$t \to bW h^0$ and $t \to bW A^0$ decays and possible CP violating effects.

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Abstract

We study the charged $t \to bW h^0$ and $t \to bW A^0$ decays in the framework of the general two Higgs doublet model, so called model III and beyond. Here, we take the Yukawa couplings complex and introduce a new complex parameter due to the physics beyond the model III, to switch on the CP violating effects. We predict the branching ratios as $BR(t \to bW h^0) \sim 10^{-6}$ and $BR(t \to bW A^0) \sim 10^{-8}$. Furthermore, we observe a measurable CP asymmetry, at the order of $10^{-2}$, for both decays.

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1 Introduction

Because of its large mass, the top quark has rich decay products and this opens a new window to test the standard model (SM) and to get some clues about the new physics, beyond. In the literature there are various studies in the SM and beyond [1]-[13]. The rare flavor changing transitions $t \rightarrow c g (\gamma, Z)$ have been studied in [4, 6], $t \rightarrow c H^0$ in [2, 6, 7, 8, 9] and $t \rightarrow c l_1 l_2$ in [10]. The SM predictions of the branching ratio ($BR$) of the process $t \rightarrow c g (\gamma, Z)$ is $4 \times 10^{-11} (5 \times 10^{-13}, 1.3 \times 10^{-13})$ [2], and $t \rightarrow c H^0$ is at the order of the magnitude of $10^{-14} - 10^{-13}$, in the SM [6], which are not measurable quantities even at the highest luminosity accelerators. Possible new physics effects are the candidates for the enhancement of the $BR$'s of the above processes. $t \rightarrow c H^0$ and $t \rightarrow c l_1 l_2$ decays have been analysed in [8] and [10], in the framework of the general two Higgs doublet model (model III). In these studies it has been observed that there could be a strong enhancement in the $BR$, almost seven orders larger compared to the one in the SM for the decay $t \rightarrow c H^0$; a measurable $BR$, at the order of the magnitude of $10^{-8} - 10^{-7}$ for the decay $t \rightarrow c l_1 l_2$. In [11] $t \rightarrow c V V$ decay has been analysed in the topcolor assisted technicolor theory.

The charged $t \rightarrow b$ transitions exist in the SM model and have been studied in the literature extensively. The top decay $t \rightarrow b W$ has been analysed (see [12] and references therein) in the two Higgs doublet model and $t \rightarrow b W Z$ decay has been studied in [13].

The present work is devoted to the analysis of the charged $t \rightarrow b W h^0$ and $t \rightarrow b W A^0$ decays in the framework of the general two Higgs doublet model (model III). This decay occurs in the tree level with the extended Higgs sector since the scalar bosons $h^0$ and $A^0$ exist in the new sector. We study the $BR$ of the above decays and obtain a measurable quantities, at the order of the magnitude of $10^{-6}$ and $10^{-8}$, respectively. Furthermore, we search the possible CP violating effects. To obtain a nonzero CP asymmetry $A_{CP}$ we take Yukawa coupling for $b h^0 (A^0) b$ transition complex and introduce a new complex parameter, where its complexity comes from some type of radiative corrections, due to the model beyond the model III (see section II). We obtain a measurable $A_{CP}$, at the order of the magnitude of $10^{-2}$ and observe that these physical quantities can give valuable information about physics beyond the SM, the free parameters existing in these models.

The paper is organized as follows: In Section 2, we present the $BR$ and $A_{CP}$ of the decay $t \rightarrow b W h^0 (A^0)$ in the framework of model III. Section 3 is devoted to discussion and our conclusions.
2 \quad t \to bW h^0 \text{ and } t \to bW A^0 \text{ decays with possible CP violating effects.}

If one respects the current mass values of $h^0(A^0)$, namely $m_{h^0} \sim 85 \text{GeV}$ ($m_{A^0} \sim 90 \text{GeV}$), the charged $t \to bW h^0(A^0)$ is kinematically possible and does not exist in the SM model. With the minimal extension of the Higgs sector the CP odd new Higgs scalar $A^0$ arises and the $t \to bW A^0$ decay in the tree level is permitted. In this model, $t \to bW h^0$ decay is possible in the tree level, where $h^0$ is the new CP even Higgs scalar and, in general, it mixes with the SM one, $H^0$. In this section, we study the $BR$ in the general two Higgs doublet model, so called model III and the possible CP violating asymmetry, beyond.

The $t \to bW h^0(A^0)$ decay is created by the charged $t \to bW$ process and the neutral $t \to t^* h^0(A^0)$ or $b^* \to bh^0(A^0)$ processes, which are controlled by the Yukawa interaction

$$\mathcal{L}_Y = \eta_i^U \tilde{Q}_{iL} \tilde{\phi}_1 U_{jR} + \eta_i^D \tilde{Q}_{iL} \phi_1 D_{jR} + \xi_{ij}^U \tilde{Q}_{iL} \tilde{\phi}_2 U_{jR} + \xi_{ij}^D \tilde{Q}_{iL} \phi_2 D_{jR} + h.c.$$

where $L$ and $R$ denote chiral projections $L(R) = 1/2(1 \mp \gamma_5)$, $\phi_i$ for $i = 1, 2$, are the two scalar doublets, $\tilde{Q}_{iL}$ are left handed quark doublets, $U_{jR}(D_{jR})$ are right handed up (down) quark singlets, with family indices $i, j$. The Yukawa matrices $\eta_{ij}^{U,D}$ and $\xi_{ij}^{U,D}$ have in general complex entries. By considering the gauge and CP invariant Higgs potential which spontaneously breaks $SU(2) \times U(1)$ down to $U(1)$ as

$$V(\phi_1, \phi_2) = c_1(\phi_1^+ \phi_1 - v^2/2)^2 + c_2(\phi_2^+ \phi_2)^2$$

$$+ c_3[(\phi_1^+ \phi_1 - v^2/2) + \phi_2^+ \phi_2]^2 + c_4[(\phi_1^+ \phi_1)(\phi_2^+ \phi_2) - (\phi_1^+ \phi_2)(\phi_2^+ \phi_1)]$$

$$+ c_5[Re(\phi_1^+ \phi_2)]^2 + c_6[Im(\phi_1^+ \phi_2)]^2 + c_7 .$$

and choosing the parametrization for $\phi_1$ and $\phi_2$ as

$$\phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H^0 \end{pmatrix} + \begin{pmatrix} \sqrt{2} \chi^+ \\ i\chi^0 \end{pmatrix} ;$$

$$\phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}H^+ \\ H_1 + iH_2 \end{pmatrix} .$$

with the vacuum expectation values,

$$< \phi_1 > = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} ; < \phi_2 > = 0 ,$$

the $H_1$ and $H_2$ becomes the mass eigenstates $h^0$ and $A^0$ respectively since no mixing occurs between two CP-even neutral bosons $H^0$ and $h^0$, in tree level. This scenerio permits one to collect SM particles in the first doublet and new particles in the second one. Furthermore the Flavor Changing (FC) interaction can be obtained as

$$\mathcal{L}_{Y,FC} = \xi_{ij}^U \tilde{Q}_{iL} \tilde{\phi}_2 U_{jR} + \xi_{ij}^D \tilde{Q}_{iL} \phi_2 D_{jR} + h.c.$$
with the couplings $\xi^{U,D}$ for the FC charged interactions

$$\xi_{ch}^U = \xi_N^{U} V_{CKM},$$
$$\xi_{ch}^D = V_{CKM} \xi_N^{D},$$

(6)

where $\xi_N^{U,D}$ is defined by the expression

$$\xi_N^{U(D)} = (V_{R(L)}^{U(D)})^{-1} \xi_{N,tt} U^{U(D)} V_{L(R)}^{U(D)}.$$  

(7)

Notice that the index ”N” in $\xi_N^{U,D}$ denotes the word ”neutral”.

Using the relevant diagrams for the $t \to bW h^0 (A^0)$ decay which are given in Fig[1] and taking into account only the real Yukawa couplings $\xi_{N,bb}^{D}, \xi_{N,tt}^{U},$ the matrix element square $|M|^2(h^0)$ ($|M|^2(A^0)$) reads

$$|M|^2_{h^0(A^0)}(p_1, p_b, k, q) = \xi_{N,bb}^{D} \xi_{N,tt}^{U} f_1(h^0 (A^0)) + (\xi_{N,bb}^{D})^2 f_2(h^0 (A^0)) + (\xi_{N,tt}^{U})^2 f_3(h^0 (A^0))$$

(8)

where

$$f_1(h^0) = 16 |V_{tb}|^2 m_b m_t \left( m_W^2 (s_2^2(h^0) - s_1^2(h^0)) + 2 s_1(h^0) s_2(h^0) \right) x_{h^0}$$
$$+ 2 s_1(h^0) \left( (s_1(h^0) - s_2(h^0)) k.(p_1 - p_b) + 2 s_1(h^0) p_1.p_b \right)$$
$$+ \frac{1}{m_W^2} \left( - (s_2^2(h^0) + 2 s_1^2(h^0)) + 2 s_1(h^0) s_2(h^0)) \right) k.q)^2 + 2 s_1(h^0) \right) \right)$$
$$+ s_2(h^0)) k.q.q.(p_1 - p_b) + 8 s_1^2(h^0) p_1.q.p_b.q$, 

$$f_2(h^0) = 8 |V_{tb}|^2 \left( - m_W^2 (s_2(h^0) + s_1(h^0))^2 x_{h^0} p_1.p_b$$
$$+ \frac{1}{m_W^2} k.q \left( (s_2(h^0) + 2 s_1(h^0))$$
$$\times (s_2(h^0)) k.q.p_1.p_b + 2 s_1(h^0) k.p_b q.p_1) - 2 s_1(h^0) s_2(h^0)) k.p_1.p_b.q$$
$$+ 2 s_1^2(h^0) (k.p_1 k.p_b - x_{h^0} q.p_1 q.p_b)$$

$$f_3(h^0) = 8 |V_{tb}|^2 \left( - m_W^2 (4 s_1(h^0) (s_1(h^0) - s_2(h^0))) x_t k.p_b + (s_1(h^0) + s_2(h^0))^2 x_{h^0}$$
$$- 4 s_1^2(h^0) x_t p_1.p_b$$
$$+ \frac{1}{m_W^2} k.q \left( (s_2(h^0) s_2(h^0) + 2 s_1(h^0)) k.q.p_1.p_b - 2 s_1(h^0) s_2(h^0) q.p_1 k.p_b + 2 s_1(h^0)$$
$$\times (2 s_1(h^0) + s_2(h^0)) k.p_1 q.p_b$$
$$+ 2 s_1(h^0) (s_1(h^0) k.p_1 k.p_b - (2 (s_1(h^0) + s_2(h^0)) x_t k.q + s_1(h^0) (x_{h^0}^2 - 4 x_t) q.p_1) q.p_b) \right).$$
\[ f_1(A^0) = 16 |V_{tb}|^2 m_s m_t \left( m_W^2 \left( s_2^2(A^0) + s_1^2(A^0) \right) x_{A^0} + \frac{1}{m_W^2} \left( 2 s_1^2(A^0) - s_2^2(A^0) \right) (k.q)^2 \right), \]
\[ f_2(A^0) = 8 |V_{tb}|^2 \left( - m_W^2 \left( s_2(A^0) + s_1(A^0) \right) \right)^2 x_{A^0} p_1 p_b \]
\[ + \frac{1}{m_W^2} k.q \left( (s_2(A^0) + 2 s_1(A^0)) s_2(A^0) k.q p_1.p_b + 2 s_1(A^0) k.p_b p_1.q \right) \]
\[ - 2 s_1(A^0) s_2(A^0) k.p_b p_1.q + 2 s_1^2(A^0) (k.p_1 k.p_b - x_{A^0} q.p_1 q.p_b) \],
\[ f_3(A^0) = 8 |V_{tb}|^2 \left( - m_W^2 \left( s_1(h^0) - s_2(h^0) \right) \right)^2 x_{A^0} p_1 p_b \]
\[ + \frac{1}{m_W^2} k.q \left( s_2(A^0) s_2(h^0) - 2 s_1(h^0) s_2(h^0) \right) k.q p_1.p_b + 2 s_1(A^0) \left( 2 s_1(A^0) - s_2(A^0) \right) k.p_1.p_b.q \]
\[ + 2 s_1(A^0) s_2(A^0) k.p_b p_1.q + 2 s_1^2(A^0) \left( k.p_1 k.p_b - x_{A^0} q.p_1 q.p_b \right) \]. \tag{9}\]

Here the functions \( s_{1(2,3)}(h^0(A^0)) \) are
\[ s_1(h^0) = - \frac{g_W}{4 m_W^2 (1 + x_t - 2 \frac{p_1.q}{m_W^2})}, \]
\[ s_2(h^0) = \frac{g_W}{2 m_W^2 (1 + x_{h^0} - y_t - 2 \frac{k.q}{m_W^2})}, \]
\[ s_{1(2)}(A^0) = (-) s_{1(2)}(h^0 \rightarrow A^0), \tag{10}\]

with weak coupling constant \( g_W \), \( x_{h^0(A^0)} = \frac{m_{h^0(A^0)}^2}{m_W^2} \), \( x_t = \frac{m_t^2}{m_W^2} \) and \( y_t = \frac{m_{H^\pm}^2}{m_W^2} \) and \( p_1, p_b, q \) and \( k \)
are four momentum of \( t \) quark, \( b \) quark, \( W \) boson and Higgs scalar \( h^0(A^0) \), respectively.

Finally, using the well known expression defined in the \( t \) quark rest frame
\[ d\Gamma_{h^0(A^0)} = \frac{(2\pi)^4}{12 m_t} \delta^{(4)}(p_1 - p_b - k - q) \frac{d^3p_b}{(2\pi)^3 2 E_b} \frac{d^3q}{(2\pi)^3 2 E_W} \frac{d^3k}{(2\pi)^3 2 E_{h^0(A^0)}} \]
\[ \times |M_{h^0(A^0)}|^2(p_1, p_b, k, q) \tag{11}\]

and the total decay width \( \Gamma_T \sim \Gamma(t \rightarrow bW) \) as \( \Gamma_T = 1.55 \text{GeV} \), we get the \( BR \) for the decay \( t \rightarrow bW h^0(A^0) \).

Now, we would like to study a possible CP violating effects, which can give comprehensive
information about the free parameters of the model used. For the process under consideration,
the CP violation can be obtained by choosing the complex Yukawa couplings in general, namely,
taking the parametrizations
\[ \xi_{N,tt}^U = |\xi_{N,tt}^U| e^{i\theta_{tt}}, \]
\[ \xi_{N,bb}^D = |\xi_{N,bb}^D| e^{i\theta_{bb}}. \tag{12}\]
However, this choice is not enough to get non-zero $A_{CP}$

$$A_{CP} = \frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}}$$ 

(13)

where $\bar{\Gamma}$ is the decay width for the CP conjugate process. This forces one to go beyond the model III and try to obtain a new complex quantity so that its complexity does not come from the Yukawa couplings but from some radiative corrections. Under the light of this discussion, we introduce an additional complex correction $\chi$ to $b \to b$ transition, which may come from the new model beyond the model III as

$$\left( \xi_{N,bb}^D + \xi_{N,bb}^{D^*} \right) + \left( \xi_{N,bb}^D - \xi_{N,bb}^{D^*} \right) \gamma_5 + \chi$$

and

$$\left( \xi_{N,bb}^{D^*} - \xi_{N,bb}^D \right) - \left( \xi_{N,bb}^D + \xi_{N,bb}^{D^*} \right) \gamma_5 + \chi \gamma_5$$

Here we take the magnitude of $\chi$ at most $|\chi| \sim 10^{-2}$, which is more than one order smaller compared to the vertex due to model III. In this case, we take the correction to the $t \to t$ transition small since the strength of $t \to t$ transition is weaker compared to strength of the $b \to b$ transition, with respect to our choice (see Discussion section).

At this stage, we introduce a model beyond the model III as follows: The multi Higgs doublet model which contains more than two Higgs doublets in the Higgs sector can be one of the candidate. The choice of three Higgs doublets brings new Yukawa couplings which are responsible with the interactions between new Higgs particles and the fermions. The Yukawa lagrangian in three Higgs doublet model (3HDM) reads

$$L_Y = \eta_{ij}^U \bar{Q}_{iL} \tilde{\phi}_1 U_{jR} + \eta_{ij}^D \bar{Q}_{iL} \phi_1 D_{jR} + \xi_{ij}^{U+} \bar{Q}_{iL} \tilde{\phi}_2 U_{jR} + \xi_{ij}^D \bar{Q}_{iL} \phi_2 D_{jR} + \rho_{ij}^U \bar{Q}_{iL} \tilde{\phi}_3 U_{jR} + h.c.$$ 

(14)

where $\rho_{ij}^{U(D)}$ is the new coupling and $\phi_3$ can be chosen as

$$\phi_3 = \frac{1}{\sqrt{2}} \left( \begin{array}{c} \sqrt{2} F^+ \\ H_3 + i H_4 \end{array} \right)$$

(15)

with vanishing vacuum expectation value. The fields $F^+$ and $H_3$ ($H_4$) represent the new charged and CP even (odd) Higgs particles, respectively. Notice that the other Yukawa couplings and Higgs particles in eq. (14) are the ones existing in the model III. Now, we choose the additional Yukawa couplings $\rho_{ij}^{U(D)}$ real and take into account the radiative corrections to the $b \to b$ transition which comes from the contributions of third Higgs doublet for the decay under consideration. Here the complexity of the parameter should come from the radiative
corrections but not from the new Yukawa couplings. We can take this complex contribution as a source for the additional part $\chi$. Since the number of free parameters, namely masses of new Higgs particles $m_{F \pm}$, $m_{H_3}$, $m_{H_4}$ and the new Yukawa couplings $\rho^{U(D)}_{ij}$, increases, there arises a difficulty to restrict them. However, the overall uncertainty coming from these free parameters lies in the contribution $\chi$ and it can be overcome by the possible future measurement of the CP violation for our process.

Finally, by using the definition

$$A^{h_0(A^0)}_{CP}(E_W, E_b) = \frac{d^2\Gamma(t\rightarrow bW h^0(A^0))}{dE_b dE_W} \frac{d^2\Gamma(t\rightarrow \bar{b}W h^0(A^0))}{dE_b dE_W}$$

(16)

we obtain the differential $A_{CP}(E_W, E_b)$ for the process $t \rightarrow bW h^0(A^0)$ as

$$A^{h_0(A^0)}_{CP}(E_W, E_b) = |\bar{\tilde{\rho}}_{N,bb}^{N}| |\chi| \sin\theta_{bb} \sin\theta_{\chi} \frac{\Phi^{h_0(A^0)}}{D^{h_0(A^0)}},$$

(17)

where

$$\Phi^{h_0} = 4 m_t s_1(h^0) |V_{tb}|^2 \left( 4 \left( 2 E_W^2 m_t s_1(h^0) (x_t - 2) - E_b^2 (2 E_W + m_t) s_2(h^0) (1 + x_t) \right) + E_b E_W \left( E_W (s_2(h^0) (1 + 3 x_{h^0} - 3 x_t) + 4 s_1(h^0) (1 + 2 x_{h^0})) + m_t (s_2(h^0) + 2 s_1(h^0) (2 x_{h^0} + x_t)) \right) + m_W^2 \left( m_t (s_2(h^0) (-1 + (x_{h^0} - x_t)^2) + 4 s_1(h^0) (1 + x_t + x_{h^0}) + 2 E_b (-2 s_1(h^0) (1 + 2 x_{h^0} + x_t) + s_2(h^0) (-1 + x_{h^0} - x_t) (2 x_t - 1)) \right) - 2 E_W (s_2(h^0) (x_{h^0} - x_t) (1 - x_t + x_{h^0}) + s_1(h^0) (4 + 2 x_{h^0} (2 + 2 x_{h^0} - x_t) + 2 x_t (3 - x_t))) \right) + \frac{8}{m_W^2} \left( E_b E_W^2 (E_b (2 E_W + m_t) s_2(h^0) - 4 E_W m_t s_1(h^0)) \right),$$

$$\Phi^{A^0} = 4 m_t s_1(A^0) |V_{tb}|^2 \left( 4 \left( 2 E_W^2 m_t s_1(A^0) (x_t - 2) - E_b^2 (2 E_W + m_t) s_2(A^0) (1 + x_t) \right) + E_b E_W \left( E_W (s_2(A^0) (1 + 3 x_{A^0} - 3 x_t) + 4 s_1(A^0) (1 + 2 x_{A^0})) + m_t (s_2(A^0) + 2 s_1(A^0) (2 x_{A^0} + x_t)) \right) + m_W^2 \left( - m_t (s_2(A^0) (-1 + (x_{A^0} - x_t)^2) + 4 s_1(A^0) (1 + x_t + x_{A^0}) + 2 E_b (2 s_1(A^0) (1 + 2 x_{A^0} + x_t) + s_2(A^0) (-1 + x_t + 2 x_{A^0} (1 - 2 x_t)) + 2 E_W (s_2(A^0) (x_{A^0} - x_t) (1 - x_t + x_{A^0}) + s_1(A^0) (4 + 4 x_{A^0} (1 + x_{A^0} - 2 x_t) + 2 x_t (3 - x_t))) \right) + \frac{8}{m_W^2} \left( E_b E_W^2 (E_b (2 E_W + m_t) s_2(A^0) - 4 E_W m_t s_1(A^0)) \right) \right),$$

(18)
with \( \chi = e^{i \theta} |\chi| \), \( \xi_{N,bb}^D = e^{i \theta_{bb}} |\xi_{N,bb}^D| \). Notice that we do not present the functions \( D(h^0) \) and \( D(A^0) \) since their explicit expressions are long. Here the functions \( s_1(h^0(A^0)) \) and \( s_2(h^0(A^0)) \) are given in eq. (10).

3 Discussion

This section is devoted to the analysis of the \( BR \) and \( A_{CP} \) of the decay \( t \to bW h^0 \) and \( t \to bW A^0 \) in the framework of model III and beyond. In our numerical analysis we use the form of the coupling \( \xi_{N,ij}^{U(D)} \), which is defined as \( \xi_{N,ij}^{U(D)} = \sqrt{\frac{4G_F}{\sqrt{2}}} \xi_{N,ij}^{U(D)} \).

Since the model III contains large number of free parameters such as Yukawa couplings, \( \xi_{N,ij}^{U(D)} \), the masses of new Higgs bosons, \( H^\pm, h^0 \) and \( A^0 \), we try to restrict them by using experimental measurements. In our calculations, we neglect all the Yukawa couplings except \( \xi_{N,tt} \) and \( \xi_{N,bb}^D \), due to their their light flavor contents. In addition to this we neglect the off diagonal coupling \( \xi_{N,tc}^{U(D)} \), since it is smaller compared to \( \xi_{N,tt} \) (see [14]). One of the most important experimental measurement for the prediction of the constraint region for the couplings \( \xi_{N,tt} \) and \( \xi_{N,bb}^D \) is the the CLEO measurement [13]

\[
BR(B \to X_s \gamma) = (3.15 \pm 0.35 \pm 0.32) \times 10^{-4}.
\] (19)

and our procedure is to restrict the Wilson coefficient \( C_t^{eff} \) which is the effective coefficient of the operator \( O_7 = \frac{e}{16\pi^2} \bar{s}_o \sigma_{\mu\nu} (m_b R + m_s L) b_\alpha F^{\mu\nu} \) (see [14] and references therein), in the region \( 0.257 \leq |C_t^{eff}| \leq 0.439 \), where the upper and lower limits were calculated using eq. (19) and all possible uncertainties in the calculation of \( C_t^{eff} \). In the case of the calculation of \( A_{CP} \), \( \xi_{N,bb}^D (\xi_{N,tt}^U) \) is taken complex (real) and a new small complex parameter \( \chi \), due to the physics beyond model III, is introduced. In the following, we choose \( |r_{tb}| = \frac{\xi_{N,bb}^D}{\xi_{N,bb}^D} |< 1 \). Notice that, in figures, the \( BR \) and \( A_{CP} \) are restricted in the region between solid (dashed) lines for \( C_t^{eff} > 0 \) \((C_t^{eff} < 0) \). Here, there are two possible solutions for \( C_t^{eff} \) due to the cases where \( |r_{tb}| < 1 \) and \( r_{tb} > 1 \). In the case of complex Yukawa couplings, only the solutions obeying \( |r_{tb}| < 1 \) exist.

In Fig. 3, we plot the \( BR(t \to bW h^0) \) with respect to \( \frac{\xi_{N,bb}^D}{m_b} \) for \( m_{H^\pm} = 400 GeV, m_{h^0} = 85 GeV \). As shown in this figure, the \( BR \) is at the order of the magnitude of \( 10^{-6} \) and it increases with the increasing values of the \( \frac{\xi_{N,bb}^D}{m_b} \). Its magnitude (the restriction region) is larger (broader) for \( C_t^{eff} > 0 \) compared to the one for \( C_t^{eff} < 0 \).

Fig. 3 is devoted to the same dependence of the \( BR(t \to bW A^0) \) for \( m_{H^\pm} = 400 GeV, m_{A^0} = 90 GeV \). For this process the \( BR \) is at the order of the magnitude of \( 10^{-8} \), almost 2 order smaller compared to the \( BR(t \to bW h^0) \). It increases with the increasing values of the
\[ \frac{\xi_{N,bb}}{m_b} \] and its magnitude (the restriction region) is larger (broader) for \( C_7^{eff} > 0 \) compared to the one for \( C_7^{eff} < 0 \). Furthermore, the restriction region is sensitive to the parameter \( \frac{\xi_{N,bb}}{m_b} \) and for \( C_7^{eff} < 0 \), upper and lower bounds almost coincide.

Fig. 4 (5) represents \( BR(t \to bWH^0(A^0)) \) with respect to \( m_{h^0}(m_{A^0}) \) for \( m_{H^\pm} = 400 \text{GeV} \) and \( \xi_{N,bb} = 30 \text{mb} \). Here the \( BR \) increases with the decreasing values of \( m_{h^0}(m_{A^0}) \). This can give a powerful information about the lower limit of the mass value \( m_{h^0}(m_{A^0}) \) with the help of the possible future experimental measurement of the process under consideration. Notice that with the increasing values of \( m_{h^0}(m_{A^0}) \) the restriction regions for \( C_7^{eff} > 0 \) and \( C_7^{eff} < 0 \) become narrower and coincide.

Now, we would like to analyse the CP asymmetry \( A_{CP} \) of the decay \( t \to bWH^0(A^0) \). To obtain a nonzero \( A_{CP} \) we take the coupling \( \xi_{N,bb} \) complex and introduce a new complex parameter \( \chi \) due to the physics beyond the model III (see section II).

In Fig 6 (7) we present the \( \sin \theta_{bb} \) dependence of \( A_{CP}(t \to bWH^0(A^0)) \) for \( |\xi_{N,bb}| = 30 \text{mb}, |\chi| = 10^{-2}, \) the intermediate value of \( \sin \theta_{\chi} = 0.5 \) and \( m_{h^0} = 85 \text{GeV} (m_{A^0} = 90 \text{GeV}) \). \( A_{CP} \) is at the order of the magnitude of \( 10^{-3} - 10^{-2} \) and slightly larger for \( C_7^{eff} < 0 \) compared to the one for \( C_7^{eff} > 0 \). Fig 8 (9) represents the \( \sin \theta_{\chi} \) dependence of \( A_{CP}(t \to bWH^0(A^0)) \) for \( |\xi_{N,bb}| = 30 \text{mb}, |\chi| = 10^{-2}, \) the intermediate value of \( \sin \theta_{bb} = 0.5 \) and \( m_{h^0} = 85 \text{GeV} (m_{A^0} = 90 \text{GeV}) \). The behavior of \( A_{CP} \) is similar to the one obtained in Fig. 6 (7). As shown in these figures, \( A_{CP} \) is a measurable quantity, which gives strong clues about the possible physics beyond the SM.

Now we will summarize our results:

- The \( BR \) of the process \( t \to bWH^0(A^0) \) is at the order of \( 10^{-6} (10^{-8}) \) in the model III and it can be measured in the future experiments. This ensures a crucial test for the new physics beyond the SM.

- The \( BR \) is sensitive to \( \xi_{N,bb} \) and the mass value \( m_{h^0} (m_{A^0}) \). This is important in the prediction of the lower limit of the mass \( m_{h^0}(m_{A^0}) \) with the possible future experimental measurement of the process under consideration.

- \( A_{CP} \) is at the order of the magnitude of \( 10^{-2} \) for the intermediate values of \( \sin \theta_{bb} \) and \( \sin \theta_{\chi} \). This a measurable quantity, which gives a strong clue about the possible physics beyond the SM and also more beyond.

Therefore, the experimental investigation of the process \( t \to bWH^0(A^0) \) will be effective for understanding the physics beyond the SM.
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Figure 1: The diagrams contribute to the decay $t \to bW^0 h^0(A^0)$. 
Figure 2: $BR(t \to bW h^0)$ as a function of $\frac{\xi_{N.b}}{m_b}$ for $m_{H^\pm} = 400$ GeV, $m_{h^0} = 85$ GeV. Here the $BR$ is restricted in the region bounded by solid lines for $C_7^{eff} > 0$ and by dashed lines for $C_7^{eff} < 0$.

Figure 3: The same as Fig. 2 but for the decay $BR(t \to bWA^0)$. 
Figure 4: $BR(t \to bW h^0)$ as a function of $m_{h^0}$ for $\bar{c}_{N,bb} = 30 m_b$, $m_{H^\pm} = 400$ GeV. Here the $BR$ is restricted in the region bounded by solid lines for $C_7^{\text{eff}} > 0$ and by dashed lines for $C_7^{\text{eff}} < 0$.

Figure 5: The same as Fig. 4 but for the decay $BR(t \to bWA^0)$. 
Figure 6: $A_{CP}(t \rightarrow bWb^0)$ as a function of $\sin\theta_b$ for $|\tilde{\xi}_{S,N,b^0}| = 30 m_b$, $m_{H^\pm} = 400 GeV$, $|\chi| = 10^{-2}$, $\sin\theta_\chi = 0.5$. Here the $A_{CP}$ is restricted in the region bounded by solid lines for $C_{eff}^A > 0$ and by dashed lines for $C_{eff}^A < 0$.

Figure 7: The same as Fig. 6 but for the decay $A_{CP}(t \rightarrow bWA^0)$.  

Figure 8: $A_{CP}(t \to bWh^0)$ as a function of $\sin \theta_\chi$ for $|\xi_{N,bb}| = 30 \text{ m}_b$, $m_{H^\pm} = 400 \text{ GeV}$, $|\chi| = 10^{-2}$, $\sin \theta_{bb} = 0.5$. Here the $A_{CP}$ is restricted in the region bounded by solid lines for $C_{eff}^7 > 0$ and by dashed lines for $C_{eff}^7 < 0$.

Figure 9: The same as Fig. 8 but for the decay $A_{CP}(t \to bWA^0)$. 