Study of inclusive $D_s^{(*)\pm}$ production in $B$ decays and measurement of $B^0 \rightarrow D^{*-} D_s^{(*)+}$ decays using a partial reconstruction technique

The BABAR Collaboration

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Abstract

Electron-positron annihilation data collected by the BABAR detector near the $\Upsilon(4S)$ resonance are used to study the inclusive decay of $B$ mesons to $D_s^{\pm}$ and $D_s^{*\pm}$ mesons, where the $D_s^{\pm}$ is reconstructed using the decay $D_s^{\pm} \rightarrow \phi \pi^{\pm}$. The production fraction of inclusive $D_s^{(*)\pm}$ and the corresponding momentum spectra have been determined. The exclusive decays $B^0 \rightarrow D^{*-} D_s^{(*)+}$ are observed with a partial reconstruction technique which uses the soft pion from the $D_s^{(*)}$ decay in association with the reconstructed $D_s^{(*)\pm}$. The beam energy constraint is used to determine the missing mass recoiling against the $D_s^{\pm}$ system, showing a clear signal for this process. From the observed rates, preliminary results for the corresponding branching fractions have been obtained.

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1 Introduction

The production of the $D_s^{(*)\pm}$ meson in B decays allows one to study the mechanisms leading to the creation of a $c\bar{s}$ quark pair. The main diagram contributing to this decay is shown in Fig. 1. Other B decay diagrams also contribute, although at a lower level, but no attempt is made to quantify their rate in this paper. As has been pointed out in Ref. [1], the $b \to c\bar{s}c$ decay rate may be large and could help to explain the theoretical difficulties [2] in accounting simultaneously for the total inclusive B decay rate and the semileptonic branching fraction of the B meson. As a longer term goal, the measurement of the rate and momentum spectrum of $D_s^{\pm}$ meson produced in B decays beyond the kinematic limit for the process $B \to D_s^{*\pm}X_c$ could be used to study $b \to u$ transitions. Despite the fact that purely hadronic final states are more difficult to understand theoretically, one may use the particular decay described in this paper to extract $V_{ub}/V_{cb}$ [3].

This document reports measurements made with the BABAR detector of both the inclusive $D_s^{(*)\pm}$ production rates and momentum spectra in B decays and the branching fractions of two specific two-body B decay modes involving a $D_s^{(*)\pm}$ meson. The latter measurements are made using a partial reconstruction technique.

2 The detector and the data sample

A description of the BABAR detector and the definition of many general analysis procedures can be found in an accompanying paper [4]. Here only the components of the detector most crucial to this analysis are briefly summarized.

Charged particles are detected and their momenta measured by a combination of a central drift chamber (DCH) with a helium-based gas and a five-layer (double-sided) silicon vertex tracker (SVT), embedded in a 1.5 T solenoidal field produced by a superconducting magnet. The charged particle momentum resolution is approximately $(\delta p_T/p_T)^2 = (0.0015 p_T + 0.005)^2$, where $p_T$ is in GeV/$c$. The SVT, with typically 10 $\mu m$ single-hit resolution, provides vertex information in both the transverse plane and in $z$.

Particles are identified using a combination of measurements from all the BABAR components. Charged particle identification exploits ionization energy loss measured in the DCH and SVT as well as Cherenkov radiation measured in a ring imaging detector (DIRC). Electrons and photons are identified by the CsI electromagnetic calorimeter.

Multihadronic events produced in $e^+e^-$ annihilation at the PEP-II collider (SLAC) and collected with the BABAR detector have been used in this analysis. These data were taken at the $\Upsilon(4S)$ resonance center of mass energy and at an energy about 40 MeV below the $B\bar{B}$ threshold. The integrated luminosity for on resonance data is 7.73 fb$^{-1}$ and 1.17 fb$^{-1}$ for off resonance.
3 Inclusive $D_s^\pm$ production

3.1 $D_s^\pm$ reconstruction

The $D_s^\pm$ mesons are reconstructed using the mode $D_s^\pm \rightarrow \phi \pi^\pm$ with $\phi \rightarrow K^+K^-$. In order to obtain a sufficiently clean sample, particle identification is necessary. To this end, both energy loss $(dE/dx)$ information from the Drift Chamber and the Vertex Detector and the DIRC (a Cherenkov imaging detector) are used to identify the kaons produced in the $\phi$ decay.

The selection is based on the likelihoods given by each detector and uses, for each track, the ratio of likelihoods for the pion and the kaon mass hypotheses $L_\pi/L_K$. If this ratio is less than unity for at least one of the considered subsystems, the particle is selected as a kaon. The DIRC is used both in the positive identification mode and the veto mode. A tighter level of identification is also available using a total likelihood defined as the product of the likelihoods of each subsystem. In this case the track is tagged as a kaon if the ratio of the total likelihoods for the pion and kaon mass hypotheses is less than unity.

Three charged tracks coming from a common vertex are then combined to form a $D_s^\pm$ candidate. Two oppositely-charged tracks have to be identified as kaons, one of these using the basic criteria and the second one using the tighter selection. The $K^+K^-$ invariant mass must be within 8 MeV/$c^2$ of the nominal $\phi$ mass (see Fig. 2). In this particular decay, the $\phi$ meson is polarized longitudinally and therefore the angular distribution of the kaons has a $\cos^2 \theta_H$ dependence, where the $\theta_H$ is the angle between the $K^+$ in the $\phi$ rest frame and the $\phi$ direction in the $D_s^\pm$ rest frame. We require $|\cos \theta_H| > 0.3$, thereby keeping 97.5% of the signal while rejecting about 30% of the background.

Using the selection criteria described above, a reasonably clean signal of $D_s^\pm$ is observed (Fig. 3). The efficiency averaged over all momenta is $(40.5 \pm 1.0)\%$. It varies as a function of the $D_s^\pm$ momentum and ranges from 30% when the $D_s^\pm$ is at rest in the $\Upsilon(4S)$ rest frame to 55% for $p^* = 5$ GeV/$c$.

A clear signal of the Cabibbo-suppressed decay mode $D_s^\pm \rightarrow \phi \pi^\pm$ is also observed. A summary of the measured signal properties is given in the Table 1. The final production rates, however, are obtained from the invariant mass spectra fitted separately for different momentum intervals (Section 3.2). The measured mass difference $m_{D_s^\pm} - m_{D_s^\mp}$ agrees with the world average value of $99.2 \pm 0.5$ MeV/$c^2$ [3].

Table 1: Fitted parameters for $D_s^\pm \rightarrow \phi \pi^\pm$ and $D_s^{*\pm} \rightarrow D_s^\pm \gamma$ decay modes.

|                     | $D_s^\pm \rightarrow \phi \pi^\pm$ | $D_s^{*\pm} \rightarrow D_s^\pm \gamma$ |
|---------------------|-------------------------------------|-------------------------------------------|
| Fit                 | $N_{D_S} = 18269 \pm 202$           | $N_{D_s^{*\pm}} = 3029 \pm 151$          |
| $M$                 | $1968.5 \pm 0.1$ MeV/$c^2$         | $\Delta M = 143.4 \pm 0.3$ MeV/$c^2$     |
| $\sigma$            | $5.40 \pm 0.07$ MeV/$c^2$          | $\sigma_{\Delta m} = 7.4 \pm 0.4$ MeV/$c^2$ |
| $M_{D_s^\pm} - M_{D_s^{*\pm}}$ | $98.7 \pm 0.2$ MeV/$c^2$      |                                           |

3.2 Inclusive $D_s^{*\pm}$ momentum spectra

The number of $D_s^{*\pm}$ mesons is extracted by fitting the $\phi \pi^\pm$ invariant mass distribution for different momentum ranges in the $\Upsilon(4S)$ rest frame. The momentum bin width is 200 MeV/$c$, which is much
Figure 2: The $K^+K^-$ invariant mass spectrum for an integrated luminosity of $1.53 \text{ fb}^{-1}$. The solid line represents a fit using a Breit-Wigner function and a 1st order polynomial.

Figure 3: The $\phi\pi$ invariant mass spectrum for an integrated luminosity of $7.73 \text{ fb}^{-1}$.

larger than the momentum resolution. The $D_{s}^{\pm}$ momentum resolution averaged over all momenta obtained from the Monte Carlo is $5.6 \pm 0.3 \text{ MeV}/c$. The fit function is a single Gaussian distribution, both for the $D_{s}^{\pm}$ and the $D^\pm$. The width of the Gaussians are constrained to be the same and the combinatorial background is accounted for by an exponential distribution. The number of $D_{s}^{\pm}$ in the off-resonance data is extracted using the same fit function but with fixed values for $M_{D^\pm}$, $M_{D_{s}^{\pm}}$ and $\sigma$ obtained from the fit to the on-resonance data.

The number of reconstructed $D_{s}^{\pm}$ as a function of their momentum in the $\Upsilon(4S)$ rest frame is shown in Fig. 4 for on- and off-resonance data. The efficiency-corrected momentum spectrum is shown in Fig. 5.

Table 2: Analytical expressions for the fragmentation functions.

| Name of function       | Analytical expression                                      |
|------------------------|------------------------------------------------------------|
| Peterson et al.:       | $f(x_p) = \frac{N}{x_p} \left( 1 - \frac{1}{x_p} - \frac{\epsilon}{1-x_p} \right)^{-2}$ |
| Collins and Spiller:    | $f(x_p) = N \left( \frac{1-x_p}{x_p} + \frac{2-x_p}{1-x_p} \epsilon \right) (1 + x_p^2) \left( 1 - \frac{1}{x_p} - \frac{\epsilon}{1-x_p} \right)^{-2}$ |
| Kartvelishvili et al.:  | $f(x_p) = N x_p^\alpha (1-x_p)$                            |

In order to determine the $D_{s}^{\pm}$ momentum spectrum from the continuum, on-resonance data with momentum higher than $2.45 \text{ GeV}/c$ and off-resonance data scaled according to the luminosity ratio have been fitted after efficiency correction using 3 different fragmentation functions (see Table 2). The product of branching fraction, $\mathcal{B}(D_{s}^{\pm} \to \phi\pi^{\pm})$, times cross-section for $D_{s}^{\pm}$ production from continuum, $\sigma(e^+e^- \to D_{s}^{\pm}X)$, is obtained by integrating the function obtained from the fit (Fig. 5). The extracted values and $\chi^2/\text{dof}$ from the fits are shown in Table 3.
Table 3 shows the contribution of the different sources to the total systematic error for $\sigma(e^+e^- \rightarrow D_s^\pm X) \cdot B(D_s^\pm \rightarrow \phi\pi^\pm)$. Using the best fit, which is obtained with the Peterson function, we find $\sigma(e^+e^- \rightarrow D_s^\pm X) \cdot B(D_s^\pm \rightarrow \phi\pi^\pm) = 8.29\pm0.41\pm0.69$ pb. From a comparison of the results obtained using the other two parameterizations, we assign a conservative systematic error of 2% due to the assumed functional form.

The measured values are in good agreement with previously published results [7]. The momentum spectrum of the $D_s$ produced in B decays is obtained by subtracting bin-by-bin the value of the fit function to the on-resonance data after efficiency correction (Fig. 6).

Table 3: The parameters for the different fragmentation functions obtained from the fit and the measured cross section $\sigma(e^+e^- \rightarrow D_s^\pm X) \cdot B(D_s^\pm \rightarrow \phi\pi^\pm)$, and the $\chi^2/dof$ of the fit. Only the statistical errors are given.

| Name of function          | Shape parameter                  | $\sigma(e^+e^- \rightarrow D_s^\pm X) \cdot B(D_s^\pm \rightarrow \phi\pi^\pm)$, pb | $\chi^2/dof$ |
|---------------------------|----------------------------------|---------------------------------------------------------------------------------|--------------|
| Peterson et al.:          | $\epsilon=(12.5\pm0.6) \times 10^{-2}$ | 8.29\pm0.41                                                                     | 1.286        |
| Collins and Spiller:      | $\epsilon=(37.6\pm2.8) \times 10^{-2}$ | 8.69\pm0.46                                                                     | 3.559        |
| Kartvelishvili et al.:    | $\alpha=1.91\pm0.07$             | 8.63\pm0.33                                                                     | 5.338        |
Table 4: The systematic errors for $\sigma(e^+e^- \rightarrow D_s^\pm X) \cdot B(D_s^\pm \rightarrow \phi\pi^\pm)$.

| Source                      | Error (%) |
|-----------------------------|-----------|
| $B(\phi \rightarrow K^+K^-)$ | 1.6       |
| Particle id efficiency      | 0.8       |
| Tracking efficiency         | 7.5       |
| Luminosity                  | 3.0       |
| Total systematic error      | 8.3       |

3.3 Inclusive $D_s^\pm$ branching fraction in $B$ decays

By integrating the efficiency corrected momentum distribution, a total $D_s$ yield from $B$ meson decays of $37050 \pm 950$ events is found. This corresponds to the inclusive branching fraction of

$$B(B \rightarrow D_s^\pm X) = \left[\frac{3.6 \pm 0.9\%}{B(D_s^\pm \rightarrow \phi\pi^\pm)}\right] \%,$$

where the first error is statistical, the second is systematic and the third is the contribution of the $D_s^\pm \rightarrow \phi\pi^\pm$ branching fraction uncertainty [5]. Recognizing that this last uncertainty is common to all measurements, our result is slightly higher than the world average $(10.0\pm0.6\% [6])$ and in good agreement with the most precise measurement performed by CLEO [8]. The different sources of systematic errors are given in detail in Table 4. The dominant uncertainty comes from knowledge of the tracking efficiency, which is still the subject of detailed study [4].

As a cross check of the continuum subtraction procedure, we also subtracted directly the off-resonance data scaled by the luminosity ratio for on- and off-resonance. By this means, one obtains an inclusive branching fraction $B(B \rightarrow D_s^\pm X) = 12.0 \pm 0.5 \pm 1.1\%$, in agreement with the value reported above.

4 Inclusive $D_s^{*\pm}$ production

4.1 $D_s^{*\pm}$ reconstruction

$D_s^{*\pm}$ mesons are reconstructed using the decay $D_s^{*\pm} \rightarrow D_s^\pm\gamma$ with the subsequent decay $D_s^\pm \rightarrow \phi\pi$. $D_s^\pm$ candidates are selected by requiring the $\phi\pi$ invariant mass to be within 2.5 standard deviations ($\sigma$) of the peak value. These are then combined with “single photons” from the event. The later are defined by the following criteria:

- $E_\gamma > 50\text{ MeV}$ where $E_\gamma$ is the photon energy in the laboratory frame
- $E_\gamma^* > 110\text{ MeV}$ where $E_\gamma^*$ is the photon energy in the $\Upsilon(4S)$ frame
Table 5: Systematic errors for $\mathcal{B}(B \to D_s^{\pm} X)$.

| Source               | Error (%) |
|----------------------|-----------|
| Signal shape         | 0.9       |
| Background shape     | 0.4       |
| Continuum subtraction| 1.8       |
| Monte Carlo statistics| 2.0      |
| Bin width            | 0.7       |
| Total for $D_S$ yield| 2.9       |
| $N_{\bar{B}B}$       | 3.6       |
| $\mathcal{B}(\phi \to K^+K^-)$ | 1.6 |
| Particle id efficiency| 0.8     |
| Tracking efficiency  | 7.5       |
| Total systematic error| 9.0     |

Table 6: Systematic errors for $\mathcal{B}(B \to D_s^{*\pm} X)$.

| Source               | Error (%) |
|----------------------|-----------|
| Signal shape         | 5.0       |
| Continuum subtraction| 1.2       |
| Monte Carlo statistics| 4.8      |
| Bin width            | 3.0       |
| Total for $D_S$ yield| 7.7       |
| $N_{\bar{B}B}$       | 3.6       |
| $\mathcal{B}(D_s^{*\pm} \to D_S\gamma)$ | 2.7 |
| Photon efficiency    | 2.5       |
| $\mathcal{B}(\phi \to K^+K^-)$ | 1.6 |
| Particle id efficiency| 0.8     |
| Tracking efficiency  | 7.5       |
| Total systematic error| 12.0    |

- In order to reduce the combinatoric background, the candidate photon should not form a $\pi^0$ with $E_{\gamma\gamma}^*>200$ MeV when combined with any other photon in the event. The $\pi^0$ mass window is $115 < M_{\gamma\gamma} < 155$ MeV/c².

The distribution of the mass difference $\Delta M = M_{D_{s}^{\pm} \gamma} - M_{D_s^{\pm}}$ is shown in the Fig. A. A clear peak with $3030 \pm 150$ events is observed. The parameters obtained from the fit are summarized in Table A.

4.2 Inclusive $D_s^{*\pm}$ momentum spectra

The decay $D_s^{*\pm} \to D_s^{\pm} \gamma$, $D_s^{\pm} \to \phi\pi^{\pm}$ is used for the measurement of the $D_s^{*\pm}$ inclusive branching fraction and the momentum spectrum. The number of $D_s^{*\pm}$ mesons is extracted by fitting the $\Delta M = M_{D_s^{\pm} \gamma} - M_{D_s^{\pm}}$ invariant mass distribution for the different momentum ranges in the $\Upsilon(4S)$ rest frame. A momentum bin width of 400 MeV/c was chosen.

The efficiency corrected momentum spectrum is shown in Fig. B. Both on- and off-resonance points corresponding to $D_s^{*\pm}$ mesons produced from the continuum have been fit using different fragmentation functions (Table C). The cross section for $D_s^{*\pm}$ produced from continuum and the values of the fit parameters are shown in Table C.

Fig. C shows the momentum spectrum of $D_s^{*\pm}$ produced in B decays where the Peterson fragmentation function is used for continuum extrapolation. Using this distribution, we find for the continuum cross section $\sigma(e^+e^- \to D_s^{*\pm}X) \cdot \mathcal{B}(D_s^{\pm} \to \phi\pi^{\pm}) = 3.48 \pm 0.39 \pm 0.38$ pb.
4.3 Inclusive $D_s^{\pm}$ branching fraction in $B$ decays

In the same way as for the $D_s^\pm$ result, we integrate the efficiency corrected $D_s^{\pm}$ distribution and obtain a total yield from $B$ meson decays of $19300 \pm 1900$ events. From this we find the inclusive branching fraction to be

$$\mathcal{B}(B \rightarrow D_s^{\pm} X) = \left(6.8 \pm 0.7 \pm 0.8\right)\times\frac{3.6 \pm 0.9\%}{\mathcal{B}(D_s^\pm \rightarrow \phi\pi^\pm)}\%,$$

where the systematic errors are given in detail in Table 6.

Table 7: The parameters for the different fragmentation functions, the measured cross section $\sigma(e^+e^- \rightarrow D_s^{\pm} X) \cdot \mathcal{B}(D_s^\pm \rightarrow \phi\pi^\pm)$, and the $\chi^2$/dof obtained from the fit. Only the statistical errors are given.

| Name of function | Parameter | $\sigma(e^+e^- \rightarrow D_s^{\pm} X) \cdot \mathcal{B}(D_s^\pm \rightarrow \phi\pi^\pm)$, pb | $\chi^2$/dof |
|------------------|-----------|-------------------------------------------------|-----------|
| Peterson et al.: | $\epsilon=(7.9\pm0.8)\times10^{-2}$ | 3.48±0.39 | 1.260 |
| Collins and Spiller: | $\epsilon=(19.3\pm2.3)\times10^{-2}$ | 3.75±0.42 | 1.288 |
| Kartvelishvili et al.: | $\alpha=2.6\pm0.2$ | 3.61±0.29 | 1.725 |
Figure 8: The on-resonance (solid circles) and scaled off-resonance (open circles) $D_s^{*\pm}$ momentum spectrum after efficiency correction. The solid line shows the fit using the Peterson fragmentation.

Figure 9: The $D_{s}^{*\pm}$ spectrum after efficiency correction and continuum subtraction using the result of the fit. The Peterson fragmentation function is used for the fit of the continuum.

5 Branching fraction for $B^0 \to D^{*-} D^{(*)+}$ decays

In addition to the measurements of inclusive production rates for $D_{s}^{\pm}$ and $D_{s}^{*\pm}$, we have extracted the branching ratios for the decays $B^0 \to D^{*-} D_{s}^{+}$ and $B^0 \to D^{*-} D_{s}^{*+}$ based on a partial reconstruction method.

5.1 The partial reconstruction method

As discussed in the introduction, no attempt is made to reconstruct the $D^0$ decays. One combines a pion with the reconstructed $D_{s}^{(*)\pm}$ where the total $D_{s}^{(*)\pm} - \pi$ charge is zero and, assuming that their origin is a $B^0$ meson, we calculate the missing invariant mass. This should be the $D^0$ mass if the hypothesis is correct. Without the constraint of the $D^0$ mass, the direction of the $B$ meson is unknown. Although its angle with respect to $D_{s}^{\pm}$ direction can be deduced, the angle $\phi$ around this direction is undetermined. Using the beam energy constraint, the missing mass, which still depending on the unknown angle $\phi$ of the $B^0$ momentum vector, is computed from:

$$m_{\text{miss}} = \sqrt{(E_{\text{beam}} - E_{D_{s}^{*\pm}} - E_{\pi})^2 - (\vec{p}_{B} - \vec{p}_{D_{s}^{*\pm}} - \vec{p}_{\pi})^2}.$$  \hspace{1cm} (3)

In this analysis the missing mass is defined using an arbitrary choice for the angle $\phi$. We use the convention that the direction of the $B^0$ meson lies in the plane $\{\vec{p}_{\pi}, \vec{p}_{D_{s}^{(*)\pm}}\}$.

*All calculations in this section are performed in the $\Upsilon(4S)$ rest frame.
5.2 Signal extraction

Fully reconstructed $D_s^\pm$ and $D_s^{*\pm}$ are selected by requiring the measured $\phi\pi^\pm$ mass or $\Delta m = m_{\phi\pi^\pm} - m_{\phi\pi^\pm}$ to be within $2.5\sigma$ of the fitted mean value. Because of high combinatorial background in the mode with a $D_s^{*\pm}$, one may find several $D_s^{*\pm}$ candidates in an event. Therefore, we form a $\chi^2$ for each candidate defined by:

$$\chi^2 = \left( \frac{M_{\text{rec}} - M_{\text{mean}}} {\sigma_\phi} \right)^2 + \left( \frac{M_{D_s^{*\pm}} - M_{D_s^{*\pm}}} {\sigma_{D_s^{*\pm}}} \right)^2 + \left( \frac{M_{\Delta m} - M_{\Delta m}} {\sigma_{\Delta m}} \right)^2,$$

and take the candidate with the lowest value. The $D_s^{(*)\pm} - \pi$ pairs satisfying the kinematic constraints for the decay $B^0 \to D^{*}D_s^{(*)+}$ are fitted to a common vertex. To reduce further the continuum background, we use the event shape variable $R_2$, defined as the ratio of the second to zeroth order Fox-Wolfram moment, and require $R_2 < 0.35$.

The missing mass distributions for the $D_s^\pm - \pi$ and $D_s^{*\pm} - \pi$ are shown in Fig. 10 and 11 respectively. A clear signal is observed for both decays. The missing mass distribution is fitted with the sum of a Gaussian distribution for the signal and a background function given by

$$f_B(x) = \frac{C_1 (x_0 - x)^{C_2}} {C_3 + (x_0 - x)^{C_2}},$$

where $x$ is the calculated missing mass, $C_i$ are the parameters of the fit and $x_0$ is the end point, $m_{D_s} - m_{\pi} = 1.871\text{ GeV}/c^2$. The results of the fits for both decay modes are summarized in Table 8.
Table 8: Selection criteria and fit parameters for the missing mass distribution in partially reconstructed $B^0 \to D^{*-}D_s^{(*)+}$ decays.

| $B \to D_s^{(*)}D^{*-}$ | $B \to D_s^{(*)}D^{*-}$ |
|------------------------|------------------------|
| $\chi^2/dof=1.25$     | $\chi^2/dof=1.09$     |
| $N_{ev} = 628\pm55$  | $N_{ev} = 195\pm29$  |
| $m_{miss} = 1866.7 \pm 0.2$ MeV/c$^2$ | $m_{miss} = 1866.3 \pm 0.2$ MeV/c$^2$ |
| $\sigma = 2.31 \pm 0.15$ MeV/c$^2$ | $\sigma = 2.66 \pm 0.36$ MeV/c$^2$ |

5.3 Branching fractions for $B^0 \to D^{*-}D_s^+$ and $B^0 \to D^{*-}D_s^{*+}$

A Monte Carlo simulation of the $B^0 \to D^{*-}D_s^{(*)+}$ decay modes has been used to find the efficiencies. It is important to note that the $B^0 \to D^{*-}D_s^{*+}$ decay mode contributes to the missing mass distribution for the $D_s^\mp - \pi$ system, even though there is a missing photon from the $D_s^{*\mp}$. We show in Table 9 the reconstruction efficiencies for the different modes.

Table 9: The efficiencies for the partially reconstructed $B^0 \to D^{*-}D_s^{(*)+}$ decay modes. The columns show the contribution of the different generated modes to the $D_s^\mp - \pi$ and $D_s^{*\mp} - \pi$ missing mass distributions in the signal region.

| True mode | Reconstructed mode |
|-----------|--------------------|
|           | $D_s^\mp - \pi$    |
|           | $D_s^{*\mp} - \pi$ |
| $B^0 \to D^{*-}D_s^+$ | 32.8\pm1.8\%       |
| $B^0 \to D^{*-}D_s^{*+}$long.pol. | 15.8\pm1.2\% 9.1 \pm0.9\% |
| $B^0 \to D^{*-}D_s^{*+}$transv.pol. | 14.2\pm1.1\% 6.0 \pm0.7\% |

Although the amount of feed through from $B^0 \to D^{*-}D_s^{*+}$ to $B^0 \to D^{*-}D_s^+$ depends on the $D_s^{*\mp}$ polarization, one sees from Table 8 that the variation is small. However the reconstruction efficiency for $B^0 \to D^{*-}D_s^{*+}$ has a much larger dependence on the polarization. Since this polarization is not known, we use the average efficiency of $(7.5 \pm 1.5)\%$, where the systematic error of 1.5\% is derived by comparing the efficiencies from the two polarization states. This is combined with the other systematic errors which are in common with the inclusive branching fractions presented in the previous sections.

For the measurement of the $B^0 \to D^{*-}D_s^+$ branching fraction, the contribution to the missing mass peak from $B^0 \to D^{*-}D_s^+$, where a random $\gamma$ is associated to the $D_s^\mp$, is negligible. The contribution of $B^0 \to D^{*-}D_s^{*+}$ to the mode $B^0 \to D^{*-}D_s^+$ is then subtracted to determine the branching fraction for the latter. The results are given in Table 10. The first error is statistical, the third reflects the uncertainty due to the error in the branching ratio for $D_s^\mp \to \phi \pi^\pm$, and the second error represents all remaining systematics. This last is dominated by the uncertainty due
to the dependence of the efficiency on the polarization of the final state.

Table 10: The measured branching fraction for $B^0 \to D^*-D_s^+$ and $B^0 \to D^{*-}D_s^{*+}$.

| Preliminary | $B \to D^+_sD^-$ | $B \to D^{*+}_sD^*$ |
|-------------|------------------|----------------------|
| $\mathcal{B} = (7.1 \pm 2.4 \pm 2.5 \pm 1.8) \times 10^{-3}$ | $\mathcal{B} = 2.54 \pm 0.38 \pm 0.53 \pm 0.64\%$ |
| PDG: $\mathcal{B} = (9.6 \pm 3.4) \times 10^{-3}$ | PDG: $\mathcal{B} = 2.0 \pm 0.7\%$ |

Finally, one should note that the reconstructed $B^0 \to D^*-D_s^{*+}$ events should allow us to measure the polarization of the $D_s^{*\pm}$ in these decays and therefore, in future analyses, it will be possible to reduce the systematic error from this source.

5.4 Background cross checks

In order to investigate further the shape of the background which is subtracted for estimating the signal, we have compared the Monte Carlo to the data. Several types of backgrounds contribute in the signal region:

1. Fake $D_s^{(*)\pm}$ and a random pion (for example coming from the other B).
2. Fake $D_s^{(*)\pm}$ and correlated pion (for example coming from the same B).
3. True $D_s^{(*)\pm}$ and a random pion.
4. True $D_s^{(*)\pm}$ and a correlated pion.

Table 11 shows the different types of backgrounds and the methods which are used to determine their level. Background types 1 + 3 are obtained by flipping the $D_s^{(*)\pm}$ direction. Background types 1 + 2 are extracted using the sidebands of the $D_s^{(*)\pm}$ mass distribution. For this purpose, we take $1.89 < M_{D_s^{(*)\pm}} < 1.95$ and $1.985 < M_{D_s^{(*)\pm}} < 2.05$ GeV/$c^2$ for the $D_s^{*\pm}-\pi$ system, and $\Delta M_{D_s^{(*)\pm}} < 300$ MeV/$c^2$ for $D_s^{*\pm}-\pi$. By flipping the $D_s^{(*)\pm}$ direction for the sidebands we find the contribution of background type 1. Therefore the difference between the distributions for flipped and non-flipped $D_s^{(*)\pm}$ direction for the sidebands gives the type 2 background contribution and thus it is possible to find the contribution of background types 1 + 2 + 3 from data alone. Fig. 12 and 13 show the resulting signal after their subtraction. The remaining background component is quite small and is estimated from the Monte Carlo. To ensure that the simulation reproduce the data well, a systematic comparison is made for the missing mass distribution obtained from the $D_s^{(*)\pm}$ signal region, the $D_s^{(*)\pm}$ sideband region, and the wrong-sign $D_s^{(*)\pm} - \pi$ combinations both in the $D_s^{(*)\pm}$ signal and the $D_s^{(*)\pm}$ sideband regions. The ratio (Data-Monte Carlo)/Monte Carlo for all these cases are determined as a function of the missing mass. We find good agreement within the errors in all cases. Table 12 summarizes this result by showing the ratio integrated over the missing mass region 1.78 to 1.87 GeV/$c^2$ for all distributions except that with the signal, for which the range 1.78 to 1.85 GeV/$c^2$ is used.
Table 11: The different data samples which can be used to determine the background in the $D^0$ signal region.

| Background                      | Flip $D_s^{(*)\pm}$ | $D_s^{(*)\pm}$ Side-bands | Side-bands flip $D_s^{(*)\pm}$ |
|--------------------------------|----------------------|---------------------------|-------------------------------|
| 1. Fake $D_s^{(*)\pm}$ + random $\pi$ | x                    | x                         | x                             |
| 2. Fake $D_s^{(*)\pm}$ + correlated $\pi$ |                      |                           |                               |
| 3. True $D_s^{(*)\pm}$ + random $\pi$   | x                    |                           |                               |
| 4. True $D_s^{(*)\pm}$ + correlated $\pi$ |                      |                           |                               |

Table 12: The comparison of the different data samples with Monte Carlo.

| Sample type                      | $B^0 \to D^{*-}D_s^+$ ($N_{\text{data}} - N_{\text{MC}})/N_{\text{MC}}$ | $\chi^2/\text{dof}$ | $B^0 \to D^{*-}D_s^{*+}$ ($N_{\text{data}} - N_{\text{MC}})/N_{\text{MC}}$ | $\chi^2/\text{dof}$ |
|---------------------------------|------------------------------------------------------------------|---------------------|------------------------------------------------------------------|---------------------|
| $D_s^{\pm}$ Signal              | 0.051$\pm$0.025                                                  | 1.008               | 0.103$\pm$0.057                                                  | 1.058               |
| Flip $D_s^{\pm}$                | -0.043$\pm$0.031                                                 | 0.841               | -0.041$\pm$0.064                                                 | 0.832               |
| $D_s^{\pm}$ Sideband            | 0.006$\pm$0.018                                                  | 1.391               | -0.031$\pm$0.053                                                 | 1.194               |
| Flip $D_s^{\pm}$ Sideband       | 0.015$\pm$0.021                                                  | 1.627               | 0.084$\pm$0.069                                                  | 1.690               |
| Wrong Sign                      | -0.031$\pm$0.029                                                 | 0.987               | 0.010$\pm$0.063                                                  | 1.088               |
| WS, $D_s^{\pm}$ Sideband        | 0.030$\pm$0.020                                                  | 1.311               | 0.034$\pm$0.065                                                  | 1.487               |

6 Conclusion

The production of $D_s^{(*)\pm}$ at the $\Upsilon(4S)$ energy (and 40 MeV below) has been studied with the BABAR detector. Preliminary measurements of branching fractions for inclusive production and for the exclusive decays $B^0 \to D^{*-}D_s^{*+}$ have been performed. The following cross sections have been found for production in the continuum:

- \[
\sigma(e^+e^- \to D_s^{\pm} X) \cdot B(D_s^{\pm} \to \phi\pi^\pm) = 8.29 \pm 0.41 \pm 0.69 \text{ pb ,}
\]
- \[
\sigma(e^+e^- \to D_s^{*\pm} X) \cdot B(D_s^{\pm} \to \phi\pi^\pm) = 3.48 \pm 0.39 \pm 0.38 \text{ pb .}
\]

Using the on-resonance data, the inclusive branching fraction for the $B$ meson decays

- \[
B(B \to D_s^{\pm} X) = \left(11.90 \pm 0.30 \pm 1.07\right) \times \frac{3.6 \pm 0.9\%}{B(D_s^{\pm} \to \phi\pi^\pm)} \%
\]
- \[
B(B \to D_s^{*\pm} X) = \left(6.8 \pm 0.7 \pm 0.8\right) \times \frac{3.6 \pm 0.9\%}{B(D_s^{\pm} \to \phi\pi^\pm)} \%
\]
have been measured. Finally the decays $B^0 \rightarrow D^{*-}D^+_s$ and $B^0 \rightarrow D^{*-}D^{(*)+}_s$ have been observed using a partial reconstruction technique and the following branching fractions have been determined:

$$B(B \rightarrow D^+_sD^{*-}) = (7.1 \pm 2.4 \pm 2.5 \pm 1.8) \times 10^{-3},$$

$$B(B \rightarrow D^{(*)+}_sD^{*-}) = (2.54 \pm 0.38 \pm 0.53 \pm 0.64)\%.$$ 

The results obtained are in a good agreement with previous measurements by other experiments.

The measurement of inclusive branching fraction of $D^{*-}_s$ from $B$ decay has been obtained for the first time.

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