THE END OF THE REIONIZATION EPOCH PROBED BY Lyα EMITTERS AT z = 6.5 IN THE SUBARU DEEP FIELD1,2

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ABSTRACT

We report an extensive search for Lyα emitters (LAEs) at z = 6.5 in the Subaru Deep Field. Subsequent spectroscopy with Subaru and Keck identified eight more LAEs, giving a total of 17 spectroscopically confirmed LAEs at z = 6.5. Based on this spectroscopic sample of 17, complemented by a photometric sample of 58 LAEs, we have derived a more accurate Lyα luminosity function of LAEs at z = 6.5, which reveals an apparent deficit at the bright end of ~0.75 mag fainter L*, compared with that observed at z = 5.7. The difference in the LAE luminosity functions between z = 5.7 and 6.5 is significant at the 3 σ level, which is reduced to 2 σ when cosmic variance is taken into account. This result may imply that the reionization of the universe has not been completed at z = 6.5. We found that the spatial distribution of LAEs at z = 6.5 was homogeneous over the field. We discuss the implications of these results for the reionization of the universe.

Subject headings: cosmology: observations — early universe — galaxies: formation — galaxies: high-redshift

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1. INTRODUCTION

The cosmic reionization was undoubtedly one of the major turning points in the early universe. The measurement of cosmic microwave background (CMB) temperature polarization by the Wilkinson Microwave Anisotropy Probe (WMAP) implies an early reionization at z = 10.9+2.7−2.3 (Page et al. 2006), and the complete Gunn-Peterson trough of Sloan Digital Sky Survey (SDSS) QSOs suggests that cosmic reionization ended at z ~ 6 (Fan et al. 2002). There are disputes over when and how the reionization has taken place and which objects were responsible for it. Although QSOs are expected to be the main contributor of ionizing photons at the bright end of the luminosity function (LF) of ionizing sources, the QSO population alone cannot account for all the required ionizing photons (Willott et al. 2005), and star-forming galaxies like Lyman break galaxies (LBGs) and Lyα emitters (LAEs) at the reionization epoch are the only alternatives that could dominate at the faint end. The census of observable galaxies at this epoch is sensitive to the ionization fraction of the universe (Yan & Windhorst 2004; Malhotra & Rhoads 2004; Bouwens et al. 2005; Stiavelli et al. 2005; Bunker et al. 2006). It is expected that the surrounding neutral intergalactic medium (IGM) attenuates the Lyα photons so significantly that the number density decline of LAEs provides a useful observational constraint on the reionization epoch (Haiman & Spaans 1999; Rhoads & Malhotra 2001; Hu et al. 2002).

There have been great advances over the past three years in detecting distant galaxies at the edge of the cosmic reionization era beyond z = 6 in both dropout searches (Dickinson et al. 2004; Bouwens et al. 2003, 2005; Kneib et al. 2004; Pello et al. 2004; Stanway et al. 2005) to find their strong Lyman breaks and narrowband (NB) searches (Hu et al. 2002; Cuby et al. 2003; Ajiki et al. 2003; Kodaira et al. 2003; Rhoads et al. 2004; Malhotra & Rhoads 2004; Taniguchi et al. 2005) to detect their Lyα emission lines. Complementary to these photometric surveys are direct spectroscopic approaches based on slitless spectroscopic searches (Kurk et al. 2004; Malhotra et al. 2005) and blind slit searches (Tran et al. 2004; Martin et al. 2006). The Subaru Telescope plays an important role in these challenging searches for high-z populations, in particular, in the Subaru Deep Field (SDF).

The major goal of this project is to construct large samples of LBGs at z ~ 4–5 and of LAEs at z ~ 4.8, 5.7, and 6.6, and to make detailed studies of these very high-z galaxy populations. The SDF’s wide-field imaging increases the chance of discovering rare
objects, such as the most distant galaxies. In addition to the improved detectability, the wide field of view is less sensitive to the potentially large cosmic scatter in the reionization history (Barkana & Loeb 2004; Somerville et al. 2004). Following our first discovery of a couple of LAEs at \( z = 6.5 \) (z6p5LAEs; Kodaira et al. 2003), Taniguchi et al. (2005, hereafter T05) have revealed for the first time a statistically useful sample of nine spectroscopically identified z6p5LAEs and estimated their total amount of star formation rate density at this high-\( z \) end. Nagao et al. (2004, 2005) also serendipitously discovered strong Ly\( \alpha \) emission at \( z > 6 \) from an \( i' \)-drop-selected sample in the SDF. Our SDF LAE sample was obtained from a general blank field without resorting to amplification of gravitational lensing by foreground clusters, providing reliable statistics about their number density, LF, and cosmic star formation rate density. High-\( z \) surveys using gravitational lensing are complementary to our survey, because they detect low-luminosity sources (Ellis et al. 2001; Hu et al. 2002; Santos 2004; Kneib et al. 2004).

In this paper, we report the discovery of eight additional spectroscopically identified z6p5LAEs, which enables a more accurate estimation of their LF. The LF beyond \( z = 6 \) puts a critical constraint on the reionization epoch, as well as on the ionizing photon budget. The Ly\( \alpha \) photons are absorbed when passing through the neutral IGM; therefore, it is naturally expected that the LF of LAEs should decline as it traces earlier times in the reionization epoch. Consequently, the observed abundance of LAEs during the reionization period should indicate the neutral fraction of IGM hydrogen \( x_{H_1}^{\text{IGM}} \) (Miralda-Escude & Rees 1998; Malhotra & Rhoads 2004) and Stern et al. (2005) found no significant evolution of the LF between \( z = 5.7 \) and \( 6.5 \), implying that the neutral fraction of the universe is already low at \( z = 6.5 \). However, their LF estimate at \( z = 6.5 \) was poorly determined, since it was combined from several independent data sets with different selection criteria. On the other hand, there are updated model predictions for the LAE’s LF during the reionization epoch (Haiman & Spaans 1999; Le Delliou et al. 2005; Haiman & Cen 2005).

In addition, we evaluate the inhomogeneity of the sky distribution for our z6p5LAE sample. The high-\( z \) galaxy survey in a general field also has an advantage for determining spatial clustering. The \( i' \)-dropout method generally samples a wide redshift range at \( 5.7 < z < 6.2 \), which corresponds to a comoving distance as deep as \( \approx 200 \) Mpc along the line of sight. The large-scale structure within this large volume probed by the \( i' \)-dropout method would be diluted in sky projection and thus cannot be revealed unless large spectroscopic samples are obtained. On the other hand, NB searches exploring only a small redshift range are more sensitive to the large-scale structure, although their thin slices of the universe are, at the same time, likely to be affected by cosmic variance (Shimasaku et al. 2004).

The detection of an inhomogeneous distribution of galaxies beyond \( z = 6 \) would be of great interest not only because it would reveal the primeval large-scale structure (Stiavelli et al. 2005; Malhotra et al. 2005; Ouchi et al. 2005), but also because it could provide evidence of patchy reionization, in which Ly\( \alpha \) flux is attenuated in one field and not in the other. In the reionization epoch, ionizing sources like LAEs would make cosmological \( H \) \& regions around them (Miralda-Escude et al. 2000). The ionized spheres around adjacent LAEs will overlap, and the space overdensity of these ionizing sources would form a large enough \( H \) \& region around them to allow high transmission of their Ly\( \alpha \) photons prior to reionization (Wyithe & Loeb 2005; Furlanetto et al. 2006). The maximum extent of the overlapped ionized regions is predicted to be \( \approx 10 \) physical Mpc (Wyithe & Loeb 2004; Furlanetto & Oh 2005), which is comparable to the field of view of the SDF.

A measurement of inhomogeneity in the spatial distribution of such a high-\( z \) population would draw a much more precise picture of the reionization process than has been previously possible. This paper is organized as follows. In §2, we describe our new spectroscopically identified z6p5LAE sample. In §3, we derive the Ly\( \alpha \) LF of our z6p5LAE sample making comparison with LFs at \( z = 5.7 \). An estimate of inhomogeneity in the sky distribution for our z6p5LAE sample is presented in §4. We present the composite spectrum of our spectroscopically confirmed z6p5LAE sample in §5. Some discussions of the implications for reionization based on our results are made in §6, and the summary of the paper is given in §7.

Throughout the paper, we analyze in the flat \( \Lambda \)CDM model: \( \Omega_m = 0.3, \Omega_\Lambda = 0.7, \) and \( H_0 = 70 \) \( h_{70} \) km s\(^{-1}\) Mpc\(^{-1}\). These parameters are consistent with recent CMB constraints (Spergel et al. 2006). Magnitudes are given in the AB system.

2. NEW SPECTROSCOPIC CONFIRMATION

Our z6p5LAE photometric candidate sample in the SDF was presented in T05, in which sample selection and star formation rate density were discussed. The sample was based on the flux excess objects in narrowband NB921 (\( \lambda_c = 9196 \) Å, FWHM = 132 Å) image compared with the very deep broadband images of the SDF (Kashikawa et al. 2004). Our comoving survey volume was as large as \( 2.17 \times 10^5 \) \( h_{70}^{-3} \) Mpc\(^3\). In T05, we found 58 photometric candidates of z6p5LAEs down to NB921 = 26.0 (5 \( \sigma \)) in the effective survey region of 876 arcmin\(^2\); nine of them had been confirmed as real by spectroscopy. In this section, we describe our extended spectroscopic confirmations of z6p5LAEs after T05. Table 1 summarizes our spectroscopic identifications of NB921-excess objects in the SDF over the last three years.
summary, we have hitherto taken spectroscopy for 22 objects that meet the photometric selection criteria of z6p5LAE and confirmed that 16 are really LAEs based on their asymmetric line profiles, one is an \([\text{O} \text{ iii}]\) emitter, and five are faint single-line emitters. We have also included another spectroscopically identified z6p5LAE discovered serendipitously.

2.1. Keck II DEIMOS Spectroscopy

The z6p5LAE candidates were observed with the Keck II DEIMOS (Faber et al. 2003) spectrograph on UT 2004 April 23–24. We also allocated slits for NB921-strong (\(z' > \text{NB921} > 1\)) emitters, irrespective of their (\(i' - z'\)) color as a LAE criterion in order to see how our selection criteria work. We used four multi-object spectroscopic (MOS) masks with an 830 line mm\(^{-1}\) grating and a GG495 order-cut filter for each 7000–9000 s. integration time. The central wavelength was set to 7500 Å for one of the four MOS masks and 8100 Å for the other three masks. The slit width was 1.0 with 0.47 pixel\(^{-1}\), giving a resolving power of ~3600. The wavelength coverage was ~5000–10,000 Å, depending on position in the mask. The typical seeing size was 0.55–1.0 during the observation. Our z6p5LAEs were almost spatially unresolved on an NB921 image with 0.98 seeing size. Assuming that our LAEs were also spatially unresolved on the slits, the effective spectral resolution may be better, depending on the source size (Rhoads et al. 2003). We also obtained spectra of standard stars BD +28 4211 and Feige 110 for flux calibration. The data were reduced with the spec2d pipeline\(^16\) for DEEP2 DEIMOS data reduction.

We allocated slits for 18 target z6p5LAE candidates, as well as NB921-strong emitters. Four of them were apparent \([\text{O} \text{ iii}]\) emitters showing their characteristic double lines and sometimes also H\(\beta\), one was an H\(\alpha\) emitter that has corresponding \([\text{O} \text{ iii}]\) emission, four were \([\text{O} \text{ ii}]\) doublets, five have apparently asymmetric single lines, and we did not obtain any signal from four targets.

2.2. Subaru FOCAS Spectroscopy

Three z6p5LAE candidates were also observed with the Subaru Faint Object Camera and Spectrograph (FOCAS) (Kashikawa et al. 2002) spectrograph in the MOS mode on UT 2004 April 24–27. Although our primary targets for this observation were \(z = 5.7\) LAEs (Shimasaku et al. 2006) in the SDF, three slits were allocated for the z6p5LAE sample. We also allocated slits for strong NB921 emitters. The spectroscopy was made with a 300 line mm\(^{-1}\) grating and an O58 order-cut filter. The spectra cover 5400–10,000 Å, with a pixel resolution of 1.34 Å. The 0.06 wide slit gave a spectroscopic resolution of 7.1 Å at 9200 Å (\(R \sim 1300\)). The spatial resolution was 0.3 pixel\(^{-1}\) with 3 pixel on-chip binning. The integration time was 12,000–16,800 s. The sky conditions were fairly good with a seeing of 0.4–0.8. The data were reduced in a standard manner. We also obtained spectra of standard stars Hz 44 and Feige 34 for flux calibration.

We allocated slits for 21 targets: 14 of them were apparent \([\text{O} \text{ iii}]\) emitters showing their double features and in some cases, H\(\beta\); one was an H\(\alpha\) emitter that has corresponding \([\text{O} \text{ iii}]\) emission; two had apparently asymmetric single lines; two had symmetric lines; and we did not obtain any signal for the two remaining targets.

2.3. Spectroscopic Results

We combined our spectroscopic sample with those reported in T05, in which nine LAEs and five single emitters are contained. One object, SDF J132520.4+273459, which was classified as a \([\text{O} \text{ iii}]\) emitter, was also observed with the FOCAS (DEIMOS). The sky spectrum is overplotted on the bottom panel with an arbitrary flux scale. The spectrum of SDF J132518.4+272122, which was identified as a LAE in this study, already appeared in T05. [See the electronic edition of the Journal for a color version of this figure.]

\(^{16}\) The data reduction pipeline was developed at University of California, Berkeley, with support from National Science Foundation grant AST 00-71048.
single emitter in T05, was reobserved with DEIMOS and was found to be a LAE based on the resulting better quality spectrum. We also obtained spectra for four [O iii] emitters and three single emitters classified as NB921 strong emitters in the same MOS observation, although these objects do not satisfy the LAE criteria and were not reported in T05. The total spectroscopic sample for this study comprises 53 objects.

It is difficult to identify a LAE at very high z with little continuum flux and a tiny signature of Lyα emission. The asymmetric line profile is the best diagnostic of high-z Lyα emission, which results from absorption by neutral hydrogen; therefore, it strongly depends on the ionization structure in and around the high-z objects. Although some bright LAEs show the continuum breaks (Kodaira et al. 2003) caused by IGM attenuation, most are too faint to detect the break at the highest z epoch. We have no other spectral features but asymmetric emission profiles that can distinguish high-z LAEs from foreground [O iii], [O iii], or Hα emitters. To quantify this asymmetry, we introduced an asymmetry statistics skewness S and weighted skewness Sw. Here we regarded the observed spectrum, which is basically a two-dimensional area of the flux (f(x)) and the pixel coordinate (x), as a distribution function with an array size of n. The S statistic is defined as

$$S = \frac{1}{\sigma^2} \sum_{i=1}^{n} (x_i - \bar{x})^3 f_i,$$

where I = \sum_{i=1}^{n} f_i, and \( \bar{x} \), \( \sigma \) are the average and dispersion of \( x_i \), respectively. The S indicator has an advantage of being independent of the line-profile modeling or fitting procedure. Our statistic S has a good correlation with other asymmetry indicators, \( a_i \) or \( a_f \) (Rhoads et al. 2003), as shown in the Appendix.

The weighted skewness Sw is the revised indicator of S so as to be more sensitive to an asymmetry; however, it does depend on the fitting procedure. We define the weighted skewness Sw as

$$S_w = S(\lambda_{10, r} - \lambda_{10, b}),$$

where \( \lambda_{10, r} \) and \( \lambda_{10, b} \) are the wavelengths where the flux drops to 10% of its peak value on the red and blue sides of the Lyα emission, respectively.

In this study, we classified our observed emission lines based on the Sw indicator as shown in the Appendix. Table 1 summarizes the identifications for our 53 spectra. We have identified apparent foreground emitters, including two Hα emitters, 22 [O iii] emitters, and four [O iii] emitters, by their multiple emission-line signatures. The properties of these emission-line galaxies at z < 1.2 will be presented in our forthcoming paper (Ly et al. 2006). The S value of these apparent foreground emitters never exceeds Sw = 3, which we set as the critical Sw value to distinguish LAEs from foreground emitters. This critical value is the same as for our z = 5.7 LAE sample (Shimasaku et al. 2006). As a result, we have so far obtained 17 LAEs at z = 6.5. All of the nine LAEs identified in T05 were classified as LAEs according to the Sw criterion, and we obtained eight additional spectroscopic confirmations of LAEs in this study.

The spectra of newly identified LAEs in this study are shown in Figure 1, and their spectroscopic properties are summarized in Table 2. For all eight LAE spectra, we did not detect any UV continuum fluxes significant enough to measure their equivalent widths reliably. Nor did we detect N v \( \lambda \lambda 1240 \), the only accessible strong high-ionization metal line indicative of AGN activity. We discuss the composite spectrum in §5. Figure 2 presents postage stamp images of these eight LAEs in all seven bands.

We have also eight single-line emitters in which we detected neither an asymmetric line having as large Sw as a LAE, nor doublet features as in the [O iii] emitters. Probably most of these are unresolved [O ii] doublet lines, based on their small Sw. In fact, all of these single lines were observed by Subaru FOCAS, whose data lacked the resolving power to separate the [O ii] doublet (\( \Delta \lambda = 6.64 \) Å) at 9160 Å. Our 58 photometric LAE candidates down to NB921 = 26.0 (5 \( \sigma \)) were selected in T05 based on the criteria that \( z' - NB921 > 1 \), \( \zeta' - NB921 > 3 \), and \( z' - z'' > 1.3 \) at \( i' < 27.87 \) (2 \( \sigma \)) and simply \( z' - NB921 > 1 \) at \( i' > 27.87 \) (2 \( \sigma \)). We also adopted another criterion for LAE candidates with no detections (<3 \( \sigma \)) in deep B-, V-, and R-band images. The 53 objects for which we obtained spectra are composed of LAE candidates and NB921-strong emitters. Twenty-two

\[17\] SDF J132518.4+272122 was classified as a single emitter in T05, although it shows a very red color (\( i' - z'' > 2.21 \)) and high enough Sw (0.173) and Sw (4.75) values. We therefore classify it as a LAE in this study.
of these 53 objects meet the criteria for our photometric sample: 16 are LAEs, one is an [O iii] emitter, and five are single-line emitters. We have another spectroscopically identified LAE that was not listed in the LAE candidate list by T05. The object is listed as No. 59 in Table 2 and is found to have a very close neighbor in the $i'$-band image (see Fig. 2), which prevented accurate aperture photometry. Sixteen LAEs meet our selection criteria out of our spectroscopic LAE sample of 17, indicating $16/17 = 94\%$ sample completeness, provided that all eight single-line emitters are foreground objects. Otherwise, the sample completeness is $(16+5)/(17+8) = 84\%$ at most, if all of the single emitters are z6p5LAEs. The simple average of these two extreme cases, 89%, is regarded as the sample completeness.

On the other hand, the sample contamination rate is estimated as follows. One [O iii] emitter satisfies our LAE criteria, suggesting a $1/22 = 4.5\%$ contamination rate. The contamination rate could be $(1+5)/22 = 27\%$ at most if all of these five single emitters were foreground objects. The contamination rate is estimated to be 16% by taking the average of these two cases. Therefore, our sample reliability factor, determined as the ratio of the number of true LAEs to the number of objects that meet our selection criteria, is evaluated to be $(1-0.16)/0.89 = 0.94$. One object found to be an apparent [O iii] emitter by spectroscopy

No. 29 in T05. This object is located near a bright star so that accurate photometry is prevented.

Fig. 2.—Thumbnail images of our eight identified LAEs. The object IDs are those of T05, except ID=59, which is not listed in the photometric catalog of T05. The $B$, $V$, $R$, $i'$, NB816, $z'$, and NB921-band images are shown from left to right. Each image is 10$^\prime$ on a side. North is up, and east is to the left. [See the electronic edition of the Journal for a color version of this figure.]
was removed from the photometric sample, whereas one LAE that happened to be found by spectroscopy but was not listed in the original candidate sample of T05 was included in the photometric sample. In the following analysis, we used this photometric sample. There were six objects for which we did not obtain any signals in spectroscopy. Five of them have NB921 > 25.5, which is close to the current spectroscopic limit.

Figure 3 shows the peak wavelength distribution of 17 confirmed LAEs, as well as 28 foreground emitters within the NB921 bandpass. The distribution of LAEs shows an apparent systematic deviation to the blue side of the NB transmission curve, in contrast to the symmetric distribution of foreground emitters. This is because of the fact that the LAE profile, having a broad red wing and sharp blue cutoff, as well as a Lyman continuum break, makes a larger NB excess when it lies at the shorter side of the transmission curve. This was also the case for LAE surveys at z = 5.7 with NB816 (Shimasaku et al. 2006; Hu et al. 2004).

3. Lyα LUMINOSITY FUNCTION

We estimated the LF of z6p5LAEs based on both our spectroscopic sample of 17 and our photometric sample of 58. The LF can be simply derived from the number density of confirmed LAEs multiplied by the spectroscopic confirmation fraction (Malhotra & Rhoads 2004; T05); however, the uncertainty in this fraction inevitably depends on the magnitude because spectroscopic confirmation is more difficult at fainter magnitudes. Thus, we estimated the range of acceptable z6p5LAE LFs as specified by the upper and lower limits.

The lower limit to the z6p5LAE LF is based on our spectroscopic z6p5LAE sample of 17, whose Lyα emission has been securely detected, although this sample is incomplete. The upper limit was estimated from the combined spectroscopic and photometric samples. The Lyα and rest-UV continuum (at 9500 Å) fluxes of our photometric sample were inferred from the NB921 and z'-band photometry using equations (7) and (6) of T05, respectively. Note that we derived the apparent Lyα luminosity uncorrected for either the dust extinction or the self-absorption evident on the blue-side cutoff of the emission line. The comparison of Lyα fluxes measured spectroscopically with those inferred from photometry for our spectroscopic z6p5LAE sample is shown in Figure 4. The correspondence is good except in a few cases. One object far out of agreement is found to have a spectrum affected by bad columns. We therefore used the photometric inferred Lyα fluxes for the remaining 41 (= 58 − 17) objects in the photometric sample.

We have to correct for detection completeness, which could crucially affect the result when calculating the LF based on a deep photometric catalog. The detection completeness as a function of apparent NB921 magnitude was estimated in almost the same way as in Kashikawa et al. (2004), that is, by counting detected artificial objects distributed on the real NB921 image. We assumed Gaussian profiles of FWHM = 1′13 for these artificial objects, which is the nominal size of our z6p5LAE sample objects (T05). The detection completeness was thus evaluated as >75% for NB921 < 25.0 and 45% at the limiting magnitude of NB921 = 26.0. In the upper limit estimate, we corrected for this detection incompleteness by number weighting according to the NB921 magnitude. Note that the upper limit can be regarded as our current best estimate for the z6p5LAE LF, because it is properly corrected for the detection incompleteness.

Figure 5 shows the cumulative Lyα LF of our z6p5LAE sample. The open circles denote the raw counts of the spectroscopic + additional photometric sample, and the filled circles are those with corrected detection completeness. The triangles denote the raw counts of the pure spectroscopic sample. Therefore, the triangles and circles are the lower and upper limits, respectively, of our estimates of the z6p5LAE LF. The error bars on the filled circles just denote the Poisson errors, although there may be other plausible error sources, such as an ambiguity in inferring the Lyα luminosity from photometric data. Taking into account the corrections with respect to the sample reliability factor (94%) evaluated in the previous section, the LF has a margin to go upward by a factor of 1.06, although this uncertainty is smaller than...
The short-dashed and dotted lines show the Schechter LFs, in which the Ly \textit{α} line is the most reliable estimate so far because of the deeper photometric data, which could affect the resulting LF to some degree. When using only the photometric inferred Ly\textit{α} luminosities for our entire 58 object sample, the best-fit Schechter parameters only change by at most \( \Delta \log (L') = 0.04 \) and \( \Delta \log (\phi') = 0.1 \) for \(-2.0 < \alpha < -1.0\), which is negligible. Moreover, we carried out a Monte Carlo simulation to investigate any possible distortion that the discrepancy between spectroscopically measured and photometrically inferred Ly\textit{α} luminosities could cause in the resulting LF. We recalculated the LF many times after assigning a random error perturbed within the same scatter as in Figure 4 to each Ly\textit{α} luminosity. With this simulation, the best-fit Schechter parameters vary with rms fluctuations of \( \sigma (\log (L')) = 0.019 \) and \( \sigma (\log (\phi')) = 0.032 \) for fixed \( \alpha = -1.5 \), suggesting again that the errors in inferring the Ly\textit{α} luminosity are expected to be small.

At lower \( z \) (3.0–5.7), several LAEs with large \( L(L\textit{Ly} \alpha) > 2 \times 10^{43} \ h_{70}^{-2} \) ergs s\(^{-1}\) have been actually identified by spectroscopy with much higher number density (Shimasaku et al. 2006; Hu et al. 2004; Maier et al. 2003; Kudritzki et al. 2000; Cowie & Hu 1998), whereas our z6p5LAELF sample includes no spectroscopically confirmed objects of such large Ly\textit{α} luminosity. Three other LAEs at \( z \sim 6.5 \) have been spectroscopically identified so far in independent surveys (Rhoads et al. 2004; Kurk et al. 2004; Stern et al. 2005) without taking advantage of the amplification by a foreground gravitational lens. All of these LAEs also have similar Ly\textit{α} luminosities of \( L(L\textit{Ly} \alpha) = 1.04–1.1 \times 10^{43} \ h_{70}^{-2} \) ergs s\(^{-1}\), consistent with our brightest LAEs.

On the other hand, at fainter luminosities of \( L(L\textit{Ly} \alpha) < 5 \times 10^{42} \ h_{70}^{-2} \) ergs s\(^{-1}\), our upper limit estimate of the z6p5LAELF almost reaches the same amplitudes as that at \( z = 5.7 \), although the amplitude difference between our upper and lower limits is too large to constrain its faint end. Our faint spectroscopic sample is still too small to establish whether there is a significant difference between the faint end of the LF at \( z = 6.5 \) and 5.7. In this study, we cannot determine the faint-end slope of the LAE LF at \( z = 6.5 \), and consequently it is difficult to constrain the true contribution of the LAE population to the entire photon budget required for full reionization.

### Table 3

| Sample | Limit | \( \alpha \) (fix) | \( \log (L'/h_{70}^2) \) ergs s\(^{-1}\) | \( \log (\phi'/h_{70}^3) \) Mpc\(^{-3}\) |
|--------|-------|-------------------|-------------------------------|--------------------------------|
| \( z = 6.5 \) | Upper | -2.0 | 42.74 ± 0.14 | -3.14^{+0.30}_{-0.34} |
| | 1.5 | 42.60^{+0.12}_{-0.14} | -2.88^{+0.24}_{-0.26} |
| | -1.0 | 42.48^{+0.10}_{-0.10} | -2.74^{+0.18}_{-0.18} |
| Lower | -2.0 | 43.30 ± 0.23 | -4.80^{+1.02}_{-1.02} |
| | 1.5 | 42.95^{+0.10}_{-0.09} | -4.17^{+0.10}_{-0.09} |
| | -1.0 | 42.75^{+0.12}_{-0.12} | -3.88^{+0.28}_{-0.28} |
| \( z = 5.7 \) | Upper | -2.0 | 43.30^{+0.12}_{-0.12} | -3.96^{+0.32}_{-0.32} |
| | 1.5 | 43.04^{+0.14}_{-0.16} | -3.44^{+0.16}_{-0.16} |
| | -1.0 | 42.84 ± 0.10 | -3.14^{+0.12}_{-0.12} |

The equivalent width of the Ly\textit{α} line are expected to be small at the bright end. As seen in Figure 4, there are possible but unsystematic errors in inferring the Ly\textit{α} luminosity from photometric data, which could affect the resulting LF to some degree.
bright end. Moreover, our survey comoving volume is comparably as large as others at $z = 5.7$ (Shimasaku et al. 2006; Hu et al. 2004). As seen in Figure 3, our effective survey depth is smaller than that estimated from the FWHM of the NB filter; however, it is more or less the same as for the $z = 5.7$ LAE sample, and its correction would not affect the result (Shimasaku et al. 2006). Therefore, our LF estimate of z6p5LAEs is highly reliable, although we cannot completely rule out the possibility that the deficiency at the bright end is caused by cosmic variance.

To illustrate the significance of the LF difference between $z = 6.5$ and 5.7, we plot the error contours for our Schechter-parameter fits in Figure 6. In this case, we compare only the upper limit LF estimate, which is the current best estimate for our z6p5LAE sample and is most appropriate for establishing the significance of the LF difference compared to $z = 5.7$. The confidence levels of the fitting were computed based on Poissonian error statistics. The best-fit parameters of the $z = 5.7$ LF are slightly different from those presented in Shimasaku et al. (2006), in which Schechter parameters were determined so as to be consistent with the NB816 number count. In contrast, here we determined these parameters simply by fitting a Schechter function to the data points. Figure 6 reveals that the $(L^*, \phi^*)$ error ellipses for $z = 5.7$ and 6.5 do not overlap each other for any $\alpha$; that is, the difference in LF between $z = 5.7$ and 6.5 is significant at more than the 3 $\sigma$ level. The difference in $L^*$ is more significant than that in the $\phi^*$. Based on Somerville et al. (2004), we evaluated the cosmic variance of our z6p5LAE sample. We assumed a one-to-one correspondence between LAEs and dark halos, and used their predictions at $z = 6$. With the comoving survey volume of $2.17 \times 10^5 h_{70}^{-3}$ Mpc$^3$ and the number density of $2.67 \times 10^{-4} h_{70}^{-3}$ Mpc$^{-3}$ (7.83 $\times$ 10$^{-5}$) for the upper (lower) limit estimate, we obtained a cosmic variance of $\sim 32\%$ ($\sim 37\%$). We also estimated a variance of $\sim 20\%$ for the $z = 5.7$ LAE sample. The possible field-to-field variance in the LF at $z = 5.7$ can be seen in Figure 11 of Shimasaku et al. (2006). As shown by the error bars in Figure 6, the 3 $\sigma$ error circles for the two epochs overlap each other when taking into account the cosmic variance; however, our upper limit estimate still differs from the $z = 5.7$ result at the 2 $\sigma$ level.

4. REST-UV CONTINUUM LUMINOSITY FUNCTION

In the previous section, the flux of the rest-UV continuum (at 9500 Å) was simultaneously derived from the NB921 and $z'$-band photometry. We derived the rest-UV (1255 Å at $z = 6.57$) continuum LF based on our photometric sample of 58 objects. The correction for detection incompleteness in NB921 was taken into account when calculating the LF, although the correction should actually be based on the completeness measured in $z'$-band, which corresponds to the rest-UV flux. However, as our Lyα-selected sample is basically constructed from an NB921 magnitude-limited sample, it is inevitable that the derived rest-UV continuum LF may be affected, especially at the faint end of the LF, by the difference in completeness of the NB921 and $z'$-bands. This is also the case for other LAE studies (Shimasaku et al. 2006; Hu et al. 2004).

Figure 7 shows the rest-UV continuum LF of our z6p5LAE sample compared with other studies at similar redshifts. No correction has been applied for dust. The vertical lines indicate the corresponding limiting magnitudes in $z'$-band. Our LF measurements at magnitudes fainter than $M_{UV} = -20.24$ (3 $\sigma$) may be uncertain because the corresponding $z'$-band magnitudes are no longer reliable. We overplot in Figure 7 other rest-UV continuum LF estimates of the SDF LAE sample at $z = 5.7$ (Shimasaku et al. 2006), the i-dropout objects at $z \sim 6$ of Bouwens et al. (2005), and the LAE sample at $z = 5.7$ of Hu et al. (2004). We neglect here a slight difference in corresponding rest-frame wavelengths ($\sim 1350$ Å at $z = 5.7$ and $\sim 1255$ Å at $z = 6.5$); assuming a flat far-UV spectral energy distribution. Our measurements agrees with these two studies very well at $M_{UV} < -20.5$. The agreement of the rest-UV continuum LF at the bright end for $z = 6.5$ and 5.7 is in clear contrast to the difference seen in the Lyα LF. It should be noted that the rest-UV continuum luminosity is not attenuated by the neutral IGM and is less affected by dust extinction than the Lyα luminosity. As far as the rest-UV continuum LF is concerned, cosmic variance is not severe for these samples. The flatter faint-end slope of the LFs of LAE samples at both $z = 6.5$ and 5.7 compared to that of i-dropouts at
$z \sim 6$ could be caused by the detection incompleteness of the LAE sample.

5. CLUSTERING PROPERTIES

Our sample of 58 z6p5LAE candidates have been extracted from a very wide field of view ($34' \times 27'$). We tried to detect a clustering signal in the z6p5LAE sample using several methods. We derived the angular two-point correlation function (ACF) $w(\theta)$ using the Landy & Szalay (1993) estimator. One hundred thousand random points were created with exactly the same boundary conditions as the SDF galaxy catalog, avoiding the mask regions in which saturated stars dominate. The top panel of Figure 8 shows the ACF for z6p5LAE. Circles denote the ACF for the 58 objects of z6p5LAE, whereas squares denote the 53 objects of the z6p5LAE sample, excluding five single-line emitters. We did not correct for the integral constraint, which is negligible in the SDF (Kashikawa et al. 2006). We estimated only Poissonian errors on $w(\theta)$, as in the previous section, we estimated the cosmic variance as

$$\sigma_n(\theta) = \{1 + w(\theta)/DD(\theta)\}^{1/2},$$

where $DD(\theta)$ is the number of random-random pairs having angular separation $\theta$. The result shows that the amplitude is almost zero for all scales, indicating that the sample has an almost homogeneous distribution. However, our z6p5LAE sample is so small that the derived ACF has a large ambiguity. Therefore, we also applied two other methods that are more robust for small number statistics to quantify the clustering strength.

First, we applied the two-dimensional Kolmogorov-Smirnov test to our sample. This test was generalized by Peacock (1983) to give the integral probability distribution in four quadrants around a certain point. To see the difference from a homogeneous distribution, we generated random points as for our ACF estimate. We found that our z6p5LAE sample was equivalent to a homogeneous distribution at the 83.3% (83.8% after removing the five single-line emitters) confidence level.

Second, we estimated the void probability function (VPF). The VPF is defined as the probability of having no galaxies in a randomly placed sphere of radius $R$, or in a circle of angular radius $\theta$ in the case of a two-dimensional sky distribution. The VPF is known to be related to the hierarchy of $n$-point correlation functions (White 1979). We adopted the same technique as Croton et al. (2004) to correct for the irregular geometry of the survey region. The result is shown as a solid line in the bottom panel of Figure 8, compared with that of a random sample indicated by the dashed line. No excess in the VPF was found for our z6p5LAE sample relative to the random sample.

These three estimates indicate that the spatial distribution of the z6p5LAE sample is homogeneous. The results were identical for all three estimates, even if we divided our sample into brighter/fainter subsamples. The homogeneous distribution of z6p5LAE is in contrast to that at lower $z$, where LAE populations are often found to trace the large-scale structures even in blank fields (Steidel et al. 2000; Shimasaku et al. 2003; Palunas et al. 2004; Ouchi et al. 2005).

As in the previous section, we estimated the cosmic variance as $\sim 32\%$ at most. We should note that NB searches exploring only a small redshift coverage are also sensitive to the large-scale structure (Shimasaku et al. 2004). We cannot rule out the possibility that we happen to see a very homogeneous region of the $z = 6.5$ universe. A survey of a much larger volume is required for further discussion.

6. Ly$\alpha$ PROFILE OF THE COMPOSITE SPECTRUM

Although each individual spectrum of our 17 z6p5LAEs has too low a signal-to-noise ratio (S/N) to infer either the internal...
First, we removed five spectra that have been taken with the poorest instrumental resolution. Each spectrum was then smoothed with an adequate Gaussian kernel chosen to produce a common instrumental resolution of FWHM = 6.41 Å. The instrumental resolution for each spectrum was practically measured from the FWHM of sky lines near the Lyα emission. The redshift was measured based on the line peak wavelength, then shifted to the mean redshift \( z = 6.556 \), and rebinned to a common pixel scale. In the process, we neglected possible systematic offsets of Lyα lines from the rest frame established by other lines, which are often found in LBG spectra (Shapley et al. 2003). The spectra were then combined by taking the average after scaling according to their peak line flux.

The top panel of Figure 9 shows the final composite spectrum from our 12 z6p5LAE sample. The composite spectrum reveals an apparently asymmetric profile with an extended red wing, which is shown clearly by a comparison with a Gaussian profile (dotted line) corresponding to the final instrumental resolution. The skewness and weighted skewness of the composite spectrum were \( S = 0.542 \pm 0.007 \) and \( S_W = 11.466 \pm 0.156 \), respectively. The blue side of the line profile is almost adequately explained by the instrumental resolution blur, as was also concluded by Hu et al. (2004) and Westra et al. (2005). Assuming that an intrinsic Lyα profile is a simple Gaussian at almost the same peak position as observed, and completely truncated at the blue side of the line, the resulting profile convolved with the instrumental resolution did not coincide with the observed profile, instead producing a large red-wing anomaly. This disagreement is inconsistent with the results for the \( z = 5.7 \) case by Hu et al. (2004).

To explain the observed profile, we considered two plausible models. The first model is the “galactic wind model” which was motivated by the similar analogy with Dawson et al. (2002) and Mas-Hesse et al. (2003). If galactic winds are present, the far side of the expanding shell back-scatters redshifting Lyα photons that would make another broadly extended Gaussian component in their line profile. We simply assumed that the Lyα photons from the blue side of the object redshift are completely absorbed by neutral hydrogen at the near side in lines of sight. This model is composed of two Gaussian profiles: one is a high-amplitude narrow Gaussian that originates from recombination Lyα photons in the central H II region, and the other is a low-amplitude broad Gaussian from Lyα photons back-scattered by a galactic wind. The middle panel of Figure 9 shows the best-fit galactic wind model. The resulting profile is shown by the solid line, which is the combination of narrow and broad Gaussians convolved with the instrumental resolution. It perfectly explains the observed profile. The best-fit parameters are listed in Table 4. The picture of large-scale outflowing of gas with velocities \( \sim 200 \) km s\(^{-1}\) is in good agreement with those of nearby H II galaxies (Kunth et al. 1998) but is somewhat smaller than those of \( z \sim 3 \) LBGs (Pettini et al. 2002) and \( z \sim 5 \) LAEs (Dawson et al. 2002; Westra et al. 2005).

The second model is the “reionization model”, in which the intrinsic Lyα line has a larger amplitude than that observed and its peak wavelength is much shorter than the observed peak position. Such a picture is generally predicted for the Lyα profile in the reionization epoch (Haiman 2002; Santos 2004). The Lyα photons would be absorbed by both the red damping wing of the Gunn-Peterson trough from outside the cosmological H II region and the residual neutral hydrogen inside the H II region. The latter’s true contribution is not yet known; thus, we simply assumed that the inside of the H II region is sufficiently optically thick to completely attenuate the blue side of the line. The damping wing scattering would be effective at wavelengths larger than

![Graph](image-url)

**Figure 9.**—The composite spectrum of our 12 z6p5LAE sample. The spectrum in the top panel shows the final composite spectrum. The dotted line denotes a Gaussian profile corresponding to the instrumental resolution. The middle panel shows the best-fit galactic wind model. The resulting profile is shown as a smooth solid line that is the combination of narrow and broad Gaussians convolved with the instrumental resolution. The bottom panel shows the reionization model. The resulting profile is shown as a smooth solid line that is the combination of the intrinsic Lyα profile and damping wing attenuation convolved with the instrumental resolution. See Table 4 for the best-fit parameters for each model. [See the electronic edition of the Journal for a color version of this figure.]

### Table 4

| Model            | Component | \( \lambda_e \) (Å) | Amplitude (ergs s\(^{-1}\) cm\(^{-2}\) Å\(^{-1}\)) | \( \sigma \) (km s\(^{-1}\)) | Offset (Å, km s\(^{-1}\)) |
|------------------|-----------|---------------------|-----------------------------------------------|--------------------------|--------------------------|
| Galactic wind... | Central H II | 9183.3               | 2.11E–17                                      | 3.32, 108.5              | –2.34, –76.5             |
|                  | Galactic wind | 9191.6               | 3.31E–18                                      | 7.93, 259.2              | +5.97, +195.1            |
| Reionization..... |           | 9179.9               | 9.00E–17                                      | 6.50, 212.4              | –5.70, –186.3            |

\(^{17}\) SDF J132518.4+272122 was classified as a single emitter in T05, although dynamics of the LAE itself or the IGM characteristics (e.g., Haiman 2002), the composite spectrum could be useful to see the general spectroscopic properties of the z6p5LAE population. We have 17 z6p5LAE spectra of different spectroscopic resolutions. First, we removed five spectra that have been taken with the poorest instrumental resolution. Each spectrum shows the best-fit galactic wind model. The resulting profile is shown as a smooth solid line that is the combination of narrow and broad Gaussians convolved with the instrumental resolution. The middle panel shows the reionization model. The resulting profile is shown as a smooth solid line that is the combination of the intrinsic Lyα profile and damping wing attenuation convolved with the instrumental resolution. See Table 4 for the best-fit parameters for each model. [See the electronic edition of the Journal for a color version of this figure.]
that corresponding to the blue edge of the H II region; thus, the red side of the line would be attenuated by the damping. We used the damping optical depth of Loeb et al. (2005). We further assumed the radius of the H II region to be 0.45 proper Mpc (Haiman 2002; Santos 2004).

The bottom panel of Figure 9 shows the cosmological H II region model fitting to the data, and the best-fit parameters are listed in Table 4. This model also explains the observed extended red wing fairly well. The predicted intrinsic Lyα luminosity from this model is 4.6 times that observed, which is roughly consistent with the case of Hu et al. (2002) and its model prediction by Haiman (2002). However, the transmission factor of ~20% of the total line flux is smaller than the factor of ~50% dimming suggested by the LF. Here, we neglect the possible luminosity dependence of Lyα attenuation, which was suggested by the LF shown in § 3. The discrepancy in Lyα attenuation between that implied by the line-profile model fitting and that from the LF difference can be reduced by assuming a larger radius for the H II regions. For example, we can obtain a ~40% transmission factor if the radius of the H II region is as large as ~0.90 proper Mpc.

Although we assume an optically thick core for the H II region, any escape of Lyα flux at the blue side would broaden the line profile, making the fit worse. We conclude that a larger contribution of the residual neutral hydrogen inside the H II region compared to the damping wing is required, although our data still lack the spectral resolution to make quantitative predictions of the density profile inside the H II region.

A better fit is obtained for the galactic wind model; however, our composite spectrum still has too low S/N and spectral resolution to determine which model is more plausible. It should also be noted that there is likely to be a scatter in FWHM among our LAE sample, and so it is unclear whether all of the LAEs have prominent red wings that appeared in the composite spectrum. While in the model, the radiative transfer process of Lyα photons through the emitting galaxy and the IGM is too complicated to justify every parameter based only on the line-profile fitting.

7. IMPLICATIONS FOR REIONIZATION

In this study, we found that the z6p5LAE LF has a clear deficit at its bright end compared with that at z = 5.7. The simplest interpretation is that the LAE population undergoes Lyα luminosity evolution from z = 6.5 to 5.7. Strictly speaking, the LAE population has some evolution in its EW from z = 6.5 to 5.7, given that we observe no evolution in the rest-UV continuum LF. The LAEs must be a very young population, having ongoing starbursts in so short period that even 100 Myr is a long time, over which their Lyα luminosity can easily drop. Nevertheless, the number density of LAEs does not change from z ~ 3 to z ~ 5.7. Thus, it is more natural to assume that this lack of LF evolution should extend up to z = 6.5, as opposed to the LAE population having strong evolution between z = 5.7 and 6.5. The number density decline from z = 5.7 to 6.5 could imply a substantial transition in the cosmic ionization state between these epochs. In this section, we offer a possible interpretation of these observational results in the context of the reionization of the universe, assuming that the nature of LAEs themselves has no drastic evolution between z = 5.7 and 6.5.

Assuming a fully ionized IGM at z = 5.7, the comparison of the LFs at z = 5.7 and 6.5 puts constraints on the neutral fraction of IGM hydrogen x H I at z = 6.5. The short-dashed and dotted lines in Figure 5 show the Schechter LF, in which the Lyα luminosities are reduced by a factor of 0.6 (L* × 0.6) and 0.4 from the LF at z = 5.7, which is still consistent with our upper and lower limit LF estimates, respectively. According to the IGM dynamical model of Santos (2004), a Lyα luminosity drop by ΔL* ~ 0.75 from the fully ionized IGM corresponds to x H I = 0.45. However, this predicted value is strongly model dependent, and even the model of Santos (2004) covers a wide range of acceptable models with different predictions of Lyα attenuation. The predicted value of x H I can be much smaller than 0.45 in some of these models. Therefore, our LF estimate could allow a neutral fraction of the IGM at z = 6.5 of 0 ≤ x H I ≤ 0.45. This upper limit of x H I at z ~ 6.5 is consistent with the recent results of Malhotra & Rhoads (2006) and Totani et al. (2006).

Haiman & Cen (2005) evaluated the LF evolution of LAEs, taking into account the luminosity dependence of the Lyα flux attenuation. In the epoch of reionization, ionizing sources like LAEs would make surrounding cosmological H II regions (Miralda-Escude et al. 2000). Based on the CDM model, the galaxies embedded in massive dark halos would collapse first, so that the ionizing sources in this era would be preferentially located in the high-density regions. The H II regions of the bright LAEs clustered in the overdense regions would overlap effectively and create a larger H II region with a high ionization fraction, which would significantly reduce the Lyα flux attenuation. As a result, it is predicted that bright LAEs should be readily observed, whereas faint LAEs are more severely attenuated. However, this luminosity dependence would just shift the Schechter LF downward by a certain factor according to x H I because the LF is steeper at the bright end. Our observed spectroscopic LF (lower estimate) is nearly consistent with such a trend, but our upper limit estimate of the z6p5LAE LF, which has a steep decline only at its bright end, is not. Our null result of finding any signals of bright LAE clustering is also inconsistent with this model. As Haiman & Cen (2005) suggested, the predicted LF profile strongly depends on the model assumptions, such as the constant escape fraction with respect to Lyα luminosity.

Assuming a clumpy IGM and discrete ionizing sources, there are two conflicting model predictions about the spatial inhomogeneity of reionization propagation. In a first phase of reionization, most of the sources are formed in high-density regions and ionize the dense gas around them. If the local neutral IGM around these sources is dense enough to allow higher recombination rates than ionization rates, the reionization will not complete in these high-density regions. Consequently, as in the model prediction by Miralda-Escude et al. (2000), H II regions would expand preferentially toward low gas density regions, and overdense regions would gradually be ionized after the epoch of overlap of cosmological H II regions (“outside-in” model). This picture is supported by hydrodynamic (Gnedin 2000) and N-body (Ciardi et al. 2003) simulations. On the other hand, if the local IGM density is low enough to help an efficient escape of Lyα photons, it is expected that the dense IGM region, in which a large H II region can be formed by overlap of ionized bubbles around high-luminosity sources, would be ionized first. It would then proceed to a void where it is dominated by only low-luminosity sources (“inside-out” model). Such a picture is predicted by Sokasian et al. (2003) and Furlanetto et al. (2006).

The key diverging point between these two models is the IGM density distribution, which Miralda-Escude et al. (2000) assume as an extrapolation from that at z = 3; however, the adequacy of that assumption is still uncertain (Furlanetto et al. 2006). These two contradictory models obviously have different predictions about the spatial distribution of observable galaxies at that epoch: galaxies residing in the underdense regions are easily observed in the outside-in model, whereas galaxies residing in the overdense regions are easily observed in the inside-out model. In turn, a more inhomogeneous galaxy distribution is predicted in
the inside-out model. Assuming that we are seeing the final stage of reionization through our observed z6p5LAE sample as deduced from the previous estimation of $0 \leq x_{\text{IGM}}^{\text{H}_1} \leq 0.45$, the homogeneous distribution found in this work agrees better with the outside-in model. Our assumed picture, in which the LAE overdense regions were still obscured by surrounding thick neutral IGM clouds at $z = 6.5$, is also consistent with our LF deficit in bright LAEs. Such an overdense region could be kept neutral until later epochs, trapping bright ionizing sources like luminous QSOs, in which the appearance of Gunn-Peterson troughs are detected at lower $z \approx 5.2 - 5.8$ (Becker et al. 2001; Djorgovski et al. 2001). Inhomogeneous reionization is also suggested by the significant variation in the IGM transmission among different QSO lines of sight (Djorgovski et al. 2006). In summary, implications for the reionization process suggested by this study are a high clumping factor of the IGM, and inhomogeneous reionization. Although we do not draw any further quantitative conclusions, we may be looking at only low-luminosity LAEs residing in low-density IGM regions at the end of the reionization epoch.

We plot in Figure 10 the relation between the local surface number density of LAEs and their Ly$\alpha$ luminosities, $L(Ly\alpha)$. The local surface number density is measured by the number of LAEs in a circle of 8 $h_7^{-2}$ Mpc radius. There is no apparent correlation between the local density and $L(Ly\alpha)$, again suggesting spatial homogeneity. It should be noted that the local number density in Figure 10 just accounts for our sample of LAEs, and at this point, there is no way of inferring the presence of other ionizing sources like Ly$\alpha$-dropout galaxies without strong Ly$\alpha$ emission. Nor did we find any clear relation between the local densities and FWHM of Ly$\alpha$ lines.

Figure 11 shows the FWHM of Ly$\alpha$ emission as a function of $L(Ly\alpha)$ for our spectroscopic z6p5LAE sample. There is a weak anticorrelation between FWHM and $L(Ly\alpha)$. Haiman & Cen (2005) predicted a similar correlation, which they proposed as an independent diagnostic of $x_{\text{IGM}}^{\text{H}_1}$, aside from the LF. The blue side of Ly$\alpha$ emission is dominantly attenuated by the residual H$\,^1$ regions, whereas the squares are from the photometric sample. [See the electronic edition of the Journal for a color version of this figure.] We plot in Figure 10 the relation between the local surface number density and the Ly$\alpha$ luminosity for our 58 z6p5LAE sample. The circles are from the spectroscopic sample, whereas the squares are from the photometric sample. [See the electronic edition of the Journal for a color version of this figure.] The local surface number density is measured by the number of LAEs in a circle of 8 $h_7^{-2}$ Mpc$^2$. The possible implications for reionization described above are still speculative because there are many unknown factors. First, we did not take into account the inherent galactic evolution of LAEs. It is suggested by previous studies that the number density of LAEs at $z = 3$ and 6 is almost unchanged, which is in contrast to the LBG population, which undergoes significant LF evolution from $z = 3$ to 6 (Ouchi et al. 2004; Bouwens et al. 2005; Yoshida et al. 2006). However, less than 20 LAEs have been confirmed spectroscopically, even at $z \approx 3$; this is not enough to determine the LF accurately. On the other hand, Bouwens et al. (2005) have found an evidence for evolution of the rest-frame continuum UV LF between $z \approx 3$ and 6. Also, there is no consensus on the spatial distribution of LAE at low redshifts. They might have an intrinsically homogeneous distribution. The inherent evolutions of Ly$\alpha$ flux, dust content, and neutral gas fraction inside LAEs themselves would also decrease the number density from $z = 5.7$ to 6.5. The complex escape mechanism of ionizing radiation from galaxies is unclear and depends strongly on assumed parameters, such as the escape fraction of Ly$\alpha$ photons, amount of dust, galactic wind, and star formation activity.
Our observed z6p5LAE LF could be more consistent with the quiescent hierarchical model prediction by Le Delliou et al. (2005) than with their model including an ongoing starburst. Finally, the IGM physical conditions during the reionization epoch are unknown, and no observational evidence has been found for the cosmological H\textsc{ii} region, which is the fundamental prediction of today’s reionization models. Although there are many ingredients to be considered, we conclude that our conjectures about reionization are plausible and provide a reasonable explanation of our results.

8. CONCLUSIONS

We carried out spectroscopic observations with Subaru and Keck to identify z6p5LAEs that were selected by NB excess at ~920 nm. Our conclusions can be summarized as follows.

1. We have identified eight new z6p5LAEs based on their significantly asymmetric Ly\textalpha emission profiles. This increases the sample of spectroscopically confirmed z = 6.5 LAEs in the SDF to 17.

2. We have constructed a large, homogeneous spectroscopic sample from the photometric sample of 58 LAE candidates to determine the Ly\textalpha LF at z = 6.5. The LF reveals an apparent deficit, at least at the bright end, compared to that at z = 5.7. The L* difference between z = 6.5 and 5.7 is ~0.75 mag for fixed α = −1.5. The difference has 3 σ significance, which decreases to 2 σ when we take into account cosmic variance. There may also be a decrease in comoving number density of LAEs from z = 5.7 to 6.5 at the faint end, although this conclusion could be modified by further follow-up spectroscopy.

3. The rest-UV continuum LF of our LAE sample at z = 6.5 is almost the same as that of the LAE sample at z = 5.7 and the i-dropout sample at z ~ 6, even at their bright ends.

4. The spatial distribution of z6p5LAEs was found to be homogeneous over the field, based on three independent methods to quantify the clustering strength. We cannot rule out the possibility that we happen to see a very homogeneous region of the z = 6.5 universe.

5. The composite spectrum of the 12 z6p5LAE objects with high spectral resolution clearly reveals an asymmetric Ly\textalpha profile with an extended red wing. The profile can be explained by either a galactic wind model composed of double Gaussian profiles or by a reionization model expected for a typical profile during the reionization epoch.

6. Our results could imply that the reionization of the universe has not been completed at z = 6.5. The decline of the z6p5LAE LF implies 0 ≤ x_{\text{H\textsc{ii}}} ≤ 0.45 based on the IGM dynamical model of Santos (2004). We conjecture that we are observing the final stage of reionization at z = 6.5, when the LAE overdense regions were still obscured by surrounding thick, neutral IGM clouds, which qualitatively agrees with our results of deficient bright LAEs and their homogeneous spatial distribution.

Our z6p5LAE spectroscopic sample is not yet large enough to make a more precise comparison with LFs at lower redshifts. At the moment, it is not clear whether the true LF of z6p5LAEs is closer to our upper or lower limit estimates. Thus, we do not conclude whether differences in L* or φ dominate in the disagreement of LF between z = 6.5 and 5.7. In this study, we could not constrain α, the faint-end slope of the LF. The faint end of the z6p5LAE sample would critically determine the LAE contribution as ionizing sources to the photon budget of cosmic reionization. Even if the number density of LAEs is low, a significant number of another star-forming population, LBGs, if they exist at this high-z epoch, could complete the reionization. Alternatively, only a small number of galaxies with huge star formation rates at very high redshift can reionize the universe (Panagia et al. 2005; Mobasher et al. 2005). It is too difficult to sample LBGs at exactly the same redshift as LAEs, whereas it is not certain what fraction of LBGs at this epoch shows strong enough Ly\textalpha emission to be observed as LAEs. Understanding the evolutionary connection between LBGs and LAEs is linked to this problem. Shimasaku et al. (2006) found from the rest-UV luminosity LF of the z = 5.7 LAE sample that ~80% or more of the LBG population would have strong Ly\textalpha emission at z ~ 6. This study shows that the rest-UV luminosity LF at z = 6.5 agrees with that of z = 5.7, suggesting the same high fraction. The faint end of the LF of z6p5LAEs may barely be determined with the spectroscopic capability of today’s 8 m telescopes. Nevertheless, steady efforts toward further spectroscopic confirmation are certainly required for z6p5LAEs.

APPENDIX

SKEWNESS: THE ASYMMETRY INDICATOR OF HIGH-Z Ly\textalpha EMISSION LINES

We describe here a statistic skewness S to measure the asymmetry of high-z Ly\textalpha emission lines. This model-independent indicator is free from fitting procedures that sometimes require smoothing of noisy spectra.

The expression S is a popular statistic, defined as the third moment of a distribution function, which describes its asymmetry (see also Kurk et al. 2004). Here, we regard the observed spectrum, which is basically a two-dimensional array of the flux (f_k) and the pixel (x_i), as a distribution function with an array size of n. Then S is defined as

\[ S = \frac{1}{I\sigma^3} \sum_{i=1}^{n} (x_i - \bar{x})^3 f_i, \]  \hspace{1cm} (A1)

where I = \sum_{i=1}^{n} f_i, and \( \bar{x} \) and \( \sigma \) are the average and dispersion of \( x_i \) defined as

\[ \bar{x} = \frac{1}{I} \sum_{i=1}^{n} x_i f_i \]  \hspace{1cm} (A2)

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This statistic is free from fitting procedures such as the $a_x$ and $a_f$ presented by Rhoads et al. (2003). Their asymmetry estimation is based on two-component Gaussian profile fitting for the red and blue sides of the emission. However, it is sometimes too difficult to determine accurately the peak wavelength $\lambda_p$ of the line, or $\lambda_{10}$, where the flux drops to 10% of its peak value, since they strongly depend on the resolving power and quality of the data.

We now estimate the error in $S$, which can be analytically derived. We here assume $\delta x_i \sim 0$ and approximately regard the first-order derivative of skewness as its error,

$$\sigma^2 = \frac{1}{T} \sum_i n_i (x_i - \bar{x})^2 f_i,$$

respectively.

This statistic is free from fitting procedures such as the $a_x$ and $a_f$ presented by Rhoads et al. (2003). Their asymmetry estimation is based on two-component Gaussian profile fitting for the red and blue sides of the emission. However, it is sometimes too difficult to determine accurately the peak wavelength $\lambda_p$ of the line, or $\lambda_{10}$, where the flux drops to 10% of its peak value, since they strongly depend on the resolving power and quality of the data.

We now estimate the error in $S$, which can be analytically derived. We here assume $\delta x_i \sim 0$ and approximately regard the first-order derivative of skewness as its error,

$$\delta S = \left[ \sum_i \left( \frac{\partial S}{\partial f_i} \delta f_i \right)^2 \right]^{0.5} = \frac{1}{T} \left\{ \sum_i \left[ \left( \frac{x_i - \bar{x}}{\sigma} \right)^3 - \frac{3S}{2} \left( \frac{x_i - \bar{x}}{\sigma} \right)^2 \right] - \frac{S^2}{2} \delta f_i^2 \right\}^{0.5},$$

where we use

$$\frac{\partial \bar{x}}{\partial f_i} = \frac{1}{T} (x_i - \bar{x})$$

and

$$\frac{\partial \sigma}{\partial f_i} = \frac{1}{2\sigma T} [(x_i - \bar{x})^2 - \sigma^2].$$

We can assume that the flux error does not depend strongly on the wavelength, as in the case of our NB filter coverage, where the night-sky window is almost free from OH emission lines. Under this assumption, the $\delta f_i$ can be regarded as $\delta f_i \sim \delta f = \text{const.}$ dominated by readout noise around the emission line in the spectrum.

This error estimate is confirmed to agree well with the rms fluctuation of $S$ evaluated by a Monte Carlo realization, in which the line-profile model was disturbed with random artificial errors as large as $\delta f$. Our estimate of skewness error in equation (A4) gives a useful analytic formula, although a more strict error estimate can only be achieved directly with Monte Carlo simulations.

We compared this statistic $S$ with $a_x$, proposed by Rhoads et al. (2003), for our NB921-excess sample in Figure 12. We calculated $S$ in the effective wavelength range of an emission line, where $f_i$ has an apparent positive signal above the continuum (sky) level. The
slight change in the effective wavelength range does not significantly affect the result. Foreground emitters shown in Figure 12 were definitely identified by their multiple spectral lines. That is, an H\textalpha emiter has corresponding [O\textsc{iii}] doublets around 7016 Å, and [O\textsc{iii}] and [O\textsc{ii}] emitters show apparent doubles by themselves (and sometimes Hβ for the [O\textsc{iii}] case). As expected, [O\textsc{ii}], [O\textsc{iii}], and H\textalpha emitters are distributed around $S = 0$ and $a_w = 1$. The resolved [O\textsc{ii}] doublet lines are expected to show negative $S$ because $\lambda3726$ is typically weaker than $\lambda3729$. There is a population \textit{(filled circles)} that have actually larger positive $S$ \textit{and} $a_w$, indicating statistically asymmetric lines with a broad red wing. We recognize these as Ly\textalpha emitters that have $S > 0.15$. Almost all the single-line emitters \textit{(triangles)} show relatively low $S$, which indicates that they are likely to be [O\textsc{ii}] emitters. The large scatter of $S$ for these single-line emitters was caused by the low S/N of their spectra.

To find a further adequate indicator sensitive to an asymmetry, we introduce \textit{weighted skewness} $S_w$, which combines the $S$ indicator and Rhoads et al. (2003)’s method. High-$z$ Ly\textalpha emission usually has a wider FWHM in the observed frame than that of foreground emitters. We define the \textit{weighted skewness} $S_w$ as

$$S_w = S(\lambda_{10,r} - \lambda_{10,b}),$$

(A7)

where $\lambda_{10,r}$ and $\lambda_{10,b}$ are the wavelengths where the flux drops to 10\% of its peak value at the redder and bluer sides of the Ly\textalpha emission, respectively. The asymmetric index $S$ is a dimensionless quantity, whereas the $S_w$ has a dimension of wavelength (here measured in angstroms). Figure 13 shows the correlation between $S_w$ and $a_w$, where the symbols are the same as those in Figure 12. We found that all the apparent foreground emitters have $S_w < 3$. The $S_w$ can distinguish between Ly\textalpha and other lines more effectively than $S$. We can set the critical value $S_w = 3$ to distinguish LAEs and foreground emitters, although there could be more or less contamination of LAEs at $S_w < 3$. This is a conservative critical value for LAEs in the sense that it assumes low contamination and low completeness.

In summary, our proposed statistic $S$ is free from fitting procedures and has an analytical error estimation formula. In addition, we made use of a revised indicator $S_w$ that proves to be more powerful when combined with the line width determined from Gaussian fitting.

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