A practical design procedure for initial sizing of heaving point absorber wave energy converters

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Abstract. Designing a wave energy converter with the proper size has always been challenging since it is a trade-off between many factors including cost, practicality, and energy output. In this paper a practical design procedure for sizing of heaving point absorbers wave energy converters is presented. Size can be represented by the body volume. Budal power bounds are deployed to obtain the body volume and annual mean absorbed power of the wave energy converter. Budal power bounds are determined for each sea state. Aiming at a specific power capture ratio, several sets of design sea states with related design volume and annual mean absorbed power are defined. With the design objective of maximizing the ratio of mean power to submerged volume, and considering suitable design constraints, the best size is obtained. The proposed procedure will be then deployed for a case study and the design will be compared with an existing similar point absorber. The results show that the mean absorbed power does not depend on the size but is a function of selected sea states. Furthermore, the comparison study reveals that the proposed design procedure yields reasonable power characteristics.

1. Introduction and background
One of the main considerations in designing wave energy converters is determining their size. A wave energy converter (WEC) should be sized to fulfill the power requirements. The design should be practical; in other words, very small or very large bodies are not practical. There have been several works on the size and geometry study of WECs in the literature; most of which are on size comparison or size optimization. In some early studies by Kan [1], Haren and Mei [2] and Thomas and Gallagher [3], geometry and size were studied with respect to the power maximization attitude. In more advanced works by Babarit et al. [4], multi objective optimization study was conducted to maximize the power and minimize the total mass. McCabe et al. [5] also optimized the shape of the WEC with the objectives including power, submerged volume, and velocity. It is reported by Bachynski et al. [6] that the idealized power take-off damping increases with the increase in the size of WEC. With the main objective of finding the best location for utilizing the point absorbers, Khojasteh et al. [7] studied the effects of the buoy draft and diameter to determine the maximum power absorption and concluded that the buoy diameter has a significant effect on the captured power while the power absorption was smaller for larger drafts. More importantly, the absorbed power depends highly to the significant wave height. Similarly, Shadman et al. [8] proposed a methodology for the geometrical optimization of heaving point absorbers. They considered the diameter and draft of the buoy as geometrical parameters to be determined in order to achieve a maximized combination of the absorbed power and the resonance bandwidth of the buoy. A preliminary design of point absorbers by using a parametric optimization study aiming to capture the
maximum energy in a target area was proposed by Erselcana İ Ö and Küükner A [9]. They considered a broad range of design variables and commented on the performance of WECs with different floated shapes. They also mentioned that increasing the floater mass has a trivial effect on the energy capture.

Knowing the optimized body size and geometry is useful, but one important issue is missing in the above-mentioned references which is that it is essential to know how the WEC’s size for specific power purposes can be determined. In a study on developing heaving point absorbers that maximize the power output, Falnes et al. [10] drew a promising conclusion that the capacity of the power take-off (PTO) system, and the maximum volume should be limited. They assumed that a commercially practical WEC should work at least one-third of the year with full capacity, derived the corresponding maximum power and used that to size the WEC. This in general leads to a lower specific power level which in turn calls for a smaller WEC volume. Furthermore, they stated that instead of having a very large power buoy, a reasonable wave-power plant should be made of an array of many small power units. They applied the Budal diagrams [11] and investigated the power output with respect to the WEC’s volume and suggested that the parameters of the WEC should be matched with the wave climate. A more detailed investigation of the arrays of point absorbers was conducted by Murai et al. [12]. They derived optimal control force parameters to maximize power generation of multi point-absorber arrays, studied different arrangements of the arrays, and concluded that the optimized array arrangement increases the power generation efficiencies by 15%.

Despite several valuable research on the size of WECs, there is yet a need for a design procedure on sizing that can be conveniently applied for initial sizing purposes. This will be proposed in this paper. In the proposed method, Budal upper bounds are implemented to characterize the absorbed power to provide a practical initial sizing of heaving point absorbers. In this paper, first, the sizing procedure is presented in Section 2. along with the implemented methods. Second, to have a better understanding of the sizing procedure, it is performed on a case study of point absorbers in a specific sea site and sea states which is introduced in Section 3. Third, the results are presented, compared with an existing similar point absorber, and discussed in Section 4. Lastly, conclusions are given in Section 5.

2. Theory and methodology

2.1. Assumptions
The following assumptions are made:

- It is assumed that the design wave height ($H_{\text{design}}$) and design wave period ($T_{\text{design}}$) are equal to significant wave height ($H_s$) and spectral peak period ($T_p$), respectively. This is because for a given sea state, $H_s$ is an indication of the wave energy and $T_p$ is the wave period of the most energetic waves in the total wave spectrum.
- Only the left-hand Budal curve is considered for power calculation (Section 2.4. ). With a fixed design volume, the power is only a function of wave height and period which are equal or less than the $H_{\text{design}}$ and $T_{\text{design}}$, hence the power follows the left hand Budal curve.
- The intersection of the left-hand Budal curve and right-hand curve is used to calculate the volume (Section 2.4. 2.5. 2.5. ).
- The PTO system is ideal, i.e., the wave energy absorbed will follow the upper limits of the Budal diagram.

2.2. The design procedure
The design workflow is summarized in Figure 1.
The design procedure consists of the following steps:

a) First, the power capture ratio is determined. This is the percentage of the sea power that the WEC is designed to capture and defines the sea states domain or target sea states (Section 2.3).

b) From the sea states, sets of $H_{\text{design}}$ and $T_{\text{design}}$ corresponding to the determined power capture ratio are determined.

c) For each set of $H_{\text{design}}$ and $T_{\text{design}}$, the design submerged volume ($V_{\text{sub}}$) is calculated.

d) The ratio of annual mean absorbed power to the submerged volume ($P_{\text{mean}}/V_{\text{sub}}$) is calculated for each set.

e) The maximum $P_{\text{mean}}/V_{\text{sub}}$ is obtained.

f) If the volume corresponding to this maximum ratio of $P_{\text{mean}}/V_{\text{sub}}$ is practical, the initial sizing is obtained. Otherwise, the next maximum ratio should be investigated until a practical size is found.

g) If none of the investigated cases result in a practical volume then the capture ratio should be modified to a lower percentage.

2.3. Power capture ratio

The power capture ratio determines the sea states to which the WEC is designed to function and is defined as follows:

\[
\text{capture ratio} = P\left( T_{p,\text{min}} < t < T_{p,\text{max}}, H_{s,\text{min}} < h < H_{s,\text{max}} \right)
\]  

where $T_{p,\text{min}}$ and $T_{p,\text{max}}$ are respectively the minimum and maximum wave periods and $H_{s,\text{min}}$ and $H_{s,\text{max}}$ are respectively the minimum and maximum wave heights corresponding to any point on the capture ratio plot. Sum of the probabilities of sea states within these limits is equal to the capture ratio. Equation (1) is visually represented as a box on the scatter diagram as presented in Figure 2.
Figure 2. A schematic capture ratio plot and its corresponding sea states and probabilities.

2.4. Budal power upper bounds

The power and volume calculations in this study are based on Budal power bounds [13]. With an incident plane wave with the wave-power level $J$ and wavelength $\lambda$, the left upper bound for the absorbed wave power for the heaving axisymmetric body in deep water will be defined as:

$$P < P_A \equiv c_A H^2 T^3$$

(2)

where $T$ and $H$ are wave period and wave height, respectively.

This upper bound does not depend on the size but depends on the body’s shape and oscillation mode. The right upper bound to the power that can be absorbed by an immersed body oscillating in heave with the volume, $V$, can be defined as:

$$P < P_B \equiv c_B \frac{VH}{T}$$

(3)

These upper bounds are shown in Figure 3. The left-hand upper bound $P_A$ is size-independent and the right-hand upper bound $P_B$ is a function of body volume. However, both upper bounds are functions of $H$ and $T$. 
2.5. The smallest required volume

Budal upper bounds are to be plotted for several sets of $H_{\text{design}}$ and $T_{\text{design}}$ along the capture ratio plot in Figure 2. Maximum absorbed power ($P_{\text{max}}$) is calculated by following the $P_A$ curve in Figure 3 and using equation (4).

$$ P_{\text{max},\text{design}} = c_A H_{\text{design}}^2 T_{\text{design}}^3 $$ (4)

In practice, $P_{\text{max}}$ is lower than the intersection-point power ($P_C$) due to the PTO system limitations. The $P_{\text{max}}/P_C$ ratio is varied for different control strategies [14]. Therefore, the power curve and consequently the WEC’s submerged volume should be calculated according to the applied PTO system. However, as mentioned earlier, this limitation is neglected in the present study and the PTO system is considered to be ideal.

For each set of $H_{\text{design}}$ and $T_{\text{design}}$, and by setting $T = T_C = T_{\text{design}}$, the WEC’s submerged volume can be determined:

$$ V_{\text{sub},\text{design}} = \frac{c_A H_{\text{design}} T_{\text{design}}^4}{c_B} $$ (5)

As well as the submerged volume, the annual mean absorbed power ($P_{\text{mean}}$) and the ratio of mean power to the submerged volume ($P_{\text{mean}}/V_{\text{sub}}$) are to be calculated. The calculation of $P_{\text{mean}}$ is explained in Section 2.6.

2.6. Mean absorbed power

Each set of $H_{\text{design}}$ and $T_{\text{design}}$ represents a sea states domain with $n$ subsets of $H_s$ and $T_p$ and their corresponding probabilities of occurrence. The sum of calculated mean power of all these subsets multiplied by their individual probabilities yields the $P_{\text{mean}}$ of that design set through equation (6).

$$ P_{\text{mean},\text{design}} = \sum_{i=1}^{n} P_{\text{mean},i} \times p_i $$ (6)

The $P_{\text{mean}}$ of each subset is calculated from the $P_A$ curve using equation (7).
where \( \tilde{T}_i \) is the mean wave period of each subset, which is estimated using equation (8) by assuming that the waves follow a JONSWAP spectrum with first and zeroth moment of \( m_0 \) and \( m_1 \), respectively. \( \tilde{H}_i \) is the mean wave height of each subset, which is estimated by equation (9) by applying the Rayleigh probability distribution to random wave heights.

\[
P_{\text{mean},i} = c_A \tilde{H}_i^2 \tilde{T}_i^3
\]  \hspace{1cm} (7)

\[
\bar{T}_i = \frac{m_{0,i}}{m_{4,i}}
\]  \hspace{1cm} (8)

\[
\bar{H}_i = \frac{\sqrt{8}}{\pi} H_{s,i}
\]  \hspace{1cm} (9)

### 2.7. Capture width ratio (CWR)

The CWR is used to measure the capture efficiency of the WEC and can be used for comparison purposes. It is calculated by using equation (10).

\[
CWR = \frac{C_W}{B}
\]  \hspace{1cm} (10)

where \( B \) is the characteristic dimension of the WEC and \( C_W \) is the capture width which is the ratio of mean absorbed power to the incident wave power resource \( P_W \) and is obtained by equation (11).

\[
C_W = \frac{P_{\text{mean}}}{P_W}
\]  \hspace{1cm} (11)

where \( P_W \) or the power per meter of wave front for a sinusoidal wave is calculated by equation (12).

\[
P_W = \frac{\rho_w g^2}{32\pi} H^2 T \approx 980 H^2 T \text{ (W m}^{-1}\text{)}
\]  \hspace{1cm} (12)

### 3. Case Study

The environmental conditions of the European Marine Energy Centre (EMEC) test site [15] for the small bottom-referenced heaving buoy (Bref-HB) form is used as the case study. The site is located on the Orkney Islands in Scotland and its scatter diagram is presented in Table 1.
### Table 1. Joint distribution scatter diagram of $H_s$ and $T_p$ of EMEC site [15].

| $H_s$ (m) | $T_p$ (s) | 4.9- | 6.3- | 7.7- | 9.1- | 10.5- | 11.9- | 13.3- | 14.7- | 16.1- | 17.5- | 18.9- | Marginal for $H_s$ |
|-----------|-----------|-----|-----|-----|-----|------|------|------|------|------|------|------|-------------------|
| 0.00-0.75 | 393       | 455 | 233 | 87  | 33  | 14   | 6    | 2    | 0    | 0    | 0    | 0    | 119               |
| 0.75-1.25  | 408       | 629 | 391 | 151 | 52  | 15   | 6    | 2    | 0    | 0    | 0    | 1223             |
| 1.25-1.75  | 200       | 508 | 448 | 174 | 62  | 20   | 7    | 1    | 0    | 0    | 0    | 1654             |
| 1.75-2.25  | 54        | 338 | 433 | 193 | 61  | 22   | 9    | 2    | 0    | 0    | 0    | 1420             |
| 2.25-2.75  | 7         | 151 | 339 | 244 | 61  | 19   | 10   | 3    | 1    | 0    | 0    | 1112             |
| 2.75-3.25  | 1         | 29  | 211 | 252 | 80  | 16   | 7    | 3    | 1    | 0    | 0    | 835              |
| 3.25-3.75  | 0         | 3   | 91  | 191 | 118 | 19   | 5    | 2    | 1    | 0    | 0    | 600              |
| 3.75-4.25  | 0         | 0   | 17  | 114 | 119 | 25   | 5    | 2    | 1    | 0    | 0    | 430              |
| 4.75-4.75  | 0         | 0   | 1   | 49  | 78  | 36   | 6    | 2    | 1    | 0    | 0    | 283              |
| 4.75-5.25  | 0         | 0   | 0   | 11  | 46  | 42   | 7    | 2    | 1    | 0    | 0    | 173              |
| 5.25-5.75  | 0         | 0   | 0   | 1   | 18  | 26   | 15   | 7    | 0    | 0    | 0    | 109              |
| 5.75-6.25  | 0         | 0   | 0   | 1   | 1   | 7    | 18   | 11   | 1    | 0    | 0    | 67               |
| 6.25-6.75  | 0         | 0   | 0   | 1   | 2   | 9    | 10   | 2    | 0    | 0    | 0    | 39               |
| 6.75-7.25  | 0         | 0   | 0   | 0   | 0   | 0    | 5    | 9    | 4    | 0    | 0    | 25               |
| 7.25-7.75  | 0         | 0   | 0   | 0   | 0   | 0    | 2    | 7    | 5    | 0    | 0    | 18               |
| 7.75-8.25  | 0         | 0   | 0   | 0   | 0   | 0    | 1    | 4    | 4    | 1    | 0    | 14               |
| 8.25-8.75  | 0         | 0   | 0   | 0   | 0   | 0    | 1    | 2    | 1    | 0    | 0    | 10               |
| 8.75-9.25  | 0         | 0   | 0   | 0   | 0   | 0    | 0    | 1    | 2    | 1    | 0    | 14               |
| 9.25-9.75  | 0         | 0   | 0   | 0   | 0   | 0    | 0    | 1    | 1    | 0    | 0    | 4                |
| 9.75-10.25 | 0         | 0   | 0   | 0   | 0   | 0    | 0    | 0    | 0    | 0    | 0    | 1                |

| Marginal for $T_p$ | 1063 | 2113 | 2164 | 1469 | 730 | 263 | 118 | 71 | 27 | 5 | 8023 |

### 4. Results and discussion

#### 4.1. Solved example

The $H_s-T_p$ plots corresponding to the 0.25 and 0.5 capture ratios are derived from the joint probability scatter diagram. Along each plot, 12 cases are selected for investigation. Figure 4 shows the 50 % capture plot as well as the case No. 3 and its corresponding probabilities.
Figure 4. Top: 50% capture plot of sea states (black curve). The shaded area shows the corresponding sea states rectangle for the Case 3. Bottom: joint probability diagram and the shaded probabilities corresponding to Case 3.

The design $V_{sub}$ and $P_{mean}$ are calculated for each case using equations (5) and (6), respectively. Note that the coefficients $c_A$ and $c_B$ for an axisymmetric body in heave mode are taken as $c_A = 245 W/m^2s^{-3}$ and $c_B = \sigma \rho g = \sigma \times 10055 W/m^3s$ where $\sigma = 1$ for periodic oscillation [14]. The ratio of $P_{mean}/V_{sub}$ can be calculated accordingly. The results are shown in Table 2. Moreover, Figure 5-Figure 7 show the changes of the $P_{mean}$ and the $P_{mean}/V_{sub}$ ratio with different design parameters.

Among the selected cases for 50% capture ratio, case number 6 ($H_{design}=2.5 m$, $T_{design} = 7.7 s$) has the highest $P_{mean}/V_{design}$ ratio equal to 0.103 kW/m³. The $V_{sub}$ for this case is 209 m³ and the $P_{mean}$ is 21.5 kW. For 25% capture ratio, the best case is number 9 ($H_{design}=2 m$, $T_{design} = 6.3 s$) with $P_{mean}/V_{sub}$ of 0.073 kW/m³, $V_{sub}$ of 76 m³, and $P_{mean}$ equal to 5.5 kW.
Table 2. Performance measures and characteristics of design sets

| Capture ratio (%) | Case No. | \( T_{\text{design}} \) (s) | \( H_{\text{design}} \) (m) | \( P_{\text{max}} \) (kW) | \( V_{\text{sub}} \) (m³) | \( P_{\text{mean}} \) (kW) | \( P_{\text{mean}}/V_{\text{sub}} \) (kW/m³) |
|-------------------|---------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| 50                | 1       | 18.2                        | 1.4                         | 2887                        | 3737                        | 14.0                        | 0.004                       |
|                   | 2       | 14.0                        | 1.4                         | 1320                        | 1311                        | 13.9                        | 0.011                       |
|                   | 3       | 11.2                        | 1.4                         | 699                         | 546                         | 13.2                        | 0.024                       |
|                   | 4       | 8.4                         | 1.7                         | 424                         | 207                         | 16.8                        | 0.081                       |
|                   | 5       | 8.0                         | 2.0                         | 493                         | 195                         | 16.7                        | 0.086                       |
|                   | 6       | 7.7                         | 2.5                         | 687                         | 209                         | 21.5                        | 0.103                       |
|                   | 7       | 7.6                         | 3.0                         | 957                         | 240                         | 23.8                        | 0.099                       |
|                   | 8       | 7.5                         | 3.5                         | 1289                        | 276                         | 24.7                        | 0.089                       |
|                   | 9       | 7.5                         | 4.5                         | 2126                        | 354                         | 24.9                        | 0.070                       |
|                   | 10      | 7.5                         | 6.0                         | 3779                        | 472                         | 24.9                        | 0.053                       |
|                   | 11      | 7.5                         | 8.0                         | 6719                        | 630                         | 24.9                        | 0.040                       |
|                   | 12      | 7.5                         | 10.0                        | 10498                       | 787                         | 24.9                        | 0.032                       |
| 25                | 1       | 18.2                        | 0.7                         | 802                         | 1970                        | 2.8                         | 0.001                       |
|                   | 2       | 12.6                        | 0.7                         | 268                         | 454                         | 2.7                         | 0.006                       |
|                   | 3       | 11.2                        | 0.7                         | 192                         | 286                         | 2.6                         | 0.009                       |
|                   | 4       | 9.8                         | 0.8                         | 135                         | 172                         | 2.5                         | 0.015                       |
|                   | 5       | 8.4                         | 0.8                         | 99                          | 100                         | 2.3                         | 0.023                       |
|                   | 6       | 7.3                         | 1.0                         | 94                          | 68                          | 3.5                         | 0.051                       |
|                   | 7       | 7.0                         | 1.1                         | 99                          | 63                          | 2.4                         | 0.037                       |
|                   | 8       | 6.5                         | 1.5                         | 150                         | 65                          | 4.0                         | 0.062                       |
|                   | 9       | 6.3                         | 2.0                         | 244                         | 76                          | 5.5                         | 0.073                       |
|                   | 10      | 6.2                         | 2.5                         | 371                         | 92                          | 6.3                         | 0.069                       |
|                   | 11      | 6.2                         | 3.0                         | 532                         | 110                         | 6.5                         | 0.059                       |
|                   | 12      | 6.2                         | 10.0                        | 5910                        | 366                         | 6.5                         | 0.000                       |

Figure 5. The changes of the \( P_{\text{mean}} \) with wave parameters. Left: 50% capture ratio. Right: 25% capture ratio.
Figure 6. The changes of the $P_{\text{mean}}/V_{\text{sub}}$ with wave parameters. Left: 50% capture ratio. Right: 25% capture ratio.

Figure 7. Decreasing the $P_{\text{mean}}/V_{\text{sub}}$ ratio with increasing the size. Left: 50% capture ratio. Right: 25% capture ratio.

The results are compared with a similar WEC concept in the same site and sea states from Babarit et al. [16] and presented in Table 3. Comparison of the results of the present study with Babarit et al. [4]. It can be seen that the $P_{\text{mean}}$ in the present study is considerably higher than that of Babarit et al [4]. This is because the ideal PTO system is considered in the present study while a linear damping passive PTO is used in [4]. However, in [4] the $CWR$ and $P_{\text{mean}}/V_{\text{sub}}$ are much higher compared to the present study. It appears that Babarit et al. [4] aimed to capture the power from all possible sea states which is equivalent to 100% capture ratio. Achieving such capture ratio is not realistic due to the structural limitations of the WEC and PTO system. A more reasonable approach is to design the WEC such that it captures a portion of sea states as defined in this paper by 50% or 25% capture ratio.

Table 3. Comparison of the results of the present study with Babarit et al. [4].

| Study              | Capture ratio (%) | $C_W$ ($m$) | $CWR$ (%) | $P_{\text{mean}}$ (kW) | $P_{\text{mean}}/V_{\text{sub}}$ (kW/m$^3$) |
|--------------------|-------------------|-------------|-----------|------------------------|---------------------------------------------|
| Present            | 50                | 8.19        | 1.1       | 21.5                   | 0.103                                       |
| Present            | 25                | 8.52        | 1.6       | 5.5                    | 0.073                                       |
| Babarit et al. [4] | 100               | 12.6        | 4.2       | 2.8                    | 0.9894                                      |
4.2. Size paradox

One may have the misunderstanding that larger point absorbers have higher power outputs. The paradox is that the power from point absorbers is not a function of their size. It was mentioned before by Falnes [17] that “small is beautiful” and smaller efficient point absorbers were proposed later by Sjökvist et al. [18]. To illustrate this, three having point absorbers with cylindrical floaters of considerably different sizes are modelled in ANSYS AQWA. As seen from the simulations results in Figure 8, the time-averaged power of the reactive PTO is the same for these three cases.

\[ \bar{P}_{PTO,max} = \frac{|F|}{8 R_{diss}} \]  

(13)

As shown in Figure 9, as the size increases, both force amplitude and damping increase. The ratio of the squared force amplitude to the damping coefficient remains nearly the same as shown in Table 4.

**Figure 8.** Changes of time-averaged power with wave period.

**Figure 9.** Left: heave damping coefficient vs. wave period. Right: force amplitude vs. wave period.
Table 4. Changes of the force, damping coefficient, and the power with size and wave period.

| Wave period (s) | Diameter (m) | Force Amplitude (N) | Damping coefficient (Ns/m) | $\frac{P_{mean}^2}{8 R_{ins}}$ (W) |
|----------------|-------------|---------------------|--------------------------|----------------------------------|
| 6.0            | 2.5         | 34900               | 738                      | 206302                           |
| 6.1            | 5           | 128000              | 9030                     | 226800                           |
| 6.3            | 7.5         | 263000              | 36100                    | 239504                           |

These results confirm the left side Budal upper bound ($P_A$) in which the power is independent of the volume and is only a function of $H$ and $T$ and therefore the size paradox.

5. Conclusion

In this paper a practical design procedure for initial sizing of heaving point absorbers is proposed. The design procedure starts with determining the the power capture ratio. Next the most optimal set of design wave height ($H_{design}$) and design wave period ($T_{design}$) which results in the maximum ratio of mean power to submerged volume ($P_{mean}/V_{sub}$) is selected. The $P_{mean}$ is calculated by only considering the left-hand Budal curve ($P_A$). Moreover, the right-hand Budal curve ($P_B$) and its intersection with the $P_A$ curve is used to find the submerged volume. If the submerged volume corresponding to the highest $P_{mean}/V_{sub}$ ratio is practical, it defines the initial size of the point absorber. The procedure is employed to size a small bottom-referenced heaving point absorber with the sea state data from European Marine Energy Centre by considering two different capture ratios. Then the results are compared with an existing similar point absorber in the same site and show that even with a lower capture ratio, the design procedure leads to a high $P_{mean}$ while keeping a reasonable capture width ratio (CWR). Furthermore, it is shown in that larger point absorbers do not yield higher power and the power is in fact governed by the sea conditions. This is confirmed by modelling point absorbers with considerably different sizes in ANSYS AQWA and plotting their time-averaged power.

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