Active Transonic Aerofoil Design Optimization Using Robust Multiobjective Evolutionary Algorithms

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The use of adaptive wing/aerofoil designs is being considered, as they are promising techniques in aeronautic/aerospace since they can reduce aircraft emissions and improve aerodynamic performance of manned or unmanned aircraft. This paper investigates the robust design and optimization for one type of adaptive technique: active flow control bump at transonic flow conditions on a natural laminar flow aerofoil. The concept of using shock control bump is to control supersonic flow on the suction/pressure side of natural laminar flow aerofoil that leads to delaying shock occurrence (weakening its strength) or boundary-layer separation. Such an active flow control technique reduces total drag at transonic speeds due to reduction of wave drag. The location of boundary-layer transition can influence the position and structure of the supersonic shock on the suction/pressure side of aerofoil. The boundary-layer transition position is considered as an uncertainty design parameter in aerodynamic design due to the many factors, such as surface contamination or surface erosion. This paper studies the shock-control-bump shape design optimization using robust evolutionary algorithms with uncertainty in boundary-layer transition locations. The optimization method is based on a canonical evolution strategy and incorporates the concepts of hierarchical topology, parallel computing, and asynchronous evaluation. Two test cases are conducted: the first test assumes the boundary-layer transition position is at 45% of chord from the leading edge, and the second test considers robust design optimization for the shock control bump at the variability of boundary-layer transition positions. The numerical result shows that the optimization method coupled to uncertainty design techniques produces Pareto optimal shock-control-bump shapes, which have low sensitivity and high aerodynamic performance while having significant total drag reduction.

Nomenclature

c = chord
C_l = lift coefficient
C_p = pressure coefficient
C_{d_{total}} = total coefficient, C_{d_{viscous}} + C_{d_{wave}}
C_{d_{viscous}} = viscous drag coefficient
C_{d_{wave}} = wave drag coefficient
f = fitness functions
K = number of uncertainty step size
Re = Reynolds number
SCB_H = height of shock control bump (%c)
SCB_L = length of shock control bump (%c)
SCB_P = peak position of shock control bump (%SCB_L)
α = angle of attack

I. Introduction

In engineering designs, it is inevitable to face uncertainty design parameters that must be considered in an optimization task to produce a set of reliable optimal solutions (high performance and low sensitivity). Some of the design variables and system input parameters cannot be achieved exactly due to uncertainties in physical quantities such as manufacturing tolerances, material properties, and environmental conditions, including temperature, pressure, velocity, etc. In conventional design, these parameters are treated as a constant value with assumption. The design model obtained by conventional design methods has good performance at the standard design point; however, using fixed/constant values for uncertain parameters makes a design model fluctuate at offdesign conditions. In other words, the design model has high sensitivity at a set of unstable conditions that produces an unstable performance [1,2]. An alternative design strategy is the use of robust design when considering uncertainty design parameters to control the sensitivity and performance of the model [3,4]. In this paper, an active flow control (AFC) device design is considered as a robust optimization application.

One of the important challenges in aeronautical engineering is to control flow over the aerofoil/wing to reduce drag while increasing lift. One of the main reasons is that the drag reduction can save mission operating costs, condense critical aircraft emissions, and increase the performance envelope of the aircraft. Such drag reduction can be achieved by implementing a type of AFC called shock control bump (SCB) [5–8] without the need to design a new aerofoil or wing planform shape.

In this paper, a natural laminar flow (NFL) aerofoil, the Royal Aircraft Establishment (RAE) 5243 (used as a baseline design), is investigated with SCB on the suction side to reduce total drag and to
extend its critical Mach and lift coefficients at high lift coefficient and transonic flow speeds. Two optimization test cases are conducted using advanced evolutionary algorithms (EAs) [9], and the first test considers a boundary-layer transition (BLT) (note that, in aerodynamics, BLT is often used as \( x_{tr} \) position at 45% of chord). The second test is conducted with uncertainty design parameters, the variability of BLT positions, and lift coefficient values using a robust/uncertainty design technique. In conventional design, aerofoil optimization is conducted at a fixed/constant BLT position. However, BLT cannot be assumed as a constant value in a real design problem, especially for the AFC device design since the shape of AFC device will change the position of BLT. Therefore, the BLT location is considered as one of the uncertainty design parameters.

The paper will show how to control the design quality while considering uncertain design parameters, and it will demonstrate how to control the transonic flow on the current aerofoil using a SCB.

The rest of the paper is organized as follows. Section II describes the robust/uncertainty design methods. Section III describes the use of SCB. Section IV considers SCB shape design dynamic analysis tools are described in Sec. III. Section V demonstrates the use of SCB. The rest of the paper is organized as follows. Section II describes the robust/uncertainty design methods.
supersonic flow to decelerate to subsonic Mach numbers by a weaker shock wave, which leads to lower wave drag.

V. Active Flow Control Bump (Shock Control Bump) Design Optimization

The NLF aerofoil, RAE 5243 [6], is selected as a baseline design. The aerofoil has a maximum thickness of 0.14 at 41% c from the leading edge and a maximum camber of 0.0186 at 54% c. The baseline design is tested at flow conditions $M_{\infty} = 0.136$, $C_l = 0.82$, and $Re = 19.0 \times 10^6$, with a BLT position at 45% of chord from the leading edge. The shock occurs at 59.5% of chord, where a BLT position is at 45% c. This baseline design will be compared with the optimal SCB designed to minimize the total drag $C_{d_{\text{Total}}}$ in Secs. V.A and V.B.

A. Shock-Control-Bump Shape Design Optimization with Boundary-Layer Transition Position at 45% c

1. Problem Definition

This test case considers a single-objective SCB design optimization on the upper surface of the RAE 5243 aerofoil to minimize the total drag at flow conditions $M_{\infty} = 0.68$, $C_l = 0.82$, and $Re = 19.0 \times 10^6$ with BLT position at 45% c from the leading edge. The fitness function is shown in Eq. (6):

$$\text{fitness } (f) = \min(C_{d_{\text{Total}}}) = \min(C_{d_{\text{Viscous}}} + C_{d_{\text{Wave}}})$$

2. Design Variables

The design variable bounds for the SCB geometry are illustrated in Table 1. The center of the SCB (50% of SCB length) will be located at the shock where the flow speed transits from supersonic to subsonic (60% of chord in this case). The SCB spans from approximately 45% of chord to 75% of chord if the SCB length is 30% of chord. The maximum length of SCB is limited to 30% c to prevent the SCB overlap and aileron control surfaces, which are usually located from 75% c to trailing edge (100% c).

3. Implementation

The optimization was computed using HAPMOEA coupled to MSES using a single 4 x 2.8 GHz processor with the following details on multiresolution/population hierarchical populations [7]:

1) The first layer has a population size of 10 with a computational grid of 36 x 213 points (node0).
2) The second layer has a population size of 20 with a computational grid of 24 x 131 points (node1 and node2).
3) The third layer has a population size of 30 with a computational grid of 36 x 111 points (node3 ~ node6).

Note that the difference in accuracy between the first and the third layers is less than 5%.

4. Numerical Results

The algorithm was allowed to run for 24 h (as time stopping criterion) and for 6135 function evaluations. Convergence occurred after 1826 function evaluations (7.6 h), as shown in Fig. 4.

![Fig. 2 Comparison of aerofoil without (left) and with SCB (right).](image1)

![Fig. 3 Cp contour obtained by RA E5243.](image2)

![Fig. 4 Convergence objective for SCB design at 45% c BLT.](image3)
Table 2 compares the aerodynamic characteristics obtained by the baseline design (RAE 5243) and the baseline design with upper SCB. It can be seen that applying SCB on the upper surface of an RAE 5243 aerofoil reduces the wave drag by 95%, which leads to 40% of the total drag reduction. This optimal SCB improves L/D by 65%.

The design variables for the optimal SCB are shown in Table 3. Figure 5 compares the geometry of the baseline design and the baseline design with optimal SCB. The baseline design with SCB starts to produce lower total drag when the Mach number is higher than 0.67. By adding the optimal SCB, the baseline design reduces its total drag by 40% and its wave drag by 40% of the total drag reduction. This optimal SCB improves the wave drag by 65%.

Table 2 Aerodynamic characteristics obtained by single-objective design approach

| Aerofoil            | C_{d_{total}} | C_{d_{wave}} | L/D   |
|---------------------|---------------|--------------|-------|
| Baseline (RAE 5243) | 0.01003       | 0.0032       | 81.72 |
| with optimal SCB    | 0.00609 (-40%)| 0.00014 (-95%)| 134.56 (+65%) |

C_{i} is fixed to 0.82.

Table 3 Optimal SCB design components

| Variables | SCB     |
|-----------|---------|
| SCB_{x}, %c | 29.22   |
| SCB_{y}, %c | 1.04    |
| SCB_{z} (%SCB_{y}) | 67.7    |

Peak position SCB_{z} is in percentage of SCB length; and the optimal SCB is located between x = 0.4516, y = 0.0858 and x = 0.7440, y = 0.0475.

optimal solution is an overoptimized solution that does not perform well before reaching the standard flow/flight conditions. Such a fluctuation should be treated as uncertainty in the design parameters, and the design engineer should take into account during the optimization. Therefore, it is necessary to use an uncertainty design technique to produce a set of solutions that have both low mean and sensitivity C_{d_{total}} by considering variable C_{i} values and BLT positions.

B. Robust Shock-Control-Bump Shape Design Optimization with Uncertainty in Boundary-Layer Transition Locations

1. Problem Definition

This test case considers a robust multiobjective SCB design optimization on the upper surface of the RAE 5243 aerofoil to minimize mean and standard deviation of total drag (C_{d_{total}} and σC_{d_{total}}) at the flight conditions M_{\infty} = 0.68 and Re = 19.0 \times 10^{6}. For uncertainty design parameters, two C_{i} and three BLT positions are considered: that is, C_{i} = [0.7, 0.82] and BLT = [25\%c, 37.5\%c, 50\%c]. These can be statistically written as BLT = 37.5\%c and rBLT = 12.5\%c. The candidate SCB model will be evaluated at six flight conditions (these BLT positions \times 2C_{i} values), as shown in Table 4. The fitness functions are shown in Eqs. (7) and (8), respectively.

\[ C_{d_{total}} \]

\[ C_{d_{wave}} \]

\[ L/D \]

Fig. 5 Baseline design with optimal SCB at 45\%c BLT (SO denotes single objective).

Fig. 6 C_{i} contour: a) C_{i} distribution and b) obtained by RAE 5243 with the optimal SCB at 45\%c BLT position.
\[ f_2 = \min(\sigma C_{d_{\text{Total}}}) = \sqrt{\frac{1}{n \times m} \sum_{i=1}^{n} \sum_{j=1}^{m} (C_{d_{\text{Total}i}} - C_{d_{\text{Total}}})^2} \quad (8) \]

where \( n \) and \( m \) represent the number of BLT positions and \( C_l \) conditions.

2. Design Variables

The design variable bounds for the SCB geometry were illustrated in Table 1. The center of the SCB (50% of SCB length) will be located at the sonic point where the flow speed transits from supersonic to subsonic (58% of chord) at 37.5% of BLT. The SCB will be located between 43% to 73% of chord if SCB length is 30% of chord.

3. Implementation

The optimization was computed using HAPMOEA coupled to MSES with the following details on multiresolution/population hierarchical populations [7]:

1) The first layer has a population size of 15 with a computational grid of 36 x 213 points (node0).
2) The second layer has a population size of 20 with a computational grid of 24 x 131 points (node1 and node2).
3) The third layer has a population size of 40 with a computational grid of 36 x 111 points (node3 ~ node6).

Note that the difference in accuracy between the first and third layers is less than 5%.

4. Numerical Results

The algorithm was allowed to run for 50 h and 2450 function evaluations using a single 4 x 2.8 GHz processor. Pareto optimal solutions are shown in Fig. 9, and their sensitivity and performance are compared with the baseline design and the optimal design from the single-objective approach (Sec. V.A). It can be seen that all Pareto members dominate the baseline for the second fitness function (standard deviation of \( C_{d_{\text{Total}}} \)), while Pareto members 1 to 9 dominate the baseline design in terms of mean and standard deviation of \( C_{d_{\text{Total}}} \). Pareto members 1 to 3 dominate the optimal design from Sec. V.A. Pareto members 1 and 3 are selected to compare aerodynamic performance with the baseline design and the optimal solution from Sec. V.A.

Table 5 compares the aerodynamic characteristics obtained by the baseline design (RAE 5243) and the baseline design with SCB obtained by Pareto members 1 and 3. It can be seen that applying the

### Table 4 Variability of flight conditions (three BLT positions x 2\( C_l \))

| BLT position, %c | Flight condition 1 | Flight condition 2 | Flight condition 3 | Flight condition 4 | Flight condition 5 | Flight condition 6 |
|------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| \( C_l \)       | 0.7                | 0.82               | 0.7                | 0.82               | 0.7                | 0.82               |
optimal SCB obtained by Pareto member 1 on the suction side of the RAE 5243 aerofoil reduces the mean total drag by 24%. This optimal SCB improves $L/D$ by 32.0%.

The mean and standard deviations obtained by the baseline design, single-objective, and robust Pareto members can be compared using cumulative distribution function (CDF) and the probability density function (PDF). Figure 10a shows the CDF obtained by the baseline design, the optimal from the single-objective design (marked as SO optimal in figure), and the robust compromise Pareto solutions (marked as robust CS). It can be seen that all solutions obtained by single-objective and robust design methods have lower mean total drag when compared with the baseline design. Pareto member 1 reduces the mean total drag by 24% when compared with the baseline, while the optimal obtained by the single-objective approach reduces total drag by 17%. The standard deviation (sensitivity) can be represented by evaluating the gradient of the lines to the CDF value of 0.5 or 1 (steep gradient = low sensitivity). The PDF is plotted in Fig. 10b to have a clear sensitivity comparison between the baseline design and the single-objective approach.

For the detailed sensitivity analysis, the baseline design, the single-objective approach, and Pareto members 1 to 3 are considered. Table 6 compares the sensitivity with respect to the variability of BLT positions and lift conditions (BLT location and lift coefficient). Applying the optimal SCB obtained by Pareto member 1 produces 26% lower total drag compared with the baseline design. The sensitivity obtained by the baseline design and all solutions is more than 2.5 times lower due to the increment of the number of uncertainty design conditions from 6 to 500. In addition, Fig. 11 compares mean and standard deviation using CDF and PDF.

One thing can be noticed is that $Cd_{\text{Total}}$ and $\sigma Cd_{\text{Total}}$ behaviors obtained by the CDF and PDF (shown in Fig. 10) considering six uncertain flight conditions are similar to the $Cd_{\text{Total}}$ and $\sigma Cd_{\text{Total}}$ obtained by the CDF and PDF (shown in Fig. 11) considering 500 flight conditions between the baseline design and Pareto members 1 to 3. In other words, the simplified robust method with six uncertain flight conditions still produces both lower total mean drag and drag sensitivity with respect to the variability of BLT positions and lift coefficient.

Table 5 shows that the length and height of SCB are reduced by approximately 5% and 4% respectively, when compared with the optimal solution from Sec. V.A (Table 3). Figure 12 compares the geometry of the baseline design and the baseline with optimal SCBs. The baseline (RAE 5243) design with

| Table 5: Comparison of fitness values obtained by robust design approach |
|-------------------------|-------------------------|-------------------------|
| Aerofoil                | $Cd_{\text{Total}}$     | $\sigma Cd_{\text{Total}}$ | $L/D$   |
| Baseline                | 0.00935                 | 0.00245                 | 87.70   |
| Optimal solution (Sec. V.A) | 0.00780 (−17%)          | 0.00219 (−11%)          | 105.13 (+20%) |
| with Pareto member 1/SCB | 0.00709 (−24%)          | 0.00185 (−24%)          | 115.66 (+32%) |
| with Pareto member 2/SCB | 0.00728 (−22%)          | 0.00158 (−35%)          | 112.64 (+28%) |
| with Pareto member 3/SCB | 0.00764 (−18%)          | 0.00145 (−41%)          | 107.33 (+22%) |
SCB obtained by Pareto member 1 has a maximum thickness of 0.14 \((t/c_{\text{max}} = 0.14)\) at 41%\(c\) from the leading edge and a maximum camber 0.0205 at 62.5%\(c\). Adding the SCB obtained by Pareto member 1 increases the maximum camber by 0.002, and its position is moved toward the trailing edge by 8.5%\(c\) while keeping the same maximum thickness as the baseline design.

Figures 13a and 13b show the pressure contour and distribution obtained by the baseline design and Pareto member 1 at 45%\(c\) BLT position. It can be seen that the strong shock on the baseline design shown in Fig. 3 is 77% weaker by adding SCB on the suction side.

The SCB for Pareto member 1 reduces the total drag by 35% and improves the lift-to-drag ratio by 53%. In addition, the shock (Fig. 3) is now moved toward the trailing edge by 2.0%\(c\).

Figure 14a compares the total drag \(C_{\text{d,Total}}\) distributions obtained by the baseline design, the optimal solution obtained in Sec. V.A, and Pareto members 1–4. The flight conditions are \(M_1 = 0.67\), \(Re = 19.0 \times 10^6\), and the BLT position at 45%\(c\). It can be seen that all solutions obtained by the single-objective and robust design methods have lower total drag when the Mach number is higher than 0.67. The optimal solution from Sec. V.A produces lower total drag \((-40\%)\) at Mach number 0.68, and Pareto members 1 and 4 reduce the total drag by 35 to 27%, respectively. Pareto member 1 has lower drag compared with other solutions when Mach is lower than 0.6775, while Pareto member 4 produces lower drag when Mach is higher than 0.685. The drag divergence Mach
number for the baseline design ($M_c = 0.66$) is extended to 0.69 by applying the optimal SCB obtained by the single-objective and robust design methods.

Figure 14b compares total drag $C_{d_{\text{Total}}}$ distributions at the flow conditions $C_l \in [0.1:1.1]$ with $M_{\text{Fixed}} = 0.68$, $Re = 19.0 \times 10^6$, and the BLT position at 45% $c$. Even though the optimal solution obtained by the single-objective method produces lower total drag, Pareto members 1–4 have a stable total drag distribution at $C_l$ range [0.6:0.82] without fluctuation due to the stable wave drag. The drag divergence $C_l$ number for the baseline design ($C_{l_{\infty}} = 0.5$) is extended to 0.8–0.9 by applying the optimal SCB obtained by the single-objective and robust design methods.

Figure 14c compares wave drag $C_{d_{\text{Wave}}}$ distributions obtained by the baseline design and single-objective and robust design methods. It can be seen that Pareto members 1–4 produce a stable wave drag when compared with the baseline design and the optimal solution obtained by the single-objective approach.

Figure 15a compares the total drag distributions at a range of Mach numbers; that is, $M_c \in [0.5:0.75]$ with $C_{l_{\text{Fixed}}} = 0.82$, $Re = 19.0 \times 10^6$, and the BLT position at 25% $c$. The optimal solution obtained in Sec. V.A and Pareto members 1–4 produce lower total drag compared with the baseline design when the Mach number is higher than 0.665. The optimal solution (Sec. V.A), Pareto members 1 and 4 reduce the total drag by 25, 24, and 23%, respectively, when compared with the...
baseline design. Pareto member 1 has lower drag when Mach is lower than 0.6775, while Pareto member 4 has lower drag when Mach is lower than 0.685. The drag divergence Mach number for the baseline design \( (M_c = 0.66) \) is extended to 0.685 by applying the optimal SCB obtained by the single-objective and robust design methods.

Figure 15b compares total drag distributions at a range of \( C_l \); that is, \( C_l \in [0.1:1.1] \) with \( M_{\text{Fixed}} = 0.68, Re = 19.0 \times 10^6 \), and the BLT at 25\(^\circ\)C. The optimal solution from Sec. V.A fluctuates at the range of \( C_l \in [0.6:0.82] \), while Pareto members 1 and 4 have a stable \( C_l \) distribution. The drag divergence \( C_l \) number for the baseline design \( (C_{l_0} = 0.6) \) is extended to 0.8 by applying the optimal SCB obtained by the single-objective and robust design methods.

Figure 15c compares wave drag \( C_{d\text{wave}} \) distributions obtained by the baseline design and the single-objective and robust design methods. It can be clearly seen that Pareto members 1–4 produce stable wave drag when compared with the baseline design and single-objective approach. It should be noticed that the critical lift coefficient numbers \( C_{l_0} \) for the baseline design, the optimal solution obtained by the single-objective approach, and the Pareto members obtained by the robust design method are 0.3, 0.4, and 0.5, respectively.

The baseline design with the optimal SCB obtained by the single-objective and robust design methods are also tested at six normal flight conditions, shown in Table 8.

The histogram shown in Fig. 16 compares the total drag obtained by the baseline design and the single-objective (Sec. V.A) and robust design approaches. It can be seen that the baseline design with the optimal SCB obtained by the robust design (denoted as robust MP1) produces lower total drag when compared with the baseline design and the optimal SCB obtained by the single-objective method. The optimal SCB/Pareto member 4 reduces the total mean drag by 36\% while lowering the total drag sensitivity by 77\%. The optimal SCB obtained in Sec. V.A reduces the total mean drag and sensitivity by 99\% and 48\%, respectively, even though it produces higher drag at flight conditions 1, 3, and 5. Figure 17 compares the lift-to-drag ratio obtained by the baseline design, the optimal SCB from Sec. V.A, and Pareto member 1. It can be seen that Pareto member 1 has the biggest lift-to-drag improvement at flight condition 4. The pressure coefficient distributions at six flight conditions are shown in Figs. A1-A6.

One example (Cond4 from Fig. 17) is shown in Fig. 18, where the pressure contours obtained by the baseline design and Pareto member 1 are illustrated. Even though the SCB obtained by Pareto member 1 is optimized at the critical flight condition, the optimal SCB/Pareto member 1 reduces the wave drag \( (C_{d\text{wave}} = 0.0025) \) obtained by the baseline design by 99.5\% \( (C_{d\text{wave}} = 0.00001) \) and reduces the total drag by 40\%, which leads to 65\% improvement of \( L/D \) when compared with the baseline design.

To summarize the design test cases (Secs. V.A and V.B), the design engineer can choose one of the solutions (Pareto members 1 to 4) obtained by the robust multiobjective design optimization due to two main reasons. The first is that, even though the optimal solution from Sec. V.A produces lower total drag at the standard/mean flight conditions (BLT position at 45\(^\circ\)C), Pareto members 1 to 4 have lower sensitivity at the variability of \( C_l \) and BLT positions [25\%c:50\%c]. In addition, it is clearly shown that applying SCB

### Table 8 Six flight conditions

| Conditions | \( M_{\text{sc}} \) | \( Re \) | \( C_l \) | \( x_{\text{Trans}}-\text{Upper} \) | \( x_{\text{Trans}}-\text{Lower} \) |
|-----------|-----------------|--------|---------|-----------------|-----------------|
| Flight condition 1 | 0.69 | \( 11.7 \times 10^6 \) | 0.54 | 0.51 | 0.54 |
| Flight condition 2 | 0.69 | \( 11.7 \times 10^6 \) | 0.69 | 0.51 | 0.54 |
| Flight condition 3 | 0.70 | \( 11.7 \times 10^6 \) | 0.38 | 0.51 | 0.54 |
| Flight condition 4 | 0.70 | \( 11.7 \times 10^6 \) | 0.50 | 0.51 | 0.54 |
| Flight condition 5 | 0.73 | \( 11.7 \times 10^6 \) | 0.22 | 0.51 | 0.54 |
| Flight condition 6 | 0.73 | \( 11.7 \times 10^6 \) | 0.34 | 0.51 | 0.54 |
obtained by the robust design method stabilizes the total drag of the baseline design at both normal and critical flight conditions. The second is that Pareto members 1 to 4 have a smaller SCB than the optimal solution obtained by the single-objective method. In other words, the manufacturer can save material and weight costs, and fewer modifications are needed to the manufacturing system.

VI. Discussion

This paper explored the practical applications of MOEA with uncertainty for SCB shape optimization. The results from two test cases raise two discussion points and possible research avenues:

1) In this paper, a simplified robust design technique considering only six uncertainty flight conditions is used, and the obtained optimal solutions produce very similar statistical (CDF and PDF) behavior when compared with the CDF and PDF curves obtained by considering the 500 uncertainty flight conditions. In other words, even though it is desirable to use a detailed robust design technique with more than 100 samplings for uncertainties conditions, this simplified robust method can be applied to a preliminary robust design optimization with low computational cost to find a set of designs that have higher mean performance and lower sensitivity. As ongoing research focuses on applying the concept of hierarchical asynchronous approach for not only using low/middle flow solvers but also using detailed/intermediate/preliminary robust design methods to save a computational cost.

2) The first discussion point on SCB design variation is that the algorithm considers only three control points, which may not be enough to capture the best SCB geometry. Therefore, more than three control points need to be considered for a detailed SCB design optimization. The second point is that the two test cases considered aerodynamic performance only, without any structural aspects. Even though SCB produces significant drag reduction, this can cause an unstable structure. The current work focuses on a multidisciplinary (aerostructure) design optimization implementation.

VII. Conclusions

In this paper, the robust evolutionary optimization technique has been implemented for the case of SCB wing/aerofoils that use AFC bump designs was developed. Analytical research shows the benefits of the coupling optimization method with robust design techniques to produce stable and high performance solutions. The use of SCB on an existing aerofoil can reduce significant transonic drag, which will save operating and manufacturing costs as well as emission reduction. Future work will focus on robust design optimization of SCB on a three-dimensional wing.

Appendix

Fig. A1 $C_p$ distribution comparison at flight condition 1 (shown in Table 8).

Fig. A2 $C_p$ distribution comparison at flight condition 2 (shown in Table 8).

Fig. A3 $C_p$ distribution comparison at flight condition 3 (shown in Table 8).

Fig. A4 $C_p$ distribution comparison at flight condition 4 (shown in Table 8).
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**Data available at http://www.mit.jyu.fi/scoma/DBW2010/ [retrieved 2011].