Double Allocation of Spreading Code Minimizing SI and PAPR for LP-OFDM UWB System

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Abstract
Self-interference (SI) occurs if the transmission is through a multipath channel. The channel distortions help to break the orthogonality between the spreading codes. In addition, the amplitude of linear precoded orthogonal frequency division multiplexing (LP-OFDM) LP-OFDM signals have strong fluctuations. Thus, it is necessary to seek or to minimize these two problems by the reduction of term SI and the amplitude of fluctuations Peak-to-Average Power Ratio (PAPR). In this paper a new method of allocation of spreading code has proposed. It consists of a double selection of spreading codes minimizing joint SI and PAPR. Simulation results show that the LP-OFDM system is optimized by this proposal compared to the conventional solution where the systems don’t operate in full load.

Keywords: LPOFDM; Linear Precoding; spreading codes; SI; PAPR

Introduction
To ensure a satisfactory quality of service, future communications systems require a high spectral efficiency and flexibility. In 1993, many studies have shown that the technical meeting in places spread spectrum and multicarrier modulation is a solution which meets these criteria [1]. Multicarrier transmission is a solution which is widely exploited in communication networks, whether local, cellular, wireline, embedded or television [2].

The resources allocation is a fundamental aspect in the design of multicarrier systems. So, with the development of powerline communications, this theme of resource allocation in orthogonal frequency division multiplexing (OFDM) systems is still relevant [3] for access networks, home networks as embedded networks because it can maximize either the throughput or the robustness of the system [4].

The LP-OFDM systems can be described as multicarrier systems using a linear precoding and modulating data to be transmitted. The LP-OFDM is based on conventional OFDM associated with a linear precoding component. The main aim of this system is to make the most flexible multicarrier system with lowered limitations and better overall system performance, without raising its complexity [4].

In mobile radio and especially in LP-OFDM system, this precoding provides additional flexibility, simplifies the separation of received signals, or makes it possible, and improves the performance of communications systems. One of the advantages of this precoding is to allow the operation of subcarriers with low signal-to-noise ratio (SNR) [5].

In this paper, a new technique for dynamic resource allocation for LP-OFDM applications has proposed. The Exploitation of the dynamic allocation for ultra wideband (UWB) systems is a real advantage because the UWB indoor channel varies slowly over time, which reduces the system complexity.

Indeed, the proposing solution deals with the selection of spreading sequences applied to LP-OFDM signals which are based on several criteria such as correlation functions. In fact, the aim is to propose the selection of optimum spreading codes according to these criteria by minimizing jointly the SI and PAPR. Furthermore, this optimized allocation procedure can increase significantly the mean BER of the system.

This paper is organized as follows. In Section 2, the considered LP-OFDM system is described. Section 3 presents the different selection criteria. In Section 4, allocation algorithm is proposed for LP-OFDM systems to reduce jointly SI and PAPR. In section 5, simulation results are discussed and presented in terms of bit error rate. Conclusions are drawn in Section 6.

System Description
The insertion of a linear precoding function in the conventional OFDM system leads to a LP-OFDM system. In this particular form, the term LP-OFDM may also be referred to the Spectrum multicarrier multiple-access (SS-MC-MA) in mobile radio communications [6].

So, the system complexity is not increased significantly with the addition of precoding function. The linear precoding component may be exploited to decrease PAPR of OFDM systems [7]. The linear precoding component makes the communication more robust against the channel selectivity, and provides natural system robustness against narrowband interferers. It provides a finer granularity in the selection of transmission rates.

In the studied LP-OFDM system, each sub-band occupied by a piconet is divided into several sub-blocks. Each one contains a number of subcarriers equal to the length L of the spreading codes in Figure 1.

Expressions of LP-OFDM Signals
The linear precoding operation is performed before the OFDM modulation. It can be written as

$$S = F_S^H D C X$$

Where $S$ is the matrix of $N$ OFDM symbols, each one is composed of $N$ time samples. $X$ is the matrix of BICM symbols to be transmitted. $C$ is the linear precoding matrix. $D$ is a distribution matrix used to allocate the data on the frequency grid called chip mapping matrix. Finally, $F_S$ is the Fourier matrix.

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The matrix of output symbols of the OFDM modulator can be reformulated and becomes:

$$\begin{bmatrix}
C_i & 0 & X_1 \\
C_b & X_b \\
0 & C_b & X_b
\end{bmatrix}$$

where $B$ is the number of sub-blocks of subcarriers in the subband with $B \times L = N$. $C_b$ is the matrix containing the $N_L$ pre-coding sequences of the sub-block $b$ ($b \in \{1 \ldots B\}$). $X_b$ is the matrix of $N_L$ vectors $N_s$ complex symbols transmitted in the sub-block $b$.

### Choice of Linear Precoding Matrix

Codes Walsh-Hadamard is generated from the Sylvester-Hadamard transform matrix. They correspond to the rows or columns of the orthogonal matrix ($L \times L$) constructed recursively as follows:

$$H_L = \begin{bmatrix}
H_{L/2} & H_{L/2} \\
H_{L/2} & -H_{L/2}
\end{bmatrix} \quad \forall L = 2^n, \ n \in \mathbb{N}^*, H_1 = +1$$

These Codes used in synchronous applications systems Multi-Carrier Code Division Multiple Access (MC-CDMA) or LP-OFDM because of the facility to generate them. So we use these codes in the precoding matrix of the LP-OFDM.

The matrix of precoding $C_b$ will correspond to the $N_L \times L$ columns of $H_L$ ($N_L \leq L$).

### Selection Criteria of Codes

#### Self-interference

The choice of orthogonal codes for LP-OFDM system overcomes the SI. This is true if the transmission of the data is considered carried out on a Gaussian channel but it is not it any more if the transmission is carried out through a multipath channel. Indeed, in this case, the orthogonality between the spreading codes is broken by the distortions introduced by the multipath channel. It is then necessary to try to minimize this term SI at reception by the implementation of single-user detection techniques.

#### The PAPR and the crest factor (CF)

The A multicarrier technique is a suitable solution for the transmission of signals over multipath channels. However, the amplitude of the signal LP-OFDM has strong fluctuations. The PAPR allows estimating the ratio between the power peak and the average power of the generated signal. The amplitude of the fluctuations is evaluated by the CF defined by:

$$CF(S(t)) = \sqrt{\frac{\text{PAPR}(S(t))}{\text{PNU}(S(t))}} = \max \left| \frac{(S(t))^2}{S(t)} \right|$$

In practice, it is desired to transmit a signal with a maximum output power without distortion which leads to a degradation of system performance. The technique of selecting low crest factor sequences can remedy to this problem. Hence the interest is to search for OFDM systems the spreading codes with low PAPR value.

### Minimizing SI

Estimate $\hat{y}_{n,j}$ of the $n$th complex symbol $x_{n,j}$ of user $j$:

$$\hat{y}_{n,j} = x_{n,j} \sum_{l=1}^{L} c_l h_{l,n} + \sum_{l=1}^{L} \sum_{p=1}^{N_L} c_l h_{l,n} c_{l,p} g_{l,p} + \sum_{l=1}^{L} c_l h_{l,n}$$

Posing $R(k-l) = [h_{l,k}, h_{l,k-1}, \ldots, h_{l,1}]$, the power of SI associated with the complex symbol $n$ can be written as:

$$P_{SI,n} = \frac{2R(1)}{\beta(1)}\sum_{l=1}^{L-1} w_l^{(n,p)} w_{l+1}^{(n,p)} + \frac{2R(2)}{\beta(2)}\sum_{l=1}^{L-2} w_l^{(n,p)} w_{l+1}^{(n,p)} + \ldots + \frac{2R(L-1)}{\beta(L-1)} w_l^{(n,p)} w_{l+1}^{(n,p)}$$

Or $w_l^{(n,p)} = c_{l,n} c_{l,p}$ is defined as the product chip to chip of the spreading codes allocated to complex symbols $n$ and $p$ in the $l$th chip.

The power of the SI is influenced by the spreading codes and by selecting the used equalization technique. At full load, $N_s=L$, the terms $\beta(i)$ are all negative and the same for each complex symbol. When $N_s < L$, the terms $\beta(i)$ are different depending on the used spreading codes.
Some complex symbols are better over others where the power of the SI will be much more important. Therefore, minimizing the negative term $\beta$ (1) can reduce the power of the SI. This reduction is achieved by judiciously selecting the $N_s$ spreading codes to use.

The use of Walsh-Hadamard codes implies that $N_c=L$. Let's denote $\Omega$ the a spreading code family composed of $N_c$. $\Omega_{NL}$ a subset of $\Omega$ compound $N_c$ Codes with $N_L < N_c$. The $J_{\Omega NL}$ is define as a function such as:

$$J_{\Omega NL} = \max_{n,p \in \Omega_{NL}, n \neq p} I(n, p) \quad (7)$$

Where $I^{(n,p)}$ is the function of interference produced by the sequence $p$ on sequence $n$. The $J_{\Omega NL}$ term takes into account the maximal degradation produced by two spreading sequences. The interference term $I^{(n,p)}$ is defined by:

$$I^{(n,p)} = T(W^{(n,p)}) \quad (8)$$

where $W^{(n,p)}$ is a vector of $L$ elements $w_l^{(n,p)}c_n c_p (l \in [1, \ldots, L])$ resulting chip to chip produced between the $n$ and $p$ spreading sequences, $T(v)$ defines the number of transitions between the elements of the vector $v$:

$$T(v) = \frac{1}{2} \sum_{l=1}^{L-1} |\text{sgn}(v_{l+1}) - \text{sgn}(v_l)| \quad (9)$$

Thus, the minimization $J_{\Omega NL}$ to preserve a subset of $N_L$ sequences for which the various vectors $W^{(n,p)}$ presents a maximum number of transitions. The selection of the optimum subset of spreading sequences is thus defined by:

$$\Omega_{NL}^{opt} = \arg \min_{\Omega_{NL}} J_{\Omega NL} \quad (10)$$

So this method can widely select the spreading codes to obtain an optimal system LP-OFDM. The principle of this complementary selection criterion is used for a BER=10^-3 the gain is $E_b / N_0=0.66$ dB in the case of the criterion of the standard deviation and second order but the gain is reduced to $E_b / N_0=0.33$ dB in the case of the mean criterion. So, According to this figure 3, they are the two criteria which are more optimal: the criterion of the standard deviation and the criterion of the second order.

**Simulation Results**

The performance are given for the simulation chain LP-OFDM in the case of a coding rate $R=1/2$ and a minimum mean square error (MMSE) detection on the channel CM1.

![Error probability curve for LP-OFDM L=16](image)

**Figure 2:** Example LP-OFDM system performance comparison in the case of a good and bad selection of the spreading codes obtained with $L=16$, $N_s=8$ and $N_s=15$.  

\[ W^{(n,p)} = W^{(n,p)}_1, W^{(n,p)}_2, \ldots, W^{(n,p)}_{L-2}, W^{(n,p)}_{L-1} \]

**Minimizing Joint SI and PAPR**

The algorithm of minimization joint power SI and PAPR or peak factor is made by steps detailed as follows:

- **Step 1:** Select the best complementary selection criteria whether the standard deviation: STD or The second order: 2nd order
- **Step 2:** Apply the complementary selection criteria already chosen earlier can get more optimal subsets
- **Step 3:** Calculate the optimal PAPR for each subset
- **Step 4:** Select the optimal subset having the minimum PAPR.

![Error probability curve for LP-OFDM L=16](image)

**Figure 4:** shows a comparison of performance between an optimum
selection using the second order criterion, minimizing SI only and the second criterion minimizing PAPR.

This dual minimization is applied to different load $N_L$. It shows an improvement in performance compared to the conventional criterion. Indeed, the Figure 4 shows an acceptable and variable gain according to load $N_L$. The best profit is shown for the low load $N_L<L$ but when $N_L$ increases towards $L$, the performance difference decreases until the limiting case where $N_L=L$ because SI tends towards 0. Consequently, the optimal subsets are equal. In this case the application of PAPR has no influence and the performance is achieved its best for full load.

**Conclusion**

In this paper, a novel method has proposed which consists of a double selection of spreading code. It can reduce jointly the SI power and the peak factor of the signal. This method show more efficient in terms of performance compared to the conventional method which uses three complementary criterions minimizing only the SI power when the system does not operate with full load.

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