Chemical freeze-out conditions in hadron resonance gas

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The hadron resonance gas model with the hadron-type dependent eigenvolume corrections is employed to fit the hadron yield data of the NA49 collaboration for central Pb+Pb collisions at the center of mass energy of the nucleon pair $\sqrt{s_{NN}} = 6.3, 7.6, 8.8, 12.3$, and $17.3$ GeV, the hadron midrapidity yield data of the STAR collaboration for Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV, and the hadron midrapidity yield data of the ALICE collaboration for Pb+Pb collisions at $\sqrt{s_{NN}} = 2760$ GeV. The influence of the eigenvolume corrections is studied.

I. INTRODUCTION

Phenomenological thermodynamic models are very useful in extracting basic parameters of the strongly interacting matter created in the relativistic nucleus-nucleus (A+A) collisions, particularly, to estimate its temperature [1–3]. The thermal parameters at chemical freeze-out – the stage of A+A collision when inelastic reactions between hadrons cease – have been successfully extracted by fitting the rich data on hadron yields in various experiments, ranging from the low energies at SchwerIonen-Synchrotron (SIS) to the highest energy of the Large Hadron Collider (LHC), within the hadron resonance gas (HRG) model [4–10]. It has been argued [11], that the inclusion into the model of all known resonances as free non-interacting (point-like) particles allows to effectively model the attraction between hadrons. Such formulation, a multi-component point-particle gas of all known hadrons and resonances, is presently the most commonly used one in the thermal model analysis.

In a realistic HRG model one also needs to take into account the repulsive interactions between hadrons. The HRG with the repulsive interactions have been successfully compared with the lattice QCD data [12–15], and it has recently been shown in Ref. [16] that the inclusion of the repulsive interactions into HRG in the form of a multi-component eigenvolume procedure can significantly change the chemical freeze-out temperature while improving the agreement with the ALICE hadron yield data compared to the point-particle HRG. In the present work we perform a similar analysis at the finite (baryo)chemical potential by considering the data on hadron yields in Pb+Pb and Au+Au collisions of NA49 and STAR collaborations. In order to study the sensitivity of the obtained results we use two different formulations of the multi-component eigenvolume HRG.

II. HADRON RESONANCE GAS

The ideal HRG (I-HGR) model corresponds to a statistical system of noninteracting hadrons and resonances and leads to the following formula for the system pressure in the grand canonical ensemble (GCE)

$$P(T, \mu_B) = \sum_j p_j^{id}(T, \mu_j) = \sum_j \frac{d_j}{6\pi^2} \int_0^\infty \frac{k^4dk}{\sqrt{k^2 + m_j^2}} \left\{ \exp \left[ \frac{(\sqrt{k^2 + m_j^2} - \mu_j)}{T} \right] \pm \eta_j \right\}^{-1},$$

(1)

where $d_j$ and $m_j$ are, respectively, the degeneracy factor and mass of $j$th particle species, $\eta_j = 1$ for fermions ($\eta_j = 0$ corresponds to the classical Boltzmann approximation). The sum in Eq. (1) runs over all known hadron and resonances. The chemical potentials $\mu_j$ for $j$th particle species are taken as $\mu_j = b_j\mu_B + s_j\mu_S + q_j\mu_Q$, where $b_j$, $s_j$, and $q_j$ correspond, respectively, to the baryonic number, strangeness, and electric charge of $j$th particle; chemical potentials $\mu_B$, $\mu_S$, and $\mu_Q$ regulate the average values of the conserved charges: baryonic number $B$, strangeness $S$, and electric charge $Q$.

In application to A+A collisions the free model parameters of the HRG model are $T$, $\mu_B$, and $V$. The strange chemical potential $\mu_S = \mu_S(T, \mu_B)$ and electric chemical potential $\mu_Q = \mu_Q(T, \mu_B)$ are found from the conditions of zero net strangeness and fixed proton-neutron ratio in the colliding nuclei, e.g., $Q/B \equiv 0.4$ for heavy nuclei. The other intensive thermodynamical functions, like particle number densities, are calculated from the pressure function by standard thermodynamic formulae. Extensive quantities, like total numbers of particles, are obtained by multiplying the corresponding densities by the system volume $V$. 

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The repulsive interactions between hadrons can be modeled by the eigenvolume correction of the van der Waals type, first proposed in Refs. [17, 19], while the thermodynamically consistent procedure for a single-component gas was formulated in Ref. [20]. In our study we use two different formulations considered within the Boltzmann statistics. We expect that the effects of quantum statistics have a minor influence on the obtained results.

The single-component eigenvolume model of Ref. [20] was generalized to the multi-component case in Ref. [21]. It was assumed that the available volume for each of the hadron species is the same, and equals to the total volume minus sum of eigenvolumes of all the hadrons in the system. This leads to the transcendental equation

\[ P(T, \mu_B) = \sum_j p_j^{\text{el}}(T, \mu_j^*) , \quad \mu_j^* = \mu_j - v_j P(T, \mu_B) , \]

with \( v_j = 16\pi r_j^3/3 \) being the eigenvolume parameter for the particle \( j \). At \( v_j = 0 \) the EV-HRG model [2] is reduced to the I-HRG model [1].

Let us assume that we have \( f \) different hadron species. The pressure as function of the temperature and hadron densities has the following form

\[ P(T, n_1, \ldots, n_f) = T \frac{\sum_i n_i}{1 - \sum_j v_j n_j} , \]

where the sum goes over all hadrons and resonances included in the model, and where \( n_i \) is the eigenvolume parameter of hadron species \( i \). The eigenvolume parameter \( v_i \) can be identified with the 2nd virial coefficient of the single-component gas of hard spheres and is connected to the hard-core hadron radius \( r_i \) as \( v_i = 4\pi r_i^3/3 \).

In the GCE one has to solve the non-linear equation [2] for the pressure. The number densities in the GCE can be calculated as

\[ n_i(T, \mu_B) = \frac{n_i^{\text{el}}(T, \mu_i^*)}{1 + \sum_j v_j n_j^{\text{el}}(T, \mu_j^*)} .\]

The multi-component eigenvolume HRG model given by Eqs. [3]-[4] is the most commonly used one in the thermal model analysis. Since this model does not consider the cross-terms in the virial expansion of the multi-component gas of hard spheres (see details below) we will refer to it as the “diagonal” model.

The virial expansion of the classical (Boltzmann) multi-component gas of hard spheres up to 2nd order can be written as [22]

\[ P(T, n_1, \ldots, n_f) \approx T \sum_i n_i + T \sum_{ij} b_{ij} n_i n_j , \quad b_{ij} = \frac{2\pi}{3} (r_i + r_j)^3 \]

are the components of the symmetric matrix of the 2nd virial coefficients.

Comparing Eqs. [3] and [5] one can see that the diagonal model is not consistent with the virial expansion of the multi-component gas of hard spheres up to 2nd order and corresponds to a different matrix of 2nd virial coefficients, namely \( b_{ij} = v_i \). For this reason we additionally consider the van der Waals like multi-component eigenvolume model from Ref. [23], which is formulated in the GCE assuming Boltzmann statistics, and which is consistent with the 2nd order virial expansion in Eq. [5]. The pressure in this model reads as

\[ P(T, n_1, \ldots, n_f) = \sum_i P_i = T \sum_i \frac{n_i}{1 - \sum_j b_{ij} n_j} , \quad \hat{b}_{ij} = \frac{2 b_{ii} b_{jj}}{b_{ii} + b_{jj}} \]

with \( b_{ij} \) given by [5], and where quantities \( P_i \) can be regarded as “partial” pressures. This eigenvolume model given by [5] is initially formulated in the canonical ensemble. In Ref. [23] it was transformed to the grand canonical ensemble. In the GCE formulation one has to solve the following system of the non-linear equations for \( P_i \)

\[ P_i = p_i^{\text{el}}(T, \mu_i - \sum_j \hat{b}_{ij} P_j), \quad i = 1, \ldots, f , \]

where \( f \) is the total number of the hadronic components in the model. The hadronic densities \( n_i \) can then be recovered by solving the system of linear equations connecting \( n_i \) and \( P_i \)

\[ T n_i + P_i \sum_j b_{ij} n_j = P_i , \quad i = 1, \ldots, f . \]

We refer to the model given by Eqs. [6]-[8] as the “crossterms” eigenvolume model (see also Ref. [24]). In practice, the solution to [7] can be obtained by using an appropriate iterative procedure. In our calculations the Broyden’s method [25] is employed to obtain the solution of the “crossterms” model, using the corresponding solution of the “diagonal” model as the initial guess.
III. CALCULATION RESULTS

In our calculations we include strange and non-strange hadrons listed in the Particle Data Tables [26], along with their decay branching ratios. This includes mesons up to $f_2(2340)$, (anti)baryons up to $N(2600)$. We do not include hadrons with charm and bottom degrees of freedom which have a negligible effect on the fit results, and we also removed the $\sigma$ meson ($f_0(500)$) and the $\kappa$ meson ($K^*_0(800)$) from the particle list because of the reasons explained in Refs. [27, 28]. The finite width of the resonances is taken into account in the usual way, by adding the additional integration over their Breit-Wigner shapes in the point-particle gas expressions. The feed-down from decays of the unstable resonances to the total hadron yields is included in the standard way.

As was mentioned before, the inclusion of the eigenvolume interactions is one of the most popular extensions of the standard HRG model. In most of the analyses dealing with chemical freeze-out which did include the eigenvolume corrections [9, 29, 30] it was assumed that all the hadrons have the same eigenvolume. It has been established that, in this case, the eigenvalue corrections can significantly reduce the densities [31, 32], and, thus, increase the total system volume at the freeze-out as compared to the point-particle gas at the same temperature and chemical potential. For this parametrization, however, the eigenvolume corrections essentially cancel out in the ratios of yields and, thus, have a negligible effect on the values of the extracted chemical freeze-out temperature and chemical potential. If, however, one considers hadrons with the different hard-core radii, then the ratios may change, and the fit quality can be improved [24, 33].

In order to test the sensitivity of the freeze-out conditions due to different hard-core hadron radii we consider two parametrizations. Our main focus will be on the bag-model inspired parametrization, with the hadron eigenvalue proportional to its mass through a bag-like constant, i.e.,

$$v_i = m_i/\varepsilon_0 .$$

Such eigenvalue parametrization had been obtained for the heavy Hagedorn resonances, and was used to describe their thermodynamics [17, 19] as well as their effect on particle yield ratios [34]. It was mentioned in the Ref. [35] that such parametrization would lead to the increase of the freeze-out temperature, but that it does not entail an improvement of the fit quality in the “diagonal” EV model, or changes in other fit parameters. Note that the eigenvalue for the resonances with the finite width is assumed to be constant for each resonance, and is determined by its pole mass.

We perform the thermal fit to the midrapidity yields of the charged pions, charged kaons, (anti)protons, $\Xi^-$, $\Xi^+$, $\Omega$, $\Omega$, $\Lambda$, $K^0_S$, and $\phi$, measured by the ALICE collaboration in the 0-5% most central Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV [36]. Note that the centrality binning for $\Xi$ and $\Omega$ hyperons is different from the other hadrons. Thus, we take the midrapidity yields of $\Xi$ and $\Omega$ in the 0-5% centrality class from Ref. [38], where they were obtained using the interpolation procedure.

The left Fig. [1] shows the temperature dependence of the $\chi^2/N_{dof}$ for three versions of the HRG model: point-particle particles, i.e. all $v_i = 0$, the two-component eigenvalue HRG model with the point-like mesons $r_M = 0$ and the (anti)baryons of fixed size $r_B = 0.3$ fm [12], and the bag-like eigenvalue HRG model with the bag-like constant in Eq. (9) fixed to reproduce the hard-core proton radius of 0.5 fm. At each temperature the only remaining free parameter, namely the system volume per unit slice of midrapidity, is fixed to minimize the $\chi^2$ at this temperature.

Presently not much is known about the eigenvalues of different hadron species, and there is no proof that parametrization [9] is the most realistic one. For instance, it can be argued, that strange hadrons should have a different (smaller) eigenvalue compared to non-strange ones. The bag-like constant $\varepsilon_0$ determines the magnitude of the hadron eigenvalues. The values of $r_p = 0.3 - 0.8$ fm have been rather commonly used in the literature [21, 24, 29, 31, 33]. Additionally, the value $r_p \approx 0.6$ fm was extracted from the ground state properties of nuclear matter within the fermionic van der Waals equation for nucleons [39]. Note that, within the bag-like parametrization, the hard-core radius $r_i$ of any hadron $i$ is related to the chosen value of $r_p$ through the relation $r_i = r_p \cdot (m_i/m_p)^{1/3}$, where $m_i$ is the mass of the hadron $i$.

As seen from the left Fig. [1] the $\chi^2/N_{dof}$ has the second minimum in the EV HRG models at high temperatures. To understand its physical origin let us consider the EV HRG model with $r_M = 0$ and $r_B = 0.3$ fm for a simple case of the $\pi NN$ mixture with with $\mu_B = 0$ (i.e. with equal average numbers of nucleons and antinucleons. Using the Boltzmann approximation, one obtains for the nucleon to pion ratio:

$$\frac{N_N(T)}{N_\pi(T)} = \exp \left[ - \frac{v_N P(T)}{T} \right] \frac{n_{N,N}^{\text{uf}}(T)}{n_{\pi,\pi}^{\text{uf}}(T)} ,$$

where pressure $P(T)$ is determined by solving Eq. (2) with $\mu_i = 0$ ($i = N, N, \pi$) and $v_\pi = 0$. Figure [2] shows the temperature dependence of the $n_N/n_\pi$ ratio for several values of $r_N$. One can see that the ratio (10) has a non-monotonic temperature dependence with a maximum in the $T$-interval from 200 to 300 MeV. An increase of $N_N/N_\pi$ at small $T$ is due to a strong increase of $n_{N,N}^{\text{uf}}(T) \sim \exp(-m_N/T)$ at low temperatures. At large $T$
FIG. 1: Left: The temperature dependence of $\chi^2/N_{\text{ dof}}$ of different fits to the ALICE data on hadron yields in 0-5% most central Pb+Pb collisions at 2.76 TeV. The solid line corresponds to the point-particle HRG model, the dashed line to $r_B = 0.3$ fm and $r_M = 0$, and the dotted line to bag-like eigenvolume HRG model (the bag-like constant in Eq. (9) is fixed to reproduce the hard-core proton radius of 0.5 fm. Right: The freeze-out parameters within three different versions of the HRG: point-particles, the “diagonal” EV model with $r_M = 0$ and $r_B = 0.3$ fm, and the “crossterms” eigenvolume HRG with $r_1 \sim m_1^{1/3}$ and $r_p = 0.43$ fm. The parameterized freeze-out curves from Refs. [10], [30], and [37], obtained within the point-particle-like HRG models, are depicted by lines.

FIG. 2: The $N/\pi$ ratio as a function of temperature in the $\pi NN$ matter with equal numbers of nucleons and antinucleons. The thick solid, dashed, and dash-dotted lines correspond to nucleon hard-core radii $r_N = 0.3, 0.4$ and 0.5 fm, respectively. The dotted line is obtained in the ideal gas limiting case $r_N = 0$. (and, thus, large system pressure $P$) the ratio $N/\pi$ starts to decrease because of a stronger EV suppression of (anti)nucleon densities as compared to pions. At fixed value of $r_N$ one can fit the $N/\pi$ ratio by choosing two different values of temperature. The higher temperature value corresponds to a denser state of the $\pi NN$ system with strong short-range interactions of mesons and (anti)baryons.

We perform the simultaneous fit of the hadron yield data of the NA49, STAR, and ALICE collaborations. The data of the NA49 collaboration includes 4 $\pi$ yields of the charged pions, charged kaons, $\Xi^-$, $\Xi^+$, $\Lambda$, $\phi$, and, if available, $\Omega$, $\Omega$, measured in the 0-7% most central Pb+Pb collisions $\sqrt{s_{NN}} = 6.3, 7.6, 8.8, 12.3$, and in the 0-5% most central Pb+Pb collisions at $\sqrt{s_{NN}} = 17.3$ GeV [40, 41]. The feeddown from strong and electromagnetic
The included eigenvolumes are fixed for a proton hard-core radius of 0.4-0.6 fm, these models describe the data well. Multi-component HRG models employing different eigenvolumes for different hadrons. For the case of mass-degenerate hadrons, the fit errors of the extracted parameters are significantly smaller in the EV models compared to the one obtained within the point-particle HRG. A similar result was obtained in Ref. [47] but by employing a different mechanism, namely, by the considering the distortion of the chemical freeze-out parameters.

The extraction of the chemical freeze-out parameters is thus rather sensitive to the modeling of repulsive interactions between hadrons. For these reasons, even when the lattice constraint is used, the uncertainties in the extraction of the chemical freeze-out parameters remain large. These large uncertainties in the values of $T$ and $\mu_B$ at chemical freeze-out seen in our analysis may indicate that the chemical freeze-out is not a sharp process which takes place on some so-called freeze-out hypersurface with very similar values of the temperature and chemical potential, but that it is rather a continuous process, happening throughout the whole space-time evolution of the system created in heavy-ion collisions, and characterized by very different values of temperatures, energy densities, and other parameters. Such a picture has been obtained within the transport model simulations of the heavy-ion collisions by analyzing the space-time distribution of the chemical “freeze-out” points of various hadrons [48].

**IV. SUMMARY**

In summary, the data of the NA49, STAR, and ALICE collaborations on the hadron yields in central Pb+Pb (Au+Au) collisions at $\sqrt{s_{NN}} = 6.3, 7.6, 8.8, 12.3, 17.3, 200, \text{ and } 2760 \text{ GeV}$ is analyzed within the two different multi-component HRG models employing different eigenvolumes for different hadrons. For the case of mass-proportional eigenvolumes, fixed for a proton hard-core radius of 0.4-0.6 fm, these models describe the data significantly better than the conventional point-particle HRG model in very wide regions in the $T$-$\mu_B$ plane. Similarly, a much broader $\chi^2$ minima are observed when mesons are assumed to be point-like while baryons have a fixed hard-core radius of $r_B = 0.3$ fm.

These results show that the extraction of the chemical freeze-out parameters is extremely sensitive to the modeling of the short-range repulsion between the hadrons, and imply that the point-particle HRG cannot be used for a reliable determination of the chemical freeze-out conditions. Even within a more conservative approach, where we rather strictly constrain the model parameters to the lattice data, we obtain a chemical freeze-out curve which differs from the one obtained in the point-particle case, has a systematically better fit quality of the data, and demonstrates a rather irregular non-parabolic $\chi^2$ profile in the vicinity of the minima. On the other hand, the entropy per baryon extracted from the data for the different energies is found to be much...
more robust: it is almost independent of the details of the modeling of the eigenvolume interactions and of the specific $T - \mu_B$ values obtained. This is consistent with the picture of continuous freeze-out, where hadrons are being frozen-out throughout the extended regions of the space-time evolution of the system rather than from the sharp freeze-out hypersurface.

The obtained results demonstrate that inclusion of the eigenvolume interactions are of crucial importance for thermal fitting the hadron yield data. It is also shown that any conclusions based on thermal fits should be based not just on the location of the $\chi^2$ minimum and its magnitude, but rather on the full profile of the $\chi^2$. In many cases the $\chi^2$ has an irregular non-parabolic structure around the minimum, thus, the standard statistical-based estimates of the uncertainties of the extracted parameters become inapplicable.

The collision energy range investigated in this work is relevant for the ongoing SPS and RHIC beam energy scan programs, as well as for the experiments at the future FAIR and NICA facilities. The presented results should be taken into account in the future analysis and interpretation of the hadron yield data within these experiments.

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[1] H. Stoecker, A. A. Ogloblin, and W. Greiner, Z. Phys. A 303, 259 (1981).
[2] J. J. Molitoris, D. Hahn, and H. Stoecker, Prog. Part. Nucl. Phys. 15, 239 (1985).
[3] D. Hahn and H. Stoecker, Phys. Rev. C 35, 1311 (1987).
[4] J. Ceylans and H. Satz, Z. Phys. C 57, 135 (1993).
[5] J. Ceylans, K. Redlich, Phys. Rev. Lett. 81, 5284 (1998).
[6] J. Ceylans, K. Redlich, Phys. Rev. C 60, 054908 (1999).
[7] F. Becattini, J. Ceylans, A. Keranen, E. Shuonen, and K. Redlich, Phys. Rev. C 64, 024901 (2001).
[8] F. Becattini, M. Gazdzicki, A. Keranen, J. Manninen, and R. Stock, Phys. Rev. C 69, 024905 (2004).
[9] A. Andronic, P. Braun-Munzinger, and J. Stachel, Nucl. Phys. A 772, 167 (2006).
[10] A. Andronic, P. Braun-Munzinger, and J. Stachel, Phys. Lett. B 673, 142 (2009).
[11] R. Dashen, S.-K. Ma, and H. J. Bernstein, Phys. Rev. 187, 345 (1969).
[12] A. Andronic, P. Braun-Munzinger, J. Stachel, and M. Winn, Phys. Lett. B 718, 80 (2012).
[13] V. Vovchenko, D. V. Anchishkin, and M. I. Gorenstein, Phys. Rev. C 91, 024905 (2015).
[14] M. Albright, J. Kapusta, and C. Young, Phys. Rev. C 91, 024915 (2014); Phys. Rev. C 92, 044904 (2015).
[15] V. Vovchenko and H. Stoecker, to be published.
[16] V. Vovchenko and H. Stoecker, arXiv:1512.08046 [hep-ph].
[17] R. Hagedorn and J. Rafelski, Phys. Lett. B 97, 136 (1980); R. Hagedorn, Z. Phys. C 17, 265 (1983).
[18] M. I. Gorenstein, V. K. Petrov, and G. M. Zinovjev, Phys. Lett. B 106, 327 (1981).
[19] J. I. Kapusta and K. A. Olive, Nucl. Phys. A 408, 478 (1983).
[20] D. H. Rischke, M. I. Gorenstein, H. Stöcker, and W. Greiner, Z. Phys. C 51, 485 (1991).
[21] G. D. Yen, M. I. Gorenstein, W. Greiner, and S. N. Yang, Phys. Rev. C 56, 2210 (1997).
[22] L. D. Landau and E. M. Lifshitz, Statistical Physics (Oxford: Pergamon) 1975.
[23] M. I. Gorenstein, A. P. Kostyuk and Y. D. Krivenko, J. Phys. G 25, L75 (1999).
[24] K. A. Bugaev, D. R. Oliinychenko, A. S. Sorin, and G. M. Zinovjev, Eur. Phys. J. A 49, 30 (2013).
[25] C. G. Broyden, Mathematics of Computation 19, 577 (1965).
[26] K. A. Olive et al. [Particle Data Group Collaboration], Chin. Phys. C 38, 090001 (2014).
[27] W. Broniowski, F. Giacosa, and V. Begun, Phys. Rev. C 92, 034905 (2015).
[28] J. R. Pelaez, arXiv:1510.00653 [hep-ph].
[29] P. Braun-Munzinger, I. Heppe, and J. Stachel, Phys. Lett. B 465, 15 (1999).
[30] J. Ceylans, H. Oeschler, K. Redlich, and S. Wheaton, Phys. Rev. C 73, 034905 (2006).
[31] V. V. Begun, M. Gazdzicki, and M. I. Gorenstein, Phys. Rev. C 88, 024902 (2013).
[32] D. Anchishkin, V. Vovchenko, J. Phys. G 42, 105102 (2015).
[33] G. D. Yen and M. I. Gorenstein, Phys. Rev. C 59, 2788 (1999).
[34] J. Noronha-Hostler, H. Ahmad, J. Noronha, and C. Greiner, Phys. Rev. C 82, 024913 (2010).
[35] F. Becattini, J. Manninen, and M. Gazdzicki, Phys. Rev. C 73, 044905 (2006).
[36] B. Abelev et al. [ALICE Collaboration], Phys. Rev. C 88, 044910 (2013); B. B. Abelev et al. [ALICE Collaboration], Phys. Rev. Lett. 111, 222301 (2013); B. B. Abelev et al. [ALICE Collaboration], Phys. Lett. B 728, 216 (2014); B. B. Abelev et al. [ALICE Collaboration], Phys. Rev. C 91, 024609 (2015).
[37] V. Vovchenko, V. V. Begun, and M. I. Gorenstein, arXiv:1512.08025 [nucl-th]
[38] F. Becattini, E. Grossi, M. Bleicher, J. Steinheimer, and R. Stock, Phys. Rev. C 90, 054907 (2014).
[39] V. Vovchenko, D. V. Anchishkin, and M. I. Gorenstein, Phys. Rev. C 91, 064314 (2015).
[40] S.V. Afanasiev et al. [NA49 collaboration], Phys. Rev. C 66, 054902 (2002); C. Alt et al. [NA49 Collaboration], Phys. Rev. C 73, 044910 (2006); C. Alt et al. [NA49 collaboration], Phys. Rev. C 77, 024903 (2008).

[41] C. Alt et al. [NA49 Collaboration], Phys. Rev. C 78, 034918 (2008); C. Alt et al. [NA49 Collaboration], Phys. Rev. C 78, 044907 (2008); C. Alt et al. [NA49 Collaboration], Phys. Rev. Lett. 94, 192301 (2005); T. Anticic et al. [NA49 Collaboration], Phys. Rev. C 85, 044913 (2012); V. Friese [NA49 Collaboration], Nucl. Phys. A 698, 487 (2002).

[42] The tabulated hadron yield data of the NA49 collaboration is available at https://edms.cern.ch/document/1075059.

[43] J. Adams et al. [STAR Collaboration], Phys. Rev. Lett. 92, 112301 (2004); Phys. Rev. Lett. 98, 062301 (2007); B. I. Abelev et al. [STAR Collaboration], Phys. Rev. Lett. 99, 112301 (2007).

[44] J. Manninen and F. Becattini, Phys. Rev. C 78, 054901 (2008).

[45] L. M. Satarov, K. A. Bugaev, and I. N. Mishustin, Phys. Rev. C 91, 055203 (2015).

[46] K. Zalewski and K. Redlich, Phys. Rev. C 93, 014910 (2016).

[47] F. Becattini, M. Bleicher, T. Kollegger, T. Schuster, J. Steinheimer, and R. Stock, Phys. Rev. Lett. 111, 082302 (2013).

[48] S. A. Bass, A. Dumitru, M. Bleicher, L. Bravina, E. Zabrodin, H. Stoecker and W. Greiner, Phys. Rev. C 60, 021902 (1999); L. V. Bravina, I. N. Mishustin, J. P. Bondorf, A. Faessler and E. E. Zabrodin, Phys. Rev. C 60, 044905 (1999).