Variation of microphysics in wind bubbles: an alternative mechanism for explaining the rebrightenings in GRB afterglows

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ABSTRACT

Conventionally, long GRBs are thought to be caused by the core collapses of massive stars. During the lifetime of a massive star, a stellar wind bubble environment should be produced. Furthermore, the microphysics shock parameters may vary along with the evolution of the fireball. Here we investigate the variation of the microphysics shock parameters under the condition of wind bubble environment, and allow the microphysics shock parameters to be discontinuous at shocks in the ambient medium. It is found that our model can acceptably reproduce the rebrightenings observed in GRB afterglows, at least in some cases. The effects of various model parameters on rebrightenings are investigated. The rebrightenings observed in both the R-band and X-ray afterglow light curves of GRB 060206, GRB 070311 and GRB 071010A are reproduced in this model.

Key words: gamma rays: bursts — ISM: jets and outflows — stars: mass loss.

1 INTRODUCTION

Gamma-ray bursts (GRBs) are attractive astrophysics phenomena and had puzzled astronomers for about twenty-four years after their discovery in 1973 (Klebesadel et al. 1973). The discovery of long-lived, multi-band counterparts of GRBs, namely, the afterglows of GRBs, in 1997 is a watershed in GRB research (Costa et al. 1997; Van Paradijs et al. 1997; Frail et al. 1997). Soon after that, the so-called fireball model is recognized as the standard model in view of the fact that it can explain most features of GRB observations well. However, as the advance of observation techniques and the accumulation of observational data, especially after the launch of Swift satellite (Gehrels 2004), a lot of unexpected behaviours appear in GRB afterglows, such as the canonical steep-shallow-normal decay and flares in X-ray afterglows, the flattish decay phase and various rebrightenings in optical afterglows (For review, see Zhang 2007).

In fact, there are more and more rebrightenings detected in GRB afterglows, including GRB 970508 (Galama et al. 1998a), GRB 990123 (Sari & Piran 1999), GRB 021004 (Lazzati et al. 2002), GRB 030329 (Berger et al. 2003), GRB 050525A (Blustin et al. 2006), GRB 050820A (Cenko et al. 2006), GRB 050721 (Antonelli et al. 2006), GRB 060206 (Stanek et al. 2007; Liu et al. 2008), GRB 070311 (Guidorzi et al. 2007a), GRB 070311 (Guidorzi et al. 2007a), GRB 071010A (Covino et al. 2008). Many different mechanisms have been proposed to explain these rebrightenings, such as density jump (Lazzati et al. 2002; Dai & Wu 2003; Tam et al. 2005), energy injection (Huang et al. 2006), two-component jet (Huang et al. 2004, 2006; Liu et al. 2008), reverse shock (Sari & Piran 1999), reverberation of the energy input measured by prompt emission (Vestrand et al. 2006), turn-on of the external shock (Stanek et al. 2007; Molinari et al. 2007), large angle emission (Panaitean & Kumar 2007), and spectral peak of existing forward shock (Shao & Dai 2005).

Among all the mechanisms, the density jump model needs to be paid special attention to, because density jump in surrounding medium of GRBs is a very natural hypothesis. Since there are more and more examples indicating that some GRBs are associated with Type Ic supernovae (e.g. SN 1998bw/GRB980425, Galama et al. 1998b; SN2003dh/GRB030329, Price et al. 2003) and many host galaxies of GRBs are in process of active star formation (Fruchter et al. 1999; Djorgovski et al. 1998), it is believed that the progenitors of long GRBs are massive Wolf-Rayet (WR) stars (Woosley 1993). Massive stars usually produce very strong stellar wind to push the initial interstellar medium (ISM) in their neighborhood away during their lifetime. The surrounding of these GRBs should be a wind bubble following the density profile $\rho \propto r^{-2}$ rather ...
than the usual homogeneous ISM. Several authors (Castor et al. 1975; Weaver 1977; Ramirez-Riuz et al. 2001) further found that beyond some typical radius of the wind bubble, the swept-up mass is too large to be pushed by the wind. As a result, the wind materials pile up at the edge of the wind bubble to form a density jump.

Lazzati et al. (2002) proposed that a density jump can lead to a rebrightening in the afterglow. In usual case, when the observing frequency is between the peak frequency ($\nu_0$) and the cooling frequency ($\nu_c$), the amplitude of the rebrightening should be proportional to the square root of the density contrast. However, if the density contrast is too high, the rebrightening will be weakened, since $\nu_c$ will decrease and become less than the observing frequency. In the more detailed numerical simulations by Huang et al. (2007), no obvious rebrightenings can be discriminated when the density jump amplitude is set to 100, which suggests that the simple density jump model is not an ideal mechanism to produce the rebrightenings. In the recent studies by Nakar & Granot (2006) and van Eerten et al. (2009), a full treatment of the transient features at the jump moment, even including the variation could resolve these problems.

We use the convenient equations developed by Huang et al. (1999, 2000a, 2000b, 2003) to describe the dynamics and radiation process of the ejecta. The evolution of the bulk Lorentz factor $\gamma$, the shock radius $R$, and the swept-up medium mass $m$, is described by three differential equations,

$$\frac{d\gamma}{dm} = -\frac{\gamma^2 - 1}{M_{ej} + em + 2(1 - \epsilon)\gamma m},$$

$$\frac{dR}{dt} = \beta c\gamma (\gamma + \sqrt{\gamma^2 - 1}),$$

$$\frac{dm}{dR} = 2\pi R^2 (1 - \cos\theta) nm_p,$$

where $m_p$ is proton mass, $M_{ej}$ is the initial mass of the outflow, $\theta$ is the half opening angle of the jet, $n$ is the number density of the environment, $\beta = \sqrt{\gamma^2 - 1}/\gamma$, and $\gamma \approx (4\gamma + 1)/(3\gamma)$ is the adiabatic index (Dai, Huang, & Lu 1999). $\epsilon$ is the radiative efficiency, which equals 1 for a highly radiative case, and equals 0 in the adiabatic case. We ignore the sideways expansion of the jet in our model, because many numerical simulations indicate that it is a very slow process (Granot et al. 2001; Cannizzo, Gehrels & Vichniac 2004; Zhang & MacFadyen 2009). We consider that the afterglow flux mainly comes from the synchrotron radiation of the shocked relativistic electrons.

Since the speed of light ($c$) is finite, photons received by the observer at a particular time $t$ are not radiated simultaneously, but come from a distorted ellipsoid determined by

$$t = \int_0^\infty \frac{1 - \beta \cos\Theta}{\beta c} dR \equiv \text{const},$$

within the jet boundaries, where $\Theta$ is the angle between the velocity of emitting material and the line of sight. This is the so-called EATS effect. We integrate over the EATS to obtain an accurate observed flux in our simulations (see Huang et al. 2007 for more details).

2.2 Environment

Massive stars usually produce very strong stellar wind during their lifetime. This stellar wind interacts with the initial ISM and forms two shocks: a reverse shock propagates back into the stellar wind and a forward shock that propagates into the ISM. The resulting surrounding medium is broken into four regions (Castor et al. 1975; Weaver 1977; Ramirez-Riuz et al. 2005; Pe`e and Wijers 2006) as shown in Figure 1. They are (from inside to outside): (1) the unshocked stellar wind; (2) the shocked stellar wind; (3) the shocked ISM; (4) the unshocked ISM.

Region (1) is a stellar wind bubble. The number density of this region is given by

$$n_1 = \frac{M}{4\pi m_p v_w r^2} \propto r^{-2},$$

where $M$ is the mass loss rate of the progenitor, $v_w$ is the launching speed of the stellar wind and $r$ is the radial distance from the central star. We fix $v_w$ as $10^6$ cm s$^{-1}$ and only vary $M$ in our simulations, since the density profile of the environment only depends on the ratio $M/v_w$.

As the stellar wind expands, the swept-up mass of the ISM increases and is finally comparable to the mass in the
wind at a radius $r_{\text{wind}}$, which is determined by (Ramirez-Ruiz et al. 2001, 2005)

$$r_{\text{wind}} = 1.6 \times 10^{18} \frac{M_{\text{w}}^{3/10} n_{\text{ISM}}^{3/10} v_{w,8}^{1/10} r_{*}}{\tau_{*}} \text{ cm},$$

(6)

where $n_{\text{ISM}}$ is the initial density of the homogeneous ISM, in units of $10^3$ cm$^{-3}$, and $\tau_{*}$ is the life time of the WR phase of the star, in units of $10^6$ yr. Beyond this radius, in region (2), the swept-up mass is too large to be pushed away by the wind. The material piles up in this region to form a density jump. Because of the effect of the reverse wind shock, the material is hot in this region. The density is approximately constant and equals to $n_2 = 4n_1(r_{\text{wind}})$, where $n_1(r_{\text{wind}})$ is the density in region (1) at the radius of $r = r_{\text{wind}}$.

As shown by Castor et al. (1975), the boundary between Region (2) and Region (3) is at the radius of

$$r_{2-3} = 1.6 \times 10^{19} \frac{M_{\text{w}}^{1/5} n_{\text{ISM}}^{1/5} v_{w,8}^{2/5} r_{*}}{\tau_{*}} \text{ cm}.$$

(7)

Region (3) is a thin, dense shell containing most of the swept-up ISM. Its width is only about $r_{2-3}/12$ and the density in this region is about $4n_{\text{ISM}}$. Here $n_{\text{ISM}}$ is also the density in region (4).

We use the density profile introduced above as the environment surrounding GRBs in this paper. As discussed by Pe’er and Wijers (2006), for a GRB event, the blast wave can not reach Region (3) in the relativistic phase. Our numerical results also prove that the fireball is in Region (1) and Region (2) during typical observable time. So we only use Region (1) and Region (2) as the environment in our work. For simplicity, we take $r_{\text{wind}}$ as a free parameter in our calculations, so that we do not need to consider the detailed values of $v_0$ and $\tau_*$.

Unfortunately, the simple density jump model alone is difficult to explain the rebrightenings in GRB afterglows (Huang et al. 2006, 2007; Nakar & Granot 2007). Moreover, the early optical and/or X-ray afterglow light curves of some GRBs are flatter than the prediction of a normal fireball in a simple wind environment. So we need to consider other effects. Varying microphysics shock parameters should be a possible solution.

\section{2.3 Microphysics parameters}

In the standard afterglow model, it is usually assumed that the microphysical parameters are constant throughout the evolution of the fireball. However, the actual microphysical processes in the relativistic shocks, for example, the energy transfer from protons to electrons and magnetic fields, are still not clearly known. It is possible that the microphysical parameters are variational. In fact, the variation of the microphysics parameters during the evolution of the fireball has been considered in many previous studies (Rossi & Rees 2003; Ioka et al. 2006; Fan & Piran 2006; Panaitescu et al. 2006; Granot, Königl & Piran 2006). Fan & Piran (2006) and Panaitescu et al. (2006) have engaged the assumption that the equipartition factors $\xi_e$ and $\xi_B$ are functions of $\gamma$ to explain the shallow decay phase in some X-ray afterglows. Here we will use a similar idea to investigate the observed rebrightenings in GRB afterglows.

In our model, the circum-burst environment is divided into two parts, i.e. Region (1) and Region (2). The material in Region (1) is the unshocked stellar wind thrown by the mass star. In Region (2) the material consists of the shocked stellar wind mixed with a small fraction of the swept-up ISM. It is hot because of the effect of the reverse wind shock (Castor et al. 1975; Weaver 1977; Ramirez-Ruiz et al. 2005; Pe’er and Wijers 2006). We can imagine that the physical condition, such as the strength of the magnetic field, the temperature and density of the material, could be different between these two regions, so the evolution of microphysics parameters may also be different accordingly. In our study, we use different parameters for these two regions. We assume that

$$\xi_e = \xi_{e,0} \gamma^{-\alpha_1},$$

(8)

$$\xi_B = \xi_{B,0} \gamma^{-\alpha_1}$$

(9)

in Region (1), and

$$\xi_e = \xi_{e,0} \gamma^{-\alpha_2},$$

(10)

$$\xi_B = \xi_{B,0} \gamma^{-\alpha_2}$$

(11)

in Region (2).

\section{3 NUMERICAL RESULTS}

In this section, we present our numerical results to show the effects of various physical parameters on the R-band light curves, using the model described in §2. For convenience, we first define a set of “standard” parameters, as shown in the second column of Table 1.

Figure 2 illustrates the effect of the parameter $\theta$ on the R-band light curves. The solid line corresponds to the “standard” parameters. The dashed line corresponds to $\theta = 0.3$ rad and the dotted line corresponds to $\theta = 0.03$ rad. We can see that when the change of microphysics parameters is considered, an obvious rebrightening appears. Interestingly, when $\theta$ is larger, the duration of the rebrightening becomes longer. This is not difficult to understand. The afterglow brightness is dominated by the high latitude emission, so that the EATS shows a ring-like pattern. As a result, the brightness will be kept on a relatively higher level after the
density jump moment, to form a flat phase. When $\theta_0$ becomes larger, the time delay of the photons from the edge of the outflow also becomes larger. So the flat phase is longer.

Environment is an important factor that affects the evolution of GRB afterglows. As mentioned before, the character of wind environment is mainly determined by the ratio $\dot{M}/v_w$. We fix $v_w$ as $10^8$ cm s$^{-1}$ and only vary $\dot{M}$ here to investigate the effect of the parameter $\dot{M}$ on the R-band light curves. The results are shown in Figure 3. The solid line corresponds to the “standard” parameters. The dashed line corresponds to $\dot{M} = 1.0 \times 10^{-6}$ M$_\odot$/yr and the dotted line corresponds to $\dot{M} = 1.0 \times 10^{-7}$ M$_\odot$/yr.

The parameter $r_{\text{wind}}$ is another factor to describe the character of the environment. The effect of $r_{\text{wind}}$ on the R-band light curve is illustrated in Figure 4. The solid line corresponds to $r_{\text{wind}} = 5.0 \times 10^{15}$ cm and the dotted line corresponds to $r_{\text{wind}} = 5.0 \times 10^{17}$ cm. We can see that the rebrightening appears earlier when $r_{\text{wind}}$ is smaller, because $r_{\text{wind}}$ determines the position of the density jump.

The effect of the parameter $\alpha_1$ on the R-band light curve is shown in Figure 5. The solid line corresponds to the “standard” parameters. The dashed line corresponds to $\alpha_1 = 1.7$ and the dotted line corresponds to $\alpha_1 = 1.3$. It is obvious that a larger $\alpha_1$ makes the flux before the rebrightening lower. This is not difficult to understand. With the increase of $\alpha_1$, the values of $\xi_e$ and $\xi_B$ before the rebrightening become smaller. This suppresses the radiation flux at early time.

The effect of the parameter $\alpha_2$ on the R-band light curve is illustrated in Figure 6. The solid line corresponds to the “standard” parameters. The dashed line corresponds to $\alpha_2 = 1.5$ and the dotted line corresponds to $\alpha_2 = 1.1$. As expected, the effect of $\alpha_2$ is similar to that of $\alpha_1$ for the same reason.

### Table 1. Modeling Parameters

| Parameters       | Standard | GRB 060206 | GRB 070311 | GRB 071010A |
|------------------|----------|------------|------------|-------------|
| $z$              | 1.0      | 4.045      | 1.0        | 0.98        |
| $E_0$ (ergs)     | $1.0 \times 10^{53}$ | $9.0 \times 10^{52}$ | $8.0 \times 10^{51}$ | $1.3 \times 10^{52}$ |
| $\theta_0$ (rad) | 0.1      | 0.06       | 0.08       | 0.11        |
| $\dot{M}$ (M$_\odot$/yr) | $1.0 \times 10^{-6}$ | $2.0 \times 10^{-5}$ | $6.0 \times 10^{-6}$ | $4.0 \times 10^{-5}$ |
| $r_{\text{wind}}$ (cm) | $1.0 \times 10^{18}$ | $3.0 \times 10^{16}$ | $2.0 \times 10^{17}$ | $5.1 \times 10^{16}$ |
| $p$              | 2.5      | 2.2        | 2.3        | 2.1         |
| $\xi_e,0$        | 0.1      | 0.3        | 0.3        | 0.3         |
| $\xi_B,0$        | 0.01     | 0.03       | 0.03       | 0.03        |
| $\alpha_1$       | 1.5      | 1.2        | 0.9        | 1.5         |
| $\alpha_2$       | 1.3      | 0.6        | 0.0        | 0.6         |

Figure 2. The effect of the parameter $\theta_0$ on the R-band light curve. The solid line corresponds to the standard parameters. The dashed line corresponds to $\theta_0 = 0.3$ rad and the dotted line corresponds to $\theta_0 = 0.03$ rad.

Figure 3. The effect of the parameter $\dot{M}$ on the R-band light curve. The solid line corresponds to the “standard” parameters. The dashed line corresponds to $\dot{M} = 1.0 \times 10^{-5}$ M$_\odot$/yr and the dotted line corresponds to $\dot{M} = 1.0 \times 10^{-7}$ M$_\odot$/yr.
4 COMPARISON WITH OBSERVATIONS

In this section we select three GRBs with obvious rebrightenings in both optical and X-ray bands, i.e. GRB 060206, GRB 070311 and GRB 071010A, and reproduce their R-band and X-ray afterglow light curves numerically, using the model described in §2.

4.1 GRB 060206

GRB 060206 was detected at 04:46:53 UT on Feb. 6 by the Burst Alert Telescope (BAT) onboard the Swift satellite (Morris et al. 2006). The temporal profile of the BAT light curve shows a single peak, with a total fluence of $8.4 \pm 0.4 \times 10^{-7}$ erg cm$^{-2}$ in the 15-350 keV band (Morris et al. 2006; Palmer et al. 2006). The total duration of the burst is $T_{90} = 7 \pm 2$ s, suggesting that it is a long-duration GRB (Palmer et al. 2006).

The UVOT telescope onboard the Swift satellite first observed the optical afterglow of GRB 060206 and found it located at the position of $\alpha = 13^h31^m43^s.416$, $\delta = +35^\circ03'03''$ (J2000.0; Boyd et al. 2006), corresponding to the Galactic extinction of $A_R = 0.033$ mag (Schlegel, Finkbeiner & Davis 1998). After that, a number of telescopes made detailed follow up observations, such as the 2-m robotic Liverpool Telescope (Monfardini et al. 2006), the Rapid Telescopes for Optical Response (RAPTOR; Woźniak et al. 2006) and the MDM telescope (Stanek et al. 2007). From the calibrated ALFOSC spectrum of the afterglow, Fynbo et al. (2006) determined the redshift of GRB 060206 as $z = 4.045$. X-ray afterglow was also detected by XRT on Swift at 58 s after the trigger (Morris et al. 2006).

There are significant rebrightenings in both the optical and X-ray afterglows of GRB 060206 at about 3000 s after the burst. Liu et al. (2008) suggested that the rebrightening comes from a jet-like ejecta with a larger viewing angle, which is produced by the central engine.

Here we try to use our model described in §2 to reproduce the rebrightenings in both R-band and X-ray light curves of GRB 060206. Our best-fit physical parameters are presented in Table 1, and our modeling curves are illustrated in Figure 7. The observed R-band data are taken from Monfardini et al. (2006), Woźniak et al. 2006 and Stanek et al. (2007), and the X-ray data are taken from the Swift XRT light curve repository (Evans et al. 2007). We can see in Figure 7 that our model can generally reproduce the light curves well. Note that at the late stage, the observed X-ray light curve is obviously too flat as compared with our theoretical result. This may be due to the contamination from a nearby source, as already mentioned by Stanek et al. (2007).
4.2 GRB 070311

GRB 070311 occurred at 01:52:50 UT on 2007 March 11 and was detected by the INTEGRAL/IBAS in IBIS/ISGRI data. The duration of the γ-ray prompt emission is about 50 s in the 20-200 keV band, with the peak flux of 0.9 photons cm$^{-2}$ s$^{-1}$ (1 s integration time) and the total fluence of $2 \times 10^{-6}$ erg cm$^{-2}$ (Mereghetti et al. 2007).

The afterglow of GRB 070311 was first discovered by the Rapid Eye Mount (REM) telescope at 55 s after the burst. A bright fading source was found at $\alpha = 03^h50^m08^s.21$, $\delta = +03^\circ22^\prime30^\prime\prime.3$ (J2000.0; Covino et al. 2007). This location has a low Galactic latitude ($l = 202^\circ.766, b = -11^\circ.998$ in Galactic coordinates), so the Galactic extinction is as much as $A_R = 2.038$ mag (Schlegel, Finkbeiner & Davis 1998). X-ray afterglow was also found by the observations of XRT on Swift at about 7000 s after the trigger (Guidorzi et al., 2007b).

The optical afterglow of GRB 070311 has complex structures. Besides a normal power law decay, there are two fast rise exponential decay (FRED) shaped pulses peaking around 80 and 140 s after the peak of the GRB and possibly accompanied by the tail of prompt γ-ray emission (Guidorzi et al. 2007a). Another structure, which is the most attractive feature, is a significant late rebrightening between 3 and 4 days after the trigger in both optical and X-ray bands (Guidorzi et al. 2007a). Guidorzi et al. (2007a) have used a power law function plus a FRED shaped pulse to fit the afterglows in both R and X-ray bands. More physically, they suggested that the late afterglow rebrightening of GRB 070311 can come from a refreshed shock. Additionally, they argued that the density jump in the surrounding medium can be the origin of the rebrightening too, but less appealing.

Here we use our model described in §2 to reproduce the late rebrightenings in both R-band and X-ray light curves of GRB 070311. We take the observed R-band data from Guidorzi et al. (2007a; for REM data) and GCN circulars (Cenko 2007; Dai et al. 2007; Garnavich et al. 2007; Halpern & Armstrong 2007a,b,c,d; Jelíněk, Kubánek & Prouza 2007; Kann 2007; Wren et al. 2007), and the X-ray data from the Swift XRT light curve repository (Evans et al. 2007). All optical data points have been corrected for the Galactic extinction (Schlegel, Finkbeiner & Davis 1998).

4.3 GRB 071010A

GRB 071010A triggered the Swift satellite at 03:41:12 UT on 2007 Oct. 10 (Moretti et al. 2007). It is a traditional long GRB with the burst duration of $T_{90} = 6 \pm 1$s. The total fluence of the burst is about $2 \times 10^{-7}$ erg cm$^{-2}$ (Kr"{i}mm et al. 2007).

TAROT telescope identified the optical afterglow of GRB 071010A firstly, only 124 s after the trigger (Klotz, Boer & Atteia, 2007). Bloom et al. (2007) further found that the position of the burst was $\alpha = 19^h12^m14^s.624$, $\delta = -32^\circ24^\prime07^\prime.16$ (J2000.0), corresponding to the Galactic extinction of $A_R = 0.263$ mag (Schlegel, Finkbeiner & Davis 1998). Spectral observations were done subsequently by Keck and the analysis of the Mg II and Fe II lines gave the redshift of the burst as $z = 0.98$ (Prochaska et al. 2007). X-ray data were also acquired by XRT observations on Swift (Guidorzi et al. 2007b), but no radio afterglow was detected at 8.46 GHz until almost 2 days after the burst (Chandra & Frail 2007).

The most interesting feature of the afterglows of GRB 071010A is the appearance of a sharp rebrightening at about...
0.6 days after the GRB, clearly seen in both optical and X-ray bands. Covino et al. (2008) have used a Beuermann et al. (1999) function, and a simple step function for the steepening after the rebrightening was interpreted as a rebrightening due to an injection of abundant energy, which was comparable to the initial energy in the fireball. The steepening after the rebrightening was interpreted as a jet break at around 1 day after the burst.

We try to use our model introduced in §2 to reproduce the R-band and X-ray light curves of GRB 071010A. In our modeling, the observed R-band data are taken from Covino et al. (2008), and the X-ray data are taken from the Swift XRT light curve repository (Evans et al. 2007). Our best fitting physical parameters are presented in Table 1, and our model can reproduce the rebrightenings and flattish decay in GRB afterglows successfully. We have shown that the observed rebrightenings in both the optical and X-ray afterglow light curves of GRB 060206, GRB 070311 and GRB 071010A can be well explained by our model.

In our study, we combine the wind bubble environments and the change of microphysics shock parameters together. Comparing with the standard fireball model, our model has three more parameters (i.e. $r_{\text{wind}}$, $\alpha_1$ and $\alpha_2$). We find that this model can produce the observed rebrightenings and flattish decay in GRB afterglows successfully. We have shown that the observed rebrightenings in both the optical and X-ray afterglow light curves of GRB 060206, GRB 070311 and GRB 071010A can be well explained by our model.

We have also investigated the effects of various parameters on the light curves numerically. We can imagine that if the stellar wind produced by the progenitor is very strong, or the launching speed of the stellar wind $v_w$ is small, or the value of $r_{\text{wind}}$ is large enough, there will be no rebrightening within the usual observation time. So, basically the wind bubble environment can also give birth to a steadily decaying afterglow that shows no rebrightening.

In our work, we neglect the effect of the reverse shock. According to the study by Dai & Lu (2002), when an ultra-relativistic blast wave interacts with a density jump medium, the resulting reverse shock is relativistic only if the amplitude of the density jump is much larger than 21. In our model, the amplitude of the density jump is only 4, so the corresponding reverse shock is Newtonian. The emission from the Newtonian reverse shock is very weak, and can be omitted. Moreover, although we use an abrupt density jump, the actual increase of density may be gradual. In this situation, the emission from the reverse shock will even be much weaker.

Currently, a complete understanding of the microphysical processes in the relativistic shocks is still lacking. Using the derived microphysical parameters from GRB modeling, people may be able to get some constraints on the shock physics. The derived parameter values of $M$ and $n_{\text{ISM}}$ are also very important. They are closely related to the evolution and the environment of the massive star. They may give some hints on the characters of the progenitor, such as the initial main-sequence mass and the metallicity. So, from the modeling parameters, we can also obtain some useful information about GRB origin.

5 DISCUSSION AND CONCLUSION

In the standard fireball model, it is assumed that the circum-burst medium density is constant or following a single $\rho \propto r^{-2}$ law. The microphysics shock parameters are also usually assumed invariant during the evolution of the fireball. These models can basically explaining many pre-Swift GRB afterglows, whose spectrum and light curves can be approximated as broken power-law functions (Panaitescu & Kumar 2001a, 2001b; Yost et al. 2003). The launch of Swift satellite (Gehrels 2004) makes it possible to observe early afterglows of many GRBs in the first few hours after the trigger. Many remarkable and unexpected features are found, such as marked rebrightenings and the flattish decay phase in early GRB afterglows.

In fact, the standard fireball model is obviously too simplified. If long GRBs indeed originate from the death of massive stars, the environment of GRBs should have complex structures rather than have a constant or single power law profile. Some analytical (Castor et al. 1975; Weaver 1977; Ramirez-Ruiz et al. 2005; Pe’er and Wijers 2006) and numerical (Ramirez-Ruiz et al. 2001) studies suggest that the circumburst density profile should be a wind bubble, associated with a few density jumps. On the other hand, the microphysics parameters, such as $\xi_e$ and $\xi_B$, may vary during the evolution of the fireball (Rossi & Rees 2003; Ioka et al. 2006; Fan & Piran 2006; Panaitescu et al. 2006;Granot, Königl & Piran 2006). Actually, the fast decrease of the cooling frequency $\nu_c$ in some GRBs suggests that $\xi_B$ may be evolving (Panaitescu et al. 2006). Some previous studies also suggest that $\xi_e$ and $\xi_B$ may be different for the forward shock and the reverse shock (Fan et al. 2002; Wei, Yan & Fan 2006), and may also be different for Region (1) and Region (2) (Gebre et al. 2007; Kamble, Resmi & Misra 2007). So, $\xi_e$ and $\xi_B$ may depend on the strength of the shock and the environment.
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