Miniaturized Microstrip Branch-Line Coupler with Good Harmonic Suppression Based on Radial Stub Loaded Resonators

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Abstract—In this paper, a novel miniaturized microstrip branch-line coupler (BLC) with good harmonic suppression using radial stub loaded resonators is proposed. The novel structure has two significant advantages, which not only effectively reduces the occupied area to 10.3% of the conventional BLC at 0.5 GHz, but also has high 14th harmonic suppression performance. The measured results indicate that a bandwidth of more than 121 MHz has been achieved while the phase difference between $S_{21}$ and $S_{31}$ is within $90^\circ \pm 1.5^\circ$. The measured bandwidth of $|S_{21}|$ and $|S_{31}|$ within $3 \pm 0.4\,\text{dB}$ are 146 MHz and 151 MHz, respectively. Furthermore, the measured insertion loss is comparable to that of a conventional BLC. To validate the design concept, a new miniaturized planar BLC with good harmonic suppression using radial stub loaded resonators is designed and fabricated. Simulated and experimental results are achieved with good agreement.

1. INTRODUCTION

Branch-line coupler (BLC) is widely used at microwave frequencies in the design of microwave circuits such as power dividers, balanced amplifiers, and balanced filters [1]. Currently there are two drawbacks for the conventional microstrip BLC design. Firstly, a conventional BLC is composed of four quarter-wavelength transmission-line sections at the designed frequency, which will result in a large occupied area especially at low frequency. Secondly, the conventional design also has harmonics that occur at integral multiples of the fundamental operation frequency. These properties will degrade the performance of the coupler. Therefore, much work has been reported in recent years to achieve both compact design and harmonic suppression for the BLC [2–15].

Usually there are two methods to design a compact planar microstrip BLC with harmonic suppression. The first method is to load the coupler with shunt open-stubs. By loading shunt open-stubs inside the free area of the BLC, a BLC was designed with a size reduction of 37% to the conventional design at 1.8 GHz [5]. Based on a similar idea, a BLC was proposed that had the properties of 42% size reduction at 2.4 GHz and 5th harmonics suppression [6]. However, further improvement should be carried out on size reduction and harmonic suppression. The second design method is to introduce slow-wave resonators in the coupler structure. Using compensated spiral compact microstrip resonant cells, a BLC was introduced with its area reduced to 24% of the conventional one together with 2nd and 3rd harmonics suppression at 2.4 GHz. However, the isolation performance is not ideal [7]. By introducing high-low impedance resonators inside the free area of the coupler, a slow-wave BLC was proposed with its area reduced to 28% of the conventional one at 2.0 GHz. Even so, it only has 2nd harmonic suppression performance [8]. On the other hand, size reduction methods were also reported in [9–11]. These couplers achieved compact size, but the harmonic suppressions needed improvement.

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A new microstrip BLC with compact size and wideband harmonic suppression using radial stub loaded resonators is present based on our previous works [12]. For this purpose, one BLC with operation central frequency located at 0.5 GHz using radial stub loaded resonators is designed, fabricated, and measured. Measured results indicate that the proposed branch coupler not only effectively reduces the occupied area to 10.3% of the conventional BLC at the same operation frequency, but also has high 14th harmonic suppression performance. Furthermore, the proposed novel coupler has a bandwidth of more than 121 MHz, while the phase difference between $S_{21}$ and $S_{31}$ is within $90^\circ \pm 1.5^\circ$. To validate the design theory, a new miniaturized planar BLC with good harmonic suppression using radial stub loaded resonators has been designed and fabricated. Good agreement between measured and simulated results is provided.

2. CIRCUIT DESIGN

The layout of the proposed BLC is shown in Fig. 1, which consists of eight radial stub resonators loaded inside the free area of a conventional BLC. Each radial stub resonator is composed of a short high-impedance line and a long low-impedance line. The length of the high-impedance line is very short and less than $\lambda/10$, where $\lambda$ is the guided wavelength at the operation frequency. Therefore, each high-impedance line can be deemed as a lumped element with negligibly small value. The inductance effect to the per unit length of the main transmission lines between two adjacent ports can be ignored since it is trivial. The capacitances caused by the low-impedance lines are loaded parallel with the main transmission lines in a distributed form. This will increase the per unit length capacitance of the main transmission lines between two adjacent ports.

![Figure 1. Topology of the proposed BLC.](image)

Figure 2 shows the equivalent circuit of the proposed BLC [15]. We can clearly see from this figure that the loaded high-low impedance resonators will introduce extra parallel capacitances denoted as $C_{11}$ and $C_{12}$ in the coupler, where $C_{11}$ and $C_{12}$ are the capacitances caused by the couplings between the loaded resonators and the ground. The propagation constant $\beta$ and working frequency are given by:

$$\beta = \omega \sqrt{L_0(C_0 + C_1)}$$

(1)
\[ f_c = \frac{1}{2\pi\sqrt{L_0C_0}} \]  

(2)

where \( L_0 \) and \( C_0 \) are the distributed inductance and capacitance for the main line of the BLC per unit length, respectively, and \( C_1 \) is the effective distributed capacitance per unit length caused by the shunt capacitance \( C_{11} \) and \( C_{12} \). The proposed BLC is designed based on the slow-wave loading mentioned above.

![Equivalent circuit of the proposed BLC.](image)

**Figure 2.** Equivalent circuit of the proposed BLC.

With further optimal design by the full-wave electronic magnetic (EM) simulation software, the final structure parameters of the proposed BLC are as follows: \( W_1 = 1.7 \text{ mm}, W_2 = 1.0 \text{ mm}, R_1 = 17.7 \text{ mm}, R_2 = 17.3 \text{ mm}, R_3 = 17.0 \text{ mm}, R_4 = 16.2 \text{ mm}, R_5 = 13.0 \text{ mm}, R_6 = 12.0 \text{ mm}, R_7 = 8.0 \text{ mm}, \theta_{01} = 20^\circ, \theta_{02} = 63^\circ, \theta_{03} = 34^\circ \). They can be easily implemented by the standard printed-circuit-board etching processes. The substrate used here has a relative dielectric constant of 2.94 and thickness of 0.762 mm, and the total area of the proposed BLC is 630.12 mm\(^2\).

3. SIMULATION AND MEASUREMENT RESULTS

Simulation was completed with HFSS 14.0. Measurement was carried out on an Agilent 8511B network analyzer. Fig. 3 shows the simulated results of \( S \)-parameters. Fig. 4 shows the measured \( S \)-parameters.

![Simulated S-parameters of the proposed BLC.](image)

**Figure 3.** Simulated \( S \)-parameters of the proposed BLC. (a) Frequency range of 0.1 to 7.5 GHz. (b) Frequency range of 0.1 to 1.0 GHz.
of the proposed BLC. We can find that they are in good agreement. Referring to the measured results in Fig. 4, the central frequency located at 0.5 GHz can be clearly observed. At this central frequency, the measured $S_{21}$ is 3.12 dB, and $S_{31}$ is 3.10 dB, while the measured bandwidth of $|S_{21}|$ and $|S_{31}|$ within $3 \pm 0.5$ dB are 146 MHz and 151 MHz, respectively.

Figure 4. Measured S-parameters of the proposed BLC. (a) Frequency range of 0.1 to 7.0 GHz. (b) Frequency range of 0.1 to 1.0 GHz.

Figure 5. Phase difference between $S_{21}$ and $S_{31}$.

Table 1. Performance comparison of other couplers.

| Ref.     | Relative Area | Harmonic Suppression |
|----------|---------------|----------------------|
| Conventional | 100%         | No                   |
| [5]      | 63%           | N/A                  |
| [6]      | 58%           | 5th                  |
| [7]      | 24%           | 3rd                  |
| [8]      | 28%           | 2nd                  |
| [9]      | 29.33%        | 4th                  |
| [10]     | 26.8%         | 2nd                  |
| [11]     | 25.0%         | 4th                  |
| This Work | 10.3%         | 14th                 |
We can also observe that the 14th harmonic signals have been effectively suppressed with $S_{21}$ and $S_{31}$ lower than a criterion of $-10$ dB from Fig. 4(a). This means that the proposed new coupler can protect specialized communication system from the interference of the unwanted signals from 1.0 GHz to 7.0 GHz. This property is very useful for modern communication system to operation in high performance. In order to study the size reduction performance, we investigated the circuit area of conventional one at the same frequency and found that the cost area is 3089.77 mm$^2$. This means that the proposed BLC can effectively reduce the occupied area to 10.3% of the conventional coupler.

Figure 5 shows the phase difference between $S_{21}$ and $S_{31}$. According to a criterion of $\pm 1.5^\circ$ around the optimum $90^\circ$ phase difference, the frequency range is from 0.44 GHz to 0.56 GHz corresponding to a bandwidth $24.0\%$. To demonstrate the superior performance of the proposed coupler, Table 1 shows the performance comparison of the proposed design with several previous designs. The advantages of the proposed coupler can be clearly observed.

4. CONCLUSION

In this work, a new miniaturized planar BLC with good harmonic suppression using radial stub loaded resonators is proposed. Due to eight radial stub resonators placed inside the free area of a conventional BLC, the novel structure has effectively reduced the occupied area to 10.3% of the conventional design at 0.5 GHz and has high 14th harmonic suppression performance. One sample microstrip BLC has been fabricated, measured, and compared with the previous designs. Results indicate that the proposed coupler has the properties of compact size, low insertion loss, and wideband harmonic suppression performance. To summarize, the proposed planar BLC is very useful for modern wireless communication systems owing to its marked properties of simple topology, compact size, and excellent performance.

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