Influence of Different Lateral Bending Angles on the Flow Pattern of Pumping Station Lateral Inflow

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Abstract
A model of the pumping station lateral inflow forebay was established to explore the influence of different lateral bending angles of the pumping station lateral inflow. The lateral bending angles were set at 45° and 60°, and the two schemes were calculated separately. Analyzing the results of the numerical simulation showed that the flow patterns of the diversion passages of different schemes were good, but the advancing mainstream of the 1# inlet passage near the sidewall was seriously deviated after entering the forebay. Most of the water can flow smoothly into the inlet passage, while a small part of the water flowed into the sidewall and formed a backflow, resulting in a large-scale backflow zone near the left sidewall of the forebay. Moreover, the flow in the backflow zone was turbulent, which affected the water inlet conditions of the 1# water flow passage. Comparing the water inlet conditions of the water passage with the numerical simulation results of 45° and 60° bending angles showed that the larger the lateral bending angle of the forebay was, the worse the flow pattern of the water flow, and the more unfavorable the pump operation.

1. Introduction
Irrigation and drainage pumping stations have played a vital role in fighting drought and waterlogging, ensuring increased agricultural production and income and developing the rural economy. The arrangement of several pumping stations is often restricted by objective factors such as water flow conditions and actual topography, such that the arrangement of lateral water intake has to be adopted. When water enters laterally, a certain angle is observed between the water flow direction and the forebay water flow direction, which may cause serious cavitation and vibration and will affect the normal operation of the pump. In rivers with much sediment, it will cause sedimentation and erosion of the bottom of the front pond. Therefore, taking effective rectification measures to improve the inlet flow pattern of the pumping station [1–4] is of great importance to the design and transformation of the pumping station as well as the economy and safety of the project operation.

For a long time, experts and scholars have carried out a large amount of rectification optimization research on the intake buildings of the pumping station and achieved fruitful results. Arboleda et al. [5] used the overall model test method, and the main rectification method was “block,” which adjusted the flow velocity distribution of the section and weakened the lateral flow velocity in the incoming flow, thus obtaining a better rectification effect. Rajendran et al. [6] used Particle Image Velocimetry (PIV) flow field display technology to capture information such as the position of the vortex near the pump inlet and, for the first time, intuitively and quantitatively revealed the vortex’s motion characteristics. Hou [7] used Computational Fluid Dynamic (CFD) methods to study the flow pattern of the pressure forebay of a pumping station, and the good agreement between the calculation results and the empirical formula showed the accuracy and reliability of the CFD calculation method. The numerical simulation results provided a basis for the hydraulic optimization design of the pressure forebay. Liu et al. [8] used gates to control the water levels of the fore and intake sump, numerically simulated the flow patterns of the fore and intake sump before and after the rectification, and concluded that a combination of several engineering
measures such as a discontinuous sill and a pressure plate was adopted. These methods can make the flow velocity distribution of the forebay uniform and effectively improve the efficiency of the pumping station. Ansar et al. [9] took the pumping station inlet tank as the research object, compared and analyzed the numerical simulation results and the test results, and verified that the results obtained by the two methods were the same regardless of whether the pumping station enters the water directly or sideways. Moreover, the numerical calculation results had a high degree of credibility and can satisfy practical applications. Cheng et al. [10] analyzed the turbulence of the forebay caused by the movement characteristics of the curved water flow in the lateral inlet pumping station, which affected the pump inlet conditions, and calculated the 3D flow field of the rectification measures with the combined bottom sill. This approach effectively improved the water inlet conditions of the forebay. Liu et al. [11] proposed adding multiple sets of bottom sills in the forebay of a multunit pumping station, using 3D turbulence numerical simulation calculations, and verifying them through hydraulic model tests, which largely eliminated the backflow and the vortex and substantially improved the flow pattern. The current research on hydraulic characteristics of pumping stations mainly includes theoretical analysis, numerical simulation, and model tests [12–17], each with its own advantages and disadvantages. With the rapid development of computer technology, numerical simulation has become more important in various research fields [18–24], and its research results have important reference value for practical engineering.

2. Numerical Calculation Model and Calculation Method

2.1. Calculation Model. The pumping station studied in this article is a pumping station hub with a lateral water intake. Three pump units are installed in the pump room. The design flow rate of each pump is 4.0 m³/s. The inlet size of the flow passage is 2.36 m (width) × 1.8 m (length). The intake level of the pumping station is 1.9 m, the elevation of the bottom of the drainage canal is 0.0 m, and the elevation of the forebay bottom is −1.0 m. The main functions of the project are flood prevention and drainage. The left side of the pumping station is a self-draining culvert. When the pumping station is operating, the self-draining culvert control gate is closed. The total width of the outlet of the forebay is B, and the length from the center of the inlet of the forebay to the center of the outlet is L. Figure 1 shows that the plan layout of the intake building of the pumping station is mainly based on the 3D modeling and numerical simulation of the original design with lateral bending angles of 45° and 60°.

2.2. Calculation Method and Meshing. ANSYS CFX software is used for numerical simulation, the standard k–ε turbulence model is used for calculation, and the MESH software is used for unstructured meshing of the entire computational domain. The size of the grid is controlled. The selected grid shape is a tetrahedron to meet the calculation requirements. The 3D model grid diagram of the pumping station intake building when the lateral angle of 45° is obtained is shown in Figure 2.

Taking the model with 45° lateral bending angle and the hydraulic loss from the inlet of the approach passage to the outlet of the inlet passage as the characteristic parameter to select the appropriate grid number, the calculation formula is as follows:

$$h_f = \frac{(P_{in} - P_{out})}{\rho g},$$

where $h_f$ is the hydraulic loss, $P_{in}$ is the total pressure at the inlet, $P_{out}$ is the total pressure at the outlet, $\rho$ is the density of water at 4°C, and $g$ is the acceleration of gravity.

The calculation results under different grid numbers are shown in Table 1 and Figure 3. The analysis of grid independence reveals that the final number of grids is 3.58 million, which has a minimal effect.

2.3. Boundary Condition Setting. The inlet of the entire calculation domain is taken from the prototype of the diversion river to the upstream diversion passage at a 10 m section, which is set as the boundary condition of the mass flow, the inlet flow rate is 12 m³/s, and the medium turbulence intensity $T_u = 5\%$. The outlet of the water flow passage is taken as the outlet of the calculation domain. The number of outlets is three. The water flow direction is perpendicular to the outlet section. Each outlet has an average static pressure of standard atmospheric pressure (1 atm) as the outlet condition. The water surfaces of the lead passage and the forebay are free liquid surfaces, and the water level of the forebay does not vary much. The shear stress effect of air on the water surface is neglected. The “rigid cover assumption” is selected in the calculation; that is, the symmetry surface boundary is used. The rest is set as a wall, and a nonslip wall is used for processing.

3. Analysis of Calculation Results

3.1. Calculation Evaluation Index. The uniformity of the axial velocity distribution on the inlet section of the flow passage is an important indicator reflecting the velocity distribution on each section. The uniformity of axial velocity distribution is used to characterize the uniformity of the axial (downstream flow direction) velocity distribution of the inlet section of the flow passage. The larger the value is, the closer it is to 100%. This finding shows that the more uniform the axial velocity distribution of the water flow at the inlet section of each flow passage is, the more in line it is with the pump inlet design conditions. The calculation formula is as follows:

$$V_{au} = \left[1 - \frac{\sum_{i=1}^{n} (V_{ai}/V_{a} - 1)^2}{n}\right] \times 100\%,$$

where $V_{ai}$ is the axial velocity of each node of the section, m/s; $V_a$ is the average axial velocity of the section, m/s; $n$ is the
Approach channel
0.0
45°
0.85B
1:8
–1.0
Forebay
Pump units
1#
2#
3#
L
B

Figure 1: Drawings of pumping station intake buildings under different lateral bending. (a) Layout drawing of the intake building of the pumping station at a 45° bending. (b) Layout drawing of the intake building of the pumping station at a 60° bending.

3.2. Feature Section Selection. Seven characteristic sections of the vertical longitudinal section and horizontal section of the forebay are selected for flow field analysis to study the hydraulic characteristics of the forebay of the project, that is, two vertical longitudinal sections perpendicular to the main flow direction and three horizontal longitudinal sections of the forebay surface layer, middle layer, and bottom layer. Figure 4(a) shows the cut vertical longitudinal section, namely, Sections 1-1 and 2.2. The coordinate of Section 1-1 is \( X_1 = 0.01 \text{ m} \), which is used as the characteristic section of each passage inlet. The flow field diagram of the 1-1 plane of the section is obtained by numerical simulation to analyze the uniformity of the axial velocity distribution on the inlet section of each flow passage. The coordinates of Section 2.2 are \( X_2 = -0.5 \text{ m} \), and the plane velocity vector diagram of Section 2.2 is obtained by numerical simulation to observe the flow pattern of the main flow in front of the water inlet passage visually.

Figure 4(b) shows the horizontal section taken, namely, surface layer a-a, middle layer b-b, and bottom layer c-c, to study the flow pattern and axial velocity distribution of the forebay surface layer, middle layer, and bottom layer. Surface layer a-a section is 0.05 m away from the water surface, and the coordinates of the surface layer, middle layer, and bottom layer are \( Z_a = 1.85 \text{ m} \), \( Z_b = 0.95 \text{ m} \), and \( Z_c = 0.05 \text{ m} \), respectively.

3.3. Numerical Simulation Results of the 45° Lateral Angle Scheme. Considering that the 3D flow field of numerical simulation is more complicated, the flow velocity vector diagram, streamline diagram, and velocity distribution cloud diagram of characteristic sections are drawn. It is conducive to reflect the flow field of the diversion passage, forebay, and water inlet passage of the lateral intake pump station three-dimensionally and intuitively and facilitate the comparative analysis and study of the flow pattern of the entire intake structure.

Figure 5 shows that the water flow in the diversion canal develops smoothly, and the flow pattern is good because the project is a side-inlet forebay. However, after entering the forebay, the main flow of the 1# inlet passage near the sidewall is severely deviated. While most of the water flows into the water inlet passage, a small part of the water is still in the left side of the forebay (this article uses the flow direction to determine the left and right sides) to form a backflow near the sidewall, touching the sidewall and forming a large-scale backflow area. The flow regime in the return zone is turbulent. Therefore, considering that the water flow in the diversion canal is relatively smooth and the water flow in the forebay is more turbulent, the focus is only on the elaboration and analysis of the flow pattern in the forebay when the lateral angle is 45°.

Figures 6(a)–6(c) show the axial velocity flow field of the surface layer, middle layer, and bottom layer in the scheme with a lateral 45° bending angle. When water flows from the...
Table 1: Calculation results of hydraulic loss under different grid numbers.

| Number of grids | 1760825 | 2463869 | 2951968 | 3579186 | 4396902 | 5490948 |
|-----------------|---------|---------|---------|---------|---------|---------|
| Total inlet pressure (Pa) | 101997 | 101996 | 101995 | 101995 | 101995 | 101994 |
| Total outlet pressure (Pa) | 101732 | 101734 | 101735 | 101736 | 101737 | 101736 |
| Hydraulic loss (m) | 0.02708 | 0.02677 | 0.02662 | 0.02652 | 0.02642 | 0.02633 |

Figure 3: Hydraulic loss under different grid numbers.

Figure 4: Schematic diagram of the position of each section. (a) Schematic diagram of vertical profile position. (b) Horizontal section position diagram.

Figure 5: 3D flow field diagram of the lateral 45° bending angle scheme.
forebay to the inlet passage, the flow velocity in the middle position of the forebay is relatively large and has a decreasing trend to both sides; most of the fluid can flow smoothly into the inlet passage, but at the left sidewall of the forebay, a backflow zone is evident, and the flow pattern of the reflux zone is extremely high. The reason for this finding is that the transverse velocity of the mainstream is large, and a small part of the fluid contacts the left sidewall, which forms a large range of backflow zone, thus forcing the inflow mainstream to deform and deflect. Comparing and analyzing the flow field maps of each horizontal section show that, during the process from the surface layer to bottom layer, the scope of the reflux area is gradually expanded, and the position of the reflux center is approximately the same. According to the coordinate diagram, the center of the surface layer and middle layer reflux area that is located at $X = 2$ m, $Y = 11$ m, the bottom layer reflux area center that is located at $X = 3$ m, and $Y = 11$ m. The influent condition of 1# inlet passage is affected by the backflow zone that occurs before the 1# inlet passage.

Figure 7 is a 2-2 plane velocity vector diagram with a 45° bending in the lateral direction. The profile position is $X_2 = 0.5$ m, close to the inlet of the flow passage. The water flow in the forebay has a certain angle of deviation to the left due to the influence of the lateral water inflow. The water flow in the forebay near the inlet of 1# inlet passage is the most skewed, and the flow is turbulent. Figure 8 is a 1-1 plane velocity cloud diagram with a 45° bending in the lateral direction. The position of the profile is $X_1 = 0.01$ m. The inlet flow patterns of 2# and 3# inlet passages are better, the velocity distribution is relatively uniform, and the overall distribution is symmetrical. However, the water flow at the inlet of the 1# passage is severely skewed due to the influence of the backflow in front of the passage. The high-speed area occurs on the left side,
and the flow velocity distribution is extremely uneven. The flow velocity distribution uniformities of the inlet section of 1#, 2#, and 3# passages are 83.46%, 91.23%, and 91.01%, respectively. The weighted average angles of the inlet section of 1#, 2#, and 3# passages are 69.02°, 71.26°, and 70.38°, respectively.

3.4. Numerical Simulation Results of the Lateral 60° Bending Angle Scheme. The position of the characteristic section selected in the plan for a 60° bending angle is the same as that for a 45° bending angle. Seven characteristic sections are selected for the analysis of the results. The coordinates of the surface layer, middle layer, and bottom layer are \( Z_a = 1.85 \text{ m} \), \( Z_b = 0.95 \text{ m} \), and \( Z_c = 0.05 \text{ m} \), respectively; the coordinates of the section perpendicular to the mainstream direction are \( X_1 = 0.01 \text{ m} \) and \( X_2 = -0.5 \text{ m} \), respectively. The selected 1-1 section is the three inlet sections of the inlet flow passage to analyze the uniformity and weighted average angle of the axial velocity distribution on the section.

Figure 9 shows that the water flow in the diversion canal is good, but a large-scale backflow zone is observed before the 1# inlet passage near the left sidewall after entering the forebay. The flow pattern in the recirculation zone is turbulent, and the main flow of the inlet water in front of the 1# inlet passage is seriously deviated. The comparative analysis shows that the flow pattern of the water flow at a lateral angle of 60° is the same as that at a lateral angle of 45°, except that the recirculation zone in front of the 1# inlet passage is larger. Therefore, considering that the water flow in the diversion passage is relatively smooth and the water flow in the forebay is more turbulent, the following only focuses on the elaboration and analysis of the flow pattern in the forebay when the lateral angle is 60°.

Figure 10 shows the axial velocity flow field diagram of each horizontal section when the lateral angle is 60°. Most of the water can flow smoothly into the inlet passage, but a clear backflow zone can be seen on the left sidewall of the forebay. The flow pattern in the return zone is extremely turbulent, and the reason is the same as when the lateral direction is 45° because the mainstream lateral velocity at this place is relatively large, and a small part of the water flow contacts the left sidewall to form a larger return zone, thereby forcing the main flow of water to deform and deflect. Comparing and analyzing the flow field diagrams of the surface layer, middle layer, and bottom layer show that, from the surface layer to the bottom layer, the scope and position of the recirculation zone are the same, but the center of the recirculation zone moves to the right and forward. According to the coordinate map, the center of the surface and middle recirculation zone is approximately located at \( X = -5 \text{ m} \) and \( Y = 11 \text{ m} \). The bottom recirculation zone center is at \( X = -4 \text{ m} \) and \( Y = 9 \text{ m} \). The flow velocity in the mainstream zone is always greater than that in the recirculation zone.
Figure 10: Velocity cloud diagram of the flow field in each horizontal section at a 60° lateral angle. (a) Surface velocity flow field diagram. (b) Midlevel velocity flow field diagram. (c) Bottom velocity flow field diagram.

Figure 11: Plane velocity vector diagram with a 60° lateral angle 2-2.

Figure 12: 1-1 planar velocity cloud diagram with a 60° bending angle in the lateral direction (unit: m/s). (a) 3# passage. (b) 2# passage. (c) 1# passage 4.
Figure 11 is a 2-2 plane velocity vector diagram. The profile position is $X_2 = -0.5$ m, near the entrance of the flow passage, and the water in the forebay has an angular deflection to the left due to the influence of the lateral water inflow. The water flow in the forebay near the inlet of 1# inlet passage is the most skewed, and the flow is turbulent.

Figure 12 is a 1-1 plane velocity cloud diagram. The section location is $X_1 = 0.01$ m. The inlet flow patterns of 2# and 3# inlet passages are better, the velocity distribution is relatively uniform, and the overall distribution is symmetrical. However, the water flow at the inlet of the 1# passage is severely skewed due to the influence of the backflow in front of the passage. The high-speed area occurs on the left side, and the velocity distribution is extremely uneven. The uniformities of the flow velocity distribution of 1#, 2#, and 3# passages are 78.05%, 90.78%, and 91.38%, respectively. The weighted average angles of the inlet sections of 1#, 2#, and 3# passages are $71.37^\circ$, $70.41^\circ$, and $70.41^\circ$, respectively.

In summary, the bottom water flow backflow area is the largest for the forebay with $45^\circ$ and $60^\circ$ lateral angles due to the large lateral velocity of the mainstream at this location, and the large-scale recirculation it forms compresses the streamlines of the mainstream area outward. The recirculation area occurs before the 1# inlet passage. According to the location where the recirculation zone occurs, the water inlet conditions of the 1# inlet flow passage are affected, which may endanger the safety of the pump.

4. Conclusion

Numerical simulations, including model establishment, setting of boundary conditions, and grid independence analysis, are carried out on the design schemes of the forebay of the inlet pumping station at $45^\circ$ and $60^\circ$ lateral angles. The turbulence model used is the standard k-ε model. Through comparative analysis of the numerical simulation results, the following conclusions are drawn:

1. For the side-inlet pump station, the flow pattern of the water in the front tank is poor during operation, a large-scale return zone is observed, and the flow velocity distribution at the inlet of the 1# passage is extremely uneven.

2. Comparing the numerical simulation results of the $45^\circ$ lateral bending angle and the lateral $60^\circ$ bending angle reveals that the larger the lateral bending angle of the forebay is, the worse the flow pattern of the water flow, and the more unfavorable the pump operation.

3. Effective engineering measures must be taken to improve the flow pattern in the forebay of the pumping station and ensure the efficient operation of the pumping station.

Data Availability

The curve data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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