Macro- and micro-mechanics of granular soil in asymmetric cyclic loadings encountered by offshore wind turbine foundations

Liang Cui1, Subhamoy Bhattacharya1, George Nikitas1, Ankit Bhat2

Received: 1 February 2019 / Published online: 20 July 2019 © The Author(s) 2019

Abstract
Offshore wind turbine foundations are subject to $10^7$–$10^8$ cycles of loadings in their designed service life. Recent research shows that under cyclic loading, most soils change their properties. Discrete Element Modelling of cyclic simple shear tests was performed using PFC2D to analyse the micromechanics underlying the cyclic behaviours of soils. The DEM simulation were first compared with previous experimental results. Then asymmetric one-way and two-way cyclic loading pattern attained from real offshore wind farms were considered in the detailed parametric study. The simulation results show that the shear modulus increases rapidly in the initial loading cycles and then the rate of increase diminishes; the rate of increase depends on the strain amplitude, initial relative density and vertical stress. It shows that the change of soil behaviour is strongly related to the variation of coordination number, rotation of principal stress direction and evolution of degree of fabric anisotropy. Loading asymmetry only affects soil behaviours in the first few hundred of cycles. In the long term, the magnitude of $(\gamma_{\text{max}} - \gamma_{\text{min}})$ rather than loading asymmetry dominates the soil responses. Cyclic loading history may change the stress–strain behaviour of a soil to an extent dependent on its initial relative density.

Keywords Discrete element modelling · Cyclic loading · Soil stiffness · Micro-mechanism

Abbreviations

\begin{align*}
\alpha & \quad \text{Parameter defining the magnitude of fabric anisotropy} \\
\alpha_{\text{max}} & \quad \text{Fabric anisotropy at maximum shear strain} \\
\alpha_{\text{min}} & \quad \text{Fabric anisotropy at minimum shear strain} \\
d_{50} & \quad \text{Diameter at which 50% of the sample’s mass is comprised of particles with a diameter less than this value} \\
e & \quad \text{Void ratio} \\
G & \quad \text{Shear modulus} \\
M_{\text{max}} & \quad \text{Maximum moments in a load cycle} \\
M_{\text{min}} & \quad \text{Minimum moments in a load cycle and} \\
M_{\text{ult}} & \quad \text{Ultimate moment capacity} \\
N_c & \quad \text{Coordination number} \\
t & \quad \text{Deviator stress} \\
s' & \quad \text{Mean stress} \\
\gamma_{\text{max}} & \quad \text{Maximum shear strain (shear strain amplitude) of a cyclic simple shear test} \\
\gamma_{\text{min}} & \quad \text{Minimum shear strain in a cyclic simple shear test} \\
\zeta_c & \quad \text{Ratio of minimum moment to the maximum moment} \\
\eta_c & \quad \text{Parameter defined to quantify the degree of asymmetry of cyclic loading} \\
\theta_a & \quad \text{Direction of the principal fabric} \\
\sigma & \quad \text{Vertical stresses on the sample in a cyclic simple shear test} \\
\tau_{\text{max}} & \quad \text{Shear stress at maximum shear strain} \\
\tau_{\text{min}} & \quad \text{Shear stress at minimum shear strain}
\end{align*}

1 Introduction

1.1 Background and motivation

Offshore wind turbine foundations are subjected to a combination of cyclic and dynamic loading arising from wind, wave, 1P (rotor frequency) and 2P/3P (blade passing frequency) loads. Designing foundations for offshore wind turbines is challenging as: (1) these are dynamically sensitive structures in the sense that natural frequencies of these...
structures are very close to the forcing frequencies \([1]\); (2) cyclic loading can induce accumulated rotation of foundation but the tolerance for the total rotation at seabed is suggested as low as 0.5° in DNV \([2]\). The soil-foundation interactions under cyclic lateral loading have been investigated intensively by field tests \([3]\), scaled model tests \([4–10]\), FEM simulations \([11]\) and DEM simulations \([12, 13]\) with majority focused on mono-pile foundations as it is the main type of foundation for offshore wind turbines. Empirical relationships for the foundation tilt or stiffness were derived from the model tests but few attention was drawn on the soil disturbances due to the limitations of monitoring technique. With the aid of numerical modelling, stress and strain field within the soils could also be visualised in addition to the foundation responses. But due to the high computational costs, the number of loading cycles in the numerical simulations for the entire soil-pile system is usually limited.

The cyclic lateral load considered in the literature is mainly symmetric two-way loading or simply loading/unloading. Only a few considered the effects of asymmetric cyclic loadings, e.g. Zhu et al. \([7, 8, 14]\). Zhu et al. \([7]\) found that the accumulated rotation of suction caisson foundation increases with decreasing \(\zeta_c\) (the ratio of minimum moment to the maximum moment), i.e. two-way cyclic loading causes more accumulated rotations. It contrasts with the findings by Zhu et al. \([8]\), where one-way cyclic loading causes more accumulated rotations. It demonstrated that it is necessary to perform a systematic study on the influence of asymmetric cyclic loading on soil-structure interactions. On the other hand, Jalbi et al. \([15]\) reviewed the wind and wave loading data from 15 offshore wind farms and determined the maximum and minimum moment applied at the mudline of a wind turbine. It was found that \(\zeta_c\) lie in the range between −0.5 and 0.5 for these wind farms. This is a combined effect of wind load with high magnitude but low frequency and wave load with low magnitude but high frequency. With increasing water depth, the magnitude of wave load increases and may change the one-way cyclic loading caused by wind load into two-way loading. A schematic diagram illustrating the variations is given in Fig. 1a.

To attain detailed information of soil-structure interactions under various conditions, it is better to consider a small zone of soils adjacent to the structure and replicate it in an element test with similar stress conditions and stress paths. Intensive investigations have been conducted using laboratory element tests to examine the accumulated deformation \([16, 17]\) and variation of stiffness \([18, 19]\) of soils under cyclic loading in different load conditions. However, these experimental studies have no access to the micro-mechanism underlying the soil responses. Discrete element modelling of cyclic tests were also widely adopted to link the macro-scale soil responses and underlying micro-mechanism during cyclic loading including \([20–22]\). However, these studies were limited to symmetric two-way loadings, which are different from the real loading scenarios in offshore wind farms as found by Jalbi et al. \([15]\). This is a knowledge gap to fill in the current study.

### 1.2 Aim and scope of the paper

Majority of current offshore wind turbines are supported by monopile foundation, which is a large steel tube typically 30–40 m in length and 3–7 m in diameter. Unlike the slender piles for offshore structure, monopile tends to rotate rather than bend under lateral load or overturning moment. Therefore, the interactions between the monopile and the soil element in front of the monopile is analogic to a cyclic simple shear scenario, where the vertical stress remains almost constant, as shown in Fig. 1b. It is noted that the vertical stress applied on Block A may fluctuate slightly due to the compaction and rearrangement of soils above Block A, but this fluctuation is negligible comparing with the vertical stress levels considered in the current study. Therefore, cyclic simple shear tests were adopted to explore the soil responses under various cyclic loading patterns and its underlying micromechanism, in particular, to study the soil stiffness and deformation responses. The cyclic loading profiles considered are illustrated in Fig. 1c, which embrace the load scenarios summaries by Jalbi et al. \([15]\) as well as previous studies.

Experimental cyclic simple shear tests on typical silica sand (RedHill 110) have been conducted in previous studies \([23]\). DEM simulations were first performed using PFC2D in the current study and compared with the experimental results. The micromechanical parameters were then analysed to find the relationships between the micromechanical parameters and macroscopic responses with particular focus on the influence of one-way and two-way loading patterns. Finally, original samples and cyclically sheared samples are simply sheared till the critical state. Variations of soil stress–strain response and volumetric response as a consequence of cyclic loading history were analysed under the critical state framework.

### 2 Description of DEM simulation programme

In the experimental study performed by Nikitas et al. \([23]\), a cyclic simple shear apparatus was used for testing cylindrical soil samples with 50 mm in diameter and 20 mm in height as suggested in ASTM D6528 \([24]\). RedHill 110 Sand, a poorly graded fine grained silica sand with \(d_{50} = 0.18\) mm and particle size distribution (PSD) curve shown in Fig. 2, was tested as this soil has been used to carry out scaled model tests on different types of foundations \([25, 26]\). Strain
controlled drained cyclic simple shear tests with symmetric two-way loading on sand with various relative densities, vertical stresses and shear strain amplitudes were performed. In the current study, a commercial DEM code PFC2D (Itasca, 2008) was used to perform the presented simulations. The experimental cyclic simple shear test is a...
three-dimensional problem; however, the current study only models a thin slice of the sample in the middle. It is obvious that a two-dimensional simulation cannot accurately represent the three-dimensional granular soil. However, there is no intention in this paper to reproduce the physical test quantitatively, but analyse the similar underlying micro-mechanism because the major and minor principal stresses in a simple shear test lie in the loading plane considered in the 2D simulations.

The sample initially generated for testing is about 20 mm in height and 50 mm in width, similar to the sample dimensions in experiments [23]. It contains 8000 disks with size ranging from 0.1 mm to 0.3 mm and \(d_{50} = 0.18\) mm, matching the \(d_{50}\) value in experiments. The PSD curve is also given in Fig. 2. Note that the PSD range is narrower in the DEM than that in experiments due to the unrealistic computational time required for simulating samples with the same particle grading as in experiments. Parameters used in DEM simulations are listed in Table 1. Two sets of samples were generated with radius expansion approach followed by 1D-consolidation (laterally confined) with particle friction coefficient, \(\mu = 0\) and 1.0, to generate relative dense and loose samples, respectively. Particle friction coefficient was then changed to 0.5 and specimens were brought to equilibrium again with the new frictional coefficient. Final void ratios (\(e\)) of the relative dense and loose samples at two different vertical stresses (\(\sigma\)) are also listed in Table 1. Note that due to different boundary velocity in consolidation stage, the loose sample reached slightly lower \(e\) at 50 kPa than that at 100 kPa.

In the modelling of the cyclic simple shear test, a drained condition is maintained, i.e. the vertical normal stress is kept at a prescribed value by stress-controlled top and bottom walls (moving in or out to maintain the required stress level). The left and right side walls were rotated about their midpoints to realise the simple shear condition. The DEM simulation program of the cyclic simple shear tests is provided in Table 2. Symmetric two-way loading were planned for comparison with experimental tests [23] and other experimental tests and DEM simulations in literature. Various soil packing densities and vertical stresses (Series A), various strain magnitudes (Series B) were considered. In addition, the effect of asymmetry of cyclic loading (i.e. one-way or two way loading) were investigated. Similar to the parameter, \(\zeta_c\), used by Zhu et al. [7], in this paper, strain ratio, \(\eta_c = \gamma_{\min}/\gamma_{\max}\), was defined to quantify the degree of asymmetry of cyclic loading as strain-controlled cyclic tests were performed in the current study. Strain ratios, \(\eta_c\), between 0.5 and −1.0 were considered to embrace the load ratios encountered in real wind farms as summarised by Jalbi et al. [15] and previous work. For easy comparison, one series of simulations were planned with the same value of \(\gamma_{\max} - \gamma_{\min}\) but various \(\eta_c\) (Series C), and two other series were planned with the same \(\gamma_{\max}\) but various \(\eta_c\) (Series D and E).

Twelve measurement circles, as depicted in Fig. 3, were defined within the sample to measure the average stress, void ratio and coordination number. The results presented in the following sections are the average value from these twelve measurement circles.

### 3 DEM simulation results

#### 3.1 Macro-scale responses

The shear stress-shear strain curve forms hysteresis loops during cyclic loadings. Stress–strain relationships for the symmetric two-way loading (Series A, B, C) are similar. Thus only results from Series E were presented in Fig. 4. While \(\eta_c\) decreases from 0.5 to −1.0 (one-way loading to
Macro- and micro-mechanics of granular soil in asymmetric cyclic loadings encountered by…

...stress–strain relationships also show different evolution trends. With $\eta_c = 0.5$, shear strain only reverses half way, shear stress reduces to a positive value slightly above zero in the first cycle. With the progress of cyclic loading, shear stress at both $\gamma_{\text{max}}$ and $\gamma_{\text{min}}$ decreases steadily. As a consequence, the negative $\tau_{\text{min}}$ at $\gamma_{\text{min}}$ approaches the same magnitude of the positive $\tau_{\text{max}}$ at $\gamma_{\text{max}}$, even though both $\gamma_{\text{max}}$ and $\gamma_{\text{min}}$ are positive values. With decreasing $\eta_c$, the $\tau_{\text{min}}$ decreases more as $\gamma_{\text{min}}$ decreases. However, the trends of $\tau_{\text{max}}$ are quite different, even though $\gamma_{\text{max}}$ remains the same. When $\eta_c > 0$, $\tau_{\text{max}}$ decreases with cyclic loading; when $\eta_c = 0$, $\tau_{\text{max}}$ remains almost constant during cyclic loading; when $\eta_c < 0$, $\tau_{\text{max}}$ increases with cyclic loading. It demonstrates that the magnitude of $\gamma_{\text{min}}$ affected the stress response at $\gamma_{\text{max}}$. Following 1000 number of loading cycles, no matter the symmetry of loading cycles (one-way or two-way), shear stress oscillates two-way symmetrically, i.e. negative $\tau_{\text{min}}$ at $\gamma_{\text{min}}$ reaches the same magnitude as the positive $\tau_{\text{max}}$ at $\gamma_{\text{max}}$.

The shear modulus ($G$) of the sample can be calculated as

$$G = \frac{\tau_{\text{max}} - \tau_{\text{min}}}{\gamma_{\text{max}} - \gamma_{\text{min}}}$$

(1)

The variations of $G$ in all simulations under cyclic loading are illustrated in Fig. 5. The magnitudes of shear moduli in the DEM simulations (e.g. 5–6.5 MPa for $\sigma = 100$ kPa, dense sample, $\gamma = (-0.52\%, 0.52\%)$) are in the same range as the values from the experimental tests [e.g. 4–6 MPa for $\sigma = 100$ kPa, relative density = 50%, $\gamma = (-0.5\%, 0.5\%)$] in Nikitas et al. [23]. Referring to Fig. 5a, for both loose samples, there is a clear increase in $G$ under cyclic loading; while for both dense samples, $G$ decreases obviously, which was not observed in the experiments. Reason for this could due to the irregular shapes of particles, wide particle grading and possible particle abrasion or crushing in experiments, which could lead to continuously densification of samples. However, these phenomena could not be easily replicated in DEM
simulations. After 6000 cycles, $G$ of the loose samples and the dense samples at a same $\sigma$ approach a same constant. As shown in Fig. 5b, $G$ increases dramatically with reducing $\gamma_{\text{max}}$ as expected, and in all cases $G$ reduces slightly during cyclic loading. The results correlated quite well with the observations from scaled model tests with different types of offshore wind turbine foundations \cite{4-6,27} and the field measurements \cite{28}.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{stress_strain_curves}
\caption{Stress–strain relationships during cyclic loadings for simulation Series E}
\end{figure}
With the same magnitude of $(\gamma_{\text{max}} - \gamma_{\text{min}})$ in Series C, the two-way loading resulted in higher $G$ than the one-way loading in the first few hundred cycles (Fig. 5c). The reason is that the true strain level for the one-way loading is larger than those for the two-way loading (i.e. $1.04\% > 0.75\% > 0.52\%$), and as expected $G$ decreases with increasing strain level. However, following large number of loading cycles, soil losts memory of initial
strain levels and the key parameter dominating the long term stiffness is the magnitude of \((\gamma_{\text{max}} - \gamma_{\text{min}})\), which are the same for the three simulations, so are the final \(G\) values. Similar phenomena also observed in the DEM simulations of pile-soil interaction under cyclic loading by Cui and Bhattacharya [12]. The main reason for this may be that asymmetry only appears in the first cycle and the remaining cycles appear to be pseudo-symmetric about a non-zero mean shear strain, \((\gamma_{\text{max}} + \gamma_{\text{min}})/2\). The different soil responses caused by asymmetric loading in the first cycle are gradually eliminated by the pseudo-symmetric loading. Samples seem to reach a cyclically stable state with response center drifted to the non-zero mean shear strain and no obvious differences between samples can be observed.

With the decreasing values of \(\eta_c\) in Series D and E, \(G\) decreases obviously as the magnitude of \((\gamma_{\text{max}} - \gamma_{\text{min}})\) increases (Fig. 5d and e), which confirms the findings from Series C that the key parameter dominating the long term magnitude of stiffness is the magnitude of \((\gamma_{\text{max}} - \gamma_{\text{min}})\). It can also be observed that \(G\) decreases in dense samples and increases in loose samples in general. The exemptions are the dense samples with \(\eta > 0\), where the magnitude of \((\gamma_{\text{max}} - \gamma_{\text{min}})\) may be not large enough to produce the same effect.

The evolutions of void ratio, \(e\), of all simulations under cyclic loading are illustrated in Fig. 6. The increasing \(G\) of loose samples could be explained by the densifications of samples (reduction in \(e\)) as observed in Fig. 6a. The \(G\) values for the dense samples reduce obviously, but they only dilated slightly. There should be other causes for the remarkable decrease of \(G\), which will be investigated further in the latter part of this paper. Moreover, \(e\) of the two samples at \(\sigma = 50\) kPa coincide, which consists with the coincidence of their \(G\) values. However, for the two samples at \(\sigma = 100\) kPa, \(e\) of the loose sample is still higher than that of the dense sample, which is also consistent with the comparison of their \(G\) values. As shown in Fig. 6b, with higher \(\gamma_{\text{max}}\), dense sample dilates slightly more in the initial stage. However, for \(\gamma_{\text{max}} = 1.04\%\), sample dilates first and then contracts slightly. As seen from the monotonic simple shear tests in the latter section (Fig. 14), this is mainly because the specimen approaches failure from 2% of shear strain thus the sample is disturbed and re-arranged significantly during cyclic loadings. As observed from Series C in Fig. 6c, the three simulations with the same value of \((\gamma_{\text{max}} - \gamma_{\text{min}})\) but different values of \(\eta_c\) shows very subtle differences in void ratio. However, with increasing value of \((\gamma_{\text{max}} - \gamma_{\text{min}})\) in Series D/E (Fig. 6d, e), void ratio reduces/increases more obviously. This confirms again that the magnitude of \((\gamma_{\text{max}} - \gamma_{\text{min}})\) rather than \(\eta_c\) dominates the responses.

3.2 Micro-scale mechanism

The observed macro-scale stress and strain responses should be underlain by the micro-scale (particle-scale) mechanism. In the following section, micro-scale parameters, including the coordination number, contact force network, fabric anisotropy, principal stress rotation, etc., were examined in details to bridge the micro–macro gaps.

3.2.1 Coordination number (\(N_c\))

The coordination number (\(N_c\)) is the average number of contacts surrounding each particle. It has a strong relation with the stress level within the sample [29]. The evolutions of \(N_c\) under cyclic loading for the four samples under various test conditions are shown in Fig. 7. It is clearly shown in Fig. 7a that the initial low \(N_c\) corresponds to initial low shear stress (thus low \(G\) in Fig. 5a). The increase in \(G\) for the two loose samples is related to the increase in \(N_c\) and the decrease in \(G\) for the dense samples agrees with the reduction in \(N_c\). When values of \(G\) coincide, the coordination numbers also coincide. As observed in Fig. 7b, with higher \(\gamma_{\text{max}}\), \(N_c\) reduces more and quicker with loading cycles, matching the reduction of \(G\). As shown in Fig. 7c, with the same \((\gamma_{\text{max}} - \gamma_{\text{min}})\), the initial value of \(N_c\) was lowest with \(\eta_c = 0\) (one-way loading) due to higher \(\gamma_{\text{max}}\); however after 100 cycles, \(N_c\) decreases to similar value for all three \(\eta_c\) values, which agrees with the trend for the \(G\) in Fig. 5c. As seen from Fig. 7d, \(N_c\) does not change significantly for \(\eta_c > 0\) but decrease more significantly with decreasing \(\eta_c\) for \(\eta_c \leq 0\), which agrees with the observations of \(G\) in Fig. 5d and e in Fig. 6d. \(N_c\) for Series E all increases remarkably with cyclic loading but the differences between various \(\eta_c\) are insignificant.

In summary, considering all observations of \(G\), \(e\) and \(N_c\), we can see that lower \(e\) (denser packing) results in higher \(N_c\), which in turn leads to higher stress level, thus higher \(G\).

3.2.2 Contact force network

The evolution of the contact force network within the dense soil sample at \(\sigma = 100\) kPa is illustrated in Fig. 8. Before cycling, the contact force network illustrates an approximately isotropic and uniform distribution (Fig. 8a). Once cycled to the maximum strain, e.g. +0.52%, the stronger contact forces are aligned to the shorter diagonal direction and weaker contact forces can be observed at the other two diagonal corners (Fig. 8b). When the specimen is cycled to −0.52%, the strong contact force direction rotated to the other diagonal direction, and the locations of the weaker contact force network also shifts accordingly (Fig. 8c). To
statistically quantify the orientations of contact forces, the contact fabric is analysed Sect. 3.3.3; to statistically quantify both the magnitudes and orientations of the contact forces, the principal directions were examined in Sect. 3.3.4.

3.2.3 Fabric

The spatial distribution of the contact force directions can be quantified by fabric. There are many evidences of the impact
of fabric anisotropy on the characteristics of granular materials [30, 31]. Therefore, it is worth to analyse the evolution of soil fabric in the current cyclic loading conditions. Various definitions of fabric can be found in the literatures [32]. The one adopted in the current study is the Fourier approximation [33], which quantifies the distribution of contact direction per radian as:
where \( a \) is a parameter defining the magnitude of fabric anisotropy and \( \theta_a \) is the direction of the principal fabric. For an isotropic sample, \( a = 0 \) and \( E(\theta) = \frac{1}{2\pi} \), which is a circle with a uniform distribution of \( \frac{1}{2\pi} \) per radian.

The histogram of spatial distribution of directions of particle contact normals for the dense sample at \( \sigma = 100 \text{ kPa} \) is illustrated in Fig. 9. The Fourier approximation function is indicated by the red ellipse with the long axis indicating the major principal direction of fabric (\( \theta_a \)). The major principal fabric direction of the initial sample is 92°. When sheared to the maximum strain (0.52% or 0.3°), the major principal fabric direction rotates to the diagonal direction (\( \theta_a \approx 130.0° \)); when it is sheared to minimum strain (−0.52% or −0.3°), the major principal fabric direction rotates to the perpendicular diagonal direction (\( \theta_a \approx 40.0° \)). Note that the sample boundaries are only rotated up to 0.6°; however, the major principal fabric direction rotates about 90°.

The evolutions of \( \theta_a \) at \( \gamma_{\text{max}} \) and \( \gamma_{\text{min}} \) for Series A and D are plotted in Fig. 10; the other Series show similar trends to Series A thus not included here. Note that the initial \( \theta_a \) at \( \gamma = 0 \) for the four samples are 83° (loose, \( \sigma = 50 \text{ kPa} \)), 165° (loose, \( \sigma = 100 \text{ kPa} \)), 80° (dense, \( \sigma = 50 \text{ kPa} \)) and 92° (dense, \( \sigma = 100 \text{ kPa} \)). It can be observed from Fig. 10a, that the rotation of \( \theta_a \) occurs slowly in loose samples. For the loose sample with \( \sigma = 50 \text{ kPa} \), \( \theta_a \) at \( \gamma_{\text{max}} \) starts from about

\[
E(\theta) = \frac{1}{2\pi} \left[ 1 + a \cos 2(\theta - \theta_a) \right]
\]
110° and increases slowly to 130° at large cycle number; while for the loose sample with σ = 100 kPa, θa at γmax starts from about 140° and decreases slowly to 130°. However, for both dense samples, θa at γmax reaches 130° in the first loading cycle and remains at 130°. Rotation of θa at γmin shows similar trend: rotation of θa occurs slowly in loose samples until it reaches 40°; θa in dense samples arrives at 40° in the first cycle. In the other simulation Series, rotation of θa does not show obvious difference with various γmin or ηc except for the Simulation D-6 with ηc = 0.5, where θa at γmin does not reduce to 40° as other simulations, but stays at 130° for γmin for about 10 cycles, then reduces slowly to 65° following 6000 loading cycles. The stabilised fabric following cyclic loading is not a unique feature for drained tests, but also observed in undrained cyclic tests [34, 35]. It is also interesting to observe that θa at γmax and θa at γmin do not symmetric about 90°, but 85° for all simulations, despite their loading asymmetry. One hypothesis for this phenomenon is the rotation direction in the first quarter of the first cycle. Further investigation will be carried out in the future to verify this hypothesis.

The magnitude of fabric anisotropy is quantified by a in Eq. (2). It has been demonstrated previously [30, 31] that larger magnitude of anisotropy can result in higher shear stress. As illustrated in Fig. 9, a relates to the aspect ratio of the red ellipse. At γmax, the long axis is along 130° and short axis is along 40°; at γmin, the long axis and short axis swap locations. Thus, the variation of fabric anisotropy from γmax to γmin can be quantified by the change of axis length along one principal direction, or a_max+a_min. On the other hand, fabric anisotropy is an indicator of shear stress magnitude, while G is determined by (τ_max−τ_min)/(γ_max−γ_min); therefore, a_max+a_min could be an indicator of G for the same level of (γ_max−γ_min). The evolutions of a_max+a_min for the five simulation Series are shown in Fig. 11. It is clear in Fig. 11a that a_max+a_min...
3.2.4 Rotation of principal directions

The average stresses within the specimen during cyclic loading were monitored and the principal stresses and principal directions were determined. It is found that the major principal directions and the major fabric directions incline similar angles to the horizontal: 130° for both the major principal directions and the major fabric directions at \( \gamma_{\text{max}} \); 40° for the major fabric directions and 50° for the major principal directions at \( \gamma_{\text{min}} \). The rotations of the major principal directions in the first three cycles were illustrated in Fig. 12. Note that the initial major principal direction of the loose sample with \( \sigma = 100 \text{kPa} \) has an approximate horizontal orientation, while the remaining three samples have approximate vertical orientations. The rotation of the major principal direction of the loose sample with \( \sigma = 50 \text{kPa} \) is slower than the other three samples in the first three cycles (Fig. 12a). The rotation of the major principal direction for various \( \gamma_{\text{max}} \) yields same values at maximum and minimum strain, but forms larger loops for larger \( \gamma_{\text{max}} \) (Fig. 12b). Apart from the loose sample with \( \sigma = 50 \text{kPa} \), for all the remaining samples with symmetric two-way loading as shown in Fig. 12a–c, majority of the principal direction rotation occur at about half the \( \gamma_{\text{max}} \) (\( \gamma_{\text{min}} \)) in the loading (unloading) stages. Outside the strain range of (\( \gamma_{\text{min}}/2, \gamma_{\text{max}}/2 \)), principal directions remain almost constant. Due to this feature, the rotation of principal direction with \( \eta_c > 0 \) in Series D and E shows some interesting characteristics. In particular, in Simulation D-6, where \( \eta_c = 0.5 \), as \( \gamma_{\text{min}} \) is only half of \( \gamma_{\text{max}} \) rotation of principal direction has not start yet before the loading changes direction in initial cycles. As a result, major principal direction remains at about 130° in the first three cycles (black curves in Fig. 12d). Rotation of principal direction for this sample gradually started after ten cycles and approaches 80° at the end of 6000 loading cycles. This delayed rotation of principal stress direction agrees with the delayed rotation of principal direction of fabric (Fig. 10b). In Simulation E-6 (loose sample with \( \eta_c = 0.5 \)), as sample is relative loose and there are more spaces for particle movements and rearrangements, even the \( \gamma_{\text{min}} \) is only half of \( \gamma_{\text{max}} \) rotation of principal direction starts from the first cycle to a smaller extent (Fig. 12e). But the shapes of the direction-strain loop are still different from majority simulations: the delay of rotation when loading direction changes at \( \gamma_{\text{min}} \) is not observed in Simulation D-6 and E-6. This is because the principal direction has yet stabilised at \( \gamma_{\text{min}} \) as other simulations with lower \( \gamma_{\text{min}} \).

3.2.5 Particle movements

Particle movements during 6000 loading cycles for a few representative simulations are displayed in Fig. 13. It can be observed clearly from Fig. 13a that for the dense sample with \( \eta_c = 0.5 \) (Simulation D-6), the particles flow anticlockwise slightly within the box due to the low value of \( \gamma_{\text{max}} - \gamma_{\text{min}} \), i.e. low intensity of vibration. As the \( \eta_c \) decreased to −1.0 (Fig. 13b), i.e. \( \gamma_{\text{max}} - \gamma_{\text{min}} \) increases, particle movements are more remarkable and there are local
vortices formed. For both simulations, no clear volumetric change can be observed, which is consistent with the void ratio observation. However, for the two simulations of loose samples (Fig. 13c and d), in addition to the local vortices, clearly inward particle movements can be observed along the top and bottom boundaries, which is again consistent with the observations of void ratios. Moreover, the particle displacements are more intensive with increasing \((\gamma_{\text{max}} - \gamma_{\text{min}})\), because there are more voids within loose samples allowing particle movement and rearrangements.

### 3.3 Effect of cyclic loading on \( p\)-\( y\) curve and critical state analysis

In the design of monopile for the offshore wind turbine, soils surrounding monopile may be replaced by a series of independent springs with their reaction forces applied to monopile specified by \( p\)-\( y\) curves. The \( p\)-\( y\) curve could be attained from the conversion of a \( \tau\)-\( \gamma\) curve [36]. Therefore, it is worth to check the variations of \( \tau\)-\( \gamma\) curve (thus \( p\)-\( y\) curve) following 6000 cycles of loading.
Figure 14 shows the normalised τ-γ curves for the original dense and loose samples (without cyclic loading) with \( \sigma = 50 \text{ kPa} \) and \( 100 \text{ kPa} \) as well as the evolutions of \( e \) during monotonic simple shear tests until shear strain \( \gamma = 52\% \). Dense samples show higher initial stiffness and higher peak stress ratios as expected. Specimen with similar initial \( e \)
Fig. 13  Particle convections in 6000 loading cycles (amplified by 2.0)

(a) Dense sample, $\sigma = 100$ kPa, $\gamma = (0.46\%, 0.92\%)$ ($\eta_c = -1.0$) – Simulation D-6

(b) Dense sample, $\sigma = 100$ kPa, $\gamma = (-0.92\%, 0.92\%)$ ($\eta_c = 0.5$) – Simulation D-1

(c) Loose sample, $\sigma = 100$ kPa, $\gamma = (0.46\%, 0.92\%)$ ($\eta_c = 0.5$) – Simulation E-6

(d) Loose sample, $\sigma = 100$ kPa, $\gamma = (-0.92\%, 0.92\%)$ ($\eta_c = -1.0$) – Simulation E-1
shows slightly higher peak stress ratio and initial stiffness under lower $\sigma$. The $e$ responses of dense samples showed clearly dilation and finally approached the critical $e$, while loose samples also showed slightly dilation.

Similar monotonic simple shear tests were also performed on those four samples followed 6000 cycles of symmetric loadings with shear strain amplitude $\gamma = \pm 0.52\%$. The stress–strain and volumetric responses during monotonic simple shear test were illustrated in Fig. 15. Comparing Fig. 15b with Fig. 6a, it is interesting to observe that loose specimen densifies during cyclic loading, with $e$ approaches constants similar to the values for dense samples; however, these values are not the critical $e$. The cyclic loading equalises the sample density which leads to very similar stress–strain response and volumetric responses of these four samples as observed in Fig. 15.

To have a better understanding of the relationship of the stress ratios and $e$ at the peak and critical states, the stress paths for the eight simulations as well as the critical state line (CSL) were plotted in Fig. 16, where the mean stress $s' = (\sigma_1' + \sigma_2')/2$, the deviator stress $q = \sigma_1' - \sigma_2'$ and $\sigma_1', \sigma_2'$ are the principal stresses. The CSL is obtained by least-square fitting of the $e$–log($s'$) values or the $q$–$s'$ values of the eight simulations at the critical state. It can be observed that the $e$ for one relative loose sample ($\sigma = 100$ kPa) is just below the critical state $e$, while the other loose sample ($\sigma = 50$ kPa) is below further (Fig. 16a). The $e$ values for the two dense samples are well below the critical state $e$. In the simple shear tests, their mean stresses first increase to the peak state value with small increases of $e$, then decrease significantly with further increases of $e$ until reaching the critical state line. It can be seen that the loose sample with $\sigma = 100$ kPa has similar response to real loose sand; the loose sample with $\sigma = 50$ kPa has similar response to medium sand; and the two dense samples behave similar to very dense sand. As shown in Fig. 16b, these four samples reach different peak failure envelops due to various initial $e$ values.

When the two loose samples subjected to 6000 cycles of symmetric shearing loadings, their $e$ values reduce significantly with mean stresses remain unchanged; while the two dense samples remain similar $e$ and mean stresses during cyclic loading (Fig. 16c). When the cyclically sheared samples are subjected to simple shear tests, all four samples have similar responses: reaching a same peak failure envelop due to similar $e$ and then dropping onto the critical state line (Fig. 16d). Therefore, cyclic loading equalises the distances between the sample state points and the critical state line. Based on the critical state soil mechanics theory, the distance between a soil state and the critical state line dominates soil responses, thus the four samples post cyclic loading show very similar responses.
Series of DEM simulations of cyclic simple shear tests with various strain profiles (one-way or two-way) were performed to explore the variations of soil characteristics under cyclic loading and its underlying micro-mechanism. It has been found that:

- Shear modulus for loose soil increases rapidly in the initial loading cycles as a result of soil densification, and then the rate of increase diminishes when void ratio approaches a constant; shear modulus of the very dense samples in DEM decreases but dilation is not the main reason.
- Under the same vertical stress and strain amplitude, shear moduli and void ratios of dense sample and loose sample approach the same values at larger number of cycles.
- Shear modulus increases with increasing vertical stress and relative density, but decreases with increasing strain amplitude as expected.
- Higher shear stress level and shear modulus are correlated to higher coordination number and higher magnitude of fabric anisotropy.
- Accumulated rotation of principal direction of fabric and major principal direction occurs slowly in loose sample, but reaches the final value in the first cycle in dense sample. In each symmetric loading cycle, majority of the principal direction rotation occurs between half of \( \gamma_{\text{min}} \) and half of \( \gamma_{\text{max}} \) in spite of the magnitude of \( \gamma_{\text{max}} \). There are delays in the reverse of principal direction rotation immediately after the boundary rotation is reversed apart from the case with \( \eta_c = 0.5 \) where the vibration intensity is low and sample has not stabilised at \( \gamma_{\text{min}} \).
- Loading asymmetry only affects soil behaviours in the first hundreds of cycles. In long term, the magnitude of

**Fig. 16** Stress path for original samples and cyclically sheared samples
Macro- and micro-mechanics of granular soil in asymmetric cyclic loadings encountered by...

(\gamma_{\text{max}} - \gamma_{\text{min}}) rather than loading asymmetry dominates the soil responses.

- Changes in the stress–strain behaviour (thus p-y curve) of soil due to cyclic loading are significantly dependent on the initial relative density and the distance between the state point and the critical state line.

This study verifies the capability of DEM in analysing the micro-mechanism underling the soil stiffness variation during cyclic loading. More studies will be carried out in the future work, in particular, non-circular disks will be considered to explore the particle shape effect. An empirical model for evolution of shear modulus will be established to include the impact of all macroscopic and microscopic parameters. These findings provide basis for improving the design codes for offshore wind turbine foundations.

Acknowledgements The authors would like to acknowledge VJ Tech Ltd and the University of Surrey, which collectively funded this project.

Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

Open Access This article is distributed under the terms of the Creative Commons Attribution 4.0 International License (http://creativecommons.org/licenses/by/4.0/), which permits unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.

References

1. Bhattacharya, S., Adhikari, S.: Experimental validation of soil–structure interaction of offshore wind turbines. Soil Dyn. Earthq. Eng. 31(5–6), 805–816 (2011)
2. DNV: Offshore Standard DNV-OS-J101 Design of offshore wind turbine structures. In: Høvik, Norway (2014)
3. Li, W., Igoe, D., Gavin, K.: Field tests to investigate the cyclic response of monopiles in sand. Proc. Inst. Civil Eng. Geotech. Eng. 168(GE5), 407–421 (2014)
4. Bhattacharya, S., Cox, J., Lombardi, D., Muir Wood, D.: Dynamics of offshore wind turbines on two types of foundations. Proc. Inst. Civil Eng. Geotech. Eng. 166(GE2), 159–169 (2013)
5. Bhattacharya, S., Nikitas, N., Garness, J., Alexander, N., Cox, J., Lombardi, D., Muir Wood, D., Nash, D.: Observed dynamic soil–structure interaction in scale testing of offshore wind turbine foundations. Soil Dyn. Earthq. Eng. 54, 47–60 (2013)
6. Cuéllar, P., Georgi, S., Baessler, M., Rücker, W.: On the quasi-static granular convective flow and sand densification around pile foundations under cyclic lateral loading. Granul. Matter 14(1), 11–25 (2012)
7. Zhu, B., Byrne, B.W., Houlshby, G.T.: Long-term lateral cyclic response of suction Caisson foundations in sand. ASCE J. Geotech. Geoenviron. Eng. 139(1), 73–83 (2013).
8. Zhu, F.Y., O’Loughlin, C.D., Bienen, B., Cassidy, M.J., Morgan, N.: The response of suction caissons to long-term lateral cyclic loading in single-layer and layered seabeds. Geotechnique 68(8), 729–741 (2018)
9. Zhang, C., White, D., Randolph, M.: Centrifuge modeling of the cyclic lateral response of a rigid pile in soft clay. ASCE J. Geo-tech. Geoenviron. Eng. 137(7), 717–729 (2011)
10. Klinkvort, R.T., Hededal, O.: Lateral response of monopile supporting an offshore wind turbine. Proc. Inst. Civil Eng. Geotech. Eng. 166(GE2), 147–158 (2013)
11. Achmus, M., Kuø, Y.-S., Abdel-Rahman, K.: Behavior of monopile foundations under cyclic lateral load. Comput. Geotech. 36, 725–735 (2009)
12. Cui, L., Bhattacharya, S.: Soil–monopile interactions for offshore wind turbines. Proc. ICE Eng. Comput. Mech. 169(4), 171–182 (2016)
13. Duan, N., Cheng, Y., Xu, X.: Distinct-element analysis of an offshore wind turbine monopile under cyclic lateral load. Proc. Inst. Civil Eng. Geotech. Eng. 170(6), 517–533 (2017)
14. Gerolymos, N., Escoffier, S., Gazetas, G., Garnier, J.: Numerical modeling of centrifuge cyclic lateral pile load experiments. Earthq. Eng. Eng. Vib. 8, 61–76 (2009)
15. Jalbi, S., Arany, L., Salem, A., Cui, L., Bhattacharya, S.: A method to predict the cyclic loading profiles (one-way or two-way) for monopole supported offshore wind turbines. Mar. Struct. 63, 65–83 (2019)
16. Wichtmann, T., Niemunis, A., Triantafyllidis, T.: Strain accumulation in sand due to cyclic loading: drained triaxial tests. Soil Dyn. Earthq. Eng. 25, 967–979 (2005)
17. Sim, W.W., Aghakouchak, A., Jardine, R.J.: Cyclic triaxial tests to aid offshore pile analysis and design. Proc. Inst. Civil Eng. Geotech. Eng. 166(GE2), 111–121 (2013)
18. Okur, D.V., Ansal, A.: Stiffness degradation of natural fine grained soils during cyclic loading. Soil Dyn. Earthq. Eng. 27, 843–854 (2007)
19. Shahnazari, H., Dehnavi, Y., Alavi, A.H.: Numerical modeling of stress–strain behavior of sand under cyclic loading. Eng. Geol. 116, 53–72 (2010)
20. Sitharam, T.G.: Discrete element modelling of cyclic behaviour of granular materials. Geotech. Geol. Eng. 21, 297–329 (2003)
21. Yin, Z.-Y., Chang, C.S., Hicher, P.-Y.: Micromechanical modelling for effect of inherent anisotropy on cyclic behaviour of sand. Int. J. Solids Struct. 47, 1933–1951 (2010)
22. Asadzadeh, M., Soroush, A.: Macro- and micromechanical evaluation of cyclic simple shear test bydiscrete element method. Particuology 31, 129–139 (2017)
23. Nikitas, G., Arany, L., Aingaran, S., Vimalan, J., Bhattacharya, S.: Predicting long term performance of Offshore Wind Turbines using Cyclic Simple Shear apparatus. Soil Dyn. Earthq. Eng. 92, 678–683 (2016)
24. ASTM: Standard Test Method for Consolidated Undrained Direct Simple Shear Testing of Cohesive Soils. In: D6528-07 (2007)
25. Lombardi, D., Bhattacharya, S., Scarpa, F., Bianchi, M.: Dynamic response of a geotechnical rigid model container with absorbing boundaries. Soil Dyn. Earthq. Eng. 49, 46–56 (2015)
26. Kelly, R.B., Houlshby, G.T., Byrne, B.W.: Transient vertical loading of model suction caissons in a pressure chamber. Geotechnique 56(10), 665–675 (2006)
27. Lombardi, D., Bhattacharya, S., Muir Wood, D.: Dynamic soil–structure interaction of monopole supported wind turbines in cohesive soil. Soil Dyn. Earthq. Eng. 49, 165–180 (2013)
28. Kühn, M.: Dynamics of offshore wind energy converters on monopile foundations—experience from the Lely offshore wind farm Paper presented at the OWEN Workshop “Structure and
29. Cui, L., O’Sullivan, C., O’Neil, S.: An analysis of the triaxial apparatus using a mixed boundary three-dimensional discrete element model. Geotechnique 57(10), 831–844 (2007)

30. Cui, L., O’Sullivan, C.: Exploring the macro- and micro-scale response characteristics of an idealized granular material in the direct shear apparatus. Geotechnique 56(7), 455–468 (2006)

31. Li, X., Yu, H.S.: Fabric, force and strength anisotropies in granular materials: a micromechanical insight. Acta Mech. 225(8), 2345–2362 (2014)

32. Cambou, B.: Micromechanical approach in granular mechanics. In: Cambou, B. (ed.) Behaviour of Granular Materials. Number 385 in CISM Courses and Lectures. Springer-Verlag, Wien (1998)

33. Rothenburg, L., Bathurst, R.J.: Analytical study of induced anisotropy in idealized granular materials. Geotechnique 39, 601–614 (1989)

34. Wang, G., Wei, J.: Microstructure evolution of granular soils in cyclic mobility and post-liquefaction process. Granular Matter 18(3), 51 (2016)

35. Wei, J., Huang, D., Wang, G.: Microscale descriptors for particle-void distribution and jamming transition in pre-and post-liquefaction of granular soils. ASCE J. Eng. Mech. 144(8) (2018). https://doi.org/10.1061/(ASCE)EM.1943-7889.0001482

36. Zhang, Y., Andersen, K.H.: Scaling of lateral pile p–y response in clay from laboratory stress–strain curves. Mar. Struct. 53, 124–135 (2017)

Publisher’s Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.