New Approach to Estimate Extreme Flooding Using Continuous Synthetic Simulation Supported by Regional Precipitation and Non-Systematic Flood Data

Carles Beneyto 1,*, José Ángel Aranda 1, Gerardo Benito 2 and Félix Francés 1

1 Research Institute of Water and Environmental Engineering, Universitat Politècnica de València, 46022 Valencia, Spain; jaranda@upv.es (J.A.A.); ffrances@upv.es (F.F.)
2 Department of Geology, National Museum of Natural Sciences (CSIC-Universidad Complutense de Madrid), 28006 Madrid, Spain; benito@mncn.csic.es

* Correspondence: carbeib@alumni.upv.es; Tel.: +34-963-877-000 (ext. 76152)

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Abstract: Stochastic weather generators combined with hydrological models have been proposed for continuous synthetic simulation to estimate return periods of extreme floods. Yet, this approach relies upon the length and spatial distribution of the precipitation input data series, which often are scarce, especially in arid and semiarid regions. In this work, we present a new approach for the estimation of extreme floods based on the continuous synthetic simulation method supported with inputs of (a) a regional study of extreme precipitation to improve the calibration of the weather generator (GWEX), and (b) non-systematic flood information (i.e., historical information and/or palaeoflood records) for the validation of the generated discharges with a fully distributed hydrological model (TETIS). The results showed that this complementary information of extremes allowed for a more accurate implementation of both the weather generator and the hydrological model. This, in turn, improved the flood quantile estimates, especially for those associated with return periods higher than 50 years but also for higher quantiles (up to approximately 500 years). Therefore, it has been proved that continuous synthetic simulation studies focused on the estimation of extreme floods should incorporate a generalized representation of regional extreme rainfall and/or non-systematic flood data, particularly in regions with scarce hydrometeorological records.

Keywords: weather generator; palaeoflood; regional extreme precipitation study; ephemeral river; fully distributed hydrology; flood quantiles; Rambla de la Viuda

1. Introduction

Accurate estimates of extreme and rare floods have been a fundamental problem in flood hydrology since pioneer work by Foster [1], and it is still present among the scientific and engineering communities in numerous papers and reports. Stedinger and Griffis [2] evaluate critical issues on flood frequency methods, recommending practical developments, among others, on: (i) extending flood records with historical and non-standard flood data (e.g., palaeofloods), which can be called non-systematic information [3]; (ii) generation of flood data from rainfall records using conceptually based and spatially fully distributed watershed models; and (iii) advances in setting realistic physical limits on precipitation and flows in a given catchment. These research topics seek to gain knowledge about the tail of the frequency distribution describing the extremes, particularly in data-poor regions, either by using regional flood methods [4], extending the flood registers [5], and improving parameter estimates related to the distribution shape with upper bounds (e.g., [6]) or identifying low outliers in flood
data [7]. Traditional flood studies (e.g., for the design of sensitive infrastructures) were based in either flood frequency analysis (FFA) for gauged basins or deterministic procedures, mainly based on the design storm, for ungauged basins. This latter approach draws from the premise that return periods of concurrent rainfall and peak discharge are assumed to be the same and that the design flood of a given return period can be estimated based on a single rainfall duration that generates the highest peak discharge (see the classical Chow et al. [8] or the Flood Estimation Handbook [9]). However, we now know that this approach is uncertain since peak discharges and hydrographs are strongly dependent on the spatio-temporal distribution of the precipitation [10] and on the initial conditions of the basin [11]. In recent years, different continuous hydrologic modeling approaches have emerged (see, for example, Grimaldi et al. [12]). An alternative method widely adopted is to combine statistical and deterministic methods in a continuous synthetic simulation (CS). The procedure involves the generation of synthetic discharge data series obtained from a stochastic weather generator (WG) combined with a hydrological model (HM). Many studies can be found in the literature following this approach with different nuances. In an early work, Cameron et al. [13] combined a modified WG developed by Eagleson [14] with the semi-distributed HM TOPMODEL. Other examples include WG synthetic datasets from Neyman–Scott rectangular pulse [15] or spatiotemporal Neyman–Scott processes [16] integrated on semi-distributed or fully distributed hydrological models. A review of different continuous synthetic simulation approaches can be found in Boughton and Droop [17].

Continuous synthetic simulation procedures can generate long series of discharges where flood quantiles can be easily interpolated from the empirical plotting positions rather than having to parameterize the discharges data series as in the traditional flood frequency analysis. Nevertheless, WGs require representative data series of observed extreme precipitation in order to perform adequately [18]. In most of the cases, there may not be sufficient extreme rainfall records, meaning that results from stochastic WG may not generate reliable extreme floods [19,20]. This problem has been addressed by several authors who have proposed different alternatives to improve the WG performance. For example, Furrer and Katz [21] distinguished the type of precipitation by fitting low to moderate intensities to a gamma distribution and high intensities to generalized Pareto distribution. Evin et al. [22] proposed the use of a heavy-tailed distribution function (E-GPD) and the integration of information from more extensive regional studies for the parametrization of the WG.

In the context of Mediterranean ephemeral rivers, WG and FFA implementation involve a number of practical problems, mostly related to frequent zero or very small flows for the entire year, a large variability of flood peak discharges, and often short observation records [7]. In arid/semiarid rivers, Metzger et al. [23] applied synthetic flood records to FFA, concluding that streams with a small number of events per year and a large coefficient of variation of the flood peaks produced the largest errors in the estimated quantiles. Regional regression models were used to improve at-site frequency curves [24], but their performance in arid/semiarid environments is not as satisfactory as in humid regions because of the higher degree of hydrological variability. The fact that longer records provide less biased estimates, as indicated by Metzger et al. [23], calls for the inclusion of historical and other non-standard flood data [25,26]. These include historical observations, interval data (estimates of flood peaks within specified ranges of magnitude and time), and palaeoflood records [27]. Palaeoflood data provide physical evidence of flooding over secular time scales and typically consist of fine-texture sediment layers accumulated on valley sides [28] and durable botanical evidence, such as scars produced by impacting floating debris and stones on riparian trees [29]. By providing information beyond the systematic records, it is generally possible to extend the observations beyond the 100-year return period and therefore reduce the estimated quantile uncertainty (e.g., [30–32]).

The main objective of this paper was to develop a methodology for a better estimation of extreme flooding based on a daily multisite WG and a fully distributed HM supported by a regional extreme precipitation study and non-systematic flood information, validating its results in a case study. Although we integrated both sources of additional information in this research, different variants of
this methodology can be applied if only one source of information is available, which will depend on the type of information available.

Under- or overestimation of flood quantiles has always been a problem in flood modeling studies. The main reason behind this is the short length of the available hydrometeorological data series. Most of the former works based in the CS approach do not account for this problem and, although solving the abovementioned issues of the initial conditions of the river basin and the characterization of the spatio-temporal distribution of the precipitation, the estimated higher quantiles still present high uncertainties. This methodology aims to contribute in this sense, obtaining better estimates of the higher flood quantiles and reducing their uncertainty by adding two extra sources of additional information for the implementation of the WG and the validation of the resulting discharges.

2. Case Study and Data Collection

The proposed approach was implemented and evaluated in the catchment of Rambla de la Viuda, a typical Mediterranean ephemeral river located in eastern Spain. The river is ca. 36 km in length and 1513 km² in catchment surface, and it originates at the confluence of River Montlleó and Rambla Carbonera, flowing into River Millars near its mouth in the Mediterranean Sea (Figure 1).

Figure 1. Study area: Rambla de la Viuda catchment.

Their headwaters are located at the Iberian Range Mountains at an elevation of 1750 m above sea level, with a substrate dominated by Jurassic and Cretaceous limestones and marls affected by the Alpine tectonic reactivated during the Neogene [33]. This bedrock lithology favors karstification processes, leading to high infiltration and percolation rates into a deep karst aquifer disconnected from the stream channels. The lower part of the catchment is located in the coastal plain where the Rambla joins the Millars River to find its way to the Mediterranean Sea. This coastal plain consists of alluvial fan deposits (mainly gravels) of Tertiary and Pleistocene age. In the upper catchment, the river channel is embedded in deep and narrow valleys, whereas in the lower part, it develops a wide alluvial channel bed, with a width-to-depth ratio of ~100 times [34].

The observed average annual rainfall is approximately 550 mm. The precipitation annual pattern consist of (i) autumn rains (September to November) recording the highest daily and monthly rainfall amounts; (ii) frontal systems linked to Atlantic zonal flow during winter (December to January) and spring (March to May), with spring giving the secondary monthly rainfall maximum; and (iii) occasional convective storms in summer, which is mostly dry [34,35]. Rambla de la Viuda streamflow patterns are strongly marked by the Mediterranean rainfall regime, high bedrock permeability due to the dominance
of karstified limestones, and high channel transmission losses. As a result, streamflow occurs with an average of 31 days per year, often lasting only 2–3 days and associated with accumulated rainfall amounts larger than 70 mm [34].

Large floods are a significant element of this irregular hydrological regime, producing up to 80% of annual discharge volume [36]. Heavy rainfalls leading to extraordinary and extreme floods are related to autumn mesoscale convective systems (MCSs) [37] fed by Mediterranean moisture and enhanced by orographic effect of the Iberian Range Mountains close to the coast. For example, the rainfall event of October, 1962, recorded ca. 300 mm in 24 h that led to severe flash flooding with a peak flow of 1500 m$^3$s$^{-1}$ at Maria Cristina Dam. This floodwater overflowed the spillway (capacity for 600 m$^3$s$^{-1}$) and spilled over the dam wall with a depth of 0.7 m. Comparable large floods overflowing the dam took place in 1920 (during dam construction), 1962, 1969, and 2000.

Meteorological records were obtained from different sources. The daily max. and min. temperatures as well as the daily precipitation series were obtained from the Spain02-v5 reanalysis dataset [38]. A total of 20 grid points (Figure 2) covering the catchment area with daily records from 1951 to 2015 (66 years). Sub-daily temperature and precipitation records (5-min) for 13 stations were obtained from the Júcar River Basin Authority (CHJ) through the Júcar Automatic Hydrological Information System (SAIH), which started recording sub-daily measurements from 1991.

![Figure 2. Location of hydrometeorological information.](image)

In terms of hydrological data, these were recorded in four points with available daily and 5-min discharge information directly from the CHJ and from the SAIH, respectively, namely two continuous flow gauges (Vall d’Alba and Montlleó) and two stations at dams (Alcora and Maria Cristina) where discharges were estimated from the balance of the reservoir level and the outflow records (Figure 2). The length of the daily discharge series ranged between 57 years at Maria Cristina dam and 14 years at Montlleó flow gauge. With regards to the 5-min records, only three high flow events (i.e., 2000, 2015, and 2018) were registered from 1991. In addition, 5-min discharge records at both Vall d’Alba and Montlleó showed strong inconsistencies and therefore they were only used to validate dry/wet conditions on the river channel.

Further information on extremes was obtained from a regional study of maximum daily precipitation [39] that was used for the additional calibration of the weather generator. In addition, non-systematic flood data were collected from documentary datasets and palaeoflood studies [27,40] in two sites, which were integrated for the validation of the GW-hydrological model methodology.
3. Methodology

The methodology consisted of four steps: (1) application of a weather generator for simulating daily precipitation and temperatures with an additional calibration of the parameters related to the extremes using a regional annual maximum rainfall study to deal with the limited length of precipitation records; (2) implementation at a daily and sub-daily scale of a fully-distributed hydrological model that can cope with the spatial variability of rainfall and catchment characteristics; (3) simulation of daily flows of the synthetic rainfall dataset in the fully distributed rainfall-runoff model; (4) comparison of the performance of flood frequency analysis from observed and synthetic flood series; and (5) incorporation of palaeoflood discharge estimates covering the past 500 years to validate synthetic discharges for high return periods in other ungauged locations but with non-systematic information. A workflow diagram of the methodology can be observed in Figure 3.

![Workflow diagram of the methodology.](image)

In the present study, the eco-hydrological model TETIS [41] was used. It is conceptual (i.e., tank structure) but with physically based parameters, and fully distributed in the space. It is a parsimonious model thanks to the incorporation of a split effective parameter structure that allows a significant reduction in the number of variables to be calibrated (only nine correction factors) facilitating the model calibration stage using an optimization algorithm [41]. Several maps were used to feed the model with the catchment geomorphological characteristics, such as slope, flow directions, and flow accumulation, which were obtained from a digital elevation model with a 100-m resolution obtained from National Geographic Institute (IGN). The hydraulic conductivity of the soil was obtained from the European Soil Database (ESDB). Capillary water content capacity of the upper soil was estimated from ESDB and by reclassifying the CORINE land use map. Hydraulic conductivity of saturated rock (used for the percolation capacity) was estimated using the map reclassified to lithological units from the Spanish Geological and Mining Institute (IGME).

Model implementation was carried out at two temporal resolutions. On the one hand, the model was implemented on a daily scale and this was used to obtain the long data series of discharges. On the other hand, a 5-min temporal resolution model was also implemented. This allowed the relation between peak and daily discharges at any point in our study area to be obtained.

With regards to the WG, after testing different models, GWEX [22] was selected. This WG was designed to focus on extreme events and incorporates a heavy-tailed distribution function for the precipitation amounts: the E-GPD [42]. It offers the possibility to introduce a tail dependence between...
at-site extremes by using a student copula to represent the dependence structure of innovations. Additionally, and what is more important, it is possible to simulate precipitation in 3-day periods for then being disaggregated to a daily scale by the method of fragments. This latter feature was particularly interesting for our case study given that the extreme events that take place in our study area last between 2 and 3 days on average.

Long synthetic data series of precipitation and temperatures were generated. These, in turn, fed the daily hydrological model obtaining the resulting discharge data series. Finally, the results were validated in two stages: (1) comparison of the flows associated with low quantiles with the observed flows at Maria Cristina Dam; and (2) comparison of the quantiles of the upper part of the distribution function with the non-systematic records previously converted into daily values.

As previously mentioned, non-systematic data were collected from previous studies reporting documentary floods and palaeoflood analysis [27,40]. Historical floods were collected from scientific and technical reports; local history books and non-systematic compilations by historians, such as Balbás [43], Fagués [44], and Fontana Tarrats [45]; and from recent compilations by Camarasa Belmonte and Segura Beltrán [34], Sánchez Adell et al. [46], and Beltrán Manrique [47]. The Rambla de la Viuda documentary flood evidence reports a total 19 large floods since CE1378, although continuous and homogeneous data started in 1959. Palaeoflood records were reconstructed on the basis of sedimentary evidence at two sites (Figure 2), namely in Rambla de la Viuda upstream of the Maria Cristina Reservoir [40] and in the Monlleó River [27]. Palaeoflood data result from the analysis of palaeostage indicators consisting of stratigraphic sequences of fine-flood sediments (mainly sand and silt), each representing an individual flood event [40]. Hydraulic studies were performed to relate the elevation of sediment layers to palaeoflood discharges, and flood age was obtained by geochronological analysis (see Ballesteros-Canovas et al. [29]). In Rambla de la Viuda, the palaeoflood record contains a total of 17 floods above a threshold of 500 m$^3$s$^{-1}$ since CE1378, whereas in the Monlleó River, it comprises 10 floods above a threshold of 470 m$^3$s$^{-1}$ since CE1475.

4. Results

4.1. Fully Distributed Hydrological Model

The following paragraphs describe the implementation of the hydrological model at both the daily scale and 5-min temporal resolutions.

4.1.1. Daily Implementation

For the daily scale model, six extreme flow events were selected from the available records in the SAIH (1959–2015) at Maria Cristina dam: 1962, 1969, 1989, 2000, 2006, and 2015. The model was fed with hourly and daily rainfall from the grid points shown in Figure 2. The calibration process was especially complex due to two specific particularities of this case study: the asynchrony between meteorological and hydrological daily data and the difficulties to evaluate flow transmission losses into the karstic and alluvial aquifers. Firstly, during the calibration process, it was observed that the maximum flow appeared one day after the maximum precipitation event occurred; however, the area of the basin was not large enough for its concentration time to be one day. Different aggregation intervals of precipitation and flow were detected, as weather stations measure daily time blocks from 07:00 to 07:00, whilst the flows are recorded at the dam from 19:00 to 19:00. If it rains in the early hours of the morning or between the afternoon and the night of any given day, with a residence time of 7 or 8 h according to the size of the Rambla de la Viuda basin, the flow can be transferred to the next day [48]. The solution, thus, consisted of advancing by one day the time series corresponding to the hydrological information, making the event of maximum precipitation and the peak flow coincide on the same day, improving the model performance in both the calibration and validation stages.

After the correction of the time lag, it was noted that during certain periods of time and despite the fact that there were registered rains, there were simulated small peak flows where the observed
hydrograph did not show them. This was considered as a clear indicator of the existence of transmission losses in the basin as a consequence of the effects of karstification and the existence of reaches where the streamflow was directly connected into the groundwater system.

TETIS allows for the introduction and extraction of external flows to the basin to consider the effects of external demands, such as irrigation channels, as well as the input of external flows from transfers. Using this characteristic and by looking into the zero-probability events, flow losses of ~8 m$^3$ s$^{-1}$ were estimated and accordingly extracted at specific reaches of the model. This removed the simulated small peaks and improved the model performance.

Lastly, and considering that the main purpose of this methodology is to estimate flood quantiles, the daily hydrological model was validated comparing the plotting positions of the 57-year period of observed annual maximum daily flows and the 66-year period of simulated ones (Figure 4). In this case, instead of comparing the flow events one-to-one, the two complete data series of observed and simulated flows were compared. However, since neither the length of both data series is the same and consequently nor are the associated probabilities, the observed and simulated flows cannot be directly related one-to-one. The used plotting position formulation was proposed by Cunnane [49]:

$$ F_i = \frac{i - \alpha}{N + 1 - 2\alpha} $$

where $i$ is the position, $N$ is the length of the data series, and $\alpha$ is a coefficient. Since this study was focused on extremes, a value of $\alpha = 0.44$ was adopted [50].

![Plotting positions of simulated and observed annual maximum daily flows in Maria Cristina dam.](image)

**Figure 4.** Plotting positions of simulated and observed annual maximum daily flows in Maria Cristina dam.

### 4.1.2. Sub-Daily Implementation

For the sub-daily implementation of TETIS, three high flow events were selected (2000, 2015, and 2018) with available records at 5-min time-steps of precipitation and temperature as well as information of observed flows and reservoir levels from the SAIH network.

In this case, a cross-calibration was performed at Maria Cristina dam, obtaining the best results in terms of the Nash–Sutcliffe index (NSE; [51]) when calibrating in the 2018 event (Figure 5). For this calibration period, an NSE index of 0.7556 was obtained, whilst an NSE index of 0.6293 and 0.3684 was obtained for the 2000 and 2015 validation periods, respectively.
Parameter Estimation

A similar approach to that proposed in Evin et al. [22] was carried out. A regional study of Spanish maximum daily precipitation [52] was used to compare the simulated flow quantiles in two steps. In this study, the coefficient of variation was regional, and the mean was local, which was used for the regionalization. The region this catchment belongs to had more than 30 years of precipitation records, which means that the estimated coefficient of variation has high reliability. Therefore, we maintained the regional coefficient of variation and only updated the local means.

Secondly, due to the systematic quantile underestimation (as shown in Figure 6), the regional study of maximum daily precipitation was used to calibrate the shape parameter $\xi$ of the marginal distribution function $E$-GDP. The final value adopted was the one that minimized the mean root mean square error (RMSE) between the observed and simulated quantiles. For this second calibration, it was decided to split the precipitation into two groups: (1) a first group that included the ordinary precipitations, that is to say, the precipitation that fell outside the autumn months, where the shape parameter was left as per default ($\xi = 0.05$); and (2) the precipitation falling during autumn months (SON), i.e., comprising all heavy precipitation events. Since the catchment dimensions can be considered small and with no great differences in terms of annual precipitation between the upper and lower parts, it was deemed appropriate to consider the catchment as a single unit. Therefore, one value of the shape parameter $\xi$, that minimized the RMSE was $\xi = 0.16$.

Figure 5. Observed and simulated sub-daily hydrographs for the calibration in the 2018 event (a), and temporal validation in the 2000 event (b) at Maria Cristina dam.

4.2. Stochastic Daily Weather Generator

The GWEX model [22] was used for simulating long data series of both precipitation and temperatures. The next section discusses the way the parameters of the WG were estimated and presents the results of the implementation.
considered small and with no great differences in terms of annual precipitation between the upper and lower parts, it was deemed appropriate to consider the catchment as a single unit. Therefore, one value of the shape parameter $\xi$ was estimated for all the rain gauges. After several iterations, the value of $\xi$ that minimized the RMSE was $\xi = 0.16$.

Figure 6. Results of WG calibration in four representative grid points.

4.3. Peak Discharge Transformation

The palaeoflood information in this case study, and very often, is presented as lower limits of the peak floods, without knowing the exact value of the peak. Therefore, there is a need for conversion between peak ($Q_p$) and daily discharges ($Q_d$) in order to exploit this information using the HM implemented at a 5-min temporal resolution (Section 4.1.2).

A set of 50 high flow events were synthetically generated by scaling the available records of precipitation and modifying the initial soil moisture. From these, 33 and 21 episodes respectively were selected to proceed with the analysis. Daily discharges were calculated by grouping the sub-daily data for each event at both locations where palaeoflood information was available and compared against the simulated peak discharges with the 5-min HM (Figure 7). The fitted potential equations have a coefficient $R$ of Sperman higher than 0.8 at both locations. Finally, palaeoflood information from [27,40] was converted into daily values using the fitted potential relationship.

4.4. Validation with the Palaeoflood Information

Figure 8 shows the plotting positions (given by Equation (1)) of the 10,000 simulated annual maximum daily discharges at Rambla de la Viuda and Montlleó palaeoflood sites. The plotting positions of the palaeoflood information can be used for the validation of the methodology. However, this non-systematic information must be statistically classified as binomial censored [31], and only can be computed the plotting position of the common censoring threshold (represented by a triangle in Figure 8) and the plotting position of the lower bound of the maximum flood (represented by an arrow in Figure 8), where the data length includes the systematic and non-systematic periods.
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5. Discussion

5.1. Flood Frequency with Weather Generators and a Regional Precipitation Study

Available discharge and precipitation records are still far from being sufficiently robust for an adequate estimation of extreme events with a high return period. Traditional purely statistical studies using systematic records have been proved to involve high uncertainty, resulting in either over- or underestimations of the simulated flood quantiles [53] and, in any case, they can only be applied in the location of the flow gauge station.

Later studies focusing on individual synthetic storms have been used for many years for infrastructure design [54]. Again, great uncertainty surrounded these studies since not necessarily the biggest storm should result in the highest flows, and these would depend upon the spatio-temporal distribution of the storm and the initial conditions of the catchment, which these studies do not rigorously account for.
A continuous synthetic simulation approach using a WG and a fully-distributed HM seems to be becoming one of the potential candidates to deal with this challenge and its use is rapidly increasing over recent years [55]. The possibility of extending the records beyond the available ones using a WG reduces the uncertainty of the calculated flood quantiles. Yet, the quality of the precipitation input data series (length, spatial density, reliability, and completeness) is critical to obtain reliable results and, therefore, extra tools and additional information must be integrated to complement their current short length and improve the performance of the WG. For example, in our case study, taking into account that the characteristic high precipitation events have an approximate return period of 7/8 years on average and these are of extreme magnitude every 20/30 years, 66 years of observed precipitation was not enough information for the WG to satisfactorily reproduce extreme events.

Traditionally, WGs have used light-tailed distribution functions to model precipitation amounts, such as the exponential, gamma, or combinations of both. However, these types of distribution where the tails exponentially decay result in underestimations in the precipitation of the most extreme events [20]. GWEX, instead, incorporates a heavy-tailed distribution function for modeling the precipitation amounts. This, along with the 3-day precipitation amounts modeling, improved the performance of the WG, reducing the underestimations of the higher flows, and, as demonstrated in the present study, could be considered as a good option when dealing with arid/semiarid climates where most of the precipitation is concentrated in few days, as in the case of the Spanish Mediterranean coastal catchments [34,35].

Evin et al. [22] suggest that robust studies are needed to adequately estimate certain weather generator parameters, particularly when trying to capture extremes. In our case and following the same approach, we incorporated the information from an available regional study of maximum annual precipitation from CEDEX [52] for a better calibration of the shape parameter $\xi$. This regional study substantially improved the performance of the WG, especially for high return periods, where the underestimation was more evident (Figure 6).

The better reproduction of precipitation data series was also reflected in the results obtained with the HM (Figure 8). However, it would not have been possible to validate the low-frequency events only with the observed discharge information, since with a systematic flood records’ length of 57 years in the case of Maria Cristina dam, only flood quantiles up approximately $T = 50$ years would have been possible to obtain with a minimum of confidence. The integration of palaeoflood records was key to validate the upper tail of the distribution function.

5.2. Non-Systematic Information

Palaeoflood information provides data on individual extreme hydrological events. Robust palaeodischarge estimations were obtained from sedimentological evidence of floodwater elevations reached by past floods [56]. By providing information beyond systematic records, it is generally possible to extend the flood frequency curve over the 50-year return period and, therefore, reduce the uncertainty of the highest quantiles. In the study carried out by Francés [3] for the Turia river basin, it was concluded that errors in the estimation decreased as the amount of information used to estimate the flood quantile of 1000 years increased, observing that the use of historical information reduced the estimation error by approximately 50% in his case study. Lam et al. [57] concluded that the uncertainty associated with estimated discharge for the 100-year return period flood was reduced by more than 50% when including palaeoflood information.

In the present study, the analysis of the reduction of the uncertainty associated with the flood quantile estimates was not in the scope. Nevertheless, the reliability of the calculated flood quantiles decreases as the return period increases [6]. In our case, only with the observed precipitation (66 years), despite being able to calculate the plotting position up to approximately $T = 50$ years, the uncertainly surrounding return periods higher than 10 years was too high to deem them valid.

However, the palaeoflood records from the studies of [27,40] provided extra information at the upper tail of the probability function. Specifically, the plotting position of the common censoring
threshold (represented by a triangle in Figure 8), which was calculated with the number of high flow events exceeding a threshold of 470 and 500 m$^3$ s$^{-1}$, allowed more robust estimates of the flood quantiles of $T = 36$ years and $T = 53$ years, respectively, to be obtained. Furthermore, it was also possible to obtain the plotting position of the lower bound of the maximum flood (represented by an arrow in Figure 8), with associated return periods of approximately $T = 500$ years at both sites.

On the other hand, palaeoflood information is usually related to the peak of the flood. Therefore, daily data series of generated flows must be converted into instantaneous flows or vice versa in order to be able to compare the results. Traditionally, this transformation has been based on empirical methods as in Fuller [58] or in deterministic methods [59,60]. Fathzadeh et al. [61] compared four different approaches, concluding that, although some of the tested methods (i.e., adaptive neuro-fuzzy inference systems and artificial neural networks) could obtain better results, it is necessary to have a robust subset of data to train more sophisticated models. In other words, the existence of robust datasets is more important than the method used.

Since these were not available in our study area, it was decided to implement the HM in a sub-daily temporal resolution (5-min). Simulating different synthetic rain events, it was possible to obtain for each the relation between daily and peak discharges at both locations where palaeoflood information was available. All these values were fitted to a potential function, obtaining satisfactory Pearson’s correlation coefficients (i.e., 0.8174 and 0.8207) (Figure 7).

5.3. A Holistic Methodological Approach to Estimate Extreme Floods

The methodology presented in this case study is an extension of the continuous synthetic simulation model. Apart from the benefits of this approach discussed before (i.e., initial conditions of the catchment and spatio-temporal distribution of the storm), we propose the integration of additional information to deal with the estimation bias on the flood quantile resulting from the short length of the existing hydrometeorological data series. This methodology can be implemented in any region regardless of its size or its climate; however, the more remarked climate variability, the greater the need to add extra sources of information due to their erratic hydrology.

In our case, an existing regional study of extreme precipitation was used to improve the calibration of the WG and palaeoflood records were included to validate the discharge series. However, this is not the only option; it is possible to apply the present methodology only having one source of information. In the case of having only the regional study of extreme precipitation, the WG can be calibrated with this; however, the resulting discharges cannot be validated. Conversely, in the case of only having palaeoflood records, although not being so straight forward, the WG can be calibrated by comparing the resulting discharge series with the palaeoflood records.

Additionally, due to their ephemeral or temporary nature, most of the streams that lead to catastrophic floods over the months of SON in the Mediterranean coast are either ungauged or only equipped with sensors capable of detecting flow for flood warning purposes. The selection of a deterministic (fully distributed and physically based) HM here was of upmost importance to capture local infiltration losses and gains. TETIS, being a fully distributed HM where the parameters are physically based, preserves the spatiotemporal distribution of the storm and allows the discharge information at any point of the catchment to be known unlike in the case of lumped or semi-distributed HMs. Thus, fully distributed models allow improvement of the understanding of flood extreme regimes in parts of the catchment where discharge records are not available, leading to better estimations of extreme floods, which, in turn, could result in improvements on the flood design of sensible infrastructures or early flood warning protocols. Furthermore, integrating them is an indispensable condition if palaeoflood information is to be incorporated, since this is limited to certain parts of the river where these records can be obtained and usually not in the same location where the flow gauge stations are located.

It is a fact, however, that many of the extreme precipitation events could have a duration lower than a day (i.e., flash floods) and some can argue that lower temporal scales are needed in order to
account for these phenomena. However, simulating long series of precipitation and discharges at sub-daily temporal resolution is, to date, not operational for medium and large catchments due to the lack of appropriate WGs and the need in any case of supercomputers, which are not to everyone’s reach. Nevertheless, the case study presented in this paper showed that a daily temporal resolution could produce satisfactory results, especially in those areas where extreme event duration is typically longer than one day as in the Spanish Mediterranean coast.

6. Conclusions

The reliability of flood estimates depends upon long and trustworthy input data series (i.e., precipitation and/or discharges). Most ephemeral rivers worldwide lack long-term and spatially fully distributed hydrometeorological information, which leads to inaccurate estimations of flood quantiles, especially those associated with high return periods. Continuous synthetic simulation models have been gaining ground over recent years to the detriment of statistical or deterministic approaches. The use of continuous stochastic meteorological models coupled with a fully distributed hydrological simulation provided a realistic approach, enabling the recreation of multiple and different situations at any point within the catchment, thus completing the frequency distributions of discharges along with the whole river network. Yet, though, long and reliable input data series of precipitation and discharges are necessary for the correct implementation of the WG and the HM, which in practice are rarely available.

The methodology presented in this paper was applied in a typical Mediterranean ephemeral river and combined a long synthetic meteorological data series within a continuous synthetic simulation approach, with the additional inclusion of a regional study of extreme precipitation and palaeoflood data, with the objective of improving the flood quantile estimations, especially those associated with low probabilities.

Our results show that the integration of more robust precipitation studies for the WG implementation clearly improved its performance. In our case, the integration of an existing regional study of annual maximum precipitation allowed reproduction of the precipitation quantiles with high return periods, where the bias was more significant.

This improvement was transferred to the simulation of discharge data series with the fully distributed HM. Here, the available palaeoflood records gave extra flood information up to $T = 500$ years as opposed to the highest quantile of $T = 50$ years obtained only with the systematic information. By having this extra information at the upper tail of the distribution, it was possible to validate the simulated extreme discharges and, at the same time, the proposed methodology.

Moreover, these estimates are not limited to the sites where flow gauge stations are located or where the palaeoflood information is available. The fully distributed HM provides reliable data on extreme flood discharges at any point of the catchment, thus leading to better knowledge of its hydrology compared with the traditional methodologies based on at site flood frequency analysis of recorded discharges or the HM modeling of a design storm.

Finally, the importance of incorporating two different sources of additional information in the methodology when trying to estimate extreme flooding was demonstrated. Whilst adding one source of additional information is essential for a better calibration of the WG, adding a second one allows for validation of the simulated discharges, thus improving the robustness of the methodology and providing higher confidence in the flood quantile estimates. These findings have important implications towards a more efficient and balanced flood risk management in general, but especially in poorly monitored catchments with high variability in their flood regime.

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**References**

1. Foster, H.A. *Theoretical Frequency Curves and the Application to Engineering Problems*; Transactions of the American Society of Civil Engineers: New York, NY, USA, 1924.

2. Stedinger, J.R.; Grifﬁs, V.W. Flood frequency analysis in the United States: Time to update. *J. Hydrol. Eng.* 2008, 13, 199–204. [CrossRef]

3. Francés, F. Using the TCEV distribution function with systematic and non-systematic data in a regional flood frequency analysis. *Stoch. Environ. Res. Risk Assess.* 1998, 12, 267–283. [CrossRef]

4. Merz, R.; Blöschl, G. Process controls on the statistical flood moments—A data based analysis. *Hydrol. Process.* 2009, 23, 675–696. [CrossRef]

5. Stedinger, J.R.; Cohn, T.A. Flood frequency analysis with historical and paleoflood information. *Water Resour. Res.* 1986, 22, 785–793. [CrossRef]

6. Botero, B.A.; Francés, F. Estimation of high return period flood quantiles using additional non-systematic information with upper bounded statistical models. *Hydrol. Earth Syst. Sci.* 2010, 14, 2617–2628. [CrossRef]

7. Cohn, T.A.; England, J.F.; Berenbrock, C.E.; Mason, R.R.; Stedinger, J.R.; Lamontagne, J.R. A generalized Grubbs-Beck test statistic for detecting multiple potentially inﬂuential low outliers in flood series. *Water Resour. Res.* 2013, 49, 5047–5058. [CrossRef]

8. Chow, V.T.; Maidment, D.R.; Mays, L.W.; Maidment, L.W.M. *Applied Hydrology*; McGraw-Hill, Inc.: New York, NY, USA, 1998; ISBN 0-07-100174-3. Available online: https://wecivilengineers.files.wordpress.com/2017/10/applied-hydrology-ven-te-chow.pdf (accessed on 13 November 2020).

9. Houghton-Carr, H. Restatement and application of the flood studies report rainfall-runoff method. In *Flood Estimation Handbook*; Institute of Hydrology: London, UK, 1999; Volume 4.

10. Emmanuel, I.; Payrastre, O.; Andrieu, H.; Zuber, F. A method for assessing the inﬂuence of rainfall spatial variability on hydrograph modeling. First case study in the Cevennes Region, southern France. *J. Hydrol.* 2017, 555, 314–322. [CrossRef]

11. Pathiraja, S.; Westra, S.; Sharma, A. Why continuous simulation? The role of antecedent moisture in design flood estimation. *Water Resour. Res.* 2012, 48, 1–15. [CrossRef]

12. Grimaldi, S.; Nardi, F.; Piscopia, R.; Petroselli, A.; Apollonio, C. Continuous hydrologic modelling for design simulation in small and ungauged basins: A step forward and some tests for its practical use. *J. Hydrol.* 2020, 125664. [CrossRef]

13. Cameron, D.S.; Beven, K.J.; Tawn, J.A.; Blazkova, S.; Naden, P. Flood frequency estimation by continuous simulation for a gauged upland catchment (with uncertainty). *J. Hydrol.* 1999, 219, 169–187. [CrossRef]

14. Eagleson, P.S. Dynamics of flood frequency. *Water Resour. Res.* 1972, 8, 878–898. [CrossRef]

15. Brocca, L.; Liersch, S.; Melone, F.; Moramarco, T.; Volk, M. Application of a model-based rainfall-runoff database as efﬁcient tool for flood risk management. *Hydrol. Earth Syst. Sci.* 2013, 17, 3159–3169. [CrossRef]

16. Cowpertwait, P.S.; Ocio, D.; Collazos, G.; De Cos, O.; Stocker, C. Regionalised spatiotemporal rainfall and temperature models for ﬂood studies in the Basque Country, Spain. *Hydrol. Earth Syst. Sci.* 2013, 17, 479–494. [CrossRef]

17. Boughton, W.; Droop, O. Continuous simulation for design flood estimation—A review. *Environ. Model. Softw.* 2003, 18, 309–318. [CrossRef]

18. Soltani, A.; Hoogenboom, G. Minimum data requirements for parameter estimation of stochastic weather generators. *Clin. Res.* 2003, 25, 109–119. [CrossRef]

19. Verdin, A.; Rajagopalan, B.; Kleiber, W.; Katz, R.W. Coupled stochastic weather generation using spatial and generalized linear models. *Stoch. Environ. Res. Risk Assess.* 2014, 29, 347–356. [CrossRef]

20. Cavanaugh, N.R.; Gershunov, A.; Panorska, A.K.; Kozubowski, T.J. On the probability distribution of daily precipitation extremes. *Geophys. Res. Lett.* 2015, 42, 1560–1567. [CrossRef]
21. Furrer, E.M.; Katz, R.W. Improving the simulation of extreme precipitation events by stochastic weather generators. *Water Resour. Res.* **2008**, *44*, 1–13. [CrossRef]

22. Evin, G.; Favre, A.-C.; Hingray, B. Stochastic generation of multi-site daily precipitation focusing on extreme events. *Hydrol. Earth Syst. Sci.* **2018**, *22*, 655–672. [CrossRef]

23. Metzger, A.; Marra, F.; Smith, J.A.; Morin, E. Flood frequency estimation and uncertainty in arid/semi-arid regions. *J. Hydrol.* **2020**, *590*, 125254. [CrossRef]

24. Zaman, M.A.; Rahman, A.; Haddad, K. Regional flood frequency analysis in arid regions: A case study for Australia. *J. Hydrol.* **2012**, *475*, 74–83. [CrossRef]

25. Merz, R.; Blöschl, G. Flood frequency hydrology: 1. Temporal, spatial, and causal expansion of information. *Water Resour. Res.* **2008**, *44*, 1–16. [CrossRef]

26. Merz, R.; Blöschl, G. Flood frequency hydrology: 2. Combining data evidence. *Water Resour. Res.* **2008**, *44*, 1–16. [CrossRef]

27. Benito, G.; Sanchez-Moya, Y.; Medialdea, A.; Barriendos, M.; Calle, M.; Rico, M.; Sopeña, A.; Machado, M.J. Extreme floods in small mediterranean catchments: Long-term response to climate variability and change. *Water* **2020**, *12*, 1008. [CrossRef]

28. Baker, V.R. Paleoflood hydrology and extraordinary flood events. *J. Hydrol.* **1987**, *96*, 79–99. [CrossRef]

29. Ballesteros-Cánovas, J.A.; Sánchez-Silva, M.; Bodoque, J.; Diez-Herrero, A. An integrated approach to flood risk management: A case study of Navaluenga (Central Spain). *Water Resour. Manag.* **2013**, *27*, 3051–3069. [CrossRef]

30. England, J.F., Jr.; Cohn, T.A.; Faber, B.A.; Stedinger, J.R.; Thomas, W.O., Jr.; Veilleux, A.G.; Kiang, J.E.; Mason, R. Guidelines for Determining Flood Flow Frequency-Bulletin 17C; Techniques and Methods 4-B5; U.S. Geological Survey: Reston, VA, USA, 2019.

31. Frances, F.; Salas, J.D.; Boes, D.C. Flood frequency analysis with systematic and historical or paleoflood data based on the two-parameter general extreme value models. *Water Resour. Res.* **1994**, *30*, 1653–1664. [CrossRef]

32. Stedinger, J.R.; Baker, V.R. Surface water hydrology: Historical and paleoflood information. *Rev. Geophys.* **1987**, *25*, 119. [CrossRef]

33. Simón, J.L.; Pérez-Cueva, A.J.; Calvo-Cases, A. Tectonic beheading of fluvial valleys in the Maestrat grabens (eastern Spain): Insights into slip rates of Pleistocene extensional faults. *Tectonophysics* **2013**, *593*, 73–84. [CrossRef]

34. Belmonte, A.M.C.; Beltrán, F.S. Flood events in Mediterranean ephemeral streams (ramblas) in Valencia region, Spain. *Catena* **2001**, *45*, 229–249. [CrossRef]

35. Mateu, J.F. La Rambla de la Viuda. Clima e Hidrología. *Cuad. Geogr.* **1974**.

36. Segura, F.S.; Camarasa, A. Balances hídricos de crecidas en ramblas mediterráneas: Pérvidas hídricas. *In Clima y Agua: La Gestión de un Recurso Climático*; Marzol, M.V., Dorta, P., Valladares, P., Eds.; La Laguna University: San Cristóbal de la Laguna, Spain, 1996; pp. 235–245.

37. Llasat, M.C.; Puigcerver, M. Cold air pools over Europe. *Theor. Appl. Clim.* **1990**, *42*, 171–177. [CrossRef]

38. Herrera, S.; Fernández, J.J.G.; Gutiérrez, J.M. Update of the Spain02 gridded observational dataset for EURO-CORDEX evaluation: Assessing the effect of the interpolation methodology. *Int. J. Clim.* **2016**, *36*, 900–908. [CrossRef]

39. Ministerio de Fomento. Dirección General de Carreteras Máximas lluvias diarias en España Peninsular. 1999. Available online: https://www.mitma.gob.es/recursos_mfom/0610300.pdf (accessed on 12 November 2020).

40. Machado, M.; Medialdea, A.; Calle, M.; Rico, M.; Sanchez-Moya, Y.; Sopeña, A.; Benito, G. Historical palaeohydrology and landscape resilience of a Mediterranean rambla (Castellón, NE Spain): Floods and people. *Quat. Sci. Rev.* **2017**, *171*, 182–198. [CrossRef]

41. Francés, F.; Vélez, J.I.; Vélez, J.J. Split-parameter structure for the automatic calibration of distributed hydrological models. *J. Hydrol.* **2007**, *332*, 226–240. [CrossRef]

42. Papastathopoulos, I.; Tawn, J.A. Extended generalised Pareto models for tail estimation. *J. Stat. Plan. Inference* **2013**, *143*, 131–143. [CrossRef]

43. Balbás, J.A. El Libro de la Provincia de Castellon. 1892. Available online: http://hdl.handle.net/10234/14914 (accessed on 12 November 2020).

44. Fogués, F. Las inundaciones de la Ribera. *An. Cent. Cult. Valencia* **1931**, 232–250.
45. Fontana Tarrats, J.M. *Historia del Clima en el Litoral Mediterráneo: Reino de Valencia más Provincia de Murcia*; Ayuntamiento de Alicante: Alicante, Spain, 1978.

46. Sánchez Adell, J.; Montins, O.; Sánchez Almela, F.E. *Elenco de Fechas para la Historia Urbana de Castellón de la Plana*; Sociedad Castellonense de Cultura: Castellon, Spain, 1993.

47. Beltrán Manrique, E. *Almazora el Mijares. Narración Histórica*; Plana C., Ed.; Hijos de F. Armengot: Castellon, Spain, 1958.

48. Vélez, J.J.; Botero, A. *Estimation of the Time of Concentration and the Lag Time at San Luis Creek Basin, Manizales*; DYNA: Medellin, Colombia, 2011; Volume 78, pp. 58–71.

49. Cunnane, C. *Unbiased plotting positions-A review*. *J. Hydrol.* 1978, 37, 205–222. [CrossRef]

50. Gringorten, I.I. *A plotting rule for extreme probability paper*. *J. Geophys. Res. Space Phys.* 1963, 68, 813–814. [CrossRef]

51. Nash, J.; Sutcliffe, J. *River flow forecasting through conceptual models part I-A discussion of principles*. *J. Hydrol.* 1970, 10, 282–290. [CrossRef]

52. CEDEX Mapa de Caudales Máximos. In *Memoria Técnica*; CEDEX Mapa de Caudales Máximos: Madrid, Spain, 1994. Available online: https://www.miteco.gob.es/es/agua/temas/gestion-de-los-riesgos-de-inundacion/memoria_tecnica_v2_junio2011_tcm30-214566.pdf (accessed on 12 November 2020).

53. Haktanir, T.; Horlacher, H.B. *Evaluation of various distributions for flood frequency analysis*. *Hydrol. Sci. J.* 1993, 38, 15–32. [CrossRef]

54. Chen, X.; Hossain, F. *Understanding future safety of dams in a changing climate*. *Bull. Am. Meteorol. Soc.* 2019, 100, 1395–1404. [CrossRef]

55. Lamb, R.; Faulkner, D.; Wass, P.; Cameron, D. *Have applications of continuous rainfall-runoff simulation realized the vision for process-based flood frequency analysis?* *Hydrol. Process.* 2016, 30, 2463–2481. [CrossRef]

56. Benito, G.; Thorndycraft, V.R. *Palaeoflood hydrology and its role in applied hydrological sciences*. *J. Hydrol.* 2005, 313, 3–15. [CrossRef]

57. Lam, D.; Thompson, C.J.; Croke, J.; Sharma, A.; Macklin, M.; Thompson, C.J. *Reducing uncertainty with flood frequency analysis: The contribution of paleo flood and historical flood information*. *Water Resour. Res.* 2017, 53, 2312–2327. [CrossRef]

58. Fuller, W. *Flood flows*. *Trans. Am. Soc. Civ. Eng.* 1914, 77, 564–617.

59. Applied hydrology. *J. Hydrol.* 1968, 6, 224–225. [CrossRef]

60. Sangal, B.P. *Practical method of estimating peak flow*. *J. Hydraul. Eng.* 1983, 109, 549–563. [CrossRef]

61. Fathzadeh, A.; Jaydari, A.; Taghzadeh-Mehrjardi, R. *Comparison of different methods for reconstruction of instantaneous peak flow data*. *Intell. Autom. Soft Comput.* 2016, 23, 41–49. [CrossRef]

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