Pausing transplants in the face of a global pandemic: Patient survival implications

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Abstract

The coronavirus disease 2019 (COVID-19) pandemic has disrupted normal operating procedures at transplant centers. With the possibility that COVID-19 infection carries an overall 4% mortality rate and potentially a 24% mortality rate among the immunocompromised transplant recipients, many transplant centers considered the possibility of slowing down and even potentially pausing all transplants. Many proposals regarding the need for pausing organ transplants exist; however, much remains unknown. Whereas the impact of the COVID-19 pandemic on the overall healthcare system is unknown, the potential impact of pausing organ transplants over a period can be estimated. This study presents a model for evaluating the impact of pausing liver transplants over a spectrum of model for end-stage liver disease-sodium (MELD-Na) scores. Our model accounts for two potential risks of a pause: (1) the waitlist mortality of all patients who do not receive liver transplants during the pause period, and (2) the impact of a longer waiting list due to the pause of liver transplants and the continuous accrual of new patients. Using over 12 years of liver transplant data from the United Network for Organ Sharing and a system of differential equations, we estimate the threshold probability above which a decision maker should pause liver transplants to reduce the loss of patient life months. We also compare different pause policies to illustrate the value of patient-specific and center-specific approaches. Finally, we analyze how capacity constraints affect the loss of patient life months and the length of the waiting list. The results of this study are useful to decision makers in deciding whether and how to pause organ transplants during a pandemic. The results are also useful to patients (and their care providers) who are waiting for organ transplants.

KEYWORDS
COVID-19 pandemic, healthcare operations, organ transplant

1 INTRODUCTION

The triumphs of modern medicine have rendered the promise of solid organ transplants—a field of medicine that draws from advances in surgery, medicine, anesthesia, critical care, immunology, and blood medicine, saving more than 26.4 million life months in the United States (Rana et al., 2015). These advances have allowed solid organ transplants to become the standard of care for many patients suffering from end-stage kidney or liver diseases. In 2019, a total of 23,401 kidney transplants and 8896 liver transplants were performed in the United States.¹ However, the coronavirus disease 2019 (COVID-19) pandemic has challenged all aspects of our modern society, including the role of solid organ transplants. In response, transplant centers propose policies that range from “business as usual” to a complete shutdown of all transplants (Ahn et al., 2020; Boyarsky et al., 2020; Kumar et al., 2020). The Centers for Medicare and Medicaid...
The second question considers the heterogeneity across patients by analyzing which categories of patients should be paused (i.e., patient-specific). Given the risk of a pandemic and the capacity of transplant centers, the possibility exists that some patients should be paused for organ transplants and others should not. For example, in the setting of liver transplants, patients with high scores from the model for end-stage liver disease (MELD) cannot be paused for liver transplants, because these patients can survive only a few days without organ transplants. Recognizing the differences in patients’ condition, Kumar et al. (2020) propose a phased approach that pauses liver transplants for patients with MELD scores below 25 and 30 when a center needs to reduce its surgical capacity by 50% and 75%, respectively. Similarly, Syed et al. (2020) propose pausing liver transplants for patients with MELD scores below 15, 20, and 30 when the severity of resource shortage is “mild,” “moderate,” and “severe,” respectively. However, these studies are perspective articles that do not have rigorous analyses to support their proposals. We fill the gap in the literature and address the second question by developing an analytical approach to identify the categories of patients whose organ transplants should be paused.

The third question considers the heterogeneity across centers by analyzing which centers should pause organ transplants (i.e., center-specific). Because the severity of the pandemic varies across different areas, the possibility exists that some centers should pause organ transplants and others should not. For example, as of December 1, 2020, the number of active COVID-19 cases per 1000 people was 45 in North Dakota and 3.25 in Vermont. Because an increase in the number of COVID-19 cases increases the risk of organ transplants, centers in North Dakota might need to pause organ transplants more than those in Vermont. To address the third question, we compare two scenarios: (1) A decision maker uses country-level data to make a nation-guidance recommendation to all centers and (2) a decision maker uses center-level data to make center-specific recommendations. Intuitively, a center-specific policy is superior to a nation-guidance policy for a center, because the former considers the situation of the center. However, how much a center-specific policy is better than a nation-guidance policy is what we address in this study.

Whereas the first three questions focus on the direct impact of the pandemic (i.e., the probability of mortality due to the pandemic), the fourth question focuses on the indirect impact of the pandemic by incorporating capacity constraints into our model. Besides preventing risk exposure of recipients to the virus after transplants, centers may have to direct scarce healthcare resources toward the care of COVID-19 patients. As a result, the capacity or throughput of centers may be reduced. For example, as of December 1, 2020, the number of ventilators in shortage was 1073 in Texas and three in Vermont. The lack of healthcare resources such as ventilators undoubtedly affects the surgical capacity of transplant centers. To analyze the impact of capacity constraints, we perform sensitivity analyses by considering scenarios with different capacity constraints. The results are useful to
policymakers in understanding the impact of capacity constraints on patient outcomes.

We make three contributions to the existing literature. First, by using a system of differential equations to capture the dynamics of a waiting list and analyzing the costs and benefits of pausing organ transplants during a pandemic, we explicitly calculate the threshold probability above which a decision maker should pause organ transplants. Second, we compare complete shutdown and tiered shutdown policies to illustrate the value of a patient-specific approach and compare national and center-specific policies to illustrate the value of a center-specific approach. Third, we analyze how capacity constraints affect the loss of patient life months and the length of the waiting list. The results of this study are useful to decision makers in deciding whether and how to pause organ transplants during a pandemic. The results are also useful to patients (and their care providers) who are waiting for organ transplants.

2 LITERATURE REVIEW

In the medical literature, a growing number of studies estimate the impact of COVID-19 on the mortality of organ transplant recipients. For example, Pereira et al. (2020) study 90 patients who received organ transplants at two New York transplant centers and were subsequently infected with COVID-19 during the first three weeks (i.e., between March 13, 2020, and April 3, 2020) of the outbreak in New York City. The authors find the probability of mortality due to COVID-19 is 18% among infected recipients and 24% among hospitalized recipients. In another multicenter study, Kates et al. (2021) study 482 patients who received organ transplants at over 50 transplant centers and were subsequently infected with COVID-19 between March 1, 2020, and April 15, 2020. The authors find 20.5% of the hospitalized recipients died within 28 days after COVID-19 infections. The authors also find old age, congestive heart failure, chronic lung disease, obesity, and abnormal chest imaging significantly increase the probability of mortality.

The increased risk due to COVID-19 raises an important question to both patients and their care providers about whether to pause organ transplants. Kumar et al. (2020) are among the first to provide a personal viewpoint on the impact of COVID-19 on organ transplants. By comparing the practices from different countries, the authors suggest mitigation strategies such as donor screening, resource planning, and a phased approach to new transplant activities. This study has two main strengths. First, the authors of this study are from different countries such as Canada, Italy, Japan, Korea, Spain, and Switzerland. Their collective experience is valuable to the transplant community, especially those that do not have a large enough sample size, to analyze the impact of COVID-19 on organ transplants. Second, the study discusses various types of organ transplants such as kidney, liver, heart, and lung transplants. The results are useful to hospital managers and policymakers in implementing organ-specific policies, because the impact of COVID-19 and medical urgency differ across different types of organ transplants. The main caveat of this study is that it is a perspective article without empirical data or theoretical models.

Massie et al. (2020) conduct simulation studies from patients’ perspective to analyze the costs and benefits of organ transplants during the COVID-19 pandemic. More specifically, the authors first analyze waitlist and posttransplant mortalities using Poisson regressions. The authors then compare transplant and nontransplant outcomes using a Markov decision model. Then, the authors use their estimated benefits of organ transplants during the pandemic as outcomes and classify patients into different groups using the classification and regression trees. Finally, the authors identify the relative importance of different patient characteristics and epidemic parameters using a random forest. Similar to Massie et al. (2020), Vinson et al. (2021) use a Markov model to analyze the impact of discarding deceased donor organs and find that, although the life expectancy of both patients on the waiting list and those receiving organ transplants decreases as the pandemic situation worsens, the benefit of organ transplants outweighs the risk of infection.

Our study differs from these studies in four main ways. First, these studies analyze the impact of COVID-19 on organ transplants from patients’ perspective. By contrast, we study the impact from decision makers’ perspective and analyze whether transplant centers should pause organ transplants, and if so, which categories of patients should be paused. Second, these studies do not consider how a patient’s health condition changes on the waiting list and how a patient’s probability of receiving an organ transplant depends on other patients on the same waiting list. By contrast, we use model for end-stage liver disease-sodium (MELD-Na) scores to model how the condition of a patient changes over time and a system of differential equations to model how the probability of receiving an organ transplant depends on the size of the waiting list. Third, whereas these studies do not account for local resource availability, we consider capacity constraints and analyze how these constraints affect patient outcomes. Finally, whereas these studies analyze only the costs and benefits to patients of pausing organ transplants, we compare different pause policies and illustrate the value of patient-specific and center-specific approaches to both patients and healthcare providers.

In the operations management literature, Arıkan et al. (2018) study the effects of organ quality, median waiting time for a transplant, and competition among transplant centers on the intent to procure organs. The authors find the intent increases with organ quality, median waiting time for a transplant, and competition among transplant centers. In particular, the authors find lower quality organs are more likely to be procured in a donation service area (DSA) with longer waiting times. Using a counterfactual study, the authors show sharing the bottom 15% quality kidneys increases the intent to procure organs. Arora and Subramanian (2019) develop a game-theoretic model to analyze how the decisions of the organ procurement organization (OPO) and the hospital affect
their respective payoffs and societal outcomes. The authors identify possible misalignments in the objectives of the social planner, the OPO, and the hospital, especially when the quality of recovered organs is heterogeneous. The authors recommend contracts that can better align the objectives without harming the OPO and the hospital when the operating room utilization is sufficiently high or low. Similarly, our study considers a hospital’s operational decisions concerning organ transplants that impact patient and societal outcomes. However, we study these decisions under a novel and complex setting of the COVID-19 pandemic.

In a recent study, Anderson et al. (2020) create a computer simulation model to analyze the impact of suspending elective surgeries on the flow of patients in a midsize hospital. The authors find the number of patients waiting for surgeries triples compared with pre-COVID-19 levels, and returning surgical rates to pre-COVID-19 levels will take 5 months if the hospital can double its surgical capacity in the short term. The authors make several recommendations to ramp up capacity for serving the pent-up demand: (1) allowing surgical staff to work overtime, (2) reactivating furloughed personnel, (3) hiring temporary workforce, (4) diverting to ambulatory surgery centers, and (5) triaging.

Our study differs from Anderson et al. (2020) in three main ways. First, from the perspective of the clinical setting, we study whether transplant centers should pause organ transplants, whereas Anderson et al. (2020) study the impact of suspending elective surgeries. Second, from the perspective of analytical methods, we use a system of differential equations to capture the dynamics of a waiting list, whereas Anderson et al. (2020) use a computer simulation model to analyze the flow of patients. Third, from the perspective of managerial insights, we compare different pause policies to reduce the loss of patient life months, whereas Anderson et al. (2020) study how much capacity increase is needed to serve the pent-up demand.

3 Mathematical Models and Pause Policies

To analyze whether a decision maker should pause organ transplants during a pandemic, we need to compare the loss of patient life months due to delays of organ transplants in the case of a pause with the loss of patient life months due to infections in the case of no pause. In this section, we first introduce a system of differential equations to capture the dynamics of a waiting list for organ transplants. We then describe how to calculate the loss of patient life months with and without pausing organ transplants. Then, we introduce different pause policies for decision makers to consider. Finally, we describe how to find the optimal pause policy and calculate the threshold probability above which a decision maker should pause organ transplants. Note that the analyses in this section are from the providers’ perspective. We calculate the threshold probability from the patients’ perspective to guide the decision of accepting or declining an organ offer in Appendix A of the Supporting Information for comparison purposes.

3.1 Differential equations

We denote by $M$ the number of patient categories (e.g., different MELD-Na scores). As an example, if patients can be divided into seven categories, we have $M = 7$. We denote by $P_m(t)$ the number of category $m$ patients on the waiting list at time $t$, where $m = 1, \ldots, M$. A smaller value of $m$ indicates a healthier category of patients (e.g., those with lower MELD-Na scores). Note the number of patients in a category changes over time, because new patients are added to the waiting list and existing patients are removed from the waiting list due to organ transplants, deaths, or inactivations. We denote the rates of patient arrival and organ transplant by $b_m$ and $r_m$, respectively. Table 1 summarizes the key parameters, their descriptions, and whether these parameters are used in the model and/or estimated empirically from the data.

To derive a system of differential equations that capture the change in $P_m(t)$, we denote by $dt$ a small change in time, during which the rates of patient arrival and organ transplant remain the same. During the time interval $dt$, the number of category $m$ patients added to the waiting list is $b_m dt$, the number of patients who receive organ transplants is $r_m dt$, the number of patients who die on the waiting list is $h_m P_m(t) dt$, and the number of patients who become inactive is $k_m P_m(t) dt$. Note the number of patients who die on the waiting list is a function of $P_m(t)$, because the number of waitlist deaths is proportional to the number of patients on the waiting list. However, the number of patients who receive organ transplants is not a function of $P_m(t)$, because the availability of organ donors does not depend on the number of patients on the waiting list.

We denote by $d_{mn}$ the rate of a patient transitioning from category $m$ to category $n$ (e.g., a patient’s health condition deteriorates). During the time interval $dt$, the number of patients transitioning to category $m$ from the other categories is $\sum_{n \neq m} d_{mn} P_n(t) dt$ and the number of patients transitioning from category $m$ to the other categories is $\sum_{n \neq m} d_{nm} P_m(t) dt$. Therefore, during the time interval $dt$, the change in the number of category $m$ patients equals

$$dP_m(t) = b_m dt + \sum_{n \neq m} d_{mn} P_n(t) dt - r_m dt - h_m P_m(t) dt - k_m P_m(t) dt - \sum_{n \neq m} d_{nm} P_m(t) dt,$$

where the first two terms indicate the number of patients added to category $m$ and the last four terms indicate the number of patients removed from category $m$. 

$$\sum_{n \neq m} d_{mn} P_n(t) dt$$

$$\sum_{n \neq m} d_{nm} P_m(t) dt$$
Taking derivative with respect to \( dt \), we have

\[
\frac{dP_m(t)}{dt} = b_m + \sum_{n \neq m} d_{mn} P_n(t) - r_m - h_m P_m(t) - k_m P_m(t) - \sum_{n \neq m} d_{mn} P_m(t), \quad m = 1, \ldots, M. \tag{2}
\]

Observing that the number of patients in each category remains almost the same (i.e., in a steady state) before the pause, we can find the steady-state solution \( P_m^\pi \) by letting \( dP_m(t)/dt = 0 \). That is,

\[
0 = b_m + \sum_{n \neq m} d_{mn} P_n^\pi - r_m - h_m P_m^\pi - k_m P_m^\pi - \sum_{n \neq m} d_{mn} P_m^\pi, \quad m = 1, \ldots, M. \tag{3}
\]

We denote by \( \pi \) a pause policy that specifies which categories of patients should be paused and the duration of the pause (denoted by \( t_m^\pi \)). We denote by \( 1(t > t_m^\pi) \) an indicator function that equals 1 for the period after the pause. Under the policy \( \pi \), we have

\[
\frac{dP_m^\pi(t)}{dt} = b_m + \sum_{n \neq m} d_{mn} P_n^\pi(t) - 1(t > t_m^\pi) r_m - h_m P_m^\pi(t) - \sum_{n \neq m} d_{mn} P_m^\pi(t), \quad m = 1, \ldots, M. \tag{4}
\]

Note that we assume the rate of organ transplants after the pause is the same as that before the pause, because the number of organ transplants depends mainly on the availability of organ donors.

### 3.2 Loss of patient life months

A patient on the waiting list may have one of the following four outcomes: (1) The patient dies and leaves the waiting list before receiving a transplant; (2) the patient receives a transplant, leaves the waiting list, and dies afterwards; (3) the patient does not receive a transplant, becomes inactive, and dies afterwards; (4) the patient does not receive a transplant and transitions to other categories. We denote by \( y_{1m} \) and \( y_{km} \) the expected life months of a category \( m \) patient who receives a transplant or becomes inactive, respectively. We calculate the expected life months of the patient (denoted by \( \hat{y}_m \)) as the absorption time to the death state. We have

\[
\hat{y}_m = \lambda_m + \mathbb{P} \text{dies} \times 0 + \mathbb{P} \text{receives a transplant} \times y_{1m} + \mathbb{P} \text{becomes inactive} \times y_{km} + \sum_\pi \mathbb{P} \text{transitions to category } n \times \hat{y}_n, \tag{5}
\]
where

\[ \lambda_m = \frac{1}{\frac{r_m}{p_m} + h_m + k_m + \sum_{n \neq m} d_{mn}}, \]

\[ \mathbb{P}(\text{dies}) = \frac{r_m}{p_m} + h_m + k_m + \sum_{n \neq m} d_{mn}, \]

\[ \mathbb{P}(\text{receives a transplant}) = \frac{r_m}{p_m} + h_m + k_m + \sum_{n \neq m} d_{mn}, \]

\[ \mathbb{P}(\text{becomes inactive}) = \frac{r_m}{p_m} + h_m + k_m + \sum_{n \neq m} d_{mn}, \]

\[ \mathbb{P}(\text{transitions to category } n) = \frac{d_{mn}}{\frac{r_m}{p_m} + h_m + k_m + \sum_{n \neq m} d_{mn}}. \]

To allow the possibility that the severity of a pandemic changes over time (e.g., COVID-19 variants), we consider multiple periods such that the probability of mortality due to the pandemic is the same within the same period and different across different periods. Without loss of generality, we consider two periods (denoted by \( t_1 \) and \( t_2 \)) in this study. We denote by \( q_{1m} \) and \( q_{2m} \) the probabilities of mortality due to the pandemic in the first and second periods, respectively.

If a decision maker does not pause organ transplants, the loss of patient life months due to the pandemic is

\[ U_{\text{NoPause}} = \sum_m (r_m t_1 q_{1m} y_{1m} + r_m t_2 q_{2m} y_{1m}), \]  

where the first and second terms indicate the loss of patient life months due to the pandemic in the first and second periods, respectively.

If a decision maker pauses organ transplants under the policy \( \pi \), some patients die without transplants, and others become sicker while waiting for organ transplants. We measure the impact of the pause policy using two metrics. The first metric is the number of extra deaths due to the pause. Intuitively, the longer the pause, the more patients who die on the waiting list. Because the rate of waitlist mortality differs across different categories of patients, we calculate this metric by patient category. We denote by \( \Delta D_m^\pi \) the number of extra deaths on the waiting list and calculate it as

\[ \Delta D_m^\pi = \int_{0}^{t_1 + t_2} h_m P_m(t) dt - h_m P_m(t_1 + t_2). \]  

The second metric is the number of extra deteriorations from healthier categories to sicker categories. We calculate this metric by patient category because the rate of deterioration differs across different categories of patients. We denote by \( \Delta T_{mn}^\pi \) the number of extra deteriorations from category \( m \) to category \( n \) and calculate it as

\[ \Delta T_{mn}^\pi = \int_{0}^{t_1 + t_2} d_{mn} P_m(t) dt - d_{mn} P_m(t_1 + t_2). \]  

We denote by \( y_{0m} \) the expected life months of a category \( m \) patient without an organ transplant. Under the pause policy \( \pi \), the loss of patient life months due to deaths on the waiting list is \( \Delta D_m^\pi (y_{1m} - y_{0m}) \), and that due to deteriorations is \( \Delta T_{mn}^\pi (y_{1m} - y_{n}) \). After the pause, the loss of patient life months depends on the probability of mortality due to the pandemic. Therefore, the total loss of patient life months across all categories is

\[ U_{\text{Pause}}^\pi = \sum_m \left( \Delta D_m^\pi (y_{1m} - y_{0m}) + \sum_{n \neq m} \Delta T_{mn}^\pi (y_{1m} - y_{n}) \right) \]

where the three terms indicate the loss of patient life months due to deaths on the waiting list, health deteriorations, and the pandemic, respectively.

### 3.3 Pause policies

In this section, we first describe the difference between the complete shutdown and tiered shutdown policies to illustrate the value of a patient-specific approach. We then describe the difference between nation-guidance and center-specific policies to illustrate the value of a center-specific approach. Finally, we describe different pause policies with examples.

#### 3.3.1 Complete shutdown versus tiered shutdown policies

Under a complete shutdown policy, a decision maker pauses organ transplants for all categories of patients for the same period. As a special case, when the pause period equals zero, the decision maker does not pause any organ transplant. Under a tiered shutdown policy, the decision maker pauses organ transplants for categories 1 to \( m \) for the same period. Note that the tiered shutdown policy includes the complete shutdown policy as a special case, because \( m = M \) means pausing all categories of patients for the same period. Intuitively, the tiered shutdown policy is superior to the complete shutdown policy, because the former considers the...
heterogeneity across different categories of patients (i.e., more patient-specific).

3.3.2 Nation-guidance versus center-specific policies

Under a nation-guidance policy, the decision maker does not consider the difference between centers and pauses organ transplants at different centers in the same way. Under a center-specific policy, the decision maker considers the difference between centers and pauses organ transplants at different centers in center-specific ways. Intuitively, the center-specific policy is superior to the nation-guidance policy, because the former considers the heterogeneity across centers (i.e., more center-specific). However, the two policies may be similar if centers are homogeneous.

3.3.3 Description of different pause policies

Considering different combinations of complete shutdown versus tiered shutdown and nation-guidance versus center-specific policies, we have four different pause policies (see Figure 1). We illustrate these policies by using a simple example with two centers (center 1 and center 2) and two categories (category 1 and category 2) of patients.

- Nation-guidance complete shutdown policy: A decision maker does not consider the difference between patient categories or the difference between centers, by pausing all organ transplants in all centers for the same period. An example of this policy is to pause both categories in center 1 and neither category in center 2.
- Nation-guidance tiered shutdown policy: A decision maker considers the difference between patient categories but not the difference between centers, by pausing the same categories of patients in all centers by the same period. An example of this policy is to pause only category 1 in both centers.
- Center-specific tiered shutdown policy: A decision maker considers both the difference between centers and the difference between patient categories, by pausing different patient categories in different centers. An example of this policy is to pause category 1 in center 1 and both categories in center 2.

3.4 Optimal pause policy and threshold probability

When the risk of a pandemic is known, a decision maker can analyze the effectiveness of a pause policy (denoted by \( \pi \)) by calculating the difference between \( U_{\text{Pause}}^\pi \) and \( U_{\text{NoPause}} \). Given the policy space \( S = \{ \text{Nation-Guidance Complete Shutdown}, \text{Nation-Guidance Tiered Shutdown}, \text{Center-Specific Complete Shutdown}, \text{Center-Specific Tiered Shutdown} \} \), a decision maker can identify the optimal policy by comparing \( U_{\text{Pause}}^\pi - U_{\text{NoPause}} \) across different policies. That is,

\[
\pi^* = \arg \min_{\pi \in S} (U_{\text{Pause}}^\pi - U_{\text{NoPause}}).
\]

When the risk of a pandemic is unknown, a decision maker cannot calculate \( U_{\text{Pause}}^\pi \) or \( U_{\text{NoPause}} \) to assess the effectiveness of a policy. However, we can derive a threshold probability above which the decision maker should follow the pause policy. To derive an expression of the threshold probability, we need to make two assumptions. First, the probability of mortality due to the pandemic is the same across different periods under consideration. Second, the probability of mortality due to the pandemic is the same across different patient categories. We derive the threshold probability by letting \( U_{\text{NoPause}} \) equal \( U_{\text{Pause}}^\pi \). That is,

\[
q^\pi = \frac{\sum_m \Delta D_{mn}^\pi (y_{1m} - y_{0m}) + \sum_{n,m>n} \Delta r_{mn}^\pi (\hat{y}_{1m} - \hat{y}_{nm})}{\sum_m r_{mnm}^\pi y_{1m}}.
\]

4 DATA AND PARAMETERS ESTIMATION

In this section, we first describe liver transplants as the clinical setting of our study. We then describe a unique set of data we obtain from the United Network for Organ Sharing
(UNOS). Finally, we explain how we empirically estimate the parameters from the data.

4.1 Background and clinical setting

The liver is one of the largest organs in the body and has many metabolic functions, such as taking toxic substances and converting them into harmless substances. Patients are at increased risk when their liver fails. A liver transplant refers to a set of surgical procedures that remove a diseased liver and replace it with a healthy liver from a donor. A liver transplant is the only cure for liver failure or insufficiency in practice, because no device or machine can perform all the functions of a liver. Patients in need of liver transplants are first evaluated by a medical team and then added to the waiting list for organ transplants.

UNOS uses the MELD score to estimate the likelihood of a patient dying without a liver transplant within the next 3 months. Before 2016, the score was calculated based on three lab test results: (1) bilirubin, (2) international normalized ratio (INR), and (3) creatinine. Since 2016, UNOS has updated the model to include an additional lab test result—serum sodium (Na). The MELD-Na score is ideal for us to categorize patients, because it captures both the sickness of patients and the priority of different patients to receive liver transplants.

When a liver becomes available, it is offered first to sicker patients (i.e., those with high MELD-Na scores) in the same DSA and then to healthier patients (i.e., those with low MELD-Na scores) in other DSAs of the same region. A DSA is a CMS-designated geographic area (usually a state) that is served by one OPO, one or more transplant centers, and one or more donor hospitals. A region consists of several neighboring DSAs/states. For example, region 5 includes Arizona, California, Nevada, New Mexico, and Utah (see Figure 2).

4.2 Data description and preparation

We obtain the organ transplant data as of September 1, 2020, from UNOS as the contractor for the Organ Procurement and Transplantation Network (OPTN). One unique feature of our data is that they include both patients who are added to the waiting list and those who are removed from the waiting list due to organ transplants, deaths, or inactivations, which allows us to track the change in the waiting list over time. Another unique feature is that our data record the change in a patient’s health status over time, because UNOS updates a patient’s MELD-Na score periodically. These panel data allow us to calculate the number of deteriorations due to delays of liver transplants. Finally, our data include detailed features of both patients and donors (e.g., demographics, blood type, and diagnoses), which allows us to control for the sickness of patients and the quality of organs when we estimate the expected life months.

We use the data from January 1, 2007, to March 31, 2018. These long-panel data allow us to estimate the rates of waitlist mortality and transition and the expected life months. However, because MELD scores were used before 2016, we need to convert them into MELD-Na scores using UNOS’ formula. We exclude pediatric patients because UNOS uses a different rule to allocate organs to these patients. We also exclude patients with status 1, because these patients are likely to die in the next few days without transplants. In addition, we exclude patients who require multiorgan transplants, because the probability of these patients receiving transplants depends on other types of organs (e.g., kidneys). Finally, we exclude patients with missing MELD-Na scores, because we cannot calculate the change in these patients’ health condition. Table 2 provides summary statistics of the observations used in this study.

4.3 Parameters estimation

In this section, we first describe how to estimate the rates of patient arrival and organ transplant, and the rates of mortality, inactivation, and transition for individuals. We then describe how to estimate expected life months.

4.3.1 Rates of arrival and transplant

We estimate the arrival rate of a category using the average number of patients added to the waiting list per day. For example, in the United States, a total of 8339 patients with MELD-Na scores between 16 and 20 were added to the waiting list between January 1, 2011, and December 31, 2015, so the arrival rate of this category is $8339 \div 1826$ days = 4.6 patients per day. We estimate the transplant rate of a category using the average number of patients who received transplants per day. During the same period, a total of 1921 patients with MELD-Na scores between 16 and 20 received transplants, so the transplant rate of this category is $1921 \div 1826$ days = 1.1 transplants per day.

Similarly, we estimate the arrival rate of patients across all categories using the average number of patients added to the waiting list per day. For example, in the United States, a total of 39,431 patients were added to the waiting list between January 1, 2011, and December 31, 2015, so the arrival rate across all categories is $39,431 \div 1826$ days = 21.6 patients per day. We estimate the transplant rate of patients across all categories using the average number of patients who received transplants per day. During the same period, a total of 15,544 patients received transplants, so the transplant rate across all categories is $15,544 \div 1826$ days = 8.5 transplants per day. Because the parameters estimated from a given category of patients may be different from those estimated from all patients as a group, these comparisons also suggest the value of the patient-specific approach.

The first two rows of Table 3 summarize the arrival rate and transplant rate of patients across all categories in the
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**FIGURE 2**  Regions defined by United Network for Organ Sharing (UNOS). Note: This figure depicts the regions defined by UNOS for organ procurement and allocation. More details about these regions are available at [https://unos.org/community/regions/](https://unos.org/community/regions/).

country and three different centers. Note that the rates of patient arrival and liver transplant in the country are larger than those in a center, because the former are calculated based on all patients in the country, whereas the latter are calculated based on only patients in a center. From the table, we see a sizable difference between the country and a center. For example, the ratio of the transplant rate and arrival rate is $8.5/21.6 = 39\%$ in the country and $0.2/0.3 = 67\%$ in center B, which suggests that patients in center B are more likely to receive organ transplants than an average patient in the country. Because the parameters at the country level may be different from those at the center level, these comparisons also suggest the value of the center-specific approach.

4.3.2 Rates of mortality, inactivation, and transition for individuals

We estimate the rates of mortality, inactivation, and transition by first calculating the respective daily rates and then the average of these daily rates. Consider a hypothetical scenario in which the number of patients on the waiting list is 9000, 10,000, and 11,000 over 3 days, and the number of patients dying on the waiting list is 5, 6, and 7 over these 3 days. The daily rates of mortality are $5/9000 = 0.056\%$, $6/10,000 = 0.060\%$, and $7/11,000 = 0.064\%$ and the rate of mortality is $(0.056\% + 0.060\% + 0.064\%) / 3 = 0.060\%$. Rows (3) and (4) of Table 3 summarize the rates of waitlist mortality and inactivation.

Table 4 summarizes the rate of transition using the country-level data. We include “death” as an additional state because some patients die on the waiting list. From the table, we see the majority of patients remain in the same category. Note the rate of a patient transitioning from a category to a nearby category is higher than that to a remote category. The rate of a patient dying on the waiting list increases as the MELD-Na score increases, which is consistent with the observation that patients with higher MELD-Na scores are more likely to die in the next few months.

4.3.3 Expected life months

We follow existing studies (see, e.g., Luo et al., 2018) to estimate a patient’s likelihood of survival using the generalized gamma survival model. The density function of the generalized gamma survival model is

$$f(t) = \begin{cases} \frac{\gamma^\gamma}{\sigma(\sqrt{\gamma})} \exp \left( \frac{\gamma t}{\sqrt{\gamma}} - u \right) & \text{if } \kappa \neq 0, \\ \frac{1}{\sigma \sqrt{2\pi}} \exp \left( -\frac{z^2}{2} \right) & \text{if } \kappa = 0 \end{cases}$$

(13)

where $\gamma = |\kappa|^{-2}$, $z = \text{sign}(\kappa)(\log(t) - \mu)/\sigma$, and $u = \gamma \exp(|\kappa|z)$.

We estimate the model by treating the parameters $\kappa$ and $\sigma$ as ancillary parameters to be estimated from the data and parameterizing $\mu_i$ as follows:

$$\mu_i = \beta_0 + \beta_1 \text{MELD-Na}_i + \beta_2 \text{Transplant}_i + \beta_3 \text{MELD-Na}_i \times \text{Transplant}_i + \beta_4 \text{PatientFeatures}_i + \epsilon_i,$$

(14)

where $\text{Transplant}$ and $\text{MELD-Na} \times \text{Transplant}$ denote liver transplant and its interaction with the MELD-Na category, respectively.

Table 5 summarizes the results from the survival model estimated at the country level. From the upper part of the
### TABLE 2
Summary statistics for the liver transplant

| Variable                        | Description                          | Mean   | Std. dev. |
|---------------------------------|--------------------------------------|--------|-----------|
| **Patient features**            |                                      |        |           |
| Age                             | Patient’s age at registration        | 54.0   | 10.9      |
| Gender                           | Patient’s gender is female           | 0.38   | 0.49      |
| Race Black                       | Patient’s race is Black              | 0.08   | 0.28      |
| Blood type AB                    | Patient’s blood type is AB           | 0.04   | 0.19      |
| Blood type B                     | Patient’s blood type is B            | 0.12   | 0.32      |
| Blood type O                     | Patient’s blood type is O            | 0.47   | 0.50      |
| Malignancy all                   | Patient has known malignancies       | 0.11   | 0.32      |
| Private insurance                | Patient has private insurance        | 0.24   | 0.42      |
| Previous transplant              | Patient had a transplant before      | 0.02   | 0.15      |
| **Diagnoses**                    |                                      |        |           |
| Alcoholic liver disease          | Patient has alcoholic liver disease  | 0.28   | 0.45      |
| Cholestatic liver disease        | Patient has cholestatic liver disease| 0.08   | 0.27      |
| Cirrhosis viral hepatitis        | Patient has hepatitis B or C         | 0.23   | 0.42      |
| Fatty liver                      | Patient has fatty liver              | 0.13   | 0.33      |
| Malignancy                       | Patient has known malignancies       | 0.06   | 0.24      |
| Metabolic liver disease          | Patient has metabolic liver disease  | 0.03   | 0.16      |
| Other                            | Patient has other diagnoses          | 0.20   | 0.40      |
| **MELD-Na**                      |                                      |        |           |
| 5–10                            | Patient’s MELD-Na score is between 5 and 10 | 0.16 | 0.37 |
| 11–15                           | Patient’s MELD-Na score is between 11 and 15 | 0.20 | 0.40 |
| 16–20                           | Patient’s MELD-Na score is between 16 and 20 | 0.21 | 0.41 |
| 21–25                           | Patient’s MELD-Na score is between 21 and 25 | 0.15 | 0.36 |
| 26–30                           | Patient’s MELD-Na score is between 26 and 30 | 0.11 | 0.31 |
| 31–35                           | Patient’s MELD-Na score is between 31 and 35 | 0.08 | 0.27 |
| 36–40                           | Patient’s MELD-Na score is between 36 and 40 | 0.09 | 0.29 |
| **Number of observations**       |                                      |        |           |
|                                 |                                      |        | 128,098   |

*Note:* The malignancy in the diagnoses category includes hepatoma and cirrhosis, fibrolamellar, cholangiocarcinoma, hepatoblastoma, hemangioendothelioma, hemangiosarcoma, angiosarcoma, any other specify (e.g., klatskin tumor, leiomyosarcoma), bile duct cancer, and secondary hepatic malignancy.

### TABLE 3
Basic information at the country level and the center level

| Parameter                           | Country       | Center A | Center B | Center C |
|-------------------------------------|---------------|----------|----------|----------|
| (1) Arrival rate (per day)          | 21.6          | 0.6      | 0.3      | 0.3      |
| (2) Transplant rate (per day)       | 8.5           | 0.2      | 0.2      | 0.1      |
| (3) Mortality rate (%)              | 0.04          | 0.04     | 0.03     | 0.05     |
| (4) Inactivation rate (%)           | 0.08          | 0.04     | 0.10     | 0.08     |
| (5) ELMs with LT (months)           | 93.5          | 108.3    | 75.8     | 88.4     |
| (6) ELMs without LT (months)        | 30.6          | 26.5     | 17.3     | 53.0     |

*Note:* Mortality and inactivation rates are for individuals. Center A locates in California and has one of the largest transplant programs in the country for more than 60 years. Center B locates in Pennsylvania and has been a pioneer in organ transplants for more than 50 years. Center C locates in Pennsylvania and is a leader in organ transplants for more than 40 years. Abbreviations: ELMs, expected life months; LT, liver transplant.

### TABLE 4
Rates of transition and mortality for individuals at the country level

| MELD-Na | 6–10 | 11–15 | 16–20 | 21–25 | 26–30 | 31–35 | 36–40 | Death |
|---------|------|-------|-------|-------|-------|-------|-------|-------|
| 6–10    | 0.99 | 0.09  | 0.02  | 0.01  | 0.00  | 0.00  | 0.00  | 0.01  |
| 11–15   | 0.11 | 0.99 | 0.20  | 0.03  | 0.01  | 0.00  | 0.00  | 0.01  |
| 16–20   | 0.03 | 0.24 | 0.99  | 0.30  | 0.05  | 0.01  | 0.00  | 0.03  |
| 21–25   | 0.01 | 0.08 | 0.50  | 0.49  | 0.54  | 0.08  | 0.02  | 0.06  |
| 26–30   | 0.01 | 0.04 | 0.22  | 1.37  | 96.08 | 1.29  | 0.18  | 0.17  |
| 31–35   | 0.00 | 0.01 | 0.09  | 0.43  | 2.45  | 92.01 | 2.50  | 0.43  |
| 36–40   | 0.00 | 0.00 | 0.03  | 0.10  | 0.38  | 1.17  | 90.00 | 1.65  |

*Note:* All rates are in percentages. Abbreviation: MELD-Na, model for end-stage liver disease-sodium.

From the table, we see all coefficients of MELD-Na are positive and significantly different from zero at the 1% significance level, which suggests patients with MELD-Na scores between 5 and 35 live longer than those with MELD-Na scores above 35 (control group). Comparing the magnitude of the coefficients, we see patients with lower MELD-Na scores live longer than those with higher MELD-Na scores.
Results and discussion

Pausing policies

Without liver transplants. Those patients in this category do not benefit from liver transplants. Interestingly, the sum of coefficients is negative (i.e., $2^{1.5578}$ $= 5.359$ $= 0.0510$) for patients with MELD-Na scores between 36 and 40. These sums of coefficients are positive, which suggests patients in these categories benefit from liver transplants. Interestingly, the sum of coefficients is negative (i.e., $2^{2.2010}$ $= 3.7383$ $= 0.0281$) for patients with MELD-Na scores between 5 and 10. Those patients in this category do not benefit from liver transplants, because they are the healthiest and can live longer without liver transplants.

For each patient category, we can estimate the effect of liver transplant by adding the coefficients of Transplant and MELD-Na $\times$ Transplant. For example, the sum of coefficients is $2^{2.2010} - 0.3539 = 0.5578$ for patients with MELD-Na scores between 31 and 35 and $2^{2.2010} - 0.6432 = 1.5578$ for patients with MELD-Na scores between 26 and 30. These sums of coefficients are positive, which suggests patients in these categories benefit from liver transplants. Interestingly, the sum of coefficients is negative (i.e., $2^{2.2010} - 2.5112 = -0.3102$) for patients with MELD-Na scores between 5 and 10. Those patients in this category do not benefit from liver transplants, because they are the healthiest and can live longer without liver transplants.

In the middle part of the table, the coefficient of Transplant is positive and significantly different from zero at the 1% significance level, which suggests liver transplant increases the survival of patients. We see all coefficients of MELD-Na $\times$ Transplant are negative and significantly different from zero at the 1% significance level, which suggests patients with MELD-Na scores below 36 benefit less than the control group (i.e., those with MELD-Na scores between 36 and 40) from liver transplants. Comparing the magnitude of the coefficients, we see that patients with higher MELD-Na scores benefit more than those with lower MELD-Na scores from liver transplants.

For each patient category, we can estimate the effect of liver transplant by adding the coefficients of Transplant and MELD-Na $\times$ Transplant. For example, the sum of coefficients is $2^{2.2010} - 0.3539 = 0.5578$ for patients with MELD-Na scores between 31 and 35 and $2^{2.2010} - 0.6432 = 1.5578$ for patients with MELD-Na scores between 26 and 30. These sums of coefficients are positive, which suggests patients in these categories benefit from liver transplants. Interestingly, the sum of coefficients is negative (i.e., $2^{2.2010} - 2.5112 = -0.3102$) for patients with MELD-Na scores between 5 and 10. Those patients in this category do not benefit from liver transplants, because they are the healthiest and can live longer without liver transplants.

In the first scenario, the two periods include 15 days and 350 days, respectively, and the probability of mortality across all categories is 40% in the first period (i.e., $q_{1/m} = 0.4$) and 20% during the second period (i.e., $q_{2/m} = 0.5$). The second scenario is similar to the first except that the probability of mortality is higher in the second period. The third scenario is similar to the first except that the probabiility of mortality is higher in the second period. The third scenario is similar to the first except that the two periods include 30 days and 335 days, respectively. The fourth scenario is similar to the first scenario except that the probability of mortality is 20% in the first period and 10% in the second period.

The right part of Table 6 summarizes the optimal nation-guidance tiered shutdown policy (see column “Nation/tiered”) and the optimal center-specific tiered shutdown policy (see column “Center/tiered”). We use the nation-guidance tiered shutdown policy as an example to illustrate the results. In the first scenario, the optimal nation-guidance plan

### Table 5

Results from the survival model estimated at the country level

| Variable               | Coefficient | Standard error |
|------------------------|-------------|----------------|
| MELD-Na                |             |                |
| 5–10                   | 3.7383***   | 0.0281         |
| 11–15                  | 3.2921***   | 0.0276         |
| 16–20                  | 2.5172***   | 0.0268         |
| 21–25                  | 1.8862***   | 0.0266         |
| 26–30                  | 1.1750***   | 0.0283         |
| 31–35                  | 0.6713***   | 0.0296         |
| 36–40                  | Control     |                |
| Transplant             | 2.2010***   | 0.0360         |
| MELD-Na $\times$ Transplant |
| 5–10                   | $-2.5112$*** | 0.0936         |
| 11–15                  | $-1.9500$*** | 0.0641         |
| 16–20                  | $-1.3152$*** | 0.0492         |
| 21–25                  | $-1.0328$*** | 0.0475         |
| 26–30                  | $-0.6432$*** | 0.0485         |
| 31–35                  | $-0.3539$*** | 0.0510         |
| 36–40                  | Control     |                |
| Patient features       | Included     |                |
| Number of observations | 103,320      |                |
| LR $\chi^2$            | 31,354       |                |

### Table 6

Description of scenarios and policies to pause organ transplants

| Scenario | $t_1$ | $t_2$ | $q_1$ | $q_2/q_1$ | Nation/ tiered | Center/ tiered |
|----------|-------|-------|-------|-----------|----------------|----------------|
| 1        | 15    | 350   | [0.4, 0.4, ..., 0.4] | 0.5 | [1] | [1] |
| 2        | 15    | 350   | [0.4, 0.4, ..., 0.4] | 1.0 | [1, 2] | [1] |
| 3        | 30    | 335   | [0.4, 0.4, ..., 0.4] | 0.5 | [1, 2] | [1] |
| 4        | 15    | 350   | [0.2, 0.2, ..., 0.2] | 0.5 | [1] | Ø |

Note: The left part of this table describes different scenarios, in which $t_1$ and $t_2$ indicate the periods under consideration, and $q_1$ and $q_2$ indicate the probabilities of mortality due to the pandemic over the periods. The right part of the table summarizes different policies, in which the numbers in the bracket indicate the categories to be paused. The duration of the pause is 30 days for all scenarios. The center-specific tiered shutdown policy is calculated based on the data of center A.

### 5 RESULTS AND DISCUSSION

In this section, we first compare different pause policies to illustrate the value of patient-specific and center-specific approaches. We then present the threshold probability above which a decision maker should pause organ transplants. Next, we discuss how capacity constraints affect the loss of patient life months and the length of the waiting list. Finally, we discuss different phases of the pandemic, potential challenges of implementing an optimal policy, and how to extend our model to other settings.

### 5.1 Pause policies

How to pause organ transplants depends on the periods (i.e., $t_1$ and $t_2$) under consideration and the mortality probabilities (i.e., $q_1$ and $q_2$) over these periods. To compare different pause policies, we consider scenarios with different periods and probabilities of mortality due to the pandemic. However, once these parameters can be estimated accurately from a growing availability of data, identifying a newer or better pause policy is possible.

The left part of Table 6 describes four scenarios as examples. In the first scenario, the two periods include 15 days and 350 days, respectively, and the probability of mortality across all categories is 40% in the first period (i.e., $q_{1/m} = 0.4$) and 20% during the second period (i.e., $q_{2/m}/q_{1/m} = 0.5$). The second scenario is similar to the first except that the probability of mortality is higher in the second period. The third scenario is similar to the first except that the two periods include 30 days and 335 days, respectively. The fourth scenario is similar to the first scenario except that the probability of mortality is 20% in the first period and 10% in the second period.

The right part of Table 6 summarizes the optimal nation-guidance tiered shutdown policy (see column “Nation/tiered”) and the optimal center-specific tiered shutdown policy (see column “Center/tiered”). We use the nation-guidance tiered shutdown policy as an example to illustrate the results. In the first scenario, the optimal nation-guidance plan

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**Abbreviation:** MELD-Na, model for end-stage liver disease-sodium. 

***$p < 0.01$.**
Comparison of policies

The optimal nation-guidance tiered shutdown policy is to pause category 1. From different rows of the table, we see the optimal nation-guidance tiered shutdown policy changes as the probability of mortality changes across different periods or different categories. For example, comparing scenarios 1 and 2, we see a decision maker should pause more categories when the pandemic is more severe in period 2. Comparing scenarios 1 and 3, we see the decision maker should pause more categories when the severe period of a pandemic lasts for a longer time.

### 5.2 Comparison of policies

To analyze the potential value of the patient-specific approach, we compare a complete shutdown policy with a tiered shutdown policy. The left part of Table 7 compares the nation-guidance complete shutdown policy and the nation-guidance tiered shutdown policy at the country level. We use scenario 1 to illustrate our results. In this scenario, the loss of patient life months is 62,204 when the country pauses all liver transplants and 54,711 when the country does not pause any liver transplant. The difference between pause and no-pause scenarios is 7493, which suggests a complete shutdown policy leads to a worse outcome than the nation-guidance policy.

Under the optimal nation-guidance tiered shutdown policy, the decision maker pauses category 1 and the loss of patient life months is 54,653. Comparing \( U_{\text{Pause}}^{\pi} \) and \( U_{\text{NoPause}}^{\pi} \) in column “Nation/tiered,” we see the nation-guidance tiered shutdown policy leads to a better outcome than the complete open policy under which the decision maker does not pause any organ transplant. Comparing \( U_{\text{Pause}}^{\pi} \) in columns “Nation/complete” and “Nation/tiered,” we see the nation-guidance tiered shutdown policy leads to a better outcome than the complete shutdown policy under which the decision maker does not pause any organ transplant. Comparing different scenarios, we see the tiered shutdown policy is always better than the complete shutdown policy, which suggests the value of the patient-specific approach.

To analyze the potential value of the center-specific approach, we compare a nation-guidance policy with a center-specific policy. The right part of Table 7 compares the nation-guidance tiered shutdown policy and the center-specific tiered shutdown policy at the center level. We use scenario 2 to illustrate the results. In this scenario, the loss of patient life months is 2539 under the nation-guidance tiered shutdown policy and 2536 under the center-specific tiered shutdown policy, which suggests the center-specific policy leads to a better outcome than the nation-guidance policy.

Comparing different scenarios, we see the potential value of the center-specific approach depends on the periods under consideration and the mortality probabilities across different periods.

### 5.3 Threshold probability

We solve the system of differential equations (4) numerically and calculate the threshold probability using Equation (12). Table 8 summarizes the threshold probability for the nation-guidance tiered shutdown policy at the country level. We use category 3 to illustrate the results. The threshold probability for patients with MELD-Na scores between 16 and 20...
TABLE 8  Threshold probability under nation-guidance tiered shutdown policy

| MELD-Na | Threshold probability |
|---------|-----------------------|
| 6–10    | 0.075                 |
| 11–15   | 0.236                 |
| 16–20   | 0.449                 |
| 21–25   | 0.567                 |
| 26–30   | 0.651                 |
| 31–35   | 0.683                 |
| 36–40   | 0.647                 |

Note: This table shows the threshold probability above which a country-level decision maker should pause transplants. For example, a decision maker should not pause any transplant if the probability of mortality is lower than 0.075, and should pause transplants for only patients with MELD-Na scores below 11 if the probability of mortality is higher than or equal to 0.075 but lower than 0.236. Abbreviation: MELD-Na, model for end-stage liver disease-sodium.

TABLE 9  Threshold probability under center-specific tiered shutdown policy

| MELD-Na | Center A | Center B | Center C |
|---------|----------|----------|----------|
| 6–10    | 0.205    | 0.209    | 0.183    |
| 11–15   | 0.377    | 0.392    | 0.294    |
| 16–20   | 0.584    | 0.573    | 0.422    |
| 21–25   | 0.680    | 0.734    | 0.521    |
| 26–30   | 0.746    | 0.861    | 0.579    |
| 31–35   | 0.803    | 0.861    | 0.635    |
| 36–40   | 0.778    | 0.898    | 0.658    |

Note: This table shows the threshold probability above which a center-level decision maker should pause transplants. Abbreviation: MELD-Na, model for end-stage liver disease-sodium.

is 0.449, which suggests a decision maker should not pause transplants for the patients with MELD-Na scores below 21 unless the probability of mortality due to the pandemic is higher than 44.9%.10

We perform the same analysis for the center-specific tiered shutdown policy at the center level. Table 9 summarizes the threshold probability for three different centers. We find that a 30-day pause of liver transplants for patients with MELD-Na scores of 16 or higher requires a mortality probability ranging from 42.2% to 89.8%. Though the threshold probability differs across centers, these large numbers suggest a decision maker should be cautious in pausing liver transplants for patients with MELD-Na scores of 16 or higher when the risk of a pandemic is unknown.

We also note center C has a lower threshold probability than the other two centers. A possible explanation is the difference in expected life months with and without liver transplants. Compared with patients in the other two centers, patients in center C have longer expected life months without liver transplants but comparable expected life months with liver transplants. Pausing liver transplants in this center reduces expected life months by less than the other centers and therefore requires a lower threshold probability.

5.4  Capacity constraints

Our main analysis focuses on the direct impact of COVID-19 on organ transplants (i.e., the probability of mortality due to the pandemic). The pandemic may affect organ transplants indirectly by reducing the capacity of transplant centers if they have to redirect scarce healthcare resources such as medical staff and beds toward the care of COVID-19 patients. In this section, we incorporate the capacity constraints into our model and analyze how these constraints affect the loss of patient life months and the length of the waiting list.

We follow Kaplan et al. (1992) to analyze the impact of overall-capacity constraints. To describe this approach, we denote by $r_m$ and $r'_m$ the capacity for patient category $m$ before and after the reduction, respectively, and by $\alpha$ the reduction in the overall capacity. Denote by $M$ the number of patient categories. The overall capacity is $\sum_{m=1}^{M} r_m$ before the reduction and $\sum_{m=1}^{M} r'_m$ after the reduction. We derive the optimal pause policy by using Equation (11) with an additional constraint that $\sum_{m=1}^{M} r'_m = \sum_{m=1}^{M} r_m - \alpha$. In the main analysis, we prioritize sicker patient categories for capacity allocation because of two reasons. First, existing studies (see, e.g., Kumar et al., 2020) suggest that transplant centers stratify patients based on their MELD-Na scores and perform transplants for only patients with high MELD-Na scores. Second, the OPTN policies prioritize sicker patient categories over healthier patient categories for liver allocation.11 In Appendix E of the Supporting Information, we allow different patient categories to have different capacity reductions.

We first analyze the impact of capacity constraints on the loss of patient life months. Figure 3 depicts the results by using scenario 1 (see Table 6) and the nation-guidance shutdown policy as an example.12 The horizontal axis indicates the reduction in the overall capacity, and the vertical axis indicates the loss of patient life months.13 From the figure, we see that the loss of patient life months increases as the reduction in the overall capacity increases. For example, when the overall capacity reduces by two transplants per day, the loss of patient life months increases by 55,815 – 54,653 = 1162, and when the overall capacity reduces by four transplants per day, the loss of patient life months increases by 58,205 – 54,653 = 3552. The relationship between the loss of patient life months and reduction in capacity is nonlinear, because the impact of capacity constraints is heterogeneous across patient categories. More specifically, given the same amount of reduction in capacity, the loss of patient life months is the largest for patients with medium MELD-Na scores and the smallest for patients with low MELD-Na scores (see Appendix D in the Supporting Information for more details). As a result, the marginal rate of the change first increases and then decreases (see Figure 3).
if we prioritize patients with higher MELD-Na scores for capacity allocation.

We then analyze the impact of capacity constraints on the length of the waiting list. Figure 4 depicts the results by using scenario 1 (see Table 6) and the nation-guidance tiered shutdown policy as an example. The horizontal axis indicates the reduction in the overall capacity, and the vertical axis indicates the average number of extra patients on the waiting list across the periods under consideration (i.e., $t_1 + t_2$). From the figure, we see that the average number of extra patients on the waiting list increases as the reduction in the overall capacity increases. For example, when the overall capacity reduces by two transplants per day, the average number of extra patients on the waiting list increases by 42, and when the overall capacity reduces by four transplants per day, the average number of extra patients on the waiting list increases by 77. The relationship between the average number of extra patients on the waiting list and reduction in capacity is nonlinear, because patients with higher MELD-Na scores are more likely to die on the waiting list than those with lower MELD-Na scores (see Appendix D in the Supporting Information for more details).

Finally, we note that the impact of capacity constraints on threshold probability is heterogeneous across patient categories. First, the threshold probability for healthier patient categories decreases, because the tiered shutdown policy prioritizes sicker patients for capacity allocation. Second, the threshold probability for sicker patient categories increases, because these patients are more likely to die on the waiting list due to scarce healthcare resources.

5.5 | Discussion and insights

The pandemic has gone through three phases since its start. The first phase is nonpharmaceutical interventions, which include federal and state policies such as stay-at-home orders, school closures, and mask mandates. These nonpharmaceutical interventions reduce human-to-human contact and therefore the transmission of the virus. The second phase is vaccine development. In December 2020, several effective and safe vaccines (e.g., Janssen/Johnson & Johnson, Moderna, and Pfizer-BioNTech) had been successfully developed and were approved for emergency use in the United States. These vaccines help reduce the probability of infection as well as the probability of mortality due to the pandemic. The third phase is the occurrence of mutations. Existing studies find mutations such as the delta and omicron variants are more contagious than the original COVID-19 virus. The risk of infection exists even for vaccinated persons. Fortunately, the risk of mortality due to the infection is lower for those who are vaccinated. The combination of higher contagiousness and lower mortality suggests transplant centers are likely to face more capacity constraints and fewer risks of performing organ transplants. Researchers and policymakers can apply our model to a current or future phase of the pandemic by updating input parameters such as the probability of mortality to the pandemic, the number of patients on the waiting list, and the capacity of transplant centers.

Regardless of the phase of the pandemic, our comparison of different pause policies suggests that the center-specific
tiered shutdown policy is a more accurate response to a pandemic. But its implementation presents three potential challenges. The first challenge relates to data collection. Whereas nation-guidance policies require data to be collected at the country level, center-specific policies require data to be collected by individual transplant centers. Data collection can be challenging to some transplant centers, especially those with limited healthcare resources. The second challenge relates to empirical estimation. Because the sample size is larger at the country level than at the center level, the results from country-level analyses are more reliable than those from center-level analyses. When a center does not have a large enough sample size, it may have to follow a nation-guidance policy. The third challenge relates to patient selection. If centers follow different policies, a patient may switch from the waiting list of one center to that of another center or join multiple waiting lists. As a result, some centers may not have enough patient volume after they resume organ transplants. Fortunately, the first two challenges can be addressed when more healthcare resources/data or new econometric techniques become available (see, e.g., Hopp et al., 2018). The third challenge can be addressed by better aligning incentives for centers and patients.

Though this study focuses on liver transplants, our model can be applied to three other settings. First, in the setting of other organ transplants such as kidney transplants, we can apply our model by replacing MELD-Na scores with the estimated post-transplant survival (EPTS) scores to capture the condition of patients waiting for kidney transplants. Second, we can apply our model to other high-acuity procedures such as cancer surgeries (classified as tier 3a by CMS). Similar to patients with kidney or liver diseases, patients with cancer need to balance the trade-off between infections due to the pandemic and health deteriorations due to the progression of cancers. We can apply our model to this setting by using the size of a tumor to capture the condition of a patient. Finally, we can apply our model to analyze the costs and benefits of pausing elective surgeries such as hip and knee replacements (classified as tier 2a by CMS). Compared with patients who need organ transplants or cancer surgeries, patients who need hip or knee replacements are likely to live for a long period even without the surgeries. But their quality of life may decrease due to the pause of elective surgeries. We can apply our model to this setting by using the quality of life or inconvenience of move to capture the condition of a patient.

6 | CONCLUSION

The COVID-19 pandemic has changed many aspects of our life, from the closure of workplaces, schools, and restaurants, to the suspension of elective surgeries and nonessential doctor visits. The pandemic has also ignited hot debates regarding pausing organ transplants. Whereas proponents believe a pause will reduce the risk of infections and save scarce healthcare resources for COVID-19 patients, opponents argue patients waiting for organ transplants will become sicker and even die on the waiting lists.

Using liver transplant as the clinical setting and a system of differential equations, we show pausing organ transplants has a sizable negative effect on waitlist length and
patient life months. Our results support the CMS and AST’s recommendations that organ transplants should not be paused, given the current risk of COVID-19 to organ transplant recipients. However, if the risk of COVID-19 increases, a decision maker may need to pause organ transplants, based on our estimated threshold probability.

We also compare different pause policies for a decision maker to consider when the risk of a pandemic is known. In particular, we compare complete shutdown and tiered shutdown policies to illustrate the value of the patient-specific approach and compare nation-guidance and center-specific policies to illustrate the value of the center-specific approach. Whereas the center-specific tiered shutdown policy is a more accurate response to a pandemic, its implementation presents potential challenges related to data collection, empirical estimation, and patient selection.

Finally, from an operations management perspective, we analyze how capacity constraints affect the loss of patient life months and the length of the waiting list. We find that, as the reduction in the overall capacity increases, both the loss of patient life months and the average number of extra patients on the waiting list increase. Interestingly, the impact of capacity constraints on both the loss of patient life months and the average number of extra patients on the waiting list is nonlinear.

The results of this study are useful to decision makers in deciding whether and how to pause liver transplants during a pandemic. The results are also useful to patients (and their care providers) who are waiting for liver transplants. Though this study focuses on liver transplants, our model can be applied to many other settings such as kidney transplants, cancer surgeries, and elective surgeries.

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ENDNOTES
1 More details are available at https://wapo.st/3GCqFvk.

2 Patients may be removed from the waiting list due to other reasons such as relocating to other states or transferring to other centers. We designate these reasons collectively as inactivations.

3 More details are available at https://data.covid.umd.edu/.

4 More details are available at https://data.covid.umd.edu/.

5 More details are available at https://www.ncbi.nlm.nih.gov.

6 More details are available at https://unos.org/policy/liver/distribution/.

7 More details are available at https://unos.org/wp-content/uploads/unos/MELD_PELD.pdf.

8 More details are available at https://optn.transplant.hrsa.gov/media/1575/policynote_20151101.pdf.

9 Because our data do not track patients who become inactive, we assume the expected life months of these patients are similar to those without organ transplants (i.e., \( y_{mm} = y_{inm} \)). This is a reasonable assumption because patients who withdraw from an organ transplant experience natural life expectancy. For patients who withdraw and relocate to other states or transfer to other centers, although they may still receive transplants at other places, from the perspective of the focal center, it is as if these patients have a natural life because the focal center’s decision no longer affects these patients’ life expectancy.

10 The threshold probability is nonlinear because the waitlist mortality rate and the benefit of receiving organ transplants are heterogeneous across patient categories.

11 More details are available at https://unos.org/policy/liver/distribution/.

12 See Appendix B in the Supporting Information for center-level analyses.

13 Figure C1 in the Supporting Information depicts the reduction in the overall capacity and the loss of patient life months in percentage numbers.

14 Figure C2 in the Supporting Information depicts the reduction in the overall capacity and the average number of extra patients on the waitlist in percentage numbers.

15 More details are available at https://www.cdc.gov/vaccines/covid-19/important-products/index.html.

16 More details are available at https://www.yalemedicine.org/news/5-things-to-know-delta-variant-covid.

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**SUPPORTING INFORMATION**

Additional supporting information may be found in the online version of the article at the publisher’s website.