A plasma wakefield acceleration experiment using CLARA beam

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Abstract

We propose a Plasma Accelerator Research Station (PARS) based at proposed FEL test facility CLARA (Compact Linear Accelerator for Research and Applications) at Daresbury Laboratory. The idea is to use the relativistic electron beam from CLARA, to investigate some key issues in electron beam transport and in electron beam driven plasma wakefield acceleration, e.g., high gradient plasma wakefield excitation driven by a relativistic electron bunch, two bunch experiment for CLARA beam energy doubling, high transformer ratio, long bunch self-modulation and some other advanced beam dynamics issues. This paper presents the feasibility studies of electron beam transport to meet the requirements for beam driven wakefield acceleration and presents the plasma wakefield simulation results based on CLARA beam parameters. Other possible experiments which can be conducted at the PARS beam line are also discussed.

Keywords: Plasma accelerators, Wakefield, FEL, Particle-in-cell.

1. Introduction

Plasma accelerators utilize the breakdown medium “plasmas” as the accelerating structures and therefore avoid the further material breakdown limit posed by the conventional accelerating structures, e.g. copper or niobium RF cavities. In principle, the wavebreaking field can reach 100 GV/m in electron beam driven plasma wakefield acceleration, e.g., high gradient plasma wakefield excitation driven by a relativistic electron bunch, two bunch experiment for CLARA beam energy doubling, high transformer ratio, long bunch self-modulation and some other advanced beam dynamics issues. This paper presents the feasibility studies of electron beam transport to meet the requirements for beam driven wakefield acceleration and presents the plasma wakefield simulation results based on CLARA beam parameters. Other possible experiments which can be conducted at the PARS beam line are also discussed.

2. CLARA facility and PARS beam line

The aim of CLARA is to develop a normal conducting test accelerator able to generate longitudinally and transversely...
Figure 1: Conceptual layout of the CLARA facility and the PARS beam line.

bright electron bunches and to use these bunches in the experimental production of stable, synchronized, ultrashort photon pulses of coherent light from a single pass FEL (free electron laser) with techniques directly applicable to the future generation of light source facilities [10]. The CLARA facility houses a photo-injector electron gun, normal conducting accelerating cavities, magnetic bunch compressor, fourth harmonic lineariser, dedicated beam diagnostic sections at low and high energies and FEL beam line, as illustrated in Fig. 1. The beam energy is 250 MeV and the maximum bunch charge is about 250 pC. The achievable bunch parameters in different operating modes are listed in Table 1 [11, 12].

For the electron beam driven PWFA experiment at PARS, a dogleg will guide the full energy CLARA beam to a parallel beam line, offset by ~1.5 m from the CLARA beam axis, contained within the CLARA shielding area. The conceptual layout of the PARS beam line is also shown in Fig. 1. It consists of the dogleg beam line, final focus, plasma cell, energy spectrometer (phosphor screen) and final beam dump (not shown). The dogleg beam line consists of arrays of dipoles and quadrupoles to guide and focus the beam from the CLARA beam line to the PARS. The final focus, which is prior to the plasma cell, is designed to focus the electron beam transversely and to match the electron beam with the plasma. A variable 10-50 cm plasma cell (a DC discharge plasma source seems feasible) will be built to test the key issues in the PWFA experiments at various beam and plasma parameter ranges. An energy spectrometer, together with a phosphor screen is employed to characterize the energy of electrons exiting the plasma cell. The final beam dump will absorb the energy of electrons after exiting the plasma cell. Prior to the final focus and plasma cell, a magnetic chicane may be needed to compress the bunch further to an extremely short length.

Figure 2: The beam line design for PARS by using 4 identical dipoles.

The proposed dogleg beam line design, using ~I transform between the dipoles using two FODO doublets, keeps the transverse beam emittance blow up due to coherent synchrotron radiation (CSR) within acceptable limits [13, 14]. Figure 2 illustrates the beam line design for PARS by using 4 dipoles, with each dipole bending angle of 6°. The optical functions are plotted in Fig. 3 from which we can see the transverse dispersion function is fully suppressed at the straight section prior to the plasma cell. Figure 4 gives the first order longitudinal dispersion $R_{56}$ and the second order longitudinal dispersion function $T_{566}$ with respect to the PARS beam line axis. Through it, the bunch can be compressed to an ultrashort pulse which is crucial to a high plasma wakefield excitation. Using the typical CLARA beam parameters, e.g. a bunch length of 75 µm, a bunch charge of 250 pC and an energy spread of 1%, we track a Gaussian beam through the PARS beam line using ELEGANT [15]. The result is shown in Fig. 5. The beam emittance growth (about 1%) is negligible before it reaches the plasma cell. It shall be noted that the small emittance change is mainly due to the CSR effects.

3. Electron beam tracking at CLARA/PARS

To qualify the tracking simulations performed using a Gaussian bunch profile, full start-to-end simulations were performed...
Figure 6: Longitudinal bunch ((a) current, (b) momentum) distribution at the exit of Linac 2 for a 100 pC electron bunch, including 3D space-charge forces, and tracked with 100 k particles in ASTRA.

Figure 7: Longitudinal bunch ((a) current, (b) momentum) distribution at the exit of Linac 4 for a 100 pC electron bunch at 250 MeV and including longitudinal space charge forces using the Elegant code for 100 k particle bunch.

from the electron source to the end of the PARS final focus line, using an ASTRA+ELEGANT computational framework. Baseline CLARA design introduces the VELA photo-injector where a Ti-sapphire laser (266 nm) illuminates a copper cathode with 76 fs pulses (1mJ energy per pulse) at a repetition rate of 10 Hz. The cathode is followed by a 2.5 cell, S-band, normal conducting cavity with an accelerating gradient of 100 MV/m [12]. Consequently, the beam is generated at the cathode using the ASTRA code [16], and the generated beam is tracked through the gun using full space charge tracking up to the first CLARA Linac where it reaches an energy of 6.5 MeV. There are two envisaged operating modes of CLARA. The first mode is a long-pulse mode, where the beam is accelerated at some relatively small off-crest phase in the first Linac, and which is magnetically compressed in the down-stream bunch compressor; and the second mode is an ultra-short-pulse mode where the beam is velocity-bunched (VB) in the first Linac, and no magnetic compression is performed. The magnetic compression scheme is designed to operate at up to 250 pC. Whereas the velocity bunched mode is limited to bunch charges of 100 pC.

To investigate the limits of achievable bunch lengths for the PARS experiment, initial work has focused on the second option, the velocity-bunched scheme, as this is expected to produce the shortest bunches from CLARA. For this scheme to work the beam must pass through the first Linac around the zero-crossing phase of the RF waveform, that is ∼90° from the crest. At this phase the head of the bunch is decelerated, whilst the tail is accelerated, which, due to the low energies involved, leads to a velocity-time correlation over the bunch. Over a subsequent drift distance, up to the entrance of Linac 2, the head and the tail of the bunch compress due to the velocity correlation and the bunch can reach peak currents of over 2 kA at 100 pC bunch charge. The beam is accelerated in Linac 2 up to 75 MeV, which limits the growth in bunch properties, primarily due to space-charge forces, in the rest of the machine. This section of the machine is also tracked in ASTRA with full space-charge forces included, however the wakefields in Linacs are not included. The output of the ASTRA simulations are then passed to the ELEGANT code, which includes longitudinal space-charge forces as well as a 1-D model of CSR. Representative wake-field models for all RF cavities after Linac 2 are also included in ELEGANT. The beam is tracked through the diagnostics and bunch-compression (switched off in this scenario) sections of the CLARA machine before being further accelerated in Linacs 3 and 4 up to the design energy of 250 MeV. Due to the high-density longitudinal structure of the electron
bunch, space-charge forces are still important at the intermediate energies, and this leads to a broadening of the electron bunch longitudinally, which reduces the peak currents at the exit of Linac 4 to approximately 600 A for a 100 pC bunch. Tuning of the exact RF phases in Linacs 1 and 2 can mitigate some of this reduction, but maximum peak currents are always less than 1 kA at 100 pC. The VB mode produces a slight longitudinal chirp in the electron bunch which, due to the very short bunch lengths, is not significantly modified by the off-crest phases in Linacs 2-4. This natural chirp leads to a longitudinal bunch shortening in the PARS beam line, due to the inherent $R_{56}$ as shown in Fig. 4. This $R_{56}$ can be used to increase the peak current at the PARS final focus system to over 3 kA at 100 pC. CSR effects can also be seen in the bunch, but due to the $-I$ phase advance designed into the system, they do not strongly affect the longitudinal bunch properties. The fully longitudinally compressed bunch is then transversely focused in the final-focus system to produce transverse beam dimensions of the order of 20 $\mu$m. Transverse focusing at higher bunch charges is significantly harder than at lower charges due to the CSR effects that are seen. The transverse beam properties are also affected by space-charge in the long transport from the exit of Linac 2 till the entrance of Linac 3. The current ELEGANT model does not include transverse space-charge forces, but initial estimates using ASTRA do show an increase in the transverse emittance by a factor of 3. The effects of transverse space-charge will be more fully characterised at a later date, and the current results therefore represent an idealised case.

The results of these simulations are demonstrated, for a 100 pC CLARA bunch. In Fig. 6 we show the beam current and momentum distribution at the exit of Linac 2, where the electron beam has been velocity bunched in Linac 1, and then accelerated approximately on-crest in Linac 2. This also corresponds to the beam distribution at the end of the ASTRA tracking run, and thus the input for ELEGANT.

In this simulation we have set Linac 1 at a phase of 91.5°, slightly off from the nominal zero-crossing phase, and Linac 2 at an off-crest phase of + 4°. This acts to limit the velocity bunching and gives peak currents of $\sim$1 kA at the exit of Linac 2, compared to the >2 kA that are possible, for a 100 pC bunch. This reduced peak current at the exit of Linac 2 has been shown to increase the achievable peak currents seen at the end of the PARS beamline by up to 2 kA, by both reducing the effects of space-charge forces in the long transport system up to Linacs 3 and 4, and increasing the longitudinal chirp on the bunch.

Figure 7 shows the same bunch at the exit of Linac 4, with an energy of 250 MeV. Here, the peak current has been reduced to only $\sim$500 A due to the broadening effects of longitudinal space-charge forces. The natural chirp on the bunch is now much more clearly defined, and this will lead to a longitudinal bunch compression in the PARS beamline. There are also 2 clear tails on the bunch distribution at the head and tail of the bunch. These tails arise within from the electron source, and it does not seem possible to mitigate those using solely electromagnetic means in the beamline. The final longitudinal bunch properties at the exit of the PARS line are shown in Fig. 8.

Tracking results for different bunch charges of 20 pC and 50 pC are also presented in comparison with the results for 100 pC. Figure 9 clearly shows the high expected peak currents of > 3 kA at 100 pC, but also peak currents of $\sim$2 kA at 50 pC and > 1 kA at 20 pC. The non-linear reduction in peak current with reducing charge is mostly due to mitigation of the space-charge effects.
broadening in the CLARA beamline at reduced bunch charges. There is also some reduction in the CSR effects in the PARS beamline itself, although this is less important for the final longitudinal bunch length. Due to the bunch tails that arise from the electron source, there is a broad background of charge in the longitudinal bunch distribution. This limits the total charge in the current spike to, at worst, 50% of the main bunch charge.

In all three cases the bunch length for the current spike is shorter than 30 fs RMS. At the exit of the PARS beamline, the bunch has to be focused transversely as well as longitudinally. Figure 9 shows the transverse bunch properties for the three different charge values shown above.

It can be seen that for a low bunch charge the transverse beam size falls to about 20 µm RMS size. However, for high charge regimes, 50 pC and 100 pC, there is some broadening of the bunch transverse size due to the increased energy spread of the beam, arising due to CSR effects in the PARS beamline. Note, however, that the increase in transverse emittance due to space-charge forces has not yet been fully characterised, and these numbers are expected to increase.

4. PARS beam parameters

According to the linear theory of PWFA [17], the maximum plasma wakefield amplitude is proportional to the bunch charge (number of electrons per bunch) and inversely proportional to the square of the bunch length. Therefore a short drive beam is in principle preferable for a high amplitude wakefield excitation. A preliminary simulation study has shown that an accelerating gradient of a few GV/m can be obtained if a short (therefore high peak current) electron bunch is used as drive beam at the PARS.

Based on the initial tracking results for VB mode mentioned above, as well as the details found in the CLARA CDR [12], we have defined the parameter settings for the PWFA experiment at the PARS beam line [12]. Table 1 summarizes the different working regimes of the beam parameters; each parameter setting can be used to study the beam-plasma interactions and test the scaling laws of PWFA. In principle three operating regimes, i.e., long pulse, short pulse and ultra-short pulse can be achieved at CLARA facility for the PWFA experimental research [18].

5. Particle-in-cell Simulations

5.1. Wakefield structures

To gain a full understanding of the wakefield excitation by using the relativistic CLARA beam as drive beam, one has to rely on detailed simulations. VORPAL is a fully explicit PIC code developed by Tech-X Corporation in Boulder, USA [19]. We use it to simulate the interactions between electron beam and plasma. Figure 10 gives a 2D simulation of typical accelerating and decelerating wakefield structure in a plasma. The parameters used in this simulation are as follows: the beam energy is 250 MeV, bunch length is 30 µm, transverse beam size is 100 µm, bunch charge is 250 pC, and plasma density is 5 × 10¹⁶ cm⁻³. The maximum longitudinal accelerating and decelerating wakefield $E_x$ is about 600 MV/m, as illustrated in Fig. 11, an order of magnitude higher than what can be achieved with conventional RF structures.

5.2. Effect of plasma density

The effect of plasma densities on the plasma wakefields, while keeping other parameters constant was investigated by using simulations at densities one order of magnitude lower than, higher than, and equal to the electron bunch density, with beam parameters expected at the proposed CLARA beam. Fig. 12, 13, and 14 show the longitudinal wakefields $E_x$ for these different situations, in a 1-D plot against $x$. Here, $x$ denotes the longitudinal beam propagation direction. The input parameters are from the short pulse mode as listed in Table 1. The beam radius used is 20 µm and the bunch length is 75 µm, which corresponds to a beam density of 3.3 × 10¹⁵ cm⁻³.

The simulation results show how the magnitude of the plasma wakefields depends on the plasma densities, and that the accelerating field is modulated at the plasma wavelength $\lambda_p$. The highest accelerating gradient is achieved for a plasma
density matching the electron beam density. It is also notable
that the wakefield amplitude decreases most rapidly for the low
density plasma, and least rapidly for the plasma equal in density
to the electron beam. The maximum accelerating field is about
2 GV/m when the plasma density is the same as the drive beam
density.

$$n_b = N_b / \left[ \left( 2 \pi \right)^{3/2} \sigma_x \sigma_z \right]$$

(1)

where $N_b$ is the number of electrons per bunch, $\sigma_x$ and $\sigma_z$
are the transverse RMS beam sizes and the bunch length,
respectively. It can be seen that the bunch density is proportional to
the number of electrons per bunch and inversely proportional to the
bunch length and the square of the transverse RMS beam size.

Based on linear theory of PWFA, the maximum wakefield
amplitude is given by

$$E_{\text{acc}} [\text{MeV/m}] = 244 \times \frac{N_b}{2 \times 10^{10}} \left( \frac{6 \mu m}{\sigma_z (\mu m)} \right)^2.$$  

(2)

It gives a maximum wakefield amplitude of about 1.2 GV/m
by using the strongly focused beam parameters, which agrees
well with the simulation results as shown in Fig. 16.

5.3. Strongly focused beam as driver

If the electron beam is subject to strong transverse focusing,
i.e., by final focus prior to the plasma cell, one expects a high-
density drive bunch can be achieved. The bunch density for a
Gaussian distributed beam is given by

$$E_{\text{acc}} [\text{MeV/m}] = 244 \times \frac{N_b}{2 \times 10^{10}} \left( \frac{6 \mu m}{\sigma_z (\mu m)} \right)^2.$$  

(2)

Meanwhile, one can also examine the particle acceleration
effect from the CLARA beam driven plasma wakefield. Figure
shows the 3D simulation result on beam energy spectrum
after propagating through a 3 cm long plasma cell for a strongly

$$E_{\text{acc}} [\text{MeV/m}] = 244 \times \frac{N_b}{2 \times 10^{10}} \left( \frac{6 \mu m}{\sigma_z (\mu m)} \right)^2.$$  

(2)

It gives a maximum wakefield amplitude of about 1.2 GV/m
by using the strongly focused beam parameters, which agrees
well with the simulation results as shown in Fig. 16.
6. Other research topics at PARS

There are many interesting research topics which can be explored using the CLARA beam driven PWFA. For example, a two-bunch acceleration experiment, i.e., one bunch for driving the wakefield and the other bunch for sampling the wakefield, can be studied at PARS facility. Based on the latest simulations, one could hope to double the energy of the CLARA beam with a 20 cm preformed plasma. In this case, the FEL seeded from the wakefield accelerated beam will enable short wavelength photon production for scientific research and industrial users.

In addition, the plasma can act as an undulator to produce a high brightness photon beam at energies between keV to MeV through betatron radiation [20]. The mechanism of the radiation production can be extensively investigated at PARS facility.

Furthermore it is possible to study the self-modulation instability (SMI) of a long electron beam in a high-density plasma. The AWAKE collaboration at CERN will investigate self-modulated SPS proton driven wakefield acceleration [21,22]. The CLARA beam has the same gamma factor as the SPS beam, and it is much easier to manipulate than the SPS beam due to its lower energy. Therefore the experimental results from CLARA/PARS will be able to give some inputs to the CERN AWAKE experiment.

Except for the aforementioned plasma wakefield acceleration experiments, a dedicated beam line at PARS will allow us to study dielectric wakefield acceleration which is currently under study at the Cockcroft Institute [23] and Daresbury laboratory [24]. Meanwhile the beam from PARS can be used to test other advanced beam dynamics issues, e.g. coherent synchrotron radiation and its countermeasures, microbunching instability, emittance exchange and some novel FEL schemes. The versatile PARS beam operation modes make it an ideal test bench for beam instrumentation R&D, e.g. the coherent Smith-Purcell radiation, coherent edge radiation and electron-optical sampling (EOS) etc.

7. Conclusions

The proposed PARS at CLARA facility will address the key issues in electron beam driven plasma wakefield acceleration. The PARS beam line has been designed and it has demonstrated that three sets of beams, e.g. long pulse, short pulse and ultra-short pulse, are feasible in the beam transport from the CLARA to the PARS. The particle-in-cell simulations show that the high accelerating gradients from a few hundreds of MV/m to several GV/m can be achieved from the plasma wakefields. In addition, this specially designed PARS beam line can be used to study other advanced beam dynamics issues and enable many beam applications.

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