By use of the AdS/CFT correspondence on orbifolds, models are derived which can contain the standard model of particle phenomenology. It will be assumed that the theory becomes conformally invariant at a renormalization-group fixed-point in the TeV region.

1 Introduction

It is a privilege to speak at the first High-Energy Physics conference to be held in Cairo, hopefully the first of many. In this talk, only an outline of the conformality idea can be described; more detail is to be found in the references.

In particle phenomenology, the impressive success of the standard theory based on $SU(3) \times SU(2) \times U(1)$ has naturally led to the question of how to extend the theory to higher energies? One is necessarily led by weaknesses and incompleteness in the standard theory. If one extrapolates the standard theory as it stands one finds (approximate) unification of the gauge couplings at $\sim 10^{16}$ GeV. But then there is the hierarchy problem of how to explain the occurrence of the tiny dimensionless ratio $\sim 10^{-14}$ of the weak scale to the unification scale. Inclusion of gravity leads to a super-hierarchy problem of the ratio of the weak scale to the Planck scale, $\sim 10^{18}$ GeV, an even tinier $\sim 10^{-16}$. Although this is obviously a very important problem about which conformality by itself is not informative, we shall discuss first the hierarchy rather than the super-hierarchy.

There are four well-defined approaches to the hierarchy problem:

- 1. Supersymmetry
- 2. Technicolor.
- 3. Extra dimensions.
- 4. Conformality.

Supersymmetry has the advantage of rendering the hierarchy technically natural, that once the hierarchy is put in to the lagrangian it need not be re-tuned in perturbation theory. Supersymmetry predicts superpartners of all the known particles and these are predicted to be at or below a TeV scale.
if supersymmetry is related to the electroweak breaking. Inclusion of such hypothetical states improves the gauge coupling unification. On the negative side, supersymmetry does not explain the origin of the hierarchy.

*Technicolor* postulates that the Higgs boson is a composite of fermion-antifermion bound by a new (technicolor) strong dynamics at or below the TeV scale. This obviates the hierarchy problem. On the minus side, no convincing simple model of technicolor has been found.

*Extra dimensions* can have a range as large as $1/(\text{TeV})^{-1}$ and the gauge coupling unification can happen quite differently than in only four spacetime dimensions. This replaces the hierarchy problem with a different fine-tuning question of why the extra dimension is restricted to a distance corresponding to the weak interaction scale.

*Conformality* is inspired by superstring duality and assumes that the particle spectrum of the standard model is enriched such that there is a conformal fixed point of the renormalization group at the TeV scale. Above this scale the coupling do not run so the hierarchy is nullified.

Conformality is the approach followed in this paper. We shall systematically analyse the compactification of the IIB superstring on $\text{AdS}_5 \times \text{S}^5/\Gamma$ where $\Gamma$ is a discrete non-abelian group.

The duality between weak and strong coupling field theories and then between all the different superstring theories has led to a revolution in our understanding of strings. Equally profound, is the AdS/CFT duality which is the subject of the present article. This AdS/CFT duality is between string theory compactified on Anti-de-Sitter space and Conformal Field Theory.

Until very recently, the possibility of testing string theory seemed at best remote. The advent of AdS/CFTs and large-scale string compactification suggest this point of view may be too pessimistic, since both could lead to $\sim 100\text{TeV}$ evidence for strings. With this thought in mind, we are encouraged to build AdS/CFT models with realistic fermionic structure, and reduce to the standard model below $\sim 1\text{TeV}$.

Using AdS/CFT duality, one arrives at a class of gauge field theories of special recent interest. The simplest compactification of a ten-dimensional superstring on a product of an AdS space with a five-dimensional spherical manifold leads to an $\mathcal{N} = 4\text{SU}(N)$ supersymmetric gauge theory, well known to be conformally invariant. By replacing the manifold $S^5$ by an orbifold $S^5/\Gamma$ one arrives at less supersymmetries corresponding to $\mathcal{N} = 2, 1$ or 0 depending on whether $\Gamma \subset \text{SU}(2), \text{SU}(3)$, or $\not\subset \text{SU}(3)$ respectively, where $\Gamma$ is in all cases a subgroup of $\text{SU}(4) \sim \text{SO}(6)$ the isometry of the $S^5$ manifold.

It was conjectured in [1] that such $\text{SU}(N)$ gauge theories are conformal in the $N \rightarrow \infty$ limit. In [2] it was conjectured that at least a subset of the
resultant nonsupersymmetric $\mathcal{N} = 0$ theories are conformal even for finite $N$. Some first steps to check this idea were made in \cite{5}. Model-building based on abelian $\Gamma$ was studied further in \cite{6, 7, 8}, arriving in \cite{8} at an $SU(3)^7$ model based on $\Gamma = \mathbb{Z}_7$ which has three families of chiral fermions, a correct value for $\sin^2 \theta$ and a conformal scale $\sim 10$ TeV.

The case of non-abelian orbifolds bases on non-abelian $\Gamma$ has not previously been studied, partially due to the fact that it is apparently somewhat more mathematically sophisticated. However, we shall show here that it can be handled equally as systematically as the abelian case and leads to richer structures and interesting results.

In such constructions, the cancellation of chiral anomalies in the four-dimensional theory, as is necessary in extension of the standard model (e.g. \cite{9, 10}), follows from the fact that the progenitor ten-dimensional superstring theory has cancelling hexagon anomaly.

We consider all non-abelian discrete groups of order $g < 32$. These are described in detail in \cite{12, 15}. There are exactly 45 such non-abelian groups. Because the gauge group arrived at by this construction is $\otimes_i SU(N_{d_i})$ where $d_i$ are the dimensions of the irreducible representations of $\Gamma$, one can expect to arrive at models such as the Pati-Salam $SU(4) \times SU(2) \times SU(2)$ type \cite{16} by choosing $N = 2$ and combining two singlets and a doublet in the 4 of $SU(4)$. Indeed we shall show that such an accommodation of the standard model is possible by using a non-abelian $\Gamma$.

The procedures for building a model within such a conformality approach are: (1) Choose $\Gamma$; (2) Choose a proper embedding $\Gamma \subseteq SU(4)$ by assigning the components of the 4 of $SU(4)$ to irreps of $\Gamma$, while at the same time ensuring that the 6 of $SU(4)$ is real; (3) Choose $N$, in the gauge group $\otimes_i SU(N_{d_i})$. (4) Analyse the patterns of spontaneous symmetry breaking.

In the present study we shall choose $N = 2$ and aim at the gauge group $SU(4) \times SU(2) \times SU(2)$. To obtain chiral fermions, it is necessary that the 4 of $SU(4)$ be complex $\mathbf{4} \neq \mathbf{4}^*$. Actually this condition is not quite sufficient to ensure chirality in the present case because of the pseudoreality of $SU(2)$. We must ensure that the 4 is not just pseudoreal.

This last condition means that many of our 45 candidates for $\Gamma$ do not lead to chiral fermions. For example, $\Gamma = Q_{2n} \subseteq SU(2)$ has irreps of appropriate dimensionalities for our purpose but it will not sustain chiral fermions under $SU(4) \times SU(2) \times SU(2)$ because these irreps are all, like $SU(2)$, pseudoreal. Applying the rule that 4 must be neither real nor pseudoreal leaves a total of only 19 possible non-abelian discrete groups of order $g \leq 31$. The smallest group which avoids pseudoreality has order $g = 16$ but gives only two families. The technical details of our systematic search will be postponed to a future publication. Here we shall present only the simplest interesting non-abelian case which has $g = 24$ and gives three chiral families in a Pati-Salam-type

\footnote{Note that were we using $N \geq 3$ then a pseudoreal 4 would give chiral fermions.}
Before proceeding to the details of the specific $g = 24$ case, it is worth reminding the reader that the Conformal Field Theory (CFT) that it exemplifies should be free of all divergences, even logarithmic ones, if the conformality conjecture is correct, and be completely finite. Further the theory is originating from a superstring theory in a higher-dimension (ten) and contains gravity by compactification of the higher-dimensional graviton already contained in that superstring theory. In the CFT as we derive it, gravity is absent because we have not kept these graviton modes - of course, their influence on high-energy physics experiments is generally completely negligible unless the compactification scale is “large" here we shall neglect the effects of gravity.

To motivate our model it is instructive to comment on the choice of $\Gamma$ and on the choice of embedding.

If we embed only four singlets of $\Gamma$ in the 4 of $SU(4)$ then this has the effect of abelianizing $\Gamma$ and the gauge group obtained in the chiral sector of the theory is $SU(N)^q$. These cases can be interesting but have already been studied. Thus, we require at least one irrep of $\Gamma$ to have $d_i \geq 2$ in the embedding.

The only $\Gamma$ of order $g \leq 31$ with a 4 is $Z_5 \times Z_4$ and this embedding leads to a non-chiral theory. This leaves only embeddings with two singlets and a doublet, a triplet and a singlet or two doublets.

The third of these choices leads to richer structures for low order $\Gamma$. Concentrating on them shows that of the chiral models possible, those from groups of low order result in an insufficient number (below three) of chiral families.

The first group that can lead to exactly three families occurs at order $g = 24$ and is $\Gamma = Z_3 \times Q$ where $Q(\equiv Q_4)$ is the group of unit quarternions which is the smallest dicyclic group $Q_{2n}$.

There are several potential models due to the different choices for the 4 of $SU(4)$ but only the case $4 = (1\alpha, 1', 2\alpha)$ leads to three families so let us describe this in some detail:

Since $Q \times Z_3$ is a direct product group, we can write the irreps as $R_i \otimes \alpha^a$ where $R_i$ is a $Q$ irrep and $\alpha^a$ is a $Z_3$ irrep. We write $Q$ irreps as $1$, $1'$, $1''$, $1'''$, 2 while the irreps of $Z_3$ are all singlets which we call $\alpha, \alpha^2, \alpha^3 = 1$. Thus $Q \times Z_3$ has fifteen irreps in all and the gauge group will be of Pati-Salam type for $N = 2$.

If we wish to break all supersymmetry, the 4 may not contain the trivial singlet of $\Gamma$. Due to permutational symmetry among the singlets it is sufficiently general to choose $4 = (1\alpha^{a_1}, 1\alpha^{a_2}, 2\alpha^{a_3})$ with $a_1 \neq 0$.

To fix the $a_i$ we note that the scalar sector of the theory which is generated by the 6 of $SU(4)$ can be used as a constraint since the 6 is required to be real. This leads to $a_1 + a_2 = -2a_3 (\text{mod } 3)$. Up to permutations in the chiral fermion sector the most general choice is $a_1 = a_3 = +1$ and $a_2 = 0$. Hence
our choice of embedding is

\[ 4 = (1\alpha, \ 1', \ 2\alpha) \]  

(1)

with

\[ 6 = (1'\alpha, \ 2\alpha, \ 2\alpha^2, \ 1'\alpha^2) \]  

(2)

which is real as required.

We are now in a position to summarize the particle content of the theory. The fermions are given by

\[ \sum_4 4 \times R_I \]  

(3)

where the \( R_I \) are all the irreps of \( \Gamma = Q \times Z_3 \). This is:

\[ \sum_3 \left[ (2_1 \alpha^i, 2_2 \alpha^i) + (2_3 \alpha^i, 2_4 \alpha^i) + (2_2 \alpha^i, 2_1 \alpha^i) + (2_4 \alpha^i, 2_3 \alpha^i) + (4\alpha^i, \bar{4}\alpha^i) \right] \]

\[ + \sum_3 \sum_4 \left[ (2_a \alpha^i, 2_a \alpha^{i+1}) + (2_a \alpha^i, 4\alpha^{i+1}) + (\bar{4}\alpha^i, 2_a \alpha^{i+1}) \right] \]  

(4)

It is convenient to represent the chiral portions of these in a quiver diagram.

The scalars are given by

\[ \sum_6 6 \times R_I \]  

(5)

and are:

\[ \sum_3 \sum_3 \left[ (2_1 \alpha^i, 2_2 \alpha^j) + (2_2 \alpha^i, 2_1 \alpha^j) + (2_3 \alpha^i, 2_4 \alpha^j) + (2_4 \alpha^i, 2_3 \alpha^j) + (2_4 \alpha^i, 2_1 \alpha^j) + (2_2 \alpha^i, 2_3 \alpha^j) \right] \]

\[ + \sum_3 \sum_3 \left\{ \sum_4 \left[ (2_a \alpha^i, 4\alpha^j) + (\bar{4}\alpha^i, 2_a \alpha^j) \right] + (4\alpha^i, \bar{4}\alpha^j) \right\} \]  

(6)

which is easily checked to be real.

The gauge group \( SU(4)^3 \times SU(2)^{12} \) with chiral fermions of Eq.\( (4) \) and scalars of Eq.\( (6) \) is expected to acquire conformal invariance at an infra-red fixed point of the renormalization group, as discussed in \([4]\).

To begin our examination of the symmetry breaking we first observe that if we break the three \( SU(4) \)'s to the totally diagonal \( SU(4) \), then chirality in the fermionic sector is lost. To avoid this we break \( SU_1(4) \) completely and then break \( SU_\alpha(4) \times SU_\alpha(4) \) to its diagonal subgroup \( SU_D(4) \). The first of these steps can be achieved with VEVs of the form \([(4_1, 2_i \alpha^i) + h.c.] \) where
we are free to choose $b$, but $k$ must be 1 or 2 since there are no $(4_1, 2_5\alpha^k=0)$ scalars. The second step requires an $SU_D(4)$ singlet VEV from $(\mathbf{4}_\alpha, \overline{4}_\alpha)$ and/or $(\mathbf{4}_\alpha, \mathbf{4}_\alpha)$. Once we make a choice for $b$ (we take $b = 4$), the remaining chiral fermions are, in an intuitive notation:

$$\sum_{\alpha=1}^{3} \left[(2_\alpha, 1, 4_D) + (1, 2_\alpha^{-1}, \overline{4}_D)\right]$$

which has the same content as as a three family Pati-Salam model, though with a separate $SU_L(2) \times SU_R(2)$ per family.

To further reduce the symmetry we must arrange to break to a single $SU_L(2)$ and a single $SU_R(2)$. This is achieved by modifying step one where $SU_1(4)$ was broken. Consider the block diagonal decomposition of $SU_1(4)$ into $SU_{1L}(2) \times SU_{1R}(2)$. The representations $(2_\alpha, 4_1)$ and $(2_\alpha^{-1}, 4_1)$ then decompose as

$$(2_\alpha, 4_1) \rightarrow (2_\alpha, 2, 1) + (2_\alpha, 1, 2)$$

and

$$(2_\alpha^{-1}, 4_1) \rightarrow (2_\alpha^{-1}, 1, 2) + (2_\alpha^{-1}, 2, 1).$$

Now if we give VEVs of equal magnitude to the $(2_\alpha, 2, 1)$, $a = 1, 2, 3$, and equal magnitude VEVs to the $(2_\alpha^{-1}, 1, 2) a = 1, 2, 3$, we break $SU_{1L}(2) \times \prod_{\alpha=1}^{3} SU(2_\alpha)$ to a single $SU_L(2)$ and we break $SU_{1R}(2) \times \prod_{\alpha=1}^{3} SU(2_\alpha)$ to a single $SU_R(2)$. Finally, VEVs for $(2_{4\alpha}, 2, 1)$ and $(2_{4\alpha}, 1, 2)$ as well as $(2_{4\alpha^{-1}}, 2, 1)$ and $(2_{4\alpha^{-1}}, 1, 2)$ insures that both $SU(2_\alpha)$ and $SU(2_{4\alpha^{-1}})$ are broken and that only three families remain chiral. The final set of chiral fermions is then $3[(2, 1, 4) + (1, 2, 4)]$ with gauge symmetry $SU_L(2) \times SU_R(2) \times SU_D(4)$.

To achieve the final reduction to the standard model, an adjoint VEV from $(\mathbf{4}_\alpha, \mathbf{4}_\alpha)$ and/or $(\mathbf{4}_\alpha, \mathbf{4}_\alpha)$ is used to break $SU_D(4)$ to the $SU(3) \times U(1)$, and a right handed doublet is used to break $SU_R(2)$.

While this completes our analysis of symmetry breaking, it is worthwhile noting the degree of constraint imposed on the symmetry and particle content of a model as the number of irreps $N_R$ of the discrete group $\Gamma$ associated with the choice of orbifold changes. The number of gauge groups grows linearly in $N_R$, the number of scalar irreps grows roughly quadratically with $N_R$, and the chiral fermion content is highly $\Gamma$ dependent. If we require the minimal $\Gamma$ that is large enough for the model generated to contain the fermions of the standard model and have sufficient scalars to break the symmetry to that of the standard model, then $\Gamma = Q \times Z_3$ appears to be that minimal choice.

Although a decade ago the chances of testing string theory seemed at best remote, recent progress has given us hope that such tests may indeed be possible in AdS/CFTs. The model provided here demonstrates the standard model can be accommodated in these theories and suggests the possibility of a rich spectrum of new physics just around the TeV corner.
2 Gauge unification

Perhaps the most encouraging aspect of conformality is that it can replace the traditional SusyGUT unification of $\alpha_3$, $\alpha_2$ and $\alpha_1$ by a group-theoretical relationship already at the TeV scale. Above this scale there is only one independent coupling which does not run.

In abelian orbifolds, the simplest three-family model occurs for $Z_7$ if we insist on $N = 0$ for supersymmetry. As shown in this leads to the value
\[
\sin^2 \theta = \frac{3}{13} = 0.231\n\]
in excellent agreement with experiment.

In this case the gauge group at the conformality scale is $(SU(3))^7$ and one of these $SU(3)$ is the color of QCD. $SU(2)_L$ is in a diagonal subgroup of two factors and the correctly-normalized $U(1)_Y$ is the remaining four factors.

This choice is not arbitrary because $Z_7$ is the smallest abelian group giving $N = 0$ and allowing survival of three families as well as an adequate scalar sector to allow spontaneous symmetry breaking to the standard $SU(3) \times SU(2) \times U(1)$ gauge group.

Here the breaking to the standard model is most easily seen by the intermediate step of trinification with unifying semi-simple gauge group $SU(3)_C \times SU(3)_L \times SU(3)_R$.

More recently, with Mohapatra and Suh, we have shown how for the non-abelian example of we arrive at $\sin^2 \theta = 0.227$ within the context of the left-right model. This is again supportive of our approach.

In the non-abelian case the conformality gauge group is $SU(4)^3 \times SU(2)^{12}$ and is broken to the Pati-Salam group $SU(4)_C \times SU(2)_L \times SU(2)_R$ as explained in. It is remarkable that the $\sin^2 \theta$ value comes out so close to experiment for both $SU(3)_C \times SU(3)_L \times SU(3)_R$ and $SU(4)_C \times SU(2)_L \times SU(2)_R$.

Some comments on the neutrino mass spectrum are in.

Of course, the fermion hierarchy for quark and lepton masses remains challenging and it will be interesting to find whether on pushing the present approach harder any light can be shed on this - at the moment there is merely sufficient freedom in identification of the physical fermions that an arbitrary mass matrix can be accommodated. To proceed further will require a more precise identification of the physical states.
3 Summary

We have shown how AdS/CFT duality leads to a large class of models which can provide interesting extensions of the standard model of particle phenomenology. The naturally occurring $\mathcal{N} = 4$ extended supersymmetry was completely broken to $\mathcal{N} = 0$ by choice of orbifolds $S^5/\Gamma$ such that $\Gamma \not\subset SU(3)$.

In $\cite{22}$, we studied systematically all such non-abelian $\Gamma$ with order $g \leq 31$. We show how chiral fermions require that the embedding of $\Gamma$ be neither real nor pseudoreal. This reduces dramatically the number of possibilities to obtain chiral fermions. Nevertheless, many candidates for models which contain the chiral fermions of the three-family standard model were found.

However, the requirement that the spontaneous symmetry breaking down to the correct gauge symmetry of the standard model be permitted by the prescribed scalar representations eliminates most of the surviving models. We found only one allowed model based on the $\Gamma = 24/7$ orbifold. We had initially expected to find more examples in our search. The moral for model-building is interesting. Without the rigid framework of string duality the scalar sector would be arbitrarily chosen to permit the required spontaneous symmetry breaking. This is the normal practice in the standard model, in grand unification, in supersymmetry and so on. With string duality, the scalar sector is prescribed by the construction and only in one very special case does it permit the required symmetry breaking.

This leads us to give more credence to the $\Gamma = 24/7$ example that does work and to encourage its further study to check whether it can have any connection to the real world.

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