Constraints on scalar-pseudoscalar and tensorial nonstandard interactions and tensorial unparticle couplings from neutrino-electron scattering

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Neutrino-electron scattering is a purely leptonic fundamental interaction and therefore provides an important channel to test the Standard Model, especially at the low energy-momentum transfer regime. We derived constraints on neutrino nonstandard interaction couplings depending on model-independent approaches which are described by a four-Fermi pointlike interaction and unparticle physics model with tensorial components. Data on $\bar{\nu}_e - e$ and $\nu_e - e$ scattering from the TEXONO and LSND experiments, respectively, are used. The upper limits and the allowed regions of scalar, pseudoscalar, and tensorial nonstandard interaction couplings of neutrinos are derived at 90% confidence level in both one-parameter and two-parameter analysis. New upper limits for tensorial unparticle physics coupling constants and mass parameters are also placed.

I. INTRODUCTION

Neutrinos play crucial roles in particle physics and cosmology. Discovery of neutrino oscillations shows that neutrinos have finite mass. There are intense experimental efforts to study their properties and interactions with matter. Therefore, they are keystones for completeness of the Standard Model (SM) [1]. Solar and atmospheric experimental data have confirmed that neutrinos do oscillate, thereby they are massive and can be mixed. Extra new interactions due to nonstandard properties of neutrinos which are often called nonstandard interactions (NSIs) of a neutrino have not been observed experimentally yet, mainly due to poor experimental sensitivities.

Recent and upcoming neutrino experiments will provide more precise measurements on intrinsic neutrino properties [2], and therefore have the potential to open a new window for the observation of NSI effects [3]. Nonoscillation experiments that have measured a neutrino cross section with high accuracy may provide profound information for neutrino interactions resulting in direct measurements of NSIs. These interactions are important not only for phenomenological [4] but also for the experimental points of view since the measurements and found evidence can suggest new physics or favor one of the existing new physics theories beyond the SM (BSM).

Neutrino-electron scattering provides quite convenient channel for testing the SM of electroweak theory, especially in low-energy regime since it is a pure leptonic process [5–9]. Advanced systems capable of making measurements at low energy and low background are necessary to observe neutrino interactions with good experimental precision. In principle, there are some advantages to studying with reactor neutrinos ($\bar{\nu}_e$): the reactors are excellent sources for a low-energy electron-type antineutrino with high neutrino flux up to around 10 MeV. Besides reactor on and off comparison providing a model-independent way of background subtraction, the reactor $\bar{\nu}_e$ spectra are understood and well known. Therefore, these advantages provide better experimental sensitivities.

This paper is a follow-up of our earlier studies on (i) nonuniversality of flavor-conserving (FC) and flavor-changing or flavor-violating (FV) NSI of neutrino, and (ii) vector and scalar unparticle physics (UP) [6]. We report experimental constraints on scalar, pseudoscalar, and tensorial NSIs and tensorial unparticle couplings via neutrino-electron elastic scattering interaction channels.

II. NEUTRINO-ELECTRON SCATTERING AND DATA

A. Standard Model

$\nu_e(\bar{\nu}_e) - e$ elastic scattering can occur via both charged current and neutral current. Therefore, their interference which is destructive also contributes to the cross section. The SM differential cross section of $\nu_e(\bar{\nu}_e) - e$ elastic scattering can be expressed in terms of the chiral coupling of $g_L$ and $g_R$ in the laboratory frame as [6, 10]

$$\frac{d\sigma}{dT}(\nu_e)_{SM} = \frac{2G_F m_e}{\pi} \left[ (g_L + 1)^2 + g_R^2 \left( 1 - \frac{T}{E^2} \right)^2 \right]$$

and

$$\frac{d\sigma}{dT}(\bar{\nu}_e)_{SM} = \frac{2G_F m_e}{\pi} \left[ g_R^2 + (g_L + 1)^2 \left( 1 - \frac{T}{E^2} \right)^2 \right]$$

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where $G_F$ is the Fermi coupling constant, $T$ is the kinetic energy of the recoil electron, $E_\nu$ is the incident neutrino energy, and $g_L = -\frac{1}{2} + \sin^2 \theta_W$ and $g_R = \sin^2 \theta_W$ are the chiral coupling constants in terms of weak mixing angle $\sin^2 \theta_W$.

**B. Input data**

Short-baseline neutrino experiments provide some advantages to study BSM. Because of the minimizing oscillation effect, short-baseline reactor neutrino experiments, where pure $\bar{\nu}_e$ is produced, unlike the mixing of different eigenstates of neutrinos as in the case of Solar and atmospheric ones, can be used to probe BSM effectively. Reactors produce high $\bar{\nu}_e$ fluxes compared to other sources. The reactor-off period provides a model-independent means of background subtraction. The studies of reactor $\bar{\nu}_e - e$ interaction provide better sensitivities to the SM electroweak parameters $\sin^2 \theta_W$ and $g_\nu, g_\lambda$ at the same experimental accuracies as those from $\nu_e$ measurements [11]. The lower neutrino energy at the MeV range also favors applications where sensitivities can be enhanced at low detector thresholds.

In this paper, the analysis is based on data from: (i) the TEXONO experiment on antineutrino-electron interactions at low energy using three different detectors located at Kuo-Sheng Reactor Neutrino Laboratory (KSNL) and (ii) the LSND experiment on neutrino electron interactions at high energy using accelerator neutrinos. The results from three independent data sets from TEXONO of $\bar{\nu}_e - e$ interaction are compared with those from the data set of LSND $\nu_e - e$ interaction.

KSNL is located at a distance of 28 m from one of the cores of Nuclear Power Plant in Taiwan with 30 m water-equivalent overburden. The 2.9 GW reactor cores are produced an average $\bar{\nu}_e$ flux of $\phi(\bar{\nu}_e) \sim 6.4 \times 10^{12}$ cm$^{-2}$s$^{-1}$ at the experimental site. Detectors has been placed in a shielding structure with 50 ton of passive materials and surrounded by active anti-Compton detectors: CsI(Tl) or NaI(Tl) for the anti-Compton detector, and a cosmic-ray veto scintillator array.

**TEXONO Experiment:** Three experimental data sets with different detectors are used as follows:

- **CsI(Tl):** $-29882/7369$ kg-days of reactor on/off data: $\bar{\nu}_e - e$ electronweak interaction cross section, $g_\nu, g_\lambda$, weak mixing angle $\sin^2 \theta_W$ and charge radius squared were measured with an effective mass of 187 kg CsI(Tl) crystal scintillator array at 3 – 8 MeV. The rms energy resolutions are 5.8%, 5.2%, and 4.0% at $^{137}$Cs, $^{40}$K, and $^{208}$Ti $\gamma$ peaks, respectively [11].

- **HP-Ge:** $-570.7/127.8$ kg-days of reactor on/off data: The limit on the neutrino magnetic moments at 90% C.L. was derived and the constraints on the couplings of axion were placed using a high-purity germanium detector with a target mass of 1.06 kg and measurements at 1264 keV [12]. The rms energy resolution of HP-Ge is 880 keV at Gallium K-shell x-ray energy [13].

**PC-Ge:** $-124.2/70.3$ kg-days of Reactor on/off data: New limits are set to neutrino milli-charge and low-mass weakly interacting massive particles with a fiducial mass of 500 g point contact germanium (PC-Ge) detector [8] in the 0.3 – 12 keV energy region. The rms energy resolution of PC-Ge is 87 keV at Gallium K-shell x-ray energy [13].

**LSND Experiment:** The Liquid Scintillator Detector at the Los Alamos Neutron Science Center uses neutrinos produced at the proton beam stop with $T_e$ of 18 – 50 MeV. The cross section for the elastic scattering reaction $\nu_e - e$ and weak mixing angle $\sin^2 \theta_W$ were measured. The energy resolution was determined from the shape of the electron energy spectrum and was found to be 6.6% at the 52.8 MeV end point [14].

**C. Analysis methods**

FC and FV NSIs, as well as scalar and vector UP were studied in our previous studies by using the data sets of CsI(Tl) and HP-Ge [6]. In this paper, we adopt the same analysis methods for the new interaction channels. A new data set of PC-Ge of TEXONO is also included for the analysis to cover the lower energy range as well.

The expected event rate of $R$ can be calculated as

$$R_X = \rho_e \int_T^{E_e} \left[ \int_{E_\nu} dE_\nu \int_X d\phi(\bar{\nu}_e) \frac{d\phi(dE_\nu)}{dE_\nu} \frac{d\nu_e}{dT} \right] dT,$$

where $\rho_e$ is the electron number density per kilogram of target mass and $d\phi/dE_\nu$ is the neutrino spectrum. The measurable differential cross section is denoted by $[d\sigma/dT]'$, which corresponds to convoluting the detector energy resolution to the physics differential cross section $[d\sigma/dT]$. In practice, for the BSM models and experimental data studied in this work, the variations of $[d\sigma/dT]$ with energy are gradual, such that the resolution smearing does not significantly alter the measured spectra in the region of interest. The difference between $[d\sigma/dT]$ and $[d\sigma/dT]'$ is less than 0.1%. Accordingly, resolution effects can be neglected in this analysis.

$R_{\text{expt}}$ and $R_X$ correspond to observed and expected event rates, respectively. $X$ represents different interaction channels such as the SM, NSI, etc. $R_{\text{expt}}$ is expressed in the unit of kg$^{-1}$MeV$^{-1}$day$^{-1}$ and kg$^{-1}$keV$^{-1}$day$^{-1}$ for CsI(Tl) and Ge data sets, respectively.

The results on physics couplings from this analysis are expressed either as a "best-fit ± statistical ± systematic"
uncertainties” at 1-σ level, or in terms of limits at 90% C.L.. The statistical uncertainties are derived by a minimum $\chi^2$ method defined as

$$
\chi^2 = \sum_{i=1}^{N} \left[ \frac{R_{\text{expt}}(i) - R_{\text{SM}}(i) - R_X(i)}{\Delta(i)} \right]^2,
$$

where $R_{\text{expt}}$, $R_{\text{SM}}$ and $R_X$ are the measured event rate, SM and $X$ (= NSI, UP, etc.) expected event rates, respectively, while $\Delta(i)$ is the statistical uncertainty of the ith bin published by the experiments. The 1-σ statistical errors in the physics couplings correspond to those values that produce $\chi^2 = \chi^2_{\text{min}} + 1$. The published systematic uncertainties of the experiments contribute to shifts of the best-fit values in the physics couplings. The two contributions are added in quadrature to give rise to the combined uncertainties, from which the 90% C.L. limits can be derived using the prescription of Ref. [15].

$$
\frac{\Delta(\nu)}{\text{expt}} = \frac{\Delta(\nu)}{\text{theory}} + \frac{\Delta(\nu)}{\text{stat}}.
$$

Both neutrino oscillation and non-oscillation experiments are sensitive to NSI parameters and can give complementary results. Non-oscillation neutrino experiments provide direct measurement of NSI while neutrino oscillation experiments are more sensitive to propagation of NSI parameters due to matter effects [4]. NSI can simply be considered as a modification of chiral coupling constants of $g_{\nu L,R}$ with additional new physics terms, in general.

Phenomenological studies of FC and FV NSIs of neutrinos have been extensively carried out with a variety of interaction channels and neutrino sources [16–21]. Experimentally new bounds for FC coupling of $\nu_e^{\text{el},L}$ and FV coupling of $\nu_\tau^{\text{el},L}$ were derived and existing bounds were improved in our earlier work by taking advantage of neglecting oscillation effects and high neutrino flux [6]. On the other hand, other NSIs of neutrinos are also possible and are of the scalar, pseudoscalar, and spin-2 tensorial types.

Figure 2. Differential cross section as a function of the recoil energy $T$ with typical reactor $\bar{\nu}_e$ spectra for scalar, pseudoscalar and tensorial NSIs at some specific coupling parameters using CsI(Tl) as a target.

III. SCALAR, PSEUDOSCALAR AND TENSORIAL NSI OF NEUTRINO

Since neutrino-electron scattering is a pure leptonic process, it provides a very convenient channel to test the SM. NSI of neutrinos is first considered as an alternative mechanism for neutrino oscillation. However, NSI is now only allowed for lower pioneers effects to the neutrino oscillation and can be used to improve the sensitivities of oscillation experiments. In this paper, investigation of some of the BSM new physics scenarios via $\nu_e(\bar{\nu}_e)-e$ elastic scattering is introduced and the results will be given in subsequent sections. In these new physics scenarios, the NSI of neutrinos is considered as a model-independent interaction, which is described as a four-Fermi pointlike or so called zero-distance interaction. Feynman diagram of different NSI for neutrino-electron scattering is illustrated schematically in Fig. 1.

![Figure 1. NSIs of neutrinos, generically described as four-Fermi interaction with new couplings.](image-url)
The effective Lagrangian for scalar and/or pseudoscalar interaction [22] can be written as

$$\mathcal{L}_{S,P} = \sum_\alpha \sum_\beta \bar{l}_\alpha (O_{S,P}) \nu_\beta \;,$$  \hspace{1cm} (5)

where $(O_{S,P})$ is a general operator with scalar/pseudoscalar interactions.

The effective Lagrangian for tensorial NSI [23] interaction can be written as

$$\mathcal{L}_{T} = e^{T}_{\alpha\beta} \sqrt{2} G_F (\bar{\nu}_\alpha \sigma^{\mu\nu} \nu_\beta) (\bar{f} \sigma^{\mu\nu} f)$$  \hspace{1cm} (6)

with $\sigma^{\mu\nu} = [\gamma^\mu, \gamma^\nu] = \gamma^\mu \gamma^\nu - \gamma^\nu \gamma^\mu$ and $\alpha, \beta = e, \mu, \tau$.

The differential cross section of scalar-pseudoscalar NSI for $\nu_e - e^-$ and $\bar{\nu}_e - e^-$, respectively, can be written as

$$\left[ \frac{d\sigma_{\nu_e,e}}{dT} \right]_{S,P}^{\text{NSI}} = \frac{2 G_F^2 m_e}{\pi} \left\{ \left( |g_{S,e}^e| + |g_{P,e}^e| \right)^2 + g_R \text{Re} \left( g_{S,e}^e - g_{P,e}^e \right) \right\} \left( 1 - \frac{T}{E_\nu} \right)^2$$

$$- \left( g_L + 1 \right) \text{Re} \left( g_{S,e}^e - g_{P,e}^e \right) \frac{m_e T}{2 E_\nu^2} \right\} \;.$$  \hspace{1cm} (7)

and

$$\left[ \frac{d\sigma_{\bar{\nu}_e,e}}{dT} \right]_{S,P}^{\text{NSI}} = \frac{2 G_F^2 m_e}{\pi} \left\{ \left( |g_{S,e}^e| + |g_{P,e}^e| \right)^2 + g_R \text{Re} \left( g_{S,e}^e - g_{P,e}^e \right) \right\} \left( 1 - \frac{T}{E_\nu} \right)^2$$

$$- \left( g_L + 1 \right) \text{Re} \left( g_{S,e}^e - g_{P,e}^e \right) \frac{m_e T}{2 E_\nu^2} \right\} \;.$$  \hspace{1cm} (8)

The measurable recoil spectra at a typical reactor flux of $\phi(\bar{\nu}_e) = 10^{13}$ cm$^{-2}$s$^{-1}$ are displayed in Fig. 2 for typical scalar, pseudoscalar and tensorial NSI parameters. The spectral shapes of NSI contributions for all types give rise to quite similar to the SM one. Accordingly, like FC and FV NSIs, the most suitable energy range to study scalar, pseudoscalar, and tensorial NSIs is in MeV energy range where the SM effects were measured with good accuracy.

Like the FC and FV NSI parameters, the scalar, pseudoscalar and tensorial NSI parameters [23–25] are also constrained by the accuracy of the SM cross section measurements. Accordingly, only Cal(T) data set for TEXONO and LSND experiments are adopted for scalar, pseudoscalar and tensorial NSI analysis.

The scalar and pseudoscalar NSI parameters $g_{S,P}^e$ given in Eq. (7) and Eq. (8) are the fitting variables in the minimum-$\chi^2$ analysis. If $g_{S}^e = g_{P}^e$ then there will be some simplifications in these equations. In this case $(g_{S,P}^e)^2$ becomes the fitting parameter.

By adopting one-parameter-at-a-time analysis, from the best fit, the contribution of tensorial interaction to the SM cross section should be just added numerically. The differential cross section of tensorial NSI can be written as [10, 23]

$$\left[ \frac{d\sigma}{dT} \right]_{T}^{\text{NSI}} = \frac{2 G_F^2 m_e}{\pi} \sum_{\beta = e, \mu, \tau} \left( \frac{\tilde{\varepsilon}_{e \beta}^T} {2 E_\nu} \right)^2$$

$$- \frac{m_e T}{2 E_\nu^2} \right\} \;.$$  \hspace{1cm} (9)
Figure 3. (a) $\Delta \chi^2$ of one-parameter-at-a-time analysis for $g^{e,e}_S$, $(g^{e,e}_{S,P})^2$, and $(g^{e,e}_T)^2$. The allowed region at 90% C.L. for TEXONO and LSND experiments in (b) $g^{e,e}_S - g^{e,e}_P$, (c) $g^{e,e}_S - (g^{e,e}_T)^2$ and $g^{e,e}_P - (g^{e,e}_T)^2$ parameter spaces. (d) Upper limits at 90% C.L. of $g^{e,e}_T$ as functions of $g^{e,e}_S$ and $g^{e,e}_P$.

\begin{equation}
\begin{align*}
g^{e,e}_S &= [3.27 \pm 6.39 \pm 3.10] \times 10^{-2}, \\
g^{e,e}_P &= [-3.27 \pm 6.39 \pm 3.10] \times 10^{-2}, \\
(g^{e,e}_{S,P})^2 &= [0.19 \pm 0.38 \pm 0.31] \times 10^{-2}, \text{ and} \\
(g^{e,e}_T)^2 &= [0.96 \pm 2.21 \pm 1.82] \times 10^{-2} \\
\end{align*}
\end{equation}

are obtained at $\chi^2_{\text{min}}/\text{dof} = 8.7/9$.

These results are converted to the bounds for the scalar and pseudoscalar NSI couplings as

\begin{equation}
\begin{align*}
-0.317 < g^{e,e}_S < 0.113 \quad \text{(for } g^{e,e}_P = 0), \\
-0.113 < g^{e,e}_P < 0.317 \quad \text{(for } g^{e,e}_S = 0), \\
|g^{e,e}_{S,P}| < 0.100 \quad \text{(for } g^{e,e}_S = g^{e,e}_P) \text{,} \quad \text{and} \\
g^{e,e}_T < 0.238 \quad \text{(for } g^{e,e}_S = g^{e,e}_P = 0) \\
\end{align*}
\end{equation}

at 90% C.L. for TEXONO CsI(Tl) data set.

The best-fit results and $\chi^2$ behaviors of the scalar, pseudoscalar, and tensorial NSI parameters of $g^{e,e}_S$, $(g^{e,e}_{S,P})^2$, and $(g^{e,e}_T)^2$ which are adopted as fitting vari-
ables are illustrated in Fig. 3(a).

Similarly,

\[ g_S^{e,e} = 0.27 \pm 0.59 \pm 0.26, \]
\[ g_P^{e,e} = -0.27 \pm 0.59 \pm 0.26, \]
\[ (g_{S=0}^{e,e})^2 = [3.47 \pm 4.78 \pm 4.36] \times 10^{-2}, \] and
\[ (g_T^{e,e})^2 = [3.96 \pm 5.47 \pm 4.97] \times 10^{-2} \] (12)

are derived for the LSND experiment, and they correspond to the limits of

\[ -0.880 < g_S^{e,e} < 0.642 \] (for \( g_S^{e,e} = 0 \)),
\[ -0.642 < g_P^{e,e} < 0.880 \] (for \( g_P^{e,e} = 0 \)),
\[ |g_{S=0}^{e,e}| < 0.375 \] (for \( g_S^{e,e} = g_P^{e,e} \)), and
\[ g_T^{e,e} < 0.401 \] (for \( g_S^{e,e} = g_P^{e,e} = 0 \)) (13)

at 90 % C.L. which are similar to published results of LAMPF experiment reported in Ref. [26] since their experimental sensitivities are similar.

The results of one-parameter-at-a-time analysis for TEXONO and LSND experiments are listed in Table I. As can be seen, TEXONO CsI(Tl) data set provides much better constraints than those from LSND or LAMPF accelerator experiments and also from the other reactor neutrino experiment data sets given in Ref. [23].

The allowed regions at 90% C.L. from two-parameter analysis in the \([g_{S,L}^{e,e}, (g_{S,L}^{e,e})^2]\) parameter spaces are displayed in Fig. 3 in which LSND results are superimposed for complementarity. The 90% CL upper limits of \(g_{P,T}^{e,e}\) as functions of \(g_S^{e,e}\) and \(g_T^{e,e}\) for the two experiments are displayed in Fig. 3(d). It can be seen that the TEXONO data provide more stringent constraints than those from LSND in both the \(g_S^{e,e} - g_P^{e,e}\) and \(g_S^{e,e} - g_T^{e,e}\) parameter spaces.

![Figure 4](image)

**Figure 4.** Interactions of a neutrino with an electron via exchange of massive mediators such as a virtual unparticle (scalar \(U_S\), vector \(U_V\), or tensorial \(U_T\)).

**IV. UNPARTICLE PHYSICS**

Unparticle physics was first presented by Georgi with two articles in 2007. Besides SM fields, a sector is assumed to be scale invariant at high energies. These fields are called Banks-Zaks (BZ) fields. In this model SM fields interact with BZ fields by an exchange of mass scale-invariant massive particles that are called unparticles [27, 28].

The effective Lagrangian is given by [23, 29]

\[ \mathcal{L}_U = C_{\mathcal{O}_U} \sum_{i=d_{BZ}} d_{BU}^{U,SM+d_{BZ}} \mathcal{O}_{SM} \mathcal{O}_U, \] (14)

where \(\mathcal{O}_U\) is the unparticle operator of scaling dimension \(d_u\) in the low-energy limit and \(C_{\mathcal{O}_{U}}\) is the dimensionless coupling constant. The unparticle operator can be a scalar, vector, spinor, or tensor type.

The unparticle can directly be studied in accelerator experiments via investigating missing energy signals in the detection channel [30], but alternatively its effect can also be examined in the neutrino-electron elastic scattering channel as being a virtual mediator particle. The latter approach is adopted in this analysis using reactor neutrinos as probes. Scalar and vector UPS for both FV and FC UP cases [6], and for tensorial UPS at a value of \((d_T, \lambda_2)\) (this work). The relevant energy ranges of the three data sets used in the present analysis are also shown.

![Figure 5](image)

**Figure 5.** Differential cross section as a function of the recoil energy \(T\) with typical reaction \(e + e\) spectra for scalar UPS at two values of \((d_S, \lambda_0)\), for vector UPS at a value of \((d_V, \lambda_1)\) for both FV and FC UP cases [6], and for tensorial UPS at a value of \((d_T, \lambda_2)\) (this work). The relevant energy ranges of the three data sets used in the present analysis are also shown.
The coupling $\lambda_2$ vs mass dimension $d_{T}$ at $\Lambda_U = 1$ TeV for the three data sets adopted for this analysis in which the long-range force result is superimposed for comparison. (b) Upper bounds on $\lambda_2$ at different energy scales $\Lambda_U$. The space above the lines is excluded.

The cross section of $\bar{\nu}_e - e$ scattering via tensorial UP exchange is given by \cite{23}

$$\frac{d\sigma}{dT} = \frac{f^2(d_T)}{\pi \lambda_{U}^{d_{T}-4}} \frac{m_{e}^{2d_{T}-3}}{T^{2d_{T}-4}} \left[ 3 \left( 1 - \frac{T}{2E_{\nu}} \right)^2 - m_{e}T \right],$$

where

$$f(d_X) = \frac{\lambda_X^2}{2\sin(d_X \pi)} A(d_X)$$

and the normalization constant $A(d_X)$ is given by

$$A(d_X) = \frac{16\pi^{5/2}}{(2\pi)^{2d_{X}}} \frac{\Gamma(d_X + 1/2)}{\Gamma(d_X - 1)\Gamma(2d_{X})}.$$

The cross section of $\bar{\nu}_e - e$ scattering via all kinds of UP exchange can be obtained by making a replacement of $d_{X} \rightarrow d_{S}, d_{V}$, or $d_{T}$ and $\lambda_X \rightarrow \lambda_0, \lambda_1$, or $\lambda_2$ representing scalar, vector, and tensorial UP interactions, respectively.

The differential cross sections of scalar, both FC and FV vector- and tensor-type UP interactions at a typical mass dimension of $d$ using TEXONO CsI(Tl), HP-Ge, and PC-Ge detector data sets are displayed in Fig. 5, where the SM contribution is superimposed for comparison. The sawtooth structures for $T \lesssim 1$ keV are due to suppression by the atomic binding energy \cite{8, 36}. As illustrated in the figure the cross sections of different UP type give different behavior with respect to the recoil energy.

As are the cases of both FC and FV vector UPs, studies in the high energy regime offer greater advantage than those at low energy for both tensorial UPs and scalar UPs with higher mass dimension of $d$. On the other hand, the low-energy regime is more favorable for scalar UPs with low mass dimension of $d$. Since the cross sections of the SM are measured more precisely in the MeV energy range, more sensitive results are expected for tensorial UPs with the CsI(Tl) detector data set compared to those from Ge detector data sets. Since different ranges of $d_{T}$ for all the data sets listed above give different and comparable sensitivities, all the three data sets of $\bar{\nu}_e - e$ are used in the tensorial UP analysis for their complementarity.

Three parameters, unparticle mass dimension $d_{T}$, unparticle energy scale $\Lambda_U$ and coupling constant $\lambda_2 = \sqrt{\lambda_{2s}^{2s} \lambda_{2e}^{2e}}$ characterizing the unparticle interactions can be probed experimentally. There is a bound on $d_{T}$ as $d_{T} \geq 2$ for the antisymmetric tensor and $d_{T} \geq 4$ for the symmetric case \cite{37}. The UP energy scale is taken to be $\Lambda_U \sim 1$ TeV as in most recent works \cite{32, 33, 38} as well as $\Lambda_U$ up to 10 TeV.

Constraints on $\lambda_2$ at different $d_{T}$ in the case of tensorial UP exchange interaction are derived at $\Lambda_U = 1$ TeV. The results are shown in Fig. 6(a), in which a long-range force result reported in Ref. \cite{33} is superimposed for comparison.

To observe the UP signal from the data and to set bounds on it, among the investigations of the
collider, CP-violation, deep-inelastic, lepton flavor-violating, hadron mixing and decay, neutrino interaction, nucleon decay experiments, and cosmological and astroparticle efforts, there is another unparticle approach that involves long-range forces operating at macroscopic distances and governed by a nonlinear power law, which was first introduced in Ref. [39]. It is based on spin-dependent interactions between electrons and related to the Newtonian gravitational inverse squared law mediated by a tensorlike ungravity interaction [40].

The upper bounds for $\lambda_2$ at different energy scale $\Lambda_T$ up to 10 TeV are shown in Fig. 6(b). As can be seen, the limits are improved by the TEXONO CsI(Tl) data set for $d_T > 2.04$, and CsI(Tl) gives rise to more stringent limits at larger $d_T$.

Since $(d\sigma/dT)_{UT}$ is proportional to $\lambda_2^2$, which can be seen from Eq. (16), the potential of placing more severe constraints on the coupling constants due to improved experimental sensitivities can only be modest. When the measurements of CsI(Tl) or sub-keV Ge can achieve 1% precision, an improvement by a factor of 3 can be expected for the sensitivity of $\lambda_2$ [6, 7, 41].

V. SUMMARY AND PROSPECTS

In summary of this article, some of the model-independent BSM new physics scenarios such as scalar, pseudoscalar, and tensorial NSIs and the tensorial component of unparticle physics are discussed. The investigation on the neutrino oscillation phenomena enter the high precision era. Therefore, the existence and contribution of NSIs would help to increase the precision of the experiments.

The experimental results of upper bounds for NSIs using data from the analysis of $\bar{\nu}_e - e$ and $\nu_e - e$ elastic scattering interaction cross section measurements are placed in the framework of these BSM scenarios and the existing experimental sensitivities are improved. We have found new constraints on the relevant parameters that are more stringent than previous laboratory constraints.

Indeed, TEXONO provides better sensitivity in NSI parameter space compared to the LSND experiment; therefore, combined results will improve the existing bounds. Moreover, with this study we extend the parameter space as well by covering the low-mass dimension of $d$ in UP physics studies.

A new research avenue to investigate BSM theories can be opened via the studies of $\bar{\nu}_e$-nucleus coherent scattering. This is one of the themes of the on-going TEXONO low-energy neutrino physics programs.

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