Spatially dependent electromagnetically induced transparency

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Recent years have seen vast progress in the generation and detection of structured light, with potential applications in high capacity optical data storage and continuous variable quantum technologies. Here we measure the transmission of structured light through cold rubidium atoms and observe regions of electromagnetically induced transparency (EIT). We use q-plates to generate a probe beam with azimuthally varying phase and polarisation structure, and its right and left circular polarisation components provide the probe and control of an EIT transition. We observe an azimuthal modulation of the absorption profile that is dictated by the phase and polarisation structure of the probe laser. Conventional EIT systems do not exhibit phase sensitivity. We show, however, that a weak transverse magnetic field closes the EIT transitions, thereby generating phase dependent dark states which in turn lead to phase dependent transparency, in agreement with our measurements.

Introduction: The coherent interaction of light with atoms can cause quantum interference between the excitation amplitudes of different optical transitions. This can dramatically change the optical response of a medium. Perhaps the most intriguing example of this is electromagnetically induced transparency (EIT) [1, 2], rendering a medium transparent for resonant probe light when simultaneously exposed to an additional control beam. The anomalous dispersion associated with the ‘transparency window’ has been exploited for the generation of slow and stopped light [3, 4], and related techniques have led to EIT based quantum memories which can store and retrieve optical information [5-9].

In this letter we report spatially varying optical transparency, achieved by exposing an atomic medium to a single light beam with an azimuthally varying polarisation and phase structure [10]. Such a light mode can be described as ‘classically entangled’ in its polarisation and angular position [11, 12]. If this light is driving a Hanle resonance [13], the left and right-handed circular polarisation components constitute the probe and control for the EIT transition respectively, leading to an azimuthal variation of the atomic dynamics.

It is well established that radially polarised light modes can be focused beyond the diffraction limit [15], and light with an azimuthal polarisation structure has been proposed for enhanced rotational sensing in so-called photonic gears [16]. The interaction of atoms with phase structured light has been exploited in a variety of experiments, for EIT systems [17-19] as well as for four-wave mixing [20]. Very recently the first phase-preserving quantum memory has been demonstrated by driving EIT transitions with light entangled in its polarisation and angular position [21, 22]. These experiments rely on the fact that phase-dependent optical information can be stored in EIT coherences. In contrast, here we generate spatially varying atomic dark states, rendering the atoms transparent to light at specific angular positions.

This self-modulation of the incident light beams effectively converts optical phase information into intensity information.

It has been shown theoretically that phase-dependent population dynamics require closed linkages between the excitation amplitudes [23]. In our case this is realised by coupling the EIT ground states via a weak transverse magnetic field. We provide a theoretical description of the phase-dependent interaction, before presenting the experimental set-up and our results.

Theory: We consider the atomic Λ system shown in Fig. 1. The atomic ground states, |g±1⟩, are Zeeman sublevels of the same hyperfine state with magnetic quantum numbers mF = ±1, coupled to the excited state |e⟩ by the left and right (±) circularly polarised components of a probe laser, respectively. In the absence of a magnetic field the process is two-photon resonant, providing ideal conditions for EIT. Any detuning from two-photon resonance:

\[
\int_{-\infty}^{\infty} g(\omega) \Delta \omega \propto |\langle e|\varphi(\omega)g\rangle|^2
\]

FIG. 1: EIT level scheme with phase dependent driving fields. a) Schematic of the atomic energy levels, optical coupling to the excited state (insets show phase represented as hue colour and intensity as saturation), and weak magnetic coupling between the ground states. b) Alternative level scheme expressed in terms of partially dressed states; the inset is a theoretical simulation of the absorption profile from |ψNC⟩ to |e⟩. Details in main text.
resonance results in reduced transparency. Here we are posing the question of whether the transparency of an atomic medium is also affected by a phase difference between the complex excitation amplitudes.

We consider probe light with an electric field amplitude

\[ \hat{E}(r, \varphi) = \frac{1}{\sqrt{2}} E_0(r) \left( \sigma_+ e^{-i\varphi} + \sigma_- e^{i\varphi} \right), \]

which is correlated in its spin and orbital angular momentum (OAM). Here \( \varphi \) denotes the azimuthal angle and \( \ell \) is an integer. A left circularly polarised photon then has a phase dependence \( e^{-i\varphi} \), corresponding to an OAM of \( -\ell h \), whereas a right circularly polarised photon has the opposite OAM [24, 25]. Each polarisation component has a uniform azimuthal intensity, with a central dark vortex opposite OAM [24, 25]. Each polarisation component has a uniform azimuthal intensity.

This light couples to the atoms via the dipole Hamiltonian

\[ \hat{H}_D = \hat{D} \cdot \hat{E} = \frac{\hbar \Omega}{\sqrt{2}} (e^{-i\varphi}|g_{-1}\rangle\langle e| + e^{i\varphi}|g_{+1}\rangle\langle e|) + h.c., \]

\[ = \hbar \Omega |g_c\rangle\langle e| + h.c. \]  

(2)

where \( E_0(r) \) is incorporated into the Rabi frequency \( \Omega = \Omega(r) \). The first line is expressed in terms of the atomic levels \( |g_{\pm 1}\rangle \), and in the second line we have introduced the \( \varphi \)-dependent partially dressed states

\[ |g_{C,NC}\rangle = \frac{1}{\sqrt{2}} (e^{-i\varphi}|g_{-1}\rangle \pm e^{i\varphi}|g_{+1}\rangle). \]  

(3)

Note that spontaneous emission causes decay with equal probability into each of the atomic ground states, so that an atom is driven out of the coupling state \( |g_c\rangle \) into the non-coupling state \( |g_{NC}\rangle \) or the unperturbed atomic state \( |g_0\rangle \) after very few absorption-emission cycles. This system exhibits phase-dependent coherences and could be employed for EIT based quantum memories for phase-encoded light. However, as \( |g_{NC}\rangle \) is rotationally symmetric, neither the atomic populations nor the absorption show phase dependence. This, of course, was expected, as phase-dependent populations require a closed loop level system, where atomic transitions combine interferometrically [23, 24].

A magnetic field, as long as it is not aligned with the probe beam propagation direction, will perturb the rotational symmetry. We consider an arbitrary magnetic field \( \mathbf{B} = B(\cos \theta \hat{z} + \sin \theta \hat{x}) \), where the light propagates along \( \hat{z} \) and for simplicity we have chosen \( \hat{x} \) to be the transverse direction of the B-field.

The total interaction Hamiltonian

\[ \hat{H} = \hat{H}_D + \hat{H}_B \]  

(4)

includes, in addition to (3), the magnetic interaction Hamiltonian, which in the weak field limit is:

\[ \hat{H}_B = g_F \mu_B \mathbf{F} \cdot \mathbf{B} \]

\[ = \hbar \beta \left[ \cos \theta \langle g_{+1}\rangle\langle g_{+1}| - \langle g_{-1}\rangle\langle g_{-1}| \right] \]

\[ - \hbar \beta \left| \frac{\sin \theta}{2} (\langle g_{0}\rangle\langle g_{+1}| + |g_{0}\rangle\langle g_{-1}| + h.c.) \right|, \]

where \( \mathbf{F} \) is the total angular momentum operator and we have defined the magnetic parameter \( \beta = g_F \mu_B B \). The first term describes the Zeeman shift of \( |g_{\pm 1}\rangle \) due to \( B_{\parallel} \), whereas the second term describes the mixing of \( |g_0\rangle \) with \( |g_{\pm 1}\rangle \), as illustrated in Fig. 1b). It is instructive to introduce a modified basis set of partially dressed states, combining \( |g_{NC}\rangle \) and \( |g_0\rangle \):

\[ |\psi_0\rangle = \frac{1}{N(\varphi)} \left[ -\cos \theta |g_{NC}\rangle + \sin \theta \cos (\ell \varphi)|g_0\rangle \right], \]

\[ |\psi_{NC}\rangle = \frac{1}{N(\varphi)} \left[ \sin \theta \cos (\ell \varphi)|g_{NC}\rangle + \cos \theta |g_0\rangle \right], \]

(6)

where \( N(\varphi) = \sqrt{1 - \sin^2 \theta \sin^2 (\ell \varphi)} \) ensures normalisation. Together with \( |g_c\rangle \) these form a complete basis set, in which the Hamiltonian (4) can be rewritten as

\[ \hat{H} = \hbar \Omega |g_c\rangle\langle e| - \hbar \beta N(\varphi) |\psi_0\rangle\langle g_c| \]

\[ - i \hbar \beta \sin \theta \sin (\ell \varphi) |\psi_{NC}\rangle\langle \psi_0| + h.c., \]

(7)

forming the ladder system shown in Fig. 1b). In this basis \( |g_c\rangle \) couples optically to the excited state and magnetically to \( |\psi_{NC}\rangle \), which in turn couples magnetically to \( |\psi_0\rangle \). Importantly, at certain angles \( \varphi_n = n\pi/\ell \) (\( n \in \mathbb{N} \)), the state \( |\psi_{NC}\rangle \) decouples completely from the optical and magnetic transitions. At those angles, all atoms will spontaneously decay into the dark state \( |\psi_{NC}\rangle \) and light can pass unhindered through the atoms. The absorption profile can be calculated by evaluating Fermi’s Golden rule, \( T_{i \rightarrow f} \propto \frac{2\pi}{\hbar} |\langle f|\hat{H}|i\rangle|^2 \):

\[ T_{\psi_{NC} \rightarrow \epsilon} \propto \frac{2\pi}{\hbar} \frac{3}{|\hbar\Omega|^2 |h\beta|^4 |\sin \theta \sin (\ell \varphi)|^2 N(\varphi)^2} \]

\[ + \frac{\theta \in \pi/2}{\frac{2\pi}{\hbar}} \frac{3}{|\hbar\Omega|^2 |h\beta|^4 |\theta|^2 |\sin (\ell \varphi)|^2}. \]

(8)

For magnetic fields that have a small transverse component to the probe light propagation, we find a sinusoidal variation of the absorption profile with a periodicity of \( 2\ell \), shown in the inset in Fig. 1b), whereas for larger \( \theta \) the absorption acquires additional structure with twice the periodicity. We will explore the dependence on the magnetic field direction in more detail in a future paper.

**Experimental Setup & Procedure:** The electric field \( \hat{E} \) is generated by passing a linearly polarised probe laser through a q-plate [10] with \( q = \ell/2 \).
Q-plates are liquid-crystal based retardation waveplates with an inhomogeneous optical axis, exhibiting an azimuthal topological charge \( q \). Applying an AC external voltage sets their retardation to \( \pi \) so that they convert left to right handed polarisation, adding an OAM of \( 2q\hbar \), and vice versa, i.e. \( \sigma_- \rightarrow \sigma_\mp \exp(\pm iq\varphi) \). Consequently, linear polarised light generates classical entanglement between polarisation and azimuthal angle of the probe laser, illustrated in Fig. 2.

Our experiments are performed on cold, trapped \(^{87}\text{Rb} \) atoms, using the hyperfine transition \( 5^2S_{1/2}(F=1) \rightarrow 5^2P_{3/2}(F'=0) \). We prepare the sample in a dynamic dark spontaneous force optical trap (SPOT) providing a high density \((2 \times 10^{11} \text{ cm}^{-1}) \) cloud in the lower \( F = 1 \) ground state, matching our theoretical model.

The linearly polarised probe beam is spatially filtered and collimated before being passed through the q-plate path, as shown in Fig. 3a). Panels b) and c) show the intensity profile of the probe beam before and after a \( q = 1 \) q-plate. Optional waveplates may be added to alter the polarisation profile. A lens images the far field of the q-plate onto the atoms which are further imaged onto a CCD camera.

An experimental run loads a standard MOT for 6 s, followed by a SPOT loading time of 250 ms. All trapping lasers are then switched off and the cloud expands for typically 3 ms to achieve the desired density of \( 2 \times 10^{11} \text{ cm}^{-1} \), chosen to produce the highest contrast absorption images. The q-plate beam is then shone through the atoms for \( \sim 1 \) ms and images are recorded in the presence of atoms \( (I_{\text{Atoms}}) \), in the absence of atoms \( (I_{\text{Probe}}) \) and without lasers \( (I_{\text{Dark}}) \).

During the MOT and SPOT loading the atoms are exposed to the typical quadrupole magnetic field generated by anti-Helmholtz coils, while stray fields are compensated by three orthogonal Helmholtz coils. During the atomic expansion we switch off the quadrupole field and add a weak linear magnetic field of 0.1 G by modifying the currents in the compensation coils.

The transparency profile can be observed directly in the transmitted probe intensity (Fig. 3b)), but in order to quantify the expected sinusoidal absorption profile we present our data in form of absorption images. The absorption coefficient is proportional to the optical density, \( \text{OD} = \log \left( \frac{I_{\text{Probe}} - I_{\text{Dark}}}{I_{\text{Atoms}} - I_{\text{Dark}}} \right) \). For beams with low intensity regions the optical density is noisy and/or undefined where the denominator is zero or negative. We therefore scale the results by a factor of \( \sqrt{I_{\text{Probe}}} \) in order to enhance the meaningful areas of interest (Fig. 3c)). This scaling of course does not affect the azimuthal sinusoidal variation but only the radial intensity profile. Note that bright areas in the absorption image correspond to positions of low light transmission and vice versa.

**Results & Discussion:** The procedure outlined above generates a probe beam containing right and left handed circularly polarised components with \( \pm 2\hbar \) units of OAM, which drive transitions from the \( m_F = \mp 1 \) ground states, respectively. The absorption profile, shown in Fig. 3b), shows four-fold symmetry, satisfying the predicted 2\( \pi \) sinusoidal absorption profile predicted in Fig. 3c).

We demonstrate that this result holds also for higher...
rotational symmetries by using probe beams generated from various different q-plates. All observed absorption profiles, shown in Fig. 4, clearly display the expected $2\ell$ lobes.

So far we have interpreted spatial transparency as a result of interference between transitions driven by the oppositely-phased right and left circular polarisation components. Alternatively, we may consider the overall probe polarisation profile. All linear polarisations can be decomposed into two circular components of equal amplitude, with their relative phase governing the polarisation angle. The probe beams considered for Figs. 3 and 4 have an azimuthally varying phase difference, corresponding to vector vortex beams. The excitation amplitudes interfere only at positions where the linear polarisation is aligned with the atom quantisation axis as set by the magnetic field, causing transparency.

Following from this argument, we further probe the EIT mechanism by changing the incident polarisation. Based on the system symmetry, one would expect that rotating the linear polarisation before the q-plate would simply turn the absorption profile. We test this experimentally by rotating a $\lambda/2$-plate placed before the q-plate. The observed absorption profiles are shown in Fig. 5a) for a few angles of the $\lambda/2$-plate. Their overall rotation, however, can perhaps be seen more clearly from the unwrapped azimuthal profiles displayed on the right panel of Fig. 5a) which combines azimuthal data from 19 individual $\lambda/2$-plate positions, confirming that the absorption profile follows the input polarisation.

We perform a similar experiment with a $\lambda/4$-plate placed before the q-plate. The relative angle of the input polarisation and the $\lambda/4$-plate governs the ellipticity of the polarisation, ranging from linear to circular. For linear polarisation we of course retrieve the patterned absorption as before. Purely circular light, however, will be converted by the q-plate into oppositely circular light and acquire OAM. It will drive only one arm of the $\Lambda$ transition and, due to the level structure shown in fig. 1a), the atoms will be driven into a dark state, namely the electronic levels $|g_{-1}\rangle$ or $|g_{+1}\rangle$, which unlike the state $|\psi_{NC}\rangle$ are spatially uniform. The resulting absorption images, as shown in Fig. 5b), reveal a clear four-lobed pattern at 0 degrees and uniform absorption at about 45 degrees. Unwrapping the data, we obtain the image on the right of Fig. 5b), showing the emergence of the absorption structure as a function of the $\lambda/4$-plate angle.

Fig. 5c), finally, shows the increase of the rotational frequency by placing a $\lambda/4$-plate after the q-plate, resulting in $4\ell$ absorption lobes. We note that the atomic system essentially behaves as an ‘inverse’ linear polariser, with its axis coincident with the quantization axis set by the magnetic field. The petal-like absorption pattern is reminiscent of the petal mode transmission patterns observed by inserting the q-plate between crossed linear polarizers - our ‘atomic polariser’ however maintains a memory of the incident light.

**Conclusion:** We have demonstrated spatially structured transparency by probing atoms with vector vortex light. The atomic absorption profile reflects the spatial polarisation variation across the probe beam. We have shown that structured transparency reflects interference between two excitation amplitudes driven by light with different spatial phase profiles, in combination with weak magnetic coupling between the Zeeman ground states. The system contains a spatially varying dark state, whose population in turn resulted in a self-modulation of the incident light beams. Spatial absorption patterns were recorded for a variety of q-plates and input polarisations, showing that the symmetry of the absorption profile is linked to the symmetry of the input polarisation pattern, whereas the contrast of the absorption profile depends on the balance between the excitation amplitudes.
While we have demonstrated spatially dependent EIT for the special case of vortex light beams, the mechanism applies to any light where the circular polarisation components have a different spatial phase profile. Furthermore, while we have used classical light fields, in principle even the circular polarisation components of a single photon could be encoded with different phase profiles, and written into atomic dark states. We hence expect that spatially dependent EIT has applications for the storage of high-dimensional optical information in phase-dependent quantum memories. Finally we note, that the ‘classical entanglement’ between polarisation and azimuthal angle of the probe laser is converted, via the Hanle resonance, into a non-local correlation between the spatial intensity profile of the transmitted light and the atomic population profile, offering perphaps a vehicle to convert single photon classical entanglement into true quantum entanglement, an effect that we plan to investigate in more detail in future.

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[1] S. E. Harris, J. E. Field, and A. Imamolu, Phys. Rev. Lett. 64, 1107 (1990)
[2] K.-J. Boller, A. Imamolu, and S. E. Harris, Phys. Rev. Lett. 66, 2593 (1991)
[3] L. V. Hau, S. E. Harris, Z. Dutton, and C. H. Behroozi, Nature 397, 594 (1999).
[4] A. Turukhin, V. Sudarshanam, M. Shahriar, J. Musser, B. Ham, and P. Hemmer, Phys. Rev. Lett. 88, 023602 (2001)
[5] D. Phillips, A. Fleischhauer, A. Mair, R. Walsworth, and M. Lukin, Phys. Rev. Lett. 86, 783 (2001)
[6] B. Julsgaard, J. Sherson, J. I. Cirac, J. Fiurášek, and E. S. Polzik, Nature 432, 482 (2004)
[7] A. I. Lvovsky, B. C. Sanders, and W. Tittel, Nat. Photonics 3, 706 (2009)
[8] H. P. Specht, C. Nölleke, A. Reiserer, M. Uphoff, E. Figueroa, S. Ritter, and G. Rempe, Nature 473, 190 (2011)
[9] G. Heinze, C. Hubrich, and T. Halfmann, Phys. Rev. Lett. 111, 033601 (2013).
[10] L. Marrucci, C. Manzo, and D. Paparo, Phys. Rev. Lett. 96, 163905 (2006)
[11] R. Speeew, Found. Phys. 28, 361 (1998)
[12] P. Töppel, A. Aiello, C. Marquardt, E. Giacobino, and G. Leuchs. [N. J. Phys. 16, 073019 (2014)]
[13] C. Marquardt, E. Giacobino, and G. Leuchs, , 1 (2014), arXiv:arXiv:1409.0213v1.
[14] F. Renzoni, W. Maichen, L. Windholz, and E. Arimondo, Phys. Rev. A 55, 3710 (1997)
[15] U. Dorn, S. Quabis, and G. Leuchs, Phys. Rev. Lett. 91, 233901 (2003)
[16] V. D’Ambrosio, N. Spagnolo, L. Del Re, S. Slussarenko, Y. Li, L. C. Kwek, L. Marrucci, S. P. Walborn, L. Aolita, and F. Sciarrino, Nat. Commun. 4, 2432 (2013)
[17] F. Töppel, M. Sluker, O. Firstenberg, A. Ron, and N. Davidson, Phys. Rev. Lett. 98, 203601 (2007).
[18] D. Moretti, D. Féltimo, and J. Tabosa, Phys. Rev. A 79, 023825 (2009)
[19] L. Vissier, a. Nicolas, L. Giner, D. Maxein, a. S. Sheremet, E. Giacobino, and J. Laurat, Opt. Lett. 38, 712 (2013)
[20] G. Walker, a. S. Arnold, and S. Franke-Arnold, Phys. Rev. Lett. 108, 243601 (2012)
[21] D.-S. Ding, Z.-Y. Zhou, B.-S. Shi, and G.-C. Guo, Nat. Commun. 4, 2527 (2013)
[22] A. Nicolas, L. Vissier, L. Giner, E. Giacobino, D. Maxein, and J. Laurat, Nat. Photonics 8, 234 (2014)
[23] S. Buckle, S. Barnett, P. Knight, M. Lauder, and D. Pegg, Opt. Acta 33, 1129 (1986)
[24] S. Franke-Arnold, L. Allen, and M. Padgett, Laser & Photonics Reviews 2, 299 (2008).
[25] A. M. Yao and M. J. Padgett, Advances in Optics and Photonics 3, 161 (2011).
[26] D. V. Kosachiov, B. G. Matisov, and Y. V. Rozhdestvensky, J. Phys. B At. Mol. Opt. Phys. 25, 2473 (1992)
[27] B. Piccirillo, V. D’Ambrosio, S. Slussarenko, L. Marrucci, and E. Santamato, Applied Physics Letters 97, 241104 (2010)
[28] N. Radwell, G. Walker, and S. Franke-Arnold, Phys. Rev. A 88, 043409 (2013)