Photogyrotactic Concentration of a Population of Swimming Microalgae Across a Porous Layer

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The light environment controls the swimming of microalgae through a light-seeking and avoiding behaviour, which is known as phototaxis. In this work, we exploit phototaxis to control the migration and concentration of populations of the soil microalga *Chlamydomonas reinhardtii*. By imaging a suspension of these microalgae in a cuvette illuminated from above by blue light, we study how phototaxis changes the stability of the suspension and demonstrate how a thin, porous layer at the top of the cuvette prevents phototaxing microalgae from sinking, leading to the up-concentration of the microalgae in the region above the porous layer. We discuss the potential implications of our findings for microalgae in biotechnological applications and the natural environment.

Keywords: microswimmers, microalgae, phototaxis, light environment, porous media, biotechnology

1 INTRODUCTION

Environmental stimuli, such as chemical gradients, gravity, light and flow shear, bias the motion of swimming microorganisms [1–3]. At the level of a population, these biases cause the formation of spectacular, often macroscopic, patterns. Inasmuch as they cause cells to congregate and interact, these patterns can be considered a form of social behaviour. Paradigmatic examples of pattern formation in swimming microbes are the waves exhibited by bacteria [4, 5] and slime mold [6] sensing chemical gradients (chemotaxis), or the bioconvection patterns formed by ciliates and microalgae [7], responding to a combination of gravity and flow shear (gyrotaxis). More specifically, the latter is a bias resulting from the combination of a torque on a swimmer due to shear in the flow and one due to gravity, caused by asymmetry in body shape, mass distribution and/or between body and flagella [8].

Recent decades have seen a marked increase in the mechanistic understanding of how biases act at the individual swimmer level and how this affects macroscopic patterns. For example, mathematical models of flowing and dispersing gyrotactic suspensions of microalgae [9–12] have been compared with measurements of algae in an uniformly rotating flow [12], sheared bioconvection patterns [13], populations of microalgae dispersing in pipe flow [14], and laboratory versions of oceanic thin layers [15]. For comprehensive summaries of current work, we refer the reader to reviews covering recent progress in the physics of swimming microbes [16, 17] and bioconvection [7]. This area of research is also closely related to active matter [18] comprising biological swimmers, as we have just described, but also synthetic [19] and biohybrid ones [20–22].

In this study, we focus on how light can be used to control and concentrate a suspension of *Chlamydomonas reinhardtii* microalgae. The bias of swimming by light is known as phototaxis and is an adaptation that allows *C. reinhardtii* and other photosynthetic microorganisms to find optimal
levels of light needed to grow [23, 24]. Recent studies have demonstrated how exposing a suspension of microalgae to light can dramatically alter the patterns they form, and even generate new ones [25]. In the absence of phototactic stimulation, bioconvection patterns form in shallow layer suspensions, e.g., a thin layer of fluid in a Petri dish, as a result of the tendency of microalgae to swim upwards (gravitaxis) and form a dense layer of cells (denser than the fluid they are suspended in) at the top of the suspension [7]. This is unstable and results in sinking "plumes," which drive a bioconvective pattern, reinforced by the cells' response to the flow (gyrotaxis), which enhances the instability by driving cells towards downwelling plumes. Bees and Williams investigated how white light from above and below a suspension of the microalgae *Chlamydomonas augustae* in a Petri dish alters the stability of bioconvection patterns, quantified by measuring the dominant initial pattern wavelength [26]. As well as changes to existing bioconvection patterns, recent investigations have also explored how shining light into a suspension can stimulate patterns that would not otherwise be there. For example, bioconvection patterns for the microalgae *Euglena gracilis* were induced by illuminating a Hele-Shaw cell from below [27]. In the absence of light, the patterns vanished. A study by Arrieta et al. also demonstrated how quickly bioconvective structures can be created, and even reconfigured by light, using it to generate "blinking plumes"; the study also provided a model of this (ignoring gyrotactic effects), and reported good agreement with the experimental observations [28].

Aside from some of the studies above, several investigations in the literature have provided theoretical analyses of bioconvection in the presence of phototaxis. These have recently been reviewed comprehensively [7, 25]. We will discuss briefly here only the model by Williams and Bees [26], which includes phototactic and gyrotactic effects, and encompasses several simpler models that have been recently proposed. The model equations, summarized in Supplementary Appendix SA, describe the coupled dynamics of fluid flow, described by a Navier-Stokes equation, and a population of swimmers, described by a continuity equation. The probability density function (PDF) for the swimmer orientation obeys a Fokker-Planck equation, with a deterministic bias due to the combined action of flow, gravity and light. Taking moments of this PDF provides the mean swimming velocity and diffusivity in the continuity equation. Williams and Bees considered three alternative models to describe the effect of phototaxis on the swimmers [26]. In model A, the speed of the cells is dependent on light intensity (photokinesis), while gravitaxis and gyrotaxis are not affected. In model B, light causes a change in the bottom-heaviness of the cells, inducing an effective gravi/gyrotactic torque. In model C, cells respond directly to an effective torque due to light, dependent either of the light direction or the gradient of its intensity (the latter was also used by [23, 28]). Williams and Bees used their model to predict the stability of bioconvection patterns for a suspension illuminated from above and below, in qualitative agreement with the experiments with *C. augustae* microalgae in a Petri dish mentioned above [29].

Our study combines a photogyrotactic suspension with porous media, materials with voids through which microbes can swim. In the environment, these can occur as the spaces between particles in soils [30]; in the laboratory they can be patterned using microfluidics, or assembled using gels or beads. There has been much recent interest in the behaviour of swimming microorganisms, such as bacteria, in porous media [31]. A few recent studies have also considered how the transport of microalgae is altered in porous chambers [32] and microfluidic arrays [33], including the deflection of negatively phototactic swimmers through obstacle arrays [34].

Thus, it is known how porous media change the transport of microswimmers and it is well established that light perturbs, and drives instabilities in, suspensions of phototactic microalgae, visibly causing the concentration of cells. However, the systematic concentration of microalgae at a given location exploiting photogyrotaxis, which was suggested by Kessler as early as 1982 [35], has hitherto not been demonstrated. In this study, we aim to show that a unique combination of phototaxis and porous media permits the concentration of microalgae at a given location in a container. We report the first "milliliter-scale" experiments demonstrating how photogyrotactic microalgae can be concentrated above a porous layer of beads overlaid onto a metal mesh. We also observe interesting photogyrotactic instabilities and accumulations in the suspension, which have not been previously reported. An "essential" model to qualitatively account for the temporal evolution of the average concentration of cells above the porous layer and for their initial spatial distribution is also developed, leaving a full theoretical analysis of the photogyrotactic dynamics leading to this concentration for future work. Finally, we discuss how, a scaled-up version of our set-up could provide the basis for a new and efficient method to harvest swimming microalgae industrially. This is desirable since harvesting microalgae industrially is expensive (up to 20–30% of the total production costs [36]), and represents a bottleneck in the production of bioproducts from microalgae.

### 2 MATERIALS AND METHODS

#### 2.1 Experimental Methods

We used the wild-type algal strain *Chlamydomonas reinhardtii* (CC125) for our studies. Single colonies of these algae were picked from slant cultures and inoculated into Tris-minimal growth media (Supplemental Material Section S1). These media are based on the standard TAP medium [37], but omit acetic acid and HCl is used to titrate to pH 7, and were chosen to ensure purely photosynthetic growth of cells so that they would be synchronised to light-dark cycles, following [38]. Indeed, liquid cultures of the microalgae were then grown in a 14:10 h light-dark cycle on a rotary shaker at 100 rpm and continuously bubbled with air, as in [38]. The shaking incubator (Infors Minintron) was maintained at a temperature of 25°C, and provided photosynthetically active radiation (PAR) at 315–365 μmol/m²s, as measured with a PAR meter (Skye SKP200). It took around 7–10 days for a culture to reach a concentration of 1–2 million cells/mL. Thereafter, it was sub-cultured by mixing 10 mL of grown algae into 140 mL of fresh Tris-minimal media until the cell count, measured with a Z2
Coulter counter (Beckman Coulter, Brea, CA), reached 1.5 million/mL; this took about a week. Subsequently, algae were diluted everyday by replacing 50 ml of the culture with fresh media. This protocol maintains the algal count between 1.2 – 1.5 million/mL with mean diameter of 4.5 – 5 μm (estimated by using the Coulter counter); the subcultures can be used for 10 – 15 days. Care was taken to do experiments with microalgae harvested during the light phase of the growing cycle to avoid variations in the swimming parameters, and in particular the swimming speed, which have been observed at the onset the dark phase [38]. All the experiments were carried out in square plastic cuvettes of external dimensions 12.5 × 12.5 × 45 mm³ (Sigma-Aldrich, filling volume 2.5 ml) filled with 2 ml of algal suspension. The imaging was performed using a monochrome CMOS camera (Pointgrey, Grasshopper3 GS3-U3-23S6M) fitted with a macro lens (Sigma 17–70 mm f2.8-4). The cuvette was illuminated from the side by a red (660 nm) square 100 × 100 mm LED array (Advanced Illumination BL1960, Rochester, VT, United States), as shown in Figure 1A. This illumination was used as it allowed to image the suspension laterally without triggering a phototactic response [3]. The concentration of microalgae in the cuvette was estimated from the transmitted light intensity across the short dimension of the cuvette by microalgae in the cuvette was estimated from the transmitted light intensity recorded by the camera (measured in arbitrary units, a. u.) can be converted into algal concentration (million/mL) from the calibration curve shown in Supplementary Figure S1. The intensity decays as I = I₀ exp (−A.C), where I₀ = 179 is the intensity in arbitrary units in the presence of cuvette containing just Tris-min medium, A = 0.22 is the attenuation coefficient and C is the algal concentration in million/mL. This exponential decay provides a mapping to concentration, with an excellent fit for intensity data higher than 50 a.u., and an R-squared value of 0.99 for a fit across the range of values (see Supplementary Figure S1). In the experiments described below, the swimmer concentration was then quantified from images by first measuring integrated pixel intensity in selected regions (see e.g., Supplementary Figure S2) of the cuvette using ImageJ, and then mapping to actual concentration values using the calibration curve just described.

For the phototaxis experiments, a blue LED (Thorlabs M470L2, nominal wavelength 470 nm) is mounted above the cuvette at a distance of 47 mm from its base. Using a PAR meter, the light intensity at the base of cuvette containing only the media was 16 – 18 μmol/m²s, whereas the intensity immediately below the LED is 150 – 160 μmol/m²s. The cuvette is separated into an upper “harvest” and a lower “reservoir” region by a porous layer of glass beads. The latter was achieved by folding a rectangular wire mesh so that it attaches to a cuvette, and overlaying it with glass beads of diameter 425 – 600 μm and various weights, as shown in Figure 1B. Glass beads of diameter 425 – 600 μm, provide a porous medium with spacings large (~50 – 200 μm) compared to the size of individual algae (<10 μm), so that the latter could easily move through the pores. To initialize experiments, first an empty cuvette was filled with an algal suspension approximately up to the mesh height and thereafter the mesh was installed. To make a porous layer of various thicknesses, beads of appropriate weight were placed over the mesh. Finally, more algal suspension was poured from the top to create a harvest region of height ≈ 0.5 cm. The experiments reported below also considered the case of a bare mesh with no beads.

2.2 Essential Model of Concentration

We present here the details of a simplified model of the concentration of swimming microalgae into the upper “harvest” region by light. The model describes the case of a suspension of microalgae with a porous layer near the top (mesh + beads), as shown in Figure 1, and we shall also apply it below to

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**FIGURE 1** Schematic showing lower reservoir and upper harvest regions, separated by a wire mesh overlaid with beads: the porous layer. (A) A blue LED is mounted on the top of the cuvette to create a phototactic bias. For imaging the suspension and concentration calibration, a deep red LED illuminate the cuvette from the side (deep red light does not elicit phototaxis [3]). (B) Glass beads of diameter 425 – 600 μm were used to create the porous layer, 70 mg of bead results in single layer, 200 mg–2 to 3 layers, and 400 mg–4 to 5 layers, respectively.
consider the case of a bare mesh. For the mesh + beads case, the suspension of microalgae is divided into three regions, an upper harvest region (u), a porous layer region (p) and a lower “reservoir” region (l). Photogyrotactic migration delivers microalgae to the upper region from the lower region through the porous region. As evident from our results and discussion (see Section 3.4, 4 below), the dynamics underpinning the concentration are complex; the challenge of describing them with a full photogyrotactic model is beyond the scope of this paper. Instead, we seek here to formulate a model to capture the essential features of the concentration process into the upper region. We make the reasonable simplifying assumption that: 1) the average concentrations in the upper, porous and lower regions evolve slowly compared to the observed photogyrotactic dynamics; we consider here spatial and temporal variations separately, and assume a steady state for the fast dynamics in the upper region. We further assume that 2) phototactic migration is the dominant process and brings cells to the upper region. We further assume that 2) phototactic swimming speed of the microalgae within the porous layer, but the swimming direction continues on average to be upwardly directed by phototaxis. In the upper harvest region, as well as the average concentration dynamics, we also consider a 0th order spatial model of phototactic concentration. To set this up, as assumed above, we posit that there is a separation of timescales between the migration of cells from the lower region (slow) and the redistribution of cells in the upper region (fast). We further assume that: 5) the effect of flow is negligible prior to the formation of the plume from the upper surface (see Figure 4B); 6) upward phototactic swimming at the maximum speed \( V_s \), and diffusion dominate the fast suspension dynamics (gyrotactic effects are negligible); 7) diffusion is assumed approximately isotropic; 8) the meniscus at the top of the suspension is flat (any effects of curvature are neglected).

With the assumptions above, denoting by \( \bar{c}_i \) the average concentrations in regions \( i = u, p, l \) for the upper, porous and lower regions, respectively, and with A the cross-sectional area of the cuvette, the average cell numbers \( N_i \) in the three regions evolve according to the following balance equations:

\[
\frac{dN_i}{dt} = - AV_s \bar{c}_i, \tag{1a}
\]

\[
\frac{dN_p}{dt} = AV_s \bar{c}_i - AV_{eff} \bar{c}_p, \tag{1b}
\]

\[
\frac{dN_u}{dt} = AV_{eff} \bar{c}_p. \tag{1c}
\]

Equation 1a describes the loss of cells from the lower region due to the phototactic flux of cells, of concentration \( \bar{c}_i \), swimming into the porous region at speed \( V_s \). Correspondingly, the porous region, as described by Equation 1b, gains an equal and opposite flux. This region also has a loss term due to cells, of concentration \( \bar{c}_p \), swimming at a speed \( V_{eff} \) into the upper region. The upper harvest region, as shown in Equation 1c, has an equal and opposite gain. The speed \( V_{eff} \) is the effective swimming speed of the microalgae within the porous layer, which is given by \[^{[39]}\]

\[
V_{eff} = V_s \frac{\tau_c}{\tau} + \frac{\lambda}{\tau}, \tag{2}
\]

where \( V_s \) is the “free” mean swimming speed of the microalgae, \( \tau_c = \frac{1}{\alpha} \) is the time between collisions with the beads in the porous layer, and \( \lambda \) is the swimmer mean free path. The timescale \( \tau = \tau_c + \tau_R \) is the total porous travel time, including the residence time \( \tau_R \) that a swimmer spends at an obstacle. These parameters were recently measured experimentally for \( C. \) reinhardtii (see Table 1). To express system (1) in terms of concentrations only, we note that the mean number of cells in regions \( i = u, p, l \) can be written as \( N_i = Ah_i \bar{c}_i \), where, as above, \( A \) is the cross-sectional area of the cuvette, and \( h_i, \bar{c}_i \) are the height and mean concentration in region \( i \), respectively. Substituting into (1), we thus obtain, dividing both sides by the respective \( h_i \),

\[
\frac{d\bar{c}_i}{dt} = -\alpha \bar{c}_i, \tag{3a}
\]

\[
\frac{d\bar{c}_p}{dt} = \beta \bar{c}_i - \gamma \bar{c}_p, \tag{3b}
\]

\[
\frac{d\bar{c}_u}{dt} = \delta \bar{c}_p, \tag{3c}
\]

where we have defined the upsweeping rate constants \( \alpha = V_s/h_i, \beta = V_s/h_p, \gamma = V_{eff}/h_p \) and \( \delta = V_{eff}/h_u \). Equation 3a has immediate solution \( \bar{c}_i(t) = k_0 e^{-\alpha t} \), where \( k_0 \) is a constant. The system of Eq. 3 can then be solved analytically by substituting this solution into (3b), and the resulting solution (e.g. by using the integrating factor \( \gamma e^\gamma t \)) into (3c). Applying the initial conditions \( \bar{c}_i(0) = \bar{c}_i^0, \bar{c}_p(0) = \bar{c}_p^0 \) and \( \bar{c}_u(0) = \bar{c}_u^0 \), where \( \bar{c}_i^0 \) represent the initial average concentrations in the three regions, we find:

\[
\bar{c}_i(t) = \bar{c}_i^0 e^{-\alpha t}, \tag{4a}
\]

\[
\bar{c}_p(t) = \bar{c}_i^0 \frac{\beta}{\gamma - \alpha} e^{-\alpha t} + \left( \bar{c}_i^0 - \bar{c}_i^0 \frac{\beta}{\gamma - \alpha} \right) e^{-\gamma t}, \tag{4b}
\]

\[
\bar{c}_u(t) = \bar{c}_u^0 - \bar{c}_i^0 \frac{\beta \delta}{\alpha(\gamma - \alpha)} e^{-\alpha t} - \left( \bar{c}_p^0 - \bar{c}_i^0 \frac{\beta}{\gamma - \alpha} \right) e^{-\gamma t}, \tag{4c}
\]

where we have defined the long-time concentration in the upper region as

\[
\bar{c}_u^{\infty} = \bar{c}_i^0 + \bar{c}_p^0 \frac{\delta}{\gamma} + \bar{c}_i^0 \frac{\beta \delta}{\alpha \gamma} \frac{h_u}{h_i} + \frac{h_p}{h_u} + \frac{h_l}{h_u}, \tag{5}
\]

and where, recalling the definitions of the constants \( \alpha, \beta, \gamma \) and \( \delta \), we have re-written \( \bar{c}_u^{\infty} \) in terms of the heights of the regions. Thus, it is clear from Equation 5 that, in this simple model, the long-time (maximum) concentration in the upper region occurs when all swimmers from the porous and lower regions have concentrated themselves into the upper region.

We also consider the “mesh-only” case (without a porous layer of beads). The derivation, shown in Supplementary Appendix SB,
is similar and provides the temporal evolution of the mean concentrations as
\[ \tilde{c}_m(t) = \tilde{c}_m^0 e^{-\alpha t}, \] (6a)
\[ \tilde{c}_p(t) = \tilde{c}_p^0 - \tilde{c}_m^0 \frac{\eta}{\alpha} e^{-\alpha t}, \] (6b)
where the superscript ‘m’ denotes concentrations in the mesh-only case, and we have defined the rate constants \( \alpha = V_s/h_l \), which is as in the porous layer model (but takes a slightly different value because of the different value of \( h_l \), see Supplementary Table S2), and \( \eta = V_s/h_u \). For the mesh-only case the concentration in the upper region at long times is given by
\[ \tilde{c}_u^\text{max} = \tilde{c}_u^0 + \tilde{c}_j^0 \frac{h_l}{h_u}, \] (7)

This corresponds to the concentration in the upper region occurring when all microalgae have swum into it from the lower region.

In the upper region we observe that cells accumulate strongly at the surface. To describe this, we can use a simplification of the Williams and Bees model [26]. By virtue of assumptions 5–8) above, as shown in Supplementary Appendix SA, the full swimmer conservation equation in the Williams and Bees model simplifies to:
\[ \frac{\partial c_u}{\partial t} = -\nabla \cdot [V_s c_u k - D \nabla c_u], \] (8)
where \( k \) is a unit vector pointing upwards and \( D \) is the diffusivity, approximated as isotropic, by assumption 7) (see Supplementary Appendix SA for more details). By assumption 1), we have a steady state, so that (8) implies
\[ V_s c_u k - D \nabla c_u = \text{const.}, \] (9)

where \( k \) is a unit vector pointing upwards. Imposing a no flux condition at the upper boundary (flat for simplicity, assumption viii) requires \( V_s c_u k - D \nabla c_u \cdot \mathbf{k} = 0 \) on \( z = h_u \), so that Equation 9 becomes
\[ \frac{dc_u}{dz} = \frac{V_s}{D} c_u, \] (10)
which integrates to
\[ c_u = k_1 e^{\frac{V_s}{D} z}, \] (11)
where we have defined a characteristic phototactic accumulation lengthscale \( l_p = \frac{D}{V_s} \), and where \( k_1 \) is a constant. To find the latter, we use the fact that the average background concentration is given by \( c_u \), that is, taking \( z = 0 \) at the bottom of the upper region and \( z = h_u \) at its top, \( c_u = \frac{h_u}{h_l} c_{u,0} \). Thus, integrating Equation 11 gives \( k_1 = c_u \left( e^{l_p/h_u} - 1 \right)^{-1} h_u/l_p \), so that finally the distribution in the upper region is given by
\[ c_u(z, t) = c_u(t) \frac{h_u}{l_p} \frac{e^{\frac{V_s}{D} z}}{e^{\frac{V_s}{D} h_u} - 1}, \] (12)
where that the mean concentration as a function of time, \( c_u(t) \), is provided by Equation 4c.

### 3 RESULTS

#### 3.1 Initial Condition for the Lower Region
Prior to considering the effect of light on a suspension of \emph{C. reinhardtii} placed in the cuvette, we will consider the initial condition of the suspension in the lower reservoir region, which will be the same starting point for all subsequent experiments. With the blue LED light off, microalgae were
mixed into the cuvette and the suspension was allowed to stabilize in the presence of only red illumination from the side (see Figure 1A), which does not elicit a phototactic response (Supplementary Video S1) [3, 40]. The suspension images and profiles are shown as a time-series in Figure 2: over a few minutes, the suspension (initial concentration ∼ 1 million/mL) settles into a distribution where the majority of cells reside at the bottom of the cuvette; a steady distribution is observable beyond 4 min. The gradient in concentration already visible for the concentration profile at t = 0 is due to a lag in transferring the cuvette to the imaging setup after mixing: some settling has already occurred at the first instance of imaging. The steady distribution observed beyond 4 min would, for other species of gyrotactic swimming algae such as *Chlamydomonas augustae* [2], also display features known as “bottom-standing plumes” (see also Figure 1A in [7]). For *C. reinhardtii*, however, the bottom-standing plume structures are not discernible in the images of the cuvette (though plumes can be seen to descend from its sides, see Supplementary Video S1), though they can be seen in a larger container (see Supplementary Figure S3). It is possible that, for this species, the cuvette width is too narrow to give rise to central bottom-standing plume structures.

### 3.2 Free Surface: Bulk Photogyrotactic Instabilities

We consider here the effect of light on a suspension of microalgae in a cuvette when the surface of the suspension is free (the metal mesh applied in the next section has been raised above the surface). This experimental scenario can be seen in Supplementary Video S2, stills of which are shown as the sequence in Figure 3. Initially the blue LED illumination is switched off and the suspension is distributed with the majority of cells at the bottom, as described in the previous section. Then the LED is switched on, and the cells in suspension phototactically respond to the light, migrating upwards toward the surface (Figure 3, t = 3 min). Concomitantly, instabilities arise throughout the suspension, resulting in meandering plumes (Figure 3, t = 3 − 5 min). These are of photogyrotactic origin, as discussed below. In the span of ∼ 6 minutes phototactic migration appears to have delivered many swimmers to the surface, leaving the bulk of the suspension depleted. This surface accumulation is gravitationally unstable because of the negative buoyancy of surface-accumulated cells: it results in the formation of a plume instability seen to originate from the middle of the meniscus of the suspension surface (Figure 3, t = 9 min). The plume structure wiggles around but once formed, is dynamically stable (Figure 3, t = 18 min), delivering cells to the bottom of the container. Once they reach this, the microalgae migrate back up to the surface to join the plume, and so forth. When the light is switched off (Figure 3, t = LED Off + 17 sec, + 3, 6 min), the phototactic migration toward the surface stops and the surface accumulation sinks as a broader, non-meandering plume. This takes the cells to the bottom of the cuvette, where they once more settle into a distribution similar to the initial one.

### 3.3 Mesh: New Phototactic Structures

In this section we consider the case of a metal mesh immersed at the top of the microalgal suspension. As described in the methods, the pore size of the mesh is 350 μm, so individual microalgae (∼ 5 μm in diameter) easily swim through it. A typical experiment is shown in Supplementary Video S3, stills of which are presented as a sequence in Figure 4A (top row). As for the free surface case, blue LED illumination is initially off, and the suspension is distributed with most cells at the bottom (Figure 4A, first still). The LED is then switched on and microalgae migrate upward in response to the light (Figure 4A, t = 3 min). The response is broadly similar to the free surface case, but there are some interesting differences. One such striking difference is that the mesh creates a pattern of light and shadow to which the microalgae visibly respond.
photogytotactically, forming accumulations (‘phototactic curtains’), see Figure 4C. The average width of photogytactic curtain feature is 630 ± 53 μm, nearly twice the mesh pore size, showing that the curtains are not the result of shadowing by the mesh, but genuine photogytactic structures originating from the response of the microalgae to the local light profile. As in the case of a free surface, when the density of cells photogytotactically accumulated at the surface becomes too high, a plume of dense cells forms and sinks. However, viscous resistance caused by the mesh pores prevents the plume from completely sinking beyond the mesh, and instead a cloud-like plume structure is seen to be trapped, hovering above the mesh (Figure 4A, t = 9, 18 min). Not all the plume-cloud is trapped, negative buoyancy is sufficient to cause some of it to escape through the mesh forming a meandering secondary plume, similar in appearance to the one observed in the free surface case (Figure 4A, t = 9, 18 min). While the light is on, these structures appear dynamically stable. As the light is switched off, however, the curtains and cloud structure disperse, cells sink through the mesh, and the escaped plume sinks down straight, again similarly to free surface case (Figure 4A, t = LED Off + 19 sec, + 3, 6 min). This emphasizes the stabilizing influence of phototaxis: none of the observed structures could be possible in the absence of the light. Both mesh and light are critical for supporting the plume-cloud.

3.4 Porous Layers: Stabilization of Photogytactic Structures and Concentration Gain

We next turn to the case where a porous layer is placed on top of the suspension. As described in the Methods, the porous layer consists of glass beads overlaid onto a metal mesh (the same as was used in the previous section). The beads are around 425 – 600 μm in diameter, which results in interparticle spacings ~ 50 – 200 μm (from microscopic observation). Thus, individual algae ~ 5 μm in diameter can swim through the porous layer. We studied the effect of light on suspensions of microalgae overlaid with porous layers, quantified by the weight of the beads placed on the mesh. A typical experiment with a layer weighing 400 mg is shown in Supplementary Video S4, and stills from this video are presented in Figure 4B. As in previous cases, the LED light is initially off and the suspension is distributed with the majority of cells at the bottom (Figure 4B, first still). When the LED is switched on, the initial suspension dynamics are similar to the mesh-only case (Figure 4B, t = 3 – 6 min), displaying instabilities as the microalgae respond to the light (but with no curtains visible). However, for this case, we were also able to observe clusters of cells swimming upwards as waves in response to the light, see Figure 5A for an example. Averaging over five such waves, we found them to have a mean speed of 190 ± 60 μm/s. This is faster than mean swimming speed of individual algal cells, 80 μm/s [38], possibly as a result of advection by upwelling fluid in the lower region of the cuvette generated by the photogytotactic suspension dynamics. The large deviation in the speed of the waves could also be due to the interaction of the waves with other photogytotactic structures and up/downwelling flows in the suspension. Once cells have had time to accumulate in the harvest region and on the surface of the suspension, a plume-cloud structure originating at the low point of the meniscus forms above the porous layer (Figure 4B, t = 9, 18 min). The plume-cloud appears more diffuse than in the mesh case. The time taken for the plume-cloud to arise in 10 out of 12 experiments used for the analysis is between 6 – 10 min from when the LED light is switched on, as shown in Supplementary Figure S4. Unlike the case of the mesh, the plume does not leak through the porous layer into the suspension: in the presence of light, the viscous resistance offered by the porous layer is sufficient to stabilize the plume-cloud. Instead of sinking the plume-cloud is observed to gradually expand into the upper region. Figure 5B charts this expansion. The lateral extent of the plume structure increases the most between 7 and 9 min after the LED has been switched on, when the plume begins to drop and propagate along the porous layer. After that the plume-cloud achieves a steady structure, probably as a result of balance between influx of cells from the surface, where the plume originated at the low point of the meniscus, and loss to the edges of the harvest region (and resorption to the suspension surface by upswimming).

In view of quantifying microalgal concentration in the upper harvest region above the mesh or the mesh + beads porous layer, it is instructive to chart the evolution of the average concentration of the suspension in this region (Supplementary Figure S2). To
identify a porous layer thickness that would not leak into the suspension below, we considered layers of several weights in trial experiments presented in Supplementary Figure S5. We found a general qualitative trend that was similar for all cases: the concentration grows as the light is switched on, and then saturates to a constant value. We focus here quantitatively on the mesh-only case and the “minimally-leaky” mesh + beads (400 mg) case, shown for three repeats in Figures 6A,B, respectively. The averaged profiles are shown in Figure 6C. This makes it clear that the concentration in the upper harvest region of both the mesh and mesh + beads cases, following a dip in concentration due to phototactic accumulation of cells to the upper surface, grows after the LED is switched on and then tends to saturate. The mesh case, however, saturates earlier, probably because of losses to the lower region, such as the plume visible in Figure 4A (9 min). Another interesting quantitative difference between the two cases is the initial rate of concentration, which appears slightly larger for the mesh case. This indicates the concentration process is initially slower when a porous layer is present, than in its absence. As discussed below using the essential model, this makes sense in terms of the microalgae having to make their way through the porous layer, which reduces the swimming speed that sets the concentration rate. The difference in swimming speed will also affect the average time it takes to form the plume, which was measured to be $7.3 \pm 0.6$ min for the mesh case, while it is $8.7 \pm 1.5$ min for mesh + beads (Supplementary Figure S4). When the LED is switched off (Figures 6A–C inset), the concentration in the upper harvest region is seen to rise briefly before steadily falling. This is because, with the light off, the concentrated algal suspension in the harvest region no longer responds phototactically and cells accumulated to the surface are released, sinking down as dense fluid. The increase in concentration due to the cells coming off the surface shows that our measurements likely underestimate the
concentration in the upper harvest region because of cells “hidden” at the surface. This could account, at least in part, for discrepancies with model predictions discussed below. For our setup, the time after switching the LED off is optimal for harvesting the suspension, yielding a harvest concentration ≈ 5 million/mL (gain ≈ 4.2 compared to the initial concentration) for the mesh + beads case, as compared to ≈ 4 million/mL cells for mesh-only (gain ≈ 3.6). This highlights the advantage of concentrating using a porous layer. The latter also slows down the rate at which the cells sink back through to the lower region, which depends on the layer thickness.

Also shown in Figure 6 are profiles charting the temporal evolution of concentration in the lower reservoir region. As for the upper region, we have measured triplicate repeat profiles for the mesh (Figure 6D) and mesh + beads (Figure 6E), and also evaluated averaged profiles (Figure 6F). We see that, after the LED is switched on, the concentration for the mesh and mesh + beads falls, as phototactic swimming into the upper regions depletes the lower region of cells. However, the depletion appears to saturate, and to a higher concentration in the case of mesh-only, reflecting the greater leakiness of the mesh, as discussed below. Insets in Figures 6D–F display how, with the LED off, the concentration in the lower region rises due the influx of cells sinking from the upper regions.

3.5 Essential Model Predictions
We have developed a simple model to capture the essential features of the phototactic concentration dynamics, and evaluate it here using parameters for *C. reinhartii* concentrated using a mesh + beads setup, as shown in Table 1. In Figure 7A, the model prediction using Equation 4c for the average concentration of cells $\bar{c}_u(t)$ in the upper harvest region is shown as a function of time (the concentration process starts at time $t = 0$, “LED on”). Qualitatively, the predicted behaviour is as in the experimental curves (Figure 6C), with the concentration initially rising and then saturating. However, quantitatively, the concentration values predicted by the essential model are much larger than those seen experimentally. Indeed, using Equation 5 and the parameters in Table 1, the essential model predicts saturation to a long-time concentration $\bar{c}_u^\infty = 8.2 \times 10^6$ cells/ml. This is of the same order of magnitude as, but
approximately double what we observe experimentally ($\approx 4 \times 10^6 \text{cells/ml}$). Part of the discrepancy is because, as mentioned above, experimental concentration curves underestimate the concentration in the upper reservoir because of swimmers phototactically accumulated and ‘hidden’ at the surface. Another possible reason is that the essential model unrealistically ignores mechanisms causing losses: as illustrated by \textbf{Equation 5}, $c_{u}^{\infty}$ corresponds to the concentration obtained when all the swimmers from the porous and lower regions swim to the upper region and do not leave it thereafter. In reality, swimmer diffusion will cause cells to be transferred from the upper to the porous region, particularly at longer times when concentration gradients between the regions are large. Another possibility not accounted for by the essential model is that, if swimmers respond to gradients of light (as opposed to just its direction, as assumed in the model), the denser suspension of swimmers in the upper region shades the region below, changing the light gradient and reducing the phototactic speed of swimmers below, and thus the rate of accumulation. \textbf{Figure 7A} also shows the model prediction for the concentration in the upper region for the mesh-only case. As in experiment, this is seen to initially rise steeper and saturate at a lower value than the case of mesh + beads; numerically, however, the predicted concentrations ($c_{u}^{\infty} = 7.5 \times 10^6 \text{cells/ml}$) are approximately double what we measured experimentally. This is for the same reasons as for the mesh + beads case, and additionally in the mesh-only case there are also losses due to the plume leaking through the mesh, as we have shown (\textbf{Figure 4A}, 9 min). The faster rise in concentration observed for the mesh-only case compared to mesh + beads, is due to the difference in upswimming rates in the two cases: for mesh + beads, swimmers are slowed down when they swim through the porous layer. The essential model also allows the prediction of the concentrations in the porous and lower regions, respectively $c_{p}^{(t)}$ and $c_{l}^{(t)}$, which are shown in \textbf{Figure 7A}. The lower region concentration is seen to decay exponentially to zero, as swimmers evacuate the lower region by phototactic upswimming. The lower region decay predictions overlap for the mesh and mesh + beads cases, so they are not separately visible in the figure (the prediction equation is the same for these cases, and parameters are practically identical). We can compare these predictions with the experimentally determined concentration profiles. As observed in the previous section, these also decay with time, but not to zero: they saturate to a fixed value (\textbf{Figure 6F}), with the mesh-only case reaching a lower value than mesh + beads due to the greater leakiness of

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Figure6.png}
\caption{Temporal concentration profiles in the upper harvest region above a mesh or mesh + beads, after the LED is switched on and off (insets), as indicated. \textbf{(A)} Three repeats for microalgae phototactically concentrating above the bare mesh. Inset: concentration rise and decay after the LED is switched off. \textbf{(B)} As in (A), but for the mesh + beads (400 mg) case. \textbf{(C)} Time point average of the concentration profiles shown in (A, B). The concentration for the mesh-only case saturates ~10 min after the LED is switched on, whereas it keeps on increasing towards a higher saturation concentration in the mesh + beads case. When the LED is switched off, the concentration initially increases and then decays, for the reasons discussed in the text. \textbf{(D)} Three repeats for profiles in the lower region for the mesh only case. Inset: concentration rise after the LED is switched off. \textbf{(E)} As in \textbf{(D)} but for the mesh + beads case. \textbf{(F)} Time point average of the concentration profiles shown in \textbf{(D, E)}. For the mesh-only case the profile decays to a constant value sooner than mesh + beads. The inset shows how the concentrations for both cases rise in the lower region after the LED is switched off, with a greater rise for the more leaky mesh-only case.}
\end{figure}
the mesh. The essential model fails to predict this saturation and the important difference between the two cases, demonstrating the need to model diffusive transfer and leaking plumes between the regions, and/or a reduction of the phototactic speed. For the porous region, the essential model predicts that the concentration, $c_\text{f}(t)$, initially rises, due to influx from the lower region outpacing losses to the upper region, and eventually decays to zero. It was not possible to optically image the microalgae in the porous region and obtain the concentration there, so we cannot make a comparison with the essential model prediction in this case.

Assuming phototaxis and diffusion processes are dominant in the upper region, and that these occur faster than the accumulation from the porous region, we can also use the spatial extension of the essential model to chart the distribution of swimming algae in the upper region, which is provided by Equation 12. We note that, since this model does not fully account for photogirotaxis, the predictions are only strictly valid prior to the formation of the plume off the upper surface, which we know from experiment occurs $\approx 9$ min after turning the light on. In Figure 7B the distribution of swimmers is charted at different points in time (prior to plume formation), predicting that the suspension becomes increasingly top-heavy as time progresses. This accumulation, with concentrations reaching $\approx 10^6$ cells/ml close to the upper boundary, is unstable against its own negative buoyancy, and eventually results in the formation of the plume we observe experimentally. As it is not possible to accurately image the accumulation of cells around the meniscus, we did not experimentally quantify the spatial concentration distribution in the upper region. However, the increasing accumulation of swimmers at the surface is clearly discernible in our image sequences, see Supplementary Video S4.

The model predicts that the cells accumulate strongly at the top of the upper region, with no sizeable concentration below a certain height. Instead, our image sequences reveal that there is also a nonzero concentration in the bottom of the upper region (indeed that is what we have measured to obtain Figures 6A–C). This could be accounted for by losses from the accumulation at the surface to the edge of the cuvette, which are not considered in our model.

4 DISCUSSION

We have shown how light from above can trigger instabilities and upwards migration in an initially quiescent suspension of C. reinhardtii microalgae within a rectangular cuvette. By imaging, we qualitatively and quantitatively studied for the first time this migration in the following cases: when a permeable metal mesh is placed at the top of the suspension; when porous layers of beads are overlaid onto the mesh; in the absence of any mesh or layer on the surface. In the latter case, light was seen to drive photogirotactic instabilities in the bulk of the suspension and upwards migration of the cells to the surface, from which, eventually, a plume structure was seen to arise. A similar phenomenology was observed when a mesh was present, except in this case the plume from the surface was partially trapped by the mesh, later giving rise to a secondary plume. By trapping the plume, the mesh allows the concentration of cells in the upper region of the cuvette (also termed “harvest region”), but this is a leaky process. However, when a porous layer of glass beads is overlaid onto the mesh, it is possible to stably concentrate the suspension in the upper harvest region while the light is switched on: the plume from the surface is trapped by the mesh, later giving rise to a secondary plume. We have charted how the mean concentration in the harvest region varies with time for the case of a mesh with a layer of beads of different weights (thicknesses), showing that a $\approx 4$-fold concentration is possible for the thickest layer weighing 400 mg (Figure 6C). Critically, we have demonstrated that it is the unique combination of light and a moderately thick porous layer of beads that makes the photogirotactic concentration of cells possible. Without the beads the accumulation of microalgae in the harvest region is
leaky. When the light is switched off, all photogyratorytactic structures fall apart, and the microalgal population sinks back down to the initial quiescent state.

We can discuss our findings in terms of what is known about the phototactic and photogyratorytactic behaviour of microalgal suspensions. When the LED is switched on, the suspension responds visibly in seconds, similarly to what has been measured for populations responding to light from an optical fibre [23], and corresponding to the time scale for C. reinhardtii to perceive light and turn to swim towards it by controlling their flagellar beat [24]. Subsequent to this initial response, the suspension displays instabilities in cell concentration and flow. Some groups of cells rise, moving as waves drifting at the swimming speed of the algae or above, probably advected by upwelling flow; others form stretching plumes; others still sink. This complex behaviour is the result of the interplay of the phototaxis and gyrotaxis of the population, coupled with the fluid dynamics of a negatively buoyant suspension. In the absence of a full photogyratorytactic model, whose development is beyond the scope of this paper, it is not possible to account for these observed patterns quantitatively. A lower bound estimate of the timescale for accumulation to the surface leading to the formation of a plume there can, however, be obtained by considering the time for cells to swim straight up to the surface at the maximum phototactic speed. For the mesh + beads (400 mg) case, the mean swimming speed of the microalgae in the lower and upper regions, with heights \( h_l \) and \( h_u \), respectively, is \( V_s \), while it is \( V_{eff} \), as given by Equation 2, in the porous region with height \( h_p \). The time to reach the surface is then \( t \sim (h_l + h_p)/V_s + h_p/V_{eff} \approx 6 \) min, using parameters in Table 1. For the mesh-only case, there is no porous layer so that \( t_m \sim (h_l + h_p)/V_s \approx 5 \) min, using parameters in Supplementary Table S2. These values are not too far from the \( \sim 9 \text{ (7) min} \) it takes for a plume instability to develop from the surface in the mesh + beads (mesh) cases (Supplementary Figure S4). This suggests, as is clear from our concentration data in the harvest region (Figure 6), that, in spite of the instabilities observed, phototaxis drives a net flux of cells upwards through the porous layer towards the harvest region, where cells accumulate at the surface. Here they distribute, with maximum concentration at the surface. The concentration becomes increasingly top-heavy (as predicted by our essential model, see Figure 7B) and eventually a plume instability develops driven by the negative buoyancy of the suspension. The plume then drops towards the porous layer, but its negative buoyancy is not great enough to sink through it. Instead, the plume is trapped in the harvest region forming a toroidal “plume-cloud” fed from the surface, whose size expands with time to the edge of the harvest region (see Figure 5B). Here it appears to stabilize, possibly due to a balance between cell gain from the surface and loss to the suspension at the edges of the cuvette. The surface accumulation and plume-cloud, and all the structures in the lower region, collapse within a few seconds of switching the LED light off. In particular, the concentrated suspension in the harvest region sinks right through the porous layer, though this takes some time for the thick (400 mg) mesh + bead layer. This collapse of the suspension structures demonstrates the essential role of phototaxis in dramatically altering the stability thresholds of the active suspension: none of the structures we have observed can exist without light.

Our essential model provides a qualitative picture of how the average concentration changes in the upper, porous and lower regions, and gives concentration values which agree in order of magnitude with what we have measured. Comparison with experiment, however, reveals that the model fails to quantitatively describe the saturation of the upper and lower concentrations. This in part because our measurements in the upper region underestimate the concentration (missing cells accumulated at the surface). However, as evidenced by the failure of the model to predict saturation in the lower region (compare Figures 6D, 7A), it is likely that quantitative agreement is not possible because critical processes have not been modelled, such as diffusive exchanges between reservoirs and/or shading effects of the cell concentration in the upper region on the phototactic speed. For the upper region, the model was applied to predict a top-heavy distribution of cells, as is observed in our image sequences. The model, however, does not reproduce the concentration of cells visible in the bottom part of the upper region, probably due to a neglect of losses from the surface accumulation at the edge of the cuvette. The model is further limited to the description of the phototactic concentration prior to the formation of the plume-cloud, whose quantitative dynamics require a fully photogyratorytactic description. Future studies should develop such a description using continuum models coupling the suspension cell and flow dynamics in response to gravity, flow and light, as has been done by Williams and Bees to describe bioconvection patterns [26]. This will present some challenges. For example, it is as yet unclear which model of the phototactic response of a population agrees quantitatively with experiment. Williams and Bees did not test their model C against experiment [29], and other studies using a similar description to model C did not include gyrotaxis [23, 28]. Alternatively, the adaptive, microscopic model of photoaxis presented in [24] could be used as the basis of an agent-based model (ABM) of the population response, and integrated with known gyrotactic responses implemented in ABMs [41], and coupled to the fluid dynamics (another challenge for ABMs). Numerical and analytical predictions from such models will predict the spatio-temporal patterns in the suspension, including the meandering photogyratorytactic plumes, the formation of propagating waves of cells and their concentration in the phototactic curtain structures we have observed. To describe the latter, accounting for the observed width of the curtain pattern, it will be necessary to develop a model coupling the local light profile (optical shadows from the mesh) to the photogyratorytactic dynamics. Photogyratorytactic models should be developed for the lower, porous and upper regions combined, and should be able predict the characteristic timescales we have observed, such as the time required for plumes to form off the upper surface (Supplementary Figure S4). Such models will also describe how the plume-cloud in the harvest region grows with time, accounting for the curvature in the meniscus (neglected in our essential model) and how this affects the plume formation.
Observation indicates that the plume forms in the lowest point of the meniscus, likely because cells accumulate there. Advanced modelling should also predict how long the mesh or porous layer is able to support the plume against sinking when the LED is on, and how long it takes to sink through the layer when the LED is switched off.

A full account of photogyrotactic dynamics will permit inclusion of processes (such as diffusion and light shading affecting phototactic speed) not included in our essential model. Predictions from these improved photogyrotactic models for the concentration in the upper, porous and lower regions, should provide better agreement with the results shown in Figure 6. In particular, it will be interesting to use these refined models to establish the parameters that determine optimal conditions for harvesting microalgae in the upper region. From a practical perspective it is desirable to obtain the largest possible volume of suspension with the highest concentration gain for a given initial mean concentration and critical parameters, such as the height of the lower, porous and upper harvest regions, and the total duration of the concentration process. In addition, it will be desirable to know how strong the light intensity should be for optimal phototactic concentration. This is a parameter which was held fixed in the present study.

Harvesting contributes a significant amount (about 20–30% [36]) of the cost for processing microalgae and bioproducts derived from them. New methods are required to reduce this cost and replace energy-intensive solutions such as centrifugation. In many applications, a concentration factor of 100 upon harvesting is desirable to remove water and allow further bioprocessing of microalgae [36]. Investigations following our study should determine if such a concentration gain, improving on the four-fold gain we have demonstrated, can be achieved using photogyrotaxis alone. Alternatively, photogyrotactic concentration could already be viable as a preliminary concentration step, as is currently done by membrane filtration [42], reducing the time spent on more costly concentration methods, such as centrifugation. Following a demonstration at the milliliter (‘cuvette’) scale, it is worth investigating if photogyrotactic concentration can be scaled up, and if it can be an energy-efficient (using inexpensive LED or natural light, and exploiting natural swimming energy for concentration), and convenient method of value in industrial microalgal bioprocessing and harvesting. Indeed, for industrially-valuable swimming microalgae, exploiting swimming in response to light, as we have here explored, has not been considered as the basis for an efficient new harvesting method. Dunaliella salina, a marine relative of *C. reinhardtii*, is cultured in ponds that are maximum 20 cm deep to allow light penetration for growth [43]. It is known that this microalga can be concentrated when a layer of freshwater is produced, artificially or by rain, at the surface of the pond [43]. The freshwater generates a gradient in the density of the suspension medium, which acts similarly to the porous layer in our study and causes the microalga to become trapped in the freshwater layer at the surface [44]. The role of photogyrotaxis in this industrially well-known concentration process [43] has not yet been investigated. However, taking into consideration the concentration physics we have uncovered in this study, it could be optimized to produce better microalgal yields from culture ponds. Density gradients cannot be exploited for freshwater microalgae (an aqueous suspending medium less dense than water is not easily found), which require a porous layer to be concentrated by upswimming. In this case, the use of glass beads for the porous layer, as in this study, represents an improvement over Kessler’s original suggestion of a fibrous porous layer [35], which, from experience with gravitactic concentration using cotton wool [13, 14, 45], is known to be liable to irreversible cell loss to the fibers (biofouling).

Finally, it is worth remembering that *C. reinhardtii* is a soil-dwelling microalga. Little is known about its ecology within soils [46], but we can speculate that in saturated soils *C. reinhardtii* may migrate across porous layers in response to daylight. Thus, the phenomenology we have uncovered in this work and the methods we have developed can be adapted to better understand the behaviour of *C. reinhardtii* and similar species in their natural environments. It will be very interesting in future studies to investigate the phototactic movements of *C. reinhardtii* in laboratory soil-like porous media, and how this social behaviour affects its photosynthetic growth in topsoil, as well as more “traditional” social behaviours, such as sex [46] and interactions with other soil microbes [47, 48].

**DATA AVAILABILITY STATEMENT**

The datasets presented in this study can be found in online repositories. The names of the repositoryrepositories and accession number(s) can be found below: https://doi.org/10.5281/zenodo.5113916.

**AUTHOR CONTRIBUTIONS**

PP carried out the experiments. OC developed the modelling. PP and OC designed the experiments, analysed the data, and wrote the paper.

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**SUPPLEMENTARY MATERIAL**

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fphy.2021.744428/full#supplementary-material
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