Ultrasmall Moment Incommensurate Spin Density Wave Order Masking a Ferromagnetic Quantum Critical Point in NbFe$_2$

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In the metallic magnet Nb$_{1-y}$Fe$_{2+y}$, the low temperature threshold of ferromagnetism can be investigated by varying the Fe excess $y$ within a narrow homogeneity range. We use elastic neutron scattering to track the evolution of magnetic order from Fe-rich, ferromagnetic Nb$_{0.98}$Fe$_{2.019}$ to approximately stoichiometric NbFe$_2$, in which we can, for the first time, characterize a long-wavelength spin density wave state burying a ferromagnetic quantum critical point. The associated ordering wave vector $q_{SDW} = (0, 0, l_{SDW})$ is found to depend significantly on $y$ and $T$, staying finite but decreasing as the ferromagnetic state is approached. The phase diagram follows a two-order-parameter Landau theory, for which all of the coefficients can now be determined. Our findings suggest that the emergence of spin density wave order cannot be attributed to band structure effects alone. They indicate a common microscopic origin of both types of magnetic order and provide strong constraints on related theoretical scenarios based on, e.g., quantum order by disorder.

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The exploration of ferromagnetic quantum phase transitions in metals has motivated numerous theoretical and experimental studies [1], which have led to the discovery of non-Fermi liquid states [2,3] and of unconventional superconductivity (e.g., Refs. [4–6]). The underlying question, however—whether a ferromagnetic quantum critical point (QCP) can exist in clean band magnets—remains controversial. Fundamental considerations [7–9] suggest that the ferromagnetic QCP is avoided in clean systems by one of two scenarios: either the transition into the ferromagnetic state becomes discontinuous (first order), or the nature of the low temperature ordered state changes altogether, for instance, into nematic or long-wavelength spin density wave (SDW) order [8,9]. Whereas there are many examples for the first scenario, including ZrZn$_2$ [2], Ni$_3$Al [3], and UGe$_2$ [4], the transition into a modulated state on the border of band ferromagnetism has proven to be more challenging to investigate. Recent reports show that this scenario may apply more widely than the comparatively simple band ferromagnets for which it was first discussed: (i) the masking of the field-tuned quantum critical end point of the continuous metamagnetic transition of Sr$_3$Ru$_2$O$_7$ by two SDW phases [10], (ii) the evolution of ferromagnetic (FM) into long-wavelength SDW fluctuations in the heavy-fermion system YbRh$_2$Si$_2$ [11], which displays a high Wilson ratio [12] and becomes FM under Co doping [13], (iii) the emergence at finite temperature of SDW order in the ferromagnetic local moment system PrPtAl [14], and the appearance of modulated magnetic order at the border of pressure-tuned FM systems CeRuPO [15], MnP [16], or LaCrGe$_3$ [17].

The band magnet NbFe$_2$ is a particularly promising candidate for investigating the SDW scenario in a clean itinerant system because it is located near the border of ferromagnetism at ambient pressure [18], enabling multiprobe studies and, in particular, neutron scattering. Ferromagnetic order can be induced at low temperatures by growing Fe-rich Nb$_{1-y}$Fe$_{2+y}$ with $y$ as small as 1% (Fig. 1 [19]). Compton scattering results on the Fe-rich side of the phase diagram have been analyzed by assuming ferrimagnetism as the ground state [20], but more direct probes of the local fields by Mössbauer spectroscopy point to ferromagnetism as the ground state [21]. The precise low temperature state for $y = 0$ has remained unidentified since early NMR studies first suggested that stoichiometric NbFe$_2$ may display low-moment SDW order [22].
Repeated attempts to detect the SDW order in neutron scattering were unsuccessful, but recent results from ESR, muon spin relaxation, and Mössbauer spectroscopy also point strongly toward SDW order [21]. Non-Fermi liquid forms of resistivity and low temperature heat capacity have been observed in slightly Nb-rich NbFe$_2$ [23].

Here, we present the outcomes of a neutron diffraction study, which for the first time demonstrates unambiguously the existence of a long-wavelength modulated magnetic state (SDW) forming on the border of ferromagnetic order at low temperatures in stoichiometric single crystals of NbFe$_2$. We track its evolution with temperature and composition and probe the underlying ferromagnetic order. We find that the SDW state indeed displays a very small ordered moment $\mu_s < 0.1 \mu_B$/Fe atom, which explains why previous neutron scattering experiments failed to detect it. Our data confirm the second-order nature of the PM-SDW phase transition and a temperature hysteresis in the SDW ordering wave vector suggests that the SDW-FM phase transition is first order. The observed characteristics of the SDW order including the evolution of its ordering wave vector, which we find decreases on approaching the FM transition, as well as our theoretical analysis of the resulting phase diagram suggest that the occurrence of long-wavelength SDW order on the border of FM in NbFe$_2$ is not coincidental but rather emerges from the proximity to a FM quantum critical point, which is buried within the SDW dome.

**Experimental.**—Large single crystals of hexagonal MgZn$_2$ (C14) Laves phase NbFe$_2$ (lattice constants $a = 4.84$ Å and $c = 7.89$ Å) with compositions chosen across the iron-rich side of the homogeneity range have been grown in a UHV-compatible optical floating zone furnace from polycrystals prepared by induction melting [25]. The single crystals have been characterized extensively by resistivity, susceptibility, and magnetization measurements, as well as by x-ray diffraction and neutron depolarization [26–28], the latter showing homogeneity in structure and chemical composition. In this Letter, three samples have been measured: (i) sample A, which is almost stoichiometric ($y = +0.003$); (ii) sample B, which is slightly Fe rich ($y = +0.015$); and (iii) sample C, which is more Fe rich still ($y = +0.020$) [24].

For the neutron scattering experiments, the samples were mounted on Al holders and oriented with $(h0l)$ as the horizontal scattering plane. In order to enhance the signal to background ratio neutron diffraction was carried out with two cold triple-axis spectrometers in elastic mode: Panda at the Heinz Maier-Leibnitz Zentrum (MLZ) [29] and 4F2 at the Laboratoire Léon Brillouin (LLB). Panda was run with neutron wave vectors $k_i = k_f = 1.57$ Å$^{-1}$, and 4F2 was used with $k_i = k_f = 1.30$ Å$^{-1}$ [24].

**Results.**—The principal discovery of SDW Bragg reflections in the Nb$_{1-x}$Fe$_{2+y}$ system is presented in Fig. 2, which focuses on the reflection (101)$^+$ at $Q = (1, 0, 1) + q_{SDW}$ with $q_{SDW} = (0, 0, l_{SDW})$. SDW Bragg reflections corresponding to an ordering wave vector $q_{SDW}$ have been confirmed for all samples in this Letter. $l_{SDW}$ shows a significant $y$ and $T$ dependence, which will be discussed further below. We have also established the SDW’s long-range character [24]. In addition to the data of the (101)$^+$ reflection discussed above, the vicinity of nuclear Bragg reflections has been scanned for further SDW satellite peaks. SDW satellite peaks are present at $Q = (1, 0, 1) + q_{SDW}$ and $Q = (1, 0, 2) + q_{SDW}$, but they are absent at $Q = (1, 0, 0) + q_{SDW}$ and at $Q = (0, 0, l) + q_{SDW}$ with $l = 1, 2, 3$ (see the inset of Fig. 1). This distribution of allowed, and forbidden satellite Bragg peaks are consistent with moment orientation along the $c$ axis, suggesting a linearly polarized SDW state rather than spiral order. Based on ac susceptibility and torque magnetometry data, the $c$ direction has been determined to be the magnetic easy axis independent of the chemical composition [30,31].

Magnetic neutron scattering from the FM order has been observed at the position of the weak nuclear Bragg point (102). Figure 3(a) shows the $T$ dependence of the intensities of the FM (102) Bragg reflections normalized by the intensities of the nuclear (102) reflections at $T_C$ for all three compositions. Conversion to FM ordered moments $\mu_{FM}$ has been obtained as described in Ref. [24]. In the Fe-rich samples B and C, FM order is observed at low
The data are shown as solid lines. The SDW order in previous neutron diffraction experiments. The figures contain selected $h$ and $l$ scans across the SDW Bragg peak demonstrating its $T$ dependence in each sample. Gaussian fits of the data are shown as solid lines. $l_{SDW}$ has significant $y$ and $T$ dependence and is located in the range $0.083(1) \leq l_{SDW} \leq 0.164(3)$ in the explored samples. The scans selected for this figure have been measured in sequences going down in $T$. The whole collected dataset (not all data shown) contains $h$ and $l$ scans from sequences going up and down in $T$ for all samples.

The SDW ordering wave vector $q_{SDW} = (0, 0, l_{SDW})$ is found to depend significantly on composition and temperature [Fig. 3(c)]; (i) the $c$-axis pitch number shifts from $l_{SDW}(T_N) = 0.157(1)$ in sample $A$ to $l_{SDW}(T_N) = 0.095(1)$ in sample $C$ (corresponding to an incommensurate modulation along the $c$ axis with a pitch in the range $\lambda_{SDW} \approx 50–100$ Å); (ii) in samples $B$ and $C$, $l_{SDW}$ shows a significant $T$ dependence, decreasing by about 20% with decreasing $T$; (iii) $l_{SDW}(T)$ stays finite at the SDW-FM transition, so there is a discontinuous change in the magnitude of the magnetic ordering wave vectors there from finite ($q_{SDW}$) to zero ($q_{FM}$); and (iv) in samples $B$ and $C$, $l_{SDW}(T)$ reproducibly displays significant thermal hysteresis with lower $l_{SDW}$ values when warming into the SDW phase from the FM state. (i) and (ii) mean that $l_{SDW}$ is being reduced upon approaching FM, and (iii) and (iv) point to the first-order nature of the SDW-FM transition.

Discussion.—The delicate SDW state of the Nb$_{1+y}$Fe$_{2-y}$ system occurs in a narrow composition and temperature range attached to the threshold of FM order (Fig. 1). Because the SDW-FM transition is first order, the emergence of the SDW state masks the FM QCP and buries it inside a SDW dome. Our neutron diffraction results have revealed the following main characteristics of the SDW state: (i) an incommensurate ordering wave vector $q_{SDW}$ with its striking dependence on $y$ and $T$, (ii) the long-range nature in contrast to what would be expected for a spin glass [32], and (iii) a small linearly polarized ordered...
not a local moment picture. However, the y and T dependent values of $q_{SDW}^{(0)}$ cannot be explained based on the electronic band structure alone.

Within density functional theory, the implications of the electronic band structure for magnetic order have been examined in detail. Direct total energy calculations for different ordering patterns [33–35] suggest that energy differences between a number of magnetic ground states are very small. Moreover, the wave vector dependence of the bare band structure derived susceptibility $\chi^0_q$ or Lindhard function [33,34] is not consistent with the long-wavelength SDW order reported here, as it does not feature a significant enhancement near the measured $q_{SDW}$ range, suggesting that SDW order in NbFe$_2$ has a more subtle origin. The observed dependence of $q_{SDW}$ [Fig. 3(c)], which decreases as the FM state is approached, indicates that $\chi^0_q$ is strongly modified by order-parameter fluctuations on the threshold of FM.

The close connection between modulated and uniform magnetic order in NbFe$_2$ is striking. It can be modeled effectively with the help of a Landau expansion of the free energy in terms of the two order parameters $M$ (for FM) and $P$ (for SDW order) [36], which in zero field reduces to

$$F/\mu_0 = \frac{a}{2} M^2 + \frac{b}{4} M^4 + \frac{\alpha}{2} P^2 + \frac{\beta}{4} P^4 + \frac{\eta}{2} P^2 M^2. \quad (1)$$

The use of this model is corroborated in this Letter by the observation that $q_{SDW}$ does not go to zero but stays finite at the SDW-FM transition. While the parameters $a$ and $b$ can be obtained from magnetization measurements, this is not possible for the parameters $\alpha$, $\beta$, and $\eta$. They can, however, be determined from the SDW ordered moment $P$ observed in our neutron scattering study. We make use of the Landau theory results that $P^2 = -a/\beta$ and that within the SDW phase the intercept $a^*$ and slope $b^*$ of the Arrott plot $H/M$ vs $M^2$, which can be determined in bulk magnetization measurements, become $a^* = a - a\eta/\beta$ and $b^* = b - \eta^2/\beta$ [36]. Writing $a = a_1(T - T_0)$ and $a = a_1(T - T_N)$, we find that the parameters characterizing the SDW order vary slowly with composition and are of similar magnitude as those characterizing the FM order, $a_1/\alpha \approx \beta/b \approx 2 \pm 1$, and that the coupling parameter $\eta \approx \beta$ [24]. This implies that the ratio $\eta/\sqrt{\beta} > 1$ throughout, which rules out phase coexistence within the two-parameter Landau theory, in agreement with experimental observations. Most importantly, the parameter values point toward a common microscopic origin for both types of magnetic order and put strong constraints on a microscopic theory of magnetism in NbFe$_2$.

A number of theoretical studies [1,8,9,37] have noted that the FM quantum critical point is unlikely to be observed in clean, 3D ferromagnets, and it will instead either be avoided by a change of the magnetic transition from second order to first order or masked by the...
emergence of long-wavelength SDW. Both scenarios can be attributed to nonanalytic terms in the free energy associated with soft modes. These contribute a singular $q$ dependence of the form $q^2 \ln q$ to $\chi^{-1}$ and thereby produce an intrinsic tendency toward long-wavelength modulated order as the FM QCP is approached. An alternative approach [38] arrived at similar conclusions by considering the contribution of order-parameter fluctuations to the free energy, when different ordered states were imposed, causing differences in the phase space available to critical fluctuations of FM and modulated magnetic order. Helical order in the local moment system PrPtAl [14] has recently been presented as a likely manifestation of this scenario, but a demonstration in a band magnet is still outstanding.

New neutron data demonstrate that SDW order emerges near the border of ferromagnetism in the C14 Laves phase system Nb$_{1-y}$Fe$_{2+y}$, burying an underlying FM QCP. This suggests that the SDW order in Nb$_{1-y}$Fe$_{2+y}$ is caused by an intrinsic instability of a ferromagnetic quantum critical point to modulated magnetic order, which has been postulated on the basis of fundamental considerations but has not before been detected in a band magnet.

The underlying data supporting this publication can be accessed through Ref. [39].

This work is based upon experiments performed at the PANDA instrument operated by JCNS at the MLZ, Garching, Germany, and at the 4F2 instrument at LLB, CEA Saclay, France. We acknowledge support by the EPSRC through Grant No. EP/K012894/1 and by the German Science Foundation (DFG) through FOR 960 (C. P.) and SFB/TR 80 (C. P.). This research project has also been supported by the European Commission under the Seventh Framework Programme through the “Research Infrastructures” action of the “Capacities” program, Contract No. CP-CSA_INFRA-2008-1.1.1, No. 226507-NMI3. We thank S. Friedemann, M. Brando, and S. Süllow for the helpful discussions.

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Correction: A data availability statement was added to this Letter.