The UHECR dipole and quadrupole in the latest data from the original Auger and TA surface detectors

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The sources of ultra-high-energy cosmic rays are still unknown, but assuming standard physics, they are expected to lie within a few hundred megaparsecs from us. Indeed, over cosmological distances cosmic rays lose energy to interactions with background photons, at a rate depending on their mass number and energy and properties of photonuclear interactions and photon backgrounds. The universe is not homogeneous at such scales, hence the distribution of the arrival directions of cosmic rays is expected to reflect the inhomogeneities in the distribution of galaxies; the shorter the energy loss lengths, the stronger the expected anisotropies. Galactic and intergalactic magnetic fields can blur and distort the picture, but the magnitudes of the largest-scale anisotropies, namely the dipole and quadrupole moments, are the most robust to their effects. Measuring them with no bias regardless of any higher-order multipoles is not possible except with full-sky coverage.
In this work, we achieve this in three energy ranges (approximately 8–16 EeV, 16–32 EeV, and 32–\infty EeV) by combining surface-detector data collected at the Pierre Auger Observatory until 2020 and at the Telescope Array (TA) until 2019, before the completion of the upgrades of the arrays with new scintillator detectors. We find that the full-sky coverage achieved by combining Auger and TA data reduces the uncertainties on the north-south components of the dipole and quadrupole in half compared to Auger-only results.

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1. Introduction

While on general grounds the anisotropies of cosmic rays (CR) at highest energies are expected to give a key to understanding of their sources, in practice the deflections of cosmic rays in (highly uncertain) magnetic fields make this task extremely difficult. Even though the angular resolution in the reconstruction of CR arrival directions is good (~1°), no anisotropies have been discovered at small angular scales of order a few degrees, likely due to a washing effect of the magnetic deflections.

Even when individual sources are not resolved, at large angular scales the anisotropies are expected to arise from a non-homogeneous source distribution in the Universe at distances of 50–100 Mpc. The effect of magnetic deflections at these angular scales, particularly for the dipole and quadrupole harmonics, may not be dominant. The non-zero dipole anisotropy in the CR distribution, with an amplitude of 6.5% in the equatorial plane, has indeed been discovered by the Pierre Auger Observatory (hereafter Auger) [1] at energies $E > 8 \text{ EeV}$. The equatorial dipole has also been measured by the Telescope Array (TA) [2], with the result in agreement with that of Auger but not significant alone due to small statistics.

Both Auger and TA observatories have incomplete sky coverage, which makes the unambiguous determination of all multipole components impossible. To achieve the full-sky coverage, they have to be combined together. However, this cannot be trivially done by simply combining the events detected by the two observatories with their nominal energy estimates, as they both have potentially different systematic uncertainties in the energy determination, and these differences may affect the sky distribution of events in a given energy range in the combined data set. The energy scales have to be cross-calibrated before combining the data. This can be done from the data themselves without any extra assumptions on the nature of the energy determination systematics [3] by comparing the data of the two observatories in the equatorial band where their exposures overlap.

The purpose of this study is to cross-calibrate energy scales of the Auger and TA observatories in the energy range $E \gtrsim 10 \text{ EeV}$ and to determine in an assumption-free way the dipole and quadrupole components of the UHECR flux in this energy range. This study is a development of the previous analyses [3–5] in the following three respects: (i) we use the updated data sets, (ii) we cross-calibrate the energy scales in three energy bins relaxing the assumption that the difference in energy scales is energy-independent and (iii) we carefully trace all sources of uncertainties and propagate them into the final result.

2. The datasets

The Pierre Auger Observatory [6] is a hybrid detector of UHECRs located in the Southern hemisphere in Argentina at a latitude of −35.2°. It consists of a surface array of 1660 water-Cherenkov detectors covering an area of approximately 3000 km$^2$, overlooked by the fluorescence detector composed of 27 fluorescence telescopes. The detector is taking data since January 2004. In this work, we use the dataset described in Ref. [7], consisting of events detected by the surface detector (SD) array from 2004 Jan 01 to 2020 Dec 31. Its geometric exposure is 110 000 km$^2$ yr sr. In order to correct for the effects of the finite energy resolution, which in the case of a decreasing energy spectrum tend to make the raw measured spectrum higher than the actual one, we divide the
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Figure 1: The combined Auger + TA effective exposure in the first energy bin, see Sect. 3. The yellow band on the left panel indicates the range of declinations visible to both observatories used for the cross-calibration of energy scales.

The effects of the tilt of the SD array and of the non-uniformity of its aperture in sidereal time were found to be minor in Ref. [1] (of the order of $1/4$ and $1/20$ of the statistical uncertainties, respectively) and are neglected in this work.

The Telescope Array [9] is a hybrid detector of UHECRs located in the Northern hemisphere in Utah, USA at a latitude of $39.3^\circ$. It is taking data since May 2008. The surface detector of TA consists of 507 plastic scintillator detectors covering an area of about 700 km$^2$. The fluorescence detector of TA is composed of 38 fluorescence telescopes arranged in 3 towers overlooking the surface detector area. In this work, we use the events with the zenith angles $\theta < 55^\circ$ detected by the TA SD array from 2008 May 11 to 2019 May 10 with the selection criteria as described in [3]. The effective exposure, accounting for the effects of the energy resolution, in the energy range used in this work depends non-monotonically on energy, with a minimum value of $13\,200$ km$^2$ yr sr in the energy bin $19.7 < \log_{10}(E/\text{eV}) < 19.8$, a maximum of $15\,400$ km$^2$ yr sr in $20.0 < \log_{10}(E/\text{eV}) < 20.1$, and a value of $15\,100$ km$^2$ yr sr in the bins $\log_{10}(E/\text{eV}) \geq 20.2$.

We assume that the effective exposure of each detector array factorizes into an effective area $E$ which depends on the energy $E$ but not on the arrival direction, and a geometric exposure $\omega_{\text{geom}}$ which only depends on the declination as described in Ref. [10]. In the case of Auger, we consider two different effective areas for vertical ($\theta < 60^\circ$) and inclined ($\theta \geq 60^\circ$) events due to the different reconstruction techniques used for these two zenith angle ranges. As an example, the combined exposure averaged over the lowest of the three energy bins in which we search for anisotropies (see Sect. 3) is shown in Fig. 1.

3. The cross-calibration of energy scale

As already mentioned, when combining data from different detectors to infer the large-scale anisotropy, it is important to ensure that the energy thresholds used for them match, otherwise spurious detections of the north-south anisotropy may arise. To eliminate this problem, we calibrate the Auger and TA energy scales to each other using the events detected in the equatorial region of
the sky where both observatories have exposure (see Fig. 1). The idea behind the cross-calibration procedure is that the true UHECR flux integrated over the common band as a function of energy, \( \phi^\text{true}(E) \), can be estimated in each of the two observatories independently. When the energy scales match, these two estimates must agree at all energies. Note that this procedure does not allow one to determine the true energy scale, only to eliminate a possible mismatch in scales between the two observatories. This is sufficient, however, for the purpose of the present analysis.

To estimate the flux we use the unbiased estimator introduced in [11], which is essentially the sum over events in the band weighted with the inverse exposure \( \omega_a \) of each observatory \( a = (\text{Auger}, \text{TA}) \). In the energy bin \( j \), defined in terms of the nominal energy of the corresponding observatory, the flux estimate is \( \phi^\text{est}_{aj} = \sum_k 1/\omega_a(n_k) \), where \( n_k \) is the arrival direction of a given event and the sum runs over the events \( k \) with energies \( E_{ak} \in [E_{aj}, E_{aj+1}) \) and arrival directions in the common band \( \delta_k \in (\delta_{\text{min}}, \delta_{\text{max}}) \). It can be shown that, provided the exposure does not vanish anywhere in the band and regardless of the variations of the flux density \( J(E, n) \) over the sky, the quantity \( \phi^\text{est}_{aj} \) is an unbiased estimator of \( \phi^\text{true}_j = \int_{E_{aj}}^{E_{aj+1}} \int_{\delta_{\text{min}}}^{\delta_{\text{max}}} J(E, n) dE d\Omega \). The latter is by definition a detector-independent quantity, and hence, in the absence of energy scale differences, the two estimators \( \phi^\text{est}_{\text{Auger},j} \) and \( \phi^\text{est}_{\text{TA},j} \) must agree within statistical uncertainties in all energy bins. The cross-calibration consists in determining the energy conversion function between the two observatories such that this requirement is satisfied. Unlike in Refs. [4, 5], where the cross-calibration was applied to energy thresholds — which is equivalent to assuming a constant energy rescaling factor — in this work we assume a functional form for the \( E_{\text{TA}} \leftrightarrow E_{\text{Auger}} \) conversion with free parameters which we fit to satisfy the flux matching conditions in the common band.

The fiducial boundaries of the common band are chosen as follows. The intersection of the Auger and TA fields of view is \((-15.7^\circ, +44.8^\circ)\), but in the areas close to the edge \( 1/\omega_a \) becomes very large, which would result in increased statistical uncertainties if the entire intersection was used. Instead, we choose a fiducial band \((\delta_{\text{min}} = -11^\circ, \delta_{\text{max}} = +43^\circ)\), which are the values that minimize the expected total statistical uncertainties rounded to the nearest degree.

We bin the events in logarithmic nominal energy bins defined as \( \log_{10}(E_{\text{Auger},j}/\text{eV}) = 18.9 + 0.1j \) and \( \log_{10}(E_{\text{TA},j}/\text{eV}) = 19.0 + 0.1j \), for \( j = 0, 1, \ldots \). The last non-empty bin is \([20.1, 20.2)\) for Auger and \([20.2, 20.3)\) for TA. We then compute the corresponding statistical uncertainties of the flux estimators as \( \sigma_{aj} = \sqrt{\sum_k 1/\omega_a(E_k, n_k)^2} \), where the sum runs over the same events as above.

We assume a power law for the energy conversion in the range \( E_{\text{TA}} \geq 10 \text{ EeV} \) characterized by two parameters \( \theta_E = (\alpha, \beta) \):

\[
E_{\text{Auger}} = E_0 e^{\alpha} (E_{\text{TA}}/E_0)^\beta, \\
E_{\text{TA}} = E_0 e^{-\alpha/\beta} (E_{\text{Auger}}/E_0)^{1/\beta}
\]

(1)

with \( E_0 = 10 \text{ EeV} \). The goal of the cross-calibration is to determine the parameters \( \alpha \) and \( \beta \). If we binned the events in corrected energies, events would move from one bin to another when the parameters are changed, producing discontinuities in the flux estimator. To avoid this technical problem, we fit both Auger and TA data to a model spectrum in the band while keeping both sets of nominal energy bins fixed. For the model spectrum we use the twice-broken\(^1\) power law

\(^1\)We find that using instead the smoothed breaks as in Ref. [8] would make only a minor difference in the goodness
\( \alpha = -0.154 \pm 0.013 \)

\( \beta = 0.937 \pm 0.017 \)

\( \rho_{\alpha\beta} = -0.177 \)

| Auger scale | TA scale |
|-------------|----------|
| \( 2.65 \times 10^{-19} \) | \( 3.14 \times 10^{-19} \) |
| \( 2.53 \) | \( 2.43 \) |
| \( 11.7 \) | \( 13.9 \) |
| \( 2.92 \) | \( 2.80 \) |
| \( 49.6 \) | \( 65.1 \) |
| \( 5.66 \) | \( 5.37 \) |

\[ \chi^2 / n_{\text{dof}} = 15.6 / 14 \ (p = 0.34) \]

Table 1: Best-fit parameter values from the spectrum fit used for the cross-calibration procedure.

with normalization \( f_0 \), break energies \( E_{AB} \) and \( E_{BC} \) and spectral indices \( \gamma_A \), \( \gamma_B \) and \( \gamma_C \), for a total of six additional parameters \( \theta_j \). For each set of resulting 8 parameters, we compute the model predictions \( \phi_{\text{pred}}(\theta_j, \theta_E) = \int_{E_j}^{E_{j+1}} f_{\text{band}}(E; \theta_j) \, dE \) where \( E \) is some (arbitrarily chosen) energy scale and the bin boundaries \( E_j \) are obtained by converting the bins of the corresponding observatory into that scale. Finally, we compute \( \chi^2 \) according to a log-normal distribution,

\[ \chi^2 = \sum_{a,j} \left( \frac{\ln \phi_{\text{est.}}^2(a_j) - \ln \phi_{\text{pred.}}^2(\theta_j, \theta_E)}{(\sigma_{a_j} / \phi_{a_j}^2)^2} \right), \]

which we found to adequately describe the probability distribution of the flux estimator in simulations provided there are \( \geq 10 \) events in the fiducial band in each energy bin, which we achieve by combining together the last energy bins of each dataset until this condition is achieved (for Auger, 19 events with \( \log_{10}(E/\text{eV}) \geq 19.9 \); for TA, 11 events with \( \log_{10}(E/\text{eV}) \geq 20.0 \), remaining with 11 bins for both Auger and TA). The resulting best fit is shown in Table 1. If the exponent \( \beta \) is fixed to 1 as corresponds to a constant rescaling factor between Auger and TA energies, the best fit becomes \( \alpha = -0.163 \pm 0.012 \) with a \( \chi^2 / n \) of 29.1/13. The energy-dependent rescaling of Table 1 is thus favored over a constant one at the 3.7\( \sigma \) level. The possible origins of such an energy-dependence are currently being investigated by the two collaborations [13].

Based on the cross-calibration results, the following energy bin boundaries have been chosen for the calculation of the dipole and quadrupole components:

| Auger scale | 8.57 \pm 0.11 \text{ EeV} | 16 \text{ EeV} | 32 \text{ EeV} |
|-------------|-----------------|--------|--------|
| TA scale | 10 \text{ EeV} | 19.47 \pm 0.32 \text{ EeV} | 40.8 \pm 1.1 \text{ EeV} |

The lowest energy of 10 \text{ EeV} (TA) is fixed by the availability of the TA events, while the other two boundaries 16 \text{ EeV} (Auger) and 32 \text{ EeV} (Auger) are chosen so as to match the previous Auger dipole analysis. The exposures in these three bins, appropriately corrected for a slight energy dependence of exposure in each observatory, are (87 400 + 24 600) \text{ km}^2 \text{ yr sr}, (87 200 + 24 600) \text{ km}^2 \text{ yr sr} and (86 600 + 24 400) \text{ km}^2 \text{ yr sr} for Auger vertical + inclined and 14 200 \text{ km}^2 \text{ yr sr}, 14 000 \text{ km}^2 \text{ yr sr} and 13 700 \text{ km}^2 \text{ yr sr} for TA.

The exposures of the two detectors are only known with an uncertainty of approximately \( \pm 3\% \) each. An over- or under-estimate of the TA-to-Auger exposure ratio by \( \pm 4.2\% \) would result in an over- or under-estimate of the parameter \( \alpha \) by 0.023, i.e. of \( E_{\text{Auger}}(E_{\text{TA}} = 10 \text{ EeV}) \) by 0.20 \text{ EeV}, as well as of \( \beta \) by \( \pm 0.06 \), meaning the relative uncertainty shrinks at higher energies. On the other hand, the effect of such an uncertainty on the final anisotropy results would almost completely cancel out those of the uncertainty in the exposure ratio itself. For this reason, we neglect this source of uncertainty in the following.

\( \frac{\Delta \chi^2}{\chi^2} < 0.3, \Delta \rho = 0.02 \) and a negligible difference in the energy conversion (\( \Delta \alpha = 4 \times 10^{-4}, \Delta \beta = 10^{-3} \)).
3.1 Propagation of the statistical uncertainty on the calibration fit

The uncertainty on the correspondence between energy thresholds causes as an “effective” uncertainty on the exposure ratio. If we overestimate e.g. the Auger threshold corresponding to a given TA threshold, we underestimate the flux in the Auger field of view. The effect on large-scale anisotropy searches can be approximated to that of overestimating its exposure, provided the anisotropies themselves do not appreciably change with energy over such a range. To quantify this uncertainty, we propagate the statistical uncertainties of the fit on $\alpha$ and $\beta$ (Table 1) to the quantity

$$\ln \left( \frac{\phi_{TA,j'}(\theta_j, \alpha_{\text{best}}, \beta_{\text{best}})}{\phi_{TA,j'}(\theta_j, \alpha, \beta)} \right) \frac{\phi_{\text{Auger},j}(\theta_j, \alpha, \beta)}{\phi_{\text{Auger},j}(\theta_j, \alpha_{\text{best}}, \beta_{\text{best}})}$$

where $\phi_{TA,j'}$ is computed as above, but over the “wide” energy bins $j'$ we are going to use for anisotropy searches, not the “narrow” energy bins $j$ used for the cross-calibration — in other words, how much we would overestimate the TA-to-Auger flux ratio if the true conversion parameters were $(\alpha, \beta)$ but we assumed they were $(\alpha_{\text{best}}, \beta_{\text{best}})$. The result is $\pm 2.5\%$, $\pm 2.5\%$ and $\pm 6.5\%$ in the first, second and third energy bin, respectively. It can be noted that these values are roughly of the order of $(\gamma - 1)$ times the relative uncertainties on the energy thresholds, as they would be in the case of a single threshold for an integral flux $\int_{E_0}^{+\infty} J_{\text{band}}(E) \, dE \propto E^{-(\gamma - 1)}$.

4. Results on large-scale anisotropies

The UHECR flux $\Phi(n)$ can be represented as a sum of spherical harmonics $Y_{l,m}$,

$$\Phi(n) = \sum_{l=0}^{+\infty} \sum_{m=-l}^{+l} a_{lm} Y_{lm}(n), \quad a_{lm} = \int_0^{2\pi} Y_{lm}(n) \Phi(n) \, d\Omega. \quad (4)$$

The coefficients $a_{lm}$ represent anisotropies on scales $O(180^\circ/\ell)$. The contribution of the two lowest non-trivial harmonics $l = 1, 2$, the dipole and quadrupole, can be rewritten in terms of a dipole vector $d$ and the symmetric traceless quadrupole tensor $Q_{ij}$ as follows,

$$\Phi(n) = \Phi_0 \left(1 + d \cdot n + \frac{3}{2} n \cdot Q_{ij} n + \cdots\right) \quad (5)$$

where $\Phi_0 = \sqrt{4\pi} a_{00}$, $d_x = \sqrt{3} a_{11}/a_{00}$, $d_y = \sqrt{3} a_{1-1}/a_{00}$, $d_z = \sqrt{3} a_{10}/a_{00}$, $Q_{xx} = 2\sqrt{3} a_{22}/a_{00}$, $Q_{xz} = \sqrt{15} a_{21}/a_{00}$, $Q_{yz} = 2\sqrt{3} a_{21}/a_{00}$, $Q_{zz} = \sqrt{15} a_{2-1}/a_{00}$, and the other components of $Q_{ij}$ can be computed from its symmetry and zero trace condition.

Using a full-sky dataset with the combined exposure $\omega(n)$ non-zero everywhere, each $a_{lm}$ can be estimated independently as $\sum_k Y_{lm}(n_k)/\omega(n_k)$. We estimate the statistic uncertainties and the correlations between them as $\sigma_{\ell m}^2 \approx \sigma_{\ell m} \rho_{\ell m, \ell m'} = \sum_k Y_{\ell m}(n_k) Y_{\ell m'}(n_k)/\omega(n_k)^2$. As for the uncertainties due to the energy cross-calibration, we compute them by computing $a_{lm}^2$ assuming the exposure $\omega^* = \omega_{\text{Auger}} + e^{k\theta} \omega_{\text{TA}}$ where $k$ is the “effective” exposure ratio uncertainty described in subsection 3.1, and taking $\sigma_{\text{sys}}(d_z) = \frac{1}{2} (d_z^* - d_z^*)$, $\sigma_{\text{sys}}(Q_{zz}) = \frac{1}{2} (Q_{zz}^* - Q_{zz}^*)$, and similarly for other components. The rotationally invariant quantities $C_1 = \frac{4\pi}{\Omega} |d|$ and $C_2 = \frac{4\pi}{\Omega} \Sigma_{ij} Q_{ij}^2$ (normalized to $C_0 = 4\pi$ i.e. to $\Phi_0 = 1$) can also be computed as $C_\ell = \frac{1}{2\ell+1} \Sigma_{m=-\ell}^{+\ell} a_{\ell m}^2$. The results in the three energy bins defined above are shown in Table 2. The spherical harmonic expansion of the UHECR flux in these bins, truncated at $\ell \leq 2$, is shown in Figure 2 in comparison with the flux estimate from the combined data in the corresponding bin, smoothed with the window size of $45^\circ$. 

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The second is due to that on the energy cross-calibration. The statistical uncertainties are uncorrelated.

The UHECR dipole and quadrupole distribution is estimated from our data. The first uncertainty is statistical, as well as slightly smaller uncertainties on the other dipole and quadrupole components.

Using full-sky data, we have estimated the dipole and quadrupole moments of the UHECR flux at the energies (Auger) [8.57 EeV, 16 EeV] [16 EeV, 32 EeV] [32 EeV, +∞] and (TA) [10 EeV, 19.47 EeV] [19.47 EeV, 40.8 EeV] [40.8 EeV, +∞].

The dipole and quadrupole moments estimated from our data. The first uncertainty is statistical, and with uncertainties on $d_z$ and $Q_{zz}$ about twice as small, as well as slightly smaller uncertainties on the other dipole and quadrupole components. None of the moments shown in Table 2 are significant with $> 3\sigma$ pre-trial significance, except the dipole along the y axis in the lowest energy bin already reported in Ref. [1].

| Energies (Auger) | [8.57 EeV, 16 EeV] | [16 EeV, 32 EeV] | [32 EeV, +∞] |
|------------------|---------------------|------------------|---------------|
| $d_x$ [%]        | $-0.7 \pm 1.1 \pm 0.0$ | $+1.6 \pm 2.0 \pm 0.0$ | $-5.3 \pm 3.9 \pm 0.1$ |
| $d_y$ [%]        | $+4.8 \pm 1.1 \pm 0.0$ | $+3.9 \pm 1.9 \pm 0.1$ | $+9.7 \pm 3.7 \pm 0.0$ |
| $d_z$ [%]        | $-3.3 \pm 1.4 \pm 1.3$ | $-6.0 \pm 2.4 \pm 1.3$ | $+3.4 \pm 4.7 \pm 3.6$ |
| $Q_{xx} - Q_{yy}$ [%] | $-5.1 \pm 4.8 \pm 0.0$ | $+13.6 \pm 8.3 \pm 0.0$ | $+43 \pm 16 \pm 0$ |
| $Q_{xz}$ [%]     | $-3.9 \pm 2.9 \pm 0.1$ | $+5.4 \pm 5.1 \pm 0.0$ | $+5 \pm 11 \pm 0$ |
| $Q_{yz}$ [%]     | $-4.9 \pm 2.9 \pm 0.0$ | $-9.6 \pm 5.0 \pm 0.1$ | $+11.9 \pm 9.8 \pm 0.2$ |
| $Q_{zz}$ [%]     | $+0.5 \pm 3.3 \pm 1.7$ | $+5.2 \pm 5.8 \pm 1.7$ | $+20 \pm 11 \pm 5$ |
| $C_1$ [10⁻³]    | $4.8 \pm 2.0 \pm 1.2$ | $7.6 \pm 4.6 \pm 2.2$ | $19 \pm 12 \pm 4$ |
| $C_2$ [10⁻³]    | $0.85 \pm 0.66 \pm 0.02$ | $3.1 \pm 2.2 \pm 0.2$ | $15.5 \pm 8.9 \pm 2.4$ |

Table 2: The dipole and quadrupole moments estimated from our data. The first uncertainty is statistical, the second is due to that on the energy cross-calibration. The statistical uncertainties are uncorrelated ($-0.1 < \rho < 0.1$) except $\rho(d_x, Q_{xx}) = \rho(d_y, Q_{yz}) = 0.45$ and $\rho(d_z, Q_{zz}) = 0.53$.

5. Discussion

Using full-sky data, we have estimated the dipole and quadrupole moments of the UHECR flux distribution without any assumptions about higher-order multipoles. The results are compatible with Auger-only ones assuming $\ell_{\text{max}} = 2$ [7], but with uncertainties on $d_z$ and $Q_{zz}$ about twice as small, as well as slightly smaller uncertainties on the other dipole and quadrupole components. None of the moments shown in Table 2 are significant with $> 3\sigma$ pre-trial significance, except the dipole along the y axis in the lowest energy bin already reported in Ref. [1].

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Figure 2: Left: Spherical harmonic expansion of the flux inferred from our data up to $\ell = 2$ (dipole and quadrupole) in the three energy bins. Right: Measured flux averaged over 45°-radius top-hat windows.
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