Observation of pendular butterfly Rydberg molecules

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Engineering molecules with a tunable bond length and defined quantum states lies at the heart of quantum chemistry. The unconventional binding mechanism of Rydberg molecules makes them a promising candidate to implement such tunable molecules. A very peculiar type of Rydberg molecules are the so-called butterfly molecules, which are bound by a shape resonance in the electron–perturber scattering. Here we report the observation of these exotic molecules and employ their exceptional properties to engineer their bond length, vibrational state, angular momentum and orientation in a small electric field. Combining the variable bond length with their giant dipole moment of several hundred Debye, we observe counter-intuitive molecules which locate the average electron position beyond the internuclear distance.
Controlling the internal and external quantum states of molecules is the central goal of ultracold chemistry \(^1\) and allows for the study of coherent molecular dynamics, collisions \(^2\)-\(^3\) and tests of fundamental laws of physics \(^4\). If the molecules additionally possess a permanent electric dipole moment, the study of dipolar quantum gases and spin systems with long-range interactions \(^7\)-\(^8\) as well as applications in quantum information processing \(^9\)-\(^11\) are possible. Rydberg molecules constitute a class of exotic molecules, which are bound by the interaction between the Rydberg electron and a ground state atom. This peculiar interaction represents a novel chemical binding mechanism, that is based on the elastic S- and P-wave scattering between the electron in a Rydberg state and a ground state perturber atom, which is located inside the electron wavefunction.

The scattering is described by a Fermi-type contact interaction with an energy-dependent scattering length \(^12\)-\(^15\). The bond length of these molecules is connected to the extension of the electron wavefunction and can reach hundreds of nanometers \(^14\),\(^16\). In the extreme case, the interaction with the ground state atom can substantially displace the electron from the ionic core, giving rise to permanent electric dipole moments in the kilo-Debye range \(^12\). This holds even in the case of homonuclear molecules due to the vanishing exchange energy. The extreme properties of Rydberg molecules make them versatile objects for the study of low-energy electron–atom scattering, precision calculation of potential energy curves \(^18\), molecular dipole–dipole interaction, Rydberg blockade and anti-blockade effects in molecular samples as well as complex molecular dynamics.

Due to the presence of a shape resonance in the P-wave scattering, a special type of Rydberg molecules with large binding energies and exceptional properties arises. These so-called butterfly molecules were predicted theoretically in 2002 (refs 19,20) but clear experimental evidence for their existence was missing so far. Here, we report on the photoassociation of butterfly Rydberg molecules and their orientation in a weak electric field. Starting from a Bose–Einstein condensate of rubidium atoms, we fully control the external degrees of freedom and spectroscopically resolve the rotational structure and the emerging pendular states in an external electric field. This not only allows us to extract the bond length, the dipole moment and the angular momentum of the molecule but also to deterministically create molecules with a tunable bond length and orientation. We anticipate direct applications in quantum chemistry, many-body quantum physics and quantum information processing.

**Results**

**Butterfly Rydberg molecules.** Butterfly Rydberg molecules are dominated by the P-wave scattering between the Rydberg electron and the ground state atom, which maximizes the gradient of the electron wavefunction at the position of the ground state atom (see Methods). As a consequence, all angular momentum states of the Rydberg electron are mixed and the electron density acquires a characteristic density distribution which resembles a butterfly (Fig. 1). The first spectroscopic evidence for the existence of this mechanism has been reported in refs 21,22. The calculation of the corresponding potential energy curves (PEC) in the Born–Oppenheimer approximation requires the diagonalization of the full Hamiltonian, which in our approach includes the fine structure in the Rydberg atom, the hyperfine interaction in the perturber atom, and all S- and P-wave scattering processes (see Methods). The PECs in the vicinity of the 25p-state are shown in Fig. 2a. The butterfly states detach from the \( n = 23 \) hydrogenic manifold and cross all lower-lying states down to the 25p-state. The red PECs are relevant for this work and the bound states in the strongly oscillating part of the PEC are the butterfly molecules under investigation. Even for the deepest potential wells the electron wave functions in these PECs possess a 15% admixture of the 25p-state, which we use to excite the butterfly molecules with a single photon transition.

**Photoassociation spectroscopy.** The experiment was performed in a Bose–Einstein condensate (BEC) of \(^{87}\)Rb with a peak particle density of \( 4 \times 10^{14} \text{ cm}^{-3} \), an atom number of \( 2 \times 10^5 \) and a temperature of 100 nK. All spin states of the \( 5S_{1/2}, F = 1 \) ground state were populated. The photoassociation of the butterfly molecules was achieved using a single photon transition to the energetic vicinity of the adiabatic free two-particle state \( 25p_{1/2} \otimes 5S_{1/2}, F = 1 \), which serves as reference point for our spectroscopy throughout this work. Since the created butterfly molecules can decay into ions by photoionization and associative ionization \(^23\), the produced ions are used as a probe for the creation of the molecule.

The experimental sequence consists of 500 ms continuous excitation and ion detection. By detuning the excitation laser up to \(-60\) GHz in steps of 2 MHz we obtain the spectrum shown to the right of Fig. 2b. As the laser detuning is gradually increased, we start to probe the bound states in the butterfly potential. We observe a plenitude of molecular states up to an energy of \(-50\) GHz. This is in accordance with the calculated PECs. Moreover, the density of molecular states drops at detunings below \(-40\) GHz, which marks the transition to a spectral region, where only the lowest bound states in each potential well are populated. The spectroscopic results directly prove the existence of butterfly molecules.

**Pendular states.** We now focus on the ground state molecules in each potential well and demonstrate, how butterfly molecules...
with selected bond length and high degree of orientation can be created. Due to the symmetry breaking caused by the localized valence electron of the perturber, butterfly molecules, along with the related class of so-called triborite molecules, are the only known homonuclear molecules with a large permanent electric dipole moment\cite{14,15,17,24}. The interaction of the dipole moment $\mu$ with an external electric field $F$ significantly changes the rotational structure of the molecule. In the simplest approximate description of a dipolar rigid rotor that neglects the coupling of the nuclear motion to the electronic and nuclear spin degrees of freedom, the eigenstates of energy $E$ need to fulfil (see Methods)

$$
(B_p^2 - \mu \cdot F - E) |\Phi\rangle = 0. \tag{1}
$$

In equation (1), the zero of the energy axis is chosen to coincide with the rotationless vibrational energy level being studied. For vanishing electric field, the molecule behaves as a rigid rotor of length $R_0$ and reduced mass $m_r = m_{Rb}/2$ using the rotational quantum number $N$, its projection on the molecular axis $M_N$ and the rotational constant $B_p = \hbar^2/2I$, where $I = m_rR^2$ represents the moment of inertia of the rigid rotor. When, on the other hand, the interaction with the electric field dominates the rotational constant ($\omega = |\mu \cdot F| / B_p \gg 1$), the molecule enters so-called pendular states\cite{25,26}, which are characterized by the quantum number $n$ and differ in the degree of orientation of the molecule with respect to the field axis (Fig. 3a). In this regime only the angular momentum projection $M_N$ remains a good quantum number, while the rotational quantum numbers $N$ are strongly mixed.

In Fig. 3b, we show the electric field-dependent spectra of the butterfly state at $-47.9$ GHz along with the fitted theory of equation (1). Due to the huge dipole moments of the butterfly molecules, fields of $1 \text{ V cm}^{-1}$ are sufficient to put the system deep in the pendular regime. Varying the electric field, we can directly observe the crossover from rotational states to pendular states. At fields of $4 \text{ V cm}^{-1}$, the degree of orientation $\omega$ exceeds previous record values\cite{26} by a factor of two. Since we photoassociate the butterfly molecules in a Bose–Einstein condensate, which has no angular momentum in the centre of mass motion, only states with $|M_N| = 0$ and $|M_N| = 1$ can be observed (see Methods). This leads to a very clean spectrum of pendular states, which, in contrast to previous studies\cite{16,17,21,22,24}, allows to determine the dipole moment $\mu$ with an estimated precision of $10 \text{ Debye}$ and the bond length $R_0$ with an estimated precision of $5 \text{ a}_0$.

Applying this method to eight of the lowest spectroscopic lines in the butterfly spectrum, we can extract the respective dipole moments and bond lengths (Fig. 2c). This additional information enables an improved interpretation of the butterfly spectrum and comparison with theory. This is demonstrated in Fig. 2b, where the orange points mark the measured bond lengths and binding energies for the eight studied lines. The energetic deviation of the measured points from the predicted bound states is only few per cent of the binding energy and is most likely explained by inaccurate $P$-wave scattering phase shifts assumed in the model. It is remarkable how well the measured bond lengths agree with the wells of the model potential. In fact, the positions of the wells are mainly determined by the strong gradient at the radial nodes of the $p$-state electronic wavefunction and thus the bond length of the butterfly molecules is an indirect measure for the position of the 25$p$ radial nodes. A comparison of the measured bond lengths with the nodes of the calculated 25$p_1/2$ wavefunction is shown in the top panel of Fig. 2b.

**Properties.** Butterfly molecules also exhibit counter-intuitive properties. In a semiclassical picture of molecules with one valence electron, the average position of the electron is always located between the two nuclei. The maximum possible dipole moment is thus limited by the bond length, as realized, for example, in an ionic bond. The strong interference of the electron caused by the scattering with the ground state atom (Fig. 1) permits the butterfly molecules to exceed this limit and locate the electron’s average position beyond the perturber (Fig. 2d). This effect is seen experimentally for the deepest bound butterfly...
molecules. The state at $-50.3$ GHz possesses a dipole moment of 380 Debye, which is 30% larger than that of two opposite charges separated by the measured bond length of 116 $a_0$. This phenomenon is even stronger in the theoretical model, which reveals a dipole moment of 442 Debye for the studied state. Throughout all investigated butterfly states the measured dipole moments are systematically lower than the calculated values but do not deviate by $>35\%$.

Due to the deep potential wells (Fig. 2b), inward tunnelling and subsequent decay should not limit the lifetime of the studied butterfly molecules. In a separate experiment using short excitation pulses (see Methods) we were able to determine the lifetimes of the strongest observed butterfly molecules. In the high-density environment of a BEC we find a lifetime of 5 $\mu$s which is mainly limited by inelastic collisions with additional ground state atoms. Extrapolating to zero ground state density to mitigate the effect of collisions we find a lifetime on the order of 20 $\mu$s, which is compatible with the lifetime of the $25p$ Rydberg state.

**Discussion**

The long lifetime along with the negligible motion of the ground state atoms in the BEC enables narrow photoassociation lines and thus a clean optical spectroscopy. This allows for the deterministic creation of vibrational ground state molecules with a selected bond length and dipole moment. In a weak electric field we can furthermore restrict the rotation of the molecule and precisely set the orientation of the molecule with respect to the field axis. This high degree of control over molecules with giant dipole moments even in a sample with only one atomic species opens many perspectives for future applications. The high precision of the molecular spectroscopy can serve as a benchmark for quantum chemical calculations of molecular states. Rydberg molecules are promising candidates to implement dipolar interactions in many-body quantum systems. The comparable energy scale of the rotational structure and the dipole–dipole interaction is unique in the world of polar molecules and will complement studies using heteronuclear alkali dimers in the rovibrational ground state. Starting from pre-associated weakly bound ground state molecules in a three-dimensional optical lattice, spin physics with pendular states are feasible. Dressing weakly bound molecules with a Rydberg molecule might even allow to study coherent tunnelling dynamics with long-range interactions. It will be interesting in the future to extend the concepts of the Rydberg blockade and anti-blockade to interacting Rydberg molecules. Butterfly molecules might also be a good starting point to prepare heavy Rydberg systems. Ultimately, pendular states of dipolar molecules could also be a building block to scalable quantum information processing.

**Methods**

**Calculation of the butterfly PECs.** Rich spectral features, such as average line shifts and collisional broadening, arise when a Rydberg atom is excited in a high-density gas. These effects have been understood since Fermi’s idea of a quasi-free electron could successfully explain the early experiments by Amaldi and Segre. Extending Fermi’s work, Omont later generalized the zero-range $S$-wave potential to higher partial waves. The contribution of the $P$-wave becomes particularly important in alkali atoms, as those show a low-energy shape resonance in the $3p$ scattering channel. To model the high-resolution spectroscopy of rovibrational diatomic Rydberg levels, we not only include the singlet electron–Rb $S$-wave and $P$-wave scattering information but also the spin–orbit splitting of the Rydberg state and the ground state $^{87}$Rb($5s_{1/2}$) hyperfine structure. Thus, the Hamiltonian for the

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**Figure 3 | Pendular states.** (a) Plot of the orbitals $|\Phi(l, \rho)|$ for pendular states $|M_N\rangle$ of a dipolar molecule with $\mu = 482$ Debye in an electric field of $1 \text{V/cm}$–1. (b) Spectroscopy of the butterfly state at $-47.9$ GHz in different electric fields. Each spectrum is normalized and shifted on the $y$ axis according to the applied electric field. The coloured lines show the eigenenergies of a rigid rotor with a permanent dipole moment in an electric field (equation (1)) for $|M_N| = 0$ (weak lines) and $|M_N| = 1$ (strong lines). The dipole moment and the bond length are adapted to fit the experimental data. In this case, we find $R_0 = 205$ $a_0$ and $\mu = 482$ Debye. The inset shows a zoom of the low-field ($\approx 30 \text{mV/cm}$–1) measurement together with the calculated position of the first five eigenstates of the dipolar rotor model with $|M_N| = 1$. We attribute the appearance of higher $\nu$ states at field strength $F = 0$ to the mixing of higher $N$ states in the residual field (see Methods).

**Figure 4 | Polarization dependent coupling strength of the pendular states.** The spectrum of the butterfly state at $-47.9$ GHz in an electric field of 0.44 V/cm–1 is shown for two different angles between the linear laser polarization and the electric field axis. While for parallel polarization (solid blue line) mainly $|M_N| = 0$ states (blue patches) are excited, we see that for orthogonal polarization (solid red line) mainly $|M_N| = 1$ states (red patches) are excited. In both cases the qualitative behaviour is nicely reproduced by the admixture of the $N=1$ state to the corresponding pendular state that is extracted from the the rigid rotor model (dashed lines).
focused to a beam waist of $40 \mu m$. Since the spacing of the vibrational levels inside the wells is vanishing overlap of the nuclear wavefunction allows only for states located in the nuclear spin degrees of freedom. Due to the particular nature of the butterfly BEC that has no angular momentum in the centre of mass motion, only rotational frequencies of $2\Omega_0$ and $2\Omega_0$ dominate the spectrum. If, on the other hand, the laser polarization is orthogonal to the electric field axis, we drive both transitions and the $|\nu_1\rho_1\lambda_1\mu_1\rangle$ states. The coupling strength is therefore proportional to the admixture of the $|\nu_1\rho_1\lambda_1\mu_1\rangle$ states. The excitation pulse has a duration of 500 ms, where $A_{\text{p}}$ represents the hyperfine structure of the perturbing atom $^{87}\text{Rb}$. The last term in equation (2) represents the hyperfine structure of the perturbing atom $^{87}\text{Rb} 5s_{1/2}$ with $A = 3.417$ GHz. The present Hamiltonian is diagonalized in a truncated basis of atomic levels, along with the electron and nuclear spin degrees of freedom for the perturbing ground state atom, that is, $|N_d,m_L,m_J\rangle \equiv |N_d,m_L,m_J,R\rangle$, where $L_1$, $I_1$ and $m_1$ are associated with the projectile $^{87}\text{Rb}$ in refs.29,31, whereas the position $\mathbf{r}_{\text{R}}$ and $\mathbf{m}_{\text{R}}$ stands for the hyperfine levels in the perturbing atom.

**Dipolar rigid rotor model.** The simplest approximate description for the observed rotational structure of the Rydberg molecules includes only the squared rotational angular momentum operator $\hat{N}_R^2$, and thus ignores coupling to the electronic and nuclear spin degrees of freedom. Due to the particular nature of the butterfly potentials also the mixing of vibrational states can be neglected. The otherwise vanishing overlap of the nuclear wavefunction allows only for states located in the well to be mixed. Since the spacing of the vibrational levels inside the wells is vanishing overlap of the nuclear wavefunction allows only for states located in the nuclear spin degrees of freedom. Due to the particular nature of the butterfly BEC that has no angular momentum in the centre of mass motion, only rotational frequencies of $2\Omega_0$ and $2\Omega_0$ dominates the spectrum. If, on the other hand, the laser polarization is orthogonal to the electric field axis, we drive both $\sigma^+$ and $\sigma^-$ transitions and thus mainly couple to the $|N_d=1\rangle$ states.

Since the BEC provides an initial state with $N = 0$, $M_d = 0$ and the usual angular momentum selection rules $\Delta N = \pm 1$ (but $N = 0\rightarrow N = 0$ forbidden) need to be fulfilled in the photoassociation process, we can only couple to $|N=1, M_d = 0\rangle$ states. The coupling strength is therefore proportional to the admixture of the $|N=1\rangle$ state.

**Data availability.** The data that support the findings of this study are available from the corresponding author upon request.

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T.N., O.T., T.E. and C.L. performed the experiment. H.O. supervised the experiment. T.N. analysed the data and prepared the manuscript. T.N., O.T., J.P.-R., C.G. and H.O. developed the theoretical model. All authors contributed to the data interpretation and manuscript preparation.

Additional information
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