Alpha-decay-correlated mass measurement of $^{206,207g,m}$Ra using an $\alpha$-TOF detector equipped multi-reflection time-of-flight mass spectrograph system

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The atomic masses of the isotopes $^{206,207}$Ra have been measured via decay-correlated mass spectroscopy using a multi-reflection time-of-flight mass spectograph equipped with an $\alpha$-TOF detector. The Ra isotopes were produced as fusion-evaporation products in the $^{51}$V+$^{155}$Ta reaction system and delivered by the gas-filled recoil ion separator GARIS-II at RIKEN. The $\alpha$-TOF detector provides for high-accuracy mass measurements by correlating time-of-flight signals with subsequent $\alpha$-decay events. The masses of $^{206}$Ra and $^{207g,m}$Ra were directly measured using a multi-reflection time-of-flight mass spectograph equipped with an $\alpha$-TOF detector. The mass excesses of $^{206,207}$Ra and the excitation energy of $^{207m}$Ra were determined to be $M_{E}=3540(50)$ keV/$c^2$, 3538(15) keV/$c^2$, and $E_{\alpha}=552(42)$ keV, respectively. The $\alpha$-decay branching ratio of $^{207m}$Ra, $\beta_{\alpha}=0.26(20)$, was directly determined from decay-correlated time-of-flight signals, and the reduced alpha width of $^{207m}$Ra was calculated to be $\delta^2 = 43^{+68}_{-34}$ keV from the branching ratio. The spin-parity of $^{207m}$Ra was confirmed to be $J^p = 13/2^-$ from decay correlated mass measurement results.

I. INTRODUCTION

The structure of heavy and superheavy nuclides are strongly influenced by shell effects, and investigations of the ground and excited state properties provide us important information for the understanding of these nuclides. The binding energy of the ground state nuclide, as a direct mapping of the shell structure, is best determined through decay and reaction $Q$-values. To preclude possible errors, which can compound in long decay chains, requires direct measurements. An exemplary case of such was the direct mass measurement of $^{150}$Ho by Penning-trap mass spectrometry at CERN/ISOLDE, wherein they found that the indirect measurements, from by $\beta$-decay spectroscopy, had an 800 keV discrepancy due to a misidentification of the excited and ground states $^{[1,2]}$.

The structure of $\gamma$-transitioning isomers has been studied with high precision based on $\gamma$-ray spectroscopy. However, there are still many nuclides in which the isomeric states undergo direct $\alpha$- or $\beta$-decay, precluding the application of $\gamma$-ray spectroscopy. Separately, there have been a number of decay spectroscopy measurements assisted by mass separation, utilizing both Penning traps and multi-reflection time-of-flight mass spectrographs (MRTOF-MS). The first experiment where such trap-assisted decay spectroscopy was performed with REX-TRAP at CERN/ISOLDE for conversion electron studies $^{[3]}$. Since then, several experiments have been performed using high-resolution mass separators coupled with a decay station $^{[4,5]}$. Apart from an effort to measure half-lives using variable storage time in an ion trap connected to an MRTOF $^{[6]}$, until now when performing trap-assisted decay spectroscopy the mass determinations and decay measurements were performed independently; the mass spectrometers have always been employed as high-resolution mass separators.
Recently, we have developed a novel detector, which we refer to as an α-TOF [10], that can simultaneously measure ion implantation (to deduce time-of-flight) and subsequent α-decay events from implanted ions. From these correlated signals, we can perform mass and decay spectroscopy for multiple nuclides simultaneously. We have previously described the use of this decay-correlated mass spectroscopy to suppress background. Other nuclear properties can be inferred using the detector; the life-time of each nuclide, for instance, can be determined from the time intervals between the time-of-flight signal and the decay signal. In this paper, we report on the decay-correlated mass spectroscopy of $^{206,207}$Ra using an MRTOF-MS equipped with an α-TOF detector, demonstrating several capabilities beyond atomic mass determination.

II. EXPERIMENTS

Decay-correlated mass measurements were performed at the SHE-Mass-II facility, jointly operated under the auspices of RIKEN Nishina Center and KEK Wako Nuclear Science Center, within the RIKEN RI Beam Factory. The experimental setup is shown in Fig. 1. A primary beam of $^{51}$V$^{13+}$ was prepared [11], pre-accelerated by the RILAC-II linear accelerator, and injected into the RIKEN Ring Cyclotron (RRC) where it was accelerated to 306.0 MeV and impinged upon targets in front of the gas-filled recoil ion separator GARIS-II [12].

Sixteen targets of $^{159}$Tb, produced by sputtering onto 3.0-µm thick Ti backing foils and having an average thickness of 460-µg/cm$^2$, were mounted on a 16-sector rotating target wheel [13], which rotated at 2000 revolutions per minute during the beam irradiation. While the peak cross-section for the desired reactions occurs well below 306.0 MeV, the RRC could not deliver a lower energy beam. As such, 12.5-µm Al foil energy degraders were also mounted on the target wheel [14], upstream of the targets. By using the energy degraders, the primary beam energy at target center was 219.1 MeV. To pass $^{207}$Ra the magnetic rigidity of GARIS-II was set to 1.66 Tm; the He-gas pressure was set to 71 Pa. Under this setting, the evaporation residues (ERs) produced in the $^{159}$Tb($^3$He, p) reaction were efficiently transported while the unreacted primary beam and other background products were suppressed by GARIS-II.

A secondary beam degrader made from 9.6-µm-thick Mylar foil was installed in the focal plane chamber of GARIS-II. The energy-degraded ERs were then stopped and thermalized in a cryogenic helium gas cell, pressurized to 100 mbar room-temperature-equivalent and cooled to 50 K. The thermalized ions were extracted from the gas cell using a traveling wave radio frequency (RF) carpet [15], transferred to an RF ion guide and transported to an RF ion trap suite. After a final cooling process in the “flat trap” [16] (see Fig. 1), the ions were orthogonally ejected from the trap and injected into the MRTOF-MS. In this experiment, the MRTOF-MS was optimized to produce a time focus after 266 laps.

If the mean time between ion implantations is too short compared to the α-decay half-life, subsequent ion implantation may occur prior to α-decay. Such events can impede decay-correlation and decay spectroscopy. Therefore, for the α-decay correlated measurements of $^{207m}$Ra ($T_{1/2} = 59$ ms), the incoming rate of total ion of $^{207}$Ra at the MRTOF-MS was limited to about 0.2 cps by reducing the primary beam current to approximately 100 pA, corresponding to an impinging beam of $6.2 \times 10^{12}$ particles per second.

Two measurement runs were performed. The first was six hours in duration, while the second was an hour-long measurement wherein ions made an extra lap in the MRTOF to confirm identifications. Making measurements at two different numbers of laps ensures that we do not erroneously misattribute TOF peaks from e.g. stable molecular ions making an arbitrary number of laps and coincidentally having a TOF similar to our analyze. In principle, by making correlations between TOF and subsequent α-decay, this precaution is not necessary, however it does provide an added layer of confirmation.

III. ANALYSIS AND RESULTS

Figure 2 shows the full-range TOF singles spectra for the two runs. In Run #1, the MRTOF-MS timing was configured such that $A/q = 103.5$ ions would make 266 laps in the MRTOF and $A/q = 103$ ions would make 267 laps; care was taken to ensure ions of both
$A/q$ were not effected by the ejection-side mirror switching [17]. Among the $A/q = 103.5$ ions, $^{207}$Ra$^{2+}$ and $^{207}$Fr$^{2+}$ were identified, while $^{206}$Ra$^{2+}$ and $^{206}$Fr$^{2+}$ were identified among the $A/q = 103$ ions. To exclude misidentification of these ions, in Run #2 the ejection mirror timing was adjusted such that $A/q = 103.5$ ions made 265 laps and $A/q = 103$ ions made 266 laps. As the same identifications were made in this hourlong cross-check measurement, we can be confident of the identifications. The lack of particularly mass selective elements between the gas cell and MRTOF automatically allows for the simultaneous study of multiple $A/q$ chains. The tune of the MRTOF used in this work resulted in $A/q = 103, 103.5$ chains having flight lengths differing by one lap, and their relative separation changes only slightly with small variations in the lap number. Other isobaric chains, however, will generally exhibit larger changes in their relative position in the time-of-flight spectrum under small variations in the lap number.

The times-of-flight were determined from TOF spectral peaks by fitting using an asymmetric Gaussian-hybrid function [18]:

$$f(t) = \begin{cases} 
A \delta t (2t - 2t_c + \delta t_c)/2\sigma^2 & (t \leq t_L), \\
A e^{-(t-t_c)^2/2\sigma^2} & (t_L < t < t_R), \\
A \delta t (2t - 2t_c + \delta t_c)/2\sigma^2 & (t \geq t_R),
\end{cases}$$

where $A$ is the Gaussian peak height, $t_c$ is the Gaussian centroid (i.e. the time-of-flight) and $\sigma$ is the standard deviation. The fit function smoothly transitions from Gaussian to exponential on both sides of the peak, with the transition point defined to be $t_L = t_c - \delta t_c$ on the left side and $t_R = t_c + \delta t_c$ on the right side.

The data in Fig. 2 has been drift-corrected using $^{85}$Rb$^+$ ions from a thermal ion source. These reference ions were measured concomitantly [19] with the analyte ions shown in Fig. 2. The time-of-flight spectra were divided into subsets of 7.5 s duration, each was fitted using Eq. [1], and then the times-of-flight of every ion (reference and analyte) in each subset were adjusted to compensate for drift.

The masses $m$ of ions with charge $q$ were determined using the single-reference method [20, 21]

$$m = \frac{q}{q_{\text{ref}}} \rho^2 m_{\text{ref}} = \frac{q}{q_{\text{ref}}} \left( \frac{t - t_0}{t_{\text{ref}} - t_0} \right)^2 m_{\text{ref}},$$

where $\rho$ is the time-of-flight ratio between the analyte and reference, and $t_0$ is the delay between the time-to-digital converter start signal and the ejection from the preparation ion trap which sends ions to the MRTOF-MS. When analyte and reference ions are isobaric, the contribution of $t_0$ becomes negligible and can be ignored. The analyte ions were identified from their time-of-flight ratios with the $^{85}$Rb$^+$ ions, using Eq. [2] with $t_0 = 40(4)$ ns. In this work $^{206, 207}$Fr$^{2+}$ ions were used as isobaric references in the precise determination of the masses of $^{206, 207}$Ra.

The $\alpha$-singles spectrum measured during Run#1 is shown in Fig. 3(a). Directly transported $^{207}$Fr, $^{207}$Ra, $^{206}$Fr, and $^{206}$Ra were observed, along with their Rn, Po, and At isotope decay products. Figures 3(b) and (c) show the TOF-correlated $\alpha$-decay spectra for $^{207}$Ra$^{2+}$ and $^{206}$Ra$^{2+}$, respectively.

The probability of an accidental coincidence is calculated from the ratio of the total coincidence time gate to the total measurement time. In the analysis of $^{207}$Ra shown in Fig. 3(b), we selected 180 ms as the coincidence time ($T_c$), which corresponds to three half-lives of $^{207}$mRa. According to this coincidence time and the counting of time-of-flight signals, we estimated that 1.8% of the $^{207}$Ra produced accidental coincidences. Consequently, the decay-coincidence gated ToF spectrum is contaminated with 8.6% of the counts being $^{207}$Ra$^{2+}$. Nonetheless, it can be seen that the isomeric component is greatly enhanced compared to singles spectrum.

In the analysis of $^{206}$Ra, shown in Fig. 3(c), we selected a coincidence time of $T_c = 960$ ms. The accidental coincidence rate induced by $^{207g/\text{Ra}}, \ 206\text{Fr},$ etc. was calculated to be 1.5%. In this case there are no isomeric states to hinder the correlation analysis.

The decay energies of $^{207}$Ra and $^{206}$Ra were determined to be 7.354(28) MeV, and 7.294(23) MeV, respectively, by application of least-square fitting of the TOF-correlated $\alpha$-decay spectra. To provide a calibration in the determination of absolute decay energy, the alpha-decay energy of $^{207}$Ra was fixed to the literature value of 7.131 MeV [22]. The intensity of $^{207}$Ra used in the fitting process was fixed by the calculated number from the $\alpha$-decay singles spectrum. These results are in agreement with literature values derived from precise $\alpha$-decay measurements [22, 23].

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**FIG. 2.** The full-range time-of-flight singles spectra for two setting of the MRTOF-MS. (a) The upper panel shows the result of the six hour measurement wherein $A/q = 103.5$ ions made 267 laps; (b) the lower panel shows the result of the one hour measurement wherein $A/q = 103.5$ ions made 265 laps. The dashed blue lines indicate the positions of the Fr and Ra isotopes, demonstrating that their relative positions were largely constant under change of lap number between the two runs. Several peaks, presumed to be stable molecular ions extracted from the gas cell were observed but did not correlate with $\alpha$-decay signals.
Figure 4 shows the time-of-flight spectra measured in the two runs, centered on the ions 206Fr2+ and 206Ra2+. The TOF singles spectra are shown in black, while the 206Ra α-decay correlated TOF spectra are shown in blue. A spurious ion species, presumably a stable molecular ion, can be seen in the tail of the 206Ra2+ case of 267 laps, but it is suppressed by the decay correlation.

Within a region of ±50 ns of the center of the 206Ra2+ spectral peaks there were 162 decay-correlated TOF events using Tc = 960 ms, out of 327 TOF singles events. The fraction of correlated events, 49(5)%, agrees well with the previously reported α-TOF efficiency 10.

The isobaric molecular ions should all have the same peak shape, and therefore we simultaneously fit the two spectra (singles and α-decay correlated) for each run with the width and exponential tail parameters conserved across all peaks. While the spurious intruder ion may exhibit a slightly different shape, its low intensity precludes any minor shape difference resulting in significant biasing of the fit parameters.

A more pressing issue, if we wish to use isobaric referencing, is the isomerism of 206Fr. Were all three states delivered, the second isomer (Ecx = 730 keV) would be resolvable in the TOF spectra with the mass resolving power of this experimental conditions (Raa ≈ 178,000) but the first isomer (Ecx = 190 keV) would be unresolvable. However, were 206Fr to be delivered as an admixture of ground state and first isomer with comparable intensities, the peak width would be noticeably broadened. As the 206Fr2+ and 206Ra2+ peaks are well-reproduced with a shared peak width, we can presume the 206Fr2+ peak is dominated by either the ground state or first isomer. In an experiment conducted at ISOLDE, the population of 206Fr produced by the spallation reaction of UCx was about two times larger than that of 206m1Fr 20, so we presume 206Fr2+ to be the highly dominant state in our analysis.

Table I summarizes the mass analysis results for 206Ra2+. The weighted average mass excess of 206Ra determined from the TOF singles spectra was ME = 3548(50) keV/e², while the decay-correlated data yielded ME = 3460(92) keV/e². Both of these values are in agreement with the ME from literature value 25, confirming the device performance.

In addition to mass measurements, the α-TOF detector allows for determination of half-lives. Figure 4 provides a histogram of the time between ion implantation and subsequent α-decay, gated on the 7250±250 keV alpha-decay energy characteristic of 206Ra in Run#1. By fitting the histogram data to an exponential decay with constant background a half-life for 206Ra of T1/2 = 260(55) ms was determined. From Run#2, totally 21 decay correlated events were obtained. These half-lives were determined to be T1/2 = 360(100) ms from the mean value, as the maximum likelihood value 27. The weighted average of Run #1 and Run #2 was calculated and the half-life of 206Ra was determined to be T1/2 = 283(48) ms, which is in good agreement with the T1/2 = 240(20) ms literature value 24. From the experimental results and literature values, a new global half-life of 206Ra, T1/2 = 248(18) ms, is obtained.
Counts / 40 ms

Counts / 3 ns

Decay time [ms]

Counts / 3 ns

Time-of-flight [μs]

FIG. 5. Decay time spectrum as a histogram of the time interval between the ion implantation signal used to determine the time-of-flight and the subsequent α-decay signal of appropriate energy: (a) full range up to 5 s, (b) the first 1.2 s. The half-life of 206 Ra was determined to be 260(55) ms by fitting this data as an exponential decay with constant background (solid red curve).

TABLE I. The measured time-of-flight ratio ρ between 206 Ra²⁺ ion and the reference ion (206 Fr²⁺), mass excess (ME) and half-life of of 206 Ra from TOF singles and decay-correlated TOF data. The mass deviations (ΔME) are comparisons with the literature value ME_{Lit} from AME2020 [25].

| laps    | ρ       | ME_{EXP} [keV] | ΔME [keV] | T_1/2 [ms] |
|---------|---------|----------------|-----------|------------|
| Singles | 267     | 1.00001266(142)| 3540(54)  | 26(57)     |
|         | 266     | 1.00001266(140)| 3594(130)| 26(131)    |
| Correlated | 267    | 1.000012256(270)| 3461(103)| 105(104)  | 260(55) |
|         | 266     | 1.000012249(556)| 3458(213)| 107(214)  | 360(100) |
| Weighted Averages | Singles | 1.000012483(131)| 3548(50)  | 18(53)     |
|         | Correlated | 1.000012255(241)| 3468(93)  | 103(95)    | 283(48) |

B. 207 Ra

A similar set of analyses was performed for 207 Ra. Figure 6 shows the time-of-flight spectra accumulated in Run #1, with the TOF singles histogram in black and the 207m Ra α-decay correlated TOF histogram in blue; due to the incoming rate of 207 Ra²⁺ (T_{1/2}=1.38 s) higher than the decay rate, it was not possible to perform decay correlations for the ground state. To minimize incidental correlations between 207 Ra²⁺ TOF and 207 Ra α-decay, the energy gate had a lower limit of 7.32 MeV (207 Fr from the 207 Ra α-decay energy) resulting in slight reduction in the efficiency. A coincidence time gate of T_c < 180 ms, corresponding to approximately three half-lives of 207m Ra, was used. This is shorter than the typical four half-lives, again to suppress the amount incidental coincidence with 207 Ra decays. Despite these efforts we find that 14% of the counts in the decay-correlated ToF spectra (blue histogram in Fig. 6) are derived from 207m Ra²⁺ as noted by the dashed green curve in Fig. 6. The two states of 207 Ra could not be resolved in the singles time-of-flight spectrum alone; the fitting of the two components did not converge, although the peak width indicated multiple components were present.

Similar to the case of 206 Ra, the spectral peaks were fit such that the TOF singles spectral peaks of 207g,m Ra²⁺ and 207 Fr²⁺, the decay-correlated TOF spectral peak of 207m Ra²⁺, and the incidentally correlated 207 Ra²⁺ had mutually-fixed values for the peak-width and exponential tail parameters; the fraction of 207g,m Ra²⁺ ions in the fit of the decay-correlated spectrum was fixed to 14%. Using the position of the isomeric state determined from decay-correlated events as a fixed parameter when fitting the TOF singles spectrum, the two-component fit reliably converged and the times-of-flight for the two states could be ascertained.

The masses of 207g,m Ra²⁺ were determined from the ratio of their times-of-flight with that of 207 Fr²⁺ using Eq. 2. Decay-correlated spectra were produced using a coincidence time of 180 ms, as previously discussed. From these measurements, the time-of-flight ratio of 207g,m Ra²⁺ were measured ρ_g = 1.000016550(38) and ρ_m = 1.000017983(109) with reference species 207 Fr²⁺. The mass excess of 207g Ra and excitation energy of 207m Ra are determined to be ME = 3538(15) keV/c² and E_{ex} = 552(42) keV respectively, which consistent with previous indirectly determined values, ME_{Lit} = 3510(60) keV/c² and E_{ex,Lit} = 554(15) keV, based on α-decay spectroscopy [22, 25].

Additionally, the half-life of 207m Ra was determined using the decay-correlated TOF events. The decay time distribution, determined with an energy gate of E_{α} ≥ 7.32 MeV applied to the data of Run #1, is shown in Fig. 7. The fitting results show that the half-life of 207m Ra is 55(9) ms in agreement with the literature value of 59(4) ms. From Run #2, we obtained only one decay-correlated event of 207m Ra. While these are low statis-
tics, it is consistent with the number assumed from the production and alpha branching ratios (discussed later). There are 317 TOF singles events of $^{207m}$Ra, and the expected correlated events based on energy gate width and detection efficiency would be 2.6 events. When considering the Poisson distribution, the probability of getting less than one event when 2.6 events are expected is 27%, which is statistically reasonable. Unfortunately, however, a similar analysis to that of Run #1 data is not possible. Therefore, the data obtained from Run #2 were used primarily to confirm the identity of $^{207}$Fe$^{2+}$ and $^{207}$Ra$^{2+}$ based on their unchanging relative times-of-flight.

The first study of $^{207m}$Ra was reported in Heßberger et al. [23]. They estimated the production ratio of $^{207m}$Ra/$^{207}$Ra to be 0.75/0.25 in the reaction system of $^{58}$Fe$^{+}$,$^{154}$Sm, and that the alpha-branching ratio of $^{207m}$Ra was $b_{\alpha} < 0.25$. Subsequent experiments by Leino et al. [29], have also supported this alpha-branching ratio.

Since we can unambiguously determine the ratio of ground state to isomer from the TOF singles spectrum, it is also possible to derive the alpha-decay branching ratio and partial half-life of $^{207m}$Ra using the alpha-TOF detector. To determine the alpha-decay branching ratio we must determine the number of alpha-decays from $^{207m}$Ra which occurred at the detector and the total number $^{207m}$Ra atoms deposited on the detector during the experiment.

While we cannot fully resolve the spectral peaks from $^{206}$Ra and $^{207m}$Ra in the alpha singles spectra of Fig. 3 (a), the fitting results indicate the total number of alpha-decays $N_{\text{sum}} = N_{206\text{Ra}} + N_{207m\text{Ra}} = 305 \pm 21.4$ from $^{206}$Ra and $^{207m}$Ra were detected. The TOF-correlated alpha-decay spectrum gated on $^{206}$Ra$^{2+}$ consisted of $N_{206\text{Ra}} = 162 \pm 12.7$. Thus, after correcting $N_{\text{sum}}$ for detector efficiency, we conclude that $N_{207m\text{Ra}} = 245 \pm 49.5$ alpha-decays from $^{207m}$Ra occurred on the alpha-TOF detector in the course of the measurement.

The total number of $^{207m}$Ra deposited on the detector can be determined from the TOF singles spectra (Fig. 5). The two-component fit of the $^{207g}$Ra$^{2+}$ spectral peak indicated a ratio of 0.60(2)/0.40(2) for the ground state to isomer yield, similar to the yield ratio observed in the $^{58}$Fe$^{+}$,$^{154}$Sm reaction system. After correcting for the TOF detector efficiency, we determined that 945 $^{207g}$Ra$^{2+}$ ions implanted upon the detector during the measurement. Thus, the alpha-decay branching ratio of $^{207m}$Ra could be determined to be 26(20)%, in agreement with the value of 25% previously reported from alpha-decay spectroscopy [28, 29].

### IV. DISCUSSION

The spin-parity of $^{207m}$Ra has tentatively assigned to $J^\pi = 13/2^+$, based on the systematics of the neighboring nuclei [22]. The single particle level diagrams for odd Ra and Rn nuclides are shown in Fig. 8. The solid red circle in Fig. 8 is the excitation energy of $^{207m}$Ra obtained from our decay-corrected mass analysis. It agrees with the prior study from alpha-decay spectroscopy. The systematics continue to suggest that spin-parity is $J^\pi = 13/2^+$. The spin-parity of $^{207}$Ra is assigned to either $J^\pi = 3/2^-$ or $5/2^-$ based on systematics. If $J_{\pi} = 3/2^-$ then the configuration is $(\pi h_{9/2})_{0}^{+}(\nu f_{5/2})_{-1}$ while if $J_{\pi} = 5/2^-$ then the configuration would be $(\pi h_{9/2})_{0}^{+}(\nu f_{5/2})_{-1}$. However, the spin-parity of $^{207g}$Ra cannot be determined from this experiment.

From our results, the reduced alpha width of $^{207m}$Ra can be evaluated to be $\delta^2 = 40^{+34}_{-38}$ keV, according to the...
Rasmussen prescription [30]. Table II describes the reduced alpha width of $^{203}\text{Ra}$ and $^{205}\text{Ra}$. Prior to our study, the reduced alpha width of $^{203}\text{Ra}$ and $^{205}\text{Ra}$ were reported to be around 60 keV for both states [31]. $^{207}\text{Ra}$ is suggested to be $13/2^+$ not only in terms of single particle level systematics, but also from the reduced alpha width systematics. The reduced width is consistent with that of the neighboring nuclides, indicating that the $\alpha$-decay of $^{207}\text{Ra}$ is not forbidden.

| Isotope | $J^m$ | $E_\alpha$ [keV] | $T_{1/2}$ [ns] | $b_\alpha$ | $\delta^2$ [keV] | Ref. |
|---------|-------|-----------------|---------------|------------|----------------|-----|
| $^{203}\text{Ra}$ | 3/2   | 7575(10)        | 50.715        | 1.0        | 45.714         | [31]|
| $^{205}\text{Ra}$ | 13/2+ | 7607(8)         | 37.379        | 1.0        | 48.348         | [31]|
| $^{207}\text{Ra}$ | 3/2   | 7340(20)        | 210.40        | 1.0        | 50.177         | [24]|
| $^{205}\text{Ra}$ | 13/2+ | 7370(20)        | 170.49        | 1.0        | 48.188         | [24]|
| $^{207}\text{Ra}$ | 3/2   | 7131(5)         | 1380.110      | 0.86       | 37.680         | [24]|
| $^{205}\text{Ra}$ | 13/2+ | 7354(28)        | 55.9          | 0.26(20)   | 43.34         | this work |

$^a$ tentatively assigned 3/2$^-$ or 5/2$^-$. 

**V. SUMMARY**

This work has shown that the correlation measurements of mass and decay properties by use of an MRTOF-MS equipped with the $\alpha$-TOF detector, proving that not only the unique determination of the excitation energy of an isomeric state, but also its branching ratio and partial half-life can be derived simultaneously. The results are in agreement with the historical $\alpha$-spectroscopy measurements, and successfully demonstrated the value of simultaneous mass and decay spectroscopy with MRTOF-MS equipped with the $\alpha$-TOF detector. In particular, the mass of $^{207}\text{Ra}$ and the excitation energy of $^{207}\text{Ra}$ were directly measured for the first time. The nuclear structure could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of this technique is expected to contribute to further investigations the nuclear structure of heavy and superheavy nuclides.

Recently, we have achieved a mass resolving power $R_m \approx 700,000$ for our MRTOF system. Additionally, the improvement of the energy resolution of the $\alpha$-TOF detector is currently underway. The combination of the MRTOF-MS and the $\alpha$-TOF detector, especially as mass and energy resolutions improve, will make a significant contribution to the investigation of the level structure of nuclides even for rare event cases such as the superheavy nuclides.

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