Do North American Migratory Barren-Ground Caribou Subpopulations Cycle?

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ABSTRACT. Unlike all other members of the deer family, subpopulations of barren-ground caribou (Rangifer tarandus groenlandicus) are typically sine-cyclic. We used Bayesian Information Criteria (BIC) to rank competing population dynamics models for 11 North American barren-ground caribou subpopulations. Nine of these subpopulations were best described as sine-cyclic with periods ranging from a minimum of 26 years (Bluenose-East and Porcupine) to a maximum of 55 years (Western Arctic); and amplitudes ranging from a minimum of 8 455 (Cape Bathurst) to a maximum of 327 432 (George River). Time series estimates of subpopulation abundance generated by the sine cycle models showed good correspondence to published subpopulation estimates of abundance for all nine sine-cyclic subpopulations (r = 0.978; p < 0.001). Lack of demographic closure (migration between subpopulations) was evident in both of the subpopulations that were not identified as sine-cyclic. Barren-ground caribou subpopulation amplitudes were mostly determined by subpopulation total range size and summer range productivity (R² = 0.962; p < 0.001) and subpopulation periods were mostly determined by amplitude, total range productivity, and land surface temperature (R² = 0.950; p < 0.001). Time series estimates of subpopulation abundance generated from the respective environmental regression models were highly correlated (r = 0.964; p < 0.001) to the published subpopulation estimates of abundance for the set of 9 sine-cyclic subpopulations. Extended (> 3 generations) subpopulation declines are a natural feature of cyclic barren-ground caribou subpopulations. Trends in species abundance based on pooled assemblages of asynchronous cyclic subpopulations should be interpreted with caution.

Key words: Bayesian Information Criteria; BIC; barren-ground caribou; species designation; COSEPAC; IUCN; cyclic species; cycle analysis; climate change; population dynamics; Rangifer tarandus groenlandicus; subpopulation

RÉSUMÉ. Contrairement à tous les autres membres de la famille des cervidés, les sous-populations de caribous de la toundra (Rangifer tarandus groenlandicus) suivent généralement un cycle sinusoïdal. Nous avons employé des critères d’information bayésiens (BIC) pour classer des modèles de dynamique des populations concurrentiels pour 11 sous-populations nord-américaines de caribous de la toundra. Neuf de ces sous-populations correspondaient mieux à une description de cycle sinusoïdal avec des périodes allant d’un minimum de 26 ans (Bluenose-Est et Porcupine) à un maximum de 55 ans (Arctique de l’Ouest); et des amplitudes allant d’un minimum de 8 455 (cap Bathurst) à un maximum de 327 432 (rivière George). Les estimations des séries chronologiques de l’abondance des sous-populations obtenues à l’aide des modèles de cycles sinusoïdaux ont affiché une bonne correspondance par rapport aux estimations publiées de l’abondance des sous-populations pour l’ensemble des neuf sous-populations de cycle sinusoïdal (r = 0.978; p < 0.001). Le manque de fermeture démographique (migration entre les sous-populations) était évident dans les deux sous-populations qui n’étaient pas considérées comme suivant un cycle sinusoïdal. L’amplitude des sous-populations de caribous de la toundra était principalement déterminée par la taille de l’aire de répartition totale et la productivité de l’aire d’estivage (R² = 0.962; p < 0.001), et les périodes de sous-populations étaient principalement déterminées par l’amplitude, la productivité de l’aire de répartition totale et la température en surface des terres (R² = 0.950; p < 0.001). Les estimations des séries chronologiques de l’abondance des sous-populations produites au moyen des modèles respectifs de régression environnementale étaient fortement corrélées (r = 0.964; p < 0.001) aux estimations publiées de l’abondance des sous-populations pour l’ensemble des neuf sous-populations de cycle sinusoïdal. Les déclins prolongés (> 3 générations) de sous-populations sont une caractéristique naturelle des sous-populations cycliques de caribous de la toundra. Les tendances caractérisant l’abondance des espèces en fonction d’assemblages regroupés de sous-populations cycliques asynchrones devraient être interprétées avec prudence.

Mots clés : critères d’information bayésiens; BIC; caribou de la toundra; désignation des espèces; COSEPAC; UICN; espèces cycliques; analyse des cycles; changement climatique; dynamique des populations; Rangifer tarandus groenlandicus; sous-population

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Our consideration of barren-ground caribou (*Rangifer tarandus groenlandicus*) population dynamics uses the terminology suggested by Cronin (2006) for contiguous wildlife subpopulations as demographically distinct components of the larger North American barren-ground caribou population. However, not all barren-ground caribou subpopulations are demographically distinct (Nagy et al., 2011; COSEWIC, 2016; ADFG, 2017; Adamczewski et al., 2019), and some barren-ground caribou subpopulations (e.g., island subpopulations and the Dolphin-Union subpopulation) are sufficiently segregated that they are genetically distinct from even the most proximate subpopulations (McFarlane et al., 2016). Since an exchange of only one migrant per subpopulation per generation is sufficient to homogenize gene pools (Mills and Allendorf, 1996), contiguous continental subpopulations of barren-ground caribou are, as expected, genetically indistinguishable (McFarlane et al., 2016) except for the Dolphin Union, Southampton Island, and Baffin Island subpopulations, which are seasonally reproductively isolated. Our use of the term “subpopulation” is strictly in a demographic (not genetic) context and assumes demographic closure is sufficient to render exchange with other subpopulations negligible with respect to population dynamics.

Periodic subpopulation estimates have documented that barren-ground caribou subpopulations exhibit regular fluctuations in abundance that have sometimes been termed cyclic (Gunn and Miller, 1986; Couturier et al., 1990; Russell et al., 2002; Gunn, 2003; Wilson and Reeder, 2005; GY, 2015; COSEWIC, 2016). Traditional ecological knowledge (TEK) also confirms that regular periodic changes in abundance are characteristic of this species (Hemming, 1975; Zalatan et al., 2006; Council of Canadian Academies, 2014; Legat et al., 2014; Hebert, 2015). The factors that regulate barren-ground caribou subpopulation dynamics are not well understood (Messier et al., 1988; Klein, 1991), but forage availability, predators, insect harassment, pathogens, decadal winter severity, habitat disturbance (e.g., development and forest fires), and climate change are all believed to influence population dynamics in other species and could also drive or influence barren-ground caribou population cycles (Kelsall, 1968; Skoog, 1968; Hemming, 1971; Fancy et al., 1989; GNWT, 2007; COSEWIC, 2016). Fluctuations in abundance influence the size of seasonal ranges and the length of migration patterns (COSEWIC, 2016). As subpopulation abundance increases, seasonal ranges expand. Conversely, as subpopulation abundance declines, seasonal ranges contract towards the traditional calving areas (Hemming, 1975). The contraction of the home range has the net effect of allowing for the recovery of previously overused seasonal pastures (Hemming, 1975; COSEWIC, 2016).

On the summer range, barren-ground caribou forage on a variety of plants such as willows, grasses, dwarf birch, mountain avens, Arctic sorrel, mushrooms, moss campion, and berries (Thorpe et al., 2001; Dumond 2007), but lichen (dominated by *Cladina* sp.) is the primary forage for barren-ground caribou on the winter range (Thomas and Hervieux, 1986; Théau et al., 2005; Collins, 2006; Andersen and Johnson, 2014; Rickbeil et al., 2017), constituting approximately 60%–80% of their diet (Thomas and Hervieux, 1986; Jandt et al., 2003; Andersen and Johnson, 2014). Manseau et al. (1996) suggest that quality and volume of available forage on summer pastures are the primary regulators of physical body condition and population abundance. Gunn (2003) suggested that delayed feedbacks in herbivore-forage dynamics might be the primary driver in barren-ground caribou cycling. Others (e.g., Klein, 1970, 1986; Parker et al., 2005) suggest barren-ground caribou abundance is mainly determined by winter foraging conditions. Within a given subpopulation range, the availability of forage is influenced by range productivity, grazing intensity, trampling, and in winter range only, forest fires (Ahti, 1959; Scotter, 1964; Zalatan et al., 2006; Collins et al., 2011; Anderson and Johnson, 2014).

Direct weather events such as snow depth and icing can affect the ability of barren-ground caribou to access vegetation (Weladji and Holland, 2003). The frequency and severity of direct weather events are influenced by biome type and large-scale patterns in climatic activity such as
the El Niño Southern Oscillation (ENSO), the Atlantic Multidecadal Oscillation (AMO) the Arctic Oscillation (AO), the Pacific Decadal Oscillation (PDO), and longer-term progressive climate trends (COSEWIC, 2016). The AO has a strong negative correlation with population trends for the Porcupine and Central Arctic subpopulations (Joly et al., 2011).

North America’s barren-lands are comprised of five main biome types: alpine tundra, shrub tundra, herb tundra, forest tundra, and boreal forest (Dyke, 2005). These five biomes are characterized by relatively low temperatures, short growing seasons, acidic nutrient-poor soils with patchy vegetation, and slow vegetation regeneration rates (Archer and Tieszen, 1980; Payette et al., 2001). The western Arctic of Alaska and Yukon is predominantly characterized by boreal forest and alpine tundra, while the eastern Canadian Arctic is predominantly shrub, herb, and forest tundra at similar latitudes (Dyke, 2005). Primary productivity follows a SW to NE gradient of decreasing net primary productivity (NPP) in northern North America (Qian, 1999; Hickel et al., 2002; Gillman et al., 2015). The gradient of NPP is driven by regional temperature trends and is clearly illustrated by the treeline isopleth. The mechanisms responsible for regional temperature trends are marine in origin and include sea surface temperature as mediated by ENSO events, the PDO, and the AMO (Liu et al., 2015).

Like all naturally occurring species, barren-ground caribou subpopulation numbers are ultimately regulated by density-dependent reductions in calf production, survival rates or both (Demerec, 1957; Tanner 1966; Caughley, 1977; McCullough, 1979, 1999; Fowler, 1981; Kie and White, 1985; Skogland, 1985; Clutton-Brock et al., 1987; Boyce, 1989; Messier et al., 1988; Bowyer et al., 2014). The discrete logistic equation (linear density effects) can exhibit convergence on carrying capacity, stable limit cycles, increasing oscillations to extinction, and even chaos depending on the population’s maximum growth rate ($\lambda_{\text{max}}$) (May, 1976; Renshaw, 1991). The maximum and minimum annual rates of population growth (or decline) for barren-ground caribou vary between subpopulations, but typically do not exceed $\lambda = 1.17$ and are not less than $\lambda = 0.83$ (Gunn, 2003). At barren-ground caribou $\lambda_{\text{max}} \leq 1.17$, the logistic equation suggests that caribou (like other deer species) would, ceteris paribus, converge on range carrying capacity (May, 1976; Renshaw, 1991; Vandermeer, 2010). Stable limit cycles are not observed until $\lambda_{\text{max}}$ is above 2.57 (May, 1976; Renshaw, 1991), which is more than double the maximum observed annual population growth rate for barren-ground caribou. Although both science and TEK agree that barren-ground caribou subpopulations experience regular fluctuations in population abundance (Meldgaard, 1986; Ferguson et al., 1998; Klein, 1991; Russell et al., 2002; Gunn, 2003; GY, 2015), no previous study has attempted to determine if these fluctuations are regular cycles.

Several barren-ground caribou subpopulations have experienced declines in abundance over approximately the last two decades (Gunn et al., 2010; CARMA, 2016; COSEWIC, 2016). Both the Committee on the Status of Endangered Wildlife in Canada (COSEWIC) and the International Union for Conservation of Nature (IUCN) have responded to the declines in subpopulation abundance by designating barren-ground caribou species as “threatened” and “vulnerable” (COSEWIC, 2016; IUCN, 2016). COSEWIC (2016) suggests barren-ground caribou subpopulation cycles are either synchronized or are currently influenced by a common factor that has interrupted their natural population trajectory. Alternatively, differences in subpopulation cycle periods could cause apparent pooled-group trends that were solely the result of damping and resonance (non-synchronous) subpopulation cycling. Periods of synchrony might be coincidental rather than caused by some factor affecting all barren-ground caribou subpopulations simultaneously.

We identified 11 North American barren-ground caribou subpopulations that had a sufficient time series of subpopulation estimates and compared linear, exponential, logistic, sine-cyclic, and wavelet cyclic functions using regression and model selection methods that ranked functions considering both fit and number of function parameters for each subpopulation. We estimated the period and amplitude for subpopulations that were best described as sine-cyclic. We pooled extrapolations of sine-cyclic subpopulations to examine the effects of damping and resonance on the population dynamics of the pooled time series. We compared the expected (extrapolated) sine-cyclic subpopulation estimates with the observed subpopulation survey estimates to test correspondence of the sine-cycle classification. We used stepwise regression to develop a suite of candidate models that employed subpopulation range specific environmental parameters, and used a model selection criterion to identify our best model. We then compared the environmental model expected values of subpopulation abundance to the observed subpopulation estimates as a test of model correspondence to nature.

**METHODS**

We identified five functions (linear, exponential, logistic, sine-cyclic, and wavelet; Fig. 1) as potential descriptions for the time series estimates of barren-ground caribou subpopulation abundance. We did not consider subpopulations that had fewer than five subpopulation estimates. Inspection of the Porcupine time series subpopulation estimates suggested a progressive increase in subpopulation abundance through consecutive cycles. We added a linear increase variable to the sine function for the Porcupine time series subpopulation estimates to test for progressive increase in the subpopulation cycle. We identified the best function based on a combination of statistical procedures that included least squares linear
regression and non-linear regression (IBM Corp., 2017), Shapiro-Wilk (S-W) test for normality of residuals (IBM Corp., 2017), and Bayesian Information Criteria (BIC) (Schwartz, 1978). We rejected function fits that did not result in a significant correlation (\( p \geq 0.05 \)) and those that resulted in a non-normal distribution of residuals (S-W \( p \leq 0.05 \)). We ranked functions based on their associated \( \Delta \text{BIC} \) (Bayesian Information Criterion) values. Our function selection criteria identified functions with \( \Delta \text{BIC} < 2 \) as equivalent functions (i.e., could not discriminate between them).

Structurally dissimilar regression models with similar correlation coefficients can be objectively ranked using Akaike's Information Criterion (AIC) and BIC criteria (Sugiura, 1978; Hurvich and Tsai, 1989; Burnham and Anderson, 2002). We used the identity \(-2 \log * (\text{log likelihood}) = n * \log(\text{RSS}/n)\) to formulate equations for AIC and BIC (Venables and Ripley, 2002) that could be calculated from the number of subpopulation estimates (n), the number of function parameters (k), and the regression sum of squares (RSS) associated with function fits for each subpopulation:

\[
AIC = n \log \left( \frac{RSS}{n} \right) + 2k \quad \text{eq. 1}
\]

\[
BIC = n \log \left( \frac{RSS}{n} \right) + k \log(n) \quad \text{eq. 2}
\]

As the number of parameters (k) in the candidate model increases relative to the sample size (n), AIC becomes negatively biased against simple models (small k) (Sugiura, 1978). This bias can lead to overfitting (i.e., inappropriate selection of complex models over simpler models) (Sugiura, 1978; Hurvich and Tsai, 1989). Hurvich and Tsai (1989) provided a corrected criterion for bias at low values of n:

\[
AICc = n \log \left( \frac{RSS}{n} \right) + 2k + \left( \frac{2k^2 + 2k}{n - k - 1} \right) \quad \text{eq. 3}
\]

We compared the AICc and BIC penalty terms (eqs. 2 and 3) to better understand the differences between the two model selection criteria for the range of sample size (n) and model parameters (k) relevant to the caribou subpopulation time series estimates and population functions we were comparing (Fig. 2). At low n/k ratios, the AICc parameter penalty for one additional parameter for simple models (low K) was much greater than the parameter penalty for more complex models (higher K) (Fig. 2), which caused a strong bias in favor of selecting simple models for a portion of the range of n/k values from our study (Fig. 2). The BIC parameter penalties were approximately proportional and thus unbiased through the same n/k range (Fig. 2). We were unable to find a previous mention of this issue, perhaps because our application employed minimal sample sizes to compare relatively simple models.

The BIC procedure identifies the best model and is the most appropriate choice when study purpose is to identify the best model (Aho et al., 2014). Compared to AICc, BIC is parsimonious and thus more prone to underfitting (Dziak et al., 2020). We based function (model) selection on BIC only and thus viewed the selection of more complex models (e.g., sine-cyclic) over simpler models (e.g., exponential) to be conservative. We ranked functions based on their associated \( \Delta \text{BIC} \) values. Our function selection criteria identified functions \( \Delta \text{BIC} < 2 \) as equivalent (could not discriminate between them) functions (Burnham and Anderson, 2002).

We generated time series estimates of pooled subpopulations (i.e., sum of all subpopulations we considered to be sine-cyclic) by extrapolating the sine function for each sine-cyclic subpopulation. We examined the pooled subpopulation time series for evidence of subpopulation synchrony or harmonics. We tested the correspondence of the sine functions to nature by comparing the sine function extrapolation to the time series of observed estimates of all the subpopulations considered sine-cyclic.

We utilized correlation and regression to explore the relationships between sine-cyclic subpopulation cycle period length and amplitude and selected subpopulation seasonal range attributes (i.e., total range area, tundra [summer] range area, forest [winter] range area, tundra percentage, mean land surface temperature [LST], NPP, and normalized difference vegetation index [NDVI]). We generated a correlation matrix of range attributes and subpopulation cycle characteristics (period and amplitude). We identified physical and biological range attributes that were significantly correlated (\( p \leq 0.05 \)) to period and to amplitude independently. Considering the results
spectral bands visible light (VIS) (0.4 to 0.7 µm) and near-infrared light (NIR) (0.7 to 1.1 µm) (Schmid, 2017). NDVI provides an estimation of the density of vegetation within a given pixel based on the reflectance of VIS and NIR light. NDVI is calculated as $\text{NDVI} = (\text{NIR} - \text{VIS})/(\text{NIR} + \text{VIS})$ (Weier and Herring, 2000). NDVI values for individual pixels range from 0.1 (stone, sand, and snow), 0.3 (sparse vegetation), 0.6 (temperate forests) to 0.8–1.0 (the highest possible density of vegetation [e.g., rainforest]). Negative values indicate the presence of water or ice (Schmid, 2017).

NDVI is a commonly used remote sensing method for assessing and monitoring ecological productivity. NDVI has been used to monitor ecosystem health, faunal habitat, faunal distribution and condition, forage quality, and disease risk (Leyquen et al., 2007). The NDVI index is calculated as

$$\text{NDVI} = (\text{NIR} - \text{VIS})/(\text{NIR} + \text{VIS})$$

where VIS and NIR refer to visible and near-infrared bands, respectively.

of the correlation matrix, we explored main and two-way interaction effects using stepwise linear regression to develop a suite of models of subpopulation period and amplitude as a function of physical and environmental variables. We ranked models using BIC and AICc criteria and compared models with $\Delta\text{BIC} < 2$ based on parsimony, fit (contribution to $R^2$), and deviation from the top model ($\Delta\text{BIC} = 0$). Using our preferred linear regression environmental model for period and deviation from the top model ($\Delta\text{BIC} = 0$), we generated subpopulation specific regression estimates of period and amplitude. We compared the environmental regression estimates to the sine function estimates of period and amplitude. Additionally, we used the environmental model estimates of period and amplitude to generate time series estimates of subpopulation numbers to compare against subpopulation estimates as a test of correspondence to nature.

Google Earth Engine (GEE) is a web-based remote sensing platform that is able to carry out spatial and temporal aggregations of satellite imagery (Sidhu et al., 2018). GEE provides public access to satellite archives from Landsat 4-8, Sentinel 1-2, MODIS to Aster, and World Health Indicators System (WHIS), which provide climate, land cover, and topographic data (Schmid, 2017). GEE allows for the spatial and temporal manipulation of these datasets using a JavaScript and Python application programming interface. We used ArcMap 10.8 to visualize, transform, and map spatial data. We geo-referenced subpopulation home ranges based on COSEWIC and CircumArctic Rangifer Monitoring and Assessment Network (CARMA) maps of barren-ground caribou subpopulations (CARMA, 2016; COSEWIC, 2016) using the North American Lambert Conformal Conic projected coordinate system. We classified the summer range as the proportion of the range north of the treeline and winter range as the proportion of the range south of the treeline. We used GEE to query LST, NDVI, and NPP data for the seasonal ranges and total ranges of the 11 barren-ground caribou subpopulations that we considered (Appendix S1). We filtered the data by date to retain only data from May to August, which we assumed would correspond to the main portion of the growing season on both the barren-lands...
TABLE 1. Using SPSS linear and non-linear regression, we compared the utility of five functions—linear \((k = 2)\), exponential \((k = 2)\), logistic \((k = 2)\), sine \((k = 4)\), and wavelet \((k = 5)\)—to describe changes in a time series of subpopulation estimates for 11 subpopulations (George River, Leaf River, Qamanirjuaq, Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, Porcupine, Central Arctic, Teshekpuk Lake, and Western Arctic) of barren-ground caribou. The regression residual sum of squares \((\text{RSS})\) associated with each function was used to calculate Bayesian Information Criteria \((\text{BIC})\) for each of the 11 subpopulations. Goodness of fit \((R^2)\) and the F-statistic were determined for each function. The Shapiro-Wilk \((\text{S-W})\) statistic was used to assess the normality of residual values. The number \((n)\) of population estimates for each subpopulation estimate ranged from 5 to 15. The number of parameters for each function \((k)\) ranged from 2 to 5. ∆BIC values less than 2.0 are bolded. We added a linear increase variable to the sine function for the Porcupine time series from 2000–18 and 2000–14, respectively. NDVI data from 2000 to 2016 were acquired from Landsat 7 at a 30 m pixel resolution. We generated a single estimate for each ecological productivity parameter \((\text{NDVI, NPP, and LST})\) on the seasonal and total ranges of each of the 11 subpopulations by averaging the pixel values of each parameter across the time series of the available data.

### RESULTS

Of the 14 North American subpopulations (Nagy et al., 2011; COSEWIC, 2016; Parlee et al., 2018), 11 subpopulations (George River, Leaf River, Qamanirjuaq, and forested areas (Post et al., 2009). LST and NPP data were acquired from MODIS satellite imagery at a 1 km pixel resolution from 2000–18 and 2000–14, respectively. NDVI data from 2000 to 2016 were acquired from Landsat 7 at a 30 m pixel resolution. We generated a single estimate for each ecological productivity parameter \((\text{NDVI, NPP, and LST})\) on the seasonal and total ranges of each of the 11 subpopulations by averaging the pixel values of each parameter across the time series of the available data. We employed the “two-step” cluster analysis method in SPSS (SPSS Inc., 2001) to create an empirical clustering of subpopulation period and amplitude using the selected variables from our regression models that significantly \((p \leq 0.05)\) increased the explanatory power \((R^2)\) of the model. The two-step method partitions the data set into a set of “k” groups, where k represents the number of clusters. Clusters were identified by assigning subpopulation variables into one of k clusters by minimizing intra-cluster variation based on Euclidean distance (Norusis, 2010). The optimal number of clusters was identified based on the silhouette measure of cohesion and separation (Norusis, 2010). The silhouette measure ranges from \([-1\) to \(+1\) where a higher value indicates that samples are well matched to their own cluster and poorly matched to neighbouring clusters. We identified the optimal number of clusters as the fewest number of clusters that produced a silhouette value greater than 0 (Norusis, 2010).
TABLE 2. We considered subpopulations sine-cyclic based on the fit ($R^2$) and Bayesian Information Criteria (BIC). Nine subpopulations (George River, Leaf River, Qamanirjuaq, Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, Porcupine, and Western Arctic) were classified as sine-cyclic. Estimates of period and amplitude were reported based on sine cycle fits to observed population abundance estimates.

| Subpopulation     | Period | SE   | Amplitude | SE    |
|-------------------|--------|------|-----------|-------|
| George River      | 51     | 2.3  | 327 432   | 19 936.6 |
| Leaf River        | 45     | 2.0  | 298 168   | 19 954.7 |
| Qamanirjuaq       | 54     | 4.1  | 228 198   | 23 735.2 |
| Bathurst          | 42     | 3.4  | 203 154   | 23 147.1 |
| Bluenose-East     | 26     | 0.1  | 71 893    | 425.1  |
| Bluenose-West     | 35     | 2.0  | 52 408    | 3 144.0 |
| Cape Bathurst     | 33     | 1.5  | 8445      | 385.3  |
| Porcupine         | 26     | 1.5  | 39 338    | 4 875.3 |
| Western Arctic    | 55     | 11.1 | 219 830   | 60 273.1 |

Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, Porcupine, Central Arctic, Teshekpuk Lake, and Western Arctic had sufficient subpopulation estimates (i.e., $\geq 5$) for a time series function analysis, and four subpopulations (Beverly, Ahiak, Dolphin-Union, and Tuktoyaktuk Peninsula) did not. The wavelet function was only fit to 6 of 11 subpopulations because of data limitations (Table 1). Cyclic (sine or wavelet) function fits to the time series subpopulation estimates were identified as the best ($\Delta$BIC < 0) population projection functions for 10 of the 11 subpopulations, but $\Delta$BIC < 2 model selection criteria did not discriminate between most function options for the Teshekpuk Lake subpopulation (Table 1). We could not discriminate between the sine and wavelet functions for the Bathurst subpopulation (Table 1). The wavelet function was the only function to meet our validation criteria for the Central Arctic subpopulation (Table 1). The sine function with the addition of a linear increase term provided the best fit to the Porcupine time series subpopulation estimates and was the top BIC model ($r = 0.946$, $p < 0.001$; $\Delta$BIC = 0; Table 1). We classified nine subpopulations—George River, Leaf River, Qamanirjuaq, Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, Porcupine, and Western Arctic—as sine-cyclic. We tested the sine functions for all nine subpopulations. The regression produced a Pearson’s $r$ correlation coefficient of $r = 0.977$ ($p < 0.001$), and Spearman’s non-parametric correlation coefficient of $r = 0.978$ ($p < 0.001$), which indicates a very strong correspondence to the sine classification.

The correlation matrix between subpopulation seasonal range attributes and cycle characteristics identified significant ($p \leq 0.05$) correlations between amplitude and period, NDVI, tundra percentage, total range area, summer range area, winter range area, and total range LST (Table 3). There were no individual range attributes that were significantly correlated with period, but amplitude was most highly correlated with period ($r = 0.822$, $p = 0.007$; Table 3). Total range LST (a physical variable) was the best single variable predictor of subpopulation amplitude ($r = 0.922$, $p \leq 0.001$; Table 3).
TABLE 3. A correlation matrix of cycle characteristics (period length and amplitude) and subpopulation range attributes. Our criteria described significant correlations as \( p \leq 0.05 \) (highlighted). Period was not significantly correlated with any range attributes, but amplitude was the best single predictor of period \( (r = 0.822; \ p = 0.007) \). Amplitude was significantly correlated with period, NDVI, tundra percentage, total range area, winter range area, and total range LST, with total range LST being the single best predictor of amplitude \( (r = 0.922; \ p < 0.001) \).

| Period | Period | Amplitude | NDVI\(^1\) | Tundra % | Total range area | Summer range area | Winter range area | Total range NPP\(^1\) | Summer range NPP | Winter range NPP | Total range LST\(^1\) | Summer range LST | Winter range LST |
|--------|--------|-----------|------------|----------|-----------------|-----------------|-----------------|-----------------|----------------|----------------|-----------------|----------------|----------------|
|        | \( \tau \) | .1 | .822 | .660 | −.364 | .498 | .331 | .480 | .405 | .116 | .346 | .645 | .160 | .349 |
|        | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Amplitude | \( \tau \) | .822 | 1 | .760 | −.677 | .835 | .667 | .786 | .443 | −.058 | .361 | .922 | .331 | .486 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| NDVI | \( \tau \) | .660 | .760 | 1 | −.469 | .622 | .707 | .496 | .223 | −.026 | .320 | .681 | .578 | .836 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Tundra % | \( \tau \) | −.364 | −.677 | −.469 | 1 | −.724 | −.391 | −.769 | −.319 | .137 | −.261 | −.685 | −.193 | −.347 |
|          | \( \rho \) | .336 | .045 | .203 | −.027 | .029 | .015 | .299 | .725 | .497 | .042 | .619 | .361 | .568 |
| Total range area | \( \tau \) | .498 | .835 | .622 | −.724 | 1 | .788 | .961 | .469 | .055 | .327 | .879 | .618 | .282 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Summer range area | \( \tau \) | .331 | .667 | .707 | −.391 | .788 | .1 | .590 | .475 | .290 | .466 | .790 | .637 | .568 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Winter range area | \( \tau \) | .480 | .786 | .496 | −.769 | .961 | .590 | .389 | −.068 | .195 | .783 | .475 | .104 | .719 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Total range NPP | \( \tau \) | .455 | .443 | .222 | −.391 | .469 | .415 | .389 | .1 | .764 | .944 | .764 | .381 | .200 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Summer range NPP | \( \tau \) | .280 | .232 | .566 | .299 | .203 | .267 | .300 | −.017 | .017 | .630 | .253 | .100 | .679 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Winter range NPP | \( \tau \) | .346 | .361 | .320 | −.261 | .327 | .431 | .195 | .944 | .762 | 1 | .612 | .416 | .421 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Total range LST | \( \tau \) | .645 | .922 | .681 | −.685 | .879 | .790 | .724 | .616 | .000 | .017 | −.080 | .265 | .260 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Summer range LST | \( \tau \) | .681 | .385 | .103 | .619 | .076 | .020 | .196 | .312 | .252 | .265 | .168 | .164 | .316 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |
| Winter range LST | \( \tau \) | .349 | .486 | .836 | −.346 | .282 | .575 | .104 | .200 | .000 | .421 | .506 | .396 | 1 |
|          | \( \rho \) | .997 | .007 | .973 | .336 | .173 | .384 | .191 | .280 | .769 | .363 | .691 | .681 | .357 |

\(^1\) NDVI = Normalized difference vegetation index; NPP = Net primary productivity; LST = Mean land surface temperature.
TABLE 4a. Linear regression and Bayesian Information Criteria (BIC) were employed to develop and compare models of sine-cyclic barren-ground caribou subpopulation amplitude as functions of environmental and biological range variables. Statistically significant ($p \leq 0.05$) models with $\Delta$BIC values < 2.0 (bolded) were regarded as equivalent. Three models (model #5, #9, and #13) met our required criteria. Model #5 was selected because it was the best model ($\Delta$BIC = 0) and explained the greatest percentage of variation ($R^2 = 0.962$). Model 13 produced an equivalent value of $R^2$, however it contained one additional variable.

| Model # | Parameters | RSS | $R^2$ | $\Delta$BIC |
|---------|------------|-----|-------|-------------|
| 1       | Total range area | 3.41E+10 | 0.694 (0.005) | 5.270 |
| 2       | Total range area, summer range area | 3.41E+10 | 0.694 (0.029) | 6.224 |
| 3       | Total range area, summer range NPP | 3.28E+10 | 0.706 (0.025) | 6.073 |
| 4       | Total range area, summer range area, summer range NPP | 3.25E+10 | 0.708 (0.083) | 6.999 |
| 5       | Total range area, summer range area, summer range NPP, summer range area × summer range NPP | 4.25E+09 | 0.962 (0.004) | 0.000 |
| 6       | Total range area, summer range area × summer range NPP | 3.34E+10 | 0.701 (0.027) | 6.142 |
| 7       | Total range mean LST, summer range area | 1.60E+10 | 0.857 (0.003) | 3.258 |
| 8       | Total range LST, summer range area, tundra percentage | 1.59E+10 | 0.858 (0.015) | 4.187 |
| 9       | Total range LST, summer range NPP | 1.08E+10 | 0.903 (0.001) | 1.737 |
| 10      | Total range LST, winter range area | 1.59E+10 | 0.857 (0.003) | 3.251 |
| 11      | Total range area, winter range NPP | 3.31E+10 | 0.703 (0.026) | 6.113 |
| 12      | Total range area, total range NPP | 3.37E+10 | 0.697 (0.005) | 6.186 |
| 13      | Total range area, summer range area, summer range NPP, summer range area × summer range NPP | 4.23E+09 | 0.962 (0.024) | 0.930 |
| 14      | Summer range area, summer range LST | 5.50E+10 | 0.507 (0.120) | 8.097 |
| 15      | Total range area, summer range area, summer range LST | 5.24E+10 | 0.780 (0.042) | 5.896 |
| 16      | Total range area, winter range area, winter range NPP, winter range area × winter range NPP | 3.16E+10 | 0.716 (0.196) | 7.842 |
| 17      | Total range area, total range NPP, total range area × total range NPP | 3.08E+10 | 0.724 (0.073) | 6.780 |
| 18      | Summer range area × summer range NPP, winter range area × winter range NPP, total range area × total range NPP | 3.21E+10 | 0.713 (0.080) | 6.939 |
| 19      | Winter range area, winter range NPP, winter range area × winter range NPP | 3.67E+10 | 0.671 (0.111) | 7.472 |
| 20      | Total range LST, winter range area, winter range NPP, winter range area × winter range NPP | 9.55E+09 | 0.914 (0.021) | 3.161 |
| 21      | Total range LST, total range area × total range NPP | 1.72E+10 | 0.846 (0.004) | 3.543 |
| 22      | Total Range Area, Total Range LST | 1.69E+10 | 0.849 (0.003) | 3.474 |
| 23      | Total range area, total range LST, summer range area × summer range NPP | 1.24E+10 | 0.889 (0.008) | 3.225 |
| 24      | Total range area, summer range LST, summer range area × summer range NPP | 2.65E+10 | 0.762 (0.051) | 6.202 |

Three of the amplitude environmental regression models were indistinguishable at $\Delta$BIC < 2 (Table 4a). Our preferred environmental regression model for amplitude was model #5 ($R^2 = 0.962$, $p < 0.007$; $\Delta$BIC = 0; Table 4a, Fig. 5). The model included total range area, summer range area, summer range NPP, and the interaction of summer range area × summer range NPP. Summer range area and summer range NPP as main effects contributed little to the final amplitude model but were necessary to include because the interaction effect (summer range area × summer range NPP) did significantly improve the model ($p = 0.007$; Table 4b). Comparison of sine function estimates of subpopulation amplitude and environmental regression model estimates of subpopulation amplitude produced a Pearson’s correlation coefficient of $r = 0.981$ ($p < 0.001$, S-W ($p = 0.518$; Fig. 5).

Three of the period environmental regression models were indistinguishable at $\Delta$BIC < 2 (Table 5a). Our preferred environmental regression model for period was model #25 ($R^2 = 0.950$, $p < 0.007$; $\Delta$BIC = 0; Table 5a, b; Fig. 6). All three BIC < 2 models included a similar combination of environmental variables: amplitude, total range area, total range productivity (i.e., total range NPP or total range area × total range NPP), and total range LST (Table 5a). Model #25 was intermediate with respect to parameter count and the best ($\Delta$BIC = 0) model. Comparison of sine function estimates of period and environmental regression model estimates of subpopulation period produced a correlation coefficient of $r = 0.975$ ($p < 0.001$, S-W ($p = 0.132$; Fig. 6).

The estimates of period and amplitude from the environmental regression models allowed extrapolation of “predicted” individual subpopulation time series values. Comparison of the extrapolated subpopulation numbers...
from the preferred environmental models to the observed subpopulation estimates \( n = 91 \) produced a significant positive correlation with symmetrical residuals \( r = 0.964, p < 0.001, \text{S-W} (p) = 0.430 \) for the set of nine sine-cyclic subpopulations (Fig. 7).

Amplitude cluster analysis was based on total range area and the interaction of summer range area \( \times \) summer range NPP. The optimal number of clusters identified was two (silhouette measure = 0.7). Cluster one (i.e., George River, Leaf River, and Porcupine) was characterized by larger total areas and higher values of summer range area \( \times \) summer range NPP (Fig. 8). Cluster two (i.e., Qamanirjuaq, Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, and Western Arctic) was characterized by smaller total range areas and lower values of summer range area \( \times \) summer range NPP (Table 6, Fig. 9).

The period cluster analysis was based on amplitude and total range LST. The optimal number of clusters was two (silhouette measure = 0.7). Cluster one (i.e., George River, Leaf River, Qamanirjuaq, Bathurst and Western Arctic) was characterized by larger amplitude values and warmer total range mean temperatures (Table 6, Fig. 9). Cluster two (i.e., Bluenose-East, Bluenose-West, Cape Bathurst and Porcupine) was characterized by smaller amplitude values and cooler total range mean temperatures (Fig. 9).

**DISCUSSION**

Of the 14 barren-ground subpopulations (Nagy et al., 2011; COSEWIC, 2016; Parlee et al., 2018), four subpopulations (Beverly, Ahiak, Dolphin-Union, and Tuktoyaktuk Peninsula) had insufficient population estimates to allow comparison of population dynamics functions. Of the 11 remaining barren-ground subpopulations, we were unable to classify two (Teshekpuk and Central Arctic) as sine-cyclic based on BIC criteria (Table 1). BIC identified the remaining nine barren-ground subpopulations (George River, Leaf River, Qamanirjuaq, Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, Porcupine, and Western Arctic) as sine-cyclic.

The wavelet function was the only function to produce \( \Delta \text{BIC} < 2.0 \) to the Central Arctic time series subpopulation estimates. The wavelet estimate of cycle period length and amplitude value converges on a sine cycle estimate of period length and amplitude value when a true sine curve is sampled symmetrically for at least one complete cycle \( (r = 1.0, p < 0.001; \text{Fig. 1}) \). However, the converse is not always true because the wavelet function can fit time series data that comprise multiple simultaneous cycles (Zhang et al., 2000). We rejected the Central Arctic subpopulation as sine-cyclic, while noting that the wavelet function was the best model \( (\Delta \text{BIC} = 0; \text{Table 1}) \).

The Porcupine subpopulation sine function fit to the observed time series population estimates was improved by the addition of a linear increase term (Table 1). The sine function that included the additional linear term was

| Model number | Model Effect                                                   | \( R^2 \) | \( \Delta \text{BIC} \) | \( \text{Change of } \) \( R^2 \) | \( \text{Model } P \) | \( \text{Change of } \) \( P \) | \( \text{Model } P \) |
|--------------|---------------------------------------------------------------|----------|-------------------------|-------------------------------|------------------|------------------|------------------|
| 1            | Total range area                                             | 0.698    | 0.005                   | 0.694                         | 0.005            | 0.005            | 0.005            |
| 2            | Total range area + summer range area                          | 0.698    | 0.027                   | 0.690                         | 0.000            | 0.000            | 0.000            |
| 3            | Total range area + summer range area + summer range NPP       | 0.711    | 0.083                   | 0.683                         | 0.004            | 0.004            | 0.004            |
| 4            | Total range area + summer range area + summer range NPP + summer range area \( \times \) summer range NPP | 0.962    | 0.254                   | 0.014                         | 0.000            | 0.000            | 0.000            |
| 5            | Total range area + summer range area + summer range NPP + summer range area \( \times \) summer range NPP + total range LST | 0.962    | 0.000                   | 0.254                         | 0.000            | 0.000            | 0.000            |

\( \gamma = \text{Net primary productivity; LST} = \text{Mean land surface temperature.} \)
the only function selected using model selection criteria (ΔBIC ≤ 2) and fit (R²) (Table 1). Annual increases in abundance and sine-cyclic fluctuations in numbers could be due to increases in annual net productivity induced by climate warming across the Porcupine range, immigration from adjacent subpopulations, or increased selection for males in the harvest beginning in 2010 (T. Hegel, pers. comm. 2018). The Porcupine, Central Arctic, and Teshekpuk Lake subpopulations are all found in Alaska and all of their ranges overlap (ADFG, 2017) (Fig. 10). The Alaska Department of Fish and Game (2017) reported that approximately 18% of collared caribou migrated from the Central Arctic subpopulation to either the Teshekpuk Lake or Porcupine subpopulations prior to the 2016 photo-census, which suggests that these subpopulations are not demographically robust. The unmodified sine function was not ranked as the best population dynamics model for the Porcupine, Teshekpuk Lake, or Central Arctic subpopulations. However, the sine-cyclic function was identified as the best model for the adjacent Western Arctic subpopulation (ΔBIC = 0; R² = 0.972; Table 1). The Western Arctic barren-ground caribou subpopulation appears to be demographically distinct from the other three Alaskan subpopulations, which appear to be demographically linked. Subpopulation fidelity (effective demographic closure) is required to establish and maintain a given sine-cycle time series.

Both BIC and fit (R²) indicated approximately equal support for the wavelet and sine function fits to the Bathurst subpopulation time series subpopulation estimates. We classified the Bathurst subpopulation as sine-cyclic to retain consistency with other sine-cyclic subpopulations in our analysis. The Bathurst subpopulation had the lowest fit (R² = 0.874) of any of the nine sine-cyclic subpopulations (Table 1) and the residuals were symmetrical (S-W (p) = 0.316). The sine-cyclic fit to the Bathurst subpopulation time series suggests that its abundance should currently be increasing, however, the most recent estimate indicates that the expected increase in the Bathurst subpopulation is not occurring (Appendix S1). The Northwest Territories believes that wolf predation could be preventing recovery from current low numbers (WRBB, 2019). Others suggest that the recovery of the Bathurst subpopulation might also be delayed due to recent increases in anthropogenic disturbance (Boulanger et al., 2012; Adamczewski et al., 2013; COSEWIC, 2016). The strong correspondence of the Bathurst subpopulation abundance estimates to the sine cycle (Table 1) suggests historical resilience of the subpopulation cycle to both natural and anthropogenic disturbance. The symmetrical distribution of variance associated with the Bathurst sine cycle is inconsistent with a history of unmitigated progressive disturbance such as incremental development or climate warming. An alternative explanation for the apparent delay in Bathurst subpopulation increase is short-term emigration of some Bathurst individuals to the three adjacent subpopulations (Bluenose East, Beverly, and Qamanirjuaq) that collectively overlap most of the Bathurst subpopulation’s range (Nagy et al., 2011; COSEWIC, 2016; McFarlane et al., 2016) (Fig. 10). Adamczewski et al. (2019) noted that about 27%

### Table 5a. Linear regression and Bayesian Information Criteria (BIC) were employed to develop and compare models of sine-cyclic barren-ground caribou subpopulation period as functions of environmental and biological range variables. Statistically significant (p ≤ 0.05) models with ΔBIC values < 2.0 (bolded) were regarded as equivalent. Three models (model #23, #24, and #25) met our required criteria. Model 25 was selected because it was the best model (ΔBIC = 0) and explained 95.0% of the variation in period (p = 0.007).

| Model # | Parameters | RSS  | R²  | ΔBIC  |
|---------|------------|------|-----|-------|
| 1       | Amplitude  | 339.27 | 0.678 (0.000) | 4.425  |
| 2       | Amplitude, total range area | 217.33 | 0.794 (0.009) | 3.638  |
| 3       | Total range area, summer range NPP | 783.67 | 0.256 (0.412) | 8.651  |
| 4       | Total range area, winter range NPP | 752.48 | 0.285 (0.365) | 8.492  |
| 5       | Total range area, tundra percentage | 791.89 | 0.248 (0.425) | 8.692  |
| 6       | Amplitude, total range LST | 253.37 | 0.759 (0.014) | 4.238  |
| 7       | Total range LST, total range area | 592.36 | 0.437 (0.178) | 7.557  |
| 8       | Amplitude, total range area, total range LST | 200.16 | 0.810 (0.030) | 4.271  |
| 9       | Amplitude, total range area, total range area × total range NPP | 174.29 | 0.834 (0.021) | 3.730  |
| 10      | Amplitude, total range area, total range LST, tundra percentage | 180.23 | 0.829 (0.078) | 4.815  |
| 11      | Amplitude, tundra percentage | 266.71 | 0.747 (0.016) | 4.438  |
| 12      | Total range area, total range LST, tundra percentage | 588.48 | 0.441 (0.367) | 8.486  |
| 13      | NDVI, total range area | 580.75 | 0.448 (0.168) | 7.480  |
| 14      | Amplitude, summer range area | 252.45 | 0.760 (0.041) | 4.224  |
| 15      | Amplitude, winter range area | 263.33 | 0.750 (0.009) | 4.388  |
| 16      | Amplitude, summer range area × summer range NPP | 286.57 | 0.728 (0.020) | 4.719  |
| 17      | Amplitude, summer range area, summer range NPP | 160.80 | 0.847 (0.018) | 3.415  |
| 18      | Amplitude, summer range area, summer range NPP, summer range area × summer range NPP | 145.70 | 0.862 (0.052) | 3.984  |
| 19      | Total range area, summer range area, summer range NPP, summer range area × summer range NPP | 247.37 | 0.765 (0.140) | 6.053  |
| 20      | Total range LST, winter range area, winter range NPP, winter range area × winter range NPP | 560.91 | 0.467 (0.549) | 9.252  |
| 21      | Amplitude, total range area × total range NPP | 253.89 | 0.759 (0.014) | 4.246  |
| 22      | Amplitude, total range area, total range NPP, total range area × total range NPP | 157.04 | 0.851 (0.060) | 4.277  |
| 23      | Amplitude, total range area, total range area × total range NPP, total range LST, total range NPP | 43.63 | 0.959 (0.028) | 0.225  |
| 24      | Amplitude, total range area, total range NPP, total range LST | 67.784 | 0.936 (0.012) | 0.993  |
| 25      | Amplitude, total range area, total range area × total range NPP, total range LST | 52.58 | 0.950 (0.007) | 0.000  |
| 26      | Amplitude, total range area × total range NPP, total range LST | 234.32 | 0.777 (0.044) | 4.886  |
of the Bathurst subpopulation cows may have emigrated and joined the Beverly subpopulation (which outnumbered the Bathurst subpopulation 12:1) on the shared winter range in spring of 2017. Additionally, the difference between the most recent Bathurst subpopulation estimate and the expected (sine-cyclic) extrapolated number ($\Delta N = 9164$) was numerically small relative to the uncertainty inherent in both modeling and subpopulation estimation variance. These various hypotheses are not mutually exclusive, and our data are insufficient to resolve them.

The sine cycle function is a symmetrical repeating time series function if there are no perturbations to disturb it. BIC model selection for sine-cyclic subpopulation dynamics with high associated $R^2$ values (range: 0.874–0.999, mean = 0.948; Table 1) and normal residuals (S-W ($p$) range: 0.950–0.051; Table 1) is evidence that sine-cyclic subpopulations are demographically distinct. These results are consistent with robust clustering of individuals into the same barren-ground caribou subpopulations based on radio-collared caribou movements (Nagy et al., 2011). Identification of the sine-cyclic model as the most correct model for demographically distinct subpopulations implies that subpopulation period and amplitude have remained relatively constant through the time period (1958–2017) in which these population estimates were developed. We tested the sine-cyclic function's overall correspondence to nature by comparing the sine-generated time series estimates to the time series of observed subpopulation estimates for all nine subpopulations (Fig. 3). That regression produced a Pearson correlation coefficient of $r = 0.977$ ($p < 0.001$) with non-normal residuals (S-W ($p$) < 0.001). Spearman's non-parametric correlation coefficient was similar ($r = 0.978$), confirming good overall correspondence of the sine cycle function to the subpopulation estimates considered as a whole.

None of the individual sine cycle fits exhibit non-normal residuals, but the pooled residuals for all nine sine-cyclic subpopulations tested non-normal (S-W ($p$) < 0.001). One possibility is that the power of tests for normality is highly dependent on sample size (Yap and Sim, 2011). The power of the Shapiro-Wilk tests for individual subpopulations was 7 to 10 times less powerful than the same test for nine pooled subpopulations ($n = 91$). Alternatively, the pooled subpopulation regression may have mixed subpopulation residuals with different variances due to individual differences in subpopulation period and amplitude.

We assumed that the subpopulation estimates developed by many different research programs over a span of approximately 58 years were reliable and sound. We received several review comments that questioned this assumption. Our response is that BIC selection of the sine cycle as the correct model is conservative, and the fit (lowest sine-cyclic subpopulation $R^2 = 0.874$; Table 1) suggests that the various subpopulation estimates were generally accurate and consistent over this time span.

Given that the observed cycles cannot be birth-pulse stable limit cycles, the causes for barren-ground
caribou sine cycles in pristine regions must be found in the ecological relationships of their trophic system, environmental constraints, seasonality of their range, and the annual migrations. Historically, North American barren-ground caribou appear to have cycled up and down to unchanging subpopulation-specific rhythms that are decades long and apparently resilient to the suite of factors currently identified as threats to their continued persistence. Each of the sine-cyclic subpopulations had unique period and amplitude values (Table 2), which formed a general NW-SE gradient of increasing cycle period length and amplitude value. This trend was unexpected given the SW-NE gradient of decreasing NPP running perpendicular to the treeline. Subpopulations with ranges in close proximity to coastal regions (e.g., Western Arctic, Qamanirjuaq, and George River) had longer periods and greater amplitudes than more continental subpopulations (e.g., Bluensoe-East, Bluensoe-West, Cape Bathurst, and Western Arctic) (Table 2).

Our best environmental regression model for amplitude (Model 5, $R^2 = 0.962, p \leq 0.001; \Delta BIC = 0$) suggests that subpopulation amplitude is mainly determined by total range area and summer range productivity (summer range area $\times$ summer range NPP). Models 9 and 13 also had associated $\Delta BIC < 2.0$. (Table 4a, b). Model 9 was only able to explain $90\%$ of the variation in amplitude (Table 4a). Model 13 was able to explain an equal ($96.2\%$) amount of variation in amplitude compared to the selected model, but the additional parameter (total range LST) did not significantly improve the explanatory power (fit) of the model (Table 4a, b).

Three of the 26 environmental regression models for period had associated $\Delta BIC \leq 2$ (Tables 5a, b). All three models contained amplitude, total range area, total range NPP, and total range LST (Tables 5a, b). We selected Model 25 ($R^2 = 0.950, p \leq 0.007, BIC = 0$) as the best model based on BIC, parsimony, and intermediate in fit compared to the other two $BIC < 2$ models (Tables 5a, b). Period was most correlated to amplitude ($r = 0.822, p \leq 0.007$; Table 3), presumably because the time required for a subpopulation
TABLE 6. Discrete values of the biological and physical variables for the amplitude (total range area, summer range area, summer range NPP, and the interaction of summer range area × summer range NPP) and period (amplitude, total range area, the interaction of total range area × total range NPP, and total range LST) multiple linear regression models. The selected model for amplitude was able to explain 96.2% ($p = 0.007$) of the variation in survey estimates of amplitude, and the selected model for period was able to explain 95.0% ($p = 0.007$) of the variation in survey estimates of period.

| Herd          | Total range area (km²) | Summer range area (km²) | Summer range NPP (kg·C/m²) | Summer range area × summer range NPP | Amplitude | Total range area × total range NPP | Total range LST (°C) |
|---------------|------------------------|-------------------------|----------------------------|--------------------------------------|-----------|-----------------------------------|---------------------|
| George River  | 933 826                | 271 427                 | 1675.22                    | 454 699 938                          | 327 432   | 2 085 168 090                     | −2.52               |
| Leaf River    | 559 628                | 258 627                 | 1564.94                    | 453 600 148                          | 298 168   | 1 191 744 615                     | −2.69               |
| Qamanirjuaq   | 132 687                | 186 544                 | 1669.58                    | 296 960 428                          | 228 196   | 629 481 750                       | −5.20               |
| Bathurst      | 496 626                | 124 837                 | 1647.77                    | 183 232 003                          | 203 154   | 1 000 393 482                     | −4.95               |
| Bluenose-East | 269 346                | 93 462                  | 1574.13                    | 137 794 765                          | 71 893    | 514 779 032                       | −5.76               |
| Bluenose-West | 126 730                | 94 458                  | 1572.81                    | 144 133 877                          | 52 408    | 219 339 214                       | −6.89               |
| Cape Bathurst | 126 730                | 94 458                  | 1572.81                    | 144 133 877                          | 52 408    | 219 339 214                       | −6.89               |
| Porcupine     | 369 268                | 242 884                 | 1618.22                    | 482 042 159                          | 39 338    | 829 453 474                       | −5.54               |
| Western Arctic| 340 044                | 155 600                 | 1974.69                    | 307 261 764                          | 219 830   | 886 348 489                       | −3.72               |

1 NPP = Net primary productivity; LST = Mean land surface temperature.
NPP were sufficient to explain 96.2% (area, summer range area, summer range NPP, and the cycling. Our regression model suggested that total range of barren-ground caribou subpopulations drive population and volume of forage availability on the seasonal ranges (al., 1996; Parker et al., 2005) have suggested that the quality values tend to have longer periods (Fig. 9). Subpopulations characterized by warmer total rangeland surface temperature and larger amplitude values (Fig. 8). Subpopulations with a larger seasonal range and period and also by determining habitat recovery times. This result can be viewed in the comparative context provided by cluster analyses (Figs. 8, 9). Subpopulations with a larger seasonal range and higher values of ecological productivity (i.e., summer range area × summer range NPP) tended to have larger amplitude values (Fig. 8). Subpopulations characterized by warmer total rangeland surface temperature and larger amplitude values tend to have longer periods (Fig. 9).

Fauchald et al. (2017) suggest that local or regional climatic trends could influence subpopulation cycle characteristics. Progressive climate change could alter forage selection and availability, calving ground preference, biome type, range boundaries, productivity, and habitat recovery times. Our environmental regression models suggest that progressively longer growing seasons and increased productivity would cause a shift to larger amplitudes with longer cycle periods. The maximum and minimum rates of population growth (or decline) for barren-ground caribou vary between subpopulations but typically do not exceed λ = 1.17 and are not less than λ = 0.83 (Gunn, 2003). Given these constraints, subpopulations with larger, more productive range areas require more time for the subpopulation to increase to levels where density effects reduce vital rates and cause the subpopulation to decline. Similarly, for larger subpopulations, declines and recoveries take longer to occur, perhaps delaying vegetation recovery by extending the over-grazing period (Mysterud, 2006). However, the high correlation of the sine cycle (constant period and amplitude) to the time series of sine-cyclic subpopulation estimates suggests that climate warming has had a negligible effect on barren-ground caribou subpopulation cycles thus far within the subpopulations we studied.

Several barren-ground caribou subpopulations have experienced declines in abundance over approximately the last two decades (Gunn et al., 2010; CARMA, 2016; COSEWIC, 2016). Both COSEWIC and the IUCN have responded to the declines in subpopulation abundance by designating barren-ground caribou species as “threatened” and “vulnerable,” respectively. COSEWIC and the IUCN determine status based on trends in population abundance over a three-generation period and use a threshold of a 50% or greater reduction in total mature individuals (when the causes of the decline are known, understood, and reversible) as one of the criteria for threatened or vulnerable species designations (COSEWIC, 2016; IUCN, 2016). Barren-ground caribou have a generation time of seven to nine years (COSEWIC, 2016; IUCN, 2016), meaning a three-generation period would be approximately 21–27 years. Our cycle analysis indicates some subpopulations (e.g., Qamanirjuaq and Western Arctic) can have cycle period lengths greater than 50 years (Table 2), which means that naturally occurring periods of increase or decline could last longer than three-generations for some barren-ground caribou subpopulations. Cyclic barren-ground caribou subpopulations neither increase exponentially without bound, nor decline exponentially to extirpation unless they are perturbed by novel ecological, climatological, or anthropogenic mechanisms. Status determinations based on exponential or linear trends over a three-generation period may be inappropriate for cyclic species.

Our pooled population abundance estimate (Figs. 4, 11) suggests that barren-ground caribou species numbers experience natural fluctuations in abundance that can result in prolonged (> three generations) periods of growth.
Barren-ground caribou partake in regular seasonal migrations, migrating north in the spring to calve on the snow covered barrens, and south in the fall to winter in the boreal forest. Subpopulation home ranges tend to expand and contract relative to population abundance. Migration between subpopulations has been documented, and continental subpopulations of barren-ground caribou are genetically indistinguishable. Our use of the term “subpopulation” is strictly in a demographic (not genetic) context and assumes demographic closure is sufficient to render exchange with other subpopulations negligible with respect to population dynamics.

or decline, including declines greater than 50%. Sine-cyclic subpopulations, by definition, spend half of their cycle at numbers below 50% of maximum levels. Periods of growth and decline are asynchronous between different subpopulations; this is apparent by the observed differences in cycle period lengths (Table 2). Subpopulations with larger amplitudes and greater maximum numbers (e.g., George River or Qamanirjuaq; Table 2) can dominate species or pooled subpopulation dynamics, obscuring any progressive changes to smaller subpopulations and imply a synchronous increase or decline across all subpopulations when no such synchrony exists.

The COSEWIC (2016) barren-ground caribou pooled population estimate included nine subpopulations (Tuktoyaktuk Peninsula, Beverly, Ahiak, Lorillard, Wager Bay, Boothia Peninsula, Southampton Island, Coats Island, and Baffin Island) that did not have a sufficient number of subpopulation estimates for our function fit analysis (Fig. 12). The COSEWIC (2016) report also excluded the George River and Leaf River subpopulations as well as the three Alaskan (Central Arctic, Teshekpuk Lake, and Western Arctic) subpopulations from their pooled estimate (Fig. 12). A comparison between the COSEWIC (2016) exponential fit and our sine cycle extrapolations that included only the six subpopulations sampled in common (Qamanirjuaq, Bathurst, Bluenose-East, Bluenose-West, Cape Bathurst, and Porcupine; Fig. 12) yielded a similar pooled 2015 subpopulation abundance estimate (COSEWIC estimate = 537,549; sine-cyclic estimate = 587,841) (Fig. 11).

The close correspondence between qualitatively distinct population projection methods emphasizes the difficulty in discriminating between naturally occurring cycle declines and human-caused population declines over a short time frame relative to cycle period (Fig. 11).

In addition to population abundance criteria, COSEWIC and the IUCN Redbook status designation systems
incorporate other information before making final status assessments (COSEWIC, 2016). Disturbance and habitat loss (from industrial exploration and development), over-hunting, climate change, and contaminants are believed to present significant risks to barren-ground subpopulations (Adamczewski et al., 2013; COSEWIC, 2016; M. Campbell, pers. comm. 2020). Our study found no evidence of progressive demographic impacts to barren-ground caribou for any of the nine sine-cyclic subpopulations up to 2017, except for the previously discussed linear increase in the Porcupine subpopulation. However, we caution that mitigation measures and harvest management protocols may have thus far reduced negative demographic impacts to undetectable levels. We suggest that historical barren-ground caribou subpopulation sine cycles could serve as a baseline for detecting both single-factor and cumulative impacts on barren-ground caribou subpopulation demography within a given management context. We suggest increasing the monitoring frequency of barren-ground subpopulations to ensure the entire cycle period is sampled symmetrically so that any progressive changes to baseline period length and amplitude value can be detected and to better understand the population dynamics of barren-ground subpopulations that experience irregular fluctuations. Changes to subpopulation period and amplitude could serve as monitoring indicators for direct and cumulative impacts on affected barren-ground caribou subpopulations.

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