Melting temperature versus crystallinity: new way for identification and analysis of multiple endotherms of poly(ethylene terephthalate)

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Abstract
Poly(ethylene terephthalate) (PET) materials with different molecular weights were isothermally crystallized from melt by systematically varying the temperature and duration of the treatment performed in the differential scanning calorimeter (DSC). Multiple endotherm peaks were observed on the subsequent heating thermograms that were separated from each other on the basis of their melting temperature versus crystallization temperature and melting temperature versus crystallinity function. By this new approach five sub-peak sets were identified and then comprehensively characterised. Wide-Angle X-Ray Diffraction (WAXD) analyses revealed that the identified sub-peak sets do not differ in crystalline forms. By analysing the crystallinity and the melting temperature of the sub-peak sets as a function of crystallization time, crystallization temperature and intrinsic viscosity, it was concluded that below the crystallization temperature of 460 K the sub-peak sets that were formed during primary or secondary crystallization transform partially or completely to a third sub-peak set during the heating run of the measurement, while above this temperature, the sub-peak set formed during primary crystallization gradually transforms to a more stable structure, with higher melting temperature. These formations and transformations are described with mathematically defined parameters as well.

Keywords Poly(ethylene terephthalate) · Isothermal crystallization · Differential scanning calorimetry · Multiple melting endotherm · Solid state polycondensation

Introduction
The usage of poly(ethylene terephthalate) (PET) still increases nowadays; in original form and as secondary raw material alike [1, 2]. Besides the packaging industry, PET is increasingly used as a technical material thanks to the achievements of the material developments (Solid State Polycondensation reaction (SSP) or chain extender additives) and the advancements in the processing technologies (foam forming, 3D printing) [3–7]. Regarding applicability
of the final products the mechanical properties are crucial, which are greatly affected by the morphology and crystalline structure formed during processing [8, 9].

The morphology of the PET crystals depends primarily on the molecular structure (molecular weight distribution, type and ratio of the comonomers, etc. [10, 11]), however the final structure is also influenced by external factors such as cooling rate, pressure, crystallization temperature, nucleating agents, orientation, etc. [12]. The crystallization of PET can be either temperature or strain induced process [13]. Temperature induced crystallization takes place when the temperature is kept between the glass transition temperature ($T_g$) and the melting temperature ($T_m$). In this case, the crystallization process is determined by the change in the Helmholtz free energy. The enthalpy needed for crystallization is the sum of the change in the volume and surface enthalpy of the transition phase. The Gibbs–Thomson approach is based on a thermodynamic consideration that the melting temperature of a finite crystallite is always lower than the equilibrium melting temperature ($T_m^0$) of a theoretically infinite crystallite (‘block’) since with the decrease in the dimensions, the Helmholtz free energy of the surface increases [14]. By using the Gibbs–Thomson equation, the equilibrium melting temperature $T_m^0$ and thus the lamella thickness can be determined [14]:

$$l_c(T_m) = \left(1 - \frac{T_m}{T_m^0} \frac{\Delta h_m}{2 \cdot \sigma_e} \right)^{-1}$$  \hspace{1cm} (1)

where $l_c$ [m] is the lamella thickness; $T_m$ [K] is the melting temperature; $T_m^0$ [K] is the equilibrium melting temperature of the infinite crystallite (564 K); $\sigma_e$ is the surface energy of the folding plane (0.106 J/m²); and $\Delta h_m$ is the volumetric melting enthalpy (2.1*10⁸ J/m³). (The data for PET material are from the research of Lu and Hay [15].) The condition for the application of this method is that the dimension of the parental plane of the lamella is large enough compared to the lateral plane. Furthermore, the lamellar thickness should be determined right before the melting temperature of the lamella. If the measurement of the lamellar thickness occurs at the crystallization temperature or its immediate surrounding then the crystallite can reorder, i.e. melt and recrystallize, and get thicker during the differential scanning calorimeter measurement (DSC).

Another significant relation has been derived by Hoffman and Weeks (H–W) giving a connection between the observed melting temperature $T_{m, obs}$, the crystallization temperature $T_c$, and the equilibrium melting temperature $T_m^0$ of the examined polymer. The equation assumes an obligate relationship between the lamellar thickness and the melting temperature of the polymer. According to this method, the melting temperatures of the material, previously isothermally crystallized at different temperatures, are plotted against the applied crystallization temperatures. Then, the intersection of the thus obtained Eq. 2 should be determined using the $T_m = T_c$ first degree equilibrium equation:

$$T_{m, obs} = \frac{T_c}{\gamma} + T_m^0 \left(1 - \frac{1}{\gamma} \right)$$  \hspace{1cm} (2)

where $\gamma$ [-] is the lamella thickening coefficient, which is the reciprocal of the slope of the H–W line. This theory assumes that the $\gamma$ is a constant.

The slope indicates the stabilization mechanism of the secondary nucleation according to Eq. 3 [16]:

$$H - W_{slope} = \frac{\sigma_{e,crystal} \Delta s_{nuclei}}{\gamma (1 + \beta) \sigma_{e,nuclei} \Delta s_{crystal}}$$  \hspace{1cm} (3)

where $H$–$W$ slope [-] is the slope of the Hoffman-Weeks curve, $\gamma$ [-] is the lamella thickening coefficient, $\beta$ [-] is the lamella widening coefficient, $\Delta s_{nuclei}$ [J/K] is the entropy change per unit volume of the secondary nuclei having a finite width during melting; $\Delta s_{crystal}$ [J/K] is the entropy change per unit volume of the lamellar crystals with infinite width during melting; $\sigma$ [J/m²] is the interfacial free energy of the folded surface.

Presuming that $\sigma_{e,crystal} \Delta s_{nuclei} \approx \sigma_{e,nuclei} \Delta s_{crystal}$ then the $H$–$W$ slope is determined primarily by the lamellar thickening and widening coefficients [16]. If there is no lamellar thickening ($\gamma \approx 1$) than the slope approximates to 1 if $\beta > 1$. This describes those processes when only few nuclei are formed, their collision is less likely, and therefore stabilization by widening of the crystallites is statistically more likely than by coalescence.

To describe the kinetics of isothermal crystallization the Avrami or, for modeling the secondary crystallization, the Lauritsen-Hoffman (L–H) methods are generally used. Lately, the Strobl model is also used to model the chain organization [17]. This model considers that the main principle of the crystal organization process is not the chain folding, but a three-step “packaging” process, during which firstly a mesomorph phase take shape by connecting the chain segments, then with the lateral growth of the surface crystallite layers are created, the coalescence of which forms the crystalline phase.

Wurm and Schick [18] concluded that the fundamental difference between the L–H and the Strobl models is that the L–H model assumes the final lamella thickness to be formed already at the beginning of the crystallization process that determines the melting temperature. However, according to the Strobl model, the final thickness of the lamella is gradually reached with the stabilization taking place behind the front line of spreading. During the stabilization process, the whole crystal surface (including the intra-lamella surfaces)
decreases thus the surface energy also decreases, therefore, according to the Gibbs–Thomson equation, the melting temperature gradually increases. The experimental results of this research group confirmed the Strobl model.

Lu et al. [15] analysed the kinetics of the isothermal crystallization of PET. The maximum growth rate of the polymer crystallites, calculated from the measured half-life, was observed in the range of 430—450 K.

Van Antwerpen and Van Krevelen [19] followed the crystallization of PET with different molecular weights by analysing the spherulite growth rate as a function of temperature. It was concluded from the results of the crystallization processes, starting from either glass or melt phase, that the temperature of the maximum growth rate does not depend on the average molecular weight. However, between 410—490 K the growth rate was found to significantly decrease with the increase of the molecular weight.

The multiple melting peaks of PET, observable after isothermal crystallization, have been evinced and researched for more than 50 years. This phenomenon is basically explained in two ways [20]: in the first case, the different melting peaks are assumed to be associated with different morphological spherulite structures, in the other case melting and recrystallization of the initial crystallite population, accompanied with growth and perfection of the crystallites formed at low temperatures, is suspected. It has to be noted that besides the commonly used DSC, there are other techniques to disclose the origin of the multi-peaked endotherms of PET. Among others, different types of advanced DSC methods, such as temperature modulated DSC [21, 22], ultrafast chip calorimetry or nanocalorimetry, which can reach even a $10^3$—$10^4$ K/s heating rate [23], or Differential Thermal Analysis (DTA) [24] can be mentioned. Methods that are based on X-ray diffraction, Wide-Angle X-ray Diffraction (WAXD), Small-Angle X-ray Scattering (SAXS) can be used as well. The calorimetric and the X-ray scattering methods can even be used in-situ. Melnikov et al. [25], developed an in-situ nano-focus X-ray scattering and nanocalorimetry equipment and revealed that in case of semirigid-chain polymers the multiple melting behaviour is not necessarily coupled to the melting–recrystallization processes. Other methods can give some information about the crystallinity structure, e.g. polarised optical microscopy [26] or FTIR [27].

The extracts of explanations of the multi-peaked endotherm curves and applied measurement procedures found in literature are summarized in Table 1.

It can be established that in former publications only the peaks representing the higher melting temperatures [20, 22, 31, 32, 34] were analysed presuming that the differences in the structure of molecular ordering are responsible for the different melting temperatures. Then evidence was also found for the recrystallization occurring during the DSC measurement. Later on three melting peaks were examined

\[20, 22, 31, 32, 34\] and for the last 20 years it has been widely accepted that the I. peak corresponds to the melting of the imperfect lamellas (formed during secondary crystallization), the II. peak is the result of the time and temperature dependent isothermal crystallization and the III. peak originates from the melting and recrystallization during the DSC measurement. The morphological explanation of the different peaks, however, varies in the different researches (Table 1). In recent investigations, the multiple melting peak phenomenon was not explained by analysing the melting peaks separately but by analysing the crystallization processes occurring in different isothermal temperature ranges with a unified approach [26].

The aim of this research is to investigate the morphology of isothermally crystallized PET and to qualitatively analyse the multiple melting peaks as a function of duration and temperature of isothermal crystallization, and also in relation to the intrinsic viscosity (IV) representing the average molecular weight. The effect of the heating rate applied during DSC measurement was considered as well. Our goal is to give an explanation for the multiple melting effects that removes conflicting issues between the former researches.

### Materials and methods

#### Materials

NeoPET 80 (Neo Group, Lithuania) type PET granulate with an IV of 0.80 ± 0.02 dl/g was used in the experiments. The molecular weight (MW) of the material was modified in two ways:

(a) MW was increased by solid-state polycondensation (SSP). SSP reactions were performed by LabSys Evo Thermogravimeter (TGA, Setaram, France) in nitrogen atmosphere. Samples were held at 323 K for 15 min to purge the chamber with nitrogen and then heated up to the SSP temperature with a rate of 10 °C/min. The applied SSP temperature was 503 K, and the applied reaction time was 8 h. At the end of the process the IV value of the resin increased to 0.99 ± 0.02 dl/g.

(b) MW was decreased by multiple extrusions. The PET was dried for 4 h at 413 K; then an LTE 26–44 (Labtech Engineering, Thailand) twin screw extruder was used for the extrusions with a rising temperature profile from 512 to 522 K. During the second extrusion cycle, the PET was processed with the same parameters as before. After the first and the second extrusion steps the IV value of the resin decreased to 0.66 ± 0.02 dl/g and to 0.59 ± 0.03 dl/g, respectively.

Accordingly, crystallization characteristics were examined on four PET grades differing in IV values.
| Ref                                      | Peak I                                                                 | Peak II                                                                 | Peak III                                                                 | Testing methods |
|-----------------------------------------|------------------------------------------------------------------------|------------------------------------------------------------------------|------------------------------------------------------------------------|-----------------|
| Bell et al. [24], 1969                  | (notation: Form II) Consists of partially stretched chains. Formed from Form I during heat treatment, cold stretching or from melt by slow cooling | (notation: Form I) Consists of folded chains                          |                                                                        | DTA             |
| Roberts [28], 1970                      |                                                                        | Perfect crystallite, formed during isothermal crystallization          | Recrystallization of the population II during DSC measurements          | DSC             |
| Sweet and Bell [29], 1972               |                                                                        | (notation: Form II) Stable population, not capable of recrystallizing at the given rate of the DSC measurement | (notation: Form I) Completely recrystallized material, independently if the primer structure contained stretched or folded chains | DSC, FTIR       |
| Groeninckx et al. [30], 1980            |                                                                        | Melting of the crystallites that were formed at the isothermal crystallization temperature | Formed by recrystallization during the measurement. When $T_m^0$ is defined by the Thomson-Gibbs equation, out of peak II and III the one with the maximum value was considered, therefore $T_m^0 = 563$ K | DSC, WAXD, SAXS |
| Zhou and Clough [31], 1988              | It can be seen approximately 10 K above $T_c$                          | The ratio increases as a function of crystallization time; from this population, $T_m^0 = 541$ K was calculated using the Hoffman-Week’s equation |                                                                        | DSC             |
| Woo and Ko [20], 1996                   | A separate population; if the $t_i$ is less than 5 min, it does not form. As a function of $T_c$, $T_m$ and the crystal-line ratio increase | A separate population; if the $t_i$ is less than 2 min, it does not form. As a function of $T_c$, the crystallization ratio increases. $T_m$ does not change as a function of $T_c$ | A separate population; by increasing $t_i$, the ratio of this form decreases. $T_m$ does not change significantly as a function of $T_c$ | DSC             |
| Medellin-Rodriguez and Phillips [32], 1996 | Contains smaller secondary branched lamellas; these lastly formed secondarily crystallized populations melt first during the DSC measurement | Contains dominant primary branched lamellas; the secondary structure represents higher ratio | Final, recrystallized spherulite structure | DSC, Optical microscope; SAXS, WAXD |
| Medellin-Rodriguez et al. [33], 1997    | The majority of this structure is formed during secondary crystallization. The ratio of this population increases with the average molecular weight | The ratio does not change with the increase in the average molecular weight | Growth during the isothermal crystallization. During measurement recrystallization can occur; the ratio of this population decreases with the average molecular weight | DSC, Optical microscope; SAXS, WAXD |
Methods

Intrinsic viscosity (IV) measurements

The average molecular weight of the PET samples was monitored by Intrinsic Viscosity measurements. The measurements were carried out according to the ASTM D4603 standard; the IV was calculated by the Billmeyer equation. The IV values of the PET materials were determined using a computer controlled RPV-1 (PSL Rheotek, USA) automatic solution viscometer equipped with an optical sensor. The IV values were measured at 30 °C in a 60/40 weight mixture of phenol/tetrachloroethane solvent with a concentration of 0.5 g/dl.

GPC measurements

Gel permeation chromatography (GPC) analysis was performed on four raw materials with different IV values to determine the molecular weight distribution and average molecular weights. 1,1,1,3,3,3-Hexafluoro-2-propanol (hexafluoroisopropanol, HFIP) eluent was used for the measurements. The GPC instrument was equipped with a Jetstream 2 plus thermostat, a Waters HPLC Pump 515, an HFIP-806 M column, and a Jasco RI-4035 differential refractometer detector. The measurement temperature was 40 °C, the flow rate was 0.5 mL/min, and the HFIP eluent contained 5 mM Na-trifluoroacetate. Evaluation of the chromatograms was performed by using PSS WinGPC software based on calibration with narrow molecular weight distribution poly(methyl methacrylate) standards.

Isothermal crystallization

Thermal characteristics of the samples were determined using a DSC131 EVO (Setaram, France) DSC device. The DSC measurements were performed in nitrogen atmosphere with a flow rate of 50 mL/min. The weight of the examined samples was between 5—8 mg and two parallel measurements were carried out in all cases. On one sample the effect of 14 different crystallization temperatures ($T_c$) were examined by following the program cycle presented in Fig. 1:

(a) The samples were heated up to 593 K with the heating rate of 10 K/min (the melting peaks were determined from the given step) then isothermal heat treatment occurred for 2 min to erase the thermal prehistory.

(b) The samples were cooled to the given $T_c$ with the cooling rate of 50 K/min.

(c) The isothermal temperature was held for different times ($t_c$); for 10 min, 1, 3, 5 or 10 h, depending on the program.
The samples were cooled to 373 K with the cooling rate of 20 K/min and then kept there for 2 min, in order to stabilize the morphology.

The examined crystallization temperatures were between 493—463 K with steps of 5 K and between 463—393 K with steps of 10 K. Molecular degradation during cyclic DSC program is not expected due to the inert atmosphere and the lack of shear force. Still, control measurements were carried out to prove that the sequence of cycle elements does not affect the DSC results, i.e. the last steps were performed with a material of the same quality as used in the whole cyclic program, and then compared. Standard deviation between the values of original and reverse cycle elements were between 0.7—1.4 K (melting temperature) and 0.3—2.4% (crystallinity) in the case of different sub-peaks. (Detailed results of control measurements can be found in the Supplementary Material I.)

Limitation of the DSC measurement is that the morphological structure – formed during the previous isothermal crystallization – cannot be analysed independently: during the DSC measurement the structure can change and researchers could only analyse the modified crystalline structure. The modifying effect of the different heating rates is usually analysed by comparison; having considered that if the heating rate is fast then

![Fig. 1 DSC program of cyclic isothermal crystallization](image)

![Fig. 2 The molecular weight distribution curves of the investigated PET samples](image)

![Fig. 3 DSC thermograms of original PET (IV = 0.80 dl/g) after one-hour isothermal crystallization at different temperatures. The classification of the sub-peak-sets is also indicated](image)

| IV (dl/g) | \( M_n \) (g/mol) | \( M_w \) (g/mol) | \( M_{peak} \) | PDI (\( M_w/M_n \)) |
|-----------|----------------|----------------|----------------|-----------------|
| 0.59      | 6 950          | 16 900         | 17 150         | 2.43            |
| 0.66      | 9 950          | 25 500         | 28 900         | 2.56            |
| 0.80      | 10 100         | 27 400         | 30 300         | 2.71            |
| 0.99      | 15 300         | 38 200         | 38 100         | 2.50            |
there is less time for the structure to change. Therefore, the effect of the heating rate on the detected endotherm peaks was analysed in our case as well. For this purpose, the used DSC cycle is almost the same as described previously, except that the samples were heated until 593 K with different heating rates (5, 10, 15, 20 or 25 K/min), then cooled to one of the three given isothermal crystallization temperatures (423, 453 or 483 K) and held there for 10 min, 1, 3, 5 or 10 h, respectively. These measurements were performed only on the samples with IV value of 0.80 dl/g.
WAXD measurements

WAXD analyses were performed on samples with an IV value of 0.80 dl/g after crystallization at 423, 453 and 483 K for 10 h. WAXD tests were performed on all three samples at two temperatures (room temperature and 488 K) with the following parameters: The samples were investigated on a Bruker D8 Discover instrument, with Cu K-alpha radiation (40 kV and 40 mA generator settings) in parallel beam geometry (with Göbel mirror) using a HTK 1200 N heating chamber and a LynxEye XE-T energy dispersive detector in high resolution 0D mode. The heating was run with 10 °C/min rate in static air atmosphere. Measurements were carried out in the 5–55°(2Theta) range with 0.014°(2Theta)/240 s steps. The peaks of PET were identified using the work of Wang et al. [35]. Crystallinity degree was determined by applying two amorphous humps according to Wang et al. (2000) and fitting the crystalline part of the pattern with individual peaks. Crystallite size for the individual peaks was calculated from the peak broadening as integral breadth corrected for the instrumental broadening, using the Scherrer formula. Integral breadth values were extracted from the measured pattern after deconvolution with empirical instrumental parametrization on NIST SRM 640d Si powder, fitting the background by 4th degree Tschebysehv polynomial function. XRD measurements were carried out in the 3DLab Fine Structure Analysis laboratory.

Results and discussion

Molecular weight analysis

The molecular weight distributions of the four PET materials, as determined by GPC measurements, are displayed in Fig. 2, while the characteristic average molecular weight (MW) and the peak MW values are shown in Table 2.

It can be seen in Table 2 that the number average molecular weight (Mn) of the used PET materials ranges from 6 950 to 15 300 g/mol and the weight average molecular weight (Mw) ranges from 16 900 to 38 200 g/mol. As the polydispersity index (PDI = Mw/Mn), which characterizes the width of the molecular weight distribution, differs only slightly between the tested substances (its value varies between 2.43 and 2.71) it was concluded that the difference between the molecular weight distribution of the materials has negligible effect on the examined multiple melting peaks or crystalline formations, on the one hand. On the other hand, the molecular weights show acceptable correlation with the IV values. As the IV value is widely used in the literature and shows strong correlation with the average molecular weight [36, 37], the IV value was decided to be used hereinafter for characterization of the PET materials.

Melting peak separation

Figure 3 shows a typical group of DSC curves obtained from original PET samples with an IV value of 0.80 dl/g.
After reaching the given isothermal crystallization temperatures (393-493 K), the crystallization time was 1 h.

Tangential sigmoid baseline was fitted on the endotherm peaks of the curves, and then the combined melting peaks were separated by the Calisto (Setaram, France) software. This program determines all the required parameters for Eq. 4 in the case of all sub-peaks:

\[
y = A \exp \left[ -\ln(2) \left( \frac{\ln \left( 1 + 2D \frac{x}{C} \right)}{D} \right)^2 \right]
\]

where \(A \, [\text{mW/g}]\) is the amplitude; \(B \, [\text{K}]\) is the position; \(C \, [\text{K}]\) is the halfwidth and \(D \, [-]\) is the asymmetry of the fitted Gaussian curve.

Crystallinity (\(\chi\)) of the endotherm sub-peaks was calculated according to Eq. 5:

\[
\chi[\%] = \frac{\Delta H_m}{\Delta H_m^0} \times 100\%
\]

where \(\Delta H_m \, [\text{J/g}]\) is the peak area (melting enthalpy) and \(\Delta H_m^0 \, [\text{J/g}]\) is the melting enthalpy of a perfect PET crystal equal to 140.1 J/g \[38\].

When \(T_m\) is displayed as a function of \(T_c\), different linear trends can be seen in the diagrams (Fig. 4a and 4b). The trends were isolated from the different sets of points and thus so-called sub-peak sets were formed. In those cases, when the individual set points overlapped with each other, the points of the \(T_m\) vs. \(\chi\) diagrams were analysed to decide which point belongs to which set (Fig. 4c and 4d). Based on the two parallel measurements the average standard deviation (SD) of \(T_m\) of sub-peaks was 0.4 K, the maximum SD of \(T_m\) of sub-peaks was 1.4 K, the average SD of \(\chi\) of sub-peaks was 1.4%, the maximum SD of \(\chi\) of sub-peaks was 3.3%. The \(\chi\) vs. \(T_m\) diagrams show similarity with the Thomson-Gibbs...
diagram when only the y-axis is analysed (Fig. 4e and 4f). However, the x-axis differs a lot: in this study on the x-axis not the change in the size of an individual crystal-lite is showed but the change in the crystallinity of the different crystalline structures.

The measured points obtained from different sets are linked together on the $\chi$ vs. $T_c$ diagram as well. For example, the typical functions of the original PET ($IV = 0.80$ dl/g) after 10 min isothermal crystallization are shown in Fig. 4a, 4c and 4e, while those after 5 h isothermal crystallization are presented in Fig. 4b, 4d and 4f, respectively. (All the diagrams can be found in the Supplementary Material II.) The functions are analysed in details in the next section.

On the obtained DSC thermograms five different sub-peak sets were identified and separated. The peak separation and classification into sub-peak-sets, performed after every DSC run, is presented in Fig. 3 on the example of the DSC thermogram series of original PET ($IV = 0.80$ g/dl) obtained after isothermal crystallisation at different temperatures. There are some similarities in the marking of the peaks with the literature [31–33, 39, 40] for example: the $T_m^1$ is similar to the peak I notation that represents those crystallites that were formed during secondary crystallization. However, a significant difference is that in this case the notation of the sub-peak sets did not occur simultaneously with the appearing order of the peaks, but they were sorted into the populations as coherence appeared between the peaks in the $T_m^1$ vs. $T_c$ and the $\chi$ vs. $T_m^1$ diagrams.

**Crystalline form analysis**

WAXD measurements at two different temperatures were performed in order to characterize the crystallinity and the crystalline form of the sample. During the tests the temperature high-temperature-measurement was chosen to be above the melting temperature of sub-peak set 1, but below the melting temperature typical of sub-peaks set 2, 3, 4, and 5. The measurements were carried out with samples $IV = 0.80$ dl/g and $t_c = 10$ h where the $T_c$ varied from 423 to 488 K.

The samples show a growing crystallinity and crystallite size which is indicated by the sharpening of the peaks, in the order of rising $T_c$ measured at room temperature (Fig. 5), which is in accordance with the changing of the calculated total crystallinity values measured by DSC. For each sample, the measurement run at 488 K...
shows an improvement in crystallite size, the peaks become sharper. As no new peaks appear on the figures of WAXD measurements performed at higher temperature, it can be stated that recrystallization during which the crystalline form does not change, cannot be detected. A small shift of peak positions is observed in case of the patterns recorded at 488 K, due to the thermal expansion of the PET lattice.

Miller indices are assigned to the peaks according to Wang et al. [35] (Table 3). However, three small intensity peaks were detected after deconvolution, which could not be indexed. These peaks are probably trace of partly modified PET structure, as a minor crystallite population associated to the main “regular” PET. A larger shift is observed for the (100) peak. It can be detected that the crystallite size of samples isotherm crystallized at 423 or 453 K differs significantly from the samples crystallized at 483 K in the direction of D_{(1-10)}, D_{(100)} and D_{(101)} which may indicate a different nucleation process. Based on the sizes measured for the first three peaks, the crystallites tend to take isometric shape at 488 K, while platy shape is the most characteristic at room temperature. It should be noted, that the crystallite parameters of samples isotherm crystallized at three different temperatures measured by high-temperature WAXD measurements show differences in certain directions probably due to structural differences.

Analysis of the sub-peak sets

In this part of the paper, the characteristics of the individual sub-peak sets are analysed as well as the evolution of these characteristics as a function of crystallization time, temperature, molecular weight, and heating rate are investigated (Fig. 6). Since some changes can occur in the sub-peak sets even during the DSC measurement (modification and/or transformation), the analysis of the direction and extent of these changes is of great importance. These were investigated by using different heating rates, assuming that by using faster heating rates there is less time available for the changes to occur.

In the followings, the complete evaluation method is presented in details on the example of sub-peak set 1, while the corresponding experimental results of sub-peak sets 2–5 can be found in the Supplementary Material III.

Appearance region

The sub-peak set 1 appears typically in the crystallization temperature range of 393—468 K, however in the case of low IV (0.59 dl/g) and short crystallization time (10 min) this sub-peak set appears even up to the crystallization
temperature of 493 K. The crystallinity represented by this sub-peak set is low (<5%). It shows some increase with increasing crystallization temperature. A logarithmic increase of crystallinity was evinced as a function of crystallization time as presented in Fig. 7a at a $T_c$ of 423 K, which is in agreement with the findings of Woo and Ko [20]. The increase of the crystalline ratio over time implies that the sub-peak set 1 is formed during the secondary crystallization [16, 41]. The increase in the melting temperature of the crystallites has also a logarithmic nature (Fig. 7b). The molecular weight that is represented by the IV value was found to have negligible impact on the crystallinity and the melting temperature of the analysed sub-peak set.

**Effect of heating rate**

The crystallinity and the melting temperature of the sub-peak set 1 as a function of the heating rate can be followed in Fig. 8a and 8b, respectively. The crystallinity decreases with decreasing heating rate, likely due to transformation. The melting temperature does not change significantly. Based on this, the initial crystalline fraction corresponding to sub-peak set 1 is assumed to be greater, but during the measurement it was transformed into another sub-peak set.

**Analysis of the Hoffman-Weeks lines**

Figure 9a shows the temperature sensitivity (slope of the Hoffman-Weeks function) of the samples with different IV values as a function of $t_c$. The slope of the functions varied between 0.90–1.20 in the analysed time range (10 min – 10 h). It can be established that the steepness of the slopes rises logarithmically in the investigated range as a function of $t_c$:

$$H - W_{slope} = a \cdot \ln(t_c / h) + b$$  \hspace{1cm} (6)

where $H$-$W_{slope}$ [-] is the slope of the function where $T_m$ is plotted against $T_c$; $t_c$ [h] is the crystallization time; $a$ [-] and $b$ [-] are model parameters.

The displacement parameter $b$ is mainly influenced by the IV value (Fig. 9b):

$$b = -0.11 \cdot IV + 1.11$$ \hspace{1cm} (7)

According to Eq. 3 when the steepness of the $H$-$W_{slope}$ is greater than 1 (heat treatment was longer than 1 h), than in classical sense lamella thinning and/or narrowing can be assumed, which is an obvious error in thermodynamic sense. It is much more probable to presume that the crystallites with increasing crystalline ratio (as a function of time) and melting temperature are not formed by lamella folding and their sizes do not increase by lamella-thickening, but they can be described with an ordering structure (according to Strobl model), which differs from folding.

**Analysis of the $T_m$ vs. $\chi$ function**

The melting temperature of sub-peak set 1 increases intensively as a function of crystallinity. The $T_m$ as a function of $\chi_1$ diagram (Fig. 4e, 4f) shows a logarithmical scheme in this set:

$$T_m = c \cdot \ln(\chi_1) + d$$ \hspace{1cm} (8)

where $c$ [-] and $d$ [-] are the first and the second (displacement) parameters of the function.

The first parameter $c$ does not show a clear trend as a function of time (Fig. 10a); however, the averages of these parameters increase linearly with IV (Fig. 10b):

$$c = 69.89 \times IV - 13.55$$ \hspace{1cm} (9)

The second parameter of the logarithmic function ($d$, displacement parameter) as a function of $T_c$ shows a logarithmic decrease (Fig. 11):

$$d = e \cdot \ln(t_c) + f$$ \hspace{1cm} (10)

where $e$ [-] and $f$ [-] are the first and the second (displacement) parameters of the function.

This means that in case of longer chains, accompanied with greater IV, with increase of the $t_c$, the higher crystalline ratios are associated with less intensively increasing $T_m$. Consequently, with increasing $t_c$ fewer molecular segments can connect parallel to the existing crystallite, especially in the case of long chains with hindered mobility.

The first parameter $e$ of Eq. 10 shows a linear decrease as a function of IV. Furthermore, the second parameter $f$ shows a linear correlation with the first parameter $e$. The functions are plotted in Fig. 12a and 12b, while the correlations are described by Eq. 11 and Eq. 12, respectively.

$$e = -20.72 \times IV + 2.23$$ \hspace{1cm} (11)

$$f = 2.03 \times e - 466.37$$ \hspace{1cm} (12)

It can be concluded from Eqs.(8, 9, 10, 11 and 12) that in the case of sub-peak set 1, the $T_m$ depends on the crystalline ratio, the IV and the $t_c$ as well:

$$T_m = (69.89 \times IV - 13.55)\ln(\chi_1)$$

$$+ (2.23 - 20.72 \times IV)\ln(t_c / h) - 42.66 \times IV + 470.9$$ \hspace{1cm} (13)
where $\chi_1$ [%] is the crystalline ratio, $T_{m1}$ [K] is the melting temperature of the first set, $IV$ [dl/g] is the $IV$ value of the examined material and $t_c$ [h] is the crystallization time.

These evaluation steps were done for all the 5 identified and separated sub-peak sets. The obtained results and establishments are summarized in Table 4. The change in the crystallinity was measured for each set on a specific temperature. It has to be noted that the summarized characteristics are valid only in the investigated range ($t_c < 10$ h; $393$ K < $T_c$ < $493$ K).

### Crystallization processes in different temperature ranges

It can be seen that sub-peak sets 1, 2 and 3 are formed in lower crystallization temperatures, but the appearance of sub-peak sets 4 and 5 is typical at higher crystallization temperatures. Therefore, these temperature ranges were analysed separately as well.

#### Sub-peaks appearing at lower crystallization temperature ($T_c < 460$ K).

At low crystallization temperature, under 440 K, only sub-peak sets 1 and 3 can be noticed in the DSC thermograms. It is presumed that out of the ordered phases that were formed during the isothermal crystallization sub-peak set 2, which was formed during primer crystallization, completely transformed into the sub-peak set 3. The sub-peak set 1, formed during secondary crystallization, only partially transformed into the sub-peak set phase 3.

By raising the crystallization temperature (440—460 K), the sub-peak set 2 transforms into sub-peak set 3 to a lesser extent, therefore it can be detected in larger ratio. Based on the value of the $H$-$W$ slope of sub-peak set 2, lamella thickening is assumed especially in case of lower $IV$, and lamella widening in case of higher $IV$. The formed sub-peak set 2 at higher $T_c$ results more stabilised structures, and these structures do not change to other sub-peak sets during the heating. This assumption is in accordance with the findings of

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### Table 4 Characteristics of the different sub-peak sets

| Sub-peak set | Crystallinity | typical appearance | $T_c$ region | $T_c$ as a function of $t_c$ | $IV$ as a function of heating rate | $H$-$W$ slope range as a function of $t_c$ | $H$-$W$ slope range as a function of $IV$ |
|--------------|---------------|-------------------|--------------|-----------------------------|-------------------------------|-----------------------------|-----------------------------|
| Sub-peak set 1 | $< 486$ K | 440—470 K | 423 K | logarithmic increase | no significant effect increase | 0.95—1.15 | logarithmic increase decrease |
| Sub-peak set 2 | $< 468$ K | 470 K | 453 K | increase until 1 h, then stagnates | no significant effect increase | 0.15—0.70 | no significant effect increase |
| Sub-peak set 3 | 470 K | 483 K | 423 K | no significant effect | no significant effect increase | -0.05—0.00 | no significant effect increase |
| Sub-peak set 4 | 470 K | 483 K | 483 K | logarithmic decrease | no significant effect decrease | 0.00—0.45 | increase decrease |
| Sub-peak set 5 | 470 K | 483 K | 483 K | logarithmic increase | no significant effect increase | 0.60—1.25 | no significant effect increase |
Baldenegro-Perez et al. [26], who detected lamella thickening and slight secondary crystallization in this crystallization temperature range by using SAXS and WAXD techniques.

By comparing the characteristics of the different sub-peak sets, it can be seen that only the sub-peak set 3 phase is significantly influenced by IV. This also implies that this phase is formed probably not from amorphous phase by nucleation, but it appears as a result of changes (growing/transformation) of already existing crystallites. These changes take place on the loops/bridges; therefore, the chain length plays important role regarding the part ratio of this type of crystalline structure. This result is important in the viewpoint of recycling since secondary PET material usually has lower IV value than original material.

The H-W slope of sub-peak set 3 is not influenced by the IV. The value of the slope is negative; therefore, it is not interpretable by the thermodynamic laws. This also confirms that the sub-peak set 3 is formed not during the isothermal crystallization, but appears during the heating of the measured samples, and evolves from sub-peak set 1 and 2.

The behaviour of sub-peak set 2, formed at lower T_c, can be explained by the adjacent re-entry model and the tightly-folded fashion model [42, 43]. This description mode is based on the intermolecular ordering of the chains and explains the formation of the crystalline layers in a multiblock view. The multiblock view (Fig. 13) describes the formation of the crystallite layers as a formation of folded rigid and amorphous flexible segments on the chains and then their organization [42].

Sub-peak set 2 is formed by the primary folded segments which can get thicker or wider by themselves. However, until their surface/volume ratio is below a critical value, during heating they merge into layers and form sub-peak set 3. In the ordering of the folded chains the loops/bridges have a crucial role. The longer molecular chains can ensure more 'bridges', therefore the part ratio of this sub-set is greater.

Sub-peaks appearing at higher crystallization temperature \((T_c > 460 \text{ K})\).

When \(T_c\) is higher than 460 K, the nature of nucleation changes. This change is probably due to the more intense moving of the molecules as a result of more thermal energy. In this case, a transitional sub-peak set is formed (sub-peak set 4), the behaviour of which set fits the Strobl model. If \(t_c\) is short, then sub-peak set 4 can be detected during the measurement. However, in case of longer crystallization time, during the crystallization or recrystallization it transforms into sub-peak set 5 logarithmically as a function of \(t_c\). Sub-peak set 5 is likely the result of the crystallization of pre-organized mesomorph parts, thereby forming the crystalline layers and lamellas. This transformation does not occur when \(t_c\) is only 10 min. When \(t_c\) is between 1 and 3 h then the transformation is partial, and when \(t_c\) is more than or equal to 5 h then it becomes complete.

**Applicability of different crystallization models for the sub-sets**

The crystallinity and the formation rate of all sub-peak sets except from sub-peak set 3 are not affected by IV, therefore by the length of the molecular chains. In case of these sub-peak sets, it is more likely that segmental ordering occurs independently from the chain length. This formation may start from chain folding (sub-peak set 2) or from the reorganisation (sub-peak set 1 and 5) of pre-organized mesomorph parts (sub-peak set 4) according to the Strobl model [17, 44] (Fig. 14). During this reorganisation the inner surface of the organised parts decreases significantly, therefore, changing the surface/volume Helmholtz free energy ratio, and by that the melting temperature [18].

![Fig. 13 Multiblock view: crystallization within the molecular chains (based on Liu et al. [42])](image1)

![Fig. 14 Strobl crystallization model (based on Strobl and Cho [44])](image2)
The behaviour of the sub-peak sets 1 and 5 is similar in many ways: their part ratio increases logarithmically as a function of time, and the values of the H-W slopes vary in a similar range. The difference between the two sets is that sub-peak set 1 is formed at lower $T_c$ and its ratio is significantly smaller. These two sub-peak sets are formed by the parallel ordering of the molecular chains as the Strobl model describes it. In case of PET, this process is more time and energy-demanding than the chain folding.

According to the H-W theory, the $T_m$ vs. $T_c$ functions are related with the thickening of the structures organised by chain folding. This approach is only applicable on sub-peak set 2. Accordingly, the equilibrium melting temperature ($T_m^0$) could be determined by the analysis of the H-W slopes of this sub-peak set. However, the obtained $T_m^0$ for this sub-peak set is only a theoretical value since at higher ranges of $T_c$, the formed structures in the material are different from the structures of sub-peak set 2.

**Conclusion**

In this research study, the crystalline phases, formed during isothermal crystallization and subsequent heating of PET, were analysed by DSC. Crystallization experiments were performed on PET materials with different molecular weight by varying the temperature and duration of the treatment. Then, the multiple endotherm peaks, appeared on the subsequent heating thermogram, were separated into sub peaks with a novel method and comprehensively analysed.

By analysing the melting temperature as a function of crystallization temperature, five sub-sets were identified and separated (the separated points fall on a straight line). From the thus created Hoffman-Weeks slopes, the mode of crystallization of the different sub-peak set was interpreted. It was concluded that only one (sub-peak set 2) fits the lamella thickening theory, while the Strobl model was found to be more suitable to describe the behaviour of the other sub-peak sets.

By analysing the crystallinity and the melting temperature of the sub-peak sets as a function of crystallization time, temperature and IV, it was concluded that different sub-peak sets are formed below and above the crystallization temperature of 460 K. In the lower temperature region, the sub-peak sets that were formed during primary or secondary crystallization are transformed partially or completely to a third sub set during the heating run of the measurement. In the higher temperature region, the sub-peak set formed during primary crystallization gradually transforms to a more stable structure.

The relationship between the crystallinity and the melting temperature of the sub-peak sets were characterised by functions. In the case of sub set 1, the function was found to be logarithmic, but for sub-peak sets 2–5, linear fit was found to be adequate in the investigated range: $t_c < 10 \text{ h;} 393 \text{ K} < T_c < 493 \text{ K}$.

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**Author contributions** Ferenc Ronkay contributed to the study conception and design. Material preparation, data collection and analysis were performed by Béla Molnár, Dóra Nagy and Katalin Bocz. GPC measurements were performed by Györgyi Szarka and Béla Iván, while WAXD measurements were carried out by Ferenc Kristály and Valéria Mertinger. The first draft of the manuscript was written by Ferenc Ronkay and all authors commented on previous versions of the manuscript. All authors read and approved the final manuscript.

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**Data Availability** All data generated or analysed during this study are included in this published article (and its supplementary information files).

**Compliance with ethical standards**

**Conflict of interest** No potential conflict of interest was reported by the authors.

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