THE EFFECT OF THE INTERSTELLAR MODEL ON STAR FORMATION PROPERTIES IN GALACTIC DISKS

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ABSTRACT

We studied the effect of interstellar gas conditions on global galaxy simulations by considering three different models for the ISM. Our first model included only radiative cooling down to 300 K, our second model added an additional background heating term due to photoelectric heating, and our third model uses an isothermal equation of state with a temperature of $10^4$ K and no explicit heating or cooling. Two common prescriptions for star formation are implemented in each case. The first is based on cosmological simulations with a low threshold for star formation but also a low efficiency. The second assumes that stars form only in high-density regions but with a higher efficiency. We also explore the effects of including feedback from Type II supernovae. We find that the different ISM types produce marked differences in the structure of the disk and temperature phases present in the gas, although inclusion of feedback largely dominates these effects. In particular, the size of the star-forming clumps was increased both by background heating and by enforcing an isothermal ISM. We also looked at the one-dimensional profiles and found that a lognormal probability distribution function (PDF) provides a good fit for all our simulations over several orders of magnitude in density. Overall, despite noticeable structural differences, the star formation properties in the disk are largely insensitive to ISM type and agree reasonably well with observations.

Subject headings: galaxies: evolution — galaxies: ISM — galaxies: spiral — ISM: structure — methods: numerical

Online material: color figures

1. INTRODUCTION

Star formation is one of the most perplexing processes in galaxies due to its immense complexity on very small scales and its apparent simplicity on very large ones. It is difficult to know what is the extent to which the small-scale physics can be ignored when considering the global evolution of galaxies.

Observationally, we know that there is a simple relationship between the surface density of gas in a disk galaxy and the surface density of star formation (Kennicutt 1998, 1989; Schmidt 1959). This should imply that star formation is a straightforward, universal process depending on average properties of the gas over many kiloparsecs. The (perhaps naive) picture is one in which gravity collapses the gas into giant molecular clouds out of which stars form, a process that is hindered by rotational shear, thermal pressure, turbulence, magnetic fields, cosmic-ray pressure, and energy injected from supernovae explosions (Mac Low 2004). Yet, when we start looking at star formation on small (parsec) scales, we find the gas out of which stars form to be a turbulent, multiphase medium, strongly affected by local conditions and not at all indicative of a global law.

So complex is the interstellar medium (ISM) that simulations that model it, in order to achieve the required resolution, are limited to considering only small sections of the galaxy (e.g., Slyz et al. 2005; Joung & Mac Low 2006; de Avillez & Breitschwerdt 2004). Until recently, it has been necessary in simulations that model an entire galaxy to simplify the structure of the ISM as an isothermal or fixed two- or three-phase body for the calculation to be at all feasible (e.g., Harfst et al. 2006; Li et al. 2005b; Robertson et al. 2004; Semelin & Combes 2002). It is not that such assumptions about the structure of the ISM are groundless. Analytical calculations performed by McKee & Ostriker (1977) put together the now traditional picture of a three-phase ISM, largely filled by hot gas from supernovae explosions. Others have suggested modifications (e.g., Cox 2005; Norman & Ikeuchi 1989), but this basic scenario is still with us.

Yet, while both of these approaches have been highly informative about the evolution and structure of galaxies, they each have disadvantages. The small-box simulations are not adequate for modelling global properties such as star formation histories, disk structure, and the Schmidt law, with the result that their main comparison points are restricted to galaxies for which we are able to observe and measure the ISM. Global models, on the other hand, cannot be used to compute the evolution of the interstellar medium, and the effect of the required simplification on the disk galaxy’s own evolution is unknown.

Recently, however, simulations have been developed that are bridging this gap. While still short of the resolution attained in kiloparsec-sized simulation boxes, these models do achieve the refinement needed to model a complete galaxy disk that includes a multiphase ISM. This paper continues the work we began in Tasker & Bryan (2006a, hereafter TB06), which examined a three-dimensional (3D) isolated galactic disk using an adaptive-mesh refinement technique. In that paper we found that a multiphase medium, with a large variety of temperatures and densities, is in good agreement with simulations performed in two dimensions by Wada & Norman (2001) and smaller scaled 3D runs by Wada et al. (2002). These results supported the small-box simulations in implying that the traditional view of the ISM as a three-phase structure in strict pressure equilibrium has some validity, although it is a significant oversimplification.

What is less clear is how important this is. The existence of the Schmidt law might imply that it is not necessary to account for the details of the ISM to achieve accurate modeling in global galaxy simulations. And, indeed, the Schmidt law and the observed star formation threshold in disk galaxies (Kennicutt 1989) have been successfully reproduced both in models with a multiphase...
ISM (TB06) and in those with a fixed isothermal ISM (Li et al. 2005a). On the other hand, the observed global structure of the ISM is far from being an uninterrupted pool of gas. Observations of the ISM in the Large Magellanic Clouds show, in addition to its turbulent nature, a complex series of H I filaments riddled with holes and shells (Kim et al. 1998). Two of our neighboring spiral galaxies, M31 and M33, show numerous holes 40 pc to 1 kpc wide (Deul & den Hartog 1990), and our own Milky Way produces plumes of gas that rise off the disk’s surface (Otte et al. 2003). Not only is it impossible to model such effects without global multiphase ISMs, but it is hard to imagine this structure not playing an integral part in the disk’s evolution. Moreover, the role of stellar feedback remains something of a mystery in both isolated galaxy simulations and in cosmological runs for which a frequently cited possible cause of discrepancies with observational data is incorrect modeling (Tasker & Bryan 2006b and references therein). Improved modeling of the ISM on a global scale could result in a fuller understanding of feedback, ultimately allowing for more accurate feedback routines in large cosmological simulations in which the resolution of individual galaxies is not yet possible.

In this paper we compare global models of isolated disk galaxies with three distinct ISM types. The first of these includes radiative cooling down to 300 K, the second type contains radiative cooling and a background photoelectric heating source, and our final type has an isothermal ISM at a constant temperature of $10^{4}$ K. For each of these models, we test two common prescriptions for star formation and the effects of feedback from Type II supernovae. The resulting structures are contrasted, and the star formation properties of the disks compared with observations.

For these simulations, we use a high-resolution adaptive mesh refinement (AMR) code, which includes a full treatment of self-gravity of the gas, rather than the fixed potential that is often used, and a more sophisticated treatment of star formation and feedback. Our simulations concentrate on hydrodynamical effects, ignoring magnetic fields and cosmic-ray pressure.

In § 2 we describe our computational approach, including details of the code we are using, and lay out the initial conditions for the problem. Sections 3 and 4 focus on the disk structure and the properties of the ISM, while § 5 looks at comparisons with observations.

2. NUMERICAL METHODS

2.1. The Code

The simulations were performed using the hydrodynamics AMR code ENZO, described in Bryan & Norman (1997), Bryan (1999), Norman & Bryan (1999), Bryan et al. (2001), and O'Shea et al. (2004). The AMR technique is particularly effective in the present work for which the resolution of a complex multiphase medium is of paramount importance. The grid cells form natural boundaries, which makes it possible to model the evolution of gas with a range of temperatures (Slyz et al. 2005; TB06). Other codes that use particle-based techniques frequently have an over-mixing problem, causing unphysical radiative losses unless algorithmic correction procedures are undertaken (Marri & White 2003; Springel & Hernquist 2003). As a result, most previous simulations have not been suited to properly model a multiphase interstellar medium, which means that the importance of the role of the ISM in star formation cannot be assessed.

For these simulations, we use a 3D periodic box of side $1 \ M_{\odot}^{-1} \text{Mpc}$. With a root grid of $128^{3}$ and eight levels of refinement, our smallest cell size, and therefore maximum resolution, is approximately 50 pc. For our higher resolution run, the cell size was decreased further to 25 pc.

To evolve the gas through time, ENZO uses a 3D version of the ZEUS hydrodynamics algorithm (Stone & Norman 1992). Radiative gas cooling followed the cooling curve of Sarazin & White (1987) down to temperatures of $10^{4}$ K and then corresponded to rates from Rosen & Bregman (1995) down to 300 K. (The exception to this involves the simulations performed with an isothermal equation of state for the gas, where no cooling is allowed.) This bottom temperature threshold is still above what would be found in the dense molecular clouds, but here we follow Rosen & Bregman (1995), who argued that this procedure crudely compensates for physical processes not modeled, such as magnetic fields, turbulence, and cosmic-ray pressure. This temperature range does take us to the upper limit of the cold neutral medium (Wolfire et al. 2003), allowing us to sample a realistic spread of phases in the gas.

In addition to cooling, the gas can also be heated through supernovae feedback (as described below) and photoelectric heating. Photoelectric heating, that is, the photoemission of UV-irradiated dust grains, is thought to be the dominant factor in the formation of the cold and warm neutral mediums (Wolfire et al. 1995). If photoelectric heating is turned on, ENZO includes the term $\Gamma_{pe} = 5.1 \times 10^{-26} \text{ergs s}^{-1}$ in the energy equation for the gas, in accord with a scheme based on Joung & Mac Low (2006) but without the dependence on the height above the disk adopted in that work. The value of $\Gamma_{pe}$ depends on the incident radiation field and, as such, can be tied to the star formation rate (SFR) in the gas. However, since we are considering Milky Way–sized galaxy disks, we follow Joung & Mac Low (2006) and adopt a number consistent with the local interstellar value. Since this value is likely to have been higher at earlier times, we also perform a run with a heating rate of $\Gamma_{bs} = 1.41 \times 10^{-24} \text{ergs s}^{-1} = 30 \Gamma_{pe}$, a value that balances the cooling rate at densities of $1.0 \text{cm}^{-3}$ at our initial temperature of $10^{4}$ K. However, the increase in heating makes a relatively small difference to the star formation properties of the disk, so this run is added to the discussion only and not included in our main analysis. Note that we do not include photoionization heating, because full radiative transfer would be required for it to be modeled properly.

ENZO forms a star particle in a grid cell if the following criteria are fulfilled (Cen & Ostriker 1992; O’Shea et al. 2004): (1) the baryon density in the grid cell exceeds a designated threshold density, (2) the mass of gas in the cell exceeds the local Jeans mass, (3) there is convergent flow into the cell (i.e., $\nabla \cdot \mathbf{v} < 0$), and (4) the cooling time of the gas in the cell is less than its dynamical time ($\tau_{cool} < \tau_{dyn}$) or the gas is at the minimum temperature allowed of 300 K. We also consider one set of galaxy disks modeled with a purely isothermal interstellar medium. In this case, the criteria noted above are relaxed to include only the first three rules, since the gas is not subject to cooling.

If a grid cell meets the required criteria for star formation, gas is removed from the cell and a star particle is formed, with mass calculated by

$$m_{*} = \epsilon \frac{\Delta t}{t_{dyn}} \rho_{gas} \Delta x^{3}, \quad (1)$$

where $\epsilon$ is the star formation efficiency (more properly the efficiency per dynamical time), $\Delta t$ is the size of the time step, $t_{dyn}$ is the time for dynamical collapse, and $\rho_{gas}$ is the gas density. A final, purely computational criteria is that even if a grid cell fulfills all the above criterion, a star particle will still not be formed if its
mass is less than a given minimum value of \( (\text{for this work}) \ 10^8 M_\odot \). Since the reason for this clause is purely numerical (a large number of small stars would greatly slow down the simulation), an override exists that creates a star below the minimum mass with a probability equal to the ratio between the mass of the would-be star particle and the minimum star mass. If this occurs, the resulting star mass is that of the minimum star mass, or 80\% of the mass in the cell, whichever is smaller. The star particle’s formation is then spread out over roughly a dynamical time, to mimic the formation of stars in the giant molecular clouds that follow the same timescale.

The star particles themselves are modeled as a collisionless system using the \( N \)-body method. By mapping their positions onto the grid via a cloud-in-cell technique to produce a discretized density field, we model the particles’ gravitational interaction with the gas. The number of star particles formed varies greatly depending on the values chosen for the threshold density and star formation efficiency described above. For our C-type star formation method, in which these values are low (see § 2.3), roughly 5 million particles were used by the end of the simulation. In our D-type algorithm these values are higher and the number of star particles formed is reduced to around 40,000.

ENZO can also include stellar feedback from Type II supernovae, which is often suggested as the main driving force for self-regulated star formation. When this feedback option is used, as it is in about half of our simulations, then \( 10^{-5} \) of the rest-mass energy of generated stars is added to the gas’s thermal energy over a time period equal to \( t_{\text{dyn}} \). This energy is equivalent to a supernova of \( 10^{51} \text{ ergs} \) for every 55 \( M_\odot \) of stars formed. The energy is deposited into the gas over one dynamical time or 10 Myr, whichever is longer. During this period the energy is injected into the cell closest to the particle’s current location.

For all simulations, we adopt a cosmological model of a \( \Lambda \)CDM universe with \( \Omega_m = 0.3, \Omega_\Lambda = 0.7, \) and \( H_0 = 67 \text{ km s}^{-1} \text{ Mpc}^{-1} \).

2.2. The Initial Conditions

The initial conditions for our disk are the same as for the simulations performed in TB06. They entail an ideal isothermal gas disk of temperature of \( 10^4 \text{ K} \) and \( \gamma = 1.67 \), whose density profile is given by

\[
\rho(r, z) = \rho_0 e^{-r^2/\alpha} \text{sech}^2 \left( \frac{z}{2z_0} \right),
\]

sitting in a static dark matter halo. The major difference between these initial conditions and the ones set out in TB06 is the gas mass in the disk, which we choose to be \( 6 \times 10^{10} M_\odot \), 6 times higher than that in TB06, bringing it into line with the estimated total disk mass of the Milky Way (we do not begin with any stars). We also change the disk dimensions slightly from TB06, selecting a scale radius \( r_0 = 3.5 \text{ kpc} \) and a scale height \( z_0 = 325 \text{ pc} \).

### Table 1

| Model | Simulation | \( \text{min } \Delta x \) (pc) | \( \epsilon \) | \( \eta_{\text{thresh}} \) (cm\(^{-3}\)) | Fb | Iso | Heat |
|-------|------------|-------------------------------|-----------------|-------------------------------|------|-----|------|
| ISM 1 | C          | 50                            | 0.05            | 0.02                          | No   | No  | No   |
|       | D          | 50                            | 0.5             | \( 10^3 \)                    | No   | No  | No   |
|       | CFDBCK     | 50                            | 0.05            | 0.02                          | Yes  | No  | No   |
|       | DFDBCK     | 50                            | 0.5             | \( 10^3 \)                    | Yes  | No  | No   |
| ISM 2 | HC         | 50                            | 0.05            | 0.02                          | No   | No  | Yes  |
|       | HD         | 50                            | 0.5             | \( 10^3 \)                    | No   | No  | Yes  |
|       | HCFDBCK    | 50                            | 0.05            | 0.02                          | Yes  | No  | Yes  |
|       | HDFDBCK    | 50                            | 0.5             | \( 10^3 \)                    | Yes  | No  | Yes  |
|       | HDHRES     | 25                            | 0.5             | \( 10^3 \)                    | No   | No  | Yes  |
| ISM 3 | IC         | 50                            | 0.05            | 0.02                          | No   | Yes | No   |
|       | ID         | 50                            | 0.5             | \( 10^3 \)                    | No   | Yes | No   |
|       | IDJEANS    | 50                            | 0.5             | \( 10^3 \)                    | No   | Yes | No   |

Our simulated galaxy disks are divided into three categories, depending on the nature of their ISMs. For the first four simulations listed in Table 1 the gas is allowed to radiatively cool down to 300 K via the cooling curves described in § 2.1. This is the same setup (although for a heavier disk) that we presented in TB06. The next five runs also allow radiative cooling along the same curve, but they include an additional photoelectric heating term, as described in § 2.1. The last three simulations use an isothermal equation of state, a popular assumption in global disk models for which it has been hard to resolve a multiphase medium. The temperature of all the gas in these runs is fixed at \( 10^4 \text{ K} \).

For each of these three ISM models, we consider two different star formation routines. These were presented in TB06, and we retain notation of C and D types used in that paper. C-type star formation has an efficiency appropriate to the galactic disk as a whole, and one that is typically used in large-scale cosmological simulations (5\%). Because this is a global average, we use a low-density threshold, allowing stars to form in relatively low-density regions (providing they meet the criteria outlined in § 2.1). Since this means that we do not follow the formation of the densest clumps, we use a Schmidt-like law to model the SFR. D-type star formation, on the other hand, makes use of the resolution in the disk and confines star formation to the densest structures, which at our resolution compare to the largest giant molecular clouds. Stars therefore form only where the density is high (\( 10^3 \text{ cm}^{-3} \)) but with a much higher efficiency per dynamical time, of 50\%.

Simulations that include stellar feedback from Type II supernovae are performed for both the disks with radiative cooling (CFDBCK and DFDBCK for C- and D-type star formation, respectively) and for disks with radiative cooling and background heating (HCDFDBCK and HDFDBCK). In addition to these simulations, we also perform runs designed to test the robustness of
our results. HDHIRES is the same as HD, but with a root grid with twice the spatial resolution and thus 8 times the mass resolution. IDJEANS uses identical conditions to ID, but adds another refinement criterion, resolving a cell when the Jeans length drops below four cell widths (at least until we reach the maximum refinement level), as suggested by Truelove et al. (1997). As mentioned in § 2.1, we also perform a run with a higher heating rate. This run is discussed in § 6 at the end of this paper.

The run times for these simulations depended greatly on whether stellar feedback was included. Without feedback, a run typically took \( \sim 40 \) hr on 8 processors of an Opteron Beowulf cluster. When feedback was introduced, the run took \( \sim 130 \) hr on 64 processors of a Xeon cluster.

3. THE STRUCTURE OF THE DISK

During the initial evolution of our galaxy disks, we see the gas fragment triggering a starburst. This process is described in detail in TB06, but for this work we want to avoid this primary collapse and compare our disks after they have reached a settled state but before any gas depletion becomes an issue. To judge where this point is, we examine the gas density in the disk over time. In the first 200 Myr, we see a clear and rapid drop in density, corresponding to the initial fragmentation. The density then settles down, decreasing slowly as stars are formed until after around 500 Myr, when the profile starts to deteriorate, especially in the nonfeedback cases, as the majority of the gas is now converted to stars. Our images and plots are therefore largely taken between 200 and 400 Myr, when the initial starburst is over and the disks still have a substantial supply of gas.

3.1. Imaging the ISM

The global structure of the ISM can be viewed using face-on projections of the disk, as shown in Figures 1, 2, and 3. Figure 1 shows projections for our first ISM type—the top four simulations listed in Table 1, all of which include radiative cooling but no background heating. From left to right, the images show gas density, temperature, pressure, and stellar density. The top two rows, which show runs without feedback, clearly show the region where the gas is gravitationally unstable. As in TB06, we see that the central gas has collapsed to form dense filaments and knots out to a clearly defined radius. Outside this region, the gas is stable and remains unperturbed. Earlier images show that the same pattern forms for the initial evolution of all the runs, with a circular perturbation moving outwards from the center of the disk, which then collapses tangentially to form filaments and knots of gas. The introduction of feedback (bottom two rows) destroys these filaments, smoothing the gas distribution regardless of the type of star formation used. The effect of this smoothing is shown both in the temperature distribution and with the disk’s pressure. Hot outflows are seen and cold gas is no longer confined to the dense star-forming knots, but rather is blown around the disk. We see below that this process acts not only to change the balance of the phases in the ISM but also to suppress the star formation, as knots of gas are destroyed before they can collapse into stars. It also affects the stability in the outer regions of the disk, which we discuss more thoroughly in § 5.2.

The feedback temperature projections also show us the first evidence of the different effects of the C- and D-type star formation routines. The C-type stars cause relatively even outflows (something we return to in the next section), resulting in a more uniform disk. The D type, on the other hand, concentrates the outflows, and so we see that one side of the disk is much colder than the other side. The position of these outflows changes as the disk evolves, but the separation of the phases is always present. This result is unsurprising if we consider the physics of each stellar type: The D-type stars only form in the densest regions, where they form efficiently and in large numbers. This produces a focusing of stellar material that is transferred to a concentrated injection of energy from supernovae. On the other hand, C-type stars form more uniformly, producing a smoother distribution and hence an even injection of energy. This is shown most clearly in the final column, displaying stellar distributions. The C-type stars, forming at much lower densities, extend smoothly out until the threshold radius for gravitational collapse. The D stars, by contrast, form only in the densest areas of the disk, confining them to the central region, where the gas has collapsed both radially and tangentially into dense knots. This result differs somewhat from what was found in TB06, where the lighter disk meant that both C- and D-type star formation algorithms produced stars only in the completely collapsed regions, whereas here we see C-type stars forming in the mildly perturbed areas of the disk (see also § 5.2).

The feedback outflows also disturb the pressure in the disk. Nonfeedback runs C and D show small-scale variations in the pressure distribution, with the dense, star-forming knots of gas being at a higher pressure than the surrounding ISM. The inclusion of feedback, especially in the focused D-type star formation, upsets this distribution, showing the large-scale hot outflows to be overpressurized with respect to the disk.

Our second ISM type includes background heating in addition to radiative cooling. Figure 2 shows the projections for runs HC, HD, HCFDBCK, and HDFDBCK for the same properties as Figure 1. Unlike the first ISM type, we see a notable difference in the C and D star formation types in the runs without feedback. The C-type star formation produces large voids that contain hot, low-density gas. This shape comes out less clearly in the stellar distribution, but the dense star clusters are confined to the filaments surrounding these holes. The holes have largely vanished in the disks that include feedback, although they all display a porous nature. The same holes are also seen in run C, but only during the first 250 Myr of the simulation. After that point, the circular wave speeds up with respect to the HC simulation and decreases in strength. Exactly why this occurs is not clear. One explanation is that the extra heating in the HC case provides an added pressure that stabilized the circular mode. Alternatively, this might be a numerical effect, and with improved resolution the porous structure would be retained in the C case as well as the HC simulation. Either way, the presence of holes in the disk is an interesting event and one that has been seen both in our own galaxy and, more dramatically, in the H i map of the LMC. Their presence has traditionally been put down to stellar winds and supernovae explosions evacuating the cool ISM (van der Hulst 1996). However, Rhode et al. (1999) was unable to find evidence of remnant star clusters in the center of the H i holes in the irregular galaxy Holmberg II, suggesting that supernovae were not present there. The issue was also investigated theoretically via two-dimensional (2D) simulations of an LMC-type galaxy performed by Wada et al. (2000), which suggested that gravitational and thermal instability alone are enough to create a porous ISM and that these are actually disrupted in the presence of frequent supernovae. This conclusion would appear to agree well with our findings that the nonfeedback run contained holes but that these largely vanish when feedback is included in the simulation.

Run HD with D-type star formation also shows some evidence of cavities, but not as strongly as HC. What is noticeable is that the dense knots of gas are far more evident in this image than in the equivalent run D for ISM 1 in Figure 1. The overall filament
structure in both HC and HD is reduced compared to the non-heated simulations, suggesting that the effect of heating is to act against the collapse, increasing the Jeans length to allow only the larger perturbation to form knots. These dense knots, however, extend out farther in the heated than in the nonheated case, although the smaller perturbations are smoothed out. We return to this quantitatively when we consider disk stability in § 5.2.

Feedback again acts to smooth the gas distribution, although less effectively than in the CFDBCK and DFDBCK cases, allowing dense knots of gas to survive, again indicative of them being larger and more tightly bound than in the ISM 1 case. We see the same symmetry to the feedback outflows with C-type star formation that we see in Figure 1, as well as the focused ejections of the D-type simulations in which the star formation is confined to a much smaller area.

The pressure distribution in the disk is almost entirely isobaric for the runs without feedback, with only the densest knots in the D-type star formation in HD being at a slightly higher pressure.

![Figure 1](image_url)
The heating of the low-density background gas also raises its pressure and causes it to be in pressure equilibrium with the disk. Feedback again acts to disrupt this in the disk, most markedly in the D-type star formation case, in which the hot gas is marked by considerably higher pressures.

Our final ISM type is for the disks with an isothermal ISM at a constant temperature, of $10^4$ K. The projections of these runs are shown in Figure 3. We see the effects of stopping the disk from cooling in the size of the knots of gas, which are visibly larger than in either ISM 1 or ISM 2 due to the higher Jeans length throughout the whole disk. As a result, the fragmentation is limited to the disk’s central region, which, especially in the case of the C-type star formation, becomes depleted of gas. The resulting cavity looks similar to that found in HC, although it is smaller and corresponds to regions of dense star clusters rather than a lower density of stars. In this respect, the C-type star formation looks more like the D type, with the majority of star formation in large clusters in the disk center. Later evolution shows this central cavity growing, leaving a gas deficit void. Overall, the disk takes on a smoother appearance.

**Fig. 2.** — Same as Fig. 1, but for the runs with cooling and photoelectric heating. Top to bottom: Simulations shown are HC, HD, HCFDBCK, and HDFDBCK. [See the electronic edition of the Journal for a color version of this figure.]
The production of larger, if fewer, dense gas knots has a dramatic effect on the stellar density for the C-type star formation run. Analysis of the star clusters (described in S. P. Gill et al. 2008, in preparation) produced by the large knots of gas reveal masses up to $10^{10} M_{\odot}$ with half mass radii on the order of a cell size. These huge dense clumps gravitationally interact with close star particles, accelerating a small fraction of them up to 1000 kms$^{-1}$, resulting in ejection from the disk in high-velocity streams. By contrast, the largest star clusters formed in the C run are a factor of 10 less in mass and much more diffuse, resulting in a significantly smaller gravitational pull on nearby star particles. In the case of D-type star formation, the star clusters are more tightly bound (since they form only in the densest gas), which makes it harder for star particles to be ejected at high velocities.

Outflows of this magnitude and speed in the IC case are not observed in real galaxies, and this is a point against using the isothermal ISM model with the C-type star formation algorithm. However, the ejection of star particles by cluster interactions raises an interesting question about star formation in the outer parts of the disk. Observationally, low-luminosity stars have been found at large radii (Ferguson et al. 2002; Boissier et al. 2006), beyond the point where the disk is traditionally gravitationally stable. How these stars got there is an open question, but they may have been produced during satellite interactions, or they may have been thrown there from interactions within the disk. Figure 3 suggests that interactions between heavy star clusters could potentially produce this effect.

The pressure projections show the isothermal model to be the least isobaric of the three ISM types. This is unsurprising when we consider that fixing the temperature forces the pressure to mirror the density distribution. We see here that the gravitationally collapsed structures are overpressurized with respect to the disk and voids of gas have low pressure.

3.2. The Vertical Profile

The vertical structure of the disk and—linked with this—the interaction between the disk and the halo are thought to play a vital part in the disk’s evolution. Indeed, de Avillez & Breitschwerdt (2004) cite the cycle of gas between the disk and the halo as being one of the primary factors in determining the phases of the ISM in their small-box simulations. They find the ability of hot gas to lift off the disk’s surface acts as a pressure release valve on the ISM. This is in keeping with the work done by Norman & Ikeuchi (1989), whose model of the hot gas being removed vertically through galactic chimneys allowed a lower filling factor than in the original picture from McKee & Ostriker (1977), more in keeping with observations.

Figure 4 shows the vertical projections of the baryonic density in our feedback runs for ISM 1, CFDBCK, and DFDBCK (the results are similar for HCFDBCK and HDFDBCK in ISM 2). The left-hand image shows the simulation with C-type star formation, whereas the right-hand one has D-type stars. Both galaxies are clearly injecting a significant amount of material out of the disk and into the halo, consistent with both Norman & Ikeuchi’s (1989) analytical picture of the ISM and de Avillez & Breitschwerdt’s (2004) small-box simulations. We have already seen in Figures 1 and 2 that the outflow gas is highly pressurized, in keeping with the release valve idea. This finding is in contrast with the simulations without feedback, where the gas is confined to the disk’s surface. These images are taken shortly after the outflows begin in the disk, at 142 Myr, when the difference between the C- and D-type star formation is sharply apparent: D-type star formation not only results in an asymmetrical distribution of gas within the disk, as seen in §3.1, but the gas is also ejected unevenly from the disk’s surface. This unevenness is most likely a result of the density threshold in the D-type star formation...
prescription, which can only be met in large clumps and so is naturally highly inhomogeneous. The right-hand panel of Figure 4 shows one outflow extending away from the bottom of the disk that has almost reached the image’s edge. A second outflow, either just starting up or condensing to fall back in, is shown at the top of the disk. The C-type star formation, by contrast, produces an even distribution either side of the disk, suggesting that gas is being emitted from both sides largely at the same time. Despite the symmetrical differences in the gas ejection of the two star formation types, neither run shows the majority of the gas leaving the gravitational pull of the galaxy. Rather, the gas cools above the disk and falls back down in a galactic fountain effect. This can be seen in Figure 5, which shows both the net mass flux as a function of height from the disk and also the outwards-bound—only gas. The mass flux is averaged over almost 200 Myr, from $t = 283–472$ Myr and over this time range the overall outflow from both C- and D-type star formation is roughly symmetrical above and below the disk. The net mass flux, however, is much smaller than the outflow, showing that the majority of the gas returns to the disk. The size of the outflow is strongly dependent on the star formation type. D-type star formation, with its concentrated clumps, produces a significantly stronger outflow than the C-type, reaching maximum mass fluxes of $30 \ M_\odot \ yr^{-1}$ compared to around $10 \ M_\odot \ yr^{-1}$. In both cases, the outflows are largely restricted to only a few kiloparsecs away from the disk. In the C-type case, there is almost nothing outside this region, whereas the D type shows evidence of outflows extending farther away from the disk and infalling gas up to heights of $20 \ kpc$. A more quantitative way of studying the vertical distribution in the disk is to examine the one-dimensional (1D) profiles. Figure 6 shows the variation of baryon density with height after $472$ Myr for each of the ISM types. The effect of changing the properties of the ISM is very striking in this plot, especially for the runs that do not include feedback. In the top panel, simulations C and D with ISM 1 are shown that have a peaked profile with a vertical scale height of about $50 \ pc$ (and that is probably unresolved in the simulation). When background heating is added for HC and HD in ISM 2 (middle panel), the disk broadens out, producing a scale height of roughly twice that in ISM 1. It is worth noting, however, that our background-heating term is a constant. A more peaked profile might have been achieved by varying the heating rate with disk height, as was done in Joung & Mac Low (2006). The background heating also affects the two star formation types in different ways: The HD profile is broadened.
to a greater extent than in HC, which becomes flattened in the central most region of the disk. In the isothermal case, the disk is more insensitive to star formation type, although the D-type star formation in ID extends to a higher $z$ than in IC. The profile shape and scale height are very similar to HD, with $z \sim 100$ pc.

The addition of feedback has the same effect on both ISM 1 and ISM 2, producing a far flatter and broader profile, indicative of the destruction of the central dense gas knots and material being distributed farther out from the disk by the outflows. Like ISM type, star formation type has little impact in this case.

Our higher resolution simulation, HDHIRES, closely follows its lower resolution counterpart, HD. Likewise, the run IDJEANS, specifically designed to resolve where the Truelove criteria for resolution is not met, is almost identical to ID. This is true for all other plots in this paper.

Over time the vertical profile remains fairly stable, although runs with C-type star formation decrease in density more quickly than the D type as the gas is used up in the disk. Feedback acts to reduce this effect and, indeed, it suppresses star formation, as we see in § 5. Heating the disk also suppresses star formation in the HD run, but it has markedly less effect on HC, which continues to lose gas. The exception to this involves the isothermal runs, which are particularly stable, especially ID, which shows much less evolution over the course of the simulation.

The vertical pressure profile of the disks is shown in Figure 7. Most noticeably, runs with ISM 1 and ISM 2 have largely isobaric profiles, as indicated in the projections. The isothermal runs (ISM 3) meanwhile have pressure proportional to density and show a clearly peaked distribution. The introduction of feedback in ISM 1 and ISM 2 raises the pressure, corresponding to the high-pressure regions we see in the radial projections in Figures 1 and 2. What is apparent now, however, is that the disk is in greater pressure equilibrium across its height, as gas is ejected from the disk’s surface. This finding shows that the gas ejection seen in Figure 4 is indeed acting as a pressure release system, as described in Norman & Ikeuchi (1989).

4. PHASES IN THE ISM

4.1. The Density PDF

Section 3 shows that the different types of ISM models make a noticeable difference to the appearance of the galaxy disk, bringing us back to our original problem: if ISM conditions affect the galaxy so much, why do observations show such a simple relation between local gas surface density and star formation properties on large scales? A way to explain this problem has been suggested by Elmegreen (2002), who noted that if the density distribution were everywhere a log-normal distribution and if
star formation occurred above a fixed density, then the Schmidt law would result. This means that despite its complex nature on very small scales, the fraction of gas dense enough to form stars would always be known from this profile. Slyz et al. (2005) points out that this conclusion does not completely hold, since no spatial information would be available from such a PDF, resulting in the possibility that the dense regions do not contain enough mass to exceed the critical Jeans limit for collapse. That aside, the presence of a universal density distribution function in our disks could indicate that such a link between the small and large scales is possible.

Previous simulation work has found evidence that a single profile could be fitted to a range of galaxies, but there is no agreement on the shape it must have. The debate largely centers on whether the PDF is best fitted by a lognormal or a power-law curve at high densities (where star formation occurs). Scalo et al. (1998) puts this discrepancy down to the nature of the gas, finding that an isothermal flow follows a lognormal distribution, while a gas with $\gamma \neq 1$ is better represented by a power-law fit. This view is contradicted in global simulations performed by Wada & Norman (2007, 2001), who do find a lognormal PDF fit without the need for an isothermal gas, although they note a steepening at high densities, which might be indicative of a power-law tail on the PDF. Kravtsov (2003) also finds a log-normal fit for his cosmological simulations of high-redshift galaxies, as do Slyz et al. (2005) in their 3D small-box simulations. But both note that at the high densities where the fit is applied, the gas is in fact nearly isothermal.

The global simulations of Wada & Norman (2001) and the cosmological simulations of Kravtsov (2003) show an insensitivity to the input physics, in particular finding that the inclusion of stellar feedback does not affect the PDF shape except at the low-density end, where Kravtsov (2003) notes that feedback produces more low-density gas. Slyz’s small-box simulations at high resolution show a greater sensitivity to the inclusion of feedback, without which the gas resides predominantly at higher densities. The normalized volume-weighted gas density PDFs for our simulations are shown in Figure 8 at two different times; the left column shows the profile at 377 Myr, when the disk has settled after the initial burst of star formation, and the right-hand column shows the profile at the end of the simulation, when the majority of the gas has been used up in the disk. The rows separate our three ISM types with the different runs labeled in the key.

At 377 Myr, all three of the ISM types show a similar shape at high density and are reasonably well matched by a lognormal fit. Disks with ISM 1 that do not include feedback show a slightly bimodal profile, indicative of a thermal instability (Vázquez-Semadeni et al. 2000). However, the introduction of feedback

![Vertical pressure profile at 472 Myr into the evolution of the simulations listed. The profile is also averaged within two radial scale heights.](image_url)

Fig. 7.—Vertical pressure profile at 472 Myr into the evolution of the simulations listed. The profile is also averaged within two radial scale heights.
smooths the profile, allowing the disk to follow a lognormal profile even at low densities. Later evolution of all runs shows an increase in the substructure of the disk, with a higher percentage of gas found at lower densities, as shown in the right-hand column of Figure 8 at 1.3 Gyr. The shape of the PDF at this time is similar to that found by Slyz et al. (2005) in their small-box simulations with feedback, although our nonfeedback simulations in this ISM show the same profile. By this stage, gas depletion is starting to become an issue in the runs without feedback, which show the high-density tail being eaten away. This is particularly true in the C-type star formation run (C), which shows greater gas loss than the D run. Feedback slows this process considerably and, while not totally preventing it, maintains its lognormal fit. The lack of substructure and reduced gas loss suggests that feedback is having a stabilizing influence on the disk.

The introduction of background heating in ISM 2 makes little difference to the profiles at 377 Myr, producing slightly more low-density gas in the feedback cases. However, the profile shows markedly less evolution than we see in ISM 1 models, maintaining a larger volume at medium densities at the end of the simulation. This effect is most noticeable in the simulations without feedback, which have a significantly higher dense gas content at $t = 1321$ Myr than their ISM 1 counterparts, C and D. The amount of low-density gas is less than in runs with ISM 1 and slightly greater in the feedback case. The heating term has the strongest effect on the D-type star formation without feedback (HD), reducing gas loss by a factor of 10 from the D case, so that it resembles the feedback runs. This results in the lognormal profile being largely maintained in the HCFDBCK, HDFDBCK, and HD cases. Our higher resolution run, HDHIRES, shows little difference from its lower resolution counterpart, HD, indicating that these results are not resolution dependent.

The isothermal ISM disks become bimodal at around 700 Myr, although this development is clearly not related to a thermal instability. This peak in the low-density gas results from material that is out of pressure equilibrium in areas such as the disk center (where star formation has consumed much of the gas) and above the disk (where we would expect the temperature to be high). The log-normal fit is slightly less good even at early times here, indicating that a power-law fit might be better. However, this issue is very hard to judge, since, like Wada & Norman (2001), we are limited by our resolution. The C- and D-type star formation runs show very little difference in this ISM.

Over the main part of the simulation, our disks show a lognormal profile in the medium- and high-density gas that is largely insensitive to ISM model, star formation type, or the introduction of feedback. This fit stretches over several orders of magnitude in density, in keeping with models by Wada & Norman (2007, 2001)

Fig. 8.—PDF of the volume-weighted gas density in the simulated galaxy disks at 377 Myr and at 1.32 Gyr. A lognormal distribution is overlaid in the top two panels.
and Slyz et al. (2005), but contradicting Scalo et al.’s (1998) statement that the gas must be isothermal to attain a lognormal fit. Substructure in the disk is clearly visible in the lower density gas, indicative of the multiphase nature of the ISM.

At late times, the gas profile fit is eroded by gas depletion in the models in which feedback or background heating are not present. The addition of background heating prevents gas depletion for the D-type star formation routine, but it has less effect on the C-type algorithm. Our pure isothermal model shows signs of gas depletion, although not as marked as in models in which cooling is allowed and feedback is not present. The increase of substructure at later times makes it difficult to determine the best profile fit. The lognormal fit is certainly satisfactory, but a power-law curve might well do as good a job, especially in the case of the isothermal run, which seems to show a steeper profile. At our resolution, however, this is still difficult to determine.

4.2. Temperature and Pressure Profile Evolution

In addition to the volume of gas at different densities, the 1D temperature distribution can also provide valuable information about the ISM. Figure 9 shows the evolution of the temperature over the course of the simulation. The top row shows the simulations that have ISM 1, while the bottom row shows ISM 2. The isothermal model (ISM 3) has, of course, only gas at 10^4 K.

All the simulations with ISM 1 follow a very similar evolution, regardless of star formation type or inclusion of feedback. Initially, the gas quickly cools from the 10^4 K starting temperature to the minimum allowed temperature of 300 K. As the disk fragments and forms stars, the gas is heated by spiral shock waves, infall onto the disk, and (in the case of runs that include feedback) supernovae explosions. By 708 Myr (third column), the gas is largely in two temperature pockets: warm gas at 10^4 K and hot gas at 10^6 K. As star formation continues, the cooler gas is either used up or heated, leaving only the hotter gas in the disk, which corresponds to the low-density peak in Figure 8.

The addition of background heating in ISM 2 results in the simulation being significantly more sensitive to stellar feedback, since the background heating has a stronger effect on the non-feedback runs. The added heating stabilizes the warm phase, resulting in the majority of gas remaining at 10^6 K over the initial part of the simulation, rather than cooling to 300 K, as in ISM 1. In this respect, these disks are most similar to the isothermal case, with the majority of their gas in the stable, warm phase. The warm phase remains throughout the simulation, but it is reduced by the addition of feedback, which converts more of the gas into the hot phase. This is a reflection of what we see in Figure 8, in which HC and HD maintained a stronger population of medium-density gas that we now see is the warm phase, whereas the runs HCFDBCK and HDFDBCK resulted in a great proportion of gas in the low-density (and therefore hot) phase.

Again, the difference between the C- and D-type star formation routines is minor, except in the case of HC and HD, where HC contains more hot gas than HD.

The final 1D study we can make of this type is the volume-weighted pressure, which is shown in Figure 10 for the same times as in Figure 8. While not completely isobaric, the range of pressures at 377 Myr in all the nonisothermal disks is reasonably small. This is especially true for ISM 2, where radiative heating raises the temperature of the lowest pressure gas (we return to this point in more detail in the next section) and least true for ISM 3. Feedback acts to broaden the distribution. ISM 1 and ISM 2 show little variation over time, implying that the disks are in rough pressure equilibrium. The isothermal case, however, evolves into a bimodal distribution by 1.32 Gyr, with a significant quantity of gas at low pressure. This feature is a direct reflection of the density in Figure 8, since the temperature cannot change.

4.3. The ISM as a Three-Phase Medium

Taking the idea of the traditional three-phase ISM portrayed by McKee & Ostriker (1977), we next looked at the evolution of
the cold, warm, and hot material in the disk over the course of the simulation. Assuming that the cold ISM consists of temperatures $<10^3$ K, the warm ISM is between $10^3$ and $10^5$ K, and the hot ISM is at temperatures above $10^5$ K, we look at the evolution of both the volume and mass fractions in the disks.

Figure 11 shows the volume-weighted (top panels) and mass-weighted (bottom panels) evolution for the disks with ISM 1. As in Figure 9, we see the majority of the gas volume initially cools, filling the cold phase. As star formation removes the dense, cold gas, the warm phase begins to dominate. SNe feedback increases the hot phase in the CFDBCK and DFDBCK runs, while the non-feedback cases become depleted of still more of gas, allowing the hot phase to dominate and eventually to encompass most of the volume in the disk. The resulting pattern is relatively independent of feedback and star formation type, although the move to the warm phase occurs slightly earlier for runs with feedback, since they have the added energy injection.

The gas mass, on the other hand, resides predominantly in the cold phase, sitting in the dense knots of matter that go on to form stars. Despite its large volume, very little mass actually resides in the hot phase (note the change of scale on the hot phase plot abscissa).

Figure 12 shows the same set of plots for ISM 2. The difference between the types of run here is much more marked. In all cases, however, very little of the gas volume is contained in the cold phase, less than that for the runs in ISM 1. This finding is in agreement with Figure 9, where we see that a significant proportion of the gas stayed at $10^4$ K and was boosted out of the cold phase by the background heating. For the runs without feedback, the majority of the volume and mass of the gas sits in the warm phase, causing the disk to be closer to isothermal in these conditions. This suggests that star formation is being suppressed in the HD and HC cases, with respect to runs C and D, as the cold star-forming gas is reduced by being moved to the warm phase. We see in §5 that this is indeed the case. The warming of the gas also causes less of the gas volume to be in the hot phase, since the cool gas has not all been depleted. The feedback runs also start with the bulk of their volume in the warm phase, but this condition is swiftly overridden by the stronger effects of the SNe energy injection, heating the gas and moving it into the hot phase.

A better way to see the phase structure of the ISM is via 2D contour plots of the density versus temperature. Figure 13 shows the volume-weighted contour plots for the disks with ISM 1 (left) and disks with ISM 2 (right) at 377 Myr. The straight black lines
mark lines of constant pressure (neglecting changes in the mean molecular mass).

The runs with ISM 1 and no feedback (i.e., C and D) show similar behavior: there is rough pressure equilibrium with 1 or 2 orders of magnitude scatter along the pressure direction (as seen earlier). The sharp feature at \( \log(T) = 2.5 \) is due to our minimum temperature cutoff and the gas residing in the narrow feature that rises to higher pressure is gravitationally bound. This is the cold, dense phase. A peak in the volume distribution can be seen for the high-temperature phase (and less clearly for the warm phase at \( T \sim 10^4 \) K). Feedback acts to broaden this distribution, as can be seen in the CFDBCK and DFDBCK runs, making the pressure equilibrium less obvious.

The heated runs (HC and HD) show a very different behavior, with a much tighter relationship between density and temperature. This difference is due to the imposition of equilibrium between

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**Fig. 11.** — Evolution of the cold, warm, and hot phases in the disk simulations with ISM 1. Here the cold phase is defined as gas less than \( 10^3 \) K, the warm phase as being between \( 10^3 \) and \( 10^5 \) K, and the hot phase as having temperatures greater than \( 10^5 \) K. The mass fraction refers to the gas only. Note the different scale for the hot ISM mass fraction.

**Fig. 12.** — Same as Fig. 11, but for ISM 2. Note the different scales on both the cold volume fraction and the hot mass fraction.
cooling and heating at low temperatures (below $10^4$ K), which leads to the cold phase having higher pressure. The increased pressure tends to force gas into the warm phase and reduces the SFR because of the reduced amount of cold, dense gas. Adding feedback on top of this effect broadens the distribution somewhat, but has a milder effect than in ISM 1.

5. OBSERVATIONAL COMPARISON

So far we have seen that the properties of the ISM play a strong role in determining the structure of the disk. We have, however, seen some evidence that a universal PDF might apply to all disks, which could allow the observational properties to be largely independent of the gas structure. This section focuses on star formation in our galaxies and compares the results with the main observational relations.

5.1. Star Formation History

Initially, we turn to the star formation history to examine the rate at which stars are forming over the course of our simulations. This is shown in Figure 14, whose three panels depict the evolution of our three ISM types over the course of the simulation. In all cases, the curves follow the same pattern as in TB06; the first 50 Myr see a sudden starburst as the disk becomes gravitationally unstable and starts to collapse. The SFR then peaks and falls off roughly exponentially as gas is used up in the disk.

Considering first the top plot, showing disks with ISM 1, we see that the runs without feedback have a steadily decreasing SFR over the majority of the simulation. In the last 200 Myr, the simulation with D-type star formation starts to show signs of reaching a constant value, evening out at roughly $1 \, M_\odot \, {\text{yr}}^{-1}$. The C-type run (C) by contrast, heads to zero star formation, and in both these cases the gas content is significantly depleted, as we see in Figure 8. The timescale for this is significantly less than for present-day spirals, as was also found in the lighter disk runs of this type in TB06, although, of course, our initial conditions do not provide an accurate cosmological starting point, so this is hard to judge. The simulations that include feedback, however, reach a steady SFR at around 600 Myr, resulting in a higher SFR by 1.3 Gyr than for the nonfeedback runs. This result shows that feedback is causing the star formation to become self-regulated, which agrees well with the images of the disks in §3.1, where feedback results the destruction of cold clumps of gas. At the end of the run, the feedback simulations have a constant SFR of around $10 \, M_\odot \, {\text{yr}}^{-1}$, which is high compared to the Milky Way, whose SFR is roughly $1 \, M_\odot \, {\text{yr}}^{-1}$.

The effect of adding background heating in ISM 2 causes an overall suppression of the SFR. In the second panel we can see that the lines are much closer together; the nonfeedback runs HC and HD having only a slightly lower SFR after 1 Gyr than the feedback cases. The background heating therefore acts in a similar way to the feedback, suppressing the formation of the cold clumps of matter that form stars. This is again consistent with Figure 2, where the filamentary structure of the gas was notably less than in Figure 1. Feedback acts to suppress star formation even more, with the lines corresponding to HCDBCK and HDDBCK lying above HC and HD, although the overall difference is smaller. The two sets of feedback runs in ISM 1 and ISM 2 show very similar evolution. At the end of the simulation, all the heated runs have a SFR between 1 and $10 \, M_\odot \, {\text{yr}}^{-1}$.

The two isothermal runs are shown in the bottom panel of Figure 14. There is a small distinction between the C- and D-type star formation evolution, and, contrary to the other simulations, the C-type star formation is generally higher than the D. This discrepancy is likely to be due to the C-type stars forming in the larger gas clumps than in the previous ISM models, due to the increased Jeans length, mimicking a behavior closer to the D-type star formation. The SFRs reach a roughly constant value after about 800 Myr, giving an end rate of $1 \, M_\odot \, {\text{yr}}^{-1}$, close to what we see for the heated cases, HC and HD, and in good agreement with the Milky Way.

5.2. The Star Formation Cutoff

The gravitational collapse of gas into cold knots of matter is the fundamental driving force of star formation in our galaxies (this issue is discussed more thoroughly in TB06 and references therein). Previous studies, both theoretical and observational, suggest that at a given radius, the density of the gas drops below a certain critical value and the disk becomes stable, preventing star formation from occurring beyond this point. Toomre (Toomre 1964) initially defined the location of this radius in terms of a stability parameter, $Q$, given by $Q = \frac{\kappa c_s}{\pi G \Sigma_g}$, where $\kappa$ is the usual epicyclic frequency, $c_s$ is the thermal sound speed as measured in the disk, and $\Sigma_g$ is the gas surface density. Toomre's

![Fig. 13. — Two-dimensional contour plots for the volume-weighted gas in the runs marked above. Plots are taken at 377 Myr. [See the electronic edition of the Journal for a color version of this figure.]](image-url)
calculations considered axisymmetric perturbations in a single-phase 2D disk which was found to become gravitationally unstable (and therefore able to form stars) when $Q < 1$. Goldreich & Lynden-Bell (1965) recalculated this value for a 3D disk to $Q < 0.67$. Observational results have also observed this star formation cutoff, with Kennicutt (1989) measuring the star formation threshold in spiral galaxies to correspond to a $Q$-value of 1.5. Observations did not allow measurement of the actual thermal sound speed of the gas, which was replaced by a velocity dispersion of 6 km s$^{-1}$.

In our disks we measured both the radial cutoff point for star formation and the Toomre $Q$ parameter for the disk’s gas at that radius. We also calculated an observed $Q$-value, whereby we adopt Kennicutt’s value of 6 km s$^{-1}$ instead of the thermal sound speed. It is worth noting, however, that these calculations were not entirely simple. The greater gas mass and smaller star particle size results in a significantly greater gravitational scatter of stars near the edge of the stellar disk than we had in TB06, so the exact edge of star formation is hard to judge. (This is, of course, true of the observational result as well, a point we return to in the next section.) We therefore take the radius where 99% of the star particles are enclosed as the stellar cutoff. The measuring of $Q$ in a multiphase disk is an even harder task to perform accurately. First, in averaging over an annulus at a given radius, a wide range of temperatures and densities is included, which produce an average $Q$, not necessary the $Q$-value at the star formation sites. Second, Toomre’s original calculations assumed linear perturbations that break down at the point of star formation. Ideally, therefore, one wants to measure the $Q$-value where the disk has become gravitationally unstable but has not yet formed stars. In TB06, such a point existed, but with our heavier disk and smaller star particles, the disk begins to form stars earlier on. We therefore measure $Q$ at the same time as in TB06, approximately 50 Myr after the start of the simulation, and note that while the disk has fragmented, stars have already started to form.

What is surprising is that we measure only a small range of values for both the cutoff radius and $Q$, as shown in Table 2. In all cases the star formation ends at a comparable radius to that in the Milky Way, which is estimated to be around 15 kpc. Within the range we do see some patterns. For the nonfeedback cases, the C-type star formation simulations form stars out to a radius several kiloparsecs greater than the D type, something we see visually in Figures 1 and 2. The reason for this is the D-type star formation’s higher density threshold, which confines stars to regions where the gas has collapsed to form the dense knots of matter. Our C-type star formation, however, can occur at much lower densities, when the gas has not fully collapsed. The exception to this is the isothermal gas, where, as previously mentioned, the larger Jeans...
length confines the C-type stars to the same region as the D type. The addition of feedback has a different effect on the two star formation types. For the C type it reduces the threshold radius, whereas for the D type the radius for star formation increases. This difference is caused by the nature of the resulting outflows from the feedback. As we see in Figure 4, feedback from C-type stars produces a smooth, continuous outflow that disrupts the dense gas and prevents stars from forming. Feedback from the D-type stars, however, comes in energetic bursts, which, as we see in Figure 5, extends the gas outflows to much higher radii. These outflows of gas can then cool and condense, fragmenting beyond the old instability threshold to push star formation out to higher radii.

A slightly surprising result is that the heated disks have higher threshold radii than we see in the nonheated cases. Since the heating has a stabilizing effect on the disk (as seen in Fig. 14) we would expect it to quench star formation in the less dense outer disk. We actually see in Figure 1 that the instabilities do extend out farther in the DC and DD case than in HDC and HDD, but the star-forming knots stop at a lower radius. This appears to be the result of the dissipation of the circular wave that we noted occurred in DC in § 3.1. As mentioned above, however, the exact cause of the dissipation is unclear.

If we look at what \( Q \) parameter this cutoff corresponds to, we find values around 1. Given that \( Q \) itself varies over several orders of magnitude, the results are very uniform, with neither ISM conditions, feedback, nor star formation type having a large effect. The only value that appears out of place is for run HDC, with \( Q = 3.49 \). Given the range of \( Q \) over the disk, this value is still in keeping with the other simulations, although its higher value may be due to problems involved in accurately measuring the star formation cutoff.

Coupled with the lower star formation cutoff, disks without heating in ISM 1 have lower \( Q \) values than the ISM 2 and ISM 3 disks. Feedback and star formation type have little effect on these values, which are all below 1. ISM 2 shows the most sensitivity to stellar conditions, with the C-type star formation in particular being more sensitive to the introduction of feedback than the D type. The isothermal ISM 3 simulations show almost no variation with star formation type. For comparison, the third column in Table 2 shows the observationally calculated \( Q \) parameter. The values are reassuringly similar to the first calculation of \( Q \), although we can see that for ISM 1, the \( 6 \, \text{km s}^{-1} \) is an overestimate of the thermal sound speed, since it raises the value of \( Q \), whereas in the other cases it is an underestimate.

### Table 2

| Simulation   | Cutoff Radius (kpc) | Toomre \( Q \) | Observed \( Q \) |
|--------------|---------------------|----------------|-----------------|
| C            | 13.3                | 0.40           | 0.82            |
| D            | 11.4                | 0.26           | 0.54            |
| CFDBCK       | 10.7                | 0.30           | 0.47            |
| DFDBCK       | 12.4                | 0.28           | 0.58            |
| HC           | 17.8                | 6.41           | 3.49            |
| HD           | 13.8                | 0.95           | 0.81            |
| HCDFDBCK     | 13.6                | 1.02           | 0.86            |
| HDFDFBCK     | 15.0                | 1.45           | 1.07            |
| HDHires      | 16.1                | 1.78           | 1.20            |
| IC           | 12.2                | 1.83           | 0.72            |
| ID           | 12.4                | 1.91           | 0.76            |
| IDJEANS      | 12.9                | 1.87           | 0.74            |

5.3. The Global Star Formation Relation

Kennicutt’s observations of disk galaxies show that the surface SFR is linked, both on a global and local scale, to the surface gas density via \( \Sigma_{\text{SF}} \propto \Sigma_{\text{gas}}^{1.5} \). In Figure 15 we show Kennicutt’s observational relation (solid line) and the results from our different simulations for the global version of this law (global Schmidt law), which gives the average surface SFR and the average gas surface density over the whole disk for different (evenly spaced) times over the 1.4 Gyr of the simulation.

Overall, the majority of the simulations reproduce the 1.5 gradient well, although all overestimate the SFR. The possible exception to this is the isothermal run with D-type star formation (IDD), whose points contain a large amount of scatter and a steep decline at a gas density of \( 10^3 \, M_\odot \, \text{pc}^{-2} \).

The overestimate in the SFR was discussed in TB06 and is likely due, at least in part, to our inability to include all the physics at the resolution of the giant molecular clouds. Without the added destructive effects of ionizing radiation and stellar winds, these clouds lifetimes will be prolonged, allowing an unphysically high proportion of their gas to be converted into stars. The other possibility is that neither of our star formation mechanisms is very accurate. A certain amount of inaccuracy is inevitable, since we do not resolve the GMCs. But recent work in this area (Krumholz & Tan 2007) suggests that while star formation occurs in the dense molecular clouds, on scales larger than a few parsecs the star formation efficiency is much lower than the 50% suggested by Lada & Lada (2003), possibly as low as 2%. This reduced efficiency will be explored in future papers.

As in TB06, we find that the addition of feedback does act to reduce the SFR, confirming that we are seeing at least the beginning of self-regulation. This effect is most evident in the simulations with C-type star formation (C, CFDBCK, HC, and HCDFDBCK), all of which lie close together on the graph. Simulations with D-type star formation also follow the observed gradient well, especially in the nonheated simulations, D and DFDBCK. This is important, since, as discussed in TB06, the C-type star formation has a Schmidt-like behavior built into it, implying that we are simply getting out what we put in. However, the same is not true for the D-type algorithm, which has a simple density cutoff and is otherwise proportional to the density.

As hinted at with the PDFs in Figure 8, the background heating in ISM 2 has a stronger effect on the HD simulation than on HC, as the higher density regions required for this type of star formation are disrupted by the increase in temperature. This results in the star formation at low densities in HD being significantly reduced in comparison to D. At these low densities the results from HD now follow the observations very closely, but at higher densities the star formation rises above what is expected. This difference suggests that the background heating has less effect at the higher densities, where the gas is collapsing despite the extra resistance. Introducing feedback reduces this effect; while still producing an overestimate of the star formation, the results are now consistent with HCDFDBCK, CFDBCK, and DFDBCK, implying that feedback is the dominant effect here.

The isothermal runs show the poorest agreement with observation here. The C-type star formation (IDC) produces a gradient slightly steeper than 1.5 for gas densities greater than around \( 6 \, M_\odot \, \text{pc}^{-2} \) but has a large scatter below that.

5.4. The Local Star Formation Relation

The Schmidt law can also be looked at on a local scale at which the values are plotted as a function of disk radii rather than time. Figure 16 shows the results for each of the simulations, in
which each point represents a different radii in the disk. The solid line has a gradient of 1.5, in agreement with the observations, but with an arbitrary normalization.

In the top row, where we show the simulations with ISM 1, we can see that runs with D-type star formation (D and DFDBCK) represent the observed gradient of the correlation between the surface gas density and SFR extremely well. Runs with C-type star formation do a reasonable job at high densities, showing a larger degree of scatter than the D-type star formation runs due to clumps being split by energy injection and gravitational interactions and reforming (something that is not observed in the D-type run due to the higher binding energy of the dense knots). At lower densities the feedback run (CFDBCK) does a noticeably poorer job at reproducing the Schmidt law, showing a sharp decrease in the SFR below gas densities of around \(2 \, M_\odot \, pc^{-2} \), a feature that is not seen in the D-type runs, which are not affected by the introduction of feedback. This feature is not seen when we introduce background heating in ISM 2 (middle row), where all simulations follow the observations very well, although there is again noticeably more scatter in the C-type run with feedback than in either the run without feedback or in the D-type simulations HD and HDFDBCK.

The isothermal run with D-type star formation follows the same pattern, and indeed there is no difference between the D, HD, and ID simulations, showing that the D-type star formation is much less influenced by its interstellar environment. The isothermal run with C stars, however, does not follow the observations well, producing a gradient that is much steeper than observed and thereby underestimating star formation at low densities and overestimating it at high densities. Overall, the range in gas densities is much less than in other C-type runs, in agreement with the results in § 3.1, that star formation is confined to a small section of the disk.

In both the global and local Schmidt-law plots, the C-type star formation extends to much lower densities than the D-type. Although this is not surprising, since the density threshold of the C type is lower, it is interesting to compare this finding to observations. As mentioned in the previous section, Kennicutt (1989) observed a sharp cutoff in the star formation in disk galaxies below a critical density. More recent observations done using the
UV data in GALEX (Boissier et al. 2006) suggest that this star formation cutoff might be a result of the observational technique, rather than the existence of a critical density. Boissier et al. (2006) looked at 46 spiral galaxies in the UV to establish where star formation ended. Previous work had been performed by examining the Hα/C11 emission from galaxies, a technique, this group argues, that makes it very difficult to observe low levels of star formation. With UV spectra, they found evidence of star formation beyond the position of the previously measured cutoff radius, suggesting that the critical density value is either lower than originally measured or possibly does not actually exist. If this is the case, then our C-type star formation is preferable in this result, since it allows star formation to occur at much lower densities, in agreement with this new result.

6. DISCUSSION

What role does the interstellar medium play in determining the star formation properties of galaxies? This question has two important consequences. The first concerns the nature of galaxy evolution, asking whether the interstellar environment can result in dramatically different structure and star formation properties.

The second consequence applies to our ability to model galaxy formation realistically or whether parsec resolution is needed to achieve accurate results.

In § 3 we visually examined projections of the galaxy disks looking at their density, temperature and pressure distributions and their star formation. Clear differences were seen between our disks, with ISM type, star formation algorithm and feedback all playing significant roles. The growth of perturbations in the disk was dominated by the conditions in the ISM. In our first ISM type, which contained only cooling, we saw the disk fragment through the production of a outgoing circular wave which collapsed tangentially to form the network of filaments and dense knots of gas we see in Figure 1. The addition of background heating in ISM 2, suppressed the formation of the weaker filaments but increased the size of the densest knots which extended further out into the disk. In our third, isothermal, ISM type, the filamentary structure was also suppressed and the size of the dense knots increased still more, confining their formation to the central region of the disk.

These differences made a difference when star formation started to occur. In our C-type (cosmological) algorithm, stars formed...
over a large fraction of the disk’s surface, although the largest clusters were confined to the densest knots of gas. In the heated case, the heavier filaments formed edges around voids of low density, hot gas that had occurred through gravitational and thermal instability alone. Such voids are reminiscent of porous ISMs seen in the H i maps of some dwarf galaxies. In ISM 1 further fragmentation had prevented this from occurring. The isothermal disk confined the stars to the central disk region where the large knots formed and the resulting heavier clusters scattered the smaller ones out of the disk. The extent of this scattering was extreme, and care should be taken if an isothermal model is used with this star formation recipe to avoid unphysical results. The effect in ISM 3 of confining the star formation to the central region meant that there was little difference between the C-type algorithm and the D-type star formation algorithm where we restricted the formation of stars to the densest clouds. This was investigated quantitatively in § 5.2 where we measured the star formation cutoff radius and compared it to the Toomre stability criterion \( Q \) at that point. In the ISM 3 case, the cutoff radius was almost identical in both the C- and D-type star formation routines whereas in ISM 1 and ISM 2, the C-type stars extended further into the disk. The \( Q \) stability criteria itself was found to be around 1, in good agreement with both analytical and observational results.

This changed again when we included feedback. In both the ISM 1 and ISM 2 cases, feedback destroyed the dense knots of gas, suppressing the star formation as we see in Figure 14. Its addition largely wipes out the structural differences between the two ISM types and their profiles, both in the projections and the vertical profiles in Figures 6 and 7 follow similar shapes. Feedback also causes gas to be ejected from the disk’s surface in a galactic fountain, something the isothermal disk is incapable of replicating. The different star formation algorithms have a much larger effect on the feedback than ISM type. The D-type algorithm, confining the star formation to the densest knots, focuses the energy injection from the feedback, causing the outflows to be bursts in different areas of the disk. The C-type, by contrast, acts equally across the disk and at a more continuous level. This has two effects on the disk. The first was seen in Figure 4 where the outflows from the disk’s surface are uneven. The second is seen in the star formation cutoff, where the feedback in the D-type case triggers fragmentation of the gas in the stable regions of the disk, extending the star formation threshold.

Section 4 further examines the ISM by looking at the evolution of its density and temperature over time. We see that background heating stabilizes a significant proportion of the gas in the warm phase in Figure 11, bringing it nearer to the isothermal state as can be seen in the 2D contour plots in Figure 13. This could explain the success of models using an isothermal ISM; it is a gross simplification of the real system, but if a single phase becomes stabilized in the disk, an isothermal gas can be a good approximation. The addition of feedback, however, dramatically increases the gas volume in the hot phase causing the heated and nonheated disks to show a wide variety of continuous phases. Both ISM 1 and ISM 2 produce disks that are largely isobaric, in keeping with analytical expectations. The addition of feedback acts as a pressure value to eject gas from the disk, ensuring the disk remains isobaric across its height. The isothermal disk, by contrast, has strong pressure variability since the fixed temperature means that the pressure has to reflect the density distribution.

In § 5 we turned to look at the observable properties of our disks, including star formation history, cutoff, and the relation between gas surface density and surface SFR (Schmidt laws). No one model produces these results significantly better than any other—a result that implies, despite structural differences, that global star formation is not strongly dependent on the interstellar environment. The disks overall produce the observed properties reasonably well, having a star formation threshold of between 11–18 kpc, in agreement with estimations for the Milky Way and producing the Schmidt observed gradient of 1.5. The slight exception to this were the isothermal cases which reproduced the observational result poorly at low densities. Of the two star formation algorithms, each has its own strengths and weaknesses. The C-type algorithm allows the extension of the Schmidt law to much lower densities, where recent observational evidence suggests there is star formation. However, the small stellar clusters gravitationally interact to be scattered in the disk, making it more difficult to determine the cutoff density for star formation and increasing the scatter in the local Schmidt relation. The D-type algorithm, meanwhile, show a tight correlation in the local Schmidt relation but appears to reproduce the gradient of the global relation less well. However, it is also the least affected by ISM type, since it considers only the densest gas structures. Possibly a hybrid of these two schemes would combine their strengths to produce the best results.

As mentioned in § 2.1, we performed an additional run with a higher background heating source. This run was identical to the HD, but with the background heating increased by a factor of 30. The main difference the additional heating had on the disk was to increase the pressure of the ISM. This occurred because the enhanced heating rate moved the gas in thermal equilibrium to higher temperature at fixed density, pushing the contours shown in Figure 13 to the right and up. This can be seen in Figure 17. The effect this has on the star formation, however, was fairly minimal. There was a slightly increased SFR at early times which led to a greater gas depletion near the end of the simulation. This resulted in the global Schmidt law following a relation identical to that seen in the HD run, but a slightly raised SFR.

Ultimately, H i images of the whirlpool galaxy and LMC tell us that the ISM plays an important role in the galaxy’s evolution and it must be born in mind that while we are able to resolve a multiphase structure in our ISM, we are no yet at the detail of the small-box simulations. However, the uniformity of our results...
for the star formation history and Schmidt laws suggest that the exact details of the gas may be simplified and still achieve a correct star formation production.

7. CONCLUSIONS

We performed high-resolution simulations of global disk galaxies with three different interstellar medium properties: our first model allowed radiative cooling of gas, and the second model allowed radiative cooling and included a background heating term, while the third model held the gas at a constant temperature. For each of these ISM models, we considered two different star formation mechanisms; a “C” type that allowed low-density formation of stars at a correspondingly low efficiency and a “D” type that only allowed star formation in the densest clumps, but with a high efficiency. We also investigated the addition of feedback from Type II supernovae for nonisothermal disks. Overall, our findings are as follows:

1. The structure of the disk is strongly affected by the ISM environment. Background heating suppresses small-scale perturbations and increases the size of the star-forming knots. This, in turn, helps to regulate star formation and reduce gas depletion in the disk. The isothermal equation of state increases the Jeans length in the disk and leads to the formation of much larger clumps (probably unphysically large) which results in extreme gravitational scattering of nearby star particles. It also confines star formation to the central region, regardless of the critical density specified in the star formation routine. This leads to gas depletion in the disk center.

2. The addition of feedback destroys star-forming clumps and causes gas to be ejected off the disk’s surface. The nature of the outflows depends on the star formation algorithm with the low threshold density, with the C-type routine producing a more continuous flow compared to the D-type strong intermediate bursts. Both cases result in star formation being suppressed in the disk as dense knots of gas are destroyed; but the feedback in the D-type case results in triggered star formation in the outer regions of the disk.

3. The structure of the ISM in both ISM 1 and ISM 2 shows a continuous range of densities and temperatures that are not well represented by a single-phase model. The addition of heating reduces the range of values found in the nonfeedback case, in particular stabilizing the warm phase at the same temperature as the isothermal ISM. However, the introduction of feedback significantly increases the range of densities and temperatures, almost eliminating the signature of background heating.

4. The PDFs for all disks are well represented by a lognormal curve over several orders of magnitude. This fit is largely insensitive to the introduction of stellar feedback or ISM environment. At later times (and for the isothermal run at earlier times) a power-law fit would also be possible, and it is hard to tell, at current resolutions, which of these two fits would work best.

5. The star formation in the disks are shown to cut off at a radius comparable to the Milky Way when the Toomre Q parameter is around 1. Exact measurements are difficult to achieve in a multiphase medium.

6. All simulations reproduce the slope of the observed relation between star formation and gas surface density well on both the global and local scale. The possible exception is the isothermal run with C-type star formation, which shows a steeper drop off in SFR on local scales. There is some evidence that D-type star formation does not produce the gradient as well as C-type on global scales and that its low-density cutoff may be higher than suggested by recent observations.

Overall, we conclude that the interstellar medium is a multiphase environment strongly affected by background heating, feedback, and cooling and that it plays a significant part in the disk’s structural evolution. It appears, however, from these preliminary calculations that its exact structure can be simplified and still achieve the correct star formation properties for disk galaxies. The exception to this is possibly the isothermal disk, which did not produce a realistic multiphase model, lead to very large clump formation, and can never produce a galactic fountain effect.

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