First-principles study of vanadium carbides as electrocatalysts for hydrogen and oxygen evolution reactions†

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Vanadium carbides have attracted much attention as highly active catalysts in both the hydrogen evolution reaction (HER) and oxygen evolution reaction (OER), while a satisfactory understanding of the underlying mechanisms still remains a challenge. Herein we apply first-principles calculations to systematically analyze the crystal structures, electronic properties, free energies during the HER and OER processes, surface energies and crystal formation energies of the three types of vanadium carbides, i.e., $V_4C_2$, $V_8C_7$ and VC. We show that all these vanadium carbides are metallic, which enables efficient electron transport from the bulk to the surface of the catalysts. All these vanadium carbides exhibit excellent HER performance but show poor OER catalytic activity. In particular, the $V_8C_7$ (110) surface shows the best catalytic performance for its relatively small $\Delta G(\text{H}^\ast)$ value ($-0.114$ eV) for HER. Emergence of natural carbon vacancies gives rise to large surface energy, proper hydrogen adsorption energy, low crystal formation energy and weak bond strength in $V_xV_y$, which guarantees its leading position among the three vanadium carbides. In addition, a remarkable resemblance between VC/$V_8C_7$ and Pt in their electronic structures on (110) and (111) surfaces are found, which indicates a Pt-like HER mechanism in these vanadium carbides. Our results thus bring new insights to the theoretical understanding of the excellent HER performance of vanadium carbides.

Transition metal carbides (TMC) have been widely investigated as HER catalysts for good electrical conductivity, wide pH applicability, low cost, and high durability. Hu and Leonard’s group synthesized several types of molybdenum carbides and, in particular, $\beta$-Mo$_2$C exhibit high catalytic activity. Our previous theoretical study also confirmed that $\beta$-Mo$_2$C has low $\Delta G(\text{H}^\ast)$ value (0.089 eV), which is close to that of Pt ($-0.085$ eV) and is therefore named as Pt-like catalyst. Tungsten carbide, another important transition metal carbide, was first found to show Pt-like catalytic characters. Wirth et al. systematically studied IVB-VIB transition metal carbides as HER catalysts in acidic condition, among which tungsten carbide displayed the best catalytic performance, and even better than molybdenum carbide. Metal carbides, especially vanadium carbide ($VC$, $V_8C_7$), have attracted extensive attention due to their higher natural abundance and lower cost compared to the aforementioned metals. Recently, Jin et al. reported a substrate-mediated method to grow vanadium carbide (VC), which was considered as high performance electrocatalysts for dye-sensitized solar cells. Synthesized vanadium carbide nanoparticles encapsulated in graphene were prepared by Yagya N. Regmi...
et al., which show excellent HER and oxygen reduction reaction (ORR) activity. Particularly, Xu et al. developed a single crystalline V₆C₇ networks, displaying high HER activity in all pH conditions, and even better than Pt@C in alkaline solution (the overpotential of V₆C₇ and Pt@C are 47 mV and 49 mV in alkaline solution, respectively). So far, plenty of works have shown that vanadium carbides, VC and V₆C₇, can be used as highly active catalysts both in HER and OER. Despite intensive studies, the underlying mechanisms responsible for the excellent catalytic performance of these vanadium carbides are, however, still elusive.

In this work, we employed first-principles calculations to systematically analyze the crystal structures, electronic properties, free energies of HER and OER process, surface energies and formation energies of three types of vanadium carbides, i.e., V₄C₃, V₈C₇ and VC. Smallest free energy |ΔG(H*)| value is found in V₈C₇ and thus it exhibits the best HER catalytic performance among these vanadium carbides. Its outstanding achievement can be explained by its large surface energy, proper hydrogen adsorption energy, low crystal formation energy (enhanced specific surface area and more active sites) and weak bond strength. Furthermore, the calculated density of states (DOS) suggest that V₆C₇ and VC (110) and (111) surfaces have homologous d-band structures with Pt (110) and (111) surfaces, implying their Pt-like HER mechanism.

2 Methodology

2.1 Computational details

The first-principles calculations were performed by the Vienna ab initio simulation package (VASP) code, based on the density functional theory (DFT) method. Projector augmented wave (PAW) based potentials were used to describe the interactions between valence electrons and ion cores. Perdew–Burke–Ernzerhof (PBE) in the generalized gradient approximation (GGA) was used to treat the exchange–correlation interactions. The structures optimization was achieved up to a precision of 10⁻⁵ eV in total energy difference, and the Hellman–Feynman forces converged to 0.01 eV Å⁻¹ on each atom. The Kohn–Sham orbitals were expanded in plane waves with cut-off energy of 500 eV. The Brillouin zone integration and k-point sampling were performed with a Monkhorst–Pack scheme of a 4 × 4 × 4 and 4 × 4 × 2 grid for bulk and slab model of vanadium carbons, and the slab thickness was set as 15 Å. The reaction barriers energies of water decomposition were explored by using the climbing image nudged elastic band (CI-NEB) method.

In this work, the adsorption energies were calculated by:

\[ E_{\text{ads}} = E_{(\text{slab}+i)} - E_{\text{slab}} - E_i \]  (1)

where \( E_{\text{ads}}, E_{(\text{slab}+i)}, E_{\text{slab}} \) and \( E_i \) are adsorption energy, total energy of species adsorbed on the slab, total energy of slab and total energy of adsorbed species, respectively. In this study, the energy of an H atom (\( E_H \)) is equal to \( \frac{1}{2} E_i \).

Gibbs free energy \( \Delta G(i^*) \) was calculated as

\[ \Delta G(i^*) = \Delta E(i^*) + \Delta ZPE(i^*) + T\Delta S(i^*) \]  (2)

where \( \Delta E(i^*) \) is adsorption energy, \( \Delta ZPE(i^*) \) is the changes in zero point energy. ZPE was calculated through frozen phonon approach, which can be estimated by \( \text{ZPE} = \frac{1}{2} \sum n \nu_i \), where \( h \) and \( \nu_i \) are Planck constant and zone center vibrational frequencies of the system; \( \Delta S(i^*) \) is entropic contribution at standard condition (\( T = 298 \text{ K} \) and \( P = 1 \text{ bar} \)), as listed in CRC Handbook.

The surface activity can be described by surface energy. The larger the surface energy, the higher the activity. Surface energy is given by:

\[ E_{\text{surf}} = \frac{E_{\text{slab}} - NE_{\text{bulk}}}{2A} \]  (3)

where \( E_{\text{slab}} \) is the total energy of the slab model, \( N \) is the number of vanadium carbides units in the slab, \( E_{\text{bulk}} \) is the total energy of bulk cell with the same number of units, and \( A \) is the surface area of the slab.

Crystal formation energy is based on:

\[ \Delta E(f(V_xC_y)) = E_{V_xC_y} - xE_V - yE_C \]  (4)

where \( \Delta E(f(V_xC_y)) \) is the total energy of vanadium carbons. \( E_V \) and \( E_C \) are total energies per atom in metallic vanadium and graphite, respectively.

2.2 Crystal structures of vanadium carbides

The crystal structure of VC belongs to the cubic rock salt family (NaCl type, \( Fm\overline{3}m \)), which contains 8 atoms (4 V atoms, 4 C atoms) per unit cell. To theoretically study the effects of carbon vacancies, we artificially built up a compound \( V_xC_y \) using the same cubic structure but with 1 carbon vacancy per unit cell (7 atoms including 4 V atoms and 3 C atoms). The emergence of natural carbon vacancies in \( V_xC_y \) alters the space group to \( P4_3\overline{3}2 \) and the number of atoms counts up to 60 (32 V atoms, 28 C atoms) in one unit cell. But the structure still remains cubic in general. In order to compare these compounds effectively, \( 2 \times 2 \times 2 \) supercell for \( V_4C_3 \) (32 V atoms, 24 C atoms) and VC (32 V atoms, 32 C atoms), one unit cell for \( V_4C_7 \) (32 V atoms, 28 C atoms) are used in the calculations such that each block contains the same amount of V atoms for all these three materials, as shown in Fig. 1. One can see that V and C atoms form VC₉ octahedral structure. Clearly, \( V_xC_y \) and \( V_xC_z \) have 8 C atoms and 4 C atoms vacancies per block, respectively. Tables 1 and S1† illustrate the lattices and sites information of vanadium carbides. The lattice parameters of \( V_xC_3, V_xC_5 \) and VC are 8.219 Å, 8.315 Å, and 8.305 Å, respectively, which are in good agreement with theoretical and experimental works. Due to the appearance of artificial carbon vacancies, the lattice constants of \( V_xC_3 \) is smaller than VC. On the other hand, formation of natural carbon vacancies changes the space group in the real material \( V_xC_7 \), which produces slightly larger lattice constant.

3 Results and discussion

To unveil the electrical conductivity of vanadium carbides, we firstly calculated their total and partial density of states (DOS),
as shown in Fig. 2. From which we can see that these vanadium carbides have similar DOS structures, and all of them exhibit metallic character. The DOS structures can be divided into two regions. The first region is from $-8$ eV to $-2$ eV, where C 2p and V 3d orbits form strong hybrid covalent bonds. Between $-2$ eV and $3$ eV near the Fermi level, is the second region, which is mainly occupied by 3d orbit of V atoms. This implies that conductive electrons are mainly transferred from bulk V atoms to surface during HER process. Furthermore, to investigate the properties of surface states, the electronic structure of these vanadium carbides surfaces (001, 110, 111) were also evaluated (see Fig. S1†). All of these surface states show metallic behavior, which ensures the efficient transportation of electrons from the bulk to the surfaces of these materials.

Fig. 3(a) presents the total reaction process of HER in acidic condition: $2\text{H}^+ + 2\text{e}^- \rightarrow \text{H}_2$. There are two possible reaction steps in HER, the first step is called Volmer, and the second step is the generation of hydrogen (Tafel step or Heyrovsky step). The details of HER process can be found in Section 1 of ESI.† The Gibbs free energy difference between the final state and initial state $\Delta G(\text{H}^*)$ is usually regarded as a good descriptor for HER process and can be computed by $\Delta G(\text{H}^*) = \Delta E(\text{H}^*) + \Delta ZPE(\text{H}^*) - T\Delta S(\text{H}^*)$ (see ESI† Section 1 for calculation details). Small values of $|\Delta G(\text{H}^*)|$ in the vicinity of zero are expected for a high-performance catalyst. In Fig. 3(b), we present the minimum $\Delta G(\text{H}^*)$ values calculated among the three surfaces (001), (110), (111) for V$_4$C$_3$, V$_8$C$_7$ and VC. The complete sets of results for all three surfaces of the three systems are shown in Tables S2–S4 and Fig. S2.† For V$_4$C$_3$, its (001) surface shows the smallest $\Delta G(\text{H}^*)$ value (0.165 eV), whereas the (110) surface has better performance for V$_8$C$_7$ and VC in good agreement with experimental studies. Moreover, our calculation also indicates that V$_8$C$_7$ has the lowest $|\Delta G(\text{H}^*)|$ magnitude among these three vanadium carbides (see Fig. 3(b)), which confirms that V$_8$C$_7$ is the most effective HER catalyst in these compounds.

Generally, HER process in the alkaline environment is poorly understood. As shown in Fig. 3(c), the HER process in an alkaline media can be expressed as $2\text{H}_2\text{O} + 2\text{e}^- + * \rightarrow \text{H}_2 + 2\text{OH}^-$. Similar to acidic media, two reaction steps called Volmer and Tafel or Heyrovsky take place in a typical process (see ESI† Section 2 for more details).Volmer step: $\text{H}_2\text{O} + \text{e}^- + * \rightarrow \text{H}^* + \text{OH}^-$, usually plays a momentous role during HER. Consequently, we adopt the water decomposition barrier energy as the descriptor for HER. The smaller barrier energy is, the better performance of a catalyst has. The calculated energy barriers on V$_4$C$_3$ (001), V$_8$C$_7$ (110) and VC (110) surfaces are displayed in Fig. 3(d). One can find that the water decomposition consists of an initial state (IS), three transition states (TS) and a final state (FS). At the initial state, the water molecular are adsorbed on V

### Table 1: Lattice information of V$_4$C$_3$, V$_8$C$_7$ and VC

| Compound | $a$ | $b$ | $c$ | Space group |
|----------|----|----|----|-------------|
| V$_4$C$_3$ | 8.219 | 90° | Fm3m |
| V$_8$C$_7$ | 8.315 | 90° | P4$_3$32 |
| VC | 8.305 | 90° | Fm3m |

Fig. 1 Crystal structures of vanadium carbides, (a) V$_4$C$_3$, (b) V$_8$C$_7$, (c) VC. Blue and brown balls are V and C atoms, respectively.

Fig. 2 Projected density of state (PDOS) of vanadium carbides, (a) V$_4$C$_3$, (b) V$_8$C$_7$, (c) VC.
atom sites. Subsequently, one hydrogen atom of water molecular approaches C atom and form C–H bond in the transition states (TS). Eventually, at the final state, water molecular splits into H* and OH*. The transition state 4(TS4) for V4C3 and transition state 2(TS2) for V8C7 and VC requires the highest energy in their own decomposition processes. These states mark the boundary beyond which the water molecules decompose. TS2 for V8C7 requests lower energy (0.169 eV) compared to TS2 in VC (0.227 eV) and TS4 for V4C3 (0.454 eV). This implies that V8C7 also exhibit better catalytic performance in alkaline condition among these three systems.

To gain further insight into the catalytic performance of vanadium carbides, we additionally analyzed the oxygen evolution reaction (OER) process of these systems. Four electrons are involved in the production of oxygens by water oxidation: 2H2O → O2 + 4H+ + 4e– (the detailed reaction steps are listed in ESI† Section 3). Commonly, over-potential (η), η = max(ΔG1, ΔG2, ΔG3, ΔG4)/e − 1.23 V, is used to access OER activity, and 1.23 V is the over-potential for water oxidation at ambient condition (T = 298.15 K, P = 1 bar, pH = 0).32 Herein, we analyzed the activity of (001), (110) and (111) surfaces of V4C3, V8C7 and VC. The calculated free energy diagrams and energy values are presented in Fig. 4 and Table S5†. For V4C3, all the reaction steps in (001) plane climb uphill when no potential is applied (U = 0 V, see Fig. 4(a)). Whereas for its (110) and (111) planes, both downhill and uphill states are seen (Fig. 4(b) and (c)). The over-potentials for these three surfaces are obtained to be 1.55 V, 6.505 V, and 6.667 V, respectively when the equilibrium potential (U = 1.23 V) is applied (detailed results are displayed in Table S5†). Similar characteristics are found for VC and V8C7 (see Fig. 4(d)–(i)). For these vanadium carbides, their (001) surfaces have smaller η values (1.55 V, 1.803 V and 1.7 V), which suggests that their (001) surfaces exhibit higher catalytic performance for OER. The (110) and (111) surfaces carry smaller negative adsorption energies in O*, OH* and OOH* steps (see Table S5†). Therefore, a larger reaction energy barrier and over-potential appear between OH* and O2 processes, which hinders the release of oxygen from the electrode surfaces. Overall, the over-potentials are relatively large when compared to that of RuO2 (0.37 V) and IrO2 (0.56 V).33 This indicates that vanadium carbides are not suitable for OER catalysts.

As discussed above, our calculations indicate that V8C7 shows better HER performance than V4C3 and VC both in acidic and alkaline media, but the exact origin is rather unclear till now. To resolve this mystery, we further studied the surface energies, hydrogen adsorption energies (ΔEΗ*), crystal formation energies of these vanadium carbides. The results are displayed in Fig. 5 and also listed in Tables S6 and S7.† As shown in Fig. 5(a), much higher surface energies are observed on (110) and (111) surfaces than (001) surface in all systems. Thus higher activity is expected on (110)/(111) surfaces and ionized hydrogen/oxygen species can be captured more easily on these two faces. More importantly, it is clear that V8C7 holds the highest surface energy records on all surfaces, which adds one
Fig. 4 Free energy diagrams of the OER process of V₄C₃, V₈C₇ and VC. (a–c), (d–f), and (g–i) are (001), (110) and (111) surfaces of V₄C₃, VC and V₈C₇.

Fig. 5 (a) Calculated surface energies (001, 110, 111) of vanadium carbons. (b) Adsorption energies of H atom curve of vanadium carbides, (c) crystal formation energy of vanadium carbides, (d) V–C bond length of V₈C₆ (001), V₈C₇ (110) and V₈C₈ (111) surfaces.
score point to outweigh \( V_4C_3 \) and VC in HER performance competition. Apart from the free energy \( \Delta G(H^*) \), hydrogen adsorption energy \( \Delta E_{\text{ads}} \) is another criterion to evaluate catalytic performance.

In principle, the first step (Volmer) in HER favors negative and small amplitudes for \( \Delta E_{\text{ads}} \); whereas positive and large magnitude of \( \Delta E_{\text{ads}} \) is more friendly in the second step (Tafel or Heyrovsky). Thus, an appropriate balance of \( \Delta E_{\text{ads}} \) close to zero has to be achieved for an excellent catalyst. Fig. 5(b) presents the calculated hydrogen adsorption energies of vanadium carbides. One can see that the hydrogen adsorption energies for \( V_8C_7 \) \( (\Delta E_{\text{ads}} \approx 0.5 \text{ eV}) \) and VC \( (\Delta E_{\text{ads}} \approx 1.5 \text{ eV}) \) is quite far away from the neutron line. This disadvantage again pushes \( V_4C_3 \) and VC behind, while \( V_8C_7 \) scores one more point in HER performance. Now we come to the crystal formation energy \( (E_f) \) and V–C bond length, as presented in Fig. 5(c) and (d) and Table S7.† Apparently, smaller \( E_f \) is seen for \( V_8C_7 \) \( (E_f = -0.617 \text{ eV}) \) when compared to \( V_4C_3 \) \( (E_f = -0.429 \text{ eV}) \) and VC \( (E_f = -0.502 \text{ eV}) \), which allows the easier occurrence of C vacancies in \( V_8C_7 \). Formation of C defects distorts V–C bonds (see Fig. S6†), which enhances specific surface area and provides more active sites. These effects add one more bonus to \( V_8C_7 \). According to bond valence theory, bond length is a measure of bond strength. The larger the bond length, the weaker the bond strength. Fig. 5(d) shows the V–C bonds lengths, which tells that \( V_8C_7 \) has the largest bond length \( (V_8C_7: 2.10 \text{ Å} > \text{VC:} 2.076 \text{ Å} > V_4C_3: 2.055 \text{ Å}) \). Thus, weaker bond strength is expected in \( V_8C_7 \) according to the bond valence theory,‡ which also contributes to the aforementioned smaller hydrogen adsorption energy \( \Delta E_{\text{ads}} \). All these factors, including higher surface energy, better hydrogen adsorption energy, lower crystal formation energy (enhanced specific surface area, more active sites) and weaker bond strength contribute additively to the total HER catalytic performance, provide a solid background for \( V_8C_7 \) to win the contest among these vanadium carbides.

Finally, in Fig. 6, we compare these vanadium carbides with the noble metal catalyst Pt by means of the density of states (DOS) and free energy \( \Delta G(H^*) \). It is clear that the characteristic of DOS for \( V_8C_7 \) and VC on (110) and (111) surfaces are rather similar to those of Pt (see Fig. 6(a) and (b)). In both vanadium carbides and Pt systems, most electronic states are located between \(-6 \text{ eV} \) and \(3 \text{ eV} \) relative to the Fermi level and all of them are metallic. Moreover, the d-band states of both (110) and (111) surfaces in \( V_8C_7 \) and VC appear to resemble those of Pt. Indeed, as shown in Fig. 6(c), the resulting best \( \Delta G(H^*) \) values of \( V_8C_7 \) \( (\approx -0.114 \text{ eV}, \text{(110) surface}) \) and VC \( (\approx -0.191 \text{ eV}, \text{(111) surface}) \) are in close proximity to Pt \( (\approx -0.085 \text{ eV}, \text{(111) surface}) \). It is fair to state that vanadium carbides \( V_8C_7 \) and VC belong to the ‘noble metal catalysis’ and posses Pt-like HER mechanism.

4 Conclusion

In summary, first-principles calculation method has been used to systematically analyze the crystal structures, electronic properties, free energies of HER and OER process, surface energies and crystal formation energies of three types of vanadium carbides, i.e., \( V_4C_3, V_8C_7 \) and VC. It is found that vanadium carbides display excellent HER performance but poor OER activity. In particular, \( V_8C_7 \) wins the championship in HER performance among these vanadium carbides. We attribute the exceptional catalytic activity in \( V_8C_7 \) compared to \( V_4C_3 \) and VC to the following factors: (I) larger surface energies trap the ionized hydrogen/oxygen species more easily. (II) More suitable hydrogen adsorption energy \( \Delta E_{\text{ads}} \) boost the HER steps. (III) Lower crystal formation energy and easier formation of C defects increase specified surface area, active sites and provide faster charge transport for HER. (IV) Larger V–C bond length and weaker bond strength contribute to the appearance of proper hydrogen adsorption energy and smaller free energy \( \Delta G(H^*) \). In addition, the remarkable resemblance between VC/\( V_8C_7 \) and Pt in their d-band density of states on (110) and (111) surfaces implies that the HER mechanism of vanadium carbides is Pt-like. Our findings thus bring new insight to the theoretical understanding of the excellent HER performance of vanadium carbides.

Conflicts of interest

The authors declare no competing financial interests.

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