Comparative Study of Bit Error Rate in LDPC Based OFDM System over AWGN Channels
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Abstract— Modern communication systems are increasingly adopting new modern technologies like OFDM and LDPC for achieving high performance, low Bit Error Rate (BER) and high capacity. The OFDM communication is very much inspired from the channel frequencies over the network. In such a network some kind of orthogonal distortion occurs over the channel called Inter Carrier Interference.

Keywords— OFDM Techniques, Bit Error Rate, LDPC code, Inter Channel Interference, QAM Modulation, TDMA Techniques.

I. INTRODUCTION

In this chapter, we firstly review some important technologies that contribute to the modern digital communication system. These techniques, including the Orthogonal Frequency Division Multiplexing (OFDM) modulation and Low Density Parity Check (LDPC) code, will be the main topic of the dissertation. Following the problem statement, dissertation objective is introduced. Finally, the outline of the dissertation will be given.

OFDM represents a different system design approach. It can be thought of as a combination of modulation and multiple access schemes that segment a communication channel in such a way that many users can share it. Whereas TDMA segments are according to time and CDMA segments are according to spreading codes, OFDM segments are according to frequency. It is a technique that divides the spectrum into a number of equally spaced tones and carries a portion of a user’s information on each tone. A tone can be thought of as a frequency, much in the same way that each key on a piano represents a unique frequency. OFDM can be viewed as a form of frequency division multiplexing (FDM), however, OFDM has an important special property that each tone is orthogonal with every other tone. FDM typically requires there to be frequency guard bands between the frequencies so that they do not interfere with each other. OFDM allows the spectrum of each tone to overlap, and because they are orthogonal, they do not interfere with each other. By allowing the tones to overlap, the overall amount of spectrum required is reduced.

II. OFDM SYSTEM DESIGN

The design of an OFDM system requires a tradeoff between various parameters as like in all communication system design. Usually, the input parameters to the design are the bit rate, available bandwidth and the maximum delay spread introduced by the channel. The design involves calculation of symbol duration, guard time, number of sub-carriers and the modulation and coding schemes among others.
2.1 OFDM System Design

In this section, we consider a typical design problem with the following requirements.

- Bit Rate : 20Mbps
- Maximum Delay Spread : 200ns
- Available Bandwidth : 15MHz

2.2 Guard Time

From the design considerations discussed previously, we see that a guard time of 4*200ns = 800ns is a reasonable choice.

2.3 Modulation and Coding

To transmit 20Mbps data, the number of bits to be transmitted in an OFDM symbol is = 20Mbps*4.8μs = 96 bits/OFDM symbol. Now, we can go for

- 16-QAM with rate (1/2) coding for each sub-carrier so that there are 2 bits per symbol per sub carrier. Thus we see that 48 sub-carriers are required in this case.
- QPSK with rate (3/4) coding for each sub-carrier so that there are 1.5 bits per symbol per sub carrier. Thus in this case, we need 64 sub carriers.

But in the latter case, 64 sub-carriers require a bandwidth of 64 * 250 KHz = 16 MHz which is greater than the available bandwidth of 15MHz. Hence the first one is a good choice in the sense that it satisfies the constraints.

III. LDPC Codes

LDPC codes were originally introduced by Gallager in his doctoral dissertation [9]. Since the discovery of turbo codes in 1993 by Berrou and the rediscovery of LDPC codes by Mackay and Neal in 1995 [10], there has been renewed interest in turbo codes and LDPC codes because their bit error rate performance approaches asymptotically the Shannon limit [4]. Much research is devoted to characterizing the performance of LDPC codes and designing codes that have good performance. Commonly, a graph, the Tanner graph, is associated with the code and an important parameter affecting the performance of the code is the girth of its Tanner graph. The Tanner graph is a special type of graph, a bipartite graph, where the nodes divide into two disjoint classes with edges only between nodes in the two different classes.

IV. Simulations and Results

4.1 OFDM Spectrum

Orthogonal Frequency Division Multiplexing method has been used for spectrum generation. The main reason of using OFDM spectrum is that it distributes the data over large number of carriers that are spaced apart at different precise frequencies.

4.2 AWGN Channel

ADDITIVE WHITE GAUSSIAN noise (AWGN) channel is a universal channel model for analyzing modulation schemes. In this model, the channel does nothing but add a white Gaussian noise to the signal passing through it. This implies that the channel’s amplitude frequency response is flat (thus with unlimited or infinite bandwidth) and phase frequency response is linear for all frequencies so that modulated signal pass through it without any amplitude loss and phase distortion of frequency components.

4.3 BER Vs SNR of the LDPC Based OFDM system in AWGN channel Using QAM

Using MATLAB Figure2 shows the BER Vs SNR of the LDPC Based OFDM system in AWGN channel using QAM modulation scheme. This figure shows the relationship between BER and SNR. The values of SNR are from – 30 db to 0 db and the scale of SNR is linear. The values of BER are from 0.1 to 0.5 and scale of BER is log.
| S. No. | SNR      | BER  |
|-------|----------|------|
| 1     | -30 db   | 0.4767 |
| 2     | -25 db   | 0.4566 |
| 3     | -20 db   | 0.4221 |
| 4     | -15 db   | 0.3649 |
| 5     | -10 db   | 0.2672 |
| 6     | -5 db    | 0.1128 |
| 7     | 0 db     | 0.0   |

BER Vs SNR of LDPC based OFDM system in AWGN channel using 2QAM

![BER Vs SNR of the LDPC Based OFDM system in AWGN channel using 2QAM](image)

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