MAGNETOSPHERIC STRUCTURE AND ATMOSPHERIC JOULE HEATING
OF HABITABLE PLANETS ORBITING M-Dwarf STARS

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ABSTRACT

We study the magnetospheric structure and the ionospheric Joule Heating of planets orbiting M-dwarf stars in the habitable zone using a set of magnetohydrodynamic models. The stellar wind solution is used to drive a model for the planetary magnetosphere, which is coupled with a model for the planetary ionosphere. Our simulations reveal that the space environment around close-in habitable planets is extreme, and the stellar wind plasma conditions change from sub- to super-Alfvenic along the planetary orbit. As a result, the magnetospheric structure changes dramatically with a bow shock forming in the super-Alfvenic sectors, while no bow shock forms in the sub-Alfvenic sectors. The planets reside most of the time in the sub-Alfvenic sectors with poor atmospheric protection. A significant amount of Joule Heating is provided at the top of the atmosphere as a result of the intense stellar wind. For the steady-state solution, the heating is about 0.1\%–3\% of the total incoming stellar irradiation, and it is enhanced by 50\% for the time-dependent case. The significant Joule Heating obtained here should be considered in models for the atmospheres of habitable planets in terms of the thickness of the atmosphere, the top-side temperature and density, the boundary conditions for the atmospheric pressure, and particle radiation and transport. Here we assume constant ionospheric Pedersen conductance similar to that of the Earth. The conductance could be greater due to the intense EUV radiation leading to smaller heating rates. We plan to quantify the ionospheric conductance in future study.

Key words: magnetohydrodynamics (MHD) – planets and satellites: atmospheres – planets and satellites: magnetic fields – planets and satellites: terrestrial planets

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1. INTRODUCTION

The simple definition of planet habitability (the ability of a planet to sustain life) is whether the surface temperature of the planet allows water to exist in a liquid form (Kasting et al. 1993). The corresponding “Habitable Zone” (HZ hereafter) is the range of possible distances from the star at which a planet can have liquid surface water. This range depends primarily on the luminosity of the host star, but it can also depend on atmospheric and planetary processes that can affect the planetary surface temperature (e.g., Tian et al. 2005; Cowan & Agol 2011; Heller et al. 2011; van Summeren et al. 2011; Wordsworth & Pierrehumbert 2013). While this intuitive definition of habitability is based on our familiarity with common life on Earth, there is growing evidence that life can arise in places and in forms we do not expect. Examples of such life forms or “Extremophiles” have been found on Earth under very cold and hot temperatures, very high pressure, high salinity, high and low pH levels, high radiation levels, and in oxygen-poor environments (e.g., see Rothschild & Mancinelli 2001).

The above definition of habitability means that the search for habitable planets is focused on Earth-like, rocky planets inside the HZ. These planets are most likely to be found around M-dwarf stars, which have low luminosity so that the HZ is very close to the star, and close enough so that planets can be detected with current observational techniques. Recent surveys using the \textit{Kepler} database have identified potential Earth-like planets in the HZ, taking into account the stellar luminosity, as well as atmospheric effects such as greenhouse gasses and cloud coverage (e.g., Dressing & Charbonneau 2013; Gaidos 2013; Kopparapu et al. 2013; Kopparapu 2013; Petigura et al. 2013; Zsom et al. 2013).

M-dwarf stars may be the most feasible targets for detecting planets in the HZ. However, these stars are typically highly active magnetically, and as a fraction of their bolometric luminosity they emit more strongly at UV, EUV and X-ray wavelengths than stars of earlier spectra types (Preibisch & Feigelson 2005). If the planets are located very close to the star (as the HZ definition requires), these close-in planets can suffer from atmospheric evaporation due to the extreme EUV and X-ray radiation (e.g., Lammer et al. 2003; Baraffe et al. 2004, 2006; Tian et al. 2005; Garcia Muñoz 2007; Penz et al. 2008; Yelle et al. 2008; Murray-Clay et al. 2009), as well as from atmospheric stripping by the extreme stellar wind and coronal mass ejections (CMEs; Khodachenko et al. 2007; Lammer et al. 2007). In order to sustain its atmosphere, a close-in planet must have a strong internal pressure that opposes the stripping. Such a pressure can be provided by either a very thick atmosphere, similar to that of Venus, or a strong intrinsic magnetic field such as that of the Earth.

The dynamics and energetics of planetary upper atmospheres are dominated by the interaction of the planetary magnetic field and magnetosphere with the stellar wind, in the case of a strong planetary magnetic field, or by the direct interaction of the atmosphere with the stellar wind, in the case of a weak field. The pressure balance between the planetary atmosphere and the wind depends on the dynamic and magnetic pressure of the wind, and on the atmospheric thermal and magnetic pressure. In addition, the orientation of the magnetic field of the wind compared to that of the planetary field dictates the energy transfer from the
wind to the planet, as it drives magnetic reconnection which leads to particle acceleration and particle precipitation at the top of the atmosphere (e.g., Kivelson & Russell 1995; Gombosi 1999). Fields that drive the ions against the neutrals result in Joule Heating. The particle precipitation can impact the local ionization and alter Joule Heating processes (see, e.g., Roemer 1969; Hays et al. 1973; Deng et al. 2011, with references therein) and atmospheric line excitation (i.e., auroral excitation Chamberlain 1961; Akasofu & Kan 1981; Kivelson & Russell 1995; Gombosi 1999; Paschmann et al. 2002; Schunk & Nagy 2004). We emphasize that this ionospheric Ohmic dissipation is different to the Ohmic dissipation used to explain the inflation of hot jupiters (see, e.g., Batygin & Stevenson 2010). The latter occurs deeper in the atmosphere and is driven by the planetary magnetic field and the strong zonal winds observed in hot jupiters (Showman et al. 2008, 2009).

Cohen et al. (2011b) investigated the plasma environment and the star-planet magnetic interaction using a global magnetohydrodynamic (MHD) model for the stellar corona and the stellar wind. In their simulation, the planet was imposed as an additional boundary condition that mimics the planetary density, temperature, and magnetic field. In a similar manner, Cohen et al. (2011a) studied the impact of a CME on the atmosphere of a close-in planet. However, in these simulations, the detailed magnetospheric structure and the energy input in to the upper atmosphere as a result of the direct interaction between the planet and the stellar wind could not be investigated.

In this paper, we present a detailed study of the magnetospheric structure and the energy deposition into the upper atmosphere in close-in Earth-like planets orbiting an M-dwarf star. We use the upstream stellar wind conditions, extracted along the planetary orbit from a model for the stellar wind, to drive an MHD model for the global planetary magnetosphere and the ionosphere. We study how the dynamics and energetics of the planetary magnetosphere and ionosphere changes as a function of the stellar wind parameters, dynamic pressure, magnetic field topology, planetary field strength, and ionospheric conductance. In addition, we investigate how the transition along the planetary orbit between sub- to super-Alfvénic regime affects the magnetosphere and the energy deposition onto the planet. The Alfvénic point is defined by the Alfvénic Mach number, $M_A = u_{sw}/v_A$, which is the ratio between the stellar wind speed, $u_{sw}$, to the local Alfvén speed, $v_A = B/\sqrt{4\pi \rho}$, with $B$ being the local magnetic field strength and $\rho$ being the local mass density. Such a transition is unique for close-in exoplanets and does not exist in the solar system, where all the planets are almost always located in a super-Alfvénic solar wind flow.

In Section 2, we describe the particular systems we study and in Section 3 we describe our numerical approach. We describe the results in Section 4 and discuss their implications in Section 5. We conclude our findings in Section 6.

2. SELECTED PLANETARY AND STELLAR SYSTEMS

In principle, the study presented in this paper is rather generic and examines the fundamental response of Earth-like planets orbiting M-dwarf stars to the energy input from the stellar wind. Recently, Dressing & Charbonneau (2013) identified three candidate Earth-like planets inside the HZ of M-dwarf stars: (1) Kepler Object of Interest (KOI) 2626.01; (2) KOI 1422.02; and (3) KOI 854.01. We choose to use the known parameters of these planet candidates (shown in Table 1) to represent three typical Earth-like planets orbiting an M-dwarf star. The magnetic fields of these planets are unknown so we assume an Earth-like magnetic field of 0.3G for all planets (with the exception of modifying the field of Planet A as described in Section 4.3). Henceforward we refer to our planet cases as “Planet A” (using the parameters of KOI 2626.01), “Planet B” (with the parameters of KOI 1422.02), and “Planet C” (with the parameters of KOI 854.01), where the planets are ordered according to their distance from the star (Planet A being the closest).

The stellar wind model (described in Section 3.1) is driven by data describing the photospheric radial magnetic field (magnetograms). Such data are not available for any of the above systems. However, several observations of stars with similar parameters to those we are interested in have been made using the Zeeman–Doppler imaging (ZDI) method (Donati & Semel 1990). These observations enable construction of surface maps of the large-scale stellar magnetic field, which can be used to drive our model for the stellar wind. It is important to mention that the validity of ZDI data has been questioned, since this reconstruction process does not take into account the Stokes components that cannot be measured, and they do not account for the small-scale magnetic field that may be significant (Reiners & Basri 2009). Garraffo et al. (2013) have shown that missing small-scale flux can have a significant effect on the predicted X-ray emission, but that the wind solutions, that are the primary interested here, are much less sensitive to this and instead depend more strongly on the large-scale field.

Morin et al. (2008) have constructed ZDI maps for a number of mid M-dwarf stars. We have identified the star EV Lac, a mid-age M3.5 class star, as a star with the most similar parameters to the systems we are interested here (in particular, the effective temperature, $T_{eff}$, while the rotation periods of these systems are currently unknown). We have constructed a magnetic map based on that of Morin et al. (2008), assuming it does not contain much small-scale structure and it represents essentially a tilted dipole with a polar field strength of 1.5–2 kG.

We stress that we choose this approach in order to generate a solution with azimuthally varying plasma conditions along the planetary orbit based on typical parameters of M-dwarf stars. This could not be achieved by using an aligned dipole, which would yield a symmetric and constant solution. Here we assume that the stellar wind parameters for EV Lac are similar to those of our planets, and that these parameters can be used to study the effects of the stellar wind on the planetary magnetosphere and ionosphere. We are interested in the tentative effects on the planet due to the close proximity of the planet to the star, the high dynamic pressure, and the strong field of the stellar wind. The use of the parameters of an active M dwarf such as EV Lac (instead of the unknown parameters or idealized parameters) represents a reasonable and tractable approach.

### Table 1: Stellar and Planetary Parameters of the KOI Systems

| Planet | $R_*$ ($R_\odot$) | Stellar Temperature ($T_\odot$) | Semi-major Axis ($R_\odot$) | $B_p$ (G) | Assumed $B_p$ (G) | $F$ (W m$^{-2}$) |
|--------|----------------|-------------------------------|-----------------------------|----------|-----------------|----------------|
| A      | 0.35           | 3482                          | 36                          | 1.37     | 0.3             | 1500           |
| B      | 0.22           | 3424                          | 51.98                       | 0.92     | 0.3             | 820            |
| C      | 0.4            | 3562                          | 90                          | 1.69     | 0.3             | 255            |
Framework (SWMF; Tóth et al. 2005, 2012), which were developed at the Center for Space Environment Modeling at the University of Michigan. The SWMF provides a set of models for different domains in space physics, such as the solar corona, the inner and outer heliosphere (i.e., the interplanetary environment and the solar wind), planetary magnetosphere, planetary ionospheres, and planetary upper atmospheres. These codes are generally speaking based on solving the extended MHD or electrodynamic equations. In addition, the SWMF includes codes for the planetary radiation environment, which are particle codes. All of these models (or part of them) can be coupled together to provide solutions for the space environment that are much more detailed and physics-based than any solution provided by each of these models independently. Our modeling approach is based on a large number of studies of planets in the solar system carried out with the SWMF in a similar manner (see publications list at the http://csem.engin.umich.edu).

In this work, we use the Stellar Corona (SC) MHD code to obtain the solution for the interplanetary environment of the three planet candidates. We then use these solutions to drive a Global Magnetosphere (GM) MHD model for these planets. In order to obtain a more realistic magnetospheric solution, as well as calculating the energy input at the top of planets. We then use these solutions to obtain a more realistic magnetospheric drive a Global Magnetosphere (GM) MHD model for these planets. Once a steady-state solution is obtained, we extract the solar wind parameters of number density, $n$, velocity, $u$, magnetic field, $B$, and plasma temperature, $T$, at a given point along the orbit of one of the planets.

The SC solution is provided in the frame of reference rotating with the star (HelioGraphic Rotating coordinates or HGR). In this coordinate system, the $\hat{Z}$ axis is aligned with the rotation axis of the star, the $\hat{X}$ axis is aligned with the initial time of the ZDI observation (longitude “0”), and the $\hat{Y}$ axis completes the right-hand system. The GM model uses the Geocentric Solar Magnetospheric (GSM) coordinate system, which is identical to the Geocentric Solar Ecliptic (GSE) system for the case of a planetary dipole perpendicular to the ecliptic plane. In this special case, the planetary GSM/GSE coordinate system is defined with $\hat{X}$ pointing from the planet to the star (negative radial direction in the stellar frame of reference assuming a circular planetary orbit), $\hat{Z}$ is pointing to the north pole of the planet (perpendicular to the ecliptic plane and the plane of orbit), and $\hat{Y}$ completes the right-hand system. With a circular planetary orbit and an aligned planetary dipole, the conversion between the coordinate systems is

$$X_{\text{GSE}} = -r_{\text{HGR}} \cos \theta_{\text{HGR}},$$
$$Y_{\text{GSE}} = \phi_{\text{HGR}},$$
$$Z_{\text{GSE}} = \theta_{\text{HGR}}.$$

The orbital speed of the planet, $U_{\text{orb}}$, could be easily considered as a constant addition to $U_{\text{GSE}}$. However, it is hard to estimate what would be the change in $B_{\text{GSE}}$, which has a strong effect on the magnetospheric current system. After carefully confirming that the Alfvén Mach number with and without the addition of $U_{\text{orb}}$ is essentially the same for all cases, we have decided to exclude this motion from our simulation.

The situation in which the planets cross into the sub-Alfvénic regime, and hence the closed magnetic loops, is similar to the sub-Alfvénic motion of Io in the magnetosphere of Jupiter, where the relative speed between Io and the ambient plasma defines the structure of the magnetosphere and the angle of the Alfvén “wings” (standing magnetic lobes as described in Neubauer 1980). In our simulation, we use the planetary frame of reference and assume the velocity field at the particular point in the wind solution represents the relative velocity between the planet and the coronal plasma.

### 3.2. Global Magnetosphere and Ionosphere Models

The GM model solves the MHD equations on a Cartesian grid for the physical domain that includes the planet as the inner boundary, and the extent of the planetary magnetosphere. The model is driven from the outer boundary that is facing the star by the upstream stellar wind conditions, which can be fixed or time-dependent. This boundary is defined with inflow boundary...
conditions for all the MHD parameters for the case of super-Alfvénic stellar wind conditions. In the case of sub-Alfvénic stellar wind conditions, the boundary conditions for the pressure are changed to float in order to diminish numerical effects on the boundary from the inner domain (this does not happen for super-Alfvénic boundary conditions). For the same reason, we also set the upstream boundary very far from the planet. The boundary conditions for all the other boundaries are set to float for all the MHD parameters.

The inner boundary in GM is defined by the planetary parameters of radius, mass, magnetic field, and density (as described in Powell et al. 1999). In order to better constrain the velocities at the inner boundary, the GM model is coupled with a model for the IE, which is a completely separate model that solves for the electric potential in the ionosphere. The IE model provides the convection electric field, which is then used to calculate the velocities at the inner boundary of GM, along with the rotational velocity of the planet.

The coupling procedure, which is described in detail in Ridley et al. (2004) and in Tóth et al. (2005), begins by calculating the field-aligned currents, \( J_r(r_I) = (\nabla \times B) \cdot b, \) at \( 3R_p \) in the GM model. The currents are then mapped assuming a dipole planetary field to the ionospheric height of 120 km, using a scaling of \( B_2 \) and \( B_3 \) at the GM inner boundary.

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\[
J_r(r_I) = [\nabla \cdot (\Sigma \cdot \nabla \Psi)]|_{r=r_I},
\]

and this potential is mapped to the inner boundary of the GM at \( 2R_p \) (for numerical efficiency, the inner boundary is set higher than \( R_p \) to reduce the planetary dipole strength and increase the numerical time step). At the final stage, the electric field, \( E = -\nabla \Psi \), and the bulk convection velocity, \( V = E \times B / B^2 \), are calculated. The velocity field (along with the rotational velocity) is applied at the GM inner boundary.

The coupling of GM and IE models enables us to specify more realistic inner boundary conditions for the GM. This improved boundary specification allows us to estimate the energy input at the top of the planetary atmosphere due to its interaction with the stellar wind and the precipitating particles. Assuming the currents and the (scalar) conductance, \( \sigma \), are known in the IE model, it is trivial to calculate the Joule Heating:

\[
Q = J \cdot E = J^2 / \sigma,
\]

from the generalized Ohm's law with \( J = \sigma E \).

We note that, in a way, the electric conductance captures all the atmospheric parameters in it (chemistry, photoionization, etc.). For the case of the Earth, a more complex conductance can be used. The conductance depends significantly on the solar EUV flux (and correlates with the radio flux in the F10.7 centimeter wavelength, see, e.g., Moen & Brekke 1993), auroral particle precipitation (e.g., Robinson et al. 1987; Fuller-Rowell & Evans 1987), and other processes that are quite dependent on understanding the environment near the planet. Global models of the upper atmosphere, such as the one described by Ridley et al. (2002) can also be used, but they are driven by the observed solar luminosity and auroral precipitation, so it is difficult to drive them properly for other planets to determine the conductance patterns. In order to avoid further uncertainties, here we choose to use a constant Pedersen conductance, \( \sigma_p \), of the order of the one used for the Earth (e.g., Ridley et al. 2004). The Pedersen conductance allows the magnetospheric currents
to close through the ionosphere, and it depends on the collision frequency between electrons and ions, \( \nu_{e,i} \), and the electron plasma frequency, \( \Omega_p^2 = n_e e^2 / \epsilon_0 m_e \):
Figure 1. Coronal solution for EV Lac. Left: color contours of the photospheric radial magnetic field used in the simulation (based on the ZDI map from Morin et al. 2008) is shown on a sphere representing $r = R_\star$. Selected coronal magnetic field lines are shown in gray. Right: selected coronal magnetic field lines are shown in gray with the equatorial plain colored with contours of the ratio between the stellar wind dynamic pressure and the dynamic pressure of the ambient solar wind base on the parameters from Table 3. Also shown are the circular orbits of the three planets, and the Alfvén surface crossing of the equatorial plain (represented by the solid white line). The locations where the upstream conditions were extracted are marked in black circles for the sub-Alfvénic regions, and in white circles for the super-Alfvénic regions. The letters “F” and “S” show the location of the fast and slow super-Alfvénic conditions for planet C.

(A color version of this figure is available in the online journal.)

Table 2
Stellar Wind Parameters Used to Drive GM

| Parameter | Planet A | Planet A | Planet B | Planet B | Planet C | Planet C | Planet C |
|-----------|----------|----------|----------|----------|----------|----------|----------|
|           | Sub-Alfvénic | Super-Alfvénic | Sub-Alfvénic | Super-Alfvénic | Sub-Alfvénic | Super-Alfvénic | Super-Alfvénic |
| $n$ (cm$^{-3}$) | 1100 | 34250 | 433 | 12895 | 46 | 3200 | 123 |
| $T$ (10$^5$ K) | 5.13 | 8.37 | 3.42 | 4.77 | 4.98 | 2.22 | 1.9 |
| $u$ (km s$^{-1}$) | $(-609, -14, 39)$ | $(-140, 101, 13)$ | $(-630, -1, 30)$ | $(-202, 102, 22)$ | $(-728, -50, -17)$ | $(-278, 92, 26)$ | $(-660, 8, 14)$ |
| $B$ (nT) | $(-1950, -377, 170)$ | $(-171, 438, 167)$ | $(-804, -173, 63)$ | $(-57, 223, 92)$ | $(240, 88, 17)$ | $(-14, 95, 42)$ | $(-244, 74, 18)$ |
| $5M_A$ | 0.46 | 2.95 | 0.73 | 4.76 | 0.88 | 7.25 | 1.3 |

Table 3
Solar Wind Parameters

| Parameter | Background Solar Wind | CME Conditions |
|-----------|-----------------------|----------------|
| $n$ (cm$^{-3}$) | 5 | 50 |
| $T$ (K) | $10^4$ | $5 \times 10^4$ |
| $u$ (km s$^{-1}$) | $(-500, 0, 0)$ | $(-1500, 0, 0)$ |
| $B$ (nT) | $(0, 0, -5)$ | $(0, 0, -100)$ |

For super-Alfvénic upstream conditions, an Earth-like magnetospheric configuration forms with the planetary field lines being draped over by the stellar wind, and a magnetopause bow shock being forming in front of the planet along with a magnetotail behind.

The transitioning between sub- to super-Alfvénic conditions occurs twice per orbit and within a short time. This has implications for the energy input into the upper atmosphere, which are discussed in Section 4.4.

4.3. Steady State Joule Heating

Figure 3 shows the distribution of the height integrated ionospheric Joule Heating, $Q_h$, (in units of W m$^{-2}$) in a format of polar plots. Each pair of panels shows the Joule Heating for one of the three planets extracted from a steady-state GM-IE simulation. The heating is clearly stronger for the closer orbit of Planet A than the more distant orbit of Planet C, for which the color scale of the plot has been extended to lower values of heating for clarity. The figure also shows that the heating is stronger for super-Alfvénic stellar wind conditions than for sub-Alfvénic conditions, and that the distribution is asymmetric, as expected, due to the asymmetric stellar wind magnetic field and magnetospheric field-aligned currents.
Figure 2. Magnetospheres of Planet A (top) and Planet B (bottom) for sub-Alfvénic (left) and super-Alfvénic (right) stellar wind conditions. Color contours show the number density (note the different scales in the panels) and selected magnetic field lines are shown in gray. The direction of the star (the direction from which the stellar wind is coming) is marked by the small yellow Sun shape. The structures and trends are similar for Planet C.

(A color version of this figure is available in the online journal.)

For comparison with the case of the Earth, we ran the model using the planetary parameters of the Earth, and upstream conditions of a typical quiet solar wind, as well as with upstream conditions of a strong CME event. The upstream parameters of these reference runs are summarized in Table 3. Figure 4 shows the ionospheric Joule Heating for Planet A and for these reference Earth cases. It shows that the heating by the ambient stellar wind conditions at close-in orbits is about four orders of magnitude higher than the case of the ambient solar wind conditions at Earth, and is even higher than the heating during a strong space weather event on Earth.

The top panel in Figure 5 shows the total area integrated power, \( P = \int Q_\text{da} \), for all the solutions, where \( da \) is the surface element of the two-dimensional ionospheric sphere. It is consistent with the trend which is usually seen in Figure 3, with the power being the greatest for the closest planet. For the Planet A, the power reaches \( 10^{14} \text{--} 10^{15} \) W, which is 0.01%--0.1% of the total incident radiation of the M-dwarf star, assuming \( L_{\text{bol}} = 4.5 \times 10^{24} \) W, \( a = 0.06 \) AU (36 \( R_\star \)), and \( P \approx (1/4)L_{\text{bol}} \left( R_\star / a \right)^2 \approx 10^{18} \) W. Since the planetary albedo is likely not zero, much of this radiation will be reflected, and the significance of the Joule Heating can be even greater. For all cases, the heating in the super-Alfvénic regime is higher than the sub-Alfvénic one, and for the case of Planet C, the heating is greater for the super-Alfvénic regime with a slow stellar wind than for the super-Alfvénic upstream conditions with a fast stellar wind. This is due to the order of magnitude density variation of the stellar wind upstream conditions, which increases the wind’s dynamic pressure (i.e., \( \rho u_w^2 \)). Moreover, the super-Alfvénic sectors are located near the helmet streamers, where the velocity component which is not parallel to the magnetic field (i.e., the non-radial component) is greater. As a result, and the upstream electric...
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Figure 3. Height-integrated Joule Heating (in W m$^{-2}$) of the ionospheres of Planet A (top), Planet B (middle), and Planet C (bottom) for sub-Alfvénic (left) and super-Alfvénic (right) stellar wind conditions displayed in polar plots of the planetary northern hemisphere. The sub-stellar point (day side) is marked by the small Sun shape. Note that the heating of Planet C is displayed on a reduced color scale (marked with *). The distribution of the Joule Heating in the southern hemisphere is similar, but is mirrored toward the night side instead of the day side.

(A color version of this figure is available in the online journal.)

Figure 3. Height-integrated Joule Heating (in W m$^{-2}$) of the ionospheres of Planet A (top), Planet B (middle), and Planet C (bottom) for sub-Alfvénic (left) and super-Alfvénic (right) stellar wind conditions displayed in polar plots of the planetary northern hemisphere. The sub-stellar point (day side) is marked by the small Sun shape. Note that the heating of Planet C is displayed on a reduced color scale (marked with *). The distribution of the Joule Heating in the southern hemisphere is similar, but is mirrored toward the night side instead of the day side.

(A color version of this figure is available in the online journal.)

field, \( \mathbf{E} = -\mathbf{u} \times \mathbf{B} \), which dictates the ionospheric electric potential and the coupling between the stellar wind and the planetary magnetosphere, is larger as well.

In the middle panel of Figure 5, we show the Joule Heating power for different planetary magnetic field strengths for the sub- and super-Alfvénic upstream conditions in Planet A, along with the reference Earth cases. The power is greater for the weaker planetary fields due to the strong penetration by the stellar wind. As the field increases to 1G, the wind is pushed back and the energy input to the upper atmosphere is reduced.
Figure 4. Height-integrated Joule Heating (in W m$^{-2}$) of the ionospheres of Planet A (top), and for ambient solar wind (bottom-left) and CME (bottom-right) conditions at Earth taken from Table 3. The display is similar to that of Figure 3. (A color version of this figure is available in the online journal.)

In addition, the total size of the heated polar cup is reduced too. Due to the uncertainties about the planetary magnetic field, here we assume a planetary dipole field aligned with the stellar rotation axis. We omit the effect of different dipole orientation, which could affect the energy input as a result of magnetic reconnection between the stellar wind and the planetary magnetosphere (e.g., a geomagnetic storm).

The bottom panel of Figure 5 shows the Joule Heating power for an ionospheric conductance of 0.25 (the value used for all simulations), 5, and 50 Siemens for the sub-Alfvénic case of Planet A, along with the reference Earth cases. As mentioned in Section 3.2, the actual ionospheric conductance depends on the atmospheric density, composition, the level of ionization, and the level of photoionization (the stellar EUV and X-ray flux). The power varies inversely with the value of the conductance. As the conductance represents the mobility of the ions, a lower value means that the ions are less mobile and collide more frequently with neutrals. As a result, the energy dissipation (or Joule Heating) increases. We note that for the case of close-in planets orbiting M-dwarf stars, the intense EUV radiation may boost the ionospheric conductance to much greater values and as a result, the Joule Heating may be lower than predicted here. However, due to the many uncertainties in defining the atmospheres of these planets, we leave the investigation of this particular issue to a future, separate study.

4.4. Time-dependent Solution for Planet A

The results presented in Sections 4.2 and 4.3 are the steady-state solutions for the different planets, which are driven by the upstream stellar wind conditions extracted from the SC solution at particular locations along their orbit. As stated in Section 4.2, the magnetospheric structure undergoes significant change as the planets move from the sub- to super-Alfvénic plasma sectors along the orbit. In order to obtain the dynamic effect of such a transition, we performed a time-dependent simulation of Planet A starting at a sub-Alfvénic sector and ending in a super-Alfvénic sector. In this time-dependent simulation, the upstream conditions in GM are updated every 2.52 hr (10 degrees of the orbit of 4.3 days) so that the change in the driving stellar wind conditions is captured (in contrast to the single set of stellar wind conditions for the steady-state).

Figure 6 shows the magnetospheric structure, as well as the Joule Heating in the ionosphere at after 2:52 hr, 22:52 hr, 25:44 hr, and 26:36 hr. The planet moves to the super-Alfvénic sector around 25:00 hr, with the white line in the lower two panels representing the $M_A = u_{sw}/v_a = 1$ line. This line also helps to identify the magnetopause bow shock built in front of the planetary magnetosphere as the planet transitions to a super-Alfvénic sector. It can be clearly seen from the top four panels in Figure 6 that there is a significant heating
Figure 5. Top: the total power (in W) of the integrated Joule Heating for all the planets and reference Earth cases. Middle: the total Joule Heating power for Planet A as a function of planetary magnetic field strength shown for the sub-Alfvénic (red) and super-Alfvénic (green) cases. Also shown are the reference Earth cases (blue). Bottom: the total Joule Heating power for Planet A for sub-Alfvénic (red) conditions as a function of the ionospheric conductance. Also shown are the reference Earth cases (blue).

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Figure 6. Results from the time-dependent simulation of Planet A for 2:52 hr, 22:52 hr, 25:44 hr, and 26:36 hr. The top panels show snapshots of the ionospheric Joule Heating with a display similar to that of Figure 3. The middle panels show $y = 0$ cuts colored with contours of number density. The solid white line represents the $MA = 1$ line as the planet passes from the sub- to the super-Alfvénic sector. The bottom panel shows the time evolution of the magnetosphere with a display similar to that in Figure 2. The direction of the star in all panels is marked by the small yellow Sun shape.

(A color version of this figure is available in the online journal.)

of the upper atmosphere as the planet transitions between the sectors.

Figure 7 shows the temporal change in the total power as a result of the planetary motion along the orbit. The total power increases by 50% as the planet moving from the sub- to super-Alfvénic sector. The heating in the sub-Alfvénic sector is 10 times higher in the dynamic simulation compared to the steady-state obtained at the same point, and the heating in the super-Alfvénic sector is 50% higher in the dynamic simulation compared to the steady-state obtained at the same point (in this case, the heating is almost 1% of the incident stellar radiative power). This is due to the fact that the dynamic simulation captures the temporal change in the magnetic field, which drives stronger field-aligned currents (the time derivative of the magnetic field is zero for the steady state, but can and does vary in the time-dependent case).

5. DISCUSSION

The results of our simulations reveal a number of interesting findings regarding close-in planets orbiting M-dwarf stars. These findings relate to the extreme space environment surrounding these planets and planetary shielding and protection, the change in the magnetospheric structure as a result of the planetary orbital motion, and the Joule Heating of the upper atmospheres as a result of the interaction with the stellar winds. Below, we discuss in detail each one of these findings.

5.1. Extreme Space Environment and Planetary Protection

Our results show in detail that the space environment of close-in exoplanets is much more extreme in terms of the stellar wind dynamic pressure, magnetic field, and temperature. Each of these parameters is about one to three orders of magnitude higher than the typical solar wind conditions near the Earth. The ultimate consequence of such an extreme environment, in the context of this paper, is the potential for stripping of the planetary atmosphere (in addition to atmospheric evaporation by the enhanced EUV/X-ray stellar radiation, Lammer et al. 2003). The process of atmospheric erosion due to the impact of an ionized wind is complex, and here we simply examine the degree to which the planetary magnetosphere is penetrated by the wind.

On this basis, a planetary magnetic field similar to that of the Earth seems to be strong enough to largely resist the stellar wind in the super-Alfvénic sectors. However, in the case of the sub-Alfvénic sectors there is no bow shock at all, and many field lines are connected directly from the stellar wind to the planet, resulting in poor atmospheric protection. As a matter of fact, Planet A is located for most of its orbit in a sub-Alfvénic plasma and the assumption of the existence of a bow shock (e.g.,
Grießmeier et al. (2004; Khodachenko et al. 2007; Lammer et al. 2007; Vidotto et al. 2011) may not be relevant for planets of this kind.

Grießmeier et al. (2004) have studied the atmospheric protection for hot-jupiter planets using scaling laws for the stellar mass loss and the planetary magnetic moment, and by estimating the atmospheric loss of neutral hydrogen. They concluded that hot-jupiters may have been significantly eroded during the early stages of the stellar system when stellar magnetic activity was high, and assuming that the mass-loss rate of young stars is comparatively high (about 100 times the current solar value, Wood et al. 2002). Other estimates of the mass loss rates of young stars suggest that the winds might not be so strong (only about 10 time the current Sun, Holzwarth & Jardine 2007; Sterenborg et al. 2011). In the case of the planets studied here, we do not include any atmospheric outflow. However, our simulations demonstrate that in order to estimate such an outflow and the degree of planetary protection afforded by a magnetic field, one should consider not only the magnitude of the stellar wind pressure, but also whether the surrounding space plasma is sub- or super-Alfvénic and the orientation of the stellar magnetic field, as it may allow stellar wind particles to flow directly into the planetary atmosphere.

5.2. Change in Magnetospheric Structure Along the Orbit

The time-dependent results show that the magnetospheres of the planets under study experience significant changes in their topology and nature on timescales of a few hours, due only to their transition through different plasma conditions along their orbit. While the magnetospheres have an Earth-like structure during times when the planet passes through super-Alfvénic sectors, they have an Io-like Alfvén wing shape during times when the planet passes through sub-Alfvénic sectors. Planet A and Planet B reside in the sub-Alfvénic sectors for most of their orbits. Surprisingly, the super-Alfvénic sectors are associated with slower wind speed. These sectors are super-Alfvénic due to the order of magnitude increase in the plasma density, which reduces the Alfvén speed in the wind.

On the Earth, the Cross Polar Cap Potential (CPCP) is the difference between the maximum and minimum ionospheric electric potential. It is associated with the solar wind driver and it becomes saturated during major CME events (e.g., Reiff et al. 1981; Siscoe et al. 2002). In the case of the planets studied here, the strong driving stellar wind is reflected in a saturated CPCP, where the magnitude of the CPCP is $10^2–10^3$ kV—much greater than a potential of about 50 kV for the ambient solar wind conditions and 1000 kV for CME conditions. Ridley (2007) and Kivelson & Ridley (2008) have discussed the dependence of the CPCP on the solar wind conditions. They showed that for larger $v_A$ (and likely sub-Alfvénic flow), the solar/stellar wind conductance, $\Sigma_A = (\mu_0 v_A)^{-1} (\mu_0$ is the permeability of free space), is smaller than the ionospheric conductance, $\Sigma_p$, and as a result, the reflected fraction of the stellar wind electric field becomes larger than the incident one and the CPCP becomes saturated. In the case of our hypothetical planets, the stellar wind is always extremely strong. Therefore, it seems likely the CPCP in these planets is always saturated, unless $\Sigma_p$ is reduced even further due to the space environment conditions so it is again smaller than $\Sigma_A$. This can prevent from the stellar wind electric field to reflect and the CPCP is again in a non-saturated state. As mentioned in Section 3.2, we leave the detailed calculation of the ionospheric conductance in close-in exoplanets to future study.

5.3. Joule Heating of the Upper Atmosphere

Our results show that there is a significant Joule Heating at the upper atmospheres of the planets as a result of interaction with the extreme stellar wind. Overall, the heating is two to five orders of magnitude higher than that of the Earth during quiet solar wind conditions. The quiet-time heating for close-in exoplanets is even higher than those obtained on Earth during a strong CME event. It is most likely that the heating is even greater during CME events on these close-in planets as the energy deposited in such events can be three orders of magnitude larger than a typical CME on Earth (Cohen et al. 2011a). The time-dependent simulation of Planet A shows that additional heating is available to the sharp and quick changes in the magnetospheric topology as the planet passes between the sub- to the super-Alfvénic sectors. In a way, these changes can be viewed as if a CME hits the planet twice in an orbit, leading to sharp and fast changes in the conditions of the driving stellar wind.

As expected, the heating decreases with the increase of the planetary field strength as the planetary magnetic pressure reduces the stellar wind forcing. Of course, this can be modified by the particular orientation of the planetary and stellar magnetic fields as further heating can be driven by magnetic reconnection,
which accelerates the precipitating electrons to higher energies (Kivelson & Russell 1995; Gombosi 1999). Our simulations also show that the heating increases with the decrease of the Pedersen conductance in the ionosphere. This is important because the conductance captures the role of the upper atmosphere in the energy input from the stellar wind. In reality, the conductance is defined by the atmospheric parameters and conditions. By estimating these parameters using a more detailed modeling (e.g., Ridley et al. 2002, 2004), one can obtain a good estimation of the conductance and the overall heating of the top-side atmosphere by the interaction with the stellar wind.

While the Joule Heating of the upper atmosphere is far smaller than the planetary core Joule Heating necessary to explain the inflation of hot Jupiter planets (Batygin & Stevenson 2010; Perna et al. 2010; Huang & Cumming 2012; Menou 2012; Rauscher et al. 2002, 2004), it is still significant in terms of the energy balance of the atmosphere. For the ambient stellar wind conditions, the heating of 10–50 W m⁻² can reach 0.1%–3% of the total stellar irradiating input shown in Table 1. As stated above, it can be even greater for periods of CMEs, as we expect the CME rate in M-dwarf stars to be high (Güdel 2007). The additional heating at the top of the atmosphere is important for modeling the atmospheres of habitable planets (e.g., Kasting et al. 1993; Spiegel et al. 2008; Heng & Vogt 2011; Tian et al. 2014) as they affect the atmospheric temperature. Therefore, these models should take in to account the atmospheric Joule Heating in the context of their pressure boundary conditions. In addition, Joule Heating at the top of the upper atmosphere transfers the energy to the thermosphere below, driving changes in the temperature, density, and pressure in the form of acoustic and gravity waves. As the changes in the magnetosphere and Joule Heating repeat along the orbit, it would be interesting to study the timescale of the change in the driving force (i.e., the stellar wind conditions along the orbit), to the propagation timescale of the planetary perturbations. However, this study is beyond the scope of this paper.

6. SUMMARY AND CONCLUSIONS

In this paper, we study the magnetospheric structure and the ionospheric Joule Heating of habitable planets orbiting M-dwarf stars using a set of MHD models. The stellar wind solution is obtained using an MHD model for the stellar corona, which is driven by the magnetic field observations and the stellar parameters of EV Lac—a mid-age M-dwarf star. We investigate how the Joule Heating affects the upper atmospheres of three hypothetical planets located at the orbits of the three KOIs around EV Lac. We use the stellar wind conditions extracted at particular locations along the planetary orbit to drive an MHD model for the planetary magnetosphere, which is coupled with a model for the planetary ionosphere. The solutions from these simulations provide the magnetospheric structure and the Joule Heating of the upper atmosphere as a result of the interaction with the stellar wind.

Our simulations reveal the following major results.

1. The space environment around close-in exoplanets can be very extreme, with the stellar wind dynamic pressure, magnetic field, and temperature being one to three orders of magnitude stronger than that at 1 AU. The stellar wind conditions along the planetary orbit change from sub- to super-Alfvénic.

2. The magnetosphere structure changes dramatically as the planet passes between sectors of sub- to super-Alfvénic plasma. While a bow shock is formed in the super-Alfvénic sectors, the planets reside in a sub-Alfvénic plasma for most of the orbit, where no bow shock is formed and the stellar wind is directed toward the planetary surface. In this case, the protection of the planetary atmosphere is poor.

3. A significant amount of Joule Heating is provided at the top of the atmosphere as a result of the planetary interaction with the stellar wind. The heating is enhanced in the time-dependent calculation as a result of the additional current due to the temporal changes in the magnetic field. For the steady-state, the heating is about 0.1%–3% of the total incoming stellar irradiation, and it is enhanced by 50% for the time-dependent case.

4. The transitioning between the plasma sectors along the planetary orbit has quantitative similarities to an exoplanet interacting with a CME.

5. The significant Joule Heating obtained here should be considered in models for the atmospheres of HZ planets in terms of the top-side temperature, density, and boundary conditions for the atmospheric pressure. We note that due to the intense EUV radiation, the ionospheric conductance in close-in planets could be much greater than Earth’s value used here so the Joule heating can be smaller.

In this work, we have studied the interaction of magnetized habitable planets with the stellar wind. However, it is not clear whether the planetary magnetic fields of these planets are strong or weak. Alternatively, planets can have a thick enough, Venus-like atmosphere that can sustain the extreme stellar wind. We leave the investigation of such an interaction for future study.

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