Experimental and numerical investigation of submicron particle deposition enhancement by patterned surface

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Abstract. Exposure to inhaling airborne particles in indoor and outdoor environments is a threat to public health. Indoor air passes through ventilation ducts and continuously circulates with the air outdoors, resulting in a higher concentration of suspended particles in indoor environments when compared to outdoor environments. Thus removing airborne particles in ventilation ducts becomes essential, especially in large buildings. Repeated surface ribs have been reported to greatly enhance the particle collection efficiency while it also causes a significant pressure drop, leading to higher energy consumption. In this study, an overall efficiency ratio is defined, taking into consideration the particle removal rate and the associated pressure drop, to evaluate the overall performance of different surface patterns in a ventilation duct. After the design and optimization processes, the semi-circular patterns are shown to have the best overall efficiency, i.e. a 1137 times increase when compared with having no patterned surface. The deposition velocity on the semi-circular surface found in simulation results were validated with a fully-developed wind tunnel experiment. This study shows that semi-circular surface patterns with a pitch-to-height ratio of 4 are recommended for the overall enhancement in the ventilation duct, especially for capturing submicron particles.

1. Introduction

The side effects of inhalation exposure to airborne particles can be reduced significantly through particle deposition in ventilation ducts. The degree of indoor air quality is assessed by the number of particular matters (PM). The demands to deposit PM, especially in the range of 0.1-1 micrometer in the ventilation duct are strong. Sippola and Nazaroff [1] investigated the particle deposition in ventilation ducts as this is the dominant entry path of outdoor air entering into buildings and circulating with indoor air. Their results indicated that surface roughness is the dominant factor for deposition in insulated ducts. Lai and Nazaroff [2] studied the deposition of 0.9-9 µm particles onto vertical walls with a roughness ranging from 10 to 250 nm. However, the surface roughness still cannot capture a large number of submicron particles because of the lower turbulence kinetic energy among the surface roughness structures. Subsequently Lai et al. [3] compared the particle deposition rate in smooth and ribbed duct air flow by experimental measurements. Their preliminary results indicated that the surface ribs can greatly increase the particle deposition. Lu and Lu [4] numerically studied the particle deposition enhancement of different micro-structured patterns (rectangular, triangular and full-circular ribbed-walls) on a turbulent channel. They defined an efficiency ratio by considering both the effects of particle deposition enhancement and drag force induced by a micro-structured surface. It is found that square ribs are an efficient and effective alternative for efficiency enhancement compared with triangular and circular ribs. But the flow drag is increased to a ratio of 9.8 compared with a plain surface. By reducing the pressure drop, the total efficiency ratio can overwhelm the micro-structured surface discussed above. Therefore,
it is valuable to investigate more micro-structured surface and optimize the dimension for higher deposition enhancement with a reduced drop in pressure.

An overall efficiency including both the particle deposition enhancement and the decrease of fluid drag were defined to compare the performance of different types of surface patterned structures. Our study covered patterned surfaces with rectangular, triangular, semi-circular and open-circular shapes. Computational fluid dynamics (CFD) simulation and experimental validation were used to compare particle deposition enhancement in turbulent flows. In our simulation, p/e varied from 3, 4, 5, 6. For each p/e, the particle diameter is 0.01, 0.02, 0.1, 0.2, 0.3, 0.5, 1, 1.2, 3, 5, 8 and 20 µm. A recommended patterned surface at a certain p/e will be suggested from both the experiment and numerical simulation to increase the energy efficiency of the current ventilation system.

2. Numerical model and methodology

2.1. Turbulent air flow

To model the turbulent airflow interaction with particle motion, a set of Reynolds-averaged Navier-Stokes (RANS) equations are selected and solved. In our numerical model, a Reynolds stress model (RSM) with velocity fluctuation correction was applied to study the anisotropic flow field [5]. The air dynamic viscosity was 1.789×10^{-5} N·s/m², and air density was 1.225 kg/m³ at a temperature of 288 K. All variables were specified at the inlet and the average inlet air velocity was 5 m/s. The Reynolds number based on average velocity and channel width was 6845. A fully developed turbulent channel flow profile was imposed at the inlet. The inlet velocity is modeled with a 1/7th power law, which is given by

\[ U = \frac{h}{2} U_{\text{mean}} \left( \frac{y}{h/2} \right)^{1/7} \quad \text{for} \quad 0 \leq y \leq \frac{h}{2} \]

\[ U = \frac{h}{2} U_{\text{mean}} \left( \frac{h-y}{h/2} \right)^{1/7} \quad \text{for} \quad \frac{h}{2} \leq y \leq h \]

\( h \) is the channel height, \( U_{\text{mean}} \) is the averaged velocity of the channel, \( y \) is the vertical position of the channel. The fully developed turbulence kinetic energy at the inlet is given as,

\[ k = \frac{\tau_w}{\rho_g \sqrt{C_p}} + \frac{y}{h/2} \left( 0.002U_{\text{free}}^2 - \frac{\tau_w}{\rho_g \sqrt{C_p}} \right) \quad \text{for} \quad 0 \leq y \leq \frac{h}{2} \]

\[ k = \frac{\tau_w}{\rho_g \sqrt{C_p}} - \frac{h-y}{h/2} \left( 0.002U_{\text{free}}^2 - \frac{\tau_w}{\rho_g \sqrt{C_p}} \right) \quad \text{for} \quad D/2 \leq y \leq D \]

\( \rho_g \) is the density of air, \( C_p \) is an empirical constant specified in the turbulent model (approximately 0.09), \( U_{\text{free}} \) equals to 8/7 of \( U_{\text{mean}} \), \( \tau_w \) is the wall shear stress.

2.2. Particle trajectory equation

The particles were tracked by Lagrangian particle tracking by considering the effect of lift force, gravitational force, drag force, and Brownian motion. The Lagrangian equations governing the particle motion are written as,

\[ m_p \frac{d\vec{u}_p}{dt} = \vec{F}_{\text{drag}} + \vec{F}_{\text{gravitation}} + \vec{F}_{\text{Brownian}} + \vec{F}_{\text{lift}} \]

Particle force terms in Equation 5 are defined in Table 1. In Table 1, the factor \( C_c \) is the Cunningham correlation, \( \Lambda \) is the mean free path, \( d_p \) is the particle diameter, \( Re_p \) is the Reynolds number of particles, \( \rho_g \) is the density of air, \( \nu_g \) is the kinematic viscosity of air, \( k_b \) is the gas constant (1.38×10^{-23}), \( T \) is the absolute temperature of air, \( \rho_p \) is the density of the particle.
Table 1. Particle trajectory equations

|                        | Submicron particles (<1µm) | Micron particles (>1µm) |
|------------------------|-----------------------------|-------------------------|
| **Particle drag force**|                             |                         |
| \( \vec{F}_{\text{drag}} = \frac{18 \mu}{\rho_p d_p^2 C_c} \) | \( \vec{F}_{\text{drag}} = \frac{18 \mu}{\rho_p d_p^2 C_D} \) |
| \( C_c = 1 + \frac{2 \lambda}{d_p} (1.257 + 0.4 e^{-(1.1 d_p/2 \lambda)}) \) | \( C_D = \frac{24}{Re_p} \) for \( Re_p < 1 \) |
|                         |                             | \( C_D = \frac{24}{Re_p} (1 + 0.15 Re_p^{0.687}) \) for \( 1 < Re_p < 400 \) |
| **Brownian motion**     |                             |                         |
| \( F_{\text{Brownian}} = \sqrt{\frac{\pi S_0}{4t}} \), \( S_0 = \frac{216 \rho_p \gamma_p k_B T}{\pi^2 \rho_p d_p^2 C_c} \) |                         |
| **Gravitational force** |                             |                         |
| \( F_{\text{grav}} = \rho g \) |                         |
| **Lift force**          |                             |                         |
| Saffman’s lift force [6] |                             |                         |

3. Numerical results and discussion

The length of the channel is 400 mm and the width of the channel is 20 mm. The height of the surface patterns is 2 mm, which was constant for all the cases. The ratio of rib height to the rib width was 0.5. Figure 1 displayed different types of patterned surface at the \( p/e \) of 3.

![Different types of patterned surfaces for particle deposition: (a) Semi-circular (b) Open circular (c) Triangular ribs (d) Rectangular ribs](image)

An overall performance \( \eta \) is applied in Equation (6) to compare the deposition and fluid performance of different patterns.

\[
\eta = \frac{V_{d-\text{rough}}/V_{d-\text{smooth}}}{F_{d-\text{rough}}/F_{d-\text{smooth}}} \tag{6}
\]

where \( V_{d-\text{rough}} \) and \( V_{d-\text{smooth}} \) are the particle deposition velocity of a patterned surface and smooth surface respectively, and \( F_{d-\text{rough}} \) and \( F_{d-\text{smooth}} \) are the flow drag for a patterned surface and smooth surface respectively. Figure 2 (a), (b), (c) and (d) illustrate the \( \eta \) for different patterned surfaces under the \( p/e \) of 3, 4, 5 and 6. It can be seen for different \( p/e \), the semi-circular surface pattern overwhelms the other micro-patterns and has the best overall efficiency. The triangular patterned surface has the lowest \( \eta \). The best \( \eta \) still occurs at the range of submicron-sized particles, while the \( \eta \) decreases with ultrafine and micron-sized particles.

The deposition velocity (\( V_d \)) in Equation (6) can be defined as Equation (7),

\[
V_d = \frac{J}{n_0} = \frac{\text{particle number deposited} / (\text{Area} \cdot t_d)}{\text{particle number} / m^3} \tag{7}
\]
Figure 2. Comparison of overall efficiency for different types of surface patterns under different p/e: (a) p/e=3 (b) p/e=4 (c) p/e=5 (d) p/e=6

4. Particle deposition experiment and validation
This study included experiments to validate the numerical results. A wind tunnel is set up to provide a fully developed turbulent channel flow [7]. In Figure 3, the wind tunnel consists of a blower, honeycomb, screen and test section. The cross-section of the tunnel is 20 mm in height times 200 mm in width. The test section was located 3 m downstream along the duct, which was 150 times the height of the channel and was sufficient for the flow to develop fully. In the test section, a holder to fit the sample was made and positioned at the centerline of the duct. The entire duct is made of transparent Perspex. The blower is driven by a frequency inverter to induce the airflow in the ducts. In order to compare the experimental results with numerical results, the frequency inverter is maintained at 275 Hz to generate a constant flow velocity of 5.5 m/s. The flow velocity is measured at the middle of the testing section by TSI Model 8386 VelociCalc Plus. In our experiment, TSI 3475 Aerosol Generator generates high-concentration monodisperse aerosols by using di-2-ethyl hexyl sebacate (DEHS) as the aerosol material. The particle size from the aerosol generator has a high concentration of 2.5 μm. A compressed cylinder supplies a constant flow rate of nitrogen at 250 l/h. The TSI 3330 optical particle sizer measures the particle concentration constantly distributed above the patterned surface.
From numerical simulation results (Section 3), the best overall efficiency among these optimized shapes is the semi-circular patterned surface. The experimental deposition velocity was tested and compared between a clean surface and the semi-circular shape at $p/e=3$, $p/e=4$, $p/e=5$ and $p/e=6$. In Figure 3, the height of the semi-circular surface is 2 mm, which is consistent with the numerical geometry. Figure 4 displays the results of a particle deposition experiment with a clean surface and semi-circular patterned surface at the $p/e$ of 4. The photos are taken by a Nikon eclipse Ni-E microscope. Figure 4(a) and (b) are views on the clean surface before and after deposition. Figure 4(c) and (d) are views displayed on the bottom surface between semi-circular structure before and after deposition. Each view in Figure 4 (a)-(d) represents a rectangular range of $790 \mu m \times 790 \mu m$. The particle deposition on the semi-circular surface is more obvious than the particle deposition on the clean surface.

A deposition velocity will be calculated based on the particle deposition number and undisturbed particle concentration (measured by GRIMM particle sizer). After the figures were observed under the
microscope, the deposited particles were contrasted against the background. The contact area of each particle was identified by using ImageJ software.

\[ A_{\text{s}-l} = \pi V_{\text{cap}} \left( \frac{\pi}{3} \left( 2 - 3\cos \alpha + \cos^3 \alpha \right) \right)^{-2/3} \sin^2 \alpha \]  

Based on the area of planar surface under the microscope visualization, the volume of aerosol deposited in each picture can be determined by Equation (8). The particle deposition number \( N_d \) can be obtained by using the volume of each droplet divided by the volume of each monodispersed aerosol. The deposition duration \( t_d \) is 10 minutes. The comparison of particle deposition velocity for different \( p/e \) of a semi-circular shape between experiment (black) and numerical simulation (red) is displayed in Figure 5. The largest discrepancy between the experiment and numerical simulation at the \( p/e \) of 4 is 26.5%. The highest deposition velocity happens at \( p/e=4 \) for the semi-circular patterned surface.

5. Conclusions

Particle deposition enhancement by various patterns of surface rib (rectangular, triangular, semi-circular and open-circular) are presented in this work by using the Reynolds stress turbulent model and Lagrangian particle tracking. The semi-circular pattern has the highest overall efficiency when compared with other patterned surfaces for all \( p/e \) conditions. The numerical simulation results were then compared and validated with experimental deposition velocity. At \( p/e=4 \), the experiment and numerical simulation both indicate the highest deposition velocity for the semi-circular patterned surface. Thus the semi-circular patterned surface is recommended to be used in ventilation ducts to enhance the particle deposition as well as increase the energy efficiency of large buildings.

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