Excitonic wave-packet evolution in a two-orbital Hubbard model chain: A real-time real-space study

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Motivated by experimental developments introducing the concept of spin-orbit separation, we study the real-space real-time evolution of an excitonic wave packet using a two-orbital Hubbard model in a chain. The exciton is created by exciting an electron from a lower-energy half-filled orbital to a higher-energy empty orbital. We carry out the real-time dynamics of the resulting excitonic wave packet using the time-dependent density matrix renormalization group. We find clear evidence of charge-spin and spin-orbit separation in real space, by tracking the time evolution of local observables. We show that the velocity of the orbiton can be tuned varying the interorbital interactions. We also present a comparative study of the dynamics of a hole in one-orbital and two-orbital Hubbard models. Moreover, we analyze the dynamics of an exciton with spin-flip excitation, where we observe fractionalized spinons induced by Hund’s interaction.

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Introduction. The dynamics of excitations in low-dimensional compounds has attracted considerable attention [1,2]. Experimentally observed excitations include holons, spinons, doublons, and excitons [3,4]. In particular, the study of excitons in multiband insulators unveiled interesting surprises [5,6]. Localized and delocalized charge-transfer excitons were observed experimentally in La$_2$CuO$_4$ and La$_2$NiO$_4$, respectively [7]. More recently, spin-orbit excitons were observed in Sr$_2$IrO$_4$ using resonant inelastic x-ray scattering (RIXS) [8]. The excitonic dynamic in Sr$_2$IrO$_4$ was described as analogous to the propagation of holes in a cuprate’s antiferromagnetic (AFM) background [9].

Due to reduced dimensionality and strong correlation effects, quasi-one-dimensional (quasi-1D) systems display exotic dynamical properties [10–12], including the fractionalization of low-energy excitations [1,3] into spin (spinons) and charge (holons) excitations propagating with different velocities [13–15]. The existence of spin-charge separation was shown experimentally early on in quasi-one-dimensional systems [16,17]. Interestingly, the fractionalization of electronic excitations is not limited to spin and charge; it can also include the orbital degree of freedom [18]. In fact, spin-orbital separation was observed experimentally in the transition metal compound Sr$_2$CuO$_3$ [19]. Using high-resolution RIXS experiments, spin-orbital separation was also observed in the ladder system CaCu$_2$O$_3$ [20].

Recently, the spin-orbit separation in Mott insulating systems was studied theoretically using the effective Kugel-Khomskii model [21]. In the limit of vanishing Hund’s coupling, the propagation of the orbiton in a ferro-orbital and antiferromagnetic chain was shown to map into a “single hole” moving in an AFM chain with its dynamics described by an effective $t$-$J$ model [21]. However, in transition metal compounds, the Hund’s interaction plays an important role, and depending on the material, it can be strong. Precisely for a strong Hund’s coupling, in the propagation of an orbiton, the interorbital ferromagnetic (FM) and AFM spin alignments (in the excited states of the superexchange process) are not equal, and the simple mapping between orbiton and $t$-$J$ hole dynamics is no longer valid [22,23]. More recently, using RIXS, the effect of Hund’s interaction on the orbiton propagation in a quasi-1D AFM compound Ca$_2$CuO$_3$ was studied [23]. It was observed that robust Hund’s interactions are required in the theoretical description to understand the experimental orbital spectrum [23].

In this Research Letter, we provide a study of spin-orbit separation in a real-time and real-space formalism by creating a finite momentum excitonic wave packet at time $t = 0$, using a one-dimensional chain with two orbitals at each site. This wave packet is created by exciting an electron from a half-filled orbital to an empty higher-energy orbital, as in experiments. Previous studies primarily focused on the spectral properties to study spin-orbit separation and for simplicity relied on Kugel-Khomskii models in the strong-coupling limit [21,22,24]. Here, we consider a more general multiorbital Hubbard Hamiltonian at intermediate coupling strengths, accounting also for charge fluctuations and with focus on the influence of the Hund’s coupling. To study the excitonic real-time dynamics, we use the time-dependent density-matrix renormalization group (t-DMRG) method [25,26]. We have observed that after creating the exciton, the hole (in the half-filled orbital) and the electron (in the empty orbital) always move together, while the spin wave packet in the half-filled orbital independently evolves from the charge wave packet. We also compare the dynamics of a hole in a one-orbital chain versus the dynamics of a hole in a two-orbital chain. Overall, at intermediate coupling and for robust values of the Hund’s interaction, we find clear evidence of spin-orbit...
The electronic interaction portion is canonical:

\[ H_{\text{int}} = U \sum_{j} n_{j\uparrow} n_{j\downarrow} + \left( U' - J_{H} \right) \sum_{j,j' < j} n_{j\sigma} n_{j'\sigma} \]

The first term is the on-site Hubbard repulsion between up and down electrons in the same orbital. The second term is the electronic repulsion between electrons at different orbitals.

The standard relation \( U' = U - 2J_{H} \) arises from the rotational invariance SU(2) symmetry of the Hamiltonian. The third term is the ferromagnetic Hund’s interaction between electrons occupying the active two orbitals \( \gamma = a, b \) of the same site. \( S_{j\gamma} \) is the total spin of orbital \( \gamma \) at site \( j \). The last term is the pair hopping between different orbitals, where \( P_{j\gamma} = c_{j\uparrow}^\dagger c_{j\downarrow}^\dagger \).

To obtain the ground state \( |\Psi_{0}\rangle \) of this model, we employed the static DMRG method. For our numerical calculations, we use a system size \( L = 36 \) with two orbitals at each site, and we kept \( m = 1200 \) states. The exciton Gaussian wave packet is created with spin up and a crystal momentum \( k_{b} \), by applying the operator

\[ \hat{h}_{1}(k_{0}) = A \sum_{j} e^{-\pi i j^2/2a^2} e^{-i k_{0} j} c_{j\uparrow}^\dagger c_{j\downarrow}^\dagger \]

to the ground state \( |\Psi_{0}\rangle \). This operator excites an electron from the half-filled orbital \( b \) to the empty orbital \( a \) [Fig. 1(b)], centered at site \( j_{0} = 18 \) and with width \( \alpha_{b} = 2.54 \). The number 2.54 implies that the size of the initial Gaussian is exactly six lattice spacings in half height, a size that we considered adequate for easy visualization. \( A \) is the normalization constant of the Gaussian wave packet. Due to the finite width \( \alpha_{b} = 1.2\pi \alpha_{b} \) of the Gaussian wave packet in momentum space, we fix the crystal momentum at \( k_{0} = -0.5\pi + 4\alpha_{b} \) (i.e., close to the highest occupied electronic level with width \( \alpha_{b} = 0.06 \)). Because we construct a wave packet with a net nonzero momentum \( |\Psi_{0}\rangle = k_{a}(\text{electron}) + k_{b}(\text{hole}) \) at time \( t = 0 \) that points in our case towards the left, the resulting time evolution will not be left-right symmetric.

We investigate numerically the time evolution of the one-exciton state \( |\Psi_{e}\rangle = \hat{h}_{1}(k_{0})|\Psi_{0}\rangle \) under the influence of \( H \), i.e., \( \langle \Psi(t) \rangle = e^{-i\hat{H}t}|\Psi_{e}\rangle \). To perform the time evolution, we have implemented the Krylov-space decomposition in the DMRG code [28,29]. For the DMRG calculations, at least 1200 states were kept during the time evolution.

To study the dynamics of the excitonic wave packet, we measure the following observables at each time step:

\[ \langle n_{ja}(t) \rangle = \langle \Psi(t) | n_{ja\uparrow} + n_{ja\downarrow} | \Psi(t) \rangle, \]

\[ \langle n_{jb}(t) \rangle = \langle \Psi(t) | n_{jb\uparrow} + n_{jb\downarrow} | \Psi(t) \rangle, \]

\[ \langle S_{ja}(t) \rangle = \langle \Psi(t) | (n_{ja\uparrow} - n_{ja\downarrow})/2 | \Psi(t) \rangle, \]

\[ \langle S_{jb}(t) \rangle = \langle \Psi(t) | (n_{jb\uparrow} - n_{jb\downarrow})/2 | \Psi(t) \rangle, \]

\[ \langle \tau_{z}(t) \rangle = \langle \Psi(t) | n_{ja} - n_{jb} | \Psi(t) \rangle, \]

where \( \langle n_{ja}(t) \rangle \) and \( \langle n_{jb}(t) \rangle \) are the orbital-resolved time-dependent charge densities of orbitals \( a \) and \( b \). \( \langle S_{ja}(t) \rangle \) and \( \langle S_{jb}(t) \rangle \) are the respective orbital-resolved \( z \) components of the time-dependent spin densities. \( \langle \tau_{z}(t) \rangle \) is the \( z \) component of the time-dependent orbital density. All these quantities are site dependent.
FIG. 2. Snapshots of the evolution of wave packets at different times: (a) charge density \(\langle n_{ja}(t)\rangle\), (b) spin density \(\langle S_{ja}^z(t)\rangle\), (c) charge density \(\langle n_{jb}(t)\rangle\), (d) spin density \(\langle S_{jb}^z(t)\rangle\), and (e) orbital density \(\langle \tau_j(t)\rangle\). At \(t = 0\), wave packets are at the center of the system, i.e., site \(j_b = 18\). (f) Positions of the peaks of the orbital (black circles) and spin (red squares) wave packets vs. \(t\). The peak positions are fitted with straight lines to extract the velocity of orbital and spin wave packets. These results were obtain at \(J_H/U = 0.25\) and \(U/W = 1.0\) using t-DMRG for a system with \(L = 36\) sites.

(a) Dynamics of an exciton in a two-orbital model. The Hamiltonian ground state, at overall quarter filling \((L = 36\) and total number of electrons \(N = 36\)) and parameters \(U/W = 1.0, J_H/U = 0.25\) [30], and \(\Delta_{zj} = 4.1\), results in a situation where orbital \(b\) is a half-filled Mott insulator with AFM-spin correlations, while orbital \(a\) remains empty. At time \(t = 0\), the process previously described leads to an exciton centered in the middle of the chain [see Fig. 1(b)], i.e., at site \(j_b = 18\). This results in a hole wave packet \(\langle n_{ja}(t)\rangle\) in orbital \(b\) [Fig. 2(a)] and an electron wave packet \(\langle n_{jb}(t)\rangle\) in orbital \(a\) [Fig. 2(a)]. The excitation of an electron from orbital \(b\) at \(t = 0\) also creates spin excitations \(\langle S_{ja}^z\rangle\) with up spins in orbital \(a\) [Fig. 2(b)] and down spins in orbital \(b\) \(\langle S_{jb}^z\rangle\) [Fig. 2(d)].

As shown in Figs. 2(a) and 2(b), with increasing time the charge wave packet \(\langle n_{ja}(t)\rangle\) and the spin wave packet \(\langle S_{ja}^z(t)\rangle\) at orbital \(a\) (the originally empty orbital) move with similar speeds toward the left from the central site \(j_b = 18\), indicating no spin-charge separation for orbital \(a\), as expected for an electron moving in an empty medium. On the other hand, in the half-filled orbital \(b\), the charge wave packet \(\langle n_{jb}(t)\rangle\) and spin wave packet \(\langle S_{jb}^z(t)\rangle\) move in opposite directions with time, providing clear evidence of spin-charge separation [see

FIG. 3. Orbital density \(\langle \tau_j(t)\rangle\) at time \(t = 5\) for three values of Hund’s interactions \(J_H/U\) and at fixed \(U/W = 1.0\). Inset: Orbiton and spinon speeds \(|v_t|\) and \(|v_s|\) are parametric with Hund’s interaction \(J_H/U\) at \(U/W = 1.0\). Figs. 2(c) and 2(d) [as expected in interacting one-orbital systems]. Interestingly, the charge wave packets \(\langle n_{ja}(t)\rangle\) and \(\langle n_{jb}(t)\rangle\) move together, as mirror images of each other [see Figs. 2(a) and 2(c)]. The bound state of an electron and hole pair minimizes the on-site interorbital interaction \(U'\) [31]. Intuitively, when the hole of orbital \(b\) and the electron in orbital \(a\) are in the same site, the strong interorbital repulsion energy \(U'\) is not active (as compared with the case where an electron in orbital \(a\) and an electron in orbital \(b\) are on the same site resulting in strong interorbital interaction \(U'\)). This results in the formation of an electron-hole bound pair exciton which moves as a single entity with increasing time \(t\) towards the left of site \(j_b = 18\) [32].

In the electron-hole pair exciton, the electron promoted from the half-filled orbital \(b\) to the unoccupied orbital \(a\) is also equivalent to creating an orbiton [22,33] because \(\langle n_{ja}(t)\rangle\) and \(\langle n_{jb}(t)\rangle\) move together as a bound state. Namely, when we use the expression “orbiton” it implies that a bound-state electron-hole pair exists. In Fig. 2(e), we show the orbiton dynamics via \(\langle \tau_j(t)\rangle\) evolving with time \(t\). The orbital wave packet \(\langle \tau_j(t)\rangle\) moves similarly to \(\langle n_{ja}(t)\rangle\) and \(\langle n_{jb}(t)\rangle\), towards the left from the central site \(j_b = 18\), while the spin wave packet \(\langle S_{ja}^z(t)\rangle\) moves toward the right. Thus our result can be reinterpreted as a signature of spin-orbit separation in real space with increasing time \(t\). To determine the velocities of the orbital and spin excitations, we monitored the positions of the peak values of \(\langle \tau_j(t)\rangle\) and \(\langle S_{ja}^z(t)\rangle\) versus time. Using simple linear fits to extract the orbiton \((v_t)\) and spinon \((v_s)\) velocities [Fig. 2(f)], we find that the orbital wave packet \((v_t = -0.91)\) has a speed only slightly faster than the spin wave packet \((v_s = 0.82)\), at \(J_H/U = 0.25\) and \(U/W = 1.0\).

Next, to study the role of the interorbital repulsion \(U'\) and Hund’s coupling \(J_H\) in the dynamics of the exciton wave packet, we calculate \(\langle \tau_j(t)\rangle\) and \(\langle S_{ja}^z(t)\rangle\) for different values of \(J_H/U\) (but only in the physical region \(0 < J_H/U < 1/3\), where \(U'\) is not smaller than \(J_H\) [30]). Figure 3 displays the orbital wave packet at time \(t = 5\) but for three different values
of $U/H$. We find that for the smaller coupling $J_H/U = 0.05$ the wave packet $\langle \tau_f(t) \rangle$ traveled only a very short distance from the central site $j_0 = 18$. However, increasing the Hund’s coupling to $J_H/U = 0.25$, still at time $t = 5$, $\langle \tau_f(t) \rangle$ traveled a larger distance (five lattice spacings) from the central site $j_0 = 18$. The inset shows the orbiton and spinon speeds $|v_1|$ and $|v_f|$, respectively, versus $J_H/U$. We find that the orbital velocity increases significantly with increasing $J_H/U$, which is in qualitative agreement with Refs. [22,23]. We believe this is because increasing $J_H/U$ reduces the interorbital interaction $U’$, which results in a less-tightly-bound electron-hole pair and thus the exciton becoming less heavy and being able to move at a faster rate $|v_f|$. On the other hand, at small $J_H/U$ the interorbital interaction $U’$ increases and results in heavier excitons, which naturally are more localized [7,31]. The larger value of orbiton velocity was observed in RIXS experiments because of the large Hund’s coupling in Ca$_2$CuO$_4$ [23]. The increase in orbiton velocity was explained in terms of the superexchange process [22,23], where the authors showed that the energy of the intermediate state during the movement of the orbiton depends on the Hund’s coupling $J_H$. For completeness, note that we find that the spin speed $|v_f|$ (inset of Fig. 3) does not change much with increasing $J_H/U$ and remains unaffected by the concomitant modifications in $U’$, which is intuitively reasonable.

(b) Comparison of dynamics of a single hole in one- and two-orbital Hubbard models. In Figs. 4(a) and 4(b), we show a comparison of the dynamics of a hole in the one-orbital Hubbard model (half-filled chain, $U/W = 1.0$) and in the two-orbital Hubbard model (quarter-filled chain, $U/W = 1.0$, $J_H/W = 1.0$, and $J_B/U = 0$) chain systems. At $t = 0$, a hole was created at the central site $j_0 = 18$, either by removing an electron at site $j_0 = 18$ for the one-orbital case or, for two orbitals, by removing an electron in orbital $a$ and exciting this electron to orbital $b$ at the same site, $j_0 = 18$. The results for the charge wave packets are remarkably different. While the charge wave packet in the one-orbital system moves quite fast and splits into left- and right-moving wave packets, the charge wave packet in the two-orbital system moves very slowly due to the formation of the strong bound state of electron (in orbital $a$) and hole (in orbital $b$). The heaviness of the bound-state electron-hole pair is natural because propagating to the next site involves two hoppings $t_a$ and $t_b$ and an intermediate state with energy proportional to $U$ (scaling as $t_a t_b / U$), while the bare hole in one orbital propagates easily with just a hopping $t_{hop}$. Interestingly, the spin wave packets in both systems move with a similar speed and towards the right from the central site $j_0 = 18$ [see Fig. 4(b)]. This is expected because after the separation of spin and charge wave packets in the two-orbital system (at quarter filling), the spin moves approximately guided by the scale $t_{hop}^2 / U$, the same scale that the spinon follows in the one-orbital half-filled system [14].

(c) Dynamics of a spin-flipped exciton in a two-orbital model. In the RIXS experiment, during the creation of orbital excitations, spin-flip processes are also allowed [22,23]. Figure 5 presents a comparison of orbiton dynamics with and without spin flip during the exciton generation, for different values of $J_B/U$. At $t = 0$, for the spin-flip process the exciton wave packet was created by the operator $A \sum_{j} e^{-i j \hbar \omega} e^{-i k_0 x} c_{j a}^\dagger c_{j b}$ acting on the ground-state wave function $|\Psi_0\rangle$. We found that the orbital velocity of $\langle \tau_f(t) \rangle$ when spin flip occurs is only slightly reduced compared with the previously described non-spin-flip case $\langle \tau_f(t) \rangle$ at $J_B/U = 0.25$ [see Fig. 5(a)]. The slower speed of the spin-flip orbiton compared with the non-spin-flip orbiton, for the multiorbital Hubbard Hamiltonian, is in contrast to the result expected from the superexchange picture [23], which predicts a faster speed of the spin-flip orbiton (the movement of the spin-flip orbiton is regulated by $t_a t_b / (U - 3 J_B)$, and that of the non-spin-flip orbiton is regulated by $t_a t_b / (U - 2 J_B)$) [34]. The slower speed of the spin-flip orbiton [Fig. 5(a)] is presumably due to an attractive interaction between spinon and orbiton in the presence of a large Hund’s coupling, as argued in Ref. [22], compared with the without-spin-flip case (where spinon and orbiton repel each other [22]). For a smaller $J_H/U = 0.05$, the results are almost identical, and the orbital wave packet moves very slowly in both cases [see Fig. 5(b)].
The spin-flip excitonic process leads to the creation of spin wave packets $\langle S_{ja}^z (t) \rangle_f$ and $\langle S_{jb}^z (t) \rangle_f$ in the spin-down state [Fig. 5(c)]. Interestingly, at large $J_H/U$ the spin-wave packet splits into two wave packets with time ($t \gtrsim 3$), traveling in opposite directions (starting at the central site $j_0 = 18$). This curious splitting of the spin wave packet $\langle S_{ja}^z (t) \rangle_f$ indicates the presence of two fractionalized spinons [35]. The left-moving wave packet $\langle S_{ja}^z (t) \rangle_f$ travels with speed similar to that of $\langle S_{jb}^z (t) \rangle_f$ of orbital $a$ and $\langle \tau_{jz} (t) \rangle_f$. This could be due to the strong Hund’s interaction between spin wave packets of orbitals $a$ and $b$, which favors parallel alignment (spin-down state) of spin wave packets $\langle S_{ja}^z (t) \rangle_f$ and $\langle S_{jb}^z (t) \rangle_f$. At large $J_H/U$, the creation of additional spinons was suggested in the spin-orbital spectrum [22]. The right-moving spin wave packet $\langle S_{ja}^z (t) \rangle_f$ moves with speed similar to that of $\langle S_{ja}^z (t) \rangle$ (without-spin-flip case) [Fig. 5(c)]. On the other hand, for smaller $J_H/U$, the spin wave packet $\langle S_{ja}^z (t) \rangle_f$ does not split into two parts. $\langle S_{ja}^z (t) \rangle_f$ (spin-flip case) and $\langle S_{ja}^z (t) \rangle$ (without spin flip) move with similar speeds [see Fig. 5(d)].

**Conclusions.** Using the Krylov-space t-DMRG method, we studied the real-time dynamics of an excitonic wave packet evolving via a two-orbital Hubbard model on a chain, at intermediate coupling $U/W$. We observed the real-space spin-orbit and spin-charge separation by monitoring the dynamics of spin, charge, and orbital wave packets. We find that the charge and spin wave packets of the higher-energy orbital $a$ move together, whereas the charge and spin wave packets of the lower-energy orbital $b$ move in opposite directions (Fig. 6). The electron in the higher-energy orbital and hole in the lower-energy orbital always move together. The interorbital interactions ($U'$ and $J_H$) play a crucial role in orbital dynamics. For example, the orbiton velocity increases significantly by increasing $J_H/U$, whereas the spinon velocity remains unchanged. Interestingly, we found that a hole in a one-orbital chain moves much faster than a hole in a two-orbital chain, because the hole in the lower-energy orbital forms a (heavy) bound pair with the electron in the higher-energy orbital. Moreover, we presented the dynamics of the spin-flipped exciton, where we found evidence of fractional spinons at large Hund’s coupling. In future work, our calculations can be extended in various directions that our group, and other groups, has experience with. For example, these calculations can be extended into chain multiorbital systems with spin block states [36,37], electronic models that realize the Hal-dane $S = 1$ chain and turn superconducting with doping [38], systems with spirals made of spin blocks [39], flux states [40], systems with spin-orbit coupling [41], ladder materials with orbital selective Mott phases [42], systems with intertwined orders [43], materials with orbital order [44], ruthenates [45], and generic $t$-$J$ models [46]. In all these different contexts, how wave packets will move is not obvious, and surprises may arise.

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