Self-compensation in manganese-doped ferromagnetic semiconductors

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We present a theory of interstitial Mn in Mn-doped ferromagnetic semiconductors. Using density-functional theory, we show that under the non-equilibrium conditions of growth, interstitial Mn is easily formed near the surface by a simple low-energy adsorption pathway. In GaAs, isolated interstitial Mn is an electron donor, each compensating two substitutional Mn acceptors. Within an impurity-band model, partial compensation promotes ferromagnetic order below the metal-insulator transition, with the highest Curie temperature occurring for 0.5 holes per substitutional Mn.

Ferromagnetism in dilute magnetic semiconductors is generally believed to be mediated by carriers—electrons or holes—originating from the magnetic dopants themselves. For example, an isolated Mn impurity in GaAs can substitute for Ga and contribute one hole, which is weakly bound to its acceptor core. GaAs samples with Mn dopant concentrations in the range 1–2% are ferromagnetic insulators, while samples in the range 3–6% are ferromagnetic metals. In the metallic phase the nominal hole concentration, \( p \), is in principle equal to the number of Mn atoms per unit volume. Measured hole concentrations are much smaller, by factors ranging from the number of Mn atoms per unit volume. Measured hole concentrations are much smaller, by factors ranging from \( \sim 3 \) for MnGaAs to \( \sim 10 \) or more for MnGe. In most theories of ferromagnetism in dilute magnetic semiconductors, reduced hole concentrations suppress the Curie temperature. The reverse scenario—raising the Curie temperature by increasing the hole concentration—is therefore of great current interest. For current theoretical reviews see Refs. 5, 6.

Recent experiments show a strong correlation between Curie temperature, carrier concentration, and the fraction of Mn found at interstitial sites. In this paper we address several questions not yet settled by experiment. (1) By what mechanism are interstitials formed, given that their calculated formation energies are considerably higher than substitutionals? (2) What determines the relative abundance of interstitials and substitutionals? (3) Under what (doping) conditions do interstitials act as compensators? (4) What role does compensation play in the ferromagnetism?

To answer these questions, we use density-functional theory (DFT) to establish the following: (i) During the MnGaAs growth, Mn adatoms follow a very simple low-energy pathway to directly form interstitial Mn near the surface. (ii) The deposition of additional As converts some of these interstitials to substitutional sites. (iii) The remaining interstitial Mn atoms act as donors, each compensating two substitutional acceptors. Finally, we show that within an impurity-band model, ferromagnetism below the metal-insulator transition is most favorable—in the sense of the highest Curie temperature—for 0.5 holes per substitutional Mn.

For MnGaAs grown by MBE, recent channeling Rutherford backscattering experiments show that as much as \( \sim 15\% \) of the total Mn may be interstitial. An open theoretical question is how interstitial Mn might be formed, under what conditions, and in what concentration. For a system in thermodynamic equilibrium, the concentration of each impurity species is determined by its formation energy. Our calculations (described below) show that the equilibrium concentration of interstitial Mn is negligible. But thermodynamic equilibrium can only be achieved if local metastable configurations can be readily overcome. We find that the energy barriers separating interstitial and substitutional configurations do not satisfy this criterion. Hence, equilibrium thermodynamics is not a reliable guide for studying the formation of interstitial Mn.

To investigate the incorporation of Mn under nonequilibrium conditions, one must identify specific reaction pathways and calculate their energy barriers. At low Mn concentrations, the growth of MnGaAs at low temperatures is governed by the potential-energy surface for individual Mn adatoms adsorbing and diffusing on the GaAs surface. We confine our attention to the GaAs(001) surface, the standard orientation for growing MnGaAs. Under As-rich conditions, the GaAs(001) surface can have several different reconstructions, all of which contain surface As dimers as a common building block. Thus we studied adsorption on a chemically reasonable model surface consisting of five layers of bulk GaAs plus a dimerized As top layer; the bottom layer was passivated. We calculated total energies and forces using pseudopotentials and the generalized-gradient approximation. To identify the lowest energy adsorption site we placed the Mn adatom at various surface sites. We found that the equilibrium concentration of interstitial Mn is negligible. But thermodynamic equilibrium can only be achieved if local metastable configurations can be readily overcome. We find that the energy barriers separating interstitial and substitutional configurations do not satisfy this criterion. Hence, equilibrium thermodynamics is not a reliable guide for studying the formation of interstitial Mn.
FIG. 1: (color) Potential-energy surface for Mn adsorption on GaAs(001), plotted in a plane normal to the surface and containing the As surface dimer. The minimum energy adsorption site is the subsurface interstitial site labeled $i$; the corresponding surface geometry is shown (light gray for As, dark gray for Ga, yellow for Mn). Typical adsorption pathways funnel Mn adatoms to this interstitial site (heavy curves) or to a cave site, $c$ (light curves). Inset: Binding energy of a Mn adatom centered on the As-dimer; for comparison, results are also shown for a Ga adatom. When additional As is deposited, the metastable Mn site, $s$, becomes more favorable and leads to partial incorporation of substitutional Mn.

one of two adsorption channels. The primary channel leads to the As-dimer bridge site. As shown in the inset to Fig. 1, there are two locally stable adsorption positions above the As dimer: a shallow metastable site 2 Å above the surface and a stable site 2 Å below the surface and more favorable by 0.8 eV. These two minima are separated by a small barrier of 0.2 eV, associated with the opening of the As dimer, which is easily overcome at normal growth temperatures. (In comparison, Ga adatoms also have two locally stable adsorption sites, in agreement with Ref. [14]. However, for Ga the interstitial position is very unfavorable, and the stable site near the surface layer ultimately leads to completely substitutional incorporation [14].) Isolated Mn adatoms that are steered into this primary channel will generally reach their equilibrium position below the As dimer. This position corresponds to a bulk interstitial site with four neighboring As atoms. With the Mn atom at this position, the As dimer above it remains intact with a slightly strained bond. A secondary adsorption channel leads, with no energy barrier, to the cave site between adjacent dimer rows; upon continued growth of GaAs this site will also correspond to a bulk interstitial site. Thus we have identified a set of very low energy pathways which initially steer isolated Mn adatoms to interstitial sites.

Although the energetics of Mn on clean GaAs leads to incorporation only at interstitial sites, the subsequent deposition of additional GaAs can change this situation and lead to partial substitutional incorporation. To illustrate this, we computed the change in Mn binding energy resulting from an additional half monolayer of Ga or As on the surface. In the presence of either a Ga or As adlayer, the surface As-dimer bond breaks and the metastable Mn site above it then corresponds to a substitutional site in the zincblende lattice. The adlayer completes the fourfold coordination of this site and hence may change its stability relative to the interstitial site. The change depends on the type of adlayer: for a Ga adlayer, the Mn interstitial site remains 0.8 eV more favorable than the substitutional site, but for an As adlayer this difference is reduced to just 0.1 eV. This reduction reflects the crossover from the case of Mn adatoms on clean GaAs (which favors interstitials) to the thermodynamic limit of isolated Mn in bulk GaAs (which favors substitutionals), and suggests that during the growth Mn will be incorporated at both interstitial and substitutional sites.

The electrical activity of a Mn impurity is determined by its formation energy as a function of its charge state. We used DFT to calculate the formation energies of substitutional and interstitial Mn using supercells containing 54 atoms, with convergence checks using 128 atoms. We fixed the chemical potentials to correspond to the As-rich, Mn-rich conditions normally used in growth. Fig. 2 shows the resulting formation energies, as a function of the Fermi level, for charge states that are stable within the GaAs bandgap. Substitutional Mn is an acceptor, with stable 1− and neutral charge states. The theoretical acceptor ionization energy is 100 meV, in good agreement with the experimental value of 113 meV [1]. Interstitial Mn is a deep donor, with stable 2+, 1+, and neutral charge states; its donor levels have not been measured experimentally. For $p$-type material, corresponding to the Fermi level near the valence band edge, each interstitial will compensate two substitutionals, in agreement with previous calculations [12, 13]. The resulting hole concentration is $p = (x − 2y)(4/\alpha^3)$, where $x$ and $y$ are the number of substitutionals and interstitials per Ga site, and $\alpha$ is the the GaAs lattice constant.

The consequences of partial compensation for ferromagnetism are different above and below the metal-insulator transition. In the metallic phase the Mn-induced impurity states broaden and merge with the GaAs valence band. Most current theories therefore consider the carriers as free holes in the valence band. In this picture the Curie temperature is proportional to $p^{1/3}$, and hence compensation can only reduce the Curie temperature. But the role of compensation is less obvious for Mn concentrations between 1 and 2%, where ferromagnetism persists experimentally even though transport data clearly show the samples to be insulating [1]. The nature of this insulating state is not currently understood. If the Coulomb $U$ is larger than the impurity band width, then this state is a Mott-Hubbard insulator and an impurity-band model with localized carriers is an appropriate starting point [14]. Below we show that within such a model, the compensation affects the magnetic interactions in a surprising way: the maximum Curie temperature is obtained not for zero compensation,
but rather for a partially compensated system with 0.5 holes per substitutional Mn.

We derive this result starting from a Zener double-exchange Hamiltonian for the motion of holes in a narrow impurity band \[13\]:

\[
H_{DE} = \sum_i \epsilon_i a_i^\dagger a_i + \sum_{i,j} t_{ij} a_i^\dagger a_j - J_H \sum_i \vec{S}_i \cdot \vec{S}_i. \tag{1}
\]

The first term describes fluctuations in the on-site impurity levels caused by the random distribution of charged (\(A^-\)) and neutral (\(A^0\)) Mn acceptors; the second term describes the hopping of holes between Mn spins; and the last term describes the exchange coupling between holes and Mn spins. The energies \(\epsilon_i\) are distributed within the disorder-broadened band width, \(W\); and \(a_i^\dagger\) and \(a_i\) are creation and annihilation operators for holes with spin \(\sigma\) at site \(i\); \(t_{ij}\) are hopping integrals; \(J_H\) is the exchange coupling constant; \(\vec{S}_i\) and \(\vec{S}_i\) are the operators for the hole and Mn (\(S = 5/2\)) spins, respectively.

It is well established that the coupling between the hole and the Mn spin is antiferromagnetic, \(J_H < 0\), and that \(S|J_H|\) is in the range 100–250 meV \[14\]. This is comparable to, or even larger than, the acceptor ionization energy. Hence the hole at site \(i\) is always antiparallel to the Mn spin, and the Hamiltonian can be reduced to a spinless form with the hopping renormalized to \(t_{ij} \cos(\theta_{ij}/2)\), where \(\theta_{ij}\) is the angle between \(\vec{S}_i\) and \(\vec{S}_j\).

To second order in the hopping, \(H_{DE}\) can be mapped to an effective Heisenberg Hamiltonian describing the interaction between Mn spins,

\[
H_{\text{eff}} = \frac{1}{2} \sum_{ij} \frac{|t_{ij}|^2}{\epsilon_i - \epsilon_j} (n_i - n_j) \left(1 + \frac{\vec{S}_i \cdot \vec{S}_j}{S(S+1)}\right), \tag{2}
\]

where \(n_i\) is the number of holes at site \(i\) (thus, \(n_i = 0\) and \(1\) correspond to \(A^-\) and \(A^0\) acceptors, respectively). Two features of \(H_{\text{eff}}\) are noteworthy. First, the effective coupling between spins falls off exponentially with their separation, \(r_{ij}\), because the hopping integrals have the form \(t_{ij} = t_0(r_{ij}) \exp(-r_{ij}/a_0)\), where \(t_0(r) \propto r/a_0\) for hydrogenic wavefunctions and \(a_0\) is the effective Bohr radius of the Mn acceptor \[17\]. Second, because of the factor \((n_i - n_j)\), interactions occur only between Mn acceptors in different charge states, that is, between \(A^0\) and \(A^-\). This implies that ferromagnetism is absent in the limiting cases of no compensation and complete compensation.

This result can be easily understood within a simple toy model. Consider the Hamiltonian \(H_{DE}\) applied to two Mn acceptors that share either zero, one, or two holes. In the case of zero holes (both \(A^-\) acceptors), there is no interaction at all. For one hole (\(A^0\) and \(A^-\)), the interaction is ferromagnetic, because the hole can lower its kinetic energy via hopping only for aligned spins. For two holes (both \(A^0\)), the interaction is always antiferromagnetic and scales as \(t_{ij}^2/J_H\). In the real system, aligning the spins in the absence of compensation drives the Fermi level into the gap between spin-up and spin-down states, making ferromagnetism unfavorable.

To find the Curie temperature of the ferromagnetic phase transition, we first note that mean-field theory is not well justified because of the exponential dependence of the integrals \(t_{ij}\) and because of the Mn positional disorder \[18\]. Instead we represent the system as a percolation network of randomly distributed sites, each occupied by either \(A^0\) or \(A^-\), with interactions only between sites with different charges. In the standard solution to this two-color percolation problem \[20\], the critical percolation radius, \(R_c\), depends on the solution of the one-color problem and on the maximum eigenvalue of the connectivity matrix for the two-color problem. In our case this leads to

\[
R_c = a \left( \frac{B_c}{(16\pi/3)x \sqrt{q(1-q)}} \right)^{1/3}, \tag{3}
\]

where \(B_c = 2.7\) is the average number of bonds within the critical radius for the one-color problem \[20\], and \(q\) is the number of holes per substitutional Mn. In general, \(q\) must be found from the electroneutrality condition and the energy levels in Fig. 2, but at reasonable temperatures the approximation \(q = 1 - 2y/x\) is extremely accurate for \(y < x/2\). Note that due to the factor \(\sqrt{q(1-q)}\), the critical radius diverges for both \(y = 0\) and \(y = x/2\), consistent with our earlier conclusion that ferromagnetism vanishes at these limits.

The Curie temperature is given within percolation theory by

\[
k_B T_c = \frac{1}{6} B_c \left( \frac{n_i - n_j}{\epsilon_i - \epsilon_j} \right) t_0(R_c)^2 \exp(-2R_c/a_0), \tag{4}
\]
The dielectric constant of GaAs [14]. This gives the Curie level to be the Coulomb gap [17, 21], given by $|\epsilon_M|$, corresponding to an interstitial fraction of two holes in different orbital states $\epsilon_i - \epsilon_j \approx e^2/\kappa r_{ij}$, where $e$ is the electron charge and $\kappa = 10.66$ is the dielectric constant of GaAs [4]. This gives the Curie temperature simply as

$$k_B T_C = \frac{B_e e^2}{108 \kappa a_0} \left( \frac{2 R_c}{a_0} \right)^3 \exp(-2 R_c/a_0).$$

We show in Fig. 3(a) the dependence of the Curie temperature on the number of holes per substitutional Mn and, equivalently for the case of pure self-compensation, on the fraction of interstitial Mn. The maximum Curie temperature is reached for $q = 0.5$ holes per substitutional Mn, corresponding to an interstitial fraction $y = x/4$.

The above theory ignores the orbital degeneracy of the impurity band. This simplification is justified if the Coulomb energy, $U$, of two holes in different orbital states is larger than both the hopping integral and the impurity band width, $W$. For the case when $U$ is smaller than $W$, the resulting overlap of the two Hubbard bands will lead to a finite density of states at the Fermi level, even without compensation. For Mn concentrations between 1 and 2% the materials are nonetheless insulating, suggesting that the states are localized by an Anderson transition induced by strong disorder. In this case, hopping—and thereby also ferromagnetic coupling—can take place not only between $A^0$ and $A^+$ but also between $A^0$ and $A^+$ acceptors. The percolation radius is still given by Eq. [3] but $q$ now must be replaced by the fraction of neutral acceptors, which must be calculated from the density of states. For a simple triangular density of states, the resulting Curie temperature is shown in Fig. 3(b). One significant new feature arises: ferromagnetism now persists even without compensation. Otherwise, the main features of the Mott-Hubbard case are obtained here as well, and the maximum Curie temperature is again reached for $q = 0.5$.

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