A Revised ΛCDM Mass Model for the Andromeda Galaxy

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ABSTRACT

We present an updated mass model for M31 that makes use of a Spitzer 3.6 μm image, a mass-to-light ratio gradient based on the galaxy’s B − R colour profile, and observed rotation curve data from a variety of sources. We examine cases where the dark matter follows a pure NFW profile and where an initial NFW halo contracts adiabatically in response to the formation of the galaxy. We find that both of these scenarios can produce a reasonable fit to the observed rotation curve data. However, a pure NFW model requires a concentration c_vir = 51 that is well outside the range predicted in ΛCDM cosmology and is therefore disfavoured. An adiabatically contracted NFW halo favors an initial concentration c_vir = 20 and virial mass 8.2 × 10^{11} M_☉, and this is in line with the cosmological expectations for a galaxy of the size of M31. The best-fit mass is consistent with published estimates from Andromeda Stream kinematics, satellite galaxy radial velocities, and planetary nebulae studies. Finally, using the known linear correlation between rotation curve shear and spiral arm pitch angle, we show that the stellar spiral arm pitch angle of M31 (which cannot be deduced from imaging data due to the galaxy’s inclination) is P = 24°7 ± 4°4.

Key words: dark matter — galaxies: fundamental parameters — galaxies: haloes — galaxies: individual (M31) — galaxies: spiral — galaxies: structure

1 INTRODUCTION

Modelling the mass distribution of M31 is a classical problem that has seen many past iterations (e.g., Einasto 1972; Kent, Huchra & Stauffer 1989; Klypin, Zhoa & Somerville 2002; Widrow, Perrett & Suyu 2003; Geehan et al. 2006). Recently, a Spitzer 3.6 μm mosaic image of M31 has become available (Barmby et al. 2006). This allows for a more accurate determination of the baryonic mass distribution in M31 than has been determined previously. Accurate mass modelling of M31 is an important tool for both exploring our ideas of cosmology, and for understanding the dynamics of newly discovered Local Group dwarf galaxies (e.g., Majewski et al. 2007; Chapman et al. 2007).

Because M31 can be studied in exquisite detail, it provides a crucial testing ground for our ideas of galaxy formation (Kent 1989; Evans & Wilkinson 2000). A problem of particular relevance for Cosmological constant plus Cold Dark Matter (ΛCDM) cosmology is the Tully-Fisher zero-point problem, which refers to the fact that standard models cannot reproduce the relation between galaxy luminosity and circular velocity (Tully & Fisher 1977) without overproducing the number density of galaxies at fixed luminosity (e.g., Gonzalez et al. 2000; Cole et al. 2000; Benson et al. 2003; Yang, Mo & van den Bosch 2003). Another problem of related concern is the cusp/concentration problem – namely that dark-matter dominated galaxy rotation curves seem to rise more slowly than predicted in ΛCDM (Moore 1994; Flores & Primack 1994; Moore et al. 1999; van den Bosch & Swaters 2001; Blais-Ouellette, Amram & Carignan 2006; Alam, Bullock & Weinberg 2002; Swaters et al. 2003; Simon et al. 2005; Dutton et al. 2005; Kuzio de Naray et al. 2006). It remains to be seen whether these problems point to some unaccounted for process in galaxy formation (e.g. Dutton et al. 2007) or to some new physics of cosmological relevance (Kaplinghat, Knox & Turner 2000; Zentner & Bullock 2002; Kaplinghat 2005; Cembranos et al. 2005; Strigari, Kaplinghat & Bullock 2007; Gnedin et al. 2007).

Recently, Dutton et al. (2007) and Gnedin et al. (2007) revisited the Tully-Fisher problem using two large well-defined samples of disc-dominated (late-type) galaxies. They both took as a starting point the “standard” model of disc
formation, which assumes that initial Navarro, Frenk & White (1997; hereafter NFW) dark haloes respond to disc formation via adiabatic contraction (AC) (Blumenthal et al. 1986; Gnedin et al. 2004; Sellwood & McGaugh 2005; Choi et al. 2006). Both groups conclude that the Tully-Fisher zero point cannot be explained if initial NFW haloes have concentrations as high as those expected for ΛCDM with $\sigma_8 \approx 0.9$ (with $c \sim 12$ for M31-size haloes, e.g. Bullock et al. 2001a, Macciò et al. 2006). Both sets of authors agree that the problem could be alleviated if AC did not operate (e.g. Somerville & Primack 1999) and Dutton et al. (2007) go on to advocate a model where disc formation induces an expansion in the underlying halo density structure. In contrast, Gnedin et al. (2007) argue that AC is a fundamental prediction in galaxy formation and instead suggest that the cosmology be changed to favor lower halo concentrations (e.g. Zentner & Bullock 2002) or that the IMF is lighter (with a stellar mass-to-light ratio $M_*/L$ lower by 0.15 dex) than the standard Kroupa (2001) assumption.

Given the fundamental issues at hand, the question of whether AC occurs in nature is of significant interest. Theory certainly favours the idea that haloes contract. Indeed, halo contraction must occur when the infall of baryons is smooth and adiabatic (e.g. Blumenthal et al. 1986; Ryden & Gunn 1987; Sellwood & McGaugh 2005) and simulations suggest that dark haloes will contract even when galaxies or galaxy clusters form quickly from an irregular collapse (Barnes 1987; Flores et al. 1993; Jesseeit, Naab & Burkert 2002; Gnedin et al. 2004; Sellwood & McGaugh 2005; Choi et al. 2006; Weinberg et al. 2008). On the other hand, there is very little observational evidence that halo contraction actually occurs in nature. For example, Zappacosta et al. (2006) performed a detailed XMM study of the radio-quiet galaxy cluster Abell 2589 and conclude that an NFW halo + AC model cannot explain the data but that a pure NFW halo provides a remarkable fit down to $\sim 1$% of the halo’s virial radius. Similarly, an investigation of seven elliptical galaxies with Chandra by the same group (Humphrey et al. 2006) finds that AC degrades the mass profile significantly unless strong deviations from a Kroupa IMF are allowed. Also, Kassin, de Jong & Pogge (2006a) and Kassin, de Jong & Weiner (2006b) found that the rotation curves of 32 out of 34 of the bright spiral galaxies they study are better fit without adiabatic contraction.

Klypin et al. (2002) have shown that the observed rotation curve of M31 is best explained with a halo model that includes AC. However, other recent M31 mass modelling papers (e.g., Widrow et al. 2003; Geehan et al. 2006) have not directly addressed the question of AC. Furthermore, M31 is essentially the only well-studied galaxy that has been shown to require AC (Klypin et al. 2002). Most other dynamical studies of galaxies tend to disfavour AC (e.g., Kassin et al. 2006a, b). Given the availability of a Spitzer 3.6 μm image, it is now appropriate to revisit this question and test the conclusion that M31 requires AC. In what follows we show that the rotation curve of M31 can only be explained without AC if an unusually high NFW concentration, $c_{\text{vir}} \sim 50$, is adopted. Such a concentration is well outside the range expected in ΛCDM haloes, and therefore this model is disfavoured. Moreover, the best-fit AC model has a slightly high NFW concentration, $c_{\text{vir}} = 20$, for typical, $\sigma_8 = 0.9$, ΛCDM haloes (Bullock et al. 2001a, Macciò et al. 2006), but it is within 1.5σ of the expected value for an M31 size halo. We speculate on the implications of these results in the conclusion section.

Our approach is unique compared to other recently published mass profiles derived from modelling the rotation curve of M31. While our method bears most similarity to that adopted by Klypin et al. (2002), we use an updated baryonic mass component, which is derived using a 3.6 μm Spitzer image. Geehan et al. (2006) used a pure NFW halo profile, and did not consider AC. Tempel et al. (2007) also use the 3.6 μm Spitzer image, yet once again, AC is not considered. Lastly, Widrow et al. (2003) used a different functional form for the halo density profile (see Evans 1993). The Evans profile is based upon an isothermal distribution function. Unlike the NFW profile, the Evans profile was not derived by fitting models to dark matter haloes produced in ΛCDM simulations. Widrow et al. (2003) then go on to fit an NFW model to their best-fitting Evans (1993) model. However, we have chosen to use the cosmologically motivated NFW halo density profile model directly.

Throughout this paper we assume a flat ΛCDM cosmology with $\Omega_m = 0.27$ and a Hubble constant of $H_0 = 75$ km s$^{-1}$ Mpc$^{-1}$. We relate virial masses ($M_{\text{vir}}$) and radii ($R_{\text{vir}}$) assuming a virial over-density relative to average of $\Delta_{\text{vir}} = 34^{1/3}$. At times we quote baryon fractions relative to the universal value with $f_b = \Omega_b/\Omega_m = 0.16$. We adopt a distance of 784 kpc to M31 (Holland 1998). As a result, an angular distance of 1′ is equivalent to a distance of 228 pc.

2 DATA

We make use of the Spitzer/IRAC 3.6 μm image of M31 (Barmby et al. 2006). The IRAC observations of M31 were taken as part of Spitzer General Observer program 3126 in 2005 August. Fifteen Astronomical Observation Requests (AORs) were used to map a region approximately $3.7 \times 1.7^\circ$ on the sky. The central $1.6 \times 0.4^\circ$ was covered by three AORs, each having two 12 s frames per position. The outer regions were covered by two AORs, each with two dithered 30 s frames per position. The pixel scale of IRAC at 3.6 μm is $0.12 \text{arcsec}$. The 3.6 μm filter is 1.2 μm broad, spanning the wavelengths 2.965–4.165 μm. For a description of the IRAC instrument see Fazio et al. (2004).

The Spitzer data are preferred over 2MASS $K_s$-band data for a few reasons. The regular 2MASS $K_s$-band image is simply not deep enough to obtain an accurate bulge/disc decomposition. Furthermore, this same 2MASS image suffers from over subtraction of the sky by about 0.5 magnitudes (T. Jarrett, private communication). A 6×2 2MASS $K_s$-band image is also available (where the data were observed with an integration time 6 times longer than the regular 2MASS survey), but it is only about 1 magnitude deeper and also hampered by uncertain sky background. The Spitzer image has a larger field of view, better depth, and a more accurate determination of the sky level.

We also use the $B - R$ colour profile of Walterbos &
Kennicutt (1987), in order to determine the stellar mass-to-light ratio as a function of radius. We have corrected this $B - R$ profile for Galactic foreground extinction, which is $E(B - V) = 0.062$ mags in the direction of M31 (Schlegel, Finkbeiner & Davis 1998). This is converted to a correction for the $B - R$ colour by using the transformation, $E(B - R) = 1.64E(B - V)$ from Schlegel et al. (1998), i.e. $E(B - R) = 0.102$ for M31. As a comparison the amount of extinction at 3.6 $\mu$m is 1.5 per cent of that at $B$, and about 34 per cent of that in the $K_s$ band.

We adopt the rotation curve data from several sources. In one case (M1) we adopt the H$\alpha$ rotation data out to 25 kpc from Rubin & Ford (1970$^2$) and extend the rotation curve to 35 kpc using HI data from Carignan et al. (2006). In another case (M2) we use the CO rotational velocities from Loinard, Allen & Lequeux (1995) and the HI from Brinks & Burton (1984) to construct an observed rotation curve out to a 30 kpc radius. This was the rotation curve adopted by Klypin et al. (2002) in their M31 model. We adopt M1 as our fiducial case here because Rubin & Ford published errors on their observed velocities. However, as we show below, both cases yield consistent results. In both cases we take into account the presence of a $10^7 M_\odot$ supermassive black hole (Bender et al. 2005) and the HI gas distribution (Carignan et al. 2006).

3 MASS MODELLING OF M31

3.1 The baryonic contribution

Our goal is to determine the best possible mass model for M31. We perform a bulge-disc decomposition in order to estimate the baryonic contribution to the rotation curve. We then determine several possible mass models. The best fit model is determined by minimizing the reduced-$\chi^2$ in a fit to the observed rotation curve.

We first extract the surface brightness profile of M31 using the Spitzer 3.6 $\mu$m image and the IRAF ellipse routine, which fits ellipses to an image using an iterative method described by Jedrzejewski (1987). In order to mask out foreground stars and satellite galaxies SExtractor (Bertin & Arnouts 1996) was used. An inclination correction was then applied to the surface brightness profile (see de Jong 1996; Seigar & James 1998a) as follows

$$\mu_i = \mu - 2.5C \log \left( \frac{a}{b} \right)$$

where $\mu_i$ is the surface brightness when viewed at some inclination, $i$, $\mu$ is the corrected surface brightness, $a$ is the major axis, $b$ is the minor axis and $C$ is a factor dependent on whether the galaxy is optically thick or thin; if $C = 1$ then the galaxy is optically thin; if $C = 0$ then the galaxy is optically thick. Since we are using infrared data, the correction for inclination is small, and in many cases completely ignored (see e.g. Seigar & James 1998a; de Jong 1996). However, Graham (2001) showed that $C = 0.91$ is a good typical value to use for the near-infrared $K_s$-band. If one adopts a simple reddening law, where extinction falls as the square of wavelength, then the value of $C = 0.97$ is appropriate at 3.6 $\mu$m, and we adopt this value here.

The resulting surface brightness profile (Figure 1) reaches a surface brightness of $\mu_{3.6} \sim 21.2$ mag arcsec$^{-2}$ at a radius of 15. This is very similar to the surface brightness found by Barnby et al. (2006). Furthermore, the PN counts of Merrett et al. (2006) predict an R band surface brightness of $\sim 23.8$ mag arcsec$^{-2}$. At these radii the metallicity of M31 is 0.4 Z$_\odot$ (Brewer, Richer & Crabtree 1995; Worthey et al. 2005). Using the Maraston (2005) population synthesis codes, one can see that the expected R-[3.6] color at this radius is $R-[3.6] \sim 2.5$, very similar to our measured surface brightness.

From this surface brightness profile, we perform a one-dimensional bulge-disc decomposition, which employs the Sérsic model for the bulge component and an exponential law for the disc component (e.g. Andredakis et al. 1995; Seigar & James 1998a; Khoroshalii, Wadadekar & Kernbahi 2000; D’Onofrio 2001; Graham 2001b; Möllenhoff & Heidt 2001; see also Graham & Driver 2005 for a review). The Sérsic (1963, 1968) $R^{1/n}$ model is most commonly expressed as a surface brightness profile, such that

$$\mu(R) = \mu_e \exp \left\{ -b_n \left( \frac{R}{R_e} \right)^{1/n} - 1 \right\},$$

where $\mu_e$ is the surface brightness at the effective radius $R_e$ that encloses half of the total light from the model (Ciotti 1991; Caon, Capaccioli & D’Onofrio 1993). The constant $b_n$ is defined in terms of the parameter $n$, which describes the overall shape of the light profile. When $n = 4$ the Sérsic model is equivalent to a de Vaucouleurs (1948, 1959) $R^{1/4}$

![Figure 1. The Spitzer 3.6 $\mu$m surface brightness profile of M31 (without correction for inclination) with decomposition into bulge and disc components. The bulge has been fitted with a Sérsic model (short dashed line) and the disc has been fitted with an exponential model (long dashed line).](image-url)
model and when \( n = 1 \) it is equivalent to an exponential model. The parameter \( b_n \) has been approximated by \( b_n = 1.9992n - 0.3271 \), for \( 0.5 < n < 10 \) (Capaccioli 1989; Prugniel & Simien 1997). The exponential model for the disc surface brightness profile can be written as follows,

\[
\mu(R) = \mu_0 \exp\left(-\frac{R}{h}\right),
\]

(3) where \( \mu_0 \) is the disc central surface brightness and \( h \) is the disc scale length. Our bulge-disc decomposition ignores the inner 4\arcsec of M31, which is dominated by an independent nuclear feature (Light, Danielson & Schwarschild 1974). The results of the bulge-disc decomposition can be seen in Figure 1. Note that although there appears to be a slight break in the disc surface brightness profile at \( \sim 4000'' \), the residuals are still very small. This break may appear due to the presence of spiral structure, evident at similar radii in the 24 \( \mu \)m of M31. Observational properties of M31 are derived from this bulge-disc decomposition and these are listed in Table 1.

With a disc scalelength of 25.92\arcmin and a surface brightness profile extending to a radius of 1.5, we are tracing the disc profile out to \( \sim 3.5 \) scalelengths. Assuming that the exponential disc profile extrapolates to infinity, our profile includes 86.1 per cent of the total disc light. Below, where we assign a mass to the disc, we extrapolate the disc profile to 6 scalelengths, which would contain 98.2 per cent of the disc light. Since Ibata et al. (2005) have shown that the disc of M31 extends to very large radii (\( \sim 70 \) kpc) with the same scalelength, our above calculation assumes no disc truncation. Both the 10 kpc ring and the 2.6 kpc bar (Beaton et al. 2007) show up as small perturbations in the surface brightness profile (Fig. 1) at radii of 46.67\arcsec and 26.67\arcsec respectively.

We now assign masses to the disc and bulge of M31. The stellar mass-to-light ratio in the \( K_s \)-band is a well-calibrated quantity (see Bell et al. 2003) which depends on \( B - R \) colour. However, a similar calibration does not exist for the Spitzer 3.6 \( \mu \)m waveband. An alternative method would be to estimate the \( K_s \)-band surface brightness profile, given the 3.6 \( \mu \)m profile, and since we know the \( B - R \) colour profile, we have chosen to determine the \( K - [3.6] \) colour dependence on \( B - R \) colour using both the Bruzual & Charlot (2003; hereafter BC03) stellar population synthesis models and the Maraston (2005; hereafter M05) stellar population synthesis models (Left Panel) and Maraston (2005) population synthesis models (Right Panel). In both cases, dashed lines represent a constant age stellar population and solid lines represent constant metallicity. The dotted lines represent the typical \( B - R \) colour of the inner disc \( (B - R = 1.79) \) and the outer disc \( (B - R = 1.40) \) from Walterbos & Kennicutt (1987).
synthesis models. The BC03 models use the stellar library of Pickles (1998), which includes stars in a wide range of spectral types (05-M10) and luminosity classes (I-V) and three metallicity groups (metal poor, metal rich and solar). The Pickles (1998) library has wavelength coverage from 0.1 \( \mu m \) to 2.5 \( \mu m \). BaSeL 3.1 spectra (see BC03 Tables 2 and 3) are then used to extend the Pickles (1998) spectra into the infrared from 2.5 \( \mu m \) to 160 \( \mu m \). The spectra of M giant stars are the only ones not observed in the Pickles (1998) library. As a result the BC03 models use synthetic M giant spectra calculated by Fluks et al. (1999), which cover a spectral range from 0.5 \( \mu m \) to 25 \( \mu m \). BaSeL 3.1 spectra (see BC03 Tables 2 and 3) are calculated by Fluks et al. (1999). These spectra are extended into the infrared using the model atmospheres of Schultheis et al. (1999), which cover a spectral range from 0.5 \( \mu m \) to 10 \( \mu m \), and 10 equally spaced stellar temperatures in the range 2600 < \( T_{eff} < 4400 \) K. The main difference between the BC03 and the M05 models is the way in which thermally-pulsing AGB (TP-AGB) stars are treated. The M05 models provide a better treatment of TP-AGB stars than the BC03 models. Furthermore, Maraston et al. (2006) find that in general the M05 models provide better fits to observations of infrared spectra of galaxies than the BC03 models. They indicate systematically lower ages and, on average, masses that are 60 per cent lower for the stellar population samples in these galaxies.

Table 1. M31 Observational Data. Hubble type taken from de Vaucouleurs et al. (1991). Distance in kpc taken from Holland et al. (1998).

| Parameter | Measurement |
|-----------|-------------|
| Hubble type | SA(s)b |
| Distance (kpc) | 784 |
| Position Angle of major axis (degrees) | 45 |
| Bulge effective radius, \( R_e \) (arcmin) | 8.45±0.43 |
| Bulge effective radius, \( R_e \) (kpc) | 1.93±0.10 |
| Bulge surface brightness at the effective radius, \( \mu_e \) (3.6 \( \mu m \)-mag arcsec\(^{-2} \)) | 16.42±0.83 |
| Bulge Sérsic index, \( n \) | 1.71±0.11 |
| Disc central surface brightness, \( \mu_0 \) (3.6 \( \mu m \)-mag arcsec\(^{-2} \)) | 17.35±0.93 |
| Inclination corrected disc central surface brightness, \( \mu_0 \) (3.6 \( \mu m \)-mag arcsec\(^{-2} \)) | 18.94±0.93 |
| Disc scalelength, \( h \) (arcmin) | 25.92±1.28 |
| Disc scalelength, \( h \) (kpc) | 5.91±0.27 |
| Disc luminosity, \( L_{disc} \) (\( L_\odot \)) | (6.08±0.60)×10\(^{10} \) |
| Bulge-to-disc ratio, \( B/D \) | 0.57±0.02 |

Table 1 shows the result of both the BC03 (left panel) and M05 (right panel) models. In both cases, the dotted lines in Figure 2 represent the \( B-R \) colour of the inner and outer disc of M31 (Walterbos & Kennicutt 1987 and Figure 3) after correction for Galactic foreground extinction. Since the M05 models provide an updated treatment of TP-AGB stars and generally provide better fits to observations than the BC03 models, from here on we concentrate on the M05 results. However, it is interesting to note that the \( K-[3.6] \) colour index predicted by the BC03 and M05 models differs by <0.03 mag (see Figure 2). Lines of constant metallicity (solid lines) and age (dashed lines) are shown. The typical metallicity in the inner few kpc of M31 is ~2.4 \( Z_\odot \), whereas in the outer disc this falls to ~0.4 \( Z_\odot \) (Brewer, Richer & Crabtree 1995; Worthey et al. 2005). From this metallicity gradient and the M05 models (Figure 2 right panel) it can be seen that the \( B-R \) colour gradient in M31 is almost entirely due to changes in metallicity, and that the \( K-[3.6] \) colour difference is < 0.1 mag. Furthermore, we can now use the \( B-R \) gradient (Figure 3) and the metallicity gradient of M31 to estimate the \( K-[3.6] \) colour as a function of radius. We find that the inner region of M31 has a colour \( K-[3.6] \) ≃ 0.25, and the outer disc (at 26 kpc) has a colour \( K-[3.6] \) ~ 0.18. Given the \( B-R \) colour profile and the K-band mass-to-light ratio calibration from Bell et al. (2003) we calculate a central mass-to-light ratio, \( M/L_K = 1.0 \pm 0.1 \) and a mass-to-light ratio at 26 kpc, \( M/L_K = 0.75 \pm 0.1 \). From the \( K-[3.6] \) colours determined in our stellar population synthesis analysis, the above mass-to-light ratios are equivalent to 3.6 \( \mu m \) mass-to-light ratios of \( M/L_{3.6} \approx 1.25 \pm 0.10 \) in the centre and \( M/L_{3.6} \approx 0.89 \pm 0.10 \) at 26 kpc (equivalent to a \( M/L \) gradient 0.13 kpc\(^{-1} \)). In our analysis, we prefer to keep the central \( (M/L_{3.6}) \) value a free parameter, and as such we allow it to vary in the range 0.05 < \( (M/L_{3.6}) < 1.5 \). This is a standard approach to adopt in mass modelling of galaxies (see Humphrey et al. 2006; Zappacosta et al. 2006) and as discussed at the end of section 3.2 and shown in Table 2, when the \( M/L_{3.6} \) is left as a free parameter, the best-fit value found is \( M/L_{3.6} = 1.15 \), i.e. consistent with the value of \( M/L_{3.6} \) derived here. We use our derived value for the 3.6 \( \mu m \) disc luminosity of \( L_{3.6} = (6.08 \pm 0.60) \times 10^{10} L_\odot \). We then use the derived disc and bulge light profiles \( L_{3.6} = L_{disc} + L_{bulge} \) to determine the stellar mass contribution to the rotation curve, \( M_* = (M/L_{3.6})L_{3.6} \).

A concern in using the 3.6 \( \mu m \) Spitzer waveband to determine the underlying stellar mass, is the effect of emission from hot dust in this waveband, although this is probably only important in or near HII regions. In order to place some constraint on this, we have chosen to explore the emission from dust in the near-infrared K-band at 2.2 \( \mu m \). Using near-infrared spectroscopy at 2.2 \( \mu m \) it has been shown that hot dust can account for up to 30 per cent of the continuum light observed at this wavelength in areas of active star formation, i.e., spiral arms (James & Scigar 1999). When averaged over the entire disc of a galaxy, this reduces to a <2 per cent effect, if one assumes that spiral arms can be up to 12° in width. At 3.6 \( \mu m \) this would therefore result in <3 per cent of emitted light from dust.

Another concern for the 3.6 \( \mu m \) waveband, would be the contribution from the Polycyclic Aromatic Hydrocarbon (PAH) emission feature at 3.3 \( \mu m \). However, ISO spectra
covering the wavelength range 5.15 to 16.5 μm have shown that PAH emission in M31 seems to be very weak (e.g., Ce

sarsky et al. 1998). Furthermore, in a survey of actively star forming galaxies, Helou et al. (2000) found that the 3.3 μm feature was also very weak when they analysed the average 2.5 – 11.6 μm spectrum of 45 galaxies. The contribution of the PAH feature to the 3.6 μm Spitzer waveband, is therefore not a major concern.

In the following section, where we model the dark matter halo, we have included a bulge surface brightness model using a deprojected Sérsic function. The function we use is from Trujillo et al. (2002) who show that the deprojected ter halo, we have included a bulge surface brightness model for not a major concern.

\[ \rho(R) = \frac{I(0) h^2 n^{-1/2}}{R e n \pi} \sqrt{\frac{h^2}{1 - C(h)}} \]

(4)

where \( R_e \) is the effective radius, \( I(0) \) is the central intensity, \( \bar{Y} \) is the stellar mass-to-light ratio, \( h = R/R_e \), \( C(h) = h_1 (\log h)^2 + h_2 \log h + h_3 \) and \( K_{\nu} \) is the \( \nu \) th-order modified Bessel function of the third kind. Trujillo et al. (2002) give values for \( \nu, p, h_1, h_2 \) and \( h_3 \) for different values of the Sérsic parameter, \( n \). In our case, where \( n = 1.71 \), we adopt values of \( \nu = 0.45394, p = 0.67930, h_1 = -0.0162935, h_2 = -0.18161 \) and \( h_3 = 0.04435 \). Finally, the constant \( f^{1/2} \) depends on the three-dimensional spatial orientation of the bulge. In our case, we assume the bulge is intrinsically spherical, and therefore \( f^{1/2} = 1 \).

It should be noted that this version of the deprojected Sérsic function (equation 4) is an approximation, but it is good enough for our purposes.

### 3.2 Modelling the dark matter halo

A range of allowed dark matter halo masses and density profiles are now explored, using two models for disc galaxy formation. In the first we assume that the dark matter halo surrounding M31 has not responded significantly to the formation of the disc, i.e., adiabatic contraction does not occur (the “no-AC” model). In this case the dark matter contribution to the rotation curve is described by a density profile similar to those found in dissipationless dark matter simulations (the NFW profile):

\[ \rho(R) = \frac{\rho_s}{(R/R_s)(1 + R/R_s)^2} \]

(5)

where \( R_s \) is a characteristic “inner” radius, and \( \rho_s \) is a corresponding inner density. This is a two parameter function and is completely specified by choosing two independent parameters, e.g., the virial mass \( M_{\text{vir}} \) (or virial radius \( R_{\text{vir}} \)) and concentration \( c_{\text{vir}} = R_{\text{vir}}/R_s \) (see Bullock et al. 2001a for a discussion). Similarly, given a virial mass \( M_{\text{vir}} \) and the dark matter circular velocity at any radius, the halo concentration \( c_{\text{vir}} \) is completely determined.

In the second class of models we adopt the scenario of adiabatic contraction (AC) and specifically use the original scheme discussed by Blumenthal et al. (1986, hereafter B86; see also Bullock et al. 2001b and Pizagno et al. 2005). We also investigate the slightly revised scheme presented in Gnedin et al. (2004, hereafter G04). As we discuss below, the G04 scheme reproduces the outer slope of the observed rotation curve of M31, but needs a very high concentration to do so.

For each AC algorithm (B86 and G04) and for the no-AC model we generate a grid of final rotation curves. We vary the baryonic contribution to the rotation curve by allowing the bulge-disc decomposition parameters for \( h \) and \( L_{\text{disc}} \) to range over their ±2σ values (see Table 1 and the previous section). The central mass-to-light ratio of the galaxy is allowed to vary over the range 0.05 < (\( M/L \)) < 1.5. From this we determine the bulge and disc contribution to the rotation curve. For the bulge a simplified spherical model is used. For the disc the potential is derived assuming zero thickness and modified Bessel functions as described by Binney & Tremaine (1987). For each set of baryonic parameters we generate a range of dark halo models with total circular velocities at 2.2 disc scalelength \( V_{2,2} \) that span the best-fit value for M31 \( (V_{2,2} = 270 \text{ km s}^{-1}) \) quoted by Rubin & Ford (1970) by a wide margin: 200 < \( V_{2,2} < 340 \text{ km s}^{-1} \). In practice we achieve each \( V_{2,2} \) value in our models by allowing the initial halo concentration to vary over > 4σ of its expected range \( c_{\text{vir}} \) = 3 – 60 (Bullock et al. 2001a; Wechsler et al. 2002; Macciò et al. 2006) and then setting the halo virial mass \( M_{\text{vir}} \) necessary to reproduce the desired value of \( V_{2,2} \). Finally, we determine the implied fraction of the mass in the system in the form of stars compared to that expected from the Universal baryon fraction, \( f_s = M_*/(f_b M_{\text{vir}}) \) and demand that \( f_s \) obeys 0.01 < \( f_s < f_b \). From this grid of choices we derive best fitting dark halo parameters by minimizing the reduced-\( \chi^2 \) for our two choices of rotation curve data. These results are summarized in Table 2.

For the most part, when minimizing \( \chi^2 \), we assume that the errors on the observational data (i.e., the rotation velocities) are not correlated. Instead we assume that they are Gaussian in nature. However, this is not the case for the Carignan et al. (2006) HI data (see Figure 4 top row and bottom right beyond 25 kpc), where the errors obviously are correlated. In order to account for the strange behaviour of the errors on these HI rotation velocities we have treated all of this data as an average rotation velocity of 226.3 km s\(^{-1}\) at 31.16 kpc. This is an idealized simplification but allows a quantitative estimate of the relative goodness of fit between models. Furthermore, although error bars are not available for the “M2” curve, we assume 10 per cent errors in the model fitting, as this is similar to the size of the errors quoted for the Rubin & Ford (1970) Hα rotation curve. We therefore quote a \( \chi^2 \) for the “M2” curve in Table 2 that is consistent with 10 per cent errors. We then determine how consistent all the derived rotation curves are with each other, by adopting the formal best fitting rotation curve as our fiducial mass model. For our “M1” curve, the number of degrees of freedom in the fit is \( \nu = 31 \). The number of data points we fit to is \( n_{\text{data}} = 37 \), and 6 parameters are determined from the fit, the NFW concentration \( c_{\text{vir}} \), the halo virial mass \( M_{\text{vir}} \), the stellar mass-to-light ratio \( M/L \), the disc luminosity \( L_{\text{disc}} \), the disc scalelength \( h \) and the bulge-to-disc ratio \( B/D \), thus leaving the degrees of freedom in the fit as \( \nu = 31 \).

The M1 rotation curve from Rubin & Ford (1970) is shown by the solid squares with error bars in Figure 3 (top left, top right, middle right, bottom left) along with our best-fitting rotation curve models (solid lines). The contribution from stellar mass (short-dashed) and dark matter (long-dash) in each case is shown along with the rather minor con-
Figure 4. Top left: Rotation curve data (solid square points) from Rubin & Ford (1970) with the best fit model, with adiabatic contraction (M1 B86 model), overlaid (solid line). For comparison the HI rotation velocities (grey open triangles) from Carignan et al. (2006) are shown (the black point corresponds to the average velocity and radius of the Carignan data that we make use of). The best fit rotation curve is decomposed into four components, the contribution from dark matter (short-dashed line), the contribution from baryonic matter (long-dashed line), the HI contribution (dotted line) from Carignan et al. (2006) and the contribution from the central $10^8 M_\odot$ black hole (dot-dashed line) from Bender et al. (2005). Middle left: Rotation curve CO and HI data (solid square points) from Loinard et al. (1995) and Brinks & Burton (1984) respectively, as used by Klypin et al. (2002). The best fit model with adiabatic contraction (M2 B86 model) is overlaid (solid line). It is decomposed into four components as in the top left panel. Bottom left: Rotation curve data from Rubin & Ford (1970; solid points) and Carignan et al. (2006; triangles) and the data as used by Klypin et al. (2002; hollow circles), with adiabatic contraction model (M1+M2 B86), overlaid. Top right: The same as the top left panel, but with the best fitting model using a modified version of adiabatic contraction (M1 G04 model) as in Gnedin et al. (2004). The long-dashed curve includes the total baryonic mass, including the HI mass and the central black hole. Middle right: The same as the top left panel, but with the best fitting model without an adiabatically contracted halo (M1 no-AC model). In all five cases the NFW concentration, $c_{\text{vir}}$, and virial mass, $M_{\text{vir}}$, are shown.
Table 2. M31 best fitting models. “M1 B86” is the best-fit model to the Hα rotation curve from Rubin & Ford (1970) (M1) using the AC prescription of B86. “M2 B86” is the best-fit B86 model to a combination of the CO rotation velocities from Loinard et al. (1995) and the H1 velocities from Brinks & Burton (1984) (M2). “M1+M2 B86” is the best-fit B86 model to the Hα rotation curve from Rubin & Ford (1970) (M1) combined with the CO rotation velocities from Loinard et al. (1995) and the H1 velocities from Brinks & Burton (1984) (M2). “M1 G04” corresponds to the M1 data fit using the modified adiabatic contraction model of Gnedin et al. (2004) and “M1 no-AC”, uses the same data without adiabatic contraction.

| Parameter                                      | M1 B86 | M2 B86 | M1+M2 B86 | M1 G04 | M1 no-AC |
|------------------------------------------------|--------|--------|-----------|--------|---------|
| Shear                                          | 0.51   | 0.50   | 0.51      | 0.54   | 0.50    |
| $V_{2.2}$ (km s$^{-1}$)                        | 275±5  | 275±5  | 275±5     | 275±5  | 275±5   |
| Disc luminosity, $L_{\text{disc}}$ ($L_{\odot}$) | $(4.9 \pm 0.6) \times 10^{10}$ | $(6.1 \pm 0.6) \times 10^{10}$ | $(5.5 \pm 0.6) \times 10^{10}$ | $(4.9 \pm 0.6) \times 10^{10}$ | $(6.1 \pm 0.6) \times 10^{10}$ |
| Disc scale length, $h$ (kpc)                   | 5.09±0.06 | 5.91±0.06 | 5.50±0.06 | 5.50±0.06 | 5.91±0.06 |
| Central disc mass-to-light ratio, $M/L$ (3.6 $\mu$m solar units) | 1.15±0.10 | 1.00±0.10 | 1.05±0.10 | 1.05±0.10 | 0.95±0.10 |
| Mass-to-light ratio gradient, $d(M/L)/dR$ (kpc$^{-1}$) | 0.013 | 0.013 | 0.013 | 0.013 | 0.013 |
| Initial NFW concentration, $c_{\text{vir}}$     | 20.0±1.1 | 16.0±1.1 | 18.0±1.1 | 40.0±1.1 | 51.0±1.1 |
| Bulir-to-disc ratio, $B/D$                      | 0.57±0.02 | 0.57±0.02 | 0.57±0.02 | 0.57±0.02 | 0.57±0.02 |
| Virial mass, $M_{\text{vir}}$ ($M_{\odot}$)    | $(8.2 \pm 0.2) \times 10^{11}$ | $(8.5 \pm 0.2) \times 10^{11}$ | $(8.4 \pm 0.2) \times 10^{11}$ | $(8.9 \pm 0.2) \times 10^{11}$ | $(7.3 \pm 0.2) \times 10^{11}$ |
| Dark matter concentration, $c_{\text{DM}}$, $R < 10$ kpc | 14.9±1.4% | 14.4±1.5% | 14.7±1.5% | 9.9±1.3% | 14.1±2.0% |
| Total mass concentration, $c_{\text{tot}}$, $R < 10$ kpc | 26.2±2.5% | 25.4±2.4% | 25.9±2.4% | 23.8±2.7% | 26.5±2.6% |
| Stellar baryon fraction, $f_*$                 | 56.7±3.9% | 59.2±4.5% | 58.1±4.2% | 56.3±6.0% | 63.5±5.6% |
| $\chi^2$                                      | 38.75  | 40.63  | 80.31     | 46.50  | 41.58   |
| Degrees of freedom, $\nu$                     | 31     | 27     | 64        | 31     | 31      |

Overlaid in the top left panel of Figure [4] is a model that includes adiabatic contraction (overall reduced-\(\chi^2 = 1.25\)). The dark halo in this case has undergone adiabatic contraction according to the B86 prescription. Our best-fitting parameters are summarized in Table 2 under “M1 B86”. We determine the halo of M31 to have a total (dark+baryonic) virial mass of $M_{\text{vir}} = (8.2 \pm 0.2) \times 10^{11} M_{\odot}$ and an initial concentration $c_{\text{vir}} = 20.0 \pm 1.1$. Our derived virial mass is almost a factor of 2 smaller than that quoted by Klypin et al. (2002). We also find a concentration that is higher than both Klypin et al. (2002), who find $c_{\text{vir}} = 12$ and Widrow et al. (2003), who find $c_{\text{vir}} = 10$. In the case of Widrow et al. (2003) it should be noted that they initially fit an isothermal model given by Evans (1993). They then fit an NFW profile to this model. Given that the isothermal model favors a constant density core, the derived NFW concentration will be artificially low and fitting an NFW model in a more direct manner may result in a higher concentration.

The model rotation curve fits the data adequately within the uncertainties. The innermost data point from the observational rotation curve is significantly lower than the model. This can be explained by the recent strong evidence for a bar, which dominates the near-infrared light out to a radius of $\sim 2.6$ kpc; in M31 (Athanassoula & Beaton 2006; Beaton et al. 2007). This bar has been used to explain the minimum seen in the observed rotation curve at a radius of $\sim 2.7$ kpc (Athanassoula & Beaton 2006). This bar may also affect the outer rotation velocities as well, although probably by less than 10 per cent. This would therefore be within the errors associated with the observed data. Indeed, shifting the outer rotation velocities systematically upward by $\sim 10$ per cent changes the best-fit models by an amount that remains within the quoted error range of the original fit (see Table 2). It should also be noted that by a radius of $25-35$ kpc the rotational velocity has dropped to $\sim 225 - 230$ km s$^{-1}$, which is similar to the rotational velocities seen at radii of $25-35$ kpc in the H1 rotation curve (Carignan et al. 2006; open triangles).

The best-fitting model without adiabatic contraction is shown by the solid line in the middle right panel of Figure [4]. This, the no-AC model, was determined in exactly the same way as our best-fit B86 AC model. As listed in Ta-
モデル、からの集中度に対する最低値。成功したフィット "M1 B86" と \( \chi^2 \) の制約を決定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仮定する。初期 NFW 実験値が保持していると仯
et al. (2007) make use of a model that is similar to a S´ersic model. The more recent models by Tamm et al. (2007) and Tempel give Klypin et al. (2002) an overall more massive bulge.

The use of the $M/L$ ratio is probably due to a combination of the fact that they are consistent with those from the more recent Hα rotation curves of Brinks & Burton (1984) to find their best fitting model a combination of data from Rubin & Ford (1970) and Klypin et al. (2002) we also find a best-fitting rotation curve consistent with our fiducial case. More importantly, if we try and fit our analysis. First, Klypin et al. (2002) use the Hα rotation curve of Brinks & Burton (1984) to find their best fitting model to the Rubin & Ford (1970) rotation curve around our best fitting model. This may be because the overall bulge mass does not change; it is just the way in which the bulge mass is distributed that changes.

The issue of turbulent gas motions is very important for low-mass galaxies with small rotation velocities (e.g., Valenzuela et al. 2007), as this requires a correction for pressure support or asymmetric drift in the mass model. The correction to the total mass is $\sim (\sigma_{\text{gas}}/V_{\text{rot}})^2$. Since the Hα and HII region rotation curves are derived from gas, it is important to understand what effect the turbulent gas motions may have on our mass model. Since, M31 is a galaxy with a high rotation velocity ($\sim 275$ km s$^{-1}$) and a turbulent velocity dispersion in galaxy discs is typically $<30$ km s$^{-1}$ (i.e. around 10 per cent of the rotation velocity) this effect is small. Indeed, if we assume that the scatter of the Hα rotation curve is derived from Hα spectroscopic observations of individual HII regions in M31. In this case, we have to assume that the errors on the Rubin & Ford (1970) rotation curve are uncorrelated, and we derive a turbulent velocity dispersion of $\sigma_{\text{gas}} = 18.3$ km s$^{-1}$. Adding this in quadrature to the maximum rotation velocity from the Rubin & Ford (1970), results in a mass difference of $\sim 0.4$ per cent for the total (baryonic + halo) galaxy mass.

As mentioned above, the preferred total (dark+baryonic) virial mass for M31 is $(8.2 \pm 0.2) \times 10^{11} M_{\odot}$. This is similar to the estimate of $\sim (7.9 \pm 0.5) \times 10^{11} M_{\odot}$ derived from satellite kinematics (Côté et al. 2000) and the total mass of $\sim 8 \times 10^{11} M_{\odot}$ from kinematics of the Andromeda Stream (Fardal et al. 2006; Geehan et al. 2006). It is also close to the lower limit of $9 \times 10^{11} M_{\odot}$ derived from kinematics of halo stars (Chapman et al. 2006). Our favored virial mass is about a factor of 2 smaller than the value favored by the Klypin et al. (2002) analysis of the M31 rotation curve. This can be attributed to three differences in our analysis. First, Klypin et al. (2002) use the H1 rotation curve of Brinks & Burton (1984) to find their best fitting model. In this study we use the Hα rotation velocities of Rubin & Ford (1970). However, we find that this is not the major driver. We find that the model rotation velocities are consistent with those from the more recent H1 study of Carignan et al. (2006), and when we fit to the same observed rotation curve as Klypin et al. (2002), we find that our best-fit model is consistent with our best-fit model to the Rubin & Ford (1970) curve. Furthermore, if we try and model a combination of data from Rubin & Ford (1970) and Klypin et al. (2002) we also find a best-fitting rotation curve consistent with our fiducial case. More importantly, Klypin et al. (2002) used the $M/L$ ratios of Bell & de Jong (2002) to determine the stellar mass from their bulge-disc decomposition. In this study we allow $M/L$ to vary freely in the range $0.05 < (M/L) < 1.50$, and find a best-fitting value close to the expected 3.6 $\mu$m mass-to-light ratios (see section 5.3).

![Figure 6. Enclosed mass as a function of radius for model M1 B86. The solid line indicates the total mass. Also indicated are the HI mass out to a 35 kpc radius (dotted line), the bulge+BH mass (short-dashed line), the disc mass (long-dashed line) and the halo mass (dot-dashed line). The data points indicate masses derived using other observational methods at fixed radii of 10 kpc, 31 kpc, 35 kpc and 125 kpc from Rubin & Ford (1970), Evans & Wilkinson (2000), Carignan et al. (2006) and Fardal et al. (2006) respectively.](image-url)
Klypin et al. (2002) perform a bulge-disc decomposition using an R band image, whereas we use a Spitzer 3.6 µm image. Using a 3.6 µm image provides a better trace of the stellar mass (e.g., Barnby et al. 2006 and references therein). Overall, we should therefore have a more accurate estimate of the baryonic mass profile in M31. Indeed, if we adopt the baryonic mass profile of Klypin et al. (2002) and try to fit either to the H I or to the Hα rotation curve, we find a best fitting model that is consistent with their result.

Typically, the best-fitting M/L values we find are in the range 0.95–1.15, depending on the model used. The lowest value of M/L = 0.95 is difficult to reconcile with the expected value, which is M/L = 1.2 ± 0.1, for a galaxy with the central B – R colour of M31. This expected value was determined by combining the Bell et al. (2003) Kσ-band M/L with the K−[3.6] colours derived from our stellar population synthesis described in section 3.1 (Figure 2). The lowest value we find (M/L = 0.95) is for our no-AC model. We also find that this model is difficult to explain in the context of ΛCDM cosmology, due to its large concentration. Our M1 B86 model reproduced the highest value of M/L = 1.15 that we find. This is consistent with the expected range of M/L values.

4 SUMMARY

In this paper we have derived new mass models for M31, based on an updated baryonic contribution to the rotation curve. The baryonic contribution is derived using a Spitzer 3.6 µm image. We find that both a pure NFW and an adiabatically contracted NFW profile can produce reasonable fits to the observed rotation curve of M31. However, the best-fit concentration of M31 for a pure NFW model is c_{vir} = 51 ± 1.1, which is disfavoured when compared to the expected value of log_{10}(c_{vir}) = 2.0 ± 0.14 (Wechsler et al. 2002; Maccio et al. 2006) in a ΛCDM cosmology (our best fitting concentration is a 4.0σ outlier). The best fit produced by the AC recipe of Gnedin et al. (2004) brings down the concentration to c_{vir} = 40, or log_{10}(c_{vir}) = 1.60, and is thus marginally consistent with ΛCDM as a ~3.7σ outlier. If one accepts ΛCDM cosmology, then the most consistent fit to the observed rotation curve seems to be that produced by the AC recipe of Blumenthal et al. (1986). In this case the concentration, c_{vir} = 20 ± 1.1, and this is consistent with the expectations of ΛCDM, to within 1.5σ.

For all of the types of model we use, the derived best-fits are in good agreement with the mass distributions derived from various other observational methods. Our estimate of the halo virial mass lies in the range M_{vir} = (7.3 ± 0.2) × 10^{12} M_{⊙} (for the M1 no-AC case) and M_{vir} = (8.9 ± 0.2) × 10^{12} M_{⊙} (for the M1 G04 case). This is in close agreement with the virial mass of ~8 × 10^{12} M_{⊙} found via kinematics of satellite galaxies (Côté et al. 2000) and the Andromeda Stream (Fardal et al. 2006; Gehan et al. 2006), and the lower limit of 9 × 10^{12} M_{⊙} found from kinematics of halo stars (Chapman et al. 2006). Our M1 B86 model, which is in closest agreement with the expectations of ΛCDM, lies in the middle of the range with a virial mass of M_{vir} = 8.2 ± 0.2 × 10^{11} M_{⊙}.

Another recent M31 mass model by Tam & Tempel & Tenjes (2007) and Tempel, Tamm & Tenjes (2007) also uses Spitzer 3.6 µm imaging to determine the total mass of M31, and they find a mass of 1.1 × 10^{12} M_{⊙} for a pure NFW model, i.e. a slightly higher mass than for our best fit. However, they did not look at the question of AC. Also, their bulge seems to have a more concentrated density profile (see Figure 6 in Tempel et al. 2007), which is probably driven by the use of rotation velocities inside 5 kpc. This may be driving the differences between our model and the model presented in Tempel et al. (2007). We have been cautious not to include rotation data within the inner few kpc in our model, since it is unclear how non-circular motions induced in this barred region will affect the overall mass model.

It is interesting that, while it has been shown that adiabatically contracted halo models do not generally fit the observed rotation curves of galaxies (e.g. Dutton et al. 2005, 2007; Kassin et al. 2006a, b; Pizagno et al. 2005), the observed rotation curve of a well-studied galaxy such as M31 can be well described by a halo that has undergone adiabatic contraction. Indeed, one either has to adopt (i) a pure NFW profile with an unphysically large concentration, within the context of ΛCDM, or (ii) an adiabatically contracted NFW profile and a more reasonable concentration. Such a scenario is in agreement with the results of Klypin et al. (2002), who claim that an adiabatically contracted halo is favoured for M31.

Much of the power in this analysis came from including the normalization and outer slope of M31’s rotation curve in our fits (where many similar studies of AC attempt to fit to just the rotation velocity at 2.2 disc scalelengths, V_{2.2}). This highlights the usefulness of extended rotation curve data in constraining general models of galaxy formation. Having rotation curve data out to large radii is essential for determining dark matter density profiles.

Studies that test the applicability of adiabatic contraction often make use of large samples of galaxies that are dominated by late-type disc-dominated galaxies, with small bulges or no bulge at all (e.g. Pizagno et al. 2005; Dutton et al. 2005, 2007; Gnedin et al. 2006; Kassin et al. 2006a, b). These “bulgeless” galaxies also tend to have very flat (or even rising) rotation curves, and it is therefore easy to explain these galaxy rotation curves without any need for adiabatic contraction. However, we suggest that early-type disc galaxies (e.g. Hubble types Sa–Sb), which have bulge-dominated centres, and rotation curves that fall-off due to the presence of a large bulge, may require adiabatic contraction. Although we have studied very few galaxies so far (M31 in this paper and two other galaxies in Seigar et al. 2006) our results indicate that in cases where rotation curves have a fall-off (two out of three cases), adiabatic contraction is favoured. This may be true for all galaxies with large bulges. If so, it may favour a secular (rather than merger-driven) origin for these bulge-dominated systems, as the gradual accumulation of central mass increases the likelihood that AC will operate.

It should also be noted that in our best-fit model, while it is consistent with the current H I data from Carignan et al. (2006), it is unclear if the rotation curve is declining or remaining flat past 30 kpc, due to the large error bars. The most important requirement for future kinematical studies of galaxies would be improved H I measurements at large radii. This will enable us to put better constraints on the halo properties of M31 and other spiral galaxies.
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APPENDIX A: THE SPIRAL ARM PATTERN OF M31

Because M31 is a highly inclined galaxy, it is difficult to learn how tightly wound its spiral arm pattern is from imaging data. However, Seigar, Block & Puerari (2004) and Seigar et al. (2005, 2006) have shown that there is a very tight correlation between the spiral arm pitch angle (i.e. how tightly wound the spiral arms are) and rotation curve shear (measured at a 10 kpc radius). Therefore the spiral arm pitch angle can be estimated from the shear measured for the M31 rotation curve. Rotation curve shear is defined as

\[ \gamma = \frac{A}{\nu} = \frac{1}{2} \left(1 - \frac{R}{dV} \frac{dV}{dR}\right), \]  

where \( A \) is the first Oort constant, \( \nu \) is the angular velocity and \( V \) is the rotational velocity at radius \( R \). The shear rate...
Figure 1. Left: A two-armed spiral viewed face-on with pitch angle $P = 24^\circ 7$, as predicted for M31. Centre: A spiral with pitch angle $P = 24^\circ 7$, viewed with the inclination and position angle of M31. Right: 24 µm Spitzer image of M31 from Gordon et al. (2006).

depends upon the shape of the rotation curve. For a rotation curve that remains flat the shear rate, $S > 0.5$ and for a continually rising rotation curve the shear rate, $S < 0.5$. Following the method described by Seigar et al. (2006) we measure the shear at a 10 kpc radius. For M31, 10 kpc is equivalent to 43.9'. The shear is measured using the prescription described by Seigar (2005) and Seigar et al. (2004, 2005, 2006). In this method an average slope is fit to the outer part of the rotation curve (i.e., past the solid-body rotation regime), and the shear is then calculated at the given radius. For M31, at a radius of 10 kpc, the shear is $S = A/\omega = 0.54 \pm 0.02$.

There is little scatter in the correlation between shear rate and pitch angle, and the line of best fit is given by

$$P = (64.24 \pm 2.87) - (73.24 \pm 5.53)S,$$

where $P$ is the spiral arm pitch angle in degrees and $S$ is the shear. From this the pitch angle for M31 is $P = 24^\circ 7 \pm 4^\circ 4$. (It should be noted that the shear at 10 kpc determined for the M1 B86 model in section 2.2 is $S = 0.52$ and for M1 G05 is $S = 0.51$. These estimates are consistent with the shear measured here. They result in pitch angles of $P = 26^\circ 2 \pm 2^\circ 2$ and $P = 26^\circ 8 \pm 2^\circ 2$ respectively, both of which are consistent with the pitch angle derived above).

Assuming a logarithmic spiral (see e.g., Seigar & James 1998b for the equations that define a logarithmic spiral), the spiral arm pattern of M31 is calculated. Figure 1 shows the predicted spiral arm pattern of M31 for a face-on view (left) and with an inclination angle, $i = 77.5^\circ$, and a position angle $45^\circ$ (de Vaucouleurs et al. 1991) appropriate for M31 (centre). It should be noted that the position and inclination angles are not fitted parameters, they are taken from the literature. The spiral arm pitch angle calculated here is larger than the HI spiral arm pitch angle of $16^\circ$ calculated by Braun (1991), although it is possible that the spiral arm pattern in the neutral gas may be a few degrees tighter than that observed in the underlying stellar distribution. A pitch angle of $16^\circ$ would be a $\sim 2\sigma$ outlier in the spiral arm pitch angle versus rotation curve shear correlation when the shear, $S = 0.54$ (see Figure 3 of Seigar et al. 2006). If this point was added to the correlation, it would be one of the larger outliers, yet the correlation would still be strong. For comparison the 24 µm image is shown in the right panel of Figure 1.

It is important to note that the spiral arm pattern shown in Figure 1 does not take into account the disc scale height and how broad the arms are. These plots are intended to illustrate show how tightly wound the arm pattern would be if viewed from face-on. When viewed close to edge-on (as is the case for M31), the scale height of the disc and breadth of the spiral arms make it virtually impossible to determine the spiral arm pitch angle directly.

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