GaN/AlN quantum dots for single qubit emitters

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Abstract

We study theoretically the electronic properties of c-plane GaN/AlN quantum dots (QDs) with the focus on their potential as sources of single polarized photons for future quantum communication systems. Within the framework of eight-band \( k \cdot p \) theory we calculate the optical interband transitions of the QDs and their polarization properties. We show that an anisotropy of the QD confinement potential in the basal plane (e.g. QD elongation or strain anisotropy) leads to a pronounced linear polarization of the ground-state and excited-state transitions. An externally applied uniaxial stress can be used to either induce a linear polarization of the ground-state transition for emission of single polarized photons or even to compensate the polarization induced by the structural elongation. (Some figures in this article are in colour only in the electronic version)

1. Introduction

Electrically triggered sources of single photons are essential building blocks for future quantum communication and quantum computing systems. Devices based on single quantum dots (QDs) are promising candidates for reliable low-cost solutions in this matter. Single-photon emitters (SPEs) with extraordinary spectral purity have been realized recently using InAs/GaAs QDs [1, 2]. Here, emission with controlled linear polarization is achieved at low temperatures by exploiting the fine-structure splitting (FSS) of the exciton ground state. At elevated temperatures, however, this splitting, of up to 500 \( \mu \text{eV} \) for large QDs [3], is smaller than the homogeneous linewidth, inhibiting a spectral separation of the co-polarized line pair. Nitride-based QDs present important alternatives for single-photon emission. In \( \mu \) photoluminescence and cathodoluminescence (CL) spectroscopy narrow emission lines from single InGaN/GaN [4–11] and GaN/AlN QDs grown on the c plane [12–16] and a plane [17] have been demonstrated. Also zinc-blende GaN/AlN QDs are under investigation [18, 19]. In the future the spectral range of nitride QDs can be extended to the long-wavelength range for fiber-optical communication employing InN/GaN [20]. Optically pumped single-photon emission from single GaN/AlN QDs has already been demonstrated [14]. For InGaN/GaN QDs a polarization mechanism based on valence-band (VB) mixing effects has been discovered recently [11, 21] that leads to a separation of differently polarized lines more than one order of magnitude larger than the FSS in InAs/GaAs QDs. Similar polarization effects have been reported for c-plane GaN/AlN QDs shortly after [15, 22].

In this paper, we show that VB mixing effects can be exploited to control the polarization of photons emitted by single GaN/AlN QDs. First, the polarization mechanism observed for InGaN/GaN QDs will be revisited in section 2. Then, we will turn our attention to the GaN/AlN system. We calculate the polarization of the optical interband transitions for GaN/AlN QDs using strain-dependent eight-band \( k \cdot p \) theory (section 3). The model accounts for piezo- and pyroelectric effects and is implemented for arbitrarily shaped QDs. It is described in more detail in the appendix.

We show that an asymmetric strain field in the growth plane inside the QDs leads to a linear polarization of the confined A- and B-type excitonic states in orthogonal directions. The in-plane strain anisotropy can originate from different sources, such as QD elongation, inhomogeneous composition profiles, etc. As examples a slight elongation
of the QDs (section 3.2) and, as an ex situ approach, the application of external uniaxial stress (section 3.3) are considered in detail.

2. Polarization effects in InGaN/GaN quantum dots

We have shown recently that emission lines from single InGaN/GaN QDs are systematically linearly polarized in the orthogonal crystal directions [1120] and [T100]—a symmetry that is non-native to hexagonal crystals [11, 21]. The polarization of the emission lines has been attributed to the character of the hole state (formed by either the A or B VB) involved in the recombination process and a slight elongation of the QDs. The InGa1−xN/GaN samples were grown in the wurtzite phase by metal–organic chemical vapor deposition on Si(111) substrates. The InGaN layers were grown at 800 °C with a nominal thickness of 2 nm using trimethylgallium, trimethylindium and ammonia as precursors. The QDs are formed by alloy fluctuations within the InGaN layer [6]. The sample has been investigated with single-QD CL employing Pt shadow masks to probe only a few QDs. Further discrimination of the single-QD lines was possible using their temporal jitter: all lines originating from the same QD show the same characteristic jitter pattern. Line groups of up to five narrow lines with the same jitter pattern could be identified [11]. An example of such a single-QD spectrum is shown in figure 1. All emission lines show a pronounced linear polarization. The polarization directions scatter around [7110] and [1110]—a symmetry that is non-native to hexagonal crystals [11, 21]. The polarization directions scatter around [1120] and [T100]—a symmetry that is non-native to hexagonal crystals [11, 21]. The polarization of the emission lines has been attributed to the character of the hole state (formed by either the A or B VB) involved in the recombination process and a slight elongation of the QDs.

The emission patterns differ significantly from the well-known polarized emission spectra of II/VI and III/V QDs with cubic crystal structure. Exchange-interaction-induced FSS of the exciton (see, e.g., [3, 23, 24]) or other excitonic complexes has not yet been reported for nitride QDs.

In contrast to InAs/GaAs QDs or GaN/AlN QDs, which grow in the strain-induced Stranski–Krastanov or Volmer–Weber growth modes, the InGa1−xN/GaN QDs form within the InGa1−xN layer due to composition fluctuations within the layer. For a theoretical description these QDs have been modeled as ellipsoids with linearly graded indium concentration [11, 21, 25]. The maximum indium concentration x_c at the QDs’ centers is 50%, while the minimum concentration x_c at the QDs’ borders is 5%. The QDs are embedded in an In_{0.05}Ga_{0.95}N quantum well with a height of 2 nm. The QDs have a height of d_z = 2 nm and lateral extensions of d_{x/y} = 4.6–5.8 nm. Henceforth x will denote the direction of the QDs’ long axes. Further details on the calculations can be found in the appendix.

The single-particle electron and hole orbitals are depicted in figure 2 for a circular QD (a) and a slightly elongated QD (b). The electron ground-state (e_0) envelope functions have s-like symmetry; the envelope functions of the first excited electron state (e_1) is p-like. In contrast, the first two hole states, h_1 and h_2, both have s-like envelope functions. Both states have sizable oscillator strengths with the electron ground state, but behave differently if the strain field within the QD is anisotropic in the basal plane, e.g., due to an elongated QD shape: h_1 aligns parallel to the QD’s long axis, h_2 perpendicular to it. An analysis of the projections of both hole states on the k · p basis states P_x and P_y yields that the P_x (P_y) projection of h_1 (h_2) increases with increasing QD elongation, while the P_y (P_x) projection decreases [21]. Consequently, the optical transition between h_1 (h_2) and e_0 is linearly polarized (perpendicular) to the long axis of the QD. The polarization increases with increasing QD elongation (figure 3).
3. GaN/AlN quantum dots

In contrast to the In$_x$Ga$_{1-x}$N/GaN QDs discussed in section 2, GaN/AlN QDs grow strain induced in the Stran ski-Krastanov or Volmer-Weber growth mode. Also their typical size and shape is known with greater accuracy. Experimental reports on the structural properties of c-plane GaN QDs (e.g. [12, 14, 26–28]) agree on the shape of the QDs, which is a truncated hexagonal pyramid. The reported heights ($h$) scatter between 1.3 and 5 nm. The aspect ratios ($h:d$, where $d$ denotes the lateral diameter) in most reports are in the range of 1:5–1:10. The model structure derived from these reports is depicted in figure 4. The model QDs have an aspect ratio of 1:5. The height of the QDs is varied for QDs with an aspect ratio of 1:5 (figure 6(a)). The model structure of c-plane GaN/AlN QDs: truncated hexagonal pyramid with height $h$ between 1.5 and 3.5 nm. The lateral diameter $d$ is determined by the dot’s aspect ratio $h:d = 1:10$ (1:5). The wetting-layer thickness is $w = 0.25$ nm.

Figure 4. Model structure of c-plane GaN/AlN QDs: truncated hexagonal pyramid with height $h$ between 1.5 and 3.5 nm. The lateral diameter $d$ is determined by the dot’s aspect ratio $h:d = 1:10$ (1:5). The wetting-layer thickness is $w = 0.25$ nm.

3.1. Single-particle energy levels

The bound states in GaN/AlN QDs are—as in the case of In$_x$Ga$_{1-x}$N/GaN QDs—formed predominantly by the A and B band. C-band contributions are small because the biaxial strain within the QDs shifts this band to much lower energies [11, 25]. As a first approximation, for each band we expect to find a ground state with an s-shaped envelope function, which is only spin degenerate. The p shell consists of two states and the d shell of three. Due to the different parities of the bulk conduction and valence bands, the electron and hole states have a finite optical matrix element if their envelope functions have the same parity, i.e. the allowed transition channels are s–s, p–p, s–d, etc. Each transition channel exists twice, once for the A-type holes and once for the B-type holes. Figure 6 shows the calculated single-particle electron and hole energy levels of all QDs considered in this work including the six energetically lowest (highest) electron (hole) states. The electron states are all formed predominantly by the conduction band ($\approx 95\%$). Therefore, the s, p and d shells can be clearly distinguished. The hole spectra, however, are more complex, because hole states are not formed by either the A or B band, but by a mixture of both bands and even a small C-band contribution. Still each hole state can be characterized by the band that contributes the most to it (see labels in figure 6). For QDs with an aspect ratio of 1:5 (figure 6(a)) the A-band s-state ($h_0 \equiv h_A; \approx 95\%$ A-band projection) and the B-band s-state ($h_1 \equiv h_B; \approx 90\%$ B-band projection) are energetically well separated from the excited hole states. Both have an unambiguously s-shaped envelope function (not shown here). The splitting between both states ($\approx 9–10$ meV) does not increase for smaller QDs, but is constant. It corresponds to the energy separation between A and B band in strained GaN. The higher excited hole states cannot be unambiguously assigned to p- or d-like orbitals. Please note that, although they have...
been labeled according to the major band contributions, this contribution sometimes does not exceed 50%. The QDs with aspect ratio 1:10 (figure 6(b)) exhibit a significantly smaller excited-state splitting for electrons and holes due to the weaker lateral confinement. An exception is the splitting between h\textsubscript{A} and h\textsubscript{B}, which is largely independent from the QD dimensions as discussed before.

3.2. Optical transitions and their polarization

In bulk GaN an anisotropy of the strain field in the basal plane changes the character of the band-edge states from A (B) type to P\textsubscript{x} (P\textsubscript{y}), if the stress is larger along y (see figure 7). The optical matrix elements involving the confined A- or B-band hole states in the QDs respond differently to an asymmetry of the confinement potential in the basal plane: they become linearly polarized in orthogonal directions. Figure 8(a) shows the oscillator strengths between the six lowest electron levels e\textsubscript{i} and the twelve highest hole levels h\textsubscript{j} (up to an energy difference e\textsubscript{i} − h\textsubscript{j} of 3.75 eV) for the QD with h:d = 1:5 and h = 2.0 nm. Figure 8(b) shows the respective spectrum for a similar QD with an in-plane elongation of 10% along [11\textsubscript{20}]. Almost all transitions of the elongated dot show a pronounced linear polarization either parallel to the elongation or perpendicular to it. The transition between the electron ground state e\textsubscript{0} and h\textsubscript{A} and (e\textsubscript{0}, h\textsubscript{B}) transitions in the s-channel is independent of the size of the QDs or their vertical aspect ratio. For (in-plane) symmetric QDs it is about 10 meV and increases for anisotropic QDs. This large separation between the orthogonally polarized lines should enable a spectral separation of both lines even at elevated temperatures. Thus, the well-defined polarization of the ground-state transition can be exploited for polarization control in future SPEs.

3.3. Control of the polarization by uniaxial stress

Since the linear polarization of the transitions is a result of the strain anisotropy, it can be induced by uniaxial stress, without any structural anisotropy of the dot. The effect of uniaxial stress on the polarization of the ground-state transition
applied stress. Thus, it is possible to control the polarization of (due to the formation of cracks or defects) or by externally by anisotropic strain relaxation in epitaxial heterostructures polarization is found at stress levels that can easily be induced easily enhanced or even inverted by the external stress.
squares). The polarization induced by the structure can be

\[ x \]

with 10% elongation along

\[ h \]

height of

\[ 2 \text{ nm} \]

for three different QDs with an aspect ratio of

\[ 1:10 \]

and a

\[ 0 \text{ nm} \]

Circles: symmetrical QD. Diamonds: QDs with 10% elongation along \( x \). Squares: QDs with 10% elongation along \( y \).

of a symmetric QD with aspect ratio 1:10 and height 2 nm is shown in figure 9 (black line and circles). A pronounced polarization is found at stress levels that can easily be induced by anisotropic strain relaxation in epitaxial heterostructures (due to the formation of cracks or defects) or by externally applied stress. Thus, it is possible to control the polarization of the emitted photons. Figure 9 also shows similar calculations for elongated QDs (blue lines and diamonds; red lines and squares). The polarization induced by the structure can be easily enhanced or even inverted by the external stress.

4. Summary

We have theoretically investigated the spectroscopic properties of c-plane GaN/AlN QDs with a special emphasis on their suitability as sources of single polarized photons. We have shown that the linear polarization of the interband transitions is effectively controlled by an anisotropic strain field within the QDs. Transitions involving either A- or B-type hole states are polarized in orthogonal directions. The separation of the A-type ground state and the orthogonally polarized B-type first excited state is \( \approx 10 \text{ meV} \) and largely independent from the QD size and shape.

A sufficient anisotropy can be induced either by a structural elongation of the QDs or by an externally applied uniaxial stress. An in-plane elongation of the QDs of only 10% leads to a polarization degree of the excitonic ground-state transition of up to 6:1, depending on the other structural parameters of the QDs. An externally applied uniaxial stress of about 300 MPa leads to a polarization degree of more than 5:1; larger stress results in a complete polarization of the emission. Moreover, a polarization resulting from structural elongation of the QDs can be compensated by external stress. This effect could be exploited for future devices, in particular to achieve a well-defined polarization in QD-based single-photon emitters.

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Appendix. Method of calculation

For the electronic structure calculations we use a three-dimensional eight-band \( k \cdot p \) model implemented on a finite differences grid. The model accounts for strain effects, piezoelectric and pyroelectric polarization, spin–orbit and crystal-field splitting, and coupling between the valence bands (VBs) and the conduction band (CB). The \( k \cdot p \) method is based on the one originally introduced by Stier et al [32]. The implementation for wurzite crystals is described in detail in [25]. Details of the calculation of radiative lifetimes are given in [33]. Few-particle corrections have been included using a self-consistent Hartree (mean-field) scheme [25]. For the In\(_{x}\)Ga\(_{1-x}\)N/GaN system material parameters from [34] have been included as described in [11]. Most of the material parameters used for the GaN/AIN system are based on the recommendations of Vurgaftman and Meyer [35]. For the parameters \( m_i^2 \), \( A_i \) and \( E_i \) we use recently developed band-dispersion parameters [34, 36] derived from accurate quasiparticle energy calculations [37]. For the valence band offset between GaN and AlN we use the value of 0.8 eV determined by Wei and Zunger [38]. As already detailed in [25], we neglect the anisotropy of the static dielectric constants \( \epsilon_r \) and use the mean value for all directions. For the refractive index of AlN we use the Sellmeier formula derived by Antoine-Vincent et al [39].

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