Optimum pole arc offset in permanent magnet synchronous generators for obtaining lowest voltage harmonics

A. Dalcali\textsuperscript{a} and M. Akbaba\textsuperscript{b}

\textit{a. Department of Electrical-Electronics Engineering, Karabük University, 78050, Karabük, Turkey.}
\textit{b. Department of Computer Engineering, Karabük University, 78050, Karabük, Turkey.}

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\begin{abstract}
In this study, the effect of parametric variation of pole arc offset distance on the performance of a Permanent-Magnet Synchronous Generator (PMSG) used in wind energy applications has been investigated. Fourier analyses of the voltage wave-shapes that are obtained by the parametric variation of the pole arc offset value have been made. The THD is determined for each voltage wave-shape. As a result of optimization study, the efficiency and output power have been kept approximately constant. The THD of the output voltage has decreased.
\end{abstract}

\begin{keywords}
Synchronous generator; Pole arc offset; Surface mounted; Voltage wave-shape; THD.
\end{keywords}

1. Introduction

Significant advancement in environmental awareness and rapid decrease in fossil-fuel sources have resulted in the increased use of cheap and environmentally-friendly renewable energy sources [1-3]. Among the renewable energy sources, wind energy takes a vital role in decreasing foreign dependence on energy, improving energy reliability, and solving some of the environmental problems. As such, the use of this component of renewable energy is rapidly increasing as the years pass by [4-9]. Different types of electrical generators used with wind turbines have some advantages and disadvantages over one another. Among them, the use of PMSG is rising rapidly in parallel to the developments in Permanent Magnet (PM) technology [3,10-14].

In synchronous generators, mainly due to the magnetic saturation and spatial configuration of the pole face, the resultant air-gap flux density is not sinusoidal. As a result, the induced voltage is also not sinusoidal [15]. This issue has many disadvantages such as deteriorating the generator performance, causing some undesired effects on customer equipment, and high circulating currents between generators and infinite bus [16,17].

Wang et al. [18], using FEM and analytic techniques, investigated the effect of pole arc to pole pitch ratio on the third harmonic of the back emf of the PM brushless DC motors. It has been proposed that at low-value pole arc to pole pitch ratio, the third harmonic of the back emf remains at the negligible level. However, this adversely affects the voltage THD, which means an increase in the harmonics of other orders, and motor performance. In [19], the effect of magnet shape and dimensions of disc type axial flux machines on the voltage distortion has been investigated. It is proposed that the voltage THD be minimum in the case of circular type magnets. It is also claimed that the
voltage THD is decreasing as the magnet thickness increases. In [20], it is shown that the no-load voltage THD of PM generators used with wind turbines is varying with the slot width and magnet pitch. Kim et al. [21] attempted to optimize the THD of PM generators by parametric variation of the number of poles, slot opening, ratio of pole angle, and pole size. It is pointed out that the pole angle and slot opening can be adjusted in such a way as to avoid 3rd voltage harmonic.

In this study, using FE analysis, design of a 2.5 kW surface-mounted PMSG suitable for use with wind turbines has been realized. Having completed the design phase, using parametric study approach, the pole arc-offset is varied between 0 to 45 mm. The shapes of the phase voltage and air-gap flux density distribution corresponding to each value of the pole arc offset value have been obtained. At the rated load, the Fourier coefficients of the voltage wave-shape have been determined. These are used to obtain THD% of the output voltage. In order to keep the output power approximately constant while varying the pole arc offset, the pole-embrace value has been also changed accordingly. In this investigation, electrical energy generation from small-scale wind turbines is targeted. Therefore, it is necessary to select a low-power and low-speed generators with large number of poles. Accordingly, a surface-mounted inner runner-type PMSG generator has been selected which features 1 pole, 2.5 kW, 120 V, 84 slots.

2. Design of PM synchronous generator

Design of PMSG starts with the following output Eq. (1):

\[ S = 11K_{w1}B_0ac\left(\frac{D}{1000}\right)^2\frac{L}{1000}n. \tag{1} \]

where \( S \) is the generator’s apparent power in VA, \( B_0 \) is specific magnetic loading in T (Wb/m²), \( D \) is the stator outer diameter in mm, \( L \) is the stack length in mm, \( K_{w1} \) is the stator winding factor, \( n \) is the rotor speed in rpm, \( ac \) is the specific electric loading in ampere-turns per meter (At/m); \( ac \) parameter mainly depends on the rated power, frequency, and voltage as expressed in Eq. (2):

\[ ac = \frac{(\delta a_c)Z}{\pi D}. \tag{2} \]

Phase voltages of a PMSG are expressed as given in Eq. (3) [15,22-24]:

\[
\begin{bmatrix}
    v_a \\ v_b \\ v_c
\end{bmatrix} =
\begin{bmatrix}
    R_a & 0 & 0 \\ 0 & R_b & 0 \\ 0 & 0 & R_c
\end{bmatrix}
\begin{bmatrix}
    i_a \\ i_b \\ i_c
\end{bmatrix}
+ 
\begin{bmatrix}
    L_{aa} & L_{ab} & L_{ac} \\ L_{da} & L_{bb} & L_{dc} \\ L_{ea} & L_{eb} & L_{cc}
\end{bmatrix}
\frac{d}{dt}
\begin{bmatrix}
    i_a \\ i_b \\ i_c
\end{bmatrix} +
\begin{bmatrix}
    e_a \\ e_b \\ e_c
\end{bmatrix}. \tag{3}
\]

In terms of magnetic flux-linkages \( \Psi_a, \Psi_b, \) and \( \Psi_c, \) the voltage equation given in Eq. (3) can be re-written in the form of Eq. (4) as follows:

\[
\begin{bmatrix}
    v_a \\ v_b \\ v_c
\end{bmatrix} =
\begin{bmatrix}
    R_a & 0 & 0 \\ 0 & R_b & 0 \\ 0 & 0 & R_c
\end{bmatrix}
\begin{bmatrix}
    i_a \\ i_b \\ i_c
\end{bmatrix}
+ 
\frac{d}{dt}
\begin{bmatrix}
    \Psi_a \\ \Psi_b \\ \Psi_c
\end{bmatrix}. \tag{4}
\]

The remaining mathematical model of the PMSG, not present in this paper, can be found in detail in [24,25]. The generator design parameters are summarized in Table 1.

Figure 1 shows a 3D image of the initial design of a surface-mounted and inner runner configuration.

![Figure 1. 3D model of PMSG: (a) Complete view of the PMSG and (b) part section.](image)

| Parameters          | Values | Parameters          | Values |
|---------------------|--------|---------------------|--------|
| Rated power (kW)    | 2.5    | Stator outer diameter (mm) | 280    |
| Rated speed (rpm)   | 428.5  | Air gap (mm)        | 0.8    |
| Rated voltage (V)   | 120    | Length of stator (mm) | 54     |
| Permanent magnet    | N35    | Pole number          | 14     |
| Stator-rotor material | M470  | Number of slots      | 84     |
PMSG. Figure 1(b) shows the 1/14 part section of the full model used in FEM, which is obtained with the aid of master-slave boundary conditions.

3. Effects of pole arc offset value on the generator design

The pole arc offset can be determined as the distance of the center of the pole arc to the center of the rotor. The pole embrace is defined as the ratio of $\theta_1$ over $\theta_2$. $\theta_2$ is the mechanical angle corresponding to one pole pitch and $\theta_1$ is the angle of one real pole covering one-pole magnet [26,27]. According to the numerically calculated machine design procedure, initial pole arc offset value is defined. Then, the solution range and step size of the pole arc offset are defined. The offset point of the synchronous generator pole arc is initially selected as 0 mm and it is varied up to a maximum value of 45 mm. Figure 2 shows the change in the size of the PM offset points variation. As the offset point value increases, the eccentricity of the tips of PM increases. This leads to a drop in the volume of the PM. As shown in Figure 2, the maximum value of pole arc centre is “45 mm”. This is the limit value and no more offset can be assigned to the defined pole number and outer diameter. At each value of the pole arc, the cogging torque, output power, efficiency, induced torque, and load line voltage are investigated.

In order to obtain the generator’s rated output power and rated voltage, the total ampere-turn value of the field winding is required. It is determined by the combined contributions of ampere-turn of the stator body, stator teeth air gap, pole face, pole body, and rotor center. All of these parts of the generator from the magnetic circuit reluctance, except for the air-gap reluctance, are all non-linear circuit elements [15,16]. At nominal load, the air-gap flux density waveforms of the generator are given in Figure 3 against the varying pole arc offset values.

More sinusoidal air-gap flux density distributions can be obtained by changing the pole arc offset. The nearest sine waveform was achieved when the offset value was set to 45 mm in the analysis. The resulting waveforms can be expressed as Fourier series given in Eq. (5) [28]:

$$B_r(\theta) = A_0 + \sum_{n=1}^{\infty} \left( A_n \cos n\theta + B_n \sin n\theta \right).$$  (5)

where $B_r$ is the radial air-gap flux density, $\theta$ is the space angle in electrical degrees, $n$ is the harmonic number, and $A_n$ and $B_n$ are Fourier coefficients.

The waveform of the voltage induced in the generator windings is a function of the magnetic flux density waveform at the air gap [29]. Therefore, a distorted flux density distribution will lead to a distorted terminal voltage waveform. The simulated induced voltage waveforms at the rated load corresponding to the varying values of the pole arc offset are illustrated in Figure 4. Similar to the air-gap flux density waveform, the best voltage waveform close to a sine wave, is obtained for an offset value of 45 mm.

The magnetic flux density distribution corresponding to 40 mm pole arc offset value is given in Figure 5. It is obtained by using master-slave boundary conditions. Careful observation of this figure reveals that the flux density distribution is convenient as far as the saturation of the used steel-sheets is concerned.

The variation of the efficiency and power of the generator, which is designed for varying pole arc offset values, is shown in Figure 6. It is already mentioned above that it is desired to keep the output power almost constant. To achieve this while varying the pole arc offset value, the pole-embrace value is also varied accordingly. In this process, it is observed that the efficiency of the generator also remains almost constant.

4. Total harmonic distortions value of the induced voltage

In power systems, uninterruptable and high-quality power is always highly demanded. Therefore, for reliable operation of the power systems, it is important to perform the Fourier analysis of the voltage waveform and investigate the harmonics content. The most common way of performing this analysis is to sample the voltage waveform, and then find the average value of each sample [30]. Then, the Fourier coefficients are obtained as given in Eqs. (6) and (7):

$$A_n = \frac{2}{m} \sum_{k=1}^{m} (y_k \times \sin(n \times \theta_k)).$$  (6)

and

$$B_n = \frac{2}{m} \sum_{k=1}^{m} (y_k \times \cos(n \times \theta_k)).$$  (7)

In the above equations, $m$ is the number of samples in one period of the voltage waveform, $\theta_k$. 

![Figure 2. Variation of the parameters of pole arc offset.](image-url)
is the center-point angle of each sample, \(k = 1, 2, \ldots, m\). \(y_k\) is the average value of each voltage waveform sample corresponding to \(\theta_k\), and \(n\) is the harmonic order. Having obtained the Fourier coefficients, the voltage waveform can be expressed as given in Eq. (8) [30]:

\[
V(\theta) = \sqrt{A_1^2 + B_1^2} \sin \left[ \theta + \tan^{-1}\left( \frac{B_1}{A_1} \right) \right] + \cdots + \sqrt{A_n^2 + B_n^2} \sin \left[ \theta + \tan^{-1}\left( \frac{B_n}{A_n} \right) \right].
\] (8)

The variations of the amplitude and phase angle of the harmonics corresponding to the various pole arc offset values are given in Table 2.

Knowing that the total voltage is composed of fundamental component and the harmonics, then it can be re-written in the form of Eq. (9) [31]:

\[
V_s(t) = V_{s1}(t) + \sum_{k=1}^{m} V_{sh}(t).
\] (9)

Here, \(V_s(t)\) is the phase voltage, \(V_{s1}(t)\) is the fundamental component, and \(V_{sh}(t)\) is the harmonic voltage component at \(f_h\) harmonic frequency. The total distortion in voltage waveform \(V_{\text{dis}}(t)\) can be expressed as given in Eq. (10) and it is measured via the concept of percent total harmonic distortion factor (THD%), which is expressed as in Eq. (11):

\[
V_{\text{dis}}(t) = V_s(t) - V_{s1}(t) \sum_{k=1}^{m} V_{sh}(t).
\] (10)

\[
\%\text{THD} = 100 \times \frac{V_{\text{dis}}}{V_{s1}}.
\] (11)

The variation of the voltage THD of the voltage
waveforms given in Figure 3 against the variation of the pole arc offset and embrace values, obtained through Maxwell analysis at the rated load, is given in Table 3. As a result of the Fourier analysis, it is observed that a pole arc offset value of 40 mm appears to be the optimum value. For this value of the pole arc offset, the following performance values are obtained: generator output power of 2454 W, efficiency of 88.24\%, and THD\% of 0.52.
Table 2. Variation of the gain and phase angles of the voltage harmonics against the pole arc offset values.

| Pole arc offset (mm) | The degree of harmonic components (n) | Amplitude of the fundamental and harmonic voltages (V) | Phase angle of the fundamental and harmonic voltages (degrees) |
|---------------------|---------------------------------------|-----------------------------------------------------|--------------------------------------------------------|
|                     | 1 (fundamental)                       | 170.86                                              | -11.63                                                 |
| 0                   | 5                                     | 0.323                                               | 19.76                                                  |
|                     | 7                                     | 0.630                                               | 19.77                                                  |
|                     | 11                                    | 2.523                                               | 3.512                                                  |
| 10                  | 1                                     | 170.207                                             | -11.64                                                 |
|                     | 5                                     | 0.252                                               | 32.15                                                  |
|                     | 7                                     | 0.538                                               | 22.61                                                  |
|                     | 11                                    | 2.554                                               | 3.36                                                   |
| 20                  | 1                                     | 170.608                                             | -11.64                                                 |
|                     | 5                                     | 0.21                                                | 80.44                                                  |
|                     | 7                                     | 0.367                                               | 33.57                                                  |
|                     | 11                                    | 2.639                                               | 3.34                                                   |
| 30                  | 1                                     | 169.79                                              | -11.64                                                 |
|                     | 5                                     | 0.334                                               | 50.59                                                  |
|                     | 7                                     | 0.237                                               | 56.71                                                  |
|                     | 11                                    | 1.93                                                | 4.66                                                   |
| 40                  | 1                                     | 168.55                                              | -11.64                                                 |
|                     | 5                                     | 0.528                                               | -34.21                                                 |
|                     | 7                                     | 0.21                                                | -45.01                                                 |
|                     | 11                                    | 0.502                                               | -28.76                                                 |
| 45                  | 1                                     | 167.376                                             | -11.64                                                 |
|                     | 5                                     | 0.601                                               | -30.99                                                 |
|                     | 7                                     | 0.264                                               | -64.37                                                 |
|                     | 11                                    | 0.419                                               | 21.37                                                  |

Table 3. Variation of % voltage THD with the variation of the pole arc and embrace.

| Offset (mm) | Embrace | THD (%) |
|------------|---------|---------|
| 0          | 0.77    | 1.538   |
| 10         | 0.78    | 1.56    |
| 20         | 0.81    | 1.713   |
| 30         | 0.84    | 1.34    |
| 40         | 0.9     | 0.52    |
| 45         | 0.99    | 0.48    |

5. Conclusion

In this paper, the optimal pole arc offset for PMSG that is expected to have low THD and high efficiency has been investigated. For the optimal design, pole arc offset value was defined as a variable parameter. While obtaining new designs by varying the pole arc offset value, utmost care has been exercised to maintain the generator output power almost constant. For this reason, as the value of the pole arc offset is varied, the embrace value is also varied in order to obtain almost constant output power value. Spatial distribution of the air-gap flux density and shape of the phase voltage, corresponding to the various pole arc offset values, have been obtained. Their Fourier analyses have been made. It is well known that as the spatial distribution of the air-gap flux density approaches to a sine wave, the harmonics of the voltage waveforms reduces. As a result, the overall performance of the generators improves. Reduced generator voltage harmonics also results in the reduced circulation currents between the generator and voltage network. As a result of the performed analyses, a pole arc offset value of 40 mm and a pole embrace value of 0.9 have been identified as highly convenient values. For these values, generator efficiency of 88.24% and THD value of 0.52% have been obtained.
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**Biographies**

**Adem Dalca** was born in Turkey in 1986. He received his MSc degree from the Institute of Science and Technology of Gazi University in 2013. He is currently a Research Assistant in Electrical and Electronics Engineering at Karabük University and also is working towards the PhD degree at the same university. His research interests include CAD of electric machines, numerical analysis of the electromagnetic field in electrical machinery.

**Mehmet Akbaba** received MSc degree in Electrical Engineering from Istanbul Technical University in 1971, and PhD degree in the same field from Strathclyde University, UK, in 1977. From 1978 to 1983, he was with the Electrical and Electronics Engineering Department, Karadeniz Technical University, Turkey, as a Graduate Assistant, Assistant professor (1978) and Associate Professor (1983), respectively. From 1983 to 2012, he was with the Electrical and Computer Engineering Departments, University of Bahrain as an Assistant Professor (1983), Associate Professor (1986) and full Professor (1995) respectively. Currently, he is with the Computer Engineering Department, Karabük University, Turkey. He has published over 70 papers in refereed journals and international conferences. His current research interests include modeling and analysis of electromechanical and photovoltaic systems and power electronics.