Measurement of the Inclusive Jet Cross Section using the $k_T$ algorithm in $p\bar{p}$ Collisions at $\sqrt{s} = 1.96$ TeV with the CDF II Detector

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We report on measurements of the inclusive jet production cross section as a function of the jet transverse momentum in $pp$ collisions at $\sqrt{s} = 1.96$ TeV, using the $k_T$ algorithm and a data sample corresponding to $1.0 \, fb^{-1}$ collected with the Collider Detector at Fermilab in Run II. The measurements are carried out in five different jet rapidity regions with $|y_{\text{jet}}| < 2.1$ and transverse momentum in the range $54 < p_T^{\text{jet}} < 700$ GeV/c. Next-to-leading order perturbative QCD predictions are in good agreement with the measured cross sections.

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I. INTRODUCTION

The measurement of the inclusive jet cross section as a function of the jet transverse momentum, $p_T^{\text{jet}}$, in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV constitutes a test of perturbative quantum chromodynamics (pQCD) [1]. In Run II of the Tevatron, measurements of the jet cross section for jets with $p_T^{\text{jet}}$ up to about 700 GeV/c [2, 3] have extended the $p_T^{\text{jet}}$ range by more than 150 GeV/c compared to Run I [4]. In particular, the CDF collaboration recently published results [2] on inclusive jet production using the $k_T$ algorithm [5] for jets with $p_T^{\text{jet}} > 54$ GeV/c and rapidity $0.1 < |y| < 0.7$, which are well described by next-to-leading order (NLO) pQCD predictions [6]. As discussed in [2], the $k_T$ algorithm has been widely used for precise QCD measurements at both $e^+e^-$ and $e^+p$ colliders, and makes possible a well defined comparison to the theoretical predictions [8]. The pQCD calculations involve matrix elements, describing the hard interaction between partons, convoluted with parton density functions (PDFs) [11, 12] in the proton and antiproton that require input from experiment. The pQCD predictions are affected by the still-limited knowledge of the gluon PDF, which translates into a large uncertainty on the theoretical cross sections at high $p_T^{\text{jet}}$ [2, 3]. Inclusive jet cross section measurements from Run I at the Tevatron [5], performed in different jet rapidity regions, have been used to partially constrain the gluon distribution in the proton. This article continues the studies on jet production using the $k_T$ algorithm at the Tevatron [2, 5] and presents new measurements of the inclusive jet production cross section as a function of $p_T^{\text{jet}}$ in five different jet rapidity regions up to $|y| = 2.1$, based on 1.0 fb$^{-1}$ of CDF Run II data. The measurements are corrected to the hadron level [13] and compared to NLO pQCD predictions.

II. EXPERIMENTAL SETUP

The CDF II detector (see Fig. 1) is described in detail in [14]. The sub-detectors most relevant for this analysis are discussed briefly here. The detector has a charged particle tracking system immersed in a 1.4 T magnetic field. A silicon microstrip detector [15] provides tracking over the radial range 1.35 to 28 cm and covers the pseudorapidity range $|\eta| < 2. The 3.1-m-long open-cell drift chamber [16] covers the radial range from 44 to 132 cm and provides $D_{\text{min}}$ separation. All $k_T$ of the $i$th protojet, $\Delta R_{i,j}$ is the distance ($y - \phi$ space) between each pair of protojets, and $D$ is a parameter that approximately controls the size of the jet by limiting, in each iteration, the clustering of protojets according to their spacial separation. All $k_{T,i}$ and $k_{T,(i,j)}$ values are then collected into a single sorted list. In this list, if the smallest quantity is of the type $k_{T,i}$, the corresponding protojet is promoted to be a jet and removed from the list. Otherwise, if

$$k_{T,i} = p_T^2_{T,i}; \quad k_{T,(i,j)} = \min(p_T^2_{T,i}, p_T^2_{T,j}) \cdot \Delta R_{i,j}^2 / D^2,$$ (1)

are computed for each protojet and pair of protojets, respectively, where $p_{T,i}$ denotes the transverse momentum of the $i$th protojet, $\Delta R_{i,j}$ is the distance ($y - \phi$ space) between each pair of protojets, and $D$ is a parameter that approximately controls the size of the jet by limiting, in each iteration, the clustering of protojets according to their spacial separation. All $k_{T,i}$ and $k_{T,(i,j)}$ values are then collected into a single sorted list. In this list, if the smallest quantity is of the type $k_{T,i}$, the corresponding protojet is promoted to be a jet and removed from the list. Otherwise, if

III. JET RECONSTRUCTION

The $k_T$ algorithm [5] is used to reconstruct jets from the energy depositions in the calorimeter towers in both data and Monte Carlo simulated events (see Section VI). For each calorimeter tower, the four-momenta [21] of its electromagnetic and hadronic sections are summed to define a physics tower. First, all physics towers with transverse momentum above 0.1 GeV/c are considered as protojets. The quantities

$$k_{T,i} = p_T^2_{T,i}; \quad k_{T,(i,j)} = \min(p_T^2_{T,i}, p_T^2_{T,j}) \cdot \Delta R_{i,j}^2 / D^2,$$ (1)

are computed for each protojet and pair of protojets, respectively, where $p_{T,i}$ denotes the transverse momentum of the $i$th protojet, $\Delta R_{i,j}$ is the distance ($y - \phi$ space) between each pair of protojets, and $D$ is a parameter that approximately controls the size of the jet by limiting, in each iteration, the clustering of protojets according to their spacial separation. All $k_{T,i}$ and $k_{T,(i,j)}$ values are then collected into a single sorted list. In this list, if the smallest quantity is of the type $k_{T,i}$, the corresponding protojet is promoted to be a jet and removed from the list. Otherwise, if
the smallest quantity is of the type $k_{T,(i,j)}$, the protojets are combined into a single protojet by summing up their four-vector components. The procedure is iterated over protojets until the list is empty. The jet transverse momentum, rapidity, and azimuthal angle are denoted as $p_{T,jet}$, $y_{jet}$, and $\phi_{jet}$, respectively.

In the Monte Carlo event samples, the same jet algorithm is also applied to the final-state particles, considering all particles as protojets, to search for jets at the hadron level. The resulting hadron-level jet variables are denoted as $p_{T, had}$, $y_{had}$, and $\phi_{had}$.

### IV. EVENT SELECTION

Events are selected online using a three-level trigger system with unique sets of selection criteria called paths. For the different trigger paths used in this measurement, this selection is based on the measured energy deposits in the calorimeter towers, with different thresholds on the jet $E_T$ and different prescale factors (see Table I). In the first-level trigger, a single trigger tower with $E_T$ above 5 GeV or 10 GeV, depending on the trigger path, is required. In the second-level trigger, calorimeter clusters are formed around the selected trigger towers. The events are required to have at least one second-level trigger cluster with $E_T$ above a given threshold, which varies between 15 and 90 GeV for the different trigger paths. In the third-level trigger, jets are reconstructed using the CDF Run I cone algorithm, and the events are required to have at least one jet with $E_T$ above 20 to 100 GeV.

| Trigger Path | Level 1 tower $E_T$ [GeV] | Level 2 cluster $E_T$ [GeV] | Level 3 jet $E_T$ [GeV] | eff. prescale |
|--------------|---------------------------|----------------------------|-------------------------|--------------|
| JET 20       | 5                         | 15                         | 20                      | 775          |
| JET 50       | 5                         | 10                         | 10                      | 34           |
| JET 70       | 10                        | 40                         | 50                      | 8            |
| JET 100      | 10                        | 90                         | 100                     | 1            |

**TABLE I: Summary of trigger paths, trigger thresholds and effective prescale factors employed to collect the data.**

Jets are then reconstructed using the $k_T$ algorithm, as explained in Section III, with $D = 0.7$. For each trigger path, the minimum $p_{T,cal}$, in each $|y_{cal}|$ region, is chosen in such a way that the trigger selection is fully efficient. The efficiency for a given trigger path is obtained using events from a different trigger path with lower transverse energy thresholds (see Table I). In the case of the JET 20 trigger path, the trigger efficiency is extracted from additional control samples, which include a sample with only first-level trigger requirements as well as data collected using unbiased trigger paths with no requirement on the energy deposits in the calorimeter towers. As an example, for jets in the region $0.1 < |y_{cal}| < 0.7$, Fig. 2 shows the trigger efficiency as a function of $p_{T,cal}$ for the different samples. The following selection criteria have been imposed:

1. Events are required to have at least one reconstructed primary vertex with $z$-position within 60 cm of the nominal interaction point. This partially removes beam-related backgrounds and ensures a well-understood event-by-event jet kinematics.

2. Events are required to have at least one jet with rapidity in the region $|y_{cal}| < 2.1$ and corrected $p_{T,cal}$ (see Section IX) above 54 GeV/$c$, which constitutes the minimum jet transverse momentum considered in the analysis. The measurements are limited to jets with $|y_{cal}| < 2.1$ to avoid contributions from the $p$ and $\bar{p}$ remnants that would affect the measured $p_{T,cal}$ in the most forward region of the calorimeter.

3. In order to remove beam-related backgrounds and cosmic rays, the events are required to fulfill $B_T/\sqrt{\Sigma E_T} < F(p_{T,cal})$, where $B_T$ denotes the missing transverse energy and $\Sigma E_T = \sum E_T$ is the total transverse energy of the event, as measured using calorimeter towers with $E_T$ above 0.1 GeV. The threshold function $F(p_{T,cal})$ is defined as $F(p_{T,cal}) = \min(2+0.0125 \times p_{T,cal}, 7)$, where $p_{T,cal}$ is the uncorrected transverse momentum of the leading jet in GeV/$c$, and $F$ is in GeV$^{1/2}$. This criterion preserves more than 95% of the QCD events, as determined from Monte Carlo studies (see Section VI). A visual scan of events with $p_{T,cal} > 400$ GeV/$c$ did not show remaining backgrounds.

Measurements are carried out in five different jet rapidity regions: $|y_{cal}| < 0.1$, $0.1 < |y_{cal}| < 0.7$, $0.7 < |y_{cal}| < 1.1$, $1.1 < |y_{cal}| < 1.6$, and $1.6 < |y_{cal}| < 2.1$, where the different boundaries are chosen to reduce systematic effects coming from the layout of the calorimeter system.
V. EFFECT OF MULTIPLE $p\bar{p}$ INTERACTIONS

The measured $p_{T,\text{cal}}^{\text{jet}}$ includes contributions from multiple $p\bar{p}$ interactions per bunch crossing at high instantaneous luminosity, $L_{\text{inst}}$. The data used in this measurement were collected at $L_{\text{inst}}$ between 0.2 × 10^{31} cm^{-2}s^{-1} and 16.3 × 10^{31} cm^{-2}s^{-1} with an average of 4.1 × 10^{31} cm^{-2}s^{-1}. On average, 1.5 inelastic $p\bar{p}$ interactions per bunch crossing are expected. At the highest $L_{\text{inst}}$ considered, an average of 5.9 interactions per bunch crossing are produced. This mainly affects the measured cross section at low $p_{T,\text{cal}}^{\text{jet}}$, where the contributions are sizeable. Multiple interactions are identified via the presence of additional primary vertices reconstructed from charged particles. The measured jet transverse momenta are corrected for this effect by removing a certain amount of transverse momentum, $\delta_{p_{T}}^{\text{mi}} \times (N_{V} - 1)$, where $N_{V}$ denotes the number of reconstructed primary vertices in the event and $\delta_{p_{T}}^{\text{mi}}$ is determined from dedicated studies of jets implemented in the HERWIG package. The simulation systematic underestimates the measured jet shapes in Run II. In the case of PYTHIA, fragmentation into hadrons is carried out using the string model as implemented in JETSET, while HERWIG implements the cluster model.

VI. MONTE CARLO SIMULATION

Monte Carlo simulated event samples are used to determine the response of the detector and the correction factors to the hadron level. The generated samples are passed through a full CDF II detector simulation (based on GEANT3, where the GFLASH package is used to simulate the energy deposition in the calorimeters) and then reconstructed and analyzed using the same analysis chain as used for the data.

Samples of simulated inclusive jet events have been generated with PYTHIA 6.203 and HERWIG 6.4 Monte Carlo generators, using CTEQ5L PDFs. The PYTHIA samples have been created using a specially tuned set of parameters, denoted as PYTHIA-TUNE A, that includes enhanced contributions from initial-state gluon radiation and secondary parton interactions between remnants. The parameters were determined from dedicated studies of the underlying event using the CDF Run I data and has been shown to properly describe the measured jet shapes in Run II. In the case of PYTHIA, fragmentation into hadrons is carried out using the string model as implemented in JETSET, while HERWIG implements the cluster model.

VII. SIMULATION OF THE CALORIMETER RESPONSE TO JETS

Dedicated studies have been performed to validate the Monte Carlo simulation of the calorimeter response to jets for the different $|y_{\text{cal}}|$ regions. Previous analyses for jets with $0.1 < |y_{\text{cal}}| < 0.7$ indicate that the simulation properly reproduces both the average $p_{T,\text{cal}}^{\text{jet}}$ and the jet momentum resolution, $\sigma_{p_{T}}^{\text{jet}}$, as measured in the data. The study is performed for the rest of the $|y_{\text{cal}}|$ regions using jets in the range $0.1 < |y_{\text{cal}}| < 0.7$ as a reference. An exclusive dijet sample is selected, in data and simulated events, with the following criteria:

1. Events are required to have one and only one reconstructed primary vertex with z-position within 60 cm of the nominal interaction point.
2. Events are required to have exactly two jets with $p_{T,\text{cal}}^{\text{jet}} > 10$ GeV/c, where one of the jets must be in the region $0.1 < |y_{\text{cal}}| < 0.7$.
3. $H_{T}/\sqrt{\sum E_{T}} < F(p_{T,\text{cal}}^{\text{jet1}})$, as explained in Section IV.

The bisector method is applied to data and simulated exclusive dijet events to test the accuracy of the simulated $\sigma_{p_{T}}^{\text{jet}}$ in the detector. The study indicates that the simulation systematically underestimates the measured $\sigma_{p_{T}}^{\text{jet}}$ by 6% and 10% for jets in the regions $0.7 < |y_{\text{cal}}| < 1.1$ and $1.6 < |y_{\text{cal}}| < 2.1$, respectively, with no significant $p_{T,\text{cal}}^{\text{jet}}$ dependence. An additional smearing of the reconstructed $p_{T,\text{cal}}^{\text{jet}}$ is applied to the simulated events to account for this effect. In the region $1.1 < |y_{\text{cal}}| < 1.6$, the measured $\sigma_{p_{T}}^{\text{jet}}$ is overestimated by 5% in the simulation. The effect on the final result is included via slightly modified unfolding factors (see Section IX). For jets with $|y_{\text{cal}}| < 0.1$, the simulation properly describes the measured $\sigma_{p_{T}}^{\text{jet}}$. Figure shows the ratio between $\sigma_{p_{T}}^{\text{jet}}$ in data and simulated events, $\sigma_{p_{T}}^{\text{data}}/\sigma_{p_{T}}^{\text{mc}}$, in different $|y_{\text{cal}}|$ regions as a function of the average $p_{T,\text{cal}}^{\text{jet}}$ of the dijet event. After corrections have been applied to the simulated events, data and simulation agree. In the region $1.1 < |y_{\text{cal}}| < 1.6$, and only for the
purpose of presentation, a 5% smearing of the reconstructed $p_{T,\text{cal}}^{\text{jet}}$ is applied to the data to show the resulting good agreement with the uncorrected simulated resolution. The relative difference between data and simulated resolutions is conservatively taken to be ±8% (see Fig. 3) over the whole range in $p_{T,\text{cal}}^{\text{jet}}$ and $|y_{\text{cal}}^{\text{jet}}|$ in the evaluation of systematic uncertainties.

The average jet momentum calorimeter response in the simulation is then tested by comparing the $p_{T,\text{cal}}^{\text{jet}}$ balance in data and simulated exclusive dijet events. The variable β, defined as

$$\beta = \frac{1 + (\Delta)}{1 - (\Delta)}, \quad \Delta = \frac{p_{T,\text{cal}}^{\text{test, jet}} - p_{T,\text{cal}}^{\text{ref, jet}}}{p_{T,\text{cal}}^{\text{test, jet}}} + \frac{p_{T,\text{cal}}^{\text{test, jet}}}{p_{T,\text{cal}}^{\text{test, jet}}}$$

is computed in data and simulated events in bins of $(p_{T,\text{cal}}^{\text{test, jet}} + p_{T,\text{cal}}^{\text{ref, jet}})/2$, where $p_{T,\text{cal}}^{\text{ref, jet}}$ denotes the transverse momentum of the jet in the region $0.1 < |y_{\text{cal}}^{\text{jet}}| < 0.7$, and $p_{T,\text{cal}}^{\text{test, jet}}$ is the transverse momentum of the jet in the $|y_{\text{cal}}^{\text{jet}}|$ region under study. Figure 3 presents the ratios $\beta_{\text{data}}/\beta_{\text{mc}}$ as a function of $p_{T,\text{cal}}^{\text{test, jet}}$ in the different $|y_{\text{cal}}^{\text{jet}}|$ bins. The study indicates that small corrections are required around calorimeter gaps, $|y_{\text{cal}}^{\text{jet}}| < 0.1$ and $1.1 < |y_{\text{cal}}^{\text{jet}}| < 1.0$, as well as in the most forward region, $1.6 < |y_{\text{cal}}^{\text{jet}}| < 2.1$. For jets with $|y_{\text{cal}}^{\text{jet}}| > 1.1$, the correction shows a moderate $p_{T,\text{cal}}^{\text{jet}}$ dependence, and several parameterizations are considered to extrapolate to very high $p_{T,\text{cal}}^{\text{jet}}$. The difference observed in the final results, using different parameterizations, is included as part of the total systematic uncertainty.

VIII. RECONSTRUCTION OF THE JET VARIABLES

The jet reconstruction in the detector is studied using Monte Carlo event samples, with modified jet energy response in the calorimeter, as described in the previous section, and pairs of jets at the calorimeter and hadron levels matched in ($y - \phi$) space by requiring $\sqrt{(y_{\text{cal}}^{\text{jet}} - y_{\text{had}}^{\text{jet}})^2 + (\phi_{\text{cal}}^{\text{jet}} - \phi_{\text{had}}^{\text{jet}})^2} < D$. These studies indicate that the angular variables of a jet are reconstructed with no significant systematic shift and with a resolution better than 0.05 units in $y$ and $\phi$ at low $p_{T,\text{cal}}^{\text{jet}}$, improving as $p_{T,\text{cal}}^{\text{jet}}$ increases. The measured $p_{T,\text{cal}}^{\text{jet}}$ systematically underestimates that of the hadron level jet. This is attributed mainly to the non-compensating nature of the calorimeter [17]. For jets with $p_{T,\text{cal}}^{\text{jet}}$ around 50 GeV/c, the jet transverse momentum is reconstructed with an average shift that varies between $-9\%$ and $-30\%$ and a resolution between $10\%$ and $16\%$, depending on the $|y_{\text{cal}}^{\text{jet}}|$ region. The jet reconstruction improves as $p_{T,\text{cal}}^{\text{jet}}$ increases. For jets with $p_{T,\text{cal}}^{\text{jet}}$ around 500 GeV/c, the average shift is $-7\%$ and the resolution is about $7\%$.

IX. UNFOLDING

The measured $p_{T,\text{cal}}^{\text{jet}}$ distributions in the different $|y_{\text{cal}}^{\text{jet}}|$ regions are unfolded back to the hadron level using simulated event samples (see Section VI), after including the modified jet energy response described in Section VII. PYTHIA-TUNE A provides a reasonable description of the different jet and underlying event quantities, and is used to determine the correction factors in the unfolding procedure. In order to avoid any potential bias on the correction factors due to the particular PDF set used during the generation of the simulated samples, which translates into slightly different simulated $p_{T,\text{cal}}^{\text{jet}}$ distributions, the underlying $p_{T,\text{cal}}$ spectrum [40] in PYTHIA-TUNE A is re-weighted until the Monte Carlo samples accurately follow each of the measured $p_{T,\text{cal}}^{\text{jet}}$ distributions. The unfolding is carried out in two steps.

First, an average correction is computed separately in each jet rapidity region using corresponding matched pairs of jets at the calorimeter and hadron levels. The correlation $(p_{T,\text{had}}^{\text{jet}} - p_{T,\text{cal}}^{\text{jet}})$ versus $(p_{T,\text{cal}}^{\text{jet}})$ (see Fig. 4), computed in bins of $(p_{T,\text{had}}^{\text{jet}} + p_{T,\text{cal}}^{\text{jet}})/2$, is used to extract correction factors which are then applied to the measured jets to obtain the corrected transverse momenta, $p_{T,\text{cor}}^{\text{jet}}$. In each jet rapidity region, a cross section is defined as

$$\frac{d^2\sigma}{dp_{T,\text{cor}}^{\text{jet}}dy_{\text{cal}}^{\text{jet}}} = \frac{1}{L} \frac{N_{\text{cor}}^{\text{jet}}}{\Delta p_{T,\text{cor}}^{\text{jet}} \Delta y_{\text{cal}}^{\text{jet}}},$$

where $N_{\text{cor}}^{\text{jet}}$ denotes the number of jets in a given $p_{T,\text{cor}}^{\text{jet}}$ bin, $\Delta p_{T,\text{cor}}^{\text{jet}}$ is the size of the bin, $\Delta y_{\text{cal}}^{\text{jet}}$ denotes the size of the region in $y_{\text{cal}}^{\text{jet}}$, and $L$ is the integrated luminosity. $N_{\text{cor}}^{\text{jet}}$ includes event-by-event weights that account for trigger prescale factors, and $\Delta p_{T,\text{cor}}^{\text{jet}}$ is chosen according to the jet momentum resolution.
Second, each measurement is corrected for acceptance and smearing effects using a bin-by-bin unfolding procedure, which also accounts for the efficiency of the selection criteria. The unfolding factors, defined as

\[ U(p_{T,\text{cor}}^\text{jet}, y_{\text{cal}}^\text{jet}) = \frac{d^2\sigma/dp_{T,\text{had}}^\text{jet}dy_{\text{had}}^\text{jet}}{d^2\sigma/dp_{T,\text{cor}}^\text{jet}dy_{\text{cal}}^\text{jet}} \]  

are extracted from Monte Carlo event samples and applied to the measured \( p_{T,\text{cor}}^\text{jet} \) distributions to obtain the final results. As shown in Fig. 6, the factor \( U(p_{T,\text{cor}}^\text{jet}, y_{\text{cal}}^\text{jet}) \) increases with \( p_{T,\text{cor}}^\text{jet} \) and presents a moderate \( |y_{\text{cal}}^\text{jet}| \) dependence. At low \( p_{T,\text{cor}}^\text{jet} \), the unfolding factor varies between 1.02 and 1.06 for different rapidity regions. For jets with \( p_{T,\text{cor}}^\text{jet} \) of about 300 GeV/c, the factor varies between 1.1 and 1.2, and increases up to 1.3 - 1.4 at very high \( p_{T,\text{cor}}^\text{jet} \). In the region \( 1.1 < |y_{\text{cal}}^\text{jet}| < 1.6 \), the unfolding factor includes an additional correction, \( f_U(p_{T,\text{cor}}^\text{jet}) \), to account for the fact that the simulation overestimates the jet momentum resolution in that region (see Section VII). The factor \( f_U(p_{T,\text{cor}}^\text{jet}) \) is computed from Monte Carlo samples as the ratio between the \( p_{T,\text{had}}^\text{jet} \) distribution smeared using the simulated \( \sigma_{\text{jet}}^\text{had} \) and the one smeared using \( \sigma_{\text{jet}}^\text{data} \) in data as extracted from the bisector method (see Section VII). The factor \( f_U(p_{T,\text{cor}}^\text{jet}) \) is about 1.03 and shows no significant \( p_{T,\text{cor}}^\text{jet} \) dependence.

\[ X. \text{ SYSTEMATIC UNCERTAINTIES} \]

A detailed study of the systematic uncertainties on the measurements has been carried out \[ 11 \]. Tables II-III show the different contributions to the total systematic uncertainty in each \( p_T^\text{jet} \) bin and \( |y^\text{jet}| \) region:

1. The measured jet energies are varied by ±2% at low \( p_T^\text{jet} \) to ±2.7% at high \( p_T^\text{jet} \) to account for the uncertainty on the absolute energy scale in the calorimeter \[ 12 \]. This introduces an uncertainty on the measured cross sections which varies between ±9% at low \( p_T^\text{jet} \) and \(+61\% \) at high \( p_T^\text{jet} \), and dominates the total systematic uncertainty on the different measurements.

2. Several sources of systematic uncertainty on the ratio \( \beta_{\text{data}}/\beta_{\text{mc}} \) are considered for the different \( |y^\text{jet}| \) regions:

   (a) The uncertainty on the definition of the exclusive dijet sample in data and Monte Carlo events introduces a ±0.5% uncertainty on the absolute energy scale for jets outside the region \( 0.1 < |y^\text{jet}| < 0.7 \), which translates into an uncertainty on the cross sections between ±2% at low \( p_T^\text{jet} \) and ±10% at very high \( p_T^\text{jet} \).

   (b) The use of different \( \beta_{\text{data}}/\beta_{\text{mc}} \) parameterizations for jets with \( |y^\text{jet}| > 1.1 \) introduces uncertainties between 12% and 23% at very high \( p_T^\text{jet} \).

   (c) In the region \( 1.1 < |y^\text{jet}| < 1.6 \), an additional \( +0\% \) -3% uncertainty on the measured cross sections, independent of \( p_T^\text{jet} \), accounts for variations in the \( \beta_{\text{data}}/\beta_{\text{mc}} \) ratio due to the overestimation of the jet momentum resolution in the simulated samples.

3. A ±8% uncertainty on the jet momentum resolution introduces an uncertainty between ±2% at low \( p_T^\text{jet} \) and \(+12\% \) at high \( p_T^\text{jet} \).

4. The unfolding procedure is repeated using HERWIG instead of PYTHIA-TUNE A to account for the uncertainty on the modeling of the parton cascades and the jet fragmentation into hadrons. This translates into an uncertainty on the measured cross sections between ±3% and ±8% at low \( p_T^\text{jet} \) that becomes negligible at very high \( p_T^\text{jet} \).

5. The unfolding procedure is also carried out using unweighted PYTHIA-TUNE A, to estimate the residual dependence on the \( p_T^\text{jet} \) spectra. This introduces an uncertainty of about ±3% to ±7% at very high \( p_T^\text{jet} \), which becomes negligible at low \( p_T^\text{jet} \).

6. The quoted ±0.23 GeV/c uncertainty on \( \delta_{\text{p}}^\text{mi} \) is taken into account. The maximal effect on the measured cross sections is about ±2%.

7. Different sources of systematic uncertainty related to the selection criteria are considered. The threshold on the \( z \)-position of the primary vertex is varied by ±5 cm in data and simulated events. The lower edge of each \( p_T^\text{jet,cal} \) bin is varied by ±3% in data and simulated events. The \( E_T \) scale is varied by ±10% in the data. The total effect on the measured cross sections is smaller than 1% and considered negligible.
Positive and negative deviations with respect to the nominal values in each $p_T^{\text{jet}}$ bin are added separately in quadrature. Figure 8 shows the total systematic uncertainty as a function of $p_T^{\text{jet}}$ in the different $|y^{\text{jet}}|$ regions, where an additional 5.8% uncertainty on the total luminosity is not included.

**XI. QCD Predictions**

The measurements are compared to parton-level NLO pQCD predictions, as computed using JETRAD [10] with CTEQ6.1M PDFs [11] and the renormalization and factorization scales ($\mu_R$ and $\mu_F$) both set to $\mu_0 = \max(p_T^{\text{jet}})/2$. Different sources of uncertainty on the theoretical predictions are considered. The main contribution comes from the uncertainty on the PDFs and is computed using the Hessian method [13]. At low $p_T^{\text{jet}}$, the uncertainty is about ±5% and approximately independent of $y^{\text{jet}}$. The uncertainty increases as $p_T^{\text{jet}}$ and $|y^{\text{jet}}|$ increase. At very high $p_T^{\text{jet}}$, the uncertainty varies between -30% and +40% for jets with $|y^{\text{jet}}| < 0.1$ and 1.6 < $|y^{\text{jet}}| < 2.1$, respectively, and it is dominated by the limited knowledge of the gluon PDF. An increase of $\mu_R$ and $\mu_F$ from $\mu_0$ to 2$\mu_0$ changes the theoretical predictions by only a few percent. Values significantly smaller than $\mu_0$ lead to unstable NLO results and are not considered.

The theoretical predictions include a correction factor, $C_{\text{HAD}}(p_T^{\text{jet}}, y^{\text{jet}})$, that approximately accounts for non-perturbative contributions from the underlying event and fragmentation of partons into hadrons (see Fig. 8 and Tables IV-V). In each jet rapidity region, $C_{\text{HAD}}$ is estimated, using PYTHIA-TUNE $\lambda$, as the ratio between the nominal $p_T^{\text{jet}}$ distribution and the one obtained after removing the interactions between $p$ and $\bar{p}$ remnants and the fragmentation into hadrons in the Monte Carlo samples. The correction decreases as $p_T^{\text{jet}}$ increases and shows a moderate $|y^{\text{jet}}|$ dependence. At low $p_T^{\text{jet}}$, $C_{\text{HAD}}$ varies between 1.18 and 1.13 as $|y^{\text{jet}}|$ increases, and it becomes of the order of 1.02 at very high $p_T^{\text{jet}}$. The uncertainty on $C_{\text{HAD}}$ varies between ±9% and ±12% at low $p_T^{\text{jet}}$ and decreases to about ±1% at very high $p_T^{\text{jet}}$, as determined from the difference between the parton-to-hadron correction factors obtained using HERWIG instead of PYTHIA-TUNE $\lambda$.

**XII. RESULTS**

The measured inclusive jet cross sections, $d^2\sigma/dp_T^{\text{jet}}dy^{\text{jet}}$, refer to hadron-level jets, reconstructed using the $k_T$ algorithm with $D = 0.7$, in the region $p_T^{\text{jet}} > 54$ GeV/c and $|y^{\text{jet}}| < 2.1$. Figure 9 shows the measured cross sections as a function of $p_T^{\text{jet}}$ in five different $|y^{\text{jet}}|$ regions compared to NLO pQCD predictions. The data are reported in Tables IV-V. The measured cross sections decrease by more than seven to eight orders of magnitude as $p_T^{\text{jet}}$ increases. Figure 10 shows the ratio data/theory as a function of $p_T^{\text{jet}}$ in the five different $|y^{\text{jet}}|$ regions. Good agreement is observed in the whole range in $p_T^{\text{jet}}$ and $y^{\text{jet}}$ between the measured cross sections and the theoretical predictions. In particular, no significant deviation from the pQCD prediction is observed for central jets at high $p_T^{\text{jet}}$. The corresponding $\chi^2$ tests, relative to the nominal pQCD prediction and performed separately in each $|y^{\text{jet}}|$ region, give probabilities that vary between 9% and 90%. A global $\chi^2$ test, applied to all the data points in all $|y^{\text{jet}}|$ regions simultaneously, gives a probability of 7%. In both cases, a detailed treatment of correlations between systematic uncertainties was considered, as discussed in Appendix A. In addition, Fig. 10 shows the ratio of pQCD predictions using MRST2004 [12] and CTEQ6.1M PDF sets, well inside the theoretical and experimental uncertainties. The uncertainty on the measured cross sections at high $p_T^{\text{jet}}$, compared to that on the theoretical predictions, indicates that the data presented in this article will contribute to a better understanding of the gluon PDF.

Finally, in the region $0.1 < |y^{\text{jet}}| < 0.7$, the analysis is repeated using different values for $D$ in the $k_T$ algorithm: $D = 0.5$ and $D = 1.0$. In both cases, good agreement is observed between the measured cross sections and the NLO pQCD predictions in the whole range in $p_T^{\text{jet}}$ (see Fig. 11 and Tables VI-VII). The corresponding $\chi^2$ tests give probabilities of 84% and 22% for $D = 0.5$ and $D = 1.0$, respectively. As $D$ decreases, the measurement is less sensitive to contributions from multiple $p\bar{p}$ interactions per bunch crossing, and the presence and proper modeling of the underlying event. For $D = 0.5$ ($D = 1.0$), the value for $\delta^{\text{semi}}_{\text{pt}}$ becomes $1.18 \pm 0.12 (3.31 \pm 0.47)$ GeV/c, and the parton-to-hadron correction factor applied to the pQCD predictions is $C_{\text{HAD}} = 1.1$ ($C_{\text{HAD}} = 1.4$) at low $p_T^{\text{jet}}$. 
XIII. SUMMARY AND CONCLUSIONS

We have presented results on inclusive jet production in \( p\bar{p} \) collisions at \( \sqrt{s} = 1.96 \) TeV for jets with transverse momentum \( p_T^{\text{jet}} > 54 \) GeV/c and rapidity in the region \( |y^{\text{jet}}| < 2.1 \), using the \( k_T \) algorithm and based on 1.0 fb\(^{-1}\) of CDF Run II data. The measured cross sections are in agreement with NLO pQCD predictions after the necessary non-perturbative parton-to-hadron corrections are taken into account. The results reported in this article should contribute to a better understanding of the gluon PDF inside the proton when used in QCD global fits.

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FIG. 1: Elevation view of one half of the CDF detector displaying the components of the CDF calorimeter.

FIG. 2: Measured trigger efficiencies as a function of $p_{T,\text{cal}}^{\text{jet}}$ for different trigger paths and in the region $0.1 < |y_{\text{cal}}^{\text{jet}}| < 0.7$. 
FIG. 3: Ratio $\sigma^\text{data}_{T,T,CAL} / \sigma^\text{mc}_{T,T,CAL}$ as a function of the average $p^\text{jet}_{T,CAL}$ of the dijet event, in different $|y^\text{jet}_{CAL}|$ regions, before (black squares) and after (open circles) corrections have been applied (see Section VII). The solid lines are fits to the corrected ratios. The dashed lines indicate a ±8% relative variation considered in the study of systematic uncertainties.

FIG. 4: Ratio $\beta_{\text{data}} / \beta_{\text{mc}}$ as a function of $p^\text{jet}_{T,CAL}$ in different $|y^\text{jet}_{CAL}|$ regions. The solid lines show the nominal parameterizations based on fits to the ratios. In the region $|y^\text{jet}_{CAL}| > 1.1$, the dashed lines indicate different parameterizations used to describe the ratios at high $p^\text{jet}_{T,CAL}$, and are considered in the study of systematic uncertainties.
FIG. 5: Correlation $\langle p_{T, \text{had}}^{\text{jet}} - p_{T, \text{cal}}^{\text{jet}} \rangle$ versus $\langle p_{T, \text{cal}}^{\text{jet}} \rangle$, as extracted from PYTHIA TUNE A simulated event samples, in the different $|y^{\text{jet}}_{\text{cal}}|$ regions.

FIG. 6: Unfolding factors, $U(p_{T, \text{cor}}^{\text{jet}}, y^{\text{jet}}_{\text{cal}})$, as extracted from PYTHIA TUNE A simulated event samples, as a function of $p_{T, \text{cor}}^{\text{jet}}$ in the different $|y^{\text{jet}}_{\text{cal}}|$ regions.
FIG. 7: Total systematic uncertainty (in percent) on the measured inclusive differential jet cross sections as a function $p_T^{\text{jet}}$ for the different $|y^{\text{jet}}|$ regions (see Tables II-III). An additional 5.8% uncertainty on the integrated luminosity is not included.
FIG. 8: Magnitude of the parton-to-hadron correction, $C_{\text{HAD}}(p_T^{\text{jet}}, y^{\text{jet}})$, used to correct the NLO pQCD predictions (see Tables IV-V). The shaded bands indicate the quoted Monte Carlo modeling uncertainty.
FIG. 9: Measured inclusive differential jet cross sections (black squares) as a function of $p_T^{\text{jet}}$ for jets with $p_T^{\text{jet}} > 54$ GeV/c in different $|y^{\text{jet}}|$ regions compared to NLO pQCD predictions (open circles). The shaded bands show the systematic uncertainty on the measurements (see Tables IV-V). A 5.8% uncertainty on the integrated luminosity is not included. The dashed lines indicate the PDF uncertainty on the theoretical predictions. For presentation, the measurements in different $|y^{\text{jet}}|$ regions are scaled by different global factors. Factors ($\times10^6$), ($\times10^3$), ($\times10^{-3}$), and ($\times10^{-6}$) are used in the regions $|y^{\text{jet}}| < 0.1$, $0.1 < |y^{\text{jet}}| < 0.7$, $1.1 < |y^{\text{jet}}| < 1.6$, and $1.6 < |y^{\text{jet}}| < 2.1$, respectively.
FIG. 10: Ratio data/theory as a function of $p_T^{\text{jet}}$ in different $|y^{\text{jet}}|$ regions. The error bars (shaded bands) show the total statistical (systematic) uncertainty on the data. A 5.8% uncertainty on the integrated luminosity is not included. The dashed lines indicate the PDF uncertainty on the theoretical predictions. The dotted lines present the ratio of NLO pQCD predictions using MRST2004 and CTEQ6.1M PDFs. The dotted-dashed lines show the ratios of pQCD predictions with $2\mu_0$ and $\mu_0$. 
$JET_T p_T = \max p_T^{\mu} / 2 = \mu_0$

CDF data ( $L = 1.0$ fb$^{-1}$ )

$\sigma^2$ corrected to hadron level

$\mu_R = \mu_F = \max p_T^{\mu} / 2 = \mu_0$

PDF uncertainties

$0.1 < |y^{JET}| < 0.7$

$D=0.5$

$D=1.0$

|<0.7|<0.7

$C_{HAD}(p_T^{JET})$

Monte Carlo modeling uncertainties

FIG. 11: (top) Measured inclusive differential jet cross sections (black squares) as a function of $p_T^{JET}$ for jets with $p_T^{JET} > 54$ GeV/c and $0.1 < |y^{JET}| < 0.7$ using the $k_T$ parameter $D = 0.5$ (left) and $D = 1.0$ (right), compared to NLO pQCD predictions (open circles). The shaded bands show the total systematic uncertainty on the measurements (see Tables VI-VII). A 5.8% uncertainty on the integrated luminosity is not included. The dashed lines indicate the PDF uncertainty on the theoretical predictions. (middle) Ratio data/theory as a function of $p_T^{JET}$ for $D = 0.5$ (left) and $D = 1.0$ (right). (bottom) Magnitude of the parton-to-hadron corrections, $C_{HAD}(p_T^{JET})$, used to correct the NLO pQCD predictions for $D = 0.5$ (left) and $D = 1.0$ (right). The shaded bands indicate the quoted Monte Carlo modeling uncertainty.
### Systematic uncertainties \(\%\) \((|y^{\text{jet}}| < 0.1)\)

| \(p_T^{\text{jet}}\) [GeV/c] | jet energy scale | \(\beta_{\text{data}}/\beta_{\text{MC}}\) | resolution | unfolding | \(p_T^{\text{jet}}\)-spectra | \(\sigma_{\text{mi}}\) |
|---------------------|----------------|----------------|------------|-----------|-----------------|----------|
| 54 - 62             | +10.3          | +1.4           | –          | –         | +2.8            | ±5.3     | ±3.0            |
| 62 - 72             | –9.3           | –2.1           | –          | –         | –3.0            | ±5.3     | ±3.0            |
| 72 - 83             | –9.4           | –2.1           | –          | –         | –3.0            | ±5.3     | ±3.0            |
| 83 - 96             | –9.4           | –2.1           | –          | –         | –3.0            | ±5.3     | ±3.0            |
| 96 - 110            | +9.5           | +2.3           | –         | –         | +2.9            | ±4.7     | ±1.0            |
| 110 - 127           | +9.8           | +2.5           | –         | –         | +3.0            | ±4.2     | ±0.9            |
| 127 - 146           | +10.4          | +2.7           | –         | –         | +3.1            | ±3.7     | ±0.8            |
| 146 - 169           | +11.2          | +2.8           | –         | –         | ±3.1            | ±3.7     | ±0.8            |
| 169 - 195           | +12.4          | +2.9           | –         | –         | ±3.3            | ±2.8     | ±0.5            |
| 195 - 224           | +13.9          | +3.0           | –         | –         | ±3.4            | ±2.5     | ±0.4            |
| 224 - 259           | +15.5          | +3.1           | –         | –         | ±3.7            | ±2.2     | ±0.3            |
| 259 - 298           | +17.4          | +3.3           | –         | –         | ±4.0            | ±2.0     | ±0.4            |
| 298 - 344           | +19.5          | +3.6           | –         | –         | ±4.3            | ±1.8     | ±0.6            |
| 344 - 396           | +22.1          | +4.0           | –         | –         | ±4.8            | ±1.0     | ±0.4            |
| 396 - 457           | +25.7          | +4.6           | –         | –         | ±5.4            | ±1.4     | ±0.8            |
| 457 - 527           | +31.3          | +5.3           | –         | –         | ±6.1            | ±1.3     | ±0.5            |
| 527 - 700           | +45.7          | +7.3           | –         | –         | ±7.4            | ±1.1     | ±0.3            |

### Systematic uncertainties \(\%\) \((0.1 < |y^{\text{jet}}| < 0.7)\)

| \(p_T^{\text{jet}}\) [GeV/c] | jet energy scale | \(\beta_{\text{data}}/\beta_{\text{MC}}\) | resolution | unfolding | \(p_T^{\text{jet}}\)-spectra | \(\sigma_{\text{mi}}\) |
|---------------------|----------------|----------------|------------|-----------|-----------------|----------|
| 54 - 62             | +9.5           | –              | –          | –         | +2.2            | ±5.3     | ±0.6            |
| 62 - 72             | +9.4           | –              | –          | –         | ±2.5            | ±5.3     | ±0.6            |
| 72 - 83             | –9.1           | –              | –          | –         | ±2.1            | ±5.3     | ±0.6            |
| 83 - 96             | –9.4           | –              | –          | –         | ±2.4            | ±5.3     | ±0.6            |
| 96 - 110            | –9.9           | –              | –          | –         | ±2.4            | ±5.3     | ±0.6            |
| 110 - 127           | –9.9           | –              | –          | –         | ±2.4            | ±5.3     | ±0.6            |
| 127 - 146           | –10.6          | –              | –          | –         | ±1.9            | ±5.3     | ±0.6            |
| 146 - 169           | –11.4          | –              | –          | –         | ±1.9            | ±5.3     | ±0.6            |
| 169 - 195           | –10.6          | –              | –          | –         | ±2.0            | ±5.3     | ±0.6            |
| 195 - 224           | –11.7          | –              | –          | –         | ±2.0            | ±5.3     | ±0.6            |
| 224 - 259           | –14.6          | –              | –          | –         | ±2.0            | ±5.3     | ±0.6            |
| 259 - 298           | –18.9          | –              | –          | –         | ±2.0            | ±5.3     | ±0.6            |
| 298 - 344           | –23.3          | –              | –          | –         | ±2.0            | ±5.3     | ±0.6            |
| 344 - 396           | –27.8          | –              | –          | –         | ±2.0            | ±5.3     | ±0.6            |

**TABLE II:** Systematic uncertainties (in percent) on the measured inclusive jet differential cross section as a function of \(p_T^{\text{jet}}\) for jets in the regions \(|y^{\text{jet}}| < 0.1\) and \(0.1 < |y^{\text{jet}}| < 0.7\) (see Fig. 2). The different columns follow the discussion in Section X. An additional 5.8\% uncertainty on the integrated luminosity is not included.
### Systematic uncertainties \( (0.7 < |y^{\text{jet}}| < 1.1) \)

| \( p_T^{\text{jet}} \) [GeV/c] | \( \beta_{\text{data}}/\beta_{\text{MC}} \) resolution unfolding \( p_T^{\text{jet}} \)-spectra \( \delta_{\text{mu}}^{\text{AT}} \) |
|---|---|---|---|
| 54 - 62 | \( -9.2 \) | \( -2.4 \) | \( -2.1 \) | | | +0.9 | ±6.3 | ±2.0 | ±1.7 |
| 62 - 72 | \( -9.9 \) | \( -2.3 \) | \( -2.2 \) | | | | | | | |
| 72 - 83 | \( -9.3 \) | \( -2.3 \) | \( -2.3 \) | | | | | | | |
| 83 - 96 | \( -9.2 \) | \( -2.3 \) | \( -2.3 \) | | | | | | | |
| 96 - 110 | \( -9.9 \) | \( -2.4 \) | \( -2.4 \) | | | | | | | |
| 110 - 127 | \( -9.3 \) | \( -2.5 \) | \( -2.5 \) | | | | | | | |
| 127 - 146 | \( -9.3 \) | \( -2.6 \) | \( -2.6 \) | | | | | | | |
| 146 - 169 | \( -11.7 \) | \( -2.7 \) | \( -2.7 \) | | | | | | | |
| 169 - 195 | \( -14.1 \) | \( -3.0 \) | \( -3.0 \) | | | | | | | |
| 195 - 224 | \( -15.9 \) | \( -3.3 \) | \( -3.3 \) | | | | | | | |
| 224 - 259 | \( -15.6 \) | \( -3.2 \) | \( -3.2 \) | | | | | | | |
| 259 - 298 | \( -16.5 \) | \( -3.6 \) | \( -3.6 \) | | | | | | | |
| 298 - 344 | \( -19.2 \) | \( -4.1 \) | \( -4.1 \) | | | | | | | |
| 344 - 396 | \( -22.7 \) | \( -4.8 \) | \( -4.8 \) | | | | | | | |
| 396 - 457 | \( -31.5 \) | \( -5.9 \) | \( -5.9 \) | | | | | | | |
| 457 - 527 | \( -55.4 \) | \( -10.4 \) | \( -10.4 \) | | | | | | | |
| 527 - 605 | \( -38.3 \) | \( -7.4 \) | \( -7.4 \) | | | | | | | |

### Systematic uncertainties \( (1.1 < |y^{\text{jet}}| < 1.6) \)

| \( p_T^{\text{jet}} \) [GeV/c] | \( \beta_{\text{data}}/\beta_{\text{MC}} \) resolution unfolding \( p_T^{\text{jet}} \)-spectra \( \delta_{\text{mu}}^{\text{AT}} \) |
|---|---|---|---|
| 54 - 62 | \( -9.4 \) | \( -2.6 \) | \( -2.4 \) | | | +0.9 | ±6.7 | ±1.3 | ±1.8 |
| 62 - 72 | \( -9.5 \) | \( -2.5 \) | \( -2.5 \) | | | | | | | |
| 72 - 83 | \( -9.3 \) | \( -2.5 \) | \( -2.5 \) | | | | | | | |
| 83 - 96 | \( -10.2 \) | \( -2.6 \) | \( -2.6 \) | | | | | | | |
| 96 - 110 | \( -10.5 \) | \( -2.6 \) | \( -2.6 \) | | | | | | | |
| 110 - 127 | \( -11.7 \) | \( -2.7 \) | \( -2.7 \) | | | | | | | |
| 127 - 146 | \( -12.8 \) | \( -2.9 \) | \( -2.9 \) | | | | | | | |
| 146 - 169 | \( -12.6 \) | \( -3.0 \) | \( -3.0 \) | | | | | | | |
| 169 - 195 | \( -16.9 \) | \( -3.8 \) | \( -3.8 \) | | | | | | | |
| 195 - 224 | \( -16.2 \) | \( -3.7 \) | \( -3.7 \) | | | | | | | |
| 224 - 259 | \( -24.7 \) | \( -5.2 \) | \( -5.2 \) | | | | | | | |
| 259 - 298 | \( -29.9 \) | \( -6.2 \) | \( -6.2 \) | | | | | | | |
| 298 - 344 | \( -37.2 \) | \( -7.3 \) | \( -7.3 \) | | | | | | | |
| 344 - 396 | \( -8.6 \) | \( -11.4 \) | \( -11.4 \) | | | | | | | |

### Systematic uncertainties \( (1.6 < |y^{\text{jet}}| < 2.1) \)

| \( p_T^{\text{jet}} \) [GeV/c] | \( \beta_{\text{data}}/\beta_{\text{MC}} \) resolution unfolding \( p_T^{\text{jet}} \)-spectra \( \delta_{\text{mu}}^{\text{AT}} \) |
|---|---|---|---|
| 54 - 62 | \( +11.6 \) | \( +2.5 \) | \( +2.5 \) | | | | | | | |
| 62 - 72 | \( +10.9 \) | \( +2.4 \) | \( +2.4 \) | | | | | | | |
| 72 - 83 | \( +10.9 \) | \( +2.4 \) | \( +2.4 \) | | | | | | | |
| 83 - 96 | \( +11.0 \) | \( +2.6 \) | \( +2.6 \) | | | | | | | |
| 96 - 110 | \( +10.3 \) | \( +2.6 \) | \( +2.6 \) | | | | | | | |
| 110 - 127 | \( +13.7 \) | \( +3.2 \) | \( +3.2 \) | | | | | | | |
| 127 - 146 | \( +16.2 \) | \( +3.7 \) | \( +3.7 \) | | | | | | | |
| 146 - 169 | \( +14.4 \) | \( +3.5 \) | \( +3.5 \) | | | | | | | |
| 169 - 195 | \( +19.2 \) | \( +4.3 \) | \( +4.3 \) | | | | | | | |
| 195 - 224 | \( +18.7 \) | \( +4.9 \) | \( +4.9 \) | | | | | | | |
| 224 - 259 | \( +24.7 \) | \( +5.2 \) | \( +5.2 \) | | | | | | | |
| 259 - 298 | \( +40.0 \) | \( +6.0 \) | \( +6.0 \) | | | | | | | |

**TABLE III:** Systematic uncertainties (in percent) on the measured inclusive jet differential cross section as a function of \( p_T^{\text{jet}} \) for jets in the regions \( 0.7 < |y^{\text{jet}}| < 1.1 \), \( 1.1 < |y^{\text{jet}}| < 1.6 \), and \( 1.6 < |y^{\text{jet}}| < 2.1 \) (see Fig. 7). The different columns follow the discussion in Section X. An additional 5.8% uncertainty on the integrated luminosity is not included.
hadron correction factors, $C_{\text{HAD}}$, are applied to the pQCD predictions (see Fig. 8). The parton-to-hadron correction factors, $C_{\text{HAD}}$, are applied to the pQCD predictions (see Fig. 8).

### Table IV: Measured inclusive jet differential cross section as a function of $p_T^{\text{jet}}$ for jets in the regions $|y^{\text{jet}}| < 0.1$ and $0.1 < |y^{\text{jet}}| < 0.7$ (see Fig. 9). An additional 5.8% uncertainty on the integrated luminosity is not included. The parton-to-hadron correction factors, $C_{\text{HAD}}(p_T^{\text{jet}}, y^{\text{jet}})$, are applied to the pQCD predictions (see Fig. 8).
TABLE V: Measured inclusive jet differential cross section as a function of $|y^{\text{jet}}|$.

| $p_T^{\text{jet}}$ [GeV/c] | $\sigma \pm (\text{stat.}) \pm (\text{sys.})$ [nb/(GeV/c)] | $\text{C}_{\text{HAD}}$ | parton $\rightarrow$ hadron |
|-----------------------------|-------------------------------------------------|----------------|--------------------------------|
| 54 - 62                     | $(12.3 \pm 2.1) \times 10^6$                    | 1.169 $\pm$ 0.125 |
| 62 - 72                     | $(5.48 \pm 0.14) \times 10^6$                   | 1.143 $\pm$ 0.103 |
| 72 - 83                     | $(2.40 \pm 0.02) \times 10^6$                   | 1.120 $\pm$ 0.085 |
| 83 - 96                     | $(1.00 \pm 0.11) \times 10^6$                   | 1.102 $\pm$ 0.070 |
| 96 - 110                    | $(1.15 \pm 0.05) \times 10^{-1}$                | 1.087 $\pm$ 0.057 |
| 110 - 127                   | $(1.73 \pm 0.21) \times 10^{-1}$                | 1.075 $\pm$ 0.047 |
| 127 - 146                   | $(6.83 \pm 0.85) \times 10^{-2}$                | 1.064 $\pm$ 0.038 |
| 146 - 169                   | $(5.02 \pm 0.35) \times 10^{-2}$                | 1.056 $\pm$ 0.031 |
| 169 - 195                   | $(8.95 \pm 1.36) \times 10^{-3}$                | 1.048 $\pm$ 0.024 |
| 195 - 224                   | $(3.04 \pm 0.45) \times 10^{-3}$                | 1.042 $\pm$ 0.019 |
| 224 - 259                   | $(9.52 \pm 1.64) \times 10^{-4}$                | 1.037 $\pm$ 0.014 |
| 259 - 298                   | $(2.53 \pm 0.56) \times 10^{-4}$                | 1.033 $\pm$ 0.009 |
| 298 - 344                   | $(6.18 \pm 1.45) \times 10^{-5}$                | 1.030 $\pm$ 0.005 |
| 344 - 396                   | $(1.11 \pm 0.31) \times 10^{-5}$                | 1.027 $\pm$ 0.001 |
| 396 - 457                   | $(1.53 \pm 0.65) \times 10^{-6}$                | 1.025 $\pm$ 0.003 |
| 457 - 527                   | $(2.17 \pm 1.25) \times 10^{-7}$                | 1.023 $\pm$ 0.007 |

Additional 5.8% uncertainty on the integrated luminosity is not included. The parton-to-hadron correction factors, $\text{C}_{\text{HAD}}(p_T^{\text{jet}}, y^{\text{jet}})$, are applied to the pQCD predictions (see Fig. 5).
| $p_T^{\text{jet}}$ [GeV/c] | Jet energy scale | Resolution | Unfolding | $p_T^{\text{jet}}$ spectra | $\delta m_i$ |
|--------------------------|------------------|------------|------------|-----------------------------|------------|
| 54 - 62                  | +9.9             | +2.4       | ±5.4       | ±0.6                        | ±0.8       |
| 62 - 72                  | +9.8             | +2.4       | ±4.8       | ±0.6                        | ±0.7       |
| 72 - 83                  | +9.8             | +2.3       | ±4.3       | ±0.6                        | ±0.6       |
| 83 - 96                  | +9.7             | +2.2       | ±3.8       | ±0.6                        | ±0.6       |
| 96 - 110                 | +9.8             | +2.2       | ±3.4       | ±0.6                        | ±0.5       |
| 110 - 127                | +10.0            | +2.1       | ±3.1       | ±0.6                        | ±0.5       |
| 127 - 146                | +9.4             | +1.9       | ±2.8       | ±0.6                        | ±0.4       |
| 146 - 169                | +11.2            | +2.1       | ±2.5       | ±0.5                        | ±0.4       |
| 169 - 195                | +12.5            | +2.1       | ±2.3       | ±0.4                        | ±0.4       |
| 195 - 224                | +14.3            | +2.2       | ±2.1       | ±0.3                        | ±0.3       |
| 224 - 259                | +16.6            | +2.4       | ±1.9       | ±0.2                        | ±0.3       |
| 259 - 298                | +19.3            | +2.7       | ±1.8       | ±0.1                        | ±0.3       |
| 298 - 344                | +22.3            | +3.1       | ±1.6       | ±0.1                        | ±0.3       |
| 344 - 396                | +25.7            | +3.7       | ±1.5       | ±0.2                        | ±0.3       |
| 396 - 457                | +30.7            | +4.5       | ±1.4       | ±0.5                        | ±0.3       |
| 457 - 527                | +39.5            | +5.5       | ±1.3       | ±1.3                        | ±0.2       |
| 527 - 700                | +52.6            | +7.4       | ±1.2       | ±1.2                        | ±0.2       |

### Systematic uncertainties \% \( (0.1 < |y^{\text{jet}}| < 0.7) \ (D = 0.5) \)

| $p_T^{\text{jet}}$ [GeV/c] | Jet energy scale | Resolution | Unfolding | $p_T^{\text{jet}}$ spectra | $\delta m_i$ |
|--------------------------|------------------|------------|------------|-----------------------------|------------|
| 54 - 62                  | +10.7            | +2.7       | ±5.6       | ±0.4                        | ±1.5       |
| 62 - 72                  | +10.4            | +2.6       | ±4.9       | ±0.4                        | ±2.6       |
| 72 - 83                  | +10.3            | +2.4       | ±4.2       | ±0.4                        | ±2.6       |
| 83 - 96                  | +10.2            | +2.3       | ±3.7       | ±0.4                        | ±2.3       |
| 96 - 110                 | +10.2            | +2.2       | ±3.2       | ±0.4                        | ±2.1       |
| 110 - 127                | +10.4            | +2.1       | ±2.8       | ±0.4                        | ±1.9       |
| 127 - 146                | +10.8            | +2.0       | ±2.5       | ±0.4                        | ±1.7       |
| 146 - 169                | +11.5            | +1.9       | ±2.1       | ±0.4                        | ±1.6       |
| 169 - 195                | +12.6            | +1.9       | ±1.9       | ±0.4                        | ±1.4       |
| 195 - 224                | +13.9            | +1.9       | ±1.6       | ±0.3                        | ±1.3       |
| 224 - 259                | +15.8            | +2.1       | ±1.4       | ±0.3                        | ±1.3       |
| 259 - 298                | +18.0            | +2.4       | ±1.3       | ±0.2                        | ±1.3       |
| 298 - 344                | +20.8            | +2.8       | ±1.1       | ±0.2                        | ±1.2       |
| 344 - 396                | +24.5            | +3.4       | ±1.0       | ±0.2                        | ±1.2       |
| 396 - 457                | +30.1            | +4.4       | ±0.8       | ±0.5                        | ±1.1       |
| 457 - 527                | +38.8            | +5.4       | ±0.7       | ±1.1                        | ±1.0       |
| 527 - 700                | +49.8            | +7.3       | ±0.6       | ±3.4                        | ±1.0       |

**TABLE VI:** Systematic uncertainties (in percent) on the measured inclusive jet differential cross section as a function of $p_T^{\text{jet}}$, for jets in the region $0.1 < |y^{\text{jet}}| < 0.7$ and using $D = 0.5$ and $D = 1.0$ (see Fig. [11]). The different columns follow the discussion in Section X. An additional 5.8% uncertainty on the integrated luminosity is not included.
TABLE VII: Measured inclusive jet differential cross section as a function of $p_T^{\text{jet}}$ for jets in the region $0.1 < |y^{\text{jet}}| < 0.7$ using $D = 0.5$ and $D = 1.0$ (see Fig. 11). An additional 5.8% uncertainty on the integrated luminosity is not included. The parton-to-hadron correction factors, $C_{\text{HAD}}(p_T^{\text{jet}})$, are applied to the pQCD predictions.
The correlations among systematic uncertainties in different $p_T^{\text{jet}}$ bins and $|y^{\text{jet}}|$ regions are studied in detail. The uncertainty on the absolute jet energy scale is decomposed into different sources considered independent but fully correlated across $p_T^{\text{jet}}$ bins and $|y^{\text{jet}}|$ regions. A $\pm 1.8\%$ uncertainty on the absolute energy scale, independent of $p_T^{\text{jet}}$, results from the sum in quadrature of four different contributions [42]: a $\pm 0.5\%$ uncertainty from the calorimeter stability versus time, a $\pm 1.0\%$ uncertainty due to the modeling of the jet fragmentation, a $\pm 0.5\%$ uncertainty from the simulation of the electromagnetic calorimeter response, and a $\pm 1.3\%$ uncertainty from the simulation of the calorimeter response at the boundary between calorimeter towers. Other contributions to the absolute energy scale uncertainty come from the description of the calorimeter response to hadrons for different ranges in hadron momentum [42].

Table VIII shows the resulting relative contributions to the quoted systematic uncertainty on the measured cross sections related to the absolute jet energy scale uncertainty.

### APPENDIX A: CORRELATIONS OF SYSTEMATIC UNCERTAINTIES

The rest of the systematic uncertainties on the measured cross sections, including that on the total integrated luminosity, are also assumed to be independent and fully correlated across $p_T^{\text{jet}}$ bins and $|y^{\text{jet}}|$ regions, except those related to the $\beta_{\text{data}}/\beta_{\text{mc}}$ ratio, for which uncertainties in different $|y^{\text{jet}}|$ regions are uncorrelated.

A global $\chi^2$ test is performed according to the formula

$$
\chi^2 = \sum_{j=1}^{76} \frac{[\sigma_j^d - \sigma_j^{\text{th}}(\bar{s})]^2}{[\delta\sigma_j^d]^2 + [\delta\sigma_j^{\text{th}}(\bar{s})]^2} + \sum_{i=1}^{17} [s_i]^2,
$$

where $\sigma_j^d$ is the measured cross section for data point $j$, $\sigma_j^{\text{th}}(\bar{s})$ is the corresponding prediction, and $\bar{s}$ denotes the vector of standard deviations, $s_i$, for the different independent sources of systematic uncertainty. The values for $\sigma_j^{\text{th}}(\bar{s})$ are obtained from the nominal NLO pQCD prediction, where $\bar{s}$ includes the uncertainty on $C_{\text{HAD}}$ but does not consider PDF uncertainties. The uncertainty on $C_{\text{HAD}}$ is assumed to be fully correlated across $p_T^{\text{jet}}$ bins and $|y^{\text{jet}}|$ regions. The sums in Eq. (A1) run over 76 data points and 17 independent sources of systematic uncertainty, and the $\chi^2$ is minimized with respect to $\bar{s}$. Correlations among systematic uncertainties are taken into account in $\sigma_j^{\text{th}}(\bar{s})$. As an example, for a given source $i$, variations of $s_i$ will coherently affect all the $\sigma_j^{\text{th}}(\bar{s})$ values if the corresponding systematic uncertainties are considered fully correlated across $p_T^{\text{jet}}$ bins and $|y^{\text{jet}}|$ regions.

### TABLE VIII: Relative contributions (in percent) to the quoted systematic uncertainty on the measured cross sections related to the absolute jet energy scale uncertainty.

The second column corresponds to a $\pm 1.8\%$ uncertainty on the absolute energy scale, as discussed in the text. Sources are considered independent and fully correlated in $p_T^{\text{jet}}$ and $|y^{\text{jet}}|$.

| $p_T^{\text{jet}}$ [GeV/c] | $p_T^{\text{jet}}$ independent uncertainty | $p < 12$ GeV/c response to hadrons | $12 < p < 20$ GeV/c $p > 20$ GeV/c |
|--------------------------|------------------------------------------|-----------------------------------|---------------------------------|
| 54 - 62                  | 90.3                                     | 37.8                              | 15.2                            | 13.5 |
| 62 - 72                  | 90.2                                     | 35.2                              | 16.1                            | 19.1 |
| 72 - 83                  | 89.9                                     | 31.9                              | 17.0                            | 24.6 |
| 83 - 96                  | 89.2                                     | 28.8                              | 17.3                            | 30.1 |
| 96 - 110                 | 88.0                                     | 26.0                              | 16.9                            | 35.8 |
| 110 - 127                | 86.4                                     | 22.7                              | 16.4                            | 41.9 |
| 127 - 146                | 84.3                                     | 20.0                              | 15.1                            | 47.7 |
| 146 - 169                | 82.1                                     | 17.2                              | 14.1                            | 52.6 |
| 169 - 195                | 79.8                                     | 14.6                              | 12.7                            | 57.0 |
| 195 - 224                | 77.6                                     | 12.5                              | 11.5                            | 60.7 |
| 224 - 259                | 75.7                                     | 10.7                              | 10.3                            | 63.6 |
| 259 - 298                | 73.8                                     | 9.1                               | 9.2                             | 66.2 |
| 298 - 344                | 72.1                                     | 7.8                               | 8.2                             | 68.3 |
| 344 - 396                | 70.5                                     | 6.8                               | 7.3                             | 70.2 |
| 396 - 457                | 69.2                                     | 5.8                               | 6.4                             | 71.7 |
| 457 - 527                | 68.0                                     | 5.0                               | 5.7                             | 72.9 |
| 527 - 700                | 66.8                                     | 4.2                               | 5.0                             | 74.2 |