Nonparametric inference for additive models estimated via simplified smooth backfitting

Suneel Babu Chatla1

Received: 10 September 2021 / Revised: 28 April 2022 / Accepted: 6 May 2022 / Published online: 15 July 2022
© The Institute of Statistical Mathematics, Tokyo 2022

Abstract
We investigate hypothesis testing in nonparametric additive models estimated using simplified smooth backfitting (Huang and Yu, Journal of Computational and Graphical Statistics, 28(2), 386–400, 2019). Simplified smooth backfitting achieves oracle properties under regularity conditions and provides closed-form expressions of the estimators that are useful for deriving asymptotic properties. We develop a generalized likelihood ratio (GLR) (Fan, Zhang and Zhang, Annals of statistics, 29(1), 153–193, 2001) and a loss function (LF) (Hong and Lee, Annals of Statistics, 41(3), 1166–1203, 2013)-based testing framework for inference. Under the null hypothesis, both the GLR and LF tests have asymptotically rescaled chi-squared distributions, and both exhibit the Wilks phenomenon, which means the scaling constants and degrees of freedom are independent of nuisance parameters. These tests are asymptotically optimal in terms of rates of convergence for nonparametric hypothesis testing. Additionally, the bandwidths that are well suited for model estimation may be useful for testing. We show that in additive models, the LF test is asymptotically more powerful than the GLR test. We use simulations to demonstrate the Wilks phenomenon and the power of these proposed GLR and LF tests, and a real example to illustrate their usefulness.

Keywords Generalized likelihood ratio · Loss function · Hypothesis testing · Local polynomial regression · Wilks phenomenon

1 Department of Mathematical Sciences, The University of Texas at El Paso, 500 West University Avenue, Texas 79968, USA