Role of convection–circulation coupling in the propagation mechanism of the Madden–Julian Oscillation over the Maritime Continent in climate models

Yi-Chi Wang¹, Wan-Ling Tseng¹*, Huang-Hsiung Hsu¹

¹Research Center for Environmental Changes, Academia Sinica, Taipei, Taiwan

Corresponding author: Wan-Ling Tseng (wtseng@gate.sinica.edu.tw)

Abstract

This study investigates the role of convection–circulation coupling on the simulated eastward propagation of the Madden–Julian Oscillation (MJO) over the Maritime Continent (MC). Experiments are conducted with the European Centre Hamburg Model Version 5 (ECHAM5) coupled with the one-column ocean model – Snow-Ice-Thermocline (SIT) and two different cumulus schemes, Nordeng (E5SIT-Nord) and Tiedtke (E5SIT-Tied). During the early phase of MJO composites, the E5SIT-Nord simulation reveals stronger intraseasonal anomalies in the apparent heat source ($Q_1$) over the convective center, however, the E5SIT-Tied produces a stronger background $Q_1$, suggesting that deep convection prevails over the MC but does not couple with the MJO circulation. Similarly, in the E5SIT-Tied simulation, in-column moisture is kept mostly by local deep convection over the MC, which is in contrast to the well-correlated relationship between moisture anomaly and MJO circulation in E5SIT-Nord. A case study based on an observational MJO reveals similar biases concerning of convection–circulation coupling emerges within a few
days of simulations. The E5SIT-Tied simulation produces weaker heating at the convective center of the MJO than the E5SIT-Nord a few days after model initiation, resulting weaker subsidence to the east and less favorable for propagation. The present findings highlight the instantaneous responses of cumulus parameterization schemes to MJO-related environmental changes can further affect intraseasonal variability through altering convection–circulation coupling over the MC. Physical schemes of moist convection are essential to realistically represent this coupling and thereby improve the simulation of the eastward propagation of the MJO.

**Keywords:** MJO, Convection Scheme, Low-Level Moistening, Climate Models
1 Introduction

The Madden–Julian Oscillation (MJO) is the dominant pattern of atmospheric intraseasonal variability in the tropics (Madden and Julian 1972; Zhang 2005; Jiang et al. 2019). Numerous observational and modeling studies have explored the fundamental physics regarding the eastward propagation and development of the MJO, including the interaction with the frictional boundary layer (Wang and Rui 1990; Hendon and Salby 1994; Maloney and Hartmann 1998; Hsu et al. 2004; Kang et al. 2013), convective intraseasonal air–sea interactions (Flatau, 1997; Waliser et al. 1999), ocean surface flux (Maloney and Sobel 2004; Maloney 2009; Kiranmayi and Maloney 2011; Andersen and Kuang 2012), moisture transport by cumulus (Benedict et al. 2007; Jiang et al. 2016, 2017), and air–sea interaction (DeMott et al., 2015, 2019). Despite the considerable progress in state-of-the-art general circulation models (GCMs) in recent decades, realistic simulations of the MJO remain difficult.

One challenge to improving models is the MJO is organized by strong coupling between MJO circulations, convection, and ocean thermodynamics. Studies have addressed numerous crucial physical processes for reproducing the MJO in GCMs, including the mean state (Kim et al. 2011; Kim et al. 2017; Jiang et al. 2018; Klingaman et al. 2020), convection simulated by cumulus parameterization schemes (CPS; Liu et al. 2005; Deng and Wu 2010; Zhou et al. 2012), convectively coupled tropical waves (Kiladis et al. 2005; Janiga et al. 2018), ocean–atmosphere interaction (Tseng et al. 2015; DeMott et al. 2015, 2019), the diurnal cycle of sea surface temperature (SST; Bernie et al. 2005; Klingaman et al. 2011), and cloud radiative feedback (Ciesielski et al. 2017; Del
Genio and Chen 2015; Jiang et al. 2011). These findings jointly reflect the complexity of
the physical processes involved in understanding and simulating the MJO.

To untangle this multifaceted problem, all coupling mechanisms must be carefully
examined. One key aspect of the MJO behavior manifested of such coupling is MJO’s
eastward propagation from the Indian Ocean to the Maritime Continent (MC) and onward
to the western Pacific (Zhang 2005). The eastward propagation of the MJO over the MC
has been challenging to simulate in GCMs (Zhang 2005) and remains so in the Coupled
Model Intercomparison Project Phase 6 models (CMIP6; Ahn et al. 2020). After the MJO
appears over the Indian Ocean, deep convection in the oscillation induces the dynamic
processes associated with the equatorial wavelike perturbations to the east over the MC,
further enhancing both low-level moisture convergence and moistening (Zhang 2005;
Jiang et al. 2020). Observational studies have suggested that the shallow convection with
bottom-heavy heating profiles that occurs before the propagation of the MJO convective
center helps precondition the development of deep convection (Kemball-Cook and Weare
2001; Kikuchi and Takayabu 2004). Such shallow convection that is associated with low-
level convergence and ascending motion moistens the lower troposphere and enhances
coupling with intraseasonal perturbations (Lappen and Schumacher 2014; Benedict and
Randall 2001). In a model experiment with prescribed heating profiles, Lappen and
Schumacher (2014) also demonstrated the essential role of the low-level heating in the
development and maintenance of the MJO.

Multiple studies have also reported that including air–sea coupling aids MJO
simulation in climate models (Tseng et al. 2015; Jiang et al. 2015; DeMott et al. 2018;
DeMott et al. 2019; Jiang et al. 2019). Crueger et al. (2013) explored the role of CPS,
ocean coupling, and model resolution by evaluating the simulation of the MJO with the
European Centre Hamburg Model (ECHAM) Version 6 under various configurations.
They have found that CPS plays an essential role in simulating MJO signatures, along
with ocean coupling. The researchers attributed the discrepancy to differences in the
sensitivity of the two CPS to tropospheric moisture (Crueger et al. 2013). However, they
did not discuss the role of convection-circulation coupling in their analysis. By jointly
using the ECHAM5 and their self-developed one-column ocean model, the Snow–Ice–
Thermocline (SIT) model, Tseng et al. (2015) successfully simulated the eastward
propagation of the MJO, observing that the low-level moisture convergence prior to the
active MJO phase over the MC played a pivotal role in preconditioning the propagation
of deep convection and circulation. The warmer SST ahead of the MJO was suggested to
destabilize the boundary layer and enhance frictional convergence, underscoring the
importance of shallow moistening for the further development of the MJO. Comparing
between models, Jiang et al. (2015) reported that the ECHAM5-SIT model was one of
the best GCMs in MJO simulations. In another study, that model was used to determine
the role of air–sea coupling in MJO simulations (DeMott et al. 2019). Although both
studies have evaluated the performance of the model in simulating the MJO, the
contribution of convection has not been addressed. Thus, the key mechanism underlying
convection–circulation coupling, which may improve MJO simulations, remains unclear.

To examine the role of convection in the mechanism of MJO propagation over the
MC with better representation of air–sea coupling, the model setup described by Tseng et
al. (2015) is used to analyze the convection–circulation coupling in the ECHAM5 model
experiments with two CPSs, namely the Nordeng scheme (E5SIT-Nord) and the Tiedtke
scheme (E5SIT-Tied). The same setup for modeling ocean coupling of SIT was used.
Using the model setup for better air–sea coupling as the basis, we investigated the role of convection–circulation coupling played in the key mechanisms for better simulating the eastward propagation of MJO in GCMs with CPS. In this study, we adopted the budget analysis of apparent heat sources ($Q_1$) and apparent moisture sinks ($Q_2$), as well as the moist static energy (MSE) budget, to the 25-year climate simulations of two model setup, with the central aim of identifying the contribution of the moisture buildup over the MC in the propagation of the MJO. To further clarify the effects of the representation of CPS on MJO propagation, we conduct a case study by using the initial conditions from the ERA-Interim reanalysis and examining the MJO evolution simulated by the two CPSs. By observing how the model biases evolve in case study provides more information about how biases in climate runs may link to the fast physics from CPS related to convection–circulation coupling. The remainder of this paper is organized as follows. The data, model, and methodology are described in Section 2. Sections 3 and 4 present the analytical results and the results from the case study, respectively. The discussion and conclusion are in Sections 5 and 6, respectively.

### 2 Data, models, and methodology

In the present study, the ECHAM5 (Roeckner et al. 1989) is used in combination with the SIT (Tu and Tsuang 2005; Tsuang et al. 2009). As its name implies, the ECHAM5 is the fifth version of the ECHAM, a GCM developed at the Max Planck Institute for Meteorology. The horizontal resolution used is T63 (~1.8°), with 31 vertical layers and a model top at 10 hPa (approximately 30 km). SIT simulates the SSTs and variability in upper ocean temperature, including that attributable to the cool-skin and diurnal warm-layer effects in the upper ocean. The turbulent kinetic energy (Gaspar et al.
of a water column is also simulated. In our experiments, SIT has 42 vertical layers, 12 of which are in the upper 10 m. In one study (Tu and Tsuang 2005), the SIT, with a 1-m resolution in the upper 10 m and a layer at 0.05 mm for reproducing the cool-skin effects at the ocean surface, realistically simulated the near-surface warm layer (Tu and Tsuang 2005). It is not conventional to combine such a high-vertical-resolution ocean model of turbulent kinetic energy to an atmospheric GCM (AGCM). To account for horizontal processes, the ocean model is weakly nudged (with a 30-day time scale) to the observed climatological ocean temperature at depths exceeding 10 m. The SIT and ECHAM exchange SST and surface fluxes at every time step (12 min) in the tropics (30° S–30° N). Elsewhere, climatological SST drives the AGCM.

Two CPS used in the present study are the Nordeng scheme, the default scheme used in the ECHAM5 (Nordeng 1994), and the Tiedtke scheme (Tiedtke 1989). The Nordeng scheme, an improved version of the Tiedtke mass flux convection scheme, considers organized entrainment and detrainment in buoyancy-related penetrative convection (Nordeng 1994). The differences between the two schemes lie mainly in the representation of deep convection regimes, particularly closures and entrainment rates (Möbis and Stevens 2012). For closures, the Tiedtke scheme uses the moisture convergence within the subcloud layer to make approximation for convective intensity (Tiedtke 1989). By contrast, the Nordeng scheme uses the quasi-equilibrium closure for the relaxation of the vertically integrated buoyancy (Nordeng 1994). For the entrainment rate, the Nordeng scheme uses additional lateral mixing; specifically, the buoyancy-driven entrainment for deep convection is included in the organized entrainment module (Nordeng 1994).
In the present study, the simulation results are analyzed using data from the Global Precipitation Climatology Project (Adler et al. 2003), data on outgoing longwave radiation and daily SST from the National Oceanic and Atmosphere Administration (Banzon et al. 2014), and atmospheric states from the ERA-Interim reanalysis (Dee et al. 2011). The simulation diagnostics package developed by the Climate Variability and Predictability MJO Working Group (CLIVAR Madden–Julian Oscillation Working Group 2009) and a 20-to-100-day filter are used to isolate and determine intraseasonal variability. The MJO phases are classified on the basis of the MJO index—that is, the leading pair of principal components from an empirical orthogonal function analysis of intraseasonal outgoing longwave radiation, under zonal winds of 850 and 200 hPa (Wheeler and Hendon 2004). Because of the strong eastward propagation tendency of the MJO, the analysis is centered on the boreal cool season (November to April). The total simulation length of each experiment is 25 years, with data in the last 24 years subjected to analysis.

To understand the simulated convection, we calculate the $Q_1$ and $Q_2$ associated with the MJO (Yanai et al. 1973), which are presented in the following equations:

\[
Q_1 \equiv \frac{\partial \bar{s}}{\partial t} + \mathbf{v} \cdot \nabla \bar{s} + \frac{\partial \bar{s}}{\partial p} = Q_R + L_v (\bar{c} - \bar{e}) - \frac{\partial}{\partial p} \bar{s} \omega' ^2 \\
Q_2 \equiv -L_v \left( \frac{\partial \bar{q}}{\partial t} + \mathbf{v} \cdot \nabla \bar{q} + \frac{\partial \bar{q}}{\partial p} \right) = L_v (\bar{c} - \bar{e}) + L_v \frac{\partial}{\partial p} \bar{q} \omega'
\]

where $c$ and $e$ represent condensation and evaporation, respectively; $q$ is the water vapor mixing ratio; $s$ is the dry static energy ($s = cpT + gz$); and $L_v$ is the latent heat of vaporization. As for $(\bar{\cdot})$, it denotes the grid scale quantity relative to the subgrid components. For the convection-dominated regions, convective activities could be inferred by comparing the $Q_1$ and $Q_2$ vertical profiles to reflect the vertical transport of
the MSE by convection. For example, deep convection regimes often have top-heavy $Q_1$ vertical profiles with peaks at approximately 300 hPa and $Q_2$ profiles with peaks at 700 hPa, indicative of upward convective transport from the lower troposphere (Yanai et al. 1973). By contrast, $Q_1$ vertical profiles in shallow convection regimes tend to be bottom-heavy, with peaks at lower atmospheric pressures (Nitta and Esbensen 1974).

The vertically integrated MSE budget is defined as follows:

$$
\langle \frac{\partial h}{\partial t} \rangle' = -\langle u \frac{\partial h}{\partial x} \rangle' - \langle u \frac{\partial h}{\partial y} \rangle' - \langle \omega \frac{\partial h}{\partial p} \rangle' + \langle LW \rangle' + \langle SW \rangle' + \langle LHF \rangle' + \langle SHF \rangle'
$$

where $h$ is the MSE ($h = cpT + gz + Lq$); $u$ and $v$ are the zonal and meridional velocities, respectively; $\omega$ is the vertical pressure velocity; $LW$ and $SW$ are the longwave and shortwave radiation fluxes, respectively; and $LHF$ and $SHF$ are the latent and sensible surface heat fluxes, respectively. The mass-weighted vertical integration from the surface to 200 hPa is denoted by $\langle \cdot \rangle$, and intraseasonal anomalies are represented by $\langle \cdot \rangle'$. All fields are isolated using a 20-to-100-day band-pass Lanczos filter (Duchon 1979).

3 ECHAM-SIT simulations of the MJO

The simulations of the MJO in two experiments involving the E5SIT-Nord and E5SIT-Tied are examined in this section. Figure 1 (a–c) presents the wavenumber–frequency spectra of simulated 850-hPa zonal winds. The E5SIT-Nord realistically simulates the 30-to-80-day eastward-propagating signals of planetary wavenumber 1 (Fig. 1b), which is consistent with the finding of Tseng et al. (2015). By contrast, the spectra of the E5SIT-Tied simulation (Fig. 1c) exhibit weaker signals over wavenumber 1. The remaining parts of the figure (1d–1f) illustrate the between-simulation differences in the eastward propagation of intraseasonal fluctuations under precipitation and 10-m zonal winds. The E5SIT-Nord simulation reproduces the distinctly observed eastward
propagation, albeit slightly more slowly, of precipitation and surface winds (Fig. 1e), whereas the E5SIT-Tied simulation presents weak intraseasonal fluctuations in precipitation which is decoupled from zonal winds at the MC (i.e., 120°–150° E). Therefore, our analysis focuses on the convection–circulation coupling associated with MJO over the MC region.

The mean states of zonal winds and precipitation rate are shown in Fig. S1, and maps of the ratio of the intraseasonal rainfall variability to the total rainfall variability are presented in Fig. S2. In line with the results of Tseng et al. (2015), the two model simulations have relatively similar mean states (Fig. S1). Both models simulate a higher ratio of intraseasonal rainfall variability to total variability than was observed (shaded area in Fig. S2), with the E5SIT-Nord model simulating the highest variability among the three datasets. By contrast, the variability simulated by the E5SIT-Tied model is weaker than what was observed. While the contribution of the mean distribution of low-level moisture to MJO propagation has been emphasized in numerous studies (e.g., Jiang 2017), it appears not to be a major factor in our simulations, considering, as shown in Fig. S3 (a–c), the dryer mean state of the E5SIT-Nord simulation (relative to the E5SIT-Tied simulation), especially below 700 hPa (Fig. S3d). An examination of model pattern correlations with ERA-Interim (from 1000 to 200 hPa) also reveals that both models effectively simulate distributions of horizontal moisture; the coefficient of correlation in the both runs exceeds 0.95 (Fig. S3e). Although the mean moisture pattern appears comparable, the convective processes that result in more accurate simulation of MJO propagation by the E5SIT-Nord are worthy of further exploration.

The evolution of essential atmospheric variables for the initiation and development of convection over the MC (10° S, 120°–150° E) are plotted with respect to the MJO life
cycle in Fig. 2. All variables underwent 20-to-100-day band-pass filtering and are plotted against the simulated MJO phases, per the procedures of Wheeler and Hendon (2004). Figure 2 (a–c) shows the moisture convergence associated with the simulated MJO phases. The low-level convergence over the MC is the strongest below 850 hPa in phases 1 and 2, and it continues shifting upward into the free troposphere starting from phase 3 (Fig. 2a). Both simulations capture the structure of low-level moisture convergence in the first two phases, but at smaller magnitudes. As shown in Fig. 2 (b–c), the simulated moisture convergence shifts to the free troposphere relatively quickly between phases 3 and 4 and becomes detached from the boundary layer. Moisture convergence is stronger and extends to higher levels in the E5SIT-Nord simulation than in the E5SIT-Tied simulation. The associated $Q_1$ and $Q_2$ over the MC region are also observable in Fig. 2 (d–f and g–i, respectively). E5SIT-Nord has a sharp contrast between convective heating and cooling during the MJO life cycle that is greater in amplitude than that in the E5SIT-Tied simulation and in the observation data. Consistent with the wave spectrum signals in Fig. 1, the magnitudes of $Q_1$ and $Q_2$ in the E5SIT-Tied simulation are substantially weaker than those in the E5SIT-Nord simulation. Notably, the observed $Q_2$ exhibits a distinct tilt, and both models simulate a rapid transition from the near-surface features to the deep convective structure in the middle troposphere. Figure 2 (j–l) presents the evolution of the MSE profiles over the MC associated with MJO phases. The vertical development of the MSE, specifically through the upward transport of moisture from the near-surface to the low-level troposphere, results in conditions conducive to deep convection (Fig. 2j). The E5SIT-Nord simulates the gradual upward development of MSE with time, whereas the E5SIT-Tied (Fig. 2k, l) simulates weak preconditioning with an unstable near-surface layer, followed by the sudden onset of high MSE and deep convection in mature phases.
As noted by Tseng et al. (2015), this moistening process, characterized by the tilting of MSE, was only captured when the ECHAM5 was used in concert with the SIT.

As tropical convection has a multiscale nature, convective activities on other time scales can affect MJO-related convection development. Figure 3 presents the unfiltered $Q_1$ and $Q_2$ in eight MJO phases, corresponding to the intraseasonal ones shown in Fig. 2 (d–i). In the reanalysis, the $Q_1$ and $Q_2$ profiles (Fig. 3a, d) reveal the evolution of the convective activities in the MJO, from the shallow convection in the earlier phases to the deep convection in the mature phases. Both models simulate heating or moistening over all phases that are stronger in magnitude than their observed counterparts. In the E5SIT-Nord experiment, the simulated $Q_1$ exhibits heating during the mature phases that is comparable to its observed counterpart; however, in phase 4, heating is greatly overestimated by as much as 4 K/day (Fig. 3b). By contrast, in the E5SIT-Tied experiment, $Q_1$ heating persists from phase 3 to phase 8 (Fig. 3c). Notably, the mean $Q_1$ in the E5SIT-Tied simulation is larger than that in the E5SIT-Nord simulation when averaged over the entire MJO life cycle, the opposite of the $Q_1$ projection on the intraseasonal time scale (Fig. 2). Unlike the prominent $Q_1$ associated with MJO convective center in the observation data and the E5SIT-Nord simulation, the $Q_1$ heating in the E5SIT-Tied simulation persists from phases 1 to 8 of the MJO, demonstrating the maintenance of deep convection over the MC. This result and its relationship with lower simulation skill of MJO is explored in later sections.

We focus on the convection activities over the MC during phases 1 and 2 of the MJO, when the deep convection center is over the Indian Ocean. Figure 4 shows the $Q_1/Q_2$ profiles over 10° S and 120°–150° E during these phases in the ERA-Interim analysis, in the E5SIT-Nord simulation, and in the E5SIT-Tied simulation. In phase 1, the peak of $Q_1$
in the reanalysis exhibits relatively homogeneous heating at a maximum rate of 1 K/day, suggesting a relative clear atmosphere with radiative heating and shallow convective heating dominate $Q_1$ (red line in Fig. 4a). The $Q_2$ profile peaks at 700 hPa, indicating drying within the planetary boundary layer (PBL) and moistening in the lower troposphere. Such profiles suggest that during this period, moisture is transported from the PBL to the lower troposphere over the MC (blue line in Fig. 4a) through bottom-heavy convection. In the E5SIT-Nord, during phase 1, the $Q_1$ value peaks at approximately 700 hPa, with a bottom-heavy profile. At the same time, the $Q_1$ and $Q_2$ peaks correspond to each other, implying that convection is shallow at this point, mainly moistening the low-level troposphere (Fig. 4b). By contrast, in the E5SIT-Tied simulation, the $Q_1$ and $Q_2$ profiles peak near 500 and 700 hPa, respectively, suggesting deep, intense convection over the MC (Fig. 4c). As shown in Fig. 4 (d–f), deep convective heating at approximately 500 hPa is higher in phase 2 in both the ERA-Interim analysis and the two simulations. As is the case in phase 1, heating is deeper and more intense in the E5SIT-Tied simulation than in the E5SIT-Nord simulation or the ERA-Interim reanalysis.

Figure 5 shows the MJO structures in phases 1 and 2, with overturning circulation indicated by vectors with $Q_1$ (shading) and moisture convergence (green contours). The shaded area and the contours of the horizontal maps represent the precipitation and sea level pressure, respectively (bottom panel in Fig. 5). In phases 1 and 2, the MJO precipitation is concentrated over the central Indian Ocean (around 80°–90° E), with a strong upward trend. At the same time, subsidence is considerable over the MC—specifically, in a region characterized by low-level moisture convergence (around 120°–150° E; Fig. 5a). During this phase, E5SIT-Nord simulates strong subsidence and low-level moisture convergence over the MC and low-level easterlies over the eastern Indian
Ocean (Fig. 5b). By contrast, E5SIT-Tied simulates very weak subsidence and easterlies over the MC and the eastern Indian Ocean, respectively, indicating weak convection–circulation coupling.

Figure S4, which presents an analysis of the MSE budget over the MC (10° S, 120°–150° E, spanning the area from the Banda Sea to the Maluku Islands and Java) during phases 1 and 2, elucidates the differences between the two simulations and the ERA-Interim reanalysis. Among the budget terms in E5SIT-Nord, those concerning horizontal and vertical advection terms contribute positively to the tendency term, which is partially cancelled out by longwave radiation. By contrast, the E5SIT-Tied simulates less vertical advection and very weak negative horizontal advection. The cancellation by longwave radiation results in an almost negligible tendency. The principal differences between the E5SIT-Nord and E5SIT-Tied simulations appears to be in the horizontal advection term and vertical advection terms, which further result in the poorer ability of E5SIT-Tied to simulate the propagation of the MJO. In phase 2, differences in horizontal advection that become the dominant term in the MSE budget increase as convection moves closer to the MC (Fig. S4b). Although the budget terms computed from the reanalysis have large MSE residuals, as in previous studies (Kiranmayi and Maloney 2011; Jiang 2017), vertical and horizontal advection likely to be crucial contributors to MSE tendency; this is highly consistent with that calculated from the E5SIT-Nord simulation.

To further visualize the coupling of moisture buildup and the MJO over the MC, we examine the large-scale circulation patterns and thermodynamics during periods when the moisture buildup over the MC is the most substantial. We first define intraseasonal moisture buildup by characterizing the duration of moisture residence in the tropospheric column before removal through rain (\(\int_{p_B}^{p_T} q dp \div [P]\)) over the southern MC (10° S–10° N,
120°–150° E), where [-] is the intraseasonal filtering, \( q \) is moisture, \( P \) is the rain rate, \( p_T \) is the pressure at the cloud top, and \( p_B \) is the pressure at the cloud bottom. The normalized convective time scale over the southern MC are calculated with respect to the lag-regressed fields to RMM1 index with ERA-Interim and two model runs in Figure S5. In ERA-Interim, convective time scale over the MC increases gradually from phase 1 (i.e., \(-20\) days), reaching the maximum in phase 2 (i.e., \(-12\) days; green line in Fig. S5), indicating moisture buildup peaks around 10 days before the deep convection activity on day 0 and under dominant shallow convection (from \( Q_2 \) in Fig. 2). Figure 6 presents the regressed structure of the \( Q_2 \), MSE, and wind fields on the time series of accumulation (Fig. S5) in the ERA-Interim reanalysis, E5SIT-Nord simulation, and E5SIT-Tied simulation. A distinct feature of MJO with convective center at the Indian ocean and dynamical responses are shown in both the reanalysis and the E5SIT-Nord simulation. Notably, a realistic structure similar to Kelvin waves with two off-equatorial MSE maxima over the eastern Indian Ocean under strong easterlies at the equatorial MC is present only in the E5SIT-Nord simulation. On the other hand, the missing of the deep convection signal over the east Indian Ocean and west MC are shown in the E5SIT-Tied run (Fig. 6c). Also in reanalysis and E5SIT-Nord, the zonal-height cross-section exhibits a tilted structure of well-collocated MSE and \( Q_2 \), which depicts a MJO structure in the developing phase (at approximately phase 2) (Fig. 6a, b). The tilted structure involves deep convection near 90° E, relatively shallow convection at 120° E, and low-level moistening by convective processes between 120° E and 150° E. The \( Q_2 \) tilt in the E5SIT-Nord is more rapid than that in the ERA-Interim reanalysis (as indicated by blue contours in the right panels of Fig. 6a, b). Such westward-tilting vertical structures have been identified in numerous observational studies (Kiladis et al. 2005; Kim et al. 2009; Tseng...
et al. 2015; Jiang et al. 2015). By contrast, the E5SIT-Tied simulation reveals local deep convection and a MSE maximum over the MC (120°–150° E), implying the MSE anomaly over MC couple only with local convection activity, not with the large-scale circulation patterns that are further linked to deep convection in the Indian Ocean. The meridional cross-section over 120°–150° E also indicates the anomalies in the deep $Q_2$ and the MSE over the MC in the E5SIT-Tied simulation (Fig. S6). By contrast, both the E5SIT-Nord simulation and the ERA-Interim reanalysis exhibit a shallower $Q_2$ and MSE structure, with the maximum at approximately 800 hPa. As in the ERA-Interim reanalysis and the E5SIT-Nord simulation, this is a precondition for the development of deep convection over the MC and the eastward propagation of the MJO when convection is still over the Indian Ocean.

The characteristics of convective moistening (i.e., $Q_2$) to rainfall categories and SST are presented as follows to investigate the impacts of convective process on environments. Figure 7 shows the $Q_2$ profiles stratified by the daily rain rate averaged over the tropical oceans (10° S–5° N, 80°–160° E) in the two model runs and the reanalysis. For low rain rates, the E5SIT-Nord simulates a more bottom-heavy $Q_2$ profile than the E5SIT-Tied does, causing greater moistening in the PBL. For high rain rates, E5SIT-Nord accurately simulates stronger drying (more latent heating) in the middle troposphere associated with strong convective activity. The two characteristics (i.e., stronger low-level moistening and stronger deep drying) of the E5SIT-Nord simulation help create more favorable environmental conditions for the propagation of the MJO. Figure 8 shows the percentage of rainfall occurrences stratified with respect to SST and rainfall intensity. The highest rainfall is noted between 28°C and 30°C (Fig. 8a, b) in both the observation and the
E5SIT-Nord simulation. By contrast, the E5SIT-Tied simulates more frequent rainfall when the SST is higher than 30°C, suggesting that the presence of convection does not allow for the simulation of a proper rainfall–SST relationship. As shown in Fig. 8c, the E5SIT-Tied tends to be overresponsive to high SST, producing an excessive amount of local convective rainfall.

4 Case study on the MJO involving two CPSs

The difference in the representation of convection–circulation coupling in the two simulations may not be directly ascribable to the representation of the convective processes in the CPS. To examine the relationship between the instantaneous convective response to the MJO circulation and convection–circulation biases found in climate runs, we conduct a simulation of an MJO case, using initial conditions from the ERA-Interim reanalysis. Having the setup of the two schemes, the simulation is initiated at the start point of October 31, 2011, when a well-developed MJO is observed over the Indian Ocean. The two experiments are then integrated for 3 days and analyzed for their differences in days 1 and 2. This setup is designed to compare the response of moist convection processes and ensure that the large-scale circulation patterns remain close to the initial conditions. The diagnostics are useful for understanding the biases caused by the model representation of convective processes from diurnal to interannual time scales (Ma et al. 2021).

Figure 9 shows the differences in circulation patterns and sea level pressure between the two simulations, in the form of a height–longitude cross-section and horizontal maps, on the first and second days after model initiation. On day 1, the convection center of the MJO is over the tropical Indian Ocean (near 90° E), with weak subsidence in the east over
the MC and the western Pacific. After 1-day integration, the E5SIT-Nord simulation produces (1) stronger upward motion associated with convective center at 90° E and (2) a stronger basin-wide subsidence over the MC and the western Pacific from 120° E to 180° E (Fig. 9a). In accompany with circulations, stronger convective drying represented by Q2 in E5SIT-Nord at the convective center compared with E5SIT-Tied (shown as green contours in Fig.9a). To the east of deep convective center of MJO, the convection over the MC in the E5SIT-Nord simulation in response to the subsidence is much shallower than that in the E5SIT-Tied simulation, especially over the Borneo, near 120° E (green contours in Fig.9a). Notably, in the E5SIT-Nord simulation, more moisture is available in the lower troposphere and less moisture is available in the PBL below 850hPa over the MC and the western Pacific (represented by MSE; shading in Fig.9a); this is indicative of stronger shallow convection that helps create a favorable environment for deep convection. In the meantime, the E5SIT-Nord presents a horizontal structure similar to Kelvin waves which appears in the zonal dipole of sea level pressure, forming easterlies over the equatorial MC and the eastern equatorial Indian Ocean (bottom panel in Fig. 9a). This implies that the deep convection heating in the E5SIT-Nord simulation produces stronger dynamic responses than E5SIT-Tied simulation.

On day 2, when the convective center moves toward the western MC, different responses attributable to the two schemes become more substantial. Relative to the E5SIT-Tied simulation, the stronger upward motion at the convective center of the E5SIT-Nord simulation leads to stronger subsidence and enhanced tropical easterlies extending to the western Pacific (arrows in the bottom panel of Fig. 9b). Notably, a more prominent structure of Kelvin waves appears in response to both winds and sea level pressure (near 130° E, 10° N; bottom panel of Fig. 9b). In addition to the enhanced easterlies, the
meridional winds at the north side of the equator also become stronger, which in turn enhances low-level convergence at the equator. Accompanying the vertical transport of shallow convection, more moisture accumulates over the low levels between 800 and 500 hPa in the E5SIT-Nord simulation, providing conditions more conductive for MJO propagation, as mentioned in other studies (Kiranmayi and Maloney 2011; Adames 2017; Maloney et al. 2019). Consistent with the findings on climatological MJO composites in Fig. 7, these features also suggest that E5SIT-Nord can simulate stronger convective heating in the deep convection regime and greater moistening in the shallow convection regime than the E5SIT-Tied can.

5 Discussion

The comparison of the two model simulations against observational data revealed the importance of proper coupling between convection and large-scale circulation patterns in climate models to the realistic simulation of the MJO. In the E5SIT-Tied simulation, the persistent but fleeting period of deep convection dries out the moisture over the MC even during MJO development, resulting in conditions that are less favorable for MJO propagation. By contrast, E5SIT-Nord better simulates the moisture buildup over the MC during MJO development, facilitating the propagation of the MJO over deep convective regions. Figure 10 presents the differences between the model simulations with regard to the convection–circulation coupling during MJO development.

Based on our results, we suggest two aspects of convection–circulation coupling that are vital to improving simulations of MJO propagation: (1) the ability to generate deep convective heating and induce subsidence to the east of convective center and (2) the ability to induce moisture buildup in the subsidence region and create an environment
that is conducive to the later development of deep convection. During the early phases of the MJO, when the convective center is located in the Indian Ocean, deep heating induces Kelvin-wave-like perturbations (e.g., easterlies and low-pressure anomalies) that extend eastward with a subsidence branch to the MC and the western Pacific (Milliff and Madden 1996; Hendon and Salby 1996; Cravatte et al. 2003; Kiladis et al. 2005). If the deep convective heating is only weakly simulated, the induced subsidence becomes too weak to suppress the deep convection over the MC region where the SST is high. The preconditioning for the propagation of the MJO to the MC also requires the buildup of low-level moisture, which is often caused by the moistening effect of shallow convection (from the transport of moisture from the PBL). Such moisture buildup is often controlled by the representation of moist convection in climate models, especially in the determination of the type of convection and the associated heating/moistening. When the convection in the model is overly sensitive to high SST, convection can be frequently triggered, depleting moisture and precluding the realistic simulation of the moistening process over the MC when MJO is approaching. Our analysis also suggests that climate models must be capable of producing the contrast between light and intense rainfall events—that is, to simulate deep heating with intense rainfall and shallow moistening with light rainfall. E5SIT-Tied is more likely to present weaker and more frequent convection than its observed counterpart and also lighter than that simulated by E5SIT-Nord. Such a tendency results in a more stable atmosphere, which makes it more challenging to model the convection–circulation coupling with MJO in E5SIT-Tied.

Numerous studies have indicated that the design of convection schemes is essential to accurately simulating the MJO, including the sensitivity of CPS to the tropospheric moisture by entrainment or detrainment (Hannah and Maloney 2014), momentum...
transport (Wu et al. 2007; Miyakawa et al. 2012), microphysical processes, intensity
closure (Zhang and Mu 2005; Peters et al. 2017), triggering (Peters et al. 2017), the
representation of stratiform convection (Fu and Wang 2009), and shallow convection
(Zhang and Song 2009). The discrepancies between simulations observed in the present
study could be attributable to various differences in the design of the Nordeng and Tiedtke
schemes, such as the sensitivity to tropospheric humidity caused by entrainment design
(Möbis and Stevens 2012). We take a diagnostic approach, interpreting these differences
in a context of convection-circulation coupling. To ensure the successful simulation of
MJO propagation, the model representations of convection must be consistent. The
similarity in the biases concerning convection–circulation coupling as observed in both
the case study and the climate simulations suggests that biases in fast convective response
can further induce intraseasonal biases. To improve the simulation of intraseasonal
variability by better representing convection–circulation coupling, it is necessary to
carefully design responses of CPS to environmental characteristics, such as wind,
humidity, and SST. The process-based diagnostic used in the present study is useful for
understanding model performance with regard to convection–circulation coupling and
can also be used to evaluate designs of CPS for MJO simulation.

Although we focus on the CPS, MJO-related convection–circulation coupling
actually depends on the combined effects of moist convection designs, including shallow
convection, the PBL, and the parameterization of air–sea interaction. For example, with
regard to application in models derived from the Community Atmospheric Model 2, Liu
et al. (2005) concluded that the Tiedtke scheme outperforms the Nordeng scheme because
of its ability to trigger convection with low-level convergence. Considering that the
ECHAM5 used here had different PBL schemes and shallow convection schemes from
Community Atmosphere Model 2, the moisture buildup processes that are involved are likely to differ substantially. The simulations in the present study considered air–sea coupling, which, according to DeMott et al. (2019), are crucial contributors to the low-level moistening observed in successful MJO simulations. Although it is beyond the scope of this study, the short period of convection in the E5SIT-Tied simulation likely allows more shortwave radiation to warm ocean regions, enhancing the SST, and further destabilizes atmosphere, causing positive feedback between convection and SST. This feedback strengthens the convective responses to SST and hinders the coupling of convection with large-scale circulation patterns such as those in the MJO. Therefore, the holistic consideration of moist convection and air–sea coupling is necessary to improve the representation of the MJO in climate models. This premise warrants further investigation.

6 Conclusion

We conducted experiments using the ECHAM model with one-column high resolution ocean model to investigate the key processes for MJO propagation over the MC in climate simulations. With models with better representation of air–sea coupling, we demonstrated that convection–circulation coupling is crucial to the modeling of MJO propagation over the MC. E5SIT-Tied simulates less moisture buildup over the MC when the deep convection in phases 1 and 2 is necessary for the propagation of the MJO over the MC. The E5SIT-Tied simulation, which does not model MJO propagation, produces local MSE anomaly which is greatly correlated with local deep convection over the MC, in contrast to the shallow convection simulated by E5SIT-Nord. Such rapid development of deep convection over the MC creates an environment that is less conducive to MJO
propagation. Differences in low-level moistening in relation to light rain events between
the two simulations indicated that E5SIT-Tied tends to remove more moisture through
convective processes in the presence of subsidence than does E5SIT-Nord. The hindcast
case study of an observed MJO indicated that the environments that are less favorable for
the eastward propagation of the MJO in the E5SIT-Tied simulation may be formed
through weaker deep convective heating at the convective center of the MJO, which in
turn leads to weaker subsidence and moisture buildup over the MC and the western
Pacific. The present findings suggest that even with air–sea coupling, MJO propagation
over the MC is highly dependent on the capacity of CPS to produce MJO-related
convection-circulation coupling, including (1) inducing strong deep convective heating
associated with convective center over the Indian Ocean and (2) forming a favorable
environment characterized by low-level moistening under the effects of a subsidence
branch to the east of convective center. If CPSs are capable of this, convection–circulation
coupling is reinforced, and the maintenance of convective processes of the MJO over the
MC is facilitated. Our analysis indicates that the instantaneous response of CPS to MJO-
related environmental changes can further affect intraseasonal variability in climate
models; thus, the response of CPS must be carefully designed. Our analysis may be used
as a process-based diagnostic for evaluating convection–circulation coupling in the MJO.
Our findings can help model developers resolve the challenge of the “MJO barrier” over
the MC, helping them better forecast MJO in their climate models.

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Figure Captions

**Fig. 1** a–c Wavenumber–frequency spectra of 850-hPa equatorial zonal winds over 10° S–10° N; d–f Lag–longitude diagrams of intraseasonal precipitation (shaded area) and 10-m zonal winds (contour) correlated with precipitation averaged over 10° S–5° N, 75° E–100° E. The contour interval is 0.1.

**Fig. 2** Vertical profiles of intraseasonal anomalies (i.e., with 20-to-100-day band-pass filtering) in a–c moisture convergence \((10^{-6} \text{ g kg}^{-1} \text{ s}^{-1})\); d–f the apparent heat source \((Q_1; \text{ K day}^{-1})\); g–i the apparent moisture sink \((Q_2; \text{ K day}^{-1})\); and j–l moist static energy \((10^3 \text{ J kg}^{-1} \text{ s}^{-1})\), with respect to Madden–Julian Oscillation phases averaged over 10° S, 120°–150° E. The variables are based on observational data from the ERA-Interim reanalysis, the Nordeng scheme (E5SIT-Nord) simulation, and the Tiedtke scheme (E5SIT-Tied) simulation.

**Fig. 3** Vertical profiles of the unfiltered composite field of the a–c apparent heat source \((Q_1; \text{ K day}^{-1})\) and d–f apparent moisture sink \((Q_2; \text{ K day}^{-1})\) plotted with respect to Madden–Julian Oscillation phases averaged over 10° S, 120–150 °E. The data are from the ERA-Interim reanalysis, Nordeng scheme (E5SIT-Nord) simulation, and Tiedtke scheme (E5SIT-Tied) simulation.

**Fig. 4** Vertical profiles of apparent heat source \((Q_1; \text{ K day}^{-1}; \text{ red lines})\) and apparent moisture sink \((Q_2; \text{ K day}^{-1}; \text{ blue lines})\) with respect to Madden–Julian Oscillation phases...
averaged over 10° S and 120°–150° E for a–c phase 1 and d–f phase 2. The data are from the ERA-Interim reanalysis, Nordeng scheme (E5SIT-Nord) simulation, and Tiedtke scheme (E5SIT-Tied) simulation.

**Fig. 5** Structure of simulated Madden–Julian Oscillation (MJO) during a–c phase 1 and d-e phase 2. The longitude–height cross-sections (averaged over 10°S–EQ) of the MJO-scaled wind circulation (vector, $u$: ms$^{-1}$, omega: 10$^{-2}$ Pa s$^{-1}$), $Q_I$ (shaded area; K day$^{-1}$), and the horizontal moisture convergence (green contour; 10$^{-6}$ g kg$^{-1}$ s$^{-1}$) in the a, d ERA-Interim reanalysis; b, e Nordeng scheme (E5SIT-Nord) simulation, and c, f Tiedtke scheme (E5SIT-Tied) simulation. The contour interval of the moisture convergence is 8 $\times$ 10$^{-6}$ g kg$^{-1}$ s$^{-1}$. The solid line is positive. Precipitation (shaded area; mm day$^{-1}$) and sea level pressure (contour; hPa). The contour interval is 30 hPa. The dashed line is negative.

**Fig. 6** Regressed structure of circulation patterns, the apparent moisture sink ($Q_2$), and moist static energy (MSE) on intraseasonal convective time scale (shown in Fig.S5) in the a ERA-Interim reanalysis, b Nordeng scheme (E5SIT-Nord) simulation, and c Tiedtke scheme (E5SIT-Tied) simulation. The MSE (J kg$^{-1}$ s$^{-1}$) is shown in the shaded area, $Q_2$ (K day$^{-1}$) is shown in blue contours, and the circulation winds (ms$^{-1}$) are shown as vectors. The left panel shows the horizontal maps of 850-hPa fields, and the right panel shows the height-longitude cross-sections averaged over 10° S. The blue contour intervals in the left and right panels are 0.2 and 0.1, respectively.

**Fig. 7** Vertical profiles of $Q_2$ (K day$^{-1}$) composited from categories of rainfall intensity (mm day$^{-1}$) over the tropical oceanic regions covering 10° S–5° N, 80°–160° E simulated
by the a Nordeng scheme (E5SIT-Nord) and b Tiedtke scheme (E5SIT-Tied); c shows the differences between the two simulations. Only the ocean grid is calculated.

**Fig. 8** Distribution of occurrence of daily rainfall with respect to rainfall intensity and sea surface temperature (SST). The categories were ranked into bins over the tropical oceanic regions covering 10° S–5° N, 80°–160° E simulated by the a Nordeng (E5SIT-Nord) scheme and b Tiedtke scheme (E5SIT-Tied); c shows the differences between the two simulations. Only the ocean grid is calculated.

**Fig. 9** Differences in circulation patterns and sea level pressure between the Nordeng scheme (E5SIT-Nord) and Tiedtke scheme (E5SIT-Tied) simulations in the form of height–longitude cross-sections over the equator and horizontal maps on a day 1 and b day 2 after model initiation. The upper panel shows MSE (shaded area; J kg⁻¹ s⁻¹), $Q_2$ (Contours; K day⁻¹, interval is -5,-1,1,5), and circulations (u, m/s; omega, 10⁻² Pa/s, with omissions for velocities under 3). The lower panel shows the sea level pressure (shaded area; hPa), and the circulations (m/s for both u and v, with omissions for circulation under 0.8 m/s).

**Fig. 10** Schematic of convection–circulation coupling in the Madden–Julian Oscillation based on the analysis of the Nordeng and Tiedtke scheme simulations during MJO development (over phases 1 and 2). Convection is represented as clouds; convection-induced subsidence and horizontal wind fields are shown as black arrows and color arrows, respectively.
Supplementary Figure Captions

**Fig. S1** Mean states of a 850-hPa zonal winds (m/s) and b precipitation (mm/day) in winter (November–April). The black contours are the sea surface temperature (°C). From top to bottom, the data are from the ERA-Interim reanalysis, Nordeng scheme (E5SIT-Nord) simulation, and Tiedtke scheme (E5SIT-Tied) simulation.

**Fig. S2** Maps of ratio of intraseasonal rainfall variability (subjected to 20-to-100-day band-pass filtering) to total rainfall variability (shaded area). Intraseasonal rainfall variability (contours; subjected to 20-to-100-day band-pass filtering). From top to bottom, the daily rainfall data are from the a Global Precipitation Climatology Project, b Nordeng scheme (E5SIT-Nord) simulation, and c Tiedtke scheme (E5SIT-Tied) simulation.

**Fig. S3** a–c Mean moisture at 700-hPa (g/kg); d Moist bias between Nordeng scheme (E5SIT-Nord) simulation, Tiedtke scheme (E5SIT-Tied) simulation, and ERA-Interim reanalysis over the tropical Indian Ocean and Maritime Continent (20° S–20° N, 90°–135° E); e Pattern correlation coefficient of moisture between the two simulations and the ERA-Interim reanalysis from 1000 to 200 hPa.

**Fig. S4** Model-simulated column-integrated MSE budget terms (J kg⁻¹ s⁻¹) during phases 1 and 2 of the Madden–Julian Oscillation. Data from the observations, Nordeng scheme simulation, and Tiedtke scheme simulation are shown in black, red, and blue, respectively. The averaged domain is 10° S-EQ, 120°–150° E.
**Fig. S5** Normalized time scale data of intraseasonal convective time scale from the ERA-Interim reanalysis (green line), Nordeng scheme (E5SIT-Nord) simulation (orange line), and Tiedtke scheme (E5SIT-Tied) simulation (blue line), averaged over 10° S–10° N, 90°–150° E.

**Fig. S6.** Latitude–height cross-sections of the regressed structure to intraseasonal convective time scale (shown in Fig. S5) in the **a** ERA-Interim reanalysis, **b** Nordeng scheme (E5SIT-Nord) simulation, and **c** Tiedtke scheme (E5SIT-Tied) simulation. The shaded area, blue contours, and vectors represent the MSE (J kg$^{-1}$ s$^{-1}$), apparent moisture sink ($Q_z$; K day$^{-1}$; contour is 0.1), and circulation winds (ms$^{-1}$), respectively. Height–latitude cross-sections averaged over 120°–150° E.
Fig. 2 a–c Wavenumber–frequency spectra of 850-hPa equatorial zonal winds over 10° S–10° N; d–f Lag–longitude diagrams of intraseasonal precipitation (shaded area) and 10-m zonal winds (contour) correlated with precipitation averaged over 10° S–5° N, 75° E–100° E. The contour interval is 0.1.
Fig. 2 Vertical profiles of intraseasonal anomalies (i.e., with 20-to-100-day band-pass filtering) in a–c moisture convergence ($10^{-6}$ g kg$^{-1}$ s$^{-1}$); d–f the apparent heat source ($Q_1$; K day$^{-1}$); g–i the apparent moisture sink ($Q_2$; K day$^{-1}$); and j–l moist static energy ($10^3$ J kg$^{-1}$ s$^{-1}$), with respect to Madden–Julian Oscillation phases averaged over 10° S, 120°–150° E. The variables are based on observational data from the ERA-Interim reanalysis, the Nordeng scheme (E5SIT-Nord) simulation, and the Tiedtke scheme (E5SIT-Tied) simulation.
Fig. 3 Vertical profiles of the unfiltered composite field of the a–c apparent heat source ($Q_1$; K day$^{-1}$) and d–f apparent moisture sink ($Q_2$; K day$^{-1}$) plotted with respect to Madden–Julian Oscillation phases averaged over 10° S, 120–150 °E. The data are from the ERA-Interim reanalysis, Nordeng scheme (E5SIT-Nord) simulation, and Tiedtke scheme (E5SIT-Tied) simulation.
Fig. 4 Vertical profiles of apparent heat source \( (Q_1; \text{K day}^{-1}; \text{red lines}) \) and apparent moisture sink \( (Q_2; \text{K day}^{-1}; \text{blue lines}) \) with respect to Madden–Julian Oscillation phases averaged over 10° S and 120°–150° E for a–c phase 1 and d–f phase 2. The data are from the ERA-Interim reanalysis, Nordeng scheme (E5SIT-Nord) simulation, and Tiedtke scheme (E5SIT-Tied) simulation.
**Fig. 5** Structure of simulated Madden–Julian Oscillation (MJO) during a–c phase 1 and d–e phase 2. The longitude–height cross-sections (averaged over 10°S–EQ) of the MJO-scaled wind circulation (vector, $u$: m s$^{-1}$, omega: 10$^{-2}$ Pa s$^{-1}$), $Q_i$ (shaded area; K day$^{-1}$), and the horizontal moisture convergence (green contour; 10$^{-6}$ g kg$^{-1}$ s$^{-1}$) in the a, d ERA-Interim reanalysis; b, e Nordeng scheme (E5SIT-Nord) simulation, and c, f Tiedtke scheme (E5SIT-Tied) simulation. The contour interval of the moisture convergence is 8 × 10$^{-6}$ g kg$^{-1}$ s$^{-1}$. The solid line is positive. Precipitation (shaded area; mm day$^{-1}$) and sea level pressure (contour; hPa). The contour interval is 30 hPa. The dashed line is negative.
Fig. 6 Regressed structure of circulation patterns, the apparent moisture sink \( (Q_2) \), and moist static energy (MSE) on intraseasonal convective time scale (shown in Fig. S5) in the a ERA-Interim reanalysis, b Nordeng scheme (E5SIT-Nord) simulation, and c Tiedtke scheme (E5SIT-Tied) simulation. The MSE (\( J \, kg^{-1} \, s^{-1} \)) is shown in the shaded area, \( Q_2 \) (\( K \, day^{-1} \)) is shown in blue contours, and the circulation winds (\( m/s^{-1} \)) are shown as vectors. The left panel shows the horizontal maps of 850-hPa fields, and the right panel shows the height-longitude cross-sections averaged over 10° S. The blue contour intervals in the left and right panels are 0.2 and 0.1, respectively.
Fig. 7 Vertical profiles of $Q_2$ (K day$^{-1}$) composited from categories of rainfall intensity (mm day$^{-1}$) over the tropical oceanic regions covering 10° S–5° N, 80°–160° E simulated by the a Nordeng scheme (E5SIT-Nord) and b Tiedtke scheme (E5SIT-Tied); c shows the differences between the two simulations. Only the ocean grid is calculated.
Fig. 8 Distribution of occurrence of daily rainfall with respect to rainfall intensity and sea surface temperature (SST). The categories were ranked into bins over the tropical oceanic regions covering 10° S–5° N, 80°–160° E simulated by the a Nordeng (E5SIT-Nord) scheme and b Tiedtke scheme (E5SIT-Tied); c shows the differences between the two simulations. Only the ocean grid is calculated.
Fig. 9 Differences in circulation patterns and sea level pressure between the Nordeng scheme (E5SIT-Nord) and Tiedtke scheme (E5SIT-Tied) simulations in the form of height–longitude cross-sections over the equator and horizontal maps on a day 1 and b day 2 after model initiation. The upper panel shows MSE (shaded area; J kg\(^{-1}\) s\(^{-1}\)), \(Q_2\) (Contours; K day\(^{-1}\), interval is -5,-1,1,5), and circulations (u, m/s; omega, 10\(^{-2}\) Pa/s, with omissions for velocities under 3). The lower panel shows the sea level pressure (shaded area; hPa), and the circulations (m/s for both u and v, with omissions for circulation under 0.8 m/s).
**Fig. 10** Schematic of convection–circulation coupling in the Madden–Julian Oscillation based on the analysis of the Nordeng and Tiedtke scheme simulations during MJO development (over phases 1 and 2). Convection is represented as clouds; convection-induced subsidence and horizontal wind fields are shown as black arrows and color arrows, respectively.