Ultrasound variants drive substantial cis heritability of human gene expression

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The vast majority of human mutations have minor allele frequencies under 1%, with the plurality observed only once (that is, ‘singletons’). While Mendelian diseases are predominantly caused by rare alleles, their cumulative contribution to complex phenotypes is largely unknown. We develop and rigorously validate an approach to jointly estimate the contribution of all alleles, including singletons, to phenotypic variation. We apply our approach to transcriptional regulation, an intermediate between genetic variation and complex disease. Using whole-genome DNA and lymphoblastoid cell line RNA sequencing data from 360 European individuals, we conservatively estimate that singletons contribute approximately 25% of cis heritability across genes (dwarfing the contributions of other frequencies). The majority (approximately 76%) of singleton heritability derives from ultrarare variants absent from thousands of additional samples. We develop an inference procedure to demonstrate that our results are consistent with pervasive purifying selection shaping the regulatory architecture of most human genes.

The recent explosive growth of human populations has produced an abundance of genetic variants with minor allele frequencies (MAFs) less than 1% (ref. 1). While many rare variants underlying Mendelian diseases have been found2, their role in complex disease is unknown3–8. Evolutionary models predict that the contribution of rare variants to complex disease is highly dependent on selection strength9–11 and that population growth can magnify their impact12–14. Recent methodological breakthroughs15–24 have enabled researchers to jointly estimate the independent contributions of low- and high-frequency alleles to complex traits, often demonstrating a large rare variant contribution probably driven by natural selection15,16. However, these studies excluded the rarest variants9 or included only well-imputed variants17. This is a problematic limitation given that some plausible evolutionary models predict that the largest contributions to phenotypic variance could be from the rarest variants9,11,12. Directly querying the role of all variants with large-scale sequencing and sensitive statistical tests has the potential to reveal important sources of missing heritability, inform strategies to increase the success rate of association studies and clarify how natural selection has shaped human phenotypes.

In this study, we develop, validate and apply an approach for inferring the relative phenotypic contributions of all variants, from singletons to high-frequency variants. We focus on the narrow-sense heritability ($h^2$) of gene expression because a growing body of literature suggests that genetic variants primarily affect disease by modifying gene regulatory programs20–23, and recent examinations have identified significant rare variant effects on transcription4. To characterize the genetic architecture of gene expression, we analyzed 360 unrelated individuals of European ancestry with paired whole-genome DNA18 and RNA19 sequencing (RNA-seq) of lymphoblastoid cell lines (LCLs). We evaluate the robustness of our approach to genotyping errors, read mapping errors, population structure, rare variant stratification and a wide range of possible genetic architectures.

Results
Building and testing our model. We developed a method to estimate the effect of rare alleles on trait variance and validated our approach with an extensive set of simulations. Before analyzing real expression data, we performed a rigorous series of simulations to identify an approach for estimating heritability that is robust to possible confounding factors. In our simulations, we used real genotype data (all variants within 1 megabase (Mb) of the transcription start or end sites of genes) and generated gene expression phenotypes across individuals while varying the number of causal variants contributing to the phenotype (from 1 to 1,000), the distribution of effect sizes (including uniform, frequency-dependent and an evolutionary-based model) and the distribution of causal allele frequencies (ranging from predominantly rare to predominantly common; see Supplementary Note). In total, we simulated 440 different genotype–phenotype models that span the range of genetic architectures that are likely to underlie complex phenotypes such as gene expression, and analyzed each simulated dataset using multiple distinct methods. These include fitting a linear mixed model via restricted maximum likelihood24,25 and Haseman–Elston regression, an alternative approach based on regressing phenotypic covariance on genotypic covariance26, which is more robust in small samples (see Supplementary Note).

Similar to previous work27, we found that for many simulation settings, jointly analyzing all variants together can result in a substantial over- or underestimate of heritability (Fig. 1a; it shows results when true $h^2 = 0.2$). One common solution is to partition sites by frequency1,13,26. We found that simply isolating rare (MAF ≤ 1%) from common variants using two partitions and performing joint

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Singletons drive the genetic architecture of gene expression. To characterize the genetic architecture of human gene regulation, we partitioned the heritability of gene expression into 20 MAF bins. We used $n = 360$ unrelated individuals of European descent with both RNA-seq data from the GEUVADIS\textsuperscript{15} project (Genetic European Variation in Disease-European Medical Sequencing Consortium) and whole-genome sequencing (WGS) data from the 1000 Genomes Project (1KGP)\textsuperscript{24}. After extensive quality control to remove genes not expressed in LCLs, our dataset included 10,203 autosomal genes (see Supplementary Note). For each gene, we extracted all variants within 1 Mb of the transcription start or end sites (corresponding to an average of 13,839 variants per gene; 35.2\% are singletons); we did not consider trans effects because of the small sample size (though we do analyze the effects of varying window size in the Supplementary Note).

To control for possible non-normality, population structure and batch effects, we quantile-normalized expression values and the small sample size (though we do analyze the effects of varying window size in the Supplementary Note). For the data we analyze in this article, the SingHer method estimated that mean effect sizes were near zero; therefore, we proceeded with Haseman–Elston regression.

When partitioning variants into multiple MAF bins, singletons are inevitably isolated into their own category. Intuitively, if some fraction of singletons are causal, then individuals with a higher singleton load will probably be phenotypic outliers. (Indeed, individuals with outlier expression patterns have been observed to have an enrichment of nearby rare variants\textsuperscript{5}.) Therefore, it is reasonable to ask what contribution singletons make to patterning phenotypic variation across a population. We investigated the theoretical properties of heritability estimation from singleton variants and show analytically that when genotypic covariance is estimated using singletons alone, Haseman–Elston regression is equivalent to regressing squared standardized phenotypes against singleton counts (see Supplementary Note).

A direct implication of our derivation is that Haseman–Elston regression is unbiased unless singletons have large nonzero mean effect sizes (violating an explicit assumption of standard linear mixed models), which are the only simulation scenarios where heritability estimates remain upwardly biased (Fig. 1a, blue points). We developed an alternative approach that produces unbiased estimates of both heritability and mean effect size in all examined cases. Intuitively, the Singleton Heritability inference with REML (SingHer) method conditions on total singleton count (per cis window) to (1) appropriately estimate total cis heritability and (2) partition singleton heritability into directional and random components (see Supplementary Note). However, because Haseman–Elston regression is well understood and flexible, we recommend its use when mean effect sizes are near zero. For the data we analyze in this article, the SingHer method estimated that mean effect sizes were near zero; therefore, we proceeded with Haseman–Elston regression.

**Fig. 1 | Simulation results.** Across a broad range of parameters, the accuracy of heritability inference improves as the number of SNP bins (partitioned by MAF) increases. a, Mean bias of total heritability (inferred-true) for different numbers of SNP bins ($K$), where each point represents the mean of 500 simulations for different parameters, and box plot summarizing the bias distribution across all parameters (indicating the median, upper and lower quartile and twice the interquartile range). b–f, Distribution of average bias across simulated parameters for each SNP bin, showing that both mean and variance of the bias decrease as $K$ increases ($n = 500$ simulations in each plot).
Fig. 2 | Partitioning heritability. Rare variants dominate the genetic architecture of human gene expression. a, Average heritability estimates across genes, partitioned across MAF bins ($h^2$, purple) after correcting for population structure using PCA (blue) and eliminating residual rare variant structure identified using a trans permutation (pink). b, The proportion of heritability attributed to each MAF bin. Singletons represent approximately 25% of the total inferred heritability, the vast majority of which is due to variants that are extremely rare in the population (inset, partitioning singletons in our data by the MAF observed in gnomAD, n > 15 k; singletons not reported in gnomAD are indicated with an asterisk). c, Cumulative $h^2$ inferred as a function of MAF for different frequency filter thresholds (purple, green, blue, brown), and when singletons are partitioned by population MAF (based on gnomAD, red). Including all SNPs and partitioning singletons by population MAF (instead of observed MAF) results in a substantially increased level of $h^2$. d, Globally rare singletons represent 56% of all singletons, but contribute 92% of $h^2_{\text{singleton}}$. Rare indels and structural variants also have enriched contributions to heritability (2.8% of singletons but 7.8% of $h^2_{\text{singleton}}$). However, singletons inferred to derive from Neanderthal introgression or having gnomAD MAF $\geq 10^{-4}$ make negligible contributions to $h^2_{\text{singleton}}$. In all cases, confidence intervals/envelopes are based on the 95% quantile range of 1,000 bootstrap simulations.

included the first ten principal components from both genetic and phenotypic data in all analyses; we present the average $h^2$ estimate across genes in each MAF bin in Fig. 2a (blue curve). We found that $h^2$ is highest for the first MAF bin (singletons). However, using a new trans permutation procedure, we detected evidence for residual population stratification in low-frequency (but not high-frequency) SNPs that could not be accounted for using principal components (pink curve; see Supplementary Note). Note that differential population structure among common and rare variants is a documented, although understudied, phenomenon in human genetics. We corrected for this population stratification bias by subtracting the permutation-based estimate from the raw principal component-corrected $h^2$ estimate, shown in purple and henceforth indicated as $h^2'$. We found that the plurality of $h^2'$ comes from singletons, but common variants also contribute a substantial amount toward $h^2'$. Low- and intermediate-frequency SNPs make a minimal contribution to $h^2'$. Note that this is a conservative correction because our trans permutations capture both the effect of stratification and true trans heritability.

Figure 2b shows the proportion of $h^2'$ explained by each MAF bin, showing that singletons represent approximately 25% of the total $h^2'$, dominating the estimates from other MAF bins. Based on population genetic theory, we hypothesized that purifying selection has constrained causal regulatory alleles to low frequency. To test this hypothesis, we sorted our singletons by their population MAF, as inferred from a large external database (gnomAD). We reasoned that some of the singletons in our dataset would be evolutionarily neutral and have an intermediate population frequency, whereas the most deleterious singletons would almost always be constrained to a low population frequency. Therefore, we partitioned the singletons observed in our data by their MAF observed in the Genome Aggregation Database (gnomAD) dataset (representing high-coverage WGS on > 15,000 individuals) and performed Haseman–Elston inference of $h^2'$ across 20 singleton bins based on their MAF observed in gnomAD. (We also partitioned by functional predictions and evolutionary conservation; see Supplementary Note.) The inset in Fig. 2b shows that the vast majority (>90%) of singleton $h^2$ is derived from variants that have a gnomAD MAF < 0.01%. This is strong evidence that natural selection constrains alleles with the largest effects on gene regulation to very low frequency. Notably, we found that 31% of our singletons were not reported in gnomAD, but this subset of variants (indicated by an asterisk in Fig. 2b) nonetheless explains approximately 80% of $h^2_{\text{singleton}}$. We confirmed that the majority of this signal is derived from true-positive singletons by analyzing a subset of 58 individuals with high-coverage WGS and estimated that 88% of $h^2_{\text{singleton}}$ is derived from variants that validate (Supplementary Note). Previous work has shown that additionally partitioning common variants by linkage disequilibrium resulted in minimal change after partitioning by MAF.

Studies of heritability typically filter out rare variants. We showed that removing any SNPs based on MAF has a direct impact on the estimate of heritability. Figure 2c shows the cumulative $h^2$ inferred as a function of MAF for different minor allele count (MAC) thresholds (averaged over all genes). We found that adding progressively rarer variants to the analysis resulted in a monotonic increase in inferred heritability. Including all variants down to singletons (purple curve) increases $h^2_{\text{total}}$ by approximately 50% ($h^2_{\text{total}} = 0.061$) compared to the case when only common variants (MAC $\geq 5$) are analyzed (brown curve, $h^2_{\text{common}} = 0.04$), indicating that common variants cannot tag heritability from lower-frequency variants (that is, ‘synthetic association’ tagging) is minimal, although rare variants can tag some common variant heritability; see Supplementary Note). However, not all singletons contribute equally to heritability and pooling them together can deflate $h^2$ estimates (a ‘singleton linkage disequilibrium’ effect previously only reported for common variants; see Supplementary Note). Partitioning singletons into 6 bins based on their observed MAF in gnomAD (red curve) increased our $h^2_{\text{total}}$ estimate to 0.082 and showed that nearly half of the total heritability (46.6%) is explained by the 27.6% of variants that are globally rare (with MAF $_{\text{gnomAD}} < 0.1\%$).
Recent studies of gene expression variation in humans have suggested that one-quarter of Neanderthal-introgressed haplotypes have cis-regulatory effects and that expression outliers are enriched for having nearby rare structural variants compared to nonoutliers. However, the overall contribution of these classes of variants to expression variation had not been characterized. We performed Haseman–Elston regression on four disjoint categories of singletons (Neanderthal-introgressed, indels/structural variants, globally rare singletons and other singletons) and found that globally rare singletons (that is, singletons in our data that are also singletons across all 2,504 samples in the 1KGP24) contribute the vast majority (92%) of singleton heritability (Fig. 2d). Rare indels/structural variants also have an enriched contribution to gene expression variation (representing 2.8% of singletons, but 6.8% of $h^2_{\text{singleton}}$), but Neanderthal-introgressed singletons and other singletons make a negligible contribution to $h^2_{\text{singleton}}$.

Genotype quality does not drive the inference of heritability. One possible confounding factor is the effect of genotyping error on heritability estimation. If heritability is biased by genotyping error and genotyping error also varies as a function of MAF, there could be differential bias across frequency bins when analyzing real data. We simulated a range of genotyping error models and found that all investigated forms of genotyping error increased the variance of heritability estimation, but did not induce a detectable upward bias (Supplementary Note).

We also performed several analyses to examine the possible confounding effects in these data (Supplementary Note). First, we ranked singletons by their reported genotype likelihood as reported for the individual carrying the singleton allele in 1KGP24 and partitioned them into four equal groups (quartiles). We then ran Haseman–Elston regression with these four groups of singletons (along with ten principal components). Notably, we found that only those singletons with high SNP quality contributed positively to our inference of heritability (see Supplementary Note). Second, since both DNA sequencing and RNA-seq are based on LCLs, it is conceivable that difficult-to-sequence regions of the genome could result in correlated errors that confound our inference. To test this, we restricted our analysis to regions of the genome passing the 1KGP strict mask and found that our inference of heritability was unchanged. We further ranked genes based on the number of exon bases passing the strict mask and found no difference in the genetic architecture of genes having high versus low overlap with the strict mask (see Supplementary Note). Finally, a subset of $n=58$ samples were sequenced at high coverage by Complete Genomics as part of the 1KGP24. We identified the singletons carried by these individuals and partitioned them into four groups by cross-classifying them as being present or absent in the Complete Genomics or gnomAD datasets. Running Haseman–Elston regression on this subset of singletons shows that $h^2_{\text{singleton}}$ is predominantly driven by singletons that replicate in the Complete Genomics data but are not reported in gnomAD (consistent with Fig. 2), and that singletons that are absent from Complete Genomics (and therefore more probably false positives) contribute negligibly to $h^2_{\text{singleton}}$ (Supplementary Note).

Selection drives the genetic architecture of gene expression. We found that rare variants are a major source of heritability of gene expression, which we hypothesized was due to purifying selection constraining the frequencies of large-effect alleles. To test this hypothesis, we performed extensive simulations of human evolutionary history and developed a method to infer the parameters of an evolutionary model for complex traits (see Supplementary Note). Our three-parameter phenotype model extends a previously described model of the pleiotropy of causal variation—captured by $\rho$, where increasing values indicate higher correlations among expression effect sizes and the fitness effects acting on causal variants—and the scaling relationship between expression effect sizes and selection coefficients ($\tau$, where increasing values indicate that the distribution of effect sizes has a longer tail toward strong effects), to include the overall strength of selection ($\phi$), a mixture parameter between strong and weak selection distributions, where $\phi=1$ corresponds to strong selection. We inferred the approximate posterior distributions for each of these parameters using rejection sampling, which compares a set of informative summary statistics from genetic data simulated under a model of European demography and selection to the observed data (see Supplementary Note). Note that our inference procedure allows each parameter to vary across genes, but we only sought to infer the distribution of the average values of $\rho$, $\tau$ and $\phi$ across genes because we did not have the statistical power to infer $\rho$ and $\tau$ for each gene. We rigorously evaluated the performance of this inference procedure with simulations and found that we could infer $\rho$ and $\tau$ with fairly high accuracy; however, $\phi$ (while broadly unbiased) is less informative (Supplementary Note).

Applying this model to our data, we found that purifying selection had a major impact on the genetic architecture of human gene expression and that a range of previously explored evolutionary models can plausibly explain the empirical data. In Fig. 3a, we plotted the posterior distributions of the mean values of $\phi$, $\rho$ and $\tau$. This suggested that, on average, the fitness effects acting on causal variants tend to follow the distribution inferred from conserved non-coding loci ($\phi=0$), but selection is pervasive in the sense that gene expression effect sizes are highly correlated with the fitness effects acting on causal variants. Figure 3b shows that our data are consistent with a ridge of evolutionary scenarios that connect models where causal alleles are highly modular (for example, effect sizes are correlated with dampered fitness effects, as in the model of Eyre-Walker, which assumes $\rho=1$ with intermediate $\tau$) and models with highly pleiotropic causal alleles and more extreme effect sizes (for example, the Simons et al. model, which assumes $\tau=1$, but a more moderate $\rho$). This observation could only be identified using our integrated model and suggests highly heterogeneous processes acting on individual genes. Our parameter inference suggests that while mean $\rho$, $\tau$ and $\phi$ can vary substantially among the best-fitting models, individual genes tend to have extreme values (that is, either 0 or 1) for all three parameters (Fig. 3a). Figure 3c shows the cumulative proportion of $h^2$ as a function of MAF from 1,000 bootstrap draws from our posterior distribution, along with the cumulative proportion of $h^2$ inferred from our data. Compared to a neutral evolutionary model (pink), the posterior draws (gray, representing points along the ridge of evolutionary phenotype models show in Fig. 2b) are all highly concordant with our data.

Discussion
There is great interest in characterizing the genetic basis for complex traits to improve our understanding of human health and disease and substantial resources are being spent to collect ever-larger cohorts to investigate the role of rare variants. Such studies will clarify what we have learned from our relatively small study of just 360 individuals. We developed, tested and applied a technique for interrogating the role of rare variants in gene regulation using a relatively small cohort of $n=360$ individuals who had whole-genome DNA sequencing and RNA-seq performed on their derived LCLs. We estimated that the total narrow-sense heritability of LCL gene expression is approximately 8.2% and that the largest contributors to gene expression heritability are the rarest of variants in our data, that is, singletons where just one copy of the allele has been observed in our sample of 720 chromosomes (MAF $=0.0014$). Globally rare variants (MAF $\text{gnomAD}<0.01\%$) explain approximately 90% of $h^2_{\text{singleton}}$, implying that many of these causal variants would remain singletons even if tens of thousands more samples were sequenced and many more
Fig. 3 | Pervasive purifying selection drives the genetic architecture of gene expression. Our model infers the strength of purifying selection acting on causal variants ($\phi$), the correlation between the fitness and the effect size of causal variants ($\rho$) and a scaling factor that transforms fitness into effect sizes ($\tau$). a. The posterior distribution of the mean of each parameter across genes (curves) and a histogram of the posterior parameter estimates for each gene. b. The joint posterior distribution of the average $\rho$ and $\tau$ across genes shows an evolutionary trade-off between the correlation and scaling of fitness and effect sizes. c. The cumulative proportion of heritability inferred from the gene expression data (dots) compared to the expected patterns from 1,000 draws from the posterior distribution (gray) and neutral expectation (pink).

Singletons would be discovered. However, given that the plurality of variants is ultrarare, do we infer more heritability than would be expected given the fraction of variants observed at these frequencies? In the Supplementary Note, we show that heritability enrichment is U-shaped as a function of MAF (on a logarithmic scale), suggesting that both rare and common alleles contribute more than twofold excess of heritability, while intermediate/low-frequency variants (MAF = 0.1–5%) constitute a dearth of heritability. This does not give us direct insight into the underlying distribution of regulatory effect sizes per causal variant, but it would be reasonable to speculate that the distribution of effect sizes for rare causal variants may be considerably larger (in absolute values) than common variants.

This excess of heritability due to ultrarare variants is best explained by pervasive purifying selection, where most cis-acting regulatory variants are deleterious. We inferred the parameters of an evolutionary model that are consistent with these data and found that for approximately two-thirds of genes, the effect sizes of cis-regulatory variants are highly correlated with how deleterious the fitness effects are on causal variants. Further, for the majority of genes, the fitness effects are more consistent with broadly defined conserved noncoding regions of the genome than the strongly selected non-synonymous or ultraconserved regions of the genome. However, while these parameters allow us to generate simulated data consistent with our observations, they remain post hoc parametric models that do not necessarily represent a generative model of how the genetic architecture of cis-regulatory variation evolved, and do not incorporate potentially important contributions from other modes of natural selection (such as positive or balancing selection, which may be rare but can have substantial impact on gene expression when they act).

Our estimate of total cis heritability is slightly larger than the previous estimates of $h^2_{cis} = 0.057$ and 0.055 in blood and adipose tissue, respectively, but lower than recent twin-based estimates of overall narrow-sense heritability $h^2 = 0.26, 0.21$ and 0.16 in adipose tissue, LCLs and skin, respectively as well as overall broad-sense heritability $H^2 = 0.38$ and 0.32 for LCLs and whole blood. Therefore, it is plausible that rare variants account for some ‘missing heritability’ in human gene expression; however, differences in population, tissue and/or technology could also explain some of these patterns and there could also be differences between the genetic architecture of cis and trans regulation.

A concurrent examination of rare variant heritability via an allele-specific expression approach reported a lower, yet substantial contribution to heritability from rare variation. However, there are fundamental differences between our analyses that probably contribute to the difference in estimates. First, the work by Glassberg et al. examined a much narrower window around genes. This leads to differences if selection has acted differently in promoters compared to more distal regulatory regions (Supplementary Note). Second, their work used a smaller sample size; thus, their definition of rare is less stringent than ours. Finally, they did not reclassify rare variants according to external reference panels, which greatly increased our estimates of rare variant heritability.

While it might at first seem logical to genotype some (or all) of these singletons in a larger panel of individuals to statistically identify the causal ones, our analysis uncovered a major challenge with this approach. Our results can only be explained if the causal alleles driving heritability are evolutionarily deleterious, with effect sizes often scaling with the strength of selection acting on them. This means that the alleles that have the greatest impact on gene expression are probably extremely rare in the broader population and are unlikely to exist in more than a few unrelated individuals in any given population. Indeed, our analysis shows that 90% of the singleton heritability is derived from alleles that are either not reported or have a MAF < 0.01% in the $n > 15,000$ samples in gnomAD. Therefore, we conclude that identifying causal alleles for transcriptional variation probably requires the incorporation of new biological information, possibly including large-scale experimental testing of singleton variants to improve functional predictions.

As the number of samples with detailed phenotype data and WGS data increases, it will be possible to apply the approach we have developed in the present study to characterize the genetic architecture of additional complex traits. Indeed, in a recent WGS study of height and body mass index, we found that rare variants comprise essentially the entirety of ‘missing heritability’ for these traits. By integrating such methods with functional genomic data, we may also learn more about the biology of causal variants, which could enable improved identification of clinically actionable variants in some cases. However, it is not clear that risk prediction from genomic data for most diseases will be feasible for otherwise healthy individuals with limited family history information. Population genetic theory tells us that rare variants only contribute a substantial source of heritability when causal alleles are evolutionarily deleterious. But the biology of human health and disease is complex. While not all human diseases themselves impart a strong fitness effect, extensive pleiotropy resulting from tightly interconnected networks of interacting proteins experiencing cell-specific regulatory mechanisms could. Indeed, under the omnigenic model of disease, variants that affect any one of these components could contribute to an individual’s risk for any disease involving any downstream pathway.

We developed an approach to examine the heritability of singleton variants and the results have important implications for future genetic studies. We rigorously evaluated the performance of our
inference procedure using extensive simulations and multiple types of permutations (see Supplementary Note). While we employed several approaches to test for the presence of confounders from population structure, genotyping/mapping error and cell line artifacts, there may be other unknown confounders that have biased the results of this study. We conservatively used quantile normalization on the expression phenotypes to enforce normality and this often reduces the overall heritability estimates (see Supplementary Note) by diminishing the impact of outliers\(^{40}\). There are several other contributors to broad-sense heritability that we have not attempted to model; they may also account for some of the heritability estimated in family-based studies, such as gene–gene interactions, gene–environment interactions and other nonadditive components.

Online content

Any methods, additional references, Nature Research reporting summaries, source data, statements of code and data availability and associated accession codes are available at https://doi.org/10.1038/s41588-019-0487-7.

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**Author contributions**
R.D.H. and N.Z. conceived and designed the study. L.H.U. and A.D. developed methods. R.D.H., L.H.U., K.H., C.Y., A.D. and N.Z. contributed to data analysis or simulations. R.D.H. and N.Z. wrote the manuscript. All authors read and approved the manuscript.

**Competing interests**
The authors declare no competing interests.

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Methods

The full methodological details can be found in the Supplementary Note accompanying this manuscript (along with the simulation results, testing robustness of model assumptions and evolutionary modeling). In this Article, we provide details of the primary methods used for data analysis.

Frequency-binned Haseman–Elston regression. Given genotypes at M SNPs over N individuals we considered additive phenotypic models such that the phenotype of individual i is $y_i = \sum_{j=1}^{M} g_j \beta_j + \epsilon_i \sim N(0, \sigma^2_I)$, where $g_j$ is the genotype of individual i at SNP j, $\beta_j$ is the effect size of SNP j and $\epsilon_i$ is the residual, independent and identically distributed, normally distributed noise of individual i.

We partitioned the SNPs into K disjoint sets determined by the MAF of each SNP (or some other characteristic indicated in the text) and estimated the contribution of SNPs in the $k^{th}$ set to the heritability of $\gamma_k = \sigma^2_k / \sigma^2_I$, where $\sigma^2_I$ is the total genetic variance and $\sigma^2_k = \sum_{j=1}^{K} \sigma^2_j$ is the total phenotypic variance, assumed to be equal to 1 going forward.

To infer the heritability of gene expression levels across individuals, we primarily relied on Haseman–Elston regression. The premise of Haseman–Elston regression is that heritability can be estimated by the correlation between the phenotypic covariance across individuals and the genotypic covariance across individuals. In practice, for a single gene, we estimate the phenotypic covariance ($P$) as the upper triangle of the outer product of quantile-normalized log(fragments per kilobase of transcript per million mapped reads) across our sample. For each of the K partitions, we estimated genotypic covariance with the rows and columns, where each column has mean 0 and unit variance, the $k^{th}$ kinship matrix is $R_k = G_k C_k M$, Haseman–Elston regression is then performed using the $\ell^m$ function in R:

$$P \approx R_1 + \ldots + R_K$$

Specifically, the regression is ordinary least squares applied to the (vectorized) strict upper triangles of these matrices, which, for N individuals, has $\binom{N}{2}$ elements. In Haseman–Elston regression, with scaled and centered genotypes and phenotypes, the effect size for the $k^{th}$ term represents the genetic variance explained by all SNPs given by $\sigma^2_k / \sigma^2_I$.

In Fig. 2 and in the Supplementary Note, we compare heritability estimates in many ways. Our primary approach to estimating uncertainty was based on rigorous bootstrapping. Except where noted, all error bars (sometimes plotted as envelopes encompassing the mean) were calculated from the 95% interquartile range of 1,000 bootstrap samples. This is an appropriate method for estimating uncertainty in independent and identically distributed data, and has previously been shown to work well in far broader settings. Further, bootstrapping is a statistically appropriate way to estimate uncertainty when analyzing functions of correlated parameter estimates, for example, when estimating total $h^2$, which is the sum across $h^2$ estimates per bin. These bootstrap intervals represent uncertainty in the across-gene average heritability estimates per category (indeed, the single-gene uncertainties are much larger) and retain any across-gene correlations that are present in the real data. Hence, our s.e.m. estimates naturally account for correlated expression.

Evolutionary modeling and parameter inference. We suppose that gene expression is evolutionarily optimized, such that mutations that affect gene expression levels are deleterious. While many different evolutionary models can encode this qualitative behavior, we chose a previously studied theoretical model that allows for variation in pleiotropy and selection strength across genes.

We used rejection sampling to infer evolutionary parameters. Rejection sampling compares a set of informative summary statistics computed on the output of model-based simulations to observed genomic and phenotypic data. The simulations that generate summary statistics that are most similar to the observed data are retained and the parameter values from the retained simulations are used to generate a posterior distribution over the true parameter values. In the present study, we took the proportion of variance explained by alleles up to minor allele count x as summary statistics, for x in $\{1,2,5,10,20,60,120,180,240,360\}$. We focused on inferring the mean strength of selection ($2N\rho$), the correlation between selection strength and effect size ($\rho$), the mean shape of the effect size distribution ($\tau$) and the selection strength on cis-regulatory variants ($\theta$, representing the proportion of regulatory variants under strong negative selection). We inferred the posterior distribution of the mean of each of these parameters across genes as our PGE analysis.

Data availability

The datasets that support the results and conclusions of the current study are available in the Nature Research Data Catalog. This dataset contains 375 individuals of European descent from 4 locations. Each of these

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individuals are contained in the 1KGP and genome sequence data were downloaded from www.1000genomes.org (ref. 24).

**Code availability**

Three open source software tools are being made available as part of this study; all are available on GitHub: (1) HEh2.R—R code that performs all the Haseman–Elston analyses and simulations discussed in this paper. It also implements the artificial intelligence algorithm for parameter inference of linear mixed models. It is available from https://github.com/hernrya/HEh2; (2) SingHer R package discussed in the Supplementary Note, with performance statistics and available from https://github.com/andywdahl/SingHer; and (3) rejection sampling: scripts demonstrating how we used rejection sampling to infer parameters of the phenotype model are available from https://github.com/uricchio/HE_scripts.

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Software and code

Policy information about availability of computer code

Data collection: No data collection was performed for this analysis. No software were used for data collection.

Data analysis: Three open source software tools are being made available as part of this study, all available on GitHub:

HEh2.R – R code that performs all H-E analyses and simulations discussed in this paper. Also implements AI algorithm for parameter inference of LMM. Available here: https://github.com/hernrya/HEh2. Contact: Ryan Hernandez <ryan.hernandez@me.com>. For data analysis, we used version posted on April 25, 2019.

SingHer R package – Singleton Heritability inference with REML, discussed in Section 2.4, with performance statistics in Table S2, and available here: https://github.com/andywdahl/SingHer. Contact: Andrew Dahl <andywdahl@gmail.com>, Noah Zaitlen <noahaz@gmail.com>. For data analysis, we used version posted August 28, 2018.

Rejection sampling: Scripts demonstrating how we used rejection sampling to infer parameters of the phenotype model are available here https://github.com/uricchio/HE_scripts. Contact: Lawrence Uricchio <uricchil@gmail.com>. For data analysis, we used version posted April 24, 2019.

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Life sciences study design

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Sample size
360 unrelated European individuals were available with deep RNA sequencing (through GEUVADIS) and whole genome sequencing (through 1000 Genomes Project).

Data exclusions
Related individuals can bias results, and therefore individuals with a relationship closer than 3rd cousin were removed. This decision was made prior to any analysis.

Replication
There was no data collection, and therefore there were no steps taken to ensure reproducibility of experimental findings. To ensure reliability of our inference, we used an alternative subset of genotype data from high coverage whole genome sequencing.

Randomization
We performed many analyses to dissect stratification.

Blinding
Our analysis is based on the inference of heritability of gene expression, as such knowledge of each individual’s expression values and genotypes were essential, and therefore blinding was not possible.

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