Slingshot non-sequential double ionization as a gate to anti-correlated two electron escape

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Non-sequential double ionization (NSDI) in strong infrared laser fields is a fundamental process accounted for by the three-step model[1]. First, one electron tunnel-ionizes in the field-lowered Coulomb-barrier and then accelerates in the laser field. This electron can return back to the core to re-collide and transfer energy to a bound electron through different pathways. In the direct one, the energy transferred suffices for both electrons to ionize shortly after re-collision. In the delayed pathway the energy transferred ionizes one of the two electrons shortly after re-collision. The other electron transitions to an excited state and ionizes later. It is generally accepted that re-collision-induced excitation with subsequent field ionization (RESI)[7, 9] prevails the delayed mechanism. In RESI, the excited electron ionizes at the field extremum, after re-collision, assisted by the laser field. In the double delayed pathway, both electrons ionize later following the energy transferred during re-collision.

At intensities below the recollision threshold, in NSDI two electrons escaping opposite to each other along the laser-field direction—anti-correlated escape—has been studied intensely by experiment and theory alike. This pattern was found to prevail, but not substantially, over correlated two-electron escape. It was observed in NSDI of several atoms driven by intense (strongly-driven) long duration pulses[24–28]. Multiple re-collisions, in the context of RESI, were put forth to explain anti-correlated two-electron escape[24–28]. Electron-electron repulsion was also suggested as a possible explanation[30, 31].

Here, we show that RESI does not necessarily prevail the delayed pathway, for strongly-driven He at 400 nm. We find a competing mechanism in the delayed pathway where the electron that ionizes later undergoes a slingshot motion due to the Coulomb interaction with the nucleus and the field. This Coulomb slingshot motion is similar to the well known gravitational slingshot that alters the motion of a spacecraft around a planet. Moreover, we find that the electron undergoing a slingshot motion ionizes around the second extremum of the laser field after re-collision. We label this mechanism slingshot-NSDI. The nucleus has a small effect on RESI. In contrast, in slingshot-NSDI the nucleus plays a decisive role with anti-correlated two-electron escape being its striking hallmark. Slingshot-NSDI is an alternative to the multiple re-collisions mechanism for explaining anti-correlated two-electron escape.

We demonstrate slingshot-NSDI in He driven by a near-single-cycle laser pulse at $5 \times 10^{14}$ W/cm$^2$ and 400 nm. Further below, we discuss slingshot-NSDI for other laser intensities and pulse durations as well. Kinetically complete experiments that employ carrier envelope phase (CEP)-controlled near-single-cycle pulses have been carried out for NSDI over a wide range of intensities[24–31]. The intensity of $5 \times 10^{14}$ W/cm$^2$ is below the recollision threshold. This corresponds to the maximum energy of the electron returning to the core, $3.17 \frac{E^2_0}{(4\omega^2)}$, which is equal to 23.7 eV at $5 \times 10^{14}$ W/cm$^2$, being equal to the energy needed to transition to the first excited state of the ion; $E_0$ and $\omega$ are the strength and frequency of the field.

We employ a three-dimensional (3D) semi-classical model[32–37]. One electron (re-colliding) tunnel-ionizes through the field-lowered Coulomb-barrier. We use the quantum mechanical Ammosov-Delone-Krainov (ADK) formula to compute the tunnel-ionization rate[35, 36]. The exit point of the re-colliding electron is along the laser-field direction and is computed using parabolic coordinates[40]. The electron momentum is taken to be equal to zero along the laser field while the transverse one is given by a Gaussian distribution[38, 39]. The initially bound electron is described by a microcanonical distribution[41].
We use a laser field of the form
\[
\tilde{E}(t) = E_0 \exp \left( -2 \ln 2 \left( \frac{t}{\tau} \right)^2 \right) \cos (\omega t + \varphi) \hat{z},
\]
where \( \varphi \) is the CEP, and \( \tau = 2 \) fs is the full-width-half-maximum of the pulse duration in intensity. We employ atomic units, unless otherwise stated. The tunnel-ionization time, \( t_0 \), is selected randomly in the time interval \([-2\tau, 2\tau]\). Once the initial conditions are specified at time \( t_0 \), the position and momentum of each electron are propagated classically in time. We do so using the three-body Hamiltonian of the two electrons with the nucleus kept fixed. All Coulomb forces and the interaction of each electron with the laser field are fully accounted for with no approximation. We also account for the Coulomb singularity by using regularized coordinates. Our results for NSDI are obtained by taking into account CEPs that range from \( \varphi = 0^\circ \) to \( \varphi = 330^\circ \) in steps of 30° and by averaging over these CEPs.

We identify the main pathways of energy transfer in each double ionization (DI) event. To do so, we compute the time difference between the re-collision time \( t_{\text{rec}} \) and the ionization time of each electron. We compare it with the time interval \( t_{\text{diff}} \) where the electron pair potential energy undergoes a sharp change due to re-collision. We find \( t_{\text{diff}} \) to be roughly equal to 1/8 laser cycle (T). We refer to the electron that, after re-collision, ionizes first as electron 1, and the one ionizing last as electron 2. For each classical trajectory, the re-collision time is defined as the time of minimum approach of the two electrons. It is identified by the maximum in the electron pair potential energy. The ionization time for each electron, \( t_i \), is defined as the time when the compensated energy \( (p_{x,i}^2 + p_{y,i}^2 + (p_{z,i} - A(t))^2)/2 - Z/r_i \) becomes positive and remains positive thereafter, with \( i = 1, 2 \) and \( p_i = p_{x,i} \hat{x} + p_{y,i} \hat{y} + p_{z,i} \hat{z}; A(t) \) is the vector potential and \( Z = 2 \). We list the conditions for direct, delayed or double delayed DI event in Table I. In the delayed pathway, the probability for electron 2 to be the re-colliding electron increases with decreasing intensity.

\[
\Delta t_1 = t_1 - t_{\text{rec}} \quad \text{&} \quad \Delta t_2 = t_2 - t_{\text{rec}}
\]

| \( \Delta t_2 < t_{\text{diff}} \) | \( \Delta t_1 < t_{\text{diff}} \) | \( \Delta t_1 > t_{\text{diff}} \) | \( \Delta t_2 > t_{\text{diff}} \) |
|---|---|---|---|
| \( t_1 < t_2 \) | \( \Delta t_2 > t_{\text{diff}} \) | \( \Delta t_2 > t_{\text{diff}} \) | \( \Delta t_2 > t_{\text{diff}} \) |

TABLE I. Conditions for energy transfer DI pathways.

At intensities above-the-recollision threshold the direct pathway dominates. The two electrons escape mostly in the same direction along the laser field, with the final momentum of each electron being roughly equal to \(-A(t_{\text{rec}})\).

At intensities well below-the-recollision threshold the delayed and double delayed pathways prevail. This is the case for He driven by a near-single-cycle laser pulse at \(5 \times 10^{14} \) W/cm² and 400 nm. We find that the two electrons escape overwhelmingly in opposite directions, see Fig. 1. In the double delayed pathway the two electrons escape with small momenta, see Fig. 1(b), whereas in the delayed pathway the momenta are larger (Fig. 1(c)). To understand the anti-correlation pattern, we focus on the delayed pathway and its contributing mechanisms.

In the delayed pathway, electron 1 escapes with momentum roughly equal to \(-A(t_{1} \approx t_{\text{rec}})\) which is mostly large, since re-collision occurs around a zero of the field. In RESI, electron 2 ionizes at a time \( t_2 \) around an extremum of the field. It does so primarily due to the laser field, and, thus, has a small final momentum, \(-A(t_2)\), along the \( \hat{z} \)-axis, see Fig. 1(c). In the new mechanism, which we refer to as slingshot-NSDI, the final momentum of electron 2 is determined both by the Coulomb field and the laser field and it has mostly large magnitude, see Fig. 1(c). Moreover, unlike RESI, in slingshot-NSDI the two electrons escape only in opposite directions.

Next, we describe slingshot-NSDI using a representative delayed pathway event for \( \varphi = 0^\circ \) that encapsulates the main features of the new mechanism. Below, the description of slingshot-NSDI and RESI applies to all CEPs where the re-colliding electron tunnel-ionizes from a minimum of the laser field. A similar description applies to CEPs where tunnel-ionization occurs from a maximum of the field. The difference is that some of the quantities plotted in Fig. 2 would be reflected with respect to the time axis. For simplicity, in Fig. 2 we focus on the times after re-collision. Electron 1 (green line) ionizes in the time interval \([0, 0.5]T\) with a positive momentum, mostly large as for all delayed events.

In slingshot-NSDI, electron 2 (black line) initially moves away from the nucleus along the \(+\hat{z}\)-axis. However, it soon returns and undergoes a close encounter with the nucleus at time \( t_{2}^{\text{ret}} \), see \( r_{z,2} \) as a function of time in Fig. 2(a1), where \( r_{z,2} \) is the \( z \)-component of the position vector \( \mathbf{r}_2 \). Indeed, \( r_{z,2} \) has a very small negative value at time \( t_{2}^{\text{ret}} \). This return of electron 2 to the nucleus leads to a slingshot motion in the time interval \( t_{2}^{\text{ret}} \) to \( t_{2} \), denoted by black arrows in Fig. 2(a1-a3). During this motion electron 2 remains close to the nucleus due to the comparable magnitude of the attractive Coulomb force.
FIG. 2. Slingshot-NSDI at 5×10^{14} W/cm^2 (a) and RESI at 7×10^{14} W/cm^2 (b) for He driven by a near-single-cycle pulse at 400 nm. Plotted as a function of time are (1) \( r_{z,1} \) and \( r_{z,2} \) (2) \( p_{z,2} \) and \( \Delta p_{z,2} \) (3) \( F^E p_{z,2} \) and \( F^E \Delta p_{z,2} \). CS is enclosed by an up and down black arrow, which represent \( p_{z,2} \) being along the +\( \hat{z} \)-axis and -\( \hat{z} \)-axis, respectively, at the start and end of CS. The beginning of the time axis is \( t_{\text{rec}} \).

and the force of the laser field. Moreover, in Coulomb slingshot (CS), the momentum of electron 2 changes significantly. It has a large positive value at \( t_{\text{ret},2} \), which has the same sign as the final momentum of electron 1, to a large negative value at the time electron 2 ionizes, \( t_2 \), see red line in Fig. 2(a2). Hence, CS results in electron 2 escaping opposite to electron 1 along the laser field. The effect of the nucleus has previously been addressed in the context of strongly-driven clusters [44].

For most slingshot-NSDI events electron 2 ionizes around the second extremum of the field in the time interval \([0.75, 1.25]T\). To explain why this is the case, we employ the energy of electron 2. Shortly after re-collision, at time \( t_{\text{init}} = t_{\text{rec}} + t_\text{diff} \), the repulsive force between the two electrons is significantly smaller than during re-collision. Hence, after this time, the energy of electron 2 changes due to the work done mainly by the field as follows:

\[
H(t) = \frac{p_{z,2}(t_{\text{init}})^2}{2} - \frac{Z}{r_{z,2}(t_{\text{init}})} + \int_{t_{\text{init}}}^{t} F^E p_{z,2} \, dt',
\]

where \( F^E(t) = -\mathcal{E}(t) \) is the force from the laser field and \( F^E p_{z,2} \) is the rate of change of the energy of electron 2. During CS, the close encounter of electron 2 with the nucleus at \( t_{\text{ret},2} \) takes place past a zero of the laser field. At this time both the momentum of electron 2 and the force from the laser field point along the +\( \hat{z} \)-axis. Roughly half a laser cycle later, in the time interval \([0.75, 1.25]T\), the slingshot motion is concluded with both the momentum of electron 2 and the force of the laser field pointing along the -\( \hat{z} \)-axis. Thus, during CS, \( F^E p_{z,2} \) is mostly positive in the first half cycle \([0.25, 0.75]T\) and the second one \([0.75, 1.25]T\) after re-collision, see red-shaded area in Fig. 2(a3). This is the reason electron 2 gains sufficient energy to ionize around the second extremum of the field after re-collision.

Next, we identify the main reason that the rate of change of the energy of electron 2 is positive during CS. We express the total momentum of electron 2 as the sum of the momentum changes due to the interaction with the nucleus and electron 1, \( \Delta p_{z,2}^C \), and with the laser field, \( \Delta p_{z,2}^E \) as follows:

\[
\begin{align*}
 p_{z,2}(t) &= p_{z,2}(t_0) + \Delta p_{z,2}^C(t_0 \rightarrow t) + \Delta p_{z,2}^E(t_0 \rightarrow t) \\
 \Delta p_{z,2}^C(t) &= \int_{t_0}^{t} \left( -\frac{Z}{|r_{z,2}|} + \frac{r_{z,2} - r_{z,1}}{|r_2 - r_1|^3} \right) \, dt' \\
 \Delta p_{z,2}^E(t) &= A(t) - A(t_0) .
\end{align*}
\]

For delayed events, the repulsive force between the two electrons is roughly zero shortly after re-collision, thus, contributing only a constant term to \( \Delta p_{z,2}^C \). We plot the momentum change due to the nucleus as well as the total momentum of electron 2 in Fig. 2(a2). It is clear that, during CS, the sharp change of the total momentum of electron 2 is mainly due to the term \( \Delta p_{z,2}^C \). Hence, the attractive force of the nucleus causes the main change in the total momentum of electron 2. Combining Eqs (2) and (3), we also plot in Fig. 2(a3) the contribution of the nucleus, \( F^E \Delta p_{z,2}^C \) (blue line), to the rate of change...
of the energy of electron 2, \( F_{\epsilon, p_{z,2}} \) (red line). We find that, during CS, the contribution of the nucleus (blue-shaded area) causes this rate to be mostly positive (red-shaded area). The contribution of the field, \( F_{\epsilon, \Delta p_{z,2}} \) (not shown), is also mostly positive during the last part of CS.

We find that the dominant mechanism of the delayed pathway is slingshot-NSDI at \( 5 \times 10^{14} \) W/cm\(^2\) and RESI at \( 7 \times 10^{14} \) W/cm\(^2\). We illustrate RESI in Fig. 2 b). In contrast to slingshot-NSDI, in RESI the momentum change of electron 2 due to the nucleus is almost a constant after re-collision, see blue line in Fig. 2 b2). Moreover, the strength of the laser field \( F_{\epsilon} \) is larger at the higher intensity. Thus, in the first half cycle, the rate of change of the force from the laser field is larger at a given extremum of the field. Hence, we conjecture that it is possible that, during CS, the contribution of the field to the rate of change of the electron energy of electron 2, \( F_{\epsilon, \Delta p_{z,1}} \). Moreover, a longer pulse allows for a more complicated interaction of electron 2 with the nucleus. This can result in electron 2 escaping in the same or opposite direction from the first electron. The above arguments are consistent with our finding that in the delayed pathway the anti-correlation pattern is more pronounced for shorter compared to longer pulses.

For He driven at 400 nm, two experiments are most relevant to the work presented here [14, 23]. In Ref. [16], excellent agreement was found between experiment and fully ab-initio quantum mechanical calculations for electron energy distributions of doubly ionized He driven by a long duration laser pulse [16]. For the latter observables, using the model described here, we achieved excellent agreement with fully ab-initio quantum mechanical calculations [36]; the latter were performed by the same theoretical group as in Ref. [16]. After submission of the present work, a study of a kinematically complete experiment for He driven by a long duration laser pulse at 400 nm and intensities of \( 3.5-5.7 \times 10^{14} \) W/cm\(^2\) was submitted and published [23]. In this latter work, the correlated electron momenta are obtained. As the intensity increases from \( 3.5 \times 10^{14} \) W/cm\(^2\) to \( 5.7 \times 10^{14} \) W/cm\(^2\), a transition from anti-correlated plus correlated to mostly correlated two-electron escape is observed. We also find such a transition taking place for He driven at 400 nm, as the intensity increases from \( 5 \times 10^{14} \) W/cm\(^2\) to \( 7 \times 10^{14} \) W/cm\(^2\), for 2 fs, 4 fs and 6 fs laser pulses, see [43].

To guide experiments, we identify favorable laser parameters for observing an anti-correlated two-electron escape mostly due to slingshot-NSDI. In the direct pathway the two electrons escape overwhelmingly in the same direction, while in the double delayed they escape mostly in opposite directions along the laser field. Thus, to observe slingshot-NSDI, the contribution to NSDI of the double delayed pathway has to be small. We find that for the currently considered low intensities, the contribution of the double delayed pathway is smaller for the shorter duration laser pulses. We have also shown that, for low intensities, slingshot-NSDI contributes most to the delayed pathway for short pulse durations. Given the above, it is essential that a short pulse duration is employed for observing slingshot-NSDI.

In conclusion, slingshot-NSDI is an important mechanism of the delayed pathway and of NSDI for a range of intensities and pulse durations for He driven at 400 nm. In slingshot-NSDI, following re-collision, the electron that ionizes last undergoes a Coulomb slingshot within roughly half a laser cycle that changes sharply the direction of the electron momentum along the laser field. This electron has a large momentum that points in the same direction as the force from the laser field both at the start and at the end of CS. Hence, during CS the laser field supplies sufficient energy to this electron leading to its ionization around the second extremum of the field. The hallmark of slingshot-NSDI is that the two electrons escape in opposite directions along the laser field. We expect slingshot-NSDI to be a significant mechanism in

![Fig. 3. Contribution of slingshot-NSDI to the delayed pathway as a function of laser intensity in steps of 0.5 x 10^{14} W/cm^2 and of pulse duration in steps of 2 fs.](image-url)
NSDI of He driven at wavelengths other than 400 nm, and to be present in other atoms and molecules.

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