The Science Case for Simultaneous mm-Wavelength Receivers in Radio Astronomy

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Abstract

This review arose from the European Radio Astronomy Technical Forum (ERATec) meeting held in Firenze, October 2015, and aims to highlight the breadth and depth of the high-impact science that will be aided and assisted by the use of simultaneous mm-wavelength receivers.

Recent results and opportunities are presented and discussed from the fields of: continuum VLBI (observations of weak sources, astrometry, observations of AGN cores in spectral index and Faraday rotation), spectral line VLBI (observations of evolved stars and massive star-forming regions) and time domain observations of the flux variations arising in the compact jets of X-ray binaries.

Our survey brings together a large range of important science applications, which will greatly benefit from simultaneous observing at mm-wavelengths. Such facilities are essential to allow these applications to become more efficient, more sensitive and more scientifically robust. In some cases without simultaneous receivers the science goals are simply unachievable. Similar benefits would exist in many other high frequency astronomical fields of research.

Keywords: Astronomical instrumentation, methods and techniques – Instrumentation: interferometers – Methods: observational – Telescopes – quasars: general – Astrometry – quasars: jets – Stars: AGB and post-AGB – Stars: formation – X-rays: binaries

1. Introduction

Very Long Baseline Interferometry (VLBI) studies at cm wavelengths is a well-established field, with advanced technological developments and analysis techniques that result in superb quality images, including those of very weak $\mu$Jy sources \cite{46} and with micro-arcsecond ($\mu$as) astrometry \cite{129}, using phase referencing (hereafter PR) techniques.

VLBI at mm and sub-mm wavelengths (hereafter mm-VLBI) can result in the highest angular resolutions achieved in astronomy and has a unique access to emission regions that are inaccessible with any other approach or at longer wavelengths, because the compact areas of interest are often self-absorbed or scatter-broadened. Therefore it holds the potential to increase our understanding of the physical processes in, for example, Active Galactic Nuclei (AGN) and in the vicinity of super-massive black holes, and for studies of molecular transitions at high frequencies.

Nevertheless the scientific applications of mm-VLBI have to date been much less widespread, the reason being that the observations become progressively more challenging as the wavelengths gets shorter because of the: limited telescope surface accuracy and efficiency, higher receiver system temperatures and lower sensitivity...
and shorter atmospheric coherence times. Also most compact extra-galactic sources used as cm-wave phase references are intrinsically weaker, if not resolved-out, at shorter wavelengths. These in turn prevent the use of phase referencing calibration techniques, which are routinely used in cm-VLBI, and all benefits resulting from them, beyond \( \sim 43 \) GHz (with a single exception (to date) of PR at 86 GHz by Porcas and Rioja 2002).

Continuous development and technical improvements have led to a sustained increase of the high frequency threshold for VLBI observations in the last two decades [e.g., 81]. Regular observations up to 86 GHz are being carried out with well established networks such as the Very Long Baseline Array (VLBA) and Global mm-VLBI Array (GMVA), most recently with the Korean VLBI Network (KVN) up to 130 GHz, and ad-hoc observations at the highest frequencies up to 240 GHz with the Event Horizon Telescope (EHT) [33]. The field of mm-VLBI will benefit from the arrival of phased-up Atacama Large Millimeter and submillimeter Array (ALMA) [98, 152] for joint VLBI observations.

The benefit of multi-frequency based calibration techniques in observations at high frequencies, which are dominated by non-dispersive fast tropospheric fluctuation errors, has long been known. It relies on using the correctly scaled calibration derived at lower frequencies to correct the higher frequencies; see, for example, [15, 6] for connected interferometers. This has been extended to VLBI observations using the frequency agility capability (i.e. fast frequency switching) of the VLBA, initially offering an increased coherence [101] and, after further development, bona-fide astrometric measurements [30, 134] at the highest frequency of 86-GHz. The first step is known as Frequency Phase Transfer (FPT), where the solutions for the low frequency \( \nu_{\text{low}} \) are applied to the high frequency \( \nu_{\text{high}} \), scaled by the ratio of the frequencies. This does not provide astrometry because of dispersive terms, such as the ionosphere, and also the inherent phase ambiguities in the phase solutions at \( \nu_{\text{low}} \). The latter is not a problem if the ratio is an integer, as then the ambiguities continue to cancel, or if the number of ambiguities are zero, which requires the positions to be well known. The FPT calibration step eliminates all the common non-dispersive residual errors on the target source. The second step provides Source Frequency Phase Referencing (SFPR) by including an additional ‘conventional’ phase referencing step on a second source, which eliminates all other common residual errors, which are mainly dispersive and/or instrumental. This switching can be over long cycle times and large angular separations, as these terms are slow changing and have weak angular dependence.

The use of this calibration technique on the VLBA has not been widespread, the reason being that the data reduction was challenging because of the fast temporal variations arising from the troposphere. Nevertheless there are a few examples of such analysis [134, 137, 90]. The KVN has introduced a new engineering development in receiver technology [61] to address this issue, with the capability for simultaneous multi-frequency observations at four bands. Using KVN observations and multi-frequency based calibration techniques it is possible to phase reference the observations at frequencies up to 130-GHz. In this document we will explore some of the scientific topics and current issues that will benefit from this technical capability.

Simultaneous multi-frequency observing enhances mm-VLBI in two main areas: massively increasing the coherence time, for observing weak sources at high frequencies, and enabling accurate astrometric registration between frequency bands. The raw increase in coherence time, even at 130-GHz, has been shown to be easily enlarged from tens of seconds to a few tens of minutes, using observations of the target source only [136]. This increase in coherence time would be the equivalent to a three-fold increase in the dish diameter, or an increase of two orders of magnitude in the recorded bandwidth. Furthermore the latter would only apply for continuum science, as this does not assist the important spectral line science cases. The coherence time can be further increased by including the observations of a calibrator source.

Accurate astrometry is required to allow bona-fide spectral index or Faraday rotation measure investigations in continuum sources and the measurements of the frequency-dependent position of the continuum cores in extragalactic radio sources [159, 67]. Spectral line models enable high-precision measurements of the structure and kinematics of the various components of the studied sources, using different tracers [e.g. 29, 146], or by using absorption of continuum flux by intervening gas [155, 109]. VLBI is the most developed area driving the demand for simultaneous mm-wavelength receivers, but it is not the only field. Time domain radio astronomy is a growth area, and for rapidly changing sources with strong mm-wavelength emission simultaneous mm-wavelength receivers add an important new capability to aid the interpretation of observations. The study of pulsars is a well-known example and is a target of the BlackHole Cam ERA project, but the examples we review in this paper are results from the spectral evolution of the strong and rapidly changing mm emission from the jets in compact X-ray
Therefore there is a wealth of possibilities opened up by the application of simultaneous multi-frequency mm-wavelength observing, using demonstrated methods and technology. In this paper we present some of the headline cases for continuum and spectral line VLBI and time-domain observations.

1.1. Current achievable sensitivities for mm-wave observatories

We review the current status and sensitivities of facilities capable of supporting simultaneous mm-wave observing. VLBA is capable of switching between receivers in 10–20 seconds, depending on the pairing. KVN was built for simultaneous observing, and this capability is now been extended to all of KaVA (the KVN and VERA Array). Table 1 lists the expected baseline sensitivities for these arrays with current standard recording bandwidths and observing modes (i.e. fast frequency switching or simultaneous), using the lowest frequency in the range (with typical coherence times) and the highest frequency in the range (with a typical post-FPT coherence time of 30 min). Overheads for FFS are included. Post-SFPR coherence time is essentially infinite, theoretically providing infinite sensitivity. A typical SFPR image for a long observation (5 hours of on-source time) would be about three times more sensitive than the FPT image (and astrometrically registered).

We note that these results are for current (2017) facilities and bandwidths, and facilities are being upgraded and/or built around the world: ALMA offers a generational leap in sensitivity and maximum frequency for interferometric arrays, additionally a number of large mm-wave single dishes have been built (Yebes 40m, LMT 50m, the ALMA 12m prototypes now located in Arizona and Greenland, KVN, Metsahovi 14m, and several others proposed). Single dish antennas can be easily upgraded to host simultaneous multi-frequency receivers, as has been done at VERA and Yebes. Discussions are on-going as to whether this should be done at ALMA, largely to aid in the long baseline observing at their highest frequencies. In addition Australia Telescope Compact Array (ATCA), ALMA and the Jansky Very Large Array (JVLA) are all capable of sub-array mode observing, which does allow for - at the very least - Frequency Phase Transfer and should allow SFPR in compact configurations.

| Facility | Freq. Range | Baseline Sensitivity (µvlow) | FPT Baseline Sensitivity (µvhigh) |
|----------|-------------|-----------------------------|----------------------------------|
| VLBA     | 22-86 (switched) | 4a                          | 8b                               |
| KaVA     | 22-43       | 10c                          | 4d                               |
| KVN      | 43-130      | 22e                          | 12f                              |

Table 1: Baseline sensitivities for the lower observing frequency in the range and for the higher observing frequency, after Frequency Phase Transfer to increase the coherence time, for current mm-wave facilities capable of this style of observing. a 1/3 cycle time of 2 min at 2 Gbps, b 1/3 cycle time of 30 min at 2 Gbps, c 2 min at 0.5 Gbps, d 30 min at 0.5 Gbps, e 1 min at 0.5 Gbps, f 30 min at 0.5 Gbps.

2. Continuum Studies

2.1. Weak Sources

The high angular resolution provided, combined with the opacity effect in high electron density regions that smother the radiation at cm-frequencies, require us to use mm-VLBI to explore the details of the innermost regions of galaxies and AGNs, by reaching a spatial resolution of a few tens of Schwarzschild radii (R_s). The Galactic Centre Sgr A*, for example, has a R_s of 10 µ-as \[\text{[142]}\], which can only be seen by overcoming the synchrotron self-absorption barriers. Although the physical mechanisms of energetic processes, such as jet formation and acceleration in AGNs have been widely studied at cm-wavelengths, our understanding at mm-wavelengths is still limited due to several considerations, such as the number of available sources, sensitivity, suitable telescopes etc. Since radio sources become generally weaker as the observing frequency increases, most radio sources are difficult to detect and image using mm-VLBI, as compared to cm-wavelengths. Most VLBI surveys of continuum sources

\[\text{[from the EVNCalc tool \url{http://www.evlbi.org/cgi-bin/EVNcalc.pl}}\]
have therefore been conducted at lower frequencies. In particular, the advent of the VLBA greatly facilitated large VLBI surveys addressing various statistical properties of AGNs; for example, their structure, compactness, brightness temperatures and spectral indices, gamma-ray connection, polarimetry and cosmological evolution (see Table 2). However, weak sources can always be imaged as long as a calibration scheme to compensate for the atmospheric disturbances is included in the experiment. This compensation does not need to be as perfect as for phase referencing, where all errors are corrected, for the simple detection of weak sources. For this, we only require an increase in the coherence time, which, combined with the large bandwidths of modern recording systems, is sufficient for this science case. For this we use FPT to remove all fast changing non-dispersive contributions.

As shown in Table 2 there is also a remarkable difference in the number of calibrator sources between cm- and mm-wavelengths. In the most recent update on the radio fundamental catalog (RFC 2016c) by Petrov [121], a total of 11,426 compact radio sources has been compiled from S/C/X/K-band observations, and of those more than 3,400 sources are listed in the VLBA calibrator surveys (e.g. VCS1 to VCS6, [123] and references therein). In comparison only 121 sources are catalogued at 3 mm [88], and these are limited to the very brightest radio sources. We note, however, that ALMA is undertaking a number of surveys [38, 5] at 3mm and above, which will significantly improve the situation particularly in the Southern Hemisphere, albeit at shorter baselines.

Together with atmospheric fluctuations, the small number of suitable telescopes and their sensitivity at mm-wavelengths make it very challenging to produce high dynamic range and high-fidelity images of radio sources. If we assume a typical Allan standard deviation of the atmospheric delay in the troposphere as \( \sim 10^{-13} \) [151, Chpt. 9], the expected coherence time for 3 mm VLBI is only about 20 seconds, and the sensitivity of radio telescopes in GMVA stations generally ranges from 1000 to 5000 Jy in system equivalent flux density (SEFD\(^2\)), which leads to a \( \sim 0.1 \) Jy 5\( \sigma \) sensitivity in that time. In such situations, VLBI observations using the simultaneous mm-wavelength receivers have demonstrated that one can compensate for phase fluctuations effectively, resulting in an order of magnitude sensitivity enhancement [73, 136]. As a result, a large number of radio sources that have never previously been detected or imaged at mm-wavelengths can now be targeted. This is crucial because our current understanding of physical processes at the centers of galaxies and AGNs has only been studied in a small number of examples, mostly bright radio sources, which may introduce statistical biases.

According to the results achieved by the KVN (where the baselines are short and the atmosphere seems particularly stable), 30 minutes integration of visibilities is possible even at 129-GHz, giving a 5 sigma detection sensitivity as low as \( \sim 25 \) mJy. This is shown in Fig. 1 where the detected source SNR is plotted as a function of integration time for no calibration, with FPT calibration, and compared to the theoretical SNR assuming no coherence losses.

Recently, KVN has commenced a Multi-frequency AGN Survey with the KVN (MASK), which is under way in order to densify the grid of available radio sources at 22, 43, 86, and 129 GHz. The early detection statistics for the first 10% of the total sample (\( \sim 1500 \)) with a 1 Gbps recording rate (64 MHz bandwidth per band) and using FPT from 22 GHz shows around a 97, 97, 90, and 60% detection rate at 22, 43, 86, and 129 GHz, respectively. After transferring calibration solutions from K to Q/W/D with a total 30 min integration at 1-Gbps, we find a 5-sigma sensitivity of 10/20/30 mJy, respectively. This result is very promising for finding many more weak sources by utilising simultaneous mm-wavelength receivers. In addition, it should be noted that simultaneous flux measurements at different frequencies give better constraints on spectral analysis, especially for AGNs that are highly variable on time scales similar to the observation length, and whose flares are associated with structural changes in the early stages of their evolution, such as Sgr A* [e.g. 87].

Nevertheless, it is very difficult to obtain high-fidelity images of compact radio sources, such as the immediate vicinity of supermassive black holes, with the few KVN baselines (max \( \sim 500 \) km), and thus, studying the structure and evolution of (sub-) pc scale emissions is demanding. In addition, the statistical study of relativistic jets using the observed distribution of brightness temperatures (\( T_b \)) and/or the intrinsic \( T_b \) of mm-VLBI cores will be challenging. Accordingly, increasing the number of mm-VLBI telescopes with simultaneous mm-wavelength receivers is a crucial requirement to deepen our understanding of galaxies and AGNs. With such a capability, mm-VLBI could observe a similar number of sources and obtain comparable sensitivity to that achieved currently.

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\( \text{http://www3.mpifr-bonn.mpg.de/div/vlbi/globalmm} / \)
Figure 1: The FRING SNR for 3C279 at 129GHz, over a range of integration times, from the single KVN baseline between Ulsan and Tamna, observed on 09 Apr. 2012. Plotted in blue are the direct detections, in red are the detections once calibrated with the scaled phase solutions from 86GHz and in green are the theoretical sensitivities, extrapolated from the SNR achieved in 0.5 min. The FPT calibrated data achieves 77% of the theoretical sensitivity even with an integration time of 30 minutes.
| Survey ID                   | Wavelength | No. Sources | Reference                  |
|----------------------------|------------|-------------|----------------------------|
| CJF survey                 | 6 cm       | 293         | Taylor et al. [148]        |
| VSOP VLBApls               | 6 cm       | 374         | Fomalont et al. [39]       |
| CJF Polarimetry survey     | 6 cm       | 177         | Pollack et al. [125]       |
| ICRF                       | 3.6 cm     | ~500        | Ojha et al. [115, 114] and references therein |
| MOJAVE                     | 2 cm       | >133        | Lister and Homan [90]      |
| 2cm Survey                 | 2 cm       | 250         | Kovalev et al. [78]        |
| VLBA Calibrator Survey     | 13 & 3.6 cm| >3400       | Kovalev et al. [80]        |
| VIPS                       | 6 cm       | 1127        | Helmboldt et al. [62]      |
| VERA FSS / GaPS            | 1.35 cm    | 500         | Petrov et al. [122]        |
| VSOP Survey                | 6 cm       | ~300        | Dodson et al. [28]         |
| TANAMI                     | 3.5 & 1.3 cm| 80          | Ojha et al. [116]          |
| mJIVE-20                   | 20 cm      | >4300       | Deller and Middelberg [22]|
| GMVA 3mm                   | 3 mm       | 123         | Lee et al. [88]            |
| ICRF 22 & 43-GHz           | 13.7 & 7 mm| ~100        | Lanyi et al. [86]          |
| KVN Q-CAL survey           | 7 mm       | 638         | Petrov et al. [124]        |

Table 2: Summary of VLBI Surveys, their wavelengths and the number of sources catalogued. The difference in scale of the number of sources in the cm and mm surveys are clear.

with cm-VLBI.

2.2. Astrometry

Astrometry provides fundamental information for a large number of fields in astronomy. An accurate (i.e. astrometric) registration of images (be they total intensity, polarised emission, spectral line or others) obtained at different frequencies is crucial to form a meaningful interpretation based on multi-frequency comparisons, in a similar manner as is required between epochs for multi-epoch temporal studies. Bona fide astrometry can be achieved with a suitable calibration strategy that removes the dominant contribution of the medium through which the signal propagates, while retaining the intrinsic astrometric signature of the source in the phase observable. If so, the astrometric accuracy is ultimately limited by the uncertainty in the precise phase observable and reaches the thermal limit of the instrument \( \sigma_{pos} \sim \theta_B / \text{SNR} \), where \( \sigma_{pos} \) is the positional accuracy, \( \theta_B \) is the synthesised beam and SNR is the Signal to Noise Ratio, which leads to \( \mu \)-as astrometry. Phase referencing does this, by interleaving observations of a second source, but this fails for frequencies beyond \( \sim 43 \)-GHz, defeated by the fast tropospheric fluctuations.

There are a number of image-based methods in AGN studies which have been used to align images between frequencies, but these are very dependent on a-priori assumptions and results will always be open to question. The core of the jet, defined as the upstream end of the jet, would seem a priori to be the best choice, since it is usually the strongest jet feature. However, opacity effects at centimetre wavelengths can move its position with observing frequency [e.g., 9]; an effect known as opacity core-shifts. Furthermore, the blending of multiple components close to the VLBI core at longer wavelengths further complicates the alignment of the images. It is therefore more convenient to choose jet components that are known to be optically thin, strong, and compact, for a more accurate determination of their position. Finding such components is not always easy, specially when comparing observations at relatively distant observing wavelengths, due to the vastly different convolving beams. An alternative method for the alignment of the images can be obtained by performing a cross-correlation of the optically thin jet emission [157], which has provided a very simple approach to derive results [e.g., 20, 43, 108]. However these image-based non-bona fide methods are prone to producing results with reduced accuracy and precision. Hovatta et al. [66] argued that any results derived without accurate phase referencing are questionable close to the core, which are the regions of most interest in mm-VLBI.

The KVN [76, 89] is the first dedicated mm-VLBI array and addresses one of the fundamental limitations of the field, the atmospheric stability, with an innovative multi-channel receiver design. KVN currently consists
of three antennas spread across South Korea, located in the campus of the Universities of Yonsei and Ulsan on the mainland, and in Tamna, on Jeju island. The observing frequencies are centred at 22, 43, 87 and 130 GHz. The multi-channel receiver \[61\] of KVN is designed for atmospheric compensation using simultaneous observations at multiple bands, which results in an effective increase of the coherence time, well beyond that imposed by atmospheric propagation. The KVN backend \[113\], combined with the SFPR calibration strategy \[30\] \[134\] \[135\] \[137\], allows high precision astrometric measurements even at the highest frequencies of 130-GHz \[136\]. The SFPR step of the calibration removes the remaining dispersive residual errors (i.e. instrumental and ionospheric propagation effects) using the interleaving observations of another source. This two-step calibration retains the astrometric signature of any source position shifts between the two frequencies in the interferometric phase. This is done for all frequency pairs which have an integer frequency ratio \(R\) (with \(R = \nu_{\text{high}}/\nu_{\text{low}}\)). We know of no demonstrated upper frequency limit and the method would be expected to work as long as the tropospheric propagation effects were non-dispersive. The baseline lengths between the KVN antennas range between 300 and 500 km, providing a spatial resolution \(\sim 1\) mas at the highest frequency band. Work is on-going to develop a global network of KVN-compatible antennas \[71\], which will provide tens of \(\mu\)-as resolution.

In Rioja et al. \[137\] we presented results of simultaneous SFPR astrometric measurements with KVN at 22 and 43 GHz for continuum sources, along with a detailed comparative study with contemporaneous observations using fast frequency switched SFPR observations, made with the VLBA. Dodson et al. \[31\] presented the demonstration for non-integer spectral line observations, with the registration of maser emission of H\(_2\)O and SiO masers of the AGB star R-LMi at 22 and 43 GHz. In Rioja et al. \[136\] astrometric VLBI measurements were successfully extended to all the four frequency bands supported by the KVN, that is up to 130 GHz. Fig. 2 shows the results from this study. More recently Yoon et al. \[160\] have successfully applied SFPR for registration of the four bands in spectral line observations, comprising the water masers at 22-GHz, and 4 SiO maser transitions at 42.8, 43.1, 86.2 and 129.3-GHz, in VX Sgr.

SFPR is primarily designed for astrometric registration between frequencies, but can produce positional astrometry with respect to an external reference point at high frequencies when combined with conventional phase referencing observations at the lower frequency. An example of such an analysis was the astrometric measurement of R-LMi \[31\], see Fig. 3. In this case the two decades time span between our observations and the Hipparcos measurements \[156\] lead to large positional uncertainties. The conventional phase referencing astrometry of the H\(_2\)O masers with respect to a quasar, then the SFPR referencing of the emission from SiO masers with respect to that from H\(_2\)O masers, allowed the positional astrometry of the star (at 43-GHz) to be determined with significantly better accuracy, reducing the uncertainty in the proper motion for R-LMi by an order of magnitude.

2.3. Faraday Rotation studies

VLBI polarimetric observations provide a unique tool to obtain information about the strength, degree of ordering, and orientation of the magnetic field on the plane of the sky in AGN jets. Simultaneous polarimetric VLBI observations at two or more frequencies allow, also, for the determination of the Faraday rotation of the plane of polarisation, since it is proportional to the square of the observing wavelength. (In practise more than two are required, to resolve ambiguities.) This can be used to determine the direction of the line-of-sight magnetic field – and therefore the three-dimensional structure of the field, given that the amount of Faraday rotation depends on the line-of-sight magnetic field strength. It provides also a way to probe the thermal plasma around the radio-emitting jet regions, since the amount of rotation depends also on the thermal electron density. This has been used to study, for example, the interaction of the jet with the external medium \[45\] \[50\] \[51\].

These Faraday rotation studies are predicated on a proper alignment of the VLBI images across different observing wavelengths, but self-calibration of the visibility data during the imaging process results in the loss of absolute positioning of the source (unless a starting model is used with an accurate position, itself derived from phase referencing). As discussed previously, registration of the VLBI images is commonly performed by looking for optically thin jet features (components) that can be unambiguously identified in all of the images, or be obtained by performing a cross-correlation of the optically thin jet emission. The concerns raised in Hovatta et al. \[65\] about the accuracy of these methods, particularly close to the core region, are discussed in Section 2.2. A bona-fide astrometric registration of the images can only be obtained through phase-referenced observations, and for mm-VLBI the best method available is SFPR. Nevertheless a number of the results discussed here are based on these non-bona-fide astrometry techniques, demonstrating the science that can be extracted.
Figure 2: The derived individual core-shifts for a subset of five sources from the S5 polar cap sample, between 22, 43, 86 and 130-GHz. (a)-(e) Polar plots of the decomposed absolute single-source position shifts between two frequencies, for five frequency pairs for the AGNs. These are shown in different colors (K → Q (red), K → W (blue), K → D (black), Q → W (green), and Q → D (cyan)). In the polar plots the position angles are shown outside the largest circle and are 0° and 90° toward north and east, respectively, and the magnitude units, as specified in the concentric circles, are in µas. f) shows the expected jet directions on an arbitrary scale. These results have been derived from the SFPR pairwise measurements, using SVD plus the alignment constraint between the jet and the position shift directions, to break the degeneracy. See Fig. 10 of Rioja et al. [136] for details.
Figure 3: The astrometric position of the AGB star R-LMi (small cross), as derived from the centroid of the SiO J=0→1 maser emission, with blue (v=1) and green (v=2) contours. The SiO masers are astrometrically registered to the H$_2$O maser emission (red contours), which is conventionally phase referenced to a known extra-galactic calibrator. The large cross indicates the Hipparcos position for this source, with the bar length being the proper motion error over the 21 years since the optical positional epoch. For details see Dodson et al. [Fig. 5][31].
Figure 4: *Left*: RadioAstron images of BL Lac at 1.3 cm from November 11, 2013. Total intensity is shown in contours, linearly polarised intensity in color scale, and white bars indicate the EVPAs. The inset panel shows the uv-coverage. *Right* shows the rotation measure map and a) two-dimensional histograms of the rotation measure and b) Faraday-corrected EVPA in the core area. For details see figures in Gómez et al. [49].
Faraday rotation analysis can be used to look for helical magnetic fields in AGN jets, which are expected to arise from the differential rotation of the accretion disk, and are thought to have an important role in the actual jet formation and collimation processes [e.g., 100, 162]. Faraday rotation measure (RM) gradients across the jet width should appear naturally if the jets are threaded by a helical magnetic field due to the systematic change in the net line-of-sight component of the magnetic field across the jet, with increasing values toward the jet boundaries [85]. The first observational evidence for the existence of such gradients in RM across the jet was given by [3] based on near-simultaneous multi-wavelength VLBA observations of the quasar 3C 273. Further observations have confirmed the transverse RM gradient in 3C 273 [164, 1, 67], as well as in other sources [44, 2, 4, 119].

One of the most comprehensive studies of Faraday rotation in AGN jets was performed by [67], in which 149 sources from the MOJAVE sample were observed with the VLBA at four frequencies between 8 and 15 GHz. Four sources, CTA 102, 4C 39.25, 3C 454.3, and 3C 273 were found to contain clear RM gradients across the jet width. The jet in 3C 273 also displayed variations in the RM screen on a time scale of months, which may require some internal Faraday rotation, produced in the jet emitting region. However, it is not clear whether this can be a universal jet launching mechanism as in some cases the required rotation measure gradients are not detected, or imply too weak a magnetic field, and an alternative cause in the shape of a Faraday screen external to the jet cannot be ruled out [149, 163].

Studying the magnetic field configuration in the vicinity of the central black holes in AGN jets requires the highest angular resolution possible, which involves VLBI observations at either progressively shorter wavelengths or larger baseline distances, such as those provided by the RadioAstron space VLBI mission. The first polarimetric RadioAstron 1.3 cm observations were performed in November 11, 2013, in which BL Lac was observed in combination with a ground array of 15 antennas (see Fig. 4). Correlated visibilities between the ground antennas and the space radio telescope have been found extending up to a projected baseline distance of 7.9 Earth diameters, yielding a maximum angular resolution of 21 μas, the highest achieved to date in astronomy [49]. Fig. 4 shows the RM image obtained by combining the RadioAstron 1.3 cm observations of BL Lac with simultaneous ground array 7 mm and 2 cm observations. The RM and Faraday-corrected EVPAs in the core area display a clear point symmetry around its centroid. This is better observed in the probability distribution function of the two-dimensional histogram for the RM and Faraday-corrected EVPAs as a function of position angle with respect to the centroid of the core, as shown in Fig. 4. This suggests that the core region in BL Lac is threaded by a large-scale helical magnetic field, as shown in relativistic magnetohydrodynamic simulations [127]. Whilst we are confident in the solidity of these results, the lack of bona-fide astrometry prevents a robust characterization of the errors associated with the alignment of the images. Furthermore, for other weaker sources a proper astrometric analysis may be required to prevent unambiguous interpretation of the results.

2.4. Opacity core-shifts, γ-ray flares, and the nature of the VLBI core

The standard Blandford & Königl conical jet model hypothesises that the core is not a physical feature in the jet, but corresponds to the location at which the jet becomes optically thin, and therefore its position shifts with observing frequency [9, 77, 48, 91]. Multi-frequency VLBI observations at centimeter wavelengths have measured this core frequency shift in multiple sources, albeit without phase-referencing [e.g., 79, 118, 145, 91]. Nevertheless phase-referenced VLBI observations have confirmed that the cm-wavelength radio core indeed is consistent with the optically thick-thin transition, in a smaller number of targets, such as 3C 395, 4C 39.25, 1038+528, 3C 390.1, M 81, M 87 and 3C454.3 [87, 58, 139, 140, 97, 59, 84 respectively].

On the other hand results of over seven years of monthly monitoring of 36 blazars (the most luminous and variable BL Lac objects and flat-spectrum radio quasars), with the VLBA at 7mm by the VLBA-BU-BLAZAR program, show that most γ-ray flares are simultaneous within errors with the appearance of a new superluminal component or a major outburst in the core of the jet, which is defined as the bright, compact feature in the upstream end of the jet [93, 70, 16]. A burst in particle and magnetic energy density is therefore required when jet disturbances cross the radio core in order to produce γ-ray flares, which can naturally be explained by identifying the radio core with a recollimation shock [54, 53, 21]. Multi-wavelength observations of blazars therefore suggest that the radio core is a physical feature (recollimation shock) in the jet at a fixed location.

We have therefore two sets of results, one suggesting that the radio core marks the transition between the optically thick-thin jet regimes while the other implies that it corresponds to a recollimation shock. A possible
solution to reconcile these apparently contradicting observational results is to consider that the Blandford & Königl core-shift at centimeter wavelengths is produced because the foot of the jet becomes optically thick at these low frequencies. On the other hand, at millimeter wavelengths one can see closer to the Black Hole, revealing a recollimation shock that was previously hidden. While the Blandford & Königl model holds for our best studied case, M87 [60], simultaneous observations at γ/X-rays, optical, infrared, and radio, together with mm-VLBI imaging, have shown that in several other radio galaxies and blazars the core indeed is inferred to lie parsecs away from the central black hole [94, 95, 18, 42].

To test this scenario we have performed numerical simulations using the finite-volume code RATPENAT, which solves the equations of relativistic hydrodynamics [120, and references therein]. The jet is launched with a Lorentz factor of 7 and an initial over-pressure of 1.5 times that of the external medium, in order to obtain a recollimation shock. Using the hydrodynamical results as input, we have then computed the synchrotron emission at different observing frequencies [for details of the numerical model used see 54, 52, 104], adjusting the model parameters so that the jet is optically thin at 86 and 43-GHz, and becomes optically thick at lower frequencies. A magnetic field in equipartition with the particle energy density is assumed. The results are shown in Fig. 5a and b. At cm-wavelengths (5 to 22 GHz) numerical simulations reproduce the opacity core-shift of a Blandford & Königl conical jet model, while at millimeter wavebands (43 and 86GHz) the core position clearly departs from this behaviour, revealing the core as an optically thin recollimation shock at a fixed jet location. Testing this scenario requires astrometric observations at millimeter wavelengths, for which the SFPR technique can provide the necessary high precision. Recent observations, see Fig. 5c, suggest that this effect has been detected for the first time, in BL-Lac, reproducing the simulations extremely closely [32].

3. Spectral Studies

3.1. Multifrequency VLBI observations of maser emission in evolved stars

3.1.1. AGB and post-AGB evolutionary phases

Most stars in the sky, with initial masses between about 0.5 and 8 $M_\odot$, reach the AGB phase (or a similar one) at the end of their lives. After this phase, most of the initial mass has been ejected to form planetary nebulae (PNe), after the short phase of protoPN. Finally, this ejected material will return to the interstellar medium, enriching it (and the new generations of stars to be formed from it) with heavy elements.

The copious mass-loss of AGB stars forms thick circumstellar envelopes (CSEs) around them. Mass-loss is a basic phenomenon in their evolution, the ejection rate tends to increase with time and, by the end of the AGB phase, it is so strong (reaching up to $10^{-3} M_\odot$ yr$^{-1}$) that most of the initial stellar mass is ejected in a relatively
short time. Then, the AGB phase ends, the stellar core becomes exposed, becoming the new central star. This new star is very compact and shows an increasingly high temperature, rapidly evolving to the blue and white dwarf phase.

The circumstellar nebula is also evolving very fast: from the nearly spherical CSE in the AGB phase, which is in relatively slow expansion (at, say, 10-15 km \( \text{s}^{-1} \)), to the strongly axisymmetric PNe around the dwarfs, which show very fast bipolar outflows, with axial velocities as high as several hundred km \( \text{s}^{-1} \), [13] [7] etc. This metamorphosis is a very fast and spectacular phenomenon. Within about 1000 yr, the star becomes a blue dwarf able to significantly ionize the nebula, which has already developed a wide bipolar shape.

The mass-loss process in AGB stars behaves, basically, in two phases, [e.g. 65]. In inner circumstellar regions, the stellar pulsation (all these old stars are strongly pulsating, in more or less regular modes) propagates in the outer atmospheric layers, leading to quite high densities during some pulsational phases, out to a few times the optical/NIR photospheric radius from the photosphere. When the gas temperature drops to about 1000 K, at a few photospheric radii, the formation of dust grains becomes very efficient and refractory material condenses.

Radiation pressure acts very efficiently on dust grains, which are dynamically coupled with gas. The result is that the whole circumstellar layers start expanding, quickly reaching (at 10-20 stellar radii) their final expansion velocity. The circumstellar dynamics, which is in fact driving the evolution of the AGB stars and the ejection of PNe, is really active only in those inner regions. The study of the inner layers of CSEs is therefore crucial to understand these phases of the stellar evolution.

### 3.1.2. SiO and H$_2$O masers from AGB stars

SiO (at 43, 86, 130, 215, ... GHz) and H$_2$O (22-GHz) masers are known to be very useful tools for studying the detailed structure and dynamics of the AGB CSEs. SiO masers come from regions at about 2-4 stellar radii, where pulsation is propagating and dust is not yet completely formed. The SiO maser lines in general come from a ring of spots, centered on the star, very probably due to the dominant tangential amplification [27, 24, etc]. On the other hand, H$_2$O masers form shortly after grain formation, when the final expansion velocity is being reached, e.g. Richards et al. [132]. The very high angular resolution of VLBI imaging at these frequencies allows very detailed mapping of such crucial shells, providing also valuable information on their dynamics. However, the complex pumping of the masers, which is not well understood (particularly for SiO), and the often poor information about the relative positions of the spots detected at the different frequencies strongly limit our studies of circumstellar masers from VLBI data.

SiO masers appear in rotational transitions \((J=1\rightarrow0, J=2\rightarrow1, J=3\rightarrow2, \ldots)\) within vibrationally excited states \((v = 1, 2, 3, \ldots)\). The various proposed pumping models agree in identifying the inversion mechanism: line trapping in the rovibrational transitions \((v \rightarrow v-1)\), which decreases the original radiative probabilities to efficiency probabilities that are relatively lower for higher-\(J\) levels; see e.g. Bujarrabal and Nguyen-Q-Rieu [14], Lockett and Elitzur [92], Gray et al. [50]. This leads to a systematic overpopulation of levels with relatively high \(J\)-values and to the inversion of the \(J \rightarrow J-1\) transitions in the \(v > 0\) states, which is particularly efficient for lower frequency lines. What is not yet well known is the source of the energy, i.e. the way in which we excite molecules from the ground \(v=0\) state, which can be collisional or radiative [68] [12]. The issue is important, because the relationship between the physical conditions for the maser emission must depend on the pumping mechanism. If we wish to probe the physical conditions based on the observed radiation we must understand how the former generates the latter. Radiative pumping tends to discriminate more clearly the conditions required for the pumping of the different \(v\)-states. The fact that the maser spots of the \(v=1\) and \(v=2\) \(J=1\rightarrow0\) lines tend to form clusters that are similar for both lines (the ring radius being slightly smaller for the \(v=2\) line) has been argued to favour collisional pumping [107] [24] [138] [75] etc. The \(J=1\rightarrow0\) masers are intense and their frequencies, around 43-GHz \((\lambda = 7 \text{ mm})\), are easily reachable at present in VLBI, therefore, they are the best observed SiO masers. However, high-resolution (<mas) observations have shown that, curiously, the spots of the two lines are practically never coincident, which is interpreted as supporting radiative pumping (Fig. 6). Of course, such a comparison is hampered by the often poor bona-fide astrometry in VLBI experiments at 7mm wavelength. Of those listed above only Rioja et al. [138] and Kamohara et al. [75] were phase referenced, and both observed with VERA. At higher frequencies (higher-\(J\)-values), conventional VLBI phase referencing experiments are more difficult and astrometry is still not yet possible (although we note that a significant number of four-band KVN observations, albeit
Figure 6: Observations of SiO $J=1-0$ $v=1$ (greys) and $v=2$ (contours) in IRC+10011, [Fig. 9[14]]. Note that both lines occupy similar regions but that, in fact, the spots are never coincident, in spite of the uncertain relative astrometry.
These new observations seem in clear contradiction with all the simple pumping models. Needless to say, the other hand, the overpopulation of sources. Therefore, the absorption of this radiation by SiO leads to an underpopulation of distributions to that for \( v = 1 \) and 2 and always with very rare coincidences at the smallest scale. On the other hand, the \( v=1 \) \( J=2 \) – 1 maser, which theoretically shares the same pumping mechanism and excitation requirements as \( v=1 \) \( J=1 \) – 0, appears in clearly different regions and at further distances than the 7mm lines. These new observations seem in clear contradiction with all the simple pumping models. Needless to say, the \( v=3 \) \( J=1 \) – 0 maser is weaker than the \( v=1,2 \) \( J=1 \) – 0 ones and the \( v=1 \) \( J=2 \) – 1 line frequency, 86-GHz, is hard to observe in VLBI, therefore, astrometry in such observations has hitherto been impossible.

A possible solution to the puzzle is the presence of line overlap. Photons emitted by a rovibrational transition of \( \text{H}_2\text{O}, p_2=1 \ 11_{6,6} – v=0 \ 12_{7,5}, \) can be absorbed by the \( v=1 \) \( J=0 \) – \( v=2 \) \( J=1 \) component, because both frequencies are almost exactly the same. \[117\] \[146\]. It can be shown that \( \text{H}_2\text{O} \) often emits strongly at that frequency in our sources. Therefore, the absorption of this radiation by SiO leads to an underpopulation of \( v=1 \) \( J=0 \) and an overpopulation of \( v=2 \) \( J=1 \) line, quenching the (otherwise expected to be intense) \( v=2 \) \( J=2 \) – 1, which is known to be anomalously weak; in fact the effects of overlap were first invoked to explain this observational fact. At the same time, this phenomenon introduces a strong over-excitation of the two 7mm masers, \( v=1,2 \) \( J=1 \) – 0, whose excitations are now strongly coupled. Calculations show that the excitation conditions of both lines are now very similar and also similar to those of the \( v=3 \) \( J=1 \) – 0 line \[69\] \[25\]. Meanwhile, \( v=2 \) \( J=2 \) – 1 now appears to require different conditions, in particular lower densities that should appear at larger distances from the star. Radiative models including line overlap can explain, at least qualitatively, all the observational results. This is not the only possible explanation; an alternative could be non-monotonic temperature gradients, e.g. due to shocks or dust formation \[133\]. However, we stress the scarcity of available data with high sensitivity and with any meaningful astrometric registration, particularly at high frequencies. We do not yet have accurate and systematic information on the relative distributions of these lines, for which not only do we need good absolute astrometry but we would also need to recover (almost) all the maser flux, to better understand the complete brightness distribution. In particular, we lack VLBI data of lines at higher frequencies, necessary to be sure that line overlap is the main (or unique) major modification of the basic pumping mechanisms.

3.1.3. Maser lines in proto-PNe

As soon as the star+nebula system leaves the AGB phase, the observation of the masers associated with them becomes more and more difficult. The reason is that the inner circumstellar masers are becoming more and more diffuse at the same time as the mass-loss rate decreases. SiO masers are very rarely observed. There is however a paradigmatic example showing both SiO and \( \text{H}_2\text{O} \) masers: the strongly bipolar nebula \( \text{OH} \) 231.8+4.2, the Calabash Nebula.

The evolution from the AGB to the PN phase is as spectacular as it is rapid. It is thought that the strong axial symmetry typical of post-AGB nebulae is due to the ejection, during the first protoPN phases, of very fast and collimated stellar jets. These jets shock the fossil slow-moving AGB envelope, generating a series of axial shocks that cross the massive CSE, inducing high axial velocities in it [see e.g., \[7\] \[13\]]. The very large amounts of energy and momentum observed in young PNe impose severe limitations on the jet launching mechanism. At present, the only way to explain the origin of such energetic flows is to assume that a fraction of the ejected CSE is reaccreted by the central star or a companion through a rapidly rotating disk \[144\] \[40\]. The jet would then be powered by a magnetocentrifugal launching process, similar to that at work in forming stars. For that to be efficient, the presence of a stellar companion (or at least a massive planet) is necessary, since otherwise the circumstellar material lacks the angular momentum to form an accretion disk. \( \text{OH} \) 231.8+4.2 is strongly bipolar, shows a very fast and massive bipolar outflow, and is known to harbor a binary star in its center. It is therefore a textbook candidate to study these crucial phenomena.
Figure 7: Observations of SiO and H$_2$O masers in OH 231.8+4.2, compared with the optical image. The uncertainty in the SiO maser position is about 200 mas, too large to definitively determine its relationship with the H$_2$O clumps. From Desmurs et al. [23], Fig. 1]
VLBI observations of SiO and H$_2$O masers have yielded very promising results (see Sánchez Contreras et al. [141], Desmurs et al. [23], and Fig. [7]). Water vapor emission comes from two regions in opposite directions along the nebula axis and their velocity field is fully compatible with the general velocity field in that direction, suggesting that the H$_2$O clumps represent the inner nebula, at the base of the bipolar flow. SiO masers occupy smaller regions and are placed almost exactly perpendicular to the axis. The movements depicted by the observations of SiO are compatible with a disk orbiting the central star(s). In principle, we are seeing in this object the whole central structure of disk plus outflow that we would like to see to confirm our ideas on the post-AGB nebular dynamics, which has not been observed to date in other sources. But the relative astrometry is poor and we are not sure that really the SiO structure is placed at the center of the nebula, between the two H$_2$O clusters. The problem is then serious, as we lack this crucial datum to draw definitive conclusions on the disk/outflow association. For the last 10 years we have been trying to improve the astrometry, but, up to now, the best SiO maser position obtained is uncertain by about 200 mas, completely insufficient for our purposes. Furthermore the SiO masers in this source have been fading over the past several years, so new VLBI measurements are more and more difficult. The VLBI data on OH 231.8+4.2 constitute a self-explanatory example of the effects of the lack of accurate and sensitive VLBI data in our studies of the inner post-AGB nebulae. We note that SFPR observations of this source with the KVN have recently been performed, and appear promising [29].

3.1.4. Summary: Evolved Stars

We have seen how important the VLBI observations of various maser lines are in the study of the most interesting layers of nebulae around AGB stars: the inner regions in which the dynamics are still active and the relevant phenomena to understand these evolutionary phases are actually taking place. In AGB stars, they harbor the grain formation and gas+dust acceleration layers; in post-AGB objects, this inner nebula includes the outflow acceleration regions and may hold the key to understanding the formation and shaping of PNe. In both cases, however, the existing VLBI data are still insufficient to address these problems, because of the lack of systematic observations with accurate astrometry and high sensitivity. Good VLBI data are also necessary to understand the SiO maser mechanism, which is still under debate.

Accurate astrometry is still difficult at 7mm. At higher frequencies, VLBI experiments are very difficult and conventional astrometry is almost impossible. In all cases, sensitivity limitations are significant and an important fraction of the total flux is lost in the interferometric process. Thanks to phase transfer between the SiO lines and from 22-GHz (where the frequency ratios are close to integer), sensitive multifrequency observations will strongly help to map several transitions, out to the sub-mm regime. They will also help to systematically obtain good relative astrometry for the different transitions.

3.2. Massive Star Formation

3.2.1. Introduction

The formation of isolated low-mass (M ~ 1 M$_\odot$) stars is now understood quite well. It proceeds through (i) mass accretion onto the protostar through a Keplerian disk, an expected result of angular momentum conservation, and (ii) ejection of material via a jet collimated along the disk axis, which removes angular momentum from the disk allowing matter to accrete onto the star. Jets are generally modeled as magneto-centrifugally driven winds, powered by the rotation and gravitational energy and channeled along the magnetic field lines either from the disk inner edge ["X-wind", [63], or across a much larger (up to 100 AU) portion of the disk ["Disk-Wind", [128].

The formation of more massive stars might require substantially different accretion/ejection processes. For the mass accretion rates predicted by theory [e.g. [143], the accretion time becomes longer than the protostar contraction time for masses $\geq$8 M$_\odot$. At this point, the star reaches the Zero Age Main Sequence (ZAMS) and, as a consequence, its radiation pressure would be sufficient to halt the inflow [159], thus preventing further increase of the stellar mass. A number of scenarios have been put forward to solve this “radiation pressure” problem for high-mass star formation: much higher mass accretion rates, competitive accretion [10] and/or stellar mergers [11] in clusters.

However, recent 3-D, radiative hydrodynamic simulations of high-mass star formation (SF) seem to indicate that accretion disks and collimated outflows could also be an effective mechanism for assembling very massive
stars, up to $\approx 140 \, M_\odot$ [e.g. 83]. The disk geometry focuses the accretion flow onto the equatorial plane, allowing the accreting material to overcome the strong radiation pressure and reach the stellar surface. These models also predict beaming of the stellar photons into the lower-density outflow cavity, which helps to alleviate the radiation pressure in the equatorial plane. The size of accretion disks around high-mass YSOs is predicted to be on the order of only a few 100 AU, whereas clustering of multiple forming stars should occur on scales of $10^3$ AU [e.g. 82].

From the above it is clear that to improve our understanding of the accretion and ejection processes in high-mass YSOs, it is essential to image linear scales as small as 10–100 AU (requiring angular resolutions <0.1 at the typical distances > 1 kpc of massive star forming regions) to resolve the gas kinematics around single objects. To this purpose very useful diagnostic tools are the intense molecular (in particular SiO, H$_2$O, and CH$_3$OH) masers often observed in proximity to high-mass YSOs. Thanks to their high brightness temperature ($\geq 10^9$ K), molecular masers can be targets of VLBI observations, which, achieving sub-milliarcsec angular resolutions, permit us to derive the proper motions of the maser “spots” (i.e., the single maser emission centers) and access the full 3-D gas kinematics. However for exact reconstruction of the kinematics the different observations have to be astrometrically registered. The only way to register mm-VLBI reliably is with the SFPR method, and the best observing efficiency for SFPR is provided with simultaneous mm-VLBI receiver systems [137]. Combining maser VLBI data with (sub-arcsecond) interferometric observations of thermal (continuum and line) emissions, one can get a very detailed view of the gas kinematics and physical conditions near the forming star. Such a study has been performed so far only towards a small number of objects [see discussion in 110]. In the following we illustrate one of the most remarkable results of maser VLBI applied to high-mass SF.

### 3.2.2. Source I in Orion BN/KL

The closest (415 pc) and best studied high-mass YSO is Source I in the Orion BN/KL region. The continuum emission of Source I, imaged at 7 mm with the JVLA by [130], is highly elongated and consistent with an accretion disk ionised by a YSO of $\approx 10 \, M_\odot$. This source has been monitored by [99] with the Very Long Baseline Array (VLBA) in vibrationally-excited SiO maser transitions every month for over three years, and a movie of the 3-D molecular gas flow was created. The SiO masers are distributed symmetrically around the ionised disk, outlining four radial arms connected by two tangential bridges. The pattern of SiO maser proper motions shows that material in the bridges rotates about the disk axis, whereas gas in the arms stream radially away from the star. Thus, the vibrationally-excited SiO masers are tracing both a compact rotating disk and a wide-angle wind emanating from the disk at radii $< 100$ AU (Fig. 8, right panel), which can be modeled in terms of a magnetocentrifugally driven wind [154]. JVLA imaging of ground-state SiO maser transitions, probing larger scales, shows that the wide-angle wind collimates into a bipolar outflow at radii of 100–1000 AU (Fig. 8, left panel) [57]. This study has provided direct evidence for the formation of a massive star via disk-mediated accretion and revealed for the first time the launch and collimation region of an outflow from a rotating compact disk on scales comparable with the Solar system. SiO masers are ideal candidates for SFPR astrometric registration, as the frequency ratio between the transitions is extremely close to integer.

### 3.2.3. Advantages of multi-frequency maser observations

High-frequency, single-dish studies have shown that the commonly observed, centimeter wavelength, masing molecules emit many masing transitions at millimeter wavelengths, too. For instance, for methanol, 16 distinct maser transitions have been detected over the frequency range 6–240 GHz [see, for instance, 34], and for water, the 16 (as of 2016, Gray et al. [55, Tab. 6]) maser lines cover the frequency range 22–660 GHz [see, for instance, 112]. These “millimeter wavelength” masers open up new perspectives for star-formation studies as, in general, for a given molecule, models of maser pumping predict that transitions at different frequencies are strongly inverted and become intense masers under varying physical and chemical conditions (described, in particular, in terms of $(n_{H_2})$ density, gas and dust temperature, molecular abundance; see, for instance, Neufeld and Melnick [111], for water, and Cragg et al. [19], for methanol masers). As an example, Fig. 9 shows the dependence of the brightness temperature of four different methanol masers on various physical parameters, as predicted by the models of Cragg et al. [19]. The intensity ratios of different maser transitions from the same molecule can thus be used to probe the physical and chemical conditions of the gas, as long as the observations are sufficiently well registered.
Figure 8: Maser kinematics in Source I. **Left Panel** Top: SiO $v=0$ and H$_2$O masers (open circles and squares, respectively – [Fig. 3][357]), velocity-integrated SiO $v=1$ masers (red contours – [17]), and 7 mm continuum (black contours – [130]), as mapped with the JVLA. Middle: expanded view of SiO $v=0$ maser proper motions in the northeastern lobe of Source I. Bottom: expanded view of the southwest lobe. Colors denote maser $V_{\text{LSR}}$ as indicated in the wedge on the bottom left corner of the bottom panel. **Right Panel** Combined (velocity-integrated) SiO $v=1$ and $v=2$ maser emission distribution (red-tone image) observed with the VLBA [Fig. 5][99], and 7 mm continuum (color map) imaged with the JVLA [130].
to ensure that the measurements arise from the same emission regions. The precision with which the physical parameters of the gas can be determined with this method clearly increases with the number of observed maser transitions. To this purpose the role of the newly-detected millimeter wavelength masers will be fundamental, as will the precision alignment of the observations in different wave bands. VLBI observations of maser emissions over an extended frequency range could in principle allow us to map the density and temperature of the gas surrounding the high-mass YSO with milliarcsecond accuracy. Whilst these observations hitherto have not been observed simultaneously, given that we can now register different transitions together using the SFPR method, such capabilities would greatly enhance the scientific return from the observations. The basic assumption of the maser models, which can be observationally verified, is that the various maser lines are effectively emerging from the same volume of gas. If applied to a large enough sample of sources, multi-frequency maser VLBI, by constraining in a consistent way the physical conditions and kinematics of the gas (see below) in the proximity of (within 10–100 AU from) the high-mass YSOs, will be very useful to track the evolutionary phase of the high-mass YSOs, which is presently poorly determined owing to insufficient angular resolution and/or ambiguous interpretation of the observables.

3.2.4. Prospects for the Future

Maser VLBI offers a unique tool to investigate high-mass SF at the smallest (∼10 AU) scales, unaccessible even to the new generation of millimeter interferometers. In the few objects studied so far using both maser VLBI and thermal interferometric observations, the maser 3-D kinematics and the $V_{\text{LSR}}$ distribution of the (thermal) tracers of high-density gas complement each other, providing a picture of the gas motion around the forming star at radii from 10 to $10^4$ AU. The results obtained seem to indicate that disks and jets could play an important role in the formation of more massive stars, as well. However, maser VLBI reveals also some new interesting kinematic features, whose significance for the stellar formation process has still to be deciphered.

In the case of maser emission, owing to the constraints imposed by the maser pumping, one can expect that a particular region of gas around the YSO offers the most suitable conditions for producing maser action in different lines (from the same molecule). In general, this expectation has been mostly confirmed by previous multi-line VLBI observations, but recent interferometric studies have also demonstrated that maser lines of very different excitation can effectively be used to trace different physical conditions, Gray et al. [e.g. discussions in 55], which predicts 50 further H$_2$O maser transitions which will fall in the ALMA bands. As an example, [64] have recently performed ALMA observations of two millimeter, water lines, the 321 GHz (1862 K above the ground state) and the 336 GHz (at 2956 K) lines, towards Source I in Orion KL. While the spatial and velocity distribution of the 321 GHz emission is elongated and traces the root of the outflow close to the surface of the accretion disk, the 336 GHz line has a compact structure and is most likely emerging from hot (∼3000 K) neutral material orbiting the YSO in an edge-on small (radius of 50 AU) ring. Therefore, VLBI observations of different maser lines from the same YSO could turn to be even more strategic for kinematic studies, if the spatial associations are registered, to determine the physical parameters of the gas.

4. Time domain observations of X-ray binary jets

Black hole X-ray binaries (BH XRBs) show much of the same physics as observed in AGN, exhibiting relativistic jets powered by an accretion flow. However, while they are typically factors of $10^2$–$10^5$ times closer than nearby AGN, their black hole masses are $10^5$–$10^8$ times smaller. This implies that the physical size scales that we can probe with high-frequency VLBI correspond to a larger number of gravitational radii in BH XRBs than in AGN. Nonetheless, since timescales close to a black hole scale with mass, BH XRBs afford us the unique advantage of studying the physical processes of jet launching and evolution in real time.

In the current phenomenological picture describing XRB outbursts [36], compact, steady jets are seen in the hard X-ray spectral state at the beginning and end of an outburst. Such compact jets have size scales of a few AU, and have been directly resolved along the jet axis in two systems, using VLBI [26, 147]. While these compact jets are believed to have a relatively low Lorentz factor ($\Gamma < 2$), $this$ $has$ $never$ $been$ $directly$ $measured$ $on$ $VLBI$ $scales$ $via$ $the$ $relative$ $proper$ $motions$ $of$ $approaching$ $and$ $receding$ $jet$ $components$. The detection of a counterjet in GRS 1915+105 was used to suggest a compact jet speed to 0.3–0.5$c via the jet/counterjet brightness ratio.
Figure 9: Effect of parameter (gas and dust temperature, gas and specific column density) variations on the brightness temperature of four different methanol masers. The four curves are labelled with the frequency of the maser transition to which they refer: 6.6, 12.1, 23.1 and 107 GHz (reproduced from Fig. 2 in Cragg et al. [19]).
but the variations between different frequencies and epochs, coupled with the uncertainty in both the jet structure (discrete or continuous flow) and the distance and inclination angle of the source makes it hard to draw definitive conclusions on the true Lorentz factor.

At the peak of the outburst, there is a transition to a softer X-ray spectral state, upon which discrete, transient ejecta are launched. These are much brighter than the compact jets, and move away from the central source with proper motions of up to tens of milliarcseconds per day, in some cases showing apparent superluminal motion [e.g. 105, 153]. While the proper motions of the ejecta can be used to place constraints on fundamental jet parameters such as speed, inclination angle, and the associated Lorentz and Doppler factors [e.g. 106, the typical large uncertainties in source distance imply that we can only place lower limits on the true Lorentz factors 35]. VLBI studies of these transient ejecta are complicated by the strong changes in jet flux density and morphology over the course of an observing run, which violate the fundamental assumptions of aperture synthesis. Such issues become a particular problem at mm-wavelengths, where the amplitude variability is stronger and the angular resolution is higher. However, for typical BH XRBs the jet structure is relatively simple, being made up of a few unresolved components. Thus, an observation can be broken up into multiple smaller chunks, which do not individually violate the key tenets of interferometry, and can be imaged and analysed separately [e.g. 26]. Alternatively, high time resolution photometry at multiple radio frequencies can be used to glean some information on the jet structure. The characteristic variability timescale at any given frequency provides a measure of the jet size scale at the surface where the optical depth is unity at that frequency (i.e. the radius of the jets). As an example, Miller-Jones et al. 103 used the minimum variability timescale seen in simultaneous 15 and 43-GHz JVLA observations of Cygnus X-3 to determine the characteristic size of the jets during a period of minor flaring, probing scales of 2–4 AU — significantly smaller than that which can be resolved with VLBI.

The combination of both a resolved radio jet and sensitive, high time-resolution photometry at multiple radio frequencies, together with simultaneous X-ray observations, can provide an enhanced and unique probe of the structure and geometry of BH XRB jets. As the X-ray variability from the accretion flow propagates downstream in the jet, we can observe it being manifested in the jet. Since we see emission from the surface of optical depth unity at any given frequency, this is seen first at optical/infrared frequencies from closest to the jet base, and moves to lower frequency with time as the fluctuations propagate downstream. This has already been demonstrated via correlations between optical/infrared and X-ray variability [17, 74], but not to date in the mm or radio bands. With simultaneous, high-sensitivity observations at multiple mm wavelengths (where the variations are stronger and less smoothed out than in the cm band), we can determine the time delay between frequencies as a perturbation propagates downstream. If the characteristic height along the jet is also known from the VLBI observations, along with the exact launch time from simultaneous X-ray observations, these then give a direct measure of the jet speed. Together with constraints on the jet radius from the characteristic variability timescales at the different frequencies, we can also probe the jet geometry, in particular the opening angle, which is typically unknown in BH XRBs 102. Thus, simultaneous observations at multiple mm bands can provide one of the few feasible means for directly measuring the jet speed and geometry.

We have started trials of this VLBI+multi-band photometry technique using observations of bright transient ejection events from the 2015 outburst of the BH XRB V404 Cyg [Miller-Jones et al., in prep, 150]. The combination of VLBI imaging and Markov chain Monte Carlo modeling of our multi-frequency light curves (Fig. 10) is providing a powerful probe of the geometry, speed, structure, and energetics of the discrete ejecta that were launched during these flaring events. This technique will subsequently be extended to the compact jets seen in sufficiently bright BH XRB outbursts. However, the existing observations have required a combination of the JVLA in sub-array mode to provide the multi-frequency photometry, and the VLBA to provide the imaging. The adoption of a simultaneous multi-wavelength mm-VLBI capability would enable such observations on a single instrument, thereby removing both the double-jeopardy and logistical complications involved in scheduling strictly-simultaneous observations on two different facilities. Clearly this combination of high-resolution spatial and time domain analysis will benefit immeasurably from observations with continuous, contemporaneous mm-wave systems such as that provided by the KVN, once the capability is extended to longer and more sensitive global baselines.
Figure 10: Simultaneous multi-frequency light curves of the 2015 outburst of the BH XRB V404 Cygni, taken using the SMA, JCMT, and the JVLA operating in sub-array mode [150]. Rapid variability corresponding to the ejection, expansion and fading of multiple jet knots (directly imaged at 2 cm with the VLBA; Miller-Jones et al. in prep.) is observed. The higher-frequency light curves peak earlier, at higher flux densities, and are less smoothed out than their counterparts at lower frequencies. This trend continues from the radio bands all the way up to the sub-mm bands, as evidenced by the JCMT observations at frequencies as high as 666 GHz [figure taken from 150].
5. Concluding Remarks

We have presented a few highlights of the science cases which would be advanced by the wide-spread adoption of recording systems capable of allowing simultaneous mm-wavelength VLBI. These are summarised in Table 3.

The science goals cover a range of spectral line and continuum VLBI science, such as AGN polarimetric studies, and alignment of maser transitions to probe different physical conditions around massive star forming regions and AGB stars. Registration between the different frequencies is essential for the scientific interpretation in these fields. New methods and technologies have allowed for registration of the mm-wavelengths. Similarly, time-sensitive observations of multiple frequencies in, for example, X-ray binaries are best delivered by systems capable of observing a wide range of frequencies simultaneously. There are a multitude of possible technological solutions that could deliver these capabilities, and these were explored in the ERATec meeting, October 2015 [8]. VLBA style fast switching has been demonstrated successfully for VLBI, but has significant observational overheads and is very unlikely to succeed at frequencies greater than 86GHz. KVN style receivers are large but have much reduced overheads and have worked at all KVN frequencies (i.e. up to 130GHz). However, a compact three-band single-Dewar receiver has recently been developed, which would be compatible with most single frequency receiver slots. Sub-arraying solutions are being investigated at the ATCA. These have demonstrated FPT and are expected to successfully demonstrate SFPR shortly, once the polarisation issues are resolved. Both ALMA and JVLA also can support sub-arraying modes. Other solutions are possible, for example there were exciting reports on innovative meta-material solutions in the ERATec meeting.

The cases presented in this paper represent the benefits that will accrue to existing scientific projects. The outcome of new technologies is always that they enable new measurements and open new scientific applications, so those listed here will only be a small subset of the expected fields of study.

| Science Case (section) | Domain | Requirements |
|------------------------|--------|--------------|
| Weak Sources (2.1)     | Continuum VLBI | mm-band phase stabilisation |
| Spatial Astrometry (2.2) | VLBI | mm-band phase referencing |
| Faraday Rotation Studies & Spectral Index (2.3 & 2.4) | Continuum VLBI | mm-band frequency references |
| Alignment of Maser transitions (3.1 & 3.2) & Evolved Star regions | Line VLBI for Star-forming regions | mm-band frequency phase referencing |
| X-ray Binaries (4)     | Temporal studies | Simultaneous mm-band observing |

Table 3: Summary table for the science goals described in this review, along with the research domain which is relevant and the instrumental requirements for delivery of such capability.

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