CORONAL HEATING DISTRIBUTION DUE TO LOW-FREQUENCY, WAVE-DRIVEN TURBULENCE

P. Dmitruk, W. H. Matthaeus, L. J. Milano, S. Oughton, G. P. Zank, and D. J. Mullan

Received 2002 January 10; accepted 2002 April 11

ABSTRACT

The heating of the lower solar corona is examined using numerical simulations and theoretical models of magnetohydrodynamic turbulence in open magnetic regions. A turbulent energy cascade to small length scales perpendicular to the mean magnetic field can be sustained by driving with low-frequency Alfvén waves reflected from mean density and magnetic field gradients. This mechanism deposits energy efficiently in the lower corona, and we show that the spatial distribution of the heating is determined by the mean density through the Alfvén speed profile. This provides a robust heating mechanism which can explain observed high coronal temperatures and accounts for the significant heating (per unit volume) distribution below 2 solar radii needed in models of the origin of the solar wind. The obtained heating per unit mass, on the other hand, is much more extended, indicating that the heating on a per-particle basis persists throughout all the lower coronal region considered here.

Subject headings: MHD — Sun: corona — turbulence

1. INTRODUCTION

The mechanism by which the solar corona is heated is a fundamental problem in astrophysics and plasma physics, and one that remains incompletely explained. An acceptable mechanism transports energy to the corona, heating it to temperatures greatly in excess of chromospheric values. This mechanism accelerates the solar wind and establishes the boundary conditions for the entire plasma heliosphere. There are several constraints on an acceptable coronal heating model. Spectrometers (Kohl et al. 1995, 1997) show that proton temperatures in polar coronal holes rise to several times 10⁶ K at heliocentric distances of 1.5–2 solar radii (Rs), and the bulk wind speed reaches 200 km s⁻¹. Remote sensing observations (Grall et al. 1996) indicate wind speeds up to 600 km s⁻¹ at 4Rs. Fluid models of the solar wind (Habbal et al. 1995; McKenzie, Banaszkiewicz, & Axford 1995; Evje & Leer 1998) support the conclusion that wind acceleration at such low altitudes requires heating low in the corona. In the fluid models, an ad hoc heating function \( Q(r) \) is assumed, which represents the energy deposition per unit volume as \( Q \approx Q_0 \exp[-(r - r_0)/L] \), where \( r \) is heliocentric distance, \( r_0 = R_s \approx 7 \times 10^5 \) km, \( L \) is a prescribed dissipation length scale, and \( Q_0 \) is chosen so that the energy flux has the required value of about \( 5 \times 10^{15} \) ergs cm⁻² s⁻¹ (Withbroe & Noyes 1977). Despite the fact that there is no direct observational evidence for the exponential heat function, it has long been known to provide (Holzer & Axford 1970; Kopp & Orrall 1976; Hammer 1982) rapid acceleration of the wind, and with \( L \approx 0.2-0.5 R_s \), it accounts for many observed features of the corona (McKenzie et al. 1995; Habbal et al. 1995; Axford & McKenzie 1997). Although some possible sources of heating are proposed, in those models there is no physical mechanism for explaining this heating function and, being an ad hoc quantity, the exact explicit exponential function expression is perhaps irrelevant, and the main point to be remarked is the requirement of strong heating per unit volume in the first solar radius of the corona. Yet other two-fluid (electron and proton) models (Tu & Marsch 1997; Marsch & Tu 1997) have included some mechanisms for the heating, based on the requirement of high-frequency waves launched from the Sun, but those high-frequency (of the order of KHz) waves have yet remained unobserved in the coronal base, where the energy is injected. In other previous approaches, Hollweg (1986), Hollweg & Johnson (1988), and Isenberg (1990) conjectured that waves are launched from the Sun at low frequencies, but magnetohydrodynamic (MHD) turbulent-like cascades are assumed to transfer the energy to higher frequencies, where ion cyclotron mechanisms can be invoked to dissipate it. This idea, recently employed by Li et al. (1999) and reviewed by Cranmer (2000) involves phenomenological turbulent rates (of the Kolmogorov & Kraichnan type), but two important problems are faced. First, a cascade in wave frequencies is assumed, which implies a turbulent cascade proceeding in the parallel (to the mean field) wavenumber direction and a linear dispersion relation to persist between parallel wavenumber and frequency. MHD simulation studies show, on the other hand, that in the presence of a strong mean magnetic field such as that in the corona, the parallel wavenumber cascade is almost completely suppressed (Shebalin, Matthaeus, & Montgomery 1983; Oughton, Priest, & Matthaeus 1994; Matthaeus et al. 1998) in favor of the perpendicular cascade. This is precisely the kind of anisotropy which is well documented (Armstrong et al. 1990) for the lower coronal density.

Second, the necessity of counterpropagating fluctuations to sustain the turbulence (Kraichnan 1965; Dobrowolny, Mangeney, & Veltri 1980) is not considered in the models, and a WKB approach is implicitly assumed. In those models, the turbulent cascade was not the central focus of study, but we believe that a useful perspective can be gained into the heating problem by further study of this issue. In this present work, instead of assuming a parallel wave cascade, we describe ab initio the conditions under which a strong (perpendicular) turbulent cascade can actually be developed and sustained by low-frequency driving at the base.
tions from density and mean field gradients provide the necessary counterpropagating fluctuations to sustain the turbulence, and this effect is fully taken into account in our model. We will employ both direct numerical simulation and turbulent phenomenologies to obtain the heating rate distribution.

We show that the heating distribution profile is related to the coronal background magnetic field and density profile; i.e., the heating and the density profile are not independent quantities. On the one hand, we find that the heating per unit volume is significant mostly within the first solar radius, with a dissipation length scale (defined as the length in which the heating decays by an order of magnitude) of a fraction of solar radius. On the other hand, the heating per unit mass varies much less dramatically and is significant through the complete domain. For a complete model, appropriate kinetic processes will need to be identified to absorb the small perpendicular-scale cascaded energy. Candidates for small-scale damping are plentiful and include oblique kinetic Alfvén waves, collisionless reconnection and associated heating at current sheets, and nonlinear beam instabilities (Leamon et al. 1998). The kinetic physics of heating is beyond the scope of the present paper. The main purpose of this work is to show that a heating distribution emerges naturally from a consistent MHD turbulent cascade driven by low-frequency fluctuations at the coronal base. This result may bring us closer to understanding the puzzle of coronal heating and the origin of the solar wind.

2. MODEL

Most coronal heating models derive their energy supply from either wave power or quasistatic field line motions originating in the photosphere or chromosphere. These differ mainly in their characteristic timescales. A general scenario for wave production in open magnetic regions has been proposed (McKenzie et al. 1995), in which activity in the network regions, driven by convective motions, provides a source of upward-traveling Alfvén waves. Higher-frequency waves are easily transported upward, whereas low-frequency waves experience greater reflection and transmit less readily into the corona (Parker 1965; Heinemann & Olbert 1980; An et al. 1990; Zhou & Matthaeus 1990; Velli 1993). However, even in the limit of sharp gradients or discontinuities, there are indications (Hollweg 1981) that a substantial energy flux can reach the coronal base (Kudoh & Shibata 1999).

Here we examine the following scenario (Matthaeus et al. 1999): MHD-scale (low-frequency) fluctuations are excited below the base of the corona on transverse length scales that are characteristic of the chromospheric network and propagate upward along the mean magnetic field, $B$. A portion of this wave flux enters the corona. Reflections from large-scale inhomogeneities within the lower corona produce counterpropagating fluctuations (Heinemann & Olbert 1980; Zhou & Matthaeus 1990), a situation that permits strong nonlinear MHD couplings (Dobrowolny et al. 1980). The couplings drive a perpendicular (to $B$) turbulent cascade, producing small-scale reconnection events that couple to kinetic processes at small scales and oblique wavevectors (Leamon et al. 1998).

In our model, we simulate the propagation of low-frequency MHD fluctuations in a medium whose properties are chosen to represent an open magnetic field region (such as a polar coronal hole) in the lower corona. We consider a section which extends in the radial direction a distance $L_{s}$ of the order of $2R_{s}$ above the surface. A sketch of such a region is shown in Figure 1.

Our goal is to compute the dynamics of transverse fluctuations of magnetic field ($b$) and velocity ($v$), as influenced by specified large-scale inhomogeneities (mean magnetic field and density gradients) as well as by local nonlinear couplings. To do this in a medium where there is a strong mean magnetic field, we use the reduced MHD (RMHD) approximation (Strauss 1976; Montgomery 1982; Zank & Matthaeus 1992). This approach is appropriate for fluctuations in a nearly incompressible plasma, where the plasma beta (ratio of thermal to magnetic pressure) is low (Zank & Matthaeus 1992). We employ the Elsasser variables $z_{\pm} = v \pm b$ [where the magnetic field is written in units of $b/(4\pi \rho)^{1/2}$, with $\rho$ = density] to represent downward (+) and upward (−) propagating fluctuations. Fluctuations depend on the radial coordinate $r$, the transverse spatial coordinates [including an areal expansion factor $A(r)$], and on time ($t$). Mean quantities such as density ($\rho$) and magnetic field ($B$) are assumed to depend only on $r$. Consistency with the RMHD assumptions (Zank & Matthaeus 1992) requires $\partial_{t} \ll \nabla_{\perp} \cdot \mathbf{v}$, $A_{\perp} \ll \rho_{\perp}$ and $\mathbf{v} \cdot \mathbf{z} = 0$, where $A_{\perp} = B/(4\pi \rho)^{1/2}$ is the Alfvén speed, which gives the propagation velocity of fluctuations in the linear limit.

In the presence of a nonuniform $A_{\perp}$, the nonlinear RMHD equations can be written (Zhou & Matthaeus 1990) as

$$\frac{\partial z_{+}}{\partial t} + V_{A} \frac{\partial z_{+}}{\partial r} = -R_{1}z_{-} + R_{2}z_{-} \cdot \nabla_{\perp} z_{-} + \eta \nabla_{\perp}^{2} z_{-} + \eta \nabla_{\parallel}^{2} z_{-},$$

$$\frac{\partial z_{-}}{\partial t} - V_{A} \frac{\partial z_{-}}{\partial r} = R_{1}z_{+} - R_{2}z_{+} - z_{-} \cdot \nabla_{\perp} z_{+} + \eta \nabla_{\perp}^{2} z_{+} + \eta \nabla_{\parallel}^{2} z_{+}, \quad (1)$$

where $\eta$ is the resistivity (assumed equal to the viscosity), and $R_{1}(r)$ and $R_{2}(r)$ are specified reflection rates due to the inhomogeneous $A_{\perp}(r)$. For a symmetric radial geometry [$A(r) = r^{2}$], $B = B_{0}(r_{0}/r)^{2}$ (with $B_{0}$ the magnetic field at $r_{0} = R_{s}$), the reflection rates are $R_{1}(r) = (1/2)(dV_{A}/dr)$ and $R_{2}(r) = (1/2)(dV_{A}/dr) - V_{A}/r$. In the case of a general geometry with cross section area $A(r)$, where $A(r) = A_{0}B_{0}/B(r)$, the reflection rates are $R_{1}(r) = (1/2)(dV_{A}/dr)$ and $R_{2}(r) = 1/2(dV_{A}/dr) + (1/2)(V_{A}/A)$. 

![Figure 1](image.png)
amplitudes are reported to range from 20 to 55 km s$^{-1}$ in the upper transition region of the Sun. These amplitudes are associated with gradients of the wave speed, which are capable of sustaining the turbulence and provide effective dissipation. In the next section, we obtain heating distribution profiles resulting from this turbulent state.

### 3. Heating Profiles

We performed numerical simulations employing several different mean magnetic field and density radial profiles. The values at the bottom boundary (Axford & McKenzie 1997; Feldman et al. 1997) have been fixed to $B_0 = 9$ Gauss and a number density of $n_0 = 3.2 \times 10^8$ cm$^{-3}$, which gives...
an Alfvén speed at the base of 1100 km s\(^{-1}\). With the assumed amplitude of fluctuations of the order of 20–55 km s\(^{-1}\), this gives an average energy input flux per unit area, \(F_{\alpha} \sim \rho_0 V_{\alpha} (z_-^2 - z_+^2)\) of the order of \(5 \times 10^5\) ergs cm\(^{-2}\) s\(^{-1}\), corresponding to the Withbroe & Noyes (1977) value. These values have to be taken as order of magnitude quantities, but a different choice would not invalidate the general argument we want to present here. In our first simulation, we consider a symmetric radial mean magnetic field profile \(B(r) = B_0(R_s/r)^2\). The mean density follows from the hydrostatic equilibrium approximation (An et al. 1990; Velli 1993; Nakariakov, Offman, & Arber 2000): \(dp/dr = -m_i R_s^2 n \rho(R_s/r)^2\), where \(\alpha_T = \mu GM/R_s TR_s\), \(\mu\) is the mean molecular weight, \(G\) the gravitational constant, \(M\) is solar mass, \(R_s\) the gas constant, and \(T\) is temperature). The quantity \(\alpha_T \approx 12\) for the Sun and a fully ionized hydrogen coronal plasma at \(T = 10^6\) K.

The number density distribution is then \(n(r) = n_0 \exp(\alpha_T (R_s/r - 1))\) and the density is \(\rho(r) = m_i n(r)\). We consider two such density profiles, shown in the top left panel of Figure 3 (solid and dotted lines), corresponding to values of \(\alpha_T = 12\) and \(\alpha_T = 6\) (representing a hotter corona). This gives two different density profiles, with the hotter corona having the shallower profile. The corresponding Alfvén speed profiles \(V_A(r) = B(r)/(4\pi \rho(r))^{1/2}\) are shown on the top right panel of Figure 3. When the system reaches a statistically steady state, the turbulent dissipation rate \(\epsilon\) (equal to the cascade rate) is computed from the fluctuating fields \(z_-, z_+\), from which the heating per unit volume is obtained as \(Q = \epsilon \rho\).

This quantity is plotted as a function of \(r\) in the bottom left panel of Figure 3. It is apparent that the dissipation per unit volume is peaked near the model coronal base. It is important to note that \(Q(r)\) decreases faster for the model with the steeper density profile. The radial distance \(\Delta r\) at which \(Q\) decreases by an order of magnitude with respect to the coronal base value \(Q_0\) is 0.36\(R_s\) and 1.1\(R_s\) for the two profiles in Figure 3. This would be the analog of the dissipation length in the ad hoc exponential heating distribution profiles. The bottom right panel of Figure 3 shows the heating per unit mass, a useful quantity to consider the heating in a per-particle basis. Over our entire domain, this quantity maintains a relatively constant value. Extended heating per unit mass fits the apparent requirement of a hot (nonadiabatic) solar wind and has also emerged in empirical models of radiation loss and other heating models (Mullan & Cheng 1994; Gibson 1973).

A third simulation has been performed employing a super radial geometry, where the mean magnetic field profile has been taken as

\[
B = 1.5 \left[ (f_{max} - 1) \left(\frac{R_s}{r}\right)^{3.5} + \left(\frac{R_s}{r}\right)^{2}\right] \text{ Gauss}.
\]

Profiles of this type have been considered in Hollweg (2000), and similar superexpansion profiles have been used by McKenzie et al. (1995), Evje & Leer (1998), and Li et al. (1999) in their solar wind models. We have taken \(f_{max} = 6\),

![Fig. 3.](image-url)
which gives a boundary value of $B_0 = 9$ Gauss. An observationally based number density is assumed in this case (Feldman et al. 1997),

\[
n(r) = 3.2 \times 10^6 \left( \frac{R_s}{r} \right)^{15.6} + 2.5 \times 10^6 \left( \frac{R_s}{r} \right)^{3.76} \text{ cm}^{-3}.
\]  

The density profile and resulting Alfvén speed profile are shown in the top panels of Figure 3 (dashed line). The obtained heating per unit volume and heating per unit mass are shown in the bottom panels of Figure 3 (dashed line). The result confirms the tendency shown for the earlier cases: this profile, with the fastest decreasing density, also has the fastest decreasing heating per unit volume. The decay length for this case is $\Delta r = 0.2R_s$. The heating per unit mass remains at a relatively constant value.

The relevant results to be extracted from these simulations for different Alfvén speed profiles is that the heating per unit volume has significant values only within the first solar radius of the lower corona, and that the radial profile of the heating is controlled by the radial profile of the density. As it will be more clear from the phenomenological analysis that follows in the next section, it is actually through the Alfvén speed profile and its gradient that this behavior is manifested.

Whether the radial profile of the heating per unit volume is exactly exponential or not is, we believe, irrelevant, and we conjecture that a steep heating profile like the ones we obtained here would work as well to explain the fast acceleration of the solar wind.

Figure 3 contains the essence of the present results, that a reasonable and efficient heating can be obtained from the MHD perpendicular turbulent cascade driven by low-frequency waves injected from the bottom. The properties of this heating are controlled by both the amount of energy injected into the system and the background profiles of magnetic field and mean density. To further illustrate this idea and, in some limiting case, to obtain an analytical expression for the heating profile in the low region of the volume considered here, we present in the following section a phenomenological approach to the previous model (eq. [1]).

4. HEATING PROFILE FROM A PHENOMENOLOGICAL MODEL

A nonlinear phenomenology (Dmitruk et al. 2001b) simplifies the study of the wave-driven RMHD heating model. We modify equation (1) as follows. The independent variables, now designated as $Z_\perp(r)$, are treated as one-dimensional wave amplitudes with the same linear transport terms (left-hand side and reflection terms) as in equation (1), but with the nonlinear and dissipative terms on the right-hand side replaced by the nonlinear models $Z_\perp^2/Z_\perp/2\lambda_\perp(r)$. This model entirely suppresses the transverse structure, with the strength of the nonlinear cascade effects represented through a single correlation length scale $\lambda_\perp(r)$. Previous investigations (Dmitruk et al. 2001b) have shown that this phenomenology portrays many of the same physical effects as wave-driven models based upon the full RMHD equations (Dmitruk et al. 2001a; Oughton et al. 2001). We expect this model to correspond to high Reynolds number, fully developed RMHD turbulence since the amplitudes $Z_-$ and $Z_+$ are strongly coupled in the adopted forms for the nonlinear terms. We extracted a heating function $Q(r)$ from a numerical solution to this phenomenological model using the same parameters as those employed in the full nonlinear RMHD simulations, and assuming a correlation length scale $\lambda_\perp(r)$ linearly increasing with radius, with a value at the coronal base set to correspond to the internetwork spacing of 30 Mm. The derived $Q(r)$ is illustrated in Figure 4 as the thin line. The direct numerical solution of the previous section is shown as the thick line. This corresponds to the simpler hydrostatic density and $1/r^2$ mean magnetic field profile (similar results are obtained for the superexpansion geometry). Despite some differences on the far region, where $dV_A/dr$ approaches 0 and the heating is very low, the agreement is pretty good, considering the extreme simplification involved in the phenomenological treatment. Of course, the phenomenology would not be useful for studies of the turbulent cascades and spectra, but it gives the right order of magnitude for the averaged quantities such as dissipation (heating), when this quantity is not extremely low. The interesting issue of how the correlation length and the strength of the cascade depend on the external parameters warrants further comparison of the phenomenology with the full nonlinear direct numerical simulation.

In Figure 5, we explore the phenomenological heat function ($Q$) obtained by varying the correlation length scale at the coronal base, with $\lambda_\perp = 1$ corresponding to 30 Mm. The limit $\lambda_\perp \rightarrow 0$ corresponds to stronger local turbulence since the implied eddy turnover time, $\lambda_\perp/z_\perp$, becomes much smaller than the wave transit time, $R_s/V_A$. Figure 5 shows that $Q$ increases as $\lambda_\perp \rightarrow 0$, while maintaining the fast radially decreasing behavior.

In this limit, an analytical asymptotic expression can be obtained. Although limited in its validity, this analysis serves to illustrate better the properties of the heating in this model. We begin by formulating a flux balance equation based upon equation (1). This takes the form $dF/dr = -A(r)Q$, where the net upward energy flux $F = pA V_A (Z_+^2 - Z_-^2)$ and $A$ is the cross section area. Note that in geometrical optics (or WKB theory for noninteracting waves; Jacques 1977) the flux balance formally requires that $Q \equiv 0$. When fluctuations are damped, $Q \neq 0$ (Hollweg 1986). Here the crucial relation that connects the heating to the Alfvén speed profile emerges by identifying $Q$ with a physically correct turbulent dissipation rate per unit volume.

![Figure 4](image-url)
Fig. 5.—Different solutions for the heating per unit volume of the phenomenological model (thin lines) for values of the correlation length $\lambda_\perp = 1, 0.5, 0.1,$ and 0.02 (in units of the internetwork length), which approach the asymptotic solution when $\lambda_\perp \to 0$. Dot-dashed line: Eq. (5).

at distance $r$, namely $Q = \rho \varepsilon$, where the dissipation rate per unit mass $\varepsilon$ is expressed in the phenomenological model as $\varepsilon \approx (Z^2_\perp |Z_-| + Z^2_\perp |Z_+|)/\lambda_\perp$. We now proceed to form an asymptotic strong turbulence limit as follows. Letting $\lambda_\perp \to 0$, one can conclude (Dmitruk et al. 2001b) that the downward flux is small, $|Z_+| \ll |Z_-|$, and that in a steady state, this limit is characterized by $|Z_+|/\lambda_\perp = |dV_A/dr|$. Thus, $\varepsilon \approx Z^2_\perp |Z_+|/\lambda_\perp$, and we obtain the asymptotic result that the dissipation per unit length can be related to the Alfvén speed profile and the energy flux: $A Q \approx \rho A Z^2_\perp |dV_A/dr| \approx V_A^{-1}|dV_A/dr| F$. Thus, the asymptotic flux balance equation can now be written as $dF/dr = -V_A^{-1}|dV_A/dr| F$, whose solution is

$$F \approx \begin{cases} F_0 (V_A / V_A^0)^2 & \text{if } r < r_m, \\ F_0 (V_A / V_A^0) & \text{if } r > r_m, \end{cases}$$

(4)

where $F_0$ is the net flux at the base and $r_m$ is the radial distance at which $V_A$ reaches its maximum value $V_{A_\infty}$.

This allows us finally to obtain an explicit expression for the heating deposition,

$$Q(r) \approx \begin{cases} A_\infty (A_0 / A) |dV_A/dr| (V_A / V_A^0) & \text{if } r < r_m, \\ A_\infty (A_0 / A) |dV_A/dr| (V_A / V_A^0) & \text{if } r > r_m, \end{cases}$$

(5)

where $F_{A_\infty} = F_0 / A_0$ is the energy flux per unit area at the base (i.e., the Withbroe & Noyes 1977 value).

For the particular case of the $A = r^2$ geometry and the isothermal atmosphere used before with $r_m \approx 3R_\odot$, this relation predicts the top dot-dashed curve of Figure 5. As seen in this figure, the phenomenological solutions for different $\lambda_\perp$ values approach this asymptotic case as $\lambda_\perp$ tends to 0. Already for $\lambda_\perp = 1/10$, the asymptotic solution would be a good approximation. This corresponds to correlation length scales of the order of 3000 km. Although much less than the typical internetwork distances, observations do not rule out correlation scales of this magnitude. Equation (5) also shows that in this limiting case, the value of the heating goes to 0 at points where $dV_A/dr = 0$, a limitation which is only apparent at corresponding very low values of $Q$ in the numerical solution. (A similar result applies for the superexpansion profile presented before, where the point at which $dV_A/dr = 0$ is $r_m \approx 1.6R_\odot$.)

For this asymptotic limit, equation (5) explicitly shows that the spatial distribution of turbulent heating is directly connected to the radial profile of the Alfvén speed, and its absolute value depends on the energy input flux. This illustrates the connection already pointed out through the direct numerical simulation results.

5. CONCLUSIONS

We have presented a model for MHD turbulence driven by low-frequency waves imposed at the lower boundary. We applied this model to an open region in the lower corona, adopting reasonable profiles for magnetic field and density. Both direct numerical simulations and phenomenological studies have been performed and compared. Results show that turbulence can be sustained due to reflection of upward-traveling waves by Alfvén speed gradients, producing a perpendicular turbulent cascade and efficient heating. The energy dissipation per unit volume is significant mostly in the lower part of the model corona, with a dissipation length scale of a fraction of solar radius. The obtained heating profile $Q$ is similar to profiles commonly used in solar wind acceleration models. However, the more general result emerges for strong turbulence that the heat function $Q(r)$ should be related to the Alfvén speed profile $V_A(r)$. This shows that the heating distribution is determined by the large-scale magnetic field and density profiles. In this way, one sees that the scale height of the heating per unit volume is directly related to the density scale height, thus explaining the spatial confinement of $Q$ as a consequence of the rapid density decrease in the lower corona. However, the deposition of heat per unit mass, $Q/\rho$, is much more extended, perhaps well beyond the lower coronal region considered in the present model. These conclusions do not rule out other models such as direct cyclotron absorption of high-frequency waves (Axford & McKenzie 1997; Tu & Marsch 1997), but they imply that it is possible to provide the proper kind of heating per unit volume using a low-frequency, wave-driven MHD turbulence mechanism.

Research supported by NASA (NAG5 7164, NAG5 8134 SEC Theory Program), NSF (ATM 9713595, ATM 0296113), and UK PPARC (PPA/G/S/1999/0059).

REFERENCES

An, C.-H., Suess, S. T., Moore, R. L., & Musielak, Z. E. 1990, ApJ, 350, 309
Armstrong, J. W., Coles, W. A., Kojima, M., & Rickett, B. J. 1990, ApJ, 358, 685
Axford, W. I., & McKenzie, J. F. 1997, in Cosmic Winds and the Heliosphere, ed. J. R. Jokipii, C. P. Sonnett, & M. S. Giampapa (Tucson: Arizona Univ. Press), 31
Chae, J., Schuhle, U., & Lemaire, P. 1998, ApJ, 505, 957
Cranmer, S. R. 2000, ApJ, 532, 1197
Dobrowolny, M., Mangeney, A., & Veltri, P. L. 1980, Phys. Rev. Lett., 45, 144
Doyle, J. G., Banerjee, D., & Perez, M. E. 1998, Sol. Phys., 181, 91
Evie, H. O., & Leer, E. 1998, A&A, 329, 735
Feldman, W. C., Habbal, S. R., Hoogeveen, G., & Wang, Y.-M. 1997, J. Geophys. Res., 102, 26905

Dmitruk, P., Matthaeus, W. H., Milano, L. J., & Oughton, S. 2001a, Phys. Plasmas, 8, 2377
Dmitruk, P., Milano, L. J., & Matthaeus, W. H. 2001b, ApJ, 548, 482
Evie, H. O., & Leer, E. 1998, A&A, 329, 735
Feldman, W. C., Habbal, S. R., Hoogeveen, G., & Wang, Y.-M. 1997, J. Geophys. Res., 102, 26905

Evie, H. O., & Leer, E. 1998, A&A, 329, 735
Feldman, W. C., Habbal, S. R., Hoogeveen, G., & Wang, Y.-M. 1997, J. Geophys. Res., 102, 26905
Gibson, E. G. 1973, The Quiet Sun (NASA SP-303: Washington)
Grall, R. R., et al. 1996, Nature, 379, 429
Grappin, R., Pouquet, A., & Leorat, J. 1983, A&A, 126, 51
Habbal, S. R., Esser, R., Guhathakurta, M., & Fisher, R. R. 1995, Geophys. Res. Lett., 22, 1465
Hagenaar, H. J., Schrijver, C. J., & Title, A. M. 1997, ApJ, 481, 988
Hammer, R. 1982, ApJ, 259, 767
Hassler, D. M., Rottman, G. J., Shoup, E. C., & Holzer, T. E. 1990, ApJ, 348, L77
Heinemann, M., & Olbert, S. 1980, J. Geophys. Res., 85, 1311
Hollweg, J. V. 1981, Sol. Phys., 70, 25
Hollweg, J. V., & Johnson, W. 1988, J. Geophys. Res., 93, 4111
Hollweg, J. V., & Johnson, W. 1988, J. Geophys. Res., 93, 9547
Hollweg, J. V., & Axford, W. I. 1970, J. Geophys. Res., 75, 6437
Jacques, S. A. 1977, ApJ, 215, 942
Jacques, S. A. 1977, ApJ, 215, 942
Kohl, J. L., et al. 1997, Sol. Phys., 175, 613
Kohl, J. L., Gardner, L. D., Strachan, L., Fisher, R., & Guhathakurta, M. 1995, Space Sci. Rev., 72, 29
Kopp, R. A., & Orrall, F. Q. 1976, A&A, 53, 363
Kraichnan, R. H. 1965, Phys. Fluids, 8, 1385
Kudoh, T., & Shibata, K. 1999, ApJ, 514, 493
Leamon, R. L., Matthaeus, W. H., Smith, C. W., & Wong, H. K. 1998, ApJ, 507, L181
Li, X., Habbal, S. R., Hollweg, J. V., & Esser, R. 1999, J. Geophys. Res., 104, 2521
Marsch, E., & Tu, C.-Y. 1997, A&A, 319, L17
Matthaeus, W. H., Oughton, S., Gosh, S., & Hossain, M. 1998, Phys. Rev. Lett., 81, 2056
Matthaeus, W. H., Zank, G. P., Zank, Oughton, S., Mullan, D. J., & Dmitruk, P. 1999, ApJ, 523, L93
McKenzie, J. F., Banaszekiewicz, M., & Axford, W. I. 1995, A&A, 303, L45
Montgomery, D. C. 1982, Phys. Scr., T2/1, 83
Mullan, D. J., & Cheng, Q. Q. 1994, ApJ, 435, 435
Nakariakov, V. M., Oughton, S., & Arber, T. D. 2000, A&A, 353, 741
Oughton, S., Matthaeus, W. H., Dmitruk, P., Milano, L. J., Zank, G. P., & Mullan, D. J. 2001, ApJ, 551, 565
Oughton, S., Priest, E. R., & Matthaeus, W. H. 1994, J. Fluid Mech., 280, 95
Parker, E. N. 1965, ApJ, 142, 1086
Shebalin, J. V., Matthaeus, W. H., & Montgomery, D. C. 1983, J. Plasma Phys., 29, 525
Strauss, H. R. 1976, Phys. Fluids, 19, 134
Ting, A. C., Matthaeus, W. H., & Montgomery, D. C. 1986, Phys. Fluids, 29, 3261
Tu, C.-Y., & Marsch, E. 1997, Sol. Phys., 171, 363
Velli, M. 1993, A&A, 270, 304
Withbroe, G., & Noyes, R. W. 1977, ARA&A, 15, 363
Zank, G. P., & Matthaeus, W. H. 1992, J. Plasma Phys., 48, 85
Zhou, Y., & Matthaeus, W. H. 1990, J. Geophys. Res., 95, 10291