Nanostructures on fused silica surfaces produced by ion beam sputtering with Al co-deposition

Ying Liu1,2 · Dietmar Hirsch1 · Renate Fechner1 · Yilin Hong2 · Shaojun Fu2 · Frank Frost1 · Bernd Rauschenbach1

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Abstract
The ion beam sputtering (IBS) of smooth mono-elemental Si with impurity co-deposition is extended to a pre-rippled binary compound surface of fused silica (SiO2). The dependence of the rms roughness and the deposited amount of Al on the distance from the Al source under Ar+ IBS with Al co-deposition was investigated on smooth SiO2, pre-rippled SiO2, and smooth Si surfaces, using atomic force microscopy and X-ray photoelectron spectroscopy. Although the amounts of Al deposited on these three surfaces all decreased with increasing distance from the Al target, the morphology and rms roughness of the smooth Si surface did not demonstrate a strong distance dependence. In contrast to smooth Si, the rms roughness of both the smooth and pre-rippled SiO2 surfaces exhibited a similar distance evolution trend of increasing, decreasing, and final stabilization at the distance where the results were similar to those obtained without Al co-deposition. However, the pre-rippled SiO2 surfaces showed a stronger modulation of rms roughness than the smooth surfaces. At the incidence angles of 60° and 70°, dot-decorated ripples and roof-tiles were formed on the smooth SiO2 surfaces, respectively, whereas nanostructures of closely aligned grains and blazed facets were generated on the pre-rippled SiO2, respectively. The combination of impurity co-deposition with pre-rippled surfaces was found to facilitate the formation of novel types of nanostructures and morphological growth. The initial ripples act as a template to guide the preferential deposition of Al on the tops of the ripples or the ripple sides facing the Al wedge, but not in the valleys between the ripples, leading to 2D grains and quasi-blazed grating, which offer significant promise in optical applications. The rms roughness enhancement is attributed not to AlSi, but to AlOxFy compounds originating mainly from the Al source.

1 Introduction
Low-energy ion beam sputtering (IBS) is a powerful bottom-up technology for generating diverse self-organized nanostructures, such as ripples and dots on different materials including amorphous SiO2 [1–7], single crystalline Si [8–12], Ge [10, 13] and Ag [14], as well as compound semiconductors GaSb [15] and InP [16]; the IBS technology offers the potential to achieve high throughput and fabrication of large areas [10, 17–19]. Ion beam parameters (species, incidence angle, energy, flux, etc) and substrate parameters (material, temperature, initial surface topography, etc) interact to generate the features of such nanopatterns. Recently, numerous experiments on sputtering with simultaneous co-deposition [20–39] and theoretical studies [40–47] on simultaneous metal co-deposition during IBS or surfactant sputtering [32–38, 46, 47] have been performed to elucidate the formation mechanism of self-organized nanostructures and to generate various nanopatterns. In principle, the simultaneous use of metal atoms modulates the sputtering yield of the substrate during IBS, which results in diverse physical and chemical phenomena (e.g., island formation or phase separation). Silicide induced by metal co-deposition has been generally considered to contribute significantly to the formation of Si nanostructures during Si erosion at normal or near normal incidences to the ion beam. To date, extensive research has been conducted on the ion erosion of smooth Si surfaces under simultaneous co-deposition of metals at normal or near normal incidences. However, very few co-deposition studies have been reported.
on either compound materials or pre-patterned substrates. Only one work investigates Al co-deposition on SiO₂ films that were thermally grown on Si [30], and this work did not focus on patterning, showing only the development of an Al thickness gradient on the SiO₂.

In fact, nanostructures on compound surfaces are considered especially promising for a wide range of applications. For example, nanopatterned SiO₂ [48–51] may offer superior performance as an anti-reflective surface in the deep ultraviolet spectral range for applications in lasers, solar cells, etc., and as quantum nanostructures on III–V semiconductor surfaces [52–54] in optoelectronics and quantum optics. Moreover, according to available experimental and simulation data, pre-patterned surfaces have shown great potential for generating novel or highly ordered patterns, or even gratings [55–58]. In addition, IBS may prove to be a fast and cost-effective nanofabrication tool for large area nanostructures with critical dimensions or wavelengths in the vicinity of 100 nm. Therefore, in this study, the IBS of a compound with metal co-deposition—specifically, of fused silica with Al co-deposition—will be investigated. To understand the formation and evolution mechanisms of such nanostructures, several comparisons will be performed between smooth and pre-rippled fused silica, smooth fused silica, and Si.

Fused silica is a typical and widely available compound of Si that contains only silicon and oxygen, and this compound is an important material for technical applications in many fields. Previous work on the ion erosion of SiO₂ revealed that pattern formation without co-deposition is enhanced when the erosion is implemented on pre-patterned surfaces rather than smooth surfaces [6]. Therefore, Al co-deposition on fused silica may further accelerate the morphology evolution and generate novel nanostructures.

Aluminum was selected as the co-deposition material for this study for the following reasons. First, the aspect ratio of fused silica can be enhanced by leveraging the difference in the sputter yields of fused silica and Al₂O₃ [7]. Second, to date, no work has been reported on the ion erosion of Si with Al co-deposition. Third, Al is often present in ion beam etching machines, and Al contaminations may affect the surface topography of fused silica in the ion beam etching or machining of this material. This last consideration is particularly relevant to applications in which the microroughness of ion beam-processed optical elements is a crucial parameter.

Therefore, in this study, a setup similar to that of Hofssäss et al. [32] was used to achieve IBS of fused silica with Al co-deposition. The Al concentration changed with the distance from an Al wedge to the samples. The formation of Al-fused silica nanostructures was analyzed and compared to analogous results for pure Si substrates using atomic force microscopy (AFM) and X-ray photoelectron spectroscopy (XPS). Section 2 introduces the experimental setup. Section 3 presents and discusses the morphologies achieved by sputtering with Al co-deposition and the relationship between the morphologies and the amount of Al deposited. The final section presents the study’s conclusions.

2 Experimental methods

The initial root mean square (rms) roughnesses of the fused silica (hereinafter denoted as SiO₂) and Si wafers were approximately 0.4 and 0.15 nm, respectively. All samples were cut to a typical size of 30 mm (in the x direction) × 15 mm (in the z direction), as shown in Fig. 1. Ion bombardment experiments were performed using a system constructed by some of the authors for the purpose of these experiments [10]. The diameter of the Kaufman-type broad beam ion source was approximately 180 mm. The IBS was performed with a 400 eV Ar ion beam with a beam current of 70 mA for a duration of 20 min, corresponding to a fluence of \(1.1 \times 10^{18}\) ions/cm² in the plane perpendicular to the ion beam. Metal co-deposition was achieved with an Al target, positioned adjacent to the SiO₂ or Si samples, as shown in Fig. 1. The target’s specifications identified the composition as 98.7% Al, 0.29% Si, 0.27% Mg, 0.52% F, and 0.06% Fe. The target was an Al wedge with an apex angle of 20°, so that the angle of the surface between a sample and the wedge was fixed to 110°. During sputtering, both the samples and the wedge were exposed to the ion beam. A fraction of Al atoms that sputtered off the wedge was directly deposited onto the sample surface, which could affect the final morphology of the sample surface, and even generate self-organized patterns. The incidence angles of the ion beam upon the sample and the Al wedge, denoted as \(\theta_1\) and \(\theta_2\), respectively, were defined as the angles between each surface normal and the ion beam, as shown in Fig. 1.
incidence angles discussed hereinafter refer to those between the ion beam and the normal of the samples, $\theta_s$.

The surface morphologies of the sputtered SiO$_2$ and Si samples were characterized by an AFM working in tapping mode within an area of $2 \times 2$ μm$^2$ and with a resolution of 1024 × 1024 pixels. The AFM data were analyzed with SPIP™ software [59]. Consequently, XPS analysis of the samples was performed to determine the concentration of deposited materials as a function of the distance to the Al target. XPS measurements were performed using monochromatic Al Kα radiation and a concentric hemispherical analyzer (CHA). The collected spectra were analyzed with Unifit 2015 software [60], and concentration calculations were performed using the Unifit software in conjunction with theoretical photoionization cross-sections, calculated electron mean-free paths, and experimentally determined instrument transmission functions.

3 Results and discussion

Section 3.1 provides a general overview of the evolving SiO$_2$ surface pattern depending on the ion incidence angle. In Sects. 3.2 and 3.3, the variations of the SiO$_2$ surface topography associated with two selected ion incidence angles are discussed in more detail. In particular, the topography’s dependence on the distance from the Al wedge (i.e., the Al concentration) is discussed. In addition, the similarities and differences between the ripple development on smooth and pre-patterned surfaces are shown. Section 3.4 compares the surface evolution of the SiO$_2$ with that of the Si with simultaneous Al co-deposition. Section 3.5 presents the XPS analysis of the ion sputtered surface with simultaneous Al co-deposition. Finally, Sect. 3.6 discusses the formation mechanism of the surface patterns.

3.1 Incidence angle dependence of smooth SiO$_2$ morphology treated by IBS with Al co-deposition

Figure 2 shows the incidence angle dependence of the morphology evolution of a SiO$_2$ wafer under IBS and Al co-deposition. The AFM images were taken at a position 2 mm from the Al target edge. In addition, to provide a clear picture of each irradiation condition, the sputtering geometry at each incidence angle is shown in Fig. 2(b′−f′), respectively. In principle, a given location on the SiO$_2$ wafer in front of the Al target received 400-eV Ar ions, sputtered Al atoms, and Ar particles backscattered from the Al target. The effect of the backscattered Ar particles upon SiO$_2$ surfaces is insignificant, and therefore, the effect is omitted in the discussion.

Figure 3a and b show the incidence angle dependence on rms roughness and on the power spectral density (PSD) evolution, respectively, of the surface under IBS with Al co-deposition. At low incidence angles ($\theta_s < 40^\circ$), the surfaces remained smooth with a roughness of approximately 0.4 nm. When self-organized nanostructures were generated at larger incidence angles of 60° and 70°, the rms roughness of these surfaces increased. The PSDs of ion incidence angles less than 40° were similar to each other but different from those of incidence angles of 60° and 70°. The incidence angle dependence of rms roughness of SiO$_2$ with Al co-deposition was very similar to those previously reported for SiO$_2$ [5], Si [22], and Ge [13] without metal co-deposition.

Most of the recent investigations of sputtering with metal co-deposition have been conducted on Si surfaces at normal incidences to the ion beam. For Si surfaces, dot patterns have been generated at or near normal incidences with concurrent metal deposition. However, in our study, no pattern was generated on SiO$_2$ at the incidence angle of $\theta_s < 40^\circ$ even with Al co-deposition. This indicated a remarkable pattern formation difference between Si and SiO$_2$, which may be due to different chemical products and their effects upon the pattern formation and growth.

The following subsection details the investigations into sputtering at the incidence angles $\theta_s$ of 60° and 70°, which correspond to incidence angles $\theta_i$ of 10° and 0°, respectively, between the ion beam and the normal of the sputtered surface of the Al wedge.

3.2 Distance dependence of smooth SiO$_2$ morphology treated by oblique IBS with Al co-deposition

Typical AFM images of the surface morphologies of smooth SiO$_2$ at distances between 2 mm and more than 20 mm from the Al wedge are shown for incidence angles of 60° (Fig. 4) and 70° (Fig. 5). To provide further insight into the effect of Al co-deposition, the rms roughnesses and XPS analyses of the samples are shown in Fig. 6. The rms roughnesses in Fig. 6a were calculated from the AFM data in Figs. 4 and 5.

3.2.1 Differences between incidence angles of 60° and 70°

Different nanostructures were formed at each incidence angle. As shown in Fig. 4, ripples decorated with dots were generated on the surface at 60°, which was very similar to a previously reported Si surface nanopatterned during an oblique 40 keV Ar$^+$ erosion with Fe co-deposition at the same incidence angle [28]. In contrast, at 70°, roof-tiles developed on the surface along the direction of the wave vector of an ion-induced ripple (Fig. 5). These results demonstrate that the incidence angle of the ion beam is a very important parameter relevant to generating different nanostructures.
The results for the incidence angle of 70° showed sharper morphological and rms roughness transitions than those at 60°. As shown in Fig. 6a, the distances corresponding to the rms roughness maxima at 60° and 70° were 12 and 6 mm, respectively. In addition, the rms roughnesses of the samples stabilized at the distances of 20 and 11 mm, respectively; at these positions, the samples would be sufficiently distant from the Al wedge that co-deposition would not occur. The distances corresponding to both the roughness maxima and stabilization at 70° were clearly less than those at 60°. These differences in the morphological and rms roughness evolutions induced by incidence angles of 60° and 70° indicated
a difference in the deposition-sputtering ratios of Al and Ar flux $\Phi_{Al}/\Phi_{Ar}$ at each incidence angle, with a larger $\Phi_{Al}/\Phi_{Ar}$ ratio resulting in a faster pattern evolution. Hence, the $\Phi_{Al}/\Phi_{Ar}$ at 70° was considered to be larger than that at 60°.

Most works on IBS with metal co-deposition have been conducted under normal incidences of the ion beam. The two most relevant reports on the IBS of Si with metal co-deposition at oblique angles have been published by (A) Redondo-Cubero et al. [28] and (B) Moon et al. [31]. In these papers, IBS was conducted at an incidence angle of 60° with Fe co-deposition (silicide-forming metal) and at 75° with Au co-deposition (non-silicide forming metal), respectively. Compared to the results reported by Redondo-Cubero et al. [28], our investigation demonstrated a similar ripple decorated with dots on the smooth SiO$_2$ at the incidence angle of 60°. However, we did not observe a morphological transition similar to that observed by Moon et al.

### 3.2.2 Similarity of rms roughness dependence on distance for both incidence angles

In both cases, with increasing distance, the rms roughness of the morphologies increased, then decreased, and finally stabilized at the level of roughness obtained without Al co-deposition (shown by the dashed and dotted lines in Fig. 6a). However, with increasing distance to the Al target, the content of the Al co-deposition on the surface reduced only monotonously, whereas that of Si increased (Fig. 6b, c). A similar dependence of rms roughness upon the co-deposited metal content has also been observed in investigations of IBS Si patterning with Fe co-deposition [25]. The evolution of rms roughness can be divided into three regions as described in the following.

In Region I, the rms roughness increased with decreasing Al content. In other words, the rms roughness decreased with increasing Al content, which can clearly be attributed to the deposition of the Al film. Therefore, the main patterning mechanism in this region is controlled by the deposition. Such a smoothing effect due to increasing impurity content has also been reported in the IBS of Si with concurrent Au [32] and Fe [25, 29] depositions.

In Region II, the rms roughness increased with increasing Al content. The Al deposition’s enhancement of the rms roughness is pronounced in this region; this effect can be attributed to the coupled effects of the ion beam sputtering and the simultaneous directional deposition with a particular sputtering and co-deposition geometry.

In Region III, with increasing distance from the Al wedge, the co-deposition of Al upon the samples became almost zero, and the rms roughness decreased to the value obtained without Al co-deposition. In this region, physical sputtering based on a Bradley–Harper (BH) [61] model dominated the pattern generation.

### 3.3 Distance dependence of pre-rippled SiO$_2$ morphology treated by oblique IBS with Al co-deposition

We used pre-rippled samples to investigate the effects of the initial surface topography or roughness on the topography evolution with simultaneous Al co-deposition. The pre-patterned ripples were prepared by sputtering for 120 min with 1200 eV Kr ions at an incidence angle of 53° and a total fluence of $1.26 \times 10^{19}$ ions/cm$^2$.

The evolved surface morphologies are shown in Figs. 7 and 8 for ion incidence angles of 60° and 70°, respectively. Figures 7f and 8f present the pre-patterned surface, both with similar ripple wavelengths (approximately 110 nm) and roughness values (approximately 6.7 nm). For an incidence angle of 60°, the ion beam direction was parallel to
the initial ripple pattern (i.e., perpendicular to the vector of the pre-ripple), whereas at 70° the ion beam direction was perpendicular to the initial ripple pattern (i.e., parallel to the vector of the pre-ripple). The rest of this subsection compares the results of pre-rippled substrates with those of smooth substrates.

**Fig. 4** Typical AFM images of smooth SiO₂ samples after sputtering with Al co-deposition at an incidence angle of 60° at distances from the Al target of **a** 2 mm, **b** 6 mm, **c** 10 mm, **d** 12 mm, **e** 30 mm, and **f** without Al co-deposition. All images were obtained with the ion beam direction, which is indicated by a white arrow in **f**. The area shown by each image is 2 × 2 μm², and the magnified insets show areas of 0.5 × 0.5 μm². **g–l** Height profiles along lines parallel to the ion beam directions in **a–f**, respectively.
Fig. 5  Typical AFM images of smooth SiO$_2$ samples after sputtering with Al co-deposition at an incidence angle of 70° at distances from the Al target of: a 2 mm, b 6 mm, c 7 mm, d 8 mm, e 20 mm, and f without Al co-deposition. All images were obtained with the same ion beam direction, which is indicated by a white arrow in f. The area shown by each image is 2×2 μm$^2$, and the magnified insets show areas of 0.5×0.5 μm$^2$. g–l Height profiles along lines parallel to the ion beam directions in a–f, respectively.
3.3.1 Comparison of morphological pattern types of pre-rippled and smooth SiO₂ surfaces

Different morphological pattern types were present on the pre-rippled SiO₂ at each incidence angle. At an incidence angle of 60°, the initial ripple pattern was not clearly recognizable at short distances from the Al wedge (Fig. 7a, b), and the surface morphology was dominated by a grain- or cauliflower-like structure. Figure 7e shows a two-dimensional (2D) ripple pattern after sputtering at 60° without Al co-deposition; one ripple in Fig. 7e with a larger wavelength of approximately 100 nm originated from the initial pre-rippled surface, whereas the other new ripple with a smaller wavelength of approximately 20 nm and a ripple vector perpendicular to that of the first ripple vector was generated because the IBS direction was perpendicular to the vector of the initial pre-ripple. The 2D-ripple shows the ripple superimposition induced by the sequential IBS of the SiO₂ surfaces. The final grain- or cauliflower-like structure arises from the comprehensive effect of both the IBS and the concurrent Al co-deposition guided by the rippled surfaces.

At an incidence angle of 70°, faceted structures appeared on the pre-rippled SiO₂ surfaces, as shown in Fig. 8a, b. With the increasing amount of Al deposition, the edge of the blazed profile becomes increasingly smooth. A quasi-blazed grating, i.e., a blazed pattern with a little rough edge can be achieved with this sputtering and co-deposition geometry.

In summary, after IBS with Al co-deposition on pre-patterned SiO₂, novel pattern types of grains and blazed profiles are generated at incidence angles of 60° and 70°, respectively. Such pattern types are different from the ripples decorated with dots and the roof-tile nanostructures that developed on the initial smooth SiO₂, as shown in Figs. 4 and 5.

When the incidence angle was 70°, the separate roof-tiles on the smooth SiO₂ became continuous blazed profiles on the pre-rippled SiO₂. According to one sputtering investigation of Si with Fe co-deposition [12] and a simulation of surfactant sputtering [34], with pre-rippled SiO₂, Al is preferentially deposited on the tops of the ripples or on the ripple sides facing the Al wedge, but not in the valleys between the ripples. The initial ripples act as a template that guides a directional Al co-deposition, resulting in the alignment and connection of deposited Al.

From a practical perspective, both the SiO₂ grains and blazed profiles with the critical dimension of approximately 100 nm may be very attractive as potential optical devices, such as UV subwavelength optical elements or diffraction gratings with periods down to 100 nm.

3.3.2 Comparison of rms roughnesses of pre-rippled and smooth SiO₂ surfaces

On the one hand, some similarities can be found between the roughnesses of pre-rippled and smooth SiO₂ surfaces. For example, as shown in Fig. 9, the rms roughness of rippled SiO₂ evolves through increasing, decreasing, and stabilizing phases, similar to the evolution of the smooth SiO₂ samples as shown in Fig. 6. Moreover, the rms roughnesses of both the smooth and pre-rippled SiO₂ surfaces stabilized at a sufficiently long distance, approaching the rms roughness obtained without Al co-deposition.

On the other hand, differences also appeared in the rms roughness evolutions of the pre-rippled and smooth SiO₂ surfaces. For rms roughness growth, at incidence angles of 60° and 70°, the enhancement of morphological roughness from smooth to pre-rippled surfaces was pronounced, which indicates the stronger ability of a pre-rippled substrate to roughen a surface. Moreover, the maximal rms roughness of the pre-rippled SiO₂ was larger than that of the smooth SiO₂. In addition, the distance range corresponding to the maximal rms roughness of the pre-rippled SiO₂ was slightly larger than that of the smooth SiO₂. These effects can be attributed to the preferential deposition of Al on the tops of
the ripples or the ripple sides facing the Al wedge, but not in the valleys between the ripples following facts, as reported in the sputtering investigation of Si with Fe co-deposition [12] and the simulation of surfactant sputtering [34].

In summary, from the comparison of the morphologies and rms roughnesses of the pre-rippled and smooth SiO$_2$ surfaces, the initial rippled SiO$_2$ morphology clearly affected the nanostructure formation and fostered the
Fig. 8  Typical AFM images of pre-rippled SiO$_2$ sample after sputtering with Al co-deposition at an incidence angle of 70° at distances from the Al target of a 2 mm, b 8 mm, c 15 mm, d 20 mm, e 25 mm, and f initial rippled substrate. The ion beam direction indicated by the white arrow in f is the same for each AFM image. g–l Height profiles along lines parallel to the ion beam direction in a–f, respectively.
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3.3.3 Comparison of results with previous investigations on the IBS of pre-patterned surfaces

Considering potential optical applications, the quasi-blazed grating profile, formed on the pre-rippled SiO₂ at the incidence angle of 70°, is a very promising result from the IBS of a compound with impurity co-deposition.

Harrison and Mark Bradley [62] have recently simulated the morphological evolution of a pre-patterned surface with IBS at an oblique incidence. The authors proposed a method of generating blazed diffraction gratings produced by ion bombardments of pre-patterned solid surfaces.

The results of our sputtering experiment both agreed and disagreed with those of the simulation by Harrison and Bradley. Although their simulation did not use exactly the same initial parameters as our sputtering experiment, both studies showed a very similar finding in the blazed profiles that can be formed on pre-patterned surfaces.

Our experiments further demonstrated the ability of co-deposition during IBS to facilitate pattern generation and growth. In Harrison and Bradley’s report [62], they emphasize that the amplitude of the initial pattern must be sufficiently large to obtain the blazed grating, indicating the opposite possibility that the initial amplitude may be too small to generate the blazed grating at the proposed oblique incidence. In our experiment, as shown in Fig. 8f–e, because of the insufficient original rms roughness of the pre-rippled surface, the treated surfaces tend to be smoother. In contrast, as shown in Fig. 8a, b, the Al co-deposition clearly improves the rms roughness of the blazed profile generated on a substrate with the same original rms roughness as those shown in Fig. 8e, f.

3.4 Distance dependence of smooth Si morphology treated by oblique IBS with Al co-deposition

In this subsection, the influence of Al co-deposition on the pattern evolution on Si surfaces is examined and compared to the previous observations of Si [11, 12, 31, 32] and SiO₂ presented above.

Figures 10 and 11 show the morphologies of the smooth Si after IBS with Al co-deposition at incidence angles of 60° and 70°, respectively, and the figures show that the morphologies depended very little on the distance between the substrate and the Al wedge. The corresponding rms roughnesses and XPS analyses of Al and Si are shown in Fig. 12a–d. Table 1 compares the morphologies and rms roughnesses of the samples with and without Al co-deposition during IBS at incidence angles of both 60° and 70°.

For Si located more than 25 mm from the edge of the Al wedge, regular ion-induced ripples were formed on the smooth Si at incidence angles of 60° and 70° as shown in Figs. 10f and 11f, which is in good agreement with previously reported sputtering of Si surfaces [11, 12].

With the introduction of Al, the ion beam-induced ripples on the Si surface were coarsened and shortened, as shown in Figs. 10a–e and 11a–e and compared in Table 1. A similar coarsening and shortening has also been reported for the IBS of Si with Ag co-deposition [32]. During the IBS of Si with either Au or Ag co-deposition, there was no silicide formation [31, 32]. The coarsening of the patterns on the Si surface is due to the simultaneous Al deposition during IBS. Such coarsening is different from previously reported coarsening with increasing sputtering time [7, 9, 12, 63–65]. Although some theoretical work has explained the coarsening based on numerical models [66, 67], a model and simulation that can accurately predict the coarsening due to the impurity co-deposition remains unavailable at this time.

In summary, with the introduction of Al, the distance dependencies of the rms roughnesses of both smooth and pre-rippled SiO₂ are pronounced. However, the distance dependencies of the morphology and roughness of smooth Si showed only a very slight correlation with the Al content. Before analyzing the nanostructures formed on the Si surface, we compared the chemical components deposited on the smooth SiO₂ and Si by XPS measurements.

3.5 Comparison of XPS analyses of smooth SiO₂ and Si surfaces

Figure 13a and b illustrate the distance dependence of the concentration of key chemical components analyzed by XPS on smooth SiO₂ and Si, respectively. Besides Al₂p, F₁s and very little Fe₂p were also detected on both samples. Both F and Fe may have originated from the Al wedge and from the chamber walls of the IBS machine because of memory...
effects from reactive ion beam etching processes. The concentrations of Fe2p on both samples and that of F1s (CFx) on the smooth Si were too small to affect the formation of nanostructures. Those chemical components that showed concentrations that depended on the distance, such as Al2p and F1s (metal fluoride), were considered to originate from the Al wedge. The effect of Al2p and F1s (metal fluoride)
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Upon nanostructure generation will be considered in the following subsection.

To determine whether or not Al silicide formed on both samples, Table 2 details the concentrations of key chemical components and the corresponding binding energy as determined by XPS. Both samples have been analyzed at a distance of 8 mm away from the Al wedge edge during sputtering.

Fig. 11 Typical AFM images of smooth Si sample after sputtering with Al co-deposition at an incidence angle of 70° at distances from the Al target of a 4 mm, b 8 mm, c 10 mm, d 15 mm, e 25 mm, and f without Al co-deposition. The ion beam direction indicated by the white arrow in f is the same for each AFM image. g-l Height profiles along lines parallel to the ion beam direction in a-f, respectively.
For SiO₂, Al exhibited only one single peak at the binding energy of 74.8 eV, which is 0.1–1.1 eV higher than previously reported data for various Al₂O₃ modifications [68]. Hence the mixed oxyfluoride AlOxFy was present, and the Al was partly bound to oxygen and fluorine. Absolutely no Al or AlSi was detected.

For Si, Al clearly occurred in two states: one with a binding energy of 72.8 eV, and the other with a binding energy of 74.8 eV. The state of Al with the binding energy of 72.8 eV may indicate AlSi. This compound has been reported to form during deposition of Al on Si at a base pressure of 10⁻⁷ Torr and a temperature of 550 °C [69]. However, our experiments were done at room temperature with background pressures of 10⁻⁵–10⁻⁶ mbar, therefore, the formation of AlSi on Si is unlikely. In addition, the concentration of Al at 72.8 eV is only 0.19%, which is too low to affect the formation of nanostructures.

For the state of Al at the binding energy of 74.8 eV, according to Sitzmann [70], silicides of ignoble metals, such as Al, are strongly attacked by oxidizing substances like O, H₂O, and F. The reaction enthalpy of the formation of Al₂O₃ or AlF₃ is larger than that of AlSi. Therefore, the compound at the binding energy of 74.8 eV is considered to be more likely AlOxFy than Al₂SiO₅.

As shown in Fig. 13a and b, because the concentration of a metal fluoride (ionic bonding of F) is distance-dependent, the metal fluorides with the binding energies of approximately 685 eV on both samples in Table 2 should come from the Al wedge. The formation of AlF₃ and Al₂O₃ immobilizes the deposited disperse Al. Al₂O₃ and AlF₃ are not able to form AlSi because high energy is needed to reduce the Al from the stable state +3 in an oxide, fluoride, or mixed deposit.

This XPS analysis clearly demonstrates that no AlSi was formed on either the SiO₂ or the Si surface. Only AlOxFy (or less likely Al₂SiO₅) compounds were detected, with a higher concentration on SiO₂ (as shown in Figs. 6b and 12b) than on Si. The higher concentration of AlOxFy on SiO₂ results from the oxygen provided by the SiO₂.

### 3.6 Discussion

We have shown the distance dependence of the morphology and rms roughness of SiO₂ and Si surfaces sputtered at oblique incidence angles with Al co-deposition. At positions sufficiently far from the Al wedge, the IBS experiments show that ripples were generated on both SiO₂ and Si by the Ar ion beam sputtering without Al co-deposition. This is in accordance with earlier studies [5, 7]. The surface evolution in these cases, at least in the low-fluence regime, can be described following the classical BH model [61]. Therefore, from the results of our experiments, sputtering based on the BH model is considered one important mechanism of

| Table 1 Morphologies of smooth Si with incidence angles of 60° and 70° |
|------------------|------------------|------------------|------------------|
|                  | I without Al     | II with Al       |                  |
|                  | 60°              | 70°              | 60°              | 70°              |
| Morphology       | Self-organized   | Short and coarsened ripple and dots |
| Wavelength (nm)  | 26               | 36               | 40–65            | 30–65            |
| Amplitude (nm)   | ~ 1              | ~ 5              | 5–10             | 3–5              |
| rms roughness (nm) | 0.6             | 2.5             | 4.7–5.1          | 2.2–3.1          |
| Comparison of rms roughness | $\text{rms}_{60°} < \text{rms}_{70°}$ | $\text{rms}_{60°} > \text{rms}_{70°}$ | $\text{rms}_{60°} < \text{rms}_{70°}$ | $\text{rms}_{70°} > \text{rms}_{70°}$ |
pattern formation, which is similar to the findings of other investigations.

The XPS analyses clearly showed no AlSi; however, these analyses indicated the formation of AlOxFy compounds. This chemical product is different from the metallic silicides previously reported from investigations into IBS of Si with metal co-deposition. Our findings are unique because the chemical products of not metallic silicides, but AlOxFy should originate in the co-deposited impurity of Al, in conjunction with the general ion beam sputtering. In the following, an alternative explanation of the observed modification of the surface morphology and simultaneous Al co-deposition is discussed based on the sputtering yields and erosion velocities of AlOxFy, SiO2, and Si, along with sputtering geometry and initial rms roughness of the surfaces. This explanation is premised on the reasonable assumption that the micro-masking of both SiO2 and Si occurs because of the differences in the sputtering yields or erosion velocities.

For a more detailed discussion of the micro-masking effect, the sputter yields or etch rates of the different materials (SiO2, Si, Al, AlOxFy) would be required. However, these data are not easy to obtain. Simulations programs such as SRIM [71] or, better, TRIMP.SP [72] can be used, but these require the correct input parameters (e.g., surface binding energy). For the compound AlOxFy these parameters are not known. Therefore, approximate calculations were conducted for 400-eV Ar ions hitting a SiO2, Si, Al, or Al2O3 surface using TRIM.SP, with the potentials and free parameters that have been suggested by Eckstein [73]. The surface binding energies for Si (4.7 eV) and Al (3.36 eV) are well established [73]. However, the surface binding energies of both oxide compounds remain difficult to obtain. In this discussion, we use the surface binding energy values estimated from experimentally estimated sputtering yields that were fitted with an analytical expression for the sputtering yield that was derived by Sigmund [74]. Following the weighted mole fraction approach [74], the surface binding energies of 10.0 eV and 4.1 eV were calculated for Al2O3 and SiO2, respectively. From the resulting sputtering yields (Fig. 14a), the erosion velocities (Fig. 14b) were calculated for an ion current density of 200 μA/cm2, based on the atomic densities of the materials.

As expected from the surface binding energy values, Al2O3 exhibited the lowest sputtering yield, and Al exhibited the highest. Different trends were demonstrated in the erosion velocities, which are responsible for the local evolution of the surface. Because of the high atomic density of Al, the erosion velocities of Si, Al, and Al2O3 were more or less the same, and SiO2 displayed the highest erosion velocities.
A similarly high etching resistance as that of Al₂O₃ can be expected for the highly nonvolatile AlF₃. Therefore, a strong SiO₂ micro-masking effect can be reasonably assumed to be caused by a mixed oxyfluoride, AlOₓFᵧ. Depending on the sputter conditions, the simultaneous Al co-deposition can be expected to enhance structural heights (e.g., rms roughness), especially in areas near the Al wedge. For Si, the micro-masking effect is expected to be less pronounced, if it occurs at all. Indeed, this is confirmed by the results presented for Al co-deposition on Si.

In addition, the sputtering geometry and the roughness of the substrates play an important role in the morphological evolution of the surface, as can be clearly observed by comparing Figs. 7 and 8. In Fig. 7, the pre-pattern was aligned parallel to the ion beam (coming from the right) as well as to the Al particle flux direction (coming from the left). Therefore, no shadowing occurred, resulting in uniform coverage with Al (or, better, AlOₓFᵧ) near the Al wedge, where the Al flux was sufficiently high; this produced an isotropic pattern on the surface (Fig. 7a, b). Further away from the wedge (Fig. 7c), the Al concentration decreased and only some regions were masked, precluding the formation of a uniform or isotropic roughness. Even further away, the topography evolution was almost unaffected by the Al and a superimposed ripple pattern developed due to the ion beam erosion of the initially parallel aligned pre-pattern, in accordance with the observations reported in [6].

These results contrast with those shown in Fig. 8, where the pre-rippled surface is aligned perpendicular to the ion beam and to the Al particle flux direction. In this arrangement, shadowing caused the Al to be predominantly deposited on the sides of the ripples facing the Al wedge (downstream from the ion beam), whereas the face pointing to the ion beam (on the upstream side) received much less Al. Therefore, the upstream side, as well as the valleys between the ripple ridges were eroded faster compared to the downstream side, which was sputtered with greater amounts of Al or AlOₓFᵧ. With increasing distance from the Al wedge, the Al concentration decreased further (Fig. 8c, d), and only some of the downstream faces received sufficient Al to show a micro-masking effect. At large distances, the topography was scarcely influenced by the Al, and the initially present ripple pattern followed an evolution typical of these ion beam conditions, except for additional roughness wavelength components originating from the pre-pattern; this result is also supported by [6].

These results are illustrated in Fig. 15, where a typical surface profile of the pre-pattern, together with the incidence directions of the Al flux and the Ar ion beam are shown, drawn to scale. The sputtering geometry in Fig. 8 corresponds to that in which the Ar ions come from the right at an incidence angle of 70° (corresponding to 20° to the sample surface) and the Al comes from the left at an incidence angle of 0° to the normal of the wedge surface (due to the 20° wedge angle) with a cosine distribution around this angle. If we consider a representative emission angle of 30° for the Al atoms from the normal of the wedge, then the angle to the substrate surface is also 10° (i.e., 80° with respect to the SiO₂ surface normal), resulting in the geometrical situation
shown in the figure, where the effect of shadowing is clearly evident.

With the ion beam erosion of the smooth Si surface, the pattern was less affected by the Al co-deposition. This can be explained by the lower concentration of AlO$_x$F$_y$ (or Al$_2$SiO$_5$) on Si compared to SiO$_2$ (Figs. 6 and 12, respectively). The differences in the erosion velocities of Si and Al or Al compounds are rather insignificant, as apparent from Fig. 14b.

Because the calculations shown in Fig. 14 are an approximation, higher Al concentrations and different (albeit small) erosion velocities may result in differences in the surface evolution with and without Al co-deposition. This may be one reason for which the Si experiments conducted at incidence angles of 60° produced a more pronounced change in topography compared to the surface sputtered without Al co-deposition (Fig. 10f).

At present, there is no model that can predict all nanostructure formation and evolution induced by IBS on mono-elemental materials. The SiO$_2$ case should be more complex than a mono-elemental material such as Si. In this paper, we focused on pattern formation on SiO$_2$ with simultaneous Al co-deposition in comparison with Si. We hope this preliminary comparison of Si and SiO$_2$ will stimulate further investigations on the formation of IBS-induced nanostructures.

4 Conclusions

To conclude, we have investigated the IBS of SiO$_2$ with simultaneous Al co-deposition. The investigation extends the investigations of IBS with impurity co-deposition from a smooth mono-elemental material (Si) to a pre-rippled binary compound (SiO$_2$), from normal to oblique incidence angles, and from the Si products of Fe, Mo, etc, to AlO$_x$F$_y$ products.

The pattern generation and evolution in such a sputtering and co-deposition configuration are attributed to the interplay between ion beam sputtering of Ar$^+$ ion driven by a BH mechanism and the directional deposition of Al atoms. Amplified sputtering yields and erosion velocities are realized by AlO$_x$F$_y$ chemical products during IBS with concurrent Al deposition, and the AlO$_x$F$_y$ products function as micro-masking that significantly enhance the rms roughness of the surface morphology.

In the region where the rms roughness increased with increasing Al content, the coupling effect of the impurity co-deposition and the initial pre-rippling of the surface significantly roughens the morphology and enriches the pattern type, such that concurrent impurity deposition is demonstrated to improve the rms roughness of a smooth surface during IBS. The rms roughness of a surface can be further improved by changing the initial substrate from a smooth to a pre-rippled surface. Furthermore, 2D nanostructures and blazed nanograting have been found to form on pre-rippled SiO$_2$ surfaces, and these patterns offer significant potential in optical applications.

To understand the formation and development mechanisms of nanostructures and to tailor diverse nanopatterns in a deterministic way, further experimental work will focus on the impurity selection (such as using impurities that are either stable or easily oxidized), time evolution, geometric configurations of the sputtering and co-deposition system, and surfaces consisting of other binary compounds. A more comprehensive simulation is needed to predict quantitatively the results obtained by IBS with concurrent impurity co-deposition on pre-rippled surfaces.

In the paper, we confined most of our focus upon the investigation of smooth and pre-rippled SiO$_2$ surfaces. Some observations on smooth Si surface have been demonstrated in this paper. The investigation on smooth Si will be conducted in detail elsewhere.

The results reported here are not only helpful to understand the formation of nanopatterns induced by IBS with simultaneous impurity co-deposition, but are also of technological relevance to identify quantitatively the effects of non-intentional process contamination on the morphologies and rms roughnesses of optical surfaces during ion beam-assisted etching techniques. Low-energy IBS is a powerful and unique tool that can be used to prepare nanostructures in both destructive and constructive approaches [75]. We believe that the sputtering and co-deposition system investigated in this paper, also known as a surfactant sputtering system, integrates destructive (sputtering) and constructive (deposition) approaches to nanostructuring and can facilitate sputtering-deposition experiments that generate novel and versatile nanostructures with many potential applications.

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