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Electronic structure and magnetic exchange interactions of Cr-based van der Waals ferromagnets. A comparative study between CrBr$_3$ and Cr$_2$Ge$_2$Te$_6$.

*Ab initio* calculations and high-pressure experiments unveil the microscopic mechanism behind the magnetic properties of two Cr-based van der Waals ferromagnets that have different electronic structure.

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Electronic structure and magnetic exchange interactions of Cr-based van der Waals ferromagnets. A comparative study between CrBr₃ and Cr₂Ge₂Te₆†

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Low dimensional magnetism has been powerfully boosted as a promising candidate for numerous applications. The stability of the long-range magnetic order is directly dependent on the electronic structure and the relative strength of the competing magnetic exchange constants. Here, we report a comparative pressure-dependent theoretical and experimental study of the electronic structure and exchange interactions of two-dimensional ferromagnets CrBr₃ and Cr₂Ge₂Te₆. While CrBr₃ is found to be a Mott–Hubbard-like insulator, Cr₂Ge₂Te₆ shows a charge-transfer character due to the broader character of the Te 5p bands at the Fermi level. This different electronic behaviour is responsible for the robust insulating state of CrBr₃, in which the magnetic exchange constants evolve monotonically with pressure, and the proximity to a metal–insulator transition predicted for Cr₂Ge₂Te₆, which causes a non-monotonic evolution of its magnetic ordering temperature. We provide a microscopic understanding for the pressure evolution of the magnetic properties of the two systems.

I. Introduction

Two-dimensional (2D) materials have increased their academic and technological relevance continuously since the successful synthesis of graphene in 2004.1 Many other materials, like transition metal dichalcogenides,2 boron nitride (BN)3 or phosphorene, have been profusely studied since then.4 Recently, long-range ferromagnetic (FM) order in several atomic-thick materials, such as FePS₃,5 CrI₃,6 and itinerant Fe₃GeTe₂,7 has been reported. The advent of long-range 2D ferromagnetism brings about new transport phenomena in two dimensions, like tunneling magnetoresistance8,9 and electrical switching of magnetic states,10 promoting 2D ferromagnets as versatile platforms for engineering new quantum states and device functionalities. Besides, 2D materials can exhibit multitude of exotic properties when combined in heterostructures.11

Layered van der Waals materials provide a unique platform to study the evolution of the magnetic exchange interactions when going from the 2D to the 3D limit. In particular, Cr-based van der Waals ferromagnets have gained attention over the past years due to their high magnetic moment and Curie temperature. In these compounds, magnetic order is determined by different exchange paths. For instance, the isotropic in-plane magnetic coupling J_{in} in transition metal dichalcogenides (TMDs), di- and trihalides and phosphosulfides, is determined by the competition between metal–metal direct exchange and indirect exchange mediated by the anions.12 These exchange paths have been found to be highly dependent on the crystal13 and electronic structure,14 and different strategies have been proposed to tune them.15,16

CrBr₃ and Cr₂Ge₂Te₆ crystallize in a lamellar structure with hexagonal symmetry (space group no. 148), forming a honeycomb network of edge-sharing octahedra, stacked with van der Waals gaps separating the Cr³⁺-rich planes, as shown in Fig. 1. Both compounds retain their bulk ferromagnetism down to the single layer limit, T_C = 34 K for CrBr₃ and T_C = 61 K for Cr₂Ge₂Te₆.
with an out-of-plane easy axis. This magnetic anisotropy is necessary to circumvent the restrictions of the Mermin–Wagner theorem, leading to a long-range FM order at the monolayer limit. Therefore, the stabilization of 2D magnetic order requires a comprehensive understanding of the magnetic exchange interactions and their evolution as a function of order parameters like dimensionality or external pressure. By combining ab initio calculations and high-pressure experiments on single crystals of CrBr₃ and Cr₂Ge₂Te₆, we explore their electronic structure, and the pressure dependence of the in- and out-of-plane exchange interactions, J_in and J_out, (shown in Fig. 1). The pressure dependence of the magnetization measurements shows a different trend of the magnetic transition temperature, T_C, for each compound. Our density-functional-theory-based calculations indicate that, while the evolution of T_C at low pressures is driven by progressive decrease of J_in for both systems, J_out is the dominant interaction in Cr₂Ge₂Te₆ at high pressure. We argue that the electronic band structure is responsible for the pressure evolution of the magnetic transition temperatures in each compound. Our work highlights the crucial role of electronic band structure to search for new materials retaining a large Curie temperature down to the monolayer limit.

The paper is organized as follows. In Section II, we describe the experimental and theoretical approaches used. Section III is devoted to report the electronic structure and magnetic exchange paths of both compounds, Section IV analyses the effect of dimensionality from the evolution of the electronic structure and magnetic properties under pressure. Finally, in Section V we provide a discussion of the results and a summary of the main conclusions of this work.

## II. Computational and experimental procedures

Electronic structure ab initio calculations were performed within the density functional theory framework using the all-electron, full potential code WIEN2K based on the augmented plane wave plus local orbital (APW + lo) basis set. For the structural relaxations, in particular the computation of the lattice parameters at different pressures, special exchange–correlation functionals were needed to deal with the out-of-plane van der Waals-type forces. The exchange–correlation term chosen to compute the exchange parameters was the generalized gradient approximation (GGA) in the Perdew–Burke–Ernzerhof scheme which is found to provide a good description of the electronic structure and magnetism. A fully-converged k-mesh of \( K_{\text{min}} K_{\text{max}} = 7.0 \) and muffin-tin radii of 2.42 a.u. for Cr, 2.07 a.u. for Ge, 2.19 a.u. for Br and 2.38 a.u. for Te, nicely converged with respect to all the input parameters in the simulations. Besides, the Curie temperature (T_C) at each pressure was obtained using 864 particles within a nearest-neighbour Heisenberg model, with the exchange parameters mapped by the Monte Carlo Metropolis algorithm. We have applied periodic boundary conditions and 10⁶ steps in total. The T_C was obtained by fitting the magnetization curves as explained in ref. 28.

![Fig. 1](image-url) Unit cells of (a) CrBr₃ and (b) Cr₂Ge₂Te₆. Cr atom in blue, Br atom in brown, Ge atom in yellow and Te atom in green. Different exchange constants are considered: an in-plane J_in that takes into account both the direct Cr–Cr exchange and the superexchange via Br or Te, and the out-of-plane J_out that couples out-of-plane Cr–Cr neighbours. (c) and (d) Show the top view of CrBr₃ and Cr₂Ge₂Te₆ unit cells, respectively.
Single crystals of CrBr$_3$ and Cr$_2$Ge$_2$Te$_6$ were synthesized from the purely elemental starting materials and provided by HQ graphene. The quality of the crystals was confirmed by X-ray diffraction and X-ray photoemission spectroscopy (XPS). X-ray absorption (XAS) and X-ray magnetic circular dichroism (XMCD) measurements up to 6 Tesla were performed at Cr L$_{2,3}$ edge at the BOREAS BL29 beamline at ALBA synchrotron. Magnetic measurements under pressure up to $P = 1$ GPa were performed in a Be–Cu cell, using a silicon oil as pressure medium, inside a MPMS SQUID from Quantum Design. The pressure was monitored in situ through the superconducting transition of a Sn pressure gauge. X-ray diffraction under pressure was carried out in a diamond anvil cell using 4:1 methanol:ethanol as pressure media. The pressure dependence of the lattice volume up to 5 GPa was fitted to the Birch–Murnaghan equation.

### III. Electronic structure and magnetism

In this section we will describe the electronic structure and magnetic interactions for both compounds. Fig. 2 shows the density of states computed with DFT for CrBr$_3$ and Cr$_2$Ge$_2$Te$_6$. In both cases, the electronic structure of Cr can be well described as a Cr$^{3+}$:d$^3$ cation with $S = 3/2$, the majority-spin t$_{2g}$ bands being fully occupied. For CrBr$_3$, the states just below and above the Fermi level have dominant Cr d character, thus suggesting a Mott insulator behaviour with a d–d energy gap (top panel in Fig. 2a). This result is in agreement with previous photoluminescence experiments.$^{20}$

On the other hand, for Cr$_2$Ge$_2$Te$_6$, the states just below the Fermi level are very broad and have dominant Te p character. A p–d energy gap is observed for this material, which suggests a charge transfer insulator behaviour. Ge atoms do not play a substantial role in the electronic structure, with a vanishing contribution close to the Fermi level (top panel in Fig. 2b).

Fig. 3a shows the experimental isotropic XAS taken at 2 K for Cr$_2$Ge$_2$Te$_6$. The isotropic spectrum is defined as the average of circular $\sigma^-$ and circular $\sigma^+$ polarized light. The two main peaks correspond to the 2p$_{3/2}$ (575 eV) and 2p$_{1/2}$ (585 eV) components of the 2p core level (split by spin–orbit coupling). The energy profile is comparable to Cr$_2$O$_3$, demonstrating a Cr$^{3+}$ oxidation state.$^{30}$

We have performed cluster calculations for the atomic-like 2p$^3$3d$^4$→2p$^3$3d$^4$ transition for Cr$^{3+}$ ($C_{3v}$ symmetry) using the crystal field theory (CFT) implemented in QUANTY.$^{31,32}$ The method accounts for the intratomic 3d–3d and 2p–3d coulomb and exchange interactions, the atomic 2p and 3d spin–orbit couplings and the local crystal field parameters $D_{q}$, $D_{s}$ and $D_{t}$. We have adopted the values of $U = 0$ eV, $F_{0}^{dd} = 0.805$ eV, $F_{2}^{dd} = 15.61$ eV, $F_{4}^{dd} = 9.78$ eV, $F_{0}^{pd} = 4.89$ eV, $G_{1}^{pd} = 2.22$ eV and $G_{3}^{pd} = 1.26$ eV as input of the Slater integrals. The calculated ground state is four-fold degenerate with spin quantum numbers $S_z \sim \pm 3/2$ and $\pm 1/2$. The main
features of the spectra are well modelled with cluster calculations despite the low symmetry of the Cr site and the mixing of $t_{2g}$ and $e_g$ orbitals, assuming $D_{h} = 0.3$ eV, $D_{e} = 0$ eV and $D_{t} = 0$ eV. In Fig. 3b, we show the $\sigma^+ \text{and } \sigma^-$ polarized light and the XMCD spectra (inset) defined as $\sigma^+ - \sigma^- \text{together with the theoretical calculation. Again, the fitting reproduces the main peaks and splittings of the spectra, although the calculation does not model the low energy tail ($\sim 572$ eV) of the XMCD spectrum (inset).

From the theoretical point of view, the different energy contributions to the magnetic ground state can be modelled separately by considering the nearest-neighbour $J_{in}$ and the $J_{out}$ exchange couplings (see ESI† for more details). Four more exchange paths including second and third nearest neighbours have been included in previous works.33 Nevertheless, as we will discuss, our simple Heisenberg-type model suffices to explain the magnetic order as a function of pressure in these compounds. The different $j$'s are shown in Fig. 1, with the $J_{in}$ and $J_{out}$ depicted as broken red and blue lines, and the Cr$^{3+}$ cations surrounded by edge-sharing trigonally distorted octahedra. $J_{in}$ is the sum of two exchange contributions, the direct Cr–Cr exchange across the octahedral edge, which is antiferromagnetic (AF) between two half-filled $t_{2g}$ bands, and the indirect Cr–(Br or Te)–Cr superexchange at approximately 90-degrees. According to Goodenough–Kanamori–Anderson rules, the indirect exchange, cation–anion–cation, can be either FM or AF, depending on the strength of the delocalization and correlation superexchange effects.12 Our results show that $J_{in} = 27.5$ K and $J_{out} = 12$ K for Cr$_2$Ge$_2$Te$_6$ and $J_{in} = 28.5$ K and $J_{out} = 6$ K for CrBr$_3$. These values were obtained by fitting total energy differences between different magnetic configurations to a Heisenberg-type Hamiltonian. All $j$'s are positive, which explain the FM order observed in the experiments for both compounds. These results lead to theoretical Curie temperatures of $77$ K for Cr$_2$Ge$_2$Te$_6$ and $69$ K for CrBr$_3$, this small overestimation is in the range of acceptable values for GGA.

Fig. 4 shows the magnetization vs. temperature at $P = 0$ GPa for CrBr$_3$ and up to 1 GPa for Cr$_2$Ge$_2$Te$_6$. The magnetic transitions appear as an upturn in the magnetization upon cooling at 37 and 63 K, respectively, following a Curie–Weiss behavior at $T > T_C$.

IV. Evolution with pressure

We have carried out ab initio calculations, complemented with high-pressure magnetic and X-ray diffraction measurements to study the evolution of the electronic structure and magnetic exchange interactions. Naively, one can interpret the effect of isotropic pressure on the magnetic exchange interactions as a smooth evolution from a 2D-toward a more 3D-like magnetic state, since the $c$-axis compressibility is expected to be much larger than that of the $a$–$b$ plane.

Fig. 2 shows the DOS and the partial DOS (pDOS) as a function of pressure for both compounds. In Fig. 2a we see that CrBr$_3$ does not undergo a substantial modification of its electronic structure with pressure. The d–d energy gap observed at $P = 0$ GPa is preserved when pressure is raised up to 6 GPa (see Fig. 5a). However, Fig. 2b shows how the p–d energy gap of Cr$_2$Ge$_2$Te$_6$ closes as pressure is increased (see Fig. 5a). Therefore, our calculations predict that Cr$_2$Ge$_2$Te$_6$ undergoes an insulator to metal transition at high pressure. The values of the band gaps presented here were obtained using GGA, which has a tendency to underestimate them. This is less so when dealing with crystal-field gaps.34 Yet, the pressure evolution should be correct in any case.

Fig. 5b shows the pressure dependence of the cation–anion–cation angle. While for the Mott insulator CrBr$_3$, the angle shows a monotonic decrease up to 10 GPa, in Cr$_2$Ge$_2$Te$_6$ the angle remains constant in the whole range of pressures up to 10 GPa. Hence, external pressure modifies the internal structure of CrBr$_3$, while in Cr$_2$Ge$_2$Te$_6$, there is a pressure induced insulator to metal transition as a consequence of the closing of the energy gap due to the change in the Te–Cr distance and not the Cr–Te–Cr angle, which remains roughly unchanged.

In order to shed light on the nature of the pressure-induced metal–insulator transition predicted by our DFT calculations
for Cr\textsubscript{2}Ge\textsubscript{2}Te\textsubscript{6}, we have performed high pressure X-ray diffraction (XRD) measurements. In Fig. 6, we plot the pressure dependence of the ratio of the lattice parameters, \(c/a\), showing a sudden decrease above 7 GPa, suggesting a structural transition. This pressure coincides with the collapse of the electronic gap, as predicted by our \textit{ab initio} calculations. Pressure-induced structural phase transitions and amorphizations have been observed before by means of high pressure X-ray diffraction between 18 and 30 GPa for Cr\textsubscript{2}Ge\textsubscript{2}Te\textsubscript{6}. However, no structural anomalies were reported at pressures relevant in this work.\textsuperscript{35}

Fig. 4 and 7 display the evolution of the magnetic transition temperature of CrBr\textsubscript{3} and Cr\textsubscript{2}Ge\textsubscript{2}Te\textsubscript{6} up to 1 GPa. As seen in the raw data and summarized in Fig. 7, the \(T_c\) of both compounds decreases as pressure is applied, in agreement with previous reports\textsuperscript{36,37} and at odds with the expectations for the pressure dependence of the exchange interaction in a localized magnetic system. Harrison\textsuperscript{38} stated that the transition temperature for a localized system increases as a function of the distance between magnetic sites as \(r^{-(l+l'+1)}\), where \(l\) and \(l'\) are the angular momentum quantum numbers. This results in a variation of the magnetic exchange interaction with volume, \(J(V)\) as 3.3 and 4.6 for direct and indirect superexchange, respectively, the so-called Bloch’s rule.\textsuperscript{39} Violations of Bloch’s rule have been observed in Mott insulators close to a metal–insulator\textsuperscript{40} and spin-Peierls to Peierls\textsuperscript{41} transitions. Bloch’s rule describes the

![Graph 1](image1.png)

**Fig. 4** (a) Magnetization vs. temperature at zero pressure for CrBr\textsubscript{3}, \(H = 0.1\ T\). Inset: Linear pressure dependence of the magnetization at 10 K. (b) Temperature dependence of the magnetization (\(H = 0.1\ T\)) up to 1 GPa for Cr\textsubscript{2}Ge\textsubscript{2}Te\textsubscript{6}. Inset: Pressure dependence of the magnetization. At 10 K and above 6 kbar (0.6 GPa) the magnetization saturates in agreement with the pressure dependence of the in and out exchange interactions, \(J_{\text{in,out}}\), see text. (Red lines are guides to eye).

![Graph 2](image2.png)

**Fig. 5** (a) Calculated energy gap as a function of pressure for both compounds, obtained using the GGA exchange–correlation functional. (b) Evolution of the Cr–X–Cr angle as a function of pressure. X represents Br or Te atoms.

![Graph 3](image3.png)

**Fig. 6** Comparison of the high pressure XRD data with the results of our \textit{ab initio} calculation for the \(c/a\) ratio. DFT predicts a transition to a metallic state around the same pressure that XRD data shows a peak.
evolution with pressure of only one exchange constant. As we have seen above, in this case there is a competition between exchange constants that evolve differently with pressure, and even the \( J_{in} \) is in itself the addition of two competing exchange mechanisms. Our data also shows a different trend for \( T_C(P) \) than the simple Bloch’s rule prediction: while the critical temperature of CrBr\(_3\) displays a slightly convex decay, the decrease observed in Cr\(_2\)Ge\(_2\)Te\(_6\) is concave and shows a clear tendency to saturation at the highest pressures analyzed in this work. This behavior seems to go in hand with the pressure dependence of the magnetization at 10 K, which increases linearly with pressure for CrBr\(_3\) (inset of Fig. 4a), but remains nearly constant above 0.6 GPa for Cr\(_2\)Ge\(_2\)Te\(_6\), inset of Fig. 4b.

As previously described, the electronic structure shows largely ionic Cr\(^{3+}\): \( S = 3/2 \) cations with a half-filled spin-polarized \( t_{2g} \) and \( e_g \) manifold. This leads to a significant gap opening at the Fermi level for Cr\(_2\)Ge\(_2\)Te\(_6\) and CrBr\(_3\), even at the LDA/GGA level, without the need to introduce strong correlation effects in the calculations. In a first approximation, this indicates that the magnetic semiconductor limit could be applicable to understand the pressure dependence of these systems. Note that for the case of Cr\(_2\)Ge\(_2\)Te\(_6\) we have only performed this analysis at pressures where the system remains a semiconductor. However, even if the system can be described in the localized limit, various different exchange interactions compete, responding differently to pressure, and this leads to a complex pressure dependence of \( T_C \). We have calculated the pressure dependence of both \( J_{in} \) and \( J_{out} \). The system is fully relaxed at different volumes (including the lattice parameters \( c/a \) ratio and the internal positions), and used the Birch–Murnaghan equation for obtaining the pressure value at each volume.\(^{42}\) We set up a magnetic supercell combining different types of AF and FM couplings between the neighbouring Cr cations. The value of the magnetic exchange constants is obtained after subtraction of the total energy difference among various magnetic configurations, assuming these follow a simplistic Heisenberg-type spin Hamiltonian with neighbouring 3/2 spins for Cr as explained before. The results are summarized in Fig. 8. The ground state presents a FM coupling at low pressures, in agreement with experiments, but the different exchange constants behave differently with pressure, although all of them remain positive at all pressures, for both compounds.

With the calculated values of the magnetic exchange constants, we have set up a Heisenberg-type Hamiltonian of interacting spins, and solved it using a classical Monte Carlo simulation. This allowed us to obtain a theoretical \( T_C \) and its evolution with pressure. Despite the overestimation of the absolute value of magnetic exchange constants, the actual pressure dependence of the calculated \( T_C \) is in good agreement with the observed experimental trend, as it can be seen from a comparison between Fig. 7a and 8c. In this figure, the theoretical values are normalized to the \( T_C \) at ambient pressure. In the Heisenberg type Hamiltonian we have included an anisotropic term as in ref. 33, since it was reported that for Cr\(_2\)Ge\(_2\)Te\(_6\) this term changes its sign with pressure.\(^{43}\) However, no influence on the value of \( T_C \) or its pressure dependence was observed due to the much smaller energy scale of the anisotropic term.

For CrBr\(_3\), \( J_{out} \) increases with pressure while \( J_{in} \) decreases (Fig. 8a). Since \( J_{in} > J_{out} \) and the number of Cr in-plane neighbours is greater than the out-of-plane, the trend of \( T_C(P) \) is
governed by $J_{in}$. Therefore, decreasing $J_{in}$ produces the decrease of $T_C$ as pressure increases, in agreement with the experimental values in Fig. 7. On the other hand, for Cr$_2$Ge$_2$Te$_6$, $J_{out}$ increases with pressure, while, initially, $J_{in}$ decreases and saturates at higher pressure (see Fig. 8b). Therefore, $J_{in}$ dominates the change of $T_C$ at low pressures, but $J_{out}$ becomes the dominant term at higher pressures. This is in agreement with the experimental evolution presented for the $T_C$ with pressure (Fig. 7). Further experimental measurements at higher pressures should confirm the minimum in $T_C$ predicted in our calculations.

V. Conclusions

To summarize, pressure effects on the electronic, magnetic and structural properties of CrBr$_3$ and Cr$_2$Ge$_2$Te$_6$ have been explored following a combination of experimental and computational approaches. Our results show that CrBr$_3$ is a Mott–Hubbard like insulator with a d–d energy gap. It follows that the system remains insulating under pressure. On the other hand, the energy gap of Cr$_2$Ge$_2$Te$_6$ is found to have p–d character, which leads to a charge transfer insulating behaviour. Our calculations predict an insulator to metal transition to occur at 6 GPa assuming no structural transition takes place. Despite the high pressure X-ray data shows a structural transition at similar pressures, whether this structural transition is accompanied with a softening of the lattice on approaching the putative insulator to metal transition or a mere structural change to a lower symmetry semiconducting state, cannot be concluded from our data. Additionally, resistivity measurements under pressure are needed to clarify this issue.

Besides, we have found that the different electronic structure of CrBr$_3$ and Cr$_2$Ge$_2$Te$_6$ and its evolution with pressure are at the root of the pressure dependence of the Curie temperature and the magnetic exchange interactions in Cr$_2$Ge$_2$Te$_6$ and CrBr$_3$. The experimental observation yields a reduction of the Curie temperature as pressure is applied, in contrast to isostructural CrI$_3$ and VI$_3$, but with a different trend for each compound. *Ab initio* calculations reveal that the microscopic origin for this trend relies on the different pressure dependence of the in-and out-of-plane magnetic exchange couplings $J_{in,\text{out}} > 0$.

While the transition temperature for CrBr$_3$ is expected to monotonically decrease with pressure, the proximity of Cr$_2$Ge$_2$Te$_6$ to the metallic limit yields a non-monotonic behaviour. This effect was explained as a different behaviour of the in-plane magnetic exchange coupling constants as a function of pressure for each compound.

This work sheds light on the competition of the different types of exchanges that may occur in several other quasi-two-dimensional magnetic materials. Similar competition between direct and indirect in-plane exchange paths and off-plane couplings may occur, such as the d–i- and trihalides. In fact, it might be at the origin of the presence or absence of magnetic ordering in the monolayer of transition metal phosphorus trisulfides (TMPS$_3$) FePS$_3$ and NiPS$_3$. Long-range order depends on the type of spin–spin interactions, which themselves compete with intrinsic fluctuations and determine the magnetic anisotropy and the stability of long-range magnetic order at the monolayer limit. We have seen that in Cr-based van der Waals structures, these spin–spin interactions (and their competitions) are strongly dependent on the evolution of the electronic structure with pressure and, therefore, reciprocally, on the dimensionality.

Conflicts of interest

There are no conflicts to declare.

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