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What If Planet 9 Is a Primordial Black Hole?

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We highlight that the anomalous orbits of trans-Neptunian objects (TNOs) and an excess in microlensing events in the 5-year Optical Gravitational Lensing Experiment data set can be simultaneously explained by a new population of astrophysical bodies with mass several times that of the Earth ($M_\oplus$). We take these objects to be primordial black holes (PBHs) and point out the orbits of TNOs would be altered if one of these PBHs was captured by the Solar System, inline with the Planet 9 hypothesis. Capture of a free floating planet is a leading explanation for the origin of Planet 9, and we show that the probability of capturing a PBH instead is comparable. The observational constraints on a PBH in the outer Solar System significantly differ from the case of a new ninth planet. This scenario could be confirmed through annihilation signals from the dark matter microhalo around the PBH.

Introduction.—As of this year, two gravitational anomalies of similar mass but very different origins remain to be explained. First, there is a growing body of observational anomalies connected to the orbits of trans-Neptunian objects (TNOs) [1–3]. These observations have been taken as evidence of a new ninth planet in our Solar System, called Planet 9 (P9), with mass $M_9 \sim 5–15M_\oplus$ and orbiting around the Sun at a distance of 300–1000 AU [4]. Second, gravitational anomalies have also been recently observed by the Optical Gravitational Lensing Experiment (OGLE). OGLE reported an excess of six ultrashort microlensing events with crossing times of 0.1–0.3 days [5]. The lensing objects are located toward the galactic bulge, roughly 8 kpc away. These events correspond to lensing by objects with mass $M \sim 0.5M_\oplus \sim 20M_\oplus$ [6] and could be interpreted as an unexpected population of free floating planets (FFPs) or as primordial black holes (PBHs).

It is remarkable that these two anomalies correspond to a similar mass scale. Perhaps the most natural explanation is that they are caused by the existence of an unknown population of planets, i.e., the OGLE anomaly should be interpreted as due to FFPs denser than the local star population [7] and P9 might be one of those planets that have been captured by the Solar System. This would imply that our models for planet formation may need to be updated to account for this new population of FFPs, but the current program to hunt for P9 would go unchanged.

We focus on a more exciting possibility: if the OGLE events are due to a population of PBHs, then it is possible that the orbital anomalies of TNOs are also due to one of these PBHs that was captured by the Solar System. In this Letter, we argue that this scenario is not unreasonable and discuss the observable implications; we estimate the probability of capture of a PBH by the Solar System, highlight that the observational constraints differ significantly between planets and PBHs, and point out that the dark matter (DM) microhalo, which generically forms around such a PBH, can lead to its discovery.

Two anomalies.—While the structure of the Solar System to semimajor axis $a \sim 100$ AU is well explained, for $a > 250$ AU there are TNO populations whose orbits cannot be readily understood. Observations of TNOs, objects with $a > 30$ AU, and extreme TNOs (eTNOs) with $a > 250$ AU exhibit the following anomalies: (i) Unexpected clustering in eTNO orbits [2,3] (ii) The existence of high perihelia ($q \sim 70$ AU) TNOs, such as Sedna, collectively called Sednoids [1,2,8] (iii) TNOs moving roughly perpendicularly to the planetary plane (with inclination $i \gtrsim 50^\circ$) [9–11] An excellent review of TNO anomalies is given in [4].

Simulations and analytic arguments indicate that these observations are at odds with the predicted dynamics assuming only the known giant planets. For instance, any coincidence of initial orbits of eTNOs will disperse under evolution (on a time scale of a 10–100 million years [12]), and Solar System simulations imply inclinations that are typically bounded by $i \lesssim 40^\circ$ [13,14].

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(iii) P9 has formed outside of the Solar System and has been up-scattered into its current orbit; or
will discuss later.

enhanced, leading to potentially detectable signals as we

transition around the electroweak scale are expected to

spectrum. An intriguing coincidence is that PBHs formed
domination, due to an increase in the primordial power

fractions are correlated with larger masses corresponding to

smaller

masses.

PBHs arise from over

densities in the early Universe[15,16] and as a result can be

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fPBH.

While an M⊙ object is too light to be an astrophysical black hole formed by stellar collapse, PBHs arise from over
densities in the early Universe[15,16] and as a result can be substantially lighter than M⊙. Formation of PBHs inferred
from OGLE has been discussed in[17–19]. We note that PBHs arise from O(1) density fluctuations during radiation
domination, due to an increase in the primordial power spectrum. An intriguing coincidence is that PBHs formed
during radiation domination via a strong first order phase transition around the electroweak scale are expected to
have mass of the same order as P9 with MBH ∼ M⊙(125 GeV/T)² [20].

Since [6] prefers fPBH < 1, we assume DM particles account for the remaining fraction: fDM = 1 − fPBH ≈ 1. In
that case, a PBH will accrete DM and form a microhalo [21–25]. Since the DM densities in these microhalos are
typically very high, DM annihilations can be significantly enhanced, leading to potentially detectable signals as we
will discuss later.

Capture probability.—There are three alternative hypotheses for the origin of P9: (i) P9 formed on its
current orbit (in situ); (ii) P9 formed in the inner Solar System and has been up-scattered into its current orbit; or
(iii) P9 has formed outside of the Solar System and has been captured. While all three scenarios are unlikely, they
are still favorable compared to the chance alignment of TNOs [3]. In case of the in situ formation, at a ∼ 500 AU,
there is typically insufficient time and material to build an Earth-mass planet [26–28]. The prospect of a planet
forming near Uranus and Neptune before being scattered to its present orbit is low since in order to fall into a stable
orbit the planet would need to be appropriately influenced by a passing star (or another mechanism) [4,29]. The
probability of capturing an FFP is estimated to be similarly improbable, with estimates differing by orders of magni-
tude depending on assumptions [29–31]. We will argue that while there is a low probability of capturing an Earth-mass
PBH, it is no more improbable than capturing an FFP of similar mass. The Solar System capture rate can be
expressed as follows:

Γ = (σνt) = ∫ n₀F(v + v₀, r) dσ dv, (2)

where F(v) and n₀ are the velocity distribution and ambient
density of the objects to be captured, dσ/dv is the differen-
tial capture cross section, and v₀, r is the velocity of the
Sun with respect to the rest frame r of the objects to be
captured.

The differential cross section (identical for PBHs and
free floaters) is significantly suppressed for relative veloc-
ities larger than 0.25 km/s [32], which is much smaller
than other velocities in the calculation. As a result, the
velocity dispersions in the integrand can be approximated
by the zero-order value F(v₀). This allows us to cancel the
common factor of dσ/dv in the ratio of PBH to FFP capture
rate, which is then well approximated by

ΓBH /ΓFFP ≈ fPBH F PBH(v₀, PBH) / F FFP(v₀, FFP). (3)

We assume that the PBH velocity distribution is the same as
the DM velocity distribution given by the standard halo model [33], with v₀, DM = 220 km/s and velocity
dispersion σPBH = v₀/√2. The local density of PBHs is related to the local DM density (ρDM = 0.4 GeV/cm³) and
the fact that PBHs comprise a fraction fPBH of this local
density,

nBH = fPBH (ρDM /M BH) ∼ 35 pc⁻³ (fBH/0.05) (5M⊙/M BH) .

As for the FFPs, there are two possibilities: while the Solar
System could capture a planet when inside a star-forming
region, for which the FFP density may be as high as
200 pc⁻³ [32], such stellar nurseries are highly disruptive
environments. Hence, a planet captured in this manner is
quite likely subsequently stripped by interactions with
nearby stars [27–29]. Instead, we consider capture in the
field, away from star-forming regions. In the field, the FFP

TABLE I. This table contains some benchmark P9 scenarios
from [4] stating central values. Here a is the central major axis, e
is the ellipticity, and i is the inclination. Deviations of O(10%) in
parameters provide comparable fits.

| Benchmark | a (AU) | e   | i (deg) |
|-----------|--------|-----|--------|
| 5M⊙      | 450    | 0.2 | 20     |
| 10M⊙     | 700    | 0.4 | 15     |
density (which we take to be similar to the local star density) is much lower: \( n_{\text{FFP}} \sim 0.2 \text{ pc}^{-3} \). However, the available time for capture is much longer and the survival probability of a captured object is effectively unity. We assume the FFP velocity dispersion is inherited from the stars in the thin disk: \( \sigma = 40 \text{ km/s} \). Remarkably, with these parameters, we arrive at

\[
\frac{\Gamma_{\text{BH}}}{\Gamma_{\text{FFP}}} \sim 1 \times \left( \frac{0.2 \text{ pc}^{-3}}{n_{\text{FFP}}} \right) \left( \frac{40 \text{ km/s}}{\sigma_{\text{FFP}}} \right)^3 \left( \frac{f_{\text{BH}}}{0.05} \right) \left( \frac{5M_\odot}{M_{\text{BH}}} \right). 
\]

We find that the rates are comparable and thus conclude that the probability that an FFP is gravitationally captured by the Solar System in ambient space is roughly comparable to capturing a 5\( M_\odot \) PBH with \( f_{\text{PBH}} \sim 0.05 \). Therefore, if one is willing to entertain the possibility that the TNO orbits indicate a captured planet, it is plausible that the gravitational source in the outer Solar System could instead be a PBH (once we establish evidence for such a PBH population).

The conclusions above assume the OGLE excess is due to PBHS. However, the OGLE events might alternatively be sourced by FFPs provided the number of Earth-mass FFPs is an order of magnitude above the estimates of \cite{34}. Although, as highlighted in \cite{6}, in building the empirical case for Earth-mass PBHS, there is an apparent gap between Jupiter-mass lensing events and the Earth-mass objects \cite{5}, whereas one would expect a continuum. Since it is challenging to explain why Earth-mass planets might be preferentially ejected from their native systems, this opens the possibility for the Earth-mass microlensing events to come from an alternate source, namely PBHS.

We note that considering the FFP explanation for OGLE, and assuming that \( \sigma \) is unaltered, this would imply an FFP capture rate which is an order of magnitude higher than the \( \Gamma_{\text{FFP}} \) calculated assuming \cite{34}. In this case, there is no motivated reason to introduce PBHS and no reason to alter the experimental search program for Planet 9; thus, we find the more interesting proposition is to consider the case in which the OGLE events are due to a PBH. Notably, in this case, there are two Planet 9 capture hypotheses corresponding to a planet or a PBH, but as we have argued above the chances of either scenario are comparable. Indeed, the main point is that \( \Gamma_{\text{PBH}} \ll \Gamma_{\text{FFP}} \) and thus the proposal that Planet 9 may be a PBH cannot be immediately discarded.

Finally, we note that gravitational capture normally occurs due to multibody interactions or drag through the local environment which leads to energy dissipation. Interestingly, the capture of an object with an extended halo presents a new mechanism for dissipation since DM particles will be shed during the encounter. This possibly improves the chance of capture, but understanding the complicated dynamics would require a dedicated study.

Dark matter.—OGLE \cite{6} indicates \( f_{\text{PBH}} \ll 1 \). If the rest is taken up by the DM component, PBHS accrete dense DM microhalos. This is fortunate since DM annihilation provides a potential detection route and in the absence of DM it would be likely impossible to detect an \( M_\odot \) PBH in the Solar System. To describe the DM profile around the PBH, one needs to consider its initial configuration and subsequent evolution. We will discuss several characteristic scales that control the properties of the halo: the influence radius \( r_{\text{in}} \), truncation distances \( r_t \) due to stripping, and (if applicable) the radius at which DM annihilations shape the halo \( r_{\text{max}} \).

The radius of influence \( r_{\text{in}} \) corresponds to the region in which the PBH dominates the local gravitational potential (assuming the uniform background density approximation) and effectively appears as an \( O(1) \) density perturbation. As a result, \( r_{\text{in}} \) corresponds to the radius that contains DM mass equal to the PBH mass,

\[
M_{\text{BH}} = \frac{4\pi}{3} \rho(t) r_{\text{in}}^3(t).
\]

The density profile of a halo is relatively simple if the DM kinetic energy can be neglected relative to its potential energy (when the kinetic energy cannot be neglected, an inner density plateau occurs associated to the DM free streaming scale \cite{23,24}). This is typically the case for \( M_{\text{PBH}} \gtrsim M_\odot \) for DM with mass \( m \gtrsim 100 \text{ GeV} \), in which case the DM profile is of the form \cite{35} (this profile is typical of self-similar secondary infall)

\[
\rho(r) = \frac{\rho_{\text{eq}}}{2} \left( \frac{r_{\text{eq}}}{r} \right)^{9/4},
\]

in terms of \( r_{\text{eq}} = r_{\text{in}}(t_{\text{eq}}) \sim 220 \text{ AU} \times (M_{\text{BH}}/5 M_\odot)^{1/3} \) the radius of influence at matter-radiation equality, and \( \rho_{\text{eq}} \equiv \rho(t_{\text{eq}}) \approx 2.1 \times 10^{-19} \text{ g/cm}^3 \) the density of Universe at matter-radiation equality.

If the DM can annihilate, the inner DM density may be depleted implying a cross-section-dependent region of constant density \( \rho_{\text{max}} = m/(\sigma v) \tau \) within a radius \( r_{\text{max}} = r_{\text{eq}}[(\sigma v) \tau \rho_{\text{eq}}/(2m)]^{1/4} \), where \( (\sigma v) \) is the thermally averaged annihilation cross section and \( \tau \) is the age of the Universe \cite{23}. For the DM models we consider in this work, \( r_{\text{max}} \) is smaller than the Schwarzschild radius \( r_{\text{BH}} \) and density plateau does not exist. This happens for

\[
(\sigma v) < 1.4 \times 10^{-54} \text{ cm}^3/\text{s} \left( \frac{m}{100 \text{ GeV}} \right) \left( \frac{M_{\text{BH}}}{5 M_\odot} \right)^{3/2}.
\]

Furthermore, the DM halo will not have indefinite extent. It will be truncated due to stripping by the Milky Way (MW), by encounters with passing stars, and by the Sun (for a PBH bound to the Solar System). Since we consider a captured PBH, it should have a similar (galactic) orbit to the Sun; thus, it will not make any especially close approaches to the center of the Galaxy. This implies very little
truncation due to the Galaxy; for an initial halo of $M_{\text{initial}} \sim 10^6 M_{\odot}$, then $r_{\text{t, MW}} \sim 10$ kpc.

Tidal disruptions from meeting individual stars can be more significant. The tidal radius $r_\star$ is dominated by the closest approach to a star. Since the PBH travels near the peculiar velocity of the Sun (10 km/s) with respect to the local rest, it has traveled around 100 kpc over $10^{10}$ years and has passed $\mathcal{O}(10^3)$ stars. The typical spacing of stars is 1 pc, and so the distance of closest approach is $r_\star \sim \sqrt{10^{-5}} \text{pc} = 650 \text{ AU}$. The tidal stripping radius due to star encounters is then

$$r_{\star, \text{t}} \sim r_\star \left( \frac{M_{\text{initial}}}{2 M_{\odot}} \right)^{\frac{1}{3}} \sim 34 \text{ AU} \left( \frac{r_\star}{650 \text{ AU}} \right) \left( \frac{M_{\text{initial}}}{10^6 M_{\odot}} \right)^{\frac{1}{3}}.$$  

Interestingly, $r_\star$ is of the same order as the inferred P9 semimajor axis. The halo mass, obtained by integrating to $r_{\star, \text{t}} \sim 34$ AU, for the profile in Eq. (5) reveals that the total halo mass is typically $\mathcal{O}(50\%)$ of a PBH of mass $5 M_{\odot} \lesssim M_{\text{BH}} \lesssim 10^6 M_{\odot}$, and so any further tidal stripping is controlled by the PBH mass. Once the PBH settles into an orbit around the Sun, the tidal radius cuts off the DM halo at

$$r_{\odot, \text{t}} \sim r_p \left( \frac{M_{\text{BH}}}{2 M_{\odot}} \right)^{\frac{1}{3}} \sim 8 \text{ AU} \left( \frac{r_p}{400 \text{ AU}} \right) \left( \frac{M_{\text{BH}}}{5 M_{\odot}} \right)^{\frac{1}{3}},$$

which contains DM mass of the order $\mathcal{O}(15\%)$ of the mass of the PBH.

Annihilation signals.—On its own, a PBH of mass $5 M_{\odot}$ has a Hawking temperature of 0.004 K, making it colder than the cosmic microwave background, and since its radius is $r_{\text{BH}} \sim 5$ cm, the power radiated by the PBH alone is minuscule. However, the DM halo around this PBH can, if annihilating, provide a powerful signal. Annihilations in the PBH halo at the position of P9 would make for a potential FERMI-LAT source. Moreover, the whole PBH population contributes to gamma ray diffuse emissions [21]. Indeed, for a non-negligible $f_{\text{PBH}}$ and DM with a thermal cross section $\langle \sigma v \rangle_0 \sim 3 \times 10^{-26}$ cm$^3$/s [i.e., classic weakly interacting massive particle (WIMP) DM], the other PBHs surrounded by DM give a diffuse gamma ray flux that is strongly excluded [24,25].

In what follows, we take a DM model that generates observable signals, but is not yet excluded, and consider a “freeze-in” DM candidate [36]. In freeze-in, the DM abundance is initially negligible and is subsequently generated by highly suppressed interactions between the standard model and the DM, controlled by a tiny coupling $\lambda \ll 1$. This leads to a relic density $\Omega_{\text{DM}} \propto m Y_{\text{FI}} \propto \lambda^2$, where $Y_{\text{FI}} = n_{\text{DM}} / s$ is the comoving DM number density.

For a specific model, we consider a DM particle $\chi$ with mass $m$ coupled to a mediator state $\phi$ with mass $M_\phi$ via a Lagrangian term $g \chi \chi \phi$, and in addition, we couple $\phi$ to some standard model operator with coupling $\lambda$. The DM relic density generated by freeze-in is parametrically

$$\Omega_{\text{DM}} \simeq 0.2 \left( \frac{m}{100 \text{ GeV}} \right) \left( \frac{\lambda}{6 \times 10^{-12}} \right)^2 \left( \frac{10 \text{ TeV}}{M_\phi} \right). \quad (7)$$

We assume an annihilation cross section to standard model particles of the form (see the Supplemental Material [37])

$$\langle \sigma v \rangle \simeq \frac{g^2 g^2 m^2}{\pi M_\phi^4}, \quad (8)$$

with the characteristic values in Eq. (7). This implies a characteristic cross section of order

$$\langle \sigma v \rangle_{\text{ch}} \simeq 1.3 \times 10^{-66} \text{ cm}^3/\text{s} \times \left( \frac{g}{10^{-2}} \right)^2. \quad (9)$$

For fixed $\lambda$, decreasing $g$ reduces the annihilation cross section while maintaining the DM abundance. More model details appear in the Supplemental Material [37] and related literature; see, e.g., [38–46]. The coupling $g$ is mostly unconstrained, and for smaller $g$ the detection prospects become worse. However, there is a modest range of coupling $g$ values (allowing $m$, $M_\phi$, and $\lambda$ to vary) which evade current exclusion bounds, while allowing for observable signals in future experiments. Moreover, one might reasonably expect for couplings to fall in this modest range, in particular since standard model gauge couplings and second and third generation Yukawa couplings have similar magnitudes. We stress, however, that we present freeze-in as an example of a potentially discoverable scenario that is not currently ruled out.

Point source limits: The flux for this freeze-in scenario can be found from the DM annihilation rate

$$\Gamma = 4 \pi \int r^2 dr \left( \frac{\rho(r)}{m} \right)^2 \langle \sigma v \rangle. \quad (10)$$

We take $\langle \sigma v \rangle \simeq \langle \sigma v \rangle_{\text{ch}}$, then $r_{\text{max}} < r_{\text{BH}}$ from Eq. (6) and thus the profile of Eq. (5) is appropriate. Cutting off the integral at the tidal stripping radius $r_{\odot, \text{t}}$, we obtain

$$\Gamma = \sqrt{\frac{3 \rho_{\text{eq}} \langle \sigma v \rangle}{8 \pi G^3 m^3}} = 10^{20} \text{ s}^{-1} \left( \frac{\langle \sigma v \rangle}{(\langle \sigma v \rangle_{\text{ch}})(100 \text{ GeV})^2} \right). \quad (11)$$

Note that the above result is independent of the PBH mass (this is not the case for $r_{\text{max}} > r_{\text{BH}}$). Given the annihilation rate, the flux $\Phi_\gamma$ and the energy flux $\Phi_E$ of photons for an observer on Earth are then

$$\Phi_\gamma = \frac{k_1 \Gamma}{4 \pi r_9^2} \quad \text{and} \quad \Phi_E = \frac{k_2 \Gamma m}{4 \pi r_9^2},$$

where $k_1$ is the average number of photons per DM annihilation within the observable band of the experiment,
while $\kappa_2$ is the fraction of energy of the DM annihilation converted into photons within the observable energy band. Both $\kappa_1$ and $\kappa_2$ are dependent on the mass and branching annihilation channel of the DM candidate and can be determined, e.g., from [47]. To obtain characteristic bounds, we set $\kappa_1 \sim 10$ and $\kappa_2 \sim 1$.

The smallest detectable photon flux in the 8-year FERMI-LAT source catalog [48] was J2143.0-5501 with $\Phi_\gamma = 8.8 \times 10^{-12}$ photons/cm$^2$/s in the band 100 MeV to 100 GeV, while the smallest energy flux in the same band was $\Phi_E = 5.96 \times 10^{-13}$ erg/cm$^2$/s due to 4FGL J1014.6+6126. Using these fluxes as upper bounds, we calculate the maximum DM annihilation cross section allowed by the photon flux limit. Taking the rate of

$$\langle \sigma v \rangle < 5.1 \times 10^{-56} \text{ cm}^3/\text{s} \left( \frac{m}{100 \text{ GeV}} \right)^2 (\gamma \text{ flux}).$$

The energy flux bound implies a comparable limit

$$\langle \sigma v \rangle < 2.2 \times 10^{-55} \text{ cm}^3/\text{s} \left( \frac{m}{100 \text{ GeV}} \right) (E \text{ flux}).$$

That the two approaches give similar bounds is a coincidence and for different mass DM, these bounds will differ. Moreover, for more massive DM candidates, these constraints weaken as the photons from annihilations become too energetic and different instruments, such as CTA [49], will play an important role.

We note that during the 8 years of data taking the source would have moved by several degrees, making source identification much harder. However, the DM annihilation signals may be easier to spot because the space-time correlation in the signal would enhance the sensitivity of the search. As a result, it is necessary to run a dedicated study in order to determine if there are any candidates that match the P9 trajectory in the FERMI-LAT data set, which we will return to in future work [50].

Diffuse photons limit: In addition to looking for the P9 PBH, there is also an observational bound from the full population of PBHs; this has previously been explored in [21–25] for thermal cross section WIMP DM.

Following [24,25], we bound the diffuse gamma ray flux due to PBH $\Phi_\gamma$ by translating the limits on decaying DM of mass $m$ and decay rate $\Gamma_{DM}$ with the identification

$$\frac{d\Phi_\gamma}{dE} \propto \frac{f(1-f^2)\Gamma}{M_{BH}} \left( \frac{\Gamma_{DM}}{m} \right).$$

For more details, please see the Supplemental Material [37].

For DM with mass $10 \text{ GeV} \lesssim m \lesssim 10^6 \text{ GeV}$, the observational limit is

$$\Gamma_{DM} \lesssim 10^{-28} \text{ s}^{-1},$$

assuming 100% decays to $\bar{b}b$, varying by only $O(1)$ over the mass range [51]. Requiring that the differential flux due to $\Gamma$ is less than the above limit for $f = 0.05$ implies a bound on the rate of

$$\Gamma \lesssim 3.7 \times 10^{23} \text{ s}^{-1} \left( \frac{M_{BH}}{5M_\odot} \right) \left( \frac{100 \text{ GeV}}{m} \right).$$

Comparing with the rate in Eq. (11) with the characteristic cross section of $\langle \sigma v \rangle_{ch}$, it is seen that the diffuse bound is readily satisfied in the DM models we consider.

Exotica.—Before closing, we note that alternative “exotic” compact astrophysical bodies may explain these observations such as DM microhalos (without PBH), e.g., [52–56], boson stars [57], or DM stars [58,59]. OGLE cannot distinguish between PBH, exotic stars, and planets; however, DM microhalos are unlikely to produce OGLE’s lensing events unless their concentration reaches values orders of magnitude above the $\Lambda$CDM expectations [60]. Another possibility is a sizeable DM halo could be shredded during the capture leading a toroidal DM mass distribution around the Sun at $\sim 500 \text{ AU}$ with total mass $\sim 10M_\odot$; this realizes the secular approximation (phase space averaged) for a compact object and is similar to the proposed toroidal baryonic distribution of [61]. Notably, each of these scenarios implies different experimental signatures, distinct from those of a rocky or gas planet.

Conclusion.—This Letter highlights that anomalous orbits of TNOs and OGLE’s short microlensing events could have the same origin and explores the intriguing scenario that they both arise due to a population of $5M_\odot$ PBHs. While the principal search strategies for a planet is to employ optical [62,63] and infrared/microwave surveys [64], the signals could be very different for a PBH (or another exotic object).

Thus, the PBH hypothesis expands the required experimental program to search for the body responsible for TNO shepherding and motivates dedicated searches for moving sources in x rays, gamma rays, and other high energy cosmic rays. Conversely, if conventional searches fail to find Planet 9 and the evidence for TNO anomalies continues to grow, the PBH P9 hypothesis will become a compelling explanation.

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