Systems NMR: single-sample quantification of RNA, proteins and metabolites for biomolecular network analysis

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Cellular behavior is controlled by the interplay of diverse biomolecules. Most experimental methods, however, can only monitor a single molecule class or reaction type at a time. We developed an in vitro nuclear magnetic resonance spectroscopy (NMR) approach, which permitted dynamic quantification of an entire ‘heterotypic’ network—simultaneously monitoring three distinct molecule classes (metabolites, proteins and RNA) and all elementary reaction types (bimolecular interactions, catalysis, unimolecular changes). Focusing on an eight-reaction co-transcriptional RNA folding network, in a single sample we recorded over 35 time points with over 170 observables each, and accurately determined five core reaction constants in multiplex. This reconstruction revealed unexpected cross-talk between the different reactions. We further observed dynamic phase-separation in a system of five distinct RNA-binding domains in the course of the RNA transcription reaction. Our Systems NMR approach provides a deeper understanding of biological network dynamics by combining the dynamic resolution of biochemical assays and the multiplexing ability of ‘omics’.

The regulation of cellular behavior is complex, and emerges from the dynamic interplay of diverse biomolecules, including proteins, RNA and metabolites. Most experimental methods, however, can only monitor a single molecule class or reaction type at a time (catalysis, bimolecular interactions and unimolecular state changes), limiting our ability to measure complex cellular dynamics. Furthermore, studies of networks often face a choice between biochemical methods—measuring dynamic (for example, time-resolved) data only for a few network components, and ‘omics’ methods—measuring a large number of components, but usually with little dynamic information in a single sample1. This lack of dynamic data covering multiple network components is among the main limitations1–4 in developing validated mechanistic, mathematical models for cellular networks, which are key to understanding the underlying logic of these networks3.

To address the above challenges, we sought to devise a nuclear magnetic resonance- (NMR) based approach that would (1) allow us to monitor ‘heterotypic’ networks and pathways—involving different molecule or reaction types—entirely, in a single in vitro sample, and (2) provide quantitative dynamic data for modeling of the network mechanisms. With certain limitations on molecule size and concentration ($\leq 50–100$ kDa, $\geq 10–50$ $\mu$M)5,6, solution NMR can monitor any reaction type or molecular class in a wide range of conditions, including unfractionated cell extracts and living cells7. The use of NMR to monitor reactions is common in chemistry8, and in recent years, NMR has also been used to follow the dynamics of small-scale reaction networks in biology. However, those studies focused on individual molecule classes; that is, metabolites9–14, proteins14,15,16 or RNA17–19.

We sought to monitor a more complex network by NMR, that comprises a wide range of different molecule and reaction types. Co-transcriptional RNA folding is an important cellular process that simultaneously involves RNA, proteins and metabolites, and is still poorly understood. RNA molecules of the same sequence may form distinct folded structures, with distinct functions and fates, depending on the effectors present during RNA transcription10,11. Insights are still limited on how the final RNA structures are influenced by co-transcriptional interactions of the transcribing RNA. The core reactions of the underlying network are RNA synthesis from metabolites, RNA folding and protein–RNA interactions (Fig. 1a). Our aims were (1) to design an assay to monitor all main components of the network simultaneously by NMR spectroscopy, using specific signatures of different molecules in NMR spectra; (2) to establish a mathematical model explaining our observations and (3) to perturb the network with proteins and drug molecules to gain system-level insight into its dynamics. This assay revealed competitive weakening of specific hnRNP A1 protein–RNA interactions by unspecific nucleotide-bearing molecules, and exposed the dynamic phase-separation of proteins in the course of RNA transcription. We termed this methodological approach ‘Systems NMR’—a potential generic name for NMR-driven reconstruction of biomolecular reaction networks.

Results

Monitoring a co-transcriptional RNA folding network. We first sought to investigate whether the RNA-binding protein UP1 (a natural fragment of hnRNP A1) would perturb the co-transcriptional folding of three cognate RNA hairpins of this protein: SMN1 and SMN2, two hairpins present in exon 7 of human SMN1 and SMN2 genes, respectively20, and the stem loop 2 (EV2) of the internal ribosome entry site of Enterovirus 71 (ref. 21) (Fig. 1b). To distinguish the RNA-specific UP1 perturbations from other changes in the
network dynamics (pH, nucleotide triphosphate concentrations), a fourth, ‘non-binding’ RNA0 (RNA zero) was designed and tested as a control (Fig. 1b and Methods).

In our experiments, the DNA template, the nucleotide triphosphates (NTPs), MgCl₂, the pyrophosphatase and the RNA-binding protein are initially mixed in an NMR tube (Fig. 2a), and then transcription is triggered by addition of the T7 RNA polymerase. The reaction network (Fig. 1a) is subsequently monitored for ~20h by repeating several NMR experiments (Fig. 2b–d and Supplementary Video 1): 1D (one-dimensional) 31P to monitor the levels of metabolites and RNA; 1D 1H, to monitor RNA folding; and 2D (two-dimensional) 1H–15N, to monitor protein interactions. Each set of measurements takes ~30 min to record, yielding an overall dataset of ~120–160 NMR spectra with ~40 time points for each individual spectrum type. The combined number of resolved quantifiable NMR signals at each time point exceeded 170: 8 in the 31P spectrum (Fig. 2b), more than 20 in the 1H spectrum (Fig. 2c) and over 150 protein backbone amide signals in the 2D 1H–15N spectrum (Fig. 2d). For quantitative modeling of the target network, ten signals were used (Supplementary Table 1): the 31P signals of inorganic phosphate (PO₄ (a placeholder for multiple PO₄ species), refer- ring to PO₄³⁻ and its protonated forms), RNA phosphate, α, β and γ-phosphate of the NTP, α and β-phosphate of nucleotide diphosphate (NDP) (Fig. 2b,c); the 1H imino signals of RNA uracils U5 (SMN1 and SMN2) or U4 (EV2) (Fig. 2f) and the 1H–15N signals of the selected UP1 residues reporting on RNA binding, His33 and Arg75 (Fig. 2g). In this study, these ten signals were sufficient to quantitatively track the key parameters of the target eight-reaction network. The data from remaining signals can still be used in subsequent studies to investigate the system in more detail. For example, to analyze individual conversion rates of four NTPs, or to analyze RNA and protein perturbations not just via overall reaction constants, but with residue-level resolution.

Among the key features of NMR is the intrinsically quantitative nature of the observed signals, which permits direct determination of certain physico-chemical molecular properties with few or no calibrations. To quantify the metabolite and RNA concentrations, we measured the integrals of corresponding signals in 31P spectra (Fig. 2b). Linewidths of NMR signals combine information about the molecule size (tumbling rate) and dynamics (lifetime) of molecular states, we therefore measured the linewidths of the well-separated imino signals of the folded RNA in 1H spectra to quantify the RNA stability (Ura5 and Ura4, see Fig. 2i). The positions of NMR signals report on the chemical environment of the corresponding atoms. Therefore, to quantify the RNA binding to the protein, we measured the shifts in the positions of selected protein ‘reporter’ signals, which shifted systematically in the 1H–15N spectra between the free and bound protein states as the more RNA was bound (His33 and Arg75, Fig. 2i).

In summary, a quantitative NMR assay was established with dedicated reporter signals to monitor metabolite, RNA and protein dynamics in one sample (Supplementary Table 1 and Supplementary Video 1).

Network model from NMR data. To integrate the measured data and evaluate our understanding of the network dynamics, a mathematical model combining ordinary differential equations (ODE) was formulated (Methods). The initial model consisted of three reactions: RNA synthesis, RNA folding and protein–RNA binding (Fig. 1a, reactions 1–3). Unexpectedly, a reduction in the total integral of 31P-containing species was observed over time (T1-relaxation-corrected), sometimes followed by sharp drops in the concentration of free PO₄ species at the end of transcription (Fig. 2h, first panel, blue trace). Further analysis revealed that the designed assay could also sense the formation of soluble MgHPO₄ aggregates, which are not directly visible in solution NMR. Extension of the network...
The behavior of a reaction network can be predicted at any concentration of reactants if the constants (fundamental parameters) of all reactions are known. Deriving these fundamental parameters from experimental data is one of the main goals of mathematical modeling of reaction networks. From a single NMR assay, we could determine the constants of five out of the eight network reactions (numbers 1–3, 7 and 8, Fig. 1a), while the constants of the other reactions (numbers 4–6) were fixed (Methods and Supplementary Table 2). The five unconstrained constants were determined by fitting the mathematical model to the time-resolved NMR observables. For each RNA (RNA0, SMN1, SMN2, EV2) at least three NMR assay replicates were recorded and fitted (Supplementary Fig. 1). For validation, four out of five multiplex-derived Systems NMR constants were compared with the constants derived by classical approaches, when a single reaction was perturbed at a time (the catalytic rate constant \( k_{\text{cat}} \), the free energy \( \Delta G \), the affinity constant \( K_d \), and the equilibrium constant \( K_{\text{eq(MgHPO}_4)_{\text{cat}}} \)). Remarkably, all tested constants were in agreement with classical methods.

The equilibrium constant for the formation of soluble MgHPO₄ aggregates (\( K_{\text{eq(MgHPO}_4)_{\text{cat}}} \)) showed an average value of 1.31 ± 0.06 mM, closely matching the 0.97 ± 0.05 mM value reported in the literature (Fig. 3a).

The expected catalytic rate constant \( k_{\text{cat}} \) closely matched the average value of 0.4 ± 0.12 nt s⁻¹ for the three short RNAs in Systems NMR datasets (Fig. 3b). Both the literature reference and the NMR \( k_{\text{cat}} \) constants are averaging the initiation and elongation phases of transcription. This is manifested in the roughly two-fold increase in the overall \( k_{\text{cat}} = 0.73 ± 0.06 \text{ nt s}^{-1} \) for the longer EV2 RNA (Fig. 3b), for which the polymerase spends more time in the faster elongation phase.

Based on the measured ultraviolet spectroscopy (UV) melting experiments (Supplementary Note 1), the free energy \( \Delta G \) of folding of the two RNA hairpins (SMN1 and SMN2, differing by a single
RNA perturbations by proteins and small molecules. The reconstructed network was then perturbed by proteins and drug candidate molecules to gain insight into the network dynamics.

To probe the effect of protein on the folded RNA, the assays were performed under two conditions: co-transcriptionally, when the UP1 protein was added from the start and during the entire period of RNA synthesis, and post-transcriptionally, when UP1 protein was added only near the end of transcription. The experiments showed that UP1 appears to (1) at least partially unwind the SMN2 hairpin and (2) forms a 2:1 complex with the EV2 RNA when UP1 is added post-transcriptionally, and only a 1:1 complex with EV2 when UP1 is present co-transcriptionally (Supplementary Fig. 2).

To probe the effect of small molecules, the reactions with SMN2 RNA were performed in presence of drug candidate molecules, recently developed to correct the aberrant splicing of exon 7 from the SMN2 gene. The experiments with SMN2 ESE1 suggested that under given co-transcriptional conditions one of the molecules may influence RNA folding, and another one reduces RNA transcription rate (Supplementary Fig. 5).

Mulitplexed monitoring of protein perturbations during RNA transcription. RNA-binding proteins often synergize or compete for binding to the same RNA. For example, the splicing of the SMN2 exon 7 is regulated by hnRNP A1, SRSF1, hnRNP G and Tra2-β1 (ref. 2). To facilitate the multiplexed analysis of interactions in this system of several RNA-binding proteins, we devised two labeling schemes that visualized the protein–RNA interaction interfaces in the RNA recognition motifs (RRM) of these proteins in one sample at the same time (Fig. 4a–c and Supplementary Note 2). RNA transcription was then performed in the presence of five [35S]N-valine-labeled protein constructs mixed together (two independent RRMs in the case of SRSF1), monitoring all valines and quantifying their perturbations in real time (Fig. 4d,e).

In summary, Systems NMR accurately quantified all core reaction constants of the target network in multiplex. All validated reaction constants matched the reference values with <2.5-fold difference.
The derivation of individual catalytic, unimolecular and bimolecular reaction constants by NMR is not uncommon, but the Systems NMR approach enables us to quantify a network with all elementary reaction types and main biomolecule classes in a single sample. Due to the non-destructive nature of NMR, each sample yields not just a snapshot of the network, but reveals its dynamics over time or another variable condition, thereby giving deeper insight into the network logic.

The different reaction constants determined from individual multiplexed NMR assays in our study appear accurate, showing <2.5-fold difference with validation values (Fig. 3). The differences between network-based and single-reaction-based assays can reveal unaccounted cross-talk reactions, such as the unspecific interactions of UP1 protein with the abortive RNAs and free NTPs detected here. Our results correlate with the recent UP1 specificity screens and suggest that in vivo UP1/hnRNP A1 protein affinity to specific RNA targets will likely be ~1,000-fold weaker than the nM-range affinities anticipated from single-reaction in vitro assays.

Another emergent behavior we detected was the RNA-driven in vitro phase-separation in a system of five protein domains (Fig. 4d), which was largely absent for individual domains under the same conditions. This observation suggests that Systems NMR could be used to probe structural perturbations of proteins in phase-separated droplets and membraneless organelles, an emerging...
research area with connections to various age-related disorders. The method can resolve residue-level signals of multiple proteins at once, does not require chemical modifications of proteins and allows monitoring of enzymatic activities within the same assay.

**NMR assay limits.** One specific requirement of the assay developed here is the need to design a ~8–10 nt-long 5’ overhang RNA sequence that minimizes interference of short abortive RNAs with specific protein–RNA interactions and RNA folding. This sequence is designed algorithmically and can be used as a separate control to identify specific RNA effects from the other network perturbations.

More broadly, for a generic reaction network, present-day solution NMR permits the direct observation of rigid molecules below ~50–100 kDa in size and at minimal concentration of ~10–50 μM. Under certain conditions, observation of 1MDa complexes can be achieved, and in combination with dissolution dynamic nuclear polarization technology, molecules at sub-μM concentrations can be transiently observed.

For catalytic reactions, NMR permits quantification of kinetic (non-equilibrium) processes on the time-scales going from seconds to hours and days. For unimolecular reactions, many NMR techniques are available, potentially allowing quantification of low-populated molecular states down to fractions of percent from the main species (~5–10 kcal mol⁻¹ in free energy difference). For bimolecular interactions, NMR currently permits direct quantification of dissociation constants in the low-μM to medium-nM range. And by monitoring competitive displacement of weak-affinity ligands, also low-nM dissociation constants can be quantified.

As suggested by the selective labeling experiments shown here (Fig. 4) and the recent multiplexed NMR kinase assays, at least a few dozen of protein-focused reactions should be observable by NMR in one sample in parallel. The same multiplexing is also feasible for metabolites, but may be challenging for RNAs due to the higher degeneracy of their NMR signals.

While small-molecule NMR signals can mostly be interpreted ab initio, the assignment of observed signals to specific molecular epitopes in macromolecules requires time. Nevertheless, the NMR signal assignments from ~7,000 unique protein and ~600 unique RNA NMR structures are already available in the Protein Data Bank (pdb.org), providing an already vast starting ground for NMR network reconstructions.

Mathematical ODE models of reaction networks can be easily formulated using rule-based modeling, and computational methods exist to efficiently estimate network parameters and perform model selection, with virtually no limitations for moderately-large networks expected in NMR assays.

**Applications.** The generalized workflow in Systems Biology consists of four steps: experiment, modeling, prediction and testing of predictions, often repeated iteratively. By uniquely providing both multiplexed and dynamic data from single samples at the first experimental stage, Systems NMR can accelerate the downstream development of accurate mathematical models, the understanding of network dynamics and the resulting predictions. Because NMR can dynamically monitor molecules in complex environments including living cells, the determination of true rates and constants for cellular networks in their natural context can generate reusable data for modeling and prediction of network dynamics.

Another advantage is that in vitro Systems NMR reconstructions provide an experimental ground of intermediate complexity, between simplified single-reaction in vitro assays and often very complex in vivo networks. Such moderate complexity may already reveal emergent network properties, such as phase-separation of RNA-binding domains observed here.

Considering specific applications, Systems NMR can advance studies of ‘heterotypic’ networks involving different molecule and/or reaction types. For example, concurrent quantification of perturbations in different parts of a biochemical network such as RNA transcription, folding and protein interactions observed here; or simultaneous quantification of catalysis and allosteric interactions in synthetic biology networks, or monitoring cross-talk between metabolic and signaling pathways.

In conclusion, combining the dynamic resolution of biochemical assays and the multiplexing ability of omics, we expect Systems NMR to pave the way to a deeper systems-level understanding of biological network dynamics both in fundamental and applied contexts.

**Online content**

Any methods, additional references, Nature Research reporting summaries, source data, statements of code and data availability and associated accession codes are available at https://doi.org/10.1038/s41592-019-0495-7.

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**Author contributions**

Y.N. conceived the idea, obtained initial funding, performed experiments, data analysis and network modeling. F.H.-T.A. supervised the project, provided infrastructure and financial support. D.I. supervised the network modeling part of the project. N.R. expressed and purified selectively labeled proteins and contributed to the transcription/NMR experiments. F.P. and M.S. supervised and provided technical and analytical support on mass spectrometry analyses. Y.N. wrote the manuscript with input from all of the authors.

**Competing interests**

The authors declare no competing interests.

**Additional information**

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phosphate-containing species were calculated stoichiometrically from 31P integrals (9–10) 2D HN spectra—His33 and Arg75 residues of UP1. Populations of α were cloned into pTX1 vector54 at SapI sites, using double-DNA templates.

DNA templates. For RNA transcription, corresponding sequences were cloned into plX1 vector at SapI sites, using double-stranded DNAs from commercial (Microsynth AG) single-stranded oligos: RNA0 (ATAGCACCACAC, TCAGCTGTTGTTGC), SMN1 (ATAGACCAACAGGGTTATCAGAAATTCCGC, TCAGCCGTTTCTGAAACCCGGTTGTTGC), SMN2 (ATAGACCAACAGGGTTATGACAAATTCCGC, TCAGCCGTTTCTGAAACCCGGTTGTTGC), SMN3 (ATAGACCAACAGGGTTATCAGAAATTCCGC, TCAGCCGTTTCTGAAACCCGGTTGTTGC), ev2 (ATAGACCAAGGATCTAAGGCTGGACACCGACATACCTTGATCC, TCAAGGATCAAGGTATGCTAGCTGGACACCGACATACCTTGATCC). Plasmids were purified using the Nucleobond Xtra Midi kit (Macherey Nagel) and the final pellets washed three times with 70% ethanol, dried and linearized by BsaI (NEB) enzyme for 15 h at 50°C in NEB1 buffer.

Proteins. All constructs and purification procedures were described earlier: UP1 (ref. ), SR51-R1M and RM2 (ref. ), Tra2-β (ref. ) and hRNPN G. After purification, proteins were transferred into transcription-NMR buffer (40 mM Tris-HCl, 0.01% Triton X-100, 5 mM dithiothreitol (DTT), pH 7.7) by dialysis, then flash-frozen and stored at −20°C.

In vitro transcription in NMR tube. Reactions were performed at 30°C, 40 mM Tris-HCl, 0.01% Triton-X100, 5 mM DTT, pH 7.7 supplemented with 5 mM of each nucleotide triphosphate (AppliChem), 24 mM MgCl₂, 1 U per ml inorganic pyrophosphatase from baker’s yeast (Sigma), 5% D.O, 50 µM 4,4-dimethyl-4-silapentane-1-sulfonic acid, 280 mM 7T RNA polymerase and 33 mN DNA template. Protein concentrations were 150 µM in single-protein reactions, and 83 µM of each protein was used for multi-protein reactions. In multi-protein experiments, 50 mM L-Arg and 50 mM L-Glu (AppliChem) were added to reduce precipitation, which correlates with UP1’s ability to phase-separate and aggregate in presence of RNA. Therefore, to estimate the HN signal position was assumed negligible because the transcription buffer pH=7.7 is far from the histidine pKa=6, and the chemical shifts of other surface-exposed UP1 histidines did not exhibit the same perturbation effects. Calculating the fraction of the bound protein under the binding model requires information on protein signal positions in the free and fully bound states. The shifts of the bound state are usually estimated as one of the parameters of the Kᵣ fitting procedure, as the asymptote of the protein saturation curve. The 150 µM UP1 protein data did not approach this saturation under the assay conditions, because of the low RNA/protein ratio, since the final concentrations of specific RNAs reached only ~120 µM, giving only ~0.8 RNA/protein ratio. Addition of pure RNA to saturate the protein under these conditions consistently led to protein precipitation, which correlates with UP1’s ability to phase-separate and aggregate in presence of RNA. Therefore, to estimate the HN signal positions of His33 and Arg75 in the saturated protein, an additional set of transcription experiments was recorded using 20 and 30 µM UP1 and the ‘high-affinity’ 15N RNA. This allowed to increase protein saturation by reducing ~61 and 41 RNA/protein ratios (~120/20 and 120/30 µM, respectively) at the end of the reaction. Due to the poor NMR sensitivity at 20–30 µM protein concentrations, the 2D HN spectra in these experiments required ~10 h acquisition time and could only be recorded as non-time-resolved spectra at end of transcription reaction, when the system reached equilibrium. The combined CSP data from the datasets with high (150 µM) and low (20–30 µM) protein concentrations gave an imperfect fit with the single-site binding model, suggesting that UP1 is already close to saturation in the assays with 20 and 30 µM UP1.

Mathematical modeling. The model was built using the BioNetGen language and resulted in eight rate equations and nine differential equations:

Rate equations

\[ v_{\text{R}} (\text{synthesis of RNA}) = k_{\text{cat, RNA}} \times \text{NTP} \]
\[ v_{\text{RNP}} (\text{RNA folding}) = \text{analytical solution, see below} \]
\[ v_{\text{R}} (\text{binding of protein to RNA}) = k_{\text{cat}} \times \text{protein} \times \text{RNA} \]
\[ v_{\text{R}} (\text{dissociation of protein – RNA complex}) = k_{\text{off}} \times \text{protein} \times \text{RNA complex} \]
\[ v_{\text{R}} (\text{synthesis of aborts}) = k_{\text{cat, aborts}} \times \text{NTP} \]
\[ v_{\text{R}} (\text{hydrolysis of pyrophosphate}) = k_{\text{epp}} \times \text{PPi} \]
\[ v_{\text{R}} (\text{formation of MgHPO}_4) = k_{\text{m}} \times \text{MgHPO}_4 \times \text{salt} \]

NMR observables. For final network modeling, ten signals were used: 2P spectra: (1) PO4 (P₀), and its protonated forms, (2) RNA, (3–5) dNTP, (4) HN, cNTP, (6–7) dNTP, (8) H spectra; U5 (SMN1/2) or U4 (EV2) imino signals; (9–10) HN spectra—His33 and Arg75 residues. Population averages were calculated from HN spectra—His33 and Arg75 residues. Populations containing species were calculated stoichiometrically from 31P integrals using cNTP integral at time = 0 as 20 mM internal calibration. Each 1P integral was T₁-relaxation-weighted using the ratios of corresponding integrals measured in the reference 1P spectra with 30 and 0.8 s interscan delays at the end of the transcription reaction, that is, \( I_{\text{up},\text{int}}/I_{\text{up},\text{int}} \times I_{\text{up},\text{int}}/I_{\text{up},\text{int}} \). NTP and dNTP populations were quantitated from HN integrals. POPC decay of the total T1-weighted 1P integral of all species. For long RNAs (~20nt), the 1D 1P signals became too broad, preventing accurate quantification at a reasonable time-resolution, so RNA concentrations were calculated from the decay of NTP signals. Due to the NMR signal degeneracy, the fractions of RNA and aborts could not be quantified within the NMR assay, and were fixed to 30 and 70%, by nucleotide mass, based on quantitative ultraviolet (260 nm) high-performance liquid chromatography (HPLC) analysis of reaction end-products.

The fraction of bound UP1 protein was derived from the chemical shift perturbation (CSP) of HN signals of His33 and Arg75. These residues were chosen as reporters for two reasons. First, they appeared to sense the same molecular environment in all four–protein RNA complexes, as they all displayed signals moving in the same direction during transcription (Fig. 2g). Based on the existing UP1-RNA/DNA structures (PDB: 4YOE, 2UP1), these two residues are located near the RNA-binding pocket, but do not directly interact with the RNA, which explains how they could sense the same epitope changes independent of the RNA sequence. Second, these signals were sensitive to the differences in affinity of the RNA binding, as the magnitude of the ‘H–N CSP varied for different protein–RNA complexes (Fig. 2g)]. In assays with 150 µM UP1 concentration, both signals appeared predominantly in fast exchange with respect to the NMR time scale, and so the fast exchange assumption was used during modeling. The experimental HN CSPs were calculated using 4HN = (\( \Delta HN + (\Delta N \times 0.2) \)). The effect of pH change on histidine signal position was assumed negligible because the transcription buffer pH=7.7 is far from the histidine pKa=6, and the chemical shifts of other surface-exposed UP1 histidines did not exhibit the same perturbation effects.

Calculating the fraction of the bound protein under the binding model requires information on protein signal positions in the free and fully bound states. The shifts of the bound state are usually estimated as one of the parameters of the Kᵣ fitting procedure, as the asymptote of the protein saturation curve. The 150 µM UP1 protein data did not approach this saturation under the assay conditions, because of the low RNA/protein ratio, since the final concentrations of specific RNAs reached only ~120 µM, giving only ~0.8 RNA/protein ratio. Addition of pure RNA to saturate the protein under these conditions consistently led to protein precipitation, which correlates with UP1’s ability to phase-separate and aggregate in presence of RNA. Therefore, to estimate the HN signal positions of His33 and Arg75 in the saturated protein, an additional set of transcription experiments was recorded using 20 and 30 µM UP1 and the ‘high-affinity’ 15N RNA. This allowed to increase protein saturation by reducing ~61 and 41 RNA/protein ratios (~120/20 and 120/30 µM, respectively) at the end of the reaction. Due to the poor NMR sensitivity at 20–30 µM protein concentrations, the 2D HN spectra in these experiments required ~10 h acquisition time and could only be recorded as non-time-resolved spectra at end of transcription reaction, when the system reached equilibrium. The combined CSP data from the datasets with high (150 µM) and low (20–30 µM) protein concentrations gave an imperfect fit with the single-site binding model, suggesting that UP1 is already close to saturation in the assays with 150 µM protein concentration (Supplementary Fig. 8). This is likely due to additional weak UP1 binding sites in the EV2 RNA, as suggested by Arg75 peak splitting in assays with 20–30 µM UP1 concentration. The chemical shifts of His33 and Arg75 residues in the fully saturated protein state for the final ODE modeling of the four main datasets (RNA0, SMN1, SMN2, EV2 at 150 µM UP1) were taken as the shifts giving best fit when simultaneously fitting the data from EV2 RNA datasets with 150, 30 and 20 µM UP1 protein concentration (Supplementary Fig. 8). All above 1P and HN data was used for global parameterization of the ODE model, and 1H imino signals were used for line shape analysis and RNA ΔG derivation.
\[ v_{F}(\text{dissociation of MgHPO}_4 \text{ salt}) = k_{\text{dissolve}} \times \text{MgHPO}_4 \]

\[ v_{R}(\text{dephosphorylation of NTPs}) = k_{\text{dephos}} \times \text{NTP} \times \text{NTP} \]

**Differential equations**

\[ \frac{d\text{NTP}}{dt} = -v_{I} - v_{F} - v_{R} \]

\[ \frac{d\text{DNA}}{dt} = +v_{R} - \frac{v_{RNA} \times v_{RF}}{v_{RNA} + v_{RF}} \]

\[ \frac{d\text{PO4}}{dt} = +v_{I} \times \frac{v_{RNA} - 1}{v_{RNA} + v_{RF}} - v_{F} \]

\[ \frac{d\text{DNP}}{dt} = +v_{R} - \frac{v_{4} \times v_{Aborts} - v_{F} \times v_{RF}}{v_{4} \times v_{Aborts} + v_{F} \times v_{RF}} \]

\[ \frac{d\text{MgHPO4}}{dt} = +v_{RF} - v_{RF} \]

\[ \frac{d\text{Aborts}}{dt} = +v_{R} - \frac{v_{4} \times v_{Aborts} - v_{F} \times v_{RF}}{v_{4} \times v_{Aborts} + v_{F} \times v_{RF}} \]

\[ \frac{d\text{protein} \times \text{complex}}{dt} = +v_{RF} - v_{RF} \]

At the given hairpin stability (\(\approx -5.5 \text{ kcal mol}^{-1}\)) the SMN and EV2 RNA2 are predominantly in a single state (99.99% folded). The expected rate of hairpin folding (\(v_{F} = 8-51 \times 10^{-5} \text{ s}^{-1}\) for ~30 nt hairpins) is three orders of magnitude faster than protein–RNA encounters at the unbiased diffusion rate (~105 M\(^{-1}\) s\(^{-1}\)).

**RNA folding \(\Delta G\) from imino signal line shape analysis.** For fitting, 1D \(^1\)H-SOFAST spectra were Fourier-transformed with no apodization function. Imino signals were fitted to a single-Lorentzian function using the lorentzfit routine (I. Wells, Lorentzfit, MATLAB Central File Exchange no. 33773, 2015). The fitted 0.2 ppm fitting window and assumed a baseline fixed at zero signal intensity. The fitted linewidth parameter (full width at half maximum) was used to derive the unfolding-driven imino-exchange rate (\(K_{\text{ex, intrinsic}}\)).

\[ k_{\text{ex}} = \text{linewidth} \times \pi \]

The contribution of base-flipping (\(k_{\text{ex, flipping}}\)) and transverse relaxation rate (\(R_{2}\)) was determined from linewidths of imino signals in purified SMN2 hairpin additionally stabilized by terminal GCs (13-base pair, GCCCGGUGUUGGC-AGAC-GCAGCAAAUCGCGC). In this stabilized RNA, the exchange by global unfolding is suppressed (\(\Delta G_{\text{eq}} = -23 \text{ kcal mol}^{-1}\)), which was confirmed by the negligible dependence of its imino integrals on temperature (not shown). The combined (\(K_{\text{ex, flipping}} \times R_{2}\)) value for imino signals in an UA pair flanked by GU and UA pairs, under transcription buffer conditions, was determined to be 61.4 s\(^{-1}\).

Imino linewidths depended on pH (the concentration of imino-exchange catalyst), indicating that the system is under the bimolecular exchange regime (EX2), and hence the measured \(k_{\text{ex}}\) reports on the equilibrium constant of RNA unfolding/\(\text{open}\) (\(K_{\text{eq, unfolding}} = K_{\text{eq}}\)). The intrinsic exchange rate \(k_{\text{ex, intrinsic}}\) (same as the exchange from the open state, \(k_{\text{ex, neutral}}\)) in the transcription buffer was measured to be \(-10^{-4}\) s\(^{-1}\) for both UTP and GTP, using a protocol described elsewhere. The final free energy of folding was determined using:

\[ K_{\text{eq, unfolding}} = k_{\text{ex, unfolding}} \times K_{\text{ex, intrinsic}} \]

**RNA purification.** RNAs for ITC and ultraviolet-melting experiments were purified by anion-exchange HPLC under denaturing 6 M urea, 80°C conditions, followed by n-butanol extraction, snap-cooling and lyophilization.

**Ultraviolet temperature melting.** For the melting experiments the RNA hairpins were produced without the single-stranded 5′ overhang to eliminate ultraviolet baseline distortions caused by this single-stranded region. The experiments used 2μM RNAs in 10 mM sodium-cacodylate, pH7.35, 5 mM MgCl\(_2\), and 25 mM l-Arg/L-Glu buffer. Details of the analysis are shown in Supplementary Note 1.

**ITC.** Experiments used conditions approximating those at the end of transcription-NMR reaction: 40 mM Tris-HCl, 0.01% Triton-X100, 2.5 mM β-Me, pH7.5, 37 mM NaPO\(_4\), 2.6 mM NTPs, 24 mM MgCl\(_2\), and 303 K. DTT was replaced with β-ME due to its instability and background heat changes. For each RNA, an RNA-to-buffer...
titration was performed and subtracted from the RNA-to-protein data. Data from the first injection point was discarded. To better represent the pool of unspecific RNAs in the transcription reaction, RNA0 was purified as a combined pool of 2–10 nt RNAs from transcription reaction. The concentration of this RNA0 pool was normalized by the average size of 5.8 nt based on HPLC-ultraviolet-weighted composition of the corresponding transcription mixture (30% full length RNA × 10 nt + 70% aborts × 4 nt average). For RNA0, SMN1 and SMN2 RNAs the ITC data was fitted with the one-site interaction model using MicroCal Origin (Supplementary Fig. 3a–c). A one-site $K_0$, was needed for all RNAs to compare it with the one-site binding model used in the ODE analysis. The standard fitting protocol of MicroCal Origin encountered local minima when fitting the one-site model to the EV2-UP1 ITC data (likely due to the known bi-modal binding of UP1 to this RNA). Therefore for EV2-UP1, the apparently one-site $K_0$ constant was derived as a mean of three different fitting protocols (Supplementary Fig. 3d–g): (1) high-affinity $K_0$ from two-site model in MicroCal Origin, (2) one-site $K_0$ fitted using a stoichiometric 1:1 equilibrium model in Affinity meter software (affinimeter.com) and (3) one-site $K_0$ fitted using a general ligand-target equilibrium binding isotherm, which only parameterizes the $K_0$ constant (without considering AH) and assumes $N=1$. All three fitting procedures yielded comparable $K_0$ for EV2-UP1 binding (4.8, 7.1 and 3.3 $\mu$M, respectively).

**Perturbation experiments.** Post-transcriptional perturbations by UP1 protein were performed by adding, 13 h after transcription start, 67.5 nmol of "N-UP1. Protein was $\sim1.500$ nmol concentration, to achieve $\pm 10\%$ dilution of the mixture. In small-molecule perturbation experiments, the SMN2 ESE1 transcription mixture was spiked co-transcriptionally with $200\mu$M of one of three molecules (NVSSM1, smn-C5 and smn-C7; ref. (71)) in 1% DMSO or 1% DMSO alone. In these experiments, SMN2 DNA template used an earlier version of the 5’ overhang sequence (5’-GCCGCCUGUA-3’), before it was optimized at three positions (3, 7, 8) to reduce its self-complementarity.

**Imino signal broadening on UP1 protein binding.** Imino signal linewidths could be primarily influenced by the (1) changes in $K_0$ exchange rate of iminos due to unfolding of the stem, (2) $k_\text{ex}$ changes due to base-flipping and (3) line broadening due to enhanced transverse relaxation ($R_2$) and B0 field inhomogeneity ($R_2\text{(B0)}$). Thus, overall linewidth equals $\Delta \nu_{\text{iso}} = \Delta \nu_{\text{ collinear}} + k_\text{ex} + k_\text{ex,base-flipping} + R_2 + R_2\text{(B0)}/c$. Contribution of B0 field inhomogeneity is considered negligibly small. The $R_2$ relaxation increase on formation of a 1 to1 RNA–UP1 protein complex was estimated to be $41/\pi Hz$, given 22.5 kDa UP1 mass, at 303 K, in phosphate buffer (0.001 g ml$^{-1}$), assuming spherical shape of the protein with $r_v = 2.4$ Å (hydration layer) and $R_2 = 5 x 10^4$ (correlation time)$^6$. **Cell culture and nuclear extracts.** Extracts were prepared using published procedures$^{26}$ from HEK293 cells grown to confluence.

**Mass spectrometry for quantification of specific protein concentrations in cell.** Pure recombinant uniformly 15N-labeled proteins were spiked into nuclear extracts at a 0.15–0.2 μM concentration. Resulting extracts were reduced, alkylated and digested using trypsin before peptide desalting and purification as previously described$^{27}$. Selected reaction monitoring (SRM) on a triple-quadrupole mass spectrometer was used for targeted proteomic measurements. SRM assays were generated as previously described$^{28}$ by selecting the 4–5 most intense transitions from samples with pure 15N-labeled recombinant proteins digested with the same protocol. Sum peak areas of transitions for each peptide were used to calculate the intensity ratio between 15N reference and 15N endogenous peptide signals. The mean and standard deviation of all peptides for each protein were used to find the concentration of endogenous proteins in nuclear extracts.

**Selective labeling.** Proteins were expressed in minimal M9 medium supplemented with 15N-Val and 13C-Phe, and with all amino acids and nucleosides in unlabeled form (Supplementary Table 3). A limiting amount of unlabeled Phe/Val was added for transaminase suppression. The 13C/$^15$N-labeled amino acids were added only 10 min before induction. Cells were harvested 3–5 h post-induction.

**Statistics.** Statistical analyses and experiment replicate numbers, where applicable, are described in the corresponding figure legends and method sections. Unless otherwise indicated the derived values and error bars correspond to the mean ± s.d.

**Reporting Summary.** Further information on research design is available in the Nature Research Reporting Summary linked to this article.

**Data availability**

Raw NMR data from the main experiments was deposited in Zenodo (10.5281/zenodo.2554066). Source data for the main figures are included in the online article. SRM-MS-Proteomics data was deposited in PeptideAtlas (PASS01365). The ODE network model was deposited in BioModels$^{6}$ (MODEL1812270001). RNA-encoding plasmids were deposited in AddGene (ID nos. 126040, 126041, 126042, 126043). Further data and code are available from the corresponding authors upon request.

**Code availability**

Main code with examples and a protocol for the Systems NMR setup is available at github.com/systemsnmr/vtnnmr.

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Reporting Summary

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When statistical analyses are reported, confirm that the following items are present in the relevant location (e.g. figure legend, table legend, main text, or Methods section).

- n/a [ ] Confirmed
- [ ] The exact sample size (n) for each experimental group/condition, given as a discrete number and unit of measurement
- [ ] An indication of whether measurements were taken from distinct samples or whether the same sample was measured repeatedly
- [ ] The statistical test(s) used AND whether they are one- or two-sided
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- [ ] For null hypothesis testing, the test statistic (e.g. F, t, r) with confidence intervals, effect sizes, degrees of freedom and P value noted
  - Give P values as exact values whenever suitable.
- [ ] For Bayesian analysis, information on the choice of priors and Markov chain Monte Carlo settings
- [ ] For hierarchical and complex designs, identification of the appropriate level for tests and full reporting of outcomes
- [ ] Estimates of effect sizes (e.g. Cohen's d, Pearson's r), indicating how they were calculated
- [ ] Clearly defined error bars
  - State explicitly what error bars represent (e.g. SD, SE, CI)

Our web collection on statistics for biologists may be useful.

Software and code

Policy information about availability of computer code

| Data collection | TopSpin 3.2 & 4.0.3 |
|-----------------|---------------------|
| Data analysis   | TopSpin 3.2 & 4.0.3  |
|                 | BioNetGen 2.17       |
|                 | Rulebender 2.0r382   |
|                 | Matlab R2011a, R2016 |
|                 | Python 2.7.14        |
|                 | ImageJ v2.0.0        |
|                 | Affinimeter v2.1710  |
|                 | Prism v5.0a          |
|                 | Cara 1.8.4           |
|                 | Skyline v3.7.0.10940 |

All important parameters used to analyze the data are described in methods section. Main Python and Matlab scripts implementing data processing and analyses are available at github.com/systemsnmr/ivtnmr, as stated in Methods section.

For manuscripts utilizing custom algorithms or software that are central to the research but not yet described in published literature, software must be made available to editors/reviewers upon request. We strongly encourage code deposition in a community repository (e.g. GitHub). See the Nature Research guidelines for submitting code & software for further information.
Data

Policy information about availability of data

All manuscripts must include a data availability statement. This statement should provide the following information, where applicable:
- Accession codes, unique identifiers, or web links for publicly available datasets
- A list of figures that have associated raw data
- A description of any restrictions on data availability

Raw NMR data from the main experiments was deposited in Zenodo (10.5281/zenodo.2554066). Source data for the main figures are included in the online article. SRM-MS-Proteomics data was deposited in PeptideAtlas (PASS01365). The ODE network model was deposited in BioModels (MODEL1812270001). RNA-encoding plasmids were deposited in AddGene (ID #126040, #126041, #126042, #126043). Main code with examples and a protocol for the Systems NMR setup is available at github.com/systemsnmr/ivtnmr. Further data and code are available from the corresponding authors upon request.

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Life sciences study design

All studies must disclose on these points even when the disclosure is negative.

| Sample size | Where statistical analyses were required, Systems NMR experiments were performed 2-4 times (biological replicates, varying DNA template batch and/or protein batch). Specific numbers of replicates are stated in corresponding figure captions. |
| Data exclusions | - To make the time dimension uniform for all transcription-NMR datasets, for ODE model fits only the data below 24 hours was used, even if more time-points were recorded.  
- In calculations of imino linewidths - the initial points of transcription, before imino signal becomes visible, were not used in quantification of RNA stability because there is no signal to quantify.  
- In ITC analyses, following the standard procedures, the first injection points, in which the ligand is contaminated with target, were not used in fitting. |
| Replication | All attempts at replication were successful. The aberrations in 31P integrals due to apparently stochastic MgHPO4 aggregation are discussed in main text. |
| Randomization | Randomization was not relevant to our study. |
| Blinding | Blinding was not relevant to our study. |

Reporting for specific materials, systems and methods

Materials & experimental systems

| n/a | Involved in the study |
|-----|-----------------------|
| ☒  | Unique biological materials |
| ☒  | Antibodies |
| ☒  | Eukaryotic cell lines |
| ☒  | Palaeontology |
| ☒  | Animals and other organisms |
| ☒  | Human research participants |

Methods

| n/a | Involved in the study |
|-----|-----------------------|
| ☒  | ChIP-seq |
| ☒  | Flow cytometry |
| ☒  | MRI-based neuroimaging |

Unique biological materials

Policy information about availability of materials

Obtaining unique materials

RNA-encoding plasmids were deposited in AddGene (ID #126040, #126041, #126042, #126043). Further plasmids (e.g. for protein production) are available upon request.
### Eukaryotic cell lines

#### Policy information about cell lines

**Cell line source(s)**

HEK293T (human embryonic kidney) cells were obtained from the European Collection of Cell Cultures (ECACC No. 85120602).

**Authentication**

Cell lines were not authenticated.

**Mycoplasma contamination**

Cell lines were not tested for mycoplasma contamination.

**Commonly misidentified lines**

(See ICLAC register)

Based on ICLAC register, no commonly misidentified lines were used.