We consider the factorization properties of on-shell QCD amplitudes with massive partons in the limit when all kinematical invariants are large compared to the parton mass and discuss the structure of their infrared singularities. The dimensionally regulated soft poles and the large collinear logarithms of the parton masses exponentiate to all orders. Based on this factorization a simple relation between massless and massive scattering amplitudes in gauge theories can be established. We present recent applications of this relation for the calculation of the two-loop virtual QCD corrections to the hadro-production of heavy quarks.
1. Introduction

Amplitudes for hard scattering processes in Quantum Chromodynamics (QCD) are of basic importance both for theory and phenomenology and precision predictions for them must include higher-order quantum corrections. An important aspect in explicit computations are the singular limits of amplitudes at higher loops. Here, one has to consider two types of limits, soft and collinear, related to the emission of gluons with vanishing energy and to collinear parton radiation off massless hard partons, respectively.

For massless QCD amplitudes the corresponding singularities are regularized by working in $d$ dimensions and appear as explicit poles in $(d - 4)$. Typically two powers in $1=(d - 4)$ are generated per loop. When massive particles are involved, some of the collinear singularities are screened by the parton masses, which gives rise to large logarithmically enhanced contributions. In both cases the structure of the singularities can be understood from the factorization property of QCD and it can be predicted to all orders based on a small number of perturbatively calculable anomalous dimensions. Moreover, factorization gives rise to an extremely simple universal multiplicative relation between a massless amplitude and its massive version in the limit when the parton masses are small with respect to all other kinematical invariants. This relation can be employed to derive virtual QCD corrections at higher loops including all logarithms in the heavy quark mass as well as all constant (mass-independent) contributions. We demonstrate the predictive power of factorization with recent results for the two-loop QCD amplitudes for heavy-quark production in hadronic collisions.

2. Factorization of QCD amplitudes

We are interested in general $2^n$ scattering processes of partons $p_i$

$$p : p_1 + p_2 \cdots p_3 + \ldots + p_n \not\to p$$

(2.1)
The corresponding scattering amplitude \( \mathcal{M}_p \) depends on the set of fixed external momenta \( \ell k_{i g}, \) masses \( m_{i g} \) and color quantum numbers \( c_{i g}, \)

\[
\mathcal{M}_p \left( \ell k_{i g}; m_{i g}; c_{i g}; \right) \frac{Q^2}{\mu^2} \alpha_s (\mu^2) \varepsilon \ ;
\]

(2.2)
as well as on the strong coupling constant \( \alpha_s \), the renormalization scale \( \mu \) and the parameter \( \varepsilon \) of dimensional regularization, \( d = 4 - 2\varepsilon \). Also, we denote explicitly the hard scale \( Q \) of the process typically related to the center-of-mass energy, e.g. \( Q = \sqrt{s} \) with \( s = (k_1 + k_2)^2 \).

Let us briefly recall the factorization of on-shell amplitudes for massless partonic processes [1, 2]. In \( d \)-dimensions we can write Eq. (2.2) as a product of functions \( \mathcal{J}_p^{(m=0)}, \mathcal{J}_p^{(m=0)} \) and \( \mathcal{H}_P \),

\[
\mathcal{M}_p \left( \ell k_{i g}; m_{i g}; c_{i g}; \right) \frac{Q^2}{\mu^2} \alpha_s (\mu^2) \varepsilon \ ;
\]

(2.3)
where we use matrix notation suppressing the color indices. The jet function \( \mathcal{J}_p^{(m=0)} \) depends only on the external partons. It collects all collinearly sensitive contributions and is color-diagonal. Coherent soft radiation arising from the overall color flow is summarized by the soft function \( S_i^{(m=0)} \), which is a matrix in color space. The short-distance dynamics of the hard scattering is described by the (infrared finite) hard function \( H_p \), which to leading order is simply proportional to the Born amplitude.

The factorization formula (2.3) organizes the singularity structure of any massless QCD amplitude. From the operator definitions for the functions \( \mathcal{J}_p^{(m=0)} \) and \( \mathcal{J}_p^{(m=0)} \) and the corresponding renormalization group properties one derives evolution equations. The solution of the latter gives rise to an all-order exponentiation in terms of well-known anomalous dimensions. As an upshot, all \( 1=\varepsilon \) terms related to the emission of gluons with vanishing energy and to collinear parton radiation off massless hard partons, respectively, exponentiate to all orders in perturbation theory, see e.g. [2,3].

Most important for our considerations is the jet function, which contains all collinear contributions from the external partons. It is therefore of the form

\[
\mathcal{J}_p^{(m=0)} = \prod_{i \neq g} \mathcal{J}_i^{(m=0)} \mathcal{J}_g^{(m=0)} = \prod_{i \neq g} \mathcal{J}_i^{(m=0)} \frac{1}{2} ;
\]

(2.4)
where \( i = q, g \) for quarks and gluons. \( \mathcal{J}_i^{(m=0)} \) is the individual jet function of each external parton, which by definition, one identifies with the (gauge invariant) form factor of a quark or a gluon, \( \mathcal{F}_i^{(m=0)} \). Of course, the latter function is well-known in QCD, see e.g. [4,5].

When masses are introduced the picture described above gets modified. However, the basic factorization of the QCD amplitude in jet, soft and hard function from Eq. (2.3) can be retained. With the exception of contributions related to heavy quark loops (see below) in the presence of a hard scale \( Q \) we can write for the partonic process (2.1)

\[
\mathcal{M}_p \left( \ell k_{i g}; m_{i g}; c_{i g}; \right) \frac{Q^2}{\mu^2} \alpha_s (\mu^2) \varepsilon \ ;
\]

(2.5)
where all non-trivial mass dependence enters in the functions \( \mathcal{J}_p^{(m)} \) and \( \mathcal{J}_p^{(m)} \), while power suppressed terms in the parton masses are neglected in \( \mathcal{H}_P \). The jet function for massive partons can
be defined in complete analogy to Eq. (2.4), i.e. we identify \( \mathcal{F}^{(m)}_{ij} \) with the massive form factor \( \mathcal{F}^{(m)}_{ij} \). This guarantees exponentiation with largely the same anomalous dimensions as in the massless case. Also the soft anomalous dimensions which govern the soft function have a smooth limit for vanishing parton masses.

In summary, from comparison of Eqs. (2.3) and (2.5) one can deduce a remarkably simple relation between a massless and a massive amplitude in the small-mass limit. Thus, QCD factorization provides us with [6]

\[
\mathcal{M}_p^{(m)} = \prod_{i=1}^2 \frac{Z^{(m)0}_{[i]} \, \mu^2 \, \alpha_s \, \varepsilon}{\mu_0^2 \, \alpha_s \, \varepsilon} \cdot \mathcal{M}_p^{(m=0)}; \tag{2.6}
\]

where we have again suppressed the color indices. \( \mathcal{M}_p^{(m=0)} \) and the corresponding massive amplitude \( \mathcal{M}_p^{(m)} \) in the small mass limit \( m^2 \gg Q^2 \) are multiplicatively related by a universal process independent function \( Z^{(m)0}_{[i]} \). With the definitions for the jet functions in Eq. (2.4), it is directly given in terms of the respective form factors,

\[
Z^{(m)0}_{[i]} = \frac{m^2}{\mu^2} \, \alpha_s \, \varepsilon = \frac{Q^2}{\mu^2} \frac{m^2}{\mu^2} \, \alpha_s \, \varepsilon \cdot \mathcal{F}^{(m=0)}_{ij} \frac{Q^2}{\mu^2} \, \alpha_s \, \varepsilon; \tag{2.7}
\]

where the index \( i \) denotes the (massive) parton and \( \alpha_s = \alpha_s(\mu^2) \). The process-independence is manifest in Eq. (2.7), because \( Z^{(m=0)}_{[i]} \) is only a function of the (process-independent) ratio of scales \( \mu^2 = m^2 \). The (process-dependent) scale \( Q \) cancels completely between the massive and the massless form factors.

Eq. (2.6) can be used to predict any massive amplitude from the known massless one, which is a great advantage in practice, as the latter is much easier to compute. Moreover, Eq. (2.6) includes not only the singular terms and the logarithms in the massive amplitude but extends even to the mass-independent constant contributions. However, there is one important side condition on Eqs. (2.6) and (2.7), concerning all terms proportional to the number of heavy quarks \( n_h \). These two-loop contributions are excluded explicitly from the definition of \( Z^{(m)0}_{[i]} \). In order to incorporate them additional process dependent terms appear as has been shown e.g. in QED for Bhabha scattering [7].

3. Hadro-production of heavy quarks

As an application of the formalism developed, we consider the pair-production of heavy quarks in the \( q\bar{q} \)-annihilation and the gluon fusion channel,

\[
\begin{align*}
q &: \quad g(k_1) + g(k_2) & Q(k_3) m + Q(k_4) m; \\
g &: \quad g(k_1) + g(k_2) & Q(k_3) m + Q(k_4) m;
\end{align*}
\tag{3.1}
\]

where \( k_i \) denote the on-shell parton momenta and \( m \) the mass of the heavy quark, thus \( k_1^2 = k_2^2 = 0 \) and \( k_3^2 = k_4^2 = m^2 \). Energy-momentum conservation implies \( k_1^\mu + k_2^\mu = k_3^\mu + k_4^\mu \) and we consider the scattering amplitude for the processes (3.1) in QCD perturbation theory,

\[
\tilde{\mathcal{M}}^{(1)}_p = 4\pi \alpha_s \tilde{\mathcal{M}}^{(0)}_p + \frac{\alpha_s}{2\pi} \tilde{\mathcal{M}}^{(1)}_p + \frac{\alpha_s}{2\pi} \tilde{\mathcal{M}}^{(2)}_p + \mathcal{O}(\alpha_s^3); \tag{3.2}
\]
which defines the series expansion in the strong coupling $\alpha_s = \alpha_s (\mu^2)$ and $\mu$ is the renormalization scale. As usual the $\overline{\text{MS}}$-scheme for the coupling constant renormalization is employed and the mass $m$ is taken to be the pole mass.

It is convenient to define the function $\mathcal{A}_p (\varepsilon \, p m \not\! q \not\! \mu)$ for the squared amplitudes summed over spins and colors as

$$\sum_{\frac{1}{2}} \mathcal{A}_p \left( \varepsilon \, p m \not\! q \not\! \mu \right) = \mathcal{A}_p (\varepsilon \, p m \not\! q \not\! \mu); \quad p = q \not\! \mu : \quad (3.3)$$

$\mathcal{A}_p$ is a function of the Mandelstam variables $s$, $t$, and $u$ given by

$$s = (p_1 + p_2)^2; \quad t = (p_1 - p_3)^2 \not\! m^2; \quad u = (p_1 - p_4)^2 \not\! m^2; \quad (3.4)$$

and has a perturbative expansion similar to Eq. (3.2).

In terms of the amplitudes the expansion coefficients in Eq. (3.5) may be expressed as

$$\mathcal{A}_p^{4 \text{gon}} (\varepsilon \, p m \not\! q \not\! \mu) = 16\pi^2 \beta_0^2 \mathcal{A}_p^{4 \text{gon}} + \frac{\alpha_s}{2\pi} \mathcal{A}_p^{6 \text{gon}} + \frac{\alpha_s}{2\pi} \mathcal{A}_p^{8 \text{gon}} + \mathcal{O} (\alpha_s^3); \quad (3.5)$$

where the results for $\mathcal{A}_p^{6 \text{gon}}$ have been presented e.g. in [8, 9] and the so-called loop-by-loop contribution in $\mathcal{A}_p^{8 \text{gon}}$ can be found in [10], both results with the complete dependence on the heavy-quark mass. The new contribution is the real part of the series expansion in the strong coupling constant $\alpha_s$.

In order to obtain $\mathcal{A}_p^{6 \text{gon}}$ from Eq. (3.6), we have to construct the appropriate functions $Z^{(m g)}_{\not\! Q}$ from the on-shell heavy-quark form factor and the massless on-shell ones, all results being known [4, 5, 12, 13] to sufficient orders in $\alpha_s$ and powers of $\varepsilon$. An explicit expression for

$$Z^{(m g)}_{\not\! Q} = 1 + \frac{\alpha_s}{2\pi} Z^{(1)}_{\not\! Q} + \frac{\alpha_s}{2\pi} \mathcal{O} (\alpha_s^3); \quad (3.9)$$

up to two loops is known [6]. As mentioned above, the definition (3.9) accounts in particular for all fermionic terms except for those linear in $n_h$. The leading $n_f$ terms $\mathcal{O} (\alpha_s)$ for the process $g g \not\! Q \not\! \bar{Q}$ in Eq. (3.1) can also be predicted, where we denote the total number of flavors with $n_f$, which is the sum of $n_l$ light and $n_h$ heavy quarks. Keeping only terms quadratic in $n_h$ and/or $n_f = n_l + n_h$ one has up to two loops,

$$Z^{(m g)}_{\not\! g} = 1 + \frac{\alpha_s}{2\pi} Z^{(1)}_{\not\! g} + \frac{\alpha_s}{2\pi} \mathcal{O} (\alpha_s^3); \quad (3.10)$$

where

$$Z^{(1)}_{\not\! g} = Z^{(1)}_{\not\! g} + \frac{2}{3\varepsilon} \eta_{T \mu} Z^{(1)}_{\not\! g} \not\! \mu \not\! \eta_0 + \mathcal{O} (\alpha_s^3); \quad (3.11)$$

with $Z^{(1)}_{\not\! g}$ known from [6, 12]. Note that $Z^{(1)}_{\not\! g}$ is also equal to the $\mathcal{O} (\alpha_s)$ term in the gluon wave function renormalization constant $Z_3$. 

Massive QCD amplitudes at higher orders
S. Moch
Exploiting the predictive power of the relation Eq. (2.6) and applying it to the processes (3.1) we get

\[ 2\text{Re} \bar{\mathcal{M}}_q^{(0)} \cdot \mathcal{M}_q^{(2)} \right|_{m=0} = 2\text{Re} \bar{\mathcal{M}}_g^{(0)} \cdot \mathcal{M}_g^{(2)} \right|_{m=0} \]

(3.12)

\[ + Z_q^{(1)} \mathcal{M}_q^{(4)} \right|_{m=0} + 2 Z_q^{(2)} \mathcal{A}_q^{(4)} \right|_{m=0} + \mathcal{O}(n_h^{-1} \eta^0) + \mathcal{O}(m); \]

\[ 2\text{Re} \bar{\mathcal{M}}_g^{(0)} \cdot \mathcal{M}_g^{(2)} \right|_{m=0} = 2\text{Re} \bar{\mathcal{M}}_g^{(0)} \cdot \mathcal{M}_g^{(2)} \right|_{m=0} \]

(3.13)

\[ + Z_g^{(1)} \mathcal{Q}_g^{(4)} \right|_{m=0} + 2 Z_g^{(2)} \mathcal{A}_g^{(4)} \right|_{m=0} + \mathcal{O}(n_h^{-1} \eta^0) + \mathcal{O}(m); \]

which assumes the hierarchy of scales \( m^2 \gg m, \) i.e. we neglect terms \( \mathcal{O}(m). \) Eqs. (3.12) and (3.13) predict the complete real part of the squared amplitudes \( \bar{\mathcal{M}}_q^{(0)} \cdot \mathcal{M}_q^{(2)} \right|_{m=0} \) except as indicated for those terms, which are linear in \( n_h. \) The real part of the two-loop massless amplitudes \( \bar{\mathcal{M}}_q^{(0)} \cdot \mathcal{M}_q^{(2)} \right|_{m=0} \) are computed in [14, 15]. The finite remainders of the latter agree with the corresponding terms constructed from the two-loop helicity amplitudes calculated of [16, 17] after the infrared subtraction procedure is performed.

In order to arrive at a complete prediction for \( \bar{\mathcal{M}}_q^{(0)} \cdot \mathcal{M}_q^{(2)} \right|_{m=0} \) including all heavy-quark loop corrections, the factorization approach in Eqs. (3.12), (3.13) is supplemented by a direct calculation of all necessary massive Feynman diagrams as an expansion in the small mass. The advantage of this approach is an independent check of Eqs. (3.12) and (3.13) as well as of the corresponding massless results. It relies on the reduction of integrals to a set of masters with the Laporta algorithm [18], the subsequent construction of Mellin-Barnes representations for all the integrals, see e.g. [19–23] and the summation of series representations [24] or the application of the PSLQ algorithm [25].

We are now able to give the result for the interference of the two-loop and Born amplitude for the scattering processes (3.1). For a SU\( (N)\) gauge theory with \( N \) denoting the number of colors, one has \( C_A = N, C_F = (N^2 - 1)/2N \) and \( T_F = 1 - 2 \) and, as mentioned above, the total number of flavors \( n_f = n_l + n_h \) is the sum of \( n_l \) light and \( n_h \) heavy quarks. Thus, for \( q\bar{q} \) ! \( \bar{Q} \bar{Q} \) and \( gg \) ! \( \bar{Q} \bar{Q} \) we have

\[ 2\text{Re} \bar{\mathcal{M}}_q^{(0)} \cdot \mathcal{M}_q^{(2)} \right|_{m=0} = 2(N^2 - 1) N^2 A_q + B_q + \frac{1}{N^2} C_q + N n_l D_q + N n_h D_{q \bar{q}} \]

(3.14)

\[ + \frac{n_l}{N} E_{q \bar{q}} + \frac{n_h}{N} E_{q \bar{q}} + (n_l + n_h)^2 F_q \]

\[ 2\text{Re} \bar{\mathcal{M}}_g^{(0)} \cdot \mathcal{M}_g^{(2)} \right|_{m=0} = (N^2 - 1) N^2 A_g + N B_g + \frac{1}{N} C_g + \frac{1}{N^3} D_g + N^2 n_l E_{g \bar{q}} + N^2 n_h E_{g \bar{q}} \]

(3.15)

\[ + n_l F_{g \bar{q}} + n_h F_{g \bar{q}} + \frac{n_l}{N^2} G_{g \bar{q}} + \frac{n_h}{N^2} G_{g \bar{q}} \]

\[ + N n_l^2 H_{g \bar{q}} + N n_h n_l H_{g \bar{q} \bar{q}} + N n_h^2 H_{g \bar{q} \bar{q}} + \frac{n_l^2}{N} I_{g \bar{q}} + \frac{n_h n_l}{N} I_{g \bar{q} \bar{q}} + \frac{n_h^2}{N} I_{g \bar{q}} \]

and all explicit expressions can be found in [11, 12].

As explained above, the factorization approach provides results for all coefficients except the terms linear in \( n_h. \) These are \( D_{q \bar{q}} \) and \( E_{q \bar{q}} \) in Eq. (3.14) and \( E_{g \bar{q}}, F_{g \bar{q}} \) and \( G_{g \bar{q}} \) in Eq. (3.15), which have been obtained from a direct calculation of the massive loop integrals as briefly sketched above. Furthermore, to have an independent cross check of the factorization formulae (3.12) and (3.13)...
the direct computation of Feynman diagrams has also been extended to the coefficients $A_q$, $D_q$, $E_q$ and $F_q$ in Eq. (3.14) and to $A_g$, $E_g$, $H_{gj}$, $H_{gh}$, $I_g$, $I_{gj}$, and $I_{gh}$ in Eq. (3.15). Of course, for the coefficients tested we have found full agreement between both methods.

4. Conclusions

We have presented a discussion of the singular behavior of on-shell QCD amplitudes with massive particles at higher orders and we have emphasized the strong similarities between scattering amplitudes with massless and massive partons in the small mass limit. In this regime, factorization relates the two amplitudes multiplicatively by a universal process independent function $Z^{(m)}_{ij}$. The present results for amplitudes generalize the massless formulae known previously [1, 2] and they extend one-loop massive results [26] to all orders. For cross sections the analogous property [27] is now known through next-to-next-to-leading order [28, 29].

We have illustrated the predictive power of the factorization ansatz with new results for heavy-quark hadro-production at two-loops in QCD [11, 12]. The results include all logarithms in the mass $m$ as well as the constant terms and they can be used as a strong check of any future complete calculation. Moreover, if combined with the threshold behavior of the amplitude, which is not known at present they can serve as a well founded basis for quantitative predictions for, say, top production at LHC to next-to-next-to-leading order. In order to obtain physical cross sections, the virtual amplitudes considered here have to be combined with the corresponding real emission contributions, of course.

In a similar spirit, one can also derive higher order QCD corrections to new heavy (colored) particles, like squark or gluino production in supersymmetric extensions of the Standard Model. Also the approach taken here may prove useful in the future in formulating subtraction schemes with massive partons for the real emission contributions beyond one loop.

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