BSM $\nu$ physics: complementarity across energies
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ABSTRACT: We reiterate that there is significant complementarity between low-energy experiments and high-energy colliders in exploring new physics associated with neutrino properties and their mass generation mechanisms. Signals of the new physics in the two energy regimes may be correlated with each other from the same underlying dynamics. We demonstrate the complementary nature by presenting the physics reaches for the Seesaw models of Type I, II and III, and for general neutrino interactions in an effective field theory framework, and in a $Z'$ model.
1 Introduction

Flavor oscillations between massive neutrinos is a firmly established phenomenon that cannot be accounted for by the Standard Model (SM). Neutrino oscillations thus strongly motivate physics beyond the SM (BSM) that is associated with the neutrino sector. New physics associated with neutrinos can be probed at different energy scales and with limited theoretical prejudice. Certain signals of the new physics in the two energy regimes may be correlated with each other from the same underlying theory. It is ultimately important to seek complementary signals to establish a consistent picture of the underlying physics.

There are three tree-level mechanisms to generate neutrino masses of Majorana type that extend the SM’s field content in a minimal manner [1]. All of these introduce new particle states, including ones with gauge charges, and thus lead to rich phenomenology, complementary in different experiments at all energy scales. Here, we summarize searches for testing these models at the Large Hadron Collider (LHC) and its upgrades. For wide-ranging reviews on tests of both tree-level and radiative neutrino mass models, see Refs. [2–4].

On the phenomenological ground, general neutrino interactions (GNI) is the most general parameterization of new physics in the neutrino sector and widely used at the low-energy probes. The effective four-fermion interactions are commonly written as

\[ \mathcal{L}_{\text{GNI}} = \frac{G_F}{\sqrt{2}} \sum_a (\bar{\nu} \Gamma_a \nu) [\bar{f} \Gamma_a (\epsilon_a + \bar{\epsilon}_a \gamma^5) f], \]  

(1.1)

where \( \Gamma_a = \{1, i\gamma^5, \gamma^\mu, \gamma^\mu \gamma^5, \sigma^{\mu\nu}\} \) are the five Lorentz structures, corresponding to scalar, pseudoscalar, vector, axialvector, and tensor interactions, respectively. \( f \) denotes quarks and charged leptons. \( \epsilon \) and \( \bar{\epsilon} \) are the effective GNI parameters, and contain four flavor indices, which are kept implicit. The GNI is not valid above the weak scale or new physics scale. For illustration of the UV completion, we introduce a neutral gauge boson \( Z' \) to show the

\[ \text{(cont.)} \]
effects at different energies. We then adopt an SM effective field theory formalism including a right-handed neutrino ($\nu_R$). We demonstrate that the low- and high-energy probes have their own merits based on Refs. [5–7].

2 Collider tests of tree-level seesaws

Collider experiments offer powerful probes of heavy states predicted by neutrino mass models. As benchmarks, direct tests of minimal tree-level scenarios typically focus on phenomenological implementations [8, 9] of the canonical Types I, II, and III Seesaw models. Phenomenological scenarios treat the masses and mixing of new particles states as independent parameters to minimize model dependence.

The Phenomenological Type I Seesaw extends the SM field content by $n_R \geq 2$ right-handed neutrinos $\nu_R$. After electroweak (EW) symmetry breaking, the model parameterizes the mixing between EW currents and neutrino mass eigenstates by the decomposition

$$\nu_\ell = \sum_{m=1}^{3} U_{\ell m}^* \nu_m + \sum_{m'=4}^{3+n_R} V_{\ell m'}^* N_{m'},$$

(2.1)

where $\nu_\ell$ is a SM neutrino of flavor $\ell$ in the interaction basis, $\nu_m$ are the three light neutrino mass eigenstates, $U_{\ell m}$ are the light-active mixing matrix elements measured in oscillation experiments, $N_{m'}$ are heavy mass eigenstates, and $V_{\ell m'}$ are active-heavy (or active-sterile) mixing matrix elements. For discovery purposes, one typically considered only the $N_{m'=4}$ states and decouples the remaining $(n_R - 1)$ heavy mass eigenstates. The states $N_k$ couple to EW bosons through mixing, and therefore can be produced in a variety of mechanisms. At the LHC, the leading channels are the Drell-Yan mechanism [10], $W\gamma$ fusion [11–14], gluon fusion [15–17], and same-sign $W^+W^-$ scattering [18, 19]. For recent comparisons of the channels at the LHC and beyond, see Refs. [14, 19, 20].

Figure 1 shows the 95% CL sensitivity to active-sterile mixing $|V_{\ell 4}|^2$ as a function heavy neutrino mass at the LHC in the trilepton and MET channel using the analysis of Refs. [20, 21] for the benchmark flavor categories: (a) $|V_{e4}|^2 = |V_{\mu 4}|^2$ with $|V_{\tau 4}|^2 = 0$, (b) $|V_{e4}|^2 = |V_{\tau 4}|^2$ with $|V_{\mu 4}|^2 = 0$, (c) $|V_{\mu 4}|^2 = |V_{\tau 4}|^2$ with $|V_{e4}|^2 = 0$. Depending on the precise flavor category, active-sterile mixing as small as $|V_{\ell N}|^2 \sim 10^{-4} - 10^{-2}$ can be reached for masses in the approximate range of $m_N \approx 200 - 1200$ GeV with 3 ab$^{-1}$ of data [20, 21]. For some signal categories, the trilepton becomes directly competitive with low-energy tests of charged lepton flavor violation [22]. Fig. 1(d) shows the same but using the same-sign $W^\pm W^\pm \rightarrow \mu^\pm \mu^\pm$ scattering channel with the analysis of Ref. [19]. The analysis shows that mixing as small as $|V_{\ell N}|^2 \sim 10^{-1}$ can be reached for as large as $m_N \sim \mathcal{O}(10)$ TeV. It is important to stress that, if discovered, measuring heavy neutrinos’ chiral couplings will be paramount to fully exploring their properties and potential couplings to other undiscovered particles [23–25].
The Type II Seesaw extends the SM field content by a scalar multiplet that is a triplet under $SU(2)_L$ and carries hypercharge $Y = 1$. In the gauge basis, this can be written as

$$\sqrt{2} \Delta = \begin{pmatrix} \Delta^+ \\ \sqrt{2} \Delta^0 \\ -\Delta^+ \end{pmatrix},$$

(2.2)

which couples at tree-level to the SM Higgs field, including through a dimension $d = 4$ operator that explicitly violates lepton number. After EW symmetry breaking, $\Delta$ acquires a
Figure 2. The branching rate (BR) of $\Delta^{\pm\pm} \rightarrow \ell_i^\pm \ell_j^\pm$ decays in the Type II Seesaw as a function of the lightest neutrino mass for the normal hierarchy (NH) and inverted hierarchy (IH) ordering of neutrino masses, and in the limit of a vanishing triplet vev. Adapted from Ref. [26].
Figure 3. (a) The luminosity required to reach $5\sigma$ ($3\sigma$) discovery (sensitivity) of Type II Seesaw scalars produced in pairs produced in $\sqrt{s} = 14$ and 100 TeV pp collisions, and which subsequently decay to multi-lepton final states. Adapted from Ref. [26]. (b) The same but for Type III leptons produced in pairs in $\sqrt{s} = 14$ and 27 TeV pp collisions. Adapted from Ref. [29].

The analogous sensitivity at a hypothetical 100 TeV pp collider. At the LHC, pairs of triplet scalars with masses in the TeV range can be discovered with the full HL-LHC data set.

The Phenomenological Type III Seesaw extends the SM field content by $n_R \geq 2$ leptonic multiplets $\Sigma$ that are triplets under SU(2)$_L$. Like the Type I Seesaw, Dirac neutrino masses are generated through Yukawa couplings involving the SM Higgs field, SM lepton doublets, and $\Sigma$. The neutral component of $\Sigma$ also carries a Majorana mass, thereby triggering a high- or low-scale Seesaw depending on model assumptions. After mass diagonalization, the mass eigenstates $N, L^\pm$ can couple to charged and neutral leptons through mixing. The decomposition of gauge states into mass states can be parameterized by [30]

$$\Sigma^\pm = Y_L L^\pm + \varepsilon T_\ell \ell^\pm \quad \text{and} \quad \Sigma^0 = Y_N N + \varepsilon_T \nu_m,$$

(2.3)

where $|Y| \sim \mathcal{O}(1)$ and $|\varepsilon_T| \ll 1$ are mixing parameters. With these couplings, Type III leptons can mediate lepton flavor violation in various low-energy observables [31, 32].

Due to their gauge couplings, triplet leptons can be produced in pairs directly from gauge interactions and through a variety of production mechanisms at proton colliders [4, 16, 29, 30]. Single production in association with a SM lepton is possible through mixing. For recent comparisons of individual channels at the LHC and beyond, see Refs [4]. Typically, decays of $N$ and $L^\pm$ occurs at tree-level to SM leptons and an EW boson via mixing. However, even in the degenerate limit, $L^\pm \to N \pi^\pm$ decays are possible at one loop [33, 34]. Such decays
are allowed even in the limit of vanishing mixing. Using the analyses of Refs. [8, 29, 30, 35], Fig. 3(b) shows the luminosity required to reach 5σ (3σ) discovery (sensitivity) of Type III Seesaw leptons produced in pairs produced in √s = 14 and 27 TeV pp collisions, and which subsequently decay to multi-lepton final states.

**The Weinberg operator at the LHC.** Neutrinoless ββ decay (0νββ) experiments are powerful probes of lepton number violation and particularly the Weinberg operator

\[ O^{\alpha\beta} = [\Phi \cdot T^c_{\alpha}] [L_{\beta} \cdot \Phi]. \]  

Here, Φ and L are the usual SM Higgs and lepton doublets, with flavor indices α, β. Despite their incredible sensitivity, a limitation of 0νββ decay experiments is their flavor dependence. These experiments are only sensitive to phenomena in the \( \ell_\alpha \ell_\beta = ee \) channel, and the production of same-sign lepton pairs involving muons or taus is kinematically forbidden.

As noted in Ref. [36], the high-\( p_T \) analogue of the 0νββ process is the same-sign \( W^\pm W^\pm \rightarrow \ell^+_\alpha \ell^-_\beta \) scattering channel, and is potentially accessible at the LHC. A full signal-versus-background analysis shows that the √s = 13 TeV LHC with \( L = 300 \) ab\(^{-1} \) (3 ab\(^{-1} \)) can exclude EFT cutoff scales below \( \Lambda \lesssim 8.3 \) (11) TeV for a Wilson coefficient of \( C^{\alpha\beta} = 1 \) in the flavor channel \( \ell_\alpha \ell_\beta = \mu\mu \) [36]. Anticipated sensitivity to the \( \ell_\alpha \ell_\beta = ee \) and \( e\mu \) channels is anticipated to be comparable, with degraded sensitivity to the \( \ell_\alpha \ell_\beta = \tau\tau, \tau e \) and \( \tau\mu \) to the smaller \( \tau \) lepton identification. It is possible to extend this an analysis to the decays of heavy and light mesons [36, 37], thereby bringing further complementarity between high- and low-energy probes of BSM in the neutrino sector.

### 3 Z’ model

In this section, we discuss a scenario where the new physics scale is not high compared to the EW scale and therefore cannot be integrated out in low-energy tests. We focus on a Z’ model associated with a new, anomaly-free \( U(1)' \) symmetry. For concreteness, we consider masses in the range \( M_{Z'} = 5 \) MeV to few TeV and its coupling \( g' < 1 \). The Lagrangian can be written as

\[ \mathcal{L} = \mathcal{L}_{SM} - \frac{1}{4} Z'^{\mu\nu} Z'^\mu Z'^\nu + \frac{1}{2} M^2_Z Z'^{\mu} Z'^\mu + Z'^\mu J^\mu_X, \]  

where \( J^\mu_X \) is the fermion current that couples to the \( Z' \) boson. For the sake of illustration, we take the following three cases for our benchmark studies [38]:

(A) \( Z_{B-3L_\mu} \), (B) \( Z_{B-\frac{3}{2}(L_\mu+L_\tau)} \), (C) \( Z_{B-3L_\tau} \).

The parameters in these models can be constrained by both low-energy probes, like neutrino oscillation and coherent elastic neutrino-nucleus scattering, and high-energy probes like the collider experiments. The results are shown in Fig. 4. The red shaded areas and dashed lines correspond to the 2σ exclusion regions by using the energy spectrum from the COHERENT CsI detector [39] and the expected 2σ limit from COHERENT with a 750 kg LAr detector and a 4-year exposure using both energy and time information [40], respectively.
Figure 4. Bounds on $g'$ as a function of $M_{Z'}$ for Cases A (upper left panel), B (upper right panel) and C (lower panel). For details of individual experiment, see Sec. 3.

The purple shaded areas and dashed lines correspond to the $2\sigma$ bounds from a global fit to neutrino oscillation data [41] and the expected $2\sigma$ exclusion limit from DUNE and T2HK combined, respectively. Regions above the brown curves are excluded by using $pp/e^+e^-\rightarrow\mu^+\mu^-Z'$ searches at CMS [42] and BaBar [43] at $2\sigma$ and 90% CL, respectively. The brown dashed curves are the $2\sigma$ expected sensitivities from the $\mu^+\mu^-Z'$ channel at HL-LHC, with an integrated luminosity of 3 ab$^{-1}$. The blue solid (dashed) curves correspond to the expected $2\sigma$ ($5\sigma$) limit using di-muon searches for Cases A and B, and di-tau searches for Case C. The blue shaded regions in the upper panels are excluded at 90% CL by the LHCb dark photon searches [44] and at $2\sigma$ by the ATLAS di-muon searches [45] with 139 fb$^{-1}$. The blue area in the lower panel is excluded at $2\sigma$ by the ATLAS di-tau searches [46] with 36.1 fb$^{-1}$. The orange curves correspond to the $2\sigma$ limit from CCFR [47, 48], and the black bands show the $2\sigma$ allowed regions that explain the discrepancy in the anomalous magnetic moment of the muon ($\Delta a_\mu = (29 \pm 9) \times 10^{-10}$ [49]).
The low- and high-energy probes are complementary to search for a wide range of $Z'$ masses. For $Z'$ masses above 10 GeV, the ATLAS and CMS experiments at HL-LHC have the best sensitivity regardless of the flavor structure of the model. For masses between 0.01 GeV–10 GeV, current LHCb data and future COHERENT data have the best sensitivity unless the $Z'$ couplings to the first and second generation leptons are suppressed, in which case neutrino oscillation experiments have the best sensitivity. For $Z'$ masses between about 5 MeV–20 MeV, DUNE and T2HK have the best sensitivity.

4 $\nu$SMEFT / SMNEFT

When the new physics scale is much higher than the weak scale, an EFT framework that is consistent with the SM gauge symmetries can be used above the weak scale. To parameterize scenarios where the mass of a heavy neutrino state is comparable to the EW scale but the scale of GNI is much larger than both, it is possible to extend the SM by right-handed neutrinos and build an effective field theory based on the given field content. The framework, known as $\nu$SMEFT or SMNEFT, reduces to the familiar SMEFT when heavy neutrinos are integrated out of the theory [50–52]. Thus, $\nu$SMEFT is a broader framework than SMEFT and can generate GNI at low energies. We focus on four operators:

1. $O_{NLQu}^{\alpha\beta\gamma\delta} = (\overline{N}_\alpha L_j^\beta)(Q_j^\gamma\epsilon^\delta)$,

2. $O_{NLdQ}^{\alpha\beta\gamma\delta} = (\overline{N}_\alpha L_j^\beta)\epsilon_{jk}(\overline{d}_\gamma Q_k^\delta)$,

3. $O_{NLdQ}^{\alpha\beta\gamma\delta} = (\overline{N}_\alpha \sigma_{\mu\nu} L_j^\beta)\epsilon_{jk}(\overline{d}_\gamma \sigma^{\mu\nu} Q_k^\delta)$,

4. $O_{HNe} = (i\overline{\phi}^\dagger D_\mu \phi) N \sigma^\mu e_R$,

where the fields are written in two-component spinors. $L$ and $Q$ are the left-handed lepton and quark doublet, respectively, $\phi$ is the left-handed Higgs doublet, and $N$ is the right-handed neutrino state. Here, $\sigma^{\mu\nu} = \frac{i}{2} [\sigma^\mu \sigma^\nu - \sigma^\nu \sigma^\mu]$, with $\sigma^\mu = (1, \vec{\sigma})$ and $\bar{\sigma}^\mu = (1, -\vec{\sigma})$. RG running is needed to combine the results from various energy scales and it has been calculated in Refs. [6, 53–55]. Generally there are degeneracies between $\nu$SMEFT Wilson coefficients at low-energy observables due to the running effects. High-energy measurements can break the degeneracies. Low-energy probes and high-energy colliders are complementary to probe various type of interactions as shown in Fig. 5.

If EW-scale sterile neutrinos contribute to the anomalous magnetic moments of charged leptons, then it is possible to parameterize their impact with the $\nu$SMEFT framework [7]. Notably, only one operator at dimension $d = 6$ can account for the difference between recent measurements and predictions for the muon’s anomalous magnetic moment, $\Delta a_\mu$. In particular, with the exception of operator $O_{HNe}$ above, all other operators at $d = 6$ either generate too small or too large $\Delta a_\mu$ [7]. Moreover, the measured value of $\Delta a_\mu$ is sufficiently large that the allowed band of $(C_{HNe}/\Lambda)$ and $m_N$, with realistic active-sterile mixing is accessible at
Figure 5. The 90% C.L. allowed regions in the $C_{NLdQ}$-$C_{NLQu}$ planes (upper panels) and $C_{NLdQ}'$-$C_{NLdQ}$ planes (lower panels) at 1 TeV with $\ell = e$ flavor (left) and $\ell = \mu$ flavor (right). The green lines (overlapping in the left panels) correspond to the bounds from pion decay with the third parameter set to zero to break the degeneracy. The red (blue) solid contours show current LHC searches with $L = 139 \text{ fb}^{-1}$ for the low-scale new physics LNP (high-scale new physics HNP) case. The brown dashed lines correspond to the projected bounds from the future LAr COHERENT experiment, with $C_{NLQu}$ is set to zero in the lower panels to obtain meaningful bounds. The red and blue dashed contours are the projected bounds from HL-LHC with $3 \text{ ab}^{-1}$ of data for the LNP and HNP case, respectively. The dashed purple contours in the left panels correspond to the projected bounds from LHeC with $3 \text{ ab}^{-1}$. 
Figure 6. (a) For a Wilson coefficient of unity and active-sterile mixing $|U_{\mu 4}|^2 = 10^{-4}$, the region in $(\Lambda, m_4)$ space that can account for the measured value of $\Delta a_\mu$ (green band); current exclusions due to direct searches for sterile neutrinos (dark red) and $H \to \mu^+\mu^-$ decays (dark blue) at $\sqrt{s} = 13$ TeV; the anticipated sensitivity at the HL-LHC in the same channels (light red and light blue); and exclusions due to requiring $m_4 < \Lambda$. (b) Same as (a) but for $\ell = e$ with present constraints (dark red) as well as anticipated sensitivity from $0\nu\beta\beta$ experiments (light red) and searches for $H \to e^+e^-$ at the HL-LHC. Figure adapted from Ref. [7].

For a Wilson coefficient of unity and active-sterile mixing $|U_{\mu 4}|^2 = 10^{-4}$, Fig. 6(a) shows the region in $(\Lambda, m_4)$ space that can account for the measured value of $\Delta a_\mu$ (green band); current exclusions due to direct searches for sterile neutrinos with $\mathcal{L} \approx 36 \text{ fb}^{-1}$ (dark red) \cite{59} and $H \to \mu^+\mu^-$ decays with $\mathcal{L} \approx 137 \text{ fb}^{-1}$ (dark blue) \cite{56, 57} at $\sqrt{s} = 13$ TeV; the anticipated sensitivity at the HL-LHC in the same channels (light red and light blue) \cite{58}; and exclusions due to requiring $m_4 < \Lambda$. By the end of the HL-LHC program, nearly the entire allowed parameter space can be explored at the HL-LHC \cite{7}.

A disagreement between experimental determinations of the electron’s anomalous magnetic moment using Cesium \cite{59} and Rubidium \cite{60} also exists. While inaccessible at the HL-LHC, the nEXO neutrinoless $\beta\beta$ ($0\nu\beta\beta$) decay experiment \cite{61} will be able to explore much of the allowed $(\Lambda, m_4)$ space. This is shown in Fig. 6(b), where the allowed space for $\Delta a_e$ is shown as are present constraints (dark red) as well as anticipated sensitivity from $0\nu\beta\beta$ experiments (light red) and searches for $H \to e^+e^-$ at the HL-LHC based on current exclusions \cite{62}. Figure adapted from Ref. [7].

Finally, other studies in the $\nu$SMEFT framework report sensitivity at the LHC to indi-
vidual operators at the LHC [24, 50, 51, 63–66] as well as proposed lepton colliders [67–70].

5  Executive summary

Through a few phenomenological examples, we reiterate that there is significant complementarity between low-energy experiments (such as DUNE) and high-energy collider experiments (such as the LHC) in exploring new physics associated with neutrino properties and their mass-generation mechanisms. Signals of new physics in the two energy regimes may be correlated with each other in the same underlying theory. We demonstrate the complementary nature by presenting the physics reaches for the Seesaw models of Type I, II and III, and for general neutrino interactions in an effective field theory framework, and in a $Z'$ model. It is crucially important to seek complementary signals to establish a consistent picture of the underlying physics associated with the mechanisms responsible for generating neutrino masses.

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