An integrated model of traffic, geography and economy in the Internet

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Modeling Internet growth is important both for understanding the current network and to predict and improve its future. To date, Internet models have typically attempted to explain a subset of the following characteristics: network structure, traffic flow, geography, and economy. In this paper we present a discrete, agent-based model, that integrates all of them. We show that the model generates networks with topologies, dynamics, and (more speculatively) spatial distributions that are similar to the Internet.

I. INTRODUCTION

As one of the most complex human constructions, the Internet is a challenging system to model. Dynamic processes of different time-scales operate simultaneously—from slow processes, like the development of new hardware, to the transport of data, which occurs at the speed of light.

These phenomena are to some extent interdependent. Traffic provides income to the service providers which is then invested in infrastructure, which can lead to changes in traffic patterns. This paper describes an agent-based model (ABM) that attempts to reproduce large-scale features of the Autonomous System (AS) level of the Internet by modeling localized and well-understood network interactions. The ASes of the Internet lend themselves naturally to discrete ABM models (4). Each AS is an economic agent, comprised of a spatially discrete network. Over time, ASes create new links to other ASes, upgrade their carrying capacity, and compete for customer traffic. The agents in the model described here, behave similarly, although we have simplified as much as possible. Specifically, the model is designed to be both simple and general enough to simulate any spatially extended communication network built by subnetworks of economically driven agents.

In previous work, Chang et al. showed that incorporating economics and geography into the Highly-Optimized Tolerance (HOT) (6) model increases the model’s accuracy (7). A related ABM model of the AS graph produces degree distributions similar to empirical observations (8). Bar et al. proposed a similar model (2), that incorporates another aspect of the real Internet—that the agents are spatially extended objects. Our model is similar in scope to this earlier work but differs in the details, most importantly by adding explicit economics (cost) to the model. Other differences include accounting for population density, simplifying the treatment of traffic flow, and not assuming a HOT framework. The previous work in this area, like much research on network models, focuses almost exclusively on degree distributions of the graphs. In this paper, we compare our results to Internet data using several topological measures (19), including degree distributions, as well as geography and traffic dynamics.

The remainder of the paper is organized as follows. First, we describe and motivate the model. Then, we characterize the time evolution, network topology, correlation between network structure and traffic flow, packet routing statistics, and geographical aspects of the networks produced by the model. Where possible, we compare the properties of these synthetic networks to observed data from the Internet.

II. AS SIMULATION MODEL

We begin with the fundamental unit responsible for network growth, an agent with economic interests (15). These agents manage traffic over a geographically extended network (which we refer to as a sub-network to distinguish it from the network of ASes) and profit from the traffic that flows through their network.

We compare the agents to the ASes that comprise the Internet. This is not an exact mapping—some of the Internet Service Providers (ISPs) have many AS numbers (e.g., AT&T), while other ASes are shared by several organizations. We make the common simplifying assumption that once an agent is introduced, it does not merge with another agent or go bankrupt (8; 22; 24). This is partially justified by the fact that the Internet, from its inception, has grown monotonically, and we seek to capture this dynamic in our model. Most other models of the AS graph enforce strict growth (22) as well and are, as ours, justified by their a posteriori ability to reproduce measured features.

We assume a network user population distributed over a two-dimensional area. Traffic is simulated by a packet-exchange model, where a packet’s source and destination are generated with a probability that is a function of the population profile. The model is initialized with one agent comprised of a network (a sub-network in our terminology) that spans one grid location (referred to as a pixel of the land-
FIG. 1 Illustration of the network growth algorithm. (a) shows the locations of four agents on the geographic grid. These are assumed to be connected by a physical network administrated by the agent, but is not explicit in the model. (b) is an example graph resulting from (a). That two agents are present in the same pixel is a necessary, but not sufficient condition for a link to form between the agents. (c) illustrates the area that each hypothetical agent can afford to expand to (the shaded region).

As time progresses, the agent may extend its subnetwork to other pixels, so that the subnetworks reach a larger fraction of the population. This creates more traffic, which generates profit, which is then reinvested into further network expansion. Through positive feedback, the network grows until it covers the entire population. In this section we describe the assumptions and most of the details of the model; the source code is publicly available from www.csc.kth.se/~pholme/asim.

An agent $i$ is associated with a set of locations $\Lambda_i$ (representing sources or end-points of traffic, and peering points), a capacity $K_i$ (limiting the rate of packets that can pass through the agent), a packet-queue $Q_i$, and a set of neighbor agents $\Gamma_i$. A necessary, but not sufficient, condition for two agents to be connected is that their locations overlap at, at least, one pixel. The locations exist on an $L_x \times L_y$ square grid. A pixel of the grid is characterized by its population $p(x,y)$ and the set of agents with a presence there $\mathcal{A}(x,y)$. The total number of agents is denoted by $n$, and the number of links between agents by $m$. These quantities, except $L_x$ and $L_y$, depend on the simulation time. The outer loop of the model then iterates over the following steps:

1. **Network growth.** The number of agents is increased. Existing agents expand geographically, and their capacities are adjusted.

2. **Network traffic.** Packets are created, propagated toward their targets, and delivered. This process is repeated $N_{\text{traffic}}$ times before the next network-growth step.

We measure simulation time $\tau$ as the number of times Step 1 is executed (the time unit between packet movements is $1/N_{\text{traffic}}$). In the remainder of this section we describe the growth and traffic steps in greater detail.

### A. Network growth

The income of an agent, during a time step, is proportional to the traffic propagated by the agent during the period. This is a simplification—in a more detailed simulation one could let the income depend both on the amount of traffic, and the prices for forwarding the packets set by business agreements. Assume an agent $i$ has a budget $B_i$ that it tries to invest so that it can increase its traffic, and thus its profit. Since there is a possibility of congestion in the model, agent $i$ tries first to remove bottlenecks by increasing its capacity $K_i$ (the number of packets that the agent can transit during one time step). When the capacity is sufficient, the agent spends the rest its budget on increasing its traffic by expanding geographically. There are three prices associated with network growth. First, the capacity price $C_{\text{capacity}}$—the price of increasing $K_i$ one unit. For simplicity we let $C_{\text{capacity}}$ be independent of the size of the agent’s subnetwork. Second, the wire price $C_{\text{wire}}$. This is the price per pixel between a new location and the agent’s closest existing location. Last, the cost $C_{\text{connect}}$ to connect two agents with locations at the same pixel.

It has been observed that the average degree (number of neighbors of an AS) in the AS graph is relatively constant over time (11, 22). We take this as a constraint in our model and let the desired average agent degree $k_D$ be a control parameter. We also assume that each agent tries to spend all of its budget, but not more than that, whenever it is updated.

The network growth step iterates over the following steps:

1. **Increase of the number of agents.** As long as the network is too dense (i.e. if $2m > k_D n$), new agents are added. New agents are situated in the pixel $(x,y)$ that has the highest available population $p(x,y)/(A(x,y)+1)$ where $A(x,y)$ is the cardinality of $\mathcal{A}(x,y)$ and $A(x,y) \geq 1$. The budget and capacity of the new agents are initialized to $B_{\text{init}}$ and $K_{\text{init}}$ respectively.

If the network is small, $n < k_D + 1$, it is not dense enough for new agents to be added in step 1. Thus, we do not apply this condition when $n$ is less than a threshold $n_0$ and call the time when $n = n_0$ is reached $t_0$.

2. **Capacity increase.** Each agent synchronously increases its subnetwork’s capacity based upon traffic from the last time step (but not more than the agent can afford). Agent $i$ invests the minimum of $(B_i/C_{\text{capacity}}\Delta T, 0, 0)$ to increase capacity ($\Delta T$ is the change in traffic propagated by $i$ since the last update).

3. **Link addition.** While $2m \leq n k_D$ (which usually means $k_D - 1$ times), choose two agents randomly that are not already connected and share a common pixel. If the budgets of both agents are larger than $C_{\text{connect}}$, then connect them.

4. **Spatial extension.** Let the agents with remaining budget to spend extend their networks. Iterate through all agents $i$ and add a location at the pixel, not in $\Lambda_i$, that has the highest available population $p(x,y)/(L(x,y)+1)$, and is not further than $(B_i - C_{\text{connect}})/C_{\text{wire}}$ from a location in $\Lambda_i$ (i.e., not further from $i$ than $i$ can afford). (See Figure 1(b)). An alternative location selector might select the point which has the lowest cost per unit of population. Unfortunately, such an algorithm is computationally prohibitive for modeled networks of the Internet’s scale.
FIG. 2 Illustration of traffic simulation. (a) A packet is created with source pixel s and target pixel t with probability proportional to the product of populations at s and t. One of the agents at the target pixel is randomly chosen as the target agent. The propagation of the packet is shown in the graph. Each agent i is associated with a queue \( Q_i \) and a capacity \( K_i \). When a packet reaches an agent, it is appended to \( Q_i \). \( K_i \) packets in the queue are relayed to neighboring agents and i’s budget is credited one unit. The arrows in (b) symbolize the packet’s route from source to destination agent. The package is routed to a neighboring agent \( j \) with probability \( \exp((d(i, t) - d(j, t))/\lambda) \) (where \( t \) is the packet’s target, \( d(\cdot, \cdot) \) gives the graph distance, and \( \lambda \) is a parameter).

The cost of each agent modification mentioned above is immediately deducted from the budget of the agent.

B. Network traffic

We model traffic with a discrete, packet-exchange model (12, 18). The packets are generated with specific source and target pixels, but the routing takes place on the network of agents. We neglect intradomain routing between the agent’s locations, assuming the time it takes for a packet to pass through an agent is independent of the specific locations it visits. The dynamics are defined as follows:

1. Packet generation. We assume that most traffic originates from direct communication between individuals and does not depend on the distance between them. So, for each pair of points \( [(x, y), (x', y')] \) on the grid, we create a packet with source \((x, y)\) and destination \((x', y')\) with probability \( P_{pkg} p(x, y) p(x', y') \). Then one agent, selected at random from the agents with a location at the pixel, is made the source node for the packet. The destination agent is randomly chosen from the agents at the destination pixel. Finally, one unit of credit is added to the sender’s budget.

2. Packet propagation. Each agent \( i \) propagates the first \( K_i \) packets from its queue (of length \( l_i \)) each time step and receives one unit credit for each propagated packet. A packet can propagate only one hop (inter-AS transmission) per time step. A packet at agent \( i \) is propagated to a neighbor \( j \) with probability \( \exp(\lambda(d(i, t) - d(j, t)) \)

(where \( t \) is the recipient AS, \( d(\cdot, \cdot) \) is the graph distance, and \( \lambda \) is a parameter controlling the deviation from shortest-path routing (23) observed in Ref. (16)).

3. Packet delivery. For all agents, delete all packets that have reached their target.

The assumption, in step 1, that the probability that two agents communicate is independent of their spatial separation is in line with the (somewhat debated) “death of distance” in the Internet age (5). We also tested communication rates that decay with the square of the distance, as observed in conventional trade firms (20), with qualitatively the same results.

Business agreements between ASes are an important factor in the Border Gateway Protocol (BGP) (23) (the Internet’s largest scale routing protocol). Next hops are often selected by cost, rather than path length. We do not explicitly include inter-AS contractual agreements, but our probabilistic propagation method has a similar effect on average path length (16).

III. NUMERICAL SIMULATIONS

A. Parameter values

Before presenting the simulation results, we describe the experimental design, and choice of parameters. First, we specify a population profile \( p(x, y) \). We primarily model population distributions, but we also model specific geographic populations (e.g. U.S.A. census data). To simplify the generation of population distributions, we neglect spatial correlations and simply model the frequency of population densities. This frequency has two important features: it is skewed (pixels with low population densities are more frequent than highly populated pixels) and fat-tailed (there are pixels with a population density many orders of magnitude larger than the average).

One probability distribution with such features is the powerlaw distribution \( \text{Prob} p \sim p^{-\chi} \). To reduce the fluctuations between different realizations of \( p(x, y) \), and prevent unrealistically high populations within a pixel, we sample the power-law distribution in the bounded interval \([1, (L_x L_y)^{1/(1-\chi)}]\) (10) with \( \chi = 3 \). Our results do not depend strongly on the distribution \( p(x, y) \). We obtain qualitatively similar result with normally distributed \( p \)-values and real population-density maps (data not shown).
In multiparameter, agent-based models, such as ours, a systematic investigation of the full parameter space is infeasible. Parameters are, if possible, obtained from real systems. We set the desired degree \( k_D = 5.52 \) as observed in Ref. (19). Unless otherwise stated, the desired size of the network is \( n_D = 16,000 \), which is the same order of magnitude as the real AS graph. Other parameters are balanced to keep runtime low (less than one day) while still engaging all aspects of the algorithm. This means, for example, that between every network update, a significant number of packets are routed through even the smallest agents, and enough packages to cause congestion pass through larger agents. Unless otherwise stated, we use the parameter set given in Table 1. Many of the results we show are from a single run, we have confirmed that the results are representative by comparing them with 20 other runs.

B. Network Growth

We begin by studying the growth of the network over time. In Fig. 3(a) we plot the number of agents and links as a function of time for one representative run. At \( \tau = \tau_0 \sim 4 \times 10^5 \) the graph is sparser than \( k_D \). Initially, the agents spend the budget they accumulate on new links (and increasing capacity). Around \( \tau \sim 1.5 \times 10^6 \), the budget of the wealthier agents is sufficient to invest in wires to new locations (see Fig. 3(b)). This creates new traffic, which causes positive feedback accelerating the traffic flow, coverage, budget, and also more congestion. Around \( \tau \sim 1.9 \times 10^6 \), \( n(\tau) \) and \( m(\tau) \) change from exponential to sub-exponential growth. As we see below, this is also the time when a significant level of congestion appears in the system. At about the same time, the entire population is serviced by the network. With the current model, the network would grow indefinitely but with decreasing returns for the agents. Alternatively one could introduce maintenance costs proportional to network size, in which case the network would reach a steady state where the budgets of the agents are balanced and no further investments can be made. For \( \tau \geq 1.9 \times 10^6 \) the increase of \( n(\tau) \) is slower than exponential. This is explained by the increasing level of congestion in the system. In Fig. 3(c) we plot the average time \( \langle \tau_p \rangle \) for a packet to travel from source to destination. \( \langle \tau_p \rangle \) is bounded from below by the average distance (number of links in the shortest path, averaged over pairs of nodes) \( \langle d \rangle \). The two curves diverge, i.e. a significant level of congestion appears, around \( N = 1000 \). The growth of \( n(\tau) \) and \( m(\tau) \) slows down at the same point. We conclude that growth slowdown comes from a congestion-driven negative feedback. The most striking feature of network growth over time is the transition from a small network, almost constant in size, to a rapidly increasing system (around \( \tau \sim 1.8 \times 10^6 \)). This effect is typical for technologies emerging from the interactions of a large number of agents—they need a critical mass of users to reach a significant fraction of the total population. One can argue that the Internet reached this critical mass in the early 1980’s when it started to span the globe. Another important point in the Internet’s history was the advent of the World Wide Web (WWW) in the early 1990’s, and with it commercial applications and access to the general public. Our model does not include applications, such as the WWW, that undeniably affect network growth. Such effects could be included by adopting a different traffic model, but for this paper we aim at simplicity and generality. In the Internet the growth of the number of ASes is slower than the exponential increase of agents predicted by the model (bpg.potaroo.net/cidr/; read January 7, 2008). One reason for the faster growth is that we do not assume that maintenance costs are proportional to income—if such costs grow super-linearly, negative feedback could dampen growth. Other external factors, such as the fact that AS numbers are allocated and assigned by a central authority (Internet Assigned Numbers Authority, www.iana.org), might also influence the actual rate of growth experienced by the Internet.

C. Degree distribution

One of the most conspicuous network structures of AS-graphs is its skewed degree distribution (first observed in Ref. (14), compatible with a power-law functional form (9). In Fig. 4(a) we compare the cumulative degree distribution of our model with that of the Internet’s. We use the model network from the example run described earlier (taking data from the simulation when \( N = 16,000 \)), and the “AS06” network of Ref. (19) (an AS-graph constructed from www.routeviews.org and www.ripe.net, with \( N = 22,688 \)). The match between the model and the real networks is striking. Preliminary studies indicate that the slope of the curve is largely insensitive to changes in parameter values. We compare this result with a generic network model that produces power-law degree distributions (the Barabási–Albert (BA) model (3)) and a simple, geographic model of the AS-graph designed by Fabrikant, Koutsioupias, and Papadimitriou (FKP) (13).

The BA model is a growth model in which one node (and \( m \)
two important components of Internet growth, namely the rich-
gets-richer effect driving the growth of the BA model and the
spatial trade-off effect of the FKP model.

A combination of these effects may explain why our model’s
degree distribution, and the curve of the real network,
lies between those of the original BA and FKP models. In our
model, the degrees of nodes do not directly affect the creation
of new links. However, preferential attachment occurs indis-

FIG. 4 The degree distribution (cumulative mass function) of a real
AS-graph (AS06) together with degree distribution of a network gen-
erated with the model (a), the BA (b) and the FKP models (c). Panel
d is a density plot that illustrates the correlation between traffic and
degree in our model runs.

FIG. 5 Radial statistics for real and model networks. Panels (a)–
(c) show the radial densities of nodes for the real AS-graph and our
algorithm (a), the BA (b) and FKP (c) model. Panels (d)–(f) show
the average degree vs. average distance \( \bar{d} \) for our algorithm, the BA,
and the FKP model respectively. The data of panels (b), (c), (e), and
(f) are plotted in Ref. (19) as well.

The FKP model is also a simple growth-model. Each time
step, one node, and a link attached to it, is added to the
graph. A new node \( i \) is assigned random coordinates in the
unit square and attached to the old node \( j \) that minimizes
\( d_0(j) + \alpha |r_i - r_j| \) (where \( d_0(j) \) is the graph distance between

In Figs. 4(b) and (c) we plot the cumulative mass function
of degree for one BA and one FKP network. The model pa-
rameter values were chosen to give networks as close as pos-
able to the real AS-graph (\( m = 5 \) for the BA model, \( \alpha = 4 \)
for the FKP model, and \( N = 22,688 \) for both). The slope of the
BA model is steeper than the real network, and the curve
for the FKP-model is flatter than the real data. To compare
the goodness-of-fit, since the curves have a similar range in
\( \log p_k \), we measure the ratio \( \theta \) of the area between the curves
and the area (in the \( \log p_k \)-\( \log k \)-space) spanned by the
extreme values of \( \log k \) and \( \log p_k \). We find \( \theta = 0.95\% \) for our
model, 4.0\% for the BA model, and 11\% for the FKP model.
Although both the BA and FKP models have been extended to
yield better data fits (17, 28), the original forms of the mod-
els illustrate two important components of Internet growth,

D. Radial structure

Structurally, the AS graph is hierarchically ordered (27)—
engineers and network operators speak of the first, second and
third tier. For the model networks, we measure a node’s posi-
tion in the hierarchy by its network centrality (19). In Fig. 5
we diagram the average fraction of nodes and the average de-
gree as functions of the average distance \( \bar{d} \) to other nodes in
the network (\( \bar{d} \) is the inverse of a centrality measure, known
as closeness centrality, so more central nodes are to the left
in the diagrams). By this method we can get a radial picture
of the AS graph structure from the center to the periphery.
put constraints on how packets are routed—for example, usually a packet cannot first be routed downwards (to customers), then upwards (to providers), in the hierarchy, even if that is a shorter path (known as the valley free rule). Gao and Wang (16) investigated the extra distance $d_e$ packets need to travel due to such reasons. They found a decaying probability distribution of $d_e$, meaning that most of the traffic actually travels via shortest paths. In our model we do not have explicit business agreements that cause hierarchical routing into the core of the network, and out again. It is, however, true for most graphs that a vast majority of shortest paths pass a restricted core of the graph (17), and our traffic model routes most traffic via short (if not the shortest) paths. The $d_e$ distribution of our model (shown in Fig. 6(a)) matches the observation of Gao and Wang (16).

We proceed to investigate the relationship between graph centrality and traffic density. This can tell us something about how congestion and fluctuations affect routing (18). If all agents have sufficient capacity for packets to always route along shortest paths, then traffic density along a link $l$ will be proportional to its betweenness centrality

$$C_B(l) = \sum_{i,j} \sigma(i,j) / \sum_{i,j} \sigma(i,j)$$

where $\sigma(i,j)$ is the number of shortest paths between nodes $i$ and $j$ passing through the link $l$, and $\sigma(i,j)$ is the total number of shortest paths between $i$ and $j$. If an AS is congested, the traffic through its links will be lower than anticipated by the betweenness of the edge. Thus, congestion patterns can be illustrated by studying betweenness and traffic load. Fig. 6(b) is a density plot of the actual traffic density as a function of betweenness of the links of the model network. For more central nodes (higher betweenness), there is a strong correlation between betweenness and traffic density—the vertices with $C_B \approx 4 \times 10^3$ span half a decade of $\rho$. For the more peripheral nodes the correlation is less clear (vertices with $C_B \approx 5 \times 10^4$ can have $\rho$-values of almost three orders of magnitude). Indeed, there seems to be a separation of agents into two classes, one with capacity to keep the traffic flowing, another with too low capacity. For links of low betweenness the traffic–betweenness correlation is weak. To summarize, congestion does affect the system, and it is most pronounced for nodes carrying little, or intermediate, traffic levels.

F. Geographic structure

We briefly discuss the spatial network structure—another feature that emerges from our model. As an example, we ran the simulation on the population density profile of the United States. In Fig. 7(a)–(d) we show the growth of the largest agent for a run with $n_D = 20, L_D = 513$ and $L_e = 323$. Lines are drawn between each node (pixel) and the agent’s nearest node at the time of the node’s addition. In this representation the length of the lines are proportional to the wire cost. Fig. 7(e) and (f) plot the locations of Tier 1 exchange points of two major Internet providers Sprint and AT&T (adapted from

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Fig. 6 Traffic patterns of the model. (a) displays the number of extra steps $d_e$ in packet navigation in the real Internet compared to our model. Panel (b) shows the probability density of agents having betweenness $C_B$ and traffic density $\rho$. The data is collected from twenty independent runs.

In Section III.B we investigated network topology and its growth. In this section we study traffic flow and how network topology affects it. In the Internet, packets do not necessarily travel the shortest distances between source and destination. Most importantly, business agreements between agents arrange agents into a hierarchy (15). The business contracts

FIG. 6 TraffiC patterns of the model. (a) displays the number of extra steps $d_e$ in packet navigation in the real Internet compared to our model. Panel (b) shows the probability density of agents having betweenness $C_B$ and traffic density $\rho$. The data is collected from twenty independent runs.
FIG. 7 The spatial expansion of a single agent with the US population density as model input. The simulation parameters are the same as the rest of the paper, except \(n_0 = 20, L_x = 513\) and \(L_y = 323\). Panels (e) and (f) represent the points of presence of AT&T and Sprint within the United States. This data was adapted from Ref. (26).

Ref. (26). There are some similarities between these real networks and the model network of Fig. (d)—all networks span the whole continent and have locations concentrated in urban areas. In future work we intend to make a statistical characterization of the spatial aspects of the networks produced by our model.

IV. DISCUSSION

We have presented a model of communication networks that, like the AS-level Internet, is built of spatially extended subnetworks that have an interest in increasing the traffic running through them. Our model networks grow slowly until they reach a critical mass where an approximately exponential growth begins; they match the degree distribution of real networks and the radial statistics closely. The degree distribution of the model, and the real world lies between the distributions of the pure BA and FKP models. Since the model incorporates aspects of both the BA and FKP models we hypothesize that, the explanation for the degree distribution of the model, and the real world, is a combined result of preferential attachment (of the BA model) and geographically constrained optimization (of the FKP model). We are able to recreate the traffic characteristic observed in real Internet traffic. If we run the model on the US population density map many features of the backbone of large, real agents are recreated.

The different aspects of the model (traffic, geography, and agents trying to increase the traffic they relay) all affect the output. In this paper we do not scrutinize the model’s parameter dependence, although preliminary studies indicate that the speed of growth (quantified by e.g. the time to reach the critical density) is strongly dependent on both the wire and attachment prices, the population density profile (a more clumped population distribution produces faster growth), and their desire to communicate. On the other hand, the network topology is rather insensitive to the population distribution, and also not very dependent on how sources and destinations are generated (e.g., introducing a distance dependence does not matter much). The specific layout of the network is, however, dependent on population profile.

Many interesting extensions of the basic model are possible. One interesting extension would, for example, be to include business agreements between the different agents (similar to Ref. (8; 24)), or change the traffic patterns from the person–to–person communication of the present model to a situation with more traffic coming from central servers. It might also be interesting to model intra-AS routing. Many of today’s ASes employ “hot-potato” routing and transfer packets to the next AS as quickly as possible, to reduce cost. Alternative intra-AS routing strategies, such as routing the packet as close to the destination as possible, could be tested within the model’s framework.

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