An improved measurement of the $2\nu\beta\beta$ half-life of $^{136}$Xe with EXO-200

J.B. Albert, M. Auger, D.J. Auty, P.S. Barbeau, E. Beauchamp, D. Beck, V. Belov, C. Benitez-Medina, J. Bonatt, M. Breidenbach, T. Brunner, A. Burenkov, G.F. Cao, C. Chambers, J. Chaves, B. Cleveland, S. Cook, A. Craycraft, T. Daniels, M. Danilov, S.J. Daugherty, C.G. Davis, J. Davis, R. DeVoe, S. Delaquis, A. Dobi, A. Dolgolenko, M.J. Dolinski, M. Dunford, W. Fairbank Jr., J. Farine, W. Feldmeier, P. Fierlinger, D. Franco, D. Fudenberg, G. Giroux, R. Gornea, K. Graham, G. Gratta, C. Hall, K. Hall, C. Hargrove, S. Herrin, M. Hughes, X.S. Jiang, A. Johnson, T.N. Johnson, S. Johnston, A. Karelion, L.J. Kaufman, R. Killick, S. Kravitz, A. Kuchenkov, K.S. Kumar, D.S. Leonard, F. Leonard, C. Liciardi, R. MacLellan, M.G. Marino, B. Mong, M. Montero Díez, D. Moore, R. Nelson, K. O'Sullivan, A. Odian, I. Ostrovskiy, C. Ouellet, A. Piepke, A. Pocar, C.Y. Prescott, A. Rivas, P.C. Rowson, M.P. Rozo, J.J. Russell, A. Sabourova, D. Sinclair, K. Skarpass, S. Slutsky, V. Stekhanov, V. Strickland, M. Tarka, T. Tolba, D. Tosi, K. Twelker, P. Vogel, J.-L. Vuillemier, A. Waite, J. Walton, T. Walton, M. Weber, L.J. Wen, U. Wichoski, J. Wodin, J.D. Wright, L. Yang, Y.-R. Yen, O.Ya. Zeldovich, and Y.B. Zhao (EXO Collaboration)

1. Physics Department and CEEM, Indiana University, Bloomington IN, USA
2. LHEP, Albert Einstein Center, University of Bern, Bern, Switzerland
3. Department of Physics and Astronomy, University of Alabama, Tuscaloosa AL, USA
4. Physics Department, Stanford University, Stanford CA, USA
5. Department of Physics, Laurentian University, Sudbury ON, Canada
6. Physics Department, University of Illinois, Urbana-Champaign IL, USA
7. Institute for Theoretical and Experimental Physics, Moscow, Russia
8. Physics Department, Colorado State University, Fort Collins CO, USA
9. Physics Department, University of Massachusetts, Amherst MA, USA
10. SLAC National Accelerator Laboratory, Stanford CA, USA
11. Institute of High Energy Physics, Beijing, China
12. Physics Department, University of Maryland, College Park MD, USA
13. Department of Physics, Drexel University, Philadelphia PA, USA
14. Physics Department, Carleton University, Ottawa ON, Canada
15. Technische Universität München, Physikdepartment and Excellence Cluster Universe, Garching, Germany
16. Department of Physics, University of Seoul, Seoul, Korea
17. Waste Isolation Pilot Plant, Carlsbad NM, USA
18. Kellogg Lab, Caltech, Pasadena, CA, USA

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We report on an improved measurement of the $2\nu\beta\beta$ half-life of $^{136}$Xe performed by EXO-200. The use of a large and homogeneous time projection chamber allows for the precise estimate of the fiducial mass used for the measurement, resulting in a small systematic uncertainty. We also discuss in detail the data analysis methods used for double-beta decay searches with EXO-200, while emphasizing those directly related to the present measurement. The $^{136}$Xe $2\nu\beta\beta$ half-life is found to be $T_{1/2}^{2\nu\beta\beta} = 2.165 \pm 0.016$ (stat) $\pm 0.059$ (sys) $\cdot 10^{21}$ years. This is the most precisely measured half-life of any $2\nu\beta\beta$ decay to date.

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I. INTRODUCTION

Nuclear $\beta\beta$ decay is a well known second-order weak transition which may occur in a number of even-even nuclei. The two-neutrino decay mode $(2\nu\beta\beta)$ has been directly observed in nine nuclei with half-lives ranging between $10^{18}$ and $10^{21}$ years [1,2], and half-lives as long as $10^{24}$ years have been established indirectly through radiochemical and geochemical means (see Ref. [2] for a review). Following Ref. [5], the $2\nu\beta\beta$ half-life $T_{1/2}^{2\nu\beta\beta}$ can be related to the nuclear matrix element $M^{2\nu}$ and the known phase space factor $G^{2\nu}$ according to

$$\frac{1}{T_{1/2}^{2\nu\beta\beta}} = G^{2\nu} g_A^4 m_e^2 |M^{2\nu}|^2$$

where $g_A = 1.2701$ and $m_e$ is the mass of the electron.
We see from eq. (1) that measurements of $2\nu\beta\beta$ half-lives effectively measure the $M^{2\nu}$ matrix elements for $\beta\beta$ source isotopes.

The interest in $\beta\beta$ decay is, of course, largely driven by the possibility of discovering lepton-number violation via the exotic neutrinoless mode ($0\nu\beta\beta$). The observation of the $0\nu\beta\beta$ decay would profoundly alter our understanding of the neutrino sector by demonstrating the Majorana nature of neutrinos and by providing information about the absolute scale of the neutrino mass spectrum.

Perhaps the simplest and most promising mechanism for the $0\nu\beta\beta$ mode is the virtual exchange of light but massive Majorana neutrinos. The half-life for the neutrinoless mode, when mediated by such massive Majorana neutrino exchange, is given by

$$\frac{1}{T_{1/2}^{0\nu}} = G^{0\nu}|M^{0\nu}|^2|\langle m_{\beta\beta} \rangle|^2$$

(2)

where $G^{0\nu}$ is the phase space factor, $M^{0\nu}$ is the nuclear matrix element, and $|\langle m_{\beta\beta} \rangle|^2$ is the effective neutrino mass. While the $G^{0\nu}$ are known for all nuclei of interest, the corresponding nuclear matrix elements need be calculated and have a substantial theoretical uncertainty [6]. Since the experimental data are available across a variety of complex nuclei, measurements of $2\nu\beta\beta$ half-lives provide an important challenge to all types of nuclear structure models and thus also to their ability to correctly evaluate the $M^{0\nu}$ matrix elements. Moreover, some authors have argued that, although the physics of the two $\beta\beta$ decay modes are quite different, nevertheless measurements of the $2\nu\beta\beta$ half-lives can constrain the particle-particle coupling constant $g_{pp}$ within the quasiparticle random-phase approximation (QRPA) [7]. This mitigates theoretical instabilities and uncertainties.

The $M^{2\nu}$ matrix elements are perhaps even more difficult to evaluate theoretically than $M^{0\nu}$ because the momentum transfer in $2\nu\beta\beta$ decay is comparable to the typical $Q$ value involved, whereas for $0\nu\beta\beta$ decay it is on average considerably larger. As a consequence, the $M^{2\nu}$ of the various nuclei are known to vary by up to an order of magnitude, whereas the $M^{0\nu}$ appear to be rather similar to each other. As a result, establishing or substantially constraining the $0\nu\beta\beta$ decay rate in a given nucleus allows one to project the corresponding rate in other nuclei.

Apart from these physics considerations, precise determinations of the $2\nu\beta\beta$ half-life, such as the one reported here, provide, to a large extent, a validation of the techniques that are also used for the measurement of the $0\nu\beta\beta$ decay and the exceedingly low backgrounds obtained in today’s experiments.

Among the several isotopes being most actively pursued for $\beta\beta$ experiments at the multi-kilogram scale and beyond, $^{136}\text{Xe}$ was the last to have its $2\nu\beta\beta$ decay observed [3] [4], in part because its small matrix element leads to a long half-life. In this article we report on a substantially improved measurement of the $2\nu\beta\beta$ half-life of $^{136}\text{Xe}$ by the EXO-200 experiment. EXO-200 has published results from two datasets, the first collected between May 21, 2011 and July 9, 2011 (Run 1), and the second collected between September 22, 2011 and April 15, 2012 (Run 2a). Run 1 data produced the first measurement of the $2\nu\beta\beta$ half-life of $^{136}\text{Xe}$ while Run 2a data placed a new limit on the existence of the $0\nu\beta\beta$ decay [5] in substantial tension with the observation claim reported in Ref. [9]. These results have been confirmed and complemented by KamLAND-Zen [4] [10].

In the interim period between Run 1 and Run 2a the EXO-200 front-end electronics were improved, the lead shield was completed, and the electronegative impurity content of the xenon was reduced by a factor of ten. Because of these improvements, the results presented in this article are based upon the more powerful Run 2a data set and take advantage of significant additional improvements to the event reconstruction methods, the Monte Carlo simulation, and a greater understanding of the detector response and behavior acquired since the publication of Ref. [5].

II. DETECTOR DESCRIPTION

A. EXO-200 detector

The EXO-200 detector has been described in detail elsewhere [11]. Here we review those features of the detector which are of particular relevance for the measurement of the $2\nu\beta\beta$ decay rate. We give special attention to the detector geometry, readout scheme, and shielding.

The centerpiece of the experiment is a liquid xenon...
The drift velocity is found to be 1.71 mm/s (see section VIII C), with the balance being composed mostly of $^{134}$Xe. LXe is a good ionizing radiation detection medium because it produces substantial ionization and scintillation signals. The LXe is housed in a cylindrical copper vessel of length $\sim 44$ cm and diameter $\sim 40$ cm, and is instrumented by two back-to-back TPCs which share a common cathode at the center of the vessel. The end caps of the vessel host identical detector packages, each of which consists of two crossed and segmented wire grids and an array of large area avalanche photodiodes (APDs) [12].

Energy deposits in the LXe produce free ionization charge and scintillation light (at 178 nm). The charge drifts along the axis of the detector towards the nearest end cap under the action of a uniform electric field, and the scintillation light is collected and measured by the APD arrays. Because the cathode has an optical transparency of 90% (at normal incidence), the scintillation light is detected simultaneously by both APD arrays while the ionization is detected only in the TPC in which it was produced.

When drifting ionization reaches the end cap detector package, it passes through the first wire grid, known as the shielding grid or induction grid, and is collected by the second wire grid which acts as the anode (see fig. 3). The shielding grid lies 6 mm in front of the anode while the APD array lies 6 mm behind it. Both grids are segmented and read out by charge sensitive preamplifiers. The amplitude of the charge collection signal on the anode wires measures the ionization energy. Because the grids are crossed at an angle of 60°, the anode and induction signals give measurements of two correlated spatial coordinates which we refer to as U (anode coordinate) and V (induction coordinate). We transform these coordinates into an orthogonal X-Y coordinate system, as illustrated in fig. 3. We refer to the anode as the U-wire system and the induction grid as the V-wire system.

The Z coordinate of the charge deposition (along the axial direction of the detector) is inferred from the product of the drift velocity and the drift time, where the start time is given by the prompt scintillation signal. The drift velocity is found to be 1.71 mm/s (see section VIII C), which agrees within 10% with previous measurements [13] at this drift field (374 V/cm from a three dimensional simulation). This field is achieved by setting the cathode, V-wire, and U-wire voltages to -8.0 kV, -780 V, and virtual ground, respectively, while the front face of each APD array is biased to $\sim (-1400$ V). This arrangement gives an electric field of 778 V/cm between the U and V wires, which is sufficient to ensure 100% charge transparency of the V-wires.

To reduce the channel count and attendant cabling mass, each wire grid is composed of 38 wire-triplets which were fabricated by photo-etching phosphor bronze sheet metal. Individual wires in each triplet have a roughly diamond-shaped cross-section with a full width of about 130 µm. The wire pitch is 3 mm, and because the wires are ganged in groups of three, charge readout channels have a 9 mm pitch, for a total grid width of 342 mm. The wire-triplets are mounted on acrylic beams which are connected to form a hexagonal shape. The optical transparency of each grid is 96% at normal incidence.

The distance from the U-wires to the cathode is 198 mm, giving a maximum charge drift time of 115.5 µs (see section VIII C). Each TPC has ten field-shaping copper rings mounted on acrylic “combs” which step down the cathode voltage to the V-wires and which ensure a uniform drift field in the bulk of the LXe. The voltage grading is achieved by a string of custom low-radioactivity 900 MΩ resistors. The inner side of the field rings and the resistor package are covered by 1.6 mm thick PTFE (Teflon) tiles capable of reflecting the 178 nm scintillation light.

Each detector package is backed by an APD array composed of 234 un-encapsulated silicon devices produced for EXO-200 using selected materials. Each device is circular with a diameter between 19.6 mm and 21.1 mm and an active diameter of 16 mm. The APDs are mounted in two hexagonal-shaped copper platters which provide a common bias voltage to the APD cathodes of -1400 V and -1380 V on the two detector sides. The APD anodes are provided a trim voltage, near ground, by their preamplifiers. The devices are hexagonally packed such that the sensitive area of each platter is 48% of the total endplate area. The interior side of each platter is covered by vacuum-deposited aluminum and MgF$_2$ to reflect...
VUV scintillation photons which do not strike the sensitive areas of the APDs. In each array one APD device is replaced with a PTFE diffuser which can be illuminated by an external laser pulser with a wavelength of 405 nm fed through optical fibers. This allows the response of the APD arrays to be periodically monitored. Ref. [12] describes the testing, performance, and selection of the APDs. The gain curve, noise, and relative quantum efficiency for each APD device was measured at LXe temperature as a function of bias voltage, and devices with similar gain characteristics were grouped together. The typical grouping is a gang of seven, although other groupings are also used. Each APD gang is monitored by a single charge sensitive preamplifier to reduce cabling material. The anode voltages of the gangs can be trimmed by as much as 100 V in groups of six channels. This allows the gains of the APD channels to be matched to within 2.5% with a nominal gain factor of 200. Each APD has a capacitance of 125 pF when biased at ~ (−1400 V), for a channel capacitance of about 1 nF. This leads to substantial but tolerable electronic noise in the front end (three gangs are disconnected due to excessive leakage current).

The charge sensitive preamplifiers for all three systems (U-wires, V-wires, and APDs) operate at room temperature outside the TPC and are connected to the detector by thin copper-clad polyimide flat cables. The flat cables penetrate into the xenon volume through custom-made epoxy seals.

The TPC vessel is fabricated from low-radioactivity copper and sealed via electron beam and TIG welding. To minimize the mass of the vessel, most of the copper is only 1.37 mm thick with stiffening features to bolster its mechanical robustness. We operate the TPC vessel at a nominal over-pressure of 8.1 kPa, and changes of more than 5.3 kPa activate a feedback system that restores the operating point by either removing or adding xenon. On the rare occasions when this occurs, the radon level and purity level of the xenon may be temporarily affected. To achieve and maintain good xenon purity with respect to electronegative contaminants such as oxygen and water, the xenon is continuously recirculated through two heated zirconium getters located outside the detector. Because the getters must act on the xenon in the gaseous phase, the LXe is evaporated, driven through the purifiers with a custom-designed xenon gas pump [13], recondensed outside and above the detector, and returned to the detector inlet through a vacuum insulated transfer line. We find that the purity of the LXe is closely correlated with the operation of this recirculation loop (see section VC2).

The installation of the detector is shown in Fig. 3. The TPC vessel is surrounded on four of six sides by a cosmic ray veto system. The entire assembly is located in a class 100 clean room which is surrounded on four of six sides by a cosmic ray veto system. The veto system consists of twenty-nine 5 cm thick Bicron BC-412 plastic scintillator panels obtained from the concluded KARMEN neutrino experiment [10]. Each panel is observed by eight photomultiplier tubes (PMTs) and is supported by 4 cm of borated polyethylene. The cleanroom laboratory is installed underground at the Waste Isolation Pilot Plant near Carlsbad, New Mexico, USA providing 1585 meters water equivalent of overburden [17].

An extensive materials screening and cleanliness campaign, described in Refs. [11, 18], was conducted during the design and construction phase of the experiment to ensure that the radioactivity of the detector would be suitable. Virtually all detector components inside the lead shield were custom fabricated for EXO-200. This effort was informed by a detector Monte Carlo simulation which predicted the background impact of each detector component. The enriched xenon itself was screened for noble gas and electronegative contaminants as described in Ref. [19].

B. Data acquisition

The fast data acquisition (DAQ) system for the EXO-200 detector integrates the readout of 226 hardware channels (76 U-wire signals, 76 V-wire signals, and 74 APD gang signals), muon veto panel output, and a high-voltage (HV) glitch detector into a single data stream. The veto system triggers asynchronously from the TPC.
when both instrumented ends of a panel record a hit within a 1 μs coincidence time window. The HV glitch monitor high-voltage transients with ∼μs duration.

Each TPC hardware channel is initially coupled to the DAQ via front-end electronics, consisting of a low-noise charge amplifier with a dual, two-stage (integration and differentiation) shaper followed by a 12 bit, 1 MS/s analog-to-digital converter. The particular values of the shaping times vary according to the type of channel (e.g. APD, U, or V). The digitized data is fed to a Trigger Electronics Module (TEM), which synchronizes the data from all hardware channels and forms detector triggers. The TEM also incorporates data from the muon veto panels and the HV glitch detector.

For the muon veto, the 2 light read-out channels for each panel, each instrumented with four PMTs, are fed into a discriminator module, which supplies a bit pattern of the panels above threshold. A valid muon trigger, both ends of any one panel are required to be simultaneously above threshold to reduce the random trigger rate. A secondary, ADC/TDC-based electronics system is available, allowing the monitoring of panel stability with detailed semiannual 60Co source calibration scans of the panels.

In the case of a trigger condition, data is written from the TEM to a control computer to be stored on disk. Muon veto or glitch detector events only initiate transfers of those particular types of records; these are later synchronized to TPC data by means of their time stamps. If a TPC trigger occurs, the TEM transfers digitized data for all 224 hardware channels for sample times starting 1024 μs before the trigger and ending 1024 μs after it. During a normal physics run, there are four types of TPC triggers used, with rough thresholds noted in parentheses: (a) individual U-wire trigger for LXe γ and β events (∼100 keV), (b) APD individual trigger for activity inside the respective APDs (∼3−4 keV), (c) APD sum trigger for LXe α events (∼25 000 photons), and (d) solicited (forced) trigger at 0.1 Hz, for monitoring detector performance. Further information on the DAQ system may be found in [11].

C. Data processing structure

The processing of data follows a tiered scheme for each run:

1. Tier 0 → Tier 1, “Rootification” : conversion of binary data files to ROOT files; low-level verification of data validity.
2. Tier 1 → Tier 2, “Reconstruction” : first two reconstruction stages, see section [IV] noise and muon taggers; calculations of waveform characteristics.
3. Tier 2 → Tier 3, “Processing” : final reconstruction stage (“clustering”), see section [IVD] data corrections (e.g. gain, grid, and purity), see section [V]
4. Tier 3 → Standard analysis scripts, “Trending” : extraction of parameters from a run (e.g. noise, threshold, etc.) useful for tracking trends over time.

D. Data analysis strategy

As expected from the materials screening campaign, we find in the data that the primary backgrounds to 2νββ in EXO-200 are gamma and beta interactions due to trace quantities of 40K, 232Th, and 238U in the detector materials. We separate these backgrounds from 2νββ candidates by taking advantage of the detector’s good energy and position resolution and its ability to perform pattern recognition. First, we label an event as being “single-site” (SS) if it is consistent with having all charge deposits confined to a single volume with a characteristic dimension of ∼2−3 mm, as expected for most 2νββ events in LXe. Otherwise the event is labeled as “multi-site” (MS). Due to the predominance of the Compton scattering process in the energy range of interest (700 keV to 3500 keV), gamma events are mostly categorized as MS as they commonly produce two or more localized charge deposits separated by at least several centimeters in LXe. Second, we calculate for each event the “standoff distance”, or the shortest distance between the various charge depositions to an anode wire or reflector surface. Gamma events and 2νββ events have distinguishable standoff probability distributions because the latter are uniformly distributed in the LXe whereas the former tend to originate in the passive detector materials and exhibit some attenuation in a detector of the size of EXO-200. Third, we measure the total energy of each event by combining the charge and scintillation signals in a manner which takes advantage of the anti-correlation between these channels to improve the energy resolution [21]. This last procedure is essential for the search for 0νββ, where the signal is a resolution-limited feature at the Q value, but is also utilized in the present measurement of the 2νββ decay.

We exploit these three variables by selecting fiducial β-like events in the data, dividing them into the SS and MS categories, and performing a simultaneous maximum likelihood fit to the energy spectra and standoff distance of both event samples. The probability distribution functions (PDFs) provided to the fit are determined by a Monte Carlo simulation of the relevant signal and background sources. This strategy is validated by comparing data and simulation for calibration sources of known activity which are periodically inserted near the detector.

In the following we describe the Monte Carlo simulation (section [III], event reconstruction (section [IV]), calibration and energy measurement (section [V]), simulation-measurement agreement (section [VI]), data quality selec-
FIG. 4. (Color online) Visualization of the simulated TPC vessel and internal copper components.

III. MONTE CARLO SIMULATIONS

The EXO-200 Monte Carlo simulation software is split into two independent components. The first component, developed within the GEANT4 simulation package [22], parameterizes the geometry of the EXO-200 detector and surroundings. The second stage uses the output from the first component – energy depositions within the simulated detector – to calculate electronic signals. The data format produced by this process is identical to that of real data and may be processed through the Tier 1 and Tier 2 reconstruction and analysis chains described in sections II C and IV.

A. Simulated geometry

The simulated geometry implements a detailed description of the TPC and its internal components and includes the surrounding HFE, cryostat and lead shield. 3-D computer-aided design (CAD) models of the detector are used and coded using GEANT4 shape primitives, as illustrated in fig. 4 for the copper components of the inner detector. An approximate geometry is used for the shape of some complex components, so a check is made to verify that the mass of materials is accurately reproduced, as shown in table I for the materials shown in fig. 4.

| Component            | Quantity | CAD Mass (kg) | GEANT4 Mass (kg) |
|----------------------|----------|---------------|------------------|
| Outer Cryostat       | 1        | 3453          | 3364             |
| Inner Cryostat       | 1        | 2843          | 2575             |
| Total Cryostat       |          | 6296          | 5939             |
| Source Tube          | 1        | 0.533         | 0.207            |
| TPC Leg              | 1        | 6.979         | 6.944            |
| HV Feed              | 1        | 0.491         | 0.303            |
| LXe Vessel           | 1        | 22.36         | 22.32            |
| APD Frame            | 2        | 3.144         | 4.440            |
| Wire Support         |          |               |                  |
| Ring                 | 2        | 2.659         | 1.468            |
| Field Ring           | 20       | 3.055         | 3.240            |
| Cathode Ring         | 1        | 0.721         | 0.728            |
| Dummy                |          |               |                  |
| Cathode Ring         | 1        | 0.323         | 0.327            |
| Total TPCs           |          | 32.753        | 32.826           |

TABLE I. Comparison between copper mass in the detector CAD model and GEANT4 model. The two models have independent implementations, and differences are understood to be due to simplifications in the GEANT4 geometry. Although these distinctions could lead to minor differences in gamma attenuation between data and simulation, this effect is expected to be small and is cross-checked by external gamma calibration source data (see section VI).

B. Simulated signal generation

The signal calculation for wire channels employs a two-dimensional (2-D), simplified geometry which assumes that U-wires and V-wires are parallel to one another, infinitely long, and perpendicular to the plane of calculation. In addition, in this configuration the V-wires lie directly above the U-wires in the Z direction. For this setup the weighting potential, \( \phi(\vec{x}) \), and electric field, \( \vec{E}(\vec{x}) \), have been calculated using Maxwell 2D [23], which allows one to model drifting charge at any location in the detector and calculate the resulting induced signal using the Shockley-Ramo theorem [24]. In this method, the charge induced on a wire by the movement of charge, \( q \), from \( y_0 \) to \( y \) is given by \( q(\phi(y) - \phi(y_0)) \), where \( \phi \) is the weighting potential for the particular wire. The weighting potential for a single U-wire channel along with example charge drift trajectories are shown in fig. 5. Charge diffusion during the drift is not modeled in this calculation. This does not significantly affect the quality of the simulation as the larger effect of transverse charge diffusion in LXe at the field used here (see e.g. [25]), produces an RMS spread of \( \sim 2 \) mm to be compared with the 9 mm wire readout pitch. The effect of longitudinal diffusion was observed when taking low-electric field...
data as it lengthened the U-wire pulse rise-time. However, this effect becomes negligible at the nominal electric field. Once signals are calculated, they are shaped with the appropriate channel transfer function. For Monte Carlo simulation production runs, white noise is added to the signal waveforms, though there exists the possibility to add real noise using event traces from solicited triggers.

To determine if the 2-D geometry is a valid approximation to use, waveform characteristics were calculated and compared for simulated wire signals and for data from a $^{238}$Th source run. In particular, the rise-time of the pulses and the time difference between maximum and minimum are calculated, (see section IV C 2). The results of this study are shown in fig. 6, where it is clear that signal generation well reproduces the distributions from data.

In addition, a fully three-dimensional (3-D) COMSOL finite element calculation was used to produce a 3-D electric field and weighting potentials for the 76 wire channels populating a single TPC at the proper 60° angle between U and V grids. Although this model is currently too slow to be used in Monte Carlo simulation production runs, calculations from it have been used during fiducial volume studies of the detector, in particular to help understand regions near the edge of the wire grid where the field configuration is complex. Results from a similar study of waveform characteristics of traces generated from this model are included in fig. 6. A comparison of the two calculations show the 2-D model to provide a valid approximation of the charge collection.

The signal generation for APD channels uses a parameterized light response function which returns the expected amount of light hitting both APD planes given a charge deposition at a given location in the detector. The light response function was derived from a Monte Carlo study of light collection in the TPC which included geometric factors, reflectance, and scattering. Effects from the anti-correlation between the ionization and scintillation (see section V D) are not simulated. The resulting unshaped APD pulse shapes are assumed to be step functions, a valid assumption given that the integration time of the APD electronics transfer function (∼1 μs) is much longer than the intrinsic APD rise-time (10-100 ns). As with U- and V-wires, these unshaped pulses are transformed with the appropriate electronics transfer functions and white noise is added.

IV. EVENT RECONSTRUCTION

Event reconstruction is the process by which waveforms are analyzed to derive information such as energy content and topology of events. The reconstruction of an event has three stages:

1. Signal finding
2. Signal parameter estimation
3. Clustering, or assembling of found signals to determine event topology

The following terminology is used in this section: a “signal” refers to a hit which is reconstructed on a particular channel, a “bundle” is a group of signals from a single channel type, and a “cluster” is a set of bundles which have been associated together to determine the event position.

A. Signal models

Signal shape templates are used extensively in reconstruction in both the signal finding and parameter extraction stages and are produced for all channels. In the case of U- and V-wires, unshaped signals are generated using the signal simulation described in section III B. A simple step function is used for APD channels. Unshaped waveforms are then filtered using the appropriate transfer function to create the final signal template shape for a given channel. Transfer functions are defined by the front-end electronics (see section II B), resulting in 3 differentiation (one stage from the preamplifier) and 2 integration stages. The values for these stages for each channel type are given in table I. It is important to note that the value of the third differentiation stage of the U-wires is a measured parameter and varies for each U-wire channel. Using the measured value for each channel was found to improve the fits used to determine signal heights (section IV C) which lead to an improved detector resolution.
FIG. 6. (Color online) Comparison of the distributions of the pulse rise-time (a) and maximum-to-minimum time (b) on U-wires between calibration data and simulations using 2-D and 3-D field maps (see section IV C 2) for $^{228}$Th data. The long tail in the rise-time distribution is due to Compton scatters. Only wire signals above 200 keV are compared, as the values of rise-time and maximum-to-minimum time for low-amplitude signals depends strongly on the waveform noise profile. The distributions are normalized to the same total number of events for comparison.

| Channel Type | Stage type | Integration | Differentiation |
|--------------|------------|-------------|-----------------|
| APDs         | 3          | 3           | 10              | 10              | 300             |
| U-wires      | 1.5        | 1.5         | 40              | 40              | 51 – 85 (nominal 60) |
| V-wires      | 3          | 3           | 10              | 10              | 60             |

TABLE II. Shaping times (all in $\mu$s) relevant to the transfer functions of different channel types. The third differentiation stage for the U-wire signals is measured for every channel by fitting to pulse shapes from charge injection data.

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B. Signal finding

It is necessary to search for signals on waveform traces because they are not always guaranteed to arrive at a given time (e.g. specified by a trigger). Two methods are used to find signals on waveform traces: applying a matched filter, and waveform unshaping. The second method is used to identify pulses closely following one another within a signal found by the matched filter.

1. Matched filter

A matched filter is used to find signals due to its simple algorithmic implementation and because it has been observed to produce stable performance over time in varying noise conditions. The filter (see, e.g. [27]) is applied in Fourier space,

$$y(t) = \hat{s}^{-1}\{X(f)H^*(f)\}$$

where $y(t)$ is the filtered signal, $\hat{s}$ is the discrete Fourier transform (FT), $X(f)$ is the FT of the original waveform, $x(t)$, and $H^*(f)$ is the complex conjugate of the FT of the transfer function, $h(t)$, for the particular channel. For APD channels, eq. (3) is further divided by the noise spectrum of the channels to whiten the spectrum. This is not performed for U-wire channels as the additional division was found to broaden the signal due to the longer U-wire shaping times, detrimentally affecting subsequent peak finding. V-wires also have no additional noise division.

U- and V-wire channels are filtered by applying the template model defined for each respective channel. APD channels, in contrast, are first assembled into two sum waveforms generated by summing together the waveforms from all channels on each APD plane. This results in two waveforms, each of which is then filtered using eq. (3) with the APD transfer function. An example of a waveform before and after filtering is shown in fig. 7. A peak-search algorithm is performed on the filtered waveforms, looking for amplitudes exceeding a certain threshold. This threshold is calculated for each waveform on an event-by-event basis to reduce the sensitivity to channel- and time-based noise variations. The algorithm proceeds by first determining the mean absolute deviation (MAD), of the waveform from its baseline, removing all parts of the waveform exceeding $(3\sqrt{\frac{2}{\pi}}) \times$ MAD, and then recalculating the MAD. This is equivalent to removing values greater than $3\sigma$ if the deviations from the baseline are normally distributed. The threshold is defined as $5(4)$
times this final MAD for wire (APD) signals.

2. Waveform unshaping

Since the matched filter is designed to find single pulses, it is ill-suited to disentangle multiple signals on a single trace when these signals arrive close to one another in time. Hence a dedicated algorithm is applied to the original waveforms after they have been identified by the matched filter. This algorithm “unshapes” the signal, obtaining the original charge deposited $q(t)$:

$$q(t) = \mathcal{F}^{-1} \{ H^{-1}(f)X(f) \}$$

(4)

with the same definitions as given for eq. (3), where $H^{-1}(f)$ is the inverse transfer function. This process is very sensitive to inaccuracies of the transfer function used due to inexact pole-zero cancellation. Detailed studies show that the procedure works best on a short (265 $\mu$s) interval centered around the pulse time found by the matched filter. $q(t)$ is subsequently reshaped with a 2 $\mu$s triangular, or moving average, filter (see e.g. [28]). The reshaped waveform is then analyzed with a peak-search algorithm to determine the presence of any additional signals.

C. Parameter estimation of signals

1. Amplitude measurement

The amplitudes of all U-, V-, and APD sum signals are measured by fitting the waveforms to their respective signal models (see section IV A). A $\chi^2$ function is built using the signal model, the data, and the output of the previous signal-finding stage:

$$\chi^2 = \sum_{l=0}^{L} \left[ \frac{x_l - b - \left( \sum_{i=0}^{N} \{ A_i f_{SM}(x_l, t_i) \} \right)}{\sigma^2_{\text{noise}}} \right]^2$$

(5)

where $x_l$ is the data sample at time $l$, $b$ is the measured baseline, $i$ is the index of the $N$ signals on the waveform, $A_i$ and $t_i$ are the amplitude and time of the $i^{th}$ signal, and $f_{SM}$ is the signal model. The baseline and the RMS noise $\sigma_{\text{noise}}$ are calculated and fixed for each waveform. $A_i$ and $t_i$ are the only floating parameters, and the values estimated during the signal fitting stage are used as initial input. The size of the fit window, $L$, extends $\pm 40 \mu s$ around the signal (defined in the finding stage). In the case of U-wires, the upper fit window limit is extended to 140 $\mu$s to include the longer undershoot induced by the larger differentiation times in the U-wire transfer functions. When multiple signals are found on the waveform traces, the fit windows are determined for each signal and combined. In the case of signals further apart than the 40 (or 140) $\mu$s, several separated fit windows are produced. An example of fits to U and V waveforms is given in fig. 8.

The $\chi^2$ function is minimized using MIGRAD [29], resulting in signal amplitudes, times and errors, in addition to the overall value of the minimized $\chi^2$ function. Before the fitting stage is completed, the results of the fits to the two APD sum signals are used to then fit individual APD gang channels separately and extract the amplitudes of each gang channel. The $t_i$ parameters from the fits to the two APD sum signals are used as input to eq. (5), but these values are fixed during the subsequent fit; only the amplitude parameter(s), $A_i$, are allowed to float when fitting the gang signals.

2. Waveform characteristics

In addition to the pulse characteristics derived from the waveform fits, several metrics are calculated directly from the U-wire waveforms for use in pulse-shape-based discrimination between “collection” and “induction” signals. In this sense, we define induction signals on U-wires as signals that occur when charge drifts close enough to
FIG. 8. (Color online) Examples of fits to a U-wire (a) and V-wire (b) on an expanded vertical scale. One can see that the V-wire peaks earlier than the U-wire signal.

A channel to induce a signal, but does not deposit on that channel. These induction signals must be corrected for so that they are not mistakenly reconstructed as a low-energy charge cluster (see section [IVD]), causing a single-site topology event to be interpreted as a multi-site event. This has particularly important implications for event classes that are predominantly SS (e.g. $0\nu\beta\beta$ and $2\nu\beta\beta$) and would be mistakenly classified as MS with a loss of efficiency.

The following discriminants are calculated:

1. Pulse timing:
   (a) The rise time of the pulse, measured from the last time the pulse crosses a minimum threshold (set to 10% of the pulse height above the baseline) to the first time the pulse crosses a maximum threshold (at 95% of the pulse height above the baseline)
   (b) The time from the pulse maximum to the following pulse minimum, defined similarly as the time between the last crossing of a maximum threshold (90% of the pulse height, measured from the pulse minimum) and the first crossing of a minimum threshold (10% of the pulse height above the pulse minimum)

2. Pulse integral: The pulses are unshaped using inverse transfer functions (see section [IVB2]), and the integral of the pulse is calculated in a window within 10 $\mu$s before and 40 $\mu$s after the pulse maximum.

3. Fit $\chi^2$: Following the standard fitting procedure for U-wire signals described in section [IVC], the same signal finding and fitting procedure is repeated for each U-wire waveform using a signal template describing a U-wire induction signal instead of the standard collection template. The fit $\chi^2$ value is then calculated for fits to both the collection and induction signal templates in a time window restricted to 20 $\mu$s before and 30 $\mu$s after the signal.

4. Nearest-neighbor amplitude: For each U-wire signal, the total energy on neighboring channels within 50 $\mu$s is calculated (U-wire induction signals reconstructed as collection signals have poor time estimations due to the template mismatch.)

Distributions of these discriminants are given in fig. 9, comparing the values for induction signals and collection signals. A full discriminator is built from a combination of these values to ensure the collection efficiency for collection signals with at least 250 keV of deposited energy is $>99.9\%$. With the chosen cut, the rejection efficiency for U-wire induction signals is 77%, integrated over the $2\nu\beta\beta$ energy spectrum. Since signals identified as induction by these selection criteria are required to have an energy deposit on a neighboring channel of $>1000$ keV, no events can be forced below the 700 keV analysis threshold due to removal of misidentified collection signals. These efficiencies were calculated using Monte Carlo studies.

**D. Signal clustering**

Once the time and amplitude of signals on U-, V-, and APD channels have been found and properly gain corrected (see section [IVB]), these signals are grouped together to form 3-D “clusters”. Since signals from different channels arising from the same charge deposit will have correlated characteristics (e.g. amplitudes and times), these characteristics can be used to guide the clustering process that proceeds in a step-wise fashion. First, signals of like channels are associated together (U-wires with other U-wires, etc.) in a process called bundling. U-wire signals identified as due to induction, using the criteria described in section [IVC2], are ignored when constructing bundles. The Z positions of these bundles are then determined by associating them with APD bundles. Finally these wire bundles are grouped together to form fully 3-D reconstructed clusters.

1. **Signal bundling**

U-wire signals on adjacent channels arriving close in time (within 3.5 $\mu$s) are bundled together. The time of
FIG. 9. Distributions of the discriminants described in the text used to identify induction signals, calculated for waveforms generated from $^{228}$Th Monte Carlo simulations. The distribution of these values for all U-wire signals is shown as the solid histogram, with the cuts used for each value denoted by the vertical dashed lines. U-wire signals must satisfy all cuts to be identified as “induction-like” signals. The cuts are chosen to ensure minimum impact on collection signals (acceptance efficiency > 99.9%), corresponding to a rejection efficiency of induction signals of 77%, integrated over the $2\nu\beta\beta$ energy spectrum. Also shown are the distributions of simulated induction pulses which were not identified as induction-like by the cuts (“Not identified”) and simulated pulses containing at least some deposition, but which were identified as induction-like (“Some deposition”).

each bundle is defined by the amplitude-weighted average of the associated signals. V-wire signals are also bundled according to time, using to the relationship:

\[ |t_i - t_0 - (2.97 \, \mu s/\text{chan})\Delta V| \leq 4.5 \, \mu s \]  

where $t_0$ is defined by the V channel with the largest amplitude, $t_i$ is determined from the V channel of interest, and $\Delta V$ is defined as the absolute channel number difference of the two signals. For example, for two V-wire signals occurring on channel 39 and 37, $\Delta V$ would be 2. This is because “outer” V signals are reconstructed earlier in time than the “central” (largest-amplitude) V-signals and the arrival time difference grows roughly linearly with the number of channels between the signal and the central signal. This occurs because the V-wire channels further from the drifting charge become shielded by the nearby wires as the charge nears the V-wire plane. In contrast to U-wire bundles, only the time of the largest V-wire signal is chosen as the time of the whole V-wire bundle; no weighted average is performed. Using the weighted time average in the V-wire bundle has been found to dilute the time correlation between U-wire and V-wire bundles.

The bundling of APD signals is performed solely based on time, associating signals if they arrive within 6 $\mu$s of one another, with the timing defined by the sum of the integration times in the APD electronics (see table II). When multiple APD signals are grouped to form a scintillation bundle, the time of the scintillation bundle is calculated by performing the weighted average over the time and energy of the component signals.
2. Determining two-dimensional (2-D) position

A determination of the 2-D event position is achieved by grouping together U- and V-wire bundles in their most likely configurations to generate charge “clusters.” The clustering stage employs probability density functions (PDFs) that describe how likely it is that a particular U-bundle is associated with a given V-bundle. There are three PDFs to: (1) describe the time difference between U- and V-bundles, (2) describe the consistency between the sum of signal amplitudes in the U- and V-bundles, and (3) ensure the resulting (U,V) coordinate is physically allowed (not all U- and V-wires intersect one another because of the hexagonal shape of the grid frame). These PDFs are described in more detail in appendix A.

The PDFs used to cluster U- and V-wire bundles together are dependent on the Z position of the U-bundle. To calculate them, an associated scintillation bundle is found in the following way: from all scintillation bundles that occurred between 3 $\mu$s after and 3 $\mu$s plus the maximum drift time before the U-wire bundle, the one scintillation bundle with the smallest absolute time difference from the U-wire bundle is chosen. The expansion of the search window on both sides by 3 $\mu$s is again given by the integration times of the APD transfer functions. If no scintillation bundle lies in that time range, the Z position is set as undetermined and the particular U-/V-bundle will not be further clustered.

The negative log of the product of the three PDFs described above defines a test metric, the “cost,” which is used as a measure of how well a U-bundle matches a V-bundle. This may be translated into the following expression:

$$\text{cost} = \sum_{i=1,2,3} -\ln P_i$$

(7)

where the sum is over the three PDFs. A lower cost indicates a better match, or a higher likelihood for a given configuration. The matching algorithm rigorously tests all combinations of the V and U-bundles with one another, including whether or not multiple bundles of one type may actually correspond to a single bundle of the other type. The best matching configuration is the one for which the sum of the cost divided by the number of connections is minimal, where the number of connections is defined as the smaller of the number of U-bundles or V-bundles. Once this has been determined, a charge cluster is created for each of the connections within the matching configuration and each charge cluster is linked with its associated scintillation bundle.

It is possible that clustering fails to associate one or more of the U-, V-, or APD bundle types together, resulting in a cluster without full 3-D position. This may occur due to a clustering error or because signals are not found because they are below threshold. This produces an associated error on the $2\nu\beta\beta$ measurement, which is quantified in section VIII D. It is also possible for clustering to skip an event completely if too many signals are found. This may introduce an error on the $2\nu\beta\beta$ efficiency if reconstruction mistakenly finds too many signals and these events are then ignored. However, the total number of skipped events is < 0.18% of the final $2\nu\beta\beta$ counts. We choose to assign an additional 0.18% error on the $2\nu\beta\beta$ measurement to account for the possibility that events are mistakenly skipped by the clustering stage in reconstruction.

To determine the analysis threshold, the efficiency to find a signal on the three types of channels (U-wire, V-wire, and APD) was studied versus deposition energy. The three types of channels exhibit efficiencies with different dependencies on deposition energy as well on position. An analysis threshold (700 keV) was chosen where all channel types demonstrated 100% signal-finding efficiency independent of the event deposition position.

V. CALIBRATIONS AND CORRECTIONS

A. TPC source calibrations

$^{137}$Cs, $^{60}$Co, and $^{228}$Th sources are utilized to calibrate the TPC response to gamma radiation. The sources have been selected to span the energy range of interest. The source activities, listed in table III, were chosen to collect calibration data quickly while not saturating the DAQ system. The $^{228}$Th source is deployed every few days to a position near the cathode to monitor the electron lifetime and measure the energy response. Occasionally all three sources are deployed in series to other positions around the TPC vessel for comprehensive calibration studies. These positions are shown in fig. 10.

![FIG. 10. The calibration source locations around the TPC vessel as viewed from above. The XYZ coordinates of the source locations are: S2 = (0.0, 0.0, -29.5 cm), S5 = (25.5 cm, 0.0, 0.0 ), S8 = (0.0, 0.0, 29.5 cm), and S11 = (0.0, 25.5 cm, 0.0). Not shown: S17 = (0.0, -25.5 cm, 0.0).]
TABLE III. EXO-200 calibration sources. The activities shown here are referenced to September 1, 2009 and were verified by gamma-ray spectroscopy within the collaboration. Other sources with greater activity are also available for deployment.

| Source   | Activity (Bq) | Half-life (years) |
|----------|---------------|-------------------|
| $^{60}$Co | 530 ± 6       | 5.27              |
| $^{137}$Cs | 2820 ± 33    | 30.1              |
| $^{228}$Th | 1417 ± 17     | 1.91              |

B. TPC channel-based corrections

The absolute U-wire channel gains were measured prior to Run 2a using a pulser coupled to the front-end electronics through a precision (1%) capacitor. The gain value, measured in units of electrons per ADC count, is calculated by a linear fit to the measured amplitude versus the injected charge. The stability of the gain values is monitored daily using a charge injection circuit which is integrated into the front-end card. This daily charge injection run is also used to monitor the time constant of the third differentiation stage of the preamplifier (see table II).

The relative U-wire gain values are also determined with $^{228}$Th source calibration data using the pair-production peak of 2615 keV gammas. The resulting channel-to-channel gain values are strongly correlated with those determined from the charge injection runs, as expected. The mean gain is $\sim 380$ electrons/ADC unit, with 30% variation over all channels. The observed drift of the U-wire gains is $< 1\%$ over the Run 2a dataset, with $< 0.1\%$ relative channel-to-channel drift. For the $2\nu\beta\beta$ half-life measurement the gain values determined from the pair-production peak are used.

The V-wires are not directly used in the energy measurement, but variations in their relative gain can affect position reconstruction and clustering. We correct for these variations using the precision pulser charge injection data. The V-wire gains as determined from these calibrations are found to vary from 300 to 360 electrons per ADC count. These gain values are accurate within 2–3%.

The APD channel gains are monitored periodically using the external laser pulser. The observed channel-to-channel gains vary by 12%, and the time variation is 1% over the Run 2a dataset. However, for the $2\nu\beta\beta$ half-life measurement, the APD signals are corrected on a channel-by-channel basis, as gain variations are absorbed in the light map correction described below.

C. TPC position-based and time-based corrections

1. APD light map

The amount of scintillation light collected by the APDs depends on the location of the energy deposition. This variation is caused by differences in the solid angle covered by the APDs and by their gain differences. 3-D correction functions are used to account for this position dependence. Such correction functions are generated from $^{228}$Th calibration runs with the source placed at the two anodes and three positions around the cathode plane. The detector volume is divided into 1352 spatial voxels (13 radial bins, 8 azimuthal bins, and 13 Z bins). The bin widths are chosen to ensure adequate statistics, and to optimally map the response in the regions with a high light collection gradient.

The light map is normalized such that the mean response is 1. A continuous correction function, $f(r, \phi, z)$, is created with a trilinear interpolation between the centers of the voxels in the light map.

Because maintenance was performed on the APD front-end boards in the middle of Run 2a, two light maps are used for this data. The first light map covers the period from October 1, 2011 until February 20, 2012, and the second covers the period from February 20, 2012 until April 15, 2012. Some representative sections of the first light map are shown in fig. [11].

For a SS event, the correction function is applied by multiplying the sum of the two APD plane signals by $1 / f(r, \phi, z)$, while for a MS event, a correction factor is deduced by taking the appropriate charge-cluster energy-weighted sum. The light map correction function improves the scintillation-only energy resolution at 2615 keV from 7.9% to 6.0% for SS events and from 8.1% to 6.3% for MS events, respectively. The largest correction factor within the fiducial volume is $\sim 15\%$ (the fiducial cut near the cathode eliminates the region of the detector that sees the largest gradient in the correction function).

2. Electron lifetime correction

Electrons drifting in LXe can be captured on electronegative impurities leading to an exponential decrease with time. This attenuation is described by

$$N_c(t) = N_0 \exp(-t/\tau_e) \quad (8)$$

where $N_0$ is the original number of electrons, $\tau_e$ is the electron lifetime, and $t$ is the drift time. We correct for this attenuation by measuring the electron lifetime every few days using the $^{228}$Th source deployed near the cathode. We divide the data in each TPC into 16 drift time bins and fit a Gaussian plus error function model to the full absorption peak in each bin. The central value of the
The light response function \( f(r, \phi, z) \) from September 22, 2011 until February 20, 2012 is shown here indicated by the color coding. For both plots the correction factor ranges from 0.70 (blue) to 1.19 (red). Panels (a) – (h): the function evaluated at 8 discrete values of the azimuthal angle \( \phi \) over the full range of \( r \) (horizontal axis, \( 0 \) mm < \( r < 168 \) mm) and \( z \) (vertical axis, \( -192 \) mm < \( z < 192 \) mm). Panels (i) – (q): the function evaluated at 9 discrete values of \( z \) over the full range of \( X \) (horizontal axis, \( -168 \) mm < \( X < 168 \) mm) and \( Y \) (vertical axis, \( -168 \) mm < \( Y < 168 \) mm). A second response function (not shown here) is used from February 20, 2012 until April 15, 2012.

The electron lifetime varies over time due to small changes in the xenon recirculation rate, occasional interruptions due to xenon pump maintenance or failure and power outages, and events where xenon gas is added to the detector by the detector monitoring system. To account for this, a piecewise polynomial is fit to the measured \( \tau_e \) history, as shown in fig. 13. Separate \( \tau_e \) are used for each TPC to allow for spatial variation in the LXe impurity content, although the two TPCs track each other quite well. A correction factor of \( \exp(t/\tau_e) \) is applied to all ionization signals in the data by evaluating the \( \tau_e \) history function at the time of each event.

3. Shielding inefficiency corrections

The shielding inefficiencies of the V grids (see e.g. [30]) produce a small residual dependence of the U-wire pulse amplitude on the \( Z \) position of the charge deposition. We measure this effect in the data by fitting the purity-corrected peak-position of the \( ^{208} \)Tl gamma line at 2615 keV as a function of \( Z \). We fit this data to the function:

\[
E_{\text{meas}} = \frac{E_0}{1 + p_0 \exp((Z-Z_{\text{max}})/p_1)}
\]

where \( E_{\text{meas}} \) is the purity corrected peak energy, \( E_0 \) is the true peak energy, \( Z \) is the \( Z \) coordinate of the energy deposit in units of mm and \( Z_{\text{max}} \) is the maximum drift peak is plotted versus drift time as shown in fig. 12, and the electron lifetime is extracted from a fit to eq. (8). It is found that the goodness-of-fit function is asymmetric around the minimum and larger electron lifetime values have larger uncertainties.
distance (192.5 mm). We find that the best fit parameters are \((p_0, p_1) = (0.043, 7.02 \text{ mm})\) and \((0.064, 8.09 \text{ mm})\) for one-wire and two-wire charge deposits, respectively. The function is then inverted to correct the measured charge deposit energy to the true energy. For events in the fiducial region this correction is much less than 1%.

### D. Rotated energy measurement

To optimize the energy resolution of the detector we take advantage of the microscopic anti-correlation between ionization and scintillation in LXe [21]. This effect is illustrated for \(^{228}\text{Th}\) source calibration data in fig. 14. The optimal energy variable is calculated by combining the charge, \(E_I\), and scintillation, \(E_S\), measurements with appropriate weights according to

\[
E_R = E_S \cdot \sin(\theta^R) + E_I \cdot \cos(\theta^R)
\]

where \(E_R\) is the “rotated” energy and \(\theta^R\) is the rotation angle.

We find that the energy resolution of the ionization channel is nearly constant in time with a value of \(\sigma/E = 3.5\%\) and 4\% at 2615 keV for SS and MS events, respectively. The scintillation-only energy resolution, however, does show significant time variation as shown in fig. 15. The exact cause of this variation is under investigation, but it is likely related to noise in the front-end electronics of the APD channels.

Due to the variation in the scintillation energy resolution, the optimal \(\theta^R\) to use in eq. (10) also varies with time. We measure \(\theta^R\) weekly with \(^{228}\text{Th}\) source calibration data and apply it to calculate the appropriate rotated energy for events in the “low-background data” (physics data) as a function of their date. This is done separately for SS and MS events. We apply the same rotation angle to all events regardless of the event energy.

After applying all corrections, the residuals defined as \((E - E_{\text{true}})/E_{\text{true}}\), are 0.36\% for \(^{137}\text{Cs}\), and 0.17\% for \(^{60}\text{Co}\) and \(^{228}\text{Th}\) sources, as shown in fig. 16. The energy measured for the \(^{40}\text{K}\) peak in the low-background data has a residual of 0.21\% and is also shown in fig. 16.

The energy resolution \(\sigma(E)\) is parameterized as a function of energy, \(\sigma^2(E) = \sigma_{\text{elec}}^2 + bE + cE^2\), where \(\sigma_{\text{elec}}\) is the electronic noise contribution, \(bE\) represents statistical fluctuations in the ionization and scintillation, and \(cE^2\) is
different than those reported in Ref. \[8\] because we now average over time.

![Energy resolution (%)](image)

FIG. 15. Energy resolutions of ionization and scintillation channels during Run 2a.

![Residual (%)](image)

FIG. 16. Residuals between the calibrated source energies and the true energies for SS and MS events. Also shown is the residual for the $^{40}$K peak (cross, MS only) which is obtained from the low-background data set.

regarded as a position- and time-dependent broadening. This parameterization is used to smear the Monte Carlo data set to produce the energy PDFs. To estimate the covariance matrix of the resolution parameters, an iterative approach (inspired by \[31\]) was developed to fit the smeared $^{228}$Th Monte Carlo spectrum to the calibration data set, with an underlying assumption that all the parameters compose a multivariate Gaussian distribution. We calculate the resolution curve $\sigma(E)$ weekly for source agreement studies (see section VI). In order to take into account the time variation of the energy resolution, the $^{228}$Th Monte Carlo data set is initially smeared by the weekly resolution parameters, then weighted by the low background live-time fraction in each week. In the end the Monte Carlo $^{228}$Th data sets are combined and fitted by using the iterative approach to get the averaged resolution parameters. The time-averaged energy resolution is plotted versus energy in fig. 17, and its values at the $\beta\beta$ decay $Q$ value are $1.84 \pm 0.03 \%$ ($1.93 \pm 0.05 \%$) SS (MS) events, respectively. These values are slightly different than those reported in Ref. \[8\] because we now average over time.

![Energy Resolution (%)](image)

FIG. 17. (Color online) (a) The fractional energy resolution ($\sigma/E$) for SS and MS events. The width of the two lines indicates the uncertainty. (b) The absolute energy resolution for SS and MS events. The cross-hatched areas indicate the uncertainty.

VI. MEASUREMENT AND MONTE CARLO SIMULATION AGREEMENT

The maximum-likelihood fit requires, as an input, probability density functions (PDFs) in energy and standoff distance space for both the signal and backgrounds. Separate PDFs, one containing SS events and the other containing MS events, are generated using the EXO-200 simulation package. The energy observable in these simulated PDFs is derived from a convolution of the measured energy resolution function (section V D) and the deposited energy given by the simulation.

An important mechanism for determining the accuracy of simulation-generated PDFs is the direct comparison of the detector response to certified calibration sources with the full detector simulation of the same source. Calibration source data, however, differs from the $2\nu\beta\beta$ signal in several significant ways. The $2\nu\beta\beta$ events are predominantly single-site ($\sim 95\%$ SS) whereas the interactions of...
photons from the external sources are mostly multi-site (~20% – 50% SS, see e.g. fig. [21]). In addition, $2\nu\beta\beta$ events occur uniformly throughout the LXe volume while the source of calibration events lies in a single point external to the LXe volume. The photons emitted by the calibration source are strongly attenuated by the LXe, concentrating the interactions in the active xenon nearest to the deployment position of the calibration source.

Because of the differences outlined above, the verification of source agreement is augmented by direct analysis of the low-background data wherever feasible (see section [VIII]). The calibration source/simulation agreement studies are partitioned as follows: (A) Source shape agreement, which compares the shapes of distributions derived from both; (B) Source rate agreement, which considers the ability of the simulation to predict the activity of the source that is observed; and (C) SS fraction agreement, which verifies the fidelity of SS/MS discrimination predicted by the simulation.

A. Source shape agreement

The shape of $^{228}$Th and $^{60}$Co calibration source energy spectra and standoff distributions were compared to the those from simulation at various calibration source deployment positions. The $^{137}$Cs source was not considered as its main feature (the 662 keV gamma-ray full-energy absorption peak) lies below the analysis energy threshold (700 keV). The primary source deployment positions near the cathode (S5 and S11) illuminate the bulk of the active LXe in both TPCs. Source calibrations near either anode (S2 and S8) are additionally used to confirm adequate modeling at each end of the TPC.

Figure [18] demonstrates, for the shape of the energy and standoff distance distributions, the agreement between $^{228}$Th calibration source (at S5) data and simulation and the agreement between $^{60}$Co calibration source (at S2) data and simulation. Figure [19] highlights the Gaussianity of the $^{228}$Th and $^{60}$Co (at S5) full-energy deposition peaks along with the excellent agreement achieved between both sets of calibration data and the simulation in the vicinity of the respective summation peaks. All of these distributions are normalized to unity to study only the shape agreement.

The ratio of $^{60}$Co calibration source spectra, below 1000 keV, to that predicted by the simulation is shown in fig. [20]. A linear parameterization as a function of energy is also shown over the data points. Both the $^{60}$Co (shown) and the $^{228}$Th calibration source data-simulation discrepancies can be parameterized by a single linear function of energy. This suggests a simple mechanism is responsible for the common disparate shapes. These linear skewing parameterizations (one for each the SS and MS energy distributions) are used in section [IXC] to estimate the systematic error induced in the $2\nu\beta\beta$ rate measurement.

B. Source rate agreement

To test the ability of the simulation to predict the observed activity of the $^{228}$Th and $^{60}$Co calibration sources, the total number of events passing all selection criteria (see section [VIII]) was compared between simulation and data. The results from simulations were normalized to the NIST-traceable activity of the respective source and the counting times of the corresponding data sets. The agreement is quantified by the fractional difference $(\text{Data} - \text{(MC Sim)})/\text{Data}$ in number of events. The results of these studies are listed in table [IV] for both calibration sources, deployed at four distinct locations, and indicate that the simulation can predict the activity of external sources within ±4%.

There are several important contributions to this result, which make it not directly reflective of the ability of the simulation to predict the detection efficiency of $2\nu\beta\beta$. In particular, the observed rate of a source depends strongly on its exact position due to solid angle changes. To quantify how the uncertainty on the source position propagates to the uncertainty on the rate, simulations were generated varying the source locations around their nominal positions. Maximum-likelihood fits between simulation and data were performed using the spatial distributions of events within the TPC at each simulated position. The error on the rates presented in table [IV] were taken from the results of these fits.

An additional important consideration is that the simulation predicts fewer MS events to be fully position reconstructed, which would result in the removal of more events in simulation. For external sources of gammarays, of which more than half are observed to be MS, this leads to a more significant under-prediction of the activity than would be expected for $2\nu\beta\beta$ decay events, of which only about 5% are observed to be MS. The effect of this under-prediction in simulation on the $2\nu\beta\beta$ rate is estimated in section [VIII] using low-background data.

C. Single-site fraction agreement

The fraction of SS events, defined as the event number ratio $SS/(SS + MS)$, is calculated from both calibration source data and source simulations. As the SS fraction is observed to be energy dependent, the discrepancy between the SS fraction of calibration source data and the SS fraction of the simulations is determined versus energy. Figure [21] shows that the maximum fractional difference between the SS fraction of calibration source data and the SS fraction of source simulations is ±10%.

From these observations, a spectral-weighted-average SS fraction error is calculated for the $2\nu\beta\beta$ spectrum. This error, determined to be 5.9%, is applied as a constraint in the fit to the low-background data set. Any remaining error on the $2\nu\beta\beta$ rate resulting from the residual energy dependence observed in the SS fraction has
been studied using the low-background data and is presented in section [IX.C.1]

VII. DATA QUALITY AND DETECTOR MONITORING

To ensure operational consistency of all relevant detector parameters over the data-taking period, a number of environmental and analytic parameters are monitored. This monitoring enables a quantitative assessment of the quality of data taken within a particular time period, which we use when selecting runs for the physics analysis. Checks include muon veto system monitoring, low-level checks, and high-level checks, the last of which requires data to be processed with the analysis framework described in sections [II.C] and [IV]. Observations made by monitoring shifters during the run are additionally taken into account to ensure that external activities not monitored by the DAQ system (e.g., construction or mine activity) do not have an adverse effect on the data. The runs selected for the physics analysis total 135.2 days, representing ~ 77% of the total low-background data taken during Run 2a (23% loss due to data quality requirements).

A. Muon veto system source campaigns

The health and response of the muon veto system is evaluated twice per year with a $^{60}$Co source and a standalone DAQ system employing a charge sensitive ADC. This monitoring program is necessary due to the large environmental temperature swings to which the system is exposed outside of the EXO-200 cleanrooms. This may lead to yellowing of the scintillator, PMT failure, or cracks in the PMT optical coupling. During these campaigns the $^{60}$Co source is placed at four different distances to each instrumented end of each of the 29 veto panels. The average signal from of backscattered $^{60}$Co gammas is determined by fitting the Compton edge, $p(x_j,t_i)$, in the spectral distributions of each instrumented detector end, where $t_i$ denotes the time of the measurement and $x_j$ the distance of the source from the PMTs. $i$ identifies the calibration campaign, $j$ numbers...
FIG. 19. (Color online) Comparison of multi-site energy distribution between data (points) and simulation (histograms) using $^{228}$Th (a) and $^{60}$Co (b) sources near the cathode (S5). Note the excellent agreement of the full-energy-deposition gamma-ray peaks all the way up to the summation peaks.

FIG. 20. (Color online) Ratio of $^{60}$Co source (at the cathode, S5) calibration spectra to that generated from simulation. Single- and multi-site events are shown in (a) and (b), respectively, and linear fits to the data are shown. Ratio plots for $^{228}$Th source data and simulation demonstrate the same behavior.
an RMS of 5.9% and $\Delta g/g = -5.2\%$ with an RMS of 8.5%, showing adequate stability in the system’s response to ionizing radiation.

B. Low-level checks

A typical low-background run has a duration of $\sim 24$ hr, although, occasionally, shorter runs are taken. A number of baseline requirements must be met for a low-background run to be used in the physics analysis:

1. Run length greater than 1800 seconds.
2. Average solicited trigger rate measured within 0.5% of its nominal value (0.1 Hz).
3. Calculated live-time no more than 30 s different than the run duration.

The run length requirement ensures enough statistics for the calculation of data quality indicators. The second and third requirements ensure that the DAQ system is operating nominally throughout the run and that no significant reductions in live-time caused by noise bursts or DAQ interruptions have been seen.

C. High-level checks

The higher level checks involve monitoring:

1. the electron lifetime $\tau_e$
2. the efficiency of muon veto system
3. rates of certain classes of events.

Runs satisfying all checks may be automatically approved to be used in the physics analysis. Those runs that do not satisfy all checks are not immediately rejected, but are instead subjected to additional scrutiny to determine their final status.

1. Electron lifetime

Even though the charge data is corrected for the effects of finite electronegative purity, as described in section V C 2, uncertainty in the electron lifetime correction or rapid changes in the purity can degrade the detector energy resolution. We calculate that this contribution is acceptably small when the electron lifetime is greater than 1 ms. We also calculate that for an electron lifetime of 1 ms, a rate of change of 500 $\mu$s/day can contribute 1.04% to the energy resolution. Hence the following requirements on the detector purity are applied:

1. $\tau_e > 1000$ $\mu$s.
2. Four or more consecutive measurements of similar electron lifetimes over several days with constant xenon recirculation. This ensures stability of the purity.
3. $\tau_e$ must not be increasing at a rate $> 50\%$ or decreasing at a rate $> 25\%$ of the previous measurement per day.

The variation of the electron lifetime during Run 2a is shown in fig. 13.

2. Muon veto panels

The absolute efficiency of the individual veto panels is monitored bi-annually as described in section VII A. The muon veto system is also monitored semi-continuously with low-background data by counting the fraction of events identified as muons in the TPC that are also tagged with a veto trigger within 2 $\mu$s. For the Run 2a dataset this fraction is $0.9618 \pm 0.0021$ on average.

The individual veto panels are monitored on a run-by-run basis as follows. Because of geometrical effects, the TPC-correlated muon rate varies among veto panels. If one or more panels do not register a single trigger during a low-background run, and those panels account for more than 5% of the average veto-TPC coincidence rate, then...
the run is rejected. This threshold was chosen so that the global veto system efficiency remains $> 90\%$, which is a requirement for achieving the background goals of the $0\nu\beta\beta$ search.

3. Event rates

Rates of different classes of events are monitored over time, as deviations from mean rates can provide an indication of a detector problem or an important environmental change. In particular, rates of the following seven classes of events are monitored, with rough, nominal rates of each class given parenthetically: (a) events tagged as noise by the analysis processing (10 mHz); (b) reconstructable events, defined as having at least one scintillation cluster and not tagged as a muon, noise, or a solicited trigger (35 mHz); (c) non-reconstructable events, those failing criteria (b) and not tagged as a muon, noise, or a solicited trigger (25 mHz); (d) events with $> 0$ keV (25 mHz); (e) events with $> 300$ keV (20 mHz); (f) events with $> 1000$ keV (3 mHz); and (g) events with $> 2000$ keV (1.5 mHz). The energy ranges in the last four classes of events are defined for ionization energy. For each of these seven rates, an acceptance region is defined so that a value falling within these limits confirms the data as high quality. An example set of plots is given for event classes (a) and (b) in figs. 22 and 23, respectively, showing the rate versus time as well as the distribution of rates of the two parameters over the data-taking period.

VIII. EVENT SELECTION REQUIREMENTS

The live-time of the data set differs from the data-taking time due to the following rejection criteria, with the percentage live-time lost due to each in parentheses:

1. 1 ms before to 25 ms after the muon veto system triggers (0.6%)

2. 1 μs before to 60 s after TPC events tagged as muons (4.5%)

3. Portions of runs flagged as coincident with poor data-taking conditions, including times during a run where one or more of the selection criteria described in section VII are not satisfied. (0.6%)

4. 60 s after the beginning and 1 s before the end of any run (< 0.1%)

These result in a total live-time reduction of 5.6% over the total data-taking time of all selected runs in the Run 2a data set. This does not exactly correspond to the sum of the above percentages because some of the criteria overlap.

Selection criterion 1 is motivated by the observed elevated event rate in the TPC following a muon veto system trigger. This rate is found to return to its nominal value after 25 ms. In addition, the analysis of the time behavior of 2.2 MeV full-energy deposition events within 25 ms following a muon trigger yields a neutron capture time in hydrogen in the HFE of $740 \pm 120 \mu s$, well within the 25 ms time window. Selection requirement 2 is motivated by the expectation of the cosmogenic activation of short-lived isotopes in and near the LXe following a muon event in the TPC. The 60 s coincidence window is determined by limiting the impact of this requirement on the live-time of the data set to be < 5%.

Data-taking times may be flagged as unacceptable (criterion 3) due to data quality concerns arising from e.g. bursts of electronic noise or mining activity. Criterion 4 ensures that neither a muon TPC event or an event within 1 s coincidence could have been missed immediately before the initiation of or immediately after the termination of a run. The application of these live-time selection criteria results in $127.6_{+0.012}^{-0.000}$ days live-time out of 135.2 days of cumulative data taking during all selected runs in the Run 2a data set.

FIG. 22. (Color online) History (a) and distribution (b) of rate of events tagged as noise. The drop in noise starting with run 2855 is due to a cooling fan change in the electronics box. The unshaded region in (b) indicates the accepted parameter values ranges.
The following data selection criteria are evaluated on an event-by-event basis. For each data reduction, the resulting loss of $2\nu\beta\beta$ signal efficiency is estimated along with an associated error. These efficiencies are used to correct the measured $2\nu\beta\beta$ rate and the associated errors on the $2\nu\beta\beta$ rate are included via a normalization term (see section IX B). The following data reductions are applied in the order that they are listed (note that event frames are 2048 $\mu$s in length). In order for events to be selected for analysis they must

1. not be in coincidence with 0.1 Hz solicited triggers (explicitly tagged by the DAQ system),
2. not be in coincidence with events tagged as noise,
3. not occur within 1 s of another TPC event (to address e.g. Bismuth-Polonium (Bi-Po) fast $\beta$-\(\alpha\) coincidences in the $^{222}$Rn and $^{220}$Rn decay chains and other correlated decays),
4. not contain more than 1 reconstructed scintillation signal,
5. not begin within 120 $\mu$s of the end of the waveform trace,
6. not contain any partially reconstructed signals (must be fully 3-D reconstructed),
7. be reconstructed inside the fiducial volume,
8. not exhibit a high light-to-charge ratio (e.g. appear to be $\alpha$-like),
9. contain total rotated energy $> 700$ keV

The estimation of systematic errors related to items are described in more detail in the following sections. The removal of solicited triggers results in a $10^{-3}\%$ reduction of signal efficiency, estimated from the probability of a solicited trigger occurring coincidently with a $2\nu\beta\beta$ event. A comparable reduction in signal efficiency ($10^{-3}\%$) has been calculated for events tagged as noise. Whereas the majority of noise events are tagged because of grossly unphysical characteristics (e.g. channel range saturation), there is a possibility that some physics events are falsely tagged as a particular class of noise. The probability of this occurring has been estimated by randomly selecting a set of events failing this cut and hand-scanning them. No false positives were found, leading to a conservative $6 \times 10^{-2}\%$ systematic error on the signal efficiency.

Events with a high light-to-charge ratio are indicative of an event including $\alpha$-particles or of events with incomplete charge collection, which may occur if the charge cloud drifts to the edges of the wire grid. This cut is highly degenerate with some of the other selection cuts and, after the previous application of all other cuts, only removes $\sim 35$ events from the 23082-event dataset. We conservatively take this ratio (0.15\%) as a systematic error.

The removal of events below the threshold of 700 keV is subject to errors in the measurement of the detector calibration and resolution. The contribution of this effect to the $2\nu\beta\beta$ measurement was found to be 0.4\%, estimated by the residual calibration error of the $^{137}$Cs 662 keV peak (see section V D).

### A. Scintillation-signal-driven data selection

Two cuts are performed, which are related exclusively to scintillation signals. Events which have a scintillation signal within 120 $\mu$s of the end of a waveform are removed because they cannot be fully reconstructed. This cut removes only 1 event from the final waveform are removed because they cannot be fully reconstructed. This cut removes only 1 event from the final dataset therefore contributing a negligible amount to the systematic error on the efficiency.

In addition, events are required to have no more than one scintillation signal in order to remove correlated decays (e.g. Bi-Po correlated decays). The false positive rate (the probability to incorrectly reconstruct more than one scintillation signal when only one real signal exists)
has been estimated by running the reconstruction software on noise trace (solicited trigger) events from data with an added simulated signal of known amplitude. This study estimates a false positive rate integrated above 700 keV of < 0.1%. This study was cross-checked by analyzing the 613 low-background events removed by this cut after applying all other analysis cuts, and was determined to remove 0.7% of all events because of an incorrectly found scintillation signal. We choose to take the more conservative value and so a normalization error of 0.7% is added to account for this effect.

| Counts / 9mm |
|-------------|
| 0           |
| 500         |
| 1000        |
| 1500        |
| 2000        |
| 2500        |

| Hexagon R (mm) | Counts / 9mm |
|---------------|-------------|
| 0             | 0           |
| 20            | 2000        |
| 40            | 2000        |
| 60            | 2000        |
| 80            | 2000        |
| 100           | 2000        |
| 120           | 2000        |
| 140           | 2000        |
| 160           | 2000        |
| 180           | 2000        |

B. 1 s event-to-event coincidence

A one-second coincidence cut on TPC events is used to reduce the presence of backgrounds arising from fast, correlated decays in the TPC that may arise, for example, after through-going muons or from the decays of radioactive species in the LXe (Bi-Po decays) not removed by the scintillation event cut. For the purpose of this cut, two TPC events are considered to be in coincidence if their DAQ triggers were not solicited, the events are not tagged as correlated noise, and both events have some scintillation signal or saturate a scintillation channel. The $2\nu\beta\beta$ signal efficiency was calculated by considering the rate of random coincidences of TPC events and was determined to be $0.931 \pm 0.002$.

C. Fiducial volume selection

The fiducial volume is chosen to include regions of the detector that are well understood and properly modeled in simulation. Since the measurement of the $2\nu\beta\beta$ half-life is not constrained by statistics, a smaller fiducial volume is chosen than was presented in [9] to minimize the impact of fiducial-volume-related systematics on the result. As in [9], since signals are fundamentally reconstructed at U- and V-coordinates parallel to the detector wire channels, the fiducial volume is chosen to be hexagonal in shape, thus avoiding effects arising from radial coordinate transformations. However, this still requires using a third coordinate (X) derived from U and V to define the hexagon. This is because the U- and V-coordinate axes are each perpendicular to two sides of the hexagon, whereas the last two sides are perpendicular to the derived X axis (see fig. 2).

The Z range of the fiducial cut is chosen to include events satisfying $182 \text{ mm} > |Z| > 15 \text{ mm}$ in both TPC halves, or $10.2 \text{ mm}$ from the V-wire planes and $15 \text{ mm}$ from the cathode. The distance from the V-wire plane ensures the grid efficiency correction to the charge energy (see section V C 3) is $\ll 1\%$. The distance from the cathode was determined from studies using the 3-D electric field model (see section H D), which demonstrated slightly distorted (not parallel in Z) charge drift trajectories within $15 \text{ mm}$ of the cathode.

![FIG. 24. (Color online) Rate of $2\nu\beta\beta$ versus hexagonal apothem. The vertical dashed line indicates the fiducial cut we have chosen to use, at an apothem of 153 mm. The data within that region is consistent with a rate that is proportional to volume.](image)

To determine the cut in the U- and V-coordinate system, the single-site $2\nu\beta\beta$ rate was studied as a function of detector position by fitting the low-background spectrum in separate hexagonal position bins. The results of this study are shown in fig. 24. We choose the apothem of the hexagonal fiducial volume to be 153 mm, as indicated in fig. 24 and illustrated in fig. 2. This cut removes events on the boundaries of the sensitive area of the hexagonal wire plane. The rate of $2\nu\beta\beta$ decay was also studied in Z position bins and found to be independent of position within the chosen fiducial volume. The fiducial volume selected in this way corresponds to 27.08 liters of liquid Xe, corresponding to 66.20 kg of $^{136}\text{Xe}$. See section IX C 5 for a discussion on the error on this number.

To understand the error on the chosen fiducial volume we first study the cluster position reconstruction accuracy in the two original coordinates - U, V. Given that the detector has a discrete wire spacing, the position resolution is finite and the expected uncertainty is given by the standard deviation of the uniform distribution. For a 9 mm wire pitch in the U- and V-directions this gives $\pm 2.6 \text{ mm}$ for uniformly distributed events.

To study the position reconstruction uncertainty in simulation we generate the distribution of differences between reconstructed cluster coordinates and true location source. The average RMS is $1.2 \text{ mm}$ in the V direction and $2.4 \text{ mm}$ in the U direction, and both distributions are centered on zero with negligible bias. The small RMS in the V direction arises due to the larger number of multi-wire events, which allow better position determination through weighted averaging. The third coordinate that defines the hexagonal volume - X - is different than the fundamental coordinates U and V because it is a combination of the two and so may be subject to an additional uncertainty due to errors in the clustering algorithm (e.g. incorrect wire association). The uncertainty on the X co-
ordinate was determined to be 2.6 mm, consistent with the individual U and V errors added in quadrature, indicating that the clustering error is negligible.

We can cross-check these numbers with the data for specific cases, in particular by using α- and β-decays from the cathode that deposit energy in both TPC halves. Such events typically originate from a common position on the cathode and can be used to check how accurately both TPCs reconstruct a shared coordinate. Because the U- (V-)wires in TPC1 are parallel to the V- (U-)wires in TPC2, these events may be used to cross-check the U and V position reconstruction. The distributions of $U_{\text{TPC1}} - V_{\text{TPC2}}$ and $V_{\text{TPC1}} - U_{\text{TPC2}}$ both have a width of 3.07 mm, consistent with the uncertainties obtained in the Monte Carlo simulation study considering that the measurement of U – V corresponds to a measurement of the sum of $\Delta U$ and $\Delta V$. The mean values are 0.4 mm for $U_{\text{TPC1}} - V_{\text{TPC2}}$ and 1.5 mm for $V_{\text{TPC1}} - U_{\text{TPC2}}$, which could be explained if the wireplanes do not exactly mirror one another. Since we do not have an independent measurement of the wireplane alignment after cooling the TPC with sufficient precision to confirm this possibility, a systematic uncertainty of 1.5 mm on the reconstructed U and V positions is included in the overall fiducial volume uncertainty to account for any residual bias.

The overall error on the reconstructed Z position for events drifting for the full length of each TPC can be determined from the drift time distributions for α particles emitted from Rn-daughter contamination on the cathode, as shown in fig. 25. The observed drift time distributions for α events originating on the cathode have means of $115.224 \pm 0.006$ μs and $115.891 \pm 0.006$ μs for TPC1 and TPC2, respectively. The widths of the drift time distributions, $\sigma_{\text{TPC1}} = 0.411 \pm 0.006$ μs and $\sigma_{\text{TPC2}} = 0.421 \pm 0.005$ μs correspond to the expected error on the determination of Z for a single cluster for a given charge drift velocity. Assuming the same drift velocity in both TPC and using the expected spacing between the wire planes gives an error on Z of $\sigma_Z = 0.42$ mm for an individual cluster. The 0.6 μs difference in the means between the TPC halves was verified using an independent analysis that determined the maximum drift time for the distribution of events observed in $^{228}\text{Th}$ calibration data with the source positioned at the cathode. This offset may be accounted for if the cathode were offset by 0.5 mm from center in the direction of TPC1, which is within the expected tolerance after vessel cool down. As with the observed U, V position bias, this offset is included as a systematic error on the Z position to account for the possibility that this bias instead arises from an error in the position reconstruction.

The respective errors on the component coordinate reconstruction are propagated to the fiducial volume error, including any possible biases introduced by the cut. A 0.42 mm spread in Z direction would only result in a systematic bias on the chosen volume if the cut position was in the region where the density of reconstructed events is different inside and outside the cut (e.g. if the cut was close to the cathode or wire planes). As this is not the case for the chosen Z cut location, there is no systematic bias in the number of selected events.

In the case of the U, V, and X directions, varying the fiducial cut by 1σ above (below) the default cut position does not result in the addition (subtraction) of an equal amount of volume. This means that for a constant density of events the cut will be biased to accept more events. We estimate this effect to be $+0.36\%$ by varying the fiducial cut and comparing the selected number of events in the hexagonal layer 1σ above and below the default cut position.

The uncertainty on the Z position of the cathode translates to the $\pm 0.3\%$ systematic error on the selected volume, given the cut position. The 1.5 mm uncertainty on U and V positions corresponds to $\pm 1.7\%$ error on the chosen volume. Combining the uncertainty in the Z and U/V directions in quadrature, the total error on the chosen fiducial volume is $\pm 1.73\%$. We choose to add the above bias of $+0.36\%$ symmetrically (i.e. $\pm 0.36\%$) in quadrature with $\pm 1.73\%$, which yields a total systematic error on the normalization due to the fiducial volume cut of 1.77%.

**D. Rejection of partially reconstructed events**

The requirement that all events are fully reconstructed ensures that the fiducial volume cut and position dependent corrections (see section V C) have been properly applied. The Monte Carlo simulation is used to calculate the efficiency of this cut, which is defined as how often, given an event of a certain energy, all clusters in the event have a reconstructed U, V, and Z position. We estimate the resultant systematic error on the $2\nu\beta\beta$ measurement by looking at the discrepancy between the simulation model and data. As noted in section V B, the simulation models fewer events with full position reconstruc-
The integral is performed over the $i$th bin in energy (200 bins, 700 keV to 3500 keV) and standoff distance (SD) (20 bins, 0 mm to 200 mm) for external sources than observed in data. To estimate the systematic difference between simulation and data for the $2\nu\beta\beta$ signal, the result of the fit to the low-background data is taken and background subtracted to obtain a more pure $2\nu\beta\beta$ sample. This is done both before and after applying the partial reconstruction cut, and the “efficiency” is calculated, defined as the integrated event count above 700 keV of the spectrum with the cut applied, divided by the number of events without the cut applied. This value (93.9 ± 0.2 (stat) %) can be compared directly to the value calculated for simulation for the $2\nu\beta\beta$ PDF (94.2%). There are two primary sources of error that come from using this background subtraction method: uncertainty from the background normalizations and the systematic discrepancy (4%) seen between simulation and data for this cut for external $\gamma$ sources. The propagation of these errors was performed by generating a toy Monte Carlo dataset, drawing the normalization of the different background components from the correlation matrix measured from the low-background fit. The 4% systematic difference observed for source data was incorporated as a corresponding error on the cut efficiency calculated for each background component. The systematic error on the $2\nu\beta\beta$ result is then taken from the $1\sigma$ width of the efficiency distribution, which translates to a 1.6% error.

Table V provides a summary of the efficiency reduction and associated systematic errors introduced by the event selection cuts presented in this section.

### IX. FIT TO THE LOW-BACKGROUND DATA

#### A. Fit model

To derive the number of $2\nu\beta\beta$ events from the Run 2a dataset we fit both single- and multi-site event sets with their corresponding probability density functions using a binned maximum likelihood method. The data are binned in energy (200 bins, 700 < $E$ < 3500 keV) and standoff distance (SD) (20 bins, 0 < $r_{SD}$ < 200 mm) and the negative log likelihood function is defined as:

$$-\ln L = \sum_i \left[ (\mu_i^{SS} + \mu_i^{MS}) - (k_{obs,i}^{SS} \ln \mu_i^{SS} + k_{obs,i}^{MS} \ln \mu_i^{MS}) \right] + G_{const}$$

(13)

where $k_{obs,i}^{SS(MS)}$ are the number of SS (MS) counts observed in a given bin $i$, $\mu_i^{SS(MS)}$ defines the expected number of SS (MS) events from the fit model in the $i$th bin, and the sum proceeds over all 4000 bins in energy and standoff distance space. $G_{const}$ are Gaussian constraints applied to the fit, which are described in more detail in section [IX.B]. $\mu_i$ may be written as:

$$\mu_i^{SS(MS)}(s, n, N) = \int_{1^{st} \text{ bin}} F_{SS(MS)}(s, n, N, y) \, dy$$

(14)

which is a function of SS/(SS+MS) fractions for each PDF, $s$, the relative number of events in different PDFs, $n$, and an overall normalization parameter, $N$, used to include the error on detector efficiency (see section [IX.B]). The integral is performed over the $i$th bin for the observables energy and standoff distance ($y = (E, r_{SD})$). $F_{SS(MS)}$ are defined as:

$$F_{SS}(s, n, N, y) = N \sum_j n_j s_j f_j^{SS}(y)$$

(15)

$$F_{MS}(s, n, N, y) = N \sum_j n_j (1 - s_j) f_j^{MS}(y)$$

(16)

where the sums are performed across the total number of PDFs included in the fit ($N_{PDF}$), $s_j$ is the relative fraction of SS events in PDF $j$ ($s = \{s_0, ..., s_{N_{PDF}}\}$), $n_j$ is the total number of events in PDF $j$ ($n = \{n_0, ..., n_{N_{PDF}}\}$), and $f_j^{SS(MS)}(y)$ is the $j$th PDF for SS (MS) events and a function of energy and standoff distance.

The list of components comprising the total model is: $2\nu\beta\beta$, $0\nu\beta\beta$, backgrounds in the copper vessel (238U, 232Th, 40K, 60Co, 65Zn, and 54Mn), backgrounds in the liquid Xe ($^{135}$Xe and $^{222}$Rn), and backgrounds in the air gap between cryostat and lead wall ($^{222}$Rn). The PDFs for the background isotopes were produced using the
standard GEANT4 Radioactive Decay Module (RDM) generator \cite{22}. For $^{232}$Th and $^{238}$U the entire chains of decays, assumed in secular equilibrium, are used. For $^{222}$Rn, only decays between $^{222}$Rn and $^{210}$Pb are used. The $\nu\beta\beta$ event generator uses the Fermi function suggested in \cite{32}.

Additional sources of radioactive background were also considered to be added to the background model, in particular $^{238}$U and $^{212}$Th in the surrounding HFE fluid. However, studies comparing the shapes of these backgrounds in both the energy and standoff distance distributions found no significant differences with the corresponding distributions from simulated backgrounds in the copper vessel and so these additional PDFs were not included in the background model of the fit. This implies that values returned from the fit (e.g. $n_{\text{Th}-232,\text{copper}}$) also include contributions from backgrounds located further away from the detector.

### B. Constraints

Using the results of additional studies, several Gaussian constraints are added to the negative log-likelihood function ($G_{\text{const}}$ in eq. (13)). In particular, these constraints contribute the following function to eq. (13):

$$G_{\text{const}}(\rho, \rho_0, \Sigma) = 0.5(\rho - \rho_0)^T \Sigma^{-1}(\rho - \rho_0)$$

(17)

where $\rho$ is the vector of constrained parameters, $\rho_0$ is the set of expectation values for each parameter and $\Sigma$ is the covariance matrix for the set of parameters. For each uncorrelated parameter, $\rho_i$ in $\rho$, eq. (17) contributes the term:

$$0.5 \left( \frac{\rho_i - \rho_{i,0}}{\sigma_i} \right)^2$$

(18)

to eq. (13), where $\rho_{i,0}$ ($\sigma_i$) is the expected value (error) of $\rho_i$. The constraints in the fit are as follows:

- $^{222}$Rn decays are monitored as a function of time and found to occur at a rate of $3.65\pm0.37 \mu$Bq/kg in the xenon. This number is used to constrain the following background contributions:
  
  1. Rn in the active xenon,
  2. $^{214}$Bi on the cathode, and
  3. Rn in the inactive xenon.

$^{222}$Rn and its daughters decay in the bulk xenon, creating positive ions which drift toward the cathode. This causes a large fraction of the $^{214}$Bi decays to occur on the surface of the cathode (item 2) rather than in the bulk (items 1 and 3). Studies of $^{214}$Bi to $^{214}$Po coincidences in the liquid xenon have shown this drift and demonstrated that 83% of these coincidences occur on the cathode, with the remaining 17% in the bulk. There is $\sim 30$ kg of inactive xenon, yielding a total activity of $\sim 110 \mu$Bq in this part of the detector. The total activity is divided correspondingly between the three types of simulated events, translated into number of events and is used as a correlated constraint during the fit. This correlation is relaxed to 90% to account for the estimated systematic error (10%) on the calculated relative fractions of items [13].

- The single-site fractions of all components ($s$) are independently constrained using the 5.9% error determined in section VIII. This means, for each PDF the term $0.5 ([s_i - s_{i,0}] / [0.059s_{i,0}])^2$ is added to eq. (13), where $s_{i,0}$ is the single-site fraction given for the $i$th PDF by the Monte Carlo simulation.

- The overall normalization, $N$, is allowed to float within constraints determined by the total externally estimated systematic errors in section IXC. This adds the term $0.5 ([N - 1]/0.0260)^2$ to eq. (13).

### C. Summary of systematic errors

In addition to the systematic errors arising from event selection cuts described in section VIII several additional components contribute systematic errors on the measured number of $\nu\beta\beta$ decays.

#### 1. Simulation model inadequacies

As noted in section VIA there is an energy-dependent discrepancy seen between measured and simulated energy distributions of $^{228}$Th and $^{60}$Co sources. This discrepancy was used to produce linear skewing functions, an example of which is shown in fig. [20]. To estimate the general effect of simulation model inadequacies on the $\nu\beta\beta$ measurement, similar linear skewing functions were also produced for the $\nu\beta\beta$ PDF by comparing the $\nu\beta\beta$ model generated from simulation with the background-subtracted low-background spectra produced in section VIII D.

The skewing functions were then used to distort the PDFs in the fit model: the functions generated for $\nu\beta\beta$ were used for “$\beta$”-like PDFs (2$\nu\beta\beta$, 0$\nu\beta\beta$, and $^{135}$Xe) and the functions for sources generated in section VIA were used for the remaining PDFs. These PDFs were used to produce $\sim 1000$ toy Monte Carlo datasets by using the expected counts for each PDF given by the low-background fit results. These toy Monte Carlo datasets were fit with the default, “unskewed” PDFs, and the best-fit $\nu\beta\beta$ value compared with the true value. With this study, it was found that the best-fit $\nu\beta\beta$ value could be biased -0.33% with respect to the true value. A systematic error on the $\nu\beta\beta$ measurement of $\pm 0.33\%$ is
added to account for this bias, without applying any correction.

2. DAQ related

While performing data quality control for Run 2a, it was determined that during a portion of the run time (5.2% of the live-time), a single U-wire channel was not being read out. Studies were performed to determine the effect on the signal efficiency by comparing the default simulated-generated PDFs with modified PDFs. These modified PDFs were the combination of the default PDFs and PDFs generated without the wire channel, added together in proportion to their respective contribution to the total live-time of the Run 2a dataset (i.e. $PDF_{mod} = 0.948 PDF_{det} + 0.052 PDF_{missing\, chan}$). The shapes of these PDFs were compared using a Kolmogorov-Smirnov test, finding no significant difference. In addition, the efficiencies for the PDFs as calculated in simulation were compared and found to be consistent within $\sim 0.1\%$. The results of these studies imply that the resulting systematic error on the $2\nu\beta\beta$ measurement due to this missing channel is less than $0.1\%$.

3. Energy scale for $\beta$-like events

As noted in [8], $\beta$-like energy depositions in the detector have a slightly different energy scale than $\gamma$-like deposits, and are reconstructed with $\sim 1\%$ higher energy. The fit to the $2\nu\beta\beta$ spectrum yields a different estimate on this scale than from studies performed using the pair-production peak of $^{208}\mathrm{Tl}$. We choose to treat this difference as a systematic error, which contributes a $0.24\%$ error to the $2\nu\beta\beta$ measurement.

4. Incomplete background model

To test how an incomplete background model may affect the fit, two additional components ($^{238}\mathrm{U}$ and $^{232}\mathrm{Th}$ chains in the HFE) were added to the model and the fit was rerun. These two components were chosen as they occupy the next largest amount of mass near the detector and the U and Th chains are generally likely sources of background. The results of this fit shifted the best-fit value of $2\nu\beta\beta$ counts $< 0.25\%$.

Additional possibilities were considered, including events arising from muons not vetoed by the muon veto. The total expected number of counts from such events with energy $>700$ keV over the Run 2a time period is $\lesssim 20$, indicating a $< 0.1\%$ effect when compared to the number of $2\nu\beta\beta$ counts.

The presence of the $2\nu\beta\beta$ decay of $^{134}\mathrm{Xe}$ was also considered, but its low Q-value ($\sim 820$ keV) would mean only the high-energy tail of the spectrum would contribute above the 700 keV analysis threshold. In addition, cross-checks performed by increasing the analysis threshold and rerunning the fit found no evidence for additional background (see fig. [29]). Because of this, any contribution due to $^{134}\mathrm{Xe}$ was considered to be much less than 0.1%.

To accommodate the possibility of an incomplete background model, we include a systematic error of 0.25% on the $2\nu\beta\beta$ measurement.

5. Xenon related

The $^{136}\mathrm{Xe}$ fraction in the $\text{enr}\mathrm{Xe}$ has been measured to be $80.672 \pm 0.014\%$ using dynamic dual-inlet mass spectrometry [34], where the uncertainty is systematic. The abundance of $^{134}\mathrm{Xe}$ is $19.098 \pm 0.014\%$ and other isotopes make up for the remaining fraction of 0.230%, dominated by 0.203% of $^{132}\mathrm{Xe}$.

The isotope fraction is measured using a sample from the gas introduced into the detector at filling. The composition in liquid phase is expected to be the same as in the gas phase to $< 0.01\%$ based on the difference of vapor pressures between $^{136}\mathrm{Xe}$ and $^{130}\mathrm{Xe}$ [34]. The conservative figure of 0.01% is used as a systematic error. In addition some dilution of the $^{136}\mathrm{Xe}$ content could have occurred because of the natural Xe used for detector commissioning desorbing over time from the plastic components inside the TPC. From solubility arguments this effect is estimated to be $< 0.04\%$ and this figure is included as a systematic.

The temperature dependence of LXe density was measured by [35, 36] and corrected to account for the small difference between $^{nat}\mathrm{Xe}$ and $^{136}\mathrm{Xe}$. The stability of the temperature of the LXe was continuously monitored by thermocouples mounted on the cryostat during the course of data taking. A variation of 0.15 K RMS was observed. The absolute temperature scale was calibrated in a test run before the start of the experiment with a reference RTD (then removed because of concerns about its radioactive background) yielding $166.6 \pm 0.2$ K, which translates into a density of $3.0305 \pm 0.0077\, \text{g/cm}^3$. This absolute temperature is consistent with that obtained as a cross-check by measuring the pressure at the onset of condensation when the detector was filled. The quadratic sum of the absolute temperature uncertainty (0.2 K) and the temperature swing observed by the thermocouples (0.15 K) results in a 0.06% uncertainty of the LXe density. The Xe-related systematics, listed above, contribute a $\pm 0.26\%$ systematic error to the $2\nu\beta\beta$ measurement.

Table [VI] summarizes the numbers used as systematic error input to the final fit.

D.  Fit Results

To obtain the best-fit model, all parameters ($n$, $s$, and $N$) were allowed to float and $-\ln L$, defined by eq. [13], was minimized. The errors on the main parameter of
instead, the NDFs for each degree of freedom (NDF) from the number of parameters using a ML fit, it is not possible to directly calculate the counts of the component PDFs are listed in table VII.

The best-fit value for $2\nu\beta\beta$ corresponds to 19042 events above 700 keV. The total error on this value is estimated by performing a profile likelihood scan, yielding a $1\sigma$ error of 538 events, which incorporates the systematic error from event selection cuts, is produced by adding in quadrature.

The cumulative $\chi^2$ for the projected energy and standoff distance distributions shown in figs. 26 and 27 are, respectively, 100.1 and 22.8 (94.0 and 23.2) for SS (MS) events. Since the best-fit parameters were determined using a ML fit, it is not possible to directly calculate the degrees of freedom (NDF) from the number of parameters and bins (see e.g. [38]). Instead, the NDFs for each of the 4 projection distributions were estimated using toy Monte Carlo simulations, performed by generating a toy data set from the best-fit parameters and rerunning the fit 5000 times. This study estimates the NDF for energy and standoff distributions to be, respectively, 113.7 and 17.2 (106.8 and 13.6) for SS and MS events, yielding a reduced $\chi^2$ of 0.88 and 1.33 (0.88 and 1.70).

A typical quantity to compare results between experiments is the observed signal-to-background ratio (SBR). Because the ML fit is performed with 2 observables (energy and standoff distance) and across 2 classes of events (single-site and multi-site), it is difficult to define one number quantifying this ratio. However, the $2\nu\beta\beta$ signal is observed to be 95% SS, consistent within the estimated systematic errors with the 98% SS predicted by the EXO-200 simulation, and so we may consider the SBR quantity purely in this class of events. The average SBR over the SS spectra is roughly 11. This quantity increases to 16 (19) as one selects the inner 60% (40%) of the fiducial volume, demonstrating the self-shielding of the xenon in addition to the power of fitting over the standoff distance observable.

### E. Final cross-checks

A series of cross-checks were performed on the fit result. The rate of $2\nu\beta\beta$ was binned versus time and the fit repeated for each time bin. The results were found

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1 We plan to present a full study of the background contributions in an upcoming publication.
FIG. 26. (Color online) Fit results. Data and PDFs for SS energy spectra shown in linear (a), log (b), with residuals (c). The residuals have been normalized by the bin error. To improve visualization of the fit results, the energy bin widths in the plot are 20 keV instead of the 14 keV bin size used during fitting. SS standoff distribution is also shown (inset). Backgrounds have been grouped together according to Rn components and components in or near the TPC vessel. The best-fit counts and errors for each PDF are given in table VII. There are fewer events in the 0νββ region-of-interest than in [8] because of the stricter fiducial volume cut.

to be consistent with a constant rate. In addition, an energy-only (without SD) fit was performed, producing a best-fit 2νββ counts value 3.0% less than the reported result. The corresponding contribution from the backgrounds on the total error increased slightly from 1.3% (table VIII) to 1.35% for the energy-only fit.

In addition to the studies performed in section IX C 4, further investigations were undertaken to test the possibility that an unknown or unconsidered background is affecting the results of the fit. It is important to note that the measured goodness-of-fit is already an indication that the chosen fit model describes the data well. This suggests that, for an unknown background to affect the 2νββ measurement, it would need to exhibit an energy spectrum and standoff distance distribution similar to 2νββ decay. As in [3] we consider two candidates satisfying these requirements, 90Y and 188Re, supported by 90Sr and 188W, which have half-lives of 28.90 yr and 69.78 d, respectively. It is important to note that the presence of these isotopes in the LXe is considered a priori unlikely as no indication of more common contaminants (e.g. metallic components from the U and Th chains) has been seen and the LXe is being continuously purified.

A ML fit to the Run 2a dataset with an added time dimension was performed, including a PDF from 188Re with an exponentially decaying time component corresponding to the 188W half-life. The results of this fit found the number of counts of 188Re to be consistent with zero and produced a best-fit value of 2νββ within 0.8% of the quoted value. To investigate any effect due to 90Y, a ML fit was performed by adding a 90Y PDF to the standard set of PDFs. The results of this fit produced a best-fit value of 2νββ within 3% of the quoted value.

A final cross-check consisted in performing the fit with increasing energy thresholds. The purpose of this cross-check is to investigate the possible presence of other unexpected backgrounds from β-decays under the 2νββ spectrum. Increasing the energy threshold would change the relative contribution of any potential background, which
FIG. 27. (Color online) Projected MS energy spectra (a) and corresponding MS standoff distance distribution (inset) for the final fit results. Residuals are shown in (b). PDF components are as in fig. 26.

FIG. 28. A comparison of this result with EXO-200 (2011) [3], and KamLAND-Zen (2012) [37].

would manifest as a change in the fit number of $2\nu\beta\beta$ events. The results of this study are shown in fig. 29, demonstrating that the $2\nu\beta\beta$ measured rate is stable under even large changes of threshold.

TABLE VIII. Summary of estimates of contributions to the final total error on $2\nu\beta\beta$ due to various components. Note that this includes errors explicitly included in the normalization term (from table VI) in addition to errors arising from other nuisance parameters (e.g. single-site fraction). The total error is taken from the profile-likelihood scan (PLL) and is not a simple sum in quadrature as the components are correlated. To estimate the statistical error, all nuisance parameters except the $2\nu\beta\beta$ counts are fixed to their best-fit values and the PLL rerun. To estimate the error component due to other sets of nuisance parameters, the following procedure is followed: after the best-fit parameters are found, the PLL is regenerated after fixing the relevant nuisance parameters to their best-fit values. The reduction of width in the resulting PLL from the original PLL yields the estimate on the error due to the particular component(s).

FIG. 29. (Color online) The fit count rate divided by efficiency of $2\nu\beta\beta$ versus energy threshold. The main result is the (red, online) triangle at 700 keV.

X. CONCLUSIONS

We have reported on an improved measurement of the $2\nu\beta\beta$ decay of $^{136}$Xe using 127.6 days of live-time collected between Sept 2011 and April 2012. The resulting half-life $T_{1/2}^{2\nu\beta\beta} = 2.165 \pm 0.016\text{(stat)} \pm 0.059\text{(sys)} \times 10^{21}$ years is measured with a total relative uncertainty of 2.83% and is dominated by systematic uncertainties. This half-life corresponds to a nuclear matrix element of $M^{2\nu} = 0.0218 \pm 0.0003 \text{ MeV}^{-1}$, the smallest among the isotopes measured to date. For comparison, in table IX we have tabulated the most precise half-life measurement of all nine nuclei for which $2\nu\beta\beta$ decay has been directly
The uncertainty in the half-life is the quadratic sum of statistic and systematic errors, as given in the cited publications. We have described in some detail the data analysis methods used for this measurement. These methods are similar to those employed to search for the $0\nu\beta\beta$ decay, that, if observed, would indicate the discovery of new physics beyond the Standard Model. While the level of precision achieved here is not required for the $0\nu\beta\beta$ decay search, it demonstrates the quality of the EXO-200 data and the power of a fully active, high resolution tracking detector with very low background.

Since April 2012 EXO-200 has accumulated an exposure several times larger than that described here. We expect to report the results of a new search for $0\nu\beta\beta$ based on this larger dataset in the near future.

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TABLE IX. Listing of the most precise measurements of $2\nu\beta\beta$ half-lives for each isotope as reported in the literature. Only direct counting experiments and ground state decays are shown here. The results are listed chronologically by year of publication. Also included are phase space factors ($G^{2\nu}$, from [3]) and nuclear matrix elements ($M^{2\nu}$) as defined by eq. (1). The total relative uncertainty on the half-life is the quadratic sum of statistic and systematic errors, as given in the cited publications, divided by the half-life. The uncertainty in $M^{2\nu}$ is derived from the experimental uncertainty on $T^{2\nu}_{1/2}$, under the assumption that the uncertainties in $G^{2\nu}$ and $g_A$ are negligible. In addition, these errors are determined to be symmetric or asymmetric following the same conventions used in assigning the half-life errors.

| Nuclide | $T^{2\nu\beta\beta}_{1/2}$ ± stat ± sys | rel. uncert. | $G^{2\nu}$ | $M^{2\nu}$ | rel. uncert. | Experiment (year) |
|---------|-------------------------------------|--------------|------------|------------|--------------|------------------|
| $^{136}$Xe | 2.165 ± 0.016 ± 0.059 · 10$^{-21}$ | ±2.83 | 1433 | 0.0218 | ±1.4 | EXO-200 (this work) |
| $^{76}$Ge | 1.84+0.09+0.11 · 10$^{-21}$ | +7.7 | 48.17 | 0.129 | +3.9 | GERDA [39] (2013) |
| $^{130}$Te | 7.0 ± 0.9 ± 1.1 · 10$^{-20}$ | ±20.3 | 1529 | 0.0371 | ±10.2 | NEMO-3 [40] (2011) |
| $^{116}$Cd | 2.8 ± 0.1 ± 0.3 · 10$^{-19}$ | ±11.3 | 2764 | 0.138 | ±5.7 | NEMO-3 [41] (2010) |
| $^{48}$Ca | 4.4+0.5 ± 0.4 · 10$^{-19}$ | ±14.6 | 15550 | 0.0464 | +7.3 | NEMO-3 [41] (2010) |
| $^{96}$Zr | 2.35 ± 0.14 ± 0.16 · 10$^{-19}$ | ±9.1 | 6816 | 0.0959 | ±4.5 | NEMO-3 [42] (2010) |
| $^{150}$Nd | 9.11+0.25 ± 0.63 · 10$^{-18}$ | ±7.4 | 36430 | 0.0666 | +3.7 | NEMO-3 [43] (2009) |
| $^{100}$Mo | 7.11 ± 0.02 ± 0.54 · 10$^{-18}$ | ±7.6 | 3308 | 0.250 | ±3.8 | NEMO-3 [44] (2005) |
| $^{82}$Se | 9.6 ± 0.3 ± 1.0 · 10$^{-19}$ | ±10.9 | 1596 | 0.0980 | ±5.4 | NEMO-3 [44] (2005) |

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Appendix A: Reconstruction Clustering Distribution Functions

Several PDFs are used when matching together U- and V-signal bundles and are described in the following.

![Graph showing relative V-energy difference against Z (mm).](image)

FIG. 30. (Color online) Total \((E_V - \rho_E(E_U))/\rho_E(E_U)\) for an event, data from Th source runs as well as low-background runs. There is a strong Z dependence for \(|Z| > 160\) mm observed, and so the energy relationship between U- and V-bundles is ignored for bundles in this region.

1. Energy

The amplitude of the induced signals is directly proportional to the amplitude of the deposition signals, and so this correlation may be used when combining U- and V-signals. The energy PDF, estimated from fits to source data, quantifies this relationship:

\[
f_{\text{energy}}(E_U, E_V, Z) = \begin{cases} 
    A & |Z| > 160 \text{ mm} \\
    A \exp \left( -0.5 \left( \frac{E_V - E_U}{\sigma_E(E_U)} \right) \right) & |Z| \leq 160 \text{ mm}
\end{cases}
\]  

(A1)

where A is a normalization constant, \(E_U, E_V\) are the amplitudes of the U- and V-bundles, respectively, in units of gain-corrected ADC counts (i.e. \(ADC_U, ADC_V\)), \(\rho_E\) is the expected value of \(E_V\) given a particular \(E_U\) and is defined as:

\[
\rho_E(E_U) = \begin{cases} 
    0 & ADC_V \quad E_U < -b_E/m_E \\
    E_V m_E + b_E & E_U \geq -b_E/m_E
\end{cases}
\]  

(A2)

with the constants \(b_E\) and \(m_E\) measured as - 30.79 ADC\(_V\)/ADC\(_U\) and 0.2378 ADC\(_V\). \(\sigma_E\) from eq. (A1)

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2 The ADC\(_U\)/unit value is very similar to keV, however, the data are not fully calibrated at this point of processing.
is the expected spread in $E_V$ given a particular $E_U$ and is defined as:

$$\sigma_E(E_U) = \begin{cases} a_E & E_U < 350 \text{ ADC} \\ c_E E_U + d_E \sqrt{E_U} & E_U \geq 350 \text{ ADC} \end{cases}$$

where $B$ is a normalization constant, $t_{U,V}$ are the times in $\mu$s of the U and V bundles, respectively, $\sigma_{\text{time}}$ is a constant (1 $\mu$s), and $\rho(Z)$ is given by:

$$\rho_t(Z) = \begin{cases} 0 & \mu s \\ \rho_0 + \rho_1 Z' + \rho_2 Z'^2 - \rho_3 Z'^3 & \frac{|Z|}{\text{mm}} \leq 185.2 \\ 3 \mu s & 185.2 < \frac{|Z|}{\text{mm}} \leq 194.1 \\ \end{cases}$$

At $|Z| > 160$ mm, effects from the anode begin to distort the reconstructed amplitudes of V-wires. This comes from the fact that the V-wire shapes change somewhat when charge is deposited closer to the anode and the method for extracting the V-wire amplitudes (fitting with a signal model) uses a template from charge deposits in the bulk.

2. Time

The relationship between the arrival times of U- and V-bundles has almost no dependence on the Z-position of the bundles throughout most of the TPC, but yields a Z-dependence as the bundles near the anode. This is a relic of reconstruction of V-wires near the anode. The time PDF is a Gaussian with a Z-dependent mean:

$$f_{\text{time}}(t_U, t_V, Z) = B \exp \left(-0.5 \left( \frac{t_U - t_V - \rho_t(Z)}{\sigma_{\text{time}}} \right)^2 \right)$$

3. U,V position

To ensure that only physically possible connections between U- and V-bundles are created, a regular hexagon is used as position PDF. The side-to-side diameter of the hexagon, defined by the detector geometry, is 342 mm. The PDF is given by:

$$f_{\text{UVpos}}(U, V) = \begin{cases} C & \text{U, V inside hexagon} \\ C \exp \left(-0.5 \left( \frac{x_{\text{perp}}}{\sigma_{\text{UV}}} \right)^2 \right) & \text{U, V outside hexagon} \end{cases}$$

where $C$ is a normalization constant, $x_{\text{perp}}$ is the nearest distance to a hexagon side, and $\sigma_{\text{UV}} = l/2 = 4.5$ mm, where $l$ is the width of a single wire channel (9 mm). See fig. 32 for a plot of the position PDF.