Harvesting the Potential of CO$_2$ before it is Injected into Geological Reservoirs

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Abstract
To store CO$_2$ in geological reservoirs, expansion valves have been used to intentionally release supercritical CO$_2$ from high-pressure containers at a source point to lower-pressure pipelines and transport to a selected injection site. Using expansion valves, however, has some shortcomings: (i) the fluid potential, in the form of kinetic energy and pressure which can produce mechanical work or electricity, is wasted, and (ii) due to the Joule-Thomson cooling effect, the reduction in the temperature of the released CO$_2$ stream might be so dramatic that it can induce thermal contraction of the injection well causing fracture instability in the storage formation. To avoid these problems, it has been suggested that before injection, CO$_2$ should be heated to a temperature slightly higher than that of the reservoir. However, heating could increase the cost of CO$_2$ injection. This work explores the use of a Tesla Turbine, instead of an expansion valve, to harvest the potential of CO$_2$, in the form of its pressure and kinetics, to generate mechanical work when it is released from a high-pressure container to a lower-pressure transport pipeline. The goal is to avoid throttling losses and to produce useful power because of the expansion process. In addition, due to the friction between the gas and the turbine disks, the expanded gas temperature reduction is not as dramatic as in the case when
an expansion valve is used. Thus, as far as CO₂ injection is concerned, the need for preheating can be minimized.

**Keywords**

CO₂ sequestration; tesla turbine; geological reservoirs

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1. Introduction

Expansion valves, including regulators, throttling valves, capillary tubes, etc., have been used to intentionally reduce the potential of a carrier fluid when it is delivered from a high-pressure container to the consumers or to the utilization sites at low specified pressure levels. In carbon capture and storage in formations beneath the earth surface, CO₂ generated from the main point source is stored in high-pressure containers. Expansion valves are usually used to release it to carrying pipelines with lower pressure for transporting it to a selected geological reservoir for long-term storage. Before injecting, CO₂ would need to be heated to a temperature slightly higher than that of the reservoir to avoid CO₂ condensation in the injection well and fracture instability in the storage formation [1-4]. Using expansion valves, however, has some shortcomings: (i) the fluid potential, in the form of kinetic energy and pressure, that can produce mechanical work or electricity, is wasted. In fact, a great deal of energy has been wasted due to all kinds of expansion valves that have been used to intentionally release and deliver natural gases from high-pressure lines to the consumers at lower specified pressure levels [5]. And (ii) the expanded CO₂ stream might be significantly cooled down due to the Joule-Thomson cooling effect. For CO₂ stored in a container of 40 °C and pressures of 25 to 15 MPa, the Joule-Thomson cooling effect could generate a decrease in the CO₂ temperature by 8 °C to 11 °C, respectively, as it expands to enter a transport pipeline of 8 MPa. Since CO₂ preheating consumes energy and expensive [6, 7], the Joule-Thomson cooling effect would dramatically increase the energy cost of injecting CO₂ in storage projects.

This work reports an exploratory study on the possibility of using a Tesla turbine, instead of a throttling/expansion valve, for releasing and delivering CO₂ from a high-pressure storage container to a transport pipeline at a lower pressure. Thus, the Joule-Thomson cooling effect is eliminated. Tesla turbines are simple, reliable, and bladeless (Figure 1). They are composed of flat, thin, and parallel co-rotating disks arranged normal to a shaft. When a working fluid is flowing through the gaps between the rotating disks, the shearing forces between the fluid and the rotating disks generate torques about the shaft producing mechanical work. Thus, when CO₂ is released through the gaps of a Tesla turbine, instead of an expansion valve, its potential, in the form of pressure, can be harvested to generate mechanical work. The novel concept of the present work is the use of a Tesla turbine as an alternative to a conventional expansion valve of any kind to avoid throttling losses and to produce useful power which can be used to generate electricity or to preheat CO₂ before injection. In addition, due to the friction between the gas and the turbine disks, the expanded gas temperature reduction is not as dramatic as is the case when an expansion valve is used. Thus, as far as CO₂ injection is concerned, the energy cost of injecting CO₂ can be minimized.
In summary, the use of a Tesla turbine as a high-pressure CO\textsubscript{2} expansion device, its potential in the form of pressure and kinetics can be harvested to generate work and heat to preheat CO\textsubscript{2}. Hence, characterizing the performance of a Tesla turbine using CO\textsubscript{2} as the working fluid is necessary. Tesla turbines have been investigated using air or water as the working fluid. Only in the last few years the Tesla turbine has been considered as a possible alternative to micro expanders for organic Rankine cycles [8, 9]. Song et al. [9] developed a code to assess the thermodynamic efficiency, as well as the power produced by a Tesla turbine working with different organic fluids. Aghagoli and Sorin [10] proposed a new transcritical carbon dioxide heat pump cycle, where a Tesla turbine was used to replace the expansion valve. They demonstrated that the coefficient of performance of the cycle is up to 16.3\% higher than the traditional cycle with an expansion valve. In addition, when the rotor angular velocity is about 1000 rad/s, the turbine power is at its maximum; increasing the inlet pressure leads to the higher torque and consequently higher turbine power. At lower inlet pressure, the coefficient of performance of the heat pump cycle is higher. However, to the best of our knowledge, there are no studies investigating the use of a Tesla turbine as an integral component for CO\textsubscript{2} expansion, transport, and injection for long-term storage. Therefore, the main objective of this work is to estimate the Tesla turbine power output and its angular velocity when supercritical CO\textsubscript{2} of high pressure is released and delivered by a lower-pressure transport pipe. Such estimation will be carried out under a wide range of inlet and outlet pressures to show that as high-pressure CO\textsubscript{2} is released through a Tesla turbine, instead of a throttling/expansion valve, its potential to generate mechanical work is not wasted and can be harvested.

2. Simple Analysis

Conventional gas turbines expand the working fluid over the (aerodynamic) blades, producing a lift force on each blade that induces torque about the rotating drive shaft. A Tesla turbine relies on the fluid wall shear stress on the disks to convert the energy of the fluid to generate torque acting on the shaft. Figure 2 shows the release of supercritical CO\textsubscript{2} from a high-pressure container into a lower-pressure transport pipe via a Tesla turbine. As it is released, supercritical CO\textsubscript{2} enters the gap between the two rotating disks and exits the turbine after circulating about 360 degrees around the

![Figure 1: A schematic of a Tesla turbine.](image)
shaft. While it flows between the disks, its momentum is reduced because part of it is used to generate torque to rotate the disks. Comprehensive assessment of Tesla turbine performance can be found in available literature [8, 11-13]. In these reports, the assessment was done through using the Navier-Stokes equations in cylindrical coordinates, under the assumptions of incompressible steady flow and neglecting the body forces.

**Figure 2** CO₂ released from a high-pressure container to a low-pressure transport pipe via a Tesla turbine; \( P_\text{in} \) and \( T_\text{in} \) are the pressure and the temperature of CO₂ leaving the high pressure container and entering turbine. \( P, T, \) and \( V \) are the pressure, the temperature, and velocity of the CO₂ stream flowing through and leaving the turbine, \( T \) is the tesla turbine).

Tamir et al. [14] reported, both experimentally and analytically, a study on Tesla stall torques with air as the working fluid. By assuming laminar flow over a flat plate, an analytical model was developed where the turbine disk is divided into four separate pieces (one-quarter of the disk for each inlet port). Each piece has a length equal to a quarter of the disk’s circumference, and a width equal to the difference between the outer and the inner disk radius. The shear force induced by the flow over these four separate pieces was assumed to be the shear induced by the laminar flow over a flat plate acting at the center of each plate. Comparing with the measured results, the model was seen to overpredict the measured Tesla turbine stall torques for inlet velocities up to 100 m/s, and under-predict the measured values for inlet velocities higher than 100 m/s. With considerations given to the uncertainties in the experimental data, the model predictions were in good agreement with the measured values, especially in the regime of high inlet flow velocities. In our present work,
we simply estimate the power harvested by CO$_2$ expansion using the pressure of the container, the pressure of the transport pipelines and the external torques as the parameters. Thus, this simple approach appears to be reasonable enough for the present calculations. The shear force induced by the flow is given as

$$F_t = 5.312U^{3/2}R_o^{3/2} \left(1 - \frac{R_i}{R_o}\right) \sqrt{\frac{\pi \rho \mu}{4} \left(1 + \frac{R_i}{R_o}\right)}$$  \hspace{1cm} (1)

Where $R_i$ and $R_o$ are the rotating disk inner and outer radius, respectively, $U$ is the velocity of CO$_2$ flowing through the gap between the disks, $\rho$ and $\mu$ are the CO$_2$ density and viscosity respectively, and the linear velocity $U$ is

$$U = V - V_D = V - R_o \omega$$  \hspace{1cm} (2)

Where $V$ (m/s) is the velocity of CO$_2$ flowing through the gap and $V_D$ (m/s) and $\omega$ (rad/s) are the tangential and the angular velocities of the rotating disks, respectively. The resulting torque, $\tau_{strs}$, is calculated by multiplying the shear forces by a lever arm equal to the distance from the disk's center to half the disk's width

$$\tau_{strs} = 10.624U^{3/2}R_o^{5/2} \left(1 - \frac{R_i}{R_o}\right) \left(1 + \frac{R_i}{R_o}\right) \sqrt{\frac{\pi \rho \mu}{4} \left(1 + \frac{R_i}{R_o}\right)}$$  \hspace{1cm} (3)

And the power, $P_w$ (W), is calculated as

$$P_w = \tau_{strs} \omega$$  \hspace{1cm} (4)

The power per unit mass, $p_w$ (J/kg) is.

$$p_w = \frac{P_w}{\dot{m}} = \frac{P_w}{(R_o - R_i) \delta \rho_{CO_2}}$$  \hspace{1cm} (5)

Where $\dot{m} = (R_o - R_i) \delta \rho_{CO_2}$ is the CO$_2$ mass flow rate, $\delta$ is the space between the rotors.

### 2.1 Turbine Angular Velocity, $\omega$ (rad/s)

As the working fluid enters and flows through the gap between the stationary disks, a velocity gradient near the disk is developed; this is responsible for the generation of the shear stress which in turn develops a torque, $\tau_{strs}$, on the disk. When the turbine is not loaded, the resisting torque is the frictional torque of the shaft. If the torque developed by the shear stress is greater than the frictional torque, $\tau_{fr}$, the disk will start rotating. If the turbine is loaded, the resisting torque is now due to the load, $\tau_{load}$, and the frictional torque, $\tau_{fr}$. With the resistant torque $\tau_r = \tau_{fr} + \tau_{load}$, the angular speed is calculated as

$$\tau_{strs} - \tau_r = I \frac{d\omega}{dt}$$  \hspace{1cm} (6)
Where \( I \) is the moment of inertia of the rotating disks. With the disk thickness \( \beta \), each channel has two rotating disks, and if the turbine density is \( \rho_t \), then the turbine mass is approximated as the mass of the channel \( m = 2\pi \rho_t R_0^2 \beta \); thus, the moment of inertia \( I \) is

\[
I = \frac{mR_0^2}{2} = \pi \rho_t R_0^4 \beta \tag{7}
\]

With Eqn. (7), the angular speed is determined as

\[
\frac{d\omega}{dt} = \frac{(\tau_{strs} - \tau_r)}{\pi \rho_t R_0^4 \beta} \tag{8}
\]

### 2.2 Calculating the Fluid Velocity \( V \)

The velocity of \( \text{CO}_2 \) at the turbine inlet is assumed to be zero. However, the velocity of \( \text{CO}_2 \) as it passes through the turbine is not negligible. Referring to Figure 2, the momentum conservation across the turbine can be written as

\[
\text{Momentum}: P_1 - \frac{F_t}{A_t} = P + \rho V^2 \tag{9}
\]

The \( \text{CO}_2 \) velocity entering the rotors is calculated from Eqn. (9) as

\[
V = \left( \frac{P_1 - \frac{F_t}{A_t} - P}{\rho} \right)^{1/2} \tag{10}
\]

Where \( A_t \) is the cross sectional area of the gap. With \( \delta \) as the gap space, \( A_t \) is approximated as

\[
A_t = (R_o - R_i) \delta \tag{11}
\]

### 2.3 Thermophysical Properties of \( \text{CO}_2 \)

Fundamental equations for calculating the thermodynamic properties of \( \text{CO}_2 \) have been reported in literature [15-17]. These equations were expressed in terms of the dimensionless Helmholtz free energy \( (A/RT) \) which depends on density and temperature and they are applicable for the temperature range from the Triple-Point to 1100 K and pressures up to 800 MPa. For the transport properties, the correlations developed by Vesovic et al [18] and Fenghour et al. [19] for the transport properties of \( \text{CO}_2 \) are used in our analysis. We then compare the results with those obtained from NIST database [20]. It was found that the average deviation is about 0.2% for \( \text{CO}_2 \) density and less than 0.1% for all other properties.

### 3. Results and Discussions

In this section we will present our results for the estimated turbine output power using the analytical equations presented in Section 2; the power output is a function of the external torques, the pressures of the container and of the transport pipelines. For a given load, the performance of
a Tesla turbine depends on the geometric parameters of the turbine (for example, the main geometric parameters are the ratio between the inlet and the outlet disk radius, the external diameter of the space between the disks, the thickness of the disks, etc.) and the operating conditions (inlet/outlet pressures, inlet/outlet temperatures). The turbine material influences its angular speed as shown by Eqn. (8). The heat transfer between the fluid and the turbine can affect the CO₂ exhaust temperature as mentioned in the introduction. Thus, both turbine material and heat transfer might have some effects on the numerical values of the calculated output power. Their roles, however, on the manner by which the output power can depend on the external torques, the pressures of the container and the transport pipelines are insignificant. Therefore, in this work, we did not include the heat transfer effect and we only looked at the effects of the operating conditions while the turbine geometric parameters as well as its material were kept unchanged. The operating conditions here are mainly the pressures and the temperatures of the high-pressure container and of the transport pipelines. Since CO₂ remains supercritical for the conditions of pressure and temperature of many geological reservoirs, its state during the injection process must be supercritical. Thus, the pressures in the transport pipelines are chosen from 8 to 12 MPa and the pressures of the high-pressure container are from 15 MPa to 25 MPa.

In a Tesla turbine, as the fluid enters at a high velocity, a velocity gradient near the disks is developed, generating the shear stress which in turn develops the torque, \( \tau_{stres} \), on the disks. When the turbine is not loaded the resisting torque is the frictional torque of the shaft. If the torque developed by the shear stress is greater than the frictional torque, \( \tau_{fr} \), the disk will start rotating. As the disk rotating speed increases, the relative velocity of the fluid with respect to the disk, \( \omega \), decreases and so is the shear stress causing the torque. Eventually, the torque due to the shear stress is balanced by the frictional torque and a steady-state condition is reached; the disk is rotating at a constant angular velocity. For the same inlet/outlet conditions, if the turbine is loaded, the resisting torque is due to the load and the frictional torques, and the rotational speed at steady state will be less than that of the steady rotational speed at no load. Thus, using steady-state condition, the performance of a Tesla turbine in terms of its angular velocity and the power output under various load conditions are determined.

Examples of such steady-state conditions are shown in Figure 3, Figure 4 and Figure 5. Figure 3 shows the results on the angular velocity, \( \omega \), and the relative velocity, \( U \), as a function of time due to the effect of the external loads while the inlet pressure and the outlet pressure are kept constant at 20 MPa and 8 MPa, respectively. The results indicate that for a given load, the angular velocity increases rapidly and levels off to a constant value after a short time. The values of the angular velocity are seen to increase as the load decreases. For example, when the load is 0.1 N-m, the angular velocity increases rapidly and reaches the steady state condition at 2382 rad/s after about 3 s. When the load is 2.5 N-m, the steady state condition is reached just after 2.1 s and the angular velocity is 278 rad/s. The effects of the external load on the relative velocity \( U \) as a function of time can be seen from Figure 3(b). For a fixed condition of the inlet and the outlet pressures, the magnitude of the relative velocity at steady state increases with the external load. In the range of the external loads and the operational pressures reported here, the relative velocity of about 180 m/s is achievable with the external load of 2.5 N-m when the operating condition is kept at 25 MPa inlet pressure and 8 MP outlet pressure.
Figure 3 (a) Angular velocity, $\omega$, and (b) the relative velocity, $U$, as a function of time. The effect of the load, (Inlet pressure = 20 MPa; Outlet pressure = 8 MPa; $T_0 = 311$ K, $R_i = 40$ mm, $R_o = 80$ mm, gap, $\delta = 0.8$ mm, disk thickness, $\beta = 0.8$ mm, and the turbine density, $\rho_t = 2500$ kg/m$^3$).

Figure 4 Angular velocity and the relative velocity as a function of time: (a) Effect of the outlet pressure, (b) effect of inlet pressure; (typical conditions: $T_0 = 311$ K, $\tau_{load} = 1.5$ N-m, $R_i = 40$ mm, $R_o = 80$ mm, gap, $\delta = 0.8$ mm, disk thickness, $\beta = 0.8$ mm, and the turbine density, $\rho_t = 2500$ kg/m$^3$).
Figure 5 Torque as a function of time, (a) the effect of the inlet pressure and (b) the effect of the outlet pressure (Load = 1.5 N-m, $T_0 = 311$ K, $R_i = 40$ mm, $R_o = 80$ mm, gap, $\delta = 0.8$ mm, disk thickness, $\beta = 0.8$ mm, and the turbine density, $\rho_t = 2500$ kg/m$^3$).

For a fixed external load, the angular velocity increases with the inlet pressure but decreases as the outlet pressure increases as shown in Figure 4 where results on the angular velocity and the relative velocity as a function of time under different operating conditions when the external load is kept constant at 1.5 N-m are presented. For the case with the inlet pressure of 25 MPa, the angular velocity levels off to 1715 rad/s after 2.36 s when the outlet pressure is 8 MPa and it decreases to 437 rad/s after 2.09 s when the outlet pressure increases to 12 MPa. Figure 4(b) shows the results when the outlet pressure is kept at 8 MPa and the inlet pressures are 15, 20, and 25 MPa. The turbine reaches a constant angular velocity of 427 rad/s in 2.42 s and to 1715 rad/s in 2.36 s as the inlet pressure increases from 15 MPa to 25 MPa. The effects of the inlet pressures and the outlet pressures on the relative velocity $U$ as a function of time are shown in Figure 4(c) and Figure 4(d). The results indicate that, for a given external load, the relative velocity is independent of the outlet pressure when the inlet pressure is kept constant, but it decreases as the inlet pressure increases if the outlet pressure is kept unchanged. The decrease in the relative velocity at higher inlet pressures is due to the fact that the momentum transfer between the working fluid and the rotating disks depends on both the relative velocity and the fluid density and viscosity. Since both the fluid density and its viscosity are higher at higher pressures, the relative velocity must be lower for the torque to be balanced by the same external load.

The effects of the inlet pressures and the outlet pressures on the torque due to the shear stress as a function of time are shown in Figure 5. The results indicate that as the steady state condition is reached, all the torques level off at the external load, independent of the operating conditions in terms of the inlet and the outlet pressures. The operating conditions, however, determine the initial value of the torque and hence they determine the maximum external load that the turbine is operational. Figure 6 shows the effects of the operating condition in terms of the inlet and the outlet pressures on the steady-state torque as a function of the eternal loads. Using supercritical CO$_2$ as the working fluid, the range of the external loads that a turbine can be operated is seen to increase with higher inlet pressures and lower outlet pressures. For example, for the outlet pressure of 8 MPa, the turbine can operate with an external load of 1.7 N-m at the inlet pressure of 15 MPa and with an external load up to 3.2 N-m when the inlet pressure is up to 25 MPa. For a constant inlet pressure at 20 MPa, the turbine with the outlet pressure of about 8 MPa can operate with an
external load of 2.5 N-m while with an outlet pressure of 12 MPa the external load is up to 1.3 N-m. The increase of the torque with the external load, shown in Figure 6, can be explained in terms of the turbine angular velocity. This is shown in Figure 7 where the angular and the relative velocities as a function of the external load are presented. As the load increases, the angular velocity decreases, and the relative velocity increases. Since the working fluid transfers more momentum to the disks at higher relative velocity as shown by Eqn. (1), a higher torque is developed.

**Figure 6** Torque as a function of load, (a) the effect of the outlet pressure and (b) the effect of the inlet pressure ($T_0 = 311$ K, $R_i = 40$ mm, $R_o = 80$ mm, gap, $\delta = 0.8$ mm, disk thickness, $\beta = 0.8$ mm, and the turbine density, $\rho_t = 2500$ kg/m$^3$).

**Figure 7** Angular velocity and the relative velocity as a function of load, Figures a and c: the effect of the outlet pressure; Figures b and d: the effect of the inlet pressure; ($T_0 = 311$ K, $R_i = 40$ mm, $R_o = 80$ mm, gap, $\delta = 0.8$ mm, disk thickness, $\beta = 0.8$ mm, and the turbine density, $\rho_t = 2500$ kg/m$^3$).
Figure 8 shows the effects of the inlet and the outlet pressures on the outlet power as a function of the external loads. The operational range of the external load increases as either the inlet pressure increases, or as the outlet pressure decreases. The power outlet depends on the inlet and the outlet enthalpies and the kinetic energies; it can be calculated using Eq. 4, \( P_w = \tau \omega \), which describes the increase of the power outlet as the angular velocity increases. Increasing the angular velocity results in a decrease of the relative velocity reducing the momentum transfer from the fluid to the disks and hence, increasing the outlet velocity. Increasing the outlet velocity, however, has a negative effect on the power output of the turbine. Thus, since the angular velocity depends on the operational torque, increasing/decreasing the operational load has both positive and negative effects on the power output. At first, the turbine power increases with the increase in the external load until a maximum point and then the turbine power decreases as the load continues to increase. For a fixed inlet pressure, both the maximum point and the operational range of the external loads decrease as the outlet pressure increases. For a fixed outlet pressure, the maximum point and the operational range of the external loads increase as the inlet pressure increases. Operating with supercritical CO\(_2\) as the working fluid, when the inlet pressure is 20 MPa, the maximum power output of 1739 W and the angular velocity of about 1241 rad/s are obtained at the external load of 1.4 N-m for the outlet pressure of 8 MPa, and the inlet pressure of 20 MPa. The range of the operational external load is up to 2.5 N-m. For the outlet pressure of 8 MPa, the operational range of the external load is up to 3.1 N-m, the maximum power of 2646 W occurs at the external load of 1.8 N-m (1469 rad/s) for the inlet pressure of 25 MPa. This power is calculated for one channel. For a turbine having 100 channels, a power output of 0.2646 MW could be harvested instead of being wasted if conventional throttling expansion valves of any kinds are used. To roughly estimate the energy required to increase the temperature of CO\(_2\) transported in an 8 MPa pipeline, we use the following equation \( \dot{Q} = \dot{m}_{CO2} c_{p, CO2} \Delta T \). If this power is used to preheat the transported CO\(_2\) to increase its temperature by 10 °C, \( \Delta T = 10 \), before injection, it is sufficient to heat an amount 0.8 Mt of CO\(_2\) per year. Goodarzi et al. [7] estimated the cost of heating to avoid cooling the reservoir to be about $0.75 per cubic meter; thus, a heating cost of about a million dollars per year would be saved.

![Figure 8](image-url)

**Figure 8** Power outlet as a function of load; (a): the effect of the outlet pressure, (b): the effect of the inlet pressure; \( T_0 = 311 \) K, friction torque, \( R_i = 40 \) mm, \( R_o = 80 \) mm, gap, \( \delta = 0.8 \) mm, disk thickness, \( \beta = 0.8 \) mm, and the turbine density, \( \rho_t = 2500 \) kg/m\(^3\).
4. Conclusion

This study presents a simple analysis to look at the performance of a Tesla turbine, in terms of its angular velocity and power, while using supercritical CO$_2$ as the working fluid. The work is based on the simple analytical model developed by Tamir et al. [14]. Keeping the turbine geometric parameters unchanged, while the inlet temperature, the inlet pressures, and the outlet pressures are used as the operating conditions. The results show that using a Tesla turbine instead of a conventional expansion valve of any kinds, to expand and deliver supercritical CO$_2$ from a high-pressure container to a lower-pressure transport pipelines, throttling losses can be avoided and its potential to generate useful mechanical work can be harvested. In addition, due to the friction between the expanded CO$_2$ and the turbine disks, its temperature reduction is not as dramatic as is the case when an expansion valve is used. Thus, as far as CO$_2$ injection is concerned, the need for preheating can be minimized.

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Author Contributions

Phuoc X. Tran thought of this problem and performed most of the derivations and all of the calculations. Mehrdad Massoudi helped in the derivation and the formulation of the problem. Both authors contributed to the writing of the paper, and both authors have read and agreed to the published version of the manuscript.

Competing Interests

The authors have declared that no competing interests exist.

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