Desynchronisation of Glycolytic Oscillations in Yeast Cell Populations

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Abstract

Glycolytic oscillations of intact yeast cells of the strain Saccharomyces carlsbergensis were investigated at both the levels of cell populations and of individual cells. Individual cells showed glycolytic oscillations even at very low cell densities (e.g. 1.0 × 10^5 cells/ml). By contrast, the collective behaviour on the population level was cell density-dependent: at high cell densities it is oscillatory, but below the threshold density of 1.0 × 10^6 cells/ml the collective dynamics becomes quiescent. We demonstrate that the transition in the collective dynamics is caused by the desynchronisation of the oscillations of individual cells. This is characteristic for a Kuramoto transition. Spatially resolved measurements at low cell densities revealed that even cells that adhere to their neighbours oscillated with their own, independent frequencies and phases.

Introduction

Synchronisation is a wide-spread phenomenon of spontaneous self-organisation, where individuals coordinate their behaviour, such that collective, macroscopic dynamics emerges [1–3]. In synchronised populations of coupled oscillators, for instance cells, all individuals adhere to a collective, common rhythm. Typical examples of synchronisation in biological systems are the blinking rhythms of male fireflies [4,5], the synchronisation of various circadian rhythms in mammals [6–8], the activity of brain areas [9,10], the synchronisation of cells in the ‘segmentation clock’ of vertebrates [11], the immune response to malaria parasites [12,13], the onset of collective behaviour in social amoebae [14], and the macroscopic, collective glycolytic oscillations of yeast cells [15].

For unicellular organisms, such as yeast, life within a community is beneficial for the long-term survival [16]. Efficient cell-cell communication is a prerequisite for the organisation of communities, and such communication among individuals may be provided by metabolic oscillations.

Glycolysis is a fundamental pathway in the energy metabolism of eukaryotic cells and it may show oscillatory dynamics. Therefore, glycolytic oscillations of NADH and other metabolites that occur in populations of the yeasts Saccharomyces carlsbergensis and Saccharomyces cerevisiae have been intensively studied [17–21]. In dense populations, the individual cells synchronise their metabolism to a joint oscillatory mode [18,22]. This has been demonstrated in experiments, where two sub-populations that oscillated with the same frequency, but at opposite phases, were blended and a new, collective oscillatory time-trace was recovered after a few minutes (i.e. after a few oscillatory cycles) [20,23].

The coupling of individual cells is believed to be based on the relay and subsequent diffusion of messenger molecules through the extracellular medium, where they are absorbed by the other cells [23]. It is conjectured that mainly acetaldehyde plays the role of the coupling molecule [20]. In addition to studies in stirred cell suspensions, the propagation of waves of glycolytic activity has recently been observed in spatially extended media, such as settled cell suspensions [24] or gel-entrapped cells [25].

During the last two decades, substantial efforts have been made to develop realistic, detailed mechanistic models, which describe the glycolysis, its oscillations, and the cell-cell communication [26,27]. Such models have been further used to study, for instance, the effect of intercellular coupling of yeast cells on the dynamics [26,28–30], or the robustness of glycolytic oscillations towards internal and external fluctuations [30,31].

Already early on, it has been observed that the dynamics of a cell population sensitively depends on cell density. At high cell densities yeast cells show synchronous, coherent oscillations. Once the cell density lies below a critical threshold, the yeast population no longer displays any collective oscillations, and rather remains quiescent [32].

The transition between collective oscillatory and stationary dynamics at the population level can follow two different mechanisms. The first of them, called ‘dynamical quorum sensing’ [33,34], consists in the simultaneous cessation of oscillatory dynamics in every cell as the cell density drops below the critical threshold. Thus, the stationary dynamics at the collective level is identical to that of all cells of the population. Alternatively, the transition between quiescence and oscillatory dynamics at the collective, macroscopic level may be due to a so-called ‘Kuramoto transition’ [35,36]. The collective oscillatory signal is generated at high cell densities, where the oscillations of all individual cells are
coherent and synchronised, both in phase and oscillation period. At low densities, the yeast cells remain oscillatory, but they lose their coherence so that each of them oscillates with its own phase. As the collective behaviour is the sum of the single cell signals, phase-incoherent oscillations will lead to a stationary collective dynamics [37,38].

How individual cells behave dynamically in low-density populations remains an important and still open question. While microscopy studies have indicated that the individual cells may still continue to oscillate at low cell densities [39], a recent study advocates that cells of *Saccharomyces cerevisiae* follow a 'dynamical quorum sensing' transition [33]. This interpretation is inferred from relaxation experiments, where, at low densities, cells are triggered to oscillate by an external stimulus, and the induced coherent oscillations were observed to decay in time [33]. Further support was drawn from studies in a flow-cell, where individual cells were quiescent and, again, could be stimulated by periodic addition of acetaldehyde to perform transient oscillations [40].

The present study aims to unravel the nature of the cell-density-dependent transition between oscillatory and stationary dynamics of intact yeast cells. The dynamics of immobilised cells of the yeast *S. carlsbergensis* is investigated at both the individual and collective level by using highly light- and position-sensitive single photon counting fluorescence detectors. We provide evidence that the dynamics in populations of *S. cerevisiae* is similar to that observed in *S. carlsbergensis*.

Materials and Methods

Experiments were performed with aerobically grown yeast cells from *Saccharomyces carlsbergensis* (ATCC 9080; American Type Culture Collection, Manassas, VA, USA) cultivated aerobically in a rotary shaker (180 rpm) in liquid semisynthetic minimal medium [22] at 28°C. The cells were grown until the glucose in the medium was just exhausted at the transition from the logarithmic to the stationary growth phase. After harvesting the cells by centrifugation at 5,000 × g at 21°C and washing them with distilled water, the wet cells were suspended in 0.1 M KH₂PO₄ buffer, pH 6.5, as a 20% (weight/volume) suspension and stirred at 25°C until they showed NADH oscillations. This generally occurred after 3–5 h of starvation. After starvation the cells were aliquoted in 1.5 ml Eppendorf cups and kept at 0°C for at most 3 days until they showed NADH oscillations. The global, collective signal of the whole population of yeast cells of *S. carlsbergensis* was measured with an inverted Nikon Ti Eclipse (Nikon GmbH, Germany) microscope, equipped with a 100 x/0.5–1.3 plan fluor lens and a position sensitive single photon counting photomultiplier tube as described previously [43]. For excitation of intracellular NADH a 8 MHz pulsed frequency-tripled Nd:vanadate laser tuned at 355 nm (HighQ Laser, Austria) was used. A dichroic mirror (z355rdc, AHF Analysentechnik, Germany) discriminated between excitation and emission. The emission light of yeast cells was filtered by a long-pass (LP 442 nm, Brightline, AHF, Germany) and a bandpass filter (FF01-440/40, Brightline, AHF, Germany) and detected by the photomultiplier. For all studied samples, the laser intensity was adjusted such that there was an incidence of 3,000–65,000 fluorescence photons/s at the detector, thus making sure that it operates under optimal conditions. The acquired photon positions were binned into frames of 512 × 512 pixels, resulting in a resolution of 0.33μm/pixel in the object space. The field of view had a diameter of 169μm. The photon flux was integrated over 2 s time intervals, which was a sufficient sampling rate to analyse glycolytic oscillations with periods in a range of ~24–70 s.

Image analysis

The global, collective signal of the whole population of yeast cells and the signal from individual cells were analysed separately. The immobilised yeast cells were randomly distributed on the coverslip. The collective signal was determined as the fluorescence light emitted from all cells in the entire area of observation. Therefore, all incident photons were summed up every second.

For the analysis of single cell signals, the position of each cell in the population was determined and its area, in pixels, marked. At any time, the single cell fluorescence *F*ₜₑₛ is the mean value of the intensity of the fluorescence signal detected in the area occupied by an individual cell

\[ F_{\text{cell}} = \sum_{a} \frac{c}{a}, \]

where *c* is the number of incident photons originating from the area *a* of the single cell. The temporal sequence of *F*ₜₑₛ yields the time evolution of the fluorescence of an individual cell. For
comparison, the amplitudes of the metabolic oscillations of the individual cells were normalised. Here, the norm was set by the oscillating amplitude of the cell in the population that showed the highest oscillatory amplitudes.

Analysis of synchronicity within populations

From the time series of each cell in a population, we subtracted the baseline to eliminate spurious drifts and trends. The baseline was computed as the walking average of the fluorescence data using a time window corresponding to one period of oscillation. After baseline subtraction, we obtained oscillations around zero and determined their frequencies by a fast Fourier transform. The typical behaviour of yeast cells at very low cell densities is 0.3%, the coherence among the collective oscillations remained oscillatory (Video S2). In fact, these individual oscillations were clearly detectable and long-lasting, even in very sparse populations (Fig. 2, where \( \rho = 0.001\% \)).

The typical behaviour of yeast cells at very low cell densities is presented in Fig. 3 and Video S2, where \( \rho = 0.01\% \). Each cell oscillated with its own phase (Fig. 3c) and the phases of the individual cells did not synchronise. Furthermore, the amplitudes of the metabolic oscillations varied, and so did the instants, when the oscillations set in in each individual cell (Fig. 3b). The low values of the order parameter \( K \) (Fig. 3d) indicated decoherence between the dynamics of the oscillating cells. Consequently, the collective fluorescence signal of the entire population showed stationary behaviour (Fig. 3a).

Experiments were performed at different cell densities to find the transition between synchronised metabolic oscillations and the loss of synchrony as function of the population density. As the cell densities were decreased to \( \rho \leq 0.3\% \), the coherence among the cells was found to diminish. Below \( \rho < 0.01\% \) collective oscillations ceased, giving way to quiescent but often noisy time traces of NADH fluorescence (Fig. 2). However, the dynamics of individual yeast cells from low-density populations \( \rho < 0.01\% \) remained oscillatory (Video S1). The time-dependent Kuramoto order parameter \( K \) was close to 1, indicating a high degree of synchronisation and coherence of the cellular oscillations (Fig. 1d). Collective, global oscillations can be observed down to cell densities of \( \rho < 0.01\% \). Below this cell density, collective oscillations ceased, giving way to quiescent but often noisy time traces of NADH fluorescence (Fig. 2). However, the dynamics of individual yeast cells from low-density populations \( \rho < 0.01\% \) remained oscillatory (Video S2). In fact, these individual oscillations were clearly detectable and long-lasting, even in very sparse populations (Fig. 2, where \( \rho = 0.001\% \)).

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The experiments show that while the individual cells remained oscillatory at all cell densities studied \( (0.001\% \leq \rho \leq 0.8\%) \), the collective behaviour changed depending on the cell density. For very dense populations, \( \rho \geq 0.3\% \), the cellular oscillations were fully synchronised, leading to well developed collective oscillations. At intermediate densities \( (0.01\% < \rho \leq 0.3\%) \) the cells became increasingly decoherent as \( \rho \) decreased, yielding transient episodes of collective oscillations. Finally, at very sparse populations \( (\rho \leq 0.01\%) \) the collective dynamics was always quiescent.

To investigate whether spatial effects played a role during the loss of synchrony, the oscillation frequencies of individual cells were determined. An overview of oscillation periods of single cells and their spatial distributions is shown in Fig. 5. In dense populations, individual cells displayed oscillations that lay within a narrow frequency band, whereas the frequency band broadened as \( \rho \) decreased below 0.3%. In such populations, we did not find any
domains, where all cells oscillated with the same frequency (or period). Instead, in some cases we observed that even adjacent cells oscillated with different periods (Fig. 5b,c).

The loss of frequency coherence among the cells in low-density populations (Fig. 5) led to a spread of oscillation periods. Their distribution was found to be Gaussian and the standard deviation \( \sigma_T \) was used as a measure for the coherence of the glycolytic oscillations. The standard deviation \( \sigma_T \) of the oscillation periods in dependence of the cell density is compiled in Fig. 6. While at \( \rho \geq 0.3\% \) the distributions of oscillation periods remained narrow (i.e., \( \sigma_T < 2\ s \)), the distributions broadened, as \( \rho \) fell below 0.3\%. As the sampling rate of the analysis was 2 s, any value of \( \sigma_T \leq 2\ s \) indicates synchronisation of the oscillations of individual cells in the population.

Alternatively, the transition from synchronised to desynchronised behaviour was determined by calculating the time-averaged order parameter \( K \) for each experiment (Fig. 7). Again, the phase synchronisation for \( \rho > 0.3\% \) was high (\( K \sim 1 \)), whereas a decrease of \( \rho \) below 0.3\% led to a loss of coherence, which is reflected by the small values of \( K \). Very close to the critical cell density \( \rho_{crit} = 0.3\% \), the standard deviations \( \sigma_K \) of the Kuramoto parameter \( K(t) \) increased, since the oscillation phases of the individual cells desynchronised transiently.

**Discussion**

More than three decades ago, the question has been risen, what happens on the single cell level, when the macroscopic, collective oscillations in yeast cell populations disappear [32]. For immobilised cells of the yeast *Saccharomyces carlsbergensis*, we now provide an answer: The individual cells continue to oscillate, even if the collective oscillations cease and the macroscopic dynamics becomes quiescent. The oscillatory dynamics of individual cells persists for very low cell densities (down to \( \rho = 0.001\% \)), where the cells are almost isolated. To determine whether the persistence of oscillations at extremely low cell densities is a specific feature of *S. carlsbergensis* or whether this behaviour is a general property of...
Figure 3. Collective and individual dynamics of *S. carlsbergensis* at a cell density of 0.01%. At $t = 0$ an aliquot of 52 mM glucose was added to the starved and immobilised cells. (a) The time-series of the macroscopic, collective fluorescence signal is noisy but quiescent. Transient reminicences of oscillations can be spotted at $200 \leq t \leq 400$ s. (b) The individual cells remain oscillatory, even at this low cell density. The normalised oscillation amplitudes of the individual cells are decoherent. The amplitude of the oscillations of the cells corresponds to 120–200 photons/s.) Note, that the time spans where individual cells show pronounced oscillatory amplitudes vary considerably from cell to cell. The cells are numbered in a random order. (c) The plot of the phases of the oscillations shows that each cell oscillates, however, with its own phase and oscillation period. A slight and transient entrainment in the oscillation phases may be observed for some cells, giving rise to the reminicences of oscillations seen at collective signal at $200 \leq t \leq 400$ s. (d) The time-dependent Kuramoto order parameter $K$ remains low at all times, indicating a complete desynchronisation among the oscillations of the individual cells.

doi:10.1371/journal.pone.0043276.g003

Figure 4. Collective and individual dynamics of *S. carlsbergensis* at a cell density of 0.1%. At $t = 0$ an aliquot of 52 mM glucose was added to the starved and immobilised cells. (a) The time-series of the macroscopic, collective fluorescence signal is quiescent. At $t = 850$ s a transient episode of synchronised, collective oscillations sets in. After 1350 s, the collective signal becomes quiescent again. (b) The individual cells remain oscillatory during the entire duration of the experiment. Remarkably, the synchronisation episode sets in as the normalised amplitudes of the glycolytic oscillations already diminishes. (The amplitude of the oscillations of the cells corresponds to 45–95 photons/s.) The cells are numbered in a random order. (c) At the begin and end of the experiment, the individual cells oscillate at their own periods and phases. The synchronisation episode at $850 \leq t \leq 1350$ s is caused by a temporary entrainment of the oscillations of the individual cells. (d) The time-dependent Kuramoto order parameter reflects the dynamics in the cell population. It remains below ~0.3 as the cells oscillate in a incoherent manner, and increases to levels of $K \sim 0.7$ during the synchronisation episode.

doi:10.1371/journal.pone.0043276.g004
yeast cells, we repeated the studies using another yeast strain, namely \textit{S. cerevisiae}. Again, the oscillations at the level of individual cells were maintained, even at such low cell densities, where the collective dynamics was stationary. As in \textit{S. carlsbergensis}, the glycolytic oscillations of individual cells of \textit{S. cerevisiae} in low-density populations are desynchronised from each other (Fig. 5). Thus, we conclude that the persistence of oscillations at the cellular level at such low cell densities, where the collective behaviour is quiescent, is a general dynamic feature of yeasts.

The disappearance of collective glycolytic oscillations at low cell densities is due to a loss of dynamic coherence among the individual cells. Below the critical density $\rho_{\text{crit}} \approx 0.3\%$, the cells continue to display glycolytic oscillations, but these oscillations lose their synchrony in phase and frequency. This desynchronisation scenario is typical for a Kuramoto transition to incoherence (or desynchronisation) [35,37,38]. It differs significantly from the recently expressed view that the cessation of collective oscillations at the population level is due to a ‘dynamical quorum sensing’ phenomenon [33], where all cells stop oscillating immediately, once the cell density is lowered below the critical threshold.

The cessation of collective oscillations occurs due to the inability of the cells to synchronise, since the extracellular messenger molecule acetaldehyde no longer reaches the necessary extracellular concentration to ensure an effective cell-to-cell coupling (communication). Interestingly, the critical cell density, where the transition in collective dynamics occurs, coincides with the emergence of small spots devoid of cells in the probe (Fig. 5). This coincidence may rise the question, whether the cell-to-cell communication between yeast cells is indeed achieved via the extracellular (mean-field) concentration of the messenger molecule (acetaldehyde), or whether a direct contact between the cells is necessary for the synchronisation to take place.

An indication of which mechanism is effective can be obtained from experiments at low cell density, e.g. $\rho \approx 0.01\%$. The cells were sparsely distributed on the coverslip, most of them isolated from each other, while another couple of cells stuck together via membrane-membrane contact (see the field of view for $\rho = 0.01\%$, Fig. 5c). It is noteworthy, that each of the adherent cells showed oscillations which differed in oscillation period and phase from that of the cell adhering to it (Fig. 5c: the three pairs of adhering cells in the centre of figure). The absence of a common frequency of oscillations in adhering cells provides support for the concept that yeast cells may indeed be coupled via the extracellular concentration of a messenger molecule.

On the other hand, at very low cell densities, a small fraction of cells remained quiescent. The reasons for this behaviour are not yet known, however, it might be due either to the intrinsic dynamics of these cells, or due to a “non-local” coupling in such reaction-diffusion systems, which suppresses their oscillations [41]. Whether such a mechanism is effective in sparse yeast cell populations will be investigated in future.
Two measures have been introduced to quantify the degree of synchronisation among the glycolytic oscillations at the cellular level. While $\sigma_T$ quantifies the synchronisation of the frequencies of the individual cells, $K$ measures the coherence of their oscillation phases. Both measures, $\sigma_T$ as a measure for the widths of the distributions of oscillatory periods (Fig. 6) and the time-averaged order parameter $K$ (Fig. 7), independently show that the transition synchrony and desynchronisation of the individual cells of a yeast population takes place at a cell density $\rho_{crit} \sim 0.3\%$.

The value of the critical cell density $\rho_{crit} = 0.3\%$ lies much higher than the cell density below which the collective dynamics settle onto a quiescent behaviour ($\rho \sim 0.01\%$). This apparent discrepancy is due to the fact that $K$ and $\sigma_T$ very accurately define the onset of desynchronisation (at the phase transition between synchronisation and desynchronisation), while the transition to collective quiescent behaviour is due to a complete decoherence of the oscillations of the individual cells. In future, we wish to analyse the transition from decoherence to the onset of coherence by making use of recently introduced techniques of synchronisation analysis [9].

The Kuramoto parameter $K$ and its standard deviation $\sigma_K$ tend to slightly increase as the cell density approaches zero (Fig. 7), although the cells continued to show glycolytic NADH oscillations. This finding reflects the loss of accuracy of the statistical measure $K$ as the number of cells becomes very low, i.e., as the cell density $\rho \to 0$. The increases in $K$ and $\sigma_K$ reflect the occurrence of intermittent episodes where a pair of cells may transiently oscillate with a comparable frequency.

Conclusions

The present study provides an answer for the long-standing, open question, how individual yeast cells behave, when the cell density falls below a critical value and the macroscopic, collective oscillations of the population cease [32]. We found that, while the collective dynamics of the entire population changes from oscillatory to stationary, the individual cells in these populations remained oscillatory. Such dynamics was even observed at the very low cell density of $\rho = 0.001\%$, where the cells are isolated from each other. However, at very diluted cell populations the oscillations of the individual cells became desynchronised. This behaviour was observed in populations of both yeasts $S. carlsbergensis$ and $S. cerevisiae$, indicating that the described dynamic transition is a generic feature of yeast.

The loss of coherence in the global, collective dynamics occurs via a ‘Kuramoto transition’, where the oscillations of the individual cells lose their phase and frequency coherence. In populations of low densities even cells adhering to each other showed oscillations that differed in frequency and period, thus, no spatial clusters, where all cells oscillated with the same frequency, were observed. These new findings need to be taken into account in new modelling studies of the transition between synchronisation and desynchronisation of yeast cell populations, especially since more recent studies in stirred suspensions tended to favour the ‘dynamical quorum sensing’ mechanism, where all cells stop to oscillate as the global, collective oscillations vanish.

Supporting Information

Video S1 Synchronised oscillatory dynamics of a population of cells from $S. carlsbergensis$ at a cell density of 0.7%. The oscillatory behaviour of a dense cell population ($\rho = 0.7\%$) in a 3D representation. The $z$-axis codes for the fluorescence intensity which is detected at any $x,y$-position of the sample. The fluorescence intensity emitted by all cells oscillates, and these oscillations are well synchronised in phase and frequency.

Video S2 Desynchronised oscillatory dynamics of a population of cells from $S. carlsbergensis$ at a cell density...
of 0.01%. The oscillatory behaviour of a sparse cell population ($\rho = 0.01\%)$ in a 3D representation. The $z$-axis codes for the fluorescence intensity which is detected at any $x,y$-position of the sample. It can be seen that, while all individual cells show metabolic NADH oscillations, these oscillations are desynchronised in phase and frequency. Thus, each cell oscillates at its own pace.

(GIF)

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