CONSTRANTS ON REIONIZATION FROM THE THERMAL HISTORY OF THE INTERGALACTIC MEDIUM

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ABSTRACT

The temperature of the diffuse, photo-heated intergalactic medium (IGM) depends on its reionization history because the thermal time scales are long. The widths of the hydrogen Lyα absorption lines seen in the spectra of distant quasars that arise in the IGM can be used to determine its temperature. We use a wavelet analysis of the Lyα forest region of quasar spectra to demonstrate that there is a relatively sudden increase in the line widths between redshifts $z \approx 3.5$ and 3.0, which we associate with entropy injection resulting from the reionization of He II. The subsequent fall-off in temperature after $z \approx 3.5$, is consistent with a thermal evolution dominated by adiabatic expansion. If, as expected, the temperature also drops rapidly after hydrogen reionization, then the high temperatures inferred from the line widths before He II reionization imply that hydrogen reionization occurred below redshift $z \approx 9$.

Subject headings: cosmology: observations — cosmology: theory — galaxies: formation — intergalactic medium — quasars: absorption lines

1. INTRODUCTION

Neutral hydrogen in the intergalactic medium (IGM) along the line of sight to quasars at redshifts $z \leq 6$ produces hundreds of Lyα absorption lines. The fact that not all flux is absorbed (i.e., the absence of a ‘Gunn-Peterson’ trough, Gunn & Peterson 1965) requires that the universe be ionized to a level far higher than can be attributed to residual ionization from recombination. At lower redshifts, $z < 3$, observed stars and quasars produce enough ionizing photons to explain the high levels of ionization, but the nature of the sources responsible for converting most of the IGM from neutral to ionized remain uncertain, as does the epoch of reionization (e.g., Barkana & Loeb 2001).

The observed mean flux decrement $D_α$ blueward of the quasar’s Lyα emission line increases with the redshift of the quasar, both because the intensity of the ionizing background radiation decreases above $z = 4$ (e.g., McDonald & Miralda-Escudé 2001) and because the mean density $ρ$ of the universe – and hence the neutral fraction $x = \rho T^{-0.7}/Γ_{II}$ for fixed values of the photo-ionization rate $Γ_{II}$ and temperature $T$ – increases. Recently, Becker et al. (2001) and Djorgovski et al. (2001) observed a sudden increase in $D_α$ in the spectra of redshift $z \sim 6$ quasars discovered by the SLOAN digital sky survey. Such a sharp rise has been predicted to mark the transition associated with a sudden epoch of reionization (e.g., Cen & Ostriker 1993; Gnedin 2000). Similarly, a sudden increase in the He II opacity has been detected around $z \sim 3$ (Reimers et al. 1997; Heap et al. 2000; Kriss et al. 2001), associated with helium reionization.

Another way to study the reionization history of the IGM is to investigate its thermal evolution. Because its cooling time is long, the low-density IGM retains some memory of when and how it was reionized (e.g., Miralda-Escudé & Rees 1994; Hui & Gnedin 1997; Haehnelt & Steinmetz 1998). The combined effects of photo-ionization heating and adiabatic expansion introduce a tight temperature-density relation in the unshocked IGM, which can be approximated by a power-law $T = T_0(ρ/\bar{ρ})^{-1}$ for densities around the cosmic mean (Hui & Gnedin 1997). A change in these parameters influences the shapes of the Lyα lines, because thermal broadening and Jeans smoothing determine the line widths (e.g., Theuns, Schaye & Haehnelt 2000). Schaye et al. (1999) used hydrodynamical simulations to demonstrate that one can accurately calibrate the relation between the minimum line width ($b$) as a function of column density ($N_{II}$) on the one hand, and the underlying $T - ρ$ relation on the other. Schaye et al. (2000) applied the method to observations in the redshift range 2.0-4.5 and found that $T_0$ peaks at $z \sim 3$, which they interpreted as evidence for the reionization of He II. Ricotti, Gnedin & Shull (2000) used pseudo hydrodynamical simulations and found a similar temperature increase, albeit only at the 0.5σ level. McDonald et al. (2001) found no evidence for temperature evolution, but their analysis neglected the important temperature dependence of Jeans smoothing. Finally, the analysis of Zaldarriaga et al. (2001) neglected hydrodynamical effects all together.

Here, we provide new evidence for a relatively sudden increase in $T_0$ at higher redshift to constrain the epoch of hydrogen reionization $z_H$ and find that the data require $z_H \leq 9$ for any reasonable value ($T_0 \leq 6 \times 10^4$ K) of the hydrogen reionization temperature.
2. HELIUM REIONIZATION

2.1. Wavelet analysis

Our analysis uses wavelets to characterize line-widths. By picking an appropriate wavelet scale (we used \( \sim 15 \text{ km s}^{-1} \)), we find that the amplitude \( A \) of the wavelet anti-correlates with the widths of the lines – and hence the temperature \( T_0 \) of the absorbing gas, \( (A) \propto T_0^{-1} \). By examining the statistics of \( A \) along the spectrum, we can look for changes in temperature in an objective way, given that the wavelet decomposition is unique. Full details can be found in Theuns & Zaroubi (2000) and Theuns et al. (2002), here we give only a brief summary of the underlying reasoning.

To investigate whether a region of given size \( V \) of the QSO spectrum has an unusual temperature, we compare the cumulative probability distribution \( C(V) \) of the wavelet amplitudes in that region, with \( C(A) \) for the spectrum as a whole. If the region is unusually hot, it will tend to have very few large wavelet amplitudes, and hence the maximum difference \( \Delta V = C_V - C \) will be large. (Note that by construction, \( |\Delta| \leq 1 \), and it is defined for a given \( \text{region} \)). Conversely, cold regions will have large, negative \( \Delta V \). In panel (a) of Fig. 1, we have plotted \( \Delta \) for regions of size \( 5000 \text{ km s}^{-1} \) along a mock spectrum of a simulation\(^7\). The mock spectrum has a jump in \( T_0 \) from \( T_0 = 2.2 \times 10^4 \) K below redshift \( z = 3.3 \) to \( T_0 = 1.5 \times 10^4 \) K above it. As expected, there is a corresponding jump in \( \Delta \) at \( z = 3.3 \), from positive values at low \( z \) to negative ones at higher \( z \).

To determine whether a high value of \( |\Delta| \) is statistically significant – and hence whether we have identified a region with an unusual temperature – we proceed as follows. We repeat the procedure with spectra where the absorption lines are randomly scrambled (with replacement, see Theuns et al. 2002), in order to wash-out any correlations in the wavelet amplitudes, resulting from intrinsic temperature fluctuations. Using these randomized spectra, we can construct the statistical probability \( P(\Delta) \) from the fraction of regions in the randomized spectra, that have a given value of \( \Delta \). Given \( P(\Delta) \), we can determine how likely a value of \( \Delta \) – and hence of a temperature deviation – in the original spectrum is. Performing this analysis, we find that the detected change in \( \Delta \) in the mock spectrum has a statistical significance of more than 99.5 per cent, shown as the full line in panel (a) (positive values refer to regions hotter than average, and vice versa for negative values). This means that in only one out of 200 random realisation, do we, by chance, get values of \( |\Delta| \geq 0.2 \). Note that we only use the simulation to generate the spectrum, and not to assign the statistical significance of a change in \( \Delta \). In the preparation of the mock spectrum, we have imposed the same biases as are present in the real data, by adding noise and instrumental broadening to the simulated lines, and by scaling the mean absorption to the observed value. We therefore believe that the method can be applied to real data with confidence.

We have applied the same wavelet analysis to high-resolution echelle spectra of quasars Q0055-2169 (emission redshift \( z_{em} = 3.6 \), Kim et al 2001), the combined spectrum of Q0302-003 (\( z = [3, 3.27] \), Kim et al 2001) and APM 0827+5255 (\( z = [3.27, 3.7] \), Ellison et al 1999) and Q1422+231 (\( z_{em} = 3.6 \), Rauch et al 1997) (panels b, c and d of Fig. 1 respectively). In each spectrum, we find a cold region at high redshift, and a hot region at lower redshift, each significant at the more than 99 percent level when compared to randomized spectra. Panels (b) and (c) appear very similar to the mock spectrum of panel (a), where we had imposed a sudden temperature increase below \( z = 3.3 \). Note that the implied temperature evolution is exactly opposite of what one would expect from photo-heating in the optically thin limit, in which case the IGM will gradually cool down. We take this as strong evidence that a large fraction of He II is reionized around redshift \( z \approx 3.3 \).

The mean wavelet amplitude scales approximately inversely with temperature: \( \langle A \rangle \propto T_0^{-1} \) (Theuns et al 2002). We have used hydrodynamical simulations to calibrate the proportionality constant, and investigate its dependence on \( \gamma \). Applying the calibration to the above QSO sample, we obtain values for \( T_0 \) in good agreement with those obtained by Schaye et al (2000) from the cutoff in the line width – column density relation, i.e., \( T_0 \approx 10^{4.1} \) for \( z \geq 3.4 \), and \( T_0 \approx 10^{4.3} \) at \( z \approx 3.0 \). This assumes the value of \( \gamma \) as determined by Schaye et al., but reasonable changes of \( \gamma \) do not change \( T_0 \) by more than \( \approx 10 \) per cent (Theuns et al. 2002). Simulations that include radiative transfer are required to investigate whether such a temperature change is consistent with He II reionization.

Other heating mechanisms, for example shock heating by galactic winds, do not have a major influence on the value of \( T_0 \) deduced from fitting the cutoff in the \( b-N_{HI} \) diagram, at least as long as the volume fraction of shocked gas remains small. This is because the method is based on identifying the narrow-est lines in a region, irrespective of whether there is also a set of much broader lines. In contrast, the wavelet method used here examines all lines in a stretch of spectrum. So the fact that both methods find similar values for \( T_0 \) suggests that photo-heating is indeed the dominant heating mechanism, and that the volume

\(^7\)The cosmological parameters for this vacuum-energy dominated, flat, cold dark matter, smoothed particle hydrodynamics (SPH) simulation are \( \Omega_m, \Omega_\Lambda, \Omega_b h^2, \sigma_8 \) = (0.3, 0.7, 0.019, 0.65, 0.9). The simulation box is 12h\(^{-1}\) Mpc on a side, and gas and dark matter are represented with 256\(^3\) particles each.
filling factor of gas that has been shocked by winds is small.

2.2. Thermal evolution

After reionization, the evolution of $T_0$ is given by

$$\frac{1}{T_0} \frac{dT_0}{dt} - \frac{1}{\mu} \frac{d\mu}{dt} = -2H + \frac{\mu \Delta}{k_B T_0},$$

(1)

where $H$ is the Hubble parameter, $k_B$ Boltzmann’s constant, $\mu$ the mean molecular weight, and $\Delta$ is the effective radiative cooling rate [in erg g$^{-1}$ s$^{-1}$]. $\Delta$ is negative (positive) for net cooling (heating) and includes photo-electric heating and cooling via recombination, excitation, inverse Compton scattering, collisional ionization, and bremsstrahlung (we use the rates listed in Appendix B of Theuns et al. 1998). For gas around the mean density, the dominant cooling process is the adiabatic expansion of the universe (the first term on the right-hand side of equation 1), except at $z > 7$ where inverse Compton cooling off the cosmic microwave background is more efficient. The radiative heating and cooling rates depend on the ionization balance of the gas, which itself depends on the temperature. By coupling equation 1 to the differential equations for the ionization balance (listed in Appendix B of Theuns et al. 1998), we can thus solve for the evolution of $T_0$ given a model for the ionizing background, an initial value for $T_0$, and the initial ionization state. We have tested this procedure using full hydrodynamic simulations and find that the evolution of $T_0$ is reproduced very well.

We assume the universe to be permeated by a uniform UV-background with a power-law spectral shape,

$$J = \begin{cases} J_{\text{HI}} \left( \frac{\nu}{\nu_{\text{HI}}} \right)^{-1.8} & \nu < \nu_{\text{HeII}} \text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \text{Hz}^{-1}, \\ J_{\text{HeII}} \left( \frac{\nu}{\nu_{\text{HeII}}} \right)^{-1.8} & \nu \geq \nu_{\text{HeII}} \end{cases} \quad (2)$$

where $\nu_{\text{HI}}$ is the H I ionization threshold. (Note that we allow for a step between the intensities of H I and He II ionizing photons, but normalize $J_{\text{HeII}}$ at the hydrogen ionization edge.) We set $J_{\text{HI}} = 4 \times 10^{-23}$, which yields a photo-ionization rate of $\Gamma_{\text{HI}} = 10^{-13}$ s$^{-1}$ and vary $J_{\text{HeII}}$ (and the corresponding ionization rate $\Gamma_{\text{HeII}}$) as described below. Because the photo-heating rate is independent of the amplitude of the UV-background as long as the gas is highly ionized, the exact value of $J_{\text{HI}}$ after hydrogen reionization is unimportant. Since He II is not always highly ionized, the thermal evolution does depend on $J_{\text{HeII}}$.

The predicted evolution of $T_0$ is compared with the data from Schaye et al. (2000) in Figure 2. We assume the IGM to be in ionization equilibrium at temperature $T_0 = 10^{4.4}$ K at redshift $z = 3.4$ as a result of He II reionization. The curves emanating from the big star then show the subsequent evolution of $T_0$, for the following imposed UV-backgrounds. The solid curve is for a constant ionizing rate of $\Gamma_{\text{HI}} = \Gamma_{\text{HeII}} = 10^{-13}$ s$^{-1}$, and the corresponding photo-heating from all species. Increasing or decreasing $\Gamma_{\text{HI}}$ by a factor 10 does not change the evolution appreciably. The short and long dashed curves ignore photo-electric heating of He II and of both H I and He I respectively. Finally, the dot-dashed line ignores photo-heating all together. The measurements of Schaye et al. (2000) below $z \sim 3$ are clearly consistent with a thermal evolution dominated by adiabatic cooling.

Prior to He II reionization, some regions will already be ionized in He II by local sources. If most of the universe is reionized significantly later, then such differences in reionization epoch will lead to spatial variations in $T_0$. The wavelet analysis by Theuns et al. (2002) can detect variations in $T_0$ of order 50 per cent, over a region of size 5000 km s$^{-1}$, yet no such fluctuations were found in the data. The wavelet analysis by Zaldarriaga (2001) also failed to detect any such temperature fluctuations. This suggests that the temperature increase is the result of the overall increase in the far UV-background following the percolation of He III regions, which prior to reionization are too small to be detected by current methods.
For example, the $z_{\text{reion}}=9.2$ curve has a reduced $\chi^2$ of 4.5 for the $5 \geq z > 3.4$ data points.

**Fig. 3.** The temperature evolution of the IGM above redshift 3.4. The solid curves indicate the evolution of the temperature at the mean density for various HI reionization redshifts $z_{\text{reion}}$, as indicated. The post-hydrogen reionization temperature is assumed to be $T_0 = 6 \times 10^4$ K and the hydrogen photo-ionization rate is $\Gamma_{H I} = 10^{-13}$ s$^{-1}$ (the short dashed line has $\Gamma_{HI} = 10^{-14}$ s$^{-1}$). The He II photo-ionization rate is adjusted so that the He III abundance $x_{\text{HeIII}} \approx 0.1$ at $z = 3.5$. The solid line connecting filled squares is for $z_{\text{reion}} = 10.2$, and a higher He II photo-ionization rate, $x_{\text{HeIII}}(z = 3.5) = 0.6$. Finally, the long dashed line has $z_{\text{reion}} = 20$, but a still higher He II photo-ionization rate, $x_{\text{HeIII}}(z = 3.5) = 0.95$. If He is mostly singly ionized at $z > 3.5$, then the rapid decrease in $T_0$ after reionization places an upper limit of $z_{\text{reion}} < 9$ on the redshift of hydrogen reionization.

The contribution of He II photo-heating at $z > 5$ is uncertain. It is likely that stars dominate the HI ionizing background at such high redshifts (e.g., Madau, Haardt, & Rees 1999), and stars emit very few He II ionizing photons. However, very massive and extremely metal poor stars could lead to a non-negligible He II ionizing background (Tumlinson & Shull 2000). The QSO contribution is also uncertain, although the paucity of faint point sources in the Hubble Deep Field does provide some constraints (Haiman, Madau & Loeb 1999). If He II reionized at $z \sim 3$, as argued in the previous sections, then the He III abundance, $x_{\text{HeIII}}$, should be small at higher $z$. We therefore set $\Gamma_{H\text{II}} = 10^{-15}$ s$^{-1}$ so that $x_{\text{HeIII}} \approx 0.1$ at redshift $z = 3.5$. This limits the plausible contribution from He II photo-heating, and allows us to put a conservative upper limit on the redshift of H I reionization, $z_{\text{reion}} < 9$.

The importance of He II heating is illustrated by the solid curve connecting the filled squares. This model has $z_{\text{reion}} = 10.2$, but the He II ionizing background is increased such that $x_{\text{HeIII}} \approx 0.6$ at $z = 3.5$. This increases $T_0(z = 4)$ significantly, although it still falls below the measured values. Finally, the long dashed line is for a model with $z_{\text{reion}} = 20$ and $\Gamma_{H\text{II}}$ further increased so that $x_{\text{HeIII}} \approx 0.96$ at $z = 3.5$. The temperature of this model is consistent with the data, yet He II is ionized at the more than 90 percent level as early as $z = 5$. Such a high level of ionization conflicts with the evidence that He II ionizes at $z \sim 3$ from the observed He II opacities and the associated increase in $T_0$.

All this leads us to the following conclusions. Two independent methods consistently find a rather sudden increase in the temperature of the IGM over the range $z \sim 3.5-3.0$, which we associate with He II reionization. If this interpretation is correct, then the He III fraction must be low at higher redshifts. Therefore, above redshifts 3.5, He II photo-heating cannot be significant and the IGM cools rapidly following H I reionization. The high values of the IGM temperature at $z \sim 4$ then require that H I reionization occurred late as well, $z_{\text{reion}} < 9$, for any reasonable value $T_0 \lesssim 6 \times 10^4$ K for the HI I reionization temperature. More plausible reionization temperatures of $T_0 \sim 4 \times 10^4$ K and $2 \times 10^4$ K would constrain the hydrogen reionization redshift further to $z_{\text{reion}} \lesssim 8$ and $z_{\text{reion}} \lesssim 7$, respectively.

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