A Physically Based Multisensor Quantitative Precipitation Estimation Approach for Gap-Filling Radar Coverage

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ABSTRACT

Weather radars and gauge observations are the primary observations to determine the coverage and magnitude of precipitation; however, radar and gauge networks have significant coverage gaps, which can underrepresent or even miss the occurrence of precipitation. This is especially noticeable in mountainous regions and in shallow precipitation regimes. The following study presents a methodology to improve spatial representations of precipitation by seamlessly blending multiple precipitation sources within the Multi-Radar Multi-Sensor (MRMS) system. A high spatiotemporal resolution multisensor merged quantitative precipitation estimation (QPE) product (MSQPE) is generated by using gauge-corrected radar QPE as a primary precipitation source with a combination of hourly gauge observations, monthly precipitation climatologies, numerical weather prediction short-term precipitation forecasts, and satellite observations to use in areas of insufficient radar coverage. The merging of the precipitation sources is dependent upon radar coverage based on an updated MRMS radar quality index, surface and atmospheric conditions, topography, gauge locations, and precipitation values. Evaluations of the MSQPE product over the western United States resulted in improved statistical measures over its individual input precipitation sources, particularly the locally gauge-corrected radar QPE. The MSQPE scheme demonstrated its ability to sufficiently fill in areas where radar alone failed to detect precipitation due to significant beam blockage or poor coverage while minimizing the generation of false precipitation and underestimation biases that resulted from radar overshooting precipitation.

1. Introduction

Accurate, high spatiotemporal resolution quantitative precipitation estimates (QPEs) are crucial for flood and flash flood operations, hydrologic forecasting, long-term climatological evaluations, and water resource management. One common source of measuring precipitation are rain gauges, which provide direct surface measurements; however, a single gauge observation based on an orifice of 80–325 cm² typically covers a region spanning many square kilometers. Large distances between gauge sites can provide an insufficient representation of precipitation. Quina (2003) showed in Florida that the correlation of gauge observations decreased significantly when the distance of nearest neighbor comparisons increased to 20 km with continued correlated degradation up to a range of 100 km. Comparisons between gauge observations at a distance of 20 km yielded a correlation of approximately 0.30 for hourly accumulations and 0.55 for daily accumulations. Young et al. (2000) found a similar decrease in correlation between nearest neighbor gauge observations with increasing distance utilizing gauge networks in Oklahoma.

Weather radars provide the spatial resolution and distribution of precipitation that gauge-based point
observations cannot, yet the estimated precipitation has greater uncertainty due to it being remotely sensed at varying elevations above the surface. Radar sampling is impacted by large spatial distances between radar sites along with range degradation and blockages in complex terrain, resulting in undersampled precipitation (e.g., Kitchen et al. 1994; Smith et al. 1996; Steiner et al. 1999; Germann and Joss 2002; Zhang et al. 2012a). Maddox et al. (2002) provides a detailed description of the restricted coverage of the Weather Surveillance Radar-1988 Doppler (WSR-88D) network at various height levels. Coverage gaps within gauge and radar networks exist in varying degrees across the contiguous United States (CONUS) and are more prominent in the western CONUS (Fig. 1).

Gauge observations and radar-derived QPEs have been combined in various methodologies to improve precipitation estimations, especially in the context of advancing radar-derived QPE accuracy (e.g., Seo and Breidenbach 2002; Smith and Krajewski 1991); however, bias adjustments of radar-derived precipitation estimates using gauge observations are only applicable where radar coverage is available. Zhang et al. (2014) defined a conceptual methodology of supplementing radar-derived QPE with a Mountain Mapper QPE product (Schaake et al. 2004) generated from hourly gauge observations interpolated onto Parameter-Elevation Regressions on Independent Slopes Model (PRISM; Daly et al. 2008, 1994) monthly precipitation climatologies. The scheme did not fully compensate for radar coverage gaps but utilized a linear longitudinal blend that used radar-based QPE only east of 100°W longitude and Mountain Mapper QPE only west of 118°W longitude. This consequently limited or removed any radar data within the intermountain western CONUS and along the Pacific coast, including regions with unobstructed radar coverage.

Other precipitation sources can also be utilized to compensate for gaps in radar and gauge observational coverage. The quality of numerical weather prediction (NWP) quantitative precipitation forecasts (QPFs), notably those generated by short-range convective allowing models (CAMs), has substantially improved skill (e.g., Clark et al. 2009; Sun et al. 2014; Yussouf et al. 2016). An assessment of two versions of the High Resolution Rapid Refresh (HRRR; Benjamin et al. 2016) modeling system along with the prototype National Severe Storms Laboratory (NSSL) Warn-on-Forecast (WoF) system by Lawson et al. (2018) demonstrated the significant progress made with 0–3-h QPFs via advanced data assimilation methods; moreover, Lundquist et al. (2019) describes how high-resolution NWP models can better represent total annual precipitation than the current collection of gauge observations in mountainous terrain. Numerous studies assessed the quality of polar-orbiting and geostationary satellite-derived QPEs and discussed the potential for satellite-derived fields to mitigate radar coverage limitations (e.g., Kuligowski 2010; Scofield and Kuligowski 2003; Stenz et al. 2016).
The following study describes a physically based approach to improve the spatial representation of precipitation by seamlessly blending various precipitation sources with the current radar coverage over the CONUS. Each precipitation input is weighted based on their observational strengths and accuracy that vary based on atmospheric and terrain properties. The objective is to generate a high spatiotemporal resolution multisensor merged QPE product (hereinafter denoted as MSQPE) within the Multi-Radar Multi-Sensor (MRMS) real-time system (Zhang et al. 2016).

2. Gap-filling scheme inputs

a. Precipitation inputs and strengths

In situ and remotely sensed precipitation along with precipitation climatologies and NWP QPFs are utilized within the MSQPE scheme. Precipitation inputs from the MRMS system include the locally gauge-corrected (LGC) radar QPE and Mountain Mapper QPE. Both products are generated every hour on a 1-km Cartesian grid. Weather radar data for MRMS are gathered from NWS dual-polarization WSR-88D radar network in the CONUS and 30 C-band single-polarization weather radars across southern Canada operated by Environment Canada. Quality control of radar data is performed for each radar site to reduce the impacts of nonmeteorological echoes (Tang et al. 2014; Zhang et al. 2016). Other corrections are applied to improve data quality, including the mitigation of beam blockages, data corruption from nonmeteorological features (e.g., wind farms), and brightband contamination (Zhang and Qi 2010; Zhang et al. 2012b; Qi et al. 2013a,b; Zhang et al. 2016). Precipitation rates were generated using an experimental dual-polarization synthetic QPE scheme in the MRMS framework for radar sites utilizing dual-polarization technology (Zhang et al. 2020). Instantaneous rates were calculated from various dual-polarization variables, including specific attenuation, which has immunity to radar calibration errors and some partial beam blockage (Wang et al. 2019). Radars without dual-polarization capabilities utilized reflectivity values to derive precipitation rates (Zhang et al. 2016). Derived precipitation rates are then modified to account for the evaporation of hydrometeors between the lowest utilized radar beam height and the surface (Martinaitis et al. 2018).

MRMS LGC radar QPE and Mountain Mapper QPE rely upon automated hourly gauge observations that pass quality control measures. MRMS ingests approximately 20 000 gauge observations per hour across the MRMS CONUS domain from the Hydrometeorological Automated Data System (HADS; Kim et al. 2009) and the Meteorological Assimilation Data Ingest System (MADIS; Miller et al. 2007; Helms et al. 2009). These hourly gauge accumulations are quality controlled through a scheme described by Qi et al. (2016) with modifications outlined by Martinaitis et al. (2018). Approximately 85% of gauge observations per hour are deemed usable for MRMS QPE generation through this scheme.

Hourly radar-based accumulations are locally bias corrected using these quality controlled hourly gauge observations through an inverse distance weighting (IDW) scheme that varies the radius of the interpolation weight each hour through a cross validation methodology to minimize interpolation errors (Zhang et al. 2016). The correction of biases within the radar-based accumulations in MRMS using gauge observations improves precipitation accuracy across the CONUS in areas of radar coverage (Zhang et al. 2016). The Mountain Mapper QPE scheme in MRMS utilizes IDW with a fixed radius of 200 km (Zhang et al. 2016). These gauge observations are critical to the Mountain Mapper QPE generation, especially in areas of complex terrain that are not sampled well by radars. The interpolation of gauge observations with precipitation climatologies in mountainous areas have provided greater precipitation accuracy in complex terrain (Schaake et al. 2004; Zhang et al. 2014).

Hourly NWP QPFs are the only non-MRMS source utilized in the study. Integrated into the scheme are the 1-h forecasts from the operational HRRR version 2 (hereinafter denoted as HRRRv2) at a 3-km horizontal resolution. HRRRv2 model configurations can be found in Lawson et al. (2018). The HRRRv2 QPFs are mapped to the MRMS 1-km Cartesian grid for spatial continuity among precipitation inputs. Satellite-based QPE from the Self-Calibrating Multivariate Precipitation Retrieval (SCaMPR; Kuligowski 2002; Kuligowski et al. 2016) algorithm using the latest Geostationary Operational Environmental Satellite (GOES) information from GOES-16 was considered for this study due to its high spatiotemporal resolution and full coverage over the CONUS with little product latency; however, analysis of SCaMPR QPEs showed that the SCaMPR algorithm struggled with capturing the proper delineation of precipitation coverage and the magnitude of precipitation across various precipitation event types (e.g., Fig. 2). The study presented here does not include a satellite QPE component in the multisensor scheme.

b. Data limitations

Each precipitation input for MSQPE has its own inherent set of limitations. Observations recorded by gauges may not always be representative of reality. The gauge orifice can be subject to blockages that can underestimate or even prevent the measuring of precipitation
Instrumentation and siting issues can result in systematic biases and improper calibration (Groisman and Legates 1994; Steiner et al. 1999; Kondragunta and Shrestha 2006; Sieck et al. 2007). Strong surface winds can lead to precipitation undercatch, and the degree of wind undercatch varies based on precipitation type and gauge shielding characteristics (e.g., Larson and Peck 1974; Wilson and Brandes 1979; Yang et al. 1998). Rain gauges have also been shown to have challenges with accurate liquid-equivalent accumulations (Metcalfe and Goodison 1992; Groisman and Legates 1994; Goodison et al. 1998; Rasmussen et al. 2012) and commonly report zero precipitation or inaccurate nonzero observations from blockages of the gauge orifice during winter events (Martinaitis et al. 2015).

Radar-derived QPEs are subject to error through improper calibration or the utilization of unrepresentative reflectivity–rain rate ($Z-R$) and reflectivity–snow rate ($Z-S$) relationships (e.g., Joss and Waldvogel 1969; Wilson and Brandes 1979; Zawadzki 1984; Austin 1987; Smith et al. 1996; Young et al. 1999). Radar-derived

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**Fig. 2.** Comparison of MRMS (a),(c) LGC radar QPE to (b),(d) SCaMPR satellite QPE for the 24-h accumulation period ending (top) 1400 UTC 20 Oct 2017 and (bottom) 1500 UTC 2 Mar 2018. All accumulations shown are compared to CoCoRaHS gauge observations with coloring denoting the bias of the gridded QPE to the recorded gauge observation (bubble plots). Yellow boxes denote areas where the SCaMPR satellite QPE missed stratiform (solid line) and convective (dashed line) precipitation events. Orange boxes denote areas where there were significant biases in the SCaMPR satellite QPE value compared to the CoCoRaHS gauge observations.
QPEs based on dual-polarization variables are dependent upon the calibration of both the horizontal and vertical channels that influence some of the dual-polarization products. Other challenges include the appropriateness of the applied precipitation rate relationships and the limitations of dual-polarization variables for different precipitation types. Sampling through the melting layer can result in erroneously high precipitation values (Smith 1986). The lowest elevation scans can be contaminated by ground clutter and nonmeteorological echoes (e.g., Young et al. 1999; Harrison et al. 2000); furthermore, nonuniform beam filling and larger sample sizes with increasing range from radar can result in nonrepresentative reflectivity data or create improper biases in precipitation (Rogers 1971; Rosenfeld et al. 1992, 1993). The aforementioned limitations of gauge observations can apply inaccurate bias corrections of radar-derived QPEs (Seo and Breidenbach 2002; Martinaitis et al. 2015).

The limitations of gauge observations and the inability to efficiently quality control observations in regions not adequately sampled by radars can also influence the quality of the Mountain Mapper QPE. The challenges of winter precipitation with rain gauges can greatly reduce the number of accurate observations; thus, the lack of observations would not allow for a proper depiction of liquid-equivalent accumulations in mountainous regions. MRMS Mountain Mapper QPEs systematically underestimate precipitation when compared to independent daily gauge observations (e.g., Martinaitis et al. 2014). Bias analyses over the western CONUS for October 2017 and April 2018 when synoptically driven rain events were prevalent consistently show an underestimation bias of approximately 20% (Fig. 3).

MRMS IDW methodology for Mountain Mapper QPE also allows for a large interpolation of a single nonzero gauge observation in a gauge-sparse region, including that of localized convective storms with large accumulation gradients. The depicted areal extent of nonzero precipitation through the 200-km interpolation radius is not representative of the true precipitation coverage, more notably for hourly accumulations < 0.508 mm (0.02 in.; e.g., Fig. 4).

NWP model QPF challenges can be driven by uncertainties from model initialization (e.g., Lin et al. 2005) and performance with radar data assimilation (e.g., Pinto et al. 2015). Duda et al. (2014) summarized other NWP challenges and ensemble forecasting that can create errors in QPFs, including uncertainties in initial conditions, systematic model error, and sensitivities to microphysics and boundary layer parameterizations. Similar challenges and uncertainties that impact model-derived QPFs can also influence other NWP parameters utilized within the MSQPE scheme. Upstream convection has also been shown to influence model biases of downstream convection based on storm motion and the subsequent impacts on moisture transport and the low-level jet (Mahoney and Lackmann 2007). Model-calculated precipitation rates, including the prediction of hydrometeor mixing ratios and fall speeds in convective-allowing models, also have uncertainty and limitations that can impact the resulting precipitation forecast.

c. Defining radar coverage gaps

It is important to understand where radar-derived precipitation might not be optimal and would require other sources to improve precipitation coverage and
accuracy. The MRMS system computes a radar quality index (RQI) that serves as a proxy for radar coverage and data uncertainty (Zhang et al. 2012a). The RQI is defined by radar beam blockage and height characteristics,

$$ RQI = RQI_{blk} \times RQI_{hgt}, $$ (1)

with two primary components: radar beam blockage $RQI_{blk}$ and radar beam height characteristics $RQI_{hgt}$, which accounts for height above radar level (ARL) and the beam location with respect to the freezing-level height and brightband thickness. The RQI is calculated on a unitless scale from 0.0 to 1.0, where a value of 1.0 represents data with the highest potential quality.

Adjustments to the Zhang et al. (2012a) logic were made for this study to better define radar coverage. $RQI_{blk}$ was modified to accommodate for beam blockage (blk) up to 60% for a beam that is at least 10 m AGL:

$$ RQI_{blk} = \begin{cases} 
1; & \text{blk} < 0.1 \\
1 - \frac{\text{blk} - 0.1}{0.5}; & 0.1 \leq \text{blk} \leq 0.6 
\end{cases} $$ (2)

A beam that has $\text{blk} > 60\%$ is not considered in the generation of seamless reflectivity maps in MRMS based on criteria used to develop hybrid scan reflectivities in MRMS; thus, the next elevation angle with $\text{blk} \leq 60\%$ is considered in the calculation. The $RQI_{hgt}$ logic is dependent on the radar beam location with respect to the freezing-level height $H_{0C}$ and a reference height $H_D$ where radar observations become less correlated with surface precipitation. Height $H_D$ is 1000 m for the MRMS CONUS domain. $RQI_{hgt}$ for areas where $H_{0C} > H_D$ is defined as

$$ RQI_{hgt} = \begin{cases} 
1; & h < H_{0C} \\
\exp \left[ -\frac{(h - H_{0C})^2}{H_1^2} \right]; & H_{0C} \leq h \leq H_{0C} + \Delta H \\
\exp \left[ -\frac{(h - H_{0C})^2}{H_{1,2}^2} \right]; & h > H_{0C} + \Delta H 
\end{cases} $$ (3)

where $h$ is the adjusted top beam height (m AGL), $H_1$ is a height-scale factor in rain (4000 m), $H_2$ is a height-scale factor in snow (3000 m), $\Delta H$ is a transition zone defaulted at 800 m for the height-scale transition from $H_1$ to $H_2$, and $H_{1,2}$ is a height scale varying linearly from $H_1$ to $H_2$ across the transition zone. Heights $H_1$ and $H_2$ are defined to vary the reduction of RQI within the two different precipitation regimes. $RQI_{hgt}$ for areas where $0 < H_{0C} \leq H_D$ is defined as

$$ RQI_{hgt} = \begin{cases} 
1; & h < H_{0C} \\
\exp \left[ \frac{(h - H_{0C})^2}{H_2^2} \right]; & h = H_{0C} 
\end{cases} $$ (4)

$$ RQI_{hgt} \text{ for areas where } H_{0C} \leq 0 \text{ is defined as} $$

$$ RQI_{hgt} = \exp \left( \frac{h^2}{H_2^2} \right). $$ (5)

The height parameters were selected subjectively based on evaluations of MRMS radar QPEs (Chen et al. 2013).
to reflect the relative radar QPE quality degradation as a function of range via beam spreading and beam overshooting of microphysical processes that play a major role in identifying near-surface precipitation intensity.

Beam height calculations changed from ARL to AGL to account for variations in beam height over complex terrain. The mathematical changes to ROI resulted in a more consistent performance based on the improved variables to account for sampling degradation with increased range from radar and height AGL along with adjustments relating to the application of freezing-level height influences (Fig. 5). The precision of the final ROI output was increased from 0.1 to 0.01 to prevent potential discontinuities during the blending of precipitation sources. These cumulative ROI improvements allow for a better representation of where optimal radar coverage exists while mitigating artifacts and discontinuities (Fig. 6).

3. Multisensor gap-filling scheme

a. Blending logic

The physical blending of multiple precipitation sources utilizes radar coverage, atmospheric conditions, and orography based on the various strengths of each precipitation input (Fig. 7). The MSQPE foundationally utilizes the equation from Zhang et al. (2014) redefined as the following:

\[
\text{MSQPE} = \frac{w_g Q_{\text{GAP}} + (1 - w_g)w_r Q_{\text{LGC}}}{w_g + (1 - w_g)w_r}. \tag{6}
\]

The LGC radar QPE \( Q_{\text{LGC}} \) is the primary precipitation input and weighted by the variable \( w_r \). The amalgamation of the remaining precipitation sources is handled by the gap-filling QPE \( Q_{\text{GAP}} \) weighted by the variable \( w_g \). The \( Q_{\text{GAP}} \) is calculated using the following logic:

\[
Q_{\text{GAP}} = Q_{\text{NWP}}(1 - w_m) + sw_m Q_{\text{MM}}. \tag{7}
\]

Integration of gap-filling HRRRv2 model 1-h QPF \( Q_{\text{NWP}} \) and the MRMS Mountain Mapper QPE \( Q_{\text{MM}} \) utilizes the Mountain Mapper weighting function \( w_m \):

\[
w_m = w_s \times w_{\text{wb}} \times (1 - w_f) \times \alpha. \tag{8}
\]

The static weighting variable \( w_s \) is defined by a gridded slope field based on topographic steepness and allows for \( Q_{\text{MM}} \) to be applied over complex terrain only. Grid cells with a slope \( \geq 5.0^\circ \) have a value of 1.00, and a buffer of 20 km is applied around these grid cells with \( w_s \) reducing linearly by 0.05 km\(^{-1} \) (Fig. 8).

The weighting variable \( w_{\text{wb}} \) utilizes the HRRRv2 model surface wet-bulb temperature \( T_{\text{wb}} \) to delineate areas of frozen precipitation versus rain to restrict the use of \( Q_{\text{MM}} \) in winter precipitation due to limitations of recording accurate liquid-equivalent accumulations. Application of the surface \( T_{\text{wb}} \) accounts for the
occurrence of frozen precipitation within environments defined by above-freezing ambient temperatures and nonsaturated relative humidity values (e.g., Matsuo and Sasyo 1981). A threshold surface $T_{wb}$ of $0.00^\circ C$ is used based on the work by Martinaitis et al. (2015) with a linear transition defined by

$$w_{twb} = \begin{cases} 
1.00; & T_{wb} \geq 2.00 \\
\frac{T_{wb}}{2}; & 0.00 < T_{wb} < 2.00 \\
0.00; & T_{wb} \leq 0.00 
\end{cases} \quad (9)$$

The blending of $Q_{NWP}$ and $Q_{MM}$ is also characterized by a delineation of warmer and cooler atmospheric environments based on the freezing-level height $f$ in meters AGL to limit the use of $Q_{MM}$ in convective precipitation using the weighting function $w_f$, which is defined as

$$w_f = \begin{cases} 
1.00; & f \geq 3000 \\
\frac{f - 1750}{1250}; & 1750 < f < 3000 \\
0.00; & f \leq 1750 
\end{cases} \quad (10)$$

The use of $f$ and its linear blending value range for defining atmospheric environments for stratiform and convective precipitation properties is modified from the surface precipitation type classification decision
tree for identifying convective precipitation (Zhang et al. 2016) based upon evaluations of precipitation events during the MSQPE product development.

The scaling factor \( s \) in Eq. (7) and the variable \( \alpha \) in Eq. (8) address some \( Q_{MM} \) deficiencies. The persistent underestimation bias of \( Q_{MM} \) is corrected through the scaling factor \( s \) set to a constant value of 1.2035 using a linear best-fit equation based \( Q_{MM} \) comparisons to independent gauge data (e.g., Fig. 3). The variable \( \alpha \) prevents the use of nonrealistic light precipitation coverage (e.g., Fig. 4) via the following logic:

\[
\alpha = \begin{cases} 
1.00; & (s \times Q_{MM}) \geq 2.032 \\
\frac{(s \times Q_{MM}) - 0.508}{1.254}; & 0.508 < (s \times Q_{MM}) < 2.032 \\
0.00; & (s \times Q_{MM}) \leq 0.508 
\end{cases}
\] (11)

The values of 0.508 mm (0.02 in.) and 2.032 mm (0.08 in.) for the linear blending of \( Q_{MM} \) are derived from extensive internal studies on the interpolation of \( Q_{MM} \) values.

The weighting functions \( w_r \) and \( w_g \) in Eq. (6) balance the combination of \( Q_{LGC} \) and \( Q_{GAP} \). The weighting function \( w_r \) for \( Q_{LGC} \) is based on the MRMS RQI product as the proxy for radar coverage. The extent of \( Q_{LGC} \) coverage is dynamically altered based on atmospheric parameters characterizing warm and cool precipitation environments via \( w_r \). The weighting of \( Q_{LGC} \) via \( w_r \) is defined as

\[
w_r = \begin{cases} 
1.00; & \text{RQI} \geq (1.00 - 0.70w_f) \\
y; & (0.60 - 0.60w_f) < \text{RQI} < (1.00 - 0.70w_f) \\
0.00; & \text{RQI} \leq (0.60 - 0.60w_f) 
\end{cases}
\] (12)

The full use of \( Q_{LGC} \) for stratiform rain and snow environments is only when \( \text{RQI} = 1.00 \) and then reduces in contribution until \( \text{RQI} = 0.60 \). The influence of \( Q_{LGC} \) is much greater in convective environments, where \( Q_{LGC} \) is fully utilized in the RQI range of 0.30–1.00 with reduced \( Q_{LGC} \) contributions until \( \text{RQI} = 0.00 \). These values were defined based on extensive analysis of and contrasting of shallow stratiform precipitation events to convective events. The contribution of \( Q_{LGC} \) within the dynamic RQI range bounded by the incorporation of \( w_f \) is calculated through the cubic polynomial function \( y \):

\[
y = (n_3 x^3) + (n_2 x^2) + (n_1 x) + n_0.
\] (13)

The \( n \) variables in Eq. (13) are quadratic functions dynamically based on \( w_f \) and are defined by the following:

\[
n_3 = 39.904w_f^2 - 40.464w_f + 0, \quad (14)
\]

\[
n_2 = -59.075w_f^2 + 53.614w_f + 3.333, \quad (15)
\]

\[
n_1 = 18.168w_f^2 - 11.674w_f - 2.833, \quad (16)
\]

and

\[
n_0 = w_f^3 - 1.5w_f + 0.5. \quad (17)
\]

The weighting of \( Q_{GAP} \) via \( w_g \) also relies upon RQI and \( w_f \); however, it also contains logic to increase the weight of \( Q_{LGC} \) at gauge observations within a certain range of radar influence. The calculations for \( w_g \) utilize the following logic:

\[
w_g = \begin{cases} 
0.00; & \text{RQI} \geq (1.00 - 0.70w_f) \\
g; & (0.60 - 0.60w_f) < \text{RQI} < (1.00 - 0.70w_f) \\
\beta; & \text{RQI} \leq (0.60 - 0.60w_f) 
\end{cases}
\] (18)

A nonzero value of \( w_g \) is based on the gauge influence function \( g \) and a background weighting function \( \beta \). The function \( g \) allows for greater weight of \( Q_{LGC} \) near gauge
locations to locally retain the gauge-corrected radar-based spatial representation of precipitation by reducing the influence of $Q_{\text{GAP}}$ via

$$g_i = \begin{cases} 
\beta \times \sin \left( \frac{\pi d}{2R_i} \right), & d \leq R_i \\
\beta, & d > R_i
\end{cases}$$

(19)

where $R_i$ is the radius of influence at a fixed value of 20 km and $d$ is the distance of a grid cell from the nearest gauge observation. The grid cell containing the gauge observation will utilize $Q_{\text{LGC}}$ while a sine function using $\beta$ creates a seamless transition between $Q_{\text{LGC}}$ at $d = 0$ and the weighted combination of $Q_{\text{GAP}}$ and $Q_{\text{LGC}}$ when $\beta \neq 0$ and $d \leq R_i$.

Grid cells outside of $R_i$ will rely solely on the background weighting function $\beta$, which dynamically changes in a similar manner to $w_f$ in order to vary the contribution of $Q_{\text{GAP}}$ for warmer and cooler atmospheric environments. The background weighting function $\beta$ utilized in $w_g$ and $g_i$ is characterized by ROI and $w_f$ and is defined as

$$\beta = \begin{cases} 
0.00, & \text{ROI} \geq (1.00 - 0.70w_f) \\
\beta_{nc}, & (0.60 - 0.60w_f) < \text{ROI} < (1.00 - 0.70w_f), \\
\beta_{\text{max}}, & \text{ROI} \leq (0.60 - 0.60w_f)
\end{cases}$$

(20)

where

$$\beta_{nc} = \beta_{\text{max}} - \left[ \frac{\text{ROI} - (0.60 - 0.60w_f)}{2 + 3w_f} \right]$$

$$\times \frac{(1.00 - 0.70w_f) - \text{ROI}}{(1.00 - 0.70w_f) - (0.60 - 0.60w_f)},$$

(21)

and

$$\beta_{\text{max}} = 0.50 - 0.30w_f.$$  

(22)

The combination of $w_f$ and $w_g$ from Eq. (6) defines the percent contribution of $Q_{\text{LGC}}$ and $Q_{\text{GAP}}$ at a grid cell (Fig. 9). The $Q_{\text{GAP}}$ and $Q_{\text{LGC}}$ would have an equal contribution for shallow stratiform rain and snow in cooler environments (i.e., when $w_f = 0.00$) at ROI $\approx 0.75$ and for convective regimes ($w_f = 1.00$) at ROI $\approx 0.05$. The resulting MSQPE undergoes one last check before producing the gridded output. The blending of precipitation inputs can generate areas of light precipitation artifacts. Hourly precipitation values $< 0.2$ mm are reset to 0.0 mm to mitigate instances of nonzero MSQPE values being collocated with hourly gauges observing no precipitation.

b. Product timing

The MRMS system ingest of gauge networks captures approximately 90% of all observations at 70 min past valid time. The data latency of gauge observations combined with the computation time to generate both $Q_{\text{LGC}}$ and $Q_{\text{MM}}$ along with the final MSQPE product results in an approximately 85-min latency from valid time for MSQPE. This makes MSQPE applicable for hydrologic model forcing along with water resourcing and climatological assessments but not for flash flood detection and warning decisions. Rate-driven events and quick basin response times would require the use of a radar-only QPE (in areas where radar coverage is provided) that have a data latency of $<90$ s to help facilitate flash flood warning decision making.

4. Evaluation methodology

Hourly MSQPE products are created for the CONUS at the top of the hour and accumulated to 24-h totals. Performance evaluations of the MSQPE product were then conducted on 43 event days west of 100°W longitude and 25 event days east of 100°W longitude (Table 1). The three input precipitation sources and the final MSQPE product were compared against independent Community Collaborative Rain, Hail and Snow (CoCoRaHS) network daily gauge observations (Cifelli et al. 2005). The comparison between CoCoRaHS gauges and the 24-h precipitation product accumulations were conducted over a 3-h period. Events over the western CONUS were evaluated over a period from 1400 to 1600 UTC in standard time and from 1300 to...
1500 UTC in daylight saving time. Eastern CONUS events were evaluated from 1200 to 1400 UTC in standard time and from 1100 to 1300 UTC in daylight saving time. This was done to utilize as many CoCoRaHS observations as possible when generally reporting at 0700 local time. CoCoRaHS gauges were removed to avoid potential biases from temporal differences. The authors also removed CoCoRaHS gauge observations that were deemed erroneous to prevent inaccurate results. Erroneous gauges were either extreme outliers or zero values in areas of significant precipitation (i.e., \( >12.7 \text{ mm} \)) based on gridded QPEs and neighboring CoCoRaHS gauges. An average of 3–6 CoCoRaHS observations were removed per event day.

Statistical metrics used to evaluate the MSQPE performance against the four input precipitation sources include the mean bias ratio (MBR), mean error (ME), mean absolute error (MAE), and Pearson linear correlation coefficient (CC), which are defined as

\[
\text{MBR} = \frac{\sum_{i=1}^{N} R_i}{\sum_{i=1}^{N} G_i},
\]

\[
\text{ME} = \frac{\sum_{i=1}^{N} (R - G)_i}{N},
\]

\[
\text{MAE} = \frac{\sum_{i=1}^{N} |(R - G)_i|}{N},
\]

and

\[
\text{CC} = \frac{\text{cov}(R, G)}{\sigma_R \sigma_G}.
\]

The term \( R \) represents the gridded precipitation source, \( G \) represents the CoCoRaHS gauge observations, \( N \) is the number of \( R \) versus \( G \) comparisons over the 3-h evaluation period, and \( \sigma \) is the standard deviation. Pairings where both \( R \) and \( G \) were not reporting precipitation were not used in the statistical analyses. The removal of \( G, R = 0 \) pairings resulted in an average of 925 \( R \) versus \( G \) comparisons for each western CONUS event and 3500 for each eastern CONUS event. Particular attention was given to the performances between the radar-based approach (i.e., LGC radar QPE) and MSQPE to demonstrate potential improvements from utilizing a radar gap-filling methodology. All precipitation products were ranked for each event day to determine how MSQPE compared to the three gridded precipitation inputs across the different statistical measures.

The \( R \) versus \( G \) comparisons were also binned into three categories: the gauge and gridded precipitation product reporting precipitation \( (G, R > 0) \), the gauge reporting precipitation but the gridded precipitation product does not \( (G > 0, R = 0) \), and the gridded precipitation product reporting precipitation but the gauge does not \( (G = 0, R > 0) \). The distributions of these categories were evaluated for the precipitation inputs and final MSQPE product. Direct comparisons between the LGC radar QPE and MSQPE will quantify how the gap-filling precipitation sources reduced the \( G > 0, R = 0 \) instances and determine if false precipitation areas are being introduced into MSQPE.

### Table 1

| Domain      | Year | Month | Dates           | Hours evaluated (UTC) |
|-------------|------|-------|-----------------|-----------------------|
| Western CONUS | 2017 | 10    | 8–9, 11–13, 19–21 | 1300–1500             |
|             |      | 11    | 1–2             | 1300–1500             |
|             |      | 11    | 13–18, 21–24, 26–28 | 1400–1600             |
|             |      | 12    | 17–18, 21, 23–24 | 1400–1600             |
|             | 2018 | 2     | 4–6, 16–20      | 1400–1600             |
|             |      | 3     | 2–3             | 1400–1600             |
|             |      | 5     | 21              | 1300–1500             |
|             |      | 6     | 17–20           | 1300–1500             |
| Eastern CONUS | 2018 | 11    | 6, 9–10, 25–27  | 1200–1400             |
|             |      | 12    | 2–3             | 1200–1400             |
|             | 2019 | 2     | 12–13, 20, 25, 27–28 | 1200–1400             |
|             |      | 3     | 2–4             | 1200–1400             |
|             |      | 3     | 10–11, 14–15, 21–23, 31 | 1100–1300             |
Two event days are also presented in detail. Included in the case analyses are the hourly percent contributions of each precipitation input to portray how each source influenced MSQPE. The calculation for the percent contribution of $Q_{LGC}$ is

$$
\text{PERC}_{LGC} = \frac{(1-w_g)w_r}{w_g + (1-w_g)w_r} + \frac{w_g}{w_g + (1-w_g)w_r}.
$$

The percent contribution fields for the precipitation inputs that create $Q_{GAP}$ are defined by the following:

$$
\text{PERC}_{MM} = (1 - \text{PERC}_{LGC})w_m, \quad \text{PERC}_{NWP} = (1 - \text{PERC}_{LGC})(1 - w_m).
$$

## 5. Overall multisensor QPE performance

### a. Comparing gridded precipitation products

Statistical measures of the 43 daily events over the western CONUS exhibited numerous improvements by MSQPE over the radar-centric LGC radar QPE (Table 2). The average overall MBR value increased from 0.747 to a more ideal 0.970. Initial underestimation biases of LGC radar QPE can be primarily attributed to the reduced radar and gauge observational density resulting in missed or underrepresented precipitation events. MSQPE produced seamless contiguous fields which mitigated the systematic underestimation bias that was a result of inadequate radar coverage. The average ME for LGC radar QPE was reduced by 75% when applying the MSQPE scheme, and the average MAE was reduced by 12% to 2.447 mm. The smaller decline in MAE may be influenced by biases in the LGC radar QPE and/or the gap-filling precipitation inputs having estimation biases. Large biases with the precipitation inputs can also explain the minimal reduction of the MAE standard deviation and the slight increase in the MBR standard deviation from 0.140 to 0.176. The average overall CC values were also improved by 11% to 0.833 along with a 47% reduction of the CC standard deviation.

The MAE and CC statistics for MSQPE outperformed the three input precipitation sources, yet some of the input sources appear to have better MBR and ME statistics over MSQPE. The HRRRv2 1-h QPFs has a more ideal median MBR value as well as better median and average ME values; however, the standard deviations of the MBR and ME values for the HRRRv2 1-h QPFs are the greatest among all evaluated products (Table 2). This can be attributed to the HRRRv2 significantly overestimating precipitation magnitudes for certain events while equally underestimating precipitation for other events. The greater range of MBR values for the HRRRv2 is more clearly demonstrated through comparing the interquartile spread between the 25th and 75th percentiles (Fig. 10a). A similar pattern of results was shown for ME values. The HRRRv2 had a better average ME value by 0.243 mm over MSQPE, yet the standard deviation and interquartile range was more than double that of MSQPE (Fig. 10b) with reduced correlation to independent gauges compared to the other inputs and final MSQPE product (Fig. 10d). The Mountain Mapper QPE was characterized by underestimation biases along with higher ME throughout the evaluated cases; however, it did have comparable MAE and CC values to MSQPE (Figs. 10c,d).

### Table 2. The median, average ($\mu$), and standard deviation ($\sigma$) of the MBR, ME, MAE, and CC statistical measures of the three input precipitation products and the MSQPE product across the 43 evaluated cases over the western CONUS domain. The best value in each statistical category is italicized.

|                  | LGC radar QPE | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE |
|------------------|--------------|---------------------|----------------|-------|
| **MBR**          | Median       | 0.747               | 0.824          | 0.963 | 0.931 |
|                  | $\mu$        | 0.747               | 0.783          | 1.032 | 0.970 |
|                  | $\sigma$     | 0.140               | 0.169          | 0.244 | 0.176 |
| **ME (mm)**      | Median       | -1.521              | -1.047         | -0.206 | -0.449 |
|                  | $\mu$ (mm)   | -1.526              | -1.081         | -0.097 | -0.380 |
|                  | $\sigma$ (mm)| 1.011               | 0.534          | 1.332 | 0.667 |
| **MAE (mm)**     | Median       | 2.699               | 2.472          | 3.176 | 2.364 |
|                  | $\mu$ (mm)   | 2.780               | 2.480          | 3.453 | 2.447 |
|                  | $\sigma$ (mm)| 0.990               | 0.865          | 1.554 | 0.801 |
| **CC**           | Median       | 0.799               | 0.858          | 0.747 | 0.861 |
|                  | $\mu$        | 0.752               | 0.810          | 0.732 | 0.833 |
|                  | $\sigma$     | 0.171               | 0.128          | 0.117 | 0.090 |
Cumulative rankings of the statistical measures further demonstrated how MSQPE was statistically superior, even though it was not the best ranked product for every case in every measure (Fig. 11). The average ranking for MSQPE was the best among the three input sources apart from MAE, where Mountain Mapper QPE had more event days with lower MAE values. MSQPE was ranked first 47.67% of the time across the four statistical categories for all event with the next closest product being Mountain Mapper QPE at 27.33% (Table 3). MSQPE was ranked first or second 88.37% of the time and had 98.84% of all first through third rankings across the four statistical categories. Instances when MSQPE did not outperform a precipitation input were not statistically significant. MSQPE MAE values not ranked first were within 0.50 mm of the best ranked product for 23 of those 25 occurrences. Of the 23 events when MSQPE did not have the best CC, the difference was less than 0.06 from the best recorded value in 21 of those cases.

Similar overall statistical analysis and cumulative rankings were conducted for the eastern CONUS cases (Table 4). The average MBR of 0.922 for LGC radar QPE was improved to 0.955 using the MSQPE scheme, and the average ME value was reduced by 33% to 0.455 mm. The HRRRv2 1-h QPFs again displayed more ideal MBR and ME values; however, the large standard deviation in these values along with the large interquartile spread demonstrates the large variability in biases in the HRRRv2 over the eastern CONUS (Figs. 12a,b). The MSQPE product had the best average MAE and CC values, yet the differences between MSQPE and the LGC radar QPE were minimal in both the overall statistics (Table 4) and the box-and-whisker representations (Figs. 12c,d).

The cumulative rankings of the 25 eastern CONUS cases highlight some of the similarities of the LGC radar QPE input and the final MSQPE product with respect to MAE and CC (Figs. 13a,d), yet MSQPE had more events ranked in the top two for the MBR and ME.
values (22) than LGC radar QPE (13). The Mountain Mapper QPE consistently displayed the greatest bias among the four products through its systematic underestimation of precipitation, and it was generally ranked third for MAE and CC values (Fig. 13b). The HRRRv2 1-h QPF MBR and CC rankings were scattered among the 25 eastern CONUS events, but it constantly had the greatest MAE and lowest CC values (Fig. 13c). The MSQPE product across the four statistical categories was ranked first at a rate of 42% followed by LGC radar QPE at 35% (Table 5), yet the combination of the LGC radar QPE with the gap-filling inputs allowed MSQPE to be ranked first or second 94% of the time. The differences between MSQPE and the best ranked input for instances when MSQPE was not ranked first were minimal. All MSQPE MAE values that were not ranked first were <0.3 mm of the best ranked input, and all CC values were within 0.007 of the best ranked input.

### b. Precipitation coverage analysis

The perspective from $G$, $R$ comparisons demonstrated an improvement in coverage while minimizing the addition of false precipitation areas for the western CONUS events. The average percent of $G$, $R$ pairings increased from 70.69% using LGC radar QPE to 78.26% with MSQPE (Table 6); moreover, MSQPE had better median, average, and standard deviation values compared to its input sources. Box-and-whisker depictions of the $G$, $R$ > 0 comparisons further
demonstrate the improvement of MSQPE over the input precipitation sources (Fig. 14a). The HRRRv2 1-h QPF had similar interquartile ranges and standard deviations, yet the median and average values were about 2%-3% lower than MSQPE. Mountain Mapper QPE also achieved similar statistical performances yet struggled in some events due to lack of gauge coverage in certain regions to interpolate nonzero observations or impacts from winter precipitation preventing the measurement of liquid equivalent values.

More significant improvements were noted in the $G > 0$, $R = 0$ analysis. The percent of instances LGC radar QPE missed precipitation decreased to 13.565% of pairings classified as $G > 0$, $R = 0$ for MSQPE (Table 6). The 75th percentile of the $G > 0$, $R = 0$ pairings was reduced from 30.85% for LGC radar QPE to 17.66% when applying the MSQPE scheme (Fig. 14b).

### Table 4. As in Table 2, but for the 25 eastern CONUS events.

|       | LGC radar QPE | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE |
|-------|---------------|---------------------|----------------|-------|
| **MBR** |               |                     |                |       |
| Median | 0.919         | 0.862               | 1.030          | 0.952 |
| $\mu$  | 0.922         | 0.839               | 1.090          | 0.955 |
| $\sigma$ | 0.061       | 0.098               | 0.243          | 0.077 |
| **ME** |               |                     |                |       |
| Median (mm) | -0.643     | -1.135              | 0.334          | -0.455|
| $\mu$ (mm)  | -0.708       | -1.208              | 0.222          | -0.475|
| $\sigma$ (mm) | 0.559       | 0.605               | 1.158          | 0.581 |
| **MAE** |               |                     |                |       |
| Median (mm) | 2.521        | 2.665               | 4.186          | 2.416 |
| $\mu$ (mm)  | 2.456         | 2.756               | 4.070          | 2.477 |
| $\sigma$ (mm) | 0.635       | 0.732               | 1.202          | 0.632 |
| **CC**  |               |                     |                |       |
| Median | 0.926         | 0.887               | 0.779          | 0.929 |
| $\mu$  | 0.907         | 0.879               | 0.771          | 0.915 |
| $\sigma$ | 0.053        | 0.055               | 0.092          | 0.038 |

![Fig. 12](image-url) As in Fig. 10, but for the 25 eastern CONUS events.
The MSQPE, Mountain Mapper QPE, and HRRRv2 precipitation products all had similar statistical performances with reduced instances of missed precipitation compared to LGC radar QPE. Only a small proportion of cases had the percent of $G > 0, R = 0$ pairings below 5%. It is assumed that inaccurate non-zero observations, nondetectable near-surface hydrometeors (e.g., fog or mist), condensation, or winter precipitation impacts (e.g., blowing snow or postevent thaw) would prevent near-zero percentages of $G > 0, R = 0$ pairings over large domains.

The LGC radar QPE performed the best overall with minimizing false precipitation coverage with an average of 7.295% of $G, R$ comparisons classified as $G = 0, R > 0$. This can be contributed to the greater percentages of missed precipitation due to insufficient radar coverage and the utilization of an evaporation correction scheme in MRMS to reduce false light precipitation (Martinaitis et al. 2018). The increase of false precipitation in MSQPE was minimal over LGC radar QPE (Table 6; Fig. 14c). This is attributed to the blending of the other precipitation sources into the MSQPE scheme that also had higher percentages of $G = 0, R > 0$ comparisons. The application of reducing blended precipitation values $< 0.2$ mm to zero also improved the MSQPE performance over the nonradar inputs.

The eastern CONUS events showed that the statistical measures among the evaluated precipitation products had similar trends to that of the western CONUS analysis with a few notable exceptions (Table 7; Fig. 15). The $G, R > 0$ comparisons for LGC Radar QPE were more comparable to Mountain Mapper QPE and HRRRv2 1-h QPF due to greater radar coverage over the eastern CONUS. The increased radar coverage also limited the average percent of $G > 0, R = 0$ comparisons over

![Fig. 13. As in Fig. 11, but for the 25 eastern CONUS events.](image)

| LGC radar QPE | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE |
|---------------|---------------------|----------------|-------|
| Rank percentage: 1 | 35.00 | 6.00 | 17.00 | 42.00 |
| Rank percentage: 1–2 | 69.00 | 14.00 | 23.00 | 94.00 |
| Rank percentage: 1–3 | 95.00 | 71.00 | 34.00 | 100.00 |
the eastern CONUS (11.216%) versus the western CONUS (22.011%). The greater radar coverage area can also explain the domain-wide performance similarities between the LGC radar QPE and the resulting MSQPE product through the G, R comparisons. One notable trend over the eastern CONUS was opposite of that over the western CONUS: the percent of G = 0, R > 0 observations decreased from the LGC radar QPE input. This is likely attributed to the nonevaporated precipitation detected by radar at farther distances being correctly removed through the blending of HRRRv2 when it generates zero values over those regions.

6. Case studies

a. 17–18 February 2018

Multiple radar coverage gaps highlighted the challenges of detecting shallow precipitation features and accurately portraying the true areal precipitation extent for this event. Prominent radar coverage gaps can be

| Table 6. The median, average (μ), and standard deviation (σ) of the three input precipitation products and the MSQPE product across the 43 evaluated cases over the western CONUS domain for the percent of G, R comparisons that are categorized into the following pairings: (a) G > 0, (b) G > 0, R = 0, and (c) G = 0, R > 0. The best value in each statistical category is italicized. |
|------------------|------------------|------------------|------------------|------------------|
|                  | LGC radar QPE    | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE            |
| G, R > 0         | Median 73.845    | 79.240            | 78.380          | 80.204           |
|                  | μ 70.694         | 77.189            | 75.467          | 78.267           |
|                  | σ 12.250         | 11.697            | 11.173          | 10.217           |
| G > 0; R = 0     | Median 20.072    | 10.148            | 12.255          | 11.516           |
|                  | μ 22.011         | 12.945            | 14.606          | 13.565           |
|                  | σ 10.833         | 9.955             | 8.875           | 7.907            |
| G = 0; R > 0     | Median 6.649     | 9.413             | 10.040          | 8.035            |
|                  | μ 7.295          | 9.866             | 9.927           | 8.167            |
|                  | σ 3.770          | 5.132             | 4.631           | 4.116            |

Fig. 14. As in Fig. 10, but for the percent of G, R comparisons that are categorized into the following pairings: (a) G, R > 0, (b) G > 0, R = 0, and (c) G = 0, R > 0.
seen over Montana, Idaho, northwest Wyoming, northern Washington, and along the Oregon coast (Fig. 16a). The Mountain Mapper QPE (Fig. 16b) and HRRRv2 1-h QPF (Fig. 16c) provided a better depiction of precipitation coverage but with differences in magnitude across the various mountain ranges and eastern Montana. The MSQPE product generated a more continuous precipitation field with more enhanced accumulations across the mountainous terrain while incorporating the HRRRv2 QPF values across the northern Plains. (Fig. 16d). The MBR, ME, and CC values for MSQPE outperformed the three input sources (Table 8). Mountain Mapper QPE exhibited a lower MAE although having a significant underestimation bias; however, the MSQPE MAE was only 0.045 mm greater but with a near-ideal MBR of 0.965. The G, R comparisons between Mountain Mapper QPE, HRRRv2 QPF, and MSQPE had similar distributions; moreover, the differences in the G, R > 0 and G > 0, R = 0 categories between MSQPE and the LGC radar QPE demonstrate how the merged precipitation approach provides a more representative depiction of precipitation coverage based on the gauge observations.

Focused analyses of the LGC radar QPE and MSQPE products over the eastern Washington to western Montana region emphasized the impacts of gap-filling prominent

Table 7. As in Table 6, but for the 25 eastern CONUS events.

|                  | LGC radar QPE | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE |
|------------------|---------------|---------------------|----------------|-------|
| G, R > 0         | Median        | 79.534              | 78.552         | 78.280| 79.831|
|                  | μ             | 78.212              | 76.812         | 76.791| 78.653|
|                  | σ             | 9.987               | 11.965         | 10.193| 9.799 |
| G > 0; R = 0     | Median        | 7.869               | 8.771          | 7.488 | 8.683 |
|                  | μ             | 11.216              | 12.468         | 7.643 | 12.518|
|                  | σ             | 7.94                | 10.508         | 4.793 | 8.045 |
| G = 0; R > 0     | Median        | 11.148              | 9.840          | 13.886| 9.199 |
|                  | μ             | 10.572              | 10.719         | 15.566| 8.830 |
|                  | σ             | 4.792               | 5.822          | 9.188 | 3.914 |

Fig. 15. As in Fig. 14, but for the 25 eastern CONUS events.
radar coverage gaps that initially resulted in zero accumulated precipitation by LGC radar QPE (Figs. 17a,b); moreover, nonzero accumulation discontinuities from beam blockages were also mitigated via the MSQPE scheme. The various radar coverage challenges resulted in 19.75% of \( G > 0, R = 0 \) pairings for LGC radar QPE and generated a poorly correlated underestimation MBR with significant error values (Table 9). This was also reflected in the scatterplot of CoCoRaHS observations versus LGC radar QPE, notably with the \( G, R \) comparisons located along the \( x \) axis (Fig. 17c).

Application of the MSQPE scheme resulted in a slight overestimation bias for this area while reducing the ME and MAE by 84.0% and 32.1%, respectively. The CC value was improved by 0.196 to 0.774, and the percent of \( G > 0, R = 0 \) pairings was significantly reduced (Table 9; Fig. 17d).

The native hourly accumulations of LGC radar QPE and MSQPE demonstrated how radar coverage issues were resolved throughout this event, especially in northern Idaho and far western Montana (Fig. 18). Percent contribution plots characterized the extent of

| Table 8. Statistical measures MBR, ME, MAE, and CC along with the percent of \( G, R \) comparisons categorized into the \( G, R > 0 \), \( G > 0, R = 0 \), and \( G = 0, R > 0 \) pairings for the three input precipitation products and the final MSQPE product over the full western CONUS study domain for the 17–18 Feb 2018 event. The best value in each statistical category is italicized. |
|-----------------|-----------------|-----------------|-----------------|-----------------|
|                 | LGC radar QPE   | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE           |
| MBR             | 0.539           | 0.756           | 1.093           | 0.965           |
| ME (mm)         | -3.116          | -1.654          | 0.619           | -0.235          |
| MAE (mm)        | 3.963           | 2.682           | 3.176           | 2.727           |
| CC              | 0.660           | 0.817           | 0.803           | 0.822           |
| \( G, R > 0 \)  | 62.94%          | 79.42%          | 79.77%          | 79.61%          |
| \( G > 0; R = 0 \) | 33.90%          | 17.81%          | 15.21%          | 16.10%          |
| \( G = 0; R > 0 \) | 3.16%          | 2.77%           | 5.02%           | 4.29%           |
radar coverage utilized by the MSQPE scheme and how the other sources compensated for the coverage (Fig. 19). The retention of radar coverage in MSQPE was minimal due to subfreezing surface temperatures reducing RQI values via Eq. (5). Mountain Mapper QPE was only locally applied during the first half of the event across the windward side of the Rocky Mountains in areas where above-freezing wet-bulb temperatures were modeled by the HRRRv2. This resulted in the HRRRv2 1-h QPFs being the dominant gap-filling source across the focused domain.

b. 12–13 February 2019

The 12–13 February 2019 event depicted how the MSQPE scheme can be applicable over the eastern CONUS while demonstrating how the overshooting of precipitation features by radars can be compensated for. The radar coverage of the 24-h accumulations ending 1200 UTC 13 February 2019 did not contain prominent gaps resulting in zero accumulated precipitation, yet circular artifacts were prevalent throughout the northern extent of the eastern CONUS domain due to overshooting precipitation (Fig. 20a). Both Mountain Mapper QPE and HRRRv2 1-h QPF had similar accumulation coverages but varying accumulation magnitudes (Figs. 20b,c), and their contributions to MSQPE yielded a more realistic depiction of

![Image of radar coverage and scatterplots](image)

**FIG. 17.** 24-h precipitation accumulation of (a) MRMS LGC radar QPE and (b) MSQPE QPE across eastern Washington, northern Idaho, and western Montana for the 24-h period ending 1400 UTC 18 Feb 2018. This focused domain is bounded by the northwest corner 49.0°N, 118.0°W and the southeast corner 44.0°N, 110.0°W. Below are the scatterplots of (c) MRMS LGC radar QPE and (d) MSQPE QPE compared to independent CoCoRaHS gauge observations. The dashed line represents the one-to-one line between the CoCoRaHS gauges and the gridded QPE values.

**TABLE 9.** As in Table 8, but for the focused domain bounded by the northwest corner 49.0°N, 118.0°W and the southeast corner 44.0°N, 110.0°W and only for the comparison of MRMS LGC radar QPE vs MSQPE of the 17–18 Feb 2018 event.

|                | LGC radar QPE | MSQPE |
|----------------|---------------|-------|
| MBR            | 0.572         | 1.087 |
| ME (mm)        | -5.046        | 1.025 |
| MAE (mm)       | 6.231         | 4.030 |
| CC             | 0.578         | 0.787 |
| G, R > 0       | 80.25%        | 98.77%|
| G > 0; R = 0   | 19.75%        | 1.23% |
| G = 0; R > 0   | 0.00%         | 0.00% |
precipitation accumulations by mitigating radar coverage challenges (Fig. 20d). Statistical analyses for this event showed MSQPE improved over all three input sources (Table 10), while the $G$, $R$ comparisons were similar between MSQPE and the three input sources.

Examination of the 24-h accumulations of LGC radar QPE and MSQPE over the New England area validated the reduction of the underestimation bias from the undersampling of hydrometeors (Fig. 21). The area from Vermont to Maine had prominent areas of LGC radar QPE accumulations of $<15$ mm with localized areas of $<5$ mm, whereas MSQPE had large areal depictions of 20–40 mm over the 24-h period ending 1200 UTC 13 February 2019 (Figs. 21a,b). The scatterplots versus CoCoRaHS observations reflected the underestimation of precipitation with LGC radar QPE and the improvement with MSQPE despite some

![Fig. 18. Hourly precipitation accumulation of (top) LGC radar QPE and (bottom) MSQPE across eastern Washington, northern Idaho, and western Montana ending at the following times: (a),(d) 1900 UTC 17 Feb 2018, (b),(e) 0100 UTC 18 Feb 2018, and (c),(f) 1300 UTC 18 Feb 2018. This focused domain is bounded by the northwest corner 49.0°N, 118.0°W and the southeast corner 44.0°N, 110.0°W.](image1)

![Fig. 19. The percent contribution of (a)–(c) LGC radar QPE, (d)–(f) Mountain Mapper QPE, and (g)–(i) HRRRv2 1-h QPF for the same 1-h time periods denoted in Fig. 18.](image2)
notable scatter remaining in the data (Figs. 21c,d). The focused domain MBR was improved from 0.771 to 0.922 with the ME and MAE being reduced by 66% and 26%, respectively (Table 11). The scatter in data for both products yielded low overall CC values, but the MSQPE product improved the CC by 7.0%. The $G, R$ comparisons were identical between LGC radar QPE and MSQPE.

Analyses of the event at the native hourly scale demonstrated how coverage areas were filled while the overshooting of precipitation was mitigated through the MSQPE logic (Fig. 22). Increased precipitation coverage was most prevalent early in the event while improved precipitation magnitudes were characterized across the duration of the event. The surface and atmospheric environment variables greatly influenced the percent contribution of the three input sources (Fig. 23). The LGC radar QPE contribution varied across the focused domain with more expansive utilization of radar-derived QPE to the south due to higher freezing-level heights associated with an occluded front. The HRRRv2 QPF was the sole source of filling radar coverage gaps for this event. The Mountain Mapper QPE did not contribute to MSQPE due to subfreezing wet-bulb temperatures in the mountainous terrain north of the occluded front and the expanded radar coverage south of the front.

7. Summary

The primary objective of the MSQPE product is to provide a methodology and a resulting high

|                          | LGC Radar QPE | Mountain Mapper QPE | HRRRv2 1-h QPF | MSQPE |
|--------------------------|---------------|---------------------|----------------|-------|
| MBR                      | 0.927         | 0.871               | 1.093          | 0.972 |
| ME (mm)                  | -0.831        | -1.458              | 1.050          | -0.316|
| MAE (mm)                 | 3.216         | 3.527               | 4.961          | 2.981 |
| CC                       | 0.875         | 0.843               | 0.773          | 0.897 |
| $G, R > 0$               | 91.81%        | 91.23%              | 92.41%         | 91.94%|
| $G > 0; R = 0$           | 3.12%         | 4.29%               | 1.83%          | 3.38% |
| $G = 0; R > 0$           | 5.07%         | 4.48%               | 5.76%          | 4.68% |
spatiotemporal resolution QPE to improve spatial representations of precipitation. Radar-derived QPE is utilized as the primary precipitation source in regions where radar coverage is deemed as adequate. Gauge observations, precipitation climatologies, and NWP short-term QPFs are seamlessly blended with the radar-based QPEs to mitigate the challenges of overshooting precipitation, significant beam blockages, and poor radar network densities. The MRMS Mountain Mapper QPE is utilized in stratiform rain only in regions of complex terrain, while HRRRv2 1-h QPFs are incorporated everywhere else as radar gap-filling solutions. An updated MRMS RQI product influences the coverage of adequate radar data. Surface and atmospheric conditions, topography, gauge locations, and precipitation values determined how each precipitation source is weighted within the MSQPE scheme.

MSQPE consistently improved upon the radar-based QPE in terms of statistical measures and the proportion of \( G, R \) comparisons depicting accurate precipitation coverages. The MSQPE technique generally had improved evaluation results over all the input precipitation sources, and when the MSQPE was not statistically the best product, the differences between it and the best ranked input precipitation product was mostly negligible. The two detailed case evaluations presented demonstrated how the MSQPE scheme can adequately fill radar coverage gaps where precipitation was not detected due to significant beam blockage or poor coverage; moreover, underestimation biases from radar overshooting precipitation features were also mitigated.

The skill of the MSQPE scheme was only as good as the quality and availability of its input sources. The LGC radar QPE was generally the superior input precipitation coverage.

**TABLE 11.** As in Table 9, but for the focused domain bounded by the northwest corner 46.0°N, 76.0°W and the southeast corner 41.0°N, 68.0°W of the 12–13 Feb 2019 event.

|                     | LGC radar QPE | MSQPE |
|---------------------|---------------|-------|
| MBR                 | 0.771         | 0.922 |
| ME (mm)             | -5.855        | -1.987|
| MAE (mm)            | 7.361         | 5.412 |
| CC                  | 0.471         | 0.504 |
| \( G, R > 0 \)      | 100.00%       | 100.00%|
| **G > 0; R = 0**    | 0.00%         | 0.00% |
| **G = 0; R > 0**    | 0.00%         | 0.00% |
source where adequate radar and gauge observations were present. Improved observational densities and data quality would inherently advance the quality of QPE, which is demonstrated by the skill of the LGC radar QPE between the western CONUS domain and the more data rich eastern CONUS domain. The HRRRv2 1-h QPFs were shown to have adequate skill in portraying observed precipitation to successfully assist in filling radar coverage gaps. Some overall statistical measures of model-derived QPF appear to have exceeded that of MRMS LGC radar QPE and Mountain Mapper QPE; however, larger standard deviations in these statistical measures were also present based on large variations of QPF biases. Operational advancements to the HRRR model would improve the gap-filling precipitation in areas where HRRR QPFs would be the primary gap-filling source. A gauge-based bias correction of NWP QPFs is under consideration to improve MSQPE skill in the gap-filling regions.

The satellite-derived QPE (i.e., SCaMPR) considered for this study had significant challenges in spatially detecting precipitation and providing accurate

![Figure 22](image_url)  
**Fig. 22.** As in Fig. 18, but for the New England area ending at the following times: (a),(d) 2100 UTC 12 Feb 2019, (b),(e) 0300 UTC 13 Feb 2019, and (c),(f) 0900 UTC 13 Feb 2019. This focused domain is bounded by the northwest corner 46.0°N, 76.0°W and the southeast corner 41.0°N, 68.0°W.

![Figure 23](image_url)  
**Fig. 23.** As in Fig. 19, but for the same 1-h time periods denoted in Fig. 22.
precipitation magnitudes. Other satellite-derived QPEs have improved precipitation detection and accuracy; however, they generally lack the short-term data latency required for real-time use or an appropriate spatial resolution to properly capture precipitation gradients. Flexibility within the MSQPE code allows for a future implementation of the MSQPE algorithm with a satellite-derived QPE component when satellite QPE performance metrics are deemed satisfactory for use. There are current efforts across the research community to improve satellite-derived QPE using the latest GOES satellites.

Continuous evaluations of the products can result in future refinements to the algorithm in order to best meet the needs of operational end-users. Research efforts to develop the MSQPE scheme in future MRMS domains over Alaska, Hawaii, the Caribbean, and Guam are also ongoing. The MSQPE scheme for these non-CONUS regions will begin with the foundational logic presented in this study and later modified to handle the unique precipitation regimes, data coverage challenges, and the availability of various observations and NWP forecasts for each future MRMS domain.

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