Detection of the TiO\(_2\) Concentration in the Protective Coatings for the Cultural Heritage by Means of Hyperspectral Data

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Abstract: Nanotechnology-based materials are currently being tested in the protection of cultural heritage: ethyl silicate or silica nanoparticles dispersed in aqueous colloidal suspensions mixed with titanium dioxide are used as a coating for stone materials. These coatings can play a key role against the degradation of stone materials, due to the deposit of organic matter and other contaminants on the substrate, a phenomenon that produces a greater risk for the monuments in urban areas because of the increasing atmospheric pollution. However, during the application phase, it is important to evaluate the amount of titanium dioxide in the coatings on the substrate, as it can produce a coverage effect on the asset. In this work, we present the hyperspectral data obtained through a field spectroradiometer on samples of different stone materials, which have been prepared in laboratory with an increasing weight percentage of titanium dioxide from 0 to 8 wt%. The data showed spectral signatures dependent on the content of titanium dioxide in the wavelength range 350–400 nm. Afterwards, blind tests were performed on other samples in order to evaluate the reliability of these measurements in detecting the unknown weight percentage of titanium dioxide. Moreover, an investigation was also performed on a test application of nanoparticle coatings on a stone statue located in a coastal town in Calabria (southern Italy). The results showed that the surveys can be useful for verifying the phase of application of the coating on cultural heritage structures; however, they could also be used to check the state of the coated stone directly exposed over time to atmospheric, biological and chemical agents.

Keywords: protective coatings; nanoparticle films; titanium dioxide; stone surface conservation; spectroradiometric data; hyperspectral signatures; cultural heritage protection

1. Introduction

Preserving memories means taking care of our past in looking to our future. Conserving the identity, in its huge variety, of our world cultural heritage will ensure solid roots are maintained for future generations. Cultural heritage encompasses a vast area and includes different types of historical and artistic goods, tangibles and intangibles. Each one of these requires a particular preservation procedure, often customized in relation to the environment with a holistic view (e.g., [1]).

There are many components of the urban landscapes which are often subjected to negative effects due to interaction with the surrounding environment. In these landscapes, historical buildings and monuments, often built in natural and artificial stone materials, are among the more exposed elements [2–4]. In fact, pollution and high concentrations of fine particulates, typical of the urban environment, play a role in accelerator the deterioration
process of outdoor surfaces (such as the façades of buildings, architectural elements and sculptures). A challenging issue for conservation is to face the deterioration of stone materials used in the artistic/architectural field (lime-based murals, limestone [5]).

The main causes of decay can be attributed to air pollution, soluble salts and biodeterioration; much research is available in the literature concerning the investigation of their mechanisms of action [6–13]. Identification of the basic principles for a correct conservation treatment is fundamental in defining appropriate actions and for the selection of materials and procedures, also taking into account the intrinsic stone properties, the degradation mechanisms and the environmental factors.

In this framework, the consolidation and protection of cultural heritage can count on innovative materials provided by nanotechnologies: consolidating products and/or protective treatments are improved by being implemented together with nanoproducts with self-cleaning and biocidal characteristics, such as titanium dioxide (TiO$_2$). These treatments are already a common practice in preservation of stone surfaces. The nanometric TiO$_2$ is considered a promising photocatalytic material because it has showed ability to catalyze the complete degradation of many organic contaminants and environmental pollutants, leading to a self-cleaning and antimicrobial effect [5,14–16].

As part of a broader contribution to the analysis of the photocatalytic properties of titanium dioxide (TiO$_2$) through a multi-analytical approach, and also considering that this nanoproduct can represent an environmental friendly alternative in the disinfection of stone surfaces, the article presents a procedure to support the control of TiO$_2$ concentration in the coatings by field spectroradiometric surveys. In Section 2 the preparation of the samples and spectroradiometric survey method are illustrated. The main results and their interpretation are discussed in Section 3. A recap of the work and some concluding remarks are reported in Section 4.

2. Materials and Methods

In the literature there are several researches aimed at the characterization of TiO$_2$-based coatings applied on different support stone materials (e.g., [14,17–20]); in particular, they analyze the biocidal and photodegradation efficiency, the color variations and hydrophobic properties, the distribution of TiO$_2$ in depth, the acid resistance and the morphological characterization. In addition, other tests were performed to study the long-term behavior of the coating subjected to artificial ageing [21]. In this work, we present a method to analyze the state of the coating through quick and contactless measurements performed directly on the application stone, so as to permit the inspection of different parts of the same object and/or on widespread cultural heritage assets. In particular, in a first phase the correlations were obtained by analyzing the percentage concentrations by weight of TiO$_2$ in the coatings, as they were provided by the production laboratory, and the hyperspectral data obtained once the same coatings were applied on stone samples. Subsequently, these correlations were used to evaluate the correspondence between the findings by the field measurements and the laboratory information on applications of coatings with an unknown TiO$_2$ concentration.

2.1. Sample Preparation in Laboratory

Marble and travertine samples were treated with formulations containing Nano Estel®, TEOS (tetraethyl orthosilicate) [23,24] and Aeroxide® TiO$_2$ P25 titanium dioxide [25].

Nano Estel is a colloid formulation wherein the particles of SiO$_2$ are dispersed in a water-based solution. The dispersed nanoparticles have a diameter not greater than 20 nm. The particles connect to each other, after the evaporation of the water, to produce a silica gel with a consolidating effect, thanks to the bridges generated between the detached particles of the support material.

Aeroxide TiO$_2$ P25 consists of particles having mean diameter of approximately 21 nm with a high photoactivity. In the presented experiment, Nano Estel and TEOS were
diluted to 3% with deionized water and, after that, mixed with different weight percentage concentrations of TiO$_2$ (from 0 to 8 wt%). These coatings, with increasing concentrations of nanoproducts, were applied on marble (Figure 1) and travertine samples.

Figure 1. Laboratory marble samples with coatings blended with solutions of increased weight percentage concentration of titanium dioxide.

Once the coatings had been applied, after 30 days for drying, surface spectral measurements were performed on samples of marble or travertine covered by Nano Estel or TEOS, respectively. In particular, for each stone material and coating the hyperspectral signatures were acquired on 7 samples: 1 of untreated stone, 1 of stone with coating (Nano Estel or TEOS) without TiO$_2$, and 5 with coating blended with an increasing TiO$_2$ weight percentage (0.5, 1, 2, 4 and 8 wt%).

2.2. Spectroradiometric Surveys

Measurements of solar reflected radiance were carried out with FieldSpec pro portable spectroradiometer (ASD Inc., Longmont, CO, USA) [26]. The instrumentation was equipped with three different spectrometers covering the 350–2500 nm spectral range: the first detector worked in the VNIR range (350–1000 nm), and the other two in the SWIR region (1001–1800 and 1801–2500 nm, respectively). These sensors are characterized by spectral resolution of 3 nm at 700 nm and 10 nm at 1400–2100 nm; spectral sampling of 1.4 and 1.1 nm in the ranges 350–1000 nm and 1001–2500 nm, respectively; and wavelength accuracy 0.5 nm. All details about the technical specifications of the instrumentation are available in [26].

The surveys were performed directly using bare fiber optic cable linked to the instrument and mounted on the pistol (i.e., without the use of specific lenses); a field of view of 25° corresponds to this configuration. The fore optic was pointed toward the target in opposite direction to the incidence of the solar rays to form an angle of about 90°, trying to keep constant the distance between the fore optic and the objects. Moreover, the distance between fiber fore optic and target was kept constant as much as possible. For each measurement, 25 spectral signatures were collected and the mean values were calculated, directly, by the acquisition software. Furthermore, for each sample 10 measurement points were performed in order to take into account variability of the local conditions due to the coating application and the base stone.

3. Results and Discussion

As already shown by Costanzo et al. [27], for marble coated with Nano Estel, we found appreciable differences among the reflectance values in the ultraviolet range (350–
400 nm) of the electromagnetic spectrum as a function of the amount of Aeroxide TiO\textsubscript{2} P25 in the coating, these changes were common to all the analyzed combinations between the stone base materials and the type of TiO\textsubscript{2} coatings (cf. Figures 2–5). This behavior is strongly linked to the weight percentage of titanium dioxide added in the coating; in fact, by analyzing the spectral signature of the titanium dioxide provided in the ASTER spectral library [28] and graphically represented in Figure 6, it can be noted there was a high slope in the wavelength range between 350 and 400 nm, with a strong decrease of the reflectance moving towards the ultraviolet range.

The comparison between the spectral signatures of the laboratory samples shows some differences between the untreated material and the stone coated with the materials prepared without TiO\textsubscript{2}; however, the differences become even more appreciable with the increase of TiO\textsubscript{2} up to 4 wt%. Instead, beyond this last value, the spectral shapes seemed more similar although much larger amounts of TiO\textsubscript{2} were blended into the coating.

To obtain a representative pattern as a function of the TiO\textsubscript{2} variation, the spectral signatures in the bands between 350 and 400 nm were compared with that obtained for the untreated stone through the spectral angle mapper (SAM) technique [29]. In fact, this technique allows calculation of the coefficient $SA$, representing the angular difference (in radians) between a given spectrum and the reference one, through the follow equation:

$$SA = \cos^{-1}\left(\frac{\sum_{i=1}^{nb} t_i r_i}{\sqrt{\sum_{i=1}^{nb} t_i^2} \sqrt{\sum_{i=1}^{nb} r_i^2}}\right)$$

Here, $nb$ is the number of the spectral bands; $t_i$ and $r_i$ are the reflectance values for the spectral band $i$ in the spectrum to be analyzed and the reference one, respectively. The pair of spectra is treated as a vector in $nb$-space, allowing us to calculate similarity between them. The zero value of the $SA$ coefficient represents the maximum similarity (i.e., spectral shapes are identical), while the increasing values define a decreasing similarity.

It is worth noting that higher $SA$ values are expected for larger concentrations of TiO\textsubscript{2}, because of the increasing differences in the ultraviolet range between spectral shapes (see Figures 2–5) compared to untreated material.

The similarities have been calculated in terms of $SA$ for each material and each coating (Figure 7). The graphs in the figure show the trends as a function of the TiO\textsubscript{2} weight: the values increase significantly up to 4 wt%; the difference, on the other hand, is practically negligible when comparing those with 4 and 8 wt%. Therefore, the correlations are able to indicate the amount of TiO\textsubscript{2} when it is less than 4 wt%, while they do not allow discrimination of larger quantities with reliability.

Moreover, the $SA$ values obtained for the different stone materials with the same coating appear comparable; therefore, only a relationship was calculated for each coating material (cf. Figure 8). In addition, some blind tests were performed to evaluate the capability to detect the unknown weight percentage concentrations of TiO\textsubscript{2} wt%. In particular, the correlations were used to evaluate the weight percentage concentration of TiO\textsubscript{2} of 12 samples: 6 of marble (cf. green triangles in Figure 8) and 6 of travertine (cf. red triangles in Figure 8). The concentrations determined by means of spectroradiometric measurements, after the application of the coating materials by brushing on the stones, were compared to those of the coating production provided by the laboratory (Table 1): the differences seem almost always contained; in fact, the absolute values are equal to or less than 0.5. Only one of the tests showed a significant deviation. It is worth pointing out that the differences can be related not only to the error introduced by correlations, but also due to the actual concentration of TiO\textsubscript{2} in the coating placed on the stone following the application method.

The correlations were also used to evaluate the concentration of TiO\textsubscript{2} in the coatings applied as a test at the foot of the statue, called “Angelo Tutelare”, exhibited in a square of the coastal urban center of Reggio Calabria city (Calabria, Southern Italy) (cf. 3D reconstruction by terrestrial laser scanning in Figure 9). Petrographic survey indicates that...
the statue was made in Greek marble, probably with waste materials from the ruins of a
temple in the Magna Graecia city [30]. The spectral signatures were acquired before and
after applying Nano Estel and TEOS coatings on small parts of the basement near the two
feet (Figure 9).

Figure 2. Spectral signatures obtained by spectroradiometric survey of the surface of marble samples prepared in laboratory
with Nano Estel coatings blended with different weight percentage concentrations of titanium dioxide (TiO$_2$). In each graph,
the gray curves represent the spectral data for different measurement areas on the same sample, each of which is the average
calculated over 25 measurements on the same area during the acquisition phase, whereas the colored curve is the mean
spectral signature. The overlap of the different signatures (bottom right graph) shows the effect due to the increasing wt% of TiO$_2$. 
Figure 3. Spectral signatures obtained by spectroradiometric survey of the surface of marble samples prepared in laboratory with TEOS coatings blended with different weight percentage concentrations of titanium dioxide (TiO₂). In each graph, the gray curves represent the spectral data for different measurement areas on the same sample, each of which is the average calculated over 25 measurements on the same area during the acquisition phase, whereas the colored curve is the mean spectral signature. The overlap of the different signatures (bottom right graph) shows the effect due to the increasing wt% of TiO₂.
Figure 4. Spectral signatures obtained by spectroradiometric survey of the surface of travertine samples prepared in laboratory with Nano Estel coatings blended with different weight percentage concentrations of titanium dioxide (TiO$_2$). In each graph, the gray curves represent the spectral data for different measurement areas on the same sample, each of which is the average calculated over 25 measurements on the same area during the acquisition phase, whereas the colored curve is the mean spectral signature. The overlap of the different signatures (bottom right graph) shows the effect due to the increasing wt% of TiO$_2$. 
Figure 5. Spectral signatures obtained by spectroradiometric survey of the surface of travertine samples prepared in laboratory with TEOS coatings blended with different weight percentage concentrations of titanium dioxide (TiO$_2$). In each graph, the gray curves represent the spectral data for different measurement areas on the same sample, each of which is the average calculated over 25 measurements on the same area during the acquisition phase, whereas the colored curve is the mean spectral signature. The overlap of the different signatures (bottom right graph) shows the effect due to the increasing wt% of TiO$_2$. 
Figure 6. Spectral signature of the titanium dioxide (ASTER spectral library [28]).

Figure 7. Spectral angle coefficient calculated from the spectral shapes obtained for the different stone materials and coatings (cf. Figures 2–5), using the untreated stones as reference. The coefficients are a function of the amounts of TiO$_2$ in the coatings. SA values are reported for travertine and marble coated with Nano Estel or TEOS.
The correlations were used to evaluate the weight percentage concentration of TiO$_2$ of 12 samples: 6 of marble (cf. green triangles in Figure 8) and 6 of travertine (cf. red triangles in Figure 8). The concentrations determined by means of spectroradiometric measurements, after the application of the coating materials by brushing on the stones, were compared to those of the coating production provided by the laboratory (Table 1): the differences seem almost always contained; in fact, the absolute values are equal to or less than 0.5. Only one of the tests showed a significant deviation. It is worth pointing out that the differences can be related not only to the error introduced by correlations, but also due to the actual concentration of TiO$_2$ in the coating placed on the stone following the application method.

**Figure 8.** Correlations between spectral angle and TiO$_2$ wt% combining data for marble and travertine with the same coatings: Nano Estel (blue circles on upper graph) and TEOS (blue circles on lower graph). In addition, the data obtained on samples with unknown TiO$_2$ wt% are also reported on the curves in order to evaluate their values (red triangles for travertine and green triangles for marble).
Table 1. Differences between TiO\(_2\) weight percentage concentrations in the coatings obtained by spectroradiometric measures and laboratory.

| Stone       | Coating     | TiO\(_2\) wt% by Laboratory | TiO\(_2\) wt% by Hyperspectral Survey | Difference of TiO\(_2\) wt% |
|-------------|-------------|------------------------------|--------------------------------------|-----------------------------|
| 1 Travertine| Nano Estel  | 10                           | ≥4                                   | -                           |
| 2 Travertine| Nano Estel  | 2                            | 1.7                                  | 0.3                         |
| 3 Travertine| Nano Estel  | 4                            | 2.2                                  | 1.8                         |
| 4 Travertine| TEOS        | 10                           | ≥4                                   | -                           |
| 5 Travertine| TEOS        | 2                            | 1.8                                  | 0.2                         |
| 6 Travertine| TEOS        | 4                            | 3.7                                  | 0.3                         |
| 7 Marble    | Nano Estel  | 1.0                          | ≥4                                   | -                           |
| 8 Marble    | Nano Estel  | 0.5                          | 1.0                                  | −0.5                        |
| 9 Marble    | Nano Estel  | 2                            | 1.6                                  | 0.4                         |
| 10 Marble   | TEOS        | 1.0                          | ≥4                                   | -                           |
| 11 Marble   | TEOS        | 0.5                          | 0.9                                  | −0.4                        |
| 12 Marble   | TEOS        | 2                            | 1.8                                  | 0.2                         |

Figure 9. Applications of TiO\(_2\)-coatings Nano Estel and TEOS on small parts of the “Angelo Tutelare” statue located in the coastal urban environment of Reggio Calabria city. The 3D reconstruction of the statue was performed by terrestrial laser scanning. The graphs show the values of TiO\(_2\) wt% in the coatings obtained through the correlations of Figure 8.

By using the previous correlations, the TiO\(_2\) wt% was evaluated in the graphs in Figure 3. Values were obtained of 1.7 wt% for the Nano Estel and 3.2 wt% for TEOS, which are in line with those from the laboratory of 2 and 3 wt%, respectively. Equal values were obtained by the hyperspectral measurements carried out on the two applications performed for each coating.

4. Conclusions

Many structures of cultural heritage significance, especially those located in urban environments, are often exposed to negative effects due to high pollution and concentrations of fine particulate. In particular, the objects and elements in stone material suffer an
acceleration of the degradation processes because of these phenomena. However, coatings containing nanoproducts such as titanium dioxide (TiO$_2$), today represent a powerful tool to mitigate stone degradation in a sustainable way. The durability of such coatings is also related to the persistence of the nanoproduct on the surface itself. This work has dealt with the detection and the monitoring of the TiO$_2$ concentration blended into the protective coatings applied on stone materials. In particular, hyperspectral data were analyzed in order to identify an indicator of the amount of TiO$_2$. The measurements carried out by field spectroradiometric sensors allowed us to obtain reflectance values for different stones and coverage materials. In particular, data analysis was performed for coatings based on Nano Estel and TEOS with addition of different weight percentage concentrations of Aeroxide TiO$_2$ P25. The spectral signatures of the coated stone depending on the amount of titanium dioxide (TiO$_2$) blended into the coating, with the effect on the wavelength ranging between 350 and 400 nm. Nevertheless, the increasing amount of TiO$_2$ had gradually less effect; results were practically negligible for values greater than 4 wt%. The data analysis allowed us to calculate a relationship for each coating regardless of the base material. Afterwards, blind tests were performed on samples of marble or travertine covered with the two coatings; the tests seemed able to identify the weight percentage concentration of TiO$_2$ with a good reliability. Furthermore, tests were performed on some applications carried out on a statue placed in a coastal urban environment. Even in this case the correlations matched with good approximation those provided by the laboratory. Further surveys will be performed on coating applications to protect architectural elements and sculpture exposed to weather, biological and chemical agents, with the purpose being to evaluate the state of the coating over time.

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