Ultrafast Momentum-Resolved Hot Electron Dynamics in the Two-Dimensional Topological Insulator Bismuthene

Julian Maklar, Raul Stuhler, Maciej Dendzik, Tommaso Pincelli, Shuo Dong, Samuel Beaulieu, Alexander Neef, Gang Li, Martin Wolf, Ralph Ernstorfer, Ralph Claessen, and Laurenz Rettig*

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ABSTRACT: Two-dimensional quantum spin Hall (QSH) insulators are a promising material class for spintronic applications based on topologically protected spin currents in their edges. Yet, they have not lived up to their technological potential, as experimental realizations are scarce and limited to cryogenic temperatures. These constraints have also severely restricted characterization of their dynamical properties. Here, we report on the electron dynamics of the novel room-temperature QSH candidate bismuthene after photoexcitation using time- and angle-resolved photoemission spectroscopy. We map the transiently occupied conduction band and track the full relaxation pathway of hot photocarriers. Intriguingly, we observe photocarrier lifetimes much shorter than those in conventional semiconductors. This is ascribed to the presence of topological in-gap states already established by local probes. Indeed, we find spectral signatures consistent with these earlier findings. Demonstration of the large band gap and the view into photoelectron dynamics mark a critical step toward optical control of QSH functionalities.

KEYWORDS: Topological insulators, quantum spin Hall effect, bismuthene, time- and angle-resolved photoemission spectroscopy, trARPES, ultrafast carrier dynamics

A promising platform for spintronic devices are two-dimensional (2D) topological insulators (TIs). Based on the quantum spin Hall (QSH) effect, 2D TIs feature an insulating band structure in their interior (here referred to as 2D bulk) surrounded by metallic states at their edges. These helical edge states (ESs) are characterized by spin-momentum locking, allowing for spin currents with opposite polarization for forward- and backward-moving electrons. As they are topologically protected by time-reversal symmetry against single-particle backscattering, they also enable dissipationless transport. However, any practical application based on helical ESs requires a large bulk band gap preventing interference with thermally excited bulk carriers at room temperature. Thus, in addition to a thorough characterization of the ES properties, also mapping out the bulk valence and conduction bands is critical. Yet, so far band structure investigations of 2D TIs are scarce and an understanding of their dynamical properties and microscopic interactions, imperative for controlling QSH functionalities, is lacking.

A suitable approach to tackle these questions is time- and angle-resolved photoemission spectroscopy (trARPES), which has been pivotal for characterizing the electronic structure and fundamental interactions of 3D TIs, the 3D analogs of QSH insulators. This method grants direct access to the energy- and momentum-dependent electron dynamics after femtosecond optical excitation and to states that are not occupied in equilibrium. Thus, trARPES allows for mapping of the transiently populated states above the Fermi level, which has been essential for a clear separation of semiconducting bulk and metallic topological in-gap states in 3D TIs. Gaining a similar understanding of the electronic structure and elementary scattering processes of 2D TIs is of strong interest from both scientific and application perspectives.

A novel platform to address this knowledge gap is the room temperature QSH candidate bismuthene, that is, a monolayer of bismuth atoms arranged in a planar honeycomb geometry on a semiconducting silicon carbide SiC(0001) substrate. Spatially resolved scanning tunneling spectroscopy (STS) measurements have demonstrated a large band gap of ~0.8 eV in bulk areas, far greater than in any other QSH system, and conductive 1D states at exposed sample edges near substrate terrace steps, as illustrated in Figure 1a. Intriguingly, in topologically nontrivial materials, additional pairs of coupled ESs can arise within the bulk areas at extended 1D defects, recently observed within the 2D bulk of
bismuthene along structure-induced domain boundaries. However, a demonstration of the elusive ESs using a momentum-resolved probe has proven challenging, as they constitute only a marginal fraction of the total surface area. Furthermore, confirmation of the theoretically predicted large indirect bulk band gap of bismuthene and characterization of microscopic carrier scattering processes are still missing, as previous studies largely relied on momentum-integrating local probes. Here, we investigate the ultrafast electron dynamics of photoexcited bismuthene at room temperature using trARPES, as illustrated in Figure 1a, allowing us to access the microscopic scattering channels from the dynamics of the nonequilibrium state prepared by optical excitation. Combining a hemispherical analyzer and a time-of-flight momentum microscope for photoelectron detection, we map the transiently populated conduction band structure and confirm the existence of a wide indirect bulk band gap of ~0.82 eV. In addition, we identify faint gap-filling spectral weight that

![Figure 1. Experimental scheme and photoelectron constant-energy contours. (a) Illustration of the trARPES experiment. An optical pump pulse excites the bismuthene sample, followed by an XUV pulse that probes the electronic distribution after a time delay, Δt. The green and blue arrows represent the two spin channels of the coupled ESs at a domain boundary and of the exposed ESs at a substrate step edge. (b) Constant-energy contours with radius $k_\parallel \approx 2 \text{ Å}^{-1}$ of bismuthene after photoexcitation ($h\nu = 1.55 \text{ eV}, \Delta t = -75$ to $+75 \text{ fs}$). Two exemplary BZs and high-symmetry points are indicated.]

![Figure 2. Electronic band-structure maps. (a) False-color plots of the trARPES measurements of bismuthene along the $\bar{\Gamma}-\bar{K}$ direction (gray line in inset) in equilibrium and (b) after optical excitation ($h\nu = 1.55 \text{ eV}$, incident fluence $F = 0.50 \text{ mJ cm}^{-2}$, $\Delta t = -40$ to $+40 \text{ fs}$). The intensity in the inset is enhanced by a factor of 5. DFT band structure calculations (black) are adopted from Reis et al.14 (c) Differential photoemission intensity (pre-excitation signal subtracted) at $\Delta t = 0 \text{ fs}$. (d, e) Energy distribution curves (EDCs) (d) at $\bar{K}$ and (e) at $\bar{\Gamma}$ in equilibrium and after weak excitation ($F = 0.14 \text{ mJ cm}^{-2}, \Delta t = -40$ to $+40 \text{ fs}$, momentum-integration $\pm 0.05 \text{ Å}^{-1}$). The red dashed curves mark best fits as described in the text. The black arrow indicates the in-gap intensity extending into the conduction band upon photoexcitation (see discussion). The direct and indirect band gaps are marked in blue.]

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temporal pro-
a single-exponential decay convolved with a Gaussian (Gaussian width as free parameter). The window integration (Δt = 0 fs) are given with one standard deviation as uncertainty. Inset: dynamics near Δt = 0 fs. The gray dashed line indicates the temporal profile of the pump-laser pulse. (c) Temporal maximum t_{max} and (d) carrier lifetimes τ from bin-wise energy- and momentum-dependent decay fits. For this, the transient photoemission intensities are extracted across the energy-momentum region shown in panel a using a sliding-window integration (ΔE = 0.1 eV, Δk = 0.15 Å⁻¹) and fitted using the function described above. Regions with low photoemission intensity or large fit uncertainties (σ_{max} > 10 fs, σ_{t} > 40 fs) are masked in gray. (e) Schematic scattering processes within the DFT band structure (see text). The in-gap states are indicated in blue.

Figure 3. Carrier relaxation dynamics. (a) Excited-state band dispersion after 1.55 eV optical excitation (F = 0.50 mJ cm⁻²). (b) Normalized photoemission intensities corresponding to boxes 1–3 indicated in panel a as a function of pump-probe delay. The solid lines show best fits using a single-exponential decay convolved with a Gaussian (Gaussian width as free parameter). The fit parameters t_{max} (temporal intensity maximum) and τ (1/τ decay constant) are given with one standard deviation as uncertainty. Inset: dynamics near Δt = 0 fs. The gray dashed line indicates the temporal profile of the pump-laser pulse. (c) Temporal maximum t_{max} and (d) carrier lifetimes τ from bin-wise energy- and momentum-dependent decay fits. For this, the transient photoemission intensities are extracted across the energy-momentum region shown in panel a using a sliding-window integration (ΔE = 0.1 eV, Δk = 0.15 Å⁻¹) and fitted using the function described above. Regions with low photoemission intensity or large fit uncertainties (σ_{max} > 10 fs, σ_{t} > 40 fs) are masked in gray. (e) Schematic scattering processes within the DFT band structure (see text). The in-gap states are indicated in blue.

connects bulk valence and conduction bands, which we attribute largely to the topological ESs located at the structural domain boundaries of bismuthene.24 Tracking the full relaxation pathway of hot photocarriers across the entire first Brillouin zone (BZ) reveals a fast depletion of the transient relaxation pathway of hot photocarriers across the entire bulk band gap in the Dirac-like crossing at the K̅ points of the hexagonal BZ.27 Excitation with near-infrared optical pulses lifts charge carriers across the bulk band gap and transiently populates conduction band states localized at K̅ and, more pronounced, at the Γ̅ points of the first and second BZs 1 eV above the valence-band maximum (VBM). Next, we focus on a momentum cut along the Γ̅–K̅ direction, which features the region of the direct optical interband transition near K̅ and the conduction-band minimum (CBM) at Γ̅. Consistent with previous studies,14 the equilibrium band structure of bismuthene features sharp spin–orbit split low-energy valence bands at Γ̅ (Figure 2a). Upon optical excitation, a weak excited carrier population at K̅ and a distinct dispersive band at the CBM at Γ̅ emerge (Figures 2b,c). Concurrently, the valence bands at K̅ are depleted by the optical transition (blue colored region in Figure 2c), and their bandwidth broadens due to scattering of the photoholes with excited quasiparticles.28,29 Band-gap renormalization by photoexcitation is particularly pronounced in 2D materials due to reduced charge carrier screening.30,31 To minimize this effect, we extract the direct and indirect band gaps at temporal pump–probe overlap using a low incident fluence of 0.14 mJ cm⁻², as shown in Figures 2d,e. At K̅, we find a direct band gap of 1.05 ± 0.02 eV, extracted from the peak positions of Gaussian fits to the upper spin–orbit split band at the VBM and to the lowest-lying CB, which is in excellent agreement with density functional theory (DFT) calculations (1.07 eV14). The indirect band gap between the VBM at K̅ and the CBM at Γ̅ extracted using a Gaussian fit with an exponentially decaying background, amounts to 0.82 ± 0.02 eV, which is in reasonable correspondence with the DFT value of 0.67 eV.14 Furthermore, the experimental value also perfectly agrees with the momentum-integrated bulk band gap of ~0.8 eV obtained from STS measurements.14 We note that already at a low fluence of 0.14 mJ cm⁻², the indirect quasiparticle band gap is weakly renormalized by ~40 meV within 100 fs, resulting from the increased screening by quasi-free photocarriers (Supplementary Figure S2). For moderate fluences, we observe a significant initial band gap reduction by ~150 meV, followed by a transient recovery, in agreement with previous studies of
2D semiconductors. Additional measurements using 3.1 eV optical excitation, providing a larger view into the dispersion of the lowest-energy conduction band, are shown in Supplementary Figure S3.

Next, to elucidate the quasiparticle scattering channels in the photocarrier relaxation processes of bismuthene, we investigate the excited-state population dynamics after 1.55 eV optical excitation along the $\Gamma-K$ direction. As the transient photoemission intensities in Figure 3b show, a CB population builds up first near $\Gamma$ (box 1 in Figure 3a), reaching its maximum intensity at 27 fs. The apparent delay with respect to temporal pump–probe overlap is due to a buildup of the excited-state population at the $\bar{K}$ valley until the end of the pump laser pulse, see the inset in Figure 3b. Subsequently, carriers appear at $\Gamma$ (box 2) with a delay of 40 fs, and last a faint intensity within the bulk band gap at $\Gamma$ (box 3) builds up, followed by a complete recovery on a time scale of 1 ps. We quantify these dynamics by employing single-exponential decay fits, characterized by the time delay at which the excited-state population reaches the maximum, $t_{\text{max}}$, and the 1/e lifetime, $\tau$. To establish the full energy- and momentum-dependent scattering pathway, we extend this evaluation of three exemplary areas by fitting the transient intensity of each energy–momentum bin across Figure 3a using a sliding integration window. The resulting energy–momentum maps of the fit parameters $t_{\text{max}}$ and $\tau$ allow us to track the arrival time of excited carriers in energy–momentum space (Figure 3c) and provide a concise overview of the lifetimes associated with particular states (Figure 3d).

Combining the results of both maps yields a detailed picture of the complete carrier relaxation pathway, schematically depicted in Figure 3e: (1) Carriers are initially injected by a vertical interband transition into the CB near $\bar{K}$ using 1.55 eV radiation. (2) The hot electrons redistribute by intervalley scattering, which spreads the carriers over an extended momentum region into the $\Gamma$ valley on a 10 fs time scale, a phenomenon commonly observed in photoexcited semiconductors. (3) Subsequently, hot carriers relax toward the CBM at $\Gamma$ via electron–electron and electron–phonon scattering within 50 fs. Although bulk bismuthene exhibits an indirect band gap of nearly 1 eV, the lifetime of the conduction band population is only on the order of few 100 fs, an orders of magnitude faster relaxation than in conventional indirect semiconductors. (4) These ultrashort lifetimes indicate a highly efficient carrier relaxation. The question naturally arises which states other than the insulating 2D bulk states in bismuthene could mediate the observed fast decay. Intriguingly, we observe faint gap-filling spectral weight reaching up to the CBM for several 100 fs after photoexcitation (Supplementary Figure S4), which we discuss below. A relaxation of the conduction band population through these in-gap states is supported by the fact that they are populated last and feature the longest lifetimes. Finally, within ~1.5 ps, also the in-gap states above the VBM are fully depleted. Note that the extracted population lifetimes are distinct from single-particle lifetimes that are directly encoded in the electron self-energy, and thus only represent an upper limit for the time scale of scattering processes.

Lastly, we examine the in-gap spectral weight, and we discuss its origin. We find that already in equilibrium a faint intensity is located at $\Gamma$ reaching up to $E_{\text{CBM}}$ (Figure 4a). Upon optical excitation, the in-gap intensity extends into the CBM (Figure 4b), resulting in the absence of an explicit gap between bulk conduction and valence bands (black arrow in Figure 2e). While it may seem obvious to assign the in-gap feature to the topological ESs that were directly probed in previous STM/STS studies, a careful examination is required.

For that, we compare the relaxation dynamics and the in-gap feature for bismuthene grown on two different substrate types, that is, intentionally miscut and planar SiC substrates (Supplementary Figure S1). Using a miscut substrate yields a high density of unidirectional, topologically protected exposed ES along the parallel substrate step edges, as illustrated in Figure 4c, while bismuthene prepared on a planar substrate features only a negligible density of (randomly oriented) substrate steps with exposed ESs. Yet, for both substrate types, additional topological ESs arise at structural phase-slip domain boundaries within the 2D bulk of bismuthene. These domain boundaries result from the fact that the $(\sqrt{3} \times \sqrt{3})$ Bi honeycombs can have three distinct registries with respect to the substrate lattice, causing the growth of domains. Pairs of helical ESs emerge at the zigzag edges on either side of these boundaries, see Figure 4d, lifting the topological protection through mutual hybridization and leading to a mixing of
different helicities, as confirmed by local tunneling spectroscopy.24

The presented characterization of the in-gap feature and relaxation dynamics was conducted on bismuthene prepared on a miscut substrate. However, in bismuthene prepared on a planar substrate featuring only a negligible density of exposed ESs, equivalent relaxation dynamics (Supplementary Figure S5) and a similar in-gap feature (Supplementary Figures S4 and S6) are observed. This leads us to the conclusion that the in-gap intensity primarily originates from topological ESs that arise at structural domain boundaries, which are present in both planar and miscut samples. The faint intensity of the in-gap states on the order of a few percent of the bismuthene bulk bands at K is consistent with the assignment to coupled ESs, as the domain boundaries constitute only a fraction of the probed surface. We further conclude that the relaxation of excited-state charge carriers must be strongly facilitated by the quasi-metallic density of states observed at such domain boundaries, enabling the rapid depletion of the conduction band population, analogous to the depletion of conduction band populations by topological surface states in photoexcited 3D TIs.25 Since we do not observe large deviations for the decay times in the case of the bismuthene sample grown on a miscut substrate (Supplementary Figure S5), any definition on the additional role of the exposed topological ESs is difficult to draw at this point. Future developments in (time-resolved) nano-ARPES featuring a nanometer spatial resolution may allow isolation of the spectral features of exposed ESs at substrate terrace steps and individual pairs of coupled ESs at domain boundaries.

While the coupled ESs at domain boundaries consistently explain the in-gap spectral weight and short photocarrier lifetimes, several alternative scenarios can potentially induce a continuous in-gap intensity. First, impurities and defects may provide additional states within the bulk band gap. However, STM/STS studies show that only domain boundaries and exposed sample edges host in-gap states, while all other sample regions remain fully gapped.18,21,24 In addition, the observed confinement of the in-gap intensity to the momentum-region near the Fermi level. However, analogous to the first line of argument, spatially resolved STS measurements unambiguously demonstrate insulating behavior in bulk regions,14 indicating that the observed continuous in-gap intensity is not connected to bulk bismuthene but rather to ESs. Thus, by excluding alternative interpretations and consistent with earlier local tunneling spectroscopy results,24 we assign the in-gap spectral weight largely to coupled ESs at domain boundaries. As ESs forming along extended 1D defects critically limit the lifetime of excited carriers and may also pose challenges for applications utilizing the spin-selective transport along exposed sample edges,24 our study underlines the need for high-quality sample surfaces.

In conclusion, we experimentally mapped the electronic band structure of the quantum spin Hall insulator bismuthene after near-infrared photoexcitation and determined the direct and indirect band gaps of ∼1.1 eV and ∼0.8 eV, respectively. Analysis of the microscopic scattering pathway of hot photocarriers revealed exceptionally fast carrier relaxation dynamics governed by faint in-gap states located within the indirect band gap, which correspond with the topological edge states arising at bismuthene domain boundaries. The demonstration of a large fundamental band gap and the in-gap spectral weight persisting at room temperature and under strong optical excitation highlight the promising role of bismuthene as an ambient-condition quantum spin Hall candidate. Additionally, due to the exceptionally large band gap, bismuthene serves as a unique platform for optically addressing novel functionalities based on the topological edge states and for studying excitons in a topologically nontrivial system. Our insights gained on quasiparticle scattering processes lays the basis for future studies of sub-band gap excitations and optical control schemes of edge-state currents.24,44

# METHODS

Sample Preparation and STM Measurements. Bismuthene was epitaxially grown on n-doped 4H-SiC(0001) substrates (0.01–0.03 Ω-cm, carrier concentration ~1018–1019 cm−3, planar and 4° miscut) in ultrahigh vacuum <10−10 mbar. Prior to growth, a smooth H-terminated SiC surface was prepared by hydrogen-based dry-etching. Growth was performed at ∼600 °C to thermally desorb the surface H-termination, while simultaneously offering Bi atoms from a commercial effusion cell.14 Successful growth of low-defect bismuthene samples was verified using low-energy electron diffraction and scanning tunneling microscopy.

Time-Resolved ARPES Measurements. After characterization, the samples were transferred to the trARPES setup using an UHV suitcase at p < 10−10 mbar. All measurements were performed at room temperature using a laser-based high-harmonic-generation trARPES setup (p-polarized probe at hv = 21.7 eV, s-polarized pump at hv = 1.55, 3.10 eV, 500 kHz repetition rate, ΔE ≈ 150 meV, Δt ≈ 40 fs) with a 6-axis manipulator (SPECS Carving).25 Photoelectrons were detected with either a hemispherical analyzer (SPECS Phoibos 150) or a time-of-flight momentum microscope (SPECS METIS 1000).26 The momentum microscope allows for parallel acquisition of the 3D photoelectron distribution I(qi, k∥, E) across a large energy and momentum range and was thus utilized for overview measurements of the electronic band structure (Figure 1). In contrast, the hemispherical analyzer allows for fast data acquisition within a limited energy-momentum window, and was thus used to map selected high-symmetry directions (Figures 2−4). The data presented in Figure 1 were acquired on a planar substrate and that in Figures 2−4 on a miscut substrate. The extreme ultraviolet (XUV) probe spot size (fwhm) was ~80 × 80 μm2. The pump spot sizes were ~260 × 200 μm2 (hv = 1.55 eV) and ~510 × 475 μm2 (hv = 3.10 eV). All fluences stated in the text correspond to incident fluences. Temporal pump–probe overlap was determined from the pump-laser-induced depletion of the valence band population, as shown in Supplementary Figure S7.

# ASSOCIATED CONTENT

* Supporting Information The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.2c01462.

STM and LEED surface characterization of the bismuthene samples, characterization of the time-dependent quasiparticle band gap, mapping of the
conduction-band dispersion after 3 eV optical excitation, additional trARPES characterization of the in-gap spectral weight, and determination of temporal pump–probe overlap (PDF).

■ AUTHOR INFORMATION

Corresponding Author
Laurenz Rettig – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany; Email: rettig@fhi-berlin.mpg.de

Authors
Julian Maklar – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany; orcid.org/0000-0003-4123-4455
Raul Stühler – Physikalisches Institut und Würzburg-Dresden Cluster of Excellence c.t.qmat, University of Würzburg, D-97070 Würzburg, Germany
Maciej Dendzik – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany; Present Address: Department of Applied Physics, KTH Royal Institute of Technology, Hannes Alfvins v 12, 114 19 Stockholm, Sweden
Tommaso Pinelli – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany
Shuo Dong – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany
Samuel Beaulieu – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany; orcid.org/0000-0001-6665-3520
Alexander Neef – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany
Gang Li – School of Physical Science and Technology, ShanghaiTech University, Shanghai 200031, China
Martin Wolf – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany
Ralph Ernststörfer – Fritz-Haber-Institut der Max-Planck-Gesellschaft, D-14195 Berlin, Germany; Institut für Optik und Atomare Physik, Technische Universität Berlin, 10623 Berlin, Germany; orcid.org/0000-0001-6665-3520
Ralph Claessen – Physikalisches Institut und Würzburg-Dresden Cluster of Excellence c.t.qmat, University of Würzburg, D-97070 Würzburg, Germany

Complete contact information is available at: https://pubs.acs.org/10.1021/acs.nanolett.2c01462

Author Contributions
J.M., M.D., R.S., S.D., S.B., T.P., A.N., and L.R. carried out the trARPES experiments; J.M. analyzed the trARPES data with support from R.S.; R.S. prepared and characterized the samples and analyzed the STM data; G.L. performed the DFT calculations; J.M. wrote the manuscript with support from L.R., R.S., R.E., and R.C.; L.R., R.E., M.W., and R.C. provided the experimental infrastructure; all authors commented on the paper.

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■ REFERENCES

(1) Avsar, A.; Ochoa, H.; Guinea, F.; Özyilmaz, B.; van Wees, B.; Vera-Marun, I. J. Colloquium: Spintronics in graphene and other two-dimensional materials. Rev. Mod. Phys. 2020, 92, 021003.
(2) Hasan, M. Z.; Kane, C. L. Colloquium: topological insulators. Rev. Mod. Phys. 2010, 82, 3045.
(3) Kane, C. L.; Mele, E. J. Quantum spin Hall effect in graphene. Phys. Rev. Lett. 2005, 95, 226801.
(4) Tang, S.; Zhang, C.; Wong, D.; Pedramrazi, Z.; Tsai, H.-Z.; Jia, C.; Moritz, B.; Claassen, M.; Ryu, H.; Kahn, S.; et al. Quantum spin Hall state in monolayer 1T’-WTe2. Nat. Phys. 2017, 13, 683–687.
(5) Chen, P.; Pai, W. W.; Chan, Y.-H.; Sun, W.-L.; Xu, C.-Z.; Lin, D.-S.; Chou, M.; Fedorov, A.-V.; Chiang, T.-C. Large quantum-spin-Hall gap in single-layer 1T’-WSe2. Nat. Commun. 2018, 9, 2003.
(6) Wu, R.; Ma, J.-Z.; Nie, S.-M.; Zhao, L.-X.; Huang, X.; Yin, J.-X.; Fu, B.-B.; Richard, P.; Chen, G.-F.; Fang, Z.; et al. Evidence for topological edge states in a large energy gap near the step edges on the surface of ZrTe5. Phys. Rev. X 2016, 6, 021017.
(7) Wang, Y.; Hsieh, D.; Sie, E.; Steinberg, H.; Gardner, D.; Lee, Y.; Jarillo-Herrero, P.; Gedik, N. Measurement of intrinsic Dirac fermion cooling on the surface of the topological insulator Bi2Se3 using time-resolved and angle-resolved photoemission spectroscopy. Phys. Rev. Lett. 2012, 109, 127401.
(8) Sobota, J. A.; Yang, S.; Analytis, J. G.; Chen, Y.; Fisher, I. R.; Kirchmann, P. S.; Shen, Z.-X. Ultrafast optical excitation of a persistent surface-state population in the topological insulator Bi2Se3. Phys. Rev. Lett. 2012, 108, 114703.
(9) Sobota, J. A.; Yang, S.-L.; Leuenberger, D.; Kemper, A. F.; Analytis, J. G.; Fisher, I. R.; Kirchmann, P. S.; Devereaux, T. P.; Shen, Z.-X. Distinguishing bulk and surface electron-phonon coupling in the topological insulator Bi2Se3 using time-resolved photoemission spectroscopy. Phys. Rev. Lett. 2014, 113, 157401.
(10) Cacho, C.; Crepaldi, A.; Battisti, M.; Braun, J.; Cilento, F.; Zacchigna, M.; Richter, M.; Beckmann, O.; Springate, E.; Liu, Y.; et al. Momentum-resolved spin dynamics of bulk and surface excited states in the topological insulator Bi2Se3, Phys. Rev. Lett. 2015, 114, 097401.
(11) Neupane, M.; Xu, S.-Y.; Ishida, Y.; Jia, S.; Fregoso, B. M.; Liu, C.; Belopolski, I.; Bian, G.; Aldoust, N.; Durakiewicz, T.; et al. Gigantic surface lifetime of an intrinsic topological insulator. Phys. Rev. Lett. 2015, 115, 116801.
(12) Sumida, K.; Kakoki, M.; Reimann, J.; Nurammadi, M.; Goto, S.; Takeda, Y.; Saitoh, Y.; Kohk, K.; Tereshchenko, O.; G"{u}dde, J.; et al. Magnetic-impurity-induced modifications to ultrafast carrier dynamics in the ferromagnetic topological insulators $\text{Sb}_2\text{V}_3\text{Te}_6$. New J. Phys. 2019, 21, 093006.

(13) Reimann, J.; Schluderer, S.; Schmid, C.; Langer, F.; Baierl, S.; Kohk, K.; Tereshchenko, O.; Kimura, A.; Lange, C.; G"{u}dde, J.; et al. Subcycle observation of lightwave-driven Dirac currents in a topological surface band. Nature 2018, 562, 396–400.

(14) Reis, F.; Li, G.; Dudy, L.; Bauenfeind, M.; Glass, S.; Hanke, W.; Thomale, R.; Schaefer, J.; Claessen, R. Bismuthene on a SiC substrate: A candidate for a high-temperature quantum spin Hall material. Science 2017, 357, 287–290.

(15) König, M.; Wiedmann, S.; Brüne, C.; Roth, A.; Buhmann, H.; Molenkamp, L. W.; Qi, X.-L.; Zhang, S.-C. Quantum spin Hall insulator state in HgTe quantum wells. Science 2007, 318, 766–770.

(16) Knez, I.; Du, R.-R.; Sullivan, G. Evidence for Helical Edge Modes in Inverted InAs/GaSb Quantum Wells. Phys. Rev. Lett. 2011, 107, 136603.

(17) Leubner, P.; Lunczer, L.; Brüne, C.; Buhmann, H.; Molenkamp, L. W. Strain engineering of the band gap of HgTe quantum wells using superlattice virtual substrates. Phys. Rev. Lett. 2016, 117, 086403.

(18) Fei, Z.; Palomaki, T.; Wu, S.; Zhao, W.; Cai, X.; Sun, B.; Nguyen, P.; Finney, J.; Xu, X.; Cobden, D. H. Edge conduction in monolayer WTe$_2$. Nat. Phys. 2017, 13, 677–682.

(19) Wu, S.; Fatemi, V.; Gibson, Q. D.; Watanabe, K.; Taniguchi, T.; Cava, R. J.; Jarillo-Herrero, P. Observation of the quantum spin Hall effect up to 100 K in a monolayer crystal. Science 2018, 359, 76–79.

(20) Sun, S.; et al. Epitaxial Growth of Ultraflat Bismuthene with Large Topological Band Inversion Enabled by Substrate-Orbital-Filtering Effect. ACS Nano 2022, 16, 1436–1443.

(21) Stühler, R.; Reis, F.; Müller, T.; Helbig, T.; Schwemmer, T.; Thomale, R.; Schäfer, J.; Claessen, R. Tomonaga−Luttinger liquid in the edge channels of a quantum spin Hall insulator. Nat. Phys. 2020, 16, 47–51.

(22) Lima, E. N.; Schmidt, T. M.; Nunes, R. W. Topologically protected metallic states induced by a one-dimensional extended defect in the bulk of a 2D topological insulator. Nano Lett. 2016, 16, 4025–4031.

(23) Pezo, A.; Focaccio, B.; Schleder, G. R.; Costa, M.; Schröter, N. B. M.; Wang, X.; Krieger, J. Structure and impurity systems by soft-X-ray ARPES. J. Electron Spectrosc. Relat. Phenom. 2019, 236, 1–8.

(24) Stein, M.; et al. Observation of an Excitonic Mott Transition through Ultrafast Core-cum-Conduction Photoemission Spectroscopy. Phys. Rev. Lett. 2020, 125, 096401.

(25) Liu, F.; Ziffer, M. E.; Hansen, K. R.; Wang, J.; Zhu, X. Direct determination of band-gap renormalization in the photoexcited monolayer MoS$_2$. Phys. Rev. Lett. 2019, 122, 246803.

(26) Ulstrup, S.; Cabo, A. G.; Miwa, J. A.; Riley, J. M.; Grenborg, S. I.; Johannsen, J. C.; Cacho, C.; Alexander, O.; Chapman, R. T.; Springate, E.; Bianchi, M.; Dendzik, M.; Lauritzen, J. V.; King, P. D. C.; Hofmann, P. Ultrafast Band Structure Control of a Two-Dimensional Heterostructure. ACS Nano 2016, 10, 6315–6322.

(27) Berton, R.; Nicholson, C. W.; Waldecker, L.; Hübner, H.; Monney, C.; De Giovanni, U.; Puppin, M.; Hoesch, M.; Springate, E.; Chapman, R. T.; et al. Generation and evolution of spin-, valley- and layer-polarized excited carriers in inversion-symmetric WSe$_2$. Phys. Rev. Lett. 2016, 117, 277201.

(28) Hein, P.; Stange, A.; Hanff, K.; Yang, L.; Rohde, G.; Rossnagel, K.; Bauer, M. Momentum-resolved hot electron dynamics at the 2H-MoS$_2$ surface. Phys. Rev. B 2016, 94, 205406.

(29) Madéo, J.; Man, M. K.; Sahoo, C.; Campbell, M.; Pareek, V.; Wong, E. L.; Al-Mahboob, A.; Chan, N. S.; Karmakar, A.; Marisela, B. M. K.; et al. Directly visualizing the momentum-forbidden dark excitons and their dynamics in atomically thin semiconductors. Science 2020, 370, 1199–1204.

(30) Dong, S.; et al. Direct measurement of key exciton properties: Energy, dynamics, and spatial distribution of the wave function. Nat. Sci. 2021, 1, e10010.

(31) Schroder, D. K. Semiconductor Material and Device Characterization; John Wiley & Sons, Ltd: Hoboken, NJ, 2005.

(32) Wang, H.; Zhang, C.; Rana, F. Surface recombination limited lifetimes of photoexcited carriers in few-layer transition metal dichalcogenide MoS$_2$. Nano Lett. 2015, 15, 8204–8210.

(33) Li, J.; Goryca, M.; Yamigeta, K.; Li, H.; Tongay, S.; Crooker, S. A. Valley relaxation of resident electrons and holes in a monolayer semiconductor: Dependence on carrier density and the role of substrate-induced disorder. Phys. Rev. Mater. 2021, 5, 044001.

(34) Lee, W.; Lin, Y.; Lu, L.-S.; Chuieh, W.-C.; Liu, M.; Li, X.; Chang, W.-H.; Kaindl, R. A.; Shih, C.-K. Time-Resolved ARPES Determination of a Quasi-Particle Band Gap and Hot Electron Dynamics in Monolayer MoS$_2$. Nano Lett. 2021, 21, 7363–7370.

(35) Yang, S.-L.; Sobota, J. A.; Leuenberger, D.; He, Y.; Hashimoto, M.; Lu, D. H.; Eisaki, H.; Kirchmann, P. S.; Shen, Z.-X. Inequivalence of Single-Particle and Population Lifetimes in a Cuprate Superconductor. Phys. Rev. Lett. 2015, 114, 247001.

(36) Kemper, A. F.; Abdurazakov, O.; Freericks, J. K. General Principles for the Nonequilibrium Relaxation of Populations in Quantum Materials. Phys. Rev. X 2018, 8, 041009.

(37) Strolov, V. N.; Lev, L. L.; Kobayashi, M.; Cancellieri, C.; Husanu, M.-A.; Chikina, A.; Schönlein, N. B. M.; Wang, X.; Krieger, J. A.; Salman, Z. k-resolved electronic structure of buried heterostructure and impurity systems by soft-X-ray ARUPS. J. Electron Spectrosc. Relat. Phenom. 2019, 236, 1–8.

(38) Tiwari, S.; Van de Put, M. L.; Sorée, B.; Vandenberge, W. G. Carrier transport in two-dimensional topological insulator nanoribbons in the presence of vacancy defects. 2D Mater. 2019, 6, 025011.

(39) McIver, J. W.; Hsieh, D. I.; Steinberg, H.; Jarillo-Herrero, P.; Gedik, N. Control over topological insulator photocurrents with light polarization. Nat. Nanotechnol. 2012, 7, 96–100.

(40) Kuroda, R.; Reimann, J.; Kohk, K. A.; Tereshchenko, O. E.; Kimura, A.; G"{u}dde, J.; H"{o}fer, U. Ultrafast energy- and momentum-resolved surface Dirac photocurrents in the topological insulator $\text{Sb}_2\text{Te}_3$. Phys. Rev. B 2017, 95, 081103.