The Proper Motion of Sagittarius A*. III. The Case for a Supermassive Black Hole

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Abstract

We report measurements with the Very Long Baseline Array of the proper motion of Sgr A* relative to two extragalactic radio sources spanning 18 yr. The apparent motion of Sgr A* is \(-6.411 \pm 0.008\) mas yr\(^{-1}\) along the Galactic plane and \(-0.219 \pm 0.007\) mas yr\(^{-1}\) toward the North Galactic Pole. This apparent motion can almost entirely be attributed to the effects of the Sun’s orbit about the Galactic center. Removing these effects yields residuals of \(-0.58 \pm 2.23\) km s\(^{-1}\) in the direction of Galactic rotation and \(-0.85 \pm 0.75\) km s\(^{-1}\) toward the North Galactic Pole. A maximum-likelihood analysis of the motion, both in the Galactic plane and perpendicular to it, expected for a massive object within the Galactic center stellar cluster indicates that the radiative source, Sgr A*, contains more than about 25\% of the gravitational mass of \(4 \times 10^6 M_\odot\) deduced from stellar orbits. The intrinsic size of Sgr A* is comparable to its Schwarzschild radius, and the implied mass density of \(\geq 4 \times 10^3 M_\odot\) pc\(^{-3}\) is very close to that expected for a black hole, providing overwhelming evidence that it is indeed a supermassive black hole. Finally, “intermediate mass” black holes more massive than \(\approx 3 \times 10^6 M_\odot\) between approximately 0.003 and 0.1 pc from Sgr A* are excluded.

Unified Astronomy Thesaurus concepts: Astrometry (80); Galactic center (565); Milky Way Galaxy physics (1056); Milky Way dynamics (1051); Supermassive black holes (1663)

1. Introduction

At the Galactic center, stars orbit an unseen mass of \(4 \times 10^6 M_\odot\) (e.g., Bohlehe et al. 2016; Gillessen et al. 2017), and the compact radio source Sgr A* projects to within \(\approx 1\) mas (\(\approx 8\) au) of the gravitational focal position (Menten et al. 1997; Reid et al. 2007) of these stars. If we are to conclude that the Galactic center harbors a supermassive black hole (SMBH), a critical question is how much of the unseen mass can be directly tied to Sgr A*. Since the luminosity of Sgr A* is only comparable to a stellar source, other information is needed to establish if it is an SMBH. To that end, we have been measuring the position of Sgr A* with the National Radio Astronomy Observatory’s\(^3\) Very Long Baseline Array (VLBA) since 1995, as a very massive object at the dynamical center of the Galaxy should be nearly motionless.

The apparent motion of Sgr A*, relative to extragalactic radio sources, contains the reflex of the Sun’s velocity in its orbit about the Galactic center, plus any intrinsic motion of Sgr A* itself. In Reid et al. (1999) and Reid & Brunthaler (2004), hereafter Papers I and II, we published results from the first 8 yr of observation. We showed that the component of the apparent motion of Sgr A* perpendicular to the Galactic plane could be explained by the motion of the Sun toward the North Galactic Pole, limiting the intrinsic motion of Sgr A* to \(\lesssim 1\) km s\(^{-1}\) in one dimension. Since a massive object embedded in a dense stellar cluster suffers gravitational Brownian motion and reaches thermal equilibrium with the perturbing stars (Chatterjee et al. 2002), the observed lack of motion for Sgr A* provided a lower limit of \(\sim 0.4 \times 10^6 M_\odot\) for Sgr A* (Reid & Brunthaler 2004). This clearly associated a very large mass with the radiative source Sgr A*, and greatly strengthened the already strong case for Sgr A* being an SMBH.

In this paper, we report new observations that now span 18 yr, reducing proper motion uncertainties by a factor of three to less than \(\pm 10\) mas yr\(^{-1}\), both in and out of the Galactic plane. Coupling these results with independent measurements of the angular motion of the Sun in its orbit about the Galactic center, we are now able to use two dimensions of velocity information to provide a stronger and more robust lower limit for the mass of Sgr A*, significantly increasing confidence that it is indeed a black hole.

2. Observations and Results

Our observations using the National Radio Astronomy Observatory’s VLBA started in 1995 and have now continued to 2013. Paper I reported early results for observations from 1995 through 1997, and observations through 2003 were reported in Paper II. Here we present new observations conducted in 2007 and 2013 under VLBA programs BR124 and BR173. As very long baseline interferometric (VLBI) technology progressed we increased the recorded data rates. For BR124 we observed with eight 8 MHz bands with Nyquist sampling and 2 bits per sample for a total sampling rate of 256 Mb s\(^{-1}\). The observations spanned 8 hr and we placed three geodetic-like blocks at the beginning, middle, and end of the tracks in order to measure and remove tropospheric and clock delays. We switched between sources every 15 s, using Sgr A* as the phase-reference for the background sources. For BR173 we observed with 16 32 MHz bands with Nyquist sampling and 2 bits per sample for a total sampling rate of 2 Gb s\(^{-1}\). These observations spanned 6 hr and we placed four geodetic-like blocks evenly spaced throughout the observations, and we switched between sources every 17 s. Details of the calibration procedures can be found in Papers I and II.

After calibration, we imaged all sources and measured their positions by fitting elliptical Gaussian brightness distributions. Table 1 lists all of our position measurements.

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of Sgr A* relative to two compact extragalactic radio sources, J1745–2820 and J1748–2907, in J2000 equatorial and also Galactic coordinates. The measurements were made at the highest astrometrically useful frequency of the VLBA of 43 GHz in order to minimize the effects of strong interstellar scattering toward the Galactic center. Position uncertainties include estimates of systematic effects, dominated by small residual errors in modeling atmospheric delays.  

2.1. Proper Motion of Sgr A*  

The positions on the sky of Sgr A*, relative to the two background sources, are plotted in Figure 1. The observations now span 18 yr and the linear trends reported in Papers I and II continue. Variance-weighted least-squares fits to the position versus time of Sgr A* relative to J1745–2820 and J1748–2907 are given in Table 2 and plotted with dashed lines in Figure 1. The results for the two background sources are consistent and differing the motions with respect to the background
Motions values are from weighted least-squares fits to the data in Table 1, with uncertainties scaled to give a reduced chi-squared of unity. Equatorial motions in the J2000 system and Galactic motions are based on Galactic coordinates transformed to J2000 as described in the Appendix of Reid & Brunthaler (2004), “Combined” motions are variance weighted averages of the individual results.

The background sources are sufficiently distant that they have negligible intrinsic angular motion, we average the two results and estimate Sgr A*’s apparent motion to be $-3.156 \pm 0.006$ and $-5.585 \pm 0.010$ mas yr$^{-1}$ in the easterly and northerly directions, respectively.

We refitted for motions in Galactic coordinates (see Table 2), yielding apparent motion components for Sgr A* in Galactic longitude of $-6.411 \pm 0.008$ mas yr$^{-1}$ and in latitude of $-0.219 \pm 0.007$ mas yr$^{-1}$. The data and fits are displayed in Figure 2. Adopting a distance to the Galactic center of $R_0 = 8.15$ kpc (Do et al. 2019;Gravity Collaboration et al. 2019; Reid et al. 2019), Sgr A* appears to be moving predominantly along the Galactic plane with a tangential (toward increasing longitude) speed of $-247.69 \pm 0.33$ km s$^{-1}$ and toward the North Galactic Pole with a speed of $-8.45 \pm 0.26$ km s$^{-1}$.

2.2. Acceleration of Sgr A*

We also investigated the possibility that Sgr A* is being accelerated by, for example, an intermediate mass black hole (IMBH). When we added an acceleration parameter in the motion fits, we obtained easterly and northerly accelerations of $-0.0026 \pm 0.0030$ mas yr$^{-2}$ and $-0.0050 \pm 0.0038$ mas yr$^{-2}$ relative to J1745–2820 and $0.0058 \pm 0.0029$ mas yr$^{-2}$ and $0.0129 \pm 0.0074$ mas yr$^{-2}$ relative to J1748–2907. A variance-weighted average of the two acceleration results gives easterly and northerly motions of $0.0017 \pm 0.0021$ mas yr$^{-2}$ and $-0.0013 \pm 0.0034$ mas yr$^{-2}$. These acceleration estimates are an order of magnitude improvement over our results in Paper II. They are consistent with no measurable acceleration, with a $2\sigma$ upper limit of $0.0080$ mas yr$^{-2}$ (0.31 km s$^{-1}$ yr$^{-1}$) for the magnitude of the two-dimensional acceleration vector. Acceleration limits are potentially interesting as they require no correction for solar
orbital acceleration, which is $\sim 10^{-7} \text{ mas yr}^{-2}$ (Gould & Ramirez 1998).

Interestingly, the stellar cluster IRS 13E has marginal evidence for an IMBH of $3 \times 10^4 \, M_\odot$ (e.g., Genzel et al. 2010). The cluster projects within $\approx 3''$ of Sgr A*, corresponding to a linear offset of $\approx 0.1$ pc. Assuming its three-dimensional distance from Sgr A* is comparable to this offset, such an IMBH would likely induce an acceleration of $-0.4 \text{ km s}^{-1}\text{yr}^{-1}$ and a linear motion of about $3 \text{ km s}^{-1}$ for Sgr A*. Figure 3 presents the regions of IMBH mass and radius from Sgr A* that are allowed for and excluded by the current observations. Our limits make an IMBH of $\approx 3 \times 10^4 \, M_\odot$ between 0.003 and 0.1 pc from Sgr A* unlikely and strongly exclude a more massive object of $\gtrsim 10^5 \, M_\odot$, as does dynamical modeling of the orbit of star S02 (S2) by Naoz et al. (2019). Note that a modest increase in the time span of our astrometric observations could better test the IMBH’s existence, since for uniform sampling acceleration accuracy improves as the 5/2 power and motion accuracy improves as the 3/2 power of time spanned.

3. Limits on the Mass of Sgr A*

Some of the so-called “S” stars have been seen projected within $\sim 0.001$ pc of Sgr A* and move at thousands of km s$^{-1}$ (Schödel et al. 2002; Ghez et al. 2005) as they orbit a dark mass concentration. In contrast, Sgr A*, which is located within 0.00004 pc of the gravitation focus of the orbiting stars (Menten et al. 1997; Reid et al. 2003, 2007), has an intrinsic motion (relative to distant quasars) of less than a few km s$^{-1}$, strongly suggesting that it is very massive. For example, Sgr A* only a $10 \, M_\odot$ black hole in an X-ray binary, which would be consistent with its meager luminosity, it too should be moving at a great speed. However, a massive object in the presence of large numbers of stars experiences gravitational Brownian motion, which is expected to result in equipartition of kinetic energy between the massive object and individual stars (Chatterjee et al. 2002; Dorband et al. 2003; Merritt et al. 2007). In Paper II, we performed detailed simulations of the motion of a massive object orbited by $\sim 10^5$–$10^7$ stars within its sphere of influence. These simulations confirmed that equipartition of kinetic energy is indeed achieved, and that a $4 \times 10^5 \, M_\odot$ object would be expected to have a (one-dimensional) motion of between 0.18 and 0.30 km s$^{-1}$, depending on the nature of the stellar-mass function. In addition, a cluster of dark stellar remnants summing to $0.4 \times 10^6 \, M_\odot$ could contribute an additional 0.2 km s$^{-1}$ to the motion of the massive object. In this context, an upper limit to Sgr A*’s intrinsic motion can provide a lower limit to its mass.

Compared to Paper II, our latest results for the apparent motion of Sgr A* have decreased the motion uncertainties by a factor of three. Also, in Paper II we used only the component of

![Figure 2. Galactic longitude and latitude vs. time for Sgr A* relative to J1745–2820 (left panels) and J1748–2907 (right panels). Dashed lines are variance-weighted least-squares fits to the data, and the residuals to those fits are shown below each plot.](image)
motion of Sgr A* perpendicular to the Galactic plane, corrected for the Sun’s motion, to provide a lower limit for the mass of Sgr A*. The motion of Sgr A* in the Galactic plane was not used since, at the time, the correction for the orbital motion of the Sun was quite uncertain (±20 km s⁻¹). The Sun’s motion in its Galactic orbit is now known to much higher accuracy, and we can now use the Galactic longitude motion to complement the latitude motion in order to more tightly and robustly constrain the mass of Sgr A*.

By modeling parallaxes and proper motions of about 150 massive young stars with maser emission, Reid et al. (2019) estimate the angular speed of the Sun in its Galactic orbit with sub-percent accuracy: \((\Theta_0 + V_\odot)/R_0 = 30.32 \pm 0.27\) km s⁻¹ kpc⁻¹, where \(\Theta_0\) is the circular orbital speed in the Galaxy at the Sun and \(V_\odot\) accounts for the Sun’s deviation from a perfect circular orbit. In Table 3, we detail the values used to remove the effects of the Sun’s motion, in order to estimate the intrinsic motion of Sgr A*, both in and out of the Galactic plane. We find that Sgr A* is nearly motionless with longitude and latitude speeds of \(-0.58 \pm 2.23\) and \(-0.85 \pm 0.75\) km s⁻¹, respectively. Since these speeds came from differing independently determined angular motions, the adopted value of \(R_0\) of 8.15 kpc used to convert the differences to linear motions appears only as a final scale factor, and since \(R_0\) is now known to better than 2% accuracy (Do et al. 2019; Gravity Collaboration et al. 2019; Reid et al. 2019), its uncertainty is not important for our application.

Table 3: Estimating Sgr A*’s Intrinsic Motion

| Description                        | \(\mu_\ell\) (mas yr⁻¹) | \(\mu_\phi\) (mas yr⁻¹) |
|------------------------------------|--------------------------|--------------------------|
| Sgr A*’s apparent motion           | –6.411 ± 0.008           | –0.219 ± 0.007           |
| Reflex of Sun’s Galactic orbit     | –6.396 ± 0.057           | –0.197 ± 0.018           |
| Difference: Sgr A*’s intrinsic motion | –0.015 ± 0.058          | –0.022 ± 0.019           |
| Difference: assuming \(R_0 = 8.15\) kpc | –0.58 ± 2.23            | –0.85 ± 0.75             |

Notes.
\(\ell\) Proper motion Galactic longitude (\(\mu_\ell\)) and latitude (\(\mu_\phi\)) from Table 2.
\(\phi\) Adopting the Galactic orbital values of the Sun from parallaxes and proper motions of masers associated with massive young stars by Reid et al. (2019). Longitudinal motion: \((\Theta_0 + V_\odot)/R_0 = 30.32 \pm 0.27\) km s⁻¹ kpc⁻¹. Latitudinal motion: \(W_\odot = 7.6 \pm 0.7\) km s⁻¹.

In order to estimate how massive Sgr A* is, we simulate the effects of the central star cluster on a massive central object. Using the same approach as in Paper II, we generate 10⁵ random configurations of stars orbiting an object with a given trial mass, follow the system for the time spanned by our observations (now 18 yr), and infer the motion of the trial object from the change in the center of mass of the orbiting stars. We compare the simulated components of motion in each of the two dimensions with trials drawn from Gaussian distributions, which are consistent with our observed intrinsic motion of Sgr A* in Galactic longitude and latitude. We keep track of the fraction of trials that give at least one component of the massive object’s velocity, which is inconsistent with our observed limits. We then repeat the simulation with different trial masses in order to trace the distribution as a function of mass. In contrast to Paper II, which only used the latitude motion of Sgr A* to compare to the simulations, we now use two components (latitude and longitude) to better constrain Sgr A*’s mass. This significantly improves both the lower limit on the mass of Sgr A* and the robustness of the mass estimate.

In Paper II we evaluated three stellar initial mass functions (IMFs): a standard IMF, a top-heavy IMF with a high-mass index flatter by 0.5, and one flatter by 1.0. Given strong evidence for a top-heavy IMF in the Galactic center region, but an uncertain flattening at high masses (e.g., Figer et al. 1999; Stolte et al. 2002; Genzel et al. 2010), we conservatively adopt the moderately flattened IMFs considered in Paper II (with an index flatter by 0.5). We assume the broken power-law radial distribution of stars given by Equation (4) of Genzel et al. (2010). Specifically, our fiducial model has a volume density of stars given by \(n_\phi(R) = 1.35 \times 10^6 (R/0.25\) pc⁻³, with \(\gamma = 1.3\) and 1.8 inside and outside of \(R = 0.25\) pc, respectively. We then generate random orbital parameters with semimajor axes between \(R = 100\) au (approximately the smallest radius observed for stars) and 2.9 pc (corresponding to the radius of the sphere of influence of a \(4 \times 10^6 M_\odot\) central mass in the Galactic center).

In Figure 4 we plot the results of these simulations with a solid blue line. We find half of the trials would be detected, were Sgr A* less massive than \(0.8 \times 10^6 M_\odot\). This provides a factor of two stronger limit than in Paper II. Importantly, our result for 95% confidence (i.e., 5% undetected) is now \(0.2 \times 10^6 M_\odot\), a factor of 200 improvement over the result in Paper II. This improvement comes mostly from the use of two dimensions of motion, compared to the one dimension...
Figure 4. Results of simulations of the motion of Sgr A*, owing to random perturbations from the central stellar cluster, compared to observed limits. Plotted are the percentages of simulations that fall below the observed limits as a function of the assumed mass of Sgr A*. All simulations assume a stellar-mass function index flatter by 0.5 compared to a standard Salpeter IMF. The blue solid line is our fiducial result, which uses the updated stellar distributions from Genzel et al. (2010) with stellar density ρ_s(R) = 1.35 × 10^6 (R/R_0)^{-3}, where R_0 = 0.25 pc is a break radius and γ is 1.3 for R < R_0 and 1.8 for larger radii. The black dashed line adds ~4000 stellar-mass black holes with a Bahcall–Wolff cusp-like radial distribution with index −7/4 in the inner 0.2 pc. For comparison, the red dotted–dashed line uses the stellar distribution from Paper II. Dotted and dashed lines indicate 5% and 50% of simulations that would not have been detected, corresponding to Sgr A* masses of about 0.2 and 1.0 × 10^6 M_⊙, respectively.

available in Paper II. For comparison, we repeated the simulations using the stellar cluster model employed in Paper II and plot the results with a red dashed–dotted line in Figure 4. The differences between the stellar cluster models results only in small differences in the final results.

Since one expects a significant population of stellar remnants to accumulate in the Galactic center, we added a population of stellar-mass black holes to the fiducial model of the central cluster and re-ran the simulations. Following the models of Freitag et al. (2006), we added a total mass of 7 × 10^4 M_⊙ in black holes between radii of 100 au and 0.2 pc. This corresponds to less than 2% of the mass within 0.2 pc of the center. We assumed a flat distribution in mass between 6 and 30 M_⊙, which results in about 4000 black holes, and a cusp-like radial distribution with a Bahcall–Wolff power-law index of −7/4. The results of these simulations are shown with the black dashed line in Figure 4. As expected, the motions of Sgr A* increase, but only modestly, and 50% of the trials would result in detections were Sgr A* to hold 1.0 × 10^6 M_⊙.

Note that all of our simulations use smooth distributions of stars, without any clumping. Since clumping would increase the simulated motion of Sgr A*, our mass limits are very conservative. Thus, we adopt a round-number mass of 1.0 × 10^6 M_⊙ as a maximum-likelihood lower limit for the mass of the radiative source, Sgr A*, when we explore its significance in the next section.

4. Is Sgr A* an SMBH?

Given that the radiative source Sgr A* likely has a mass greater than 10^6 M_⊙, how does this help answer the question “is it a black hole”? If one can show that sufficient mass is contained within a small enough volume, Einstein’s theory of general relativity requires a black hole. This leads to a maximum mass density that matter can achieve before a black hole forms. Thus, the case for the existence of SMBHs centers on observations of objects that approach a critical mass density. The size of a black hole of a given mass can be defined by its Schwarzschild radius, R_{Sch} = 2GM/c^2, where G is the gravitational constant, M is the mass of the black hole, and c is the speed of light. However, any matter that comes within 3R_{Sch} of a (nonrotating) hole cannot achieve a stable orbit and falls directly into the black hole. Thus, a critical mass density to require a black hole, ρ_{crit} would be the mass divided by the volume enclosed by 3R_{Sch}:

ρ_{crit} = \frac{M}{(4\pi/3)(3R_{Sch})^3}.

Substituting the relation for R_{Sch}, we find

ρ_{crit} = \frac{c^6}{288\pi G^3 M^2}.

Note that this density depends inversely as the square of the mass. An alternative “linear” density, ϕ_{crit} defined as M/3R_{Sch} provides a simple mass-independent parameter that can be used to establish a black hole:

ϕ_{crit} = \frac{2G}{3c^2}.

Table 4 lists critical linear and volume density limits as established from various observations and updated from Reid (2009). The first table entry is for globular clusters, which can have upwards of ~10^6 stars within a radius of ~1 pc. This provides a reference point for relatively high stellar densities that are commonly achieved in galaxies. The last table entry gives the critical linear and volume densities for a theoretical SMBH of 4 × 10^6 M_⊙ assuming a radius of 3R_{Sch}. If one can show that these critical densities are achieved, the case for an SMBH is established with near certainty.

Now we consider systems only with enclosed mass estimates from well-defined Keplerian orbits. The second entry in Table 4 is based on observations of water masers in the center of the galaxy NGC 4258. VLBI observations with angular resolution of 0.4 mas show that these masers originate from a slightly warped, thin disk of gas within an angular radius of about 3 mas (2 × 10^4 au at the distance of the galaxy). The observed rotational speeds of 900 km s⁻¹ are consistent with Keplerian orbits about a central mass of 4 × 10^4 M_⊙. The
implied volume density is nearly five orders of magnitude above stellar densities in globular clusters, effectively ruling out a cluster of normal stars. However, it is not sufficient to rule out clusters of compact stellar remnants (e.g., white dwarfs, neutron stars, or stellar black holes).

The third entry in Table 4 is based on infrared observations of stars that orbit an unseen mass in the center of the Milky Way. These observations by groups at the Max Planck Institute for Extraterrestrial Physics (e.g., Gillessen et al. 2017) and UCLA (e.g., Boehle et al. 2016) require a central mass of \(4 \times 10^6 M_\odot\) within a radius of 100 au. One star (S2; S02) has been seen to complete nearly two elliptical orbits and multiple stars have traced partial orbits. All stars show a common gravitational focal position, which coincides with the radio source Sgr A* to within \(\approx 0.001\) (Menten et al. 1997; Reid et al. 2007), and require the same central mass. The inferred mass density of \(8 \times 10^{15} M_\odot\) pc\(^{-3}\) is high enough to rule out very long-lived clusters of stars, as well as a speculative proposal of a central “ball” of heavy fermions (Munyanzeza & Viollier 2002).

The fourth entry in Table 4 refers to the VLBI observations of the proper motion of Sgr A* reported in this paper. As shown in Section 3, Sgr A* appears to move along the plane of the Milky Way in a manner that can be completely accounted for by our orbit about the center of the Milky Way. This provides an upper limit of \(\sim 1\) km s\(^{-1}\) for the intrinsic motion of Sgr A* itself. Stars near Sgr A* have been observed to move at thousands of km s\(^{-1}\), and the only way that Sgr A* can be motionless is for it to be extremely massive. Both theory and direct simulations of the gravitational “Brownian” motion of a supermassive object at the center of the observed stellar cluster require Sgr A* to be in near thermal equilibrium with the stars within its sphere of influence. Our detailed simulations of the effects of the central stellar cluster on the expected motion of Sgr A*, described in Section 3, constrain its mass to likely exceed \(1 \times 10^6 M_\odot\). A long history of VLBI observations have gradually improved measurements of the intrinsic size of Sgr A*; the most recent show Sgr A*’s emission has a radial extent of \(\sim 0.18\) au (Doeleman et al. 2008), which is comparable to the Schwarzschild radius for a \(4 \times 10^6 M_\odot\) black hole.

Combining the lower limit for Sgr A*’s mass (from its lack of motion) with the size of the source yields both linear and volume mass densities that are within a factor of about three of the general relativity limit for a black hole. This provides overwhelming evidence for an SMBH at the center of the Milky Way.

5 These observations, and those for dozens of other galaxies, certainly provide strong evidence that SMBHs are found at the centers of active galaxies. Were one to place \(10^7\) stars inside a radius of \(0.1\) pc, the system would be dynamically unstable. Less massive stars would be expelled while dynamical friction would cause massive stars to sink to the center where they could possibly form a black hole. These observations rule out long-lived clusters of normal stars as providing the central gravitational mass (Maoz 1998). However, this conclusion is based on the assumption of an isolated stellar cluster. The possibility of a quasi-steady-state condition, wherein stars beyond the 0.1 pc radius are gravitationally perturbed and enter the central region, replenishing those expelled, has yet to be considered in detail.

6 The measured apparent size of Sgr A* is slightly smaller than that given by \(3R_\text{SMBH}\). This is as expected for the radiation from material in a disk orbiting the black hole at \(3R_\text{SMBH}\). Since the approaching material on one side is moving toward us at nearly the speed of light, this emission is boosted by relativistic aberration and Doppler shifts, causing this side to dominate the emissions.

5. Conclusions

In summary, infrared observations of stars orbiting an unseen mass concentration provide extremely strong evidence for an SMBH at the center of the Milky Way. Radio observations associate that unseen mass with the radiative source Sgr A*, and its lack of motion requires a huge mass to reside within a region of a few Schwarzschild radii. If, following the infrared observations, there was any doubt that Sgr A* is an SMBH, the radio observations should remove that doubt.

Facility: VLBA.

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References
Boehle, A., Ghez, A. M., Schödel, R., et al. 2016, ApJ, 830, 17
Chatterjee, P., Hernquist, L., & Loeb, A. 2002, ApJ, 572, 371
Do, T., Hees, A., Ghez, A., et al. 2019, Sci, 365, 664
Doeleman, S. S., Weinstein, J., Rogers, A. E. c., et al. 2008, Natur, 455, 78
Dorband, E. N., Hensendorf, M., & Merritt, D. 2003, JCoPh, 185, 484
Figer, D. F., Kim, S. S., Morris, M., et al. 1999, ApJ, 525, 750
Freitag, M., Amaro-Seoane, P., & Kalogera, V. 2006, ApJ, 649, 91
Genzel, R., Eisenhauer, F., & Gillessen, S. 2010, RVMP, 82, 3121
Ghez, A. M., Salim, S., Hornestein, S. D., et al. 2005, ApJ, 620, 744
Gillessen, S., Plewa, P. M., Eisenhauer, F., Sari, R., et al. 2017, ApJ, 837, 10
Gould, A., & Ramírez, S. V. 1998, ApJ, 497, 713
Maoz, E. 1998, ApJL, 494, L181
Menten, K. M., Reid, M. J., Eckart, A., & Genzel, R. 1997, ApJL, 475, L111
Merritt, D., Berczik, P., & Laun, F. 2007, AJ, 133, 533
Munyanzeza, F., & Viollier, R. D. 2002, ApJ, 564, 274
Naoz, S., Will, C. M., Ramirez-Ruiz, E., et al. 2019, arXiv:1912:04910v1
Reid, M. J. 2009, IMPV, 18, 889
Reid, M. J., & Brunthaler, A. 2004, ApJ, 616, 872
Reid, M. J., Menten, K. M., Brunthaler, A., et al. 2019, ApJ, 885, 131
Reid, M. J., Menten, K. M., Genzel, R., et al. 2003, ApJ, 587, 208
Reid, M. J., Menten, K. M., Trippe, S., Ott, T., & Genzel, R. 2007, ApJ, 659, 378
Reid, M. J., Readhead, A. C. S., Vermeulen, R. C., & Treuhaft, R. N. 1999, ApJ, 524, 816
Schödel, R., Ott, T., Genzel, R., et al. 2002, Natur, 419, 694
Stolte, A., Grebel, E. K., Brandner, W., & Figer, D. F. 2002, A&A, 394, 459