VERY HIGH ENERGY \( \gamma \)-RAY AFTERGLOW EMISSION OF NEARBY GAMMA-RAY BURSTS

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ABSTRACT

The synchrotron self-Compton (SSC) emission from gamma-ray burst (GRB) forward shock can extend to the very high energy (VHE; \( E_\gamma \gt \) 100 GeV) range. Such high energy photons are rare and are attenuated by the cosmic infrared background before reaching us. In this work, we discuss the prospect to detect these VHE photons using the current ground-based Cherenkov detectors. Our calculated results are consistent with the upper limits obtained with several Cherenkov detectors for GRB 030329, GRB 050509B, and GRB 060505 during the afterglow phase. For five bursts in our nearby GRB sample (except for GRB 030329), current ground-based Cherenkov detectors would not be expected to detect the modeled VHE signal. Only for those very bright and nearby bursts like GRB 030329, detection of VHE photons is possible under favorable observing conditions and a delayed observation time of \( \lesssim 10 \) hr.

Key words: gamma rays: bursts – ISM: jets and outflows – radiation mechanisms: non-thermal

1. INTRODUCTION

On 1997 February 28, the first X-ray afterglow of a gamma-ray burst (GRB) was detected, leading to the identification of its progenitor at cosmological distances (Costa et al. 1997). In a few days, the afterglow faded away with time as a power law. This behavior is satisfactorily explained in the spherical (isotropic) fireball model involving relativistic ejecta decelerated by circumburst medium (Mészáros & Rees 1997). The introduction of collimated jets relaxes the energy requirement of GRBs by a factor of several hundred, as well as explains the steeper temporal decay of afterglows (Rhoads 1999; Sari et al. 1999).

GRBs are extragalactic sources of GeV and probably higher energy photons. Evidence of a distinct high-energy component has been accumulated by EGRET on board the Compton Gamma-Ray Observatory: (1) Hurley et al. (1994) reported the detection of long-duration MeV–GeV emission of GRB 940217 lasting up to 1.5 hr after the keV burst, including an \( \sim 18 \) GeV photon. This burst is the longest and the most energetic among those GRBs with detected high-energy emission so far; (2) González et al. (2003) revealed a high-energy component of GRB 941017 temporally and spatially different from the low-energy component.

In the fireball model, synchrotron emission of shock-accelerated electrons is commonly thought to produce prompt \( \gamma \)-ray emission as well as afterglow emission at lower energies (e.g., Sari et al. 1998). It is natural to expect that these photons are inverse-Compton up-scattered by electrons, giving rise to a higher energy component peaking at sub-GeV to TeV energies (Wei & Lu 1998; Sari & Esin 2001). When electrons scatter the self-emitting synchrotron photons, synchrotron self-Compton (SSC) emission is resulted. In the external shock scenario, the temporal profile of the SSC emission from forward shock electrons is similar to that of the low energy afterglow emission and no significant time lag is expected.

The Swift satellite, thanks to its rapid response time and accurate localization, has started a new era of research on GRBs. Different modifications to the standard afterglow model are put forward to explain the peculiar behaviors exhibited in the X-ray light curves, in particular the shallow declining phase (Zhang et al. 2006; Nousek et al. 2006). Recently, the SSC emission of the modified forward shock has been extensively discussed in the literature (Wei & Fan 2007; Gou & Mészáros 2007; Fan et al. 2008; Galli & Piro 2007; Yu et al. 2007) and applied to the case of GRB 940217 (Wei & Fan 2007).

The AGILE (Astro-rivelatore Gamma a Immagini L’Eggero) satellite, launched on 2007 April 23, is dedicated to high-energy \( \gamma \)-ray astronomy. The Fermi Gamma-ray Space Telescope (FGST) was launched on 2008 June 11. The Large Area Telescope (LAT) on board covers the energy range from 20 MeV to 300 GeV and its effective area is about five times larger than that of EGRET at GeV energies. The first GRB observations with LAT have resulted in detection of photons with energies larger than \( \sim 1 \) GeV from several GRBs (Omodei 2008; Tajima et al. 2008). Dermer et al. (2000), Zhang & Mészáros (2001b), and Wang et al. (2001) predicted promising and detectable SSC emission from the forward shock with FGST out to \( z \approx 1 \).

Most of the discussions in the literature have focused on the afterglow emission from tens of MeV to GeV. LAT can also detect very high energy (VHE; \( \gt \) 100 GeV) afterglow emission. However, with a small effective area \( \sim 10^4 \) cm\(^2\), it is very hard to have a significant detection at such high energy. Imaging atmospheric Cherenkov telescopes such as H.E.S.S.\(^6\), MAGIC,\(^7\) and VERITAS\(^8\) may serve better at energies above \( \sim 100 \) GeV because of their much larger effective area (\( \sim 10^5–10^7 \) cm\(^2\)) and a high rejection rate of hadronic background. The effective collecting area of Cherenkov telescopes increases with energy (Aharonian et al. 2006b). Some of these large area Cherenkov detectors have been used to set constraints on the possible VHE afterglow component of GRBs (Albert et al. 2007; Horan et al. 2007; Aharonian et al. 2009). It is thus desirable to see whether these results are consistent with the predictions of the fireball model. Our aim of this paper is also to investigate the prospect of

\(^6\) http://www.mpi-hd.mpg.de/hfm/H.E.S.S./H.E.S.S.html
\(^7\) http://wwwmagic.mppmu.mpg.de/
\(^8\) http://veritas.sao.arizona.edu/
significant detections in the future. To have a reliable estimate of the afterglow emission at energies above 100 GeV, one needs to calculate the forward shock emission (both synchrotron and SSC emission of the shocked electrons) carefully. The attenuation of VHE photons by the cosmic infrared background is also taken into account. Since the attenuation effect for photons with an energy > 100 GeV is more severe for high-redshift GRBs, we limit our GRB sample to nearby events.

This paper is organized as follows: in Section 2, we describe the GRB afterglow model, introduce the code that is used in the afterglow modeling and the calculation of the SSC emission from GRB forward shock. In Section 3, we present the expected results of the SSC model using reasonable parameter values for GRBs. In Section 4, we describe the GRB sample which includes six nearby GRBs with sufficient multiwavelength afterglow data and predict their corrected energy flux after the attenuation by the cosmic background during the afterglow phase, which is then compared with the available observational data. We summarize our results and discuss their implications in Section 5. We conclude in Section 6.

2. AFTERGLOW MODELING

2.1. GRB Afterglow Model

While synchrotron emission is widely considered to be responsible for the radio, optical, and X-ray afterglows (e.g., Sari et al. 1998), inverse Compton scattering of forward shock photons is considered in detail by Wei & Lu (1998, 2000) and Sari & Esin (2001). Inverse Compton scattering may considerably change the temporal and spectral behavior of GRB afterglows, and its cooling effect on electrons accelerated in external shocks will contribute to the photon spectra at sub-GeV to TeV energy range (Mészáros & Rees 1994; Dermer et al. 2000; Zhang & Mészáros 2001b; Wang et al. 2001).

In the afterglow model, both synchrotron emission and inverse Compton emission are taken into account. It is assumed that: (1) the external medium is homogeneous with a density $n$ or a wind profile $n \propto R^{-2}$; (2) the relativistic jet is uniform, i.e., energy per solid angle is independent of direction within the jet; (3) the shock parameters ($\epsilon_e$ and $\epsilon_B$, fractions of the shock energy given to the electrons and the magnetic field, respectively) are constant; (4) the energy distribution of electrons accelerated in shocks follows $dN_e/dE \propto E^{-p}$; (5) the typical achromatic flattening in the afterglow light curve is due to energy injection in the form $E_k \propto t^{1-q}$ (Cohen & Piran 1999; Zhang & Mészáros 2001a) or $E_k \propto [1 + (t/T)^2]^{-1}$ with $T$ being the initial spindown time scale (Dai & Lu 1998).

The parameters involved in this afterglow model include: $E_0$ (the initial isotropic outflow energy), $\theta_0$ (the initial half-angle of the jet), $n$ (the density of the homogeneous external medium) or $A$ (the wind parameter), $p$ (the power-law index of energy distribution of shock-accelerated electrons), $\epsilon_e$, and $\epsilon_B$ (shock parameters). In the case where energy injection is necessary, three additional parameters—$L_{ej}$ (the injected luminosity in the rest frame), the timescale of energy injection, and $q$—are included.

2.2. A Brief Description of the SSC Model

The code used in our afterglow modeling and the prediction of the SSC emission is that developed by Fan et al. (2008), who carry out numerical calculations of synchrotron and SSC emission of the external forward shock in the afterglow phase. The reverse shock emission, predicted in the fireball model but not detected in most events (Roming et al. 2006; Rykoff et al. 2009), is not taken into account.

The key treatments (see Section 3 of Fan et al. 2008 for details) are as follows. (1) The dynamical evolution of the outflow is followed using the formulae in Huang et al. (2000), which describes the hydrodynamics in both relativistic and non-relativistic phases. (2) The arbitrary assumption that the distribution of shocked electrons is always in a quasi-stationary state is considered to be unsatisfactory and the energy distribution of electrons is calculated by solving the continuity equation with the power-law source function $Q = K \gamma^{-p}$, normalized by a local injection rate (Moderski et al. 2000). (3) The observed flux is integrated over the “equal-arrival surface”. (4) The Klein–Nishina correction of the inverse Compton emission has been included. (5) Energy injection into the outflow is considered necessary in reproducing some multifrequency afterglow data of some GRBs. This may change the dynamics significantly.

By fitting the low-energy multiwaveband afterglows, from radio to X-ray band, parameters involved in the afterglow model are gotten. Simultaneous afterglow data in at least two well separated wavebands are needed to get a relatively well constrained set of parameters.

A rough estimate of the energy-integrated VHE afterglow flux (without correction by the cosmic background) is given by

$$F_{\gamma} \propto \frac{(1+z)L_{ssc}^{ssc}}{D_L^2} \max{(\nu_{ssc}^{-2}, \nu_T^{-2})}$$

where $L_{ssc}$ is the total luminosity of the SSC emission (see Equations (23)–(27) in Fan et al. 2008, for the expression), $\nu_{ssc}$ and $\nu_T$ are the typical SSC emission frequency and the SSC cooling frequency of the forward shock electrons (see Equations (33) and (34) in Fan et al. 2008, the case of $k = 0$, for the expressions), and $D_L$ is the luminosity distance of the event.

3. MODEL PREDICTION

High-energy photons, especially those in the TeV range, will be attenuated by the cosmic background light. Various models of the spectral energy distribution of the cosmic infrared background are proposed (Primack et al. 2001; Totani & Takeuchi 2002; Kneiske et al. 2002; Stecker et al. 2006), but all these models give comparable opacities for low redshifts. In this work, a level consistent with a study of two distant blazars and galaxy counts is used (P0.45; Aharonian et al. 2006a).

We adopt reasonable values of parameters for nearby GRBs and predict the spectra in the high-energy to VHE range. After corrected for the attenuation by extragalactic background, we compare them with the sensitivity levels of $\gamma$-ray instruments.

Parameters assumed and the time-averaged spectra, including both synchrotron and SSC components from the forward shocks, are shown in Figure 1. For this fictitious burst, current Imaging atmospheric Cherenkov telescopes would be more likely than space satellites such as EGRET, AGILE/GRID, and FGST/LAT to detect the modeled emission, as seen in Figure 1.

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9 The cooling of the forward shock electrons by the so-called “central engine afterglow” emission (the emission powered by the re-activity of the central engine in the afterglow phase, like the flares e.g., Nousek et al. 2006) or the plateaus followed by a sudden drop (e.g., Zhang 2009) and the corresponding inverse Compton emission can also be calculated self-consistently. But for our current sample such emission was not seen.
4. VERY HIGH ENERGY AFTERGLOW EMISSION OF NEARBY GRBS

For photons with energy higher than \( \sim 100 \) GeV, the attenuation due to interaction with background photons is significant if the source has a high redshift. Therefore nearby bursts (those with \( z < 0.25 \)) are chosen in this study.

4.1. The GRB Sample

To predict the VHE afterglow emission of nearby GRBs and compare the calculated results with the sensitivity of different \( \gamma \)-ray telescopes, GRBs in our sample must satisfy: nearby events to alleviate the attenuation effect; at least two independent waveband low-energy afterglows are recorded to get relatively constrained parameters; the low-energy afterglow can be reproduced according to the afterglow model.

In this work, we consider nearby GRBs (\( z < 0.25 \)) with relatively high luminosity and multiwavelength afterglow data sufficient to meaningfully constrain the properties of the GRBs (i.e., the model parameter values as described in Section 2.1) up to 2007 March. Five GRBs meet such criteria: GRB 030329, GRB 050509B, GRB 050709, GRB 060505, and GRB 060614. Though having a relatively large redshift of \( z \sim 0.55 \), GRB 051221A is also considered in this work because it is one of the brightest short GRBs detected so far.

GRB 030329 triggered the High Energy Transient Explorer, HETE-2 (Vanderspek et al. 2004). Very detailed BVRI afterglow light curves, spanning from \( \sim 0.05 \) to \( \sim 80 \) days, were compiled by Lipkin et al. (2004). Tiengo et al. (2004) reported \( XMM-Newton \) and Rossi-XTE (RXTE) \( \gamma \)-ray time observations of this burst. Based on the emission and absorption lines in the optical afterglow, a redshift of \( z = 0.1685 \) has been identified (Greiner et al. 2003).

The X-Ray Telescope (XRT) on board \( Swift \) began observations of GRB 050509B \( 62 \) s after the trigger of the Burst Alert Telescope (BAT; Gehrels et al. 2005). Optical and infrared data were reported in Bloom et al. (2006), Prochaska et al. (2005) and Bloom et al. (2005) reported a redshift of \( z \sim 0.22 \) based on numerous absorption features and a putative host galaxy, respectively.

GRB 050709 was discovered by HETE-2 (Villasenor et al. 2005). Its prompt emission lasted 70 ms in the \( 3-400 \) keV energy band, followed by a weaker, soft bump of \( \sim 100 \) s duration. The optical counterpart of this burst was observed with the Danish 1.5 m telescope at the La Silla Observatory. The observations started 33 hr after the burst and spanned over the following 18 days (Hjorth et al. 2005). Observations with the \( Chandra \) X-ray observatory revealed a faint, uncataloged X-ray source inside the HETE-2 error circle (Fox et al. 2005), which was coincident with a pointlike object embedded in a bright galaxy (Jensen et al. 2005) at \( z = 0.16 \) (Price et al. 2005).

GRB 051221A was localized by BAT (Cummings et al. 2005) and also simultaneously observed by the Konus-Wind instrument. The X-ray (\( \sim 10^{-3} - (2 \times 10)^{6} \) s; Burrows et al. 2006) and the optical (\( \sim 10^{-3} - (4 \times 10)^{3} \) s; Soderberg et al. 2006) afterglow light curves of GRB 051221A were well detected, while in the radio band only one detection followed by several upper limits are available (Soderberg et al. 2006). Soderberg et al. (2006) detected several bright emission lines, indicating a redshift of \( z = 0.5464 \).

GRB 060505 was detected by BAT in the 15–150 keV band (Palmer et al. 2006; Hullinger et al. 2006). Ofek et al. (2006) reported the detection of the optical transient, later confirmed by several instruments (e.g., Cobb et al. 2006; Schmidt et al. 2006). Based on the detection of the host galaxy emission lines, a redshift of \( z = 0.125 \) was proposed by Price et al. (2006) and confirmed by Fugazza et al. (2006). Note that the classification of GRB 060614 is ambiguous in the commonly used long/short burst scheme, since it has a long duration but no accompanying SN (Gehrels et al. 2006; Fynbo et al. 2006).

4.2. Constraining the Model Parameters

The available multifrequency afterglow data are then used to obtain the model parameters. In this work, we have reproduced the multifrequency afterglow data of GRB 030329 and GRB 060614.

The well-sampled distinguishing afterglow behavior of GRB 030329 has gained much attention. Some authors concentrated on the rebrightening occurring at 1.6 days after the trigger and considered different mechanisms to explain the rebrightening features seen in the optical light curves (Huang et al. 2006). We concentrate on the multiwaveband emission, from radio (Berger et al. 2003), optical (Lipkin et al. 2004), to X-ray band (Tiengo et al. 2004) for the purpose in this paper. We show in Figure 2 that, with a certain set of parameters, the numerical results can describe the observed data in all three wavebands. Fluctuations were captured in \( R \) band afterglow light curves after \( 5 \times 10^{4} \) s from the burst trigger, which may imply the multiple
energy injection into the outflow (Huang et al. 2006) or a two component jet (Berger et al. 2003). We ignore these details and focus on the general trend of the optical emission (particularly, in our calculation the energy of the relativistic ejecta is a constant). As shown in Figure 2, the difference is that in the time range (5 × 10^5)–10^5 s our approach gives a (little bit) brighter optical emission, so will be the high-energy emission.

The modeled and observed afterglow light curves of GRB 060614 are shown in Figure 3. Energy injection, starting around 30 minutes after the GRB onset, is needed in the afterglow modeling to reproduce the increase in flux (instead of simple power-law decay seen in other GRBs). The early X-ray flux before 500 s from the burst trigger, which is much brighter than the modeled flux, results from the dominating contribution from the prompt emission.

Table 1 lists the physical parameters derived from the afterglow modeling for GRB 030329 and GRB 060614. Parameters of GRB 050509B, GRB 050709, GRB 051221A, and GRB 060505 are taken from the literature, also listed in Table 1.

4.3. VHE Gamma-ray Observational Data

We are interested in VHE observations during the afterglow phase when the SSC is likely to dominate (see Section 5). VHE γ-ray afterglow data of three of the GRBs in the sample (i.e., GRB 030329, GRB 050509B, and GRB 060505) are available.

4.3.1. GRB 030329

Horan et al. (2007) reported a total of 4 hr of observations, which spanned five nights, using the Whipple 10 m telescope.

No evidence for VHE γ-ray signal was found during any of the observation periods. When combining all data, a flux upper limit of 1.4 × 10^{-11} erg cm^{-2} s^{-1} was derived. The first observation, lasting for about an hour, was started 64.6 hr after the burst. The 99.7% c.l. flux upper limit above an energy of ~ 400 GeV derived from this observation is shown in Table 2, as well as in Figure 4.

The 28 minute H.E.S.S. observation of GRB 030329 were taken 11.5 days after the burst (Tam et al. 2008). Since the burst position was located above the northern hemisphere, the zenith angle of the GRB observation was relatively large, i.e. 60°, resulting in an energy threshold of 1.36 TeV. No evidence for VHE γ-ray signal was found. The 99% c.l. flux upper limit (> 1.36 TeV) is 3.4 × 10^{-11} erg cm^{-2} s^{-1}, assuming a photon index of Γ = 3.

4.3.2. GRB 050509B

The observations of this burst using the STACEE detector employ an “on-off observation mode” and contain two 28 minute on/off pairs. The first on-source observation started 20 minutes after the burst and the second 80 minutes after the burst. After data quality cuts, about 18 minutes of useful on-source data remain in each observation. No evidence for VHE γ-ray signal above the energy threshold of 150 GeV was reported by Jarvis et al. (2008). The 95% c.l. flux upper limits (above 10 GeV, assuming a photon spectrum of dN/dE ∼ E^{-2.5}) were 3.8 × 10^{-10} erg cm^{-2} s^{-1} and 4.5 × 10^{-10} erg cm^{-2} s^{-1} for the

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| GRB     | z      | E0(erg)    | n0 (cm^{-3}) | p | ε_e | ε_B | L_{\text{jet}} | q | Injection Timescale(s) | References |
|---------|--------|------------|--------------|---|-----|-----|-------------|---|----------------------|------------|
| 030329  | 0.1685 | 1.4 × 10^{53} | 0.31         | 100 | 2.01 | 0.1 | 0.001       | ... | ...                  | This work  |
| 050509B | 0.2248 | 2.75 × 10^{48} | 0.5          | 1   | 2.2  | 0.15 | 0.046       | ... | ...                  | 1          |
| 050709  | 0.16  | 3.77 × 10^{50} | 0.5          | 6 × 10^{-3} | 2.6  | 0.4 | 0.25        | ... | ...                  | 2          |
| 051221A | 0.5465 | 10^{52}     | 0.1          | 0.01 | 2.4  | 0.3  | 2 × 10^{-4} | 2 × 10^{48} magnetar wind | < 1.5 × 10^4 | 3          |
| 060505  | 0.089 | 2.6 × 10^{50} | 0.4          | 1   | 2.1  | 0.1  | 0.008       | ... | ...                  | 4          |
| 060614  | 0.125 | 5 × 10^{50}  | 0.08         | 0.05 | 2.5  | 0.12 | 2 × 10^{-4} | 10^{48} | 10^{3–2} × 10^4 | This work  |

References. (1) Bloom et al. 2006; (2) Panaitescu 2006; (3) Fan & Xu 2006; (4) Xu et al. 2009.
Figure 4. Modeled time-integrated 0.1 GeV – 20 TeV afterglow spectra of six GRBs, in comparison with VHE upper limits (triangles). Dotted and solid lines represent the spectra with and without correction by the cosmic infrared background, respectively. For GRB 030329, GRB 050509B, and GRB 060505, the spectra were integrated over the corresponding time intervals during which the upper limits were derived, as shown in Table 2. For GRB 030329, thick (upper) lines indicate the modeled spectrum for the Whipple observation time, and thin (lower) lines for the H.E.S.S. observation time. The data points are plotted at the corresponding average photon energies. The modeled spectra of the remaining three bursts are obtained by integrating the spectra over a time period of 2 hr, starting from 10 hr after the trigger.

Table 2

| GRB    | Telescope | $T_{OBS} - T_{GRB}^{a}$ | Exposure Time | Energy Threshold (GeV) | Energy Flux Upper Limit Set by Observations (erg cm$^{-2}$ s$^{-1}$) | Predicted Energy Flux (erg cm$^{-2}$ s$^{-1}$) | References |
|--------|-----------|-------------------------|---------------|------------------------|------------------------------------------------------------------|-----------------------------------------------|------------|
| 030329 | H.E.S.S.  | 11.5 days               | 28 minute     | 1360                   | $3.4 \times 10^{-11}$                                             | $8.5 \times 10^{-15}$                         | 1          |
| 030329 | Whipple   | 64.55 hr                | 65.2 minute   | 400                    | $5.8 \times 10^{-11}$                                             | $6.7 \times 10^{-13}$                         | 2          |
| 050509B| STACEE    | 20 minute/80 minute     | 28 minute     | 150                    | $3.8 \times 10^{-10}/4.5 \times 10^{-10}$                         | $2.2 \times 10^{-10}/8.4 \times 10^{-17}$    | 3          |
| 060505 | H.E.S.S.  | 19.4 hr                 | 2 hr          | 450                    | $8.8 \times 10^{-12}$                                             | $2.5 \times 10^{-15}$                         | 1          |

Note. 
$^{a}$ The time between the start of the GRB and the beginning of observations for different telescopes.

References. (1) Tam et al. 2008; (2) Horan et al. 2007; (3) Jarvis et al. 2008.
first and second on-source observation, respectively (A. Jarvis 2008, private communication).

4.3.3. GRB 060505

The H.E.S.S. observations began 19.4 hr after the burst and lasted for 2 hr (Tam et al. 2008). No evidence for VHE $\gamma$-ray signal was found. The 99% c.l. flux upper limit ($> 0.45$ TeV) is $8.8 \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$, assuming a photon index of $\Gamma = 3$.

4.4. Comparison to Observations

Based on the parameters obtained in Section 4.2, the GeV–TeV emission is obtained using the code described in Section 2.2.

We depict the calculated high-energy afterglow spectrum in Figure 4, which shows the time-integrated high-energy afterglow spectrum of these six events. The solid and dashed lines represent the intrinsic SSC spectra and corrected spectra for each GRB, respectively. The absorption is based on the cosmic infrared background model “P0.45” (Aharonian et al. 2006a)\(^\text{10}\). Such a model is constrained by the upper limits provided by two unexpectedly hard spectra of blazars at optical/NIR wavelengths and is close to the lower limit from integrated light of resolved galaxies.

In order to compare with the VHE observational data which are usually given in integrated photon fluxes, we integrate the spectra above the energy threshold. We consider first the GRBs are usually given in integrated photon fluxes, we integrate the light of resolved galaxies.

In order to compare with the VHE observational data which are usually given in integrated photon fluxes, we integrate the spectra above the energy threshold. We consider first the GRBs with VHE data. These include GRB 030329, GRB 050509B, and GRB 060505. In Table 2 we list the modeled integrated energy fluxes after correction due to interaction with photons from cosmic infrared background, as well as the VHE $\gamma$-ray observations and the derived upper limits. All predicted fluxes are below the upper limits derived from the VHE observations.

We then investigate whether a sensitive VHE instrument is expected to detect the predicted VHE signal from nearby GRBs during the late afterglow phase. We use H.E.S.S. sensitivity as an example of an array of sensitive atmospheric Cherenkov telescopes. The sensitivity level of the H.E.S.S. detector is shown in Figure 5, assuming a $\Gamma = 2.6$ spectrum (Aharonian et al. 2006b). Assuming softer spectra, the level is higher, and the difference is about 50% between $\Gamma = 2.0$ and $\Gamma = 3.0$ (c.f. Aharonian et al. 2005). We show the temporal evolution of energy fluxes ($>200$ GeV) of six GRBs in our sample in Figure 5, indicating that only the VHE signal from GRB 030329 may be above the H.E.S.S. sensitivity. For GRB 030329 which is a bright burst with low redshift, the expected energy flux would be high enough to be detected with a delayed observation time of $\lesssim 10$ hr if the GRB position was favorable, i.e., with zenith angle $< 20^\circ$ (and thus an energy threshold of $\sim 200$ GeV is attained).

5. DISCUSSION

In this paper, we have calculated the SSC emission from the forward shock electrons following Fan et al. (2008). We shall discuss here the importance of other radiation processes in the late afterglow phase.

Possible VHE $\gamma$-ray emission initiated from protons has been suggested (Totani 1998; Böttcher & Dermer 1998). However, the proton-synchrotron component, as well as the hadron-related photo-meson electromagnetic components, is in most cases overshadowed by the SSC component of electrons in the afterglow phase. This is especially the case for the parameter values of $\epsilon_e$ and $\epsilon_B$ used here in the modeling of these six GRBs (e.g., Zhang & Mészáros 2001b).

Additional inverse Compton component will play a role and will enhance any VHE emission. SSC is, in general, only a lower limit. Another possible contribution to VHE emission is related to the “central engine afterglow” emission, like the flares (e.g., Falcone et al. 2007) or the plateaus followed by a sudden drop (e.g., Zhang 2009). The SSC radiation of the late internal shocks or the external inverse Compton radiation in the external forward shock front may be able to give rise to some VHE emission signals (see Fan & Piran 2008 for a review). However, no “central engine afterglow” emission has been reported in the late afterglow phase for the six bursts we studied. So it is hard for us to estimate its ability to enhance the detectability of the VHE emission.

As shown in Figure 5, we only expect detectable signal using a sensitive ground-based $\gamma$-ray detector for a bright and nearby GRB like GRB 030329. The rate of such nearby and energetic GRBs is very uncertain. GRB 940217 might have been another event of this kind (Wei & Fan 2007).

Several factors that reduce the chance of detecting VHE photons can be summarized as follows: firstly, as a result of large zenith angles (e.g., $60^\circ$ for GRB 030329), the energy thresholds of some observations are relatively high ($\sim 1.4$ TeV). Any VHE photon is severely attenuated by the cosmic infrared background, unless the level is very low. Secondly, the observations were taken at very late epochs, e.g., 11.5 days after the burst for H.E.S.S. observations of GRB 030329, when expected VHE flux had largely decayed. Thirdly, the fraction of low-redshift GRBs is small, e.g., see the catalog in Butler et al. (2007). For GRB 051221A (at $z = 0.55$) studied here, the attenuation is severe at energies $\gtrsim 200$ GeV.

Despite these practical limitations, detection of VHE afterglow emission of GRBs is probable. Those GRBs close enough ($z < 0.5$) and with an intrinsic high luminosity (like GRB 030329), can be detected above $\sim 200$ GeV when the observation is taken within $\sim 10$ hr after the burst. From Equation (1), GRBs with low $z$, large $E_0$, large $\epsilon_e$, and small $\epsilon_B$ are more

\(^{10}\) This implies a gamma ray horizon at a redshift of about 0.2 (0.05) for 500 GeV (10 TeV) gamma rays.
likely to be detected in the VHE band. Besides, in general the expected VHE afterglow flux decays as $t^{-\alpha}$ where $\alpha$ is at least one. Thus, observations with shorter delay are more likely to probe the predicted VHE emission.

The main purpose of this work is to provide a relatively reliable prediction of the detectability of the VHE emission from nearby GRBs. It is also interesting to explore the role of the VHE afterglow emission in revealing the GRB physics. Perhaps the most robust conclusion is that the VHE emission in late afterglow phase cannot be attributed to the synchrotron radiation of the forward shock, for which the maximal photon energy is $\approx 30\Gamma/(1+z)$MeV (Cheng & Wei 1996), where $\Gamma$ is the bulk Lorentz factor of the decelerating outflow. In general, for $\epsilon_B^G \gg \epsilon_e$, the inverse Compton emission is expected to be very weak. So the detection of VHE afterglow emission from GRBs requires that $\epsilon_B^G \ll \epsilon_e$, in support of the current radio/optical/X-ray afterglow modeling (e.g., see Table 1). Together with Swift, AGILE, FGST, and some ground-based optical telescopes, ground-based $\gamma$-ray detectors can provide us continuous spectra in the optical to TeV energy band during the afterglow phase. A self-consistent modeling of these data in a very wide energy band, in principle, will impose very tight constraint on the physical parameters and on the environment. However, given the small number of the VHE photons expected from a single burst, we do not expect that the VHE emission can help us a lot to achieve such goals.

6. CONCLUSIONS

In this work, we discuss the prospect of detecting VHE $\gamma$-rays with current ground-based detectors in the late afterglow phase. During this phase, the dominant radiation process in the VHE $\gamma$-ray regime is the SSC emission from the forward shock electrons. Klein–Nishina effects and attenuation by the cosmic infrared background, both known to suppress the VHE $\gamma$-ray spectra, were taken into account. To minimize the attenuation effect, we chose a sample of six nearby GRBs in this study. We have calculated the detailed SSC emission numerically using the model developed by Fan et al. (2008), with a set of parameters which are able to reproduce the available multiband afterglow light curves. The results are consistent with the upper limits obtained using VHE observations of GRB 030329, GRB 050509B, and GRB 060505.

Moreover, assuming observations taken 10 hr after the burst, the VHE signal predicted from five GRBs is below the sensitivity level of a current sensitive atmospheric Cherenkov detectors mainly due to the low fluence of these outflows. For those bright and nearby bursts like GRB 030329, a VHE detection is possible even with a delayed observation time of ~10 hr.

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