Modelling the connection between ultraviolet and infrared galaxy populations across cosmic times

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ABSTRACT

Using a phenomenological approach, we self-consistently model the redshift evolution of the ultraviolet (UV) and infrared (IR) luminosity functions across cosmic time, as well as a range of observed IR properties of UV-selected galaxy population. This model is an extension of the 2SFM (2 star formation modes) formalism, which is based on the observed ‘main sequence’ of star-forming galaxies, i.e. a strong correlation between their stellar mass and their star formation rate, and a secondary population of starbursts with an excess of star formation. The balance between the UV light from young, massive stars and the dust-reprocessed IR emission is modelled following the empirical relation between the attenuation (IRX for IR excess hereafter) and the stellar mass, assuming a scatter of 0.4 dex around this relation. We obtain good overall agreement with the measurements of the IR luminosity function up to z ≈ 3 and the UV luminosity functions up to z ≈ 6, and show that a scatter on the IRX–M relation is mandatory to reproduce these observables. We also naturally reproduce the observed, flat relation between the mean IRX and the UV luminosity at L_{UV} > 10^{9.5} L_{⊙}. Finally, we perform predictions of the UV properties and detectability of IR-selected samples and the vice versa, and discuss the results in the context of the UV-rest-frame and sub-millimetre surveys of the next decade.

Key words: galaxies: evolution – galaxies: luminosity function, mass function – galaxies: statistics – infrared: galaxies – ultraviolet: galaxies.

1 INTRODUCTION

Galaxy evolution in the cosmological context is an important topic of modern astrophysics. In particular, processes that drive star formation and gas accretion within galaxies are not well understood. Observational constraints from deep surveys should provide insights for solving this complex problem. Obtaining accurate star formation rate (SFR) estimates for statistically significant samples of galaxies is thus particularly important. In deep photometric surveys, the rest-frame far-ultraviolet (hereafter UV) continuum emitted by blue, young and massive stars is a good probe of the SFR. Unfortunately, dust in star-forming regions absorbs a large fraction of the UV photons and reprocesses them into mid- and far-infrared (hereafter IR) emissions. The fraction of escaping UV photons can be estimated by computing the ratio between the IR and UV luminosity density (L_{DIR}/L_{DUV}), which are estimated integrating the UV (e.g. Arnouts et al. 2005; Cucciati et al. 2012) and IR (e.g. Le Floc’h et al. 2005; Magnelli et al. 2009; Rodighiero et al. 2010; Casey et al. 2012; Gruppioni et al. 2013) luminosity functions. This quantity evolves from ~60 per cent in the local Universe up to ~90 per cent at z ~ 1.5 (e.g. Takeuchi, Buat & Burgarella 2005; Burgarella et al. 2013).

To measure the SFR in galaxies, it is thus crucial to estimate accurately the fraction of UV light reprocessed by dust. The easiest method is to measure both unabsorbed UV and reprocessed IR emissions to trace the full intrinsic UV light emitted by young stars. Nevertheless, even the deepest and most recent IR surveys (e.g. Herschel) are limited by the confusion phenomenon (Dole et al. 2004; Nguyen et al. 2010) and the low sensitivity of the detectors as compared to the optical regime. Indeed, the majority of high-redshift UV galaxies cannot be detected in IR. For these IR-undetected galaxies, the correction for dust attenuation has to be estimated using UV and optical data only. For instance, Meurer, Heckman & Calzetti (1999) proposed a relation, which links the attenuation to...
the UV continuum slope, calibrated using observations in the local Universe. This relation was tested up to \( z \sim 2 \) (e.g. Buat et al. 2005; Reddy et al. 2010; Heinis et al. 2013). However, such analyses are either based on samples detected in both IR and UV, which could introduce a selection bias, or based on stacking analyses (Reddy et al. 2010; Heinis et al. 2013), which does not allow us to measure the scatter. Furthermore, the Meurer et al. (1999) relation may also be subject to aperture effects (Overzier et al. 2011; Takeuchi et al. 2012). The understanding of selection effects caused by the limited depth of IR observations and the very different dust attenuation observed in galaxies is thus crucial to estimate accurately the SFR density in the high-redshift Universe.

These selection effects can be studied using phenomenological models. In particular, the 2SFM (2 star formation modes; Béthermin et al. 2012; Sargent et al. 2012) model was motivated by the finding of a strong correlation between the SFR and the stellar mass (M) of star-forming galaxies, called main sequence (MS), which evolves with redshift in normalization (e.g. Daddi et al. 2007; Elbaz et al. 2007; Noeske et al. 2007). This strong correlation suggests that the bulk of the stars are formed in galaxies following secular processes. Sargent et al. (2012) showed that the IR luminosity function can be reproduced well by adding to the MS a minor population (\( \sim 3 \) per cent of the whole population) of starburst (SB) that display a strong excess of SFR compared to the MS. This population is thought to have SFR driven by short-lasting, extreme events such as major mergers (Elbaz et al. 2007, 2011; Tacconi et al. 2008; Daddi et al. 2010; Genzel et al. 2010). Béthermin et al. (2012) show that galaxy number counts from the mid-infrared to the radio can be reproduced considering distinct spectral energy distributions (SED) for MS and SB galaxies. Using a method based on abundance matching, Béthermin et al. (2013) have also shown that the 2SFM model efficiently predicts the large-scale fluctuations of the cosmic IR background produced by dusty, star-forming galaxies, thereby probing the link between IR galaxies and dark matter haloes. This modelling approach is thus very efficient for reproducing and interpreting IR observables. As Sargent et al. (2012) did not consider the unobscured component of SFR emitted in the UV by star-forming galaxies, we propose in this paper to extend the model to the UV.

Our extension to UV emission requires a well-constrained prescription for how the intrinsic UV light emitted by young stars is redistributed between the unattenuated UV escaping from galaxies and the IR reprocessed by dust. Here, we use the link between the stellar mass and the IR excess (IRX, defined as log(\( L_{IR}/L_{UV} \)), where \( L_{IR} \) and \( L_{UV} \) are respectively the IR and UV luminosities) found by several observational studies (Pannella et al. 2009; Heinis et al. 2014; Pannella et al. in preparation). We note that we could also have used the relation between IRX and SFR. However, this relation is more difficult to measure in an unbiased and consistent way, because SFR estimates require, at least, UV flux measurements, and corrections for dust attenuation. The trends observed on samples detected in both UV and IR are less clear and have a large scatter (e.g. Buat et al. 2012). In this paper, we show that an IRX–M relation based on the stacking analysis of Heinis et al. (2014), after addition of a dispersion, is capable of reproducing the statistical properties of UV galaxies.

In Section 2, we describe the construction of our empirical model. In Section 3, we present our predictions for UV and IR luminosity function evolution and compare these with observations. In Section 4, we use our model to interpret key IR properties of UV-selected populations. In Section 5, we present additional predictions of our model and discuss the UV-detectability of ALMA sources. We conclude in Section 6.

In this paper, we assume a WMAP-7-year cosmology (Larson et al. 2010) and a Salpeter (1955) initial mass function (IMF), converting from a Chabrier (2003) IMF where necessary.

## 2 Model Description

Our model is based on empirical relations derived from recent observational studies. We use the following steps to derive the evolution of the statistical UV and IR properties of galaxies with cosmic time:

(i) Our analysis is based on the observed mass functions of Ilbert et al. (2013) which allow us to fix the number of galaxies with a certain stellar mass in a given cosmological volume (Section 2.1);

(ii) We then assume an SFR–M relation and a scatter around it following Sargent et al. (2012) to stochastically assign an SFR to each galaxy (Section 2.2);

(iii) Finally, we apply the observed IRX–M relation of Heinis et al. (2014) to predict the relative fraction of UV light that escapes star-forming galaxies and that is reprocessed by dust, respectively (Section 2.3);

(iv) Additional refinements to the model, e.g. the special treatment of the dust attenuation in SBs and the evolution of the IRX–M relation at \( z < 1 \), are described in Section 2.4.

### 2.1 Mass function

As our starting point we use the mass functions of star-forming galaxies at different redshifts (\( 0 < z < 4 \)) to predict their expected number per comoving volume in various mass and redshift bins. Our analysis thus neglects the passive galaxy population. The version of the 2SFM model used by previous analyses was based on the evolving mass functions of Ilbert et al. (2010) which cover the redshift range of \( z \lesssim 2 \). These have now been extended to \( z \sim 4 \) by Ilbert et al. (2013). As such we use the full range of mass functions of this latter study, i.e. \( 0.2 < z < 4 \). As well as extending to higher redshifts, Ilbert et al. (2013) also found steeper low-mass tails at all redshifts, implying greater numbers of low-mass galaxies per comoving volume. The parametric form of this mass function, as presented in Ilbert et al. (2013) and implemented in this model version, is given by

\[
\phi(M) \, d\log(M) = \exp \left( -\frac{M}{M^*} \right) \left[ \phi_1^* \left( \frac{M}{M^*} \right)^{\alpha_1} + \phi_2^* \left( \frac{M}{M^*} \right)^{\alpha_2} \right] \times \left( \frac{M}{M^*} \right) \log(10) \, d\log(M),
\]

where the values for \( M^* \) (i.e. the location of the knee of the stellar mass function), \( \phi_1^* \), \( \phi_2^* \), \( \alpha_1 \) and \( \alpha_2 \) are given in table 2 of Ilbert et al. (2013) for each redshift slice. Above \( z = 1.5 \), \( \phi_2^* \) is fixed to 0, thus, equation (1) becomes a simple Schechter function with parameters \( \phi^* \) and \( \alpha \). For redshifts lower than 0.2, the evolution of the Ilbert et al. (2013) mass-function parameters is extrapolated from the higher redshift values. We note that our extrapolation is consistent with Baldry et al. (2012) at \( z = 0.06 \) (i.e. the highest redshift of that study). Finally, we note that the redshift bins of Ilbert et al. (2013) are typically too broad for use in our model, leading to discontinuities in the galaxy redshift distributions and over- or underestimates of source counts at the extremes of each redshift bins. To avoid this, we linearly interpolate their bins on to a finer redshift grid with logarithmic spacing \( \Delta \log(z) = 0.05 \). The evolution of the mass function of star-forming galaxies used in our analysis is shown in Fig. 1 (upper panel).
2.2 Link between stellar mass and SFR

To derive the specific SFR ($sSFR = SFR/M$) for the galaxy population described by our chosen mass functions (see above) we use the same parametric representation of the MS as Béthermin et al. (2012):

$$sSFR_{MS}(M, z) = sSFR_{MS,0} \left( \frac{M}{10^{11} M_\odot} \right)^{\beta_{MS}} (1 + \min(z, z_{evo}))^{\gamma_{MS}},$$

where $sSFR_{MS}$ is the SFR of a $10^{11} M_\odot$ galaxy lying exactly at the centre of the MS, $\log(sSFR_{MS,0}) = -10.2$ yr$^{-1}$, $\beta_{MS} = -0.2$, $z_{evo} = 2.5$ and $\gamma_{MS} = 3$. These values are based on observational calibrations as discussed in Sargent et al. (2012) and Béthermin et al. (2012). The chosen scenario for the SFR–$M$ relation, described by equation (2), i.e. a rising power law, following by a plateau beyond $z = 2.5$, is illustrated in Fig. 1 (central panel). Recent studies (e.g. de Barros, Schaerer & Stark 2014) suggest that, once the impact of nebular emission lines on the near-IR photometry (which leads to an overestimate of the stellar mass) is correctly taken into account, sSFRs continue to increase beyond $z = 2.5$. However, the mass functions of Ilbert et al. (2013), the observational calibration of the sSFR evolution and the measurements of the IRX–$M$ relation have all been computed neglecting this phenomenon. Since SFRs and IRXs are observed properties, updating the masses has a proportional impact on these relationships, which cancels when we assume these updated masses in our analysis. As such, correcting for nebular emission has no impact on the derived UV and IR galaxy properties.

To describe the dispersion around this relation, we used the probability distribution of Sargent et al. (2012) which incorporates both MS and SB galaxies and is based on the empirical results of Rodighiero et al. (2011). The result of Sargent et al. (2012) was based on a sample of $z \sim 2$ star-forming galaxies with $M > 10^{10} M_\odot$, and is parametrized as a double log-normal law decomposed into MS and SB components:

$$p(\log(sSFR)) \propto \exp\left(-\frac{(\log(sSFR) - \log(sSFR_{MS}))^2}{2\sigma_{MS}^2}\right) + r_{SB} \exp\left(-\frac{(\log(sSFR) - \log(sSFR_{MS}) - B_{SB})^2}{2\sigma_{SB}^2}\right),$$

where $\sigma_{MS}$ and $\sigma_{SB}$ are the standard deviations of MS and SB log-normal distributions respectively, $sSFR_{MS}$ is the central SFR value for MS galaxies at $z \sim 2$, $r_{SB}$ is the relative amplitude between SB and MS galaxies and $B_{SB}$ (interpreted as the average sSFR ‘boost’ for SB galaxies in Sargent et al. 2012) is the ratio between the sSFR loci of SB and MS galaxies. This is illustrated by Fig. 1 (lower panel).

As our model incorporates galaxies spanning a wide range of masses and redshifts, we must modify the probability distribution of Sargent et al. (2012) to take this into account. For this, we adopt the same assumptions as adopted by Béthermin et al. (2012) to reproduce IR number counts. To summarize:

(i) $\sigma_{MS} = 0.15$ dex, $\sigma_{SB} = 0.2$ dex and $B_{SB} = 0.6$ are kept constant throughout$^1$ (i.e. unchanging with respect to either mass

$^1$ Following Béthermin et al. (2012), the measured values of $\sigma_{MS}$ and $\sigma_{SB}$ are corrected for artificial broadening effects, already noted in Rodighiero et al. (2011), namely (a) cosmological evolution within finite redshift bins, and (b) instrumental noise. $\sigma_{SB}$ is slightly larger than $\sigma_{MS}$ because of the scatter about the mean sSFR-boost observed for SB (see discussion in Sargent et al. 2013).
or redshift) for simplicity. Furthermore, Sargent et al. (2012) found no evidence for evolution of these parameters;

(ii) sSFRMS evolves with redshift and mass as described previously (equation 2);

(iii) Following Béthermin et al. (2012), and consistent with the indications for somewhat lower SB contribution at $z = 0$ found in Sargent et al. (2012), we set $r_{SB} \propto (1 + z)$ at $z < 1$, followed by a constant, $r_{SB} = 0.024$ (Hopkins et al. 2010; Sargent et al. 2012) at higher redshifts (equation 3 in Béthermin et al. 2012).

2.3 Relation between stellar mass and dust attenuation

Dust-enshrouded star-forming regions absorb UV light emitted by young stars and emit it as IR radiation. As such, the relation between dust attenuation and stellar mass, hereafter called ‘attenuation relation’, can be used to compute the ratio between the IR and UV luminosity for our star-forming galaxies, as shown in several studies (e.g. Pannella et al. 2009, Heinis et al. 2014; Pannella et al. in preparation). We used the following parametric form for the IRX–$M$ relation:

$$\text{IRX} = \log\left(\frac{L_{\text{IR}}}{L_{\text{UV}}}\right) = \alpha \left(\log\left(\frac{M}{M_\odot}\right) - 10.35\right) + \text{IRX}_0,$$

where $\alpha = 0.71 \pm 0.21$ and $\text{IRX}_0 = 1.32 \pm 0.11$ following Heinis et al. (2014), who do not see any evolution of this relation between $z = 1.5$ and $z = 4$. This relation was measured only for galaxies with $M > 10^{10.5} M_\odot$ while we here extrapolate it also to lower masses and beyond this redshift range. Heinis et al. (2014) base their work on UV-detected populations but their findings are similar to new results obtained by Pannella et al. (in preparation) with a purely mass-selected sample of star-forming galaxies.

From the SFR, we then derive the UV and IR luminosity emitted by the galaxy, assuming an energy balance between the SFR probed by unattenuated UV light and reprocessed IR, i.e. $SFR = SFR_{\text{IR}} + SFR_{\text{UV}}$. The link between SFR and, IR or UV, luminosities is computed following Kennicutt (1998): $SFR_{\text{IR}} = K_{\text{IR}} \times L_{\text{IR}}$ with $K_{\text{IR}} = 1.7 \times 10^{-10} M_\odot \, \text{yr}^{-1} \, L_\odot^{-1}$ and $SFR_{\text{UV}} = K_{\text{UV}} \times L_{\text{UV}}$ with $K_{\text{UV}} = 2.8 \times 10^{-10} M_\odot \, \text{yr}^{-1} \, L_\odot^{-1}$. The IR luminosity is the total bolometric emission of the galaxy from 5 to 1000 $\mu$m rest frame and the UV luminosity is the monochromatic luminosity at 150 nm rest-frame. Combining these three equations and the IRX–$M$ relation, we obtain

$$L_{\text{IR}} = \frac{\text{SFR}}{K_{\text{UV}}} \frac{10^{\text{IR}}}{1 + \frac{K_{\text{IR}}}{K_{\text{UV}}} 10^{\text{IRX}}} \quad \text{and} \quad L_{\text{UV}} = \frac{\text{SFR}}{K_{\text{UV}}} \frac{1}{1 + \frac{K_{\text{UV}}}{K_{\text{IR}}} 10^{\text{IRX}}}.$$

2.4 Refinements

The attenuation relation used in our model (Heinis et al. 2014) is derived from a stacking analysis and hence provides no information on the dispersion around this mean relation. This kind of measure is difficult to perform and could be strongly biased by selection effects. Buat et al. (2012) studied the IR emission of a sample of UV-selected galaxies at $z \sim 1.5$ and found a mean relation between IRX and $M$ that is fully consistent with the one of Heinis et al. (2014) which we adopt for our predictions. Buat et al. (2012) measure the observed scatter around the mean relation to be 0.30 dex. This value must be considered a lower limit in view of the incompleteness of their sample, in which galaxies have to be detected both in the UV and IR. A value of 0.3 dex is also representative of the dispersion found on IRX at redshifts from 0 to 2 for a given UV luminosity (Heinis et al. 2014 and references therein). Pannella et al. (in preparation) estimated a dispersion of 0.4 dex using the Herschel detections up to $z = 1.3$ in the deepest regions of the H-GOODS survey. Wyuts et al. (2012) report that the dispersion of the attenuation relation is independent of stellar mass. We will thus assume a constant log-normal scatter of 0.4 dex (1 mag) versus $M$ for simplicity.

Takeuchi et al. (2005) have found that the ratio between the IR and the UV luminosity density increases by a factor of $\sim 3$ ($\sim 0.5$ dex) from redshift 0 to 1. The evolution of this integrated property cannot be reproduced by the simplest version of our model because of the adopted non-evolution of the IRX–$M$ relation and the weak evolution of the mass function of star-forming galaxies (Ilbert et al. 2013; Muzzin et al. 2013) below $z = 1$. To solve this problem, we thus assume a slightly evolving normalization of the IRX–$M$ relation:

$$\text{IRX}_0 = \text{IRX}_0 - 0.5 \times (1 - z) \quad \text{at} \quad z < 1.$$

We could have also assumed an evolution of the slope of the relation, but we chose to use an evolving normalization for simplicity. Indeed, Buat (2013) found lower attenuations at fixed mass in the local Universe. In a similar way, Pannella et al. (in preparation) found also a lower normalization of the IRX–$M$ relation in their $z = 0.5$–1 bin than at $z > 1$. This evolution of IRX at fixed mass can be also connected with the evolution of the average ratio between dust and stellar mass (Béthermin et al., in preparation; Tan et al., in preparation), and the increase of disc-opacity observed by Sargent et al. (2010), below $z = 1$. This modification of the individual properties of galaxies correctly reproduced that evolution of $L_{\text{D28}}/L_{\text{D28}}$ at low redshift. We explicitly show how much this modification impacts the predictions of the model in Section 3.3. While Heinis et al. (2014) find the attenuation relation to remain constant at high redshift, Cucciati et al. (2012) and Burgarella et al. (2013) report a decreasing integrated $L_{\text{D28}}/L_{\text{D28}}$ at $z > 2$. These two observations do not contradict each other as the higher mean transparency of the Universe at high redshift is naturally recovered by our model because of the decrease of $M^*$ at high redshift (Ilbert et al. 2013; Muzzin et al. 2013). The star formation budget at very high redshift is thus dominated by lower mass galaxies and the average attenuation is accordingly lower.

In the simplest implementation of our model SB galaxies are much less attenuated than MS galaxies with a similar SFR because of their lower mass. This disagrees with the observational results of e.g. Wuyts et al. (2011). We hence adopt another prescription whereby SB activity is taken to be fully dust obscured. Specifically, we assume that star formation in SB galaxies is split between two processes such that $SFR = SFR_{\text{MS}} + SFR_{\text{SB}}$: extended star formation – subject to the same mass-dependent attenuation (see equation 4) as normal MS galaxies – and one or several compact SB regions, probably induced by major mergers, which are heavily dust enshrouded and consequently emit only in the IR. We showed in Sargent et al. (2013) that it is possible to statistically establish by how much the activity of starbursting galaxies of a given sSFR-excess has been boosted with respect to their pre-burst state on the star-forming MS. For the present analysis, we use these sSFR-dependent boost-distributions (see Sargent et al. 2013, section 4.2.3) to compute the relative importance of the two star-formation modes for a given SB galaxy. The surplus SFR activity, $SFR_{\text{SB}}$ (i.e. the difference between the SFR in the SB state and the SFR prior to the onset of the burst phase), is assumed to be fully dust obscured, while the remainder, $SFR_{\text{MS}}$, is identified with the only partially obscured, extended component of the star-formation activity in the SB galaxy.
3 UV AND IR LUMINOSITY FUNCTIONS

3.1 Computation of the luminosity function and uncertainties

The computation of the IR and UV luminosity functions is difficult to perform analytically, because our model uses several scaling laws including a dispersion around them. We thus use the simpler method of constructing mock catalogues that we generate following the prescriptions detailed in Section 2. Luminosity functions are then derived by counting the number of galaxies in each redshift slice and luminosity bin, and dividing it by the volume of the redshift slice and the size (in dex) of the luminosity bin.

The mock catalogues are generated as follows.

(i) We generate a mock catalogue containing only $M$ and $z$ based on the mass function described in Section 2.1 (equation 1). In practice, we use a 2 deg$^2$ field, to reach a compromise between sufficient statistics and computation time, and split it by redshift slices of $\Delta \log (1+z) = 0.05$. Mock galaxies are then generated based on the mass function at the centre of each slice. Redshifts are drawn in the slice assuming a flat distribution. The number of objects predicted by the mass function diverges at low mass. Consequently, we apply a mass cut of $10^6 M_\odot$. We have checked that this low mass cut has no impact on the luminosity functions in the regime where data points are available.

(ii) We assign an (s)SFR for each mock galaxy based on the prescriptions of the 2SFM model described in Section 2.2. To do this, we first compute $s\text{SFR}_{\text{MS}}$ from the $M$ and $z$ of each object using equation (2). We then compute the SB fraction ($f_{\text{SB}}(z)$) given by the ratio between the integration of the SB probability distribution (i.e. second part of equation 3) and the sum of the whole probability distribution. Following $f_{\text{SB}}(z)$, we can now draw a type (i.e. MS or SB). Then, we draw an sSFR for MS type along a Gaussian centred on $s\text{SFR}_{\text{MS}}$ and with a $\sigma_{\text{MS}}$ standard deviation; and for SB type along another Gaussian centred on $s\text{SFR}_{\text{SB}} = s\text{SFR}_{\text{MS}} + B_{\text{SB}}$ and with a $\sigma_{\text{SB}}$ standard deviation.

(iii) We decompose the SFR in an UV and IR component. For each MS galaxy, we compute the expected IRX from $M$ with equation (4) and draw its actual IRX assuming a scatter of 0.4 dex ($1\,\text{mag}$). We then compute the $L_{\text{UV}}$ and $L_{\text{IR}}$ using equation (5). For each SB object, we decompose the SFR into an MS and an SB component based on the boost-function formalism of Sargent et al. (2013). The MS component is treated as previously explained. The IR luminosity emitted by the SB component is assumed to be fully obscured, such that $L_{\text{IR,SB}} = s\text{SFR}_{\text{SB}}/K_{\text{IR}}$.

We generated several mock catalogues. Our best model follows all the prescriptions listed in Section 2, including the refinements described in Section 2.4. We also generated a mock catalogue without scatter on the IRX–$M$ relation and another one without low-redshift modification of this relation. To derive confidence region for the best model, we generated 50 Monte Carlo mock catalogues using parameter values drawn randomly in their error region as summarized in Table 1.

### Table 1. Central values and uncertainties on the parameters used in our model. These values come from previous works of Béthermin et al. (2012), Sargent et al. (2012), Heinis et al. (2014) and Ilbert et al. (2013).

| Parameter | Description | Value ± Error |
|-----------|-------------|---------------|
| $s\text{SFR}_{\text{MS},0}$ | sSFR on the MS at $z = 0$ and $M = 10^{11} M_\odot$ ($\text{in log(yr}^{-1})$) | $-10.2 \pm 0.1$ |
| $\beta_{\text{MS}}$ | Slope of the sSFR–$M^*$ relation at a given redshift | $-0.2 \pm 0.04$ |
| $\gamma_{\text{MS}}$ | Evolution of the normalization of the MS with redshift | $3 \pm 0.2$ |
| $\sigma_{\text{MS}}$ | Width of the MS log-normal distribution (in dex) | $0.15 \pm 0.003$ |
| $r_{\text{SB}0}$ | Relative amplitude of SB log-normal distribution compared to MS | $0.012 \pm 0.003$ |
| $\sigma_{\text{SB}}$ | Width of the SB log-normal distribution (in dex) | $0.20 \pm 0.07$ |
| $B_{\text{SB}}$ | Boost of sSFR in SB (in dex) | $0.6 \pm 0.07$ |
| $\omega$ | Attenuation relation IRX = $\alpha \log M + \text{IRX}_0$ (Heinis et al. 2014) | $0.71 \pm 0.21$ |
| $\text{IRX}_0$ | Normalization of the IRX–$M^*$ relation | $1.32 \pm 0.11$ dex |

All parameters and errors required to evaluate equation 1 are listed in table 2 of Ilbert et al. (2013), converted to a Salpeter IMF.
3.3 Comparison with observed UV luminosity functions at $z < 4$

In Fig. 3, we compare our model predictions with the UV luminosity functions measured by various authors (Steidel et al. 1999; Arnouts et al. 2005; Wyder et al. 2005; Bouwens et al. 2007; Reddy et al. 2008; Hathi et al. 2010; Oesch et al. 2010; Cucciati et al. 2012). We used the same redshift bins as Cucciati et al. (2012), who cover the largest redshift range with their study. There is good overall agreement between the confidence region of the model (grey area) and the data points. This shows how efficient our approach is in spite of involving very few scaling laws. We do find that our model is systematically higher than the Cucciati et al. (2012) points at the faint-end between $z = 0.4$ and $z = 0.8$, but this offset is always within the confidence region of the model. This could be caused by a problem of incompleteness in the faintest magnitude bins of the literature studies. Our model is also $2\sigma$ higher than Oesch et al. (2010) measurements at $L_{UV} > 10^{10} L_\odot$ in the range $1.7 < z < 2.5$, but agrees with the other authors in this regime.

We switched off the modification of the IRX–$M$ relation at low redshift to quantify its impact. The yellow dashed lines represent the prediction of the model with a non-evolving relation. Between $z = 0.6$ and $z = 1$, there is only a mild impact, since the offset from the constant IRX–$M$ relation at higher redshift is small. At lower redshift, the model without low-$z$ evolution systematically underestimates the bright end; the faint end is not affected by changes to the IRX–$M$ relation. Our model thus favours a scenario with a minor
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Figure 3. UV luminosity function from $z \sim 0$ to $z \sim 4$. Black solid lines represent the UV luminosity function derived from our best model. Red dotted lines represent the same model, but without scatter on the attenuation relation. Yellow dashed lines represent the best model, but without evolution of the IRX–$M$ relation at low redshift. Grey areas represent the one sigma confidence region of our best model. Coloured points are measurements from various observational studies (Steidel et al. 1999; Arnouts et al. 2005; Wyder et al. 2005; Bouwens et al. 2007; Reddy et al. 2008; Hathi et al. 2010; Oesch et al. 2010; Cucciati et al. 2012)

evolution of the IRX–$M$ relation at low redshift, implying slightly more transparent galaxies at fixed stellar mass in the local Universe.

We also studied the effect of the scatter on the IRX–$M$ relation. The red dotted lines in Fig. 3 show the model predictions in absence of scatter. There are almost no changes below the knee of the UV luminosity function, but the model without scatter underpredicts the number of objects ($\sim 0.5$ dex) above the knee of the luminosity function by an order of magnitude. A scatter is thus mandatory to reproduce the bright end of the UV luminosity function. Indeed, because of the existence of a MS, only intermediate- and high-mass ($\gtrsim M^*$) galaxies can produce a sufficient SFR and thus intrinsic UV luminosity. However, because of the IRX–$M$ relation, the more massive the object is, the higher its attenuation will be. The scatter generates a population of intermediate-mass galaxies with a lower attenuation and thus a bright observed UV luminosity. To test this hypothesis, we selected $L_{UV} > 10^{11} L_\odot$ galaxies at $1.7 < z < 2.5$ in the catalogue based on our best model (with a scatter of 0.4 dex) and compute their median mass and IRX. We found $6 \times 10^{10} M_\odot$ and 0.81, respectively. The median IRX at this mass is 1.62. UV bright populations are thus $M^*$ galaxies, which are negative outliers of the attenuation relation. Finally, we tested various values for the scatter on the attenuation relation and found that the UV luminosity function is well reproduced only for scatters in the 0.2–0.5 dex interval, in agreement with the observational estimates cited in Section 2.4.
3.4 Comparison with UV luminosity function of high-redshift LBGs

We extended our model to $z > 4$ as a first-order test of whether the simple ingredients we assumed at lower redshift are sufficient for reproducing high-redshift measurements as well. Unfortunately, we currently have no access to IR data at these redshifts, but UV luminosity functions were measured using the Lyman-break-selection technique (Steidel et al. 1996). However, our parametric mass function based on Ilbert et al. (2013) was calibrated only up to $z = 4$. We thus used the fit of a compilation of mass function measurements coming from $K$-band-selected and Lyman break galaxies (LBG)-selected populations performed by Sargent et al. (in preparation). Basic features of this compilation are a successive steepening of the faint-end slope, a quickly declining characteristic density, and a decreasing $M^*$ with redshift. We assume no evolution of the sSFR–$M$ and IRX–$M$ relation beyond a redshift of 4 for the sake of simplicity.

Fig. 4 shows the comparison between our model (black solid line) and the data of Bouwens et al. (2007) and Steidel et al. (1999) at $z \sim 5$ and 6. All the data points lie in the confidence area of our empirical predictions (grey area). This demonstrates the predictive power of our method and suggests that a non-evolving IRX–$M$ and SFR–$M$ relation at high- $z$ is a fair hypothesis to interpret the current data. In a similar way as at lower redshifts, it is clear that a scatter on the attenuation relation is necessary to reproduce the bright-end of the UV luminosity functions at $z \sim 5$ and 6.

4 IR PROPERTIES OF UV SELECTED POPULATION

The IR properties of UV-selected population are not expected to be similar to those of the full population. Our model is a useful tool to understand how this selection biases the obtained results. We now discuss recent observational results obtained on these UV-selected populations, and how they can be interpreted by our model.

4.1 Mean attenuation in UV-selected galaxies

Heinis et al. (2013) studied the mean IRX of UV-selected populations, measured with a stacking analysis as a function of $L_{UV}$ at $z \sim 1.5$. The results are compatible with a plateau at $10^{6.9} \pm 1.0$ between $10^{9.5}$ and $10^{11} L_\odot$ (see Fig. 5). The flat trend come from the mix of low- and high-mass galaxies in each UV bin, but is not trivial to understand, because of the rising IRX–$M$ relation (Heinis et al. 2014). However, our best model also predicts a flat trend in this $L_{UV}$ range (blue solid line on Fig. 5). This result is essentially caused by the scatter on the attenuation relation, since we find a rising trend in the absence of dispersion (red dotted line on Fig. 5). This is another indication for the importance of the scatter in order to be able to model simultaneously the statistical properties UV and IR populations. At fixed UV luminosity, there is thus a mix between galaxies with higher SFR (mass) and attenuation and others with lower SFR (mass) and attenuation. This picture is consistent with the distribution in the IRX–$M$ diagram of populations selected by UV luminosity recovered from the simulation of (Heinis et al. 2014). Nevertheless, there is a 2$\sigma$ systematic discrepancy around $10^{10} L_\odot$. We tried to modify the scatter and the IRX–$M$ relation...
to reproduce this feature without success. This could be caused by cosmic variance, but also a clue of an higher complexity of real galaxy populations. Finally, our model predicts a rising relation with \( L_{\text{UV}} \) at \( L_{\text{UV}} < 10^{5.5} L_{\odot} \), in contrast with Heinis et al. (2013) who have found clues of a decreasing trend for their three faintest points. Measurements at lower UV luminosity will thus be a challenging test for our model.

4.2 Absence of strongly-attenuated, UV-bright galaxies

The results of Heinis et al. (2013) were obtained in a stacking analysis and do not provide any information about the dispersion around the IRX–\( L_{\text{UV}} \) relation. Buat et al. (2012) have studied the distribution of IR- and UV-detected population between \( z = 0.95 \) and \( z = 2.2 \) in the same diagram. This type of analysis could be biased by the need of a double detection. However, we note that they found no objects with \( \log(L_{\text{UV}}) \geq 10.7 L_{\odot} \) and \( \chi > 1.6 \) (hatched region in Fig. 5) in a 0.028 deg\(^2\) field, where all galaxies should be detected in both UV and IR. Whereas, on average, SB galaxies represent only 3 per cent of the entire population, they contribute 55 per cent in this particular area of the IRX–\( L_{\text{UV}} \) diagram. We will thus use this constraint on the IRX–\( L_{\text{UV}} \) diagram to test the impact of our model prescription for attenuation in SBs (see Section 2.4). When applying the same attenuation for MS and SB galaxies, we count 1.72 objects (\( P[N = 0] = 0.17 \)) in the empty region of the IRX–\( L_{\text{UV}} \) plane. If we assume that sSFR\(_{\text{SB}}\) is completely reprocessed into IR we count 0.99 objects (\( P[N = 0] = 0.37 \)) in the same region. Therefore, observations slightly favour our refined recipe for attenuation in SB. Nevertheless, studies on larger fields are necessary to conclusively test the validity of our assumptions in this regime.

5 PREDICTIONS

All predictions presented in this section are based on our ‘full’ model, i.e. the realization with a scatter on IRX–\( M \) relation, a special treatment of the SBs, and an evolution of the IRX–\( M \) relation below \( z = 1 \).

5.1 Contribution of IR-selected populations to the UV luminosity function

We used our model to predict how much IR galaxies above various luminosity cuts contribute to the UV luminosity function (see Fig. 6 left-hand panel). At all redshifts, we note that the bright-end of the UV luminosity function is predominantly populated by IR-bright galaxies. This is expected, because UV-bright galaxies are essentially \( M^* \) galaxies with a median IRX of 0.81 (see Section 3.3). These objects thus mainly emit in the IR. The sub-\( L^* \) regime is populated by IR-faint sources, and ultradep IR observations are necessary to recover a significant fraction of these objects in the IR. This part of the UV luminosity function is dominated by low-mass galaxies, which have correspondingly low attenuations and low SFRs, and so, low IR luminosities. We also note in the left-hand side of Fig. 6 that the UV luminosity distribution of IR-selected sources peaks around the knee of the UV luminosity function for a large range of IR-luminosity cuts (\( 10^{10} \)–\( 10^{13} L_{\odot} \)). The mean UV luminosity of IR-selected population thus slowly evolves as a function of \( L_{\text{IR}} \) (1 dex in UV for 2.5 dex in IR). Indeed, the brighter \( L_{\text{IR}} \) is, the more massive and attenuated the galaxy will be. Consequently, a strong increase of \( L_{\text{IR}} \) involves only a weak one of \( L_{\text{UV}} \), because the highest SFR is partially compensated by a higher attenuation.

5.2 Contribution of UV-selected populations to the IR luminosity function

We then studied the contribution of UV-selected galaxies to the IR luminosity function (see Fig. 6 right-hand panel). We found that the brightest IR galaxies (>\( 10 L_{\odot} \)) are not the brightest UV galaxies, contrary to what was found for the opposite case in Section 5.1. SB galaxies dominate this regime and are very attenuated (see Section 2.4). Consequently, they tend to be missed by shallow UV surveys. In contrast, the sub-\( L^* \) galaxies are well recovered by UV surveys, because they are in general less attenuated. We also note that the \( L_{\text{IR}} \) distribution of galaxies above a given \( L_{\text{UV}} \) is much broader than in the opposite case. IR-selected populations have thus more homogeneous \( L_{\text{UV}} \) than \( L_{\text{IR}} \) of UV-selected populations. Overall, UV selections are better suited to study low-mass, low-SFR populations, because of their low attenuation. But, IR selections are better suited to study massive, strongly-star-forming galaxies, which tend to be missed by UV surveys because of their strong attenuation. Our model thus confirms the complementarity of UV and IR data, and confirms the commonly accepted fact that UV is better to probe low SFR and IR is better to probe the high SFR.

5.3 Will the sources of millimetre deep surveys be detected in UV?

In the following years, ALMA, NIKA on PdBI and CCAT will perform deep IR continuum surveys around a wavelength of 1 mm. Detecting the UV rest-frame counterpart of such sources will be useful to constrain the dust attenuation of these distant objects, and better understand the stellar, gas and dust content of such objects. Our model enables us to estimate the typical depth of rest-frame UV surveys requested to match the sensitivity of future millimetre surveys. Fig. 7 shows the fraction of UV-detected sources as a function of the depth of the survey in the millimetre domain and in UV-rest-frame. To simplify the reading of this plot, we defined \( m_{\text{UV}} \) as the apparent magnitude of a source at \( 150 \times (1 + z) \) nm. This corresponds to FUV, \( U, R, I \) and \( J \) band for sources at \( z = 0 \), \( z = 1 \), \( z = 2.65 \), \( z = 4.35 \) and \( z = 7.15 \), respectively. The fluxes in the millimetre band at 850 \( \mu \)m and 1.3 mm are computed using the IR SED templates of Magdis et al. (2012). This library provides two distinct templates for MS galaxies, and SBs that depend only on redshift (but not on, e.g. luminosity once the redshift is fixed). Following Béthermin et al. (2012), we assume a scatter of 0.2 dex on the parameter \( (U) \), which represents the mean intensity of the radiation field and which correlates with dust temperature. Using this SED library, galaxy number counts (including counts split in different redshift bins) from the mid-IR to millimetre wavelengths are correctly reproduced with the 2SFM formalism (Béthermin et al. 2012).

The typical depth of surveys performed at the confusion limit with the next generation of millimetre cameras on thirty-metre class telescopes (NIKA2 at IRAM, LMT, CCAT) will be \( \sim 0.5 \) mJy (Béthermin et al. 2011). These telescopes will be able to cover fields of 0.1–10 deg\(^2\) at this sensitivity. An optical depth of \( m_{\text{UV, rest}} \sim 26.5 \) (COSMOS; Capak et al. 2007)\(^2\) will thus provide the UV luminosity.

\(^2\)The depth of the GALEX imaging in COSMOS, i.e. of the observer-frame UV-coverage of COSMOS is shallower than quoted here. We use \( m_{\text{UV, rest}} \) to denote the apparent magnitude at the wavelength which samples the rest-frame UV-emission of galaxies at different redshifts. The bulk of the sources we consider here are at \( z > 1 \) and thus have rest-frame UV emission that falls into observed optical bands, for which the sensitivity is around 26.5 mag.
luminosity to >80 per cent up to z ∼ 2.5. At z > 5, a depth of 29 mag will be necessary. This depth is nowadays reached in field of only few arcmin². The new generation of millimetre interferometers (ALMA and NOEMA) will be able to probe fluxes one order of magnitude fainter in fields of few arcmin² or less. In this case, a typical magnitude of 29, which is already reached in HUDF (Coe et al. 2006), will allow us to detect the >80 per cent of UV counterparts at z < 5. At larger redshift, a depth of ∼30 will be necessary. This should be possible with the James Webb Space Telescope.

6 CONCLUSION

We modelled the evolution of the UV and IR emissions of galaxies across cosmic times based on the 2SFM formalism, built from the empirically measured evolution of the MS of star-forming galaxies, and the observed IRX–M relation assuming a 0.4 dex scatter around it. This modelling work allows us to better understand the connection between the IR-selected and UV-selected populations. Our main findings are as follows.
Figure 7. AB apparent magnitude at $(1+z) \times 150$ nm at which a given fraction of galaxies (colour coded) are detected as a function of their (sub-)millimetre flux. Left-hand panels correspond to fluxes at 850 µm and right-hand panels to fluxes at 1300 µm. Various redshift slices are presented, from the lowest on the top panels, to the highest on the bottom panels.

(i) Our model is able to consistently predict the co-evolution of the IR luminosity function up to $z \sim 3$ and the UV luminosity function up to $z \sim 6$.

(ii) We showed that scatter on the IRX–$M$ relation has no effects on the IR luminosity function. This is not the case for the UV, where a scatter of $\sim 0.4$ dex is necessary to reproduce the UV luminosity function. This is caused by the fact that the UV bright galaxies are not the most massive or the most star forming, but $M^*$ galaxies, which are negative outliers of the attenuation relation.

(iii) We recover naturally a flat mean IRX–$L_{\text{UV}}$ relation measured by stacking in Herschel data of UV-selected sources as a consequence of the scatter on the IRX–$M$ relation, the shape of the mass function and the SFR–$M$ relation.

(iv) We performed predictions from our model and showed that IR-selected populations have similar $L_{\text{UV}}$ around the knee of the UV luminosity function, while UV-selected populations can have very different IR properties. Overall, the IR-selection is very efficient for selecting massive and/or strongly-star-forming galaxies, but UV is much better suited for studying the low-mass, weakly-star-forming galaxies.

This simple model will be useful to understand the selection bias of various studies of star formation in distant galaxies, and especially the IR-selected sample from the next generation of deep interferometer surveys or large single-dish surveys.
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REFERENCES

Arnouts S. et al., 2005, ApJ, 619, L43
Baldry I. K. et al., 2012, MNRAS, 421, 621
Béthermin M., Dole H., Lagache G., Le Borgne D., Penin A., 2011, A&A, 529, A4
Béthermin M. et al., 2012, ApJ, 757, L23
Béthermin M., Wang L., Doré O., Lagache G., Sargent M., Daddi E., Cousin M., Aussel H., 2013, A&A, 557, A66
Bouwens R. J., Illingworth G. D., Franx M., Ford H., 2007, ApJ, 670, 928
Buat V., 2013, Earth Planets Space, 65, 1095
Buat V. et al., 2005, ApJ, 619, L51
Buat V. et al., 2012, A&A, 545, A141
Burgarella D. et al., 2013, A&A, 554, A70
Capak P. et al., 2007, ApJS, 172, 99
Casey C. M. et al., 2012, ApJ, 761, 140
Chabrier G., 2003, PASP, 115, 763
Coe D., Benitez N., Sánchez S. F., Jee M., Bouwens R., Ford H., 2006, AJ, 132, 926
Cucciati O. et al., 2012, A&A, 548, A108
Daddi E. et al., 2007, ApJ, 670, 156
Daddi E. et al., 2010, ApJ, 714, L118
de Barros S., Schaerer D., Stark D. P., 2014, A&A, 563, A81
Dole H. et al., 2004, ApJS, 154, 87
Elbaz D. et al., 2007, A&A, 468, 33
Elbaz D. et al., 2011, A&A, 533, A119
Genzel R. et al., 2010, MNRAS, 407, 2091
Gruppioni C. et al., 2013, MNRAS, 432, 23
Hathi N. P. et al., 2010, ApJ, 720, 1708
Heinis S. et al., 2013, MNRAS, 429, 1113
Heinis S. et al., 2014, MNRAS, 437, 1268
Hopkins P. F., Younger J. D., Hayward C. C., Narayanan D., Hernquist L., 2010, MNRAS, 402, 1693
Ilbert O. et al., 2010, ApJ, 709, 644
Ilbert O. et al., 2013, A&A, 556, A55
Kennicutt R. C., Jr, 1998, ApJ, 498, 541
Larson D. et al., 2011, ApJS, 192, 16
Le Floc’h E. et al., 2005, ApJ, 632, 169
Magdis G. E. et al., 2012, ApJ, 760, 6
Magnelli B., Elbaz D., Chary R. R., Dickinson M., Le Borgne D., Frayer D. T., Willmer C. N. A., 2009, A&A, 496, 57
Magnelli B., Elbaz D., Chary R. R., Dickinson M., Le Borgne D., Frayer D. T., Willmer C. N. A., 2011, A&A, 528, A35
Meurer G. R., Heckman T. M., Calzetti D., 1999, ApJ, 521, 64
Muzzin A. et al., 2013, ApJ, 777, 18
Noeske K. G. et al., 2007, ApJ, 660, L43
Nguyen H. T. et al., 2010, A&A, 518, L5
Oesch P. A. et al., 2010, ApJ, 725, L150
Overzier R. A. et al., 2011, ApJ, 726, L7
Pannella M. et al., 2009, ApJ, 698, L116
Reddy N. A., Steidel C. C., Pettini M., Adelberger K. L., Shapley A. E., Erb D. K., Dickinson M., 2008, ApJS, 175, 48
Reddy N. A., Erb D. K., Pettini M., Steidel C. C., Shapley A. E., 2010, ApJ, 712, 1070
Rodighiero G. et al., 2010, A&A, 515, A8
Rodighiero G. et al., 2011, ApJ, 739, L40
Salpeter E. E., 1955, ApJ, 121, 161
Sanders D. B., 2003, J. Korean Astron. Soc., 36, 149
Sargent M. T. et al., 2010, ApJ, 714, L113
Sargent M. T., Béthermin M., Daddi E., Elbaz D., 2012, ApJ, 747, L31
Sargent M. T. et al., 2013, preprint (arXiv:1303.4392)
Steidel C. C., Giavalisco M., Pettini M., Dickinson M., Adelberger K. L., 1996, ApJ, 462, L17
Steidel C. C., Adelberger K. L., Giavalisco M., Dickinson M., Pettini M., 1999, ApJ, 519, 1
Tacconi L. J. et al., 2008, ApJ, 680, 246
Takeuchi T. T., Buat V., Burgarella D., 2005, A&A, 440, L17
Takeuchi T. T., Yuan F.-T., Ikeyama A., Murata K. L., Inoue A. K., 2012, ApJ, 755, 144
Wuyts S. et al., 2011, ApJ, 742, 96
Wuyts E., Rigby J. R., Gladders M. D., Gilbank D. G., Sharif K., Gralla M. B., Bayliss M. B., 2012, ApJ, 745, 86
Wyder T. K. et al., 2005, ApJ, 619, L15

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