Know Your Personalization: Learning Topic level Personalization in Online Services

Anirban Majumder
Bell Labs Research, Bangalore, India
anirban.majumder@alcatel-lucent.com

Nisheeth Shrivastava
Bell Labs Research, Bangalore, India
nisheeth.shrivastava@alcatel-lucent.com

ABSTRACT
Online service platforms (OSP), such as search engines, news-websites, ad-providers, etc., serve highly personalized content to the user, based on the profile extracted from her history with the OSP. Although personalization (generally) leads to a better user experience, it also raises privacy concerns for the user—she does not know what is present in her profile and more importantly, what is being used to personalize her content. In this paper, we capture OSP’s personalization for an user in a new data structure called the personalization vector (η), which is a weighted vector over a set of topics, and present efficient algorithms to learn it.

Our approach treats OSPs as black-boxes, and extracts η by mining only their output, specifically, the personalized (for an user) and vanilla (without any user information) contents served, and the differences in these content. We believe that such treatment of OSP’s is a unique aspect of our work, not just enabling access to (so far hidden) profiles in OSPs, but also providing a novel and practical approach for retrieving information from OSPs by mining differences in their outputs.

We formulate a new model called Latent Topic Personalization (LTP) that captures the personalization vector in a learning framework and present efficient inference algorithms for determining it. We perform extensive experiments targeting search engine personalization, using data from both real Google users and synthetic setup. Our results indicate that LTP achieves high accuracy (R-pre = 84%) in discovering personalized topics. For Google data, our qualitative results demonstrate that the topics determined by LTP for a user correspond well to his ad-categories determined by Google.

Categories and Subject Descriptors
H.2.8 [Database Management]: Database Applications—Data mining

Keywords
personalization; online service providers; topic modeling

1. INTRODUCTION
Personalization is being used by most on-line service platforms (OSP) such as search, advertising, shopping etc. Their goal is to lure users by offering a better service experience customized to their individual interests. A popular trend is to employ profile based personalization, where OSPs build extensive profiles for the user (based on her past interactions such as search queries, browsing history, links shared, etc.) and personalize content using this profile. Several popular services employ such personalization, e.g. search results, movie recommendations, etc.

While OSPs track rich user data in their histories alone, they can infer much more information about them by mining this raw data. Informally speaking, OSPs can determine a user’s interests and biases on different categories, which can later be used (along with the history) for personalizing content for her. For example (see [20] for details), Google is shown to have inferred users political affiliations (republican or democratic) and use it to re-rank search results.

For a user, this raises a significant privacy concern—she does not know what was tracked in her history, what has been inferred, and more importantly, is currently being used to personalize her content. Moreover, as both the personalization techniques and the data they operate on are the key differentiators for the OSPs (their secret sauce), they do not reveal either of them, making it even harder for an user to understand how personalization is being done (for her).

In this paper, we aim at extracting a user’s profile from the OSP. We model this profile as a weighted personalization vector over topics, where the weight on a topic indicates her interest in it (higher means more interested). Informally, a topic is any concept or phenomenon that the user could be interested in, e.g. a specific sport, preference over cuisines, favorite author, movie genre, etc.

Our goal is not to reverse-engineer the OSP’s inference algorithms. In fact, we treat the OSP as a black-box and assume that we only have access to its output, i.e. the (personalized) content served by the OSP to a user on different queries. The central idea in our approach is to get both personalized content (served for the user) and vanilla content (served for a new/not logged in user) for the same query and analyze their differences. Through careful inspection of

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1 http://privacy.microsoft.com/en-us/Bing.mspx
2 http://support.google.com/websearch/bin/answer.py?answer=1710607
3 Netflix: http://www.netflixprize.com
4 More specifically, we define it as a distribution over bag of words, a common definition in the topic modeling literature (see Section 3).
5 The query could point to a static page, e.g. reviews and other information on a movie, or dynamically generated, e.g. search results.
these two types of content, we identify the hidden user profile (summarized through a weighted set of topics) used by the OSP to serve personalized content.

There is very little concrete information available on the techniques the OSPs use to personalize content. Our paper provides a novel approach to tackle this problem, giving insights into the hidden user profiles without the knowledge of the specific inference techniques used by the OSP or the history of the user. We believe that this idea of comparing the differences in output to extract the hidden personalized topics is a unique aspect of our paper and opens a new direction in privacy research that can be aimed at commercial OSPs.

As an example, consider the case of a search engine. For any search query, we can get the personalized and vanilla results by making the query from a browser with and without logging in, respectively. These results are basically two ranked lists with some urls in the latter moved up or down in the former (i.e. re-ranked), based on the user’s profile. We study these re-rankings over multiple queries and determine the topics of interest for the user that can best explain these differences.

For the rest of the paper, we focus our attention on search engine personalization. However, our techniques can easily be extended to other services where a) we can observe both vanilla and personalized content and b) the content is offered as ranked lists of items (e.g. urls, movies, products, etc.). For example, we can apply it to movie recommendations by Netflix based on the personalized (and vanilla) ranked list of related movies presented when a user visits a particular movie page.

1.1 Search Personalization and Re-ranking

Although the exact details of personalization for search engines are not publically available, recent works in the web search community have thrown some light on them [8, 23, 18]. The common underlying theme for these techniques is to first populate the vanilla result using the semantics of the query string and then personalize it by re-arranging the items in this list, using the profile information. Therefore, conceptually, the vanilla and personalized contents are re-ordering of the same set of items. We take advantage of this re-ranking of results to determine the topics present in the user’s profile with the OSP.

It is important to observe that the assumption of vanilla and personalized results being re-rankings of same set of urls, does not preclude the generality of our approach. This assumption can easily be lifted by simply adding the extra urls in one list to the end of the other list. The important point is that personalization, by definition, will affect the ranks of the results shown, which is what we use in this paper.

Note that the topics that we learn may not be explicitly maintained by the search engine (or an OSP in general); in fact their profile data could consist of parameters completely unrelated to, and may not even map to, our definition of topics. Our paper hinges on the intuition that a user profile can be succinctly captured by a set of topics that reflects her interests. Any search engine (or OSP) that personalizes results based on her interests must give higher preference to the results matching these topics. Thus our approach of finding topic-level personalization is fairly generic—it can work with OSPs who do not necessarily maintain topic-based profiles of users and without the knowledge of the inference algorithms they use.

An alternate approach to recreate the user profile could be via mining the inputs to the search engine (i.e. the user’s search query logs, results clicked, browsing history etc.) [8, 23, 22]. However, this approach has several shortcomings compared to us. First of all, it is very hard to catch up to the commercial techniques used by OSPs that are usually more advanced and rapidly evolving. Secondly, due to the proprietary nature of OSPs, it is not clear what algorithm or even what part of the history is being used by them. Finally, in many cases the history information may not be available publicly (i.e. while a Google user’s search history is available, past ads served are not), limiting the effectiveness of these approaches. In contrast, our approach is agnostic to OSP’s personalization scheme and can work even when the history is not public.

1.2 Our Contributions

The main contributions of the paper are as follows.

- We propose a new direction in privacy research that gives users a glimpse of their profile information being used by commercial OSPs to serve personalized content. We formally capture this information as a personalization vector over topics that provides a concise and accurate summary of the user profile.
- We propose a novel way to compute this personalization vector based on the personalized and vanilla content served by an OSP. This formulation treats the OSP as a black-box and hence can work with a variety of on-line services. We believe that this is a unique aspect of our work and can open a new direction for privacy research by enabling access to (so far hidden) profile information in OSPs.
- We present a probabilistic model (named Latent Topic Personalization, or LTP) that captures the intuition behind our approach. LTP is both expressive and leads to computationally efficient inference algorithms (LTP-INF and LTP-EM) that find the personalization vector on real data-sets.
- Our experiments with synthetic data-sets generated by a state-of-the-art personalization engine show that LTP can learn the personalization parameters very accurately, achieving on average 84% precision in learning personalized topics.
- We perform experiments on a novel real-life data-set containing the personalized and vanilla query results collected from 10 Google users. Our qualitative results demonstrate that the personalized topics determined by LTP for a user correspond well to his ad-categories determined by Google.

2. RELATED WORK

Search personalization: A large body of work exists on personalizing search results using user-profiles [8, 23, 18], that collectively give overwhelming evidence of its benefits. More recently, researchers have also explored creating
profiles using topic models [22] and other textual information [23]. These works are not competitors of our paper, but rather serve as a motivation for us, as they highlight the existence and importance of profiles in the state-of-the-art in personalization.

Another body of work explores short-term and session based personalization [1,8], that personalize based on user’s current intention, based on his recent history or session. While such approaches are not aligned with our idea, there are two important points to note—a) they do no imply profile-based personalization does not happen, rather, they are typically used in conjunction with each other [1,13], and b) since they are applicable only during a session, it is easy to remove their affect by making sure no coherent session is tracked during our data collection (by doing the queries in a random order or adding sufficient delays).

Researchers have also found that personalization is not always beneficial and have proposed various approaches, such as click-entropy [26,27], dynamic user interests [13] and query difficulty [31], to filter queries that should not be personalized (irrespective of user’s profile). Such filtering is very hard replicate in our approach since the output may not contain any information to model them. We therefore allow for existence of this hidden process in our model via a latent variable deciding (randomly) if personalization happens on a query (see Section 4.4 for details).

In a paper contemporary to ours, Hannak et al. [9], study the parameters (location, demographics, etc.) that effect personalization in Google search. While these parameters give insights on what inputs influence personalization in practice, it is very different from the topic-based approach we take to capture the hidden user profiles.

**Topics Models:** Although topic models are clearly a popular tool for processing textual information and have also been used in personalization, there is no work to our knowledge that models the differences in two documents (or two ranked set of documents) as us. A recent work by Bischof et al. [2] comes close—they find exclusive topics (that are sufficiently different from each other) so that the documents can be classified into a non-overlapping hierarchy. While this also involves finding topics which are present in some documents and not in others, it is still very different from our approach of finding a consistent (may not be exclusive) set of personalized topics that can differentiate personalized and vanilla content.

**Privacy:** Finally, our problem stems from the general area of privacy of user data. Various studies have highlighted problems of privacy in information leaks from OSPs [11,17,10]. Korolova et al. [10] showed how targeted ads can pinpoint individual users in Facebook, Mao et al. [17] analyzed tweets to find vacation plans and medical conditions for real users, etc. However, these studies are focused on finding instances of privacy leaks from the entire OSP network and do not help users understand leaks in their own account. Other approaches of privacy preserving personalization aim at building systems from scratch that ensure certain norms are preserved in the personalized output, e.g. grouping user profiles [29,30] to preserve k-anonymity or making a differentially private recommender system [13]. Recently, Chen et al. [6] presented a more user centric approach that gives user control over fine grained categories (represented as a fixed hierarchical taxonomy) which they want personalization on.

These techniques, however, require the users to switch to these new systems which is not practical.

### 3. Problem Formulation

In this section, we introduce our notations and define the technical problem that we consider in this paper.

#### 3.1 Notation

Let $I = \{i_1, i_2, \cdots \}$ be the universe of all the items being present at the personalization server, where, an item might represent a url (for search engines like Google, Bing, etc.), a product web-page (for e-commerce sites like Amazon, Netflix, etc.) or an advertisement (for ad servers). For a query $q$, let $\pi_q$ and $\sigma_q$ denote the personalized and vanilla results. In the following discussion, we will often drop the subscript $q$, when the query is understood from the context.

As mentioned earlier, both $\pi$ and $\sigma$ are treated as permutations over a finite set of items $I' \subset I$. Technically, a ranking/permutation $\pi$ is a bijection from a set to itself. For any permutation $\pi$, $\pi(i)$ denotes the item assigned at rank (position) $i$, hence $\pi = (\pi(1), \pi(2), \cdots)$. The notation $\pi^{-1}(d)$ denotes the rank $i$ of an item $d \in I$ in $\pi$ such that $\pi(i) = d$. For any two permutations $\pi$ and $\sigma$, we use the notation $\sigma^{-1}(\pi(i))$ to denote the rank of the item $\pi(i)$ in $\sigma$. Observe that $\pi^{-1}(\pi(i)) = i$. We use $S_i$ to denote the set of all permutation over $n$ items.

We assume that there are $T$ topics $\{\beta_1, \beta_2, \cdots, \beta_T\}$ in our system where each topic $\beta_k$ is defined as a multinomial distribution over a fixed vocabulary $V$. For each word $w \in V$, we have a parameter $\beta_{k,w} = \Pr(w \mid \beta_k)$ such that $\sum_{w \in V} \beta_{k,w} = 1$. Each item in $I$ is represented by its topic-map $\theta$, which is a multinomial distribution over the set of topics. By inspecting the components of $\theta_i$, one can infer how related the item is to a particular topic.

We now describe our representation of topic-level user profile information. For each user $u$ and topic $\beta_k \in \beta$, we associate a variable $\eta_{u,k} \in R$. It captures the importance of $\beta_k$ (more relevant topics have higher values) for serving personalized content to $u$. The complete profile information (we name it as latent personalization vector) is denoted by $\eta_u = (\eta_{u,1}, \eta_{u,2}, \cdots, \eta_{u,T})$. We often drop the subscript $u$ and refer to it simply as $\eta$ whenever the user is understood from the context.

#### 3.2 Problem

Our strategy to learn the personalization vector $\eta$ is to repeatedly frame queries to the search engine and observe the difference between its vanilla and personalized results. For a given user $u$, we first sign-in to her account and submit a query. This gives the search engine an opportunity to personalize the result by using $u$’s profile information and through this process, we obtain the personalized result $\pi$. Next, we submit the same query in an anonymized form, by removing all cookies from the http request, thus removing all account details (but keeping all other parameters same such as IP address, User-Agent, etc.). This time the server sends back the vanilla result $\sigma$. We expect that as this process is repeated many times, the cumulative difference between these two kinds of results will become statistically signifi-
cant and contain substantial evidence for $\eta$. In this paper, we study the following problem: *Given pairs of query results $(\sigma_1, \pi_1), (\sigma_2, \pi_2) \cdots (\sigma_m, \pi_m)$, how do we learn the latent personalization vector $\eta$, for a given user?*

**Non-profile factors** Although personalization normally yields its benefits by presenting more relevant results to the users, it is also known to be less effective and even detrimental in many cases. For example, while personalizing results are known to work well for short and ambiguous queries [21] where user searching same query may be looking for completely different things, for common and specific queries two users with very different profiles are normally looking for the same information and are satisfied with the same (ordering of) results. In such cases, even though user’s profile implies re-ranking, the server may decide not to personalize. This creates a problem for our approach as a search engine’s decision whether to personalize the result of a search query or not, is influenced not only by the topical content of the query result, but also through other filtering processes that are hidden from us.

We take care of this in our model by introducing a latent parameter that, during training phase, filters out such inexplicable events and reduces the noise in the personalization vector. In our experiments with the Google data-set, we found several instances of queries with results at higher ranks having higher “scores” (see Section 4 for definition of scores) the ones at lower ranks, that were not personalized, while another query with similar scores was personalized. Without this latent parameter, these instances would have reduced the effectiveness of learning $\eta$.

### 4. LTP MODEL

The goal of topic-based personalization learning is to capture the following information: topics on which personalization takes place and a weight vector corresponding to the degree of personalization on these topics. In addition, the approach has to scale with large number of queries. To meet these objectives, we first propose Latent Topical Personalization model (LTP) to study the problem from a Bayesian perspective. Following that, we develop efficient variational inference and estimation techniques for learning the parameters of this model.

#### 4.1 Model Description

We now formally describe the proposed LTP model. LTP models (Figure 1) both topics and personalization. It involves a *topic block* to model the topical content creation of the items and a *personalization block* to model the personalized responses (i.e. $\pi_1, \pi_2, \cdots, \pi_m$).

**Topic Block** The topic block follows the description of standard topic models (c.f. LDA [3]) and we present it here for the sake of completeness. The generative process for the topic block is as follows

- For each topic $\beta_k, k = 1, 2, \cdots, T$
  1. Sample $\beta_k \sim \text{Dirichlet}(\nu)$.

- For each item $i \in I$
  1. Sample its topic-map $\theta_i \sim \text{Gaussian}(0, \text{diag}(\alpha^2))$.
  2. For each word position $j = 1 \cdots n_i$ for item $i$
     - (a) Sample topic $K_{i,j}$ with $\Pr(K_{i,j} = k) \propto e^{\theta_i,k}$.
     - (b) Sample word $W_{i,j} \sim \text{Multinomial}(\beta_{K_{i,j}})$.

The joint distribution for the topic-block can be written as

$$p(\theta, K, W, \beta, \nu) = \prod_{i=1}^n p(\theta_i \mid \alpha) \cdot \prod_{k=1}^T p(\beta_k \mid \nu) \cdot \prod_{i=1}^n \prod_{j=1}^{n_i} p(K_{i,j} \mid \theta_i) \cdot p(W_{i,j} \mid K_{i,j}, \beta_{1\cdots T})$$ (1)

**Personalization Block** Our design of the personalization block is little more involved. The main difficulty stems from the non-profile based factors, which may lead to no re-ranking of results even when the user profile (i.e. $\eta$) indicates personalization should happen. In LTP, we achieve it by introducing a latent switch variable $z$ (refer to Figure 1). Independently, for each query, we sample $z$, governed by a prior parameter $\tau$ and based on its value decide whether to allow topical personalization or not. The parameter $\tau$ is user-specific and controls the rate at which topical personalization takes place (for that user).

Based on the value of $z$, we pick a probability distribution over permutations and sample $\pi$ from it. Probabilistic models on permutations have recently been applied to solve various problems related to ranking [21]. Probability distributions defined over permutations can be broadly categorized into two types—*distance based* and *score based*. In a distance based model [19], the probability of a permutation is defined according to its distance from a central permutation. They have rich expressive power as they can incorporate a wide variety of distance functions over permutations but are, in general, computationally inefficient.

Score based models [12], on the other hand, are very efficient as they divide permutation construction into stages and assign scores on each stage such that the final probability is a combination (multiplication) of stage-wise scores. However, being defined as a specific function over scores, they have limited expressive power e.g. they can not take into account any central permutation in the generative process. For LTP, we have a central permutation (vanilla list $\sigma$) and want to model $\pi$ as being generated from it. Further, as explained later, we define scores on items as a function $\eta$. Therefore, we need a model which combines the notion of distance with scores and is computationally efficient.

The probability distribution $f$ (Figure 1) is a process for generating the personalized response $\pi$, and is decomposed...
Figure 2: An example illustrating the steps of \( f \). We have assumed \( \mu = 1 \). At each stage, the actual outcome is marked in blue and the most likely outcome is marked in red.

![Table](image)

The working principle for the generative process for the personalization block can be described as

- For each user \( u \)
  1. Sample \( \tau \sim \text{Beta}(\delta, \delta) \).
  2. Sample \( \eta \sim \text{Gaussian}(0, \text{diag}(\gamma^2)) \).

- For each query \( q_i, i = 1, 2, \ldots, m \)
  1. Sample \( z_i \sim \text{Bernoulli}(\tau) \) to decide whether to allow topical personalization.
  2. If \( z_i = 1 \), sample \( \pi_i \sim g(\cdot | z_i, \lambda, \theta, \eta) \).
  3. Else, sample \( \pi_i \sim f(\cdot | \sigma, \mu) \).

The joint distribution for the personalization block can be written as

\[
p(\pi, z, \tau, \eta \mid \theta, \delta, \mu, \lambda, \sigma) = p(\eta \mid \gamma) \cdot p(\tau \mid \delta) \prod_{i=1}^{m} p(z_i \mid \tau) \cdot g(\pi_i \mid z_i, \lambda, \theta, \eta) \cdot f(\pi_i \mid \sigma_i, \mu_i)^{1-z_i}.
\]

Finally, the full joint distribution for LTP can be obtained by multiplying Equations 1 and 3. We treat the parameters \( \nu, \alpha, \beta, \gamma \) as constant and do not consider learning them. However, the parameters \( \mu \) and \( \lambda \) that controls the permutation models need to be learned. We have assumed a Gaussian prior on \( \eta \). The role of this prior is to set \( \eta \) to zero when we do not observe any significant difference between \( \pi \) and \( \sigma \) i.e. \( \pi_i \approx \sigma_i \).

We first assume that \( \lambda \) and \( \mu \) are predefined constants and describe the inference (LTP-INF) of the personalization vector \( \eta \) based on these values in Section 4.2. We will then use LTP-INF to also estimate these parameters in Section 4.3.

4.2 Inference of Personalization Vector

The key inferential problem that we study in this work is to obtain the posterior distribution on the latent variables i.e. to determine \( p(\theta, K, \beta, z, \tau, \eta \mid \sigma, \lambda, \mu) \). As with simpler topic models, the exact inference is intractable and therefore, we resort to approximate inference techniques. Given the non-conjugacy of \( \pi \) and \( \theta \), sampling based techniques...
are unlikely to be efficient. In this paper, we propose a variational approximation scheme. In a variational inference, one defines a family of simpler distribution over the latent variables to approximate the true posterior distribution. This family of distribution is indexed by additional parameters (called variational parameters) which are tuned so as to minimize the KL divergence with the true posterior.

We first simplify the inference by breaking it into two parts. For the first part, we ignore the dependency between the topic and the personalization block. Therefore, our strategy is to first infer the topics and use the inferred topics and the topic-maps of the items to carry out inference for the personalization block. This will simplify the exposition greatly and the ideas that we develop here will carry over naturally to the general case of inferring the blocks jointly. We revisit the inference for the complete model in Section 4.4. Inference for the topic block follows standard techniques (see e.g. [3]) and therefore, we omit the details here. For the rest of this sub-section we assume that the topics have been inferred and develop an inference scheme for the personalization block.

For the personalization block, the key inferential problem is to obtain the posterior distribution \( p(z, \tau, \eta \mid \sigma, \lambda, \mu) \). This posterior is approximated with the help of a variational distribution \( r \). Figure 3 illustrates its graphical model representation. The personalization vector \( \eta \) is assumed to be Gaussian with the following density

\[
r(\eta \mid \tilde{\eta}) = \frac{1}{4\pi^2} \exp \left( -\frac{1}{2\tilde{\eta}^2} (\eta - \tilde{\eta})' (\eta - \tilde{\eta}) \right)
\]

Here, the variational parameter \( \tilde{\eta} \) represents the mean of the gaussian and its variance is \( \gamma \)^2. For query \( q \), we assume that \( z_i \) is sampled from a Bernoulli distribution with parameter \( \phi_i \in (0, 1) \). Finally, for user \( u \), we assume that \( \tau \) is sampled from a beta distribution having the following density function

\[
r(\tau \mid \kappa_1, \kappa_2) = \frac{\Gamma(\kappa_1 + \kappa_2)}{\Gamma(\kappa_1)\Gamma(\kappa_2)} \tau^{\kappa_1 - 1}(1 - \tau)^{\kappa_2 - 1}
\]

where the parameters \( \kappa_1, \kappa_2 > 0 \) and \( \Gamma(x) \) is the Gamma function. We use the notation \( \Psi(x) \) for the digamma function which is defined as \( \frac{\Gamma’(x)}{\Gamma(x)} \).

The next step in our variational analysis is to learn the particular value of the parameters \( (\phi, \kappa_1, \kappa_2, \tilde{\eta}) \) that minimizes the KL divergence between \( r \) and the true posterior \( p \). It can be shown that minimizing the KL divergence has the same effect as maximizing the following objective function,

\[
\mathbb{L}(\phi, \kappa_1, \kappa_2, \tilde{\eta}) = \mathbb{E}_r [\ln p] + \mathbb{H}(r)
\]

where \( \mathbb{H}(r) \) is the entropy and \( \mathbb{E}_r \) denotes expectation w.r.t the distribution \( r \).

We use block coordinate-wise ascent to maximize the expression in Equation [4]. Intuitively, we perform fixed point iterations by updating one block of parameters at a time, keeping all other parameters fixed to their most recent value. The update rule for parameters \( \phi_1, \ldots, m, \kappa_1, \kappa_2 \) are obtained by setting the partial derivatives of \( \mathbb{L} \) to zero. Due to our choice of \( r \), the update rules for \( \phi, \kappa_1, \kappa_2 \) are particularly simple and have closed-form expressions.

To maximize \( \mathbb{L} \) with respect to \( \tilde{\eta} \), we use the conjugate gradient algorithm\(^4\). The objective function for \( \tilde{\eta} \) can be written as

\[
\mathbb{L}(\tilde{\eta}) = -\frac{1}{2\tilde{\eta}^2} \tilde{\eta} + \sum_i (1 - \phi_i) \cdot \mathbb{E}_r [\ln g(\pi_i \mid \sigma_i, \theta, \lambda)]
\]

It can be proved that \( \mathbb{L} \) is concave (with respect to \( \tilde{\eta} \)) and therefore, using simple optimizers like conjugate gradient, we will be able to obtain the global maximum \( \tilde{\eta} \). Algorithm 1 summarizes the inference procedure. Due to page limits, we omit the derivations and refer to the full version of the paper [15] for details.

### 4.3 Parameter Estimation

We now focus our attention at learning \( \lambda \) and \( \mu \). We use Maximum Likelihood Estimators (MLE) for this, where one finds the value of the parameters that maximizes the (log) likelihood of the observed data i.e. the following expression

\[
\ln p(\pi \mid \lambda, \mu, \sigma) = \sum_{i=1}^m \ln p(\pi_i \mid \lambda, \mu, \sigma_i)
\]

However, to calculate the likelihood function, we have to marginalize over the latent variables which is difficult in our model for both real variables \( (\eta, \tau) \), as it leads to integrals that are analytically intractable, and discrete variables \( (z_1, \ldots, m) \), it involves computationally expensive sum over exponential (i.e. \( 2^m \)) number of terms.

We use the variational Expectation Maximization (EM) algorithm to circumvent this difficulty. In the E-step, Algorithm 1 approximates the true posterior distribution over the latent variables, using the current estimates of the parameters. The variational parameters learned in this step

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\(^4\)Refer to [3] for the proof.

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Algorithm 1 LTP-INF: Variational Inference Algorithm for LTP

1: **Input** Training data-set \((\pi, \sigma)_{1,2 \ldots, m}\); values for \( \lambda, \gamma, \delta, \mu; \)
2: **Output** Values \((\phi_1, \kappa_1, \kappa_2, \tilde{\eta})\) that maximize \( \mathbb{L} \);
3: **Initialization** Randomly initialize to \((\phi_1^{(0)}, \kappa_1^{(0)}, \kappa_2^{(0)}, \tilde{\eta}^{(0)})\) such that \( 1 > \phi_1^{(0)} > 0 \) and \( \kappa_1^{(0)}, \kappa_2^{(0)} > 0 \);
4: \( i \leftarrow 0 \);
5: while \( \Delta \) has not converged do
6: \( i \leftarrow i + 1 \);
7: \( \kappa_1^{(i)} \leftarrow \delta + \sum_{j=1}^m (1 - \phi_j^{(i-1)}) \);
8: \( \kappa_2^{(i)} \leftarrow \delta + \sum_{j=1}^m \phi_j^{(i-1)} \);
9: for \( j = 1 \ldots m \) do
10: \( \mu_j \leftarrow \Psi(\kappa_2^{(i)}) - \Psi(\kappa_1^{(i)}) + \ln f(\pi_j \mid \sigma_j, \mu) - \mathbb{E}_r [\ln g(\pi_j \mid \eta_j, \sigma_j, \theta, \lambda)] \);
11: \( \phi_j^{(i)} \leftarrow 1/(1 + e^{\delta \mu_j}) ; // Update \phi_i * / \)
12: end for
13: \( \tilde{\eta}^{(i)} \leftarrow \arg \max_{\tilde{\eta}} \mathbb{L}(\phi_1^{(i)}, \kappa_1^{(i)}, \kappa_2^{(i)}, \tilde{\eta}) ; // Use conjugate gradient to optimize this block */ \)
14: \( \Delta \leftarrow \mathbb{L}(\phi_1^{(i-1)}, \kappa_1^{(i-1)}, \kappa_2^{(i-1)}, \tilde{\eta}^{(i)}) \);
15: **end while**
16: **return** \((\phi_1^{(i)}, \kappa_1^{(i)}, \kappa_2^{(i)}, \tilde{\eta}^{(i)})\)

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http://en.wikipedia.org/wiki/Nonlinear_conjugate_gradient_method

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Algorithm 2 LTP-EM: Variational EM Algorithm for LTP

1: **Input** Training data-set $(\pi, \sigma)_{i=1, \ldots, m}$
2: **Output** Values $(\lambda', \mu')$ that maximize Equation 5
3: **Initialization** Randomly initialize $(\lambda(0), \mu(0))$ s.t. $0 \leq \lambda(0) \leq 1$ and $\mu(0) > 0$.
4: **while** $(\lambda, \mu)$ have not converged **do**
5: **E-step** /* The variational inference step */
   - $(\phi'_1, \ldots, \phi'_m, \kappa'_1, \kappa'_2, \tilde{\eta}') \leftarrow \text{LTP-INF}(\sigma, \pi, \lambda(i), \mu(i));$
   - $\Lambda(i)(\lambda, \mu) \leftarrow \mathcal{E}_{r(\phi'_1, \kappa'_1, \phi'_2)}[\ln p];$
6: **M-step** /* Learn new estimates of the parameters */
   - $(\lambda(i+1), \mu(i+1)) \leftarrow \arg\max_{\mu > 0, \lambda > 0} \Lambda(i)(\lambda, \mu)$
7: $i \leftarrow i + 1$
8: **end while**
9: **return** $(\lambda(i), \mu(i))$

are used in the subsequent M-step to maximize the likelihood function (over the true parameters $\lambda$ and $\mu$).

Algorithm 2 summarizes the steps of the variational EM. It can be shown that the constraint maximization problem in step 6 is a concave program and therefore, can be solved optimally and efficiently [4].

4.4 Learning Topic Distributions

For inference in the topic block (Figure 1), we augment our variational distribution with additional parameters in the following way. Topic distribution $\beta_k$ is sampled from a Dirichlet prior with parameters $\tilde{\beta}_{k, w} \mid w \in V$. The topic assignments $K_{i, j}$ are sampled from a multinomial distribution with parameters $\omega_{i, j} \mid \pi$ and $\theta_i$ is sampled from a normal distribution with mean $\bar{\theta}_i$ and variance $\alpha^2 I$. Using the same recipe as in Section 3.2 (c.f. Equation 1), we arrive at the following simple update rule for learning the topic distributions

$$\tilde{\beta}_{k, w} = \nu + \sum_{i,j \mid \omega_{i, j, k}} \omega_{i, j, k} \cdot W_{i, j, w}$$

The topic assignments $\omega_{i, j}$ also has a closed form update rule as given by $\omega_{i, j, k} \propto \exp(\mathcal{E}_r[\ln \theta_i] + \mathcal{E}_r[\ln \beta_{k, w}])$.

The main difficulty in learning topic-maps (i.e. $\theta_i$’s) stems from the coupling between the personalization and the topic blocks through $\theta$. While determining $\mathcal{E}_r[\ln g(\pi \mid \eta, \theta, \sigma, \lambda)]$ (step 8 of Algorithm 1), we now have to take expectation over $\theta$, in addition to $\eta$. However this calculation is analytically tractable due to our assumption of independence and gaussian priors on $\theta$ and $\eta$. We use gradient descent on $\theta$ to solve it. The rest of the calculation remains unchanged.

5. EXPERIMENTS

In this section, we describe a comprehensive set of experiments designed to evaluate the accuracy and effectiveness of our techniques.

5.1 Data-sets

The input to our algorithm consists of a set of queries and the personalized and vanilla results (i.e. $\pi, \sigma$ pairs) for them, returned by a search engine. During the training phase, we present these queries to LTP and let it learn the personalization vector $\eta$. Once $\eta$ is learned, the next step is to validate it, by measuring how well it corresponds to the ground truth. However, in practice, such validation schemes are often difficult to design as the search engines do not reveal the actual user profile. We therefore perform our experiments on both real-world data-set comprised of Google search history of a few users, and a large scale synthetic data-set.

5.1.1 Google Search Personalization

We collected search history data from 10 real Google users in Nov 2012. We fetched their past search queries using Google API that returns a sample of about 1000 web queries from her history (it also contains other queries like map, image, etc. that we ignored). We retrieved on average 850 distinct queries for each user.

We issued each distinct query in his history (in a randomized order) to Google both with and without their login credentials to retrieve the search results. For a given query, both the results were fetched at the same time (within a few seconds of each other) and using the identical connection parameters such as user-agent (UA), IP-address, http headers (except cookies), etc. This process removes non-profile based personalizations such as those based on context of the current session (randomized order breaks any coherent context in user’s history), IP address or location, time-of-the-day (the whole data collection for a user took only a few minutes), browser or OS type, etc. Hence the differences in results should be only due to user’s profile.

We then parsed the result pages and extracted the ranked results. We ignored the paid links (at top and bottom of the page) and any map, image, or other embedded group of results that some queries return. We then used the Mallet toolkit to extract topics from the urls separately for each user. Due to privacy considerations, we then anonymized the entire data set by mapping each url, query and topic to (randomly generated) IDs. Our algorithms were run on this anonymized data.

We found ample evidence of profile based personalization on Google—roughly 30% queries received personalized results, i.e. had differences in the ranks of urls in personalized and vanilla results. We also found that the personalization is much more subtle compared to the impression we get from search personalization literature (and our experiments with AlterEgo server)—most queries (~70%) were not personalized and while there were some queries with fair amount of personalization, on an average, we observed very little difference between the results.

5.1.2 AlterEgo

We use an open source search personalization engine called AlterEgo [15] to generate the synthetic dataset. AlterEgo contains implementation of various popular profiling and

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Google, however, publishes the categories of topics used to serve personalized ads. Unfortunately, this data is not quite helpful as the categories are very high level and do not convey rich enough information.

We used the snippets that Google returns along with the search results to obtain text for the urls.

The avg. EMD (earth mover’s distance) over queries with personalization was 5.9 (e.g. the EMD of moving a single url at rank 5 to rank 1 is 4).

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personalization techniques; we used their “unique matching” technique for our experiments. In our simulation, we used AlterEgo as a surrogate personalization engine i.e. we obtain the vanilla result from Google and use AlterEgo to personalize it. The benefit of this approach is that we can train AlterEgo on topics of our choice and use this information to validate the model output $\eta$. The work-flow and details of the data generation steps are presented below.

**Generating Topics** We extracted a set of 500 topics by running Mallet on approximately 420k urls obtained from the Delicious dataset [28]. We manually select 50 topics and label them into 10 categories (examples are health, cooking, science, finance, etc.); these topics serve as a ground-truth for us. The selection of these topic categories and urls (used in the next step) is intended to simulate a typical user behavior, where, a user is interested in $\approx 10$ categories of topics.

**Training AlterEgo** For each topic, we inspect the topic-maps of the urls and identify the ones which have significant (> 0.2) weight (on this topic). These urls are used to train AlterEgo profile. We generated 10 profiles trained on a subset of 1 to 10 topics (i.e. 10 profile for 1 topic, 10 profile on 2 randomly selected topics, and so on), generating a total of 50 profiles.

**Queries** We generated 500 queries for each topic by randomly combining the top 10 relevant words from them. This gives us a total of 5k queries (over 10 categories). For each query, we retrieved the vanilla results from Google. Note that, if a query is related to a topic used for training the profile, only then AlterEgo will be able to personalize it. Otherwise, the vanilla and personalized results will be more or less identical.

### 5.2 Implementation Details

We use JOptimizer [14], a java based open source optimization package for solving the convex program in Algorithm 2 (step 6) All our experiments are carried out on a Intel Pentium IV machine with 3.0GHz processor and 4GB of RAM.

We use the following values of the hyper-parameters $\delta = 2.0, \gamma = 1.0$. For computational efficiency, we used Mallet for inference in the topic-block (see Figure 1) and do not use the inference process described in Section 4.1.

### 5.3 Results with the AlterEgo data-set

In this section, we summarize the result of our experiments with the AlterEgo data-set.

#### 5.3.1 Precision-Recall

Our first set of experiments are designed to evaluate the accuracy of LTP in correctly learning the personalized topics. On each AlterEgo profile, we train LTP and learn the personalization vector $\eta$. Next we compare it with the actual list of topics that were used to train this profile (by AlterEgo). Let $T_{act}$ be the true set of personalized topics and $T_{\eta}$ be the one inferred by LTP. For this experiment, we measure the precision and recall values, where precision is defined as $\frac{|T_{act} \cap T_{\eta}|}{|T_{act}|}$ i.e. the fraction of reported topics that are actually personalized and recall by $\frac{|T_{act} \cap T_{\eta}|}{|T_{\eta}|}$ i.e. the fraction of the original personalized topics that we are able to identify.

| P@1 | P@3 | P@5 | R-pre | P@1+1 | P@5+3 | MAP |
|-----|-----|-----|-------|-------|-------|-----|
| 97.80 | 84.02 | 70.69 | 84.66 | 70.69 | 54.44 | 97.60 |

Table 1: Performance (in %) of LTP in finding personalized topics (with AlterEgo data-set).

We re-order the topics based on the (decreasing) value of $\eta$ computed by LTP. For each $k$, we declare the top-$k$ topics (with maximum $\eta$ values) as personalized and calculate the precision and recall value for this decision. Table 1 summarizes the precision scores obtained by LTP. Specifically, we evaluate its performance in terms of Precision@1 (P@1), P@3, P@5, R-precision (R-pre) and mean average precision (MAP) [5, 7]. Note that the size of actual topics was quite different for different runs (varies from 1-10). Hence, along with the top-$k$ topics, we also study the precision at $|T_{act}+k|$ (denoted as P@$k+1$).

In Figure 4 we illustrate the recall performance of our algorithm. At the expense of low precision ($< 0.4$), LTP is able to retrieve all the personalized topics (recall $\geq 0.93$) and its recall performance is relatively insensitive to precision; however, if we require high precision ($> 0.8$), the recall drops to $\approx 0.5$. As evident from the figure, a typical operating characteristic of LTP is precision $\approx 0.7$ and recall $\approx 0.7$, which is achieved when we return top-3 topics.

#### 5.3.2 Classification Tests

In this section, we develop two classification tests to evaluate LTP’s predictive power. For both these experiments, we randomly split the $\pi, \sigma$ list into data-sets D1 (80%), used for training LTP, and D2 (20%), used for testing. We repeat this split with 10 random seeds and report the average number in all the data presented below.

**Query Disambiguation** In this experiment, while testing on D2, we hide which result is personalized and which one is vanilla and the task of the model is to determine the correct labels.

We proceed with the classification task in the following way. Let $\eta'$ be the parameter learned by LTP during the training. For input lists $l_1$ and $l_2$, LTP calculates the likelihood values $p(l_1 \mid l_2, \eta')$ and $p(l_2 \mid l_1, \eta')$ and whichever likelihood is higher is assigned to the personalized result i.e. if $p(l_1 \mid l_2, \eta') > p(l_2 \mid l_1, \eta')$ then $l_1$ is declared to be the.

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13We also did experiments with their “matching” technique, and got very similar results which are omitted due to lack of space.

14http://www.joptimizer.com/
Table 2: Summary of results with the AlterEgo dataset

| #topics | Accuracy ($\mu \pm \sigma$) LTP-EM | Accuracy ($\mu \pm \sigma$) LTP-INF | Time (secs) LTP-EM | Time (secs) LTP-INF |
|---------|----------------------------------|----------------------------------|------------------|------------------|
| 1       | .74 ± 0.09                       | .72 ± 0.09                       | 80.7             | 22.7             |
| 2       | .72 ± 0.06                       | .70 ± 0.09                       | 154.3            | 31.5             |
| 3       | .70 ± 0.05                       | .68 ± 0.06                       | 221.6            | 42.4             |
| 4       | .69 ± 0.04                       | .67 ± 0.05                       | 272.2            | 53.7             |
| 5       | .69 ± 0.05                       | .67 ± 0.05                       | 336.1            | 69.8             |
| 6       | .67 ± 0.04                       | .65 ± 0.05                       | 333.2            | 70.7             |
| 7       | .65 ± 0.04                       | .65 ± 0.05                       | 342.5            | 71.1             |
| 8       | .63 ± 0.04                       | .63 ± 0.04                       | 348.2            | 73.6             |
| 9       | .63 ± 0.05                       | .62 ± 0.05                       | 354.4            | 76.4             |
| 10      | .62 ± 0.02                       | .62 ± 0.02                       | 359.2            | 79.5             |

Table 2: Summary of results with the AlterEgo dataset

personalized result and vice versa. We name this test as $P-V$ disambiguation for a given profile. Over all the test points in D2, the fraction of queries that were labeled correctly is referred to as disambiguation accuracy.

Table 2 summarizes the result of this experiment. In summary, we achieve disambiguation accuracy in the range of 62-74%. For each profile, we collect the accuracy values for the 10 different runs and report its mean and standard deviation ($\mu \pm \sigma$). Observe that our accuracy decreases slightly as the AlterEgo profile is trained with more and more topics.

Table 3 also reports the training time of LTP-EM. For profiles trained with many topics, LTP-EM takes more time to converge. We repeat the experiment with LTP-INF with the parameter values fixed to $\lambda = 0.9$ and $\mu = 10.0$. As the results show, LTP-INF is up to 5 times faster to train but achieves slightly lower accuracy. The accuracy however, improves slightly ($< 3\%$) if we increase the amount of training data (D1) from 80% to 90% (not shown in the table).

Figure 5: Performance of LTP in user classification (with AlterEgo data-set).

User Classification For this experiment, we consider groups of users (i.e. profiles) and develop a classification test within the group members. We vary the size of the group from 2 to 10 and for each group size, randomly pick 10 groups. For each group $G$, we present a ($\pi, \sigma$) pair to LTP but do not reveal the user it belongs to. The task of the model is to correctly predict the user.

We again use the likelihood test for this task. Specifically, for each user $u \in G$ and input ($\pi, \sigma$), we calculate $p(\pi \mid \sigma, \eta_u)$ ($\eta_u$ learned during training) and output the user for which the likelihood attains its maximum value.

In Figure 5, we summarize the result of this experiment. There are two parameters in this experiment - the size of the group and the number of topics used to train AlterEgo for each profile in the group. For simplicity, we present here results for the homogeneous case, where we combine profile which are trained on the same number of topics. Observe that the accuracy reported by LTP is significantly higher than a random guess (which is 1/g, g being the group size). The accuracy decreases slightly if profiles are trained with many topics. We believe this reduction in accuracy is also an artifact of our data generation—profiles trained on multiple topics can (and do) have topics in common, that will make it hard to distinguish personalized response on two profile trained on the same topic.

In summary, these results, together with the precision-recall values from last section highlight that our model fits the data well and learns the correct set of personalized topics on synthetic data.

5.4 Results with the Google dataset

In this section we describe the results with the Google data-set. Note that since we do not know the actual personalization on different topics (ground truth) for a real Google user, we cannot perform the precision-recall experiments as with AlterEgo dataset, and resort to only query disambiguation and user classification test described above. However, we also perform some qualitative tests that give ample indication that we have found a good personalization vector.

5.4.1 Qualitative Evidences for Correctness of $\eta$

We now present our analysis on finding qualitative correctness of $\eta$ using evidences of personalization. An evidence is an instance of $\pi, \sigma$ where results were re-ranked such that the ones with $\eta$ were moved up. Note that while such evidence have no statistical significance, they are much more helpful for a user’s understanding of his profile compared to the personalization vector. Such evidences are a core feature of the privacy toolkit we are building (see Section 6).

Figure 6 shows an example evidence of personalization happening on a user’s account. The result for query Q (“how to decide mixing of markov chain”) and theta values for two relevant topics T1 (about “Algorithms” defined by words algorithm, design, complexity) and T2 (about “Probability” defined by words probability, distribution) are shown. For

We also performed experiments on the general case (e.g. by grouping profiles trained on 3 topics with 5 topics). The results are similar and not repeated here.
As our analysis shows, U2 is has a high weight on topic T1 (compared to U2, which leads to this personalization. The user can therefore see not just his inferred interests (more relevant with a user) than queries), but also the wiki link U1 (in the box), although less relevant to the query, is placed higher in the personalized results. Figure 6: An example to illustrate the difference between personalized (left) and vanilla (right) search results (for a real user) returned by Google.

Table 4: Accuracy of LTP over 9 Google users.

| User Id | 15 Topics | 20 Topics | 50 Topics | 100 Topics |
|---------|-----------|-----------|-----------|------------|
| 1       | .74±.05   | .70±.05   | .70±.06   | .73±.04    |
| 2       | .68±.05   | .70±.04   | .70±.04   | .65±.03    |
| 3       | .67±.13   | .72±.14   | .72±.13   | .73±.11    |
| 4       | .54±.08   | .51±.06   | .55±.06   | .59±.07    |
| 5       | .54±.11   | .47±.09   | .49±.11   | .43±.09    |
| 6       | .85±.07   | .78±.05   | .84±.04   | .81±.07    |
| 7       | .73±.04   | .70±.05   | .71±.06   | .73±.06    |
| 8       | .66±.03   | .62±.03   | .61±.04   | .64±.03    |
| 9       | .52±.04   | .52±.03   | .50±.04   | .54±.04    |

Table 5: User classification accuracy on Google data.

| Group | Number of Topics |
|-------|-----------------|
| Size  | 15 | 20 | 50 | 100 |
| 2     | .59±.06 | .61±.06 | .65±.04 | .58±.05 |
| 3     | .48±.04 | .53±.05 | .60±.05 | .50±.06 |

Table 4: Accuracy of LTP over 9 Google users.

Figure 6: An example to illustrate the difference between personalized (left) and vanilla (right) search results (for a real user) returned by Google.

this user, $\eta$ value for T1 is very high compared to T2. Observe that the wiki link U1 (in the box), although less relevant to the query, is placed higher in the personalized results. As our analysis shows, U2 is high in weight on topic T1 compared to U2, which leads to this personalization. The user can therefore see not just his inferred interests (more relevant with a user) than queries), but also the wiki link U1 (in the box), although less relevant to the query, is placed higher in the personalized results.

We next move to another qualitative analysis of $\eta$ by comparing it directly with the categories Google itself associates with a user.

We try to match topics with high $\eta$ (top-k such topics) with the broad categories in Google. Table 4 shows the result of such matching for 3 users. Take for example, the “Anime and Manga” category, that was also assigned a very high $\eta = .6$ (compared to an average value of .004) by LTP.

Such anecdotes show that our techniques have, in fact, learned the personalization vector correctly.

5.4.2 Quantitative Experiments

Query Disambiguation Table 4 summarizes the result of query disambiguation on the Google dataset. We first study the effect of number of topics (T) chosen for the user. We notice that only a few topics 15-50 are enough to get good accuracy for any user. Our accuracy results differ significantly for different users, varying from as low

16Shown in Google ads preference manager https://www.google.com/settings/ads/onweb/
7. REFERENCES

[1] P. N. Bennett, R. W. White, W. Chu, S. T. Dumais, P. Bailey, F. Borisuyk, and X. Cui. Modeling the impact of short-and long-term behavior on search personalization. In SIGIR, 2012.

[2] J. Bischof and E. Airoldi. Summarizing topical content with word frequency and exclusivity. ICML, 2012.

[3] D. M. Blei, A. Y. Ng, and M. I. Jordan. Latent dirichlet allocation. J. Mach. Learn. Res., 2003.

[4] S. Boyd and L. Vandenberghe. Convex Optimization. Cambridge University Press, 2004.

[5] C. Buckley and E. M. Voorhees. Retrieval evaluation with incomplete information. In SIGIR, 2004.

[6] G. Chen, H. Bai, L. Shou, K. Chen, and Y. Gao. Ups: efficient privacy protection in personalized web search. In SIGIR, 2011.

[7] N. Craswell, A. P. de Vries, and I. Soboroff. Overview of the tec-2005 enterprise track. In TREC, 2005.

[8] Z. Dou, R. Song, and J. R. Wen. A large-scale evaluation and analysis of personalized search strategies. In WWW, 2007.

[9] A. Hannak, P. Sapiezynski, A. M. Kakhki, B. Krishnamurthy, D. Lazer, A. Mislove, and C. Wilson. Measuring personalization of web search. In WWW, 2013.

[10] A. Korolova. Privacy violations using microtargeted ads: A case study. In ICDMW, 2010.

[11] J. Lindamood, R. Heatherly, M. Kantarcioglu, and B. Thuraisingham. Inferring private information using social network data. In WWW, 2009.

[12] R. D. Luce. Individual choice behavior: A theoretical analysis. Wiley, 1959.

[13] J. Luxenburger, S. Elbassuoni, and G. Weikum. Matching task profiles and user needs in personalized web search. In CIKM, 2008.

[14] A. Machanavajjhala, A. Korolova, and A. D. Sarma. Personalized social recommendations: accurate or private. VLDB Endowment, 2011.

[15] A. Majumder and N. Shrivastava. Know your personalization: Learning topic level personalization in online services. Arxiv, abs/1212.3390, 2012.

[16] C. L. Mallows. Non-null ranking models. Biometrika, 1957.

[17] H. Mao, X. Shuai, and A. Kapadia. Wpes. In Proc. workshop on Privacy in the electronic society, 2011.

[18] N. Matthijs and F. Radlinski. Personalizing web search using long term browsing history. In WSDM, 2011.

[19] A. K. McCallum. Mallet: A machine learning for language toolkit. http://mallet.cs.umass.edu.

[20] E. Pariser. The Filter Bubble: What the Internet Is Hiding from You. Penguin Press, 2011.

[21] T. Qin, X. Geng, and T. Y. Liu. A new probabilistic model for rank aggregation. In NIPS, 2010.

[22] D. Sontag, K. Collins-Thompson, P. N. Bennett, R. W. White, S. Dumais, and B. Billerbeck. Probabilistic models for personalizing web search. In WSDM, 2012.

[23] B. Tan, X. Shen, and C. X. Zhai. Mining long-term search history to improve search accuracy. In SICKDD, 2006.

[24] J. Teevan, E. Adar, R. Jones, and M. Potts. History repeats itself: repeat queries in yahoo’s logs. In SIGIR, 2006.

[25] J. Teevan, S. T. Dumais, and E. Horvitz. Personalizing search via automated analysis of interests and activities. In SIGIR, 2005.

[26] J. Teevan, S. T. Dumais, and E. Horvitz. Potential for personalization. TOCHI, 2010.

[27] J. Teevan, S. T. Dumais, and D. J. Liebling. To personalize or not to personalize: modeling queries with variation in user intent. In SIGIR, 2008.

[28] R. Wetzker, C. Zimmermann, and C. Bauckhage. Detecting trends in social bookmarking systems: A del.icio.us endeavor. IJDWM, 2010.

[29] Y. Xu, K. Wang, B. Zhang, and Z. Chen. Privacy-enhancing personalized web search. In WWW, 2007.

[30] Y. Zhu, L. Xiong, and C. Verdery. Anonymizing user profiles for personalized web search. In WWW, 2010.

[31] Z. A. Zhu, W. Chen, T. Wan, C. Zhu, G. Wang, and Z. Chen. To divide and conquer search ranking by learning query difficulty. In CIKM, 2009.