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Suppressed Auger scattering and tunable light emission of Landau-quantized massless Kane electrons

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The Landau level laser has been proposed a long time ago as a unique source of monochromatic radiation, widely tunable in the THz and infrared spectral ranges using an externally applied magnetic field. In spite of decades of efforts, this appealing concept never resulted in the design of a reliable device. This is due to efficient Auger scattering of Landau-quantized electrons, which is an intrinsic non-radiative recombination channel that eventually gains over cyclotron emission in all materials studied so far: in conventional semiconductors with parabolic bands, but also in graphene with massless electrons. The Auger processes are favored in these systems by Landau levels (or their subsets) equally spaced in energy. Here we show that this scheme does not apply to massless Kane electrons in gapless HgCdTe alloy, in which undesirable Auger scattering is strongly suppressed and the sizeable cyclotron emission observed, for the first time in the case of massless particles. The gapless HgCdTe thus appears as a material of choice for future technology of Landau level lasers.

When a magnetic field is applied to a solid, the continuous density of electronic states transforms into a set of discrete energy levels, known as Landau levels (LLs). Electrons excited in such a ladder may recombine with emission of photons. This process can be viewed as an inverse of cyclotron resonance and it is referred to as cyclotron emission. The idea to construct the LL laser by achieving stimulated cyclotron emission is as old as the experimental realization of the very first laser itself. The tunability represents a great advantage of this concept. The strength of the magnetic field defines the spacing between LLs, and therefore, also the emission frequency of the laser. This frequency typically corresponds to the far infrared (terahertz) spectral range. The successful realization of the LL laser would thus bridge the so-called terahertz gap, which still exists despite a considerable effort of several generations of physicists.

There is, however, a fundamental difficulty that has been recognized during the very first attempts to test the concept of a LL laser. In conventional materials, with quadratically dispersing electronic bands, and therefore, with equally spaced LLs, $E_N^S = \hbar\omega_c(N + 1/2)$ for $N = 0, 1, 2$, cyclotron emission is an intrinsically weak process. This is due to two independent processes which compete with cyclotron emission: reabsorption of cyclotron radiation and Auger inter-LL recombination (Fig. 1a). The latter becomes at higher pumping rates extremely efficient for electrons within the equidistant LL ladder, and in consequence, the excited LLs become depleted with a characteristic rate proportional to the number of electrons in this level ($\tau^{-1} \propto n$). Stronger pumping, either optical or electrical, in systems with parabolic bands does not enhance cyclotron emission, but instead, increases the probability of Auger scattering. The inversion of population thus cannot be achieved. Electrons promoted via Auger processes to higher LLs then relax via non-radiative channels, most often by emission of optical phonons.

To overcome this obstacle, various systems with non-equidistant LLs have been proposed as appropriate materials for a LL laser. These may be found, for instance, in different narrow-gap materials or in the valence band of zinc-blende semiconductors. So far, stimulated cyclotron emission was achieved only in bulk germanium in which a non-equidistant spacing of valence-band LLs was created by crossed electric and magnetic fields, as was also the case in graphene. In other attempts, quantum cascade structures have also been tested to achieve efficient cyclotron emission.

Renewed impetus to investigate cyclotron emission came along with the fabrication of graphene, which was considered as an ideal system with non-equidistant LLs.
for the implementation of the LL laser\textsuperscript{10,20}. Its conical band may be viewed as an extreme case of non-parabolicity and implies a specific sequence of Landau levels, $E_N^D = \pm v \sqrt{2e\hbar B N}$ for $N = 0, 1, 2, \ldots$, with the $\sqrt{N}$ spacing, typical of massless Dirac electrons (Fig. 1b). However, to the best of our knowledge, no cyclotron emission, let alone the Landau level laser based on graphene, has been reported so far, despite pertinent theoretical predictions and numerous experimental attempts\textsuperscript{10,20–26}.

This surprising lack of optical emission seems to be a consequence of Auger scattering. Initially, such processes were expected to vanish in Landau-quantized graphene, but finally they were experimentally proven to be present and very efficient\textsuperscript{27,28}. The reason behind is simple. The LL spectrum in graphene: $E_N^D \propto \sqrt{N}$ for $N = 0, 1, 2, \ldots$, includes subsets of equidistant levels. For instance, LLs with indices $N = 0, \pm 1, \pm 4, \pm 9, \ldots$ or $0, \pm 2, \pm 8, \pm 18, \ldots$ are equally spaced and may thus support, similar to conventional materials, efficient Auger recombination (Fig. 1b). Notably, such a conclusion is valid not only for graphene, but for any other system with a conical band described by the Dirac Hamiltonian for particles with a zero rest mass.

Fortunately, one may find other systems with massless electrons, described by a Hamiltonian that differs from the Dirac one. In such systems, equidistantly spaced LLs may be avoided and undesirable Auger scattering possibly suppressed. In this paper, we test Landau-quantized 3D massless Kane electrons\textsuperscript{29–32} against the efficiency of Auger scattering and against the possibility of efficient LL emission. This type of massless electrons appears in conventional bulk zinc-blende semiconductors when their energy band gap – the parameter responsible for the generation of the non-zero band mass of electrons and holes, and therefore, also Schrödinger-like behavior of these carriers – vanishes, for instance, in the ternary compound HgCdTe explored in this paper.

In magnetic fields, the conical band of 3D massless Kane electrons splits into LLs, or more precisely, Landau bands, which resemble those of massless Dirac electrons\textsuperscript{33}:

$$E_{N,\sigma}^K(k) = \pm v \sqrt{2e\hbar B (N - 1/2 + \sigma/2) + \hbar^2 k^2},$$

where $N = 1, 2, 3, \ldots$ is the LL index, $k$ the momentum along the applied magnetic field and $v$ the velocity parameter. However, the splitting due to spin is given by $\sigma = \pm 1/2$ and differs from the one known for genuine Dirac-type electrons ($\sigma = \pm 1$). As a result, the LL spectrum of massless Kane electrons (Fig. 1c): $E_N^K \propto \sqrt{N}$ for $N = 0, 1, 3, 5, \ldots$, does not include any subsets of equally spaced LLs at $k = 0$, where the maxima in the density of states are. In contrast, 3D Dirac electrons with $\sigma = \pm 1$ display at $k = 0$ the spacing $E_N^D \propto \sqrt{N}$ where $N = 0, 1, 2, 3, \ldots$, which is identical to that of 2D graphene.

Moreover, there exists a set of narrowly spaced LLs, which originates from the weakly dispersing (nearly flat) band. In the simplest approach, these LLs do not disperse with $B$: $E_{n,\sigma}^B = 0$ for $n = 0, 2, 3, 4, \ldots$. Excitations from this flat band to conduction-band LLs constitute a dominant contribution to the optical response at low photon energies and follow the standard selection rules, $N \rightarrow N \pm 1$, for electric-dipole transitions\textsuperscript{31,32,34}.

To test Landau-quantized electrons in gapless HgCdTe for the presence of Auger scattering, we have employed a degenerate pump-probe technique, using the free-electron
FIG. 2. Pump-probe experiments and Auger scattering of Landau-quantized massless Kane electrons. (a) and (b) False-color maps of induced transmission $\Delta T/T$ measured at $T = 10$ K and for laser photon energies $\hbar \omega = 78$ meV (upper panel) and $61$ meV (lower panel) as a function of the time delay and magnetic field, showing both, pronounced induced transmission ($\Delta T/T > 0$) and absorption ($\Delta T/T < 0$). (c-e) Selected pump-probe transients. The inter-LL excitations in (d) and (e) follow the standard selection rules for electric-dipole transitions which are active in linearly polarized light, $N \rightarrow N \pm 1$, and schematically shown in the corresponding insets.

To illustrate the observed behavior in greater detail, three selected pump-probe traces are plotted in Figs. 2c-e. At $B = 0$, the observed induced transmission (bleaching) is primarily due to electrons excited from the fully occupied heavy-hole-like flat band to the upper conical band (inset of Fig. 2c). The contribution of excitations from the lower cone is considerably weaker. The induced transmission exhibits a nearly mono-exponential decay, with a characteristic time, $\tau \approx 70$ ps, which is comparable to that in other gapless systems with conical bands, such as graphene. This relaxation may be associated with the emission of phonons.

When the magnetic field is applied, one observes a pronounced change in $\Delta T/T$ transients. For particular values of $B$, the second component develops, with a characteristic decay time in the nanosecond range. This is illustrated in Fig. 2d, where the $\Delta T/T$ trace collected at $B = 5.4$ T and $\hbar \omega = 78$ meV is plotted. In this particular case, electrons are pumped from the flat band to two lowest lying conduction-band LLs, see the inset of Fig. 2d. The faster component, with a relaxation rate not much different from the zero-field one ($\tau \approx 80$ ps), can be associated with the relaxation of electrons excited into the lowest Landau band ($E_{K}^{1,\uparrow}$). This relaxation of electrons from states with finite-momentum towards $k \approx 0$ is probably due to emission of phonons. Most likely, electrons relax via emission of acoustic phonons. The slow component, appearing only when electrons are laser emitting $\sim 3$-ps-long pulses in the mid-infrared range. The results are plotted in Figs. 2a and b, in the form of false color-maps, for two different photon energies of the laser. These maps show pump-probe transients, i.e., the pump-induced relative change of transmission, $\Delta T/T$, as a function of the applied magnetic field and time delay between pump and probe pulses. One immediately concludes that $\Delta T/T$ undergoes a fairly complex evolution in both, its amplitude and sign, on a characteristic time scale extending up to nanoseconds.
pumped resonantly from/to states around $k \approx 0$, reflects the existence of long-living electrons at the bottom of the $E_{1,1}^L$ Landau band. Another example of the slowly decaying component in the pump-probe transient is shown in Fig. 2e. This $\Delta T/T$ trace was collected at $B = 8$ T and $\hbar \omega = 61$ meV, when only the lowest LL in the conduction band ($E_{1,1}^K$) is pumped close to zero-momentum states.

Experiments with circularly polarized radiation represent another way to visualize how the relaxation of photoexcited electrons in gapless HgCdTe is slowed-down when the magnetic field is applied. Pump-probe transients collected using a linearly polarized pump pulse, but with a circularly polarized probe pulse are depicted in Fig. 3. In this particular case, electrons are excited by the pump pulse from the flat band to the lowest lying LL only, as schematically shown by the vertical arrow in the inset of Fig. 3. The transient recorded using $\sigma^-$-polarized probe shows positive $\Delta T/T$, with an initial fast decay due to the relaxation of electrons to the bottom of $E_{1,1}^K$ level and slower component indicating a nanosecond-long lifetime of excited electrons around $k \approx 0$. Different behavior, i.e., strong induced absorption $\Delta T/T < 0$, is observed when the probing beam is $\sigma^+$ polarized. In this latter case, the induced absorption is primarily due to the $E_{1,1}^K \rightarrow E_{2,1}^K$ transition which becomes activated due to electrons promoted to the $E_{1,1}^K$ level by the pump pulse. This excitation corresponds to the fundamental cyclotron mode, which becomes resonant with the laser photon energy ($\hbar \omega = 61$ meV) just at the selected magnetic field of $B = 6.2$ T.

Let us now discuss the main findings of our pump-probe experiments. These show that electrons in Landau-quantized gapless HgCdTe relax with relatively long decay times, at the scale of nanoseconds. In addition, the presented pump-probe experiments were performed at relatively high photon fluences, $\sim 0.5 \mu$J.cm$^{-2}$. These translate, for the chosen photon energy, into the photon flux of $10^{14}$ cm$^{-2}$ per pulse. Due to the relatively large absorption coefficient [1], which in the linear regime, at $\hbar \omega \approx 70$ meV and $B = 0$, reaches $\lambda \approx 3 \times 10^3$ cm$^{-1}$, a significant part of the flux is absorbed in the explored 3-$\mu$m-thick layer of gapless HgCdTe. This corresponds to more than $10^{16}$ cm$^{-3}$ electrons promoted from the flat band to the upper conical band by a single pump pulse. Since there is no decay observed at the scale of the pulse duration ($\sim 3$ ps), this number serves as a rough estimate of the electron density in the sample just after the pump pulse.

One may compare this carrier density and the deduced relaxation time, with the results obtained in conventional semiconductors, where a strong decrease of relaxation time with the electron density has been reported: $\tau \propto n^{-1}$, see Refs. 3, 13, and 36. In conventional semiconductors, the nanosecond decay times are only found at very low carrier densities in the excited LL, in the range of $10^{12}$-$10^{13}$ cm$^{-3}$. For the carrier density close to $10^{16}$ cm$^{-3}$ in a parabolic-band semiconductor, one expects the electron relaxation time to drop down to the sub-picosecond range [1] due to efficient Auger processes.

This is more than three orders of magnitude less than relaxation times observed in gapless HgCdTe in a magnetic field. This indicates that Auger scattering is indeed strongly suppressed for Landau-quantized massless Kane electrons as compared to other materials explored so far. We interpret this suppression as a direct consequence of the specific LL spectrum, which does not include any subset of equidistant levels (around $k \approx 0$).

Since the rate inter-LL Auger scattering follows the degeneracy of Landau levels ($\propto B$) and the strength of interaction between Landau-quantized electrons ($\propto \sqrt{B}$) [37], we expect similarly long lifetimes also at lower magnetic fields. Let us also note that the observed lifetime of electrons, even though unusually long as compared to any so-far explored Landau-quantized semiconductor or semimetal [3], remains significantly shorter than spontaneous cyclotron radiative lifetime. This latter time can be for massless electrons estimated using the simple formula $\tau_{\text{sp}}^{-1} \sim \alpha \omega_c (v/c)^2$, where $\alpha$ is the fine structure constant, $c$ speed of light in vacuum and the characteristic $\omega_c$ cyclotron frequency ($\tau_{\text{sp}} \approx 10^{-6}$ s in the THz range for $v = 10^6$ m/s). Hence, there still exist other (non-radiative) channels which dominate the recombination, such as electron-phonon interaction giving rise to emission of phonons.

The observed slowing-down in the relaxation dynamics of electrons induced by the magnetic field, with the overall lifetime of photo-excited electrons in the nanosecond range, call for cyclotron emission experiments. We have performed such experiments in the THz spectral range, which is the most relevant one for applications of the future Landau level laser technology. To generate cyclotron emission, the sample was placed in a superconducting coil at liquid helium temperature and electri-
cally pumped, using ms-long current pulses, see Methods section. The emitted radiation was analyzed using a photoconductive InSb detector, with a spectrally narrow (cyclotron-resonance-like) response, tunable by a specially dedicated coil. The collected cyclotron emission spectra are plotted in Fig. 4a for selected values of the magnetic field applied to the sample.

A brief inspection of the emission spectra leads us to a conclusion that they feature a single emission band. It position in the spectrum is tunable in the THz range by a relatively low magnetic field (tens of millitesla) and it roughly follows a \( \sqrt{B} \) dependence, which is typical of massless electrons (Fig. 4b). This also agrees well with results of cyclotron absorption experiments performed on the same sample, see Fig. 4c and Ref. 31. However, a closer look at the lineshape suggests that several emission modes actually contribute. Theoretically, one indeed expects several cyclotron emission modes in the interval given by the linewidth (FWHM \( \sim 4 \) meV). In Fig. 4b, the dashed lines show the positions of cyclotron emission modes with the final states of electrons in the four lowest lying conduction-band LLs: \( E_N^{K_{N+1,\uparrow(\downarrow)}} \rightarrow E_N^{K_{N,\uparrow(\downarrow)}} \) for \( N = 1 \) and 2. It is thus the spacing of these cyclotron modes, together with primarily elastic scattering processes, which is responsible for the observed width of the emission band. The mutual intensities of individual modes then determine the position of the maximum of the emission band. At higher \( B \), the relative weight of modes from higher LLs increases, which reflects the distribution of electrons among LLs established by electrical pumping and which leads to a slowing-down of the \( \sqrt{B} \) dependence.

Even though the cyclotron emission observed in the used configuration is primarily due to spontaneous recombination, it is worth to discuss conditions required to obtain stimulated emission and gain. To achieve the light amplification comparable to, e.g., quantum cascade lasers, the gain coefficient has to approach \( g = \Delta n \sigma \sim 10 \text{ cm}^{-1} \), where \( \Delta n \) stands for the population inversion and \( \sigma = \lambda^2/(2\pi) (\tau_{\text{tot}}/\tau_{\text{sp}}) \) is the stimulated emission cross-section. The typical spontaneous cyclotron emission lifetime of massless electrons in the THz range reaches \( \tau_{\text{sp}} \sim 1 \mu s \) and the total lifetime, which dominantly reflects elastic scattering, may be estimated (its lower limit) from the linewidth of the emission line: \( \tau_{\text{tot}} \sim 1 \text{ ps} \). Taking the characteristic wave length of \( \lambda = 300 \mu \text{m} \), we obtain the cross-section \( \sigma \sim 10^{-11} \text{ cm}^{-2} \). This implies the necessity to achieve the population inversion \( \Delta n > 10^{11} \text{ cm}^{-3} \). Our simple estimate, see Supplementary materials, indicates that such a population inversion should be achievable at least in the pulsed mode.

To conclude, we have demonstrated, for the first time, cyclotron emission of massless electrons. This emission was observed in gapless HgCdTe – a system hosting 3D massless Kane electrons. The existence of sizeable cyclotron emission is directly related to their particular Landau level spectrum, which comprises only non-equidistantly spaced levels. The systems hosting massless Kane electrons are thus promising candidates for an active medium of a Landau level laser, which would, in this particular case, operate in the THz and infrared spectral ranges and would be widely tunable by very low magnetic fields.
Methods

Sample growth. The sample was grown using standard molecular-beam epitaxy on a (013)-oriented semi-insulating GaAs substrate. The growth sequence started with ZnTe and CdTe transition regions, followed by the MCT epilayer with gradually changing cadmium content x. The prepared MCT layer contains a region with x ≈ 0.17 of thickness d ≈ 3.2 μm. For more details about the explored sample see Ref. 31.

Pump-probe spectroscopy. The free-electron laser FELBE provided frequency-tunable Fourier-limited radiation pulses. In the experiments described in this paper, photon energies of hω = 61 and 78 meV were chosen. The pulse duration was about 3 ps, the repetition rate was 13 MHz. The pulses were split into pump and probe pulses by a pellicle beam splitter. The polarizations of pump and probe beams were controlled independently. Frequency-tunable quarter-wave plates (from Alphalas GmbH) were used for the generation of circularly polarized radiation. Both the pump and probe beam were focused on the sample in the magnet cryostat by an off-axis parabolic mirror (effective focal length: 178 mm). The spot size on the sample was ∼ 0.5 mm (FWHM). The pump fluence was ∼ 0.5 μJ cm−2, the fluence of the probe beam was about 10% of the pump fluence. The time delay between pump and probe pulses was varied using a mechanical delay stage.

Emission measurements. To measure radiation emitted due to inter-LL recombination of electrons, the radiation was guided, using a copper light pipe, to an InSb photoconductive detector spatially separated from the coil inside which the sample was placed. The used detector has narrow-band (∼ 60 GHz) and field-tunable response due to cyclotron resonance absorption.

This tunability is ensured by a specially dedicated superconducting coil and allows us to analyze the radiation in the spectral range of 0.4-2.5 THz. All emission experiments operated in a pulsed mode (using current pulses for pumping), with the pulse duration of 7 ms and with the peak-to-peak value of electric field up to 12 V/cm. The duty circle was tuned in such a way that the average power consumption of emitter did not exceed 13 mW (to avoid sample heating). The signal on the InSb detector was collected using a conventional lock-in technique.

Additional information

The authors declare no competing financial interests. Correspondence and requests for materials should be addressed to M.O.

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Author contributions

The experiment was proposed by M.O. and M.P. The sample was grown by N.N.M. and S.A.D. Time-resolved and cw magneto-optical experiments were carried out by M.O., M.M., S.W., C.F. and M.H. The cyclotron emission experiments were performed by D.B., C.C., F.T. and W.K. All coauthors discussed the experimental data and interpretation of results. M.O. and M.P. wrote the manuscript, all coauthors commented on it.

Data and code availability

The data that support the findings of this study as well as the code for modelling of cyclotron mode energies are available from the corresponding author on reasonable request.
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See Supplementary materials.