Asymmetry of projected increases in extreme temperature distributions

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A statistical analysis reveals projections of consistently larger increases in the highest percentiles of summer and winter temperature maxima and minima versus the respective lowest percentiles, resulting in a wider range of temperature extremes in the future. These asymmetric changes in tail distributions of temperature appear robust when explored through 14 CMIP5 climate models and three reanalysis datasets. Asymmetry of projected increases in temperature extremes generalizes widely. Magnitude of the projected asymmetry depends significantly on region, season, land-ocean contrast, and climate model variability as well as whether the extremes of consideration are seasonal minima or maxima events. An assessment of potential physical mechanisms provides support for asymmetric tail increases and hence wider temperature extremes ranges, especially for northern winter extremes. These results offer statistically grounded perspectives on projected changes in the IPCC-recommended extremes indices relevant for impacts and adaptation studies.

Figure SPM.3 from the International Panel on Climate Change's Special Report on Extremes (IPCC SREX) depicts three simplified scenarios of how temperature extremes could shift as a result of climate change (Figure 1). The first, "Shifted Mean", is an increase in the entire probability distribution of temperature, leading to an equivalent increase in the distribution of all temperature extremes. The second, "Increased Variability", is a symmetric widening of the variability of temperature, leading to intensification of extremes in both tails. The third, "Changed Symmetry", is asymmetric, where the statistics of the lower tail temperatures would remain approximately at historical intensities and that the distribution of the uppermost extremes would increase. We use this concept to motivate the framework and hypothesis of this study. Emerging literature suggests that non-Gaussian, power law tail distributions and hence weather or climate extremes may be generated from simplified physics-based models with state-dependent noise. The processes generating extremes within fully coupled Global Climate Models (GCMs) such as the CMIP5 suite, and indeed in the real climate system, are likely to be more complex. Thus, the adoption of even seemingly intuitive mechanistic explanations is useful but must be done with care. The work in this paper was motivated by the contrast between the simplicity of the IPCC depiction of temperature extremes versus the underlying complexity. Here we analyze statistical properties of the tails under a changing climate with a 14-member ensemble of CMIP5 GCMs and reanalysis datasets.

The growing awareness and salience of the occurrence, severity, and societal impacts of weather extremes motivates detailed exploration of the degree to which recent observations may be attributed to climate change or, given assumed emissions trajectories, how the statistical attributes of the extremes may change over the next century. Trends in temperature extremes in particular have recently been attributed to anthropogenic climate change with relatively high confidence.

In addition, several initial examinations of the latest collection of GCMs, the CMIP5 suite, have provided useful insights on aggregate projected and historically simulated statistics of extreme temperature events. Two studies analyzed a large subset of the CMIP5 repository in terms of 27 impacts-relevant temperature and precipitation extremes indices. The first compared CMIP5 and CMIP3 historical simulations to four reanalysis datasets and the HadEX2 gridded observational dataset. This study found that the CMIP5 models simulated extremes with skill comparable to CMIP3 as measured visually and via squared-error based metrics, with some modest improvements. The second subsequently explored CMIP5 and CMIP3 projections under several climate change scenarios. Results show that extremes indices based on daily minima are generally projected to increase more than maxima in terms of spatial-temporally aggregate intensity, duration, and frequency, corroborating past work.

Extreme value theory is an alternative framework from which to garner statistically rigorous insights into temperature tail behavior. One recent study performed an analysis with regard to projected changes in temperature and precipitation extremes in all available CMIP5 models using the Generalized Extreme Value (GEV) model. Findings resembled the group’s previous similar work with the CMIP3 generation of models.
Results

Figures 2–3 shows multimodel ensemble projected changes in percentiles of spatial-temporally pooled seasonal extrema. Projections are broken down by all combinations of the following factors: (1) tail type - seasonal maxima versus minima, (2) season - summer versus winter, (3) terrain type - land versus ocean, and (4) region - South Pole or SP (−90° to −60°), Southern Hemisphere Extratropics or SHEX (−60° to −30°), Tropics or TX (−30° to 30°), Northern Hemisphere Extratropics or NHEX (30° to 60°), and North Pole or NP (60° to 90°). Figure 2 shows results only over land and Figure 3 only over ocean. Multimodel averages are plotted along with surrounding uncertainty defined as the lower and upper bounds of ensemble changes.

In general, all percentiles of extremes are projected to increase in almost all cases. However, in most cases, there is an upward trend in the change of the percentiles, showing that the highest percentiles of most extrema are projected to increase more than the lowest ones, for each respective extrema (summer or winter and minima or maxima) in isolation. This suggests that a metric of “asymmetry” in extrema projections can be constructed by subtracting the change in the 5th percentile of extrema from the change in the 95th percentile. Notably, we do not compare extremes across seasons or compare maxima events to minima events; all following inferences about asymmetry that hold generically are made within seasons and tails.

Figure 4 displays statistical maximum likelihood estimates of asymmetry for all combinations of the four factors described above, as averaged over all GCMs. This allows for an examination of the relationship between each of the four factors described above and multimodel ensemble variability with asymmetry through the lens of a linear mixed effect statistical model (Methods).

In general, there is consensus: asymmetry is greater than zero for more than 80% of the data points used in the analysis. The most dramatic asymmetry is found for winter minima events, especially those over ocean. These patterns are most pronounced in the NHEX and NP regions. Over land, the asymmetry is particularly pronounced for summer maxima and winter minima. From an impacts perspective, these are important to note since they suggest a wider range of temperature extremes within each season. Over land, summer maxima events show more asymmetry than summer minima. Dichotomously, winter minima events exhibit larger asymmetry than winter maxima over land. The Discussion section briefly touches on plausible physical hypotheses for broad asymmetry patterns summarized here and in Figure 4.

In some cases, estimates of asymmetry may be relatively less robust than others due to smaller data samples. For instance, there is little land north of 70° N, lending a smaller effective sample size to the estimation of asymmetry for NP extrema over land. Similarly, in the SP region, there is little ocean south of 65° S. Overall, though, asymmetry results are robust and based on stable estimates of extrema percentiles for each combination of the four factors (see Methods for details on robustness).
Systematic differences among ensemble members explain a significant but small (5%) proportion of variance in the asymmetry metric. In total, all of the four factors in addition to these systematic GCM differences account for 30% of the variance in projected asymmetry. A large portion of variance (~70%) in asymmetry is not accounted for by the factors suggests that other factors, such as fine spatial scale, internal model variability and/or more complex tail processes likely also play roles.

We utilize extreme value theory not only to compute statistics of the extrema percentiles (see Methods) but also as a framework for examining the reliability with which the CMIP5 ensemble simulates tail properties. Figures 5 and 6, for land and ocean respectively, show that the broad latitudinal patterns simulated by historical CMIP5 runs are generally well aligned with reanalyses. GEV models fit location, scale, and shape parameters to time series of seasonal extrema at each grid point. The three parameters respectively describe typical or average values of seasonal extrema, their variability, and the behavior of the uppermost portion of the tail. Ensemble simulations of all three parameters generally follow latitudinal patterns of reanalyses, suggesting their ability to simulate the statistical properties of extremes with fidelity at aggregate scales. This realism provides additional confidence in projections of asymmetric changes in extremes. There are several notable outlying patterns, including for example the scale parameter behavior of the mirocesm and mirocesmchem GCMs. In addition, there is larger ensemble spread in simulations of scale and shape parameters closer to the poles. The Supplementary Information (SI) provides further support for the fitness of the GEV models by testing the significance of their shape parameters (Figure S1). In addition, we reach similar conclusions regarding the historical reliability of the CMIP5 ensemble by conducting the same analysis as Figures 5–6 and Figure S1, respectively, using the alternative Generalized Pareto Distribution model (Figures S2–S4).

To further examine robustness of the asymmetric change insights, we conduct the full asymmetry analysis described in Methods but on deseasonalized data from three GCMs. Results are found to be extremely similar to those found here and can be found in the SI: Figure S5 and Table S5.

**Discussion**

While virtually all statistics of temperature extremes are projected to increase, GCMs consistently show asymmetry in projected changes of seasonal extrema. For each of summer and winter maxima and minima, the highest percentiles will increase significantly more than will the lowest. These insights most closely resemble the third panel of the cartoon IPCC SREX scenarios (Figure 1), suggesting a wider range of extreme temperature events across the globe in the future. In Figure 1, pure changes in location parameters correspond to shifts in typical or average extreme events, scale to changes in the width of the distribution of extremes, and shape to the behavior of the uppermost extremes, or the heaviness of the tail. We do note, however, that there is an interpretative difference between our analysis and the SREX component of Figure 1. Namely, the SREX shows the full temperature distribution and how it could change conceptually, and we explore only the tails in terms of summer and winter maxima and minima.
minima, all four in isolation. Our results suggest that the uppermost tail statistics of all types of extrema will increase more than the lowest tail statistics, which does not translate directly to the bottom panel of the SREX concept (“Changed Symmetry”). In this study, the effect is similar but is projected within all four classes of extremes (summer and winter maxima and minima): in each class, the most intense extremes (i.e., the 95th percentiles) will increase more than the least intense (i.e., the 5th percentiles).

The linkage between the GEV model parameters and the projections of asymmetric changes is intuitive and can be related to a large extent to the idealized concept of Figure 1. In many cases, asymmetry appears to be more reflective of widening of total extremes variability (i.e., the scale parameter, Figure 1 b and e) in some other cases, larger increases in the highest percentiles and less so the lowest ones (i.e., the shape parameter, Figure 1 c and f). We emphasize that the GEV itself does not create the asymmetric insight; rather, the nature of the asymmetry can be understood by examining the scale and shape GEV parameters that ultimately reflect the behavior of the extremes of GCM data outputs themselves. Details can be found in the SI: Figure S6 and Table S6.

Literature on trends in the variability of temperature extremes in observations reveals a mixture of results. One study found decreasing trends in the variance of intraannual daily minima of observed 20th century temperature but a less clear signal for corresponding maxima. Similarly another study identified decreasing variability in observed record breaking (cold and hot) temperatures, more so in winter than in summer. On the other hand, one study points toward increasing variability in temperatures as a likely driver of the European heatwave of 2003, suggesting that increases purely in the location of temperature distributions were unlikely to have produced such events. Similarly, this study points to a wider range of temperature extremes in the future as a function of asymmetric in projected changes of their percentiles.

A broad hypothesis is that natural processes that have driven anomalously cool weather or dampened the intensity of extremes will continue to do so within a warming trend, while a climate change signal may exhibit relatively more influence over the events in the uppermost extremes of both tails. For example, literature has linked La Niña and the North Atlantic Oscillation with persistent anomalously cold extremes within a longer term warming trend. Although some literature points to observed and simulated decreases in cold air outbreaks often located downstream from atmospheric blocking events, one study suggests they will persist and even increase in frequency in some regions in the future due to atmospheric circulation changes and natural variability that counters greenhouse effects. In addition, asymmetry could be explained by projections of increased interannual temperature variability. Differences in asymmetric projections broken down by the four factors shown in Figure 4 could serve as a hypothesis generation tool for exploring potential physical mechanisms. A rudimentary physical basis for our results showing stronger asymmetric winter projections further north is the larger synoptic variability ultimately due to the greater equator-to-pole temperature gradient in the winter. Considering the most prominent asymmetry specifically over the northern hemispheric ocean in winter, it may be useful to consider how variability in sea ice cover projections interacts with temperature extremes. Recent research suggests Arctic amplification of warming could lead to increases in the probability of both cold
and heat waves in the mid-latitudes, driven by warming-influenced dynamics of atmospheric north-south Rossby waves. Projections of a wider range of extreme temperature behavior may have consequences for many stakeholders. Although seasonal extrema studied here do not directly measure common impacts-relevant temperature extremes\(^9,10\), they may serve as a basis for extrapolating to likely impacts. For example, asymmetric changes may lead to increases in the intensity of heat waves and yet occasional persistence of cold waves, both of which have had significant effects on public health and mortality\(^{24}\). A wider spectrum of temperature extremes within seasons could also have implications for agricultural production yields\(^{21–22}\) and marine ecological stability\(^{23–36,37}\) since these impact areas can be sensitive to seasonal temperature thresholds. A wider spectrum of temperature extremes could also increase energy demand and potentially fossil fuel consumption\(^{38–40}\), helping to induce a positive warming feedback. Another potential consequence of asymmetry relates to human perception of the existence and danger of climate change conditional on firsthand experience with related natural hazards\(^{41}\). Persistent cold extremes\(^{42}\) and even long cooling periods\(^{43}\) do not necessarily imply a lack of global warming; however, literature\(^{41,44}\) suggests that people who have experienced extreme weather events that are typically associated with climate change may be more prone to perceive global warming as a significant threat. Regionally heterogeneous manifestations of relatively cold events or occasionally dampened extremes could conceivably create or change geographical and political patterns in public perception\(^{41,44}\) and hence impact policy.

**Methods**

Summer and winter maxima of daily maximum temperature are obtained from a 14-member CMIP5 ensemble of GCMs as well as three reanalysis surrogate observation datasets. Likewise, summer and winter minima of daily minimum temperature are obtained from the same datasets. Summer is defined as June-July-August (JJA) in the Northern Hemisphere and December-January-February (DJF) in the Southern Hemisphere, and winter is defined as DJF and JJA in the Northern and Southern Hemispheres, respectively. All these data are obtained for historical (1970–1999) and, for GCMs only, future (2070–2099) periods. Future GCM data is obtained for the Relative Concentration Pathway 4.5 (RCP4.5) moderate greenhouse gas emissions trajectory scenario\(^{14}\). The climate models and reanalysis datasets are summarized in SI: Table S7.
GEV and GPD models are fit separately to each of the four classes (summer maxima, summer minima, winter maxima, and winter minima) of extrema at each grid point for all GCMs and reanalyses. All minima are negated to enable the model-fitting process and transformed back afterward. To assess ensemble skill in emulating historical statistical attributes of extremes, historical parameters from GEV and GPD fits are averaged over latitudinal bands, for land (Figure 5) and ocean (Figure 6 and Figure S3). Shape parameters are almost always significantly less than 0 or not statistically differentiable from 0, and almost without exception never greater than 0, for both models (Figures S1 and S4).

We perform a bootstrap resampling analysis similar to recent work with seasonal extrema data to obtain robust estimates of changes in the distributions of extrema. Specifically, at each grid cell, for each GCM, and separately for each of summer and winter maxima and minima (generally stated, extrema), we treat future extrema data (29 data points) as a pool of approximately independent data to iteratively resample from with replacement. We draw 29 samples with replacement from this pool 100 times. In each of those 100 random samples of size 29, we fit GEV parameters via maximum likelihood and subsequently simulate a random realization from the fitted parameters. As such, we expect to obtain robust estimates of extrema percentiles where sufficient realizations exist. Rarely, unstable (i.e., large) estimates of large shape parameters led to unrealistic bootstrap realizations. In these cases, where resultant temperature was simulated to be above 375 Kelvins for maxima or below 180 Kelvins for minima, these realizations were discarded and replacement realizations were simulated. We note that the asymmetry results described next do not change materially if the bootstrap analysis is not employed; the bootstrap enhances confidence in the robustness of the particular extrema percentiles used subsequently.

Separately for each of summer and winter maxima and minima, we estimate spatial fields of historical climatology $Z$ by averaging historical seasonal extrema at each grid cell over time. Then, for each grid cell, we subtract $Z$ from each $T = 1, \ldots, 29$ historical seasonal extrema spatial fields $H_T$, which yields 29 spatial fields $\Delta H_T = H_T - Z$. We perform the same operation for the $S = 1, \ldots, 100$ bootstrapped future spatial fields of extrema, $F_S$, which yields 100 spatial temporal fields $\Delta F_S = F_S - Z$. $\Delta F$ and $\Delta H$ represent the three-dimensional concatenation of 100 future and 29 historical spatial fields, respectively, and are considered deviations from the historical climatology $Z$ in Kelvins.

We define four factors, with their levels in parentheses: $X_1$ - Tail type (minima or maxima), $X_2$ - Season (summer or winter), $X_3$ - Terrain type (land or ocean), $X_4$ - Region (SP, SHEX, TX, NHEX, or NP). Over each possible combination of the four and for each of the 14 GCMs, denoted $X_0$, we obtain percentiles (0.05, 0.1, 0.25, 0.5, 0.75, 0.9, 0.95) from each of $\Delta F$ and $\Delta H$ defined as $P_F$ and $P_H$, respectively, where subscripts $F$ and $H$ denote “Future” and “Historical”, respectively. As percentiles increase, events always increase in temperature (i.e., 95th percentile of winter minima is hotter than the 5th). These percentiles are subtracted from each other to yield $\Delta P = P_F - P_H$ that shows projected changes in the distribution of extrema deviations (Figures 2–3). We note that percentiles for each combination of factors may be obtained from effective sample sizes that differ substantially, and as such especially the more extreme percentiles (0.05 and 0.95) may be relatively more robust with larger sample sizes. For example, closer to the poles, size of grid cells becomes smaller and as a result the effective sample size of those regions shrinks. Because of this and since the bootstrap also implies that estimates of more extreme percentiles (e.g., 0.01 and 0.99 and beyond) are less robust, we do not venture that far into the tails in the following asymmetry analysis.

Next, we describe relationships between the $X_1$ through $X_4$ and the asymmetry inferred visually from Figures 2 and 3. “Asymmetry”, or for short, $Y$, in extrema projections is constructed by subtracting the change in the 5th percentile of extrema ($\Delta P_{05}$) from the change in the 95th percentile ($\Delta P_{95}$), i.e., $Y = \Delta P_{95} - \Delta P_{05}$. We fit a linear mixed effect model to obtain maximum likelihood estimates relationships between four factors, $X_1$ through $X_4$, as well as their two way interactions, with $Y$ and to estimate how much variability in $Y$ can be explained by systematic GCM differences, $X_0$. Those estimates, as well as their variability in terms of inter-GCM differences, are portrayed for each possible combination of $X_1$ through $X_4$ in Figure 4. More details on the linear model implementation and results can be found in the SI.

To further test the robustness of the asymmetry insight, we select three GCMs and repeat the above entire GEV bootstrap-driven asymmetry analysis but first remove a historical daily seasonal cycle from each grid cell of each GCM’s historical and future output. This analysis ensures that the findings in this study are not an artifact of...
seasonal timing (e.g., seasonal maxima or minima that will tend to be repeatedly extracted from very specific times of the year). Indeed we find this analysis strongly implies the robustness of the asymmetric projections to seasonal timing of extremes (SI, Figure S5 and Table S5).

Similar analyses are performed using the GPD. When using the GPD, we choose grid-wise 99% percentiles as the location parameters and fit scale and shape parameters to data exceeding those thresholds. With the GPD, the location parameters for both 20th century and projected data are estimated directly as percentiles and therefore they are not associated with statistical model-fitting uncertainty. Of primary interest here is whether the GPD analysis reveals similar patterns compared to the GEV model, especially in terms of evaluating historical GCM runs against reanalysis statistics. Outputs related to the GPD can be found in the SI, Figures S2–S4.

Figure 6 | The same results are displayed as in Figure 5 but using only ocean grid cells.
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**Acknowledgments**

The authors thank all members of the Sustainability and Data Sciences (SDS) Lab at Northeastern University for their valuable comments. All data processing and analysis was conducted in the statistical software R with R add-on packages “ncdf”, “ismev”, “POT”, “evd”, and “lme4”. The work was (partially) funded by the United States (US) National Science Foundation (NSF) Expeditions in Computing Grant # 1029711.

**Author contributions**

E.K. and A.R.G. designed the research. E.K. performed the research with significant input from A.R.G. E.K. and A.R.G. wrote the manuscript.

**Additional information**

**Supplementary information** accompanies this paper at http://www.nature.com/scientificreports

**Competing financial interests:** The authors declare no competing financial interests.

**How to cite this article:** Kodra, E. & Ganguly, A.R. Asymmetry of projected increases in extreme temperature distributions. *Sci. Rep.* 4, 5884; DOI:10.1038/srep05884 (2014).

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