Sliding Friction at a Rubber/Brush Interface

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We study the friction of a poly(dimethylsiloxane) (PDMS) rubber network sliding, at low velocity, on a substrate on which PDMS chains are end-tethered. We thus clearly evidence the contribution to friction of the pull-out mechanism of chain-ends that penetrate into the network. This interfacial dissipative process is systematically investigated by probing the velocity dependence of the friction force and its variations with the grafting density and molecular weight of the tethered chains. This allows us to confirm semi-quantitatively the picture of arm retraction relaxation of the grafted chains proposed in models of slippage at a network/brush interface.

I. INTRODUCTION

The mechanical properties of an interface between polymers strongly depend on the ability to form entanglements by interdiffusion of chains between the bodies in contact. Extraction of these bridging chains then plays a major role in energy dissipation during the rupture of the interface. This pull-out mechanism, which is relevant in adhesion, seems to be also most important in friction. Indeed, different experimental studies of the shear properties of “model” interfaces, formed between an entangled or crosslinked sample and a solid surface on which chains are attached or adsorbed, have shown that friction is influenced by the presence of connecting macromolecules at the interface. This is for instance the case in problems of slippage of polymer melts flowing along a substrate.

Durlat et al. thus evidenced the role of surface-grafted chains on the transition between high and low interfacial friction when a poly(dimethylsiloxane) (PDMS) melt flows on a brush or pseudo-brush of the same polymer. Léger et al. also showed that for melts of Styrene-Butadiene Rubber (SBR), the entanglement-disentanglement mechanism between bulk and surface macromolecules could give rise to a “stick-slip” behaviour.

In these examples, the overall response of the system is the combined result of both the surface chains dynamics and the bulk chains reptation. In order to probe the effect of grafted molecules in the simpler case where the bulk is a permanent network, other authors investigated the velocity-dependent frictional response of an elastomer sliding on a brush: Brown first pointed out that tethered chains could either enhance or lower the friction, depending on their areal density. Casoli et al. further studied the behaviour of such rubber/brush interfaces at high sliding velocities and showed that the presence of the surface-anchored chains could lead to strong departure from the expected linear relation between friction force and velocity.

A central question for understanding these polymer friction problems is that of the dynamics of penetration of an end-tethered chain into a network. This has been the subject of theoretical and numerical works in the case of a static interface, which show that after an initial stage of rapid penetration — on time scales on the order of the Rouse time $\tau_R$ of the chain — the dynamics is controlled by arm retraction of the grafted chain, which results in slow relaxations (logarithmic in time). This arm retraction mechanism is also expected to control friction when a highly entangled polymer melt slips on a grafted surface. Different regimes for the velocity dependence of the friction force are thus predicted, depending on the respective values of the advection time, $D_e/V$ (where $D_e$ is the mesh size of the network formed by the melt), and the relaxation time $\tau_{arm}$ of all or part of the grafted chain.

Though a rather good agreement has been obtained between experimental results on melts flows and the above theoretical predictions for the threshold velocities between the different regimes, there is up to now no quantitative test of the model concerning the velocity dependence of the friction force. Indeed, the picture given in the model for frictional dissipation by pull-out — though such a mechanism must actually take place at the interface — cannot be validated from the existing experimental data, since no systematic investigation of the friction force has been done on systems where the molecular control parameters are varied.

In this paper, we present an experimental study of friction of a rubber network sliding on a brush, at low slip velocities such that the grafted chains are able to penetrate in the elastomer. We first briefly describe the experimental techniques used for samples preparation and for friction force measurements. The different results obtained, which depend on grafting density and molecular weight of the tethered chains, are then presented and discussed in the framework of the existing friction model cited above.

II. EXPERIMENTS

Our experiments involve the contact between a lens of poly(dimethylsiloxane) (PDMS) elastomer and a “bimodal” brush — i.e. made of chains of two different length — grafted on a flat substrate (figure 1).
obtain brushes of short chains which can be pictured as a network.

short chains and long connectors which can penetrate into the is in contact with a bimodal brush made of densely grafted short chains and long connectors which can penetrate into the network.

A. Samples preparation

Elastomers are obtained using the following method: chains of α,ω-vinyl-terminated PDMS (fractionated in the laboratory from commercial oils (Rhodia)) are crosslinked by hydrosilation of the vinyl ends with the Si-H groups of a tetrafunctional crosslinker, in the presence of a Pt complex catalyst. The ratio of hydride to vinyl functions is adjusted in order to optimize the connectivity of the network, and the crosslinking is made under dry nitrogen. Flat/convex lenses of elastomer are obtained by putting droplets of the unreacted melt/crosslinker mixture on a non-wetting surface. After reaction at 110°C for 12h, the networks formed are washed for ten days in a solution of toluene containing a dodecanethiol, in order to extract the unreacted chains and to inhibit the cataly
ist. We thus prepared two series of PDMS elastomers made from chains of molecular weight \( M_w = 9 \) or 23 kg.mol\(^{-1} \) (i.e. roughly once and twice the critical weight for entanglements), of respective polydispersity \( I = 1.14 \) and 1.17.

The bimodal brushes are prepared as follows: a short (4 siloxane monomers) SiH-terminated monochlorosilane is first grafted on the silica layer of a silicon wafer. A melt of PDMS containing a mixture of short (\( M_w = 5 \) kg.mol\(^{-1} \), \( I = 1.16 \)) and long (\( M_w = 114 \), 89, 58, 35 or 27 kg.mol\(^{-1} \), resp. \( I = 1.25 \), 1.28, 1.60, 1.33, 1.11) chains is then spread on this H-terminated sublayer. The chains in the melt are all α-vinyl,ω-methyl-terminated, and grafting occurs by hydrosilation of the vinyl ends at 110°C for 12h. After rinsing by sonication in a solution of toluene and thiol, we measure by ellipsometry the dry thickness \( h \) of the grafted layers, and deduce from this the chains areal density \( \Sigma \), which reads \( \Sigma = h/(Za^2) \), where \( Z \) is the polymerization index of the grafted chains and \( a \approx 0.5 \) nm the size of a monomer.

(i) Grafting from a melt of short 5 kg.mol\(^{-1} \) chains leads to a dry thickness \( h_{short} = 3.6 \pm 0.3 \) nm, i.e. \( \Sigma_{short} = 0.41 \pm 0.03 \) nm\(^{-2} \). This thickness is comparable to the size of the unperturbed chains \( R_0 \approx a\sqrt{Z} \approx 4 \) nm, and corresponds to a density \( \Sigma_{short} \gg 1/R_0^2 \). We thus obtain brushes of short chains which can be pictured as a dense layer of overlapping gaussian coils. The role of this layer is to prevent direct contact between the elastomer and the silane sublayer or the silica surface.

(ii) Choosing the weight ratio of short to long chains in the grafting mixture then allows to obtain bimodal brushes of a given density of long chains\( \Sigma = (h − h_{short})/(Za^2) \), which can be adjusted between 0 and 0.08 nm\(^{-2} \) for the different molecular weights used here (the total thickness \( h \) ranges from \( h_{short} \) to \( h \approx 15 \) nm for the highest \( M_w \)). In the following, \( \Sigma \) always refers to the areal density of the long “connectors”, with \( \Sigma > 1/R_0^2 \) except for the two lowest densities which are in the “mushroom” regime of non overlapping chains.

We systematically prepare brushes of various \( \Sigma \), along with a reference brush with \( \Sigma = 0 \), from the same wafer, i.e. from the same H-terminated silane layer.

B. Force measurement setup

Friction measurements are performed on a setup designed for this study (figure 2): a lens of elastomer, maintained by a horizontal glass plate, is brought in contact with a brush-bearing substrate. This substrate is fixed at the free end of a double cantilever spring (stiffness 400 N.m\(^{-1} \)), the second end of which is driven at constant velocity 3 nm.s\(^{-1} \), \( < V < 330 \) nm.s\(^{-1} \). A capacitive displacement gauge measures the spring bending, which allows us to access the friction force \( F \) in the range 50 μN–50 mN. The contact area \( S \) between the lens and the flat is monitored optically. The normal force is not measured in this experiment but the sphere/flat indentation depth is fixed instead, which amounts to work at given contact diameter, in the range 200–400 μm.
III. RESULTS

Typical results obtained in steady sliding are presented in figure 3, where the mean friction stress $\sigma = F/S$ is plotted against sliding velocity for various grafting densities of connectors. We have checked that $\sigma$ does not depend on the contact size $S$ in the experimentally accessible range.

![Figure 3](image-url)  
**FIG. 3:** Friction stress $\sigma$ vs sliding velocity $V$ (both scales are logarithmic), for connectors of $M_w = 114$ kg.mol$^{-1}$ and elastomer of $M_w = 23$ kg.mol$^{-1}$. ($\bullet$): $\Sigma = 0$; ($\circ$): $\Sigma = 0.0016$ nm$^{-2}$; ($\triangle$): $\Sigma = 0.021$ nm$^{-2}$. The solid line is a fit of the $\Sigma = 0$ data with $\sigma = \sigma_0 + kV$, $\sigma_0 = 1.8$ kPa, $k = 10^8$ Pa.s.m$^{-1}$. Stick-slip is systematically observed at low velocities.

(A) Friction on short chains brushes

At $\Sigma = 0$, i.e. when sliding on the dense brush of short chains only, the stress increases linearly with velocity after a low-velocity plateau. As seen in figure 3, the data are well fitted by $\sigma = \sigma_0 + kV$. The plateau value $\sigma_0$ can vary from 2 to 10 MPa from sample to sample, but the coefficient $k$ takes a constant value $k = 10^8$ Pa.s.m$^{-1}$.

The steady sliding regime does not span the whole range of velocities: at $V$ lower than a critical value $V_c$, we observe stick-slip oscillations, i.e. unstable sliding, down to the lowest accessible velocity. The bifurcation from stable to unstable sliding is continuous, without hysteresis: the force signal smoothly goes from small sine-shaped oscillations at $V \sim V_c$ to large amplitude triangular oscillations at $V \ll V_c$. The critical velocity $V_c$ can vary from 0.1 to 3 $\mu$m.s$^{-1}$ from sample to sample.

The scattering on $V_c$ and $\sigma_0$ mentioned above will be discussed in section IV.

(B) Role of connectors

Adding long connectors, whatever their molecular weight, to the short chains brushes has different effects:

(i) The friction stress depends non-linearly on velocity, and tends to grow as a weak power law of $V$ at high $\Sigma$ (figure 3).

(ii) The stress in steady-sliding increases quasi-linearly with the grafting density (see figures 3 and 4), up to a crossover value of the density $\Sigma_0 \approx 0.02-0.03$ nm$^{-2}$, above which $\sigma$ reaches a plateau, as can be seen in figure 4. The slope of the quasi-linear part of $\sigma(\Sigma)$ slightly depends on the velocity at which the stress is measured, and increases, typically, by a factor of 3 or 4 when $V$ varies over 3 decades.

![Figure 4](image-url)  
**FIG. 4:** Friction stress $\sigma$ vs grafting density $\Sigma$ for connectors of $M_w = 114$ kg.mol$^{-1}$ and elastomer of $M_w = 23$ kg.mol$^{-1}$, at $V = 0.3$ $\mu$m.s$^{-1}$ ($\bullet$), $V = 10$ $\mu$m.s$^{-1}$ ($\circ$), $V = 100$ $\mu$m.s$^{-1}$ ($\triangle$).

(iii) The critical velocity $V_c$ decreases with the grafting density of connectors, as illustrated in figure 5.

![Figure 5](image-url)  
**FIG. 5:** Critical velocity $V_c$ (normalized by its value at $\Sigma = 0$) as a function of grafting density, for $M_w = 27$ kg.mol$^{-1}$ ($\circ$); $M_w = 58$ kg.mol$^{-1}$ ($\bullet$); $M_w = 114$ kg.mol$^{-1}$ ($\triangle$).

(C) Molecular weight effects

We observe the following when varying the molecular weight of the connectors:
(i) At a given areal density $\Sigma < \Sigma_0$ (i.e. in the linear regime of $\sigma(\Sigma)$), the sliding stress $\sigma$ increases with the molecular weight of the long chains, as illustrated in figure 6.

(ii) At high grafting density, the $\sigma(V)$ power law exponent grows from 0.2 to 0.5 as $M_w$ decreases from 114 to 27 kg.mol$^{-1}$.

(iii) The critical velocity $V_c$ is lower for longer connectors (figure 1).

Finally, we do not notice any effect of the molecular weight between crosslink points of the elastomer. All the features described above are quantitatively identical for $M_w = 9$ or 23 kg.mol$^{-1}$.

IV. DISCUSSION

A. Origin of the stick-slip instability

We first want to come back on the possible mechanism responsible for the stick-slip observed at low velocities. An entanglement/disentanglement process between the grafted chains and the network cannot be invoked here, since unstable sliding is also observed on short chains brushes which are more likely unreacted sites from the H-terminated silane sublayer used for hydrosilation. These sites, may transform in silanol groups under ambient humidity, and become adsorption sites for the PDMS chains. This leads us to propose the following picture. Once the contact is made between the elastomer and the grafted layer, the short chains brush swells, which allows the elastomer chains to access the underlying adsorption sites. When sliding, the frictional response then depends on both the elastomer/brush and the elastomer/defects interactions:

At high velocities, the elastomer chains do not have time to adsorb on defects and friction is governed by the PDMS/PDMS interactions only, which results in similar $\sigma(V)$ curves whatever $\Sigma_{short}$.

At low velocities, an adsorption/desorption mechanism under shear can occur between the network and the pinning sites (the defects), akin to that proposed by Schallamach for rubber friction. This leads to:

(i) a higher sliding stress and critical velocity $V_c$ when $\Sigma_{short}$ is lower, i.e. when the pinning sites are more numerous,

(ii) a friction stress which decreases with velocity, which is the source of the mechanical instability observed.

The low velocity plateau $\sigma_0$, attributable to this pinning mechanism, would then appear as a minimum at the crossover between the velocity decreasing and increasing regimes.

This qualitative picture is consistent with the fact that the critical velocity $V_c$ is lowered in the presence of connectors (figure 5), since slow penetration of the long chains in the network is needed before accessing the pinning sites on the substrate.

![Figure 6: Friction stress $\sigma$ vs sliding velocity $V$, for $\Sigma = 0$ (▲) and for $\Sigma \approx 0.01$ nm$^{-2}$ of different connectors.(•): $M_w = 27$ kg.mol$^{-1}$; (●): $M_w = 35$ kg.mol$^{-1}$; (♦): $M_w = 114$ kg.mol$^{-1}$.](image)

![Figure 7: Sliding stress as a function of velocity. (▲): short chains brush $\Sigma_{short} = 0.37$ nm$^{-2}$; (●): short chains brush $\Sigma_{short} = 0.43$ nm$^{-2}$; (●): $\Sigma = 0.05$ nm$^{-2}$ of $M_w = 114$ kg.mol$^{-1}$ connectors and low density sublayer; (♦): $\Sigma = 0.05$ nm$^{-2}$ of $M_w = 114$ kg.mol$^{-1}$ connectors and high density sublayer](image)
B. Friction induced by grafted chains

We now concentrate on the results obtained in steady sliding.

When the elastomer slides on a dense brush of short chains, the friction stress obeys a relation of the form $\sigma = \sigma_0 + kV$, with $k = 10^8$ Pa.s.m$^{-1}$ (figure 3). At this type of interface, since the brush is dense and no entanglement can be formed, we expect the frictional response to be close to that of an interface between two surfaces of densely packed monomers: $\sigma_{mono} = \zeta_1 V/a^2$, where $\zeta_1$ is the monomeric friction coefficient and $a$ the monomer size. From the value of $k$ above, using $a = 0.5$ nm, we obtain $\zeta_1 = ka^2 = 2.5 \times 10^{-11}$ N.s.m$^{-1}$. This value is fully consistent with $\zeta_1 \simeq 10^{-11}$ N.s.m$^{-1}$ deduced from self-diffusion$^{20}$ or viscoelastic measurements$^{21}$. Partial penetration and chain stretching effects might account for the fact that the value deduced from our experiments is slightly larger than the previously reported ones.

The presence of long grafted chains at the interface leads to a friction stress which is systematically higher than on the short chains brush and which depends non-linearly on sliding velocity. This result is due to penetration of these chains inside the network and to their subsequent pull-out. Indeed, the characteristic time scale of our experiments, given by $D_e/V$ (where $D_e \sim a\sqrt{N_c} \simeq 5$ nm is the mesh size of the elastomer, $N_c \simeq 100$ being the number of monomers between entanglements$^{20}$), ranges from $10^{-2}$ to $10^{-5}$ s for velocities between 0.3 and 300 $\mu$m.s$^{-1}$. This is much larger than the Rouse time between entanglements for PDMS ($\tau_R = \tau_1 N_c^2 \simeq 3 \times 10^{-7}$ s, with $\tau_1 = 3 \times 10^{-11}$ s), and also larger than the longest Rouse time of the grafted chains used ($\tau_R = 7 \times 10^{-5}$ s for $M_w = 114$ kg.mol$^{-1}$). We are thus in a situation where the grafted chains can always relax inside the network, i.e. the first, rapid penetration step predicted by O’Connor et al$^{22}$ or Deutsch et al$^{23}$ can always occur at the interface. During shear, this penetrated part will then allow to stretch the portion of chain confined outside the network, and thus contribute to the friction force until being pulled out.

We have shown that, at a given velocity, the friction stress increases with the grafting density of tethered chains before reaching a plateau. This result is in full agreement with what Casoli et al. observed for friction on a similar PDMS rubber/brush system$^{24}$, it is also consistent with the density dependence of the adhesion energy at such interfaces, which exhibits a plateau or a maximum at an optimal density$^{26}$. The first increase of $\sigma$ with $\Sigma$ confirms the picture of friction enhancement by chain penetration/pull-out. It is important to note that this regime is observed at areal densities essentially larger than the mushroom limit, which means that grafted chains overlap and can entangle outside the elastomer. Hence, though the friction stress increases quasi-linearly with $\Sigma$, we believe that the tethered chains cannot be considered as independent and that their dynamics is influenced by interactions between neighbours, as stated by Casoli et al$^{24}$ or as observed in the simulations of Deutsch et al$^{23}$. The friction stress plateau is attributable to the swelling limit of the elastomer, as discussed in previous studies on that type of interface$^{25}$: the number of monomers that can penetrate into the network region close to the interface is limited by the network elasticity$^{26}$.

Our results seem to contrast with those obtained by Brown$^{20}$ in the first study of friction at such rubber/brush interfaces. Indeed, he concluded that grafted chains had mostly a lubricating effect. This difference is certainly due to the substrates used in the studies: Brown grafted PDMS chains in a polystyrene layer, whereas we used bi-modal brushes. We have checked in a control experiment that the friction stress when sliding on a thin layer of PS is at least one order of magnitude larger than when sliding on a short chains brush of PDMS. Brown’s results then come from a progressive screening of the PS substrate while the thickness of the PDMS layer increases. Both works are thus not in contradiction but cannot be compared directly.

Eventually, the non-linearities induced by grafted chains may have different origins:

(i) The force needed to pull the chains out of the network may depend non-linearly on velocity.

(ii) The stress due to network deformations in the vicinity of the interface might be non-linear.

(iii) The response of the thin layer formed by the portions of chains confined outside the network may be shear-thinning, which is suggested by the power law dependence of $\sigma$ on $V$ at high grafting densities.

The relative weight of these mechanisms is not straightforward to estimate, all the more than most of our data have been obtained in a range of grafting density where interactions between tethered chains can certainly not be disregarded, which renders data analysis more complex.

We believe nonetheless that the third mechanism, i.e. the rheology of a thin entangled layer, dominates at high $\Sigma$: if we estimate, for instance, that a layer of long chains ($M_w = 114$ kg.mol$^{-1}$) of thickness $h \simeq 10$ nm is sheared at a rate $\dot{\gamma} = V/h$, we find that $\dot{\gamma}$ is in the range $1-10^4$ s$^{-1}$ for $0.01 \mu$m.s$^{-1} < V < 100 \mu$m.s$^{-1}$. Over this range the stress $\sigma \sim V^{0.2}$, which is consistent with the shear-thinning behaviour observed both in bulk rheology of polymer melts$^{25,26}$ (at shear rates $\dot{\gamma} > \dot{\gamma}_c \sim 1/\tau_{rep}$, where $\tau_{rep}$ is the reptation time of the chains) and in a recent study of the shear response of PDMS melts highly confined between rigid walls$^{27}$. Now, if we evaluate an effective viscosity $\etaeff = \sigma h/V$ from our data, we find that $\etaeff$ decreases from $10^4$ to 10 Pa.s when $\dot{\gamma}$ increases from 1 to $10^4$ s$^{-1}$, with $\etaeff \sim \dot{\gamma}^{-0.8}$. For comparison, we expect, for a melt of chains with $M_w = 114$ kg.mol$^{-1}$, the bulk viscosity to decrease from its newtonian plateau $\eta_{bulk} \simeq 10$ Pa.s above $\dot{\gamma} > 1/\tau_{rep} \simeq 10^3$ s$^{-1}$. We thus clearly see that $\etaeff \gg \eta_{bulk}$, which is consistent with the fact that in our experimental situation...
where chains are end-tethered, the characteristic relaxation time should rather be on the order of the time for arm retraction \(^{11,12,13,24}\) (see next section), which is much larger than the reptation time governing the bulk rheology of melts. Both the strong increase of \(\eta_{eff} \gg \eta_{bulk}\) and its power law dependence are in good agreement with what has been observed in shear response of confined melts\(^{27}\). This suggests that the frictional response at high grafting densities is controlled by the rheology of a thin layer of chains outside the elastomer, the behaviour of which is strongly influenced by confinement and tethering effects.

On the opposite, we can now focus on the results obtained on the brushes with the lowest \(\Sigma\), in the mushroom regime, where the third mechanism should not be relevant. We perform a detailed analysis of these results in the next section.

### C. Molecular weight and chain pull-out effects

One of the last points we want to discuss is the role of molecular weights (of the grafted chains or of the elastomer) on friction.

Let us first recall that no difference was noted between the frictional response of elastomers made from chains of \(M_w = 9\) or 23 kg.mol\(^{-1}\), i.e. containing \(N = 120\) or 310 monomers. This means that on the time scale of the network solicitation, the entanglements which might be trapped in the chemical network do not have time to relax, and that the effective mesh size of the elastomer is not fixed by the total number of monomers between crosslinks but rather by the number of monomers between entanglements \(N_e \simeq 100\). In the following, we will thus consider that the mesh size of the network is \(D_e \sim a\sqrt{N_e} \simeq 5\) nm.

The role of grafted chains length can be understood qualitatively as follows: the longer the chains, the more entanglements they form with the network, the higher the friction stress. This picture might however be too naive since the penetration dynamics of the chains may be faster for shorter chains, which would oppose the simple entanglement effect mentioned before.

This last point deserves a more refined approach. We will now analyse the low grafting densities results on the basis of the model originally proposed by Rubinstein et al.\(^\text{22,13}\), in an attempt to understand more precisely the molecular weight and the chain pull-out effects.

We briefly recall the main features of this friction model. The authors consider the situation of an elastomer sliding at a given velocity on a weakly grafted smooth surface, the sliding stress then being \(\sigma(V) = \sigma_{bare}(V) + \Sigma F_c(V)\), where \(\sigma_{bare}\) is the contribution of the bare surface and \(F_c\) the force on one grafted chain. The tethered chains are supposed to be independent. To determine \(F_c\), the assumption is made that this friction situation is analogous to that where a single chain is pulled by its head, at constant \(V\), through a network of fixed obstacles. In this latter situation, the only possible relaxation mode of the chain is arm retraction. The relaxation time of the whole chain of \(Z\) monomers is that of a thermally activated process, given by \(^{11,12,13,24}\)

\[
\tau_{arm}(Z) = \tau_1 Z^2 \exp\left(\mu Z/N_e\right)
\]

where \(\mu\) is a constant of order 2 and \(\tau_1\) is a microscopic time. As long as the advection time, \(D_e/V\), is larger than \(\tau_{arm}(Z)\), i.e. as long as \(V < V_1 = D_e/\tau_{arm}(Z)\), the whole chain can relax in the network and the force on its head reads

\[
F_c = F_e \frac{V}{V_1}
\]

where \(F_e = kT/D_e\) (\(k\) is the Boltzmann constant and \(T\) the temperature).

For velocities \(V > V_1\), the head of the chain is stretched in straight tube of diameter \(D_e\) whereas only a tail of \(q\) monomers has time to relax and adopt a “ball” shape, the relaxation time of the relaxed tail being

\[
\tau_{arm}(q) = \tau_1 Z^2 \exp\left[\mu q^2/(ZN_e)\right]
\]

In this regime, the force is the sum of two terms:

\[
F_c = kT/D_e + [Z - q(V)]\zeta_1 V
\]

where the first term of the right-hand-side is the force on the relaxed part of the chain and the second one is the contribution, by Rouse friction, of the stretched part. \(\zeta_1\) is a monomeric friction coefficient. The number \(q(V)\) is determined by \(V\tau_{arm}(q) = D_e\).

As the velocity is increased, the ball shrinks and the stretched part grows, until \(q \approx \sqrt{ZN_e}\), i.e. until \(V \approx V_2 = D_e/\tau_1 Z^2\). Above this threshold, the entropic barrier for arm retraction vanishes, and the size of the ball is then controlled by the tube length fluctuations of a chain subunit of \(q\) monomers, with relaxation time

\[
\tau_R(q) = q^2\tau_1/N_e^2
\]

The number \(q\) is thus determined by \(\tau_R(q) = D_e/V\) and the force is always given by expression\(^3\).

The contributions to friction of the ball and of the stretched part become comparable at \(V \approx V_3\) = \(V_2/(Z/N_e)\), and for \(V \gg V_3\) the friction force is \(F_c \simeq Z\zeta_1 V\).

Let us estimate the values of these different velocity thresholds for the parameters of our PDMS systems. We take \(\zeta_1 \approx 1.5 \times 10^{-11}\) N.s.m\(^{-1}\) (deduced from self-diffusion measurements\(^\text{20}\)), \(\tau_1 = \zeta_1 a^2/(3\pi^2 kT) \approx 3 \times 10^{-11}\) s, \(Z = 1540\) for the longest connectors and \(Z = 365\) for the shortest ones. \(V_1\) varies from \(10^{-11}\) \(\mu m.s^{-1}\) for \(Z = 1540\) to about \(1\) \(\mu m.s^{-1}\) for \(Z = 365\), \(V_2\) increases from 10 to 200 \(\mu m.s^{-1}\), and \(V_3\) from 200 to 700 \(\mu m.s^{-1}\). We can thus consider, for all practical purposes and in view of the uncertainty on the values of the microscopic parameters, that the first low-velocity regime
is never reached experimentally in steady-sliding. The range of velocity covered in our study should correspond to a friction force mainly governed by expression 4 with \( q \) controlled by \( \tau_{\text{arm}} \) or \( \tau_R \) depending on chain length. The friction force per grafted chain should then increase slowly, starting from \( F_c = kT/D_c \simeq 8 \times 10^{-13} \text{ N} \), as velocity is increased.

In order to compare our results with the model predictions, we now have to extract from the data the friction force per grafted chain. We do so by assuming that, at low grafting densities in the mushroom regime, all contributions are additive. We consider that the total friction stress measured is \( \sigma(V) = \sigma_{\text{short}}(V) + \Sigma F_c(V) \), where \( \sigma_{\text{short}}(V) \) is the friction stress measured without long connectors, and deduce \( F_c \) from this. The friction force per connector thus evaluated is reported in figure 8, as a function of sliding velocity, for four different molecular weights and two grafting densities per molecular weight.

It can be seen in figure 8 that \( F_c \), as expected, do not depend on \( \Sigma \), and that the friction force decreases for shorter the connectors (see also figure 9b). In particular, the value of \( F_c \) at \( V = 0.3 \mu \text{m.s}^{-1} \) is found to decrease from \( 10^{-12} \) to \( 10^{-13} \text{ N} \) as \( M_w \) goes from 114 to 27 kg.mol\(^{-1} \). Now, if we scale the experimental curves \( F_c(V) \) by the low-velocity value of \( F_c \), it appears that whatever the molecular weight of the connectors, the force per chain has the same velocity dependence (figure 8b): it increases with \( V \), by a factor of 3 or 4 over three decades of velocity, and may eventually fall at the highest velocity. Note here that this relative increase with \( V \) is consistent with the slope variation of the linear part of \( \sigma(\Sigma) \) reported in section III.

Three main features of these experimental results are in good semi-quantitative agreement with the theoretical predictions, bearing in mind that the model is totally free of fitting parameters (we used for the microscopic parameters \( \tau_1 \) and \( \zeta_1 \) values determined by independent techniques):

(i) the order of magnitude of the low-velocity values of the force per chain is consistent with \( F_c = kT/D_c \simeq 8 \times 10^{-13} \text{ N} \),

(ii) \( F_c \) increases weakly with velocity (see figure 8b),

(iii) \( F_c \) increases quasi-linearly with chain length at high velocities (see figure 8b).

From this we can conclude that chain pull-out is certainly the mechanism which governs friction at low grafting density, and that the picture of arm retraction proposed in the model accounts well for the weak velocity dependence observed experimentally.

However, discrepancies exist between experimental and theoretical results:

(i) the model does not account for the observed decrease of \( F_c \) with connectors length at low \( V \),

(ii) no molecular weight dependence is experimentally noted for the relative increase of \( F_c \) with \( V \) (figure 8b), whereas the model predicts a weaker velocity dependence for shorter connectors (figure 8b).

We believe that these discrepancies have the following origin. In the model, the assumption is made that the chain is pulled through but stays in the network, which is not the case experimentally since tethered chains are really extracted from the elastomer. As discussed by Brown, this difference might have an impact on the absolute value of \( F_c \) since the extracted part of a connector, outside the network, is probably less confined than assumed theoretically. Moreover, the two lowest molecular weights of connectors used in our study are such that \( Z/N_c \) is close to one, and are thus weakly entangled with the elastomer, which may correspond to a situation at the limit of validity of the model and make quantitative comparison difficult. Finally, at high velocity, we estimate from equation 5 that the number of monomers in the penetrated part is around 150, i.e. very close to \( N_c \). Full disentanglement of the grafted chains at high \( V \) may thus account for the drop of \( F_c \).

V. CONCLUSIONS

We have perform an extensive experimental study of sliding friction at a rubber/brush interface. We have thus been able, by means of a simple friction force measure-
ment on a macroscopic contact, to access detailed information on the molecular mechanisms at play during sliding at such an interface, and we have shown that:

(i) friction is very sensitive to the degree of heterogeneity of the surfaces: the presence of defects in the brushes is evidenced by the appearance of unstable sliding (stick-slip), and variations of 10 to 20% on surface coverage could lead to fivefold variations on the sliding stress or the critical velocity at the instability threshold.

(ii) in steady sliding, the interfacial response is clearly influenced by penetration of the grafted chains into the rubber network. At low grafting density, frictional dissipation is governed by the chain pull-out mechanism, whereas at high grafting density it seems to be dominated by the rheology of the thin entangled layer made of the elongated extracted chains, confined out of the elastomer.

(iii) our experimental data at very low grafting densities and the theoretical predictions by Rubinstein et al.12,13 are in satisfactory agreement as far as friction force level and velocity dependence are concerned. This provides, to our knowledge, the first semi-quantitative evidence that grafted chains relaxation in the network during steady sliding occurs by arm retraction, as previously inferred from stress relaxation experiments on network/brush or brush/brush interfaces.29 Discrepancies observed on molecular weight dependence of the friction force suggest both model refinements and experimental prospects. In particular, data obtained with different mesh sizes of the elastomer (with a polymerization index between crosslink points $N < N_c$) would provide information on the contribution to friction of the elastomer chains, and would allow to work in a less ambiguous regime where the polymerization index of the grafted chain is much larger than that of the network.

FIG. 9: (a) Theoretical predictions for $F_c/F_e$ as a function of velocity. (---): $Z=1540$ monomers; (— —): $Z=1200$; ( ----): $Z=470$; (--- -): $Z=365$. Symbols: experimental data for $F_e/(0.3 \mu m.s^{-1})$ from figure 8a. (b) Force per chain as a function of the polymerization index $Z$ of the grafted chains. Symbols: experimental data at $V = 1 \mu m.s^{-1}$. (○); $V = 60 \mu m.s^{-1}$ (●); $V = 200 \mu m.s^{-1}$ (■). Theoretical predictions at $V = 1 \mu m.s^{-1}$ ( - - ); $V = 60 \mu m.s^{-1}$ ( --- ); $V = 200 \mu m.s^{-1}$ ( — ).

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17 More precisely, for brushes made from the same wafer, if the reference brush ($\Sigma = 0$) has a low $\Sigma_{short}$, all the results
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