Two-Dimensional Metal–Chalcogenide Films in Tunable Optical Microcavities

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Supporting Information

ABSTRACT: Integration of quasi-two-dimensional (2D) films of metal–chalcogenides in optical microcavities permits new photonic applications of these materials. Here we present tunable microcavities with monolayer MoS$_2$ or few monolayer GaSe films. We observe significant modification of spectral and temporal properties of photoluminescence (PL): PL is emitted in spectrally narrow and wavelength-tunable cavity modes with quality factors up to 7400; a 10-fold PL lifetime shortening is achieved, a consequence of Purcell enhancement of the spontaneous emission rate.

KEYWORDS: Molybdenum disulfide, gallium selenide, 2D materials, tunable microcavities, Purcell effect, photonics

The discovery and research into remarkable properties of graphene has sparked interest in two-dimensional (2D) metal chalcogenides (MCs). MCs are a large family of compounds that include layered van der Waals crystals. Among them are many semiconducting materials with a variety of band gap energies attractive for use in optoelectronics. For light-emitting applications, some of the layered materials such as for example molybdenum and tungsten dichalcogenides need to be thinned down to a single atomic unit cell (e.g., S–Mo–S for MoS$_2$), as only in this form do they behave as direct band gap semiconductors. Layered III–VI crystals such as GaSe, InSe, and so forth are also attractive for 2D photonics as they exhibit direct band-gaps in films with a variety of thicknesses from a few to tens of nanometers, thus enabling flexibility in the device design. However, for materials of both types, use of thin films in photonic applications will require overcoming relatively low emission and absorption efficiency generally characteristic of thin layers of any semiconducting material.

One of the ways to enhance light absorption/emission in a semiconductor is to embed it in a microcavity (Fabry–Perot, photonic crystal, etc.) or a waveguide. So far, this has mainly been applied to graphene. Enhancement of photoluminescence (PL) in semiconducting MoS$_2$ and WSe$_2$ films coupled to photonic crystal cavities has also been demonstrated. More recently, strong exciton–photon coupling has been observed in a dielectric cavity containing synthesized MoS$_2$ layers, emphasizing the dramatic effect optical cavities may have on the properties of thin films. Here we demonstrate tunable external cavity devices where thin films are deposited on a planar distributed Bragg reflector (DBR) and the cavity is completed by another DBR having a concave shape. We show that in this mirror configuration it is possible to form cavity modes confined in three dimensions and having mode volumes as low as 1.6 $\mu$m$^3$ and quality factors, Q, up to 7400. This design allows tunability of the cavity size by adjusting the vertical displacement of the two mirrors and, therefore, allows spectral matching of the cavity mode wavelength with that of the emitter embedded in the device: we demonstrate wavelength tuning over 80 nm limited by the spectral width of the emitter only. We realize such devices for single atomic layers of molybdenum disulfide (MoS$_2$) and few monolayer thick gallium selenide (GaSe) films and observe major modification of the emission spectra and strong peak PL intensity increase compared with the same films but with the top mirror moved out of the optical path. Using time-resolved PL spectroscopy, we directly observe the Purcell enhancement of the spontaneous emission rate for films placed in the cavity by measuring a 10-fold shortening of PL lifetimes in GaSe films. The enhancement of the radiative rate is further confirmed in continuous-wave (cw) PL: we observe clear PL saturation at high powers for a GaSe film on a flat DBR and no saturation for PL of the same film inside a cavity. By performing finite-difference time-domain (FDTD) calculations, we show that the enhancement generally

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observed PL intensity enhancement is also due to the highly directional cavity mode emission having narrow angular distribution and enabling improved light coupling to the collection optics.

**Experimental Procedure.** Figure 1a schematically shows a tunable microcavity formed by a planar bottom DBR and a top DBR having a concave shape. Both mirrors have reflectivity exceeding 99% for the design wavelength of 650 nm and a stop band of 200 nm as shown in Figure 1b. The calculated electric field distribution inside the cavity in Figure 1c shows confinement of the mode in both vertical and lateral directions (see Supporting Information). Arrays of concave mirrors with different nominal radii of curvature, \( R_c \), from 5.6 to 25 \( \mu \text{m} \) are patterned using focused ion beam milling of a high flatness silica substrate (Supporting Information). Both the top and the bottom DBRs are fabricated by coating the substrates with 10 pairs of quarter-lambda SiO\(_2\)/TiO\(_2\) layers. Monolayer MoS\(_2\) and thin sheets of GaSe of thicknesses ranging from 30 to 100 nm have been obtained by mechanical cleavage of bulk crystals. GaSe films were deposited straight on the flat DBR substrate, whereas the MoS\(_2\) films were first deposited on a polymer and then transferred onto the flat DBR using standard transfer techniques. The thickness of the sheets was verified using atomic force microscopy.

Optical measurements were performed with the DBRs and samples placed at a temperature of 4.2 K. Both the flat and the concave DBR substrates were attached to XYZ nanopositioners. This permitted two types of PL experiments: (i) PL detection from the film on the flat DBR with the top DBR moved out of the optical path (the “half-cavity” configuration); (ii) PL from the films placed inside a full cavity, for which the top mirror was moved above the place on the film excited with the laser. Importantly, this experimental arrangement also permits control of the vertical cavity length, \( L_{\text{cav}} \), enabling wavelength tuning of the cavity modes as described with the following expression:

\[
\frac{1}{\lambda_{q,m,n}} = \frac{1}{2L_{\text{opt}}} \left[ q + m + n + 1 \frac{\pi}{\lambda_c} \text{arccos} \left( 1 - \frac{L_{\text{cav}}}{R_c} \right) \right]
\]

Here, \( q \), \( m \), and \( n \) are longitudinal (\( q \)) and transverse (\( m, n \)) mode numbers for Hermite Gauss cavities. \( L_{\text{opt}} \) is the effective optical length of the cavity, which differs from the physical length \( L_{\text{cav}} \) due to penetration of the cavity mode into the DBRs. In our case, \( L_{\text{opt}} = L_{\text{cav}} + 1.25 \mu\text{m} \), which is determined experimentally so that the mode wavelengths can be described with eq 1.

A laser diode at 532 nm and charge-coupled device were used for cw PL studies. For the time-resolved measurements a frequency-doubled pulsed titanium sapphire laser (at 415 nm) was used for excitation, and PL detection was carried out with a streak camera. The excitation laser was focused onto the sample with a lens having a focal length of 7.5 mm (lens 1 in Figure 1), resulting in a spot size on the film of 7 \( \mu\text{m} \). The PL was collected by the same lens and was focused outside the cryostat by another lens (lens 2 in Figure 1) in a fiber delivering light to the detection system.

**Results. Spectral Modification of PL by the Cavity.** Figure 2 shows low-T PL spectra for MoS\(_2\) and GaSe films excited by a 532 nm cw laser. Broad spectra are obtained for the films in the “half-cavity” configuration. Here an excitation power density on the film of 6.5 kW/cm\(^2\) was used for excitation, and PL detection was carried out with a streak camera. The excitation laser was focused onto the sample with a lens having a focal length of 7.5 mm (lens 1 in Figure 1), resulting in a spot size on the film of 7 \( \mu\text{m} \). The PL was collected by the same lens and was focused outside the cryostat by another lens (lens 2 in Figure 1) in a fiber delivering light to the detection system.

Monolayer MoS\(_2\) and thin sheets of GaSe of thicknesses ranging from 30 to 100 nm have been obtained by mechanical cleavage of bulk crystals. GaSe films were deposited straight on the flat DBR substrate, whereas the MoS\(_2\) films were first deposited on a polymer and then transferred onto the flat DBR...
MoS$_2$ (black) is shown together with the cavity emission for the top microcavity formed by placing the concave top mirror in the optical path. The narrow cavity modes are measured in PL when the blue lines show spectra measured for different longitudinal modes described in eq 1 with a multiplication factor used for the cavity mode PL. (b) PL of GaSe 43 nm film and cavity PL in resonance with the low energy shoulder of the GaSe spectrum. Both in (a) and (b), the PL intensity is presented in counts per second per square micron of the emitter (see text for explanation of normalization procedure).

Figure 2 shows PL spectra observed for 2D film emission in a cavity for the same laser excitation density of 6.5 kW/cm$^2$ incident on the film. The spectra with sharp peaks in Figure 2a show PL measured for a cavity with a MoS$_2$ monolayer. The strongest peaks around 675–680 nm correspond to longitudinal modes described in eq 1 with $m, n = 0$. The green, red, and blue lines show spectra measured for different top mirrors with nominal radii of curvature, $R_c$, of 16, 10, and 5.6 $\mu$m, respectively. The measured Q-factors for the strongest modes in the spectra are 4000, 3000 and 1800, respectively. PL from modes with $m, n \neq 0$ is also observed at shorter wavelengths.

For the full cavity having a concave DBR with $R_c = 16, 10$, and 5.6 $\mu$m, the intensity (in counts/s/$\mu$m$^2$) at the wavelengths corresponding to the mode PL peaks is greater than the MoS$_2$ monolayer PL by $\approx 10, 30$, and 60 times, respectively. Note that for each experiment one of the longitudinal modes was tuned in resonance with MoS$_2$ PL roughly at the same wavelength. For this, the vertical size of the cavity was adjusted to values varying from $L_{cav} \approx 1.9 \mu$m for the mirrors with $R_c = 5.6$ and 10 $\mu$m, and $L_{cav} \approx 2.9 \mu$m for the mirror with $R_c = 16 \mu$m. PL enhancement by a factor of 10 is also observed for the GaSe film in Figure 2b. Here a cavity with $L_{cav} \approx 4.2 \mu$m and a concave mirror with $R_c = 25 \mu$m was used, and a Q-factor of 3100 was observed.

By changing the distance between the two mirrors, and therefore the cavity length, the cavity resonance wavelength, $\lambda_{res}$, is tuned according to eq 1. In experiment, this is achieved by changing the voltage on the piezo element of the nanopositioner where the top DBR is attached. Figure 3 demonstrates the tuning for a cavity with a MoS$_2$ monolayer. It is seen that the cavity modes can be tuned over a range of about 40 nm by gradually changing the cavity length. The bright peak marked in the plot corresponds to a fundamental longitudinal mode with $q = 12$ for the optical cavity length of around $L_{cav} = 4.2 \mu$m. Apart from this mode, several other transverse modes with $m, n \neq 0$ are also visible. The emission of the MoS$_2$ monolayer is centered at around 680 nm, and the intensity of the cavity modes is enhanced when they are tuned past this spectral window. Using a similar pair of mirrors, we were also able to tune the modes around the emission window of GaSe down to $\approx 600$ nm. In general, the tuning is only limited by the size of the stop band, which is $\approx 200$ nm in our case (see Figure 1b).

Temporal Modification of PL by a Cavity: Purcell Enhancement. The PL enhancement observed in Figure 2 can arise as a combined result of angular redistribution of light emission and enhancement of the spontaneous emission rate (Purcell enhancement). Here direct evidence for the Purcell enhancement is obtained from time-resolved PL measurements on GaSe films by comparing the radiative lifetimes with and without the effect of the cavity. Figure 4a shows PL decay curves for a 43 nm GaSe film excited at 415 nm with a pulsed laser. In both half- and full-cavity configurations the time-averaged excitation density was 2.6 kW/cm$^2$. The cavity length is adjusted to $L_{cav} \approx 2.9 \mu$m (an $R_c = 10 \mu$m cavity is used) so that a longitudinal cavity mode is coupled into the low energy shoulder of the GaSe emission at 613 nm as in Figure 2b. As seen in Figure 4a, without the effect of the cavity, PL decay with a lifetime of $\tau_{sp} \approx 700$ ps is observed, whereas in the full-cavity configuration the PL lifetime $\tau_{sp} \approx 70$ ps (both times are obtained using fitting with monoexponential decay functions). This measurement signifies the enhancement of the spontaneous emission rate in the tunable cavity device.

Figure 4b presents further evidence for the enhancement of the radiative recombination rate in a microcavity. Here we show PL power-dependences of the 43 nm thick GaSe film in the half- and full-cavity configurations measured with a 532 nm cw laser. For the full cavity we use the same $L_{cav}$ and $R_c$ as for the time-resolved experiments. The plot shows integrated PL intensity calculated under the full-cavity mode spectrum centered at 613 nm and having a fwhm of 0.15 nm (red squares), and under the same bandwidth of GaSe PL at the same center wavelength in the half-cavity case (blue squares). The reduced transmission of the green laser through the top DBR is taken into account, and the data are plotted as functions of the actual laser power incident on the GaSe film. In the case of the half-cavity configuration, a clear sublinear PL intensity...
growth with power is seen. PL saturation is observed at around $P = 10 \text{ mW}$, indicating that the optical pumping rate exceeds the relatively low recombination rate $1/\tau_{\text{rec}}$ ($\tau_{\text{rec}} \approx 700 \text{ ps}$) of the localized exciton states in GaSe.\textsuperscript{29,30} In contrast to this, a much stronger PL increase with power is found for the cavity mode in the full-cavity configuration. No PL saturation is observed, indicating that the spontaneous recombination rate remains higher than the excitation rate in the whole range of powers used. This striking difference clearly indicates that the carrier radiative lifetime is markedly shorter in the case when the full cavity is formed,\textsuperscript{31} the effect quantified with the 10-fold PL decay time shortening in Figure 4a.

**Calculation of the PL Enhancement in a Cavity.** We start by estimating the PL enhancement due to increased directionality of the cavity mode toward the collection optics. For this the angular width of the fundamental cavity mode was calculated and compared with the radiation pattern for a dipole placed directly on the lower DBR but with no upper mirror using the FDTD technique\textsuperscript{32} (see Supporting Information for more details).

Figure 5 shows the simulated power radiated per unit solid angle in the far field for several mirror radii-of-curvature and separations as well as for the case without a top mirror. Only the upward flux is shown although the total flux radiated in all directions was calculated. We consider three cavities with parameters corresponding to the devices experimentally measured in Figure 2a: cavities C1, C2, and C3 are used having $R_c$ of 16, 10, and 5.6 $\mu$m and $L_{\text{cav}}$ of 2.98, 2.05, and 1.82 $\mu$m, respectively.

In Figure 5, it is observed that in the case when no top mirror is present, the PL is emitted in a broad range of angles, whereas markedly more directional distributions are observed for the three cavities. We estimate that for the light to be collected by the objective placed above the microcavity (lens L1 in Figure 1c), light should be emitted within a 16.7$^\circ$ cone. We then obtain that in the case where no top mirror is present only 9% of the total power is collected through the objective. We find that for the cavities C1, C2, and C3, the fractions of power within $\pm 16.7^\circ$ are 47%, 44% and 20% respectively. The marked lowering for the cavity with the smallest $R_c$ occurs because of scattering at the discontinuity between curved and planar regions of the top mirror (in the real cavity structures this discontinuity may be less sharp and its effect less pronounced).

We thus find, that compared to the case when no top mirror is present, “geometrical” PL enhancements with factors $F_P$ of 5.3, 4.9, and 2.2 occur in cavities C1, C2, and C3, respectively.

Further to the angular distribution, the FDTD method employed above can be used to calculate the Purcell enhancement factors, $F_P$, using the calculated values for $V$ and $Q$ (Supporting Information). We obtain the following Purcell factors for the three considered cavities: $F_{P1} = 41$, $F_{P2} = 59$, and $F_{P3} = 70$. We also calculate the Purcell factor $F_P = 51$ for the cavity used in the time-resolved measurements with $L_{\text{cav}} \approx 2.9 \mu$m and $R_c = 10 \mu$m. These values for $F_P$ are for the emitter in perfect spatial and spectral overlap with the cavity mode. These values of $F_P$ provide an upper limit to the Purcell factor achievable in a cavity. In the experiment, we deal with an inhomogeneously broadened ensemble of spectrally narrow emitters distributed in a few $\mu$m diameter area of a 2D film. This means that spatial and spectral averaging of the Purcell enhancement will occur and a value of $F_P$ lower than given above is expected\textsuperscript{33} as discussed in the next subsection.

**Discussion.** First we note that the effect of nonradiative processes needs to be taken into account for the interpretation of the experimentally measured data and comparison with the theory. Using a simple approximation, we will take into account only three processes: optical pumping, a nonradiative decay with a time $\tau_{\text{nr}}$, and a radiative decay with $\tau_{\text{r}}/F_P$ ($F_P = 1$ for a
bare thin film and $F_P > 1$ is expected for emitters in resonance with the cavity mode). The “state-filling” effects as observed in Figure 4b will be neglected. It is easy to show that the cw PL intensity $I_{PL} \propto \tau_{nr}/(\tau_{nr} + \tau_{P}/F_P)$ and the characteristic PL decay time $\tau_{nr} = \tau_{nr}(\tau_{nr}/(\tau_{nr} + \tau_{P}/F_P))$.

In our work, direct evidence for the Purcell enhancement is obtained for the GaSe film in Figure 4. It can be shown that the ratio of $\approx10$ of the experimentally measured $\tau_{nr}$ values in the half- and full-cavity configurations corresponds to the lower limit for the Purcell enhancement factor (reached if $\tau_{nr} \gg \tau_{r}$). The observation of the Purcell enhancement is itself an indirect evidence that $\tau_{r}$ is of the order or shorter than $\tau_{nr}$ for the localized excitons in GaSe.

In the case of MoS$_2$ monolayer films $\tau_{r}/F_P \gg \tau_{nr}$ for reasonable values of $F_P$. (We measure PL decay times of $\approx10$ ps for MoS$_2$ monolayer films in the half-cavity configuration.) In this case, nonradiative processes dominate, and the Purcell enhancement is not expected to be observable in time-resolved PL measurements. On the other hand, it is easy to show that in the absence of “state-filling” effects (as is the case for MoS$_2$) and for $\tau_{r}/F_P \gg \tau_{nr}$, the cw PL intensity $I_{PL} \propto F_P$ in a cavity. Taking into account the geometrical enhancement due to the more directional cavity PL emission into the collection optics, $I_{PL} \propto F_P F_{PL}$. By dividing the experimentally observed total PL enhancements of 10, 30, and 60, reported in Figure 2a, by the maximum expected $F_P$ of $\approx5$, we obtain the lower limit for the PL enhancements caused purely by the Purcell effect. Thus, for Figure 2a the lower limits for $F_P$ from $\approx2$ to $\approx12$ are estimated.

For cavities investigated in both the time-resolved and cw measurements, the calculated maximum Purcell enhancements in the range of 41–70, as found in the previous subsection, exceed those observed in the experiment. One of the reasons for this discrepancy is the lowering of the measured Q-factors from their calculated values occurring as a result of cavity imperfections. In our work the calculated Q-factors are $\approx2.5$ times higher than the measured values. Furthermore, in order to reflect the finite in-plane size of the mode and varied coupling to the mode of independent emitters at different wavelengths, spatially and spectrally averaged Purcell enhancement should be calculated.33 In general the averaged Purcell factors are lower than the maximum values for the perfect spatial and spectral emitter-mode overlap. The averaging procedure requires the summation of $I_{PL}$ (in the case of cw PL enhancement) or of the simulated PL decay curves (in the case of lifetime shortening) over the emitters in the ensemble. The total PL or average characteristic PL decay time may then be determined. However, the result is sensitive to the ratio ($\tau_{r}/F_P$) since both $\tau_{PL}$ and $I_{PL}$ depend on these parameters. At this stage, insufficient information exists about the nonradiative decay processes in 2D films for such averaging to be carried out accurately.

Conclusions. In conclusion, we report on fabrication of tunable dielectric microcavities confining the photonic field in all three directions and comprising 2D films of metal–chalcogenides and show that the films’ spectral and temporal PL properties are strongly modified by the cavity. We observe strong cw PL enhancement for MoS$_2$ and GaSe films placed inside the microcavity by up to a factor of 60 and directly measure the shortening of the PL lifetime in GaSe films by a factor of 10. Both cw and time-resolved observations provide evidence for the Purcell enhancement of the spontaneous emission rate in the studied cavities.

This work opens a route to a wide range of devices using 2D films and various van der Waals heterostructures as optically active materials. An advantage such devices would offer compared with traditional semiconductors is compatibility with a wide range of substrate materials including various dielectrics, polymers, and flexible substrates, permitting a wide choice of materials for fabrication of microcavities and waveguides.

Currently, the most advanced metal–chalcogenide heterostructures are built from exfoliated films, and the use of vertical cavity geometry in photonic applications is the most practical and advantageous, as the lateral device sizes are of the order $10–50$ $\mu$m only. Use of other geometries such as waveguide, widely employed in semiconductor lasers and modulators, will only be applicable for synthetic films with sizes as large as a few hundreds of micron or larger.

Finally, we note that excitons in transition–metal dichalcogenides (MoS$_2$, W$_2$S$_2$, etc.) also exhibit large binding energies and high oscillator strength and are therefore promising for observation of room temperature polariton effects,22 opening a new field of devices utilizing highly nonlinear optical phenomena and cavity QED in a new material system of van der Waals crystals.

■ ASSOCIATED CONTENT

5 Supporting Information

Additional details for the sample and device design and fabrication, further characterization data for the microcavities used in the experiments, and detailed account of the results of FDTD calculations of the optical modes in the external cavity devices used in our work. This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes

The authors declare no competing financial interest.

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