Parallel charge sheets of electron liquid and gas in La$_{0.5}$Sr$_{0.5}$TiO$_3$/SrTiO$_3$ heterostructures

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We show here a new phenomenon in La$_{0.5}$Sr$_{0.5}$TiO$_3$/SrTiO$_3$ (LSTO/STO) heterostructures; that is a coexistence of three-dimensional electron liquid (3DEL) and 2D electron gas (2DEG), separated by an intervening insulating LSTO layer. The two types of carriers were revealed through multi-channel analysis of the evolution of nonlinear Hall effect as a function of film thickness, temperature and back gate voltage. We demonstrate that the 3D electron originates from La doping in LSTO film and the 2D electron at the surface of STO is due to the polar field in the intervening insulating layer. As the film thickness is reduced below a critical thickness of 6 unit cells (uc), an abrupt metal-to-insulator transition (MIT) occurs without an intermediate semiconducting state. The properties of the LSTO layer grown on different substrates suggest that the insulating phase of the intervening layer is a result of interface strain induced by the lattice mismatch between the film and substrate. Further, by fitting the magnetoresistance (MR) curves, the 6 unit cell thick LSTO is shown to exhibit spin-orbital coupling. These observations point to new functionalities, in addition to magnetism and superconductivity in STO-based systems, which could be exploited in a multifunctional context.

The surface or interfacial conductivity in transition metal oxides is a potential candidate for and has been exploited in multifunctional oxide-based electronics$^{1-5}$. Strontium titanate (SrTiO$_3$ or STO) occupies a central position in STO-based systems, which could be exploited in a multifunctional context.

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B is the applied magnetic field and \( m^* \) is the effective mass, and electron mobility of valence states\(^{27} \) (50% of Ti\(^{3+} \) due to the Ti valences. When doping 50% of La into STO, dopants in a stoichiometric LSTO render Ti into two a function of thickness measured at room temperature. The extrapolated dash line is guide to the eyes and that of magnitude change between 5 and 6 uc samples. (c) Zoom-in of sheet conductance and sheet carrier density as a function of thickness measured at room temperature. The extrapolated dash line is guide to the eyes and that suggests an insulating layer of 5 uc.

Figure 1. Abrupt MIT. (a) Quadratic function between sheet resistance and temperature indicates an electron liquid behaviour. (b) Sheet conductance versus thickness measured at 2 and 300 K showing a more than 6 orders of magnitude change between 5 and 6 uc samples. (c) Zoom-in of sheet conductance and sheet carrier density as a function of thickness measured at room temperature. The extrapolated dash line is guide to the eyes and that suggests an insulating layer of 5 uc.

varying the ratio of La to Sr, \( \text{Sr}_{1-x}\text{La}_x\text{TiO}_3 \) changes from a Mott insulator \((x = 1, \text{LaTiO}_3)\) to a single-band conductor, and further to a band insulator \((x = 0, \text{STO})\). Structurally, La dopant transforms \( \text{Sr}_{1-x}\text{La}_x\text{TiO}_3 \) from \( \text{Pm3m} (x = 0) \) to \( \text{Ibm3m} (0.2 \leq x < 0.7) \) and to \( \text{Pbnm} (0.7 < x \leq 1)^{28} \). The case for 50% La doped STO is particularly interesting, due to the Ti valences. When doping 50% of La into STO, dopants in a stoichiometric LSTO render Ti into two valence states\(^{27} \) (50% of Ti\(^{3+} \) and 50% of Ti\(^{4+} \)). This turns LSTO into a polar compound with an alternating polarity of \(+0.5e \) and \(-0.5e \) \((\text{La}^{3+}\text{Sr}^{2+}0.5\text{O}^{2-} \) and \( \text{Ti}^{3+}\text{Ti}^{4+}0.5\text{O}^{2-} \))\(^{29} \). Following the prediction of the polar catastrophe model\(^{21} \), the alternating polarity should lead to a charge transfer from LSTO to STO surface (assuming there is no screening by the free electrons), and the electrons at STO surface would exhibit properties similar to those at the LAO/STO interface. However, LSTO has to be an insulator to satisfy the requirements of the polar catastrophe. By applying biaxial strain, we were able to transform the electrical properties of thin LSTO to an insulating state, and to generate two conducting channels in the system; one is in the LSTO film and the other at the interface between LSTO and STO. Various LSTO films were prepared on different substrates and behaviour of the two channels of carriers for different LSTO thicknesses at different temperatures, and under the influence of applied magnetic and electric fields were studied.

Results

Temperature dependence of transport property. The sheet resistance \( R_S \) of all LSTO films were measured in a Van der Pauw geometry. In these measurements, Aluminum contacts are created by ultrasonically bonding aluminum wires that penetrate through the LSTO film down to the interface between LSTO and STO, allowing the electrical probing of both the film and interface using the same wire. Figure 1a summarizes their temperature dependence, which shows a \( T^2 \) dependence. This is typical of EL system where electron-electron scattering dominates. Figure 1b shows the sheet conductance as a function of film thickness at 2 and 300 K, suggesting a sharp MIT with a critical thickness of 6 uc. When the thickness is less than 6 uc, LSTO films turn into an insulating phase with a conductance below our measurement limit. While the sheet conductance progressively increases as film thickness increases at 300 K, it jumps by more than six orders of magnitude when the thickness reaches 6 uc at 2 K. The sheet conductance is almost constant at low temperature (2 K) and this might be a result of the dominating scattering induced by structural defects in LSTO due to the STO structural phase transition at 105 K. Figure 1c shows the sheet conductance and carrier density of LSTO films for different thicknesses at 300 K obtained by Hall measurements (discussed in the next section). Within the first 20 uc, all data points fall onto a line intersecting zero conductance at 5 uc. In other words, the data extrapolates to an insulating layer of 5 uc, which is consistent with the critical thickness of 5 uc (Fig. 1b). The abrupt MIT in LSTO/STO is particularly interesting due to the more than 6 orders of magnitude change in conductance within one uc in contrast to the more gradual MITs observed in other conducting oxides, such as \( \text{LaNiO}_3 \) and \( \text{SrVO}_3 \).

Nonlinear Hall resistance. Further investigations were conducted by performing Hall measurement. While the 6 uc LSTO/STO sample shows a linear Hall resistance \( (R_{xy}) \), samples with a thickness greater than 6 uc show a nonlinear \( R_{xy} \) at low temperatures \((<100 \text{ K})\). There are four possible origins for nonlinear \( R_{xy} \): (i) quantum effect due to strong magnetic field above the weak field limit, (ii) anomalous Hall effect due to ferromagnetism, (iii) multi-band nature of materials which leads to different types of carriers in the material, and (iv) spatially separated multi-channel of carriers with different mobilities. The weak field limit, above which quantum effect can be observed, can be expressed as:

\[
\omega_c \tau > 1
\]

where \( \omega_c \) is cyclotron frequency and \( \tau \) is the mean time between scattering events. Considering \( \omega_c = eB/m^* \), where B is the applied magnetic field and \( m^* \) is the effective mass, and electron mobility \( \mu = e\tau/m^* \), the weak field limit can be rewritten as:
Figure 2. Comparison of Hall resistance measured in two different types of contacts. Hall resistance $R_{xy}$ of a 30 uc LSTO/STO is measured at 2 K using two different contact methods. Silver contacts, which electrically contact only the LSTO, show linear $R_{xy}$. Wire bonds, which contact both LSTO and the interface of LSTO/STO, show nonlinear $R_{xy}$.

This sets a limit for the applied magnetic field above which the Hall resistance can become nonlinear. Considering the linear low field (below 2.5 T) of $R_{xy}$ gives Hall mobility values for our samples ranging from 200 cm$^2$V$^{-1}$s$^{-1}$ (300 K) to 900 cm$^2$V$^{-1}$s$^{-1}$ (2 K), corresponding to a lowest possible weak field limit of $1/\mu = 1/\mu B > 1$ or $B > 1/\mu$  

$$R_{xy} = \frac{e}{\text{c}} \left[ (\mu_1 n_1 + \mu_2 n_2) + (\mu_1 \mu_2 B^2 n_1 + n_2) \right]$$

where $n_1, \mu_1, n_2, \mu_2$ are the density and mobility of the two types of carriers, respectively.

As shown in Fig. 3, the density of one of the carriers ($n_2$, indicated by black dots) is an order of magnitude higher than that of the other ($n_1$), while its mobility ($\mu_1$) is significantly lower than its counterpart ($\mu_2$). The $n_1$ starts to appear in the fitting results when LSTO is 6 uc, and it increases proportionally with film thickness while $\mu_1$ decreases. This indicates that $n_1$ originates from La doping in the LSTO film. (Because the La dopants are in the LSTO film, we use "3D" to denote $n_1$ carrier in analogy to the bulk doping effect.) On the other hand, low density $n_2$ starts to appear at 8 uc, and $n_2$ also show little dependence on film thickness, which is a manifestation of its 2D nature. The "3D" carrier density for 30 uc sample at room temperature is about $8 \times 10^{14}$ cm$^{-2}$. Considering effective thickness of 25 uc and 0.39 nm as $c$ axis lattice parameter, this measured carrier density is...
only 10.3% of expect carrier density from 50% Sr doping. The unexpected low carrier density is possibly due to different reasons which require further investigation, namely (i) surface depletion which can be as thick as 16.5 nm and 5.3 nm at 2 K and 200 K respectively in 5% La doped SrTiO3 films grown on SrTiO3 substrate33; (ii) increase on the thickness of interval insulating layer as increasing total film thickness; (iii) depletion originated from SrTiO3 substrates and one example on LaTiO3/SrTiO3 heterostructure is discussed in ref. 34; and (iv) structurally ordered phases of La2Sr3−x2TiO3n+135.

In order to investigate the scattering processes, temperature dependence of $R_{xy}$ was studied with film thickness fixed at 60 uc (Fig. 3d). Nonlinear $R_{xy}$ was only observed when temperature drops below ~100 K. The temperature dependence of the $n_1$ and $\mu_1$ suggests that the 3D carriers exhibit an EL nature. In an EL system, electron-electron interaction dominates, thus the electron mobility inherently increases with decreasing density, as is the case for $n_1$ and $\mu_1$ plotted in Fig. 3e,f. The 2D carriers vanishes when increasing temperature above ~100 K. Furthermore, while $n_2$ varies by more than an order of magnitude over the range of 100 to 10 K, $\mu_2$ shows little change, which points towards electron gas behaviour. The temperature dependence of both carriers in our system is similar to that observed in other systems8,19,36,37. The increase in carrier concentration of 2DEG at low temperature has also been observed in Nb-doped STO38, and is yet to be understood. The decrease in carrier mobility of the 3DEL at high temperatures is due to phonon scattering38,39.

The temperature dependence of Hall resistance shows that the low carrier density carrier starts to emerge at ~40 K (see Fig. 3e,f). Thus, electric field effect experiments were also performed at 40 K in order to see whether the carriers can be turned on and off by the field. Even though it is still lower than that at 2 K, STO at 40 K still has a relatively large dielectric constant of ~400039–41, which is sufficient in inducing significant changes in nonlinear

Figure 3. Nonlinear Hall effect in LSTO films. (a–c) Evolution of Hall resistance $R_{xy}$, carrier density and mobility as functions of LSTO thicknesses. All data are collected at 2 K with no back gate voltage ($V_g$) applied. The $R_{xy}$ is linear for 6 uc, but becomes increasingly nonlinear as the film thickness grows. (d–f) Temperature dependence of nonlinear Hall effect, carrier density and mobility for 60 uc LSTO. Nonlinear Hall effect was only observed under 100 K. (g–i) $V_g$ dependence of nonlinear Hall effect, carrier density and mobility for 60 uc LSTO measured at 40 K.
Hall resistance. The leakage current from drain to gate was well below 100 nA range and the source-drain current was fixed below 1 μA. The back gate experiment also answers an important question: is the 2DEG located at the top surface of the LSTO film or at the interface of LSTO/STO heterostructures? With the 0.5 mm STO substrate as the dielectric material, the 2DEG shall be tunable by the electrical field only if it were to be located at the interface between the conducting LSTO film and STO substrate. Additionally, the carrier density \( n_2 \) should increase when the back gate voltage increases. If the 2D carriers are at the top surface of LSTO film, the back gate voltage will not be able to tune \( n_2 \) due to the screening effect by the thick metallic LSTO film. Thus we conclude that the 2DEG is at the surface of STO substrate. As the back gate voltage (\( V_g \)) increases from -50 to 50 V, \( n_2 \) and \( \mu_2 \) increase, while \( n_1 \) and \( \mu_1 \) remain constant. These field effect dependencies of the two types of carriers and the fact that LSTO films have a 6 uc critical thickness (i.e. the 5 uc or lower LSTO films are insulating) point to the conclusion that the two types of carriers are spatially separated by an insulating intervening layer in the LSTO/STO heterostructure. There are two charge sheets in LSTO/STO heterostructures, namely a high density but low mobility 3DEL in the LSTO film and a high mobility but low density 2DEG at the interface between LSTO film and STO substrate.

**Effect of Strain.** In order to understand the origin of the insulating intervening LSTO layer, 15 uc LSTO films were grown on five different substrates, namely LAO (rhombohedral, 3.791 Å), NdGaO\(_3\) (NGO, orthorhombic, 3.859 Å), (LaAlO\(_3\))\(_0.3\)(Sr\(_2\)AlTaO\(_6\))\(_{0.7}\) (LSAT, cubic, 3.868 Å), STO (cubic, 3.905 Å) and DyScO\(_3\) (DSO, orthorhombic, 3.944 Å). All films are of good quality and have surface peak-to-peak roughness of 1 uc. Figure 4 summarizes the temperature dependence of the sample resistance. Among those substrates, the least compressive strain (0.13%) is provided by STO, and this results in a metallic LSTO with the lowest resistance. As the amplitude of compressive strain increases (from STO, LSAT, NGO to LAO), the metallic state is gradually suppressed. While the compressive strain introduced by LSAT (1.07%) only leads to weak localization behaviour at low temperatures, slightly larger compressive strain from NGO (1.30%) causes a complete semiconducting behaviour. The highest 3.04% compressive strain in the LSTO/LAO system turns the film into a complete insulator. On the other hand, the tensile strain introduced by DSO, despite its relatively small value (0.87%), turns the LSTO film to an insulator. From the extreme sensitivity of the electron transport behaviour of ultrathin LSTO films against strain, we conclude that the strain is one of the possible origins for the 5 uc insulating layer in the LSTO/STO heterostructure. There are two charge sheets in LSTO/STO heterostructures, namely a high density but low mobility 3DEL in the LSTO film and a high mobility but low density 2DEG at the interface between LSTO film and STO substrate.

**Weak anti-localization.** The magnetic field dependence of the carriers was investigated by MR measurements on both 6 uc (Fig. 5a) and 60 uc (Fig. 5b) samples under different back gate voltages (\( V_g \)). In large magnetic fields, all measured LSTO samples show positive MR. However, as shown in Fig. 5a, the 6 uc LSTO/STO shows WAL under all \( V_g \) while the 60 uc LSTO/STO sample does not show any sign of WAL. Since 6 uc LSTO/STO heterostructure...
has only a thin layer of La-induced EL on the surface of LSTO, the WAL in 6 uc LSTO provides information on
dimension confinement effect on the electron liquid. For a 2D system in a perpendicular magnetic field, WAL can
be fitted by the Hikami-Larkin-Nagaoka (HLN) formula\(^4\):

\[
\Delta \sigma_{xx}(B) = \sigma_{xx}(B) - \sigma_{xx}(0) = \alpha \cdot \frac{e^2}{2\pi^2\hbar} \ln \left( \frac{1}{2} \frac{B_0}{B} + \frac{B_0}{B} \right) - \ln \left( \frac{B_0}{B} \right)
\]

(4)

where \(\Psi\) is the digamma function, \(B_0 = \frac{4h}{eL}\), \(L\) is the dephasing length, and \(\alpha\) is governed by the interaction symmetries. Using metal-oxide-semiconductor field-effect transistor (MOSFET) as a prototype, Hikami et al. discovered that the value of \(\alpha\) in Eq. 4 is 1 for orthogonal case, 0 for unitary case and \(-0.5\) for symplectic case\(^4\).

In the symplectic case, the system has strong spin-orbit interaction and no magnetic scattering. Recently, it was also reported that \(\alpha\) can be \(-1 = -(1/2 + 1/2)\) in a top gated topological insulator Bi\(_2\)Se\(_3\), reflecting a change in the effective number of coherent channels\(^4\). In our study, these coherent channels are associated with the surface and interface charge sheets. As shown in Fig. 5c, the MR behaviours of the 6 uc sample are modulated by the electric

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**Figure 5.** Magneto-transport studies of 6 uc LSTO/STO heterostructure. Magnetoresistance of (a) 6 uc LSTO/STO heterostructures and (b) 60 uc LSTO/STO heterostructures under different back gate voltages. Weak anti-localization is observed in 6 uc LSTO/STO heterostructures, indicating the existence of spin-orbital coupling. (c) Hikami–Larkin–Nagaoka (HLN) fitting on the spin-orbital coupling in 6 uc LSTO/STO heterostructures under different gate voltages.
field effect and are well fitted by the HLN formula, confirming the existence of spin-orbit coupling in the 6 uc LSTO/STO. As the $V_g$ varies from 25 to −45 V, the HLN fitting returns an $\alpha = -0.5$, indicating a single coherent channel. This is consistent with the conclusion we drew from our Hall effect results. When the $V_g$ is set at 50 V, $\alpha$ becomes 1, indicating the appearance of two independent coherent channels. This is due to the formation of an additional channel at the interface under sufficiently large gate voltage, similar to the switching of 2DEG in 60 uc LSTO/STO using back gate experiments presented above. As the film thickness increases, however, the bulk LSTO dominates and the WAL is masked as shown in Fig. 5b for the 60 uc case, where the WAL cusp at low magnetic field is absent. This is highly possible due to the change of dimensionality of the top charge sheet from 2D to 3D.47,48.

Discussion

Configuration of the charge sheets. Our results show that the 2DEG is at top surface of STO substrate and the 3DEL is in the LSTO film. The location of the 2DEG is primarily confirmed by electric field effect experiments on LSTO/STO heterostructures with LSTO thicknesses of 5, 60 and 300 uc (see Supplementary Information). The density of 3DEL in LSTO thin film is consistently proportional to the LSTO film thickness. Due to the strain induced by STO, a 5 uc insulating intervening LSTO layer is formed and it spatially separates the two charge sheets. The 5 uc LSTO is found to be insulating in all different thicknesses of the LSTO film on STO.

Mechanism of multi-channel charge sheets. The two types of carriers and their behaviour are commonly observed in STO-based heterostructures and superlattices, including LaVO$_3$/STO heterostructure,46 LSTO/STO heterostructure,47 LSTO/STO superlattice,48 LTO/STO heterostructure,49, LSTO/STO superlattice50 and including charge leakage system of LTO/STO superlattice51. The low-density and high-mobility carriers are always located at the STO side, primarily due to the strong dielectric screening by high dielectric constant of STO at low temperatures. In all of these systems, the temperature dependence of the carriers shows similar behaviour: high-density carriers associate with thermal activation, while low-density carriers start to be observed only from around 100 K and lower. More strikingly, the low-density high-mobility 2DEG carriers have opposite trends to those at LAO/STO interface. More investigations are still required to understand the electron behaviours in these classes of systems.

In our LSTO/STO heterostructures, polarization in LSTO is most likely the origin for the appearance of 2DEG on the STO side. It has been proposed that “charge leakage” effect can be the origin of conductivity in LTO/STO system.49, However, “charge leakage” contradicts the thickness dependence MIT observed in LSTO/STO heterostructures. Furthermore, all STO-based multi-carrier heterostructures (LaVO$_3$/STO heterostructure,46,50 LTO/STO heterostructure,51 LSTO/STO superlattice,52 and including charge leakage system of LTO/STO superlattice53) are consisting of a polar over layer. This indicates that polarization plays a crucial role in the formation of the 2DEG.

Spin-orbital coupling. The spin-orbit coupling has been used to create and control spin-related properties in many material systems, such as topological insulators,46,50,51 conventional semiconductor heterostructures,52,53, and LAO/STO oxide interfaces.54, According to ref. 55, sub-bands structure in a quantum well is able to induce spin-orbit interaction and electrons in the 6 uc LSTO/STO occupy different d orbitals (sub-bands) of the Ti atoms.46,57. We therefore hypothesize that the spin-orbital coupling at 6 uc LSTO/STO is due to the intrinsic spin-orbit coupling in the doped-STO.55,56. The proposed model agrees with vanishing of spin-orbit coupling in thick 60 uc LSTO and the tunability of spin-orbit coupling in 6 uc LSTO with electric field. Increasing the thickness increases the dimensionality of the quantum well from 2D to 3D and back gated fields influence the occupancy of the sub-bands. The tunable spin-orbit coupling in LSTO/STO heterostructures could be a potential platform for creating new spin-related functionalities.

In summary, we observed an abrupt MIT without an intermediate semiconducting state in LSTO grown on STO when the LSTO film thickness is decreased from 6 to 5 uc. From our nonlinear $R_g$ study with films thicker than 8 uc, two charge sheets are characterized as a 3DEL in the LSTO film and a 2DEG at the LSTO/STO interface. The transport properties of LSTO films on different substrates demonstrate that a 5 uc insulating layer, which spatially separates the two types of carrier, is created in the LSTO/STO heterostructure by the lattice mismatch between LSTO and STO. Further MR measurement of the 6 uc heterostructure shows WAL. Based on the HLN fitting on the MR, a gating dependent spin-orbit coupling is shown. As the film thickness increases, an extra channel of 2DEG becomes visible. This is consistent with the conclusion we drew from our Hall effect results. When the $V_g$ is set at 50 V, $\alpha$ becomes 1, indicating the appearance of two independent coherent channels. This is due to the formation of an additional channel at the interface under sufficiently large gate voltage, similar to the switching of 2DEG in 60 uc LSTO/STO using back gate experiments presented above. As the film thickness increases, however, the bulk LSTO dominates and the WAL is masked as shown in Fig. 5b for the 60 uc case, where the WAL cusp at low magnetic field is absent. This is highly possible due to the change of dimensionality of the top charge sheet from 2D to 3D.47,48.

Methods

Target preparation. A polycrystalline LSTO target used for the thin film depositions were prepared from high purity La$_2$O$_3$ (99.999%), TiO$_2$ (99.999%) and SrO (99.9%) powders. The powders were carefully weighed, mixed and ground for several hours before being sintered at 600 °C for 8 hours and sintered again at 900 °C for 10 hour. Next, the powders were ground into powder, pressed into pellets and calcinated at 1300 °C for 36 hours.

Substrate preparation. To achieve single-terminated surfaces for STO, the substrates (CrystalTec GmbH) were treated with buffered hydrofluoric acid and annealed at 950 °C for 1.5 hour in air. The terminations for various substrates and for films after growth were confirmed by atomic force microscopy.

Film growth. Epitaxial LSTO films were grown on STO single-crystal substrates in a pulse laser deposition (PLD) system using a Lambda Physik KrF excimer laser with wavelength 248 nanometer, pulse width of approximately 15 ns and system base pressure of $10^{-8}$ Torr. The laser energy density was maintained at 1.6 J/cm$^2$ with
a frequency of 1 Hz for all the depositions. The layer-by-layer growth was monitored by in situ reflection high energy electron diffraction (RHEED) (see Fig. 5a for an example) with ~15 pulses per unit cell growth rate in this study. The temperature was set at 850 °C and the oxygen partial pressure was fixed at 10⁻⁴ Torr during the whole process including warming, deposition and cooling processes. Although the 10⁻⁴ Torr is not on the higher side of oxygen partial pressure, there is no obvious oxygen vacancies created during the growth. If there were oxygen vacancies, there could have been induced conductivity in all samples. However, there is no conductivity observed in thin LSTO/STO sample with LSTO thickness smaller than 6 uc. Similarly, there should be no conductivity from the diffusion of Sr or other elements as well. In addition, 10⁻⁴ Torr of oxygen partial pressure was also reported having no influence on the electrical conductivity. After the growth, samples were cooled to room temperature in a ramping rate of 30 degree per minute. To demonstrate the atomic flat surface, an image measured by atomic force microscopy on 11 uc LSTO films on STO substrate is shown in Fig. S1b. The correct elemental composition and excellent crystalline quality were confirmed by Rutherford backscattering spectroscopy and channeling experiments (Fig. S3).

Transport measurement. The sheet resistance $R_s$ and the carrier concentration $n$ were obtained as a function of temperature from 300 to 2 K by applying a d.c. current of 1 μA. The measurement geometry was Van der Pauw geometry on square shaped samples (5 × 5 mm²). Ohmic contacts were formed by ultrasonically bonding Al wires. The method of ultrasonically bonding is a typical way of creating electrically contact to the interface 2DEG, due to its capability in penetrating through thick oxide layers, such as LaVO₃, Al₂O₃, and LAO. For the Hall measurements the magnetic field $B$ was varied between ± 9 T.

HLN fitting. WAL is characterized as a sharp suppression of resistance at low magnetic field. The expression of Eq. 4 is valid for 2D WAL in perpendicular magnetic fields. The equation contains two free parameters, namely the prefactor $\alpha$ and the dephasing length $L_\phi$. The experimental data of MR used for fitting is the original MR data without background subtraction. The two parameters are obtained by fitting the experimental curves in MatLab. In the fitting, $\alpha$ were varied with a 0.5 interval without any range limitation and $L_\phi$ are kept completely free. In the process of fitting, the best fit of HLN is the fit with the minimum root mean square (RMS) value. In the Fig. 5c, the best fit and raw data are plotted together with fitted values of $\alpha$ and $L_\phi$.

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