Strong- to weak-coupling superconductivity in high-Tc bismuthates: Revisiting the phase diagram via SR

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Abstract: Several decades after the discovery of superconductivity in bismuthates, the strength of their electron-phonon coupling and its evolution with doping remain puzzling. To clarify these issues, polycrystalline hole-doped Ba$_{1-x}$K$_x$BiO$_3$ (0.1 ≤ x ≤ 0.6) samples were systematically synthesized and their bulk and microscopic superconducting properties were investigated by means of magnetic susceptibility and muon-spin rotation and relaxation (SR), respectively. The phase diagram of Ba$_{1-x}$K$_x$BiO$_3$ was reliably extended up to x=0.6, which is still found to be a bulk superconductor. The lattice parameter a increases linearly with K content, implying a homogeneous chemical doping. The low-temperature superfluid density, measured via transverse-field SR, indicates an isotropic fully gapped superconducting state with zero-temperature gaps ∆0/kBTc = 2.15, 2.10, and 1.75, and magnetic penetration depths λ0 = 219, 184, and 279 nm for x = 0.3, 0.4, and 0.6, respectively. A change in the superconducting gap, from a nearly ideal BCS value (1.76kB Tc in the weak-coupling case) in the overdoped x = 0.6 region, to much higher values in the optimally doped case, implies a gradual decrease in electron-phonon coupling with doping.

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Strong-to weak-coupling superconductivity in high-$T_c$ bismuthates: Revisiting the phase diagram via $\mu$SR

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Several decades after the discovery of superconductivity in bismuthates, the strength of their electron-phonon coupling and its evolution with doping remain puzzling. To clarify these issues, polycrystalline hole-doped Ba$_{1-x}$K$_x$BiO$_3$ (0.1 $\leq x \leq$ 0.6) samples were systematically synthesized and their bulk and microscopic superconducting properties were investigated by means of magnetic susceptibility and muon-spin rotation and relaxation ($\mu$SR), respectively. The phase diagram of Ba$_{1-x}$K$_x$BiO$_3$ was reliably extended up to $x$ = 0.6, which is still found to be a bulk superconductor. The lattice parameter $a$ increases linearly with $K$ content, implying a homogeneous chemical doping. The low-temperature superfluid density, measured via transverse-field $\mu$SR, indicates an isotropic fully gapped superconducting state with zero-temperature gaps $\Delta_0/k_B T_c$ = 2.15, 2.10, and 1.75, and magnetic penetration depths $\lambda_0$ = 219, 184, and 279 nm for $x$ = 0.3, 0.4, and 0.6, respectively. A change in the superconducting gap, from a nearly ideal BCS value (1.76$k_B T_c$ in the weak-coupling case) in the overdoped $x = 0.6$ region, to much higher values in the optimally doped case, implies a gradual decrease in electron-phonon coupling with doping.

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I. INTRODUCTION

Decades ago, superconductivity (SC) with critical temperatures $T_c$ up to 34 K was discovered in perovskite-type bismuthates [1–3]. Despite extensive studies using various techniques, their pairing mechanism is still under debate [3]. The parent compound BaBiO$_3$ is an insulator, which exhibits charge-density-wave (CDW) order and undergoes multiple structural phase transitions [4–6]. The suppression of the insulating character and of the CDW order upon Ba/K or Bi/Pb substitutions eventually leads to a superconducting phase in Ba$_{1-x}$K$_x$BiO$_3$ or BaBi$_{1-y}$Pb$_y$O$_3$ [3], with the highest $T_c$ reaching 34 K near $x_K$ $\sim$ 0.37 [see Fig. 1(c)]. Neutron powder-diffraction measurements show that, for 0.2 $\leq x \leq$ 0.37, Ba$_{1-x}$K$_x$BiO$_3$ exhibits a cubic-to-orthorhombic phase transition before entering the superconducting phase, while for $x \geq 0.37$, the cubic structure persists down to the superconducting phase [7,8]. However, close to $x = 0.32$, a mixture of different phases has also been found [8]. According to our Rietveld refinements of x-ray powder diffraction (XRD) data, samples with 0.1 $\leq x \leq$ 0.25 exhibit a mixture of orthorhombic and cubic phases [9]. Later on, it was confirmed that, at low temperatures, the distortion observed in the superconducting Ba$_{1-x}$K$_x$BiO$_3$ samples with $x$ $\sim$ 0.32–0.4 is more consistent with a tetragonal symmetry [10]. Systematic studies of the Ba$_{1-x}$K$_x$BiO$_3$ crystal structure as a function of doping and temperature are clearly not only in high demand, but also crucial to understand their properties. Indeed, bismuthates rank among the most interesting systems, where the interplay between structural, charge, and electronic instabilities gives rise to new and remarkable phenomena.

According to the phase diagram shown in Fig. 1, the lack of either magnetic order or magnetic fluctuation in bismuthates hints at a nonmagnetic superconducting pairing. To date, two pairing mechanisms, in the two extremes of coupling strengths, have been proposed in order to explain the unexpectedly high $T_c$ of doped bismuthates. One mechanism considers a strong coupling of electrons to high-energy phonon modes, leading to the formation of polarons. The polaron then bind into Cooper pairs through a retarded electron-phonon interaction with the low-energy phonon modes [11–13]. Recently, a large electron-phonon coupling constant $\lambda_{ep}$ $>$ 1, strong enough to account for the high $T_c$ in Ba$_{1-x}$K$_x$BiO$_3$, has been experimentally and theoretically proposed [14,15]. An alternative mechanism suggests that the pairing is mediated by high-energy charge excitations [16]. This mechanism does not require a strong coupling; i.e., the superconducting energy gap can be close to 1.76$k_B T_c$, the canonical weak-coupling BCS-theory value.
suggest a \textit{doping-dependent coupling strength}, a scenario which does not exclude either of the above mechanisms, thus accounting for the widely different experimental results.

To validate the above hypothesis on the evolution of the coupling strength with doping, the study of the superconducting gap and of its symmetry across the entire phase diagram of Ba$_{1-x}$K$_x$BiO$_3$ is crucial, in particular in the overdoped region, mostly overlooked due to the lack of high-quality samples. Here, by improving the synthesis conditions, we could obtain high-quality Ba$_{1-x}$K$_x$BiO$_3$ samples (0.1 \( \leq x \leq 0.6 \)), of which those with \( x = 0.3-0.6 \) show bulk superconductivity. In this paper, we report on the systematic magnetization and muon-spin rotation and relaxation (\( \mu \)SR) investigation of the hole-doped Ba$_{1-x}$K$_x$BiO$_3$ system in the range 0.1 \( \leq x \leq 0.6 \). By using transverse-field (TF) \( \mu \)SR measurements, we study the microscopic superconducting properties, including the gap symmetry, the zero-temperature magnetic penetration depth, and the gap values across the whole superconducting phase region of Ba$_{1-x}$K$_x$BiO$_3$ to clearly demonstrate the decrease of the SC coupling strength with doping.

\section*{II. EXPERIMENTAL DETAILS}

Polycrystalline Ba$_{1-x}$K$_x$BiO$_3$ samples were synthesized via solid-state reaction methods \cite{9}. The room-temperature XRD, measured using a Bruker D8 diffractometer, confirmed the samples’ purity and the lack of extra phases. The atomic ratios in the various Ba$_{1-x}$K$_x$BiO$_3$ samples were measured by x-ray fluorescence (XRF) spectroscopy on an AMETEK Orbis Micro-XRF analyzer. The linear behavior of the in-plane lattice parameter (extracted from the Rietveld refinements; see Fig. 1(a) and the Supplemental Material \cite{9}) vs K content indicates the successful and homogeneous Ba/K substitution in all the studied samples [see inset in Fig. 1(b)]. The magnetic susceptibility measurements were performed on a Quantum Design magnetic property measurement system (MPMS). The bulk \( \mu \)SR measurements were carried out at the general-purpose (GPS), the multipurpose (Dolly), and the high-field and low-temperature (HAL-9500) surface-muon spectrometers at the Swiss muon source of Paul Scherrer Institut, Villigen, Switzerland. The \( \mu \)SR data were analyzed by means of the \textsc{musrfit} software package \cite{18}.

\section*{III. RESULTS AND DISCUSSION}

\textbf{Characterization of bulk superconductivity.} The superconductivity of Ba$_{1-x}$K$_x$BiO$_3$ (0.1 \( \leq x \leq 0.6 \)) was characterized by magnetic susceptibility measurements, performed in a 1-mT field, using both field-cooled (FC) and zero-field-cooled (ZFC) protocols. As shown in Fig. 2(a), the ZFC susceptibility, corrected to account for the demagnetization factor, indicates bulk superconductivity below \( T_c = 29.5, 26.5, \text{ and } 10.3 \) K for \( x = 0.3, 0.4, \text{ and } 0.6 \), respectively. For \( x \leq 0.2 \), no superconducting transition could be detected down to 1.8 K. For \( x = 0.25 \), the \( \chi(T) \) curve shows a superconducting transition at 25 K with a rather small superconducting fraction (below 1%). The other samples, with a K content between 0.3 and 0.4, exhibit bulk superconductivity, too (see the phase diagram). To perform TF-\( \mu \)SR measurements on superconductors, the applied magnetic field should exceed the lower

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure1.png}
\caption{(a) A typical room-temperature XRD pattern and Rietveld refinements for Ba$_{0.5}$K$_{0.5}$BiO$_3$. The crystal structure is shown in the inset. (b) Structural and superconducting phase diagram of Ba$_{1-x}$K$_x$BiO$_3$, constructed according to Refs. \cite{3,6,7}. The inset shows the in-plane lattice parameter as a function of K content, with the red symbols referring to data to Ref. \cite{7} and the blue symbols to our XRD data. For 0.1 \( \leq x \leq 0.25 \), due to a mixture of phases, the relevant lattice parameter is not shown. (c) Enlarged symbols to our XRD data. For 0.1 \( \leq x \leq 0.6 \), of which those with \( x = 0.3-0.6 \) show bulk superconductivity.}
\end{figure}
critical field $\mu_0 H_1$, so that the additional field-distribution broadening due to the flux-line lattice (FLL) can be quantified from the field-dependent magnetization, as obtained from a linear fit to the $M(H)$ data for $x = 0.3$ case at several temperatures below $T_c$. Here, $\Delta M(H) = M(H) - M_{\text{linear}}(H)$, where $M_{\text{linear}}$ is the linear low-field magnetization, as obtained from a linear fit to the $M(H)$ data (see Fig. S2 in the Supplemental Material [9]). As indicated by the dashed line, at $\mu_0 H_1$, $\Delta M(H)$ starts deviating from zero value. The $M(H)$ data for all the samples are reported in the Supplemental Material [9]. The estimated $\mu_0 H_1(T)$ values are shown in the main panel of Fig. 2(b) as a function of temperature. The solid lines represent fits to $\mu_0 H_1(T) = \mu_0 H_1(0) [1 - (T/T_c)^2]$ and yield lower critical fields of about 8 mT for all the Ba1$_x$K$_{1-x}$BiO$_3$ samples (see details in Table I).

Transverse-field $\mu$SR. The TF-$\mu$SR time spectra were collected at various temperatures up to $T_c$, following a FC protocol. To track the additional field-distribution broadening due to the FLL in the mixed superconducting state, a magnetic field of 50 mT, i.e., rather large compared to the lower critical fields of Ba1$_x$K$_{1-x}$BiO$_3$, was applied above $T_c$. Figure 3(a) shows two representative TF-$\mu$SR spectra for Ba1$_{0.3}$K$_{0.7}$BiO$_3$, collected above and below $T_c$, with the other samples showing similar features. The enhanced depolarization rate below $T_c$ reflects the inhomogeneous field distribution due to the FLL, causing an additional distribution broadening in the mixed superconducting state, as clearly seen from the fast-Fourier-transform (FFT) spectra shown in Figs. 3(b) and 3(c). Since the relaxations are mostly Gaussian-like, the TF-$\mu$SR asymmetry could be modeled by

$$A_{\text{TF}} = A_i \cos(\gamma \mu B t + \phi) e^{-\sigma^2/2} + A_{bg} \cos(\gamma \mu B_{bg} t + \phi).$$

Here $A_i$ and $A_{bg}$ represent the initial muon-spin asymmetries for muons implanted in the sample and sample holder (i.e., background), respectively, with the latter not undergoing any depolarization. $B_i$ and $B_{bg}$ are the local fields sensed by implanted muons in the sample and sample holder, $\gamma \mu = 2\pi \times 135.53$ MHz/T is the muon gyromagnetic ratio, $\phi$ is the shared initial phase, and $\sigma$ is a Gaussian relaxation rate. Given the nonmagnetic nature of the sample holder, $B_{bg}$ coincides with the applied magnetic field [see dashed line in Figs. 3(b) and 3(c)] and was used as an intrinsic reference.

In the superconducting state, the measured Gaussian relaxation rate $\sigma$ includes contributions from both the FLL ($\sigma_{\text{sc}}$) and a temperature-invariant relaxation due to nuclear magnetic moments ($\sigma_{\text{n}}$) (see also ZF-$\mu$SR below). The FLL-related relaxation can be extracted by subtracting the nuclear contribution according to $\sigma_{\text{sc}} = \sqrt{\sigma^2 - \sigma_{\text{n}}^2}$. For small applied magnetic fields [with respect to the upper critical field $H_{c2}$ ($H_{\text{appl}}/H_{c2} \ll 1$)], the magnetic penetration depth $\lambda$ can be obtained from $\sigma_{\text{sc}}(T)$ [19,20]:

$$\frac{\sigma_{\text{sc}}^2(T)}{\gamma \mu^2} = 0.00371 \frac{\Phi_0^2}{\lambda^4(T)},$$

with $\Phi_0$ the quantum of magnetic flux. For Ba1$_x$K$_{1-x}$BiO$_3$, $H_{c2}$ is much higher than the applied magnetic field [21,22], implying the validity of the above equation. The derived inverse square of the magnetic penetration depth (proportional to the superfluid density $\rho_s$) is shown normalized to the zero-temperature values in Fig. 4. The temperature-independent

| Parameter | $x = 0.3$ | $x = 0.4$ | $x = 0.6$ |
|-----------|-----------|-----------|-----------|
| $T_c(\chi)$ (K) | 29.0 | 26.5 | 10.3 |
| $T_c(\mu$SR) (K) | 28.9 | 25.5 | 9.1 |
| $\mu_0 H_1$ (mT) | 7.7 | 8.4 | 7.8 |
| $\Delta_0 (k_B T_c)$ | 2.15 | 2.10 | 1.75 |
| $\Delta_0$ (meV) | 5.35 | 4.61 | 1.37 |
| $\lambda_0$ (nm)$^2$ | 219 | 184 | 279 |

*Derived from TF 50 mT $\mu$SR measurements.

**TABLE I. Superconducting parameters of Ba$_{1-x}$K$_x$BiO$_3$ as determined from magnetization and TF-$\mu$SR and fit parameters related to ZF-$\mu$SR data collected above and below $T_c$ in Ba$_{0.3}$K$_{0.7}$BiO$_3$.
behavior of the superfluid density for $T/T_c < 1/3$ clearly suggests the absence of excitations and, therefore, a nodeless $s$-wave superconductivity in Ba$_{1-x}$K$_x$BiO$_3$. By converse, for a nodal superconductor, the superfluid density is expected to depend on temperature below $T_c/3$, as examples in $p$- or $d$-wave superconductors [23,24]. To gain further insight into the superconducting pairing symmetry of Ba$_{1-x}$K$_x$BiO$_3$, the temperature-dependent superfluid density $\rho_{sc}(T)$ was further analyzed by using a fully gapped $s$-wave model:

$$\rho_{sc}(T) = 1 + 2 \int_{\Delta(T)}^{\infty} \frac{E}{\sqrt{E^2 - \Delta^2(T)}} \frac{\partial f}{\partial E} dE,$$

(3)

where $f = (1 + e^{E/k_B T})^{-1}$ is the Fermi function and $\Delta(T)$ is the superconducting gap function. The temperature variation of the superconducting gap is assumed to follow $\Delta(T) = \Delta_0 \tanh[1.82(1.018(T_c/T - 1))^{0.51}]$ [25], where $\Delta_0$, the zero-temperature gap value, is the only adjustable parameter. The solid lines in Fig. 4 are fits to a single-gap $s$-wave model, which yields magnetic penetration depths

FIG. 4. Normalized superfluid density vs temperature, as determined from TF-μSR measurements for (a) $x = 0.3$, (b) $x = 0.4$, and (c) $x = 0.6$. The solid lines represent fits to a fully gapped $s$-wave model (see text). For $x = 0.4$, the GPS data are highly consistent with those reported in Ref. [17] collected in a field of 200 mT. The tiny mismatch between the theoretical value and experimental data near $T_c$ might be related to the broad superconducting transition (see Fig. 2). The fitting parameters are summarized in Table I.

$\lambda_0 = 219(3)$, 184(2), and 279(2) nm, and gap values $\Delta_0/k_B T_c = 2.15(2)$, 2.10(3), and 1.75(3), for $x = 0.3$, 0.4, and 0.6, respectively. The data sets at higher fields (500 and 200 mT for $x = 0.3$ and 0.4, respectively) exhibit almost identical features as those at 50 mT, further confirming the single-gap nature of superconductivity in the Ba$_{1-x}$K$_x$BiO$_3$ family. Close to optimal K doping (e.g., $x = 0.3$ and 0.4), the derived gap values are significantly larger than the BCS value of $1.76 k_B T_c$, while upon overdoping (e.g., $x = 0.6$), the gap is more consistent with the BCS value in the weak-coupling limit. Since normally the SC gap scales with the coupling strength, a progressive increase of K doping in Ba$_{1-x}$K$_x$BiO$_3$, from the optimal- to the over-doped regime, seems to correspond to a change from strong to weak electron-phonon coupling. While from these results one can infer that the overall coupling constant $\lambda_{ep}$ decreases, this can potentially be weakened also by a reduction in the density of states at $E_F$, rather than a decrease in the electron-phonon scattering matrix elements per se [26]. In any case, the fully gapped state and the strong electron-phonon coupling are also supported by recent photoemission measurements [14].
In Ba_{1-x}K_{x}BiO_{3} the regime, this behavior becomes more complex and shows a nonmonotonic dependence of the superfluid density and the critical temperature [28,29]. When moving across the optimal doping towards the overdoped regime, the cuprates show a linear relationship between the superfluid density and the carrier density (known also as superfluid density s) and the superfluid density decrease significantly. To conclude whether a "boomerang"-like (i.e., nonmonotonic) behavior is confirmed also here, further doping values are required. In addition, for an independent access to the coupling strength \( \lambda \) of the asymmetry correspond to the powder average of the local internal fields with respect to the initial muon-spin direction. The solid lines in Fig. 5 represent fits to each data set by considering an additional Lorentzian relaxation \( A_2 \), i.e., \( A_{ZF} = A_1 G_{KTe} e^{-t/T_c} + A_{bg} \). Here \( A_1 \) and \( A_{bg} \) are the same as in the TF-\( \mu \)SR case [see Eq. (1)].

The resulting fit parameters are also summarized in Table I. The weak Gaussian and Lorentzian relaxation rates reflect the small nuclear moments in Ba_{1-x}K_{x}BiO_{3}. In both the normal and the superconducting states, the relaxations are very similar (within the experimental error), as demonstrated by the practically overlapping ZF-\( \mu \)SR spectra above and below \( T_c \). This lack of evidence for an additional \( \mu \)SR relaxation below \( T_c \) excludes a possible TRS breaking in the superconducting state of Ba_{1-x}K_{x}BiO_{3}.

IV. DISCUSSION

In this study we pursued a twofold goal: to reliably extend and revisit the superconducting phase diagram of Ba_{1-x}K_{x}BiO_{3} and to reconcile the seemingly contradictory mechanisms put forward to explain its superconductivity.

As for the first point, Ba_{1-x}K_{x}BiO_{3} represents a very interesting system among oxide superconductors, to be compared against the cuprates. Prominent differences include the isotropic character of Ba_{1-x}K_{x}BiO_{3} and its lack of half-filled d orbitals, in contrast to the two-dimensional nature of cuprates that contain Cu in a 3d\(^{9}\) state. However, detailed studies, as the one presented here, have been hampered by the lack of high-quality Ba_{1-x}K_{x}BiO_{3} single crystals. Due to the high reactivity and volatility of K\(_2\)O, bulk Ba_{1-x}K_{x}BiO_{3} samples can only be prepared in a vacuum or dry environment (often at low temperatures), or by means of high-pressure and high-temperature techniques. Our successful systematic synthesis of Ba_{1-x}K_{x}BiO_{3} phase diagram using different techniques and to confirm once more (this time over the whole phase diagram, and not only for one composition, as in Ref. [14]), the conventional nature of its superconductivity.

As for the second point, over the years, different experimental techniques (e.g., photoemission, tunneling, and optics) have provided conflicting estimates for the electron-phonon coupling strength \( \lambda_{ep} \) in Ba_{1-x}K_{x}BiO_{3}. Such enduring controversy has been complicated by the fact that only rarely were high-quality materials available across the whole K-doping range and not always could they be studied systematically. By showing that the coupling regime is doping dependent, our systematic \( \mu \)SR investigation of the entire family finally clarifies this long-standing issue and offers new insights concerning the pairing mechanism in Ba_{1-x}K_{x}BiO_{3}.

V. SUMMARY

By successfully synthesizing high-quality samples of the Ba_{1-x}K_{x}BiO_{3} bismuthates (with \( x \) up to 0.6), we could systematically revisit their superconducting phase diagram. Bulk superconductivity in the range 0.3 \( \leq x \leq 0.6 \) (with \( T_c \sim 10-30\,K \)) was characterized by magnetization measurements, followed by microscopic \( \mu \)SR experiments. The temperature variation of the superfluid density, as determined via TF-\( \mu \)SR, reveals a fully gapped superconductivity in...
Ba$_{1-x}$K$_x$BiO$_3$, independent of doping and is well described by an isotropic $s$-wave model. At the same time, the derived superconducting-gap values strongly suggest a doping-induced *crossover from strong- to weak-coupling*, a finding which can account for the seemingly contradictory models previously used to explain the superconductivity of the bismuthates. Finally, the lack of spontaneous magnetic fields below $T_c$, as revealed by ZF-$\mu$SR measurements, indicates that time-reversal symmetry is preserved in the superconducting state of Ba$_{1-x}$K$_x$BiO$_3$.

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