On-chip optical event horizon

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The interaction of waves in nonlinear Kerr waveguides are, under some circumstances, similar to the physics occurring at the horizon of black and white holes. Here, we investigate this analogy in an integrated nonlinear photonic structure through the reflection of a continuous wave on an intense pulse. The resulting frequency conversion of the continuous wave is experimentally demonstrated in a silicon photonic wire waveguide and confirmed by simulations using the generalized nonlinear Schrödinger equation. This demonstration paves the way to efficient all-optical signal processing functionality integrated on a CMOS-compatible waveguide platform.

The manipulation of optical signals by light itself through the interaction of pulses in nonlinear media is an active research area. The goal is to develop low power consumption ultra-fast all-optical devices, for replacing electronics-based systems used today. In this respect, the realization of an all-optical transistor has attracted a lot of attention from the scientific community over the past decades, and still constitutes an active area of research [1]. However, mandatory arduous criteria have to be fulfilled for its demonstration [1], in particular fan-out and cascadability, which are the most difficult to meet. Recently, it has been shown that such devices, with at their heart the strong light-light interaction arising at an optical event horizon, can be realized [2, 3].

The optical analogue of an event horizon occurs when an intense pulse, propagating in a nonlinear waveguide, prevents a weak probe wave traveling at a different velocity from passing through it. This analogy is both interesting for fundamental science as for practical applications. It has been shown that an optical event horizon can mimic the effect of a black or white hole. As such it can act as a laboratory scale universe, to research effects such as the Hawking radiation [4, 5]. Moreover, because of the inherent frequency shift that takes place during the interaction between the two waves, the phenomenon has been pointed out as a mechanism for efficiently converting the frequency of a signal [6]. Note that, the Cherenkov radiation, also known as dispersive wave generation in the extensively studied context of supercontinuum generation, constitutes also an efficient way for the transfer of energy far from the pump wavelength [7].

The first demonstrations of optical event horizons have been realized in optical fibers, by superimposing at the fiber input a weak probe wave together with an intense pulse [4, 8]. More recently, they have been studied through the collision between pulses, generated in topographic fibers designed for that purpose [9]. In these experiments, the weak nonlinearity of silica results in the need for pulses with kilowatt peak power and long interaction lengths, clearly preventing the use of optical fibers for the aforementioned integrated low power applications. Nonlinear interactions in silicon nanophotonic waveguides, on the contrary, arise for watt-level peak power pulses and for millimeter-scale propagation lengths. Such a platform has thus successfully been used, amongst other, for supercontinuum generation at telecommunication wavelengths in millimeter size optical chips [10–12]. In addition, these nanophotonic structures are fully CMOS-compatible making them very good candidates for the realization of integrated low power optical functionalities in a, low-cost, high volume fabrication platform. In this letter, we experimentally demonstrate, to the best of our knowledge the first optical event horizon in an integrated photonic nonlinear structure through the reflection of a weak continuous probe wave on an intense pump pulse. These results pave the way to all-optical functionalities based on the optical analogue of an event horizon in a CMOS-compatible platform.

Our demonstration is realized in a 22 mm-long silicon-on-insulator waveguide with a height of 220 nm and a width of 880 nm. This waveguide has been carefully chosen for its linear dispersion properties. It possesses a zero-dispersion wavelength at 1740 nm (see in the inset of Fig. 1), located between the telecom C-band where the probe is positioned and the pump wavelength positioned around 2 μm in the anomalous dispersion regime.

When propagating in the waveguide, the nonlinear interaction between a continuous probe wave (CW probe) at ωprobe and a pump wave at ωpump can be interpreted as a cascaded-four wave mixing mechanism, leading to a frequency conversion of the CW probe. It has been shown that the conversion from the probe wavelength to a single higher-order idler wavelength component ωidler is efficient when the resonant condition [8, 13]:

\[ D(\omega_{idler} - \omega_{pump}) = D(\omega_{probe} - \omega_{pump}), \] (1)
is fulfilled. The wavenumber $D(\omega - \omega_{\text{pump}}) = \beta(\omega) - \beta_0 - \beta_1 \times (\omega - \omega_{\text{pump}})$ [where $\beta_0 = \beta(\omega_{\text{pump}})$ and $\beta_1 = d\beta/d\omega|_{\omega_{\text{pump}}}$] is the wavenumber of a linear wave at a frequency $\omega$ in a reference frame co-moving with the pump pulse at a frequency $\omega_{\text{pump}}$. In the temporal domain, this frequency shift is the result of the nonlinear phase imprinted upon the CW wave by the pump pulse.

The evolution of the wavenumber $D$ as a function of wavelength for different pump wavelengths is displayed in Fig. 1 for the waveguide used in the experiment. Considering a CW probe at 1541 nm (see dashed line as well as the P point on the blue curve), we can infer from this figure that the idler wave satisfying the resonance condition Eq. (1) (see the I point for the blue curve) is located on the other side of the minimum of the wavenumber $D$ versus wavelength curve (VM point for the blue curve). This peculiar position corresponds to the wavelength that is group velocity matched with the pump wave. For a 2165 nm pump (blue curve), the CW probe at 1541 nm travels faster than the pump and the change in the group velocity resulting from the frequency shift prevents the CW wave to cross the pump pulse. The trailing edge of the pump pulse thus corresponds to an optical horizon for the probe, similar to a white-hole horizon. A similar reasoning can be made for a probe traveling slower than the pump, in this case the leading edge of the pump is similar to a black-hole horizon.

In the experiments, the intense pump pulse at a wavelength of 2085 nm is generated by an optical parametric oscillator (OPO, Spectra Physics OPAL) delivering 180 fs pulses (full width at half maximum, FWHM) at 82 MHz repetition rate. The CW probe, for which the wavelength can be tuned from 1538 nm to 1545 nm, is generated by a CW laser followed by an Er-doped fiber amplifier. At the amplifier output, the CW beam is collimated and the two beams are combined by means of a dichroic mirror. The beams are then coupled into the photonic nanowire using a microscope objective, each of
them exciting only the quasi-TE mode of the waveguide. At the wire output, the light is collected by a lensed fiber and sent to an optical spectrum analyzer (OSA). The experimental output spectra recorded in the range 1250 nm-1700 nm, i.e., up to the wavelength cut-off of our OSA, are displayed in Fig. 2(a) for an on-chip peak pump power of 6.5 W and a 500 µW CW probe. In the experiment, the pump power was progressively increased until the reflection of the probe was clearly visible in the spectrum. The corresponding simulations are shown in Fig. 2(b). These simulations were performed by solving the generalized nonlinear Schrödinger equation (GNLSE), where higher-order chromatic dispersion terms and the first order dispersion of the nonlinearity are included:

\[
\frac{\partial A(z, t)}{\partial z} = i \sum_{k=2}^{7} \frac{i^k}{k!} \beta_k \frac{\partial^k A(z, t)}{\partial t^k} - \frac{\alpha_0}{2} A(z, t) + i \gamma (1 + \frac{i}{\omega_{pump}} \frac{\partial}{\partial t}) A(z, t) \int_{-\infty}^{+\infty} R(t') |A(z, t - t')|^2 dt'.
\]

In this equation, \( A(z, t) \) is the slow-varying envelope of the electric field, \( \beta_k \) are the dispersion coefficients associated with the Taylor series expansion of the propagation constant around the pump frequency \( \omega_{pump} \), \( \alpha_0 = 2\text{dB/cm} \) is the linear loss coefficient, \( \gamma = (234 + iv15) \text{ W}^{-1}\text{m}^{-1} \) is the complex nonlinear parameter and \( R(t') \) is the response function accounting for the instantaneous and delayed Raman contributions to the nonlinearity. The effects of free carriers are not included in this model because we have numerically verified that their contributions are negligible in our experimental configuration.

At the input peak power needed to observe the reflection, it can be seen in Fig. 2 (black curves) and Figs. 3(a,b) and 4 that the pump pulse propagation in the anomalous dispersion region leads to the generation of a supercontinuum extending from 1.3 µm to 2.2 µm. As shown previously, the spectral broadening is the result of self-phase modulation, soliton splitting, as well as the emission of a dispersive wave (DW) [12, 14]. The DW is generated in the normal dispersion region, around 1330 nm. This wavelength corresponds to the degenerate case in the resonant condition Eq. (1) where \( \omega_{probe} = \omega_{pump} \). It is thus given by the crossing points between the \( D \) curves and the horizontal black line in Fig. 4. When only the pump pulse is coupled in the waveguide, only the DW is visible in the recorded output spectrum shown in Fig. 2(a). The output spectrum for the CW alone is shown as the gray curves in Fig. 2 and is essentially undistorted because of the low CW power and the normal dispersion.

However, when both the pump and the CW probe are propagating together, the output spectra show other distinctive features. Close to the probe wavelength a wide pedestal can be seen. It is generated during the first part of the propagation dynamics [see Fig. 3(c)] and is the result of the cross phase modulation on the CW probe which overlaps with the input pump pulse. On either sides of the probe, two narrow peaks, labeled RS and RAS in Fig. 2 can also be identified. These peaks are \( \pm 17 \text{ THz} \) away from the wavelength of the CW probe and correspond to the generation of Raman anti-Stokes (RAS) and Raman Stokes (RS) photons from the probe wave, as confirmed by canceling in simulation the delayed nonlinear term in Eq. (2). The remaining features are the two broad peaks labeled Idler #1 and #2. Their positions agree quite well with the numerical simulations and are clearly shifted toward the probe for decreasing probe wavelength. The simulated spectral and temporal evolution along the propagation distance plotted in
Fig. 3(c)-(d) show that the reflection of the CW probe actually occurs after the soliton fission that follows the temporal pulse compression [Note that, as expected and contrary to [2] [8], the reflection of the probe onto the pump is not clearly visible in the simulated temporal evolution plotted in Fig. 3(d) because the probe is a continuous wave giving an almost temporal uniform background]. The fundamental solitons resulting from the fission have a pulse duration of 70 fs and are centered around 2115 nm, 2165 nm and 1995 nm. The simulations displayed in Fig. 4 with an input pulse corresponding to one of these fundamental solitons with the same peak power as just after the fission (1.8 W) clearly show that, in our experiment, the Idler #1 wave is the result of the reflection of the probe on the soliton emitted at 2165 nm and the Idler #2 is related to the reflection on the soliton at 2115 nm. The idler wavelengths at 1436 nm and 1457 nm, respectively, are in excellent agreement with the GNLS modeling and the experimental results reveals that in our experiment the reflection takes place after the soliton fission. An even better demonstration is thus in principle possible by resorting to shorter pump pulses of the order of 50 fs. Our experimental results improve the understanding of nonlinear interactions in silicon waveguides with ultrashort pulses and foster further study of the potential of on-chip efficient frequency converters and all-optical transistors based on the physics of the optical analogue of an event horizon.

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**Fig. 4.** Simulated output spectra for a 500 µW CW input probe at 1541 nm together with a 6.5 W, 180 fs sech²-shaped input pump wave at 2085 nm (red curve) or with a 1.8 W, 70 fs sech²-shaped input pump wave at 2115 nm (yellow curve) or at 2165 nm (blue curve). The corresponding output spectrum, recorded with a Fourier transform optical spectrum analyser, for a 6.5 W, 180 fs input pump wave at 2085 nm is shown in the inset in the wavelength range 1700 nm-2400 nm. The red curve is shifted by 10 dB for clarity.

The idler wavelength also gets closer to that wavelength in accordance with Fig. 1. Note that since a CW probe has been used in this proof of principle experimental work, only a very small part of the probe interacts with the pump pulse train. The frequency conversion is thus not expected to be efficient. However, by replacing the CW probe by a pulsed probe, the frequency conversion can be very efficient as previously shown [6]. For non negligible frequency conversion, the resulting spectral change on the soliton pump pulse affects its velocity, a mechanism that has been recognized to be suitable to make useful optical transistors [1] [2].

In conclusion, we have experimentally studied an optical analogue of an event horizon in a silicon on insulator nanophotonic waveguide. We have unambiguously observed the frequency conversion of a CW wave when propagating with an intense pump pulse. This conversion occurs when its wavelength is close to the wavelength that is group velocity matched with the pump. The excellent agreement between the GNLS modeling and the experimental results reveals that in our experiment the reflection takes place after the soliton fission. An even better demonstration is thus in principle possible by resorting to shorter pump pulses of the order of 50 fs. Our experimental results improve the understanding of nonlinear interactions in silicon waveguides with ultrashort pulses and foster further study of the potential of on-chip efficient frequency converters and all-optical transistors based on the physics of the optical analogue of an event horizon.

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