Title: How we choose multi-component rewards

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Abstract

Realistic, everyday rewards contain multiple components. An apple has taste and size. However, we choose in single dimensions, simply preferring some apples to others. How can such single-dimensional relationships refer to multi-dimensional choice options? Here, we investigated stochastic choices of two-component milkshakes. The revealed preferences were intuitively graphed as indifference curves that indicated how much of one component was traded-in for obtaining one unit of the other component without a change in preference, thus defining the orderly integration of multiple components into single-dimensional estimates. Options on higher indifference curves were preferred to those on lower curves. The systematic, non-overlapping curves satisfied leave-one-out tests, followed decoder predictions and correlated with Becker-DeGroot-Marschak auction-like bids. These single-dimensional estimates of multi-component options complied with rigorous concepts of Revealed Preference Theory and encourage formal investigations of normal, irrational and pathological decisions and their neural signals.

Keywords: Bundles, decision-making, reward, stochastic choice, psychophysics
Introduction (960 words with refs)

We like apples, in particular if they are sweet. We can state our preference in words, but this may not be accurate because of poor introspection, faulty memory or erroneous report. It would be more accurate to observe our choice between different apples by which we reveal our preference at that moment. But how do we make that choice? When choosing between apples, we may prefer a sweeter one even if it is a bit smaller; we would trade-in some size for more sweetness. As the trade-off illustrates, our preference among apples does not come from any component alone but from their combination. Every reward or economic good constitutes a bundle with multiple components, attributes or dimensions, and thus is formally a vector. The bundle components may be integral parts of a good, like the sweetness and size of the apple, or consist of distinct entities, like the steak and vegetable of a meal. Importantly, each component contributes to the choice of the bundle. Without considering the multi-component nature of choice options, we can only study gross choices or exchanges, like between an apple and a pear (not really a choice for an apple lover), or between a movie ticket and a meal (not good when hungry). Thus, to understand realistic, fine-grained choices, we should consider that choice options have multiple components.

In contrast to the multi-dimensionality of realistic, vectorial choice options, revealed preferences and subjective reward value (‘utility’) are single-dimensional. When faced with two options, a rational decision maker can only prefer one option or its alternative or be indifferent to the options (completeness axiom; see Mas-Colell et al. 1995). With repeated, stochastic choices, preferences are revealed by choice probability (McFadden 2004); the probability of choosing one option over its alternative varies in a graded, scalar manner. Correspondingly, the utility of one choice option can only be higher, lower or equal to that of its alternative. Further, neural signals reflecting choice options vary only along a single dimension at any given moment and thus are also scalar. Hence the question: how can single-dimensional revealed preferences, utility and neural signals emerge from vectorial, multi-component choice options? In particular, can we test the issue empirically using well worked-out theoretical concepts that should reduce possible confounds?

The issue of vectorial-to-scalar transformation can be formally approached by considering that the same scalar measure may arise from oppositely varying vector components. I may trade-in a larger, less sweet apple for a smaller but sweeter one without loss or gain in utility (I do not want to lose anything, nor is it easy to gain anything). Thus, the increase in sweetness is compensated by the decrease in size. This trade-off is captured by Revealed Preference Theory, whose two-dimensional indifference curves (IC) provide a convenient graphic formalism (Fisher 1892; Samuelson 1937; 1938). Equally revealed preferred but differently composed multi-component bundles are plotted on one and the same IC. The continuous nature of these ICs is an important indicator for the systematic trade-off that indicates the well-ordered integration of the relative values of multiple bundle components into single-dimensional preference and utility. For these reasons, ICs are a mainstay of economic theory and textbooks (Laidler & Estrin 1989; Kreps 1990; Varian 1992; Mas-Colell et al. 1995; Perloff 2009).

Previous research investigated multi-component choice options without referring to the IC concept. The tests include the quality and price of television sets (Simonson 1989), comfort and fuel consumption of cars (Simonson 1989), payoff amount and probability (Tversky 1969; Soltani et al. 2012; Levy et al. 2012), shape and color of cards (Fellows 2016), artificial objects and appendages (Pelletier & Fellows 2019), various food components (Suzuki et al. 2017; DiFeliceantonio et al. 2018; Harris et al. 2018), hats and shoes (Thurstone 1931), pastries and payoffs (MacCrimmon & Toda 1969), and monetary token from two accounts (Choi et al. 2007; Kurtz-David at al. 2019). More formal studies used ICs to represent hypothetical outcomes, such as hats and shoes (Thurstone 1931), pencils or pastries and payoff (MacCrimmon & Toda 1969), and monetary token (Choi et al. 2007; Kurtz-David et al. 2019). The formal IC scheme is also useful for explaining inconsistencies
of economic choices (Rieskamp et al. 2006; Chung et al. 2017; Gluth et al. 2017). However, what is missing from past work are empirical designs that apply the IC formalisms of Revealed Preference Theory to controlled laboratory situations for a wide range of studies. In building on previous research, the purpose of the present study was to empirically estimate formal ICs of revealed preference relationships that take all components properly into account. The design used the rigorous concepts of Revealed Preference Theory and should be suitable for testing further aspects of revealed preferences in normal humans, for detecting fine-grained “irrational” anomalies in normal and brain-damaged humans who fail to properly consider all components of choice options, for studying underlying normal and pathological brain processes, and for comparing the data with behavioural choices and high-precision single-neuron recordings in animals. These goals imposed substantial constraints, including specific event timing and the use of types and amounts of payouts that are comparable to the immediate and tangible liquid and food rewards of animal studies (Kagel et al. 1975; Pastor-Bernier et al. 2011). The repeated trials necessary for statistical data analysis of human imaging (and animal neurophysiology) required us to study stochastic preferences (McFadden 2004; Stott 2006). Sitting in front of a computer monitor, our participants viewed two discrete choice options (rather than verbal information) that contained the same two fatty and sugary milkshakes in independently varying quantities. We varied bundle composition and psychophysically estimated indifference points (IP) at which an original and a changed bundle were chosen with equal probability.

Results

Basic properties of indifference curves. Participants repeatedly chose between two composite visual stimuli that represented two-component bundles (see Methods notion 1; Fig. 1a). Each bundle stimulus consisted of two colored vertical rectangles; blue indicated component A, a low-sugar high-fat milkshake; red indicated component B, a high-sugar low-fat milkshake; a vertically positioned bar inside each rectangle indicated the amount of each milkshake (higher was more). We assessed choices between a preset Reference bundle and a Variable bundle whose component A was set to a specific test amount and whose component B varied pseudorandomly across a wide range (Fig. 1b). The choice probabilities in all 24 participants followed the change of component B in an orderly fashion, thus revealing monotonic preference relationships (notions 2 - 4; Fig. 1c). We derived the indifference point (IP; $P = 0.5$ for each bundle) from six repetitions using the probit choice function (Eqs. 1, 2); each IP required 42 choices. Thus, a two-dimensional IP indicated the amounts of the two components of the Variable Bundle that was as much revealed preferred, and had the same utility, as the constant Reference Bundle. To obtain a series of IPs, we repeated this procedure by setting increasing amounts of component A in the Variable bundle while keeping the Reference Bundle constant. All IPs of such a series were as much revealed preferred as the constant Reference Bundle and, by transitivity, equally revealed preferred to each other.

We obtained single ICs from such a series of five equally revealed preferred IPs by hyperbolic fitting (Eqs. 3, 3a) (notions 5 and 6; Fig. 1d, e). Such an IC defined the trade-off between the two bundle components at equal preference: it indicated how much of component B a participant gave up for obtaining one unit of component A. The continuous ICs were asymmetric between the x-axis and y-axis, indicating different subjective weighting of the two milkshakes; the convex IC curvature suggests that lower amounts of both milkshakes together were as much preferred as higher amounts of singular milkshakes (possibly reflecting gradually flattening, concave utility functions and/or complementarity between high-sugar and high-fat components).

We estimated three sets of 5 IPs with their respective, hyperbolically fitted ICs by presetting the Reference Bundle to three different amounts of component B (2.0 ml, 5.0 ml or 8.0 ml; component A being always 0.0 ml). Fig. 2a (inset) shows the psychophysical assessment of an example IP. Although the ICs varied in slope and curvature between...
participants (for two example participants, see Fig. 2a, b; for all participants, see Fig. 3), the ICs of bundles with larger reward amounts were located farther away from the origin, thus reflecting higher revealed preference (notion 7). The three ICs were well ordered and failed to overlap. Only the 95% confidence intervals overlapped partly in four of the 24 participants (17%). Closer inspection of Figs. 2a, b and 3 shows that some bundles on higher ICs had a smaller amount of component B than bundles on lower ICs, indicating revealed preference despite partial physical non-dominance (notion 8; involving overcompensation by higher amount of component A).

Taken together, the continuous nature of the ICs with their multiple IPs indicated the orderly and systematic emergence of single-dimensional utility and stochastic preference from differently composed vectorial bundles, in compliance with the basic concepts.

IC coefficients. The shape of ICs reflects the trade-off between the components and can be quantified by slope and curvature coefficients of hyperbolic fits (Eq. 3a). The global IC slope, between y-axis and x-axis intercepts, was measured as ratio of the two regression coefficients \( \beta_2 / \beta_1 \) in Eq. 3; it indicated how much the participant was globally willing to give up in order to obtain one unit of the other component; the measure reflected the relative utility (currency) of the two bundle components. The IC slopes steeper than -45° indicate that a participant gave up a higher amount of component B (high-sugar, y-axis) for a smaller amount of component A (high-fat, x-axis), thus indicating higher subjective value of fatty than sugary milkshake. The IC slope was -71° ± 6.5° (mean ± standard error of the mean, SEM; range -45° to -76°; \( N = 24 \) participants; Fig. 2c). The higher valuation of high-fat component A over high-sugar component B amounted to a factor of 3:1 in 18 of the 24 participants (75%). The predominantly asymmetric trade-off between the milkshake components documents that each component contributed to bundle preference in its own distinct way.

The IC curvature showed substantial convexity in 18 of the 24 participants (75%), as indicated by \( \beta_3 \) coefficients from the hyperbolic fit (Eq. 3) that were significantly larger than 0.0 (8.89; mean ± 5.9 SEM; \( p < 0.05 \), t-test; Fig. 2d). For graphically assessing IC curvature, we measured the distance between the IC center and a straight line connecting equally revealed preferred bundles at the x- and y-intercepts, in units of ml on the y-axis (Fig. 2e). This distance ranged from 0.09 ml (quasi-linear IC) to 3.76 ml (most convex IC) (mean of 1.28 ml ± 0.19 SEM; Fig. 2f). The distribution of the IC distance was overall similar to that of the \( \beta_3 \) curvature coefficient from Eq. 3. The two highest histogram bars in Fig. 2f show data from six participants with rather similar, considerably convex IC, and from six other participants with rather similar but quasi-linear IC. Thus, the coefficients confirmed numerically the well-ordered nature of the representation of revealed preferences by the ICs.

Control for other choice variables. To test whether the choices reflected the components of the bundles rather than other, unrelated factors, we performed a logistic regression analysis separately for each of the 24 participants, using the following regressors: amount of each bundle component, reaction time, Reference Bundle position on participant’s monitor, and previous trial choice (Eq. 5). The standardized beta (\( \beta \)) coefficients and p-values were assessed for each participant and then averaged across all 24 participants; they demonstrated that the choice of the Variable Bundle was negatively correlated with the amount of component B in the Reference Bundle (RefB: \( \beta = -0.43 ± 0.16 \) mean ± SEM; \( P = 0.020 ± 0.005 \)) (component A was constant 0.0 ml, see Methods) and positively correlated with both components A and B in the Variable Bundle (VarA: \( \beta = 0.67 ± 0.16 \); \( P = 0.009 ± 0.004 \); VarB: \( \beta = 0.94 ± 0.33 ; \ P = 0.012 ± 0.009 \) (Fig. 2g)). The beta (\( \beta \)) coefficients for these three variables differed significantly from 0 (\( P = 0.012, P = 0.0088 \) and \( P = 0.00028 \), respectively; one-sample t-test), confirming the validity of the \( \beta \)'s. Thus, more frequent choice of the Variable Bundle correlated with lower amounts in the Reference Bundle and with higher amounts of either component in the Variable Bundle. The result suggests that...
both bundle components, rather than a single component alone, were important for the observed preference relationships. The remaining variables, including reaction time, position of Reference Bundle on the monitor and previous trial choice, failed to significantly account for current choice of the Variable Bundle ($P = 0.754 – 0.988 \pm 0.003 – 0.290$). Thus, the revealed preference relationships concerned the bundles with their two components rather than other task factors.

To assess potential consumption effects, we searched for signs of satiety. We followed choice probability across the total test duration in each of the 24 participants. We selected two bundles that were situated above and below the IP, respectively. These two bundles contained high-sugar low-fat (above IP) and low-sugar high-fat (below IP) milkshakes. We plotted choice probability over six repeated test steps (Extended Data Fig. 1). Choice probabilities fluctuated only insignificantly, without conspicuous upward or downward trend (above IP: $F(5, 41) = 0.28, P > 0.05$; below IP: $F(5, 41) = 1.53, P > 0.05$; 1-way repeated measures Anova with post-hoc Tukey Test). Even at the final, sixth step, choice probability differed only insignificantly from any other step. Thus, the revealed references did not seem to be importantly confounded by satiety for neither sugar nor fat within the amounts and concentrations used in our experiment.

**Internal validation of indifference curves.** We performed a leave-one-out analysis to assess the contribution of individual bundles to the ICs obtained from hyperbolic fits to the empirically estimated IPs. We removed one IP at a time (except the initial Reference Bundle at $x = 0.0$) from the set of five IPs to which a given IC had been fitted, and then refitted the IC with the remaining four IPs using the same hyperbolic model (see Methods, Eqs. 3, 3a). This was done separately for each of the three ICs, separately in all 24 participants (total of 288 IPs removed from 72 ICs). We found consistency in the refitted ICs in four measures (Fig. 4a). First, none of the 72 refitted ICs overlapped with the refitted ICs at different levels in the same participant, thus demonstrating maintained IC separation despite one left-out IP. Second, none of the 72 refitted ICs overlapped with the 95% confidence intervals of original ICs at different levels, confirming IC separation despite one left-out IP. Third, most refitted ICs (66 of 72 ICs, 92%) fell inside the 95% confidence intervals of the original ICs, and the remainder curves (6 of 72 ICs, 8%) showed only some portions outside the 95% confidence intervals of the original ICs, thus refuting possible overweighted influence of individual IPs on ICs. Fourth, numeric comparisons showed only insignificant deviations between refitted ICs and the IPs that had been left out when refitting the curves (vertical distance of $0.05 \pm 0.13$ ml in all 24 participants; mean $\pm$ standard error of the mean, SEM; $N = 336$; $P = 0.98$ against normal distribution; t-test) (Fig. 4b, c), confirming absence of overweighted IP influence on ICs. These four results suggest that the hyperbolically fitted ICs captured the IPs consistently and provided valid representations of the revealed preferences.

We used a linear support vector machine (SVM) decoder as different statistical procedure to confirm the contribution of each IP to the two-dimensional representation of revealed preferences by ICs. In each participant, we set a given test bundle to one of the psychophysically determined IPs (Fig. 5a) and assessed the accuracy with which the decoder assigned that bundle to its original preference level (each preference level was defined by a series of empirically estimated IPs but was not a fitted IC). SVM decoding accuracy ranged largely from 70% to 100% ($P = 2.055 \times 10^{-101}$), although a few lower values were observed (Table 1 left).

We supplemented the SVM analysis by visualization of decoding using linear discriminant analysis (LDA). The considerable amount of data necessary for reasonable LDA required us to pool data from several participants, which violates a basic tenet of economic theory that prohibits pooling of subjective preferences across individual participants. To somewhat contain expected inaccuracies, we normalized IPs across participants (z-score normalization for reward $B$ along the y-axis; reward $A$ had been set experimentally to identical values on the x-axis) and restricted the analysis to specific subsets of participants.
The LDA confirmed the SVM results in all subsets (Fig. 5); the first linear discriminant assigned bundles to the three revealed preference levels, as shown by spatial separation of the three colored groups, with a numeric accuracy of 80-100% \((P = 1.148 \times 10^{-9}/)\). By contrast, the second discriminant failed to accurately assign bundles to different positions on same preference levels, as shown by the mix of the five shapes representing bundle position. These characteristics were seen in six participants whose fitted ICs showed the highest similarity in convexity (Fig. 5b, c), in six participants with linear ICs (Fig. 5d, e) and, for comparison, in all 24 participants (Fig. 5f, g) (for distinction of participants based on IC curvature, see two highest bars in Fig. 2f). Thus, LDA decoding followed the fundamentals of ICs: preference between bundles across ICs but indifference along ICs.

Taken together, the two decoders confirmed three distinguishable levels of IPs, and LDA confirmed indifference between IPs on same levels. As these IPs constituted the basis for the hyperbolic fitting of the three ICs, the decoder results validated also the fitting procedure and confirmed that the estimated ICs represented well the revealed preferences.

**Mechanism-independent validation of indifference curves.** The ordered representation of revealed preferences by our ICs can be further validated by comparison of the key features of ICs with subjective values inferred from a different estimation mechanism. To this end, we used a monetary Becker-DeGroot-Marschak (BDM) bidding task that is equivalent to a second-price auction and estimates participants’ truthful, ‘incentive compatible’ bids on a trial-by-trial basis. The property of truthful revelation makes BDM an indispensable tool of experimental economics and explains its increasing popularity in neuroscientific studies of human decision making (Plasmmann, O’Doherty & Rangel 2007; Medic et al. 2014).

For these comparisons, the same 24 participants made monetary BDM bids (UK pence) for 15 bundles that had been set, individually in each participant, to five psychophysically estimated IPs on each of the three preference levels (in ml of each of the two component milkshakes). Each preference level was defined by IP bundles that were equally revealed preferred to the initial Reference Bundle with component A set to 0.0 ml (Fig. 6a; the same 15 bundles were used for hyperbolic IC fitting). Although BDM estimates typically derive from single-shot choice, we obtained averaged BDM estimates for each bundle from 12 repetitions, thus aiming to approach the nature of data collection during stochastic choice with psychophysical estimation of each IP (42 trials).

The BDM bids followed the ordered preference levels, as shown by significant positive correlation between the bids for same-level bundles (means from all five bundles) and the three levels (Spearman rank correlation: \(\rho = 0.60 \pm 0.05\); mean ± SEM; \(N = 24\) participants; \(P < 0.01\); confirmed by one-way Anova with post-hoc Tukey-Kramer test between all bundles across the three levels: \(P < 0.01\) (Fig. 6b; red, green, blue). A random-effects analysis separately for each of the 24 participants (Eq. 8) demonstrated a relationship of BDM bids to preference level (PrefLev: \(\beta = 0.47 \pm 0.09\), mean across all 24 participants ± SEM; \(P = 0.016 \pm 0.015\); \(\beta\)-coefficient difference from 0: \(P = 0.00026\), one-sample t-test) and bundle amount (AmBundle: \(\beta = 0.15 \pm 0.13\); \(P = 0.020 \pm 0.017\); \(P = 0.0278\), rather than trial number (TrialN: \(\beta = -0.10 \pm 0.25\); \(P = 0.726 \pm 0.354\), previous trial bid (PrevBid: \(\beta = 0.12 \pm 0.11\); \(P = 0.676 \pm 0.427\) or consumption history (Consum: \(\beta = 0.12 \pm 0.11\); \(P = 0.224 \pm 0.185\)) (all \(\beta\)’s were standardized) (Fig. 6c). A specific analysis (Eq. 9) demonstrated that the BDM bids reflected both bundle components (component A: \(\beta = 0.6534 \pm 0.0866\), mean ± SEM; \(P = 0.0324 \pm 0.0150\); \(\beta\) difference from 0: \(P = 1.1613 \times 10^{-7}\), one-sample t-test; component B: \(\beta = 0.6425 \pm 0.0585\), \(P = 0.0289 \pm 0.0202\); \(\beta\) difference from 0: \(P = 1.2770 \times 10^{-10}\)). Thus, the BDM bids followed well the revealed preference levels and took both bundle components into account.

The BDM bids were similar for equally revealed preferred bundles. To comply with the notion of trade-off between different bundle components, equally revealed preferred bundles should elicit similar BDM bids despite varying bundle composition. We conducted a one-way Anova on all BDM bids for bundles positioned on the same preference level, separately for
each level and each participant. The bids for bundles located on the same revealed preference
level failed to differ statistically (low level: \( P = 0.54 \pm 0.06; \) medium level: \( P = 0.69 \pm 0.06; \)
high level: \( P = 0.78 \pm 0.05; \) mean \( \pm \) SEM, \( N = 24 \) participants). Only three participants
showed significantly different bids for bundles on the medium preference level, and one
participant showed different bids for bundles on the high preference level (\( P < 0.05 \)). Thus, most participants showed similar BDM bids for equally revealed preferred bundles on same
revealed preference levels (while being sensitive to bundle amounts, as shown by increasing
bids across levels). The BDM bids confirmed the equal-preference trade-off between bundle
components independent of the binary choice mechanism used for assessing revealed
preferences.

The BDM bids were internally consistent. We used decoders to test the distinction of
bundle position across but not along preference levels. Using BDM bids, a binary SVM
decoder showed good accuracy of assigning a test bundle to its original preference level in
individual participants (mostly 50-70%; \( P = 3.789 \times 10^{-5} \)) but failed to distinguish bundles
along same levels (43-51%; \( P = 0.1433 \)) (Table 1 right). We used an LDA, which is able to
decide several levels together, as supplementary test and found good visual assignment of the
test bundles (Fig. 6a) to the three revealed preference levels in our population of 24
participants (first discriminant; numeric accuracy of 88-100%; \( P = 9.46 \times 10^{-12} \); Fig. 6d;
three colored symbol groups) but not to different positions on same preference levels (second
discriminant; numeric accuracy of 43-51%; mix of shapes) (note the reservations above when
combining data from multiple participants). Thus, the BDM bids followed well the two-
dimensional scheme of revealed preference represented by the ICs.

The BDM bids matched well the revealed preference ICs in direct comparison. A
stronger mechanism-independent validation of the IC scheme may be achieved by direct
graphic comparison between BDM bids and hyperbolically fitted ICs. To this end, we
estimated isolines that were fit to BDM bids using Eqs. 9, 9a and compared them with ICs
that had been hyperbolically fitted to IPs (Eqs. 3, 3a). The BDM isolines derived from
averaged 12 BDM bids, and the revealed preference ICs derived from fits to IPs estimated
from 42 stochastic choices. We found that the BDM isolines increased for IPs on increasing
preference levels (farther away from the origin), but were similar for IPs on the same
revealed preference level (same distance from origin) (Fig. 7a). The BDM isolines matched
the revealed preference ICs within their 95% confidence intervals (CIs) in every one of the 24
participants (Fig. 7b). Statistical comparisons showed significantly higher CIs of BDM
isolines compared to revealed preference ICs (Fig. 7c; \( P < 0.0884 \times 10^{-8} \), Wilcoxon paired
test; \( N = 24 \) participants). Despite their larger variability, both BDM isoline slope and
curvature coefficients, derived from the respective \( \beta_2 / \beta_1 \)-ratio and \( \beta_3 \) regression coefficient
in Eq. 9, failed to differ significantly from the respective slope and curvature coefficients of
revealed preference ICs (Eq. 3; Fig. 7d, e; both \( P > 0.05 \), Wilcoxon test on BDM vs. IC
coefficients paired from each participant; \( N = 24 \)). Thus, despite larger variability, the BDM
bids matched well the revealed preference ICs when assessed in a comparable way.

Taken together, the different estimation mechanism of BDM bidding provided good
validation of the estimated revealed preferences and their graphic representation by ICs.

Discussion
This study shows that ICs representing revealed preferences among multi-dimensional choice
options can be reliably estimated in a controlled and unequivocal manner using immediate
consumption of small payouts in repeated trials. The preferences followed critical
assumptions of formal theory that define the emergence of scalar utility and preference
measures (choice probability) from vectorial choice options, in particular the continuous,
graded trade-off between bundle components that transcends physical bundle composition.
These preferences were graphically well represented by the asymmetric and nonlinear ICs.
Lack of overlap between ICs, validation by leave-one-out statistics and accuracy of SVM and
LDA decoding demonstrate proportionate contribution of individual bundles to robust preference representations by ICs. The BDM bids corresponding to the ICs provided a mechanism-independent validation of the revealed preferences. These empirical results demonstrate revealed stochastic preferences in humans in controlled, non-verbal, laboratory setting. Further, the systematic ICs correspond well to, and thus implement, the abstract schematic graphs in economic textbooks and decision research that are used for explaining human choices (Laidler & Estrin 1989; Kreps 1990; Varian 1992; Mas-Colell et al. 1995; Perloff 2009). In following these concepts, the currently estimated, well-structured ICs represent orderly revealed preferences that would allow the distinction from irrational preferences not fully capturing the multi-component nature of choice options, including lexicographic preferences restricted to single components. These properties make the currently developed tests suitable for concept-driven studies of rational and irrational behaviour in normal and brain-damaged humans.

The representation of vectorial, multi-component choice options by single-dimensional neural signals is an open question in neuroeconomics. Our behavioural tests provide a formal, concept-driven foundation for investigating such signals in humans. These tests require repeated trials rather than one-shot tests typical for experimental economics; the multi-trial nature is well captured by stochastic choice theories that facilitate data interpretation due to decades of decision research. The immediately consumed future rewards and assure reliable cooperation by the participants, thus reducing interfering and confounding brain activity. We were particularly interested in estimating whole maps of well-ordered, fitted ICs derived from multiple IPs that conform to predictive mathematical functions, rather than testing preferences for a few bundles with limited general validity. As a result, neuroeconomic work using the demonstrated empirical tests could investigate decision mechanisms not resolvable by purely behavioural examination. For example, it is unknown whether the bundle components are combined into a common neural utility estimate or are coded separately and integrated at a later stage. The ensuing neural decision process might occur between whole bundles with all components integrated, or involve hierarchical or parallel component-by-component comparisons. The systematic ICs may also allow to investigate neural underpinnings of specific theories, such as the switching of attentional processes between components conceptualized by multialternative decision field theory (Roe et al. 2001). Finally, our detailed ICs would be helpful for investigating neural mechanisms underlying inconsistent decision making when choice options are added (independence of irrelevant alternatives, IIA), beyond the decoy and attraction effects already being addressed (Chung et al. 2017; Gluth et al. 2017).

Our quantitative, psychophysically controlled preference assessment required repeated choices (Green & Swets 1966). Such a multi-trial approach is dictated by statistical requirements of neural studies, corresponds to the standard elicitation of choice functions in reinforcement learning (Sutton & Barto 1998) and allows comparison with animal studies requiring similar schedules (Kagel et al. 1975; Pastor-Bernier et al. 2017). In humans and monkeys, these methods deliver systematically varying choice probabilities rather than single, all-or-none selection. The visible trial-by-trial variations are assumed to reflect underlying random processes that make the choice process stochastic, as captured by choice probability and probabilistic choice functions in random-choice theories (Luce 1959; McFadden & Richter 1990; McFadden 2004; Stott 2006). We appreciate that our multi-trial schedule is at odds with the frequently employed, standard, single-shot, deterministic assessment of ICs in experimental economics (Thurstone 1931; MacCrimmon & Toda 1969), but we believe that the obtained consistent and robust ICs validate the approach.

Economic choice often involves substantial but imaginary sums of money and consumer items, or random, singular payouts (Simonson 1989; Simonson, Tversky 1993; Rieskamp et al. 2006). By contrast, our payout schedule was tailored to requirements of
neural studies and allowed the participants to actually consume the chosen rewards over tens
and hundreds of trials (while controlling for satiety effects), as is typically required for
animal experiments. These behavioural choices resembled small daily activities, such as
consuming snacks and drinks, and were met by the good motivation of our participants. In
this way, we obtained well-ordered ICs that provided valid representations of revealed
preferences, without requiring imagined items or unreasonably large sums of money.

Empirical investigations of economic choice of multi-component options have revealed
several inconsistencies, including reference biases, differences between willingness-to-pay
and willingness-to-sell, and violations of independence of irrelevant alternatives such as the
similarity, compromise, asymmetric dominance and attraction effects (Tversky 1972; Knetsch
& Sinden 1984; Simonson 1989; Tversky & Simonson 1993; Bateman et al. 1997; Rieskamp
et al. 2006). These phenomena may well be due to the intrinsically adaptive nature of
biological processes (Soltani et al. 2012; Li et al. 2018), rather than invalidating the revealed
preference concept itself. We aimed to avoid interference from adaptive processes by
designing stable and highly reproducible test conditions in a well-controlled laboratory
environment, non-reliance on verbal report, single, uninterrupted test sessions, singular
changes of bundle components, constant direction of testing (from top left to bottom right on
the revealed preference map), and preventing satiety by limiting total milkshake intake to 200
ml. As a result, our IPs remained stable over successive testing steps. We used the exact same
conditions for eliciting BDM bids, which may have facilitated their correspondence to
revealed preference ICs. With these testing conditions, we avoided some known
compromising factors, which might help to identify more basic factors underlying decision
irregularities.

The coefficients of hyperbolic fits to the ICs characterize numerically the representation
of revealed preferences. The slope coefficient indicates the relative weighting of the two
milkshakes. For example, the amount of equally revealed preferred single milkshakes
(graphed at the respective x-axis and y-axis intercepts of the two-dimensional map) was
lower for high-fat (component A) than high-sugar (component B) milkshakes in our
participants, which was represented by a IC slope steeper than -45 degrees; thus, participants
would have revealed preferred high-fat over high-sugar milkshakes if they came in same
amounts. Such asymmetric IC slopes are also seen with various bundles in primates (Pastor-
Bernier et al. 2017). A key reason for the asymmetry may be the use of a physical amount
scale; in addition, the revealed preference among the milkshake bundles depended also on
their fat and sugar content, for which there is no simple common physical scale. Thus, the
scaling of milkshakes in units of physical amount would explain the IC asymmetry. Further,
the slope for identical bundle compositions varied between our participants, which
demonstrates an additional subjective component in revealed preferences. Despite these
scaling and subjectivity issues, our estimated ICs had well-ordered slopes and failed to
overlap.

Further, the convex IC curvature in most of our participants indicated that
unproportionately smaller amounts of combined sugar-fat milkshakes (at IC center) were
equally revealed preferred as larger amounts of milkshakes containing primarily sugar or fat
(positioned closer to IC boundaries near x- and y-intercepts). The BDM isolines confirmed
the convex curvature; unproportionately smaller amounts of combined sugar-fat milkshakes
(at isoline center) elicited the same bids as larger amounts of milkshakes containing primarily
sugar or fat (positioned closer to isoline x- and y- intercepts). A previous study found
comparable data for BDM bids; food snacks containing sugar-fat combinations elicited
higher bids than snacks with similar calories but derived only from fat or sugar
(DiFeliceantonio et al. 2018). However, not all ICs must be convex; bundles with one
unattractive component showed concave ICs in primates (Pastor-Bernier et al. 2017). In
addition, IC convexity may be ascribed to concave utility of each bundle component (Perloff
2009); more of the same component (closer to IC x- or y-intercepts) has lower marginal gain,
and therefore the decision-maker is willing to trade in more of a component of which she has
much for one unit of the other component of which she has little. This may be the reason why
most participants showed convex ICs. Thus, the systematic estimates of the defining slope
and curvature coefficients suggest that the ICs reliably represented well-ordered preferences
for the milkshake bundles.

The estimating mechanism for BDM bids differed substantially from that underlying
revealed preference ICs. Both the auction-like bidding and the mechanics of cursor
movement differed from the choice between two simultaneously presented options. BDM
bidding is incentive compatible, such that erroneous or deceiving bids lead to suboptimal
outcome, as conceptualized by the expected cost of misbehaviour (Lusk et al. 2007); bidders
should state exactly their subjective value to avoid paying an exaggerated price or foregoing a
desired object. With these properties, BDM bidding constituted a well-controlled,
authoritative test for eliciting true subjective values, thus providing a useful validation
mechanism for preferences that were revealed by binary choice. Indeed, the obtained SVM-
and LDA-consistent BDM bids followed the preference scheme of ICs, namely higher bids
for revealed preferred bundles and similar bids with choice indifference despite varying
bundle composition. Most strikingly, hyperbolically fitted BDM isolines closely resembled
the hyperbolically fitted revealed preference ICs, both in terms of graphics and numeric
coefficients. The only notable difference was higher BDM bid variability. Our data align well
with, and extend, the previously noted correspondence between binary choices and BDM bids
for single-component options and bundle choices on paper or via verbal communication
(Roosen et al. 2017). Thus, the BDM estimating mechanism resulted in bids that
corresponded well to the graphic scheme of ICs conceptualized by Revealed Preference
Theory and thus validated our empirical IC assessments.
Methods

Participants. A total of 24 participants (11 males, 13 females; mean age 25.4 years, range 19-36 years) completed the binary choice task for measuring revealed preferences and performed the BDM control task. None of the participants had diabetes or lactose intolerance, nor did they require specific diets, to avoid medical and cultural interference. All participants had a known appetite for milkshakes and provided written informed consent based on a detailed information sheet. The Local Research Ethics Committee of the Cambridgeshire Health Authority approved the study.

Implementation of concepts. Revealed Preference Theory conceptualizes observable preference relationships between multi-component choice options. Decision makers reveal their preference at the moment of choice. We respected general notions of discrete choice models: the employed choice sets were exhaustive and had finite numbers of options (two), and their options were mutually exclusive. The statistical analysis of neural responses in humans and animals requires the use of multiple trials. Therefore, we used a version of Revealed Preference Theory in which preferences are stochastic (McFadden 2004). Thus, we assessed revealed preference from the probability of multiple choices, rather than by traditional single-shot economic tests. The probability of choosing one option over its alternative varies in a graded manner and thus is scalar. As in our parallel behavioural and neurophysiological work on monkeys (Pastor-Bernier et al. 2017; 2019), we implemented these concepts using the following notions (Fig. 1):

1) Participants made choices between two bundles that contained the same two distinct milkshakes in independently varying scalar amounts (component A, component B, each measured in ml; Fig. 1a). Thus, each choice option consists of a two-dimensional bundle vector. We kept effort cost for obtaining any bundle and budget constant for all choice options for better task control and data interpretation (single keyboard button press).

2) Revealed stochastic preference is inferred from the measured probability of repeated choice. The probability of choosing a given bundle depends on all components of all bundles present on that trial (as opposed to ‘lexicographic’ preferences that follow only one component) (Fig. 1b, c).

3) Equal choice probability for two bundles indicates equal revealed stochastic preference ($P = 0.5$ each bundle). The point at which both bundles are chosen with equal probability (point of subjective equivalence or choice indifference point, IP) is estimated from an S-shaped psychophysical function fitted to the probabilities of repeated choices while varying one component of one bundle and keeping all other components constant (Fig. 1c).

4) Every bundle has a subjective value (‘utility’) for the decision maker that depends only on the reward amounts of both milkshakes. A bundle is chosen with a higher probability than any other bundle in the same option set if and only if its utility is higher than in any other bundle in that choice set. In other words, the preference relationship between two bundles is monotone if the higher utility of one bundle implies that it is preferred to its alternative (Mas-Colell et al. 1995). A bundle is chosen with equal probability of $P = 0.5$ against another bundle if the two bundles have the same utility. Notions (2) - (4) are compatible with basic assumptions of stochastic choice theories (Luce 1959; McFadden & Richter 1990; McFadden 2004; Stott 2006) (although we analyzed the choices with the probit model rather than McFadden’s logit model because of its less restrictive assumptions; see below).

5) Each bundle is graphically displayed at the intersection of the x-coordinate (component A) and y-coordinate (component B) of a two-dimensional graph (Fig. 1d). Equally revealed preferred bundles are graphically represented as two-dimensional IPs and align on an indifference curve (IC) (Fig. 1e). Multiple IPs aligned on a single, continuous IC reflect the orderly and systematic emergence of scalar utility and choice probability from the vectorial bundle components.
(6) Bundles can be equally revealed preferred despite variation in bundle composition, such that some amount of one component is given up in order to gain one unit of the other component without change in preference (marginal rate of substitution, MRS). This trade-off is graphically characterized by two parameters: (i) the IC slope, which reflects the relative utility (currency) of the two bundle components and can be variable and asymmetric between x-axis and y-axis; (ii) the curvature, which captures any slope change between IC center and IC periphery (Fig. 1d).

(7) Bundles with larger amounts of both components are revealed preferred to bundles with smaller amounts (as long as the ‘value function’ for each component does not decrease with amount, indicating that ‘more is better’) (Fig. 1e). Any bundle that lies above an IC (farther away from the origin) is revealed preferred to any bundle that lies on that IC, any bundle that lies on an IC is revealed preferred to any bundle that lies below that IC (closer to the origin), and thus any bundle on a higher IC is revealed preferred to any bundle on a lower IC.

(8) The preference relationship between two bundles may hold even when one component of the revealed preferred bundle comes with a smaller amount than the alternative bundle (physical non-dominance, requiring overcompensation by the other bundle component) (Fig. 1e, arrows).

Experimental design. We measured repeated choices between two options, each of which contained two milkshakes; the liquids constituted rewards, as evidenced by the participants’ voluntary consumption. A more complete and traditional description of Revealed Preference Theory includes budget constraints (Mas-Colell et al. 1995); however, in this initial empirical study, we aimed to obtain as straightforward and easily interpretable empirical data as possible and therefore did not test aspects of budget constraint. In particular, the acquisition of any chosen bundle always required exactly one single finger movement (button press on a computer keyboard).

We used quantitative stimuli to represent the two milkshakes and their amounts in each of the two bundles (Fig. 1a). Each bundle stimulus consisted of two vertically aligned rectangles. The colour of each rectangle indicated the bundle component. After extensive piloting with various liquids and liquidized foods, we found milkshakes with a controlled mix of sugar and fat to give the most reliable behavioural performance. As the milkshakes were delivered separately, with a 500 ms interval (see below), drinks containing either only sugar or only fat were deemed to be too unnatural. Thus, in our bundles, component A (top, blue) consisted of a low-sugar high-fat milkshake (25% whole milk, 75% double cream, no sugar), and component B (bottom, red) consisted of a high-sugar low-fat milkshake (10% sugar in skimmed milk). The vertical position of a bar in each rectangle indicated the physical amount of each component (higher was more). The milkshakes were delivered using a custom-made syringe pump system with silicone tubing approved for delivery of food stuffs (VWR International Ltd). The pump was controlled using a National Instruments card (NI-USB-6009) via the Matlab Data Acquisition Toolbox. The Psychtoolbox in Matlab (Version R2015b) running on a Dell Windows computer served for stimulus display and recording of behavioural choices.

In the choice task, each participant revealed her preference in choices between the two composite stimuli representing the two bundles (Fig. 1a). The two bundle stimuli appeared simultaneously at pseudorandomly alternating fixed left and right positions on a computer monitor in front of the participant; each bundle stimulus contained the same two milkshakes with independently set amounts. Both bundle stimuli appeared after a short, pseudorandomly varying interval (mean 0.5 s) following an initial central fixation cross. The participant made a choice between the two bundle stimuli by pressing a single button once (left or right computer keyboard arrow for corresponding choice of left or right bundle). Reaction time was defined as the interval between the appearance of the two bundle stimuli and the participant’s key press. The two milkshakes from the chosen bundle were delivered together
with a probability of $P = 0.2$; i.e. every fifth chosen bundle was paid out on average using a Poisson distribution, and there was no payout of any milkshake on the remaining trials.

Constant B was delivered after a constant interval of 500 ms after component A. This constant delay, rather than simultaneous delivery or pseudo-randomly alternating sequential liquid delivery, prevented uncontrolled liquid interactions, maintained discriminability of the liquids and amounted to constant temporal discounting. Thus, the utility for component B derived not only from this milkshake alone but also from temporal discounting due to longer delay. Although participants were instructed to not eat or drink up to four hours prior to the testing, satiety was a concern due to the high sugar and fat content of the milkshakes. We addressed the issue by the $P = 0.2$ payout schedule, by limiting each payout to maximally 10.0 ml, and by delivering not more than 200 ml of total liquid to each participant on each session.

We used a standard psychophysical staircase procedure (Green & Swets 1966) to estimate the IP at which each of the two bundles were chosen with equal probability ($P = 0.5$ each option), revealing equal preference for each option. The procedure required repeated testing, which was also required for the subsequent neuroimaging experiment with the same participants (to be reported elsewhere).

We started the psychophysical procedure by setting, in the Reference Bundle, component A to 0.0 ml and component B to 2.0 ml, 5.0 ml or 8.0 ml (Fig. 1b). We then varied the alternative Variable Bundle in a systematic fashion; first, we set its component A one unit higher (mostly 0.5 ml, 1.0 ml or 2.0 ml higher), thus specifying the amount of component A gained by the participant from the choice; then we selected randomly (without replacement) one amount from a mean of 7 fixed amounts of component B (multiples of 0.5 ml), spanning the whole, constant range of tested amounts; we repeated the selection until all 7 amounts had been tested once (Fig. 1c). Then we estimated each IP from 6 repetitions using sigmoid fitting (see Eqs. 1, 2 below), requiring 42 choices per IP. At the IP, the amount of component B was usually lower in the Variable Bundle compared to the Reference Bundle. In this way, we assessed at each IP how much of component B the participant was willing to give up in order to gain one unit of component A, always relative to the constant Reference Bundle.

We obtained further IPs in choices between the constant Reference Bundle and the Variable Bundle whose amounts of component A increased step-wise, thus advancing from top left to bottom right on the two-dimensional x-y indifference map. We are aware that the unidirectional progression of testing may lead to somewhat different IP estimates than testing in the opposite direction or in random sequence (Knetsch 1989). However, in this initial study, we were primarily interested in the systematic assessment of consistent IPs rather than exploring potential pitfalls.

To obtain three levels of revealed preference, we used three starting amounts of component B in the Reference Bundle (2.0 ml, 5.0 ml, or 8.0 ml). In total, we estimated 4 IPs (from 5 test bundles) at each of 3 levels of revealed preference, resulting in a total of 12 IPs, derived from 504 choices among 84 different option sets in each participant (7 psychophysiologically tested amounts for each of 12 IPs; 6 repetitions).

**Statistical analysis.** In order to estimate the choice IPs numerically, we obtained a sigmoid fit to the empirically assessed choice frequencies via a general linear regression. To do so, we used the Matlab function `glmfit` (Matlab R2015b; Mathworks) on a binomial distribution with a probit link function, which is the inverse of the normal cumulative distribution function (G).

Specifically, the generalized linear regression $y = \beta_0 + \beta_1 \text{Bvar} + \varepsilon$ can be rewritten after applying the link function as:

$$G(y) = \beta_0 + \beta_1 \text{Bvar} + \varepsilon$$

with $y$ as number of times the subject chose the Variable Bundle in the current block from a series of six repetitions, $\beta_0$ as offset constant, $\beta_1$ as regression slope coefficient, Bvar as...
reward amount (ml) of component B in the Variable Bundle, and ε as residual error. We choose the probit model because it assumes that random errors have a multivariate normal distribution, which makes it attractive as the normal distribution provides a good approximation to many other distributions. The model does not rely on the assumption of error independence and is used frequently by econometricians (Razzaghi 2013). By comparison, the logit model is computationally simpler but has more restrictive assumptions of error independence. As preliminary data had revealed a similar fit for the logit as for the probit model we used the probit model due to its less restrictive assumptions. Thus, we estimated the IPs from the sigmoid fit provided by the probit model, using the following equation:

\[ \text{Indifference Point} = - \left( \beta_0 / \beta_1 \right) \quad \text{Eq. 2} \]

with \( \beta_0 \) and \( \beta_1 \) as coefficients of the general linear regression (Eq. 1). By using a probit instead of a logit function, we obtained the coefficients from the output of the probit analysis (Amemiya 1981).

We obtained single ICs, separately for each individual participant, from a set of individual IPs by weighted least-mean-square, non-linear regression (as opposed to the probit regression for estimating each IP). We applied a weight in order to account for within-participant choice variability; the weight was the inverse of the standard deviation of the titrated amount of the B-component at the corresponding IP (the IP having been estimated by the probit regression analysis). We estimated the best-fitting \( \beta \) coefficients from least-mean-square fitting to obtain the equal-revealed-preference IC (which is a utility level) and wrote the basic hyperbolic equation in our notation as:

\[ \text{IC} = \beta_0 + \beta_1 B + \beta_2 A + \beta_3 BA + \epsilon \quad \text{Eq. 3} \]

with A and B as amounts of components A and B (ml) referring to the x-axis and y-axis, respectively, \( \beta_1 \) and \( \beta_2 \) as slope coefficients of the least-mean-square, non-linear regression, and \( \beta_3 \) as curvature coefficients. As IC is a constant, we merged the other constants offset (\( \beta_0 \)) and error (\( \epsilon \)) into a common final constant k. To draw the ICs, we computed the amount of component B as a function of component A from the derived equation:

\[ B = k - (\beta_2 / \beta_1) A + \beta_3 A \quad \text{Eq. 3a} \]

To graphically display a fitted IC (Fig. 2a, b), we plotted the preset amount of component A on the x-axis, and the computed fitted amount of component B (Eq. 3a) on the y-axis. The error on the hyperbolic curve was measured as 95% confidence interval. The higher the error around an IP the less weight was given to this point when the IC was calculated. This model resulted in good fits in earlier work (Pastor-Bernier et al. 2017). In this way, the IPs of 5 equally revealed preferred but differently composed bundles aligned as a single fitted IC. The three ICs representing increasing revealed preference levels (low, medium, high) were located increasingly farther away from the origin (Figs. 1e; 2a, b). The indifference map of 3 x 5 IPs was unique for each participant (Fig. 3).

The IC shape is derived from the hyperbolic fit and is quantified by two coefficients: slope and curvature. The IC slope coefficient, derived from the ratio of regression slope coefficients (\( \beta_2 / \beta_1 \)), reflects the currency relationship between the components and describes the participant’s preference for component A relative to component B. For example, an IC slope of - 60° indicates that component A is valued twice as much as the same ml amount of component B. The curvature coefficient (\( \beta_3 \)) quantifies the constancy in the trade-off between bundle components. A linear curve (curvature coefficient = 0) indicates a constant rate of exchange for the bundle components, indicating that the components are perfect substitutes. A more convex IC (curvature coefficient > 0) indicates a varying rate of
exchange, suggesting that the participant is giving up lesser amounts of component B to obtain one unit of component A when advancing on the IC from top left to bottom right. For a more intuitive measure, we quantified the curvature by measuring the largest perpendicular distance between the IC and the line between the x-axis and y-axis intercepts (Fig. 2e):

\[ d = \text{max}(B_{IC} - B_{linearIC}) \]  

Eq. 4

with d as maximal perpendicular distance (ml) (whereas \( \beta_3 \) is a best-fitted, estimated parameter, and thus less conservative), \( B_{IC} \) as amount of component B on the IC (ml), and \( B_{linearIC} \) as amount of component B at the line connecting the x- and y-intercepts (constant amount of component A, x-axis; ml). This simple curvature measure indicates the effect of curvature on the trade-off between the two components, in ml of component B.

We used logistic regression on trial-by-trial choices to confirm that the measured choices were explained by bundle components rather than other factors. In a random-effects analysis, we fitted a logistic regression to the data from each individual participant and then averaged the obtained \( \beta \) coefficients and p-values across all participants. We used the following regression:

\[ y = \beta_0 + \beta_1 \text{RefB} + \beta_2 \text{VarA} + \beta_3 \text{VarB} + \beta_4 \text{RT} + \beta_5 \text{VarPos} + \beta_6 \text{PChoice} + \epsilon \]  

Eq. 5

with y as either 0 or 1 (not-choice or choice of Variable Bundle), A and B as amounts of bundle components A and B (ml), RefB as amount of component B in the Reference Bundle (ml), VarA and VarB as amount of components A and B in the Variable Bundle (ml), RT as reaction time (ms), VarPos as left or right position of the Variable Bundle on the computer monitor relative to the Reference Bundle (0 or 1), and PChoice as choice in the previous trial (0 or 1) (Fig. 2g). Each \( \beta \) coefficient was standardized by multiplication with standard deviation of the respective independent variable and division by standard deviation of y (dependent variable). A subsequent one-sample t-test against 0 served to assess the significance of the beta (\( \beta \)) coefficients in the population of the 24 participants.

Satiety may have occurred and could have affected the preferences for the two bundle components in an uncontrolled manner, even though the bundle rewards were only paid out on every fifth trial on average and were limited to a total of 200 ml. A prime suspected effect might have been a differential devaluation between the two bundle components that would result in changed currency relationship between the two components. Such change between the two components should be manifested as gradual change in instantaneous choice probability near the IPs over repeated test steps of 42 trials each (Extended Data Fig. 1). We calculated the instantaneous choice probability as:

\[ y = \sum_{n=1}^{6} (CV/TS) \]  

Eq. 6

with y as instantaneous probability (\( P = 0.0 \) to 1.0), CV as not-choice or choice of Variable Bundle (0 or 1), and TS as test step (1-6).

We used a leave-one-out analysis to assess the meaningful representation of revealed preferences by the fitted ICs and to test the accuracy of the hyperbolic IC fit to the IPs. In this analysis, we removed one IP per IC (but not the initial Reference Bundle set at \( x = 0 \)), fitted the curve again with the hyperbolic model and assessed the deviation between the original IC and the IC with the left-out IP. We defined the deviation as the difference of component B between the original, left-out IP and the refitted IC (Fig. 4b):

\[ d = B_{IP} - B_{refit} \]  

Eq. 7

with d as difference (in ml; y-axis), \( B_{IP} \) as amount of component B of the left-out IP (ml), and \( B_{refit} \) as amount of component B on the refitted IC (ml). Thus, a difference of 0 ml suggested
that removal of one IP did not affect the shape of the IC at all, whereas any difference unequal to 0 ml quantified the violation of this assumption.

Decoding of preference levels. To confirm the contribution of each IP to the two-dimensional representation of revealed preferences, we determined the accuracy (in percent correct) with which a randomly selected bundle, defined by the amounts of the two components A and B (in ml), could be assigned to its original revealed preference level as opposed to any one other level (binary distinction). By definition, each bundle that was psychophysically estimated to be as much revealed preferred as the Reference bundle constituted an IP; all bundles to which participants were choice indifferent against the same Reference Bundle constituted a series of IPs. In our experiment, three different Reference Bundles defined three preference levels (low, medium, high: component B: 2.0 ml, 5.0 ml or 8.0 ml, respectively; component A was always 0.0 ml; Fig. 5a). The decoder used as inputs only bundles at the psychophysically estimated IPs (to which an IC was fitted using Eqs. 3, 3a), rather than bundles positioned on the fitted ICs.

Our main test employed a binary support vector machine (SVM) decoder separately on each individual participant. We used similar methods as previously described for predicting choice from neuronal activity (Tsutsui et al. 2016). The SVM algorithm considered 5 IP bundles from each of 2 revealed preference levels (total of 10 IPs that had been assessed 12 times at each position in each participant) (Fig. 5a). Each of the 2 preference levels was associated with a matrix of 2 columns (containing the x- and y-coordinates of bundle components A and B, respectively) and 5 rows (containing the 5 bundles). The 5 bundles were randomly selected (with replacement) from 60 bundles on each level (due to the random procedure with replacement, some bundles may have entered the algorithm multiple times, and not all five bundles may have been used for a given analysis). We left out 1 randomly selected bundle from the 10 bundles, trained the SVM algorithm with the remaining 9 bundles, and assessed whether the SVM decoder assigned the left-out bundle to its original revealed preference level or to another level. Thus we used 90% of the data for training the decoder and 10% for testing its classification performance. We repeated this procedure 10 times with the same selected 2 x 5 bundles but with a new randomly selected left-out bundle and calculated decoder accuracy as percent correct classification in these 10 trials. We repeated the random selection of the 2 x 5 bundles and the 10-trial accuracy assessment 150 times. For final decoding accuracy, we averaged the percentages from these 150 iterations (Table 1). We applied this procedure separately to all three possible combinations of two revealed preference levels (i.e. low and medium, medium and high, low and high). The SVM was implemented with custom written software in Matlab R2015b (Mathworks) using the functions svmtrain and svmclassify with linear kernel (our previous work had shown that use of nonlinear kernels did not improve decoder performance; Tsutsui et al. 2016).

We supplemented the SVM procedure with binary linear discriminant analysis (LDA) that provided visualization of the different levels of revealed preference (Fig. 5). We used the same IPs and the same data matrices as for the SVM analysis (and the same IPs as used for the hyperbolic fitting of the three indifference curves, ICs). We obtained two variances; the discriminant 1 eigenvector captured the best separation between the three revealed preference levels as ’across-level variance’ (colors in Fig. 5); the discriminant 2 eigenvector captured the best within-level separation between five bundles on each of the three preference levels as ’within-level variance’ (symbols in Fig. 5). The results indicate visually the discrimination accuracy on the two axes of the 2-dimensional plots. We also assessed the numeric accuracy of decoding as percent of correctly assigning a randomly selected bundle to its original revealed preference level. The decoder used the Matlab functions fitcdiscr and predict on z-normalised data from individual participants. For the LDA, our limited data required pooling from multiple participants. As revealed preferences are private and subjective, and therefore difficult to compare between individual participants, the LDA results should be considered as merely supportive and not as stand-alone data.
Mechanism-independent validation of revealed preferences. To relate the estimated
revealed preferences to inferred utility, we implemented a Becker-DeGroot-Marschak (BDM)
mechanism akin to a second price auction (Becker et al. 1964). The BDM value bids were
then compared with the three levels of revealed preference within each participant.
In the BDM, the participant received a fresh monetary endowment (20 UK pence) on
each trial. The participant bid for a bundle against a pseudorandomly set computer bid
(retrieved from a normal distribution with replacement). If the participant’s bid was higher
than or equal to the computer bid then she received both component rewards of the bundle
and paid an amount equal to the computer bid. If her bid was lower than the computer bid,
she lost the auction, paid nothing and did not receive any bundle reward. The participant was
informed about a win or a loss immediately after placing the bid; when winning the bid, the
participant received the bundle rewards in the same sequence and frequency (every fifth trial
on average) as in the choice task assessing revealed preferences.
We showed each participant single bundles that were randomly selected (without
replacement) from a set of 15 bundles (5 equally revealed preferred bundles at each of 3
levels; the 15 bundles had been used to fit the 3 ICs shown in Fig. 2a, b and Fig. 3). A given
bundle was set to the participant’s psychophysically estimated IP (Fig. 6a). We presented each
of the 15 bundles 12 times, resulting in 180 trials in total, and considered the mean of these
bids as the BDM-estimated utility. The participant indicated her bid by moving a cursor
horizontally on the computer monitor with left and right keyboard arrows (Fig. 6a inset). The
BDM bid was registered from the cursor position at 5.0 s after onset of presentation of the
horizontal bidding scale.
We first assessed the basic question whether the monetary bids increased for higher
valued bundles but were similar for equally valued bundles (which constituted IPs), using
Spearman rank correlation analysis confirmed by one-way Anova with post-hoc Tukey-
Kramer test. Then we performed a random-effects analysis with a general linear regression
with a normal (Gaussian) link function on separate data from each participant and averaged
the obtained β coefficients and their p-values across participants. We used the following
regression:
\[ y = \beta_0 + \beta_1 \text{PrefLev} + \beta_2 \text{AmBundle} + \beta_3 \text{TrialN} + \beta_4 \text{PrevBid} + \beta_5 \text{Consum} + \varepsilon \quad \text{Eq. 8} \]
with y as monetary bid, PrefLev as revealed preference level (low, medium, high), AmBundle
as summed ml amount of components A and B in the currency of component A (A + (k -
(β2/β1)A + β3A) as in Eq. 3a), TrialN as trial number, PrevBid as BDM bid in previous trial
(£UK pence), and Consum as accumulated drinks consumption for component A and
component B up to this point in the experiment (ml) (Fig. 6c). Each β coefficient was
standardized by multiplication with standard deviation of the respective independent variable
and division by standard deviation of y (dependent variable). A subsequent one-sample t-test
against 0 assessed the significance of the beta (β) coefficients in all 24 participants.
To assess the internal consistency of BDM bids, we used binary SVM analysis on bids
from individual participants in analogy to SVM decoding of preference levels. We tested the
same IPs as used for hyperbolic IC fitting (Fig. 6a). Each of the 2 preference levels was
associated with a matrix of 1 column (containing the bids to each bundle) and 5 rows
(containing the 5 bundles). The remainder of the bundle selection, leave-out and repetition
procedure was identical to that used for the SVM decoding of preference levels (see above).
Thus, the SVM decoder for BDM bids assessed the accuracy with which the left-out bundle
belonged to its original revealed preference level. We supplemented the SVM analysis of the
BDM bids with analogous LDA for supportive visualization.
Finally, we compared hyperbolically fitted BDM isolines directly with hyperbolically
fitted revealed preference ICs (rather than with revealed preference levels just described),
separately for each individual participant. This procedure required to present BDM bids on
the same scale as revealed preference ICs. To this end, we fitted isolines of same BDM-bids
in analogy to fitting same-preference ICs. We fitted a hyperbolic function to the measured
mean BDM bids in analogy to Eq. 3:

\[ \text{BDMBid} = \beta_0 + \beta_1 B + \beta_2 A + \beta_3 BA + \epsilon \]  
Eq. 9

with \( \beta_1 \) and \( \beta_2 \) as regression slopes, and \( \beta_3 \) as curvature coefficients, and A and B as amounts
of components A and B (ml), respectively. Coefficients \( \beta_1 \) and \( \beta_2 \) were standardized by
multiplication with standard deviation of components B and A, respectively (independent
variables), and division by standard deviation of BDMBids (dependent variable). We obtained
separate \( \beta \) coefficients from all participants and averaged them and their p-values across
participants. A subsequent one-sample t-test used the individual beta (\( \beta \)) coefficients from all
24 participants to test overall significance against 0.

To compare BDM bids with ICs, we graphically displayed BDM isolines along which
all mean BDM bids were equal. As a BDM isoline is a constant, we merged the constants
offset (\( \beta_0 \)) and error (\( \epsilon \)) into a common final constant \( k \). To draw the BDM isolines, we
computed the amount of component B as a function of component A from the derived
equation:

\[ B = k - \left( \frac{\beta_2}{\beta_1} \right) A + \beta_3 A \]  
Eq. 9a

To display a three-dimensional map, we graphed colored BDM isoline zones on the z-axis as
a function of the amounts of components A (x-axis) and B (y-axis) (Fig. 7a). For a two-
dimensional map of BDM isolines, we plotted the preset amount of component A on the x-
axis and the amount of component B computed from the isolines (Eq. 9a) on the y-axis (Fig.
7b). For comparison, we plotted the revealed-preference ICs on the same two-dimensional
map using the same scale. We also compared numerically, separately for each participant,
confidence intervals and slope and curvature coefficients between hyperbolically fitted
BDMBids (Eq. 9a) and hyperbolically fitted revealed preference ICs (Eq. 3a), using the
paired Wilcoxon test (Fig. 7c-e).

Data availability: Data are available from the authors upon reasonable request. A Reporting
Summary for this article is available as a Supplementary Information file.
Fig. 1 | Binary choice task and experimental design. 

a. Bundle stimuli for binary choice. Each bundle contained two components with amounts between 0.0 and 10.0 ml. Component (Comp) A: low-sugar high-fat milkshake, Comp B: high-sugar low-fat milkshake. Participants chose between the Reference Bundle and the Variable Bundle, whose locations on a computer monitor alternated pseudorandomly between fixed left and right positions.

b. Psychophysical test design. In the Reference Bundle, components A and B were set to 0.0 ml and 8.0 ml, respectively; in the Variable bundle, component A was set to a specific test amount while the amount of component B was psychophysically varied (dashed arrows).

c. Psychophysical assessment of two example choice indifference points (IP; choice probability P = 0.5 each option; yellow and green) in a typical participant. During repeated trials, the participant chose between the preset Reference Bundle and the Variable Bundle. Component A of the Variable Bundle was set to specific test amounts (here 0.5 ml and 2.0 ml, respectively). Component B of the Variable Bundle varied between seven randomly selected amounts of component B. IPs were estimated from choice probabilities, p (Bundle 1) and p (Bundle 2), respectively, using the probit model (Eqs. 1, 2).

d. Schematic indifference curve (IC), fitted by a hyperbola (Eqs. 3, 3a) to all equally revealed preferred but differently composed bundles. Yellow and green dots show IPs relative to the bundle marked by blue dot, as estimated in B, C.

e. Schematic map of three ICs. Increasing distance from origin represents higher utility; all bundles on higher ICs are revealed preferred to all bundles on lower ICs. Heavy dots denote a preference relationship between two bundles with oppositely varying physical amounts of component A (top-IC bundle is revealed preferred to mid-IC bundle despite lower physical amount of component A; partial physical non-dominance).

Fig. 2 | Empirical indifference curves (IC) representing revealed preferences.

a. Typical convex ICs from an example participant, as seen in 18 of the 24 participants. Component A was a low-sugar high-fat milkshake; component B was a high-sugar low-fat milkshake. Solid lines show hyperbolically fitted ICs, dotted lines show 95% confidence intervals of fits. Dots show bundles that are equally preferred on the same IC (IPs). Inset: psychophysical assessment of indifference point (IP) marked on highest IC (test points in blue, IP estimated by probit regression in red).

b. Typical linear ICs from another example participant, as seen in 6 of the 24 participants.
c, d. Distributions of slope and curvature, respectively, of hyperbolically fitted ICs from all 24 participants (coefficients β2 / β1 and β3 in Eq. 3, respectively). N = number of participants.

E. Scheme of intuitive numeric assessment of IC curvature: maximal vertical distance (ml of component B on y-axis) between fitted IC (curve) and a straight line connecting the x-axis and y-axis intercepts. A distance of > 0.0 ml indicates convexity, whereas a 0.0 ml distance indicates perfect linearity.

f. Distribution of convex curvature, as measured using the scheme shown in E. The two peaks indicate six participants each with similarly near-linear ICs and similarly convex ICs, respectively.

g. Specificity of bundle choice, as opposed to unrelated parameters. Bar graph showing standardized beta (β) regression coefficients for choice of Variable Bundle over Reference Bundle (Eq. 5), derived from each individual participant and averaged across all 24 participants. RefB, component B in Reference Bundle; VarA and VarB, components A and B in Variable Bundle; RT, reaction time; VarPos, left-right position of Variable Bundle stimulus; PChoice, choice in previous trial. Error bars show standard error of the mean (SEM). *P ≤ 0.02.
Fig. 3 | **Empirical indifference curves (IC) from all 24 participants.** Note the fanning out of the confidence intervals towards the bottom right in each graph (thin lines), which likely reflects the progression of choice testing: the Reference Bundle was kept constant at the y-axis intercept \((x = 0)\), whereas testing with the Variable Bundle progressed from top left to bottom right. Same conventions as for Fig. 2.

Fig. 4 | **Leave-one-out validation of estimated indifference curves (ICs).**

a, Graphic assessment with an example participant: hyperbolically refitted ICs with one left-out indifference point (IP) (solid lines), plotted together with 95% confidence intervals of the original hyperbolically fitted ICs (dotted lines). The refitting resulted in 4 new ICs (partly overlapping) at each of three levels. None of the refitted IPs fell outside the original confidence intervals.

b, Scheme of numeric assessment: distance in ml (in ml on y-axis, red) between the left-out IP on the original IC (heavy black dot on black curve) and the refitted IC (green).

c, Histogram of distance between refitted ICs and left-out IPs across all subjects. Skewness was -0.12, suggesting rather symmetric distribution around the mean (modeled in red).

Fig. 5 | **Visualization of bundle decoding using Linear Discriminant Analysis (LDA).**

a, Schematics of bundle decoding at psychophysically estimated points of equal revealed preference (indifference points, IPs, plotted along the dotted lines). Following the notions of revealed preference, LDA should show accurate decoding across the three preference levels (green, blue, red) but not along each level.

b, LDA bundle distinction between three levels of revealed preference (81-100% binary numeric decoding accuracy between two levels; first discriminant) but not along same preference levels (second discriminant) in \(N = 80\) bundles from six participants (6P) with similar convex ICs (same convention applies to all panels). Bundles on the three preference levels are colored blue, green and red according to distance from origin, red being highest. The five bundles on each preference level are marked from top left to bottom right with ‘○’, ‘⋆’, ‘+’, ‘x’ and ‘□’ symbols. Due to the arbitrariness of the scale, numbers are not indicated.

c, As b but for partly physically non-dominating bundles (one lower component in preferred bundle than in alternative bundle (97-100% accuracy; first discriminant).

d, As b but for six participants with linear ICs (90-100% accuracy).

e, As d but for partly physically non-dominating bundles (96-100% accuracy).

f, As b but for all 24 participants (18 with convex IC, six with linear ICs) (83-100% accuracy).

g, As f but for partly physically non-dominating bundles (97-100% accuracy).

Fig. 6 | **Characteristics of BDM bids for bundles at different revealed preference levels.**

a, Schematics of positions of bundles used for eliciting BDM bids at psychophysically estimated points of equal revealed preference (indifference points, IPs, plotted along the dotted lines). Following the notions of trade-off and increasing revealed preference, BDM bids should be similar for equally valued bundles (along the dotted lines) but higher for revealed preferred bundles (farther away from origin). We tested 5 bundles per level, 3 levels, 12 repetitions, total of 180 bids. Inset: BDM task. Each participant bid for the visually presented two-component (A, B) bundle by moving the black dot cursor using the leftward and rightward horizontal arrows on a computer keyboard. Numbers indicate example bids (in UK pence).

b, Mean BDM bids from a typical participant. The bids were rank ordered (Spearman Rho = 0.83, \(P < 0.001\)) across bundles positioned on increasing indifference curves (blue, green, red) and failed to overlap between lowest, medium and highest levels. There was a significant difference for BDM bids between levels but not within levels (*\(P < 0.001\); two-way Anova followed by Tukey-Kramer test). Data are shown as mean ± SEM (standard error of the mean), \(N = 12\) bids per bar.
c, Specificity of monetary BDM bids, as opposed to unrelated parameters. Bar graph showing the standardized beta ($\beta$) regression coefficients for BDM bids (Eq. 8), derived from each individual participant and averaged across all 24 participants. Abbreviations: PrevLev, revealed preference level (low, medium, high); AmBundle, summed currency-adjusted amount of both bundle components; TrialN, trial number; PrevBid, BDM bid in previous trial; Consum, accumulated drinks consumption. Error bars show SEMs. * $P < 0.020$.

d) Visual decoding by Linear Discriminant Analysis (LDA) of BDM bids for bundles on different preference levels (first discriminant; 88-100% numeric decoding accuracy; $P = 9.46 \times 10^{-12}$) and along same preference levels (second discriminant; 43-51% accuracy) ($N = 243$ bundles; all 24 participants). The LDA used scalar BDM bids for bundles positioned at IPs shown in Fig. 6a. Same conventions as for Fig. 5a.

Fig. 7 | Comparison between BDM bids and indifference curves (IC).

a, Three-dimensional representation of hyperbolically fitted BDM isolines from a typical participant (mean ± SEM). The BDM bids were made for bundles that had been placed on psychophysically estimated revealed preference indifference points (black dots). The BDM isolines were similar along same levels and increased across revealed preference levels.

b, Match between hyperbolically fitted isolines of mean BDM bids (black; Eqs. 9, 9a) and hyperbolically fitted revealed preference ICs (blue, green, red; ± 95% confidence intervals, CI, shaded) from a typical participant. Thus, the BDM isolines fell within the respective CIs of the revealed preference ICs.

c, Confidence intervals of fitted BDM isolines (red) and revealed preference ICs (blue) from all 24 participants (averaged along each isoline/IC). The larger 95%CIs of BDM isolines (BDMiso) suggest more variability compared to revealed preference ICs.

d, e, Comparison of slope and curvature coefficient estimates, respectively, between BDM isolines (red) and revealed preference ICs (blue; same data as shown in Fig. 2c, d) from all 24 participants.
Table 1. Decoding accuracy, as assessed with support vector machine.

| Participant | Bundles | BDM bids |
|-------------|---------|----------|
|             | Lev1 vs. Lev2 | Lev2 vs. Lev3 | Lev1 vs. Lev2 | Lev1 vs. Lev3 | Lev2 vs. Lev3 |
| C – convex IC | 83.9 | 99.8 | 68.8 | 70.6 | 81.0 | 54.4 |
| L – linear IC | 86.8 | 99.5 | 68.7 | 44.0 | 51.0 | 47.4 |
| C1          | 72.7 | 96.0 | 58.7 | 56.6 | 71.3 | 59.3 |
| C2          | 88.0 | 99.5 | 67.6 | 67.7 | 76.3 | 62.5 |
| C3          | 99.1 | 100.0 | 81.4 | 64.8 | 69.9 | 49.8 |
| C4          | 93.7 | 99.5 | 61.9 | 53.5 | 65.9 | 54.0 |
| C5          | 66.2 | 75.5 | 49.5 | 70.0 | 72.2 | 43.6 |
| C6          | 72.9 | 81.8 | 52.6 | 49.8 | 67.2 | 62.6 |
| C7          | 80.0 | 100.0 | 80.0 | 68.4 | 83.8 | 62.1 |
| C8          | 99.6 | 100.0 | 69.8 | 47.0 | 46.6 | 43.7 |
| C9          | 90.2 | 99.5 | 55.4 | 68.9 | 75.7 | 53.1 |
| C10         | 96.8 | 100.0 | 71.2 | 47.3 | 57.9 | 47.1 |
| C11         | 86.1 | 87.7 | 56.7 | 58.7 | 60.9 | 48.2 |
| C12         | 80.0 | 100.0 | 80.0 | 63.2 | 74.3 | 56.8 |
| C13         | 99.8 | 100.0 | 85.5 | 67.8 | 78.6 | 54.8 |
| C14         | 100.0 | 100.0 | 90.0 | 57.8 | 62.5 | 50.4 |
| C15         | 100.0 | 100.0 | 100.0 | 44.8 | 70.9 | 68.4 |
| C16         | 99.9 | 99.9 | 55.3 | 68.1 | 75.3 | 51.7 |
| C17         | 100.0 | 100.0 | 88.6 | 43.5 | 65.8 | 59.6 |
| C18         | 100.0 | 100.0 | 95.9 | 69.2 | 84.9 | 70.1 |
| L19         | 100.0 | 100.0 | 83.6 | 62.2 | 66.0 | 44.4 |
| L20         | 100.0 | 100.0 | 100.0 | 54.8 | 52.5 | 45.9 |
| L21         | 100.0 | 100.0 | 100.0 | 63.2 | 58.4 | 47.8 |
| L22         | 100.0 | 100.0 | 80.0 | 61.4 | 68.5 | 57.7 |

Accuracy is shown in % of numbers of bundles and BDM bids correctly assigned to one of the two tested revealed preference levels (averages from 150 iterations of classification of 10 pseudorandomly selected bundles / BDM bids from two tested revealed preference levels). Bundles were tested at psychophysically assessed choice indifference points (IP) on one of three revealed preference levels (corresponding to the three indifference curves, IC, fitted to the IPs). The tested bundles had been pseudorandomly selected from 5 unique estimated IPs on each of two revealed preference levels under study. BDM: Becker-DeGroot-Marschak auction-like bidding mechanism. Lev1, Lev2, Lev3: revealed preference levels, numbered according to distance from origin. The 24 participants were labelled as C or L according to their IPs being fitted best to convex or linear ICs.
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Author contributions
K. V., A. P.-B., F. G. and W.S. designed the research, K. V. performed the experiments, K. V., A. P.-B. and A.S. analyzed the data, K. V. and W.S. wrote the manuscript.

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EXTENDED DATA

Extended Data Fig. 1 | Satiety control.

A, Choice function obtained by sigmoid fit with the probit model. From seven randomly selected fixed amounts of component B in the Variable Bundle, the two colored dots show two amounts associated with choice probabilities closest to the indifference point (IP).

b, Lack of satiety across typical test duration. Choice probabilities varied insignificantly above (blue) and below (orange) the IP across six repeated choice steps, using 42 trials at each step. Data were averaged from all 24 participants. The total duration of the six steps was 20 ± 1.38 minutes (mean ± SEM).
Figure 1
**Figure 2**

- **A**: Graph showing the relationship between Component A (ml) and Component B (ml) with lines indicating different Beta values.
- **B**: Similar graph to **A** but focusing on Attribute B (ml).
- **C**: Histogram showing the distribution of Slope with bars indicating frequency.
- **D**: Histogram showing the distribution of Curvature with bars indicating frequency.
- **E**: Graph showing the relationship between Component B (ml) and Component A (ml) with bars indicating Vert dist (ml).
- **F**: Bar graph showing the distribution of Beta (standardized) with error bars indicating variability.
- **G**: Bar graph showing the distribution of different variables with error bars indicating variability.
Figure 3

Component A (ml)

Component B (ml)
Figure 5

A. Graph showing Component B (ml) vs. Component A (ml).

B. Convex ICs with N=80 in 6P.

C. Convex ICs with N=54 in 6P.

D. Linear ICs with N=74 in 6P.

E. Linear ICs with N=53 in 6P.

F. All ICs with N=243 in 24P.

G. All ICs with N=192 in 24P.

Legend:
- Convex ICs
- Linear ICs
- All ICs

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Figure 6

A. BDM Bidding

B. BDM Bids (pence)

C. Beta (standardized)

D. Second linear discriminant

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Figure 7

(A) 3D scatter plot showing the relationship between Component A and BDM bids. The plot includes a trend line and error bars.

(B) Graph showing the frequency of Component B (ml) against Component A (ml). The graph includes multiple lines for different conditions.

(C) Bar chart showing the frequency of Confidence Interval (ml) with two conditions: ICs and BDMiso.

(D) Graph showing the number of participants against Slope. The graph includes bins for different slope values.

(E) Graph showing the number of participants against Curvature. The graph includes bins for different curvature values.
