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Abstract. While the nucleus-to-cytoplasmic (N:C) ratio has traditionally been used for assessing cell malignancy, most N:C measurement techniques are time-consuming and performed on thin histological sections, which prohibit assessment of three-dimensional cell structure. A combined ultrahigh frequency ultrasound (US) and photoacoustic (PA) technique was used to assess the size and N:C ratio of cultured cancer cells in three dimensions (3D). The diameters of the cells and their stained nuclei were obtained by fitting the power spectrum of backscattered US pulses and emitted PA waves, respectively, to well-established theoretical models. For comparison, an imaging flow cytometer (IFC) was also used to determine the two-dimensional cell and nucleus sizes from large cell populations using brightfield and fluorescence images, respectively. An N:C ratio was calculated for each cell using the quotient of the measured nucleus diameter and the total cell diameter. The mean N:C ratios calculated using the sound-based approach were 0.68, 0.66, and 0.54 for MCF-7, PC-3, and MDA-MB-231 cells, respectively, and were in good agreement with the corresponding values of 0.68, 0.67, and 0.68 obtained using the IFC. The combined US and PA technique, which assesses cellular N:C ratio in 3D, has potential applications in the detection of circulating tumor cells in liquid biopsies.

Keywords: ultrahigh frequency; biological cell; nucleus-to-cytoplasmic; cell sizing; nucleus sizing.

1 Introduction

The development of new techniques and methods for cancer diagnosis is an active area of scientific and clinical research. Currently, the most commonly used technique for cancer diagnosis is histological assessment of tissue samples excised from the potentially cancerous tissue via optical microscopy.1 Albeit the gold standard, histological assessment of tissue samples via optical microscopy is a time-consuming and low-throughput process that lacks the ability to adequately assess three-dimensional (3-D) cell structure, a critical component of accurate diagnostics.2 One of the most prevalent characteristics of cancerous cells is an enlarged nucleus due to the increased amounts of chromatin present within malignant cells. This hallmark of malignancy led to the development of the nucleus-to-cytoplasm (N:C) ratio, defined as the ratio of the cross-sectional area of the nucleus divided by that of cytoplasm, which has since become a commonly used parameter in tumor staging and grading.3 Most N:C assessment techniques are typically performed in two dimensional (2-D) thinly sliced histological sections; hence, they may not accurately represent the true 3-D cell structure and may not accurately represent the N:C ratio of the cells being examined. Furthermore, it has been well reported that interobserver variability exists between pathologists using optical microscopy images to calculate the N:C ratio.4–6

These shortcomings have led to the development of alternative systems for N:C ratio quantification. Emerging technologies such as digital image analysis using HALO imaging-analysis software in urine cytology,7 immunofluorescence microscopy paired with ImageX,8 and 3-D multiphoton microscopy9 have been used to assess the N:C ratio but all require a lengthy imaging/analysis time for individual cells. Flow cytometry (FC) overcomes the drawback of slow analysis speeds at the expense of direct measurements of cell morphology. FC can quantitatively assess large cell populations using signals from emitted fluorescence as well as transmitted and scattered light from each cell with speed, automation, and objectivity.10 Although conventional FC is superior to optical microscopy in its speed and automation, it lacks the ability to generate absolute values for cell or nucleus size.11 Recent flow cytometric advances have seen the development of a new modality, imaging flow cytometry (IFC), which combines conventional light microscopy with high-quality CCD cameras in the context of a conventional FC system to image single cells in suspension at high resolution.12–14 Imaging of single cells in suspension is advantageous as it mimics biological cells in flow, such as those that would be found in the blood.14,15 IFC analysis software provides analytic tools that utilize feature-based image-gating strategies to characterize cell size, shape, and intensity patterns.16 IFC incorporates the high-quality image resolution and morphological content of optical microscopy while maintaining the high-throughput, automation, and population statistics of conventional FC.17 In previous studies, IFC has been used to generate images of single cells...
Photoacoustic (PA) imaging is a hybrid modality based on the PA effect that has generated much interest due to its ability to image vasculature without the need for exogenous contrast agents, as well as biological processes involving neural dynamics and myelin distribution. In the PA effect, a sample is irradiated with short (typically nanosecond) laser pulses, inducing a thermoelastic expansion of the light-absorbing chromophores, which in turn generate pressure waves that can then be detected using ultrasound (US) transducers. These recorded PA waves can subsequently be used to generate images that reflect the spatial distribution of optical absorbers within the sample. Alternatively, signal analysis techniques can be applied to individually acquired PA radio-frequency (RF) lines to ascertain information pertaining to the morphology of the source object. When applied to PA signals containing ultra-high frequencies (UHFs), such techniques enable the extraction of 3-D morphological information of optically absorbing cells such as RBCs and melanocytes. Combining PA spectral analysis techniques with an equivalent US-based technique, capable of determining the size of liquid droplets from features in the power spectrum of backscattered US waves, we have previously been able to assess the N:C ratio in cultured cancer cells. However, our previous work only demonstrated the use of these techniques for a single cell line with a small sample size and used published N:C ratio values as a preliminary means of technique validation. Here, we present an improved spectral analysis technique for the 3-D assessment of the N:C ratio and compare the results of our technique to 2-D IFC measurements of cell populations from the same cell lines.

2 Methods

2.1 Cell Preparation

Cells used for experimentation were prepared as follows: (1) MCF-7 and MDA-MB-231 cells were cultured in Dulbecco’s modified Eagle medium (Sigma-Aldrich) containing 10% fetal bovine serum by volume and (2) PC-3 cells were cultured in Roswell Park Memorial Institute medium (Sigma-Aldrich) containing 10% fetal bovine serum by volume. Once confluent, cells were trypsinized and resuspended in phosphate-buffered saline (PBS). The cells were then incubated in a dark room at room temperature for 15 min with a 1:200 solution of DRAQ-5 (Thermo Fisher), a fluorescent nuclear dye. DRAQ-5 staining enabled the production of both fluorescence and PA signals from the cell nucleus. After staining, all cells were washed three times in PBS. The final cell pellet was resuspended in 200 μl of PBS and was aspirated and expelled into the reservoir of a 25-gauge needle several times to form a single-cell suspension. To prepare the sample for analysis with the US/PA technique, 2 μl of the cell suspension was added to an aliquot containing 18 μl of molten 0.5% (w/v) agarose in PBS at 40°C. At these low concentrations, agarose has acoustic properties similar to that of water and, once solidified, gently immobilizes the cells in a spherical shape for the duration of the measurement procedure. A thin layer of cell-containing molten agarose was pipetted onto a glass-bottomed Petri dish (MatTek), which had previously been coated with a layer of 0.5% agarose. Prior to measurement, the dish was left to solidify at room temperature for 30 min. The remainder of the single-cell solution was transferred to a 1.5-ml low-retention microfuge tube to be used for the IFC experiments.

2.2 Image Flow Cytometer Cell Measurement and Image Processing

An Amnis ImageStream® MarkII IFC (MilliporeSigma) equipped with a 5-laser 12-channel system was used for image acquisition. The channels on the IFC correspond to spectral imaging bands. In this study, channels 1 (420 to 480 nm), 9 (570 to 595 nm), and 11 (660 to 740 nm) were used for acquisition along with a 642-nm laser (150 mW). Cell image analysis was carried out using the Amnis IDEAS® software platform (version 6.2). The nucleus diameter and cell diameter were determined using a custom workflow in IDEAS, which is illustrated in Fig. 1(a). As shown in Fig. 1(a) plot I, the gradient root-mean-squared feature was applied to the acquired MCF-7, PC-3, and MDA-MB-231 images, and the corresponding values were plotted on a normalized relative frequency distribution to discriminate between unfocused (low gradient) and focused (high gradient) cell images. Plot II depicts the area and aspect ratio features combined to discriminate between images containing single cells [green region of interest (ROI)] from those containing multiple cells. In our workflow, we included cell images with an aspect ratio between 0.6 and 1 to avoid cell fragments and other debris. Plot III shows the raw centroid X feature, defined as the number of pixels in the horizontal axis from the upper left corner of the image to the center of the mask, plotted against a normalized relative frequency distribution to remove clipped cell images. Lastly, plot IV depicts a positive gate for DRAQ-5-positive cells that was obtained using fluorescence intensity and area features. Through gating for solely DRAQ-5-positive cells in plot IV, we exclude cell images containing calibration beads, which are required for alignment of the sample stream during imaging. Figure 1(b) shows the masks used for the image analysis process. Eroded masks were applied to the final cell population to enable an accurate measurement of the cell diameter (i.e., the diameter of the circle with the same area of the masked object) using the native diameter function in IDEAS. This function was also applied to the masked nucleus image to assess the diameter of the cell nucleus.

2.3 Ultrasound/Photoacoustic Cell Measurement and Signal Processing

The US and PA measurements were performed using a dual modality UHF PA microscope (Kibero GmbH, Germany). The system consists of an inverted Olympus IX81 optical microscope equipped with a 10x objective (Olympus, Japan). The microscope was modified to incorporate a pulsed 532-nm laser with a 330-ps pulse width and 4-KHz repetition rate (Teem Photonics Inc., France), and a UHF single-element transducer with a central frequency of 375 MHz and a −6 dB bandwidth of 150 MHz. The transducer and objective were aligned such that their focal zones overlapped one another. Pulse-echo US was used to insonify the cells, and laser irradiation of the sample induced a PA wave originating from the cell nucleus. The 375-MHz US transducer was used to record both the backscattered US and the emitted PA signals from the cell and nucleus,
respectively. All measurements were performed at 37°C. The Petri dishes containing the cells were filled with PBS to provide acoustic coupling and were placed on a translation stage located between the optical objective and the transducer. Cells were located using the optical objective and were translated into the confocal transducer/objective focal zone for measurement. While the location of the features in the power spectrum used for cell and nucleus sizing is robust to the spatial location of the cell within the acoustic detection volume, centering the cell in the focal zone provides optimal signal-to-noise ratio (SNR) in the time and frequency domains and increases the prominence of the spectral features. A total of 200 US and 200 PA signals were acquired from each cell for signal averaging. To prevent measurement of the same cell multiple times, the sample was manually translated in a raster pattern until measurements from 50 unique cells had been acquired.

The workflow for the spectral fitting technique used for both the US and the PA RF-lines is provided in Fig. 2. First, a peak detector algorithm was used on the recorded US and PA time-domain signals—the time interval between the two peaks was converted to a distance using the speed of sound to provide a first approximation of the size of the cell and nucleus, respectively. The time-domain signal was then multiplied by a Tukey window and Fourier transformed, with a spectral resolution set to 1 MHz. The US and PA power spectra were then normalized by an appropriate (i.e., US or PA) reference spectrum accordingly to eliminate the system response. As a last step prior to fitting, the power spectra were windowed from 200 to 550 MHz to match the approximate transducer bandwidth and were normalized.

A dictionary containing the theoretical power spectra from 1 MHz to 1 GHz in steps of 1 MHz was generated for spherical absorbers with radii ranging from 0.05 to 50 μm in steps of 0.05 μm using the Diebold model for power spectra emitted by a spherical absorber. A speed of sound of 1527 m/s and density of 1000 kg/m³ were used for the background liquid (PBS), and corresponding values of 1560 m/s and 1050 kg/m³ were used for the cells. The estimated cell/nucleus sizes acquired from the time-domain signal were used to constrain the portion of the dictionary used for fitting. For an estimated time-domain radius $a$, the block of power spectra from $a-1$ μm to $a+1$ μm was extracted and gated from 200 to 550 MHz to match the measured power spectra. Finally, an inner product was performed between the measured power spectrum and each theoretical spectrum in the extracted dictionary block. The maximum value for the product corresponded to the radius in the dictionary, which provided the best fit to the measured spectra. Owing to the factor of two difference in the argument for US backscatter from cell-like liquid droplets and PA emissions from spherical droplets, the same dictionary could be used for both US and PA fittings—the final values only needing to be scaled by a factor of 0.5 for the US measurements (i.e., the power spectra for a spherical PA source of 10-μm radius is equivalent to that of the US backscattered power spectra from a liquid droplet with a radius of 5 μm).

### 3 Results

#### 3.1 Image Flow Cytometer

For this study, we investigated two different breast cancer cell lines (MCF-7 and MDA-MB-231), as well as PC-3 prostate cancer cells. To determine a baseline for the distribution of cell and nucleus sizes for each cell line, a total of 14,377 MCF-7 cells, 33,678 PC-3 cells, and 18,862 MDA cells were imaged using the IFC. For each cell line, 85% of the acquired images were discarded in the gating process due to the presence of alignment beads, multiple cells or cell fragments in the field of view, or cells that were out of focus in the images. Examples of rejected cell images are shown in Appendix A (Sec. 6).
small percentage of cells, the size of the nucleus mask was greater than the size of the cell mask; these images were further excluded from the final datasets. The above exclusion process ensured highly curated datasets consisting of 2164 MCF-7 cells, 4824 PC-3 cells, and 2981 MDA cells, which were then used to determine cell and nucleus size distributions for each cell line using IFC.

A summary of the results of the IFC image analysis for each cell line is provided in Table 1. Comparing the mean equivalent spherical diameters, the MCF-7 cells were the largest (18.88 ± 2.86 μm), followed by the PC-3 (18.24 ± 2.22 μm), and finally the MDA (16.93 ± 2.34 μm). The nuclei of the various cell lines followed a similar trend, with the equivalent spherical nuclear diameter of the MCF-7 cells (12.68 ± 1.94 μm) comparable with the diameter of the PC-3 nuclei (12.20 ± 1.86 μm); however, the size of the average MDA cell nucleus was smaller than the other two cell lines at 11.51 ± 1.83 μm. Histograms of the cell and nucleus size distributions for each of the cell lines are provided in Figs. 3(a)–3(c). For each cell in each of the cell line datasets, an N:C ratio was then calculated using the ratio of the cell’s equivalent spherical nucleus diameter to the equivalent spherical diameter. The resultant mean N:C ratios for the MCF-7, PC-3, and MDA lines were 0.68 ± 0.08, 0.67 ± 0.07, and 0.68 ± 0.08, respectively.

Table 1 A summary of the SASAM and image flow cytometer measurements for each cell line.

| Cell line | MCF-7 | PC-3 | MDA |
|-----------|-------|------|-----|
|           | SASAM (n = 37) | IFC (n = 2004) | SASAM (n = 43) | IFC (n = 4651) | SASAM (n = 43) | IFC (n = 2723) |
| Cell diameter (μm) | 15.2 ± 3.5 | 18.88 ± 2.86 | 15.4 ± 2.9 | 18.24 ± 2.22 | 14.2 ± 3.0 | 16.93 ± 2.34 |
| Nucleus diameter (μm) | 10.2 ± 3.5 | 12.68 ± 1.94 | 10.2 ± 3.6 | 12.20 ± 1.86 | 7.2 ± 2.9 | 11.51 ± 1.83 |
| N:C | 0.68 ± 0.19 | 0.68 ± 0.08 | 0.66 ± 0.19 | 0.67 ± 0.07 | 0.54 ± 0.19 | 0.68 ± 0.08 |
Representative merged IFC brightfield and fluorescence images of cells with N:C ratios ranging from 0.1 to 0.9 are shown in Fig. 4.

### 3.2 SASAM Cell Analysis

Sequential UHF US and PA measurements were performed on 50 unique cells for each cell line. Representative measured US and PA signals from the same cell are shown in Figs. 5(a) and 5(b), respectively. The envelope of each time-domain signal was observed to have either one or two peaks depending on the size of the cell or nucleus being measured. When two peaks are observed, the distance corresponding to the time between the two maxima in the signal envelope provides a rough approximation of the cell or nucleus size and can be used as a constraint in the dictionary fitting algorithm. When only one peak is present in the time-domain signal, the full width at half maximum (FWHM) of the envelope is instead used as an indication of scatterer/absorber size. Since the temporal length of the signals from the cell were longer than that of the PA signals from the nucleus, two well-defined peaks were more commonly observed in the US measurements compared to the PA.

![Fig. 3](image)

**Fig. 3** Histograms generated from the IFC measurements depicting the distribution of cell and nucleus sizes for the (a) MCF-7 cells, (b) PC-3 cells, and (c) MDA cells.

![Fig. 4](image)

**Fig. 4** Examples of cells having N:C ratios ranging from 0.1 to 0.9, as indicated in the top left corner of each image. The cell cytoplasm has been pseudocolored green, and the nucleus is shown in grayscale. The scale bar in each image is 7 μm.
measurements. While a majority of the US/PA measurement pairs were found to have good agreement with at least one of the prepopulated signals in the dictionary, in cases where the fits for either the US or PA measured signal were clearly erroneous for either the US or the PA measurement, both US and PA data points were omitted from the final population statistics. Common reasons for exclusion were: the SNR of either the US or PA signal was inadequate for visualizing spectral features, erroneous fitting results (e.g., where the calculated nucleus size was greater than the cell size), and cells for which the power spectra corresponding to the cell or nucleus sizes predicted by the fitting method were in clear disagreement with the measured spectra. Representative examples of excluded signals are shown in Appendix B (Sec. 7). The total number of cells for which both the US and the PA signals were adequately fit was 37 for the MCF-7 cells, 43 for the PC-3 cells, and 43 for the MDA cells. A summary of the derived values is provided in Table 1. For the MCF-7 line, the measured cells ranged from 8μm to 28μm in diameter, as determined from the US signals, and the mean cell diameter was calculated to be 15.2 ± 3.5 μm. In contrast, the diameters of the PC-3 cells were more tightly distributed, with diameters ranging from 10 to 22 μm, and a mean diameter of 15.4 ± 2.9 μm. The MDA cells also had a size distribution from about 8 to 21 μm in diameter but were the smallest cells on average with a mean diameter of 14.2 ± 3.0 μm. The size of the MCF-7 nuclei, as determined by the PA signals, ranged from 5 to 20 μm in diameter with a mean diameter of 10.2 ± 3.5 μm. The size of both the PC-3 and MDA cell nuclei ranged from ~4 to 20 μm in diameter and had mean diameters of 10.2 ± 3.6 and 7.2 ± 2.9 μm, respectively. Using the measured values for the cell and nucleus diameters, the N:C ratio was calculated on a cell-by-cell basis for each cell line. The mean N:C ratios were 0.68 ± 0.19, 0.66 ± 0.19, and 0.54 ± 0.19 for the MCF-7, PC-3, and MDA cells, respectively. Box-and-whisker plots showing the resultant distribution of N:C ratios are shown in Fig. 6.

A two-sample t-test was used to test for similarity between the means of the three cell lines. A statistically significant difference (p < 0.05) was observed between the mean diameter of the PC-3 and MDA cells; however, no statistically significant difference was observed when the other combinations of cell types were compared. In contrast, a significant difference (p < 0.001) was observed for the means of the nucleus diameter when comparing either the MCF-7 or PC-3 populations with the MDA. Significant differences (p < 0.01) were found when comparing the N:C ratios for the MCF-7 and MDA, and the PC-3 and MDA cell populations.

4 Discussion
Owing to the widespread use of the N:C ratio in cancer diagnosis, the ability of morphologists to repeatably and reliably determine the ratio in histology has recently been scrutinized. Vaickus and Tambouret found that trained morphologists were prone to overestimations of the ratio, especially at lower N:C values. The authors cited the irregularly shaped cytoplasm of the cells in the histological samples as one of the potential reasons for this discrepancy. In contrast, a larger study by Zhang et al. found that trained participants were adept at identifying both high (>0.7) and low (<0.3) N:C ratios but were less accurate at intermediate N:C ratios. Newer techniques, such as those based on quantitative image analysis, have the

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**Fig. 5** Representative (a) US and (b) PA signals from the same MDA-MB-231 cell. The corresponding power spectra are shown in (c) and (d), along with the best-fit power spectrum from the dictionary.
potential to overcome some of these challenges; however, these
techniques are limited to thinly sliced histology samples and
cannot be translated to the analysis of emerging diagnostic tec-
niques such as liquid biopsies for circulating tumor cell (CTC) detection.  

In this study, an IFC system was used as a means for optically
determining the average cell and nucleus diameters for each
population of suspended cells. Our intent was for the technique
to act as a comparator for the values derived from the US/PA
spectral fitting algorithm. While IFC excels at imaging and
acquiring 2-D morphology of large cell populations, there are
some inherent disadvantages with the technique. The most criti-
cal of these is that the IFC is dependent on the masks and fea-
tures used for gating the population and selecting the images that
will be used to generate the statistical results. Care must be taken
to ensure that the different masking algorithms used are appro-
perate for the cell population being analyzed and that the images
being analyzed contain no anomalies or artifacts. For example,
in the present study, we found that the cell mask used in the
IDEAS software tended to incorporate some of the “halo” delin-
eating the edge of the cell cytoplasm, causing the overall cell
size to be overestimated by 1 to 2 μm, if an additional erosion
mask was not used. In addition, images had to be excluded from
the analysis workflow due to the presence of cellular debris or
alignment beads in the image or if the cell was out of focus, off
center, or clipped in the field of view. While the final number of
cells analyzed was sufficient to generate statistical values with
low standard deviation for each cell line, the low percentage
(~15%) of usable cell images from the total number of acquired
images indicates that rare constituents, such as CTCs, which
may be at concentrations as low as 1000 per 10 ml sample
volume, could go undetected by current IFC techniques.

To the best of our knowledge, there is currently no method
that is accepted as the standard for determining the 3-D
morphology of a population of cells and their nuclei while in
suspension such as the constituents of liquid biopsies would be.
In contrast to conventional N:C assessment methodologies, the
dual-modality US/PA technique we present here—which infers
the 3-D structure of the cell/nucleus directly from the acquired
US and PA signals—is free of user bias and provides quantita-
tive values for the N:C ratio. Furthermore, both the US and the
PA interrogation modalities are highly specific to the cell and
stained nucleus, respectively. We have previously demonstrated
that waveforms of US signals backscattered from individual
biological cells are unaffected by cell nuclei since they are
acoustically homogeneous at UHFs.  

The only exception to this was the US/PA MDA cell group, which had an N:C ratio of 0.54.
The large standard deviation due to the small sample
size may account for this discrepancy.

Our ultimate goal is to integrate this algorithm into a device
that would be capable of screening a blood sample for the pres-
ence of CTCs based on their morphological differences (i.e., cell
size, nucleus size, N:C ratio) with normally occurring blood
cells. To this end, we investigated the possibility of differentiating between the three different cancer cell lines using our algorithm. The results of the t-tests comparing the cell diameters indicate that while the distributions of the MDA and PC-3 cells were significantly different from one another, there was no statistically significant difference between the distribution of cell diameters in the MCF-7 population when compared to either the PC-3 or MDA populations. Thus, for these cell lines, cell size alone cannot be used as a reliable metric for identification of cell type. Using a device that relied only on the overall cell size, such as filtration or electrical impedance measurement, the three cell lines used in this study would be nearly indistinguishable. However, when the nucleus and N:C ratio are additionally considered, differentiation of the MDA cells from the other two cell lines becomes possible, as the distributions of these parameters for the PC-3 and MCF-7 cell lines were both significantly different ($p < 0.001$ for the nucleus size, and $p < 0.01$ for the N:C ratio), when compared to the MDA line. For the number of cells analyzed here, the ability of the US/PA technique to discriminate between the MCF-7 and the PC-3 cell lines was limited due to high standard deviation of the reported mean values; however, when larger cell populations are analyzed, we believe that this will not greatly affect the technique’s ability to detect CTCs in a blood sample. Most leukocytes in the blood are between 8 and 11 μm in diameter, enabling the detection of CTCs in the blood by size-based techniques (e.g., filtration) alone. However, techniques based solely on cell size can misclassify large leukocytes and small CTCs. Consideration of additional metrics such as the nucleus size and N:C ratio could further improve the sensitivity of current size-based techniques.

Our previously reported spectral fitting algorithms required at least two spectral minima to fall within the bandwidth of the 400-MHz transducer and were thus incapable of sizing spherical cells or organelles with diameter smaller than ~3.5 μm when using US, or ~7 μm when using PA. These limitations are acceptable when using US to determine cell size since most animal cells typically have diameters between 10 and 20 μm. However, as the IFC measurements revealed, in some cases, cell nuclei can be as small as 4.5 μm in diameter and so our previous algorithm would be insufficient for determining the size of small nuclei from their emitted PA signals. The inner product spectral fitting technique presented here is advantageous in that it uses the entire frequency-domain spectrum within the transducer bandwidth to deduce the size of the absorber. Thus, cells and nuclei that are smaller than the above limits and have fewer than two spectral features can readily be sized. Another advantage of the present algorithm is that the equations governing the shape of the power spectrum for spherical cells and nuclei with acoustic properties similar to their surroundings differ only by a factor of 2 in the argument. This means that the same dictionary can be used to determine the size of both cells and nuclei, reducing the computational time and complexity of the algorithm. One limiting factor of the current technique is that the theory used for predicting absorber size from the PA power spectra is only valid for spherical absorbers. Thus, nuclei with high aspect ratios would not be able to be fit using the current technique. Going forward, we plan to incorporate analytical models capable of accurately determining the morphology and orientation of nonspherical nuclei, such as those shaped like prolate and oblate spheroids. Incorporating models such as these would increase the robustness and accuracy of the present technique and potentially eliminate some of the disagreements observed in some of the discarded power spectrum fits.

5 Conclusion

In this work, we sought to validate the cell, nucleus, and N:C ratio values obtained using our sound-based technique with population values obtained using the optical IFC device. We demonstrate that, while there were slight differences in the overall size of the cells predicted by the two techniques, good agreement between the two techniques was observed, especially for the calculated N:C ratio values. We have recently reported on an acoustic flow cytometer that sized cell diameter using only US methods and have since incorporated a pulsed laser into our system to enable differentiation of RBCs and white blood cells via simultaneous US/PA detection. Going forward, we plan on translating the presently reported N:C assessment technique to this high-throughput US/PA device to enable large-scale investigations of cell population statistics, as well as the detection of cancer cells spiked into a blood sample.

6 Appendix A: Examples of Rejected Imaging Flow Cytometer Cell Images, as Well as Reasons for Rejection

Examples of cells that were excluded from the IFC analysis by means of gating are shown in Fig. 7. In Fig. 7(a), the imaged cell is out of focus, resulting in a large “halo” at the cell periphery, which would lead to an overestimation of the cell diameter.

![Fig. 7](image-url)
Figure 7(b) depicts an image that was rejected on the grounds that two cells were detected in the ROI. Finally, Fig. 7(c) shows an image of a cell which was “clipped” at the edge of the image ROI, and thus unsuitable for analysis.

### 7 Appendix B: Examples of Rejected Ultrasound/Photoacoustic Cell Measurements

The graphs in Fig. 8 provide examples of RF-lines and power spectra which were excluded from analysis. In Fig. 8(a) the acquired PA waveform has poor SNR, causing an estimation of nucleus size from the PA power spectrum [Fig. 8(b), right] that is larger than the fit cell diameter [Fig. 8(b), left]. Conversely, in Fig. 8(c) there is increased noise in the acquired US RF-line, leading to a poor fit in the US power spectrum [Fig. 8(d), left] and an under-estimation of cell size.

**Disclosures**

M.C.K. and M.J.M. have financial interests in Echofos Medical Inc., which, however, did not support this work. The remaining author declares no competing financial interests.

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**Fig. 8** For the power spectra, the fit diameter is indicated above the graph axis. In (a), the noisy PA signal resulted in a power spectrum (b) with minima placement indicative of a nucleus size larger than that of the cell size. In (c), a noisy US spectrum resulted in a poor fit to the theoretical US backscatter, causing (d) the cell size to be underestimated.
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