Measurement of Jet Shapes in High-$Q^2$
Deep Inelastic Scattering at HERA

ZEUS Collaboration

Abstract

The shapes of jets with transverse energies, $E_T^{\text{jet}}$, up to 45 GeV produced in neutral- and charged-current deep inelastic $e^+p$ scattering (DIS) at $Q^2 > 100$ GeV$^2$ have been measured with the ZEUS detector at HERA. Jets are identified using a cone algorithm in the $\eta$–$\varphi$ plane with a cone radius of one unit. The jets become narrower as $E_T^{\text{jet}}$ increases. The jet shapes in neutral- and charged-current DIS are found to be very similar. The jets in neutral-current DIS are narrower than those in resolved processes in photoproduction and closer to those in direct-photon processes for the same ranges in $E_T^{\text{jet}}$ and jet pseudorapidity. The jet shapes in DIS are observed to be similar to those in $e^+e^-$ interactions and narrower than those in $\bar{p}p$ collisions for comparable $E_T^{\text{jet}}$. Since the jets in $e^+e^-$ interactions and $e^+p$ DIS are predominantly quark initiated in both cases, the similarity in the jet shapes indicates that the pattern of QCD radiation within a quark jet is to a large extent independent of the hard scattering process in these reactions.
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1 Introduction

The internal structure of a jet is expected to depend mainly on the type of primary parton, quark or gluon, from which it originated and to a lesser extent on the particular hard scattering process. For cone jet algorithms [1, 2] a useful representation of the jet’s internal structure is given by the jet shape [3]. At sufficiently high jet energy, where fragmentation effects become negligible, the jet shape should be calculable by perturbative Quantum Chromodynamics (pQCD). pQCD predicts gluon jets to be broader than quark jets as a consequence of the gluon-gluon coupling strength being larger than that of the quark-gluon coupling [4]. Measurements of the jet width in $e^+e^-$ interactions at LEP1 have shown that gluon jets are indeed broader than quark jets [5]. The dependence of the structure of quark and gluon jets on the production process can be investigated by comparing measurements of the jet shape in different reactions in which the final-state jets are predominantly quark or gluon initiated.

Measurements of the integrated jet shape were made in $\bar{p}p$ collisions at $\sqrt{s} = 1.8$ TeV using charged particles [6] as well as both neutral and charged particles [7], and a qualitative agreement with $O(\alpha_3^2)$ QCD calculations [8] was found. Measurements of the integrated and differential jet shapes were made in $e^+e^-$ interactions at LEP1 using both neutral and charged particles [9] and were found to be well described by leading-logarithm parton-shower Monte Carlo calculations. It was observed [9] that the jets in $e^+e^-$ are significantly narrower than those in $\bar{p}p$ and most of this difference was ascribed to the different mixtures of quark and gluon jets in the two production processes.

Measurements of the integrated jet shape in quasi-real photon proton collisions at HERA have recently been presented [10] and were found to be well described by leading-logarithm parton-shower Monte Carlo calculations except for the inclusive production of jets with high jet pseudorapidity ($\eta^{\text{jet}}$) and low jet transverse energy ($E_T^{\text{jet}}$). Fixed-order perturbative QCD calculations at the parton level [11] are able to describe the measured jet shapes within the uncertainties on the matching between the theoretical and experimental jet algorithms.

At HERA, jet production has been observed in both neutral- [12, 13] and charged-current [14] deep inelastic ep scattering (DIS) at large $Q^2$ (where $Q^2$ is the virtuality of the exchanged boson). In this paper, measurements of the differential and integrated jet shapes in neutral- and charged-current DIS at $Q^2 > 100$ GeV$^2$ are presented. The data sample used in this analysis has been collected with the ZEUS detector in $e^+p$ interactions at the HERA collider. To compare with measurements of the jet shapes in $\bar{p}p$, $\gamma p$ and $e^+e^-$ collisions, jets are searched for with an iterative cone algorithm [10] with radius $R = 1$ in the pseudorapidity ($\eta^{\text{jet}}$) - azimuth ($\varphi$) plane of the laboratory frame. Jets have been selected with jet transverse (with respect to the proton beam direction) energy $E_T^{\text{jet}} > 14$ GeV and jet pseudorapidity in the range $-2 < \eta^{\text{jet}} < 2$. The jet shape has been measured using the ZEUS calorimeter and corrected to the hadron level. The measurements are presented as functions of $E_T^{\text{jet}}$ and $\eta^{\text{jet}}$. The measured jet shapes are compared to similar measurements in other reactions and to leading-logarithm parton-shower Monte Carlo calculations.

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1 The ZEUS coordinate system is defined as right-handed with the Z-axis pointing in the proton beam direction, hereafter referred to as forward, and the X-axis horizontal, pointing towards the centre of HERA. The pseudorapidity is defined as $\eta = -\ln(\tan(\theta/2))$, where the polar angle $\theta$ is taken with respect to the proton beam direction.
2 Experimental setup

During 1995 and 1996 HERA operated with protons of energy $E_p = 820$ GeV and positrons of energy $E_e = 27.5$ GeV. The ZEUS detector is described in detail in [13, 14]. The main subdetectors used in the present analysis are the central tracking system positioned in a 1.43 T solenoidal magnetic field and the uranium-scintillator sampling calorimeter (CAL). The tracking system was used to establish an interaction vertex and to select neutral- and charged-current DIS events. The CAL is hermetic and consists of 5918 cells each read out by two photomultipliers tubes. Under test beam conditions the CAL has energy resolutions of $18\%/\sqrt{E}$ for electrons and $35\%/\sqrt{E}$ for hadrons. Energy deposits in the CAL were used to identify the scattered positron, to find jets and to measure jet energies. Jet energies are corrected for the energy lost in inactive material in front of the CAL. This material is typically about one radiation length. The effects of uranium noise were minimised by discarding cells in the electromagnetic (EMC) or hadronic (HAC) sections if they had energy deposits of less than 60 MeV or 110 MeV, respectively. A three–level trigger was used to select events online [14, 15, 16].

3 Data selection

Neutral-current (NC) DIS events have been selected offline from the ZEUS 1995 data sample, which corresponds to an integrated luminosity of 6.3 pb$^{-1}$, using criteria similar to those reported previously [17, 18]. The main steps are briefly discussed here. The scattered positron candidate has been identified by using the pattern of energy deposits in the CAL [19]. The energy ($E_{e'}$) and polar angle ($\theta_{e'}$) of the positron candidate have been determined from the CAL measurements. The $Q^2$ variable has been reconstructed by the double-angle method ($Q^2_{DA}$) [20], which uses $\theta_{e'}$ and an angle that corresponds to the direction of the scattered quark in quark-parton model type events. This second angle has been determined from the CAL measurements of the hadronic final state. The following requirements have been imposed:

- A positron candidate of uncorrected energy $E_{e'} > 10$ GeV. This cut ensures a high and well understood positron finding efficiency and suppresses background from photoproduction events, where the scattered positron escapes down the rear beampipe.

- $y_e < 0.95$, where $y_e = 1 - E_{e'}(1 - \cos \theta_{e'})/(2E_e)$. This condition removes events where fake positron candidates are found in the forward region of the CAL.

- The total energy not associated with the positron candidate within a cone of radius 0.7 units in the $\eta - \varphi$ plane around the positron direction must be less than 5 GeV. This condition removes photoproduction and DIS events where part of a jet has been falsely identified as the scattered positron.

- A track is required to match the positron candidate identified in the CAL for $\eta_e < 2$, where $\eta_e$ is the pseudorapidity of the positron candidate. This requirement suppresses cosmic rays, beam-halo muons, photoproduction and DIS events where an electromagnetic shower in the CAL has been falsely identified as the scattered positron.

- For $\eta_e > 2$ the transverse energy of the positron candidate should be larger than 20 GeV. This requirement further reduces the number of fake positrons in the forward region of the CAL.
38 GeV < (E − p_Z) < 65 GeV, where E is the total energy as measured by the CAL, \( E = \sum_i E_i \), and \( p_Z \) is the Z-component of the vector \( \vec{p} = \sum_i E_i \vec{r}_i \); in both cases the sum runs over all CAL cells, \( E_i \) is the energy of the calorimeter cell \( i \) and \( \vec{r}_i \) is a unit vector along the line joining the reconstructed vertex and the geometric centre of the cell \( i \). This cut removes events with large initial-state radiation and further reduces the background from photoproduction.

Events have been removed from the sample if there was a second positron candidate with energy above 10 GeV and without a track match, and the energy in the CAL after subtracting that of the two positron candidates is below 10 GeV. This requirement removes elastic Compton scattering events (\( ep \rightarrow e\gamma p \)).

\( \vec{P}_t / \sqrt{E_t} < 3 \) GeV\(^{1/2} \) where \( \vec{P}_t \) is the missing transverse momentum as measured with the CAL (\( \vec{P}_t \equiv \sqrt{p_X^2 + p_Y^2} \)) and \( E_t \) is the total transverse energy in the CAL. This cut removes cosmic rays and beam-related background.

The vertex position along the beam axis must be in the range \(-30 < Z < 36 \) cm.

\( Q^2_{DA} > 100 \) GeV\(^2 \).

Charged-current (CC) DIS events have been selected offline from the ZEUS 1995 and 1996 data samples, which correspond to an integrated luminosity of 14.8 pb\(^{-1} \), using criteria similar to those reported in [14]. The \( Q^2 \) variable has been determined using the method of Jacquet-Blondel (\( Q^2_{JB} \)) [21], which uses the information from the hadronic energy flow of the event. The following conditions have been imposed:

- \( \vec{P}_t / \sqrt{E_t} > 11 \) GeV. This cut ensures high trigger efficiency.
- \( \vec{P}_t / E_t > 0.5 \). This cut rejects photoproduction and beam-related background.
- The vertex position along the beam axis should lie in the range \(-30 < Z < 36 \) cm.
- At least one track should point to the vertex. This requirement rejects cosmic rays and beam-gas interactions.
- The number of tracks not associated to the vertex must be less than 20% of the total number of tracks. This cut further reduces the background from beam-gas interactions.
- The difference \( \Delta\phi \) between the azimuths of the net transverse momentum as measured by the tracks associated with the vertex and as measured by the CAL has been required to fulfill \( |\Delta\phi| < 1 \) rad. This requirement removes overlays of cosmic rays on ep interactions.
- \( P^\text{tracks}_t / P_t > 0.1 \), where \( P^\text{tracks}_t \) is the net transverse momentum of the tracks associated with the vertex (this condition has not been applied if \( P_t > 25 \) GeV). This cut rejects beam-related background, in which \( P_t \) is pointing to small polar angles, and events with additional non-ep related energy deposits in the CAL (mainly cosmic rays).
- The event has been removed from the sample if there was an isolated positron candidate with energy above 10 GeV and a track match. This condition removes NC DIS events.
- Pattern recognition algorithms based on the topology of the CAL energy distribution were applied to reject cosmic rays and beam-halo muons.
\( Q^2_{\text{corr}} > 100 \text{ GeV}^2 \), where \( Q^2_{\text{corr}} \) denotes the corrected value of \( Q^2_{JB} \) as described in \([14]\). The resolution in the reconstruction of \( Q^2 \) is \( \approx 25\% \).

A search for jet structure using the CAL cells (see Section 5) has been performed on both samples (NC and CC DIS), and events with at least one jet of ‘corrected’ transverse energy (see Section 5) \( E_T^{\text{jet}} > 14 \text{ GeV} \) and \(-1 < \eta^{\text{jet}} < 2\) have been retained. The selected sample of NC (CC) DIS consists of 6926 (231) events containing 7092 (233) jets. In both cases, the background from photoproduction has been estimated using Monte Carlo techniques and was found to be below 1%.

4 Monte Carlo simulation

The response of the detector to jets and the correction factors for the jet shapes have been determined from samples of Monte Carlo (MC) events.

NC and CC DIS events have been generated using the LEPTO program \([22]\) interfaced to HERACLES \([23]\) via DjangO \([24]\). The HERACLES program includes photon and \( Z^0 \) exchanges and first-order electroweak radiative corrections. The CTEQ4D \([25]\) NLO proton parton densities have been used. The hadronic final state is simulated using the colour-dipole model \([26]\) including the leading-order (LO) QCD diagrams as implemented in ARIADNE \([27]\) for the QCD cascade. As an alternative, samples of events have been generated using the model of LEPTO based on first-order QCD matrix elements plus parton-shower (MEPS). For the generation of the samples with MEPS, the soft colour interactions option has been switched off.

In addition, a sample of NC DIS events has been generated using the PYTHIA program \([28]\): a lowest-order electroweak calculation including initial- and final-state QCD radiation in the leading-logarithm parton-shower approximation. In this case, events have been generated using the MRSA \([29]\) set of proton parton densities and the first-order QCD matrix elements have not been included. In all cases, the LUND string model \([30]\) as implemented in JETSET \([28]\) is used for modelling the fragmentation into hadrons.

All MC generated events have been passed through the ZEUS detector and trigger simulation programs \([16]\). They have been reconstructed and analysed by the same program chain as the data.

5 Jet search and energy corrections

An iterative cone algorithm in the \( \eta - \varphi \) plane \([1,2]\) is used to reconstruct jets from the energy measured in the CAL cells for both data and MC generated events, and also from the final-state hadrons for MC generated events. A detailed description of the algorithm can be found in \([10]\). The jets reconstructed from the CAL cell energies are called \( \text{cal} \) jets and the variables associated with them are denoted by \( E_T^{\text{jet}_{\text{cal}}}, \eta^{\text{jet}_{\text{cal}}} \) and \( \varphi^{\text{jet}_{\text{cal}}} \). The axis of the jet is defined according to the Snowmass convention \([2]\), where \( \eta^{\text{jet}_{\text{cal}}} (\varphi^{\text{jet}_{\text{cal}}}) \) is the transverse–energy weighted mean pseudorapidity (azimuth) of all the CAL cells belonging to that jet. The energy sharing of overlapping jets is dealt with using the following procedure. Two jets are merged if the overlapping energy exceeds 75% of the total energy of the jet with the lower energy; otherwise two different jets are formed and the common cells are assigned to the nearest jet. The cone radius \( R \) used in the jet search is set equal to 1.

For the MC generated events, the same jet algorithm is also applied to the final-state particles. The jets found are called \( \text{hadron} \) jets and the variables associated with them are denoted
by \( E_{T,\text{had}}^{\text{jet}}, \eta_{\text{had}}^{\text{jet}}, \) and \( \varphi_{\text{had}}^{\text{jet}}. \) Hadron jets with \( E_{T,\text{had}}^{\text{jet}} > 14 \text{ GeV} \) and \(-1 < \eta_{\text{had}}^{\text{jet}} < 2\) are selected.

The comparison of the reconstructed jet variables between the hadron and the cal jets in MC generated events \[^{[31]}\] shows no significant systematic shift in the angular variables \( \eta_{\text{cal}}^{\text{jet}} \) and \( \varphi_{\text{cal}}^{\text{jet}} \) with respect to \( \eta_{\text{had}}^{\text{jet}} \) and \( \varphi_{\text{had}}^{\text{jet}}. \) However, the transverse energy of the cal jet underestimates that of the hadron jet by an average amount of \( \approx 16\% \) with an r.m.s. of \( 11\%. \) This effect is due mainly to energy losses in the inactive material in front of the CAL and is corrected for using the following procedure. The transverse energy corrections to cal jets averaged over the azimuthal angle are determined using the samples of MC generated events \[^{[31]}\]. These corrections are constructed as multiplicative factors, \( C(E_{T,\text{cal}}^{\text{jet}}, \eta_{\text{cal}}^{\text{jet}}), \) which, when applied to the \( E_T \) of the cal jets, give the ‘corrected’ transverse energies of the jets, \( E_T^{\text{jet}} = C(E_{T,\text{cal}}^{\text{jet}}, \eta_{\text{cal}}^{\text{jet}}) \times E_{T,\text{cal}}^{\text{jet}} \[^{[31]}\].

6 Jet shape

The differential jet shape is defined as the average fraction of the jet’s transverse energy that lies inside an annulus in the \( \eta - \varphi \) plane of inner (outer) radius \( r - \Delta r/2 \) \((r + \Delta r/2)\) concentric with the jet defining cone \[^{[3]}\]:

\[
\rho(r) = \frac{1}{N_{\text{jets}}} \frac{1}{\Delta r} \sum_{jets} \frac{E_T(r - \Delta r/2, r + \Delta r/2)}{E_T(0, R)},
\]

where \( E_T(r - \Delta r/2, r + \Delta r/2) \) is the transverse energy within the given annulus and \( N_{\text{jets}} \) is the total number of jets in the sample. The differential jet shape has been measured for \( r \) values varying from 0.05 to 0.95 in \( \Delta r = 0.1 \) increments. The integrated jet shape defined by

\[
\psi(r) = \frac{1}{N_{\text{jets}}} \sum_{jets} \frac{E_T(0, r)}{E_T(0, R)}
\]

is also used. By definition, \( \psi(R) = 1 \). It has been measured for \( r \) values varying from 0.1 to 1.0 in \( \Delta r = 0.1 \) increments.

The following procedure is used to reconstruct the differential jet shape from the CAL cells in data and MC generated events: for each jet the sum of the transverse energies of the CAL cells assigned to the jet, \( E_{T,\text{cal}}(r - \Delta r/2, r + \Delta r/2) \), with a distance \( r' = \sqrt{(\Delta \eta)^2 + (\Delta \varphi)^2} \) to the jet axis between \( r - \Delta r/2 \) and \( r + \Delta r/2 \) is determined and divided by \( E_{T,\text{cal}}(0, R) \). The differential jet shape as measured with the CAL, \( \rho_{\text{cal}}(r) \), is then defined in analogy with eq. \(^{[1]}\), where the sum now runs over all the cal jets in the selected sample and \( N_{\text{jets}} \) is the total number of cal jets in the sample. Similarly, the integrated jet shape as measured with the CAL, \( \psi_{\text{cal}}(r) \), is defined in analogy with eq. \(^{[2]}\).

The same jet shape definition as used above for the CAL cells is applied to the final-state particles in the case of MC generated events and the resulting differential (integrated) jet shape is denoted by \( \rho_{\text{had}}^{\text{MC}}(r) \) \((\psi_{\text{had}}^{\text{MC}}(r))\).

6.1 Jet shape correction

The differential and integrated jet shapes as measured with the CAL are corrected back to the hadron level using the samples of MC generated events. The corrected differential and integrated jet shapes, \( \rho(r) \) and \( \psi(r) \), refer to jets at the hadron level with a cone radius of one unit in the \( \eta - \varphi \) plane. The measurements are given for jets with \( E_T^{\text{jet}} > 14 \text{ GeV} \) and \(-1 < \eta^{\text{jet}} < 2\) in the kinematic region \( Q^2 > 100 \text{ GeV}^2 \).
The corrected jet transverse energy is used only to select the sample of jets \(E_{T}^{jet} > 14\ \text{GeV}\) and to study the dependence of the jet shape as a function of \(E_{T}^{jet}\). The reconstructed jet shapes are then corrected for acceptance and smearing effects using the samples of MC generated events. The correction factors also take into account the efficiency of the trigger, the selection criteria, the purity and efficiency of the jet reconstruction, and the effects of the energy losses due to inactive material in front of the CAL. The corrected differential (integrated) jet shape is determined bin-by-bin as 

\[
\rho(r) = G_{MC}^{cal}(r) \cdot \rho_{cal}(r) \quad \text{and} \quad \psi(r) = F_{MC}^{cal}(r) \cdot \psi_{cal}(r),
\]

where the correction factors are defined as 

\[
G_{MC}^{cal}(r) = \frac{\rho_{MC}^{had}(r)}{\rho_{MC}^{cal}(r)} \quad \text{and} \quad F_{MC}^{cal}(r) = \frac{\psi_{had}^{MC}(r)}{\psi_{cal}^{MC}(r)}
\]

and are determined separately for each region of \(\eta^{jet}\) and \(E_{T}^{jet}\).

For this approach to be valid, the uncorrected jet shapes in the data must be described by the MC simulations at the detector level. As shown later, this condition is satisfied by the ariadne and MEPS simulations in all \(\eta^{jet}\) and \(E_{T}^{jet}\) regions studied. The samples of events generated with ariadne are used to correct the jet shapes. The correction factors \(G_{MC}^{cal}(r)\) do not show a strong dependence on \(\eta^{jet}\) or \(E_{T}^{jet}\) and vary between 0.7 and 1 for \(r \geq 0.15\). The correction factors for the integrated jet shape \(F_{MC}^{cal}(r)\) differ from unity by less than 25% for \(r \geq 0.2\). Close to the centre of the jet the correction factor \(G_{MC}^{cal}(r = 0.05) \equiv F_{cal}^{MC}(r = 0.1)\) is large and varies between 1.4 and 1.7 depending on \(\eta^{jet}\) and \(E_{T}^{jet}\).

The jet shapes have been also reconstructed using tracks instead of CAL cells both in data and MC generated events. Since the use of tracks gives an improved spatial resolution for the transverse-energy flow of the charged particles within a jet, this study provides a cross-check of the resolution in \(r\) for the jet shape reconstructed using the CAL. The resulting corrected jet shapes are consistent with those using the CAL cells within the uncertainties of the measurements (see next section).

### 6.2 Systematic uncertainties

A detailed study of the sources contributing to the systematic uncertainties of the measurements has been carried out [32]. The uncertainties have been classified into four groups:

- The energy corrections to the jets and the correction functions to the jet shapes in NC and CC DIS have been evaluated using the MEPS generator. The changes induced in \(\rho(r)\) are typically below 10%.

- The absolute energy scale of the \(cal\) jets in the MC generated events has been varied by \(\pm 3\%\). The resulting corrected \(\rho(r)\) changes typically by less than 3%.

- Variations in the simulation of the CAL response to low-energy particles yielded changes in \(\rho(r)\) typically below 3%.

- Variations in the simulation of the trigger and a variation of the cuts used to select the data within the ranges allowed by the comparison between data and MC simulations resulted in negligible changes in the corrected jet shapes.

For the measurements of jet shapes in NC DIS, the statistical errors are negligible compared to the systematic uncertainties. Conversely, the statistical errors dominate in the CC DIS analysis. The total positive (negative) systematic uncertainty on \(\rho(r)\) at each value of \(r\) has been determined by adding in quadrature the positive (negative) deviations from the central value. The systematic uncertainties have been added in quadrature to the statistical errors and are shown as error bars in the figures.
Results

7.1 Jet shapes in DIS

The differential and integrated jet shapes are measured for jets in the reactions

\[ e^+ p \rightarrow e^+ (\nu) + \text{jet} + X \]

with \( Q^2 > 100 \text{ GeV}^2 \). Jets are required to have \( E_T^{\text{jet}} > 14 \text{ GeV} \) and \(-1 < \eta^{\text{jet}} < 2 \). There are 6018, 855 and 53 events in the NC DIS data sample with \( Q^2 \) in the range 100 – 1000 GeV\(^2\), 1000 – 5000 GeV\(^2\) and 5000 – 25000 GeV\(^2\). The corresponding numbers for the CC DIS data sample are 84, 123 and 24 events.

Jet shapes in NC DIS

The measured differential jet shapes in NC DIS for different regions in \( \eta^{\text{jet}} \) and \( E_T^{\text{jet}} \) are shown in Figures 1 and 2, respectively. The differential jet shape exhibits a prominent peak at the centre of the jet. It decreases by a factor \( \approx 40 \) from the centre of the jet (\( r = 0.05 \)) to the edge of the jet (\( r = 0.95 \)). Figure 3 shows the measured average fraction of the jet’s transverse energy that lies inside an inner cone of radius \( r = 0.5 \) concentric with the jet defining cone, \( \psi(r = 0.5) \), as functions of \( \eta^{\text{jet}} \) and \( E_T^{\text{jet}} \). Note that \( \psi(r = 0.5) \) has been measured in ranges of \( E_T^{\text{jet}} \) and the data points in Figure 3 (lower plot) are located at the weighted mean in each \( E_T^{\text{jet}} \) range. It is observed that the jets become narrower as \( E_T^{\text{jet}} \) increases. The measured \( \psi(r = 0.5) \) exhibits no significant dependence on \( \eta^{\text{jet}} \).

The predictions of ARIADNE, MEPS and PYTHIA are compared to the measured jet shapes in Figures 1 to 3. The predicted jet shape of the colour-dipole model (ARIADNE) describes the measured jet shape well in all \( \eta^{\text{jet}} \) and \( E_T^{\text{jet}} \) regions considered. The predicted jets of PYTHIA tend to be narrower at low \( E_T^{\text{jet}} \) than those in the data (see Figure 3). In the case of MEPS, the predicted jets show a tendency to be broader at low \( \eta^{\text{jet}} \) than those in the data.

Jet shapes in CC DIS

The results for \( \rho(r) \) in CC DIS for different regions of \( E_T^{\text{jet}} \) are shown in Figure 4. The differential jet shape shows similar general features to those of the jets in NC DIS. Figure 5 shows the measured \( \psi(r = 0.5) \) as functions of \( \eta^{\text{jet}} \) and \( E_T^{\text{jet}} \). The measured \( \psi(r = 0.5) \) exhibits no significant dependence on \( \eta^{\text{jet}} \) and its dependence on \( E_T^{\text{jet}} \) is similar to that observed in NC DIS. The predictions of ARIADNE and MEPS (see Figures 4 and 5) provide a reasonable description of the measured jet shape.

The measured jet shapes in NC DIS are compared with those in CC DIS in Figure 6 and found to be very similar in each region of \( E_T^{\text{jet}} \). Measurements of the ratio of the differential jet shapes in CC and NC DIS, \( \rho^{\text{CC}}(r)/\rho^{\text{NC}}(r) \), for the same regions of \( E_T^{\text{jet}} \) as above are also shown in Figure 6 (lower part of each plot) and found to be compatible with unity. In these measurements some of the systematic uncertainties common to NC and CC DIS cancel. The median of the \( Q^2 \) distribution has been determined for the NC and CC DIS samples of jets in each \( E_T^{\text{jet}} \) region: 310 GeV\(^2\) (450 GeV\(^2\)) for 14 < \( E_T^{\text{jet}} \) < 21 GeV, 710 GeV\(^2\) (1000 GeV\(^2\)) for 21 < \( E_T^{\text{jet}} \) < 29 GeV, 1260 GeV\(^2\) (1600 GeV\(^2\)) for 29 < \( E_T^{\text{jet}} \) < 37 GeV and 2000 GeV\(^2\) (2200 GeV\(^2\)) for 37 < \( E_T^{\text{jet}} \) < 45 GeV in the NC (CC) DIS samples of jets. Some differences are observed in the \( Q^2 \) distributions of the two processes for a given range in \( E_T^{\text{jet}} \). As a cross-check, the jet shapes in NC and CC DIS have been measured in a common region of \( Q^2 \) for each range in \( E_T^{\text{jet}} \) and no significant difference has been found. Therefore, the observation that the jet
shapes in NC and CC DIS are very similar, for the same range of $E_T^{jet}$, is independent of the different $Q^2$ distributions in these processes.

7.2 Comparison to jet shapes in photoproduction

In photoproduction, two types of QCD processes contribute to jet production at LO [33, 34]: either the photon interacts directly with a parton in the proton (direct process) or the photon acts as a source of partons which interact with those in the proton (resolved process). It has been noted that resolved processes dominate jet photoproduction in the entire $E_T^{jet}$ region studied [31]. In the case of dijet photoproduction the contributions of resolved and direct processes can be separated [35] by using the variable $x_{\gamma}^{OBS} = (\sum_{jets} E_T^{jet} \cdot e^{-\eta^{jet}})/(2E_\gamma)$, where the sum runs over the two jets of highest $E_T^{jet}$ and $E_\gamma$ is the initial photon energy. This variable represents the fraction of the photon’s momentum participating in the production of the two jets with highest $E_T^{jet}$. The LO direct and resolved processes largely populate different regions of $x_{\gamma}^{OBS}$, with the direct processes being concentrated at high values.

In Figure 7 the measured integrated jet shape in NC DIS are compared to those in dijet photoproduction [10] for two different regions: $x_{\gamma}^{OBS} \geq 0.75$ and $x_{\gamma}^{OBS} < 0.75$. The comparison between the jet shapes in NC DIS and dijet photoproduction is made for the same ranges of $\eta^{jet}$ and the $E_T^{jet}$ spectrum is similar in these two processes. The jets produced in NC DIS are narrower than those in dijet photoproduction but closer to those dominated by direct processes ($x_{\gamma}^{OBS} \geq 0.75$). This comparison can be understood in terms of the large fraction of final-state quark jets expected in NC DIS ($e^+q \rightarrow e^+q$) and direct processes in photoproduction (dominated by the subprocess $\gamma g \rightarrow q\bar{q}$). The remaining differences may be attributed to the contribution from the direct subprocess $\gamma q \rightarrow qg$ and that of resolved processes, in which the jets are broader as shown by the measurements in dijet photoproduction with $x_{\gamma}^{OBS} < 0.75$.

7.3 Comparison to measurements in $e^+e^-$ and $\bar{p}p$ collisions

The measured jet shape in NC (CC) DIS with $Q^2 > 100$ GeV$^2$ for jets with transverse energy between 37 and 45 GeV, with a mean of 40 GeV (41 GeV), is compared to the measurements of the jet shape corrected to the hadron level in $\bar{p}p$ collisions by CDF [6] and DØ [7] and in $e^+e^-$ interactions by OPAL [8]:

- The CDF data [6] have been obtained using an iterative cone algorithm with $R = 1$ similar to that used here. The measurements shown are for jets with transverse energy between 40 and 60 GeV, with a mean of 45 GeV, and pseudorapidity $0.1 < |\eta^{jet}| < 0.7$. The contribution to the jet shape due to the underlying event was found to be small [2]. If a jet shares more than 75% of its energy with a jet of higher energy, the two are merged together; otherwise, they are defined as distinct and the particles common to both jets are assigned to the nearest jet.

- The DØ data [7] have been obtained also using an iterative cone algorithm with $R = 1$ similar to that used here. The jet direction was defined according to a convention different from that of Snowmass; however, this difference is not expected to have a significant effect on the results [30]. The jet shape has been measured for jets with transverse energy between 45 and 70 GeV, with a mean of 53 GeV, and pseudorapidity $|\eta^{jet}| < 0.2$. The jet shape has been corrected to remove the small contribution due to the underlying event.

\[ \text{In NC and CC DIS the underlying event is not expected to contribute in the kinematic region studied here.} \]
Two jets were merged if more than 50% of the $E_T$ of the jet with smaller $E_T$ was contained in the overlap region; otherwise, the two jets were not merged and each particle in the overlap region was assigned to the nearest jet.

- The OPAL data [9] have been obtained using a cone algorithm especially designed to emulate that of the CDF measurements, i.e. defining the cone in the $\eta - \phi$ plane, using $R = 1$, demanding $|\eta^{jet}| < 0.7$ and measuring the transverse energy flow. The jet shape has been measured for jets with energy greater than 35 GeV, with a mean of 40.4 GeV. The $e^+e^-$ data have no underlying event. Overlapping jets are treated using the same procedure as CDF.

The measured differential jet shapes in NC and CC DIS are compared to that measured in $e^+e^-$ interactions in Figure 8 and are found to be similar. The ratio of the differential jet shapes in NC DIS and $e^+e^-$ interactions, $\rho^{NC}(r)/\rho^{e^+e^-}(r)$, is also shown in Figure 8 (lower part of the figure) and is found to be compatible with unity within the uncertainties of the DIS measurements, which are dominant. For the selected samples of jets, the jet shapes in $e^+e^-$ interactions and DIS are expected to be similar due to the large fraction of final-state quark jets in these two processes. However, some differences may appear since there are configurations of colour flow (for example, that of initial-state QCD radiation) in DIS which are not present in $e^+e^-$. The striking similarity in the jet shapes indicates the large extent to which the pattern of QCD radiation within a quark jet is independent of the hard scattering process in these reactions.

The measured integrated jet shapes in DIS are compared to those in $e^+e^-$ interactions and $\bar{p}p$ collisions in Figure 9. The measured jets in DIS at HERA are found to be narrower than those in $\bar{p}p$ collisions. The measurements in $\bar{p}p$ collisions have been performed for jets with slightly higher energy than those in NC and CC DIS. This difference cannot explain the discrepancy in the jet shapes since the jets become narrower as the jet energy increases. As stated in [9], most of the difference between the jet shapes in $e^+e^-$ interactions and $\bar{p}p$ collisions can be ascribed to the larger fraction of gluon jets in the latter reaction. The comparison between the measured jet shapes in DIS and $\bar{p}p$ collisions suggests that, also in this case, the difference can be attributed to differences between quark and gluon jet properties.

### 8 Summary and conclusions

Measurements have been presented of the differential and integrated jet shapes in neutral- and charged-current deep inelastic $e^+p$ scattering at $\sqrt{s} = 300$ GeV using data collected by ZEUS in 1995 and 1996. The jet shapes refer to jets at the hadron level with a cone radius of one unit in the $\eta - \phi$ plane and are given for the kinematic region $Q^2 > 100$ GeV$^2$. Jets with $E_T^{jet} > 14$ GeV and $-1 < \eta^{jet} < 2$ have been considered. The jets become narrower as $E_T^{jet}$ increases. No significant $\eta^{jet}$ dependence of the jet shape has been observed. The measured jet shapes in neutral- and charged-current DIS are found to be very similar.

The measurements of jet shapes have been compared to the predictions of Monte Carlo generators using different models for the QCD radiation. The colour-dipole model as implemented in ARIADNE provides a reasonable description of the measured jet shapes in all $\eta^{jet}$ and $E_T^{jet}$ regions studied. The parton-shower approach without first-order QCD matrix-elements predict jets which are slightly narrower at low $E_T^{jet}$ than those in the data for all the $\eta^{jet}$ regions studied. The inclusion of first-order QCD matrix-elements improves the description of the data for $\eta^{jet} > 1$, but leads to jets which are slightly broader for $\eta^{jet} < 1$. 

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The jets in neutral-current DIS are narrower than those in dijet photoproduction but closer to those in direct-photon processes for the same ranges in jet transverse energy and pseudorapidity. The jets in DIS are found to be narrower than those in $\bar{p}p$ collisions. This difference can be attributed to a larger contribution of gluon jets in $\bar{p}p$ collisions. The measured jet shapes in neutral- and charged-current DIS are similar to those in $e^+e^-$ interactions for comparable ranges of jet transverse energy. Since the jets in $e^+e^-$ interactions and deep inelastic $e^+p$ scattering are predominantly quark initiated, the similarity in the jet shapes indicates that the pattern of QCD radiation within a quark jet is to a large extent independent of the hard scattering process in these reactions.

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Figure 1: Measured differential jet shapes corrected to the hadron level, $\rho(r)$, in neutral-current DIS with $Q^2 > 100 \text{ GeV}^2$ for jets with $E_{T}^{jet}$ above 14 GeV in different $\eta^{jet}$ regions (black dots). The error bars include the statistical and systematic uncertainties added in quadrature (typically smaller than the dots). The predictions of PYTHIA (dotted lines), ARIADNE (solid lines), and MEPS (dashed lines) are shown for comparison. The predictions have been obtained by an integration over the same bins as for the data and are presented as smooth curves joining the calculated points.
Figure 2: Measured differential jet shapes corrected to the hadron level, $\rho(r)$, in neutral-current DIS with $Q^2 > 100$ GeV$^2$ for jets in the $\eta^{jet}$ range between $-1$ and 2 in different $E_T^{jet}$ regions (black dots). The error bars include the statistical and systematic errors added in quadrature. The predictions of PYTHIA (dotted lines), ARIADNE (solid lines), and MEPS (dashed lines) are shown for comparison. The predictions have been obtained by an integration over the same bins as for the data and are presented as smooth curves joining the calculated points.
Figure 3: The measured integrated jet shape corrected to the hadron level at a fixed value of $r = 0.5$, $\psi(r = 0.5)$, as a function of $\eta_{\text{jet}}$ (upper plot) and $E_{T,\text{jet}}$ (lower plot), in neutral-current DIS with $Q^2 > 100$ GeV$^2$ for jets with $E_{T,\text{jet}} > 14$ GeV in the $\eta_{\text{jet}}$ range between $-1$ and $2$ (black dots). The error bars include the statistical and systematic errors added in quadrature. The predictions of PYTHIA (dotted lines), ARIADNE (solid lines), and MEPS (dashed lines) are shown for comparison. The predictions have been obtained by an integration over the same bins as for the data and are presented as smooth curves joining the calculated points.
Figure 4: Measured differential jet shapes corrected to the hadron level, $\rho(r)$, in charged-current DIS with $Q^2 > 100 \text{ GeV}^2$ for jets with $-1 < \eta^{\text{jet}} < 2$ in different $E_T^{\text{jet}}$ regions (black dots). The predictions of ARIADNE (solid lines) and MEPS (dashed lines) are shown for comparison. The predictions have been obtained by an integration over the same bins as for the data and are presented as smooth curves joining the calculated points.
Figure 5: The measured integrated jet shape corrected to the hadron level at a fixed value of $r = 0.5$, $\psi(r = 0.5)$, as a function of $\eta^{jet}$ (upper plot) and $E_T^{jet}$ (lower plot), in charged-current DIS with $Q^2 > 100$ GeV$^2$ for jets with $E_T^{jet} > 14$ GeV in the $\eta^{jet}$ range between $-1$ and $2$ (black dots). The inner error bars represent the statistical errors of the data, and the outer errors bars show the statistical and systematic uncertainties added in quadrature. The predictions of ARIADNE (solid lines) and MEPS (dashed lines) are shown for comparison. The predictions have been obtained by an integration over the same bins as for the data and are presented as smooth curves joining the calculated points.
Figure 6: Measured differential jet shapes corrected to the hadron level, $\rho(r)$, in charged-current DIS with $Q^2 > 100$ GeV$^2$ for jets with $-1 < \eta^{jet} < 2$ in different $E_T^{jet}$ regions (open circles). The measured jet shapes corrected to the hadron level for jets in neutral-current DIS with $Q^2 > 100$ GeV$^2$ with $-1 < \eta^{jet} < 2$ are shown for comparison (open squares). Measurements of the ratio $\rho^{CC}(r)/\rho^{NC}(r)$ are shown underneath each plot. The inner error bars represent the statistical errors of the data, and the outer error bars show the statistical and systematic uncertainties added in quadrature.
Figure 7: Measured integrated jet shape corrected to the hadron level, $\psi(r)$, in neutral-current DIS with $Q^2 > 100$ GeV$^2$ for jets with $E_T^{jet}$ above 14 GeV and $-1 < \eta^{jet} < 2$ (black dots). The measured jet shape corrected to the hadron level for jets in dijet photoproduction with $E_T^{jet}$ above 14 GeV and $-1 < \eta^{jet} < 2$ is shown for comparison: for dijet production with $x_{\gamma}^{OBS} < 0.75$ (stars) and for dijet production with $x_{\gamma}^{OBS} \geq 0.75$ (open circles).
Figure 8: Measured differential jet shapes corrected to the hadron level, $\rho(r)$, in neutral-(charged-) current DIS with $Q^2 > 100$ GeV$^2$ and a median of 2000 GeV$^2$ (2200 GeV$^2$) for jets with $\eta^{jet}$ in the range between $-1$ and $2$ and $37 < E_T^{jet} < 45$ GeV are shown as squares (open circles). The measurements in CC DIS have been obtained for the same values of $r$ as those in NC DIS, and for an easier comparison the measurements are plotted at $r + 0.025$. The measurements of the jet shape in $e^+e^-$ interactions by OPAL (black dots) is shown for comparison. The ratio of differential jet shapes in NC DIS and $e^+e^-$ interactions, $\rho^{NC}(r)/\rho^{e^+e^-}(r)$, is shown in the lower part of the figure.
Figure 9: Measured integrated jet shapes corrected to the hadron level, $\psi(r)$, in neutral-(charged-) current DIS with $Q^2 > 100$ GeV$^2$ for jets with $\eta^{\text{jet}}$ in the range between $-1$ and $2$ and $37 < E_T^{\text{jet}} < 45$ GeV are shown as stars (diamonds). The measurements of jet shapes in $\bar{p}p$ collisions by CDF (triangles) and DØ (circles) and in $e^+e^-$ interactions by OPAL (squares) are shown for comparison.