Analysis of Bitcoin Vulnerability to Bribery Attacks Launched Through Large Transactions

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Abstract—Bitcoin uses blockchain technology to maintain transactions order and provides probabilistic guarantee to prevent double-spending, assuming that an attacker’s computational power does not exceed 50% of the network power. In this paper, we design a novel bribery attack and show that this guarantee can be hugely undermined. Miners are assumed to be rational in this setup and they are given incentives that are dynamically calculated. In this attack, the adversary misuses the Bitcoin protocol to bribe miners and maximize their gained advantage. We will reformulate the bribery attack to propose a general mathematical foundation upon which we build multiple strategies. We show that, unlike Whale Attack, these strategies are practical. If the rationality assumption holds, this shows how vulnerable blockchain-based systems like Bitcoin are. We suggest a soft fork on Bitcoin to fix this issue at the end.

Index Terms—Bitcoin, Blockchain, Bribery Attack, Markov Chain, Double Spending, Security.

I. INTRODUCTION

Bitcoin was introduced in 2008 as a peer to peer electronic currency and its aim was to make online transactions outside the classic financial system possible [1]. This was one of the first practical efforts toward bringing trust to transactions in a zero-trust environment [2], [3]. Study of the digital currency history before that [4] shows decades of research did not lead to a large-scale deployment of e-cash, and with the emergence of Bitcoin, all those efforts have been dwindled [5]–[10]. Blockchain [11], as the core of Bitcoin, is a data structure to save the history of transactions in a distributed system. Each block in blockchain uses another data structure called Merkle tree [12] to store transactions.

Bitcoin provides probabilistic guarantee to prevent double-spending, assuming that no attacker’s computational power exceeds 50% of the network mining power. In this paper, we design a novel attack scenario to show that Bitcoin’s probabilistic guarantee on double spending can be hugely undermined. Miners are expected to be rational and work based on some monetary incentives. In our proposal, the attacker misuses Bitcoin standard mechanisms to bribe miners and increase their advantage in a way that they are encouraged to follow the attacker’s lead. We will show that this new attack can be more efficient, practical and cheaper than the Whale Attack if the attacker adopts right strategies in distributing the bribe money even when paying the bribe out of the already spent money. We design a few of such strategies and analyze them analytically by using a Markov model of ours. The results show that this new attack can be quite challenging for blockchain-based cryptocurrencies like Bitcoin and necessitate taking additional preventive measures in the design of such cryptocurrencies. Two solutions will also be proposed at the end of the paper that make soft-forks on Bitcoin. In summary, the contributions of this work are:

- Proposing a new mathematical model for Bribery attack and laying the foundations for further research.
- Design and evaluation of new strategies that can decrease the attack cost and increase the success probability.
- Introduction of a commitment mechanism to make the attack more practical and decrease the attack cost and increase the success probability.

The rest of the paper is organized as follows. In Section II we will review the state of the art attacks on Bitcoin. In Section III and IV the proposed attack and its mathematical analysis will be presented. Numerical analysis of different attack strategies will be discussed in Section V. The paper is finally concluded in Section VI.

II. RELATED WORK

Previous literature presented different types of attacks on Bitcoin. Double spending is the first and the most common attack introduced in the field of cryptocurrencies [13], [14]. In 51% attack adversaries have control over the majority of the network hash power. A method to prevent such attacks is explored in [15]. Some types of attacks pertain to client-side applications, the security measures they have adopted, users’ mistakes, etc. Many Bitcoin users lost their money due to security breaches and poor key management of wallets [16]–[18]. In Sybil attack a single attacker controls multiple nodes in the network or creates multiple identities by spawning up multiple virtual machines and IP addresses [19]–[21]. In [22], a new attack for Bitcoin was introduced by combining double-spending with Sybil attack. In eclipse attack [23], an adversary takes control of a sufficient number of IP addresses and practically separates the victim (miner) from the public network. Stubborn Mining [24] is a generalized Selfish-Mining [25] by defining new strategies and combining them with eclipse attack to increase the earnings of miners. Block withholding attack was initially proposed by Rosenfeld in 2011. There are two types of block withholding attack [26]. One, known as the Finney Attack, aims for financial gain when a double spending occurs. The second type is meant to cause financial harm to a pool operator. There are other attacks for
Bitcoin like Time Jacking attack \cite{27}, DDoS \cite{28}, \cite{29}, etc. which are categorized in four groups in \cite{23}: Double spending, Wallet attacks, Network attacks, Mining attacks.

Bribery attack, which is categorized in the same family as the attack studied in this paper, was introduced in \cite{30} and implemented in \cite{31} as smart contracts to let a briber exchange bribes with miners. In this attack, an adversary obtains the majority of computational power through bribing for a limited duration. This research article did not provide any modeling or analysis of the attack whatsoever. A way of giving incentives for adversarial purposes was proposed in \cite{32} under the name of Whale Attack. In Whale Attack the attacker tries to issue whale transactions with high transaction fees to encourage miners to work on the forked chain. As mentioned in \cite{32}, the miners’ revenue from the transaction fees does not exceed 0.00016BTC for each 257-byte transaction, unless the attacker uses exorbitant transaction fees to pay the bribery. A new study \cite{33} uses out-of-band bribing to decrease the cost of attack and make it practical and efficient. However, its drawback is that the attacker loses money if the attack fails. In in-band bribing, the attacker bribes out of the money he/she has spent as in double-spending and thus, if the attack fails, the attacker loses nothing, except perhaps the computational power used during the attack. A more recent study \cite{34} tried to model bribery attack by considering three parties; the attacker, the honest miners, the bribed miners. This study assumed that the bribed miners participate in a pool, and analyzed the bribed miners profit based on the computational power of the pool. It was shown that such an assumption would reduce the attack cost but creating such a pool can be impractical. Unlike this study, we analyze the attack based on the current pools in the network.

In the next section, we will deeply analyze the Bribery attack and show how effective this attack can be made by using the outputs of the proposed analysis framework.

III. THE PROPOSED BRIERY ATTACK

A. Assumptions

We assume that miners are rational. The rationality assumption is the expectation that miners will select, from a series of choices, the one(s) that will maximize their profit. We also assume that the distribution of mining power remains constant during the attack, and it is known to all parties. We normalize the network computational power to 1 (or %100).

B. Attack Process in a Nutshell

Suppose that Alice, who controls a minority of the computational power in the Bitcoin network, attempts to launch a double-spending attack against a seller whose name is Bob. First, Alice does a large transaction with Bob. After the transaction is included in the chain, Alice starts working on a fork by creating a block that does not include that transaction, but keeps this matter private. Alice needs to create at least one block in her chain before the transaction is confirmed. This block has some special transactions in which Alice transfers some BTC to new addresses she has created before. After Alice’s transaction to Bob is confirmed (generally, in 6 blocks time), Bob sends Alice the purchased goods, and Alice releases her block(s) and tries to "bribe" other miners to mine on her fork. To do this, Alice discloses the private key(s) (of one or more) of the account(s) that she has transferred the money to in the block(s) she has just created. Rational miners who see the private key(s), may decide to work on Alice’s fork. They will create a new transaction to send the BTCs in the disclosed account to their accounts, and then try to create new blocks on Alice’s block. As soon as a miner finds a solution, Alice confirms it by disclosing the next private key. If she manages to give sufficient incentives to attract enough mining power to her fork, the second branch will take over the main one and the transaction between Alice and Bob will be undone.

Unless Alice encourages other miners to work on her fork, she cannot hope for her attack to be successful, because she has a small fraction of the network computational power. If mining on Alice’s fork is deemed more profitable by rational miners, they will join Alice’s fork. She needs to keep convincing miners to mine on her fork, while making sure that the attack remains profitable for her at the end.

In order to initiate the attack, Alice needs at least one block in her fork that contains transactions to the account IDs to be published. Assuming that a transaction needs six blocks to be confirmed, the attacker should have at least %14.28 of the network computational power. With such a power, the attacker can (in average) create one block in 70 minutes, that is the time required for the creation of 6 blocks by other miners (with %85.72 of the power) in the main fork.

IV. MATHEMATICAL ANALYSIS OF THE ATTACK

We first describe a basic analysis of our attack by using a Markov model. Some parts of the analysis are similar to the work done in \cite{32} to analyze the Whale Attack. However, we diverge at some point as that study only includes a special case of the attack, compared to our analysis which is generic and comprehensive. We also introduce some practical strategies that Alice can adopt to reduce the attack cost and increase her success rate.

A. A Basic Analysis

In our analysis we will use the notations listed in Table.1 We have:

\[
\lambda = \sum_{\forall i} P_i, \quad \mu + \sum_{\forall i} \lambda_i = 1 \tag{1}
\]

In the basic analysis, we denote Alice’s forked chain by \(X\) and the main chain by \(Y\). We define \(D_t\) to be the difference between these chains:

\[
D_t = L(Y, t) - L(X, t), \quad D_0 = C - l + 1 \tag{2}
\]

Based on (2), we develop a model for Bitcoin as shown in Fig.1. The figure shows an absorbing Markov chain. State \(V\) is the state in which all miners are disappointed to mine on
The number of blocks that are required for confirmation of
a transaction (6 in practice)
Set of all miners in descending order
The Bitcoin mining reward (6.25 BTC at the time of writing)
Set of all states in attack Markov chain
The mining power of miner $i$
The forked chain and the main chain, respectively.
The length of $X$ at time $t$ from the starting point of fork
The length of $Y$ at time $t$ from the starting point of fork
The number of blocks that are required for confirmation of
a transaction assuming that the chain starts from state $i$. This implies that entry $D_0$ (of $e$) will be the average number of states the attack goes through before it succeeds or fails.

In state $i$, Alice proposes $R_i$ as the reward of mining on $X$. At this time, a rational miner named $m$ with a mining power of $P_m$ wants to select the more profitable chain to mine on. If $m$ chooses $X$, then he receives the block reward only if the attack ultimately succeeds. Conditioned on the attack success, $m$ receives the rewards with a probability of $P_{X,S_i}/(\mu_i+P_m)$. If $P_{X,S_i}$ is the probability that the attack is successful at $i$, and $P_{Y,F,i}$ is the probability of the attack failure at $i$, miner $m$, between $X$ and $Y$, chooses the one that maximizes its expected profit. Mining on chain $X$ is profitable for miner $m$ in state $i$ when:

$$R_i > \frac{P_{Y,F,i} \times (P_m + \mu_i)}{\lambda_i \times P_{X,S_i}} \times F - F$$

To calculate $P_{Y,F,i}$ and $P_{X,S_i}$ in (4), one can use Theorem 11.6 of [35]. For this purpose, we need the transition probability matrix which in turn needs the bribe distribution (i.e. the interdependence between probability matrix and bribe distribution). To overcome this interdependence, we need a strategy in distributing the bribe which is designed and explained in the next section. In a special case, if the transition probability in the Markov chain remains constant during the attack time (worst case: none of the miners accepts the bribe), then $m$ will use (3) to decide if $X$ is more profitable than $Y$. This special case is the whole thing that the authors in [32] wanted to reach.
condition is: \[ \text{successful (failure, thus, (11) shows the average cost of attack when it is inline bribing, she will not lose anything in case of attack offer. Equation (10) shows the average attack cost regardless of the network power, and } D_0 = 6, \text{ then Alice should offer 876.2 BTC as the bribe before any event occurs. If the first event occurs on Alice’s chain, then she should offer an additional bribe of 371.9 BTC to keep her chain profitable to miner } m. \text{ The more events occur on her chain, the less bribe she needs to offer. Equation (10) shows the average attack cost regardless of its success or failure. Since in our scenario the attacker uses inline bribing, she will not lose anything in case of attack failure, thus, (11) shows the average cost of attack when it is successful (AS).}

\[
R_i > \frac{(1 - \left(\frac{\lambda}{\mu + \mu_p}\right)^{i+1}) \times (P_m + \mu)}{\lambda \times \left(\frac{\mu + \mu_p}{\lambda - \mu_p}\right)^{i+1}} \times F - F
\]  

\[
\text{AttackCost} = \sum_{i=0}^{W-1} P_{X,S,i} \times P_m \times (R_i + F) > \sum_{i=0}^{W-1} P_{Y,F,i} \times P_m \times F \quad (9)
\]

\[
\text{AttackCost}_{AS} = \sum_{i=0}^{W-1} B_{V,i} \times P_{D_{N_0,t}} \times R_i \quad (11)
\]

In the equations, \( N_{D_0,i} \) is obtained from (4), and \( B_{ij} \) is obtained from (5). If Alice’s goal is only to attract \( m \) to her chain and if she visits each state at most once (that is when all the events happen on chain \( X \)), the value of AttackCost for the above example will become 1495.6 BTC. It is worth knowing that this attack will succeed with a probability of \( \%0.26 \). As Alice mines on her chain too, she will try to obtain the bribe money she has offered as an ordinary miner. This has not been noted in any of the previous studies as far as we know. So in our example, the expected reward that Alice will earn is 997.1 BTC and \( m \)’s reward will be 498.5 BTC.

As we saw above, in the basic analysis, the cost of attack is very high and the probability of success is too low. These render the attack impractical. The reason is that the analysis assumed that there was only one rational miner in the network and ignored others’ computational power. To extend the analysis and to make the attack more practical, we need a bribing strategy. In the following section we will propose some strategies that reduce the AttackCost and increase the success probability.

### B. Attack Strategies

To extend the analysis to a network in which more than one rational miner exist, we need bribing strategies. Here, we propose and analyze three:

- ‘Biggest Fish First while Keeping the Previous Catch (BFF)’
- ‘Constant-Rate Bribing’ strategy (CRB).
- ‘Guaranteed Variable-Rate Bribing with Commitment’ strategy (GVC).

1) **BFF Strategy:** In this strategy, and in each state of the Markov chain, Alice tries to attract the next biggest miner from chain \( Y \) and bring it to \( X \), while preserving the miners she has attracted in previous states. In the following theorem, we will prove that selecting the biggest miner at each step is the best choice Alice can make in this strategy.

**Theorem 1:** Consider two miners, \( m_1 \) and \( m_2 \), with the computational powers \( P_{m_1} \) and \( P_{m_2} \), respectively. Assuming that \( P_{m_1} > P_{m_2} \), it is more profitable for the attacker to select \( m_1 \) as the target to add to chain \( X \) than \( m_2 \).

**Proof:** Based on:

\[
\begin{align*}
P_{Y,F,i,(m_2)} & > P_{Y,F,i,(m_1)} \\
& \text{or} \\
& P_{X,S,i,(m_2)} < P_{X,S,i,(m_1)}
\end{align*}
\]

and on (8):

\[
\begin{align*}
R_{i,m_2} & = \frac{(P_{m_2} + \mu)}{\lambda \times (\frac{\mu + P_{m_2}}{\lambda - P_{m_2}})^{i+1}} \times F - F \\
& = \frac{(\lambda - P_{m_2}) \times P_{Y,F,i,(m_2)}}{\lambda \times P_{X,S,i,(m_1)}} \times F - F \\
& > \frac{(\lambda - P_{m_1}) \times P_{Y,F,i,(m_1)}}{\lambda \times P_{X,S,i,(m_1)}} \times F - F \\
& = \frac{(P_{m_1} + \mu)}{\lambda \times P_{X,S,i,(m_1)}} \times F - F \leq R_{i,m_1}
\end{align*}
\]

in which \( R_{i,m_1} \) is the required bribe for \( m_1 \) in state \( i \).

Theorem 1 states that at each step, the biggest miner is the best choice to target. In BFF, Alice uses **Algorithm 1** to calculate the bribe amount at each state of the Markov chain, and miners use **Algorithm 2** to choose the chain to mine on.

In BFF, bribery in state \( i \) is profitable for \( m_{j^*} \in C_{-i} \) (assuming that miners are indexed according to their computational power). Alice tries to attract new miner(s) to her chain as well as keeping the previous miners that were attracted in the previous states. Let us assume that \( i \) is the current state. If the miners on \( Y \) find a block, the attack returns to state \( i + 1 \) and in this case, we assume that the miner who has joined \( X \) in state \( i \) will go back to \( Y \). The attacker presumably offers bribe in state \( i + 1 \) again, which will be the subject of Alice’s decision in this new state. There are certain situations the miner decides to stay on \( X \), but the consideration serves to establish an upper bound on the cost of the attack, since it underestimates the fraction of miners who might decide to...
mine on X. Line 2 in Algorithm 1 states that there is no bribe for states before \( i = C \).

2) CRB Strategy: In CRB, Alice offers a constant bribe at each step of the attack, with commitment. For each event in chain X, she releases the private key to a new account that has K Bitcoins. At each state, miners check to see if the bribes from the current state to V is profitable enough to join X. This strategy can persuade more miners to join if Alice chooses a proper value for K. By using (12), miner m can calculate the required bribe for each state, and find the minimum value of K for itself using (12).

\[
K_m = \frac{\sum_{i=Current\ State}^{V+1} N_{D,i} \times R_{im}}{\sum_{i=Current\ State}^{V+1} N_{D,0,i}} \geq K
\]  

\( K_m \) is the expected amount of constant bribe for m who rationally uses (12) to decide. It is obvious that going forward along the chain towards state V increases the success probability and makes K profitable for other miners too.

3) GVC Strategy: In BFF, the uncertainty about attack’s future increases its cost and the average number of times the first few states are visited in the Markov chain. As the amount of bribe in the initial attack states is high, frequent visits to them increase the cost significantly. GVC tries to give the miners the information needed to forecast the future through long-term calculation of the attack’s profitability. GVC assures miners that there will be enough bribe in the coming states in order to keep mining on Alice’s chain. This strategy attracts more miners at a lower cost. In GVC, Alice can off the chain guarantees (e.g. by smart contracts [56]) to assure miners that she will release the required bribe in the next states. This way, Alice is committed to release the private keys to the accounts holding the advertised Bitcoin bribes, until the attack finishes.

In this strategy, when the attack starts, Alice announces the amount of bribe for each state. She releases her commitment to these bribes too. CRB is a special case of GVC in which miners do not take other miner’s rationality into account and the value of bribe is constant, i.e. \( R_i = K; \forall i \leq C \).

Because of the commitments in GVC, miners estimate the computational power distribution at each state by seeing which miner can be convinced by the bribe. Here, we assume that there is no bribery in the states beyond C. The strategy tries to find a formula for \( R_i \) to increase the attack success probability and to decrease its cost. Alice can advertise a vector of bribes rather than a formula. We denote this vector by \( \bar{R} \). In GVC, miners calculate the probability of state transitions, and calculate the profitability of X and Y. Then they choose a chain to mine on. The calculation of profitability is a two-step job that is shown in Algorithm 3. Miners can pre-compute both steps of the algorithm. For the 2nd step, miners will have a vector of actions, i.e. action, that shows the action to be taken in state i. Each entry of the vector is either JoinX or JoinY.

Algorithm 2 Determining the profitable chain in state i

```plaintext
1: for each new Event do
2:   if i is not V or W then
3:     \( R_i = \) current offered bribe;
4:     if (equation (5) is valid) then
5:       JoinX();
6:     else
7:       JoinY();
8:     end if
9:   end if
10: end for
```

Algorithm 3 Finding NewMarkov and the profitable chain.

1: IST STEP (Obtaining NewMarkov)
2: Miners = Sort the miners in descending order ;
3: for each state i do
4:   List = 0;
5:   for each m in Miners do
6:     if m is the next biggest miner on Y;
7:       if (The (8) is valid for m) then
8:         Add m to List;
9:       else
10:         Adjust the transition probabilities from state i to \( i-1 \) & \( i+1 \) based on the sum of powers in List;
11:     end if
12:   end for
13:   end for
14: Break;
15: end if

16: // 2ND STEP (Obtaining the profitable chain)
17: for each new Event do
18:   i = Current State
19:   if my power is not included in i and i is not V or W then
20:     \( R_i = \) Current proposed bribe(s);
21:     if (The (7) is valid) then
22:       JoinX();
23:     else
24:       JoinY();
25:     end if
26:   end if
27: end for

Algorithm 1 Finding the required bribery for \( m_{j} \) in state i

```plaintext
1: for each new Event do
2:   j = C - i; // i is the Current State
3:   if i is not V or W then
4:     Add \( m_{j} \) (jth biggest miner) from Y to X;
5:     \( E = \) obtain \( R_{i,m_{j}} \) for \( m_{j} \) based on [8];
6:     if (there is already bribery in the network) then
7:       Release \( (E - existing\ bribe(s)) \) as the bribe;
8:     else
9:       Release E as the bribe;
10: end if
11: end if
12: end for
```
Now, we have FinalMarkov that can be used to calculate the attack cost and success probability for GVC.

C. The Future of Bribery Attack

In the future, the bribery attack for cryptocurrencies like Bitcoin in which reward goes down with time, will be one of the most prominent attacks. Since the only factor needed to compare the profitability of two chains is their block rewards (because the transaction fee in the main chain can be neutralized by the transaction fee in the attacker’s chain), by halving the block reward, the required bribe to persuade miners to mine on the attacker’s chain will decrease too.

D. Possible Countermeasures

One solution to overcome this attack is limiting the amount of BTC that a user can transfer. The limitation is closely related to the amount of block reward. If the attacker’s budget remains constant, decreasing the reward increases the attack success chance. So, in some cryptocurrencies like Bitcoin, mining algorithm should be equipped with a mechanism that adjusts the limit every years (when the reward falls). However, this solution has a drawback, since the attacker can transfer BTC with multiple addresses in the same block.

The other solution for the drawback is limiting the whole transferred BTC in each block. Like before, there should be a mechanism to adjust the limit in this solution. Such solution should take into account the situation in which there is no block reward and the only reward is the transaction fee. In any case, at least a soft-fork is necessary.

V. Numerical Analysis

In our analyses, we use the realistic mining power distribution of the Bitcoin pools available at http://www.btc.com (Table |). We assume Alice, i.e. the attacker, is the largest of those pools (μ = 0.2123), and P2 is m (the largest miner on Y). We further assume that Alice has created at least one block on her chain during block confirmation on the main chain and also we assume that the states i > C do not include any bribe.

We analyze the following strategies:

- Basic Strategy (BS): Only one rational miner (i.e. m) is targeted by Alice. This is similar to the Whale Attack.
- BFF: Targeting the next biggest miner on Y in each state.
- CRB: We analyze cases in which bribery is done to attract m as the biggest miner. Other miners may join X in the states close to V, and our analysis will take those into account too. We will analyze two types of this strategy, CRB1 and CRB2. In CRB1, regardless which state the attack started, Alice calculates the value of K for m from state C. In CRB2 Alice starts calculating the bribe from D0 and leaves the bribe for states j: j > D0 zero.
- GVC: To make it comparable with other strategies, we assume that this strategy is used only to attract m to Alice’s chain. It is clear that Alice may decide to offer bribe in the final states based on BaseMarkov to decrease the amount of bribe needed in the earlier states (to persuade m).
TABLE II

| Abbr. | Pool Name | Power | Abbr. | Pool Name | Power |
|-------|-----------|-------|-------|-----------|-------|
|       | Whole Network | 1     | P8    | BTC.TOP   | 0.0716 |
| P1    | BTC.com   | 0.2123| P9    | BitFury   | 0.0543 |
| P2    | AntPool   | 0.1284| P10   | Bitcoin.com | 0.0247 |
| P3    | Poolin    | 0.0988| P11   | Huobi.pool | 0.0247 |
| P4    | unknown   | 0.0963| P12   | BitClub    | 0.0123 |
| P5    | F2Pool    | 0.0938| P13   | WATLCN    | 0.0074 |
| P6    | ViaBTC    | 0.0866| P14   | Bixin     | 0.0049 |
| P7    | SlushPool | 0.0815| P15   | Eobot     | 0.0025 |

![Graph](https://example.com/graph.png)

Fig. 3. Success probability of different bribery attack strategies.

In all of the above strategies, we only focus on the results with minimum attack cost. Figure 3(a) depicts the success probability of attack in different strategies when they try to attract \( m \) to Alice’s chain. In this figure, x-axis shows the starting state of the attack and y-axis shows the success probability. For example if the attack starts from \( i = 4 \), and Alice takes the BFF strategy, then the success probability will be around 60%. The figure shows a low success probability for the BS strategy compared to other strategies. All the results have been calculated from Alice’s point of view. In this view, there is no bribing in the states \( i > C \), and the transition probability remains constant. In GVC and CRB, the miners’ point of view is the same as Alice’s, because the commitment disclosures that there will be no bribe money in the states \( i > C \). In other strategies, miners also counted themselves in for the states \( i > C \) and during the calculation of the required bribe. They left Alice’s chain when they saw that the chain was not profitable anymore. In these strategies, the success probability from the miners’ point of view is higher than those of Fig. 3(a).

The other interesting result is the cost of attack in different strategies. Fig. 3(b) shows the minimum of average cost regardless of the attack result, and, Fig. 3(c) shows the minimum of average cost when the attack succeed. The figures show the minimum of average cost for each strategy when they try to attract \( m \) to Alice’s chain, and for different values of \( i \) (starting state). For example, if \( i = 4 \), the average cost of CRB2 will be about 192 BTC. These figures show a high average cost for the BS strategy. Combined with Fig. 3(a), the results show the inefficiency of the BS strategy. To calculate the attack cost (for BFF and BS, based on (10) and (11)), \( R_i \) is obtained from the point of miner’s view, and \( N_{D_{0ij}} \) from the point of attacker’s view.

Fig. 3 shows the bribe amount in each state for different values of \( i \) (as the starting point of attack). It is clear that by increasing the bribe in each state for any strategy, the success probability of that strategy will go up. However, in the results, the calculation focuses only on the minimum cost of attack when Alice tries to attract \( m \) as the biggest miner on the main chain. In the figure we have two types of GVC; GVC\(_{AC}\) and GVC\(_{RAC}\). The former focuses on the minimum average cost regardless of the attack result and the later focuses on the minimum average cost when the attack succeed. Based on the figure, Alice should offer [25.51, 6.43, 72.25, 37.02, 8.6, \( \epsilon \)], where \( \epsilon = \text{One Satoshi} \), as the bribe vector as well as commitment on the vector if she follows the GVC\(_{AC}\) strategy. In this example, the average cost of attack and success probability will be 105 BTC and 43.25, respectively. In almost all cases, the GVC strategy yields the lowest cost and offers reasonable success probabilities compared to other strategies. As shown in the figure, there is no change in bribe distribution for the BS, BFF and CRB1 strategies with different values of \( i \). Because these strategies only take specific miner(s) into account in each state thus letting other miners select the main chain as the profitable chain. For all \( i \) values in Fig. 3, the GVC strategy tries to apply bribe based on BaseMarkov in the final states. Such a distribution makes huge savings in the bribe spent in the earlier states. That is why in some states (e.g. in the middle states, like 2 or 3), the amount of bribe is higher than that of the earlier states. By comparing GVC with BS and BFF, the amount of bribes in the states \( i = 3 \) and below, follow similar patterns, but increasing the bribe in these states in GVC and making commitment on them, decreases the required bribe for the states \( i = 4 \) and above.

In the previous figures, the amount of block reward is assumed to be 6.25 BTC. Fig. 5 depicts the attack cost in the future for different values of Bitcoin block reward. As shown, the cost of attack falls down dramatically as the block reward is halved (rate 1/2). If the value of BTC remains almost constant (or its growth rate is equal to or less than 2), the attack cost in Fig. 5 shows that bribery attack will be a big challenge in the future of cryptocurrencies.

VI. Conclusion

In this paper, a novel analysis was done on the bribery attack which also generalized the previous analyses in this domain. Moreover, new strategies were presented to substantially reduce the cost of attack and increase its success probability. It was shown that unlike the Whale Attack, an attacker can make bribery attack practical by designing and adopting right strategies. The strategies introduced, analyzed and simulated in this paper only serve as examples, yet they show how destructive this attack can be. The main contribution of the
paper is paving the way by giving a rather general framework for the bribery attack that can accommodate any strategy. The distribution of computational power in the cryptocurrency’s network influences the type of strategy adopted. It was shown that this attack will be a big challenge in the future of cryptocurrencies as the block rewards fade gradually. Two solutions were also proposed to mitigate the effect of this attack. The solutions make soft-forks on Bitcoin thus it can remain backward-compatible. As a future work, we want to work on the solutions proposed to bribery attack, and more specifically, on obtaining an effective limit on the amount of BTC in each transaction (1st solution) or in the whole block’s transactions (2nd solution). These depend on some variables like block reward and level of confirmation in the target cryptocurrency.

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