Quantum interference of topological states of light

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Topological insulators are materials that have a gapped bulk energy spectrum but contain protected in-gap states appearing at their surface. These states exhibit remarkable properties such as unidirectional propagation and robustness to noise that offer an opportunity to improve the performance and scalability of quantum technologies. For quantum applications, it is essential that the topological states are indistinguishable. We report high-visibility quantum interference of single-photon topological states in an integrated photonic circuit. Two topological boundary states, initially at opposite edges of a coupled waveguide array, are brought into proximity, where they interfere and undergo a beamsplitter operation. We observe Hong-Ou-Mandel interference with $93.1 \pm 2.8\%$ visibility, a hallmark nonclassical effect that is at the heart of linear optics–based quantum computation. Our work shows that it is feasible to generate and control highly indistinguishable single-photon topological states, opening pathways to enhanced photonic quantum technology with topological properties, and to study quantum effects in topological materials.

RESULTS

Our device implements the off-diagonal Harper model, which describes a 1D lattice that exhibits topological boundary states (17, 32, 33). The time-varying Hamiltonian of this model is given as

$$\hat{H}(t) = \sum_{n=1}^{N-1} \kappa_n(t) (\hat{a}_n \hat{a}^\dagger_{n+1} + \hat{a}^\dagger_n \hat{a}_{n+1})$$

where $\hat{a}_n$ and $\hat{a}^\dagger_n$ are annihilation and creation operators acting on lattice site $n$, $\kappa_n(t)$ is the coupling strength at time $t$ between site $n$ and site $n + 1$. In the off-diagonal Harper model, the coupling strengths follow the periodic function

$$\kappa_n(t) = \kappa_0 \left[1 + \Lambda(t)\cos(2\pi b n + \phi(t))\right]$$

where $\kappa_0$ is the nominal coupling coefficient between two adjacent lattice sites, $b$ controls the periodicity of the lattice, $\Lambda(t)$ controls the size of the spectral gaps and correspondingly defines the confinement of the boundary state at time $t$, and $\phi(t)$ is a time-varying phase. By carefully choosing the value of $b$, gaps appear in the energy spectrum of the system that allow topological pumping by adiabatically varying $\phi(t)$ (17). Carefully choosing $\phi(t)$ ensures the appearance of topological boundary modes on the edges of the array. Both $\phi(t)$ (17) and $\Lambda(t)$ can be used to manipulate the boundary states. Here, we vary $\Lambda(t)$ to confine, de-localize, and interfere the boundary states; this procedure is reminiscent of changing the length of a topological superconductor and interfering its Majorana modes (3).

An array of coupled waveguides in the nearest neighbor approximation implements the same tight-binding Hamiltonian as Eq. 1, where the waveguide separation controls the coupling strength. We experimentally characterized the relationship between the waveguide separation and the coupling strength $\kappa_n(t)$ (see Materials and Methods for details), which enabled us to design an array with the desired...
Hamiltonian. Because we vary the \( \kappa_n \), terms along the length of the array, we make the transformation from a time-varying to a distance-varying Hamiltonian with the relationship \( z = \frac{\tau}{c} \), where \( z \) is the position, \( c \) is the speed of light, and \( n \) is the waveguide effective refractive index.

Initially, two photonic states are localized at the edges of the array; they are spectrally and spatially isolated from the bulk modes, start with the same energy, and are spatially isolated from one another. Interference can occur when these states are adiabatically delocalized from the edges to the bulk of the lattice by reducing the bulk gap size.

We designed two devices, each consisting of 10 waveguides with symmetric coupling strengths \( \{ \kappa_1, \kappa_2, \kappa_3, \kappa_4, \kappa_5, \kappa_6, \kappa_7, \kappa_8, \kappa_9, \kappa_{10} \} \) and \( \tilde{b} = 2/3 \). The first device has fixed \( \Lambda(0) = 0.6 \) to demonstrate and confirm the confinement of the topological boundary states, as illustrated in Fig. 1A. In the second device, illustrated in Fig. 1B, we vary \( \Lambda(z) \) from \( \Lambda(0) = 0.6 \) to \( \Lambda(L/2) = 0.1 \), where \( L \) is the total length of the array. This reduces the localization of the two boundary modes, causing them to interfere. By tuning the central coupling coefficient \( (c) \), a 50:50 beamsplitter is realized before relocalizing the states to the sides of the device, where \( \Lambda(L) = 0.6 \). For both devices, waveguides 1 to 5 (and due to symmetry, 10 to 6) have five photonic supermodes (eigenstates), which are shown in Fig. 1C.

Exciting the boundary states of each array requires injecting into the mode labeled B in Fig. 1C. As shown in Fig. 1 (A and B), we achieved this by extending the two edge waveguides to the input facet of the chip (see section S1 for details). To model the bulk-band spectrum of the photonic supermodes in Fig. 1C, we calculated the eigenvalues of both devices, shown in Fig. 1 (D and E), along the length of the array. The approximate bulk energy bands are shaded in blue, and the eigenvalues corresponding to the boundary states are plotted in red (labeled B and D). As the Hamiltonian is implemented on a photonic platform, each eigenvalue is proportional to the effective refractive index of the corresponding photonic supermode (34). If eigenvalues are similar in magnitude, then the corresponding eigenstates will scatter between modes; however, eigenstates between the energy bands are resilient to scattering.

Our devices were fabricated using the direct-write technique (35, 36), as it enables high-precision control of the waveguide coupling coefficients. We implement the direct-write technique by translating a borosilicate chip while focusing a femtosecond laser into the bulk (see Methods and Materials for more details on the chip fabrication).

We characterized each device using laser light at 808 nm, to match the wavelength of our single-photon source, and measured the output with a charge-coupled device (CCD) camera. We calculated the fidelity between the measured output distribution across the whole array and the simulated result as \( F = \sum_i \sqrt{P_i^S P_i^M} \), where \( P_i^S \) (\( P_i^M \)) is the simulated (measured) intensity of light at the output of waveguide \( i \) after normalization. The intensity distribution is equivalent to the output single-photon probability distribution. Here, the simulation is based on the physical parameters of our device. We note that depicting the boundary-state supermodes (labeled B and D in Fig. 1C) as being confined to two waveguides is an approximation and, in a real device, they exponentially decay beyond the edge waveguides—this phenomenon is inherent to any bound mode in a spectral gap.

Figure 2A shows the measured output intensity and simulation results for the stationary topological boundary state when injecting into the left even-mode eigenstate, and the fidelity is \( F = 97.1% \). Figure 2B shows the results for the TBS. We measured fidelity for the left and right inputs of \( F = 96.3 \) and 97.8%, respectively. These fidelities are very high and are mainly limited by fabrication imperfections.

In the quantum interference experiment, we used a coupling setup to collect photons from the outer waveguides (1, 2, 9, 10). When selecting only these waveguides, we calculated the reflectivity of the TBS to be 49.9% (50.7%) for the left (right) input, which is very close to 50%—a requirement for high-visibility quantum interference.

Figure 3A shows our setup for measuring HOM interference. We generated pairs of photons using a free-space spontaneous parametric downconversion.
down conversion (SPDC) source before coupling into two polarization-maintaining optical fibers (PMFs). We inserted narrow-band filters to ensure that the photon wavelengths are matched and one fiber is positioned on a translation stage to enable a tunable delay (see section S2 for full details on the photon pair source). We measure the visibility of the interference by controlling the distinguishability of the photons with the tunable delay.

We first injected single photon pairs into a commercially available fiber-coupled 50:50 beamsplitter (FBS) with PMF for the input, ensuring that the photons have the same polarization when they interfere. The output fibers are coupled to APDs that emit an electrical pulse when a photon is detected. We performed coincidence measurements of the APD signals with a timing card. We measured the HOM dip, shown in Fig. 4A, with visibility $V_{\text{FBS}} = 94.5 \pm 0.5\%$. We calculated error bars on the plot using Poissonian statistics (see section S3 for HOM dip error calculation). We detected and subtracted accidental coincidences due to stray ambient light and dark counts from the signal by applying an electronic time delay to one detector. As the beamsplitter reflectivity is close to ideal ($r = 49.0 \pm 0.1\%$), the visibility is limited predominately by the spectral distinguishability of the generated photon pairs.

We then replaced the 50:50 FBS with our waveguide chip, as shown in Fig. 3B. We injected single photons simultaneously into both boundary states of the TBS and varied the delay such that we could perfectly match the arrival times. We measured the HOM dip, shown in Fig. 4B, with a visibility of $V_{\text{TBS}} = 93.1 \pm 2.8\%$; this gives a relative visibility $V_{\text{relative}} = \frac{V_{\text{TBS}}}{V_{\text{FBS}}} = 98.5 \pm 3.5\%$, confirming that the quantum interference of topological boundary states in our device is close to ideal. The measurement noise for the TBS chip is increased due to coupling losses, leading to a significantly lower count rate and, consequently, a decreased signal-to-noise ratio.

DISCUSSION

Here, we have demonstrated that single photons localized to topological boundary states can undergo high-visibility quantum interference. To this aim, we used a laser-written photonic circuit that represents one of the most complex examples of a continuous waveguide array.

Fig. 2. Characterization of the stationary boundary-state device and the TBS. We characterized the output of the chip using laser light and a CCD camera. (A) The normalized output intensity distribution of the stationary boundary state. (B and C) The normalized output intensity distribution of the TBS with injection into the left and right inputs, respectively.

Fig. 3. Experimental setup for interfering topological boundary states. (A) Setup to characterize the indistinguishability of the photon pairs generated from a SPDC source. The photons are interfered in a 50:50 beamsplitter via PMF. The output of the beamsplitter is pigtailed with single-mode fiber (SMF) connected to single-photon avalanche photodiodes (APDs). We measured coincidence counts between the two detectors with a timing card. CW, continuous wave; BiBO, bismuth triborate. (B) To perform the indistinguishability measurements of single photon topologically protected states, we replaced the pigtailed beamsplitter in (A) with the TBS device. We used PMF, multimode fibers (MMFs), and free-space lenses to couple photons to the device.
with engineered coupling coefficients varying along the propagation direction. This technology enables future studies of quantum effects in topological materials that are challenging or impossible to probe due to, for example, large magnetic field requirements or excessive noise (2). Moreover, the TBS could be extended to other topological models such as the Su, Schrieffer, and Heeger model of a 1D dimer chain (37). We anticipate that the TBS presented in this work will combine with other leading work in topological photonics (8, 22) to help solve challenges currently faced in quantum photonics, including pump filtering for photon generation and robust photon transport.

MATERIALS AND METHODS

Device design and simulation

The relationship between waveguide separation and coupling coefficient is characterized with a test chip containing varying spaced waveguides. This relationship follows an exponential decay \( \kappa = ae^{-bd} \), where \( a = 115 \text{ cm}^{-1} \) and \( b = 0.36 \text{ mm}^{-1} \) are experimentally measured constants and \( d \) is the separation between the waveguides. We can invert this function to find the waveguide separation necessary to achieve the desired coupling coefficients in Eq. 2. These \( \kappa_n(z) \) coupling coefficients control the transfer of the topological boundary state from the sides of the array to the center.

We numerically optimized the coupling coefficient \( c \) in Eq. 1 such that the boundary states couple with 50% probability. This implements a 50:50 beamsplitter operation. Finally, the waveguide separations were adjusted to transfer the boundary states back to the sides of the array.

Device fabrication

We used the femtosecond direct-write technique for fabricating waveguides in borosilicate glass (35, 36). Our SPDC source generates photons close to the 808-nm wavelength, and we fabricated waveguides that are single mode at this wavelength. The waveguides were fabricated by focusing a femtosecond-pulsed laser with a repetition rate of 1 MHz and energy of 220 nJ per pulse in the bulk of a borosilicate substrate (Eagle2000, Corning) by means of a 50x microscope objective (numerical aperture, 0.6). Waveguides were patterned by translating the sample at the constant speed of 40 mm/s. The resulting waveguides exhibit relatively low propagation losses (0.5 dB/cm) and a slightly elliptical guided mode, with an average diameter of ~8 μm.

The separation between neighboring waveguides controls the rate of coupling. There is, inevitably, coupling between next-nearest-neighbor waveguides; however, the coupling decays exponentially with distance, and hence, we can approximate to a nearest-neighbor model.

SUPPLEMENTARY MATERIALS

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/4/9/eaat3187/DC1

Section S1. Experimental setup

Section S2. SPDC source

Section S3. HOM interference on the TBS with a visibility of 93.1 ± 2.8%. The error bars shown are based on Poissonian statistics.

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