A Graphical Approach to Radio Frequency Quadrupole Design

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Abstract

The design of a radio frequency quadrupole, an important section of all ion accelerators, and the calculation of its beam dynamics properties can be achieved using the existing computational tools. These programs, originally designed in 1980s, show effects of aging in their user interfaces and in their output. The authors believe there is room for improvement in both design techniques using a graphical approach and in the amount of analytical calculations before going into CPU burning finite element analysis techniques. Additionally an emphasis on the graphical method of controlling the evolution of the relevant parameters using the drag-to-change paradigm is bound to be beneficial to the designer. A computer code, named DEMIRCI, has been written in C\textsuperscript{++} to demonstrate these ideas. This tool has been used in the design of Turkish Atomic Energy Authority (TAEK)’s 1.5 MeV proton beamline at Saraykoy Nuclear Research and Training Center (SANAEM). DEMIRCI starts with a simple analytical model, calculates the RFQ behavior and produces 3D design files that can be fed to a milling machine. The paper discusses the experience gained during design process of SANAEM Project Prometheus (SPP) RFQ and underlines some of DEMIRCI’s capabilities.

1 Introduction

The Radio Frequency Quadrupoles (RFQ) are in use at the low beta sections of all modern ion accelerators since their invention by Kapchinsky and Teplyakov in late 1970s \cite{1}. For light ions such as $H^+$ and $H^-$ operating in 300-400 MHz range, the RFQ type of choice is the, so called, "4-vane" RFQ \cite{2}. The design of a 4-vane RFQ, which is the focus of this paper, and its manufacture require precise calculation of the relevant parameters, a good understanding of the materials and high precision machining \cite{3}. In fact, this accelerating structure is nothing but a body (cylindrical, square or octagonal vessel) containing four carefully crafted modulated vanes, two vertical and two horizontal symmetrically distributed along the beam axis. The high precision modulation requirement on the vanes can be met by the computerized milling tools, i.e. CNC machines. However, the art of designing an efficient RFQ and the study of its beam dynamics properties necessitate repetitive lengthy calculations: an ideal task for computers. Although the two of commercially available programs \cite{4}\cite{5}, profit from years of experience in accumulator building, the main design ideas and especially the user interaction components can benefit from modern tools and concepts. Additionally, the commonly used Unix-like environment provided by Linux and OSX workstations does not have access directly to these two Microsoft Windows specific software packages.

A new project in the form of a computer code, written in C\textsuperscript{++}, called DEMIRCI\textsuperscript{1} \cite{6} is started to explore the potential of the modern concepts such as object oriented programming and ROOT environment \cite{8}. This tool helps the designer to create an RFQ model which would achieve certain goals such as a final target energy or a fixed total accelerator length in a fully graphical environment. It calculates a large number of design and beam dynamics parameters such as energy at the end of the cavity, power dissipation and cavity quality factor for each cell. It also allows the designer to visualize a large set of parameters change along the RFQ. Another property of this tool is the interoperability with similar software in the field, either directly using the user interface or by simple exchange of plain text files.

This paper focuses on the algorithmic side of the project omitting all the installation details and instructions on how to use the actual code. These details are described elsewhere \cite{6}. However it might be interesting for the reader to know that the project has been used successfully in multiple Unix-like environments such as OSX, Scientific Linux and Ubuntu Linux. At the writing of this note the project source code is under further development and is not open to general public, however a binary at the current state for most common platforms

\textsuperscript{1}meaning “blacksmith” in Turkish
2 Design Procedures

The classical procedure used in designing 4-vane RFQs has been around since LANL designed the first proof of principle (PoP) device. This procedure is known as the “LANL Four Section Procedure (FSP)” method [9]. According to this method, the RFQ is divided into 4 sections named as radial matching section (RMS), shaper section, gentle buncher section and acceleration section. After the steady state beam at the entrance of the RFQ is matched to time dependent electric field in the RMS, an RF bucket is formed in the shaper to prepare the beam for the gentle buncher. While the beam is being bunched, the space charge effect is also attempted to be reduced concurrently. After the beam becomes bunched, it is accelerated to the final energy at the accelerator section.

The potential between the electrodes of a single RFQ cell is given [10] by

\[
U(r, \theta, z) = \frac{V}{2} \sum_{m=1}^{\infty} A_{0m} \left( \frac{r}{r_0} \right)^{2m} \cos(2m\theta) \sum_{n=0}^{\infty} A_{nm} I_{2m}(nkz) \cos(2m\theta)
\]

where \( r \) and \( \theta \) are spherical coordinates for which \( z \) represents the beam direction, \( V \) is the inter-vane voltage, \( k \) is the wave parameter given by \( k \equiv 2\pi/\lambda \beta \), with \( \lambda \) being the RF wavelength and \( \beta \) being the speed of the ion relative to the speed of light. Also, \( r_0 \) is mean aperture of the vanes, \( I_{2m} \) is the modified Bessel function of order \( 2m \) and the \( A_{nm} \) are the multipole coefficients whose values depend on the vane geometry.

Kapchinsky and Teplyakov argued that for practical purposes the above potential can be approximated only by the lowest order terms in the sums (hence the name “2-term potential”) to calculate the EM fields around the tips of the electrodes i.e. near the beam axis. More recently, modern tools have added few more terms to this initial approximation, in fact LANL design software uses the eight lowest order terms of Equation (1) to characterize the EM fields in the presence of the modulated vanes. The other commercially available software, LIDOS, gives users the possibility to design RFQs in three steps; first the main parameters are defined and design optimizations are made, then accurate RF fields calculations are made with a multipole expansion of the Eqn (1) and finally beam simulations are performed to understand the beam dynamics effects.

2.1 New design procedure

The parameters needed to define an RFQ can be divided into two categories: the ones which can be a function of RFQ length and the ones which are constant for a given RFQ. The resonant frequency (\( f \)), the initial ion energy (\( E_{in} \)), the input beam current (\( I \)) and the bravness factor (in terms of the Kilpatrick value) can be cited as examples to the latter. The four parameter vectors falling into the first category are: the synchronous phase (\( \phi \)), the cell modulation (\( m \)), the minimum bore radius (\( a \)) and the inter-vane voltage (\( V \)). This last one, together with \( R/\rho \) could be kept constant along the RFQ length to simplify the design and manufacture. In case of DEMIRCI, a typical parameter’s variation along the RFQ can be seen in Fig. 1. The points represented by the blue squares in Fig. 1 are the so called "reference cells" for which the values of the four key parameters are defined by the designer. In this particular example, Fig. 1 shows 20 reference cells for an RFQ of 200 cells in total. The values of the parameters at the cells in between the reference ones are obtained by interpolation assuming a simple linear function. The number of reference cells and the total number of RFQ cells are all user defined variables. The designer might choose to define the values of the parameters for each cell, or to simply define boundary conditions for different regions of the RFQ and let the interpolation function do the rest. As a safety check, the software library ensures the monotonic increase of the reference cell numbers. Therefore a new design can be made in a pure graphical way, by simply relocating individual reference cells by using the mouse pointer e.g. to change the shape of the synchronous phase curve or by moving a complete curve, e.g. to increase the inter-vane voltage which is a constant in simple designs. This new paradigm allows quick testing of various design ideas concerning the four critical parameter vectors: \( \phi \), \( m \), \( a \) and \( V \). Although the non-graphical user interface, i.e. the command line, also exists and it could be more adequate for parameter scan studies, the graphical method has proven itself to be both more intuitive and more pedagogical for the new designers.

Once the reference curves and the other parameters are selected, the designer can simply do the interpolation and calculate all the relevant functions for each cell. The evolution of the ion beam starts with cell 0 and progresses through all cells by calculating all the variables of interest. A few simple formulas leading to the calculation of the length of the \( n^{th} \) cell, \( L_n \), the acceleration efficiency at \( n^{th} \) cell, \( A_n \), and the total energy of the ions of mass \( m \) and charge \( q \), after the \( n^{th} \) cell, \( E_n \) are reproduced below to give the reader an overview of the type of repetitive calculations needed to design an RFQ:

\[
\beta_n = \sqrt{1 - \left( \frac{m}{E_{n-1}} \right)^2}
\]
\[
L_n = \beta_n \lambda / 2
\]
Cell Modulation

Figure 1: Cell modulation ($m$) versus cell number. $m$ is a typical RFQ parameter which changes with cell number. The meaning of blue squares and red line is explained in the text.

\begin{align*}
  k_n &= 2 \pi / (\lambda \beta_n) \\
  A_n &= \left( m_n^2 - 1 \right) / \left( m_n^2 I_0[k_n a_n] + I_0[k_n a_n m_n] \right) \\
  E_n &= E_{n-1} + \frac{1}{4} q \pi A_n V_n \cos(\phi_n)
\end{align*}

At the end of the calculations, few important parameters are presented to the designer: these are the final ion beam energy, the RFQ total length which is the sum of all cell lengths, the time needed for the ions to travel the RFQ cavity, the maximum EM power needed by the RFQ and its quality factor, $Q$. The details of the RF power and quality factor calculations will be discussed in the next section. Remaining parameters can be optimized by specifying a goal such as a desired output beam energy. The number of RFQ cells can be changed from the default value of 200 to allow the design of longer RFQ cavities. A shorter design is simpler to obtain by setting a target value for the exit ion energy. All the scalar RFQ parameters can be tuned using the number entry boxes at the upper right side of the designer window which can be seen in Fig. 2.

Additionally, there are checks along the calculations which inform the user that a critical parameter is overrun. For example, the designer is warned if the inter-vane voltage is too high and induces an electric field above the preselected Kilpatrick limit. If such a warning is given, it is up to the designer to check the details of the problem by plotting the parameter in question and to solve it by re-optimizing the RFQ. Building the RFQ designer software on top of the pre-existing ROOT libraries provides all the non-essential but necessary functionality, such as defining the parameters of interest, loading and saving of the configuration and output files. Additionally, all the graphics routines in DEMIRCI are based on the ROOT libraries. This design decision allows a robust, mature and multi-platform GUI experience for the designer. A section of the user interface dealing with parameter selection is shown in Fig. 3. DEMIRCI provides easy plotting of the evolution of the relevant parameters along the RFQ. The graphical results can also be easily customized (such as the formatting of the curves or the addition of a gridline) according to the taste of the user.

2.2 Power and quality factor calculations

RF power requirements and the quality of the final accelerating cavity are essential quantities to measure the realizability of the designed device. In DEMIRCI, the RF power dissipation on the cavity walls is calculated using the lumped circuit model assuming a Cu structure \[11\]. This assumption is expected to be valid for both Oxygen Free Electric Copper (OFE Cu) cavities and also cavities made from other materials and electro-coated with Cu: the skin depth at radio frequencies is less than 10\(\mu\)m, which is much less than typical coating thickness validating the approach. The relevant quantity to consider is the power loss per unit length on the RFQ wall surfaces.
Finally, in all calculations the duty factor (d.f.) is assumed to be 100%, therefore the designer is expected to report the actual power values according to the d.f. of the planned device.

It is denoted as $P^S_\ell$ and given as:

$$ P^S_\ell = \sqrt{\frac{4+3\pi}{32\sigma}}(\omega C_\ell)^{3/2}V^2, $$

(3)

where $V$ is the vane voltage, $\omega$ is resonant angular frequency, $\sigma$ is the conductivity of the wall material (usually Cu), and $C_\ell$ is the capacitance per unit length. Although this last value can be assumed to be a constant around 120 pF/m, a better approximation can be found in the literature: $C_\ell = 48 \times 10^{-12} (r_0/\lambda)^{-1/6}$ for $0.002 \leq r_0/\lambda < 0.008$ \cite{11} where $\lambda$ is the RF wavelength and $r_0$ is radial aperture. An additional power requirement is due to the need of filling the RFQ volume with EM energy. Again the quantity to consider is the power loss per unit length in the RFQ volume. It is denoted as $P^V_\ell$, the maximum power which can be stored into the volume, and given \cite{12} as:

$$ P^V_\ell = 8c^2\varepsilon_0^2E_0^2/\omega C_\ell, $$

(4)

where $c$ is the light speed and $\varepsilon_0$ is the permittivity, both at vacuum and $E_0$ is the axial electric field. These formulas contain simplifications and assumptions to facilitate calculation (e.g. constant $E_0$). Therefore the maximum power that can be fed into the cavity becomes the sum of the above two terms: $P_{\text{max}} = P^S_\ell + P^V_\ell$ where the power terms without the subscript $\ell$ mean integration over length. The power needed by a specific machine depends on the beam current and final energy: $P_{\text{need}} = P^S + P^V$ where

$$ P^V = I_{\text{beam}} \times E_{\text{beam}}. $$

(5)

In order to calculate another important RFQ property, namely the quality factor of the cavity denoted as $Q$, the electric ($U^E$) and magnetic ($U^B$) components of the stored energy are to be calculated separately:

$$ U^E = \frac{\varepsilon_0}{2} \int |E_0|^2 dV, $$

(6)

$$ U^B = \frac{1}{2\mu_0} \int |B_0|^2 dV. $$

(7)

With these definitions, $Q$ can be written as:

$$ Q = \frac{\omega U^E + U^B}{P^S + P^V}, $$

(8)

where $P^S$ is the power loss on the surface and $P^V$ is the power loss in the volume of the RFQ. A reasonable scenario is adapted for these calculations: the electric and magnetic fields are assumed to be constant and at their maximum values. The overestimation of the power requirements resulting from this approach is expected to counteract the impediments of the simplistic model. Finally, in all calculations the duty factor (d.f.) is assumed to be 100%, therefore the designer is expected to report the actual power values according to the d.f. of the planned device.

2.3 Machining the vanes

Vane shape calculation is the final output expected from such a software as it can be fed to an electromagnetic equation solver program for further analysis. The vane tip extrema position in radial direction is defined as part of the design process. The axial position ($z$) of each extrema is calculated by DEMIRCI library. An interpolation between consecutive extrema using generic sine function allows the definition of a continuous 2D surface:

$$ V(z) = c + A \sin(kz + \phi), $$

(9)

where the coefficients $c$, $A$ and $\phi$ can be solved for each cell. Although the user can request the functions to be evaluated at any interval to produce a discreet version of the vane profile the typical precision requirement for mechanical productions can be met with a $10\mu$m step size. In Fig. 4 vane shape calculated by DEMIRCI is presented as a function of the RFQ length. Such an output file can be taken as input by a CAD program for 3D visualization and further processing.

3 Prometheus RFQ as a Design Example

The SPP RFQ, at TAEK’s SANAEM, aims to gain the necessary knowledge and experience to construct a proton beamline needed for educational purposes. A Proof of Principle (PoP) accelerator with modest requirements of achieving at least 1.5 MeV proton energy, with an average beam current of at least 1 mA is under development. This PoP project has also the challenging goal of having the design and construction of the entire setup in Turkey within three years: from its ion source up to the final diagnostic station, including its RF power supply. There are also two secondary goals of this project: 1) Training accelerator physicists and RF engineers on the job; 2) To encourage local industry in accelerator component construction. The design requirements of this machine can
Table 1: SPP RFQ design parameters.

| Parameter  | Value |
|------------|-------|
| $E_{in}$ (keV) | 20    |
| $E_{out}$ (MeV) | 1.5   |
| $f$ (MHz)    | 352.2 |
| $V$ (kV)     | 60    |
| $I$ (mA)     | >1    |
| KP           | 1.5   |
| $R_0$ (mm)   | 2.8   |
| $\rho$ (mm)  | 2.5   |

Figure 5: SPP RFQ beam dynamics parameters as calculated by DEMIRCI.

be found in Table 1. The input energy was selected to keep the RFQ short for a 1.5 MeV output energy and at the same time to satisfy the current requirements. The operating frequency was selected to be compatible with similar machines in Europe and therefore to benefit from the already available RF power supply market. Other parameters such as the inter-vane voltage, Kilpatrick value etc. were chosen to be adequate for a first time machine.

The calculation and visualization of the evolution of the most critical accelerator cavity and beam parameters along the RFQ length was the SPP RFQ which is DEMIRCI's one of the very first applications. The plot containing the evolution of the cell length, beam energy, modulation, synchronous phase and radial aperture can be found in Fig. 5.

3.1 Interoperability and Compatibility

The interoperability between different programs is essential for both cross-check and continuity reasons. Especially when a new software library is introduced, the input-output file level compatibility ensures quick verification of the procedures and results. Additionally file level compatibility ensures the continuous processing of the ion beam from one end of the beamline to the other using different software, each suitable to the properties of a particular section. DEMIRCI was written with these goals in mind: it can process input parameters produced by other programs and it produces output files compatible with most of the existing software packages in the field. The compatibility between DEMIRCI and similar programs in the field, for basic parameters such as beam energy, RFQ length, quality factor and so on, is given in Table 2. The input parameters used by different programs are all the same, originating from the previously discussed design of the SPP RFQ. As one may notice, the difference is usually of the order of few percent which can be considered as acceptable for a design program based solely on two term potential. The results from different software libraries for calculating the parameters along the RFQ are discussed below.

3.1.1 DEMIRCI-LIDOS

The LIDOS.RFQ.Designer software package has three modules for designing, analyzing and simulating. LIDOS also uses 8 term potential while it is calculating main parameters. In this connection there is almost full consistency between LIDOS and DEMIRCI calculation results as are seen from Fig. 6 and Fig. 7. An approximate 1% discrepancy between LIDOS and DEMIRCI plots is due to different calculation procedure.

3.1.2 DEMIRCI-TOUTATIS

TOUTATIS [13] is a beam dynamics simulator for high intensity RFQs and makes this using Poisson solver for fields which provides to get values such as space charge effects or cavity fields between the electrodes. It interacts with DEMIRCI for RFQ beam dynamics simulation purposes. It describes an RFQ beamline with an input file containing different sections. The section that deals

Table 2: Results from DEMIRCI’s calculations as compared to other programs results. Keys are T:TOUTATIS, L:LIDOS, C:CST, S:SUPERFISH

| Parameter                  | DEMIRCI | Other | %Δ  |
|----------------------------|---------|-------|-----|
| RFQ Length (m)             | 1.555   | 1.585 | 1.89|
| Exit Energy (MeV)          | 1.54    | 1.52  | 1.32|
| Travel Time (ns)           | 249.9   | 265.8 | 5.98|
| Quality Factor             | 10461.6 | 10341.6| 1.17|
| RF Power (W/cm)            | 128.12  | 123.56| 3.69|
|                           | 125.08  | 123.56| 0.03|
Figure 6: Comparisons of the DEMIRCI and LIDOS results for main parameters.

Figure 7: Design geometry comparisons of DEMIRCI and LIDOS.

Figure 8: Comparisons of the results from DEMIRCI and TOUTATIS.

Figure 9: The RFQ segment gap definitions window.

with the RFQ cells has a channel block definition compatible with PARMTEQ. DEMIRCI’s default output file is compatible with this channel block definition containing RFQ cell parameters (inter-vane voltage, aperture, synchronous phase etc.) given in 17 columns. In fact, DEMIRCI’s current version relies on TOUTATIS for all beam dynamics simulations. In Fig. 8 a comparison of the main parameters obtained from DEMIRCI and TOUTATIS.

An important parameter is the RFQ length which is typically in the order of few meters. However, with today’s CNCs, the optimal machining length is about 80-90 cm. Therefore RFQs are designed to be built and assembled in longitudinal sections. As the gap that occurs between different sections affects directly the behavior of the ion beam inside the RFQ, it is important to incorporate it into the beam dynamics simulations. Although DEMIRCI doesn’t directly use the section gaps for its calculations, it is possible to define any number of gaps and associated properties (such as location, width, etc.) as shown in Fig. 9 and to estimate the beam dynamics effects by running the design in TOUTATIS.
3.1.3 LANL software suite

LANL software suite for RFQ design is perhaps one of the most commonly used computer codes which can take an input file from DEMIRCI. SUPERFISH [14] is the most common computer program to calculate fields in 2-D cartesian coordinates for any cylindrically symmetric shape. As SUPERFISH is an essential tool with years of experience, it is inevitable that DEMIRCI, professing being one of the standard computer codes, can produce SUPERFISH compatible output given an RFQ design. On the other hand, PARMTEQ is a common program that designs and makes beam dynamics calculating up to 8 term potential.

4 Conclusions and Prospects

DEMIRCI is a fast, Unix based modern tool using graphical techniques for RFQ design. It uses analytical formulae based on two term potential to compute the light ion beam behavior in an RFQ. It also permits the user to achieve optimizations with specific goals such as a final accelerator length or a final ion beam energy. It interacts with similar software in the field, for result cross check and for further study of the RFQ and beam properties. Lastly, it can produce the horizontal and vertical vane shapes which can be fed into 3D solvers for more accurate electromagnetic and thermal studies based on finite element analysis techniques.

A number of additions and enhancements are being planned for this new tool. The first goal is to use the more complex 8 term potential to allow a more realistic calculation of the EM fields inside the RFQ. This enhancement is expected to further reduce the small deviations in the results obtained with this tool and similar ones. Furthermore, addition of beam dynamics calculations would make DEMIRCI a more complete solution for the RFQ design.

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