The ALMaQUEST Survey. VII. Star Formation Scaling Relations of Green Valley Galaxies

Lihwai Lin1, Sara L. Ellison2, Hsi-An Pan3,4, Mallory D. Thorp2, Po-Chieh Yu5, Francesco Belfiore6, Bau-Ching Hsieh1, Roberto Maiolino7,8, S. Ramya9, Sebastián F. Sánchez10, and Yung-Chau Su1,11

1 Institute of Astronomy & Astrophysics, Academia Sinica, Taipei 10617, Taiwan; lihwailin@asiaa.sinica.edu.tw
2 Department of Physics & Astronomy, University of Victoria, Finneroy Road, Victoria, British Columbia, V8P 1A1, Canada
3 Max-Planck-Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany
4 Department of Physics, Tamkang University, No.151, Yingzhuang Rd., Tamsui Dist., New Taipei City 251301, Taiwan
5 College of General Studies, Yuan-Ze University, Taoyuan 32003, Taiwan
6 INAF—Osservatorio Astrofisico di Arcetri, Largo E. Fermi 5, I-50157 Firenze, Italy
7 Cavendish Laboratory, University of Cambridge, 19 J.J. Thomson Avenue, Cambridge CB3 0HE, UK
8 University of Cambridge, Kavl Institute for Cosmology, Cambridge, CB3 0HE, UK
9 Indian Institute of Astrophysics, II Block, Koramangala, Bengaluru 560 034, India
10 Instituto de Astronomía, Universidad Nacional Autónoma de México, Circuito Exterior, Ciudad Universitaria, Ciudad de México 04510, Mexico
11 Department of Physics, National Taiwan University, 10617, Taipei, Taiwan

Received 2021 May 19; revised 2022 January 12; accepted 2022 January 13; published 2022 February 23

Abstract

We utilize the ALMA-MaNGA QUEnch and STar formation (ALMaQUEST) survey to investigate the kpc-scale scaling relations, presented as the resolved star-forming MS (rSFMS: $\Sigma_{\text{SFR}}$ versus $\Sigma_{H_2}$), the resolved Schmidt–Kennicutt relation (rSK: $\Sigma_{\text{SFR}}$ versus $\Sigma_{H_2}$), and the resolved molecular gas MS (rMGMS: $\Sigma_{H_2}$ versus $\Sigma_{H_2}$), for 11,478 star-forming and 1414 retired spaxels (oversampled by a factor of $\sim 20$) located in 22 GV and 12 MS galaxies. For a given galaxy type (MS or GV), the retired spaxels are found to be offset from the sequences formed by the star-forming spaxels on the rSFMS, rSK, and rMGMS planes, toward lower absolute values of sSFR, SFE, and $f_{H_2}$ by $\sim 1.1$, 0.6, and 0.5 dex. The scaling relations for GV galaxies are found to be distinct from that of the MS galaxies, even if the analyses are restricted to the star-forming spaxels only. It is found that, for star-forming spaxels, sSFR, SFE, and $f_{H_2}$ in GV galaxies are reduced by $\sim 0.36$, 0.14, and 0.21 dex, respectively, compared to those in MS galaxies. Therefore, the suppressed sSFR/SFE/$f_{H_2}$ in GV galaxies is associated with not only an increased proportion of retired regions in GV galaxies but also a depletion of these quantities in star-forming regions. Finally, the reduction of SFE and $f_{H_2}$ in GV galaxies relative to MS galaxies is seen in both bulge and disk regions (albeit with larger uncertainties), suggesting that, statistically, quenching in the GV population may persist from the inner to the outer regions.

Unified Astronomy Thesaurus concepts: Galaxies (573)

Supporting material: animation

1. Introduction

One of the central keys in probing galaxy evolution lies in the understanding of how the star formation in galaxies is regulated, triggered, and suppressed. All of these processes are closely linked to the amount of the molecular gas that is available to fuel star formation, conventionally parameterized by the gas fraction, and the physical conditions of the gas that determine whether the gas is able to collapse to form stars, represented by the star formation efficiency (e.g., Wong & Blitz 2002; Bigiel et al. 2008; Sargent et al. 2014; Saintonge et al. 2017; Tacconi et al. 2018; Sánchez 2020).

With the advent of Integral Field Unit surveys and high spatial resolution radio/mm observations, the connection between star formation, stellar properties, and molecular gas contents have been explored recently at (sub)kpc scales with statistical samples (e.g., Lin et al. 2019b; Ellison et al. 2020a, 2020b; Barerra-Ballesteros et al. 2020; Brownson et al. 2020; Morselli et al. 2020; Sánchez 2020; Ellison et al. 2021a, 2021b; Pessa et al. 2021; Sánchez et al. 2021). Using 14 galaxies from the ALMA-MaNGA QUEnch and STar formation (ALMaQUEST) survey (Lin et al. 2020), Lin et al. (2019b) established the scaling relations among the star formation rate surface density ($\Sigma_{\text{SFR}}$), stellar mass surface density ($\Sigma_*$), and $H_2$ mass surface density ($\Sigma_{H_2}$) for star-forming spaxels of MS galaxies on kpc scales. The three variables are found to form a 3D linear (in log) relation with associated scatter. As a result, each pair of these quantities displays a tight sequence, dubbed the resolved star-forming MS (rSFMS: $\Sigma_{\text{SFR}}$ versus $\Sigma_*$), the resolved Schmidt–Kennicutt relation (rSK: $\Sigma_{\text{SFR}}$ versus $\Sigma_{H_2}$), and the resolved molecular gas MS (rMGMS: $\Sigma_{H_2}$ versus $\Sigma_{H_2}$). Similar results have also been obtained with a larger set of ALMaQUEST galaxies (Ellison et al. 2020b), EDGES-CALIFA (Sánchez 2020; Sánchez et al. 2021), PHANGS (Pessa et al. 2021), and other nearby galaxies (Morselli et al. 2020). These works have led to several interesting findings. For instance, the kpc-scale relations are found to resemble the global relations, implying that the global scaling relations could be originated from local processes at subgalactic scales (Sánchez et al. 2013; Wuyts et al. 2013; Cano-Díaz et al. 2016; Abdurro’uf & Akiyama 2017; Hsieh et al. 2017; Pan et al. 2018a; Lin et al. 2019b; Cano-Díaz et al. 2019; Vulcani et al. 2019; Enia et al. 2020; Sánchez 2020). Studies of the scatters, correlation coefficients, and galaxy-to-galaxy variation, as well as the covariance of the these scaling
relations, suggest that rSFMS (and hence the global SFMS) could simply be a consequence of the combination of rSK and rMGMS (Lin et al. 2019b; Morselli et al. 2020; Ellison et al. 2021a; Baker et al. 2022; Pessa et al. 2021). Moreover, Ellison et al. (2021a) find significant correlations between the scaling relations and properties such as Sérsic index and total stellar mass. On the other hand, Sánchez et al. (2021) explore the correlations between the residuals of the three scaling relations in the EDGE-CALIFA sample and find that the scatter of the 3D scaling relation is dominated by the measurement errors and hence does not have a physical origin. Other explanations also include the hydrostatic midplane pressure being the primary driver in regulating local star formation, given its strong correlation with \( \Sigma_{\text{SFR}} \) (Barrera-Ballesteros et al. 2020).

Despite the detailed characterization of star-forming spaxels in the aforementioned studies, most previous work has focused on galaxies that are still actively forming stars (i.e., past studies have restricted themselves to star-forming spaxels in star-forming galaxies). Whether the resolved scaling relations still hold or not in galaxies departing from the MS, such as the green valley (GV) or quiescent populations, is less explored. Furthermore, it is also less clear how the non-star-forming spaxels behave, particularly for the quenched or “retired” regions where the star formation has already ceased or is largely suppressed. The “retired” regions are conventionally identified as those having H\( \alpha \) EW \(< 3 \) A (Stasinska et al. 2008; Cid Fernandes et al. 2010; Sánchez et al. 2014; Ellison et al. 2021b). Under this definition, they are often referred to areas whose emission lines are primarily photoionized by aging stellar populations rather than newly formed stars, even though they could actually have just as much star formation as some spaxels in regions with fewer old stars present to add ionization. Ellison et al. (2021b) undertook a first initiative to investigate the molecular gas fraction in the retired spaxels, using eight of the ALMaQUEST galaxies, and found that, in a given galaxy, the retired spaxels form an rMGMS sequence that is several times lower compared to that of the star-forming spaxels, indicating lower gas fractions in retired regions. The distinction between gas fractions in star-forming and retired spaxels is seen even within a given galaxy.

The ratios of the two variables in the rSFMS, rSK, and rMGMS represent the three normalized quantities, the specific star formation rate \( \text{sSFR} = \Sigma_{\text{SFR}} / \Sigma_{\text{BH}} \), star formation efficiency \( \text{SFE} = \Sigma_{\text{SFR}} / \Sigma_{\text{BH}} \), and molecular gas fraction \( f_{\text{H}_2} = \Sigma_{\text{H}_2} / \Sigma_{\text{BH}} \), respectively. As the rate of forming stars depends on both the amount of molecular gas and the efficiency of converting molecular gas into stars such that \( \text{sSFR} = \text{SFE} \times f_{\text{H}_2} \), characterizing the scaling relations in retired areas or quenched galaxies can shed light on the relative contributions between SFE and \( f_{\text{H}_2} \) to sSFR in quenching star formation. With the \( ^{12}\text{CO}(1-0) \) observations obtained from the Atacama Large Millimeter Array (ALMA) of three Mapping Nearby Galaxies at Apache Point Observatory (MaNGA; Bundy et al. 2015) selected GV galaxies, Lin et al. (2017) reported a stronger depletion in \( f_{\text{H}_2} \) in the bulges compared to the disk regions of GV galaxies (also see Sánchez et al. 2018; Brownson et al. 2020), consistent with an inside-out quenching scenario (Belfiore et al. 2018; Ellison et al. 2018; Lin et al. 2019a). However, a larger sample is required in order to confirm the trend.

In this work, we extend the study of the star formation scaling relation carried out by Lin et al. (2019b), which was based on well-selected star-forming spaxels of the MS population, to retired regions, as well as comparing scaling relations of GV galaxies with MS galaxies in the ALMaQUEST sample. We aim at characterizing and comparing the scaling relations between different types of spaxels (retired versus star-forming) and galaxies (MS versus GV) in order to gain a full picture of the connection between star formation and gas properties at kpc scales. In addition, we also quantify the suppression of SFE and \( f_{\text{H}_2} \) in bulges and disks of GV galaxies separately, to investigate whether there is a preferential location within galaxies for the quenching to start.

Throughout this paper, we adopt the following cosmology: \( H_0 = 70 \) km s\(^{-1}\) Mpc\(^{-1}\), \( \Omega_m = 0.3 \) and \( \Omega_L = 0.7 \). We use a Salpeter initial mass function (IMF).

2. Sample and Observations

2.1. The ALMaQUEST Survey

The ALMaQUEST survey (Lin et al. 2020) maps the \( ^{12}\text{CO}(1-0) \) distributions with ALMA for 46 galaxies selected from the MaNGA survey (Bundy et al. 2015; Law et al. 2015; Wake et al. 2017). The sample consists of galaxies with a wide range of specific star formation rates (sSFR), including starburst (SB), MS, and GV galaxies. The ALMA observations were carried out with a spatial resolution that is matched to the point-spread function (~2.5") of MaNGA, enabling a joint study of stellar and gas properties at the same physical scales (corresponding to a physical scale of 0.9–6 kpc). The details of the sample characteristics and data reduction are given in the ALMaQUEST survey paper (Lin et al. 2020). In this work, the \( H_2 \) mass surface density, \( \Sigma_{\text{H}_2} \), is computed from the CO luminosity by adopting a constant conversion factor \( (\alpha_{\text{CO}}) \) of 4.35 \( M_\odot \) (K km s\(^{-1}\) pc\(^2\))\(^{-1}\) (e.g., Bolatto et al. 2013).

We can first compare the ALMaQUEST sample with other spatially resolved IFS and molecular gas observations in nearby galaxies. For example, the PHANGS-MUSE survey (PI: E. Schinnerer; E. Emsellem et al. 2022, in preparation) offers resolved observations with >10 times better spatial resolution, down to 50–100 pc for 19 star-forming disk galaxies selected from the PHANGS-ALMA survey (Leroy et al. 2021). However, the PHANGS-MUSE survey only targets galaxies on the star formation MS, and therefore does not sample galaxies going through the quenching phase (e.g., GV) such as those included in the ALMaQUEST survey. On the other hand, the EDGE-CALIFA survey (Bolatto et al. 2017) consists of a larger size of sample (126 galaxies) with resolved CO observations selected from the CALIFA (Sánchez et al. 2012) survey with a typical physical resolution of ~1.4 kpc. Although EDGE-CALIFA contains galaxies over a wide range in environment, morphological type, and star formation rate, the primary component of the survey is also the MS population. Only a handful of galaxies below the MS with CO detections are included in the sample. Therefore, the ALMaQUEST complements the existing spatially resolved CO data sets by adding a couple of tens more galaxies in the GV as well as central starbursts (Ellison et al. 2020a; Lin et al. 2020).

The MaNGA data cubes utilized in this work are taken directly from the MaNGA DR15 PIPE3D (Sánchez et al. 2016b, 2016) value-added products (Sánchez et al. 2018), including the global properties, which are integrated over the MaNGA bundle field-of-view, and the spaxel-based measurements of \( \Sigma_{\text{BH}} \) and emission-line fluxes. By using the Balmer...
decrement computed at each spaxel and a Milky Way extinction curve with $R_v=3.1$ (Cardelli et al. 1989), we correct the dust extinction of the emission line fluxes. The extinction-corrected H$\alpha$ flux is converted to the SFR following the method given by Kennicutt (1998) with a Salpeter IMF. $\Sigma_{s}$ and $\Sigma_{SFR}$ are then computed using the stellar mass and SFR derived for each spaxel, normalized to the physical area of one spaxel with an inclination correction. We note that, for a given spaxel, in principle there are mixed contributions from both the newly formed stars and old stellar populations to the H$\alpha$ emission line whereas the latter dominates the retired spaxels. Without performing a sophisticated decomposition (e.g., Smirnova-Pinchukova et al. 2021) to distinguish the ionization contributions, the underlying assumption in this work is that the H$\alpha$ emission in the star-forming spaxels is purely from active star formation. On the other hand, since the H$\alpha$ emission in the retired regions is mostly powered by evolved stars rather than new star formation, the SFR estimated using the H$\alpha$ to SFR conversion serves only as an upper limit for retired spaxels (Sarzi et al. 2010; Yan & Blanton 2012; Singh et al. 2013; Belfiore et al. 2017; Hsieh et al. 2017; Cano-Díaz et al. 2019; Ellison et al. 2021b).


### 2.2. Sample Selection and Spaxel Classification

Traditionally, “GV” was defined as the sparse region located between the blue cloud and red sequence in the color–magnitude diagram (e.g., Martin et al. 2007; Wyder et al. 2007). It was later found that, depending on the color combination (e.g., UV versus optical), the selected GV galaxies may or may not trace well the populations that are in the transitional phase from the star-forming to the quiescent populations (Salim 2014; Nyiriensgipjumna et al. 2021). Therefore, alternative methods, such as the location on the SFR versus $M_*$ plane (Belfiore et al. 2018; Jian et al. 2020, 2022), sSFR (Lin et al. 2017; Starkenburg et al. 2019), and D4000 break (Anthopolo et al. 2017; Starkenburg et al. 2019), have been adopted, in addition to the conventional color selections (Martin et al. 2007; Schiminovich et al. 2007; Wyder et al. 2007; Salim 2014; Schawinski et al. 2014). The term “GV” has now been widely used to refer to the transitioning galaxies in terms of their star formation activities. As our primary goal is to compare the difference between galaxies experiencing quenching with respect to the typical star-forming galaxies, we first exclude 12 ALMaQUEST galaxies that were explicitly selected due to their starbursting nature (Ellison et al. 2020a) from our analysis. For the remaining 34 galaxies, we group them with an sSFR threshold of $10^{-10.5}$ yr$^{-1}$, above and below which correspond to the MS (12 galaxies) and GV (22 galaxies) samples, respectively. As described in Lin et al. (2020), all the ALMaQUEST galaxies are detected in CO. In other words, the GV galaxies used throughout this work are CO-detected galaxies with sSFR below the typical MS galaxies, and hence represent transitioning objects.

For the purpose of selecting star-forming spaxels, we first limit our analyses to spaxels having signal-to-noise (S/N) $> 3$ for the H$\alpha$ and H$\beta$ lines and S/N $> 2$ for the [O III] and [N II] lines. We then classify each MaNGA spaxel into regions where the dominant ionizing source is star formation, composite, or AGN using the BPT diagnostic based on the [O III]/H$\beta$ versus [N II]/H$\alpha$ line ratios (Kewley et al. 2001, 2006). Equation (3) of Cid Fernandes et al. (2010) is then applied to further separate the AGN regions into Seyfert and LI(N)ER regions. We identify star-forming spaxels to be those satisfying both BPT classified star-forming criteria and the H$\alpha$ equivalent width (EW) $> 6$ Å cut. The retired spaxels are identified as those having H$\alpha$ EW $< 3$ Å and S/N $> 3$ in H$\alpha$. In addition to the aforementioned selection criteria, we also restrict our subsequent analyses to galaxies having S/N $> 3$ in the CO line and $\Sigma_\alpha > 10^{-1.1} (M_\odot \text{ kpc}^{-2})$. Even though the PIPE3D stellar products only contain spaxels with continuum S/N $> 3$, our $\Sigma_\alpha$ cut helps further remove spaxels with anomalously small values in the stellar mass surface density. These selections lead to the final 6122 (5356) and 108 (1306) star-forming and retired spaxels in MS (GV) galaxies used in this study, respectively. We note that, while the cut in the CO enables the study of the scaling relations in the three-parameter ($\Sigma_{SFR}$, $\Sigma_\alpha$, and $\Sigma_{H\alpha}$) space, by selection, we will miss retired spaxels that are below the CO detection threshold. We will discuss the potential impact in relevant selections (Sections 3.1.1 and 3.1.3).

Since the H$\alpha$ EW is the ratio of the line flux (partly if not entirely due to star formation) to the stellar continuum flux, which approximately scales with stellar mass, it is anticipated that the H$\alpha$ EW is a good proxy of sSFR (e.g., see Belfiore et al. 2018). In Figure 1, we show the spaxel distribution of the 34 galaxies used in this study on the $\Sigma_{SFR}$ versus $\Sigma_\alpha$ plane, with the color scaled with the H$\alpha$ EW. It can be seen that both the distributions of sSFR (bearing in mind that sSFR is the ratio between $\Sigma_{SFR}$ and $\Sigma_\alpha$) and H$\alpha$ EW are continuous, decreasing

---

**Figure 1.** Distribution of the 34 ALMaQUEST galaxies on a spaxel-by-spaxel basis in the $\Sigma_{SFR}$ and $\Sigma_\alpha$ plane, with the colorscale varying according to the H$\alpha$ EW in log. The upper left and lower right red contours represent the distributions for spaxels classified as star-forming and retired regions, respectively.

---

[12] Lin et al. (2019a) applied a more stringent selection of retired spaxels to be those satisfying both the BPT LI(N)ER criteria and the H$\alpha$ EW $< 3$ Å cut, in order to ensure that the emissions are primarily photoionized by the old stellar populations. However, this leads to very few retired spaxels in MS galaxies, given a small size of the ALMaQUEST MS sample. To increase the number of retired spaxels in MS galaxies, we release the LI(N)ER constraint in this work. Nevertheless, we note that the results and conclusions presented in Section 3 remain very similar even if we follow the selection as done in Lin et al. (2019a) by imposing the LI(N)ER cut on top of the H$\alpha$ EW cut.
from the upper-left toward the lower-right region on this diagram. In other words, there is a fairly good correspondence between Hα EW and SFR. The two red contours show the distributions of the star-forming spaxels (upper left contours) and the retired spaxels (lower right contours) identified using the criteria described. Our selections of star-forming and retired spaxels indeed represent the regions with high and low sSFR, respectively.

2.3. Bulge and Disk Decomposition

As one of our science goals is to compare \( f_{\text{BH}} \) and SFE between the bulge and disk regions, we follow a similar procedure as described in Lin et al. (2017) to separate the bulge and disk regions for the galaxies used in this work. The two-component fitting is achieved using GALFIT Peng et al. (2002, 2010) on the SDSS \( r \)-band images. We fit the Sérsic index to \( n = 1 \) for the disk component and treat the Sérsic index of the bulge component as a free parameter.\(^{13}\) As the two-component fitting is sensitive to the initial conditions, the determination of the sky level, and the dust obscuration of the images, sometimes the best fit may yield unrealistic solutions—for example, unphysically large bulge size. As one can see from the SDSS images shown in Figure 2, the majority of our targets are disk-dominated with a small bulge. To ensure that our measurements of the bulge regions are not contaminated by those in the disks, we take a rather conservative approach by imposing an upper limit of the intrinsic bulge size to be \( 2'' \) in radius,\(^{14}\) corresponding to \( \sim 1.2 \) kpc at the typical redshift (\( z \sim 0.03 \)) of our sample. Once we obtain the effective radius \( (R_e) \) of the bulge, we compute the observed effective radius \( (R_e^{\text{obs}}) \) by convolving it with the PSF size of both MaNGA and ALMA beams (\( \sim 2''/5 \)). We then define the “bulge” region to be \( r < R_e^{\text{obs}} \). The SDSS \( gri \) composite images with bulge regions overlaid of the 34 ALMaQUEST galaxies used in this work are shown in Figure 2. We visually checked the derived bulge sizes. We find that the enclosed areas provide a reasonable representation of the bulge regions. Varying the upper limit of the intrinsic bulge size between \( 1''/25 \) to \( 4'' \) does not significantly impact any of our conclusions. Although the upper limit of the intrinsic bulge size is checked by eye, in order to mitigate the impact of this choice and/or potential contamination from any overlap region between the bulge and disk, we also define the “disk” region to be \( r > 2 \times R_e^{\text{obs}} \) (denoted by the green circles in Figure 2) when performing subsequent analyses that compare the properties between the bulge and disk regions.

Among the 34 galaxies used in this sample, seven galaxies potentially host a photometric bar based on visual inspections. Previous works have suggested that the presence of a bar could induce gas inflow, trigger a starburst, and finally lead to the quench of its host (e.g., Alonso-Herrero & Knapen 2001; Hunt et al. 2008; Ellison et al. 2011; Carles et al. 2016; Géron et al. 2021). Therefore, it is possible that the properties of a bar could be distinct from the disk regions and contaminate our results. We find that roughly half of the bars (4/7) in our sample can be classified as retired regions while the other half (3/7) are consistent with composite spaxels. However, as mentioned above, we have imposed an \( r > 2 \times R_e^{\text{obs}} \) criterion for the selection of disk regions, which alleviates the concern that the contribution from the bars could dominate the results in the disk component.

3. Results

3.1. Scaling Relations in Star-forming and Retired Spaxels between MS and GV Galaxies

Figure 3 shows the spaxel distributions (individual points) for all spaxels detected in CO and Hα with \( S/N > 3 \) and \( \Sigma_s > 10^{4.1} M_\odot \) in the \( \Sigma_s-\Sigma_{\text{SFR}}-\Sigma_{\text{H}_2} \) 3D space for spaxels in both MS (blue symbols) and GV (green symbols) galaxies. Their projections on the rSFMS, rSK, and rMGMS for MS (blue colors) and GV (green colors) galaxies are also shown as contours. It can be seen that, although the spaxels of GV galaxies in general also form sequences in the rSFMS, rSK, and rMGMS 2D planes, they exhibit a clear offset from the MS galaxies, hinting that there is fundamental difference between MS and GV in terms of their sSFR, SFE, and \( f_{\text{BH}} \). While part of this result is somewhat expected, since the GV galaxies by design are selected to be those with lower global sSFR, the deficit in SFE and \( f_{\text{BH}} \) for GV galaxies suggests that both effects contribute to the low sSFR of GV.

For each galaxy, we compute the fractions of spaxels classified as star-forming or retired. The number of galaxies with a given fraction of star-forming and retired spaxels is shown in the upper and lower panels of Figure 4, respectively. Compared to MS galaxies (shown as blue bars), GV galaxies (shown as green bars) tend to have a lower fraction of star-forming spaxels and a higher fraction of retired spaxels. One central question is therefore to understand whether the low sSFR of GV galaxies is driven by purely the lower fraction of star-forming spaxels or a global reduction of SFE and \( f_{\text{BH}} \), in all different types of spaxels. In order to address this question, in the following subsections we discuss the three scaling relations for star-forming and retired spaxels, separately for MS and GV galaxies. We fit each of the subsamples using the orthogonal distance regression (ODR) fitting method with a power law parameterized as the following:

\[
\log_{10} \frac{\Sigma_{\text{SFR}}}{M_\odot \text{yr}^{-1} \text{kpc}^{-2}} = a \times \log_{10} \frac{\Sigma_s}{10^8 M_\odot} + b \quad (1)
\]

\[
\log_{10} \frac{\Sigma_{\text{SFR}}}{M_\odot \text{yr}^{-1} \text{kpc}^{-2}} = a \times \log_{10} \frac{\Sigma_{\text{H}_2}}{10^8 M_\odot} + b \quad (2)
\]

\[
\log_{10} \frac{\Sigma_{\text{H}_2}}{M_\odot \text{kpc}^{-2}} = a \times \log_{10} \frac{\Sigma_s}{10^8 M_\odot} + b, \quad (3)
\]

where \( a \) and \( b \) denote the slope and the normalization of the scaling relations in log, respectively. The obtained best-fit parameters (\( a \) and \( b \)) for various subsamples presented in Section 3.1.1—Section 3.1.3 are listed in Table 1. It is worth noting that the measurements of each spaxel are not fully independent, though, since the size of spaxel (\( 0''/5 \)) is oversampled by a factor of \( \sim 20 \) with respect to the PSF size (\( \sim 2''/5 \)). However, the types of the analyses presented in this work are found to be robust against the binning resolution (e.g., see Ellison et al. 2021a). On the other hand, the uncertainty of the fits could be underestimated due to the oversampling. To account for this effect, we take a rather conservative approach. We multiply the derived uncertainty of the fits by a factor of

\(^{13}\) On the other hand, the Sérsic index was fixed to \( n = 4 \) for the bulge component in the work of Lin et al. (2017).

\(^{14}\) The typical SDSS seeing (FWHM) is \( \sim 2''/5 \), and therefore a 2'' bulge (in radius) is resolved, but not much.
square root of the oversampled factor, assuming that the oversampled data points are highly correlated. The reported uncertainties in subsequent sections and Table 1 therefore serve as a conservative estimate.

3.1.1. The Resolved Star-forming Main Sequence Relation (rSFMS)

We first compare the rSFMS between star-forming and retired spaxels for MS and GV galaxies separately. Figure 5 shows the rSFMS of star-forming spaxels (left panels) and retired spaxels (right panels) for MS (top panels) and GV (bottom panels) galaxies. The blue dashed line represents the rSFMS derived from star-forming spaxels in main-sequence galaxies (i.e., a fit to the points in the top left panel) and is the same reference line shown in all panels to guide the eyes. The derived slope for the star-forming spaxels of the MS galaxies is 1.11, in good agreement with previous results using the ALMaQUEST sample, despite the sample selection and the S/N ratio cuts in the final spaxels differing slightly in detail (Lin et al. 2019b; Ellison et al. 2020a). Our result is also in broad agreement with the slopes found in other studies, ranging from 0.6 to 1.3 (Sánchez et al. 2013; Cano-Díaz et al. 2016; González Delgado et al. 2016; Hsieh et al. 2017; Cano-Díaz et al. 2019; Erroz-Ferrer et al. 2019; Enia et al. 2020; Morselli et al. 2020; Sánchez et al. 2021).

Figure 2. The SDSS gri composite images of the 34 ALMaQUEST galaxies used in this work. The magenta hexagons denote the MaNGA footprints. The white circle marks the outer boundary of the areas identified as a bulge region while the green circle denotes the inner boundary of the disk component. The MaNGA plate identifier is shown in white in the upper left corner of each panel.
The solid lines are the best fit of the data points in a given panel (blue: star-forming spaxels; red: retired spaxels). The retired spaxels in either MS or GV galaxies are both found to lie below the MS rSFMS curve, offset by nearly one order of magnitude. One thing to note is that, as we mentioned earlier, the MS galaxies are dominated by the star-forming spaxels and hence the number of retired spaxels used here is very limited. A larger sample would be beneficial to better characterize various properties of the retired spaxels in the MS galaxies.

The slope of the retired sequence is also found to be close to unity, consistent with other resolved studies (Hsieh et al. 2017; Cano-Díaz et al. 2019). The lower values of $\Sigma_{\text{SFR}}$ (or H$\alpha$ flux) at a given $\Sigma_*$ in retired spaxels were previously known as the “LI(N)ER” or retired sequence (Hsieh et al. 2017; Cano-Díaz et al. 2019), in which the H$\alpha$ emissions were attributed to contributions primarily from evolved stars rather than new star formation (Sarzi et al. 2010; Yan & Blanton 2012; Singh et al. 2013; Belfiore et al. 2017). As we mentioned earlier, the H$\alpha$-based SFR for retired spaxels is therefore considered to be an upper limit (e.g., Cano-Díaz et al. 2019). As a result, the actual difference in $\Sigma_{\text{SFR}}$ between star-forming and retired spaxels at a given $\Sigma_*$ could be even greater than what we see here. Also as mentioned in Section 2.2, our selection of retired spaxels does not contain regions without CO detections, i.e., regions not forming stars at all due to the lack of cold molecular gas. If included, they would further enlarge the difference in $\Sigma_{\text{SFR}}$ between star-forming and retired spaxels at a given $M_*$.

Another crucial feature revealed in Figure 5 is that the $\Sigma_{\text{SFR}}$ of star-forming spaxels in GV galaxies is also found to be lower than that in MS galaxies at a given $\Sigma_*$, suggesting that the star formation in GV galaxies is suppressed even in regions classified as star-forming. The difference in the derived slopes and the normalizations between MS and GV are greater than 6$\sigma$ (see Table 1). Our result therefore indicates that the depletion in the sSFR of GV galaxies may appear to be a global phenomenon within the galaxies, not restricted to certain areas. This is consistent with some of the recent complementary works that studied the SFR radial profile of GV galaxies and found a global reduction with respect to MS galaxies at all radii (e.g., Belfiore et al. 2018; Ellison et al. 2018; Brownson et al. 2020).

3.1.2. The Resolved Schmidt–Kennicutt Relation (rSK)

Figure 6 compares the rSK relation of star-forming and retired spaxels for both MS and GV galaxies. It is evident that the retired spaxels of either MS or GV galaxies tend to lie below the rSK relation formed by the MS star-forming spaxels —in other words, at lower SFE. When comparing the star-forming spaxels between MS and GV galaxies (the upper left and lower left panel, respectively), we find that the GV star-forming spaxels also deviate from the MS rSK curve toward a lower $\Sigma_{\text{SFR}}$ at a given $\Sigma_\text{H}_2$. The best fit of the slope ($a = 0.81 \pm 0.05$) and the normalization ($b = -2.13 \pm 0.02$) of star-forming spaxels in GV galaxies is found to be at least 4$\sigma$ away from that ($a = 1.02 \pm 0.03$; $b = -1.94 \pm 0.01$) in MS galaxies. In other words, the efficiency of converting the molecular gas into stars in the GV galaxies is suppressed not only in retired but also in star-forming spaxels. This is in good agreement with a previous finding that the deviation of rSK from the ensemble relation strongly correlates with the global sSFR (Ellison et al. 2021a).
of retired spaxels is systematically lower by a factor of \( \sim 5 \) than that of star-forming spaxels. Similarly, a depletion of \( f_{\text{H}_2} \) of retired spaxels is systematically lower by a factor of \( \sim 5 \) than that of star-forming spaxels. Similarly, a depletion of \( f_{\text{H}_2} \) is also found in central AGN regions relative to the star-forming regions in EDGE-CALIFA (Ellison et al. 2021c). Here, we take a step further to investigate the variation of molecular gas fraction by separating the galaxies into MS and GV categories with a larger ALMaQUEST sample. Figure 7 is analogous to Figures 5 and 6 but for the rMGMS relation. Similarly, the retired spaxels of either MS or GV galaxies occupy the regions below the reference relation formed by the MS star-forming spaxels, hinting at a lower gas fraction in the retired regions, as previously reported by Ellison et al. (2021b). As mentioned in Section 2.2, our retired spaxels do not include those falling below the CO S/N cut, which would lie further below from the rMGMS reported here—in other words, an even lower gas fraction.

Meanwhile, the star-forming spaxels of GV galaxies are also found to lie below the reference line (i.e., the rMGMS of star-forming spaxels in MS galaxies). While the slopes between the GV star-forming spaxels and the MS star-forming spaxels are both close to unity (0.97 ± 0.04 versus 1.06 ± 0.04), there is an 8σ difference in the normalization (6.66 ± 0.01 versus 6.82 ± 0.02). Our finding is consistent with a complementary analysis performed by Ellison et al. (2021a), who found a dependence of the offset from the median rMGMS relation on the global sSFR.

3.1.4. Distributions of sSFR, SFE, and \( f_{\text{H}_2} \)

Having inspected the distributions of star-forming and retired spaxels for both MS and GV galaxies on the rSFMS, rSK, and rMGMS planes, we then compare the ratios of the parameters of these relations, i.e., the sSFR, SFE, and \( f_{\text{H}_2} \), in star-forming and retired spaxels to better quantify the differences. Figure 8 shows the distribution of spaxel-based sSFR (left panels), SFE (middle panels), and \( f_{\text{H}_2} \) (right panels) for star-forming (blue) and retired (red) regions. The upper and lower three panels are spaxels belonging to the MS and GV galaxies, respectively. The purple dotted line represents the median value for the star-forming spaxels in MS galaxies as a reference line, and is the same between the corresponding upper and lower panels. The median values of the associated histograms, \( m \), are reported in each panel. In both GV and MS galaxies, the retired spaxels show values lower than those of star-forming spaxels by \( \sim 1.1, 0.6, \) and 0.5 dex in sSFR, SFE, \( f_{\text{H}_2} \), respectively. Bearing in mind that the SFE and sSFR estimates in retired regions are conservative upper limits, the actual offsets could be even larger. Our results therefore suggest that the deficit in the sSFR of retired regions relative to the star-forming regions can be attributed to not only the reduction in the gas fraction as reported by Ellison et al. (2021b) but also the reduced SFE.

An important feature clearly seen from Figure 8 is that the star-forming spaxels in GV galaxies also exhibit lower sSFR, SFE, and \( f_{\text{H}_2} \) compared to the star-forming spaxels in MS galaxies by 0.36, 0.14, and 0.21 dex, respectively. We perform a Kolmogorov–Smirnov test (KS test) to further examine whether the distributions in the above quantities of star-forming spaxels in the MS galaxies relative to that in the GV population are significant or not. The resulting \( p \)-values are 0.0, 3.94e-177, and 1.87e-273 for sSFR, SFE, and \( f_{\text{H}_2} \), respectively. These tiny \( p \)-values rule out the null hypothesis that the two samples (star-forming spaxels of MS galaxies versus star-forming spaxels of GV galaxies) can be drawn from the same population. In other words, the gas properties and hereby the star formation rates in GVs are different from MS galaxies not only because there are

![Figure 4](image_url)

**Figure 4.** Number of galaxies as a function of the percentage of star-forming (upper panel) and retired (lower panel) spaxels. MS galaxies are shown in blue whereas GV galaxies are shown in green.

### 3.1.3. The Resolved Molecular Gas Main Sequence Relation (rMGMS)

The relationship between \( \Sigma_{\text{H}_2} \) and \( \Sigma_* \) at (sub)kpc scales has been investigated recently to gain insight into the role of molecular gas abundance in shaping galaxy properties (e.g., Wong et al. 2013; Lin et al. 2019b; Barrera-Ballesteros et al. 2020; Morselli et al. 2020; Ellison et al. 2021a; Pessa et al. 2021; Sánchez et al. 2021). It was found that these two quantities for star-forming regions in nearby galaxies form a very tight relation, dubbed the rMGMS (e.g., Lin et al. 2019b). Recently, Ellison et al. (2021b) extended the study of rMGMS to retired spaxels by using eight ALMaQUEST galaxies and showed that \( f_{\text{H}_2} \) of retired spaxels is systematically lower by a factor of \( \sim 5 \) than that of star-forming spaxels. Similarly, a depletion of \( f_{\text{H}_2} \) is also found in central AGN regions relative to the sector.
Table 1
Best-fit Parameters ($a$ and $b$) for the Three Resolved Scaling Relations (see Equations (1)–(3)) Using the Orthogonal Distance Regression (ODR) Fitting Method

| Subsample             | $a$ (rSFMS) | $b$ (rSFMS) | $a$ (rSK)  | $b$ (rSK)  | $a$ (rMGMS) | $b$ (rMGMS) | Number of spaxels |
|-----------------------|-------------|-------------|------------|------------|-------------|-------------|------------------|
| SF spaxels in MS     | 1.11 ± 0.06 | −2.13 ± 0.03| 1.02 ± 0.03| −1.94 ± 0.01| 1.06 ± 0.04 | 6.82 ± 0.02  | 6122             |
| SF spaxels in GV     | 0.75 ± 0.05 | −2.40 ± 0.02| 0.81 ± 0.05| −2.13 ± 0.02| 0.97 ± 0.04 | 6.66 ± 0.01  | 5356             |
| Retired spaxels in MS| 1.07 ± 0.32 | −3.29 ± 0.35| 1.20 ± 0.43| −2.65 ± 0.22| 0.92 ± 0.23 | 6.45 ± 0.26  | 108              |
| Retired spaxels in GV| 1.25 ± 0.11 | −3.71 ± 0.11| 1.80 ± 0.22| −2.76 ± 0.08| 0.73 ± 0.09 | 6.44 ± 0.09  | 1306             |

Figure 5. Number densities of star-forming (left panels; blue scales) and retired (right panels; red scales) spaxels on the rSFMS plane for MS (top panels) and GV (bottom panels) galaxies. The solid lines represent the best fit of the data points (blue for star-forming spaxels and red for retired spaxels) shown in each panel. The best-fit parameters are listed in Table 1. The blue dashed lines are the same reference lines in each panel, corresponding to the best fit of the rSFMS derived for the star-forming spaxels in MS galaxies (i.e., a fit to the spaxels in the top left panel).
fractionally more quenched areas in GVs but also because the gas contents are also different in the star-forming regions between GV and MS populations.

3.2. SFE and $f_{H_2}$ in the Disk and Bulge Regions of GV Galaxies

Having studied the scaling relations and the offset in sSFR/SFE/$f_{H_2}$ of GV galaxies relative to the MS galaxies, we now turn to the investigation of the dependence of SFE and $f_{H_2}$ on the location within galaxies. For each of the ALMaQUEST MS and GV galaxies, we measure the median values of spaxel-based sSFR, SFE, and $f_{H_2}$ in the bulge and disk regions separately. Since the “bulge” region defined in this analysis refers to the inner region enclosed by a certain radius (either the effective radius of the bulge or a given upper limit; see Section 2), it is important to keep in mind that we may not be able to remove the disk contribution in the inner regions. Another thing to note is that, although the ALMaQUEST target selection does not impose a morphology criterion, the majority of our sample tends to have a small bulge. Therefore, we are

---

**Figure 6.** Number densities of star-forming (left panels; blue scales) and retired (right panels; red scales) spaxels on the rSK plane for MS (top panels) and GV (bottom panels) galaxies. The solid lines represent the best fit of the data points (blue for star-forming spaxels and red for retired spaxels) shown in each panel. The best-fit parameters are listed in Table 1. The blue dashed lines are the same reference lines in each panel, corresponding to the best fit of the rSK derived for the star-forming spaxels in MS galaxies (i.e., a fit to the spaxels in the top left panel).
not able to investigate in detail how the star formation and/or gas properties of galaxies depend on the presence of bulges, as explored in Koyama et al. (2019). With these caveats in mind, we only focus on the comparison of the sSFR, SFE, and $f_{H_2}$ between the MS and GV populations for a given structural component, instead of attempting to discuss the impact of the bulge on these quantities.

Figure 9 compares the median spaxel values of sSFR (left panel), SFE (middle panel), and $f_{H_2}$ (right panel) of the bulge (light circles) and disk (dark triangles) regions between MS (blue colors) and GV (red colors) galaxies. As bulges tend to have larger values of $\Sigma_*$ compared to the disks, and therefore may occupy distinct regions in terms of the $\Sigma_*$ range, we plot sSFR, SFE, and $f_{H_2}$ as a function of $\Sigma_*$ in Figure 9 for the clarity of the data points. Visually, it is clear from the left panel that there is an apparent sSFR offset between the MS and GV galaxies, either in the disk or in the bulge regions. In other words, while the averaged lower global sSFR of GV compared to MS galaxies is by design, what we show here is that the depleted sSFR is present in both the bulge and disk regions. To
quantify the amount of sSFR depletion, we bootstrap the measurement of the sSFR separately for the bulge and disk components of MS and GV galaxies, each with 10,000 iterations. We find that the sSFR in GV galaxies is reduced by \(0.61\pm0.10\) dex and \(0.65\pm0.16\) dex in the disk and bulge regions, respectively, compared to that in MS galaxies. While the relative offset seems comparable between the bulges and disks, it is worth noting that, in both MS and GV galaxies, the absolute sSFR values in the bulges are smaller than those in the corresponding disks. In other words, both MS and GV galaxies possess older stellar populations in the central regions compared to the outer parts of galaxies.

The middle panel of Figure 9 shows that the values of SFE for GV galaxies are systematically lower than those of the MS galaxies, either in the disk or bulge regions. By repeating the bootstrapping, we find that the median values of \(\log_{10}(\text{SFE yr}^{-1})\) in the disks are \(-8.99\pm0.05\) and \(-9.34\pm0.06\) for MS and GV, respectively. On the other hand, the medians of \(\log_{10}(\text{SFE yr}^{-1})\) in the bulge components are found to be \(-9.13\pm0.06\) and \(-9.55\pm0.08\) for MS and GV, respectively. In other words, GV galaxies show a reduction of SFE in the disk and bulge with respect to the MS galaxies by \(0.35\pm0.08\) dex and \(0.42\pm0.10\) dex, respectively. This trend suggests that the depleted SFE we see in Section 3.1 is a global feature, persisting from the inner to the outer regions.

In the right panel of Figure 9, we plot the median \(f_{H_2}\) of the bulge and disk regions, separately, for MS and GV galaxies.

Again, we determine the median values of \(f_{H_2}\) through the bootstrapping analysis. The medians (in log) in the disks are found to be \(-1.20\pm0.05\) and \(-1.45\pm0.04\) for MS and GV, respectively, whereas in the bulges the median values of \(f_{H_2}\) (in log) are determined to be \(-1.38\pm0.09\) and \(-1.71\pm0.12\) for MS and GV, respectively. This leads to an \(f_{H_2}\) depletion in GV relative to MS by a factor of \(0.25\pm0.06\) dex and \(0.34\pm0.16\) in the disk and bulges, respectively. The reduced \(f_{H_2}\) in the bulge regions of GV relative to MS, however, is only significant at a 2\(\sigma\) level. We then additionally run a KS test comparing the \(f_{H_2}\) distributions of the bulge component between MS and GV galaxies and obtain a \(p\)-value of 0.16. The non-negligible \(p\)-value, together with the 2\(\sigma\) significance in the \(f_{H_2}\) offset between MS and GV, indicates that the difference in \(f_{H_2}\) of bulge is only marginal, likely due to the small statistics.

In summary, we find a trend similar to that reported in Lin et al. (2017) and Brownson et al. (2020), namely that, statistically, GV galaxies exhibit lower \(f_{H_2}\) and SFE across the entire galaxy compared to that of MS galaxies, and both low \(f_{H_2}\) and SFE contribute to the sSFR suppression in either the disk or the bulge region of GV galaxies. The reduction of \(f_{H_2}\) in the GV bulges, however, awaits confirmation with a larger sample in the future.

The correlation between SFE and \(f_{H_2}\) has been studied not only using global quantities (Pan et al. 2018b; Dou et al. 2021) but also at kpc scales (Ellison et al. 2020a; Brownson et al. 2020). Next,
we investigate whether or not the two quantities, $f_{\text{HI}}$ and SFE, are correlated with each other in our sample. In Figure 10, we present the relation between $f_{\text{HI}}$ and SFE on a galaxy-by-galaxy basis, separately for MS (blue symbols) and GV (red symbols). Triangles and circles denote the disk and bulge regions, respectively. The Pearson correlation coefficient ($r_p$) and Spearman correlation coefficient ($\rho$) are found to be 0.10 and 0.24 between SFE and $f_{\text{HI}}$, respectively, indicating that there is no correlation between the strength of these two quantities. We also note that there are several cases that show high $f_{\text{HI}}$ but low SFE, representing galaxies where the molecular gas is still present but unable to form stars efficiently. Overall, the larger scatter in the SFE versus $f_{\text{HI}}$ relation suggests that the relative contributions between the SFE and $f_{\text{HI}}$ in lowering the sSFR in GV galaxies vary from case to case.

4. Summary and Discussion

In this work, we present the kpc-scale scaling relations of the rSFMS, rSK, and rMGMS for 12 main-sequence (MS) and 22 GV galaxies drawn from the ALMaQUEST survey in order to investigate the distributions of sSFR, SFE, and $f_{\text{HI}}$. For each of the two categories of galaxies (i.e., MS and GV), we identify in total $\sim$11,500 star-forming and $\sim$1400 retired regions on a spaxel-by-spaxel basis. Our main findings are:

1. The distribution of spaxels of GV galaxies in the three-dimensional space formed by the $\Sigma_{\text{SFR}}$, $\Sigma_{\text{S}}$, and $\Sigma_{\text{HI}}$, is offset from that in MS galaxies (Figure 3). The fraction of star-forming (retired) spaxels decreases (increases) from MS to GV galaxies (Figure 4).

2. The retired spaxels form different sequences from the star-forming spaxels in both GV and MS galaxies on each of the three relations: rSFMS (Figure 5), rSK (Figure 6), and rMGMS (Figure 7). More specifically, for a given $\Sigma_{\text{S}}$, retired spaxels show lower $\Sigma_{\text{SFR}}$ and lower $\Sigma_{\text{HI}}$ than star-forming spaxels. For a given $\Sigma_{\text{HI}}$, retired spaxels show lower $\Sigma_{\text{SFR}}$ compared to star-forming spaxels. In turn, the sSFR, SFE, and $f_{\text{HI}}$ of retired spaxels are found to be lower than those of star-forming spaxels by $\sim$1.1, 0.6, and 0.5 dex, respectively (Figure 8).

3. Compared to the star-forming spaxels in MS galaxies, the star-forming spaxels in GV galaxies show lower values of $\Sigma_{\text{SFR}}$ and $\Sigma_{\text{HI}}$ for a given $\Sigma_{\text{S}}$ and show lower $\Sigma_{\text{SFR}}$ for a given $\Sigma_{\text{HI}}$ (Figures 5—7). More quantitatively, the sSFR, SFE, and $f_{\text{HI}}$ of star-forming spaxels in GV galaxies show a reduction by 0.36, 0.14, and 0.21 dex, respectively, when compared with those of star-forming spaxels in MS galaxies (Figure 8). The Kolmogorov—Smirnov test indicates that the sSFR (as well as SFE or $f_{\text{HI}}$) between the star-forming spaxels in MS and GV populations are not drawn from the same distribution.

4. When separating a galaxy into bulge and disk regions, we find that SFE is depleted by 0.42±0.10 (0.35±0.08) dex whereas $f_{\text{HI}}$ is lowered by 0.34±0.16 (0.25±0.06) in the bulge (disk) regions of GV galaxies with respect to those of the MS galaxies. This result suggests that SFE and $f_{\text{HI}}$ can be suppressed in both the inner and outer regions of GV galaxies with respect to the MS galaxies. The significance of the result on the $f_{\text{HI}}$ suppression in the bulge GV relative to the MS galaxies, however, is only marginal, and a larger sample would be required to robustly quantify the reduction of $f_{\text{HI}}$.

The lower SFE and $f_{\text{HI}}$ of retired spaxels compared to star-forming spaxels suggest that the cessation of star formation in retired regions is caused by processes that not only reduce $f_{\text{HI}}$ but also affect SFE. On the other hand, it is quite intriguing that GV galaxies exhibit lower sSFR, SFE, and $f_{\text{HI}}$ than MS galaxies even for star-forming spaxels. This suggests that the overall suppressed star formation in GV galaxies with respect to that in MS galaxies is not only associated with the increased fraction of non-star-forming spaxels as illustrated in Figure 4, but is also related to a globally suppressed sSFR in star-forming regions. This is in line with some previous IFS studies that show a suppressed SFR at all radii for galaxies below the MS (Belfiore et al. 2018; Ellison et al. 2018; Medling et al. 2018; Sánchez et al. 2018; Wang et al. 2019). In a forthcoming paper (H.-A. Pan et al. 2022, in preparation), we will examine the radial distribution of the star formation and gas properties in detail for the entire ALMaQUEST sample.

In this work, we confirm the picture established in Lin et al. (2017) that, as galaxies move away from the MS toward the
quenched state, both the SFE and $f_{\text{HI}}$ tend to decrease in the disk and bulge regions. Using a sample 10 times larger, we are further able to better quantify the effects of SFE and $f_{\text{HI}}$ in both disk and bulge areas. The relatively lower $f_{\text{HI}}$ and SFE found in the central regions of galaxies is in agreement with recent studies (Lin et al. 2017; Sánchez et al. 2018; Brownson et al. 2020; Ellison et al. 2021b), which favor an inside-out quenching scenario (e.g., Lin et al. 2019a). Several processes, including turbulence, magnetic fields, AGN feedback, and the so-called “morphological quenching” may provide pathways to suppress SFE in galaxies (Martig et al. 2009; Fabian 2012; Federrath & Klessen 2012). Not all of them, however, are able to explain the reduced (central) gas fractions at the same time. Among various quenching processes, the most plausible mechanism that is able to account for the depleted gas fraction and SFE is the AGN feedback, which may be able to not only to expel gas away from the central regions, but also to inject the turbulence to suppress star formation (Morganti 2017; Sánchez et al. 2018; García-Burillo et al. 2021). Indeed, Ellison et al. (2021c) have recently demonstrated low central molecular gas fractions in the central regions of AGN host galaxies. Alternatively, it is possible that there may be two types of processes that operate together, one affecting SFE, one removing the gas. Our current analyses on the data, however, are not able to disentangle whether the reduced SFE and $f_{\text{HI}}$ share a common source or not, in particular because there is a lack of correlation between SFE and $f_{\text{HI}}$ (Figure 10).

Many global studies of molecular gas contents have investigated the dependence of the distance from the star-forming MS on the gas fraction or SFE (e.g., Huang & Kauffmann 2014; Scoville et al. 2016; Bolatto et al. 2017; Saintonge et al. 2017; Tacconi et al. 2018; Colombo et al. 2020; Lin et al. 2020; Piotrowska et al. 2020). While the relative importance between the gas supply and star formation efficiency is still controversial, depending on the choice of the gas tracer and the range of the star formation rate sampled (e.g., within or outside the SFMS), it becomes clear that both the gas fraction and SFE contribute to the change in sSFR to a certain level. Recent resolved studies have also attempted to address this issue by associating the local sSFR with SFE and $f_{\text{HI}}$ at (sub)kpc scales (Lin et al. 2017; Ellison et al. 2020b; Brownson et al. 2020; Morselli et al. 2020). Similarly, it is found that both SFE and $f_{\text{HI}}$ play roles in regulating the star formation rate above and below the rSFMS, but the relative contributions depend on the properties of host galaxies as well as nature of cold gas. For example, Ellison et al. (2020b) studied the gas content for well-selected star-forming spaxels from the ALMaQUEST galaxies and concluded that SFE is the primary driver determining the scatter of the rSFMS, with $f_{\text{HI}}$ playing a secondary role. When analyzing several GV galaxies, Lin et al. (2017) and Brownson et al. (2020) found that the suppressed star formation in GV galaxies can be attributed to both the deficit in SFE and $f_{\text{HI}}$ in either inner or outer regions. On the other hand, when including the atomic gas, Morselli et al. (2020) found that the total gas fraction has a stronger effect than SFE on the distance from the rSFMS. In this work, we triple the sample size of GV galaxies used in previous studies (Lin et al. 2017; Brownson et al. 2020) and find that, statistically, the lower SFE in GV galaxies plays a role comparable to that of the lower $f_{\text{HI}}$ in reducing the sSFR in GV galaxies. Our results suggest that the suppressed star formation in GV galaxies does not always require a strong depletion in molecular gas. This is in line with some previous global studies that found that SFE is correlated with sSFR or the distance from the MS in the low sSFR regime (i.e., transitioning and retired galaxies) (e.g., Colombo et al. 2020; Lin et al. 2020).

In fact, there are a handful of cases in our sample where the gas fraction is comparable to that of MS but with very low SFE, resulting in low sSFR. One piece of important information currently missing in the current work is the content of dense molecular gas, which is a direct fuel of star formation. In a future paper (L. Lin et al. 2022 in preparation), we will report the properties of the dense molecular gas in GV galaxies, to elucidate whether the low SFE is caused by a lack of dense gas (such as HCN or HCO+) or not.

We thank the anonymous referee for providing helpful comments that greatly improved the quality of this work. We would also like to thank C. A. López-Cobá for providing a list of barred galaxies used in this work. This work is supported by the Academia Sinica under the Career Development Award CDA-107-M03 and the Ministry of Science & Technology of Taiwan under the grant MOST 108-2628-M-001-001-MY3. R.M. acknowledges the ERC Advanced Grant 695671 “QUENCH” and support by the Science and Technology Facilities Council (STFC).

The authors would like to thank the staffs of the East Asia and North America ALMA ARCs for their support and continuous efforts in helping produce high-quality data products. This paper makes use of the following ALMA data: ADS/ALMA##2015.1.01225.S, ADS/ALMA##2017.1.01093.S, and ADS/ALMA##2018.1.00541.S, and ADS/ ALMA##2018.1.00558.S. ALMA is a partnership of ESO (representing its member states), NSF (USA) and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI (Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/ NRAO, and NAOJ.

Funding for the Sloan Digital Sky Survey IV has been provided by the Alfred P. Sloan Foundation, the U.S. Department of Energy Office of Science, and the Participating Institutions, SDSS-IV acknowledges support and resources from the Center for High-Performance Computing at the University of Utah. The SDSS website is www.sdss.org. SDSS-IV is managed by the Astrophysical Research Consortium for the Participating Institutions of the SDSS Collaboration including the Brazilian Participation Group, the Carnegie Institution for Science, Carnegie Mellon University, the Chilean Participation Group, the French Participation Group, Harvard-Smithsonian Center for Astrophysics, Instituto de Astrofisica de Canarias, The Johns Hopkins University, Kavli Institute for the Physics and Mathematics of the Universe (IPMU)/University of Tokyo, Lawrence Berkeley National Laboratory, Leibniz Institut für Astrophysik Potsdam (AIP), Max-Planck-Institut für Astronomie (MPIA Heidelberg), Max-Planck-Institut für Astrophysik (MPA Garching), Max-Planck-Institut für Extraterrestrische Physik (MPE), National Astronomical Observatory of China, New Mexico State University, New York University, University of Notre Dame, Observatário Nacional/MCTI, The Ohio State University, Pennsylvania State University, Shanghai Astronomical Observatory, United Kingdom Participation Group, Universidad Nacional Autónoma de México, University of Arizona, University of Colorado Boulder, University of Oxford, University of Portsmouth,
