Long Distance Cavity Entanglement by Entanglement Swapping Using Atomic Momenta

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Abstract
We propose a simple technique to generate entanglement between distant cavities by using entanglement swapping involving atomic momenta. For the proposed scheme, we have two identical atoms, both initially in their ground state, each incident on far apart cavities with particular initial momenta. The two cavities are prepared initially in superposition of zero and one photon state. First, we interact each atom with a cavity in dispersive way. The interaction results into atom-field entangled state. Then we perform EPR state measurement on both atomic momenta state which is an analog of Bell measurement. The EPR state measurement is designed by passing the atoms through cavity beam splitters which transfers the atomic momentum state into superposition state. Finally, these atoms are detected by the detector. After the detection of the atoms, we can distinguish that cavities in one of the Bell states. This process leads to two distant cavity fields entanglement.

Keywords: Entanglement swapping, external degrees of freedom, cavities entanglement, Bragg diffraction, Atomic momentum state, matter-wave interaction.

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1. Introduction

Entanglement, a non-local trait of quantum theory, has many applications in quantum informatics [1]. The cavity quantum electrodynamics (QED) techniques are used to generate atom-field, atom-atom and field-field entanglement [2]. Entanglement in the atomic external degrees of freedom using Bragg diffraction is also proposed [3, 4]. Bragg diffraction of atomic de-Broglie waves from optical cavity also covers some aspects of quantum information [5, 6].

Entanglement swapping, an important technique of entanglement, entangles two parties that have never interacted before. Entanglement swapping between two photons that have never coexisted is demonstrated [7]. Bell measurements are much useful in quantum communication protocols such as teleportation [8] and entanglement swapping [9]. Entanglement swapping is used in quantum repeaters [8], in order to overcome the limiting effect of photon loss in long range quantum communication.

In this paper, we use a simple technique i.e. atomic interferometry for swapping entanglement between atoms and cavities. This way we are able to entangle distant cavities without direct interaction. For the proposed scheme, we have two cavities which are in superposition state of zero and one photon. The cavity superposition state is experimentally demonstrated by Rauschenbeutal et al. [10]. First, we interact two atoms, initially in their ground state having momentum $|P_0\rangle$, $i\epsilon\{1, 2\}$ each with a cavity in Bragg diffraction regime. Bragg scattering allows only one of the two directions of propagation for each atom along the cavity field which are the incident and exactly opposite one. The detuning is large as compared to single photon Rabi frequency and hence atom practically stays in the ground state and the state of the field does not change. We take any order of Bragg scattering in order to allow varying separation between the atoms after the interaction. The non-resonant interaction entangles the atoms in their external degrees of freedom i.e. in their momentum states with the cavities. Then these entangled atoms are passed through beam splitter. For this purpose we use two beam splitters, one for non deflected atomic momentum state and second for deflected atomic momentum state. The beam splitter brings the atomic momentum state of these indistinguishable atoms in superposition state. A cavity in the superposition state of zero and one photon can be used as a beam splitter [11]. At last, after passing through the beam splitter, these identical atoms are detected. Here, we use four detectors for four possible momentum splits. The detection process gives us the information that the two cavities are in which Bell state. Thus entanglement between atoms is swapped to that between two far away cavities.

Our paper proceeds as follow: In Sec. 2 we explain the Bragg diffraction of atom from cavity field and the formation of atom-field entanglement. In Sec. 3 we analyze the action of beam splitter which transfers the atomic momentum component into superposition state. We then briefly explain the detection process and the final result. Finally we conclude in Sec. 4 and give experimental parameters to perform our proposed scheme in the laboratory.
2. Bragg atom-field interaction

For the proposed scheme, we first entangle two atoms with their respective cavity fields by atom-field interaction in Bragg Regime. For the purpose, we consider two atoms, \( A_1 \) and \( A_2 \), both initially in their ground state, \( g_1 \) and \( g_2 \), having transverse momentum state, \( |P_{l_0}\rangle \), where, \( i = 1, 2 \) stands for atoms, \( A_1 \) and \( A_2 \) and \( P_{l_0} = \frac{l_0}{2} \hbar k \) with \( l_0 \) a positive even integer. We have two cavities, \( C_1 \) and \( C_2 \), which are in superposition state of zero and one photon i.e. \( (|0\rangle + |1\rangle)/\sqrt{2} \) as shown in Fig. 1. This superposition can be generated by first passing a two level atom in its excited state for half a Rabi cycle through the field. We dispersively interact atom, \( A_1 \), with cavity, \( C_1 \), and atom, \( A_2 \), with cavity, \( C_2 \). The off-resonant interaction is followed to avoid decoherence that stems from spontaneous emission. Large detuning and large interaction time ensure conservation of energy which leads to only two possible directions of scattering for atoms, first the incident one, \( P_{l_0} \), and second exactly opposite to the incident transverse momentum direction, \( P_{-l_0} \). The off-resonant Bragg diffraction invokes only the virtual transition among different atomic levels [11].

The initial state vector for the system before interaction is

\[
|\Psi(0)\rangle = \frac{1}{\sqrt{2}} \sum_{i=1,2} (|0_i\rangle + |1_i\rangle) \otimes |g_i, P_{l_0}(i)\rangle.
\]

(1)

Total Hamiltonian governing this atom-field interaction under the dipole and rotating wave approximation with atom of mass, \( M \), and centre of mass momentum, \( P \), is [3]

\[
\hat{H} = \frac{\hat{P}^2}{2M} - \frac{1}{2} \hbar \omega_0 \hat{\sigma}_z + \hbar \nu \hat{a}^\dagger \hat{a} + \hbar g \cos(k \hat{x}) [\hat{\sigma}_+ \hat{a} + \hat{\sigma}_- \hat{a}^\dagger].
\]

(2)

Here, \( \hat{\sigma}_\pm \) and \( \hat{\sigma}_z \), are the Pauli operators, \( \hat{x} \) is position operator of atom, \( \hat{a} \) (\( \hat{a}^\dagger \)) is field annihilation (creation) operator, \( g \) is the vacuum Rabi frequency and \( \Delta \) is the detuning between the atomic transition frequency, \( \omega_0 \), and the field frequency is \( \nu \). We follow the large detuning case where we have no direct atomic transition and it is rare to find the atom in their excited state. Hence, the system may be governed by following effective Hamiltonian, under the adiabatic approximation as

\[
\hat{H}_{\text{eff}} = \frac{\hat{P}^2}{2M} - \frac{\hbar |g|^2}{2\Delta} \hat{\sigma}_- \hat{\sigma}_+ (\cos 2k\hat{x} + 1).
\]

(3)

The state of each \( i \)th atom-field pair at any time \( t \) is given as

\[
|\Psi(t)\rangle = \frac{1}{\sqrt{2}} \sum_{i=-m}^{m} \left( C_{0,\tilde{P}_i} |0, g_i, \tilde{P}_i^{(i)}\rangle + C_{1,\tilde{P}_i} |1, g_i, \tilde{P}_i^{(i)}\rangle \right),
\]

(4)

where, \( m \) is the total number of the orders of deflections and \( \tilde{P}_i = P_{l_0} + l\hbar k \), \( l \) being an even integer. Time evolution of the state vector is given by Schrodinger equation

\[
i\hbar \frac{\partial |\Psi(t)\rangle}{\partial t} = H_{\text{eff}} |\Psi(t)\rangle
\]

(5)
We show dispersive interaction of atoms with cavity fields. The atoms with initial momentum, \( |P_{i0}\rangle \), interact with the cavities which are in superposition of zero and one photon state. The interaction time is set such that when the cavities are in zero photon state, the atoms do not get deflected and have same momentum \( |P_{i0}\rangle \) as initial one. For one photon state of the cavities, the atoms are deflected and have momentum \( |P_{i-l_0}\rangle \).

We have

\[
\cos 2k\hat{x} |\hat{P}\rangle \sim |\hat{P}_{l+2}\rangle + |\hat{P}_{l-2}\rangle
\]

and we drop the unchanged atomic ground state vector \( |g_i\rangle \). Under condition of Bragg scattering with only two possible directions of deflection \( l = 0 \) with \( \hat{P}_0 = P_{i0} \) and \( l = -l_0 \) with \( \hat{P}_{-l_0} = P_{-l_0} \). Thus we obtain the state of each \( i \)th atom-field pair after interaction as

\[
|\Psi(t)\rangle = \frac{1}{\sqrt{2}} \left( |0_i, P_{(i)}^{(l_0)}\rangle + C_{1,0_l}(t)|1_i, P_{(i)}^{(l_0)}\rangle + C_{1,-l_0}(t)|1_i, P_{(i)}^{(-l_0)}\rangle \right)
\]

where, \( C_{n,\pm l_0} \) is the probability amplitude of the atom exiting with momentum \( P_{\pm l_0} \) or \( P_{-l_0} \) when there are \( n \) photons in the field and is given as

\[
C_{n,\pm l_0}(t) = e^{-iA_{n_{l_0}}t} \left[ C_{n,\pm l_0}(0) \cos \left( \frac{1}{2}B_{n_{l_0}}t \right) + iC_{n,\mp l_0}(0) \sin \left( \frac{1}{2}B_{n_{l_0}}t \right) \right]
\]

where,

\[
A_n = \begin{cases} 
- \frac{(|g|^2n/4\Delta)^2}{\omega_{rec}(l_0-2)(2)} & \text{for } l_0 \neq 2 \\
0 & \text{for } l_0 = 2
\end{cases}
\]

and

\[
|B_n| = \begin{cases} 
\frac{(|g|^2n/2\Delta)^{\nu/2}}{(2\omega_{rec})^{\nu/2-1}|(l_0-2)(l_0-4)\ldots4.2|} & \text{for } l_0 \neq 2 \\
\frac{|g|^2n/2\Delta}{|g|^2n/2\Delta} & \text{for } l_0 = 2
\end{cases}
\]

Initially both atoms are sent with momentum \( P_{i0} \), so probability of finding the exiting atom in either directions flips as a cosine function of interaction time.
We adjust the interaction time of atoms with fields to ensure that if there is one photon in the fields, the atoms definitely get deflected. The adjusted time is thus \( t = r \pi / |B_n| \), where \( r \) is an odd integer. For first order Bragg scattering, this time simplifies to \( t = \frac{2r \pi \Delta}{|B_1|} \). The wave function of the two atom-field pairs is

\[
\Psi(t) = \frac{1}{\sqrt{2}} \left( \langle 0_1, P_{l_0}^{(1)} | + i e^{-i \phi} | 1_1, P_{l_0}^{(1)} | \right) \otimes \left[ \frac{1}{\sqrt{2}} \left( \langle 0_2, P_{l_0}^{(2)} | + i e^{-i \phi} | 1_2, P_{l_0}^{(2)} | \right) \right],
\]

where, \( \phi = r \pi A_1 / B_1 \). The atoms in their external degrees of freedom becomes entangled with their respective cavity fields. The combined state of the system can be written as

\[
\Psi(t) = \frac{1}{2} \left( \langle 0_1, 0_2, P_{l_0}^{(1)}, P_{l_0}^{(2)} | + i e^{-i \phi} | 0_1, 1_2, P_{l_0}^{(1)}, P_{l_0}^{(2)} | + i e^{-i \phi} | 1_1, 0_2, P_{l_0}^{(1)}, P_{l_0}^{(2)} | - e^{-i \phi} | 1_1, 1_2, P_{l_0}^{(1)}, P_{l_0}^{(2)} | \right).
\]

After adding and subtracting some terms and rearranging, we have

\[
\Psi(t) = \frac{1}{4} \left( | P_{l_0}^{(1)}, P_{l_0}^{(2)} | + e^{-i \phi} | P_{l_0}^{(1)}, P_{l_0}^{(2)} | \right) (|00\rangle - |11\rangle) \\
+ \frac{1}{4} \left( | P_{l_0}^{(1)}, P_{l_0}^{(2)} | - e^{-i \phi} | P_{l_0}^{(1)}, P_{l_0}^{(2)} | \right) (|00\rangle + |11\rangle) \\
+ \frac{1}{4} | i e^{-i \phi} \left( | P_{l_0}^{(1)}, P_{l_0}^{(2)} | + | P_{l_0}^{(1)}, P_{l_0}^{(2)} | \right) (|10\rangle + |01\rangle) \\
+ \frac{1}{4} | i e^{-i \phi} \left( | P_{l_0}^{(1)}, P_{l_0}^{(2)} | - | P_{l_0}^{(1)}, P_{l_0}^{(2)} | \right) (|10\rangle - |01\rangle).
\]

Here, we entangle the cavities and atoms in four EPR states, separately, and all the four states are also entangled with each other. Measurement of atoms in one of the EPR states, projects the two cavities into a corresponding Bell state. We discuss this process in next section.

### 3. EPR State Measurement on Atomic Momenta EPR States

The scheme proposed in this paper is to develop entanglement between two far away cavities. EPR state measurement on atomic momentum states collapses the field states into one of the four EPR states. For EPR measurement on atomic momenta we pass these entangled atoms through beam splitters. We have two beam splitters, BS\(_1\) and BS\(_2\). The beam splitters are cavities prepared in superposition of zero and one photon. The atomic momentum components, \(|P_{l_0}^{(1)}\rangle\) and \(|P_{l_0}^{(2)}\rangle\), pass through beam splitter BS\(_2\), and momentum components, \(|P_{l_0}^{(1)}\rangle\) and \(|P_{l_0}^{(2)}\rangle\), pass through beam splitter BS\(_1\) as shown in Fig. 2. Mirror can be used to deflect atoms to desired cavities. Here, the two atoms are indistinguishable. The dispersive interaction of atoms with cavity beam splitter for an interaction time, \( t = \frac{2 \pi \Delta}{g'} \), transfers the atomic momentum states into superposition state. Here, \( \Delta' \) is atom-beam splitter field detuning and \( g' \) is
Figure 2: For EPR state measurement on atomic momenta, the atoms are passed through the beam splitter $BS_1$ and $BS_2$ and are finally detected by the detector $D_1$, $D_2$, $D_3$ and $D_4$. The undeflected components pass through beam splitter $BS_1$ and deflected components interact with $BS_2$. The beam splitters are cavities prepared in superposition of zero and one photon. The two cavities $C_1$ and $C_2$ get entangled after detection of the atomic momenta states.

vacuum Rabi frequency. The atoms or beam splitting cavities can be oriented such that atoms undergo first order Bragg scattering. The beam splitter action is performed as follows

\begin{align}
|P_{l_0}^{(1)}\rangle &\rightarrow |P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, \\
|P_{l_0}^{(2)}\rangle &\rightarrow i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle, \\
|P_{-l_0}^{(1)}\rangle &\rightarrow |P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, \\
|P_{-l_0}^{(2)}\rangle &\rightarrow i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle. \\
\end{align}

When the beam splitter action is performed, the first factor of the first term of Eq. (11) becomes

\begin{align}
|P_{l_0}^{(1)}\rangle + e^{-i2\phi}|P_{-l_0}^{(1)}\rangle &\rightarrow \left(|P_{l_0}^{(1)}\rangle + i|P_{l_0}^{(2)}\rangle, i|P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle\right) \\
&\quad + e^{-i2\phi}\left(|P_{-l_0}^{(1)}\rangle + i|P_{-l_0}^{(2)}\rangle, i|P_{-l_0}^{(1)}\rangle + |P_{-l_0}^{(2)}\rangle\right) \\
&= i(|P_{l_0}^{(1)}\rangle, P_{l_0}^{(1)}\rangle + |P_{l_0}^{(2)}\rangle, P_{l_0}^{(2)}\rangle) \\
&\quad + e^{-i2\phi}|P_{-l_0}^{(1)}\rangle, P_{-l_0}^{(1)}\rangle + e^{-i2\phi}|P_{-l_0}^{(2)}\rangle, P_{-l_0}^{(2)}\rangle. \\
\end{align}
Similarly, the first factor of the second term in Eq. (11) after the action of Beam splitter is

\[ |P_0^{(1)}, P_0^{(2)} \rangle - e^{-i2\phi} |P_{-l_0}^{(1)}, P_{-l_0}^{(2)} \rangle \rightarrow \left( |P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle, i|P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle \right) \]

\[ - e^{-i2\phi} \left( |P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle, i|P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle \right) \]

\[ \rightarrow i(|P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle) + |P_{0}^{(2)} \rangle \]

\[ - e^{-i2\phi} |P_{-l_0}^{(1)} \rangle - e^{-i2\phi} |P_{-l_0}^{(2)} \rangle, \]

(14)

and that of the third term of Eq. (11) is

\[ |P_0^{(1)}, P_{-l_0}^{(2)} \rangle - |P_{-l_0}^{(1)}, P_{0}^{(2)} \rangle \rightarrow \left( |P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle, i|P_0^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle \right) \]

\[ - \left( |P_{-l_0}^{(1)} \rangle + |P_{0}^{(2)} \rangle, i|P_{-l_0}^{(1)} \rangle + |P_{0}^{(2)} \rangle \right) \]

\[ = 2 \left( |P_0^{(1)}, P_{-l_0}^{(2)} \rangle - |P_{-l_0}^{(1)}, P_{0}^{(2)} \rangle \right), \]

(15)

and the same for the fourth term of Eq. (11) transform as

\[ |P_{l_0}^{(1)}, P_{-l_0}^{(2)} \rangle + |P_{-l_0}^{(1)}, P_{l_0}^{(2)} \rangle \rightarrow \left( |P_{l_0}^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle, i|P_{l_0}^{(1)} \rangle + |P_{-l_0}^{(2)} \rangle \right) \]

\[ + \left( |P_{-l_0}^{(1)} \rangle + |P_{l_0}^{(2)} \rangle, i|P_{-l_0}^{(1)} \rangle + |P_{l_0}^{(2)} \rangle \right) \]

\[ = 2i \left( |P_{l_0}^{(1)}, P_{-l_0}^{(2)} \rangle - |P_{-l_0}^{(1)}, P_{l_0}^{(2)} \rangle \right). \]

(16)

The interaction time of atoms with cavity fields, acting as beam splitter, can be controlled by using velocity selector.

For the detection of direction of atomic momentum component we use four detectors, D1, D2, D3 and D4 [14]. The detectors are placed in the spatial paths of the atoms in different directions of propagation of atoms, which correspond to different momenta. Click in the detector corresponds to presence of atom in that direction and hence with that particular momentum. Recently, detectors have been built which can efficiently detect fast moving Rydberg atoms [15]. A click in detector D1 corresponds to momentum direction \( |p_{l_0}^{(2)} \rangle \), a click in detector D2 corresponds to momentum direction \( |p_{-l_0}^{(1)} \rangle \), a click in detector D3 corresponds to momentum direction \( |p_{0}^{(1)} \rangle \), and a click in detector D4 corresponds to momentum direction \( |p_{l_0}^{(1)} \rangle \) as shown in Fig. 2. Combining Eqs. (13)-(16) with Eq. (11), the state of the cavities for different detector clicks are as given in Table 1. Here, from various combination of clicks on detectors, we can distinguish between \( |\psi^+ \rangle \), \( |\psi^- \rangle \), and \( |\phi^+ \rangle \) or \( |\phi^- \rangle \). Hence after the detection of atoms we can tell that cavities are in which Bell state. It must be noted as with linear optics Bell state measurement, this process will only be able to distinguish between states \( |\psi^+ \rangle, |\psi^- \rangle \) and \( \{|\phi^+ \rangle, |\phi^- \rangle \} \). States \( |\phi^+ \rangle \) and \( |\phi^- \rangle \) cannot be distinguished.
| Cavities’ State       | Detectors’ click                                      |
|----------------------|------------------------------------------------------|
| $|\phi^+\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$ | 2 Atoms in either $D_1$, $D_2$, $D_3$, or $D_4$.     |
| $|\phi^-\rangle = \frac{1}{\sqrt{2}} (|00\rangle - |11\rangle)$ | 2 Atoms in either $D_1$, $D_2$, $D_3$, or $D_4$.     |
| $|\psi^+\rangle = \frac{1}{\sqrt{2}} (|10\rangle + |01\rangle)$ | Coincidence between $D_1$ and $D_4$ or $D_2$ and $D_3$. |
| $|\psi^-\rangle = \frac{1}{\sqrt{2}} (|10\rangle - |01\rangle)$ | Coincidence between $D_2$ and $D_4$ or $D_1$ and $D_3$. |

Table 1: The entangled state of the two cavities corresponding to different clicks in the four detectors.

Deterministic optical Bell measurement schemes rely either on non-linear interactions which are highly inefficient in practice [15], or using ancilla entangled photons [17] which require large interferometers to combine the signal and ancilla modes and give near deterministic Bell measurement with asymptotically large ancilla states. Recently single-mode squeezers together with beam splitters have been proposed to give up to 64.3% success probability [18]. The EPR state analogs of these near deterministic Bell measurements require further study.

4. conclusion

We have proposed a scheme for entangling long distance cavities by entanglement swapping. For this purpose the external degrees of freedom of atomic momenta are first entangled with cavity fields. We then propose a method to perform Bell measurement on atomic momenta states which in turn swaps entanglement to cavity fields. The Bell measurement process involves additional cavity fields which act as a beam splitters for atomic momenta.

The Scheme that we have proposed for cavities entanglement in Bell states, possesses stronger non locality. The microwave regime cavity QED have life time up to seconds and high fidelity can be achieved as proposed by Khosa et.al. [19]. They consider the passage of 15-20 helium atoms under the first order Bragg diffraction through a quantized cavity field. We perform quantum measurement on atomic momentum state of neutral atoms which are easy to handle and manipulate than a photonic flying qubit. The external atomic momentum states are more useful states against decoherence [20]. Our scheme is experimentally feasible as Bragg Scattering of atoms in optical regime has already been demonstrated by G. Rempe and his co-worker at $\lambda = 780$ nm for $^{85}$Rb atoms [21].

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