Three-dimensional (3D) topological insulator (TI) has emerged as a unique state of quantum matter and generated enormous interests in condensed matter physics. The surfaces of a 3D TI consist of a massless Dirac cone, which is characterized by the $Z_2$ topological invariant. Introduction of magnetism on the surface of a TI is essential to realize the quantum anomalous Hall effect and other novel magneto-electric phenomena. Here, by using a combination of first-principles calculations, magneto-transport and angle-resolved photoemission spectroscopy (ARPES), we study the electronic properties of gadolinium (Gd)-doped Sb$_2$Te$_3$. Our study shows that Gd doped Sb$_2$Te$_3$ is a spin-orbit-induced bulk band-gap material, whose surface is characterized by a single topological surface state. Our results provide a new platform to investigate the interactions between dilute magnetism and topology in magnetic doped topological materials.

Keywords: Angle resolved photoemission spectroscopy (ARPES), magnetism, topological insulator, gadolinium-doped, doping, Dirac state

1 INTRODUCTION

In topological quantum materials (TQMs), the interplay of magnetism and topology can give rise to profoundly alluring phenomena including quantum anomalous Hall effect (QAHE), topological electromagnetic dynamics, and generate new states such as magnetic Dirac and Weyl semimetals, axion insulators, etc. (Hasan and Kane, 2010; Li et al., 2010; Qi and Zhang, 2011; Hasan et al., 2015). Although multiple intrinsic magnetic TQMs have been proposed theoretically (Tang et al., 2016; Wang, 2017), their experimental realizations are rare, other than a few exceptions of magnetic Weyl, multiferromagnetic magnetic material, and nodal-line fermionic phase compounds (Hosen et al., 2018; Belopolski et al., 2019; Kabir et al., 2019). Recently, a new magnetic topological insulator has been theoretically proposed and later experimentally realized in thin-films and single crystals of MnBi$_2$Te$_4$ (Chen et al., 2019; Li et al., 2019; Otrokov et al., 2019; Zhang et al., 2019). This system possesses a long-range antiferromagnetic (AFM) order and contributes a pragmatic platform to understand many compelling phenomena and phases, such as QAHE (Deng et al., 2020), axion insulator phase (Liu et al., 2020; Regmi et al., 2020), high number Chern insulator (Ge et al., 2020), and AFM TIs (Otrokov et al., 2019). Despite these recent developments, there are still several mysteries and challenges concerning the topological electronic structure and its interplay with magnetism. Specifically, there is little information on how topological properties are effected by dilute...
magnetism and how magnetic dopants can modify the electronic structure of a material. Time reversal symmetry in topological materials can be broken by doped magnetic impurities, yielding gap at the Dirac point (Chen et al., 2010; Katmis et al., 2016). Earlier attempts have been made to investigate the doped magnetic materials or the proximity effect in magnetic heterostructure of topological materials and magnetic insulators, in which the magnetic response is weak (Chang et al., 2013; Chang et al., 2015). Typically, increased levels of dopants may raise the exchange field, but lower the sample quality and reduce electronic mobility (Xu et al., 2012; Checkelsky et al., 2014; Li et al., 2016). Consequently, QAHE has been realized at very low temperatures in some previous experiments (Chang et al., 2013; Chang et al., 2015). These shortcomings have dragged behind the pace of the advancement of these materials for potential applications. Therefore, to generate more robust application platforms, we must find magnetic dopants that promote strong exchange fields at very low concentrations.

To date, doped TIs have been studied by doping 3d transition metals such as V, Cr, Mn, Fe, and Cu, where the doping generates various magnetic properties such as ferromagnetism, antiferromagnetism, and superconductivity (Zhou et al., 2006a; Hor et al., 2010; Haazen et al., 2012). But to realize the QAHE, very low temperatures are needed to enhance the magnetic moments and suppress bulk dissipation channels, therefore improved materials are required (Kou et al., 2014). To address this challenge, we utilize magnetism of 4f-electron elements as an alternative to 3d transition metals to dope the topological material. Due to their well-shielded 4f shell, the large moment rare earth (RE) ions (especially gadolinium) are expected to behave like localized magnetic moments in the host matrix, leading to an overall paramagnetic behavior in the doped system (Jensen and Mackintosh, 1991). However, measurements of RE-doped systems as well as pure RE metals have revealed a variety of magnetic properties, which are often complex and unpredictable (Jensen and Mackintosh, 1991). Previous studies of doped 3D TIs have indicated that the size of the Dirac gap increases with the size of the magnetic moment and increased gap size provides greater flexibility for exploring magnetic TI physics (Chen et al., 2010). Hence, large magnetic moment doping studies have already been conducted by utilizing Dy or Ho with moments 2–3 times larger than those typically observed in 3d transition metal-doped systems (Harrison et al., 2015).

Although some RE-doped systems such as Gd doped Bi2Te3 and Bi1.09Gd0.06Sb0.85Te3 have been studied by ARPES to confirm the existence of the topological surface state (TSS) (Harrison et al., 2014; Shikin et al., 2019), to date, no study of Gd doped Sb2Te3 has been performed to probe the effect of dilute magnetism in it with its basic transport or electronic properties. Therefore, we utilize ARPES, thermodynamic and magneto-transport experiments, complemented by first principle calculations to investigate both the bulk and surface states of Gd0.01Sb1.99Te3. The low-temperature electrical resistivity of Gd0.01Sb1.99Te3 reveals a subtle antiferromagnetic ordering below 2.4 K. For the first time, we report the direct observation of single Dirac cone at the Γ point in the dilute magnetic topological material Gd0.01Sb1.99Te3 by scanning over the entire Brillouin zone (BZ) of this crystal using ARPES and first-principles calculations. Our findings would initiate a new stage to study the interplay between dilute magnetism and topology in doped topological materials.

2 CRYSTALS GROWTH, CRYSTAL STRUCTURE, AND SAMPLE CHARACTERIZATION

The growth condition of Gd doped Sb2Te3 is similar to previously reported undoped Sb2Te3 (Sultana et al., 2018). Single crystals of Gd0.01Sb1.99Te3 were grown by melting the stoichiometric mixture of elemental Gd, Sb and Te at temperature of 1123 K for 24 h in a sealed vacuum quartz tube. The sample was then cooled down over a period of 48 h until it reaches 893 K, and was stored at this temperature for additional 96 h before quenching in liquid nitrogen. In this way, crystals of centimeter size with a shiny surface could efficiently be attained. Magnetization, electrical resistivity (four-probe method), and heat capacity measurements have been performed using a Quantum Design DynaCool-9 system equipped with a 9 T superconducting magnet and VSM, ETO, and HCP options. The phase purity of the sample was confirmed, with no observation of contaminated phases, by a powder x-ray diffraction (XRD) method (PANalytical X’Pert PRO diffractometer). The XRD pattern was well fitted with the hexagonal structure of Gd0.01Sb1.99Te3, with space group R3m.

The trigonal crystal structure (R3m, #166) of Sb2Te3 and 3D bulk BZ along with its projection onto the [001] surface with the high symmetry points (marked) are presented in Figures 1A,B, respectively. Figure 1C shows the core level spectrum which shows the characteristics peaks for Te and Sb elements. In Figure 1D, the theoretically obtained bulk band structure of Gd doped Sb2Te3 is shown. The first-principles calculations were carried out on a 500 atom unit cell to capture the dilute Gd concentration and the AFM coupling between pairs of impurities (see Supplementary Figures S1 and S2 for more detail). Additionally, the system was treated using spin-orbit coupling and full non-collinear magnetism for all atomic species. A direct band gap of 0.18 eV is observed at the Γ high symmetry point of the BZ, with the remaining valence bands in the range of 0.45–0.75 eV below the Fermi level. Noticeably, at the Γ point, the hole-like valence band is robust against the Gd-doping, whereas the well localized Gd-4f states produce a flat Gd-4f impurity level, which cuts the electron-like conduction band, producing a narrow gap.

In order to determine the magnetic properties of Gd0.01Sb1.99Te3, we have performed a detailed magnetization and magnetic susceptibility measurements. We have also used the magnetic measurements, together with energy dispersive spectroscopy (EDS) studies (see Supplementary Figures S3 and S4 for more detail), to precisely determine the level of Gd content in our crystals. Figure 1E shows the temperature dependence of the magnetic susceptibility of Gd0.01Sb1.99Te3 single crystals with the applied magnetic field parallel to the c
axis. Whilst the parent antimony telluride is itself a diamagnetic material (Van Itterbeek et al., 1966), our crystals display a characteristic Curie-Weiss magnetic susceptibility, confirming the presence of Gd in our Sb₂Te₃ crystals. The experimental data have been analyzed using a modified Curie-Weiss law (CW), \[ \chi(T) = \frac{C}{T - \theta} + \chi_0 \]
where C is the Curie constant, \( \theta \) is the Weiss temperature, and \( \chi_0 \) is the temperature-independent contribution, most probably associated with the parent Sb₂Te₃. By fitting the CW law to the experimental data of our crystals yields, \[ \chi_0 = -1.90 \times 10^{-4} \text{ emu/mol}, \theta = -1.19 \text{ K}, \text{ and } C = 0.0664 \text{ emu K mol}^{-1}. \] The effective moment \( \mu_{eff} = 0.7288 \mu_B/\text{f.u.} \) is calculated with \( \chi_0 \) taken out. The magnitude and negative sign of \( \chi_0 \) agrees well with the previously obtained magnetic susceptibility values of Sb₂Te₃, \(-2.3 \times 10^{-4} \text{ emu/mol} \) (Zhou et al., 2006b). Furthermore, the negative Weiss temperature, \( \theta = -1.19 \text{ K} \) suggests a possible tendency toward antiferromagnetic interactions among the Gd spins in this material. Assuming that the Curie term results only from localized trivalent Gd atoms, \( \mu_{eff} = \sqrt{N\mu_{Gd}^2} \), where \( N \) and \( \mu_{Gd} \) is the concentration of Gd atoms and the magnetic moment of the Gd atoms, respectively. Since the effective magnetic moment of the Gd³⁺, \( ^{8}\text{S}_7/2 \) states with theoretical \( J = 7/2 \), is 7.94 \( \mu_B \), the concentration of Gd atoms is estimated to be 0.84%. The inset of Figure 1E shows the field dependence of the magnetization of our sample measured at various temperatures. The isotherms show a characteristic Brillouin-like curvature expected for a Curie-Weiss paramagnet with saturation at high magnetic fields. The solid red curve is a fitting of the modified Brillouin function \[ M = N\mu_B B(x) + \frac{\chi_0 B}{k_B T} \] at 2 K, where \( B(x) \) is the Brillouin function with \( x = \frac{\mu_B H}{k_B T} \). Here, \( N \) is estimated to be 0.89%, which is in good agreement with the Gd concentration derived from the magnetic susceptibility data. The value ~0.9% is also very close to ~1% obtained by the EDS and scanning electron microscopy methods (see Supplemental Figure S3 for more detail and Supplementary Figure S4 for the XRD data of this system). Therefore, we conclude that the concentration of Gd impurities in our sample to be close to 1%, and we use this value for the remainder of our paper.

The temperature dependence of the electrical resistivity of Gd₀.0₁Sb₁.₉₉Te₃ shows a typical metallic behavior in the whole measured temperature range (Figure 1F). Inset of Figure 1F presents the magnetoresistance (MR) of the sample, at various temperatures.
temperatures. As seen from the figure, the magnetoresistivity is relatively small (about 3.5%) and exhibits ~ $H^2$ dependence characteristic of metallic systems. Interestingly, at low temperatures, (Figure 1G), there is a weak anomaly in the $\rho(T)$ curve at around 2.4 K. This transition is shifted by applying a magnetic field as strong as 0.2 T, in a manner typical for antiferromagnetic systems. Though the negative value of $\theta$ might suggest the presence of long-range antiferromagnetic ordering in Gd$_{0.01}$Sb$_{1.99}$Te$_3$, a lack of clear anomalies in both $\chi(T)$ and $C_p(T)$ (see Supplementary Figure S5) indicate that the magnetic ordering is not a bulk phenomena. In some doped systems, the low-temperature anomaly might originate from the formation of antiferromagnetic (due to $-\theta$) droplets or clusters in the crystal (Kovaleva et al., 2012). Interestingly, a TI doped with magnetic impurities can exhibit a long-range magnetic order on the surface, and such ordering can be independent of a bulk magnetic ordering (Chen et al., 2010; Hor et al., 2010). Such ordering (with or without bulk magnetic order) can also lead to the breaking of TRS, that can result in a gap opening at the Dirac point making the surface state massive. More studies, however, are required to draw any firm conclusions on the nature of the low-temperature behavior in this material.

3 ELECTRONIC STRUCTURE MEASUREMENT BY ARPES

Synchrotron-based ARPES measurements of the electronic structure of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ were performed at ALS BL 10.0.1 with a Scienta 4000 hemispherical electron analyzer. The samples were cleaved in situ in an ultra high vacuum conditions (5x10$^{-11}$ Torr) at 8 K. The energy resolution was set to be better than 20 meV and the angular resolution was set to be better than 0.2° for the synchrotron measurements. The Gd$_{0.01}$Sb$_{1.99}$Te$_3$ specimens were found to be very durable and did not exhibit any signs of deterioration for the typical measurement period of 20 hours. A small sample piece cut from the crystal was mounted on a copper post. We then used silver epoxy to attach a ceramic post on the top of the sample. The whole set was then loaded into the measurement chamber for in situ cleavage before the measurement.

To elucidate the electronic structure of Gd$_{0.01}$Sb$_{1.99}$Te$_3$, we measure the electronic dispersion maps and the Fermi surface of our sample using high-resolution ARPES. Figure 2A reveals the Fermi surface map of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ in the paramagnetic state (T = 8 K), with the constant energy contours at various binding energies with photon energy of 55 eV. A star shaped Fermi pocket around the center of the BZ (Γ point) is observed and by moving towards the higher binding energy, we find that the star shape gradually evolves into a flower shaped pocket. The density of states at $E_F$ is distributed over this star shaped pocket enclosing the Γ point. A circular hole like feature is also observed at the Γ point, which is the position of the TSS (evolving with the increasing binding energy). Additionally, the enlarging shape of the central pocket as binding energy increases confirms the hole like nature of the band around the Γ point.

In order to reveal the nature of the bands along various high symmetry directions, we present photon energy and temperature dependent ARPES-measured dispersion maps in Figures 2B,C, respectively. Where the photon energies are noted in the plots. Figure 2B shows the measured dispersion maps along the $K$-$\Gamma$-$K$ direction at various photon energies. From the leftmost Figure 2B, we observe one interesting hole like band in the vicinity of the Fermi level (blue dotted line) and one M-shaped band (green dotted line) around 250 meV below the Fermi level. Moving from left to right panels in Figure 2B, the relative intensity of various features changes with photon energy due to the matrix element effect, but the positions of the hole-like band, and the M shaped band do not evolve and look exactly the same (more details are presented in Supplementary Figures S6A,B). From our overall observation, we can conclude that the linearly dispersive states close to the Fermi level originate from the surface. To further clarify the structure and the hole like band near the Fermi level, the second derivative plot is presented in Supplementary Figure S7A, which more precisely confirms the presence of one hole like band close to the Fermi level along the $K$-$\Gamma$-$K$ direction. Additionally, dispersion maps along the $M$-$\Gamma$-$M$ direction with its band structure calculation and second derivative plots are presented in Supplementary Figures S7B and S8A-C, where one linear hole like band is observed in the vicinity of the Fermi level.

From the linear dispersion maps presented in Figure 2B, we observe a single Dirac cone in the vicinity of the Fermi level. Now, to test the robustness of the observed surface states of Gd$_{0.01}$Sb$_{1.99}$Te$_3$, we carry out a series of temperature-dependent ARPES measurements at photon energy of 60 eV. Figure 2C shows the temperature dependent dispersion maps of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ along the $K$-$\Gamma$-$K$ direction of the BZ. We notice that in the paramagnetic state, Gd$_{0.01}$Sb$_{1.99}$Te$_3$ features very similar energy-momentum dispersions at various higher temperatures ranging from 8K to 100K, establishing the robustness of the observed surface states in this magnetic system.

4 ELECTRONIC STRUCTURE CALCULATIONS

First-principles calculations were carried out using the pseudopotential projected augmented wave method (Kresse and Joubert, 1999) implemented in the Vienna ab initio simulation package (Kresse and Hafner, 1993; Kresse and Furthmüller, 1996) with an energy cutoff of 420 eV for the plane-wave basis set. Exchange-correlation effects were treated using the generalized gradient approximation (GGA) (Perdew et al., 1996), where only the Γ-point was used to sample the Brillouin zone of the super cell crystal structure. A 4 × 4 × 1 super cell of Sb$_2$Te$_3$ was considered to achieve the dilute doping (2%) of antiferromagnetically ordered Gd impurities. A total energy tolerance of 10$^{-6}$ eV was used in self-consisting the charge density. Spin orbit coupling effects were included in a self-consistent manner. To compare our super cell band dispersion to the ARPES spectra, we unfolded the bands into the primitive cell using BandUp (Medeiros et al., 2014;
Further benchmarks were performed with the full-potential linearized augmented plane wave (FP-LAPW) method implemented in a WIEN2k package (Blaha et al., 2001). More details are presented in Supplementary Figure S2.

5 OBSERVATION OF SINGLE DIRAC CONE

From the electronic structure measurement of Gd$_{0.01}$Sb$_{1.99}$Te$_3$, we observe the surface state through static ARPES, where we extrapolate the data from momentum distribution curves (MDCs) and find the approximate position of the Dirac point above the Fermi level. More elaborately, to observe the position of Dirac point above the Fermi level, first, we focus on the dispersion map of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ in Figure 3A, where we observe one hole-like band crossing the Fermi level. Since we are unable to see the features above the Fermi level using standard ARPES techniques, we extrapolate the data from the MDC curve from Figure 3A in order to find out the expected position of the Dirac point shown in Figure 3B. Thus we observe the approximate position of the Dirac point around 150 meV above the Fermi level (see Supplementary Figures S9 and S10 for more detail), which is comparable with the previously observed Dirac point position for primitive Sb$_2$Te$_3$ (180 meV) (Zhu et al., 2015). Hence, adding small amount of Gd made the position of the Dirac point closer to the Fermi level. Now, from the theoretically obtained bulk band electronic structure for both doped and pristine Sb$_2$Te$_3$ compounds, (Figures 3C,D, respectively), one can see that the electron-like bands of the Gd doped system are shifted closer to the Fermi level.
the Fermi level with respect to those of the pristine system (to compare with the surface state of the pristine system, see Supplementary Figure S1C). With the hole-like bands aligned for both doped and pristine systems, we are able to identify that the band gap is narrower in the Gd-doped Sb$_2$Te$_3$ as compared to pristine Sb$_2$Te$_3$.

From these bulk band structure calculations, it is clear that a small amount of added Gd in Sb$_2$Te$_3$ (Figure 3C) did not make a huge overall change of the bulk bands compared to the pristine Sb$_2$Te$_3$ (Figure 3D). The main difference of including Gd is that, the electron-like band at $\Gamma$ comes closer to the Fermi level. Again, from the surface state calculation of primitive Sb$_2$Te$_3$ (see Supplementary Figure S1C), we already observe non trivial Dirac-like band at the $\Gamma$ high symmetry point. Hence, we can predict that, from Gd doped Sb$_2$Te$_3$ surface state calculation, we would be able to see a similar surface state close to the Fermi level, like that observed in the primitive Sb$_2$Te$_3$ system. Additionally, from the bulk band calculation of Figure 3C, we find that adding small amount of Gd does not disturb any major or minor bands compared to the bands of the pristine Sb$_2$Te$_3$ (Figure 3D).

Therefore, we can conclude that including Gd we would see the similar Dirac-like non-trivial surface state of Sb$_2$Te$_3$ at the $\Gamma$ point, where the electron like band would be closer to the Fermi level.

6 SUMMARY

In summary, we use detailed magnetic, electrical transport, and ARPES measurements together with DFT calculations to study the electronic structure of the Gd-doped Sb$_2$Te$_3$ topological insulator. The magnetic and transport measurements show that Gd doping gives rise to local magnetism with Curie-Weiss-like behavior of the magnetic susceptibility and show some indications of possible magnetic ordering at 2.4 K. We observe the surface state from the electronic structure measurement of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ through static ARPES. The surface states are directly associated with the 4f-electron magnetism of gadolinium. We predict the approximate position of the Dirac point around 150 meV above the Fermi level. We show that adding a small amount of gadolinium introduces dilute magnetism into it, and that does not prevent the formation of the Dirac state in a relatively wide temperature range. Hence, our overall electronic structure reveals topological non-trivial surface state above the Fermi level in this material, which could be a promising platform to study the effect of dilute magnetism on the electronic structures and topology of similar doped materials.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

MN conceived the study; AP synthesized the samples and performed the electrical transport characterizations; YL was involved in sample preparation; XD, and KG performed the transport and magnetization measurements; FK performed the measurements with the help of MH, GD, YL, KD, CS, SR, AS, LP, JB, MC, and MN; CL and J-XZ performed the ab initio calculations; FK, CL, J-XZ, KG, and MN wrote the manuscript with the input from all authors; MN was responsible for the overall research direction, planning, and integration among the different research units.

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FIGURE 3 | Comparison of band structure of parent Sb$_2$Te$_3$ and Gd$_{0.01}$Sb$_{1.99}$Te$_3$. (A) Experimental band dispersion map of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ along the $\overline{K}$-$\overline{\Gamma}$-$K$ direction. (B) Extrapolation of Dirac cone by fitting the peak positions of the MDCs from (A). (C) DFT bulk band calculation of Gd$_{0.01}$Sb$_{1.99}$Te$_3$ along the $\overline{K}$-$\overline{\Gamma}$-$K$ direction. (D) DFT bulk band calculation of parent Sb$_2$Te$_3$ along the $\overline{K}$-$\overline{\Gamma}$-$K$ direction. All the experimental data were collected at ALS beamline 10.0.1.
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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fmats.2021.706658/full#supplementary-material

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