INFLUENCE OF THE AIR LAYER BETWEEN THE CONDUCTOR AND THE LAYER OF INSULATING MATERIAL IN CABLE PRODUCTS

Evgenia V. Ivanova¹, ², Olga S. Yashutina¹, Stanislav V. Shidlovskiy²
¹National Research Tomsk Polytechnic University, 634050 Tomsk, Russia
²National Research Tomsk State University, 634050, Tomsk, Russia

Abstract. There are developed mathematical model of physical and chemical processes of polymerization adhesive coating stranded cable. There are shown difference in the temperature distribution along the radius of the finished product in the presence of an air gap between the conductor and the rubber sheath. Also, due to the need to change process parameters with possible loose contacts inside the cable. Such as the temperature of the heating surface, feeding speed and dwell time in the oven.

1 Introduction

Production of cables is a long and energy-intensive process. The result is a whole product length of 100 meters. In this case, even a small marriage invalid. It is believed that contact between the conductor and the layer of insulating material of the finished cable product is ideal, in shell tightly to the copper conductor. Acceptable dimensions of gaps, as a rule, does not exceed 0.01 mm [1].

The aim of this study was to determine the possible impact of the presence of the air layer between the copper wire and the rubber shell, exceeds the limit, the polymerization on the final products of the cable sheath.

2 Problem statement

Numerical simulation was carried out in the system shown in Fig. 1. It was assumed that the cable consists of a copper conductor, an air layer and a rubber sheath. Considered axial symmetric system.

Figure 1. Schematic of the field of solving the problem: 1 - steel wire, 2 - air layer 3 - cable sheath.

In the numerical simulation used the following assumptions do not impose significant restrictions on the common statement of the problem:

1. The cable has a right cylindrical shape.
2. We consider a fragment of a perfectly insulated cable end.
3. The thermal characteristics of the material strands, the cable sheath and the air in the heating chamber does not depend on temperature.
4. The activation energy of the polymerization process is constant with temperature.
5. The cable is stationary relative to the camera.

a Corresponding author: zhenya1@tpu.ru

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3 Mathematical model

A mathematical model of heat and mass transfer system “hot air – cable” in a cylindrical coordinate system (Fig. 1) for \(0 < t < t_p\) can be formulated in the form of a typical stationary differential equations of mathematical physics [2, 3].

The heat equation for the core (\(0 < r < R_1, 0 < z < Z_1\)):

\[
\rho_1 C_1 \frac{\partial T_1}{\partial t} = \lambda_1 \left( \frac{\partial^2 T_1}{\partial r^2} + \frac{1}{r} \frac{\partial T_1}{\partial r} + \frac{\partial^2 T_1}{\partial z^2} \right). \tag{1}
\]

The heat equation for the air layer (\(R_1 < r < R_2, 0 < z < Z_1\)):

\[
\rho_2 C_2 \frac{\partial T_2}{\partial t} = \lambda_2 \left( \frac{\partial^2 T_2}{\partial r^2} + \frac{1}{r} \frac{\partial T_2}{\partial r} + \frac{\partial^2 T_2}{\partial z^2} \right). \tag{2}
\]

The energy equation for the insulating sheath (\(R_2 < r < R_3, 0 < z < Z_1\)):

\[
\rho_3 C_3 \frac{\partial T_3}{\partial t} = \lambda_3 \left( \frac{\partial^2 T_3}{\partial r^2} + \frac{1}{r} \frac{\partial T_3}{\partial r} + \frac{\partial^2 T_3}{\partial z^2} \right) + q_3 \rho_3 \frac{d\phi_3}{dt}; \tag{3}
\]

\[
\frac{d\phi_3}{dt} = (1 - \phi_3) \kappa_3^0 \exp \left( - \frac{E_3}{R_1 T_3} \right). \tag{4}
\]

The initial (\(t = 0\)) conditions:

\(T = T_0\) at \(0 < r < R_3, 0 < z < Z_1\);

\(\phi = \phi_0\) at \(R_2 < r < R_3, 0 < z < Z_1\).

The boundary conditions at \(0 < t < t_p\):

\[
\frac{\partial T_1}{\partial z} = 0 \quad \text{at} \quad z=0, 0 < r < R_3; z=L, 0 < r < R_3;
\]

\[
\frac{\partial T_2}{\partial r} = 0 \quad \text{at} \quad r=0, 0 < z < Z_1; r=R_3, 0 < z < Z_1;
\]

\[-\lambda_1 \frac{\partial T_1}{\partial r} = -\lambda_2 \frac{\partial T_2}{\partial r}, T_1 = T_2 \quad \text{at} \quad r=R_1, 0 < z < Z_1;\]

\[-\lambda_2 \frac{\partial T_2}{\partial r} = -\lambda_3 \frac{\partial T_3}{\partial r}, T_2 = T_3 \quad \text{at} \quad r=R_2, 0 < z < Z_1.\]

The system of non-stationary differential equations with appropriate boundary conditions is solved by finite difference method [4]. Difference analogs of differential equations solved locale-no-one-dimensional method and variable direction [4]. To solve the two-dimensional difference equations applied sweep method using a four-point implicit scheme [4].

4 Results and discussion

It can be seen that the presence of the air layer, exceeding the limit value considerably influences the temperature distribution along the radius of the finished product (Fig.2). The surface of the cable is heated to considerably higher temperatures, which can lead to burnout of the shell. Also, due to gapping may be incorrectly selected process parameters (time, speed of pulling, the temperature of the heating surface), which in turn may affect the polymerization of the shell.

It is necessary to control the fit sheath to core in the manufacture of cable products to improve the quality of the finished product (the degree of polymerization of the rubber should be close to 1).
Figure 2. Distribution of temperature: a) without an air layer between the sheath and conductor, b) in the presence of the air layer of 0.5 mm.

Figure 3. Temperature dependence of the copper wires in the center of cable products from the thickness of the air layer.
5 Conclusion

The developed mathematical model, algorithms for the numerical solution of heat and mass transfer can be used to analyze the quality of the insulation of cable products and energy efficiency of polymerization processes in their production [5-9]. Also, the proposed model can be used as predictive modes when selecting curing typical cables and the relevant parameters (temperature in the furnace, the heating time, pull the speed, etc.).

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