Adaptive Mesh Refinement for Astrophysics Applications with ParalleX

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Abstract—Several applications in astrophysics require adequately resolving many physical and temporal scales which vary over several orders of magnitude. Adaptive mesh refinement techniques address this problem effectively but often result in constrained strong scaling performance. The ParalleX execution model is an experimental execution model that aims to expose new forms of program parallelism and eliminate any global barriers present in a scaling-impaired application such as adaptive mesh refinement. We present two astrophysics applications using the ParalleX execution model: a tabulated equation of state component for neutron star evolutions and a cosmology model evolution. Performance and strong scaling results from both simulations are presented. The tabulated equation of state data are distributed with transparent access over the nodes of the cluster. This allows seamless overlapping of computation with the latencies introduced by the remote access to the table. Because of the expected size increases to the equation of state table, this type of table partitioning for neutron star simulations is essential while the implementation is greatly simplified by ParalleX semantics.

Index Terms—Adaptive mesh refinement, astrophysics applications, ParalleX

I. INTRODUCTION

Among the most challenging problems in computational science is simulating the rich phenomenology of numerical relativity based astrophysical events like the collision of neutron stars combining electo-magnetics, extreme gravity, and neutrinos. Such complex simulations may provide the necessary signatures essential for the first arcane observations of gravitational waves from new instruments like the Laser Interferometric Gravitational Observatory (LIGO). To minimize unnecessary computational work, Adaptive Mesh Refinement (AMR) algorithms have been employed, greatly advancing the means of scientific discovery. However, like an increasing number of computational techniques in the emergent many-core era, true AMR-based problem performance can be severely limited by exhibiting strong scalability; in some cases taking weeks to compute a result but unable to effectively employ more than a few hundred processor cores using conventional practices such as the Communicating Sequential Processes (CSP) execution model [1] as reflected by the MPI based programming model [2]. A new computational strategy, replacing CSP, may be required to achieve dramatic increases in performance and continue to benefit from Moore’s Law.

The ParalleX execution model [3]–[5] is offered as a means of addressing these critical computational requirements. Performance for strong-scaled science codes like the HAD AMR [6] problem is determined by four factors: peak per unit capability, efficiency, scalability, and availability. The first is an innate property of a given hardware system and the last is related to issues of reliability (fault tolerance) and protection (i.e., security) both of which are outside the scope of the study being reported on. ParalleX is an experimental execution model developed to exploit runtime resource management and task scheduling to dramatically improve per locality (an equivalent of a traditional compute node) efficiency and increase scaling of the number of localities that may be effectively employed. ParalleX is a synthesis of complementing semantic constructs delivering a dynamic adaptive framework for message-driven multi-threaded computing in a global address space context with constraint-based synchronization to exploit locality and manage asynchrony. The result is introspective runtime alignment of computing requirements and computing resources while managing asynchrony of operation across physically distributed resources. ParalleX has been first implemented in the form of the HPX runtime system [7], [8] developed to support the semantics and mechanisms comprising ParalleX targeting conventional SMP and commodity cluster computing platforms. This experimental software package is developed to test the semantics of ParalleX, to measure the overhead costs of software implementation, and to provide a superior environment for extreme scale applications.

This paper discusses the results of employing the ParalleX execution model and applying the HPX runtime system to the HAD AMR simulation system for astrophysics applications with an emphasis on numerical relativity problems. These have proven to be exceptionally challenging and exemplify the growing set of strong-scaled algorithms that are failing to benefit from Moore’s Law. This paper shows significant advances realized through improved efficiency with respect to static conventional methods and provides promising, although non-conclusive, results towards distributed scalability. The paper concludes with the implications of these results for future work.
II. ADAPTIVE MESH REFINEMENT FOR ASTROPHYSICS APPLICATIONS

Each of the two applications explored here each have several important physical scales. Each of these scales must be adequately resolved in order to properly understand the underlying dynamics. In the cosmology application, (see section VII) the gradients at the domain wall and the subsequent break require modeling several scales in the midst of exponential growth. In the neutron star problem, the scales range from the internal dynamics of the individual stars to the gravitational wave zone. Strong scaling of such applications is typically poor [9]. For medium sized applications, this often means that an AMR simulation would require weeks to months of runtime on a relatively small number of processors. Due to the prevalence of such type simulations in astrophysics, we explore AMR in the context of the ParalleX execution model.

III. THE PARALLEX EXECUTION MODEL

The ParalleX execution model [4], [5], [8], [10] was developed with the goal of specifying the next execution paradigm essential to the full exploitation of future technology advances and computer architectures in the near term as well as to guide co-design of computer architecture and programming models in conjunction with supporting system software in the long term. ParalleX is intended to catalyze innovation in system structure, operation, and applications to realize practical Exascale processing capability by the end of this decade.

The development of ParalleX is motivated by two challenges we face when developing certain classes of applications with conventional models. Scaling-impaired applications, such as the described astrophysics adaptive mesh refinement codes, are usually unable to effectively exploit a relatively small number of cores in a multi-core system. Such applications will likely also be unable to exploit future Exascale computing systems. Four factors are inhibiting their scalability:

- **Starvation**, the unavailability of useful work either globally or locally.
- **Latency**, delays due to remote accesses or service requests.
- **Overhead**, the critical time and work required to manage parallel resources and concurrent tasks which would not be required for pure sequential execution.
- **Waiting for contention resolution**, delays due to conflicts for shared physical or logical resources.

The ParalleX execution model strives to overcome these limitations through four principal properties:

- Exposure of intrinsic parallelism, especially from meta-data, to meet the concurrency needs of scalability by systems in the next decade.
- Intrinsic system-wide latency hiding for superior time and power efficiency.
- Dynamic adaptive resource management for greater efficiency by exploiting runtime information.

- A global name space to reduce the semantic gap between application requirements and system functionality both to enhance programmability and to improve overall system utilization and efficiency.

While ParalleX incorporates many useful concepts developed elsewhere, some extending back as far as three decades, it constitutes a new synthesis of these as well as innovative ideas in a novel schema that is distinct from conventional practices and that exhibits the necessary properties identified above to increase application and system scalability. The form and function of the current ParalleX model consist of six key concepts or management principles: ParalleX Processes (PX-processes), the Active Global Address Space (AGAS), threads (PX-threads) and their management, parcel transport and their management, Local Control Objects (LCOs), and percolation [11]. With the exception of PX-processes and percolation, all have been incorporated in a C++ prototype runtime implementation of ParalleX called HPX (High Performance ParalleX) [7], [8]. We will highlight these concepts throughout this paper wherever they relate to our results.

IV. THE HPX RUNTIME SYSTEM

A walkthrough description of the HPX architecture is found in Figure 1. An incoming parcel (delivered over the interconnect) is received by the parcel port. One or more parcel handlers are connected to a single parcel port, optionally allowing to distinguish different parts of the system as the parcel’s final destination. An example for such different destinations is to have both normal cores and special hardware (such as a GPGPU) in the same locality. The main task of the parcel handler is to buffer incoming parcels for the action manager. The action manager decodes the parcel, which contains an action. An action is either a global function call or a method call on a globally addressable object. The action manager creates a PX-thread based on the encoded information.

All PX-threads are managed by the thread manager, which schedules their execution on one of the OS-threads allocated to it. Usually HPX creates one OS-thread for each available core. Several scheduling policies have been implemented for the thread manager, such as the global queue scheduler, where all cores pull their work from a single, global queue, or the local queue scheduler, where each core pulls its work from a separate queue. The latter supports work stealing for better load balancing. In the local scheduler, a queue is created for each of the OS-threads dedicated to the thread manager. These queues are placed in a contiguous block of local memory. When an OS-thread is searching for work, it first checks its own queue. If there is no work there, the OS-thread begins to steal work by searching for work in other queues.

If a possibly remote action has to be executed by a PX-thread, the action manager queries the global address space (AGAS) to determine whether the target of the action is local or remote to the locality that the PX-thread is running on. If the target happens to be local, a new PX-thread is created and passed to the thread manager. This thread encapsulates the work (function) and the corresponding arguments for that
Fig. 1. Modular structure of HPX implementation. HPX implements the supporting functionality for all of the elements needed for the ParalleX model: AGAS (active global address space), parcel port and parcel handlers, HPX-threads and thread manager, ParalleX processes, LCOs (local control objects), performance counters enabling dynamic and intrinsic system and load estimates, and the means of integrating application specific components.

The Active Global Address Space (AGAS) provides global address resolution services that are used by the parcel port and the action manager. AGAS addresses are 128bit unique global identifiers (GIDs). AGAS maps these global identifiers to local addresses, and additionally provides symbolic mappings from strings to GIDs. The local addresses that GIDs are bound to are typed, providing a degree of protection from type errors. Any object that has been registered with a GID in AGAS is addressable from all localities in an instance of the HPX runtime. AGAS also provides a powerful reference counting system which implements global garbage collection.

Lightweight Control Objects (LCOs) are the synchronization primitives upon which HPX applications are built. LCOs provide a means of controlling parallelization and synchronization of PX-threads. Semaphores, mutexes and condition variables [12] are all available in HPX as LCOs. Futures [13] are another type of LCO provided by HPX, and are discussed in greater detail later in this paper.

Local memory management, performance counters (a generic monitoring framework), LCOs and AGAS are all implemented on top of an underlying component framework. Components are the main building blocks of remotable actions and can encapsulate arbitrary, possibly application specific functionality. Actions expose the functionality of a component. An action can be invoked on a component instance using only its GID, which allows any locality to invoke the exposed methods of a component. In the case of the aforementioned components, the HPX runtime system implements its own functionality in terms of this component framework. Typically, any application written using HPX extends the set of existing components based on its requirements.

V. Using Shen Equation of State Tables

The Shen equation of state (EOS) tables of nuclear matter at finite temperature and density with various electron fractions within the relativistic mean field (RMF) theory [14] are a set of three dimensional data arrays enabling high precision interpolation of 19 relevant parameters required for neutron star simulations. While these tables are currently relatively small in size (about 300 MBytes), it is expected that over the next year a new set of tables ensuring higher resolution will be published. The size of the new tables is expected to be in the range of several GBytes. This will prevent loading the whole data set into main memory on each locality. In conventional, MPI based applications the full tables would have to be either loaded into each MPI process or a distributed partitioning scheme would have to be implemented. Both options are either not viable or difficult to implement.
A. The Overhead of Eager Futures

Many HPX applications, including the astrophysics applications detailed here, utilize Futures for ease of parallelization and synchronization. In HPX, Futures are implemented as two types of LCOs (Eager Futures and Lazy Futures). The astrophysics applications detailed in this paper make extensive use of Eager Futures. For this reason, the overheads of these constructs is a large factor in the total overhead of the HPX runtime in our code. In this subsection, we give a description of Futures, outline a performance test for measuring the overhead of Futures, and present the results of the test.

As shown in Figure 2, a Future encapsulates a delayed computation. It acts as a proxy for a result initially not known, most of the time because the computation of the result has not completed yet. The Future synchronizes the access of this value by optionally suspending PX-threads requesting the result until the value is available. When a Future is created, it spawns a new PX-thread (either remotely with a parcel or locally by placing it into the thread queue) which, when run, will execute the action associated with the Future. The arguments of the action are bound when the Future is created. Once the action has finished executing, a write operation is performed on the Future. The write operation marks the Future as completed, and optionally stores data returned by the action.

When the result of the delayed computation is needed, a read operation is performed on the Future. If the Future’s action hasn’t completed when a read operation is performed on it, the reader PX-thread is suspended until the Future is ready.

Our benchmark for Future overhead created a fixed number of Futures, each of which had a fixed workload. Then, asynchronous read operations were performed on the Futures until all of the Futures had completed. A high resolution timer measured the wall-time of the aforementioned operations. The test was run on an 8-socket HP ProLiant DL785 (each socket sports a 6-core AMD Opteron 8431) with 96 Gbytes of RAM (533 MHz DDR2). Trials were done with varying workloads and OS-threads. 5 runs were done for each combination of the parameters, and the results were averaged to produce a final dataset. The numbers are presented in Figure 3.

The scaling results in Figure 3 call for some explanation. The parabolic curves are formed primarily by contention in the thread queue scheduler. As the number of OS-threads is increased, the contention on the thread queue scheduler also increases, due to a higher number of concurrent searches for available work. This increased contention occurs in both global queue schedulers (where all OS-threads poll the same work queue, and must obtain exclusive access to said queue for some period of time) and to a lesser degree in local queue schedulers (where work stealing occurs, which causes queue contention, albeit to a lesser degree than in the global queue scheduler). As we increase the workload in each Future, OS-
threads spend more time executing the workloads and less time searching for more work. This decreases contention on the queues. Adding a new OS-thread is beneficial as long as the contention overhead that it causes is not greater than the parallel speedup that it provides.

B. The Overhead of the ShenEOS Table Partitioning

We created an HPX component encapsulating the non-overlapping partitioning and distribution of the Shen EOS tables to all available localities, thus reducing the required memory footprint per locality [15]. A special client side object ensures the transparent dispatching of interpolation requests to the appropriate partition corresponding to the locality holding the required part of the tables (see Figure 4). The client side object exposes a simple API for easy programmability.

The second part of this section describes the setup and results of the measurements we performed in order to estimate the overheads introduced by distributing the Shen EOS tables across all localities. To evaluate the scalability and associated overheads of the distributed implementation of the Shen EOS tables, a number of tests has been performed, all of them with a fixed number of total data accesses (measuring strong scaling). The tests have been run on a different number of localities and varying number of OS-threads per locality. The current HPX implementation supports only a centralized AGAS server that may be invoked in two configurations: either as a standalone task on a dedicated locality or as a part of one of the user application tasks. Our tests used a standalone AGAS server, firstly to avoid interfering with the user workload and secondly to eliminate the generation of asymmetric AGAS traffic on localities hosting data tables. Unlike the client applications, the AGAS server used a fixed number of OS-threads throughout the testing to ensure that sufficient processing resources are available to the incoming resolution requests.

The tests were performed on a small heterogeneous cluster. The cluster consists of 18 localities (excluding the head node) connected by Gigabit Ethernet network. Two of the machines are 8-socket HP ProLiant DL785s, with 6-core AMD Opteron 8431s and 96 Gbytes of RAM (533 MHz DDR2). The other 16 localities are single-socket HP ProLiant DL120s, with Intel Xeon X3430s and 4 Gbytes of RAM (1332 MHz DDR3). All machines run x86-64 Debian Linux. Torque PBS was used to run multi-locality tests.

Figure 5 shows the execution times collected for the data access phase with a special test application executed on up to 16 localities and 1, 2, and 4 OS-threads per locality. The total number of distributed partitions was set at 32 to preserve the AGAS traffic pattern when run on a different number of localities; all partitions were uniformly distributed across the test localities. The number of queries to the distributed ShenEOS partitions was set to a fixed number of 16K. Each of these queries created a Eager Future encapsulating the whole operation of sending the request to the remote partition, schedule and execute a PX-thread, perform the interpolation based on the supplied arguments for the ShenEOS data, sending back the resulting values to the requesting PX-thread, and resuming the PX-thread which was suspended by the Future in order to wait for the results to come back.

The graph demonstrates that the overhead of distributed table implementation does not increase significantly over the entire range of available localities. While the scaling is much better when the number of localities remains small (up to 4), the overall time required to service the full 16K data lookup requests remains roughly constant, which proves the quality of the implementation. The test application itself does not execute
VI. COSMOLOGY APPLICATION

In cosmology, inflation is driven by the inflaton field, which is a scalar field with a nonlinear potential. Quantum fluctuations in the inflaton field will result in some regions of space-time expanding more rapidly than other regions. The boundary between these regions is the domain wall, where the inflaton field changes from one vacuum value to another over a small region. The cosmology code models the dynamics of the domain wall. The scalar field is the inflaton field with a $\psi^4$ potential. The initial data are a kink, modeling the transition from one vacuum state to another. This application aims to study the stability and dynamics of the domain wall during the cosmological expansion. The domain wall eventually has to break because the region that is expanding more rapidly does so exponentially. Depending on how the domain walls break or snap, there may be observational signatures in the cosmic microwave background.

The dynamics of the domain wall during expansion encompass many temporal and spatial scales making it an excellent candidate for AMR simulation. The system of equations has nine variables ($\phi, \Pi, \chi, a, f, g, b, q, r$) and two independent variables ($t$ and $z$):

\[
\begin{align*}
\frac{\partial \phi}{\partial t} &= \Pi \\
\frac{\partial \Pi}{\partial t} &= \Pi (f/a + q/b) + (3ag/b^2 - a^2r/b^3) \chi + (a/b)^2 \frac{\partial \chi}{\partial z} - a^2\lambda(\phi^2 - v^2) \\
\frac{\partial \chi}{\partial t} &= \frac{\partial \Pi}{\partial z} \\
\frac{\partial f}{\partial t} &= a(-f/q)/(ab) + 2g^2/b^2 - agr/b^3 + a\frac{\partial g}{\partial z}/b^2 + a^2\lambda(\phi^2 - v^2)/4 \\
\frac{\partial g}{\partial t} &= \frac{\partial f}{\partial z} \\
\frac{\partial b}{\partial t} &= q \\
\frac{\partial q}{\partial t} &= b(-f/q)/(ab) - 3agr/b^3 + 3a\frac{\partial g}{\partial z}/b^2 + a^2\lambda(\phi^2 - v^2)/4
\end{align*}
\]

where $\lambda = 1$, $v = 0.1$, and the boundary condition is periodic. The system is evolved with second order differencing in space and third order Runge-Kutta integration in time. The AMR algorithm is Berger-Oliger [16] but uses tapering [17] to reduce noise at coarse-fine interfaces. The algorithm is implemented using dataflow LCOs, thereby replacing global barriers with constrained synchronization. Performance results on a quad-core Intel Nehalem (2.8 GHz) cluster with 1333 MHz DDR3 memory are detailed in Figure 6.

VII. CONCLUSION

In this paper we have presented performance and scaling measurements for two key astrophysics applications built with the High Performance ParalleX C++ library (HPX). We have presented overhead measurements for one of the building blocks of these applications (Futures) and an application specific distributed partitioning component (ShenEOS). The results of these benchmarks show sufficiently good strong-scaling behavior to conclude that these components will not significantly impede full neutron star applications when fully integrated therein. The amortized overhead for creating, using and deleting one Future object has been established to be approximately 40 microseconds.

We have also presented distributed AMR scaling results for a cosmology application. Astrophysical applications using AMR, which are known to expose unsatisfactory strong scaling behavior when implemented using conventional (MPI based) techniques, are not only easier to implement when built on top of HPX, but also exhibit promising strong scaling characteristics in distributed runs.

Future work will be focusing on reducing the overheads introduced by HPX and developing currently unimplemented parts of the ParalleX execution model (such as PX-processes.
Reducing the overhead of Futures and the HPX scheduling subsystem will improve HPX’s scaling potential. To enable HPX applications to utilize thousands of localities for a single application, the overheads of the contention on the centralized AGAS server must be reduced by distributing the AGAS subsystem across multiple localities.

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