Constraining the False Positive Rate for *Kepler* Planet Candidates with Multi-Color Photometry from the GTC

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Accepted ... Received ...; in original form ...

** ABSTRACT **
Using the OSIRIS instrument installed on the 10.4-m Gran Telescopio Canarias (GTC) we acquired multi-color transit photometry of four small ($R_p \lesssim 5 R_\oplus$) short-period ($P \lesssim 6$ days) planet candidates recently identified by the *Kepler* space mission. These observations are part of a program to constrain the false positive rate for small, short-period *Kepler* planet candidates. Since planetary transits should be largely achromatic when observed at different wavelengths (excluding the small color changes due to stellar limb darkening), we use the observed transit color to identify candidates as either false positives (e.g., a blend with a stellar eclipsing binary either in the background/foreground or bound to the target star) or validated planets. Our results include the identification of KOI 225.01 and KOI 1187.01 as false positives and the tentative validation of KOI 420.01 and KOI 526.01 as planets. The probability of identifying two false positives out of a sample of four targets is less than 1%, assuming an overall false positive rate for *Kepler* planet candidates of 10% (as estimated by Morton & Johnson 2011). Therefore, these results suggest a higher false positive rate for the small, short-period *Kepler* planet candidates than has been theoretically predicted by other studies which consider the *Kepler* planet candidate sample as a whole. Furthermore, our results are consistent with a recent Doppler study of short-period giant *Kepler* planet candidates (Santerne et al. 2012). We also investigate how the false positive rate for our sample varies with different planetary and stellar properties. Our results suggest that the false positive rate varies significantly with orbital period and is largest at the shortest orbital periods ($P < 3$ days), where there is a corresponding rise in the number of detached eclipsing binary stars (i.e., systems that can easily mimic planetary transits) that have been discovered by *Kepler*. However, we do not find significant correlations between the false positive rate and other planetary or stellar properties. Our sample size is not yet large enough to determine if orbital period plays the largest role in determining the false positive rate, but we discuss plans for future observations of additional *Kepler* candidates and compare our program focusing on relatively faint *Kepler* targets from the GTC with follow-up of *Kepler* targets that has been done with warm-Spitzer.

** Key words:** binaries: eclipsing – planetary systems – techniques: photometric

1 INTRODUCTION
The *Kepler* space mission has discovered, to date, 61 transiting planets as well as over 2,000 planet candidates and 2,000 eclipsing binary stars ([Batalha et al. 2012; Prša et al. 2011; Slawson et al. 2011](http://kepler.nasa.gov)). With such a vast number of planet candidates, it can be difficult to decide which to focus follow-up efforts on. Recent studies have tried to address this issue by estimating the false positive rate for the *Kepler* sample. Based on the list of 1,235 *Kepler* planet candidates published by [Borucki et al. (2011b)](http://kepler.nasa.gov), it has been predicted that as many as ~95% of these candidates are true planets ([Morton & Johnson 2011](http://kepler.nasa.gov)). However, previous studies have not taken into account how different subsets of *Kepler* targets may have different false positive rates. For example, there is a rapid rise in the number of detached eclipsing binary stars that have been discovered by *Kepler* at orbital periods of less than ~3 days, and such systems can mimic planetary transits ([Prša et al. 2011; Slawson et al. 2011](http://kepler.nasa.gov)). This suggests that there may be corresponding changes in the
false positive rate with orbital period. Because the probability of observing a transit event increases as the orbital period of the planet decreases, many of Kepler’s planet candidates have short periods. Thus it is necessary to be cautious when estimating false positive rates over the whole Kepler sample. While observational studies with warm-Spitzer support predictions of low false positive rates over the entire Kepler sample (Désert et al. 2012), biases in target selection can affect observationally-constrained false positive rates (see § 4 for further discussion). We also note that a recent imaging study has found that nearly 42% of their sample of 98 Kepler planet candidate hosts has a visual or bound companion within 6 arcseconds of the target star (Lillo-Box et al., in preparation). Such studies emphasize the need for follow-up imaging to exclude blend scenarios imitating planet candidates or contaminated transit depths.

The false positive scenarios we consider in this paper are those that result from stellar eclipsing binaries that are either in the background (or, in rare cases, foreground) or bound to the target star and are not always easy to identify with Kepler due to the flux from the different stars being blended together within Kepler’s photometric aperture (~6 arcsec). As discussed by, e.g., Colon & Ford (2011), different techniques can be used to eliminate many, but not all, blends. Multi-color transit photometry is an efficient method for recognizing blends that cannot be spatially resolved, as measuring the transit depth in different bandpasses (i.e. the transit color) allows one to test the planet hypothesis. This is possible since the magnitude of the transit color changes as long as the blended stars have significantly different colors.

Colon & Ford (2011) presented multi-color transit photometry of a Kepler target, KOI 565.01, that was first announced by Borucki et al. (2011a) to be a super-Earth-size planet candidate but later recognized as a likely false positive due to measurements of a centroid shift away from the location of the target on the CCD during transit (Borucki et al. 2011b). In Colon & Ford (2013), we used near-simultaneous multi-color observations acquired using the narrow-band tunable filter imaging mode on the Optical System for Imaging and Low Resolution Integrated Spectroscopy (OSIRIS) installed on the 10.4-m Gran Telescopio Canarias (GTC) to confirm that KOI 565.01 is indeed a false positive, as we both resolved a stellar eclipsing binary ~15 arcsec from the target and measured a color change in the “unresolved” target+eclipsing binary system. Thus, Colon & Ford (2014) demonstrated the capability of the GTC/OSIRIS for efficient vetting of planet candidates via its capabilities for near-simultaneous multi-color photometry within a single transit event.

In this paper, we present observations of four Kepler planet candidates specifically selected to have small radii and short orbital periods ($R_p \lesssim 5 R_\oplus$ and $P \lesssim 6$ days). Measuring the false positive rate for this extreme subset of planet candidates will allow us to test if there is a correlation between the false positive rate and different planetary and stellar properties. As in Colon & Ford (2011), the observations presented here were acquired with the GTC/OSIRIS. However, these observations used broadband filters in lieu of the narrow-band tunable filters in order to collect more photons and to obtain greater wavelength coverage (and thereby probe greater color differences). In §2 we discuss our target selection criteria, and we discuss the corresponding observations for our four targets in §3. In §4 and §5 we describe our data reduction and light curve analysis procedures, and we present results for each target in §6. We include a discussion of our results and how they relate to the distribution of eclipsing binaries that have been discovered by Kepler as well as previous estimates of the false positive rate for the Kepler sample in §7. In particular, we discuss theoretical estimates from Morton & Johnson (2011) and observational constraints from studies by Désert et al. (2012) and Santerne et al. (2012). Finally, we summarize our results and conclusions in §8 and we also discuss our plans for future observations of additional Kepler targets with the GTC.

2 TARGET SELECTION

Recent studies (e.g., Lissauer et al. 2011, 2012) have demonstrated that a majority of the planet candidates in Kepler’s multi-planet candidate systems should in fact be real planets. Considering these studies, for our program we target only those candidates found in single systems as determined by Borucki et al. (2011a). From the sample of candidates in single systems, we selected targets based on the following criteria:

- orbital period ($P$) $\lesssim 6$ days
- planet radius ($R_p$) $\lesssim 6 R_\oplus$
- transit depth (at center of transit; $\delta$) $> 500$ ppm
- transit duration (first to fourth contact; $\tau$) $\lesssim 2.5$ h
- Kepler magnitude ($K_p$) $< 15.5$
- vetting flag $> 1$

As discussed in the previous section, there is a significant rise in the number of detached eclipsing binary stars compared to planet candidates at short orbital periods. This is also illustrated in Fig. 1 where we show histograms of the number of planet candidates, detached eclipsing binaries, and all “other” eclipsing binaries (i.e. all binaries that are not listed as detached in Lawless et al. 2011) as a function of orbital period. Therefore, we focus on constraining the false positive rate only for planet candidates with short orbital periods, where the presence of eclipsing binaries is greatest. Our decision to focus on small candidates is due to there being a dominant population of Neptune-size or smaller candidates in the Kepler sample. We set constraints on the transit depth, duration and Kepler magnitude due to limitations of our observing technique, so as to measure the transit depth and color precisely. Furthermore, we want to do this while maintaining a reasonable observing cadence, hence the limits on the Kepler magnitude of our targets. Finally, we exclude candidates that have vetting flags of 1, as those have been previously confirmed as planets.

Along with the above constraints on the planetary and stellar properties, we have several observational constraints due to limitations of the GTC/OSIRIS. First, we rule out candidates that have no observable transits from the location of the GTC (which is located on La Palma at the Observatorio del Roque de los Muchachos). Then, we exclude those that did not have multiple transits observable during bright or grey time (during the 2011 observing season). We also exclude transit events that occur outside altitudes of
Vetting Kepler Planet Candidates

Figure 1. Histograms illustrating the number of *Kepler* planet candidates (solid blue line; based on [Borucki et al. 2011b](#)) and detached and all “other” eclipsing binaries (dotted red and dashed black lines, respectively; based on [Slawson et al. 2011](#)) as a function of orbital period. We also show a histogram (dash-dot green line) based on the recently released list of 2,321 KOIs from [Batalha et al. 2012](#). The right-hand y-axis shows the percentage of systems relative to the total number of target stars observed by *Kepler* in Q1. Note that only systems with orbital periods of up to 10 days are shown. While there is a substantial number of “other” (primarily semi-detached and overcontact) eclipsing binaries at the shortest orbital periods (which may be less likely to be flagged as potential planets), there is still a greater-to-comparable number of short-period detached eclipsing binaries compared to short-period planet candidates, which indicates the potential for eclipsing binaries to infiltrate the short-period planet candidate sample. The orbital periods of the KOIs we observed are indicated with vertical long-dashed gray lines and are labeled accordingly.

Figure 2. Radius versus orbital period of *Kepler* planet candidates. The locations of the four KOIs we observed are indicated with filled red squares and are labeled accordingly. The locations of the targets observed with warm-*Spitzer* by [Desert et al. 2012](#) are indicated with filled blue squares. The filled gray circles and the open gray circles respectively represent all KOIs presented by [Borucki et al. 2011b](#) and [Batalha et al. 2012](#) out to orbital periods of 200 days. Note the prominence of KOIs smaller than \(\sim 0.1 R_J\).

\(~35\)–72 degrees, so as to avoid high airmass and vignetting that occurs at high altitudes due to limitations of the GTC dome.

Finally, we did not check the *Kepler* light curves\(^2\) for each target that fit all of the above criteria prior to acquiring observations. However, as we discuss in §\(^3\) for future observations we plan to check the *Kepler* light curves for secondary eclipses and V-shaped eclipses, either of which could indicate *a priori* that the target is not a transiting planet but instead a stellar eclipsing binary.

These selection criteria led us to acquire observations of four planet candidates between April and September 2011: KOI (*Kepler Object of Interest*) 225.01, 420.01, 526.01 and 1187.01. In Table 1 we list some of the properties of each of our targets as determined by [Borucki et al. 2011b](#). [Borucki et al. 2011b](#) flagged KOI 225.01 as possibly having ellipsoidal variations. KOI 1187.01 has the shortest period of all the planet candidates announced by [Borucki et al. 2011b](#). In Figures 2, 3 and 4 we illustrate different properties of our targets in comparison to the sample of 1,235 KOIs and the corresponding 997 host stars from which our targets were chosen. The sample of KOIs observed with warm-*Spitzer* [Desert et al. 2012](#) is also illustrated in these figures for comparison (we discuss the *Spitzer* sample in more detail in §\(^7.1\)). Our targets and the corresponding observations are described in detail in §\(^3\) below.

### 3 Observations

We acquired photometry of each target and several nearby reference stars around the predicted time of a transit event. For each observation, we used the GTC/OSIRIS to acquire near-simultaneous multi-color photometry by alternating between two broadband “order sorter” filters\(^3\) that were custom made for OSIRIS: 666±36 nm and 858±58 nm. Both bandpasses were specifically chosen so as to minimize effects of telluric absorption and emission while also allowing for ample wavelength coverage. In order to decrease dead time, all observations used 1×1 binning, a fast pixel readout rate of 500 kHz and a single window located on one CCD chip. The size of the window varied for each observation, but each window was large enough to contain the target and several reference stars. We note that all observations except those for KOI 1187 were conducted in queue (service) mode. In

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\(^2\) Available at [http://archive.stsci.edu/kepler/](http://archive.stsci.edu/kepler/)

\(^3\) [http://www.gtc.iac.es/en/pages/instrumentation/osiris.php](http://www.gtc.iac.es/en/pages/instrumentation/osiris.php)
Table 1. KOI Properties

| KOI | KIC     | KP  | Teff (K) | b (deg) | P (days) | τ (hr)  | δ (ppm) | Rp (R_⊕) | Rp/R_⋆ |
|-----|---------|-----|----------|---------|----------|---------|----------|----------|--------|
| 225 | 5801571 | 14.784 | 6037    | 9.177   | 0.836598 | 1.2452  | 2571     | 4.9      | 0.04932 | 1.2452  |
| 420 | 8352537 | 14.247 | 4687    | 16.412  | 6.010401 | 2.2582  | 2700     | 4.3      | 0.0474  |
| 526 | 9157634 | 14.427 | 5467    | 12.426  | 2.104719 | 1.7639  | 926      | 2.6      | 0.0305  |
| 1187| 3814972 | 14.489 | 5286    | 10.846  | 0.3705285| 0.7778  | 1835     | 2.5      | 0.03961 |

All values are from Borucki et al. (2011b). The KIC number refers to the Kepler Input Catalog number for each target. Note that b is the Galactic latitude of the KOI host star, τ is the transit duration and δ is the transit depth as measured in the Kepler bandpass.

Figure 3. Signal-to-noise ratio (SNR) per transit as a function of orbital period for Kepler planet candidates. The SNR per transit for each KOI was computed from the transit depth, the transit duration and either the 6-hour combined differential photometric precision (CDPP) from Q3 data (for the Borucki et al. 2011b list) or the 6-hour CDPP from Q1-Q6 data (for the Batalha et al. 2012 list). The colors and symbols are the same as in Figure 2.

Figure 4. Kepler magnitude (Kp) versus effective temperature for the 997 KOI host stars published in Borucki et al. (2011) and the additional 926 KOI host stars published in Batalha et al. (2012). The colors and symbols are the same as in Figs. 2 and 3 and also avoided bad pixels in the center of the CCD chip. During the observations, the target’s centroid coordinates shifted by < 9 pixels in the x-direction and ~ 2 pixels in the y-direction. Several images were lost due to technical issues, and a few of the images towards the end of the observations were discarded due to the beginning of twilight.

3.1 KOI 225.01

We observed the transit event of KOI 225.01 on 2011 April 13 under clear conditions and during dark time, with observations beginning at 03:10 UT and ending at 06:12 UT, during which time the airmass ranged from ∼ 1.66 to 1.07. The exposure time was 50 s (for both bandpasses), with ∼40 s of dead time following each exposure. Seeing varied between 1.2 and 2.0 arcsec until about 05:00 UT, at which point the seeing improved to < 1 arcsec and a slight defocus was introduced in order to avoid saturation. A diffuse, dark band was present in all the images (a result of a very bright star located just outside the CCD), so the target was positioned on the CCD such that it was outside this region

3.2 KOI 420.01

Observations of the 2011 September 13 transit of KOI 420.01 took place from 21:48 UT (2011 September 13) to 01:30 UT (2011 September 14). Observations occurred during bright time and under photometric conditions, and the airmass ranged from 1.07 to 1.84. The exposure time was set to 40 s, with a corresponding 20 s of dead time following each exposure. The seeing roughly ranged from 1.1-1.8 arcsec throughout the observations, though at the beginning of the observations the seeing conditions changed drastically enough from one image to another that some of the reference stars were saturated. We explicitly exclude any saturated refer-
ence stars from our analysis (see \textsuperscript{5} for further details). The seeing stabilized and improved after about 23:00 UT, enough so that a slight defocus was implemented to avoid saturation. The target’s centroid coordinates shifted by \(\lesssim 4\) pixels in either direction during the observations.

### 3.3 KOI 526.01

The 2011 September 11 transit of KOI 526.01 was observed under photometric conditions and during bright time. Observations began at 21:37 UT on 2011 September 11 and ended at 00:00 UT on 2011 September 12. The airmass ranged from 1.05 to 1.22 and the seeing was stable between 0.6 and 0.8 arcsec. A slight defocus was implemented, yielding a defocused FWHM of 0.8-1.0 arcsec. An exposure time of 10 s was used, with 20 s of dead time between exposures. As in observations of KOI 225.01, a dark band caused by a bright star outside the CCD window was present in all images, so we placed the target star appropriately far away from the band so that the photometry would not be affected. The centroid coordinates of the target shifted by less than 4 and 2 pixels in the x- and y-directions, respectively. Twice during the observations the primary mirror segments lost alignment and produced distorted images: first around 22:30 UT and again at 00:00 UT. We discarded a few images from the first instance, but the issue with the mirror could not be readily fixed during the second instance, and the observations were forced to end early, around the time of the transit egress.

### 3.4 KOI 1187.01

We observed the 2011 June 12 transit event of KOI 1187.01, with observations taking place from 22:31 UT (2011 June 11) to 02:01 UT (2011 June 12). Observations took place during bright time and under clear conditions, and the airmass ranged from 1.90 to 1.05. Seeing was excellent and ranged from 0.6 to 0.9 arcsec during the night. Due to the excellent seeing conditions, the exposure time was set to 5 s. There were 24 s of dead time following each exposure. During the observations, the target’s centroid coordinates shifted by \(\lesssim 4\) pixels in either direction.

### 4 DATA REDUCTION

We used standard IRAF procedures for bias subtraction and flat-field correction (using dome flats taken for each bandpass) for each target. Due to nonuniform illumination by the lamp, we added an illumination correction to the final flat-field image for each target (except KOI 225). The illumination correction was performed using the IRAF task \textit{mkillumflat} within the \textit{noao.imred.ccdred} package, which removes the large scale illumination pattern from the flat field by smoothing the flat field image. For KOI 225, the final flat-field for the 666 nm filter showed a strong gradient after performing an illumination correction, so we chose to use the flat-field image as it was. To be consistent, we did not perform an illumination correction on the 858 nm final flat-field for KOI 225 either. We used the IDL Astronomy User’s Library\textsuperscript{4} implementation of DAOPHOT (Stetson 1987) to perform aperture photometry on each target and several nearby reference stars as well as on other potential sources of the transit signal (i.e. stars within \(\sim 20\) arcsec of each target). For each target, we tested different apertures and chose a final aperture based on that which resulted in the smallest scatter in the baseline (out-of-transit) flux ratios (i.e., the target star flux divided by the ensemble reference star flux). For KOI 225, 420, 526 and 1187 our final aperture was 25, 23, 15 and 14 pixels (equivalent to approximately 3.2, 2.9, 1.9 and 1.8 arcsec). Sky background subtraction took place during the aperture photometry process, with annuli chosen to be far enough away from each star that the flux from a given star would not be included within the sky annulus. While these procedures were performed for each bandpass separately, we considered the results for each bandpass and used the same aperture and sky annulus for each data set for a given target. Note that in many cases a smaller aperture and sky annulus were used for the stars within \(\sim 20\) arcsec of a given target due to the small separations between some of the stars and the potential for blending. For reference, we present a reduced science image showing the field of view around KOI 1187 in Figure 5. Once aperture photometry and sky subtraction were completed, we proceeded with light curve analysis as discussed in \textsuperscript{5} below.

### 5 LIGHT CURVE ANALYSIS

For each target, we computed light curves for each bandpass by dividing the total flux measured from the target by the total weighted flux of an ensemble of reference stars, where the flux from each reference star was weighted accordingly after discarding outlying flux values (resulting from either technical issues or variable sky conditions). During the analysis, several reference stars were found to be obviously variable or saturated, so we excluded those stars from the analysis. This resulted in us using 10, 4, 2 and 9 reference stars in the field near KOI 225, 420, 526 and 1187 to compute the reference ensemble flux. Next, each light curve for each target was normalized to the mean baseline flux ratio as measured in each bandpass. The light curves were then corrected for changes in airmass as well as for drifts in the centroid coordinates of the target on the CCD and the sharpness of the target’s profile \([2.35/\text{FWHM})^2\]. The latter corrections were done via external parameter decorrelation (see, e.g., Bakos et al. 2007, 2010). We note that due to the lack of data for KOI 526 during the transit egress and post-transit, our attempts to correct those light curves produced skewed results. Therefore, all further analysis for KOI 526 is based on the uncorrected light curves.

The corresponding observation times for each light curve for each target were computed from the UTC timestamps given in the image headers. We converted the UTC time at mid-exposure to Barycentric Julian Dates in Barycentric Dynamical Time (BJD TDB) via an online calculator described in Eastman et al. (2011) in order to

\footnote{\url{http://idlastro.gsfc.nasa.gov/}}
Figure 5. Image of the field of view around KOI 1187 as acquired using the GTC/OSIRIS and the 666/36 nm order sorter filter. The target is labeled accordingly and is contained within a black circle equivalent to twice the aperture used in the reduction process. The unlabeled stars contained in black circles are the nine reference stars used in our analysis. The larger red circle around KOI 1187 has a radius of $\sim 20$ arcsec, and the six brightest stars located within this circle (excluding the target) are the stars that we investigated as potential sources of the transit signal.

match the time coordinate system that the ephemerides from Borucki et al. (2011b) are given in.

The photometric uncertainties were computed from the photon noise of the target star and the reference star ensemble, the noise in the sky background around the target and each reference used in the ensemble, and scintillation noise. The resulting median photometric uncertainties for each light curve for each target are given in Table 2. In each case, the photon noise of the target is the primary source of error. Finally, in order to investigate the presence of red noise in our data, we computed the standard deviation of the flux ratios for different bin sizes and found that all our data follow the trend expected for white (Gaussian) noise. Despite this result, we also investigate potential residual systematics via a “prayer-bead” analysis, which we discuss below.

Table 2. Photometric Precisions

| KOI | $\sigma_{666\text{nm}}$ (ppm) | $\sigma_{858\text{nm}}$ (ppm) |
|-----|----------------|----------------|
| 225 | 476            | 540            |
| 420 | 501            | 428            |
| 526 | 1223           | 1100           |
| 1187| 1447           | 1295           |

After correcting the light curves for each target (except for KOI 526 as discussed above), we proceeded to fit synthetic models to each light curve, following the approach taken by Colón et al. (2010). We assumed each observed transit event was a planetary transit, and we used the planetary transit light curve models from Mandel & Agol (2002) to fit limb-darkened models to our data. Specifically, for each target, we fit for the following parameters:

- time of mid-transit ($t_0$)
- transit duration (first to fourth contact; $\tau$)
- impact parameter ($a \cos i/R_*$)
- planet-star radius ratio ($R_p/R_*$)
- two limb darkening coefficients ($c_1$ and $c_2$)
- baseline flux ratio
- (linear) baseline slope

The limb darkening coefficients that we fit for are defined as $c_1 \equiv u_1 + u_2$ and $c_2 \equiv u_1 - u_2$, where $u_1$ and $u_2$ are linear and quadratic limb darkening coefficients. For KOI 526, we note that we held the transit duration fixed to the value from Borucki et al. (2011b) in order to fit a model to our partial transit.

Initial guesses for the mid-transit time, transit duration, impact parameter and radius ratio were based on the values and their corresponding uncertainties as given in Borucki et al. (2011b). Values for the limb darkening coefficients were interpolated from the Claret & Bloemen (2011) models for the Sloan r' and z' filters and are based on the stellar parameters given in Borucki et al. (2011b). Due to the potentially larger than estimated uncertainties in the stellar parameters (see, e.g., Borucki et al. 2011b), we did not allow the limb darkening coefficients to be completely free parameters in the fitting process. Rather, we kept the coefficients fixed at self-consistent values during the fitting process, but we tested a range of fixed values for the coefficients. Similarly, we tested a range of initial guesses for the other parameters based on the uncertainties for the plane-
tary and stellar parameters. Best-fitting models were identified via a Levenberg-Marquardt minimization scheme.

Our light curve fitting procedure for each target is as follows. First, we fit models to each light curve individually, corrected the data against the best-fit baseline flux ratio and slope, subtracted the best-fit models and discarded any data points lying greater than 3σ from the residuals. Then, we used the corrected light curves and fit models to them in a joint analysis, where we forced the impact parameter, transit duration, mid-transit time, baseline flux ratio and baseline slope to be the same for both light curves. However, we allowed different values for the radius ratio and limb darkening coefficients to be fitted to the different light curves. The results from the joint analysis were then used to correct the individual light curves as in the first step described above. A final joint analysis was then applied to the “final” corrected light curves. During this final stage, we also performed a “prayer-bead” analysis as was done in Colón et al. (2010).

Specifically, we performed a circular shift on the residuals for each light curve (computed after removing the best-fit model) and constructed synthetic light curves by adding the shifted residuals back to the best-fit model. The joint analysis described above was applied to each synthetic light curve, and we use the dispersion of the best-fit parameters to calculate uncertainties on each parameter. This accounts for any additional systematic noise sources in the data. We present results from our light curve analysis in §6.

6 RESULTS

We present the light curves and the corresponding best-fit models for each target in Figures 6, 7, 8 and 9. While not shown here, we had also generated light curves for the potential sources of each transit signal (i.e. stars that could have been blended with the target within Kepler’s aperture) following a similar procedure as described above. We generated light curves for 10, 3, 3 and 6 stars within ∼ 20 arcsec of KOI 225, 420, 526 and 1187. Upon visual inspection, we found that none of these light curves showed a transit signal during the time of the transit event, indicating that the transits that we observed either occur due to an object transiting the target star or an object transiting an unresolved star that is blended with the target star. We also present the transit color (666 nm − 858 nm) of each target in the bottom panel of Figures 6−9, which was computed by taking the average of each pair of flux ratios in the 666 nm light curve and dividing by the corresponding points in the 858 nm light curve. Therefore, in Figures 6−9, a positive color indicates a redder transit and a negative color indicates a bluer transit.

In Table 3, we report best-fit model parameters for each target based on the model with the smallest χ² value, but we note that the parameter uncertainties are based on the full set of best-fit values and their corresponding uncertainties as found during the “prayer-bead” analysis. Specifically, for a given parameter, the upper error bar is a result of subtracting the best-fit value (from the model with the smallest χ²

We specifically used mpfitfun, which is publicly available at http://www.physics.wisc.edu/~craigm/idl/idl.html

Figure 6. Light curves, residuals, and color based on observations of the 2011 April 13 transit of KOI 225.01 acquired at 666 nm (in blue) and 858 nm (in red). The circles are observations and the solid curves are the corresponding best-fit models (see text for further details). Representative photometric error bars for each light curve are shown on the left-hand side of the top panel. The black horizontal dashed line illustrates the depth of the transit as measured in the Kepler bandpass (see Table 1). Residuals from the fits for each light curve are also shown in the top panel, with a horizontal dotted line indicating the level at which the residuals were offset (for clarity). The bottom panel shows the color as computed from the two light curves as well as a representative error bar on the left-hand side of the panel and a horizontal dotted line that illustrates a color of zero (for reference).

Figure 7. Same as Figure 6 but for the transit of KOI 420.01 as observed on 2011 September 13.
value) from the maximum sum of a fitted value and its associated measurement uncertainty as determined from the full set of models computed during the “prayer-bead” analysis, and likewise for the lower error bar. In general, we find that the formal 1σ errors for the best-fit parameters are comparable to those errors computed based on the results from the “prayer-bead” analysis, which indicates that any residual systematics in the data (i.e. those not removed by external parameter decorrelation or airmass corrections) have a negligible effect on our results. Furthermore, the distribution of each best-fit light curve parameter over all permutations is smaller than the uncertainties given in Table 3, which further indicates that the results presented here are robust.

Finally, as suggested by the referee, we consider whether we can use astrometry from our images to provide additional constraints on the properties of the targets we observed. A preliminary astrometric analysis does not suggest that any of the KOIs we observed are due to a blend with another star that was resolved by our observations. Furthermore, despite the large aperture used by Kepler, the astrometric precisions from Kepler are extremely high (<0.004 arcseconds for a single 30 min exposure; Monet et al. 2010), and to the best of our knowledge, no significant centroid shifts were measured by Kepler for any of our KOIs.

We discuss specific results for each target individually in the following sections.

6.1 KOI 225.01

The light curves presented in Figure 6 are prominently V-shaped, which alone suggests a possible non-planetary transit event. Considering the shape of the light curves and the significant difference in the transit depths as measured in the GTC bandpasses, we deduce that KOI 225.01 is most likely a stellar eclipsing binary system. Specifically, we find that the best-fit planet-star radius ratios differ at a level of >11σ, which is a clear indication that this object is not a planet. The transit depth in the Kepler bandpass is also significantly different from those measured in the GTC bandpasses. In particular, the transit depth is notably different between the Kepler bandpass and the blue GTC bandpass (around 666 nm), even though they probe fairly similar wavelength regimes. We primarily attribute this difference to dilution in the Kepler photometry, since there is a relatively bright star near KOI 225 that appears to have slightly contaminated one of the pixels used in the Kepler photometry. As noted in Borucki et al. (2011b), this target’s light curve had possible ellipsoidal variations, also suggesting that the system contains an eclipsing binary. Furthermore, after our observations had been conducted, Slawson et al. (2011) listed this target in their eclipsing binary catalog.

Finally, Ofir & Dreizler (2012) recently conducted an independent analysis of the Kepler data set and identified KOI 225.01 as a false positive due to the detection of significant differences between the odd and even eclipse events. Since we measure a deeper eclipse in the bluer GTC bandpass, this indicates that during the eclipse more blue light is blocked, and therefore the secondary (eclipsing) component is redder than the primary star. In Table 3, we provide an updated ephemeris and eclipse duration, though we note that likely due to the non-planetary transit light curve shape, the best-fit model yielded an impact parameter that reached the upper boundary limits during the fitting process. Therefore, the resulting best-fit light curve parameters

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7 As determined from target pixel files downloaded from http://archive.stsci.edu/kepler/
8 We refer the reader to Slawson et al. (2011) for further details on how some KOIs were rejected as planet candidates and subsequently added to the eclipsing binary catalog.
Table 3. Best-Fit Model Parameters

| KOI  | $t_0$ (BJD−2454900) | $\tau$ (hr) | $a \cos i/R_*$ | $R_p/R_\star$ (666 nm) | $R_p/R_\star$ (858 nm) | $c_1$ (666 nm) | $c_2$ (666 nm) | $c_1$ (858 nm) | $c_2$ (858 nm) |
|------|---------------------|-------------|----------------|------------------------|------------------------|--------------|--------------|--------------|--------------|
| 225.01 | 764.70659$^{+0.00096}_{-0.00096}$ | 1.7466$^{+0.0214}_{-0.0214}$ | 1.0 | 0.1739$^{+0.0034}_{-0.0034}$ | 0.1318$^{+0.0026}_{-0.0012}$ | 0.6548 | 0.0152 | 0.5034 | -0.0398 |
| 420.01 | 918.49049$^{+0.00049}_{-0.00049}$ | 2.1188$^{+0.0560}_{-0.0379}$ | 0.6270$^{+0.0998}_{-0.0498}$ | 0.0552$^{+0.021}_{-0.0021}$ | 0.0647$^{+0.0544}_{-0.0535}$ | 0.7581 | 0.4729 | 0.5837 | -0.2011 |
| 526.01 | 916.46330$^{+0.00041}_{-0.00170}$ | 1.7639 (fixed) | 0.7456$^{+0.0727}_{-0.0727}$ | 0.0714$^{+0.0023}_{-0.0023}$ | 0.0635$^{+0.0103}_{-0.0103}$ | 0.6920 | 0.2466 | 0.5339 | 0.0869 |
| 1187.01 | 824.52863$^{+0.00039}_{-0.000145}$ | 0.5066$^{+0.0390}_{-0.0285}$ | 0.9345$^{+0.0427}_{-0.0427}$ | 0.0469$^{+0.0074}_{-0.0070}$ | 0.0924$^{+0.0174}_{-0.0173}$ | 0.6895 | 0.2387 | 0.5370 | 0.0886 |

Note that the time of mid-transit, $t_0$, is technically given in BJD−TDB (Barycentric Julian Date in Barycentric Dynamical Time). See text for further details.

are likely somewhat skewed, but this does not change the significance of our results.

Sawson et al. (2011) report a period that is twice as long as that found by Borucki et al. (2011b). If correct, then either what Borucki et al. (2011b) believed were transit events were actually a combination of primary and secondary eclipses or the eclipsing binary has a large enough inclination that all eclipse events are primary eclipses and the secondaries are unobservable from our line-of-sight. If we assume that the period found by Sawson et al. (2011) is correct (and was determined, for instance, by measuring different depths for successive transits, which led to this KOI being rejected), then it is necessary to consider how this affects any correlation between the orbital period and the false positive rate for Kepler targets. We refer the reader to Slawson et al. (2011) for further discussion.

6.2 KOI 420.01

As illustrated in Figure 8, the transit depths as observed in the GTC light curves are consistent within $\sim 2.8\sigma$, and we did not resolve any potential sources of the transit signal within $\sim 20$ arcsec of the target, so we deduce that this target is not a false positive and is instead a validated planet. The best-fit parameters from our light curve models are given in Table 3 and include an updated ephemeris, transit duration, and impact parameter. We note that the impact parameter given in Borucki et al. (2011b) has an associated uncertainty of 1, and Batalha et al. (2012) report an impact parameter of 0.57 with a relatively large uncertainty of 0.52, so we provide a much stronger constraint on this parameter here. Finally, based on our measured planet-star radius ratios and the revised stellar radius (0.69 $R_\odot$ compared to the value of 0.83 $R_\odot$ reported by Borucki et al. 2011b) given in Batalha et al. (2012), we find KOI 420.01 to have a radius that is between $\sim 4.15$ and 4.87 $R_\oplus$ (slightly larger than the value of 3.65 $R_\oplus$ found by Batalha et al. 2012).

6.3 KOI 526.01

Despite only observing a partial transit with the GTC (as illustrated in Figure 9, we find that the transit depths clearly match each other, with planet-star radius ratios that are consistent within $\sim 1.2\sigma$. While the Kepler depth is much shallower, there appears to be no significant contamination from nearby stars in the Kepler photometry (see footnote in Batalha et al. 2012). Given that even the transit depths in the Kepler and the blue GTC bandpass are significantly different, and that dilution appears to not be the source, we believe this object warrants further investigation beyond the scope of this paper. For instance, it is possible that stellar variability in the target star or a blended star impacted both the GTC and Kepler’s measured transit depths. Regardless, since the depths between the GTC bandpasses are consistent, this target still passes our validation test. As in the case for KOI 420.01, we found no stars within $\sim 20$ arcsec of the target that showed a transit signal at the expected time of the transit, so we also validate KOI 526.01 as a planet. Table 3 includes an updated ephemeris and impact parameter (recall that the transit duration was held fixed due to fitting only a partial transit). Again, as for KOI 420.01, Borucki et al. (2011b) found an uncertainty of 1 on the impact parameter, and Batalha et al. (2012) report an impact parameter of 0.80±0.34, so our observations and models provide a much stronger constraint on the impact parameter, which we find has an associated uncertainty of 0.0771. Based on our measured planet-star radius ratios and assuming a stellar radius of 0.92 $R_\odot$ (from Batalha et al. 2012 and slightly larger than the value of 0.80 $R_\odot$ reported by Borucki et al. 2011b), we calculate that KOI 526.01 has a radius between $\sim 6.37$ and 7.16 $R_\oplus$. We note that this is over twice the radius of 3.11 $R_\oplus$ measured by Batalha et al. (2012).

6.4 KOI 1187.01

As in the case of KOI 225.01, the light curves for KOI 1187.01 (shown in Figure 10) appear to be fairly V-shaped. Furthermore, visual inspection of the GTC light curves shows that there is clearly a significant difference in the GTC transit depths. However, we find that the best-fit planet-star radius ratios only differ at a level of $\sim 1.8\sigma$, likely due to the large uncertainty in the radius ratio measured for the 858 nm light curve. We attribute this large uncertainty

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9 We use the term validated to mean that the planet candidate is most likely a planet based on our observations but it is not a confirmed planet because there is not independent evidence (e.g., Doppler or transit timing variations) for the planet model.

10 Kepler light curves for this target show baseline variability at a level of $\sim 1\%$. 
to a combination of the relatively poor photometric precisions achieved for this target combined with the degeneracy between the impact parameter (measured to be nearly equal to 1) and the planet-star radius ratio. To reconcile these measurements with what we find visually, we compute weighted mean colors and their uncertainties for the in-transit and out-of-transit data. We find a mean in-transit color of $-0.00425 \pm 0.00050$ and a mean out-of-transit color of $-0.000160 \pm 0.000212$, which differ significantly at a level of $\sim 5.8 \sigma$. Therefore, despite the consistent measured radius ratios, there is an obviously significant color change during the transit event, so we argue that KOI 1187.01 is in fact a false positive and not a planet.

Contrary to KOI 225.01, the transit of KOI 1187.01 is deeper in the redder GTC bandpass than in the bluer GTC bandpass. This implies that during the eclipse, more red light is blocked than blue light, and the smaller (eclipsed) GTC bandpass. This implies that during the eclipse, more light is deeper in the redder GTC bandpass than in the bluer bandpass. As discussed in §6.1 above and below in Figure 1, this might imply that we are not probing planet candidates with orbital periods of less than 6 days, but instead we are actually probing a sample of eclipsing binaries with periods as long as 12 days. However, since there is still a comparable population of eclipsing binaries and planet candidates with longer periods (e.g. out to at least 10 days), as illustrated in Figure 1, we believe this period discrepancy would not affect our conclusion that a population of short-period eclipsing binaries can significantly contaminate short-period planet candidates. Candidates that are initially identified as planets but are actually eclipsing binaries will tend to have shorter apparent periods (their periods will double when they are identified as eclipsing binaries), which strengthens our argument for contamination of the planet sample at short periods, since this effect would further reduce the ratio of planets to eclipsing binaries at periods of less than approximately 3 days.

Finally, we note that with the technique presented here, it is not possible for us to identify cases where a planet candidate is actually a binary star composed of two stars that have the same temperature, as there would be no measurable color change during the transit event. This suggests that some of our potentially validated planets could still be false positives. However, Kepler’s photometry should be able to distinguish if the transit depths differ between every other transit (i.e. odd-even transit depths), which would identify a candidate as a false positive. In cases where a significant odd-even ratio is measured, this can also be used to reconcile the issue with the orbital periods described above. To the best of our knowledge, no significant odd-even ratio was found for our validated planets, KOI 420.01 and KOI 526.01.

Recently, a new list of Kepler planet candidates was announced, bringing the total number of candidates to 2,321 (Batalha et al. 2012). As illustrated in Figures 1–3 and 10, the new catalog follows the same general distribution of orbital periods, planet radii, stellar magnitudes, temperatures, and Galactic latitudes as the Borucki et al. (2011b) catalog, but there is notably a greater number of smaller and shorter-period planet candidates in the new catalog. This serves to emphasize the need to observationally constrain the false positive rate for such small, short-period planets. We note that this new catalog was generated using improved vetting metrics, so it should have a higher

11 Some high signal-to-noise ratio eclipsing binaries are more likely to have correctly determined radii, so some short-period planet candidates that are actually eclipsing binaries are correspondingly more likely to have accurate radii.
fidelity than previous ones (i.e., the Borucki et al. 2011b catalog). However, the KOIs from the Borucki et al. (2011b) catalog have not been vetted against the improved metrics described in Batalha et al. (2012), so both KOI 225.01 and KOI 1187.01 are still included in the updated catalog as potential planet candidates. Also, Batalha et al. (2012) remark that potential KOIs are not vetted against the shape of their light curves, so planet candidates with V-shaped transit light curves (such as KOI 225.01 and KOI 1187.01) are not immediately rejected. Given ongoing parallel efforts to identify planet candidates and KOIs and that Slawson et al. (2011) previously identified both KOI 225.01 and KOI 1187.01 as eclipsing binaries, we recommend that the eclipsing binary catalog be consulted before following up any given planet candidate.

7.1 Comparison to Theoretical Studies

A recent study by Morton & Johnson (2011) provided theoretical estimates of the false positive rate for Kepler planet candidates. Morton & Johnson (2011) specifically estimated that nearly 90% of the 1,235 candidates presented by Borucki et al. (2011b) had a false positive probability of less than 10%. For our targets in particular, Morton & Johnson (2011) computed the following false positive probabilities: 0.01 (KOI 225.01), 0.04 (KOI 420.01), 0.03 (KOI 526.01) and 0.03 (KOI 1187.01). It is interesting to note that the target with the lowest false positive probability is one that ended up being a false positive. However, we note that the false positive probabilities from Morton & Johnson (2011) are only valid for non-V-shaped transit signals. Therefore, considering that both KOI 225.01 and KOI 1187.01 appear to have somewhat obviously V-shaped transits, the low false positive probabilities computed for these targets by Morton & Johnson (2011) are not appropriate. A recent study by Morton (2012) improves upon the analysis from Morton & Johnson (2011) by taking the transit shape into account when computing the false positive probability for a given target. From their new analysis, Morton (2012) calculate a false positive probability of > 0.99 for KOI 225.01 and 0.76 for KOI 1187.01, which is consistent with our observations. The caveat about the transit shape also affects the overall assumed false positive rate for the Kepler sample, as Morton & Johnson (2011) did not separate planet candidates with V-shaped transit signals from those with non-V-shaped transit signals. This means that we should not interpret their findings as 90-95% of Kepler planet candidates are planets. However, we can use their averaged false positive probabilities as a starting point for the overall false positive rate for the Kepler sample. Despite any caveats, we estimate the probability of detecting 2 or 3 false positives out of 4 or 5 targets observed. Assuming a binomial distribution and a false positive rate of 10% for Kepler planet candidates Morton & Johnson (2011), we estimate that the probability of detecting 2 false positives from a sample of 4 targets is less than 1% (and less than 5% for detecting 3 false positives from 5 targets). Thus, we use this to emphasize that the false positive rate for current Kepler planet candidates with radii less than ~ 5 R⊕ and orbital periods less than ~ 6.0 days is likely much higher than 10%.

In regards to the full Kepler sample, Morton & Johnson (2011) found that the false positive probability varied with the depth of the transit as well as the magnitude and Galactic latitude of the target star, but they did not investigate how the probability might vary with orbital period or transit duration (though they claim that such properties would serve to decrease their probability estimates and thus their estimates are upper limits). Specifically, our results support their finding that the false positive rate increases slightly with magnitude, as our two faintest targets ended up being false positives. They also find a general increase in the false positive probability with increasing transit depth (though there are some local minima and maxima; e.g., see Figure 7 in Morton & Johnson 2011) and with decreasing Galactic latitude. In our case, the target with the largest transit depth (as measured in the Kepler bandpass) was KOI 420.01, which we validated as a planet. While we find no obvious correlation in our sample between Kepler’s measured transit depths and the false positive rate, dilution is an important factor that has to be considered (e.g., as illustrated by our light curves for KOI 225.01 in Figure 6, as some of the depths measured by Kepler may be underestimated. In regards to Galactic latitude, in Figure 10) we show the cumulative distribution of the Galactic latitudes for the Batalha et al. (2012) KOI list and the Slawson et al. (2011) catalog of eclipsing binaries, which illustrates that the samples have the same general distribution. Furthermore, our false positives are indeed located at lower latitudes, which supports the argument by Morton & Johnson (2011) that there is a slight increase in the false positive rate with decreasing Galactic latitude. We present a similar figure in Figure 11 where we show the cumulative distribution of the Galactic latitudes for the Kepler eclipsing binaries along with separate distributions for stars that host short-period (P \( \leq \) 2 days) and long-period (P > 2 days) planet candidates. We see that the distribution for the stars that host short-period candidates matches the eclipsing binary distributions more so than the sample of long-period candidates. Therefore, Figure 11 further illustrates the likely contamination of short-period planet candidates by eclipsing binaries. In Figure 12 we illustrate how the number of eclipsing binaries varies with Galactic latitude, and we find that overall the fraction of Kepler targets that are eclipsing binaries is about the same as a function of Galactic latitude. This further implies a nearly consistent presence of eclipsing binaries that could plague the Kepler planet candidate sample.

7.2 Comparison to Observational Studies

Désert et al. (2012) have used warm-Spitzer follow-up of KOIs to find a low false positive rate consistent with the estimates from Morton & Johnson (2011). Overall, our sample includes shorter period planets than their sample, as well as fainter targets (excluding their sample of M dwarf stars). Given that only planet candidates with the shortest orbital periods (<< 2 days) are likely to be significantly contaminated by non-detached eclipsing binaries, it is not entirely surprising that Désert et al. (2012) found a low false positive rate for their sample of planet candidates with periods of ~1.8–100 days.

Recently, Santerne et al. (2012) presented a Doppler study of short-period giant Kepler planet candidates. They...
targeted a sample of 46 Kepler planet candidates with transit depths greater than 0.4%, orbital periods less than 25 days, and host stars brighter than 14.7 magnitude (Kp). Based on their radial velocity follow-up observations, Santerne et al. (2012) estimate a false positive rate of 34.8±6.5% for this subset of Kepler planet candidates. While we probed a different (and smaller) population of Kepler planet candidates, our observed false positive rate of 50% (with large uncertainty due to our small sample size) for small, short-period Kepler planet candidates is supported by their observations. The study by Santerne et al. (2012) also supports our argument that different populations of Kepler targets likely have different false positive rates associated with them.

8 CONCLUSION

We acquired multi-color transit photometry of four small ($\sim 2.5 - 4.9$ R$_\oplus$), short-period ($\sim 0.37 - 6.0$ days) Kepler planet candidates with the GTC. Based on the transit color, we identified two candidates as false positives. For two, we find further evidence supporting the planet hypothesis, consistent with validated planets. We also remind the reader of KOI 565.01, which was a planet candidate observed in a similar fashion and that was also found to be a false positive (albeit it was selected from the first KOI catalog published by Borucki et al. 2011a; Colón & Ford 2011). While we find a high false positive rate (2/4 or 3/5, if we include KOI 565) in our small sample, we caution that this is likely not representative of the entire sample of Kepler planet candidates, due to the small number of targets we observed and the specific properties of these candidates (e.g. the orbital period and size). Nevertheless, our results demonstrate the importance of considering these properties when evaluating the false positive probability of specific systems. While our findings seem to contradict the theoretical estimates from Morton & Johnson (2011), the low false positive rate that they estimate is based on the assumption that all candidates had passed preliminary false-positive vetting metrics based on Kepler photometry and astrometry. Thus, if we consider the obviously V-shaped transits for KOI 225.01 and KOI 1187.01 to imply a false positive nature for these KOIs, then according to Morton & Johnson (2011) the low false positive probabilities for these targets are not accurate. The false positive rate for our sample is also much larger than the observational constraints from Desert et al. (2012)
Figure 12. Histograms of the number of detached (red) and all “other” (gray) eclipsing binaries from Slawson et al. (2011) as a function of orbital period. Each panel shows a different bin of Galactic latitude. As in Figure 1, the righthand y-axis shows the percentage of systems relative to the total number of target stars observed by Kepler in Q1. There is a roughly consistent number of eclipsing binaries in each latitude bin (except for the highest latitudes), which suggests a consistent presence of eclipsing binaries that could contaminate potential planet candidates. While there are fewer eclipsing binaries at the highest latitudes, there are also correspondingly fewer planet candidates at those latitudes (see Figure 10).