V \lesssim V_{\text{sky}}) \\ 7.3 \times 10^{-5} \times 10^{-0.2(V_{\text{sky}}-8.36-2V+16)/\sqrt{A_{100\text{fof}}V_{\theta,5}}} & (V \gtrsim V_{\text{sky}}) \end{array} \right\}.$$  

(14)

We see the photon statistics are sufficient for a single IACT to reach $10^{-6}$ precision in one hour exposures for a V = 8 target.

The angle of linear polarization $\theta$ can also be measured, using the formula $2\theta = \tan^{-1}(u/q)$, where $u$ and $q$ are the normalised Stokes parameters. The telescope can estimate these parameters as $u = (N_\parallel - N_\perp)/(N_\parallel + N_\perp)$ and $q = (N_\parallel - N_\perp)/(N_\parallel + N_\perp)$. It can then be shown that when the sky and source polarization are weak, the photon noise introduces an uncertainty in the angle equal to the values of $\sigma_{p_*}$ in equations (13) divided by $2p_*$. If the sky exposure is long enough ($t_{\text{sky}} \gtrsim t_{\text{obs}}/\sqrt{1 + N_\parallel/N_{\text{sky}}}$), the uncertainty in the measured polarization angle due to Poisson noise is:

$$\sigma_{\theta} \approx \left\{ \begin{array}{ll} 0.25 \times 10^{0.2(V-8)/\sqrt{A_{100\text{fof}}V_{\theta,5}}}p_{0.01} & (V \lesssim V_{\text{sky}}) \\ 0.21 \times 10^{-0.2(V_{\text{sky}}-8.36-2V+16)/\sqrt{A_{100\text{fof}}V_{\theta,5}}}p_{0.01} & (V \gtrsim V_{\text{sky}}) \end{array} \right\},$$  

(15)

where $p_{0.01} = p_*/0.01$.

As with photometry, the systematics are unknown and may dominate. Because the sky is highly polarized, it will have to be subtracted to a very high precision; for comparison, Huovelin & Piirila (1990) demonstrated the ability to subtract off the sky to 1/500 precision. Hough et al. (2006) found that sky noise was negligible with 5 arcsec apertures except on moonlit nights, but an IACT would effectively have ~600 times greater sky noise. More severely, the degree and direction of polarization change with direction on the sky; this effect on sky channel observations, which would have to be at least a few arcminutes away for an IACT, would introduce some systematic errors. Fox (1992) estimate (with a sky observation 4 arcmin away and using 15 arcsec apertures) that this effect could be severe on moonlit nights for stars with $V \gtrsim 3$, although it could be much smaller on moonless nights. Furthermore, polarization induced by the Cherenkov telescopes themselves may limit polarimetry. Aluminium-coated mirrors with revolution symmetry induce a polarization signal of $\sim 3 \times 10^{-8}(\delta\theta/1 \text{ arcmin})^2$, where $\delta\theta$ is the angle between the revolution axis and the
source, if the integrated light from the entire PSF is considered (Sanchez Almeida & Martinez Pillet 1992). The individual facets of IACTs are tilted at angles of up to $\sim 10^\circ$ degrees (e.g., Bernlohr et al. 2003), so they individually induce polarizations of order $\sim 10^{-4}$ -- $10^{-3}$. However, the overall shape of an IACT primary reflector is parabolic; if the polarizations of the facets cancel each other out, the remaining polarization could be very small ($10^{-5}$ -- $10^{-7}$). These systematics need to be considered further before use of IACTs as high precision optical polarimeters. In any case, high-speed lower-precision polarimetry of bright transients like gamma-ray bursts (GRBs), seems possible with IACTs.

5 APPLICATIONS

The low angular resolution of IACTs generally makes them suitable for bright sources or small integration times, in contrast to typical ELTs which can go down to very faint magnitudes. Although this makes IACTs unsuitable for much ELT science, there are still several interesting targets of sufficient brightness that might be studied by IACTs. These span a range of different science opportunities, given below:

Occultations – Lunar occultations of bright stars are commonly used to measure stellar diameters (e.g., Richichi 1994). These measurements do not require difficult millamagnitude differential photometry, but instead rapid measurements of large magnitude changes. Indeed, Deil et al. (2009) has already shown that IACTs excel for such situations.

A more exotic possibility is occultations of bright stars by kilometre-scale Kuiper Belt Objects. Diffraction around these objects produces variability at the several percent level (e.g., Roques, Moncuquet, & Sicardy 1987, Bianco et al. 2009, Schlichting et al. 2009). The brightness fluctuation is of order a few percent and lasts a fraction of a second (e.g., Roques & Moncuquet 2000). An array of telescopes, as in most IACTs, could probe the two-dimensional structure of the diffraction pattern. In the Fresnel regime, this provides an independent measure of the occulting body’s distance; combined with the transit time, the velocity is then determined.

Exoplanets – Exoplanet transits occur when a planet occults a star from the vantage point of Earth, causing its apparent brightness to drop a small amount (1% or less for sun-like stars). They are especially periodic, occurring once per planet orbit and last for a few hours. IACTs have already conducted $\sim 1$ per cent optical photometry with the Crab pulsar (Hinton et al. 2006, Lucarelli et al. 2008), thus demonstrating in principle they can observe transits of Jupiter-sized exoplanets around sun-like stars. However, the systematics are probably different for the $\sim$ hour long observations of exoplanet transits and the sub-second Crab pulsations. IACTs are not well-suited for transit searches (at which small telescopes perform better; see Pepper, Gould, & Depoy 2003), but instead for follow-up. With their short integration times, IACTs can finely sample transit light curves for Transit Timing Variation and Transit Duration Variation studies (Miralda-Escudé 2002, Holman & Murray 2003, Agol et al. 2005). These variations are expected to be of order seconds to minutes, compared to the hour time-scales of the transit itself. If the technical challenges of differential photometry (§2.2) can be overcome and photon-limited statistics achieved, the transits of planets around giant stars (e.g., Assef, Gaudi, & Stanek 2009) or small planets around sun-like stars might be detectable.

Transiting exoplanets can also be studied spectroscopically, including detecting and characterising the atmospheres of transiting exoplanets (Brown 2001, Charbonneau et al. 2002). However, these applications generally require $R \approx 10^3$ and therefore a multi-fibre instrument to harness the light collecting power of an IACT.

Finally, IACTs could quickly collect the photons needed for detecting the polarized reflected light of an exoplanet (Seager, Whitney, & Sasselov 2000) or the changes in a star’s polarization during an exoplanet transit (Carciofi & Magalhães 2005). A claimed polarimetric detection of HD 189733b is controversial (Berdugina et al. 2008, Wiktorowicz 2009), but, if real, the detection appears to be strongest in blue bands because of Rayleigh scattering in the exoplanet’s atmosphere (Berdugina et al. 2011), and IACTs have an advantage at bluer bands where the dark sky backgrounds are lower.

Stars – The low angular resolution of IACTs limits them to the brightest and nearest stars, but IACTs remain suitable for monitoring their short time-scale photometric variability. The brightest stellar flares reach $\Delta V \approx 0.1$ and last for minutes to days (Schafer, King, & Delvannis 2006, Bentley et al. 2009). IACTs are potentially useful for binary star studies; photon-limited photometry could even be used to detect relativistic beaming effects (e.g., Loeb & Gaudi 2003, Zucker, Mazeh, & Alexander 2007).

Most nearby stars have very small intrinsic polarizations ($\lesssim 10^{-5}$), but interstellar (e.g., Tinbergen 1982, Bailey, Lucas, & Hough 2010) dust can be studied through induced polarizations. The brightest X-ray binaries, like Cygnus X-1, have $V \approx 9$, and might be studied polarimetrically by IACTs to constrain the inclination of the binary orbit (c.f. Wiktorowicz & Matthews 2008).

Gamma-ray bursts – The brightest GRBs approach or even exceed $V_{\text{sky}}$ for time periods of minutes (such as GRB080319B, peaking at $V \approx 5.3$, Racusin et al. 2008, Bloom et al. 2004). MAGIC has a fast slew time of $\lesssim 30$ seconds for anywhere on the sky (Bretz et al. 2003), while HESS and VERITAS have slew times of 2-3 minutes for any location on the sky (Hinton 2004, Huenemesky 2007). With their huge collection areas, IACTs could construct millimagnitude optical light curves of GRBs or other transients within the first few minutes of their triggers, with 100 millisecond sampling times. As has been suggested before (e.g., Beskin et al. 1999, Oña-Wilhelmi et al. 2004, Hinton et al. 2008), such observations could even be concurrent with TeV observations (e.g., Aharonian et al. 2009), if the central pixel is used for optical photometry and the remaining field of view for gamma-ray observations, as with MAGIC (Lucarelli et al. 2008).

Spectroscopy of GRBs with IACTs could rapidly constrain the redshifts and properties of gas in the host galaxy and intervening intergalactic medium. This may prove use-

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$^3$ HEGRA previously measured the polarization of Cherenkov pulses to within a few percent (Boering et al. 2001).
ful in time-dependent studies of the geometry of intergalactic metal-line absorbers on GRB sightlines (e.g., Frank et al. 2002, D’Elia et al. 2010).

Finally, the optical polarization of GRB afterglows is a powerful discriminant of emission mechanisms and the magnetic field structure in GRB afterglows (e.g., Gruzinov & Waxman 1999). Observations of afterglows on time-scales of hours to days typically find polarizations of order a few percent (e.g., Covino et al. 1999), with time-scales of hours to days typically find polarizations of order a few percent (e.g., Covino et al. 1999), with some afterglows reaching ∼ 10 per cent linear polarization (e.g., Bersier et al. 2003). However, there are few constraints on the early optical polarization of GRB afterglows; Mundell et al. (2007) found an upper limit of ∼ 8 per cent on optical polarization a few minutes after GRB 060418. IACTs can rapidly collect the photons needed for early time polarization measurements for the brightest GRBs to relatively high precisions (from eq. 14, obtained with an echelle and a single slit (eq. 10). Finally, polarimeters like PlanetPol already have demonstrated that precise polarimetry can be done with ∼ 5 arcsec apertures, even on moonlit nights (Hough et al. 2006). The downside of increased angular resolution would be that bright sources would saturate more quickly.

An IACT-like telescope in space would have many advantages. All scintillation and systematic noise due to the atmosphere would vanish. A spaceborne IACT-like telescope could therefore take full advantage of the massive light collecting power to approach "micromagnitude" photometry of V = 8 sources within a few hours of integration time. Alternatively, crude (σV ∼ 0.1) "microsecond" photometry could be achieved (c.f., Deil et al. 2009). The sky background for polarimetry would likewise mostly vanish. Herschel demonstrates that ∼ 4 metre telescopes are viable in space, and optical telescopes would need sophisticated cooling systems only for the detector. Furthermore, spaceborne telescopes would evade NIR skyglow (Leinert et al. 1998), which might prove useful in investigating secondary eclipses of exoplanets (e.g., Charbonneau et al. 2003).

6 CONCLUSIONS

Diffraction-limited ELTs have many advantages, in that they can examine faint sources necessary for studies involving areas like cosmology, distant Galactic stars, and direct imaging of exoplanets, but the telescope itself is very costly. IACTs already have achieved ELT-scale apertures and are very inexpensive, but are only effective for bright sources, and the low angular resolution means that complex instruments are necessary. For high spectral resolution optical spectroscopy in particular, the instrument may in fact be more expensive than the IACT itself. Between the two extremes, telescopes of intermediate optical quality may use simpler instrumentation while still being relatively cheap. A telescope with θ_psv = 10 arcsec, for example, would have no disadvantage down to V = 14 even on moonlit nights. The smaller source images may make techniques for high speed CCD imaging more practical (O’Donoghue 1995). Increased angular resolution would also facilitate higher R spectroscopy, up to ∼ 10^8 with an echelle and a single slit (eq. 10). Finally, polarimeters like PlanetPol already have demonstrated that precise polarimetry can be done with ∼ 5 arcsec apertures, even on moonlit nights (Hough et al. 2006). The downside of increased angular resolution would be that bright sources would saturate more quickly.

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