OBTAINING THE KINEMATICS SOLUTION OF AN AERIAL MANIPULATOR USING THE SHUFFLED FROG-LEAPING ALGORITHM

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This paper concentrates on deriving the real-time kinematics solution of a manipulator attached to an aerial vehicle, while the vehicle’s movement itself is not analyzed. The manipulator kinematics solution using Denavit-Hartenberg model was introduced, too. The fundamental scope of this paper is to get a global online solution of the design configurations with a weighted objective function subject to some constraints. Adopting the resulted forward kinematics equations of the manipulator, the trajectory planning problem turns into an optimization task. Several and well-known computing methods are documented in the literature for solving constrained complicated nonlinear functions, where in this study a shuffled frog-leaping algorithm (SFLA) is suggested, which is one of the artificial intelligence techniques and regarded as a search method. It is a constrained metaheuristic and population-based approach. Moreover, it is able to solve the inverse kinematics problem considering the mobile platform, in addition to avoiding singularities, since it does not demand the inversion of a Jacobian matrix. Simulation experiments were carried out for the trajectory planning of a six degree-of-freedom (DOF) aerial manipulator, and the obtained results confirmed the feasibility and effectiveness of the suggested method.

Keywords: inverse kinematics, metaheuristics methods, evolutionary algorithms, techniques, shuffled frog-leaping algorithm.

Introduction

The inverse kinematics (IK) solver is a primary problem in robotic manipulation, particularly when demand real-time and precision in calculations. Mathematically, the numerical solution of kinematics is intricate because of the high degree of nonlinearity. Furthermore, the Linear and dynamic programming techniques usually fail or reach local optimum in solving NP-hard problems with a large number of variables and nonlinear objective functions. Moreover, Traditionally Jacobian-based solutions are identified to scale inadequately with the high number of degrees of freedom (DOF) [1] in addition to singularities existence. In contrast [2] presented a comparative study of several methods based on the Jacobian matrix, clarifying that the modified Levenberg-Marquardt method is much better for a quite large set of random configurations than others but may lose convergence compared to Jacobian transpose and Pseudocode inverse methods. Recently many researchers [3] proposed a new method for solving real-time IK without using the Jacobian matrix based on the position of end-effector (ee), using numerical and analytical mathematical tools but not mentioned exactly the performance as the time consuming to get the solution, in [4] also applied alike method for \((2n + 1)\) DOF hyper-redundant manipulator arm. Authors in [5] combined two methods as a real-time IK solver for a human-like arm manipulator based on closed-form analytical equations for a given position while others [6] presented an online adaptive strategy based on the Lyapunov stability theory in addition to Radial Basis Function Network (RBFN) and quadratic programming which requires a complex hardware resources, the simulation was done for the position of ee in addition to avoid obstacles and was conducted on the 7-DOF PA-10 robot manipulator. In [7] a kinematic and time-optimal trajectory planning was considered for redundant robots, two approaches were presented, joint space decomposition and a numerical null-space method for a given pose. They were tested by 7-DOF industrial robots and demand high consuming time for resolving IK. Now metaheuristics optimization algorithms are an encouraging alternative approach to traditional IK techniques due to their strong performance on challenging and high-DOF problems in many various domains, the solution can be solved by minimizing an objective function. [8, 9] proposed an SFLA and MSFLA respectively, that for a high dimensional continuous function optimization. These methods yield a strong robustness and best convergence also presented a comparative study for PSO, SFLA, MSFLA, and MSFLA-EO. Which designated that MSFLA is better than others. In [10] a modified SFLA was assumed for obtaining the optimum preventive maintenance scheduling of generating units in power system. While [11] presented a comparative study
Proposed Optimization Techniques for solving kinematics

The evolutionary optimization algorithms can solve the complicated nonlinear equations completely and efficiently. The solution of the inverse kinematics for the manipulator is a very difficult problem to obtain by traditional approaches. Besides, the suggested strategies do not require the inversion of any Jacobian matrix, and then it avoids singularities configurations. In this paper, two algorithms are used to optimize this problem, the differential evolution and the modified shuffled frog-leaping algorithms. In general, this optimization technique is based on the forward kinematics equations, which always produces a solution in cooperation with an objective function. Hence, the general aspect of the problem can be expressed as minimizing \( J(\Theta) \), constrained by \( \Theta_{\min} \leq \Theta \leq \Theta_{\max} \). Furthermore, the objective function could be defined as the weighted sum of the errors as follows

\[
J(\Theta) = \sum_{i} w_i |\epsilon_i| + \lambda \sum_{i} \epsilon_i^2
\]

where \( \epsilon_i = \text{error}_i \) and \( \lambda \) is a weighting factor.

Table 1. Link parameters of the manipulator’s arm-part

| Modified denavit hartenberg | Standard denavit hartenberg |
|-----------------------------|-----------------------------|
| \( a_{i-1} \) | \( a_i \) [cm] | \( d_i \) [cm] | \( \theta_i \) | Initial value of \( \theta_i \) | Joint offset |
| \(-\pi/2\) | \( l_0 \) | 0 | \( \theta_1 \) | \( \pi/2 \) | \(-\pi/2\) |
| \( \pi/2 \) | \( l_1 \) | 0 | \( \theta_2 \) | \( -\pi/2 \) | \( \pi/2 \) |
| 0 | \( l_2 \) | 0 | \( \theta_3 \) | \( -\pi/2 \) | \( \pi/2 \) |
| \(-\pi/2\) | 0 | \( l_3 + l_4 \) | \( \theta_4 \) | 0 | \( \pi/2 \) |
| \( \pi/2 \) | 0 | 0 | \( \theta_5 \) | \( -\pi/2 \) | \( \pi/2 \) |
| \(-\pi/2\) | \( l_5 \) | 0 | \( \theta_6 \) | 0 | 0 |

The space of all joint variables is referred to as the joint-space \( \Theta=[\theta_1, \theta_2, \ldots, \theta_6]^T \). Here we have been concerned with computing the Cartesian space representation from the knowledge of the joint-space information. Hence the homogeneous transformations of the links were used \( ^iT \). If the robot’s joint-position sensors are estimated by servomechanisms, the Cartesian position and orientation of the hand-part can be computed by \( ^6T \) [12].

Manipulator Kinematics

In order to determine the relationship between the coordinate frames, which are assigned to robots’ links and joints, homogeneous transformations are required. Three parameters are employed to describe the rotation while another three parameters are used to define the translation. Accordingly, the Denavit-Hartenberg (DH) convention was used to describe kinematically the rigid motion by assigning the values of four quantities for each link, two describe the link itself, and two describe the link’s connection to a neighboring link. Where \( \theta, a, d \) and \( \alpha \) are the joint angle, link length, link offset and link twist between joints. While \( T_i \) is the homogeneous transformation matrix between the frames that is a function of \( \theta \) while the other three parameters are constant. The data in Table 1 represent link parameters of the arm-part based on DH strategy in two formulas: standard and modified DH. Whereas the standard simulation form of LabVIEW Robotics module was used, in order to validate the design. The position of all links of an arm-part manipulator can be specified with a set of 6 joint variables from the shoulder’s joints till wrist’s joints. This set of variables is often referred to as a 6×1 joint vector [12].
\[
J(\Theta) = \sigma P_{error}(\Theta) + \varepsilon O_{error}(\Theta) = \\
= \sigma \|P_G - P_k(\Theta)\| + \varepsilon \|O_G - O_k(\Theta)\|.
\]

Where \(P_{error}(\Theta)\) and \(O_{error}(\Theta)\) represent the position and orientation errors respectively and could be computed as a difference in distance between the target and current position, in this work we used an Euclidean formula as a representation of distance. While the parameters \(\sigma\) and \(\varepsilon\) are the weights of the position and the orientation, respectively. Let 
\(G = (P_G, O_G)\) be a given target end-effector pose while 
\(E(\Theta) = (P_k(\Theta), O_k(\Theta))\) is the current end-effector pose in the workspace corresponding to configuration \(\Theta = [\theta_1, \theta_2, \ldots, \theta_n]^T\) which can be calculated using forward kinematics, where \(P\) refers to the 3D position vector of pose while \(O\) refers to the vector of Roll-Pitch-Yaw Euler angles of pose (in radians), respectively. Which the optimization algorithms are exploring directly in the configuration space of the manipulator. Hence, each individual \(\Theta_i = [\theta_{i1}, \theta_{i2}, \ldots, \theta_{in}, \ldots, \theta_{in}, \ldots]\\)

represents the position and orientation error between where the end-effector would be at configuration \(\Theta_i\) and the target end-effector pose. In order to enforce joint limits, each dimension \(j\) of element \(\Theta_i\) should be limited to searching in the range of valid joint angles \(\Theta_i \in [\Theta_{\text{min}}, \Theta_{\text{max}}]\). This can be realized by clamping each dimension \(j\) within these bounds at each iteration immediately after it is updated.

**Modified Shuffled Frog-Leaping Algorithm**

The shuffled frog-leaping algorithm (SFLA) was developed by Eusuff and Lansey in 2003 [8]. It is a member of the Memetic algorithm family, a particular type of meta-heuristic optimization approaches and evolutionary algorithms, which is based on population. It is inspired by the memetic evolution of frogs exploring food in a lake, which consolidates the benefits of the genetic-based memetic algorithms (MAs) and by the social behavior-based particle swarm optimization [9]. generally, the SFLA incorporates two alternating processes: a local exploration in the sub-memplex and a global information exchange among all memeplexes. The SFLA optimization achievement basically relies on two facts, the first one is the evolution process on each memeplex that embraces different cultures of frogs, where the culture stimulates a fitness value, and serves as a local search within memeplex analogous to PSO algorithm which imitates the social behavior of the leaping action of frogs searching for food. The second fact is an idea held within each frog which can be influenced by the ideas of other frogs from other memeplexes throughout the shuffling rule, this animates the cooperation process which it implies an adaptation idea and improves the success rate of discovering the solution in the optimization puzzle. In this process, a modification was applied to the frog-leaping action that enhances the exploration manner in the space [10, 11]. Moreover, the randomization strategy in the evolution process provides the algorithm the ability to discover the local best solution within search space stochastically in addition to the communication process that possibly finds a global optimum solution in shorter time. The local search and the shuffling processes continue until the defined convergence criteria are satisfied. The pseudocode of the algorithm is presented in Algorithm 1.

The MSFLA meta-heuristic strategy is summarized in the following steps:

a. Initialization step, construct the population \(NP\) of frogs randomly similar to the first step in DE algorithm, then Select \(m\), and \(n\), where \(m\) is the number of memeplexes and \(n\) is the number of frogs in each memeplex. Therefore, the total amount of frogs \(NP\) can be calculated as \(NP = mn\), additionally, the \(i\)th frog is expressed as a vector with a dimension equal to the configuration space as follows 
\(\Theta_i = (\Theta_{i1}, \Theta_{i2}, \ldots, \Theta_{in}), i = 1, 2, \ldots, NP\).

b. Rank step, compute the performance value \(f_i\) for each frog \(\Theta_i\). Sort the \(NP\) frogs in a descending order according to their fitness. Save them in an array \(U = \{f_i, \Theta_i\}; i = 1, 2, \ldots, NP\\), so that \(i = 1\) denotes the frog with the best performance value and could save it as a \(\Theta_g\) in each iteration while the algorithm is running.

c. Partition Step, partition array \(U\) into \(m\) memeplexes \(Y_1, Y_2, \ldots, Y_m\), each including \(n\) frogs, such that
\(Y^k = \{\Theta^k_i, f^k_i | \Theta^k_i = \Theta_{(k + m(i-1))}\}; k = 1, \ldots, m\).

In this process, the first frog goes to the first memeplex, the second frog goes to the second memeplex, frog \(m\) goes to the \(m\)th memeplex, and frog \(m+1\) goes back to the first memeplex, etc.

d. Memetic Evaluation step, evolve each memeplex \(Y^k; k = 1, \ldots, m\) according to the frog-leaping
Algorithm 1. The pseudo-code of the Shuffled Frog-Leaping Algorithm

Initialization:
Population ← \{Θ₁, Θ₂, ..., Θ_j, ..., Θ_{np}\};
m ← number of memeplexes;
n ← quantity of frogs in each memeplex;
l ← 1, iN
while (convergence criteria is satisfied Or until met iN) do
  Rank Step: Evaluate each frog Θ_j using a fitness function;
  Partition Step:
  Construct an array U of frogs and their fitness’s values;
  Sort the array U in descending order based on the fitness column;
  Construct (U^k; k = 1, ..., m) memeplexes each including n frogs;
  Evaluation Step:
  for ℓ ← 1, iM do
    for k ← 1, m do
      Determine the worst and best frogs position based on their fitness’s values;
      Improve the worst frog position using a leaping distance;
    end for
  end for
  Shuffle Memeplexes Step: combine the evolved memeplexes;
  Check Convergence: Update the population best frog’s position Θ_g;
  l ← l + 1;
end while

Simulation Results and Discussions

In this work, we solved the inverse kinematics of a redundant manipulator with six joints to follow a destination pose. The manipulator’s joints correspond to the variable θ_j : j = 1, 2, ..., 6 are constrained. The DH table is presented in Table 1. In the inverse kinematics experiments, the desired end-effector pose for the arm-part of the manipulator was determined by this vector

\[ G = (P_e, O_e) = (x, y, z, roll, pitch, yaw) = (-20, 3, 40, 0, 10, 15). \]

Moreover, the parameters of the objective function were adjusted as follows \( ε = 1 - σ = 0.7 \), so there is a balance between position and orientation to be optimized. In case of MSFLA, the parameters of the algorithm were introduced in Table 2, and a summary of the results of utilizing the algorithm for multiple scenarios was introduced in Table 3.
Table 2. Setting of the MSFL Algorithm

| \( m \) | Number of memeplexes | \( n \) | Number of frogs within memeplexes | \( C_L \) | Amount of Leaping |
|-------|----------------------|-------|----------------------------------|-------|-----------------|
| 3     |                      | 1.3   |                                  |       |                 |

Hereafter, Fig. 1 displays the values of the objective function, while Fig. 2 and Fig. 3 represent the position and orientation of the manipulator’s end-effector after applying the solutions to validate IK solver.

Table 3. Inverse Kinematics Results of MSFL Algorithm

| Tests | Population | \( iN \) | \( iM \) | \( J(\Theta) \) | Total Error | Execution Time [ms] | Reaching Target 
\((x, y, z, roll, pitch, yaw)\) |
|-------|------------|---------|---------|----------------|-------------|---------------------|----------------|
| 1     | 20         | 30      | 10      | 11.618         | 29.71       | 729                 | \((-15.7365, 5.43, 52.57, 6.63, 12.66, 16.164)\) |
| 2     | 30         | 30      | 10      | 7.6614         | 12.08       | 1045                | \((-21.183, 2.915, 50.77, -0.201, 10.01, 14.85)\) |
| 3     | 40         | 30      | 15      | 10.5382        | 19.21       | 1685                | \((-25.08, 8.56, 46.81, -6.2, 9.6, 5.4251)\) |
| 4     | 40         | 40      | 30      | 18.4625        | 18.46       | 4526                | \((-25.23, 8.34, 47.59, -2.53, 8.62, 14.13)\) |
| 5     | 60         | 40      | 30      | 8.2925         | 8.292       | 6645                | \((-24.46, 0.0421, 44.59, 1.65, 11.16, 14.05)\) |
| 6     | 80         | 50      | 40      | 11.024         | 11.02       | 13540               | \((-26.998, 3.594, 42.87, -0.068, 9.81, 15.67)\) |
| 7     | 100        | 60      | 60      | 29.774         | 29.77       | 24191               | \((-20.03, 30.039, 39.971, -7.71, 3.679, -0.72)\) |
| 8     | 130        | 70      | 60      | 0.1511         | 0.649       | 46282               | \((-20.09, 2.99, 40.004, 0.208, 9.64, 14.89)\) |
| 9     | 170        | 60      | 50      | 0.6168         | 2.168       | 40459               | \((-20.151, 2.84, 40.09, 0.89, 10.36, 16.15)\) |
| 10    | 200        | 90      | 40      | 0.1139         | 0.298       | 57362               | \((-19.927, 3.0072, 39.98, -0.134, 10.105, 14.89)\) |
| 11    | 200        | 100     | 60      | 0.0729         | 0.378       | 92779               | \((-20.002, 2.998, 39.99, -0.137, 10.151, 14.92)\) |
| 12    | 200        | 120     | 80      | 2.7672         | 5.8164      | 150246              | \((-20.48, 4.153, 40.49, 0.807, 4.087, 13.787)\) |
| 13    | 200        | 200     | 100     | 2.6713         | 1.9339      | 318481              | \((-19.27, 2.235, 41.94, -0.979, 10.88, 11.48)\) |
| 14    | 250        | 90      | 40      | 0.003          | 0.016       | 69818               | \((-19.99, 3.00023, 39.99, 0.0049, 10.006, 14.99)\) |
| 15    | 250        | 140     | 80      | 1.266          | 6.553       | 215027              | \((-20.3, 40, -7.01976e -10, 10.15)\) |
| 16    | 250        | 140     | 100     | 4.647e-9       | 1.05e-8     | 260325              | \((-20.09, 2.97, 40.0008, -1.687, 6.689, 13.57)\) |
| 17    | 300        | 140     | 80      | 1.01e-9        | 3.33e-9     | 255989              | \((-20.3, 40, 1.1648e -9, 10.15)\) |
| 18    | 500        | 90      | 40      | 5.49e-10       | 9.9e-10     | 136888              | \((-20.3, 40, -1.6626e -11, 10.15)\) |
| 19    | 500        | 200     | 100     | 3.02e-15       | 1.56e-14    | 681646              | \((-20.3, 40, 3.22962e -15, 10.15)\) |
| 20    | 1000       | 30      | 45      | 0.0968         | 0.025       | 95197               | \((-20.031, 3.04, 40.04, -0.0037, 10.96, 14.876)\) |

Fig. 1. The objective function values after applying IK-MSFLA solver

Fig. 2. The end-effector position of the manipulator after applying the solutions to validate IK-MSFLA solver
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В данном исследовании предлагается модифицированный алгоритм прыжка лягушки (SFLA), который является одним из методов искусственного интеллекта и рассматривается как метод поиска. Это ограниченный метаэвристический и популяционный подход. С его помощью представляется возможным решение обратной кинематической задачи с учетом мобильности платформы. Кроме того, данный метод предотвращает появление сингулярных точек, поскольку он не требует инверсии матрицы Якоби. Результаты экспериментального моделирования для планирования траектории манипулятора с шестью степенями свободы подтвердили целесообразность и эффективность предлагаемого метода.

Ключевые слова: манипулятор, обратная кинематика, метаэвристические методы, эволюционный алгоритм, методы оптимизации, алгоритм прыжка лягушки.

Получено 12.09.2018