A CHEOPS Search for Massive, Long-period Companions to the Warm Jupiter K2-139 b

Alexis M. S. Smith and Szilárd Csizmadia
Department of Extrasolar Planets and Atmospheres, Institute of Planetary Research, German Aerospace Center

Received 2022 March 21; revised 2022 April 22; accepted 2022 May 11; published 2022 June 28

Abstract

K2-139 b is a warm Jupiter with an orbital period of 28.4 days, but only three transits of this system have previously been observed—in the long-cadence mode of K2—limiting the precision with which the orbital period can be determined and future transits predicted. We report photometric observations of four transits of K2-139 b with ESA’s CHaracterising ExOPlanet Satellite (CHEOPS), conducted with the goal of measuring the orbital obliquity via spot-crossing events. We jointly fit these CHEOPS data alongside the three previously-published transits from the K2 mission, considerably increasing the precision of the ephemeris of K2-139 b. The transit times for this system can now be predicted for the next decade with a 1σ precision less than 10 minutes, compared to over one hour previously, allowing the efficient scheduling of observations with Ariel. We detect no significant deviation from a linear ephemeris, allowing us to exclude the presence of a massive outer planet orbiting with a period less than 150 days, or a brown dwarf with a period less than one year. We also determine the scaled semimajor axis, the impact parameter, and the stellar limb darkening with improved precision. This is driven by the shorter cadence of the CHEOPS observations compared to that of K2, and validates the subexposure technique used for analyzing long-cadence photometry. Finally, we note that the stellar spot configuration has changed from the epoch of the K2 observations; unlike the K2 transits, we detect no evidence of spot-crossing events in the CHEOPS data.

Unified Astronomy Thesaurus concepts: Extrasolar gaseous giant planets (509); Exoplanet astronomy (486); Exoplanets (498)

Supporting material: machine-readable table

1. Introduction

The atmospheres of many transiting exoplanets will be probed by Ariel, ESA’s M4 mission, which is due to launch in 2029 (Tinetti et al. 2018). Among the list of potential targets for Ariel is K2-139 b (Edwards et al. 2019). Maintaining accurate ephemerides of these targets is vital for the efficient operation of the mission. K2-139 b is one of the targets of interest of the ExoClock Project† (Kokori et al. 2022a, 2022b), which aims to monitor the Ariel targets and improve their ephemerides, and is listed as a “high” priority target as of 2022 March.

The issue of decaying ephemerides has also been studied recently from the point-of-view of NASA’s Transiting Exoplanet Survey Satellite (TESS; Ricker et al. 2015), which is expected to supply many of the bright targets for atmospheric characterization with Ariel and the James Webb Space Telescope (JWST; Gardner et al. 2006). Dragoni et al. (2020) found that if no further transits are observed, then around 80% of the best exoplanetary targets for JWST (as selected by Kempton et al. 2018) would have transit timing uncertainties greater than 30 minutes by the time of the earliest possible JWST observations.

Many systems will be (re)observed by TESS, which has completed its initial survey of the southern (Cycle 1) and northern (Cycle 2) skies, and is currently reobserving many of the Cycle 1 and 2 sectors. Klagyivik et al. (2021), for instance, recently updated the ephemerides of several transiting exoplanetary systems originally discovered by CoRoT (Moutou et al. 2013; Deleuil et al. 2018). However, according to the Web TESS Viewing Tool‡, no observations of K2-139 b are planned within the first five years of TESS operations (up to and including Sector 69). Many systems can also be observed from the ground, with relatively small telescopes (e.g., Edwards et al. 2020, 2021a, 2021b); however, longer-period systems such as K2-139 b are challenging targets for ground-based observations given their less frequent transits and longer transit durations.

K2-139 b was discovered during the repurposed Kepler satellite’s K2 mission (Howell et al. 2014). Photometry from K2’s Campaign 7 revealed three transits of K2-139 b, and the system was subsequently observed and confirmed as a true planetary system by Barragán et al. (2018; hereafter B18). According to B18, K2-139 b is a warm Jupiter with a radius of $R_{\text{Jup}} = 0.808 \pm 0.034 R_{\text{Jup}}$ orbiting an active K0V star every 28.4 days. Radial velocity (RV) measurements of the star from the FIES, HARPS, and HARPS-N spectrographs allowed the mass of the planet to be determined as $M_{\text{Jup}} = 0.083 \pm 0.003 M_{\text{Jup}}$. The 1σ uncertainty on the K2-139 b transit time predicted by the ephemeris of B18 reaches 30 minutes by early 2022, the time of the earliest JWST observations, and is well over an hour by the end of the decade, when Ariel may observe the system.

The spin–orbit angle or obliquity, i.e., the angle between the axis of stellar rotation and the orbital axis, of warm Jupiters is particularly interesting. Dynamical migration, whether through Kozai–Lidov cycles (Kozai 1962; Lidov 1962; Fabrycky & Tremaine 2007) or planet–planet scattering (Rasio & Ford 1996;
Weidenschilling & Marzari 1996) is expected to lead to planets on high-obliquity orbits. Warm Jupiters (unlike the closer-orbiting hot Jupiters) are not thought to experience strong enough stellar tidal forces to later coplanarize their orbits. This means that the obliquities of warm Jupiters offer a unique insight into migration history.

While the obliquity has been measured for a significant sample of hot Jupiters, mostly via the Rossiter–McLaughlin effect—but also through Doppler tomographic observations, gravity-darkened transits, and by spot-crossing events—this is not the case for the warm Jupiters. According to TEPCat (Southworth 2011), there are only nine obliquity measurements for warm Jupiters, compared to 120 for hot Jupiters. This is a result both of there being fewer known transiting warm Jupiters (49) than hot Jupiters (453), and of the difficulty, noted above, of observing the transits of longer-period planets from the ground.

Anomalies compatible with spot-crossing events were observed in all three transits observed by K2, and B18 note that this could be exploited to measure the obliquity of the system. This technique has been previously applied to the WASP-4 system (Sanchis-Ojeda et al. 2011) among others. Here, we present CHaracterising ExOPlanet Satellite (CHEOPS) observations of K2-139 with the goal of constraining the obliquity, as well as updating the orbital ephemeris, of K2-139 b.

2. CHEOPS Observations and Data Reduction

CHEOPS (Benz et al. 2021) is a small (0.32 m diameter) telescope designed for high-precision monoband photometry of individual exoplanetary systems. CHEOPS was launched in 2019 December, and science operations commenced in 2020 April, with several studies (e.g., Lendl et al. 2020; Barros et al. 2022) already published reporting results from the mission. We observed four transits of K2-139 b with CHEOPS, under the Guest Observers’ program AO-1-005 (PI: Smith).

The original aim was to observe four consecutive transits, to see if we could constrain the orbital obliquity of the system. Given the stellar rotation period of 17.24 ± 0.12 days (B18), and the orbital period of 28.4 days, we would expect around 29 per cent of the stellar hemisphere visible during the first transit to be visible during the second transit, 41 per cent during the third, and 88 per cent during the fourth transit. We could therefore have expected to observe K2-139 b crossing the same spots in multiple transits if the obliquity is close to zero, and the spots have sufficient longevity, which B18 suggests they may.

Due to scheduling constraints, however, we in fact observed two consecutive transits in 2020 June and July, and a second pair of consecutive transits in 2021 June and July. Each “visit” consisted of seven consecutive orbits of the CHEOPS satellite, or around 11.5 hr. With a G-band magnitude of 11.5, K2-139 is a relatively faint target for CHEOPS, and therefore an exposure time of 60 s was used. Further details of the observations are given in Table 1.

The data were reduced using the standard CHEOPS data reduction pipeline (DRP v13; Hoyer et al. 2020), which produces light curves using four different aperture radii: a “DEFAULT” radius of 25 pixels, a slightly smaller “RINF” radius of 22 pixels, a larger “RSUP” radius of 30 pixels, and an “OPTIMAL” radius. The size of the latter is determined on a per-visit basis, to account for the differing brightnesses of different targets, and is determined by minimizing the noise-to-signal ratio (Hoyer et al. 2020). All four visits of K2-139 have the same optimized aperture radius of 15 pixels. We extracted each of these four light curves, corrected for the “ramp” effect, using PYCHEOPS (Maxted et al. 2022). We tested each light curve, finding as expected that the light curves produced using the OPTIMAL radius give the highest signal-to-noise; this light curve is shown in Figure 1 and in Table 2.

3. Stellar Characterization

The previous characterization of K2-139 relied on a co-added FIES spectrum (B18). Here, we update the stellar characterization by fitting the spectral energy distribution (SED) of K2-139 using ARIADNE7 (Vines & Jenkins 2022). The Phoenixv2 (Husser et al. 2013), BTSettl (Allard et al. 2012), Castelli & Kurucz (2003), and Kurucz (1993) stellar atmospheric model grids were fitted to catalog photometry (Appendix A), constrained by the Gaia parallax. ARIADNE uses multiple model grids in order to account for the systematic errors arising from differences between different stellar atmosphere models. Gaussian priors from B18’s characterization were applied to Teff and [Fe/H], and the distance was constrained using the Gaia DR2 parallax (Gaia Collaboration et al. 2018). Reddening was accounted for, with AV limited to the maximum line-of-sight value from the SFD Galactic dust map (Schlegel et al. 1998; Schlauf & Finkbeiner 2011). Bayesian model averaging is employed by ARIADNE to derive the uncertainties from the posterior parameter distribution. The distributions for each model are averaged, weighted by the relative probability of each model, leading to smaller uncertainties than those obtained from any single model. ARIADNE has previously been used to characterize the primary star in several systems, both eclipsing binaries (Acton et al. 2020), and exoplanetary systems (Smith et al. 2021, 2022).

The stellar parameters resulting from our SED fit are listed in Table 3, where they are compared to the parameters from B18. Most parameters are in excellent agreement (discrepancies less than 1σ), but the stellar age from ARIADNE is significantly different to the gyrochronological value of B18. However, we note that the 3σ limits to the age from ARIADNE extend from as young as 43 Myr up to the current age of the universe; we conclude that the stellar age is poorly-determined. We use the new stellar mass and radius, along with the RV semiamplitude measured by B18 to determine the mass and radius of K2-139 b (Table 4).

4. Modeling the Photometry

4.1. Transit Model

We model the CHEOPS photometry using the Transit Light Curve Modeller (TLCM; Csizmadia 2020). The transits are

---

5 Throughout this work, we define hot Jupiters as having $M_p > 0.3 M_{\text{Jup}}$ and $P_{\text{orb}} < 10$ days, and warm Jupiters as planets with $M_p \geq 0.3 M_{\text{Jup}}$ and $10 \text{ days} \lesssim P_{\text{orb}} < 100$ days.

6 Note that the pixel scale of CHEOPS is approximately 1 pixel = 1″ (Benz et al. 2021).

7 https://github.com/jvines/astroARIADNE
modeled with the following fitted parameters: the planetary orbital period \((P_{\text{orb}})\), the transit epoch \((T_0)\), the scaled orbital semimajor axis \((a/R_\star)\), the planet-to-star radius ratio \((R_p/R_\star)\), the transit impact parameter \((b)\), and the limb-darkening coefficients \(u_+\) and \(u_-\) (which are related to the quadratic coefficients \(u_a\) and \(u_b\) by \(u_+ = u_a + u_b\) and \(u_- = u_a - u_b\)).

4.2. Systematics

In addition to the transit signal, we model the dominant source of systematic noise, which arises from the rotation of the satellite on its orbital period of 98.7 minutes (Benz et al. 2021). The roll angle of the spacecraft is provided as an additional light-curve column by the DRP (see Table 2), and is used to model the systematics. Adopting a similar approach to that employed by the PYCHEOPS software (Maxted et al. 2022), we model the roll angle dependent systematics of each CHEOPS visit with a function of the form,

\[
f_{\text{RA}} = \sum_{j=1}^{n_{\text{reg}}} = \alpha_j \sin(j\theta) + \beta_j \cos(j\theta)
\]

where \(\theta\) is the spacecraft roll angle, and the coefficients \(\alpha_j\) and \(\beta_j\) are fit as MCMC jump parameters within TLCM. We experimented with different values of \(n_{\text{reg}}\), and adopted \(n_{\text{reg}} = 2\) after determining that higher-order terms offer little-to-no improvement in the \(\chi^2\) of the model fit, and a higher Bayesian information criterion (BIC) value.

After initial modeling, as described above, it was apparent that there are additional sources of noise in the light curves, which we attribute to stellar activity. B18 reported variations in the K2 light curve with an amplitude of 1%–2%, modulated on the stellar rotation period of \(17.24 \pm 0.12\) days. We model this as a polynomial function of time for each CHEOPS visit, with the coefficients of the polynomial fitted in TLCM. We ultimately choose a linear function of time; we determined using the BIC that higher-order terms are not justified. Additionally, we modeled the remaining red noise present in the light curves with the wavelet approach of Carter & Winn (2009), as implemented in TLCM (Csizmadia et al. 2021), fitting for an additional two parameters: the white noise \((\sigma_w)\) and red noise \((\sigma_r)\) levels. This results in us fitting for a total of 33 parameters: seven parameters to describe the transits, and 26 for the various systematics (comprising four roll angle coefficients and two coefficients in time per transit, plus the two wavelet terms).

We also tested an alternative approach to modeling the roll angle dependent systematics. By excluding the data taken during transit, we plotted the out-of-transit flux as a function of roll angle for each of the four CHEOPS visits. We then

| Visit No. | Start Date (UTC) | Duration (h) | No. of Data Points | File_key | Efficiency\(^a\) (%) |
|-----------|------------------|--------------|--------------------|----------|----------------------|
| 1         | 2020 Jun 27 23:29 | 11.52        | 461                | CH_PR210005_TG000101_V0200 | 69.4     |
| 2         | 2020 Jul 26 11:38 | 11.52        | 561                | CH_PR210005_TG000201_V0200 | 64.2     |
| 3         | 2021 Jun 03 14:53 | 11.51        | 406                | CH_PR210005_TG000202_V0200 | 71.7     |
| 4         | 2021 Jul 01 22:33 | 11.46        | 469                | CH_PR210005_TG000203_V0200 | 66.6     |

Note.  
\(^a\) The efficiency is the fraction of the visit spent collecting data.

Figure 1. CHEOPS photometry of K2-139 produced by the DRP using the OPTIMAL aperture.
4.4. Spot-crossing Signal

Unlike the K2 transits, we see no evidence of a spot-crossing signal in any of the CHEOPS transits. In order to be certain that we did not miss any such signal, we also looked at the light curves and their residuals produced using each of the four photometric apertures (Section 2), fitted both with and without the wavelet red noise model. We also verified that a spot-crossing signal of the type seen in the K2 data would not be removed by our modeling of the systematic noise in the CHEOPS light curves. We did this by modeling the K2 spot-crossing signal with a toy model, and injecting this signal into the CHEOPS light curves, before fitting them with the procedure described above. This injected signal has an amplitude of 800 ppm, and a duration of 120 minutes. For comparison, the longest gap in the CHEOPS light curves is around 50 minutes, with gaps of 20–30 minutes more typical. The signal was still visible in the CHEOPS light curves, even after fitting them with the wavelet model. In common with B18, we find that excluding the K2 points affected by the spot crossings’ results in a change to the transit parameters, which is much smaller than the 1σ uncertainties on those parameters. We therefore opt not to exclude these points from the final fit.

4.5. Transit Timing

To measure the time of midtransit for each of the observed transits of K2-139 b, we refit each transit light curve individually, with $P_{orb}$ fixed to the value of our joint fit, and with priors corresponding to the posterior distribution of our joint fit placed on the other transit parameters. These transit times and their uncertainties are listed in Table 5, where they are also compared to the ephemeris reported by B18, and the ephemeris determined from our joint fit. Although the four CHEOPS transits show significant timing deviation from the B18 ephemeris, this is due to the insufficient precision of the period determined by B18, from just three sparsely-sampled transits. Our newly-determined $P_{orb}$ is six times more precise, and with this ephemeris, there is no evidence for any significant TTVs—the measured deviations of 2–7 minutes from our ephemeris are comparable to the timing precision of 1–7 minutes on the individual transits (Figure 4).

4.6. Orbital Eccentricity and Stellar Density

Alongside the K2 photometry, B18 fitted 19 RV measurements of K2-139, made with three different telescopes/spectrographs. They determined that a simple Keplerian model was a poor fit to the RVs, which are affected by stellar activity. To model this activity, they fit two additional sine curves to the

4.3. Joint fit with K2 Data

After modeling the CHEOPS data alone (the results of which are displayed in the middle column of Table 4, alongside the corresponding values from B18), we also performed a joint modeling of the CHEOPS and K2 photometry. Because the effective exposure time of the K2 data is relatively long (1800 s), we subdivide each exposure into five (as was done in e.g., Smith et al. 2018). We opt not to fit for separate limb-darkening coefficients in the two bandpasses, which is justified because (i) the bandpasses are overlapping and very similar (Figure 2), and (ii) the sparsely-sampled K2 data do not enable strong constraints to be placed on the limb-darkening coefficients.

Appendix B lists the limb-darkening coefficients obtained from our various fits, as well as theoretically calculated coefficients for the Kepler and CHEOPS bandpasses, computed using the ATLAS stellar models (Claret & Bloemen 2011; Claret 2021). As expected, given the very similar bandpasses, the differences between the theoretical values for Kepler and CHEOPS are small, and much smaller than the uncertainties on our fitted coefficients. The theoretical values also lie well within the 1σ uncertainties on our fitted coefficients.

A fit with separate limb-darkening parameters for the two instruments results in coefficients for K2 that are compatible with those obtained jointly, but less-precisely determined. Finally, the resulting transit parameters are not affected by our choice to fit for only a single set of limb-darkening coefficients, with the differences between the two parameter sets less than 1σ. The resulting parameters from the joint fit using a common set of limb-darkening coefficients are shown in the final column of Table 4, and the photometry is plotted alongside the best-fitting model in Figure 3.

| Parameter | Unit | Stellar Parameters of K2-139 |
|-----------|------|-----------------------------|
| $T_{\text{eff}}$ | K | 5340 ± 110 | 5245±113 |
| log$g$ | cgs | 4.50 ± 0.09 | 4.53 ± 0.05 |
| [Fe/H] | dex | 0.22 ± 0.08 | 0.20±0.09 |
| $v\sin i$ | km s$^{-1}$ | 2.8 ± 0.6 | ... |
| Distance | pc | 152 ± 10 | 156.5±20 |
| Age | Gyr | 1.8 ± 0.3 | 8.9±11 |
| $A_v$ | mag | 0.07 ± 0.05 | 0.05±0.06 |
| $R_t$ | $R_\odot$ | 0.862 ± 0.032 | 0.863±0.019 |
| $M_t$ | $M_\odot$ | 0.919 ± 0.033 | 0.883±0.023 |

Note. Only a sample is given here; the full table is available electronically from the CDS.

(Table is available in its entirety in machine-readable form.)

**Table 2**

| BJD$_{TDB}$ | Flux | Flux Uncertainty | Spacecraft | Roll Angle (°) |
|------------|------|-----------------|------------|----------------|
| 9028.503166 | 0.988975 | 0.000755 | 272.762 |
| 9028.503861 | 0.900507 | 0.000744 | 269.035 |
| 9028.504556 | 0.990557 | 0.000737 | 265.331 |

To model this activity, they fit two additional sine curves to the

To model this activity, they fit two additional sine curves to the
data, at the stellar rotation period and its first harmonic. This fit resulted in a small orbital eccentricity, $e = 0.13^{+0.12}_{-0.08}$, and a poorly-determined argument of periastron, $\omega = 124^{+175}_{-79}$. Since the B18 eccentricity value is consistent with zero at the 2$\sigma$ level, and relatively little information about orbital eccentricity is conveyed by transit light curves, we opt to impose a circular orbit solution, by fixing $e = 0$.

The stellar density calculated from the mass and radius produced by ARIADNE is $\rho_s = 1937 \pm 124$ kg m$^{-3}$, whereas the density from our fit to the K2 and CHEOPS transits is $\rho_s = 2593 \pm 211$ kg m$^{-3}$, which differ by around 2.7$\sigma$. We therefore tried fitting the light curves again, this time fixing $e$ and $\omega$ to the best-fitting values of B18. All of the resulting parameters and uncertainties are virtually identical to those from the circular orbit fit (with agreements well within 1$\sigma$), except we find $a/R_s = 43.3^{+0.9}_{-1.0}$, which is discrepant from the circular value by 2.4$\sigma$. The stellar density calculated with this value of $a/R_s$ is $\rho_s = 1905 \pm 183$ kg m$^{-3}$, which is in excellent agreement with the ARIADNE value. This suggests that the orbit of K2-139 b may indeed be slightly eccentric. We propose that a new RV study of K2-139 is needed to resolve the question of K2-139 b’s orbital eccentricity.

## 5. Results and Discussion

### 5.1. Updated System Parameters and Ephemeris

Our combined modeling of the K2 and CHEOPS photometry has resulted in better-determined transit parameters, particularly $a/R_s$ and the limb-darkening coefficients, which benefit from the shorter cadence of the CHEOPS observations. The precision in $R_p/R_s$ is, however, not improved by the CHEOPS data. This validates the approach of modeling the long-cadence K2 data using subexposures—this technique is still able to

![Figure 2. Comparison of Kepler/K2 (dashed line) and CHEOPS (solid line) instrument response as a function of wavelength. The Kepler data are taken from the Kepler Science Center, and the CHEOPS data from the ESA website.](https://www.cosmos.esa.int/web/cheops/performances-bandpass)
follow-up observations with e.g., Ariel to be planned and executed efficiently.

5.2. Transit Timing

As reported in Section 4.5 and Table 5, we find no evidence for TTVs. Our individual transit timings from CHEOPS have relatively large uncertainties, which is caused by poor sampling of the ingress and egress phases of the transits. Borsato et al. (2021) measured the transit times of several warm Jupiters with CHEOPS, achieving precisions ranging from around 20 s to about 4 minutes, depending on the brightness of the host star, and the efficiency of the in/egress phases. This range of precision is similar to that achieved by the CoRoT satellite for CoRoT-1b, whose data also suffered from some gaps (Csizmadia et al. 2010). K2-139 is fainter than all of the

Figure 3. Transit photometry of K2-139. The top panel shows the combined K2 and CHEOPS light curve, phase folded and with all the systematics and the red-noise wavelets subtracted. The original data points are plotted as small gray points, and the larger red circles are the same data binned in phase, with a bin width corresponding to 10 minutes. Below are the residuals to our best-fitting model. The lower panel shows the individual K2 and CHEOPS light curves, labeled with the corresponding instrument name and the UT date of midtransit, and vertically offset for clarity. In all cases, our best-fitting model is shown as a solid green line.
targets studied by Borsato et al. (2021), and none of our transits has good coverage of both ingress and egress, which is needed for the most-precise transit times. Good coverage of both ingress and egress would lead to transit times with a precision of around 30–60 s, as measured with CHEOPS for WASP-103 (Barros et al. 2022), which is slightly fainter than K2-139.

The presence of TTVs could be indicative of the presence of a companion planet; warm Jupiters are found to have companions more frequently than hot Jupiters (Huang et al. 2016). A full exploration of the properties of the external perturbers not excluded by our nondetection of TTVs is beyond the scope of this work. We can, however, place indicative upper limits on the maximum allowed mass of a putative outer planet, $M_c$, for a given orbital period, $P_c$, and eccentricity, $e_c$, of the perturber, using Equation (2) of Holman & Murray (2005) $^9$:

\[
M_c = \frac{16\pi}{45} M_* \frac{\Delta t_{\text{max}}}{P_{\text{orb}}} \left( \frac{P_c}{P_{\text{orb}}} \right)^2 (1 - e_c)^3, \tag{2}
\]

where $\Delta t_{\text{max}}$ is the maximum allowed TTV amplitude. We adopt $\Delta t_{\text{max}} = 15$ minutes, which is approximately three times the mean uncertainty on the timing of the CHEOPS transits.

In Figure 5 we plot the maximum allowed perturber mass as a function of orbital period for several values of $e_c$. Our constraints are not particularly strong, but we are able to exclude the presence of a massive planet orbiting with a period less than around 150 days or a brown dwarf with $P_c \lesssim 1$ yr. Much of the parameter space, however, is not excluded; for instance, the outer massive planet (or brown dwarf) in the K2-99 system, which is clearly visible in the RV measurements of the system (Smith et al. 2017, 2022), is only expected to induce TTVs for the inner warm Jupiter with an amplitude of just a few minutes. We would not have detected such a signal in our observations of K2-139, nor would we have detected the outer brown dwarf in the CoRoT-20 system (Deleuil et al. 2012; Rey et al. 2018).

5.3. Starspots

We conclude that there is no evidence for any spot-crossing event in the CHEOPS light curves, which suggests that there were no sufficiently large starspots along the transit chord at the time of these observations. This could be due to chance, or due to the reduced chromospheric activity at a quieter phase of K2-139’s stellar cycle.

Unfortunately this means that we are unable to place any constraint on the obliquity of K2-139 b. Measuring this quantity for warm Jupiters remains very interesting because the orbital distance of these systems means that their orbits are unlikely to be significantly affected by stellar tidal forces acting to circularize and coplanarize them. This means that an obliquity measurement for K2-139 b would represent the primordial obliquity, following whatever migration processes led the planet to its current orbit. Since different migration processes are expected to result in orbits with different obliquities, measuring this parameter for a sample of warm Jupiters would offer significant insight into migration history. Measuring the obliquity of K2-139 b may be possible via the Rossiter–McLaughlin effect, but any ground-based transit observation of this system is challenging given the lengthy orbital period and transit duration (there is at most one opportunity per year to observe a complete transit of K2-139 b from a given observing site).

CHEOPS is an ESA mission in partnership with Switzerland with important contributions to the payload and the

---

$^9$ With the location of the $\pi$ corrected as per Borkovits et al. (2011).
ground segment from Austria, Belgium, France, Germany, Hungary, Italy, Portugal, Spain, Sweden, and the United Kingdom.

This work has made use of data from the European Space Agency (ESA) mission Gaia (https://www.cosmos.esa.int/gaia), processed by the Gaia Data Processing and Analysis Consortium (DPAC; https://www.cosmos.esa.int/web/gaia/dpac/consortium). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the Gaia Multilateral Agreement.

This research has made use of the NASA Exoplanet Archive, which is operated by the California Institute of Technology, under contract with the National Aeronautics and Space Administration under the Exoplanet Exploration Program.

This publication makes use of The Data & Analysis Center for Exoplanets (DACE), which is a facility based at the University of Geneva (CH) dedicated to extrasolar planets data visualization, exchange and analysis. DACE is a platform of the Swiss National Centre of Competence in Research (NCCR) PlanetS, federating the Swiss expertise in Exoplanet research. The DACE platform is available at https://dace.unige.ch. We thank the anonymous referee for their careful reading of the manuscript, and for their comments, which improved the quality of this paper.

Sz.Cs. is supported by Deutsche Forschungsgemeinschaft Research Unit 2440: Matter Under Planetary Interior Conditions: High Pressure Planetary and Plasma Physics.

Facilities: CHEOPS, Gaia.

Software: TLCM (Csizmadia 2020), astropy (Astropy Collaboration et al. 2013; Price-Whelan et al. 2018).

Appendix A
Catalog Photometry of K2-139 used in the SED Fit

In this appendix, we list (in Table 6) the catalog photometry used for the SED fit of K2-139.

| Band         | Magnitude          |
|--------------|--------------------|
| 2MASS H      | 9.7680 ± 0.0220    |
| 2MASS J      | 10.1770 ± 0.0220   |
| 2MASS Ks     | 9.6600 ± 0.0230    |
| Johnson V    | 11.6780 ± 0.0130   |
| Johnson B    | 12.5090 ± 0.0150   |
| Tycho B      | 12.6210 ± 0.2050   |
| Tycho V      | 11.7400 ± 0.1370   |
| GaiaDR2 G    | 11.4626 ± 0.0005   |
| GaiaDR2 RP   | 10.8661 ± 0.0017   |
| GaiaDR2 BP   | 11.9296 ± 0.0022   |
| SDSS g'      | 12.0400 ± 0.0050   |
| SDSS i'      | 11.2250 ± 0.0120   |
| SDSS r'      | 11.4200 ± 0.0330   |
| SkyMapper u  | 13.8500 ± 0.0130   |
| SkyMapper v  | 13.4450 ± 0.0090   |
| SkyMapper g  | 11.8630 ± 0.0020   |
| SkyMapper r  | 11.4550 ± 0.0040   |
| SkyMapper i  | 11.9390 ± 0.0030   |
| SkyMapper z  | 11.1380 ± 0.0030   |
| WISE W1      | 9.6040 ± 0.0230    |
| WISE W2      | 9.6770 ± 0.0200    |
| GALEX (NUV)  | 18.3790 ± 0.0610   |
| TESS         | 10.9139 ± 0.0062   |
Appendix B
Comparison of Limb-darkening Coefficients for K2-139

In this appendix, we list (in Table 7) the limb-darkening coefficients for K2-139 obtained from our various fits.

References

Acton, J. S., Goad, M. R., Casewell, S. L., et al. 2020, MNRAS, 498, 3115
Allard, F., Homeier, D., & Freytag, B. 2012, RSPTA, 370, 2765
Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A, 558, A33
Barragán, O., Gandolfi, D., Smith, A. M. S., et al. 2018, MNRAS, 475, 1765
Barros, S. C. C., Akinsanmi, B., Boué, G., et al. 2022, A&A, 657, A52
Benz, W., Broeg, C., Fortier, A., et al. 2021, ExA, 51, 109
Borkovits, T., Csizmadia, S., Forgács-Dajka, E., Hegedűs, T., 2011, A&A, 528, A53
Borsato, L., Pietro, G., Gandolfi, D., et al. 2021, MNRAS, 506, 3810
Carter, J. A., & Winn, J. N. 2009, ApJ, 704, 51
Castelli, F., & Kurucz, R. L. 2003, in IAU Symp. 210, Modelling of Stellar Atmospheres, ed. N. Piskunov, W. W. Weiss, & D. F. Gray (San Francisco, CA: ASP), A20
Claret, A. 2021, RNAAS, 5, 13
Claret, A., & Bloemen, S. 2011, A&A, 529, A75
Csizmadia, S., 2020, MNRAS, 496, 4442
Csizmadia, S., Renner, S., Barge, P., et al. 2010, A&A, 510, A94
Csizmadia, S., Smith, A. M. S., Cabrera, J., et al. 2021, arXiv:2108.11822
Deleuil, M., Aigrain, S., Moutou, C., et al. 2018, A&A, 619, A97
Deleuil, M., Bonomo, A. S., Ferraz-Mello, S., et al. 2012, A&A, 538, A145
Dragomir, D., Harris, M., Pepper, J., et al. 2020, AJ, 159, 219
Edwards, B., Anisman, L., Changeat, Q., et al. 2020, RNAAS, 4, 109
Edwards, B., Changeat, Q., Yip, K. H., et al. 2021a, MNRAS, 504, 5671
Edwards, B., Ho, C. S. K., Osborne, H. L. M., et al. 2021b, arXiv:2111.10350
Edwards, B., Mugnai, L., Tinetti, G., Pascale, E., & Sarkar, S. 2019, AJ, 157, 242
Fabrycky, D., & Tremaine, S. 2007, ApJ, 669, 1298
Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2018, A&A, 616, A1
Gardner, J. P., Mather, J. C., Clampin, M., et al. 2006, SSRv, 123, 485
Holman, M. J., & Murray, N. W. 2005, Sci, 307, 1288
Howell, S. B., Sookeeck, C., Haas, M., et al. 2014, PASP, 126, 398
Hoyers, S., Guterman, P., Demangeon, O., et al. 2020, A&A, 635, A24
Huang, C., Wu, Y., & Triaud, A. H. M. J. 2016, ApJ, 825, 98
Husser, T.-O., Wende-von Berg, S., Dreizler, S., et al. 2013, A&A, 553, A6
Kempton, E. M. R., Bean, J. L., Louie, D. R., et al. 2018, PASP, 130, 114401
Klagyivik, P., Deeg, H. J., Csizmadia, S., Cabrera, J., & Nowak, G. 2021, FrASS, 8, 210
Kokori, A., Tsiaras, A., Edwards, B., et al. 2022a, ExA, 53, 547
Kokori, A., Tsiaras, A., Edwards, B., et al. 2022b, ApJS, 258, 40
Kozai, Y. 1962, AJ, 67, 591
Kurucz, R. L. 1993, VizieR On-line Data Catalog, VI/39
Lendl, M., Csizmadia, S., Delone, A., et al. 2020, A&A, 643, A94
Lidov, M. L. 1962, P&SS, 9, 719
Maxted, P. F. L., Ehrenreich, D., Wilson, T. G., et al. 2022, MNRAS, 514, 77
Moutou, C., Deleuil, M., Guillot, T., et al. 2013, Icar, 226, 1625
Price-Whelan, A. M., Sipőcz, B. M., Günther, H. M., et al. 2018, AJ, 156, 123
Rasio, F. A., & Ford, E. B. 1996, Sci, 274, 954
Rey, J., Bouchy, F., Stalport, M., et al. 2018, A&A, 619, A115
Ricker, G. R., Winn, J. N., Vanderspek, R., et al. 2015, JATIS, 1, 014003
Sanchis-Ojeda, R., Winn, J. N., Holman, M. J., et al. 2011, ApJ, 733, 127
Schlaufly, E. F., & Finkbeiner, D. P. 2011, ApJ, 737, 103
Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, ApJ, 500, 525
Smith, A. M. S., Acton, J. S., Anderson, D. R., et al. 2021, A&A, 646, 1813
Smith, A. M. S., Breton, S., Csizmadia, S., et al. 2022, MNRAS, 510, 5035
Smith, A. M. S., Cabrera, J., Csizmadia, S., et al. 2018, MNRAS, 474, 5523
Smith, A. M. S., Gandolfi, D., Barragán, O., et al. 2017, MNRAS, 464, 2708
Southworth, J. 2011, MNRAS, 417, 2166
Tinetti, G., Drossart, P., Eccleston, P., et al. 2018, ExA, 46, 135
Vines, J. I., & Jenkins, J. S. 2022, MNRAS, 513, 2719
Weidenschilling, S. J., & Marzari, F. 1996, Natur, 384, 619