Abstract: We introduce new classes of tubular domains with geometric singularities at infinity. Among the peculiar spectral properties that we observe in respective models, there is the compactness of the resolvent despite the infinite volume of a twisted tube or sheared ribbon and the raise of dimension for the essential spectrum in a ruled strip.