Performance Analysis of Regular and Irregular LDPC Codes on SPIHT Coded Image Data

Shahnas P * ·

* Department of ECE, MDIT, Kozhikode, Kerala, India.

* Corresponding Author: shaz087@gmail.com

Received : 14th May 2020, Accepted : 28th August 2020

Abstract: The LDPC (Low Density Parity Check Code) has shown interesting results for transmitting embedded bit streams over noisy communication channels. Performance comparison of regular and irregular LDPC codes with SPIHT coded image is done here. Different error sensitive classes of image data are obtained by using SPIHT algorithm as an image coder. Irregular LDPC codes map the more important class of data into a higher degree protection class to provide more protection. Different degree protection classes of an LDPC code improves the overall performance of data transmission against channel errors. Simulation results show the superiority of irregular LDPC over regular LDPC codes.

Keywords: SPIHT Algorithm, LDPC, Image Data, LDPC codes.

1. Introduction

Any communication system begins with source coding which compresses the entire data bits to the minimum necessary to represent the information in the message, that ensures efficient utilization of bandwidth. But compressed data streams are very sensitive to channel errors because their most redundant bits are removed. The heterogeneous nature of compressed data demands for an efficient data processing method other than the content-blind normal processing. Suitable channel coding methods must be used to assure the reconstructed image quality. Sometimes the synchronization between the encoder and the decoder may be lost due to a single bit error which may lead to poor quality image. Powerful error correcting codes are required for the transmission of any kind of data through the erroneous channels. Low Density Parity Check (LDPC) codes combined with soft decision decoding could achieve best results in digital data transmission.

LDPC code is a type of Linear Block code which is specified by its sparse parity check matrix which contains a very less number of 1’s in comparison with the number of 0’s. They were first introduced by Gallager with very good error performance near Shannon limit. They
can be represented through matrices of ‘m’ rows and ‘n’ columns and can also be described via
Tanner graphs having bit nodes representing n bits in the codeword and check nodes
representing m parity check equations. LDPC codes are decoded iteratively using this graphical
representation of their parity-check matrix.

Tanner graph is a bipartite graph in which an edge is drawn between a bit node and a
check node if and only if the bit is included in the parity check equation. A cycle in a Tanner
graph is a path containing edges drawn from a node back to the same node. The minimum length
of any cycle in the graph is termed as its Girth. Short cycles in graphs are generally considered
worse while using iterative decoding. The number of edges connected to each node is known as
its degree.

Bit nodes with large degrees collect more information from their adjacent check nodes
and protected well.

Depending on the structure of the parity check matrix LDPC codes are classified into
Regular and irregular codes. Regular LDPC have a constant number of 1’s in every column and
every row whereas irregular LDPC codes do not have a fixed number of non-zeros per column
or per row and thus it varies the level of error protection over a codeword. While looking at the
graphical representation, It’s also possible to see the regularity of the code. The incoming edges
for every bit-node and check-nodes are the same for regular codes, but it is different for irregular
codes. Research on UEP low-density parity-check (LDPC) codes can be found in [1-3]. Weight-
increasing parity-check matrix and systematic encoding is used for the analysis of irregular LDPC
codes in [1]. The irregular LDPC codes have inherent unequal Error Protection property.

In this work, we present a SPIHT coded image transmission system using regular and
irregular LDPC codes. Progressive Edge Growth (PEG) algorithm is used for the construction
of sparse parity check matrix of LDPC codes. The source encoding is done by SPIHT algorithm
and the output of SPIHT coder is given to the channel coder using LDPC codes to provide
required protection to the source coded data.

2. SPIHT (Set Partitioning in Hierarchical Trees) coding algorithm

SPIHT algorithm generates embedded bit streams of the given image data so that the
compressed data can be partitioned into different error sensitive classes. It is a wavelet-based
image compression technique which views the wavelet coefficients as a group of spatial
orientation trees. The algorithm mainly works through four steps as (i) Initialization (ii) Sorting
Pass (iii) Refinement Pass and (iv) Quantization-step updates [4]. At the receiver side the
reconstructed image is updated in every step. The decoding can be stopped anywhere because
of the embedded nature of bitstream.
3. LDPC Code Construction

The capacity approaching LDPC codes are constructed using the PEG algorithm mentioned in paper [5]. It is a systemized method for constructing Tanner graphs having a large girth. The algorithm establishes edges between bit nodes and check nodes progressively in an edge-by-edge manner. Selection of the degree distribution of bit nodes and check nodes is important while designing irregular LDPC codes to achieve better performance.

An edge selection procedure is started with the number of bit nodes (n), the number of check nodes (m), and the bit node degree sequence \( D_s = \{d_0, d_1, \ldots, d_{n-1}\} \), such that establishing a new edge on the graph has a little impact on the girth. After that the graph with this new edge is updated, and this procedure continues with the placement of the next edge. The graph grows by optimizing each local girth in an edge-by-edge manner. The most important thing is to find out the most distant check node and place an edge between the bit node and that distant check node.

PEG Algorithm is used for generating good regular and irregular LDPC codes of short and moderate block lengths. Once the parity-check matrix \( H \) is created, the data to be transmitted over the channel is encoded using a systematic encoder.

A good degree distribution for irregular LDPC code with different protection classes can be attained using Gaussian approximation (GA) algorithm discussed in paper [6]. For a specific Error protection application, the fraction sequence \( \alpha \) and code rate \( R \) are determined first. The code word bits are divided into different classes each having different error protection capability. All the bit nodes of the same protection class are assigned the same degree. More protection can be provided to important classes of data by providing more degree to the corresponding bit node of LDPC code.

4. Simulation Results in Image Transmission

The irregular LDPC code with rate \( R \) is divided into \( N_c \) classes ordered in decreasing order of their error correction capability. The redundant bits of the codeword are associated with the last class and all the previous classes are for information bits. An embedded SPIHT coded stream compressed into \( N_c - 1 \) progressive quality layers is given to the channel coder. The code words are then transmitted over an AWGN channel.

Irregular LDPC code having length \( N=256 \) is divided into 3 protection classes having proportion distribution \( p= (0.17, 0.33, 0.5) \) with degree \( d = (9, 3, 2) \). With these parameters the \( H \) matrix is generated. For the test images of size 512x512, an embedded bit stream generated by SPIHT algorithm is divided into 2 protection classes and maps each class into the bit nodes with different degrees. A regular LDPC code with bit node degree 3 is also constructed using the PEG algorithm for the comparison in which all the data bits are mapped to the same degree.
protection class. Table 1. shows the average PSNR performance of regular and irregular codes in embedded bitstream of "Lena" image over AWGN channel. The reconstructed images with regular and irregular LDPC codes are shown in Figure 1. Reconstructed image qualities show that irregular LDPC code outperforms the regular LDPC code for compressed embedded bit streams.

**Table 1.** Comparison of Regular and Irregular LDPC Codes with different Eb/N0.

| Eb/No(dB) | Regular-PSNR (dB) | Irregular-PSNR (dB) |
|-----------|-------------------|---------------------|
| 1.0       | 2.34              | 9.23                |
| 1.2       | 4.17              | 11.44               |
| 1.4       | 6.03              | 15.20               |
| 1.6       | 8.56              | 21.75               |
| 1.8       | 11.71             | 24.97               |
| 2.0       | 16.23             | 28.23               |

(a) for Eb/No 1dB  (b) for Eb/No 1.4dB  (c) for Eb/No 1.8dB  (d) for Eb/No 2dB

(e) for Eb/No 1dB  (f) for Eb/No 1.4dB  (g) for Eb/No 1.8dB  (h) for Eb/No 2dB

**Figure 1.** Reconstructed Images of Lena for EEP and UEP for different Eb=No for regular (a, b, c, d) and irregular (e, f, g, h) LDPC codes
5. Conclusion

In this work gray scale images were source coded using SPIHT algorithm to generate the embedded bitstream of the input image and the compressed data were prioritized. Regular and Irregular LDPC codes were constructed using PEG algorithm for transmission of image through the error-prone channel. Simulation results show that Irregular LDPC codes outperforms the Regular LDPC codes for compressed embedded bit stream of images. The inherent error protection property of irregular LDPC code makes its performance better in terms of improved average bit-error rate (BER).

References

[1] Xiumei Yang, Dongfeng Yuan, Piming Ma, Mingyan Jiang, New Research on Unequal Error Protection (UEP) Property of Irregular LDPC Codes, Consumer Communication and Networking Conference, 2004CCNC2004, First IEEE, (2004) 361-363.
[2] Suayb S. Arslan, Pamela C. Cosman, Laurence B. Milstein, Concatenated Block Codes for Unequal Error Protection of Embedded Bit Streams, IEEE Transaction on Image Processing, 21(2012) 1111-1122.
[3] Betelhem Mateos Mekisso, Bachelor of Science in Electrical Engineering, Arba Minch University, Unequal Compressive Imaging, July, 2011.
[4] [Amir Said, William A. Pearlman, A New, Fast, and Efficient Image Codec Based on Set Partitioning in Hierarchical Trees, IEEE Transactions on Circuits and Systems for Video Technology, 6(1996) 243-249.
[5] Y. Hu, E. Eleftheriou, and D. M. Arnold, Regular and irregular progressive edge growth Tanner graphs, IEEE Transactions on Information Theory, 51(2005) 386398.
[6] Piming Ma and Kyung Sup Kwak, Unequal Error Protection Low-Density Parity-Check Codes Design Based on Gaussian Approximation in Image Transmission, IEEE Communications Society subject matter experts for publication in the WCNC 2009 proceedings.

Acknowledgements: NIL

Conflict of interest: NIL

About the License: © 2020 The Author. This work is licensed under a Creative Commons Attribution 4.0 International License which permits unrestricted use, provided the original author and source are credited.