A Novel Solid-State Thermal Rectifier Based On Reduced Graphene Oxide

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Recently, manipulating heat transport by phononic devices has received significant attention, in which phonon – a heat pulse through lattice, is used to carry energy. In addition to heat control, the thermal devices might also have broad applications in the renewable energy engineering, such as thermoelectric energy harvesting. Elementary phononic devices such as diode, transistor and logic devices have been theoretically proposed. In this work, we experimentally create a macroscopic scale thermal rectifier based on reduced graphene oxide. Obvious thermal rectification ratio up to 1.21 under 12 K temperature bias has been observed. Moreover, this ratio can be enhanced further by increasing the asymmetric ratio. Collectively, our results raise the exciting prospect that the realization of macroscopic phononic device with large-area graphene based materials is technologically feasible, which may open up important applications in thermal circuits and thermal management.

With the development of solid-state devices, the integrated circuits can be built up by diodes and transistors. The conventional diodes and transistors can realize “on” and “off” state by controlling the electrical conduction. If the thermal conduction can be well controlled, we can also realize thermal circuits by using these novel phononics devices. In addition to information processing, the thermal devices might also have broad applications for heat control/management in the future. Recent years, some theoretical proposals for thermal rectifier have been put forward, include structures based on one-dimensional nanotubes and nanowires1–9, and two-dimensional graphenes10–13. The first solid-state thermal rectifier has been reported experimentally by C. W. Chang et al.14 in carbon nanotubes. However, it is still a challenge to create macroscale phononic devices based on these nanoscale architectures. Inspired by the study of thermal rectifier in nanoscale, an oxide thermal diode made of two cobalt oxides with different thermal conductivities have been experimentally demonstrated15,16. The working mechanism for this two-segment diode is that they have thermal conductivities with different temperature dependence. From a simple classical heat conduction analysis, the rectification of this two-segment diode is proportional to the difference in thermal conductivity, and inversely proportional to the interface resistance17. In most bulk materials, the large interface contact resistance between the two segments limits the enhancement of the rectification ratio. Thus it is indispensable to develop single component thermal rectifier.

In this work, for the first time, we demonstrated macroscopic scale thermal rectification phenomenon in asymmetric reduced graphene oxide (rGO) materials. According to recent efforts, rGO can be used to fabricate paper-like films with large area, excellent mechanical property, high thermal conductivity and electrical conductivity18–20. It has been demonstrated theoretically that compared to single-layer graphene, a larger rectification ratio can be achieved in multi-layer structures, due to the presence of layer-layer interactions17. Combined with the availability of high quality, here we use a “rGO paper” material composed of stacked rGO to make thermal rectifier. Benefit from their high thermal conductivity and strong temperature dependence around room temperature, high thermal rectification ratio is achieved in both triangular and two-rectangular shaped rGO based thermal rectifier, which is in good agreement with the numerical calculation.

Results

The optical photograph of the rGO paper is shown in Fig. 1(a). Figure 1(b) illustrates the surface of rGO film. Some ripples of graphene can be seen clearly. Figure 1(c) shows the cross-section of rGO. The film thickness is ~50 μm. Figure 1(d) presents the Energy Dispersive X-ray (EDX) spectrum of rGO film. The film is mainly...
The thickness is 50 mm. (d) EDX spectrum of rGO paper. There remains little oxygen atoms. (e) Schematic view of the measurement system. A triangular rGO structure is tested. (f) Schematic view of the devices.

The thermal rectification coefficient is defined as $R = \frac{P_-}{P_+}$, where $P_+$ and $P_-$ are the heat power in the positive and negative directions, respectively. With the increase of $\Delta T$, heat power monotonically increases. The experimental results for $W_{\text{bottom}}/W_{\text{top}} = 9/2$ and 9/7 samples can be found in Supplementary Fig. S6, S7 online. Our measurement system is shown in Fig. 3(a). Figure 3(b) and 3(c) show the monitored point 1 (point 2) temperatures as a function of time under the positive (negative) temperature bias direction, respectively. We also found that the magnitude of the heat power in the negative direction ($P_-$) is significantly larger than that in the positive direction ($P_+$), which corresponds to thermal rectification effect. As shown in Fig. 3(d), the rectification coefficient is 1.06 at $|\Delta T| = 15.3$ K. The measured value of $R$ is 1.10 at $|\Delta T| = 46.5$ K. The inset shows the experimental thermal power $P_+$ and $P_-$ as a function of temperature difference $|\Delta T|$. With the increase of $\Delta T$, thermal power monotonically increases. The experimental results for $W_{\text{bottom}}/W_{\text{top}} = 9/2$ and 9/7 samples can be found as Supplementary Fig. S6, S7 online.

Two-rectangular shaped rGO paper with $W_{\text{bottom}}/W_{\text{top}} = 9/2, 9/5$, and 9/7 are used to address the impact of width ratio. Figure 3(e) shows the heat power versus the $W_{\text{bottom}}/W_{\text{top}}$ ratio of the rGO paper. The heat power $P_+$ in the positive direction stays constant under different width ratio. However, the heat power $P_-$ in the negative direction increases linearly with the $W_{\text{bottom}}/W_{\text{top}}$. As shown in Fig. 3(f), the rectification coefficient increases linearly with the width ratio of the rGO paper. It is indicated that the rectification effect can be enhanced by increasing the ratio of $W_{\text{bottom}}/W_{\text{top}}$.

Combining the results for both triangular and two-rectangular shaped graphene thermal rectifier, it is clear that the thermal rectification effect is more obvious in triangular shaped rGO paper. As the phonon scattering just happens at the junction of the two-rectangular shaped rGO, the rectification of heat power by shape effect is limited. Meanwhile, the phonon scattering happens along the whole bevel edge for the triangular shaped rGO, so it has larger thermal rectification coefficient. This is consistent with the idea proposed by C. Dames that interface thermal contact has negative impact on thermal rectification.

**Discussion**

To understand the underlying mechanism of the rectification phenomenon, we perform finite element simulation to study the heat flux and temperature distribution in the system. For the macroscopic asymmetric shape thermal rectifier, the Fourier’s law can be written as:

$$J = -k|x,T(x)| \frac{dT(x)}{dx}$$

(2)

Where, $x$ is the position, $T(x)$ is the temperature at that position, $k$ is the thermal conductivity of the rGO.

Our simulations are based on a model that the rGO paper is in contact with high and low temperature heat baths. The dimensions of rGO paper are in the range of the experimental observation. In our simulations, we only consider the steady-state case. The temperature dependent thermal conductivity of the rGO paper can be written as:

$$k(h,T) = \left[3.8 \times 10^{-6}T + 1.5 \times 10^{-8}T^2 + 32 \times (1 + 0.5/h)T^{-2}\right]^{-1}$$

(3)
where $T$ is the absolute temperature and $h$ is the thickness of rGO paper.

Natural convection and radiation as the heat transfer mechanism between the system and the surrounding air are established. The surrounding environment is assumed to be stationary air at atmospheric pressure. The finite element modeling is used to perform a steady-state thermal analysis of the system to evaluate temperature profile. Ansys Multiphysics22, a finite element analysis program, is employed.

The simulation results of the temperature distribution under positive heat flux direction and negative direction are shown in Fig. 4(a) and 4(b), respectively. Here, for the positive direction, temperatures at points 1 and 2 are set as 74°C and 27.5°C, respectively. And the temperatures at points 1 and 2 are set as 27.5°C and 74°C in negative direction. It is found that the temperature shows small gradient in wide rectangular shaped rGO and large gradient in narrow rectangular shaped rGO, both in Fig. 4(a) and 4(b). As the thermal conductivity of rGO paper depends on temperature, it is indicated that the averaged total thermal conductivity $k_{av}$ is different in positive and negative directions. We also show the temperature profile (see Supplementary Fig. S8 online) along the two-rectangular shaped sample. In the junction, there exhibits discontinuity in the temperature profile due to the sudden structural changes. The large temperature gradient region is a result of the presence of high

Figure 2 | Testing results of the 60° triangular shaped solid-state thermal rectifier. Monitored temperatures (left axis) and current (right axis) as a function of time at points 1 and 2 of (a) positive direction and (b) negative direction, respectively. Measured (c) heat power and (d) rectification coefficient versus temperature difference $|\Delta T|$. In Figure 2 (c) and (d), the first point is $|\Delta T| = 12.7$ C ($T_1 = 37.9$ C, $T_2 = 25.2$ C in positive direction); The second point is $|\Delta T| = 21.6$ C ($T_1 = 51.3$ C, $T_2 = 29.7$ C in positive direction); The third point is $|\Delta T| = 30.8$ C ($T_1 = 64.1$ C, $T_2 = 33.3$ C in positive direction); The fourth point is $|\Delta T| = 39.1$ C ($T_1 = 76.1$ C, $T_2 = 37$ C in positive direction). Measured (e) heat power and (f) rectification coefficient versus angle $\Theta$ under $|\Delta T| = 40$ K. In Figure 2(f), the first point is $\Theta = 20^\circ$ ($T_1 = 73.4$ C, $T_2 = 33.4$ C in positive direction); The second point is $\Theta = 40^\circ$ ($T_1 = 73.8$ C, $T_2 = 33.8$ C in positive direction); The third point is $\Theta = 60^\circ$ ($T_1 = 77.5$ C, $T_2 = 37.5$ C in positive direction).
resistance to heat flow at the junction, which translates to a reduction in the heat flux of the structure. The asymmetric geometry may lead to different radiation heat losses to the ambient. So the thermal radiation power in positive and negative direction should be compared with the total power. Based on the Stepan-Boltzmann’s law \( F = \sigma T^4 \), the thermal radiation power can be written as:

\[
P_{\text{radiation}} = \sigma T^4 \times S
\]

Where, \( \sigma = 5.67 \times 10^{-8} \text{Wm}^{-2}\text{K}^{-4} \) is the Stepan constant, \( T \) is the absolute temperature and \( S \) is the surface area of the rGO paper. As the temperature is gradient from high to low, the temperature profile is simulated by finite element modeling. Then the thermal radiation power can be calculated by Eq. (4). As shown in Fig. 4(c), the thermal radiation power in positive directions is consistent with that in the negative directions. And both are much lower than the total power. It is indicated that the total power gap for positive and negative directions have little relation with the thermal radiation. So the thermal radiation of rGO paper can be neglected. The rectification effect is mainly caused by thermal conduction. As shown in Fig. 4(d), the calculated rectification coefficient versus the temperature difference \( |\Delta T| \) under \( W_{\text{bot}}/W_{\text{top}} = 4.5 \). We also calculated the heat power and rectification coefficient versus \( W_{\text{bot}}/W_{\text{top}} \) under \( |\Delta T| = 40 \text{ K} \). As shown in Fig. 4(e) and 4(f), the theoretical results are accordance with experimental results.

Figure 3 | Schematic structure and experimental results of the two-rectangular shaped solid-state thermal rectifier. (a) Schematic view of the devices. Monitored temperatures (left axis) and current (right axis) as a function of time at points 1 and 2 of (b) positive direction and (c) negative direction under \( W_{\text{bot}}/W_{\text{top}} = 4.5 \), respectively. (d) Measured rectification coefficient versus temperature difference \( |\Delta T| \) under \( W_{\text{bot}}/W_{\text{top}} = 4.5 \). Inset is heat power versus temperature difference \( |\Delta T| \). In Figure 3 (c) and (d), the first point is \( |\Delta T| = 15.3 \text{ C} \left( T_1 = 37.8 \text{ C}, T_2 = 22.5 \text{ C} \right) \) in positive direction; The second point is \( |\Delta T| = 26.6 \text{ C} \left( T_1 = 51.2 \text{ C}, T_2 = 24.6 \text{ C} \right) \) in positive direction; The third point is \( |\Delta T| = 37.8 \text{ C} \left( T_1 = 64.3 \text{ C}, T_2 = 26.5 \text{ C} \right) \) in positive direction; The fourth point is \( |\Delta T| = 46.5 \text{ C} \left( T_1 = 74 \text{ C}, T_2 = 27.5 \text{ C} \right) \) in positive direction. Measured (e) heat power and (f) rectifying coefficient versus \( W_{\text{bot}}/W_{\text{top}} \) under \( |\Delta T| = 40 \text{ K} \). In Figure 3(f), the first point is \( W_{\text{bot}}/W_{\text{top}} = 9/7 \left( T_1 = 69.6 \text{ C}, T_2 = 29.6 \text{ C} \right) \) in positive direction; The second point is \( W_{\text{bot}}/W_{\text{top}} = 9/5 \left( T_1 = 68.5 \text{ C}, T_2 = 28.5 \text{ C} \right) \) in positive direction; The third point is \( W_{\text{bot}}/W_{\text{top}} = 9/2 \left( T_1 = 66.9 \text{ C}, T_2 = 26.9 \text{ C} \right) \) in positive direction.
As rGO paper is sensitive to humidity, we make a contrast experiment to verify the effect of humidity on our measurement. There is no obvious change before and after dry (see Supplementary Fig. S9 online). It is indicated that humidity has little impact on our experiment results.

From our simulation results, it is obvious that according to the shape effect, the temperature profile depends on the heat flux directions. In the temperature range of our experiment, the thermal conductivity of rGO paper decreases with temperature. For the positive heat flux direction, the wide segment is at high temperature contact, which corresponds to high average temperature and leads to low effective thermal conductivity. In contrary, for the negative heat flux condition, the whole system is under a "lower" average temperature, which results in higher heat flux. Thus the temperature gradient dependent averaged thermal conductivity results in the thermal rectification.

In the two-segment oxide based thermal rectifier\textsuperscript{15,16}, its working mechanism is the different temperature dependence of thermal conductivity. In these two-component systems, the interface thermal contact has negative impact on thermal rectification\textsuperscript{17}. However, thermal interface material is still an emerging area. In this work, we propose to create macroscopic thermal rectifier based on rGO materials. This is a single component system, thus avoiding the issue of interface thermal resistance. Here the rectification ratio depends on the change of thermal conductivity with temperature. Figure 5(a) shows the temperature dependent thermal conductivity of rGO with different thickness, which are calculated according to the empirical fitting equation (3). When temperature is higher than about 200 K, thermal conductivity decreases with temperature, and the slope of the temperature dependent thermal conductivity increase with thickness, converges to a constant value when thickness is beyond 10 μm.

Figure 4 | Finite element modeling (FEM) simulation results of the two-rectangular shaped solid-state thermal rectifier. Simulation results of the temperatures distribution in (a) positive direction and (b) negative direction, respectively. (c) The total heat power (Experiments) and the thermal radiation power (Calculation) versus temperature difference |ΔT|. (d) Calculated and measured rectification coefficient versus the temperature difference |ΔT| under W_{bot}/W_{top}=4.5. Calculated and measured (e) heat power and (f) rectification coefficient versus W_{bot}/W_{top} under |ΔT|=40 K.
Figure 5(b) shows the thickness dependent rectification ratio. As expected, the rectification increases with thickness, and converges when thickness is larger than 10 μm, due to the impact of thickness on temperature dependent thermal conductivity. Furthermore, it is worth to address the advantage of rGO material by comparing with other common used materials. Figure 5(c) shows the temperature dependent thermal conductivity of 50 μm rGO paper, bulk cooper, 700 nm cooper thin film, single crystalline silicon layer and poly silicon. It is obvious that rGO paper has a high thermal conductivity as well as cooper. Moreover, around room temperature, it has more remarkable temperature dependence than those for cooper and single crystalline silicon film. Thus it is expected to result in larger thermal rectification ratio in our proposed rGO materials than those created by cooper and single crystalline silicon films.

In summary, we demonstrated macroscopic thermal rectifier using rGO. The rectifier exhibits rectification which depends on the asymmetric shape. We analyzed the triangular and two-rectangular shaped rGO thermal rectifier experimentally. It is found that 60° triangular shaped sample has a rectification coefficient of 1.28 and the rectification coefficient is increased with the increasing of the angle. In addition, the two-rectangular shaped sample has the rectification coefficient of 1.10 which could also be enhanced by increasing the width ratio. Using finite element modeling, the rectification effect for two-rectangular shaped samples was analyzed. The simulation results were in accordance with that of the experimental results. Although asymmetric heat flux is observed in the rGO system, it is worth to mention that it is not an ideal thermal rectifier, as heat flux in the low heat flux direction is not zero. According to electrical rectifier, an ideal thermal rectifier should "stop" heat flux in one temperature bias direction. This needs further work to reduce the heat flux in the low heat flux direction to make this device for better thermal management performance. Our results shed light on macroscopic phononic device with large-area graphene based materials, and may open up its important applications in thermal circuits and thermal management.

Methods
Sample preparation. Graphene oxide paper was prepared according to the Ref.25, then it was reduced by acid in one hour according to the Ref.26. The rGO detail preparation method is described in supplementary information.

Characterizations. The surface morphology and chemical composition of rGO film were observed by SEM/EDX (DI-3100). The precise chemical composition and structure of rGO film was obtained by the X-ray photoelectron spectroscopy (XPS, Physical Electronics Inc.), X-ray diffractometer (XRD, Rigaku Inc.) and Raman spectroscopy using wavelength of 532 nm (HORIBA Inc.).

Measure system setting up. First, the rGO samples were cut into triangular shape. Then rGO samples are suspended on two heaters. The two resistive heaters with R = 1245 Ω is used to apply heat current I, into the rectifier. The silver paste (Kyocera Chemical CT285) is used to establish good thermal contact between heaters and samples. The heaters are placed on the foam to reduce the heat leakage from the substrate. Two micro thermocouples with 50 μm dimension (KRC ST-50) are attached on two sides of the rectifier to monitor the temperature in the presence of the heat current. At last, a radiation shield is covered on the whole system to protect the heat fluctuation from the environment.

Test methods. To explore the thermal rectification effect, first, the electrical current is applied to one of the heater. This establishes a temperature bias between the two sides. Here we denote the positive heat flux direction when the bottom of rGO paper (point 1 as shown in figure 2) is at a higher temperature, and the negative heat flux direction when the top (point 2) is at a higher temperature. When the system arrives at non-equilibrium stationary state, we record the input power of the heater. In our measurements, we keep the same stationary state temperature difference |ΔT| for both positive and negative temperature bias direction, and record the heat power in the positive direction (P+) and negative direction (P-), respectively. If the thermal rectification effect existed in the system, the value of P+ and P- should be different. The similar approach has been used by D. Sawaki et al. to study the thermal rectification in oxide materials16.
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Author contribution

H.T. made and tested the samples, simulated the results and wrote the manuscript. T.L.R. and G.Z. oversaw all research phases, optimized the devices performance and revised the manuscript. D.X. analysed the test results and revised the manuscript. L.T.L. guided the experiment and revised the manuscript.

Additional information

Supplementary information accompanies this paper at http://www.nature.com/scientificreports

Competing financial interests: The authors declare no competing financial interests.

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