INTRODUCTION

Predation and competition for resources represent two major factors determining the survival of species at low and intermediate trophic levels (Sih, Crowley, McPeek, Petranka, & Strohmeier, 1985). Hence, there is strong selection for increasing defense against predation and competitiveness. However, species optimizing one functional trait commonly have to pay costs regarding other traits due to physiological, energetic, and genetic constraints (Stearns, 1989). Trade-offs between defense and competitiveness have been frequently found...

Not attackable or not crackable—How pre- and post-attack defenses with different competition costs affect prey coexistence and population dynamics

Elias Ehrlich | Ursula Gaedke

Abstract

It is well-known that prey species often face trade-offs between defense against predation and competitiveness, enabling predator-mediated coexistence. However, we lack an understanding of how the large variety of different defense traits with different competition costs affects coexistence and population dynamics. Our study focusses on two general defense mechanisms, that is, pre-attack (e.g., camouflage) and post-attack defenses (e.g., weaponry) that act at different phases of the predator–prey interaction. We consider a food web model with one predator, two prey types and one resource. One prey type is undefended, while the other one is pre- or post-attack defended paying costs either by a higher half-saturation constant for resource uptake or a lower maximum growth rate. We show that post-attack defenses promote prey coexistence and stabilize the population dynamics more strongly than pre-attack defenses by interfering with the predator’s functional response: Because the predator spends time handling “noncrackable” prey, the undefended prey is indirectly facilitated. A high half-saturation constant as defense costs promotes coexistence more and stabilizes the dynamics less than a low maximum growth rate. The former imposes high costs at low resource concentrations but allows for temporally high growth rates at predator-induced resource peaks preventing the extinction of the defended prey. We evaluate the effects of the different defense mechanisms and costs on coexistence under different enrichment levels in order to vary the importance of bottom-up and top-down control of the prey community.

KEYWORDS

coexistence, competition–defense trade-off, defense against predation, functional response, indirect facilitation, predator–prey cycles
in nature and may explain the high diversity of strategies along the gradient of being defended or highly competitive (Agrawal, 1998; Coley, Bryan, & Chapin, 1985; Hillebrand, Worm, & Lotze, 2000). Predation may enable coexistence of competing species facing a trade-off between defense and competitiveness. This mechanism is known as keystone predation (Leibold, 1996; Menge, Berlow, Blanchette, Navarrete, & Yamada, 1994; Paine, 1966) or analogously as killing the winner in a microbial context (Thingstad, 2000; Winter, Bouvier, Weinbauer, & Thingstad, 2010): A competitive superior species is suppressed by predation promoting the inferior but defended competitor which allows them to coexist. Several studies highlighted the importance of this predator-mediated coexistence in experimental and natural communities (e.g., Ciro-Pérez, Carmona, Lapesa, & Serra, 2004; Fauth & Resetarits, 1991; McPeek, 1998).

Species evolved a variety of defense strategies to reduce their predation risk ranging from camouflage, apparent dead, mimicry, aposematism, warning calls, weaponry, chemical defense to escape behavior (Endler, 1991; Lima & Dill, 1990). These defense mechanisms interact in different ways with the predator. Some of them even hamper the predator, for example, chemical defenses, while others do not, for example, camouflage, which may have strong implications for the occurrence of predator-mediated coexistence. Furthermore, the type of defense costs regarding competitiveness (resource uptake affinity or growth rate) plays an important role for coexistence. Theory already showed that predator-mediated coexistence crucially depends on the environmental conditions (Chase et al., 2002), for example, the enrichment level (Genkai-Kato & Yamamura, 1999; Leibold, 1996; Proulx & Mazumder, 1998), the prey switching behavior of the predator (Abrams & Matsuda, 1993; Fryxell & Lundberg, 1994; Murdoch, 1969), the magnitude of the trade-off between defense and competitiveness (Abrams, 1999; Kasada, Yamanichi, & Yoshida, 2014; Tirok & Gaedke, 2010), and the difference in both the defense level and the competitiveness between the prey types (Becks, Ellner, Jones, & Hairston, 2010; Ehrlich, Becks, & Gaedke, 2017; Jones & Ellner, 2007). However, the role of different defense mechanisms and competition costs in prey communities remains unclear but holds promise to be decisive for their coexistence and the occurring population dynamics. Here, we want to evaluate explicitly the effects of different defense mechanisms and compare the influence of different defense costs in terms of competitiveness on prey coexistence and population dynamics.

Following Bateman, Vos, and Anholt (2014), we distinguish between two general types of defense mechanisms: pre-attack and post-attack defenses that act at different phases of the predation sequence, that is, prey encounter, detection, attack, capture, manipulation, consumption, and digestion. A pre-attack defense implies that the predator does not attack the prey, for example, because it senses the defense, the prey is camouflaged or avoids habitats where predators occur. A post-attack defense means that the prey is attacked but survives, for example, due to weaponry, escape behavior or robustness. In contrast to pre-attack defenses, the predator invests time and energy to handle prey with a post-attack defense which reduces its potential to consume another undefended prey (see Table 1). Hence, a post-attack defended prey interferes with the functional response of the predator for edible prey which may result in a lower top-down control of the total prey community, while pre-attack defended prey does not. Thus, we expect different coexistence patterns and population dynamics in dependence of the defense mechanism.

We also distinguish between two general cost types of the defense in respect to resource competition: either having a reduced performance at low resource concentrations or growing slower independent of the resource concentrations. Referring to the Monod equation (Monod, 1950), this corresponds either to a higher half-saturation constant for resource uptake or a lower maximum growth rate. There is empirical evidence from phytoplankton and plant communities that both cost types are ecologically relevant (Agrawal, 1998; Lind et al., 2013; Meyer, Ellner, Hairston, Jones, & Yoshida, 2006; Yoshida, Hairston, & Ellner, 2004). However, a comparison of how both cost types affect the prey community is still missing.

Previous studies on predator-mediated coexistence in diamond-shaped food web models often implicitly assumed pre-attack defenses (Abrams, 1999; Fryxell & Lundberg, 1994; Yamauchi & Yamamura, 2005) and considered either a higher half-saturation constant (Becks et al., 2010; Jones & Ellner, 2007; Yoshida, Jones, Ellner, Fussmann, & Hairston, 2003) or a lower maximum growth rate as costs (Abrams, 1999; Kasada et al., 2014; Yoshida et al., 2016).

### Table 1

Comparison of the predator’s handling time spent per prey individual and the resulting energy gain of the predator for an undefended prey (a) and for prey types with three different defense mechanisms (b–d). $T_a$ represents the time needed for attacking and capturing a prey individual and $T_m$ is the manipulation and digestion time spent after capturing the prey.

| Defense mechanism | Handling time | Energy gain | Examples |
|-------------------|---------------|-------------|----------|
| a) Undefended ($q_2 = 1, q_1 = 1$) | $T_a + T_m$ | Yes | - |
| b) Pre-attack defense ($p_1 = 0, q_1 = 1$) | 0 | No | Camouflage, mimicry, aposematism, apparent dead |
| c) Post-attack defense ($p_1 = 1, q_1 = 0$) | $T_a$ | No | Weaponry, escape behavior, robustness, autotomy |
| d) Digestion resistance (see Appendix S1) | $T_a + T_m$ | No | Algae with thickened cell walls or snails surviving gut passage in predators |
2007). In this study, we explicitly model pre-attack and post-attack defenses and both cost types. The modeled diamond-shaped food web involves a basal resource, two competing prey types with a trade-off between defense and competitiveness, and one predator species. One prey type is undefended, while the other type is defended either by a reduced probability of being attacked or a lower probability of being consumed when attacked. We consider defense as a continuous trait with values ranging from completely defended to nearly undefended. The costs for defense are either a higher half-saturation constant or a lower maximum growth rate. By varying the values of both traits of the defended prey independently, we generate different magnitudes of the trade-off quantifying the costs of being more or less defended. For each trait combination, we test for coexistence and check whether the populations cycle or are in steady state. This enables us to evaluate how the different traits promote maintenance of prey diversity and stabilize the dynamics. We analyze these effects under different enrichment levels (different resource concentrations) in order to vary the relative importance of bottom-up and top-down control.

2 | METHODS

We consider a diamond-shaped food web model with one predator (P), two prey types (Ai), and one resource (N) limiting the growth of the prey. The two prey types face a trade-off: Ai is defended but has costs in respect to resource competition while A2 is undefended and highly competitive. The following model description is divided into four parts. At first, we present the different defense mechanisms of Ai and derive the respective functional response of the predator. Second, we describe the different competition costs based on the resource-dependent growth function of the prey types. Third, we apply the model to a fully parametrized chemostat system, and finally, we explain how to analyze the effect of the different defense mechanisms and costs on prey coexistence and the population dynamics for the considered system.

2.1 | Defense mechanisms

The predator attacks the prey Ai with the probability pi and then consumes the captured prey with the probability qi. While A2 is completely undefended (q2 = 1), A1 is able to defend against predation at different phases of the predation sequence (Bateman et al., 2014). We distinguish between two general defense mechanisms: pre-attack defenses (p1 < 1) and post-attack defenses (q1 < 1). A third special defense mechanism where the prey is attacked and consumed (p1 = q1 = 1) but survives passing the digestive system of the predator is investigated in Appendix S1.

According to Brodie, Formanowicz, and Brodie (1991), we assume that the defended prey is specialized only on one defense mechanism, that is, if p1 < 1 then q1 = 1 and vice versa, as investing in one strategy reduces the fitness advantage of the other. The main difference between the defense mechanisms lies in how they affect the predator’s functional response. We consider a Holling type II functional response of the predator implying that it spends a certain handling time for each attacked prey individual before it is able to attack the next prey item. Thus, the rate of consumption of the predator saturates with increasing prey density. The handling time comprises the time for attacking and capturing the prey (Tc) and, if the prey is consumed, the time for manipulating and digesting it (Tm). The two prey type version of the Holling disk equation is then given by

$$F_i = \frac{ap_i q_i A_i}{1 + ap_i (T_c + q_i T_m) A_i + ap_2 (T_c + q_1 T_m) A_2}$$

where $a$ represents the encounter rate (Bateman et al., 2014; Holling, 1959; Ruffler, Van Dooren, & Metz, 2006). It should be mentioned here that the attack probability $p_i$ scales the encounter rate $a$ in the presented version of the type II functional response (Equation 1). Therefore, the product of $a$ and $p_i$ can be interpreted as the effective attack rate on Ai.

The key to understand the effects of the different defense mechanisms on the functional response of predator is the handling time spent per prey individual. A completely undefended prey individual demands the full handling time of the predator attacking and manipulating it, that is, $T_c + T_m$ (Table 1a). A pre-attack defended prey individual with $p_1 = 0$ is not attacked and thus demands no handling time of the predator (Table 1b) allowing the predator to focus on the undefended prey. In contrast, for a post-attack defended prey individual with $q_1 = 0$, the predator invests the attack time $T_c$ without making use out of it (Table 1c).

$$F_i = \frac{ap_i q_i A_i}{1 + ap_1 (c_j T + q_1 (1-c_j) T) A_i + ap_2 (c_j T + q_2 (1-c_j) T) A_2}$$

If $c_j$ has very low values, pre- and post-attack defenses do not differ substantially in their effect on the predator, while high values of $c_j$ imply high differences in handling times needed for a pre- and post-attack defended prey (see Equation 2 and Table 1).

2.2 | Defense costs with respect to competitiveness

An empirically well-established resource-dependent growth model is the Monod equation with the parameters maximum per capita growth rate $\beta$, and half-saturation constant $K_i$, that is, the resource concentration where the growth rate reaches half of the maximum (Monod, 1950). The Monod equation is equivalent to a Holling type II functional response but is not restricted to predator–prey
interactions and has been applied also to autotrophic organisms taking up nutrients (e.g., Becks et al., 2010; Raatz, Gaedke, & Wacker, 2017; Yoshida et al., 2003). The per capita growth rate of $A_i$ in dependence of $N$ is described by

$$G_i = \frac{N}{K_i + N}. \quad (3)$$

We distinguish here between two general types of defense costs of $A_i$ with respect to competitiveness: a reduced growth rate at low but not at high resource concentrations ($K_1 > K_2$) or a lower growth rate independent of the resource concentration ($\beta_1 < \beta_2$). Both cost traits ($K_i$ and $\beta_i$) are relevant in nature, and their implications can be understood based on two extreme cases. First, for very high resource concentrations ($N \gg K_i$), the per capita growth rate of $A_i$ reaches its maximum and is independent of the half-saturation constant ($G_i = \beta_i$, see Equation 3). Second, for very low resource concentrations ($N \ll K_i$), the per capita growth rate of $A_i$ is given by $G_i = (\beta_i/K_i)N$ (see Equation 3) and thus depends on both cost traits. According to that, $\beta_i/K_i$ can be interpreted as the slope of the growth function at very low $N$ which is defined as the resource affinity. In the absence of mortality, the prey type with the higher resource affinity would be competitive superior (Button, 1978; Healey, 1980; Smith, Merico, Wirtz, & Pahlow, 2014). However, given a certain rate of natural mortality $\delta$, the competitiveness depends on the equilibrium resource concentration $N_i^*$ at which the gross growth rate equals the mortality, that is, $G_i = \delta$ (Tilman, 1982). Following Equation 3, the equilibrium resource concentration of a prey type $A_i$ in monoculture is given by

$$N_i^* = \frac{K_i}{\delta - 1}. \quad (4)$$

The undefended prey $A_2$ has a lower equilibrium resource concentration than the defended prey $A_1$ ($N_2^* < N_1^*$) and thus outcompetes $A_1$ in the absence of predation. We use the ratio $N_2^*/N_1^*$ as a measure of relative competitiveness of $A_i$ which allows us to compare the effects of the different defense costs (higher $K_1$ or lower $\beta_i$) on competition. For costs arising from $K_1 > K_2$ ($\beta_1 = \beta_2$), $N_2^*/N_1^*$ equals $K_2/K_1$. For costs originating from $\beta_1 < \beta_2$ ($K_1 = K_2$), it is given by $(\beta_1 - \delta)/(\beta_2 - \delta)$ (see Equation 4).

### 2.3 | Chemostat model

Here, we put the diamond-shaped food web model with the previously derived functional responses and growth functions into an ecologically relevant context. We consider a chemostat system which is characterized by a continuous inflow of medium with resources and outflow of medium with resources and organisms (Smith

| Parameter/Variable | Value | Unit | References |
|--------------------|-------|------|------------|
| $N$                | –     | $\mu$mol N/L | –          |
| $A_i$              | –     | ind./mL | –          |
| $P$                | –     | –    |            |
| $N_i$              | 80, 160 or 240 | $\mu$mol N/L | TVC        |
| $\delta$           | 0.8   | per day | TVC        |
| $\chi$             | $2.7 \times 10^6$ | ind./$\mu$mol N | Lutz Becks, unpublished data |
| $\chi_P$           | $170 \times 10^{-6}$ | – | Becks et al. (2010) |
| $\alpha$           | 0.073 | mL/day | Calculated from Becks et al. (2010) |
| $T$                | $9.091 \times 10^{-3}$ | day | Calculated from Becks et al. (2010) |
| $c_s$              | 0.5   | –    | NM         |
| $\rho_i$           | $p_1$ varied, $p_2 = 1.0$ | – | Lutz Becks, unpublished data |
| $q_i$              | $q_1$ varied, $q_2 = 1.0$ | – | Lutz Becks, unpublished data |
| $K_i$              | $K_1$ varied, $K_2 = 2.2$ | $\mu$mol N/L | Lutz Becks, unpublished data |
| $\beta_i$          | $\beta_1$ varied, $\beta_2 = 1.6$ | per day | Noemi Woltermann, unpublished data |

TVC. Typical values used in chemostat experiments with rotifers and algae as they enable sufficient rotifer densities but avoid light limitation (e.g., Becks et al., 2010; Yoshida et al., 2003); NM, No measurements available. For simplicity, we assume that the fraction of $T$ spent for attacking and manipulating the prey is equal, that is, $c_s = 0.5$ (sensitivity analysis in Appendix S3).
\( \chi \) describes the conversion efficiency of resources into prey individuals. The parameter \( \delta \) which represents the mortality rate of the prey and the predator. The resource concentration in the supplied medium \( N_i \) determines the quantity of inflowing resources. An increase in \( N_i \) implies an enrichment of the system. The changes of the resource concentration and population densities over time are defined by the following differential equations

\[
\frac{dA_i}{dt} = \delta(N_i - A_i) - \frac{1}{\chi} G_i A_i - \frac{1}{\chi} G_i A_2
\]

\[
\frac{dP}{dt} = G_i A_i - \beta P - \delta A_i
\]

\[
\frac{dN_i}{dt} = \chi P F_i + \chi P F_2 - \delta P
\]

with \( i = 1, 2 \). The parameter \( \chi \) describes the prey’s conversion efficiency of resources into prey individuals. The parameter \( \chi P \) describes the efficiency with which consumed prey individuals are converted into predator individuals. To reach a suitable parametrization, we refer our model to an empirically well-studied rotifer-algae system with Brachionus calyciflorus as a predator and different genotypes of Chlamydomonas reinhardtii as prey (Becks, Ellner, Jones, & Hairston, 2012; Becks et al., 2010). For details on the values and units of the parameters and the state variables, see Table 2. For the given system, \( A_1 \) and \( A_2 \) represent different genotypes of the same algal species. However, mechanistically, there is no difference between analyzing coexistence of different species or genotypes of an asexually reproducing species without horizontal gene transfer.

2.4 | Analysis of coexistence and population dynamics

The traits of the undefended prey \( A_2 \) are fixed. By varying the defense level and the defense costs of \( A_1 \) independently, we generate different slopes of the trade-offs. In order to understand the individual effects of the different traits, we vary only the value of one defense trait and one cost trait at a time. The other trait values are equal to those of \( A_2 \). This results in different types of trade-offs (TO) which we consider: p-K-TO, q-K-TO, p-\( \beta \)-TO, and q-\( \beta \)-TO. First, we analyze how the different defense mechanisms (\( p_1 < p_2 \) or \( q_1 < q_2 \)) affect prey coexistence and the population dynamics, that is, whether cycles or steady state occur. Secondly, we compare the effect of different costs of defense (\( K_1 > K_2 \) or \( \beta_1 < \beta_2 \)) on these properties.

In order to find the coexistence regions in the trait space, we applied a numerical approach of Jones and Ellner (2007) which calculates the condition for a coexistence equilibrium where all net growth rates equal zero. A following linear stability analysis of these equilibria informs about the population dynamics. A steady-state occurs in case of a stable equilibrium. For an unstable equilibrium, coexistence with cycling population densities is possible. To check the basin of attraction of the respective attractor, that is, the range of possible initial conditions leading to it, we perform an invasion analysis. We check whether \( A_1 \) can invade a resident community with \( N, A_2 \) and \( P \) which reveals whether coexistence is also reached with very low population densities of \( A_1 \). For further details on the analysis, see Appendix S2 in Supporting Information. To investigate details of the population dynamics, we did numerical integrations for selected parameter combinations with the odeint solver of the SciPy package in Python (Jones, Oliphant, & Peterson, 2001). For all simulations shown in the main text, we use the same setting of initial population densities \( N = N_1, A_1 = A_2 = 10^5 \) ind./mL, \( P = 1 \) ind./mL and a simulation time of 60 days.

3 | RESULTS

3.1 | General patterns of prey coexistence and population dynamics

To explain the patterns of coexistence and population dynamics in general, we focus initially on the trade-off (TO) between attack probability \( p \), that is, pre-attack defense, and half-saturation constant \( K \) (p-K-TO) under three levels of resource supply, that is, \( N_i = 80, 160, 240 \) \( \mu \)mol N/L (a–c). The traits of the undefended prey \( A_2 \) are kept constant (green dot). The attack probability \( p_1 \) and the half-saturation constant \( K_1 \) of the defended prey \( A_1 \) which determines its relative competitiveness \( N_1^*/N_2^* \) (cf. Methods, Equation 4) are varied within the shown trait space. The capital letters display which prey types survive in the different parts of the trait space. The black lines enclose the part of the trait space where a coexistence equilibrium exists while blue dots mark where it is locally stable (steady state). The dashed orange line represents the invasion boundary above which \( A_1 \) can invade a resident community with \( A_2 \). The numbers indicate special cases which occur at intermediate and high enrichment levels (b, c): ① Only \( A_2 \) survives as the coexistence equilibrium is unstable and \( A_1 \) cannot invade, ② multistability between coexistence and survival of only \( A_2 \), ③ multistability between survival of \( A_1 \) and survival of \( A_2 \). The crosses mark trait combinations used in Figure 5.
constant $K$ (p-K-TO). We consider three different enrichment levels, that is, $N^*_1 = 80$, 160, and 240 $\mu$mol N/L, to reveal the sensitivity of these patterns to the productivity of the system (Figure 1a–c).

For a low resource supply ($N^*_1 = 80$ $\mu$mol N/L), the defended prey $A_1$ dies out and only the undefended prey $A_2$ survives if the relative competitiveness $N^*_2/N^*_1$ (cf. Methods, Equation 4) of $A_1$ is very low, that is, $A_1$ has a high half-saturation constant $K_1$ (Figure 1a). For higher values of $N^*_2/N^*_1$, $A_1$ and $A_2$ may coexist. The range of possible $N^*_2/N^*_1$ values enabling coexistence increases with a decreasing attack probability $p_1$ (Figure 1a). At low values of $p_1$, both prey types coexist for relatively low $N^*_2/N^*_1$ values and even for high $N^*_2/N^*_1$ values close to 1 (very low defense costs). The latter case implies a very high fitness of $A_1$ as it has favorable values for both traits. However, such a highly defended $A_1$ cannot outcompete $A_2$ as long as its competitiveness is lower than that of $A_2$ ($N^*_2/N^*_1 < 1$) because $A_1$ needs $A_2$ to maintain the predator $P$ and thus its advantage of being defended. In the absence of $P$, $A_1$ would be inferior compared to $A_2$ as long as its competitiveness is slightly lower than that of $A_2$. At high values of $p_1$, $A_1$ can maintain $P$ by itself for $N^*_2/N^*_1$ close to 1 and thus outcompetes $A_2$ (Figure 1a).

For low levels of resource supply ($N^*_1 = 80$ $\mu$mol N/L), both prey types coexist in a steady state; that is, the coexistence equilibrium is always stable (Figure 1a). Furthermore, the outcome of coexistence is independent of the initial conditions as the predator $P$ and thus its advantage of being defended. In the absence of $P$, $A_1$ would be inferior compared to $A_2$ as long as its competitiveness is slightly lower than that of $A_2$. At high values of $p_1$, $A_1$ can maintain $P$ by itself for $N^*_2/N^*_1$ close to 1 and thus outcompetes $A_2$ (Figure 1a).

3.2 | Comparison of different defense mechanisms

To demonstrate the effects of the different defense mechanisms on coexistence and population dynamics, we chose an intermediate resource supply ($N^*_1 = 160$ $\mu$mol N/L) where coexistence with population cycles occurs and the defended prey $A_1$ is able to outcompete the undefended prey $A_2$ for a significant part of the trait space (Figure 1b). The results for $N^*_1 = 80$ and 240 $\mu$mol N/L are given in Appendix S3 (Figures C1 and C2).

Comparing the different types of defense–competition trade-offs, we find qualitatively the same regions of coexistence in the trait space but with greatly differing importance (Figure 2a–d). A post-attack defense ($p_1 = 1$, $q_1 < 1$) promotes coexistence more strongly than a pre-attack defense ($p_1 < 1$, $q_1 = 1$) and stabilizes the dynamics. This observation is independent of the type of costs for the defense (Figure 2a–d). We elucidate the effects of the different defense mechanisms based on the comparison of the attack probability–half-saturation constant trade-off (p-K-TO, Figure 2a) and the consumption probability–half-saturation constant trade-off (q-K-TO, Figure 2c). The part of the trait space where the defended prey $A_1$ outcompetes the undefended prey $A_2$ is smaller for the q-K-TO while the coexistence region increases (Figure 2a,c). The region where $A_1$ goes extinct remains constant. The changes in the coexistence patterns can be explained with the different growth functions of the predator $P$ resulting from the different defense mechanisms. We consider two comparable levels of the different defenses ($p_1 = 0.45$ or $q_1 = 0.45$) having the same costs ($N^*_2/N^*_1 = 0.5$). The population dynamics clearly reveal that the growth rate of $P$ is higher for the p-K-TO compared to the q-K-TO although the amount of total available prey $(\Sigma\pi_A)$ is slightly lower during the predator growing phase (Figure 3a,b). The resulting higher biomass of $P$, that is, the higher top-down control, in case of the p-K-TO drives the undefended prey $A_2$ to extinction (Figure 3a).

More generally, the growth rates of $P$ are equal for the p-K-TO and the q-K-TO in the absence of $A_1$, but they diverge for the different types of defenses with an increasing density of the defended prey $A_1$ (Figure 3c). With higher shares of $A_1$, the predator is increasingly handling "noncrackable" prey for the q-K-TO which dampens its growth in comparison with the p-K-TO. At high densities of $A_2$, an increasing density of $A_1$ leads even to a reduction of growth in case of the q-K-TO, while there is a slight increase in growth for the p-K-TO (Figure 3c). When $A_2$ is absent, $P$ dies out in case of the q-K-TO because the gross growth rate of $P$ based on a post-attack defended $A_1$ lies below the mortality rate even for high densities of $A_1$ resulting in a negative net growth of $P$ (Figure 3c). Therefore, $A_1$ cannot outcompete $A_2$ as it needs $A_2$ to maintain the predator and thus its advantage in respect to defense. In addition, $A_2$ indirectly facilitates $A_1$ as it reduces the grazing loss of $A_2$ by keeping the predator handling "noncrackable" food items (Figure 3c). The described effects of the post-attack defense on predator growth result in the coexistence of both prey types for an extended trait space. These effects are absent in case of the pre-attack defense leading to the extinction of $A_2$. The lower growth rates of $P$ in case of the q-K-TO explain the more...
frequent occurrence of steady states (Figure 2c). Cycles require sufficient deflections of population densities, that is, high minima of prey densities, which are prevented due to the lower growth rates of $P$.

### 3.3 Comparison of different defense costs

We now compare the effects of different cost types based on the trade-off between attack probability and half-saturation constant ($p$-$K$-TO) or maximum growth rate ($p$-$\beta$-TO). A higher half-saturation constant $K_1$ rather than a lower maximum growth rate $\beta_1$ as defense costs allows the defended prey $A_1$ to survive even at lower values of relative competitiveness $N_2^*/N_1^*$ of $A_1$ compared to $A_2$ (cf. Methods, Equation 4). The capital letters display main regions in the trait space with different competition outcomes: Only the undefended prey survives ($A_2$), only the defended prey survives ($A_1$), or both prey types coexist ($A_1A_2$). Coexistence equilibria exist within the region surrounded by black lines, while blue dots indicate where they are locally stable. The dashed orange line marks the invasion boundary of $A_1$. For further details on other regions with multistability, see Figure 1. The black dots with Roman numerals mark trait combinations for which population dynamics and growth functions are shown in Figure 3 (I, II) and Figure 4 (III, IV).

**FIGURE 2**  Comparison of different types of trade-offs between defense and resource competition regarding their effect on coexistence and population dynamics of a defended prey $A_1$ and an undefended prey $A_2$ at an intermediate resource supply ($N_i = 160 \mu$mol N/L). The trait values of $A_1$ are varied within the shown trait space. The defense occurs either prior to an attack by a predator via a lower attack probability $p_1$ (a, b) or after being attacked by a lower consumption probability $q_1$ (c, d). The costs of the defense are either a higher half-saturation constant $K_1$ (a, c) or a reduced maximum growth rate $\beta_1$ (b, d). Both cost traits affect the relative competitiveness $N_2^*/N_1^*$ of $A_1$ compared to $A_2$ (cf. Methods, Equation 4). The capital letters display main regions in the trait space with different competition outcomes: Only the undefended prey survives ($A_2$), only the defended prey survives ($A_1$), or both prey types coexist ($A_1A_2$). Coexistence equilibria exist within the region surrounded by black lines, while blue dots indicate where they are locally stable. The dashed orange line marks the invasion boundary of $A_1$. For further details on other regions with multistability, see Figure 1. The black dots with Roman numerals mark trait combinations for which population dynamics and growth functions are shown in Figure 3 (I, II) and Figure 4 (III, IV).
The effect of the enrichment level

So far, we analyzed how the different defense mechanisms and costs affect the proportion of the trait space leading to coexistence at a certain resource supply (Figure 2). Now, we fix the trait values of both prey types but vary the enrichment level \( N \) to evaluate the maintenance of coexistence under altered environmental conditions. Pre-attack and post-attack defenses differ in their implications for coexistence within a broad range of intermediate defense levels (Figure 2). The type of costs is most relevant at high cost levels and intermediate to high defense levels (Figure 2). According to the general pattern that post-attack defenses promote coexistence and stabilize the dynamics compared to pre-attack defenses, we chose such trait combinations of the defended prey, that is, an intermediate defense level with low costs and a high defense level with high costs (marked in Figure 1), to examine how the differences in coexistence patterns depend on the enrichment level (Figure 5a,b).

At an intermediate level of defense with low costs, coexistence is promoted by the post-attack defense in comparison with the pre-attack defense, independent of the type of costs (Figure 5a). The post-attack defense allows the prey types to stably coexist over a wide range of enrichment levels from low to very high resource supplies while in case of the pre-attack defense coexistence is only possible for a low resource supply (Figure 5a). Contrastingly, at a high level of defense and costs, the coexistence patterns diverge between the different cost types but are rather independent from the defense mechanism. Costs with respect to the half-saturation constant enable coexistence for lower and especially higher enrichment levels compared to costs regarding the maximum growth rate (Figure 5b).

Sensitivity analysis

In Appendix S3, we show how the coexistence and population dynamics of the prey types depend on the amount of the attack time relative to the manipulation time which is defined by \( c_a \) (fraction of total handling time spent for attacking). With higher values of \( c_a \), the post-attack defense increasingly promotes coexistence and stabilizes the dynamics, while the results for the pre-attack defense are independent of \( c_a \) (Appendix S3: Figures C3 and C4). Furthermore, we check the sensitivity of our results with respect to the encounter rate \( a \), the total handling time \( T \), the conversion efficiency of the predator \( \chi_P \), the conversion efficiency of the prey \( \chi \), the resource concentration in the supplied medium \( N_r \), the dilution rate \( \delta \), the maximum growth rate of the undefended prey \( \beta_2 \), and its half-saturation constant \( K_2 \). The general pattern that post-attack defenses promote coexistence and stabilize the dynamics compared to pre-attack defenses is independent of these parameter values. The same holds for the observed pattern that costs regarding the half-saturation constant promote coexistence and the occurrence of cycles more strongly than costs with respect to the maximum growth rate (Appendix S3: Figures C5–C7). Obviously, the exact trait values for the occurrence of coexistence equilibria and their local stability depend on the values of all parameters.

DISCUSSION

We compared the effects of pre-attack and post-attack defenses with different costs in respect to resource competition on
The population densities of the resource $N$ (μmol N/L), both prey types $A_1$ (10^5 ind./mL) and the predator $P$ (ind./mL) are plotted over time $t$. The pre-attack defended prey $A_1$ ($p_1 = 0.05$) has either a higher half-saturation constant ($K_1 = 10$ μmol N/L) (a) or a reduced maximum growth rate ($β_1 = 1.064$ per day) (b) compared to the undefended prey $A_2$. The black dashed lines enclose one growing phase of $A_1$ at high resource concentrations (peak marked with dot) after strong grazing of $A_2$ by $P$. (c) Per capita growth rates of the prey types without mortality in dependence of the resource concentration are represented by the thick lines. The thin vertical green and blue lines show the resource concentration at equilibrium in monoculture $N^*_i$ of each prey type where lower values of $N^*_i$ imply higher competitiveness. The horizontal black dashed-dotted line represents the dilution rate, that is, the mortality of the prey without the predator. The dots illustrate the realized growth rate of the respective defended prey at the resource peaks shown in (a, b).

FIGURE 4 (a) Population dynamics for a trade-off between pre-attack defense and half-saturation constant (trait combination III in Figure 2a) or (b) maximum growth rate (trait combination IV in Figure 2b). The population densities of the resource $N$ (μmol N/L), both prey types $A_1$ (10^5 ind./mL) and the predator $P$ (ind./mL) are plotted over time $t$. The pre-attack defended prey $A_1$ ($p_1 = 0.05$) has either a higher half-saturation constant ($K_1 = 10$ μmol N/L) (a) or a reduced maximum growth rate ($β_1 = 1.064$ per day) (b) compared to the undefended prey $A_2$. The black dashed lines enclose one growing phase of $A_1$ at high resource concentrations (peak marked with dot) after strong grazing of $A_2$ by $P$. (c) Per capita growth rates of the prey types without mortality in dependence of the resource concentration are represented by the thick lines. The thin vertical green and blue lines show the resource concentration at equilibrium in monoculture $N^*_i$ of each prey type where lower values of $N^*_i$ imply higher competitiveness. The horizontal black dashed-dotted line represents the dilution rate, that is, the mortality of the prey without the predator. The dots illustrate the realized growth rate of the respective defended prey at the resource peaks shown in (a, b).

Coexistence and population dynamics in a diamond-shaped food web. The post-attack defense promoted coexistence and stabilized the dynamics more than a pre-attack defense. Post-attack defended individuals damp the growth of the predator by keeping it handling them which indirectly facilitates the undefended prey. This mechanism enabled coexistence at trait combinations where the defended prey would outcompete the undefended one in case of a pre-attack defense. Costs regarding resource competition were either a higher half-saturation constant or a lower maximum growth rate. The former cost type promoted coexistence and cycling population densities more than a lower maximum growth rate by allowing the defended prey to realize high growth rates at temporally high resource concentrations which prevents its extinction even if it has a very low competitiveness.

The main difference between both defense mechanisms is that a post-attack defended prey affects the functional response of the predator consuming an undefended prey while a pre-attack defended prey does not. In a previous study of Grover (1995), inedible plants were generally described as interfering when they negatively affect the growth of the herbivore consuming an edible plant. This interference weakens the interaction between the predator and its prey. In food web theory, weak interactions are known to stabilize the population dynamics (McCann, 2011; McCann, Hastings, & Huxel, 1998). In fact, several authors (Grover, 1995; Kretzschmar, Nisbet, & Mccauley, 1993; Vos, Berrocal, Karamaouna, Hemerik, & Vet, 2001) showed that interfering inedible species stabilized dynamics in comparison with noninterfering inedible ones which resembles the effect observed in our study, while they did not reveal the potential of interfering defended prey to enhance coexistence. This was not possible in their systems because the defended prey was completely inedible. Thus, it could not maintain the predator by itself and always had to coexist with the undefended prey. Contrastingly, we considered defense as a continuous trait. At low and intermediate defense levels, the defendned prey is able to outcompete the undefended prey. The trait range where this competitive exclusion of the undefended prey occurred was strongly reduced by the post-attack defense, while the trait range allowing coexistence increased in comparison with a noninterfering pre-attack defense due to indirect facilitation. The relevance of our results is supported by empirical studies revealing that low to intermediate defense levels frequently occur in nature (White, Kaul, Knoll, Wilson, & Sarnelle, 2011) and that defended prey types may outcompete undefended prey types even if they have costs for their defense (Kasada et al., 2014).

FIGURE 5 Coexistence of two prey types depending on the level of resource supply $N_i$ (μmol N/L), that is, the enrichment level, for different trade-offs (TO) between pre-attack ($p$) or post-attack defense ($q$) and the half-saturation constant ($K$) or maximum growth rate ($β$). The bars indicate the range where both prey types stably coexist, implying that a coexistence equilibrium exists and the defended prey can invade the undefended prey. The defended prey has either (a) an intermediate defense level and low costs ($p_1$ or $q_1 = 0.4, N_2^*/N_1^* = 0.8$) or (b) a high defense level and high costs ($p_1$ or $q_1 = 0.1, N_2^*/N_1^* = 0.2$). These trait combinations are indicated in Figure 1.
presented mechanism of indirect facilitation among prey species may provide an explanation why apparent competition, that is, an increasing density of one prey species indirectly reduces the density of the other prey species via the predator (Holt, 1977), is not always observed in nature (Chaneton & Bonsall, 2000).

If attacking defended prey types hampers predator’s growth, the question arises whether the predator adapts and entirely disregards the defended prey implying that post-attack defenses become pre-attack defenses. Pre-attack defenses are also favorable from the point of view of the defended prey which is then able to better outcompete a competing undefended prey. Accordingly, predator and defended prey may evolve toward avoiding interactions with each other which would mean that being not attacked is the prevailing defense strategy. This reasoning is supported by the observation that many defended prey species show warning signals to deter the predator from attacking them (Blount et al., 2012; Stevens & Ruxton, 2012) and that predators often show behavioral changes to avoid defended prey species (White et al., 2011; Xu, Nielsen, & Kiørboe, 2018). However, not attacking defended prey species implies a higher grazing pressure on undefended prey species which may reduce their population densities leading to the dominance of defended prey species. The resulting lack in food may cause predators to attack the defended prey (Barnett, Bateson, & Rowe, 2007; Fryxell & Lundberg, 1994). However, if the defense of the prey is very effective, such prey switching behavior of the predator is unlikely. Several studies highlighted the importance of the interplay between the predator’s diet choice and the level of defense for prey coexistence and population dynamics (Abrams & Matsuda, 1993; Fryxell & Lundberg, 1994; Yamauchi & Yamamura, 2005). Another argument for the occurrence of post-attack defenses in nature is the inability of predators to discriminate between undefended and defended prey. This may hold especially for predators with nonselective feeding strategies, like, for example, filter feeding Daphnia sp. consuming filamentous algae (Peter & Lampert, 1989). Furthermore, it strongly depends on the costs of the prey which defense mechanisms evolve (Bateman et al., 2014). Post-attack defenses may evolve if pre-attack defenses are very costly, for example, if avoiding habitats with predators substantially lowers the possibility of resource acquisition (Verdolin, 2006).

The used categorization into pre- and post-attack defenses is based on mechanistic considerations regarding their effect on the invested handling time of the predator. Even if these categories are relevant for a broad range of defense mechanisms, they may not apply to every specific defense strategy. For example, several algal species are digestion-resistant; that is, they are attacked and ingested by the zooplankton but survive the gut passage (Demott & McKinney, 2015; Meyer et al., 2006; Porter, 1973). The same holds also for some species of aquatic snails eaten by mallards (van Leeuwen, van der Velde, van Lith, & Klaassen, 2012; Wada, Kawakami, & Chiba, 2012). Such digestion resistance may promote coexistence and stabilize the dynamics even more than post-attack defended prey (see Appendix S1). Furthermore, toxicity of a prey may differ in the consequences on prey coexistence from the defense mechanisms considered here, especially when it interferes not only with the predator but also with the competitor (Hiltunen, Barreiro, & Hairston, 2012). However, for a large variety of defense strategies, for example, aposematism, weaponry or mimicry, the used classification regarding the phase at which the defense interrupts the predation sequence is adequate. We distinguished between early (pre-attack) and late (post-attack) defenses (Bateman et al., 2014). Of course, in nature there are gradients between pre- and post-attack defenses, that is, the handling of the predator aborts at different points in time which can be mimicked by varying the parameter $c_a$ (see Appendix S3). In the presented model, $c_a$ was defined as the fraction of handling time invested in attacking prey. However, in a more general sense, $c_a$ can be interpreted as the timing of a defended prey to abort the predation sequence relative to the total handling time, that is, a large $c_a$ corresponds to a late defense and vice versa. Therefore, the given equation of the predator’s functional response for two prey types (Equation 2) can be applied to multiple defense mechanisms acting at different phases of the predation sequence.

Hammill, Kratina, Vos, Petchey, and Anholt (2015) provided first empirical evidence that inedible prey species promote persistence of edible ones based on an experiment with a flatworm feeding on ciliates. However, despite the wide-spread occurrence of post-attack defenses, we found no study specifically analyzing their effect on coexistence and comparing it to pre-attack defenses. Thus, our research may serve as a starting point for future empirical studies on the maintenance of functional diversity within prey communities due to indirect facilitation of undefended prey species by post-attack defended prey species.

Quantifying defense costs is often difficult as it requires knowledge about the functional property of the prey which is influenced by an altered allocation of resources to implement the defense. Furthermore, the costs may be system specific and may vary depending on the environment (Siemens, Garner, Mitchell-Olds, & Callaway, 2002; Strauss, Rudgers, Lau, & Irwin, 2002); for example, they may occur only when a competitor is present (van Velzen & Etienne, 2015). We focussed on two major cost traits of defended prey types which describe their resource-dependent growth kinetics: a higher half-saturation constant which implies a reduced competitiveness at low resource concentration, and a lower maximum growth rate which reduces growth independent of the resource concentrations. Studies on plankton organisms revealed that trade-offs between maximum growth rates and defenses frequently occur (Agrawal, 1998; Meyer et al., 2006) but half-saturation constant-defense trade-offs were found as well (Becks et al., 2010; Yoshida et al., 2004). Furthermore, there is indication from phytoplankton organisms that the maximum growth rate and the half-saturation constant are often positively correlated (Edwards, Klausmeier, & Litchman, 2013; Litchman, Edwards, & Klausmeier, 2015). Thus, Aksnes and Egge (1991) and Smith et al. (2014) suggested an alternative mechanistic formulation of nutrient-uptake kinetics for phytoplankton organisms which accounted implicitly for this correlation. They used the affinity, that is, the slope of the uptake function at resource concentrations close to zero, instead
of the half-saturation constant as a parameter describing the performance at low resource concentrations. However, the outcome would be similar: a lower affinity rather than a lower maximum growth rate as defense costs promote coexistence and destabilizes the dynamics because it allows for temporally high growth rates of the defended prey at resource peaks.

In the context of plant communities, there is an ongoing debate on the costs of defenses against herbivory. Several studies indicated that there is often no interspecific trade-off between defense and competitiveness as a higher resource supply adversely affected defended plants (Lind et al., 2013; Viola et al., 2010). In fact, Lind et al. (2013) demonstrated that defended plants are commonly the better competitor when resources are depleted but perform less well at high resource concentrations. Such multidimensional trade-offs may be included in future studies considering specific prey communities and their cost type/s of defense.

The coexistence of defended and undefended prey types critically depends on the relative importance of bottom-up and top-down control, that is, the enrichment level of the system (Bohannan & Lenski, 2000; Leibold, 1996; Proulx & Mazumder, 1998). Higher enrichment levels promote the defended prey as its disadvantage regarding resource competition gets less important relative to its advantage of being defended against predation. Thus, our insights on how the competitive exclusion of an undefended prey by an immediately defended prey is prevented in case of post-attack defense may prevail more in systems with an intermediate or high resource supply (Figure 5a). A high system productivity reduces also the potential extinction risk of the defended prey if the defense costs arise from a high half-saturation costs where resource peaks permit temporally high growth rates of the defended prey (Figure 5b). Hence, we conclude that the current trend of anthropogenic eutrophication of ecosystems enhances the necessity to discriminate between different defense mechanisms and their associated costs.

ACKNOWLEDGMENTS

We thank Toni Klauschies, Lutz Becks, and Thomas Kiørboe for fruitful discussions on the results, and Janne Hülsemann, Michael Raatz, Christopher Klausmeier, and two anonymous reviewers for valuable comments on an earlier version of the manuscript. This research was funded by the German Research Foundation (DFG, GA 401/25-1) and the Open Access Publishing Fund of University of Potsdam.

CONFLICT OF INTEREST

None declared.

AUTHORS’ CONTRIBUTION

EE had the principal idea; EE and UG designed the study; EE did the mathematical and numerical analyses and wrote the manuscript on which UG commented.
Sterns, S. C. (1989). Trade-offs in life-history evolution. *Functional Ecology*, 3(3), 259. https://doi.org/10.2307/2389364

Stevens, M., & Ruxton, G. D. (2012). Linking the evolution and form of warning coloration in nature. *Proceedings of the Royal Society B: Biological Sciences*, 279(1728), 417–426. https://doi.org/10.1098/ rspb.2011.1932

Strauss, S. Y., Rudgers, J. A., Lau, J. A., & Irwin, R. E. (2002). Direct and ecologic costs of resistance to herbivory. *Trends in Ecology and Evolution*, 17(6), 278–285. https://doi.org/10.1016/S0169-5347(02)02483-7

Thingstad, T. F. (2000). Elements of a theory for the mechanisms controlling abundance, diversity, and biogeochemical role of lytic bacterial viruses in aquatic systems. *Limnology and Oceanography*, 45(6), 1320–1328. https://doi.org/10.4319/lo.2000.45.6.1320

Tilman, D. (1982). *Ecology*, 65, 787–807.

van Velzen, E., & Etienne, R. S. (2015). The importance of ecological viruses in aquatic systems. *Limnology and Oceanography*, 60(6), 1748–1759. https://doi.org/10.4319/lo.2015.60.6.1748

Verdolin, J. S., ... van der Velde, G., van Lith, B., & Klaassen, M. (2012). Experimental quantification of long distance dispersal potential of aquatic snails in the gut of migratory birds. *PLoS One*, 7(3), e32292. https://doi.org/10.1371/journal.pone.0032292

van Velzen, E., & Etienne, R. S. (2015). The importance of ecological costs for the evolution of plant defense against herbivory. *Journal of Theoretical Biology*, 372, 89–99. https://doi.org/10.1016/j.jtbi.2015.02.027

Vos, M., Berrocal, S. M., Karamaouna, F., Hemerik, L., & Vet, L. E. M. (2001). Plant-mediated indirect effects and the persistence of parasitoid-herbivore communities. *Ecology Letters*, 4, 38–45. https://doi.org/10.1046/j.1461-0248.2001.00191.x

White, J. D., Kaul, R. B., Knoll, L. B., Wilson, A. E., & Sarnelle, O. (2011). Large variation in vulnerability to grazing within a population of the colonial phytoplankter, *Microcystis aeruginosa*. *Limnology and Oceanography*, 56(5), 1714–1724. https://doi.org/10.4319/lo.2011.56.5.1714

Winten, C., Bouvier, T., Weinbauer, M. G., & Thingstad, T. F. (2010). Trade-offs between competition and defense specialists among unicellular planktonic organisms: The “killing the winner” hypothesis revisited. *Microbiology and Molecular Biology Reviews*, 74(1), 42–57. https://doi.org/10.1128/MMBR.00034-09

Xu, J., Nielsen, L. T., & Kierboe, T. (2018). Foraging response and acclimation of ambush feeding and feeding-current feeding copepods to toxic dinoflagellates. *Limnology and Oceanography*, in press, https://doi.org/10.1002/ino.10782

Yamauchi, A., & Yamamura, N. (2005). Effects of defense evolution and diet choice on population dynamics in a one-predator-two-prey system. *Ecology*, 86(9), 2513–2524. https://doi.org/10.1890/04-1524

Yoshida, T., Ellner, S. P., Jones, L. E., Bohannan, B. J. M., Lenski, R. E., & Hairston, N. G. Jr (2007). Cryptic population dynamics: Rapid evolution masks trophic interactions. *PLoS Biology*, 5(9), e235. https://doi.org/10.1371/journal.pbio.0050235

Yoshida, T., Hairston, N. G., & Ellner, S. P. (2004). Evolutionary trade-off between defense against grazing and competitive ability in a simple unicellular alga, *Chlorella vulgaris*. *Proceedings of the Royal Society B: Biological Sciences*, 271(1551), 1947–1953. https://doi.org/10.1098/rspb.2004.2818

Yoshida, T., Jones, L. E., Ellner, S. P., Fussmann, G. F., & Hairston, N. G. (2003). Rapid evolution drives ecological dynamics in a predator-prey system. *Nature*, 424(July), 303–306. https://doi.org/10.1038/nature01767

**SUPPORTING INFORMATION**

Additional supporting information may be found online in the Supporting Information section at the end of the article.

**How to cite this article:** Ehrlich E, Gaedke U. Not attackable or not crackable—How pre- and post-attack defenses with different competition costs affect prey coexistence and population dynamics. *Ecol Evol*. 2018;8:6625–6637. https://doi.org/10.1002/ece3.4145