Revisiting the hot matter in the center of gamma-ray bursts and supernova

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ABSTRACT

Aims. Hot matter with nucleons can be produced in the inner region of the neutrino-dominated accretion flow in gamma-ray bursts or during the proto-neutron star birth in successful supernova. The composition and equation of state of the matter depend on the dynamic $\beta$-equilibrium under various neutrino opacities. The strong interaction between nucleons may also play an important role. We plan to extend the previous studies by incorporating these two aspects in our model.

Methods. The modification of the $\beta$-equilibrium condition from neutrino optically thin to thick has been modeled by an equilibrium factor $y$ ranging between the neutrino-free-escaping case and the neutrino-trapped case. We employ the microscopic Brueckner-Hartree-Fock approach extended to the finite temperature regime to study the interacting nucleons.

Results. We show that the composition and chemical potentials of the hot nuclear matter for different densities and temperatures at each stage of $\beta$-equilibrium. We also compare our realistic equation of states with those of the free gas model. We find the neutrino opacity and the strong interaction between nucleons are important for the description and should be taken into account in model calculations.

Key words. dense matter – equation of state – gamma-ray bursts: general – neutrinos – nuclear reactions, nucleosynthesis, abundances – supernovae: general

1. Introduction

Gamma-ray bursts (GRBs) and supernova (SNs) are extremely powerful explosions in the universe. In the centers of these objects, hot dense matter may be generated. The properties of the matter, such as its composition and equation of state (EoS), are very important for the studies of GRBs and SNs.

First, for the central engines of GRBs, one of the plausible candidates is the neutrino-dominated accretion flow (NDAF) around a rotating stellar-mass black hole. Such systems may originate from the merger of two compact objects or a collapsar. The NDAF model has been widely applied to explain the energy production process in GRBs (see, e.g., Popham et al. 1999; Narayan et al. 2001; Kohri & Mineshige 2002; Di Matteo et al. 2002; Kohri et al. 2005; Lee et al. 2005; Gu et al. 2006; Chen & Beloborodov 2007; Janiuk et al. 2007; Kawanaka & Mineshige 2007; Lei et al. 2009; Liu et al. 2007, 2008, 2010a, b, 2012a, b, 2013; Sun et al. 2012; Kawanaka & Kohri 2012; Kawanaka et al. 2013). Hot matter approaching nuclear densities ($\rho \sim 10^{10} - 10^{13}\text{g cm}^{-3}$ and $T \sim 10^{9} - 10^{11}\text{K}$) may appear in the inner regions of those disks, so a proper description for them should be included in the NDAF model. Liu et al. (2007) studied the radial structure and the neutrino annihilation luminosity of the NDAF. They introduced arbitrarily a bridging formula to treat the radial distribution of the electron fraction between neutrino optically thin and thick limits, thanks to an analytical relation of the chemical potential equilibrium obtained for the former case by Yuan (2005). But they ignored the strong interaction between nucleons, and simplified the calculations by suggesting that there was no difference between the number density and the energy density. Kawanaka & Mineshige (2007) paid attention to the difference of the number density and the energy density, but an active connection between neutrino optically thin and thick limits was not included in their calculations. Therefore, a more improved theoretical NDAF model should be presented, especially for the inner region of a disk.

Second, SNs (or collapsars) have also been widely calculated or simulated in the past decade (see, e.g., MacFadyen et al. 2001; Proga et al. 2003; Buras et al. 2006; Burrows et al. 2007; Iwakami et al. 2008; Hammer et al. 2010). In a successful SN, the birth of a proto-neutron star (PNS) may mainly go through several distinct steps (see, e.g., Prakash et al. 2001). The first step lasts less than one minute, during which the star with a neutrino-trapped core of mass experiences the core bounce and the passage of a shock through the star’s mantle. The outer mantle is both accreting matter from the surrounding area and losing energy due to the thermal neutrino emission. In the second step, the accretion is no longer important and neutrino cooling dominates. During the above two steps, a hot dense state ($\rho \sim 10^{12} - 10^{14}\text{g cm}^{-3}$ and $T \sim 10^{10}\text{K}$) is present both in the core and in the outer part. In such a state the neutrino production exists along with their transportation, hence the dynamics of the production process should play an important role in the calculation and simulation of SNs, where the opacity has to be taken into account.

Finally, because neutrino radiation is the main cooling mechanism for the hot matter of GRBs and SNs, the chemical potential equilibrium in the matter may depend on the neutrino opacity, namely the dynamics of the $\beta$ processes (Imshennik et al.)
Also, nucleons may interact with each other in such dense matter, thus an improved EoS including the strong interaction becomes imperative. In this paper, we then focus on the effects of the dynamics of the $\beta$ processes and the strong interaction on various input microphysics of GRBs and SNs, such as the relative composition and the EoS of the matter.

Accordingly, we assume that the nuclei are dissolved completely into nucleons, therefore nuclear many-body theories are applicable for the deriving of nucleonic chemical potentials. Incorporating the strong interaction between nucleons will certainly affect the constituent chemical potentials, the composition and the EoS of the matter. The employed nuclear model is the microscopic Brueckner-Hartree-Fock (BHF) approach widely used for the study of dense stellar matter and neutron star properties.\cite{1997NuPhA.620..279B, 1999NuPhA.638..111B, 1999NuPhA.620..273B, 2003PhRvL..90k1102B, 2004PhRvC..70b5804Z, 2006Chen2006, 2008Peng2011, 2011Chen2011, 2011Liu2011a, 2013Chen2013, 2014Burgio2014} as we shall discuss in section 2.2. We stress that our aim is not to model the centers of GRBs and SNs; rather, we want to explore how the properties of the hot matter in the center depend on the strong-interaction composition and the EoS of the matter. The employed nuclear microphysics of GRBs and SNs, such as the reaction rates of the $\beta$ processes, namely $\beta$-captures, $\beta$-equilibrium conditions, and the strong interaction on various input microphysics of GRBs and SNs, such as the relative composition and the EoS of the matter.

The paper is organized as follows. In section 2, we establish our physical model and describe in details the numerical methods for the calculation. In section 3, numerical results are presented. We present our main conclusions in section 4.

2. Model

2.1. $\beta$ equilibrium of the hot nuclear matter

For the hot matter where neutrino are completely trapped, the system can achieve its equilibrium via the following $\beta$ processes,

\begin{align}
\bar{e}^- + p &\rightarrow n + e^+ , \\
e^+ + n &\rightarrow p + \bar{\nu}_e , \\
n &\rightarrow p + e^- + \bar{\nu}_e .
\end{align}

The reaction rates of the $\beta$ reactions are equal to those of the corresponding inverse processes. Because the photons are also trapped (the chemical potential of photons $\mu_{\gamma} = 0$), the chemical equilibria $\gamma + \gamma \rightarrow \gamma^*$ or $\gamma^* \rightarrow \gamma + \gamma$ give

\begin{equation}
\mu_{\gamma} = -\mu_{\bar{e}^-} .
\end{equation}

Then by writing $\mu_{\bar{e}^-} \equiv \mu_e$, the usual chemical equilibrium condition can be applied as

\begin{equation}
\mu_n + \mu_{\bar{e}^-} = \mu_p + \mu_e ,
\end{equation}

or

\begin{equation}
\mu_n = \mu_p + \mu_e ,
\end{equation}

if the chemical potential of the trapped neutrinos is zero. These are the well-known chemical equilibrium conditions which are generally used to determine the composition of the hot matter under $\beta$ equilibrium.\cite{2006Nicotra2006, 2008Peng2011, 2011Liu2011a, 2011Burgio2011, 2013Chen2013}

However, if neutrinos can leave the system freely, the $\beta$-equilibrium of the $\beta$ reactions cannot be treated as a chemical equilibrium problem. In such circumstance the steady state of the hot matter is achieved under the following condition:

\begin{equation}
\lambda_{\beta p} \lambda_{\beta n} = \lambda_{\beta e^-} + \lambda_n ,
\end{equation}

where $\lambda_{\beta p}, \lambda_{\beta n}$ stands for the rate of the $e^\pm$-captures,

\begin{equation}
e^- + p \rightarrow n + \nu_e ,
\end{equation}

\begin{equation}
e^+ + n \rightarrow p + \bar{\nu}_e ,
\end{equation}

and $\lambda_n$ is the rate of neutron decay,

\begin{equation}n \rightarrow p + e^- + \bar{\nu}_e .
\end{equation}

The reaction rates $\lambda$ should be functions of the temperature $T$ and the constituent chemical potentials. Compared with the rate of positron capture by neutrons $\lambda_{\beta e^-}$, the rate of neutron decay $\lambda_n$ in this case could be neglected, therefore the $\beta$-equilibrium condition is reduced to $\lambda_{\beta p} = \lambda_{\beta n}$\cite{2003Beloborodov2003, 2003Pruet2003, 2005Yu2005}, and finally

\begin{equation}
\mu_\nu = \mu_p + 2\mu_e ,
\end{equation}

after the used assumption of the elastic approximation (e.g.,\cite{2005Yu2005}). Again zero chemical potential is applied for neutrinos.

By combining Eqs. (6) and (11) we introduce an equilibrium factor $\chi$ in the range of [1, 2], to explore the effect of the dynamics of the $\beta$ processes, namely

\begin{equation}
\mu_\nu = \mu_p + \chi \mu_e ,
\end{equation}

where $\chi = 1$ suggests completely neutrino-trapped matter, and $1 < \chi < 2$ corresponds to the matter with a certain amount of freely-escaping neutrinos.

To find the composition and the EoS of the matter, for each baryon number density $n_B$, Eq. (12) should be solved together with the charge neutrality condition,

\begin{equation}
n_{\bar{e}^-} - n_{e^-} = n_p ,
\end{equation}

and the conservation of the baryon number,

\begin{equation}
n_n + n_p = n_B .
\end{equation}

The nucleonic chemical potentials are derived from the free energy density of the nuclear matter, based on the finite-temperature BHF nuclear many-body approach (as illustrated below in section 2.2). The chemical potentials of the non-interacting leptons $e^\pm$ are obtained by solving numerically the free Fermi gas model at a finite temperature. Specifically, the number density of species $i$ ($i = e^\pm$) is written as

\begin{equation}
n_i(T) = \int_0^\infty \frac{g}{(2\pi\hbar)^3} n_i^F(k, T) dk ,
\end{equation}

where $(2\pi\hbar)^3$ is the "unit" volume of a cell in the phase space and $g$ is the number of states of a particle with a given momentum $k$. For $e^\pm$ leptons, $g$ equals 2. Finally, $n_i^F(k, T)$ is the Fermi–Dirac–Statistic,

\begin{equation}
n_e^F(k, T) = \frac{1}{\exp[(E(k) - \mu_e)/k_BT] + 1} ,
\end{equation}

\begin{equation}
n_{\bar{e}}^F(k, T) = \frac{1}{\exp[(E(k) + \mu_e)/k_BT] + 1} ,
\end{equation}

where $k_B$ is the Boltzmann constant and the energy $E(k) = \sqrt{k^2 + m_e^2}$ with $m_e$ being the mass of the electrons or positrons.

Once the nucleonic and leptonic chemical potentials are determined, one can proceed to calculate the composition of the hot $\beta$-equilibrium matter by solving Eqs. (13) and (14) together with
Eq. (12). Then the total energy density $\rho$ and the total pressure $P$ of the system are:

$$\rho = \rho_l + \rho_B \; ,$$

(18)

$$P = P_l + P_B \; ,$$

(19)

where $\rho_l$ and $P_l$ are the standard contributions of the leptons:

$$\rho_l = \frac{8\pi}{(2\pi)^3} \int_0^\infty (f_e - f^-)(E(k))k^2dk \; ,$$

(20)

$$P_l = \frac{8\pi}{3(2\pi)^3} \int_0^\infty (f_e - f^-)k^4/E(k)dk \; .$$

(21)

We present in the following subsection how the contributions of baryons ($\rho_B$, $P_B$) are determined.

### 2.2. BHF nuclear many-body approach

Currently, one of the most advanced microscopic approaches to the EoS of the nuclear matter is the BHF model (Baldo et al. 1999). Recently, this model was extended to the finite-temperature regime within the Bloch-De Dominicis formalism (Bloch & De Dominicis 1958, 1959). The central quantity of the BHF formalism is the $G$-matrix, which in the finite-temperature expansion (Bloch & De Dominicis 1958, 1959, Baldo et al. 1999, Baldo & Ferreira 1999) is determined by solving numerically the Bethe-Goldstone equation, and can be written in operatorial form as

$$G_{ab}[W] = V_{ab} + \sum_{c=p,p} \sum_{i<j} W_{ac} |pp_i > < p| W_{ij} + i\hbar \partial_{\chi} [G_{ab}[W]] \; .$$

(22)

where the indices $a, b, c$ indicate pairs of nucleons and the Pauli operator $Q$ and energy $E$ determine the propagation of intermediate nucleon pairs. In a given nucleon-nucleon channel $c = (12)$ one has

$$Q_{(12)} = [1 - n^{f}_{i} (k_1)][1 - n^{f}_{j} (k_2)] \; ,$$

(23)

$$E_{(12)} = m_1 + m_2 + e_1(k_1) + e_2(k_2) \; ,$$

(24)

with the single-particle (s.p.) energy $e_i(k) = k_i^2/2m_i + U_i(k)$, the above-mentioned Fermi distribution $n^{f}_{i}(k) = (e^{e_i(k) - \mu_i}/1 + 1)^{-1}$, the starting energy $W$, and the two-body interaction (bare potential) $V$ as fundamental input. The various s.p. potentials within the continuous choice are given by

$$U_i(k_1) = \text{Re}\sum_{2n,p} \sum_{k_2} n(k_2) \left\{ G_{i(12)}[12] \left[ E_{i(12)} \right]_{k_1k_2} G_{i(12)}[12] \right\}_{k_1k_2} \; ,$$

(25)

where $k_i$ generally denote momentum and spin. For given partial densities $n_i$ $(i = n, p)$ and temperature $T$, Eqs. (22-25) have to be solved self-consistently along with the equations for the auxiliary chemical potentials $\mu_i$, $n_i = \int n_i(k)$. Regarding the interactions, we use the Argonne $V_{18}$ nucleon-nucleon potential (Wiringa et al. 1995) together with the microscopic nuclear three-body forces (TFB) (Grange et al. 1985, Lejeune et al. 2000, Zuo et al. 2002). The including of TBF accomplishes excellently two important tasks. First, the corresponding zero-temperature nuclear EoS reproduces the nuclear matter saturation point correctly and fulfills several requirements from the nuclear phenomenology (Baldo et al. 1997). Second, the main relativistic effect can be taken into account, and the results in our nonrelativistic scheme agree well with the predictions of the corresponding relativistic approaches (Zuo et al. 2002).

Once the different s.p. potentials for the species $i = n, p$ are known, the free energy density of nuclear matter has the following simplified expression

$$f = \sum_i \left\{ \int_{-\infty}^{\infty} n_i^f(k) \left[ k^2/2m_i + 1/2 U_i(k) - T s_i \right] \right\} \; ,$$

(26)

where

$$s_i = -\int_{-\infty}^{\infty} \left( n_i^f(k) \ln n_i^f(k) + [1 - n_i^f(k)] \ln [1 - n_i^f(k)] \right) \; ,$$

(27)

is the entropy density for component $i$ treated as a free gas with s.p. spectrum $e_i(k)$ (Baldo 1999, Baldo & Ferreira 1999).

All thermodynamic quantities of interest can then be computed from the free energy density, Eq. (26), namely, the "true" chemical potentials $\mu_i$ $(i = n, p)$, internal energy density $\rho_B$, and pressure $P_B$ are

$$\mu_i = \frac{\partial f}{\partial n_i} \; ,$$

(28)

$$s = -\frac{\partial f}{\partial T} \; ,$$

(29)

$$\rho_B = f + Ts \; ,$$

(30)

$$P_B = n^2 \frac{\partial (f/m)}{\partial n} = \sum_i \mu_i n_i - f \; .$$

(31)

### 3. Results

For both GRBs and SNe, a hot state with nucleons exists with $\rho \sim 10^9 - 10^{14} \text{g cm}^{-3}$ and $T \sim 10^9 - 10^{11} \text{K}$. We adopted these parameter ranges in our model. One additional parameter $\chi$, the so-called equilibrium factor, is introduced to incorporate the effect of the neutrino opacity, and its value should be between 1 and 2, as discussed in the previous section.

We first display in Fig. 1 the chemical potentials of both electrons and neutrons (red lines for $\mu_e$, and green ones for $\mu_n$) as a function of the energy density $\rho$ at two fixed temperatures $T = 10^{10} \text{K}$ (filled symbol) and $T = 10^{11} \text{K}$ (open symbol), for both $\chi = 1$ (solid lines) and $\chi = 2$ (dashed lines) cases, respectively.
$T = 10^{10}$K (filled symbol) and $T = 10^{11}$K (open symbol), for both $\chi = 1$ (solid lines) and $\chi = 2$ (dashed lines) cases. Regardless of the temperature, the electron chemical potentials are always positive and increase monotonously with the density. Since electrons are treated as a degenerate fermi gas, the corresponding degenerate pressures are expected to increase with the density as well. However, $\mu_e$ changes its sign from negative to positive at high densities (around 10$^{14}$g cm$^{-3}$), which simply means that the strong interaction dominates for such dense matter. We mention here the nuclear saturation density is about 2.5$\times$10$^{14}$g cm$^{-3}$. Moreover, we find that the equilibrium factor $\chi$ affects $\mu_e$ only slightly. Its influence on $\mu_e$ is evident, but mainly at the high-density region. With the increase of $\chi$ parameter, the electron chemical potential $\mu_e$ is largely reduced, which means there is a reduced lepton fraction in the matter. Also, compared with the low temperature ($T = 10^{10}$K) case, we find much rapid increases of both $\mu_e$ and $\mu_0$ at high temperature ($T = 10^{11}$K) case.

Those results should have significant impacts on the study of the NDAF model, since we know that, there is a wide range of density in the inner region of the disk (see, e.g., Liu et al. 2007, 2008, $\rho \sim 10^9 - 10^{13}$g cm$^{-3}$, and for a typical accretion rate of 1$M_\odot$ s$^{-1}$, the neutrino optical depth would change from thick to thin if one moves away from the central black hole. Therefore, one should include the dependence of the constituent chemical potentials on the equilibrium condition, the temperature and the energy density, as demonstrated in the above figure.

We then show the compositions of the matter in Fig. 2 (for $T = 10^{10}$K) and Fig. 3 (for $T = 10^{11}$K). The relative fractions $n_i/n_0 (i = n, p, e^-, e^+)$ are plotted as a function of the energy density $\rho$, for both $\chi = 1$ (solid lines) and $\chi = 2$ (dashed lines) cases. In the low temperature case of $T = 10^{10}$K (Fig. 2), the proton fractions are very similar to the electron fractions, and they both increase with the density as a result of an increased electron chemical potential $\mu_e$ and the charge neutrality condition (Eq. [13]). On the contrary, the positron fractions decrease very quickly with increasing density as a natural result of the Fermi-Dirac distribution employed for the leptons. Here neutrons compose most of the matter (larger than $\sim 70\%$), and the matter is practically npe$^-$ for the chosen temperature $T = 10^{10}$K.

If the matter is much hotter, for example $T = 10^{11}$K in Fig. 3 at relatively low density (below 10$^{11}$g cm$^{-3}$), a large amount of $e^\pm$ pairs exist regardless the choice of $\chi$ parameter. This means the efficient creation of the $e^\pm$ pair is the characteristic of a hot nuclear system.

Fig. 4 shows the compositions as a function of $\chi$ parameter at two fixed densities $\rho = 10^9$g cm$^{-3}$ (left panel) and 10$^{13}$g cm$^{-3}$ (right panel) for $T = 10^{11}$K. At low densities around 10$^9$g cm$^{-3}$, the variation of the equilibrium parameter $\chi$ affects only trivially the relative fractions, as one might also notice in Fig. 3. But at high densities the $\chi$ dependence becomes important, thus the accretion matter in the inner region of the disk should be more appropriately modeled in the NDAF model.

Finally we summarize our results of EoSs in Fig. 5 for two temperatures $T = 10^{10}$K (red lines) and $T = 10^{11}$K (green lines), and for both $\chi = 1$ (solid lines) and $\chi = 2$ (dashed lines) cases. The predictions of the free gas model are also shown in thin lines for comparison. In both models, the higher temperature, the stiffer EoS. Because electrons contribute equally to our model and the free gas model, the differences between the thick and thin lines arise from the difference in the nucleon part. Our realistic EoSs (thick lines) usually lie below the ones based on the free-gas approximation (thins lines) because it is the long-range gravity who dominates in the matter, not the short-range nucleon-nucleon force, except at high densities. The strong interaction can not be ignored in such dense matter.
As commonly recognized, the pressure from nucleons should dominate in the inner region of the NDAF when the mass accretion rate is larger than $0.01 M_\odot$ s$^{-1}$ (see, e.g., Chen & Beloborodov 2007; Liu et al. 2007). As shown above, the nucleonic EoS is subject to change if we include more microscopic physics beyond the simple standard free gas model. Such simple model is widely used in the NDAF or collapsar models (see, e.g., Popham et al. 1999; MacFadyen et al. 2001; Chen & Beloborodov, 2007; Liu et al. 2007). For an improved study, a detailed database of the resulting pressure with the change of the temperature, the density, and the neutrino opacity should be built.

4. Conclusion

In this paper, various properties of the hot nuclear matter possible in the inner regions of GRBs and SNe have been revisited. We employ the microscopic BHF approach to account for the strong interaction between nucleons, and calculate the nucleonic chemical potentials and the nucleonic EoS in this method. We introduce a parameterized chemical potential equilibrium bridging between neutrino optically thin and thick limits, and show the compositions and the EoSs of the matter at several temperatures under different chemical potential equilibria, labeled by the so-called equilibrium factor $\chi$. We also display the comparison of the EoSs with those of the free gas model. We find that, for the description of the hot matter the effect of the neutrino opacity and the strong interaction can be very important. They should be taken into account in future model calculations.

For example, since one popular central engine model that powers GRBs consists of a black hole and a NDAF with a hypercritical mass accretion rate, and the neutrino annihilation luminosity in the NDAF model can be significantly affected by the matter properties of the inner region of the disk, we will revisit the NDAF model by incorporating the findings of the present work in the description of the inner region, to verify more convincingly whether the NDAF model still can be one of the candidates of the central engines of GRBs.

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Fig. 5. EoSs for two temperatures $T = 10^{10}$ K (red lines) and $T = 10^{11}$ K (green lines), and for both $\chi = 1$ (solid lines) and $\chi = 2$ (dashed lines) cases. The predictions of free gas model are also shown in thin lines for comparison.