On the connection of Gamma-rays, Dark Matter and Higgs searches at LHC

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(Dated: February 20, 2022)

Motivated by the upcoming Higgs analyzes we investigate the importance of the complementarity of the Higgs boson chase on the low mass WIMP search in direct detection experiments and the gamma-ray emission from the Galactic Center measured by the Fermi-LAT telescope in the context of the $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$. We obtain the relic abundance, thermal cross section, the WIMP-nucleon cross section in the low mass regime and network them with the branching ratios of the Higgs boson in the model. We conclude that the Higgs boson search has a profound connection to the dark matter problem in our model, in particular for the case that $(M_{WIMP} < 60 \text{ GeV})$ the $\text{BR}(H \rightarrow 2 \text{ WIMPs}) \gtrsim 90\%$. This scenario could explain this plateau of any mild excess regarding the Higgs search as well as explain the gamma-ray emission from the galactic center through the $bb$ channel with a WIMP in the mass range of $25 - 45 \text{ GeV}$, while still being consistent with the current limits from XENON100 and CDMSII. However, if the recent modest excesses measured at LHC and TEVATRON are confirmed and consistent with a standard model Higgs boson this would imply that $M_{WIMP} > 60 \text{ GeV}$, consequently ruling out any attempt to explain the Fermi-LAT observations.

I. INTRODUCTION

The nature of the Dark Matter (DM) is one of the biggest mysteries of the universe and lies on the interface of particle physics, astrophysics and cosmology. It is common sense that, in order to determine its nature, a complementary search in direct and indirect detection plus collider experiments is necessary. The long standing DAMA/LIBRA experiment reports with significance of $8.9\sigma$ the detection of an annual modulation with a phase and period consistent with elastically scattering dark matter, a WIMP (Weakly Interacting Massive Particle) [1] with a mass of $\sim 7 \text{ GeV}$, with a WIMP-nucleon cross section of $\sim 10^{-41} \text{ cm}^2$ [2]. The CRESST and CoGeNT experiments observed recently some excess events consistent with WIMP scattering off a nuclei with similar spectrum of events [3, 4]. The CoGeNT collaboration has reported an annual modulation with an amplitude higher than DAMA but also consistent with the WIMP hypothesis. Those observations seem to point to an imminent WIMP discovery in the near future. However the DAMA modulation is arguable since there are analyses which claim that this modulation could be due to cosmic ray muons [5], while others disagree with the muon hypothesis by declaring that the phases are $\sim 3\sigma$ off [6] and the scattering rates are different. With respect to the CoGeNT excesses, the uncertainties in the rise time cut may result in a sizable contamination of surface events in CoGeNT data and therefore a fraction of these excess events is expected to be residual surface events [2]. Lately a large background contamination is expected in the CRESST detector by $^{206}\text{Pb}$ decays and $\alpha$ particles [7]. Furthermore these signals appear to be in conflict with the other experiments such as CDM-SII and XENON10. In particular, the CDMS collaboration has searched for this modulation in their last run but no annual modulation was found [8]. Conversely, the XENON detector which measures ionization and scintillation and has the strongest constraints in this mass range, suffers non-negligible uncertainties in the scintillation efficiency at low recoil energies as discussed in [9], making it difficult to interpret their resulting limits at low energy range. Likewise, it is important to mention that at such low energies the backgrounds observed by CDMS are not well understood, somewhat limiting their ability to probe the region implied by CoGeNT and DAMA-LIBRA [10]. Be that as it may, one could evoke non-Maxwellian distributions and/or tidal streams to alleviate the tension among those experiments [11]. In summary the claim whether these signals reported recently are due to dark matter or not is still debatable. Besides this search for dark matter at low energy recoils, an important and enlightening mono-photon and mono-jet search has been performed at the LHC and the strongest limits in the $\sim 1 \text{ GeV}$ mass window have been put for the case of light mediators [12]. Moreover an interesting and promising search for dark matter is ongoing in a variety of ground based and space based telescopes [13]. In particular the Fermi Gamma Ray Telescope have been collecting data for almost four years from the region surrounding the center of the Milky Way which is both astrophysically rich and complex, and is predicted to contain very high densities of dark matter. By analyzing the morphology and spectrum of the gamma ray emission from this region, several groups [14, 15] have found an evidence of a spatially extended component which peaks at energies between $300 \text{ MeV}$ and $10 \text{ GeV}$ which can be either explained by the annihilation of dark matter particles in the inner galaxy, or through collisions of high energy protons (that are accelerated by the Milky Way’s supermassive black hole) with gas. If interpreted as dark matter annihilation products, the emission spectrum favors dark matter particles with a mass in the range
Following the complementarity of these three approaches in the context of the $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$, $331_{LHN}$ for short [14, 15]. Besides featuring many of the standard model (SM) virtues it addresses fundamental questions such as the dark matter signals [19] as well as many theoretical questions, such as number of families [16] and neutrinos masses, among others [17]. We will not dwell on the nice features of the model, but we recommend those works aforementioned for those who are interested in more detailed descriptions. Despite the cold dark matter problem has been already investigated in the context of 331 models in Ref. [19], here we will also investigate indirect detection signals, derive the branching ratios of Higgs boson in direct and indirect detection searches by analyzing the impact of the ongoing Higgs boson chase on the parameter space of the model, such as to explain the gamma-ray emission from the galactic center, while obeying the current bounds coming from direct detection experiments such as XENON100 and CDMSII.

We shortly describe the model in section II by introducing its main ingredients. In section III we discuss in more details the direct and indirect evidences for dark matter as well as our reasonings. Further in section IV we discuss the impact of the Higgs boson search on our results and network them with the Dark Matter problem. Lastly, we present our conclusions.

II. THE 3-3-1 LHN MODEL

Our framework is the $331_{LHN}$ model [16], which is a direct extension of the electroweak sector of the SM. In order to allow the reader to follow our reasonings we will briefly discuss the content of the model hereafter.

A. Fermionic content

Likewise the SM, the leptonic sector is placed with left-handed fields appearing in triplets, $f_{aL} = (\nu^0_L, t^0_L, N^0_L)^T$ transforming as $(1, 3, -1/3)$ and right-handed ones in singlets, $e_{aR}$ as $(1, 1, -1)$ and $N^n_R$ as $(1, 1, 0)$, where $a = 1, 2, 3$ correspond to the three families. In the hadronic sector, the first two families are placed as anti-triplets $Q_{aL} = (d^0_{aL}, -u^0_{aL}, d^0_{aL})^T$ as $(3, 3, 0)$, with $i = 1, 2$, while the third one is arranged as triplet, $Q_{aL} = (u^0_{aL}, d^0_{aL}, u^0_{aL})^T$ as $(3, 3, 1/3)$ and, the right-handed quarks are singlets with hypercharges equal to their electric charges similarly to the SM. The first two and the third family of left-handed quarks are in different representations due to an anomaly cancellation requirement adequately described in previous works [14]. The primed fermions are the exotic ones, singlets under the SM gauge group. Similarly to the SM, all fermions acquire Dirac mass terms through a spontaneous symmetry breaking mechanism in the Higgs sector presented hereunder.

B. Scalar content

It was noticed that by introducing a global symmetry $U(1)_G$ where,

$$G(\tilde{N}_{L/R}, \tilde{u}_{3L/R}, \tilde{d}_{3L/R}, V_\mu, U^0_\mu, U^0_L, \chi^0, \chi^-, \eta^0, \rho^-, \sigma^0) = +1,$$

that we could avoid undesirable mixings in the gauge and scalar sector and, in addition, obtain the lightest particle charged under this symmetry to be stable. All this procedure was already discussed in details in Ref. [19], hence we skip it here. In summary, we introduce three scalar triplets, namely,

$$\chi = (\chi^0, \chi^-, \chi^0)^T,$$

$$\rho = (\rho^+, \rho^0, \rho^-)^T,$$

$$\eta = (\eta^0, \eta^-, \eta^0)^T,$$

along with the following Yukawa Lagrangian,

$$-L^Y = f_{ij} Q^v_{iL} \chi^v a_{jR} + f_{13} Q^v_{1L} \chi^v a_{3R} + g_{5a} Q^v_{L} \eta^v a_{R} + h_{3a} Q^v_{3L} \eta^v a_{R} + g_{5a} Q^v_{L} \rho a_{R} + h_{5a} Q^v_{L} \rho a_{R} + G_{ab} \tilde{f}_{aL} \rho e _{bR} + g_{ab} \tilde{f}_{aL} \chi_{N^b} + H.c.,$$

where the triplets $\eta$ and $\chi$ both transforming as $(1, 3, -1/3)$ and $\rho$ as $(1, 3, 2/3)$ and in Eq. $6$ we are using the family indexes $i = 1, 2$ and $a = 1, 2, 3$.

For our analyses, the most important feature in this model is that the $U(1)_G$ symmetry implies that the charged particles under this symmetry are produced in pairs, like R-parity in supersymmetric theories [20], and hence the lightest typical 331LHN model’s particle will be stable. In this way the model can provide two (non-simultaneous) WIMP candidates, $N_1$ and $\Phi$, where $N_1$ is a heavy neutrino and $\Phi$ is a complex neutral scalar, which arises from the combination of the $\chi^0$ and $\eta^0$ scalar fields after the diagonalization procedure [16]. Here we will explore only the case where the scalar $\Phi$ is the dark matter candidate. The reason relies on the fact that the other possible WIMP, $N_1$, has an excluded WIMP-nucleon cross section in the low mass regime, which is exactly the region of mass we are interested in this work. All this being said, we will use the terminology WIMP to refer to our scalar $\Phi$ from now on. In the next section we will investigate the status of our model with respect to the direct and indirect detection searches of dark matter.

III. DIRECT AND INDIRECT DETECTION

Among the CDM candidates, the WIMPs are the most promising ones for providing a thermal cross section roughly at the electroweak scale, naturally leading to the appropriate relic density, as well as because the current and next generation of direct and indirect detection experiments are sensitive to the parameter space where most of the theoretical models rely on. Before examining the status of our model concerning those searches, we will scan the parameter space of the model...
and check if our WIMP can account for the total observed dark matter abundance by computing,

$$\Omega h^2 = 2.742 \times 10^8 \frac{M_{WIMP}}{\text{GeV}} Y(T_0),$$  \hspace{1cm} (4)

where $Y(T_0)$ is the number density over entropy evaluated today.

We used the Micromegas package where we implemented the model in, to take into account all the processes which contribute to the relic abundance of our WIMP, $\Phi$, automatically [21]. These processes were explicitly exhibited in Ref. [19]. In FIG. 1 we show the abundance of the WIMP as a function of its mass and in FIG. 2 as a function of the mass of Higgs boson in the low mass WIMP regime, $M_{WIMP} < 60 \text{ GeV}$.

From FIG. 1 we can clearly see that our model has a large region where our WIMP, $\Phi$, provides the right abundance according to WMAP7 [22]. From FIG. 2 we cannot see any bias towards a light Higgs boson ($M_H < 130 \text{ GeV}$) and therefore by looking at the abundance dependence on the Higgs boson mass only, we cannot extract any information relevant to the Higgs boson search differently from some doublet Higgs models [23]. Now that we have confirmed that our dark matter candidate can reproduce the right abundance, we will investigate if our model is also consistent with current limits from direct detection experiments.

Since we have a flux of WIMPS surrounding us we expect to observe these WIMPs by detecting WIMP-nucleon scatterings in underground detectors. The measured quantities vary according to the detector technology, be that as it may, after making some assumptions concerning the dark matter distribution, all of them convert their results into the simple cross section (in the spin-independent case),

$$\sigma_0 = \frac{4 \mu^2}{\pi} (Z f_p + (A - Z) f_n)^2,$$  \hspace{1cm} (5)

where $Z$ is the atomic number, $A$ is the atomic mass and $f_p$ and $f_n$ are effective couplings with protons and neutrons, respectively, and depends on the particle physics input of a given model. It is important to emphasize that these couplings are obtained numerically in our model by the MicrOMEGAs package by following the recipe described in Ref. [21].

As aforementioned, the direct detection signals observed by CoGeNT, CRESST and DAMA may not be due to WIMP scatterings, so under the null hypothesis we are only concerned whether our WIMP candidate has a WIMP-nucleon cross section below the current bounds.

In FIG. 3 we have plotted the WIMP-nucleon cross section as function of the WIMP mass. Green (blue) scatter refer to points where the WIMP provides the correct abundance (is under abundant). Correct abundance means $0.098 \leq \Omega h^2 \leq 0.122$ while the under abundant regime is for $0.01 \leq \Omega h^2 \leq 0.098$.

In FIG. 3 we have plotted the WIMP-nucleon cross section as function of the WIMP and Higgs boson masses, respectively. It may be noticed that the majority of the points are excluded by the XENON100 experiment, however we still have a worthwhile region which is completely consistent with the current limits. It is important to emphasize though, that the ongoing SuperCDMS at SNOWLAB, which will have a larger exposure by increasing the mass of the detector plus a
better handle in discriminating surface events for implement-
ing the new izip Germanium detectors, and the XENON1T for
ing better statistics.

Center would be one of the best place to search for, since it
has been thought that if a sizable fraction of dark matter par-
search for dark matter annihilations in our neighborhood. It
limits by roughly an order of magnitude.

In order to pin down the properties of the dark matter parti-
cle and find out the nature of the dark matter, we should also
model in the near future, since they expect to improve their
the correct abundance (is under abundant). Correct abundance means
of events (events with less contamination of cosmic rays), a
group has concluded that after subtracting the point source
emission and the cosmic rays background, a residual emi-
sion from the inner 5 degrees surrounding the Galactic Center
was present \[15\], which is in good agreement with previous
works \[4\]. A number of proposals have been put forth to explain
this gamma-ray emission. Since the morphology of the
gamma-ray emission is not entirely point like, the black
hole hypothesis might be ruled out, and because 44 out of
46 of the resolved millisecond pulsars by Fermi-LAT have
a spectrum index larger than one, is somewhat unlikely to
explain this gamma-ray emission through millisecond pul-
sars, because in order to explain this observed gamma-ray flux
a large population of pulsars with a hard spectral index (1.0)
would be required. As we aforementioned this is not sup-
ported by the current data. By using a Navarro-Frank-White
(NFW) \[21\] profile with an inner slope of $\gamma = 1.3$, which is
suggested by cosmological simulations of Milky Way sized halos
\[25\], it was concluded that 70% up to 100% of this
gamma-ray emission is due to dark matter annihilations.

In order to explain this gamma-ray emission a dark matter par-
ticle should annihilate mainly to $b \bar{b}$ and have a mass in the
$\sim (15 - 45)$ GeV range as well as a thermally averaged an-
nihilation cross section of $10^{-26} \text{cm}^3/\text{s}$ represented in
the green region in FIG. 5. In FIG. 5 we show the thermal
cross section of our WIMP candidate as function of its mass
for the case that it annihilates dominantly to $b \bar{b}$ (> 50%)
From FIG. 5 we notice that our WIMP might be the ori-
gin of the gamma-ray emission from the GC and, at the
same time, explain the dark matter abundance indicated by
WMAP7 within the $(25 \text{ GeV} \leq M_{\text{WIMP}} \leq 40 \text{ GeV})$ mass
range as well as that we cannot conclude anything concern-
ing the dependence on the Higgs mass once the three regions:
114 GeV $\leq M_H \leq 116$ GeV, 129 GeV $\leq M_H \leq 131$ GeV
and 149 GeV $\leq M_H \leq 151$ GeV provide an equality good fit
to the favored region to explain the gamma-ray emission from
the GC.

By analyzing the Fermi-LAT data from August 4th, 2008
and August 3rd, 2011 and using the ULTRACLEAN class
of events (events with less contamination of cosmic rays), a
has concluded that after subtracting the point source
emission and the cosmic rays background, a residual emi-
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was present \[15\], which is in good agreement with previous
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to the favored region to explain the gamma-ray emission from
the GC.

So far we have proved that our model is consistent with
the current measurements regarding direct detection on the
WIMP-nucleon cross section in the low mass regime as well
as reproduce the right abundance indicated by WMAP7. Fur-
thermore we have shown that our model has a scalar WIMP,
namely $\Phi$, which can explain at least the majority of gamma-
ray emission coming from the GC. Now we will explore the
complementarity of the ongoing Higgs boson search with the
results we have discussed previously.

\section{Higgs Connection}

Since we are at the LHC era the complementarity has be-
come a promising and achievable way to shed some light in

\footnote{By modifying the main code in MicrOMEGAs we where able to store only
the points where the annihilation to $b \bar{b}$ was the dominant one.}
new physics models and, most importantly, disentangle them from other models. Therefore, we will network the ongoing Higgs measurements with the gamma-ray emission from the Galactic center and the bound coming from leading direct detection experiments, CDMS and XENON100. The Higgs boson is the only particle predicted by the SM of particle physics that has not yet been experimentally observed. Its observation would be a major step forward in our understanding of how particles acquire mass. Conversely, not finding the SM Higgs boson at the LHC and TEVATRON would be very intriguing and would lead to a greater focus on alternative theories that extend beyond the SM, with associated Higgs-like particles such as the 331 class of models. While at TEVATRON the Higgs associated production with $b\bar{b}$ in the final state is the most important channel to look for the Higgs, at the LHC is the Higgs production via gluon fusion with $\gamma\gamma$ in the final state. The latter because of its great invariant mass resolution and efficient background rejection. Another channel that has been pursued is the $\tau\bar{\tau}$, for providing a good signal to noise ratio [24]. Since previous and current collider experiments have not observed any mild excess consistent with a SM model Higgs boson, LEPII, TEVATRON and LHC have excluded the mass range $M_H < 115$ GeV and $M_H = 127 - 600$ GeV for a SM Higgs boson. This plateau can be interestingly explained if the Higgs boson decays dominantly to a pair of DM particles, particularly WIMPs [27]. This is exactly what happens in our model for the case that $M_{WIMP} < 60$ GeV. In FIG. 5 we exhibit the branching ratio for the Higgs boson into a pair of WIMPs as a function of the WIMP mass for different Higgs masses (see analytical expressions in Appendix 4). We can confirm from FIG. 5 that the Higgs boson decays with a branching ratio larger than 90% into WIMPs. For the case that $M_{WIMP} = 20$ GeV and $M_H = 125$ GeV we obtained $BR(H \rightarrow \gamma\gamma) \simeq 2.9 \times 10^{-5}$ and $BR(H \rightarrow b\bar{b}) \simeq 1.4 \times 10^{-2}$, and $BR(H \rightarrow \tau\bar{\tau}) \simeq 7.9 \times 10^{-4}$.

However this scenario would require an even more strug-
FIG. 7. Ratio of the branching ratios $H \rightarrow \gamma\gamma$ in the 331 model and in the SM for the case that $M_{WIMP} > 60$ GeV.

FIG. 8. Ratio of the branching ratios $H \rightarrow b\bar{b}$ in the 331 model and in the SM for the case that $M_{WIMP} > 60$ GeV.

FIG. 9. Ratio of the branching ratios $H \rightarrow \tau\bar{\tau}$ in the 331 model and in the SM for the case that $M_{WIMP} > 60$ GeV.

Moreover we have discussed the possibility of explaining 70% up to 100% of the Fermi-LAT observed gamma-ray emission from the galactic center through a dominant annihilation into $b\bar{b}$ final states with a WIMP mass in the $(25 - 40)$ GeV range in FIG. 5, showing that the 331LHN model has a large amount of parameter space to offer a plausible explanation for these events.

Additionally, we have networked the struggling probe for WIMPs in underground experiments with the ongoing Higgs boson search at Tevatron and LHC. We have concluded that, in case our WIMP explains the gamma-ray emission from the galactic center, the Higgs boson decays primarily to a pair of WIMPs. In particular in FIG. 3 we have exhibited that, $BR(H \rightarrow 2WIMPs) \geq 90\%$, with $BR(H \rightarrow \gamma\gamma) \simeq 2.9 \times 10^{-5}$, $BR(H \rightarrow b\bar{b}) \simeq 1.4 \times 10^{-2}$, and $BR(H \rightarrow \tau\bar{\tau}) \simeq 7.9 \times 10^{-4}$, for the case that $M_H = 125$ GeV and $M_{WIMP} = 20$ GeV. It is important to emphasize that the branching into a pair of photons in 331LHN, for example, is roughly two orders of magnitude smaller than the SM. Furthermore, we have obtained that in the scenario where $M_{WIMP} < 60$ GeV, we could explain the non-observation of any mild excess at Tevatron and LHC, as well as link the nature of the dark matter with Higgs boson paradigm, which soon will unveil where the physics beyond the SM lies on. This would demand additional efforts on the side of collider search since the branching ratio for Higgs decay into SM particles would be very suppressed in the 331LHN model.

Notwithstanding, if the recent modest excesses measured at Tevatron and LHC are confirmed in the near future and they turn out to be consistent with a SM Higgs, this completely rules out the DM hypothesis to explain the gamma-ray emission from GC in our model, once this implies that $M_{WIMP} > 60$ GeV and only in this mass range our model recovers the SM predictions. Lastly, we have shown in FIGS. 3 - 5 that under the latter hypothesis our model predicts no deviations from the SM Higgs boson decay channels into $\gamma\gamma$, $b\bar{b}$, and $\tau\bar{\tau}$, which are the most promising channels for searching a light Higgs boson.

We also remark that for the regime where $M_{WIMP} < M_Z/2$ no bound can be derived regarding the invisible width of the Z boson, because all decay modes which involve a WIMP in the final state have at least one 331 particle which is much heavier than the Z boson.

V. CONCLUSIONS

We have probed the low mass WIMP window, $M_{WIMP} < 60$ GeV, in the 331LHN model and checked if it can reproduce the right abundance of dark matter inferred by WMAP7 satellite in FIGS. 1 - 2. Subsequently, we have shown that a sizable region of the parameter space is constrained by the current bounds derived by the XENON100 and CDMSII collaborations and a largish and promising region is completely consistent with those in FIGS. 3 - 4. The upcoming XENON1T and SuperCDMS projected limits which are expected to improve by one order of magnitude their limits will be sensitive enough to further restrict our model or reveal its plausibility.

ACKNOWLEDGMENTS

We would like to thank Chris Kelso, Dan Hooper, LianTao, Daniele Alves, A. Semenov as well as A. G. Dias for valuable discussions and/or comments. CASP and PSRS are supported by the Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq), FSQ by Coordenação de Aperfeiçoamento de Pessoal de Nível Superior (CAPES) and DR has been supported in part by UdeA/2011 grant: IN1614-CE.
Appendix A

The invisible width \( H \to WIMP + WIMP \) in our model is given by,

\[
\Gamma_{WIMP} = \frac{\lambda_{H\Phi\Phi}^2}{32\pi} \sqrt{\frac{M_H^2 - 4M_W^2}{M_H^2}} \frac{v^2}{M_W^2}, \quad (A1)
\]

where,

\[
\lambda_{H\Phi\Phi} = \frac{-1}{\sqrt{2}(1 + \frac{v^2}{M_W^2})} (3\lambda_2 v + \frac{v^3}{2V^2} + \lambda_7 \frac{v^3}{V^2} + \lambda_7 v + \frac{v}{2}). \quad (A2)
\]

WIMP refers to the scalar \( \Phi \) in the model. Here \( v = \sqrt{\frac{v^2}{2}} \), and \( V \) is the scale of symmetry breaking of the 331 model, which we assume to be \( \gtrsim 1 \text{ TeV} \). Different values for \( V \) produce similar results.

It is important to notice that these couplings in Eq. (A2) are determined by the mass of the WIMP and Higgs boson, through the following equations,

\[
M_{WIMP}^2 = \frac{\lambda_7 + 1/2}{2} (v^2 + V^2), \quad (A3)
\]

\[
M_H^2 = 3\lambda_2 v. \quad (A4)
\]

Therefore, fixing \( V \) in few TeV and plugging Eq. (A2) - (A4) into Eq. (A1), we can express the invisible width as a function of the Higgs boson and WIMP masses only. For \( M_H \sim 120 \text{ GeV} \), and \( 20 \text{ GeV} \leq M_{WIMP} \leq 60 \text{ GeV} \), the WIMP is the heaviest particle which the Higgs can decay to. For this reason the branching ratio of the Higgs boson into a pair of WIMPs is dominant in this mass range as we may observe in Fig. 3.

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