COMpletely co–bouNded sChur multipli ers

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Abstract. A linear map \( u: E \to F \) between operator spaces is called completely co-bounded if it is completely bounded as a map from \( E \) to the opposite of \( F \). We give several simple results about completely co-bounded Schur multipliers on \( B(\ell_2) \) and the Schatten class \( S_p \). We also consider Herz-Schur multipliers on groups.

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