Direct Atomic Simulations of Facet Formation and Equilibrium Shapes of SiC Nanoparticles

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**ABSTRACT:** Understanding the shapes of nanoparticles is an important interdisciplinary problem because particle shapes can affect their properties, functionality, and applications. Advances in nanoscale imaging probes have revealed exquisite details of nanofaceting phenomena. However, quantitative theoretical predictions have not kept up the pace with experimental advances, and the atomic pathways of facet formation are largely unknown due to a lack of direct observations and simulations. Here we examine facet formation in spherical and cubic SiC nanoparticles and in SiC nanowires using molecular dynamics simulations reaching microseconds. We characterize layer-by-layer formation, diffusional motion along edges and corners, and determine energy barriers. We find that the equilibrium shapes are identical regardless of the initial shape of SiC nanoparticles or nanowires. For spherical and cubic nanoparticles, (110) facets form within 10 ns by lateral liquid-like diffusion of atoms. In contrast, faceting in SiC nanowires also involves normal diffusional motion with a higher energy barrier and hence much longer faceting times. These results have important implications for molecular-level understanding of the synthesis and stability of ceramic nanocrystals and nanowires.

**INTRODUCTION**

Ceramic nanocrystals such as SiC are widely used in electronics,\(^1\) photonics,\(^7\) biosensors, drug delivery,\(^3,4\) and structural applications.\(^5\) Silicon carbide is attractive due to its high mechanical strength. Accordingly, mechanisms and transitions during mechanical loading of silicon carbide have been studied in experiments\(^6,7\) and molecular simulations.\(^8,9-11\) On the nanoscale, the shape of crystals directly affects their properties.\(^12-15\) Despite advances in nanoscale imaging\(^16-20\) and modeling, the detailed atomic mechanisms of nanocrystal formation has not been directly observed in experiments or simulation.\(^16,21,22\) The transformation of a crystalline particle from any initial shape to its equilibrium crystal shape involves a series of complex processes.\(^23-26\) The final equilibrium shape has facets resulting from the minimization of surface free energy for a given volume.\(^27\) The equilibrium shape of a nanocrystal is uniquely determined by the Wulff construction\(^28\) according to the surface free energy associated with all crystal directions, resulting in certain planes being preferred. For instance, the expected equilibrium shape for a crystal with (110) planes having the lowest surface energy is a rhombic dodecahedron, possibly truncated by other facets if they have sufficiently low surface energy to intersect at the edges or corners. At finite temperature, a facet can grow in either the lateral or normal direction via the formation of steps and kinks. The latter results from the diffusion of adatoms from edges and corners.\(^29\) The edges and corners between facets can become rounded, but the dominant facets remain intact.\(^30\)

The formation of a fully grown step or layer may require multiple events to occur, and involve energy barriers that prevent the particle from reaching its equilibrium shape if the surface area of the facet is sufficiently large.\(^31,32\) In the absence of step-producing defects, Mullins\(^32\) has shown that the nucleation energy for growing layers on a facet is prohibitively large and the particle may become kinetically immobilized if the facet is larger than a nanometer. Kinetic Monte Carlo simulations have revealed a similar nucleation barrier.\(^33\) However, the detailed atomic mechanisms of facet formation in nanocrystals have not yet been observed experimentally or computationally with a model where all atomistic mechanisms are available. In this article, we show that facet formation on a ceramic, silicon carbide, can be obtained in direct molecular simulations.
dynamics simulations, and study the detailed mechanisms involved in the faceting process.

RESULTS AND DISCUSSION

Here we examine how spherical, cubic, and cylindrical silicon carbide nanoparticles in vacuum undergoing volume-preserving shape changes reach the same equilibrium shape by different dynamical mechanisms, crossing significantly different energy barriers over time scales varying by 3 orders of magnitude. Figure 1 shows how a (110) facet forms in an SiC particle that was initially a sphere of diameter 8 nm. In (a), we see (110) facets, and also island-like (111) facets. In the final configuration, the mean distance from the center of the particle to the (110) planes is 3.73 nm and to the (111) plane 3.90 nm, which by Wulff construction gives the ratio of surface energies \( E_{110}/E_{111} = 0.956 \), and that the equilibrium shape is a rhombic dodecahedron truncated by a regular octahedron. Colors in (a–c) indicate layer depth on one of the (110) facets, and correspond to the colors in (d,e). (d) scatters the height distribution of particles in the 5 top layers of the crystal through time, and shows that the interplay between rows on the facet is important in the faceting process. (e) shows the numbers of particles in each layer of the colored facet through time, and guides the interpretation of (d). (d,e) only shows the number of atoms in the crystal layers on the facet indicated by colors in (a–c), and thus, even though the number of atoms of the particle as a whole is conserved, the number of atoms in (e) is not conserved.

Figure 1. Faceting of silicon carbide nanoparticles. (a–c) Snapshots of silicon carbide nanoparticle (n-SiC) with diameter 8 nm faceting during a molecular dynamics simulation. (a) Initial configuration taken at 0.02 ns, (b) partly faceted particle after 139 ns, and (c) fully faceted particle after 400 ns. In (b) and (c), we see (110) facets, and also island-like (111) facets. In the final configuration, the mean distance from the center of the particle to the (110) planes is 3.73 nm and to the (111) plane 3.90 nm, which by Wulff construction gives the ratio of surface energies \( E_{110}/E_{111} = 0.956 \), and that the equilibrium shape is a rhombic dodecahedron truncated by a regular octahedron. Colors in (a–c) indicate layer depth on one of the (110) facets, and correspond to the colors in (d,e). (d) scatters the height distribution of particles in the 5 top layers of the crystal through time, and shows that the interplay between rows on the facet is important in the faceting process. (e) shows the numbers of particles in each layer of the colored facet through time, and guides the interpretation of (d). (d,e) only shows the number of atoms in the crystal layers on the facet indicated by colors in (a–c), and thus, even though the number of atoms of the particle as a whole is conserved, the number of atoms in (e) is not conserved.
Between the facets on the n-SiC, there are edges and corners along which surface Si and C diffuse with diffusion constants around $3.1(2) \times 10^{-6}$ cm$^2$/s and $4.4(3) \times 10^{-6}$ cm$^2$/s, respectively.

To examine the effect of the initial nanocrystal shape, we also simulated a cubic nanocrystal with length 8 nm and faces in the (001) directions, and a cylindrical nanocrystal of diameter 4 nm and length 8 nm along the [011] crystal direction. These were also performed at $T = 2200$ K. The particle shapes are nearly identical for the sphere and the cube after 1 $\mu$s, but the cylindrical particle differs. Figure 2 shows the initial shapes (a–c), the final shapes (d–f), and the fraction of the surface area being (110) or (111) facets (g) for the sphere, the cube, and the cylinder. Just like the sphere, the cube transforms into a nanocrystal with 12 (110) and 8 (111) facets. In Figure 2g, we use the facet area fraction as an indication of the facet formation. We observe that this fraction stabilizes in 0.1 $\mu$s for the cube and 0.6 $\mu$s for the sphere. The cylindrical nanoparticle also develops (110) and (111) facets, and its facet area fraction stabilizes after 0.3 $\mu$s, but the shape of this nanoparticle is different from the other ones even after 1 $\mu$s. Note that the faceting times are not directly comparable since the nanoparticles have different volumes.

To investigate the faceting of the cylindrical nanocrystal in more detail, we plot the distance between opposing (110) planes. This, along with snapshots of the particle at various stages of the faceting formation, is shown in Figure 3. We again observe the initial faceting phase of 0.3 $\mu$s. During this time, pairs of facets inclined with respect to the major axis move closer to each other, reaching approximately the same value (5.5 nm) after 0.1 $\mu$s. The planes normal to the major axis converge to a higher separation distance (6.3 nm) after 0.3 $\mu$s. However, the distance between the facet pair parallel to the major axis remains constant through 1 $\mu$s at 2200 K. These are the largest facets. The volume freed by facet pairs only moving toward each other is taken up as lateral growth of facets, ultimately resulting in the formation of corners. Lateral movement and facet area growth result in the formation of two relatively sharp (100) corners, which can be seen in the snapshot after 1 $\mu$s.

The oblate shape of the nanocrystal has to be metastable because it is asymmetric in the (110) planes. Contrary to the sphere and the cube, the cylinder has reached a shape where it cannot get closer to the equilibrium shape by removing atoms from a layer and using them for lateral growth of other facets. It has to grow new layers on top of the largest facets to get closer to equilibrium, and at this point, it seems stuck in a metastable state. In order to kick the system out of its metastable shape, the temperature is raised to 2361 K to see whether it reaches the equilibrium shape. This heating causes a shape change, as can be seen in the shaded part of Figure 3. After 200 ns at 2361 K, all facet pairs converge to same separation distance, and the particles reach the equilibrium shape. The dark blue facet pair takes about 0.2 $\mu$s before it also converges to the same separation distance 5.5 nm. The nanocrystal shape is monitored for 0.6 $\mu$s at 2361 K, and we do not observe any changes in the shape of the nanocrystal. The final shape resembles the final shapes of nanocrystals with spherical and cubic initial configurations.

The oblate shape is metastable due to an energy barrier to the normal motion of sufficiently large facets. To estimate the magnitude of this barrier, we measure the growth rate in 63 simulations at varying temperatures between 2275 and 2385 K. These simulations were run between 200 and 500 ns depending on the time needed to grow new layers. We monitor the time dependence of the number of atoms on top of the largest (110) facet in all of these simulations to determine the nucleation time for new layers on the facet as a function of layer depth and temperature. This number abruptly grows when a new layer is nucleated, so it is sharply defined. Figure 4a,b shows how this number develops for four layers growing in a simulation at 2295 K. Figure 4c shows the waiting times for a single layer height for all simulations. From this Arrhenius plot, we estimate the energy barrier for each layer height; see Figure 4d. This barrier is estimated to 14 eV for the first four layer heights on top of the metastable oblate shape.

### CONCLUSIONS

This study demonstrates that processes such as faceting and crystal growth can be within the reach of microsecond molecular dynamics simulations. Here, we have provided insights into the detailed faceting mechanisms of SiC. The results and methods are of general importance in the synthesis of nanocrystals and nanowires. Other materials and processes should be studied using similar approaches to gain insight into what mechanisms are general and what are specific to SiC.

Molecular dynamics studies of faceting also open up for more detailed studies of crystal growth procedures and how they are related to the resulting nanocrystal geometry. They may also let us address competing processes between crystal growth and deformation during healing and recrystallization of faceting systems experiencing external mechanical forcing.

### METHODS

SiC-3C was prepared with a lattice constant of 4.358. To prepare initial nanocrystals, we created a block of bulk SiC-3C in a cubic...
simulation box of (40 nm)$^3$ (sphere), (30 nm)$^3$ (cube), or (23.4 nm)$^3$ (cylinder), and then deleted atoms that were outside the region defined by the geometrical shape of that initial nanocrystal. This method can lead to nonstoichiometry, which we amended by adding particles to the void to regain stoichiometry. We performed molecular dynamics simulations of the silicon carbide nanocrystal (see, e.g., ref 35 for best practices of MD simulations). We used a force field consisting of two-body and three-body terms. Simulations were run with periodic boundary conditions using an NVT Nosé–Hoover type thermostat with a damping time of 1 ps. Equations of motion were integrated with the Velocity Verlet scheme using a time step of 2 fs. The simulation box sizes were such that the nanocrystal did not interact with its periodic image. All simulations were run on NVIDIA P100 computing cards using the GPU package in LAMMPS. Diffusion coefficients were calculated using the mean squared displacement of the top three surface layers over 100 ps.

ASSOCIATED CONTENT

Supporting Information
The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.cgd.9b00612. Brief descriptions of how the energy barriers for normal growth on facets were measured, and details of facet evolution on cylindrical n-SiC (PDF)

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Notes
The authors declare no competing financial interest.

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