EVOLUTION OF COLD STREAMS AND THE EMERGENCE OF THE HUBBLE SEQUENCE

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ABSTRACT
A new physical framework for the emergence of the Hubble sequence is outlined, based on novel analyses performed to quantify the evolution of cold streams of a large sample of galaxies from a state-of-the-art ultra-high resolution, large-scale adaptive mesh-refinement hydrodynamic simulation in a fully cosmological setting. It is found that the following three key physical variables of galactic cold inflows crossing the virial sphere substantially decrease with decreasing redshift: the number of streams \( N_{\text{90}} \) that make up 90% of concurrent inflow mass flux, average inflow rate per stream \( M_{\text{90}} \) and mean (mass flux weighted) gas density in the streams \( n_{\text{gas}} \). Another key variable, the stream dimensionless angular momentum parameter \( \lambda \), is found to instead increase with decreasing redshift. Assimilating these trends and others naturally leads to a physically coherent scenario for the emergence of the Hubble sequence, including the following expectations: (1) the predominance of a mixture of disproportionately small irregular and complex disk galaxies at \( z \gtrsim 2 \) when most galaxies have multiple concurrent streams, (2) the beginning of the appearance of flocculent spirals at \( z \sim 1-2 \) when the number of concurrent streams are about \( 2-3 \), (3) the grand-design spiral galaxies appear at \( z \lesssim 1 \) when galaxies with only one major cold stream significantly emerge. These expected general trends are in good accord with observations. Early-type galaxies are those that have entered a perennial state of zero cold gas stream, with their abundance increasing with decreasing redshift.

Key words: cosmology: theory – galaxies: formation – galaxies: high-redshift – galaxies: interactions – hydrodynamics – methods: numerical

Online-only material: color figures

1. INTRODUCTION
Despite the commendable successes, a systematic physical theory for the origin of the Hubble (1926) sequence—the holy grail of galaxy formation—remains elusive. While the greatly increased richness in observational data has prompted revisions in the classification (van den Bergh 1976; Sandage & Binggeli 1989; Cappellari et al. 2011; Kormendy & Bender 2012) that have provided more coherence along each sequence and counterpart identifications across different sequences (e.g., S0 versus S sequences), it has not, for the most part, significantly improved the clarity of our physical understanding of the Hubble sequence. It seems that this perpetual state of perplexity does not stem from a lack of freedom to parameterize input physics, such as in the semi-analytic and other phenomenological approaches. Rather, there are key physical ingredients that are not understood to even be parameterized. One such physical ingredient is the environment, which is a difficult problem to address computationally, due to the twin requirements of capturing the large-scale environment and small-scale structure, and to parameterize due to diversity. Our recent analysis has shown that the quenching and color migration for the vast majority of galaxies may be primarily due to environment effects (Cen 2014b), which has recently received significant observational support (e.g., Lin et al. 2014; Carollo et al. 2014; Muzzin et al. 2014).

There is enough both direct evidence and theoretical insights gained in galaxy interactions (e.g., Mihos & Hernquist 1996) or analyses (e.g., Fall & Efstathiou 1980; Mo et al. 1998) to conclude that angular momentum is another key physical ingredient in galaxy formation theory. The possibility that the angular momentum dynamics of gas accretion is complex in a cosmological setting and different from that of dark matter (Bullock et al. 2001) is under-appreciated. Recent studies have begun to show that angular momentum dynamics of gas and stars in the inner regions are only loosely, at best, related to that of dark matter halos (e.g., Hahn et al. 2010; Cen 2014a). One could suggest that the diversity of galaxies and their evolution—the Hubble sequence and its emergence—may be substantially governed by the complexity and trends of dynamics of cold (\( T < 10^5 \) K) gas streams with respect to their number, mass flux, density, and angular momentum, since they provide the main fuel for galaxy formation. Such suggestion is, so far, without formal proof. This study provides analyses on cold streams, utilizing a large sample of ultra-highly resolved galaxies from an ab initio Large-scale Adaptive-mesh-refinement Omniscient Zoom-In cosmological hydrodynamic simulation of the standard cold dark matter model. It is shown that the cold gas accretion flows display physical trends that can provide a self-consistent account for the origin of the emergence of the Hubble sequence. This study is built on insights from recent innovative work (Kereš et al. 2005; Dekel & Birnboim 2006; Nelson et al. 2013) that suggests, to varying degrees, a two-mode gas accretion onto galaxies, in contrast to the classic description of gas cooling following virialization heating (Rees & Ostriker 1977; Silk 1977; Binney 1977; White & Rees 1978). There are currently significant quantitative differences concerning the cold streams from different simulation groups (see references above), which may be, in part, due to different tracking methods. The method for identifying cold gas streams described in Section 2 may be used to enable a uniform comparison. This Letter is the fourth in the series “On the Origin of the Hubble Sequence.”

2. COSMOLOGICAL SIMULATIONS AND IDENTIFICATION OF COLD STREAMS
The reader is referred to Cen (2014b) for detailed descriptions of our simulations. Briefly, a zoom-in region of comoving size of \( 21 \times 24 \times 20 h^{-3} \) Mpc\(^3\) is embedded in a \( 120 h^{-1} \) Mpc
periodic box and resolved at 114$ h^{-1}$ pc physical. Cosmological parameters are from WMAP7 (Komatsu et al. 2011): $\Omega_M = 0.28$, $\Omega_b = 0.046$, $\Omega_{\Lambda} = 0.72$, $\sigma_8 = 0.82$, $H_0 = 100 h$ km s$^{-1}$ Mpc$^{-1} = 70$ km s$^{-1}$ Mpc$^{-1}$ and $n = 0.96$. The zoom-in region is centered on a cluster of mass of $\sim 3 \times 10^{14} M_{\odot}$ at $z = 0$, and hence represents a 1.8$ r_e$ fluctuation for the volume. As a result, the development of structure formation is somewhat more advanced compared to that of the cosmic mean, and we take that into account when drawing conclusions with respect to the universe as a whole. Equations governing motions of dark matter, gas and stars, and the thermodynamic state of gas are followed, using the adaptive mesh refinement cosmological hydrodynamic code Enzo (Bryan et al. 2014). The simulations include a metagalactic UV background (Haardt & Madau 2012) with self-shielding (Cen et al. 2005), a metallicity-dependent radiative cooling (Cen et al. 2014). Star particles are created in cells that satisfy a set of criteria (Cen & Ostriker 1992), essentially equivalent to the Kennicutt (1998) law. Each star particle is tagged with its initial mass, creation time, and metallicity; star particles typically have masses of $\sim 10^6 M_{\odot}$. Supernova feedback from star formation is modeled following Cen et al. (2005). At any epoch stellar particles are grouped using HOP (Eisenstein & Hut 1998) to create galaxy catalogs. For each galaxy we have its exact star formation history, given its member stellar particles formation times. None of the galaxies used in the analysis contains more than 1% in mass, within the virial radius, of dark matter particles other than the finest particles. Galaxy catalogs are constructed from $z = 0.62$ to $z = 1.40$ at a redshift increment of $\Delta z = 0.02$ and from $z = 1.40$ to $z = 6$ at a redshift increment of $\Delta z = 0.05$. Thus, when we say, for example, galaxies of stellar masses $10^{10}$–$10^{11} M_{\odot}$ in the redshift range $z = 2$–3, it means that we include galaxies with stellar masses from $10^{10}$ to $10^{11} M_{\odot}$ from 21 snapshots ($z = 2, 2.05, \ldots, 2.95, 3$). For the four redshift ranges analyzed, $z = (0.62$–1, 1–2, 2–3, 3–4), there are (5754, 9395, 4522, 1507) galaxies of stellar mass in the range $10^{10}$–$10^{11} M_{\odot}$, and (628, 964, 232, 28) galaxies of stellar mass in the range $10^{11}$–$10^{12} M_{\odot}$.

Proper identification of gas streams has not been demonstrated so far. Visual inspection may be able to pick out prominent ones, although it lacks the ability to separate out multi-stream streams and becomes impractical for large samples. Real-space searches for filamentary structures for large-scale structures have enjoyed some success (e.g., Bond et al. 2010), but the following two issues make them less usable for gas streams. First, non-radial streams could easily bend during travel, possibly resembling structures that may look like spirals; even radial streams will bend due to fluid drag. Second, gas along a stream is generally broken up (due to thermal and gravitational instabilities as well as other interactions) to look more like a pearl necklace than a creek. We have explored using some constants of motion to devise an automated scheme and finally focused on the angular momentum vector. We find that the following two variables—the amplitude of the total specific angular momentum ($J$) and the cosine of the angle $[\cos(\theta)]$ between the total specific angular momentum and a fixed vector (say, $z$ direction)—define a parameter space for identifying and separating out co-evol distinct streams.

Operationally, for a galaxy we accumulate inflow gas flux in the radial range ($1$–$1.3$)$ r_e$ ($r_e$ = virial radius) in the $J$ = $\cos(\theta)$ plane with $50 \times 50$ grid points, uniformly spanning the $J$ range $[0, 20] \times 10^5$ km s$^{-1}$ kpc and $\cos(\theta)$ range $[-1, 1]$. Inflow gas is defined as gas with the radial component of its velocity pointing to the center. Only gas with $T \leq 10^5$ K is included. The mass flux of each fluid cell $i$ in the radial range ($1$–$1.3$)$ r_e$ is computed as $4 \pi \rho_i v_i r_i^2 / (\Delta x_i / r_i^2)$, where $\rho_i$ is gas density, $v_i$ the radial velocity, $\Delta x_i$ the cell size, $r_i$ radial distance from the center, and the sum is performed over all cells in the radial range. The $4 \pi$ and the sum term serve to ensure that fluxes are properly normalized, when all the gas cells in the radial shell are collected, regardless of the thickness of the radial shell. Once mass fluxes are accumulated in the two-dimensional (2D) parameter plane, smoothing is applied to smooth out fluctuations among adjacent entries in the 2D phase plane. The choice of the smoothing window size does not alter the results in a material way, as long as oversmoothing is avoided; a three-point boxcar smoothing is used. With the smoothed flux map, we employ a procedure analogous to the DENMAX scheme used to identify dark matter halos (Gelb & Bertschinger 1994). Each entry is propagated along the steepest uphill gradient until it reaches a local maximum of flux and is said to belong to that local maximum. All entries in the 2D plane belonging to a same maximum are collected together to define one distinct stream, with a number of attributes, including the mean location in the parameter plane, total flux, flux-weighted gas density, and temperature. We rank order the streams according to their fluxes, and define $N_{90}$ as the top number of streams that make up 90% of the total concurrent cold gas inflow rate. If the 90% falls between two streams, we linearly interpolate to find $N_{90}$, which hence could be a non-integer. When there is no significant stream, $N_{90} = 0$. Figure 1 demonstrates how well this phase-space identification scheme works. For this galaxy at $z = 3$, the identification scheme finds nine significant streams with the top three streams making up 90% of the cold influx. Even through it is not easy to visually discern all streams, it appears that nine are consistent with the three-dimensional (3D) rendering in the top panel. The fact that the scheme picks out nine streams in this complex setting is a convincing demonstration of its efficacy. It is evident that there are indeed three major streams around the virial sphere, seen as three prominent yellow tubes with purple spines. Part of the motivation of this Letter is to demonstrate this method of cold stream identification in a complex cosmological setting that may be used by other authors.

3. RESULTS

Figure 2 shows the probability distribution function (PDF) of the number of streams ($N_{90}$). The three most important trends are immediately visible. First, larger galaxies tend to have more streams at $z > 2$, although for the two mass ranges considered the differences become insignificant at $z \lesssim 2$. Second, $N_{90}$ steadily and significantly decreases with decreasing redshift. The median $N_{90}$ is $(2.3, 4.0)$ for $(10^{10}$–$10^{11}, 10^{11}$–$10^{12}) M_{\odot}$ galaxies at $z = 3$–4, which becomes $(2.0, 3.5)$ at $z = 2$–3, $(1.6, 1.9)$ at $z = 1$–2 and $(1.0, 1.6)$ at $z = 0$. Third, the rate of decrease of $N_{90}$ with decreasing redshift appears to be faster for the higher-mass galaxies.

Figure 3 shows the PDF of cold inflow rate per stream, $\dot{M}_{90}$, defined as 90% of the total cold accretion rate divided by $N_{90}$. There is a significant decline with decreasing redshift, with the median $\dot{M}_{90}$ being $(33, 52)$ $M_{\odot}$ yr$^{-1}$ for $(10^{10}$–$10^{11}, 10^{11}$–$10^{12}) M_{\odot}$ galaxies at $z = 3$–4, declining to $(21, 50)$ $M_{\odot}$ yr$^{-1}$ at $z = 2$–3, $(13, 20)$ $M_{\odot}$ yr$^{-1}$ at $z = 1$–2 and $(5, 8)$ $M_{\odot}$ yr$^{-1}$ at $z = 0$. The rapid decrease of both $\dot{M}_{90}$ and $N_{90}$ (seen in Figure 2) with decreasing redshift makes it clear that the total cold gas inflow rate has experienced a very dramatic decline with decreasing redshift—a factor of $\sim 10$ from $z = 3$–4
a stream, and $M_v$ and $r_v$ are the virial mass and radius of the galaxy. One feature is observed to stand out: lower-mass galaxies (blue histograms) tend to have streams with higher $\lambda$ than higher-mass galaxies (red histograms). Whether this trend has some bearing on the dominance of elliptical galaxies at the high-mass end among galaxies should be clarified with further studies. For the high stellar galaxies of $10^{11}$–$10^{12} M_\odot$ (red histograms), $\lambda$ evolves little over the entire redshift range, whereas the less massive subset ($10^{10}$–$10^{11} M_\odot$, blue histograms) displays a steady increase of $\lambda$ from $z = 4$ to $z = 0.62$. It is intriguing that the fraction of $\lambda$ exceeding 1 is substantial at $z \lesssim 2$, which is likely instrumental to the emergence of large-scale spiral structures below $z = 2$.

Figure 5 shows the PDF of mean density of inflow cold gas. Three trends are noted. First, the stream density depends strongly on redshift, with the median being $\sim 10^{-2}$ cm$^{-3}$ at $z = 2$–4, $\sim 10^{-3}$–$10^{-2.5}$ cm$^{-3}$ at $z = 1$–2 and $10^{-3.5}$–$10^{-3}$ cm$^{-3}$ at $z = 0.62$–1. Second, while the more massive galaxies, on average, tend to have somewhat higher stream gas density than less massive galaxies at lower redshift ($z = 0.6$–1), the difference gradually diminishes toward higher redshift. This particular trend, while slightly puzzling, can be reconciled if there is a natural selection effect where strong streams can survive in the midst of gravitational heating environment. Third, at $z = 0.62$–1 there is a dramatic increase of galaxies with very low density streams, which likely reflects the increased importance of hot accretion at low redshift.

4. A NEW PHYSICAL SCENARIO FOR THE EMERGENCE OF THE HUBBLE SEQUENCE

The quantitative, new characterizations and trends presented in Section 3 on cold gas streams—their number, mass flux, density, and angular momentum—provide the physical basis to construct a working framework. Rather than detailed quantitative descriptions, which are beyond the scope of this Letter and will be carried out separately, we provide a set of three key physical elements as a useful guide to investigating, in the context of the standard cold dark matter model, the general morphological trends of galaxies with redshift—the emergence of the Hubble sequence. A consequential but necessary ansatz is that the formation of prominent spiral structures as well as star formation in galaxies have cosmological origins and are primarily fed by cold streams.

1. Origin of small, clumpy Galaxies at $z > 2$. While galaxy mergers and interactions may play varying roles, ultimately, the morphological traits of galaxy formation are expected to be largely governed by the nature of gas supply and dynamics, with feedback perhaps regulating the quantity of star formation. Given that most galaxies at $z > 2$ have $N_{90} \geq 2$ cold gas streams of high gas density ($n_g$) that is more conducive to fragmentations (e.g., Dekel et al. 2009), the expectation is that feeding of and interactions between multiple concurrent streams at high redshift would result in a population of galaxies with fragmented, clumpy, and frequently multiple (gaseous and stellar) disks. This is in line with the observed increasing dominance of a mixture of disk-like, irregular, and clumpy galaxies toward high redshift (e.g., Förster Schreiber et al. 2009; Chevance et al. 2012; Murata et al. 2014). Interactions of streams are effective at producing low angular momentum gas, with the expectation that galaxies at high redshift are disproportionately small in size compared to their low-redshift
Figure 2. Probability distribution functions (PDFs) of $N_{90}$ in four separate redshift ranges, $z = 3–4$ (top left panel), $z = 2–3$ (top right panel), $z = 1–2$ (bottom left panel), and $z = 0.62–1$ (bottom right panel). In each panel, two different stellar mass ranges are shown, $10^{10}–10^{11} M_\odot$ (blue histograms) and $10^{11}–10^{12} M_\odot$ (red histograms). The vertical dashed lines indicate the median of the PDF of the same color.

(A color version of this figure is available in the online journal.)

Figure 3. PDF of cold inflow rate per stream, $\dot{M}_{90}$, defined to be 90% of the total cold accretion rate divided by $N_{90}$, for four separate redshift ranges, $z = 3–4$ (top left panel), $z = 2–3$ (top right panel), $z = 1–2$ (bottom left panel), and $z = 0.62–1$ (bottom right panel). In each panel, two different stellar mass ranges are shown, $10^{10}–10^{11} M_\odot$ (blue histograms) and $10^{11}–10^{12} M_\odot$ (red histograms). The vertical dashed lines indicate the median of the PDF of the same color.

(A color version of this figure is available in the online journal.)
Figure 4. PDF of $\lambda (\equiv j/\sqrt{2GM_vr_v})$ for individual streams in the top $N_{90}$, for four separate redshift ranges, $z = 3–4$ (top left panel), $z = 2–3$ (top right panel), $z = 1–2$ (bottom left panel), and $z = 0.62–1$ (bottom right panel). In each panel, two different stellar mass ranges are shown, $10^{10}–10^{11} M_\odot$ (blue histograms) and $10^{11}–10^{12} M_\odot$ (red histograms). The vertical dashed lines indicate the median of the PDF of the same color.

(A color version of this figure is available in the online journal.)

Figure 5. PDF of mean density of inflow cold gas in four separate redshift ranges, $z = 3–4$ (top left panel), $z = 2–3$ (top right panel), $z = 1–2$ (bottom left panel), and $z = 0.62–1$ (bottom right panel). In each panel, two different stellar mass ranges are shown, $10^{10}–10^{11} M_\odot$ (blue histograms) and $10^{11}–10^{12} M_\odot$ (red histograms). The mean density is averaged over all streams for each individual galaxy, weighted by inflow mass fluxes of individual streams. The vertical dashed lines indicate the median of the PDF of the same color.

(A color version of this figure is available in the online journal.)
counterparts, a trend that is observed (e.g., Trujillo et al. 2006) and seen in simulations (e.g., Joung et al. 2009).

2. Emergence of spiral structures at $z \lesssim 2$. Galaxies have multiple concurrent cold streams ($N_{\text{cold}}$) of high accretion rates ($M_{\text{cold}}$), lower angular momenta ($\lambda$), and high gas densities ($n_{\text{gas}}$) at $z > 2$, each of which is detrimental to the formation of grand spiral structures. It appears that nature has arranged against grand design spiral formation at high redshift with plenty of insurance. While one can not come up with a set of sufficient conditions for the emergence of grand design spirals, it seems physically reasonable to assume that not having more than one concurrent major cold streams is requisite for the emergence of grand design spirals. Our analysis indicates that this condition is expected to occur at $z \lesssim 1$, suggesting that major spiral galaxies begin to emerge at $z \lesssim 1$. The significantly larger $\lambda$ for galaxies in the stellar mass range $10^{10-11} M_\odot$ than $10^{11-12} M_\odot$ (see Figure 4) is interesting, implying that the largest galaxies in the universe at any redshift possess less favorable conditions to form large spirals. Between $z = 1-2$, about one-half of the galaxies have one or two concurrent streams, which we suggest give rise to flocculent spirals stemming from a collection of disjoint but relatively frequent inflow streams. These expectations are in agreement with extant observational indications (e.g., Elmegreen & Elmegreen 2014).

3. Conditions for early-type Galaxy formation. The physical conditions for the emergence of early type galaxies are naturally diametrically opposed to those of irregular galaxies. For early-type galaxies there is no cold gas stream penetrating into the virial sphere with no recurrence. This condition is physically more natural than the proposed transition to hot accretion based on halo mass threshold (Kereˇs et al. 2005; Dekel & Birnboim 2006; Nelson et al. 2013), which would be inconsistent with significant star formation in massive galaxies at high redshift. High density environment is shown to be a good proxy for the emergence of early-type galaxies (Cen 2014b). Because massive halos are associated with high overdensities of large-scale structure, more massive early-type galaxies are expected to have emerged earlier, consistent with observations (e.g., Mortlock et al. 2013). For the same reason, early-type galaxies are expected to be somewhat older in clusters than in the field, in agreement with observations (e.g., Thomas et al. 2005). One also expects that while early-type galaxies occur at all redshifts, their abundance is expected to increase with decreasing redshift as more regions become dynamically hot, in agreement with observations (e.g., Renzini 2006). However, below $z \sim 1$ the rate at which the abundance of giant ellipticals increase is expected to drop off, as the nonlinear $M_{\text{halo}}$ starts to significantly exceed the mass scales of giant ellipticals, in agreement with observations (e.g., Borch et al. 2006).

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REFERENCES

Binney, J. 1977, ApJ, 215, 483
Bond, N. A., Strauss, M. A., & Cen, R. 2010, MNRAS, 406, 1609
Borch, A., Meisenheimer, K., Bell, E. F., et al. 2006, A&A, 453, 869
Bryan, G. L., Norman, M. L., O’Shea, B. W., et al. 2014, ApJS, 211, 19
Bullock, J. S., Kolatt, T. S., Sigad, Y., et al. 2001, MNRAS, 321, 559
Cappellari, M., Emsellem, E., Krajnović, D., et al. 2011, MNRAS, 416, 1680
Carollo, C. M., Cibinel, A., Lilly, S. J., et al. 2014, arXiv:1402.1172
Cen, R. 2011, ApJ, 741, 99
Cen, R. 2014a, ApJL, 785, L15
Cen, R. 2014b, ApJ, 871, 11
Cen, R., Kang, H., Ostriker, J. P., & Ryu, D. 1995, ApJ, 451, 436
Cen, R., Nagamine, K., & Ostriker, J. P. 2005, ApJ, 635, 86
Cen, R., & Ostriker, J. P. 1992, ApJL, 399, L113
Chevance, M., Weijmans, A.-M., Dame, M., et al. 2012, ApJ, 754, L24
Conselice, C. J., Mortlock, A., Bluck, A. F. L., Grützbauch, R., & Duncan, K. 2013, MNRAS, 430, 1051
Dekel, A., & Birnboim, Y. 2006, MNRAS, 368, 2
Dekel, A., Sari, R., &COVERINO, D. 2009, ApJ, 703, 785
Eisenstein, D. J., & Hut, P. 1999, ApJ, 498, 137
Elmegreen, D. M., & Elmegreen, B. G. 2014, ApJ, 781, 11
Fall, S. M., & Efstathiou, G. 1980, MNRAS, 193, 189
Förster Schreiber, N. M., Genzel, R., Bouche, N., et al. 2009, ApJ, 706, 1364
Gebhardt, K., & Blumer, E. 1994, ApJ, 436, 467
Haardt, F., & Madau, P. 2012, ApJ, 746, 125
Hahn, O., Teyssier, R., & Carollo, C. M. 2010, MNRAS, 405, 274
Hopkins, A. M., & Beacom, J. F. 2006, ApJ, 651, 142
Hubble, E. P. 1926, ApJ, 64, 321
Joung, M. R., Cen, R., & Bryan, G. L. 2009, ApJL, 692, L1
Kennicutt, R. C., Jr. 1998, ApJ, 498, 541
Kereˇs, D., Katz, N., Weinberg, D. H., & Davé, R. 2005, MNRAS, 363, 2
Komatsu, E., Smith, K. M., Dunkley, J., et al. 2011, ApJS, 192, 18
Kormendy, J., & Bender, R. 2012, ApJS, 198, 2
Lin, L., Jian, H.-Y., Fousaud, S., et al. 2014, ApJ, 782, 33
Mihos, J. C., & Hernquist, L. 1996, ApJ, 464, 641
Mo, H. J., Mao, S., & White, S. D. M. 1998, MNRAS, 295, 319
Mortlock, A., Conselice, C. J., Hartley, W. G., et al. 2013, MNRAS, 433, 1185
Murata, K. L., Kajisawa, M., Taniguchi, Y., et al. 2014, ApJ, 786, 15
Muzzin, A., van der Burg, R. F. J., McGee, S. L., et al. 2014, arXiv:1402.7077
Nelson, D., Vogelsberger, M., Genel, S., et al. 2013, MNRAS, 429, 3353
Rees, M. J., & Ostriker, J. P. 1977, MNRAS, 179, 541
Renzini, A. 2006, ARA&A, 44, 141
Sandage, A., & Binggeli, B. 1984, ApJ, 89, 919
Silk, J. 1977, ApJ, 211, 63H
Thomas, D., Maraston, C., Bender, R., & Mandes de Oliveira, C. 2005, ApJ, 621, 673
Trujillo, I., Förster Schreiber, N. M., Rudnick, G., et al. 2006, ApJ, 650, 18
Turk, M. J., Smith, B. D., Oishi, J. S., et al. 2011, ApJ, 192, 9
van den Bergh, S. 1976, ApJ, 206, 883
White, S. D. M., & Rees, M. J. 1978, MNRAS, 183, 341