Article

Determining the Most Sensitive Socioeconomic Parameters for Quantitative Risk Assessment

Marin Akter 1,* , Rubaiya Kabir 2, Dewan Sadia Karim 2, Anisul Haque 2, Munsur Rahman 2, Mohammad Asif ul Haq 3, Momtaz Jahan 2 and Tansir Zaman Asik 2

1 Department of Mathematics, Bangladesh University of Engineering and Technology, Dhaka-1000, Bangladesh
2 Institute of Water and Flood Management, Bangladesh University of Engineering and Technology, Dhaka-1000, Bangladesh
3 Department of Electrical and Electronic Engineering, Green University of Bangladesh, Begum Rokeya Sarani, Dhaka -1207, Bangladesh
* Correspondence: marin.akter12@gmail.com; Tel.: +88-(0)-1516147854

Received: 12 June 2019; Accepted: 14 August 2019; Published: 3 September 2019

Abstract: Risk assessment of climatic events and climate change is a globally challenging issue. For risk as well as vulnerability assessment, there can be a large number of socioeconomic indicators, from which it is difficult to identify the most sensitive ones. Many researchers have studied risk and vulnerability assessment through specific set of indicators. The set of selected indicators varies from expert to expert, which inherently results in a biased output. To avoid biased results in this study, the most sensitive indicators are selected through sensitivity analysis performed by applying a non-linear programming system, which is solved by Karush-Kuhn-Tucker conditions. Here, risk is assessed as a function of exposure, hazard, and vulnerability, which is defined in the Intergovernmental Panel on Climate Change (IPCC) Fifth Assessment Report (AR5), where, exposure and vulnerability are described via socioeconomic indicators. The Kolmogorov-Smirnov statistical test is applied to select the set of indicators that are the most sensitive for the system to assess risk. The method is applied to the Bangladesh coast to determine the most sensitive socioeconomic indicators in addition to assessing different climatic and climate change hazard risks. The methodology developed in this study can be a useful tool for risk-based planning.

Keywords: risk assessment; socioeconomic indicators; sensitivity analysis; non-linear programming; Kolmogorov-Smirnov test

1. Introduction and Statement of Problem

1.1. Overview of the Research

Climate change’s impact has become the most important threat to human civilization. For the past few decades, climate change has increasingly affected the lives of people and all climate sensitive sectors. Due to the increasing scarcity of economic, social, and technical resources, various strategies for adaptation to climate change are in high-priority. Assessing risk is to examine the underlying socioeconomic, institutional, and, to a lesser extent, political and cultural factors. In order to minimize the risks of climate change, the identification of affected areas in planning and prioritization of adaptation processes becomes very important [1,2]. Several past studies quantified and compared vulnerability that generates risk by using an index [3]. To help increase consciousness, expedite development of plans and strategies, and aid decision making, composite indices are used. These are a set of collaborative, analytical, and communicative tools [4,5]. Development of suitable indicators
for risk assessment has gained awareness since the ground-breaking paper of Smit and Wandel [6] and the IPCC assessment report published in 2007 [7]. In risk assessments, indicators are used to ‘measure’ and ‘characterize’ the hazard, exposure, sensitivity, and adaptive capacity of a system. There is a growing necessity to develop indicators to assess risk to determine the strength of response plans over time and to better understand the fundamental processes. Risk is one of the most common techniques that utilizes indicators (different hazards and socioeconomic parameters), which represent the properties and characteristics of a given system [8,9]. Downing et al. [9] states that vulnerability indicators (i.e., comprising sensitivity and adaptive capacity indicators) can help identify and target vulnerable regions, sectors or populations, raise awareness, and be part of a monitoring strategy. Adger et al. made a proper distinction between the specific and generic parameters of climate change [10]. Brooks et al. provided an index of possible proxy indicators to evaluate the effect of climate change at national and regional levels [11]. Transfer between different scales of analysis is not possible in case of indicators, as they are context specific [12]. Procedures for indicator selection mainly follow two general approaches: one based on a conceptual understanding of relationships and another based on theoretical (statistical or mathematical) relationships. In most of the previous studies, researchers selected many indicators based on peer-reviewed studies [13,14]. In some studies, indicators were selected from local stakeholder workshops or expert opinion based on field survey [15], which are highly biased.

We are aware of the fact that risk assessment is generally uncertain where the uncertainty is originated from composite interactions of hazards and socioeconomic impacts. To date, most of the studies that proposed policy suggestions for improved adaptation strategies for risk reduction did not clearly explore the theoretical basis for the selection of indicators [16]. Incorporation of a multitude of strongly correlated variables in the vulnerability index can lead to inaccurate conclusions, as shown by Kocur-Bera [17]. Sensitivity analysis can be one possible solution to this problem, which is performed on multiple variables that constitute an index [18]. It is less resource intensive than generating an ensemble of a large number of variables.

1.2. Research Gap, Research Objectives, and Significance

Sensitivity analysis provides a powerful means of learning about the degree of sensitivity of all the socioeconomic parameters of the system. It primarily studies the degree of impact of each indicator on the composition of the indices [19]. This technique may be used to come up with a functional relationship between a small group of parameters and the response of the system output [20–22]. Baker et al. identified the sensitivity analysis method as one of the key quantitative analyses for risk management, as it can provide the groundwork for planning adaptation operations to minimize the risks associated with climate change [23]. The tool can also be used for the identification of uncertainties to prioritize additional research or data collection [24].

Various methods such as the differential method, analysis of variance (ANOVA), linear regression analysis (RA), response surface method (RSM), mutual information index (MII), fourier amplitude sensitivity test (FAST), Sobol’s method [25], and non-linear programming [26] can be used to perform sensitivity analysis.

In this study, non-linear programming is applied to the sensitivity analysis, which can be viewed as a part of mathematical optimization. Non-linear programming deals with optimization problems where the objective function or some of the constraints are non-linear. This method covers the whole system where the risk is assessed. In this study, the selected system is the coastal zone of Bangladesh.

This study is focused on solving the prime answer of the question, “How sensitive are single indicators and how does single indicator sensitivity influence the overall risk of the system?” In this study, risk is defined according to IPCC AR5 [27] to formulate the non-linear programming and to select the most sensitive indicators. This gives the ranking of the set of indicators. Within this ranking, a statistical test is performed to select the most sensitive indicators, which can be used to assess the risk in the selected system.
2. Method

Methodology of this study includes study area selection, selection of hazard and socioeconomic indicators in the study area, methodology and formulation of non-linear programming, solution of the non-linear programming, and statistical analysis to detect significant change.

2.1. Study Area Selection

To apply the methodology developed in this paper, a study area is needed where the required data of socioeconomic indicators are available. The coastal area of Bangladesh (Figure 1) is found suitable for this purpose. The extent of this coast covers a long distance inland [28] where about one-fourth of the country’s total population lives [29]. This population may increase to almost double by mid-century [30]. The coexistence of availability of resources [31], high poverty rate [32], and natural hazards [33] makes the selection of socioeconomic parameters complicated in this area. Data from available socioeconomic indicators in the study area are used to determine the most sensitive ones to assess risk.

![Figure 1. Area map.](image)

2.2. Hazards in the Study Area

The study area is vulnerable due to different types of natural hazards. The dominant hazards in this area are storm surges, floods, salinity, and river erosion (Figure 2). Necessary data for hazard assessment is extracted from model simulation results [34]. Storm surge is the result of cyclonic event that occurs in pre-monsoon (April–May) and post-monsoon (October–November) seasons. The main impact zone of storm surge is confined within the landfall location along the exterior coast [35]. Storm surge hazard (Figure 2a) is assessed by combining surge depth and cyclonic wind speed. Flooding is caused by combined action of fluvial flow from upstream rivers and tide from sea and occurs mainly during monsoon (June–September). The northern parts of the coast which are not protected by polders
(an encircled embankment) are mainly affected by flood [36]. The parameter used for flood hazard assessment (Figure 2b) is flood depth. Salinity in the study area is represented by the river salinity. Salinity intrusion in the region occurs during dry season (December–March). Salinity magnitude is the maximum in western and eastern region, whereas the central region has the minimum salinity [37]. Salinity hazard is assessed (Figure 2c) by using salinity magnitude in the rivers and estuaries. Erosion in the study area are mainly confined along the river banks [38]. To assess erosion hazards (Figure 2d), the total eroded area along the river bank is used as the hazard parameter.

![Figure 2. Hazards in the study area: (a) Storm Surge, (b) Flood, (c) Salinity, and (d) Erosion.](image)

2.3. Available Socioeconomic Indicators to Assess Risk in the Study Area

From the available data sources, 23 socioeconomic indicators are preliminary selected that can be used to assess risk in the area due to the four hazard indicators mentioned in Section 2.2. All of these 27 indicators (4 hazards and 23 socioeconomic) are divided into different domains. The methodology developed in this study is applied to determine the most sensitive indicators from this preliminary list to assess risk in the study area. Table 1 shows the preliminary selected indicators in different domains, their role in assessing risk, sources of data and data units.
Table 1. Total lists of hazards and socioeconomic indicators.

| Domain          | Indicators                              | Impact on Risk                                                                 | Data Source and Data Unit                                                                 |
|-----------------|-----------------------------------------|--------------------------------------------------------------------------------|------------------------------------------------------------------------------------------|
| **Exposure**    | Cropped Area                            | Negative impact on risk due to its exposure to hazard [39,40].                  | Data source: [41]. Data unit: Percentage of Cropped Area per unit of administrative area. |
|                 | Number of Household                     | Increased number of households causes increased risk [42,43].                  | Data source: [41]. Data unit: Percentage of Number of Household per unit of administrative area. |
|                 | Population Density                      | Increased population density increases exposed population to risk [43,44].       | Data source: [41]. Data unit: Total number of population per unit of administrative area.  |
| **Sensitivity** | Female to Male Ratio                    | Female population are more sensitive to risk than male population. Increased number of female populations increases risk. | Data source: [29]. Data unit: Ratio of female to male population.                         |
|                 | Poverty Rate                            | Poor people are sensitive to hazards. So, higher poverty rates are indicative of higher risk due to same hazard. | Data source: [29]. Data unit: Percentage of extreme poor lies below poverty line.         |
|                 | Dependent Population                    | Dependent population in an area are the women, children, and elderly people. These group of population are considered as less able to adaptation against risk [42,44,45]. | Data source: [29]. Data unit: Percentage of summation of women, children and elderly population to the total population of an administrative unit. |
|                 | Disabled People                         | Physically and mentally disabled people are more sensitive to hazard because of their inability and slow response during a hazard event [46]. | Data source: [29]. Data unit: Percentage of total disabled people to total number of population in an administrative unit. |
|                 | Unemployed Population                   | Unemployment decreases the coping capacity and increases the sensitivity and susceptibility to risk [47]. | Data source: [29]. Data unit: Percentage of total unemployed population to total population in an administrative unit. |
| **Adaptive Capacity** | Growth center                          | Growth center is an economic indicator. Increased number of this indicator indicates better economic strength and better adaptive capacity against vulnerability [48]. | Data source: [29]. Data unit: Number of growth center per 5000 of population in an administrative unit. |
|                 | Plantation                              | Plantation is considered as a buffer against storm surge hazard that reduces the initial thrust of the hazard. Reduction of hazard means reduction of risk [49]. | Data source: [34]. Data unit: Forest area (natural and artificial) per unit of administrative area. |
|                 | Aquaculture                             | Shrimp cultivation is the dominant aquaculture in the study area. Aquaculture is considered as an alternative livelihood to adapt against salinity hazard. | Data Source: [34]. Data unit: Shrimp cultivated area per unit of administrative area.       |
|                 | Cyclone shelter                         | Cyclone shelter is a structural adaptive measure against storm surge hazard. Increased number of cyclone shelter reduces number of human casualty and thus reduces storm surge risk [43,50]. | Data source: [51]. Data unit: Number of cyclone shelter per unit of administrative area. |
| **Cropping intensity** | Cropping intensity                     | Cropping intensity is an indicator of agricultural activity. Increased cropping intensity means increased adaptive capacity that reduces risk against hazard [39,46,52] | Data source: [41]. Data unit: Percentage of gross cropped area per net cropped area in an administrative unit. |
| **GDP**         | Gross Domestic Product (GDP)            | Gross Domestic Product (GDP) is an economic indicator. Higher GDP means better ability to recover from loss and reduce risk from hazard [53]. | Data source: [29]. Data unit: Gross Domestic Product per capita.                           |
| **Irrigation Equipment** | Irrigation Equipment                   | Shallow tube-well (Stw), Deep tube-well (Dtw), and Low Lift Pump (LLP) are known irrigation equipment in the study area. Increased number of Irrigation Equipment enable a farmer to better adapt with the hazard and thus reduce risk. | Data source: [29]. Data unit: Number of irrigation equipment per unit of cropped land area. |
Table 1. Cont.

| Domain                  | Indicators                                                                 | Impact on Risk                                                                 | Data Source and Data Unit                                                                 |
|-------------------------|-----------------------------------------------------------------------------|--------------------------------------------------------------------------------|------------------------------------------------------------------------------------------|
| Polder Area             | Polder is an encircled embankment constructed to prevent flood in the study area. Increased number of polders reduces flood and thus reduces flood risk [43,54]. | Data source: [53]. Data unit: Percentage of total poldered (embanked) area per administrative unit. |                                                                                           |
| Presence of Lifeline    | Lifeline is represented by water supply, sanitation and electricity. Higher number of line utilities are considered to increase adaptive capacity against vulnerability and thus reduces risk [43-45]. | Data source: [29]. Data unit: Percentage of tap water and other pond types surface water sources and percentage of connected sanitary and electricity lines per unit area of an administrative unit. |                                                                                           |
| Loan                    | Loan is considered as the credit facility by co-operative society and banks, particularly to recover from loss due to hazard. Increased loan facilities thus reduce risk due to hazard [55]. | Data source: [29]. Data unit: Percentage of total account holder per total number of populations in an administrative unit. |                                                                                           |
| Literacy Rate           | Literate people know better how to adapt with the vulnerability and reduce risk [42,44,45] | Data source: [29]. Data unit: Percentage of number of literate people per unit of administrative area. |                                                                                           |
| Number of Health care Provider | Health care providers play an important role to reduce human casualty during a hazard, which acts to reduce vulnerability and risk of the community [56]. | Data Source: [29]. Data unit: Percentage of health care provider compared to total population in an administrative unit. |                                                                                           |
| Paka and Semi-paka house | Paka and Semi-paka houses represent households which are structurally strong to resist impacts of hazard. Presence of these housing types reduces risk [43,45]. | Data source: [29]. Data unit: Percentage of Paka and Semi-paka houses compared to total number of households in an administrative unit. |                                                                                           |
| Communication Infrastructure | Communication infrastructure is represented by all types of structural measures related to communication. It acts as an adaptive capacity for a community and reduces vulnerability and risk during a hazard [43,44,57]. | Data source: [29]. Data unit: Weighted sum of length of different types of structural measures used for communication purpose in an administrative unit. |                                                                                           |
| Road Density            | Increased road density in an area increases the mobility during the time of hazard. This makes it possible to utilize other adaptive measures that reduces risk. | Data source: [29]. Data unit: Total road length in an administrative unit. |                                                                                           |

2.4. Non-Linear Programming to Determine the Most Sensitive Indicators

As mentioned earlier, the central research question of this paper is: ‘What are the most sensitive indicators that determine risk in a system?’ To answer this question, non-linear programming is applied to determine the most sensitive indicators in the study area from the list described in Section 2.3.

A non-linear programming system is a system that solves an optimization problem where some of the constraints are non-linear or the objective function is non-linear. A general constraint and unconstraint non-linear programming problem is to select n decision variables \(x_1, x_2, \ldots, x_n\) from a given feasible region in such a way as to optimize (minimize or maximize) a given objective function \(f(x_1, x_2, \ldots, x_n)\) of the decision variables [58]. The feasible region is defined as a boundary where all possible points of a non-linear programming problem satisfy the problem’s constraints [58]. A flow chart describing non-linear programming is shown in Figure 3.
2.4.1. Unconstrained Non-Linear Programming

The simplest non-linear programming problem is that of minimizing or maximizing a function [58].

\[ f : \mathbb{R}^N_x \rightarrow \mathbb{R}. \]  

(1)

An unconstrained non-linear programming problem is given by

\[ \min_{x \in \mathbb{R}^N_x} f(x) \]  

(2)

Where \( f : \mathbb{R}^N_x \rightarrow \mathbb{R} \) is a smooth and real valued objective function of the vector \( x \in \mathbb{R}^N_x \).

2.4.2. Constrained Non-Linear Programming

The problem is called a non-linear programming problem (NLP) if the objective function is non-linear and/or the feasible region is determined by non-linear constraints [58]. Thus, in minimization form, the general non-linear programming is stated as:

Minimize

\[ f(x_1, x_2, \ldots, x_n) \]  

subject to:

\[ g_1(x_1, x_2, \ldots, x_n) \leq b_1 \]  

(4)

\[ g_m(x_1, x_2, \ldots, x_n) \leq b_m \]  

(5)

where each of the constraint functions \( g_1 \) through \( g_m \) is given and \( b_1, b_2, \ldots, b_m \) are constant vectors.
2.5. Development of Non-Linear Programming System

There are some ‘disturbance parameters’ that are responsible for creating the ambiguous results in risk as well as vulnerability. To avoid chaos in risk and vulnerability analysis, a non-linear programming system is incorporated. For the development of this system, risk, hazard, exposure, and vulnerability are needed to be used as the constraints and the objective function under the system. For these, 23 (out of total 27, where 4 are hazard parameters) possible socioeconomic indicators (Section 2.3) are selected in this study area [27]. Risk is a multiplicative function (non-linear combination) of hazard, exposure, and vulnerability, where vulnerability is a simple linear combination of sensitivity and adaptive capacity [27].

In this research, the non-linear programming systems are developed from the linear and non-linear combination of parameters (Section 2.3) that are called decision variables. Here, risk is considered as an objective function and constraints are developed from the weighted scores of parameters for each spatial unit of the study area (a total of 139 administrative unit named as ‘upazila’). The relative weighted scores are calculated using PCA [59]. PCA gives a correlation matrix that identifies the principal component for a system [59]. Pearson correlation coefficient was used to find the weights of the parameters that describe how much an indicator can explain a component vector.

The coefficients of $x_1, x_2, x_3 \ldots \ldots x_{27}$ of each constraint of (1) are weights of indicators computed by applying PCA. The constant vectors $(a, b, c, d, e)$ which are defined in Section 2.4 are found to be maximum value from the weighed values of risk of upazilla. Mathematically, risk along with constraints to minimize risk is defined as:

\[
\begin{align*}
\text{Objective Function} & \quad \text{minimize } Risk = \text{Exposure} \times \text{Hazard} \times \text{Vulnerability} \\
\text{Constraints,} & \\
\text{Exposure} & = 0.38 x_1 + 0.38 x_2 + 0.24 x_3 \leq 0.78 (= a) \\
\text{Exposure + Sensitivity} & = 0.0919x_1 + 0.11x_2 + 0.06x_3 + 0.111x_4 + 0.051x_5 + 0.042x_6 + 0.09x_7 + 0.054x_8 \leq 0.54 (= b) \\
\text{Sensitivity} & = 0.013x_4 + 0.055x_5 + 0.0439x_6 + 0.107x_7 + 0.046x_8 + \leq 0.44 (= c) \\
\text{Hazard*Exposure} & = (0.38 x_1 + 0.38 x_2 + 0.24 x_3)(0.317x_{24} + 0.14x_{25} + 0.29x_{26} + 0.27x_{27}) \leq 0.337 (= d) \\
\text{Adaptive Capacity,} & \\
0.072x_9 & + 0.073x_{10} + 0.105x_{11} + 0.078x_{12} + 0.078x_{13} + 0.12x_{14} + 0.044x_{15} + 0.042x_{16} \\
0.109x_{17} & + 0.052x_{18} + 0.0812x_{19} + 0.052x_{20} + 0.037x_{21} + 0.018x_{22} + 0.033x_{23} \geq 0.64 (= e)
\end{align*}
\]

2.6. Solution of Non-Linear Programming System with Karush-Kuhn-Tucker (KKT) Conditions

In modern non-linear programming algorithms, the Fritz John and the Karush-Kuhn-Tucker conditions are directly applicable to practical optimization problems [60]. In this research, Karush-Kuhn-Tucker conditions [60] are used to solve the non-linear programming system. A prerequisite for stating KKT conditions is the Lagrangian function [60,61]. Consider the non-linear programming in general:

\[
\begin{align*}
\min f(y) \\
\text{s.t } g(y) & \leq 0 \\
\text{h(y)} & = 0
\end{align*}
\]

where $g(y)$ is a function of the inequality constraint and $h(y)$ is a function of the equality constraint.
The Lagrangian function is defined by:

$$L(y, l_0, \lambda, \mu) = l_0 f(y) + \sum_{i=1}^{N_g} \lambda_i g_i(y) + \sum_{j=1}^{N_h} \lambda_j h_j(y)$$  \hspace{1cm} (8)

Where $\lambda_i = [\lambda_1, \lambda_2, \cdots, \lambda_{N_g}]$, $\mu_j = [\mu_1, \mu_2, \cdots, \mu_{N_h}]$

$$g(y) = \begin{bmatrix} g_1 \\ g_2 \\ \vdots \\ g_{N_g} \end{bmatrix} \quad \text{and} \quad h(y) = \begin{bmatrix} h_1 \\ h_2 \\ \vdots \\ h_{N_h} \end{bmatrix}$$ \hspace{1cm} (9)

Taking $l_0 = 1$ for KKT condition,\hspace{1cm}

(i) $\nabla_y L(y^*, 1, \lambda, \mu) = 0$

(ii) $\nabla_{\mu} L(y^*, 1, \lambda, \mu) = h(y^*) = 0$

(iii) $\nabla_{\lambda} L(y^*, 1, \lambda, \mu) = g(y^*) \leq 0$

(iv) $\lambda^T g(y^*) = 0$

(v) $\lambda \geq 0$

where gradient $\nabla f = \left[ \begin{array}{c} \frac{\partial f}{\partial y_1} \\ \vdots \\ \frac{\partial f}{\partial y_{N_g}} \end{array} \right]$

Necessary conditions for KKT [60] are:

(1) $f(y)$ is to be feasible to apply the above constraints (iv) and (v).

(2) Gradients of (iii), (iv), and (v) improve objectives and satisfies the following equations:

$$\nabla f(x^*) - \sum_{i=1}^{K} \lambda_i^* \nabla h_i(y^*) - \sum_{j=1}^{m} \lambda_j^* \nabla g_j(y^*) = 0$$

$$\lambda_i^* g_i(y^*) = 0 \quad \text{(Complementary Slackness)}$$ \hspace{1cm} (11)

(3) It satisfies to the positive Lagrangian multiplier $\lambda^* \geq 0$.

Using these conditions, a set of equations are formulated for the required values of variables (decision parameters) to minimize the objective functions.

Applying the above methodology, a MATLAB code to solve the non-linear programming problem (Equation 1) is developed.

2.7. Statistical Analysis to Detect Significant Change

Two risk levels are developed for all spatial units (in this case spatial unit is the ‘upazila’, which is an administrative unit one step below the district level). One risk level is based on the base risk scores of each upazila, considering all 23 socioeconomic indicators. The other risk level is developed by using the risk scores calculated by elimination of indicators one-at-a-time. Statistical tests are performed to examine whether there are significant changes between these two risk levels. To detect statistically significant change between two risk levels, the Kolmogorov-Smirnov test [62–65] is performed. The test is performed by calculating the difference between two risk levels $c_1$ and $c_2$. To perform these tests,
the following hypotheses are applied where $C_{1i}$ is the base risk score considering 23 indicators and $C_{2i}$ is the risk score after elimination of indicators one-at-a-time:

$$H_0 : C_{1i} = C_{2i}; \text{there is no significant change between two curves} \quad (12)$$

$$H_1 : C_{1i} \neq C_{2i}; \text{there is a significant change between two curves} \quad (13)$$

Cumulative distributions of $c_1$ curve and $c_2$ curve are $C_{f1i}, C_{f2i}$. Cumulative distributions are calculated by the following formulae:

For $C_{f1i}$

$$C_{f11} = C_{11}$$
$$C_{f12} = C_{11} + C_{12}$$
$$C_{f13} = C_{11} + C_{12} + C_{13}$$
$$\vdots \vdots \vdots \vdots \vdots$$
$$C_{f1N} = C_{11} + C_{12} + C_{13} + \cdots + C_{1N} \quad (14)$$

where N is number of upazila.

Moreover, for $C_{f2i}$

$$C_{f21} = C_{21}$$
$$C_{f22} = C_{21} + C_{22}$$
$$C_{f23} = C_{21} + C_{22} + C_{23}$$
$$\vdots \vdots \vdots \vdots \vdots$$
$$C_{f2N} = C_{21} + C_{22} + C_{23} + \cdots + C_{2N} \quad (15)$$

The distance (D) between cumulative distributions are calculated as the maximum distance by applying the following formula

$$\text{Distance}(D) = \sup_{1 \leq i \leq 138} (C_{f1i} - C_{f2i}) \quad (16)$$

Here, 138 represents the total number of spatial units (in this case upazila). Distance (D) implies the dissimilarity between two curves.

3. Results and Discussion

A non-linear programming system with inequality and equality constraints is designed from 27 (23 socioeconomic and 4 hazards) possible parameters (decision variables) by using normalized scores of each parameter. This non-linear programming problem is solved by KKT conditions and it gives the rank of indicators during the risk minimization process (which is the ultimate target). Variation of the coefficient of variables in the objective function describes the sensitivity of the parameters (decision variables). A MATLAB code is developed for the solution of the non-linear programming problem where one function ‘lambda’ is defined in the code named as the Lagrangian multiplier. This ‘lambda’ displays the lower limit and the upper limit of the coefficients of variables of the objective function. If the coefficients of variables of the objective function vary within the range between the lower limit and the upper limit, risk (the objective function) is optimized (minimized), otherwise the risk varies. This implies that the range between the lower and upper limit gives the rank among the indicators where lower deviation gives the most sensitive parameter and higher deviation gives the least sensitive parameter (Table 2). Based on this ranking (Table 2), domain specific indicators are arranged according to their ranking (Table 3).
3.1. Selection of the Most Significant Indicators

The most significant indicators are selected by applying a process of elimination of indicators among the ‘ranked indicators’, which are determined by applying non-linear programming (Table 2). Elimination criteria is based on measuring ‘statistically significant’ change (10% dissimilarity between the c1 and c2 levels) when one indicator is ‘eliminated’ from the system. In order to evaluate how much effect a single parameter can have on the overall analysis, the analysis is performed repeatedly
by excluding the parameters one-at-a-time, while keeping the total number of ‘used’ parameters the same for each case. The elimination process is started by excluding the least significant indicator first and the process is repeated by eliminating each indicator one-at-a-time. To measure statistically significant change of the risk score (when one is eliminated from the system) from the base risk score, the Kolmogorov-Smirnov test is applied in testing the difference between the two risk scores. Both the risk scores are cumulatively distributed, and the maximum difference is found between the two cumulative risk scores which implies the percentage of dissimilarity. Table 4 represents the elimination list of indicators and Figure 4 shows the insignificant change due to the elimination process.

Table 4. Elimination list of indicators.

| Indicators       | Domain          |
|------------------|-----------------|
| Elimination_1    | Road Density    |
| Elimination_2    | Presence of Lifeline |
| Elimination_3    | Number of Health care Provider |
| Elimination_4    | Unemployed Population |

For the fifth elimination, when the second least sensitive indicator (Disabled People) from the sensitivity domain is excluded, the dissimilarity is found to be above 10% of the base risk score, as shown in Figure 5. Similarly, when the fourth least sensitive indicator from the adaptive capacity domain (Literacy Rate) are eliminated, more than 10% dissimilarity is calculated (Figure 6). Thus, we can conclude that these two parameters show significant dissimilarity from the base risk score, which entitles them to be included in the most sensitive indicators.

Completion of statistical analysis gives the final set of indicators (19 socioeconomic indicators are finally selected from a list of 23 as described in Section 2.3), which are the most sensitive socioeconomic indicators for risk assessment in the study area (Table 5).
The most sensitive domain specific indicators selected in Table 5 are applied to assess storm surge risk in the study area (Figure 7). The risk map shows risk zones varying from very high to very low (Figure 7). The risk map generated in this way by using the most sensitive indicators can be used in risk-based planning. If we consider ‘the most sensitive indicators’ as the ‘most sensitive sectors’ that generate high risks due to ‘inadequate investment’, then policy makers can decide in which sector they will invest to minimize risk in a location. As sensitivity of these indicators are determined from a system approach, policy makers can view the system response from the generated risk map after an investment is made in a specific sector that is considered the most sensitive for the system. In this way, investment on a less sensitive sector can be avoided in risk-based planning. The method can be made dynamic by re-computing the most sensitive indicators with the changed biophysical and socioeconomic settings.
Table 5. List of most sensitive domain specific socioeconomic indicators.

| Indicators | Exposure | Adaptive Capacity | Sensitivity |
|------------|----------|-------------------|-------------|
| Cropped Area | | | |
| Number of households | | | |
| Population density | | | |
| Cyclone shelter | | | |
| Plantation | | | |
| Polder | | | |
| Growth Centre | | | |
| GDP | | | |
| Irrigation Equipment | | | |
| Paka and Semi-paka house | | | |
| Loan | | | |
| Communication Infrastructure | | | |
| Cropping intensity | | | |
| Aquaculture | | | |
| Literacy Rate | | | |
| Female to male ratio | | | |
| Poverty Rate | | | |
| Dependent Population | | | |
| Disabled People | | | |

Figure 7. Risk map in the study area by applying the most sensitive indicators.

4. Conclusions and Recommendations

The sensitivity analysis made in this study shows that non-linear programming is effective to select the most sensitive indicators for risk assessment. It helps avoid the multi-collinearity and
disturbance among the parameters. It provides an appropriate insight into the problems associated with the system under constraints. Using this method, it is possible to assess how sensitive a solution is due to any change in one or more parameters. In this research, for sensitivity analysis, risk is considered as an objective function under some inequality and equality constraints that are developed with the values of each parameter (indicators) for each spatial unit for different domains—i.e., exposure, sensitivity, adaptive capacity, and hazards. This system is solved by the KKT conditions. This creates a ranking among the indicators. For statistical analysis, a Kolmogorov-Smirnov test is performed for the selection of a set of indicators that are most sensitive for the system. This test is performed by eliminating indicators one-at-a-time from the ranked indicators. By repeating the process for each indicator, the most sensitive indicators for quantitative risk assessment are found. This method was applied with regard to the Bangladesh coast in an effort to determine the most sensitive domain specific socioeconomic indicators, which assessed risk due to four dominant hazards in the region. The methodology developed in this study can be a useful tool in risk-based planning. Policy makers can decide which sector they will invest that will effectively minimize risk in a specific location and can avoid investing on the less sensitive sector. At the same time, they will be able to visualize the system response due to investment on the most sensitive sector. The method has limited applicability for the region where amount of data availability is too low with questionable accuracy.

**Author Contributions:** Conceptualization, M.A.; Data curation, R.K., D.S.K. and T.Z.A.; Formal analysis, M.J.; Methodology, M.A.; Resources, M.R.; Supervision, A.H.; Writing – review & editing, M.A.u.H.

**Funding:** International Development Research Centre: 107642.

**Acknowledgments:** This work was carried out under the Collaborative Adaptation Research Initiative in Africa and Asia (CARIAA), with financial support from the UK Government’s Department for International Development (DFID) and the International Development Research Centre (IDRC), Canada. The views expressed in this work are those of the creators and do not necessarily represent those of DFID and IDRC or its Board of Governors. Website: [www.deccma.com](http://www.deccma.com).

**Conflicts of Interest:** The authors declare no conflict of interest.

**References**

1. UNFCCC. Climate change: Impacts, Vulnerabilities and Adaptation in Developing Countries. Available online: [http://unfccc.int/resource/docs/publications/impacts.pdf](http://unfccc.int/resource/docs/publications/impacts.pdf) (accessed on 18 August 2019).
2. Krishnamurthy, P.P.; Lewis, K.; Choularton, R.J. A methodological framework for rapidly assessing the impacts of climate risk on national-level food security through a vulnerability index. *Glob. Environ. Chang.* 2014, 25, 121–132. [CrossRef]
3. Hahn, M.M.; Riederer, A.A.; Foster, S.S. The livelihood vulnerability index: A pragmatic approach to assessing risks from climate variability and change—A case study in mozambique. *Glob. Environ. Chang.* 2009, 19, 74–88. [CrossRef]
4. Bapista, S.R. *Design and Use of Composite Indices in Assessments of Climate Change Vulnerability and Resilience*; USAID: Washington DC, USA, 2014; Available online: [http://www.ciesin.org/documents/Design_Use_of_Composite_Indices.pdf](http://www.ciesin.org/documents/Design_Use_of_Composite_Indices.pdf) (accessed on 18 August 2019).
5. Sullivan, C.; Meigh, J. Targeting attention on local vulnerabilities using an integrated index approach: The example of the climate vulnerability index. *Water Sci. Technol. J. Int. Assoc. Water Pollut. Res.* 2005, 51, 69–78. [CrossRef]
6. Smit, B.; Wandel, J. Adaptation, adaptive capacity and vulnerability. *Glob. Environ. Chang.* 2006, 16, 282–292. [CrossRef]
7. Cruz, R.R.; Harasawa, H.; Lal, M.; Wu, S.S.A.; Punsalmaa, B.; Honda, Y.; Jafari, M.; Li, C.; Huu Ninh, N. Asia. Climate Change 2007: Impacts, adaptation and vulnerability. In *Contribution of Working Group II to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change*; van der Linden, P., Parry, M., Canziani, O., Palutikof, J., Hanson, C., Eds.; Cambridge University Press: Cambridge, UK, 2007; pp. 469–506.
8. Gallopín, G.G. Environmental and sustainability indicators and the concept of situational indicators. A system approach. *Environ. Model. Assess.* 1996, 1, 101–117. [CrossRef]
9. Downing, T.E.; Butterfield, R.E.; Cohen, S.; Huq, S.; Moss, R.; Raham, A.; Sokona, Y.; Strphen, L. *Vulnerability Indices: Climate Change Impacts and Adaptation*; Policy Series, 3; UNEP: Nairobi, Kenya, 2001.

10. Adger, W.N.N.; Brooks, G.; Agnew, B.A.; Eriksen, S. *New Indicators of Vulnerability and Adaptive Capacity; Technical Report 7*; Tyndall Centre for Climate Change Research: Norwich, UK, 2005.

11. Brooks, N.; Adger, W.N.; Kelly, P.M. The determinants of vulnerability and adaptive capacity at the national level and the implications for adaptation. *Glob. Environ. Chang.* 2004, 15, 151–163. [CrossRef]

12. Vincent, K. Uncertainty in adaptive capacity and the importance of scale. *Glob. Environ. Chang.* 2007, 17, 12–24. [CrossRef]

13. Gizachew, L.; Shimelis, A. Analysis and mapping of climate change risk and vulnerability in Central Rift Valley of Ethiopia. *Afr. Crop. Sci.* J. 2014, 22, 807–818.

14. Žurovec, O.; Čadro, S.; Sitaula, B.K. Quantitative assessment of vulnerability to climate change in rural municipalities of Bosnia and Herzegovina. *Sustainability* 2017, 9, 1208. [CrossRef]

15. Wiréhn, L. *Climate Vulnerability Assessment Methodology: Agriculture under Climate Change in the Nordic Region*; Linköping University Electronic Press: Linköping, Sweden, 2017; Volume 732.

16. Eakin, H.; Luers, A.A. Assessing the vulnerability of social-environmental systems. *Annu. Rev. Environ. Resour.* 2006, 31, 365–394. [CrossRef]

17. Kocur-Bera, K. Sensitivity Analysis of the Index of a Rural Municipality’s Vulnerability to Losses Resulting from Extreme Weather Events. In Proceedings of the “Environmental Engineering” 10th International Conference, Vilnius Gediminas Technical University, Vilnius, Lithuania, 27–28 April 2017.

18. Krawczyk, E.; Wrzesińska, J. The use of sensitiveness analysis to the effectiveness’ risk of building and implementation of the cadastre communications system, Zeszyty Naukowe SGGW w Warszawie. *Ekonomika i Organizacja Gospo-darki Żywno-stwuwe* 2009, 74, 111–121.

19. Tate, E. Social vulnerability indices: A comparative assessment using uncertainty and sensitivity analysis. *Nat. Hazards* 2012, 63, 325–347. [CrossRef]

20. Fronzek, S.; Carter, T.T.; Räisänen, J.; Ruokolainen, L.; Luoto, M. Applying probabilistic projections of climate change with impact models: A case study for sub-arctic palska mires in Fennoscandia. *Clim. Chang.* 2010, 99, 515–534. [CrossRef]

21. Saltelli, A.; Nardo, M.; Saisana, M.; Tarantola, S. Composite indicators: the controversy and the way forward. In *Statistics, Knowledge and Policy Key Indicators to Inform Decision Making: Key Indicators to Inform Decision Making*; OECD Publishing: Paris, France, 2005; pp. 359–372.

22. Dessai, S.; Hulme, M. Assessing the robustness of adaptation decisions to climate change uncertainties: a case study on water resources management in the East of England. *Glob. Environ. Chang.* 2007, 17, 59–72. [CrossRef]

23. Baker, S.; Ponniah, D.; Smith, S. Survey of Risk Management in Major UK Companies. *J. Prof. Issues Eng. Educ. Pract.* 1999, 125, 94–102. [CrossRef]

24. Cullen, A.C.; Frey, H.C. *Probabilistic Techniques in Exposure Assessment*; Plenum Press: New York, NY, USA, 1999.

25. Nguyen, A.T.; Reiter, S. A performance comparison of sensitivity analysis methods for building energy models. *Build. Simul.* 2015, 8, 651–664. [CrossRef]

26. Fiacco, A.V. Sensitivity analysis for nonlinear programming using penalty methods. *Math. Program.* 1976, 10, 287–311. [CrossRef]

27. IPCC. *Impacts, Adaptation and Vulnerability. Contribution of Working Group II to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change*; Canziani, M.L., Palutikof, O.F., van der Linden, J.P., Hanson, P.J., Eds.; Cambridge University Press: Cambridge, UK, 2007; pp. 7–22.

28. Islam, R. Pre and post tsunami coastal planning and land use policies and issues in Bangladesh. In Proceedings of the Workshop on Coastal Area Planning and Management in Asian Tsunami-Affected Countries, Bangkok, Thailand, 27–29 September 2006.

29. Bangladesh Bureau of Statistics (BBS). *Community Series 2011, Planning Division, Ministry of Planning; Government of the People’s Republic of Bangladesh*: Dhaka, Bangladesh, 2011.

30. World Bank. *Implications of Climate Change on Fresh Groundwater Resources in Coastal Aquifers in Bangladesh*. In *Agriculture and Rural Development Unit, Sustainable Development Department, South Asia*; World Bank: Washington, DC, USA, 2009.

31. GoB (Government of Bangladesh). *State of the Coast; Integrated Coastal Zone Management Program; Ministry of Water Resources and Water Resources Planning Organization*: Dhaka, Bangladesh, 2006.
32. Dasgupta, S.; Kamal, F.A.; Khan, Z.H.; Choudhury, S.; Nishat, A. River Salinity and Climate Change: Evidence from Coastal Bangladesh, Policy Research Working Paper 6817; World Bank: Washington, DC, USA, 2014.

33. Bangladesh Bureau of Statistics (BBS), World Bank and World Food Programme. Updating Poverty Maps of Bangladesh; BBS: Dhaka, Bangladesh, 2009.

34. Guariguata, M.R.; Cornelius, J.P.; Locatelli, B.; Forner, C.; Sánchez-Azofeifa, G.A. Mitigation needs adaptation: Tropical forestry and climate change. Mitig. Adapt. Strateg. Glob. Chang. 2008, 13, 793–808. [CrossRef]

35. Holand, I.S. Lifeline Issue in Social Vulnerability Indexing: A Review of Indicators and Discussion of Indicator Application. Nat. Hazards Rev. 2015, 16. [CrossRef]

36. Haque, A.; Kay, S.; Nichols, R.J. Present and future fluvial, tidal and storm surge flooding in coastal Bangladesh. In Ecosystem Services for Well-Being in Deltas; Nicholls, R.J., Hutton, C.W., Adger, W.N., Hanson, S.E., Rahman, M.M., Eds.; Palgrave Macmillan: London, UK, 2018.

37. Shamsuddoha, M.; Chowdhury, R.K. Climate Change Impact and Disaster Vulnerabilities in the Coastal Areas of Bangladesh; COAST Trust: Dhaka, Bangladesh, 2007.

38. Haque, A.; Nichols, R.J. Floods and the Ganges-Brahmaputra-Meghna delta. In Ecosystem Services for Well-Being in Deltas; Nicholls, R.J., Hutton, C.W., Adger, W.N., Hanson, S.E., Rahman, M.M., Eds.; Palgrave Macmillan: London, UK, 2018.

39. Hiremath, D.B.; Shiyani, R.L. Analysis of Vulnerability Indices in Various Agro-Climatic Zones of Gujarat. Indian J. Agric. Econ. 2013, 68, 122–137.

40. Wu, J.; Lin, X.; Wang, M.; Peng, J.; Tu, Y. Assessing Agricultural Drought Vulnerability by a VSD Model: A Case Study in Yunnan Province, China. Sustainability 2017, 9, 918. [CrossRef]

41. Akter, M.; Jahan, M.; Kabir, R.; Karim, D.S.; Haque, A.; Rahman, M. Risk Assessment based on Fuzzy Synthetic Evaluation along Bangladesh Coast. Sci. Total Environ. (Elsevier) 2018, 658, 818–829. [CrossRef] [PubMed]

42. Soil Resource Development Institute (SRDI). Reconnaissance Soil Survey Reports; Ministry of Agriculture, Government of People’s Republic of Bangladesh: Dhaka, Bangladesh, 2008.

43. Armas, I.; Gavris, A. Social vulnerability assessment using spatial multi-criteria analysis (SEVI model) and the Social Vulnerability Index (SoVI model)—A case study for Bucharest, Romania. Nat. Hazards Earth Syst. Sci. 2013, 13, 1481–1499. [CrossRef]

44. Kabir, R. Determination of critical risk due to storm surges in the coastal zone of Bangladesh. Master’s Thesis, Institute of Water and Flood Management, Bangladesh University of Engineering and Technology, Dhaka, Bangladesh, November 2017.

45. World Bank. Economics of Adaptation to Climate Change. 2011. Available online: http://www.worldbank.org/en/news/feature/2011/06/06/economics-adaptation-climate-change (accessed on 18 August 2019).

46. Toufiqu, K.A.; Mohammad, Y. Vulnerability of Livelihoods in the Coastal Districts of Bangladesh. Bangladesh Dev. Stud. 2013, XXXVI, 95–120.

47. Hemingway, L.; Priestley, M. Natural hazards, human vulnerability and disabling societies: a disaster for disabled people? Rev. Disabil. Stud. Int. J. 2014, 2. Available online: http://hdl.handle.net/10125/58270 (accessed on 21 August 2019).

48. Satterthwaite, D. Climate change and urbanization: Effects and implications for urban governance. In Proceedings of the United Nations Expert Group Meeting on Population Distribution, Urbanization, Internal Migration and Development, DESA, New York, NY, USA, 21–23 January 2008; pp. 21–23.

49. Nakhooda, S.; Watson, C. Adaptation Finance and the Infrastructure Agenda; Working Paper 437; Overseas Development Institute: London, UK, 2016.

50. DECCMA. DELtAs Vulnerability and Climate Change. 2018. Available online: http://generic.wordpress.soton.ac.uk/deccma/wp-content/uploads/sites/181/2017/02/online-version_small_Climate-Change-Migration-and-Adaptation-in-DeltasKey-findings-from-the-DECCMA-project.pdf (accessed on 1 January 2019).

51. Zanetti, V.B.; Junior, W.; Freitas, D. A Climate Change Vulnerability Index and Case Study in a Brazilian Coastal City. Sustainability 2016, 8, 811. [CrossRef]

52. CEGIS. Report on Cyclone Shelter Information for Management of Tsunami and Cyclone Preparedness, Centre for Environmental and Geographic Information Services (CEGIS); Ministry of Food and Disaster Management: Dhaka, Bangladesh, 2009.

53. Cutter, S.L.; Bryan, J.B.; Lynn, S.W. Social vulnerability to environmental hazards. Soc. Sci. Q. 2003, 84, 242–261. [CrossRef]
54. Xenarios, S.; Nemes, A.; Golam, W.S.; Sekhar, N.U. Assessing vulnerability to climate change: are communities in flood prone areas in Bangladesh more vulnerable than those in drought-prone areas? *Water Resour. Rural Dev.* 2017, 7, 19. [CrossRef]

55. Bruijn, K. Resilience indicators for flood risk management systems of lowland rivers. *Int. J. River Basin Manag.* 2004, 2, 199–210. [CrossRef]

56. World Bank. Agriculture Finance & Agriculture Insurance. 2018. Available online: http://www.worldbank.org/en/topic/financialsector/brief/agriculture-finance (accessed on 18 August 2019).

57. Paterson, J.; Berry, P.; Ebi, K.; Varangu, L. Health care facilities resilient to climate change impacts. *Int. J. Environ. Res. Public Health* 2014, 11, 13097–13116. [CrossRef]

58. Jeong, D.H.; Ziemkiewicz, C.; Ribarsky, W.; Chang, R.; Center, C.V. *Understanding Principal Component Analysis Using a Visual Analytics Tool*; Charlotte Visualization Center, UNC Charlotte: Charlotte, NC, USA, 2009.

59. Ruszczyński, A. *Nonlinear Optimization*; Princeton University Press: Princeton, NJ, USA, 2006; ISBN 978-0691119151.

60. Emil, G. Optimality Conditions. 2013. Available online: http://www.eng.newcastle.edu.au/eecs/cdsc/books/cce/Slides/OptimalityConditions.pdf (accessed on 18 August 2019).

61. Zuzana, N. The Karush-Kuhn-Tucker Conditions. 2015. Available online: https://www.cs.cmu.edu/~ggordon/10725-F12/slides/16-kkt.pdf (accessed on 18 August 2019).

62. Chakravarti, I.M.; Laha, R.G.; Roy, J. *Handbook of Methods of Applied Statistics*; John Wiley and Sons: Hoboken, NJ, USA, 1967; Volume I, pp. 392–394.

63. John, C.; Cleveland, W.; Kleiner, B.; Tukey, P. *Graphical Methods for Data Analysis*; Wadsworth, Inc.: Wadsworth, OH, USA, 1983.

64. Chatfield, C. *The Analysis of Time Series: An. Introduction*, 4th ed.; Chapman & Hall: New York, NY, USA, 1989.

65. Cleveland, W. *Elements of Graphing Data*; Wadsworth, Inc.: Wadsworth, OH, USA, 1985.

© 2019 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).