Fuzzy-Sliding Mode Speed Control of Permanent Magnet Synchronous Motor Using NPC Converter

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Abstract
These days, the researches on permanent magnetic synchronous motors (PMSMs) as mechanical power sources have obtained more and more attention. The popular strategies applied to control the machine speed presents higher standards for torque response speed and accuracy of the PMSMs control system. To follow the reference motor speed as quick as possible, a sliding mode (SM) motor speed controller that can decouple q-axis and d-axis currents is proposed. Moreover, to mitigate the well-known chattering phenomenon caused by the discontinuous term in a steady state of the conventional sliding mode control, a Fuzzy logic algorithm is introduced. The proposed Fuzzy-SMC performance is tested in simulation using MATLAB/Simulink environment. To eliminate the chattering phenomenon a combination of the command in sliding mode and the fuzzy logic is adopted. The proposed method also can guarantee the robust control of PMSMs under model parameters (resistance, inductance) and load torque variations. Based on the obtained results, it is clear that a fuzzy sliding mode controller can perform better than the conventional PI controller in terms of rising time, overshoot, settling time, and steady-state error. The effectiveness of the combined Fuzzy-SM Controller also can guarantee the robust control of PMSMs and shows that this command did not depend on machine parameters (resistance, inductance) comparing to other existing commands and the chattering effect is reduced using this proposed method.

Keywords: PMSM, Sliding Mode Control, Fuzzy logic, Speed control, NPC.

1. INTRODUCTION
The development of digital calculators such as DSP and FPGA improves the numerical PMSM control drives. These modern platforms allow developing nonlinear controls that improve the performance of the systems with different noise and uncertainties i.e., robust control [1], direct torque control[2], intelligent control[3] …, adaptive control[4] and sliding mode control (SMC)[5]. This last method is applied in many control fields [6][7].

The main drawback of the conventional PI is the sensitivity to parameter uncertainty and variation. In Many Applications, the SMC is attractive and recommended compared to conventional PI. In [8]a sliding mode control is used to ensure a high-accuracy positioning of a six-phase induction machine in both healthy and faulted modes. The research work of Lin. C[9] proposed an adaptive non-singular terminal sliding mode tracking control is designed to provide faster convergence and higher precision control for robotic systems. Besides, the SMC can be combined with other approaches to ensure the stability of system control [10].

However, the SMC suffers from well-known drawbacks such as the chattering phenomenon induced at a steady state due to the discontinuous term in the control law. Moreover, once used associated with conventional vector control to control the speed of PMSM, it leads to vibration. Subsequently, the torque ripple and power losses increase considerably. Various methods have been proposed to overcome the charting problems, such as complementary sliding-mode method[11], reaching law method [12],[13], and high-order sliding-mode method [14],[15]. By making the discontinuous gain a function of the sliding-mode surface, the chattering are reduced in [13]. Sliding Mode Control is assumed to construct the speed and current integrated controller in[16], using a novel Exponential Law. In the research work of Murat Karabacak et al.[17], they proposed a modelling, design, and simulation a tackling control approach based on adaptive backstepping speed tracking control to solve an uncertain occurred in permanent magnet synchronous motor PMSM, their numerical result confirms that strong robustness can be generated by the proposed controller to solve all uncertainties parameter. Jinpeng Yu et al. [18] developed an adaptive fuzzy tracking to control based backstepping to control the chaotic PMSM drive system, they compare the conventional backstepping technique with an adaptive backstepping technique, as a result, the developed adaptive technique can delete the chaos of PMSM drive systems and also track successfully the reference signal. A comparative study conducted by the research team of Bouzeria H et al. [19] where the fuzzy logic technics are used to control the PMSM speed for a water pumping application, PMSM has to works in its maximum efficiency whatever the weather condition, they have compared and analyzed the performance between controllers based fuzzy logic and controllers based proportional integrator according to the speed and load.
variation test. B. Adhavan et al. [20] Presented a fuzzy logic approach to control the PMSM by applying space vector modulation, a comparative study between the conventional PI controller and the design Fuzzy logic controller proves that the fuzzy logic controller presents a good performance.

Dandan et al. [21] focused to develop a controller-based sliding mode capable to control the torque of a permanent magnet synchronous motor (PMSMs) for an electric vehicle, this allows to delete the chattering phenomenon by adopting exponential reaching law, as result, robust control of PMSM is reached under model parameter and variation torque.

In these works, the main idea is to smooth the control action across the sliding surface. For this, the PI speed controller is replaced by an SM controller to make the control of PMSM presents no dependency in terms of parameter variation. However, a Fuzzy logic algorithm is introduced to adjust the weight of the SM gain, in such a way, it can be taken large than the standard value during the transient period to conserve the SMC performance and reduce the chattering effect in steady-state.

2. PERMANENT MAGNET SYNCHRONOUS MOTOR MODEL

Voltage and flux equations of permanent magnet synchronous motor expressed in the d-q reference frame are given by [10]:

\[
v_d = R_d i_d + \frac{d\phi_d}{dt} - \omega \phi_q \tag{1}
\]

\[
v_q = R_q i_q + \frac{d\phi_q}{dt} + \omega \phi_d \tag{2}
\]

\[
\phi_d = L_d i_d + \phi_f \tag{3}
\]

\[
\phi_q = L_q i_q \tag{4}
\]

Since the electromagnetic torque is described by:

\[
T_e = \frac{3}{2} p \left[ \phi_d i_q + (L_d - L_q) i_d i_q \right] \tag{5}
\]

Besides, the second law of Newton allows to deduce the following mechanical equation:

\[
J \frac{d\omega}{dt} = T_e - B \omega - T_l \tag{6}
\]

Where:

- \( v_d, v_q \) d and q axis stator voltages.
- \( i_d, i_q \) d and q axis stator currents.
- \( \Phi_d, \Phi_q \) d and q axis stator flux.
- \( L_d, L_q \) d and q axis stator inductances.
- \( T_e, T_l \) electromagnetic and load torque.
- \( R_s \) stator resistance.
- \( \phi_f \) flux linkage created by rotor magnets.

\( J \) moment of inertia.
\( B \) coefficient of viscosity.
\( p \) number of poles pairs.
\( \omega \) electrical frequency.
\( \omega_r \) rotor speed.

Angular frequencies are related as a function of the number of pair pole:

\[
\omega = p \omega_r \tag{7}
\]

Hence, the state equation of permanent magnet synchronous motor is deduced as follow:

\[
\begin{align*}
\frac{di_d}{dt} &= -\frac{R_d}{L_d} i_d + \frac{p L_d}{L_q} \omega_l i_q + \frac{1}{L_d} v_d \\
\frac{di_q}{dt} &= -\frac{R_q}{L_q} i_q - \frac{p L_d}{L_q} \omega_l i_d - \frac{p \phi_f}{L_q} \omega + \frac{1}{L_q} v_q \\
\frac{d\omega}{dt} &= \frac{3 p}{2J} \left[ \phi_d i_q + (L_d - L_q) i_d i_q \right] - \frac{B}{J} \omega - \frac{T_l}{J} \tag{8}
\end{align*}
\]

3. NEUTRAL POINT CLAMPED CONVERTER (NPC)

3.1 Configuration of NPC converter

Neutral Point Clamped (NPC) inverters, which are diodes connected to the midpoints of the voltage sources, protecting the external switches against excessive voltages. This topology requires rigorous control of the voltages of each capacitor and the balancing of the voltages becomes complex beyond three levels. Also, the number of diodes increases very rapidly with the number of levels.

The structure of the neutral point clamped converter is sketched in Figure 1. The continuous side is divided into two equal voltages using two capacitors.

![Figure 1: Configuration of NPC converter.](image)

Each leg is composed of four IGBTs connected in series. Each leg is expected to be completed by two clamp diodes. For one
phase, when IGBT Q1 and Q2 are turned on, the output is connected to \( V_p \); when Q2 and Q3 are on, the output is connected to \( V_o \); and when Q3 and Q4 are on, the output is connected to \( V_n \). The switching states of the IGBTs are listed in Table 1.

| IGBT | \( V_{out}=V_p \) | \( V_{out}=V_o \) | \( V_{out}=V_n \) |
|------|----------------|----------------|----------------|
| Q1   | On            | Off            | Off            |
| Q2   | On            | On             | Off            |
| Q3   | Off           | On             | On             |
| Q4   | Off           | Off            | On             |

3.2 Sinusoidal Modulation using Multiple Carrier Waves (SPWM)

The multilevel SPWM modulation method is based on the comparison between the sinusoidal reference and many vertically shifted carrier signals.

For two levels, the scheme is illustrated in Figure. 2. During a PWM period, if the modulation wave is greater than the upper carrier wave, switch Q1 is on and Q3 is off. In contrast, if the modulation wave is greater than the lower carrier wave, switch Q2 is on and Q4 is off.

![Figure 2](image)

**Table 1.** Switching states

3.2 Sinusoidal Modulation using Multiple Carrier Waves (SPWM)

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SLIDING MODE CONTROLLER DESIGN

Sliding Mode Control (SMC) has a proven history of its performance. It is considered as a nonlinear control method that presents good performance. It has been employed in several applications investigated in the literature [6][7] and has been applied to different systems with various behaviors. The implementation of sliding mode control is simple; it is based on state-space equations of the studied system and robust against external disturbances and process change.

Sliding Mode Control is known also as a Variable Structure Controller (VSC) since it is a discontinuous controller. In VSC, the idea is to bring the plant states to a user-defined surface called a sliding surface.

Sliding mode control is designed through three steps, which are:

- **Choice of the control surface**
  Considering the nonlinear system defined by the following form:
  \[
  \dot{X} = g(X,t) + b(X,t)u(X,t)
  \]
  Where \( X \in \mathbb{R}^n, u \in \mathbb{R}^m, g(X,t) \in \mathbb{R}^n, b(X,t) \in \mathbb{R}^{nm} \),
  \( g(X,t) \) and \( b(X,t) \) are two non-linear functions, continuous, and limited.
  The sliding surface is given by:
  \[
  S(X) = \left( \frac{d}{dt} + \delta \right) e^{n-1} e
  \]
  Where \( e = X^\text{ref} - X \), \( X^\text{ref} = [x^\text{ref}, x^\text{ref}, x^\text{ref}, ...]^T \),
  \( e \) is the error, \( \delta \) is a positive constant, \( X^\text{ref} \) is the reference signal, and \( X \) is the state variable.

- **Convergence condition**
  Lyapunov function defines the convergence condition:
  \[
  S(X), \dot{S}(X) \leq 0
  \]

- **Control calculation**
  Usually, the basic control law of sliding mode control that can guarantee the asymptotic stability for such systems is given by:
  \[
  u = u^\text{eq} + u^n
  \]
  Where \( u \) is the control signal is the equivalent control, and \( u^n \) is the switching term which defined by the sign function of the sliding surface multiplied by a positive constant:
  \[
  u^n = -k \cdot \text{sign}(S(X))
  \]
  Where \( k \) is a positive constant, \( S(X) \) is the switching function, and \( \text{sign}(.) \) is the sign function.

Let us apply this theory to control the speed of the PMSM. The sliding surface is defined below:

\[
S(\omega) = \omega^* - \omega
\]

Calculating the derivative of the sliding surface, and neglecting of speed dynamics, yielding:

\[
\dot{S}(\omega) = -\frac{3p\omega_q}{2J} i_q + \frac{B}{J} \omega + \frac{1}{J} T_e
\]
In this case, the control is the quadratic current, the control law is calculated as:

$$i_q^* = \frac{2}{3 p f L f} \left( B \omega_r + T_L^* - k \text{sgn}(S(\omega_r)) \right)$$  \hspace{1cm} (16)$$

Where the load torque was estimated from the speed and the PMSM quadratic control current $i_q$ based on the Eq.8 at steady state as follows:

$$T_L^* = \frac{3 p f L f}{2} i_q - B \omega_r$$  \hspace{1cm} (17)$$

Now, for the direct current, the sliding surface is defined as:

$$S(i_d) = i_d^* - i_d$$  \hspace{1cm} (18)$$

As one mentioned before the direct current should be controlled to zero. However, the derivative of the sliding surface becomes:

$$\dot{S}(i_d) = R i_d - \frac{p L_q}{L_d} \omega_q i_q - \frac{1}{L_d} v_d$$  \hspace{1cm} (19)$$

Therefore, the control law is calculated as follows:

$$v_d^* = R i_d - \frac{p L_q}{L_d} \omega_q i_q - k \text{sign}(S(i_d))$$  \hspace{1cm} (20)$$

It seems from Eq. (16) and Eq. (20), that the control law contains the discontinuous term which ensures the stability and the sliding control attraction. Nevertheless, it generates ripples depending on the value of $k$. To mitigate this gain effect, a fuzzy logic method is proposed.

The sliding mode control scheme of the PMSM is outlined in Figure.3.

To minimize the chattering phenomenon, a mitigation term is calculated using fuzzy logic. The principle is to multiply the discontinuous term of sliding mode with a mitigation term calculated using the Sugeno fuzzy inference technique. The fuzzy controller has two inputs; the sliding surface $S$ and the measured angular speed $\omega$. The proposed scheme to control PMSM using the fuzzy sliding mode technique is illustrated in Figure.4.

Five fuzzy sets are used to describe the distance between the operating point and sliding surface, and three fuzzy sets are exploited to outline the speed range. Furthermore, three additional fuzzy sets are presented to define the appropriate mitigation value in the output of the fuzzy block as shown in Figure.5.

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**5. CHATTERING MINIMIZATION USING FUZZY LOGIC**

To minimize the chattering phenomenon, a mitigation term is calculated using fuzzy logic. The principle is to multiply the discontinuous term of sliding mode with a mitigation term calculated using the Sugeno fuzzy inference technique. The fuzzy controller has two inputs; the sliding surface $S$ and the measured angular speed $\omega$. The proposed scheme to control PMSM using the fuzzy sliding mode technique is illustrated in Figure.4.

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**Figure 3.** Sliding mode control of PMSM.

**Figure 4.** FSMC scheme.

**Figure 5.** Inputs and outputs fuzzy sets
However, the fuzzy inputs/outputs rules are arranged in table 2.

| Input | S-- | S- | S | S+ | S++ |
|-------|-----|----|---|----|-----|
| Ω-    | e++ | e+ | e | e+ | e++ |
| Ω     | e++ | e+ | e | e+ | e++ |
| Ω+    | e++ | e+ | e | e+ | e++ |

The resulting control surface of the proposed fuzzy controller is illustrated in Figure 6.

Figure 6. The control surface of the fuzzy controller.

6. SIMULATION RESULTS

The Fuzzy Sliding Controller of the PMSM using the NPC converter is implemented in MATLAB/Simulink and the results are compared with the conventional sliding controller. The block diagram of the sliding mode control of PMSM with Fuzzy chattering minimization is shown in figure 10.

The simulation is conducted on a 3.6 KW PMSM. It is then simulated by placing the conventional sliding controller first, then Fuzzy Sliding Controller in a second time.

A load torque of 15 Nm is applied at the start. Figure 7 shows the response of the system with conventional sliding mode control and fuzzy sliding mode control for a reference speed of 80 rad/s. It is clear that the performance of the fuzzy sliding mode controller is better than that of the conventional sliding controller in terms of its peak overshoot and settling time. Nevertheless, chattering is unreduced sliding mode combined with fuzzy logic as illustrated in Figure 8.

For optimum operation at maximum electromagnetic torque, the solution is to keep the direct current ids (in the d axis) equal to zero and to regulate the motor speed by the transverse current iq (in q axis) via the voltage Vq (in q axis) as shown in the diagram in Figure 9.

The reduction of the current in the d axis makes it possible to reduce the losses by Joule effect, therefore the optimization of the efficiency in the stator of the synchronous permanent magnet machine.

Figures from (11) to (18) present the results of the simulation of control by sliding mode in combination with fuzzy logic with an increase in the value of the stator resistance (+ 150% RS and + 200% RS) and an increase in the values of the inductances Ld, Lq (+ 150% (Ld, Lq) and + 200% (Ld, Lq)).

The simulation’s results show that the control by sliding mode and applied fuzzy logic is insensitive to parametric variations. Therefore, this command presents good robustness concerning the parametric variations.

Figure 7 illustrates a comparison of the synchronous machine speed response using the sliding mode controller and Fuzzy sliding mode controller, the Fuzzy sliding mode controller is better comparing to sling mode controller of which It provides a fast-dynamic response.

Figure 8 enlarges a range of mechanical speed response. This zoom is done between the instants [0.375s 0.4s]. It is deductible that the undulations of the Fuzzy sliding Mode Controller which are estimated to ‘0.6 rad/s’ are more reduced compared to the Sliding Mode Controller (a deviation of 1.8 rad/s).

Figure 8. Zoom of the mechanical speed response.
Figure 10. Overall block diagram of the proposed control system.

Figure 9 illustrates the evolution of the currents in the axes d and q. It can be noticed that the servo current $I_d$ is zero while $I_q$ tends towards 19A.

Figure 11 illustrates a performance comparison of the synchronous machine speed response using sliding mode controller and Fuzzy sliding mode controller by changing the values of machine parameters ($L_d$ & $L_q$) as reference input.

An increase in these two parameters by 150% generated at the output two different responses, the FSMC response presents the best output performance.

Figure 11. The response of mechanical speed using SMC on the FSMC Vs Reference signal.

Figure 12. Zoom 1 of the response of mechanical speed using SMC on the FSMC Vs Reference signal.
An enlargement range of the mechanical speed response (From the base on figure.11) is provided between the instants [0.375s 0.4s]. it appears that the undulations of the Fuzzy sliding Mode Controller are estimated as 0.6 rad/s are more reduced comparing to the Sliding Mode Controller which consists of a gap of 1.4 rad/s.

Figure .13 illustrates a comparison of the synchronous machine speed response using sliding mode controller and Fussy sliding mode controller by changing the values of machine parameters ($L_d$ & $L_q$). An increase in these two parameters by 200%.

Figure 13. The response of mechanical speed using conventional on the fuzzy controller for a 200% increase in the $L_d$ and $L_q$ value.

Figure 14. Zoom 2 of the mechanical speed using conventional on the fuzzy controller for a 200% increase in the $L_d$ and $L_q$ value.

Figure 15. The response of mechanical speed using conventional on the fuzzy controller for a 150% increase in the Rs.

Figure 16. Zoom 3 of the mechanical speed using conventional on the fuzzy controller for a 150% increase in the Rs.

Figure 17. The response of mechanical speed using conventional on the fuzzy controller for a 200% increase in the Rs.

Figure 18. Zoom 4 of the mechanical speed using conventional on the fuzzy controller for a 200% increase in the Rs.

The figures 13, 15 and 17 enlarge a range of the mechanical speed response using conventional on the fuzzy controller for s set-int point of a 200% increase related to the $L_d$ and $L_q$ value, an increase of 150% related to the Rs, and an increase of 200% related to the Rs, respectively. Their related illustration are tacked in the instant between [0.375s 0.4s]. Zoom 2 in figure 14, provide an average undulation range of FSMC= 0.6 rad/s and SMC=1.4 rad/s, moreover, Zoom 3 in
figure 16, provide an average undulation range of FSMC= 0.7 rad/s and SMC=1.4 rad/s, and finally, Zoom 3 in figure 18, provide an average undulation range of FSMC= 0.6 rad/s and SMC=1.4 rad/s

7. CONCLUSION

Load variations and sensitivity to mechanical motor parameters are the important features required in PMSM speed control. Those advantages are ensured with the developed combination of the SM controller and the Fuzzy logic algorithm used to minimize the chattering phenomenon. First, an SM controller is designed using the electrical and mechanical PMSM equations, and the load torque is estimated using motor quadrature current and speed. Moreover, the SM discontinues term effects that manifest in current chattering and torque oscillation, are eliminated using a sliding mode associated with the fuzzy logic algorithm.

Simulation Results show good performances obtained with proposed control, with a good choice of parameters of control. The simulation results show Fast response and robust performance to parametric variation and disturbances in all the systems. The components $l_d$ and $l_q$ is regulated using the proposed control so that $l_d$ is zero

The Fuzzy Sliding Mode Controller combines the intelligence of fuzzy logic with the Sliding Mode technique. The effectiveness of this combination is validated through simulation test. Indeed, the chattering effect is reduced using fuzzy logic and the speed variation of the motor under loaded condition is reduced.

APPENDIX

PARAMETERS OF THE SYNCHRONOUS MACHINE

| Designation                  | Value            |
|------------------------------|------------------|
| Frequency                    | 50 Hz            |
| Pole pairs (p)               | 2                |
| Stator phase resistance ($R_s$) | 1.35 Ω           |
| d axis inductance ($L_d$)    | 7.66 mH          |
| q axis inductance ($L_q$)    | 17 mH            |
| Permanent magnet flux ($\Phi_p$) | 0.158 Wb       |
| Moment of inertia (J)        | 0.0035 kg.m²     |
| Damping coefficient (B)      | 0.001Nm/rad/s    |

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