Josephson π-state in superconductor-Luttinger liquid hybrid systems

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Josephson current through a Luttinger liquid (LL) under a magnetic field is theoretically studied. We derive an analytical expression of Josephson current for clean interfaces, by using quasiclassical Green’s function and functional bosonization procedure. We show that critical currents can be renormalized by electron-electron interactions at perfect transparency when LL is adiabatically connected with superconductors. We also find that a generation of π-state, due to spin-dependent energy shift in Andreev bound states (ABS), is prohibited even at zero temperature when the strength of repulsive interactions reaches some critical value. The suppression of π-state is caused by the low energy fluctuations propagating in LL, and making the Zeeman splitting in ABS blurred.

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Transport phenomena in one-dimensional (1D) structures are strongly affected by electron-electron interactions. Fermi liquid description breaks down due to electron correlation, and systems are believed to behave as Luttinger liquids (LLs), where low-lying excitations are collective modes rather than single-particle excitations. This gives rise to characteristic phenomena such as spin-charge separation and charge fractionalization. These behaviors have been verified experimentally, e.g., in carbon nanotubes (CNTs) and quantum wires on GaAs/AlGaAs heterostructure. Inspired by advances in microfabrication techniques, hybrid structures connecting LL with other conductors have attracted attentions from theoretical and experimental sides as candidates of new mesoscopic electronic devices.

Recently, superconducting proximity effect on CNTs in contact with superconductors was reported in a couple of experiments. There are some previous works about Josephson currents in superconductor-Luttinger liquid (S-LL) hybrid systems. In such systems, electron-electron interactions modify the normal and the Andreev reflection (AR) process, and lead to unique power law behaviors of low energy properties. Fermi liquid description breaks down due to electron-electron interactions at perfect transparency when LL is adiabatically connected with superconductors. We also find that a generation of π-state, due to spin-dependent energy shift in Andreev bound states (ABS), is prohibited even at zero temperature when the strength of repulsive interactions reaches some critical value. The suppression of π-state is caused by the low energy fluctuations propagating in LL, and making the Zeeman splitting in ABS blurred.

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ity. Throughout this paper, $\hbar$ and $k_B$ are set to unity.

We apply a so-called Hubbard-Stratonovich transformation to the interaction terms \[17\], and obtain the action using auxiliary field $\phi_{a,s}(x,t)$ as follows

$$
S[\phi] = \int dt dx \left[ L_0(\psi^\dagger, \psi) + L_1(\phi) + \sum_{a,s} \phi_{a,s}(x,t) \rho_{a,s}(x,t) \right]. \tag{2}
$$

Here, $L_0$ and $L_1$ are the Lagrangian densities of free fermions and collective fluctuations; they can be expressed in matrix form as

$$
L_0 = [\psi, (i \frac{\partial}{\partial t} + h \epsilon_0 \hat{\tau}_z \hat{\Sigma}_z + h \hat{\tau}_z) \psi],
$$

$$
L_1 = [\phi, \hat{g}^{-1} \phi],
$$

where $\hat{g}$ represents interactions, and

$$
\hat{\tau}_i = \begin{pmatrix} \sigma_i & 0 \\ 0 & \sigma_i \end{pmatrix}, \quad \hat{\Sigma}_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}
$$

with $\sigma_i$ being usual Pauli matrices. Throughout the paper, quantities with gareth denotes $(4 \times 4)$ matrices, and those with boldface $(2 \times 2)$ matrices. 1st and 3rd row correspond to right and left moving electrons with spin up, and 2nd and 4th row to left and right moving holes with spin down. From Eq.(2), one can regard LL as the free fermions propagating in the bosonic “environment” \[13\]. Here the free fermion part includes the role of topological term in usual bosonization method. Therefore, we treat $\phi(x,t)$ as “local scalar potential” for a time, and average it in terms of fluctuation fields. One can obtain quasi-classical Green’s function in LL by solving Eilenberger equation \[19\]

$$
iv_F \frac{\partial}{\partial t} \hat{g}(x,t,t') |\phi\rangle + \left[ (i \frac{\partial}{\partial t} + h \hat{\tau}_z \hat{\Sigma}_z + \phi(x,t) \hat{\Sigma}_z, \hat{g}(x,t,t') |\phi\rangle \right] = 0, \tag{6}
$$

where \([\cdots]\) denotes commutator.

In a similar fashion, one can construct the stationary Green’s functions in S regions \[21\]. Here, it is assumed that the magnetic field is not applied to S region. In Fourier representation with respect of time difference, they are given by

$$
\hat{g}^{L(R)}_s(x, \epsilon) = \hat{U}(\hat{g}_0(\epsilon) + \hat{g}^{L(R)}_s(x, \epsilon))\hat{U}^\dagger, \tag{7}
$$

where $\hat{U} = \exp[i \hat{\tau}_z/4]$. $\hat{g}_0(\epsilon) = (\epsilon \hat{\tau}_z + i \Delta \hat{\tau}_y) / \Omega(\epsilon)$ is the one at far from the interfaces, and

$$
\hat{g}^{L(R)}_s(x, \epsilon) = \hat{C}^{L(R)}_s(\epsilon) e^{\mp 2i \Omega(\epsilon) \frac{\epsilon}{v_F} \frac{L/2}{\epsilon}} \times
\begin{pmatrix}
1 & \mp \alpha(\epsilon)^{\mp 1} \\
-\alpha(\epsilon)^{\mp 1} & 0 \\
0 & 1 \\
-\alpha(\epsilon)^{\mp 1} & -1
\end{pmatrix}, \tag{8}
$$

where $L$ (R) depicts S of left (right) hand side. Here, $\Omega(\epsilon) = \sqrt{\epsilon^2 - \Delta^2}$ and $\alpha(\epsilon) = \Delta(\epsilon + \Omega(\epsilon))$. One can see that $\alpha(\epsilon)$ is equal to the AR amplitude for interfaces with non-interacting normal conductor. We determine coefficients $\hat{C}^{L(R)}_s(\epsilon)$ by applying boundary conditions at the interfaces $x = \pm L/2$. Since we focus on the junction with clean interfaces, the boundary conditions are that they are continuous along a trajectory, i.e., $\hat{g}(\pm \frac{L}{2}, 0, t, t' |\phi\rangle = \hat{g}(\pm \frac{L}{2}, 0, t, t' |\phi\rangle \tag{21}$.

If $L$ is larger than coherence length $\xi = v_F / \pi \Delta$, we find that ABS has the following form

$$
E^{(n)}_{a,s} = \frac{v_F}{2L} \left[ (2n + 1) \pi + a \chi - s \gamma - \Phi_{a,s} \right]
$$

$$
= \epsilon_{n,s} - \frac{v_F}{2L} [a \chi + \Phi_{a,s}], \tag{9}
$$

where $n$ is an integer, and $\gamma = 2Lh / v_F$ (mod $2\pi$) is phase shift due to the magnetic field. Here, the influence of the auxiliary field appears as a small energy shift and is

$$
\Phi_{a,s} = \theta_{a,s}(\frac{L}{2}, t) + \theta_{a,-s}(\frac{L}{2}, t) - (\frac{L}{2} \rightarrow - \frac{L}{2}), \tag{10}
$$

with $\theta$’s being “gauge” fields in terms of the fluctuations defined by $(\partial_t + a v_F \partial_x) \theta_{a,s}(x, t) = \phi_{a,s}(x, t) \tag{18} \tag{22}$. To evaluate the effect of $\Phi_{a,s}$ to the Josephson current, we have to average the Green’s function in terms of auxiliary $\phi$ fields; $\langle \hat{g}(x, t, t') \hat{g}(x, t, t') \rangle >_\phi$, where

$$
< \cdots >_\phi = \frac{\int \prod_{a,s} D\phi_{a,s} \cdots e^{i S_{\text{ind}}[\phi]}}{\int \prod_{a,s} D\phi_{a,s} e^{i S_{\text{ind}}[\phi]}}. \tag{11}
$$

Here, $S_{\text{ind}} = \int dt dx L_1$ is the action for the fluctuations induced by the interactions and forms a gaussian in terms of $\theta$ fields. Considering that spin-charge separation is still valid, $S_{\text{ind}}$ has the following form after unitary transformation \[18\]

$$
S_{\text{ind}} = \frac{i}{2} [\theta, M \theta], \quad M = \begin{pmatrix} M_p & 0 \\ 0 & M_s \end{pmatrix}, \tag{12}
$$

where $j = \{\rho, \sigma\}$ specifies charge wave or spin wave fluctuations. One see that $M$ corresponds to the inverse of Green’s function of the fluctuations. Josephson current with s-wave symmetry is related only to charge bosons of the charge waves (i.e. $\theta_{\rho,c} = \sum_{a,s} \theta_{a,s}/2$) and phase bosons of the spin waves (where $\theta_{\sigma,p} = -\sum_{a,s} a s \theta_{a,s}/2) \tag{3}$. Thus, it is sufficient to have the knowledge of the propagators of these components. The concrete forms in Fourier representation are

$$
M^{-1}_{\rho,c}(k, \omega) = i \pi \left[ \frac{v_F K_{\rho,c}^{-1} - 2}{\omega^2 - v_F^2 k^2} + D_0^\rho(k, \omega) \right], \tag{13}
$$

$$
M^{-1}_{\sigma,p}(k, \omega) = i \pi \left[ \frac{v_F K_{\sigma,p} - 2}{\omega^2 - v_F^2 k^2} + D_0^\sigma(k, \omega) \right], \tag{14}
$$

where

$$
D_0^\rho(k, \omega) = (v_j - v_F) \left[ \frac{\omega^2 + v_F v_j k^2}{(\omega^2 - v_F^2 k^2)(\omega^2 - v_F^2 k^2)} \right]. \tag{15}
$$


Here, $K_j$ and $v_j = u_jv_F$ are usual Luttinger parameter and propagation velocity of $j$ component.

Total Josephson current through the system can be obtained, summing up the contributions from all the ABSs. Because of the spin-charge separation, renormalization of the spin-up current and the spin-down one is exactly the same. Here we assume that excitation momentum unit of electron-electron interactions is included only in $\Upsilon$, and $\Upsilon$ obtained, summing up the contributions from all the ABSs.

Because of the spin-charge separation, renormalization of the “environment” at the interfaces directly affect the AR. Note that the exponent of renormalization differs from the one due to normal backscattering, e.g., at high barrier potential $\alpha (\pi T/D)^{K_{\rho}^{-1} + K_{\rho}^{-2}}$. Therefore, we consider that it is Cooper pair tunneling process that the interactions renormalize. To see this explicitly, we utilize conventional tunnel Hamiltonian $H_T = \sum_{a,s} (T_1 \Psi_{a,s}(-\frac{L}{2}) \Psi_{a,s}(\frac{L}{2}) + T_2 \Psi_{a,s}(\frac{L}{2}) \Psi_{a,s}(-\frac{L}{2}) + H.c.)$

with $\Psi_{a,s}(x)$ and $\tilde{\Psi}_{a,s}(x) = e^{i(a_k x + \theta_{a,s})}$ being annihilation operators in S and LL. At zero temperature, the second order perturbation of $H_T$ at each interface, which corresponds to single AR process, is proportional to

$$\int dt < e^{i(\theta_{\uparrow - 1}(\frac{L}{2}, t) + \theta_{\uparrow - 1}(\frac{L}{2}, t) - \theta_{\uparrow + 1}(\frac{L}{2}, t))} >_0 \propto (\frac{v_F}{D})^{K_{\rho}^{-1} + K_{\rho}^{-2}} \Upsilon (T \to 0).$$

This is in agreement with the result of Fazio et al. [4]. One can verify that higher order contributions are consistent with Eq.(16) as far as the power law dependence is concerned [13].

Current-phase relations for different values of $K_{\rho}$ are shown in Fig. 2 (Hereafter, we employ the parameters, such as $\Delta$ and $L$, modeling the experiment by Kasumov et al. [5]). Owing to the Zeeman phase shift $\gamma$, the positive slopes are found to appear at $\chi = \pi$ ($\pi$-state). This is the same result as in S-F junction except the suppression (enhancement) by the repulsive (attractive) interactions [13]. However, the suppression by the repulsive interactions ($K_{\rho} < 1$) can play a key role as for the generation of $\pi$-state. We calculate the temperature dependence of the sub-critical current $J_{\pi}$ which provides an indication of the existence of the $\pi$-state (see Fig. 3). In presence of the repulsive interactions, there is the regime for finite $\gamma$ where the $\pi$-state does not occur even at absolute zero, although finite Josephson current can flow. The condition for the existence of a $\pi$-state is given by

$$\Lambda = - \sum_{m=1}^{\infty} \cos(m\chi) (\frac{v_F}{D})^{(K_{\rho}^{-1} + K_{\rho}^{-2}) m^2} > 0.$$ (19)

In non-interacting case ($K_{\rho} = K_{\sigma} = 1$), $\Lambda = 0.5$ for finite $\gamma$. In contrast, if the Coulomb interactions are strong enough ($K_{\rho} \lesssim 0.2$) as in CNTs [2], the metastable $\pi$-state cannot be generated as such.
This behavior can be verified also from Josephson potential $E_J(\chi, \gamma)$. As a criterion for determining the existence of the metastable state, we estimate the transmissivity $T_\pi$ from the bottom of the $\pi$-state. $T_\pi$ is numerically calculated as a function of $K_\rho$ and $K_\sigma$ within WKB method, and the result is shown in Fig. 4. One can see that there is a critical value of interaction strength, where $T_\pi$ reaches unity and the generation of $\pi$-state is prohibited completely. In the vicinity of the critical point, the tunneling probability becomes

$$T_\pi \sim 1 - \left( \frac{\pi^3}{2} \right)^{\frac{1}{2}} \sqrt{\frac{C \nu_F}{\pi^2 L \Lambda}},$$

(20)

where $C$ denotes junction capacitance. The disappearance of the metastable state is caused by the fact that the Zeeman splitting in ABSSs becomes blurred due to the collective excitations arising from the interactions in LL.

In practice, for repulsive interactions, the LDOS near the interfaces can be roughly estimated by

with the exponents $\zeta_j = (K_j^{-1} + K_j - 2)/4$ and $\eta = (K_\rho^{-1} + K_\sigma - 2)/4$. Here $\delta$ is the finite spectral weight of each ABSS and $\Gamma(x)$ is Gamma function. We further fix the phase difference $\chi$ between the superconductors to zero for simplicity [12]. The first term in right hand side show that the spectral weight is spread out through distribution function. In this light, the repulsive interactions can be interpreted to raise the effective temperature of the junction system. In the second one, which originates in $\Phi_{n,s}$ of Eq.(10), the repulsive interactions suppress the Andreev resonance. For attractive case ($K_\rho > 1$), on the other hand, it becomes easier to generate the metastable state. An attractive back-scattering, in general, cannot be neglected. However, it does not change the situation qualitatively; because the attractive back-scattering tends to enhance the superconducting correlation [22]. Besides, in contrast to $K_\rho$, small $K_\sigma$ enhances the critical current, and makes the $\pi$-state incident. This reveals a reflection of the symmetry of Cooper pairs in superconductors.

Finally, we mention the effect of breakdown of spin-charge separation due to the Zeeman effect. We have focused on the case where spin-charge separation is valid. This assumption may be acceptable for the system on electron doped GaAs which has small Lande’s g-factor ($\sim -0.4$) [4]. If, e.g., InSb quantum wires ($g \sim -50$ [24]) are prepared, however, our approach needs some corrections. In such a case, the charge- and spin-density fluctuations exhibit coupled oscillation, whose coupling strength is proportional to $r = (v_{F\uparrow} - v_{F\downarrow})/(v_{F\uparrow} + v_{F\downarrow})$. Therefore, $M$ in Eq.(12) has off-diagonal elements. This leads to different renormalization for spin-up and spin-down currents, and the ratio of renormalization factor has the following expression

$$\frac{Y_\uparrow}{Y_\downarrow} = \left[ \sinh \left( \frac{L}{2u_{\uparrow}-L_T} \right) / \sinh \left( \frac{L}{2u_{\downarrow}+L_T} \right) \right]^{4r(u_\rho K_\rho^{-1} + u_\sigma K_\sigma^{-1})/u_\downarrow^2} \times \left[ \sinh \left( \frac{L}{2(1+r)L_T} \right) / \sinh \left( \frac{L}{2(1-r)L_T} \right) \right]^2,$$

(22)

where $u_\downarrow$ denotes velocity renormalization of the normal mode [14]; the explicit form is given by

$$u_\downarrow^2 = \frac{1}{2} \left[ (u_\rho^2 + u_\sigma^2 + 2r^2) \pm \sqrt{(u_\rho^2 - u_\sigma^2)^2 + 4r^2(u_\rho K_\rho^0 + u_\sigma K_\sigma^0)(u_\rho K_\rho^{-1} + u_\sigma K_\sigma^{-1})} \right].$$

(23)
is the action of symmetric potential \( \Upsilon \). This indicates that the macroscopic nature is inevitably related with many body correlations in 1D configuration. Our method can be easily applied to hybrid systems of superconductors with other symmetries or interacting conductor with higher dimensions \([21, 29]\). Experimentally in semiconducting heterostructure, one can vary the carrier density and the effective interactions to some extent by gate voltage \([30]\). Further tunnel junctions between 1D-2DEG have been also examined \([31]\). It may be feasible in the future to construct the system under consideration, using S-2DEG-S junction with a gate \([32]\).

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