Adv Syst Sci Appl 2017; 4: 22-33
Published online at http://ijassa.ipu.ru/ojs/ijassa/article/view/255

Hybrid PAPR Reduction Scheme for Universal Filter Multi-Carrier Modulation in Next Generation Wireless Systems

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Abstract: Universal filter multi carrier (UFMC) is one of the promising multi carrier modulation techniques for next generation wireless communication systems. UFMC seems to be most attractive because it provides better sub carrier separation like FBMC (Filer Bank Multi Carrier) and less complexity like OFDM (Orthogonal Frequency Division Multiplexing). But this technique suffers from limitation of higher Peak to Average Power Ratio (PAPR). In this paper a Hybrid PAPR reduction technique SC- UFMC have been proposed using SLM (Selective Mapping) and Clipping. The performance of proposed technique is evaluated for various design parameters including filter length, FFT size and Bits per sub carrier. The simulation results show that hybrid technique provides better PAPR reduction as compared with conventional SLM and clipping techniques.

Keywords: UFMC, OFDM, FBMC, PAPR, SLM.

1. INTRODUCTION

Orthogonal Frequency Division Multiplexing (OFDM) is the most popular multi-carrier modulation technique which is being used in 4th generation wireless communication [1]. But in the last few years, the number of users and the demand for higher data rates has increased exponentially so, next generation wireless communication systems must be able to deal with large numbers of users and provide a much higher data transmission rate using less complex systems. In order to serve all these requirements, various new multi carrier modulation techniques like Filter bank Multi carrier (FBMC), Universal Filter Multi Carrier (UFMC) and Generalized Frequency Division Multiplexing (GFDM) have been introduced [2,3].

In FBMC, each subcarrier is individually filtered and provides robustness against inter-carrier interference (ICI) effects [4]. However, FBMC systems utilize filters, whose length is multiple times of samples per multi-carrier symbol resulting in increased complexity of the system. Universal Filtered Multi-Carrier (UFMC) is a novel multi-carrier modulation technique, which combines the features of FBMC and OFDM. UFMC filters groups of subcarriers instead of per subcarrier like FBMC or a complete signal in a single shot like OFDM. This allows reducing the filter length considerably as compared to FBMC. So, it is less complex like OFDM and provides better subcarrier separation like FBMC [5]. The main drawback of all these multicharrier modulation techniques is high Peak to Average Power Ratio [7,8]. Various PAPR reduction techniques have been proposed in literature and are implemented on OFDM and FBMC. The conventional techniques for PAPR reduction include Selective Mapping (SLM), Compinging,

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Tone reservation, Clipping and Filtering, Partial Transmit Sequence (PTS) and Active Constellation Extension (ACE) [9]. These techniques have been implemented with Orthogonal Frequency Division multiplexing, but little efforts have been done for PAPR reduction in Universal Filtered Multi-Carrier [10]. Clipping is the simplest and extensively used method for PAPR reduction. Selective mapping is a suitable match for the subcarrier nature of UFMC.

In this paper a novel hybrid PAPR reduction technique SC-UFMC for UFMC systems has been proposed. This technique is implemented by using SLM and Clipping PAPR reduction techniques. It is observed that this Hybrid technique provides better results when compared with the individual performances of SLM and Clipping techniques.

2. UFMC WAVEFORM GENERATION

For next generation wireless communication systems, a new waveform is required which should achieve the asynchronous reception and transmission, non-orthogonal waveforms for better spectral efficiency and low latency. UFMC has been introduced as a new waveform design representing a generalization of this principle targeting to collect the advantages while avoiding the disadvantages of other modulation techniques [11,12]. UFMC is the method which combines the advantages of orthogonality of OFDM and concept of filter bank in FBMC. Instead of filtering each carrier like in FBMC, blocks of carriers called sub-bands are filtered. Each sub-band contains a number of carriers and the filter length will depend upon the width of the sub-band [13]. Fig. 2.1 shows the process of transmission and reception in a UFMC system. Here, the complex symbols generated from the modulator (QPSK or QAM) are applied to serial to parallel converter resulting in a block of streams and fed as input to their respective IFFT. The length of \( N \) points IFFT output is converted back to serial per block and that output will be filtered with a pulse shaping filter of length \( L \).

The transmitted signal can be given as:

\[
x_k = \sum_{p=1}^{B} F_{p,k} V_{p,k} X_{p,k}
\]

As shown in Fig. 2.1, the overall bandwidth and the total number of subcarriers are divided into number of sub bands. Now, the input data stream of \( k^{\text{th}} \) user, \( x_k \) is divided into multiple sub streams denoted by \( X_{p,k} \) for \( p \in \{1, \ldots, B\} \). Here \( B \) is the total number of sub streams or sub bands. A sub band in UFMC may also correspond to Physical Resource Block (PRB) in LTE.

Then, the signal of each sub band is applied to individual \( N \) point IFFT represented by matrix \( V \). The output of IFFT is converted to the serial form and applied to the respective filter represented by matrix \( F \). \( F \) is a Toeplitz matrix, composed of the filter impulse response, performing the linear convolution in equation (2.1) [14]. For \( p^{\text{th}} \) sub band, where \( p \) varies from 1 to \( B \), \( X_{p,k} \), \( V_{p,k} \) and \( F_{p,k} \) represents data blocks, IFFT matrix and the filter respectively. For filter length \( L \) and IFFT matrix of size \( N \), the symbol \( x_k \) of duration \( N+L-1 \) is generated at the output of transmitter section.
Fig. 2.1. UFMC Transceiver

Fig. 2.2 shows the spectrum for UFMC waveform with sub bands $B=10$ and each sub band is having 20 sub carriers. The complete process of data transmission and reception is shown in Fig. 2.1.

At the receiver, after passing through RF-link section the signal is applied to time domain pre-processing window to suppress interference. After windowing, the signal will be converted into $2N$ parallel streams; here $N$ is the number of subcarriers. The demodulated signal is sent to the de-mapper, which is a demodulator to retrieve the data bits from the received symbols. The generated waveform is shown in Fig. 2.2.

The block-wise filtering provides flexibility to the system and may be used to avoid the main drawbacks of FBMC. UFMC supports short bursts data transmission, as well as operation in fragmented bands. The filter provides protection against inter-symbol interference (ISI), as well as robustness for supporting multiple access users which are not perfectly time-aligned. Due to the possibility to reduce guard bands, and to avoid need of CP, UFMC is spectrally more efficient than CP-OFDM [15].
3. PEAK TO AVERAGE POWER RATIO

UFMC has numerous advantages over other modulation techniques, but it also suffers from high Peak to Average Power Ratio (PAPR). The PAPR is the relation between the maximum power of a sample in a given transmitted symbol divided by the average power of that symbol. PAPR occurs when in a multicarrier system the different sub-carriers are out of phase with each other. There are a large number of independently modulated subcarriers in a multicarrier system which are different with respect to each other at different phase values. When all the subcarriers achieve the maximum value simultaneously, this will cause the output envelope to suddenly increase which causes a 'peak' in the output, and when they are added up coherently for transmission purpose give a large peak value which is very large as compared to average value of the sample. The ratio of the peak to average power value is termed as Peak-to-Average Power Ratio [16]. The mathematical valuation of PAPR is defined in equation (3.1).

$$\text{PAPR} = \left( \frac{\text{max}(|x[n]|^2)}{E(|x[n]|^2)} \right)$$  \hspace{1cm} (3.1)

Where, $|x[n]|$ is the amplitude of $x[n]$ and $E$ denotes the expectation of the signal. This higher PAPR causes saturation in the power amplifier which produces inter modulation products among sub bands and also increases out of band radiation (OOB).
3.1. Conventional PAPR Reduction Techniques

There are various PAPR reduction techniques which can be used to improve performance of multicarrier modulation systems. Some of them are:

3.1.1. Selective Mapping (SLM) Technique

In SLM, from the original data block several candidate data blocks are generated and all the data blocks are having the same information. After this a phase rotation is applied to each block and passed from its respective iDFT and a block with minimum PAPR is selected for transmission [17].

3.1.2. Companding

Companding is an easy and less complex method of PAPR reduction, the basic idea is to expand the small signal in the transmitter section and compression is carried out at the receiver side. In this technique, we enlarge the small signals while compressing the large signals to increase the immunity of small signals from noise. This compression is carried out at the transmitter end, after the output is taken from IFFT block. There are two types of companders: $\mu$-law and A-law companders [18].

3.1.3. Partial Transmit Sequence

In PTS original data block is partitioned into $N$ disjoint sub blocks. The subcarriers in each sub block are rotated by the same phase factor such the PAPR of the combination can be minimized. PTS scheme reduces PAPR with some additional complexity and it also affects spectral efficiency of the system because side information is also required to be transmitted. It does not produce any distortion in system [19].

3.1.4. Clipping and filtering

This is one of the simplest techniques for PAPR reduction. The principle is to define a clipping level for data transmission above which the input signal is clipped off and peaks of signal are reduced [20]. Let, there is a signal $y[n]$ which is to be transmitted and $y_c[n]$ is its clipped version which can be denoted as:

$$y_c[n] = \begin{cases} 
-A & y[n] \leq -A \\
y[n] & |y[n]| < A \\
A & y[n] \geq A 
\end{cases} \quad (3.2)$$

Where A is the clipping level. After clipping out of band radiations are produced this can be reduced by using filtering after clipping.

3.1.5. Tone Reservation

In this scheme, some subcarriers are reserved within the transmitted bandwidth and appropriate value is assigned to these reserved tones [21]. These reserved subcarriers don’t carry any data information, are only used for reducing PAPR.

3.1.6. Active Constellation Extension (ACE)

In ACE, at each block, some of the outer signal constellation points are extended towards outside of the constellation such that the PAPR of the resulting block is reduced. It is transparent to the receiver. There is no loss of data rate and no side information is required.

However, all these PAPR reduction techniques were introduced for OFDM systems and due to different frame structure of UFMC signal, these techniques cannot be effectively utilized in UFMC systems.
4. PROPOSED HYBRID SCHEME

Various PAPR reduction techniques introduced for OFDM system are discussed in the previous section and we tried to apply all these techniques on UFMC systems. It has been observed that SLM and Clipping are suitable PAPR reduction techniques for UFMC systems and can reduce PAPR very effectively with a small increase in system complexity. On the other hand, schemes like PTS, ACE and TR makes the system very complex and it is very difficult to apply these techniques on the frame structure of UFMC systems.

In this work, we have proposed a novel Hybrid technique for PAPR reduction in UFMC by using SLM and Clipping. Unlike existing SLM and Clipping schemes for OFDM systems, the proposed method exploits the nature of sub-block data transmission of UFMC. In UFMC data is generated in the form of sub blocks which are groups of subcarriers. The advantages of SLM and Clipping have been exploited in this Hybrid technique. In Clipping some distortion is produced but in SLM there is no any distortion while on the other hand SLM produces data rate loss but in Clipping there is no any data rate loss. So, in this work we have combined these two schemes so that we can exploit the advantages of both schemes. Both techniques have the advantage that the power of the system doesn’t increase. Hence, we can decrease PAPR with the same power which is used by the system when no PAPR reduction technique is applied.

4.1. Hybrid (SC-UFMC) PAPR Reduction Technique

The basic block diagram of Hybrid technique is shown in Fig. 4.1. The waveform generated by the UFMC modulator is given to the serial to parallel converter where several candidate blocks are generated from original data block. This is done to find a block with minimum PAPR for transmission. After generating candidate blocks a phase rotation is applied to each block and applied to IFFT of their respective. Because of the varying assignment of data to the transmit signal, it is called selective mapping. The core is to choose a particular signal which is having desired properties out of n signals representing the same information. Finally, we select a block with minimum PAPR, the signal generated by this selector is applied to clipper for removing the higher peaks. For this a particular thershold value is defined above which all the signal is clipped so that peak to average power ratio can be reduced.

The signal generated by UFMC is given in equation 2.1 and after applying a phase rotation the signal become as given in equation (4.1).

\[ x = \sum_{p=1}^{B} F_{p,k} V_{p,k} X_{p,k} p(n) \]  

(4.1)
Where, $p(n)$ denotes the phase rotation of the signal, after this signal after FFT is applied to clipper. Let the threshold for the signal is $A$. Then the final signal will be:

$$x_c = \begin{cases} x, & |x| < A \\ A, & |x| > A \end{cases}$$

Hence, by using this technique we selected a block with minimum PAPR and then a clipper circuit is used to clip of the peaks of that block so that we can reduce peak to average power ratio of signal to a great extent.

5. SIMULATION SETUP AND RESULTS

To compare the proposed Hybrid (SC-UFMC) technique with conventional SLM (S-UFMC) and Clipping (C-UFMC) techniques, MATLAB platform has been used. All the simulation work, including comparison and performance evaluation of proposed technique with variation in design parameters was done by using MATLAB platform.

5.1. Simulation Setup

Table 5.1 provides the simulation set up to evaluate the performance of proposed PAPR reduction technique. The proposed technique is also compared with three other techniques as original (UFMC), with Selective mapping (S-UFMC), with Clipping (C-UFMC) and Hybrid (SC-UFMC) to analyze the effectiveness in PAPR reduction. The performance of the proposed method is evaluated and compared on the basis of variation in FFT size, Bits Per sub carrier, filter length and modulation order.

| Parameter            | Values                  |
|----------------------|-------------------------|
| FFT Size             | 2048, 1024, 512, 256    |
| Sub Band Size        | 20                      |
| Number of Sub bands  | 10                      |
| Modulation order     | QAM (4, 16, 64)         |
| Bits per Sub Carrier | 2, 4, 6                 |
| Filter Length        | 43, 63, 83              |

In Fig. 5.1 Peak to Average Power Ratio of UFMC, SLM scheme (S-UFMC), Clipping scheme (C-UFMC) and Hybrid scheme (SC-UFMC) with FFT Size 1024, Filter length 43, Bits per subcarrier 2 and modulation order 4 are shown. It can be concluded that the proposed hybrid schemes have improved PAPR reduction performance as compared with the two conventional schemes for PAPR reduction.
5.2. Performance evaluation of SC-UFMC with variation in design parameters

This section presents performance evaluation of SC-UFMC with variation in design parameters (FFT Size, Bits per sub carrier and Filter length).

5.2.1. Variation in FFT Size

Fig. 5.2 shows the PAPR of UFMC signal and performance of three PAPR reduction techniques at FFT size 2048. It can be observed that SC-UFMC is providing better PAPR reduction than other two techniques.

![Fig. 5.2. Performance of various PAPR reduction techniques with different FFT Sizes](image-url)
As shown in Fig. 5.2, C-UFMC shows better performance than S-UFMC, so effectiveness of SC-UFMC is analyzed with different values of design parameters with respect to C-UFMC. Table 5.2 is showing that SC-UFMC performs more effectively with larger FFT size.

### Table 5.2. Effectiveness with variation in FFT size

| FFT Size | % Effectiveness of SC-UFMC |
|----------|---------------------------|
| 256      | 4.23%                     |
| 512      | 27%                       |
| 1024     | 28.15%                    |
| 2048     | 30.14%                    |

#### 5.2.2 Variation in Bits per Sub carrier

Performance of various PAPR reduction techniques with 2 Bits per sub carrier is shown in Fig. 5.3 from here it can be observed that proposed scheme is showing better results than conventional schemes. All the schemes are showing different values when we change any of the design parameters as shown in Fig. 5.3, here we are changing bits per sub carriers.

![PAPR with variation in Bits per sub carrier](image)

**Fig. 5.3.** Performance of various PAPR reduction techniques with different Bits per sub carrier

As shown in Table 5.3 with increase in Bits per sub carrier, SC-UFMC is being more effective and at 6 bits per sub carrier it is having maximum PAPR reduction.

### Table 5.3. Effectiveness with variation in Bits per Sub carrier

| Bits per Sub carrier | % Effectiveness of SC-UFMC |
|----------------------|----------------------------|
| 2                    | 30.14%                     |
| 4                    | 37.62%                     |
| 6                    | 58.60%                     |
5.2.3 Variation in Filter length

With changing filter length, PAPR of original UFMC signal as well as performance of PAPR reduction techniques also get affected as shown in Fig. 5.4.

![PAPR with variation in Filter length](image)

**Fig. 5.4.** Performance of various PAPR reduction techniques with different Filter lengths

It can be observed from table 5.4 that at higher filter length proposed scheme performed less effectively and a better PAPR reduction can be obtained with lower filter length.

| Filter Length | %Effectiveness of SC-UFMC |
|---------------|--------------------------|
| 43            | 36.79%                   |
| 63            | 14.57%                   |
| 83            | 8.40%                    |

### 6. CONCLUSION

In this paper, a novel hybrid scheme SC-UFMC for PAPR reduction of UFMC signals is proposed. Simulation results and analysis shows that the Hybrid scheme is an efficient PAPR reduction method for UFMC systems, and it can provide better PAPR reduction performance than the conventional SLM and Clipping schemes. Further, the effect of various design parameters on PAPR reduction in SC-UFMC has been analyzed and it is concluded that the proposed technique provides effective PAPR reduction than conventional schemes.

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