Influence of Iron Core on Critical Current and Inductance of an HTS Double Pancake Coil

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Abstract. In a high temperature superconducting (HTS) DC induction heater, an HTS coil and an iron core are essential to generate DC magnetic field and form the magnetic circuit. To understand effect of the iron core on the critical current and the inductance of the HTS coil, we prepared a double pancake coil (DPC) and an iron core in this study, and measured the critical current and inductance of the DPC. The experimental results were compared with the numerically calculated ones as well. The measured critical currents of the DPC without and with the iron core are 89 A and 84 A, respectively. Thus, the iron core does affect the critical current. Moreover, the measured inductances are 6.94 mH and 45 mH. The measured data of the critical currents and the inductances are in good agreement with the calculated results.

Keywords: Comsol; HTS coil; Inductance; Iₜₐₘ; Magnetic field.

1 Introduction

To ameliorate the poor efficiency of a traditional induction heater, a novel high temperature superconducting (HTS) DC induction heater has been suggested and being studied for commercial application [1]-[2]. A commercial industry-scale HTS DC induction heater with capacity of 1MW has been planned to be built in Shanghai Superconductor technology Co., Ltd. and Shanghai Jiao Tong University, China from 2014. For the HTS DC induction heater, an HTS coil is applied to generate DC magnetic field, and an iron core is necessary to form the magnetic circuit. Accordingly the critical current (Iₜₐₘ) and the inductance of the HTS coil will be changed because of the iron core, which are the most important parameters of the HTS coil. Based on the critical current, the operating current of the coil is determined. And the inductance decides

2 Experiment

Fig. 1 shows a photograph of the insulated double pancake coil (DPC). As illustrated in Fig. 1, the DPC was wound on an anodizing aluminium bobbin; the bobbin was attached to a G10 panel; and the solder is used to connect both ends of the coil to current-leads. In the DPC, second generation (2G) HTS wire was insulated by Kapton tape [2].

The HTS wires in this paper are from SuNAM company, whose dimensions are 4.2 mm width and 0.25 mm thickness including a 20 μm copper stabilizing layer in each side [3]-[4]. Besides, two brass tapes of 40 μm thickness are reinforced on the wire, for improve mechanical properties. And Table I lists the specifications of the HTS wire and the DPC.

**Fig.1 Photograph of the double pancake coil.**

Fig. 2 indicates the photograph of the iron core mounting the double pancake coil in a liquid nitrogen bath. Considering the actual structure, the iron core is...
designed with twin air gaps [1]. The iron core and the LN$_2$ bath are separable. Therefore, the double pancake coil and the bath will be separate from the iron core when the DPC is tested without the iron core.

### Table 1. Specifications of the HTS wire and the DPC

| 2G HTS wire | Width and thickness | Critical current, self-field |
|-------------|---------------------|----------------------------|
|             | 4.2 mm × 0.25 mm    | 170 A @ 77K                |

| Double pancake coil | Bore size of bobbin | Inner and outer diameters of coil | Turns of DPC | Total length of wire | Width and thickness of insulator |
|---------------------|---------------------|----------------------------------|--------------|---------------------|--------------------------------|
|                     | 230 mm              | 245 mm, 277 mm                   | 58 turns × 2 layers | 94 m               | 4.3 mm × 0.025 mm              |

For the inductance evaluation of the DPC, the AC voltage and current are measured for the DPC. The AC voltage includes two parts: One is an inductive component from the inductance of the coil; the other is a loss component from the AC loss of the coil. Due to the AC loss is hysteresis loss and the loss voltage of the coil linearly depends on the frequency, the AC voltage and current are measured at a low frequency, 0.25 Hz, to neglect the loss voltage and obtain the inductive voltage. Entire experiments are undergone at LN$_2$ temperature of 77 K.

### 3 Numerical model

In order to compare with the experimental data, a commercial finite element method (FEM) software, COMSOL Multiphysics, is utilized to analyse the critical current and the inductance of the DPC as numerical analysis. Fig. 3 illustrates the three-dimensional (3D) geometric model for the numerical analysis according to the actual dimensions. More detailed specifications of the iron core and the DPC are shown in Fig. 3 and the Table. The large quantity of mesh elements from the 3D geometry model will affect the calculated time. For improving the calculated speed, a quarter of the model is applied, and also the DPC is modelled as one coil. The material property of the iron core used in this analysis is referred to that in the material library of the COMSOL.

Generally, the critical current of superconducting coils is definitive by the one of the wire with the minimum critical current density [5]. This is because that once a point of the coil is quenched, the voltage of the whole coil will increase to the critical value quickly due to the voltage of the quench point. The same method is applied to calculate the critical current of our DPC. As shown in Fig. 4, only the perpendicular component of the external magnetic field is considered in the critical current analysis. The data are provided from SuNAM company and can be expressed as:

\[ I_c = 6.90 + 111e^{-4.50B} + 52.0e^{-0.519B} \]  

(1)

where $I_c$ denotes the critical current of the wire in the DPC, and $B$ denotes the perpendicular intensity of the external magnetic field.

The inductions of the double pancake coil can be calculated by using the Maxwell’s equation and its auxiliary equation. The vector magnetic potential is analyzed from (1). Then, $B$, $H$ and $W_H$ are calculated by (3)-(4). Finally, the $L$ can be calculated by (5).

\[ \nabla \times \left( \nabla \times \vec{A} \right) = \mu \vec{J} \]  

(2)

\[ \vec{B} = \nabla \times \vec{A} \]  

(3)

\[ W_H = \frac{1}{2} \int \vec{B} \cdot \vec{H} \, dv \]  

(4)
where $B$ is the magnetic flux density, $H$ means the magnetic field intensity, $A$ denotes the vector magnetic potential, $J$ is the current density, $\mu$ is the permeability of the material, $I$ the current, $L$ the inductance and $W_H$ the magnetic field energy, respectively.

4 Results and discussions

4.1 Critical current

Fig. 5 shows the V-I characteristic curves of for the DPC with and without the iron core. As depicted in Fig. 5, the $I_c$ of the DPC without the iron core is 89 A, and the one with the iron core is 84 A [2]. That is, the critical current is somewhat decreased for the existence of the iron core. Moreover, $n$-values are 42 and 18, respectively [6]. Thus, the $n$-value is greatly dependent on the iron core.

For elucidating the effect of the iron core on the magnetic field distribution, the magnetic field is calculated by the commercial program COMSOL. Furthermore, the $I_c$ of the DPC is analysed based on the data for the magnetic field distribution of the radial direction (x-axis). The radial direction of the DPC is perpendicular to the surface of the 2G HTS wire. Fig. 6 shows the calculated magnetic flux density distribution of the radial direction and the minimum critical current density for the cross section of the DPC without or with the iron core. A symbol, $\varphi$, means the direction of the current in the DPC.

As indicated in Fig. 6, the maximum magnetic flux densities are 313 mT and 351 mT, respectively. The perpendicular intensity of the magnetic flux without the iron core is obviously smaller than that with the iron core. On the contrary, the minimum critical current density for the DPC without the core at the point of maximum magnetic densities, 87.2 A/mm$^2$, is larger than that with the iron core, 80.8 A/mm$^2$. According to the minimum critical current densities and the sectional area of the wire in Table I, we can obtain the critical currents, 91.7 A and 84.8 A, for the DPC without and with the iron core, respectively. These values are in good agreement with the measured ones of Fig. 5. Moreover, the critical current of the DPC will be changed according to different positions in the iron core.

4.2 Inductance

Fig. 7 shows the instantaneous voltage and current of the DPC. As shown in Fig. 7(a) and (b), it can be known that the phase between the coil voltage and the coil current is close to 90°, and the voltage leads the current. From the experimental data, the inductances of the DPC for both cases are obtained, which are 6.94 mH and 45 mH, respectively [2]. This can be explained that the magnetic field energy becomes larger because of the iron core.

Fig. 8 presents the calculated magnetic field distribution of the coil with the iron core at the critical current, 84 A. Through the magnetic field analysis, the inductance with the core is 42.4 mH, which is calculated from (2)-(5). Similarly, the calculated inductance without the iron core is 7.02 mH. These calculated values correspond well with the measured ones.
the inductance. And then the critical current and the inductance were experimentally investigated for the DPC with or without the iron core. Moreover, the test results were discussed with numerical data.

The tested $I_c$ of the DPC without and with the core are 89 A and 84 A, respectively. And the n-values are 42 and 18. Thus the $I_c$ and the n-value significantly depend on the iron core. These experimental results correspond well with the simulated ones. For inductance results of the DPC with and without the core, the measured data are 6.94 mH and 45 mH, respectively. Therefore, the discharging and charging time for the core will be much longer than that with no the iron core. The measured inductances also correspond well with the calculated ones.

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