Establishments of Empiric Intervening Formulas Methods, Procedures and Mathematical Elementary Algorithms: Medical Applications

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Abstract: Background: updating methods, procedures and mathematical elementary algorithms, constitute a tool of work for the reliability of the results of any study, and in medical applications. Aims: confirming the behavior of the experimental intervening data the modelation, through the linear regression equations, according to the methods, procedures and mathematical elementary algorithms, the ones that they are not necessary in knowledge and abilities of differential calculus. Method: they use the theoretic methods: Analysis synthesis, induction deduction and abstraction concretion. Process of understanding, explanation and interpretation. Methods, procedures and mathematical algorithms, as well as statistical methods and information-technology professional programs are applicable. Results: empiric formulas follow on from a mathematical model, which confirms the behavior of the experimental data by means of the simulation, a medical problem gets worked out, the correlation coefficient is checked for sampling, a confidence interval of the linear correlation coefficient estimates itself, helped in information-technology professional programs. Conclusions: they indicate methods, procedures and the mathematical elementary algorithms to construct a model, which confirm the behavior of the experimental data, and theoreticians for simulation, as from nature and the logical order of the study, helped for information-technology professional programs.

Keywords: Experimental Data, Mathematical Elementary Methods, Medical Applications

1. Introduction

It is important to understand, explain and interpret the experimental data, by means of a model to establish, which verifies the information, the nature and the logic of the data, according to the experimentation for the collection, processing, presentation and interpretation of the processed data, from the efficient use of mathematical and statistical tools designed for these purposes [1-3].

It is necessary to master the concepts and definitions, methods, procedures, and mathematical algorithms, which facilitate the handling of information for the interpretation of the scientific problem that is solved in a study. [1-3]

Use as examples those that involve parameters and statistics known to students, such as the linear correlation of random variables, and examples carefully selected for their simplicity and importance according to the results obtained from the available scientific literature [1-3]. The importance of these variables, and the relationships to be established, are assumed from the components: academic, labor and research. [1]

It is necessary to have professional problems, in which statistical inference techniques are used so that they value as a result making the decisions, [1-3] to be followed in diagnoses and therapies to be applied in individuals, families and communities, where they provide their services of Health.

In general, significant guidelines and regulations are specified and clarified for the optimal development of the training of health professionals in undergraduate and
graduate studies, from the didactic and scientific-
methodological point of view.

In the teaching-learning process, patterns should not be set
in the way of proposing and solving different situations by
way of examples, exercises, and problems to avoid
sterotypes, which are transmitted among the teachers of a
discipline, for years of work, based on the results obtained.

Therefore, the following scientific problem is defined:
How to establish a linear regression model for medical
experimental data, based on the mastery of the contents of
elementary mathematics, without resorting to the classical
knowledge and skills of differential calculus?

The objective of this work is to confirm the behavior of the
experimental data represented, according to elementary
mathematical methods, procedures and algorithms, in which
the knowledge and skills of differential calculus are not
necessary.

2. Materials and Methods

Theoretical methods are used: analysis - synthesis,
induction - deduction, abstraction - concretion. The method
to construct curves of elementary functions, [4-6]
comprehension, explanation and interpretation processes.
Mathematical and statistical methods, procedures and
algorithms are applied.

The empirical methods applied are mainly framed in
participant and non-participant observation, in order to delve
into the problem and obtain information on the main
difficulties that affect the teaching-learning process, from the
classes, as forms of teaching organization. Socialization
workshops are held to assess the viability of the effectiveness
of the proposed didactic alternative.

They select 10 professors from the discipline of Health
Research Methodology of the Department of Medical
Informatics of the Holguín Medical Sciences University are
nominated, the intended sample according to their work
experience in teaching, and interviews are carried out with
open questions to identify: The beliefs, opinions, and
motivations of health professionals about the usefulness of
inferential statistics in professional practice. The following
difficulties are revealed:

Variations in the way of analyzing and using the concepts
studied are not always favored in the different teaching
activities in undergraduate and graduate studies in order to
stimulate creative thinking in medical problem situations that
require it.

1. There is no consolidated work strategy to delve into
alternatives that develop creative capacities of health
professionals.

2. Little use of professional statistical packages to solve
professional problems and ratify the results obtained.

3. The creation and elaboration of situations that break
with the schemes of traditional teaching, based on the
systematization and integration of undergraduate and
postgraduate content, is insufficient.

A documentary review of the programs of the discipline
Methodology of Health Research is carried out, in general the
curricula of Medical Sciences, previous and current, the
programs of the Master's Degree in Primary Health Care,
scientific review of books, articles, and monographs referring
to inferential statistics.

3. Results

The objectives proposed in different programs, the
methodological guidelines, stimulate the creative thinking of
teachers and students, thus stimulating the development of
mental capacities, given the bilateral nature of the teaching-
learning process.

It is important to create health situations to be faced by the
General Practitioner in his professional work that show the
need to interpret the association between random variables
that describe the evolution of processes in individuals,
families, and communities to consolidate the knowledge and
skills related to the Concepts addressed in inferential
statistics, from experimental data.

The analysis of the following problems is proposed, which
are previously oriented, which guarantees the active and
creative participation of health professionals. [7-9]

The empirical formulas to be established are obtained in
the updated scientific literature on the application of the
contents of Higher Mathematics; However, this discipline is
not taught in the Medicine career, which is why it constitutes
a challenge, the search for an alternative from the basic
mathematical knowledge and skills to deduce these equations
from the least squares method (MCM) [10-12].

Problem 1. Establish the empirical formulas for the points
(x_i; y_i) located approximately on the line r, defined by the
equation \( y_i = a + b x_i \), the ordinate and abscissa of the points
(x_i; y_i) with i=1, 2,…, N; They are obtained as results of
experimental measurements that are examined as data, for the
coefficients a and b of the equation of the line, which
constitute unknown quantities to be determined.

The following illustrates how medical problems are solved
using the MCM. [12, 13]

Problem 2. Given the results of the measurements of the
magnitudes of doses in milligrams (mg) of a certain drug,
and the reduction of the heartbeat per minute (beats/min).

a. Determine the regression equation.
b. Mean the regression equation according to the study.
c. What is the dose for a reduction of 13 beats/min?
d. Establish the rate of change of the reduction in heartbeat
and the dose of the drug in patients.
e. Check the error of the experimental data and the
regression equation [14, 15].

It is important to check the results obtained in the study
sample at the population level, for which the following is
proposed:

Problem 3. Verify the correlation of the results, from
contrasting the following statement: The correlation
coefficient is less than or equal to 0.70 at the population level
with a significance level of 5%. Given the following
measurements of the dose (mg) of a drug to reduce
(beats/min) of the heart in patients, based on a randomly selected sample, making a comparison [15-20].

It is not enough to confirm the results; it is revealing to specify between which values the linear correlation coefficient is found, for other samples of that population.

Problem 4. Estimate a 95% confidence interval for the correlation value in the population of the Reduction (beats/min), according to the dose (mg) of the drug, proposed in problem 3.

Table 1. Results of the measurements of the doses (X) and the beats for minutes (Y).

| Records | Dosis (X)mg | Reduction (Y)beats/min | Square (X<sup>2</sup>) | Product X*Y |
|---------|-------------|------------------------|------------------------|------------|
| 1       | 0.5         | 10                     | 0.25                   | 5          |
| 2       | 0.75        | 8                      | 0.5625                 | 6          |
| 3       | 1           | 12                     | 1                      | 12         |
| 4       | 1.25        | 12                     | 1.5625                 | 15         |
| 5       | 1.5         | 14                     | 2.25                   | 21         |
| 6       | 1.75        | 12                     | 3.0625                 | 21         |
| 7       | 2           | 16                     | 4                      | 32         |
| 8       | 2.25        | 18                     | 5.0625                 | 40.5       |
| 9       | 2.5         | 17                     | 6.25                   | 42.5       |
| 10      | 2.75        | 20                     | 7.5625                 | 55         |
| 11      | 3           | 18                     | 9                      | 54         |
| 12      | 3.25        | 20                     | 10.5625                | 65         |
| 13      | 3.5         | 21                     | 12.25                  | 73.5       |
| Σ       | 26          | 198                    | 63.375                 | 442.5      |

4. Discussion

Problem 1: The differences of the ordinate are given by the equation

\[ y_i - a - bx_i = \varepsilon_i \]  

To determine the coefficients \( a \) and \( b \) in such a way that the errors are in absolute value as close to zero (as small as possible); thus the sum of the squares of the errors is as small as possible, it is designated

\[ U = \sum_{i=1}^{n} \varepsilon_i^2 \]  

In other words, the sum of the errors in absolute value is minimal. When substituting, the following expression is displayed:

\[ U(a, b) = \sum_{i=1}^{n} (y_i - a - bx_i)^2 \]  

The difference of the function \( U \), which depends on \( a \) and \( b \), around the point \((a_0; b_0)\) follows as:

\[ U(a_0 + (\pm \delta_1); b_0 + (\pm \delta_2)) - U(a_0; b_0) \]  

values positive reals \( \delta_1 \) and \( \delta_2 \). The difference is developed [9-11];

\[ U(a_0 + (\pm \delta_1); b_0 + (\pm \delta_2)) - U(a_0; b_0) \]  

thus the following addends are obtained:

\[ \Sigma n(a_0 + (\Sigma x_i)b_0 - (\Sigma y_i))(\pm \delta_1) + 2(\Sigma x_i)(b_0 + (\Sigma x_i)a_0 - (\Sigma x_i)y_i))(\pm \delta_2) + 2((\Sigma x_i)(\pm \delta_1)(\pm \delta_2) + n(\pm \delta_1)^2 + (\Sigma x_i)(\pm \delta_2)^2 \]  

reaches its minimum value, if the difference:

\[ U(a_0 + (\pm \delta_1); b_0 + (\pm \delta_2)) - U(a_0; b_0) \geq 0 \]  

the experimental data are chosen in such a way that:

\[ \sum_{i=1}^{n} x_i \geq 0 \]  

the product coefficients and the squares of \( \delta_1 \) and \( \delta_2 \) are positive real values, which are eliminated to reduce the difference of the increment of the function at the point \((a_0; b_0)\), by imposing the required conditions, cancel the linear coefficients of \( \delta_1 \) and \( \delta_2 \). The following system of linear equations is obtained (9):

\[ n a_0 + (\sum_{i=1}^{n} x_i)b_0 = \sum_{i=1}^{n} y_i \]  

\[ (\sum_{i=1}^{n} x_i)(a_0 + (\sum_{i=1}^{n} x_i^2))b_0 = \sum_{i=1}^{n} x_iy_i \]  

The formulas for the coefficients \( a_0 \) and \( b_0 \) are determined. When

\[ \frac{\sum_{i=1}^{n} x_i}{n} \neq \frac{\sum_{i=1}^{n} x_i^2}{\sum_{i=1}^{n} y_i} \]  

then, the system of equations has a unique solution, which is possible because they are conditions that the researcher imposes on his experimental design, and is part of the scientific rigor, to guarantee that the information collected provides the equation of the mathematical model, which adjusts the results obtained.

Sometimes given the nature, and the behavior of the logical order of the experimental data, do not allow to impose these required conditions; In other words, there is not always a straight line that optimizes the results obtained by experimentation, that is, it does not have a square error close to zero.

The inequality

\[ U(a_0 + (\pm \delta_1); b_0 + (\pm \delta_2)) - U(a_0; b_0) \geq 0 \]  

holds for any positive real values \( \delta_1 \) and \( \delta_2 \). That is, the function \( U(a; b) \) that depends on the independent variables \( a \) and \( b \), has a

\[ U_{minimo relativo}(a_0; b_0) \leq U(a_0 + (\pm \delta_1); b_0 + (\pm \delta_2)), \]  

which is classified as an absolute extreme. Comparing to the proposal accomplished by Escalona-Fernández [6, 10].

To carry out calculations and checks, it is recommended to use computer programs, such as Liber Office Calc, which provides valuable help. The experimental data are organized in tabular form, as presented in problem 2, in accordance with the formulas to be used. A file must be previously created with the records of the information to be processed.

In the worksheet, the data option is activated, then options are displayed, when pointing in the last panel of the "Statistics" list, options are offered with a double click, access to "Regression", in this the columns with the registered data \( x_i, y_i \) Thus, the values of the "Slope" and the
"Intersection" are obtained, that is, the numerical values of the coefficients of the linear regression line. Other options allow determining the sample correlation coefficient, T, F, Z tests; Chi Square, among others.

Problem 2: a. Record 6 in the table 1:

\[ \sum_{i=1}^{13} x_i = 26; \sum_{i=1}^{13} x_i^2 = 63.375; \sum_{i=1}^{13} y_i = 198; \sum_{i=1}^{13} x_i y_i = 442.5 \]  \hspace{1cm} (13)

They substitute themselves in (9):

\[ 13*a_0 + 26*b_0 = 198, \]
\[ 26*a_0 + 63.375*b_0 = 442.5 \]

The condition

\[ \frac{\sum x_i^2}{n} = \frac{26}{13} = 2 \neq \frac{\sum x_i^2}{\sum x_i} = \frac{63.375}{26} \]  \hspace{1cm} (14)

is checked to guarantee the existence and the uniqueness of the solution, it is obtained approximately that: \( a_0=7.05 \) and \( b_0=4.09 \); are the coefficients of the regression equation, which is defined as:

Reduction beats/min = 7.05 + 4.09 * (dose mg) \hspace{1cm} (15).

b. It is established that the reduction in heart beats in patients is 4.09 times the applied dose, and 7.05 beats per minute are added to the reduction due to other factors not considered in the study.

c. Then, 13 beats/min = 7.05 + 4.09 * (dose mg), then dose mg = (13 - 7.05) / (4.09), that is, the dose is equal to 1.45 mg of the drug for a reduction of 13 beats per minute.

d. Increasing the dose of the drug applied to patients by one milligram (1 mg) reduces approximately 4 (4.09) beats per minute.

e. The experimental data are evaluated in the (theoretical) regression equation, the calculated error is expressed, this is almost zero, therefore, the efficiency of the established mathematical model is ratified, the real and theoretical results are compared by simulation.

\[ \sum_{i=1}^{13} e_i = \sum_{i=1}^{13} (y_i - 7.05 - 4.09 x_i) = 0.00000000000001 \]  \hspace{1cm} (16)

Making a comparison [11].

An effective behavior of the drug is manifested, from different doses, in different patients, according to the study measurements.

The ratification of the regression model is related to the verification of sufficient conditions, based on the necessary conditions imposed. On the contrary, when the error is not small, the regression model: Linear, logarithmic and potential does not fit the experimental results.

Problem 3: 1) Hypothesis formulation:

\( H_0: \rho \leq 0.70 \), the linear correlation at the population level is less than or equal to 0.70.

\( H_1: \rho > 0.70 \), the correlation is greater than 0.70.

2) The significance level is selected \( \alpha=0.05 \)

3) The T-student distribution is used for the calculated statistic: \( t_{cal}=4.85 \)

4) \( t_{0.95; 12 GL}=2.18 \). As a criterion statistic (the statistician) belongs to the critical domain (because \( t_{0.95; 12 GL}=2.18 < t_{cal}=4.85 \)). Therefore the null hypothesis is rejected.

5) It is convenient to assume the correlation coefficient at the population level is greater than 0.70 at the population level with a significance level of 5% and 12 degrees of freedom.

Problem 4: It is known that to determine the confidence interval for \( \rho \):

\[ [Z_{a/2} < \frac{Z_r - Z_{a/2}}{\sqrt{n}} < Z_{1-a/2}] = 1 - \alpha. \]  \hspace{1cm} (17)

Where:

\[ Z_r \text{ asympt } \sim N \left( \frac{1}{2} \ln \frac{1+\rho}{1-\rho}; \frac{1}{n-3} \right) \]  \hspace{1cm} (18)

For \( Z_{0.95}=1.83 \)

The confidence interval:

\[ (Z_1 = Z_r - (\frac{1}{\sqrt{n-3}}); Z_2 = Z_r + (\frac{1}{\sqrt{n-3}})) \]  \hspace{1cm} (19)

The values are determined (\( Z_1 = 1.21; Z_2 = 2.45 \))

\[ (\rho_{inf} = \frac{e^{Z_1} - 1}{e^{Z_1} + 1}; \rho_{sup} = \frac{e^{Z_2} - 1}{e^{Z_2} + 1}) = (0.84; 0.99) \]  \hspace{1cm} (20)

Making a comparison [15-20].

With a confidence level of 95% and 12 degrees of freedom, the true value of the correlation \( \rho \) in the population is between the values 0.84 (lower limit); and 0.99 (upper limit), that is: 0.84 < \( \rho < 0.99 \).

In general, it is important to establish an association between random variables, whose conditions to be imposed meet the requirements demanded by the researchers, according to the design of the experiment, and the aspects to be checked, which are illustrated in the solutions to problems 1, 2, 3 and 4; These are basic considerations to be followed as an alternative to the proposed didactic strategy.

The group of teachers, from the bank of problems created by the General Physician, previously oriented; the results of which are verified by professional computer programs.

5. Conclusions

The basic consideration of the didactic strategy that is proposed as an alternative to be followed in this work indicates:

1. Methods, procedures and elementary mathematical algorithms to build a linear regression model, which confirm the behavior of experimental and theoretical
data by simulation, according to the nature and logical order of the study.

2. The empirical formulas are established by the MCM, in which the knowledge and skills of differential calculus are not necessary, these procedures; and formulas are applied to medical problems, supported by professional computer programs, the sample correlation coefficient is verified, which is estimated by an interval at the population level.

It is recommended to carry out methodological and collective workshops with the professors of the discipline Methodology of Health Research to deepen the design of the didactic strategy that is proposed in order to stimulate creative thinking, and perfect the bank of problems, as well as updating methods, and statistical inference techniques.

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