Formation of Solar system analogues II: post-gas phase growth and water accretion in extended discs via N-body simulations

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ABSTRACT
This work is the second part of a project that attempts to analyze the formation of Solar system analogues (SSAs) from the gaseous to the post-gas phase, in a self-consistently way. In the first paper (PI) we presented our model of planet formation during the gaseous phase which provided us with embryo distributions, planetesimal surface density, eccentricity and inclination profiles of SSAs, considering different planetesimal sizes and type I migration rates at the time the gas dissipates. In this second work we focus on the late accretion stage of SSAs using the results obtained in PI as initial conditions to carry out N-body simulations. One of our interests is to analyze the formation of rocky planets and their final water contents within the habitable zone. Our results show that the formation of potentially habitable planets (PHPs) seems to be a common process in this kind of scenarios. However, the efficiency in forming PHPs is directly related to the size of the planetesimals. The smaller the planetesimals, the greater the efficiency in forming PHPs. We also analyze the sensitivity of our results to scenarios with type I migration rates and gap-opening giants, finding that both phenomena act in a similar way. These effects seem to favor the formation of PHPs for small planetesimal scenarios and to be detrimental for scenarios formed from big planetesimals. Finally, another interesting result is that the formation of water-rich PHPs seems to be more common than the formation of dry PHPs.

Key words: planets and satellites: dynamical evolution and stability - planets and satellites: formation - methods: numerical

1 INTRODUCTION
During the past years, improvements in the exoplanet detection techniques and the increase in the quantity and quality of the missions, have led to the discovery of exoplanets of all kinds. To date, the number of confirmed exoplanets rises to 3798 and continues growing (http://exoplanet.eu/ Schneider et al. 2011). In particular, the number of rocky planets has grown the most during the last years, discovered mainly by the Kepler mission (https://www.nasa.gov/mission_pages/kepler). The number of gas giant exoplanets in orbits with semimajor-axis greater than ~1 au has also grown, and many of these rocky and gas giant planets are part of multiple planetary systems, 633 until now. Moreover, multiple planetary systems with more than one gas giant planet have also been detected. From this, many of these multiple planetary systems present a central star similar to our sun. However, to date, we have not yet been able to detect planetary systems similar to our own Solar system. This is, planetary systems formed simultaneously by at least a giant planet with a mass of the order of Saturn or Jupiter in the outer zones of the disc, and by rocky planets in the inner zone, particularly by rocky planets within the habitable zone.

Several works studied the formation of terrestrial planets and water accretion process in different dynamical scenarios or within the framework of the formation of our Solar system. For example, Raymond et al. (2004) and Raymond et al. (2006) analyzed the effects produced by a Jovian planet located in the outer zones of the disc on the formation and dynamics of terrestrial planets around sun.
like stars. Later, Mandell et al. (2007) explored the formation of terrestrial-type planets in planetary systems with one migrating gas giant around solar-type stars. They also considered planetary systems with one inner migrating gas giant and one outer non-migrating giant planet. Fogg & Nelson (2009) examined the effect of giant planet migration on the formation of inner terrestrial planet systems and found that this phenomena does not prevent terrestrial planet formation. Salvador Zain et al. (2017) focused on the formation and water delivery within the habitable zone in different dynamical environments and also around solar-type stars. These authors considered planetary systems that harbor Jupiter or Saturn analogues around the location of the snowline and found that the formation of water-rich planets within the habitable zones of those systems seems to be a common process. More recently Raymond & Izidoro (2017) showed that the inner Solar system’s water could be a result of the formation of the giant planets. These authors find that when the gas disc starts to dissipate, a population of scattered eccentric planetesimals cross the terrestrial planet region delivering water to the growing Earth.

During our first work (Ronco et al. 2017; hereafter PI) we improved our model of planet formation which calculates the evolution of a planetary system during the gaseous phase to find, via a population synthesis analysis, suitable scenarios and physical parameters of the disc to form Solar system analogues (SSAs from now on). We were specially interested in the planet distributions, and in the surface density, eccentricity and inclination profiles for the planetesimal population at the end of the gas-phase obtained considering different formation scenarios, with different planetesimal sizes and different type I migration rates.

The aim of this second work is to analyze the formation of SSAs during the post-gas phase through the development of N-body simulations, focusing on the formation of rocky planets and their water contents in the inner regions of the disc, particularly on the habitable zone. To do so, and in order to analyze the formation of SSAs in a self-consistently way, we make use of the results obtained in PI as the initial conditions for our N-body simulations and form final planetary systems from different planetesimal sizes. Many works in the literature that analyze the post-gas-phase formation of planetary systems, in particular the formation of rocky planets in the inner regions of the disc, considered arbitrary initial condition (Chambers 2001; Raymond et al. 2004, 2006; O’Brien et al. 2006; Mandell et al. 2007; Raymond et al. 2009; Walsh et al. 2011; Ronco & de Elía 2014). However, as it was already shown by Ronco et al. (2015), more realistic initial conditions, obtained from a model of planet formation, lead to different accretion histories of the planets that remain within the habitable zone than considering ad hoc initial conditions. We also analyze the differences in the results of planetary systems that were affected by the type I migration regime (Tanaka et al. 2002) during the gas-phase, and by planetary systems with gas giant planets that were able to open a gap in the disc and were affected by type II migration.

This work is then organized as follow. In Section 2, we summarize our model of planet formation explained in detailed in PI; in Section 3, we describe the initial conditions for the development of our N-body simulations, obtained from the results of PI; in Section 4, we describe the most important properties of the N-body code and then show our main results in Section 5. Then, we compare our results with the observed potentially habitable planets and with the current gas giant population in Section 6. Finally, discussions and conclusions are presented in Section 7 and Section 8, respectively.

### 2 SUMMARY OF THE GAS-PHASE PLANET FORMATION MODEL

In PI we improved a model of planet formation based on previous works (Guilera et al. 2010, 2011, 2014), which we now called PLANETALP. This code describes the formation and evolution in time of a planetary system during the gaseous phase, taking into account many relevant phenomena for the planetary system formation. The model presents a protoplanetary disc, which is characterized by a gaseous component, evolving due to an α-viscosity driven accretion (Pringle 1981) and photoevaporation (D’Angelo & Marzari 2012) processes, and a solid component represented by a planetesimal and an embryo population. The planetesimal population is being subject to accretion, ejection (Laakso et al. 2006) and scattering (Ida & Lin 2004; Alibert et al. 2005) by the embryos, and radial drift due to gas drag including the Epstein, Stokes and quadratic regimes. The embryo population grows by accretion of planetesimals (Inaba et al. 2001), gas (Ida & Lin 2004; Miguel et al. 2011; Mordasini et al. 2009; Tanigawa & Ikoma 2007), and due to the fusion between them taking into account their atmospheres (Inamdar & Schlichting 2015), while they migrate via type I (Tanaka et al. 2002) or type II (Crida et al. 2006) migration mechanisms. We also consider that the evolution of the eccentricities and inclinations of the planetesimals are due to two principal processes: the embryo gravitational excitation (Ohtsuki et al. 2002), and the damping due to the nebular gas drag (Rafikov 2004; Chambers 2008). The particularities and the detailed description of the implementation of each phenomena can be found in PI and in Guilera et al. (2014).

In PI we also described the method, initial parameters and initial formation scenarios considered to synthesize a population of different planetary systems around a solar-mass star, with the particular aim of forming SSAs. Following Andrews et al. (2010), the gas and solid surface density profiles are modeled as

\[
\Sigma_g(R) = \Sigma_0^g \left(\frac{R}{R_c}\right)^{-\gamma} e^{-\left(\frac{R}{R^*}\right)^{2\gamma}}, 
\]

\[
\Sigma_p(R) = \Sigma_0^p \eta_{\text{ice}} \left(\frac{R}{R_c}\right)^{-\gamma} e^{-\left(\frac{R}{R^*}\right)^{2\gamma}}, 
\]

where \(\Sigma_0^g\) and \(\Sigma_0^p\) are normalization constants, with \(\Sigma_0^g = 0.0153\) the primordial abundance of heavy elements in the sun (Lodders et al. 2009), and \(\eta_{\text{ice}}\) is a parameter that represents the increase in the amount of solid material due to the condensation of water beyond the snowline, given by 1 if \(R \geq R_{\text{ice}}\) and given by \(1/\beta\) if \(R < R_{\text{ice}}\), where \(R_{\text{ice}}\) is the position of the snowline at 2.7 au (Hayashi 1981).

The variable parameters, which were taken randomly from range values obtained from the same observational works (Andrews et al. 2010), are the mass of the disc, \(M_d\),...
between 0.01M⊙ and 0.15M⊙, the characteristic radius Rc between 20 au and 50 au, and the density profile gradient γ between 0.5 and 1.5. The factor β in the solid surface density profile is also taken randomly between 1.1 and 3. The viscosity parameter α for the disc and the rate of EUV ionizing photons fH2 have a uniform distribution in log between 10⁻⁴ and 10⁻², and between 10⁻⁴ and 10⁴, respectively (D’Angelo & Marzari 2012).

The formation scenarios considered include different planetesimal sizes (rₚ = 100 m, 1 km, 10 km and 100 km) but we consider a single size per simulation. The type I migration rates for isothermal-discs were slowed down in 1% (f_migI = 0.01) and 10% (f_migI = 0.1). We also considered the extreme cases in which type I migration was not taken into account (f_migI = 0) or was not slowed down at all (f_migI = 1).

We also constrained the disc lifetime τ, between 1 Myr and 12 Myr, following Pfalzner et al. (2014), and considering only those protoplanetary discs whose combinations between α and f_H2 satisfied this condition.

Finally, the random combinations of all the parameters gave rise to a great diversity of planetary systems which were analyzed in PI. From this diversity, only 4.3% of the total of the developed simulations formed planetary systems that, at the end of the gaseous phase were SSAs. Recalling from PI, we define SSAs as those planetary systems that present, at the end of the gaseous phase, only rocky planets in the inner region of the disc and at least one gas giant planet, like Jupiter or Saturn, beyond 1.5 au. The great majority of these SSAs were found in formation scenarios with small planetesimals and low/null type I migration rates. These SSAs presented different properties and architectures, for example, different number of gas giant planets and icy giant planets, and different final planetesimal profiles. Moreover, from a range of disc masses between 0.01M⊙ and 0.15M⊙, SSAs were formed only within discs more massive than M₅ ≥ 0.04M⊙ since low-mass discs have not enough solid material to form massive cores before the disc dissipation timescales. However, these SSAs were not sensitive to the different values of R_c, γ, β, α and τ, since we found them throughout the whole range of values considered for each of these parameters. The mean values for the disc parameters that formed SSAs were < M₅ > = 0.1M⊙, < R_c > = 32.8 au, < γ > = 0.95, < β > = 2.07, < α > = 3.4 × 10⁻⁵ and < τ > = 6.45 Myr.

It is important to remark that the planetary systems obtained at the end of the gaseous phase and which are going to be considered as initial conditions for the post-gas growth, were formed within the framework of a planetary formation code that, although presents important physical phenomena for the formation of a planetary system during the gaseous phase, it also presents certain limitations. Some of these limitations are, for example, the use of a radial 1D model to compute the evolution of a classical α-disc, the consideration of isothermal discs and the corresponding type I migration rates for such discs, and the lack of the calculation of the gravitational interactions between embryos. Then, the initial conditions for the N-body simulations carried out in this work are dependent on the physics of our planetary formation model and more detailed treatments of the physics could affect the final embryo and planetesimal configurations of planetary systems at the end of the gaseous phase. For example, recent works which consider non-isothermal discs have shown that type I migration rates could be very different with respect to previous isothermal type I migration rates (Paardekooper et al. 2010, 2011). Moreover, for non-isothermal discs, migration convergent zones are generated, acting as traps for migrating planets (Hellary & Nelson 2012; Bitsch et al. 2015). On the other hand, the presence of a dead zone along the disc could also affect both, the planet migration and the planetesimal radial drifts. Guilera & Szandor (2017) showed that even in isothermal discs, the presence of a dead zone in the disc leads to pressure maxima at the edges of such zones acting as traps for migrating planets and also as convergent zones for drifting planetesimals. Finally, alternative models for α-discs, as wind-discs, have been proposed to model the evolution of the gaseous component of protoplanetary discs, showing different final disc structures (Suzuki et al. 2010, 2016). These differences are important and could affect models of planetesimal formation and planet migration.

### 3 INITIAL CONDITIONS

The goal of this second work is to study and analyze the evolution of the post-gas phase of planetary systems that resulted in SSAs at the end of the gaseous phase. From this, Fig. 8 of PI showed some of the embryo and planetesimal distributions of the different scenarios of SSAs at the end of the gaseous phase.

Some of the final configurations obtained after the gas is completely dissipated are used in this work as initial conditions to develop N-body simulations. Since one of our main goals is to analyze the formation of rocky planets within the habitable zone (HZ) of SSAs, we focus on the long-term evolution of planetary systems between 0.5 au and 30 au. We are not interested in the formation of close-in planets very near the central star. Thus, we do not consider planetary embryos neither planetesimals inside 0.5 au.

Table 1 and Fig. 1 show the main properties of the chosen outcomes of the results of PI that are going to be used to analyze the late-accretion stage. Due to the high computational cost of N-body simulations of this kind it is not viable to develop simulations for each SSA found. Thus we have to choose the most representative one for each formation scenario. Therefore, the chosen outcomes shown in Fig. 1, that represent the embryo distributions and the planetesimal surface density profiles of SSAs at the end of the gaseous phase, were carefully selected from each formation scenario, this is taking into account the different planetesimal sizes and different type I migration rates, considering that it was the most representative of the whole group.

As it was explained in PI, a water radial distribution for the embryos and planetesimals was included in our model of planet formation. The colorscale in Fig. 1 shows the water contents in embryos at the end of the gaseous phase. As the fraction per unit mass of water in embryos and planetesimals, at the beginning of the gaseous phase, was given by

\[
 f_{H_2O}(R) = \begin{cases} 
 0, & \text{if } R \leq R_{ice} \\
 \frac{\beta - 1}{\beta}, & \text{if } R > R_{ice} 
 \end{cases}
\]  

(3)
the water contents in embryos at the end of the gaseous phase, which represent the initial water contents for the post-gas phase evolution, vary, on the one hand according to the \( \beta \) value considered for each scenario, and on the other hand due to the growth of each embryo during the gas phase. As we mentioned before, \( \beta \) takes random values from 1.1 (which represents a 9% of water by mass) to 3 (which represents a 66% of water by mass). The planetesimal population remains always the same regarding water contents: planetesimals inside 2.7 au remain dry and planetesimals beyond 2.7 au contain the amount of water by mass given by Eq. 3. As we already mentioned, the last four columns of Table 1 show the main properties related to water contents in each formation scenario considered to develop N-body simulations.

It is important to note that, at the end of the gaseous phase, we are able to distinguish which is the origin of the water content of each planet. This is, we can know the percentage of water by mass at the end of the gaseous phase due to the accretion of planetesimals and the percentage of water by mass due to the fusion between embryos.

An interesting difference between some of the formation scenarios considered, is that due to the position of the formed giant planets during the gaseous phase, not all the SSAs present a water-rich embryo population inside the giant locations. This topic will play an important role in the analysis of the water contents in planets within the HZ at the end of the N-body simulations, and it will be attended in the following sections.

![Figure 1](image_url)

**Figure 1.** Chosen SSAs configurations at the end of the gaseous phase, to develop N-body simulations in a mass vs. semimajor-axis vs planetesimal surface density plane. Each colored point represents a planetary embryo, the black and grey big dots represent Jupiter and Saturn analogues, respectively, while the colored points with black borders represent icy giants, like Neptune-like planets. The solid black line in all the planetary systems represents the planetesimal density profile when the gas is already gone. The colorscale represents the final amounts of water by mass in each planet and the size of each planet is represented in logarithmic scale.
4 PROPERTIES OF THE N-BODY SIMULATIONS

Our N-body simulations begin when the gas is already dissipated in the protoplanetary disc. The numerical code used to carry out our N-body simulations is the MERCURY code developed by Chambers (1999). In particular, we adopted the hybrid integrator, which uses a second-order mixed variable symplectic algorithm for the treatment of the interaction between objects with separations greater than 3 Hill radii, and a Burlisch-Stoer method for resolving closer encounters.

The MERCURY code calculates the orbits of gas giants, planetary embryos and planetesimals. When these orbits cross each other, close encounters and collisions between the bodies may occur and are registered by the MERCURY code. It is important to mention that in our simulations, collisions between all the bodies are treated as inelastic mergers, which conserve mass and water content and because of that our model does not consider water loss during impacts. As a consequence, the final mass and water contents of the resulting planets should be considered as upper limits.

Given the high numerical cost of the N-body simulations and in order to perform them in a viable CPU time, we only consider gravitational between planets (embryos and giant planets), and between planets and planetesimals, but planetesimals are not self-interacting. This is, planetesimals perturb and interact with embryos and giant planets but they ignore one another completely and they cannot collide with each other (Raymond et al. 2006). It is important to remark that these planetesimals are in fact superplanetesimals. While the size of the planetesimals is only relevant during the gas phase when planetesimals interact with the gaseous component of the disc due to the drift of the nebular gas (see PI), the size ceases to be relevant in the post-gas phase during the N-body simulations. Thus, due to the numerical limitations of N-body simulations regarding the limited number of bodies that has to be used, it is not possible to consider, in a consistently way, realistic planetesimals of the proposed sizes in PI, this is planetesimals of 100 m, 1 km, 10 km and 100 km. Instead, we have to consider higher mass superplanetesimals that represent an idealized swarm of a larger number of real size planetesimals. Thus, from now on when we speak about planetesimals we are referring to superplanetesimals.

As we already mentioned, we are interested in the post-gas evolution of planetary systems similar to our own, and this is why we consider planetary embryos and planetesimals, in extended discs, between 0.5 au and 30 au. The number of embryos varies between 40 and 90 according to each scenario and present physical densities of 3 gr cm$^{-3}$. We consider 1000 planetesimals in all the developed simulations with physical densities of 1.5 gr cm$^{-3}$. Since the remaining mass in planetesimals, at the end of the gaseous phase, in simulations with planetesimals of 100 km and type I migration rates reduced to a 0.1% are too high, we cut the disc until 15 au in order to be able to consider 1000 planetesimals. The choice of considering only 1000 planetesimals, all with the same mass for each scenario, has to do with the fact that considering more planetesimals would be unviable taking into account the time needed to run these simulations, and since this is a number that will allow us to study in a moderately detailed way the evolution of this population throughout the whole disc.

Since terrestrial planets in our Solar system may have formed within 100 Myr - 200 Myr (Touboul et al. 2007; Dauphas & Pourmand 2011; Jacobson et al. 2014), we integrate each simulation for 200 Myr. To compute the inner orbit with enough precision, we use a maximum time step of six days which is shorter than 1/20 th of the orbital period of the innermost body in all the simulations. The reliability of all our simulations is evaluated taking into account the criterion of energy $|dE/E| < E_d$, where $E_d$ is an energy threshold and it is considered as $10^{-3}$. However, in order to conserve the energy to at least one part in $10^3$, we carry out simulations assuming shorter time steps of four and up to two days, depending on the requirement of each simulation. Those simulations that do not meet this energy threshold value are directly discarded.

To avoid any numerical error for small-perihelion orbits, we use a non-realistic size for the sun radius of 0.1 au (Raymond et al. 2009). The ejection distance considered in all our simulations was 1000 au. This value is realistic enough for the study of extended planetary systems and is also a value that allows us to reduce the total number of bodies of our simulations as time passes. Higuchi et al. (2007) found that planetesimals with semimajor-axis > 1000 au increase their perihelion distances outside the planetary region (100 au) due to the fact that they would already be affected by galactic tides. In addition, Versas & Evans (2013) showed that wide-orbit planets with semimajor-axis greater than 1000 au are substantially affected by galactic tides while closer-in planets, at ~ 100 au, are only affected if the host star is near the galactic center, within the inner hundred parsecs.

The semimajor-axes of the planetesimals are generated using an acceptance-rejection method taking into account the surface density profile of planetesimals shown with black curves in each formation scenario of Fig. 1. As it was explained before, the orbital eccentricities and inclinations for the planetesimal population are results of the gas-phase evolution (see PI). Each planetesimal surface density profile has an eccentricity and inclination profile that are also used as initial conditions for this population. Figure 2 shows the eccentricity profile (black curve) of the planetesimal surface density profile (red curve) of the results of $\delta_8$, as an example. For embryos and giant planets, the initial eccentricities and inclinations are taken randomly considering values lower than 0.02 and 0.5$^\circ$, respectively. Recalling from PI, embryos and giant planets evolve in circular and coplanar orbits during the gaseous phase. Thus, to be consistent with our model of planet formation we initiate the N-body simulations with low values for the eccentricities and inclinations. It is worth mentioning that the model developed in PI does not yet consider the gravitational self-stirring of embryos and giant planets. Therefore, this limitation in our model could change the configurations of our SSAs at the end of the gaseous stage.

The rest of the orbital parameters, such as the argument of pericenter $\omega$, longitude of ascending node $\Omega$, and the mean anomaly $M$ are also taken randomly between 0$^\circ$ and 360$^\circ$ for the gas giants, the embryos and the planetesimals.

Due to the stochastic nature of the accretion process,
we perform 10 simulations with different random number seeds per each formation scenario (see Table 1).

5 RESULTS

In this section we describe the main results of our N-body simulations for the formation of planetary systems from SSAs configurations. It is worth remembering that the considered architecture of a SSA consists on a planetary system with rocky planets in the inner region of the disc and at least one giant planet, a Jupiter or Saturn analogue, beyond 1.5 au. The main goal of our work is to study the formation process of the whole system, focusing on the formation of rocky planets and the water delivery within the HZ. As we have developed a great number of N-body simulations taking into account different planetesimal sizes and different migration rates, and in order to show our results in an organized way, we first describe the results of scenarios formed from planetesimals of 100 km, 10 km, 1 km and 100 m that did not undergo type I migration and that present gas giants that had not managed to open a gap during the gas phase, as the reference scenarios.

The sensitivity of the results to different type I migration rates and to giant planets that open a gap in the gas disc, are going to be exposed in the subsequent sections.

5.1 The habitable zone

One of the goals of this work is to analyze the formation of rocky planets within the HZ and their final water contents. The HZ was first defined by Kasting et al. (1993) as the circumstellar region inside where a planet can retain liquid water on its surface. For a solar-mass star this region remains between 0.8 au and 1.5 au (Kasting et al. 1993; Selsis et al. 2007). Later, and particularly for the Solar system, Kopparapu et al. (2013a,b) proposed that an optimistic HZ is set between 0.75 au and 1.77 au. These limits were estimated based on the belief that Venus has not had liquid water on its surface for the last 1 billion years, and that Mars was warm enough to maintain liquid water on its surface. The authors also defined a conservative HZ determined by loss of water and by the maximum greenhouse effect provided by a CO2 atmosphere, between 0.99 au and 1.67 au. However, locating a planet within these regions does not guarantee the potential habitability, taking into account that if the orbits of planets found inside these regions are too eccentric, they could be most of the time outside them, and this could avoid long times of permanent liquid water on their surfaces. In order to prevent this situation, in previous works that also analyze the formation of rocky planets within the HZ, we considered that a planet is in the HZ and can hold liquid water if it has a perihelion $q \leq 0.8$ au and an aphelion $Q \leq 1.5$ au (Ronco & de Elía 2014), or has conservative or optimistic chances to be habitable if it has a perihelion $q \geq 0.75$ au and an aphelion $Q \leq 1.77$ au, and if it has a perihelion $q \geq 0.99$ au and a aphelion $Q \leq 1.67$ au, respectively (Ronco et al. 2015).

Williams & Pollard (2002) showed that the planetary habitability would not be compromised if the planet does not stay within the HZ during all the integration. If an ocean is present to act as a heat capacitor, or the atmosphere protects the planet from seasonal changes, it is primarily the time-averaged flux that affects the habitability over eccentric orbits. In this sense, Williams & Pollard (2002) determined that the mean flux approximation could be valid for all eccentricities. However, Bolmont et al. (2016) explored the limits of the mean flux approximation varying the luminosity of the central star and the eccentricity of the planet, and found that planets orbiting a 1 $\oplus$ star with eccentricities higher than 0.6 would not be able to maintain liquid water throughout the orbit.

Kopparapu et al. (2014) improved the analysis of the HZ boundaries founding a dependence between the limits of the HZ with the masses of the planets. Assuming H2O (inner HZ) and CO2 (outer HZ) atmospheres, their results indicated that larger planets have wider HZs than smaller ones. Particularly, Kopparapu et al. (2014) provided with parametric equations to calculate the corresponding HZ boundaries of planets of 0.1 $M_{\oplus}$, 1 $M_{\oplus}$ and 5 $M_{\oplus}$. They determined that for a $1 L_{\odot}$, the inner conservative boundary of a planet of 0.1 $M_{\oplus}$ is 1.005 au, for a planet of 1 $M_{\oplus}$ is 0.95 au, and for a planet of 5 $M_{\oplus}$ is 0.917 au, while the outer limits remain the same for the three of them and is 1.67 au.

In this work, on the one hand we consider that those planets with masses lower than 0.1 $M_{\oplus}$ present the same inner HZ boundary of a planet of 0.1 $M_{\oplus}$, planets with masses between 0.1 $M_{\oplus}$ and 1 $M_{\oplus}$ present the same inner HZ boundaries of a planet of 1 $M_{\oplus}$, and planets with masses between 1 $M_{\oplus}$ and 5 $M_{\oplus}$ present the same inner HZ boundaries of a planet of 5 $M_{\oplus}$. Planets with masses greater than 5 $M_{\oplus}$ also present the inner HZ boundaries of a planet of 5 $M_{\oplus}$.

On the other hand, we also calculate the time-averaged incident stellar flux for the inner and outer HZ limits of an eccentric planet, in terms of the solar flux following

$$F_{* \text{eff}}^* = \frac{F_{* \text{eff}}}{(1 - e^2)^{1/2}}.$$ 

Figure 2. Eccentricity profile (black curve) for the planetesimal surface density profile (red curve) of the end of the gas-phase evolution of scenario $S_8$ of Fig. 1. The oscillations in the eccentricity profiles of planetesimals are caused, during the gaseous phase (see PI), by the embryo gravitational excitation (Ohtsuki et al. 2002) and by the damping due to the nebular gas drag (Radzievsky 2004; Chambers 2008). The zoom shows some planetesimals in black points. All of them, the 1000 planetesimals, represent the mass in planetesimals available between 0.5 au and 30 au, located on top of the eccentricity profile.
where $F_{\text{eff}}$ is the effective flux from a circular orbit. Then, following Williams & Pollard (2002) we can draw constant flux curves in the semimajor-axis vs eccentricity plane for the HZ boundaries.

Therefore, given the previous mentioned works and our considerations, the adopted criteria for the definition of the HZ and the class of potentially habitable planets, PHPs from now on, is as follows:

(i) If a planet presents, at the end of the N-body simulations, a semimajor-axis between its HZ boundaries, and has a perihelion $q$ greater, and an aphelion $Q$ lower than the limit values for their HZ boundaries, we consider this planet is a PHP class A.

(ii) If a planet presents a $(a, e)$ pair that remains inside the constant flux curves associated to the inner and outer HZ edges, and has an eccentricity lower or equal than 0.6, we consider this planet is a PHP class B.

(iii) Finally, if a planet remains within a 10% of the inner or the outer constant flux curve, and has an eccentricity lower or equal than 0.6, we consider this planet is a PHP class C.

Although planets of the three classes will be considered as PHPs, the most important ones, taking into account the inner and outer HZ boundaries and the mean flux boundaries are those of class A and B. Planets of class C, for being in a region that extends in a 10% on both sides of each boundary, are considered as marginally habitable but PHPs at last. Figure 3 shows, as an example, the different HZ regions for a planet of $5M_\oplus$. These regions are reduced if we consider less massive planets since larger planets have wider HZs than smaller ones.

Regarding final water contents, we consider that to be a PHP of real interest, a planet has to harbor at least some water content, better if this content is of the order of the estimations of water on Earth. The mass of water on the Earth surface is around $2.8 \times 10^{-4}M_\oplus$, which is defined as 1 Earth ocean. However, as the actual mass of water in the mantle is still uncertain, the total mass of water on the Earth is not yet very well known. However, Lécuyer & Gillet (1998) estimated that the mantle water is between $0.8 \times 10^{-4}M_\oplus$ and $8 \times 10^{-4}M_\oplus$, and Marty (2012) estimated a value of $2 \times 10^{-3}M_\oplus$. Thus, taking into account the water reservoirs that should be in the Earth’s mantle and the mass of water on the surface, the present-day water content on Earth should be around 0.1% to 0.2% by mass, which represents between 3.6 to 7.1 Earth oceans. Moreover, Abe et al. (2000) suggested that the primitive mantle of the Earth could have contained between 10 and 50 Earth oceans. However, other authors assumed that the current content is not very different from the one that was accreted during the formation process (see Raymond et al. 2004, and references therein). Although to be a PHP of real interest the planet has to present at least some water content, we do not consider a minimum for this value since we could not ensure the potential non-habitability for lower values.

5.2 Description of the reference scenarios

Here we describe the most important characteristics of the four reference scenarios: planetary systems formed from planetesimals of 100 km, 10 km, 1 km and 100 m and without suffering migration regimes during the gaseous phase.

5.2.1 Scenarios with planetesimals of 100 km

Main perturber: A gas giant planet similar to a Saturn-like\(^1\) planet acts as the main perturber of the systems. This giant is initially located at 2.97 au and then migrates inward due to an embryo-driven migration until it ends up located between 1.57 au and 1.97 au at the end of the evolution, with a mass ranging between 171.4$M_\oplus$ and 190$M_\oplus$ (this is $1.8M_\oplus$ and $2M_\oplus$) taking into account the whole group of simulations.

General dynamical evolution: The dynamical evolution of all the simulations performed with planetesimals of 100 km is very similar. Figure 4 six snapshots in time of the semimajor-axis eccentricity plane of SIM4 as an example of the whole group. The initial conditions correspond to $S_4$ in Fig. 1. From the very beginning, the inner embryo population, which does not coexist with planetesimals, gets high eccentricities due to their own mutual gravitational perturbations and particularly with the giant planet. The planetary embryos evolved through collisions with planetesimals and other embryos. Particularly, the collisional events between the inner embryos happened within the first million year of evolution where, at that time, only one planet remains in the inner zone of the disc.

Mass remotion: Between a 30% and a 40% of the initial embryos, and between a 6% and a 14% of the initial planetesimals survive at the end of the simulations. Considering mean values for all the simulations, a 2.76% of the initial embryos collide with the central star while a 24.7% is accreted, and a 39% of is ejected from the systems. The

\(^1\) From PI we remember that our consideration of a Saturn-like planet is a giant planet with an envelope that is greater than the mass of the core but its total mass is less than 200$M_\oplus$. 

Figure 3. Habitable zone class A, B and C for a planet of $5M_\oplus$. 

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Figure 4. Time evolution of SIM$_4$ of the scenario with planetesimals of 100 km and without considering type I migration. The shaded areas represent the HZ regions already described in Section 1. From now on, all the HZ regions plotted are the widest possible, which correspond to a planet of 5M$_{\oplus}$. Planets are plotted as colored circles, planetesimals are plotted with black dots and the giant planet, which is a Saturn-like planet in this case, is represented in grey. The size of the Saturn-like planet is fixed and is not in the same scale for the rest of the planets. The same happens with the planetesimal population, each planetesimal adopts a size of half the size of the smallest embryo, independently of its mass. Then, the size for the rest of the planets is represented by a linear relation between the mass and the size, where the size for the smallest embryo is the double of the size of the planetesimals, and the size of the biggest planet is smaller that the size for the Saturn-like planet. The color scale represents the fraction of water of the planets with respect to their total masses. This scenario always presents a Mega-Earth in the inner region per simulation. Half of them are completely dry as it can be seen in this case. This scenario does not form PHPs within the HZ.

rest of them remains in the inner zone$^2$ as a Mega-Earth$^3$ and in the outer zones of the disc coexisting simultaneously

$^2$ From now on, when we talk about planets or planetesimals from the inner zone, we are referring to those planets or planetesimals that are located inside the giants location at the beginning of the N-body simulations. Similarly, planets or planetesimals from the outer zone are those planets or planetesimals that are located beyond the giants location at the beginning of the N-body simulations.

$^3$ We classify the formed rocky planets as Mega-Earths if they present masses between 8M$_{\oplus}$ and 30M$_{\oplus}$, Super-Earths if they present masses between 2M$_{\oplus}$ and 8M$_{\oplus}$ and Earth-like planets if their masses are lower than 2M$_{\oplus}$ and greater than half an Earth. with a planetesimal population. The planetesimals suffer a similar process. They are located behind the giant and are perturbed by the giant and the surrounding planets. Considering all the simulations, the great majority (~ 84.3%) are ejected from the systems and only a few collide with the central star (3.1%) or are accreted (2.5%) by the surrounding planets. Following these results, the accretion of planetesimals is an inefficient process in this scenario. The rest of the planetesimals (~ 10%) presents high eccentricities at the end of the evolution suggesting that if we extended the simulations by a few million years more, this population would probably end up being completely ejected from the systems.
**Inner region:** Inside the final location of the giant we always find a Mega-Earth with final mass in a range of $14.5 M_{\oplus}$ to $26 M_{\oplus}$, located between 0.37 au and 0.79 au. The seeds of these Mega-Earths where initially located always inside the snowline between 0.56 au and 2.37 au, with an initial mass between $1.70 M_{\oplus}$ and $6.76 M_{\oplus}$. During the evolution of the systems, these seeds also migrated inwards finally settling between 0.37 au and 0.79 au. Half of these Mega-Earths are completely dry at the end of the evolution. The other half present amounts of water by mass due to the accretion of very few water-rich planetesimals. However, none of them lie within the HZ. This is why this scenario is not interesting from an astrobiological point of view, the efficiency in forming PHPs is completely null.

**Outer region:** Beyond the giant, a mixture of dry and water-rich planets, and a planetesimal population with high mean eccentricities can be found until $\sim$ 400 au. This mix of material was found in all the developed simulations and the average number of dry planets found in the outermost regions is $\sim$ 4. The gravitational interactions between the gas giant and the embryo population cause that some of the internal embryos are injected into the outer zones of the disc, however no water-rich embryos from beyond the snowline are injected in the inner regions.

Finally, after 200 Myr of evolution, the planetary systems resulting from $S_{G}$ in figure 1 are composed by a dry Mega-Earth at around 0.55 au in half of the cases, a Saturn-like planet near or in the outer edge of the HZ, and of several planets beyond the giant planet.

### 5.2.2 Scenarios with planetesimals of 10 km

**Main perturbers:** In these systems two Jupiter-like planets with masses of $0.79 M_{J}$ and $0.64 M_{J}$, and initially located at 3.73 au and 5.88 au, respectively, act as the main perturbers. After 200 Myr of evolution the innermost giant is located at around 2.85 au and the outermost giant is located at around 5.78 au.

**General dynamical evolution:** From the begining, the inner embryos are quickly excited by the two Jupiter-like gravitational perturbations and by the perturbations with each other. The planetesimal population, which remains behind the gas giants, is also perturbed. However, very few planetesimals are able to cross the giant barrier. Therefore, inner planetary embryos grow almost only by the accretion of other embryos within the first Myr of evolution. As an example of this scenario figure 5 shows six snapshots in time of the semimajor-axis eccentricity plane of $S_{G}$.

**Mass remotion:** During the evolution of the systems a $\sim$ 8% of the initial embryo population collides with the central star, a 19.8% is accreted, and a $\sim$ 37.7% is ejected from the system, considering the whole group of simulations. The planetesimals are mostly ejected from the systems ($\sim$ 77.1%) due to the interactions with the giants and the outer planets. Only a few collide with the central star (1.7%) or are accreted (1.3%) by the surrounding planets. In this scenario, as in the previous one, the planetesimal accretion is also a very inefficient process along the entire length of the disc.

**Inner region:** Inside the orbit of the giant planets we find between 1 and 2 planets. Considering the 10 developed simulations the trend shows that is more likely to find 2 planets instead of 1. These planets are completely dry Super-Earths or dry Mega-Earths with masses in a range of $3.56 M_{\oplus}$ to $15.96 M_{\oplus}$. However, the trend is to find planets more massive than $10 M_{\oplus}$. In this scenario, 5 of 10 simulations formed one PHP. Although most of them are class A, all of them are completely dry because their accretion seeds come from the region inside the snowline. Their masses range between $3.56 M_{\oplus}$ and $11.57 M_{\oplus}$. The properties of these PHPs can be seen in table 2.

**Outer region:** Beyond the gas giants, planets and planetesimals survived until 400 au - 500 au. In these systems, the mix of material is less efficient than for planetesimals of 100 km. We only find one dry planet in the outer zone, beyond the giants, in half of the simulations.

- It seems that the gravitational interactions between the gas giants and the embryos in this case are stronger than with planetesimals of 100 km and instead of injecting dry embryos into the outer zone, they directly eject them out of the system.

Finally, at the end of the evolution, the planetary systems resulting from $S_{G}$ in figure 1 are formed mostly by two dry Super or Mega-Earths, two Jupiter-like planets between $\sim$ 2.85 au and 5.78 au, and by several planets beyond these giants. In 5 of 10 simulations we find a dry PHP.

### 5.2.3 Scenarios with planetesimals of 1 km

**Main perturbers:** A Saturn-like planet and a Jupiter-like planet act as the main perturbers of these systems. The Saturn-like planet is the gas giant which is closer to the central star and is initially located at 4 au. This planet finishes located between 1.68 au and 2.97 au due to an embryo-driven migration after 200 Myr of evolution and presents a mean mass of $46 M_{\oplus}$ (0.48M$\oplus$). This inward migration is significant but it is not enough to disperse all the solid material of the inner zone of the disc as it does, for example, the Saturn-like planet of the scenario of 100km. The Jupiter-like planet, originally located at 5.67 au, finishes always located around $\sim$ 4.6 au with a mass of $1.6 M_{J}$.

- **Icy giants:** Unlike the previous scenarios, this one presents two Neptune-like planets between the rocky em-

| SIM    | $a_{i}$ [au] | $a_{f}$ [au] | Mass [M$_{\oplus}$] | W [%] | Habitable class |
|--------|--------------|--------------|---------------------|-------|-----------------|
| SIM1   | 1.85         | 1.30         | 10.80               | 0     | A               |
| SIM2   | -            | -            | -                   | -     | -               |
| SIM3   | -            | -            | -                   | -     | -               |
| SIM4   | 1.22         | 1.01         | 14.41               | 0     | B               |
| SIM5   | -            | -            | -                   | -     | -               |
| SIM6   | -            | -            | -                   | -     | -               |
| SIM7   | -            | -            | -                   | -     | -               |
| SIM8   | 1.99         | 1.17         | 6.86                | 0     | A               |
| SIM9   | 2.15         | 1.45         | 11.57               | 0     | A               |
| SIM10  | 0.57         | 0.94         | 3.56                | 0     | C               |

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4 From PI, the adopted definition for an icy giant planet is that of a planet which presents a mass of the envelope greater than 1% of the total mass, but lower than the mass of the core. Particularly, if
Figure 5. Time evolution of a simulation of the scenario with planetesimals of 10 km and without considering type I migration. The shaded areas represent the HZ regions already described in Section 1. Planets are plotted as colored circles, planetesimals are plotted with black dots and the giant planets, which are Jupiter-like planets in this case, are represented in black. The size of the Jupiter-like planets is fixed and is not in the same scale for the rest of the planets. The same happens with the planetesimal population, each planetesimal adopts a size of half the size of the smallest embryo, independently of its mass. Then, the size for the rest of the planets is represented by a linear relation between the mass and the size, where the size for the smallest embryo is the double of the size of the planetesimals, and the size of the biggest planet is smaller that the size for a Saturn-like planet, like in the previous scenario.

The color scale represents the fraction of water of the planets with respect to their total masses. This scenario form dry PHPs within the HZ.

bryos and the gas giant planets, at the beginning of the simulations (see S3 in Fig. 1) with masses of $\sim 15M_\oplus$ and $\sim 17M_\oplus$.

**General dynamical evolution:** From the beginning, the embryos are excited due to the mutual perturbations between them and with both, the icy and the gas giants. The first most common result, found in 6 of 10 simulations, is that one of the two Neptunes is ejected from the systems within the first $\sim 0.1$ Myr. The second most common result, which happens in 5 of the 6 simulations mentioned before, is that the other Neptune is scattered towards the outer zone of the disc presenting encounters with an excited planetesimal population. Here it can be seen the importance of the dynamical friction produced by the planetesimals that dampens the eccentricity and inclination of the Neptune-like planet. The mass available in planetesimals to produce this effect is, during this process, high enough to cause the planet to settle in the mid-plane of the disc in less than $\sim 1$ Myr. We can see in figure 6 six snapshots in time of the semimajor-axis eccentricity plane of SIM10 as an example of this scenario. Although is not the most common result, we find that in 3 of the 10 simulations one of the Neptune-like planets survives inside the giants locations and finishes within the HZ while the other one is ejected.

**Mass remotion:** During the simulations, a 15.8% of
Table 3. Principal properties of the planets that remain within the HZ in scenarios with planetesimals of 1 km and without type I migration. The planets with * are the Neptune-like planets. The row in bold corresponds to the results of Fig. 6.

| SIM  | $a_i$ [au] | $a_f$ [au] | Mass [M$_{\oplus}$] | W [%] | Habitable class |
|------|------------|------------|---------------------|-------|----------------|
| SIM$_1$ | —         | —         | —                   | —     | —              |
| SIM$_2$ | —         | —         | —                   | —     | —              |
| SIM$_3$ | 2.92      | 1.39      | 15.37*              | 39.10 | A              |
| SIM$_4$ | 3.43      | 1.14      | 17.32*              | 38.91 | A              |
| SIM$_5$ | —         | —         | —                   | —     | —              |
| SIM$_6$ | —         | —         | —                   | —     | —              |
| SIM$_7$ | 1.07      | 0.97      | 2.55                | 0     | B              |
| SIM$_8$ | —         | —         | —                   | —     | —              |
| SIM$_9$ | —         | —         | —                   | —     | —              |
| SIM$_{10}$ | 3.43 | 1.41      | 17.32*              | 38.91 | A              |

the initial embryo population collides with the central star, a 12.7% is accreted, and a 46.73% is ejected from the system. Only between 1 and 2 planets remain inside the giants, the rest of them are located beyond them. The planetesimals, perturbed by the giants and outermost planets, are mainly ejected from the system (~ 84.4%). Only a few collide with the central star (0.6%) or are accreted (0.8%) by the surrounding planets. Only a ~ 14.0% of the initial planetesimals survives at the end of the simulations with semimajor-axis almost greater than 20 au and mean high eccentricities. Here again, the planetesimal accretion is an inefficient process, above all, in the inner region of the disc, since no planet originally located in the inner zone has succeeded in accreting planetesimals coming from beyond the giants.

**Inner region:** The inner zone of the disc in general presents one or two planets. The trend shows that is more likely to find one, which in almost all the cases is a Super-Earth. However, in 3 of the 10 simulations one of inner planets is a Neptune-like planet. With the exception of the Neptune-like planets, the inner planets are completely dry and present masses in a range between 1.1M$_{\oplus}$ and 6.18M$_{\oplus}$.

In general, this scenario achieved to form one PHP in 4 of 10 simulations but, as we mentioned before, 3 of that 4 PHPs are Neptune-like planets, which present high water contents. The other PHP is a dry Super-Earth of 2.55M$_{\oplus}$. The properties of these PHPs can be seen in table 3.

**Outer region:** Beyond the giants, there is a planet and a planetesimal population until ~ 400 au. In most of the simulations the planets in this outer region of the disc are water-rich planets, and we do not see planets from the inner zone. Moreover, in most of the cases, one of these planets is one of the Neptune-like planets, originally located between 2.6 au and 2.9 au.

Finally, at the end of the simulations, the planetary systems resulting from $S_4$ in figure 1 are formed by one or two inner planets which are dry Super-Earths or water-rich Neptune-like planets. A Saturn-like is followed by a Jupiter-like planet, and other several planets and planetesimals are beyond them. We find PHPs in 4 of 10 simulations. One of them is a dry Super-Earth and the other 3 are Neptune-like planets that were not scattered. The common result regarding these Neptunes in the HZ, is that they did not suffer collisions either from embryos or from planetesimals, reason why they could have conserved their primordial envelopes during all the evolution. Thus, although their final locations define them as PHPs, it is, in fact, very likely that they are not. Therefore, this scenario is not really interesting.

### 5.2.4 Scenarios with planetesimals of 100 m

**Main perturbers:** These simulations present two Jupiter-like planets of 1.49M$_J$ and 5M$_J$, located at around ~ 9.9 au and ~ 19.3 au during all the evolution, respectively, as the main perturbers of the system.

- **Icy giants:** Two Neptune-like planets of ~ 13M$_{\oplus}$ and ~ 15M$_{\oplus}$ are located between the inner embryo distribution and the Jupiter analogues, at 6.82 au and at 7.80 au, respectively, at the beginning of the simulations (see $S_1$ in Fig. 1).

**General dynamical evolution:** As from the beginning, the inner embryos get excited very quickly acquiring very high eccentricities. This causes that the orbits of these objects cross each other, leading to accretion collisions, ejections and collisions with the central star.

- From the beginning, these collisions may occur between dry and water-rich embryos since these two different populations are not separated by a big perturber as in the previous scenarios.

The fate of the Neptune-like planets is always the same. The trend shows that one of them is ejected from the system within the first million year of evolution, while the other one, which in most of the cases the inner Neptune, stays in the inner zone. The most common result among the simulations is that this Neptune-like planet do not suffer collisions of any kind. Thus, it could retain its primitive atmosphere. We show in Fig. 7 six snapshots in time of the evolution of SIM$_{10}$, as an example of this scenario. The initial conditions correspond to $S_1$ in Fig. 1. Although in these scenarios the planetesimal population resides in the inner zone of the disc, they are initially located between 5 au and 7 au, just beyond one of the Neptunes. Thus, this population does not directly interact with the inner embryo population between 0.5 au and 4 au.

**Inner region:** The inner region of the disc presents between 2 and 3 planets and in all the simulations one of these inner planet is one of the Neptune-like planets. The others are dry or water-rich Earths, Super-Earths or Mega-Earths with masses in a range between 1.02M$_{\oplus}$ and 9.10M$_{\oplus}$.

- This scenario forms 6 PHPs, 5 of them are, unlike the ones in previous scenarios, Super-Earths with very high water contents what indicates that their accretion seeds come from beyond the snowline.

The masses of these PHPs are between 2.64M$_{\oplus}$ and 7.14M$_{\oplus}$. The most interesting characteristics of these PHPs can be seen in table 4.

**Outer region:** This scenario does not present any kind of objects, nor planets nor planetesimals, beyond the giants after 200 Myr of evolution.

- Planetary systems in this case extend only up to the position of the outermost Jupiter analogue at ~ 20 au. This is a direct consequence of the initial conditions which do not present an embryo and planetesimal population beyond the gas giants. Besides, the strong gravitational interactions between the two gas giants with the inner embryo and planetesimal population only manage to eject bodies outside the
systems and not to disperse them towards the outer zones of the disc.

**Mass remotion:** In this scenario, and considering all the simulations, a $\sim 50\%$ of the embryos collides with the central star, a $\sim 35\%$ is ejected from the system and a $\sim 23\%$ is accreted by other embryos. The planetesimal population is excited mostly by the gas giants but also by the Neptune-like planet, and in only $\sim 20$ Myr this population is completely removed from the system.

- As, unlike the other scenarios the planetesimals are initially located inside the giants, an important percentage of them collide with the central star ($\sim 11\%$) while the great majority is ejected from the system ($89\%$).

Only a $0.3\%$ of the planetesimals are accreted during the whole evolution of the systems. Thus, although the location of these bodies is different from the other scenarios, the accretion of planetesimals is still a very inefficient process.

In conclusion, the planetary systems of this scenario resulting from $S_1$ in figure 1 present between 2 and 3 planets in the inner zone of the disc, one of which is a Neptune-like planet. In 6 of 10 simulations we find a water-rich Super-Earth PHP class A or B. Then we find a Neptune-like planet around 3 au and 2 Jupiter analogues beyond $\sim 10$ au. This scenario results to be interesting since formed PHPs with high primordial water contents.

**Figure 6.** Time evolution of SIM$_7$ of the scenario with planetesimals of 1 km and without considering type I migration. The shaded areas represent the HZ regions already described in Section 1. Planets are plotted as colored circles, planetesimals are plotted with black dots and the giant planets, which are a Saturn-like planet and a Jupiter-like planet in this case, are represented in grey and black, respectively. The two big colored planets with black borders represent the two Neptune-like planets. The sizes of the Saturn-like and Jupiter-like planets are fixed and are not in the same scale for the rest of the planets. The same happens with the planetesimal population, each planetesimal adopts a size of half the size of the smallest embryo, independently of its mass. Then, the size for the rest of the planets is represented by a linear relation between the mass and the size, where the size for the smallest embryo is the double of the size of the planetesimals, and the size of the biggest planet is smaller that the size for a Saturn-like planet, like in the previous scenario. The color scale represents the fraction of water of the planets with respect to their total masses. This scenario forms 4 PHPs within the HZ, but 3 of those 4 are the Neptune-like planets. In this particular case the planet that remain within the HZ is a Super-Earth of $2.55M_{\oplus}$ classified as a PHP class B.
Figure 7. Time evolution of SIM of the scenario with planetesimals of 100 m and without considering type I migration. The shaded areas represent the HZ regions already described in Section 1. Planets are plotted as colored circles, planetesimals are plotted with black dots, the two big colored circles with black borders are Neptune-like planets and the two black circles represent Jupiter analogues of 1.49M_J and 5M_J. The size of the Jupiter-like planets is fixed and is not in the same scale for the rest of the planets. The same happens with the planetesimal population, each planetesimal adopts a size of half the size of the smallest embryo, independently of its mass. Then, the size for the rest of the planets is represented by a linear relation between the mass and the size, where the size for the smallest embryo is the double of the size of the planetesimals, and the size of the biggest planet is smaller than the size for a Saturn-like planet, like in the previous scenario. The color scale represents the fraction of water of the planets with respect to their total masses. This is the first scenario that form water-rich PHPs.

5.3 Comparison between planetesimal sizes

Here we highlight the most important differences and similarities between the reference scenarios formed by planetesimals of different sizes and without migration rates during the gaseous phase, focusing mainly on the inner regions where potentially habitable planets form.

- Following panels S_1, S_4, S_6 and S_9 in figure 1 it can be seen that the mass of the main perturbers of the different scenarios grows as the size of the planetesimals decreases. During the evolution of the N-body simulations, those less gas giant planets, like the Saturn-like planet in scenarios of 100 km and the Saturn-like planet in scenarios of 1 km, suffered a significant inward embryo-driven migration. This migration particularly placed the Saturn-like planet in scenarios of 100 km at the outer edge of the HZ, preventing the formation of PHPs.

- Regarding the global configuration of the different scenarios at the end of the gaseous phase we can see that scenarios formed with planetesimals of 100 m are quite different from those formed with planetesimals of 1 km, 10 km and 100 km. Just by looking at the initial conditions in Fig. 1, and comparing S_1 with S_4, S_6 and S_9, it can be seen that: 1) the planetesimal population is located inside the giants positions, instead of outside, 2) the gas giants are much further away from the central star than they are in the other scenarios, and 3) a water-rich embryo population is directly next to the dry one, in the inner region of the disc. These differences in the initial conditions conduct to different results in the final configurations of the N-body simulations.
The mass remotion mechanisms, this is embryo and planetesimal remotion via accretion, collisions with the central star and via ejections of the systems, are quite similar in all the scenarios being the most efficient mechanism the ejection, both of embryos and planetesimals. The remotion of planetesimals is completely efficient for the scenario formed by planetesimals of 100 m.

- The inner regions of all the scenarios are generally configured quickly, within the first 1 Myr of evolution for scenarios of 100 km and 10 km, and within the first 10 Myr and 50 Myr for scenarios of 1 km and 100 m, respectively.

- The efficiency in the formation of PHPs seems to be higher for scenarios formed from small planetesimals than from bigger ones, being completely null for planetesimals of 100 km. The final masses of these PHPs are in a wide range of values. The masses of the PHPs of the scenario formed from planetesimals of 100 m are in the range of the Super-Earths, while the masses of the PHPs in the other scenarios are in the range of the Super and Mega-Earths. It is important to remark that, in scenarios with planetesimals of 1 km, 3 of the 4 PHPs founded where Neptune-like planets that do not present any interest. Regarding water contents, the only PHPs of real interest that present water contents are those formed in scenarios with planetesimals of 10 km.

- The previous sections described the general results of the default N-body simulations performed considering different planetesimal sizes and no type I migration. Since one of the important results of PI was that the most favorable scenarios for the formation of SSAs were planetary systems with low/null type I migration rates, we also performed N-body simulations for those SSAs at the end of the gaseous phase, that presented type I migration rates reduced to a 1% and to a 10%. The goal of this section is not to describe in detail, as we did before, the particular results of each of these simulations, but to give a global view of what are the effects that this phenomenon produces and how the previous results could change because of it.

We performed 10 different simulations for each scenario S2, S3, S4, S5, S8, and S10, that represent planetary systems with type I migration rates reduced to a 1% and to a 10%. Those simulations with type I migration reduced to a 1% do not present significant differences from the ones without type I migration. For example, the initial conditions of S9 (100 km without type I migration) and S10 (100 km with type I migration reduced to 1%) are very similar and thus, the final configurations of the N-body simulations are similar too. Although the mass of the Saturn-like planet of S10 is smaller than the Saturn-like planet of S9 in a factor ∼ 3, the main result is that none of these scenarios form planets in the inner region of the disc. Something similar occurs between S6 (10 km without type I migration) and S7 (10 km with type I migration reduced to 1%) although S6 presents 2 gas giants as main perturbers and S7 presents only 1. The main results show that the inner region of the disc presents between 1 and 2 dry planets with masses in the range of the Super and Mega-Earths, and that some of them, between 3 and 5, are completely dry PHPs. In the same way, the results concerning scenarios of 1 km with type I migration reduced to a 1% and without type I migration, are also similar: the main result shows that both scenarios form dry PHPs. Regarding scenarios of 100 m, both kinds of simulations, with migration reduced to a 1% and without type I migration, form water-rich PHPs.

The results of PI showed that only very few planetary systems formed from planetesimals of 100 m and 10 km were able to form SSAs at the end of the gaseous phase with type I migration rates reduced to a 10%. Although this is an uncommon result, we still performed simulations for this scenarios, whose initial conditions are represented by S1 (for scenarios with planetesimals of 100 m) and by S8 (for scenarios with planetesimals of 10 km).

For scenarios with planetesimals of 10 km, the type I migration during the gaseous-phase, favors the giant planet to form closer to the central star. In this case, this result is detrimental to the formation of PHPs. However, for scenarios with planetesimals of 100 m it seems to be just the other way around. We will describe these situations in more detail below.
Figure 9 shows initial and final configurations of planetary systems formed from planetesimals of 100 m (bottom) and 10 km (top). The left panel shows the initial conditions at the beginning of the N-body simulations and the right panel shows the N-body simulations results. On the one hand, comparing the two scenarios of 10 km, with and without type I migration, we can see that type I migration during the gaseous stage, leads the giant planet of the system to locate closer to the central star than the inner giant is in the scenario without migration. This result, which is a natural consequence of type I migration, and the fact that the position of the giant could also change during the post-gas evolution of the system due to an induce migration via the gravitational interactions with the surrounding embryos and planetesimals, is unfavorable for the formation of PHPs. In fact, we already described that the simulations with 10 km planetesimals and no type I migration were able to form 5 dry PHPs. However, the 10 simulations developed with 10 km planetesimals and type I migration rates reduced to a 10% were not able to form PHPs at all. On the other hand, comparing the two scenarios of 100 m, with and without type I migration, we can see that in spite of the fact that type I migration manages to locate the giant further inside, regarding the position of the innermost giant in the scenario without type I migration, in this case, this effect favors the formation of PHPs. In fact, as we have already comment in section ??, the simulations with planetesimals of 100 m and no type I migration were able to form 6 water-rich PHPs. However, the 10 simulations developed with type I migration rates reduced to a 10% were able to form 11 PHPs, 9 are classified as PHPs class A and 2 class B. The final masses of these PHPs are between 0.93M_J and 3.73M_J, with water contents between 24.3% to 33.5%. It would seem then, that there is a preferential location for the inner giants, in terms of the efficiency in the formation of PHPs. We will return to this point later.

To conclude, scenarios with type I migration rates highly reduced, do not present significant differences from those scenarios without type I migration. However, scenarios with type I migration rates that represent a 10% of the Tanaka et al. (2002) type I migration rates, show different results for planetary systems formed from small and big planetesimals. This phenomena seems to favor the formation of PHPs in scenarios with small planetesimals, but definitely avoids their formation in scenarios formed from big planetesimals.

5.5 Results sensitivity to scenarios with gap-opening giants

Another important phenomenon that could modify the final configuration of the planetary systems, is the type II migration. The type II migration occurs when a planet is massive enough to fulfill the Crida et al. (2006) criteria, therefore to open a gap in the disc, which depends not only on the mass and the position of the planet but also on the Hill radius of the planet, the viscosity and the height scale of the disc (see PI for more details). This phenomenon, which was included in the model of planet formation of PI, produced an inward migration during the gaseous phase, only for this gap opening giant, and an increase in its mass due to the accretion of gas and other planets in its path. It is important to remark that the location of the gas giant at the end of the gaseous phase is not a consequence due only to the type II migration, but because once type II migration is turned on, the planet, which moves inward, accretes other planets in its path. Recall from PI that the resulting semimajor-axis of a fusion between two planets is given by the conservation of angular momentum (see eq. 33 in PI).

It has been proved by many models that an inward giant planet migration shepherds some planets captured at inner mean motion resonances with the giant, which are then dispersed into outer orbits, leading to the formation of planetary systems with an inner compact planet population and an outer much more scattered planet population (Fogg & Nelson 2005, 2006; Raymond et al. 2006; Fogg & Nelson 2007; Mandell et al. 2007). Particularly, Fogg & Nelson (2009) have showed that including a viscous gas disc with photoevaporation in an N-body code and although the type II inward migration, it is still possible to form planets within the HZ in low-eccentricity warm-Jupiter systems if the giant planet makes a limited incursion into the outer regions of the HZ. Our model of planet formations does not yet include the scattering effects from a migrating giant planet or the gravitational interactions between planets that can lead to resonance captures. Therefore, the results of our N-body simulations could be affected by the initial conditions which could had underestimated the number of planets in the inner zone of the systems at the end of the gaseous phase.

The main difference between the opening gap giant planets with those which did not, is their final mass. Gap opening planets are, in general, more massive than those that did not. Table 5 shows the ranges of masses for those giants that opened and did not opened a gap, in the scenarios with planetesimals of different size. The ranges are in Saturn and Jupiter masses due to the fact that we find both types of planets in scenarios with 100 m, 1 km and 10 km. As it can be seen in the table, the masses of those giants that opened a gap in the disc during the gaseous phase is greater than the other ones.

| Scenario | Giants that did not opened a gap | Giants that opened a gap |
|----------|----------------------------------|--------------------------|
| 100 m    | 0.81M_S − 5M_J                  | 5.63M_J − 9.92M_J        |
| 1 km     | 0.48M_S − 4M_J                  | 7.23M_J                  |
| 10 km    | 1.33M_S − 0.8M_J                | 1.88M_J − 2.10M_J        |
| 100 km   | 0.56M_S − 1.90M_S               | 3.23M_J                  |

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In order to see if there were significant differences between the default scenarios and scenarios without type I migration but with at least one giant that managed to turn on type II migration, we run more simulations. We chose one initial condition for each planetesimal size that presents a gas giant that has opened a gap. This is, we chose 4 new initial conditions and we run 10 simulations per each of these 4 scenarios changing, as we did before, the seed. Figure 10
shows, in a similar way as figure 10 does, a comparison between simulations of the two extreme reference scenarios of 100 km and 100 m without type I and type II migration and scenarios of 100 km and 100 m without type I migration but with the type II migration activated. The left panels show the initial conditions at the beginning of the N-body simulations, this is, the final results at the end of the gaseous phase, and the right panels show the N-body simulations results after 200 Myr of evolution.

A global result, found in all the new simulations, is that, due to the high mass of the new opening gas giants, those scenarios which present a planet and planetesimal population beyond the gas giants, do not present a mix of dry and water-rich material in the outer zone of the disc. This is, the inner dry embryos are directly ejected from the systems and are not scattered towards the outer regions.

Regarding the efficiency in forming PHPs, in scenarios with planetesimals of 100 km, it still remains completely null. None of the simulations with planetesimals of 100 km, without type I migration and with a planet that opened a gap, managed to form PHPs. The gap opening Jupiter-like planet in the scenario of 100 km of figure 10 (the big black point with a white cross) have 3.22MJ and is located around ~2 au, while the Saturn-like planet in the scenario of 100 km which did not opened a gap presents a mass of 0.5MJ and is located, initially at 2.96 au and finally at ~1.7 au. For scenarios of 10 km, the production of PHPs in the 10 simulations performed with a planet that opened a gap is lower than in the default scenarios. This scenario formed 2 dry PHPs instead of 4 with masses of ~2M⊕ and 11M⊕. Following with scenarios of 1 km, in this case the PHP production was similar. Both scenarios, with and without an opening gas giant, produced 5 PHPs with masses ranging from 0.9M⊕ to ~6M⊕. Finally, scenarios with planetesimals of 100 m and a giant planet that opened a gap formed 9 PHPs with masses between 5.28M⊕ and 11M⊕, 3 more than in the default case. In these scenarios, the gap opening Jupiter-like planet has a mass of 5.63MJ against the 1.49MJ of the Jupiter-like planet that did not opened a gap, and the first one is located around 6.38 au while the second one is located at 10 au. This analysis of the comparison between the whole group of simulations, with and without a gap opening planet, shows us that the type II inward migration coupled with the increase of the mass of the giant seems to act in a similar way as type I migration and with a planet that opened a gap, managed to form PHPs. The gap opening Jupiter-like planet in the scenario of 100 km of figure 10 (the big black point with a white cross) have 3.22MJ and is located around ~2 au, while the Saturn-like planet in the scenario of 100 km which did not opened a gap presents a mass of 0.5MJ and is located, initially at 2.96 au and finally at ~1.7 au. For scenarios of 10 km, the production of PHPs in the 10 simulations performed with a planet that opened a gap is lower than in the default scenarios. This scenario formed 2 dry PHPs instead of 4 with masses of ~2M⊕ and 11M⊕. Following with scenarios of 1 km, in this case the PHP production was similar. Both scenarios, with and without an opening gas giant, produced 5 PHPs with masses ranging from 0.9M⊕ to ~6M⊕. Finally, scenarios with planetesimals of 100 m and a giant planet that opened a gap formed 9 PHPs with masses between 5.28M⊕ and 11M⊕, 3 more than in the default case. In these scenarios, the gap opening Jupiter-like planet has a mass of 5.63MJ against the 1.49MJ of the Jupiter-like planet that did not opened a gap, and the first one is located around 6.38 au while the second one is located at 10 au. This analysis of the comparison between the whole group of simulations, with and without a gap opening planet, shows us that the type II inward migration coupled with the increase of the mass of the giant seems to act in a similar way as type I migration.
migration do. Although this is the outcome of our simulations, more simulations should be carried out to confirm this trend. These effects seem to favor the formation of PHPs for scenarios with small planetesimals and to be detrimental for scenarios formed from big planetesimals.

5.6 Possible range of mass and location of the inner giant to form PHPs

With the aim of exploring the possible range of masses and semimajor-axis of the inner giant planet to form PHPs, we performed histograms taking into account all the simulations in where we found PHPs, without differentiating them according to the size of the planetesimals, the type I migration rates, or the gap opening. As it is shown in the top left panel in Fig. 11, more than the 70% of the PHPs were formed in planetary systems with the innermost giant planet located between 3 au and 6 au. Then, following the top right panel of Fig. 11, it seems that a possible range for the mass of the inner giant planet to form PHPs could be between 1M_J and 3M_J since we find more than the 60% of the PHPs within these values. These top panels do not distinguish from planetary systems with one, two or three gas giants, but the middle and the bottom histograms do. If we distinguish planetary systems with only one gas giant from those with two gas giants, we find some differences. For those systems with one giant, a possible range for the location and mass for the giant planet, to form PHPs, is between 3 au and 4 au and between 4M_J and 5M_J, respectively. However, for those planetary systems with two gas giants, the majority of the PHPs were formed in systems with the inner giant around 6 au and between 1M_J and 3M_J.

It is however important to remark that these results are obtained only considering the results of the developed N-body simulations, which do not present a detailed sample of the semimajor-axis distribution of the inner gas giants between 1.5 au and 10 au. Thus, although the sample of N-body simulations carried out in this work helps us to explore the ranges of mass and position for the inner giant planet to form PHPs, this sample is not enough to determine an optimal mass and an optimal position for the inner giant planet to form PHPs, even more if we want to discriminate between systems with one and two giants. In order to determine a precise value of the mass and location of a giant planet to efficiently form PHPs, it is necessary to develop a greater number of N-body simulations from a better and also greater selection of initial conditions. Since we count with these initial conditions from the results of PI, we will return to this analysis in future works.

6 CONTRAST WITH THE OBSERVED PLANET POPULATION

One of the goals of this work is to contrast the final configurations of SSAs with those planetary systems already observed that present at least some similarities with this population. It is, however, important to remember that the goal of PI and this paper is not to reproduce the current exoplanet population, but to generate a great diversity of planetary systems, particularly SSAs, without following any observable distribution in the disc parameters. Then, once the late-accretion stage has finished and the final configurations of SSAs have been obtained, our goal is to contrast our results with the current planetary systems population which present, on the one hand, gas giants like Saturn or Jupiter beyond 1.5 au and, on the other hand, rocky planets in the inner regions, particularly in their HZs. To do this, we are only going to take into account those planetary systems around solar-type stars with masses in the range of ~ 0.8M_☉ to 1.2M_☉ which present at least one giant planet beyond 1.5 au and those planetary systems which present planets of interest near or in the HZ. As we have already mentioned at the beginning, planetary systems similar to our own have not yet been discovered. However, it is possible that planetary systems with detected gas giants present rocky planets in the inner zone of the disc, and also, it could be possible that planetary systems with detected rocky planets present gas giants not yet discovered, particularly if they present large semimajor-axis and low eccentricities.

This section is then divided by taking into account the comparison with two different observed planet populations: the PHPs population and the gas giant planet population.

6.1 PHPs population

Since the CoRoT (Barge et al. 2008) and Kepler (Borucki et al. 2010) missions began to work, our conception of the existence of other worlds has changed.
Table 6. Potentially habitable planets around solar-mass stars from http://phil.upr.edu. * planet candidate/unconfirmed. * estimated value for rocky composition when not available.

| Name               | Mass [M$_\odot$] | Radius [R$_\oplus$] | Spectral Type |
|--------------------|------------------|----------------------|---------------|
| Kepler-452 b       | 4.7$^*$          | 1.6                  | G             |
| Kepler-22 b        | 20.4$^*$         | 2.4                  | G             |
| Kepler-69 c        | 6.0              | 1.7                  | G             |
| Kepler-439 b       | 19.5$^*$         | 2.3                  | G             |
| tauCeti e$^*$      | > 4.3            | 1.6$^*$              | G             |
| HD-40307 g$^*$     | > 7.1            | 1.8$^*$              | K             |
| KOI 7235.01$^*$    | 1.4              | 1.1                  | G             |
| KOI 6425.01$^*$    | 3.5$^*$          | 1.5                  | G             |
| KOI 7223.01$^*$    | 3.7$^*$          | 1.5                  | G             |
| KOI 7179.01$^*$    | 1.5$^*$          | 1.2                  | G             |
| KOI 4450.01$^*$    | 9.9$^*$          | 2.0                  | G             |
| KOI 4054.01$^*$    | 10.1$^*$         | 2.0                  | G             |
| KOI 7587.01$^*$    | 14.9             | 2.2                  | G             |
| KOI 6734.01$^*$    | 13.1             | 2.1                  | G             |
| KOI 7136.01$^*$    | 17.4             | 2.3                  | G             |
| KOI 6676.01$^*$    | 7.0$^*$          | 1.8                  | F             |
| KOI 5475.01$^*$    | 5.0              | 1.7                  | F             |
| KOI 7554.01$^*$    | 9.9$^*$          | 2.0                  | F             |
| KOI 5236.01$^*$    | 9.9$^*$          | 2.0                  | F             |
| KOI 4103.01$^*$    | 14.4$^*$         | 2.2                  | K             |
| KOI 5202.01$^*$    | 7.3$^*$          | 1.8                  | F             |
| KOI 6343.01$^*$    | 8.4$^*$          | 1.9                  | F             |
| KOI 7470.01$^*$    | 8.4$^*$          | 1.9                  | K             |
| KOI 5276.01$^*$    | 15.2$^*$         | 2.2                  | K             |
| KOI 7345.01$^*$    | 21.1$^*$         | 2.4                  | F             |
| KOI 4458.01$^*$    | 25.9$^*$         | 2.5                  | F             |
| KOI 3946.01$^*$    | 20.7$^*$         | 2.4                  | F             |
| KOI 7040.01$^*$    | 14.7$^*$         | 2.2                  | F             |

considerably. During their working years, these missions were able to find a very high number of rocky planets with similar sizes to that of the Earth, as never before, giving rise to the exploration of this particular type of exoplanets. At present, both missions have ceased to function, but there are others on the way that will help to continue the study, detection and characterization of rocky planets, such as TESS (Transiting Exoplanet Survey Satellite) and CHEOPS (CHaracterising ExOPlanets Satellite). TESS (Ricker et al. 2010) is expected to discover thousands of exoplanets in orbit around the brightest stars in the sky through the transit method, and CHEOPS (Broeg et al. 2013), which will complement TESS, will characterize already confirmed exoplanets using photometry of very high precision to determine the exact radius of planetary bodies of known mass, between 1M$_\oplus$ and 20M$_\oplus$.

Till now, Kepler has discovered a total of 2244 candidates, 2327 confirmed planets and 30 small, less than twice Earth-size, HZ confirmed planets around different types of stars, while the K2 mission, which is still working, has discovered 480 new candidates and 292 confirmed planets (https://www.nasa.gov/mission_pages/kepler/).

In order to contrast our simulations with observations, we consider those N-body simulations that, after 200 Myr of evolution, present PHPs. Then, we contrast the simulated PHPs with the observed ones, only considering those PHPs from http://phil.upr.edu that orbit stars with masses in the range of ~0.8M$_\odot$ to 1.2M$_\odot$ (see table 6). It is important to remark that we are not making a precise statistical com-

6.2 Gas giant planet population

The population of giant planets, in particular hot-Jupiters, which was at first the most abundant and easy to be detected by both the Doppler and the transit techniques, is today, in front of the enormous amount of terrestrial-type exoplanets...
discovered by Kepler, a rare population (Batalha 2014). It is then believed that the rate of occurrence of giant planets is greater beyond 2 au and particularly around the location of the snowline (see Fischer et al., 2014, and references therein). However, it is still not so easy to detect gas giant planets on wide and circular orbits since Barnes (2007) showed that planets with eccentric orbits are more likely to transit than those planets with circular orbits with the same semimajor-axis by a factor of \((1 - e^2)^{-1}\), where \(e\) is the eccentricity of the planet.

To date, ~500 gas giant planets (more massive than Saturn) orbiting solar-type stars with masses in the range of ~0.8\(M_\odot\) to 1.2\(M_\odot\) were confirmed. From this, only ~142 are orbiting their star beyond ~1.5 au. However none of these giant planets has yet an associated rocky planet in the inner regions of the system, much less in the HZ. This does not strictly mean that these rocky companions in the inner zone of the disc do not exist. It is possible that the giants are camouflaging the signals of the rocky planets and that this makes it more difficult to detect them. Thus, again, we need to be careful when comparing the giant planets in our simulated planetary systems with those confirmed giants beyond 1.5 au, since they may still be part of planetary systems very different to Solar system analogues.

In order to contrast our simulated gas giant population with the observations, we are only going to take into account those single or multiple planetary systems, with one or more gas giants with masses greater than 0.3\(M_\oplus\) beyond 1.5 au. We also take into account those multiple planetary systems with more than two gas giants beyond 1 au. Figure 13 shows semimajor-axis vs eccentricity vs mass planes for planetary systems with only one gas giant (top panels) and with two gas giants (bottom panels) (http://exoplanet.eu/ Schneider et al. 2011). Each diagram shows the confirmed gas giant planets with masses greater than Saturn in colored squares (planetary systems with only one gas giant) and points (planetary systems with two gas giants) along with the gas giant planet population of all our simulations. Those gas giants in planetary systems that present PHPs at the end of the N-body simulations are shown in black squares (planetary systems with only one gas giant) and points (planetary systems with two gas giants), while the gas giants in planetary systems that did not form PHPs are represented in grey.

In general, it can be seen that in those planetary systems with only one gas giant (top panels) the range of semimajor-axis and masses of the simulated gas giants is pretty well represented by the confirmed population of giant planets. However, this does not seem to happen for the eccentricity range. The least eccentric confirmed exoplanet of the selected sample has an eccentricity of 0.02, whereas we form planets with up to more than one order of magnitude less eccentric. This population of planetary systems with very low eccentric gas giants seems to be not yet detected, and in particular, it seems to be the one that is able to form PHPs. It is also interesting to remark that those simulated gas giants with eccentricities higher than 0.2, semimajor-axis greater than ~1.5 au and masses greater than ~0.3\(M_\oplus\) and which are overlapped with the observed and confirmed gas giants, are part of planetary systems that were not efficient in forming PHPs (grey squares).

Something similar seems to happen in planetary systems with two gas giant planets (bottom panels). In this kind of planetary systems, although the range in mass is well represented by the confirmed population of giant planets, the ranges of semimajor-axis and eccentricities are not. In this sense, we are forming a population of planetary systems with very low eccentric gas giants in wider orbits extended until ~30 au that seems to be not yet detected. And again, this population seems to be efficient in forming PHPs.

We then ask ourselves if in fact this population of very low eccentricities and wide orbits is a natural result of the evolution of the simulations, and therefore is, indeed, a population not yet detected, or if it is a consequence of the initial conditions imposed by our model of planet formation, where at the beginning and at the end of the gaseous stage the planets are in circular and co-planar orbits. A detailed study of the evolution of the semimajor-axis and eccentricities of our giants shows us that the gravitational interactions between these bodies and the rest of the planets of the system, which are consider during the evolution of the N-body simulations, lead to significant changes in their eccentricities although do not lead to planet-planet scattering events that involve gas giant planets. For planetary systems with only one giant planet, the registered changes in the giants eccentricities during the late-accretion stage reach values higher than an order of magnitude of the initial eccentricities.
systems with two gas giants these changes are even greater, and the eccentricities can increase even more. Then, this population of planetary systems with giant planets of low eccentricities is, within the framework of having considered initial (this is at the beginning of the N-body simulations) quasi-circular and co-planar orbits for the giants, a natural result of its own orbital evolution. It is however important to highlight that more realistic treatments for the gaseous phase evolution of these systems could lead to different gas giant planet configurations. Our model of planet formation for this stage does not include the gravitational interactions between planets. These interactions could lead to encounters between giants increasing their eccentricities as the gas dissipates and scattering other planets in their way. On the other hand, this effect could also cause planets to be trapped in mean motion resonances. Both situations can in turn lead to different final configurations for the planetary systems at the end of the late accretion stage.

7 DISCUSSION

In the present work, we carry out N-body simulations aimed at studying the late accretion in Solar system analogues (SSAs), and the formation of potentially habitable planets and water delivery. To interpret the results of our simulations it is very important to mention some points concerning the evolution of our systems during the gaseous phase as well as once the gas has dissipated.

According to that mentioned in Section 3, we select 10 scenarios of work in order to carry out our analysis concerning the late-accretion stage in SSAs. The evolution of such systems during the gaseous phase was obtained from the work developed by Ronco et al. (2017), PI.

It is worth noting that, as it was mentioned in Section 2, the model of planet formation of PI, from which we obtain the initial conditions to develop N-body simulations, presents limitations. Some of these limitations are the consideration of isothermal discs and the corresponding type I migration rates for such discs, and the lack of the calculation of the gravitational interactions between embryos. The consideration of more complex physics during the gaseous phase could alter the final results of embryo and planetesimal distributions at the end of the gaseous phase and thus significantly change our results on the final planet mass, their locations and water contents at the end of the late-accretion stages.

Particularly, as it was mentioned before, type I migration rates for non-isothermal discs could be very different for those in isothermal discs such as they could stop or even change the migration direction of the planets (Paardekooper et al. 2010, 2011). The consideration of gravitational interactions between planets during the gaseous phase could allow the planets to be trapped in mean motion resonances (MMR) and this could avoid a fast orbital decay into very inner zones of the disc (Masset & Snellgrove 2001). Moreover, the consideration of this effect, as it was shown by Morbidelli & Crida (2007) within the framework of our Solar system is that, if Jupiter was able to open a gap in the disc and migrate inward through type II migration, and if at the same time Saturn was able to migrate faster towards Jupiter, they could have been locked in a 2:3 (MMR) and could have stopped or even reversed the migration of both planets together. On the other hand, the interactions between giant planets in the inner regions of the disc when the gas is already removed due to photoevaporation, can lead to the ejection of one or two planets exalting the eccentricities of the remaining ones. Then, all these considerations, which were not taken into account in PI, can change the final results of our N-body simulations.

It is also important to remark that the 10 scenarios of work chosen to carry out our investigation show differences concerning the number and the physical and orbital properties of the giant planets that host. On the one hand, 5 of those 10 scenarios start the post-gas phase with a single giant planet, whose mass ranges from 0.45M$_J$ to 4M$_J$. On the other hand, the other five systems of work host two gaseous giants at the beginning of the post-gas stage, most of which show masses of the order of the Jupiter’s mass.

In those 5 scenarios of work that host 2 gaseous giants, the initial orbital separation between them ranges between 4.1 and 11.7 mutual Hill radii. It is worth noting that none of the N-body simulations developed in the present research produced close encounters between the massive giant planets of the system, which seems to be consistent with the works developed by Gladman (1993), Chambers et al. (1996), and Marzari (2014). Obviously, an analysis concerning the stability of the system of 2 giant planets is more complex since they are immersed in a population of embryos and planetesimals in our scenarios of study. However, this simple consideration allows us to understand the absence of close encounters between the massive giant planets in all our N-body simulations.

From this, we must remark that the SSAs formed in the present research did not experiment resonance capture processes during the gaseous phase while they did not undergo strong dynamical instability events that involve the massive giant planets. Thus, the proposed analogy between the systems formed in our simulations and the Solar system should be carefully interpreted if scenarios of formation such as the Grand Tack model (Walsh et al. 2011) and the Nice model (Tsiganis et al. 2005) are accepted. Studies concerning the formation and evolution of systems that host giant planets and undergo strong instability events between them will be addressed in future works.

On the other hand, it is interesting to note that our rocky planets grow fundamentally from the giant impacts they undergo once the gas disk dissipates, a process that lasts about 100 Myr. Late formation stages like the “late veneer” or the “heavy bombardment” on our Earth are not present in our simulations. If our Solar system experienced three stages of formation given by the stage of giant impacts, the late-veneer, and finally the heavy bombardment (see Raymond et al. 2013, and references therein), the planets of our simulated systems only suffer the first stage, not being affected by later ones in which a population of planetesimal remnants reshape them.

Our N-body simulations form, after 200 Myr of evolution, planetary systems similar to our own with rocky planets in the inner zone of the disc and at least one gas giant beyond 1.5 au. One of the goals of this work is to analyze the formation of planets within the HZ. The simulations performed were able to form two very different kinds of PHPs: dry and water-rich (this is, planets that come from beyond
the snowline or planets that have accreted at least an embryo from this region). Taking into account the 4 default scenarios described in this work, the most common type of PHPs seems to be the dry ones since we formed them in 3 of those 4 scenarios. However, considering the final number of PHPs formed within all the developed simulations, and considering that the most common result from PI was to form SSAs in scenarios with planetesimals of 100 m, it seems that the most common PHPs are the water-rich ones instead of the dry ones, since a 65% of the whole PHPs population is formed by water-rich planets (almost all of them formed in scenarios with planetesimals of 100 m), and a 35% is formed by dry planets.

One of the limitations of our model, which is important to remark, is that the high water contents in those water-rich PHPs must be considered as upper limits due to the fact that we do not take into account water loss during impacts. However, the great majority of our water-rich PHPs do not suffer from a great number of giant collisions. Thus, their primordial water amounts could survive during the whole evolution. Moreover, Dvorak et al. (2015) showed that the water retained in fragments after a collision remains on the target for impact velocities $v \leq 1.3 \text{v}_{\text{esc}}$, while more than 80% of the water stays as well in strongly inclined hit-and-run scenarios. Another interesting result is that, due to the fact that all our water-rich PHPs come from beyond the snowline, their water contents are primordial. This result is in concordance with the results of Salvador Zain et al. (2017) who also found that all water contents of the HZ planets in systems that harbor a Jupiter-mass planet around the snowline, are also primordial.

If, although the water contents have to be considered as upper limits, they could have remained in their great totality until the end of the evolution. We wonder then what is the effect of such water contents in the habitability.

Some authors argue that too large amounts of water may be detrimental for the potential habitability (Alibert 2014; Kitzmann et al. 2015). These authors claim that a too large water layer can lead to the existence of a high pressure ice layer at the bottom of the global ocean, and this could prevent the Carbonate-silicate cycle from occurring. This could be a problem since the Carbonate-silicate cycle is fundamental to maintain the temperature of the surface for long periods of time (Alibert 2014), and could be particularly problematic for stars such as the sun, which suffer variations in their flux at relatively short timescales. Moreover, Kitzmann et al. (2015) showed that an unstable CO$_2$ cycle could limit the extension of the HZ for ocean planets. Other studies, such as the work developed by Abbot et al. (2012), found that the weathering behavior is not sensitive to the land fraction for those planets which are covered by oceans, as long as the land fraction is greater than 0.01. This result suggests that those partially covered water planets may have a HZ similar to a planet which is not. Moreover, although these authors indicate that water worlds could have narrower HZ, they could be capable of “self-arresting” a moist greenhouse effect, and could become planets with partial ocean coverage. Recently, Noack et al. (2016) also concluded that water-rich planets may be habitable and could allow the developing of life as we know it, if these water-rich planets present shallow oceans, a low planet mass, or a high surface temperature. They find that small-massive planets with less than one Earth mass can be habitable even for substantial amounts of water. However, Super-Earths covered with oceans can only be considered as habitable planets, if they contain low percentages of water by mass. Although this is a topic that is still under debate and that the only existence of liquid water is definitely not enough to determine habitability, water-rich planets seem to be common in the Universe (Raymond et al. 2004; Simpson 2017). We

Figure 13. Comparison between the observations and the developed simulations. This plot shows eccentricity vs semimajor-axis, mass vs eccentricity and mass vs semimajor-axis planes for planetary systems with one gas giant (top panels) and two gas giants (bottom panels). The colored squares and points represent the locations of the gas giant planets in planetary systems with only one and two gas giants, respectively, beyond 1.5 au and with masses greater than Saturn. The black squares and points represent the locations of the gas giants in simulated planetary systems that present PHPs, in planetary systems with only one and two gas giants, respectively. The grey squares and points represent the locations of the gas giants in simulated planetary systems that do not present PHPs, in planetary systems with only one and two gas giants, respectively. The colored areas represent the range in semimajor-axis, eccentricity and mass, in where we find planetary systems with one or two gas giants, that were able to form PHPs.
particularly find them in planetary systems without gas giant planets in high (de Elía et al. 2013) and low-mass discs (Ronco & de Elía 2014; Ronco et al. 2015), in planetary systems around low-mass stars (Dugaro et al. 2016), and in planetary systems with different gas giant planets as main perturbers (Salvador Zain et al. 2017), and because of that we still consider them present a particular interest.

Another important topic that could affect the habitability of our PHPs due to the possible absence of plate tectonics is their final masses, since the great majority of them are Super-Earths (39%) and, to a lesser extent, Mega-Earths (31%), with masses very different from that of our planet. However, Valencia et al. (2007) show that plate tectonics, which are a necessary condition for the development of life, can also be found in Super-Earths. These authors show that, as the planetary mass increases, the subduction process, and therefore the plate tectonics, becomes easier. Therefore, massive Super-Earths are very likely to exhibit plate tectonics and therefore, to keep life possible. On the other hand, Morard et al. (2011) showed that, for masses greater than 2M⊕, the Super-Earths cores could be entirely solid, this precludes the existence of a liquid metallic core driven by magnetic fields. The lack of magnetic fields is detrimental to the potential habitability given that they are those that favor the existence and permanence of an atmosphere for long periods of time.

Finally, and following with our model limitations, we believe that a more realistic treatment of the collisions, including fragmentation and hit-and-run collisions (Chambers 2013) rather than assuming that all impacts lead to a perfect merger of the colliding bodies, should be included in future works. Quintana et al. (2016) presented results of N-body simulations of the late stage formation of Earth-like planets around sun-like stars with Jupiter and Saturn analogues perturbing the system and including a collision model that follows Leinhardt & Stewart (2012) and Chambers (2013). They found that, globally, when fragmentation is considered the number of final planets and their masses are similar to those formed in the standard model without fragmentation and hit-and-run collisions. However, the collision history of the final planets is different and the accretion timescales are usually doubled in the fragmentation simulations. Thus, we consider that this improvements in the treatment of collisions will allow us to determine in more detail the orbital and physical properties of the planets formed in our simulations, particularly the final masses and amounts of water by mass of the formed PHPs.

8 CONCLUSIONS

In this work we carry out a great number of N-body simulations aimed at analyzing the global formation of the post-gaseous phase of SSAs, particularly focusing in the formation of rocky planets within the HZ and their final water contents. The initial conditions to start the simulations were provided by the results of PI (Ronco et al. 2017). In that first work we analyzed the evolution, during the gas-phase, of different planetary systems, particularly of those which were at the end of the gaseous phase similar to our own, considering different planetesimal sizes and different type I migration rates.

The main results of our simulations, which are analyzed for planetary systems that did not experienced type I migration rates during the gaseous phase, show that the efficiency in the formation of potentially habitable planets (PHPs) seems to strongly depend on the size of the planetesimals from which these systems were formed. Planetary systems formed from small planetesimals are the most efficient ones. Moreover, this kind of planetary systems, formed from small planetesimals of 100 m, is the only one capable of forming water-rich PHPs. Bigger planetesimals of 1 km and 10 km also form PHPs but completely dry, and planetary systems formed from planetesimals of 100 km do not form PHPs at all.

We also test the sensitivity of the results to scenarios that experienced type I migration rates during the gaseous phase and that were also able to form giant planets massive enough to open a gap in the gas disc and to turn on type II migration. Our results show that planetary systems which experienced very low type I migration rates do not present significant differences to the results of those SSAs that did not, and that planetary systems which experienced type I migration rated reduced to a 10% seems to favor the formation of PHPs in scenarios formed from small planetesimals but is detrimental for the formation of PHPs in scenarios formed from big planetesimals. Those planetary systems which were able to form giant planets that opened gaps in the gas discs during the gaseous phase seem to act in the same way as type I migration does. Analyzing all the developed simulations, it also seems that there might be an optimal mass and location for the inner giant planet of the system regarding the efficiency of forming PHPs. Although we estimate those values around ~ 6 au and between 1M J and 2M J taking into account all the developed simulations in this work, a most detailed set of numerical simulations considering a the semimajor-axis distribution of the inner gas giants between 1.5 au and 10 au should be developed in order to properly determine these values. It is however important to remark that we count with all the information to do this work in a near future.

Finally, we make a comparison between our simulated planetary systems and the current potentially habitable planet population and gas giant population. Although this kind of comparisons must be analyzed carefully since, to date, no planetary systems similar to our own have been yet discovered, this is, none of the observed (confirmed and candidates) potentially habitable planets present a gas giant companion beyond 1.5 au, we are able to form PHPs in a region of the mass vs semimajor-axis diagram that is currently being explored. Moreover, the simulated giant planet population that was capable of forming PHPs occupies a region of the semimajor-axis vs eccentricity diagram of extended semimajor-axis and very low eccentricities, and to date a population with these characteristics has not been yet discovered. We believe that the discovery of exoplanets with these properties is a challenge of future missions. Particularly, Hippke & Angerhausen (2015) explored the potential of future missions such as PLATO 2.0 in detecting Solar system analogues, and showed that the discovery of Venus and Earth-like planets transiting stars like our sun is feasible at high signal-to-noise ratio after collecting 6 yrs of data. They also showed that, due to the high number of observed stars by PLATO, the detection of single-transit events by cold gas
giant's like Jupiter, Saturn, Uranus, and Neptune analogues, will be possible. These future detections, particularly those of cold gas giants, will allow us to associate this population with the potential existence of planets in the HZ.

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REFERENCES

Abbot D. S., Cowan N. B., Ciesla F. J., 2012, ApJ, 756, 178
Abe Y., Ohtani E., Okuchi T., Righter K., Drake M., 2000, Water in the Early Earth, pp 413–433
Alibert Y., 2014, A&A, 561, A41
Alibert Y., Mordasini C., Benz W., Winnisdorffer C., 2005, A&A, 434, 343
Andrews S. M., Wilner D. J., Hughes A. M., Qi C., Dullemond C. P., 2010, ApJ, 723, 1241
Barge P., et al., 2008, A&A, 482, L17
Barnes J. W., 2007, PASP, 119, 986
Batalha N. M., 2014, Proceedings of the National Academy of Science, 111, 12647
Bitsch B., Johansen A., Lambrechts M., Morbidelli A., 2015, A&A, 575, A28
Bolmont E., Libert A.-S., Leconte J., Selsis F., 2016, A&A, 591, A106
Borucki W. J., et al., 2010, Science, 327, 977
Borucki W. J., et al., 2012, ApJ, 745, 129
Broeg C., et al., 2013, in European Physical Journal Web of Conferences. p. 03005 (arXiv:1305.2270), doi:10.1051/epjconf/20134703005
Chambers J. E., 1999, MNRAS, 304, 793
Chambers J. E., 2001, Icarus, 152, 205
Chambers J., 2008, Icarus, 198, 256
Chambers J. E., 2013, Icarus, 224, 43
Chambers J. E., Wetherill G. W., Boss A. P., 1996, Icarus, 119, 261
Crida A., Morbidelli A., Masset F., 2006, Icarus, 181, 587
D’Angelo G., Marzari F., 2012, ApJ, 757, 50
Dauphas N., Pourmand A., 2011, Nature, 473, 489
Dugoro A., de Elía G. C., Brunini A., Guilera O. M., 2016, A&A, 596, A54
Dvorak R., Maindl T. I., Burger C., Schäfer C., Speith R., 2015, A&A, 588, A10
Faggar D. A., Howard A. W., Laughlin G. P., Macintosh B., Mahadevan S., Sahlmann J., Yee J. C., 2014, Protostars and Planets VI, pp 715–737
Fogg M. J., Nelson R. P., 2005, A&A, 441, 791
Fogg M. J., Nelson R. P., 2006, International Journal of Astrobiology, 5, 199
Fogg M. J., Nelson R. P., 2007, A&A, 461, 1195
Fogg M. J., Nelson R. P., 2009, A&A, 498, 575
Gladman B., 1993, Icarus, 106, 247
Guilera O. M., Sándor Z., 2017, A&A, 604, A10
Guilera O. M., Brunini A., Benvenuto O. G., 2010, A&A, 521, A50
Guilera O. M., Fortier A., Brunini A., Benvenuto O. G., 2011, A&A, 532, A142
Guilera O. M., de Elía G. C., Brunini A., Santamaría P. J., 2014, A&A, 565, A96
Hayashi C., 1981, Progress of Theoretical Physics Supplement, 70, 35
Hellary P., Nelson R. P., 2012, MNRAS, 419, 2737
Higuchi A., Kokubo E., Kinoshita H., Mukai T., 2007, AJ, 134, 1693
Hipple M., Angerhausen D., 2015, ApJ, 810, 29
Ida S., Lin D. N. C., 2004, ApJ, 604, 388
Inaba S., Tanaka H., Nakazawa K., Wetherill G. W., Kokubo E., 2001, Icarus, 149, 235
Inamdar N. K., Schlichting H. E., 2015, MNRAS, 448, 1751
Jacobson S. A., Morbidelli A., Raymond S. N., O’Brien D. P., Walsh K. J., Rubie D. C., 2014, Nature, 508, 84
Jenkins J. M., et al., 2015, AJ, 150, 56
Kasting J. F., Whitmire D. P., Reynolds R. T., 1993, Icarus, 101, 108
Kitzmann D., et al., 2015, ArXiv e-prints 1507.01727
Kopparapu R. K., et al., 2013a, ApJ, 765, 131
Kopparapu R. K., et al., 2013b, ApJ, 770, 82
Kopparapu R. K., Ramirez R. M., SchottelKotte J., Kasting J. F., Domagal-Goldman S., Eymet V., 2014, ApJ, 787, L29
Laakso T., Rantala J., Kaasalainen M., 2006, A&A, 456, 373
Lecuyer C., Gillet P., and Robert F., 1998, Chem. Geol., 165, 429A$S261
Leinhardt Z. M., Stewart S. T., 2012, ApJ, 745, 79
Lodders K., Palme H., Gail H. P., 2009, Landolt Börnstein, Mandell A. M., Raymond S. N., Sigurdsson S., 2007, ApJ, 660, 823
Marty B., 2012, Earth and Planetary Science Letters, 313, 56
Marzari F., 2014, MNRAS, 442, 1110
Masset F., Suelgrová M., 2001, MNRAS, 320, L55
Miguel Y., Guilera O. M., Brunini A., 2013, MNRAS, 427, 204
Morard G., Bouchet J., Valencia D., Mazevet S., Guyot F., 2011, High Energy Density Physics, 7, 141
Morbidelli A., Cría A., 2007, Icarus, 191, 158
Mordasini C., Alibert Y., Benz W., Naef D., 2009, A&A, 501, 1161
Noack L., et al., 2016, Icarus, 277, 215
O’Brien D. P., Morbidelli A., Levison H. F., 2006, Icarus, 184, 39
Ohtsuki K., Stewart G. R., Ida S., 2002, Icarus, 155, 436
Paardekooper S.-J., Baruteau C., Kley A., Kley W., 2010, MNRAS, 401, 1950
Paardekooper S.-J., Baruteau C., Kley W., 2011, MNRAS, 410, 293
Pfalzner S., Steinhausen M., Menten K., 2014, ApJ, 793, L34
Pringle J. E., 1981, ARA&A, 19, 137
Quintana E. V., Barclay T., Borucki W. J., Rowe J. F., Chambers J. E., 2016, ApJ, 821, 126
Rafikov R. R., 2004, AJ, 128, 1348
Raymond S. N., Izidoro A., 2017, Icarus, 297, 134
Raymond S. N., Quin N., Lunine J. I., 2004, Icarus, 168, 1
Raymond S. N., Quin N., Lunine J. I., 2006, Icarus, 183, 265
Raymond S. N., O’Brien D. P., Morbidelli A., Klaiber N. A., 2009, Icarus, 203, 644
Raymond S. N., Schlichting H. E., Hersant F., Selsis F., 2013, Icarus, 226, 671
Richer G. R., et al., 2010, in American Astronomical Society Meeting Abstracts #215, p. 459
Ronco M. P., de Elía G. C., 2014, A&A, 567, A54
Ronco M. P., de Elía G. C., Guilera O. M., 2015, A&A, 584, A47
Ronco M. P., Guilera O. M., de Elía G. C., 2017, MNRAS, 471, 2753
Salvador Zain P., de Elía G. C., Ronco M. P., Guilera O. M., 2017, preprint (arXiv:1710.04617)
Schneider J., Dedieu C., Le Sidaner P., Savalle R., Zolotukhin I., 2011, A&A, 532, A79
Selsis F., Kasting J. F., Levrard B., Paillet J.,Ribas I., Delfosse X., 2007, A&A, 476, 1373
Simpson F., 2017, MNRAS, 468, 2803
Suzuki T. K., Muto T., Inutsuka S.-i., 2010, ApJ, 718, 1289
Suzuki T. K., Ogihara M., Morbidelli A., Crida A., Guillot T., 2016, A&A, 596, A74
Tanaka H., Takeuchi T., Ward W. R., 2002, ApJ, 565, 1257
Tanigawa T., Ikoma M., 2007, ApJ, 667, 557
Touboul M., Kleine T., Bourdon B., Palme H., Wieder R., 2007, Nature, 450, 1206
Tsiganis K., Gomes R., Morbidelli A., Levison H. F., 2005, Nature, 435, 459
Valencia D., O’Connell R. J., Sasselov D. D., 2007, ApJ, 670, L45
Veras D., Evans N. W., 2013, MNRAS, 430, 403
Walsh K. J., Morbidelli A., Raymond S. N., O’Brien D. P., Mandell A. M., 2011, Nature, 475, 206
Williams D. M., Pollard D., 2002, International Journal of Astrobiology, 1, 61
Wolfgang A., Rogers L. A., Ford E. B., 2016, ApJ, 825, 19
de Elía G. C., Guilera O. M., Brunini A., 2013, A&A, 557, A42

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