Coherent properties of single rare-earth spin qubits

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Rare-earth-doped crystals are excellent hardware for quantum storage of photons. Additional functionality of these materials is added by their waveguiding properties allowing for on-chip photonic networks. However, detection and coherent properties of rare-earth single-spin qubits have not been demonstrated so far. Here we present experimental results on high-fidelity optical initialization, efficient coherent manipulation and optical readout of a single-electron spin of Ce$^{3+}$ ion in a yttrium aluminium garnet crystal. Under dynamic decoupling, spin coherence lifetime reaches $T_2 = 2$ ms and is almost limited by the measured spin-lattice relaxation time $T_1 = 4.5$ ms. Strong hyperfine coupling to aluminium nuclear spins suggests that cerium electron spins can be exploited as an interface between photons and long-lived nuclear spin memory. Combined with high brightness of Ce$^{3+}$ emission and a possibility of creating photonic circuits out of the host material, this makes cerium spins an interesting option for integrated quantum photonics.
The outstandingly long optical coherence times of rare-earth-based crystals result in efficient memories for quantum states of single photons and of entangled photon pairs. Even longer coherence storage times can be achieved in nuclear spin memories. In these quantum memories, the quantum state of a photon is stored in an electron or nuclear spin wave created in an ensemble of spins. This type of memory is suitable for storage at a single photon level and, therefore, is an essential ingredient of quantum repeaters and quantum-computing protocols based on linear optics. However, ensemble-based rare-earth quantum computer designs lack certain functionalities such as error correction that are essential for scalability. This problem can be resolved by addressing single rare-earth spins individually. In the last 2 years, detection of several rare-earth species at a single ion level was demonstrated, although no long-lasting spin coherence for single ions was demonstrated so far. In this Article, we for the first time demonstrate optically addressable rare-earth single-spin qubit in an oxide crystal, namely, cerium ion in yttrium aluminium garnet (YAG), which can be optically initialized, coherently manipulated with microwaves and read out optically.

Results

Optical isolation of a single Ce$^{3+}$ in YAG. Experimentally, individual cerium ions were identified in an ultra-pure YAG crystal using confocal microscopy at $T \approx 3.5$ K (see Methods section and Supplementary Fig. 1). In order to improve the fluorescence collection efficiency of the microscope, a solid immersion lens (SIL) was fabricated on the surface of the sample by focused ion beam (FIB) milling. Cerium ions were excited by a frequency-doubled femtosecond Ti:sapphire laser at 460 nm matching the wavelength of the phonon-assisted absorption band of Ce$^{3+}$ in YAG. Their emission associated with the 5$d$→4$f$ transition was detected in a 475–630-nm spectral window. The image of individual cerium ions under the SIL is shown in Fig. 1b. The single nature of the photon emitter was confirmed with photon antibunching measurements as indicated in Fig. 1c. The detected emission of an individual cerium ion amounts to $60\rightarrow 70 \times 10^3$ photons s$^{-1}$. The emission spectrum of the ions is indicated in Fig. 1d, showing broadband phonon-assisted emission and a sharp zero-phonon line at 489 nm (see Fig. 1e) characteristic for cerium ions. Cerium fluorescent centres can be created in YAG crystal by ion implantation (see Fig. 1f and Methods section for the details on implantation). The yield of fluorescent cerium ions was estimated to be at least 8%. It is believed that the yield can be significantly improved by thermal annealing in a reducing atmosphere.

Initialization of the spin state. The electronic level structure of cerium substitutional impurities in ceramic crystals is shown in Fig. 1a. The strongest transition between the ground 4$f$(1) and the optically excited 5$d$(1) spin doublets under $\sigma^+$ circularly polarized excitation is the spin flip transition $|4f(1)\uparrow\rangle$→$|4d(1)\uparrow\rangle$. The other three transitions are almost three orders of magnitude weaker. However, decay back to the two ground states is equally probable. Repeated excitation results in efficient pumping of the ion into spin-up ‘dark’ state, thereby initializing the cerium spin.

To further reveal the pumping dynamics of the cerium spin, a magnetic field of 490 G parallel to the excitation beam was applied to the sample, the excitation laser was chopped such that the cerium centre is excited with a train of pulses and the time-dependent emission was recorded. A typical optical correlation signal obtained for a single Ce$^{3+}$ centre under pulsed laser excitation is shown in Fig. 1f. The absence of the fluorescence peak at zero delay indicates single nature of the photon emitter.

Figure 1 | General properties of a single Ce$^{3+}$ ion in YAG. (a) Electronic level structure of Ce$^{3+}$ ion in YAG crystal. Blue arrows pointing upwards indicate electronic transitions under laser excitation, while green arrows pointing downwards represent cerium fluorescence. Relative strengths of optical transitions between the lowest 4$f$ and the lowest 5$d$ spin doublets (396:1) are shown for circularly polarized excitation light propagating along the $x$ axis of the local Ce$^{3+}$ symmetry frame. External magnetic field along the $y$ direction splits the spin doublets. Spin-up and spin-down states are indicated by short up- and down-arrows next to the corresponding energy level. (b) Confocal scan of individual cerium centres under the SIL. The scale bar is 2 µm. The dashed circle indicates boundary of the SIL. (c) Photon-correlation signal taken on a single Ce$^{3+}$ centre under pulsed laser excitation (see Methods section for details on antibunching measurements). The absence of the fluorescence peak at zero delay indicates single nature of the photon emitter. (d) Typical spectrum of a single cerium ion at 3.5 K. (e) High-resolution spectrum of Ce$^{3+}$ in the vicinity of its zero-phonon line (ZPL). The positions of ZPLs for distinct cerium centres are slightly different depending on the local environment of each centre. (f) Focused beam of cerium ions (300 keV) was used to create a grid of Ce$^{3+}$-doped spots in YAG single crystal. The scale bar is 10 µm.

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Optical detection of Ce$^{3+}$ spin resonance. The initialized spin can be manipulated by microwave radiation resonant with the spin transition of the ground 4f(1) state. For that purpose, a microwave structure was created on the surface of the sample right next to the location of the SIL. This allowed us to record optically detected magnetic resonance (ODMR) spectra of individual cerium ions. Once the frequency of microwaves matches that of the spin transition, the population from the $|4\rangle\rangle$ state is pumped back into $|4\rangle\rangle$ and the overall fluorescence yield increases. A typical ODMR spectrum of a single cerium ion is shown in Fig. 3a. Linewidths of ODMR spectra are in the range of 10–15 MHz varying slightly for different cerium centres. The width of the ODMR line is determined by two factors: inhomogeneous broadening of the line because of random magnetic field produced by $^{27}$Al nuclei and microwave power broadening. Since Ce$^{3+}$ can occupy six magnetically inequivalent sites in YAG, in general, six distinct positions of ODMR peak are possible. A combination of measured ODMR frequency and known g-tensor of the ground-state Ce$^{3+}$ spin allowed us to determine the orientation of individual cerium sites. In our (110) oriented crystal, the ODMR resonances were at 640 and 1,310 MHz and four nearly degenerate ones around 1,550 MHz. For further experiments, we were choosing the centres having their local $y$ axis (we adopted the axes assignment from the work) oriented along the magnetic field and the excitation beam (640 MHz) since for these centres the theoretical predictions for spin initialization fidelity is the best.

Coherent manipulation of Ce$^{3+}$ spin. The first step towards coherent manipulation of cerium electron spin is detection of Rabi oscillations under strong microwave driving. Experimentally, the circularly polarized laser excitation was chopped such that only a few tens of laser pulses are used to initialize the spin in $|4\rangle\rangle$. After this, a microwave pulse at resonant frequency of variable duration was applied (see Fig. 3b). Finally, a short laser pulse train having identical circular polarization was applied to read out the population of the $|4\rangle\rangle$ spin state. The result of the measurement is shown in Fig. 3c. The frequency of Rabi oscillations has square-root dependence on microwave power. The decay time of oscillations is longer than determined by the inhomogeneous linewidth indicating partial locking of the spin by microwaves.

Dephasing of cerium spin was measured by decay of Hahn echo signal (a sequence of $\pi/2-\tau-\pi-\tau-\pi/2$ microwave pulses, see inset in Fig. 4a). The result yields a value of $T_2=2\tau=240$ ns, where $\tau$ is the free evolution time between $\pi/2$ and $\pi$ pulses. Fast decoherence in YAG can be explained by the presence...
of the dense bath of $^{27}$Al having spin of $I = 5/2$ accompanied by large magnetic moment $\mu_{\text{Al}} = 3.64 \mu_N$ with $\mu_N$ being nuclear magneton. Fluctuating nuclear spins produce magnetic noise at the location of Ce$^{3+}$ reducing coherence time. Theoretical analysis of the nuclear spin bath showed that the contribution of octahedrally coordinated $^{27}$Al nuclei to decoherence is the largest (see Supplementary Methods).

**Dynamic decoupling of Ce$^{3+}$ spin from the nuclear bath.** Dynamic decoupling exploiting sequences of $\pi$ microwave pulses allows for an enormous increase in decoherence time$^{20}$. Decoherence is caused by the averaging over a phase factor $C(t) = \langle e^{i\phi(t)} \rangle$ the Ce$^{3+}$ spin acquires during free evolution.

\[ \pi \text{ pulses applied with frequency } 1/\tau \text{ effectively eliminate noise spectral components } \nu_{\text{noise}} < 1/\tau \text{ and thus lead to lenghtening of coherence lifetime.} \]

We used Carr–Purcell–Meiboom–Gill (CPMG) microwave decoupling sequence$^{21,22}$ (see Fig. 4b). The maximum number of refocusing pulses applied was 24,576. This allowed us to extend decoherence time up to 1.97 ms. The measured CPMG-echo signals shown in Fig. 4c agree well with the ones simulated by noise spectrum analysis and cluster expansion method$^{23}$ (see Supplementary Fig. 3). The dependence of the decoherence time on the number of CPMG pulses allows one to discriminate the influence of nuclear and electronic spin baths. The latter is composed of residual transition metal spin impurities such as Cr$^{3+}$ and Fe$^{3+}$. Electron and nuclear spin baths have...
significantly different noise spectral densities. The noise of the electron spin bath is best described by a Lorentzian-shaped spectrum characterized by a long spectral tail. This leads to a $N^{1/3}$ dependence of the coherence time $T_2^{\star}$. On the other hand, nuclear spin noise is characterized by a much harder cutoff leading to a linear dependence of $T_2$ on $N$. The experimentally measured dependence shown in Fig. 4d is $T_2 \propto N^{0.88}$ indicating that both nuclear and electron spin baths lead to decoherence with former contribution prevailing. Stretched-exponential fits of $\exp\left(-\left(t/T_2\right)^{\gamma}\right)$ to CPMG-echo signals result in exponentials $\gamma$ between 6 and 12 confirming the existence of hard cutoff of the nuclear spin noise spectrum as described in Supplementary Methods. These results suggest that changing the host material to a low nuclear spin one—that is, yttrium orthosilicate in which rare-earth ions show the longest coherence and population lifetimes $^{26,27}$, should greatly increase coherence lifetime in our single spin experiments. Changing the host material has almost no effect on the atomic-like polarization selection rules of $\text{Ce}^{3+}$ crucial for initializing its spin state. Preliminary measurements instead show extended coherence lifetime in the excited $5d$ state in yttrium orthosilicate compared with YAG (see Supplementary Fig. 4).

Discussion

An important asset of YAG and similar materials is that they are suitable for integrated photonic circuit fabrication, for example, in the form of thin films on low refractive index substrates (quartz) $^{28,29}$. Subsequent FIB milling would allow for creating on-chip photonic circuits with low attenuation ($1.5 \text{ dB cm}^{-1}$) $^{1}$ for single photons, which would include waveguides, cavities and so on. This would result in technologically simple realization of an on-chip integration of cerium spin qubits and, simultaneously, in obtaining access to longer-living isolated nuclear spins magnetically coupled the electron spin of $\text{Ce}^{3+}$.

Methods

Experimental setup. Optical studies of single $\text{Ce}^{3+}$ ions were performed in a home-built confocal microscope in which the crystal was mounted on a cold finger of a helium flow cryostat. An optical access was arranged through a window. The microscope objective lens of numerical aperture 0.95 was mounted inside the cryostat on a piezo nano-positioner. A toroidal permanent magnet was fixed on the objective lens to provide magnetic field parallel to the propagation direction of the excitation laser beam. The fluorescence of cerium ions was collected by the same objective lens and detected with a single photon counting avalanche photodiode (APD). To perform photon-correlation measurements, the fluorescence signal was split by a 50/50 beamsplitter and detected by two separate APDs. The signals of the two APDs were analysed by Becker and Hickl time-correlated single-photon counter card. In order to measure the emission spectra, the fluorescence was deflected by a mirror mounted on a flip mount on a grating spectrometer equipped with a cooled CCD camera. For measurements involving microwaves, a high-power MW amplifier ($50 \text{ dB}$ amplification, $30 \text{ W maximum output power}$) was used. The frequency of microwaves was swept by a software-controlled MW synthesizer. The microwaves were applied to the sample by a single copper wire positioned next to the SIL. The wire was lithographically defined on the surface of the crystal and electroplated. The cross-section of the wire amounted to $20 \mu\text{m}$ wide and $10 \mu\text{m}$ high with its length being several hundred microns. The wire was electrically contacted to the microwave source on one side and to the $50\Omega$-terminated drain on the other. No measures were taken to ensure impedance matching. However, the measured MW loss in the wire amounted to only 6 dB.

Sample preparation. In order to improve fluorescence collection efficiency, a solid immersion microlens was fabricated directly on the surface of the sample by FIB milling. The lens had a shape of half-a-sphere with the radius of 5 $\mu\text{m}$. In order to perform spin manipulations with microwaves, a copper microwave structure was created next to the location of the SIL by lithographic means. Even though the microwave structure was not impedance-matched to the outer MW network, the measured overall MW loss amounted to only 6 dB.

Details on initialization of $\text{Ce}^{3+}$ spin state. The pumping dynamics of the ground-state spin state was revealed in the following way. A finite train of circularly polarized laser pulses (the duration of the pulse is $100$ fs) was shot on the single $\text{Ce}^{3+}$ centre. The train contained 140 pulses with the repetition rate 2.5 MHz. The average laser power within the train was 50 $\mu\text{W}$ at the entrance aperture of the microscope objective lens. After each pulse train, the cerium ion spin was allowed to relax to thermal equilibrium for 50 ms. After that, the excitation of the ion with the finite pulse train was repeated and the signals obtained for each pulse train were averaged. The resulting signal was fitted with an exponential decay function multiplied by two step-functions (step-up and step-down) in order to simulate the beginning and the end of the excitation pulse train.

Implantation of cerium ions. YAG crystals were implanted in EIKO FIB with accelerating voltage 100 kV. Ions were extracted from the liquid metal ion source Ce-Si-Au. Ions were separated with built-in Wien filter so that $\text{Ce}^{3+}$ were implanted with the energy of $300 \text{ keV}$. With the simulations performed in the SRIM software, we obtain penetration depth of $62 \text{ nm}$ with straggler of $18 \text{ nm}$. Crystal was implanted with pattern of dots with fluences of $10^{10} \text{ cm}^{-2}$ and $2 \times 10^{15} \text{ cm}^{-2}$. This corresponds to $~10^{-4}$ and $2 \times 10^{-3}$ ions implanted per spot. In order to activate the implanted ions, thermal annealing was performed in argon atmosphere at $1,100 ^\circ \text{C}$ for $1 \text{ h}$. The activation yield was estimated by comparing the brightness of the implanted spots with the brightness of a single native cerium ion.

References

1. de Riedmatten, H., Afzelius, M., Staudt, M. U., Simon, C. & Gisin, N. A solid-state lightmatter interface at the single-photon level. Nature 456, 773–777 (2008).
2. Clausen, C. et al. Quantum storage of photonic entanglement in a crystal. Nature 469, 508–511 (2011).
3. Saglamyurek, E. et al. Broadband waveguide quantum memory for entangled photons. Nature 469, 512–515 (2011).
4. Longdell, J. J., Fraval, E., Sellers, M. J. & Manson, N. B. Stopped light with storage times greater than one second using electromagnetically induced transparency in a solid. Phys. Rev. Lett. 95, 063601 (2005).
5. Heinze, G., Hubrich, C. & Halfmann, T. Stopped light and image storage by electromagnetically induced transparency up to the regime of one minute. Phys. Rev. Lett. 111, 033601 (2013).
6. Vivaldi, V. C., Sangouard, N., Afzelius, M. & Gisin, N. High-bandwidth quantum memory protocol for storing single photons in rare-earth doped crystals. New J. Phys. 15, 095012 (2013).
7. Timoney, N., Usmani, I., Jober, P., Afzelius, M. & Gisin, N. Single-photon-level optical storage in a solid-state spin-wave memory. Phys. Rev. A 88, 022324 (2013).
8. Sangouard, N., Simon, C., de Riedmatten, H. & Gisin, N. Quantum repeaters based on atomic ensembles and linear optics. Rev. Mod. Phys. 83, 33–80 (2011).
9. Knill, E., Laflamme, R. & Milburn, G. J. A scheme for efficient quantum computation with linear optics. Nature 409, 46–52 (2001).
10. Longdell, J. J., Sellers, M. J. & Manson, N. B. Demonstration of conditional quantum phase shift between ions in a solid. Phys. Rev. Lett. 93, 130503 (2004).
11. Kolossov, R. et al. Optical detection of a single rare-earth ion in a crystal. Nat. Commun. 3, 1029 (2012).
12. Yin, C. et al. Optical addressing of an individual erbium ion in silicon. Nature 497, 91–94 (2013).
13. Kolossov, R. et al. Mapping spin coherence of a single rare-earth ion in a crystal onto a single photon polarization state. Phys. Rev. Lett. 111, 120502 (2013).
14. Utikal, T. et al. Spectroscopic detection and state preparation of a single praseodymium ion in a crystal. Nat. Commun. 5, 3627 (2014).
15. Robbins, D. J. J. Electrochem. Soc. 126, 1550–1555 (1979).
16. Varney, C. R., Mackay, D. T., Reda, S. M. & Selim, F. A. On the optical properties of undoped and rare-earth-doped yttrium aluminium garnet single crystals. J. Phys. D Appl. Phys. 45, 015103 (2012).
17. Morigaki, K. Optically detected magnetic resonance. Semiconduct. Semimet. 21C, 155–191 (1984).
18. Lewis, H. R. Paramagnetic resonance of $\text{Ce}^{3+}$ in yttrium aluminium garnet. J. Appl. Phys. 37, 739–741 (1966).
19. van der Ziel, J. P., Sturge, M. D. & van Uitert, L. G. Optical detection of site selectivity for rare-earth ions in flux-grown yttrium aluminium garnet. Phys. Rev. Lett. 27, 508–511 (1971).
20. Viola, L. & Lloyd, S. Dynamical suppression of decoherence in two-state quantum systems. Phys. Rev. A 58, 2733–2744 (1998).
21. Carr, H. Y. & Purcell, E. M. Effects of diffusion on free precession in nuclear magnetic resonance experiments. Phys. Rev. 94, 630–638 (1954).
22. Melboom, S. & Gill, D. Modified spin echo method for measuring nuclear relaxation times. Rev. Sci. Instrum. 29, 688–691 (1958).
23. Yang, W. & Liu, R.-B. Quantum many-body theory of qubit decoherence in a finite-size spin bath. Phys. Rev. B 78, 085315 (2008).
24. de Lange, G., Wang, Z. H., Risté, D., Dobrovitski, V. V. & Hanson, R. Universal dynamical decoupling of a single solid-state spin from a spin bath. Science 330, 60–63 (2010).
25. Medford, J. et al. Scaling of dynamical decoupling for spin qubits. Phys. Rev. Lett. 108, 086802 (2012).
26. Yan, Y. et al. Measurement of linewidths and permanent electric dipole moment change of the Ce 4f–5d transition in Y2SiO5 for qubit readout scheme in rare-earth ion based quantum computing. Phys. Rev. B 87, 184205 (2013).

27. Könz, F. et al. Temperature and concentration dependence of optical dephasing, spectral-hole lifetime, and anisotropic absorption in Eu3+:Y2SiO5. Phys. Rev. B 68, 085109 (2003).

28. Wu, Y.-C., Parola, S., Marty, O., Villanueva-Ibáñez, M. & Mugnier, J. Structural characterizations and waveguiding properties of YAG thin films obtained by different solgel processes. Opt. Mater. 27, 1471–1479 (2005).

29. Choe, J. Y. Luminescence and compositional analysis of Y3Al5O12:Ce films fabricated by pulsed-laser deposition. Mat. Res. Innovat. 6, 238–241 (2002).

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P.S. and K.X. contributed equally to this work; P.S., K.X., R.R., M.J., N.K., A.D.W. and R.K. performed the experiments; P.S., K.X. and R.K. designed the experiments; P.S., K.X. and R.K. analysed the data; N.Z., N.Y. and C.D. performed theoretical calculations; R.K., N.Z. and J.W. wrote the paper; J.W. supervised the project.

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