Feature point matching for camera localization suffers from scalability problems. Even when feature descriptors associated with 3D scene points are locally unique, as coverage grows, similar or repeated features become increasingly common. As a result, the standard distance ratio-test used to identify reliable image feature points is overly restrictive and rejects many good candidate matches. We propose a simple coarse-to-fine strategy that uses conservative approximations to robust local ratio-tests that can be computed efficiently using global approximate k-nearest neighbor search. We treat these forward matches as votes in camera pose space and use them to prioritize back-matching within candidate camera pose clusters, exploiting feature co-visibility captured by clustering the 3D model camera pose graph. This approach achieves state-of-the-art camera localization results on a variety of popular benchmarks, outperforming several methods that use more complicated data structures and that make more restrictive assumptions on camera pose. We also carry out diagnostic analyses on a difficult test dataset containing globally repetitive structure that suggest our approach successfully adapts to the challenges of large-scale image localization.

1. Introduction

In this paper we consider the problem of estimating the full 6DOF camera pose of a query image with respect to a large-scale 3D model such as those obtained from a Structure-from-Motion (SfM) pipeline [25, 32, 15, 23]. A typical approach is to detect distinctive 2D feature points in a query image and perform correspondence search against feature descriptors associated with 3D points obtained from the SfM reconstruction. This initial matching is performed in descriptor space (e.g., SIFT [13] or SURF [3]) using an approximate k-nearest neighbor search implementation [16, 17]. Candidate 2D-3D correspondences are then further filtered using robust fitting techniques (e.g., RANSAC variants [9, 30, 14]) to identify inliers and the final camera pose estimated using an algebraic PnP solver and non-linear refinement. Camera localization is a fundamental building block in many computer vision algorithms (e.g., incremental bundle adjustment), can provide strong constraints on object recognition (see e.g., [31, 7]), and is useful in robotics applications such as autonomous driving and navigation.

Unfortunately, the performance of standard camera localization pipelines degrades as the size of the 3D model grows. Finding good correspondences becomes difficult in the large-scale setting due to two factors. First, standard 2D-to-3D forward matching is likely to accept bad correspondences of a query feature with the model since the feature space becomes cluttered with similar descriptors from completely different locations. Standard heuristics for identifying distinctive matches, such as the distance ratio-test of Lowe [13], which compares the distance to the nearest-neighbor point descriptor with that of the second-nearest neighbor, fail due to proximity of other model feature descriptors. Second, increasingly noisy correspondences obtained from the matching stage drives up the runtime of the robust pose estimation step, whose complexity typically grows exponentially with the number of outliers. These difficulties are particularly evident in large urban environments, where repeated structure is common and local features become less distinctive [29, 1].

Related Work: These problems are well known and have been approached in several ways in the literature. Works such as [12, 11] focus on generating a simplified 3D model that contains only a representative subset of distinctive model points, yielding faster localizations. With a smaller model and prioritized search, it becomes possible to replace the traditional approach of 2D-to-3D forward matching, with 3D-to-2D back matching, allowing the ratio test to be performed in the query image’s sparser feature space.

An alternative to removing points from the model is to cluster and quantize model points in the feature descriptor space. [19] use vocabulary trees to speed up forward matching by assigning each model point and each query feature to a vocabulary word, yielding faster runtimes since the vo-
Prioritized Back Matching
Cluster-Wise Ratio Test
3D points
Camera clustering
Cluster Voting
\([R, t]\)
PnP Solver
SfM Model
Multiple NN Matching

Figure 1. Overview of our camera localization pipeline. We exploit multiple nearest neighbor search and leverage camera pose clustering to identify potential landmarks where the query image was taken. The red colored boxes denote the steps defined in Section 2. We explore cluster co-visibility to prioritize back matching of model features. This strategy, shown in the blue boxes, is explained in Section 3.

cabulary used is generally smaller than the size of the model point cloud. A linear search for the first and second nearest neighbors is performed within each word bin, and a ratio test filters out non-distinct correspondences. Additionally, [20] use active search in the vocabulary tree to prioritize back matching of 3D points close to those that have already been found and terminate early as soon as a sufficient number of matches have been identified.

A very different approach is taken in the works of [34, 27]. Camera localization is framed as a Hough voting procedure, where the geometric properties of SIFT features (scale and orientation) provide approximate information about likely camera pose from individual point correspondences. By utilizing focal length and camera orientation priors, each 2D-to-3D match casts a vote into the intersection of a visibility cone and a hypothesized ground-plane. Orientation and model co-visibility are further used to filter out unlikely matches, rapidly identifying the potential camera locations.

Our Contribution: Inspired by this prior work, we propose a fast, simple method for camera localization that scales well to large models with globally repeated structure. Our approach avoids complicated data structures and makes no hard a priori assumptions on camera pose (e.g., gravity direction of the camera). Our basic insight is to utilize a coarse-to-fine approach that rapidly narrows down the region of camera pose space associated with the query image. Specifically, we formulate a linear time voting process over camera pose bins defined by clustering the camera-model pose graph of the SfM model we are matching against. This voting serves to identify model views likely to overlap the query image and allows us to prioritize back matching of those views to the query image while exploiting co-visibility constraints and local ratio testing.

Figure 1 gives an overview of our pipeline. Our first contribution (Section 2) is to introduce and analyze two ratio-tests that can be used to find distinctive matches in a pool of candidates produced by global k-nearest neighbor search (kNN). Our second contribution (Section 3) uses these forward matches as votes to prioritize back matching of model images against the query image. Extensive experimental evaluation (Section 4) suggests this approach scales well and outperforms existing methods on several benchmark datasets.

2. Ratio Tests for Global Matching

Forward-matching of query image points against a model is effective when the model is small. In such models, approximate nearest-neighbors are often true correspondences and ratio-testing is effective at discarding bad matches. In this section we first establish that clustering the model and performing forward-matching within each cluster is sufficient to recover this good performance for large models (Section 2.1). We then describe how to approximate exhaustive cluster-wise matching by global forward-matching using approximations to the local ratio test (Section 2.2) followed by back-matching.

2.1. Clustering and Exhaustive Local Matching

A naive approach to solving camera localization at large scale is to simply divide the 3D model into clusters and perform matching and robust PnP pose estimation for each cluster. This avoids the problems of global repetition and difficulties of high density in the feature space. However, this is largely impractical from a computation point of view: we need to build an approximate nearest-neighbor data structure for each cluster and match to each cluster separately at test time. Consider a kd-tree, where searching for a match in a set with \(N\) descriptors is logarithmic in the set size: \(O(\log(N))\). If we divide the model into \(|C| = N/S\) clusters of constant size \(S\), execution time is dominated by the number of clusters which grows linearly in the model size, \(O(|C|\log(N/S)) = O(N/S\log(S)) > O(\log(N))\). While not practical at scale, we take this exhaustive local match-
Table 1. Quantitative results on the Eng-Quad dataset using a standard localization framework applied to model clusters. Performing localization separately in each cluster improves the number of localized cameras and the median error localization accuracy. This improvement comes at the expense of runtime due to exhaustive local matching.

| #clusters | #images | #inliers | ratio | error [m] | Fwd [s] | RNSC [s] | total [s] |
|-----------|---------|----------|-------|-----------|---------|----------|----------|
| 1 (global)| 517     | 51       | 0.29  | 80.23     | 523.69  | 56.82    | 603.52   |
| 50        | 512     | 66       | 0.54  | 0.45      | 12.10   | 43.92    | 56.22    |
| 500       | 517     | 51       | 0.49  | 29.20     | 80.23   | 523.69   | 603.52   |

Local Matching is Effective: To evaluate clustering and local matching, we use the Eng-Quad dataset from [8], and build two SfM models using COLMAP [23]. The first model contains only the training image set, while a second model bundles both the training and test images and is used for evaluating localization accuracy. We geo-registered the resulting reconstructions with a GIS model provided by the authors, so that the scale of the SfM model is approximately metric. 5129 training images of the 6402 were bundled, and 520 out of 570 test images were additionally bundled in the test model. The resulting point cloud has 579,859 3D points and 2,901,885 observations. We refer to these multiple observations as views of the point.

We construct a scene matrix $S$ whose $(i, j)$ entry contains the number of points that image pair $I_i, I_j$ share in the SfM model. We performed spectral clustering [2-4] on the scene matrix using the 50 largest eigenvectors and produce three different granularities: no clustering at all (purely global), 50 clusters, and 500 clusters. For exhaustive local matching, we matched a query image against every cluster and select the one that produces the smallest localization error. For matching to a cluster, we use FLANN [17] to find the first and second NN of each query point and apply a standard ratio test with a $\tau = 0.7$ threshold. We ran RANSAC on each set of candidate cluster correspondences using a P3P solver [10] and a focal length prior based on the image EXIF metadata. Similar to [12], an image is considered to be successfully matched if it has at least 12 inlier correspondences with a reprojection error less than $\epsilon = 6$px.

As Table 1 shows, exhaustive local matching (within each cluster) performs well relative to global matching, with lower median error and fewer failures. However, the execution time grows roughly linearly with respect to the number of clusters, motivating our coarse-to-fine strategy.

2.2. Local Ratio Tests for Global Matches

How can we get the benefits of local cluster-wise matching while maintaining the computational cost associated with a single global nearest-neighbor search? Cluster-wise matching considers a nearest-neighbor per-cluster for each query point. To try and recover this larger pool of candidate correspondences from global search, we propose to retrieve the global top k nearest-neighbors for each query point. Fortunately, approximate kNN searches are not substantially more costly since those points typically live in adjacent leaves of the kd-tree (which must be explored even for a 1-NN retrieval). A larger set of candidate matches can address the problem of repeated structure by retrieving the set of multiple scene points that might correspond to a query point. However, it also results in a k-fold increase in outliers which we now address.

We define a view $v \in V$ as the 2D point observation of a 3D point $p \in P$ in a particular model image $I \in \mathcal{I}$. Given a camera pose clustering $C$ of the SfM model images, we assign the view descriptors of each image to their corresponding cluster $c \in C$. Note that these clusters divide images in disjoint groups, but they do share common points, as a 3D point can have multiple views belonging to images assigned to different clusters. For a query image $I$ with query...
features $Q$, we search for $k$ approximate nearest neighbors using a global kd-tree structure built from all model views $V$.

**Global $k$-ratio tests:** We start with a conservative global ratio-test (Algorithm 1) to prune candidate matches by comparing the distance ratio of the first and $k + 1$ nearest neighbors retrieved, as proposed by [33]. If the ratio is greater than threshold $\tau$, we drop the query point. Otherwise, all $k$ nearest neighbors pairs $\{(q, v_1), \ldots, (q, v_k)\}$ are included in the set of putative correspondences $M$. This global ratio test is much more conservative than the standard first vs second NN test. In the remainder of this paper, we will refer to this global test as $k$-ratio, defined formally as $\frac{\|q - v_1\|}{\|q - v_k\|} \leq \tau$. The standard first versus second NN test will be referred as $l$-ratio.

**Lemma 1.** If a candidate match fails the global $k$-ratio test, it also fails the local $l$-ratio test.

**Proof.** Let $\{v_{c1}, v_{c2}\} \subseteq \{v_1, \ldots, v_k\}$ be the first and second local nearest neighbors of a particular query feature $q$. Since the global set $\{v_1, \ldots, v_k\}$ is sorted by ascending distance, this implies that $\|q - v_{c2}\| \leq \|q - v_{k+1}\|$, and $\|q - v_{c1}\| \geq \|q - v_1\|$. Formally,

\[
\frac{\|q - v_{c1}\|}{\|q - v_{c2}\|} \geq \frac{\|q - v_{c1}\|}{\|q - v_{k+1}\|} \geq \frac{\|q - v_1\|}{\|q - v_{k+1}\|} \leq \tau
\]

Hence, the local 1-ratio will always be equal or greater than the global $k$-ratio. This guarantees that any correspondence rejected by the $k$-ratio test would also have failed the local 1-ratio test. A correspondence passing the $k$-ratio test might not pass the local 1-ratio test, so the local 1-ratio test is a more stringent criteria.

**Cluster-wise ratio tests:** After the initial global filtering, we would now like to perform local ratio testing within each cluster. When more than two candidate matches for a query point belong to the same cluster, we can simply re-rank them and apply a standard 1-ratio test. For example, suppose two global matches $(q, v_2)$ and $(q, v_3)$ which are the second and fourth global NN of the query feature $q$ fall in the same cluster. If $v_2$ and $v_3$ are view of distinct 3D points, then they are necessarily the first $(q, v_{c1})$ and second $(q, v_{c2})$ local nearest-neighbors of $q$ in that cluster (see Figure 2). Any lower ranked matches within the cluster can be ignored and the 1-ratio test applied to this pair.

In some cases, only a single global match falls within a cluster. While this match passed the global k-ratio, it still may not be locally discriminative and we can no longer perform an exact local 1-ratio test since we don’t have immediate access to the 2nd nearest neighbor within that cluster. Instead we develop a bound based on the triangle inequality to define an alternate test for such cases which we refer to as the $t$-ratio test.

Given a local correspondence $v_{c1} \in c$, we define $v_{NN} = kNN(v_{c1}, c, 1)$ as the nearest neighbor of view $v_{c1}$ in the feature space defined by cluster $c$. Since $v_{NN}$ is obtained purely from training data, we can pre-compute it offline and access it at test time. We define the $t$-ratio test as:

\[
\frac{\|q - v_{c1}\|}{\|q - v_{c2}\|} + \frac{\|v_{c1} - v_{NN}\|}{\|q - v_{NN}\|} \leq \tau
\]

Although we missed the local 2nd nearest neighbor in the global search, the distance $\|v_{c1} - v_{NN}\|$ provides useful information on how far away the 2nd nearest neighbor might be.

**Lemma 2.** If a candidate match fails the $t$-ratio test, it also fails the local 1-ratio test.

**Proof.** Let $q$ be a query feature, $v_{c1}$ and $v_{c2}$ the first and second local nearest neighbors in a cluster $c$, and $v_{NN} = kNN(v_{c1}, c, 1)$. We can bound the distance to the second nearest neighbor by the inequalities:

\[
\|q - v_{c2}\| \leq \|q - v_{NN}\| \leq \|q - v_{c1}\| + \|v_{c1} - v_{NN}\|
\]

where the first inequality holds since $\|q - v_{c2}\| \leq \|q - v\| \forall v \in c \setminus v_{c1}$, and the second holds by the triangle inequality. Thus,

\[
\frac{\|q - v_{c1}\|}{\|q - v_{c2}\|} \geq \frac{\|q - v_{c1}\|}{\|q - v_{c1}\| + \|v_{c1} - v_{NN}\|}
\]

Consequently, a singleton match that fails the $t$-ratio test will always fail the local 1-ratio test. The $t$-ratio test thus only filters correspondences that would have failed the local ratio test if $v_{c2}$ was available.

**Back matching and fitting:** To provide additional robustness to outliers, we can back match views (model feature point descriptors) which were indicated as candidate correspondences from the forward matching. For any such candidate matching view, we search for the first and second nearest neighbor matches using a kd-tree built over the query image features and apply the 1-ratio test. We then select as the final set of correspondences the intersection of pairs $(q, v)$ that passed the forward and back matching process. This implies that these pairs are best buddies [6], since each $q$ and $v$ of a pair are both discriminative features in the query and model feature space.

**2.3. Cluster-wise ratio-tests are effective**

The cluster-wise ratio test, defined in Algorithm 2, prunes a large number of non-discriminative correspondences while still maintaining the locally unique matches.
Algorithm 2 Cluster-Wise Ratio Test

INPUT: matches \( \mathcal{M} \), clusters \( \mathcal{C} \), threshold \( \tau \)

\( \mathcal{M}_F = \emptyset \)

for \( c \in \mathcal{C} \) do

for \((q, v_{c_1}) \in \mathcal{M} \) with \( v_{c_1} \in c \) do

if \((q, v_{c_2}) \in \mathcal{M} \) with \( v_{c_2} \in c \) then

\[ \alpha(q, c) = \frac{|q-v_{c_1}|}{|q-v_{c_2}|} \]  

\( \triangleright \) local 1-ratio test

else

\[ v_{NN} = kNN(v_{c_1}, c, 1) \]

\[ \alpha(q, c) = \frac{|q-v_{c_1}|}{|q-v_{NN}|} \]  

\( \triangleright \) t-ratio test

end if

if \( \alpha(q, c) \leq \tau \) then

\( \mathcal{M}_F = \mathcal{M}_F \cup (q, v_{c_1}) \)

end if

end for

end for

return \( \mathcal{M}_F \)

| #clusters | #images | #nn | ratio | err. | #v | | | RNNSC | total | total |
|-----------|---------|-----|------|-----|---|---|---|------|------|
| 1         | 481.00  | 1.15 | 0.73 | 0.09 | 0.006 | 0.008 | 0.032 | 0.013 | 0.046 | 0.039 |
| 50        | 477.00  | 0.59 | 0.66 | 0.024 | 0.008 | 0.009 | 0.015 | 0.014 | 0.061 | 0.015 |
| 500       | 480.00  | 0.63 | 0.61 | 0.024 | 0.008 | 0.009 | 0.015 | 0.014 | 0.061 | 0.015 |
| 5129      | 482.00  | 1.36 | 0.55 | 0.008 | 0.009 | 0.009 | 0.008 | 0.009 | 0.070 | 0.061 |

Table 2. Quantitative results on the 520 test image set using the proposed localization framework of algorithm 2 and best-buddy filtering. We used 5 nearest neighbors in the k-NN search. We evaluated four spatial subdivisions, including a finest clustering in which each camera in the model is considered a single cluster. Localization accuracy is competitive with exhaustive local matching with achieving runtimes comparable to global matching.

The complexity of this algorithm is linear in the number of forward correspondences \( N_F \). For every local NN \( v_{c_2} \), we simply look for its second NN pair \( v_{c_1} \) within the list of \( k \) nearest neighbors. The list of intra-cluster nearest neighbors \( v_{NN} \) can be pre-computed offline and accessed at constant time. Hence, at most \( N_F \) ratio tests will be performed.

We evaluated this cluster-wise approach using the same settings as our gold standard baseline experiment. We added a finer division of the model, consisting on atomic clusters of a single image each. Table 2 shows the localization performance on these different granularities. A single global cluster gives surprisingly good results in the number of localized cameras, although it provides worse camera position results. This is due to the restrictiveness of the ratio test in denser search spaces, yielding fewer inliers and missing some discriminative correspondences that would improve results. As we increase the number of clusters, the localization errors are reduced (8 cm on average) thanks to the cluster-wise ratio test which provides more high confidence matches (at the expense of longer RANSAC runtimes). We obtain best results using the finest clustering (a single model camera per cluster), successfully localizing 482 images. Compared to the gold standard of exhaustive local matching (Table 1), our localization results are competitive. More cameras are successfully localized by exhaustive local matching but our approximate strategy is three orders of magnitude faster. Finally, we note that in this setting the forward matching (against a few million descriptors) now constitutes the main speed bottleneck, a problem we address in the next section.

3. Accelerating Matching by Pose Voting

Short of simplifying the model (e.g., as pursued by [11, 12]), how might we further accelerate the matching process? A natural strategy is to carry out forward matching incrementally and stop as soon as we have a sufficient number of matches to guarantee a good result. From this perspective, we can view forward matching as “voting” for the location of the query camera. Unlike [34, 27] where votes were cast into a uniformly binned camera translation space, our bins are adaptively determined by the clustering of the model camera pose graph. Once we have accumulated enough votes to narrow down the camera pose to one of a few clusters, we can terminate forward matching and carry out back matching with little loss in accuracy.

3.1. Location recognition using cluster-wise forward matching

To analyze how many votes are needed to determine the correct cluster, we frame the problem as that of location recognition [18, 28, 2, 22], namely producing a short ranked list of model images that depict the same landmarks as the query image (e.g., same buildings, statues, etc.).

Using the finest granularity clustering (1 image per cluster), which provided the most discriminative correspondences in Section 2.3, we rank the model images in order of the number of votes (count of matches that passed the cluster-wise ratio test). We follow the evaluation procedure of [5], reporting if there exists at least one image among the top-\( k \) images that shares 12 or more fundamental matrix inliers. We benchmark performance on two different datasets: Eng-Quad and Dubrovnik [12].

The results in Table 3 are inspiring. Algorithm 2 is able to recognize the location of all 800 test images in the Dubrovnik dataset using 200 random features passing the k-ratio test. Results on the more challenging Eng-Quad dataset provide almost 92% accuracy on recognizing the landmarks of the 520 query images for which we have a ground truth pose. It is also interesting to see that a random subset of a few hundred query features achieves nearly as good recognition results as using all image features (a query image usually has 5,000 to 10,000 features). This suggests that the forward matching can be made significantly faster while still maintaining good recognition performance.
3.2. Prioritized Back Matching

Determining the correct cluster or identifying a model image (location recognition) is not the same as camera localization and additional matches are likely needed to estimate the final camera pose using a PnP solver and nonlinear refinement. To reap the speed benefits of subsampling, we thus modify our framework slightly. We use forward matching with a subset of \( N_F \) query features in order to identify likely pose clusters. We then perform back matching within candidate pose clusters in order to find a larger set of matches used for fine camera pose estimation. This back matching is carried out using a greedy prioritized search over clusters ranked by votes and further exploits co-visibility information encoded in the SfM model to find additional distinctive matches that were not identified during the forward (sub-sampled) matching.

Algorithm 3 describes our greedy approach. Given the set of forward matches found using 2, we start by selecting the most voted cluster (or model image) \( c^* \) and back-matching all of its views against the query image using the standard 1-ratio test with threshold \( \tau \). The correspondences \( M_{c^*} \) found are added to the pool of back matched pairs \( M_B \) used for the fine pose estimation. These back matches are also treated as votes. We use the SfM model’s camera-point visibility graph \( G \), to cast votes for other images that observe the same views as in \( M_{c^*} \). These new votes increase the likelihood of neighboring clusters to be selected for subsequent rounds of back-matching. To avoid introducing noise into the voting process, we only allow a back-matched image to cast votes if it returns 12 or more matches. The algorithm terminates when \( M_B \) is sufficiently large to guarantee a good camera localization, or a certain total number of clusters have been back-matched.

### Algorithm 3 Prioritized Back Matching

**INPUT:** forward matches \( M_F \), clustering \( C \), query features \( Q \), threshold \( \tau \), minimum number of matches \( N_B \), scene graph \( G \)

\( H = \{ (q,v) \in M_F : v \in c \} \quad \forall c \)

\( \Rightarrow \) Cast votes

\( M_B = \emptyset, \quad V_C = \emptyset \)

while \((|M_B| < N_B) \land (|V_C| \leq 20)\) do

\( c^* = \arg\max_{c \in V_C} H \)

\( \forall v \in c^* \) do

\( q_1, q_2 = kNN(v, Q, 2) \)

\( c_v = \frac{1}{|v−q_1|} \cdot \frac{1}{|v−q_2|} \)

if \( \alpha_v \leq \tau \) then

\( M_{c^*} = M_{c^*} \cup (q_1, v) \)

end if

end for

\( M_B = M_B \cup M_{c^*} \)

if \( |M_{c^*}| \geq 12 \) then

\( \forall (q,v) \in M_{c^*} \) do

\( \forall c' \in C \) with \( v \in c' \) do

\( H_{c'} = H_{c'} + 1 \)

end for

end for

end if

\( V_C = V_C \cup c^* \)

end while

return \( M_B \)

### Algorithm 4 Camera Localization

**INPUT:** Query features \( Q \), Model features \( V \), co-visibility graph \( G \), camera clusters \( C \), NN search depth \( k \), ratio test threshold \( \tau \), match count thresholds \( N_F, N_B \), projection error threshold \( \epsilon \)

\( M = \text{GLOBAL-FORWARD-MATCH}(Q, V, N_F, \tau) \)

\( M_F = \text{CLUSTER-WISE-RATIO-TEST}(M, C, \tau) \)

\( M_B = \text{PRIORITY-BACK-MATCH}(M_F, N_B, G, \tau) \)

\( I_F, \delta = \text{ROBUSTFITTING}(M_B, \epsilon) \)

if \( |\delta| \geq 12 \) then

return Camera Pose \( I_P \)

else

return Error - Pose not found

end if

### 4. Benchmark Evaluation

We evaluated our final localization pipeline (Algorithm 4) on three different datasets: Eng-Quad, Dubrovnik, and Rome. Rome is a large dataset of 16,179 training images, 1,000 of which were used for test. Dubrovnik is a popular 6,844 image dataset whose SfM model is roughly aligned to geographic coordinates, allowing for metric quantification of localization error. While Eng-Quad has fewer images, it is perhaps the most challenging due to the presence of strongly repeated structures in the modern architectural designs it depicts. When using P3P, we used EXIF metadata for Eng-Quad test images and ground-truth focal lengths from the SfM models for Dubrovnik and Rome.
Dubrovnik correctness: After carefully analyzing the original models provided for Dubrovnik, we found that the focal lengths provided were often larger than expected, which in turn resulted in large errors in camera location and poor alignment between projection of 3D points and the corresponding 2D features. These problems are evident in results published elsewhere. For example, [21] report better results using P4Pf [4] than using P3P with the given focal lengths. This is contrary to what it should be expected: knowing the ground truth focal length (P3P) should outperform joint estimation of pose and focal length (P4Pf).

For this reason, we rebuilt a new version of the Dubrovnik model using the same set of keypoints provided for the original dataset and the excellent SfM package COLMAP [23]. We aligned the new model with the original one using a RANSAC-based Procrustes analysis so that the scale is approximately metric. After alignment, only 3853 of the recovered 6844 images were located within 3 meters from their original position in the model further validating our concerns. Our reconstruction provided ground-truth for 777 of the 800 query images.

Anytime performance: The runtime of our algorithm for camera localization depends on two parameters: \( N_F \) and \( N_B \). Setting these parameters trades off localization accuracy with faster execution times. Figure 3 shows the influence of these variables using the Eng-Quad dataset. We benchmarked forward matching times by randomly sampling query features until a desired number \( N_F \) pass the global ratio under fixed values for \( N_B \). Similarly, we fixed \( N_F \) and evaluated different values for \( N_B \). In both cases, the range of values tested vary from 50 up to 500 matched features. Figure 3 shows the number of registered images under these different configurations, and the time spent to achieve such a level of performance.

Experimental details: We tested our localization pipeline using the following settings: for each dataset, we built a global kd-tree index using all model views. We request \( k = 5 \) nearest neighbors and check 128 leaves. We set \( \tau = 0.7 \) across all of our ratio tests. We set \( N_F = 200 \) and \( N_B = 200 \) to provide a good balance between camera localization and speed performance. To prevent algorithm 3 to loop excessively we stop after 20 images have been evaluated. Experiments were performed using a single thread on an Intel i7-5930 CPU at 3.50GHz. We compare our results with [19, 20], as they provide an implementation of their localization procedure. Their code was executed in a single thread on an Intel i7-3770 CPU at 3.40GHz on the Eng-Quad and corrected Dubrovnik datasets, using the generic vocabulary tree provided with their code.

Localization results: We successfully localized all images in Dubrovnik, except one image in the corrected version using P4Pf. We achieved the smallest localization errors for all quartiles, and obtained a higher number of cameras localized within the 18.3m threshold while reporting few errors beyond the 400m mark. Our method yielded larger average error with respect to the original Dubrovnik model due to its underlying defects, despite finding a substantial higher number of inlier correspondences. [26] and [34] (after RANSAC), who use a shape-voting approxi-
Figure 4. Qualitative localization results. Left column: model images (gray) are highlighted in red if they have at least one vote from our cluster-wise ratio test. Our prioritized back matching algorithm quickly recognizes model images depicting the same landmarks (green). Right column: correspondences used for fine camera pose estimation (yellow), along the localized camera, depicted in green. The ground truth camera position is indicated with a red circle. Best viewed zoomed. See supplementary material for additional figures.

The localization performance benefits of our approach are even more pronounced on Eng-Quad, due to its difficult characteristics. Compared to [19, 20], we successfully localize 100 and 50 additional cameras respectively, improving all localization errors except the first quartile when using P4Pf. Our prioritized back matching algorithm allows faster runtimes than [12, 34] and is competitive with those of [19, 20]. Notably, our approach adapts better to the more difficult Eng-Quad dataset, spending more time retrieving images with sufficient correspondences. On the other hand, we quickly recognize landmarks in Dubrovnik with the first or second top ranked images, yielding faster localization times.

5. Discussion

Alternatives to large-scale image localization have focused on reducing the density of the search space to quickly find discriminative correspondences. Here we have shown that retrieving multiple global nearest neighbors and filtering them using approximations to the ratio test can quickly identify candidate regions of pose space. Such regions can be further refined by back matching to yield state-of-the-art results in camera localization and location recognition, even for datasets with challenging global repeated structure.
References

[1] R. Arandjelović and A. Zisserman. Dislocation: Scalable descriptor distinctiveness for location recognition. In Asian Conference on Computer Vision, pages 188–204. Springer, 2014.

[2] G. Baatz, O. Saurer, K. Köser, and M. Pollefeys. Large scale visual geo-localization of images in mountainous terrain. In Computer Vision—ECCV 2012, pages 517–530. Springer, 2012.

[3] H. Bay, A. Ess, T. Tuytelaars, and L. Van Gool. Speeded-up robust features (surf). Computer vision and image understanding, 110(3):346–359, 2008.

[4] M. Bujnak, Z. Kukelova, and T. Pajdla. A general solution to the p4p problem for camera with unknown focal length. In Computer Vision and Pattern Recognition, 2008. CVPR 2008. IEEE Conference on, pages 1–8. IEEE, 2008.

[5] S. Cao and N. Snavely. Graph-based discriminative learning for location recognition. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, pages 700–707, 2013.

[6] T. Dekel, S. Oron, M. Rubinstein, S. Avidan, and W. T. Freeman. Best-buddies similarity for robust template matching. In 2015 IEEE Conference on Computer Vision and Pattern Recognition (CVPR), pages 2021–2029. IEEE, 2015.

[7] R. Díaz, S. Hallman, and C. C. Fowlkes. Detecting dynamic objects with multi-view background subtraction. In Computer Vision (ICCV), 2013 IEEE International Conference on, pages 273–280. IEEE, 2013.

[8] R. Díaz, M. Lee, J. Schubert, and C. C. Fowlkes. Lifting gis maps into strong geometric context for scene understanding. In 2016 IEEE Winter Conference on Applications of Computer Vision (WACV), pages 1–9, March 2016.

[9] M. A. Fischler and R. C. Bolles. Random sample consensus: a paradigm for model fitting with applications to image analysis and automated cartography. Communications of the ACM, 24(6):381–395, 1981.

[10] L. Kneip, D. Scaramuzza, and R. Siegwart. A novel parametrization of the perspective-three-point problem for a direct computation of absolute camera position and orientation. In CVPR, 2011.

[11] Y. Li, N. Snavely, D. Huttonlocher, and P. Fua. Worldwide Pose Estimation using 3D Point Clouds. In ECCV, 2012.

[12] Y. Li, N. Snavely, and D. P. Huttonlocher. Location recognition using prioritized feature matching. In European Conference on Computer Vision, pages 791–804. Springer, 2010.

[13] D. G. Lowe. Distinctive Image Features from Scale-Invariant Keypoints. IJCV, 60(2):91–110, Nov. 2004.

[14] L. Moisan, P. Moulon, and P. Monasse. Automatic homographic registration of a pair of images, with a contrario elimination of outliers. Image Processing On Line, 2:56–73, 2012.

[15] P. Moulon, P. Monasse, and R. Marlet. Adaptive structure from motion with a contrario model estimation. In ACCV. 2012.

[16] D. M. Mount and S. Arya. Ann: library for approximate nearest neighbour searching. 1998.

[17] M. Muja and D. G. Lowe. Flann, fast library for approximate nearest neighbors. In International Conference on Computer Vision Theory and Applications (VISAPP09). INSTICC Press, 2009.

[18] T. Sattler, M. Havlena, K. Schindler, and M. Pollefeys. Large-scale location recognition and the geometric burstiness problem. In The IEEE Conference on Computer Vision and Pattern Recognition (CVPR), June 2016.

[19] T. Sattler, B. Leibe, and L. Kobbelt. Fast image-based localization using direct 2D-to-3D matching. ICCV, 2011.

[20] T. Sattler, B. Leibe, and L. Kobbelt. Improving image-based localization by active correspondence search. In European Conference on Computer Vision, pages 752–765. Springer, 2012.

[21] T. Sattler, C. Sweeney, and M. Pollefeys. On sampling focal length values to solve the absolute pose problem. In European Conference on Computer Vision, pages 828–843. Springer, 2014.

[22] G. Schindler, M. Brown, and R. Szeliski. City-scale location recognition. In 2007 IEEE Conference on Computer Vision and Pattern Recognition, pages 1–7. IEEE, 2007.

[23] J. L. Schönberger and J.-M. Frahm. Structure-from-motion revisited. In IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2016.

[24] J. Shi and J. Malik. Normalized cuts and image segmentation. IEEE Transactions on pattern analysis and machine intelligence, 22(8):888–905, 2000.

[25] N. Snavely, I. Simon, M. Goesele, R. Szeliski, and S. M. Seitz. Scene Reconstruction and Visualization From Community Photo Collections. Proceedings of the IEEE, 98(8):1370–1390, Aug. 2010.

[26] L. Svarm, O. Enqvist, F. Kahl, and M. Oskarsson. City-scale localization for cameras with known vertical direction. IEEE Transactions on Pattern Analysis and Machine Intelligence, 2016.

[27] L. Svarm, O. Enqvist, M. Oskarsson, and F. Kahl. Accurate localization and pose estimation for large 3d models. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, pages 532–539, 2014.

[28] A. Torii, R. Arandjelovic, J. Sivic, M. Okutomi, and T. Pajdla. 24/7 place recognition by view synthesis. In The IEEE Conference on Computer Vision and Pattern Recognition (CVPR), June 2015.

[29] A. Torii, J. Sivic, T. Pajdla, and M. Okutomi. Visual place recognition with repetitive structures. In The IEEE Conference on Computer Vision and Pattern Recognition (CVPR), June 2013.

[30] P. H. Torr and A. Zisserman. Mlesac: A new robust estimator with application to estimating image geometry. Computer Vision and Image Understanding, 78(1):138–156, 2000.

[31] S. Wang, S. Fidler, and R. Urtasun. Holistic 3d scene understanding from a single geo-tagged image. 2015.

[32] C. Wu. Towards linear-time incremental structure from motion. In 2013 International Conference on 3D Vision-3DV, pages 127–134. IEEE, 2013.
[33] A. R. Zamir and M. Shah. Image geo-localization based on multiple nearest neighbor feature matching using generalized graphs. *IEEE transactions on pattern analysis and machine intelligence*, 36(8):1546–1558, 2014. 4

[34] B. Zeisl, T. Sattler, and M. Pollefeys. Camera pose voting for large-scale image-based localization. In *Proceedings of the IEEE International Conference on Computer Vision*, pages 2704–2712, 2015. 2, 5, 7, 8