A new drilling method—Earthworm-like vibration drilling

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Abstract

The load transfer difficulty caused by borehole wall friction severely limits the penetration rate and extended-reach limit of complex structural wells. A new friction reduction technology termed “earthworm-like drilling” is proposed in this paper to improve the load transfer of complex structural wells. A mathematical model based on a “soft-string” model is developed and solved. The results show that earthworm-like drilling is more effective than single-point vibration drilling. The amplitude and frequency of the pulse pressure and the installation position of the shakers have a substantial impact on friction reduction and load transfer. An optimization model based on the projection gradient method is developed and used to optimize the position of three shakers in a horizontal well. The results verify the feasibility and advantages of earthworm-like drilling, and establish a solid theoretical foundation for its application in oil field drilling.

Introduction

A complex structural well is a series of well types with the characteristics of a horizontal well. It can be divided into different directional wells in terms of the ratio λ of horizontal depth and vertical depth, such as a directional well (0 < λ < 2), a common extended reach well (2 ≤ λ < 3) and a high ratio extended reach well (λ ≥ 3) [1]. Drilling a complex structural well can ensure hitting the pay zone successfully and achieve good formation protection. In addition, such a well is compatible with future stimulation to efficiently and economically increase well production and improve the final recovery rate. Because of the significant difficulty of controlling the well trace of a complex structural well, directional drilling represents a key technology in the construction of such wells. At present, two well-track controlling modes have been developed: slide steering and rotatory steering. The slide steering controlling mode has wider application than the rotatory steering controlling mode because of its better cost-performance. However, the drill-string does not rotate in the slide steering mode, which results in substantial friction between the drill-string and the borehole wall and decreases axial load transfer efficiency. The weight component of the upper drill-string cannot be transmitted to the drill bit, and the penetration rate decreases. Therefore, efficiently reducing the friction between the drill-string and the borehole wall during the directional drilling of a complex structural well...
has substantial significance and has been an important issue in petroleum drilling engineering for many years [2].

Many scholars have performed friction reduction research, which can be generally divided into two types: decreasing the normal contact force or decreasing the frictional coefficient. The former includes optimizing the well track and using light drill pipe. The latter includes developing high-performance lubricant as well as using a cylindrical roller sub and a non-rotating protective joint [3]. All these methods are classified as passive friction reduction and achieve a limited application effect. As early as 1983, Roper proposed decreasing the friction between the drill-string and borehole wall by adding vibrators in the drill-string [4]. In recent years, several petroleum technology service companies began to perform application research on this idea, with a focus on vibrator development [5–7]. Compared with the vibrator development research, the research on friction reduction mechanisms and the load transfer rule of the drill-string under vibration conditions have been neglected. The mechanisms of friction reduction by vibrating the drill-string primarily include (a) the change of static friction to dynamic friction via axial and torsional vibrations [8], (b) the change in the direction of the dynamic friction by such vibrations, which decreases the average friction force during a vibrating cycle [9, 10] and (c) the periodic decrease in the normal contact force caused by lateral vibration [11]. Several scholars have developed models to calculate the load transfer of the drill-string under various vibration conditions [12–15]. In these models, the vibrator is typically treated as a sinusoidal exciting force that acts on the disperse node. However, in fact, the exciting force generated by a disc valve structure vibrator is bidirectional (such as Agitator: upward 25% and downward 75%), and the stiffness of the vibrator equals the stiffness of the disc spring used in the shaker sub. In addition, the deficiency of limited action distance caused by adding only one vibrator in the drill-string is increasingly apparent as the designed horizontal displacement of a complex structural well increases. Multi-point vibration technology, which is realized by adding several vibrators in the drill-string has become the predominant approach of friction reduction technology based on vibrating the drill-string. It also represents the preferred technique to meet the increasingly urgent friction reduction demand expected in the future.

The concept and method of bionics have permeated many research areas and industries. Based on the idea of multi-point vibration technology, the authors find that the assembly of multi-point vibration is closely resembles the segmented body of an earthworm. Every vibrator and adjacent drill-string are equivalent to one earthworm somite. An earthworm can generate a backward wave along its body by controlling the shrink and relaxation of muscle in its somites and can adjust the friction force between a somite and the cavity wall by controlling the bristle that extends from and retracts into the somite. These movements enable the earthworm to move forward while compressing and devouring soil and forming a cave [16, 17]. In this process, the earthworm decomposes the necessary large friction of its entire as it moves forward into the smaller friction of each somite moving forward. Inspired by the earthworm’s decomposition and use of friction, the authors propose a new friction reduction method termed the earthworm-like drilling scheme (Fig 1). A hydraulic pulse generator and more than one shaker are mounted in the drill-string from bottom to top. The hydraulic pulse generator can motivate a sinusoidal positive pressure pulse by exploiting the throttling effect. Then, the shakers can elongate axially a maximum of 10 to 15 mm (which equals the moving clearance 7) after receiving the positive pulse pressure generated by the hydraulic pulse generator and subsequently shorten to the original condition after the pulse pressure disappears. The upper sub 1 and sleeve 2 are connected into a whole by a thread, and the center shaft 4 and lower sub 3 are connected to another whole by a thread. All the parts of the shaker are revolution solid except the match position of the bottom of center shaft 4 and sleeve 2 (see section view A-A in Fig 1) which is hexagonal. This specific hexagonal structure causes the center shaft to only
slide axially relative to sleeve 2 to transmit the axial load and torsion torque of the drill-string. The upper sub 1, center shaft 4 and sleeve 2 constitute a high-pressure chamber 9. The center shaft 4 and sleeve 2 constitute a low-pressure chamber 10. In the drilling process, the high-pressure chamber fills with high-pressure drilling fluid and the low-pressure chamber fills with the low-pressure drilling fluid of the annulus. Four forces act on the center shaft 4 in the axial direction: ① the pressure difference between the high-pressure chamber and the low-pressure chamber, ② the spring force difference between the disc springs in the high-pressure chamber and the low-pressure chamber, ③ the force from lower sub 3 and ④ the weight component of center shaft 4. The displacement and density of the drilling fluid, the bit nozzle pressure drop and the circulating pressure loss when drilling a well are in a specific range and can be calculated. Then, the force balance of ①, ② and ④ can be realized through choosing a suitable disc spring stiffness of the shaker. Therefore, the small force from lower sub 3 can make the moving clearance 7 equal zero. Because the drill-string segment in which the shakers are installed is compressed, all the shakers can remain “closed” during the drilling process if there is no positive pulse pressure. When drilling, the positive pressure pulse excited by the hydraulic pulse generator with certain frequencies and amplitudes spreads upward inside the drill-string. Then, the shakers elongate in an orderly manner when the pulse pressure passes through, and the shakers shrink under the axial compressive force after the pressure pulse disappears. The combination of positive pulse pressure and axial compressive force makes the shakers vibrate periodically. In the presence of the weight component of the drill-string in the axial direction, the drill-string moves forward smoothly. Because there is only one hydraulic pulse generator, the pressure consumption is much less than that of multi-point vibration technology, which involves mounting several hydraulic pulse generators.

In this paper, the load transfer characteristics, advantages and feasibility of earthworm-like drilling are researched. First, a model is established to analyze the forces and motion of a drill-string with one or several shakers, and a finite difference method with second-order accuracy is adopted to solve this numerical model. Second, the load transfer effect under different parameters (such as amplitude of exciting force, frequency, installation distance and phase difference of the shakers) of three-point earthworm-like drilling are analyzed to determine the influence of these factors on the weight on the bit and the optimum parameters. The load transfer characteristics, advantages and feasibility of earthworm-like drilling are researched.
transfer effect under low frequency (<10Hz), which can be termed “wriggle drilling”, is studied by changing the amplitude of the exciting force. Third, an optimizing model based on the projection gradient method is used to optimize the position of three shakers in a horizontal well drill-string. The purpose of this paper is to prove the feasibility and describe the advantages of earthworm-like drilling and establish a solid theoretical foundation for this technology’s application in field drilling by comparing the load transfer characteristics of single point vibration, multi-point vibration and earthworm-like vibration drilling.

Modeling

Governing differential equation

The drill-string does not rotate in the directional drilling process. Substantial friction and drag are applied on the drill-string by the borehole wall, which means that rotation and lateral motion can be ignored. The existence of friction and drag makes buckling less likely, particularly in the horizontal section [18]. Therefore, axial motion becomes the primary motion of the drill-string. In this paper, we focus on the effect of axial earthworm-like excitation on the load transfer characteristics in the directional drilling of a complex structural well. The following assumptions are adopted. (a) The cross section of the drill-string is annular. We ignore the clearance between the drill-string and the borehole wall. (b) Each shaker is viewed as a length of the drill-string, and the sinusoidal exciting force of the same amplitude, frequency and inverse direction are applied on both ends of the shaker. (c) The damping forces that act on the drill-string include friction and viscous damping of the drilling fluid. The mechanical resistance that results from the drill-string pressing into the borehole wall and sticking is not considered. (d) Only the axial dynamic effect of the drill-string is considered, and the shear force and bending moment of the cross section of the drill-string are ignored.

Based on the four assumptions, a micro-element ds is extracted from the drill-string. In natural curvilinear coordinates (\(\bar{e}_r, \bar{e}_\theta, \bar{e}_z\)), the forces that act on the micro-element include internal tension force \(T\), normal contact force \(F_e\), friction force \(F_f\), the damping force and the buoyant weight of drilling (Fig 2).

According to the equilibrium condition of forces, we can obtain the following equation:

\[
\frac{\partial T(s,t)}{\partial s} + F_e(s,t) = \nabla^2 \bar{u}(s,t) \quad \text{and} \quad F_f(s,t) = \bar{g}_s(s,t) \bar{e}_z \quad \text{and} \quad g_r(s,t) = \rho(s)A(s) \frac{\partial^2 \bar{u}(s,t)}{\partial t^2} \bar{e}_r ,
\]

where \(F_{\text{top}}\) is the hook load, WOB is the weight on bit, \(\bar{e}_r, \bar{e}_\theta, \bar{e}_z\) and \(\bar{e}_b\) are unit base vectors in a natural curvilinear system, \(\bar{e}_z\) is the vector of the submerged drill-string weight, \(T\) is the internal tension force, \(F\) is the normal contact force, \(F_f\) is the axial friction force, \(c\) is drilling fluid drag, \(\rho\) is the density of the drill-string, \(g_s\) is the linear buoyant weight of the drill-string, \(u\) is the axial displacement of the drill-string, \(s\) is well depth, \(A\) is the cross-section area of the drill-string and \(t\) is time.

The following simpler equilibrium equation can be derived from the Taylor expansion in \((s, t)\) of variables by omitting higher order terms:

\[
\frac{\partial T(s,t)}{\partial s} + F_e(s,t) - \left[ F_f(s,t) + c(s,t) \frac{\partial u(s,t)}{\partial t} \right] \bar{e}_z + g_r(s,t) \bar{e}_z = \rho(s)A(s) \frac{\partial^2 \bar{u}(s,t)}{\partial t^2} \bar{e}_r .
\]
We separate internal force $\mathbf{T}$ and distributed lateral contact force $\mathbf{F}$ into components in natural curvilinear coordinates ($\mathbf{e}_t$, $\mathbf{e}_n$, $\mathbf{e}_b$):

\[
\mathbf{T}(s, t) = T_t(s, t) \mathbf{e}_t + T_n(s, t) \mathbf{e}_n + T_b(s, t) \mathbf{e}_b
\]

\[
\mathbf{F}(s, t) = F_n(s, t) \mathbf{e}_n + F_b(s, t) \mathbf{e}_b
\]

where $T_t(s, t)$, $T_n(s, t)$ and $T_b(s, t)$ are the internal tension force that acts on the cross section in the $\mathbf{e}_t$, $\mathbf{e}_n$ and $\mathbf{e}_b$ directions, respectively, and $F_n$, $F_b$ are the lateral contact force that acts on the drill-string in the principal normal $\mathbf{e}_n$ and binormal direction $\mathbf{e}_b$, respectively.

We use the Frenet-Serret equations for the centerline of the borehole [19]:

\[
\mathbf{e}_t = \frac{k_n}{k_b} \mathbf{e}_n \quad \mathbf{e}_n = \frac{k_b}{k_n} \mathbf{e}_t
\]

\[
\mathbf{e}_b = -\frac{k_n}{k_b} \mathbf{e}_n \quad \mathbf{e}_n = \frac{k_b}{k_n} \mathbf{e}_t\]

\[
\mathbf{e}_t = -\cos \theta \mathbf{e}_i + \frac{k_n}{k_b} \sin \theta \mathbf{e}_n + \frac{k_n}{k_b} \sin^2 \theta \mathbf{e}_b
\]

\[
\mathbf{e}_n = \frac{k_b}{k_n} \mathbf{e}_t
\]

\[
\mathbf{e}_b = -\frac{k_n}{k_b} \mathbf{e}_n
\]
where \( \alpha, \varphi \) and \( \bar{\alpha} \) are the deviation angle, azimuth angle and mean deviation angle, respectively, and \( k_{\alpha}, k_{\varphi} \) and \( k_b \) are the rate of change of the deviation angle, the rate of change of the azimuth angle and the total bending curvature, respectively.

The following scalar equations can be obtained by substituting Eqs (3)–(5) into Eq (2).

In the \( \vec{e}_t \) direction:

\[
\frac{\partial T_t}{\partial s} - F_f(s, t) - c \frac{\partial u}{\partial t} + g \cos \bar{\alpha} = \rho A \frac{\partial^2 u}{\partial t^2}
\]  

(6)

In the \( \vec{e}_n \) direction:

\[
F_n + T_t k_b + g \frac{k_{\alpha}}{k_b} \sin \alpha = 0
\]  

(7)

In the \( \vec{e}_b \) direction:

\[
F_b + g \frac{k_{\varphi}}{k_b} (\sin \alpha)^2 = 0
\]  

(8)

According to mechanics of materials theory, the internal tension force \( T_t \) in the axial direction for a slender rod can be written in the following form:

\[
T_t = EA \frac{\partial u}{\partial s}
\]  

(9)

where \( E \) is the elastic (Young’s) modulus of the drill-string.

The distributed lateral contact force between the drill-string and borehole wall can be obtained by combining Eqs (7) and (8):

\[
F = \sqrt{F_n^2 + F_b^2} = \left[ \left( Tk_b + g \frac{k_{\alpha}}{k_b} \sin \alpha \right)^2 + \left( g \frac{k_{\varphi}}{k_b} (\sin \alpha)^2 \right)^2 \right]^{\frac{1}{2}}
\]  

(10)

Friction force \( F_f \) is calculated by the Coulomb friction model, which assumes the following form:

\[
F_f = \mu F \quad \text{if } v \leq 0, \mu = \mu_s
\]

\[
F_f = \mu F \quad \text{if } v > 0, \mu = \mu_d
\]  

(11)

where \( \mu \) is the instantaneous friction coefficient in the \( \vec{e}_t \) direction, \( \mu_s \) is the static friction coefficient, \( \mu_d \) is the dynamic friction coefficient and \( v \) is the velocity of the drill-string.

**Boundary and initial conditions**

Drillers are required to do their best to maintain a constant hook load, which means the sum of the friction force and the nominal weight on bit (WOB) can be considered a constant value. The hook load can be calculated by static analysis of the drill-string under the condition that the frictional coefficient equals the static friction coefficient and that the nominal weight on bit equals zero and remains constant in the later calculation.

\[
T_t \big|_{s=0} = G_t - \text{WOB} - F_f = EA \frac{\partial u}{\partial s} \bigg|_{s=0}
\]  

(12)

where \( T_t \big|_{s=0} \) represents the hook weight, and \( G_t \) is the axial component of gravity of the entire drill-string.
To more clearly observe the effect of vibration on load transfer and WOB, we set the ROP to a constant value. Then, the displacement of the drill bit can be calculated by the following equation:

$$u_{j,t} = \text{ROP} \cdot t$$  \hspace{1cm} (13)

where ROP is rate of penetration, \(L\) is the entire length of the drill-string and \(t\) is time.

The hydraulic pulse generator begins to operate after the drill-string reaches a steady state. The pulse pressure excited by the hydraulic pulse generator is sine-shaped with an amplitude of \(P_0\) and a frequency of \(f\). This pulse pressure propagates upward and decreases with the increase in propagation distance, while its frequency remains constant. The pulse pressure applied on all shakers can be calculated by the following equations:

$$P_i(t) = P_0 \cdot \exp\left(-\frac{2}{aD} \sqrt{\frac{\pi \mu_p f}{\rho}} z_i\right) \cdot \sin(2\pi ft)$$  \hspace{1cm} (14)

$$F_{e,i}(t) = A_i P_i(t)$$  \hspace{1cm} (15)

$$\varphi_i = \frac{z_{i+1} - z_i}{a}$$  \hspace{1cm} (16)

where \(P_i(t)\) is the pulse pressure applied on the \(i\)th shaker \((i = 1, 2, 3, \ldots; \text{the first shaker is the one closest to the hydraulic pulse generator})\), \(P_0\) is the amplitude of the pulse pressure excited by the hydraulic pulse generator, \(z_i\) is the distance between the \(i\)th shaker and the hydraulic pulse generator, \(a\) is the propagation velocity of the pulse pressure inside the drill-string, \(D\) is the inner diameter of the drill-string, \(\mu_p\) is the viscosity of the drilling fluid, \(f\) is the frequency of the pulse pressure, \(F_{e,i}(t)\) is the exciting force of the \(i\)th shaker, \(A_i\) is the carrying area of the pulse pressure of each shaker and \(\varphi_i\) is the phase difference between the \((i+1)\)th shaker and the \(i\)th shaker, which means the time the \(i\)th shaker receives the pulse pressure is \(\varphi_i\) seconds earlier than the \((i+1)\)th shaker.

We assume the initial velocity of the entire drill-string equals zero. The initial displacement of the drill bit is set to zero, and the initial displacement of the other part of the drill-string can be calculated by the static force balance.

$$\frac{\partial u}{\partial t} |_{t=0} = 0$$  \hspace{1cm} (17)

$$u|_{t=0} = \Phi(T_i), u(L)|_{t=0} = 0$$

where \(\Phi\) is the initial displacement distribution of the drill-string.

**Solution method**

The finite difference method is chosen to solve the preceding model which is essentially an elastic wave propagation problem. Dispersing the governing differential equation by the central difference scheme, we transform the governing differential equations into algebraic equations and solve using MATLAB programming. First, the entire drill-string is divided into \(N\) units from the top to the bottom of the well. We set time step \(\tau\) and space step \(h\) and form difference grids. Then, the node displacement of the drill-string can be expressed as \(u(p \cdot h, k \cdot \tau)\), abbreviated \(u(p,k)\). In the governing differential equation, the nonlinear term \(\frac{\partial^2 u}{\partial x^2}\) occurs. To effectively address this nonlinear term, the governing differential equation is integrated for
random node $p$ in interval $[(p - \frac{1}{2})h, (p + \frac{1}{2})h]$. The following equation can be obtained:

$$
\left( \frac{EA}{h_s} \frac{\partial u}{\partial s} \right)^{p+\frac{1}{2}} - \left( \frac{EA}{h_s} \frac{\partial u}{\partial s} \right)^{p-\frac{1}{2}} = u(p, k + 1) - u(p, k) - u(p, k - 1) - \frac{2\pi}{\tau} \int_{(p-\frac{1}{2})h}^{(p+\frac{1}{2})h} \frac{u(p, k + 1) - u(p, k - 1)}{2\pi} ds + \int_{(p-\frac{1}{2})h}^{(p+\frac{1}{2})h} g \cos \theta ds
$$

(18)

where $\text{sgn}()$ is the sign function, $h$ is space size and $\tau$ is the time step.

We denote as follows:

$$
T^{p+\frac{1}{2}} = \left( \frac{EA}{h_s} \frac{\partial u}{\partial s} \right)^{p+\frac{1}{2}} = EA \frac{u(p + 1, k) - u(p, k)}{h}
$$

(19)

$$
T^{p-\frac{1}{2}} = \left( \frac{EA}{h_s} \frac{\partial u}{\partial s} \right)^{p-\frac{1}{2}} = EA \frac{u(p, k) - u(p - 1, k)}{h}
$$

(20)

$$
F_j(p, k) = \text{sgn}(u(p, k) - u(p, k - 1)) \int_{(p-\frac{1}{2})h}^{(p+\frac{1}{2})h} F_{jds}
$$

(21)

$$
C^{p} = \int_{(p-\frac{1}{2})h}^{(p+\frac{1}{2})h} c ds
$$

(22)

$$
A^{p} = \int_{(p-\frac{1}{2})h}^{(p+\frac{1}{2})h} \rho Ads
$$

(23)

$$
g^{p} = \int_{(p-\frac{1}{2})h}^{(p+\frac{1}{2})h} g \cos \theta ds
$$

(24)

If we substitute Eqs (19)–(24) into (18), we obtain the recurrence algorithm of drill-string axial displacement:

$$
u(p, k + 1) = \frac{2\tau^2}{2A^p + C^p} \left[ T^{p+\frac{1}{2}} - T^{p-\frac{1}{2}} - F_j(p, k) + g^{p} + \frac{2A^p}{\tau^2} u(p, k) + \left( \frac{C^p \tau - 2A^p}{2\tau^2} \right) u(p, k - 1) \right]
$$

(25)

The difference solution format (25) is explicit. If the displacement of the foregoing two time horizons is known, the displacement of the drill-string at any moment can be calculated. Then, the drilling parameters, such as the axial tension force and weight on bit, can be calculated.

To ensure the solution is convergent, time step $\tau$ and space step $h$ should satisfy a certain relationship. The convergence condition can be expressed as follows:

$$
\tau \leq \frac{h}{\sqrt{\rho}}
$$

(26)

**Results and discussion**

**Comparison of three vibration manners**

The purpose of earthworm-like drilling is to improve the friction reduction effect of the drill-string. At present, this technology only has application potential and requires additional study.
research if it is to be more effective than the single-point vibration approach, which is currently widely used, and multi-point vibration drilling, which is limited to maximum pumping pressure. In this section, the friction reduction effect of the three described vibration manners are compared. We adopt a horizontal well section with a length of 3000 m as an example and apply axial force $F_{\text{top}}$ on the top of the drill-string. The value of $F_{\text{top}}$ equals the static friction of the whole drill-string. Therefore, the WOB increment after applying vibration equals the friction force that is released. The other calculation parameters are as follows: $\mu_s = 0.35$, $\mu_d = 0.25$, ROP = 0.001 m/s, $P_0 = 4$ MPa, $a = 1200$ m/s, $f = 24$ Hz and $t = 50$ s. The bottom hole assemblies (BHAs) of the various drilling manners are shown in Fig 3. BHA-1, BHA-2, BHA-3 and BHA-4 are the bottom hole assemblies of single-point vibration drilling, three-point vibration drilling, three-point earthworm-like vibration drilling and five-point earthworm-like vibration drilling, respectively. All hydraulic pulse generators can generate positive pressure pulse, and the shakers can only receive this pulse pressure which gradually damps as the propagation distance increases. The hydraulic pulse generators simultaneously begin to operate when the time equals 0.5 seconds.

Fig 4 shows the influence of different vibrating manners on weight on bit. As can be observed from Fig 4, single-point vibration drilling has the lowest weight on bit, which indicates that single-point vibration drilling has the worst friction reduction effect. The order of the remaining three tested manners from worst to best are three-point earthworm-like drilling, three-point vibration drilling and five-point earthworm-like drilling. Multi-point vibration drilling is more effective than single-point vibration drilling under the same conditions. The drop-off of the friction reduction effect due to pulse pressure attenuation can be offset by

![Fig 3. Bottom hole assemblies (BHAs) of different drilling manners.](https://dx.doi.org/10.17504/protocols.io.3ctgn)
adding to the number of shakers. It is worth noting that the load transfer is not successive due to the stick-slip of the drill-string. However, the stick-slip is alleviated to a certain extent under vibrating conditions.

Fig 5 shows the maximum and root mean square acceleration of the drill-string during vibration. From Fig 5, single-point vibration drilling (i.e., BHA-1) has the highest average velocity and higher maximum velocity in most positions than earthworm-like drilling. The drill-string between the first and third shakers in three-point vibration drilling (i.e., BHA-2) has the highest maximum velocity. The five-point earthworm-like drilling (i.e., BHA-6) has the lowest maximum and average velocity, which means the motion of the drill-string in this manner is relatively gentle and homogeneous.

Fig 6 shows the maximum and root mean square acceleration along the drill-string during vibration. From Fig 6, the drill-string between the first and third shakers in three-point vibration drilling (i.e., BHA-2) has higher maximum acceleration. The maximum accelerations of the other vibration manners appear at 2250 m and gradually decay to both sides. The maximum acceleration of three-point earthworm-like drilling (i.e., BHA-3) is relatively low. The
The root mean square acceleration of all vibration manners is nearly the same and attains the maximum value at the position of the shakers.

From the preceding analysis, we can observe that the friction reduction and the load transfer effect of earthworm-like drilling are superior to those of single-point vibration drilling and multi-point vibration drilling due to its full use of pressure energy. Additionally, earthworm-like drilling has relatively low velocity and acceleration, which is good for drill-string life and downhole safety.

**Influence factors**

The load transfer effect of earthworm-like drilling is affected by many engineering parameters. In this section, we adopt three-point earthworm-like drilling (i.e., BHA-3) as an example to investigate the influence of the amplitude and frequency of the pulse pressure, the installation...
distance of the shakers and the phase difference of the exciting force on the load transfer characteristics of earthworm-like drilling.

The amplitude and frequency of the pulse pressure are the most important parameters of the hydraulic pulse generator and determine the exciting force of each shaker. Fig 7 shows the influence of the amplitude and frequency of the pulse pressure on the WOB. The frequency of pulse pressure \( f \) in Fig 7A is 24 Hz. From Fig 7A, the mean value of weight on bit increases gradually with the increase in the amplitude of the pulse pressure, while the fluctuation of weight on bit and stick-slip decrease with the increase in the amplitude of the pulse pressure. The reason for this phenomenon is that a larger proportion of the drill-string can move and maintain the dynamic friction state when the amplitude of the pulse pressure is higher. Therefore, the amplitude of the pulse pressure of the shakers should be improved to obtain larger WOB and a higher rate of penetration in the application process on the premise of maintaining safety. In addition to the amplitude of the pulse pressure, the frequency of the pulse pressure is another important parameter for earthworm-like drilling because of its influence on the attenuation and propagation distance of the pulse pressure. Fig 7B shows the influence of frequency on weight on bit under the condition \( P_0 = 2 \) MPa. From Fig 7B, WOB first increases and then decreases with the increase in frequency and reaches a maximum value when \( f = 96 \) Hz, which means 96 Hz is the optimum frequency for this case. The reason is that more drill-string can move and maintain the dynamic friction state as the frequency increases to 96 Hz. In addition, the amplitude of the pulse pressure gradually decays with the increase in frequency. The increase in frequency increases the vibration energy that acts on the drill-string while also increasing the attenuation of the pulse pressure amplitude and decreasing the propagation distance. Therefore, there is an optimal frequency value for each specific case.

As mentioned in the introduction, the mechanism of friction reduction by axially vibrating the drill-string includes (a) changing static friction to dynamic friction and (b) changing the friction direction. However, reversed friction is not conducive to the downward movement of the drill-string. Only the exciting force together with the buoyant weight of the drill-string behind the neutral point can push the drill-string downward. Based on these knowledge, the maximum increase in WOB after applying vibrations to the drill-string is equal to the friction
released by the entire drill-string changing from the static friction coefficient to the dynamic friction coefficient plus the amplitude of the exciting force. Therefore, if the frequency can be appropriately decreased and the amplitude of the pulse pressure can be improved simultaneously, the maximum weight on bit can further increase. Because the frequency is very low, we can temporarily term it earthworm-like wriggle drilling. Fig 8 shows the change in WOB under low frequencies (i.e., 2 Hz, 6 Hz and 10 Hz). From Fig 8, the increase in WOB increases with the increase in the pulse pressure amplitude and frequency at low frequency. To obtain higher WOB and compensate for the deficiency of low frequency, the amplitude of the pulse pressure should be appropriately adjusted. The preceding analysis verifies the feasibility of earthworm-like wriggle drilling.

Earthworm-like drilling requires mounting several shakers in the drill-string to guarantee friction reduction and the load transfer effect. If the vibrations generated by neighboring shakers overlap, the vibration of the drill-string in the overlap region will weaken or strengthen, which results in a poor friction reduction effect or drill-string fatigue damage. Therefore, the distance between shakers is an important parameter for earthworm-like drilling. Fig 9 shows
the effect of the distance between shakers on weight on bit and the acceleration distribution of the drill-string. From Fig 9A, the maximum and fluctuation amplitude of weight on bit increase as the distance between shakers decreases. As shown in Fig 9B and 9C, the maximum acceleration of the drill-string is significantly larger than root mean square acceleration. This phenomenon occurs because the instantaneous acceleration of a drill-string micro-element depends on its stress conditions. In this research, the stresses that act on a drill-string micro-element include the axial internal force, gravity and the frictional force. The axial internal force is influenced by the exciting force of the shakers. As is well-known, stick slip of the drill-string is inevitable in slide drilling. When a micro-element of the drill-string converts from the stick state to the slip state, the frictional force acting on this micro-element converts from static friction to dynamic friction which is relatively less. If the amplitude of the exciting force acts on this micro-element at this moment and the direction of the exciting force accords with the motion direction of the micro-element, the acceleration of the micro-element will reach its maximum value. However, the mean and root mean square accelerations of the micro-element are the concentrated...
expression of the acceleration during the entire simulation time. The change in the motion and state of the micro-element results in fluctuant acceleration, which makes the maximum acceleration of the micro-element is significantly larger than the mean or root mean square accelerations. In addition, it can be observed from Fig 9C that each shaker has an effective action distance. This effective action distance is determined by the vibration parameters, damping and the vibration system itself. From the standpoints of friction reduction and drill-string safety, it is better to have no overlap regions between the action distances of different shakers. Additionally, it is not beneficial for friction reduction if the border of action regions of neighboring shakers is too distant. From Fig 9C, the root mean square acceleration of most of the drill-string increases with the decrease in distance between shakers, which benefits friction reduction.

The discussion regarding the distance between shakers illustrated in Fig 9 includes the noticeable impact of the distance on WOB. In addition to the distance between shakers, the phase difference of the exciting force (i.e., the working time difference of shakers) may be another reason for this phenomenon. Fig 10 shows the influence of the phase difference of neighboring shakers on WOB and drill-string acceleration. The calculating parameters are as follows: frequency $f = 25$ Hz.

![Graphs showing effect of phase difference on WOB and accelerations](https://dx.doi.org/10.17504/protocols.io.kfbctin)

**Fig 10. Effect of phase difference of shakers on WOB and accelerations.** (A) Change in weight on bit in the bottom hole with time. (B) Maximum acceleration along the drill-string. (C) Root mean square acceleration along the drill-string. [https://dx.doi.org/10.17504/protocols.io.kfbctin](https://dx.doi.org/10.17504/protocols.io.kfbctin)
and amplitude of pulse pressure $P_0 = 4 \text{ MPa}$. The propagation velocities of the pressure wave are $1171.875 \text{ m/s}$ (for $0T$), $1153.8 \text{ m/s}$ (for $T/4$), $1136.4 \text{ m/s}$ (for $T/2$) and $1119.4 \text{ m/s}$ (for $3T/4$).

From Fig 10A we can observe that the phase difference has no influence on the maximum and minimum value of weight on bit. Indirectly we can deduce that WOB is not affected by the pressure pulse velocity. From Fig 10B and 10C we can observe that there is little difference between the maximum and root mean square accelerations of the drill-string under different phase differences. Based on the preceding analysis, we conclude that phase difference has little influence on drill-string friction reduction and load transfer. Therefore, the propagation velocity of the pulse pressure wave will not influence the application effect of earthworm-like drilling. The explanation for this phenomenon is that each shaker has an effective action distance due to the damping effect of the borehole wall and the drilling fluid. The phase difference does not influence the effective action distance of the shakers. If the distance between shakers is long enough, there is no interaction between them. The drill-string eventually reaches a steady vibration state, and the phase difference of the shakers does not create constructive and destructive interference.

Optimal model

The preceding investigations were performed in a horizontal hole section. The actual well track typically includes a straight section, a deviated section and a curved portion. Therefore, an optimal design based on the mathematical model developed in the Modeling section is required if earthworm-like drilling is to be applied in the field. To ensure the strength of the drill-string, axial force $T_t$ and variation amplitude of axial force $\Delta \bar{T}$ of the drill-string should be less than strength $T_{max}$ and fatigue strength $\Delta \bar{T}_{max}$, respectively, which typically have the following relationship $\bar{T}_{max} = (0.2 \sim 0.5)T_{max}$. In addition, the minimum interval of shakers $D_{min}$ should exceed a certain value in case vibrators interfere with one another. Considering the length of an on-site drill pipe is nine to ten meters, we set $D_{min} = 9 \text{ m}$. We combine the objective function and the constraint condition as follows:

$$\max f(x) = \Delta \text{WOB}$$

$$\begin{cases} 
T \leq T_{max} \\
\Delta \bar{T} \leq \Delta \bar{T}_{max} \\
x_{\text{excite}_{i+1}} - x_{\text{excite}_i} \geq D_{min}
\end{cases}$$

(27)

where $\Delta \text{WOB}$ is the increment of weight on bit, $\Delta \bar{T}$ is the variation amplitude of the axial force, $T_{max}$ is the strength of the drill-string, $\Delta \bar{T}_{max}$ is the fatigue strength of the drill-string and $x_{\text{excite}_i}$ is the position of the $i$th shaker.

We rewrite Eq (27) in the standard form of a nonlinear constrained optimization problem:

$$\min f(x) = \min(-\Delta \text{WOB}) \quad x \in \mathbb{R}^n, y \in \mathbb{R}^m$$

$$\begin{cases} 
p_i(x,y) \geq 0 \\
y = h(x)
\end{cases}$$

(28)

where $f(x)$ is the objective function, $x$ is the parameter that requires optimization and which must be solved by the model developed in section two and $y = h(x)$ is the procedure parameter.

We substitute $y = h(x)$ into constraint condition $p_i(x,y) \geq 0$. Eq (28) can be further simplified as follows:

$$\min f(x) = \min(-\Delta \text{WOB}) \quad x \in \mathbb{R}^n$$

$$\begin{cases} 
g_i(x) \geq 0 \\
i = 1, 2, \ldots, m
\end{cases}$$

(29)

where $g_i(x) \geq 0$ is the constraint condition.
In this paper, the nonlinear optimization problem is solved by the projection gradient method. Because the constraint conditions include the nonlinear condition, we must linearize the nonlinear constraint conditions before solving. The partial derivative of \( g(x) \) with respect to \( x \) can be calculated using the interpolation method:

\[
\frac{\partial g_i}{\partial x_j} = g_i(\ldots, x_{j-1}, x_j + \Delta x_j, x_{j+1}, \ldots) - g_i(\ldots, x_{j-1}, x_j, x_{j+1}, \ldots) \quad i = 1, \ldots, m; j = 1, \ldots, n \tag{30}
\]

Calculating all \( \frac{\partial g_i}{\partial x_j} \) each time, \( n + 1 \) points are required for approximate calculation. Assuming the original value of the \( k \) step iteration \( x^{(k-1)} = [x_1^{(k-1)}, x_2^{(k-1)}, \ldots] \), and taking the first-order approximations of the Taylor series expansion of \( g(x) \) near \( x^{(k-1)} \), we obtain:

\[
g(x) = g(x^{(k-1)}) + \sum_{j=1}^{n} \frac{\partial g_j}{\partial x_j} (x_j - x_j^{(k-1)}) \tag{31}
\]

\( g(x^{(k-1)}) \) and \( \frac{\partial g_j}{\partial x_j} \) are constant for every iteration. Thus, the constraint conditions are converted into a first-order form, which means that the constraint can be expressed as the sum of the product of the matrix, the unknown quantity and a constant. Then, the nonlinear constraint problem (Eq (29)) is translated into the following linear constraint problem:

\[
\begin{align*}
\min f(x) &= \min \left( -\Delta \text{WOB} \right) & x \in \mathbb{R}^n \\
\text{s.t.} & \quad Ax + b \geq 0
\end{align*}
\tag{32}
\]

where \( A_y = \frac{\partial g_j}{\partial x_j}, b_j = g(x^{(k-1)}) - \sum_{j=1}^{n} \frac{\partial g_j}{\partial x_j} x_j^{(k-1)} \).

This linearly constrained problem can be solved by the projection gradient method after linearization. The calculation steps are as follows:

(a) Taking the initial feasible point \( x^{(0)} \), i.e. \( Ax^{(0)} + b \geq 0 \), permissible error \( e > 0 \), let \( k = 0 \).

(b) Calculating \( I(x^{(k)}) = \{ i | \sum_{j=1}^{n} A_i x_j + b_i = 0, i = 1, \ldots, m \} \) and dividing \( A \) and \( b \) into \( a = (A_1, A_2), b = \left( \begin{array}{c} b_1 \\ b_2 \end{array} \right) \), make \( A_1 x^{(k)} = b_1, A_2 x^{(k)} > b_2 \).

(c) If \( I(x^{(k)}) = \emptyset \), then \( P = I \); otherwise, \( P = I - A_1 (A_1^T A_1)^{-1} A_1^T \).

(d) Let \( d^{(k)} = -P \nabla f(x^{(k)}) \). If \( ||d^{(k)}|| \leq e \), go to step (f), otherwise, go to Step e.

(e) Find \( \alpha_k > 0 \), and make \( f(x^{(k)} + \alpha_k d^{(k)}) = \min_{0 \leq \alpha \leq \alpha_k} f(x^{(k)} + \alpha d^{(k)}) \), where

\[
\alpha_0 = \left\{ \begin{array}{c}
\min \left\{ \left( A_2^T x - b_2 \right) \mid (A_2^T d)_i < 0 \right\} \\
\infty, \\
\left( A_2^T d \right)_i \geq 0
\end{array} \right. 
\]

Otherwise let \( x^{(k+1)} = x^{(k)} + \alpha_k d^{(k)} \), \( k = k + 1 \), and go to Step (b).

(f) Calculating \( \lambda = (A_1^T A_1)^{-1} A_1^T \nabla f(x^{(k)}) \), if \( \lambda \geq 0 \), then, \( x^{(k)} \) is the optimal solution, else let \( \lambda_i = \min \{ \lambda_j \} < 0, A_i = (a_{i_1}, \ldots, a_{i_{n-1}}, a_{i_n}, \ldots, a_{i_k}), P = I - A_i (A_i^T A_i)^{-1} A_i^T, d^{(k)} = -P \nabla f(x^{(k)}) \), and go to Step (e).

We adopt an ideal horizontal well as an example. The depth of the well is 4200 m. The kick-off point and the landing point are 1290 m and 2190 m, respectively, and the build-up rate is 0.0524 rad/30 m. The drill-string consists of Ø127 mm drill pipe. Other parameters used in this example are listed in Table 1.
The positions of the shakers are optimized to obtain maximum WOB by applying the previously described optimization method. The initial mount positions of the three shakers are 1740 m, 2945 m and 3700 m. The hydraulic pulse generator is mounted at the same position as the first shaker nearest the drill bit. The amplitude and frequency of the pulse pressure excited by the hydraulic pulse generator are 4 MPa and 30 Hz, respectively. Fig 11 shows the change in WOB over time before and after shaker position optimization. From Fig 11, WOB increases about 30 KN after optimizing the positions of the shakers in the drill-string. The new positions of the shakers are 2684 m, 3300 m and 3921 m. Compared with their initial positions, the shakers move toward the bottom of the well. The reason is that the friction between the horizontal segment of the drill-string and the borehole is larger than that of the building-up section on the premise of ignoring the effect of the bending moment on the normal contact force. Setting the positions of shakers in the horizontal segment is conducive to decreasing friction. In addition, the shakers move close to one another after position optimization because of the influence of shaker position on weight on bit, as discussed in the section Influence factors.

Table 1. Parameters used in the example.

| Parameter                  | Value          |
|----------------------------|----------------|
| drill-string outer diameter | 127 mm         |
| drill-string inner diameter | 108.6 mm       |
| density (g/cm³)             | 7.85           |
| elasticity modulus (GPa)    | 210            |
| static frictional coefficient | 0.35          |
| dynamic frictional coefficient | 0.25          |
| time size τ (s)             | 0.0005         |
| space size h (m)            | 5              |
| bottom hole ROP (m/s)       | 0.001          |
| initial WOB (N)             | 0              |

https://dx.doi.org/10.17504/protocols.io.kf6cti6

Fig 11. Comparison of WOB and positions of shakers before and after position optimization. (A) Change in weight on bit with time. (B) Change of positions of shakers. https://dx.doi.org/10.1371/journal.pone.0194582.g011
Conclusions

A new friction reduction technology, termed “earthworm-like drilling” is proposed in this paper. A mathematical model based on a “soft-string” model is established to verify the technology’s feasibility and advantages. A comparison of three vibration manners reveals that multi-point vibration drilling is more effective than single-point vibration drilling under the same conditions. Compared with multi-point simultaneous vibration, the decrease in the friction reduction effect of earthworm-like drilling due to pressure pulse attenuation can be offset by increasing the number of shakers. The amplitude and frequency of the pulse pressure and the installation position of the shakers have a substantial impact on friction reduction and the load transfer effect. Frequency also affects the attenuation and propagation distance of the pulse pressure aroused by the hydraulic vibrators. In addition, an optimization model based on the projection gradient method is established and used to optimize the position of three shakers of a horizontal well. WOB increases significantly after the position optimization. The new positions of the shakers move toward the bottom of well, and the shakers are close to one another. Based on the discussion of the feasibility, advantages and influence factors of earthworm-like drilling presented in this paper, earthworm-like drilling is a technology with broad application prospects.

Nomenclature

Roman symbols:

- \( a \) propagation velocity of pressure pulse inside the drill-string, m/s
- \( A \) cross-section area of drill-string, \( m^2 \)
- \( A_c \) carrying area of pressure pulse of each shaker, \( m^2 \)
- \( c \) drilling fluid drag, \( N \cdot s/m^2 \)
- \( D \) inner diameter of drill-string, m
- \( D_{min} \) minimum interval of vibrators, m
- \( E \) elastic(Young’s) modulus of drill-string, Pa
- \( \vec{e}_g \) vector of submerged drillstring weight
- \( \vec{e}_n, \vec{e}_b \) unit base vectors in natural curvilinear system
- \( f \) frequency of vibration, Hz
- \( f(x) \) objective function
- \( F, F_n, F_b \) normal contact force and its components in \( \vec{e}_n \) and \( \vec{e}_b \) direction, N
- \( F_e \) exciting force, N
- \( F_f \) axial friction force, N
- \( F_{top} \) hook load, N
- \( g_s \) linear buoyant weight of drill-string, N/m
- \( g(x) \) constraint condition
- \( G_t \) axial component of gravity of the whole drill-string, N
- \( k_\alpha \) rate of change of deviation angle, rad/m
- \( k_\phi \) rate of change of azimuth angle, rad/m
- \( k_b \) total bending curvature, rad/m
- \( L \) length of drill-string, m
- \( P \) pressure pulse applied each shaker, Pa
- \( P_0 \) pressure pulse amplitude excited by hydraulic pulse generator, Pa
- \( P' \) pressure pulse amplitude after propagating \( x \), Pa
- \( q \) propagation distance of pressure pulse, m
- ROP rate of penetration, m/s
Greek symbols:

- $\alpha$: deviation angle, rad
- $\varphi$: azimuth angle, rad
- $\Phi$: initial displacement distribution of drill-string, m
- $\bar{\alpha}$: mean deviation angle, rad
- $\rho$: density of drill-string, kg/m$^3$
- $\mu$: instantaneous friction coefficient in $\overrightarrow{e}_i$, direction
- $\mu_s$: static friction coefficient
- $\mu_d$: is dynamic friction coefficient
- $\mu_{pv}$: viscosity of drilling fluid, Pa $\cdot$ s

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