Particle size effects in the antiferromagnetic spinel CoRh$_2$O$_4$

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Abstract

We report the particle size dependent magnetic behaviour in the antiferromagnetic spinel CoRh$_2$O$_4$. The nanoparticles were obtained by mechanical milling of bulk material, prepared under sintering method. The XRD spectra show that the samples are retaining the spinel structure. The particle size decreases from 70 nm to 16 nm as the milling time increases from 12 hours upto 60 hours. The magnetic measurements suggest that the antiferromagnetic ordering at $T_N \approx 27$K exists in bulk as well as in nanoparticle samples. However, the magnitude of the magnetization below $T_N$ increases with decreasing particle size. Considering the fact that Rh$^{3+}$ has strong octahedral (B) site occupation and no change in $T_N$ of bulk and nanoparticle samples, we believe that the observed magnetic enhancement is not related to the cationic redistribution between tetrahedral (A) and octahedral (B) sites of the spinel structure. In our opinion, the observed effect is a consequence of decreasing coherent length of antiferromagnetic coupled core spins and increasing number of the frustrated shell in the core-shell model of anoparticle.

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I. INTRODUCTION

The nanoparticle spinel ferrites are under the intensive investigation in recent years because of their potential applications in nanoscience and technology as high density magnetic recording media, magnetic carriers in ferro fluids, magnetically guided drug carrier etc. [1]. The theoretical interest for such type of materials are growing up to understand the structural and magnetic modifications taking place in a system when the dimension of the particles (crystal size) are reduced to atomic scale [2–5]. Several novel phenomena like magnetic quantum tunneling [2], superparamagnetism, surface spin canting [6], grain boundary effect [7], non-equilibrium cation distributions among the inequivalent lattice sites [8] are attracting the spinel ferrites. In spinel lattices the anions (O\(^{2-}\), S\(^{2-}\) ions) form a cubic close packing, in which the interstices are occupied by tetrahedral (for m A sites or sublattice) and octahedral (form B sites or sublattice) coordinated cations to the oxygen anions. The competition between various type of superexchange interactions via O\(^{-2}\) ions, i.e., intersublattice superexchange interactions (J\(_{AB}\)) between ions of both sites and intra-sublattice superexchange interactions (J\(_{AA}\) and J\(_{BB}\)) between ions of same site, shows a variety of magnetic states like ferrimagnet/ferromagnet, antiferromagnet, superparamagnet and spin glass in spinel oxides [3]. When the particles size are reduced in the nanometer scale a drastically different kind of magnetic behaviour were observed in spinel oxides in comparison with the bulk material [5,9]. This has been explained in terms of site disorder, i.e., the cations redistribution between A and B sites [10,11] and finite size scaling effect [12].

It is established that for long range ferrimagnetic ordering in spinel oxide, the necessary condition is |J\(_{AB}\)| >> |J\(_{BB}\)| >> |J\(_{AA}\)| [13]. However, if we compare the antiferromagnetic ordering temperature (T\(_N\)) of two typical normal spinel antiferromagnets ZnFe\(_2\)O\(_4\) with T\(_N\) \(\sim\) 10K (where only J\(_{BB}\) exist) and CoRh\(_2\)O\(_4\) with T\(_N\) \(\approx\) 27K (where only J\(_{AA}\) exist) [14], it can be understood that |J\(_{BB}\)| >> |J\(_{AA}\)| may be true only for long range order ferrimagnetic spinels (where both A and B sites are occupied by magnetic ions) but not for all the cases, particularly, for the spinels with magnetic ion only on A site. Unfortunately, most of the
reports deal with the nanoparticle spinels where either B or both A and B sites are occupied by magnetic ions [8,6,10]. It will be very interesting to investigate the particle size effect on antiferromagnetic spinels with magnetic moment only on A sites. Recently, M. Sato et al. [15] reported the disappearance of antiferromagnetic ordering at 33K of bulk Co$_3$O$_4$ spinel and the appearance of a variety of magnetic phases like ferrimagnet, superparamagnet and spin glass when the particle size is reduced to nano scale. For Co$_3$O$_4$ spinel oxide, the B site is fully occupied by non-magnetic Co$^{3+}$ (3d$^6$) ions and A site is occupied by magnetic Co$^{2+}$ ions, which gives rise to long range antiferromagnetic order due to Co$^{2+}$-O$^{2-}$-Co$^{2+}$ ($J_{AA}$) superexchange interactions with $J_{AB} = J_{AA} = 0$ [15]. CoRh$_2$O$_4$ (structure: (Co$^{2+}$)$_A$[Rh$^{3+}$]$_2$O$_4$) with $T_N \approx 27$K is an analogue of Co$_3$O$_4$ (structure: (Co$^{2+}$)$_A$[Co$^{3+}$]$_2$O$_4$), where Co$^{3+}$ is replaced by non-magnetic Rh$^{3+}$ (4d$^6$) ions [14]. Recently, a significant research interest is focusing on the geometrically frustrated antiferromagnets (Ising or Heisenberg in nature). The change of degeneracy and topology of the antiferromagnetic ground state (Neel order) of such a system can show various kind of interesting magnetic properties such as quantum disordered ground states [16], quantum zero-temperature spin fluctuation effect, where the system do not order and remain in a ”collective paramagnetic state” down to zero temperature [17]. The degeneracy of the antiferromagnetic ground states can be reduced by introducing random non-magnetic dilution [18] or by strain induced positional disorder [19]. Even some authors introduced the concept of ordering in geometrically frustrated system due to disorder while the degeneracy is reduced in the system [16,18]. Mechanical milling is one of the most convenient method which can introduce the positional disorder in the lattices and simultaneously reduce the particle size of the material.

In this paper, we address the nature of magnetic order as a function of particle size in CoRh$_2$O$_4$ prepared by mechanical milling. The samples are characterized by XRD and magnetization measurements have been performed using SQUID magnetometer.
II. EXPERIMENTAL

We have synthesized nano particles CoRh$_2$O$_4$ spinel oxide by mechanical milling of the bulk material using Fritsch Planetary Mono Mill "Pulverisette 6". For bulk material, the stoichiometric mixture of Co$_3$O$_4$ (99.5% from Fluka) and Rh$_2$O$_3$ (99.9 % from Johnson Matthey) oxides was taken for CoRh$_2$O$_4$ composition. The mixture was mechanically ground for 2 hours and was pelletized. The pelet was sintered at 1000$^0$C for 12 hours and at 1200$^0$C for 48 hours. The sample was then cooled to room temperature at 2-3$^0$C/minute. A typical crystalline spinel structure was confirmed by X ray diffraction (XRD) spectra using Philips PW1710 diffractometer with Cu K$_\alpha$ radiation. The bulk material was powdered using a 80 ml agate vial with 10 mm agate balls. We intentionally did not use the stainless bowl and balls to avoid any kind of contamination of transition metals (Fe, Cr, Ni). The samples were milled with ball to powder mass ratio 12:1 and at a rotational speed of 300 rpm. Small amount of samples were taken out from the bowl after 12 (mh12 sample), 24 (mh24 sample), 36 (mh36 sample), 48 (mh48 sample) and 60 (mh60 sample) hours of milling for our studies. The dc magnetization measurements were performed using SQUID (quantum design) magnetometer.

III. RESULTS AND DISCUSSION

A. Structural properties

The X ray diffraction spectra (Fig.1) show that the crystalline nature of bulk CoRh$_2$O$_4$ decreases with increasing milling time. It should be noted that the crystalline peaks of milled samples, as shown for 311 line (Fig. 1b), shows small shift to higher scattering angle (2$\theta$) with respect to the bulk sample. However, there is no extra lines in XRD spectra for as milled samples in comparison with bulk sample. This suggests that small amount of lattice disorder or lattice strain is introduced in the system as the particle size is reduced by mechanical milling but without changing the crystal symmetry of spinel structure [20,21].
The decrease of lattice parameter (see Table 1) suggest that it is related with the decrease of particle size as a function of milling time [22]. The transmission electron micrographs (TEM) confirm the decrease of particle size from 70 nm (12 hours milling) to 16 nm (60 hours milling) (see Table 1). The broad lines in XRD spectra is due to this decrease of particle size, where the thermal fluctuation of the small coherent (crystalline) zones broaden the peaks [21]. The XRD peak shift of the milled samples suggest that the non-uniform microstrain developed at the lattice sites during mechanical process may also contribute such type of peak broadening [7]. In literature the small shift of XRD peak is very often neglected. But a critical observation of this type of shift is very important in correlating the physical properties with mechanical strain induced change in a sample [20].

B. Magnetic properties

The inset of Fig. 2 (left scale) shows the zero field cooled (ZFC) and field cooled (FC) magnetization data for CoRh$_2$O$_4$ bulk sample, measured at 100 Oe dc magnetic field. The bulk sample shows antiferromagnetic ordering at $T_N \approx 27.5K \pm 0.5K$ and magnetic irreversibility between ZFC and FC magnetization below $T_N$. The ZFC magnetization data at $T > 50K$ are well fitted with Curie-Weiss law (Fig.2 inset, right scale)

$$\chi = \frac{C}{T - \theta_A} \quad (1)$$

The Curie constant ($C = N\mu_{eff}^2/3k$, $N$ is the number of CoRh$_2$O$_4$ formula unit per gram of the sample) gives the effective magnetic moment ($\mu_{eff}$) = 4.60$\pm$0.10 $\mu_B$) per formula unit for the bulk sample. The asymptotic Curie temperature ($\theta_A$) is $\approx -(45 \pm 2)K$. These values are consistent with the reported values $\mu_{eff} = 4.55 \mu_B$) and -30K for bulk CoRh$_2$O$_4$ spinel [14]. The negative value of $\theta_A$ indicate that on lowering the temperature the antiferromagnetic ordering is saturated at $T_N \approx 27.5K$ and the system shows strong antiferromagnetic ordering below 27.5K. This indicate the magnetic phase of our bulk CoRh$_2$O$_4$ sample is consistent with the reported one. Interestingly, all the milled samples (with smallest particle size $\sim 16$ nm) are showing (Fig.2, log-log scale) antiferromagnetic ordering at $T_N \approx$
(27.5±0.5)K with magnetic irreversibility between ZFC and FC magnetization when temperature decreases below $T_N$. The larger value of FC magnetization than ZFC magnetization below $T_N$ suggests the field induced metastable magnetic state during field cooling process of the samples [23]. It is also found that the ZFC magnetization data at $T > 50$K fit with Curie-Weiss law (Fig.2 inset, right scale), as an example shown for mh60 sample, for all the milled samples. The effective magnetic moment ($\mu_{eff}$) and $\theta_A$ values are shown in Table 1. We see that the effective magnetic moment value is increasing with decreasing the particle size. Similar kind of magnetic enhancement was observed by F. Liu et al. [24] and was attributed as a function of the reduction of coordination number of the surface spins when the dimensionality of ferromagnetic particles were reduced. The ratio of $\theta_A$ and $T_N$ is always greater than 1. According to ref. [25], if this ratio quantify the degree of magnetic frustration in a geometrically frustrated antiferromagnet, then we can say that geometrical frustration and the instability of antiferromagnetic ordering is increasing with decreasing the particle size by mechanical milling of bulk CoRh$_2$O$_4$ spinel. The main characteristic feature is that both the ZFC and FC magnetization are increasing at $T<<T_N$, which is very similar to paramagnetic or superparamagnetic [26] or ferrimagnetic contribution [15] in the samples. Even, the increase in the magnitude of magnetization below $T_N$ can be assigned due to the increasing number of uncompensated/frustrated spins [27] as the particle size decreases. However, the temperature dependence of inverse of zero field cooled susceptibility ($H/ZFC$) at $T < T_N$ shows downward curvature in Fig.3. Interestingly, inset of Fig.3 shows that $H/ZFC \propto T^{\alpha}$ below 10K and the constant value $\alpha$ increases with decreasing particle size. This indicates that the magnetization below $T_N$ are something different from a typical paramagnet or superparamagnetic behaviour, where inverse of susceptibility should be linear with temperature and $\alpha$ should be 1. M. Sato et al. [15] suggested similar kind of magnetic behaviour below $T_N$ due to the appearance of ferrimagnetic phase when the particle size of the antiferromagnetic spinel Co$_3$O$_4$ was reduced to 15 nm.

The most important feature in Fig.4 is that the excess amount of zero field cooled magne-
tization of milled samples $\Delta M_{mb} (= M_{zfc}^{\text{milled}} - M_{zfc}^{\text{bulk}})$ over the bulk sample not only increases at $T < T_N$, but also depend on the particle size. We have found in Fig.4 inset that $\Delta M_{mb}$ vs $T$ follows a scaling law at $T << T_N$ in the form

$$\Delta M_{mb} = (\Delta M_{mb})_0 T^{-(0.937 \pm 0.002)}$$  

where the constant $(\Delta M_{mb})_0$ depends on the particle size and linearly increases as $8.952 \times 10^{-3}$, $1.475 \times 10^{-2}$, $2.111 \times 10^{-2}$, $2.821 \times 10^{-2}$, and $3.576 \times 10^{-2}$ (in emu/g unit) for mh12, mh24, mh36, mh48 and mh60 samples, respectively.

The excess in of FC magnetization over the ZFC magnetization (Fig.5a), i.e., $\Delta M_{FZ} = M_{FC} - M_{ZFC}$ increases below $T_N$ in a typical manner which has similar character as the uncompensated interfacial antiferromagnetic spins exhibit in Ni$_{81}$Fe$_{19}$/CoO bilayers [28]. In case of spinel oxides, the surface cations have various number of next nearest neighbours on both A and sites. When the particle size are reduced to nanometer range, some of the exchange bonds are broken and coordination number to oxygen ions are also decreased. This results a distribution of net exchange fields, which control the surface magnetism of the particle [6]. This exchange field is proportional to the spin density of the uncompensated antiferromagnetic spins at the surface [28]. The magnitude of $\Delta M_{FZ}$ will depend on the number of uncompensated spins and also the exchange interactions between field aligned (uncompensated surface) spins and the antiferromagnetic core spins. This argument invokes the core/shell picture [6] for our samples, where the shell thickness, consisting of uncompensated spins, is increasing with decreasing the particle size by decreasing the core volume.

The zero field cooled magnetization at 100 Oe, 1 kOe and 1 Tesla field for rh48 sample (particle size $\sim 19$ nm) (Fig.5b) do not show any appreciable change of $T_N$ with fields. This suggests that dominant antiferromagnetic order (LRAO) still exists for the nano particle samples. However, it is the fact that long range antiferromagnetic ordering is proportional to the divergence of magnetization at $T_N$. Qualitatively, we can say, LRAO is proportional to the difference between peak magnetization ($M_{ZFC}^{\text{peak}}$) at $T_N$ and minimum of magnetization ($M_{ZFC}^{\text{min}}$) below $T_N$. Following this argument, we see (Fig.5a, inset) the difference
between peak magnetization and minimum magnetization below $T_N$, i.e., $\Delta M_{pm} = (M_{ZFC}^{\text{peak}}\text{-}M_{ZFC}^{\text{min}})/M_{ZFC}^{\text{peak}}$, reduces from 27\% (for bulk sample) to 0.5\% (for mh60 sample). This confirms that although antiferromagnetic ordering is still observed below $T_N$, the magnetic disorder is increasing when the particle size decreases by mechanical milling [19].

Fig.6 shows the zero field cooled magnetization as a function of magnetic field at 5K for all the samples. The straight line nature of $M$ vs $H$ plot for $H = -3$T to $+7$T range shows a typical antiferromagnetic bulk sample. The antiferromagnetic nature is still very prominent for mh12 sample. But the downward curvature of the $M$ vs $H$ curve (see for mh36 and mh60 samples) in the positive field range suggests that some magnetic contribution is increasing as the particle size decreases. From the Arrot plot ($M^2$ vs $H/M$), we have found no spontaneous magnetization for any samples, where as the linear extrapolation of the data (for $H \geq 4$ Tesla) to the $M$ axis gives some finite values of $M_0T$ for all milled samples. The $M(H)$ data, therefore, confirm that there is no ferromagnetic ordering in system. The magnetic contribution arising in decreasing the particle size can be attributed as disorder and dilution effect in antiferromagnetic spinel [15]. The increase of $M_0T$ (Fig.6 inset) with increasing the milling time indicates that although the samples does not show any ferromagnetic spontaneous magnetization but field induced magnetic ordering is possible for antiferromagnetic nano particles [29]. Fig.7 shows the $M$ vs $H$ data at different temperatures for the 48 hours milled sample. The linear extrapolation of $M$ for $H \geq 4$T to $H= 0$T axis shows (Fig. 7 inset) that the magnetization ($M_{0T}$) first decreases with increasing temperature down to $\approx 16$K and then increasesupto 27K. The temperature dependence of $M_{0T}$ is very similar to the temperature dependence of magnetization at $T < T_N \approx 27.5$K for the same sample. This type of magnetic behaviour suggests that there is certainly a competition between antiferromagnetic order and magnetic order due to disorder effect in the nano particle samples [18]. Further, it can be suggested that the disorder effect will dominate as the temperature is well below of $T_N$. 
IV. SUMMARY

The bulk CoRh$_2$O$_4$ spinel is an antiferromagnet with ordering temperature $T_N \approx 27.5$K. When the particles size of CoRh$_2$O$_4$ are reduced by mechanical milling, the signature of antiferromagnetic order at $\approx 27.5$K are still observed upto particle size $\approx 16$ nm. In case of nano particles, the magnetization below $T_N$ is enhanced with respect to the bulk sample, which is followed by a scaling law. Since the antiferromagnetic ordering temperature at $T_N$ is unchanged, the enhancement in magnetization can not be attributed due to the site exchange [30] between Co$^{2+}$ and Rh$^{3+}$ ions when the particle size decreases by mechanical milling. Under this circumstances, the tetrahedral (A) sites occupy magnetic Co$^{2+}$ ions and octahedral (B) sites occupy non-magnetic Rh$^{3+}$ ions and excludes the possibility of conventional ferrimagnetic contribution in this system. The temperature dependence of the inverse susceptibility below 10K also suggest that the enhancement of magnetization is not due to typical superparamagnetic contribution of the nano particles.

Therefore, we are introducing the core-shell structure of the nano particles [6]. The core consists of antiferromagnetic spins and shell consists of few layers of surface spins. The surface spins are coupled by superexchange interactions (via O$^{2-}$ ions) to the core spins. In case of bulk sample the length scale of antiferromagnetic interactions can span upto many particles. When the particle size is reduced to nanometer scale by mechanical milling, some of the A-O-A superexchange bonds are broken and become frustrated. These frustrated bonds (surface spins) will create exchange anisotropy field at the interfacial surface [6,28]. This type of anisotropy field will give rise a preferential magnetic ordering of the loosely bound shell spins, whereas the tightly bound core spins will remained as antiferromagnetically aligned.
V. CONCLUSIONS

Based on our dc magnetic measurements, it can be concluded that the total magnetization of the nanoparticle $M = M_{\text{core}} + M_{\text{shell}}$, where $M_{\text{core}}$ is magnetic contribution from core spins and $M_{\text{shell}}$ is magnetic contribution from shell spins. The competition between magnetic ordering of shell spins and the antiferromagnetic ordering of core spins guide the magnetic behaviour of our samples. The shell thickness is increasing in expense of core volume when the particle size decreases. This is related to the decrease of coordination number of the surface (shell) spins and increase of magnetized state of the surface spins due to increasing random exchange fields, as the size of the particle decreases. Consequently, the magnetic moment will be enhanced in nanoparticles. This is called disorder induced magnetic ordering in antiferromagnetic nanoparticle.

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Table 1. Particle size (from TEM photographs), Lattice parameter (Å) (from XRD data), 311 peak position (from XRD data), effective magnetic moment ($\mu_{\text{eff}}$) (from M vs T data), Asymptotic Curie temperature ($\theta_A$) (from M vs T data) as a function of milling hours.

| Sample milling time | Particle size | $a$ (Å)     | $2\theta$ (deg) | $\mu_{\text{eff}}$ ($\mu_B$ unit) | $\theta_A$ (K) |
|---------------------|---------------|-------------|-----------------|-----------------------------------|----------------|
| bulk 0h             | few µm        | 8.465±0.002 | 35.47           | 4.599                             | -44.23         |
| mh12 12h            | 70 ±1 nm      | 8.485±0.002 | 35.56           | 4.603                             | -42.80         |
| mh24 24h            | 50 ±1 nm      | 8.427±0.002 | 35.75           | 4.609                             | -42.05         |
| mh36 36h            | 32 ±1 nm      | 8.449±0.002 | 35.71           | 4.627                             | -41.84         |
| mh48 48h            | 19 ±1 nm      | 8.468±0.002 | 35.67           | 4.653                             | -43.81         |
| mh60 60h            | 16 ±1 nm      | 8.459±0.002 | 35.64           | 4.755                             | -51.00         |
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Fig. 1 a) shows the XRD spectra of bulk and milled (mh12, mh24, mh36, mh48 and mh60) samples. b) shows the 311 peak of XRD spectra. The arrow indicates the position of 311 peak.
Fig. 2. Inset (left scale) shows the ZFC and FC magnetization at $H = 100$ Oe for bulk sample. Inset (right scale) shows $H/M$ for bulk and mh60 samples for $H = 100$ Oe. The main panel shows the ZFC and FC magnetization for bulk, mh12, mh24, mh36, mh48 and mh60 samples at $H = 100$ Oe. $T_N$ represent the antiferromagnetic ordering temperature. Solid and dotted lines guide to eye.
Fig. 3 Temperature dependence of inverse zero field cooled susceptibility ($H=100$ Oe/$M_{ZFC}$) for milled samples. The inset shows the experimental data (point symbol) and fit data (lines).
Fig. 4 Temperature dependence of the excess ZFC magnetization of milled samples, measured at $H = 100$ Oe, over bulk sample. The inset shows the expt data (points) and fit data (line) to eq. (2)
Fig. 5  

a) The temperature dependence of excess FC magnetization over ZFC magnetization for all bulk and milled samples. The inset shows the % change of ZFC peak magnetization at $T_N$ over the minimum ZFC magnetization at approx. 15K.

b) Zero field cooled $M/H$ vs $T$ at $H = 100$ Oe, 1 kOe and 1 Tesla for 48 hrs milled (mh48) sample.
Fig. 6 M vs H (in the range: -3 T to 7T) for bulk, mh12, mh 36 and mh 60 CoRh$_2$O$_4$ samples. Left and right arrow indicate the M axis for the corresponding sample. The inset shows the linear extrapolation of M at H>4T to H =0T value.
Fig. 7 M vs H for 48 hrs milled (mh48) sample. The inset shows the magnetization at 7T and linear extrapolation of M (for H > 4T) data to 0T.