I. INTRODUCTION

Three dimensional topological insulators (TIs) caught attention soon after their prediction, for reviews see [1–3]. The band structure at the surface is the reason for their unique features: alike to graphene, the surface states of topological insulators are characterized by a linear energy dispersion, which is described by the zero mass Dirac equation. The single Dirac cone in TIs, however, leads to a spin-momentum locking and, with that, to new physics. Renowned techniques such as angle resolved photoemission spectroscopy (ARPES) or magneto-transport measurements, for review see [4], are applied to access and characterize surface carriers in TIs. New opportunities to study Dirac fermions are offered by nonlinear high frequency transport phenomena, which scale with the second or third power of radiation electric field. A plethora of such effects has been theoretically discussed and observed in TIs systems including circular and linear photogalvanic effects in three dimensional (3D) TI [5–19], edge photogalvanics in two dimensional (2D) TI [20–24], quantum interference controlled photocurrents, ultrafast photocurrents in TI states, transient photocurrents in the topological surface state measured by ARPES and its modifications, inverse spin-galvanic effect, and harmonic generation, for review see [25]. The advantage is that some of them can be used to excite solely the surface states even in TI materials with a high carrier density in the bulk and even at room temperature.

In this work we present a systematic study of the photogalvanic effect in a wide frequency range extending over two orders of magnitude from \( f \approx 0.6 \) to 60 THz. The experiments were carried out on various (Bi,Sb)Te based 3D TIs at room temperature. The samples, besides their composition, discriminate due to their Fermi level position or bulk carrier concentration. For low frequency radiation and normal incidence the photocurrent is caused by the linear photogalvanic effect. The spectra measured reveal that they follow the Drude high-frequency conductivity varying with the radiation frequency as \( 1/[1 + (2\pi f \tau)^2] \), where \( f \) is the radiation frequency and \( \tau \) is the scattering time of surface states carriers. These results are analyzed applying the microscopic theory developed in the Refs. [11,17] and provide an access to the room temperature scattering times and mobilities of the surface states. In some samples we observed a resonance-like increase of the LPGE at high frequencies in the range from 30 to 60 THz. The enhancement of the LPGE current is attributed to the photoionization of Dirac fermions in the surface states to the conduction/valence band. We discuss the microscopic model of this phenomenon and show that the photocurrent is formed by a shift contribution or an asymmetric relaxation of the photo-excited electrons/holes. Furthermore, in this frequency range and applying oblique incidence, we also observed a circular photogalvanic effect driven by the radiation helicity.

II. SAMPLES AND TECHNIQUE

For this study, we used molecular beam epitaxy (MBE) grown (Bi\(_{1-x}\)Sb\(_x\))\(_2\)Te\(_3\) based 3D TIs including a pure Bi\(_2\)Te\(_3\) sample [26–28], Bi\(_2\)Te\(_3\)/Sb\(_2\)Te\(_3\) heterostructures with different thicknesses of the Sb\(_2\)Te\(_3\) layer [22,23] and (Bi\(_{1-x}\)Sb\(_x\))\(_2\)Te\(_3\) ternary systems [29]. The samples, grown on a (111) oriented silicon substrate, were characterized by in-situ ARPES measurements, from which the energy dispersion and the Fermi level position were obtained. All samples composition, Fermi velocities and energies with respect to the Dirac point are summarized in Tab. 1. The latter varies from -35 up to 500 meV.
TABLE I: Samples compositions, Fermi energies $E_F$, and Fermi velocities $v_F$, together with scattering times $\tau$ obtained from the frequency dependencies of the linear photogalvanic effect. The scattering times are extracted with a tolerance value of 10%. The corresponding values of the carrier mobilities $\mu$ are calculated from the scattering times and the Fermi energies $E_F$. Note that the latter values are measured by in-situ ARPES and, in particular for $(\text{Bi}_{0.06}\text{Sb}_{0.94})_2\text{Te}_3$ with $E_F$ close to zero, may yield overestimated values of $\mu$, see [42].

| Sample | $E_F$ (meV) | $d_{\text{ST}}$ = 7.5 nm | $d_{\text{ST}}$ = 15 nm | $d_{\text{ST}}$ = 25 nm | $(\text{Bi}_{1-x}\text{Sb}_x)_2\text{Te}_3$ |
|--------|------------|---------------------------|------------------------|------------------------|--------------------------------|
|        | 500        | 140                       | 30                     | -35                    | 500                            |
| $v_F$ ($10^5$ m/s) | 4.3        | 5.2                       | 2.2                    | 2.5                    | 5.1                            |
| $\tau$ (ps)     | > 0.25     | 0.06                      | 0.06                   | 0.08                   | > 0.25                         |
| $\mu$ (cm$^2$/Vs) | > 940      | 1230                      | 1030                   | 1420                   | > 1330                         |

FIG. 1: Photocurrent $J_{x,y}$ measured along $x$- and $y$-directions and normalized on the radiation intensity $I$ in (a) Bi$_2$Te$_3$, (b) (Bi$_{0.06}$Sb$_{0.94}$)$_2$Te$_3$, (c) (Bi$_{0.57}$Sb$_{0.43}$)$_2$Te$_3$, and (d) Bi$_2$Te$_3$/Sb$_2$Te$_3$ heterostructure with Sb$_2$Te$_3$ thickness of 15 nm. Solid lines show fit after Eq. (1), see also Eq. (4) and discussion. Note that the polarization independent offset $D$ ($D'$), being much smaller than the amplitude $A(f)$, is subtracted in these plots. The insets in panel (a) and (b) define the angle $\alpha$ and show the experimental setup. Arrows on top illustrate the polarization plane orientation for several angles $\alpha$.

In the ternary systems ARPES measurements showed that in the ternary alloy with an Antimony concentration $x = 0.94$ the Fermi energy $E_F$ lies close to the Dirac point. Note that a reduced bulk carrier concentration is found at $x = 0.43$, see [44]. In the heterostructures, where Sb$_2$Te$_3$ layers are grown on a 10 nm Bi$_2$Te$_3$ layer, the Fermi level is tunable by varying the $p$-type Sb$_2$Te$_3$ thickness $d_{\text{ST}}$, see [42,43]. X-ray diffraction (XRD) measurements were performed to confirm the alignment of the substrate with the thin TI layer and to determine the in-plane crystallographic axes. With knowledge of the latter, the samples were cut along directions of high symmetry into 7 x 4 mm$^2$ pieces. The samples were electrically contacted in the middle of the edges parallel to the $x$- and $y$-directions, see inset in Fig. 1(a).

To cover a wide range of frequencies numerous sources of continuous wave (cw) and pulsed infrared/terahertz laser radiation were applied including optically pumped molecular terahertz lasers [45,46], free electron lasers (FELBE) at the Helmholtz-Zentrum Dresden-Rossendorf [47,48], a quantum cascade laser (QCL) [49,50] as well as $Q$-switched and transversely excited atmospheric pressure (TEA) CO$_2$ lasers [51,52]. The lasers operated at single frequencies in the range from $f \approx 0.6$ to 60 THz (corresponding photon energies range from $h\omega = 2.5$ to 250 meV, where $\omega = 2\pi f$ is the angular frequency). For the low frequency range from 0.6 to 3 THz a line-tunable pulsed molecular laser was used with CH$_3$F, D$_2$O and NH$_3$ as active media [53-55]. The laser generated single pulses with a duration of about 100 ns with a repetition rate of 1 Hz. The radiation intensity on the sample surface was about 10 kW/cm$^2$. Furthermore, low frequency measurements were performed in the range from $f = 1.8$ to 10 THz with the tunable free electron laser FELBE 1 (U-27) operating in the quasi $cw$ regime. The FELBE provided picosecond micro-pulses with repetition rates in the MHz range and an average power of tens of mW.

Radiation with frequencies of about 30 THz was obtained by pulsed line-tunable $Q$-switched and TEA CO$_2$ lasers. The $Q$-switched laser provided pulse durations of hundreds of nanoseconds with a peak power of about 1 kW and a repetition rate of about 120 Hz [56]. The operation mode of the TEA CO$_2$ lasers [51] was similar to the one of the molecular terahertz lasers. Further lines in this range and at higher frequencies up to 60 THz were obtained applying the free electron laser FELBE 2 (U-100), operating in the same regime as FELBE 1 described above. Radiation with $f = 58$ THz was additionally provided by a $cw$ quantum cascade laser with a power of about 10 mW.

The peak power of the radiation was monitored, depending on the system, with Mercury Cadmium Telluride (MCT) [57] and photon-drag [58] detectors, as well as with pyroelectric power meters. The beam positions and profiles were checked with pyroelectric cameras [58] or thermal sensitive paper. The radiation was focused onto spot sizes of about 1 to 4 mm diameter, depending on the radiation frequency. Experimental geometry included normal as well as oblique incidence. In experiments at normal incidence, front and back illumination was used with corresponding angles of incidence $\theta = 0$ and 180$^\circ$, see inset in Fig. 1(b). The back illumination was used to ensure that the signal is caused by the linear photogalvanic effect, being in focus of this work, and to ensure...
that there is only a negligible contribution of the photon drag effect\textsuperscript{17}, which, if present, can affect the frequency dependence of the photocurrent. In the measurements applying oblique incident radiation, aimed at the search for the circular photogalvanic effect\textsuperscript{80} in 3D TI at terahertz frequencies\textsuperscript{63,64}, the angle of incidence $\theta$ was varied between $-40^\circ$ and $40^\circ$ with the $(yz)$ plane of incidence.

In the majority of the experiments, linearly polarized radiation with an azimuthal angle $\alpha$ defining the orientation of the radiation electric field vector in the sample’s plane and the $y$-axis, see inset in Fig. 1(a), was applied. The angle $\alpha$ was varied either by rotation of half-wave plates or a grid wire placed behind a quarter-wave Fresnel rhomb, which was set to provide circularly polarized radiation. To study the helicity dependence of the signal quarter-wave Fresnel rhombs or plates were used. In this geometry, the radiation helicity was varied as $P_{\text{circ}} \propto \sin 2\varphi$, where the rotation angle $\varphi$ was defined as an angle between the laser polarization plane and the optical axis of the polarizers\textsuperscript{61,62}. Note that for $\alpha = 0$ as well as for $\varphi = 0$ the incident radiation was linearly polarized with electric field vector parallel to the $y$-axis.

The induced photocurrents were detected as a voltage drop across load resistors at room temperature. The signals were recorded either with GHz oscilloscopes, in case of the pulsed gas laser systems, or with lock-in technique, in case of the modulated quasi $cw$ radiation of FELBE and $cw$ radiation of the QCL. The photocurrents were measured in two directions, $x$ and $y$, perpendicular to each other and parallel to the sample edges, see insets in Fig. 1.

### III. EXPERIMENTAL RESULTS

A photocurrent excited by normal incident linearly polarized radiation was detected for all used frequencies and samples. It is characterized by the same overall behavior: It scaled quadratically with the radiation electric field, had a response time of picoseconds or less, and exhibited a characteristic polarization dependence. Figure 1(a) presents an example of the photocurrent variation upon rotation of the radiation polarization plane obtained in $\text{Bi}_2\text{Te}_3$ excited with radiation frequency $f = 3.3$ THz. The figure shows that the photocurrent scales after

$$\begin{align*}
J_x(\alpha)/I &= A(f) s_1 + D(f), \\
J_y(\alpha)/I &= -A(f) s_2 + D'(f),
\end{align*}$$

where $s_1 = -\cos 2\alpha$ and $s_2 = -\sin 2\alpha$ are the Stokes parameters of light defining the electric field orientation in the $x, y$ coordinate system and in a $45^\circ$ rotated one, respectively\textsuperscript{63,64}. Note that in all experiments the polarization independent offset $D(f)$ and $D'(f)$ was much smaller than $A(f)$, and therefore, is out of scope of this paper. Figures 1(b)-(d) show exemplary $J_x(\alpha)$ measured for further three samples including ($\text{Bi}_1-x\text{Sb}_x$)$_2\text{Te}_3$ ternaries with two different Sb concentrations $x$ and one of the $\text{Bi}_2\text{Te}_3/\text{Sb}_2\text{Te}_3$ heterostructures. Experiments with front and back illumination demonstrated that the polarization dependence itself, and sign and value of the coefficients $A(f)$ do not change. This result was the same in all samples and for all frequencies used in this work (data not shown). The dependence of the coefficient $A(f)$ on the frequency is shown in Fig. 2. The data reveal that in
a wide range of frequencies the photocurrent decreases with the frequency increase and can be well fitted by

\[ A(f) \propto 1/[1 + (2\pi f \tau)^2]. \quad (2) \]

At high frequencies, however, a substantial deviation from this behavior has been detected for several samples: the photocurrent drastically increases as compared to the values expected from Eq. (2), reaches a maximum and then decreases, see Figs. 2(b), (d) and 3(a). Note that, while the used discrete frequencies clearly indicate the photocurrent enhancement, they do not allow a characterization of the peak with a satisfactory resolution. As addressed above, the overall behavior at these frequencies including its polarization and angle of incidence dependencies remained unchanged, as shown in Figs. 1(b), (d) and 3(b).

For oblique incidence and linearly polarized radiation we observed the same dependence \( J(\alpha) \), however, the amplitude \( A(f) \) depending on sample and radiation frequency decreased or increased (data not shown, for the origin see Ref. [17]). Using elliptically polarized radiation, however, we observed that in the direction normal to the plane of incidence the polarization dependence was modified. Besides the LPGE, varying after Eq. (3), see also Eq. (7) and discussion. Inset shows the Stokes parameters \( s_1 \) and \( s_2 \), see [63, 64]. These characteristic polarization dependencies have been observed for all samples and frequencies used, see Figs. 1(b) and 3(b).

The fact, that in the experiments the photocurrent amplitude \( A(f) \) remains unchanged for front and back illumination excludes sizable contribution of the photon drag effect and provides a clear evidence for the photogalvanic effect in the surface states as a cause of the photocurrent.[11, 17] Indeed, the photogalvanic effect is determined only by the in-plane electric field orientation, see Eq. (4), and is insensitive to the radiation propagation direction. The photon drag current on the other hand, being proportional to the photon momentum \( q \), reverses its sign at inversion of the photon wavevector \( q_z \), see also Eq. (11). Therefore, a substantial contribution of the photon drag effect should result either in different magnitudes \( A(f) \) for front and back excitation or, if dominating, even in a change of the photocurrent direction.

For small photon energies, at which Drude absorption dominates and direct optical transitions are not possible, the linear photogalvanic effect is shown to be caused by the asymmetric scattering of Dirac fermions driven back and forth by the terahertz electric field[11, 17]. For elastic scattering by Coulomb impurities the photogalvanic coefficient \( \chi \) is given by [11]

\[ \chi = e v_F^2 \frac{2\tau}{E_F} \Xi \sigma(f) \quad (5) \]

in which \( e \) is the electric charge, \( \Xi \) the asymmetric scattering, \( \sigma(f) \) is the high frequency (Drude) conductivity given by

\[ \sigma(f) = \frac{e^2 E_F \tau}{4\pi \hbar^2 [1 + (2\pi f \tau)^2]^2}. \quad (6) \]

Equations (5) and (6) reveal that the amplitude of the photocurrent should scale after Eq. (2). Our measurements performed in a wide frequency range, apart from
the resonant-like increase at high frequencies observed in some samples, confirm this frequency dependence, see Figs. 2 and 3. Consequently, the investigation of the photogalvanic effect allows one to analyze the Drude conductivity of the surface states, which provides an access to the scattering times. In our data the latter one can be extracted for (Bi$_{0.06}$Sb$_{0.94}$)$_2$Te$_3$ and Bi$_2$Te$_3$/Sb$_2$Te$_3$ heterostructures with different thicknesses of Sb$_2$Te$_3$. For these samples the condition $\omega \tau \approx 1$ is fulfilled, see Figs. 1(b) and (d), in the studied frequency range. The values of $\tau$ can be estimated from the fit functions and are summarized in Tab. 1. Taking into account the Fermi level position, known from in-situ ARPES (see Tab. 1), we obtained room temperature mobilities of the Dirac states in these samples ranging from 1000 cm$^2$/Vs up to several thousands. These are of the same order of magnitude as the ones measured in transport experiments for low temperature from 2 up to 77 K, see e.g. Refs. [44,66].

The frequency dependencies of the photocurrent obtained for Bi$_2$Te$_3$ and (Bi$_{0.57}$Sb$_{0.43}$)$_2$Te$_3$ show that the photocurrent scales as $1/f^2$ down to the lowest frequencies used here, see Figs. 2(a) and (c). This indicates that the value $\omega \tau$ remains substantially larger than unity. Consequently, the scattering times in these samples are at least by one order of magnitude larger than that for previously discussed samples. To determine $\tau$ in these samples further measurements with substantially lower frequencies at which $\omega \tau$ becomes less than unity are required.

Now we turn to the photocurrent enhancement observed at high frequencies in several samples. Our results, in particular the polarization dependence for unchanged coefficients $A$ for front and back illumination reveal that this photocurrent is also caused by the linear photogalvanic effect in the surface states. The fact that it is characterized by a non-monotonic frequency dependence and a magnitude by $10 \div 100$ times larger as compared to the Drude-like photocurrent clearly indicates that other types of optical transitions must be responsible for the photocurrent formation. This could be either direct optical transitions from the Dirac cone to the bulk states (photoionization) or interband transitions within the Dirac cone.

Direct optical transitions induced by linearly polarized radiation can give rise to a photocurrent in systems of sufficiently low spatial symmetry (piezoelectric class). An example of such systems is the trigonal surface of topological insulators studied here. Two contributions to the photocurrent, which are of different microscopic origin, are possible. First, the photocurrent can originate from the shift of electron wave packets in the real space at optical transitions (shift contribution). Second, the photocurrent can emerge as a result of asymmetric relaxation of the excited electrons/holes. The latter mechanism of the photocurrent formation contains two stages. At the first stage, the optical excitation by linearly polarized radiation leads to an anisotropic distribution of carriers in the momentum space which is described by the stationary correction to the electron distribution function scales as a square of the ac electric field magnitude. The phenomenon is known in semiconductor physics as the optical alignment of electron momenta. At the second stage, the relaxation of the stationary correction to the distribution function by trigonal scatterers gives rise to a directed flow of carriers, i.e., an electric current. Similar two-step mechanisms of the photocurrent formation have been considered for the surface photocurrents in metals and bulk GaAs, as well as for quantum well structures.

In the idealized pure linear dispersion model, the photoionization, which results in the depopulation of Dirac states and population of excited bulk states, optical transitions and, consequently, related photocurrents are excited in the range provided by $\hbar \omega > E_F - E_F^*$. This is because the photoionization picture requires that the initial states of the direct optical transitions are occupied. Furthermore, to excite such transitions the final states must be empty. Therefore these transitions take place only in a certain range of photon energies. In real structures, the dispersion is more complicated and condition are not as straightforward. That is particularly the case in the such samples as our heterostructures combining two different materials. Nevertheless, the photocurrent due to photoionization must show a non-monotonic resonant-like frequency dependence as observed in experiments, see Fig. 2 and 3(a). According to band structure calculations, the above condition is fulfilled for photon energies corresponding to the enhanced photocurrent in all three Bi$_2$Te$_3$/Sb$_2$Te$_3$ heterostructures and the (Bi$_{0.06}$Sb$_{0.94}$)$_2$Te$_3$ sample. Therefore, the model is relevant for the experiments. While this qualitatively description of the resonance seems to be appropriated, a theory is not yet developed and is crucially needed. In the (Bi$_{0.57}$Sb$_{0.43}$)$_2$Te$_3$ sample the Fermi energy is substantially above than the edge of the conduction band, which results in the hybridization of the surface states and exclude photoionization. We attribute the observed resonance in this sample to surface photocurrents served by bulk carriers.

Assuming again ideal Dirac fermion bands, interband transitions become possible for photon energies larger than the double Fermi energy. Such systems are characterized by a constant probability as experimentally shown for graphene, where a value of 2.3% of the optical absorption has been reported. It seems thus unlikely that such transitions are the origin of the observed resonant-like photocurrent.

In experiments in pure Bi$_2$Te$_3$ no deviation from the Drude-like behavior was found, see Fig. 2(a). Band structure calculations for our samples demonstrate that in Bi$_2$Te$_3$ samples with $E_F = 500$ meV direct optical transitions are prohibited in the whole range of used photon energies (up to 250 meV).

At last but not least we discuss the circular photogalvanic effect (CPGE) detected at oblique incidence, see Fig. 3. The observed polarization dependence as well as...
the dependence on the angle of incidence are in full agreement with the phenomenological theory of the CPGE in the surface states, which are characterized by the $C_{3v}$ point group symmetry. The corresponding photocurrent for the $(yz)$ plane of incidence is given by:

$$J_x^{\text{circ}}(\varphi) = \gamma t_p t_n E_0^2 P_{\text{circ}} n \sin \theta = C(f, \theta) I \sin 2\varphi,$$

in which $\gamma$ is the CPGE constant, $E_0$ is the electric field amplitude in vacuum, $t_p$ and $t_n$ are transmission coefficients after Fresnel’s formula for linear $p$- and $s$-polarizations, and $n$ is the refraction index. All the LPGE resonance addressed above, we attribute the observed CPGE to the photoionization of the surface states. The microscopic mechanism, however, needs to take into account selective excitation of spin branches by circularly polarized radiation which follows from the selection rules. Such processes have been previously considered for 3D TIs excited with near infrared radiation and for 2D TIs excitation of electrons from helical edge states to bulk conduction band states. To conclude on the mechanism responsible for the circular photocurrent observed in our experiments further measurements are required, in particular, a detailed study of the frequency dependencies of the CPGE is needed. This is a subject of future work and is out of scope of the current paper.

V. CONCLUSION

To summarize, extensive investigation of the spectra of the photocurrent excited at normal incidence demonstrated that in very different samples and wide range of terahertz frequencies it is caused by the linear photogalvanic effect at Drude-like free carrier absorption. These experiments show that spectral studies of the linear photogalvanic effect in the terahertz/microwave range allows one to measure the mobility of the surface states carriers. We emphasize that the photogalvanic effect can only be excited in non-centrosymmetric surface states. Thus the frequency behavior of the Drude conductivity can be studied even at room temperature and in materials with substantial conductance in the bulk, where conventional surface electron transport can not be applied. Besides the LPGE caused by Drude absorption we also observed a enhanced linear photogalvanic effect and the circular photogalvanic effect excited by infrared radiation, which are attributed to the “ionization” of surface states at high frequencies.

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Note that the highest mobility value, extracted for $(\text{Bi}_{0.06}\text{Sb}_{0.94})_2\text{Te}_3$ corresponds, on the first glance surprisingly, to the shortest scattering time. This is due to the very small value of the Fermi energy obtained from ARPES and in fact can be overestimated.

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