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Social Simulation of Intergroup Conflicts Using a New Model of Opinion Dynamics

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The social identity theory proposed by Tajfel et al. provides insight into how group membership and self-categorization cause intergroup prejudice and discrimination, finally leading to social conflicts. However, unanswered questions remain: under what conditions can an “in-group” and an “out-group” transform conflictual intergroup behavior into a more harmonious relationship and avoid social conflict? Opinion dynamics theory and social simulation are appropriate methods to answer this question. In this study, a new model of opinion dynamics proposed by Ishii is adopted, and we conduct simulations of intergroup conflicts. The new model, along with social simulations, presents how an in-group and an out-group can develop social harmony and avoid social conflict. According to our simulations, when the two groups trust their members 100%, the opinion inside an in-group converges. However, intragroup opinion diverges as trust within the group gets lower. On the other hand, intergroup opinion converges when the intergroup trust is higher than 50%. If intergroup trust is higher than 80%, then the intergroup opinions of the two perfectly overlap. Furthermore, if intragroup trust is 70% and intergroup trust is as low as 50%, the two groups’ opinions completely polarize. We also calculated additional cases where intragroup trust was fixed at 70%, but for one-third of an in-group member trust an out-group with various values. Finally, a method to avoid further social crises can be obtained by examining real-world cases of partisan conflicts in recent America.

Keywords: divided society, opinion dynamics, social crisis, social simulation, the social identity theory, in-group, out-group, social conflicts in the United States

1. INTRODUCTION

Throughout world history, too many cases of social conflict have been observed. By examining cases of social conflicts, we can develop a method to avoid further social crises. Therefore, we conducted a simulation of conflict between the two groups in this study.

Prejudice and discrimination are the causes of social conflicts. According to social identity theory, intrapersonal or interpersonal psychological processes are not a cause of prejudice and discrimination. If anything, prejudice and discrimination derive from intergroup antagonism [1, 2]. People decide which social group to belong to for a sense of pride, involvement, stability, and meaning [3–5]. In deciding which group to support, they identify the social group they belong to as their “in-group” and distinguish other groups as “out-groups,” often in harmful or discriminative ways [6]. They strengthen a sense of unity with the party members of the in-group and start to support its issues. This self-categorization and group membership work as a
social-cognitive schema (norms, values, and beliefs) for their group-related behavior. The perception of belonging to the in-group is sufficient to cause intergroup prejudice, ethnocentrism, stereotypes, and discrimination, even in the absence of material conflict or previous group hostility [2, 3].

Social identity theory is critical because it offers a foundation for understanding how group membership and self-categorization cause intergroup prejudice and discrimination, and they finally lead to social conflicts [2]. Thousands of empirical studies have been conducted by scholars of social science, and most of these empirical studies adopt experimental methods [1, 7, 8]. However, there remain unanswered questions. Under what conditions can an in-group and an out-group transform conflictual intergroup behavior into a more harmonious relationship and avoid social conflict? From prior empirical studies, achieving or sustaining a harmonious relationship is assumed to be nearly impossible for an in-group and an out-group [1]. Here, opinion dynamics theory and social simulation are appropriate methods to answer the question. Based on the bounded confidence model [9–11], opinion dynamics can present how an in-group and an out-group can develop social harmony and avoid social conflict.

Grounded upon opinion dynamics theory, several models have been developed to explain social conflicts [12–16]. In particular, Javarone established a variation of the classical voter model to study the best strategies to gain a popular consensus with two competitors [16–18]. Our model is distinct in two aspects. First, we use the theory originating from Ishii [19, 20], a straightforward extension of the bounded confidence model to the theory of opinion dynamics that sets trust and distrust for intergroup dimension and intragroup dimension. According to Ishii's theory, \( D_{ij} \), which appeared in Hegselmann-Krause's opinion dynamics theory before, is considered a coefficient of trust, and if it posits a negative value, that means a relationship is distrustful. Second, we refer to the social identity theory initially proposed by Tajfel as a key [6]. With the opinion dynamics model and social simulations, the social identity theory helps understand how consensus within social groups is formed, and intergroup conflicts arise or mitigate.

In this study, we simulate intergroup and intragroup opinion dynamics using Ishii's model. In previous works, based on the foundational model developed by Ishii and Kawahata [19, 20], we incorporated trust and distrust into the model. It was also established that consensus-building aspects depend on the ratio between trust and distrust coefficients [21, 22]. Thus, it is recognized that the model can be applied to illustrate real-world examples of social conflicts [22]. Therefore, in this study, we adopt a model to examine real-world examples of social conflicts. We assume that a society consists of two groups, and the severity of the conflict between the two is related to the intragroup and intergroup relatability.

2. THEORY OF OPINION DYNAMICS

Opinion dynamics is a discipline that follows the process of consensus building within societies. The theory of opinion dynamics can be divided into a theory that treats people's opinions in society as binary values and a theory that treats the opinions of people in society as continuous values. Theories that treat binary opinions include the voter model [23] and theories that apply magnetism theory in solid-state physics [24].

The theory that expresses people's opinions in society as continuous values is called the bounded confidence model. In the bounded confidence model, if person \( i \)'s opinion is expressed as \( I_i(t) \), it is considered to be influenced by the opinions of others \( I_j(t) \) by the following formula:

\[
I_i(t + \Delta t) = I_i(t) + \lambda (I_j(t) - I_i(t)).
\]

where \( \lambda \) is a convergence factor, and the time required for consensus building differs depending on the value of \( \lambda \). The above equation is the fundamental equation of the bounded confidence model by Deffuant et al. [9, 10]. On the other hand, the fundamental equation of the Hegselmann-Krause model [11] is the following equation,

\[
I_i(t + \Delta t) = I_i(t) + \lambda_{ij}(I_j(t) - I_i(t)).
\]

where \( \lambda_{ij} \) is a convergence factor, and the time required for consensus building differs depending on the value of \( \lambda_{ij} \). The above two models, the Deffuant model and the Hegselmann-Krause model, are almost equivalent. The time convergent factor \( \lambda_{ij} \) is a positive number so that society's opinions form a consensus. The difference in the initial settings of the bounded confidence model calculation is related to how many opinions the society agrees.

In contrast to the bounded confidence model shown above, Ishii et al. modified the meaning of time convergence coefficient \( \lambda_{ij} \) to \( D_{ij} \) as the coefficient of trust. Here, Ishii assumes that \( D_{ij} > 0 \) for a trust relationship between two people, and \( D_{ij} < 0 \) for a distrust relationship between two people [19, 20]. According to the extension, the value of opinion \( I_i(t) \) could be either positive or negative. In Ishii's opinion dynamics theory, opinions within the society are assumed to be on a one-dimensional axis. Thus, the negative opinion merely indicates an opinion opposite to the positive opinion. For example, if the positive opinion is a liberal one, the negative opinion would be conservative. If the positive opinion is conservative, the negative opinion would be liberal.

Following the grounding theory [20], we assume that people disregard an opinion far from their opinion. An opinion that is close to themselves will not be affected. Thus, we use the following function instead of \( D_{ij}(I_i(t) - I_j(t)) \) to include the two effects:

\[
D_{ij}\Phi(I_i, I_j)(I_j(t) - I_i(t))
\]

where

\[
\Phi(I_i, I_j) = \frac{1}{1 + \exp(\beta(|I_i - I_j| - b))}
\]

This function is called the Sigmoid function, and it works as a smooth cutoff function at \(|I_i - I_j| = b\). Using the Sigmoid function, we assume that if the opinions of the two are far apart, one's opinion will not be influenced by the opinion of the other. The
factor $I_i - I_j$ means that agent $i$ is not affected by agent $j$. As a result, an opinion that is close to the subject or an opinion that is far away from the subject will not be affected. In the theory of Hegselmann-Krause [7], they only use the step function instead of the Sigmoid function. The Sigmoid function should be used here because the function makes the cutoff smooth; however, there is no significant difference from the step function in the actual opinion dynamics calculation.

The influence of the mass media can be added to the following mathematical model [25, 26]: In the actual calculation, the effect $A(t)$ of the mass media is, for example, the number of seconds spent in reporting or advertising on a relevant item [25]. $A(t)$ denotes the pressure from mass media at a time $t$. The coefficient $c_i$ shows how much impact media gives to each agent. The coefficient $c_i$ can have different values for each person, and it can be either positive or negative. If the coefficient $c_i$ is positive, person $i$ moves their opinion toward the mass media. On the contrary, if the coefficient $c_i$ is negative, a person’s opinion changes against the mass media [27, 28].

Therefore, including mass media effects, the change of opinion of an agent can be expressed as follows:

$$\Delta I_i(t) = c_i A(t) \Delta t + \sum_{j=1}^{N} D_{ij} \Phi(I_i(t), I_j(t))(I_i(t) - I_j(t)) \Delta t,$$  

where $\Delta I_i(t) = I_i(t + \Delta t) - I_i(t)$. According to the Ishii’s opinion dynamics theory [20], $D_{ij}$ is an asymmetric matrix. $D_{ij}$ and $D_{ji}$, $D_{ij} \neq D_{ji}$, and $D_{ij}$ and $D_{ji}$ can have different signs. Here, $D_{ij} > 0$ corresponds to the trust relationship between the two people, and $D_{ij} < 0$ corresponds to the distrust relationship between the two.

Long-term behavior requires attenuation; that is, topics will be forgotten over time. Hence, we introduced exponential attenuation to the model as follows:

$$\Delta I_i(t) = -\alpha \Delta I_i(t) \Delta t + c_i A(t) \Delta t + \sum_{j=1}^{N} D_{ij} \Phi(I_i(t), I_j(t))(I_i(t) - I_j(t)) \Delta t.$$  

In previous studies [25, 26], the mass media effect was defined as the amount of time for a television advertisement. The definition worked without any issues. We obtained a suggestion from those studies, and here we define the mass media effect of the model as $c_i A(t)$. In the actual simulation shown below, we assume that $c_i = 1$, for simplicity.

$$\Delta I_i(t) = c_i A(t) \Delta t + \sum_{j=1}^{N} D_{ij} \Phi(I_i(t), I_j(t))(I_i(t) - I_j(t)) \Delta t$$  

In the calculation below, we set $A(t)$ as 0.00, and $c_i$ is set as unity. Throughout this article, $A(t)$ is set to be zero for simplicity to concentrate on the effect of $D_{ij}$.

We assumed a case of two people, $N = 2$. Based on the model [20], the equations for the two-people model are

$$\Delta I_A(t) = c_A A(t) \Delta t + D_{AB} \Phi(I_A(t), I_B(t))(I_A(t) - I_A(t)) \Delta t$$  

$$\Delta I_B(t) = c_B A(t) \Delta t + D_{BA} \Phi(I_B(t), I_A(t))(I_A(t) - I_B(t)) \Delta t$$

Let us suppose two people cases: In the first case, the two trust each other, and the two distrust each other in the second case. The former case is shown in Figure 1A, and the latter case is shown in Figure 1B. If the two trust each other, their opinions converge: they form a consensus. However, if the two distrust each other, their opinions diverge: they never reach an agreement.

In the bounded confidence model, the multi-polarization of social opinions is brought about by ignoring distant opinions (shown in Equation 4) or by the step function. However, in Ishii’s opinion dynamics theory, it is assumed that the multi-polarization of social opinions is brought about by repulsion of opinions or distrust. According to Ishii’s theory, the repulsion of opinions could occur even among people whose opinions are relatively close. Ishii’s theory is more realistic in setting than the ordinally bounded confidence model.

The theory of opinion dynamics shown in this section can be applied to studies on real-world social conflicts using social simulations. With this opinion dynamics theory, calculating the convergence of opinions is enabled. In the same manner, calculating the divergence of opinions is enabled. The calculation

![Figure 1](image.png)  
**FIGURE 1** Calculation result for $N = 2$. (A) $D_{AB} > 0$ and $D_{BA} > 0$. (B) $D_{AB} < 0$ and $D_{BA} < 0$. 

with social simulation performed for the cases with 300 people is shown in the following sections. In the calculations, a connection of the people was simulated by a random network model. Here, 30% of the people are assumed to be connected. Figure 2 shows an example of a consensus building, where the coefficient $D$ represents trust between people. The coefficient $D$ posited a positive value by a random number from 0 to 1. In Figure 3, coefficient $D$ presents trust among people. The coefficient $D$ posited a random number in the range of $-1$ to 1, and the ratio of the positive and negative values was set to be equal. In this case, people's opinions were diffused and never reached a consensus.

3. SETTING OF SOCIAL SIMULATION CALCULATION

In this section, we explain how to check the division of society using a social simulation. Owing to the capacity of our computer, the number of people used in the simulations had to be limited to 300. We confirmed that our calculations with 300 people presented the same results with 500 or even 1,000 people. However, we limited the number of people to 300 because calculations with 1,000 people took a long time. Additionally, if we set more than 1,000 people, it is reasonable to assume that the way people connect in the real world should be scale-free [29]. In implementing calculations with the scale-free network, it is essential to set a person as a “hub.” In a given scale-free network, a “hub” person maintains strong influence within a network, that is, each scale-free network is determined by the hub's opinion and hence unique: it is difficult to identify the general characteristics of the scale-free network from its uniqueness. Let us inform Ishii's opinion dynamics model calculations with a scale-free network have already been done elsewhere [21, 30]. Hence, calculations using the scale-free network are technically feasible for us; however, because of the aforementioned reason, a scale-free network is not adopted in this study.

We evenly divide the 300 population society: we create two groups with 150 members within a society. Let us name the two groups as group A (an “in-group”) and group B (an “in-group”). As it is supposed in the social identity theory [1–3, 6], group A is an “out-group” if seen from group B and vice versa. In this study, we assume that the members of a group sometimes trust and sometimes distrust members of the other group. Figure 4 shows a schematic illustration of our model in the calculation.

We set the initial opinion value for the 300 population society to be randomly assigned between $-20$ and $+20$. We randomly set the coefficient of trust ($D_{ij}$). For cases of positive value, $D_{ij}$ posits between 0 and +1 as a random number. For the cases of negative value, $D_{ij}$ is between $-1$ and 0 as a random number.

As shown in Figure 3, opinions converge within an in-group, and a consensus is formed when a degree of trust among the people who belong to the in-group posits a positive value. Our calculation shows that when coefficient $D$ is higher than 55%, an in-group forms a consensus [21, 30]. Since this result can be applied to any of the two coexisting in-groups, we can assume consensus will be built when the degree of trust among members of an in-group is higher than 55%. However, how intergroup trust against an out-group from an in-group matters is still unknown. Therefore, we calculate that in the next section of this article.

We performed the following two calculations in the following section. In the first calculation (Figure 5), intergroup trust was set to zero, and intragroup trust was set to varying degrees. Then, we changed intragroup trust to 55% (Figure 6) and changed intergroup trusts to varying degrees.
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4. RESULTS

In Figure 5, we set the intergroup trusts against out-groups as 0%, and we changed the intragroup trust to varying degrees. Our prior studies show that two groups can reach an intragroup consensus, as shown in Figures 5B,C [17, 18]. In the cases shown in Figures 5D–G, we cannot even confirm intragroup consensus formation. Since the intergroup trusts are set to zero, intragroup opinions diverge. Furthermore, in those cases, the two groups never reached an intergroup consensus.

In Figure 6, we set the intragroup trust as 55%. Then, we changed the intergroup trust to varying degrees. The results are shown in Figure 6. In Figure 6B, there is no intergroup consensus, as shown in Figure 5. However, in Figures 6C–F, the intergroup opinions between groups A and B overlapped because of the high intergroup trust. This result shows that there were no serious conflicts between the two groups. A complete consensus building occurs when intergroup trusts are as high as 80% (Figure 6G).

We then assumed that the members of group B are not united. In our assumption, 50 out of the 150 members of group B (we call this subgroup B-1) maintain intergroup trust toward group A and vice versa. However, there is no trust between group A and the rest of the group B members. The members of groups A and B, including members of B-1, have an intragroup trust of 70% (Figure 7). In Figure 8, the members of group A and group B, including the members of B-1, have an intragroup trust of 50%. In Figure 8, we changed the value of intergroup trust for B-1. Whereas, the members of B-1 have intergroup trust toward group A and vice versa, there is no trust between group A and the rest of group B members.

The green line in Figure 7 represents B-1. When the intergroup trust of B-1 toward group A is lower than 50%, both group A and group B form intragroup consensus (see Figures 7F,G). In Figure 7F, we can see that few people from B-1 reached a consensus with Group A. Here, very few members from B-1 function as “out-group” inside of group B. However, in Figures 7B,C, a large number of B-1 members reach consensus with group A. In those cases, intragroup consensus-buildings within group B (depicted in the blue line) are hindered as B-1 leans toward group A.
Figure 8 shows a case where the intragroup trusts of the two groups are 50%. In this case, they can form no consensus. When the intergroup trust of B-1 exceeds 50%, group B-1 starts to overlap with group A. In Figure 8E, the B-1 members form a consensus with group A (the opinion distribution for this case is shown in Figure 9). Members of B-1 (depicted in the green line) and group A members work together to form a consensus. This consensus building is due to the high intergroup trust between group A and group B-1.

5. DISCUSSION AND CONCLUSION

In this study, we evaluated the conflict between two groups by applying opinion dynamics with simulations. We simulated the society, which was divided into two groups. Social division becomes decisive when an in-group embraces strong distrust against an out-group. If both an in-group and an out-group present a mixture of trust and distrust, the division is not decisive.

According to our simulation shown in Figure 5, when the two groups trust their members 100%, the opinion inside an in-group converges. However, intragroup opinion diverges as trust within the group gets lower, as shown in Figure 5. In Figure 6, intragroup trust is fixed at 55%. Here, intragroup opinion converges when the intergroup trust is higher than 50%. If intergroup trust is higher than 80%, then the intergroup opinions of the two perfectly overlap.

Furthermore, in Figure 7, the intragroup trusts of the two groups are fixed at 70%. Intergroup opinions do not overlap, even when intergroup trust is 70%. If intergroup trust is 70% and intergroup trust is as low as 50%, the two groups’ opinions completely polarize.

We also calculated additional cases where intragroup trust was fixed at 70%, but for one-third of an in-group member (B-1), trust an out-group (group A) with various values (Figure 7). For example, when one-third of the in-group members, i.e., B-1, trust an out-group with 60% of trust or higher, group B’s opinion diverges and comes closer to the opinion of A (Figures 7B–E). In contrast, when B-1 trusts its out-group with a trust of 50% or lower, group B’s opinion converges and will not get closer to A’s opinion (Figures 7F,G). In Figure 8, the intragroup trusts of the two groups are fixed at 50%. The opinion of group B starts to diverge as the intergroup trust from B-1 to A grows large.

The most important limitation lies in that there is much randomness in the model. As the authors tested only a single realization of the model in this article, it is still unclear how representative the results in this article are. Those uncertainties of the estimates are going to be studied as the next step of the research project. Hence, in subsequent studies, we will run several model realizations to check the robustness of trust threshold.
estimates. Please see forthcoming papers by Okano and Ishii [31, 32] and other related articles [21, 30].

Finally, after intergroup conflict studies using opinion dynamics theory with simulations, how can we explain examples of the real world? Recently in the United States, conflicts have arisen between the two political groups, that is, Republicans and Democrats. From a social identity perspective, partisanship functions in similar ways to other forms of group membership. American voters think of themselves as partisans, either the Republicans or Democrats, by calling to mind a mental image of the sort of people they associate with each party and then assessing the coherence of this image with their self-image [2]. The two parties have been severely divided, and each party has become more cohesive than ever in the last two decades. To say nothing about political ideology, Republicans and Democrats nowadays differ in lifestyles [33, 34]. They do not marry each other. The cars they ride, the food they eat, and the TV programs they prefer are all different. In other words, in-party members trust those who belong to the same party in all respects. However, they do not even try to nurture trust between an out-party. Under these circumstances, the two parties’ intragroup trusts are supposed to be very high, as shown in Figure 5B: Republicans and Democrats become more cohesive and antagonistic toward its out-group.

Nowadays, Republicans and Democrats struggle over many issues. There are many conflicts of controversial issues within the society of the United States. For example, gun control, gay marriage, abortion, immigration, racial equality, health insurance, legalization of marijuana, and belief in conspiracy theory are such cases. In the United States, these fierce conflicts have arisen between Republicans and Democrats [35]. On a feeling thermometer, a scale ranging from cold (0) to neutral (50) to warm (100), affinity among co-partisans has consistently hovered within the 70–75 range. By contrast, affinity between opposing partisans has plummeted from 48 in the 1970s to 20 today [36]. Correspondingly, Republicans and Democrats will not agree on the issues because of their hate for an out-party. This situation is similar to our simulations shown in Figures 5B, C.

How can the United States survive this interparty hostility and avoid falling into a social crisis? As we see in Figure 5, if intraparty trusts go down to 55%, the two parties will not reach a consensus because interparty trust is 0%. However, interparty consensus will be achieved when intraparty trusts are lower than 55%, and interparty trusts are higher than 50% (Figure 6). To fix interparty antagonism and reach an agreement, both parties have to endeavor to create divergence of opinions within the party and find ways to enhance interparty trust.
FIGURE 8 | Cases in which no intergroup trust exists between group A and group B. The intragroup trusts for group A and group B are fixed at 50%. However, 50 people in group B (B-1) have intergroup trust toward group A. (A) Is the model's schematic view. In (B–E), there are various intergroup trusts between the B-1 and group A. For instance, the trust 70% means that 70% of the trust ($D_{ij}$) exists between the B-1 and group A. The red lines correspond to the opinion trajectories of group A. The blue lines are those of group B except for the B-1 subgroup. The green lines are the opinion trajectories of B-1.

FIGURE 9 | Opinion distribution for the case shown in Figure 8E at time = 10.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author/s.

AUTHOR CONTRIBUTIONS

NO did almost calculation and modeling of the calculation. AI and MN supervised her as graduate student. All authors contributed to the article and approved the submitted version.

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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