How to turn a scripting language into a domain specific language for computer algebra

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Abstract
We have developed two computer algebra systems, meditor [9] and JAS [12]. These CAS systems are available as Java libraries. For the use-case of interactively entering and manipulating mathematical expressions, there is a need of a scripting front-end for our libraries. Most other CAS invent and implement their own scripting interface for this purpose. We, however, do not want to reinvent the wheel and propose to use a contemporary scripting language with access to Java code. In this paper we discuss the requirements for a scripting language in computer algebra and check whether the languages Python, Ruby, Groovy and Scala meet these requirements. We conclude that, with minor problems, any of these languages is suitable for our purpose.

1 Introduction
In this paper we summarize the numerous discussions that resulted from our encounter as developers of two computer algebra systems (CAS) written in Java [9, 12] that have grown independently during the past 7 years (roughly). The focus of this paper is the scripting requirements for a computer algebra system. We compare various design choices and solutions and conclude that modern scripting languages are suitable for our tasks. We first give some background information on computer algebra systems design and discuss the scripting requirements in section 2. In section 3 we investigate whether modern scripting languages are suitable for our tasks. In the next section we give an overview of the state of our software and then conclude with our findings. Although we focus on computer algebra the topic of this paper is relevant to all kinds of interactive scientific software which want to allow users to input mathematical expressions.

After the construction of the first mature programming languages, like FORTRAN or later C, thousands of program libraries have been developed. More-
over, the popularity of a programming language is often based on the portfolio of available algorithms in the programming libraries. The quality and extent of the library is considered so important, for example for current scripting languages like Perl, PHP or Ruby, that these come with built-in support for online access and easy installation of new program modules by means of CPAN, Pear or Gem facilities. Also Java’s success is influenced by its standardized and comprehensive libraries on which every programmer can depend when writing and deploying their own programs.

In computer algebra the situation is quite different. Java was the first programming language to encompass the requirements for the implementation of algebraic algorithms in their full diversity: interfaces for the specification of algebraic structures and dynamic data-structures with run-time support for it (for example garbage collection). Of course, Lisp allows dynamic data-structures, but because of its sloppy typing system, it seems unsuitable for a CAS library. Second, the user-interface requirements for writing down arbitrary expressions in the desired algebraic structures hinder the success of algebraic libraries. Most computer algebra software has some form of an algebraic expression language with an interpreter and some GUI support to edit and transform the expressions. Actual programming languages (like Java) cannot fulfill these requirements, the construction of elements of algebraic structures, although possible, is tedious and far away from the paper-and-pencil form of expressions.

As we have shown with JSCL and JAS, the first aspect of algebraic libraries has been solved for Java, others have established libraries in C++, like GiNaC [4]. For the second point the situation is only slowly changing. Improvements are seen around scripting languages, notably the Python language was the first to demonstrate facilities to allow the nearly paper-and-pencil form of expressions to be entered [2][20]. In this paper, we investigate current scripting languages for their suitability for the user interface requirements of computer algebra systems. We do not discuss issues around graphical user interfaces and editor components for computer algebra.

1.1 Algebraic libraries

Historically, computers were first built to automate numerical tasks. Since then, numerous attempts were made to supplement these with some symbolic capabilities. The language of choice for that purpose, as inferred from the resulting products [5], is either C (Mathematica, Maple) or LISP (Macsyma/Maxima, Axiom, Reduce). There are attempts in C++ (MuPAD), but they are not as advanced. Despite the advantages of object oriented programming, programmers working in natural science (for example physics) object against using OOP. One reason is the perceived better performance of procedural languages, say FORTRAN. Another reason is that there exist large well tested libraries, developed over decades, which would have to be recoded in an OOP language. So we see OOP code mainly in new developments or as ‘glue’ code to tie together legacy codes. In computer algebra there is not much published on object oriented algorithm implementation. There is a first paper on CAS with SmallTalk [1]
and the ongoing work of the Axiom developers can, to some extent, be viewed as object oriented [8]. Newer approaches start with [23] in Common Lisp, then using C++ [4, 18]. Approaches using Java are [16, 17, 21] and [19, 9, 12, 13, 14].

1.2 Scripting languages

In parallel to the aforementioned symbolic packages, a means for user interaction was also researched, which resulted in the widely adopted form of the command line interface (CLI). Some projects however left the concern aside, and centered on library development alone. In that respect, GiNaC for instance can not be used interactively. It can only be called from other programs, which is a bit frustrating. Command line interfaces on the other hand usually come with a corollary scripting capability (interpreter).

The latter is often used in turn to develop higher-level extension libraries. The drawback to this approach is that the system ends up being developed in two (or more) different languages, one being usually a general purpose, compiled language, for the kernel and core libraries, and the other(s) (an) interpreted, domain specific, language(s), for the extensions. As a result, there are as many different, obviously incompatible extension languages for algebra, as there are products.

Hence today, computer algebra systems universally resort in some extent to domain specific languages (DSL). This is unfortunate, because it implies the additional burden of setting up a whole grammar, parsing mechanisms, etc. Even in projects like Xcas/Giac [18] that seek to eliminate a specific language for extensions, leveraging the features of the host language instead (operator overloading etc.) there is the need for parsing user input.

An attempt to counter the multiplication of extension languages is made by the Sage project [20], which aims to unite several libraries in the fold of one scripting interface. But there is still the dichotomy between the script, which is Python, and the various pieces of (compiled) code. As a matter of fact, there are plans to rewrite the engine in Python [2].

The Java platform could bring a solution based on its scripting framework (JSR-223): one could take one of its existing, widely used, general purpose scripting languages to handle user inputs. As it happens, there are increasingly many available: Beanshell, Rhino, Jython, JRuby, Groovy, Jaskell (for Python, Ruby, Groovy and Scala see [7, 22, 6, 15]). Beanshell is used by meditor. JAS on its hand uses Jython.

2 Desired language features for computer algebra

The interactive use of a CAS mainly consists of entering algebraic expressions and calling methods to compute a desired result or to transform the expressions to some other forms. For example in algebraic geometry one could want to enter
Here, \( f \) and \( g \) are variables, which get assigned polynomial literals. A list \( F \) is constructed from the polynomials and a Gröbner base \( G \) is computed. From these parts, ideals \( I \), \( J \) are constructed and an ideal intersection \( K \) is computed.

In this example the first two lines are the greatest problem for the scripting language. The remaining lines can easily be achieved in almost any scripting language, perhaps with some different ‘syntactic sugar’. The first problem with polynomial literals (or similar expressions) comes from the use of variables \( x \), \( y \) and \( z \) which have no assigned value and no definition in the history of the script execution. The second problem is the use of language operators like \( * \), \( + \) or \( ** \) on a mixture of number literals and variable literals. A third problem arises from the use of operators like \( / \) in \( 5/9 \) on number literals which is ambiguous, as it is not clear if we mean integer division, floating point division or even creation of rational numbers. Finally the software must understand that \( f \) is a polynomial in the ring \( \mathbb{Q}[x, y, z] \) and \( g \) is a polynomial in the ring \( \mathbb{Z}[w, x, z] \), and eventually that \( F \) must be a subset of the ring \( \mathbb{Q}[w, x, y, z] \). Subsequent computations would then take place in the last ring.

In the rest of this section we study the requirements on a scripting language which arise from such computations: the definition of symbols (variable literals), operator usage and coercions.

### 2.1 Definition of symbols

An important need relates to syntax. Writing polynomials natively (without quotes) in usual notation, like \( 1+x+2*x^2 \), is a must for computer algebra. Currently, not many languages can do that acceptably. A symbol like \( x \) here will be an object in the sense of OOP. In \([2]\) for instance it is declared as follows:

```python
>>> from sympy import *
>>> x, y = symbols('x', 'y')
```

This initializes the language variables ‘\( x \)’ and ‘\( y \)’ to objects of class `Symbol`. Additionally all single letter variables and some greek letter names are pre-defined during SymPy initialization. Note, however, there is no way to avoid self-confusion if one later assigns it to a variable with different name.

```python
>>> z = x
```

Now ‘\( z \)’ points to a symbol with name ‘\( x \)’. In Sage \([20]\) a polynomial ring declaration and polynomial expression is made as:
We see that, contrary to SymPy, Sage needs the ring to be known before variables are instantiated. We envision the same kind of declaration as in these two projects.

Hence, in conjunction with the next point ‘operator overloading’ we will be able to build expressions from number literals, symbols, function names and operators. These expressions will in turn be able to be used in further arithmetic constructs, converted to other types, and so on.

2.2 Operator overloading

We want to use operator overloading to emulate the way arithmetic operators act on numeric types, this time for symbolic types. In a scripting language, it is required in two places. First, in expressions containing symbols, the evaluation must be suppressed when an operator encounters a symbol as operand. Second, when expressions contain (sub-)expressions involving objects form the Java libraries, the operation must use the respective class methods.

For example in $2\times3+x$, the ‘+’ operation may not try to operate on symbol ‘x’, but $2\times3$ should be evaluated and simplified to 6. Or, if $f$ and $g$ are of type MultivariatePolynomial, an expression like $f-g$ should use the subtract() method of the respective class and simplify the expression to $f.subtract(g)$.

How exactly operator overloading must be implemented is debated. There are different levels of language support, depending on whether it can be customized, what operators can be used, and so on. There is also the problem of precedence.

Java has limited support for operator overloading: ‘+’ is used both for numeric types and Strings. Some proposed changes to the JDK consist in extending it to BigInteger and BigDecimal (as in Groovy), or to a new interface (e.g. Arithmetic) that would be implemented by java.math.* and any other user defined classes like Complex, Matrix, and so on.

An important problem relates to the use of ‘^’ for pow. Because of the legacy of C, where it is used for exclusive or, nearly all modern language have the atavism of not being able to use it for this purpose. Even when it can be overloaded, it doesn’t have correct precedence.

There is a similar problem regarding rationals, like $1/2$ which is evaluated to 0 in many existing languages. Or even worse, the standard behavior of $/$ is redefined to mean floating point division and to return 0.5.

2.3 Conversions / Coercions

Suppose we have to find an implementation for an operator on incompatible algebraic types. In Perl, the operator would force the operands to be converted as required. In strongly typed object oriented languages we face a problem. In the Java library code we simply require all types to be defined at compile
time, but in the interpretation of a script this seems overly restrictive. During script execution there should be an attempt to find an algebraic structure where the operands can be embedded into and the operator has a meaningful implementation.

In Axiom [8], if no information is given, then first the most general type of the two operand expressions is searched. Then both expressions are transformed to this ‘bigger’ type and then the method is called. So for the polynomial ring \( K[x] \) as a set: it contains \( x \) and also all elements of \( K \). For \( 1 + x \) the system would deduce that 1 is in \( K \) and that the bigger set which also contains \( x \) is then \( K[x] \).

This is difficult to deduce from object oriented expressions. For the expression \( 1.add(x) \) one must find out that the result is in \( K[x] \), represented by some object, say \( \text{univPolyX} \) and rewrite the expression to \( \text{univPolyX.valueOf}(1).add(\text{univPolyX.valueOf}(x)) \). In a similar way one could handle \( x + y \) as \( x.add(y) \) and rewrite it to \( \text{polyXY.valueOf}(x).add(\text{polyXY.valueOf}(y)) \). The latter supposes among other things that the variable names are at hand.

A different approach would defer the evaluation of the expression \( 1.add(x) \) until more type information is available or provided by the user. Also Axiom has a notation to explicitly request a type for an expression and Sage is going the same way in requesting the specification of a polynomial ring before objects from the ring are entered in expressions, as we have noted (section 2.1).

We must pay special attention to the case where one or the other operand is of a numeric type. The statement \( a+b \) will be internally translated into either \( a.add(b) \), which is a unary instance call, or \( add(a,b) \), which is a binary static call, depending on how operator overloading is implemented. In the first option, there is a problem when \( a \), which is called the ‘target’, is numeric, that is, a primitive type and not a true object. Then we must either have it converted, if possible implicitly, to a reference type, which additionally must be able to be overloaded, or to swap it with \( b \), which is called the ‘argument’, putatively a reference type here. The latter mechanism is called ‘double dispatch’.

3 Assessment of scripting languages

With the list of requirements from section 2 we now examine whether modern scripting languages (see figure 1 for a genealogy) can be used to implement a scripting front-end to a CAS. We focus on languages which have an implementation which can access Java library code, such as Python with Jython [7, 11], Ruby with JRuby [22, 10] and the systems Groovy [6], Scala [15] which are directly implemented with Java code access.

The scripting language moreover must support some kind of strong typing, as otherwise objects or methods from the back-end Java libraries of the wrong type could be used. Strong typing means that constructed objects have types which define the allowed methods of the object. Using undefined methods or parameters with wrong types is considered a type error and an exception is thrown.
Figure 1: Genealogy of scripting languages
There are more issues to consider when selecting a scripting language, such as performance, availability, graphical user interface capabilities or size of their community. We do not compare the languages with respect to these issues in this paper.

In order to compare the different languages, we define a toy application that tries to capture the key issues of a real CAS implementation. We try to setup classes, so that we can print the expression ‘1+x’ from the previous section, with only declaring ‘x’ to be a symbol, like ‘x = Sym(‘x’).’

The main classes in the following examples are a Sym class representing symbols and an Expr class representing arbitrary expressions. In both classes we let the + operator return an Expr. For Sym, the ‘to string’ method returns the string name of the symbol and for Expr the ‘to string’ method returns the concatenation of the left and right operands with the operator in the middle. The other operators *, -, / etc. can then be implemented similarly. For function representation, such as sin(x) we will use a Func class, which holds the name of the function and expressions of all arguments.

3.1 Python

The code of Expr and Sym for Python follows. The method __add__ is called when the interpreter encounters a + operation on symbols or expressions. __radd__ interchanges (reverses) the operands of +. The __str__ method is like Java’s toString() and __init__ is Python’s constructor method.

```python
class Expr:
    def __init__(self,left,op,right):
        self.left=left
        self.op=op
        self.right=right
    def __add__(self,other):
        return Expr(self,'+',other)
    def __radd__(self,other):
        return Expr(other,'+',self)
    def __str__(self):
        return str(self.left)+'+'+str(self.right)

class Sym:
    def __init__(self,name):
        self.name=name
    def __add__(self,other):
        return Expr(self,'+',other)
    def __radd__(self,other):
        return Expr(other,'+',self)
    def __str__(self):
```

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return str(self.name)

print(1+2) # --> 3
x=Sym('x'); y=Sym('y')
print(1+x) # --> 1+x
print(x+y) # --> x+y

In this sample, we instantiate two arithmetic objects, we add them, and we print the result. This is the way real world objects like polynomial or matrix would behave in our envisioned setting. We see that the operator overloading implementation is perfectly suited to our purpose (\_\_add\_\_ method). Regarding what happens if the target is numerical, Python uses double-dispatch (\_\_radd\_\_ method).

Regarding the power issue, Python uses **. The Sage crew have addressed the problem by preparsing the input to convert from ^ to **.

For fractions, there has been talk in the Python community about changing Python so 2/3 returns the floating point number 0.6666..., and making 2//3 return 0, which is of no use as far as computer algebra is concerned.

### 3.2 Ruby

The Ruby language and its interpreter is capable of redefining built-in classes and implementing methods for coercion between classes. In Ruby, numbers are objects, so 1+2 is an abbreviation of 1.+2. 1.class returns Fixnum, and + is a valid method name, which can be overridden (not overloaded).

```ruby
class Expr
  def initialize(left,op,right)
    @left=left; @op=op; @right=right
  end
  def +(other)
    Expr.new(self,'+',other)
  end
  def coerce(other)
    [Num.new(other),self]
  end
  def to_s
    "#{@left}#{@op}#{@right}"
  end
  attr_reader :left, :op, :right
end

class Sym
  def initialize(name)
    @name=name
  end
```

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def +(other)
    Expr.new(self,'+',other)
end

def coerce(other)
    [Num.new(other),self]
end

def to_s
    "#{@name}"
end
attr_reader :name
end

class Num
    def initialize(value)
        @value=value
    end
    def +(other)
        Expr.new(self.value,'+',other)
    end
    attr_reader :value
end

puts 1+2  # -> 3
x = Sym.new('x'); y = Sym.new('y')
puts 1+x  # -> 1+x
puts x+y  # -> x+y

When Ruby encounters an expression like 1+x and cannot find a suitable method to add a Sym to a Fixnum it calls a method coerce(1) on the Sym object. If we implement coerce as wrapping Fixnum in class Num, which is aware of our expression tree, we get the desired effect. This is sort of a mix between Python’s __radd__ and Scala’s implicit conversion (see below). The resulting expression tree can then be printed via its to_s() methods or be transformed in any desired way. The method initialize() is the constructor method. @name denotes instance variables and #{@left} denotes substitution of the variable @left in a string.

Instead of using the coerce method we could also extend the built-in class Fixnum with the following implementation.

class Fixnum
    alias plus_old +
    def +(other)
        if other.class == Sym or other.class == Expr
            Expr.new(self,'+',other)
        else
            self.plus_old(other)
        end
    end
end
In this case we redefine the method +() of the built-in class Fixnum to respect our new symbol and expression classes Sym and Expr. If +() encounters one of them, it constructs a new Expr node. The old meaning of + is remembered as an alias, plus_old, and is called on Fixnums. The other classes where + must be overridden are Bignum, Rational, Float, BigDecimal and Complex.

Lastly, regarding the fraction problem, Ruby defines ‘/’ to mean construction of a rational number when the module ‘rational’ is loaded.

### 3.3 Groovy

In Groovy, the method plus() is called when the interpreter encounters a + operation.

```groovy
class Expr {
    Object left
    String op
    Object right
    Expr plus(Object other) {
        return new Expr(left:this,op:"+",right:other)
    }
    String toString() {
        return left.toString()+op+right.toString()
    }
}

class Sym {
    String name
    Expr plus(Object other) {
        return new Expr(left:this,op:"+",right:other)
    }
    String toString() {
        return name
    }
}

class Arithmetic {
    static Expr plus(Integer a, Object b) {
        return new Expr(left:a,op:"+",right:b)
    }
}

use(Arithmetic) {

```
println(1+2) // -> 3
x = new Sym(name:"x"); y = new Sym(name:"y")
println(1+x) // -> 1+x
println(x+y) // -> x+y
}

In this language, numbers are objects, so `1.class` returns `java.lang.Integer` and `1+2` is a shortcut of `1.plus(2)`. If we want the second operand to be non-numerical, we have to resort to the `use(Classname)` construct, as is done in [3]. `Arithmetic` is a so called 'category class', a class with only static method definitions. Within the `use` block the interpreter uses the method `plus` from `Arithmetic` when a `+` operation on numbers and `Objects` is encountered.

Another option in Groovy is to use the ‘ExpandoMetaClass’ construct:

```java
Integer.metaClass.plus = {
  Integer other -> delegate-(-other)
}

Integer.metaClass.plus = {
  Object other -> new Expr(left:delegate,op:"+",right:other)
}
```

This avoids the ‘use’ block. Here we have used a subtract operator trick, but in a real implementation it would require to re-implement original operators in low-level java.

Regarding the fraction issue, Groovy computes `1/2` as a float `0.5`. It also computes a BigInteger to some power as BigDecimal `2G**200 -> 1.6069380442589903E60`. Obviously these choices were made with no symbolic or algebraic computation concern (though the suffix `G` for BigInteger literals could be useful). It is however possible to overload the `div` operator as seen above, so that `1/2` does what we want.

### 3.4 Scala

In Scala, `+` is a valid method name, so it is used to define the addition of objects. Here is how the sample is coded in Scala:

```scala
class Expr(left:Any,op:String,right:Any) {
  def +(other:Any)=new Expr(this,"+",other)
  override def toString=left+op+right
}

class Sym(name:String) {
  def +(other:Any)=new Expr(this,"+",other)
  override def toString=name
}```
class Num(value:Int) {
    def +(other:Any)=new Expr(value,"+",other)
}

implicit def int2num(n: Int): Num = new Num(n)

println(1+2) // -> 3
val (x,y) = (new Sym("x"),new Sym("y"))
println(1+x) // -> 1+x
println(x+y) // -> x+y

To be able to mix numeric operands, we have to use the ‘view’ mechanism
(implicit keyword) which is a generalization of auto-(un)boxing in Java. Based
on this mechanism the expression 1+x will be rewritten as int2num(1)+x.

Regarding the power issue, ** has a wrong precedence (same as *, based on
the first character), and the only possible single ASCII character are ? and \
which shows that computer algebra was not taken into account in the design
of the language (until now). Unicode can be used though, which would allow
special chars as ‘up arrow’ (and the Greek alphabet, but this is a different
matter).

Regarding the fractions, they could be handled with the 1%%2 syntax, with
%% an operator on a symbolic type, which would return a Frac(1,2) object for
instance.

4 State of current software and future work

In the designs of our computer algebra systems, meditor and JAS, we have
been using Beanshell and Jython as scripting front-ends to the algebraic Java
libraries.

With Jython, we provided the scripting classes Ring and Ideal. Ring is an
interface to the Java class GenPolynomialRing. Its string constructor is passed
to a Java string tokenizer, which returns a polynomial ring object. Given the
ring object, it is possible to construct a polynomial ideal Ideal in this ring from
a string representation, also via a Java string tokenizer. So the example from
section 2 reads in JAS as:

jas> r = Ring("Q(w,x,y,z) G")
jas> I = r.ideal("( (x**3 y + x**2 z - 5/9),\n(y**4 - z**6 + 7 w) )" )
jas> I = I.GB(); J ...
jas> K = I.intersect( J )

Regarding meditor, the advantage of Beanshell is that its syntax is almost
identical to Java. This is also its drawback since it lacks the features that we
have discussed. The way that meditor deals with the example is as follows:
In both programs, polynomials are represented as strings instead of expressions in the host language. Parsers had to be implemented and maintained and have fewer possibilities to spot errors in the denotation of polynomials. This is very rudimentary compared to the possibilities of the scripting languages investigated in this paper.

Note, with our custom parsers we could allow the multiplication operator ‘*’ to be optional, which seems to be impossible with scripting languages.

For future development we have to decide whether we follow the ‘nested expression’ approach (based on class Expr) used in our toy sample code or if we implement the nested expression in our back-end Java libraries or if we directly use suitable existing polynomial classes from the library. That is, instead of defining new classes Sym and Expr in our scripting language we could reuse existing Java classes like Expression, or PolynomialRing or implement classes similar to Sym and Expr directly in Java.

The Expression class of meditor is a kind of polynomial capable of extending variables dynamically, so it could directly be substituted for Expr. For JAS, there are only fixed variable number polynomials GenPolynomial which need a polynomial ring factory before any of them can be created. In this case we can implement collectSymbols(expr) and mostGeneralNumberType(expr) methods which will give a list of all symbols occurring in an expression and the maximal type for the coefficients. With this we can implement a polynomial or ring constructor, as in:

```
cas> r = PolynomialRing( [ expr, ... ] )
cas> p = Polynomial( expr )
```

Alternatively, we could define the algebraic structure by hand and use a factory method, like valueOf(), to coerce expressions to the desired type:

```
cas> r = PolynomialRing(Q,'w,x,y,z')
cas> F = [ r.valueOf(f), r.valueOf(g) ]
```

We will investigate these issues in future implementation studies with any of the scripting languages. As a side condition we will try to maintain some kind of compatibility with SymPy and Sage.
5 Conclusion

For the interactive use of our computer algebra systems there is a need of a scripting front-end for the Java libraries. We propose to use a contemporary scripting language with access to Java code. The requirements for a scripting language in computer algebra is to be able to define symbols, override arithmetic operators and the ability to extend built-in classes. The languages Python, Ruby, Groovy and Scala have been selected because they all can call Java library code and are strongly typed.

Working with simplified toy code we showed how to implement the required features. All languages can define symbols and can override arithmetic operators.

With Python one can define arithmetic operators with reversed arguments to meet our requirements. So we can achieve our goals with the least effort. We only have to implement \texttt{\_\_r\_\_} methods for all classes we want to interact with.

Ruby can use explicit coercion methods for all kinds of unknown methods for built-in number classes. So to achieve our goals we have to implement an expression tree aware wrapper class for numbers and to implement \texttt{coerce()} methods for our new expression tree classes. Alternatively Ruby can extend built-in classes to add new methods or override existing methods.

Groovy can specify a context where an arithmetic operator is used with a desired implementation. Since a context requires to be enclosed in braces, users would have to type a closing brace before the code could be interpreted. Alternatively, build-in classes can be extended, but this requires a re-implementation of original operators in low-level java. To reach our goals we have to implement overloaded methods for all classes we want to interact with.

In Scala we can define global methods to achieve desired object coercions (transformations) to our data types. Scala’s view mechanism detects a missing connection and finds the global method according to the required method signature. So to reach our goals we have to implement global coercion methods for all classes we want to interact with. Most of the work is then done via implicit conversion.

The extension of built-in classes may add a performance penalty compared to context specific overriding, which we have not studied.

To conclude, with minor problems any of these languages is suitable for our purpose.

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