A Quantized $\nu = 5/2$ State in a Two-Subband Quantum Hall System

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The evolution of the fractional quantum Hall state at filling 5/2 is studied in density tunable two-dimensional electron systems formed in wide wells in which it is possible to induce a transition from single to two subband occupancy. In 80 and 60 nm wells, the quantum Hall state at 5/2 filling of the lowest subband is observed even when the second subband is occupied. In a 50 nm well the 5/2 state vanishes upon second subband population. We attribute this distinct behavior to the width dependence of the capacitive energy for intersubband charge transfer and of the overlap of the subband probability densities.

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Introduction and key findings - Currently, there is strong interest in the even-denominator fractional quantum Hall state (FQHS)\(^1\,2\) at filling factor $\nu = 5/2$, partially because of its potential relevance for topological quantum computation resulting from the non-Abelian statistics its quasi-particle excitations are predicted to obey\(^3\). The 5/2 state is usually studied in GaAs/AlGaAs-heterostructures with a single heterointerface or relatively narrow quantum wells (QWs) where electrons occupy only the first subband (1SB). By widening the quantum well the physics is enriched. The accessible density range in these samples is large enough to substantially populate the second subband (2SB). This adds an additional degree of freedom and produces novel ground states as exemplified by the appearance of quantum Hall states at filling 1/2\(^4\) and 1/4\(^5\) as well as quantum Hall ferromagnetic phases absent in single subband systems\(^6\,8\). The total filling factor $\nu_T$, i.e. the ratio of the electron density $n$ and the Landau level (LL) degeneracy, is then the sum of the subband fillings: $\nu_T = \nu_{1SB} + \nu_{2SB}$. Recently, the 5/2 state was investigated in such wide QWs\(^7\,11\). The incompressible 5/2 quantum Hall state was observed when the 2SB was empty, but was lost upon populating it. Instead a compressible composite fermion liquid formed in the half filled lowest LL of the 2SB while $\nu_{1SB} = 2$. This literature also suggested that the 5/2 state is stabilized just before the 2SB is occupied\(^11\).

Here, we report that in very wide QWs, the 2D system formed by the 1SB condenses in the 5/2 fractional quantum Hall state even when the 2SB is occupied. The 5/2 state continues to exist as an incompressible fluid over a wide range of fillings of the 2SB. This is different from previous reports on two-SB systems\(^7\,10\) where quantum Hall features follow the total filling factor. We attribute the dramatic difference between previous reports and our data to the increased QW width in our samples resulting in a larger spatial separation of the charge distributions of the two SBs. This suppresses intersubband scattering and increases the Coulomb energy involved when transferring charge between the two SBs. The existence of a quantized 5/2 state in close proximity to an independent 2DES of variable density (formed by the 2SB electrons) may enable to study their interaction.

Samples and measurements - Magnetotransport experiments were carried out on 400 µm wide Hall bars of single sided modulation doped GaAs/AlGaAs heterostructures containing an 80, 60 or 50 nm wide QW. The spacer thickness is 66 nm for the 80 and 60 nm QW samples and 82 nm for the thinnest QW. The samples are overdoped either using a short period superlattice doping (60 and 80 nm QW)\(^12\) or conventional DX center doping (50 nm QW). An in-situ grown doped QW, located 800 nm below the 2DES, serves as a backgate (BG) to tune the electron density. Resistance measurements were performed with standard lock-in technique in a dilution refrigerator with a base temperature below 20 mK.

Figure 1(b) shows the longitudinal resistance in the density versus magnetic field plane measured on the 80 nm quantum well sample. Panel (a) shows the Hall resistance for selected densities. At lower densities electrons occupy only the 1SB and a 5/2 quantized Hall state is observed. At higher $n$ when also the 2SB is populated the 5/2 state for the total electron density loses its quantization. The longitudinal resistance no longer vanishes and the Hall plateau disappears in accordance with previous observations\(^8\,11\). The 5/2 state of the 1SB, however, persists as an incompressible quantum Hall state over a wide range of fillings of the 2SB: the longitudinal resistance still vanishes and the Hall resistance still shows a plateau at filling factors ($\nu_{1SB} = 5/2, \nu_{2SB} > 0$). Yet, the plateau is found at progressively lower $R_{xy}$ as is expected when the total density increases. Meanwhile the 2SB electrons go through a series of integer and fractional
quantum Hall states as indicated in panel (b). The overall structure shows that the fixed filling factors of the 1SB and 2SB correspond to a zigzag course. This can be understood as a consequence of intersubband charge transfer as addressed below and in [13].

Hence, we have realized a compound system in which a 2DES condensing in a quantized 5/2 state coexists with a second 2DES whose density we can vary (in our current samples) between 0 < ν2SB < 1. Here we investigate the transport properties of this system. Even though the 5/2 state is known to be very fragile, we find it surprisingly undisturbed by the presence of the partially populated 2SB. Figure 2(c) displays the activation energy (obtained from temperature dependent measurements) along the line of constant filling factor ν1SB = 5/2 as a function of the total density. In the ν2SB = 0 regime its absolute value and density dependence are comparable to our previous findings on a 30 nm QW [14]. When the 2SB is populated the activation energy Δν1SB=5/2 can only be determined where the electrons in the 2SB condense into an incompressible state and thus do not contribute to the longitudinal resistance (other regions are shaded in blue). There, Δν1SB=5/2 remains independent of the 2SB filling within the experimental uncertainty. This underlines that the only weakly changing density of the 1SB determines this state, while the influence from the 2SB is small. We note that intersubband scattering may affect this state. However, in our samples the mobilities drop only by about one third upon population of the 2SB, indicating that intersubband scattering is not such a large effect.

Our observation of a 5/2 state in the 1SB at a non integer filling of the 2SB implies that the topmost occupied LLs of both SBs are pinned at the same energy. Otherwise, it would be energetically favorable to transfer electrons from one SB to the other, filling up the lower of the partially populated levels (see [13] for details). But such intersubband charge transfer quickly aligns the topmost partially filled SB levels due to the additional capacitive energy involved. Charge transfer then stops until one of the Landau levels is completely filled. This energy depends strongly on the QW width. We address this theoretically below. We first look at the QW width dependence in experiment. We observe the (ν1SB = 5/2, ν2SB > 0) state also in a 60 nm QW as illustrated in Fig. 2(a). However, the behavior in a 50 nm QW (panel b) is different. In contrast to the wider QWs, no quantum Hall features associated with only the 1SB or 2SB show up once the 2SB is populated. Rather, nearly all features follow the total filling factor. The 5/2 quantized Hall state disappears once the 2SB gets populated. This is identical to what has been reported previously on QWs of up to 57 nm width [15, 16]. We conclude that the QW width plays a crucial role in observing the incompressible 5/2 state when two SBs are occupied.

Intersubband charge transfer - As mentioned above, a partial filling of the topmost Landau levels of both SBs requires the alignment of these LLs. This is possible because these levels can be shifted with respect to each other when charges are transferred between the two subbands [13]. The individual SB densities (and wavefunctions) can be obtained by carrying out self-consistent

FIG. 1: (Color) Transport data of a 2DES residing in an 80 nm wide quantum well. An in-situ grown backgate allows a variation of the electron density. (a) Hall resistance for selected densities (given in 10\(^{11}\)/cm\(^2\)). (b) Longitudinal resistance (see Fig. 2(b) for a colorbar). Upon occupation of the second subband its electrons show integer and fractional quantum Hall states (examples indicated on the left). Meanwhile, the 5/2 state of the lower subband continues to exist. Its quantization is apparent from a plateau in \(R(x)\) for a colorbar). Upon occupation of the second subband its electrons show integer and fractional quantum Hall states (examples indicated in panel (b). The over-
calculations for each point in the density versus magnetic field plane, taking into account the \(B\)-dependent density of states (DOS) \[16\]. Here, we choose a different approach. We perform self-consistent calculations only for \(B = 0\) and treat the magnetic field induced effects perturbatively. This gives some insight into the importance of the magnetic field. The magnetic field induced changes are limited by the degeneracy of the LLs and charge transfer is an effective distance. If the SB probability densities \(|\Psi_1(z)|^2\) and \(|\Psi_2(z)|^2\) with \(\Psi_{1,2}\) the wavefunctions of the 1SB and 2SB) are well separated the distance of their maxima can be used as an approximate value for \(d^{\text{eff}}\). Here we calculate it for partially overlapping probability densities. The transfer of \(\epsilon \Delta n\) between the two SBs creates a charge density \(\rho(z) = \epsilon \Delta n (|\Psi_1(z)|^2 - |\Psi_2(z)|^2)\) inside the QW. The resulting Hartree energy per unit area is \(E_H = \frac{1}{2} \int dz dz' \rho(z) v(z - z') \rho(z')\), with \(v(z) = -|z|/(2\epsilon_0)\) denoting the Coulomb interaction between two homogeneously charged parallel planes. The energy shift between the SBs is then \(\epsilon \Delta V = \partial E_H/\partial (\Delta n)\), such that, with \(f(z) = |\Psi_1(z)|^2 - |\Psi_2(z)|^2\), the effective distance can be written as
\[
d^{\text{eff}} = -\frac{1}{2} \int dz dz' f(z)|z - z'|f(z').
\]
In Fig. 4 we display results for our specific heterostructures and also convert \(d^{\text{eff}}\) into the energy shift per unit of transferred areal charge \(\Delta V/\Delta n\). In the wider QW samples \(d^{\text{eff}}\) increases with the total density reflecting a progressively larger separation between the charges occupying the 1SB and 2SB. The 50 nm QW shows a qualitatively different behavior, namely \(d^{\text{eff}}\) is approximately constant and remains small when the 2SB starts to be populated.

From Fig. 4, we conclude that in general for narrower QWs more charges need to be transferred between the two SBs in order to align their topmost partially filled LLs. At the same time the total charge that can be transferred is limited by the degeneracy of the LLs and charge
This overlap enhances the probability for intersubband probability densities related to a larger overlap between the charge or probable regions of coexisting fractional SB filling factors. For the 2SB becomes occupied. Our calculations indicate a similar effect: It mixes the otherwise orthogonal 1SB and 2SB wavefunctions, provided that the probability densities associated with these wavefunctions overlap in space. Indeed, we observe in tilted field experiments (detailed results will be published elsewhere) that in the 80 nm QW a co-existence of partially filled LLs in both SBs is maintained even up to a tilt angle of 70°. In a 60 nm QW already at 10° tilt angle, all single subband quantum Hall states have vanished once the 2SB becomes occupied. Hence, these tilted field measurements support the conjecture that a larger spatial overlap between the SB probability densities is responsible for the lack of single subband QH features once the 2SB becomes occupied in narrower QWs such as our 50 nm QW sample.

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Such charge transfer is evident, for example, from the negative slope of the FQHS of the 1SB when increasing the total density in our 60 nm sample: a small amount of charge is progressively transferred back from the 1SB to the 2SB. More details can be found in [13].

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We recently learned of independent measurements indicating the coexistence of subbands with partial filling factors. These regions are less extended than reported here, which can be explained by the smaller QW widths used there. See [arXiv:1109.1391v1].