Model Checking Active Database Rules under Various Rule Processing Strategies

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An active database is a database system that can react to internal, as well as external, database events. The reactive behavior of an active database is determined by a predefined set of active database rules, along with a rule processing strategy. A common problem associated with active database systems is the possible non-termination of the active database rules. Previous work on the analysis of the conditions required for the termination of active database rules has only considered limited rule processing strategies. This paper proposes an approach for automatically detecting the non-termination of active database rules using a model checking technique. With this approach, a general framework for modeling active database systems is first proposed. This framework is useful for analyzing the behavior of rules with different rule processing strategies and for allowing the adoption of different contexts and different execution coupling modes for the active database rules. Based on the proposed modeling framework, the termination property of active database rules with various rule processing strategies is next checked using SPIN, a model checking tool. Through experimental results, we demonstrated the feasibility of using this method.

1. Introduction

An active database is a database system that has the functionality to react to internal, as well as external, database events. On the other hand, a traditional database is limited to responding to external events that can include user queries or outside applications. Since 1980, the extra functionality of an active database, which allows the integration of reactive behavior in a centralized and timely manner, has attracted the attention of researchers and has led to the development of a number of systems, including Starburst, SQL-3, HiPAC, and Chimera.

The reactive functionality of active database systems can be described by rules, which have three components: an event, a condition, and an action. The event defines the trigger for the given rule; the condition defines when the given rule is activated; and the action defines the action that must be taken based on the activated rule. The behavior of an active database rule system depends not only on a predefined set of rules, but also on the rule processing strategy that is adopted by the system. It is usually difficult to predict the behavior based on the interactions of the active database rules associated with a given rule processing strategy.

One of the most common problems in an active database system is the non-termination of active database rules, since a given rule may indefinitely trigger another rule. In general, detecting the termination of active database rules is known as the undecidable problem. Most of the previous research that analyzed active database rules has focused on static analysis and has provided the principal conditions for the termination of rules, including acyclicity in the trigger-graph of the rules. However, static analysis cannot be used to predict or specify the undesirable behavior of active database rules. In addition, previous work on the termination analysis of active database rules has only considered limited rule processing strategies.

To remedy this gap, our paper proposes an approach for automatically checking the termination of active database rules with different rule processing strategies using a model checking technique. Model checking is a verification technique that can exhaustively check whether or not a finite state transition system satisfies the temporal logic property. It is automatically performed using the currently available model checkers.

Specifically, we propose a modeling framework for constructing an abstract finite model of an active database system with different rule processing strategies. This model is parametric in several contexts and several coupling modes used in the existing active database sys-
tems 4,7,13,21). The model is also amenable to verification by the model checker, SPIN 10. We determine how to automatically check the termination property of the rules in the proposed model using model checking.

Thus, the proposed method is the first termination checking method of active database rules that is not limited to specific contexts and execution coupling modes of the active database system. Moreover, the proposed termination checking of the active database rules is automatically performed using model checking and, if the termination property does not hold, one can specify the undesirable behavior of the active database rules by analyzing a counterexample output from the model checker. We believe that the proposed approach can be applied and extended for analyzing rule behaviors in various active database systems with different features of rule processing.

This paper is organized as follows. Section 2 introduces the rules, the rule processing strategies of active database systems, and model checking with SPIN. Section 3 explains the proposed modeling framework, which can deal with various contexts and execution coupling modes. Section 4 describes how, based on the proposed modeling framework, model checking can be used to determine the termination property of rules. Section 5 shows the experimental results obtained when the proposed method is applied to a sample rule set with different rule processing features. Section 6 briefly discusses the related work. Section 7 summarizes the main conclusions that can be drawn from the study.

2. Preliminaries

2.1 Active Database Rules

An active database system consists of a set of rules that describe the desired reactive behaviors. An active database rule consists of three components: an event, a condition, and an action, with the following syntax:

\[
\text{ON}[\text{event}] \text{ IF}[\text{condition}] \text{ DO}[\text{action}].
\]

Example 1 Figure 1 shows two sample data tables, ‘Emp’, which contains the records employee’s ‘id’ and employee’s ‘rank’, and ‘Bonus’, which contains the records employee’s ‘id’ and employee’s ‘amount’ of bonus. Now, consider the following two rules, \(r_1\) and \(r_2\), which are given in Fig. 2. The rules add the following reactive behaviors to an active database system *a*: Rule \(r_1\) signifies that whenever \(\text{Emp}(\text{rank})\), the rank of an employee, is updated, \(\text{Bonus}(\text{amount})\), the amount of the employee’s bonus, is increased by 10, if \(\text{Emp}(\text{rank})\) is even. Rule \(r_2\) signifies that whenever \(\text{Bonus}(\text{amount})\), the amount of the employee’s bonus is updated, \(\text{Emp}(\text{rank})\), the rank of the employee is increased by 1.

Active database rules are characterized by two models: a knowledge model and an execution model 8,17. The knowledge model describes the structural characteristics of the rules, while the execution model captures the runtime characteristics of the rule processing. The knowledge model is characterized by the event type and action type, as well as the context of the conditions and the actions. Event types include data modification (e.g., insert and update) and clock (e.g., at 13:00 every Monday). Two or more events can be combined, and this is also considered to be a single event. Action types include data retrieval and modification, transaction operations, such as commit or abort, and an external call.

The execution model is characterized by the conflict resolution policy, the scheduling policy, and the coupling mode of the rules. When mul-

\begin{table}[h]
\centering
\begin{tabular}{|c|c|}
\hline
\textbf{Table Emp} & \\
\hline
\textbf{id} & employee’s id \\
\hline
\textbf{rank} & employee’s rank \\
\hline
\end{tabular}
\end{table}

\begin{table}[h]
\centering
\begin{tabular}{|c|c|}
\hline
\textbf{Table Bonus} & \\
\hline
\textbf{empid} & employee’s id \\
\hline
\textbf{amount} & employee’s bonus \\
\hline
\end{tabular}
\end{table}

\begin{figure}[h]
\centering
\begin{tabular}{|c|c|}
\hline
\textbf{r_1} & \\
\hline
\text{ON} update(\text{Emp}(\text{rank})) & \\
\text{IF} \text{\empid} \mod 2 = 0 & \\
\text{DO} update(\text{Bonus}(\text{amount})) & \\
\text{Bonus}(\text{amount}) = \text{Bonus}(\text{amount}) + 10 & \\
\hline
\end{tabular}
\caption{Sample active database rules.}
\end{figure}

\textsuperscript{a} The definition of rules, \(R_1\) and \(R_2\), given in Fig. 2, is implicit in that the definitions of the rules are given independently of which entries in the table’s tuples are used for the events, the conditions, and the actions. Such an abstraction is used in the definition of active database rules, since the explicit semantics of the definitions are derived based on the rule description languages.
multiple rules are triggered and activated at the same time, the conflict of rules is resolved based on the numerical or relative priorities of the rules according to the conflict resolution policy. Multiple rules are executed sequentially or in parallel based on the scheduling policy.

In this paper, for simplicity, we will assume that the event and action types are only data modifications and that the rules and the transactions are executed sequentially. These assumptions have been made in previous research papers\(^1,9,18\).

2.2 Rule Processing of Active Database Systems

Figure 3 shows the general abstract architecture of an active database system, which is reproduced from Ref. 17). An active database system consists of several principal components (rectangles in the figure) and data stores (circles in the figure), as illustrated in Fig. 3. Once a set of active database rules has been defined in a rule base, an active database system performs rule processing as follows:

- The Event Detector detects the events of interest to the system. Data modification events are noticed from the database.
- The Condition Monitor evaluates the conditions of rules associated with the detected events and stores the rules whose conditions are evaluated to true in a conflict set.
- The Scheduler chooses and runs a rule from the conflict set according to the conflict resolution policy.
- The Query Evaluator executes the database queries, such as transaction queries and conditions and actions resulting from the rules. When evaluating such queries, the query evaluator accesses not only the current state of the database but also, if necessary, past states, history, of the database.

The behavior of the active database rules depends on the rule processing strategy, that is, the knowledge and execution model of the rule processing adopted by the system. Among the characteristics of the knowledge and execution model, the contexts and the coupling modes of rules are important factors in determining the termination of rules. Therefore, in this paper, for the knowledge model, we focused on the rule contexts, while for the execution model, we focused on the coupling modes of rules.

**Context** indicates which state of a database is used in the rule processing. Let \(D_T, D_E, D_C,\) and \(D_A\) denote the states when the current transaction starts, the event occurs, the condition is evaluated, and the action is executed. In this paper, we consider the choices in Table 1 as the contexts for the condition, condition-context, and for the action, action-context. These contexts are, in fact, used in existing active database systems\(^4,7,13,21\).

**Execution coupling mode** consists of the event-condition mode and the condition-action mode. The event-condition mode determines when the condition is evaluated after the corresponding event has occurred. The condition-action mode determines when the action is executed after the corresponding condition was evaluated. The following coupling modes are supported in current active database systems\(^4,7,13,21\):

- **Immediate**, where the condition (action) is evaluated (executed) immediately after the event (condition) of the rule.
- **Deferred**, where the condition (action) is evaluated (executed) anywhere within the same transaction as the event (condition) of the rule.
- **Decoupled** (or detached), where the condition (action) is evaluated (executed) as a different transaction.

| Choices | Condition-Context | Action-Context |
|---------|-------------------|----------------|
| \(C_1\) | \(D_C\)           | \(D_A\)        |
| \(C_2\) | \(D_T\)           | \(D_T\)        |
| \(C_3\) | \(D_E\)           | \(D_E\)        |

| Modes    | Event-Condition | Condition-Action |
|----------|-----------------|------------------|
| \(M_1\)  | Immediate       | Immediate        |
| \(M_2\)  | Immediate       | Deferred         |
| \(M_3\)  | Deferred        | Immediate        |
| \(M_4\)  | Deferred        | Deferred         |
| \(M_5\)  | Decoupled       | Decoupled        |
In this paper, we will consider the five choices given in Table 2 for the event-condition mode and the condition-action mode.

2.3 Model Checking and SPIN

Model checking is a verification technique that exhaustively checks whether or not a system modeled using a finite state transition system satisfies the property expressed by the temporal logic formula. Since, given a transition system and a temporal logic formula, model checking can be automatically and rapidly performed using existing tools, it has recently regained the attention of researchers. Model checking is also helpful in locating system errors, since whenever a system model does not satisfy a property formula, a counterexample that gives the system behavior that violates the property is given as the output.

SPIN is known as one of the most powerful model checkers. An input model to SPIN is described in Promela (Process Meta-Language) which has C-like syntax. A Promela model consists of one or more asynchronous processes with data objects, non-deterministic constructs, and communication primitives. Processes can communicate via synchronous and asynchronous message passing with buffered channels or shared memory. SPIN verifies the claims specified by the Linear Temporal Logic (LTL) formulae or process invariants, which can express the basic safety and liveness properties. SPIN performs on-the-fly verification and supports several useful state search and compression strategies. With our approach, we used SPIN because of its powerful verification capability. Furthermore, SPIN was used since an active database system can easily be modeled as an asynchronous process system using Promela.

3. Modeling of Active Database Systems under Different Rule Processing Strategies

3.1 Basic Modeling Framework

Figure 4 illustrates our abstract model of an active database system. We constructed the model based on the general active database architecture in Fig. 3, by adding the model of transactions. This transaction model is necessary for checking the behavior of active database rules. As will be explained below, the proposed model is thus slightly different from the architecture in Fig. 3. The difference lies only in the facility of modeling and abstraction and thus does not affect the generality of the proposed modeling framework.

The state of the proposed model is determined from the states of four types of data storage illustrated using circles in the figure, DB, DB₀, RuleBase, and ConflictSet, and buffered channels ch_query, ch_event, ch_cond, ch_action where

- DB denotes the current database state;
- DB₀ denotes the list of the database past states;
- RuleBase denotes the defined set of rules;
- ConflictSet denotes the current conflict set of rules;
- ch_event denotes the channel buffering detected events;
- ch_cond denotes the channel buffering conditions to be evaluated, and
- ch_action denotes the channel buffering ac-
tions to be executed.

The proposed model consists of the following four processes (illustrated using rectangles in the figure): Manager, Scheduler, Evaluator, and Transaction. The Process Manager models the behavior of the event detector and the condition monitor. The Process Scheduler models the behavior of the scheduler, while the process Evaluator models the behavior of the query evaluator of the active database system. The Process Transaction models the users or the applications that send transactions to the database system. The processes read and update the data storage and buffered channels, as well as communicate with each other via synchronous or asynchronous message passing through the channels. The behavior of each process is as follows:

**Process Transaction**

This process generates and sends the transaction queries (data operations) to the buffered channel, ch_query. The Process Evaluator will receive the transaction queries via asynchronous message passing through the channel. In the model, we allow the transaction to consist of multiple data modification operations. However, we fixed the length of the transactions so that the state model is finite.

**Process Manager**

This process non-deterministically chooses a rule among the rules having the highest priority from the ConflictSet and sends a request to the Process Evaluator to execute the action of the rule. The identifier of the rule to be activated is sent via asynchronous message passing using the buffered channel, ch_action.

**Process Evaluator**

This process evaluates the following three kinds of data operations: transaction queries requested by the Process Transaction, rule conditions requested by the Process Manager, and rule actions requested by the Process Scheduler.

(a) Evaluation of the transaction queries: After receiving a transaction query from the channel, ch_query, the query is evaluated and a new event corresponding to the query is sent to the channel, ch_event. This evaluation procedure is finished when an acknowledgment message is received from the synchronous channel called ack_eval.

(b) Evaluation of the rule conditions: After receiving the identifiers of the rules from the channel, ch_cond, the rule conditions are evaluated, and the results of the evaluation are sent to the channel ch_answer. The evaluation procedure is finished when an acknowledgment message is received from the channel called ack_exe.

(c) Execution of the rule actions: After receiving the rule identifier from channel ch_action, the rule action is executed, and a new event corresponding to the action is sent to channel ch_event. This evaluation procedure is finished when an acknowledgment message is received from the channel ack_eval.

To evaluate these three kinds of operations, this process accesses the data from either DB or DB_p. In the case of (a) and (c), a new event may occur after the evaluation. In these two cases, the acknowledgment is received from channel ack_eval after the Process Manager notices the new event and sends the additional rules triggered by the event to ConflictSet. In the case of (b), the acknowledgment is received from channel ack_exe after the Process Scheduler has sent the activated rule to the channel ch_action. Waiting for the acknowledgment prevents the evaluation procedures of (a), (b), and (c) from being intermingled with the other procedures.
3.2 Modeling Different Contexts and Execution Coupling Modes

The basic framework for modeling an active database system was proposed in Section 3.1, and the modeling framework is applicable to active database systems with different rule processing strategies. In this section, we explain how to model active database systems with the contexts given in Table 1 and the coupling modes given in Table 2, based on the modeling framework.

Modeling of Contexts

Let us examine the condition-context and the action-context. We consider the three choices, $C_1$, $C_2$, and $C_3$, shown in Table 1. In our modeling framework, as shown in Fig. 4, the Process Evaluator reads the current and/or the past database states when evaluating data operations. Active database systems with $C_1$, $C_2$, or $C_3$ are then straightforwardly modeled by selecting the state of the database to be read by the Process Evaluator.

In the case of $C_1$, $D_{C_1}$, the state when the condition is evaluated, is the condition-context state, and $D_{A_1}$, the state when the action is executed, is the action-context state. Hence, to model $C_1$, we let the Process Evaluator access $DB_1$, that is, the current state of the database when evaluating conditions and executing actions.

In the case of $C_2$, $D_{C_2}$, the state when the transaction starts, is used for the condition-context and the action-context. Hence, to model $C_2$, we store the state when the current transaction starts in $DB_{Ch}$ and let the Process Evaluator access $DB_{Ch}$ when evaluating the conditions and executing the actions.

In the case of $C_3$, $D_{C_3}$, the state when the corresponding event occurs, is used for the condition-context and the action-context. To model $C_3$, we store the state when each event occurs in $DB_{Ch}$. When evaluating a condition or a rule action, we let the Process Evaluator access the state of the $DB_{Ch}$ corresponding to the event of the rule.

Modeling of Coupling Modes

Let us examine the coupling modes that consist of the event-condition mode and the condition-action mode. We consider the five choices, $M_1$, $M_2$, $M_3$, $M_4$, and $M_5$, given in Table 2. In our model framework, the Process Evaluator performs three types of evaluations: (a) the transaction query evaluation, (b) the condition evaluation, and (c) the action execution. Operations for (a), (b), and (c) are respectively received from the buffered channels $ch_{query}$ (from the Process Transaction); $ch_{cond}$ (from the Process Manager); and $ch_{action}$ (from the Process Scheduler). As shown in Table 3, an active database system with $M_1$, $M_2$, $M_3$, $M_4$, or $M_5$ is then modeled by assigning priorities to the three channels to determine the order of receiving operations in the Process Evaluator.

In the case of $M_1$, the coupling modes for both the event-condition and the condition-action are Immediate, and thus the condition (the action) has to be evaluated (executed) immediately after event occurrence (the condition evaluation). Mode $M_1$ is modeled by giving a higher priority to channels $ch_{cond}$ and $ch_{action}$ than to channel $ch_{query}$.

In the case of $M_2$, the event-condition mode is Immediate and the condition-action mode is Deferred. Thus the condition has to be evaluated immediately after event occurrence, while the action has to be executed within the same transaction. Thus, mode $M_2$ is modeled as follows. Since the event-condition mode is Immediate, the higher priority is given to channel $ch_{cond}$ than to channels $ch_{action}$ and $ch_{query}$. $T_{end}$ in the table denotes a Boolean variable that is true during the period after the current transaction is completed and before the next transaction starts. Since the condition-action mode is Deferred, the higher priority is given to channel $ch_{action}$ when $T_{end}$ is true. This guarantees that the action is executed within the same transaction.

In the case of $M_3$, the event-condition mode is Deferred and the condition-action mode is Immediate. Thus, mode $M_3$, like mode $M_2$, is modeled as follows. The higher priority is given to channel $ch_{action}$ than to channels $ch_{cond}$ and $ch_{query}$. The higher priority is given to channel $ch_{cond}$ than channel $ch_{query}$ when $T_{end}$ is true.

In the case of $M_4$, the event-condition and the condition-action modes are both Deferred. Mode $M_4$ is modeled by giving a higher priority to channels $ch_{cond}$ and $ch_{action}$ than channel $ch_{query}$ when $T_{end}$ is true.

In the case of $M_5$, the event-condition and the condition-action modes are Decoupled. Thus the condition (action) is evaluated (executed) as a different transaction after terminating the transaction associated with the corresponding...
event (condition). Mode $M_5$ is modeled by giving a higher priority to channel $ch\_query$ than to channels $ch\_cond$ and $ch\_action$ if $T\_end$ is false; otherwise a higher priority is given to channels $ch\_cond$ and $ch\_action$ than to channel $ch\_query$.

4. Termination Checking of Active Database Rules

In order to verify the behavior of the active database rules, we first translate the proposed model described in Section 3 into the equivalent Promela model. Then, we check the termination property of rules using the Promela model and SPIN.

4.1 Promela Model of Active Database Rule Systems

The proposed model for the active database systems can be easily translated to an equivalent Promela model. We briefly illustrate the translation of our active database system model with the sample rule sets, $R_1$ and $R_2$, as shown in Example 1, the context, $C_1$, and the coupling mode, $M_1$. Sample Promela code is given in Appendix A. (For more details about Promela syntax, see Ref. 10.)

Initialization

Lines 1 to 5 define the number of rules, the size of the conflict set, the maximum number of operations in a transaction, the maximum number of transactions, and the size of buffered channels. Note that the state space of a Promela model is required to be a minimum in order to avoid the state explosion problem and hence to be verifiable by model checking. In the example Promela code, we set the values of variables in Lines 2 to 5 to be a minimum level required for checking the termination of the example rule set $R_1$ and $R_2$. These values should be determined to be suitable for checking a given target rule set.

Lines 7 to 26 declare global variables and user-defined types. The variable, $emp\_rank$, represents the current value of the record, $Emp(rank)$, while the variable, $bonus\_amount$, represents the current value of the record, $Bonus(amount)$. For simplicity, in this example, we abstracted a data model in such a way that the tables $Emp$ and $Bonus$ contain one tuple with the same employee’s id. (In the case of $C_2$ or $C_3$, $DB,p$ is necessary, and thus we prepared a buffered channel, which stores the past record states, $D_T$ or $D_E$.) The rule set, $rules[N]$, represents $RuleBase$, while the rule buffer, $cs$, represents $ConflictSet$. User-defined types, $event\_type$ and $rule\_type$, represent respectively the types of events and rules.

Lines 28 to 40 declare the communication channels in Fig. 4. In order to model the channel priorities in Table 3, channels $ch\_query$, $ch\_event$, $ch\_cond$, $ch\_answer$, and $ch\_action$ are declared as asynchronous communication channels with a fixed buffer size. In our model, multiple messages (data operations or rules) are needed to be buffered in channels $ch\_cond$, $ch\_answer$, and $ch\_action$ but not in $ch\_query$ and $ch\_event$. Hence, in the example Promela program, the buffer sizes of $ch\_query$ and $ch\_event$ are set to one, while the buffer sizes of $ch\_cond$, $ch\_answer$, and $ch\_action$ are set to the value of $size\_buffer$. Other channels $ch\_schedule$, $ack\_eval$, and $ack\_exe$ are declared as synchronous channels, because they need only to pass a message but not to buffer a message.

Line 42 declares the Boolean variable, $T\_end$, in Fig. 4.

Lines 45 to 77 declare the initial process. The initial process declares $RuleBase$ and creates the process for $Transaction$, $Manager$, $Scheduler$ and $Evaluator$. Promela processes are executed concurrently and scheduled non-deterministically. Using $d\_step$ and atomic statements reduces the state space and prevents the statements that are to be executed from being interfered with by other processes.

Process Transaction

Lines 79 to 103 declare the Process Transaction. This process chooses the data operation for the transaction and sends it to channel $ch\_query$. The last operation of the transaction is specially marked so that the Process $Evaluator$ can know the tail of the current transaction. In Promela execution semantics, each statement is either blocked or executable. As for the $do$-statement and the $if$-statement, if more than one of these state-

| Modes | Priorities of Channels       |
|-------|-----------------------------|
| $M_1$ | $ch\_query < ch\_cond = ch\_action$ |
| $M_2$ | $
eg T\_end \rightarrow ch\_query = ch\_action < ch\_cond$ $T\_end \rightarrow ch\_query < ch\_action < ch\_cond$ |
| $M_3$ | $
eg T\_end \rightarrow ch\_query = ch\_cond < ch\_action$ $T\_end \rightarrow ch\_query = ch\_cond < ch\_action$ |
| $M_4$ | $
eg T\_end \rightarrow ch\_query = ch\_cond = ch\_action$ $T\_end \rightarrow ch\_query < ch\_cond = ch\_action$ |
| $M_5$ | $
eg T\_end \rightarrow ch\_cond = ch\_action < ch\_query$ $T\_end \rightarrow ch\_query < ch\_cond = ch\_action$ |
ments is to be executable, that is, the guards of the statements are true, then one of the statements is non-deterministically selected and executed. In checking the model, SPIN exhaustively explores all possible behaviors. The Process Transaction models the possible transactions by selecting the transaction operations non-deterministically.

**Process Manager**

Lines 105 to 174 declare the Process Manager. When an event is received from the channel ch_event, this process finds the rules in rules triggered by the event and sends the identifiers for the triggered rules to the channel ch_cond. When the evaluation results are received from the channel ch_answer, this process sends to cs the identifiers for the rules whose conditions are true. After both procedures, T_end is set to false if cs, ch_cond, and ch_action are empty, that is, there are no rules to be evaluated or executed; otherwise a scheduling request is sent to the channel ch_schedule.

**Process Scheduler**

Lines 176 to 197 declare the Process Scheduler. When a scheduling request is received from the channel ch_schedule, this process non-deterministically chooses a rule from cs and sends the identifier for this rule to the channel ch_action. In Promela, a non-deterministic receive operation from a buffered channel is described using the operator ‘??’.

**Process Evaluator**

Lines 199 to 262 declare the Process Evaluator. This process receives data operations from the three channels ch_query, ch_cond and ch_action, and evaluates the operations received. The receiving order from the three channels follows the channel priority in Table 3 and then the different execution coupling modes can be easily modeled as explained in Section 3.2.

In the case of M1, the channel priority is ch_query < ch_cond = ch_action in Table 3. This priority is expressed by Lines 208, 230, and 246. Lines 208, 230, and 246 respectively represent the conditions of receiving operations from the channels ch_query, ch_cond and ch_action. Line 208 signifies that an operation is received from the channel ch_query if the channel ch_query is not empty and the both channels ch_cond and ch_action are empty. This implies that ch_query < {ch_cond, ch_action}. On the other hand, Line 230 (246) signifies that an operation is received from the channel ch_cond (ch_action) only if the channel is not empty. This implies that ch_cond > {ch_query, ch_action} (ch_action > {ch_query, ch_cond}). Therefore, by Lines 208, 230, and 246, the channel priority for M1 can be expressed. Promela models for M2 to M5 are also easily obtained by changing the lines in this way, according to the channel priorities in Table 3.

### 4.2 Termination Checking

In our Promela model of an active database system, we can easily express the termination property for the rules using Promela’s progress label, as shown in Lines 140 and 164 of the Promela code in Appendix A.

```
137 if
138 :: T_end==1 && (len(ch_cond)==0)
139 & & (len(ch_action)==0) ->
140 progress1: T_end = 0
141 :: else -> skip
142 fi;
```

In SPIN, progress is the label name for specifying the liveness properties. A statement marked by the progress label is required to be visited an infinite number of times in any infinite execution sequence. In our Promela code, the statements labeled with progress are executable if and only if there remain no rules to be evaluated or executed. Therefore, this implies that rule processing is terminated. If there is an execution sequence where the rule processing is never terminated, the statement labeled with progress is not visited and SPIN detects an error, as well as reporting the counterexample execution sequence.

**Example 2** Appendix B shows the result of checking whether there are any non-progress execution cycles for the sample Promela model given in Appendix A. The result shows that, for the sample model, no errors are detected and, thus, rules, R1 and R2, under the Context, C1, and Coupling mode, M1, satisfy the termination property.

Note that, for rules R1 and R2, a previous static checking method in 1) detects a cycle representing a potential non-termination. Differently from the previous method, the proposed model checking method can answer that rules R1 and R2 indeed terminate mutual triggering as a result of an exhaustive search on the proposed finite active database model, since condition evaluation for rules is explicitly considered in our modeling.
TABLE 1

(a) Termination Property

|     | M₁ | M₂ | M₃ | M₄ | M₅ |
|-----|----|----|----|----|----|
| C₁  | True | True | False | False | False |
| C₂  | False | False | False | False | False |
| C₃  | True | True | True | True | True |

(b) Time and Memory needed for Model Checking

|     | M₁ | M₂ | M₃ | M₄ | M₅ |
|-----|----|----|----|----|----|
| C₁  | Time (s) | 0.320 | 0.400 | 0.160 | 1.370 | 1.410 |
|     | Memory (Mbyte) | 325.886 | 326.910 | 324.657 | 339.505 | 339.300 |
| C₂  | Time (s) | 0.330 | 0.330 | 0.330 | 0.330 | 0.330 |
|     | Memory (Mbyte) | 322.302 | 322.302 | 322.302 | 322.302 | 322.302 |
| C₃  | Time (s) | 0.450 | 0.710 | 0.700 | 0.890 | 0.730 |
|     | Memory (Mbyte) | 327.934 | 331.723 | 331.62 | 333.976 | 332.337 |

Fig. 5 Experimental results.

Note that in our approach each data item involved in rule processing is explicitly modeled. Because of this fine grained representation and of the exhaustive state search with the model checking technique, the proposed method can carry out exact termination detection, which means that it does not allow any false negatives.

SPIN verifies the claims specified by the LTL\(^{11}\) formulae in addition to the process invariants. Therefore, other desirable safety properties can also be checked using our Promela model. For example, suppose that the Query Evaluator must answer a request from the Condition Manager in active database systems. In our model, this property is expressed using LTL as follows: \(\square (\negempty(ch\_cond) \rightarrow \negempty(ch\_answer))\), which then can be verified using SPIN.

5. Experiment

In the experiment, we checked the termination property of the sample rules, \(R_1\) and \(R_2\), in Example 1 for different contexts and coupling modes by applying the proposed method. (In previous works\(^{1,9,18}\), using almost identical rules as \(R_1\) and \(R_2\), termination checking had been performed assuming only a specific context and coupling mode.)

First, we constructed the Promela models for every pair of contexts, \(C_1\) to \(C_3\), and coupling modes, \(M_1\) to \(M_5\), as explained in Section 4. Next, using SPIN, we checked the termination property of the Promela models. For model checking, we used a Linux workstation with an Intel Xeon 3.0 GHz and 4 GB memory.

Figure 5 shows the experimental results. Figure 5-(a) shows the result of model checking the termination property for each pair of contexts and coupling modes. Based on the results, we know whether or not, depending on the contexts and coupling modes, a given rule set satisfies the termination property. For the cases where an error is detected by the model checking, we can obtain the counterexample trace that results in the rule processing to violate the termination property.

When the context is \(C_1\) and the coupling mode is \(M_3\), \(M_4\), or \(M_5\), the termination of rules \(r_1\) and \(r_2\) does not hold in the following counterexample trace: After the execution of a transaction query that updates the value of \(\text{rank}\) to an even number, rule \(r_1\) and rule \(r_2\), triggered by \(r_1\), are consecutively executed, resulting in an odd value of \(\text{rank}\). Subsequently, rule \(r_1\) triggered by \(r_2\) is executed after another transaction query updated the value of \(\text{rank}\) to an even number. In this way \(r_1\) and \(r_2\) are executed indefinitely. This can happen when the context is \(C_1\) and the event-condition mode is not Immediate, that is, the coupling mode is \(M_3\), \(M_4\), or \(M_5\).

If the context is \(C_2\), the termination of rules \(r_1\) and \(r_2\) does not hold regardless of coupling modes. The counterexample trace is as follows: The value of \(\text{rank}\), \(x\), is even, when a transaction starts. After a query of a transaction updated the value of \(\text{rank}\), rule \(r_1\) is executed and thereafter rule \(r_2\) triggered by \(r_1\) is executed. Subsequently, \(r_1\) and \(r_2\) are indefinitely executed by turns, since value \(x\) of \(\text{rank}\) when the transaction started is used for the condition evaluation of \(r_1\) and thus \(r_1\) is activated repeatedly.

Figure 5-(b) shows the time and memory required for model checking. For all cases, less than 1.5 seconds was needed, with a memory usage of about 330 Mbytes.

6. Related Work

As mentioned in Section 1, termination
checking of active database rules is generally an undecidable problem. Most previous works on analyzing active database rules have focused on static analysis \cite{1,2,6,12,14,19,20}.

Aiken, et al. \cite{1} first presented the concept of a trigger-graph of rules and the approach using the trigger-graph basically predicts possible non-termination of active database rules by investigating sufficient conditions for termination, such as acyclicity in the trigger-graph.

Thereafter, in order to improve the accuracy of predicting potential non-termination, several techniques like the refinement of the trigger-graph and the investigation of more accurate termination conditions for the trigger-graph approach have been proposed \cite{2,6,12,14,19,20}.

However, to the best of our knowledge, no previous trigger-graph approaches have presented a general method that can deal with various contexts and coupling modes including immediate, deferred, and decoupled, unlike our proposed method. For example, only the decoupled coupling mode was addressed in Ref. 6).

Most previous work has addressed the problem of analyzing the behaviors of single events; however, there is little work on the verification of the complex behavior of composite events. An exception is Ref. 19), where termination analysis for composite events is addressed. Although for simplicity we assumed single events in the paper, it is not difficult to deal with composite events in the proposed approach. Specifically, such composite events can be described in Promela using, for example, user-defined record structures.

Unlike static methods previously proposed, our approach automates rule analysis with no need to create a new program. By using an existing model checking tool, not only the verification result (whether terminating or non-terminating) but also the non-terminating rule execution can be automatically obtained.

Model checking has been applied for active database rule analysis in two previous works \cite{9,18}. However, so far, the general modeling framework applicable to active database systems with various rule processing strategies has not been considered.

In Ref. 9), Ghazi and Huth presented an abstract model framework for active database management systems and implemented a prototype of the Promela code generator. In their model, an active database system was simply modeled as two concurrent processes called system and environment. In their model, questions dealing with how to model data operations for query evaluation, condition evaluation, and action execution were not addressed.

In Ref. 18), Ray, et al. verified the termination of rules using the model checker SMV \cite{15}. Their model assumed that only specific execution semantics were used for the rules, that is, a transaction consisted of a single data operation, that rule processing was performed only after a transaction was committed, and that the contexts for the condition and the action were limited to the current state of the data.

7. Conclusion

This paper’s main contribution is a new method to model check active database rules with different contexts and coupling modes. First, we proposed the modeling framework, which is applicable to various active database systems with different contexts and coupling modes. Next, we presented how to translate our model to Promela and how to check the rule behavior using the SPIN model checker. Finally, using sample rules, we showed that the proposed method can efficiently check the termination of the rules with different contexts and coupling modes. To the best of our knowledge, this is the first time that the rule termination has been checked for context cases, $C_2$ to $C_3$, and coupling mode cases, $M_2$ to $M_5$.

The main difficulty in model checking active database rules is how to make an appropriate finite state model that represents the behavior of the active database rules. Since general model checking tools can only handle finite state models that do not cause state explosion, it is necessary to make an efficient finite abstraction of an active database system model.

Since our active database model incorporates some degree of abstraction, the proposed termination checking is not an exact method, like the previous works on rule termination analysis. However, the proposed method is more accurate than, for example, the previous work in Refs. 1), 12), 14), in the sense that the proposed method (1) can predict the termination of rules that are decided to terminate by the previous work, (2) can predict the termination of rules that are predicted to possibly non-terminate by the previous work, and (3) can predict the non-termination of rules that are decided not to terminate by the previous work and can furthermore specify undesirable behavior of the rules.
7.1 Discussion and Further Work

Here we discuss some questions raised by our approach and further works.

- How accurate is the proposed method, compared to the previous trigger-graph approach?

Because of the very different nature of the proposed approach and the trigger-graph approach, they have different strength and weakness with respect to the accuracy.

Although the proposed method has advantages over the trigger-graph approach as described in Section 6, it has also weakness with respect to accuracy. Specifically, the accuracy of the proposed method is suffered from the size of the model, since model checking tools can only handle finite state models of limited size. Thus we would conclude that our approach can be best utilized, by using it together with the trigger-graph approach in a complementary fashion.

- What is the advantage of using the proposed method for actual active database systems?

The functionality of active database rules has started attracting more attention, not only in the traditional database systems area but also in the field of various databases and applications, for example, XML\textsuperscript{16}, sensor databases\textsuperscript{22}, etc. The proposed approach is intended not to depend on particular settings and thus can be helpful for rule analysis in various environments with different rule contexts and execution semantics.

Moreover, the proposed approach can be useful for complementing the previous methods. In the cases where further analysis is needed after the conventional methods predicted the potential non-termination, the proposed method can be used for a more detailed analysis, thus improving the accuracy of detecting non-termination of active database rules.

- How well does the proposed method scale?

The scalability of the proposed method depends on the state space size of the active database model and the verification power of the model checking tool. The state space size of the active database model is determined from many factors such as the number of rules, the type of events, the complexity of the conditions, etc. Consequently, the quantitative evaluation of scalability of the proposed method is not easy.

Our future work will evaluate the applicability of the proposed model through case studies using actual active database rules. Many active database rules can be set in active databases. We conjecture that, even in such cases, the rules that must be checked can be separated into small-to-moderate sized groups so that the proposed method can handle each of these groups of rules. We also anticipate that model checking tools will be continuously improved to handle more complex system models.

Applying model checking of an infinite behavior model to termination analysis of active database rules is also an interesting topic for further study.

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Appendix

A.1 Example Promela Program

```promela
1 #define num_R 2  //number of rules/
2 #define num_CS 4  //size of the conflict set/
3 #define N 2  //maximum number of operations in a transaction/
4 #define M 2  //maximum number of transitions/
5 #define size_buffer 4  //size of buffered channels/
6
7 typedef mtype{  //type of rules
8 byte m;
9 byte field;
10 byte table;
11 byte operation;
12 byte mtype;
13};
14
15 typedef event_type{  //type of events
16 byte bonus_amount;  //current value of Bonus(amount) in DB
17 byte emp_rank;  //current value of Emp(rank) in DB
18 byte amount;
19 byte m;
20};
21
define Rules[0..2];  //RuleBase: Set of rules/
22
23 ch_action = [size_buffer] of {byte};  //{rule-id}
24 ch_query = [1] of {bool,mtype,mtype,mtype,byte};  //{1 iff end of transaction,operation,table,field,value}
25 ch_event = [1] of {mtype,mtype,mtype,byte};  //{update,emp,rank,bonus,amount};
26 ch_schedule = [0] of {bool};  //{rule-id}
27 ch_cond = [size_buffer] of {byte};  //{rule-id}
28 ch_eval = [size_buffer] of {byte,bool};  //{result of evaluation}
29
30 ch_conflict = [num_CS] of {byte};  //ConflictSet/
31 ch_schedule = [0] of {bool};  //{rule-id}
32 ch_answer = [size_buffer] of {byte,bool};  //{result of evaluation}
33 ch_query = [1] of {bool,mtype,mtype,mtype,byte};  //{1 iff end of transaction,operation,table,field,value}
34
35 ch_conflict = [num_CS] of {byte};  //ConflictSet/
36
37 ch_schedule = [0] of {bool};  //{rule-id}
38 ch_answer = [size_buffer] of {byte,bool};  //{result of evaluation}
39
40 ch_schedule = [0] of {bool};  //{rule-id}
41
42 bool T_end;
43
44 bool T_end;
45
46 (/
47 declare RuleBases/
48
d_step{  //declare RuleBases
49 Rules[0].event.operation = update;
50 Rules[0].event.table = emp;
51 Rules[0].event.field = rank;
52 Rules[0].condition = 1;
53 Rules[0].action.operation = update;
54 Rules[0].action.table = bonus;
55 Rules[0].action.field = amount;
56 Rules[0].action = 10;
57 Rules[0].event.field = rank;
58 Rules[0].condition = 1;
59 Rules[0].event.operation = update;
60 Rules[0].event.table = bonus;
61 Rules[0].event.field = amount;
62 Rules[0].event.field = rank;
63 Rules[0].condition = 0;
64 Rules[0].event.operation = update;
65 Rules[0].event.field = rank;
66 Rules[0].event = 1;
67 Rules[0].action = 1;
68");
69
70 //run processes/
71 atomic{
72 run Transaction();
73 run Manager();
74 run Scheduler();
75 run Evaluator();
76
77 }
78
79 proto type Transaction{}}
byte n; /*current number of operations in a transaction*/
byte m; /*current number of operations in a transaction*/
byte id; /*id of a rule to be executed*/

bool b;
byte id; /*id of a rule to be executed*/

proctype Scheduler(){
  :: nempty(CS) -> ch_schedule!1
  ack_exe!1
  :: else -> skip
  progress2: T_end = 0
  :: T_end==1 && (len(ch_action)==0) ->
    if
      :: empty(CS) ->
        if
          remain, set T_end to FALSE, otherwise call Scheduler*/
        /*if ConflictSet is empty and no rules to be executed*/
          if
            ch_query?tail,update,emp,rank,1
          od
        :: empty(ch_answer) -> break
        fi
      :: result -> CS!i
        if
          ch_answer?i,result;
        :: nempty(ch_answer) ->
          do
            atomic{
              :: nempty(ch_answer) -> /*receiving evaluation results*/
                fi
              :: else -> ack_eval!1
              fi
            }
            :: nempty(CS) -> ch_schedule!0
            ack_eval!1
            :: else -> skip
            od
          :: else ->
            if
              :: (trg==0) ->
                i=0; trg = 0; m++ /*tail of a transaction*/
              :: (i>=num_R) -> break
              :: else -> i++
            i++
            ch_cond!i; trg = 1;
        /*request condition evaluation to Evaluator*/
        && ev_field==Rules[i].event.field ->
          ev_operation==Rules[i].event.operation &&
          ev_table==Rules[i].event.table
        :: ev_operation==Rules[i].event.operation
        :: (i<num_R) ->
          i=0; trg = 0;
        atomic{
          /*receiving an event*/
          ch_event?ev_operation,ev_table,ev_field,ev_m;
          end:do
          bool result; /*evaluation result*/
          bool trg; /*TRUE if any rule is triggered*/
          byte ev_m, i;
          mtype ev_operation,ev_table,ev_field;

  proctype Manager(){
    od
  od
  :: break
  od
)
profotype Scheduler(){
byte id; /*id of a rule to be executed*/
bool b;

A.2 Example Output of SPIN

T. ./pan-1
(Spin Version 4.2.6 ~ 27 October 2005)
+ Partial Order Reduction

Full statepace search for:
  never claim +
  assertion violations + (if within scope of claim)
  non-progress cycles + (fairness disabled)
  invalid end states + (disabled by never claim)

State-vector 156 bytes, depth reached 808, errors: 0
27741 states, stored (41570 visited)
73537 states, matched
115107 transitions (= visited+matched)
127857 atomic steps
hash conflicts: 1445 (resolved)

Stats on memory usage (in Megabytes):
4.550 equivalent memory usage for states (stored*(State-vector + overhead))
3.877 actual memory usage for states (compression: 85.21%)
State-vector as stored = 132 byte + 8 byte overhead
2.097 memory used for hash table (=w19)
320.000 memory used for DFS stack (=m1000000)
319.824 other (proc and chan stacks)
0.088 memory lost to fragmentation
325.886 total actual memory usage

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