An intrinsic mass generation mechanism for exotic ELKO dark matter fields is scrutinized, in the context of the very special relativity (VSR). Our results are reported on unraveling inequivalent spin structures that educe an additional term on the associated Dirac operator. Contrary to the spinor fields of mass dimension 3/2, this term is precluded to be absorbed as a shift of some gauge vector potential, regarding the equations for the dark spinor fields. It leads to some dynamical constraints that can be intrinsically converted into a dark spinor mass generation mechanism, with the encoded symmetries maintained by the VSR. The dynamical mass is embedded in the VSR framework through a natural coupling to the kink solution of a $\lambda\phi^4$ theory for a scalar field $\phi$. Our results evince the possibility of novel effective scenarios, derived from exotic couplings among dark spinor fields and scalar field topological solutions.

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is affected by the transformation $V \mapsto V + \frac{1}{2\pi} \xi^{-1} d\xi$, which indeed corresponds to the addition of an gauge potential extra term. Such an exotic term may be therefore absorbed by an external abelian gauge potential, representing an element of the cohomology group $H^1(M, \mathbb{Z}_2)$. In the context of the (exotic) Dirac equation. Notwithstanding, concerning exotic ELKO dark spinor fields the possibility of such an intrinsic coupling to SM gauge fields is null. Since gauge fields interactions with ELKO are suppressed, ELKO fields are able to probe purely the space-time topology. It consistently reinforces the above mentioned darkness of such fields. This paper is organized as follows: in the next Section, the exotic structure underlying ELKO dark spinor fields is briefly revisited. In Section III we identify some similarities between the exotic Dirac operator and the covariant derivative embedded into the framework of the VSR, so that the Klein-Gordon equation for a massive particle can be reproduced. By identifying the VSR preferential direction with a dynamical dependence on the framework of the VSR, exotic ELKO dark spinor fields are able to probe purely the space-concerning exotic ELKO fields the possibility of such an intrinsic coupling to SM gauge fields is null. It evinces the possibility of novel scenarios for the mechanism of dynamical mass generation, as well as for exotic couplings with scalar field topological solutions. In Section IV we conclude and provide novel perspectives on the potentially relevant and prominent results addressed in this paper.

II. EXOTIC ELKO DARK SPINOR FIELDS

ELKO spinor fields $\lambda(p)$ are defined as eigenspinors of the charge conjugation operator $C = \begin{pmatrix} 0 & i\theta \\ -i\theta & 0 \end{pmatrix} K$, in the precise sense that $C\lambda(p) = \pm \lambda(p)$, where, given the rotation generators $J$, the Wigner’s spin-1/2 time reversal operator $\Theta$ satisfies $\Theta J \Theta^{-1} = -J^\dagger$. The operator $K$ is responsible to $\mathbb{C}$-conjugate spinor fields appearing on the right. The plus [minus] sign stands for self-conjugate [anti self-conjugate] spinor fields $\lambda^{S/A}(p)$ [$\lambda^{\dagger S/A}$(p)]. The complete form of ELKO can be explicitly obtained through the solution of the equation of helicity $(\sigma \cdot \hat{p})\lambda^{A/S}(p) = \pm \lambda^{A/S}(p)$, where $\hat{p} = p/\|p\|$. The four boosted spinor fields are

$$\lambda^{S/A}_{(\mp, \pm)}(p) = \sqrt{\frac{E + m}{2m}} \left( 1 \mp \frac{p}{E + m} \right) \lambda^{S/A}_{(\mp, \pm)}(0), \quad \lambda^{S/A}_{(\mp, \pm)}(0) = \left( \pm i \Theta |\phi^\pm(0)|^* \right)$$

The (Weyl) spinors fields $\Theta |\phi^\pm(0)|^*$ and $\phi^\mp(0)$ have opposite helicities.

Prior results moreover evince that ELKO can be expressed through a linear combination of Dirac particle and antiparticle fields, and the prescription $p_\mu \mapsto i\nabla_\mu$ holds for ELKO: $\lambda^{S/A}(x) = \lambda^{S/A}(p) \exp(\epsilon^{S/A} i p_\mu x^\mu)$, where $\epsilon^S = -1$ and $\epsilon^A = +1$.

Besides the standard ELKO spinor fields $\lambda(x)$, one can get a second type of ELKO, denoted hereupon by $\hat{\lambda}(x)$, associated to an inequivalent spin structure, that reflects a modification of the covariant derivative $[29, 32]$

$$\hat{\nabla}_X \hat{\lambda}(x) = \nabla_X \hat{\lambda}(x) - \frac{1}{2} \left[ X \cdot (\xi^{-1}(x)d\xi(x)) \right] \hat{\lambda}(x),$$

where $X$ denotes a vector field. The so called exotic term in Eq.(1) is assumed to be re-scaled as $\frac{1}{2\pi} (\xi^{-1}(x)d\xi(x))$, an integer of a Čech cohomology class. The exotic Dirac operator can be written thereupon as

$$i\gamma^\mu \nabla_\mu = i\gamma^\mu \nabla_\mu + \frac{1}{2} \xi^{-1}(x)d\xi(x),$$

and the exotic Dirac equation then becomes

$$(i\gamma^\mu \nabla_\mu + (\xi^{-1}(x)d\xi(x))/2 \pm m|)\psi(x) = 0,$$

where $\psi$ denotes a Dirac spinor field. As sustained in [28, 32], one can express $\xi(x) = \exp(2i\theta(x)) \in U(1)$, so that the exotic term yields $\xi^{-1}(x)d\xi(x) = 2i\gamma^\mu \partial_\mu \theta(x)$. One hence obtains the explicit form for the coupled system of equations for the exotic ELKO as

$$(i\gamma^\mu \nabla_\mu + i\gamma^\mu \partial_\mu \theta(x))\delta^+_{\pm} \pm m|E^+_{\pm}| \hat{\lambda}^{S/A}(x) = 0, \quad \xi^{\mp}_{(\pm, \mp)} = -1$$

1 The boosts here presented are Lorentz boosts, although $\text{SIM}(2)$ VSR boosted ELKO can be derived as in [23]. For our aim in what follows Lorentz boosts suffice, and therefore shall be adopted.
or, more explicitly — taking into account Eq. (2):

\[
\begin{pmatrix}
  (i\gamma^\mu \nabla_\mu \otimes \otimes \otimes \otimes) \chi^{S/A}_{\{\pm, \mp\}} & \chi^{S/A}_{\{\pm, \pm\}} \\
  \chi^{S/A}_{\{\pm, \mp\}} & \chi^{S/A}_{\{\pm, \pm\}} \\
  \chi^{S/A}_{\{\pm, \mp\}} & \chi^{S/A}_{\{\pm, \pm\}} \\
  \chi^{S/A}_{\{\pm, \mp\}} & \chi^{S/A}_{\{\pm, \pm\}} \\
\end{pmatrix} - im \begin{pmatrix}
  \chi^{S/A}_{\{\pm, \mp\}} \\
  \chi^{S/A}_{\{\pm, \pm\}} \\
  \chi^{S/A}_{\{\pm, \mp\}} \\
  \chi^{S/A}_{\{\pm, \pm\}} \\
\end{pmatrix} = 0.
\]

The exotic operator \(i\gamma^\mu \nabla_\mu + i\gamma^\mu \partial_\mu \theta \pm m \mathbb{I}\) annihilates each of the four exotic Dirac spinor fields used to construct \(\chi^{S/A}_{\{\pm, \mp\}}(x)\), as prescribed by the standard Dirac dynamics. However, since the operator in (3) couples the \(\{\pm, \mp\}\) degrees of freedom \(\mathbb{I} = 1\), the modified exotic Dirac operator does not annihilate ELKO fields. By observing the off-diagonal nature of the mass term in Eq. (3) one should notice the differences from a phenomenological off-diagonal Majorana mass term introduced in the context of the Dirac equation \(\mathbb{I} = 1\).

Since the prerequisites for the ELKO dynamics are established \(\mathbb{I} = 1\), we drive our attention to the procedure for obtaining the corresponding effective dispersion relation derived from the exotic Dirac operator. By analogy with the relativistic quantum mechanics terminology, we shall discuss whether the exotic Dirac operator can be considered as a square root of the Klein–Gordon operator — in the sense that \((i\gamma^\mu \nabla_\mu + i\gamma^\mu \partial_\mu \theta - m \mathbb{I})(i\gamma^\mu \nabla_\mu + i\gamma^\mu \partial_\mu \theta + m \mathbb{I}) = (g^{\mu\nu} \nabla_\mu \nabla_\nu + m^2)\mathbb{I}\). This feature must remain true for the 5LKO and its exotic partner:

\[
((i\gamma^\mu \nabla_\mu + i\gamma^\mu \partial_\mu \theta)\delta_\alpha^\beta \pm m \mathbb{I}\delta_\alpha^\beta)((i\gamma^\mu \nabla_\mu + i\gamma^\mu \partial_\mu \theta)\delta_\alpha^\beta \pm m \mathbb{I}\delta_\alpha^\beta) = (g^{\mu\nu} \nabla_\mu \nabla_\nu + m^2)\delta_\alpha^\beta,
\]

since the introduction of an exotic spin structure does not modify the Klein–Gordon propagator fulfillment by dark spinor fields. The corresponding Klein-Gordon equation for the exotic ELKO field is hence provided by

\[
(\Box + m^2 + g^{\mu\nu} \nabla_\mu \nabla_\nu \theta + \partial^\mu \theta \nabla_\mu + \partial^\mu \overline{\theta} \partial_\mu \theta)\lambda(x)_{\{\pm, \mp\}}^{S/A} = 0.
\]

This equation can reproduce the same Klein-Gordon propagator for standard and exotic ELKO as well. For the exotic case, it demands the constraint

\[
(\Box \theta + \partial^\mu \theta \nabla_\mu + \partial^\mu \overline{\theta} \partial_\mu \theta)\lambda(x)_{\{\pm, \mp\}}^{S/A} = 0
\]

which can be formulated without restricting the theory to any particular condition as those assumed in \(\mathbb{I} = 1\).

III. THE EXOTIC TERM IN THE VSR FRAMEWORK

Instead of assuming the constraint given by Eq. (5) howsoever, one can suppress the effective mass term \(m\) from the formalism, by assuming the exotic Dirac operator

\[
i\gamma^\mu \nabla_\mu = i\gamma^\mu (\nabla_\mu + \partial_\mu \theta).
\]

Accordingly, it could be straightforwardly embedded into the framework of the VSR, when the exotic term \(\partial_\mu \theta(x)\) is identified with a dynamical preferential direction vector \(\phi(x)v_\mu\), where \(\phi(x)\) is a scalar field with mass-dimension equal to one. Thereafter obtaining the (preliminarily) massless Klein-Gordon equation from Eq. (6) as

\[
(\Box + g^{\mu\nu} v_\mu v_\nu \phi^2 + g^{\mu\nu} v_\mu \partial_\nu \phi + v^\mu \phi \nabla_\mu)\lambda(x)_{\{\pm, \mp\}}^{S/A} = 0,
\]

one can investigate some constraints on the preferential vector \(v_\mu\).

In order to shed some new light on the character of the exotic function \(\theta(x)\) in terms of \(\phi(x)\), let us identify the scalar field \(\phi\) with the kink solution of the \(\lambda \phi^4\) theory. The re-scaled Lagrangian density for the scalar field of the \(\lambda \phi^4\) theory has the form

\[
\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - s^2 \frac{\lambda}{4} (\phi^2 - \frac{m^2}{\lambda})^2,
\]

for which \(m\) is the mass of the scalar field, \(\lambda\) denotes the dimensionless coupling parameter, and \(s^2 = g_{\mu\nu} a^{\mu\nu} a^{\mu\nu}\), with \(a^{\mu\nu} = v^{\mu} \sqrt{\frac{1}{\lambda} - \frac{\phi^2}{\lambda} + \phi^4}\). The tensor \(a^{\mu\nu}\) is assumed to be anti-symmetric and \(u_\mu\) is an unitary quadri-velocity \((u^2 = g_{\mu\nu} u^\mu u^\nu = 1)\). The corresponding equation of motion yields

\[
\Box \phi = \left(\frac{d^2}{dt^2} - \nabla^2\right) \phi = s^2 (m^2 \phi - \lambda \phi^3),
\]
and the re-scaled kink solution can be written as
\[ \phi_s(x) = \frac{m}{\sqrt{2}} \tanh \left( \frac{m}{\sqrt{2}} q \right), \]  
with \( q = s^\mu x_\mu \).

Substituting the kink solution above into the ansatz relation \( \partial_\mu \theta(x) = \phi(x) v_\mu \), one forthwith finds that
\[ \theta(x) = \log \left[ \cosh \left( \frac{m}{\sqrt{2}} q \right) \right]. \]
Therefore one can compute immediately
\[ \partial^\mu \partial_\mu \theta + \Box \theta = \frac{m^2}{2} s^2 \tanh[q^2] + \frac{m^2}{2} s^2 (1 - \tanh[q^2]) = \frac{m^2}{2} s^2. \]
Since \( h^{\mu\nu} \) is an anti-symmetric tensor, one should notice that \( u_\nu h^{\mu\nu} u_\mu = 0 \). One can thus parameterize the ELKO spinor field quadri-momentum \( p_\mu \) by \( p_\mu = \mu u_\mu \) in order to have
\[ \partial_\mu \theta(x) \nabla^\mu \lambda^{S/A}_{\{\pm, \bar{\tau}\}}(x) \propto u_\nu h^{\mu\nu} u_\mu = 0. \]
The results from Eqs. \([12,13]\) substituted into Eq. \([7]\) lead to
\[ \left( \Box + \frac{m^2}{2} s^2 \right) \lambda^{S/A}_{\{\pm, \bar{\tau}\}}(x) = 0, \]
which is typically the KG equation for a massive particle for which the dispersion relation would be given by \( p^\mu p_\mu = (m^2 s^2)/2 \). The result above eliminates the constraint given by Eq. \([5]\) and reproduces the dynamics of the KG equation with a dynamical mass given by \( \mu = ms/\sqrt{2} \).

IV. CONCLUDING REMARKS

The VSR dynamical mass generation mechanism that we have suggested exactly reproduces the dispersion relations of SM fields, making the mechanism consistent with the VSR proposal. It indeed emulates the conditions for generating dynamical masses that emerge in the context of dark matter coupling to dark energy intermediated by scalar fields \([34,37]\). Obviously, additional and natural questions may arise in a systematic formulation of quantum field theories carrying VSR symmetries \([23]\). The main outstanding exotic dark spinor field feature is that it can be indeed considered in a variety of problems, wherein SM spinor fields cannot. Observational aspects on such a possibility have been proposed at LHC, where ELKO dark matter fields signatures can be elicited, at center of mass energy around 7 TeV. It robustly indicates the number of events that stimulates more specific analysis about the ELKO particle at high energy experiments \([35]\). ELKO dark matter fields are manifestly non-local, although they present locality when the field propagation is along the preferred axis \([17,23,33,40]\). Such axis can be chosen as the dynamical preferential direction \( v_\mu \), provided by the exotic term. Inmate difficulties to formulate a complete QFT for ELKO may be circumvented in our formalism, since such choice makes the ELKO a local field.

Any attempt to construct an appropriate QFT describing ELKO fermionic fields must accomplish their unexpected and interesting properties: non-locality, the existence of an inherent preferred axis (along which ELKO is local), mass dimension one, as well as the Lorentz symmetry-breaking provided by the ELKO dynamics \([6,17,23,39,40]\). The VSR has been evinced as a paramount promising arena to develop such still lacking theory \([23]\). Furthermore, such formalism can be investigated in a Hopf algebras scenario, considering a state-space with symmetries of the Poincaré group. One uses the deformed Hopf algebras framework to construct an event-space with symmetries of the SIM(2) VSR group, in close analogy to the results already accomplished for the E(2) VSR group \([41,42]\).

The ELKO dark spinor fields characterization is obtained through the topologically impelled introduction of an additional term \( i\gamma^\mu \partial_\mu \theta(x) \) in the Dirac operator, that cannot be absorbed by any external gauge field. Even acting effectively in producing the exotic dispersion relation that we have obtained, modifications like \( i\gamma^\mu \partial_\mu \theta(x) \rightarrow i\gamma^\mu \partial_\mu (\theta(x) + \beta(x)) \) with \( \partial_\mu \theta(x) \partial^\mu \beta(x) = 0 \), besides contributing to the dynamical mass term, can provide the preliminary conditions for the constraint on the metric spacetime structure, that emerges through the physical assumption that the exotic dark spinor fields satisfy the Klein-Gordon propagator for massive particles. Therefore, our results heretofore assert that all the quantum field theoretical structure, that seems to be most suitable for describing dark matter, are maintained through the constraints previously applied to \( \theta(x) \), when they are applied to \( \beta(x) \). Reverbating some previous conclusions, it means that the VSR reflects symmetries associated with rods and clocks for dark matter in the same way that theory of special relativity does for SM fields \([23,43]\).
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