Longitudinal multiple imputation approaches for body mass index or other variables with very low individual-level variability: the \texttt{mibmi} command in Stata

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Abstract

**Background:** In modern health care systems, the computerization of all aspects of clinical care has led to the development of large data repositories. For example, in the UK, large primary care databases hold millions of electronic medical records, with detailed information on diagnoses, treatments, outcomes and consultations. Careful analyses of these observational datasets of routinely collected data can complement evidence from clinical trials or even answer research questions that cannot be addressed in an experimental setting. However, missingness is a common problem for routinely collected data, especially for biological parameters over time. Absence of complete data for the whole of an individual’s study period is a potential bias risk and standard complete-case approaches may lead to biased estimates. However, the structure of the data values makes standard cross-sectional multiple-imputation approaches unsuitable. In this paper we propose and evaluate \texttt{mibmi}, a new command for cleaning and imputing longitudinal body mass index data.

**Results:** The regression-based data cleaning aspects of the algorithm can be useful when researchers analyze messy longitudinal data. Although the multiple imputation algorithm is computationally expensive, it performed similarly or even better to existing alternatives, when interpolating observations.

**Conclusion:** The \texttt{mibmi} algorithm can be a useful tool for analyzing longitudinal body mass index data, or other longitudinal data with very low individual-level variability.

**Keywords:** Multiple imputation, Body mass index, Cleaning, Longitudinal data
only downside of proceeding with a complete cases analysis (effectively ignoring the issue) is a loss of statistical power. This loss is not always negligible, however, especially in multiple regression analyses with many predictors where even low levels of ‘missingness’ on individual variables can result in a high total percentage of cases being dropped from analysis.

In the typical MAR scenario, the values (or categories) of a variable are associated with whether information for another variable, predictor or outcome, is missing or not. For example, under the quality and outcomes framework which is a UK primary care pay-for-performance scheme, physicians are incentivized to record the blood pressure of certain chronic condition patient groups (e.g. diabet es). Since the introduction of the scheme in 2004, annual systolic and diastolic blood measurements are almost complete in UK Primary Care Databases (Clinical Practice Research Datalink or CPRD, The Health Improvement Network or THIN, QResearch), for diabetes patients. However, data is more often missing for other patient groups, especially before 2004. Estimating the relationship between a diagnosis of diabetes and blood pressure levels is not straightforward in this context and a complete-case analysis could provide biased estimates. Currently, multiple imputation (MI) is considered the best practice to deal with this problem [3], with a possible alternative being inverse probability weighting [4]. The better performance of MI over other approaches, such as observation carried forward and complete cases, has been repeatedly confirmed [5, 6], although it is not a panacea [7]. There are ways to assess whether data are MAR [8], for example, by assessing the relationship between a predictor’s values and missingness or not in the outcome through a logistic regression. Arguably, MAR is an inaccurate term for this type of missingness and the term ‘informative missingness’ is often preferred.

In the most challenging case, data missing under a MNAR mechanism, the value of the variable that is missing is related to the reason why it is missing, and it can be a predictor or, more worryingly, an outcome. For example, body mass index (BMI) is more likely to be measured and recorded for obese patients and more likely to be missing for patients who do not look overweight. Data values that are MNAR cannot be reliably estimated from information about other variables, unless the mechanism of missingness is known, which is very uncommon. Although multiple imputation can offer some protection against MNAR mechanisms, identifying and effectively controlling for such a mechanism can very challenging [9, 10].

Multiple imputations for longitudinal data are particularly challenging, since it is necessary to account for variable correlations both within and between time points in the generation of the imputed values. Nevalainen et al. proposed an extension to cross-sectional methods for the longitudinal data setting [11], which was recently implemented in the very useful twofold algorithm for Stata [12], evaluated and found to perform well under MCAR assumptions [13]. Imputations for longitudinal sequences have been found to perform better when based on observations from each person, rather than group averages [14]. For a relatively stable over time biological parameter such as BMI, correlations with other variables within and between time points can be expected to be very small compared to BMI correlations across time points. Although models of group averages should account for these issues, we hypothesise that, specifically for BMI, there is very little information to be gained from other covariates, if they are available. Therefore we should be able to reliably impute BMI values between existing observations (interpolations) for each person, which will also give us flexibility to generate more realistic individual BMI trends rather than fluctuations around a trend mean.

To this end, we developed mibmi, a cleaning and multiple imputation algorithm for BMI or other variables with very low individual-level variability. The cleaning aspect of the algorithm identifies and sets to missing outliers that are very likely to be error values and can bias inference. The algorithm focuses on each individual to produce interpolations (between observations) and extrapolations (before first or after last observation) in a longitudinal setting for the variable of interest, provided at least two observations are available for an individual. The generated datasets are compatible with the mi family of commands in Stata.

Methods

The command includes two cleaning options. Standard cleaning limits values to a logical pre-specified range and a more advanced option uses regression-based cleaning for each individual. Provided the variable of interest is BMI and weight and height have been provided, the algorithm will use these in addition to BMI observations at all available time points, to first establish the most reliable height estimate and use that to correct BMI and/or weight values. In the standard multiple imputation setting, the command will interpolate measurements of interest for patients with at least 2 observations over the time period. Residuals are used to quantify interpolation prediction errors, for all possible time-window lengths, and these are used to introduce uncertainty in the interpolation estimates, in a multiple imputations setting. Imputed values are drawn from normal distributions, the means for which are provided by the ipolate command and the standard deviations are the standard errors for the predictions for the respective time-window length. A similar approach
is used for extrapolations, if requested. The algorithm workflow for both interpolation and extrapolation is presented in Fig. 1. User defined MNAR assumptions are also allowed, under which values can be imputed through either interpolation or extrapolation. The command is computationally demanding and can take a long time to run for very large populations, especially when both interpolations and extrapolations are requested. Time-windows can be in years, months or even days, provided data completeness is reasonable. For example, in UK primary care databases, BMI is routinely recorded for people with certain chronic conditions at least once every year, since physicians are incentivized to measure it. In a clinical trial BMI may be recorded on a weekly basis and hence a much smaller time-window for analysis may be desirable.

Cleaning
In the standard cleaning approach, the algorithm simply sets values below 8 or above 210 to missing. BMI values outside this range are extremely unlikely,
across all ages [15]. If height and weight are provided, similar range restrictions are applied, between 0.81 and 2.3 m and 15–500 kgs (if age is also provided the lower limits only apply to individuals aged 10 or over). The upper and lower values threshold can be edited by the user.

Under the more advanced regression-based cleaning setting, weight and height values, when available, are used to compute a BMI score for comparison against the recorded BMI values. First, height observations are used to estimate the median height value. Since we assume height to be constant over time (unless age is provided, in which case the approach is limited to those aged 18 or over), height is replaced with the median value in all time points. Next, potentially more reliable BMI values are calculated using the ‘corrected’ height value and the available weight values (again, taking age into account if provided). As in standard cleaning, BMI values are set to missing if they are outside the [8, 210] range.

In the final step of the regression-based cleaning (and first if weight and height are not provided, for example when the variable of interest is not BMI), a linear regression of time on the variable of interest is executed, for each individual with three or more observations. We run a separate ordinary least squares model for each individual, analogous to some extent to previously proposed random-effects modelling [16]. For time points where the ratio of absolute model residual value (observation minus prediction) over the observation is higher than 0.5 (50%), the observation is assumed to be unrealistic and is dropped. The value rejection threshold can be set by the user in the [0, 10] range.

**Interpolation**

The main feature of the algorithm is imputation of missing values between observations, for each individual. Although the command and methods were originally developed for BMI imputation, they should be relevant to any variable with very low individual-level variability.

In the first step, available observations are used to quantify the error of predictions using the ipolate command. For each possible distance between time points, existing observations are missing and impute them using ipolate. Subtracting each estimate from the actual observation we calculate the root mean square deviation, which we aggregate across all cases for each time-window width. Assuming a time-window width $i$, taking values between 2 (e.g. between time points 1 and 3, 2 and 4 etc) and $k−1$, if $k$ is the number of time points:

$$\text{irmsd}_i = \sqrt{\frac{1}{n} \sum_{j=1}^{n} (\text{pred}_{ij} - \text{obs}_{ij})^2}$$

where $n$ is the total number of cases for which a comparison is possible, across individuals and time-windows of size $i$. For example, assuming 5 time points, $\text{irmsd}_2$ is calculated across all patients with complete observations for time points 1–3, 2–4 and 3–5: values for time points 2, 3 and 4, respectively, are assumed to be missing and are estimated and then compared to the observed values as described by (1). In other words, the root mean square deviation is calculated pooled across all possible time windows (of a specific width) and all individuals.

The second step involves the actual imputation of missing values, using interpolation. For each individual, any observations that can be interpolated are identified. For each set of values to be imputed, between two observations in time points $t_α$ and $t_β$, the time-window width is identified and linked to the respective root mean square deviation calculated in step 1. Next, the group of values is imputed sequentially, starting from time point $t_α$ + 1. For $t_α$ + 1, the value to be imputed is randomly drawn from $N(mv_{t_α+1}, \text{irmsd}_{t_α−t_α})$, where $mv_{t_α+1}$ is the interpolation value provided by the ipolate command for time point $t_α + 1$ using $t_α$ and $t_β$ values. The next time point for which a value is imputed is $t_α + 2$ (assuming $t_β − t_α > 2$), randomly drawn from $N(mv′_{t_α+2}, \text{irmsd}_{t_α−t_α})$, where $mv′_{t_α+2}$ is the interpolation value provided by the ipolate command for time point $t_α + 2$ using $t_α + 1$ and $t_β$ values. In other words, for each imputed value, the immediately previous value is always taken into account, whether observed or imputed. This approach allows for imputed values that do not fluctuate unrealistically around a mean but rather simulate trends of increasing, decreasing or stable values between observations. The more imputed variables are generated, the more of these possible trends are simulated.

**Extrapolation**

The algorithm will also allow missing values for an individual to be extrapolated, in a process based on the ipolate or regress commands. The extrapolation process involves three steps.

In the first step, the available dataset is edited and reshaped to allow for the comparison of predictions with observations, for all possible extrapolations. For example, if an individual’s observations are available for time points $t_α$, $t_β$, $t_γ$ and $t_δ$, the algorithm will ‘drop’ values to generate subsets on which the comparisons will take place. In this case it will generate four subsets by dropping $t_α$, $t_α$, $t_β$, $t_β$, $t_δ$ and $t_δ$, allowing the evaluation of what would be extrapolated values. A minimum of two observations need to be available for a subset to be of use, hence only patients with at least three observations are involved in this part of the extrapolation process. All generated sub-datasets are then combined in a single temporary file.
The temporary file is then used to calculate root mean square deviation estimates, in a similar way as for interpolation, but in this case they are much larger (since the methods we use to empirically quantify deviation are less accurate). Users can choose either an interpolate or a computationally more expensive regress based estimation for all the values that were ‘dropped’ in the previous step, with the former using the closest two and the latter using all available observations. For each possible distance \( t \) between the ‘dropped’ value to be imputed and the closest observation, the root mean square deviation is estimated using (1). In this case, however, we call it \( \text{ermsd} \) with \( n \) in the formula being the total number of cases in the temporary file, for which a comparison is possible for time distance \( t \).

In the last step, for each individual, the missing values that can be estimated using extrapolation are identified and linked to the respective root mean square deviation calculated in the previous step. As with interpolation, extrapolation values are imputed sequentially for each individual, starting from the time point closest to an observation. Assuming an observation exists for time point \( t_0 \) and an extrapolation can be calculated for \( t_0 + 1 \), the value to be imputed will be randomly drawn from \( N(mv_{t_0+1}, \text{ermsd}_1) \), where \( mv_{t_0+1} \) is the extrapolation value provided by \textit{ipolate} or \textit{regress} for time point \( t_0 + 1 \). Assuming \( t_0 + 2 \) can be extrapolated, it is randomly drawn from \( N(mv_{t_0+2}, \text{ermsd}_2) \), where \( mv_{t_0+2} \) the extrapolation value provided by \textit{ipolate} or \textit{regress} for time point \( t_0 + 2 \), but including the imputed value for \( t_0 + 1 \) in the process. The algorithm continues sequentially and imputes values for all time points where an extrapolations is possible, for each individual, simulating realistic variable trends (as many for each individual as the number of variables to be generated in the imputation process). Draws for both interpolation and extrapolation are effectively constrained to acceptable values in the \([8, 210]\) range, although in our experience this constraint should never have to be invoked for interpolations and only very rarely for extrapolations. It should also be noted that each drawn interpolation or extrapolation is assumed to be exact, within the specific dataset, and only through a multiple imputation process will the uncertainty in the estimate be fully captured.

### The \texttt{mibmi} command

#### Syntax

\begin{verbatim}
\texttt{mibmi varname1 varname2 varname3 [ varname4 ], [ weight(varname) height(varname) clean xclean xclnp(#) xnomi xsimp minum(#)}
\texttt{extrapolate rxextrapolate imnarl(#) xmnarl(#) pmnarl milng lolim(#)}
\texttt{uplim(#) seed(#) nodi ]}
\end{verbatim}

#### Variables

The command requires three variables to be provided, in the following order: the unique within time individual identifier (\textit{varname1}); a linear time variable to define monthly, yearly or other time-windows (\textit{varname2}); and the main variable of interest, usually the BMI (\textit{varname3}). An optional variable with the age in years can also be provided (\textit{varname4}), which is used in the simple cleaning process, if requested. Also note that the data needs to be in long rather than wide format, in relation to time. A backup variable for the original variable of interest is created in \texttt{_varname3}.

#### Options

**Cleaning**

- \texttt{weight(varname)} Weight in kilograms. If provided along with height, both variables will be used to correct BMI and/or height and weight observations. Only relevant for BMI imputation.
- \texttt{height(varname)} Height in metres. If provided along with weight, both variables will be used to correct BMI and/or height and weight observations. Only relevant for BMI imputation.
- \texttt{clean} Standard cleaning option requested to set unrealistic values to missing (default is >210 or <8). Assuming the variable of interest is BMI, if weight and height have been provided they are also cleaned at this stage, taking age into account if it has been provided.
- \texttt{xclean} More advanced cleaning option that uses regression modelling to identify unrealistic changes in the variable of interest, which are very likely input errors, and set them to missing. If BMI is the variable of interest, provided weight and height values will be taken into account: first, weight, height and BMI values are investigated longitudinally to try to verify the subject’s height (accounting for age, if provided). Then, using this ‘most likely’ height value, BMI values are corrected if needed. The second stage, which is the only stage if the variable of
interest is not BMI, involves running a regression model for each subject to identify unrealistic changes in BMI and set them to missing. The threshold over which the observations are set to missing is set with the `xclnp(#)` option.

`xclnp(#)` Threshold for regression cleaning, defined as absolute residual value (i.e. observed minus prediction) over observed value. The default value is 0.5 (i.e. 50%).

`xnomi` By default the command is a multiple imputation command. This option suppresses multiple imputations and hence allows the command to be used solely for cleaning.

`xsimp` By default the command is a multiple imputation command. This option suppresses multiple imputations and allows simple imputation, with no standard errors calculated and implemented in either intrapolations or extrapolations. It can be issued with the `ixtrapolate` or `rxtrapolate` options.

**Multiple imputation**

`minum(#)` Number of multiple imputations. The default is five.

`ixtrapolate` Requests extrapolation (in addition to interpolation), using the `ipolate` command. Standard errors for `ipolate` predictions are calculated (for various time-windows), by removing observed BMI values and calculating model performance for them. The `ipolate` command is then used to sequentially impute extrapolated values: starting from the time points closest to the observed values and moving further away. At each stage, values are drawn from a normal distribution the mean for which is provided by the `ipolate` command and its standard deviation is the standard error for the predictions for the respective time-window.

`pmnar` Indicates that a percentage change, rather than an absolute value increase/decrease, is to be used for the MNAR mechanism(s). If this option is specified, options `imnar(#)` and `xmnar(#)` will accept values in the $[-90, 90\%]$ range, indicating a percentage change between $-90$ and $90\%$. Users should be aware that increases and decreases are not symmetrical under this option.

`miling` Requests the multiple imputations dataset in `mlong` format instead of `wide`, the default.

**Other**

`lolim(#)` Lower value threshold below which observations are dropped when using option `clean` and imputations are constrained. The default value, for adult BMI, is set to 8.

`uplim(#)` Upper value threshold above which observations are dropped when using `clean` and imputations
are constrained. The default value, for adult BMI, is set to 210.

`seed(#)` Set initial value of random-number seed, for the simulations. The default is 7. See `set seed`.

`nodi` Do not display progress. Not recommended since imputation can take a very long time for large databases.

**Saved results**
The `mibmi` command does not return any scalars but an edited dataset, `mi` compatible if imputations are performed. In that case, additional variables are included. The `mi` standard variable `_mi_miss` includes binary information on whether values are missing or not. Variables `_mi_ipat` and `_mi_xpat` flag patients for which at least one value has been interpolated or extrapolated, respectively (the latter is only present if extrapolations have been requested). Assuming the default `mi wide` format is used, imputed variables are available in the usual Stata format `_i_varname3`, including observed and imputed values (the number of variables is defined by `minum(#)`). Finally, `_i_iinfo` and `_i_xinfo`, if extrapolations are requested, include information on the imputed observations and the validity of the imputed values for the respective variable, i.e. they flag whether the imputation process would have provided a value outside the predefined logical range and had to be corrected by setting to the minimum or maximum allowed. Such a scenario is extremely unlikely for interpolations and `_i_iinfo` variables do not really vary (zero for all imputed values, missing for observations). However, it does happen for extrapolations, although rarely, and on occasion the `_i_xinfo` variables include non-zero values. This seems to be more likely with the default and faster `ipolate` approach, which only accounts for two observations during the prediction process and is more sensitive to extreme or incorrect values.

**Example**
We explore the `mibmi` command with an anonymized sub-sample of diabetes patients from the Clinical Practice Research Datalink (CPRD). The algorithm was used on the full sample, in a recent investigation of the relationship between biological variables and mortality [17]. Here we present a significantly reduced sub-sample, edited using random processes to overcome sharing restrictions. The dataset holds information on age (in years), mean weight (in kg), height (in metres), mean BMI and the number of different drugs prescribed, from 1 April 2004 to 31 March 2012, aggregated into eight financial years (1 April to 31 March). In this series of examples we demonstrate the use of `mibmi` in cleaning and imputing BMI data, before using multi-level Poisson regression modelling to quantify the association between BMI and the number of drug prescription over an 1-year period (in either simple analyses or a multiple imputation framework).
We present BMI characteristics for two representative time points: 2009/10 (year 10) and 2011/12 (year 12), the last year of the study. At least one BMI measurement is available for 2605 of 3252 eligible individuals in 2009/10 (80.1%) and for 2315 of 3487 in 2011/12 (66.4%). A few very high BMI values are obviously erroneous. Nevertheless, we make no corrections and proceed to investigate the relationship between average BMI and polypharmacy, using a multi-level Poisson regression model.
The analysis on the original dataset indicates that the relationship between BMI and polypharmacy is very weak and non-significant. Next, we only use the simple cleaning approach of the \texttt{mibmi} command to remove unrealistic BMI values and correct using the provided weight and height, if possible.
A handful of extreme BMI observations were set to missing but further corrections have been performed, based on available weight and height measurements. We repeat the multi-level Poisson regression analysis on this cleaned dataset.

```
. mibmi patid year BMI age, clean xnomi
. sum BMI if year==10, detail

| Percentiles | Smallest |     |
|-------------|----------|-----|
| 1%          | 19.5     | 13.6|
| 5%          | 22.7     | 15.4|
| 10%         | 24.2     | 16  |
| 25%         | 26.8     | 16.6|
| 50%         | 30.4     | 16.6|
| 75%         | 34.5     | 61.2|
| 90%         | 39.5     | 64.6|
| 95%         | 43       | 65.5|
| 99%         | 51.9     | 149 |

| Largest | Std. Dev. |     |
|---------|-----------|-----|
| Mean    | 31.22808  | 6.739653|
|         | 45.42292  |     |
|         | 2.833741  |     |
|         | 39.60801  |     |

. sum BMI if year==12, detail

| Percentiles | Smallest |     |
|-------------|----------|-----|
| 1%          | 19       | 14.7|
| 5%          | 22.3     | 14.9|
| 10%         | 24.1     | 15.2|
| 25%         | 26.8     | 15.6|
| 50%         | 30.4     | 16.6|
| 75%         | 34.8     | 60.4|
| 90%         | 39.4     | 60.4|
| 95%         | 42.8     | 60.4|
| 99%         | 52.7     | 61  |

| Largest | Std. Dev. |     |
|---------|-----------|-----|
| Mean    | 31.27124  | 6.53911|
|         | 42.75996  |     |
|         | .9336805  |     |
|         | 4.69274   |     |
```
Analysis on the (simply) cleaned datasets suggests there is statistically significant relationship between BMI and polypharmacy. Next, we go one step further with the \texttt{mibmi} command by requesting simple and advanced cleaning on the original dataset.
A few more values are dropped due to regression cleaning (with a low 20% threshold defined by the `xclnp(#)` option). Repeating the analysis, we obtain similar results.

```
. mibmi patid year BMI age weight height clean xclnp(0.2) xnomi
Regression cleaning, patients completed (1000s of 4633):
    ....4633
. sum BMI if year==10, detail

| Percentiles | Smallest | BMI value (mean) |
|-------------|----------|------------------|
| 1%          | 19.48738 | 13.61082         |
| 5%          | 22.62626 | 15.427           |
| 10%         | 24.28097 | 16.01948         |
| 25%         | 26.75853 | 16.13539         |
| 50%         | 30.34607 | Mean             |
| 75%         | 34.41049 | 58.65837         |
| 90%         | 39.29687 | 58.94834         |
| 95%         | 42.77614 | 63.88196         |
| 99%         | 51.64055 | 65.09373         |

. sum BMI if year==12, detail

| Percentiles | Smallest | BMI value (mean) |
|-------------|----------|------------------|
| 1%          | 19.07347 | 14.97018         |
| 5%          | 22.4323  | 15.1418          |
| 10%         | 24.08822 | 15.73361         |
| 25%         | 26.75386 | 15.98455         |
| 50%         | 30.40625 | Mean             |
| 75%         | 34.74889 | 58.63347         |
| 90%         | 39.46992 | 60.19419         |
| 95%         | 42.86502 | 60.47346         |
| 99%         | 52.46133 | 61.59169         |
```

```
Next, we use `mibmi` not only to clean the data but also to generate a set of three MI variables holding imputed values.
mibmi patid year BMI age, weight(weight) height(height) clean xclean xclnp(0.2) minum(3)
Regression cleaning, patients completed (1000s of 4633):
....4633
Calculating variation between observed and interpolated BMI (6 steps)
.......4633
Imputing, patients completed (1000s of 4633):
....4633
   . sum _1_BMI if year==10, detail

    _1_BMI

Percentiles  Smallest
          1%      19.4       13.6
           5%      22.7       15.4
        10%      24.2       16.0       Obs        2780
       25%      26.7       16.6   Sum of Wgt.       2780
       50%      30.3     Mean       31.21903
      75%      34.4       65.5
     90%      39.5  65.94265   Variance     45.93442
    95%      43.0  68.66491   Skewness     2.75556
   99%      52.1     149   Kurtosis     37.03378
   . sum _1_BMI if year==12, detail

    _1_BMI

Percentiles  Smallest
          1%       19.0       14.9
           5%      22.4       15.2
        10%      24.2       15.6       Obs        2307
       25%      26.8       15.7   Sum of Wgt.        2307
       50%      30.4     Mean       31.28314
      75%      34.8       59.1
     90%      39.4       60.4   Variance     42.66367
    95%      42.8       60.4   Skewness     .9416641
   99%      52.7       61   Kurtosis     4.697162
   . tab mi miss

   _mi_miss  Freq.  Percent   Cum.
          0    17,491      74.39     74.39
          1      6,021      25.61    100.00
     Total     23,512     100.00
   . tab _1_info, missing

   _1_info  Freq.  Percent   Cum.
          0      1,152       4.90      4.90
          .    22,360     95.10    100.00
     Total     23,512     100.00
   . tab mi ipat

   _mi_ipat  Freq.  Percent   Cum.
          0    17,491      74.39     74.39
          1      6,021      25.61    100.00
     Total     23,512     100.00
We focus on the characteristics of variable \_1\_BMI, but the imputed cases (not imputed values) are identical across all three variables. For 2009/10 (year 10) and each imputation set, the algorithm imputed 179 observations (2780 now, compared to 2601 when only using simple and advanced cleaning). Unsurprisingly, no values are interpolated for the last time point, 2011/12 (year 12). Three new variables provide information on the interpolation process: \_mi\_miss flags all missing BMI observations; \_l\_iinfo flags cases where interpolated values for \_1\_BMI were unrealistic and had to be constrained (in this example there were none, amongst the 1152 that were imputed); and \_mi\_ipat flags all patients for whom at least one observation was interpolated, at any point in time. The role of \_mi\_ipat is to allow users to easily obtain the number of patients with at least one interpolation:

```
. keep if \_mi\_ipat==1
(17491 observations deleted)
. duplicates drop patid, force
Duplicates in terms of patid
(5141 observations deleted)
. count
  880
```

Using this interpolation dataset to run multiple imputation analyses, with the \mi\ estimate prefix, we obtain similar results.

```
. mi xtset patid
   panel variable: patid (unbalanced)
. mi estimate, irr: xtpoisson all_drugs_1y BMI i.year
(4401 m=0 obs. now marked as complete)
(3270 m=0 obs. now marked as incomplete)
(55791 values of imputed variable BMI in m>0 updated to match values in m=0)

. mi estimate, irr: xtpoisson all_drugs_1y BMI i.year
```

---

| all_drugs_1y | IRR  | Std. Err. | t     | P>|t| | [95% Conf. Interval] |
|--------------|------|-----------|-------|-----|---------------------|
| BMI          | 1.010885 | .0010804 | 10.13 | 0.000 | 1.008769 1.013004 |
| year         |       |           |       |       |                     |
| 2005/6       | 1.032222 | .016886 | 1.94  | 0.053 | .9996514 1.065855  |
| 2006/7       | 1.068995 | .0172694 | 4.13 | 0.000 | 1.035678 1.103384  |
| 2007/8       | 1.088244 | .0174757 | 5.27 | 0.000 | 1.054526 1.12304  |
| 2008/9       | 1.120471 | .0178594 | 7.14 | 0.000 | 1.086009 1.156028  |
| 2009/10      | 1.128084 | .0181358 | 7.50 | 0.000 | 1.093093 1.164196  |
| 2010/11      | 1.158014 | .0188572 | 9.01 | 0.000 | 1.121638 1.195569  |
| 2011/12      | 1.172456 | .0198488 | 9.40 | 0.000 | 1.134191 1.212011  |
| _cons        | 2.388141 | .0845235 | 24.60 | 0.000 | 2.228093 2.559685  |
| /lnalpha     | -1.930755 | .0336021 | -1.996614 | -1.864896 |
| alpha        | .1450386 | .0048736  | .1357943 | .1549123 |
Finally, we can use all four aspects of mibmi with the original dataset: simple and advanced cleaning, interpolation and extrapolation.

> mibmi patid year BMI age weight height clean xclean xclnp(0.2) iextrapol
> ate minum(3)
Regression cleaning, patients completed (1000s of 4633):
.....4633
Calculating variation between observed and interpolated BMI (6 steps)
......
Calculating variation between observed and extrapolated BMI (6 steps)
......
Imputing, patients completed (1000s of 4633):
.....4633
> . sum _1_BMI if year==10, detail

| Percentiles | Smallest  |
|-------------|-----------|
| 1%          | 19.1      |
| 5%          | 22.3      |
| 10%         | 24        |
| 25%         | 26.6      |
| 50%         | 30.2      |
| 75%         | 34.49384  |
| 90%         | 39.3      |
| 95%         | 42.98726  |

| Largest | Std. Dev. |
|---------|-----------|
| Obs     | 3011      |
| Sum of Wgt. | 3011 |
| Mean    | 31.0892   |
| Std. Dev. | 6.866588 |

For 2009/10 (year 10) and each imputation set, the algorithm now imputed 410 observations, of which 213 are extrapolations (3011 now, compared to 2780 with interpolation and cleaning and 2601 with cleaning only).

For the last time point, 2011/12 (year 12), 416 values were imputed with extrapolation (2723 now, compared to 2307 before). Additional new variables provide information on the extrapolation process: _1_xinfo flags cases where interpolated values for _1_BMI were unrealistic and had to be constrained (in this example there was one...
amongst the 1183 extrapolated values); and _mi_xpat flags all patients for whom at least one observation was interpolated, at any point in time (with a role similar to _mi_ipat, allowing users to obtain the number of patients with at least one extrapolation).

Results from a multiple imputation analysis on the final dataset obtained with mibmi were similar to those previously obtained, as expected. Practically, the requested imputations are assuming MCAR missingness since there is no conditional missingness on observed data, and hence inference estimates should be very similar to what we observed previously. However, this is not necessarily the case for standard errors (although in this example they are):

```
.mi xtsset patid
   panel variable:  patid (unbalanced)

.mi estimate, irr: xtpoisson all_drugs_1y BMI i.year
(8708 m=0 obs. now marked as complete)
(1577 m=0 obs. now marked as incomplete)
(55791 values of imputed variable BMI in m>0 updated to match values in m=0)

Multiple-imputation estimates
Imputations =    3
Random-effects Poisson regression
Number of obs = 20957
Group variable: patid
Number of groups = 4334
Random effects u_i - Gamma
Obs per group: min = 1
   avg = 4.8
   max = 8
Average RVI = 0.0022
Largest FMI = 0.0192
DF: min = 5603.51
   avg = 2.69e+08
   max = 1.01e+09
Model F test:  Equal FMI
   F(  8, 1.3e+06) = 26.82
Within VCE type: OIM
   Prob > F = 0.0000

| all_drugs_1y | IRR   | Std. Err. | t     | P>|t| | [95% Conf. Interval] |
|--------------|-------|-----------|-------|------|----------------------|
| BMI          | 1.010908 | 0.0010641 | 10.31 | 0.000 | 1.008824 1.012996 |
| year         |       |           |       |      |                      |
| 2005/6       | 1.036132 | 0.0167588 | 2.19  | 0.028 | 1.0038 1.069505    |
| 2006/7       | 1.072188 | 0.0170877 | 4.37  | 0.000 | 1.039214 1.106207  |
| 2007/8       | 1.091743 | 0.0172737 | 5.55  | 0.000 | 1.058407 1.126129  |
| 2008/9       | 1.125405 | 0.0176589 | 7.53  | 0.000 | 1.091321 1.160554  |
| 2009/10      | 1.102981 | 0.017306  | 6.25  | 0.000 | 1.069578 1.137427  |
| 2010/11      | 1.134063 | 0.0179397 | 7.95  | 0.000 | 1.099441 1.167775  |
| 2011/12      | 1.074656 | 0.0175422 | 4.41  | 0.000 | 1.040818 1.109594  |
| _cons        | 2.380235 | 0.0830446 | 24.86 | 0.000 | 2.222886 2.548723  |

/lnalpha -1.884659 0.0325785 -1.948512 -1.820806
alpha .1518809 .0049481 .142486 .1618952
```
Performance

To assess the performance of mibmi, in relation to the recently presented twofold algorithm, we used a version of the diabetes patients dataset we presented previously. For this exercise, the dataset included additional information on HbA1c (glucose), systolic and diastolic blood pressure and total cholesterol. First, we applied the mibmi algorithm with the simple and regression cleaning options to obtain a more reliable measure for BMI, thus not allowing extreme and erroneous values to affect the comparison. Then we performed two assessments of performance, when one or three values were missing between two observations for each individual. We did not choose to evaluate through a simulations framework since the assumptions under which we have simulated the data would be critical to the analyses and the evaluation could be seen as self-fulfilling prophecy. Rather, we used real data to assess deviations from observations. Therefore, we could not evaluate the performance (e.g. coverage, power) of the inferential models since the true effects and associations were unknown.

In the first assessment, we randomly selected 10,000 people with 3 or more BMI measurements over the study period and we randomly set one BMI observation per person to missing. We then used mibmi, with both simple (×1) and multiple imputation options (×100), and twofold in which we used all five available biological parameters for the multiple imputations. Under a multiple imputations approach, we obtained 100 BMI variables, for each algorithm. Each set was then aggregated and we obtained their mean value for each of the 10,000 ‘missing’ observations. Finally, these aggregates, as well as the simple imputation BMI from mibmi, were compared to the ‘true’ BMI values to calculate absolute mean differences (mean error). Table 1 presents the overall results and for interpolated and extrapolated values separately, since the underlying principles in their imputations are different, for mibmi at least. Performance for interpolated values appears to be similar while twofold performs better for extrapolations.

In the second assessment, which focused on interpolation, we again randomly selected 10,000 people but this time with 5 or more BMI measurements over the study period. Next, for each individual, we randomly set three concurrent BMI observations to missing but ensuring these were observations that would be imputed as interpolations under the mibmi algorithm (i.e. observations were available both before and after these ‘missing’ values, for all patients). As before, we used mibmi, with both simple and multiple imputation options, and twofold with the five available biological parameters for the multiple imputations and we aggregated to obtain mean errors. Results are presented in Table 2, both overall and for each of the three sequential observations that we set to missing. Performance was better with mibmi, especially for the second time point, the one furthest away from observations. A prediction example using a single patient is presented in Fig. 2.

These results indicate that, for interpolating BMI values, there is little useful information in other biological parameters and the additional effort of obtaining them is not justified. The mibmi algorithm generates realistic linear or curvilinear trends for BMI over time and the higher computational complexity pays off more as the number of concurrent missing values increases. However, for extrapolating BMI values, performance is better with the twofold fully conditional specification algorithm and use of all biological parameters, at least when only two observations per individual are available. In such a scenario, each extrapolation is based on an individual-level model that uses only two observations

| Cases   | Methoda | Obs.  | Mean   | Std.Dev | Min   | Max   |
|---------|---------|-------|--------|---------|-------|-------|
| Allb   | Simple  | 10000 | 1.113  | 1.353   | 0.000 | 26.900|
|        | mibmi   | 10000 | 1.120  | 1.351   | 0.000 | 26.888|
|        | Twofold | 10000 | 0.949  | 1.026   | 0.000 | 15.481|
| Interpolation | Simple  | 6132  | 0.801  | 0.819   | 0.000 | 11.651|
|        | mibmi   | 6132  | 0.808  | 0.819   | 0.001 | 11.429|
|        | Twofold | 6132  | 0.804  | 0.810   | 0.000 | 11.180|
| Extrapolation | Simple | 3868  | 1.606  | 1.808   | 0.000 | 26.900|
|         | mibmi   | 3868  | 1.614  | 1.805   | 0.000 | 26.888|
|         | Twofold | 3868  | 1.179  | 1.260   | 0.001 | 15.481|

a Simple refers to a single imputation that ignores variability in the observations (option xsimp); mibmi refers to the default multiple imputation approach with the command and 100 imputations; twofold refers to the twofold algorithm described in the paper and 100 imputations
b All refers to both interpolations (between observations imputations) and extrapolations (not between observations imputations)
which, unsurprisingly, can generate extreme values in some cases. Although the accuracy of extrapolation predictions might improve for \texttt{mibmi} as the number of available observations increases, performance with the \texttt{twofold} algorithm should remain better.

**Discussion**

In this paper we presented \texttt{mibmi}, a new command for cleaning and imputing BMI values, or other variables with very low individual-level variability, in longitudinal settings. Using a pseudo-anonymised dataset from

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**Table 2 Mean errors between observed and imputed BMI values, three sequential missing values per individual (interpolation only)**

| Cases      | Method* | Obs. | Mean | Std.Dev | Min | Max   |
|------------|---------|------|------|---------|-----|-------|
| All\(^b\)  | Simple \(\times 1\) | 30,000 | 0.980 | 1.002 | 0.000 | 16.017 |
|            | mibmi \(\times 100\) | 30,000 | 0.989 | 1.004 | 0.000 | 16.034 |
|            | Twofold \(\times 100\) | 30,000 | 1.137 | 1.155 | 0.000 | 18.318 |
| Time point 1 | Simple \(\times 1\) | 10,000 | 0.935 | 0.945 | 0.000 | 9.829  |
|            | mibmi \(\times 100\) | 10,000 | 0.943 | 0.947 | 0.000 | 9.779  |
|            | Twofold \(\times 100\) | 10,000 | 1.094 | 1.114 | 0.000 | 18.318 |
| Time point 2 | Simple \(\times 1\) | 10,000 | 1.059 | 1.068 | 0.000 | 16.017 |
|            | mibmi \(\times 100\) | 10,000 | 1.069 | 1.071 | 0.000 | 16.034 |
|            | Twofold \(\times 100\) | 10,000 | 1.234 | 1.231 | 0.000 | 17.126 |
| Time point 3 | Simple \(\times 1\) | 10,000 | 0.947 | 0.984 | 0.000 | 10.645 |
|            | mibmi \(\times 100\) | 10,000 | 0.955 | 0.985 | 0.000 | 10.538 |
|            | Twofold \(\times 100\) | 10,000 | 1.084 | 1.111 | 0.000 | 13.473 |

\(^a\) Simple refers to a single imputation that ignores variability in the observations (option \texttt{xsimp}); \texttt{mibmi} refers to the default multiple imputation approach with the command and 100 imputations; \texttt{twofold} refers to the twofold algorithm described in the paper and 100 imputations

\(^b\) All refers to aggregates across all three time points
the Clinical Practice Research Datalink we described the command’s cleaning and imputation functions over a few examples and we also assessed its performance. The command is available to download from the ssc archive by typing `ssc install mibmi` within Stata. Alternatively readers can automatically download from the first author’s personal web page by typing `net from http://stataanalysis.co.uk` within Stata and following the instructions.

We argue that `mibmi` can be a useful tool for researchers who wish to use longitudinal values for BMI or other variables with very low individual-level variability, in descriptive or inferential analyses. The command is fully compatible with the `mi` family of Stata and we incorporated numerous features to allow for flexibility in the imputation process, allowing the user to assume certain MNAR mechanisms. The same processes could be used for imputation of other parameters, providing one can assume very strong correlation over time and linearity.

The algorithm’s advantage is its ability to provide multiple datasets with imputed values for the variable of interest when no other information is available, except for an individual identifier and time. For interpolations, BMI performance was overall better than in other multiple imputation approaches that use additional biological data. Because of the command’s individual by individual approach, the interpolation and, especially, extrapolation processes are computationally expensive and, for very large datasets (of hundreds of thousands of patients), the command can take weeks to execute. When multiple imputation is selected, we recommend 5 generated datasets. However, the process can be parallelized and for large centralized data repositories, like the UK Primary Care Databases (CPRD, THIN, QResearch), `mibmi` could be applied once at a high level and the imputed BMI values distributed to users when requested, on a protocol-by-protocol basis. The algorithm will effectively ignore patients with fewer than 2 BMI values over time and hence researchers are unlikely to have a complete final dataset to analyze. Also note that users who extrapolate may take care to impute at appropriate times only (e.g. not when age <18).

In the context of BMI imputation, when additional biological information is available (e.g. blood pressure values), we advise its use in conjunction with `twofold`, especially for extrapolations. In the first step, users can execute `mibmi` to obtain a more reliable BMI variable through the cleaning options and generate interpolated values for patients with at least two observations over the study period. In the second step they can use the generated variable with the `twofold` algorithm, to obtain multiple imputations for BMI and other variables.

**Abbreviations**
BMI: body mass index; CPRD: Clinical Practice Research Datalink; EMR: electronic medical records; MAR: missing at random; MCAR: missing completely at random; MNAR: missing not at random; THIN: the health improvement network; UK: United Kingdom.

**Authors’ contributions**
EK designed and developed the command and wrote the manuscript. RP, DR and DAS critically commented on both the manuscript and the functionality of the command. All authors read and approved the final manuscript.

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**Competing interests**
The authors declare that they have no competing interests.

**Availability of data and materials**
The command is freely available to download. We are not allowed to share CPRD data.

**Consent for publication**
Not applicable.

**Ethics and consent statement**
This study is based on data from the Clinical Practice Research Datalink (CPRD) obtained under licence from the UK Medicines and Healthcare products Regulatory Agency. However, the interpretation and conclusions contained in this paper are those of the authors alone. The study was approved by the independent scientific advisory committee (ISAC) for CPRD research (reference number: 16/115R). No further ethics approval was required for the analysis of the data.

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