Determining the local dark matter density with LAMOST data

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ABSTRACT

Measurement of the local dark matter density plays an important role in both Galactic dynamics and dark matter direct detection experiments. However, the estimated values from previous works are far from agreeing with each other. In this work, we provide a well-defined observed sample with 1427 G & K type main-sequence stars from the LAMOST spectroscopic survey, taking into account selection effects, volume completeness, and the stellar populations. We apply a vertical Jeans equation method containing a single exponential stellar disk, a razor thin gas disk, and a constant dark matter density distribution to the sample, and obtain a total surface mass density of $78.7^{+3.9}_{-3.7} \, M_\odot \, pc^{-2}$ up to 1 kpc and a local dark matter density of $0.0159^{+0.0047}_{-0.0057} \, M_\odot \, pc^{-3}$. We find that the sampling density (i.e. number of stars per unit volume) of the spectroscopic data contributes to about two-thirds of the uncertainty in the estimated values. We discuss the effect of the tilt term in the Jeans equation and find it has little impact on our measurement. Other issues, such as a non-equilibrium component due to perturbations and contamination by the thick disk population, are also discussed.

Key words: Galaxy: kinematics and dynamics – Galaxy: disk – dark matter

1 INTRODUCTION

The local dark matter density is an important quantity not only because it can anchor the total dark matter mass of the Galactic halo, but also because it gives strong constraints in the search for dark matter particles in ground-based laboratories (Read 2014). Since Oort (1932, 1960), this value has been measured in many works with different models and observational samples (e.g. Kuijken & Gilmore 1989a,b,c; Holmberg & Flynn 2000, 2004; Weber & de Boer 2010). However, these results are far from agreeing with each other. Fig. 1 demonstrates the discrepant results, most of which are from recent survey data in the past three years (Smith et al. 2012; Garbari et al. 2012; Zhang et al. 2013; Bovy & Rix 2013; Bienaymé et al. 2014; Piffl et al. 2014; McKee et al. 2015). Further comparisons with historic works are displayed in Read (2014). The discrepancies may be due to two factors: 1) different assumptions, simplifications, and dynamical modelling methods have been used in the different works and 2) selection effects, systematics in the parameterizations, and the analysis methods for observed data differ greatly across the various works. In this sense, results cannot be compared naively unless differences in the modeling and observations are well understood.

In general, modelling techniques can be divided into two types: one is to constrain the local dark matter density with the vertical kinematics of stars in the solar neighborhood (e.g. Kuijken & Gilmore 1989a,b,c; Holmberg & Flynn 2000, 2004; Garbari et al. 2012; Zhang et al. 2013), while the other utilizes measurements of the rotation curve (e.g. Dehnen & Binney 1998; Fich et al. 1989; Merrifield 1992; Sofue et al. 2009; Weber & de Boer 2010; Catena & Ullio 2010; McMillan 2011; Piffl et al. 2014). Even in only the first category, different model assumptions may lead to quite...
Comparison of the measurements of the local dark matter density in the past three years. The points are from Smith et al. (2012; S12), Garbari et al. (2012; G12), Zhang et al. (2013; Z13), Bovy & Rix (2013; BR13), Piffl et al. (2014; PB14), Bienaymé et al. (2014; BF14), and McKee et al. (2015; M15). Our result is shown as the red square with error bar.

The aim of this work is to provide an observed dataset with a broad range of studies to be undertaken on the Milky Way. The on-going LAMOST survey (Zhao et al. 2012) is observing spectra for several millions of stars in low resolution and will provide the largest spectroscopic sample within a few kpc around the Sun in the next few years (Deng et al. 2012). We construct the observed sample from the LAMOST data carefully taking account of selection effects, volume completeness, reliable distance estimates, and sufficiently accurate vertical velocities.

Figure 1. Comparison of the measurements of the local dark matter density using the vertical Jeans equation method on a well defined dataset from the first estimate the local dark matter density using the vertical stellar kinematics. In the first of a series of works, we compared the minimum assumption method developed by themselves with the Holmberg & Flynn method (Holmberg & Flynn 2009) using data from an N-body simulation. They found that the assumed form of the distribution function in the Holmberg & Flynn method may be violated when the Galactic disk is not isothermal and axisymmetric, or when the observed data is beyond about 1 scale height. Therefore, systematic comparisons between various models are necessary so that the assumptions can be assessed. However, model comparison can not be properly made unless the observed data are carefully chosen with a good understanding of the uncertainties in the observables (stellar parameters, distance, and kinematics) and the selection effects.

The observed data used in previous works are from quite different sources with different systematics in parameter determination and selection effects. For example, the distances from the Sloan Digital Sky Survey (hereafter SDSS) estimated by An et al. (2009) are 9% smaller than those of Ivezić et al. (2008), according to Zhang et al. (2013). The sky coverage of SDSS, a northern sky survey, is quite different from the Radial Velocity Experiment (hereafter RAVE), a southern sky survey. Consequently, proper motions used in RAVE-based measurements (Bienaymé et al. 2014; Piffl et al. 2014) may have unknown systematics compared with those provided by SDSS, which are used by Zhang et al. (2013), due to the lack of uniform calibrations. The stellar tracers used are also different, e.g. Zhang et al. (2013) used K dwarfs while Bienaymé et al. (2014) used red clump stars. All these differences can significantly affect the results.

The methodology is based on a Bayesian approach (Carlin et al. 2015) and 71 ± 6 M⊙ pc−2, respectively, within a vertical distance of 1.1 kpc from the Galactic mid-plane near the Sun. Recently, Garbari et al. (2012) constrained the parameters of their improved vertical Jeans equation method using a Markov Chain Monte Carlo (hereafter MCMC) technique and obtained a local dark matter density of ρDM = 0.025±0.014 M⊙ pc−3 using the same data as Kuijken & Gilmore (1989b, hereafter KG). Zhang et al. (2013) applied a similar method to K dwarf stars from SDSS DR8 and derived a local dark matter density of ρDM = 0.0065 ± 0.0023 M⊙ pc−3.

The paper is organized as follows. In section 2, we first choose the data sample and then correct for selection effects. In section 3, we detail the vertical Jeans equation method suitable for the dataset. The results and discussion are shown in section 4. Finally, we conclude in section 5.

2 DATA

LAMOST (also called the Guoshoujing telescope) is a 4-metre quasi-meridian reflective Schmidt telescope being used for a spectroscopic survey (Cui et al. 2012; Zhao et al. 2012). The survey with millions of stellar spectra enables a broad range of studies to be undertaken on the Milky Way (Deng et al. 2012). The LAMOST DR2 catalogue contains 4,136,482 spectra, of which 1,085,404 spectra have atmospheric parameter estimates (Wu et al. 2014). Distances are estimated from a Bayesian approach (Carlin et al. 2015) with uncertainties of about 20%.

This large dataset covers the solar neighborhood well and thus provides an ideal database for the selection of the data sample for the measurement of the local dark matter density. First, we select about 4000 stars located with b > 85°, i.e. close to the north Galactic pole, so that the radial velocities estimated from the spectra are approximately equal to the vertical velocities (a more detailed discussion is in section 2.2). Hence, the vertical kinematics of these stars avoid proper motions, which are far less reliable than the radial velocities. Second, we select stars of a specific spectral type as the tracer population. It is noted that main-sequence stars with T eff > 6000 K are dominated by young stars with age < 4 Gyr and thus may not be as relaxed as old stars (Tian et al. 2015). Therefore we only select stars with 4000 < T eff < 6000 K to ensure that most of the tracers are already in equilibrium. Stars with T eff < 4000 K are not selected because atmospheric parameters cannot be
Dynamical modelling requires stars from both low and high z (here z represent the vertical height above the equatorial plane) regimes in order to detect both the baryonic component and the dark matter. Consequently, we select stars located between 200 and 1500 pc in z. However, not all types of spectroscopically observed stars are volume complete in this range of z because of the limiting magnitude, r = 17.8 mag, for the survey. Stars with J band absolute magnitudes between 3 and 4.5 mag are selected as they are volume complete in the vertical range from 200 pc to 1500 pc.

It is noted that multiple populations with different scale heights in the dataset may increase the uncertainty and induce systematics in the measurement of dark matter density (Hessman 2015). We therefore only select stars in the dataset (Skrutskie et al. 2006), since it covers more than 90% of the LAMOST data. The selection function for a given line of sight and a sufficiently small region in the color–magnitude (CM) plane, is toward the north Galactic pole.

The positions of the observed sample used in this work in heliocentric Cartesian coordinates. The positive x is toward the Galactic centre, and the positive z is toward the north Galactic pole.

It is noted that multiple populations with different scale heights in the dataset may increase the uncertainty and induce systematics in the measurement of dark matter density (Hessman 2015). We therefore only select stars in the thin disk by requiring [Fe/H].

Figure 2. The positions of the observed sample used in this work in heliocentric Cartesian coordinates. The positive x is toward the Galactic centre, and the positive z is toward the north Galactic pole.

2.1 Selection effects and stellar density

In general, sampling from a spectroscopic survey is significantly affected by the survey’s selection strategy, observational conditions, data reduction and so on. These induce substantial sample selection effects which must be taken into account in the determination of the stellar density.

For the LAMOST survey, although the field of view covers 20 square degrees, only fewer than 3000 stars within the field can be observed (the remaining ~1000 fibers are used for galaxies, special objects, flux standards, sky background and so on.). According to Carlin et al. (2012), the selection function in the LAMOST survey is simple. Indeed, no selection bias is found in color indices in the survey by comparing the DR2 catalogue with the corresponding input catalogue. The only selection effect is in magnitudes because 1) bright stars are easier to observe than fainter ones; and 2) the stellar density of brighter stars is much lower than that of the fainter ones, thus the sampling rate for bright stars is higher than that for the fainter ones.

Therefore we assume that for a given line of sight and a sufficiently small region in the color–magnitude (CM) plane, LAMOST observed stars are a subsample selected from a photometric catalogue, which is taken to be complete. In this work, we use the 2MASS catalogue as the photometric dataset (Skrutskie et al. 2006), since it covers more than 90% of the LAMOST data. The selection function for a given line of sight, θ, and a small CM bin can be written as

\[ f_{2MASS, \theta, CM}(z) = \varpi_{\theta, CM} f_{LAMOST, \theta, CM}(z) , \]  

where z is the vertical distance, \( f_{2MASS, \theta, CM}(z) \) the stellar density of 2MASS at z and is unknown, \( f_{LAMOST, \theta, CM}(z) \) is the stellar density of the LAMOST data at z and can be estimated from the spectroscopic sample. \( \varpi_{\theta, CM} \) in eq. (1) is the ratio of the number of stars from the photometric catalogue to that from the spectroscopic data within θ and CM. The total stellar density at z should be

\[ \nu_{obs}(z) = \sum_{CM, \theta} f_{2MASS, \theta, CM}(z) \]

\[ = \sum_{CM, \theta} \varpi_{\theta, CM} f_{LAMOST, \theta, CM}(z) . \]  

The dots with error bars in Fig. 3 show the stellar density profile with bin size of 100 pc. Errors are estimated from bootstrap resampling. It is clear that the stellar density profile is approximately a straight line in log ν vs. z which implies that the majority of stars in our sample belong to the thin disk with a single scale height.

2.2 Velocity dispersion

The uncertainty in the line-of-sight velocities from the LAMOST spectra is around 5 km s\(^{-1}\) (Gao et al. 2014).

Figure 3. The dots with error bars are the vertical stellar density for our observational sample. The red solid line is the best fit exponential density profile model.
the Galactic latitude of the sample stars is larger than 85°, the line-of-sight velocity can be approximately used as the vertical velocity. Thus, we avoid the large uncertainty from proper motions, which suffer from significant systematic biases and have uncertainties that increase with the distance.

In order to verify that the difference between the line-of-sight velocity and the vertical velocity is negligible, we run a Monte Carlo simulation using a simple but well-motivated model for the Milky Way disk in the same range of the Galactic latitude as the observed sample:

\[ \nu(z) \propto \exp(-\frac{z}{h}), \quad h = 300 \text{ pc}, \]
\[ \sigma_z(z) = v_0 \times \frac{z}{z_0}, \quad v_0 = \frac{10}{3} \text{ km s}^{-1}, \quad z_0 = 100 \text{ pc}, \]
\[ \sigma_r = \sigma_\phi = 2 \sigma_z, \]
\[ \langle v_r \rangle = \langle v_\phi \rangle = 0 \text{ km s}^{-1}, \]
\[ \langle v_z \rangle = 220 \text{ km s}^{-1}, \]

where \( \nu(z) \) is the vertical stellar density profile, \( \langle v_i \rangle \) and \( \sigma_i \) are the mean velocity and velocity dispersion respectively in three dimensions in the cylindrical coordinates. The simulation result is shown in Fig. 4. The estimated line-of-sight velocity dispersions at are consistent with the red dashed line, which gives the input model vertical velocity dispersions.

The dots with error bars in Fig. 5 show the vertical velocity dispersions derived from the line-of-sight velocities of our observed sample. The velocity dispersions are derived from the standard deviations of the velocities and the measurement errors of the velocities have been removed by deconvolution assuming Gaussian errors.

It is worth pointing out that the binning in \( z \) used in Figs. 3 and 4 is just for plotting. The fitting procedure we employ for our model parameters uses the spatial and kinematic information for individual stars without binning (see the logarithmic likelihood function eq. (17) in section 3.3).

3 METHOD

In this work, we focus on the vertical Jeans equation method following [Garbari et al. 2012] and [Zhang et al. 2013]. The first three assumptions of the method are as follows:

1) the Milky Way is axisymmetric;
2) the stars used for tracing the gravitational potential are individually in dynamical equilibrium;
3) the tilt term in the Jeans equation below (eq. 4) is negligible.

3.1 Vertical Jeans equation

For an axisymmetric system, the vertical part of the Jeans equation in cylindrical coordinates is

\[ \frac{\partial}{\partial z} (\nu \sigma_z^2) + \frac{1}{R \nu \partial R} (R \nu \sigma_z^2) = -\nu \frac{\partial \Phi}{\partial z}, \tag{4} \]

where \( \sigma_z^2 = \sigma_{z_1}^2 \sigma_{z_2}^2 \) is the velocity dispersion tensor [Binney & Tremaine 2008], \( \Phi \) the Galactic potential, \( \nu \) the vertical stellar density profile of the tracers. The density profile, \( \nu \), the velocity dispersion, \( \sigma_z^2 \), and the Galactic potential, \( \Phi \), in eq. 4 only depend on the vertical distance \( z \). Here we assume that the tilt term, \( \frac{1}{R \nu \partial R} (R \nu \sigma_z^2) \), is negligible since we only consider a small volume, e.g. an cone with width of 0.1 kpc and thickness of 1.5 kpc around the Sun [Garbari et al. 2012] [Zhang et al. 2013] [Read 2014]. Then eq. (4) can be simplified as

\[ \frac{d}{dz} [\nu(z) \sigma_z^2(z)] = -\nu \frac{d \Phi(z)}{dz} \bigg|_{R_0}, \tag{5} \]

where \( \Phi(z) \big|_{R_0} \) is the vertical gravitational potential in the solar vicinity, \( R_0 \) is the Sun’s distance to the Galactic centre. Further discussion about whether the tilt term can be neglected is in section 4.4.

3.2 One-dimensional Poisson equation

In one dimension, the vertical mass distribution is connected with the Galactic potential via the following one-

Figure 4. The result of the Monte Carlo simulation for the verification of the replacement of the vertical velocities with the line-of-sight velocities. The red dashed line stands for the input vertical velocity dispersions. The blue dots with error bars show the vertical velocity dispersions recovered from the line-of-sight velocities.

Figure 5. The dots with error bars represent the vertical velocity dispersion for our observational sample. The red solid line is the best fit of the velocity dispersion and the two red dashed lines show the 1-σ region of the PDF for velocity dispersion.
dimensional Poisson equation:
\[ 4\pi G \rho_{\text{tot}}(z)R_0 = \left. \frac{d^2 \Phi(z)}{dz^2} \right|_{R_0}. \]  
(6)

We assume that

4) the Galactic potential comprises baryonic matter (stars and gas) and dark matter.

Thus,
\[ \Phi(z) = \Phi_{\text{disk}}(z) + \Phi_{\text{gas}}(z) + \Phi_{\text{DM}}(z), \]  
(7)

where \( \Phi_{\text{disk}}(z), \Phi_{\text{gas}}(z), \) and \( \Phi_{\text{DM}}(z) \) are the potentials of the stellar disk, the gas disk, and the dark matter, respectively. Similarly,
\[ \rho_{\text{tot}}(z) = \rho_{\text{disk}}(z) + \rho_{\text{gas}}(z) + \rho_{\text{DM}}(z), \]  
(8)

where \( \rho_{\text{tot}}(z), \rho_{\text{disk}}(z), \rho_{\text{gas}}(z), \) and \( \rho_{\text{DM}}(z) \) are the densities for the total mass, the stellar disk, the gas disk, and the effective dark matter including the circular velocity term, respectively. \( \rho_{\text{DM}}(z) \) can be written as [Garbari et al. 2011]
\[ \rho_{\text{eff}}(z) = \rho_{\text{DM}}(z) - \frac{1}{4\pi G R} \left. \frac{\partial}{\partial R} V_c^2(R) \right|_{R_0}, \]  
(9)

where, \( V_c^2(R)\big|_{R_0} \) is the circular velocity at the solar circle. Here, we assume that

5) in the solar neighborhood, the rotation curve is flat [Bovy et al. 2012a].

Under this assumption, the last term on the right hand side of eq. [9] can be neglected, i.e. \( \rho_{\text{eff}}(z) = \rho_{\text{DM}}(z) \). Hereafter, we use \( \rho_{\text{DM}}(z) \) instead of \( \rho_{\text{eff}}(z) \).

3.3 Modelling \( K_z \)

The first derivative of the Galactic potential \( \Phi(z) \) represents the gravitational force perpendicular to the Galactic plane,
\[ K_z(z) = -\frac{d\Phi(z)}{dz}. \]  
(10)

Combining eqs. [5], [6], and [10], the vertical stellar density profile and velocity dispersion of the tracer stars can be related to gravitational force (including the dark matter contribution) by,
\[ \frac{d}{dz} \left[ \nu(z) \sigma_z^2(z) \right] = \nu(z) K_z(z). \]  
(11)

Additional assumptions are required to model the mass distribution in the solar neighborhood:

6) the vertical mass distribution of stellar disk is exponential with scale height \( z_h \);

7) the gas disk is razor thin, i.e. without thickness;

8) the dark matter density is a constant in the volume covered by our sample.

With these assumptions, the total vertical mass distribution can be written as
\[ \rho_{\text{tot}}(z) = \rho_{*,0} \exp \left( -\frac{z}{z_h} \right) + \Sigma_{\text{gas},0} \delta(z) + \rho_{\text{DM}}. \]  
(12)

Function \( K_z \) can be obtained by integrating eq. [10],
\[ K_z(z) = -\int_0^z 4\pi G \rho_{\text{tot}}(z') dz' \]
\[ = -2\pi G \left\{ \Sigma_* \left[ 1 - \exp \left( -\frac{z}{z_h} \right) \right] + \Sigma_{\text{gas}} + 2\rho_{\text{DM}} \right\} z, \]  
(13)

where \( \Sigma_* \) is the total surface mass density of the stellar disk, \( \Sigma_{\text{gas}} \) the surface density of the gas disk, which is taken as 13.2 M\( \odot \) pc\(^{-2}\) [Flynn et al. 2006], and \( \rho_{\text{DM}} \) the local dark matter volume density. At the mid-plane, we have \( \left. \frac{d\Phi(z)}{dz} \right|_{z=0} = 0 \) because of symmetry. According to the observed data, the stellar density of the tracers can be assumed to be a single exponential profile,
\[ \nu(z) = \nu_0 \exp \left( -\frac{z}{h} \right). \]  
(14)

The four free parameters in the stellar density profile and the \( K_z \) model is denoted as \( \mathbf{p} = (h, \Sigma_*, \rho_{\text{DM}}, z_h) \).

The velocity dispersion can be solved analytically by integrating eq. [11],
\[ \int_{z_0}^z \frac{d}{dz'} \left[ \nu(z') \sigma_z^2(z') \right] \right|_{z_0} = \int_{z_0}^z \nu(z') K_z(z'), \]
\[ \sigma_z^2(z) = \frac{1}{\nu(z)} \int_{z_0}^z \nu(z') K_z(z') \left( z' - z_0 \right) \sigma_z^2(z_0), \]  
(15)

\[ \sigma_z^2(z) = f(z) + \frac{\nu(z_0) \sigma_z^2(z_0) - \nu(z_0) f(z_0)}{\nu_0 \exp \left( -\frac{z_0}{h} \right)}, \]  
(16)

where
\[ f(z) = 2\pi G h \left\{ \Sigma_* \left[ 1 - \frac{z_0}{h + z_0} \exp \left( -\frac{z}{z_0} \right) \right] + \Sigma_{\text{gas}} + 2\rho_{\text{DM}} \left( z + h \right) \right\} \]  
(17)

and \( z_0 \) is the boundary condition for the integration. Eqs. [15] and [16] imply that the contribution of the baryonic matter increases as a negative exponential with \( z \), while the contribution of the dark matter increases linearly. It is known that \( h \) is about 300 pc for the thin disk and since most of the baryonic matter is contributed by the stellar thin disk, \( z_h \) may be slightly larger because of the thick disk, but cannot be too different from \( h \). Thus, the baryonic matter should dominate the low \( z \) regime within a few hundred pc above the Sun. The dark matter will take over when \( z \) is beyond a few scale heights (\( z \sim 1 \) kpc). Therefore, in order to accurately measure the contributions from both the baryons and dark matter the observed sample has to cover both the low \( z \) (\( \sim 200 \) pc) and high \( z \) (\( \sim 1500 \) pc) regimes.

In practice, we find the best-fitting parameters \( \mathbf{p} \) using the following steps without binning the data:

1) The initial conditions of the model parameters \( \mathbf{p} \) are chosen.

2) The stellar density profile and the velocity dispersion within the range from 100 pc to 300 pc are used as the boundary condition \( \nu(z_0) \sigma_z^2(z_0) \big|_{z=200 \text{ pc}} \).

3) The stellar density profile \( \nu_{\text{model}}(z) \) and the vertical velocity dispersion profile \( \sigma_{z,\text{model}}(z) \) are predicted according to eqs. [14] and [15] for the given \( \mathbf{p} \).
The log-likelihood is given by,

$$\ln L = -n \ln(A) - \sum_i \varpi_i z_i/h$$

$$- \sum_i \ln[\sqrt{2\pi} \sigma_{z_i, \text{model}}(z_i)]$$

$$- \frac{1}{2} \sum_i \left[ \frac{v_i - m_v}{\sigma_{z_i, \text{model}}(z_i)} \right]^2,$$

where \(i = 1, \cdots, n\) is the label of the tracers, \(m_v\) is the mean velocity as a free parameter, and \(\varpi_i\) is the weight of the \(i\)-th star (see section 3.1). \(A\) is the normalization parameter of the number density,

$$A = \frac{1}{\int_{z_{\text{min}}}^{z_{\text{max}}} \nu_0 \exp(-\frac{z}{h}) dz},$$

where, \(z_{\text{min}}\) and \(z_{\text{max}}\) are the lower and upper limits of the vertical distance of the tracer population, respectively.

Finally, we run MCMC using emcee\(^1\) (Foreman-Mackey et al. 2013) to obtain the best fit parameters.

4 RESULTS AND DISCUSSIONS

We apply the model described in section 3 to the LAMOST sample selected in section 2. In the MCMC phase, we use 50 chains each with 50000 steps. The posterior probability density functions (PDFs) of the four parameters are shown in Fig. 6. The best-fitting values, i.e. the median values in the MCMC random drawing, are listed in Table 1. The model predicted vertical stellar density and velocity dispersion profiles are over-plotted in Figs. 3 and 5, respectively. In Fig. 5, the red solid line is the model velocity dispersion and the red dashed lines are the 1-\(\sigma\) region. Both vertical profiles are in good agreement with the binned data, although, as previously stated, we use the unbinned data in the model fitting. The best-fitting value of the scale height of the exponential stellar density profile is 293.8 \(\pm\) 0.5 pc, which is consistent with previous works (Jurić et al. 2008).

The model predicted \(K_z(z)\) force is shown in Fig. 7. The solid line is the best-fitting \(K_z(z)\), and the two dashed lines indicate the 1-\(\sigma\) region. \(K_z(z)\) increases with vertical distance \(z\) due to the contributions of the stellar disk and the dark matter halo. The total surface density up to 1 kpc can be immediately derived from,

$$\Sigma_{\text{tot, } |z|<1.0 \text{ kpc}} = K_z(z < 1.0 \text{ kpc})/(2\pi G).$$

We obtain \(\Sigma_{\text{tot, } |z|<1.0 \text{ kpc}} = 78.7^{+3.9}_{-4.7} M_\odot \text{ pc}^{-2}\), within which the stellar disk contributes \(\Sigma_\star = 40.5^{+7.1}_{-6.6} M_\odot \text{ pc}^{-2}\), and the local dark matter density is \(\rho_{\text{DM}} = 0.0159^{+0.0047}_{-0.0037} M_\odot \text{ pc}^{-3}\).

If we consider the non-flat nature of the rotation curve, the last term at the right hand side of eq. (9) is about \(-0.0024 M_\odot \text{ pc}^{-3}\) in the solar neighborhood according to Binney & Merrifield (1998). With this adjustment, \(\rho_{\text{DM}} = 0.0135^{+0.0031}_{-0.0027} M_\odot \text{ pc}^{-3}\). It is noted that \(\Sigma_\star\) and \(\rho_{\text{DM}}\) are anti-correlated, and constrained by the total surface density (Garbari et al. 2012). The bottom-left panel of Fig. 6 shows this anti-correlation.

4.1 Comparison with other works

The total surface density within 1 kpc, \(\Sigma_{\text{tot, } |z|<1.0 \text{ kpc}} = 78.7^{+3.9}_{-4.7} M_\odot \text{ pc}^{-2}\) obtained here is slightly larger than those from previous works, e.g. Zhang et al. (2013) inferred 67 \(\pm\) 6 \(M_\odot \text{ pc}^{-2}\) and Bienaymé et al. (2014) gave 68.6 \(\pm\) 1.0 \(M_\odot \text{ pc}^{-2}\), but our result is still consistent with theirs within the uncertainties. The local dark matter density, \(\rho_{\text{DM}}\), estimated here is 0.0159 \(\pm\) 0.0037 \(M_\odot \text{ pc}^{-3}\), which is also consistent with previous results. Compared with recent works, our result is larger than Zhang et al. (2013, by about 1-\(\sigma\), but similar to Piffl et al. (2014), 0.0154 \(M_\odot \text{ pc}^{-3}\), and Bienaymé et al. (2014), 0.0143 \(\pm\) 0.0011 \(M_\odot \text{ pc}^{-3}\) (see Fig. 4). As we have argued in section 1, a serious comparison should not simply examine the values and their error bars: the large differences in the observed data and models must be taken into account as well.

4.2 The uncertainty of the results

The uncertainty of our result is around 30 percent which is similar to that of Zhang et al. (2013) but larger than two RAVE-based works published in 2014 which have an uncertainty of around 10 percent (Piffl et al. 2014, Bienaymé et al. 2014). One reason is that the results of their estimates from the Galactic rotation curve (e.g. Piffl et al. 2014) usually have small error bars due to the strong assumptions about the Galactic halo shape (Read 2014), while the local measures usually have larger errors. Another likely reason is due to random noise. If we assume that our model can

\(^1\) Emcee is an MIT licensed pure-Python implementation of Goodman & Weare’s Affine Invariant MCMC Ensemble sampler.
perfectly describe our solar neighborhood, the uncertainty should only come from sampling noise and observational errors. Below we use a Monte Carlo simulation to quantify the influence of sampling noise.

Using our model, we generate three groups of mock data (all of which assume a local dark matter density of $0.01 \, M_\odot \text{pc}^{-3}$) with three sampling densities (i.e., number of stars per unit volume): 1) sampling density of Group 1 is 100 stars per 100 pc, similar to LAMOST DR2; 2) Group 2, 150 stars per 100 pc; 3) Group 3, 200 stars per 100 pc. Each group contains 100 sets of data. We quantify the influence of random noise by calculating the averaged $\rho_{DM}$ and its variance for the three groups. Fig. 8 shows the results from the three groups. The uncertainty is around 20% of the median value for a sampling density equal to 100 stars per 100 pc, 10% for 150 stars per 100 pc, and 5% for 200 stars per 100 pc. It means that with the current LAMOST DR2 sample, the contribution to the uncertainty from the sampling noise is about two-thirds of the total uncertainty which is 30% based on our model. The remaining one-third of the total uncertainty may come from the measurement er-
errors of velocities, distances, and stellar parameters, or from the systemic errors.

4.3 The scale height of the stellar mass distribution

The scale height of the stellar mass distribution, $z_h$, is $588^{+192}_{-102}$ pc, which is not well constrained. In the model fitting procedure a prior $z_h < 800$ pc is imposed. It is noted that the $z_h$ study also suffered from a large uncertainty in this parameter. [Bienaymé et al. 2014] simply fixed $z_h$ as 300 pc. The reason may be that, the Jeans equation method is not sensitive to $z_h$. Unfortunately our sample does not contain enough stars located within $z < 300$ pc to better constrain this quantity.

As shown in Fig. 6, it is clear that $\Sigma$, or $\rho_{DM}$ is almost uncorrelated with $z_h$. If we fix $z_h = 300$ pc, the local dark matter density, $\rho_{DM}$, is $0.0144 \pm 0.005 M_\odot pc^{-3}$, a change of less than 10%. If we relax the prior to $z_h < 6000$ pc, the local dark matter density significantly increases as shown in Fig. 6. This is because, when $z_h$ is larger than 2000 pc, the contribution of the stellar disk is negligible and the increase in the vertical velocity dispersion depends only on the dark matter. However, such a large $z_h$ seems unrealistic since we know that the dominating stellar component is the thin disk with a scale height of around 300 pc.

4.4 Tilt term

The tilt term in eq. (1)

$$\frac{1}{R_v} \frac{\partial}{\partial R} (R\nu\sigma^2_{Rz}),$$

(20)

is related to the vertical number density, $\nu(z)$, the cross term of velocity dispersion tensor, $\sigma^2_{Rz}$, and their partial derivative with respect to the radius $R$. In most previous works, this term has been neglected (e.g. [Garbari et al. 2012, Zhang et al. 2013]). However, using SDSS/SEGUE G-type dwarf stars, [Büdenbender et al. 2015] found that the tilt angle variation with height can be empirically described by the relation

$$\alpha_{tilt} = (-0.90 \pm 0.04) \arctan(|z|/R_0) - (0.01 \pm 0.005).$$

(21)

Here, $\alpha_{tilt}$ is the tilt angle defined as

$$\tan(2\alpha_{tilt}) = \frac{2\sigma^2_{Rz}}{\sigma^2_{R} - \sigma^2_{z}}.$$

(22)

They concluded that, the tilt term cannot be ignored, [Silverwood et al. 2015] subsequently modelled the tilt term and investigated its influence using simulation data. They found that the contribution to the tilt term by thick disk stars is about 9% in $K_s$ at $z = 1.5$ kpc, while the contribution from the thin disk stars is only about 5% at the same height (see their Fig. 2). Since we use only the thin disk stars in this work and the maximum height in our sample is 1.5 kpc, the influence of the tilt term can be neglected if the [Silverwood et al. 2015] findings are accepted. To confirm this, we run a modified model taking into account the tilt term modelled by [Silverwood et al. 2015] and found a local dark matter density of $0.0155^{+0.0057}_{-0.0057} M_\odot pc^{-3}$, which is consistent with our previous result.

4.5 A non-equilibrium component of the disk

A fundamental assumption of the measurement of the local dark matter density is that the tracers have to be individually in equilibrium so that the collisionless Boltzmann equation-based models can be applied. However, recent observations found some evidence of asymmetric vertical motions in the Galactic disk, which violate the equilibrium assumption ([Williams et al. 2013, Carlin et al. 2013, Xu et al. 2015]). They are likely wave modes induced by vertical perturbations due to dwarf satellites, the triaxial dark matter halo, or spiral structures. Theoretical works show that

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**Figure 8.** The uncertainty caused by the sampling rate. The x-axis is the sampled stars per 100 pc. The y-axis is the averaged dark matter density estimate. The error bars show the 1 σ dispersions.

**Figure 9.** The bottom-left panel shows the 2-D PDF of $z_h$ and $\rho_{DM}$ with a much broader prior ($z_h < 6000$ pc). The contours show the 0.5, 1.5, and 2 σ levels. The top panel and the bottom-right panel show the 1-D PDF of $\rho_{DM}$ and $z_h$, respectively. The solid line of each panel indicates the median value, while the two dashed lines indicate the 1-σ regions.
about 20% of stars in the disk may be perturbed by dwarf satellites and the mean vertical velocity can be shifted by 5–10 km s\(^{-1}\) (Gómez et al. 2013). Using LAMOST data, Carlin et al. (2013) also found that the mean vertical velocity is shifted by at most 10 km s\(^{-1}\). This challenges the methodology of the local dark matter density determination, not only because of the non-equilibrium stars themselves but also because of their effects on other stars which may lead to systematic errors.

We run a simple test to evaluate this effect. We give an additional vertical velocity of 40 km s\(^{-1}\) for a subset of 20% of randomly selected stars to mimic a perturbation. The vertical velocity distribution is no longer symmetric, as shown by the black line in the top panel of Fig. 10. The derived velocity dispersion without considering the non-equilibrium component increases by about 4 km s\(^{-1}\) with a shift of the mean velocity by about 8 km s\(^{-1}\). This would lead to an overestimation of the local dark matter density by approximately 40%. The observed velocity distribution of the LAMOST sample located at the vertical distance between 0.5 kpc and 0.6 kpc, as used in this work, is shown in the bottom panel of Fig. 10. Although it is hard to identify an additional velocity component, it does show a slight asymmetry. In future works, we plan to address this issue by combining about 1000 stars toward the South Galactic Pole with the LAMOST sample such that the wave modes in the vertical velocity can be identified and fully considered in an improved measurement of the local dark matter density.

4.6 The thick disk contaminations

In section 2 we use [Fe/H] > -0.5 dex to remove the thick disk. In this section we test how many thick disk stars still remain after this cut and whether they affect the measurement of the \(K_\alpha\) force. The potential contamination from the thick disk mostly affects the high \(z\) regime. For G type stars (roughly corresponding to 5300 < \(T_{\text{eff}}\) < 6000 K), the thick disk contamination under this criterion is \(\sim 33\%\) at 600 < \(z\) < 1500 pc according to the data in Liu & van de Ven (2012) with a similar cut in volume\(^2\). For K type stars (roughly corresponding to 4000 < \(T_{\text{eff}}\) < 5300 K), according to Fig. 1 in Zhang et al. (2013), the thick disk contamination (defined as [\(\alpha/\text{Fe}\] > 0.25 dex) is also quite low, similar to that for G type stars. Considering the mixture of the thick disk stars, the scale height of our sample is 10% larger than the scale height of the thin disk.

We further perform a simple test to estimate how significant these contaminations would be in the velocity dispersion. According to Zhang et al. (2013), the thin disk (roughly corresponding to their group I with a scale height of \(\sim 260\) pc) has \(\sigma_z \sim 21\) km s\(^{-1}\) at 600 < \(z\) < 1500 pc and possibly contaminating thick disk stars (mostly from their group II with scale height \(\sim 450\) pc) have \(\sigma_z \sim 28\) km s\(^{-1}\). If the 33\% stars are from the thick disk contamination, then the derived velocity dispersion with contamination would be about 3 km s\(^{-1}\) larger than that of the thin disk. In this case, we will overestimate the local dark matter density \(\rho_{\text{DM}}\) by about 20\%, and the value of \(\rho_{\text{DM}}\) becomes 0.0133 \(M_\odot\) pc\(^{-3}\). Future data releases of LAMOST will contain information on [\(\alpha/\text{Fe}\)], which will reduce the contamination of thick disk stars significantly.

5 CONCLUSION

Determination of the local dark matter density from the vertical motions of the stars is an important application in Galactic dynamics; it is also an important input parameter in determining the dark matter flux in direct detection experiments. However, in the past century, the estimated values by many works are far from being in agreement with each other. Either the dynamical models and/or the ob-

\(^2\) The thick disk is defined as [\(\alpha/\text{Fe}\] > 0.25 dex. The data is selected with \(b > 70^\circ\) instead of 85\(^\circ\) to ensure sufficient stars in the statistics.
erved data significantly affect the measured values. In this work, we build a well-defined observational sample based on the LAMOST spectroscopic survey. Uncertainties in stellar parameters, distances, lines-of-sight velocities, selection effects, volume completeness, and stellar populations are all carefully taken into account. We finally obtain a sample with 1427 G & K type main-sequence stars, most of which belong to the thin disk population following an exponential vertical density profile. Based on this sample we execute a series of modeling works to estimate the local dark matter density. We start with the vertical Jeans equation method and assume a single exponential stellar mass distribution, a razor thin gas disk, and a constant dark matter distribution within 1.5 kpc. We estimate the posterior probability density function for the model parameters, including the surface mass density of the disk and the local volume mass density of the dark matter, with Markov Chain Monte Carlo simulations. We obtain a total surface mass density of $78.7^{+3.9}_{-3.7} M_\odot$ pc$^{-2}$ up to 1 kpc and a local dark matter density of $0.0159^{+0.0037}_{-0.0027} M_\odot$ pc$^{-3}$ if the rotation curve is flat.

Although these results are consistent with most recent works, the agreements may be fortuitous because neither the methods nor the data are the same. Even relative uncertainties are not comparable because oversimplified assumptions can lead to unrealistically smaller errors. We found that for our case the sampling noise of the observed data contributes about two-thirds of the uncertainty in our determination of the local dark matter density. The tilt term, a non-equilibrium component induced by perturbations and contaminations from the thick disk for example, can explain the remaining uncertainty.

In future works, we plan to combine LAMOST data for the observed northern Galactic pole with new data from the southern Galactic pole to identify better any non-equilibrium components and to improve estimation of both the vertical stellar density and the velocity dispersion profile. This augmented sample will enhance our ability to evaluate different assumptions within dynamical models. In the end, this will be beneficial in improving local dark matter density determinations.

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REFERENCES

An, D., Pinsonneault, M. H., Masseron, T., et al. 2009, ApJ, 700, 523
Bahcall, J. N., 1984a, ApJ, 287, 926
Bahcall, J. N., 1984b, ApJ, 276, 169
Bahcall, J. N., Flynn C., Gould A., 1992, ApJ, 389, 234
Bienaymé, O., Robin, A. C., Creze, M., 1987, A&A, 180, 94
Bienaymé, O., Soubibian, C., Mishenina, T. V., Kovtyukh, V. V., Siebert, A., 2006, A&A, 446, 933
Bienaymé, O., Famaey, B., Siebert, A., et al. 2014, A&A, 571, 92
Binney, J., Merrifield, M., Galactic Astronomy, Princeton, NJ : Princeton University Press, 1998
Binney, J. & Tremaine, S., 2008, Galactic Dynamics: Second Edition, Princeton University Press
Bovy, J., Allende Prieto, C., Beers, T. C., et al. 2012a, ApJ, 759, 131
Bovy, J., Tremaine, S., 2012b, ApJ, 756, 89
Bovy, J., Rix, H.-W., 2013, ApJ, 779, 115
Bièn, A., van de Ven, G., Watkins, L. L., 2015, MNRAS, 452, 956
Carlin, J. L., et al., 2012, RAA, 12, 755
Carlin, J. L., DeLauagay, J., Newberg, H. J., et al. 2013, ApJ, 777, 5
Carlin, J. L., Liu, C., Newberg, H., et al. 2015, AJ, 150, 4
Catena, R., Ullio, P., 2010, JCAP, 8, 4
Creze, M., Chereul, E., Bienaymé, O., Pichon, C., 1998, A&A, 329, 920
Cui, X. Q., Zhao, Y. H., Chu, Y. Q., Li, G. P., et al. 2012, RAA, 12, 1197
Deng, L. C., Newberg, H., Liu, C., et al. 2012, RAA, 12, 735
Dehnen, W., Binney, J., 1998, MNRAS, 294, 429
Fich, M., Blitz, L., Stark, A. A., 1989, ApJ, 342, 272
Flynn, C., Holmberg, J., Portinari, L., Fuchs, B., Jahreiss, H. 2006, MNRAS, 372, 1149
Gao, S., Liu, C., Zhang, X. B., et al. 2014, ApJ, 788, 37
Garbari, S., Read, J. I., Lake, G., 2011, MNRAS, 416, 2318
Garbari, S., Liu, C., Read, J. I., Lake, G., 2012, MNRAS, 425, 1445
Gómez, F. A., Minchev, I., O’Shea, B. W., et al. 2013, MNRAS, 429, 159
Hessman, F. V., 2015, A&A, 579, A123
Hill, E. R., 1960, Bull. Astron. Inst. Netherlands, 15
Holmberg, J., Flynn, C., 2000, MNRAS, 313, 209
Holmberg, J., Flynn, C., 2004, MNRAS, 352, 440
Ivezić, Ž., Sesar, B., Jurić, M., et al. 2008, ApJ, 684, 287
Jurić, M., et al., 2008, ApJ, 673, 864
Kapteyn, J. C., 1922, ApJ, 55, 302
Kuijken, K., Gilmore, G., 1989a, MNRAS, 239, 571
Kuijken, K., Gilmore, G., 1989b, MNRAS, 239, 605
Kuijken, K., Gilmore, G., 1989c, MNRAS, 239, 571
Kuijken, K., Gilmore, G., 1991, ApJ, 367, L9
Liu, C., van de Ven, G., 2012, MNRAS, 425, 2144
McKee, C. F., Parravano, A., Hollenbach, D. J., 2015, arXiv:1509.05334
McMillan, P. J., 2011, MNRAS, 414, 2446
Merrifield, M. R., 1992, AJ, 103, 1552
Moni Bidin, C., Carraro, G., Méndez, R. A., Smith, R., 2012, ApJ, 751, 30
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Oort, J. H., 1932, Bulletin of the Astronomical Institutes of the Netherlands, 6, 249
Oort, J. H., 1960, Bulletin of the Astronomical Institutes of the Netherlands, 15, 45
Piffl, T., Binney, J., McMillan, P. J., et al. 2014, MNRAS, 445, 3133
Read, J. I., 2014, arXiv:1404.1938
Siebert, A., Bienaymé, O., Soubiran, C., 2003, A&A, 399, 531
Silverwood, H., Sivertsson, S., Steger, P., Read, J. I., Bertone, G., 2015, arXiv:1507.08581
Smith, M. C., Whiteoak, S. H., Evans, N. W., 2012, ApJ, 746, 181
Sofue, Y., Honma, M., Omodaka, T., 2009, PASJ, 61, 227
Skrutskie, M. F., et al., 2006, AJ, 131, 1163
Tian, H.-J., et al., 2015, ApJ, 809, 145
Weber, M., de Boer, W., 2010, A&A, 509, A25
Williams, M. E. K., et al. 2013, MNRAS, 436, 101
Wu, Y., Du, B., Luo, A., et al., 2014, IAUS, 306, 340
Xu, Y., Newberg, H. J., Carlin, J. L., et al. 2015, ApJ, 801, 105
Zhang, L., Rix, H.-W., van de Ven, G., Bovy, J., Liu, C., Zhao, G., 2013, ApJ, 772, 108
Zhao, G., Zhao, Y. H., Chu, Y. Q., Jing, Y. P., Deng, L. C. 2012, RAA, 12, 723