Signal and contrast effects due to T2 decay during k-space readout of UTE (ultrashort TE) sequences

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Abstract

In ultrashort TE (UTE) imaging, the short T2 values of the tissues of interest are comparable to the k-space readout duration, which result in significant T2 decay during k-space readout. This decay consequently causes significant effects on signal and contrast in UTE sequences, which we evaluate in this paper using models that incorporate the gradient slew rate $slew$ and maximal constant gradient strength $g_{max}$, in conjunction with objects of diameter $L$. The resulting signal and contrast relationships demonstrate steep signal changes between T2 values of ~50–500µs, corresponding to high T2 weighted contrast in this range. When $\gamma g_{max}^2/(4\pi \cdot slew) > 1/(2L)$, termed the “ramp only” regime, $g_{max}$ has no significant effect whereas decreasing $slew$ leads to decreases in signal amplitude and shifts the contrast peak to higher T2 values. When $\gamma g_{max}^2/(4\pi \cdot slew) < 1/(2L)$, termed the “mixed gradient” regime, both $g_{max}$ and $slew$ have significant effects, where decreases in either $g_{max}$ or $slew$ lead to lower signal amplitudes and shifts the contrast peak to higher T2 values. Under typical scan settings, the “ramp only” regime is usually dominant. Further, we demonstrate an unusual dependence of T2 weighted signal and contrast on object size, whereby objects with smaller values of $L$ demonstrate lower signal amplitudes and peak contrast at higher T2 values, compared to otherwise identical objects with larger $L$. These results improve understanding of T2 weighted signal and contrast properties in short T2 tissue imaging with UTE.

INTRODUCTION

In recent years, there has been significant improvement in the ability of MR to directly image bone, the deep layers of cartilage, and other tissues with T2 values of milliseconds or less, that normally produce negligible signal due to rapid T2 decay when imaging with standard pulse sequences [1–5]. Various strategies have been developed to detect signal from such short T2 tissues. In particular, the ultrashort TE (UTE) pulse sequence is one technique where acquisition of the MR signal occurs as soon after the end of the radiofrequency (RF) excitation pulse as possible, with data sampling beginning immediately at k-space center (gradients off) and then proceeding along a radial center-out trajectory for each k-space line with data sampling occurring both during the gradient ramp as well as...
after the maximal gradient value is attained. This approach allows the bulk of the signal in k-space center to be sampled rapidly after RF excitation, with readout of each radial k-space line typically lasting several hundred microseconds. TE is defined as the time between the end of the RF pulse and the beginning of the read gradient, with TE as low as 8 µs being possible using special transmit-receive switching hardware, but typically ranging between 40–200µs for clinical scanners [5].

The signal and contrast properties in short T2 tissue imaging with UTE are different from conventional imaging of long T2 tissues. Due to the extremely short TE, minimal T2 decay occurs during the TE interval when imaging short T2 tissues with UTE. Instead, appreciable decay can occur during RF excitation [6] and k-space readout [7] in UTE sequences, as the duration of these intervals may be comparable to the T2 values of the tissues of interest (milliseconds or less). While the RF duration in UTE can be minimized using very short hard RF pulses (RF pulses of 100µs or less can typically give sufficient signal), the lower limits of k-space readout duration is constrained by gradient limitations to ~500µs. Therefore, depending on the RF duration, T2 decay during k-space readout can be the primary and dominant source of T2 weighted contrast in short T2 tissue imaging with UTE.

The effect on signal due to T2 decay during UTE k-space readout was previously analyzed on point sources assuming constant gradient strength [7]. However, due to gradient slew rate limitations, significant portions of k-space readout in UTE sequences actually occur during the gradient ramp prior to reaching the maximal constant gradient strength. In this manuscript, we therefore use a gradient model that includes both the ramp and maximal constant components to evaluate the differential effects on signal and contrast, of the ramp slew rate (slew) and the gradient constant maximal strength (gmax). Using radially symmetric objects of diameter \(L\) as source spin densities, we find that slew has much greater effect on signal and contrast than gmax when in the “ramp only” regime of \(\gamma \cdot g_{\text{max}}^2/(4\pi \cdot \text{slew}) > 1/(2L)\), whereas both slew and gmax have effect when in the “mixed gradient” regime of \(\gamma \cdot g_{\text{max}}^2/(4\pi \cdot \text{slew}) < 1/(2L)\). Additionally, we find that object size itself is an important parameter in determining signal and contrast, where objects of smaller \(L\) exhibit greater signal loss than objects of larger \(L\) of identical T2 values. We present below the theoretical and numerical results from our analysis, along with experimental verification using gadolinium/manganese chloride solution based short T2 phantoms.

**THEORY AND SIMULATION**

The effects of T2 decay occurring during k-space readout on the resulting image, is equivalent to applying a filter function on the acquired k-space data prior to Fourier transform [8]. To obtain the filter function, the time domain expression for T2 decay \(e^{-t/T2}\) is reparametrized by substitution of the k-space readout trajectory \(k(t)\) [8]. Because UTE employs a radially symmetric “center-out” k-space trajectory that begins on a linear gradient ramp and continues after reaching the constant gradient strength [5], the k-space trajectory is quadratic in time during the gradient ramp, and linear after the constant gradient is reached:

\[
\frac{\gamma \cdot g_{\text{max}}^2}{4\pi \cdot \text{slew}} > \frac{1}{2L}
\]

\[
\frac{\gamma \cdot g_{\text{max}}^2}{(4\pi \cdot \text{slew})} < \frac{1}{2L}
\]

\[
\text{Object size itself is an important parameter in determining signal and contrast, where objects of smaller } L \text{ exhibit greater signal loss than objects of larger } L \text{ of identical T2 values. We present below the theoretical and numerical results from our analysis, along with experimental verification using gadolinium/manganese chloride solution based short T2 phantoms.}

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where \( t \) is time, \( \text{slew} \) is the gradient ramp slew rate, and \( g_{\text{max}} \) is the constant gradient strength.

Substitution of this k-space trajectory into \( e^{-t/T_2} \) yields the following decay filter function \( \text{Dec}(k) \):

\[
\text{Dec}(k) = \begin{cases} 
  e^{-\frac{k r_{\text{ramp}}}{\gamma g_{\text{max}}^2 (4\pi \text{slew})}} & \text{for } k \leq k_{\text{ramp}} \\
  e^{-\left(\sqrt{\frac{4\pi^2 k^2}{\gamma g_{\text{max}}^2 (4\pi \text{slew})^2}} + 2\pi(k-k_{\text{ramp}})\right)} & \text{for } k > k_{\text{ramp}}
\end{cases}
\]

where \( k_{\text{ramp}} = \frac{\gamma g_{\text{max}}^2 (4\pi \text{slew})}{\sqrt{4\pi^2 k^2 + 2\pi k (k-k_{\text{ramp}}) \gamma g_{\text{max}}^2 (4\pi \text{slew})}} \) is \( k \) at the end of the ramp interval. Since UTE does not use refocusing pulses, \( \text{Dec}(k) \) is valid for both \( T_2 \) and \( T_{2^*} \) decay effects. The resulting effect of \( \text{Dec}(k) \) on the image \( I(r) \) of an object with spin density \( s(r) \) and corresponding k-space signal \( S(k) \equiv \text{FT}[s(r)] \), is then given by:

\[
I(r) = \text{FT}[\text{Dec}(k)S(k)]
\]

In figure 1A, we plot \( \text{Dec}(k) \) for varying \( T_2 \) values using typical gradient values of \( \text{slew} = 70 \text{ mT/m/ms} \) and \( g_{\text{max}} = 40 \text{ mT/m} \). When \( T_2 \) is relatively long (e.g. \( T_2 = 10\text{ms} \)), \( \text{Dec}(k) \approx 1 \) for all \( k \), and therefore has minimal effect on the final image. When \( T_2 \) is short, \( \text{Dec}(k) \) curves demonstrate progressive decay for increasing values of \( k \) towards the periphery of k-space, due to the “center-out” sampling trajectory of UTE. The degree of decay becomes greater for decreasing \( T_2 \) values, such that for very short \( T_2 \) values, most of \( \text{Dec}(k) \) is essentially zero except at the most central region in k-space (see figure 1A).

To analyze and quantify the effects of \( \text{Dec}(k) \) on signal and contrast in UTE, we applied \( \text{Dec}(k) \) to a 1D “box image” model, where the source spin density \( s(r) \) was chosen to be a one dimensional box of length \( L \), with sinc function as the associated \( S(k) \) (note mild Gaussian smoothing was also applied to eliminate Gibbs ringing). \( \text{Dec}(k)S(k) \) and \( I(r) \) of this “box image” model are shown in figures 1B–C, demonstrating increasing decay in \( \text{Dec}(k)S(k) \) and \( I(r) \) with decreasing \( T_2 \) values. To permit detailed theoretical analysis, we also evaluated an additional “box k-space” model (similar approach to references [9,10]), where the source spin density \( s(r) \) is chosen to be a sinc function, with the corresponding \( S(k) \) to be a box function of limits \( k_L = \pm 1/(2L) \) in k-space. The box function \( S(k) \) in k-space of this “box k-space” model is much more tractable to detailed analysis, while yielding qualitative and quantitatively similar results to the “box image” model (see below, and also references [9, 10]). In figures 1D–E, we demonstrate that decreasing \( T_2 \) values also leads to increasing decay in \( \text{Dec}(k)S(k) \) and \( I(r) \) for the “box k-space” model.

Defining signal as the central image amplitude \( M \equiv I(0) \) and contrast as \( W \equiv \delta M/\delta \ln T_2 \) [9,11], we then calculated the dependence of \( M \) and \( W \) on \( T_2 \), i.e. the \( T_2 \) weighted signal and contrast relationships due to \( T_2 \) decay during UTE readout. Exact solutions for \( M \) and \( W \) for
the “box k-space” model are given below, whereas for the “box image” model, \( M \) and \( W \) could only be obtained numerically.

\[
M \equiv I(r=0) = \left\{ \frac{LT^2}{\pi} \left( \gamma \frac{slew}{2} T^2 - e^{-\sqrt{\frac{2\pi}{\gamma_slew L} T^2}} \left( \sqrt{\frac{2\pi \gamma_{slew}}{L} + \gamma_slew T^2} \right) \right) \right\} \text{ if } k_{ramp} \geq k_L
\]

\[
W = \frac{\partial M}{\partial \ln T^2} = \left\{ \frac{LT^2}{\pi} \left( \gamma \frac{g_{max}}{slew T^2} \right) \left( 1 - e^{-\sqrt{\frac{2\pi}{\gamma_{slew} L} T^2}} \left( \sqrt{\frac{2\pi \gamma_{slew}}{L} + \gamma_slew T^2} \right) \right) \right\} \text{ if } k_{ramp} \geq k_L
\]

In figures 2A–B, we plot \( M \) and \( W \) versus \( T^2 \) for both the “box image” and “box k-space” models, using sample gradient parameters of \( slew = 70 \text{ mT/m/ms} \) and \( g_{max} = 40 \text{ mT/m} \), and \( L = 10 \text{ mm} \). For \( M \), significant signal losses are evident for \( T^2 \) values below ~10 ms, with a particularly steep drop between ~500 \( \mu \text{s} \) and ~50 \( \mu \text{s} \). For \( T^2 \) values below ~10 \( \mu \text{s} \), \( M \) is negligible. Correspondingly, there is high \( W \) between \( T^2 \) values of ~500 \( \mu \text{s} \) and ~50 \( \mu \text{s} \), consistent with high \( T^2 \) weighted contrast in this range. On the other hand, when \( T^2 \) is greater than ~10 ms or less than ~10 \( \mu \text{s} \), the \( T^2 \) weighted contrast \( W \) is essentially zero.

Similar analytic results can be obtained in 2D and 3D using disks and spheres of diameter \( L \) as the \( s(r) \) for the “box image” model, and sinc-like functions of \( J_1(\pi L r)/r \) and \( (\sin(\pi L r) - \pi L r \cos(\pi L r))/2\pi^2 r^3 \) as the \( s(r) \) for the “box k-space” model. Exact equations for \( M \) and \( W \) in the 2D and 3D “box k-space” models are provided in appendix 1. \( M \) and \( W \) versus \( T^2 \) curves for 2D and 3D are also plotted in figures 2A–B, showing similar curves to 1D except slight shifts to higher \( T^2 \) values. Small quantitative differences between the “box object” and “box k-space” models are also present in 2D and 3D, whereas in 1D the two models yielded virtually identical results. We find empirically that good quantitative agreement between the two models in 2D and 3D can be obtained by substituting an effective diameter \( L_{eff} = \alpha L \) in place of \( L \) in the “box k-space” model, with \( \alpha = 0.85 \) in 2D and \( \alpha = 0.75 \) in 3D.
Effects on signal and contrast by the gradient parameters slew and gmax: “ramp only” versus “mixed gradient” regimes

Since readout duration and k-space trajectory speeds are determined by the gradient parameters slew and gmax, these two parameters significantly influence the degree of T2 decay that occurs during UTE readout, and consequent effects on M and W. In general, higher slew and gmax values lead to faster k-space trajectories, shorter readout durations, and therefore less T2 decay effects on M and W. Conversely, lower slew and gmax values lead to slower k-space trajectories, longer readout durations, and therefore greater T2 decay and signal loss effects on M and W (see below).

Depending on the exact values of slew and gmax, two distinct behaviors exist in UTE, which we term the “ramp only” and “mixed gradient” regimes. The “ramp only” regime occurs when slew is sufficiently low or gmax is sufficiently high such that k_{ramp} > 1/(2L) (i.e. \(\gamma \cdot gmax^2/(4\pi \cdot \text{slew}) > 1/(2L)\)); the “mixed gradient” regime occurs when slew is sufficiently high or gmax sufficiently low such that k_{ramp} < 1/(2L) (i.e. \(\gamma \cdot gmax^2/(4\pi \cdot \text{slew}) < 1/(2L)\)). The behaviors of these two regimes can be understood conceptually using the “box k-space” model, where all of S(k) is contained within the limits of \(k_{L}=±1/(2L)\). When in the “ramp only” regime, k_{ramp} > 1/(2L) and therefore signal acquisition of S(k) during k-space readout occurs only during the gradient ramp portion of readout, so that only slew affects M and W (and not gmax). In contrast, when k_{ramp} < 1/(2L) in the “mixed gradient” regime, a significant amount of S(k) signal acquisition also occurs during the maximum constant gradient portion of k-space readout, and therefore M and W demonstrate dependence on both slew and gmax. Note that the above interpretations of the “ramp only” and “mixed gradient” regimes are effective even when not using the “box k-space” model, since 1/(2L) is a reasonable approximation of the k-space signal extent of S(k) for any given object of size L.

The effects of gmax on signal and contrast, as well as its differential effects between the “ramp only” and “mixed gradient” regimes, are illustrated in figures 3A–B where M and W are plotted for gmax values between 100 and 1 mT/m, with fixed slew = 70 mT/m/ms and L = 10 mm. For these fixed values of slew and L, the “ramp only” regime corresponds to gmax > 13 mT/m and the “mixed gradient” regime corresponds to gmax < 13 mT/m. In figure 3A, we see that the “ramp only” regime curves of M and W (gmax = 100 and 30 mT/m) are identical and overlapping, reflecting the lack of dependence on gmax in the “ramp only” regime. In comparison, the “mixed gradient” regime curves of M in figure 3A (gmax = 10, 3, and 1 mT/m) demonstrate increasing signal loss in M across all T2 values with an overall shift of the M curves to higher T2 values as gmax is decreased (note that the gmax = 10 mT/m curve is nearly identical to the two “ramp only” regime curves, since the value of gmax = 10 mT/m is still very close to the transition between the two regimes). CorRESPONDingly, in figure 3B, we observe that the “ramp only” regime curves of W for gmax = 100 and 30 mT/m are identical and overlapping, whereas the “mixed gradient” regime curves of W for gmax = 10, 3, and 1 mT/m demonstrate shifts to higher T2 values as gmax is decreased. These behaviors are also illustrated by plotting the peak contrast T2 value (T2_{maxW}) versus gmax in figure 3C, where we find constant T2_{maxW} in the “ramp only” regime, compared to increasing T2_{maxW} for decreasing values of gmax in the “mixed gradient” regime.

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In figures 4A–B, we examine the effects of \textit{slew} on signal and contrast by plotting \( M \) and \( W \) for varying \textit{slew} values between 1000 and 10 mT/m/ms, with fixed \( g_{\text{max}} = 10 \text{ mT/m} \) and \( L = 10 \text{ mm} \). For these values of \( g_{\text{max}} \) and \( L \), the “mixed gradient” regime occurs when \( \text{slew} > 43 \text{ mT/m/ms} \) and the “ramp only” regime occurs when \( \text{slew} < 43 \text{ mT/m/ms} \). For the “mixed gradient” regime curves of \( M \) and \( W \) in figures 4A–B (\textit{slew} = 1000, 300, and 100 mT/m/ms), we see that decreasing \textit{slew} leads to increasing signal loss in \( M \) with corresponding shifts of the \( M \) and \( W \) curves to higher \( T_2 \) values. For the “ramp only” regime curves of \( M \) and \( W \) in figures 4A–B (\textit{slew} = 30 and 10 mT/m/ms), further decreases in \textit{slew} similarly lead to increasing signal loss in \( M \) and corresponding shifts of the \( M \) and \( W \) curves to higher \( T_2 \) values, except the changes are even more pronounced in the “ramp only” regime than the curves in the “mixed gradient” regime. Plotting \( T_2_{\text{maxW}} \) versus \textit{slew} in figure 4C similarly demonstrates increasing \( T_2_{\text{maxW}} \) for decreasing \textit{slew} in both the “mixed gradient” and “ramp only” regimes, with the trend more pronounced in the “ramp only” regime.

To examine whether the “ramp only” or the “mixed gradient” regime is more commonly encountered in typical scanning conditions, we evaluated a range of \textit{slew} and \( g_{\text{max}} \) values in figure 5 to see which regime they gave rise to (with varying \( L \) values). We found that \textit{slew} and \( g_{\text{max}} \) values used in typical scanning conditions (e.g. \textit{slew} = 70–200 mT/m/ms and \( g_{\text{max}} = 20–40 \text{ mT/m} \)) generally give rise to the “ramp only” regime, except when \( L \) is relatively small (< 3 mm). In contrast, the “mixed gradient” regime occurs only when very high values of \textit{slew} or very low values \( g_{\text{max}} \) are in use, or when imaging very small objects of small \( L \). Therefore, under typical scanning conditions, the “ramp only” regime is dominant, and the signal and contrast behaviors of \( M \) and \( W \) in UTE are largely influenced by the gradient parameter \textit{slew} rather than \( g_{\text{max}} \).

**Dependency of signal and contrast on \( L \)**

In addition to \textit{slew} and \( g_{\text{max}} \), another parameter that affects signal and contrast due to \( T_2 \) decay during UTE readout, is the size of the object being imaged. This unusual dependency [8] occurs because larger objects have more centrally distributed \( S(k) \) in k-space compared to smaller objects. Since the decay filter function \( \text{Dec}(k) \) in UTE has greater decay in k-space periphery (see figure 1A), \( \text{Dec}(k) \) causes less signal loss in larger objects with more centrally distributed \( S(k) \) than smaller objects with more peripherally distributed \( S(k) \).

As a result, objects with smaller \( L \) demonstrate decreased signal \( M \) and corresponding shifts of the \( M \) and \( W \) curves to higher \( T_2 \) values, when compared to objects with larger \( L \). This is shown in figures 6A–B, where \( M \) and \( W \) curves are plotted for varying values of \( L = 100, 30, 10, 3, \) and 1mm, with fixed \( \text{slew} = 70 \text{ mT/m/ms} \) and \( g_{\text{max}} = 10 \text{ mT/m} \). In figure 6C, plotting \( T_2_{\text{maxW}} \) versus \( L \) similarly demonstrates increasing \( T_2_{\text{maxW}} \) for decreasing \( L \). Of note, this size dependence is observed in both the “ramp only” and “mixed gradient” regimes (in figures 6A–B, the “ramp only” regime is represented by \( L = 100 \) and 30 mm, whereas the “mixed gradient” regime is represented by \( L = 10, 3, \) and 1 mm).

We note here that our analysis thus far has implicitly assumed object size \( L \) to be greater than the size of a single voxel \( \Delta r \). This assumption \( L > \Delta r \) ensures that the limits of \( S(k) \), i.e. \( k_L = 1/(2L) \), is within the data sampling boundaries of each k-space line, i.e. \( k_{\text{max}} = 1/(2\Delta r) \). If
L is smaller than the voxel size (i.e. \( L < \Delta r \)), then \( k_L \) is greater than \( k_{\text{max}} \) and the portions of \( S(k) \) extending beyond \( k_{\text{max}} \) in k-space are truncated and not sampled. This truncation effect can also significantly impact signal and contrast, leading to complex results when occurring together with T2 decay effects during readout. The combined effects of having both truncation and T2 decay during readout can be modeled by adding \( \text{Trunc}(k) \) to Eq. (3):

\[
I(r) = \text{FT} [\text{Dec}(k) \text{Trunc}(k) S(k)]
\]

where \( \text{Trunc}(k) = 1 \) if \( k < k_{\text{max}} \) and \( \text{Trunc}(k) = 0 \) if \( k > k_{\text{max}} \). The resulting effects on signal and contrast after adding \( \text{Trunc}(k) \) are complex and will not be discussed in further detail here. Specific examples of such analyses have been performed for point source objects in UTE radial projection sampling trajectories [7] and Cartesian/spiral sampling trajectories [12] assuming constant gradients without ramp.

**Image blurring**

In addition to signal loss, T2 decay during UTE radial projection readout also causes image blurring. The amount of blurring conferred on a point source assuming a constant gradient has been calculated by Rahmer et al. by analyzing the full-width half max of the point spread function [7]. Similarly, for our analysis, we can also calculate the blurring conferred by T2 decay during readout using the full-width half max in the “box image” model, where we define blurring as the amount of increased box size beyond its original length \( L \) due to blurring, i.e. \( \Delta L = \text{FWHM} - L \). In figure 7A, we plot \( \Delta L \) for varying values of \( g_{\text{max}} \) between 100 and 1 mT/m, with fixed \( \text{slew} = 70 \text{ mT/m/ms} \) and \( L = 10 \text{ mm} \). Similar to signal loss, \( g_{\text{max}} \) has no effect on blurring in the “ramp only” regime for \( g_{\text{max}} = 100 \) and 30 mT/m; whereas decreasing \( g_{\text{max}} \) in the “mixed gradient” regime for \( g_{\text{max}} = 10, 3 \) and 1 mT/m leads to increasing blurring. In figure 7B, we plot \( \Delta L \) for varying values of \( \text{slew} \) between 1000 and 10 mT/m, with fixed \( g_{\text{max}} = 40 \text{ mT/m} \) and \( L = 10 \text{ mm} \).

Again, similar to signal loss, there is increased blurring for decreasing \( \text{slew} \) of 1000, 300, and 100 mT/m/ms in the “mixed gradient” regime, as well as for decreasing \( \text{slew} \) of 30 and 10 mT/m/ms in the “ramp only” regime (with the effect more pronounced in the “ramp only” regime). In figure 7C, we plot \( \Delta L \) for varying object sizes of \( L \) from 100 to 1mm, and again, we see that there is increased blurring as the object size is decreased from 100 to 1mm.

**MATERIALS AND METHODS**

Numerical simulations and theoretical analyses were performed using Mathematica version 8 (Wolfram Research, Champagne, Illinois). All simulations where performed assuming a FOV of 64 mm with a matrix size of 256, yielding a voxel size of 0.25mm and \( k_{\text{max}} = 2000 \text{ m}^{-1} \). Simulations with \( \text{slew} = 70 \text{ mT/m/ms} \) and \( g_{\text{max}} = 40 \text{ mT/m} \) have ramp time of 0.571 ms, constant plateau sampling time of 0.889 ms, and total sampling time of 1.46 ms for the simulation. Simulations with \( \text{slew} \) fixed at 70 mT/m/ms while varying \( g_{\text{max}} \) at 100, 30, 10, 3, and 1 mT/m have corresponding ramp times of 1.158, 0.428, 0.142, 0.043, 0.014 ms, constant plateau sampling times of 0, 1.351, 4.626, 15.636, 46.966 ms, and total sampling times of 1.158, 1.78, 4.769, 15.679, 46.98 ms, respectively. Simulations with \( g_{\text{max}} \) fixed at
10 mT/m and varying slew of 1000, 300, 100, 30 and 10 mT/m/ms have corresponding ramp times of 0.01, 0.033, 0.1, 0.333, 1.0 ms, constant plateau sampling times of 4.692, 4.681, 4.647, 4.531, 4.197 ms, and total sampling times of 4.702, 4.713, 4.747, 4.864, 5.197 ms, respectively. When deriving predicted signal amplitude curves for the spherical phantom experiments, we instead used FOV of 150 mm with a matrix size of 256 and \( k_{\text{max}} = 853.33 \) m\(^{-1}\) to match the experimental conditions. In addition, we also included in our simulations for the phantom experiments the small amounts of predicted amplitude loss from T2 decay during the 0.04 ms RF pulse [6] and the 0.03 ms TE interval.

We constructed short T2 phantoms by filling spherical plastic containers of inner diameters 10 mm and 38 mm, with gadolinium DTPA and manganese chloride doped water solutions. Varying concentrations of manganese chloride and gadolinium led to phantoms having a range of T2 values between 0.1 and 10 ms. We imaged these phantoms using a 3D ultrashort TE sequence on a GE 3T scanner with 40µs hard RF excitation pulse, TE 30 µs, FOV 150 mm \( \times \) 150 mm, and 5000 k-space projections regridded to a 256 \( \times \) 256 image matrix. One set of experiments was performed by imaging 10 mm phantoms while keeping \( \text{slew} \) fixed at 70 mT/m/ms while varying \( \text{gmax} \) at 40, 20, 10, and 5 mT/m (by setting bandwidth at 125, 62.5, 31.25, 15.63 kHz) – which led to corresponding ramp times of 0.552, 0.28, 0.144, 0.064 ms, constant plateau sampling times of 0.232, 0.888, 1.968, 4.032 ms, and total sampling times of 0.784, 1.168, 2.112, 4.096 ms, respectively. Another set of experiments was performed by imaging 10mm phantoms while keeping \( \text{gmax} \) fixed at 10 mT/m (bandwidth fixed at 31.25 kHz) and varying \( \text{slew} \) of 122, 68 and 34, and 18 mT/m/ms – which led to ramp times of 0.08, 0.144, 0.288, 0.56 ms, constant plateau sampling times of 2.0, 1.968, 1.888, 1.776 ms, and total sampling times of 2.08, 2.112, 2.176, 2.336 ms, respectively. The last set of experiments was performed by imaging both 10mm and 38mm phantoms with \( \text{slew} \) fixed at 70 mT/m/ms and \( \text{gmax} \) fixed at 10 mT/m (bandwidth 31.25 kHz) – with corresponding ramp time of 0.144 ms, constant plateau sampling time of 1.968 ms, and total sampling time of 2.112 ms.

**RESULTS**

We performed experimental verification of our theoretical/numerical results by scanning spherical 10mm and 38 mm diameter MnCl\(_2\)/gadolinium solution phantoms with a range of T2 values between ~100µs and ~10ms. A 3D UTE sequence with hard pulse excitation was utilized, with varying \( \text{slew} \) and \( \text{gmax} \) values. Sample images from our scans are given in figure 8A.

We first scanned the 10mm diameter phantoms with \( \text{slew} \) fixed at 70 mT/m/ms and varying \( \text{gmax} \) values of 40, 20, 10, and 5 mT/m. With these values of \( \text{L} \) and \( \text{slew} \), the transition from “ramp only” to “mixed gradient” regimes occurs when \( \text{gmax} \) drops below 13 mT/m. The measured signal intensities are plotted in figure 8B. As expected, the \( \text{gmax} = 40 \) and 20 mT/m measurements do not demonstrate significant differences as they correspond to the “ramp only” regime where \( \text{gmax} \) has no effect. In comparison, the “mixed gradient” regime measurements with \( \text{gmax} = 10 \) and 5 mT/m show decreasing signal as \( \text{gmax} \) is decreased. The predicted theoretical curves for these values of \( \text{gmax}, \text{slew}, \) and \( \text{L} \) are plotted for comparison, demonstrating good agreement with the measured values.
We then scanned the 10mm diameter phantoms with fixed $g_{\text{max}}$ at 10 mT/m and varying $slew$ values of 122, 68 and 34, and 18 mT/m/ms. For these values of $g_{\text{max}}$ and $L$, the transition between the “mixed gradient” to “ramp only” regimes occurs when $slew$ decreases below 43 mT/m/ms. As plotted in figure 8C, decreasing $slew$ leads to decreasing signal intensities in both the “mixed gradient” and “ramp only” regimes – but with the changes greater when in the “ramp only” regimes with $slew = 30$ and $15$ mT/m/ms. Again, the predicted theoretical curves are in good accordance with the measured values (figure 8C).

Finally, we scanned both 10mm and 38mm diameter phantoms, with fixed $g_{\text{max}} = 40$ mT/m and $slew = 70$ mT/m/ms. The larger 38mm diameter phantoms demonstrate greater signal intensities compared to smaller 10mm diameter phantoms of identical T2 values (figure 8D), as predicted by our theoretical analysis. The measured values also demonstrate good accordance with predicted theoretical curves.

**DISCUSSION**

We modeled the T2 weighted signal and contrast properties due to decay during k-space readout for UTE sequence imaging, using a gradient model that incorporates both the gradient ramp $slew$ rate and the maximal constant gradient strength $g_{\text{max}}$, with objects of size $L$. For the “ramp only” regime, $slew$ is the primary gradient parameter affecting signal and contrast. In comparison, when in the “mixed gradient” regime typified by high $slew$ values, low $g_{\text{max}}$ values, or small object sizes $L$, both $slew$ and $g_{\text{max}}$ significantly affect signal and contrast. Typical values of $slew$ and $g_{\text{max}}$ used in scanning generally give rise to the “ramp only” regime, such that $slew$ is usually the dominant parameter affecting signal and contrast behaviors due to T2 decay during UTE readout. In general, decreasing $slew$ (and decreasing $g_{\text{max}}$ when in the “mixed gradient” regime) decreases signal and shifts the contrast peak to higher T2 values. Knowing the effects of varying $slew$ and $g_{\text{max}}$ can be important in various practical scanning situations, such as: a) when comparing the slew rates of different coil sets on a scanner (one may desire a lower slew rate to reduce bioeffects such as peripheral nerve stimulation), b) when comparing the performance of different scanners using different coil sets and slew rates, and c) when varying the scanner bandwidth (which alters $g_{\text{max}}$) in order to adjust imaging effects on chemical shift and SNR.

Additionally, we find that the diameter $L$, an intrinsic property of the source object, also has effect on signal amplitude – where objects of decreasing $L$ demonstrate decreased signal with contrast peak at higher T2 values. Although the dependence of signal and contrast on $L$ is somewhat unusual, similar effects have been described in other situations where the readout duration is long compared to the T2 values of interest – e.g. imaging with EPI and FSE long echo train sequences [8,13]. Further, it has been recently demonstrated that measured phase also depends on object size in UTE imaging of short T2 tissues, due to related mechanisms [9].

The signal curves for $M$ demonstrate steep slopes between T2 values from ~50us to 500us, with corresponding high contrast $W$ in this range of T2 values. Since clinically relevant pathologies typically manifest as increases in T2 in the organ/tissue of interest, this suggests high inherent sensitivity of UTE imaging in disease detection for tissues with T2 values in
this range, such as cortical bone (T2 ~350µs). For other short T2 tissues whose T2 values fall outside of this range (e.g. tendons and ligaments of T2 ~2–3 ms), our results may also provide a method to increase contrast, by adjusting $slew$ and $g_{\text{max}}$ to modify the $W$ curves and expected $T_{2\text{maxW}}$ values. We do caution, however, that adjusting $slew$ and $g_{\text{max}}$ may simultaneously lead to tradeoffs in resolution due to T2 blurring (see above section on blurring, and reference [5]), and therefore must be carefully considered.

An active area of investigation is the development of quantitative UTE-based techniques to correlate measured tissue signal intensities with disease. One such example is bone water quantification where cortical bone signal intensities measured with UTE are used to estimate proton density and cortical bone water content in osteoporosis [14, 15]. Our models should help improve proton density quantification by determining the amount of T2 weighting due to decay during readout that is embedded in the measured signal intensities. The models of T2 weighted signal and contrast determination presented in this paper should be generally beneficial in the development of current and future UTE based quantitative methods.

Recent interest in short T2 imaging has led to the use of numerous other sequences such as SWIFT, ZTE, and WASPI [1–4]. For all of these sequences, T2 decay during k-space readout should play an important and perhaps dominant role in T2 weighted signal and contrast, due to the comparable k-space readout durations and short T2 tissues. One distinction, however, is that many of these sequences begin the k-space readout with the gradient already at its maximal value $g_{\text{max}}$ (no k-space sampling on the gradient ramp) – in which case T2 weighted signal and contrast due to decay during k-space readout can be analyzed via the same approach as described here, but with $slew=\infty$ resulting in $g_{\text{max}}$ being the dominant gradient parameter instead. Further, since smaller objects with more peripherally distributed $S(k)$ will experience greater T2 decay during k-space readout via similar mechanisms, the signal and contrast dependence on object size described here should be similarly present in those other short T2 imaging techniques.

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\[ M_{3D} = \begin{cases} 
\frac{3L^3}{4\pi^3} T^2 \gamma 
& \left\{ \begin{array}{l}
\frac{30\text{slew}^3 T^2 \gamma^3}{\pi^3} T^2 \\
-\frac{1}{L^2} - \sqrt{2\pi / T^2 \text{slew} \gamma} \frac{L}{L^2} \left( \sqrt{\frac{2\pi \text{slew} \gamma}{L} + \text{slew} T^2 \gamma} \right) \\
+30\pi L \text{slew}^2 T^2 \gamma^2 + 10 \sqrt{2L} (\pi \text{slew} \gamma)^{3/2} T^2 \\
+ \frac{2 \text{slew} \gamma}{L^{5/2}} + 5\pi \text{slew} T^2 \gamma \\
if \text{slew} T^2 \gamma > 1/(2L)
\end{array} \right. \\
\frac{g_{\max}^2 \gamma^2}{\text{slew}^2 (g_{\max}^2 + 4g_{\max} \text{slew} T^2 + 8\text{slew}^2 T^2)} \\
\frac{g_{\max}^2 \gamma^2}{\text{slew}^2} \frac{2\pi}{L^2} \left( g_{\max} T^2 \gamma^2 + 2\pi g_{\max} L T^2 \gamma + \pi^2 \right) \\
+ \frac{\gamma}{\text{slew}^2} \left( 120\text{slew}^2 T^2 \gamma - e^{-g_{\max} / \text{slew}} \gamma \left( +20g_{\max}^2 \text{slew}^2 T^2 \gamma (g_{\max} \gamma + 3\text{slew} T^2 \gamma) \\
+g_{\max}^4 (g_{\max} \gamma + 5\text{slew} T^2 \gamma) \right) \right) \\
if \text{slew} \gamma \leq 1/(2L)
\end{cases} \]
\[ W_{\text{3D}} = \frac{6L^3T_2}{\pi} \left( \frac{T_2}{2\pi} - \frac{\sqrt{2\pi}}{T_2^2 \sqrt{\text{slew}^3 L^2}} e^{-\sqrt{2\pi / T^2 \text{slew}^3 L^2}} \left( 30L^2 \text{slew}^3 T^2 T^2 \gamma^2 \left( \sqrt{2\pi \text{slew} \gamma / L} + \text{slew} T \gamma \right) \right) + 30\pi \text{slew}^2 T^3 \gamma^2 \right) \\
+ 10T^2 \sqrt{2\pi \text{slew}^3 \gamma^3 / L} + \sqrt{2\pi \text{slew} \gamma / L} + 5\pi^2 \text{slew} T \gamma \right) \\
+ \frac{1}{2\pi^2} \left( 30\text{slew}^3 T^2 \gamma^3 - \frac{1}{L^2} e^{-\sqrt{2\pi / T^2 \text{slew}^3 L^2}} \left( 30L^2 \text{slew}^2 T^2 \gamma^2 \left( \sqrt{2\pi \text{slew} \gamma / L} + \text{slew} T \gamma \right) + 30\pi \text{slew}^2 T^3 \gamma^2 \right) \\
+ 10T^2 \sqrt{2\pi \text{slew}^3 \gamma^3 / L} + \sqrt{2\pi \text{slew} \gamma / L} + 5\pi^2 \text{slew} T \gamma \right) \right) \text{ if } k_{\text{ramp}} \geq 1 / (2L) \\
+ \frac{6L^3T_2}{\pi} \left( \frac{\gamma}{8\pi^2} e^{-\gamma / \text{slew} T^2} g_{\text{max}} \left( \frac{\text{max}^2 \gamma^2 (g_{\text{max}}^2 + 4 \text{slew}^2 T_{\text{2max}} + 8 \text{slew}^2 T_{\text{2}}^2)}{\text{slew}^2} \right) \\
- 4e^{\left( \frac{\gamma}{\text{slew}^2} - \frac{2\pi}{L^2} \right)^2 / 2g_{\text{max}} T^2} \left( 2g_{\text{max}}^2 L^2 T^2 \gamma^2 + 2\pi g_{\text{max}} L T^2 \gamma + \pi^2 \right) \right) \\
+ \frac{\gamma T^2}{8\pi^2} \left( e^{-\gamma / \text{slew} T^2} g_{\text{max}} \left( \frac{\text{max}^2 \gamma^2 (g_{\text{max}}^2 + 4 \text{slew}^2 T_{\text{2max}} + 8 \text{slew}^2 T_{\text{2}}^2)}{\text{slew}^2} \right) \\
- 4e^{\left( \frac{\gamma}{\text{slew}^2} - \frac{2\pi}{L^2} \right)^2 / 2g_{\text{max}} T^2} \left( 2g_{\text{max}}^2 L^2 T^2 \gamma^2 + 2\pi g_{\text{max}} L T^2 \gamma + \pi^2 \right) \right) \\
+ e^{-\gamma / \text{slew} T^2} g_{\text{max}} \left( \frac{\text{max}^2 \gamma^2 (16T^2 \text{slew}^2 + 4 \text{slew} T_{\text{2max}} \text{slew})}{\text{slew}^2} \right) \\
- 4e^{\left( \frac{\gamma}{\text{slew}^2} - \frac{2\pi}{L^2} \right)^2 / 2g_{\text{max}} T^2} \left( 4g_{\text{max}}^2 L^2 T^2 \gamma^2 + 2\pi g_{\text{max}} L \gamma \right) \\
+ \frac{2e^{\left( \frac{\gamma}{\text{slew}^2} - \frac{2\pi}{L^2} \right)^2 / 2g_{\text{max}} T^2}}{g_{\text{max}} L^2 T^2 \gamma^2} \left( 2g_{\text{max}}^2 L^2 T^2 \gamma^2 + 2\pi g_{\text{max}} L T^2 \gamma + \pi^2 \right) \\
+ \frac{\gamma}{\text{slew}^2} \left( 600T^4 \gamma \text{slew}^5 - e^{-\gamma / \text{slew} T^2} \sqrt{\frac{\text{max}^2 \gamma^2}{\text{slew}}} \left( 5 \text{slew}^2 T^2 \gamma + \text{max} \gamma \right) \right) \right) \text{ if } k_{\text{ramp}} \leq 1 / (2L) \]
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Fig 1. Effects of the filter function $\text{Dec}(k)$ on k-space signal $S(k)$ and the resulting image $I(r)$
A) $\text{Dec}(k)$, the k-space filter function given in equation 2, represents the effects of T2 decay during UTE k-space readout. 
B–C) $\text{Dec}(k)S(k)$ and $I(r) = \text{FT}[\text{Dec}(k)S(k)]$ in the “box image” model showing increasing decay for decreasing T2 values. 
D–E) $\text{Dec}(k)S(k)$ and $I(r) = \text{FT}[\text{Dec}(k)S(k)]$ in the “box k-space” model showing increasing decay for decreasing T2 values. Length is displayed in units of voxel size $\Delta r$, and k-space is displayed in units of $k_{\text{max}} = 1/(2\Delta r)$. Parameters for Figure 1 were set at: $s\text{lew} = 70$ mT/m/ms, $g_{\text{max}} = 40$ mT/m, $L = 10$ mm, $\Delta r = 0.25$ mm, and $k_{\text{max}} = 2000$ m$^{-1}$.
Figure 2. T2 weighted signal and contrast curves due to the effects of Dec(k)

A) Signal \( M \) versus \( T2 \) (with \( L = 10 \) mm, \( slew = 70 \) mT/m/ms, \( g_{\text{max}} = 40 \) mT/m), for 1D/2D/3D “box image” and “box k-space” models. Steep signal drop occurs between \( T2 \sim 500\mu s \) and \( 50\mu s \). 

B) Contrast \( W \) versus \( T2 \) (with \( L = 10 \) mm, \( slew = 70 \) mT/m/ms, \( g_{\text{max}} = 40 \) mT/m). Corresponding to the steep portions of the \( M \) versus \( T2 \) curves, there is high \( W \) for \( T2 \) values between \( 500\mu s \) and \( 50\mu s \).
Fig 3. The effects of $g_{\text{max}}$ on signal and contrast

A) $M$ versus T2 curves for $g_{\text{max}} = 100, 30, 10, 3,$ and $1$ mT/m (with $slew = 70$ mT/m/ms, $L = 10$ mm). The transition from “ramp only” to “mixed gradient” regimes occurs at $g_{\text{max}} = 13$ mT/m, such that the $g_{\text{max}} = 100$ and 30 mT/m curves correspond to the “ramp only” regime and the $g_{\text{max}} = 10, 3,$ and $1$ mT/m curves correspond to the “mixed gradient” regime. The “ramp only” regime curves are identical and overlapping because $g_{\text{max}}$ has no effect in the “ramp only” regime. In the “mixed gradient” regime, lower $g_{\text{max}}$ causes decreased signal $M$ at all T2 values. Note that the $g_{\text{max}} = 10$ mT/m curve is very close to the transition between the two regimes, such that it is adjacent to but not identical to the two “ramp only” regime curves. B) Corresponding $W$ versus T2 curves. The “ramp only” regime curves for $g_{\text{max}} = 100$ and 30 mT/m are identical and overlapping. In the “mixed gradient” regime, the curves are shifted to higher T2 values as $g_{\text{max}}$ is decreased. C) $T_{2,\text{maxW}}$, the T2 value at which peak contrast $W$ occurs, is plotted versus $g_{\text{max}}$. $T_{2,\text{maxW}}$ is constant when in the “ramp only”, whereas $T_{2,\text{maxW}}$ increases for decreasing $g_{\text{max}}$ in the “mixed gradient” regime.
**Fig 4. The effects of slew on signal and contrast**

A) $M$ versus T2 curves for $slew = 1000, 300, 100, 30,$ and $10$ mT/m/ms (with $g_{max} = 10$ mT/m/ms, $L = 10$ mm). The transition from “mixed gradient” to “ramp only” regimes occurs at $slew = 43$ mT/m/ms, such that the $slew = 1000, 300,$ and $100$ mT/m/ms curves correspond to the “mixed gradient” regime and the $slew = 30$ and $10$ mT/m/ms curves correspond to the “ramp only” regime. In both regimes, lower $slew$ causes decreased signal $M$ at all T2 values.

B) Corresponding $W$ versus T2 curves. In both regimes, the curves are shifted to higher T2 values as $slew$ is decreased.

C) $T_{2_{max}}W$ versus $slew$. $T_{2_{max}}W$ increases for decreasing $slew$ in both regimes.
Fig 5. Combinations of $g_{\text{max}}$ and $slew$ that correspond to “ramp only” versus “mixed gradient” regimes
The range of $g_{\text{max}}$ and $slew$ values that correspond to the “ramp only” regime are color-shaded, for $L = 100, 30, 10,$ and $3$ mm. A dashed box surrounds a region of $slew$ between $70–200$ mT/m/ms and $g_{\text{max}}$ between $20–40$ mT/m, signifying sample “typical” scanning conditions.
Figure 6. The effects of object size $L$ on signal and contrast

A) $M$ versus $T2$ curves for $L = 100, 30, 10, 3,$ and $1$ mm (with $g_{max} = 10$ mT/m, $slew = 70$ mT/m/ms). The “ramp only” regime is represented by the $L = 100$ and $30$ mm curves, whereas the “mixed gradient” regime is represented by $L = 10, 3,$ and $1$ mm curves. In both regimes, smaller $L$ causes decreased signal $M$ at all $T2$ values. 

B) Corresponding $W$ versus $T2$ curves. In both regimes, the curves are shifted to higher $T2$ values as $L$ is decreased. 

C) $T2_{maxW}$ versus $L$ curves. $T2_{maxW}$ increases for decreasing $L$ in both regimes.

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Figure 7. Blurring effects due to T2 decay during UTE readout
Blurring is defined as the amount of increased box size (at full-width half max) beyond its original length $L$, i.e. $\Delta L = \text{FWHM}-L$ (see text for full details). Similar to signal loss, there is more blurring as when $g_{\text{max}}$ is decreased in the “mixed gradient” regime, when $slew$ is decreased, and for smaller $L$. A) $\Delta L$ versus T2 curves for $g_{\text{max}} = 100, 30, 10, 3, \text{ and } 1 \text{ mT/m}$ (with $slew = 70 \text{ mT/m/ms, } L = 10 \text{ mm}$). B) $\Delta L$ versus T2 curves for $slew = 1000, 300, 100, 30, \text{ and } 10 \text{ mT/m/ms}$ (with $g_{\text{max}} = 40 \text{ mT/m, } L = 10 \text{ mm}$). C) $\Delta L$ versus T2 curves for $L = 100, 30, 10, 3, \text{ and } 1 \text{ mm}$ (with $g_{\text{max}} = 40 \text{ mT/m, } slew = 70 \text{ mT/m/ms}$).
Figure 8. Experimental validation using spherical short T2 solution phantoms
A) Sample 3D UTE images of 10mm and 38mm diameter spherical phantoms of varying gadolinium/manganese chloride concentrations, with T2 values of 10.1, 2.0, 1.1, 0.74, 0.34, and 0.19ms. B) Measured signal intensities from 10mm diameter phantoms are plotted (“•”) at varying values of $g_{\text{max}} = 40, 20, 10,$ and 5 mT/m (with $\text{slew} = 70$ mT/m/ms). Good agreement with predicted theoretical curves is demonstrated, including in the “ramp only” regime measurements for $g_{\text{max}} = 40$ and 20 mT/m (the transition from “ramp only” to “mixed gradient” regime occurs at $g_{\text{max}} = 13$ mT/m). C) Measured signal intensities from 10mm diameter phantoms (“•”) for varying $\text{slew} = 122, 68, 34,$ and 18 mT/m/ms, show good agreement with predicted theoretical curves. D) Measured signal intensities from 10mm and 38mm diameter phantoms (“•”) with $\text{slew}$ of 70 mT/m/ms and $g_{\text{max}}$ of 40 mT/m. The smaller 10mm diameter phantoms demonstrate lower signal intensities compared to the larger 38mm diameter phantoms, in good agreement with theoretically predicted curves.