Calibration of a star formation and feedback model for cosmological simulations with Enzo

Boon Kiat Oh,1⋆ Britton D. Smith,1,2 John A. Peacock,1 and Sadegh Khochfar1
1Institute for Astronomy, University of Edinburgh, Royal Observatory, Edinburgh EH9 3HJ, United Kingdom
2San Diego Supercomputer Center, University of California, San Diego, 10100 Hopkins Drive, La Jolla, CA 92093

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ABSTRACT
We introduce a new methodology for efficiently tuning sub-grid models of star formation and supernovae feedback in cosmological simulations, and at the same time understanding their physical implications. Based on a set of seventy-one zoom simulations of a Milky-Way (MW) sized halo, we explore the feasibility of calibrating a widely-used star formation and feedback model in the Enzo simulation code. We propose a novel way to match observations, using functional fits to the observed baryon makeup over a wide range of halo masses. The model MW galaxy is calibrated using three parameters: the star formation efficiency ($f^*$), the efficiency of thermal energy from stellar feedback ($\epsilon$) and the region into which feedback is injected ($r$ and $s$). We find that changing the amount of feedback energy affects the baryon content most significantly. We then identify two sets of feedback parameter values that are both able to reproduce the baryonic properties for haloes between $10^{10}$ $M_\odot$ and $10^{12}$ $M_\odot$. We can potentially improve the agreement by incorporating more parameters or physics. If we choose to focus on one property at a time, we can obtain a more realistic halo baryon makeup. Contrasting both star formation criteria and the corresponding combination of optimal feedback parameters, we also highlight that feedback effects can be complementary: to match the same baryonic properties, with a relatively higher gas to stars conversion efficiency, the feedback strength required is lower, and vice versa. Lastly, we demonstrate that chaotic variance in the code can cause deviations of approximately 10% and 25% in the stellar and baryon mass in simulations evolved from identical initial conditions.

Key words: cosmology:theory – galaxies:formation – galaxies:evolution – galaxies:haloes

1 INTRODUCTION
The large-scale structure of the universe can be understood quite precisely by considering models that consist purely of dark matter. Numerical simulations of structure formation in such models have been performed with high accuracy and progressively higher resolution and larger box size (Efstathiou et al. 1985; Moore et al. 1999; Springel et al. 2008; Diemand et al. 2008; Klypin et al. 2011). But on the baryonic side, limitations in numerical resolution mean that several baryonic processes are not simulated from first principles. These processes include fundamental phenomena of the transformation of cold gas to stars, feedback from the energy released by stars, supernovae and massive black holes. Such effects are implemented using a subgrid approach in cosmological hydrodynamical simulations (Springel & Hernquist 2003; Governato et al. 2010; Agertz et al. 2013; Shimizu et al. 2019). If these analytical implementations are too simplistic, they risk being sensitive to poorly determined parameters, thus limiting their capability to make robust predictions. Improving the accuracy of subgrid physics requires both a better understanding of physical processes and identification of their limitations.

Feedback processes are essential in order to solve fundamental issues in numerical simulations such as the ‘overcooling problem’ (Cole 1991; White & Frenk 1991; Blanchard et al. 1992) and the ‘angular momentum problem’ (Katz & Gunn 1991; Navarro & White 1994; Hummels & Bryan 2012). Overcooling results in the formation of too massive galaxies particularly in high-resolution simulations (Dave et al. 2001). Feedback is also important for shaping the density profile of dark matter haloes (Pontzen & Governato 2012; Martizzi et al. 2013; Davis et al. 2014). In addition to these issues of small-scale subgrid physics, cosmological simulations contain additional uncertainties. In the absence of feedback, Genel et al. (2018) highlighted differences in the properties of galaxies induced by very slight changes in the initial positions of dark matter particles. Even if a galaxy is evolved from identical initial conditions, the simulation code can introduce variances which result in fluctuations in the simulated properties between repetitions of the same simulation (Keller et al. 2019). The problem is alleviated by the self-
regulating nature of feedback (Keller et al. 2019) and highlights the need to understand the impact that subgrid implementations have on the resulting properties of galaxies in simulations.

Feedback processes that inject energy into the gas are therefore integral to numerical simulations. For smaller mass haloes, the energy comes mainly from supernova explosions. In contrast, for more massive ones, the main energy sources are active galactic nuclei (AGN) (Sijacki et al. 2007; Booth & Schaye 2009; Teyssier et al. 2011) and gravitational heating as a result of infalling clumps of matter (Dekel & Birnboim 2006; Khochfar & Ostriker 2008). However, it is unclear how the energy should be distributed between generating motion and heating the gas. For supernova feedback alone, various techniques have been employed across different simulation codes (Stinson et al. 2006; Cen & Ostriker 2006; Dubois & Teyssier 2008; Dalla Vecchia & Schaye 2012; Smith et al. 2018). Each technique has its own advantages and disadvantages. For instance, the relatively recent mechanical feedback model (Kimm & Cen 2014; Kimm et al. 2015; Hopkins et al. 2018) is insensitive to numerical resolution and ensures convergence, but it requires the simulation to be of sufficiently high resolution. Given the huge diversity in the method of implementation, it is not unusual to expect significantly different outcomes (Thacker & Couchman 2000; Springel & Hernquist 2003; Okamoto et al. 2005; Oppenheimer & Davé 2006; Schaye et al. 2010), and variation in feedback effects is the most significant source of uncertainty in a cosmological simulation. In particular, the role of resolution should be emphasised: the resolution in cosmological simulations is limited but feedback occurs on all scales, so rigorous numerical convergence cannot be expected. The subgrid parameterisation, or at least the subgrid parameter values, will need to change according to the resolution in order to match calibrating observations, and there is no guarantee that all predicted galaxy properties will then be independent of resolution.

To reproduce a realistic picture of the observed universe, there is thus a need to control the parameters of the appropriate subgrid routines (Okamoto et al. 2014; Schaye et al. 2015). These are matched to match specific observational properties of the galaxy population. By matching related properties, the simulation can then be used to answer a wide range of questions. For example, the feedback implementation in the ‘Evolution and Assembly of GaLaxies and their Environments’ (EAGLE) simulation project is calibrated to reproduce the observed $z = 0.1$ galaxy stellar mass function (GSMF), the relation between the mass of galaxies and their central black holes and realistic galaxy sizes (Schaye et al. 2015). The Illustris group calibrate their parameters to match various observational scaling relations and galaxy properties at low and intermediate redshifts (Vogelsberger et al. 2014). Despite the calibrations, there are shortcomings in each simulation. For example, Illustris recognised that the decrease of their simulated cosmic star formation rate density was too slow, leading to an update in their feedback prescription, resulting in the introduction of IllustrisTNG (Pillepich et al. 2018).

In contrast to these fully cosmologically representational box simulations, zoom simulations focus computational resources on smaller volumes (Springel et al. 2008; Griffen et al. 2016; Wang et al. 2015). In particular, Wang et al. (2015) studied a halo mass range from dwarf masses ($5 \times 10^9 M_\odot$) to Milky Way (MW) masses ($2 \times 10^{12} M_\odot$). They included baryonic processes and were able to reproduce the stellar to halo mass relation from abundance matching (Behroozi et al. 2013b; Moster et al. 2013; Kravtsov 2013) across a wide range of redshifts. However, they did not account for the mass of gas remaining in the haloes, and this is an important issue for the present analysis.

In this paper, we use zoom simulations of MW haloes to introduce a new approach to tuning subgrid models, which will be used to quantify the stellar and gas mass present in such a halo at $z = 0$. In particular, we examine the degree of calibration allowed in the model introduced by Cen & Ostriker (1992). Although more recent models are available in the literature, the Cen & Ostriker model remains one of the most widely used models in Enzo simulations and we adopt it as a test case. We calibrate the parameters governing star formation and feedback via a comparison with the inventory of baryonic and gravitating masses of cosmic structures presented in McGaugh et al. (2010), in particular the mass fraction of baryons in the halo and the conversion efficiency of gas into stars. Using our novel methodology, we will discuss the constraining power of the above set of observations as well as limitations in the employed subgrid models.

This paper is structured as follows. Section 2 describes the generation of initial conditions used in the simulations, the code, and setup used to evolve them. Also, we describe the parameters used for calibration and analysis tools used to extract and analyse the results. Section 3 presents the properties from McGaugh et al. (2010) that we attempt to match, along with the observational fit of the Kennicutt–Schmidt relation (Kennicutt et al. 2007). Section 4 describes the results from various simulations: effects of single parameter variation, calibration of parameters to results from McGaugh et al. (2010) and performance of the simulations to match other constraints. Lastly, the results are summarised and discussed in Section 5.

2 SIMULATION SETUP AND ANALYSIS

This section provides an overview of the simulation setup and the associated subgrid physics. In particular, the focus is on a MW-sized halo, at which mass scale we expect that AGN feedback will be subdominant (Bower et al. 2006; Behroozi et al. 2010; Storchi-Bergmann 2014). The main parameters investigated will thus be related to star formation efficiency and supernova feedback, and one aim of this investigation is indeed to see to what extent we can reproduce the baryonic properties of the MW using solely these ingredients. As described by Crain et al. (2015), the resulting baryonic properties of the halo are very sensitive to the variations of feedback parameter values. Therefore, a detailed explanation of the role of each parameter in the physical model is necessary.

The cosmological parameters in this suite of simulations are taken from WMAP-9 (Bennett et al. 2013). The key parameters are $\Omega_m = 0.285$, $\Omega_\Lambda = 0.715$, $\Omega_b = 0.0461$, $h = 0.695$ and $\sigma_8 = 0.828$ with the usual definitions. With these parameters, we generate initial conditions with Multi-scale Initial Conditions (MUSIC) for cosmological simulations (Hahn & Abel 2011). We derive all zoom simulations from the parent simulation with a volume of $L = 100 h^{-1}$ cMpc with 256$^3$ particles.

The simulation is evolved using Enzo, an adaptive mesh-refinement (AMR) code (Bryan et al. 2014). Enzo uses a block-structured AMR framework (Berger & Colella 1989) to solve the equations of hydrodynamics in an Eulerian frame using multiple solvers. In the simulations presented here, we use the ZEUS (Stone & Norman 1992) hydro solver in combination with an N-body adaptive particle-mesh gravity solver (Efstathiou et al. 1985). Parameter space exploration is performed mainly on the star formation and feedback routines; the results of this exploration will be outlined extensively in Section 2.1 and 2.2. Lastly, the chemistry and cooling processes are handled by the Grackle library (Smith et al. 2017). We use the equilibrium cooling mode from Grackle, which utilises
the tabulated cooling rates derived from the photoionisation code CLOUDY (Ferland et al. 2013) together with the UV background radiation given by Haardt & Madau (2012).

The MW-sized halo is initially identified from a dark matter only parent simulation through its merger history and final dark matter halo mass. It is isolated, has not experienced a major merger in its merger history since at least \( z = 2 \) and has a final mass of approximately \( 10^{12} \, M_\odot \). A major merger is defined as a merger of haloes with a 10:1 mass ratio. The particles within a high-resolution region, typically larger than the virial radius, then undergo additional levels of refinement in mass while the region’s spatial resolution is increased. Each nested level is equivalent to an increase in spatial and mass resolution by a factor of two and eight, respectively. Contamination occurs if larger mass particles cross the region of interest (O’Toole et al. 2014). In our simulations, we define a high-resolution region of three virial radii from the centre of the halo to carry out the refinement (Simpson et al. 2018) as a preventive measure. We use three nested levels, giving an effective resolution of \( 2048^3 \) particles or a nested dark matter particle mass of \( 1.104 \times 10^7 \, M_\odot \). This nested simulation is evolved with an additional five levels of AMR which is only allowed around particles within the high-resolution region, resulting in a maximum resolution of eight levels of spatial refinement or 2.196 comoving kpc (ckpc). This simulation setup is similar to that presented in a wide range of works with different aims over several years such as Becerra & Escala (2014), Norman et al. (2015), Butsky et al. (2017), Butsky & Quinn (2018), Hummels et al. (2018) and Holguin et al. (2019). In the more recent works by John et al. (2019), Peebles et al. (2019), Hummels et al. (2019), Prasad et al. (2020) and Chen & Chen (2020), the Cen & Ostriker model is still employed in high resolution hydrodynamical simulations.

From the high-resolution region of the MW halo, we identify an additional smaller halo with a mass of approximately \( 10^{10} \, M_\odot \). We then run a separate simulation zooming in only on this halo with two additional levels of initial nesting. The purpose of this smaller halo is to test the universality of the optimal feedback parameters from the MW zoom simulation. Due to the additional nesting levels, the dwarf is made up of approximately the same number of dark matter particles as in the MW halo. The increased mass resolution translates into an effective resolution of \( 512^3 \) particles or a nested dark matter particle mass of \( 1.715 \times 10^5 \, M_\odot \). Because of the additional nested levels, we reduce the number of AMR levels to three, maintaining a constant maximum spatial resolution of 2.196 ckpc.

### 2.1 Star formation parameters

This paper employs the model described by Cen & Ostriker (1992) with modifications for the purpose of calibration. This model is one of the most commonly used in Enzo. The conditions required for star formation in a cell include:

(i) No further refinement within the cell
(ii) Gas density greater than a threshold density: \( \rho_{\text{gas}} > \rho_{\text{threshold}} \)
(iii) Convergent flow: \( \nabla \cdot \mathbf{v} < 0 \)
(iv) Cooling time less than a dynamical time: \( t_{\text{cool}} < t_{\text{dyn}} \)
(v) Gas mass larger than the Jeans mass: \( m_{\text{gas}} > m_{\text{jeans}} \)
(vi) Star particle mass is greater than a threshold mass

For the cooling time criterion (iv), there is a check for gas with temperature less than 11,000 K that overrides the check for \( t_{\text{cool}} < t_{\text{dyn}} \). In general, the equilibrium temperature for gas with number density above \( 1 \, \text{cm}^{-3} \) is less than \( 10^4 \, \text{K} \), so both rapidly cooling gas and cold, neutral gas will be successfully flagged for star formation.

We set \( \rho_{\text{threshold}} \) to be 1000 times the total mean density. This condition allows star formation to occur in a cosmological setting where the mean density is a function of redshift. If all the conditions are fulfilled, the algorithm generates a ‘star particle’ within the grid cell with a mass

\[
m_* = m_{\text{gas}} \times \frac{\Delta \tau}{t_{\text{dy}}} \times f_*
\]

where \( m_{\text{gas}} \) is the gas mass in the cell, \( \Delta \tau \) is the timestep, \( t_{\text{dy}} \) is the dynamical time and \( f_* \) is a dimensionless efficiency factor. The mass of the generated star particle is compared to a user-defined minimum star particle mass. If the mass exceeds the threshold, a star particle will be created. It is positioned in the centre of the cell and possesses the same peculiar velocity as the gas in the cell. It is treated dynamically as all other particles. An equivalent mass of gas to that of the star particle is then removed from the cell to ensure mass conservation.

To calibrate the simulation, certain aspects of the star formation criteria are modified. These include the Jeans instability check, time dependence of star formation, threshold stellar mass and the value of \( f_* \). The following sections will explain the role that each parameter plays: they are organized in the order that each factor is used in the star formation condition check.

#### 2.1.1 Jeans instability check

In item (v) of the list of conditions in Section 2.1, the creation of star particles is only allowed when the gas mass exceeds the Jeans mass of the cell. This criterion is aimed at low resolution simulations that cannot resolve local Jeans masses. However, modern implementations with better resolution resolve such clouds with multiple cells at the star formation threshold density. When the spatial resolution of the simulation is high enough to resolve the Jeans length, this particular check in the star formation routine instead restricts star formation that can occur because an individual cell needs to wait until enough mass has accumulated within it.

#### 2.1.2 Minimum star particle mass

Once a cell fulfils all five conditions for star formation, the final barrier to star formation is the minimum mass of a star particle that will be inserted into the simulation. This threshold is explicitly designed to prevent the production of too many star particles, which can increase computational costs significantly. However, the inability to exceed this minimum star particle mass can lead to a build-up of potential star-forming gas in surrounding cells. This accumulation then reaches a point where a burst in star formation occurs.

#### 2.1.3 Timestep dependence of star formation

Two factors affect the mass of the star particle to be compared to the threshold value as seen in Equation 1: \( \Delta \tau/t_{\text{dy}} \) and \( f_* \). They correspond to the timestep dependence of star formation and a conversion factor respectively. The \( \Delta \tau/t_{\text{dy}} \) factor aims to explicitly satisfy the Kennicutt–Schmidt (KS) relation, which states that a fraction \( f_* \) will turn into stars over a dynamical time. However, this factor is introduced at multiple points in the star formation process, which impedes the promptness of star formation and its associated feedback by only converting a limited amount of gas into stars. By opting for a timestep independent star formation, the factor \( \Delta \tau/t_{\text{dy}} \)
is removed from the calculation shown in Equation 1, resulting in a stellar mass of
\[ m_*= m_{gas} \times f_s, \tag{2} \]
where the symbols have the same meaning as in Equation 1. In this timestep independent approach, the simulation instantaneously converts \( f_s \) of gas into stars in each timestep and the associated feedback will immediately start regulating further star formation. This formulation alters the star formation timescale in the original Cen & Ostriker model from \( t_{dyn}/f_s \) to \( \Delta t/f_s \). This modification greatly improves the efficiency of the star formation and feedback processes but requires further adjustments as discussed in detail in later sections.

As we show in Sections 4.2 and 4.3, the timestep independent star formation model generally leads to a smoother buildup of stellar mass, but not without some additional effects. When we contrast the performance of the simulation, a simulation employing timestep dependent star formation will take roughly a month to complete whereas a similar setup with timestep independent star formation completes in approximately two days, reflecting the production of fewer star particles. Shorter run times allow for more exploration of the parameter space. However, this choice has significant impact on the resulting KS relation. These effects will be quantified and discussed in Section 4. In summary, we calibrate the feedback in two different star formation setups as detailed in Table 1. The reasons for two setups will be discussed in Section 4.3.

### 2.1.4 Star formation efficiency factor, \( f_s \)

As mentioned, regardless of the timestep dependence of star formation, there exists an efficiency factor, \( f_s \), in both Equations 1 and 2. This parameter regulates the conversion efficiency of identified gas mass in a cell to star particles: \( f_s \) can vary from zero to unity but not including the limits where none or all the identified gas mass in the cell is converted to stellar mass respectively. The latter scenario will remove all the gas from the cell, resulting in a cell having a density of zero, crashing the simulation.

### 2.2 Feedback parameters

Although the creation of a star particle is immediate, feedback happens over a longer timescale, designed to mimic the gradual process of star formation. In each timestep, the star forming mass is given by
\[ m_{form} = m_0 \left( \frac{1+t-t_0}{t_{dyn}} \right) \exp \left( -\frac{t-t_0}{t_{dyn}} \right) \left[ 1+\frac{t \Delta t-t_0}{t_{dyn}} \right], \tag{3} \]
where \( m_0 \) is the star particle mass, \( t_0 \) and \( t \) are the creation time of the star particle and current time in the simulation respectively. Through this implementation, according to Equation 3, the rate of star formation increases linearly and peaks after one dynamical time before declining exponentially (Smith et al. 2011).

We adopt the Smith et al. (2011) modification of the Cen & Ostriker (2006) thermal supernova feedback model. The star particles add thermal feedback to a set of neighbouring grids with size and geometry that can be tuned by the user, as distributed stellar feedback. This feedback continues until 12 dynamical times after its creation. In each timestep, feedback is deposited in the form of mass, energy, and metals.

Mass is removed from the star particle and returned to the grid as gas, given by
\[ m_{ej} = m_{form} \times f_{ej}, \tag{4} \]
where \( f_{ej} \) is the fraction of mass removed. The momentum of this gas is
\[ p_{feedback} = m_{ej} \times v_{particle}, \tag{5} \]
where \( v_{particle} \) is the velocity of the star particle and is conserved by Equation 6. It is dependent on both rest mass energy (\( \epsilon \)) and a user-defined fraction, \( \eta \). The amount of feedback energy injected as thermal energy is given by
\[ E_{feedback} = m_{form} \times c^2 \times \epsilon \tag{6} \]
where \( \epsilon \) and \( c \) are the feedback efficiency and speed of light respectively. For an \( \epsilon \) value of \( 10^{-5} \) (Cen & Ostriker 1992), an energy of \( 10^{51} \text{ erg} \) is injected for every \( \sim 56 \text{ M}_\odot \) of stars formed. Metals are returned to the grid cells and their corresponding metallicity is given by
\[ Z_{feedback} = m_{form} \times \left[ \left( 1-Z_{star} \right) \times \eta + f_{ej} \times Z_{star} \right], \tag{7} \]
where \( Z_{star} \) and \( \eta \) are the star particle metallicity and the fraction of metals yielded from the star respectively.

We assume that 25\% of the mass is removed from the star particle and returned to the grid as gas (\( f_{ej} = 0.25 \)) with 10\% of this returned gas being metals (\( \eta = 0.1 \)), consistent with Cen & Ostriker (1992). These values result in a total metal yield of 0.025 of the mass of the star particle, similar to the calculations by Madau et al. (1996). Also, this metal yield is consistent with average values in the MW, with a mean SFR of \( \sim 3 \text{ M}_\odot \text{yr}^{-1} \), a core-collapse supernova rate of 1 per 40 years, and an IMF-averaged metal yield of \( \sim 3 \text{ M}_\odot \) per supernova (Smith et al. 2011). Therefore, we leave the values of both \( f_{ej} \) and \( \eta \) unaltered.

Instead, we focus on the factors that influence the energy injection, both in terms of the amount and the physical extent. We select three factors in the feedback implementation to be varied for the calibration of the simulations. They are \( \epsilon \), radius of feedback \( r \) and number of cells \( n \) within \( r \). The first parameter is related to the amount of feedback energy emitted by the star particle (see Equation 6) while the remaining parameters work together to define the extent of energy injection. These will be described in more detail in the following sections.

#### 2.2.1 Feedback efficiency, \( \epsilon \)

The amount of feedback energy injected as thermal energy is given by Equation 6. It is dependent on both rest mass energy \( m_{form} \times c^2 \) and a user-defined fraction, \( \epsilon \). The former relies on the amount of stellar mass created per timestep (see Equation 3), and the latter defines the percentage of the rest mass energy injected into the IGM. Together with Equation 4, this implementation is similar to the temporal release of Galactic Superwind energy and ejected mass from stars into the IGM discussed in Cen & Ostriker (2006).

| Setup | Jeans instability check | Minimum star particle mass [M_\odot] | Timestep dependence of star formation |
|-------|-------------------------|--------------------------------------|--------------------------------------|
| 1     | ✓                       | 10^5                                 | ✓                                    |
| 2     | ✓                       | 0                                    | ×                                    |
Calibrating star formation and feedback

2.2.2 Feedback energy injection extent

In the original feedback method described by Cen & Ostriker (2006), all of the feedback energy is injected into the grid cell housing the star particle. However, Smith et al. (2011) modified this to allow the feedback to be spread across multiple zones as a means of bypassing the over-cooling issue, where too much energy injected into a single grid cell can result in easy dissipation of the energy before it can impact further star formation. In general, when individual supernovae are not resolved, injected thermal energy is lost to radiative cooling before it can be converted into kinetic energy. This is because the temperatures reached by this method (few × 10^5 K to few × 10^6 K) correspond to very short cooling times due to metal line cooling. Gas typically needs to be heated to greater than ~ 10^7 K before cooling times become longer than the sound crossing time of a grid cell, a necessary condition for conversion into kinetic energy. Before methods that employ direct injection of kinetic energy were introduced (Simpson et al. 2015), the solution introduced by Smith et al. (2011) was to simply add feedback material to a larger region. The larger region will still suffer from some over-cooling issues, but more of the metals (and other feedback material) is able to reach areas of lower density and longer cooling times. Smith et al. (2011) showed that this method was at least somewhat successful in reducing unphysically high star formation rates. In the absence of distributed injection, the thermal energy is radiated away before it can be converted into kinetic energy to drive material outward. This setup is known as distributed stellar feedback, and it is described by \( r \) and \( s \). These parameters work together to define the physical extent of the injection of feedback from the star particle. We can visualise it in terms of a cube surrounding the star particle in the centre. \( r \) is the distance of the cell from the star particle. When \( r = 1 \), it refers to a 3 × 3 × 3 cube since all the cells are within one cell distance away from the star particle. Similarly, when \( r = 2 \), it refers to a 5 × 5 × 5 cube around the star particle. These alternatives are illustrated in two dimensions in the left and right panel of Figure 1 respectively.

The parameter \( s \) gives the number of steps allowed to be taken from the star particle within the cube determined by \( r \). Referring to the left panel of Figure 1, setting \( s = 2 \) corresponds to an allowable two steps of movement away from the star particle, specifying injection within the cells labelled 1 and 2 in the 3 × 3 cube. As the value of \( r \) increases, shown in the right panel of Figure 1, so the maximum accessible value of \( s \) increases. These increased values translate to more flexibility in the usage of distributed stellar feedback.

In summary, we calibrate our simulations with \( \epsilon, r, s \), and \( f_s \) to match the observations. For the remainder of the paper, when discussing the combination of parameters in a simulation setup, they will be referred to as a vector with components \((\epsilon, r, s, f_s)\), e.g., \((1.0 \times 10^{-3}, 1.3, 0.1)\).

2.3 Analysis

Haloes are identified using the Robust Overdensity Calculation using k-Space Topologically Adaptive Refinement (ROCKSTAR) halo finder (Behroozi et al. 2013a). It is a 6-dimensional phase-space finder, using both positions and velocities of particles to locate and define a halo. In regions where the density contrast is insufficient to distinguish which halo hosts a given particle, ROCKSTAR can differentiate subhaloes and major mergers that are close to the centres of their host haloes. This feature is particularly useful in identifying main haloes when creating zoom simulations of lower mass haloes. Analysis of the simulation results is then carried out using the yt analysis toolkit (Turk et al. 2011).

3 OBSERVATIONAL CALIBRATIONS

3.1 Baryon content of cosmic structures

The main observables matched in this suite of simulations are taken from the work of McGaugh et al. (2010), where the authors attempted to quantify the distribution of baryonic mass within cosmic structures. Galaxies are broadly categorised into rotationally supported and pressure supported systems. These are further divided into stellar dominated spiral galaxies and gas dominated galaxies for the rotationally supported system, and elliptical galaxies, local group dwarfs and some clusters of galaxies for pressure supported systems. The primary method for determining the total mass budget in the different systems is their equivalent circular velocity \( V_c \) obtained through various methods described in detail in McGaugh et al. (2010) and summarised in Table 2.

In their analysis, McGaugh et al. (2010) chose to present their results using \( r_{500} \), a radius where the enclosed density is 500 times the critical density of the universe. The main result presented in Figure 2 of McGaugh et al. (2010) relates the fraction of expected baryons that are detected,

\[
f_d = \frac{m_b}{f_b \times m_{500}},
\]

and the conversion efficiency of baryons into stars,

\[
f_s = \frac{m_s}{f_b \times m_{500}},
\]

where \( m_b \) and \( m_{500} \) refer to the baryonic and total mass within this radius respectively, and \( f_b \) is the universal baryon fraction determined to be 0.17 ± 0.01 (Komatsu et al. 2009). One important point to note is that these fractions are dependent on the choice of radius. To facilitate comparison of our results with this paper, we

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Table 2. Methods of determining \( V_c \) for different gravitationally bound systems (see McGaugh (2005); Hoekstra et al. (2005); Gavazzi et al. (2007); Walker et al. (2007, 2009); Simon & Geha (2007); Giodini et al. (2009)).

| Gravitationally bound systems | Methods |
|-----------------------------|---------|
| Stellar dominated spiral galaxies | Rotation velocities |
| Gas dominated galaxies | Baryonic Tully-Fisher relation |
| Elliptical galaxies | Gravitational lensing |
| Local group dwarfs | Direct measurement |
| Clusters of galaxies | Hot X-ray emitting gas |

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\[ r = MNRAS, 000, 1–18 (2019) \]
produced the following fitting formula to the data from Figure 2 in McGaugh et al. (2010), which we illustrate in Figure 2:

\[
\frac{f_d}{f_d^0} = 1 + e^{-x}, \tag{10}
\]

and

\[
\frac{f_s}{f_s^0} = 0.91 \exp \left( \frac{-x^2}{2} \right) \times \frac{f_d}{f_d^0}, \tag{11}
\]

where

\[
x = \log_{10} \left( \frac{m_{500}}{M_\odot} \right) - 12.91 \tag{12}
\]

and

\[
y = \log_{10} \left( \frac{m_{500}}{M_\odot} \right) - 12.19 \tag{13}
\]

We aim to calibrate our suite of simulations to yield a good match to these fits. Also, we will compare our simulated galaxy properties to the Kennicutt–Schmidt relation, which serves as an additional constraint.

3.2 Kennicutt–Schmidt relation

The KS relation is a measure of the correlation between gas surface density and the SFR per unit area. From the work of Schmidt (1959); Kennicutt (1989, 1998); Kennicutt et al. (2007); Bigiel et al. (2008), there appears to be a tight correlation between these measured properties on galactic scales (∼ kpc). This strong relation makes it one of the critical observations that simulations with star formation attempts to match.

We adopt a similar methodology to that of the AGORA project (Kim et al. 2016). The SFRs are calculated using the mass of star particles and time-averaged over the past 20 Myrs of the simulation snapshot. Together with the gas density, they are then deposited onto a fixed resolution grid of 750 pc, consistent with the methodology of Bigiel et al. (2008), to derive the SFR and gas surface density required by the KS relation. As in Section 3.1, these values are obtained within \( r_{500} \) of the halo. In fact, we find that the conclusions drawn are insensitive to changes in the grid resolution. With non-zero SFR surface density patches, we will also compare our results to

\[
\log \Sigma_{\text{SFR}} = 1.37 \log \Sigma_{\text{gas}} - 3.78, \tag{14}
\]

which is obtained from the best observational fit given by Equation 8 in Kennicutt et al. (2007).

4 RESULTS

4.1 MW galaxy zoom simulations with Setup 1

We explore the parameter space by switching on the Jeans instability check, applying timestep dependent star formation and setting a threshold star particle mass of \( 10^5 M_\odot \) (Setup 1); see Table 1. With this setup, we run a total of 22 simulations by modifying \( f_s \) (see Equation 1), \( \epsilon \) (see Equation 6), \( r \) and \( s \) (see Section 2.2.2), as shown in Figure 3. This explored region of parameter space is motivated both physically and numerically. Cen & Ostriker (1992) applied a value of \( \epsilon = 10^{-4.5} \), which is similar to other work (Ostriker & Cowie 1981; Dekel & Rees 1987). The values of \( r \) and \( s \) are restricted by the maximum number of cells used to define a grid. Lastly, we can constrain the range of values that \( f_s \) can take with the ratio of \( f_s \) to \( f_d \). From McGaugh et al. (2010), \( f_s \) is limited between 0.1 and 0.9 approximately across the halo mass range.

Out of the 22 simulations, we classify the runs into those that reached \( z = 0 \) (completed) and those that did not (failed) since we are interested in the relevant properties at \( z = 0 \). A fraction of the simulations were unable to reach the final redshift due to uncorrectable errors in the hydrodynamics solver, mostly associated with extreme star formation and/or feedback parameters. Since the failed simulation contains extreme feedback parameters, e.g., large amount of feedback energy, it is unlikely that this prescription will result in the best match to the observed properties, presented in Section 4.1.1. Overlapping points with conflicting conclusions exist in Figure 3 because as we are showing the 2-dimensional projection of the 3-dimensional parameter space.
Figure 3. Overview of parameter space exploration using a total of 22 different combinations of \( f_\ast, \epsilon \) and \( r \) with Setup 1. The plots are \( \epsilon \) against \( f_\ast \) (top left), \( \epsilon \) against \( r \) (top right) and \( r \) against \( f_\ast \) (bottom left). The green dots and red crosses represent runs that reached and failed to reach \( z = 0 \) respectively. We can identify regions of parameter space more likely to result in the inability of the simulation to reach \( z = 0 \) and the causes are explained in more detail in Section 4.1.

4.1.1 Comparison to baryonic properties from McGaugh et al. (2010) – Setup 1

Initially, we attempted to cover the parameter space optimally with minimal numbers of simulations using Latin Hypercube Sampling (McKay et al. 1979). We wanted to minimise the maximal distance between various points in our feedback parameter space as described by Heitmann et al. (2009). However, due to the failure of several runs to reach \( z = 0 \), it is not possible to obtain a space-filling design. Therefore, we try a more fundamental approach to quantify how changing each parameter will affect the observables. This result is presented in Figure 4, showing a plot of \( f_s \) against \( f_d \) across a range of \( m_{500} \).

From the initial values of \((1.0 \times 10^{-5}, 1, 3, 0.1)\), we vary \( \epsilon \) only, which corresponds to a change in the strength of feedback. Increasing the strength of feedback reduces both the \( f_s \) and \( f_d \) parameters of the halo (see the blue arrow in Figure 4). This evolution can be easily explained by the increased expulsion of gas due to stronger feedback, reducing the amount of fuel available to form stars, which leads to a decrease in \( f_s \). The removal of gas also causes the amount of baryons within \( r_{500} \) or \( f_d \) to decrease.

We then try to increase \( f_\ast \). This change has a direct impact on the total stellar mass as more gas mass is converted into stars. However, this increased star formation yields stronger feedback. Therefore, the net result of increasing \( f_s \) is similar to increasing \( \epsilon \), which decreases both \( f_s \) and \( f_d \) (see the green arrow in Figure 4). To a lesser extent, however, this effect is evident from the small transition of the cyan point to the purple point on the top right of the plot. To improve the clarity of an increase in \( f_\ast \), we add another green arrow connecting another set of data points (grey and light green dots). This difference in the impact of \( f_\ast \) also suggests its sensitivity to other feedback parameters.

The last parameters to adjust are \( r \) and \( s \). Essentially, we are increasing the size of the cube into which the feedback energy is injected (see Figure 1). By increasing \( r \) (and, correspondingly, \( s \)), \( f_s \) and \( f_d \) are reduced, similarly to the effect of increasing \( \epsilon \) and \( f_s \). However, this phenomenon only persists until \( r = 3 \) and \( s = 9 \), which corresponds to a \( 7^3 \) box or 343 cells centred around the star particle. Beyond this point, the trend changes when a further extension of the feedback injection decreases \( f_s \) but increases \( f_d \), indicating the presence of a turnaround point. As energy is deposited further from the star particle, the gas is kept away at a larger distance from the centre of the gravitational potential well as seen in Figure
Enclosed Gas Mass $[M_\odot]$  

$0.0$ $0.2$ $0.4$ $0.6$ $0.8$ $1.0$ $1.2$ $1.4$  

$0.0$ $0.2$ $0.4$ $0.6$ $0.8$ $1.0$ $1.2$ $1.4$  

Figure 4. Graph of the stellar mass fraction $f_s$ against the detected baryon fraction $f_d$ across a range of $m_{500}$. The colour coded curve shows the values of $f_s$ and $f_d$ corresponding to the mass range indicated. Cross marks on this curve shows the values to be matched. It includes the mean of $m_{500}$ with the upper and lower limits given by the maximum and minimum $m_{500}$ from the simulations plotted. Dots represent simulation with different feedback parameters and contrasting coloured arrows show effects of increasing a particular parameter. From the ensemble of simulations, $(2.5 \times 10^{-5}, 1.3, 0.2)$ yielded the most realistic baryonic makeup for the simulated MW galaxy. For a detailed description, refer to Section 4.1.1.

Figure 5. Cumulative plot of $m_{\text{gas}}$ against halo radius. The different coloured lines represent simulations of various $r$ and $s$. As the extent of feedback injection is increased beyond $r = 3$ and $s = 9$, the amount of baryons in the outer region of the halo is significantly higher. This trend highlights the inhibition of gas collapse to form stars as the extent increases, providing support for the explanation given in Section 4.1.1 for the trend in Figure 4.

As a result, $m_\odot$ decreases as fewer stars form due to a deprivation of fuel for star formation while $m_{\text{gas}}$ increases as more gas is now present. Increasing the physical extent of feedback injection beyond $r = 3$ and $s = 9$ only serves to dilute the amount of feedback energy per cell, leading to gas remaining near the virial radius of the halo. Thus $f_d$ increases while $f_s$ decreases. Furthermore, the average number of cells within a single grid in an Enzo simulation is not likely to be much larger than about $7^3$, so extending beyond $r = 3$ and $s = 9$ should be avoided as feedback is only deposited on the local grid. When a star particle lies on the edge of a grid, Enzo shifts the feedback region in order to contain it entirely within the grid. This practice is common to all of the feedback methods within Enzo, as communicating feedback information across different grids introduces significant computational complexity and cost.

From the 16 completed simulations, the combination of parameters that yielded the most MW-like properties in the halo is $(2.5 \times 10^{-5}, 1.3, 0.2)$, which is represented by the pale green dot in Figure 4. The halo contains a stellar mass comparable to the MW while having approximately 50% more baryon mass than the MW halo. This point is the closest match to the target for the region of parameter space that we sampled. The next best set of parameters that produce halo properties matching the target is $(5.0 \times 10^{-5}, 1.3, 0.1)$. While it provides a better $f_d$ agreement, the value of $f_s$ is approximately zero. From the trends and the best match in Figure 4, further improvement in the agreement of halo properties will only be marginal. In order to achieve a better agreement, we suggest including other free parameters or even modifying the star formation and feedback model. Furthermore, this set of parameter
is determined for a quiescent halo as discussed earlier. Success of this calibrated feedback prescription is likely to be dependent on the growth history as well. However, it is not within the scope of this work to design such modifications or test the robustness of our calibration against different merger histories.

4.1.2 Kennicutt–Schmidt relation – Setup 1

As discussed earlier, the KS relation provides an additional constraint on the feedback calibration beyond the global baryon makeup of a MW halo. To apply this constraint, we use the methodology described in Section 3.2 to compare and contrast with the observed KS relation (blue line) in Figure 6. We also include a rough approximation of the observed values of nearby galaxies from Bigiel et al. (2008) in the form of blue hatched contours.

The results show that the simulation data intersect with observations and the fit given by Equation 14, but the slopes of the simulation data differ from the KS relation in every feedback prescription. Most of our simulations manage to reproduce the characteristic ‘threshold’ gas density value of approximately $10 \ M_{\odot} pc^{-2}$, which marks the transition point between high and low star formation efficiency and is apparent from the blue hatched contour. The slopes of the relations in the simulations do not appear to be significantly different from each other despite changes in the subgrid physics parameters. However, they are consistently steeper than the gradient of the observed relation.

When increasing $e$, we observe a shift towards lower SFR but higher gas density from the transition between the green circles ($1.0 \times 10^{-5}$, $1.3$, 0.1) and the red squares ($5.0 \times 10^{-4}$, $1.3$, 0.1). This shift can be explained by the higher feedback energy budget associated with a larger $e$ value, which inhibits further star formation. The simulation data points are insensitive to any increase in $r$ until $r = 3$. Beyond which, comparable SFR densities are associated with higher gas densities (compare green crosses ($r = 4$) and pink diamonds ($r = 5$)). This trend is consistent with the explanation provided for Figure 5. Lastly, from the data points of ($1.0 \times 10^{-5}$, $1.3$, 0.1) and ($1.0 \times 10^{-5}$, $1.3$, 0.2), it appears that increasing $f_d$ does not affect the relation significantly.

The best parameter values (purple hexagon) lie along with the KS relation fit but deviate from observations as they are clustered around high gas densities. This discrepancy with Bigiel et al. (2008) suggests that the combination of $e$ and $f_d$ is too strong, creating patches of lower gas surface density. However, adjustment of either factor will, in turn, affect $f_s$ and $f_f$, leading to a halo that reproduces the KS relation instead of the observations of McGaugh et al. (2010).

4.1.3 Haloes in the high-resolution region – Setup 1

Since we specify a safety factor of three virial radii to prevent contamination of the MW halo in the zoom simulation, there are other central and satellite haloes of varying mass in this region. Figure 7 illustrates the properties of other central haloes in the simulation with the best feedback prescription of ($2.5 \times 10^{-4}$, $1.3$, 0.2). This plot is not presented in a similar way to Figure 4 because we are looking at a range of halo masses. Instead, we populate Figure 2 with the corresponding $f_s$ and $f_d$ of various central haloes in the high-resolution region of the MW galaxy zoom simulation.

We present the graph of $f_d$ against $m_{500}$ on the upper panel and $f_s$ against $m_{500}$ on the lower panel of Figure 7. The black lines are Equations 10 and 11 fitted to the observations (blue dots). From the graph of $f_d$ on the lower panel, the properties either match observation well or do not form stars at all ($f_s = 0$), which is represented by a red star and grey cross respectively. The same cannot be said for the $f_d$ relation on the left where there are vastly different properties with no apparent relation to the $f_d$ values. We see lower mass haloes with $f_d$ reaching 1.4, exceeding that of the universal baryon fraction while possessing $f_s$ that is close to observations. These haloes are in contrast to the MW halo (rightmost red star), which hints at the need for additional modifications required to understand and determine if this discrepancy is a numerical byproduct due to the fractional mass resolution of the lower mass halo. Therefore, we attempt a zoom simulation of a dwarf galaxy around $10^{10} M_{\odot}$, resolved by a comparable number of dark matter particles to the MW halo, to investigate if the conclusion from Figure 7 is due to resolution and whether this feedback prescription is universal.

4.2 Dwarf galaxy zoom simulations with Setup 1

Using the combination of parameters ($2.5 \times 10^{-4}$, $1.3$, 0.2), we implement the feedback prescription in a dwarf galaxy with a mass of approximately $10^{10} M_{\odot}$. However, the results indicate an absence of stars within the halo, consistent with Figure 7. Reviewing the star formation routine (see Section 2.1), we find that the Jeans instability check is the bottleneck of star formation. Due to the spatial resolution implemented in this dwarf galaxy, according to the discussion in Section 2.1.1, the Jeans instability check restricts star formation that should occur in reality. Therefore, to allow star formation, we switch off this Jeans instability check in the star formation routine. We label such runs as NJ.

Figure 8 illustrates the virial (black) and stellar mass evolution (red) in the dwarf galaxy with different setups (solid vs. dashed lines). As expected, removing the Jeans mass criterion allows stars to form in the dwarf galaxy zoom simulation (solid red line). However, star formation starts around $z \approx 2$, which is late as compared to the MW zoom simulation, for which star formation commenced at $z \approx 6.5$. Further investigations yielded the conclusion that the star formation threshold mass is the next limiting factor. Therefore, we reduce the threshold mass for star particle creation to zero, which relaxes the condition for star formation, allowing star particles to be created at $z = 8$ in the simulation. On top of these changes, we switch off the timestep dependence of star formation. This results in Setup 2 as shown in Table 1.

The purpose of $\Delta t/\Delta t_{dyn}$ in Equation 1 is to ensure the adherence of star formation to the KS relation. However, in Equation 3 where feedback is modelled to occur across time, there are additional factors of $\Delta t/\Delta t_{dyn}$ present to regulate these processes according to the KS relation. Hence, by switching to timestep independent star formation, we improve the promptness of the feedback. Lastly, since star formation is now instantaneous once conditions are met, high-density regions of gas are absent, reducing the time used to calculate the hydrodynamical evolution in the simulation. This absence of high-density gas is evident from the number of timesteps required for the evolution to reach $z = 0$ and the time per timestep. For an identical feedback prescription, Setup 1 takes 1263 timesteps and $\sim 435 \ s$ per timestep to reach $z = 0$, which is in stark contrast to Setup 2 where it takes 663 timesteps and $\sim 125 \ s$ per timestep for the simulation to reach $z = 0$. The net result is an improvement in the speed of completion of simulations from weeks to days.

In summary, we modify the setup to switch off the Jeans instability check, turn off the timestep dependence of star formation and remove the requirement of a minimum star particle mass. This results in Setup 2 shown in Table 1. This setup enables us to recover a more realistic star formation history beginning at $z \sim 8$ (see Figure 8), which is the main motivation for the switch in setup.
Figure 6. A graph of SFR surface density against gas surface density illustrating the KS relation. Different coloured points are simulation data from sub-kpc resolution consistent with rough approximation from the observations in nearby galaxies by Bigiel et al. (2008) represented by the blue hatched contours. The blue line is derived from the observational fit of Kennicutt et al. (2007). There is overlap between the simulation and observation but there are differences that will be discussed in Section 4.1.2.

Figure 7. Graph of (a) the detected baryon fraction $f_d$ against $m_{500}$ and (b) the stellar mass fraction $f_s$ against $m_{500}$ with equations described in Section 3.1. The black line represents the fit given by Equation 10 and 11. The blue dots are points from McGaugh et al. (2010) and the crosses and stars are properties of haloes with various mass from the most refined region in the simulation. The black cross and red star refer to haloes in the most refine region with zero and non zero $f_s$ respectively. Other than the most massive halo (MW halo), other haloes struggle to contain the appropriate amount of stars and gas. Refer to Section 4.1.3 for a detailed description.
4.3 Simulations with Setup 2

Due to star formation issues in the dwarf galaxy zoom simulations, we make significant changes in the simulation setup. In Section 4.2, we show that the stellar mass of a dwarf galaxy at $z = 0$ changed from zero to $\approx 10^8 \, M_\odot$ by switching to Setup 2. We now have to review the results of the MW galaxy presented in Section 4.1. Figure 9 shows the evolution of the dark matter and stellar mass of the MW halo in different setups. The lines and labels are similar to Figure 8.

From the identical dark matter mass evolution in Figure 9 for different setups (black lines), we know that we are comparing the same halo across simulations. However, the stellar mass evolution paints a different picture. Comparing both setups, although the haloes start forming stars at the same time ($z = 6.5$), the simulation using Setup 2 has a lower initial and final stellar mass as a result of its corresponding relaxed star formation conditions. With the minimum mass of the star particles set to zero, the stars are allowed to form with a smaller mass, which explains a lower starting point in Setup 2. Between $z = 1$ and $z = 0$ in Setup 1, we note a spike in stellar mass due to the build up of gas eligible for star formation (see Section 2.1.3). Despite these differences in the star formation history, the most significant one is the stellar mass of the halo at $z = 0$. The final stellar mass of the MW halo in Setup 1 is approximately $10^{10} \, M_\odot$, which is two orders of magnitude higher than that in the new run with a value of roughly $10^8 \, M_\odot$. This difference means that these haloes have vastly different $f_d$ and $f_s$.

Due to the non-linear coupling of the various processes, changing individual prescriptions always requires new parameter fitting (Crain et al. 2015). With a new star formation setup, we have to re-explore the feedback parameter space with Setup 2. However, we have two distinct advantages as compared to before. The first is that we understand the general effects changing the feedback parameters have on the $f_s$ and $f_d$ of the halo (see Figure 4). Secondly, the simulations will complete much faster, allowing us to obtain more data points, both in general feedback parameter space and in the region around the best match to observations. This improvement will help us narrow down the feedback prescription, and possibly identify more than one combination that yields a close match.

4.4 MW galaxy zoom simulations with Setup 2

We perform the following parameter space exploration with Setup 2 in Table 1. With this setup, we run a total of 49 simulations in order to calibrate the feedback prescription, and we make a similar classification as before, shown in Figure 3. We summarise the various properties of the halo of interest of simulations with Setup 1 and 2 in Table 3. This table includes simulations that will be discussed in Sections 4.5 and 4.6.

From the 49 simulations, only one simulation with $(3.0 \times 10^{-5}, 1.1, 1.0)$ failed to reach $z = 0$ due to the complete removal of gas when stars form. The process of iteration started from the best combination of parameters found in Section 4.1.1. $(2.5 \times 10^{-4}, 1.3, 0.2)$ and progressed based on the trends found in Figure 4 to move the simulation data point closer to the target. This process will be explained later. We introduce a measure of closeness between the simulated and the observed galaxy properties via the Cartesian distance to the target,

$$d = \sqrt{(f_s(\text{sim}) - f_s(\text{obs}))^2 + (f_d(\text{sim}) - f_d(\text{obs}))^2}, \quad (15)$$

where subscripts sim and obs refers to simulation and observation respectively. Lower values of $d$ represent a more realistic simulated galaxy in terms of both $f_s$ and $f_d$. For the goodness of fit of individual properties, we refer to Table 3.

Comparing the feedback parameter values covered in both Setup 1 and 2, it is clear that they do not cover an equal area of parameter space. The main differences lie in the usage of high $f_s$.  

However, we do not compare the properties of the dwarf galaxy to observations for reasons that will be explained in Section 4.3.
while having low values of $r$ and $\epsilon$ in Setup 2 as compared to Setup 1. There are two significant volumes of parameter space not covered in Setup 2: large values of $\epsilon$ coupled with low $r$ and $f_\ast$, and large values of $r$ with low values of $\epsilon$ and $f_\ast$. Also, there are regions (intermediate values of $\epsilon$ and $f_\ast$, high values of $r$ and intermediate values of $f_\ast$) in the parameter space of Setup 2 that are not sampled. The reason why we do not have any simulations in these regions will be explained in the next section with Figure 10.

4.4.1 Comparison to Baryonic properties from McGaugh et al. (2010) – Setup 2

We will identify the best star formation and feedback parameters through an iterative process beginning from the initial point $(2.5 \times 10^{-4}, 1_3, 0.2)$ from before, applying the knowledge of trends from Figure 4. We use arrows to represent the general movement of data points due to the initial adjustments of $f_\ast$ and $\epsilon$ before using $r$ and $s$ for the finer last adjustments on the $f_\ast$ and $f_d$ plane. We present this with a representative set of simulations in Figure 10, similar to Figure 4 by starting from the best combination of parameters (blue dot) in Setup 1. It is evident that identical feedback prescription in different settings produced a MW with disparate $f_\ast$ and $f_d$. In Setup 2, the previously optimal values produced a MW galaxy with minimal stellar mass. This small amount of stars at $z = 0$ is a result of the relaxed star formation conditions producing numerous small star formation events, which instantly yield feedback and reduces future star formation.

From the starting point, we increase $f_\ast$ from 0.2 to 0.9 (see green arrow in Figure 10). This trend indicates that as $f_\ast$ increases, $f_d$ decreases while $f_\ast$ stays constant, which is in agreement with the combination of effects of the green and blue arrows shown in Figure 4. Despite only having two data points, we know from the direction given by the green arrow in Figure 4 that it will have the same effect on the properties as increasing $\epsilon$ (blue arrow). Therefore, if we increase $f_\ast$ further in Figure 4, we can expect it to follow the last blue arrow, which is a horizontal motion of decreasing $f_d$ with constant $f_\ast$. Together with the immediate feedback from stars, increasing $f_\ast$ converts more gas into stars, which reduces the amount of gas, leading to the decline in $f_d$. Although more stars form initially, the feedback is stronger, reducing the amount of gas available to form more stars as the halo aged, resulting in a constant $f_\ast$. Therefore, we increase $f_\ast$ in an attempt to move the data point as far left as possible in Figure 10 in preparation for the next step. The simulation with $f_\ast = 1.0$ does not produce a MW galaxy with significantly different $f_\ast$ and $f_d$. Furthermore, this value of $f_\ast$ caused the only failed run from 49 simulations. Hence, we settle on a $f_\ast$ value of 0.9 (orange dot) as the starting point for the next phase of iteration.

After obtaining the minimal $f_d$ with $(2.5 \times 10^{-4}, 1_3, 0.9)$, we attempt to increase $f_\ast$ and $f_d$ in the next iteration to move closer to the target. From what we have learned from Figure 4, we can achieve this by either decreasing $\epsilon$ or $r$. Since $r$ is already at a minimum, lowering $\epsilon$ is the only option. We present only a representative set of data points connected by the blue arrows to illustrate the general change in $f_\ast$ and $f_d$ due to smaller $\epsilon$ values. This increase in $f_\ast$ and $f_d$ is in agreement with Figure 4, explained by the less efficient
baryon expulsion, which leads to higher star formation and retention of gas within $\Sigma_{500}$.

The final step is to adjust $r$ and $s$ to improve the match to the observed $f_5$ and $f_d$. Initially, we maintain the injection of feedback energy in a cube and increase the size, i.e., from $r = 1$ and $s = 3$ to $r = 2$ and $s = 6$. The aim is to obtain a point to the top right of the target and increase $r$ and $s$ correspondingly to move it towards the target as predicted by Figure 4. However, we do not obtain any good fit. Coupled with an upper limit to the extent of feedback injection where $f_d$ increases instead beyond $r = 3$ and $s = 9$ (see Figure 4), we decide to change the shape of energy injection from a cube to just the adjacent cells centred around the star particle. In parameters terms, we change $r = 1$ and $s = 3$ to $r = 1$ and $s = 1$. As a result, the feedback energy is injected into four instead of 27 cells, effectively increasing the energy concentration per cell by approximately an order of magnitude. This increased energy density causes a larger decrease in $f_d$ than in $f_5$. In contrast, increasing the extent of feedback injection maintained in a cube region generates a comparable change in both $f_d$ and $f_5$.

We determine $(2.5 \times 10^{-3}, 1, 0.9)$ and $(3.0 \times 10^{-3}, 1, 0.9)$ as the two sets of parameters able to produce the smallest $d$ value (see Table 3). Given the vast area of unexplored parameter space and the starting point of the iterative process, we justify that the steps taken constitute the most reasonable route through parameter space that can produce a close match to observations. The starting values of $(2.5 \times 10^{-4}, 1, 0.2)$ define the boundaries where values can be adjusted. $r$ and $f_5$ are almost at the minimum, meaning they can only increase while $\epsilon$ can either decrease or increase. Furthermore, the low $f_5$ of the starting point of properties in Figure 10 suggests that the current feedback is too strong that it restricts star formation.

Together with the trends of changing parameters, the possible motions of the data point are a horizontal movement to the left or right, and diagonally right. The worst possible option is to increase $\epsilon$, moving the data point to the left. This choice leaves us stranded because we cannot create further motion since $r$ and $f_5$ are already close to their minimum values. The next possible option is to increase $r$ above 3, causing the data to move horizontally right. The next steps associated with this first movement will be decreasing $\epsilon$ to iterate data points towards the top right before increasing $f_5$ to reduce the data to match the target. However, given the initial movement away from the target, we believe that this will not produce a better match than what is presented. The most plausible option is to decrease $\epsilon$, moving the data point along the blue arrow indicated in Figure 10. $f_5$ can then be increased to move it down diagonally left towards the target while fine-tuning $r$ and $s$. This change is preferred over increasing $r$ because of the turn around expected beyond $r = 4$, which limits the degrees of freedom. However, following this option will generate a combination of parameters similar to what we have found. Out of the possible options to move the initial point in parameter space, we have chosen the path that will produce the best match to fit the observational data from McGaugh et al. (2010). Since the argument put forth does not mention the possibility of an ideal set of parameters lying in the region of parameter space.
energy injection that lowers the gas density. more efficient conversion of gas into stars, leading to more feedback and compare it to the fit given by Equation 14 and observations of nearby galaxies by Bigiel et al. (2008), shown in Figure 11. There is a clustering of points around the fit but no slope can be deduced from the points. Also, the simulated gas density is too low for comparison to observational data. We believe the concentration of points around low surface gas density is due to the relaxed star formation criteria and the higher \( f_\epsilon \) and \( f_s \). These conditions result in a more efficient conversion of gas into stars, leading to more feedback energy injection that lowers the gas density.

While \( 3.0 \times 10^{-5}, 1_1, 0.9 \) and \( 2.5 \times 10^{-5}, 1_1, 0.9 \) recover \( f_\epsilon \) and \( f_s \) well, there is an absence of patches with high gas surface density, restricting our ability to probe the KS relation in that regime. This absence also suggests that feedback might have been too efficient in driving gas out of the central region of the galaxy. Comparing Setup 2 to Setup 1, the former is not as good in recovering the KS relation. Setup 2 provides a relatively more instantaneous conversion of gas into stars, which drives gas surface density to lower values. Despite the similarity in the stellar mass in Setup 1 and 2, the buildup of the mass is different. The star particles formed in Setup 2 are numerous and less massive as compared to Setup 1, which impacts the surrounding medium in different ways. Coupled with the high conversion efficiency of gas to stars, it empties the central region of the galaxy of gas, explaining why the gas surface density is low.

4.4.2 Kennicutt–Schmidt relation – Setup 2

In this section, we will present the agreement of star formation in the simulation with the KS relation described in Section 3.2. As in Figure 6, we choose non-zero SFR patches within \( r_{500} \) at \( z = 0 \) and compare it to the fit given by Equation 14 and observations of nearby galaxies by Bigiel et al. (2008), shown in Figure 11. There is a clustering of points around the fit but no slope can be deduced from the points. Also, the simulated gas density is too low for comparison to observational data. We believe the concentration of points around low surface gas density is due to the relaxed star formation criteria and the higher \( f_\epsilon \) and \( f_s \). These conditions result in a more efficient conversion of gas into stars, leading to more feedback energy injection that lowers the gas density.

While \( 3.0 \times 10^{-5}, 1_1, 0.9 \) and \( 2.5 \times 10^{-5}, 1_1, 0.9 \) recover \( f_\epsilon \) and \( f_s \) well, there is an absence of patches with high gas surface density, restricting our ability to probe the KS relation in that regime. This absence also suggests that feedback might have been too efficient in driving gas out of the central region of the galaxy. Comparing Setup 2 to Setup 1, the former is not as good in recovering the KS relation. Setup 2 provides a relatively more instantaneous conversion of gas into stars, which drives gas surface density to lower values. Despite the similarity in the stellar mass in Setup 1 and 2, the buildup of the mass is different. The star particles formed in Setup 2 are numerous and less massive as compared to Setup 1, which impacts the surrounding medium in different ways. Coupled with the high conversion efficiency of gas to stars, it empties the central region of the galaxy of gas, explaining why the gas surface density is low.
the level of agreement with observations is much better in Figure 12 than Figure 7 as points lie closer to the fit. For haloes below $10^{10}\,M_\odot$, it is plausible that the lack of mass and spatial resolution is the cause of their inability to form stars. On the other hand, the larger mass haloes that suffer the same problem require future zoom simulations to be carried out in order to identify the root of the issue.

4.5 Dwarf galaxy zoom simulation with Setup 2

We conduct zoom simulations of a dwarf galaxy with $m_{\text{vir}}$ of approximately $10^{10}\,M_\odot$ as an additional test of the universality of the feedback parameters in different halo mass bins. We described how we pick this dwarf galaxy from the high-resolution region of the MW zoom simulation in Section 2. Similarly, we increase the number of nested levels to keep the number of particles defining the halo constant with that of the MW while keeping the spatial resolution constant. We then compare the $f_s$ and $f_d$ of the halo to McGaugh et al. (2010) in Figure 13.

We present a close-up view of the parameter space in Figure 13 because we are showing results from zoom simulations of the dwarf galaxy using the two best sets of parameters only. It is clear that the $f_s$ and $f_d$ of the simulated galaxy in both feedback prescriptions are comparable to the target. We expect good agreement based on the results of Figure 12. Therefore, we argue that this feedback prescription is insensitive to mass resolution with a smaller mass halo having a lower and higher resolution in Figures 12 and 13 respectively. However, it is also essential to investigate the dependence of the feedback prescription on spatial resolution in future work.

4.6 Chaos and variance

Recognising the argument put forth by Keller et al. (2019) for chaotic variance in numerical simulations, we conduct our zoom simulations twice on different processors. They have identical initial conditions and feedback prescriptions but evolved on different combinations of processors in the same computing cluster. The aim is to find out how much the halo properties would differ from each
other due to the usage of a different set of processors. We quantify this difference in Figure 14.

Dots and stars in Figure 14 represent the pair of simulations with $(3.0 \times 10^{-5}, 1, 0.9)$ (blue) and $(2.5 \times 10^{-5}, 1, 0.9)$ (red) respectively. Despite both of them being close to the target, $f_s$ and $f_d$ for each pair can differ as much as running a simulation with a different set of feedback parameters. Comparing $(3.0 \times 10^{-5}, 1, 0.9)$ run 2 to $(4.0 \times 10^{-5}, 1, 0.9)$ in Figure 10, the simulated galaxies have similar values of $f_s$ and $f_d$. This variance is also apparent from the values of $m_{500}$ where the maximum, minimum and the mean values are shown by the black crosses.

Looking at Figure 14, the deviation in $f_s$ from the pair of simulations is comparable to the 10% difference in stellar mass concluded in Keller et al. (2019) despite not using identical processors. However, the deviation in total baryon mass is as high as 33%, possibly arising from the coupling of star formation and feedback where a 10% difference in stellar mass affects the feedback significantly. There is not a consistent trend observed in Figure 14, i.e., increase or decrease in $f_s$ both cause an increase in $f_d$. We attribute this to these ratios containing a mixture of stellar and gas mass. Due to the complex coupling of star formation and feedback, it is difficult to disentangle the contribution of each component. For example, increasing stellar mass results in a decrease in gas mass but it is unclear which is the more dominant effect. As a result, the baryonic composition of the halo can differ drastically.

5 SUMMARY AND DISCUSSION

We introduce a new method for efficient tuning of sub-grid models in simulations of galaxy formation. Our focus is to explore the physical implications and limitations of a widely used star formation model with the Enzo simulation code. This suite of simulations is also the first application of numerical simulations calibrated to match the baryon content and stellar fraction properties presented by McGaugh et al. (2010). Using the star formation routine of Cen & Ostriker (1992) and the thermal supernova feedback of Cen & Ostriker (2006), we select factors such as $f_s$ to tune the conversion efficiency of gas to stars, $s$ for the feedback energy budget, and lastly, both $r$ and $z$ to calibrate the extent of feedback injection in the simulations. We also identify additional parameters that require adjustments in order to achieve realistic star formation histories. They are the Jeans instability check, the star particle threshold mass and the timestep dependence of star formation. These directly influence the criteria used to determine the occurrence of star formation. With these parameters, we aim to determine the extent of the calibration freedom offered by the Cen & Ostriker model, which is commonly used in Enzo.

It is remarkable that there is such a small variance associated with the data presented by McGaugh et al. (2010). This is the main reason why we strive to improve the agreement between our simulation results and observations as much as possible. However, it is also important to note the possibility of underestimates in the errors and unaccounted systematics. The method of determining the mass of the halo from observations affects the amount of scatter too. If abundance matching is used, $m_*$ will have a lot more scatter than $m_h$ in the Tully-Fisher plane at low mass, leading a corresponding amount of scatter in $f_s$ and $f_d$. Since most of the mass in low mass rotating galaxies is gas and not stars, one can also question the applicability of extrapolating abundance matching relations to such low masses.

With the mentioned parameters, we produce a MW galaxy with realistic baryon and stellar fraction when compared to the observations of McGaugh et al. (2010) with our suite of simulations. We achieve this agreement with two different setups shown in Table 1. Setup 1 utilises a timestep dependent star formation with Jeans instability check and a star formation threshold mass of $10^5 M_{\odot}$. We attempt a total of 22 simulations with this setup and find that $(2.5 \times 10^{-5}, 1, 0.2)$ managed to reproduce the observed $f_s$ and $f_d$. However, the simulated MW galaxy in this feedback prescription does not match the observed KS relation very well. By applying this
feedback prescription to a zoom simulation of a dwarf in this setup, we find star formation starting too late as compared to the simulated MW galaxy. To resolve this issue, we propose switching to a timestep independent star formation setup with no Jeans instability check and threshold mass (Setup 2). However, due to the non-linear coupling of the various processes in the simulation, a new prescription requires re-exploration of subgrid parameters.

We begin an iterative process from \((2.5 \times 10^{-5}, 1.3, 0.2)\) in Setup 2, concluding with two sets of parameters that produced a close fit to the \(f_s\) and \(f_\text{d}\) with the use of 49 simulations. They are \((2.5 \times 10^{-5}, 1.1, 0.9)\) and \((3.0 \times 10^{-5}, 1.1, 0.9)\). As in Setup 1, there are issues with the KS relation of the simulated galaxy. However, these feedback prescriptions performed remarkably well in matching the baryonic makeup of haloes between \(10^{10} \, M_\odot\) and \(10^{12} \, M_\odot\) in the high-resolution region to observations. A perfect feedback prescription that is able to replicate all the observables in the universe does not exist. If the prescription is tuned to certain observables, it might fail to reproduce others, which then requires further iterations to the feedback implementation (e.g. Pillepich et al. (2018)).

The main difference between setups is the conditions for star formation, and this is reflected in the best values of the feedback parameters we find. In Setup 2, with more relaxed star formation criteria, \(f_s\) is high, and \(\epsilon\) is low as compared to Setup 1. In Setup 2, star particles form with ease, of lower mass but have a larger quantity. In order to match the same observed value of \(f_s\) with Setup 1, we use a higher value of \(f_\text{s}\), creating star particles with higher mass. However, since we demand a good agreement with the observed \(f_\text{d}\), we have to lower the feedback energy efficiency from these higher mass star particles. This adjustment results in a lower \(\epsilon\) as compared to Setup 1. Therefore, combining the values of feedback parameters with the star formation criteria, we show the complementary characteristics of different aspects of the feedback processes.

In Setup 2, the points coalesce around low gas surface density, with more gas being converted to stars due to the higher value of \(f_\text{s}\) and the relaxed star formation criteria. As a result, in the recovery of the KS relation in both simulation setups, Setup 2 did not perform as well as Setup 1. This inability to obtain an appropriate slope of the KS relation in both setups hints at a fundamental limitation of the Cen & Ostriker (1992) model. In terms of matching other observed properties, this feedback prescription requires more tuning or parameters.

Looking at the other haloes in the high-resolution region in Setup 2, all but three of the haloes within \(10^{10} \, M_\odot\) and \(10^{12} \, M_\odot\) with the calibrated star formation and feedback prescription are an excellent fit to \(f_s\) and \(f_\text{d}\) observed by McGaugh et al. (2010). In comparison to the results from Setup 1, the feedback prescriptions in Setup 2 is better suited for zoom simulations of less massive haloes. We verify this claim with the zoom simulations of a dwarf galaxy of \(10^{10} \, M_\odot\) with these feedback prescriptions. Through the haloes in the high-resolution region of the MW zoom simulation and the halo in the dwarf galaxy zoom simulation, we demonstrate the insensitivity of our feedback prescription on the mass resolution. However, we have to conduct the same test with much lower mass haloes as well as with different spatial resolutions. On top of the resolution, the universality and robustness of the feedback prescription should also be extended to galaxies with various star formation and merger history.

As we demonstrate, non-deterministic variance in the calculated predictions is a cause for concern; more computational resources need to be invested in order to understand, quantify and minimise these effects. Nevertheless, the Cen & Ostriker model failed to reproduce completely all of the empirical constraints investigated, which strongly indicates that the model needs further improvement in order to achieve a better match to observations.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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