Analysis of cold formed steel sheet pile for earth retaining wall.

Análisis de tablestacas de acero conformadas en frío para muro de contención de tierra

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ABSTRACT
Failure loads of sheet pile having various profiles such as U, Z and Omega/Hat profiles under compression was carried out by using equations of strength of materials and compared the failure load under various modes such as Euler’s buckling, torsional buckling and failure load due to yielding. Compared the strength of various profiles under flexure by using finite element analysis. Sheet pile can be analyzed as a unit cell for the simplified finite element analysis. For selecting the unit cell sheet pile with omega/Hat section was analyzed for profile containing one to eight numbers and checked the convergence of bending stress and maximum lateral deflection. Interlocks were analyzed for three different conditions such as plane interlock, interlock filled with bitumen and welded interlock. Location of interlock and neutral axis of the wall will affect the stability of the structure. Sheet piles with various cross sections were analyzed and studied the shear stress and bending stress along the cross section. From the structural performance of various cross sections omega/hat section can be considered as the most efficient cross section for the cold formed steel sheet pile because of its more load carrying capacity under compression and high torsion resistance and less bending stress. Results from the finite element analysis for the selection of unit cell shows that the stress and deflection value was converge at the sheet pile having 6 numbers of profiles.

RESUMEN
Las cargas de rotura de tablestacas que tienen varios perfiles, como los perfiles U, Z y Omega / Hat bajo compresión, se llevaron a cabo mediante el uso de ecuaciones de resistencia de materiales y se comparó la carga de rotura en varios modos como el pandeo de Euler, pandeo torsional y carga de falla debido flexible. Se comparó la resistencia de varios perfiles bajo flexión mediante el análisis de elementos finitos. La tablestaca se puede analizar como una
celda unitaria para el análisis simplificado de elementos finitos. Para seleccionar la celda unitaria de tablestacas con sección omega / Hat, se analizó el perfil que contenía de uno a ocho números y se verificó la convergencia de la tensión de flexión y la deflexión lateral máxima. Los enclavamientos se analizaron para tres condiciones diferentes, como el enclavamiento plano, el enclavamiento relleno con betún y el enclavamiento soldado. La ubicación del enclavamiento y el eje neutral de la pared afectará la estabilidad de la estructura. Se analizaron tablestacas con varias secciones transversales y se estudiaron el esfuerzo cortante y el esfuerzo de flexión a lo largo de la sección transversal. A partir del rendimiento estructural de varias secciones transversales, la sección omega / hat puede considerarse como la sección transversal más eficiente para la tablestaca de acero conformada en frío debido a su mayor capacidad de carga bajo compresión y alta resistencia a la torsión y menor esfuerzo de flexión. Los resultados del análisis de elementos finitos para la selección de la celda unitaria muestran que el valor de tensión y deflexión convergía en la tablestaca que tenía 6 números de perfiles.

INTRODUCTION

Sheet piles are the structural units which are connected together via interlocking edges to form a wall which can retain solid or liquid. It has number of applications such as retaining walls, river bank protection, cofferdams etc. Fig.1 shows various applications of steel sheet pile. Based on the materials it can be of steel, concrete, wood, etc. But due to more strength and quality control, steel sheet piles are generally preferred. Steel sheet piles can be hot rolled steel sheet piles and cold formed steel sheet piles based on the type of steel used. Fig.2 shows various applications of steel sheet piles. Cold formed steel sections are generally thin sections as compared to hot rolled steel sections. Moreover, cold formed steel sections are preferred over hot rolled steel sections because of their high strength to weight ratio, easy prefabrication, mass production, fast and easy installation and economy.

a) Earth retaining wall
b) River bank protection
c) Coffer Dam
d) Protection for construction pit

Fig. 1 Various applications of steel sheet pile
The loads governing the design of a sheet pile wall include applied forces from soil, water, and surface surcharges and the impact from external objects. Horizontal forces applied by soils include, active pressures and passive pressures. Water forces include hydrostatic pressures, which can occur due to differential water levels on either side of the wall. Surcharges include uniform or variable, strip or line and point loads, which rest on the soil surface in the vicinity of the wall and can increase the lateral pressures on the wall.

STRUCTURAL PERFORMANCE OF VARIOUS PROFILES OF STEEL SHEET PILE

Comparison Of Various Profiles

There are 3 types of sheet pile profiles which are mainly used for the purpose of retaining wall, Z, U and Omega/Hat profiles. Dimension of the sections used for the comparison study is shown in fig 3. The thickness of the profile considered as 6, 7 and 8mm respectively for Z, U and omega/hat section. For the purpose of numerical studies each of the profiles are selected in such a way that they have same cross sectional area, span (Profiles of same weight) and fixed at one end.
From the following Table 1 for a given weight the moment of inertia of the Z section is $1.601 \times 10^8 \text{ mm}^4$ which is slightly higher than the moment of inertia of the other two sections. Omega section gives the less value of moment of inertia of $9.6 \times 10^7 \text{ mm}^4$. Torsion constant for omega section obtained as $119466.66 \text{ mm}^4$ which is higher than the other two sections and Z section shows less value of torsion constant of $67248 \text{ mm}^4$. It shows the torsional response of the profile.

**Table 1 Comparison of various profiles based on properties**

| Profile          | Z profile | U profile | Omega profile |
|------------------|-----------|-----------|---------------|
| **Functional advantages** | Interlocking joints are away from the centre line of the wall which gives protection for the interlocks. | Interlocking joints are away from the centre line of the wall which gives protection for the interlocks. | Large width reduces the number of piles and installation time. |
| **Applications** | Can be used for intermediate to deep wall construction. | Can be used for intermediate to deep wall construction. | Can be used for shallower wall construction. |
| **Cross-sectional area (mm$^2$) for a weight of 270.48 Kg and Length of 6m** | 5600 | 5600 | 5600 |
| Parameter                        | Value 1           | Value 2           | Value 3           |
|---------------------------------|-------------------|-------------------|-------------------|
| Moment of inertia (mm$^4$)      | $1.601 \times 10^8$ | $1.215 \times 10^8$ | $9.6 \times 10^7$ |
| Torsional constant J (mm$^4$)   | 67248             | 91466.66          | 119466.66         |
Selected profile for the embedded sheet pile

Design of cantilever sheet pile wall can be done by as per IS 9527 part-(III) clause 8.1.1. As per the code pile section can be designed for the maximum bending moment caused by various forces. By using this bending moment suitable section for the sheet pile can be selected by calculating modulus of section of the profile. Omega section of 9.5 mm thickness has been selected. Cross section of the selected section is shown in fig.4 its properties are tabulated in table

![Diagram of selected profile for the embedded sheet pile]

**Fig.4 Selected profile for the embedded sheet pile**

| Properties of selected section | Thickness  |
|-------------------------------|------------|
|                               | 9.5mm      |
| Cross section area            | 13691.4mm² |
| Weight                        | 172 kg/m   |
| Moment of inertia             | 48336×10⁴mm⁴ |
| Section modulus               | 2050×10⁶mm³ |

**RESULTS AND DISCUSSIONS**

**Finite Element Analysis of Embedded Sheet Pile Cantilever Retaining Wall**

Finite element analysis of the retaining wall shown in fig.5. Analysis is carried out by considering the unit cell containing 6 numbers of profiles and considered the aspect ratio is 3. Longitudinal bending stress and deflection of the wall was obtained. Fig.6 shows the loading, deflection and longitudinal stress diagram. Table 3 gives the maximum bending stress and deflection values. Maximum bending stress of 369.7 MPa is occurring at the support. Maximum deflection is at top of the wall which is 134.6 mm.
G.L

\( \varnothing = 30^\circ \)
\( \gamma = 16 \text{ kN/m}^3 \)

G.W.T

\( \varnothing = 30^\circ \)
\( \gamma' = 6 \text{ kN/m}^3 \)

\( \varnothing = 30^\circ \)
\( \gamma' = 6 \text{ kN/m}^3 \)

Fig. 7 Sheet pile embedded in sandy soil
Fig 6 Unit cell for the sheet pile analysis
(a) Schematic loading diagram (b) loading diagram in finite element
(c) Deflection diagram (d) longitudinal stress diagram

369.7 MPa
(Maximum stress)
Table 3 Maximum longitudinal stress and Maximum displacement from the finite element analysis of embedded sheet pile

|                        | Value                  |
|------------------------|------------------------|
| Maximum longitudinal stress | 369.7 MPa (at support) |
| Maximum displacement    | 134.6mm (at top)       |

Finite Element Analysis of Sheet Pile Joints

Sheet pile having length of 1m, thickness of 6 mm cross-section shown in fig.7 fixed at the bottom, is considered for the finite element analysis of joint. Unit load of 1N/mm² applied to the joint.

Analysis of Interlock Joints for Various Cross Sections

Interlocks for different cross sections are located on different positions. After interlocking each profile the wall is acting as a single structure. Bending stress will be minimum at the neutral axis of the wall and maximum at the sides. Maximum shear stress will be at the neutral axis and minimum at sides. At the loading condition shear stress is transferred through the interlocks.

Analysis of interlock in 'U' section

In 'U' type profiles interlock is located at center line of the wall. Four nodded thin shell type of linear quadrilateral element of aspect ratio 3 is used for the finite element analysis. Four numbers of profiles are connected. Bending stress values and shear stress values along the cross section is obtained from the analysis is shown in Table 4. Fig. 8 shows the depth of cross section v/s bending stress and Fig. 9 shows depth of cross section v/s shear stress. From the graph it shows that bending stress gives zero at the height of 195 mm and where shear stress shows maximum value of 3.58 MPa. Shear stress is
minimum at the ends of the section with value of 0.13 MPa and 0.1 MPa. Shear stress is transferred through the interlock during loading condition and it is maximum at the neutral axis. Interlocks are the weakest point in the sheet pile wall it will affects by more shear stress, it leads to the inter pile slippage and finally leads to the failure of the wall.

Table 4 Bending stress and shear stress values along the cross section for U profile sheet pile

| Height of cross section (mm) | Bending stress (MPa) | Shear stress (MPa) |
|-----------------------------|----------------------|-------------------|
| 0                           | -12.05               | 0.13              |
| 39                          | -3.47                | 2.23              |
| 78                          | -2.66                | 2.66              |
| 117                         | -1.85                | 3.03              |
| 156                         | -1.01                | 3.317             |
| 195                         | 0                    | 3.58              |
| 234                         | 0.52                 | 3.54              |
| 273                         | 1.42                 | 3.39              |
| 312                         | 2.28                 | 3.16              |
| 351                         | 3.13                 | 2.84              |
| 390                         | 12.01                | 0.1               |

Fig. 8 Height of cross section v/s bending stress for U profile sheet pile
Analysis of interlock in ‘Z’ section

In Z section sheet piles the number of interlocks per unit length is more compare to the other profiles and it is located at the outer end of the section at both sides of centerline of the wall. Four nodded thin shell type of linear quadrilateral element of aspect ratio 3 is used for the finite element analysis. Four profiles are connected. Shear stress and bending stress values obtained by the analysis is tabulated in the table 5. Fig. 10 shows the depth of cross section v/s bending stress and fig. 11 shows depth of cross section v/s shear stress. The neutral axis of the wall is located 150 mm from the bottom of the section. From the table the maximum shear stress and zero bending stress at the cross section height of 150 mm. It shows that maximum shear stress is occurs at the area of neutral axis where bending stress is zero. Fig 11 shows that at the end of the section shear stress is minimum. So that interlock will affected by zero or negligible value of shear stress, it gives the safety to the interlock and stability for the wall.
Table 5 Shear stress and bending stress values along the cross section for Z profile sheet pile

| Height of cross section (mm) | Bending stress (MPa) | Shear stress (MPa) |
|-----------------------------|----------------------|-------------------|
| 0                           | -13.531              | 0.08              |
| 28.2                        | -6.08                | 3.35              |
| 56.4                        | -4.8                 | 3.8               |
| 84.6                        | -3.01                | 3.92              |
| 112.8                       | -1.412               | 4.13              |
| 150                         | 0                    | 4.15              |
| 169.2                       | 0.91                 | 4.12              |
| 197.4                       | 1.93                 | 4.033             |
| 225.6                       | 3.53                 | 3.75              |
| 253.8                       | 4.5                  | 3.56              |
| 282                         | 6.522                | 3.03              |
| 300                         | 13.96                | 0.082             |

Table 6 Shear stress and bending stress values along the cross section for Z profile sheet pile

| Height of cross section (mm) | Bending stress (MPa) | Shear stress (MPa) |
|-----------------------------|----------------------|-------------------|
| 0                           | -13.19               | 0.096             |
| 10.8                        | -4.26                | 3.78              |
| 21.6                        | -2.53                | 4.25              |
| 32.4                        | -1.63                | 4.44              |
| 43.2                        | -0.39                | 4.67              |
| 54                          | 0.472                | 4.7               |
| 64.8                        | 1.78                 | 4.67              |
| 75.6                        | 2.45                 | 4.47              |
| 86.4                        | 4.17                 | 4.18              |
| 97.2                        | 3.74                 | 4.19              |
| 108                         | 7.08                 | 3.85              |
| 118.8                       | 14.78                | 0                 |
Analysis of interlock in Omega/Hat section

Interlocks arrangement in omega profile is same like Z profile. It located at the outer end of the wall. But it is located only one side of the center line of the wall. The number of sheet pile
per unit length is less compare to the other profiles
due to its large width. Four nodded thin shell type of linear quadrilateral element of aspect ratio 3 is used for the analysis. From the analysis bending stress and shear stress distribution values along the cross section is obtained and it is tabulated in table 6. Fig 12 shows height of section v/s bending stress and fig.13 shows height of section v/s shear stress.

Fig.12 Height of cross section v/s bending stress for Omega/Hat profile sheet pile
SUMMARY AND CONCLUSIONS

The salient conclusions of the present study are as follows:

• Different types of steel sections are using such as U, Z and omega/hat sections. Among these sections Omega section is the most effective cross section for cold formed steel retaining wall. It has more torsion resistance, compressive resistance and low bending stress and low deflection.

• Type of loads acting, Depth of penetration and design of sheet pile wall can be done by using IS 9527 part (III).

• Finite element analysis of the sheet pile retaining wall can be done by using a four noded thin shell type of linear quadrilateral element with aspect ratio 3.

• Finite element analysis of the retaining wall can done by considering the sheet pile as a unit cell containing 6 numbers Omega/ Hat profiles.

• Hook and grip interlock is using for cold formed steel sheet piles. Interlocks are welded or applied by some adhesive material like bitumen to make the interlock leak proof and to prevent interpile slippage. Compared to plane interlock and interlock with weld, Interlock filled with bitumen gives low deflection and low bending stress under loading.

• Interlocks are the weakest points in sheet pile wall. Position of interlock and location of neutral axis will affect the stability of the structure. In loading condition, load is transferred through the interlocks by shear stress. Shear stress will be maximum at the neutral axis of the structure.

• In case of U section position of interlock and neutral axis are same. More stress will act to the interlock. It causes the interlock slippage, it leads to the failure of sheet pile wall.
Interlock for Z and Omega/Hat section is away from the neutral axis of the wall where shear stress is zero or negligible.

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