MRXCAT: Realistic numerical phantoms for cardiovascular magnetic resonance

Lukas Wissmann1, Claudio Santelli1,3, William P Segars2 and Sebastian Kozerke1,3*

Abstract

Background: Computer simulations are important for validating novel image acquisition and reconstruction strategies. In cardiovascular magnetic resonance (CMR), numerical simulations need to combine anatomical information and the effects of cardiac and/or respiratory motion. To this end, a framework for realistic CMR simulations is proposed and its use for image reconstruction from undersampled data is demonstrated.

Methods: The extended Cardiac-Torso (XCAT) anatomical phantom framework with various motion options was used as a basis for the numerical phantoms. Different tissue, dynamic contrast and signal models, multiple receiver coils and noise are simulated. Arbitrary trajectories and undersampled acquisition can be selected. The utility of the framework is demonstrated for accelerated cine and first-pass myocardial perfusion imaging using k-t PCA and k-t SPARSE.

Results: MRXCAT phantoms allow for realistic simulation of CMR including optional cardiac and respiratory motion. Example reconstructions from simulated undersampled k-t parallel imaging demonstrate the feasibility of simulated acquisition and reconstruction using the presented framework. Myocardial blood flow assessment from simulated myocardial perfusion images highlights the suitability of MRXCAT for quantitative post-processing simulation.

Conclusion: The proposed MRXCAT phantom framework enables versatile and realistic simulations of CMR including breathhold and free-breathing acquisitions.

Keywords: Cardiovascular magnetic resonance, Image reconstruction, XCAT, Numerical phantom

Background

Advanced acquisition strategies and image reconstruction have become major research topics in cardiovascular magnetic resonance (CMR). New techniques are commonly validated using numerical phantoms. However, computer simulations are often based on oversimplified and unrealistic models. Furthermore, the lack of standardized reference models has resulted in a large diversity in simulation methods hampering appropriate cross-validation. Comparability is, however, of particular relevance in CMR, where cardiac and respiratory motions add to simulation complexity.

Image reconstruction has evolved into a significant branch of MRI research. Considerable efforts have been invested into the development of non-Cartesian and accelerated data acquisition strategies, as they permit reduced scan time, increased spatial and/or temporal resolution or a combination of these benefits [1-4]. Despite the growth of the research field, it remains difficult to benchmark the various image reconstruction approaches. Among others, one reason for this is the lack of comparability between simulation setups.

Simulation models can be divided in two groups. Analytical numerical phantoms mathematically describe the simulated anatomy and the imaging experiment. The first analytical phantom to be used widely for imaging simulations was the Shepp-Logan head phantom [5]. Further development led to computationally more complex cerebral phantoms specifically designed for MRI, using elliptical shapes [6-9] or combinations of different geometrical contours [10]. Voxel based phantoms, on the other hand, are usually derived from acquired images of a single volunteer or patient, with a few segmented tissue types only
and adapted to the purpose of the study [11]. This has led to a plethora of numerical phantoms used by individual research groups. Voxel based phantoms are realistic and easily accessible, but limited to the acquisition parameters they are based on, such as spatial and temporal resolution. Furthermore, for voxel based phantoms the image to k-space relation is approximated by the discrete Fourier transform, which ignores k-space truncation errors. These effects are omitted with analytical phantoms, where the continuous Fourier transform is well-defined. In contrast, analytical phantoms usually do not incorporate motion as required in CMR.

A practical approach to numerical phantoms is the integration of advantages of both analytical and voxel-based methods into hybrid phantoms. Hybrid phantoms address the key limitations of analytical and voxel-based approaches, leading to a versatile, realistic and reproducible simulation framework. The Mathematical Cardiac-Torso (MCAT) and the extended Cardiac-Torso (XCAT) phantoms present such approaches by combining voxel-based in-vivo data with non-uniform rational B-splines (NURBS) or polygon meshes to define anatomical objects [12-14]. The anatomical information in XCAT is based on the Visible Human Project of the National Library of Medicine [15].

Several numerical phantoms for CMR applications have been proposed so far, including analytical [16], voxel based [17] and hybrid models [18-25]. These in part allow for reproducible figures of merit based on known simulation parameters such as spatial resolution. Despite the attempt to generate versatile and realistic phantoms, none of the above-mentioned studies have made their phantoms available to the community. Therefore, reproducibility is limited and reimplementation of the phantom is cumbersome.

In this paper, a hybrid numerical CMR phantom referred to as MRXCAT is presented. MRXCAT is a simulation framework designed for research on CMR sampling and reconstruction strategies in the presence of motion. In order to promote comparability and reproducibility in CMR simulation research, MRXCAT is made available online to the community [26]. Cine and myocardial perfusion MRXCAT implementations are presented alongside with reconstruction and post-processing examples as showcase applications.

Mathematically, the MRXCAT phantom \( D(\mathbf{k}, t) \) in k-t space is expressed as

\[
D(\mathbf{k}, t) = \sum_{i=1}^{NS} R_i \circ G \cdot F[S(N_{c}, r_c, \mathbf{x}_c)] \cdot C_m(T_1, T_2, \rho, c(t)) \cdot O_i(\mathbf{x}, t) + n(\mathbf{x}, t),
\]

where \( O_i(\mathbf{x}, t) \) is the XCAT object, which is a function of space and time, and \( n(\mathbf{x}, t) \) denotes object noise. The circle denotes application of the operator on the left hand side of \( \circ \) onto the object on the right hand side. Consecutive operations are applied from right to left. \( T \) is the tissue operator, which depends on relaxation times \( T_1, T_2 \), the proton density \( \rho \) and the contrast agent concentration \( c(t) \). The sequence operator \( C_m \) implements the signal model \( m \) with various parameters including echo time \( T_E \), repetition time \( T_R \), flip angle \( \alpha \) and number of repetitions \( N_R \). Coil operator \( S \) applies coil sensitivities of \( N_c \) receive coils with radius \( r_c \) and location \( \mathbf{x}_c \) as input. After Fourier transform \( F \), the gridding operator \( G \) and the sampling operator \( R_i \) convert the raw k-space phantom into simulated MRI data, as detailed below. The index \( i \) refers to k-space segmentation. In segmented acquisition, the full XCAT and noise objects are created for each segment \( i \) and the sampling operator \( R_i \) extracts the segment \( i \) from the full k-space data.

**XCAT object module**

A number of physiological parameters such as heart beat and respiratory cycle duration can be adjusted in XCAT. Several parameters are defined at the XCAT input including spatial and temporal resolution, matrix size, slice offcentres and angulation and the number of simulated heart beats. The timing information allows setting the temporal resolution during the heart phase and the number of segments needed to acquire the full k-space. XCAT produces binary masks of different organs and tissue types. The blood pool and myocardial tissue of the atria and ventricles in the left and right heart are divided into eight individual partitions. Arteries, veins and pericardium form separate compartments.

**Tissue and sequence operators**

Using the tissue and sequence operators \( T \) and \( C_m \), the organ masks (XCAT object \( O_i \)) are assigned realistic MR signal intensities based on tissue properties \( T_p, T_m \) proton density \( \rho \) and contrast agent concentration \( c(t) \). The concentration is used to simulate dynamic contrast enhancement by shortening \( T_1 \). Sequence timing parameters such
as repetition time \( T_R \), echo time \( T_E \), number of repetitions \( N_R \) and the flip angle \( \alpha \) are at hand. Finally, signal model \( m \) converts these parameters to signal intensities. Examples of available signal models are balanced SSFP [27,28] and saturation-recovery gradient echo sequences [29,30].

Dynamic contrast enhancement during first-pass myocardial perfusion is simulated based on a population average arterial input function (AIF) from six healthy volunteers. A contrast dose of 0.025 mmol/kg b.w. and a short saturation delay (30 ms) were used to ensure linearity between signal intensity and contrast agent concentration [31]. Mid-ventricular signal intensity vs. time curves were extracted from the left ventricle and manually shifted in time to the same bolus arrival time before averaging, which mitigates temporal broadening of the AIF peak by averaging. The population average AIF was fitted by a 3-parameter gamma-variate function to obtain a first-pass AIF of the contrast bolus [32]. The myocardial concentration-time curve is obtained by convolution with a Fermi function [30]. The blood pool and myocardial concentrations are then converted to signal intensities using the relationship between \( T_1 \) and concentration \( c(t) \),

\[
R_1 = \frac{1}{T_{1,0}} + c(t) \cdot R,
\]

where \( T_{1,0} \) is the baseline tissue \( T_1 \) in the absence of contrast agent and \( R \) the relaxivity of the contrast agent.
Coil operator and noise object

Three-dimensional coil sensitivities are simulated using the Biot-Savart law,

\[
\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} \oint_{\text{coil}} i \, dl \times \left( \mathbf{r} - \mathbf{r}' \right),
\]

by discretising the integral and calculating the effective magnetic field at the voxel positions of the XCAT masks. Normalized sensitivity masks are multiplied with the phantom yielding one dataset per coil. Adjustable parameters in this module are the number of receive coils \( N_C \), the radius \( r_C \) and position \( \mathbf{x}_C \) of the individual coil elements. The coil elements are arranged on one or more circles around the MRXCAT phantom to mimic typical cardiac coil arrays around the chest. Note that the Biot-Savart law is only valid in the near field approximation, i.e. for field strengths < 4 T. Since most CMR protocols are designed for 3 T or lower field strength the approximation is considered a valid assumption.

A spatial low-pass filter option is implemented at this point with variable filter strength to obtain realistic signal intensities at tissue interfaces. White Gaussian noise is added to obtain the desired signal-to-noise ratio (SNR). In case of dynamic contrast enhancement, the noise level is defined by the contrast-to-noise ratio (CNR). After this step, the fully sampled Cartesian MRXCAT phantom is available.

Gridding and sampling operators

The image-domain phantom is transformed into \( k \)-space via discrete Fourier transform \( F \). The gridding operator \( G \) allows interpolation of the data onto non-Cartesian trajectories. To apply these trajectories, the non-uniform fast Fourier transform (NUFFT) implementation by J. Fessler [33] and the NUFFT wrapper by M. Lustig [2] are used, which are available online [34,35]. The sampling operator \( R \) defines the sampled \( k \)-space profiles and enables application of undersampling schemes by omitting certain \( k \)-space lines. If the simulated acquisition consists of multiple \( k \)-space segments, the required segment is extracted from the full \( k \)-space. The MRXCAT phantom production is repeated for each segment to yield the final MRXCAT phantom, which is saved as MATLAB output. Other output formats such as the ISMRMRD data structure [36] are possible.

MRXCAT examples and in-vivo comparison

To allow comparison of the numerical phantoms with in-vivo CMR, cine and first-pass myocardial perfusion in-vivo data were acquired in two healthy volunteers. CMR was performed on two Philips Achieva scanners (Philips Healthcare, Best, The Netherlands) at 1.5 T and 3 T field

Figure 2 MRXCAT software structure. Geometry, timing and physiology parameters are set at the XCAT input. The tissue and sequence operators depend on tissue properties, sequence parameters and the signal model \( m \). The coil operator and noise object use coil geometry and SNR as input. The trajectory governs the effect of the gridding and sampling operators.
strengths. All volunteers gave informed consent according to institutional policy. Cine in-vivo parameters were: spatial resolution: 1.56×1.56 mm², 10 mm slice thickness, field-of-view: 400×400 mm², \( T_R = 3.4 \) ms, \( T_E = 1.7 \) ms, flip angle = 50°, 20 heart phases. Parameters for in-vivo myocardial perfusion imaging were: spatial resolution: 2.14×2.25×5 mm³, field-of-view: 360×360×80 mm³, \( T_R = 1.97 \) ms, \( T_E = 0.78 \) ms, flip angle = 15°. Perfusion image acquisition was performed using a 10-fold accelerated saturation-recovery gradient echo sequence with a saturation delay of 150 ms followed by \( k-t \) PCA reconstruction [37]. A gadolinium bolus (Gadovist, Bayer Healthcare, Zurich, Switzerland) with a contrast agent dose of 0.025 mmol/kg b.w. was applied during a breathhold acquisition of 30 time frames.

Example cine and myocardial perfusion MRXCAT phantoms were generated with \( T_I \) and \( T_2 \) values according to textbook literature [38]. Relative proton densities were extracted from a proton-density weighted in-vivo measurement. Two-dimensional (2D) cine MRXCAT parameters were equal to the in-vivo measurement, except for the number of heart phases, which was set to 24 to enable 8-fold undersampling and \( k-t \) reconstruction without zero-filling (cf. below). An SNR of 20 and 15 segments were simulated. Parameters for simulated first-pass myocardial perfusion imaging were as in-vivo except for the in-plane resolution, which needed to be isotropic in XCAT and was set to 2.14×2.14 mm². Further parameters were: CNR of 30, 40 profiles from acquisition start to \( k \)-space centre, contrast agent dose: 0.075 mmol/kg b.w., contrast agent relaxivity: \( R = 5.6 \) l/mmol·s, 32 acquired time frames with one image per heartbeat. Rest and stress myocardial blood flow were set to 1.0 and 3.5 ml/g/min, respectively.

**Image reconstruction and quantification from undersampled data**

Both the 2D cine and the 3D myocardial perfusion fully sampled Cartesian phantoms were retrospectively undersampled and reconstructed using \( k-t \) PCA [39] and \( k-t \) SPARSE [40]. For both cases, an acceleration factor of \( R = 8 \) was chosen. To visualise local variations in reconstruction accuracy, error maps were calculated by subtracting the reconstructed images from the fully sampled reference phantom reconstruction. All error maps were normalized by the average signal intensity over all time frames of the reference image to yield percentage errors. Root mean square error (RMSE) values were calculated for each case to estimate the total error. Quantification of myocardial blood flow (MBF) was performed on the myocardial perfusion reconstruction results. Using the XCAT masks, signal intensity-time curves were extracted from left ventricle and myocardium and converted back to contrast agent concentration using equation (2) and the signal model. The signal intensity-time curves allow display of temporal filtering effects introduced by image reconstruction from undersampled data. The concentration vs. time curves were quantified using Fermi model deconvolution [30]. Analysis of the MBF from fully sampled versus undersampled data enabled estimation of the additional uncertainty introduced by undersampling compared to measurement noise.

The MRXCAT extension for XCAT was implemented in MATLAB (MathWorks, Natick, MA, USA). All computations were run on a laptop PC equipped with an Intel i7 m620 2.67 GHz CPU with 2 cores and 8 GB memory. Computation performance numbers were assessed for all computational tasks.

The MRXCAT extension to XCAT is available online: www.biomed.ee.ethz.ch/mrxcat [26].

**Results**

Figure 3 gives an overview of the MRXCAT cine phantom. Examples at systole and diastole are shown in inspiration and expiration states. Temporal profile plots of breathhold MRXCAT cine, free-breathing MRXCAT cine and in-vivo breathhold cine data are demonstrated (Figure 3c). Individual coil maps of a simulated 8-element cardiac coil array are displayed in Figure 3f.

In Figure 4 the whole-heart myocardial perfusion MRXCAT phantom is displayed. Apical, mid-ventricular and basal slices at the time points of bolus arrival in the right and left ventricle as well as in the myocardium are shown in Figure 4a. In-plane profiles as a function of time extracted from the breathhold, free-breathing phantom and in-vivo acquisition are demonstrated in Figure 4b. A cardiac region-of-interest (ROI) is shown in Figure 4c. In addition, the effect of timing of the saturation pulse with respect to the image acquisition is shown for a long saturation to acquisition delay of 150 ms relative to a short saturation delay of 10 ms to demonstrate the non-linearity between MR signal and contrast agent concentration [41].

Figure 5 shows the results of image reconstruction of the breathhold 2D cine MRXCAT phantom with 8-fold data undersampling. A cardiac ROI and a profile through the slice as a function of heart phase are shown. Absolute error maps reveal that both \( k-t \) PCA and \( k-t \) SPARSE yield reconstructed images of good quality. Reconstruction errors are found at the borders of the myocardium, where cardiac contraction causes most motion. The RMSE in the cardiac ROI was 10.0% and 10.2% for \( k-t \) PCA and \( k-t \) SPARSE, respectively.

Figure 6 illustrates reconstruction results for the 8x undersampled myocardial perfusion phantom at time points of bolus enhancement in the left ventricle and myocardium. Error maps show pronounced edge effects for \( k-t \) SPARSE, whereas the error distribution in \( k-t \) PCA is more homogeneous. Signal intensity-time curves
Figure 3 MRXCAT cine phantom overview. Full field-of-view at systole and expiration (a) and at diastole and inspiration breathhold (b). (c) Profiles along dashed line in (b) for 24 heart phases for breathhold and free-breathing MRXCAT with 15 segments and the breathhold in-vivo case for comparison. (d-e) Cardiac region-of-interest at different cardiac phases for breathhold MRXCAT (d) and in-vivo scan (e). (f) Single coil images from 8 individual coils.
for four voxels in the heart are plotted. The RMSE was 16.1% and 14.4% for \( k-t \) PCA and \( k-t \) SPARSE, respectively. Fermi model based MBF quantification in eight mid-ventricular slices of the simulated stress perfusion image is shown for reference, \( k-t \) PCA and \( k-t \) SPARSE reconstructions in six angular sectors per slice. Mean and standard deviation of MBF were 3.48 ± 0.13 ml/g/min in the reference image, 3.48 ± 0.36 ml/g/min for 8× \( k-t \) PCA and 3.55 ± 0.33 ml/g/min for 8x \( k-t \) SPARSE.

Total computation times for MRXCAT generation were 38 and 124 minutes for the breathhold and free-breathing cine phantom, respectively. For the perfusion phantom, calculations took 13.6 and 10.7 minutes for breathhold and free-breathing simulations. In all cases, the vast majority of the time was spent generating the XCAT anatomy. The large difference between cine and perfusion computation times mainly stems from the fact that 360 XCAT time frames were created for cine (24 heart phases, 15 segments), while only 32 time frames were needed for perfusion. By executing only the MATLAB part of MRXCAT, calculation times spanned from 54 s (breathhold cine) to 166 s (free-breathing perfusion).

**Discussion**

In this work a CMR extension to the XCAT phantom has been proposed to enable realistic simulation to aid and benchmark image reconstruction and quantitative post-processing approaches.

The MRXCAT framework is composed of several sequential software modules, which enable user interaction
via parameters at each stage of the simulation. The XCAT hybrid phantom, which is used to simulate anatomy and motion, delivers realistic and generalized tissue masks. Although the XCAT object is rasterised, the drawbacks of voxel based phantoms can be addressed by increasing the spatial resolution in XCAT. The spatial resolution is typically on the order of millimetres in human CMR. Thus, the $0.33 \times 0.33 \times 1 \text{ mm}^3$ voxel size of the Visible Human segmentation [13] is sufficient for most CMR applications. All subsequent software parts act on that rasterised XCAT object, which simplifies implementation and data handling in array-based numerical software. The individual operators or software modules allow setting parameters specific for tissue and sequence, receiver coils, measurement noise and k-space characteristics. The independency between modules potentially enables parallel computing and division of large data portions into chunks on computers with less available memory.

The use of MRXCAT phantoms for research on accelerated imaging was exemplified using $k-t$ PCA and $k-t$ SPARSE. The effect of cardiac contraction in conjunction with image acceleration was showcased with the cine phantom, where the biggest residual errors after

Figure 5 MRXCAT cine reconstruction example. Diastolic and systolic heart phases and profile along the dashed line in (a) for all heart phases. Reference images (a), reconstruction results and difference maps using 8x $k-t$ PCA (b) and 8x $k-t$ SPARSE (c). The gray values for all error maps were scaled from 0 to 30%.
reconstruction remain at the inner and outer border of the myocardium. Using the myocardial perfusion showcase, the effect of signal changes due to contrast agent administration was demonstrated. In this example, residual reconstruction errors mainly stem from temporal filtering of the signal-time curves. Moreover, MRXCAT phantoms can be used for the development of post-processing methods such as myocardial blood flow quantification. A key advantage of quantification using MRXCAT is that noiseless ground truth is always at hand and available for assessment of errors.

The XCAT phantom produces masks with well-defined, sharp tissue boundaries. There is no partial volume effect. This issue was accounted for by adding a low-pass filter module before noise addition. A similar problem is the missing organ texture in XCAT, which has recently been addressed [42]. Organ heterogeneity, however, is currently not incorporated in MRXCAT.

Limitations

MRXCAT allows simulating cine and dynamic single-shot and segmented data acquisition. However, MRXCAT assumes instantaneous acquisition of the individual segments. Extending the framework to enable individual timing of single k-space lines would require full XCAT masks for each k-space line. Since the XCAT part of MRXCAT is the computationally most time-consuming step, this would yield unacceptably long simulation times.

MRXCAT is based on signal equations rather than Bloch equations. As such, it is suitable for the simulation of sampling strategies, trajectory optimization and post-processing methods. However, a number of error sources are excluded, such as magnetic field inhomogeneity, magnetization evolution across time frames or signal alteration due to motion during sampling. For those applications, other simulation frameworks based on solving Bloch equations may be more suitable.
Conclusions
The MRXCAT framework is a versatile tool for simulation in CMR research. Applications to cine and perfusion CMR have shown example usage of the framework. Extensions to other CMR modalities, such as diffusion or flow encoded MRI, are possible.

Abbreviations
AIF: Arterial input function; CMR: Cardiovascular magnetic resonance; CNR: Contrast-to-noise ratio; MBF: Myocardial blood flow; MCAT: Mathematical cardiac-torso; MRXCAT: Magnetic resonance extended cardiac-torso; NUFFT: Non-uniform fast Fourier transform; NURBS: Non-uniform rational B-splines; RMSE: Root mean square error; ROI: Region-of-interest; SNR: Signal-to-noise ratio; XCAT: Extended cardiac-torso.

Competing interests
The authors declare that they have no competing interests.

Authors’ contributions
LW, CS, SK devised MRXCAT in Matlab, created phantom examples, performed image reconstruction and post-processing, WPS implemented off-centres and angulation options in XCAT for this study, LW, SK acquired in-vivo data for reference and prepared the manuscript. All authors read and approved the final manuscript.

Author details
1 Institute for Biomedical Engineering, University and ETH Zurich, Gloriastrasse 35, Zurich 8092, Switzerland. 2 Department of Radiology, Carl Ravin Advanced Imaging Laboratories, The Duke University Medical Center, Durham, USA. 3 Division of Imaging Sciences & Biomedical Engineering, King’s College London, London, UK.

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References
1. Block KT, Frahm J. Spiral imaging: a critical appraisal. J Magn Reson Imaging. 2003; 21:557–68.
2. Lustig M, Donoho D, Pauly JM. Sparse MRI: The application of compressed sensing for rapid MR imaging. Magn Reson Med. 2007; 58:1182–95.
3. Tsao J, Kozerke S. MRI temporal acceleration techniques. J Magn Reson Imaging. 2012; 36:543–60.
4. Deshmane A, Gulani V, Griswold MA, Seiberlich N. Parallel MR imaging. J Magn Reson Imaging. 2012; 36:53–72.
5. Shepp LA, Logan BF. The Fourier reconstruction of a head section. IEEE Trans Nuc Sci. 1974; 21:21–43.
6. Smith MR, Chen L, Hui Y, Mathews T, Yang J, Zeng X. Alternatives to the use of the DFT in MRI and spectroscopic reconstructions. Int J Imaging Syst Technol. 1997; 8:558–64.
7. Van de Walle R, Barrett HH, Myers KJ, Altbach MI, Desplanches B, Gmitro AF, Camerlo J, Lemahieu I. Reconstruction of MR images from data acquired on a general nonregular grid by pseudoinverse calculation. IEEE Trans Med Imaging. 2000; 19:160–70.
8. Koay CG, Sarlis JE, Ozarslan E. Three-dimensional analytical magnetic resonance imaging phantom in the Fourier domain. Magn Reson Med. 2007; 58:430–6.
9. Gach HM, Tanase C, Boada F. 2D & 3D Shepp-Logan Phantom Standards for MRI. In: 9th International Conference on Systems Engineering. 2008; p. 521–6.
10. Guerquin-Kern M, Lejeune L, Pruessmann KP, Unser M. Realistic analytical phantoms for parallel magnetic resonance imaging. IEEE Trans Med Imaging. 2012; 31:526–36.
11. Caon M. Voxel-based computational models of real human anatomy: a review. Radio Environ Biophys. 2004; 42:229–35.
12. Segars WP, Tsui BMW. MCAT to XCAT: The evolution of 4-D computerized phantoms for imaging research. Proc IEEE. 2000; 97:1954–68.
13. Segars WP, Sturgeon G, Mendonca S, Grimes J, Tsui BMW. 4D XCAT phantom for multimodality imaging research. Med Phys. 2010; 37:4902–15.
14. Segars WP, Mahesh M, Beck TJ, Frey EC, Tsui BMW. Realistic CT simulation using the 4D XCAT phantom. Med Phys. 2008; 35:3800–8.
15. The Visible Human Project. [http://www.nlm.nih.gov/research/visible/visible_human.html]
16. Ngo TM, Fung GS, Tsui BM, McVeigh E, Herzka DA. Three dimensional digital polyhedral phantom framework with analytical fourier transform and application in cardiac imaging. In: Proc ISMRM. 2011: p. 1310.
17. Aja-Fernandez S, Cordero-Grande L, Albewia-Lopez C. A MRI phantom for cardiac perfusion simulation. In: 9th IEEE International Symposium on Biomedical Imaging (ISBI). 2012: p. 638–41.
18. Veress AI, Segars WP, Weiss JA, Tsui BMW, Gullberg GT. Normal and pathological NCAT image and phantom data based on physiologically realistic left ventricle finite-element models. IEEE Trans Med Imaging. 2006; 25:1604–16.
19. Sharif B, Bresler Y. Physiological Improved NCAT Phantom (PINCAT) Enables In-Silico Study of the Effects of Beat-To-Beat Variability on Cardiac MR. In: Proc ISMRM. 2007: p. 3418.
20. Sharif B, Derbyshire JA, Faranesh AZ, Bresler Y. Patient-adaptive reconstruction and acquisition in dynamic imaging with sensitivity encoding (PARADISE). Magn Reson Med. 2010; 64:501–13.
21. Tobon-Gomez C, Sukno FM, Butakov C, Huget M, Frangi AF. Simulation of late gadolinium enhancement cardiac magnetic resonance studies. In: Engineering in Medicine and Biology Society (EMBC). 2010: p. 1469–72.
22. Tobon-Gomez C, Sukno FM, Bijens BH, Huget M, Frangi AF. Realistic simulation of cardiac magnetic resonance studies modeling anatomical variability, trabeculae, and papillary muscles. Magn Reson Med. 2011; 65:280–8.
23. Veress AI, Segars WP, Tsui BMW, Gullberg GT. Incorporation of a left ventricle finite element model defining infarction into the XCAT imaging phantom. IEEE Trans Med Imaging. 2011; 30:915–27.
24. Wissmann L, Schmidt JFM, Kozerke S. A Realistic 4D numerical phantom for quantitative first-pass myocardial perfusion MRI. Proc ISMRM; 2013; 21:1322.
25. Tang J, Hall N, Rahimim A. MRI assisted motion correction in dual-gated 3D myocardial perfusion PET imaging. In: Nuclear Science Symposium and Medical Imaging Conference Record (NSS/MIC); 2012: p. 4054–7.
26. MRXCAT - Numerical Phantoms for Cardiac MRI. [http://www.biomed.ee.ethz.ch/mrxcat]
27. Oppelt A, Graumann R, Barfuss H, Fischer H, Hartl W, Schajor W. FISP - A new fast MRI sequence. Etronematica. 1986; 54:15–8.
28. Bernstein MA, King KF, Zhou XJ. Basic pulse sequences. In: Handbook of MRI Pulse Sequences. 2004: p. 594.
29. Brix G, Schad LR, Deimling M, Lorenz WJ. Fast and precise T1 imaging using a TOMROP sequence. Magn Reson Imaging. 1990; 8:551–6.
30. Jerosch-Herold M, Wilke N, Stillman AE. Magnetic resonance quantification of the myocardial perfusion reserve with a Fermi function model for constrained deconvolution. Med Phys. 1998; 25:73–84.
31. Goldstein TA, Jerosch-Herold M, Missetbwitz B, Zhang H, Gropler RJ, Zheng J. Fast mapping of myocardial blood flow with MRI first-pass perfusion imaging. Magn Reson Med. 2002; 48:166–79.
32. Fessler JA, cliffon BP. Nonuniform fast fouriers transforms using min-max interpolation. IEEE Trans Signal Process. 2003; 51:560–74.
33. Fessler JA. Image reconstruction toolbox. [http://web.eecs.berkeley.edu/~mlustig/code/index.html]
34. Lustig M. SparseMRI V0.2. [http://www.eecs.berkeley.edu/~mlustig/SparseMRI.html]
35. ISMRM Raw Data Format (ISMRMRD). [http://ismrmrd.sourceforge.net/]
36. Vitanas V, Manka R, Giese D, Pedersen H, Plein S, Boesiger P, Kozerke S. High resolution three-dimensional cardiac perfusion imaging using compartment-based k-t principal component analysis. Magn Reson Med. 2011; 65:575–87.
37. Bernstein MA, King KF, Zhou XJ. Table of constants and conversion factors. In: Handbook of MRI Pulse Sequences. 2004: p. 961.
38. Pedersen H, Kozerke S, Ringgaard S, Nehrke K, Kim WY. k-t PCA: temporally constrained k-t BLAST reconstruction using principal component analysis. Magn Reson Med. 2009; 62:706–16.
39. Lustig M, Santos JM, Donoho DL, Pauly JM. k-t SPARSE: High frame rate dynamic MRI exploiting spatio-temporal sparsity. In: Proc ISMRM. 2006: p. 2420.
41. Gatehouse PD, Elkington AG, Ablitt NA, Yang G-Z, Pennell DJ, Firmin DN. Accurate assessment of the arterial input function during high-dose myocardial perfusion cardiovascular magnetic resonance. *J Magn Reson Imaging*. 2004; 20:39–45.

42. Bond J, Frush D, Samei E, Segars WP. Simulation of anatomical texture in voxelized XCAT phantoms. In: Proc SPIE 8668, Medical Imaging. 2013. 86680N.