Experimental study of isovector spin sum rules

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(Dated: September 24, 2008)

We present the Bjorken integral extracted from Jefferson Lab experiment EG1b for 0.05 < Q^2 < 2.92 GeV^2. The integral is fit to extract the twist-4 element \( F_2^{p,n} \) which appears to be relatively large and negative. Systematic studies of this higher twist analysis establish its legitimacy at \( Q^2 \) around 1 GeV^2. We also performed an isospin decomposition of the generalized forward spin polarizability \( \gamma_0 \). Although its isovector part provides a reliable test of the calculation techniques of Chiral Perturbation Theory, our data disagree with the calculations.

PACS numbers: 13.60.Hb, 11.55.Hx, 25.30.Rw, 12.38.Qk, 24.70.+s

INTRODUCTION

The Bjorken sum rule [1] relates an integral over the spin distributions of quarks inside the nucleon to its axial charge. This relation has been essential for understanding the nucleon spin structure and establishing, via its \( Q^2 \)-dependence, that Quantum Chromodynamics (QCD) describes the strong force when spin is included. The Bjorken integral has been measured in polarized deep inelastic lepton scattering (DIS) at SLAC, CERN and DESY [4]-[7] and at moderate four-momentum transfer squared \( Q^2 \) at Jefferson Lab (JLab) [8], see e.g. Ref. [9] for a review. The variable \( Q^2 \) is inversely related to the space-time scale at which the nucleon is probed. In the perturbative QCD (pQCD) domain (high \( Q^2 \)) the sum rule reads [10]:

\[
\Gamma_i^{p,n}(Q^2) = \int_0^1 dx \left( g_i^p(x, Q^2) - g_i^n(x, Q^2) \right) = \frac{g_A}{6} \left[ 1 - \frac{\alpha_s}{\pi} - 3.58 \frac{\alpha_s^2}{\pi^2} - 20.21 \frac{\alpha_s^3}{\pi^3} + \ldots \right] + \sum_{i=2}^{\infty} \frac{\mu_{2i}^{p,n}(Q^2)}{Q^{2i-2}}
\]

where \( g_i^p \) and \( g_i^n \) are the spin-dependent proton and neutron structure functions, \( g_A \) is the nucleon axial charge that controls the strength of neutron \( \beta \)-decay, \( \alpha_s(Q^2) \) is the strong coupling strength and \( x = Q^2/2M\nu \), with \( \nu \) the energy transfer and \( M \) the nucleon mass. The bracket term (\( \mu_2 \), known as the leading twist term) is mildly dependent on \( Q^2 \) due to pQCD soft gluon radiation. The other term contains non-perturbative power corrections (higher twists). These are quark and gluon correlations that need to be understood to describe the nucleon structure away from the large \( Q^2 \) limit. The \( Q^2 \)-dependence of \( \mu_2(Q^2) \) is calculable in principle from pQCD. In practice, this has been done for \( \mu_2 \) and \( \mu_4 \) only [11]. We stress that, as is almost always the case with pQCD, although the \( Q^2 \)-dependences are known, the absolute values of \( \mu_2 \) and \( \mu_4 \) are unknown and need to be measured or computed by non-perturbative means.

Besides its contribution to establishing pQCD (at high \( Q^2 \)), the Bjorken sum rule can be used to extract higher twists, to check lattice QCD calculations (at moderate \( Q^2 \)), and to test effective theories of the strong force (at low \( Q^2 \)). In addition, Bjorken sum data and phenomenological models at lower \( Q^2 \) can be described with a nearly constant “effective strong coupling” \( \alpha_{s,q} \) [12, 13]. The lack of \( Q^2 \)-dependence of \( \alpha_{s,q} \) opens new avenues for non-perturbative QCD calculations using the AdS/CFT correspondence [14].

The elastic contribution to the Bjorken sum is usually not included because the generalized Bjorken sum rule is derived at large \( Q^2 \) where such contribution is negligible. Furthermore, the Bjorken sum rule naturally connects to the Gerasimov-Drell-Hearn sum rule [15] in which the elastic is inessential. Consequently, when presenting the experimental measurement of the Bjorken sum, the elastic contribution will not be included. We refer to ref. [10] for a discussion on whether to include or not the elastic contribution to the GDH sum rule. However, for higher twist analysis, all reactions should be included for a meaningful higher twist extraction [16]-[18]. Therefore, in the part of the paper discussing higher twist extraction, the elastic contribution to the Bjorken sum will be added.

In this paper, new data from the JLab CLAS EG1b experiment [20]-[22] taken on polarized proton and deuteron targets are used to extract the Bjorken integral over an extended \( Q^2 \) range: 0.05 < \( Q^2 < 2.92 \) GeV^2.
compared to the previous JLab range $0.15 < Q^2 < 1.5$ GeV$^2$.

The extension down to $Q^2 = 0.05$ GeV$^2$ allows us to compare to Chiral Perturbation Theory ($\chi$PT) calculations in a domain where the chiral approximation should be valid. The moderate $Q^2$ range had been precisely measured $^8$. The new data set, of equivalent precision, provides a useful check. In particular, it verifies the neutron results, which come mostly from $^3$He in Ref. $^8$ and from the deuteron in this paper. At larger $Q^2$ ($\gtrsim 1$ GeV$^2$, where Eq. $^11$ holds), higher twists can now be studied with a statistical precision typically improved by a factor of 2. Previous work $^8$ has shown the necessity of precise $Q^2$ mapping at moderate $Q^2$ ($\gtrsim 1$ GeV$^2$) because of the surprisingly small size of the overall higher twist effect. One might be tempted to lower the $Q^2$ values at which the analysis is done (see Eq. $^1$) but this is not reliable due to the fast $1/Q^{2i-2}$ rise of twist $i$ contributions at low $Q^2$ and to the increasing uncertainty of the evolution of the twist-2 parts. The main contributor at low $Q^2$ to this uncertainty is the strong coupling constant $\alpha_s(Q^2)$.

The Bjorken integral is advantageous compared to the individual moments $\Gamma^p_1$ and $\Gamma^n_1$ because of simplifications arising from its non-singlet (p-n) nature: at moderate $Q^2$ lattice QCD calculations are easier and more reliable because disconnected diagrams, which cannot be easily computed on the lattice, cancel out. At higher $Q^2$, the (p-n) simplification provides a sum rule (the Bjorken sum rule) based on more solid grounds than the sum rules for individual nucleons (the Ellis Jaffe sum rules $^19$). Nevertheless, calculations based on $\chi$PT and data for $\delta_{LT}$ on the neutron $^27$ strongly disagree. This calls for more low $Q^2$ studies, especially the yet unmeasured $\delta_{LT}$ $^30$. The data discussed in this paper were taken with a longitudinally polarized target and hence cannot be used to extract $\delta_{LT}$. However, the generalized forward spin polarizability $\gamma_0$ can be obtained and, just like the Bjorken integral, its isovector part $\gamma_0^p - \gamma_0^n$ offers the same advantages as $\delta_{LT}$ for checking the calculation techniques of $\chi$PT. We will also report on these results.

### TABLE I: The measured $(\Gamma^p_{1,\text{meas}})$ and total $(\Gamma^p_{1,\text{tot}})$ Bjorken integrals for different $Q^2$ points (in GeV$^2$). The experimental systematic uncertainty $\sigma_{\text{stat}}$ is given in the 3$^{rd}$ column. Total systematics uncertainty, including the low and large-$x$ extrapolations, $(\sigma_{\text{syst}})$ and statistical uncertainty $\sigma_{\text{stat}}$ on $\Gamma^p_{1,\text{tot}}$ are given in the 5$^{th}$ and 6$^{th}$ columns.

| $Q^2$ | $\Gamma^p_{1,\text{meas}}$ | $\sigma_{\text{syst}}$ | $\Gamma^p_{1,\text{tot}}$ | $\sigma_{\text{syst}}$ | $\sigma_{\text{stat}}$ |
|-------|-----------------|----------------|-----------------|----------------|----------------|
| 0.054 | 0.0028          | 0.0105         | 0.0119          | 0.0078         |
| 0.078 | -0.0085         | 0.0112         | 0.0019          | 0.0070         |
| 0.101 | 0.0076          | 0.0105         | 0.0206          | 0.0114         |
| 0.132 | 0.0129          | 0.0124         | 0.0296          | 0.0158         |
| 0.188 | 0.0209          | 0.0181         | 0.0464          | 0.0223         |
| 0.269 | 0.0153          | 0.0152         | 0.0411          | 0.0215         |
| 0.382 | 0.0197          | 0.0139         | 0.0150          | 0.0039         |
| 0.496 | 0.0184          | 0.0110         | 0.0097          | 0.0225         |
| 0.592 | 0.0318          | 0.0143         | 0.1027          | 0.0228         |
| 0.707 | 0.0513          | 0.0174         | 0.0945          | 0.0201         |
| 0.844 | 0.0507          | 0.0157         | 0.1021          | 0.0193         |
| 1.01  | 0.0656          | 0.0152         | 0.1236          | 0.0200         |
| 1.20  | 0.0625          | 0.0161         | 0.1307          | 0.0192         |
| 1.44  | 0.0118          | 0.0141         | 0.1322          | 0.0186         |
| 1.71  | 0.0695          | 0.0129         | 0.1605          | 0.0182         |
| 2.05  | 0.0616          | 0.0118         | 0.1678          | 0.0177         |
| 2.44  | 0.0458          | 0.0098         | 0.1666          | 0.0167         |
| 2.92  | 0.0483          | 0.0079         | 0.1789          | 0.0106         |
| 3.48  | 0.0404          | 0.0050         | 0.1872          | 0.0095         |

### BJORKEN SUM EXTRACTION AND COMPARISON WITH CHIRAL PERTURBATION CALCULATIONS

The measurements of structure functions $g_1^p$ and $g_1^d$ are described in Refs. $^{20-22}$. The data cover an invariant mass range up to $W = 3$ GeV for $0.054 \leq Q^2 \leq 2.92$ GeV$^2$. Since experimental moments are integrated over a finite $W$ range, the data have to be supplemented by models for large $W$. We used the model described in Ref. $^{20}$ down to $x = 0.001$. This part is known from DIS experiments. The rest is determined using a Regge parametrization $^8$ which was compared to that of Bass and Brisudova $^{28}$ and found consistent with it. A parameterization was also used to estimate the contributions between pion threshold ($1.08$ GeV) and $1.15$ GeV $^{20}$.

The Bjorken integral is obtained from $\Gamma^p_1$ and $\Gamma^d_1$ assuming:

$$\Gamma^p_{1,-n} = 2\Gamma^p_1 - \Gamma^d_1 / (1 - 1.5\omega_d),$$

with the deuteron D-state probability $\omega_d = 0.05 \pm 0.01$ $^{29}$. The data are given in Table I (a more detailed table is given in $^{30}$ and shown in Fig. I) The elastic contribution ($x = 1$) is excluded. Data from SLAC E143 $^3$, HERMES $^7$, JLab CLAS EG1a (proton and deuteron), and JLab Hall A E94010 (neutron from $^3$He) combined with CLAS EG1a (proton) $^8$ are also shown for comparison.

There is excellent agreement between the Bjorken inte-
The agreement between interpretation of the low $Q^2$ in Fig. 1. The model of Burkert and Ioffe \cite{31} (continuous and with the two phenomenological models shown data also agree well with the SLAC and HERMES experi-
ments and with the two phenomenological models shown

At moderate $Q^2$, we observe a strong variation of the Bjorken integral, in contrast to the high $Q^2$ region. Together with our data at the lowest $Q^2$ points, the kinematic constraint $\Gamma_1 \rightarrow 0$ when $Q^2 \rightarrow 0$ suggests a small $Q^2$-dependence of $\Gamma_{p-n}^{p-n}$ at low $Q^2$ as well. This would agree with the fact that the $\Gamma_1$ slope at $Q^2 \approx 0$ is given by the generalized GDH sum rule which predict a small $Q^2$-dependence.

At low $Q^2$ the data are consistent up to $Q^2 \approx 0.2$ GeV$^2$ with the $\chi PT$ calculations of Bernard et al. \cite{33} and up to $Q^2 \approx 0.35$ GeV$^2$ for those of Ji et al. done in the heavy baryon approximation \cite{34}. The range of validity of the $\chi PT$ calculations seems larger than of individual nucleons \cite{9}, \cite{22} possibly because the $\Delta_{1232}$ resonance is suppressed in the Bjorken integral \cite{33}. This result, however, is not trivial: Good agreement was expected between $\delta_{LT}$ and $\chi PT$ results since the $\Delta_{1232}$ is strongly suppressed at low $Q^2$ for $\delta_{LT}$. However, its measurement for the neutron \cite{27} disagrees strongly with $\chi PT$ calculations.

To quantitatively compare with $\chi PT$ calculations, we fit our results up to a maximum $Q^2$ ranging from 0.30 to 0.50 GeV$^2$ (fits on lower $Q^2$ ranges are imprecise, and higher $Q^2$ data may lie out of the region of validity for $\chi PT$). We included the data from Ref. \cite{8} in the fit. Our fit form is:

$$\Gamma_{p-n}^{p-n} = \frac{\kappa_n^2 - \kappa_p^2}{8M} Q^2 + aQ^4 + bQ^6$$

in which $\kappa$ is the anomalous moment of the nucleon and $a$ and $b$ are fit parameters. The first term in Eq. 2 stems from the Gerasimov-Drell-Hearn sum rule \cite{9}. We find $a = 0.80 \pm 0.07(stat) \pm 0.23(syst)$ and $b = -1.13 \pm 0.16(stat) \pm 0.39(syst)$ with $\chi^2/dof = 1.50$. The $Q^4$ term agrees well with the results from Ji et al. ($a = 0.74$) but not with those of Bernard et al. ($a = 2.4$). The fit underscores the importance of the $Q^6$ term (not calculated yet in $\chi PT$). This was also noticed for $\Gamma_1^{p}$ and $\Gamma_1^{n}$ \cite{22}.

At high $Q^2$, the leading twist pQCD calculation is given by the bracket term of Eq. 1 and is represented by the gray band in Fig. 1. It agrees reasonably well with the data. This implies that the total higher twist contribution is relatively small even down to $Q^2 \approx 1$ GeV$^2$ where one would expect higher twist contributions to be significant. Higher twists, which measure parton correlations, are weighted by $1/Q^{(t-2)}$ (with $t$ being the twist number) and are related to the confinement mechanisms and to scattering off coherent quarks. Because of these reasons, it was initially expected that higher twists would play an important role at $Q^2 \approx 1$ GeV$^2$. Higher twists can be positive or negative but there is no fundamental reason to expect a well-tuned cancellation of different terms in

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig1.png}
\caption{(Color online) The Bjorken integral $\Gamma_{p-n}^{p-n}(Q^2)$. The solid blue circle give the results from this work with the horizontal band giving the systematic uncertainties. Other symbols show the data from experiments E143 \cite{3} (open diamonds), E155 \cite{4} (open star), HERMES \cite{7} (open triangles) and JLab \cite{8} (open circles and open squares). For those, the error bars represent the quadratic sum of the statistic and systematic uncertainties. The gray band represents the leading-twist NNLO pQCD calculation. The curves correspond to $\chi PT$ calculations \cite{33, 34} and phenomenological models \cite{31, 32}.}
\end{figure}
the higher twist series that would make the overall higher twist contribution small. However, this seems to be the case experimentally, at least around $Q^2 \approx 1$ GeV$^2$. One of the aims of the higher twist analysis reported here is to establish whether higher twists are intrinsically small, or whether the terms in the higher twist series conspire to cancel.

**HIGHER TWIST ANALYSIS**

The first higher twist correction term in Eq. 11 is

$$\mu_4^{p-n} = \frac{M^2}{9} \left( a_2^{p-n} + 4a_2^{p-n} + 4f_2^{p-n} \right),$$

where $a_2$ and $d_2$ are known. They are given by moments of the leading twist part of $g_1$ and the twists 2 and 3 parts of $g_2$: $a_2 = \int x^2 \, dx \left( 2g_1 + 3g_2 \right)$ and $d_2 = \int x^2 \, dx \left( 2g_1 + 3g_2 \right)$. The twist-4 term that we wish to extract is $f_2^{p-n}$. To perform a higher twist analysis, the elastic contribution includes the elastic contribution estimated from form factor parameterizations [38].

The twist-4 term that we wish to extract is $f_2^{p-n}$. To perform a higher twist analysis, the elastic contribution includes the elastic contribution estimated from form factor parameterizations [38].

The moment $\Gamma_4^{p-n}$, which was free to vary within its experimental uncertainties, is shown in Fig. 2. In Eq. 1, $\alpha_s$ is computed up to next to leading order. A fit of polarized quark distributions [38] yields $A_2^{p-n} = 0.031 \pm 0.010$ at $Q^2 = 1$ GeV$^2$, whereas $d_2^{p-n} = -0.007 \pm 0.010$ is obtained from Ref. 15 and Ref. 33 evolved to 1 GeV$^2$. The EG1b data on $\Gamma_1^{p-n}$, together with the world’s data, can then be fit to extract $f_2^{p-n}$ using Eqs. 11 and 3. To account for twists greater than rank 4, we include a coefficient $\mu_6^{p-n}/Q^4$. For consistency, former data on $\Gamma_4^{p-n}$ were reanalyzed using the same model as used in this paper to extrapolate to low $x$. For both JLab data sets (Ref. 8 and the present data), the point-to-point correlated uncertainties have been separated from the uncorrelated ones. The latter are added in quadrature to the statistical uncertainties. The correlated systematics are propagated independently, as is the uncertainty arising from $\alpha_s$. The result of the fit done in the $Q^2$-range from 0.66 to 10 GeV$^2$ in $f_2^{p-n}$ ($Q^2 = 1$ GeV$^2$) = $-0.101 \pm 0.027^{+0.063}_{-0.071}$ with $\mu_4/M^4 = 0.084 \pm 0.011 \pm 0.022$. The first uncertainty is the quadratic sum of the statistical and the point-to-point uncorrelated uncertainties. The second one is the point to point correlated uncertainty.

The result for $f_2^{p-n}$ is plotted in Fig. 3 (square) along with the result from Ref. 8 (triangle) and theoretical predictions (In addition to $f_2$ and $\mu_4$, the third fit parameter mentioned in Figs. 2 and 3 is $g_4$, which was free to vary within its experimental uncertainty). As discussed in the introduction, only the $Q^2$-dependence of $f_2$ is known from pQCD. The absolute value can be computed solely from non-perturbative means and is difficult to obtain with Lattice QCD. For these reasons, only phenomenological models are available for comparison with our results.

![FIG. 2: (Color online) World data on the Bjorken integral, including the elastic contribution. The error bars represent the quadratic sum of the statistic and point-to-point-uncorrelated systematic uncertainties for the JLab data, and the quadratic sum of the statistic and full systematic uncertainties for the rest of the data. The continuous line is our three parameter fit in the $Q^2$-range from 0.66 to 10 GeV$^2$.

![FIG. 3: $f_2^{p-n} (Q^2 = 1$ GeV$^2$) for the fits performed over the 0.66 < $Q^2$ < 10 GeV$^2$ range for this study and Ref. 8 (JLab A/B). Calculations [11, 41] are shown by the bands. Sum rule (1) refers to Ref. 11 and (2) to Ref. 41.]

- At $Q^2 = 1$ GeV$^2$, the leading twist term $\mu_2^{p-n}$ and higher twist terms $\mu_4^{p-n}$ and $\mu_6^{p-n}$ are of similar sizes but with alternating signs and with $\mu_4^{p-n}$ and $\mu_6^{p-n}$ mostly canceling each other.

- To study the systematics associated with this higher twist analysis and to check the legitimacy of our procedure at low $Q^2$, we conducted several tests:
  1. We repeated the fit for several $Q^2$ ranges;
  2. We reiterated this work adding a $\mu_8^{p-n}/Q^6$ term to study the convergence of the twist series (the resulting $f_2^{p-n}$ is shown in Fig. 3 by the solid circle);
  3. We investigated the dependence on the low $x$ extrapolation using different Regge-based parameterizations;
4. We extensively studied the stability of the fit for different choices of number of parameters and of $Q^2$ ranges by using different models that reproduce the data reasonably well. We used ranges from $0.47 < Q^2 < 10$ to $3 < Q^2 < 10$ GeV$^2$ and we fit with functional forms with highest term from $\mu_6/Q^3$ to $\mu_{12}/Q^{10}$.

All observations supports the validity of our extractions. See Ref. [30] for details.

**COLOR POLARIZABILITIES**

Combination of higher twist coefficients can be interpreted in terms of color polarizabilities, which describe the response of the color magnetic and electric fields to the spin of the nucleon. The color electric and magnetic polarizabilities [40, 45] are $\chi_E = (2d_2 + f_2)$ and $\chi_B = (4d_2 - f_2)$. Using the value of $f_2^{p-n}$ extracted from the fit with $Q^2_{min} = 0.66$, we obtain $\chi_E^{p-n} = -0.077 \pm 0.050$ and $\chi_B^{p-n} = 0.024 \pm 0.028$. The point-to-point correlated and uncorrelated uncertainties on $f_2$ were added in quadrature. Our higher twist analysis yields $|f_2^{p-n}| \gg |d_2^{p-n}|$ (a feature predicted by models [43] and [44]). Consequently $\chi_E^{p-n} \approx \frac{2}{3} f_2^{p-n}$ and $\chi_B^{p-n} \approx -\frac{1}{3} f_2^{p-n}$.

**ELECTROMAGNETIC POLARIZABILITY**

We now turn to the generalized forward spin polarization $\gamma_0$. Spin polarizabilities characterize the coherent response of the nucleon to photons. They are defined using low-energy theorems in the form of a series expansion in the photon energy. The first term of the series comes from the spatial distribution of charge and current (form factors) while the second term results from the deformation of these distributions induced by the photon (polarizabilities). Hence, polarizabilities are as important as form factors in understanding coherent nucleon structure. Generalized spin polarizabilities describe the response to virtual photons. The low energy theorem defining the generalized forward spin polarization is:

$$\gamma_0 = \frac{16\alpha M^2}{Q^6} \int_0^{x^2} x^2 \left( g_1 - 4M^2 x^2 g_2 \right) dx,$$

where $g_2$ is the second spin structure function and $\alpha$ is the fine structure constant. Similar relations define the generalized longitudinal-transverse polarizability $\delta_{LT}$:

$$\Delta \gamma_L = \frac{2\alpha}{M^2} \int_0^{x^2} x^2 (g_1 + g_2) dx.$$


| \( Q^2 \) (GeV\(^2\)) | \( \gamma_0^{p-n} \) | \( \gamma_0^{p+n} \) | Stat. | Syst. |
|-----------------|-----------------|-----------------|------|------|
| 0.1             | 1.53            | -2.51           | 0.120 | 0.490 |
| 0.26            | 0.470           | -0.869          | 0.021 | 0.177 |
| 0.42            | 0.159           | -0.241          | 0.006 | 0.058 |
| 0.58            | 0.0835          | -0.0845         | 0.0040| 0.0233|
| 0.74            | 0.0441          | -0.0299         | 0.0037| 0.0090|
| 0.9             | 0.0217          | -0.0103         | 0.0016| 0.0040|

TABLE II: Isovector and isoscalar parts of the generalized forward spin polarizability \( \gamma_0 \).

the \( \chi PT \) calculation of one of the isospin components of \( \gamma_0 \) along with agreement for the other component might have allowed us to identify a missing piece, such as for example a short range interaction due to heavy mesons, in the \( \chi PT \) calculations. However, the discrepancy between data and \( \chi PT \) calculations for both isospin components does not allow us to draw such conclusion. This suggests that the non-resonant background is responsible.

FIG. 4: The isovector \( \gamma_0^{p-n} - \gamma_0^{p+n} \) (top) and isoscalar \( \gamma_0^{p+n} + \gamma_0^{p-n} \) (bottom) generalized forward spin polarizabilities together with \( \chi PT \)-based calculations and the results from the MAID model. The proton and neutron data are respectively from CLAS 22 and Hall A 27.

**SUMMARY AND CONCLUSION**

The Bjorken integral was extracted from polarized proton and deuteron data for \( 0.054 < Q^2 < 2.92 \) GeV\(^2\). The results for intermediate \( Q^2 \) (the parton to hadron transition domain) are consistent with previous JLab data in which the neutron information was extracted from polarized \(^3\)He. This region exhibits a strong \( Q^2 \)-behavior, both from pQCD evolution and from some higher-twist effects. On the other hand, in the high-\( Q^2 \) domain the Bjorken integral is rather flat. The data together with kinematic constraints at \( Q^2 \rightarrow 0 \) also suggest a small \( Q^2 \)-dependence, in qualitative agreement with the generalized GDH sum predictions.

At the lowest \( Q^2 \) accessed by our data, \( \chi PT \) calculations agree better with the Bjorken integral (an isovector quantity in which the \( \Delta_{1232} \) resonance does not contribute) than with moments on individual nucleons. This is not trivial since the \( \chi PT \) calculations fail to describe the generalized spin polarizability \( \delta_{LT} \) in which the \( \Delta_{1232} \) is also suppressed.

Data on the generalized forward spin polarizability \( \gamma_0^{p-n} \) are not reproduced by the \( \chi PT \)-based calculations even though the \( \Delta_{1232} \) does not contribute.

It is clear from previously published data on \( \delta_{LT} \) and our analysis of \( \gamma_0 \) that the \( \Delta_{1232} \) resonance contribution is not responsible for the discrepancy between data and calculations. The discrepancy between the \( \chi PT \) calculations and the data occurs in all isospin channels, which makes it less likely that it is due to the contribution from heavier mesons in the chiral expansion.

The low \( Q^2 \) \( \chi PT \) regime has been recently mapped by two additional dedicated experiments in CLAS using polarized proton 49 and deuteron targets 20 and one in Hall A using polarized \(^3\)He 25. These experiments will provide further precision tests of \( \chi PT \) calculation techniques.

The moderate \( Q^2 \) data (1 to 3 GeV\(^2\)) allow us to extract higher twist contributions and color polarizabilities. The twist-4 coefficient was found to be large: \( f_2^{p-n} \approx -0.1 \) at \( Q^2 = 1 \) GeV\(^2\) (compare to \( \Gamma_1^{p-n} = 0.125 \), \( a_2^{p-n} = 0.031 \) and \( d_2^{p-n} = -0.007 \)). The uncertainty on \( f_2^{p-n} \) remains relatively large (\( \approx 70\% \)); however, we have completed several systematic studies both with the existing data as well as simulated data (with no statistic fluctuations) that indicate our result is stable. The sign and magnitude of \( f_2^{p-n} \) agree with a recent analysis performed on \( g_1 \) directly 50. The observation that higher twist effects on \( \Gamma_1^{p-n} \) are small overall does not imply that the net higher twist effect on the structure function \( g_1^{p-n} \) is small at any \( x \). It is important to study the \( x \)-dependence of the higher twists, as is done in Ref. 50. That \( |f_2| \) is significantly larger than \( d_2 \), and that \( f_2 < 0 \), agrees well with the prediction of the two-scale model 44. Overall the net effect of higher twists is small, because of a cancellation between the twist 4 and twist 6 terms that are of similar sizes but opposite signs. This trend has also been seen for higher twist analyses done on the unpolarized structure function \( F_2 \) 51. This can be interpreted within a vector dominance framework: the oscillating signs arise from the development in series of the vector meson propagator \( \propto 1/(Q^2 - M_m^2) \) where \( M_m \) is the meson mass.

This work is supported by the U.S. Department of Energy (DOE) and the U.S. National Science Foundation. The Jefferson Science Associates operate the Thomas Jef-
ferson National Accelerator Facility for the DOE under contract DE-AC05-84ER40150.

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