Precision measurement of the half-life and the decay branches of $^{62}\text{Ga}$

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Abstract

In an experiment performed at the Accelerator Laboratory of the University of Jyväskylä, the β-decay half-life of $^{62}\text{Ga}$ has been studied with high precision using the IGISOL technique. A half-life of $T_{1/2} = 116.09(17)$ ms was measured. Using β-γ coincidences, the γ intensity of the 954 keV transition and an upper limit of the β-decay feeding of the $0^+\rightarrow 0^+$ state have been extracted. The present experimental results are compared to previous measurements and their impact on our understanding of the weak interaction is discussed.

1 Introduction

Studies of superallowed $0^+ \rightarrow 0^+$ pure Fermi transitions and the precise determination of their ft value are important as tests for the weak interaction theory. The corrected Ft-value of these transitions serves as a stringent test for the Conserved Vector Current (CVC) hypothesis, for the determination of the vector coupling constant $G_\nu$ of nuclear β-decay and for the validity of the three-generation Standard Model through the determination of the $V_{ud}$ element of the Cabbibo-Kobayashi-Maskawa (CKM) quark mixing matrix. The following relation links the coupling constant $G_\nu$ to the corrected Ft-value $[1]$

$$F_t = ft(1 + \delta_R^v)(1 + \delta_{NS}^v - \delta_C^v) = \frac{k}{2G^2(1 + \Delta_R^v)} \quad (1)$$

Here, $f$ is the β-decay phase space factor, $t$ is the partial half-life, $k$ is a constant ($k/\hbar c = (8120.271 \pm 0.012) \times 10^{-10}$ GeV$^{-4}s$) $[1]$, $\delta_R$, $\delta_{NS}$ and $\delta_C$ are radiative corrections and $\delta_C$ accounts for the deviation of the parent and daughter states from perfect isospin symmetry. Presently, nine transitions have been measured to a precision equivalent or better than $10^{-3}$ : $^{10}\text{C}$, $^{14}\text{O}$, $^{26}\text{Al}^m$, $^{34}\text{Cl}$, $^{38}\text{K}^m$, $^{42}\text{Sc}$, $^{46}\text{V}$, $^{50}\text{Mn}$ and $^{54}\text{Co}$ $[1,2]$. The data concerning these transitions confirm the CVC hypothesis at the $3 \times 10^{-4}$ precision level but until very recently the unitarity of the first row of the CKM matrix was not confirmed at more than 2.2 standard deviations $[2,3]$. New measurements seem to indicate that the value of the up and strange mixing matrix element ($V_{us}$) was too low $[4]$. The new value of $V_{us}$ could indicate that unitarity may be completely restored ($\Sigma V^2_{ij} = 0.9999(16)$ instead of 0.9968(14) before). However, more measurements are certainly needed to confirm this finding.

Deviation from unitarity would have important consequences for the description of the weak interaction through the Standard Model. However, before claiming new physics beyond the standard model, a very careful determination of the corrected $F_t$-value is needed, where especially the isospin symmetry breaking factor $\delta_C$ is an important input. In fact, different model calculations predict that this correction could strongly increase for heavier N=Z, odd-odd nuclei. Therefore measurements for these heavier nuclei are needed to test the evolution of the correction and thus to check nuclear models used for the calculations.

The aim of this work is a precise determination of

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the half-life of $^{62}$Ga as well as of its decay branches which are part of the inputs necessary to calculate the corrected $Ft$ value for $^{62}$Ga. This experiment constitutes part of the efforts \[1\] at IGISOL in Jyväskylä to measure the half-life and the $\beta$-decay branching ratios as well as, using the new IGISOL ion trap, the masses of $^{65}$Zn and $^{62}$Ga in order to extract the Q value of the reaction.

The half-life has been measured several times \[2, 3, 4\] in the past, however, except for the very recent experiment performed at GSI \[5\], the precision on the result was too low to be included in the CVC test and the determination of the CKM matrix unitarity. The results presented in this paper achieve the necessary precision concerning the half-life.

## 2 Experimental setup

The $^{62}$Ga activity was produced via the $^{64}$Zn(p,3n) fusion-evaporation reaction. The $\beta$ decay of $^{62}$Ga was studied after mass separation using the IGISOL technique \[11, 12\] which is independent of the chemical and physical properties of the elements and well suited for short-lived activities. The 3 mg/cm$^2$ $^{64}$Zn target used as the entrance window of the light-ion guide was bombarded with a 48 MeV proton beam (20 $\mu$A) from the $k = 130$ Jyväskylä cyclotron.

The 40 keV mass-separated $A=62$ beam was impinging on a 1/2 inch wide movable tape at the end of the central IGISOL beam line. The tape was located at the center of a $4\pi$ cylindrical plastic scintillator (2 mm thick, 12 mm diameter entrance hole) which was used for $\beta$ detection. The scintillation light was collected by two 2-inch photomultiplier tubes in coincidence through a special light guide. The coincidence requirement allowed us to remove most of the photomultiplier noise. The $\beta$-particle detection efficiency was 90 %. Three co-axial germanium detectors (40% relative efficiency) in close geometry were used in order to provide $\beta$-$\gamma$ and $\beta$-$\gamma$-$\gamma$ coincidence data. They were mounted at a typical distance of 40 mm from the source point and had a total photopeak efficiency of 3.4 % at 1 MeV.

To provide grow-in and decay sequences of the activities, the IGISOL beam was pulsed ($T_{ON} = 400$ ms, $T_{OFF} = 1600$ ms) and the implantation tape was moved at the end of the beam-off period. We added a 100 ms beam off sequence just before the beam-on period as shown in figure 1. This yielded a well-defined background and allowed for a clean separation of the different contributions ($^{62}$Ga, $^{62}$Cu, constant background) in the decay spectrum.

In order to minimize systematic effects linked to the data acquisition system, we used three independent acquisition systems (DAQ) which worked with different parameters (fixed dead time, type of records and spec-

![Figure 1: Schematic view of the beam-on/beam-off cycle used in the present experiment together with the acquisition cycle and the tape transport.](image)

### Table 1: Characteristics of the three independent data acquisition systems used during the experiment.

| DAQ | Fixed dead time | Time binning | Running mode | Recorded data |
|-----|-----------------|--------------|--------------|---------------|
| N°1 | 30 $\mu$s       | 1 ms/ch      | listmode     | time distribution |
|     |                 |              | $\beta$ energy spectra |                |
|     |                 |              | $\gamma$ energy spectra |                |
|     |                 |              | counting rate |                |
| N°2 | 5 $\mu$s        | 1 ms/ch      | cycle        | time distribution |
|     |                 |              |              |                |
| N°3 | 5 $\mu$s        | 10 ms/ch     | run          | time distribution |
|     |                 |              |              |                |

3 Half-life measurements

The first paragraph of this section will be devoted to the way we did the analysis for each acquisition system.
In the second part, we will investigate the possible systematic error sources as well as the influence of the different contaminants and finally we will present the half-life results.

3.1 Analysis with three acquisition systems

As mentioned above, DAQ 1 stored the data in an event-by-event mode. As in addition to the time distribution also the energy signals from the photomultipliers were written on tape, software conditions allowed to remove the noise contribution to the events stored. Different cuts were applied; however, no influence on the half-life could be observed.

As the data were written in listmode, the beam-on/beam-off cycles could be reconstructed offline and time spectra were obtained for each cycle. Therefore, the data from DAQ 1 and DAQ 2 could be analysed on a cycle-by-cycle basis which will be described shortly in the following.

Before accepting a cycle for further analysis, different checks were performed: i) the counting rate for the cycle had to be higher than a user defined limit (we tested different limits in order to make sure that the counting rate limit does not alter the half-life. We finally used 20 counts per cycle as the limit). ii) A fit of the time distribution of each cycle was performed with a function taking into account the different contributions to the time spectrum. This fit had to yield a reduced $\chi^2$ value of better than 5 (other values were tested as well, but no influence could be found on the half-life).

Cycles which passed these two selection criteria were then corrected channel-by-channel for the dead-time. For this purpose, each channel content was divided by a correction factor of $f_{dt} = 1/(1 + t_{dt}R)$ where $t_{dt}$ is the fixed dead-time and $R$ is the counting rate per second in each channel. After this correction, the cycles were summed up to yield the time spectrum for a given run.

In order to make sure that the data analysis does not introduce any bias to the half-life, a set of simulation data was generated for each accepted cycle using the same counting rate for the different contributions ($^{62}$Ga, $^{62}$Cu, constant background), as determined during the cycle fitting mentioned above. For the half-life, fixed values were used for $^{62}$Ga (116.2 ns) and for $^{62}$Cu (584.4 s). We should mention that due to its very long half-life (9.186 h) compared to both $^{62}$Ga and $^{62}$Cu, we always considered the $^{62}$Zn contribution as a constant background. These simulated data were subject to the same dead-time as the fixed dead-time used experimentally (30 $\mu$s and 5 $\mu$s for DAQ 1 and DAQ 2, respectively). This procedure created a simulated data set equivalent to the experimental data, except that the input half-life was known. The aim was to obtain the input half-life after treatment of the simulated data with the same programs as the experimental data.

More details about the selection criteria, the fitting procedure and the generation of the simulated data sets can be found in reference [10].

The data acquisition DAQ 3 stored all the data for a given run. Therefore, no correction for the fixed dead-time was possible. However, as could be shown with the data from DAQ 2, the dead-time correction, for a fixed dead-time as short as 5$\mu$s and the counting rate of the present experiment (less than 1000/s), had only a minor influence (0.08ms) on the half-life determined. Assuming the same change in half-life for DAQ 3, we will corrected the half-life from DAQ 3 by this time and add it quadratically to the error for DAQ 3.

For the whole body of data, the further analysis was then very similar. In a first fit with fixed half-lives for $^{62}$Ga and $^{62}$Cu, the fit parameters for the counting rates of the different contributions were determined. This fit was performed over the whole time range of the cycles. A second fit over the whole time range was then performed with the $^{62}$Ga half-life as an additional free parameter. The final fit was performed on the decay part of the spectrum only, with three free parameters: the $^{62}$Ga rate and half-life as well as the background rate. The parameters describing the $^{62}$Cu contribution were kept at the values from the previous fit. The fact that we fixed the $^{62}$Cu contribution does not influence the fit results in any significant way. In fact, due to its rather long half-life (584.4 s), the $^{62}$Cu contribution can basically be treated as a constant background in the decay part of the time distribution (see below).

This third fit yielded the final half-life value for each run and each data acquisition system.

3.2 Systematic errors and possible influences of contaminants

As we performed part of the fits on the whole time range of the cycles, the beam-on and beam-off times are crucial for a good description of the experimental spectra by the fit. In order to study the influence of the exact time stamp when the beam was switched on or off, we performed fits to the data with fixed switching times (100 ms and 500 ms after the start of a cycle) and with variable switching times, where the times were treated as fit parameters. As the quality of the fit and thus the resulting half-life depended strongly on these times, we finally used fixed values, however, as adjusted in the analysis where they were treated as free parameters.

An important correction to the half-life comes from the dead-time. In order to study the influence of this correction, we performed tests with different fixed dead-times generated by hardware for DAQ 1 and DAQ 2. The half-life values determined for $^{62}$Ga for fixed dead-times of 2$\mu$s and 5$\mu$s were in nice agreement. In ad-
dition, DAQ 3 had a much longer dead-time of 30 µs. After correction we obtained half-life values in agreement with DAQ 1 and DAQ 2 for each run.

An independent check of the dead-time correction as well as of other parts of the analysis procedure was performed with the simulated data mentioned above. As shown below, after analysis of these data the input half-life was nicely reproduced.

Another check performed on the data was to start the fit later in the time spectrum. If the spectra were affected by a significant dead-time, a fit from the beginning of the decay curve should yield a longer half-life than a fit where the first part of the decay-time distribution is excluded. Such a behaviour could be explained by the fact that the first part of the time distribution is more subject to dead-time due to its higher counting rate than a later part in the time distribution. However, no effect was observed.

As the IGISOL system is not chemically selective, all mass A=62 nuclei produced in the reaction are transported to the detection station. This means for example that much more $^{62}$Cu and $^{62}$Zn was deposited on the collection tape. However, as mentioned above, due to its rather long half-life $^{62}$Zn is not of concern. In contrary, $^{62}$Cu has to be considered as its production rate was about 250 times higher than the one of $^{62}$Ga. Therefore we tested different procedures in order to take into account the $^{62}$Cu distribution. It turned out that this contaminant could be treated as a constant contamination in the decay part of the spectrum. In fact, whatever we did with the $^{62}$Cu contribution, the fit adjusted the level of the background in the opposite way, as it is expected for a basically constant contribution from $^{62}$Cu.

Finally, the fact that consistent results have been obtained for the three acquisition systems indicates that acquisition related phenomena like the dead-time were treated correctly.

### 3.3 Half-life results

Approximately $10^7$ β decay events of $^{62}$Ga were recorded. Figure 2 presents the experimental data and the result of the fit for one run together with its extracted half-life.

The half-life determined for each run and each acquisition system as well as the reduced χ² value for each individual fit are shown in figure 3. The half-lives scatter around 116 ms and the reduced χ² values are close to unity except for one low-statistics run. The error-weighted average yields the final half-life for each data acquisition system and its associated analysis. However, due to the fact that the averaging procedure does not give an acceptable reduced χ² value for two of the data acquisition systems, we normalized the error bars of the individual half-lives for each run by the square root of the reduced χ² value, as proposed by the Particle Data Group [14]. The new average obtained with the increased error bars yields the final result for each data set. These results are given in table 2. As our final result we adopt the error-weighted average of these three results. However, as the data for the three acquisition systems originate from the same data sample, we keep as the final error the smallest error bar of the three data acquisitions. This result is therefore 116.09(17) ms. It will be compared below to other experimental half-lives.

![Figure 2: Experimental data and fit for one run. The fit was performed with two exponential components plus a constant background. The lines show the different contributions of $^{62}$Ga, $^{62}$Cu and the background. The fits yields a half-life of 116.27(72) ms. It corresponds to about $6 \times 10^5$ $^{62}$Ga detected for this particular run.](image)

![Table 2: Half-lives determined for each acquisition system. These values are already corrected for the reduced χ² value of the averaging procedure for the different runs. For DAQ 3, we corrected for the dead time as discussed above and increased the error accordingly. The last column corresponds to the error-weighted average value of the three acquisition systems together with the smallest of the individual error bars.](image)
4 Branching ratios

Another goal of the experiment described here was to measure branching ratios for all important decay branches, in particular for allowed Gamow-Teller branches and non-analog Fermi transitions, with the Fermi transition to the first excited 0\(^{+}\) state in \(^{62}\)Zn located at 2.33 MeV being the most important transition to measure. If observed, the branching ratio for the 0\(^{+}\) \(\rightarrow\) 0\(^{+}\) transition allows for a direct comparison to theoretical prediction of one part of the isospin-mixing correction \(\delta_{c}\).

Figure 5 shows the \(\beta\)-gated \(\gamma\)-ray spectra in the vicinity of the 954 keV \(\gamma\)-ray from the decay of the first excited 2\(^{+}\) state in \(^{62}\)Zn. After efficiency correction and normalisation to the number of \(^{62}\)Ga implanted, we find a \(\gamma\) branching ratio for this line of (0.11 ± 0.04) %.

5 Discussion and conclusions

Our experimental result for the half-life of \(^{62}\)Ga of \(T_{1/2} = 116.09(17)\) ms is in nice agreement with all previous half-life measurements (see table 3 and figure 6). It is the second most precise value ever measured. The fact that all experimental half-lives are in agreement gives some confidence that the half-life of \(^{62}\)Ga is known now with sufficient precision in order to serve for the determination of the corrected \(F_t\) value for the super-allowed \(\beta\) decay of \(^{62}\)Ga. By averaging the experimentally measured half-life values, we obtain the new recommended half-life of \(^{62}\)Ga of 116.175(38) ms.

Several \(\beta\)-decay branching ratio measurements of \(^{62}\)Ga have been published recently \([5, 9, 15]\) and they are all in excellent agreement with our results. As mentioned above, we find that the intensity of the 954 keV

According to selection rules, the 2\(^{+}\) state can not be fed directly by an allowed \(\beta\) decay. The explanation is that the 2\(^{+}\) state acts as a collector state which collects most of the \(\beta\)-decay strength from higher-lying 0\(^{+}\) and 1\(^{+}\) levels. Therefore, we searched also for \(\gamma\)-\(\gamma\) coincidences with the 954 keV. However, no clear indication for a \(\gamma\) cascade was found with \(\gamma\)-ray energies below 2.8 MeV. In particular, we looked for a 1376 keV \(\gamma\) transition from the first excited 0\(^{+}\) to the first excited 2\(^{+}\) state. However, neither the \(\gamma\)-\(\gamma\) coincidence data with the 954 keV line nor a direct analysis of the singles spectrum at 1376 keV yielded any evidence for such a line. From the direct search, we established an upper limit of 0.039 % (95 % confidence level) for the branching ratio for this transition by fitting the germanium spectra with a Gaussian plus a linear background term.
Table 3: Experimental results of half-life measurements for $^{62}$Ga. The error-weighted average value of all measurements is presented in the last column.

|               | Alburger [6] | Chiba et al. [7] | Davids et al. [8] | Hyman et al. [9] | Blank et al. [10] | Present work | Average   |
|---------------|--------------|------------------|-------------------|------------------|-------------------|--------------|-----------|
| Half-life (ms)| 115.95(30)  | 116.4(15)        | 116.34(35)        | 115.84(25)       | 116.19(4)        | 116.09(17)  | 116.175(38) |

Figure 5: Gamma-energy spectrum from the germanium detector array. The 954 keV line corresponding to the de-excitation of the first excited $2^+$ state to the ground state in $^{62}$Zn is indicated.

Based on his results for the branching ratios in conjunction with shell-model calculations, Hyman et al. [9] determined a branching ratio of 99.8(1) % for the super-allowed $\beta$ decay from the ground state of $^{62}$Ga to the ground state of $^{62}$Zn, a result which is not altered by our new results.

Similar agreement is obtained for the upper limit for the feeding of the excited $0^+$ state at 2.33 MeV fed by a forbidden Fermi transition. Our limit of 0.039 % (95% confidence limit) compares well with a limit of 0.017% [5] and 0.043% [9] (one-sigma limits) obtained earlier. In a two-level mixing model, this upper limit can be compared to the part of the isospin correction $\delta_c$ which is due to level mixing [10]. From our new limit of 0.039%, we calculate an upper limit of the mixing matrix element of $\delta_{IM} = 0.21$ which can be compared to theoretical results from Ormand and Brown of $\delta_{IM} = 0.169$ and 0.079 [11] using two different $fp$ shell interactions and from Towner and Hardy of $\delta_{IM} = 0.085(20)$ [3]. Our upper limit is still in agreement with these predictions, which means that more precise experimental data for the feeding of the $0^+_2$ state in $^{62}$Zn are needed to distinguish between the different model predictions.

Figure 6 presents a partial decay scheme for $^{62}$Ga which summarizes the different branching ratios, the half-life, and the $\beta$-decay Q value. These values will be used to determine the $ft$ value for the super-allowed $\beta$ decay of $^{62}$Ga.

The experimental results now available for the $\beta$ decay of $^{62}$Ga, i.e. the Q value of 9171(26) keV [8], the half-life of 116.175(38) ms, and the branching ratio of 99.8(1)% yield a $ft$ value of $ft=3056(47)$ s. Finally, by taking into account the correction factors as calculated by Towner and Hardy [3], we derive a corrected $Ft$ value of $Ft=3057(47)$ s. This value is basically the same as the one for $ft$, as the correction factors nearly compensate each other.

This result agrees well with the average $Ft$ value, 3072.2(8) s, obtained from the nine well-known super-allowed decays of nuclei with 10\textless$A$\textless54. However, the poor precision on $Q_{EC}$ and to some extent on the branching ratio severely limits the precision one can achieve for the moment on the $Ft$ value for $^{62}$Ga. Mass measurement campaigns on $^{62}$Ga and $^{62}$Zn are planned or have recently started at ISOLTRAP at CERN and at the new JYFL-trap in Jyväskylä to reach a precision for both systems of the order of $10^{-8}$. More experiments on the precise measurement of the branching ratios are planned for the near future. Therefore, a high-precision $Ft$ value can be expected in the near future for $^{62}$Ga. These results together with results recently published for $^{74}$Rb [18] will allow us to test the
Table 4: Experimental results of branching-ratio measurements for the decay of the first excited $2^+$ in $^{62}$Ga to the ground state. The error-weighted average value of all measurements of 0.112(11)% is presented in the last column.

|                | Blank [5] | Hyman et al. [9] | Döring et al. [15] | Present work | Average       |
|----------------|-----------|------------------|--------------------|--------------|---------------|
|                | 0.12(3) % | 0.120(21) %      | 0.106(17) %        | 0.11(4) %    | 0.112(11) %   |

Figure 7: $\beta$ decay scheme of $^{62}$Ga indicating the $Q$ value, the half-life as well as the branching ratios.

CVC hypothesis through $\beta$ decay of higher-Z nuclei, to verify the isospin correction terms more carefully, and to yield a better understanding of the weak-interaction standard model.

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