SINGLE-LEPTON TOP SIGNALS WITH A $b$-TAG AT THE TEVATRON

V. Barger$^a$, E. Mirkes$^a$, J. Ohnemus$^b$, and R.J.N. Phillips$^c$

$^a$Physics Department, University of Wisconsin, Madison WI 53706, USA
$^b$Physics Department, University of California, Davis, CA 95616, USA
$^c$Rutherford Appleton Laboratory, Chilton, Didcot, OX11 0QX, UK

Events with a leptonic $W$-decay plus jets should contain top-quark signals, but a QCD $W +$ jets background must be separated. We compare transverse $W$-momentum, jet multiplicity, and $b$-tagging separation criteria, and find that the main background after tagging comes from mistagging. We illustrate how to extract the mass $m_t$ via event reconstructions and how to confirm signal purity by lepton angular distributions.
Searches for the $t$-quark are intense at the Fermilab Tevatron $p\bar{p}$ collider. The main characteristics of $t\bar{t}$ pair production and decay are well known. Current lower limits on $m_t$ are well above $M_W + m_b$, assuming the Standard Model (SM), so all signals contain $t\bar{t} \to W^+bW^-\bar{b}$. As an experimental trigger, at least one $W$ is usually required to decay leptonically $W \to \ell\nu$ ($\ell = e, \mu$), providing a distinctive isolated high-$p_T$ lepton and large missing-$p_T$ (denoted $\not{p}_T$); but large backgrounds, especially from QCD production of $W + \text{jets}$, remain to be separated. If the second $W$ also decays leptonically and one $b$-jet is tagged, the resulting $\ell\ell'b$ signal may be comparatively clean, but the event rate is not large and the top mass cannot be directly reconstructed due to missing neutrinos.

The advantages of single-lepton top signals, where the second $W$ decays hadronically $W \to q\bar{q}'$, are both larger event rate and direct top mass reconstructibility; the draw-back here is the inherent uncertainty in QCD $W + \text{jets}$ background calculations at the parton level, especially for high jet multiplicity $n_j$. Some way must therefore be found to control or eliminate this background. Since the top signals contain four hard partons $b\bar{b}qq'$ while the QCD background has typically low $n_j$ and few $b$-quarks, the usual approach is to require large $n_j$ and $b$-tagging of at least one jet; calculations then predict that the background is severely reduced relative to the signal, assuming this background comes mainly from $Wb\bar{b} + \text{jets}$ production with genuine $b$-jets.

In the present Letter we point out that the main background actually comes from mistagged events containing no true $b$-jets. We find that the transverse momentum $p_T(W)$ of the trigger $W$ is another important characteristic, and investigate the interplay of $p_T(W)$, $n_j$, and $b$-tagging criteria in separating single-lepton top signals from $W + \text{jets}$ backgrounds. The decay $t \to bW$ has a Jacobian peak at $p_T(W) = (m_t^2 - M_W^2)/(2m_t)$ in the $t$-restframe, giving a broad $p_T(W)$ lab-frame distribution unlike the QCD background. We find that the background $p_T(W)$-dependence differs less from the signal after imposing $n_j \geq 3$; nevertheless a $p_T(W)$ cut can be helpful for heavier top $m_t \gtrsim 170$ GeV. Once selection cuts have been imposed, we illustrate how the mass $m_t$ can be found by event reconstructions, with fitting criteria that further suppress backgrounds, and show how the signal purity can eventually
be confirmed by lepton decay distributions. Our conclusions are detailed in (i)–(viii) below.

Analytic next-to-leading order calculations \[5\] of inclusive $W$ production agree well with CDF data \[6\] but cannot address jet multiplicity with specific acceptance cuts, and anyway exist only for $n_j \leq 2$. We therefore make Monte Carlo parton-level calculations of $W + n$-jet backgrounds at leading order \[4,7,8\], interpreting final partons as jets if they satisfy the cuts, and imposing typical acceptance cuts:

\[
p_T(\ell, \text{jet, missing}) > 20 \, \text{GeV}, \quad |\eta(\ell)| < 1.1, \quad |\eta(j)| < 2.0, \quad \Delta R(jj, j\ell) > 0.4. \tag{1}
\]

Here $\eta = \ln \tan(\theta/2)$ is pseudo-rapidity, $(\Delta R)^2 = (\Delta \phi)^2 + (\Delta \eta)^2$, and $\theta$ and $\phi$ are polar and azimuthal angles relative to the beam. The $\Delta R$ cuts approximate some effects of jet-finding and lepton-isolation criteria. We assume that at least one of the final jets is $b$-tagged by a vertex detector (neglecting additional tagging via semileptonic decays, since the extra neutrino would blur reconstructions of \(t \to Wb\) kinematics). For $W +$ jets production, we neglect quark masses (valid at high $p_T$) and use the scale $Q = \langle p_T(j) \rangle$ with the MRS set D0 parton distributions \[9\] and 4 flavors. The signals from $t\bar{t}$ production and decay are calculated at lowest order, without $t$-fragmentation effects because of the short top lifetime.

However, we normalize the cross section to $O(\alpha_s^3)$ calculations, taking central values from Ref. \[10\] (similar central values are given in Ref. \[11\]). To all calculations we add gaussian lepton- and jet-smearing prescriptions \[12\], based on CDF values \[13\], and evaluate $\tilde{p}_T$ from the overall $p_T$ imbalance.

In the CDF experiment, the efficiency for tagging one or more $b$-jets in a $t\bar{t}$ event is about 0.30, corresponding to a probability $\epsilon_b \simeq 0.16$ per $b$-jet; the probability of a fake $b$-tag is estimated to be $\epsilon_q \simeq \epsilon_g \simeq 0.01$ per light-quark or gluon jet \[14\]. We assume a probability $\epsilon_c \simeq 0.03$ for a bogus $c$-jet tag. The cross section for each final configuration is multiplied by the corresponding probability that at least one of the jets is tagged; e.g. the tagged cross sections for $Wgggg$, $Wc\bar{c}gg$, $Wbbq$ production contain factors 0.04, 0.08, 0.32, respectively.

Tagged signal and background cross sections, for separate jet multiplicities $n_j$, are shown versus $p_T(W)$ in Fig. 1(a). Solid curves denote the $n_j = 3$ and $n_j = 4$ signals for the case
$m_t = 150$ GeV ($n_j \leq 2$ signals are negligible). Dashed curves show total $n_j = 1, 2, 3, 4$ backgrounds from $W +$ jets. For comparison, the contribution from $Wb\bar{b}jj$ final states, containing two true $b$-jets, is shown by a dash-dotted curve. Figure 1(a) shows that

(i) The backgrounds from $Wb\bar{b}+j$ channels that contain genuine $b$-jets and have attracted most attention, contribute much less than fake-tags. If cleaner tagging becomes possible, better background suppression will follow.

(ii) The $W +$ jets background has narrower $p_T(W)$ dependence than the $t\bar{t}$ signal; the signal gets broader as $m_t$ increases.

(iii) Higher-multiplicity background components differ less sharply from the signal in their $p_T(W)$ dependence.

Figure 1(b) compares integrated cross sections above a minimum cutoff $p_T(W) > p_T^{\text{min}}$, for multiplicities $n_j = 3, 4$. Dashed curves again denote background, solid (dotted) curves denote signals for $m_t = 150$ (170) GeV; in each case the lower curve refers to $n_j = 4$ and the upper curve refers to the combined $n_j = 3, 4$ cross section. These results point to further conclusions:

(iv) For any given $p_T^{\text{min}}$ and luminosity, $n_j = 4$ is always the best choice. Adding $n_j = 3$ to $n_j = 4$ data gives more signal events $S$ but much more background $B$, such that both $S/B$ and the statistical significance $S/\sqrt{B}$ are decreased.

(v) For $m_t \lesssim 150$ GeV with $n_j = 4$, $p_T^{\text{min}}$ cuts confer little advantage; they improve $S/B$ but reduce $S/\sqrt{B}$, leaving cleaner but less significant signals.

(vi) For heavier top, the broader signal can justify a $p_T^{\text{min}}$ cut; e.g. for $m_t = 170$ GeV and $n_j = 4$, a cut $p_T(W) > 50$ GeV increases $S/B$ by 25% with no loss of significance. Greater advantages accrue for yet larger $m_t$.

With a selected class of 4 jet events with a single-lepton and a $b$-tag, which are dominantly from $t\bar{t}$, there are various ways to extract $m_t$ (see e.g. Ref. [2,4]); we illustrate three.

(a) We can infer the neutrino longitudinal momentum from the $W \to \ell \nu$ mass shell constraint, within a two-fold ambiguity, assuming $p_T(\nu) = p_T$. Then the distribution of invariant mass $m(\ell\nu b_{\text{tag}})$ has a peak at $m_t$ on a combinatorial background. Each of the two
(b) Another approach is to identify two final untagged jets arising from $W \rightarrow jj$, satisfying an approximate mass-shell constraint

$$ |m(jj) - M_W| < 15 \text{ GeV.}$$

(2)

Then the tagged jet $b_1$ and the remaining fourth jet $b_2$ are both presumably $b$-jets (in the desired $t\bar{t}$ events), and the distributions of invariant mass $m(jjb_1)$ and $m(jjb_2)$ each contain a peak at $m_t$ on a combinatorial background (that is smaller because no two-fold ambiguity is present in $W \rightarrow jj$). This approach is illustrated in Fig. 2(b), for $m_t = 150$ GeV and $n_j = 4$; the distributions $m(jjb_1)$ and $m(jjb_2)$ are summed, giving 2 counts per event. It makes no difference here whether one or both of the non-$W$ jets are tagged; both are regarded as $b$-jets.

(c) A better method is to reconstruct both leptonic and hadronic $W$’s. There are then 4 ways to pair these $W$’s (one $W$ still has the two-fold ambiguity) with the two remaining jets (presumed to be $b$ and $\bar{b}$); each pairing gives two top masses $m_{t1}$ and $m_{t2}$. We select the pairing in which $m_{t1}$ and $m_{t2}$ are closest, subject to a reasonable limit

$$ |m_{t1} - m_{t2}| < 50 \text{ GeV,}$$

(3)

and their mean value defines the reconstructed top mass $\tilde{m}_t$:

$$ \tilde{m}_t = (m_{t1} + m_{t2})/2.$$  

(4)

The two-fold $W \rightarrow \ell\nu$ ambiguity and pairing ambiguities are thus resolved and a sharper $t$-mass peak results, as shown in Fig. 2(c) for $m_t = 150$ GeV with $n_j = 4$. The integrated $t\bar{t}$ signal here is 0.22 pb and the background is 0.017 pb, corresponding to 4.6 events on a background of 0.4 events with the present accumulated luminosity 21 pb$^{-1}$ at CDF. For $m_t = 170$ GeV the signal is 0.12 pb. Figure 2 indicates a further conclusion:
(vii) Full reconstruction as in (c) gives the cleanest and narrowest peak, hence best $m_t$ resolution.

We note that a different kind of approach is to use a maximum-likelihood analysis on individual signal events, with the background suppressed by tagging with $p_T(W)$ and/or $n_j$ cuts.

The final event sample, after all cuts, can be examined to confirm the characteristics expected of a $t\bar{t}$ signal. First, the $p_T(W)$ distribution should agree with Fig. 1. Second, the charged-lepton rapidity distribution should be forward/backward symmetric, unlike QCD $W$-events; Fig. 3(a) compares the asymmetry $A(y_\ell) = \pm[d\sigma/dy(y_\ell) - d\sigma/dy(-y_\ell)]/[d\sigma/dy(y_\ell) + d\sigma/dy(-y_\ell)]$ for charged leptons. (The $\pm$ sign is equal to the lepton’s charge and $y > 0$ is the hemisphere in the $p$ beam direction.) Also decay distributions in the Collins-Soper frame (where the $W \rightarrow \ell\nu$ reconstruction gives simply a $\pm \cos \theta$ ambiguity), offer further distinctive differences between signal and background; see Figs. 3(b) and 3(c). There are shape differences in both $\phi$ and $|\cos \theta|$ distributions, especially the latter. We conclude

(viii) Charged lepton distributions offer additional purity checks on a selected $t\bar{t}$ signal.

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Fig. 1. $p_T(W)$ and $n_j$ characteristics of $b$-tagged $t\bar{t}$ signals (solid and dotted curves), total $W+\text{jets}$ backgrounds (dashed curves), and the background contribution from $Wb\bar{b}jj$ events (dash-dotted curve): (a) differential cross sections versus $p_T(W)$ for various jet multiplicities $n_j$, (b) integrated cross sections for $p_T(W) > p_T^{\text{min}}$.

Fig. 2. Illustrations of three invariant mass reconstructions described in the text, for the case $m_t = 150$ GeV with $n_j = 4$: (a) leptonic $W+b$, (b) hadronic $W+b$, (c) best fit to $t\bar{t}$ kinematics.

Fig. 3. Angular distributions of charged leptons, after cuts: (a) forward/backward asymmetry versus lepton rapidity $y_\ell$, (b) Collins-Soper azimuthal dependence, (c) Collins-Soper $|\cos \theta|$ dependence. Solid (dashed) curves denote $t\bar{t}$ signals ($W+\text{jets}$ backgrounds).
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Figure 3