Raman Excitation of Hydrogen Molecules to v = 1 State

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ABSTRACT: Coherent anti-Stokes Raman scattering (CARS) can reveal a molecule’s vibrational spectrum to a great extent. Instantaneous interaction of Stokes and pump beams stemming from powerful pulsed lasers excites a molecule’s vibrational modes in CARS. In this technique, combining two visible laser beams could create spectra resonances relating to vibrational transitions. In this work, Raman excitation of Hydrogen molecules to v = 1 state is achieved by CARS spectroscopy. CARS measurements are successfully carried out for H2 S-branch and Q-branch transitions using our laser system. This measurement proves the feasibility of CARS experiment which could be employed to excite molecules to a specific rovibrational state. Moreover, experiments conducted for CARS signal with respect to various gas pressures differing between 200 and 600 torr for S-branch transition of H2 molecule.

Keywords: H2, Coherent anti Stokes Raman scattering, S-branch, Q-branch

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INTRODUCTION

Terhune and Maker first observed coherent anti-Stokes Raman scattering (CARS) (Terhune & Maker, 1965; Terhune & Maker, 1963). Non-linear Raman processes is one of such spectroscopic technique which has been feasible with employment of lasers. Spontaneous Raman (Anderson, 1971; Buric et al, 2009; Farahani & Gogolla, 1999; Tang et al, 2020), Resonance Raman (Kiefer & Bernstein, 1972; Liu et al, 2013; Saito et al, 2003; Xie et al, 2009), Inverse Raman (Takaya et al, 2019; Yeung, 1974), Hyper Raman scattering (Babenko et al, 2020; Madzharova et al, 2017; Verdieck et al, 1970; Zhu et al, 2018) and Raman-induced Kerr effect (Ando et al, 2020; Heiman et al, 1976; Kakinuma & Shirota, 2018) are amongst various examples of Raman processes. CARS is a very effective non-linear spectroscopic technique that has been used in various applications such as temperature and concentration measurement, molecular relaxation processes, gas-phase and plasma diagnostics and femtosecond chemistry (El-Diasty, 2011; Lempert & Adamovich, 2014; Tolles et al, 1977; Zeltikov, 2000). CARS spectroscopy has been a common means of detection for modern optical experiments and comprehensively mentioned in literature (Christensen et al, 2019; Eckbreth, 1996; Eesley, 2013; Harvey & Nibler, 1978; Jiang et al, 2020; Kifer, 1980; Short et al, 2015; Yan et al, 2018; Yang et al, 2018).

CARS is very promising for its potential to obtain analytical and spectroscopic knowledge relating to Raman active resonances in matter including gas, liquid and solid (Jones et al, 2019; Kushwaha et al, 2018; Portnov et al, 2010). CARS is generally used in applications such as in chemistry, physics, and related fields to determine a structural fingerprint through which molecules can be identified. CARS is also employed for species selective microscopy and combustion diagnostics by exploiting the selectivity of vibrational modes (Cutler et al, 2018; Ehn et al, 2017; Goodhead et al, 2015; Zhang & Cheng, 2018). In this technique, combining two visible laser beams could create spectra resonances relating to vibrational transitions. CARS exhibits a third-order non-linear process. Compared to second-order non-linear effect, it can be applied to both an isotropic and a non-centrosymmetric medium. Additionally, it has a conversion efficiency for coherently producing photons that are significantly greater than spontaneous Raman scattering (CARS can achieve \(10^5\) increase in efficiency of conversion (Begley et al, 1974)). That is a very practical tool to obtain luminescent samples’ spectra such as electric discharges, impurities, fluorescent materials and combustion systems as well as some solutes (Butler et al, 2016; Dedic et al, 2017; Sarri et al, 2019; Teramoto & Ono, 2014; Tolles et al, 1977). Because of advantages mentioned above, in this paper, we employ CARS technique for experimentally determining the pump wavelength that will be used in the Stimulated Raman Pumping (SRP) scheme (Candan, 2016).

In CARS, two laser fields with \(\omega_1\) and \(\omega_2\) frequencies mix in a medium in order to produce a non-linear polarisation that oscillates at \(2\omega_1 - \omega_2\) frequency since it is an optical phenomenon that is coherent and third order non-linear process. This is resonantly enhanced when \(\omega_1 - \omega_2\) frequency difference coincides with a Raman active transition in the active sample as displayed in Figure 1. \(\omega_1\) and \(\omega_2\) are corresponding to \(\omega_{\text{pump}}\) and \(\omega_{\text{Stokes}}\) fields, respectively. The resulting field produced at \(2\omega_1 - \omega_2\) required to match in phase with non-linear polarisation produced by pump field in \(\omega_1\) and \(\omega_2\) frequencies. This process is described according to following expression:

\[
2k(\omega_1) - k(\omega_2) = k(2\omega_1 - \omega_2). \tag{1}
\]

The wave vector mismatch \(\Delta k\) becomes finite because of material dispersion (Ochkin, 2009; Regnier et al, 1974). Additionally, dispersion rate in dilute gases becomes very low. The rotation-vibration resonances’ coherence length in Hydrogen molecule happens to be \(\approx 10\) cm for a collinear geometry (Regnier et al, 1974).
Figure 1. Energy levels of CARS is demonstrated. This process is a coherent and non-linear optical phenomenon of third order where $\omega_{\text{pump}}$ and $\omega_{\text{Stokes}}$ combine through a medium to produce a signal with frequency of $2\omega_{\text{pump}} - \omega_{\text{Stokes}}$. The resultant signal is resonantly improved once $\omega_{\text{pump}} - \omega_{\text{Stokes}}$ coincide with vibrational constant of energy levels.

The CARS process needs two high-powered (commonly pulsed) laser fields that have $\omega_p$ and $\omega_s$ frequencies which are tightly focused into sample. Therefore, owing to non-linear mixing of two laser beams, an output beam is generated in the medium that is coherent and similar to a moderate intensity laser beam at frequency $2\omega_p - \omega_s$. The efficiency rate of frequency $\omega_s$ strongly depends on the present molecular resonances at a frequency difference that equals to $\omega_p - \omega_s$, the laser power, the number density of species and the resonance line width (Kliwer et al, 2012; Tolles et al, 1977).

**CARS wavelength calculation**

In the Raman Spectrum, vibrations and rotations of molecules are in visible rage. Molecules including $\text{H}_2 \text{, N}_2 \text{ or O}_2$ can be studied only with Raman spectroscopy as their rotations and vibrations happens to be infra-red inactive. Raman active molecules needs to follow rules of selection for Raman spectrum. Raman spectroscopy happens to be two-photon phenomenon. For vibrational transitions, the selection rules follow $\Delta v = \pm 1$ in the Raman spectrum, in which Stokes transitions are corresponding to $\Delta v = +1$, and anti-Stokes transitions to $\Delta v = -1$. Moreover, that obey $\Delta J = 0, \pm 2$ for the rotational transitions in which the S-branch, Q-branch and O-branch transitions are labelled as $\Delta J = +2, \Delta J = 0$ and $\Delta J = -2$, respectively.

In this paper, wavelength of CARS is determined in $\text{H}_2$. For calculating CARS wavelength in $\text{H}_2$, S-branch transition is selected. This occurs from $v'' = 0, J'' = 1$ to $v' = 1, J' = 3$. $v'' = 0, J'' = 1$ quantum state is selected since at the room temperature it is the most populated state. For this particular transition, vibrational constant ($\omega_{\text{vib}}$) is equal to $4712.91 \text{ cm}^{-1}(\bar{v}_v)$ (Dabrowski, 1984; Turner et al, 1977). In our calculations, the wavenumber units are employed in terms of frequency. Initially, we established the Stokes laser (IR laser) wavelength. Therefore, the wavelength of Stokes line is determined to be at $1064.555 \text{ nm}$. Utilizing expression of $\bar{v}_p = \bar{v}_v + \bar{v}_s$, in which $v_v$ and $v_s$ are assigned to pump and Stokes wavenumbers, respectively. After that, $\bar{v}_p = 14106.51 \text{ cm}^{-1}$ could be determined. Next, wavelength of CARS could be determined using $\bar{v}_{\text{cars}} = \bar{v}_v + \bar{v}_p$ expression. Thus, that enable us to calculate $\bar{v}_{\text{cars}} = 18819.42 \text{ cm}^{-1}$ as illustrated in Figure 2.
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Figure 2. Figure shows CARS process in $\text{H}_2$ molecules. 708.893 nm pump beam stimulates the $\text{H}_2$ at $v'' = 0$, $J'' = 1$ to another level (virtual). After that, 1064.555 nm Stokes beam instantaneously brings the molecule down to a rovibrationally excited state of $v' = 1$, $J' = 3$. Next, 708.893 nm probe beam excites it to another nonreal state once more. Finally, because it does not remain in this nonreal state, the molecule spontaneously must deexcite to the ground state together with releasing 531.370 nm CARS photon.

Moreover, wavelength of CARS signal is determined for Hydrogen molecule’s Q-branch transition that stems from $v'' = 0$, $J'' = 1$ level and reaches to $v' = 1$, $J' = 1$. Scattering rate is related to polarisability tensor of the transition squared (Eckbreth, 1996). Scattering intensity of Q-branch is greater than S-branch because the scattering intensity is related to the Placzek-Teller coefficients of each transition. Therefore, Q-branch transition’s CARS signal is much higher compared to S-branch. Vibrational constant equals to 4155.25 cm$^{-1}$ for this transition and the corresponding wavelengths are determined. Thus, if we apply 1064.555 nm Stokes beam, then 738.07 nm resulting pump beam can be determined. Therefore, 564.84 nm CARS signal occurs in the measurement.

MATERIALS AND METHODS

Experimental setup

In order to conduct CARS experiment, two laser beams need to be employed. Pump and Stokes beam are generated using a dye laser (Continuum, ND6000, USA) and custom-made laser (Continuum, USA), respectively. For realizing the experiment, we need to both spatially and temporally coincide these two beams in a $\text{H}_2$ containing glass cell.

Laser system

Dye laser

Dye laser is used to produce pump beam in the experiment. This laser is injected using pulsed laser comprising Nd:YAG crystal as gain medium (Quanta-Ray Pro-series, Spectra-Physics) that contains 532 nm frequency doubled output and has a repetition rate of 10 Hz. In order to produce the necessary tunable output of the dye laser (700 to 740 nm wavelength rage), 114 mg L$^{-1}$ and 20 mg L$^{-1}$ dye solution of LDS 750 in methanol were employed for oscillator and amplifier, respectively. Thus, necessary tunable 719 nm output was generated.

IR laser (Custom-built)

IR laser beam is employed to be Stokes beam in the experiment. For optical Stark acceleration/deceleration, a high-energy, chirped laser has explicitly constructed and built at UCL (Coppendale et al, 2011; Maher-McWilliams et al, 2012). The laser system consists of two pulsed
outputs. It is primarily originated in a laser of 1064 nm Nd:YVO₄ microchip which could quickly tune the frequency using a cavity containing an electro-optic crystal. A laser diode is injection-locked the output and a fibre amplifier is used to magnifies the output to 1 W power. Next, the resultant beam is splitted into separate pulses employing pulse shaper. Later, generated pulses are separated and then connected to separate fibres in which one of them is 55 m longer compared to other one. The resultant difference in path generates 275 ns time delay. Once the microchip laser is being chirped, that produces a frequency variation which is well-defined. After exiting fibres, two pulses are magnified using different flash lamp stages and high intensities are produced using pulsed Nd:YAG amplifiers. Such laser system can produce two high power beams that have flat-top temporal shapes. In this system, the frequency change can be chirped by 1.1 GHz during the pulse of 140 ns (Coppendale et al, 2011). Prior to the experiment, wavemetre (HighFinesse GmbH, WS-6, Germany) and Burleigh wavemetre (WA- 2000, USA) are employed to calibrate ND6000 and custom-built laser wavelength, respectively.

Optical setup

Optical setup of CARS experiment is demonstrated in Figure 3. Experiment contains different laser beams that are nearly co-propagating. 1064 nm IR beam is utilized as Stokes beam. 708 nm dye laser beam is employed as pump beam. Because linearly polarising pump and Stokes beams are very important (Bartlett et al, 2008), a λ/2 plate is positioned in path of Stokes beam for parallel polarization. Once two fields possess same polarisation, output signal could be significantly improved. 15 cm lens is used for focusing two collinear beams into gas cell. Following the intersection of beams being spatial and temporal overlapped, a green colour CARS signal is produced as illustrated in Figure 3. For separating the resultant beam, a few additional optics are utilized. Another 15 cm lens is employed for collimating the beams at the end of the gas cell. M4 mirror is installed following the collimating lens for filtering majority of the remaining pump and Stokes beam. Next, F1 and F2 are used filters for filtering the residual small part of beams. F2 blocks residual part of Stokes one while F1 merely allows produced beam of CARS signal. Finally, just CARS beam gets to the photodiode and the generated signal is delivered to the scope for detection before we automatically record it on PC.
Alignment

Spatial overlap
Because CARS experiment involves two nearly co-propagating laser beams, we need to spatially align these beams into a confocal point. In order to successfully overlap them, a specifically devised plate having a hole is mounted onto both collimating and focusing lens as illustrated in Figure 3. Initially, 1064 nm Stokes beam needs to be aligned via the holes on the plate using beam walking technique. When that is accomplished, 708 nm pump beam is passed via both holes by the beam walking. Following that, pin hole with a 50 µm diameter is positioned on a movable stage at beam focus for ensuring the two beams are fully aligned at focal point. At first, 50 µm hole is modified in which the Stokes beam focuses. Next, the pump beam is passed via the pin hole. As a result, two beams are spatially intersected.

Temporal overlap
The temporal overlapping of the pulses is accomplished using different delay generators (Stanford Research Systems, Model DG535, USA). Two pulses are initiated employing 5 V output from IR laser through autonomously controlled delay generators. Generated pulses are uncovered using a photodiode and directed to oscilloscope (LeCoy, Wavepro 7300, USA) in which level of overlapping could be seen and controlled.

Data acquisition
A photodiode is used to identify produced signal as illustrated in Figure 3. We first observed on scope and then it is being logged on computer. In the measurement, the signal is attained using the photodiode and all data points are averaged before being saved. The dye laser is scanned around the anticipated peak to obtain the data. Once signal is detected, the data attained on the oscilloscope are logged on PC. Prior to examining the pump laser for recording the signal, as illustrated in Figure 2, the projected pump beam’s peak wavelength is determined and then, the resultant wavelength of CARS signal is established.

RESULTS AND DISCUSSION
The parameters for experiment are needed to be optimized prior to carrying out the measurements. Firstly, dye laser and IR laser power outputs were improved to be adequately high in order to conduct the CARS experiment. The beam intensities are required to be roughly $10^{10}$ W cm$^{-2}$ to accomplish the CARS measurement. Dye laser possessed 5 mJ pulse$^{-1}$ output power and 10 ns pulse duration. Custom laser acquired 70 mJ pulse$^{-1}$ output power and 140 ns pulse duration. The beam waist was evaluated to become 68 µm for pump and 46 µm for Stokes beam. Consequently, at focus, the pump and Stokes beam intensities were determined to be 5 x $10^9$ W cm$^{-2}$ and 1 x $10^{10}$ W cm$^{-2}$. Additionally, 10% H$_2$ in Neon gas mixture was employed in the gas cell for carrying out the measurement.

Measured CARS signal
Initially S-branch transition in H$_2$ was investigated for measuring the CARS signal. The obtained signal of the S-branch transition in H$_2$ is demonstrated in Figure 4 at pressure of 600 torr. In this transition, the H$_2$ molecules at v" = 0, J" = 1 are promoted from to v' = 1, J' = 3. Between 708.800 and 709.000 nm, we scanned the pump laser in order to generate CARS signal meanwhile 1064.555 nm Stokes beam is being fixed. 0.005 nm step size was applied to dye laser during scanning stage for not skipping the resonant peak of the signal. 708.90 nm peak of CARS signal was obtained. Therefore, the resultant 531.370 nm CARS wavelength was measured which corresponds to green light.
Figure 4. CARS signal of H$_2$ molecule for transition of S-branch is demonstrated. 708.899 nm pump and 1064.555 nm Stokes beam are employed. Resultant 531.370 nm wavelength of CARS signal is found.

Figure 5. CARS signal with respect to various gas pressures in H$_2$ molecule for S-branch transition that differ from 200 to 600 torr.
CARS signal’s pressure dependence

The signal’s dependence on pressure measurement is conducted for determining the signal intensity on the pressure. Figure 5 indicates the dependence of CARS signal on pressure that is number density in interaction region. The measurement was performed for various pressures ranging between 200 and 600 torr. The signal rises with respect to increasing the molecules’ number density as shown in Figure 5. Once pressure reaches to 200 torr, the signal practically vanishes. However, the CARS signal strength enhances dramatically by inserting additional amount of gas. A gas mix of 10% Hydrogen in Neon were utilized for measurements. Consequently, Hydrogen molecules produces a relative density of 10% in the gas mix.

![Graph showing CARS signal dependence on pressure](image1)

**Figure 6.** CARS signal of H₂ molecule for S-branch transition depending on various gas pressures that vary from 200 to 600 torr.

| Pressure (Torr) | 200 | 300 | 400 | 500 | 600 |
|----------------|-----|-----|-----|-----|-----|
| CARS signal (mV) | 7   | 10  | 15  | 30  | 55  |

**Table 1:** Measured pressures with respect to obtained CARS signal.

![Graph showing CARS signal dependence on pump wavelength](image2)

**Figure 7.** The enhanced CARS signal for transition of Q-branch in H₂ is demonstrated. 738.070 nm pump beam wavelength occurs as 1064.555 nm Stokes beam is fixed. Thus, subsequent 564.840 nm CARS signal is generated.
Figure 6 demonstrates CARS signal at various gas pressures. These data are fitted to a function (i.e. an exponential) on the Origin lab program. The signal grows exponentially while the pressure increases in the measurements. Hence, an agreement between our data and CARS theory has been achieved.

**Q-branch transition measurement**

An enhanced CARS signal is generated by investigating Q-branch transition of the H$_2$. The Q-branch signal strength is measured to be significantly enhanced compared to the preliminary measurements of the S-branch since Q-branch transition probability is much bigger than S-branch. In the Q-branch transition measurement, H$_2$ molecules at $v'' = 0, J'' = 1$ are excited to $v' = 1, J' = 1$. The signal of Q-branch transition is shown in Figure 7. Pump has a peak of 738.070 nm whereas it is 1064.555 nm for Stokes beam. Therefore, resultant beam has a peak at 564.840 nm that happens to be in the green region of the solar spectrum. In our measurement, the produced CARS signal is so intense that it could be observed by naked eyes. The fact that CARS signal could be viewed by naked eyes implies a substantial rise in the H$_2$ molecules’ numbers being promoted to excited vibrational state $v' = 1$.

**CONCLUSION**

The wavelength of pump to be utilized in the SRP was successfully establish. Measurements of CARS experiment are effectively carried out for transitions of S- and Q-branch in H$_2$. On one hand, the wavelength of pump was established to be used in projected SRP on the other hand, we validated the laser setup is feasible for generating H$_2$ molecules at $v' = 1$ quantum state. Even though we evaluated the CARS signal of H$_2$ S- and Q-branches in the measurements, the O-branch of H$_2$ transition can be identified using the same procedure as well. Moreover, CARS experiment could be utilized to ascertain the temperature of the molecule by establishing a number of rovibrational level populations of a molecule. The constraint in CARS method is that it is not very effective at low number densities since its efficiency is exceedingly reliant on the molecules’ number density.

CARS spectroscopy has become a well-established method. Many experiments are described on establishing of the gas, rotational and vibrational temperatures of H$_2$ molecules in discharge plasmas (Dedic et al, 2017; Lempert & Adamovich, 2014; Shirley & Hall, 1977; Yatom et al, 2013) including concentration measurement (Jensen et al, 2019; Kearney et al, 2013; Ran et al, 2019; Regnier et al, 1974) by utilizing CARS method. CARS has similarly been employed in part to accomplish for preparing the oriented and aligned H$_2$ and HD molecules using stimulated Raman pumping(Bartlett et al, 2008; Choi et al, 2019; Follick et al, 2011; Lim et al, 2020). CARS method has recently been applied in Raman microspectroscopy for both in-vivo and in-vitro tissue diagnostics(Gong et al, 2020; Krafft et al, 2012; Moura et al, 2016). CARS has a significant potential in bioanalytical and biomedical sciences because of its non-invasive and label-free nature.

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**Conflict of Interest**

I declare that there is no conflict of interest during the planning, execution and writing of the article.
Author’s Contributions

I hereby declare that the planning, execution and writing of the article was done by me as the sole author of the article.

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