Band gap determination using absorption spectrum fitting procedure

Nader Ghobadi

Abstract

In this article, using the Tauc model, the absorption spectrum fitting method was applied to estimate the optical band gap and width of the band tail of the CdSe nanostructural films that requires only the measurement of the absorbance spectrum, and no additional information such as the film thickness or reflectance spectra is needed. Samples are prepared by chemical bath deposition method. Fabricated nanostructural thin films are thick but are composed from nanoparticles.

Keywords: Absorption spectrum fitting, Thin film, Nanostructured material, Chemical synthesis

Background

The semiconductor nanoparticles have properties between molecules and bulk solid semiconductors. Their physicochemical properties are found to be strongly size dependent [1-8]. It is well known that the nano-scale systems show interesting physical properties such as increasing semiconductor band gap due to electron confinement [8-11]. Surface atoms play an important role in governing the electronic and optical properties in nanomaterials. The estimation of energy band gap in nanostructural semiconductors is somewhat difficult because surface atoms edges of the valence and conduction bands are not abrupt and the tail states complicate the definition of the true optical gap [1-8]. The aim of this paper is to explain how one can determine the energy band gap in nanostructural semiconductors that only requires the measurement of the absorbance spectrum and without the need of additional information, such as the film thickness or reflectance spectra [12,13]. Cadmium selenide belongs to the binary metal chalcogenides of group AII-BVI semiconductors and is a widely used AII-BVI semiconductor where its bulk band gap ($E_g = 1.74$ eV) lies in the solar energy spectrum. Chemical bath deposition (CBD) method is presently attracting considerable attention as it does not require sophisticated instrumentation. It is relatively inexpensive, easy to handle, convenient for large area deposition, and capable of yielding good quality thin films. The characteristics of the chemically deposited CdSe thin films by CBD strongly depend on the growth condition, and by changing the deposition key parameters one can control thickness, size of nanoparticles, and the energy band gap of the obtained thin films.

Brus considered a model for the energy band gap with particle size that yields the following expression for the band gap, $E_R$, of the quantum dot,

$$E_R = E_g + \frac{\hbar^2 \pi^2}{2 R^2} [1/m_e + 1/m_h] - 1.8 e^2/\varepsilon R$$

Where $E_R$ is the bulk band gap, and $R$ is the radius of the quantum dot; $m_e$, $m_h$, and $\varepsilon$ are electron mass, hole mass, and dielectric constant, respectively. The third term arises due to the Coulomb attraction [8-10].

Methods

The CdSe thin films were grown on ordinary glass slides ($26 \times 7.6 \times 0.2$ mm). Before deposition, the substrates were washed in detergent, rinsed in acetone, ultrasonically cleaned, and finally rinsed again with a mixture of double distilled water and methanol. The substrates were kept in vacuum. The deposition solution was prepared by a process similar to that used by Mane et al. [14]. A 400 ml of 0.25 M cadmium acetate (to provide Cd$^{2+}$ ions) was taken in a glass beaker with 1,000 ml capacity, under constant stirring, and then 25% ammonia was added to this solution slowly. At first the solution became milky and further addition of excess ammonia made the solution clear and transparent. A 400 ml of
freshly prepared 0.25 M Na$_2$SeSo$_3$ [14] was added slowly to the solution. The glass substrates were vertically immersed in the deposition solution with volume (12 x 19 x 15 cm), and the bath solution was covered.

In order to control the rate of film growths, the bath temperature was kept constant at desired value (room temperature). In order to control the pH, ammonia is added to the solution which contains Cd$^{2+}$ ions. At the end of the deposition process, all the deposited substrates were removed from the chemical bath at suitable intervals (4 to 24 h) and were washed with deionized water and methanol to remove the loosely adhering CdSe nanoparticles on the film. The coating of one side of each substrate was removed by cotton swab moistened with dilute HCl, and then the films were dried in the air and finally placed in the desiccators.

The overall reaction is shown as [15]

$$[\text{Cd(NH}_3)_4]^{2+} + \text{Se}^2- \rightarrow \text{CdSe} + 4\text{NH}_3$$

The films were structurally characterized by X-ray diffraction (XRD) using a Philips Analytical X-ray diffractometer (Royal Philips Electronics, Amsterdam, The Netherlands) in the 2θ geometry. The optical absorption was measured by a UV–vis spectrometer. Surface morphology was investigated by scanning electron microscopy.

| Table 1 Energy band gap and width of band tail for CdSe nanoparticle films at pH = 12 |
|----------------------------------------|--------|--------|
| Samples (deposition time in hours)    | $E^\text{asf}_{\text{gap}}$ (eV) | $E^\text{tail}$ (eV) |
| 6                                     | 3.93   | 1.07   |
| 8                                     | 3.58   | 1.05   |
| 24                                    | 2.52   | 2.32   |

**Results and discussion**

Absorption spectra fitting procedure

In crystalline semiconductors, the following equation has been obtained to relate the absorption coefficient to incident photon energy [16,17]:

$$\alpha(\nu)h\nu = B(h\nu - E^\text{gap})^m.$$  

where $E^\text{gap}$, $B$, and $h\nu$ are the optical gap, constant, and incident photon energy, respectively; $\alpha(\nu)$ is the absorption coefficient defined by the Beer-Lambert’s law as $\alpha(\nu) = \frac{2.303 \times \text{Abs} (\lambda)}{d}$, where $d$ and Abs are the film thickness and film absorbance, respectively. For more precise determination of $\alpha$, it is necessary to perform corrections to the absorption due to reflection; also, $m$ is the index which can have different values of 1/2, 3/2, 2, and 3 [18]. To introduce the absorption spectrum fitting (ASF) method, one can start with Equation 3 and rewrite it as a function of the wavelength ($\lambda$):

$$\alpha(\lambda) = B(hc)^m h \frac{1}{\lambda_g^2} \left(1 - \frac{1}{\lambda^2}ight)^m$$

where $\lambda_g$, $h$, and $c$ are wavelengths corresponding to the optical band gap, Planck’s constant, and velocity
of light, respectively. Using the Beer-Lambert’s law, it is possible to rewrite Equation 4 as follows:

\[
\text{Abs}(\lambda) = B_1 \lambda \left( \frac{1}{\lambda^m} - \frac{1}{\lambda_g^m} \right) + B_2
\]

where \( B_1 = [B(\hbar c/m)^{m-1} \times d/2.303] \) and \( B_2 \) is a constant which take into account the reflection. Using Equation 5, one can calculate the optical band gap by an absorbance spectrum fitting method without any need to the film thickness. Thus the value of band gap, in electron volt, can be calculated from the parameter \( \lambda_g \) using \( E_{\text{gap}} = \frac{1239.83}{\lambda_g} \); in other words, the value of \( \lambda_g \) can be extrapolating the linear of the \( \left( \frac{\text{Abs}(\lambda)}{\lambda} \right)^m \) vs. \( 1/\lambda \) curve at \( (\text{Abs}(\lambda)/\lambda)^2 \) = 0. By using the least squares technique, it was observed that the best fitting occurs for \( m = 1/2 \).

Extrapolating the straight-line portion of the plots shown in Figure 1 to zero \( (\text{Abs}(\lambda)/\lambda)^2 \) gives the corresponding \( E_{\text{gap}} \) (eV) values (Table 1). The dependence of the optical gap on the deposition time for as-deposited thin films is shown in Figure 1 and Table 1. It is obvious that the optical gap is decreased by increasing the deposition time because with increasing deposition time, the size of the particles grows and the energy band gap decreases.

Width of the tail of localized states

It has been suggested that the Urbach’s rule may be used to relate the absorption coefficient to the incident photon energy [12] as

\[
\alpha(\nu) = a_0 \exp\left(\frac{h\nu}{E_{\text{tail}}}\right)
\]

where \( a_0 \) is a constant and \( E_{\text{tail}} \) is width of the tail of localized states (Urbach energy) corresponding to the optical transition between localized states adjacent to the valence band and extended state in the conduction band which is lying above the mobility edge. In ASF procedure, Equation 5 can be written as

\[
\text{Abs}(\lambda) = D_3 \exp\left(\frac{h\nu}{E_{\text{tail}}/\lambda}\right)
\]

where \( D_3 = (a_0 d/2.303) \). Therefore, the values of \( E_{\text{tail}} \) in electron volts, were obtained from the slope of the linear region of the \( \ln(\text{Abs}) - 1/\lambda \) curves using the equation \( E_{\text{tail}} = \frac{1239.83}{\text{slope}} \); the least squares method \((R^2 = 0.9982 – 0.9994)\) was employed to calculate the \( E_{\text{tail}} \) values. Results of these calculations have been presented in Table 1 (see Figure 2). The width of the band tail is increased by increasing of the deposition time (see Table 1). As the deposition time increases, the thin film thickness also increases. The fabricated samples with chemical bath deposition method have a typical characteristic that is composed from nanoparticles and have a natural disorder which is furthermore treated as an amorphous...
semiconductor. Because of this effect, deposition time increases as the width of band tails increases.

**X-ray diffraction analyzing of samples**

X-ray diffraction patterns for CBD-CdSe thin films on the glass substrate are shown in Figure 3. As deposition time is increased, the intensity and the line width of the XRD patterns get higher and smaller, respectively. The obtained results are shown in Table 2. The samples’ X-ray patterns illustrate that the crystal structure of the CBD-CdSe is cubic [15].

**Scanning electron microscopy**

Figure 4 shows the scanning electron microscope (SEM) picture of the 24-h deposition time at pH = 12.1 with magnification $\times$ 30,000. It can be observed that the CdSe thin film covers the substrate. From the picture, it is obviously seen that the film is composed of small, nanosized grains. We cut the sample after the deposition. The substrate and sample images are shown separately.

**Conclusions**

The aim of this paper is to explain how one can determine the energy band gap in nanostructural semiconductors that only requires the measurement of the absorbance spectrum and no additional information is needed, such as the film thickness or reflectance spectra. The cadmium selenide nanoparticle films have been deposited by chemical bath deposition method (CBD). Fabricated nanostructural thin films are composed of small nanosized grains. Using the Tauc model, the absorption spectrum fitting method (ASF) was employed to estimate the optical band gap. Surface atoms in nanostructural semiconductors have a characteristic role. ASF method presents the width of band tail for nanostructural semiconductors.

**Competing interest**

The author declares that he has no competing interest.

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**References**

1. Brus, LE: Quantum crystallites and nonlinear optics. Appl Phys A 53, 465 (1991)
2. Millo, O, Katz, O, Cao, YW, Banin, U: Imaging and spectroscopy of artificial-atom states in core/shell nanocrystal quantum dots. Phys Rev Lett 86, 5751 (2001)
3. Wang, Y, Herron, N: Nanometer-sized semiconductor clusters: materials synthesis, quantum size effects, and photophysical properties. J Phys Chem 95, 525 (1991)
4. Kale, RB, Sartale, SD, Chougule, BK, Lokhande, CD: Growth and characterization of nanocrystalline CdSe thin films deposited by the successive ionic layer adsorption and reaction method. Semicond Sci Technol 19, 980 (2004)
5. Inokuma, T, Arai, T, Ishikawa, M: Size effects on the temporal dynamics of edge emission in CdSe microcrystals embedded in a germanate glass matrix. Phys Rev B 42, 1623 (1990)
6. Greenwood, NN, Earnshaw, EA: Chemistry of the Elements. Pergamon, Oxford (1990)
7. Bawendi, MG, Carolli, PJ, Wilson, WL, Brus, LE: Luminescence properties of cadmium selenide quantum crystallites: resonance between interior and surface localized states. J Phys Chem 96, 1335 (1992)
8. Alivisatos, AP: Semiconductor clusters, nanocrystals, and quantum dots. Science 271, 933 (1996)
9. Brus, LE: A simple model for the ionization potential, electron affinity, and aqueous redox potentials of small semiconductor crystallites. J Chem Phys 79, 5566 (1983)
10. Brus, LE: Electron–electron and electron–hole interactions in small semiconductor crystallites: the size dependence of the lowest excited electronic state. J Chem Phys 84, 4403 (1984)
11. Brus, LE: Electronic wave functions in semiconductor clusters: experiment and theory. J Phys Chem 90, 2655 (1986)
12. Souri, D, Shomalian, K: Band gap determination by absorption spectrum fitting method (ASF) and structural properties of different compositions of (60 – x) V2O5–40TeO2–xSb2O3 glasses. J Non-Cryst Solids 355, 1597–1601 (2009)
13. Alarcon, LE, Arieta, A, Camps, E, Muñoz, F, Nadal, S, Santiago, EV: Comparison and semiconductor properties of nitrogen-doped carbon thin films grown by different techniques. Appl Surf Sci 254, 413 (2007)
14. Mane, RS, Lokhande, CD: Chemical deposition method for metal chalcogenide thin film. Mater Chem Phys 65, 1–31 (2000)
15. Kale, RB, Lokhande, CD: Band gap shift, structural characterization and phase transformation of CdSe thin films from nanocrystalline cubic to nanorod hexagonal on air annealing. Semiconf Sci Technol 20, p1–p9 (2005)
16. Mott, NC, Davis, EA: Electron processes in non-crystalline materials. Clarendon, Oxford (1979)
17. Tauc, J, Ment, A: States in the gap. J Non-Cryst Solids 569, 8–10 (1972)
18. Chopra, N, Mansingh, K, Chudha, GK: Electrical, optical and structural properties of amorphous V2O5–TeO2 blown films. J Non-Cryst Solids 194, 126 (1990)