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Engineered Magnetization Dynamics of Magnonic Nanograting Filters

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Abstract: Magnonic crystals and gratings could enable tunable spin-wave filters, logic, and frequency multiplier devices. Using micromagnetic models, we investigate the effect of nanowire damping, excitation frequency and geometry on the spin wave modes, spatial and temporal transmission profiles for a finite patterned nanograting under external direct current (DC) and radio frequency (RF) magnetic fields. Studying the effect of Gilbert damping constant on the temporal and spectral responses shows that low-damping leads to longer mode propagation lengths due to low-loss and high-frequency excitations are also transmitted with high intensity. When the nanowire is excited with stronger external RF fields, higher frequency spin wave modes are transmitted with higher intensities. Changing the nanowire grating width, pitch and its number of periods helps shift the transmitted frequencies over super high-frequency (SHF) range, spans S, C, X, Ku, and K bands (3–30 GHz). Our design could enable spin-wave frequency multipliers, selective filtering, excitation, and suppression in magnetic nanowires.

Keywords: magnonic filters; magnetization; width-modulation; nanowires

1. Introduction

Spin signal processing such as filtering, frequency multiplication, and excitation in GHz bands could enable on-chip integration for compact microwave data communication, data storage, as well as information transfer in ferromagnetic waveguides [1,2]. Many of these functionalities could be established within the same physically defined structure via magnonic crystals (MCs) on the nanoscale. MC are spin waveguides that can be rationally designed [3] or dynamically reconfigured [4] for functional spin transfer by engineering the voltage or magnetic field induced spin-wave dispersion dynamics. Spin-wave eigenmodes in magnetic nanomaterials are the outcomes of spin-wave dispersion effects originating from the total effective magnetic field arising from an exchange, geometry related, anisotropy, and external excitation terms [5,6]. Several methods have been implemented to produce the desired spin transmission spectra. Realizing a geometry-driven energy band gap formation allows enabling several prominent features to emerge, such as guided information carrier by periodic arrays of nanostrips [7,8] and width–modulated nanogratings [9–12]. Besides that spatial periodic variation of saturation magnetization, alternating nanostrips, filters, and phase shifters were investigated with different material classes [8,13–16], where Y3Fe5O12 (YIG) and permalloy were the common types for MC. YIG provides lower damping and low loss propagation of spin-waves [1,17]. Permalloy is an optically reflective magnetic metal with higher saturation magnetic moment which makes this material useful for Kerr and Brillouin light scattering microscopy [9,10,12,18].

Magnonic crystals could provide spin-wave band-pass [19] or band-reject [12,17] spectral filtering through their magnon band gaps. MC width variation leads to the modulation of the spin-wave wavevectors, and consequently to the formation of frequency rejection bands in the spin-wave transmission characteristics. Further analysis of the temporal
effects of such nanograting wires is needed in order to understand the contribution of material parameters such as Gilbert damping on the spin-wave dynamics evolution and the spin-wave mode propagation. In addition, geometry parameters are important to consider in terms of their contribution to the time and frequency profiles of the spin-wave dynamics and transmission behavior in MC. Steady state transmission spectrum should also be analyzed in terms of the excitation conditions which are concerned with RF signal frequencies and the bias field conditions.

Here, we model the temporal and spatial magnetization dynamics in nanogratings. The spectrum of spin waves propagating in the MC filter is important to understand the effect of modulation on the overall spectral transmission. Material- and geometry-related parameters concerned with the structure presented here, are worth investigating to evaluate its performance as a nanograting filter. We look at the effect of increasing the excitation frequency of an RF signal applied to the nanowire, which contributes to the excitation of the eigenmode in the structure.

2. Materials and Methods

In this work, Object-Oriented Micromagnetic Framework (OOMMF) simulations were performed on the filter structure shown in Figure 1a. OOMMF solves Landau-Lifshitz-Gilbert (LLG) equation using finite-difference methods [20–23].

\[
\frac{\partial m}{\partial t} = -\gamma m \times H_{\text{eff}} + \alpha m \times \frac{\partial m}{\partial t}
\]

\[
H_{\text{eff}} = H_{\text{ex}} + H_{\text{demag}} + H_{\text{uniaxial}} + H_{\text{DC}} + H_{\text{RF}}
\]

where, \( m \) is the normalized magnetization vector, \( \gamma \) is the gyromagnetic ratio, \( \alpha \) is the Gilbert damping constant. Equation (1) is comprised of two terms: the first term describes the magnetization precession under the presence of an effective magnetic field \( H_{\text{eff}} \) and the second term captures the Gilbert damping effect. The damping term helps reach the minimum energy state by forcing the magnetization to orient itself parallel to the effective field [24]. \( H_{\text{eff}} \) can be written as the sum of the terms: the exchange field \( H_{\text{ex}} \), demagnetization fields \( H_{\text{demag}} \), uniaxial magneto-crystalline anisotropy \( H_{\text{uniaxial}} \) as well as DC and RF external magnetic field terms \( H_{\text{DC}}, H_{\text{RF}} \) as in Equation (2). \( H_{\text{demag}} \) is the demagnetizing field, which provides a major contribution, resulting from shape anisotropy [25].

Here, three main geometric parameters of the nanograting object were investigated in our study by aligning the demagnetizing field along the long axis and in-plane, where the long axis of the nanowire was parallel to the horizontal plane. The micromagnetic simulations have been run under a finite mesh size of \( 5 \times 5 \times 10 \text{ nm}^3 \) with a simulation time step of 2 ps [26], which is sufficient to run the simulation with parametric sweeps. The geometry under test is depicted in Figure 1a: an excitation region of 500 nm length, and this region followed by a finite periodic structure with a grating region in the middle of the nanowire. The total length of the structure has been kept at 1000 nm and the thickness is set to 10 nm. The grating region includes the periodic features with period count \( N \), periodicity \( P \), grating spacing \( W \), and trench width \( L \) as shown in the figure. For further analysis, the effects of geometric dimensions \((W, P, N)\), Gilbert damping parameter, and the RF excitation frequency on the nanowire filter’s magnetization dynamics and its spectral magnetization output were modelled to observe the mode transition behavior in detail.
Figure 1. Filter geometry applied external RF and DC magnetic field regions and transmission along with x-axis magnetization. (a) The simulated nanowire geometry with the orientations of external RF and DC magnetic field (respectively, \( H_{AC} \) and \( H_{DC} \)) excitations (dimensions not to scale). The effect of increasing Gilbert damping coefficient on transient \( M_x \) in (b) time and (c) frequency (for 8–10 ns time window) domains (the rest of the parameters were held fixed).

To observe the spin-wave propagation and magnetization dynamics through the nanograting filter geometry, a 1000 mT external DC magnetic field is applied on the wire along the z-axis. Along with this field, the nanowire is also excited by a 3 GHz, 500 mT amplitude continuous RF sinusoidal external magnetic field in the +x-direction of the red dashed rectangular region. This configuration leads to Forward Volume Spin Waves (FVSWs), which propagate in the magnetized media with an in-plane propagation wave vector \[27,28\]. After applying the DC and RF external magnetic fields, spins will precess and eventually settle along the z-direction again due to damping. Material parameters used in the simulations are saturation magnetization \( M_s = 840 \times 10^3 \) A m\(^{-1}\) and the exchange constant \( (A_{ex}) \) is \( 13 \times 10^{-12} \) J m\(^{-1}\). The uniaxial anisotropy constant \( K_1 \) is 100 J m\(^{-3}\) set along the +z-axis, while Gilbert damping constant \( \alpha = 0.013 \). In this study, the small uniaxial magnetic anisotropy effect \( K_u \) was added to the simulation since it can be present in magnetic materials used in thin film MC. Earlier experimental studies showed that in thin YIG films, perpendicular magnetic anisotropy could arise due to lattice strain \[29\] and in permalloy, growth-induced anisotropy emerges due to off stoichiometry \[30\].

These material constants are close to Permalloy’s parameters. Permalloy’s intrinsic Gilbert damping and uniaxial anisotropy constant \( K_u \) could vary due to surface strain, stoichiometric variations and growth-induced effects. Thus, the change of the spectral and temporal characteristics are investigated for permalloy-like materials.

While investigating the effect of geometry, each parameter is varied in discrete steps while keeping the others fixed. For investigating the effect of damping and RF excitation field frequencies, the geometry has been fixed with \( N = 5, W = 24 \) nm, \( L = 10 \) nm, and \( P = 20 \) nm. For investigating the effect of \( N \), the geometry and excitation conditions are fixed with \( W = 24 \) nm, \( L = 10 \) nm, \( \alpha = 0.013 \) and \( f = 3 \) GHz. For investigating the effect of \( P \), the geometry and excitation conditions are fixed with \( W = 24 \) nm, \( L = 10 \) nm, \( \alpha = 0.013 \) and \( f = 3 \) GHz. The remaining section on the right contains the grating and is also 500 nm fixed in total length. We swept \( P \) and \( N \) parameters and obtained the spectra and
the temporal results accordingly. The grating region changes in length according to the changes in the period length $P$ or the period count $N$. In all cases, the overall length of the right region is fixed at 500 nm so that the total length of the structure is fixed at 1000 nm. The average magnetization dynamics of the spin-wave components of the overall structure were calculated in the time domain and Fourier transform was applied on the time domain transmission dynamics to obtain the individual spin-wave spectra.

3. Results and Discussion

We include the results of varying material properties; Gilbert damping coefficient ($\alpha$) and $M_s$, varying RF signal excitation frequency and the change in the width modulated grating geometry, on the output magnetization temporal profiles and their steady-state spectra of the nanowire filter.

3.1. Effect of Damping, and $M_s$ on $M_x$ and $M_z$ Transient and Steady State Responses

The effect of damping on both transient and steady-state responses of the magnetization in the nanograting structure are shown, respectively, in Figures 1b and 2b. Small damping values allow for longer and higher-frequency oscillations in $M_x$ time profile (see Figure 2a). This is also shown in $M_z$ time response, which causes a lower slope for lower damping values. So higher Gilbert damping reduces the energy required to shift to steady-state and for spins to transport such energy. To translate this effect into the frequency domain, Figures 1c and 2b show the resulting excited frequency peaks of filter nanowire modes. $M_x$ peak intensities are reduced for higher damping and the overall spectral magnitude is lower. Increasing Gilbert damping re-shifts the frequencies of the excited modes, so the higher frequency mode peaks are shifted toward lower frequency magnitudes while the 3 GHz peak remains unchanged even in magnitude.

![Figure 2](image_url)

**Figure 2.** Damping coefficient dependence of z-axis transmission, where 3 GHz RF signal is used for the excitations. The effect of increasing Gilbert damping coefficient on transient $M_z$ in (a) time and (b) frequency (for 8–10 ns time window) domains (the rest of the parameters were fixed). The nanogratings with lower damping coefficients transmit higher-frequency oscillations with higher transmission ratios.

3.2. Effect of Frequency of RF Signal on $M_x$ and $M_z$ Steady State Responses

The RF excitation signal which is applied along the longitudinal axis of the nanowire has a significant contribution to the spectral features and modes of the nanograting filter response, as shown in Figure 3. The $M_x$ spectra in Figure 3a show the different excitation frequency peaks of the RF signal along the longitudinal direction. The first neighbors around the zero-bias peak signed with star labels are an indication of the excitation frequency. A higher frequency excited peak (at around 10 GHz) at each spectrum curve
appears unaffected by the increasing excitation frequency, which may imply that the magnetization response along this magnetization component does not affect higher frequency modes resulting from spin-wave generation in the nanowire. In Figure 3b of the $M_z$ spectra, the excited modes’ intensities also experience an increase with the higher frequencies of the excitation signal, while a 7.5 GHz excited peak appearing for the same nanowire geometry and material settings is clearly unaffected by this change. This shows a possible frequency-selective property of the nanowire structure prone to any change in an applied RF signal frequency.

![Figure 3](image-url)

Figure 3. Effects of external RF magnetic field excitation. The effect of increasing excitation frequency of RF signal on (a) $M_x$ and (b) $M_z$ spectral peaks’ intensities and positions/frequencies, for 8–10 ns time window. The damping coefficient is kept at the value of 0.013 for all cases.

3.3. Effect of Nanograting Structure Geometry on $M_x$ and $M_z$ Responses

This section is concerned with discussing the resulting changes in the width-modulated central structure on the average magnetization dynamics of the overall nanowire. Each parameter is evaluated while keeping the rest of the geometry and the material properties unchanged.

3.3.1. Periodicity (N) and Period Length (P)

Figure 4 demonstrates the changes in the magnetization ($M_x$) orientation over the nanowire from increasing both N and P. Wherefrom Figure 4a for $N > 12$, the average magnetization flips to the negative direction of the $x$-axis and becomes more negative as $N$ increases. This change is a result of the increase in the contribution of the demagnetization field to the overall effective field across the structure as $N$ becomes larger. The same can be concluded from Figure 4b, as $P$ forces a change in the overall $M_x$ due to the demagnetizing field, causing it to be more negative as $P$ goes beyond 50 nm. The non-zero magnetization in steady state for both plots of $N$ and $P$ indicates that not all the magnetic moments are oriented in the same direction. Some portion of the moment along the z-direction causes a shifting of the overall signal from the equilibrium [31].
Figure 4. The effect of increasing the (a) periodicity N and (b) period P of the nanograting structure on $M_z$ temporal plots. Other geometry parameters are fixed. Material parameters; $\alpha = 0.013$ and $M_s = 840 \times 10^3$ A m$^{-1}$. Excitation frequency is 3 GHz with 500 mT RF and 1000 mT DC bias field.

3.3.2. Filter Response for W (nm)

Another way to relate the output spectrum of the nanowire to the selectively produced mode is to cause W to become narrower or wider, within the given structure width. This is demonstrated in Figure 5, where spectral peaks are shifted to higher frequencies as W increases. Since the MC is excited at DC (0 Hz) and 3 GHz, these driving forces appear as steady-state peaks in all spectra. The major peaks other than 0 Hz and 3 GHz are attributed to the demagnetizing field-driven effects. Figure 5 shows that increasing the width W from 12 to 28 nm shifts the high frequency peak from 5 to 10 GHz.

Figure 5. $M_z$ spectra resulting from changing W (nm), for 8–10 ns time window. Dashed lines are an indication of the excitation frequency for three cases.
4. Conclusions

In this paper, the magnetization dynamics for nanowires are modelled by systematically varying Gilbert damping constants, nanowire geometric parameters, and RF excitation frequency to elucidate their effects on the spin-wave modes and their temporal behavior. Gilbert damping causes the overall magnetization vectors to decay faster in time and their energy spectra are reduced. Spectral peaks tend to shift toward lower frequencies as the structure is subjected to higher damping. This property constitutes the selective frequency response as a filter. It is also observed that increasing the excitation frequency of the RF signal in the longitudinal axis affects the magnitude of the resulting spectrum while keeping certain excited mode peaks unaffected along x and z components. Variation in the geometry of the width modulation section of the structure plays a role in defining the amount of contribution of the demagnetizing field along the nanowire by changing the N and P values. The spectrum peaks shift to higher frequencies as W increases.

Previous studies on similar but bulk-like micron-thick structures [14] showed reflection-less magnon dynamics and tunable band structures. From a practical standpoint, a reflection-less magnonic crystal could be the building block needed for eliminating the back-coupling between the cascaded magnon devices such as filters, logic gates, MC-based frequency multiplexers and demultiplexers. A detailed investigation of the material property, external field and geometry dependence of this structure with this study could shed light on magnon dynamics and spectral characteristics in thin film MC. Thus, this study could pave the way to more advanced cascaded magnon logic structures.

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