Compact continuum source-finding for next generation radio surveys.

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ABSTRACT

We present a detailed analysis of four of the most widely used radio source finding packages in radio astronomy, and a program being developed for the Australian Square Kilometer Array Pathfinder (ASKAP) telescope. The four packages; SExtractor, SFind, IMSAD and Selavy are shown to produce source catalogues with high completeness and reliability. In this paper we analyse the small fraction (∼1%) of cases in which these packages do not perform well. This small fraction of sources will be of concern for the next generation of radio surveys which will produce many thousands of sources on a daily basis, in particular for blind radio transients surveys. From our analysis we identify the ways in which the underlying source finding algorithms fail. We demonstrate a new source finding algorithm Aegean, based on the application of a Laplacian kernel, which can avoid these problems and can produce complete and reliable source catalogues for the next generation of radio surveys.

Key words: techniques: image processing, catalogues, surveys

1 INTRODUCTION

Source finding in radio astronomy is the process of finding and characterising objects in radio images. The properties of these objects are then extracted from the image to form a survey catalogue. The aim of large scale radio imaging surveys is to provide an unbiased census of the radio sky, and hence the ideal source finder is both complete (finds all sources present in the image) and reliable (all sources found and extracted are real).

Most of the standard source finding algorithms that have been developed over the last few decades are highly complete and reliable, missing only a small fraction of sources. These problem cases are generally dealt with in pre or post-processing, or manually corrected in the source catalogue.

Next generation radio surveys such as the Evolutionary Map of the Universe (EMU; Norris et al. 2011) and the ASKAP Survey for Variables and Slow Transients (VAST; Chatterjee et al. 2010) planned for the Australian SKA Pathfinder (ASKAP; Johnston et al. 2008) Telescope will produce large area, sensitive maps of the sky at high cadence, resulting in many times more data than previous surveys. Data processing will need to be fully automated, with limited scope for manual intervention and correction. Hence the small number of missing or incorrectly identified sources produced by current source-finders will pose a substantial problem. In particular, in blind surveys for radio transients, missed sources and false positives in an epoch will cause the transient detection algorithms to trigger on false ‘events’. VAST will need to extract thousands of sources from survey images at a cadence of ∼5 seconds. A source finding algorithm which is 99% complete and reliable at a signal-to-noise ratio of 5, will be producing ∼10,000 false sources, and missing ∼10,000 real sources per day. Whilst it is possible to remove false sources from a catalogue, the missing real sources are lost forever. The large data rates of telescopes like ASKAP will make it impossible to store each observation, and thus no reprocessing of the data will be possible.

The way in which a source finding algorithm fails to detect a real source is often assumed to be related to noise, and that it is random. In this paper we test this assumption and show that whilst many sources are missed due to random noise related effects, there is also a component that is deterministic and related to the underlying algorithm. By analysing the source finding algorithms and their modes of failure we identify ways in which the algorithms could be im-
proved and use this knowledge to build an algorithm which can produce catalogues that are more complete and more reliable than those currently available.

In this paper we discuss the problem of source-finding for Stokes I continuum radio emission in the context of next generation radio imaging surveys. We will not deal directly with the additional complications introduced by spectral line data, polarization data or extended sources and diffuse emission. The focus of this paper is on upcoming surveys for ASKAP, however the results will be equally applicable to future radio surveys on other SKA pathfinder instruments such as the MWA (Lonsdale et al. 2009) and SKAMP (Adams et al. 2004), and of course the SKA itself.

In § 2 we outline the main approaches to source-finding in radio astronomy, and then in § 3 describe four of most widely used source finding packages. § 4 gives some examples of the way that source finding packages are used to create catalogues for large surveys and transient studies. § 5 describes the test data that was used in the analysis of the source finding algorithms, and § 6 describes the evaluation process. The instances in which the source finding algorithms fail to find or properly characterise sources are described in § 7. § 8 describes a new source finding algorithm, AEGEAN, which has been designed to overcome many of the problems suffered by existing source finding packages. We summarise our conclusion in § 9.

2 SOURCE-FINDING IN RADIO ASTRONOMY

In a broad sense, source finding in radio images involves finding pixels that contain information about an astronomical source. Most approaches to source finding in radio astronomy follow a similar method: (i) background estimation and subtraction; (ii) source identification; (iii) source characterisation; and (iv) cataloguing. In this section we outline the standard method taken in each of these steps.

In the discussion that follows we consider a source to be a signal of astronomical importance that can be well modeled by an elliptical Gaussian. By this definition a radio galaxy with a typical core/jet morphology would be made up of three sources, one for the jet and each of the lobes. The grouping of multiple sources into a single object of interest (like a core/jet radio galaxy) is not in the realm of source finding or classification as it relies on contextual information to make such an association.

2.1 Background estimation and subtraction

The first step in source finding is determining which parts of the image belong to sources and which belong to the background (e.g., Huyvn et al. 2011). The most common way in which this separation is achieved is to set a flux threshold that divides pixels in to background or source pixels. This process is referred to as thresholding.

A straightforward case would involve a background that is dominated by thermal noise, which is without structure and is constant across the entire image. In such a case a single threshold value can be chosen that will result in all sources above that threshold being detected, and some small number of false detections. A varying background can be accounted for by calculating the mean and rms noise in local sub-regions, which is then used to normalize the image before applying a uniform threshold in signal-to-noise. The selection of a threshold limit is often a balance between detecting as many real sources as possible and minimising the number of false detections. Typically a $5\sigma$ threshold limit is used in a blind survey, with higher or lower limits chosen for larger or smaller regions of sky.

False detection rate (FDR) analysis (Hopkins et al. 2002) determines the threshold limit that will result in a number of falsely detected pixels that is lower than some user defined limit.

In cases where the background has structure, an image filter must be used to remove the background structure before the source-finding stage. The way in which the background structure is removed depends on the cause and type of structure that is present. A common example is diffuse emission in the galactic plane, with compact sources embedded within. A discussion of background filtering techniques is beyond the scope of this paper, and in our analysis we assume the images have been pre-processed and are free of background structure. For an evaluation of background estimation see Huyvn et al. (2011).

2.2 Source Identification

Source identification is the process by which pixels that are above a given threshold are grouped into contiguous groups called islands. Each island corresponds to one or more sources of interest. The process of finding sources is complete at this stage. The format of the catalogue is just a list of pixels that belong to each of the islands, which is not of general astronomical utility. Source characterisation is required to convert these islands of pixels into a more useful form.

2.3 Source Characterisation

Source characterisation involves measuring the properties of each source, for example the total flux and angular size. The best source characterisation method is strongly dependent on the nature of the sources that are to be studied. Point sources, by definition, have the shape of the point-spread-function (PSF) of an image, making the PSF shape important in the characterisation process. Images that are produced from radio synthesis observations have been deconvolved and the complicated PSF of the instrument has been replaced with an appropriately scaled Gaussian. Observations with sufficient $u, v$ coverage will do not need to be deconvolved as they have a PSF that is already nearly a Gaussian. In either case, compact sources will appear as Gaussian, and so an island of pixels can be characterised by a set of Gaussian components.

In lower resolution radio surveys such as the NVSS (45 pc) (Condon et al. 1998) and SUMSS (45 × 45 arcsec) (Mauch et al. 2003), a majority of objects are unresolved and can be characterised by a single Gaussian. However, in higher resolution surveys such as FIRST (5 arcsec) (Becker et al. 1993), a significant fraction of the sources are partially extended or have multiple components, and so multiple Gaussians are required to represent them.
Fitting a number of Gaussian components to an island of pixels is straightforward ([Condon 1997]), but is highly sensitive to the choice of initial parameters. Gaussian fitting can converge to unrealistic or non-optimal parameters due to the many local minima in the difference function. Effective multiple Gaussian fitting requires two things: an intelligent estimate of the starting parameters, and sensible constraints on these parameters. None of the widely used source-finding packages have an algorithm for robustly estimating initial parameters for a multiple Gaussian fit.

Two approaches have been developed which try to address the difficulty of obtaining accurate initial parameters for multiple Gaussian fitting: de-blending, and iterative fitting. A de-blending based approach breaks an island into multiple sub-islands, each of which is fit with a single component. In an iterative fitting approach, the difference between the image data and the fitted model (the fitting residual) is evaluated in order to determine weather an extra component is required. This analysis will repeat until an acceptable fit is achieved, or a limit on the number of components has been reached. De-blending and iterative fitting are both susceptible to source fragmentation, whereby a single true source is erroneously represented by multiple components.

Once each island of pixels has been characterised the fitting parameters are catalogued.

2.4 Cataloguing

The final stage in source finding is extracting the source parameters and forming a catalogue of objects in the field.

A catalogue should contain an appropriate listing of every parameter that was fit, along with the associated uncertainties. In addition to the fitted parameters, a source finding algorithm should report instances where the source characterisation stage was inadequate or failed. By reporting sources that were not well fit, a catalogue can remain complete despite having measured some source parameters incorrectly. Poorly fit sources can easily be re-measured, whereas excluded sources are missed forever. If it is not possible to construct a reasonable facsimile of the true sky using only the information provided in the source catalogue then the source finding process has not been successful.

3 SOURCE-FINDING PACKAGES AND THEIR ALGORITHMS

Most of the major source-finding packages in astronomy are based on a few common algorithms. In this section we outline the features of these packages.

Source finding packages that rely on wavelet analysis were not considered in this work as none of the most widely used source finding packages rely on wavelet analysis.

3.1 SExtractor

SExtractor (SE; [Bertin & Arnouts 1996]) was developed for use on optical images from scanned plates. The speed and ease of use of SExtractor has made it a popular choice for radio astronomy despite its optical astronomy origins. SExtractor is a stand alone package for Unix-like operating systems.

The source finding and characterisation process that SExtractor follows can be modified via an extensive parameter file. For this work the following parameters were used:

- DETECT_MINAREA = 5
- THRESH_TYPE = ABSOLUTE
- DETECT_THRESH = 125µJy
- ANALYSIS_THRESH = 75µJy
- MASK_TYPE = CORRECT
- BACK_SIZE = 400
- BACK_FILTERSIZE = 3

The first four parameters instruct SExtractor to detect all sources with a peak pixel brighter than $5\sigma = 125\mu$Jy/beam. The source characterisation is then carried out on islands of pixels that are brighter than $3\sigma = 75\mu$Jy/beam that contain at least 5 pixels. The final three parameters ensure that the measured flux of a source is corrected for the effects of nearby sources, and that the background is estimated using a box of $3 \times 400$ pixels on a side. This large background size results in a background that is less than $1\mu$Jy for each of the tested images. The parameters DEBLEND_NTHRESH and DEBLEND_MINCONT are used by SE in the source characterisation stage, when deciding how many components are contained within an island of pixels. The ability of SE to characterize sources was found to be insensitive to these parameters for the simulated images used in this work.

3.2 IMSAD

Image Search and Destroy (IMSAD) is an image based source finding algorithm in MIRIAD ([Sault et al. 1995]). The threshold is user-specified either as an absolute flux level or as a signal to noise ratio (SNR) with the background noise determined from a histogram of pixel values. Only pixels that are brighter than the threshold are used in the fitting process. For the analysis presented in this work we specify a threshold of $5\sigma = 125\mu$Jy/beam. IMSAD performs a single Gaussian fit to each island of pixels.

3.3 Selavy

Selavy is the source finding package that is being developed by ASKAPsoft as part of the data processing pipeline for ASKAP. Selavy is a source finding package that is able to work with spectral cubes and continuum images, and includes a number of different algorithms and approaches to source finding. Selavy is related to the publicly available Duchamp software ([Whiting, 2012, MNRAS, in press]). Selavy is a version of the Duchamp software that has been integrated into the ASKAPsoft architecture to run on a highly parallel system with distributed resources. In the context of compact continuum source finding the only difference between Selavy and Duchamp is that Selavy is able to parameterize and island of pixels with multiple Gaussian components. Selavy was given a threshold of $5\sigma = 125\mu$Jy/beam for source detection.

1 http://www.atnf.csiro.au/people/Matthew.Whiting/Duchamp
3.4 SFIND

SFIND (Hopkins et al. 2002) is implemented in MIRIAD and uses FDR analysis to set the detection threshold. Source characterisation is performed using the same Gaussian fitting subroutine as that use by the MIRIAD task imefit.

A varying background is calculated by SFIND by dividing the image into sub-regions of (user defined) size, and measuring the mean and rms of each region. In an image which contains a high density of sources, or sub-regions which contain a particularly bright or extended source, the calculated mean and rms will be contaminated by the sources. For sub-regions where this occurs the result is a mean and rms value that is significantly different from the adjacent sub-regions, which can cause sources on the boundaries to be normalised such that their shape and flux distribution are not preserved. For an image which is constructed to have a zero mean and constant rms, these contamination effects can be largely removed by setting the size of the sub-regions to be larger than the given image.

The rejection of sources which fail to be fit with a Gaussian rejects many instances of sources that have very few pixels. This has the effect of further decreasing the false detection rate for the catalogue, since a false positive source can cause sources on the boundaries to be normalised such that their shape and flux distribution are not preserved. For an image which is constructed to have a zero mean and constant rms, these contamination effects can be largely removed by setting the size of the sub-regions to be larger than the given image.

In this work we selected the sub-regions to be larger than the given image, and adjusted the FDR parameter until the automatically selected threshold was at \(5\sigma = 125\mu\text{Jy/beam}\).

3.5 FloodFill

FloodFill is an algorithm which performs the second stage of source finding, separating the foreground from the background pixels, and grouping them into islands that are then passed on to the source characterisation stage. We describe FloodFill as implemented in the new source finding algorithm, AEGEAN, which is described in Hancock et al. (2011, in prep). Although used by Murphy et al. (2007), the details of the algorithm have not been described in the astronomical literature (although see Roerdink & Meijster 2001).

FloodFill takes an image and two thresholds (\(\sigma_s\) and \(\sigma_f\), with \(\sigma_s \geq \sigma_f\)). Pixels that are above the seed threshold \(\sigma_s\) are used to seed an island, whilst pixels that are above the flood threshold \(\sigma_f\) are used to grow an island. Given a single pixel above \(\sigma_s\), FloodFill considers all the adjacent pixels. Adjacent pixels that are above \(\sigma_f\) are added to the island and pixels adjacent to these are then considered. This iterative process is continued until all adjacent pixels have been considered. The operation of FloodFill is demonstrated in a simplistic ‘image’ in Figure 1. In panel A the brightest pixel in the image has been chosen to seed the island, and is coloured yellow. The adjacent pixels are coloured cyan. In panel B the pixels that are adjacent to the seeding pixel are added to the island as they are brighter than \(\sigma_f = 4\). Pixels adjacent to the island are now considered. The process is repeated in panel C. In panel D some of the adjacent pixels have been rejected so the search for new pixels halts. In panel E there are no longer any pixels above the seed limiting of \(\sigma_s = 5\) so all remaining pixels are flagged as background pixels (panel F).

The operation of FloodFill is invariant to changes in the order in which the seed pixels are chosen. The output of FloodFill is a disjoint list of islands, each of which contains contiguous pixels that are above the \(\sigma_f\) limit. FloodFill does not perform any source characterisation, although it is able to report the flux of an island of pixels by summing the pixel intensities. The fluxes that are reported by FloodFill have a positive bias which can be corrected as described by Hales et al. (2011, in prep).

3.6 AEGEAN

FloodFill forms the basis for two new source finding algorithms: BLOBCAT (Hales et al. 2011, in prep) and AEGEAN. Both algorithms begin with a set of islands identified by FloodFill but characterise these islands differently. The BLOBCAT program characterises each island of pixels without assuming a particular source structure, where as AEGEAN assumes a compact source structure in order to fit multiple components to each island. Here we outline the AEGEAN algorithm, with a detailed description differed to §7.

The AEGEAN algorithm has been implemented in Python and uses FloodFill to create a list of islands of pixels. AEGEAN was set to use a single background threshold of \(5\sigma\) to seed the islands, and a flood threshold of \(4\sigma\) to grow
the islands. This threshold was set to $5\sigma = 125\mu \text{Jy/beam}$ so that we are detecting sources above an SNR of 5.

AEGEAN uses a curvature map to decide how many Gaussian components should be fit to each island of pixels, and the initial parameters for each component. A Python implementation of the MPFit library is used to fit the Gaussian components with appropriate constraints. Each island of pixels is thus characterised by at least one Gaussian component.

### 3.7 Source finding in radio surveys

The process of creating a catalogue of sources from survey images involves more than running one of the source finding packages described in §3. Since the observing strategy, hardware and data reduction techniques can vary widely between surveys, standard source finding packages are typically used only as a starting point for the creation of a source catalogue. The time required to carry out the observations for a large area sky survey is typically spread over multiple years. This prolonged observing schedule is usually accompanied by multiple iterations of calibration, data reduction and source detection, so that by the time the final observations are complete it is possible to produce a survey catalogue using a source finding pipeline that has been refined over many years.

The NRAO Very Large Array (VLA) Sky Survey (NVSS, Condon et al. 1998), drew upon observations from 1993-1996, during which time the AIPS source finding routine SAD was modified to create VSAD. The survey strategy for the NVSS was devised to give noise and sidelobe characteristics that were both low, and consistent across the sky. The configuration of the VLA was varied across the sky to ensure a consistent resolution throughout the survey. The survey strategy was thus designed to produce images that were nearly uniform across the sky, making the task of source finding as easy as possible. The completeness and reliability of the NVSS catalogue was improved in the years subsequent to the completion of the survey with the final stable release in 2002.

The Sydney University Molonglo Sky Survey (SUMSS, Mauch et al. 2003) and Molonglo Galactic Plane Survey (MGPS-2, Murphy et al. 2007) both used the source finding package VSAD, however the single purely East-West configuration of the telescope meant that the resolution varied with declination, and the regularly spaced feeds produced many image artefacts. The changing resolution and image artefacts meant that the source finding algorithm produced many false detections. The image artefacts appeared as radial spokes or arcs around bright sources. In order to rid the source catalogue of falsely detected sources, a machine learning algorithm was implemented (Mauch et al. 2003; Murphy et al. 2007). The machine learning algorithm was able to discriminate between real and false sources, but required substantial training to achieve high completeness and reliability.

An archival transients survey has recently been completed using the data from the SUMSS survey (Bannister et al. 2011). In an archival search spanning 20 years of observations, the need for a fast source detection pipeline is not important, as fast transients will not be detected, and slow transients will remain visible for years to come. In the Bannister et al. (2011) survey, regions of sky with multiple observations were extracted from the archival SUMSS data. These regions of sky were analysed for sources which either changed significantly in flux, or which were detected in only a subset of the images. The SFRN package was used to detect sources, which were then remeasured using the Miriad routine imfit. A complication that was encountered in the analysis of the SUMSS data, was the contamination of candidate source lists due to source finding errors. False positive detections and missed real sources both appear as sources which are only detected in a subset of all the images, and thus appear to be transient sources. The light curve of each transient event therefore needed to be double checked in order to remove such occurrences.

A similar transient detection project was carried out with new observations from the Allen Telescope Array, in the ATA Transients Survey (ATATS, Croft et al. 2011). Side-lobe contamination in the ATA images is much lower than that in the SUMSS images used in the Bannister et al. (2011) study, however falsely detected sources in the individual images still resulted in false transient detections and required further processing to remove.

The process of finding sources and creating a catalogue extends beyond the operation of a source finding package and has previously required substantial manual intervention. The next generation of telescopes, particularly the dedicated survey instruments, will be able to complete observations on a much shorter time scale than current generation telescopes, and thus the time spent creating the refining the source catalogue will become a larger fraction of the total effective survey time. Source finding packages that are able to produce more accurate, complete and reliable catalogues will provide a better starting point for the final version of the survey catalogue.

### 4 TEST DATA

We used a simulated data set to evaluate the source-finding algorithms described in §3. A simulated data set has the advantage that we are able to control the image properties (such as rms noise) and that we know the input catalogue.

Matching recovered sources with a true list of expected sources is an important part of the analysis presented in this paper. With any real data set, the list of expected sources comes with some degree of uncertainty, in that these lists are recovered from incomplete and noisy reconstructions of the radio sky. To avoid such uncertainties we generated a master catalogue of sources, which was then used to create a simulated image of the sky. With absolute control over the input catalogue and image characteristics, we are able to make more definitive statements about the quality of the catalogues that are produced.

The master source catalogue was generated with the following constraints:

(i) Fluxes: The source peak flux are distributed as $N(S) \propto S^{-2.3}$, and within the range (25 $\mu$Jy, 10 Jy).

2 code.google.com/p/agpy/source/browse/trunk/mpfit/mpfit.py revision 235
(ii) Positions: Sources were randomly distributed in space within one of ten regions of sky similar to that in Figure 2. Source clustering was not considered.

(iii) Morphologies: The major and minor axes of each source were randomly distributed in the range $0 - 52''$ with position angles in the range $(-90\ deg, +90\ deg)$.

A simulated sky image was created, which contained each of the sources in the input catalogue. The image has a $30''$ synthesized beam, and a $25\mu Jy/\text{beam}$ rms Gaussian background noise. The sources were injected with a peak flux and morphology as listed in the catalogue. The size of the image is 4801x4801 pixels with a scale of $6''$ per pixel, resulting in a synthesised beam sampling of 5 pixels per beam. Regions of sky exterior to the catalogue contain noise but no sources.

The simulated data-set can be found online at www.physics.usyd.edu.au/~hancock/simulations

5 SOURCE-FINDING EVALUATION

The source finding packages described in §3 were used to generate a catalogue of sources from the simulated images. Each source finding package was run with a 5σ threshold. In the case of SFIND, the FDR was chosen so that the resulting threshold was equal to 5σ.

The source finding algorithms were evaluated by comparing these catalogues with the input source catalogue. Three standard metrics that have been used in the comparison of catalogues, and hence source finders, are the completeness, reliability, and flux distribution, as defined and discussed in §5.1 - §5.5 below.

5.1 Cross matching of catalogues

Much of the analysis that will be discussed in §5.2 - §5.5 relies on the cross-identification of sources from two catalogues. A common criterion for accepting cross-identifications between catalogues is to choose the association with the smallest sky separation, up to a maximum matching radius. To decrease the chances of false associations we also consider the flux of the source when choosing between multiple matches within a matching radius of $30''$. The distance in phase space, $D$, is given by:

$$-\log(D) = \frac{(\alpha_1 - \alpha_2)^2}{\sigma^2_{\alpha}} + \frac{(\delta_1 - \delta_2)^2}{\sigma^2_{\delta}} + \frac{(S_1 - S_2)^2}{\sigma^2_{S}}$$

where $(\alpha, \delta)$ are (RA,DEC), $S$ is the flux, and $\sigma_{\alpha} = \sigma_{\delta} = 30''$ is the size of the convolving beam, and $\sigma_{S} = 25\mu Jy/\text{beam}$ is the image rms noise.

5.2 Flux Distribution

The analysis of the flux distribution of a catalogue does not require catalogues to be cross-matched. Since the input source catalogue was constructed with a particular flux distribution, we should expect to see this distribution replicated in the output catalogues. Figure 3 shows the flux distribution for each of the source finders compared to the input distribution. Except for Selavy, each of the catalogues have a flux distribution that is consistent with the input catalogue.

An excess of sources can be a sign of spurious detections, whilst a lack of sources can be due to incompleteness. If a source finding algorithm has a flux distribution that deviates from the ideal case, it indicates that something is wrong however the cause of the problem cannot be identified from this graph alone. Selavy has around double the number of sources at all flux levels as it suffers from source fragmentation. Since the fragmented components are close to the true position of the original source, the completeness and reliability of Selavy are only partly compromised.

5.3 Completeness

The completeness of a catalogue at a flux $S_0$ is often defined as the fraction of real sources with true flux $S \geq S_0$ that are contained within the catalogue. In practice the completeness is measured as the number of sources with a measured flux $S \geq S_0$ that are contained within the catalogue. The two measures are comparable at large SNR, but when the SNR is $\sim 5$ the flux of a source can be in error by $\sim 20\%$. The completeness relative to the measured source fluxes is also effected by Eddington bias, whereas the completeness relative to the true source fluxes is not.

The completeness of a source finder was determined by matching the simulated catalogue with each of the source finding catalogues. The completeness of a catalogue at a flux $S_0$ is then the fraction of real sources of flux greater than $S_0$ which are contained within the given catalogue. Figure 4 shows completeness as a function of injected SNR for each of the source finders. Plotted alongside each of the completeness curves is a theoretical expectation of completeness for comparison. The expected completeness has been determined by taking each of the sources in the input catalogue and calculating the probability that it will be seen at a particular flux level, given the known rms in the image. The expected completeness is calculated as

![Figure 3. The source count distribution of the catalogued sources. The true source count distribution is shown as a dotted line. Selavy consistently reports twice the true number of sources.](image_url)
Figure 2. Simulated image of the sky. The black line delineates the region of sky containing the injected sources. The colour bar ranges from $-5\sigma$ to $33\sigma$.

\[
C(S_0) = \frac{\sum S P(S > S_0)}{\sum S > S_0 N(S)} \tag{2}
\]

\[
P(S > S_0) = \frac{1}{\sigma} \sqrt{\frac{4 \log 2}{\pi}} \int_{S_0}^{\infty} e^{-4 \log 2 \left( \frac{S - S_0}{\sigma} \right)^2} dS' \tag{3}
\]

\[
= \frac{1}{2} \text{Erfc} \left( \frac{\sqrt{4 \log 2 (S_0 - S)}}{\sigma} \right)
\]

where $P(S > S_0)$ is the probability that a source of flux $S$ will be seen at a flux greater than $S_0$ after noise has been included, and $N(S)dS$ is the number of sources with flux between $S$ and $S + dS$. Erfc is the complementary error function. At SNR $> 6$ all of the source finding packages produce catalogues that are greater than 99% complete. The high completeness is due to, and responsible for, the widespread use of the given source finders. The different levels of completeness shown in Figure 4 is a direct result of the source finding algorithms implemented by each of the packages. The performance of SFIND is comparable to the other source finders above an SNR of 7, but less complete below this SNR. The lower completeness is a result of SFIND’s focus on minimising the false detection rate, as is shown in Figure 5. Selavy and AEGEAN are the most complete source
finding packages at all SNRs, however Selavy achieves this at a cost of an increased false detection rate (see §5.4 and Figure 4). AEGEAN is able to achieve high completeness and low false detection rate at all SNRs. The completeness of each of the source finding packages is summarised in Table 1.

5.4 False Detection Rate

The false detection rate (FDR) of a source finding package at a flux $S_0$, is defined as the fraction of catalogued sources with $S \geq S_0$ which are not identified with a real source. The FDR of a source finder was determined by matching the resulting catalogue with the simulated source list. Catalogued sources which are not within $30''$ of a true sources are considered false detections. The false detection rate of a source finding algorithm is related to the commonly used metric of reliability by:

$$\text{FDR} + \text{Reliability} = 100\%$$  \hspace{1cm} (4)

In Figure 5 the FDR is plotted as a function of SNR for each of the source finding packages. Substituting a flux of $S = 0.1 uJy$ into equation 3 and considering the area of sky covered by the simulated images we expect that there is less than one false detection due to random chance. Thus an ideal source finding algorithm should have an FDR of zero. The > 1% FDR peaks shown in Figure 5 (especially for IMSAD) are due to islands of multiple sources that have not been properly characterised. SExtractor, IMSAD and Selavy have a higher false detection rate than SFIND and AEGEAN, as the former are not able to accurately characterise islands of pixels.

The single sources that are fragmented into multiple sources by Selavy often have positions that are close enough to the true position that they are registered as false detections. This is evident in Figure 5.

IMSAD suffers from the reverse problem to Selavy, in that it will never break islands into multiple components even when they contain multiple sources. The position that is reported by IMSAD in such situations can be sufficiently far from the true position that these islands are registered as false detections. All of the false detections for IMSAD above an SNR of 20 in Figure 5 are due to this flaw.

The reliability of each of the source finding packages is summarised in Table 1.

5.5 Measured parameter correctness

For all measured catalogue sources that were identified with a true source it is possible to compare the measured parameters to the known true values.

Figure 6 shows the median absolute deviation (MAD) in position, as a function of SNR, for each of the source finding algorithms. The MAD is calculated for each SNR bin and is not a cumulative measure. An ideal source finding algorithm will have a typical error in position that is proportional to $C / \text{SNR}^2$ where $C$ is a constant that depends on the source characteristics.
on the morphology of the source and the convolving beam (see Condon (1997) for detailed a calculation). The MAD in position of an ideal source finding algorithm is calculated semi-analytically by assuming that each source in the input catalog has measurement error of $C/\text{SNR}^2$. This ideal curve is plotted in Figure 6.

As is expected, the accuracy with which a source position can be measured increases with flux, and is in agreement with the performance of an ideal Gaussian fitting routine, which is shown as a dotted curve in Figure 6. The deviations from ideal behaviour that can be seen in Figure 6 for the various source finders at high SNR are artifacts of the reporting accuracy of the packages. For example, IMSAD reports positions to a resolution of 0.1″ and therefore cannot achieve a median absolute deviation in position better than $\sim 0.1″$. SFIND has similar problems at an SNR of $\gtrsim 3000$. The median absolute position deviation for AEGEAN and Selavy will also deviate from ideal, but at an SNR in excess of the 40,000 reported in Figure 6. SExtractor does not use Gaussian fitting to characterise source positions and therefore does not perform as well as the ideal at SNR greater than 50. At an SNR of $< 100$ Selavy has a median absolute position deviation that is higher than the ideal. This is because of source fragmentation.

Figure 7 shows the MAD in flux as a fraction of total flux, as a function of SNR. Again the ideal behavior of a Gaussian fitter has been shown by a dashed curve. Overall the source finding packages report fluxes that are consistent with the expected ideal Gaussian fit, the exceptions being SExtractor above an SNR of 50, and Selavy at an SNR below 50. SExtractor deviates from the ideal and has a plateau at 1% flux accuracy. In this work we use the corrected isophotal fluxes (FLUX_ISOCOR) from SExtractor. Of all the methods that are available for measuring fluxes in radio synthesis images, the corrected isophotal fluxes was found to be the most accurate. Selavy deviates from the ideal case and has a flux accuracy of about 1/2 of ideal. The cause of this deviation is source fragmentation in which each component has only a fraction of the total true flux (see §5.2 and Figure 4).

5.6 Initial evaluation summary

Each of the source finding algorithms conforms to a high standard of completeness and reliability, and is able to produce a robust catalogue of a statistically large number of sources, with accurate measurements of position and flux. The completeness of the AEGEAN source finding package is as good or better than any of the other packages, and has been achieved without sacrificing reliability. In the context of next generation radio surveys, we are interested in the small differences between each of these source finders, and in how to optimize the approach to avoid even the residual small level of incompleteness and false detection rate. In surveys such as EMU (Norris et al. 2011), with an expected 70 million sources, an FDR of even 1% translates into 700,000 false sources. This clearly has an impact on the study of rare or unusual behaviour. In particular we are interested in how the source finding algorithm affects the final output catalogue at a level that is far more detailed than previously explored. With this in mind we now delve into specific cases in which existing source finding packages fail.

6 MISSED SOURCES

We are now at the stage where we can consider the real sources that were missed by the source finding packages, as well as the false detections that these programs generate. There are two populations of sources that are missed by one or more of the source finding packages as will be discussed in §6.1 below.

6.1 Isolated faint sources

In the simulated image, for which no clustering was taken into account, 99.5% of the islands contained a single source. The first population of sources that was not well detected by the source finding algorithms are isolated faint sources. These sources have a true flux greater than the threshold, but have few or no pixels above the threshold
due to the addition of noise. SFIND and SExtractor require an island to have more than some minimum number of pixels for it to be considered a candidate source. IMSAD, Selavy and AEGEAN have no such requirement. The number of sources that are not seen in a catalogue due to the effects of noise can be calculated directly and is essentially the inverse problem to that of false detections. A correction can be applied to any statistical measure extracted from the catalogue in order to account for these missed sources. The only way to recover all sources with a true flux above a given limit, is to have a threshold that is well below this limit, either by producing a more sensitive image, or by accepting a larger number of false detections. Since this noise affected population of sources cannot be reduced by an improved source finding algorithm, and can be accounted for in a statistically robust way, we will consider this population to be non-problematic.

6.2 Islands with multiple sources

The second population of sources that is not well detected by the source finding packages are the sources that are within an island of pixels that contains multiple components. Examples of such islands are shown in Figures 8, 9, and 10. If a source finding algorithm is unable to correctly characterise multiple sources within an island, some or all of these sources will be missed. There are two approaches used by the tested algorithms to extract multiple sources from an island of pixels – iterative fitting and de-blending. Each of these approaches can fail to characterise an island of sources for different reasons, and will now be discussed in detail.

6.2.1 Iterative fitting

The first approach to characterising an island of multiple components is an iterative one which relies on the notion of a fitting residual. The fitting residual is the difference between the data and the model fit. In the iterative approach a single Gaussian is fit to the island and the fitting residual is inspected. If the fitting residual meets some criterion then the fit is considered to be ‘good’ and a single source is reported. If the residual is ‘poor’ then the fit is redone with an extra component. Once either the fitting residual is found to be ‘good’ or some maximum number of components has been fit, the iteration stops and the extracted sources are reported. A disadvantage of this method is that if the number of allowed Gaussians ($n$) is poorly chosen, islands containing single faint sources can have a ‘better’ fitting residual when fit by multiple components, and source fragmentation occurs. When a source is fragmented it is difficult to extract the overall source parameters from the multiple Gaussians that were used in the fitting of the source. In particular the source flux is not simply the sum of the flux of the fragments. If the chosen value of $n$ is too small then not all of the sources within an island will be characterised. These uncharacterised sources will contaminate the fitting of the previously identified sources resulting in a poor characterisation of the island.

When the flux ratio of components within an island of pixels becomes very large, an iterative fitting approach can fail. The cause of this failure is related to the performance of an ideal Gaussian fitting routine. Figure 8 shows the fractional error in measuring the amplitude of a Gaussian. For high SNR sources, the absolute flux error can be orders of magnitude below the rms image noise, so it may be expected that the maximum flux in the fitting residual should also be at or below the rms image noise. However the main contribution to the flux seen in the fitting residual is not from amplitude errors but from errors in estimating the FWHM of the source.

The amplitude difference between a (1D) Gaussian of amplitude $A$ and FWHM of $\theta = 2\sqrt{2\log 2}\sigma$ and a second Gaussian of identical amplitude $A$ and FWHM of $\theta' = \theta + \Delta\theta$, is given by $F(x)$:

$$F(x) = A \left( e^{-\frac{x^2 + 2\Delta\theta^2}{\theta'^2}} - e^{-\frac{x^2 + 2\Delta\theta^2}{\theta^2}} \right),$$

which has maxima at

$$x_0^2 = \ln \frac{\theta'}{2\ln 2} \left( \frac{\theta'^2 - \theta'^2}{\theta'^2 - \theta^2} \right).$$

As a fraction of the true flux, the maximum residual is then

$$\frac{F(x_0)}{A} = \left( \frac{2\Delta\theta}{\theta} \right) \times \left( 1 + \frac{2\Delta\theta}{\theta} \right)^{\frac{x_0}{\Delta\theta}}$$

The typical error in the measurement of $\theta$ is $\sigma$ (Condon 1997)

$$\frac{\Delta\theta}{\theta} = \frac{\mu(\theta)}{\theta} \approx \frac{\sigma}{A}.$$
SNR of $F(x_0)/\sigma$ will not be detected by an iterative fitting method. The fitting residual exceeds $5\sigma$ at an SNR as low as 11. Therefore, even an ideal Gaussian fitting routine will miss $5\sigma$ sources that are within the same island as a source of $\geq 11\sigma$ if an iterative approach is taken. If two Gaussian components are fit to an island of pixels such as that shown in Figure 10 and the positions are left unconstrained, the fainter component will migrate towards one of the maxima in the fitting residual. The brighter source will then be characterised by two Gaussians, and the fainter source by none. The final result, is that neither of the sources will be well characterised. It is therefore essential that a source finding algorithm has some method for determining the number of Gaussian components within an island, as well as a way to stop the fitting process from mis-characterising the two sources. A process called sectioning or de-blending is a common method.

6.2.2 Sectioning or de-blending

A second approach to characterising islands with multiple sources is to use the distribution of flux within the island to determine the number of components to be fit, and then fit the components. This approach relies on some a priori knowledge of what a source looks like to break an island into components. SFIND, SE, and AEGERN all use a form of sectioning to generate an initial estimate of the number of sources to be fit, as well as the starting parameters.

It is possible to create a statistical measure that will account for the number of sources that are missed because there are multiple sources within an island of pixels. This would, however, require detailed knowledge of the source finding algorithm, the flux distribution of the source population, and the flux dependent two-point correlation function. The complexity of this calculation means that it is never computed and sometimes not even considered. Since many variable phenomena appear in or near known sources (e.g., radio supernovae in galaxies, extreme scattering events within our own Galaxy, and more), an inability to accurately characterise this population of sources will make it difficult or impossible to reliably detect and characterise many variable events.

7 THE NEW SOURCE FINDING PROGRAM: AEGERN

With an understanding of how the underlying algorithms affect a source finder’s ability to find and accurately characterise islands of pixels, we have created a new source finding algorithm. The goal of the new algorithm is to incorporate the reliability and completeness performance of the packages studied in § 3, whilst improving on their ability to characterise islands of pixels. The source finding algorithm is called AEGERN, as it deals with many islands.

As background estimation and subtraction are not part of the focus of this work, AEGERN has been designed with only a simple background estimation algorithm. For the analysis presented, AEGERN was run with a detection threshold of 125\mu Jy/beam. AEGERN uses the FloodFill algorithm described in § 6.1 to create islands of pixels.

AEGERN makes use of the notion of a single curvature
map to characterise an island of pixels. The curvature $\kappa$ of a function $f(x)$ is given by:

$$\kappa = \frac{f''}{(1 + f'^2)^{3/2}}$$  \hspace{1cm} (10)\hspace{1cm} \text{(Reilly, 1982)}.$$

For a Gaussian with a FWHM of $k$ pixels,

$$f'(x) = \frac{-16 \ln 2}{k^2} e^{-\frac{28 \ln 2}{k^2} x^2},$$  \hspace{1cm} (11)$$

so that $f''$ has a maxima at $x = k/\sqrt{2}$, and

$$f'' \leq \frac{1}{k^2} \frac{(\ln 2)^2}{2^9}.$$  \hspace{1cm} (12)$$

For a Gaussian with $k \geq 1$, $f'' \ll 1$ and we can approximate

$$\kappa \simeq f''.$$  \hspace{1cm} (13)$$

The curvature of a surface in a particular direction can be defined using Equation 12, where the differentiation is along a unit vector in the chosen direction. Molinari et al. (2011) calculate the curvature of their input image in four image directions in order assist their source finding and characterisation. We combine these four curvature measurements to calculate the mean curvature of an image. For an image convolved with a Gaussian with a FWHM of $k$ pixels, the (mean) curvature, $\bar{\kappa}$ is equal to the mean of $\kappa$ calculated in any two orthogonal directions (Reilly, 1982). The discrete 2D Laplacian kernel

$$L_{xy}^2 = \begin{bmatrix} 1 & 1 & 1 \\ 1 & -8 & 1 \\ 1 & 1 & 1 \end{bmatrix},$$  \hspace{1cm} (14)$$

calculates the sum of the second derivatives in four directions. Convolving the input image with $L_{xy}^2$ will therefore produce a map of $2\bar{\kappa}$ - a single curvature map.

Islands of pixels are fit with multiple Gaussian components. The number of components to be fit is determined from a curvature map. The curvature map will be negative around local maxima. Groups of contiguous pixels that have negative curvature and fluxes above the threshold are called summits. An island of pixels will contain one or more summits. Aegean fits one component per summit, with the parameters of each of the components are taken from the corresponding summit. The position and flux are initially set to be equal to the brightest pixel within a summit, and the shape parameters (major/minor axis and position angle) are set to be the same as the convolving beam. Figure 12 shows an example of two islands that contain multiple sources with the island boundaries and regions of negative curvature delimited. In the example in the left panel of Figure 12 there are three regions of negative curvature that are completely within the green island. This island is fit with three Gaussians. In the example in the right panel of Figure 12 there are two regions of negative curvature that overlap with the island of pixels. One component is contained entirely within the island, whilst the other is only partly within the island. Only the region of negative curvature that is within the green island is considered when estimating the initial parameters of the components. Both of the islands depicted in Figure 12 contains a source that is bright enough that the expected fitting residual would be brighter than any of the other components within the island, and therefore an iterative fitting approach would only fit a single component (see §6.2.1). Since the island of pixels in the right panel of Figure 12 has two summits, Aegean is able to accurately detect and characterise both components. Islands of pixels that contain only a single source have only a single summit and are fit with a single component.

To avoid faint components migrating to the fitting residual of brighter components, the position of each of the components is constrained to be within the corresponding summit. The flux of each component must be greater than $5\sigma$. For low SNR sources, the true flux can be significantly different from the intensity of the brightest pixel in the summit, $S_{\text{max}}$. For high SNR sources, the noise variations are less important and beam sampling effects become more important.

For an image with a sampling rate of $k$ pixels per beam a source of flux $S$ which is located at the intersection of
therefore given by:

\[ S_{\text{max}} = S \cdot \exp \left( -\frac{\frac{\sqrt{2}}{2k}}{\theta^2} \right) \cdot \exp \left( -\frac{2\ln 2}{\theta^2} \right) \]  

where \( \theta \) is the FWHM of the source. The flux of each component is therefore constrained to be less than \( S_{\text{max}} \cdot 2\pi + 3\sigma \).

A Gaussian function has negative curvature from the centre of the source. The intensity of the peak pixel is synthesised beam, and must remain smaller than the minor axes of a component must be larger than the synthesised beam size. The major and minor axes of a component is fit with the PSF.

Figure 12. Two examples of the curvature analysis scheme. The greyscale represents the flux density map and ranges from \(-3\sigma\) (white) to \(+10\sigma\) (black). The green contour is at \(5\sigma\) and represents the island boundary. The red contours are where the curvature map changes from positive to negative. Regions surrounded by a red contour have negative curvature and are the local maxima.

four pixels will effectively be sampled \( \sqrt{2} \cdot 3/2k \) pixels from the centre of the source. The intensity of the peak pixel is therefore given by:

\[ S_{\text{max}} = S \cdot \exp \left( -\frac{\sqrt{2}}{2k} \right)^2 + 3\ln 2 \]  

\[ = S \cdot 2^{-\frac{k}{\theta^2}} \]  

Aegean makes use of a curvature image which is derived from the input image with a Laplacian transform. Using the curvature image Aegean is able to accurately determine the number of compact components within an island of pixels and produce a set of initial parameters and limits for a constrained fit of multiple elliptical Gaussians.

Aegean has been shown to produce catalogues with a 5\(\sigma\) completeness that is better than our estimation of an ideal source finder. This completeness has been achieved without sacrificing reliability, and Aegean is the most reliable of the tested algorithms. The next generation of radio surveys will be sensitive enough that \(\sim 5\%\) of the islands in the image will contain multiple components and therefore the ability to characterise such islands is of critical importance. Aegean is able to accurately characterise islands of pixels which contain multiple compact components.

We have shown that in order to improve the reliability and completeness of source catalogues it is necessary to perform constrained multiple Gaussian fitting. An accurate estimation of initial parameters and sensible constraints are both critical when multiple component Gaussian fitting is performed. We have demonstrated a method for estimating and constraining the fitting parameters which is based on the curvature of the image. We anticipate that by adopting the Aegean algorithm, the next generation of radio continuum surveys will be able to achieve more complete, reliable and accurate catalogues without relying on significant manual intervention.

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8 CONCLUSIONS

Using a simulated data set, we have assessed the performance of some widely used source finding packages, along with the ASKAPsoft source finding program Selavy. These source finding packages are found to produce complete and reliable catalogues of isolated compact sources. We identify two populations of sources that are not well detected by the source finding packages. The first population being faint sources close to the detection limit, and the second being sources which are within an island of pixels containing multiple components. Islands of pixels with multiple components are found to be poorly characterised by source finding packages that take an iterative fitting approach to characterisation. Source finding packages that estimate the number of components in an island prior to fitting are less likely to mis-characterise the island. We have developed a new source finding package, Aegean, which is able to characterise the number of components within an island of pixels more accurately than any of the other packages tested.
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