General-relativistic neutrino-radiation magnetohydrodynamics simulation of black hole-neutron star mergers for seconds

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Seconds-long numerical-relativity simulations for black hole-neutron star mergers are performed for the first time to obtain a self-consistent picture of the merger and post-merger evolution processes. To investigate the case that tidal disruption takes place, we choose the initial mass of the black hole to be 5.4\(M_\odot\) or 8.1\(M_\odot\) with the dimensionless spin of 0.75. The neutron-star mass is fixed to be 1.35\(M_\odot\). We find that after the tidal disruption, dynamical mass ejection takes place spending \(\lesssim 10\) ms together with the formation of a massive accretion disk. Subsequently, the magnetic field in the disk is amplified by the magnetic winding and magnetorotational instability, establishing a turbulent state and inducing the angular momentum transport. The post-merger mass ejection by the magnetically-induced viscous effect sets in at \(\sim 300-500\) ms after the tidal disruption, at which the neutrino luminosity drops below \(\sim 10^{49.5}\) erg/s, and continues for several hundreds ms. A magnetosphere near the rotational axis of the black hole is developed after the matter and magnetic flux fall into the black hole from the accretion disk, and high-intensity Poynting flux generation sets in at a few hundreds ms after the tidal disruption. The intensity of the Poynting flux becomes low after the significant post-merger mass ejection, because the opening angle of the magnetosphere increases. The lifetime for the stage with the strong Poynting flux is 1–2 s, which agrees with the typical duration of short-hard gamma-ray bursts.

I. INTRODUCTION

The opening for the era of the gravitational-wave astronomy was heralded by the first observation of a binary black hole merger, referred to as GW150914 \cite{1}. To date, \(\sim 80\) binary black hole merger events have been already observed by advanced LIGO and advanced Virgo \cite{2,3}. In addition to binary black holes, a couple of neutron-star binaries have been also observed. In particular, associated with the first binary neutron star merger event, GW170817 \cite{4}, a wide variety of the signals of the electromagnetic counterpart were successfully detected \cite{5,6}, and the multi-messenger astronomy including gravitational-wave observation was opened from this event.

In addition the gravitational-wave signals from the black hole-neutron star mergers referred to as GW200105 and GW200115 were detected in 2020 \cite{7}. These events proved that black hole-neutron star binaries exist in nature. Although any electromagnetic counterpart was not detected for these two events, a number of numerical-relativity simulations for the black hole-neutron star mergers have predicted that tidal disruption of the neutron star and subsequent mass ejection should take place if the parameters of the source (black-hole mass, black-hole spin, and neutron-star compactness) are in an appropriate range \cite{8,9}. If the remnant black hole is rapidly spinning and is surrounded by a magnetized massive torus, an ultra-relativistic jet is likely to drive a short-hard gamma-ray burst \cite{10,12}. In the presence of mass ejection, the \(r\)-process nucleosynthesis inevitably proceeds \cite{13,15}, and subsequently, the ejecta should shine with a high luminosity associated with the thermal energy generated by the radioactive decay of neutron-rich heavy elements \cite{14,15}. Since the sensitivity of gravitational-wave detectors and electromagnetic telescopes is improved year by year, it is quite natural to expect that electromagnetic counterparts of black hole-neutron star mergers are observed in the near future, if the distance to the source is within several hundreds Mpc, and thus, black hole-neutron star mergers are among the promising sources for the multi-messenger astronomy. In this situation, the theoretical studies to elucidate the entire process from the tidal disruption to the post-merger evolution are required to predict the observable signals.

In the last 15 years, a variety of numerical-relativity simulations have been performed for black hole-neutron star mergers \cite{16,60} improving the input physics and grid resolutions, and the processes of tidal disruption and subsequent accretion disk formation, merger remnants, dynamical mass ejection, gravitational waves, and neutrino emissivity have been extensively studied. However, all these work have focused primarily on the inspiral to early merger stages, and hence, the long-term post-merger process has not been explored in these simulations. To compensate this drawback, many numerical simulations (viscous hydrodynamics or magnetohydrodynamics simulations) have been also performed for exploring long-term evolution of the accretion disks (or tori) around a black hole \cite{51,60}, and studied the post-merger mass ejection mechanisms and the properties of the post-merger ejecta.
These work have reported that the post-merger mass ejection is driven primarily by a viscous hydrodynamics effect induced by the magnetohydrodynamics turbulence in the accretion disks and by a Lorentz force associated with the amplified magnetic fields. Although these work are important for understanding the post-merger mass ejection mechanisms, the initial conditions for the simulations were ad hoc or some of important physical inputs were absent, and hence, the conclusive quantitative details such as quantitative properties of the post-merger ejecta have not been fully understood yet.

In order to acquire the full understanding of the black hole-neutron star mergers and associated mass ejection processes, we need to perform a self-consistent simulation starting from an inspiral stage throughout the post-merger stage. Specifically, the post-merger evolution has to be followed at least for a few seconds, because the post-merger mass ejection takes place spending the timescale of $\sim 1$ s. Furthermore, to explore the generation mechanism of short-hard gamma-ray bursts, a simulation with the duration $\gtrsim 1$ s is needed because the typical duration of them is $\sim 1$ s with the longest duration of $\sim 2$ s [11, 12]. Keeping in mind these timescales, in this paper, we perform general-relativistic neutrino-radiation magnetohydrodynamics simulations of black hole-neutron star mergers for $\approx 1$–2 s. Here, we emphasize that both the neutrino radiation transfer and magnetohydrodynamics effects are inevitable elements for determining the evolution of the merger remnant. In this long-term simulation with the relevant physics, the magnetohydrodynamics turbulence and associated angular-momentum transport in the accretion disk are naturally taken into account, and furthermore, a black-hole magnetosphere in the vicinity of the rotation axis of the remnant spinning black hole, which could be suitable for generating a short-hard gamma-ray burst, also naturally emerges.

This paper is organized as follows. In Sec. [II] we briefly summarize the method and initial setup for the numerical simulation. In Sec. [III] we present the numerical results focusing on the entire evolution process, mass ejection mechanisms, and collimated electromagnetic outflow developed near the rotation axis of the black hole. Finally, we conclude this work in Sec. [IV]. Throughout this paper, we adopt the geometrical units in which $G = c = 1$, where $G$ and $c$ are the gravitational constant and the speed of light, respectively.

**II. METHODS**

Our numerical implementation for the present simulations is the same as that in Ref. [11] except for the ideal magnetohydrodynamics part for which we implement the scheme used in Ref. [39]. Specifically, we solve Einstein’s equation by a puncture-Baumgarte-Shapiro-Shibata-Nakamura (BSSN) formalism [67, 71], incorporating a Z4c-type constraint-propagation prescription [38, 72]. In this work, the original version of the BSSN formalism [67] is employed. The fourth-order finite-differencing scheme is applied to discretize the gravitational-field equation. Magnetohydrodynamics equations are solved in a high-resolution shock capturing scheme [73, 75] together with the second-order constrained-transport scheme [76] and Balsara’s flux-preserving mesh refinement scheme [77]. Neutrino transfer is handled using a leakage-based scheme [75] together with a truncated moment formalism using a closure relation for the free-streaming component [79, 80]. Neutrino heating and absorption on free nucleons are incorporated using the updated numerical procedure [81].

The simulation is performed using a fixed-mesh refinement (FMR) algorithm with the equatorial symmetry imposed at $z = 0$. The $i$-th refinement level covers a half cubic region of $[-L_i : L_i] \times [-L_i : L_i] \times [0 : L_i]$ where $L_i = N \Delta x_i$ and $\Delta x_i$ is the grid spacing for the $i$-th level. The grid spacing for each level is determined by $\Delta x_i = 2\Delta x_{i+1}$ ($i = 1, 2, \cdots, i_{\text{max}} - 1$) with $\Delta x_{i_{\text{max}}} = 400$ m for low-resolution runs and $\Delta x_{i_{\text{max}}} = 270$ m for high-resolution runs. $i_{\text{max}}$ is chosen to be 9 or 10. The values of $N$ are 170 or 192 for low-resolution runs and 234 or 282 for high-resolution runs, respectively (cf. Table I).

During the merger stage, the black hole is kicked mainly by the back reaction of the dynamical mass ejection and the resulting velocity is $200$–$400$ km/s in our present setting. Thus, the black hole moves toward a refinement boundary of the finest FMR level with time and eventually escapes from the highest-resolution level in the absence of any prescription. To keep the black hole in the highest-resolution level, we control the shift vector by modifying the evolution equation in the following prescription:

$$\partial_t \beta^i = \frac{3}{4} \tilde{\gamma}^{ij} (F_j + \partial_t F_j \Delta t) - \frac{v^i_{\text{BH}}}{T_{\text{relax}}}$$

for $T_{\text{sta}} < t < T_{\text{sta}} + T_{\text{relax}},$ \hspace{1cm} (1)

$$\partial_t \beta^i = \frac{3}{4} \tilde{\gamma}^{ij} (F_j + \partial_t F_j \Delta t)$$

for other cases, \hspace{1cm} (2)

where $\beta^i$ is the shift vector, $\tilde{\gamma}^{ij}$ is the conformal three-metric, $F_i = \delta^{ik} \partial_k \tilde{\gamma}^{ij}$ is the auxiliary variable in the original version of the BSSN formalism, $\Delta t$ is the time-step interval, and $v^i_{\text{BH}}, T_{\text{relax}},$ and $T_{\text{sta}}$ are constants which we determine appropriately based on the numerical result. $v^i_{\text{BH}}$ is the coordinate velocity of the black-hole center (the location of the puncture) just before modifying the shift vector, which is of order $10^{-3} c$ as we already mentioned. $T_{\text{relax}}$ is the relaxation time, which we choose $T_{\text{relax}} = 40$ ms. $T_{\text{sta}}$ is the starting time of this prescription, and it is set to be $T_{\text{sta}} \approx 100$–$200$ ms depending on the model.

We stop the time evolution of the gravitational field at a certain moment after the ratio of the rest mass of the remnant disk to the black-hole mass drops below $10^{-2}$. This prescription is reasonable because the self-gravity of the matter located outside the black hole can be safely...
neglected and the gravitational field is approximately stationary in such a low-mass disk stage.

For modeling the neutron-star matter, we employ a nuclear-theory-based finite-temperature equation of state (EOS) referred to as DD2 [82] for a high-density range and Helmholtz EOS [83] for a low-density range. Initial data are given by calculating a quasi-equilibrium state of black hole-neutron star binaries in a quasi-circular orbit assuming the neutrinoless beta-equilibrium cold state [41]. The initial gravitational mass of the neutron star is set to be $M_{\text{NS}} = 1.35M_\odot$ following Ref. [41]. The circumferential radius of the isolated spherical neutron star of mass $1.35M_\odot$ is $\sim 13.2$ km with this EOS.

For the initial black-hole mass, we choose $M_{\text{BH},0} = 5.4M_\odot$ or $8.1M_\odot$; the mass ratio of the black hole to the neutron star is $Q := M_{\text{BH},0}/M_{\text{NS}} = 4$ or 6. The initial dimensionless spin parameter of the black hole is set to be 0.75. With such a spin, tidal disruption of the neutron star with $M_{\text{NS}} = 1.35M_\odot$ takes place for a wide range of $Q$. The initial orbital angular velocity $\Omega_0$ is set to be $m_0\Omega_0 = 0.056$ for $Q = 4$ and 0.064 for $Q = 6$, where $m_0$ is the sum of the initial black-hole mass and neutron-star mass, i.e., $m_0 = M_{\text{BH},0} + M_{\text{NS}} = 1.35(Q + 1)M_\odot$. In this initial setup, the binary merges after about three orbits. We note that the binary parameter for $Q = 4$ is the same as that employed for the DD2 EOS in our previous paper [41].

We initially superimpose a poloidal magnetic field confined in the neutron star. Following our previous work [39], the poloidal field is given in terms of the vector potential as

$$A_j = \{-y - y_{\text{NS}}\} \delta_j^x + (x - x_{\text{NS}}) \delta_j^y \}
\times A_b \max(P/P_{\max} - 10^{-3}, 0)^2,$$

where $(x_{\text{NS}}, y_{\text{NS}})$ is the coordinate position of the neutron-star center (location of the maximum rest-mass density) on the orbital plane, $P$ is the pressure, $P_{\max}$ is the maximum pressure, and $j = x, y,$ and $z$. $A_b$ is a constant and is chosen so that the initial maximum magnetic-field strength $b_{0,\max}$ is $3 \times 10^{16}$ G or $5 \times 10^{16}$ G. These values are chosen to get a strong magnetic field in the remnant disk formed after tidal disruption of the neutron star in a short timescale after the merger. The strong magnetic field is required to resolve the fastest growing mode of the magnetorotational instability (MRI) [54, 55] in the accretion disk with the limited grid resolution, because its wavelength is proportional to the magnetic-field strength. Although such strong fields are not realistic in orbiting neutron stars, the resulting turbulent state in the accretion disk established by the MRI is not likely to depend strongly on the initial magnetic-field strength. Thus, it is natural to consider that the resulting strong magnetic field and turbulent state will be established even for the case that we start a simulation from a much weaker magnetic-field strength in the presence of a sufficient grid resolution. We also note that even with $b_{0,\max} = 5 \times 10^{16}$ G, the electromagnetic energy (of order $10^{49}$ erg) is much smaller than the internal energy and gravitational potential energy (of order $10^{53}$ erg) of the neutron star. We do not consider the effect of the neutrino viscosity to the MRI supposing that the magnetic-field strength could be enhanced to be $\gtrsim 10^{14}$ G due to the rapid winding in the main region of the accretion disk (see Sec. III B) even if the early growth of the MRI is suppressed [58, 57].

We perform 7 simulations changing the black-hole mass, value of $b_{0,\max}$, and grid resolution. The parameters and quantities for the 7 models employed in this study are summarized in Table I. Numerical simulations with the low-resolution setting are always performed for the duration of $\geq 1$ s. In particular for $Q = 4$ models, the low-resolution simulations are performed for $\gtrsim 2$ s. On the other hand, the high-resolution simulations are performed only for $\lesssim 1$ s because such simulations require an extremely high computational cost. However, as we show below, the results for the low-resolution runs are quantitatively similar to those for the corresponding high-resolution runs, and hence, we consider that a fair convergence is achieved even with the low-resolution runs. The computational time with the low-resolution setting for 2 s is about 1400 hours using 64 nodes of our Sakura cluster in which 1 node has 2 Intel Xeon Gold 6248 CPUs (1 node has 40 cores).

### III. RESULTS

#### A. Overview of the evolution

First, we summarize the entire merger process found in a seconds-long simulation presenting the result for model Q4B5L for which the system was evolved up to $\sim 2.1$ s. Figure 1 displays the snapshot for the rest-mass density, absolute value of the magnetic-field strength, electron fraction $Y_e$, and temperature $T$, respectively, on the $x$-$z$ plane. The magnetic-field strength is defined by $b = (b_0 b^\parallel)^{1/2}$ where $b^\parallel$ is the magnetic field in the frame comoving with fluid and the temperature is shown by multiplying the Boltzmann’s constant $k$ and in units of MeV.

In the present choice of the dimensionless spin parameter for the black hole and the fairly large radius of the neutron star, the neutron star is tidally disrupted by the black hole before the binary reaches the innermost stable circular orbit both for $Q = 4$ and 6. During the tidal disruption process, the neutron-star matter located in the black-hole side falls into the black hole. Specifically, $\sim 80\%$ of the neutron-star matter falls into the black hole in a short timescale of a few ms. On the other hand, the neutron-star matter located distant from the black hole forms a one-armed spiral structure. Due to the subsequent angular-momentum transport inside the spiral arm and the dynamical evolution of the black-hole spacetime resulting from the matter infall into it, a part of the matter in the outer part of the spiral arm gains specific energy and angular momentum. The matter which gains
TABLE I. Key parameters and quantities for the initial conditions together with the parameters of grid setup for our numerical simulations. $M_{BH,0}$: initial black-hole mass, $b_{0,\text{max}}$: initial maximum magnetic-field strength, $\Omega_0$: initial orbital angular velocity, $M_{ADM,0}$: initial ADM mass, $\Delta x_{\text{max}}$: the grid spacing for the finest refinement level, $L_1$: the location of the outer boundaries along each axis, and the values of $N$ and $t_{\text{max}}$. For all the models, the neutron-star mass is $1.35M_\odot$ and the initial dimensionless black-hole spin is 0.75. Note that $M_{ADM,0}$ is by $\sim 1\%$ smaller than $m_0 = (6.75$ and $9.45M_\odot$ for $Q = 4$ and 6) because of the presence of the gravitational binding energy.

| model | $M_{BH,0} [M_\odot]$ | $b_{0,\text{max}}$ [G] | $\Omega_0$ | $M_{ADM,0} [M_\odot]$ | $\Delta x_{\text{max}}$ [m] | $L_1$ [km] | $N$ | $t_{\text{max}}$ |
|-------|----------------------|-----------------------|-----------|----------------------|-----------------------|-----------|-----|----------------|
| Q4B5H| 5.400                | $5 \times 10^{16}$    | 0.056     | 6.679                | 270                   | $1.62 \times 10^4$ | 234 | 9             |
| Q4B5L| 5.400                | $5 \times 10^{16}$    | 0.056     | 6.679                | 400                   | $1.74 \times 10^4$ | 170 | 9             |
| Q4B3L| 5.400                | $3 \times 10^{16}$    | 0.056     | 6.679                | 400                   | $1.74 \times 10^4$ | 170 | 9             |
| Q6B5H| 8.100                | $5 \times 10^{16}$    | 0.064     | 9.368                | 270                   | $3.90 \times 10^4$ | 282 | 10            |
| Q6B5L| 8.100                | $5 \times 10^{16}$    | 0.064     | 9.368                | 400                   | $3.97 \times 10^4$ | 194 | 10            |
| Q6B3H| 8.100                | $3 \times 10^{16}$    | 0.064     | 9.368                | 270                   | $3.90 \times 10^4$ | 282 | 10            |
| Q6B3L| 8.100                | $3 \times 10^{16}$    | 0.064     | 9.368                | 400                   | $3.97 \times 10^4$ | 194 | 10            |

TABLE II. The mass $M_{BH}$ and the dimensionless spin parameter $\chi_{BH}$ of the remnant black hole evaluated at $t = 100$ ms together with the gravitational-wave and neutrino energy emitted before $t = 100$ ms, $E_{GW}$ and $E_\nu$, and the rest mass of the matter located outside the black hole at $t = 100$ ms, $M_{BH,0}$. All the quantities related to the mass or energy are described in units of $M_\odot$.

| model | $M_{BH}$ | $\chi_{BH}$ | $E_{GW}$ | $E_\nu$ | $M_{BH,0} [M_\odot]$ |
|-------|----------|-------------|----------|---------|----------------------|
| Q4B5H | 6.466    | 0.856       | 0.069    | 0.008   | 0.129                |
| Q4B5L | 6.400    | 0.838       | 0.066    | 0.008   | 0.135                |
| Q4B3L | 6.396    | 0.838       | 0.066    | 0.008   | 0.138                |
| Q6B5H | 9.145    | 0.837       | 0.117    | 0.007   | 0.097                |
| Q6B5L | 9.138    | 0.832       | 0.112    | 0.007   | 0.104                |
| Q6B3H | 9.145    | 0.838       | 0.117    | 0.007   | 0.097                |
| Q6B3L | 9.136    | 0.833       | 0.112    | 0.007   | 0.106                |

sufficient specific energy eventually becomes dynamical ejecta, while the other part in the spiral arm which is bound to the remnant black hole forms an accretion disk. The timescale of this stage is $\lesssim 10$ ms (see the first row of Fig. 1 for the resulting state). All these processes have been studied by a number of previous numerical-relativity work and our present result on the tidal disruption and disk formation processes is essentially the same as the previous findings.

The mass, $M_{BH}$, and the dimensionless spin parameter, $\chi_{BH}$, of the remnant black holes evaluated at $t = 100$ ms are summarized in Table I. Irrespective of the runs, the black-hole mass and dimensionless spin are increased by $\approx 1.05M_\odot$ and $\sim 0.1$, respectively, due to the matter infall. The black-hole mass is by $\sim 0.3M_\odot$ smaller than the initial Arnowitt-Deser-Misner (ADM) mass. The reason for this is that a part of the neutron-star matter forms an accretion disk and ejecta, and in addition, gravitational waves and neutrinos carry away the energy (see Tables I and II) in the inspiral and early merger stages.

We also list the total gravitational-wave and neutrino energy emitted before $t = 100$ ms, $E_{GW}$ and $E_\nu$, and the rest mass of the matter located outside the apparent horizon at $t = 100$ ms, $M_{BH,0}$. In Table I. By comparing $M_{BH}$ and $M_{BH,0} - E_{GW} - E_\nu - M_{BH,0} - 1$, we can assess how good (or bad) the energy conservation is satisfied in our simulation. It is found that for $Q = 4$, the energy conservation is satisfied with about 0.1% and 1.1% error for high- and low-resolution runs of $Q = 4$ model, and with $\leq 0.1\%$ and about 0.1% error for high- and low-resolution runs of $Q = 6$ model, respectively. The reason that the accuracy depends strongly on the grid resolution for $Q = 4$ (i.e., for the smaller black-hole mass) is that the accuracy for resolving the black hole depends strongly on it. This is found by taking a look at the value of the black-hole mass for $Q = 4$: For the low-resolution runs, the black-hole mass is underestimated. However, the error of $\lesssim 1\%$ at $t = 100$ ms is still in an acceptable level, indicating the reliability of the numerical results.

After the spiral arm winds around the black hole, a compact accretion disk is formed. The orbital period at the innermost region of the accretion disk is 1–2 ms. During the tidal disruption process, the neutron-star matter which eventually forms an accretion disk experiences a strong differential rotation stage in the spiral arm, and then, a toroidal magnetic field is developed from the initially poloidal magnetic field by winding. After the formation of the accretion disk, the winding continues to enhance the toroidal magnetic-field strength, in particular in the innermost region of the accretion disk. After the sufficient amplification of the magnetic-field strength, an outward expansion of the matter is driven toward the polar direction due to the enhanced magnetic pressure, and as a result, poloidal fields for which the strength is comparable to that of the toroidal fields are also generated. With these strong magnetic fields, the wavelength for the fastest growing mode of the MRI becomes $\sim 10$ km and can be numerically resolved. Then, a turbulent state associated with the MRI is developed, and eventually, an MRI dynamo is activated in the accretion disk.

This can be also observed from a spacetime diagram of the toroidal-field strength. In Fig. 2 we plot the average value of the toroidal field as a function of time and polar angle $\theta = \tan^{-1}(\sqrt{x^2 + y^2/z})$ for models Q4B5L and...
FIG. 1. The snapshot for the rest-mass density $\rho$ (g/cm$^3$), magnetic-field strength $b = \sqrt{b^2}$ (G), electron fraction $Y_e$, and temperature $T$ ($kT$ in units of MeV) on the $x$-$z$ plane with $[-2000 \text{ km} : 2000 \text{ km}]$ for both $x$ and $z$ for model Q4B5L. Note that the green region in $Y_e$ found in the left side at the first and second rows shows the dynamical ejecta and fall-back matter. See also an animation: https://www2.yukawa.kyoto-u.ac.jp/~kota.hayashi/Q4B5L-2000a.mp4

Q4B5H. Here, $x$, $y$, and $z$ are defined with respect to the black-hole center. The toroidal field is defined by $b_\phi = (xb_y - yb_x)/\sqrt{x^2 + y^2}$. The average is performed with respect to the azimuthal angle $\varphi = \tan^{-1}(y/x)$ at the selected radius of $r := \sqrt{x^2 + y^2 + z^2} \approx 50 \text{ km}$. From Fig. 2 we find the so-called butterfly structure irrespective of the grid resolution: The polarity of the toroidal magnetic field is reversed due to the turbulent
FIG. 2. The profile of the average toroidal magnetic field along the polar direction ($\theta$) at $r \approx 50$ km as a function of time for models Q4B5L (top panel) and Q4B5H (bottom panel).

motion in a periodic manner with the period of $\sim 20$ local orbital periods ($\approx 2.5$ ms). It is also found that strong magnetic-field regions move from the accretion disk to the polar region in the early stage, producing a global magnetic-field structure (see also the magnetic-field strength in the second row of Fig. 1).

During this turbulent stage, angular momentum is transported from the inner to the outer region of the accretion disk due to the effective viscosity induced by the turbulence. In addition to this effective viscous process, magnetohydrodynamics effects such as the magneto-centrifugal effect [89] which results from a global magnetic field play an important role for expelling the matter from the central region. Due to these effects, the matter near the innermost stable circular orbit loses its angular momentum and falls into the black hole, while the matter in the outer part of the disk receives angular momentum and expands gradually. As a result, the rest-mass density and the temperature in the disk decrease in the viscous timescale of order $100$ ms to $1$ s (see the third to fifth rows of Fig. 1).

In addition to the disk expansion toward the equatorial direction, the matter expands toward the direction perpendicular to the orbital plane (see the entire panels of Fig. 1). Our interpretation for this expansion is that the magnetic tower effect plays a role: During the evolution of the accretion disk, the toroidal magnetic-field strength is enhanced by the MRI and winding. As a result, the magnetic pressure is enhanced to be high enough for the accretion disk to expand toward the direction perpendicular to the orbital plane (and thus the disk becomes a torus), although the serious baryon contamination in the vicinity of the rotational axis is prevented by the centrifugal force on the matter. This effect produces a funnel structure around the rotational axis (see the second to fifth rows of Fig. 1).
Not only the magnetohydrodynamics effect but also the neutrino cooling plays an important role for the evolution of the accretion disk. In the early stage of the accretion disk, the maximum density is $\gtrsim 10^{12}$ g/cm$^3$ and the maximum temperature is several MeV. In addition to the high density and high temperature, the disk is massive with the mass $\gtrsim 0.1 M_\odot$ in the early stage. In such a stage, neutrino luminosity becomes higher than $10^{53}$ erg/s which is comparable to or higher than the viscous heating rate for a compact disk with a high viscous parameter $[61]$. During the stage that the neutrino luminosity is as high as the viscous heating rate, the matter in the accretion disk is not affected significantly by the viscous heating effect, although the accretion disk gradually expands due to the viscous/magnetohydrodynamics angular-momentum transport and magnetic pressure resulting from the enhanced magnetic-field strength. However, with the expansion, the density and temperature of the accretion disk decrease, and consequently, the neutrino luminosity sharply decreases because the neutrino emissivity is approximately proportional to $T^6$ $[90]$. As the neutrino luminosity drops below the viscous heating rate, neutrinos cannot efficiently carry away the thermal energy from the accretion disk and the thermal energy generated by the viscous effect influences the evolution of the accretion disk. Specifically, convective motion of the matter at the innermost region of the disk, in which the viscous heating efficiency is highest, is excited and blobs of the matter viscously heated in the vicinity of the black hole are moved toward the outer region of the disk $[1]$. As a result, the matter in the outer part of the disk obtains the thermal energy and the heated matter eventually becomes unbound from the system to be the post-merger ejecta (cf. the second and third rows of Fig. $[1]$). This mechanism is the same as that found in our viscous hydrodynamics simulations $[61]$. This post-merger mass ejection continues from $0.2$–$0.3$ s to $\sim 1$ s after the merger (i.e., after the formation of the accretion disk). We note that in addition to this viscous-heating effect, purely magnetohydrodynamical effects such as magnetic-centrifugal effect $[39]$ could also play a role for the mass ejection.

In parallel with the accretion-disk evolution, a magnetosphere is developed in the low-density region near the rotational axis (see Fig. $[1]$). For the merger of black hole-neutron star binaries that experience tidal disruption, such a low-density region is naturally developed because the matter is primarily ejected toward the equatorial direction. During the magnetohydrodynamics evolution of the accretion disk, a mass outflow toward the direction perpendicular to the equatorial plane is driven by the activity of the accretion disk. However, the density in the vicinity of the rotation axis is still preserved to be low because of the presence of the centrifugal force on the injected matter. Thus the accretion of the matter into the black hole proceeds primarily from the disk in the equatorial direction. In ideal magnetohydrodynamics, the accretion of the matter accompanies the infall of the magnetic flux into the black hole. Although the magnetic field comoving with the infalling matter falls together into the black hole, the magnetic-field line located outside the black hole can expand toward the outer direction in particular along the rotational axis which has low matter density and low gas pressure (see Sec. $[III C]$).

Such magnetic fields eventually develop a magnetosphere for which the magnetic-field lines are nearly aligned with the rotational axis (except for the vicinity of the black hole $[1]$. The magnetic pressure in such a region is lower than the gas pressure of the surrounding thick torus which is formed after the activity of the accretion disk is enhanced (see the second to fifth rows of Fig. $[1]$). In other word, the size of the magnetosphere is determined by the structure of the thick torus.

The magnetic-field lines penetrate the black hole spinning rapidly with the dimensionless spin $\gtrsim 0.8$, and thus, they are subject to the Blandford-Znajek mechanism $[92]$ by which the rotational kinetic energy of the black hole is converted to the outgoing Poynting flux. In the presence of the matter for which the rest-mass energy density is comparable to or larger than the electromagnetic energy density, the Poynting flux cannot propagate away efficiently. However, the density decreases with time because the matter in the vicinity of the black hole falls into the black hole and a part of the matter is expelled by the magnetic pressure. Hence, eventually, electromagnetic waves generated by the Blandford-Znajek effect can propagate away (cf. the second to fifth rows of Fig. $[1]$). If an efficient conversion of the electromagnetic energy to the kinetic energy of the matter occurs during the subsequent propagation, a gamma-ray burst jet may be launched. Since the magnetic field has a collimated structure, the electromagnetic emission is also collimated. This collimated emission continues as far as the gas pressure by the thick and dense torus confines the magnetosphere (see Sec. $[III C]$).

We note that the evolution processes described above are qualitatively universal irrespective of the black-hole mass, initial magnetic-field strength, and grid resolution. In the following subsections, we describe the quantitative details about the accretion disk evolution, mass ejection, and generation of strong Poynting flux in the magnetosphere.

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1. See the following animation for the entropy per baryon (s/k) and for the convective activity:

   https://www2.yukawa.kyoto-u.ac.jp/~kota.hayashi/

   Q4B5L-2000a.mp4

2. Although we find it in our present simulation, it is not conclusive whether an aligned magnetic field with constant polarity is always formed or not: see, e.g., Refs. $[35]$ $[69]$ $[81]$ for related work.
B. The evolution of the accretion disk and post-merger mass ejection

In this subsection, we present the quantitative details on the evolution of the accretion disk and on the mass ejection. Figure 5 shows the rest mass of the matter located outside the apparent horizon \( M_{> \text{AH}} \) (dashed curves) and the accretion disk mass \( M_{\text{disk}} \) (solid curves) as functions of time. Figure 6 shows the rest mass of the unbound matter (ejecta) \( M_{\text{eje}} \) as a function of time. These quantities are defined by

\[
M_{> \text{AH}} := \int_{r>r_{\text{AH}}} \rho u^t \, d^3x + M_{\text{esc}},
\]

\[
M_{\text{eje}} := \int_{-h u_t > h_{\text{min}}, r>r_{\text{AH}}} \rho u^t \, d^3x + M_{\text{esc}},
\]

\[
M_{\text{disk}} := M_{> \text{AH}} - M_{\text{eje}},
\]

where \( \rho u_t := \rho \sqrt{-g} u^t \) with \( g \) the determinant of the spacetime metric, \( g_{\mu \nu} \), \( u^t \) the time component of the four velocity \( u^\mu \), and \( r_{\text{AH}} \) denotes the coordinate radius of the apparent horizon with respect to the black-hole puncture. \( M_{\text{esc}} \) denotes the rest mass escaping from the computational domain, which is calculated from

\[
M_{\text{esc}} := \int \rho \sqrt{-g} u^t \, dS, \quad \text{if } t \leq 20 \text{ ms},
\]

\[
M_{\text{esc}} := \int M_{\text{esc}} \, dt, \quad \text{if } t > 20 \text{ ms}. \tag{8}
\]

The surface integral is performed near the outer boundaries of the computational domain.

The ejecta component is identified by considering the Bernoulli criterion; i.e., we regard the matter located outside the apparent horizon that satisfies \( h u_t < h_{\text{min}} \) as the unbound component. Here, \( u_t (<0) \) is the lower time component of the four velocity \( u^\mu \), and \( h_{\text{min}} \) is the minimum specific enthalpy for a given electron fraction \( Y_e \) and it is obtained from the tabulated EOS employed. The value of \( M_{> \text{AH}} \) for \( t \lesssim 20 \text{ ms} \) is in approximate agreement with that in our previous paper [11] in which magnetohydrodynamics and resulting viscous effects were absent. In the present simulation, by contrast to the one in Ref. [11], for \( t > 20 \text{ ms}, M_{> \text{AH}} \) continuously decreases due to the matter accretion into the black hole induced by the angular-momentum transport resulting from the magnetohydrodynamics effects as already mentioned in Sec. [11, A]. We note that the curves of \( M_{> \text{AH}} \) depend only weakly on the initial magnetic-field strength and grid resolution.

The value of \( M_{\text{eje}} \) steeply increases at two characteristic moments. The first increase is found right after the tidal disruption, and the steep increase continues only for a few ms, comparable to the dynamical timescale of the system. Thus, this mass ejection component is the dynamical ejecta. The rest mass for this component is \( \approx 0.05 M_\odot \) and \( \approx 0.04 M_\odot \) for models with \( Q = 4 \) and 6, respectively. The result for \( Q = 4 \) is in good agreement with our previous result [11]. After the steep increase, the value of \( M_{\text{eje}} \) remains approximately constant for the next few hundreds ms, reflecting that an efficient mass ejection activity is quiescent during this time. In this quiescent stage, however, the accretion disk is actively evolved due to the MRI and associated turbulent motion, and the density and temperature of the disk decrease (see, e.g., Fig. 5 for the rest-mass density) due to the expansion of the disk resulting from the angular-momentum transport process and enhanced magnetic pressure. As a result of the decrease in temperature, the neutrino luminosity eventually drops below the viscous heating rate (cf. Fig. 6), and then, the post-merger mass ejection driven by the viscous heating sets in. (Here, viscous heating implies the shock heating associated with the MRI turbulence.) Thus, the second steep increase of \( M_{\text{eje}} \) that starts at \( t \sim 300–500 \text{ ms} \) is triggered by the quick damping of the neutrino luminosity (see Fig. 6). We emphasize here that even in the presence of pure magnetohydrodynamics process (not viscous process resulting from the MRI turbulence), the post-merger mass ejection appreciably occurs only after these onset time, and since the post-merger mass ejection continues for several hundreds ms, simulations with the duration shorter than \( 500 \text{ ms} \) cannot clarify this ejection process.

The rest mass of the post-merger ejecta is \( \approx 0.035 M_\odot \) and \( \approx 0.020 M_\odot \) for models with \( Q = 4 \) and 6, respectively, and these values are about 10% of the disk mass at its formation (at \( t \sim 10 \text{ ms} \)). For both \( Q = 4 \) and 6, the dynamical ejecta is the primary component of the ejecta in the present setting, and this tendency is stronger for the larger mass ratio, as discussed, e.g., in Refs. [9, 32]. The onset time of \( t \sim 300–500 \text{ ms} \) for the post-merger mass ejection depends on the initial magnetic-field strength and grid resolution by 100–200 ms. Our interpretation for this difference is that the magnetohydrodynamics turbulence is a stochastic process, and hence, the angular-momentum transport process can depend on the difference in the initial-field strength and grid resolution. However, the total ejecta mass and the properties of the post-merger ejecta do not depend strongly on them (see below on the electron fraction and velocity of the ejecta). Figures 5 and 6 display the time evolution of the maximum rest-mass density \( \rho_{\text{max}} \) and the total neutrino luminosity \( L_\nu \), respectively. For generating Fig. 6, we define the merger time \( t_{\text{merger}} \) as the time at which the rest-mass density reaches its local minimum value for the first time; i.e., \( t \approx 10 \) and 13 ms for \( Q = 4 \) and 6, respectively. These figures indeed show that the density and neutrino luminosity steeply decrease at \( t \approx 300–500 \text{ ms} \). This simultaneous decrease clearly elucidates that the evolution of the accretion disk and the timing of the post-merger mass ejection are controlled by the neutrino cooling. We also note that after the onset of the post-merger mass ejection, the accretion rate of the matter into the black hole also decreases steeply with time: see the left panel of Fig. 7.

One interesting point is that the curve of \( L_\nu \) well re-
FIG. 3. The time evolution of the rest mass of the matter located outside the apparent horizon (dashed curves) and the accretion-disk mass (solid curves) for all the runs with $Q = 4$ (left panel) and $Q = 6$ (right panel).

FIG. 4. The time evolution of the rest mass of the unbound matter for all the runs with $Q = 4$ (left panel) and $Q = 6$ (right panel).

Reflects the evolution of the accretion disk. From $t - t_{\text{merger}} \approx 1 \text{ ms}$ to $\sim 20 \text{ ms}$, $L_\nu$ increases by orders of magnitude both for $Q = 4$ and 6. This reflects the temperature increase during the formation of the accretion disk (e.g., due to the compressional heating and shock heating) and the subsequent enhancement of the turbulent state in the accretion disk due to the MRI (see, e.g., Fig. 8 which shows the increases of the electromagnetic energy in this stage). Subsequently, $L_\nu$ monotonically decreases for $t - t_{\text{merger}} \gtrsim 20 \text{ ms}$, because in this stage, the accretion disk expands due to the angular-momentum transport process and enhanced magnetic pressure, and the density and temperature decrease gradually. However, the thermal energy generated by the viscous heating due to MRI turbulence is consumed primarily by neutrino cooling prior to the onset of the post-merger mass ejection. Hence, the expansion of the accretion disk does not rapidly proceed, and thus, the mass ejection due to the thermally generated energy is suppressed. It is found that $L_\nu$ decreases approximately as $t^{-1.6}$ in this stage, and the decrease is fairly mild. However, after $L_\nu$ decreases below $\approx 10^{51.5} \text{ erg/s}$ as a result of the disk expansion and resulting decrease of the temperature, the neutrino emission rate becomes smaller than the thermal energy generation rate due to the MRI turbulence (viscous heating). Then, the turbulent heating is used for the outward expansion of the disk efficiently, in particular through the convective motion from the inner to outer region (see footnote 1), and the post-merger mass ejection is driven. (We note that the critical neutrino luminosity, which is $\sim 10^{51.5} \text{ erg/s}$ in the present case, should depend on the disk mass because the luminosity should be ap-
proximately proportional to it.) Subsequently, the neutrino luminosity exponentially drops at $t \approx 300$–500 ms irrespective of the binary mass ratio and the initial choice of the magnetic-field strength. Specifically, this post-merger mass ejection sets in when the temperature for most of the disk matter decreases below $\sim 3$ MeV (see the top panel of Fig. 10 for a mass distribution with respect to the temperature as a function of time). This critical temperature at the onset of the post-merger mass ejection is quantitatively the same as that found in general relativistic neutrino-radiation viscous hydrodynamics simulations of black hole-torus systems [61, 62]. However, the time at the onset of the post-merger mass ejection is earlier than that in the viscous hydrodynamics result for the similar black-hole mass cases [62]. As indicated in Refs. [53, 59, 66], the inherent magnetohydrodynamics effects such as magento-centrifugal effect [89] are likely to accelerate the mass ejection from the disk. The neutrino luminosity of $\approx 10^{51.5}$ erg/s at the onset of the post-merger mass ejection which we find in this paper is indeed similar to that found in our recent magnetohydrodynamics study [66].

Figure 7 plots the mass accretion rate onto the black hole calculated by $-dM_{\text{AH}}/dt$ and a neutrino emission efficiency defined by $L_\nu/(-dM_{\text{AH}}/dt)$. After the early matter infall associated with the onset of the merger, the mass accretion rate has a peak at $t - t_{\text{merger}} \sim 10$ ms. This is due to the fact that the magnetic-field strength is amplified in the accretion disk and the mass accretion rate is enhanced (cf. Fig. 8). After the peak, the mass accretion
The time evolution of the accretion rate calculated from \( -dM_{AH}/dt \) (left panel), and neutrino emission efficiency \( L_\nu/(-dM_{AH}/dt) \) (right panel) for all the runs with \( Q = 4 \).

The rate decreases monotonically with time approximately as \( \propto t^{-2} \) for \( t - t_{\text{merger}} \lesssim 50 \text{ ms} \) and as \( \propto t^{-1} \) in the subsequent stage before the onset of the post-merger mass ejection. After the onset of the post-merger mass ejection, the mass accretion rate drops steeply. Broadly speaking, the curve of the neutrino emission efficiency reflects that of \( L_\nu \). However, the peak comes at \( t - t_{\text{merger}} \sim 40-50 \text{ ms} \), which is slightly later than the peak time of the neutrino luminosity and mass accretion rate. The reason for this is that \( L_\nu \propto t^{-1.6} \) while \( -dM_{AH}/dt \propto t^{-2} \) for \( t - t_{\text{merger}} \lesssim 50 \text{ ms} \) and subsequently \( -dM_{AH}/dt \propto t^{-1} \), and thus, the peak is shifted at \( t - t_{\text{merger}} \sim 50 \text{ ms} \). The maximum neutrino emission efficiency is \( \sim 8-10\% \). Keeping the difference in the disk mass in mind, this value agrees broadly with those found in our viscous hydrodynamics simulations for similar black-hole mass (\( M_{BH} = 6M_\odot \)) and dimensionless spin (\( \chi = 0.8 \)) [62].

Figures 8 and 9 show the time evolution of the electromagnetic energy, \( E_B \), and the ratio of the electromagnetic energy to the internal energy, \( E_{\text{int}} \), respectively. Here, \( E_B \) and \( E_{\text{int}} \) are defined, respectively, by

\[
E_B := \frac{1}{8\pi} \int_{r>r_{AH}} u^\mu \sqrt{-g} b_\mu b^\mu d^3x, \tag{9}
\]

\[
E_{\text{int}} := \int_{r>r_{AH}} \rho_* \varepsilon d^3x, \tag{10}
\]

and \( \varepsilon \) denotes the specific internal energy. Here we note that the energy-momentum tensor in the ideal magnetohydrodynamics is written as

\[
T_{\mu\nu} = \rho u_\mu u_\nu + P g_{\mu\nu} + \frac{1}{4\pi} \left( b^\alpha b_\alpha u_\mu u_\nu + \frac{1}{2} b^\alpha b_\alpha g_{\mu\nu} - b_\mu b_\nu \right), \tag{11}
\]

and with \( h = c^2 + \varepsilon + P/\rho \), we have

\[
u^\mu \sqrt{-g} T_{\mu\nu} u^\nu u^\nu = \rho_* (c^2 + \varepsilon) + \frac{1}{8\pi} \nu^\mu \sqrt{-g} b^\mu b_\mu. \tag{12}
\]

Here we recover \( c \) to clarify the physical units. Thus, the choice of \( E_{\text{int}} \) and \( E_B \) stems from Eq. (12).

During the merger stage, the magnetic-field strength is amplified quickly in a short timescale of a few ms. This is initially induced by the magnetic winding associated with the differential rotation in the accretion disk. In the Keplerian disk with the presence of the poloidal magnetic field of the cylindrically radial component \( B^\phi \), the strength of the toroidal magnetic field \( B^T \) increases approximately linearly with time until a saturation as (e.g., Ref. [93])

\[
B^T \approx \frac{3}{2} B^\phi \Omega t, \tag{13}
\]

where \( \Omega \) denotes the local angular velocity. For a black hole with the dimensionless spin of 0.8, the angular velocity at the innermost stable circular orbit of the black hole is \( \Omega_{\text{ISCO}} \approx \Omega_{\text{ISCO}} \approx 5.43 \times 10^{14} \text{ G} \) at the formation of the accretion disk in the present simulations. This is the reason that the initial steep amplification to \( E_B > 10^{50} \text{ erg} \) is found in our present simulations. Because the winding timescale is quite short, the magnetic-field amplification by \( \sim 3 \) orders of magnitude in \( \lesssim 100 \text{ ms} \) is possible even in the absence of other instabilities such as MRI: Even for the initial value of \( B^\phi = 10^{12} \text{ G} \), the toroidal field can be amplified to \( \sim 10^{15} \text{ G} \) in \( \sim 100 \text{ ms} \). After the sufficient amplification of the toroidal magnetic field, an outward expansion of the accretion disk is driven toward the polar direction due to the enhanced magnetic pressure and a poloidal field with its strength comparable to that of the toroidal field.
FIG. 8. The time evolution of the electromagnetic energy evaluated for the outside of the apparent horizon for all the runs with $Q = 4$ (left panel) and $Q = 6$ (right panel).

FIG. 9. The time evolution of the ratio of the electromagnetic energy to the internal energy evaluated for the outside of the apparent horizon for all the runs with $Q = 4$ (left panel) and $Q = 6$ (right panel).

is also generated. We note that the Kelvin-Helmholtz instability that takes place during the winding of the spiral arm around the black hole and collision between different parts of the spiral arm may also contribute partly to the magnetic-field amplification.

After the initial amplification of the magnetic-field strength, the ratio of $E_B/E_{\text{int}}$ reaches $\sim 0.05-0.1$. Then, the magnetic-field growth is saturated. The electromagnetic energy at the saturation, $E_{B,\text{sat}}$, is smaller for the smaller value of the initial magnetic-field strength. However, the relative difference in the saturated electromagnetic energy between models with different initial magnetic-field strengths is not as large as that in the initial electromagnetic energy. Furthermore, the electromagnetic energy for $t \gtrsim 30$ ms depends only weakly on the initial condition (as well as on the grid resolution).

Thus, we infer that the amplification and saturation of the magnetic-field strength take place in a universal manner irrespective of the initial magnetic-field strength.

When reaching the saturation, the typical magnetic-field strength is $10^{15}$ G (cf. Fig. 2) and the maximum rest-mass density is $\sim 10^{11} - 10^{12}$ g/cm$^3$ in the innermost region. Thus the Alfvén velocity is $\approx b/\sqrt{4\pi \rho} \approx 9 \times 10^8$ cm/s $(b/10^{15}$ G)$/(\rho/10^{11}$ g cm$^{-3}$)$^{-1/2}$ and the wavelength of the fastest growing mode of the MRI is typically $\sim 10$ km [83]. As a result, the wavelength of this unstable mode is covered by tens of grid points in our setting, and hence, the effect of the MRI comes into play subsequently. With the evolution of the disk, the typical magnetic-field strength and rest-mass density decrease, but in the equipartition stage (see below), the
Alfvén velocity is always of order $\sqrt{E_B/E_{\text{int}}} (\sim 10\%)$ of the sound speed, which changes weakly with time. Thus, the wavelength of the fastest growing mode of the MRI is always covered by tens of grid points in the present setting. Indeed, our numerical analysis shows that the wavelength is covered by $\sim 10$ grid points for the region with $\rho = 10^{11}$ g/cm$^3$, and more (several tens of) grid points for lower density region.

After the MRI starts playing a role, a turbulent state is developed in the accretion disk and an effective viscosity is induced. We evaluate the following ratio of the anisotropic stress to the pressure

$$\alpha_{ij} := \left\langle \frac{1}{P} \rho \mathbf{u}_i \mathbf{u}_j - \frac{1}{4\pi} \mathbf{b}_i \mathbf{b}_j \right\rangle_{\text{ave}},$$

where $i \neq j$ $(i, j = x, y, z)$ and $\langle \cdots \rangle_{\text{ave}}$ denotes the spatial average for the region with $z \geq 0$ and $\rho \geq 10^7$ g/cm$^3$. $\mathbf{u}_i$ is defined by $\mathbf{u}_i = \langle \mathbf{u}_i \rangle_{t, \text{ave}}$, where $\langle \cdots \rangle_{t, \text{ave}}$ denotes the local time average of $\mathbf{u}_i$. The time average needs to be subtracted from $\mathbf{u}_i$ to eliminate the contribution of coherent motion (not random motion) for evaluating the anisotropic stress associated with the turbulent motion. We find that all the components of $\alpha_{ij}$ are $\approx 0.02$ at the onset of the post-merger mass ejection depending only weakly on the initial magnetic-field strength and grid resolution. The values of $\alpha_{ij}$ are comparable to the viscous alpha parameter often employed in the viscous hydrodynamics simulations (e.g., Refs. [61, 62]). In this stage, the ratio of $E_B/E_{\text{int}}$ is preserved to be of $O(10^{-3})$. As a result of the viscous angular-momentum transport, the matter in the inner region of the accretion disk falls into the black hole while the matter in the outer part expands outward. Because of the matter infall into the black hole, the rest mass of the accretion disk decreases (see Fig. [3]), and associated with the decrease in the rest mass, the electromagnetic energy decreases with time although the ratio of $E_Q/E_{\text{int}} = O(10^{-2})$ is preserved. Thus, for $t \geq 100$ ms, the accretion disk is in an equipartition state. It is interesting to point out that the electromagnetic energy decreases approximately in proportion to $t^{-1}$. All these features are found both for the models of $Q = 4$ and $Q = 6$ irrespective of the initial magnetic-field strength and grid resolution.

Now we turn our attention to the properties of the ejecta. The bottom panel of Fig. [10] displays the mass distribution of the remnant matter with respect to the electron fraction $Y_e$ for model Q4B5H. This shows that there are two characteristic peaks of $Y_e$ at the regions around 0.05 and of 0.25–0.35, respectively. The former peak is associated primarily with the dynamical ejecta and the latter is with the accretion disk for $t \lesssim 400$ ms and post-merger ejecta for $t \gtrsim 400$ ms. This figure clearly shows that the dynamical ejecta component with $Y_e = 0.03$–0.07 comes directly from the neutron star, because the values are unchanged from the beginning. That is, this dynamical ejecta component is not essentially affected by thermal and weak processes in the merger and post-merger stages.

By contrast, the electron fraction of the post-merger ejecta is found to be determined by the evolution process of the accretion disk, in which the typical electron fraction increases from $\sim 0.05$ to $\sim 0.25$ for $0 < t \lesssim 200$ ms. As already mentioned, in this stage, the accretion disk gradually expands due to the viscous angular-momentum transport and magnetic pressure by the amplified magnetic-field strength, and its rest-mass density and temperature monotonically decrease. In the disk with its optical depth to neutrinos $\gtrsim 1$, the electron fraction is determined predominantly by the reaction equilibrium between electron/positron capture reactions if the temperature is high enough (typically $kT \gtrsim 2$–$3$ MeV; see Refs. [62, 65]) for their timescale to be shorter than that of viscous evolution. Due to the disk expansion, the electron degeneracy becomes weak, and as a result, the electron fraction is shifted to higher values in the reaction equilibrium state. With the decrease of the temperature, the neutrino luminosity decreases approximately in proportion to $T^6$. As already mentioned, the post-merger mass ejection sets in when the neutrino luminosity drops below $\sim 10^{51.5}$ erg/s, which occurs for $t \gtrsim 300$ ms. The typical value of $Y_e$ for the post-merger ejecta is determined around this timing, resulting in $Y_e \approx 0.25 \pm 0.10$.

Figure [11] displays the rest-mass histogram as functions of the electron fraction and velocity for the ejecta component for the models for which the simulation duration is longer than 1 s. The mass histogram is derived for the ejecta component outgoing from the radius of $\approx 10^4$ km. As described in the previous paragraphs, there are two distinct $Y_e$ components for the ejecta, and this feature is clearly observed in Fig. [11]. The dynamical ejecta component always has $Y_e \approx 0.03$–0.07 irrespective of the black-hole mass. By contrast, the distribution of $Y_e$ for the post-merger ejecta component depends on the black-hole mass in the present results. Specifically, for larger black-hole mass, the value of $Y_e$ tends to be larger. As a result, the peak of $Y_e$ changes from $\sim 0.25$ for $Q = 4$ to $\sim 0.31$ for $Q = 6$. This is in agreement with our finding in viscous hydrodynamics studies [62], and the reason is as follows: In the condition that the disk mass has an approximately identical value, the density of the disk can be higher for the lower black-hole mass (the lower mass ratio, $Q$, in the present context), because the tidally disrupted matter can have a more compact orbit around the black hole due to the smaller radius of its innermost stable circular orbit. Associated with this effect, the temperature is enhanced due to the compression and stronger shock heating, resulting in the higher neutrino emissivity and reducing the entropy per baryon of the matter in the accretion disk (cf. Fig. [6]). With the lower entropy per baryon, the degree of the electron degeneracy becomes higher and the neutron-richness is enhanced. Therefore, for the lower black-hole mass, the electron fraction of the post-merger ejecta becomes slightly lower. Figure [11] shows that this effect is found irrespective of the initial-magnetic field strength and grid resolution (thus it is physical).
The right panel of Fig. 11 presents the rest-mass histogram as a function of the ejecta velocity. Again, there are two components. Here, the low-velocity component with \( v/c \lesssim 0.08 \) stems primarily from the post-merger ejecta, while the high-velocity component stems from the dynamical ejecta. We note that the velocity distribution for the dynamical ejecta is in good agreement with that in our previous study \[41\], and the typical velocity of the post-merger ejecta agrees approximately with that found in viscous hydrodynamics simulations (e.g., Refs. \[61\] \[62\]). As we reported in Ref. \[32\], the velocity of the dynamical ejecta is at highest \( \sim 0.4c \). This is in contrast to the case of binary neutron star mergers in which the maximum ejecta velocity can be \( \gtrsim 0.8c \) \[95\].

Our present results confirm that there are two distinct ejecta components, low-\( Y_e \) and high-velocity component, and relatively-high-\( Y_e \) and low-velocity component, as many previous numerical work have suggested. By our self-consistent simulations, the distinction of two components emerges clearly. The former (dynamical ejecta) is likely to synthesize heavy \( r \)-process elements, while the latter (post-merger ejecta) is likely to synthesize rela-
FIG. 11. Mass histogram as functions of the electron fraction (left panel) and the velocity (right panel) of ejecta for the models with the simulation duration longer than 1 s (models Q4B5H, Q4B5L, Q4B3L, Q6B5L, and Q6B3L).

respectively light $r$-process elements as well as heavy ones (e.g., Refs. 53 [96]). Then, the former component is likely to shine as a red kilonova while the latter one is likely to contribute to a blue-kilonova component [52]. However, the detailed light curve and spectrum are determined by a non-trivial radiation transfer effect [97]. It is also likely that the light curve depends on the mass ratio $Q$. Thus, a nucleosynthesis calculation and radiation transfer simulation are topics to be explored as follow-up work.

C. Magnetic field in the funnel region and the relation to short gamma-ray bursts

In addition to aforementioned ejected matter (dynamical and post-merger ejecta), we find a launch of an outflow of the matter and Poynting flux in the narrow funnel region established near the rotational axis of the black hole (see Fig. 12). In particular, the isotropic Poynting luminosity estimated for most of the runs is comparable to the typical luminosity of short-hard gamma-ray bursts [11, 12]. In this section, we discuss the quantitative details on this result.

Irrespective of the black-hole mass, initial magnetic-field strength, and grid resolution, tidal disruption of the neutron star takes place in our present setting and a magnetized accretion disk is formed around the central black hole. As already mentioned in the previous subsections, the magnetic-field strength is increased by the winding and MRI, and then, a turbulent state is established at $\sim 30$–40 ms after the tidal disruption. Subsequently, the accretion disk evolves primarily by the viscous effect stemming from the MRI turbulence. As already mentioned in the previous subsection, the magnetic-field strength is determined by an equipartition state, i.e., by the internal energy of the matter, which is typically $\rho c_s^2$ where $c_s$ is the sound speed of order $10^9$ cm/s in the dense region of the disk. Since $E_B/E_{\text{int}}$ is of $O(10^{-2})$, the magnetic-field strength can be approximated as $\sim 0.1 \sqrt{8\pi \rho c_s^2} \sim 5 \times 10^{14} (\rho/10^{12} \text{ g cm}^{-3})^{1/2} (c_s/10^9 \text{ cm s}^{-1}) G$ near the inner edge of the accretion disk. The order of this field strength is indeed found in the accretion disk (see, e.g.,

FIG. 12. Snapshots of the rest-mass density profile (blue and green contours) with the magnetic-field lines (pink curves), unbound matter (white color) and its velocity (green arrow) for model Q4B5L at $t = 300$ ms. Magnetic-field lines penetrating the black-hole horizon are displayed. See also the following link for the time evolution: https://www2.yukawa.kyoto-u.ac.jp/~kota.hayashi/Q4B5L-3D.mp4
By the viscous angular-momentum transport, the matter in the innermost part of the accretion disk falls continuously into the black hole, and in this infall, the magnetic fluxes also fall in. As a result, the poloidal magnetic-field lines for which the field strength is $\gtrsim 10^{14}$ G at the horizon penetrate the black hole. Here, the infall magnetic fluxes do not have aligned polarity because the accretion process is determined by the turbulence in the accretion disk, and hence, the magnetic-field strength on the horizon does not monotonically increase. On the other hand, the poloidal magnetic fields in the polar region are twisted by the black-hole spin, and hence, the field strength could be larger than that for the accretion disk in the presence of a rapidly spinning black hole. Due to the twisting associated with the black-hole spin, the poloidal magnetic field strength dominates over the poloidal one in the vicinity of the black hole (cf. Fig. 12).

However, such amplified magnetic fields do not immediately form a global magnetosphere. The reason for this is that at tidal disruption, a dense atmosphere ($\rho \sim 10^{7}$ g/cm$^{3}$) is formed in the polar region by the matter expelled by shocks generated during the wind- ing and shock heating in the spiral arm. The matter also comes from the accretion disk due to its turbulent activity. Although a part of the matter in the polar region near the black hole eventually falls into the black hole, a certain fraction of the matter has to be expelled by the magnetic force to form a low-density magnetosphere. For this, the toroidal magnetic field amplified by the twisting due to the black-hole spin plays an important role, because a tower-like outflow is driven from the neighbourhood of the black hole by this magnetic effect [34]. Hence, eventually, the matter energy density decreases below the magnetic energy density of $b^{2}/8\pi$ in the polar region of the black hole. This is satisfied for $\rho < b^{2}/8\pi c^{2} = 4.4 \times 10^{9}(b/10^{14} G)^{2}$ g/cm$^{3}$. Then, the magnetic pressure pushes the matter toward the outward direction along the rotation axis, establishing a low-density region near the rotational axis. During this process, the magnetic-field lines also expand outwardly, and a large-scale magnetosphere near the rotational axis is formed. In this region, the poloidal field is dominant (see Fig. 12). As a result, the rest-mass density decreases in the black-hole polar region, leading to the formation of the so-called funnel structure. At the funnel wall, the magnetic pressure is lower than the gas pressure of the surrounding thick torus and envelope, and hence, the magnetosphere is sustained by the surrounding matter.

Inside the funnel wall, the electromagnetic energy dominates over the rest-mass energy, and thus, an approximately force-free magnetosphere is formed. Here, the typical ratio of the electromagnetic energy density to the rest-mass energy density is 10–100. In such a region, the rotational kinetic energy of the black hole is extracted by the Blandford-Znajek mechanism [92] and transformed into the Poynting flux which propagates outward. Figure 13 shows the time evolution of $L_{iso}$: an isotropic Poynting luminosity, which we define using the Poynting luminosity for $\theta < 10^{\circ}$ and $r \approx 1500$ km as

$$L_{iso} := \frac{2}{1 - \cos(10^{\circ})} L_{\theta<10^{\circ},r\approx1500\ km},$$

where

$$L_{\theta<10^{\circ},r\approx1500\ km} := -\int_{\theta<10^{\circ},r\approx1500\ km} T_{t} r \sqrt{-g} ds,$$

We here choose a particular value ($10^{\circ}$) for the surface integral because the opening angle of the funnel region is initially as narrow as $\sim 10^{\circ}$ (see Figs. 14 and 15).

Figure 13 shows that the typical maximum value of $L_{iso}$ is of order $10^{50}$ erg/s and $L_{iso}$ varies with time irrespective of the black-hole mass and initial magnetic-field strength. This varying isotropic luminosity together with the opening angle of $\theta \sim 10^{\circ}$ (cf. Fig. 15) is in
a fair agreement with those for short-hard gamma-ray bursts [11, 12].

The stage with a high value of $L_{\text{iso}} \gtrsim 10^{50}$ erg/s continues broadly for 1 s. Subsequently, the isotropic luminosity starts decreasing. This is due to the fact that the opening angle of the funnel region increases and the magnetic-flux density is reduced. Remember that the funnel region is determined by the gas pressure of the thick torus at the funnel wall. In the long-term evolution of the accretion torus, the rest-mass density and associated gas pressure around the funnel wall decrease with time due to the post-merger mass ejection. On the other hand, the total magnetic flux penetrating the black hole does not significantly decrease in the ideal magneto-hydrodynamics, and thus, the decrease in the magnetic pressure is not as significant as the gas pressure at the funnel wall. As the rest-mass density decreases, thus, the magnetic pressure exceeds the gas pressure at the original position of the funnel wall, and as a result, the funnel wall expands gradually.

Figure 14 displays the snapshot of the toroidal magnetic field together with the poloidal magnetic-field lines on the $x$-$z$ plane at selected time slices. This indeed shows that the configuration of the magnetic-field lines changes from an aligned collimated one near the rotational axis to a more spread one for late time with $t \gtrsim 1$ s.

Since the collimation of the poloidal magnetic-field lines is loosened, the Poynting flux in the vicinity of the rotational axis also decreases gradually. Figure 15 shows that the opening angle of the strong Poynting-flux region increases from $\lesssim 10^\circ$ to $\sim 20^\circ$ and the intensity of the Poynting flux becomes weak with time. The reason that the peak of the Poynting flux is located near the funnel wall is that the magnetic-field lines near the funnel wall penetrate the equatorial regions of the spinning black hole, and hence, the Blandford-Znajek effect can be more efficient. If the Poynting flux indeed determines the luminosity of short-hard gamma-ray bursts, its brightness also should decrease for $t \gtrsim 1$ s. This mechanism could be interpreted as a reason that the timescales of short-hard gamma-ray bursts are less than 2 s with the typical timescale of $\sim 1$ s. Specifically, our numerical results propose that the timescale of $\sim 1$ s is determined by the evolution timescale of the accretion disk (torus), which is determined by the neutrino cooling and magneto-hydrodynamics turbulence (effectively viscous process) that control the post-merger mass ejection.

A word of the caution is appropriate here. First, the turbulence and dynamo activated by the MRI in the accretion disk are stochastic processes. This implies that the poloidal magnetic-field flux penetrating the black hole could not be precisely predicted. For example, by the accretion of the magnetic fields with a random polarity, the magnetic flux that penetrates the black hole may be smaller than that in the accretion disk. Hence, it is reasonable that the magnetic-field strength could not be always as strong as the one necessary for explaining typical short-hard gamma-ray bursts. Indeed, for model Q6B3H, the Poynting luminosity is by one order of magnitude lower than those for other models. In this case, the magnetic-field strength on the black-hole horizon is about 1/3 of those for other models. Therefore, broadly speaking, there are two possible cases: (1) A magnetosphere with strong poloidal magnetic fields is formed near the rotational axis of a spinning black hole. In this case, the maximum isotropic Poynting luminosity of $10^{50}$–$10^{51}$ erg/s consistent with typical short-hard gamma-ray bursts can be generated; (2) Due to the stochastic process of the MRI-induced turbulent motion, poloidal magnetic fluxes falling from the disk are not aligned well, and the poloidal magnetic field formed around the black hole is not strong enough to appre-

FIG. 14. The snapshot of the toroidal magnetic field (color profile) together with the poloidal magnetic-field lines (curves) on the $x$-$z$ plane at selected time slices for model Q4B5L. See also the following link for an animation: https://ww2.yukawa.kyoto-u.ac.jp/~kota.hayashi/Q4B5L-mf.mp4
Fig. 15. The angular distribution of the Poynting flux on a sphere of $r \approx 1500$ km for model Q4B5L at different time slices. The bright color displayed in the polar region stems from the Blandford-Znajek effect, while for other regions, the magnetic fields accompanying with the outflowing matter contribute mainly to the Poynting flux. The opening angle of the Poynting flux in the polar region is shown to increase with time. See the following link for an animation: https://www2.yukawa.kyoto-u.ac.jp/~kota.hayashi/Q4B5L-f3D.mp4

In our simulations, we find accretion disks which do not satisfy the condition for the magnetically-arrested disk [98]. We calculate the total magnetic flux on the upper semi-sphere of the horizon $\Phi_{BH}$ and calculate the time evolution of $\phi_{BH} := \Phi_{BH}/\sqrt{\dot{M}(GM_{BH}/c^2)c}$ where $\dot{M}$ denotes the rest-mass accretion rate onto the black-hole horizon calculated by $-dM_{AH}/dt$ (see the left panel of Fig. 7), and $c$ and $G$ are recovered to clarify the physical units. In our results, $\Phi_{BH} = (1-4) \times 10^{27}$ G cm$^2$, and the value of the dimensionless quantity, $\phi_{BH}$, increases with the decrease of $\dot{M}$ in time (see the left panel of Fig. 7). Specifically, irrespective of the initial magnetic-field strength and grid resolution, $\phi_{BH} \sim 1$ at $t = 100$ ms and $\sim 5$ at $t = 2$ s for $Q = 4$ and it is slightly smaller for the runs with $Q = 6$. Thus in our simulation time, $\phi_{BH}$ is much smaller than 50, which is proposed to be necessary to establish the magnetically-arrested disk [98]. In the early stage of its evolution, the accretion disk is the so-called neutrino-dominated accretion disk, for which the mass accretion rate is fairly large, the infall magnetic fluxes are determined by the equipartition condition in the disk, and thus, it seems to be difficult to form a disk which satisfies the condition for the magnetically-arrested disk. Our results are quantitatively similar to the model BT in Ref. [59], in which the authors considered the evolution of an accretion disk around a spinning black hole with the initial condition of a purely toroidal magnetic field. Our results together with the results in Ref. [59] suggest that in the absence of an extremely strong poloidal magnetic field on the disk from the beginning, the magnetically-arrested disk might not be formed as a remnant of neutron-star mergers in $t \sim 10$ s. We emphasize, however, that as we have described in this subsection, an intense Poynting flux can be generated even if the condition for the magnetically-arrested disk is not satisfied for the case that the rest-mass density along the rotational axis of the black hole becomes sufficiently low in a few hundreds ms after the onset of the merger.

Before closing this section, we note the following point: The present simulations are performed imposing the
equatorial-plane symmetry to save the computational costs. In this setting, asymmetric motion in the turbulent state of the accretion disk is neglected. To fully understand the effects of the turbulent motion in the disk and resulting formation of the magnetosphere, we needed to remove such an unphysical symmetry. To clarify the importance of the asymmetric motion and also to explore the case that the orbital angular momentum and black-hole spin are misaligned, we plan to perform a simulation with no plane symmetry in the next step.

IV. CONCLUSION

We have reported our new results of general-relativistic neutrino-radiation magnetohydrodynamics simulations for the black hole-neutron star merger. The mass of the black hole and neutron star are chosen to be realistic values ($M_{BH,0} = 5.4$ or $8.1 M_{\odot}$ and $M_{NS} = 1.35 M_{\odot}$), and we prepare a rapidly spinning black hole with the dimensionless spin of 0.75 to consider the case that the neutron star is tidally disrupted in a close orbit. The simulations were performed for $\sim 2$ s in the longest case to self-consistently explore the dynamical mass ejection, remnant disk evolution, post-merger mass ejection, and collimated Poynting flux generation near the rotational axis of the black hole which may be related to short-hard gamma-ray bursts.

We found that the matter with the mass of 0.04–0.05 $M_{\odot}$ is ejected dynamically right after tidal disruption of the neutron star in the timescale of $\lesssim 10$ ms as found in Ref. [11]. Then an accretion disk with the initial rest mass of 0.2–0.3$M_{\odot}$ is formed around the remnant black hole. In the accretion disk, the magnetohydrodynamics effects such as MRI and winding amplify the magnetic field within the timescale of order 10 ms, and the angular-momentum transport caused by the turbulent motion initially induces the mass accretion into the black hole and disk expansion. In the turbulent process, the thermal energy is generated and in the first $\sim 300–500$ ms, the thermal energy is dissipated by the neutrino emission.

However, with the expansion of the accretion disk due to the angular-momentum transport and magnetic pressure, the neutrino luminosity eventually drops below $\sim 10^{51.5}$ erg/s. Then, the neutrino cooling does not play a role for carrying away the thermal energy from the accretion disk, and the thermal energy generated by the turbulent (effectively viscous) process can be fully used for the mass ejection. Then, the post-merger mass ejection sets in. In the present study, the rest mass of the post-merger ejecta is $\sim 0.035 M_{\odot}$ and $\sim 0.020 M_{\odot}$ for the models with $Q = 4$ and 6, respectively. This post-merger mass ejection continues from $t \sim 0.3$ s to $\sim 1$ s.

Before the post-merger mass ejection sets in, a low rest-mass density funnel with aligned magnetic-field lines is formed near the rotational axis of the spinning black hole. This funnel region is magnetically dominant and is approximately in a force-free state. In this region, the Blandford-Znajek mechanism extracts the rotation kinetic energy of the rapidly spinning black hole, and a collimated Poynting flux is generated with the opening angle of $\sim 10^\circ$. The estimated maximum isotropic Poynting luminosity is $10^{50–51}$ erg/s. Together with the opening angle of the Poynting flux with $\sim 10^\circ$, these numbers are in a fair agreement with the typical short-hard gamma-ray bursts [11, 12]. The high Poynting luminosity stage continues for $\sim 1$ s and the luminosity subsequently decreases with time due to the expansion of the funnel wall and resulting decrease of the magnetic-flux density. The expansion of the funnel region is caused by the decrease of the rest-mass density and gas pressure around the funnel wall which takes place due to the post-merger mass ejection. As already mentioned, the post-merger mass ejection sets in after the neutrino luminosity drops and the duration of the post-merger mass ejection is determined by the viscous timescale of the accretion disk. Therefore our present results propose that the typical duration of the short-hard gamma-ray bursts is determined by the evolution timescale of the accretion disk. Specifically, the timescales of the neutrino cooling and viscous evolution in the accretion disk (torus) determine the duration of short-hard gamma-ray bursts.

As we have demonstrated in this paper, second-long simulations for neutron-star binaries are inevitable to self-consistently explore the entire merger and post-merger processes. This is the case not only for black hole-neutron star binaries but also for binary neutron stars. We need to focus on our effort along this line in the future. For the case that a black hole is formed soon after the merger, we expect that the evolution process is qualitatively the same as that found in this paper, although the quantitative properties of the post-merger ejecta such as the mass and the typical electron fraction are likely to depend sensitively on the mass of the remnant black hole and disk. For the case of binary neutron star mergers resulting in a massive neutron star, the post-merger evolution process can be influenced significantly by the presence of it. If strong global magnetic-field lines anchored by the massive neutron star are formed soon after the merger, the post-merger mass ejection is likely to be significantly influenced by the associated magnetohydrodynamics effects such as the magneto-centrifugal effect [49].

To explore this possibility, we need to consistently follow the evolution of the magnetic-field configuration from the merger throughout the post-merger stages. Long-term accurate magnetohydrodynamics simulations that can clarify the evolution of the magnetic-field structure is in particular desired in the future.

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