Spectrum Sensing for Cognitive Radio Based on Feature Extraction and Deep Learning

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Abstract. In cognitive radio, spectrum sensing is used to determine whether the primary user is using the spectrum based on the signal received on a specific frequency band, thereby determining whether the secondary user can use the spectrum. The main problem faced by spectrum sensing is how to identify the existence of the primary signal under the condition of low signal-to-noise ratio (SNR). Compared with traditional technologies, deep learning methods can identify the features of input data more efficiently and accurately. Based on convolutional neural network (CNN), this paper regard spectrum sensing as a binary classification problem. In the method we proposed, different features of received are extracted, and a dataset of feature matrices obtained under different SNRs is constructed for the training of the CNN network. Experiment results show that under the condition of low signal-to-noise ratio, the performance of our method is improved compared with the traditional method, and the combination of different features can improve the sensing accuracy.

1 Introduction

For the past few years, the increasing demand for higher data rates requires more spectrum resources. However, with the rapid development of wireless communication technology such as 5G, the spectrum resources become rarer and rarer [1]. To further improve spectrum utilization, cognitive radio technology has been proposed [2]. It is a method that can let secondary users (SU) reuse the spectrum in an unlicensed way while licensed primary users (PU) are inactive. Thus, unused spectrum resources can be utilized. For this purpose, SUs needs to frequently detect the state of the spectrum occupation of the PUs and feedback the result of spectrum sensing. To avoid interference, SUs has to identify the existence of the primary signal under the condition of a low signal-to-noise ratio (SNR) to know whether it is available or not [3].

Tradition spectrum sensing methods use different signal features, including energy detection [4,5], pilot detection [6,7], cyclostationary detection [8,9], and so on. The problem is that these methods can’t achieve good performance when the SNR is relatively low. Compared with traditional methods, deep learning and CNN has more powerful capabilities in extracting spatial features of the input. With the
convolutional layer, CNN can extract deeper features of the input and achieve higher recognition accuracy. Many deep learning methods have been used for spectrum sensing. In [10], the authors used received signal sequence as the input of the CNN and determine whether the received signal contains primary signal. The problem was that the method didn’t extract signal features, and the signal sequences will be hard to recognized when the SNR is low. In [11], the authors used power spectrum of the received signal as the input of the CNN, while the power of signal will be severely affected when the SNR is low. In [12], the authors used both energy and cyclostationary feature as the input of the CNN. The problem of this method was that cyclostationary features can be represented more comprehensively.

A spectrum sensing method based on feature extraction and CNN is proposed in this paper. In the work, a received signal sequence is represented by energy, power spectrum and cyclostationary feature. When a SU sense the spectrum, it samples the received signal and extract the three features. Then, the three features are combined and a feature matrix is built. The matrix is fed in the CNN. By the convolution operation, the three features can be calculated simultaneously, and the signal can be analyzed more comprehensively.

The rest of the paper is organized as follows. In Section II, how to extract different signal features and build feature matrix is introduced. In Section III, a CNN network is constructed and models are trained, then the result is analyzed. In section IV, whether the combination of three features is better than signal feature for spectrum sensing based on CNN is tested. Finally, the conclusion is made in Section V.

2 Feature Extraction
Spectrum sensing can be considered as a binary classification problem:

\[
\begin{align*}
H_0 &= n(t) \\
H_1 &= s(t) + n(t)
\end{align*}
\]

where \( T \) represents sampling time. \( H_0 \) represents received signal only contains noise \( n(t) \), and \( H_1 \) represents received signal contains primary signal \( s(t) \). Primary signals are always bandpass modulated signals, including ASK, PSK, and so on. In our method, SUs will sample the received signal and extract the energy feature, power spectrum feature and cyclostationary feature respectively. To combine the three features, we use two \( 64 \times 1 \) vector to present energy feature and power spectrum feature, one \( 64 \times 2 \) matrix is used to represent cyclostationary feature. Finally, the three features are combined to construct a \( 64 \times 4 \) feature matrix to present a received signal sequence. The steps to build the matrix are as follows.

2.1 Energy feature
To extract the energy feature of the received signal sequence, the signal sequence is evenly divided into 64 segments, and the average energy of each segment is calculated. The test statistic for energy feature extractor is expressed by:

\[
T(y) = \frac{1}{N} \sum_{n=1}^{N} |y(n)|^2
\]

where, \( y(n) \) is the signal samples and \( N \) is the number of signal samples in one segment. Then the energy feature vector can be expressed as \( T_{\text{energy}} = (T_1, T_2, ..., T_{64})^T \). In the work, the vector is used to express the energy feature of a received signal sequence.

2.2 Power spectrum feature
Signal power is another characteristic of the signal, and the power spectral density can reflect the power distribution of the signal. Assume that the finite-length received signal sequence is \( x(n) \), the estimation of power spectral density can be expressed by:

\[
S_x(k) = \frac{1}{N} |X(k)|^2 = \frac{1}{N} |\text{FFT}[x(n)]|^2, \quad k = 0,1, ..., N - 1
\]
where, $\text{FFT}[x(n)]$ is the Fourier transform of the received signal sequence $x(n)$. Since the period of $\text{FFT}[x(n)]$ is $N$, the calculated power spectrum estimate takes $N$ as the period. By using the Welch power spectrum density estimator in MATLAB, the power spectrum of a signal samples sequence can be obtained. One of the results is shown in Figure 1.

![Welch Power Spectral Density Estimate](image)

**Figure 1.** The result of Welch power spectrum density estimator of two received signal sequences. Left is the power spectrum density of the signal sequence which contains primary signal and SNR is 0. Right is the power spectrum density of the signal sequence which only contains noise.

Then, the spectrum is sampled for 64 times and another $64 \times 1$ power spectrum feature vector $P_{\text{power}} = (P_1, P_2, ..., P_{64})^T$ is obtained.

### 2.3 Cyclostationary feature

Modulated signals have periodic autocorrelation. The autocorrelation function is expressed by:

$$R_x(t, \tau) = E\{x(t)x(t - \tau)\}$$

(4)

where, $\tau$ is a constant lag. Autocorrelation function is periodic in time $t$ only for $T_0$. It can be expressed by:

$$R_x(t, \tau) = R_x(t + T_0, \tau)$$

(5)

Then, the Fourier transform of autocorrelation function can be expressed by:

$$R_x(\alpha, \tau) = F(R_x(t, \tau))$$

(6)

where, $\alpha$ is cyclic frequency. Then the spectral domain transform can be calculated through 2-D transform in frequency and cyclic frequency:

$$S_x(\alpha, f) = F(R_x(\alpha, \tau))$$

(7)

Cyclostationary feature of a signal sequence can be get through the communication toolbox in MATLAB. One of the cyclostationary feature of the signal samples sequence is shown in Figure 2.
Figure 2. The cyclostationary feature in spectral domain of two received signal sequences. Left is the cyclostationary feature of the signal sequence which contains primary signal and the SNR is 0. Right is the cyclostationary feature of the signal sequence which only contains noise.

It can be found that the feature values are mainly focused on the straight line corresponding to $\alpha = 0$ and $f = 0$. To express the cyclostationary feature, the $\alpha$ and $f$ are set as 0 respectively, then the spectral correlation is sampled for 64 times and two $64 \times 1$ cyclostationary feature vectors $CS_\alpha$ and $CS_f$ is obtained. Finally, through feature extraction, the $64 \times 4$ feature matrix of a received signal sequence is obtained. The format of the matrix is expressed in Table 1. As shown in Table 1, the first column is the energy feature vector, the secondary column is the power spectrum vector, the third and fourth column is the cyclostationary feature vectors.

Table 1. The format of the feature matrix of a received signal sequence.

| Samples | $T_{\text{energy}}$ | $P_{\text{power}}$ | $CS_\alpha$ | $CS_f$ |
|---------|---------------------|---------------------|-------------|--------|
| 1       | $T_1$               | $P_1$               | $CS_{\alpha 1}$ | $CS_{f1}$ |
| 2       | $T_2$               | $P_2$               | $CS_{\alpha 2}$ | $CS_{f2}$ |
| ...     | ...                 | ...                 | ...         | ...    |
| 64      | $T_{64}$            | $P_{64}$            | $CS_{\alpha 64}$ | $CS_{f64}$ |

3 Deep Learning Based System Model
In cognitive radio system, a SU determines whether the spectrum is idle or busy depending on the received signal, then decides whether it can reuse the spectrum. The system structure proposed in this paper can is shown in Figure 3.

Figure 3. The structure of feature extraction an CNN based spectrum sensing system
To sense the spectrum, the SU samples the received signal. Then the signal samples sequence is fed in the feature extractor to generate the feature matrix corresponding to the signal sequence. Then the matrix is fed in CNN model. The CNN model will do binary classification to decide whether the received signal contains primary signal or not.

3.1 CNN network architecture

CNN has achieved good results in areas such as image classification tasks [13]. In our method, we also consider spectrum sensing as a binary classification task. To evaluate whether the feature matrix can be used to train CNN model and do spectrum sensing, a CNN network is constructed in the work and models are trained, then the performance is evaluated. The CNN network can be termed as “SenseNet”, and the structure of the network is shown in Figure 4.

![Image: The structure of the “SenseNet”](image)

**Figure 4.** The structure of the “SenseNet”.

As shown in Figure 4, The format of the input layer is equal to the format of the $64 \times 4$ feature matrix formed by the extracted signal features. The two convolution layer uses four $2 \times 2$ convolution kernels and Zero-padding is 1, stride is set as 1 an 2, correspondingly. 8 different feature maps are obtained in the end of two convolution layers. The operations of the convolution layer can be expressed by:

$$X(l) = f(W(l) \odot X(l - 1) + b(l))$$

where, $X(l)$ is the output of the $l$ convolutional layer. $W(l)$ is the weight of the $l$ convolutional layer. $b(l)$ is the bias of the $l$ layer. $\odot$ is convolution operation, and $f$ is activate function. In the method, Sigmoid is used as activate function. Sigmoid function can be expressed by:

$$Sigmoid(x) = \frac{1}{1 + e^{-x}}$$

The sigmoid function image is an S-shaped curve with a value range between (0,1), as shown in Figure 5. Sigmoid function can increase the nonlinearity of the network and map an input to the interval of (0,1).
Pooling layer can remove unimportant data and further reduce parameter need to be trained. Max pooling layer is added after the convolutional layer, the kernel size is 2 and the stride is 1. Finally, four 2×32 feature maps are obtained after two convolutional later and two pooling layer.

Four fully connection layers are added in the end of the CNN. Fully connection uses Softmax as activate function. Each neuron in each layer of the fully connection layer is fully connected with all neurons in the previous layer, and the data features extracted by the convolution are analyzed and integrated, and the final prediction classification evaluation result is output. Finally, two outputs are set. The two outputs correspond to $H_0$ and $H_1$.

3.2 Dataset generation
To generate a dataset to train the network, In MATLAB, two kinds of bandpass modulated signals QPSK and 8PSK are simulated, the carrier frequency is 10kHz. The pulse shaping filter used is raised cosine filter with roll-off factor of 0.5. The signal passes through a multi-path Rayleigh fading channel, path delays vector is [0s, 0.001s]. The noise is assumed to be Gaussian white noise. It is set that the signal passes through AWGN channel, the SNR changes from -20 to 5.

In the method, it is assumed that SU samples the signal for 1280 times. After passing through the Rayleigh channel and AWGN channel, the received signal is sampled 1280 times, and the sample sequence is fed in feature extractor to generate feature matrices. The train dataset contains two type “signal 0” and “signal 1”. The “signal 0” only contains the feature matrixes corresponding to noise samples, and the “signal 1” contains the feature matrixes corresponding to the signals including primary signal and noise. Every signal type contains more than 5000 data. To evaluate the performance of the model under different SNRs, the test dataset that contains two types of data under different SNRs is generated, and every dataset corresponding to one SNR contains more than 1000 data.

3.3 Experiment results
The model is trained on the train dataset, and the trained model is tested on the test dataset. Based on PyTorch library, the training process can be expressed in Figure. 6.

Figure 5. Sigmoid activation function.
The process of model training. Dataset and DataLoader class provided in PyTorch is used to load data. The network is set to be trained for 50 epochs, and the model with best sense accuracy is saved. Then, the test dataset is used to evaluate the performance of the spectrum sensing model. The performance of spectrum sensing is evaluated through two parameters probability of detection ($P_d$) and probability of false alarm ($P_f$), which can be expressed as:

$$P_d = P(\text{decide } H_1|H_1) \quad P_f = P(\text{decide } H_0|H_0)$$

(10)

To evaluate the performance of the model by the two parameters, for QPSK and 8PSK signal sequences, $P_d$ and $P_f$ are calculated under different SNRs. The results are shown in Figure. 7.
As shown in Figure 7, with the increase of SNR, $P_d$ increases and $P_f$ decreases. When the SNR is larger than -10, $P_d$ will exceed 80% and $P_f$ will be less than 10%. Compared with traditional spectrum sensing method [4-9], this method has better performance when the SNR is relatively low. Through the experiment results, it can be found that for both signal types, when the SNR is small (< -14), the performance of the model is relatively bad. The probability of detection is not high enough while the probability of false alarm is not low. While if SNR is large enough (> -10), the performance is good. The probability of detection is high (>80) and the probability of false alarm is almost 0. The results verifies that the feature extraction can be used for spectrum sensing based on deep learning.

4 Feature Types Comparison

To further evaluate whether the combination of different feature types can improve the sensing accuracy, the data containing only energy and power features and the data containing only cyclostationary feature to train the models is used to train model respectively. Every type of the two data is $64 \times 2$ matrix. The structure of the network is the same, while the input format is changed from $64 \times 4$ to $64 \times 2$.

4.1 Experiment results

Used the same method proposed in Section III, the test results for the two types of the data are obtained. The test results are shown in Figure. 6 and Figure 7.

Figure 8. The performance corresponding to different data types for QPSK signal. Where, E & P refers to energy feature with power feature, CS refers to cyclostationary feature.
4.2 Result discussion
As shown in Figure 8 and Figure 9, through the experiment results, it can be found that use the combination of the three feature types to build the data and train model can achieve better sense accuracy. The results show that when the SNR is lower than -6dB, the model that trained on the energy and power feature can’t achieve good performance, that is while the $P_d$ is high, the $P_f$ is also high. It means that the model can’t recognize the signal type accurately, each type is likely to be recognized as another type.

Compared with energy and power features, when cyclostationary feature is used to do spectrum sensing, the $P_f$ is relatively low. However, the $P_d$ is not high enough when the SNR is lower than 0dB. It can be found that by combining all the kinds of features, the CNN model can make tradeoff between different features, which means the model can reduce $P_f$ and improve $P_d$ to a certain extent. The results verify that by combining several types of features, CNN model can learn received signal sequence more comprehensively and make more accurate decision.

5 Conclusion
In this paper, for spectrum sensing, a method based on feature extraction and deep learning is proposed. In the work, a novel feature extractor is proposed and the feature matrix extracted is used to train network. Finally, the model trained can be used to do spectrum sensing. The experiment results show that the method can achieve better performance than traditional spectrum sensing methods. To further test whether the method combining more types of signal features can improve sense performance, different data types corresponding to different combinations of features is generated and different models are trained. The experiment results verifies that the performance of the method that combines different features is better than that only use one or two kinds of feature. Based on the method, more kinds of signal features and advanced CNN structure can be explored to improve the performance of spectrum sensing models.

6 References
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