The Gaia-ESO Survey.
Mg-Al anti-correlation in iDR4 globular clusters

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ABSTRACT

We use Gaia-ESO Survey iDR4 data to explore the Mg-Al anti-correlation in globular clusters, that were observed as calibrators, as a demonstration of the quality of Gaia-ESO Survey data and analysis. The results compare well with the available literature, within 0.1 dex or less, after a small (compared to the internal spreads) offset between the UVES and the GIRAFFE data of 0.10-0.15 dex was taken into account. In particular, we present for the first time data for NGC 5927, one of the most metal-rich globular clusters studied in the literature so far with [Fe/H]=−0.49 dex, that was included to connect with the open cluster regime in the Gaia-ESO Survey internal calibration. The extent and shape of the Mg-Al anti-correlation provide strong constraints on the multiple population phenomenon in globular clusters. In particular, we studied the dependency of the Mg-Al anti-correlation extension with metallicity, present-day mass, and age of the clusters, using GES data in combination with a large set of homogenized literature measurements. We find a dependency with both metallicity and mass, that is evident when fitting for the two parameters simultaneously, but no significant dependency with age. We confirm that the Mg-Al anti-correlation is not seen in all clusters, but disappears for the less massive or most metal-rich ones. We also use our dataset to see whether a normal anti-correlation would explain the low [Mg/α] observed in some extragalactic globular clusters, but find that none of the clusters in our sample can reproduce it, and more extreme chemical compositions (like the one of NGC 2419) would be required. We conclude that GES iDR4 data already meet the requirements set by the main survey goals, and can be used to study in detail globular clusters even if the analysis procedures were not specifically designed for them.

Key words. Surveys – Stars: abundances – globular clusters: general – globular clusters: individual : NGC 5927

1. Introduction

The phenomenon of multiple populations in globular clusters (GCs) has been intensively studied in the last 20-30 years, but we still lack a clear explanation of its origin (Gratton et al. 2012). The abundance variations pattern pinpoints the CNO-cycle burning of hydrogen as the major source of the phenomenon, because most of the elements that are observed to vary in GCs are used as catalysts in various CNO sub-cycles, where they are depleted or accumulated depending on the particular reaction rates. However, a hot debate is still ongoing on which types of polluters convey the processed material into the GC interstellar gas reservoir, and how it is recycled to pollute a fraction of the GC stars or accumulated depending on the particular reaction rates. How- ever, the peculiar chemistry observed in GCs. Another advantage of studying Mg and Al is that they suffer much less internal mixing compared to C and N, or even Na and O, therefore the observed abundances do not depend on the evolutionary status of a star.

The Gaia-ESO survey (GES, Gilmore et al. 2012; Randich et al. 2013), that is being carried out at the ESO VLT with FLAMES (Pasquini et al. 2000), observed GCs as calibrators for the astrophysical parameters (AP) and abundance ratios (Pancino & the Gaia-ESO Survey collaboration 2016) hereafter P16).

Part of the observed GCs were included in the fourth internal data release (iDR4), that is based on data gathered from December 2011 to July 2014 and from which the next GES public release will be published through the ESO archive system. The iDR4 data also include relevant archival data obtained with FLAMES in the GES setups. A particular advantage of the adopted observing setups is that they allow for an accurate measurement of the Mg and Al abundance ratios with both the UVES and GIRAFFE spectrographs, thus providing statistical samples comparable to those recently obtained by APOGEE (Mészáros et al. 2015) and the FLAMES GC survey (Carretta et al. 2009a,b; 2011, 2013a, 2014). The paper is organized as follows: in Section 2 we describe the data treatment and sample selection; in Section 3 we present the results and explore their robustness; in Section 4 we describe

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1 http://archive.eso.org/cms.html
and discuss the behaviour of the Mg-Al abundance variations; in Section 5 we summarize our findings and conclusions.

2. Data sample and treatment

The GES iDR4 data on GCs are all based on the UVES setup centred around 5800 Å and on the two GIRAFFE setups HR 10 (5339–5619 Å) and HR 21 (8484–9001 Å). The selection of calibration targets, which include GCs, was described in detail by P16. Briefly, 14 GCs were selected to adequately cover the relevant metallicity range, from [Fe/H] = −2.5 to −0.3 dex, 11 of which were analyzed in iDR4. A few less studied GCs were included at the beginning of the survey, owing to pointing constraints (see P16 for more details), and in particular the sample includes NGC 5927, one of the most metal-rich GCs available. The selection of stars was focussed on red giants, except in NGC 5927 where mostly red clump stars were selected because of the high differential reddening and the need to maximize cluster members. Stars already having GIRAFFE archival observations in the ESO archive were prioritized, to increase the wavelength coverage by including the GES setups. Stars already observed with UVES were not repeated. A few fibers were dedicated to re-observe with UVES some GIRAFFE targets and vice-versa, to allow for cross-calibration.

All iDR4 data were reduced as described in detail by Sacco et al. (2014) for spectra taken with UVES (Dekker et al. 2000) at high resolution (R = λ/δλ ≈ 47 000) and by Jeffries et al. (2014) for spectra taken with GIRAFFE (Pasquini et al. 2000) at intermediate resolution (R = 16 000–20 000). Briefly, the UVES pipeline (Modigliani et al. 2004) was used to process UVES spectra, performing the basic reduction steps. Additional data analysis was performed for UVES with specific software developed at the Arcetri Astrophysical Observatory. GIRAFFE spectra were processed with a dedicated software developed at CASU (Cambridge Astronomy Survey Unit).

2.1. Abundance analysis

The GES abundance analysis of UVES spectra was described in detail by Smiljanic et al. (2014) and Casey et al. (in preparation), while the analysis of GIRAFFE spectra by Recio-Blanco et al. (in preparation). Both are carried out by many research groups, using several state-of-the-art techniques. Because of the GES complexity, the data analysis is performed iteratively in each internal data release (iDR), gradually adding not only new data in each cycle, but also new processing steps to take into account lessons learned in the previous iDRs (offsets or trends identified through early science projects) or to increase the number of elements measured (from molecules, or faint features), or finally by adding detail to the measurements (corrections for non-LTE, rotational velocities, veiling, and many more). This methodology allows for a better quantification of the internal and external systematics, that are evaluated in a process of homogenization of all node results, producing the final GES recommended APs and abundance ratios, as described by P16 and Hourihane et al. (in preparation).

To make the GES data analysis as uniform as possible, the analysis of F, G, and K type stars relies on a common set of atmospheric models (the MARCS grid, Gustafsson et al. 2008), a common linelist (Heiter et al. 2015b), and – for those methods that require it – a common library of synthetic spectra (computed with MARCS models and based on the grid by de Laverty et al. 2012). The Solar reference abundances adopted in this paper were those by Grevesse et al. (2007). As mentioned, iDR4 abundances are computed in the LTE regime, and only future releases will include non-LTE corrections. Moreover, the GES

![Fig. 1. Example of the small (compared to the errors and internal spreads) residual offsets in [Fe/H] between UVES and GIRAFFE in GES iDR4 data, in two of the sample GCs: NGC 2808 (top panels) and NGC 1851 (bottom panels). The left panels show [Fe/H] as a function of T eff and the right ones of log g. UVES stars are plotted as cyan symbols, with their median [Fe/H] as a cyan line. GIRAFFE stars are plotted as magenta symbols, with their median [Fe/H] as a magenta line. The reference [Fe/H] from Harris (1996, 2010) is plotted as an orange line.](#)

| Cluster       | [Fe/H]_UVES (dex) | RV_{UVES} (km s\(^{-1}\)) | log(M/M_⊙) | [Fe/H]_GES (dex) | RV_{GES} (km s\(^{-1}\)) | N_e |
|--------------|------------------|-----------------------------|-------------|------------------|-----------------------------|-----|
| NGC 104 (47 Tuc) | −0.72            | −18.0                       | 6.05±0.04   | −0.71±0.02       | −17.6±0.8                   | 119 |
| NGC 362      | −1.36            | 223.5                       | 5.53±0.04   | −1.12±0.03       | 222.3±0.6                   | 73  |
| NGC 1851     | −1.18            | 320.5                       | 5.49±0.04   | −1.07±0.03       | 320.2±0.5                   | 89  |
| NGC 1904 (M 79) | −1.60           | 205.8                       | 5.20±0.04   | −1.51±0.03       | 205.2±0.5                   | 30  |
| NGC 2808     | −1.14            | 101.6                       | 5.93±0.05   | −1.03±0.03       | 103.7±1.4                   | 45  |
| NGC 4833     | −1.85            | 200.2                       | 5.20±0.21\(^b\) | −1.92±0.03       | 200.6±1.0                   | 28  |
| NGC 5927     | −0.49            | −107.5                      | 5.32±0.21\(^b\) | −0.39±0.04       | −102.5±0.7                   | 85  |
| NGC 6752     | −1.54            | −26.7                       | 5.16±0.21\(^b\) | −1.48±0.04       | −26.3±0.7                   | 57  |
| NGC 7089 (M 2) | −1.65            | −5.3                        | 5.84±0.05\(^e\) | −1.47±0.03       | −1.8±1.3                    | 46  |

Table 1. Basic properties of the GC sample, listing: [Fe/H] and RV from Harris (1996, 2010); the present-day mass from McLaughlin & van der Marel (2005) annotated with “*”; from Mandushev & H96 (1991) annotated with “†”; the median [Fe/H] and RV from GES data; and the number of GES member stars analyzed.

\(^a\) errors and internal spreads; \(^b\) uncertainty on [Fe/H] is ±0.04 dex; \(^e\) uncertainty on RV is ±0.8 km s\(^{-1}\).
homogenous analysis relies on a rich set of calibrating objects (including GCs), selected as described by P16. In particular, the external calibration of FGK stars in iDR4 relies mostly on the Gaia benchmark stars \cite{Jofre2014,Blanco-Cuaresma2014,Heiter2015a,Hawkins2016}.

When comparing the iDR4 abundances obtained from UVES and GIRAFFE, small (i.e., comparable to the internal spreads) offsets in the abundance ratios were found (~0.10–0.15 dex, depending on the GC), as shown by P16. For the present analysis, we reported the [Fe/H] GIRAFFE measurements to the UVES scale using the median abundance of the two samples in each GC. We observed that once the [Fe/H] offsets were corrected this way, there were no significant residual offsets when comparing the UVES and GIRAFFE measurements of the other elements considered in this paper. In any case, in the GES cyclic processing the recommended values of RVs, APs, and chemical abundances generally improve from one iDR to the next (see Randich et al., in preparation, and P16). We thus expect the offsets to reduce considerably in future GES releases. Most importantly, as Figure 1 shows, in iDR4 there are no significant trends of [Fe/H] as a function of $T_{\text{eff}}$ or logg for either UVES or GIRAFFE results.

### 2.2. Sample selection

We applied the same quality selection criteria of the GES public release (that will be described in the ESO release documentation) to the iDR4 recommended results. For the cool giants in GCs, these are: $\delta T_{\text{eff}}/T_{\text{eff}} < 5\%$, $\delta \log g < 0.3$ dex, and $\delta$[Fe/H] < 0.2 dex. We also left out all stars that lacked AP or RV determinations.

We then selected GC probable members using the median [Fe/H] and RV generally agree with reference literature values \cite{Harris1996,Harris2010}. The members selection was quite straightforward, because the vast majority of field stars have roughly Solar metallicity and RV approximately $\pm 50$ km s$^{-1}$, thus the GC stars differ significantly from field stars in at least one of [Fe/H] or RV.

The above selections lead to highly varying sample sizes for UVES and GIRAFFE depending on several factors like spectral quality (S/N ratio, spectral deficits), observing conditions (sky, seeing), availability of previous information (photometry, membership, other archival data), and cluster (crowding, GC compactness, distance, metallicity). Of the 11 GCs included in iDR4 (see P16, for the selection criteria of calibrating objects) only 10 contained at least 5 red giants after the quality and membership selections. Of these, we excluded M 15 because the iDR4 analysis of its very metal-poor spectra did not provide satisfactory results. The final list of 9 analysed GCs is presented in Table 1 along with some relevant properties. The final sample contained 510 stars (159 with UVES and 351 with GIRAFFE) in 9 GCs, that had Mg or Al measurements. The stars and their relevant properties are listed in Table 2.

We stress again that the size and quality of the presented GC sample are comparable to the two largest GC surveys presented in the literature so far, i.e., the FLAMES GC survey and the APOGEE sample.

### 3. Results

#### 3.1. A quality control test on the Na-O anti-correlation

We started by comparing our results for the well studied Na-O anti-correlation with: the FLAMES GC survey by Carretta et al. (2009a, 2011, 2013), the NGC 6752 study by Yong et al. (2005), and the M2 studies by Yong et al. (2014) and Meszaros et al. (2015). We restricted the comparisons to high-resolution studies (R>15 000) of red giants. The results are plotted in Figure 2 where only UVES measurements appear because oxygen is not included in the GES GIRAFFE setups.

As can be seen, the GES measurements agree well with the literature ones, in spite of the different methods, linelist selections, models, and data sets involved. The median offsets, measured by taking the difference between the median abundances obtained by GES and in the literature for each GC, were in general lower than ±0.1 dex. We note that for 47 Tuc the GES data are less spread than the literature ones in [O/Fe], but they do not sample the full extension of [Na/Fe], most probably because of the quality selection criteria described in Section 2.2 that penalize oxygen abundances derived mostly from the weak [O I] line at 6300 Å. We also note that the GES data for NGC 2808 show two well separated clumps of stars while the literature data apparently display a more continuous distribution. We ascribe this to our small sample which, being randomly chosen, picked stars near two most populated peaks of the underlying distribution, which contains five separate groups (Carretta2015). The apparently continuous distribution of literature data is mostly driven by the GIRAFFE measurements (brown dots), which are more numerous but less precise than the UVES ones (gold dots).

We present here for the first time [Na/Fe] and [O/Fe] abundance ratios for NGC 5927, one of the most-metal rich GC studied with high resolution spectroscopy in the literature so far. NGC 5927 displays the same stubby Na-O anti-correlation as 47 Tuc, the other metal-rich GC in the sample: while the upper [Na/Fe] limit is the same as any other GCs, and is governed

### Table 2. List of the 510 stars that were selected from GES iDR4 as probable members and analyzed in this paper. The table is available in its entirety online and at CDS, here we show a portion to illustrate its contents. The reported errors are the result of the complex GES homogenization procedure and thus include random and systematic error sources.

| CNAME       | Cluster   | $T_{\text{eff}}$ (K) | $\delta T_{\text{eff}}$ (K) | logg (dex) | $\delta \log g$ (dex) | [Fe/H] (dex) | $\delta$[Fe/H] (dex) | log $\epsilon_{\text{Al}}$ (dex) | $\delta$ log $\epsilon_{\text{Al}}$ (dex) | log $\epsilon_{\text{Mg}}$ (dex) | $\delta$ log $\epsilon_{\text{Mg}}$ (dex) |
|-------------|-----------|----------------------|----------------------------|------------|------------------------|--------------|----------------------|---------------------------------|-----------------------------------|---------------------------------|--------------------------------------|
| 12593863-7051321 | NGC4833   | 4673                 | 124                        | 1.308      | 0.246                  | -1.844       | 0.103                | 5.61                            | 0.07                              | 5.94                            | 0.13                                  |
| 13003136-7053486 | NGC4833   | 4675                 | 132                        | 1.207      | 0.239                  | -1.920       | 0.106                | 5.60                            | 0.07                              | 5.59                            | 0.13                                  |
| 12587546-7053278 | NGC4833   | 4678                 | 127                        | 1.316      | 0.261                  | -2.024       | 0.119                | 5.29                            | 0.07                              | 5.73                            | 0.13                                  |
| 12592040-7051156 | NGC4833   | 4623                 | 123                        | 1.130      | 0.252                  | -1.922       | 0.101                | 5.55                            | 0.07                              | 5.50                            | 0.13                                  |
| 12593863-7051321 | NGC4833   | 4613                 | 123                        | 1.112      | 0.254                  | -1.920       | 0.108                | 5.55                            | 0.07                              | 5.66                            | 0.14                                  |
| 12593089-7050304 | NGC4833   | 4673                 | 124                        | 1.308      | 0.246                  | -1.844       | 0.103                | 5.61                            | 0.07                              | 5.94                            | 0.13                                  |
Fig. 2. Na-O anti-correlation. Panels show different GCs, sorted by increasing metallicity from left to right and from top to bottom. Dotted lines mark the Solar abundance ratios, dashed lines the typical halo α-enhancement. GES UVES data are plotted in cyan diamonds; literature data from the FLAMES GC survey are plotted in brown for GIRAFFE and in gold for UVES; NGC 6752 and M 2 data by [Yong et al. (2005)] and [Yong et al. (2014)] are plotted in green; the 47 Tuc analysis by Cordero et al. (2014) is plotted in blue. Typical (median) errorbars are reported on the lower-left corner of each panel.

by the equilibrium abundance of the NeNa hot cycle, the lowest [Na/Fe] abundances are slightly super-Solar rather than sub-Solar, as expected for field stars at the same metallicity, as further discussed in Section 4.3.

In conclusion, the presented comparison confirms that the atmospheric parameters resulting from the GES homogenized analysis are well determined (see also P16).

3.2. Mg-Al anti-correlation

The Mg-Al anti-correlation for the selected iDR4 stars is plotted in Figure 3 along with the available literature data. In contrast to the Na-O anti-correlation, we present both UVES and GIRAFFE measurements. Our measurements compare well with the literature, with small offsets that are <0.1 dex, i.e., within the quoted errors, as in the Na-O case.

For NGC 1904 there are few stars and they appear quite scattered. For the other 8 GCs, however, we clearly see that the Mg-Al anti-correlation has a variable extension. Four GCs have a well-developed and curved Mg-Al anti-correlation: NGC 2808, NGC 4833, NGC 6752, and M 2. Two GCs have a stubby Mg-Al distribution: NGC 362 and NGC 1851 which mostly display an [Al/Fe] spread and no significant [Mg/Fe] spread. The two most metal-rich GCs in the sample, 47 Tuc and NGC 5927, show no clear signs of an anti-correlation. This behaviour was already noted by Carretta et al. (2009a), who explicitly mentioned the GC present-day mass and metallicity as the two main parameters driving the extent of the Mg-Al anti-correlation (see Section 4 for more discussion on this point).

We did not detect any significant variation of the combined abundance of Mg and Al. This is consistent with no net production of these elements, but just the result of the conversion of Mg into Al during the Mg-Al cycle. Concerning the Al-Si branch of the Mg-Al cycle (see also Yong et al. 2005, Carretta et al. 2009a), we looked for Si variations in our sample, but unfortunately GES iDR4 contains only a few Si measurements that pass all the criteria employed to select the sample stars. Inspection of the [Si/Fe] ratio as a function of [Al/Fe] or [Mg/Fe] for the few stars with reliable Si measurements in iDR4 did not reveal any clear trend.

4. Discussion

To put our results in context, we combined the GES iDR4 data with the FLAMES GC survey (Carretta et al. 2009a,b) and the APOGEE survey (Meszaros et al. 2015) measurements. Literature data were shifted in both [Fe/H] and the [El/Fe] abundance ratios by small amounts (<0.1 dex) to place them on the GES iDR4 scale. The shifts were computed using the median values of key elements for the GCs in common among studies. The combined sample contains ~1 300 stars in 28 GCs, having both Mg and Al measurements (or 2 500 stars if one counts also the stars having Na or O, but missing one of Mg or Al).

In the next sections, we discuss some of the Mg-Al anti-correlation properties that were apparent during a preliminary exploration of the combined sample. We leave the discussion of other elements to the following GES releases, where more stars, more GCs, and more elements will be available, and the whole GES intercalibration procedure will be more refined.

4 We had M 2 in common with the APOGEE survey and 6 GCs in common with the FLAMES GC survey (see also Figures 2 and 3). The handful of stars in common among the various studies was not sufficient to compute reliable shifts, and was removed from the sample, retaining with precedence the GES data, then APOGEE ones, and then the FLAMES GC survey ones.
4.1. Comparison with field stars

We started by examining the Na-O and Mg-Al anti-correlation as a function of metallicity, and we compared the available GC measurements with the Milky Way (MW) field population. Because iDR4 contains mostly MW stars with [Fe/H] $\geq$ −1.0 dex, we added metal-poor stars extracted from the SAGA database (Suda et al. 2008). Figure 4 shows the comparisons. Oxygen measurements in iDR4 are still quite spread out, because they are often based solely on the weak [O I] line at 6300 Å, and they rely on the generally lower S/N ratio of field star spectra compared to GC stars (see P16 for details), but the bulk measurements follow the expected trend. In spite of the heterogeneity of the sample and of our relatively simple homogenization method, the agreement among the plotted studies is remarkably good.

Two important things should be noted at this point. The first is that both GES and the FLAMES GC survey use similar instrumental setups, wavelength ranges, and S/N ratios. GES is targeting mostly MW field stars of higher metallicity, while the FLAMES GC survey was focused on the Na-O anti-correlation. As a result, neither of these surveys contains many measurements at [Fe/H] $\leq$ −1.7 dex, and in particular, they do not contain many stars with low values of [Al/Fe] or [Mg/Fe] because they mostly rely on spectral lines that become weak at those metallicities. On the contrary, APOGEE measurements are obtained with a different wavelength range and using different features and selection criteria, and therefore that sample contains many more stars with low Al or Mg, as can be seen in Figure 4. On the other hand, GES data add NGC 5927 to the sample, extending the [Fe/H] coverage to [Fe/H] $\approx$ −0.49 dex, while the two previous systematic studies considered here reached [Fe/H] $\approx$ −0.7 dex with 47 Tuc and M 71.

As was noted by others before, the lower boundary of the Na and Al distribution in GCs is aligned with the typical field star value at any given metallicity. Similarly, the upper boundary of the O and Mg distribution in GCs is aligned with the typical field-star $\alpha$-enhancement at any given metallicity. This supports the idea that the main contributors to the chemistry of normal stars in GCs (often called first generation stars or unenriched stars) are mostly SNe II, like for the field stars at the same metallicity, with SNe Ia intervening only above [Fe/H] $\approx$ −1.0 dex.

The abundance of anomalous stars (often called second generation or enriched stars) is thought to be governed by CNO cycle processing at high temperatures (Kraft 1994; Gratton et al. 2005). The extent of Na variations in GC stars changes slightly with [Fe/H]. This is mostly governed by the lower boundary variations of [Na/Fe] in GC stars, that follow the field population behaviour as discussed. The upper boundary – governed by the equilibrium abundances reached in the Ne-Na cycle – shows only moderate variations in our sample, being roughly at [Na/Fe] $\approx$ +0.6 dex, and contained within ±0.15 dex. The extent of [Al/Fe] variations in GC stars, instead, changes dramatically with [Fe/H] both in the upper and lower boundaries. While it was suggested that [Fe/H] is not the sole parameter governing Al variations (see also Section 4.2), the Al spread clearly varies with metallicity, from a maximum of $\Delta$[Al/Fe] $\approx$ 1.5 dex and more below [Fe/H] $\approx$ −1.0 dex, to $\Delta$[Al/Fe] $\leq$ 0.5 dex above that metallicity, where the spread become compatible with measurement uncertainties.

These considerations lead us to believe that the entire sample of 1 300 stars should be used when studying the behaviour of the Mg-Al anti-correlation with GC properties, to increase the parameter coverage and the statistical significance of the analysis.

5 Both GES and the FLAMES GC survey contain several upper limits in the most metal-poor GCs, that are not plotted in this paper.

6 We remark here that an extremely homogeneous and populous sample would be required to better quantify this important aspect.
4.2. Mg-Al anti-correlation extension

We have seen that a clear variation of the [Al/Fe] spread with [Fe/H] is apparent in Figure 4 and this is not only caused by the natural [Al/Fe] variations observed for field stars (the lower [Al/Fe] boundary). The question of which GC properties govern the extension (or presence) of the Mg-Al anti-correlation has been explored previously in the literature (see, e.g., Carretta et al. 2009a,b, Mészáros et al. 2015, Cabrera-Ziri et al. 2016 for example). Both [Fe/H] and present-day mass were mentioned as the most important parameters in those works. However, when only [Fe/H] was considered (Figure 4 by Cabrera-Ziri et al. 2016), only weak correlations were found, with large spreads and unclear statistical significance. In that case, 25 GCs were examined with typically 10–20 stars per GC. Here, we can profit from our combined sample of 28 GCs with ≈50 stars each on average, as described in Section 4.1, and re-examine these parameters as drivers of the Mg-Al anti-correlation.

We therefore proceeded to fit the data using two different indicators of the anti-correlation extension, the standard deviation of the [Al/Mg] distribution and its maximum variation, i.e., the difference between the maximum and minimum values of [Al/Mg] for each GC. The two indicators will be expressed as \( \sigma_{[\text{Al}/\text{Mg}]} \) and \( \Delta_{[\text{Al}/\text{Mg}]} \) in the following Figure 5 shows the results graphically, where it is apparent that the most massive GCs tend to have higher values with both indicators in the plot as a function of [Fe/H], and the most metal-poor ones also have higher spread in the plot as a function of log M. If we were to fit the two parameters separately, we would obtain very high spreads and very weak relations even with our larger sample.

We therefore employed a linear fit on both parameters simultaneously and we obtained the following results:

\[
\sigma_{[\text{Al}/\text{Mg}]} = 0.19(\pm0.06) \text{ log } M - 0.20(\pm0.05) [\text{Fe/H}] - 0.94(\pm0.33)
\]

\[
\Delta_{[\text{Al}/\text{Mg}]} = 0.67(\pm0.21) \text{ log } M - 0.53(\pm0.17) [\text{Fe/H}] - 3.16(\pm1.11)
\]

The fits are also reported in Figure 5. The p-values of the \( \sigma_{[\text{Al}/\text{Mg}]} \) and \( \Delta_{[\text{Al}/\text{Mg}]} \) are 0.0001493 and 0.0005242, respectively, suggesting that it would be improbable to obtain the observed distribution by chance (if the chosen model was correct). The errors on the coefficient are also relatively low, suggesting that the two-parameter linear model is a reasonable description of the data. We thus can conclude that both parameters are independent of log M.

We remark here that both indicators are subject to measurement and statistical biases. Measurement effects (most notably outliers) tend to produce an overestimate of the Mg-Al extension, while sampling effects (small sample sizes) tend to produce an underestimate.

Here and in the following, we use the word model in the statistical sense, i.e., a way of describing the data phenomenologically and not a physical model.

It is important to stress at this point that no mass-metallicity relation is apparent in Galactic GCs.

Figure 4 is an example of the striking power of such a sample, and reveals the importance of [Fe/H] as a driving parameter for the presence and extent of the Mg-Al anti-correlation.
and it does not mean that [Fe/H] and logM are the only two parameters at play, especially considering that the errors on the derived coefficients are of about $\pm 30\%$, and that the residual distributions, although centered on zero, have relatively large spreads: $\text{med}(r.m.s._{\text{[Al/Fe]}}) = -0.005 \pm 0.768$ and $\text{med}(r.m.s._{\text{[Mg/Fe]}}) = +0.014 \pm 0.258$. In the present analysis, we have not used the errors in the fit, because of the heterogeneity of the data sources and therefore of error determinations, but even accounting for that, the relatively large spreads could point towards some extra parameter. We also tried a different model, adding a quadratic term in both [Fe/H] and logM but the fit did not improve significantly. Similarly, when adding the age parameter from [Marin-Franch et al. 2009] or from [VandenBerg et al. 2013] as a third linear term, the coefficient was always low ($<0.001$), and the quality of the fit was worse than that of the two-parameters one.

A full statistical analysis of the relation between anti-correlation parameters and GC properties will be presented in a forthcoming paper, when the analysis of the whole GES sample of stars in all the observed GCs will be completed, and we will also have data on the [C/Fe] and [N/Fe] ratios.

The Mg-Al anti-correlation is a problem for the scenarios based on fast rotating massive stars (FMRS, [Decressin et al. 2007]) or massive interacting binaries (MIB, [de Mink et al. 2009]), which activate CNO burning in their cores but require very high masses (well above 100 $M_\odot$) and some tweaking of the reaction rates to reproduce the Mg-Al observations. More massive stars would be required like the super-massive stars (SMS, $\sim 1000 M_\odot$, [Denissenkov et al. 2015]), but these are not observed and therefore their postulated physics is highly uncertain. We expect a metallicity dependency for SMS because of the strong wind mass loss [Vink et al. 2011] that would lead to the formation of smaller SMS at higher metallicity. Asymptotic Giant Branch polluters (AGB), that activate CNO burning in the shell and also hot-bottom burning at high masses, can explain naturally the Mg-Al observations, because both the depletion of Mg and the production of Al are extremely sensitive to the AGB star metallicity [Ventura et al. 2016]. However, we remark here that none of the scenarios presented in the literature so far is entirely free from serious shortcomings [Renzini et al. 2015]. We also remark that no conclusive answer can be drawn by considering one anti-correlation only and this, like other works, has to be considered as a preliminary exploration.

The correlation of the Mg-Al extent with present-day GC mass has not been explained in detail in any of the scenarios proposed so far. It would be necessary to explore whether the observed mass variations among Galactic GCs (presently in the range $10^4$–$10^5 M_\odot$) are sufficient to significantly change the ability of the forming GCs (with their unknown initial masses) to retain the polluters ejecta.

4.3. Low-Mg in extragalactic GCs

It was reported by various authors ([Larsen et al. 2014] [Colucci et al. 2014] [Sakari et al. 2015]) that the integrated light, high-resolution abundance determinations of extragalactic GCs tend to have [Mg/Fe] significantly below that of MW GCs, around [Mg/Fe]$=0$ dex and lower, rather than 0.3–0.4 dex. This observational fact is difficult to explain with problems in the abundance analysis alone: the comparison by [Colucci et al. 2016] highlights an underestimate of [Mg/Fe] of $\sim 0.2$ dex with integrated light spectroscopy for some Galactic GC, while Larsen et al. (in preparation) find systematic effects of 0.1 dex at most. The Mg underabundance is not seen in other $\alpha$-element abundances, that are consistent with the typical $\alpha$-enhancement expected from metal-poor GCs in the respective galaxies. In other words, [Mg/$\alpha$] in these metal-poor, extragalactic GCs is lower than in MW GCs with similar metallicity.

Figures 3 and 4 show that some Galactic GCs – not all – contain a fraction of stars well below [Mg/Fe]$=0$ dex. The question then is whether the fraction of low-Mg stars and the Mg spread caused by a normal Mg-Al anticorrelation would be sufficient to produce an average GC $<\text{[Mg/Fe]}$ close to Solar or even lower, as observed in extragalactic GCs (Larsen 2016). While a deeper investigation of this topic is outside the scope of the present paper, we can use the collected GES and literature samples to understand if anti-correlations are at least a viable explanation for the observed low [Mg/$\alpha$] abundances in many extragalactic GCs. In practice, we averaged the [Mg/$\alpha$] measurements for stars in each GC, which is appropriate because they are based on relatively weak absorption lines, but can be an incomplete representation of the abundance in the whole GC and on the proportions of stars with different Mg content. Integrated light measurements, on the other hand, represent a complete average – weighted by star brightness and cut by limiting magnitude – of a GC (see [Colucci et al. 2016] for a comparison between the two methods).

We collected literature data on extragalactic GCs in M 31 ([Colucci et al. 2009, 2014] [Sakari et al. 2015]), the LMC (Large Magellanic Cloud, [Mucciarelli et al. 2008, 2009, 2010, 2014], [Johnson et al. 2006] [Matekula et al. 2012], the Fornax dwarf galaxy ([Letarte et al. 2006] [Larsen et al. 2012a], and WLM (Wolf-Lundmark-Melotte galaxy, [Larsen et al. 2014]). To illustrate the effect, we plotted the data for extragalactic GCs together with the MW field samples and the Galactic GCs from the collection described in the previous section (Figure 5). The Figure shows the average or integrated abundance of each GC, where the $\alpha$-elements are represented by Ca and Si, that are present in all the used studies. As can be noticed, many extragalactic GCs have normal $\alpha$-enhancement but low [Mg/Fe], and as a result their [Mg/$\alpha$] ratios are below zero. The MW GCs however, all have [Mg/Fe] $\geq 0.4$ dex – with very few exceptions – and have a spread compatible with the errors and the internal Mg spread of Figure 4.

To our knowledge, the only Galactic GC that contains a sufficient fraction of stars (50%) with a sufficiently low [Mg/Fe] is NGC 2419 ([Mucciarelli et al. 2012], reaching as low as [Mg/Fe]$=-1.0$ dex. Based on the complicated chemistry of NGC 2419, it was suggested that it has extragalactic origin ([Mucciarelli et al. 2012] [Cohen & Kirby 2012] [Carretta et al. 2013b] [Ventura et al. 2012]), which would fit the observed data trend. On the other hand Rup 106, which is known to have low [Mg/Fe] ([Villanova et al. 2013]), has a perfectly normal [Mg/$\alpha$], because its stars are not $\alpha$-enhanced. We conclude that it is difficult to explain the low integrated [Mg/$\alpha$] values of many extragalactic GCs with the typical Mg-Al anti-correlation observed in Galactic ones. A more extreme Mg depletion and a larger fraction of stars with such low Mg would be required, similarly to what observed in NGC 2419.

Apart from the extreme morphology of the Mg-Al anti-correlation observed for example in NGC 2419 (an internal effect), there is an additional explanation for the low average
Fig. 6. The average [Mg/Fe], [α/Fe], and [Mg/α] of our collected GES and literature sample of 28 MW GCs (green circles, see Section 4.1 and of the literature sample of extragalactic GCs (purple squares, see Section 4.3). The MW reference population is drawn from the GES iDR4 sample (black dots) and from the SAGA database of metal-poor stars (grey dots). We also plotted NGC 2419 as a yellow upward triangle and Ru 106 as a yellow downward triangle.

[Mg/α] of some extragalactic GCs, linked to the global chemical evolution of their host galaxies (an external effect). It has been observed that in dwarf galaxies [Mg/Fe] is lower than the average α-enhancement for stars close to the "knee" of the [α/Fe] trend. This was explained considering that SNe Ia produce some amounts of Ca, Si, and Ti but not Mg, which is produced only by SNe II (Tsujimoto & Bekki 2012). In that case, we should observe a progressively lower [Mg/α] in the field stars as [Fe/H] increases (as in Figure 10 by Mucciarelli et al. 2012, for the LMC). The exact distribution would be governed by the global star formation rate of each galaxy, which governs the metallicity at which the knee occurs.

Both the external and internal explanations appear viable at the moment, and they might also operate simultaneously. Further information could be obtained: (1) by obtaining large and homogeneous samples of field stars with [Mg/α] and [Fe/H] measurements to compare with the available GC measurements on a galaxy-by-galaxy basis, and (2) by obtaining for the nearest extragalactic GCs large sample of individual star abundances.

5. Summary and conclusions

We used GES iDR4 data on calibrating globular clusters to explore the Mg-Al anti-correlation, which is well measured in the GES observing setups and varies significantly from one GC to the other, and therefore can provide strong constraints on the GC properties that control the anti-correlation phenomenon.

Even if iDR4 is a preliminary and intermediate data release, it was the first one in which many different loops of the internal and external calibration were closed in the complex GES homogenization workflow (see P16, Hourihane et al., in preparation, and Randich et al., in preparation). As result, the agreement between UVES and GIRAFFE is within the quoted uncertainties, with 0.10–0.15 dex median differences; there are no significant trends of abundance ratios with the APs, in particular with $T_{\text{eff}}$ or logg; and there are small offsets with the high-resolution literature data of no more than 0.1 dex. We also add a new GC, NGC 5927, one of the most metal-rich GCs, that was included in GES to facilitate the internal calibration in conjunction with open clusters.

Given the excellent agreement with the literature, we assembled a homogenized database of $\approx 1300$ stars in 28 GCs with [Fe/H], [Mg/Fe], and [Al/Fe] measurements from GES iDR4, the FLAMES GC survey (Carretta et al. 2009a and other papers cited above), and the APOGEE survey (Mészáros et al. 2015). We explored two different open topics as a demonstration of the presented data quality. The first topic concerns the dependency of the Mg-Al anti-correlation extension with GC global parameters. In particular, it was suggested by Carretta et al. (2009a) that the extension depends on both mass and metallicity, but no formal analysis was performed in that paper owing to the limited sample. The suspicion was supported by the Mészáros et al. (2015) data. However a different analysis by Cabrera-Ziri et al. (2016) found a very weak relation between the Mg-Al extension and [Fe/H] with a large spread and low statistical significance from a literature database of 20 GC measurements. We profited from our large homogenized sample, that includes NGC 5927, and we employed a linear fit on cluster mass and metallicity simultaneously. Our analysis removes any remaining doubt about the fact the the Mg-Al anti-correlation extension depends on both mass and metallicity. Adding age as a third parameter worsened the fit and we concluded that the Mg-Al anti-correlation does not change significantly with age.

We also explored another open topic related to the low [Mg/α] measured in some extragalactic GCs (Larsen et al. 2014; Colucci et al. 2014; Sakari et al. 2015), to see whether a highly extended Mg-Al anti-correlation could explain the observed trends. We made the reasonable hypothesis that an average of the available individual star abundances is comparable with the abundances obtained by integrated light spectroscopy (see Colucci et al. 2016 and references therein). We concluded that a normal anti-correlation, no matter how extended, would not reproduce those low [Mg/α] values. A more extreme chemical composition, like that of NGC 2419 (Mucciarelli et al. 2012; Cohen & Kirby 2012; Carretta et al. 2013b; Ventura et al. 2012) would be required. Besides this explanation, related to the internal GC chemical properties, there is another external explanation related to the global chemical evolution properties of the host galaxy and the yields of SNe type Ia and II, but the data available so far do not allow to discriminate between the two, that could be either mutually exclusive or coexist in different GC populations.

We conclude that the GES data have a quality sufficient to explore the presented and many other topics related to the chemistry of GCs, providing clear results. When the whole sample of GCs and of the observed stars will be analyzed, including also elements that are not completely determined in iDR4, it will be possible to statistically analyze the entire set of elements that vary in GCs.

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