Measurement of the top quark pair production cross section in the lepton+jets channel in proton-antiproton collisions at $\sqrt{s}=1.96$ TeV

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We present a measurement of the inclusive top quark pair production cross section in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV utilizing data corresponding to an integrated luminosity of 5.3 fb$^{-1}$ collected with the D0 detector at the Fermilab Tevatron Collider. We consider final states containing one high-$p_T$ isolated electron or muon and at least two jets, and we perform three analyses: one exploiting specific kinematic features of $t\bar{t}$ events, the second using $b$-jet identification, and the third using both $t\bar{t}$-jet identification, and the third using both.

Assuming a top quark mass of 172.5 GeV, we obtain $\sigma_{t\bar{t}} = 7.78^{+0.77}_{-0.64}$ pb. This result agrees with predictions of the standard model.

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I. INTRODUCTION

The inclusive $t\bar{t}$ production cross section ($\sigma_{t\bar{t}}$) is predicted in the standard model (SM) with a precision of 6% to 8% [1–5]. Due to the large mass of the top quark, many models of physics beyond the SM predict observable effects in the top quark sector which can affect the top quark production rate. For example, the decay of a top quark into a charged Higgs boson and a $b$ quark ($t \to H^+ b$) would affect the value of $\sigma_{t\bar{t}}$ extracted from different final states [6–8]. In the SM, the top quark decays with almost 100% probability into a $W$ boson and a $b$ quark.

In this article, we present a new measurement of the inclusive top quark production cross section in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV in the lepton+jets ($ell$+jets) final state where one of the $W$ bosons from the top quark decays hadronically into a $q\bar{q}$ pair and the other leptonically into $e\nu_e$, $\mu\nu_\mu$, or $\tau\nu_\tau$. We consider both direct electron and muon decays, as well as secondary electrons and muons from $\tau$ decay, but not taus decaying hadronically. If both $W$ bosons decay leptonically, this leads to a dilepton final state containing a pair of electrons, a pair of muons, or...
an electron and a muon, all of opposite electric charge. If only one of the leptons is reconstructed, the dilepton decay chain is also included in the signal. We also include events where both W bosons decay leptonically, and one lepton is an electron or muon and the other a hadronically decaying τ lepton. The $t\bar{t}$ processes where both W bosons decay hadronically contribute to multijet production, which is considered as a background process in this analysis.

We measure the $t\bar{t}$ production cross section using three methods: (i) a “kinematic” method based on $t\bar{t}$ event kinematics, (ii) a “counting” method using $b$-jet identification, and (iii) a method utilizing both techniques, referred to as the “combined” method. The first method does not rely on the identification of $b$ quarks while the second and third methods do. Thus they are sensitive to different systematic uncertainties. The combined method allows the simultaneous measurement of the $t\bar{t}$ production cross section and of the contribution from the largest background source.

The analysis is based on data collected with the D0 detector [9] in Run II of the Fermilab Tevatron Collider with an integrated luminosity of $5.3 \pm 0.3 \text{ fb}^{-1}$. The results of this analysis supersede our previous measurement [10], which was done with a fifth of the dataset considered here. A result from the CDF Collaboration is available in Ref. [11]. Recently, the ATLAS and CMS Collaborations reported first measurements of the $t\bar{t}$ cross section in pp collisions at $\sqrt{s} = 7.0 \text{ TeV}$ [12, 13].

In 2006, the D0 detector was substantially upgraded: a new calorimeter trigger was installed [14] and a new inner layer was added to the silicon microstrip tracker [15]. We split the data into two samples: Run IIA before this upgrade (on which our previous $t\bar{t}$ cross section measurement was performed) and Run IIB after it. The corresponding integrated luminosities are 1 fb$^{-1}$ and 4.3 fb$^{-1}$, respectively.

II. D0 DETECTOR

The D0 detector contains a tracking system, a calorimeter, and a muon spectrometer [9]. The tracking system consists of a silicon microstrip tracker (SMT) and a central fiber tracker (CFT), both located inside a 1.9 T superconducting solenoid. The design provides efficient charged-particle tracking in the detector pseudorapidity region $|\eta_{\text{det}}| < 3$ [16]. The SMT provides the capability to reconstruct the $p\bar{p}$ interaction vertex (PV) with a precision of about $40 \mu m$ in the plane transverse to the beam direction, and to determine the impact parameter of any track relative to the PV [17] with a precision between 20 and 50 $\mu m$, depending on the number of hits in the SMT, which is key to lifetime-based $b$-jet tagging. The calorimeter has a central section covering $|\eta_{\text{det}}| < 1.1$, and two end calorimeters (EC) extending the coverage to $|\eta_{\text{det}}| \approx 4.2$. The muon system surrounds the calorimeter and consists of three layers of tracking detectors and scintillators covering $|\eta_{\text{det}}| < 2$ [18]. A 1.8 T toroidal iron magnet is located outside the innermost layer of the muon detector. The luminosity is calculated from the rate of $pp$ inelastic collisions measured with plastic scintillator arrays, which are located in front of the EC cryostats.

The D0 trigger is based on a three-level pipeline system. The first level consists of hardware and firmware components. The microprocessor-based second level combines information from the different detector components to construct simple physics objects, whereas the software-based third level uses the full event information obtained with a simplified reconstruction [19].

III. EVENT SELECTION

Events in the 1+jets channel are triggered by requiring either an electron or a lower-$p_T$ electron accompanied by a jet for the $e$+jets channel, a muon and a jet for the $\mu$+jets final state in Run IIA, and a muon for the $\mu$+jets final state in Run IIB. These samples are enriched in $t\bar{t}$ events by requiring more than one jet of cone radius $R = 0.5$ [20] reconstructed with the “Run II cone” algorithm [21], with transverse momentum $p_T > 20 \text{ GeV}$ and pseudorapidity $|\eta_{\text{det}}| < 2.5$. Furthermore, we require one isolated electron with $p_T > 20 \text{ GeV}$ and $|\eta_{\text{det}}| < 1.1$, or one isolated muon with $p_T > 20 \text{ GeV}$ and $|\eta_{\text{det}}| < 2.0$, and missing transverse energy $E_T > 20(25) \text{ GeV}$ in the $e$+jets ($\mu$+jets) channel. The PV must be within 60 cm of the detector center in the longitudinal coordinate so that it is within the SMT fiducial region. In addition, the jet with highest $p_T$ must have $p_T > 40 \text{ GeV}$. The high instantaneous luminosity achieved by the Tevatron leads to a significant contribution from additional $p\bar{p}$ collisions within the same bunch crossing as the hard interaction. To reject jets from these additional collisions, we require all jets in Run IIB to contain at least three tracks within each jet cone that originate from the PV. Events containing two isolated leptons (either $e$ or $\mu$) with $p_T > 15 \text{ GeV}$ are rejected.

The $b$-jets are identified using a neural network formed by combining variables characterizing the properties of secondary vertices and of tracks with large impact parameters relative to the PV [22]. Details of lepton identification, jet identification and missing transverse energy calculation are described in Ref. [19].

We split the selected $t\bar{t}$+jets sample into subsamples according to lepton flavor ($e$ or $\mu$) and jet multiplicity, and between Run IIA and Run IIB. For the measurements with $b$-tagging, we split the data into additional subsamples according to the number of tagged $b$-jet candidates ($0$, $1$ or $> 1$).

IV. SAMPLE COMPOSITION

Top quark pair production and decay is simulated with the ALPGEN Monte Carlo (MC) program [23] assuming a
The top quark mass of $m_t = 172.5$ GeV (used for all tables and figures in this paper unless stated otherwise). The fragmentation of partons and the hadronization process are simulated using PYTHIA [24]. A matching scheme is applied to avoid double-counting of partonic event configurations [26]. The generated events are processed through a GEANT-based [25] simulation of the D0 detector and the same reconstruction programs used for the data. Effects from additional $p\bar{p}$ interactions are simulated by overlaying data from random $p\bar{p}$ crossings over the MC events.

The background can be split into two components: “instrumental background,” where the decay products of a final state parton are reconstructed as an isolated lepton, and “physics background” that originates from processes with a final state similar to that of $t\bar{t}$ signal. In the $e$+jets channel, instrumental background arises from multijet (MJ) production when a jet with high electromagnetic content mimics an electron; in the $\mu$+jets channel, it occurs when a muon contained within a jet originates from the decay of a heavy-flavor quark ($b$ or $c$ quark), but appears isolated.

The dominant physics background is from $W$+jets production. Other physics backgrounds are single top quark, diboson, and $Z$+jets production with $Z \rightarrow \tau\tau$, and $Z \rightarrow ee$ ($Z \rightarrow \mu\mu$) in the $e$+jets ($\mu$+jets) channel. The contributions from these background sources are estimated using MC simulations and normalized to next-to-leading order (NLO) predictions. Diboson events ($WW$, $WZ$ and $ZZ$) are generated with PYTHIA, single top quark production with the COMPHEN generator [27], and $Z$+jets events, with $Z \rightarrow ee$, $\mu\mu$, and $\tau\tau$, are simulated using ALPGEN. For the $Z$+jets background, the $p_T$ distribution of the $Z$ boson is corrected to match the distribution observed in data, taking into account a dependence on jet multiplicity. All simulated samples are generated using the CTEQ6L1 parton distribution functions (PDFs) [28]. The main background contribution, which is $W$+jets events, is discussed further below.

The MJ background is estimated from data using the “matrix method” [19]: Two samples of $\ell$+jets events are designed categorized by the stringency of the lepton selection criteria: the “tight” sample used for the signal extraction is a subset of a “loose” set which is dominated by background. The number of MJ events is extracted using the $\ell$+jets data sample of loose leptons that do not fulfill the tight isolation criteria.

In $W$+jets production, the $W$ boson is produced through the electroweak interaction, and additional partons are generated by QCD radiation. Several MC generators are capable of performing matrix element calculations for $W$ boson production including one or more partons in the final state, however these are performed only at tree level. Therefore, the overall normalization suffers from large theoretical uncertainties. For this reason, only the differential distributions are taken from the simulation while the overall normalization of the $W$+jets background is obtained from data by subtracting the physics and instrumental backgrounds and the $t\bar{t}$ signal. This is done as a function of jet multiplicity for each of the analysis channels. The $W$+jets contribution is divided into three exclusive categories according to parton flavor: (i) “$W$+hf” is the sum of all $W$ events with a $b\bar{b}$ of $c\bar{c}$ quark pair and any number of additional jets; (ii) “$W$+c” has events with a $W$ boson produced with a single charm quark and any number of additional jets; and (iii) “$W$+lhf” has $W$ bosons that are produced with light flavor jets. These three processes are generated by the LO QCD generator ALPGEN. The relative contributions from the three classes of events are determined using NLO QCD calculations based on the MCFM MC generator [29]. We correct the $W$+hf ($W$+c) rate obtained from ALPGEN by a K-factor of $1.47 \pm 0.22$ ($1.27 \pm 0.15$) relative to the $W$+lf rate.

We verify the factor ($f_H$) which needs to be applied to the LO $W$+hf rate in control samples which use the same selection criteria as for the signal sample, but require exactly one or exactly two jets. To extract $f_H$, we split the events into samples without a $b$-tagged jet and with at least one $b$-tagged jet, and adjust $f_H$ iteratively until the prediction matches the data. The resulting $f_H$ value is consistent with the above NLO K-factor from MCFM. In the combined method, we measure $f_H$ (assuming the same factor for the $b\bar{b}$ or $c\bar{c}$ components of $W$+hf) simultaneously with the $t\bar{t}$ cross section. This
TABLE 2: Numbers of selected “loose” ($N_L$) and “tight” ($N_T$) events used as input for the MJ background estimate as a function of jet multiplicity for samples before and after applying the $b$-tagging criteria.

|       | $e$+jets |       |       | $\mu$+jets |       |       |
|-------|----------|-------|-------|------------|-------|-------|
|       | 2 jets   | 3 jets| >3 jets| 2 jets     | 3 jets| >3 jets|
| $N_L$ | 16634    | 4452 | 1109  | 7198       | 1751  | 516   |
| $N_T$ | 7649     | 1681 | 448   | 5905       | 1360  | 390   |
| $N_L$ | 996      | 450  | 196   | 413        | 187   | 129   |
| $N_T$ | 453      | 198  | 112   | 317        | 140   | 109   |
| $N_L$ | >1 $b$-tag  | 73  | 78    | 45        | 33    | 45    | 38    |
| $N_T$ | >1 $b$-tag  | 48  | 45    | 33        | 28    | 38    | 35    |

Run IIb

|       | 2 jets   | 3 jets| >3 jets| 2 jets     | 3 jets| >3 jets|
|-------|----------|-------|-------|------------|-------|-------|
| $N_L$ | 37472    | 8153 | 1914  | 17581      | 3457  | 925   |
| $N_T$ | 20423    | 4118 | 1012  | 15290      | 2904  | 783   |
| $N_L$ | 2917     | 1130 | 465   | 1364       | 506   | 278   |
| $N_T$ | 1500     | 648  | 289   | 1139       | 426   | 236   |
| $N_L$ | >1 $b$-tag  | 251 | 218   | 164       | 125   | 126   | 127   |
| $N_T$ | >1 $b$-tag  | 184 | 154   | 127       | 109   | 114   | 119   |

reduces the uncertainties on the measured $\sigma_{tt}$ and provides a measurement of this factor including the systematic uncertainties.

V. EFFICIENCIES AND YIELDS OF $ttbar$ EVENTS

Selection efficiencies and $b$-tagging probabilities for each of the $\ell$+jets channels are summarized in Tables 3 and 4, respectively. To calculate these efficiencies, we separate the $\ell$+jets $ttbar$ MC events where only one W boson decays to $e$ or $\mu$ from the dilepton $ttbar$ events where both W bosons decay leptonically, but only one lepton is reconstructed.

We apply the same $b$-tagging algorithm to data and to simulated events, but correct the simulation as a function of jet flavor, $p_T$, and $\eta$ to achieve the same performance for $b$-tagging as found in data. These correction factors [22] are determined from data control samples, and are used to predict the yield of signal and background events with 0, 1, and > 1 $b$-tagged jets. We also correct lepton and jet identification and reconstruction efficiencies in simulation to match those measured in data.

Table 5 summarizes the predicted background and the observed numbers of events in $e$+jets and $\mu$+jets data with 0, 1, and > 1 tags, together with the prediction for the number of $ttbar$ event candidates obtained assuming the production cross section measurement from the combined method.

VI. KINEMATIC METHOD

In this and the following sections we present the methods used to measure the $ttbar$ cross section. The results of the three methods are presented in Sec. X, after a discussion of the sources of systematic uncertainties in Sec. IX.

A. Discrimination

In the kinematic analysis, we use final states with 2, 3 or > 3 jets, thereby defining twelve disjoint data sets. To distinguish $ttbar$ signal from background, we construct a discriminant that exploits differences between kinematic properties of $ttbar$ $\ell$+jets signal and the dominant $W$+jets background using the multivariate analysis toolkit TMVA [30]. The multivariate discriminant function is calculated by a random forest (RF) of decision trees. We use 200 trees for the RF, with the boosting type [31] set to “bagging,” and separation mode set to the “Gini index” without pruning [32].

We split both the $ttbar$ and the $W$+jets MC events into two equal samples, and use one for training and testing of the RF discriminant and the other to create discriminant distributions (templates) for fits to data. For all other sources of events, we use the trained RF discriminant to obtain the templates.

We choose input variables that separate signal and background and are well described by the MC simulation. To reduce the sensitivity of variables that are based on the jets in the events to the modeling of soft gluon radiation and to the underlying event, we include only the five highest-$p_T$ (leading) jets in these definitions. The variables chosen as inputs to build the RF discriminant are:

Aplanarity: The normalized quadratic momentum ten-
TABLE 3: Selection efficiencies for $t\bar{t}$ $\ell$+jets and dilepton contributions to the $\ell$+jets channels. The uncertainties on the efficiencies from limited MC statistics are of the order of (1–2)\%.

|               | $c$+jets |          |          | $\mu$+jets |          |          |
|---------------|----------|----------|----------|------------|----------|----------|
|               | 2 jets   | 3 jets   | > 3 jets | 2 jets     | 3 jets   | > 3 jets |
| $t\bar{t} \to \ell + \text{jets}$ | 0.043    | 0.103    | 0.097    | 0.026      | 0.069    | 0.070    |
| $t\bar{t} \to \ell\ell + \text{jets}$ | 0.108    | 0.040    | 0.009    | 0.067      | 0.027    | 0.006    |

TABLE 4: $b$-tagging probabilities for $t\bar{t}$ $\ell$+jets and dilepton contributions to the $\ell$+jets channels. The uncertainties on the $b$-tag probabilities from limited MC statistics are of the order of (1–2)\%.

|               | $c$+jets |          |          | $\mu$+jets |          |          |
|---------------|----------|----------|----------|------------|----------|----------|
|               | 2 jets   | 3 jets   | > 3 jets | 2 jets     | 3 jets   | > 3 jets |
| $t\bar{t} \to \ell + \text{jets}$ | 0.431    | 0.470    | 0.458    | 0.417      | 0.464    | 0.458    |
| $t\bar{t} \to \ell\ell + \text{jets}$ | 0.470    | 0.459    | 0.460    | 0.461      | 0.456    | 0.438    |

$\mathcal{M}$ is defined as

$$
\mathcal{M}_{ij} = \frac{\sum_o p_i^o p_j^o}{\sum_o |p|^2},
$$

where $\vec{p}^o$ is the momentum vector of a reconstructed object $o$, and $i$ and $j$ are the three Cartesian coordinates. The sum over objects includes up to the first five jets, ordered by $p_T$, and the selected charged lepton. The diagonalization of $\mathcal{M}$ yields three eigenvalues $\lambda_1 \geq \lambda_2 \geq \lambda_3$ with $\lambda_1 + \lambda_2 + \lambda_3 = 1$, that characterize the topological distribution of objects in an event.

The aplanarity is defined as $\mathcal{A} = \frac{1}{2} \lambda_3$ and reflects the degree of isotropy of an event, with its range restricted to $0 \leq \mathcal{A} \leq 0.5$. Large values correspond to spherically distributed events and small values to more planar events. While $t\bar{t}$ final states are more spherical, as is typical for decays of massive objects, $W$+jets and MJ events tend to be more planar.

Sphericity: The sphericity is defined as $\mathcal{S} = \frac{1}{2}(\lambda_2 + \lambda_3)$, and $t\bar{t}$ events tend to have higher values of $\mathcal{S}$ than background events. Values of $\mathcal{S}$ range from zero to one.

$H_T^3$: The scalar sum of the transverse momenta of up to five leading jets ($H_T$) and the transverse momentum of the lepton.

$H_T^2$: The $p_T$ of the third jet or the scalar sum of the $p_T$ of the jets with the third and fourth, or third to fifth largest $p_T$ in the event, for events with three, four, or more jets, respectively. As these jets correspond largely to gluon radiation for the $W$+jets background events but mainly to $W$ decays in the $t\bar{t}$ production, on average $H_T^3$ has higher values for the latter process.

$M_T^{\ell}$: The transverse mass of the dijet system for $\ell + 2$ jets events. Since $H_T^3$ is not defined in $\ell + 2$ jets events, we use $M_T^{\ell}$ in this channel instead.

$M_{\text{event}}$: The invariant mass of the system consisting of the lepton, the neutrino and up to five leading jets. The energy of the neutrino is determined by constraining the invariant mass of the lepton and vector $E_T$ (as the neutrino) to the mass of the $W$ boson. Of the two possible solutions for the longitudinal momentum of the neutrino, we use the one with the smaller absolute value. On average, $M_{\text{event}}$ is larger for $t\bar{t}$ events than for background.

$M_T^{2+\ell}$: Transverse mass of the system consisting of the second leading jet, the lepton and the neutrino, where the energy of the neutrino is determined the same way as in the case of $M_{\text{event}}$.

Figure 1 shows distributions for several of the input variables in the data compared to the sum of expected contributions from $t\bar{t}$ signal and backgrounds for the $\ell+$> 3 jets channel. The outputs of the RF discriminant are presented in Fig. 2 for the $\ell + 2$, $\ell + 3$ and $\ell + > 3$ jets channels.

Figure 1 indicates good agreement of data with expectation for $m_{\nu} = 172.5$ GeV. Similar levels of agreement between data and prediction are observed in all other
FIG. 1: (Color online) Distributions of input variables used in the RF discriminant for the $\ell+3$ jets channel in data overlaid with the predicted background and $t\bar{t}$ signal calculated using $\sigma_{t\bar{t}} = 7.78$ pb as measured using the combined method.

channels. The normalizations shown in Fig. 2 are based on the results of the kinematic method. The distributions in Figs. 2(a, c, e) are the results when only fitting $\sigma_{t\bar{t}}$; Figs. 2(b, d, f) show the result when the $t\bar{t}$ cross section is fitted together with other parameters, as shown in Eq. 2 and described in Sec. VIB.

B. Cross Section Measurement

To measure the $t\bar{t}$ cross section for the kinematic analysis, we perform a binned maximum likelihood fit of the distributions in the RF discriminant to data. We use templates from MC for dilepton and $\ell+j$ets contributions to the $t\bar{t}$ signal, as well as for $WW$, $WZ$, $ZZ$, $Z+jets$, single top quark ($s$- and $t$-channel), and $W+jets$ backgrounds. The MJ template comes from data, and the amount of MJ background is constrained within the uncertainties resulting from the matrix method.
TABLE 5: Yields for $e^+\text{-jets}$ and $\mu^+\text{-jets}$ with 0, 1, and $> 1$ $b$-tagged jets. The number of $t\bar{t}$ events is calculated using the cross section $\sigma_{t\bar{t}} = 7.78$ pb measured by the combined method. Uncertainties include statistical and systematic contributions. Due to the correlations of the systematic uncertainties between the samples, the uncertainty on the total predicted yield is not the sum of the uncertainties of the individual contributions.

| Channel          | Sample | 0 $b$-tags | 1 $b$-tag | $> 1$ $b$-tags |
|------------------|--------|------------|-----------|----------------|
| $e^+2$ jets      | $W + jets$ | 21019 ± 517 | 1360 ± 90 | 101 ± 13 |
|                  | Multijet | 2531 ± 301 | 197 ± 25 | 6 ± 1 |
|                  | $Z + jets$ | 1169 ± 159 | 68 ± 15 | 5 ± 2 |
|                  | Other | 858 ± 85 | 148 ± 19 | 21 ± 3 |
|                  | $t\bar{t}$ | 245 ± 22 | 265 ± 22 | 79 ± 9 |
|                  | Total | 25821 ± 458 | 2038 ± 97 | 213 ± 18 |
|                  | Observed | 25797 | 2043 | 232 |
| $e^+3$ jets      | $W + jets$ | 3358 ± 151 | 316 ± 26 | 29 ± 4 |
|                  | Multijet | 675 ± 70 | 75 ± 8 | 7 ± 1 |
|                  | $Z + jets$ | 271 ± 40 | 26 ± 6 | 2 ± 1 |
|                  | Other | 30 ± 4 | 8 ± 1 | 2 ± 0 |
|                  | $t\bar{t}$ | 289 ± 27 | 381 ± 30 | 147 ± 14 |
|                  | Total | 4765 ± 124 | 839 ± 37 | 194 ± 16 |
|                  | Observed | 4754 | 846 | 199 |
| $e^+ > 3$ jets   | $W + jets$ | 440 ± 73 | 55 ± 10 | 6 ± 1 |
|                  | Multijet | 141 ± 15 | 23 ± 3 | 2 ± 0 |
|                  | $Z + jets$ | 43 ± 7 | 6 ± 2 | 1 ± 0 |
|                  | Other | 30 ± 4 | 8 ± 1 | 2 ± 0 |
|                  | $t\bar{t}$ | 202 ± 24 | 322 ± 31 | 180 ± 19 |
|                  | Total | 857 ± 51 | 413 ± 25 | 190 ± 18 |
|                  | Observed | 899 | 401 | 160 |
| $\mu^+2$ jets    | $W + jets$ | 17386 ± 321 | 1081 ± 69 | 81 ± 10 |
|                  | Multijet | 208 ± 117 | 38 ± 24 | 1 ± 1 |
|                  | $Z + jets$ | 1142 ± 155 | 68 ± 15 | 5 ± 2 |
|                  | Other | 682 ± 67 | 118 ± 15 | 17 ± 2 |
|                  | $t\bar{t}$ | 155 ± 14 | 163 ± 14 | 50 ± 6 |
|                  | Total | 19573 ± 235 | 1468 ± 77 | 154 ± 14 |
|                  | Observed | 19602 | 1456 | 137 |
| $\mu^+3$ jets    | $W + jets$ | 2895 ± 100 | 201 ± 20 | 24 ± 3 |
|                  | Multijet | 87 ± 29 | 14 ± 5 | 0 ± 0 |
|                  | $Z + jets$ | 222 ± 31 | 19 ± 5 | 2 ± 1 |
|                  | Other | 138 ± 14 | 32 ± 4 | 7 ± 1 |
|                  | $t\bar{t}$ | 198 ± 18 | 262 ± 21 | 103 ± 10 |
|                  | Total | 3540 ± 77 | 589 ± 28 | 136 ± 12 |
|                  | Observed | 3546 | 566 | 152 |
| $\mu^+ > 3$ jets | $W + jets$ | 481 ± 53 | 63 ± 8 | 7 ± 2 |
|                  | Multijet | 27 ± 9 | 6 ± 2 | 0 ± 0 |
|                  | $Z + jets$ | 29 ± 5 | 4 ± 1 | 1 ± 1 |
|                  | Other | 23 ± 3 | 7 ± 1 | 2 ± 0 |
|                  | $t\bar{t}$ | 151 ± 17 | 240 ± 22 | 135 ± 14 |
|                  | Total | 711 ± 39 | 318 ± 17 | 145 ± 14 |
|                  | Observed | 674 | 345 | 154 |

We account for systematic uncertainties in the maximum likelihood fit by assigning a parameter to each independent systematic variation. These “nuisance” parameters are allowed to vary in the maximization of the likelihood function within uncertainties, therefore the measured $t\bar{t}$ cross section can be different from the value obtained if the parameters for the systematic uncertainties are not included in the fit. The effects of a source of systematic uncertainty that is fully correlated among several channels are controlled by a single parameter in these channels.

The likelihood function is defined as:

$$ L = \prod_{j=1}^{12} \left( \prod_{i} P^{j}(n_{i}^{e}, \mu_{i}) \right) P^{j}(N_{LT}^{e}, N_{LT}) K \mathcal{G}(\nu_k; 0, SD), $$

where $\mathcal{G}(\nu_k; 0, SD)$ denotes the Gaussian probability density with mean at zero and width corresponding to one standard deviation (SD) of the considered systematic uncertainty. $P(n, \mu)$ denotes the Poisson probability density for observing $n$ events, given an expectation value of $\mu$. $N_{LT}$ denotes the number of events in the “loose” but not “tight” (“loose–tight”) sample required by the method. The value of $N_{LT}$ is restricted within Poisson statistics to the observed number of events, $N_{LT}^{o}$, in the “loose–tight” sample, ensuring the inclusion of the statistical uncertainty in the MJ prediction. The first product runs over twelve data sets $j$ and all bins of the discriminant $i$; $n_{i}^{e}$ is the content of bin $i$ in the selected data sample; and $\mu_{i}$ is the expectation for bin $i$. This expectation is the sum of the predicted background and the expected number of $t\bar{t}$ events, which depends on $\sigma_{t\bar{t}}$. The last product runs over all independent sources of systematic uncertainties $k$, with $\nu_k$ being the corresponding nuisance parameters and $K$ the total number of independent sources $k$.

Since the discriminant for the MJ background is not determined from MC simulation but from the “loose–tight” data sample, it has a small contribution from events with leptons in the final state. This contamination of the MJ distribution is taken into account by using the corrected number of events expected in each bin of the discriminant functions used in Eq. 2:

$$ \mu_{i}(N_{LT}^{e}, N_{LT}^{W}, N_{LT}^{MC}, N_{LT}^{MJ}) = \left( f_{i}^{T} N_{LT}^{T} + f_{i}^{W} N_{LT}^{W} + \sum_{m} (f_{i}^{MC} N_{LT}^{MC}) \right) \times \left( 1 - \frac{\varepsilon_{b} - \varepsilon_{s}}{1 - \varepsilon_{b} - \varepsilon_{s}} \right) + f_{i}^{MJ} \left( N_{LT}^{MJ} + \frac{\varepsilon_{b} - \varepsilon_{s}}{1 - \varepsilon_{b} - \varepsilon_{s}} (N_{LT}^{T} + N_{LT}^{W} + N_{LT}^{MC}) \right), $$

where $N_{LT}^{T}, N_{LT}^{W}, N_{LT}^{MC}, N_{LT}^{MJ}$ are the numbers of $t\bar{t}$, $W + jets$, MC background (diboson, single top quark, $Z + jets$) and MJ events in the tight lepton sample, index $m$ runs over all small backgrounds estimated from MC, and $f_{i}^{T}$ is the predicted fraction of contribution $x$ in bin $i$.

We minimize the negative of the log-likelihood function of Eq. 2 as a function of $t\bar{t}$ cross section and the nuisance parameters. The fit results for the $t\bar{t}$ cross section and the nuisance parameters are given by their values at
the minimum of the negative log-likelihood function, and their uncertainties are defined from the increase in the negative log-likelihood by one-half of a unit relative to its minimum. Results of the fit are presented in Sec. X.
FIG. 2: (Color online) Output of the RF discriminant for (a) and (b) $\ell+2$ jets, (c) and (d) $\ell+3$ jets and (e) and (f) $\ell+>3$ jets events, for backgrounds and a $t\bar{t}$ signal based on the cross section obtained with the kinematic method. The ratio of data over MC prediction is also shown. The left plots (a, c, and e) show the results with the nuisance parameters fixed at value of zero. The right plots (b, d, and f) show the results when the nuisance parameters are determined simultaneously with the $t\bar{t}$ cross section in the fit. In the left and right plots the contribution from the $t\bar{t}$ signal is normalized to the results of the cross section measurement, $\sigma_{t\bar{t}} = 7.00$ and 7.68 pb, respectively.
VII. *b*-TAGGING METHOD

A. Discrimination

The SM predicts that the top quark decays almost exclusively into a $W$ boson and a $b$ quark ($t \rightarrow Wb$). Hence, besides using just kinematic information, the fraction of $t\bar{t}$ events in the selected sample can be enhanced using $b$-jet identification. To measure the $t\bar{t}$ cross section, we use final states with exactly three jets and more than three jets and further separate each channel into events with 0, 1, and $>1$ $b$-tagged jets, obtaining 24 mutually exclusive data samples.

B. Cross Section Measurement

As discussed in Sec. IV, before applying $b$-tagging, the contribution from the $W+\text{jets}$ background is normalized to the difference between data and the sum of $t\bar{t}$ signal and all other sources of background. Since the $W+\text{jets}$ background normalization depends on the $t\bar{t}$ cross section, the measurement of the cross section and the $W+\text{jets}$ normalization determination are performed simultaneously. Details of this method, as well as the general treatment of systematic uncertainties are described in Ref. [33]. The fit of the $t\bar{t}$ cross section to data is performed using a binned maximum likelihood fit for the predicted number of events, which depends on $\sigma_{t\bar{t}}$. The likelihood is defined as a product of Poisson probabilities for all 24 channels $j$:

$$\mathcal{L} = \prod_{j=1}^{24} \mathcal{P}(n_j, \mu_j) \mathcal{P}(N^o_{LT}, N_{LT}) \prod_{k=1}^{K} \mathcal{G}(\nu_k; 0, \text{SD}),$$

and systematic uncertainties are incorporated into the fit in the same way as described in Sec. VI B. Figure 3 shows the distributions of events with 0, 1, and $>1$ $b$-tagged jets for events with three and more than three jets in data compared to the sum of predicted background and measured $t\bar{t}$ signal using $b$-tagging method. Results for this method are given in Sec. X.

FIG. 3: (Color online) Distributions of events with 0, 1, and $>1$ $b$-tagged jets for (a) $\ell+3$ jets and (b) $\ell+>3$ jets, for backgrounds and contributions from $t\bar{t}$ signal for $\sigma_{t\bar{t}} = 8.13$ pb as measured using the $b$-tagging method.
VIII. COMBINED METHOD

In the combined method, kinematic information and b-jet identification are used. We split the selected sample into events with 2, 3, and > 3 jets and into 0, 1, and > 1 b-tagged jets and construct RF discriminant functions as described in Sec. VI for the channels dominated by the background.

For events with > 2 jets but no b-tagged jet, we construct a RF discriminant using the same six variables as for the kinematic method described in Sec. VI. For events with three jets and one b-tag, we construct discriminants using only $A$, $H_T^b$, and $M_{T^b}$. For all other subchannels, we do not form RF discriminants, but use the $b$-tagging method described in Sec. VII. The signal purity is already high in those channels except for the ones with two jets, which do not have a sizable signal contribution and are used to measure the $W$+jets heavy-flavor scale factor $f_H$ which is the source of one of the largest uncertainties in the $b$-tagging analysis.

To reduce this source of uncertainty, we measure $f_H$ simultaneously with $\sigma_{tt}$, assuming that $f_H$ for $Wb\bar{b}$ production is the same as for $Wc\bar{c}$ production and that it does not depend on the number of jets in the event. Since sources of uncertainty such as light-flavor jet tagging rates are correlated with the value of $f_H$, and in turn, $f_H$ is anti-correlated with the $tt$ cross section, the total uncertainty on the measured $\sigma_{tt}$ decreases. The main constraint on $f_H$ is provided by the 2-jets channels with 0, 1, and > 1 b-tagged jets. For this reason the RF discriminant was not used for the 2-jets channels in contrast to the measurement using only kinematic information (Sec. VI).

The cross section is measured using the likelihood function of Eq. 2 for channels where a RF discriminant is calculated, and using Eq. 4 for all other channels where the $b$-tagging method is performed. In the minimization procedure, we multiply appropriate likelihood functions for each channel and perform a fit to data assuming the same $tt$ cross section for all considered channels. Systematic uncertainties for each channel are incorporated as described in Sec. VI.B. The $W$+jets heavy-flavor scale factor enters the calculation of the predicted number of $W$+jets events, $N(W) \propto N(W + 1f) + f_H N(W + hf) + f_Wc N(W + c)$, where $f_Wc$ denotes the scale factor needed for $W+c$ events. A change in $f_H$ results in a change in the predicted number of $W$+jets events in each tag category without changing the total number of $W$+jets events in the sample prior to applying the $b$-tagging requirement which is normalized to data.

Figure 4 shows the distribution of the RF discriminant for the $\ell+3$ jets and $\ell+>3$ jets channels containing no b-tagged jets and for the $\ell+3$ jets channel containing one b-tagged jet. Figure 5 shows distributions of the number of jets for events with different numbers of b-tagged jets. In both figures we use the measured values of $\sigma_{tt}$ and $f_H$ (see Sec. X) as well as the nuisance parameters obtained from the fit.

![Figure 4](image1.png)

**FIG. 4:** (Color online) Output of the RF discriminant for (a) $\ell+3$ jets, (b) $\ell+>3$ jets for events without b-tagged jets, and (c) $\ell+3$ jets with one b-tagged jet, for backgrounds and contributions from $tt$ signal for a cross section of 7.78 pb as measured with the combined method.

IX. SYSTEMATIC UNCERTAINTIES

Different sources of systematic uncertainty can affect selection efficiencies, $b$-tagging probabilities, and the distributions of the RF discriminants. The sources that affect the selection efficiencies are electron and muon identification efficiencies, electron and muon trigger efficiencies, modeling of additional $p\bar{p}$ collisions in the MC.
The uncertainties due to $b$-tagging include corrections to the $b$, $c$, and light-flavor jet tagging rates, the track multiplicity requirements on jets which are candidates for $b$-tagging (called “taggability”), and on the possible differences in the calorimeter response between $b$ jets and light flavor jets. In addition, uncertainties in selection efficiencies and $b$-tagging probabilities can arise from limited statistics of MC samples and from the modeling of $tt$ signal. The latter includes PDF uncertainty, the difference between tuning of $b$-fragmentation to LEP or SLD data [34], the difference between simulations using ALPGEN or MC@NLO [35], and between PYTHIA or HERWIG [36] for parton evolution and hadronization, and the uncertainties on modeling color re-connections and on calculating initial and final state radiation. The uncertainty on the PDF is estimated by evaluating the effect of 20 independent uncertainty PDF sets of CTEQ6.1M [37] on the selection efficiency and $b$-tagging probabilities, and adding the resulting uncertainties in quadrature.

The uncertainties on the MJ background obtained from the matrix method include systematic uncertainties on $\epsilon_b$ and $\epsilon_{\bar{b}}$ as well as statistical uncertainties due to the limited size of the samples used to model MJ background. Uncertainties on the flavor composition of $W$+$jets$ and $Z$+$jets$ processes are also taken into account.

Uncertainties on the jet energy scale [38] (JES) and jet reconstruction and identification efficiencies affect the selection and $b$-tagging efficiencies, and the discriminant distributions. The discriminant distributions are also affected by the limited statistics used to form the templates. In the combined method, systematic uncertainties that affect the discriminant distributions include taggability and tagging rates for $b$, $c$, and light-flavor jets. The uncertainty on the integrated luminosity is 6.1% [39], affecting the estimates of signal and background yields obtained from simulation.

Jet energy scale, jet energy resolution, and jet reconstruction and identification uncertainties have a large effect on the discriminant distributions for $W$+$jets$ background and as a result, a large effect on the measured $\sigma_{tt}$. Their influence can be reduced by including events with two jets, dominated by the $W$+$jets$ background, in the fit. Due to the correlation of the considered systematic uncertainties between the different channels, the corresponding nuisance parameters are constrained by the background-dominated two-jet channels, and affect the result mostly through the samples with more jets, where the $tt$ content is higher.

The cross section fit with a simultaneous extraction of the nuisance parameters also results in a better agreement between data and the signal plus background prediction for the discriminant distribution in background dominated samples. An example of this effect is illustrated in Fig. 2, where we perform a comparison of data and the total signal plus background prediction for the case in which only the $tt$ cross section is a free parameter of the fit and for the case in which also the nuisance parameters are determined from the fit. Improvements can be seen when the additional parameters associated with systematic contributions are varied.

We take into account all correlations between channels

| Number of jets | Number of events | Number of events | Number of events | Number of events | Number of events | Number of events | Number of events |
|----------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
| 2              | 1000             | 1000             | 1500             | 1500             | 1500             | 2000             | 2000             |
| 3              | 2500             | 2500             | 2500             | 2500             | 2500             | 3000             | 3000             |
| 4              | 3500             | 3500             | 3500             | 3500             | 3500             | 4000             | 4000             |
| 5              | 4500             | 4500             | 4500             | 4500             | 4500             | 5000             | 5000             |

FIG. 5: (Color online) Jet multiplicity distributions for events with (a) 0, (b) 1, and (c) $>1$ $b$-tagged jets for backgrounds and contributions from $tt$ signal for a cross section of 7.78 pb as measured with the combined method.

simulation, corrections on the longitudinal distribution of the PV in the MC simulation and data-quality requirements (summarized under “other” in the tables of uncertainties), uncertainties on the normalization of the background obtained using MC, and uncertainties on the modeling of the signal.

The uncertainties due to $b$-tagging include corrections to the $b$, $c$, and light-flavor jet tagging rates, the track multiplicity requirements on jets which are candidates
and run periods. All uncertainties are taken as correlated between the channels except for contributions from MC statistics, trigger efficiencies, and the isolated lepton fake rate required by the matrix method. Systematics uncertainties measured using independent Run IIa and Run IIb data sets and are dominated by the limited statistics of these data sets are taken as uncorrelated, including trigger efficiencies, jet energy scale, jet identification, jet energy resolution, taggability, and lepton identification.

X. RESULTS

We quote the results for the \( t\bar{t} \) cross section measurements using the three different methods described above, assuming a value of the top quark mass of 172.5 GeV. In Sec. X D we discuss the dependence of the cross section measurement on the assumed value of the top quark mass.

A. Kinematic method

Table 6 shows the measured cross section in the \( e+\) jets and the \( \mu+\) jets channels, and for the combined \( \ell+\) jets channel for the kinematic method. Table 7 lists the corresponding uncertainties. For each category of systematic uncertainties listed in Table 7, only the corresponding nuisance parameters are allowed to vary. The column “Offset” shows the absolute shift of the measured \( t\bar{t} \) cross section with respect to the result obtained including only statistical uncertainties. The columns “+\( \sigma \)” and “−\( \sigma \)” list the systematic uncertainty on the measured cross section for each category. For the “fit result” all nuisance parameters are allowed to vary at the same time, which can result in a different “offset” and different uncertainties on the final \( t\bar{t} \) cross section than expected from a sum of the individual “offsets” and systematic uncertainties. The uncertainty given in the row “fit result” refers to the full statistical plus systematic uncertainty.

In the final fit, all nuisance parameters vary by less than one SD from their mean value of zero. This also applies for the two other methods used for the extraction of the cross section.

The consistency of results between the \( e+\) jets and \( \mu+\) jets channels is studied using an ensemble of 10,000 generated pseudo-experiments, each representing a single simulation of the results from the data sample, assuming \( \sigma_{t\bar{t}} \) measured in the combined \( \ell+\) jets channel. We vary the number of signal and background events in each pseudo-experiment within Poisson statistics about their mean values. For each pseudo-experiment, we measure the cross section in the \( e+\) jets and \( \mu+\) jets channels by performing a likelihood fit in which the parameters corresponding to individual sources of systematic uncertainty are varied randomly according to Gaussian functions, taking into account the correlations between the \( e+\) jets and \( \mu+\) jets channels. We record the difference between \( \sigma_{t\bar{t}} \) in both channels and calculate, as a measure of consistency, the probability that it is equal to or larger than the measured difference as shown in Table 6. The two measurements are found to be consistent with a probability of 22%.

B. \( b \)-tagging method

Table 8 gives the results of the \( b \)-tagging method for the \( e+\) jets, \( \mu+\) jets, and combined \( \ell+\) jets channels, and Table 9 gives the systematic uncertainties. The consistency of these results is checked with pseudo-experiments performed in the same way as described in the previous section. We find that the \( \sigma_{t\bar{t}} \) values measured in the \( e+\) jets and \( \mu+\) jets channels are consistent with a probability of 8%.

C. Combined method

Table 10 shows results for \( \sigma_{t\bar{t}} \) and \( f_H \) in \( e+\) jets, \( \mu+\) jets and \( \ell+\) jets channels for the combined method and Table 11 gives the systematic uncertainties. The relative uncertainties on \( \sigma_{t\bar{t}} \) for the combined and the kinematic methods are comparable. This is expected because the measurements are systematically limited. Compared to the kinematic method, the combined method has improved statistical sensitivity. On the other hand, we include more sources of systematic uncertainty, such as the relatively large \( b \)-tagging uncertainty, which reduces slightly the final precision.

D. Top quark mass dependency for the combined method

Different selection efficiencies lead to a dependence of \( \sigma_{t\bar{t}} \) on \( m_t \). This is studied using simulated samples of \( t\bar{t} \) events generated at different values of \( m_t \) using the ALPGEN event generator followed by PYTHIA for the simulation of parton-shower development. The resulting measurements are summarized in Table 12 and can be
parametrized as a function of $m_t$ as

$$\sigma_{tt}(m_t) = \frac{1}{m_t} \left[ a + b(m_t - m_0) + c(m_t - m_0)^2 + d(m_t - m_0)^3 \right],$$

where $\sigma_{tt}$ and $m_t$ are in pb and GeV, respectively, and $m_0 = 170$ GeV, $a = 5.78874 \times 10^9$ pb GeV$^4$, $b = -4.50763 \times 10^7$ pb GeV$^4$, $c = 1.50344 \times 10^5$ pb GeV$^2$, and $d = -1.00182 \times 10^3$ pb GeV.

In Fig. 6 we compare this parameterization to three approximations to $\sigma_{tt}$ at next-to-next-to-leading-order (NNLO) QCD that include all next-to-next-to-leading logarithms (NNLL) in NNLO QCD [1, 2, 4].

Table 7: Measured $t\bar{t}$ cross section and the breakdown of uncertainties for the kinematic method in the $\ell$+jets channel. The offsets show how the mean value of the measured cross section is shifted due to each source of systematic uncertainty. In each line, all but the considered source of systematic uncertainty are ignored. The $\pm$ give the impact on the measured cross section when the nuisance parameters describing the considered category are changed by $\pm 1$ SD of their fitted value.

| Source                  | $\sigma_{tt}$ [pb] | Offset [pb] | $+\sigma$ [pb] | $-\sigma$ [pb] |
|-------------------------|--------------------|-------------|----------------|----------------|
| Statistical only        | 7.00               | +0.28       | -0.28          |                |
| Muon identification     |                    | -0.02       | +0.05          | -0.05          |
| Electron identification |                    | +0.14       | +0.13          | -0.12          |
| Triggers                |                    | -0.08       | +0.10          | -0.09          |
| Background normalization|                    | +0.07       | +0.06          | -0.06          |
| Signal modeling         |                    | -0.22       | +0.20          | -0.18          |
| Monte Carlo statistics  |                    | +0.00       | +0.02          | -0.02          |
| MJ background           |                    | +0.01       | +0.00          | -0.05          |
| $f_{tt}$                |                    | +0.13       | +0.03          | -0.03          |
| Jet energy scale        |                    | +0.26       | +0.00          | +0.00          |
| Jet reconstruction and identification |  | +0.55       | +0.18          | -0.16          |
| Luminosity              |                    | +0.45       | +0.50          | -0.44          |
| Template statistics     |                    | +0.00       | +0.04          | -0.04          |
| Other                   |                    | -0.01       | +0.13          | -0.12          |
| Total systematics       |                    | +0.61       | -0.55          |                |
| Fit result              | 7.68               | +0.71       | -0.64          |                |

Table 8: Measured $t\bar{t}$ cross section using $b$-tagging for separate and combined $\ell$+jets channels. The first quoted uncertainty denotes the statistical, the second the systematic contribution. The statistical uncertainty is scaled from the statistical only $\sigma_{tt}$ result in Table 9 to the final $\sigma_{tt}$. The total uncertainty corresponds to the one in the row “Fit result” in Table 9.

| Channel                  | $\ell$+jets | $\mu$+jets | $\ell$+jets |
|--------------------------|-------------|------------|-------------|
| $\sigma_{tt}$ [pb]       | 7.40 ± 0.32 | 7.88 ± 0.40 | 8.13 ± 0.25 |

XI. CONCLUSION

We measured the $t\bar{t}$ production cross section in the $\ell$+jets final states using different analysis techniques. In 5.3 fb$^{-1}$ of integrated luminosity collected with the D0 detector, for a top quark mass of 172.5 GeV, we obtain:

$$\sigma_{tt} = 7.78^{+0.77}_{-0.67} \text{ (stat + syst + lumi) pb},$$

using both kinematic event information and $b$-jet identification and simultaneously measuring the cross section and the ratio of $W$+heavy flavor jets to $W$+light flavor jets. The precision achieved is approximately 9%. A result of similar precision from the CDF Collaboration is available in Ref. [11]. All our results are consistent with the theoretical predictions of $\sigma_{tt} = 6.41^{+0.51}_{-0.42}$ pb [1] and $\sigma_{tt} = 7.46^{+0.48}_{-0.67}$ pb [2].

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TABLE 9: Measured $t\bar{t}$ cross section and the breakdown of uncertainties for the $b$-tagging method in the $\ell+\text{jets}$ channel. The offsets show how the mean value of the measured cross section is shifted due to each source of systematic uncertainty. In each line, all but the considered source of systematic uncertainty are ignored. The $\pm\sigma$ give the impact on the measured cross section when the nuisance parameters describing the considered category are changed by $\pm 1$ SD of their fitted value.

| Source                        | $\sigma_{t\bar{t}}$ [pb] | Offset [pb] | $+\sigma$ [pb] | $-\sigma$ [pb] |
|-------------------------------|--------------------------|-------------|----------------|----------------|
| Statistical only              | 7.81                     | +0.24       | +0.05          | -0.05          |
| Muon identification           | -0.05                    | +0.06       | -0.05          |                |
| Electron identification       | +0.17                    | +0.13       | -0.13          |                |
| Triggers                      | -0.13                    | +0.11       | -0.11          |                |
| Background normalization      | -0.00                    | +0.08       | -0.08          |                |
| Signal modeling               | +0.04                    | +0.24       | -0.27          |                |
| $b$-tagging                   | +0.05                    | +0.34       | -0.32          |                |
| Monte Carlo statistics        | -0.01                    | +0.09       | -0.10          |                |
| MJ background                 | -0.00                    | +0.06       | -0.06          |                |
| $f_H$                         | -0.04                    | +0.18       | -0.19          |                |
| Jet energy scale              | +0.05                    | +0.09       | -0.09          |                |
| Jet reconstruction and identification | +0.02               | +0.17       | -0.16          |                |
| Luminosity                    | -0.02                    | +0.53       | -0.46          |                |
| Other                         | -0.00                    | +0.14       | -0.13          |                |
| Total systematics             |                         | +0.77       | -0.72          |                |
| Fit result                    | 8.13                     | +1.02       | -0.90          |                |

TABLE 10: Measured $t\bar{t}$ cross section and the $W+\text{jets}$ heavy flavor scale factor $f_H$ for separate and combined $\ell+\text{jets}$ channels, using both kinematic information and $b$-tagging. The first quoted uncertainty denotes the statistical, the second the systematic contribution. The statistical uncertainty is scaled from the statistical only $\sigma_{t\bar{t}}$ result in Table 11 to the final $\sigma_{t\bar{t}}$. The total uncertainty corresponds to the one in the row “Fit result” in Table 11.

| Channel | $\epsilon+\text{jets}$ | $\mu+\text{jets}$ | $\ell+\text{jets}$ |
|---------|------------------------|-------------------|-------------------|
| $\sigma_{t\bar{t}}$ [pb] | $7.22 \pm 0.32^{+0.70}_{-0.63}$ | $8.43 \pm 0.39^{+0.80}_{-0.70}$ | $7.78 \pm 0.25^{+0.73}_{-0.59}$ |
| $f_H$ | $1.74 \pm 0.13^{+0.21}_{-0.21}$ | $1.26 \pm 0.12^{+0.38}_{-0.17}$ | $1.55 \pm 0.09^{+0.17}_{-0.19}$ |

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The impact parameter is defined as the distance of closest approach of the detected particle to the interaction vertex. The offsets show how the mean value of the measured cross section is shifted due to each source of systematic uncertainty. In each line, all but ±1 SD of their fitted value. The ±σ give the impact on the measured cross section when the nuisance parameters describing the considered category are changed by ±1 SD of their fitted value. The uncertainty on $\sqrt{N}$ is the statistical plus systematic uncertainty. The uncertainty on $\bar{\sigma}_{t\bar{t}}$ is the combined statistical plus systematic uncertainty. 

TABLE 11: Measured $t\bar{t}$ cross section and the breakdown of uncertainties for the combined kinematic and $b$-tagging method in the $\ell+\text{jets}$ channel. The offsets show how the mean value of the measured cross section is shifted due to each source of systematic uncertainty. In each line, all but ±1 SD of their fitted value.

| Source                          | $\sigma_{t\bar{t}}$ [pb] | Offset [pb] | $+\sigma$ [pb] | $-\sigma$ [pb] |
|--------------------------------|--------------------------|-------------|----------------|---------------|
| Statistical only               | 7.58                     | +0.24       | -0.24          |               |
| Muon identification            | -0.04                    | +0.05       | -0.05          |               |
| Electron identification        | +0.14                    | +0.12       | -0.12          |               |
| Triggers                       | -0.09                    | +0.09       | -0.11          |               |
| Background normalization       | +0.00                    | +0.07       | -0.06          |               |
| Signal modeling                | -0.06                    | +0.23       | -0.21          |               |
| $b$-tagging                    | -0.14                    | +0.12       | -0.12          |               |
| Monte Carlo statistics         | -0.01                    | +0.06       | -0.06          |               |
| Fake background                | -0.01                    | +0.06       | -0.04          |               |
| Jet energy scale               | -0.00                    | +0.02       | -0.02          |               |
| Jet reconstruction and identification | +0.18 | +0.18 | -0.17          |               |
| Luminosity                     | +0.12                    | +0.51       | -0.44          |               |
| Template statistics            | +0.00                    | +0.03       | -0.03          |               |
| Other                          | +0.01                    | +0.14       | -0.13          |               |
| Total systematics              |                          | +0.65       | -0.58          |               |
| Fit result                     | 7.78                     | +0.77       | -0.64          |               |

TABLE 12: The $t\bar{t}$ cross sections measured using the combined method for different assumed top quark masses. The uncertainty is the combined statistical plus systematic uncertainty.

| $m_t$ [GeV] | $\sigma_{t\bar{t}}$ [pb] |
|-------------|--------------------------|
| 150         | 10.27±1.10±0.88          |
| 160         | 9.94±0.86±0.79           |
| 165         | 8.56±0.82±0.71           |
| 170         | 8.09±0.77±0.68           |
| 172.5       | 7.78±0.68                |
| 175         | 7.65±0.79                |
| 180         | 7.46±0.74                |
| 185         | 7.06±0.67                |
| 190         | 6.85±0.66                |

[16] The rapidity $y$ and pseudorapidity $\eta$ are defined as functions of the polar angle $\theta$ and parameter $\beta$ as $y(\theta, \beta) \equiv \frac{1}{2} \ln \left[ (1 + \beta \cos \theta)/(1 - \beta \cos \theta) \right]$ and $\eta(\theta) \equiv y(\theta, 1)$, where $\beta$ is the ratio of a particle’s momentum to its energy. We distinguish detector $\eta$ ($\eta_{\text{det}}$) and physics $\eta$, where the former is defined with respect to the center of the detector and the latter with respect to the PV interaction vertex.

[17] The impact parameter is defined as the distance of closest approach ($d_{ca}$) of the track to the PV in the plane transverse to the beamline. The impact parameter significance is defined as $d_{ca}/\sigma_{d_{ca}}$, where $\sigma_{d_{ca}}$ is the uncertainty on $d_{ca}$.

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FIG. 6: (Color online) Experimental and theoretical [1, 2, 4] values of $\sigma_{t\bar{t}}$ as a function of $m_t$. The point shows $\sigma_{t\bar{t}}$ measured using the combined method, the black line the fit with Eq. 4, and the gray band with its dashed delimiting lines the corresponding total experimental uncertainty. Each curve is bracketed by dashed lines of the corresponding color that represent the theoretical uncertainties due to the choice of PDF and the renormalization and factorization scales (added linearly).