Starburst evolution: free–free absorption in the radio spectra of luminous IRAS galaxies

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ABSTRACT

We describe radio observations at 244 and 610 MHz of a sample of 20 luminous and ultra-luminous IRAS galaxies. These are a subset of a sample of 31 objects that have well-measured radio spectra up to at least 23 GHz. The radio spectra of these objects below 1.4 GHz show a great variety of forms and are rarely a simple power-law extrapolation of the synchrotron spectra at higher frequencies. Most objects of this class have spectral turn-overs or bends in their radio spectra. We interpret these spectra in terms of free–free absorption in the starburst environment.

Several objects show radio spectra with two components having free–free turn-overs at different frequencies (including Arp 220 and Arp 299), indicating that synchrotron emission originates from regions with very different emission measures. In these sources, using a simple model for the supernova rate, we estimate the time for which synchrotron emission is subject to strong free–free absorption by ionized gas and compare this to expected H II region lifetimes. We find that the ionized gas lifetimes are an order of magnitude larger than the plausible lifetimes for individual H II regions. We discuss the implications of this result and argue that those sources which have a significant radio component with strong free–free absorption are those in which the star formation rate is still increasing with time.

We note that if ionization losses are important, the resulting curvature of the radio spectrum would much reduce the often observed deficit in fluxes above ~10 GHz.

Key words: galaxies: active – infrared: galaxies – radio continuum: galaxies.

1 INTRODUCTION

The radio emission from star-forming galaxies is the result of two emission processes, non-thermal synchrotron, and thermal bremsstrahlung, or free–free emission. Synchrotron is by far the dominant component in the 1–10 GHz range and is characterized by a power-law emission spectrum, \( f_\nu \propto \nu^{-\alpha} \), where \( \alpha \approx 0.8 \). Free–free emission has an almost flat spectrum and the emission falls with frequency only as \( \nu^{-0.1} \). Therefore, towards higher frequencies free–free emission becomes increasingly important and radio spectra are expected to show a flattening beyond ~10 GHz.

In luminous infrared galaxies (LIRGs) and ultra-luminous infrared galaxies (ULIRGs), although such a flattening is sometimes seen, the majority of radio spectra, even when measured to 23 GHz, show no such flattening. In fact, there is a tendency for the spectra to steepen (Clemens et al. 2008). Despite this, Clemens et al. (2008) showed that the spectral index between 8.4 and 23 GHz is flatter for sources with high values of the far-infrared–radio flux ratio, \( q \). As these sources, with an excess of infrared relative to radio emission, are expected to be younger, they would be expected to have proportionately more free–free gas and thus shallower spectral indices at high frequencies.

As we will see later, the radio spectra of LIRGs and ULIRGs also hold surprises towards low frequencies, with spectra showing a variety of bends and turn-overs. From a theoretical standpoint, there is more than one way in which the radio spectrum may flatten towards low frequencies. There are those processes that absorb radio photons, free–free absorption and synchrotron self-absorption and those that cause energy losses of the relativistic electron population directly. Of these, ionization losses have been considered by Thompson et al. (2006) as a cause for the flattening of starburst radio spectra towards low frequencies. However, as illustrated by these authors, the flattening is rather gradual. Our data show evidence of rapid changes in spectral index and also inversions of the
spectra, much more consistent with an absorption process with a strong energy dependence.

Both free–free absorption and synchrotron self-absorption could rapidly absorb the power-law synchrotron spectrum towards low frequencies. However, synchrotron self-absorption requires extremely high brightness temperatures in order to be significant, and these are just not attained (with the possible exception of UGC 8058) in our sources (Condon et al. 1991). We therefore consider free–free absorption to be the defining mechanism for the spectral shapes of this sample, especially at low radio frequencies.

Here we describe new observations of a sample of LIRGs and ULIRGs at 244 and 610 MHz made with the Giant Metrewave Radio Telescope (GMRT), which we combine with archival data and our previous 23 GHz data to produce well-sampled radio spectra across this wide frequency range. We consider the structure of the starbursts in these objects that is implied when their radio spectra are described in terms of the free–free absorption of a synchrotron power law.

2 SAMPLE SELECTION

Our sample is based on that of Condon et al. (1991) who made 8.4 GHz observations of the 40 ULIRGs brighter than 5.25 Jy at 60 μm. In Clemens et al. (2008), we described new observations at 23 GHz and the collection of archival data for a sub-sample of 31 of the 40 described by Condon et al. (1991). Some objects were excluded for observational reasons, as described in Clemens et al. (2008). Only 20 of these 31 objects were observed at the GMRT at 244 and 610 GHz simply due to observing constraints.

3 OBSERVATIONS

Observations at 244 and 610 MHz were made between 2008 January 13 and 16 at the GMRT. The two frequencies were observed simultaneously using the ‘dual’ mode, with one polarization for each frequency. The total bandwidth of 8 (16) MHz was split into 64 (128) channels at 244 (610) MHz. The total integration times for the sources were between 30 and 120 min with scans on-source being interleaved between scans of phase calibrators approximately every 30 min. Both 3C 147 and 3C 286 were used as flux calibrators.

Data reduction was carried out using the National Radio Astronomy Observatories (NRAO) Astronomical Image Processing System (AIPS). After initial, channel-based, editing to remove data affected by interference, bandpass calibration was applied using one of the flux calibrators. The data were calibrated in the standard way by forming a ‘channel 0’ data set from the average of 10 channels near the centre of the band. The complex gains from this process were then copied to the line data before reducing the number of channels to a factor of 10 for the purpose of map making.

Maps were made by Fourier transformation of the data in each channel to produce ‘dirty’ images and beams (AIPS task ‘imagr’). The images and beams were then combined to produce a single continuum image and beam for each source, thus avoiding bandwidth smearing. The resulting maps were deconvolved using the clean algorithm and the combined beam. Where the source was sufficiently bright, self-calibration was further applied (varying only the antenna phases) to improve the signal-to-noise ratio. The final maps typically had resolutions of 13 and 5 arcsec and rms noise levels of 5 and 0.5 mJy at 244 and 610 MHz, respectively.

Flux densities were measured by direct integration on the maps via the AIPS task tvstat. These integrated fluxes (reported in Table 1) have errors which include both the rms noise and calibration errors.

4 RESULTS

4.1 Low frequency radio spectra

The radio spectra shown in Fig. 1 show various forms at low frequencies. These include an almost straight power law from 22 GHz down to 244 MHz (e.g. IC 1623), a single turn-over at low frequencies (NGC 1614), evidence of two turn-overs (e.g. IR 03359+1523) and a gradual flattening towards low frequencies (e.g. NGC 2623). In addition, IR 08572+3915 shows an almost flat spectrum. This may rise at frequencies below 1 GHz but the data point at 610 GHz has a large error and is marginally consistent with a spectrum that remains flat.

The flattening of the radio spectra is due to absorption of the power-law synchrotron emission, \( S \propto \nu^{-\alpha} \), where \( \nu \) is the frequency. In all but one case, this must be free–free absorption by ionized gas in the sources because the brightness temperatures are not high enough for synchrotron self-absorption to be important. Only UGC 8058\(^1\) has an 8.4 GHz surface brightness sufficiently

| Source        | D (Mpc) | \( f_{244} \) (Jy) | \( f_{610} \) (Jy) |
|---------------|---------|------------------|------------------|
| NGC 34        | 77.1    | –                | –                |
| IC 1623       | 71.3    | –                | –                |
| CGCG 436–30   | 123.6   | –                | –                |
| IRAS 01364–1042 | 187.2  | –                | –                |
| III Zw 35     | 108.7   | –                | –                |
| UGC 2369      | 123.5   | 0.040 ± 0.020    | 0.066 ± 0.004    |
| IRAS 03359+1523 | 140.1  | <0.060          | 0.038 ± 0.005    |
| NGC 1614      | 60.9    | 0.250 ± 0.040    | 0.202 ± 0.005    |
| NGC 2623      | 76.1    | 0.161 ± 0.030    | –                |
| IRAS 08572+3915 | 235.8  | <0.050          | 0.011 ± 0.006    |
| UGC 4881      | 162.7   | 0.060 ± 0.010    | 0.056 ± 0.007    |
| UGC 5101      | 164.1   | 0.310 ± 0.030    | 0.212 ± 0.004    |
| IRAS 10173+0828 | 193.7  | <0.030          | 0.010 ± 0.002    |
| IRAS 10565+2448 | 170.0  | 0.080 ± 0.020    | 0.102 ± 0.007    |
| Arp 148       | 142.2   | 0.080 ± 0.020    | 0.058 ± 0.005    |
| UGC 6436      | 139.4   | 0.020 ± 0.010    | 0.032 ± 0.004    |
| Arp 299       | 48.0    | 2.350 ± 0.090    | 1.300 ± 0.030    |
| IRAS 12112+0305 | 292.1  | 0.035 ± 0.020    | 0.032 ± 0.006    |
| UGC 8058      | 172.6   | 0.590 ± 0.020    | 0.403 ± 0.020    |
| UGC 8387      | 96.8    | 0.240 ± 0.005    | 0.164 ± 0.008    |
| NGC5256       | 115.9   | 0.410 ± 0.040    | 0.225 ± 0.006    |
| UGC 8696      | 157.3   | 0.394 ± 0.020    | 0.222 ± 0.008    |
| IRAS 14348–1447 | 326.7  | <0.060          | 0.030 ± 0.006    |
| I Zw 107      | 166.0   | 0.180 ± 0.020    | 0.090 ± 0.005    |
| IRAS 15250+3609 | 218.7  | –                | –                |
| NGC 6286      | 80.3    | 0.500 ± 0.030    | 0.309 ± 0.010    |
| NGC 7469      | 66.4    | –                | –                |
| IC 5298       | 110.6   | –                | –                |
| Mrk 331       | 72.3    | –                | –                |

\(^1\)Although this source is known to contain compact radio emission from an active galactic nucleus which shows variability on time-scales of years, Ulvestad et al. (1999) show that this variability is likely confined to frequencies above 5 GHz. In our spectrum the data points at 1.4, 4.8, 8.4, 15 and 22.5 GHz were, in any case, all made on the same date and a turn-over is already seen between 1.4 and 4.8 GHz. See Section 4.4.
high that synchrotron self-absorption may be important (Condon et al. 1991).

The shape of the low-frequency spectrum depends, almost entirely, on the quantity and distribution of ionized gas with respect to the source of synchrotron emission. The free–free optical depth is \( \tau_\nu \propto n_e^2 L \nu^{-2.1} \), where \( n_e \) is the ionized particle density, \( \nu \) is the frequency, \( L \) is the path-length along the line of sight and \( n_e^2 L \) is the emission measure. Radio spectra will show a turn-over where \( \tau_\nu = 1 \). If the frequency of this turn-over is \( \nu_t \), then the optical depth is given by \( \tau_\nu = (\nu/\nu_t)^{-2.1} \).

The radio spectra of normal, star-forming galaxies have been reviewed in detail by Condon (1992). The spectra are the result of emission from a medium containing both synchrotron and free–free emitting gas. Based on observational results, Condon assumed that the thermal emission contributes 10 times less than synchrotron emission at 1 GHz. Based on equation (6) of Condon, the radio surface brightness therefore varies with frequency according to

\[
\frac{S}{\Omega} \propto T_e (1 - e^{-\tau_\nu}) \left[ 1 + \frac{1}{H} \left( \frac{\nu}{\text{GHz}} \right)^{0.1-\alpha} \right] v^2,
\]

where \( S \) is the flux density, \( \Omega \) is the area subtended by the source, \( T_e \) is the electron temperature and \( H \) is the thermal fraction. For synchrotron emission that contributes 10 times that of thermal emission at 1 GHz, as assumed by Condon (1992), \( H = 0.1 \). Fig. 4 of Condon shows the family of curves that result from varying the turn-over frequency, the frequency at which the optical depth \( \tau_\nu = 1 \). In Fig. 2, we illustrate the effect of varying \( H \) for a fixed turn-over frequency.

Because we do not have measurements of the source size, \( \Omega \), at every measured frequency equation (1) is only applicable under the assumption that the size of each source is not a function of frequency. Although cosmic-ray diffusion is known to make this untrue for some nearby objects, the very short synchrotron lifetimes expected in the present sample should ensure very similar source sizes at all frequencies under study here.

For normal galaxies, the spectral index is close to \(-\alpha\) at intermediate frequencies (5 GHz) and flattens towards higher frequencies due to the increasing contribution of free–free emission. Towards low frequencies, the spectra turn over due to the effects of free–free absorption. The frequency at which this turn-over occurs depends on the emission measure of the ionized gas. As pointed out by Condon, real sources, such as M82, may be expected to show a flattening of the radio spectrum towards low frequencies rather than a turn-over due to source inhomogeneity.

We use equation (1) as a starting point for the analysis of our radio spectra of luminous IRAS galaxies.

Each turn-over frequency in our spectra, and some have more than one, is the result of absorption by ionized gas with a different emission measure. Therefore, by fitting one or more components described by equation (1) we can determine \( n_e^2 L \) for our sample galaxies via the standard expression for the free–free absorption
Figure 1 – continued
coefficient (equation 1 in Condon 1992). This step requires an assumption for the electron temperature, which we take to be $10^4$ K. In fitting equation (1) to the data, we consider the following cases.

(i) The spectrum is straight to the lowest measured frequency (e.g. IC 5298) – no turn-over can be estimated.

(ii) The spectrum shows a single turn-over. Either only a single absorbed component is visible (e.g. NGC 1614) or there is evidence of another component whose flux continues to rise to the lowest measured frequency (e.g. UGC 5101). In this case we fit equation (1) allowing $\alpha$, $H$ and the turn-over frequency to vary. If data points are insufficient, we fix $\alpha = 0.8$. We allow for the presence of an unabsorbed component by fitting an additional power law with the same power-law index. For those objects where only one component is seen, we provide a limit to the possible contribution of an unabsorbed component by finding the maximum contribution of a straight power law that is consistent with the lowest frequency data point. We refer to this as model 1.

(iii) The spectrum shows two clear turn-overs (e.g. IRAS 03359+1523). We fit two components obeying equation (1), but fix $H = 0.1$ and $\alpha = 0.8$. For each component, we fit the turn-over frequency and the flux ratio of the components. If equation (1) is represented by $f_i$, then fit $f = f_1 + xf_2$. In this case, if component $f_2$ has the lower break frequency, the constant $x$ represents the relative area covered by $f_2$, i.e. $\Omega_2/\Omega_1$, because we measure integrated fluxes rather than surface brightnesses. We refer to this as model 2.

Equation (1) was fitted to the data via a non-linear least-squares procedure that minimized $\chi^2$-squared between the data and model. We limited the number of parameters that were allowed to vary so as to remain fewer than the number of data points. In Table 2, we list the model used and associated fit parameters. In some cases, where parameter values were fixed, reasonable fits could not be obtained with a power-law index of $\alpha = 0.8$ and/or $H = 0.1$. In these, alternative fixed values were used, as indicated in Table 2.

If the best-fitting solution passed through less than three quarters of the data points, the fit was deemed to be poor. In these cases, shown as dot-dashed lines in Fig. 1, the derived quantities are uncertain and appear in parentheses in Table 2. In these cases, a good fit would require either a more complex model or more parameters to be varied within the adopted model, beyond those permitted by the data.

The model fits are shown in Fig. 1. We note that the values of $H$, and to a lesser extent $\alpha$, are often rather poorly constrained by the data. $H$ tends to be poorly determined because it is mostly constrained by high frequency data points beyond 8.4 GHz. Here the fractional thermal emission should be significant (in normal galaxies, $\gtrsim 30$ per cent of the emission at 8.4 GHz is thermal). Equation (1) is a spectrum that flattens towards higher frequencies. However, as already noted in Clemens et al. (2008) the radio spectra of LIRGs and ULIRGs often do not show the flattening expected due to free–free emission and frequently show a steepening. Indeed, Fig. 1 shows several examples where the model over-predicts the flux at $>10$ GHz. The fitted thermal fractions, which are generally much lower than 0.1, are a consequence of the fact that only a spectral flattening is permitted by equation (1). This shows that there is an effect that is not taken into account in the simple model that we apply here and is discussed in Section 6.1.

The spectral index, $\alpha$, on the other hand, is poorly constrained by the limited number of data points when the turn-over frequency occurs at frequencies so high that no part of the spectrum is approximately straight.

However, we are mainly concerned with identifying the frequency of the turn-over seen towards longer wavelengths and the relative strength of the two emission components in those cases where a second component is present. These values are only very weakly affected by the value of $H$ and weakly by the value of $\alpha$.

4.2 General form of the radio spectra

In almost all cases, our low frequency radio data have revealed the presence of a turn-over in the radio spectrum. Although the turn-overs are often at frequencies above 610 MHz, such turn-overs were previously detected only at a single frequency. For an object with only three or four measured fluxes, there was little justification for fitting anything other than a straight line to the data.

The addition of low frequency radio data to the spectra of this sample of LIRGs and ULIRGs shows that the spectra are frequently more complex than previously thought. Galaxies that showed evidence of turn-overs above 1.4 GHz, and would have been expected to show fluxes in contrast with decreasing frequency, often show spectra that actually rise again (e.g. NGC 2623). Although Condon (1991) pointed out that free–free absorption in real sources is likely to result in rather broad turn-overs or just a flattening of the spectrum due to source inhomogeneity, we often see rather more complex spectra, indicative of at least two emission components. This was unexpected.

Given our limited sensitivity at 244 and 610 MHz as well as the fact that there are rarely data below 244 MHz, it is likely that all sources in our sample have more than one emission component; we either do not detect the emission or have not observed at sufficiently low frequencies.

The presence of radio emission components with different characteristic turn-over frequencies tells us that there are populations of relativistic electrons in environments with diverse emission measures. There is more than one physical scenario consistent with this result, and we will discuss this issue in Section 5.1, but the most simple explanation may be that there are starbursts occurring in
two or more nuclei (as most of these galaxies are probably merger remnants, this would seem plausible). If either the mean ionized gas density or the path-length through the ionized gas to the supernovae were different in the two nuclei, different turn-over frequencies would result. A reference to the 8.4 GHz, 0.25 arcsec resolution maps of Condon et al. (1991) shows that although some sources with two emission components do indeed show two spatially resolved nuclei (e.g. Arp 220), there are others that do not (e.g. NGC 2623) and also sources that show a single component radio spectrum but have two radio-bright nuclei (e.g. IRAS 14348–1447). Of course, higher resolution data may reveal additional double nuclei and additional radio data at lower frequencies may reveal second emission components where only one is currently detected. Therefore, we cannot, at present, identify separate emission components with separate starburst nuclei.

For all objects with sufficient data, we provide the 8.4 GHz flux ratio of the two model components in Table 2 or an upper limit where only a single component is detected.

### 4.3 Star formation rates

In order to estimate the star formation rates associated with each emission component, we make use of the calibration of Panuzzo et al. (2003) (based on Bressan, Silva & Granato 2002). This relates the 8.4 GHz luminosity to the star formation rate for stars with a Salpeter initial mass function (IMF) and masses in the range 0.15–120 M⊙ via $SFR = 258.4 \times 10^{-23} L_{8.4} M⊙ yr^{-1} (WHz)^{-1}$. In Table 2, we give the observed 8.4 GHz luminosities and implied star formation rates. For those objects with two emission components, we show the star formation rate for each. For galaxies in which two emission components are clearly detected, both imply high star formation rates. Although a high star formation rate is a requirement for detection at frequencies below 1.4 GHz if the radio emission is derived from supernova explosions, the significant fraction of sources in which two such components are detected (13/23 with data below 1.4 GHz) means that this is not uncommon among such galaxies. The radio emission at low frequencies is not therefore limited to the 8.4 GHz medium (with a lower emission measure).

In those objects where only a single component is detected, the upper limits on the fractional contribution of a component with a lower frequency turn-over only constrain the star formation rate to be <10 per cent that of the main component in three cases. The radio emission from luminous infrared galaxies is therefore consistent with high star formation rates in regions with two distinct emission measures (but see Section 5).
4.4 UGC 8058

UGC 8058 (Mrk 231) is the only source in our sample with a radio-loud active galactic nucleus (AGN). Vega et al. (2008) found that the contribution of the AGN to the bolometric luminosity was 24 per cent. The AGN is also variable, although the variability is seen only above 5 GHz (Ulvestad et al. 1999). Fig. 1 shows that our model succeeds in fitting the radio data for this source perfectly well as two absorbed components. The discontinuity is probably due to radio emission from the AGN that is seen only above 4.8 GHz due to strong absorption. In this case, the absorption may be synchrotron self-absorption or free-free absorption. The spectrum implies that at the epoch of observation of the data above 1.4 GHz (1995 November 17), the AGN contributed 66 per cent to the radio emission at 8.4 GHz (see Table 2). The radio emission at lower frequencies is therefore derived almost entirely from star formation, and we can use this fact to estimate the star formation rate. In Table 2, we give the star formation rate for this component alone. The models of Vega et al. (2008) assumed that AGN did not emit in the radio. Interestingly, the model for this source fitted well the low frequency radio data, but under-predicted the radio emission above 5 GHz.

4.5 Emission measures

Table 3 shows the emission measures derived from the fitted turn-over frequencies listed in Table 2. Also shown are the mean ionized gas densities implied by calculating the physical source sizes via the angular sizes measured at 8.4 GHz and distances given by

Table 3. Emission measures.

| Source       | $EM_1$ ($10^6$ cm$^{-6}$ pc) | $n_1$ (cm$^{-3}$) | $EM_2$ ($10^8$ cm$^{-6}$ pc) | $n_2$ (cm$^{-3}$) |
|--------------|------------------------------|-------------------|------------------------------|-------------------|
| NGC 34       | $\lesssim 3$                | -                 | -                            | -                 |
| IC 1623      | 23                           | 330               | -                            | -                 |
| CGCG 436–30  | $\lesssim 3$                | -                 | -                            | -                 |
| I01364–1042  | 11                           | 290               | -                            | -                 |
| III Zw 35    | 8.2                         | 310               | -                            | -                 |
| UGC 2367     | 0.8                         | 100               | -                            | -                 |
| I03359+1523  | 14.0                        | 1400              | 0.32                         | 68                |
| NGC 1614     | 0.24                        | -                 | -                            | -                 |
| I05189–2524  | 6.2                         | 200               | -                            | -                 |
| NGC 2623     | 9.9                         | 290               | -                            | -                 |
| I05872+3915  | 56                          | 780               | -                            | -                 |
| UGC 4881     | 0.32                        | 47                | -                            | -                 |
| UGC 5101     | 3.7                         | 190               | -                            | -                 |
| I10173+0828  | 90                         | $\gtrsim 1200$    | 1.8                          | $\gtrsim 166$    |
| I10565+2448  | 0.40                        | 35                | -                            | -                 |
| Arp 148      | 0.20                        | 42                | -                            | -                 |
| UGC 6436     | 0.66                        | -                 | -                            | -                 |
| Arp 299      | 62                          | 900               | 0.38                         | 70                |
| I2112+0305   | 15                          | 310               | 0.24                         | 40                |
| UGC 8058     | 53                          | $\gtrsim 950$     | 0.12                         | $\gtrsim 44$     |
| UGC 8387     | 31                          | -                 | 0.36                         | -                 |
| NGC 5256     | 0.074                       | 24                | -                            | -                 |
| UGC 8696     | 3.1                         | 130               | -                            | -                 |
| I14348–1447  | 3.1                         | 120               | -                            | -                 |
| IIZw 107     | 31                          | 460               | -                            | -                 |
| I5250+3609   | 16                          | $\gtrsim 500$     | -                            | -                 |
| Arp 220      | 13                          | 410               | 0.28                         | 59                |
| NGC 6286     | 0.14                        | -                 | -                            | -                 |
| NGC 7469     | 13                          | 560               | -                            | -                 |
| IC 5298      | $\lesssim 3$                | -                 | -                            | -                 |
| Mrk 331      | $\lesssim 3$                | -                 | -                            | -                 |

Condon et al. (1991). Our observations rarely resolve the sources, so we do not have a direct measure of the source sizes at 244 and 610 MHz. These could, in principle, be larger than those at 8.4 GHz due to cosmic-ray diffusion, but the synchrotron lifetime is anyway so short that the effect on the source size should be negligible. We cannot exclude the possibility, however, that the low-frequency radio emission comes from a more extended distribution of supernovae. However, such an extended component would also emit at 8.4 GHz and should have been detected by Condon et al. as extended halo emission. It is therefore probably reasonable to use the source sizes as measured by Condon et al. (1991).

Free–free absorption towards individual supernova remnants has been used to derive emission measures in M82 (Wills et al. 1997). A large fraction have turn-overs that are evident at 1.4 GHz, implying emission measures of $\geq 10^6$ cm$^{-6}$ pc. Other studies have identified regions with emission measures as high as $4 \times 10^5$ cm$^{-6}$ pc (Seaquist, Bell & Bignell 1985) and Clemens & Alexander (2004) derived a value of $10^7$ for the centre of the luminous IRAS galaxy, UGC 8387, based on high resolution radio data. Emission measures as high as $1.8 \times 10^8$ cm$^{-6}$ pc have been found for compact sources in the ‘Antennae’ galaxies by Neff & Ulvestad (2000). For those objects which were observed at 244 and 610 MHz, we find emission measures in the range of $0.07–140 \times 10^6$ cm$^{-6}$ pc.

For those sources in which two absorbed components are seen, we have fixed the thermal fraction of both so that $H = 0.1$. In this case, the spectra imply that the less absorbed component covers a much larger area than the more absorbed component, because equation (1) implies lower brightness temperatures for lower turn-over frequencies. Because we measure integrated fluxes, a larger source area is needed to fit the data. Of course, this may not reflect the true source structure. The component whose turn-over lies at a lower frequency may instead have a much lower thermal fraction. The similarity between decreasing the thermal fraction by a factor of, say, 10 and increasing the source size by a factor of 10 for a given turn-over frequency is shown in Fig. 2. At frequencies near the turn-over, and below, the resulting spectra are rather similar. At higher frequencies there is a significant difference, as the thermal emission contributes a larger fraction of the total. There is little difference, then, for the low frequency end of the model fits between these two possibilities, although at higher frequencies we limit our ability to fit the data. However, as mentioned above, the high frequency data are poorly modelled, and so constraining the thermal fraction at $\nu \gtrsim 10$ GHz is unreliable in any case.

To summarize, the relative strength of the two emission components places a constraint either on the relative physical area of each (thermal fraction of both fixed) or on the difference in thermal fraction between the two. A combination of these two extremes is also permitted, of course. In Table 2 we give the value of $\chi$, which is the relative physical area covered by the less absorbed component or, almost equivalently, the factor by which this component is poorer in thermal emission. For example, the component with a lower frequency turn-over in Arp 220 is either more spatially extended by a factor of 40 than the component with the higher frequency turn-over or has a thermal fraction 40 times lower.

5 IMPLICATIONS FOR STARBURST EVOLUTION

As discussed in Condon et al. (1991), with the exception of UGC 8058, there is little evidence that any of the galaxies in our

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2The two values we derive here for UGC 8387 straddle this value.
sample contain a radio-loud AGN. Vega et al. (2008), in fact, demonstrate that star formation alone is sufficient to explain the radio emission of every source except UGC 8058. In what follows, we assume that the radio emission is derived entirely from processes linked to star formation.

In this section, we focus particularly on the presence of two radio emission components in many sources in order to investigate the structure and evolution of the starbursts in these galaxies.

5.1 Relation between supernovae and ionized gas

As we have seen, the form of the radio spectra shown in Fig. 1 implies that synchrotron emission commonly emerges from at least two distinct regions with quite different emission measures. Such a situation could arise either because supernovae occur in two different environments or because cosmic rays are transported from one environment to the other after their acceleration in supernova shocks. Because higher energy electrons lose energy to synchrotron and inverse Compton losses more rapidly than low energy electrons, the low energy electrons emit synchrotron photons for longer and can therefore be transported further from their source. If all supernovae occur in dense ionized medium, consistent with regions of higher emission measure, the lower energy electrons may be transported to regions of lower emission measure while the more energetic particles end their synchrotron emitting lives still within the dense gas.

If the transport of relativistic electrons within H II regions is well described by a diffusion coefficient, then they can be transported a distance \( d \sim (Dt)^{1/2} \) before ceasing to emit synchrotron radiation (Condon 1992). Although we do not know the value of \( D \) in our sources, it has been estimated for the starburst galaxy NGC 2146 by Lisenfeld et al. (1996) to be in the range of \( 1-4 \times 10^{28} \text{cm}^2 \text{s}^{-1} \). If relativistic electrons emitting at 244 GHz have a synchrotron lifetime, \( \tau_s \sim 5 \times 10^4 \text{yr} \) in the strong magnetic fields characterizing these sources, then they could be transported a distance \( d \sim 80 \text{pc} \). As giant H II regions have sizes of the order of 10 pc and relativistic electrons may be transported by methods more efficient than diffusion (outflows or winds), the escape of relativistic electrons from H II regions seems feasible.

However, our radio spectra are characterized by quite distinct components, as opposed to a gradual change in the spectral index. Because the synchrotron lifetime is only a weak function of the emission frequency, \( \tau_s \propto v^{-1/2} \), the difference in the lifetime of electrons emitting at 8.4 GHz and at 244 MHz is only a factor of 6 for a given magnetic field strength. Given the inevitable inhomogeneity of these sources on parsec scales, it seems extremely unlikely that distinct spectral breaks could be caused by the preferential escape of lower energy cosmic rays.

It is far more likely, in fact expected, that supernovae occur in different environments. If the supernovae responsible for the synchrotron emission are those with progenitors with masses of \( \geq 8 \text{M}_\odot \) (Portinari, Chiosi & Bressan 1998), then synchrotron emission is generated for \( \sim 50\text{Myr} \) (for solar metallicity) after a burst of star formation, i.e. the lifetime of an \( 8 \text{M}_\odot \) star. Massive stars are born in dense molecular clouds, which they then ionize once luminous. Once these stars have formed, the parent cloud immediately starts to be disrupted, first by stellar winds and then by the first supernova explosions, which will occur after \( \sim 3 \) million years for a \( 100 \text{M}_\odot \) star.

The synchrotron emission component that shows the higher frequency turn-over, implying a higher emission measure, should therefore originate from cosmic rays accelerated by the most massive stars, which end their lives while still embedded in their parent H II regions. The less absorbed synchrotron component has its origin in supernova explosions of less massive stars (down to \( 8 \text{M}_\odot \)) that outlive the parent H II region.

In those sources with two emission components the lifetime of H II regions is therefore bounded, on the low side, by the lifetime of the most massive stars, \( \sim 3\text{Myr} \), and on the high side by the lifetime of an \( 8 \text{M}_\odot \) star. Only if H II region lifetimes lie in this range will emission components with very different emission measures be seen. For sources in which the burst of star formation began more recently than 50 Myr ago, the constraint on the H II region lifetime becomes \( 3\text{Myr} \lesssim \tau_{\text{H II}} \lesssim \tau_{\text{age}} \). The observed fraction of emission in each radio component constrains the lifetime within this range. Below, we attempt to estimate the mean H II region lifetime from the observed spectra.

5.2 H II region lifetimes

The H II region lifetime derived from the relative strength of the two radio emission components depends on various starburst parameters that are not known. These are the IMF, the temporal evolution of the star formation rate and the synchrotron emission from a supernova as a function of the progenitor mass. Bearing these limitations in mind, we can none the less make use of the modelling carried out in Vega et al. (2008). In this work, we modelled the spectral energy distribution from the near-infrared to the radio of the present sample of LIRGs and ULIRGs with starburst models. For each object, both the starburst age, \( \tau_{\text{age}} \), and the e-folding time of an assumed exponentially decaying burst, \( \tau_b \), were derived.

Because the starburst time-scales in these objects are thought to be very short, i.e. of the same order as the lifetime of the stars that undergo supernovae, we cannot assume that the supernova rate bears a one-to-one relation to the star formation rate. After the start of a burst, which then decreases in intensity with time, the supernova rate will initially rise. We estimate the supernova rate as follows. If the mass of a star and its lifetime are related via \( M(t) \), then for an IMF, \( \psi(M) \), the number of stars as a function of their lifetime is \( \psi(M(t)) \). If a star occurred at time \( t = 0 \), then at later time, \( \tau_{\text{age}} \), the number of stars about to end their lives is \( \psi[M(\tau_{\text{age}} - t)] \). The total supernova rate at time \( \tau_{\text{age}} \) is then given by

\[
SNR = \int_{t_{\text{age}} - t_{\text{max}}}^{t_{\text{age}} - t_{\text{min}}} \phi(t) \psi[M(t_{\text{age}} - t)] \, dt.
\]

If \( t_{\text{min}} \) and \( t_{\text{max}} \) are, respectively, the lifetimes of the most massive and least massive stars that end their lives as Type II supernovae (\( t_{\text{min}} \sim 3\text{Myr} \) for a \( 100 \text{M}_\odot \) star and \( t_{\text{max}} \sim 50\text{Myr} \) for an \( 8 \text{M}_\odot \) star) and if \( t_{\text{age}} \leq t_{\text{max}} \), then \( t = 0 \), but if the burst is older than the lifetime of the longest lived supernova precursors, so that \( t > t_{\text{age}} - t_{\text{max}} \), then \( t = (t_{\text{age}} - t_{\text{max}}) \). \( \phi(t) \) is the star formation rate.

Some fraction of the supernovae, occurring at the time-dependent rate given by equation (2), will explode while still embedded in their parent H II regions. These will be those stars with lifetimes shorter than the H II region lifetime, \( \tau_{\text{H II}} \). In equation (2), the lower limit on the integral becomes \( (t_{\text{age}} - t_{\text{max}}) \) in this case.

Because the synchrotron emitting lifetime of relativistic electrons, \( \sim 10^4-10^5 \) yr in our frequency range, is much shorter than any time-scale that characterizes the starbursts, we can interpret this supernova rate directly as the radio emission, if we assume that the radio emission per supernova is independent of the progenitor mass.

\[ \text{SNR} = \int_{t_{\text{age}} - t_{\text{max}}}^{t_{\text{age}} - t_{\text{min}}} \phi(t) \psi[M(t_{\text{age}} - t)] \, dt. \]
with lifetimes shorter than \( t_{\text{H II}} \) will explode as supernovae while still within the H II region, while those with lifetimes \( > t_{\text{H II}} \) will produce supernovae external to H II regions.

By using the starburst e-folding time and starburst ages, as given by Vega et al. (2008), we can plot, for each source, the time variation of the total supernova rate and the fraction of supernovae occurring while still embedded in H II regions. The fraction of supernovae occurring in H II regions as a function of the H II region lifetime, \( t_{\text{H II}} \), for a given \( t_{\text{age}} \) and \( t_b \) is shown in Fig. 4.

If we assume that the observed radio spectra reflect the properties of the mean H II region, then these fractions can be compared with the observed radio flux ratio as given by the values of \( f_{2}/f_{1} \) in Table 2. If \( f_{1} \) then refers to radio emission from supernovae occurring within H II regions, while \( f_{2} \) refers to that produced outside H II regions. For each source, we therefore find the value of \( t_{\text{H II}} \) and these are given in Table 4.

6 DISCUSSION

Individual H II regions cannot have lifetimes as long as those given in Table 4. They can only remain ionized for a time equal to the lifetime of the least massive stars with sufficient ionizing flux. This is only a few Myr. Therefore, at least for an exponentially decreasing burst, the H II regions that cause the free–free absorption cannot be those that host most of the supernovae explosions that generate the radio emission. Younger star-forming regions, still rich in ionized gas, may lie along the line of sight to a region of supernovae, however, and cause the free–free absorption. Such a situation would naturally result if star formation were initiated in the nuclei of the mergers and then propagated outwards, perhaps triggered by supernova shocks. In addition, this would create a shell-like (foreground screen) geometry for the ionized gas and free–free absorption would be much more efficient. Therefore, what we actually constrain is not the lifetime of an individual H II region in the usual sense, but rather the time for which ionized gas, sufficient to cause the observed absorption, persists along the line of sight. This ionized gas need not be in a single ‘H II region’. In what follows, we refer to ‘regions of ionized gas’ to avoid the connotation of a single cloud of gas.

But how does the situation change if the starburst is in an increasing phase? For a rising star formation rate the required ionized...
Table 4. Derived H\textsc{ii} region survival times for a Salpeter IMF. \( T \) is the lesser of the source age as derived in Vega et al. (2008) and 50 Myr, the lifetime of an 8 \( M_\odot \) star. \( t_{\text{esc}}^{\text{HII}} \) are the survival times for exponentially decreasing star formation rates and \( t_{\text{esc}}^{\text{HII}} \) for exponentially increasing star formation. In both cases, the e-folding time for the star formation in each source is as derived in Vega et al. (2008).

| Source      | \( t_{\text{age}} \) (Myr) | \( t_{\text{esc}} \) (Myr) | \( T \) (Myr) | \( t_{\text{esc}}^{\text{HII}} \) (Myr) | \( t_{\text{esc}}^{\text{HII}} \) (Myr) |
|-------------|-----------------------------|-----------------------------|---------------|----------------------------------------|----------------------------------------|
| NGC 34      | 75                          | 65                          | 50            | --                                     | --                                     |
| IC 1623     | 43                          | 24                          | 43            | 33                                     | 25                                     |
| CGCG 436–30 | 32                          | 24                          | 32            | --                                     | --                                     |
| I0364–1042  | 19                          | 14                          | 19            | --                                     | --                                     |
| IIIZw 35    | 35                          | 35                          | 35            | --                                     | --                                     |
| UGC 2369    | 69                          | 36                          | 50            | >45                                    | >40                                    |
| I0359+1523  | --                          | --                          | --            | --                                     | --                                     |
| NGC 1614    | 69                          | 50                          | 50            | >42                                    | >30                                    |
| I05189–2524 | 5.6                        | 6                           | 6             | --                                     | --                                     |
| NGC 2623    | 53                          | 30                          | 50            | 43                                     | 39                                     |
| I08572+3915 | 3.9                        | 3                           | 3.9           | 1                                      | 1                                      |
| UGC 4881    | 97                          | 44                          | 50            | >41                                    | >36                                    |
| UGC 5101    | 28                          | 22                          | 28            | 23                                     | 15                                     |
| I10173+0828 | 16                          | 14                          | 16            | 8                                      | 8                                      |
| I1056+2448  | 81                          | 60                          | 50            | >46                                    | >44                                    |
| Arp 148     | 54                          | 27                          | 50            | >39                                    | >25                                    |
| UGC 6436    | 98                          | 34                          | 50            | >47                                    | >46                                    |
| Arp 299     | 57                          | 43                          | 50            | 39                                     | 27                                     |
| I12112+0305 | 7.6                        | 7                           | 7             | 4                                      | 4                                      |
| UGC 8058    | 37                          | 26                          | 37            | 31                                     | 27                                     |
| UGC 8387    | 52                          | 33                          | 50            | 45                                     | 39                                     |
| NGC 5256    | 43                          | 15                          | 43            | --                                     | --                                     |
| UGC 8696    | 45                          | 37                          | 45            | 34                                     | 22                                     |
| I14348+1447 | 15                          | 14                          | 15            | >12                                    | >11                                    |
| IZw 107     | 59                          | 40                          | 50            | 46                                     | 44                                     |
| I15250+3609 | 19                          | 16                          | 19            | --                                     | --                                     |
| Arp 220     | 22                          | 20                          | 22            | 16                                     | 15                                     |
| NGC 6286    | 44                          | 23                          | 44            | >36                                    | >16                                    |
| NGC 7469    | 87                          | 45                          | 50            | --                                     | --                                     |
| IC 5298     | 79                          | 60                          | 50            | --                                     | --                                     |
| Mrk 331     | 81                          | 35                          | 50            | --                                     | --                                     |

Figure 5. Effect of a rising star formation rate. The black curves are the same as those in Fig. 4 while the red curves are for a starburst that rises in time as \( \psi(t) \propto e^{t/b} \). The green lines show the effect of a flatter IMF for high mass stars (\( dn/dM \propto M^{-2.12} \); Baldry & Glazebrook 2003) for an exponentially decreasing burst.

significantly flatter than the Salpeter value for high mass stars, as proposed by Baldry & Glazebrook (2003). However, the magnitude of the effect is very small, as shown in Fig. 5. Shorter stellar lifetimes also result if source metallicities are higher than solar. For a metallicity 2.5 times the solar value (\( Z = 0.05 \)) an 8 \( M_\odot \) star lives for 32 Myr, rather than 50 Myr (Fagotto et al. 1994).

Until now, we have assumed that the free–free absorption is caused by gas that has been ionized by the UV photons of young, massive stars. If this were not the case, then the time for which a region can remain ionized is no longer limited by the lifetime of massive stars. An AGN can, in principle, ionize large volumes of interstellar medium if it emits strongly at UV wavelengths and shorter. Vega et al. (2008) estimated the AGN contribution to the bolometric luminosity in the present sample of infrared luminous sources and found that only 9/30 sources have an AGN contribution that exceeds 10 per cent. Only IRAS 08572+3915 was found to be AGN dominated, with a 52 per cent contribution from an AGN. Although AGN, where present, may contribute to the ionizing flux of a source, it seems unlikely that this would dominate over the contribution from star formation, which certainly produces ionizing radiation, and almost always dominates the AGN in terms of bolometric luminosity. An AGN that contributed additional ionizing flux, over and above that produced by star formation, would also create an excess of free–free emission, visible as a flattening of the spectra towards higher frequencies. As mentioned above, and discussed in the next section, we actually find a deficit of free–free emission with respect to that expected for star formation alone.

Finally, we note that the values that we derive for \( t_{\text{esc}}^{\text{HII}} \) are similar to the values of the ‘escape time’ found in Vega et al. (2008) and reproduced in Table 4. This escape time parametrizes the time that elapses before stars escape the confines of the molecular clouds in which they were formed, and is described in Silva et al. (1998). The escape time is largely constrained by the spectral shape in the mid- and far-infrared. Both these escape times and the values of \( t_{\text{esc}}^{\text{HII}} \) that we derive above, which are an order of magnitude larger than the values found in normal star-forming galaxies, suggest that the star formation in these objects is embedded in very large regions of dense gas. The effects of age-dependent extinction are thus also seen in the radio regime, as in other parts of the spectrum.

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6.1 Where is the thermal emission?

The thermal fractions shown in Table 2 are almost always lower than the 0.1 assumed by Condon (1992) for 'normal' galaxies. Despite this, there are still many instances where the data lie below the fitted curve. Among these, there are those that show a steepening of the spectra towards higher frequencies (e.g. Arp 299), something that even a complete absence of thermal emission cannot achieve. The simple model we apply to these sources therefore fails at high frequencies. There is some additional effect influencing the radio emission in these LIRGs that is not required to fit the radio spectra of normal galaxies.

The absorption of ionizing photons by dust can reduce the quantity of ionized gas in ULIRGs (Valdés et al. 2005), thus reducing the thermal emission. However, although this effect may be present, it cannot explain the spectra of those sources for which the spectra actually steepen above ~10 GHz.

As discussed in Clemens et al. (2008), synchrotron aging is not expected to cause a steepening of the radio spectra towards high frequencies in these sources because the synchrotron lifetime is very short. One actually expects spectra to be globally steeper than those of normal galaxies. The fact that this is not the case has been discussed by Thompson et al. (2006). These authors consider the effects of ionization losses on the radio spectra of starburst galaxies and find that the radio spectra gradually flatten towards low frequencies and that the spectral indices in the GHz range are similar to those of normal galaxies. If ionization losses are indeed important in these kinds of galaxies, it seems likely that the effects of ionization losses could explain why we observe unexpectedly steep spectra at high frequencies in Fig. 1.

7 CONCLUSIONS

We have combined new measurements of the 244 and 610 MHz fluxes, obtained with the GMRT, of a sample of 20 LIRGs and ULIRGs with existing radio data. The resulting radio spectra show a range of bends and turn-overs that can be well explained in terms of free–free absorption. In several cases, two radio components with different emission measures are necessary to fit the data.

For those objects with two emission components, we estimate the fraction of radio emission associated with each. Via a simple model for the temporal evolution of the supernova rate, we estimate the fraction of supernovae occurring inside and outside of their parent H II regions as a function of the H II region lifetime. For simple exponentially decreasing star formation rates, the lifetimes so derived are too long for them to refer to single H II regions. Altering the form of the high mass end of the IMF or the metallicity has relatively little effect on this result. However, if the star formation rate for these sources is currently rising, rather than declining, the derived H II region lifetimes are very much reduced. The effect of a rising star formation rate is to increase the number of younger (high mass) supernovae occurring within H II regions, relative to the number of older (lower mass) supernovae occurring outside H II regions. The star formation rate rise times should be much less than the lifetime of the least massive stars that produce Type II supernovae. Despite this reduction, the derived ages remain longer than those plausible for individual H II regions. Such large ages imply that the physical situation is one in which younger H II regions obscure older star formation regions along the line of sight. This situation would arise naturally if star formation propagated outwards during a burst. Because a rising star formation rate creates conditions more conducive to free–free absorption, and the fact that the number of sources with two emission components is close to 50 per cent, it is likely that those in which only a single emission component is present are those with falling star formation rates.

The existence of two emission components in the radio therefore points to an age-dependent extinction analogous to that seen at other wavelengths. In the case of radio emission, the most massive stars, which end their lives earlier, produce synchrotron emission that is subjected to preferentially more free–free absorption than those, lower mass, stars that live for longer.

The observed over-prediction of fluxes at frequencies above ~10 GHz may be resolved if the intrinsic synchrotron spectrum were not straight, but had a steeper spectral index at higher frequencies due to ionization losses, as modelled by Thompson et al. (2006).

The two radio components in UGC 8058 can be identified with the radio-loud AGN and star formation, the former contributing 66 per cent of the radio emission. This interpretation is consistent with the model of Vega et al. (2008).

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