Water Dynamics Around Proteins: T- and R-States of Hemoglobin and Melittin

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Abstract

The water dynamics, as characterized by the local hydrophobicity (LH), is investigated for tetrameric hemoglobin and dimeric melittin. For the T₀ to R₀ transition in Hb it is found that LH provides additional molecular-level insight into the Perutz mechanism, i.e., the breaking and formation of salt bridges at the α₁/β₂ and α₂/β₁ interface is accompanied by changes in LH. For Hb in cubic water boxes with 90 Å and 120 Å edge length it is observed that following a decrease in LH as a consequence of
reduced water density or change of water orientation at the protein/water interface the
$\alpha/\beta$ interfaces are destabilized; this is a hallmark of the Perutz stereochemical model
for the T to R transition in Hb. The present work thus provides a dynamical view
of the classical structural model relevant to the molecular foundations of Hb function.
For dimeric melittin, earlier results by Cheng and Rossky [Nature, 1998, 392, 696699]
are confirmed and interpreted on the basis of LH from simulations in which the protein
structure is frozen. For the flexible melittin dimer the changes in the local hydration
can be as much as 30% than for the rigid dimer, reflecting the fact that protein and
water dynamics are coupled.

Introduction

Hemoglobin is one of the most widely studied proteins due to its essential role in transporting
oxygen from the lungs to the tissues. The two most important structural states of this pro-
tein are the deoxy structure (T$_0$), which is stable when no ligand is bound to the heme-iron,
and the oxy structure (R$_4$), which is stable when each of the four heme groups have a ligand,
such as oxygen, bound to them. The state with the quaternary structure of R$_4$, but with no
heme-bound ligands is the R$_0$ state. Despite strong experimental evidence that T$_0$ is signif-
ically more stable than R$_0$, with an equilibrium constant of $K_{T_0}^{R_0} = 6.7 \times 10^5$,[1]
molecular dynamics (MD) simulations appear to indicate that the R$_0$ state is more stable. Specifically,
simulations have found that when hemoglobin is initialized in the T$_0$ state it undergoes a
spontaneous transition into the R$_0$ state on sub-$\mu$s time scales.[2,3] Understanding the origins
of this discrepancy between the measured and simulated relative stabilities of the R$_0$ and T$_0$
states is essential to establishing the reliability of simulation-based studies of Hemoglobin
and other large biomolecules.

In a recent simulation study, it was found that the T$_0 \rightarrow$ R$_0$ transition rate depends sensi-
tively on the size of the simulation cell.[4] Specifically, simulations of hemoglobin initialized
in the T₀ state and placed in a periodically replicated cubic solvent box with side length of 75 Å, 90 Å, and 120 Å, underwent transition towards the R-state structure after 130 ns, 480 ns, and 630 ns, respectively. Furthermore, in a simulation box with side-length of 150 Å, hemoglobin remained in the T₀ state for the entirety of a 1.2µs simulation. The extrapolated trend in these findings implies that T₀ is the thermodynamically stable state in this largest simulation cell for which the diffusional dynamics of the environment are correctly captured. The results also suggested that such a large box is required for the hydrophobic effect, which stabilizes the T₀ tetramer, to be manifested. While the statistical significance of this conclusion has been a topic of recent discussion in the literature,⁵,⁶ the dynamic stability of the T₀ state exhibits a clear systematic dependence on the size of the solvent box. Further analysis is required to provide conclusive evidence of the role of the hydrophobic effect and to reveal the mechanistic origin of the dependence of the thermodynamic stability of the T₀ state on the simulation box size. In this study we specifically address the role of system size variations in solvent dynamics.

The present work addresses the system size question by analyzing the molecular structure of the hydration layers surrounding tetrameric hemoglobin (Hb) and dimeric melittin. The particular focus is on whether there are characteristic changes in local hydration that accompany global transitions involving reorientation of the subunits - i.e. the decay of the T-state for Hb and the reconfiguration of the helices in melittin - and whether and how these changes are effected by the size of the solvent box. Extending the study to the melittin dimer, which is much smaller than Hb, provides information about the generality of this analysis. In addition, melittin was also studied previously as an example for hydrophobic hydration.⁷ Melittin is a small, 26-amino acid protein found in honeybee venom that crystallizes as a tetramer, consisting of two dimers, related by a two-fold symmetry axis.⁸,⁹ Previous work has characterized the behaviour of the hydrophobic binding surface of melittin and the solvent exposed surface residues. While these surface residues are characterized by a well-defined
orientation of the water molecules, water molecules in the hydrophobic regions are more dynamical, exploring different water configurations. Here, similar simulations with a frozen melittin dimer in different box sizes are carried out and analyzed. In addition, the protein is also allowed to move freely which provides information about the solvent-solute coupling which has not been considered before.[7]

The analysis is based on a recently developed method of characterizing the hydrophobicity of a surface based on a statistical analysis of the configurational geometries of interfacial water molecules.[10] This method, described in more detail in the “Analysis of Aqueous Interfacial Structure” section, generates an order parameter, $\delta \lambda_{\text{phob}}$, which quantifies the statistical similarity of sampled water configurations to those that occur at equilibrium near an ideal hydrophobic surface. When applied to water configurations sampled from a particular nanoscale region of a protein surface, $\delta \lambda_{\text{phob}}$ can be interpreted as a local measure of hydrophobicity and thus be extended to map the spatial and temporal variations of a protein’s solvation shell.

In the following section the simulations and computational methods are described. Then, in the Results section, analyses and interpretations of protein hydration structure are presented. Results for hemoglobin are described first, including analysis of previous simulations in different simulation box sizes. Results for melittin are described second. Finally, conclusions are drawn.

**Computational Methods**

**Molecular Dynamics Simulations**

**Simulations of Hemoglobin (Hb):** The Hb-simulations (for the sequence see Figure S1)
were described previously, and only the necessary points without technical details are reported here. The molecular dynamics trajectories were run in cubic water boxes with box lengths 90 Å, 120 Å, and 150 Å which are analyzed in the following. Each simulation was run for 1 µs or longer and for selected box sizes, additional repeat simulations were carried out. The trajectories analyzed in the present work are those from Ref. and the reader is referred to that manuscript for additional details on the production runs.

Simulations of Melittin: MD simulations of the melittin dimer were carried out using CHARMM and the CHARMM36 force field. The TIP3P water model was used, the same as that used for Hb. The dimer structure (PDB:2MLT) was used as the starting structure. It was solvated in a cubic water box of length 51.051 Å (4066 water molecules). In addition, simulations with a box length of 60 Å were performed to assess whether, in analogy to Hb, there were effects of increased solvent box sizes on the stability, dynamics and water structuring of melittin dimer. A 16 Å cut-off was applied with a Particle Mesh Ewald scheme and a 1 fs time step was used in the MD simulations. Although more physically realistic fixed point charge water models exist (e.g. TIP4P), the use of TIP3P here is mandatory for consistency because the CHARMM force field was parametrized with it. It is certainly of interest to include water polarization in corresponding simulations, but such a study is beyond the scope of the present work.

The following protocol was used. Two steps of minimization were performed: 50 steps with the Steepest Descent algorithm, followed by 50 steps with the Newton-Raphson algorithm. The system was then heated and equilibrated using the velocity Verlet algorithm for 25 ps with a Nose Hoover thermostat at 300 K. This was followed by a 100 ns NVT production simulation, for which coordinates were recorded every 1 ps. In a first set of simulations, the protein dimer was fixed and only the solvent water was allowed to move. This allows direct comparison with the work of Cheng and Rossky. In a separate set of 100 ns simulations
the protein was allowed to move and only bonds involving hydrogen atoms molecules were constrained using SHAKE.  

Analysis of Aqueous Interfacial Structure  
The hydration structure of the simulated proteins was characterized following a recently developed computational method.  This method is based on the concept that deformations in water’s collective interfacial molecular structure encode information about the details of surface-water interactions.  These deformations are quantified in terms of the probability distribution of molecular configurations, as specified by the three-dimensional vector,  

\[ \vec{\kappa} = (a, \cos \theta_{OH_1}, \cos \theta_{OH_2}) \]  

where \( a \) is the distance of the oxygen atom position to the nearest point on the instantaneous water interface, as defined in Ref., and \( \theta_{OH_1} \) and \( \theta_{OH_2} \) are the angles between the water OH bonds and the interface normal.  

Here, this method is used to compute the time dependent quantity, \( \delta \lambda^{(r)}_{\text{phob}}(t) \), which describes the local hydrophobicity (LH) of residue \( r \), at time \( t \). More specifically, \( \delta \lambda^{(r)}_{\text{phob}}(t) = \lambda^{(r)}_{\text{phob}}(t) - \langle \lambda^{(r)}_{\text{phob}} \rangle_0 \), where,  

\[
\lambda^{(r)}_{\text{phob}}(t) = -\frac{1}{\sum_{a=1}^{N_a(r)} N_w(t;a)} \sum_{a=1}^{N_a(r)} \sum_{i=1}^{N_w(t;a)} \ln \left[ \frac{P(\vec{\kappa}^{(i)}(t)|\text{phob})}{P(\vec{\kappa}^{(i)}(t)|\text{bulk})} \right].
\]  

(1)  
Here the summation over \( N_a(r) \) is over the atoms in residue \( r \) and the summation over \( N_w(t;a) \) is over the water molecules within a cut-off of 6Å of atom \( a \) at time \( t \), and \( \vec{\kappa}^{(i)}(t) \) denotes the configuration of the \( i \)th molecule in this population. \( P(\vec{\kappa}|\text{phob}) \) is the probability to find configuration \( \vec{\kappa} \) at an ideal hydrophobic surface and \( P(\vec{\kappa}|\text{bulk}) \) is the probability to find that same configuration in the isotropic environment of the bulk liquid. As described in Ref., these reference distributions were obtained by sampling the orientational distribution of water at an ideal planar hydrophobic silica surface and the bulk liquid, respectively. The
quantity \(\langle \lambda_{\text{phob}} \rangle_0\) is the equilibrium value of \(\lambda_{\text{phob}}\) for configurational populations sampled from the ideal hydrophobic reference system.

Values of \(\delta\lambda_{\text{phob}}^{(r)}\) close to zero indicate that water near residue \(r\) exhibits orientations that correspond to those found at an ideal hydrophobic surface. Hydrophilic surfaces interact with interfacial water molecules and lead to configurational distributions that differ from that of an ideal hydrophobic surface. These differences are typically reflected as values of \(\delta\lambda_{\text{phob}}^{(r)} > 0\), with larger differences giving rise to larger positive deviations in \(\delta\lambda_{\text{phob}}^{(r)}\). Values of \(\delta\lambda_{\text{phob}}(r) \geq 0.5\) are used as indicative of hydrophilicity. For the number of unique water configurations used to compute \(\delta\lambda_{\text{phob}}^{(r)}\) here, fluctuations of \(\delta\lambda_{\text{phob}}^{(r)}\) are expected to fall within \(-0.24 \leq \delta\lambda_{\text{phob}}^{(r)} \leq 0.27\) (95\% confidence interval) at the hydrophobic reference system, making sustained values of \(\lambda_{\text{phob}}^{(r)} \geq 0.5\) highly indicative of local hydrophilicity. The fluctuations in \(\delta\lambda_{\text{phob}}^{(r)}\) as a function of time provide information about changes in the local solvation environment.

**Results**

**Hydration Dynamics around T\(_0\)- and R\(_0\)-State Hemoglobin**

Figure 1 (top) illustrates the structure of Hb for the sequences of the \(\alpha\) and \(\beta\) chains) with the \(C_\alpha\) atoms of the residues analyzed specifically shown as van der Waals spheres. The first set of residues we study are the ones in Perutz’ stereochemical model,\(^\text{21}\) which are involved in the salt bridges and the \(\alpha/\beta\) shearing motion (Table 1). The shearing motion involves a change in the H-bonds at the \(\alpha_1/\beta_2\) interface. In the T\(_0\) structure, the side chain of Thr41\(\alpha_1\) occupies a notch formed by the main chain of Val98\(\beta_2\) and a hydrogen bond is present between Tyr42\(\alpha_1\) and Asp99\(\beta_2\). After the transition to the R\(_4\) state, the same notch is occupied instead by Thr38\(\alpha_1\) and the previous hydrogen bond is substituted by one between Asp94\(\alpha_1\)
and Asn102β2. The same conformational change occurs at the α2/β1 interface.

Other R-state structures, including R2, RR2 and R3, also exist and present intermediate states between T0 and R4. The difference between all Hb forms emerges from differences in the position of the β2-subunit relative to the α1-subunit at the switch region. This can be shown by superimposing the Cα atoms of the α1β1 dimers and computing the RMSD for the α2β2 dimer with the T0 Cα atoms structure as a reference (Figure 1 top panel) for all Hb forms extracted from crystal structures and for the T0 Hb structure simulated in different water box sizes. The same applies to superimposing the Cα atoms of α2β1 dimers and computing the RMSD of the nonsuperimposed regions (α1β2 dimer, and also on the α carbons) with the T0 structure as a reference point (Figure 1 left bottom panel). And as a measure of quaternary variation, the complete α1β1 α2β2 tetramer was superimposed on the Cα atoms (Figure S2 3rd panel from top). It is found that these different RMSD results follow the same trends when comparing different R forms and box sizes. R3 shows the most shift and is closest to T0, followed by RR2 and lastly by the R2 and R3 structures.

Figure 1 also shows that the large quaternary structural difference between the T and R forms is accompanied by significant changes in the α1-α2 and β1-β2 iron-iron distances; they are reduced in the R-states, most notably for the R3 structure (right panels). This movement of the subunits has a large effect on the interdimer interface (as observed in the interaction distances reported in Figure S3) and thus on the central water cavity relative to the T0 structure. There is also the change in the Cα-Cα distance between His146β1 and His146β2 and the Cα-Cα distance between His143β1 and His143β2, as well as the change in the θ angle between the two planes containing His146β1-Feβ1-Feα1 and His146β2-Feβ2-Feα2. The angle between the α1β1 and α2β2 subunits is smaller in all R-forms compared to the T structure (Figure S2, bottom panel). These values explain the shorter distances between His146β1 and His146β2, and between His143β1 and His143β2 reported in Figure S2 (first two panels from
Figure 1: Top: Representation of Hb with the Cα atoms of the residues relevant to Perutz’ stereochemical mechanism shown as yellow spheres. The iron atoms (green spheres) are connected with green dashed lines, indicating the distances reported. Blue, red, grey, and gold ribbon structures for α1, β1, α2, and β2 subunits of Hb. Bottom: Quaternary structure differences of Hb structures found in the simulations, based on the structural comparison of the α1β1 and α2β2 subunits. Black, gold, red, and green traces for simulations in the 75 Å, 90 Å, 120 Å, and 150 Å boxes, respectively. Left panels: (top) RMSD of the nonsuperimposed α2β2 subunit after superimposing the α1β1 subunit (Cα carbon atoms were used for both superposition and RMSD calculation); (bottom) RMSD of the nonsuperimposed α1β2 subunit after superimposing the α2β1 subunit. Right panels: Iron-Iron distances between the αs and βs of each subunit. Horizontal dashed lines indicate the corresponding values from all known Hb structures (T0, R2, RR2, R3 and R4).
Hence, the $\beta$-cleft entrance to the central water cavity is narrowed (compared to the $T_0$ structure with the largest central cavity) and this leads to less water entering the central cavity. The decrease in the number of water molecules in the central cavity was noted in our previous paper where water molecules present in the central cylinder for the different box sizes were counted (see Figures 5-figure supplement 3 and 4 in Ref.).

Local structural changes around His146 resulting from differences in the position of the $\beta_2$-subunit relative to the $\alpha_1$-subunit are also observed (Figure S3). In all R forms compared to the T structure, the water-mediated contact (His146$\beta$)COO–OC(Pro37$\alpha$) and the salt bridges between (His146$\beta$)COO–NZ(Lys40$\alpha$) and (His146$\beta$)NE2–COO(Asp94$\beta$) are absent. Further, the salt bridge missing in the $T_0$ form between (His146$\beta$)COO and NE(His2$\beta$) is observed only in the $R_4$ form.

Specific H-bonds at the $\alpha_1\beta_2$ dimer interface involved in the shearing motion were also analyzed (Figure S4). First, the hydrogen bond between Thr38$\alpha_1$ and His97$\beta_2$, present in the $R_3$ structure but missing in the RR$_2$ and R$_2$ intermediate structures, was sampled in our simulations. Second, the hydrogen bond between Tyr42$\alpha_1$ and Asp99$\beta_2$ present only in the $T_0$ structure and absent in all R-forms was observed for the stable $T_0$ state simulation (150 Å box) and was absent in all boxes with transitions. Finally, the hydrogen bond between Arg92$\alpha_1$ and Gln39$\beta_2$ or Glu43$\beta_2$ present in RR$_2$ and missing in all other states was observed.

The conformational differences between the T and R states affect the hydration environment in a manner that can be related to $\delta\lambda_{\text{phob}}^{(r)}$. Based on the results of previous simulations, the set of residues for which $\delta\lambda_{\text{phob}}$ changes most across the transitions was selected. Figure 2 (top panel) reports the $C_\alpha$ His146$\beta_1$–His146$\beta_2$ separation, which serves as an indicator of the T-to-R transition for the simulations in the 90, 120, and 150 Å boxes. For the simulations in the two smaller boxes, three red transitions are evident between the $T_0$-state (at early times)
and the $R_0$-state (at late times, see Figure 1 in Ref.\textsuperscript{4}), as indicated by the red dashed lines in Figure 2. Structural changes are accompanied by changes in the number of hydration waters. For the simulation in the largest (150 Å) box, for which no transition occurs, the $C_\alpha$ His146$\beta_1$–His146$\beta_2$ separation is constant and the average hydration is larger than 0.95 (see bottom row in Figure 2).

(a) Results for Hb 90 Å box: Local hydrophobicity (LH) for residues identified as the Perutz stereochemical model (see Table 1). The LH analysis for the 1 $\mu$s simulation is carried out with a time resolution of 0.5 ns. A cut-off of 6 Å from the protein is chosen to distinguish between interfacial and bulk water. The structural transitions for the 90 Å box occur at $t = 470$ ns, $t = 770$, and $t = 891$ ns, as indicated by the distance $r_{\text{His146}}$ between the $C_\alpha$ atoms of the two His146 residues in the $\beta_1$ and $\beta_2$ chains. The total number of interfacial water is found to correlate with this distance (see bottom row of Figure 2). Whenever the distance between the two His146 residues (see reference\textsuperscript{4}) decreases abruptly (as indicated by the red dashed lines), the relative number of water molecules $r_w$ within the 6 Å cut-off increases. The value of $r_w = N_{\text{wat}}/N_{\text{max}}$ was determined as the instantaneous number $N_{\text{wat}}$ of water molecules for a specific snapshot and the maximum $N_{\text{max}}$ encountered along the entire trajectory.

To obtain more detailed information, $\delta \lambda_{\text{phob}}(t)$ was analyzed for the residues listed in Table 1; see Figure 3. For certain residues, structural transitions (at $t = 470$ ns, $t = 770$ ns, and $t = 891$ ns) are accompanied by abrupt rather than by gradual changes in local hydrophobicity of individual residues. Examples include Val98$\beta_1$, Thr41$\alpha_1$, or Asp94$\alpha_1$. By contrast, Tyr42$\alpha_1$ shows a gradual decrease in $\delta \lambda_{\text{phob}}$ over most of the 1 $\mu$s simulation. There are also changes in LH away from overall structural transitions, e.g. for Val98$\beta_2$, Asp99$\beta_2$, and Asn102$\beta_2$ at 200 ns, further discussed below. Except for Val98$\beta_1$ all residues that show a substantial decrease in their hydrophilic ($\delta \lambda_{\text{phob}} \sim 0.5$) versus hydrophobic ($\delta \lambda_{\text{phob}} \sim 0$)
Figure 2: Top: The Cα His146β1–His146β2 separation as a function of time for the 90, 120 and 150 Å box from left to right. Raw data in black and running averages over 50 ns in green. The arrows on the right-hand side indicate the His146β1–His146β2 separation (r_{His146,CαCα}) in the 2DN2 (T0) and 2DN3 (R4) crystal structures. Bottom: The hydration (“H2O ratio”) of the entire protein, expressed in terms of r_w = N_{wat}/N_{max}. The vertical red dashed lines indicate the transition times for the three steps observed in the 90 Å and 120 Å boxes (see Figure 1B of reference).  

character [Thr41α1, Tyr42α1] or an increase [Thr38α1, Asp94α1, Asp99β2] are at the α1/β2 interface. This suggests that the decay for the 90 Å box is triggered primarily by the hydration around residues that are involved in the α1/β2 contacts.

Based on the data in Figure the T0 → R0 transition in the 90 Å box is accompanied by significant changes in the hydration environment at certain locations around the α1/β2 contact. This observation is consistent with Perutz’ conclusion. We quote, “[..]Where is the force that changes the quaternary structure applied[..]The evidence is overwhelmingly in favor of the contacts α1β2[..]” The significant changes in hydration around the α1β2 contact suggest the possibility that the T0 → R0 transition is driven by solvent thermodynamics.
Table 1: The residues of Hb for which the local hydrophobicity $\delta\lambda_{\text{phob}}$ is analyzed from Perutz’ stereochemical model. For each residue its involvement in specific contacts is reported.

| Residue      | Role in the protein                      |
|--------------|------------------------------------------|
| Arg141$$\alpha_1$$ | $\alpha$ C-terminal salt bridge         |
| Val1$$\alpha_2$$      | $\alpha$ C-terminal salt bridge         |
| Asp126$$\alpha_2$$     | $\alpha$ C-terminal salt bridge         |
| Lys127$$\alpha_2$$     | $\alpha$ C-terminal salt bridge         |
| Tyr140$$\alpha_1$$     | $\alpha$ proximity to the C-terminal residue |
| His146$$\beta_1$$      | $\beta$ C-terminal salt bridge          |
| Lys40$$\alpha_2$$      | $\beta$ C-terminal salt bridge          |
| Asp94$$\beta_1$$       | $\beta$ C-terminal salt bridge          |
| Tyr145$$\beta_1$$      | $\beta$ salt bridge involved in His146$$\beta_1$ motion |
| Val98$$\beta_1$$       | $\beta$ salt bridge involved in His146$$\beta_1$ motion |
| Thr38$$\alpha_1$$      | $\alpha_1 - \beta_2$ shearing           |
| Thr41$$\alpha_1$$      | $\alpha_1 - \beta_2$ shearing           |
| Tyr42$$\alpha_1$$      | $\alpha_1 - \beta_2$ shearing           |
| Asp94$$\alpha_1$$      | $\alpha_1 - \beta_2$ shearing           |
| Cys93$$\beta_2$$       | $\alpha_1 - \beta_2$ shearing           |
| Val98$$\beta_2$$       | $\alpha_1 - \beta_2$ shearing           |
| Asn102$$\beta_2$$      | $\alpha_1 - \beta_2$ shearing           |
| Asp99$$\beta_2$$       | $\alpha_1 - \beta_2$ shearing           |

(b) Results for Hb 120 Å box: For the simulation in the 120 Å box most of the residues involved in the salt bridges, like those in the 90 Å box, show only minor variations in $\Delta\langle\delta\lambda_{\text{phob}}\rangle$ except that of Tyr145$$\beta_1$$ and Val98$$\beta_1$$ which have the largest variations along the trajectory (see Figure 4B). It is found that the LHSs of all other residues in Figures 3A, B and 4A, B behave similarly in the simulations of the 90 Å and 120 Å boxes. For Val98$$\beta_1$$, instead of decaying to $\Delta\langle\delta\lambda_{\text{phob}}\rangle \approx 0$ as in the simulation of the 90 Å box, the value of $\Delta\langle\delta\lambda_{\text{phob}}\rangle$ in the 120 Å box remains at or above 0.5 throughout the entire simulation. Hence, the $T_0 \rightarrow R_0$ transition is again mainly associated with motion at the $\alpha_1/\beta_2$ interface (see Figure 4C,D). An example of a transition that follows the mechanism described by Perutz is the transition at 620 ns at the $\alpha_2/\beta_1$ interface, where the cleavage of the Tyr42$$\alpha_2$$ and Asp99$$\beta_1$$ salt bridge is clearly visible (see Figure S4 middle panel and Figure S5).
Several of the residues at the $\alpha_1/\beta_2$ interface show pronounced changes in local hydrophobicity that coincide with structural transitions (Figures S3 and S4). However, a few residues in Figure 4D also show LH changes that are not necessarily linked directly to a tertiary structural change (“step”); they are Val98$\beta_2$, Asp99$\beta_2$, and Asn102$\beta_2$ at around 500 ns, further discussed below. For the transitions at 620 ns and 840 ns there is again a clear change in LH for Thr38$\alpha_1$, Thr41$\alpha_1$, and Asp94$\alpha_1$, the most pronounced of them involving Thr38$\alpha_1$. These observations also indicate that the nature of the transition at 470 ns (step1) in the 90 Å and at 620 ns (step1) in the 120 Å box is different and may be explained by the transition to different intermediate R-forms (see next paragraph).

For the decaying structures in the 90 Å and 120 Å boxes the following is observed. In the 90 Å box, a transition from $T_0$ to $R_3$ starts at 470 ns (step1), where the His146–His146 separation drops from 31 Å to 25 Å bringing the Hb structure closer to $R_3$ (22 Å, Figure S2, first panel). This $T_0$ to $R_3$ transition is completed at 780 ns (step2, Figure S2, the presence of the $R_3$ structure at 780 ns is marked in all the panels by a cyan dashed line). At $\sim$ 880 ns (step3) a next transition from $R_3$ to $R_2$ occurs (the $R_2$ structure is marked by a violet dashed line in Figure S2). For the rest of the simulation until 1 µs, the $R_{R_2}$ and $R_4$ states are sampled (Figure S2, $R_{R_2}$ and $R_4$ states are indicated by a green dashed line and a blue arrow, respectively). Conversely, in the 120 Å box, at step1 at 620 ns a $T_0$ to $R_2$ transition starts by decaying to an unknown intermediate. It is continued at 840 ns (step2) to bring the structure closer to $R_2$. The transition to $R_2$ is completed by 920 ns (step3, Figure S2), the presence of the $R_2$ structure at 920 ns is indicated in all the panels by a vertical violet dashed line).

(c) Results for Hb 150 Å box: For the 150 Å box the previous MD simulations did not find a structural transition. The values of $\delta\lambda_{\text{phob}}$ for all residues involved in the salt bridges (Figure 5, columns A and B) do not deviate significantly from their average value.
Figure 3: Local hydrophobicity for the simulation in the 90 Å box. Moving average (MA) over 50 ns of δλ_{phob} as a function of time for residues involved in the C-terminal salt bridges (column A), additional salt bridges (column B) and the α_{1}β_{2} (columns C and D); see Table 1.

The amplitude of the fluctuations are typically smaller than for the simulations in the 90 Å and 120 Å boxes. For the residues at the α_{1}β_{2} interface there are variations for Thr38α_{1}, Thr41α_{1}, Tyr42α_{1}, and Asp94α_{1} (see Figure 5).

The clearest difference between the simulation in the 150 Å and the two smaller boxes is the behaviour for residues Val98β_{2}, Asp99β_{2}, and Asn102β_{2}. As an example, the water occupation around Val98β_{2} is analyzed by computing the radial distribution function g(r) between the C_{α} of the residue and the surrounding hydration water for different parts of the
trajectory. The radial distribution functions $g(r)$ in Figure S6 show that they are close in shape to one another but differ in magnitude for the early phase of the trajectory in the 120 Å and 150 Å box. They change in shape after the transition at 840 ns in the smaller of the two boxes. A pronounced signature in LH is also found in the 120 Å and 150 Å boxes for Thr38α1 between 800 and 900 ns. The signatures in LH for the 150 Å box can be related to formation of a Thr38α1–Asp99β2 salt bridge (Figure S7). Breaking and reforming of salt bridges involving Val98β2, Asp99β2, and Asn102β2 is also responsible for the sharp increase in LH around these three residues in the 90 Å box around 200 ns, see Figures 3D and S8.
It is notable that the LH around the three residues already starts to change before the salt bridge actually breaks.

Changes of the LH of each residue can be due to a) internal motion of a residue or b) the influence of neighbouring residues. Both of these are potentially followed by water displacement or influx which change Δλ_{phob}. For the transition at t = 840 ns in the 120 Å box, changes in the local water occupation around Val98β_2 obtained by analysis of radial distribution functions (see Figure S6) do not necessarily lead to changes in LH. The g(r) for the
time intervals 0 to 620 ns and 620 ns to 840 ns are very similar (red and green lines in Figure S6) while the LH changes from 0.8 at early times to 1.2 after $t \sim 500$ ns, see Figure 4. The water influx is a consequence of the reconfiguration of the H-bonding network including the Tyr42$\alpha_1$–Asp99$\beta_2$ salt bridge (see Figure S9) and the rearrangement of the carboxy group of the sidechain of Asp99$\beta_2$ due the rehydration of the side chain. These effects are also mirrored by the Asp99$\beta_2$ carboxy orientation (see dihedral time series reported in Figure S11) which demonstrates that before the transition at 840 ns the side chain follows a two-state behaviour but after the transition almost free rotation occurs (see also Figure S4). This change is accompanied by increased hydration of the side chain (bottom panel of Figure S11).

Comparing Figures 3 to 5 it is noted that even when Hb is still in its T$_0$ state (i.e. before 470 ns, the first transition in the 90 Å box), differences in LH, mainly at the $\alpha_1/\beta_2$ interface are observed. Examples include residues Thr41$\alpha_1$ and Tyr42$\alpha_1$ for which LH oscillates or decreases in the 90 Å box but remains constant in the two larger boxes before 470 ns. The finding that destabilization of the $\alpha_1/\beta_2$ interface is at the origin of the T$_0$ to R$_0$ transition is consistent with the Perutz stereochemical model. Conversely, the LH around the C-terminal salt bridge residues is very similar for the simulations in the three different box sizes, except for Val98$\beta_1$ and Tyr145$\beta_2$.

(d) Spatio-temporal analysis based on two-dimensional correlation maps: To better understand the coupling of local hydration dynamics and the structural transitions, two-dimensional correlation maps were generated which are referred to as local hydrophobicity cross correlation maps (LH-CCMs). Similar to dynamic cross correlation maps (DCCMs) for residues $i$ and $j$ the quantity

$$C_{ij} = \frac{\langle \Delta \lambda_{\text{phob}}^{(i)} \Delta \lambda_{\text{phob}}^{(j)} \rangle}{\sqrt{\langle (\Delta \lambda_{\text{phob}}^{(i)})^2 \rangle \langle (\Delta \lambda_{\text{phob}}^{(j)})^2 \rangle}} \quad (2)$$
was determined for each interval for which Hb was in a particular conformational state as shown in Figure [1].

Figure 6: Difference of Local Hydrophobicity $\Delta C_{ij}$ Cross Correlation Map (LH-CCM) for the 120 Å box. Panel A: difference between [0-620] and [620-840], i.e. "transition at 620" for entire protein. Panel B: difference between [620-840] and [840-920], i.e. "transition at 840" for the $\alpha_1/\beta_2$ interface. Panel C: difference between [620-840] and [840-920], i.e. "transition at 840" for the $\alpha_2/\beta_1$ interface. The cross correlations for the individual states are given in Figure S12. Only values $\Delta C_{ij} \geq 0.30$ are reported. Color code: $0.30 \leq \Delta C_{ij} < 0.35$ (purple), $0.35 \leq \Delta C_{ij} < 0.40$ (red), and $0.40 \leq \Delta C_{ij} < 0.45$ (orange).

Figure 6A reports the difference between the local hydrophobicity cross correlation maps between time intervals 0 to 620 ns and 620 to 840 ns for the 120 Å box for values of $\Delta C_{ij} > 0.3$. This map indicates that correlations in LH and their difference can depend on both the sequence and spatial proximity of two residues. The correlation in LH up to 620 ns (i.e. before
the first transition, see Figure S10) is large ($C_{ij} > 0.30$) for residues that play an active role in interface transitions between the two subunits (Figure 6 above the diagonal) and for regions that are spatially close (on the diagonal). An example for sequence proximity is the Val98$\beta_1$-Asp99$\beta_1$ region (feature C in Figure 6A and Figure S9). Changes in LH are a direct consequence of the Asp99$\beta_1$-Tyr42$\alpha_2$ salt bridge cleavage during the transition at 620 ns (see Figure S5) that leads to a change in the orientation of the peptide bond between Val98$\beta_1$-Asp99$\beta_1$ (Figure S9) and corresponding decrease in the LH of both, Asp99$\beta_1$ and Tyr42$\alpha_2$. Examples for spatial proximity of residues are the two clusters (labelled A and B in Figure 6A) that are at the $\alpha_2\beta_1$ shearing interface. This change in hydrophobicity in one of the two important stabilizing regions of the protein (the other being the $\alpha_1/\beta_2$ interface), indicates its possible involvement in the destabilization of the T$_0$ structure.

A more detailed view of the LH cross correlations for the $\alpha_1/\beta_2$ interface for the 120 Å box is provided in Figure S10 (for LH-CCMs in the 90 Å and 150 Å boxes see Figures S13 and S14). Figure S10 shows the LH cross correlations for residues involved in the $\alpha_1/\beta_2$ shearing motion up to 620 ns. The clusters (A to E) in Figure S10 involve correlated changes in LH at the $\alpha_1/\beta_2$ interface, whereas for cluster F no direct contact is present. In cluster A the correlation is caused by the Thr41$\alpha_1$-Arg40$\beta_2$ salt bridge present before the transition at 620 ns. Cluster B is dominated by the water-mediated Asp94$\alpha_1$-Arg40$\beta_2$ salt bridge before the transition at 620 ns; it is a weak interaction due to the large distance ($\sim$ 6 Å) between the proton and the anion. After the transition this salt bridge becomes the dominant interaction in which Arg40$\beta_2$ is involved. The C cluster is dominated by the $\pi$-stacking interaction between Tyr140$\alpha_1$ and Trp37$\beta_2$. A weak salt bridge of the Thr38$\alpha_1$ and Asp99$\beta_2$ sidechains with the Thr41$\alpha_1$ sidechain and Asp99$\beta_2$ NH peptide bond are responsible for the D cluster. The NH peptide bond of Asn97$\alpha_1$ and the Asp99$\beta_2$ side chain lead to cluster E. Overall, this figure provides a dynamic view of the stereochemical model proposed by Perutz. This is illustrated, for example, by the fact that all clusters (A to F) are extended, rather than the
usual point-to-point contacts (i.e., the salt bridges) alone.

Next, the transition in the 120 Å box at 840 ns is discussed from the perspective of the LH-CCMs (see Figure 6 panels B and C). They show the difference between the LH-CCMs for the time intervals [620-840] ns and [840-920] ns, respectively. During the process two salt bridges are broken (Thr41α1–Asp99β2 and Thr41α1–Arg40β2, which is water mediated) and two new salt bridges are formed (Thr38α1–Asp99β2 and Asp94α1–Arg40β2) and Asn97α1 - Asp99β2 continues to show a bimodal behaviour, see Figure S15. It is found that the reformation of these salt bridges between residues involved in the “Perutz mechanism” (Thr38α1, Thr41α1, Asp94α1 and Asp99β2) is also reflected in the difference cross correlation maps (Figure 6B and C). They confirm that most of the changes for this transition occur at the α1/β2 interface. Also, these two panels show that changes in the LH-CCMs are not necessarily symmetric for the α1/β2 and α2/β1 interfaces. Such a “dynamical asymmetry” (i.e., it is found in the molecular dynamics simulations) has also been observed for insulin dimer for which the X-ray structure has C2 symmetry or is very close to symmetric with only small local deviations from it.

As previous results have shown, the relative stability of the T0 state depends on the size of the simulation cell. Analysis of hydration structure via δλ(r)phob has the ability to reveal when and where protein hydration properties differ between differently sized simulation cells. To highlight this point, the statistics and dynamics of δλ(r)phob for Hb in the T0 state in the 90 Å and 150 Å simulation boxes are compared in Figure 7. It summarizes the values of δλ(r)phob over the residues that comprise the α1/β2 and α2/β1 interfaces, as a function of simulation time. Most notably, as the conformational transition from the T0 state to the R0 state progresses, there is a distinct shift towards values of δλ(r)phob near zero. This indicates that the interfacial water structure shifts from that observed at a hydrophilic surface towards that observed at a hydrophobic surface (Figure 7A). The shift in interfacial water structure is also
apparent from the probability distribution, $P(\delta\lambda^{(r)}_{\text{phob}})$, for the different simulation box sizes. During the first 500ns of the trajectories the probability distributions overlap (Figure 7B), showing that the interfacial water structure does not differ significantly. However, during the last 500 ns of the trajectories the probability distribution for the 90Å simulation box has a significant shift towards lower values of $\delta\lambda^{(r)}_{\text{phob}}$, corresponding to a more hydrophobic character of the interface (Figure 7C).

Figure 7: Comparison of the interfacial water structure for residues that are part of the $\alpha_1/\beta_2$ and $\alpha_2/\beta_1$ interfaces. The black and red lines correspond to simulations carried out in 90Å and 150Å solvent boxes, respectively. The marker indicates the center of a time interval. Panel A: The expectation value of $\delta\lambda^{(r)}_{\text{phob}}$ as a function of time, averaged over 50 ns time intervals. Panel B: The distribution of $\delta\lambda^{(r)}_{\text{phob}}$ values during the first 500 ns of the trajectories. Panel C: The distribution of $\delta\lambda^{(r)}_{\text{phob}}$ values during the last 500 ns of the trajectories.

**Hydration Dynamics around Melittin**

As a second example, the analysis of water hydration for Hb has been extended to melittin. It is a well studied prototype of a protein complex that is stabilized through hydrophobic interactions. Melittin is a small, 26-amino acid protein (for the sequence, see Figure S16) found in honeybee venom that crystallizes as a tetramer, consisting of two dimers (see Fig-
Cheng and Rossky characterized the behaviour of the hydrophobic surface of the melittin dimer and of the surrounding surface residues by simulations in which the structure of the melittin dimer was frozen. They found that in hydrophilic regions the water molecules have a well defined orientation, while in the hydrophobic regions, the waters are more mobile and explore different configurations. To further explore the hydration dynamics, simulations with a frozen melittin dimer in different box sizes are carried out and analyzed. In additional simulations, the protein was also allowed to move freely. These provide information about the solvent-solute coupling.

Figure 8: Left: A- and B-helices with the Gly1, Gly3, and Gly12 residues represented as spheres. The A-helix is slightly bent at the C-terminal end for the rigid and flexible simulations. The RMSD of the two chains of the dimer is 1.6 Å. Right: Time evolution of $\delta \lambda_{\text{phob}}$ for the 6 glycine residues in the melittin dimer. The results of the simulations for the rigid (cyan) and flexible (black) protein are reported. The orange and red line represent the average $\delta \lambda_{\text{phob}}$ for each residue during the simulation. Gly12 is less hydrophilic than the other Gly residues since it is located in the hydrophobic region of the protein.

It is of interest to analyze whether $\delta \lambda_{\text{phob}}$ encapsulates corresponding information, and whether simulations of water around a rigid melittin dimer, as carried out in Ref. 7 and around a flexible dimer lead to qualitatively similar results. Since the results for Hb depend on the box size, simulations are also carried out with different box sizes.
Figure 9: Flexible melittin in the 51 Å and 60 Å boxes. In Panels A the center-of-mass distance between the two monomers ($r_{cm-cm}$) is reported as function of time (black: raw data; green: moving average). Around 80 ns, a rearrangement of the two monomers is associated with an increase of $r_{cm-cm}$. The chain length ($r_{end-to-end}$) for the two segments (black and red for the raw data for chain A and B, green and blue for their moving average), are illustrated in Panels B. The RMSD with respect to the initial structure of the protein is shown in Panels C. During the time evolution, the number of water surrounding the protein seems not to be influenced by the structural changes as shown in Panels D.

The structural variations together with the overall hydration of the flexible melittin dimer in the different water box sizes are reported in Figure 9. In all simulations the end-to-end separation of the two helices (see Figure 9B) as defined by the $C_{\alpha}-C_{\alpha}$ separation of the two terminal residues Gly1 and Gln26 is stable, indicating that the helices (the $H_2O$ ratio) remain intact. Consequently, the structural transition that occurs after 80 ns in the 51 Å box (Figure 9C) and appears to occur towards the end of the simulation in the 60 Å box involves
the dimerization interface. This is confirmed by panel A, which reports an increase of the center-of-mass distance \( r_{cm-cm} \) between the two helices at the same time as the RMSD in panel C increases. The degree of hydration (Figure 9D) defined as \( r_w = N_{wat}/N_{max} \) remains essentially constant throughout the simulations.

The protein-water interface is analysed using the same methodology as that used for Hb. The Willard-Chandler interface is calculated setting \( r_{cut} = 25.0 \, \text{Å} \) and the likelihood (\( \delta \lambda_{phob} \)) of the interfacial water with the reference TIP3P water model is determined with a 6 Å cut-off. Figures 8 and S17 show the time evolution of selected residues. Figure 8 shows the temporal evolution, \( \delta \lambda_{phob} \), of glycine residues Gly1, Gly3, and Gly12 for chains A and B for both the rigid and the flexible dimers. The \( \delta \lambda_{phob} \) for the rigid dimer is essentially constant, as expected. The results reported are all averages over 2 ns windows.

Table 2: Average \( \delta \lambda_{phob} \) for the glycine residues for the 100 ns simulation (see Figure 8).

| Residue | 51 Å flexible | 51 Å rigid | 60 Å flexible | 60 Å rigid |
|---------|---------------|------------|---------------|------------|
| 1A      | 1.068         | 1.583      | 0.989         | 1.598      |
| 3A      | 1.090         | 1.604      | 0.983         | 1.616      |
| 12A     | 0.965         | 0.882      | 0.979         | 0.945      |
| 1B      | 1.192         | 1.614      | 0.921         | 1.587      |
| 3B      | 1.156         | 1.584      | 0.927         | 1.568      |
| 12B     | 0.917         | 0.799      | 0.968         | 0.826      |

For the rigid monomer (blue traces in Figure 8) the LH is constant along the entire 100 ns simulation for both box sizes and the averages differ by 10 % at most (Gly12A). For the flexible dimer (black traces) the instantaneous LH fluctuates around well-defined average values except for Gly12B which has a slight increase in its dynamics during the early phase of the simulation, particularly in the 60 Å box. In the simulation in both box sizes the amplitude of LH fluctuates between 0 and 1.6, i.e. between being hydrophobic and hydrophilic. Since Gly is an aliphatic/neutral residue, the changing hydrophilicity must be a consequence of its embedding along the peptide chain and the water structuring around it. Overall, it is
found that Gly12A and 12B, which are near the middle of the helix, are less hydrophilic (see Figure 8 and Table 2) than Gly1 and Gly3, which are positioned at or near the terminus. This difference is more pronounced for the rigid dimer.

Figure S17 shows the LH for the residues investigated by Cheng and Rossky\cite{note1} for the 51 Å box while those for the 60 Å box are given in Figure S18. The average $\delta \lambda_{phob}$ are neutral or hydrophilic. Good qualitative agreement with Ref\cite{note1} is found for residues Val8A (hydrophilic), Leu9A, Ile13A, Ile13B (residues with a decreasing level of hydrophobicity), and Ile20B.

Figure 10: Difference in hydrophobicity for the residues in the melittin dimer hydrophobic pocket as defined in Ref\cite{note1} for the rigid simulations in the 51 and 60 Å boxes. They are residues Val5, Val8, Leu13, Leu16, Ile20. The data reported is $\Delta \delta \lambda = \delta \lambda_{60} - \delta \lambda_{51}$, i.e. the change in LH from the simulation in the two water boxes. The maximum instantaneous change in $\Delta \delta \lambda_{phob}$ due to the box size is 40 %; most differences are 20 % or less.

It is also of interest to compare the difference in hydrophobicity for simulations of rigid melit-
tin in the two water boxes because all differences must arise from the size of the water box. Figure 10 shows the difference between the 51 Å and the 60 Å boxes in LH of the residues in the hydrophobic pocket. The average fluctuations are of the order of 0.1 units with maximum differences of 0.4 units. The difference between simulations with rigid and flexible melittin can also be seen when comparing the radial distribution functions, $g(r)$, between $C_\alpha$ atoms of selected residues and water and the corresponding water occupations $N(r)$ (see Figures S19 and S20). The residues were chosen in accord with the results from Table 3. For example, in the 51 Å box for rigid melittin the values for Val5A and Val5B are $\delta \lambda_{\text{phob}}^{51\text{A}} = 1.19$ and 1.48, respectively, which change to 1.25 and 1.49 in the larger 60 Å box; i.e., this is a change of 5% at most. Figure S19A shows that $g(r)$ for Val5A and Val5B are very similar for both water box sizes. This suggests that the difference of $\sim 0.25$ in Table 3 for the two water boxes must arise from the orientation of the water molecules within the 6 Å cut-off.

Conversely, for flexible melittin the differences for LH in the two water boxes can be substantial. As an example, Leu9B $\delta \lambda_{\text{phob}}^{51\text{A}} = 0.81$ is compared with $\delta \lambda_{\text{phob}}^{60\text{A}} = 1.07$ for the two box sizes. This is also evident from Figure S20A and B (right panel) for which $g(r)$ and $N(r)$ have increased amplitudes for the larger water box. For Val5B, $\lambda_{\text{phob}}^{51\text{A}} = 1.05$ is larger in the smaller box than $\lambda_{\text{phob}}^{60\text{A}} = 0.86$, whereas the amplitude of $g(r)$ up to the 6 Å cut-off in the larger box is larger than that in the smaller box. Hence, the difference found in the two box sizes must arise from the angular orientations of the water molecules relative to the protein surface. These analyses suggest that both the distance-dependence (reflected in $g(r)$ and $N(r)$) and the angular orientation, as measured by $\lambda_{\text{phob}}$, can depend on box size and potentially influence the thermodynamic stability of the two proteins.

The average hydrophobicity for each residue during the simulation is reported in Figure 11A (black for chain A and red for chain B). The decreased hydrophobicity of the central part of the chains (from Val5 to Leu16) is highlighted by the lower $\delta \lambda_{\text{phob}}$ (of 0.1-0.2 units) compared
Figure 11: Average $\delta\lambda_{\text{phob}}$ per residue for the 100 ns simulation for chains A (black) and B (red) for the flexible (panels A and C) and the rigid (panels B and D) melittin dimer. The top row is for the 51 Å box and the bottom row for the 60 Å box. The value of the LH ranges from $0.50 < \delta\lambda_{\text{phob}} < 1.00$ for the flexible dimer and between $0.00 < \delta\lambda_{\text{phob}} < 1.50$ for the rigid dimer. For the rigid dimer, the central part of the A-helix has consistently lower values of LH compared with the C- and N-terminal parts. For chain B larger variations in LH are found for some of the residues due to its different structure. The periodicity of the red traces (panels B and D) reflects the helical structure which is apparent for monomer B but less so for monomer A. For flexible melittin the variation of LH along the sequence is much smoother than for rigid melittin as a consequence of dynamical averaging.
with the C- and N-terminal parts. The main difference between the simulation results for
the flexible (left) and rigid (right) melittin dimer is the amplitude of the fluctuation of the
hydrophobicity, but not its sign. Simulations of rigid melittin in the 51 Å (panels A and B)
and 60 Å boxes (panels C and D) are similar to one another but they differ along the trajec-
tory by up to $\Delta\delta \lambda \sim 0.4$ (see Figure 10). There are also differences between the A (black)
and B chains (red) for rigid melittin. The difference in the monomer structures (RMSD of
1.6 Å) leads to significant differences in $\delta \lambda$ (see Figures 11A and B. As an example, Leu13A
is considerably more hydrophobic ($\delta \lambda_{\text{Leu13A}} = 0.7$) than Leu13B ($\delta \lambda_{\text{Leu13B}} = 1.4$). Inspection
of the dimer structure shows that Leu13A points toward the dimerization interface whereas
Leu13B points away from it into the solvent. For flexible melittin (panels A and C), the
LH for the A and B chains are more similar to one another for both box sizes. This is a
consequence of averaging along the structural dynamics. It also suggests that simulations on
the 100 ns time scale are sufficient to converge $\delta \lambda$ for melittin. Nevertheless, there remain
certain differences between simulations in the two water boxes for individual residues, e.g.
$\langle \delta \lambda_{\text{Val5B}}^{51} \rangle = 1.05$ vs. $\langle \delta \lambda_{\text{Val5B}}^{60} \rangle = 0.86$, see Figure 11 and Table 3.

Table 3: Average $\delta \lambda_{\text{phob}}$ for the hydrophobic residues from Figure 1 in Ref. 7

| Residue | 51 Å flexible | 51 Å rigid | 60 Å flexible | 60 Å rigid |
|---------|---------------|------------|---------------|------------|
| Val5A   | 0.976         | 1.185      | 1.003         | 1.246      |
| Val8A   | 0.929         | 1.322      | 0.941         | 1.375      |
| Leu9A   | 0.954         | 0.875      | 0.889         | 0.876      |
| Leu13A  | 0.967         | 0.741      | 1.030         | 0.756      |
| Leu16A  | 0.909         | 0.808      | 0.917         | 0.824      |
| Ile20A  | 1.019         | 1.049      | 1.071         | 0.992      |
| Val5B   | 1.046         | 1.484      | 0.861         | 1.494      |
| Val8B   | 1.038         | 0.889      | 0.806         | 0.877      |
| Leu9B   | 0.814         | 0.900      | 1.071         | 0.867      |
| Leu13B  | 1.016         | 1.393      | 1.006         | 1.373      |
| Leu16B  | 0.835         | 0.637      | 1.012         | 0.626      |
| Ile20B  | 1.087         | 0.845      | 0.988         | 0.824      |

Finally, the two-dimensional LH-CCM (see Figure S21) for all four systems and their differ-
ences between rigid and flexible dimer (bottom row of Figure S21) have been determined. As can be anticipated from Figure 10, the LH cross correlation maps for the two box sizes are similar for rigid melittin dimer (see Figure S22 left panel). On the other hand, the differences between rigid and flexible melittin dimer in the two boxes are considerably larger, as the bottom row of Figure S21 demonstrates. While for the 51 Å box differences primarily occur at the interface (upper left quadrant), differences for the larger 60 Å box occur both at the interface and along the two helices. Furthermore, the amplitude of the differences increases in going from the 51 Å to the 60 Å box.

The difference between flexible melittin dimer in the 51 Å and 60 Å boxes is shown in Figure S22, right panel. Increasing the box size leads to more pronounced cross correlation peaks between the beginning of helix A and the end of helix B. A slightly less pronounced increase in the correlation is found for the end of chain A and the beginning of chain B. Corresponding radial distribution functions are reported in Figure S23. Even for rigid melittin in the 51 Å (red) and 60 Å (blue) boxes (e.g. for Gly3A and Gln26B) there are slight differences between the \( g(\mathbf{r}) \). Compared with rigid melittin, the \( g(\mathbf{r}) \) for flexible melittin are all less structured. Except for Ile2B they also agree well for the two box sizes.

For the rigid and flexible dimer, differences for the two box sizes also occur as shown in the \( \Delta CCC \) map (Figure S22). They effect the local hydrophobicity which is computed from the water structuring. For the rigid protein surface the differences are essentially independent of box size, as shown in the left panel. For the flexible dimer there are significant differences. They arise both from protein structural changes and the surrounding water structuring. In this context it is interesting to note that \( g(\mathbf{r}) \) around Leu9A and Leu9B in Figure S20 in the 60 Å box are virtually identical, whereas the LH differs by almost 15 % (0.89 vs. 1.07, see Table 3). As LH includes both the distance between the water oxygen atom relative to the protein surface and the angular orientation of the OH vector, this difference in LH
is likely to be related to different orientations of the water network around Leu9A and Leu9B.

Conclusions

The present work analyzed the local hydrophobicity around key residues at the protein interfaces for hemoglobin and melittin. It was found that the local hydrophobicity measure for Hb provides valuable insight into the effect of different box sizes from MD simulations. Specifically, analysis of the local hydrophobicity cross correlation coefficients for Hb provided a dynamical view of Perutz’s stereochemical model involving breaking and formation of salt bridges at the $\alpha_1/\beta_2$ and $\alpha_2/\beta_1$ interfaces. Also, the more detailed analysis of the simulations in the 90 Å and 120 Å boxes demonstrates that they decay to known but different intermediate structures upon destabilization of the $\alpha/\beta$ interface following a decrease in LH, i.e. as a consequence of reduced water density or change of water orientation at the protein/water interface. This is consistent with earlier findings\(^4\) that reported a reduced number of water-water hydrogen bonds for the smaller boxes, which influences the equilibrium between water-water and water-protein contacts and hence the water activity. The present results also support recent extensive simulation studies of the Aβ peptide which show that the hydrophobic surface area increases significantly in small cells along with the standard deviation in exposure and backbone conformations.\(^29\) As is also reported here (see Figure 7), hydrophilic exposure was found to dominate in large boxes whereas hydrophobic exposure is prevalent in small cells. This suggests there is a weakening of the hydrophobic effect in smaller water box sizes.

Early experiments indicate that $T_0$ is significantly ($\sim 8$ kcal/mol, equivalent to $K_{T_0} \approx 6.7 \times 10^5$) more stable than $R_0$.\(^1\) Also, the rate for the $R_0 \rightarrow T_0$ has been determined as $15700 \pm 700$ s\(^{-1}\) at 303 K, corresponding to a transition time of $\sim 20$ µs.\(^30\) As shown in
Ref.\textsuperscript{31} this implies that the T\textsubscript{0}→R\textsubscript{0} transition occurs on a time scale of 1 to 10 s by use of the Arrhenius equation. This is far too long to be sampled directly by MD simulations with explicit solvent in a statistically meaningful way. As an example, for association free energies in protein-ligand and protein-protein interactions from replica exchange coarse grained simulations, a total simulation time of > 5 \textmu s was deemed necessary for convergence\textsuperscript{32} and similar studies were carried out for protein-ligand interactions using atomistic force fields.\textsuperscript{33,34} Alternative approaches, such as conjugate peak refinement, string methods, or nudged elastic band in explicit solvent are also ways to more quantitatively investigate the transition state region.\textsuperscript{35–37} However, to quantify differences between the T\textsubscript{0} and R\textsubscript{0} structure or structures evolving towards the R\textsubscript{0} state (as done here), explicit knowledge of the transition state region is not required.

For the melittin dimer the role of box size on the hydration dynamics was expected to be smaller, based on earlier work on the hydrophobic effect.\textsuperscript{38} Nevertheless, the analysis of rigid melittin dimer, which was studied in previous work,\textsuperscript{7} suggests that the water distribution is affected by the box size for the 51 Å and 60 Å boxes. These differences become more pronounced when the protein structure is allowed to change in the simulations.

Complementary to radial distribution functions \(g(r)\), the local hydrophobicity (LH) provides a time-dependent quantitative local measure characterizing the water dynamics and structure around a protein. When combined with time-dependent structural information a more complete picture for the coupled protein-water dynamics emerges. It provides valuable information about thermodynamic manifestations of structural changes at a molecular level.
Data and Code Availability

The water-structure analysis code used to calculate \( \delta \lambda_{phob} \) is publicly available at https://github.com/mjmn/interfacial-water-structure-code.

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