Future perspectives for a weak mixing angle measurement in coherent elastic neutrino nucleus scattering experiments.

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After the first measurement of the coherent elastic neutrino nucleus scattering (CENNS) by the COHERENT Collaboration, it is expected that new experiments will confirm the observation. Such measurements will allow to put stronger constraints or discover new physics as well as to probe the Standard Model by measuring its parameters. This is the case of the weak mixing angle at low energies, which could be measured with an increased precision in future results of CENNS experiments using, for example, reactor antineutrinos. In this work we analyze the physics potential of different proposals for the improvement of our current knowledge of this observable and show that they are very promising.

PACS numbers: 13.15.+g, 12.15.-y

I. INTRODUCTION

Neutrinos are one of the most elusive particles. With a small cross section, its detection has been always a challenge for the experimentalist. Despite this difficult task, neutrino physics is in a precision era with increasingly accurate measurements \cite{1,2}. Among the

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recent progress in this field is the detection, for the first time, of the coherent elastic neutrino-nucleus scattering (CENNS). This reaction was proposed \cite{5} just after the discovery of the weak neutral currents \cite{6} and recently detected by the COHERENT collaboration \cite{7}. Besides the natural interest in confirming this recent detection, there are different issues that are of current interest in nuclear and neutrino physics. Many new physics scenarios can be probed, as it has been proposed in the case of Non Standard Interactions (NSI) \cite{8,11}, a $Z'$ gauge boson \cite{12,15}, electromagnetic neutrino properties \cite{16,17} and even the case of an sterile neutrino \cite{18,21}. Methods alternative to inverse beta decay (IBD) of reactor neutrino detection can also shed light in the so called reactor neutrino anomaly \cite{22}, as we have pointed out in \cite{18}.

Reactor neutrinos have a great tradition of discoveries, since the first neutrino detection \cite{23} and in the last decades they have played an important role in establishing the three neutrino oscillation paradigm \cite{1}. IBD has been the golden channel in reactor neutrino detection. However there are other interesting neutrino reactions that can also be used to probe neutrino fluxes from reactors, as is the case of elastic neutrino-electron scattering (ENES) detected for the first time in the seventies \cite{24} and measured with increased precision by the TEXONO \cite{25} and MUNU \cite{26} Collaborations; and more recently of CENNS measured at the neutron spallation source by the COHERENT Collaboration \cite{7}. It is expected that in the near future improved measurements of ENES reaction can be provided by the GEMMA experiment \cite{27}.

The expectation for a new measurement of the weak mixing angle in CENNS has already been studied in the past, for example for the case of the TEXONO \cite{17} and the CONUS \cite{28} proposals. Here we focus in the case of the CONNIE \cite{29,31}, MINER \cite{32}, and RED100 \cite{33} research programs and reanalyse the TEXONO and CONUS case studies in order to compare them on an equal footing and to contrast the importance of different characteristics of each experiment. In particular, we note here how sensitivities can depend on the experiment detection targets due to a different protons to neutrons proportion.

The dependence of CENNS cross section on the weak charge $Q_W$ allows the study of the weak mixing angle at extremely low momentum transfer, a region where an improvement in the accuracy of this parameter is very much needed \cite{34,35}, particularly in measurements with neutrino interactions \cite{36}. We will show that, although the sensitivity to the weak charge is relatively small in CENNS, it will be possible to have competitive measurements...
of the $\sin^2 \theta_W$ in the low energy regime if the systematic uncertainties are under control. We will discuss that, besides the importance of high statistics, the proportion of protons to neutrons in a given target will also play an important role.

II. CENNS EXPERIMENTS WITH REACTOR ANTI NEUTRINOS

Several future proposals plan to measure CENNS with increased statistics, opening the possibility to test the Standard Model in the ultra-low energy regime. To study the sensitivity of these proposals to the weak mixing angle, we start by considering the CENNS cross section, given by the following expression [37]

$$\left( \frac{d\sigma}{dT} \right)_{\text{coh}}^{\text{SM}} = \frac{G_F^2 M}{2\pi} \left[ 1 - \frac{M T}{E_\nu^2} + \left( 1 - \frac{T}{E_\nu} \right)^2 \right] \left[ Z g_p^p F_Z(q^2) + N g_n^n F_N(q^2) \right]^2. \quad (1)$$

Here, $M$ is the mass of the nucleus, $E_\nu$ is the neutrino energy, and $T$ is the nucleus recoil energy; $F_{Z,N}(q^2)$ are the nuclear form factors that are especially important at higher momentum transfer, as can be the case of neutrinos coming from spallation neutron sources, while for reactor antineutrinos, they have a minimal impact and will be considered as equal to one in this work. The neutral current vector couplings (including radiative corrections) are given by [37],

$$g_p^p = \rho_{\nu N}^{NC} \left( \frac{1}{2} - 2 \hat{\kappa}_{\nu N} \hat{s}_Z^2 \right) + 2\lambda^{uL} + 2\lambda^{uR} + \lambda^{dL} + \lambda^{dR}$$

$$g_n^n = -\frac{1}{2} \rho_{\nu N}^{NC} + \lambda^{uL} + 2\lambda^{dL} + 2\lambda^{dR} \quad (2)$$

where $\rho_{\nu N}^{NC} = 1.0082$, $\hat{s}_Z^2 = \sin^2 \theta_W = 0.23129$, $\hat{\kappa}_{\nu N} = 0.9972$, $\lambda^{uL} = -0.0031$, $\lambda^{dL} = -0.0025$, and $\lambda^{dR} = 2\lambda^{uR} = 7.5 \times 10^{-5} \text{[38]}."

From the previous expressions for the vector couplings, it is straightforward to note that the dependence on the weak mixing angle appears only on the protons coupling and, therefore, nuclei with larger protons to neutrons proportion could be more sensitive to this measurement. On the negative side, we can also notice that this contribution is small in comparison with the neutron one. Despite this, a high statistics CENNS experiment will be sensitive to this coupling and, therefore, the weak mixing angle can be measured with a precision similar to the one at current measurements in this low energy regime. Currently, most of the
proposals are working with a relatively small amount of material and considering upgrades in the near future. In what follows, we will consider the optimistic case of the upgraded, high statistics, detectors that are the ones that have the possibility to make an accurate measurement.

For estimating the number of expected events (SM) in the detector, we use the expression,

\[ N_{\text{events}}^{\text{SM}} = t \phi_0 \frac{M_{\text{detector}}}{M} \int_{E_{\nu_{\text{min}}}}^{E_{\nu_{\text{max}}}} \lambda(E_{\nu}) dE_{\nu} \int_{T_{\text{min}}}^{T_{\text{max}}(E_{\nu})} \left( \frac{d\sigma}{dT} \right)^{\text{coh}}_{\text{SM}} dT, \]

where \( M_{\text{detector}} \) is the mass of the detector under study, \( \phi_0 \) is the total neutrino flux, \( t \) is the data taking time period, \( \lambda(E_{\nu}) \) is the neutrino spectrum, \( E_{\nu} \) is the neutrino energy, and \( T \) is the nucleus recoil energy. The maximum recoil energy is related to the neutrino energy and the nucleus mass through the relation \( T_{\text{max}}(E_{\nu}) = \frac{2E_{\nu}^2}{M + 2E_{\nu}} \).

In our analysis, in order to forecast the sensitivity of the CENNS experiments, we will use two different approaches: we will perform a \( \chi^2 \) analysis of each proposal, considering that the future experiment will measure the number of events predicted by the Standard Model. To compute this values we will use the predicted value for the weak mixing angle at zero momentum transfer (\( \sin^2 \theta_W = 0.2386 \)). With this value as the test experimental value, we will perform a fit considering different values of the systematic uncertainties, plus the extreme benchmark case of only statistical error. A second approach, also used in the present article, will be the computation of the \( \chi^2 \) function considering the predicted statistical error and the systematics coming from the reactor neutrino spectrum [39], this method has been previously used for the case of ENES experiments [36]. For the reactor neutrino spectrum we will use the expansion discussed in Ref. [22], while for energies below 2 MeV the computations reported in Ref. [40] were considered. In each case we assumed as a benchmark one year of data taking.

As already mentioned above, in our first approach we will consider an analysis based on the function

\[ \chi^2 = \frac{(N_{\text{events}}^{\text{SM}} - N^{\text{th}})^2}{\sigma_{\text{stat}}^2 + \sigma_{\text{syst}}^2}, \]

where the theoretical prediction for the number of events \( N^{\text{th}} \) will depend on the value of the weak mixing angle and we will considered different values for the future systematic error \( \sigma_{\text{syst}} = pN^{\text{th}}/100 \), where \( p \) will be the percentage of systematic uncertainty. For our second approach, we will consider the current level of uncertainty in the reactor antineutrino spectrum as an input.
We have computed the expected number of events taking into account the experimental details of each proposal, summarized in Table I. For the RED100 proposal \cite{33} we consider a 100 kg target of Xe, a material that is currently of great interest for coherent scattering \cite{41} and that has reached a low energy threshold in different tests \cite{42}. A 500 eV threshold is expected in the case of the RED100 experiment. New analyses in this direction are encouraging and it is expected that the detector will perform even better \cite{43}; however, for our analysis we will restrict to this more conservative estimate. The RED100 experiment will be located at the Kalinin power plant. In the case of CONNIE, we consider the most optimistic case of a 1 kg Si detector, with a 28 eV threshold, located at 30 m from the Angra-2 reactor. As for the MINER proposal, we perform our computations considering a detector that will be made of $^{72}$Ge and $^{28}$Si. The proportion between these two materials is of 2 : 1 and the threshold energy is expected to reach 10 eV. The antineutrino source in this case will be a non-comercial TRIGA-type pool reactor that delivers mainly $^{235}$U antineutrinos \cite{44}. We will consider an event rate of 5 kg$^{-1}$ day$^{-1}$ \cite{32} and, as in the case of all other proposals, one year of data taking. For the case of TEXONO, we have considered their proposed High-purity Germanium detectors as a target with the threshold energy $T_{\text{thres}} \sim 100$ eV \cite{45,46} exposed to an antineutrino flux coming from the Kuo-Sheng nuclear power plant. Finally, in the case of the CONUS proposal we follow \cite{28}, where a detector of up to 100 kg of germanium is considered, with a recoil energy threshold as low as 100 eV.

| Proposal | $T_{\text{thres}}$ (eV) | Baseline Z/N | Det. Tec. | Fid. Mass |
|----------|-----------------|--------------|-----------|-----------|
| CONNIE   | 28              | 30 m         | 1.0       | CCD (Si)  |
|          | 0.70            | 1 kg         |           |           |
| RED100   | 500             | 19 m         | 0.70      | Lq.Xe     |
|          | 10.70           | 100 kg       |           |           |
| MINER    | 10              | 1 m          | 0.81  $^{72}$Ge:$^{28}$Si (2:1) | 30 kg |
| TEXONO   | 100             | 28 m         | 0.79      | HPGe      |
|          | 1 kg            | 1 kg         |           |           |
| CONUS    | 100             | 10 m         | 0.79      | HPGe      |
|          | 100 kg          | 100 kg       |           |           |

*TABLE I: List of some experimental proposals to detect CENNS with reactor antineutrinos.*
**FIG. 1:** Expected sensitivity of the RED100(left), CONNIE(center) and MINER(right) detectors to the weak mixing angle. The dotted-dashed line (black) and the dashed line (blue) are the curves considering only statistical errors, and they correspond to a 100% and 50% efficiency, respectively. The case including systematic errors from the reactor neutrino spectra with a 100% efficiency is shown by the solid (black) line.

## III. WEAK MIXING ANGLE SENSITIVITY

With the information given above, we have computed the expected sensitivity to the weak mixing angle, $\sin^2 \theta_W$. We have assumed that the future experimental setups will measure exactly the Standard Model prediction and computed the corresponding fit as mentioned in Eq. (4) for three different cases: (i) when the experiment is capable of an optimal efficiency (100 %), (ii) when it reaches an efficiency of 50 %, and (iii) in the case when we include the current systematic uncertainty corresponding to the theoretical antineutrino flux, with a statistical error corresponding to a 100 % efficiency. We can see the results of this analysis in Fig. (1), where we show the cases of CONNIE [29–31], MINER [32] and the RED100 [33] proposals. For the value of the weak mixing angle, we have considered the extrapolation to the low energy regime:

$$\sin^2 \theta_W(0)_{\text{MS}} = \kappa(0)_{\text{MS}} \sin^2 \theta_W(M_Z)_{\text{MS}}$$

with $\kappa(0) = 1.03232$ [47].

From Fig. (1) we can notice that the perspectives for a precise measurement of the weak mixing angle are promising, and that they are dominated by the systematic error from the reactor spectrum. However, it is expected that this error will be reduced, thanks to the
progress in the current knowledge of the reactor spectrum from its direct measurement at IBD experiments. We can also notice that for the case of the CONNIE collaboration, it will be necessary to have a higher mass detector in order to reduce the statistical error. This is due to the fact that the detector has very low mass and the target material is also lighter. We show in Table II the corresponding 1σ error for sin²θ_W for the three different configurations under discussion. We have also included for comparison the results for CONUS and TEXONO. We can see that the results can be competitive, especially if systematical errors can be reduced.

In order to have a better idea of the dependence of the sensitivity on the systematics, we have plotted in Fig. 2 the expected error on the weak mixing angle, depending on the systematic error that each particular experiment can reach. In this case, we have also included the result for the Texono and the Conus proposals. From this figure, it is possible to see that CONNIE is slightly less affected by the systematics than other experiments. Being an experiment where the proportion of protons to neutrons is higher, this result seems natural, while among Texono and CONUS, the dependence is very similar, since they use the same target material.

### Table II: Expected sensitivity to the weak mixing angle. For each experiment we quote the 1σ expected sensitivity in the case of a 50 % (100%) efficiency of the experiment and for the case of a systematic error equal to that of the current reactor spectrum uncertainty. The results are shown in terms of δ(sin²θ_W) as well as in percent.

| Experiment | δ sin²θ_W | % | δ sin²θ_W | % | δ sin²θ_W | % |
|------------|-----------|---|-----------|---|-----------|---|
| TEXONO     | 0.0015    | 0.6| 0.0011    | 0.5| 0.0028    | 1.2|
| RED100     | 0.0004    | 0.2| 0.0003    | 0.1| 0.0031    | 1.3|
| MINER      | 0.0010    | 0.4| 0.0007    | 0.3| 0.003     | 1.3|
| CONNIE     | 0.0023    | 1.0| 0.0017    | 0.7| 0.003     | 1.3|
| CONUS      | 0.0003    | 0.1| 0.0002    | 0.1| 0.0023    | 1.0|
FIG. 2: Expected sensitivity to $\sin^2 \theta_W$ (in percent) for the different proposals under consideration, depending on the systematic uncertainty to be achieved, in percent. In the left panel is shown the expected error on the weak mixing angle for the experiments under study in Fig. (1). In the right panel are shown TEXONO and CONUS, two proposals that use the same nucleus as a target and, therefore, have a similar dependence.

IV. DISCUSSION AND CONCLUSIONS

The weak mixing angle is one of the fundamental parameters of the Standard Model and it has been measured with great accuracy at the $Z$-pole [38]. At very low momentum transfer there are also measurements of this important quantity, although the precision is lower. The main results in this energy window come from the measurement of the weak charge, such as in the recent measurement by Qweak [51], and from atomic parity violation experiments [38], a measurement that will be improved by the P2 [52], SoLID [53] and Moller [54] experiments. Both measurements are extracted from the weak charge in protons or electrons. The measurement of the weak mixing angle at the low energies in neutrino scattering processes has plenty of room for improvement [36] and the CENNS experiments have the potential to obtain a competitive accuracy, provided that systematic errors can be reduced.

In this work we have computed the expected sensitivity for different CENNS proposals and we have shown the viability of such a measurement with a reasonable accuracy. Moreover, if the systematic errors can be reduced, the measurement of the weak mixing angle from
FIG. 3: Expected sensitivity of CENNS experiments to the weak mixing angle compared with the SM prediction \cite{34, 48}, in the $\overline{MS}$ renormalization scheme. Electron weak charge $Q_W(e)$ comes from Moller scattering \cite{49}, and both the former \cite{50} and recent \cite{51} measurements of the proton weak charge $Q_{Weak(P)}$ are also shown.

CENNS experiments can be even better than the one coming from electron weak charge. We show this potential in Fig (3) the result of Table II is presented in a graphical representation comparing the future measurement of the weak mixing angle in CENNS with current measurements. We can see that the CENNS experiments can really give a good measurement of this observable through a different and new channel.

Acknowledgments

This work was supported by CONACYT-Mexico, SNI (Sistema Nacional de Investigadores), and PAPIIT project IN113916. A. Parada was supported by Universidad Santiago de Cali (USC) under grant 935-621118-3.

[1] P. F. de Salas, D. V. Forero, C. A. Ternes, M. Tortola, and J. W. F. Valle (2017), 1708.01186.
[2] Valencia-Globalfit, http://globalfit.astroparticles.es/ (2018).
[3] I. Esteban, M. C. Gonzalez-Garcia, M. Maltoni, I. Martinez-Soler, and T. Schwetz, JHEP 01, 087 (2017), 1611.01514.
[4] F. Capozzi, E. Lisi, A. Marrone, and A. Palazzo (2018), 1804.09678.
[5] D. Z. Freedman, Phys. Rev. D9, 1389 (1974).
[6] F. J. Hasert et al., Phys. Lett. B46, 121 (1973), [,5.11(1973)].
[7] D. Akimov et al. (COHERENT), Science 357, 1123 (2017), 1708.01294.
[8] J. Barranco, O. G. Miranda, and T. I. Rashba, Phys. Rev. D76, 073008 (2007), hep-ph/0702175.
[9] J. Barranco, A. Bolanos, E. A. Garces, O. G. Miranda, and T. I. Rashba, Int. J. Mod. Phys. A27, 1250147 (2012), 1108.1220.
[10] J. Billard, J. Johnston, and B. J. Kavanagh (2018), 1805.01798.
[11] P. B. Denton, Y. Farzan, and I. M. Shoemaker (2018), 1804.03660.
[12] I. M. Shoemaker, Phys. Rev. D95, 115028 (2017), 1703.05774.
[13] D. K. Papoulias and T. S. Kosmas, Phys. Rev. D97, 033003 (2018), 1711.09773.
[14] Y. Farzan, M. Lindner, W. Rodejohann, and X.-J. Xu, JHEP 05, 066 (2018), 1802.05171.
[15] S.-F. Ge and I. M. Shoemaker (2017), 1710.10889.
[16] T. S. Kosmas, O. G. Miranda, D. K. Papoulias, M. Tortola, and J. W. F. Valle, Phys. Rev. D92, 013011 (2015), 1505.03202.
[17] T. S. Kosmas, O. G. Miranda, D. K. Papoulias, M. Tortola, and J. W. F. Valle, Phys. Lett. B750, 459 (2015), 1506.08377.
[18] B. C. Cañas, E. A. Garcés, O. G. Miranda, and A. Parada, Phys. Lett. B776, 451 (2018), 1708.09518.
[19] T. S. Kosmas, D. K. Papoulias, M. Tortola, and J. W. F. Valle, Phys. Rev. D96, 063013 (2017), 1703.00054.
[20] B. Dutta, Y. Gao, R. Mahapatra, N. Mirabolfathi, L. E. Strigari, and J. W. Walker, Phys. Rev. D94, 093002 (2016), 1511.02834.
[21] E. Garces, B. Cañas, O. Miranda, and A. Parada, J. Phys. Conf. Ser. 934, 012004 (2017).
[22] G. Mention et al., Phys. Rev. D83, 073006 (2011), 1101.2755.
[23] F. Reines and C. L. Cowan, Phys. Rev. 107, 641 (1957).
[24] F. Reines, H. S. Gurr, and H. W. Sobel, Phys. Rev. Lett. 37, 315 (1976).
[25] H. T. Wong et al. (TEXONO), Phys. Rev. D75, 012001 (2007), hep-ex/0605006.
[51] D. Androić et al. (Qweak), Nature 557, 207 (2018).

[52] D. Becker et al. (2018), 1802.04759.

[53] P. A. Souder, Int. J. Mod. Phys. Conf. Ser. 40, 1660077 (2016).

[54] J. Benesch et al. (MOLLER) (2014), 1411.4088.