Anomalous circularly polarized light emission caused by the chirality-driven topological electronic properties

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Chirality of organic molecules is characterized by selective absorption and emission of circularly-polarized light (CPL). A consensus for chiral emission (absorption) is that the molecular chirality determines the favored light handedness regardless of the light-emitting (incident) direction. Refreshing above textbook knowledge, we discover an unconventional CPL emission effect in organic light-emitting diodes (OLEDs), where oppositely propagating CPLs exhibit opposite handedness. This direction-dependent CPL emission boosts the net polarization rate by orders of magnitude in OLED devices by resolving the long-lasting back-electrode reflection problem. The anomalous CPL emission originates in a ubiquitous topological electronic property in chiral materials, i.e., the orbital-momentum locking. Our work paves the way to design novel chiroptoelectronic devices and reveals that chiral materials, topological electrons, and CPL have intimate connections in the quantum regime.
Introduction

Chirality characterizes parity symmetry-breaking where a molecule cannot be superposed on its mirror image in chemistry and biology\textsuperscript{1,2}. Chiral enantiomers exhibit opposite chiroptical activity when coupling to light\textsuperscript{3,4}. In physics, chirality usually refers to the spin-momentum locking of particles such as Weyl fermions\textsuperscript{5,6} and the circular polarized light. Chiral organics were recently reported to exhibit a topological feature\textsuperscript{7}, in which the electronic orbital and momentum are locked together, to rationalize the intriguing spin selectivity in DNA-type molecules\textsuperscript{8,9}. Hence given the intimate relationship between electronic states and light-matter interactions, we were inspired to raise a question: Can topological electronic properties enhance chiroptical activity and therefore advance the rapidly developing (chir)optoelectronic technology\textsuperscript{10,11}?

A future industrial application of organic chiral emissive materials is in circularly polarized organic light-emitting diodes (CP-OLEDs)\textsuperscript{12}, which should eliminate the $\sim50\%$ internal light loss caused by the contrast-enhancing circular polarizer in OLED displays. Such efficiency gains occur via direct circularly polarized electroluminescence (CP-EL) from the CP-OLED, which can pass through the contrast-enhancing polarizer unhindered.\textsuperscript{13} The effectiveness of this strategy depends on the degree of circular polarization of EL, where higher polarization gives better efficiency for the display in the presence of such polarizers.\textsuperscript{14}

Since the first CP-OLED reported in 1977\textsuperscript{15}, the chirality of material in a device was also assumed to be identical to its chirality measured optically in a thin-film (i.e., without current flows). In another word, CP-EL was considered nearly the same process as CP photoluminescence (CP-PL)
[or the inverse process of optical circular dichroism (CD)] due to shared electronic transition, and its CP emission is determined by the product of electric and magnetic transition dipole moments.\textsuperscript{16,17} Thus most efforts in this field were made on developing more twisted chiral emitter with stronger magnetic transition dipoles to improve optical chirality\textsuperscript{18,19}, without taking current flows in an OLED device into considerations.

More importantly, in terms of device engineering, reflective back-electrode is another key issue. In all prior studies of chiral emissive materials, CP emission is conventionally expected to exhibit the same handedness in both emission directions (forward and back) from the point of recombination, thus any back reflection within the device will invert the handedness of CP emission travelling backwards and cancels out the forward CP emission, reducing the net EL circular polarization that exits the device through the transparent electrode\textsuperscript{18,20–22}. Consequently, the magnitude of EL circular polarization from devices becomes much smaller than the corresponding CP-PL which does not suffer issues of reflection\textsuperscript{20}(Figure 1a). Even though constructing semi-transparent OLEDs can, to some extent, mitigate the problem of reflection, such a strategy reduces the overall the device performance in a displays, negating to the original intention of energy saving at the polarizer.\textsuperscript{18}

Among all CP-OLEDs reported, chiral polymeric materials\textsuperscript{14,23–26} demonstrate significant circular polarization in PL and EL, several orders of magnitudes stronger than other chiral emissive systems\textsuperscript{18,27–29} (see Figure 2a). Despite the analysis above, when constructing optoelectronic devices from such materials, their CP-EL remains equal, or sometime is even enhanced compared to
CP-PL or CD. Although previous theoretical\textsuperscript{30,31} and experimental\textsuperscript{14,23,24} work attributed the strong optical circular dichroism to a predominately excitonic origin, these analyses cannot account for the comparable or enhanced circular polarization in EL devices, given the expected detrimental effect of back-electrode reflection.

In this work, we discover an anomalous light emission phenomenon from chiral polymeric CP-OLEDs. For the chiral polymeric materials under study, CP-EL exhibits opposite handedness in forward and backward emission directions, counter-intuitive to what is usually expected in EL or PL (Figure 1b). With such direction-dependent CP emission, the back-reflected light exhibits the same handedness as the forward emission, avoiding the polarization cancellation which occurs in devices using other materials and boosting the net CP-EL exiting the device\textsuperscript{18,20}. Furthermore, for the first time, we investigate the origin of current flows on the CP-EL, where the its handedness can also be switched by reversing the current flow in an OLED. We propose that the directional CP-EL observed is caused by the topological nature of the electronic wave functions in chiral polymers. Because of orbital-momentum locking\textsuperscript{7}, the current flow induces nonequilibrium orbital polarization in electron and hole carriers. Therefore, finite angular momentum transfers from electron/hole orbital to the photon spin in the optical transition. When they have the same spin, the counter-propagating CP lights exhibit opposite handedness. This orbital polarization effect rationalizes that the handedness of CP light is determined both by the current direction and the emission direction. This model reveals an exotic CP-EL mechanism from the electric transition dipole caused by current-induced time-reversal breaking, generally displaying larger circular polarization than PL or CD which involve both electric and magnetic transition dipoles. Our work paves a path to design novel
chiroptoelectronic devices with strong circular polarization.

Results

Chiral polymer blend consisting of an achiral light-emitting polymer (i.e., poly(9,9-dioctylfluorene-alt-benzothiadiazole), F8BT, Fig. 1) and a non-emissive chiral additive (i.e., $P$-aza[6]helicene) was selected for the investigation of CP-EL. Annealed chiral polymer blends demonstrate strong and robust induced optical CD with the absorption dissymmetry factor ($g_{abs}$) of $\sim 0.6$ (see Fig. S1$^{13,23}$, calculated in the following way:

$$g_{abs} = \frac{A_L - A_R}{A} = \frac{\Delta A}{A},$$

(1)

where $L/R$ stands for left/right-handed CP light and $A$ refers to the absorbance. To investigate how emission direction affects the CP-EL, CP-OLEDs were fabricated using both conventional and inverted device structures where the transparent electrode (i.e., Indium Tin Oxide, ITO) serves as anode and cathode, respectively (Figs. 1c and 1d).

With a fixed current flow direction (Figs. 1c and 1d), when measuring the EL through transparent ITO, left-handed CP light is observed in a conventional device where the light emits in the same direction as the electron injection. A positive EL dissymmetry factor $g_{EL}$ of $+0.54$ can be calculated following:

$$g_{EL} = \frac{I_L - I_R}{(I_L + I_R)/2},$$

(2)

where $I_{L/R}$ is the irradiance recorded from the CP-OLEDs. However, despite a fixed absolute stereochemistry of chiral material in the emissive layer of both devices, the sign of the CP-EL
Figure 1: **Device-structure dependent circular polarized (CP) Electroluminescence (EL).**  
(a) Normal circular polarization effect where CP-EL is emission direction-independent. (b) Anomalous circular polarization effect where CP-EL is emission direction-dependent. Device structures of (c) conventional and (d) inverted CP-OLEDs. EL of F8BT:[P]-aza[6] helicene-based CP-OLEDs recorded from (e) conventional and (f) inverted CP-OLEDs. Inset: Molecular structure of F8BT and [P]-aza[6]helicene.
signals was found to be dependent on the device structures. When the emission direction relative to the current direction is switched, the inverted CP-OLED emits right-handed circularly polarized light through ITO with a $g_{EL}$ of $-0.33$. Apart from the emission direction-dependent CP-EL signals in conventional versus inverted devices, we detected no evidence of erosion of $g_{EL}$ by the reflective electrodes. Compared with other reported CP-OLEDs\textsuperscript{18,27–29}, polyfluorene-based CP-OLEDs we developed exhibit one of the highest known $g_{EL}$ values (Fig. 2a). In contrast, lanthanide complexes exhibit intrinsically high PL dissymmetry ($g_{PL}$)$^{20}$, but the $g_{EL}$ recorded from the transparent electrode dramatically decreases when increasing the thickness of the reflective metal electrode. This is similarly observed in other small molecule CP-OLEDs\textsuperscript{18,27–29} (Fig. 2b).

To compare our results with other previously reported CP-OLEDs, we performed CP-EL measurements on semi-transparent OLEDs in both conventional and inverted CP-OLEDs (Fig. 2c). Surprisingly, emission direction-dependent CP-EL behavior was observed in both device structures, where the CP-EL from forward and backward emission (i.e., through semi-reflective electrode) exhibit the opposite handedness. Considering this emission direction-dependent dissymmetry factor is only observable in EL but not for CP-PL or CD of the chiral thin films (Fig. S2), we speculate that this behavior is associated with the flow of charge carriers within the devices. To unambiguously describe and compare the emission direction-dependent CP-EL signals in two device architectures, we define the emission direction relative to the charge carrier flow direction (See Fig. 2c). Specifically, emission from the transparent ITO in the conventional device and the emission from semi-transparent Au in the inverted device are defined as directionally aligned with with the electron flow. Conversely, emission from the opposite electrodes in conventional and inverted
Figure 2: Emission-direction-dependent CP emissions relative to charge carrier flow directions. (a) Summary of reported CP-OLEDs using different types of chiral emitters including polyfluorene, lanthanide complex, thermally assisted delayed fluorescent emitter (TADF), and phosphorescent emitters. Detailed information on molecular structures and corresponding citations can be found in Table S1 and Scheme S1. (b) Comparison of $|g_{EL}|$ values reported from polyfluorene (inverted device in this work), lanthanide complex (data points from Ref.20), and phosphorescent emitter (data points from Ref.18) as a function of reflective electrode thickness. The trends are represented as the solid lines. (c) Schematic diagram of semi-transparent conventional (top) and inverted (bottom) CP-OLEDs based on F8BT:[P]-aza[6]helicene. Red arrows stand for the EL emitted along the electron flow direction and blue arrows stand for the EL emitted along the hole flow direction. Interlayers are removed for clarity. (d) Summary of $g_{EL}$ measured from both sides of the semi-transparent CP-OLEDs. Detailed spectra for data point in b and d can be found in Figs. S3 and S4.
devices is defined as directionally aligned with the hole flow. In contrast to other chiral emitters in OLED devices\textsuperscript{18,20}, we find $|g_{EL}|$ of net emission from the transparent electrode increases when increasing the thickness of the reflective electrode (Figs. 2b and 2d) for our chiral polymeric materials. As summarized in Fig. 2d, regardless of device structure used, F8BT:[P]-aza[6]helicene based CP-OLEDs demonstrate positive $g_{EL}$ when emission occurs along the direction of electron flow and switch to negative $g_{EL}$ when emission occurs along the hole flow direction. This indicates that the previously observed inversion of CP-EL sign from conventional versus inverted devices (see Fig. 1) is due to emission direction-dependent CP-EL relative to the electron flow direction. Given this outcome, the reflective electrode in our system results in reflected light with an identical sign to the forward emission, resulting in a comparable or boosted net CP EL signal (Fig. 2b).

**Discussions**

Our CP-EL data exhibits profound features, distinct from those obtained with other chiral emitters in OLEDs (Fig. 2b). Besides extremely large $g_{EL}$, the CP-EL handedness can be switched both by the current flow direction and by the light emission direction. In other words, the emitted photon seems to retain a memory of the direction of recombining electrons and holes, despite the fact that initial carrier velocities are usually ignored to understand the light emission process\textsuperscript{32}. Such an outcome indicates salient time-reversal symmetry (TRS)-breaking in the ground state and the excited state. The exciton-coupling model\textsuperscript{30,31} cannot explain such direction-dependent CP-EL, because it is based on quantum states with TRS.
It is known that helicene additive promotes the F8BT polymer to forms chiral assemblies in solid-state thin films\textsuperscript{30,33}. The chiral polymer blend is the real-space channel for both current flow and light emission. When propagating electrons meet counter-propagating holes in an OLED, they form bound excitons by losing their velocities and then emit photons. A similar process dominates the light emission for PL in which excited electrons/holes exhibit zero net velocity. It is also the case for some EL where the carrier flow and light emission occur at different regions so that carrier velocities are quenched (e.g., emissive dopants in host matrices\textsuperscript{34}). Electrons and holes can also directly recombine by remembering their propagating direction. As we will show, the electron/hole momentum is locked to its orbital angular momentum (OAM) in a chiral molecule. In CP-EL, opposite current flow leads to opposite OAM polarization in electrons/holes and eventually induces opposite spin of the CP light, i.e., the direction-dependent CP handedness. In the following discussions, we refer OAM or orbital to that of the electron/hole and refer spin to that of CP light if not specified.

Next, we will revisit the general theory that describes the CP emission effect. According to Fermi’s golden rule, the emission rate of CP light is,

\[
I_{L/R} = \frac{2\pi}{\hbar} |\langle 0 | H' | 1 \rangle|^2 \delta(\epsilon_1 - \epsilon_0 - \hbar\omega) \tag{3}
\]

where |0⟩ (|1⟩) represents the ground (excited) state with energy \(\epsilon_0\) (\(\epsilon_1\)), \(H'\) is the light interaction Hamiltonian \(H' = -eE \cdot r - m \cdot B\) with \(m\) being the magnetic moment, \(E\) and \(B\) are the light electric and magnetic fields, respectively, and \(\hbar\omega\) is the photon energy. For right/left-handed light traveling along the \(z\) axis, the electric and magnetic fields are \(E = E_0(1, \pm i, 0)/\sqrt{2}\) and
\[ \mathbf{B} = \frac{E_0}{c(\mp i, 1, 0)} / \sqrt{2}. \]

Therefore, the leading term of CP light emission can be derived as,

\[ I_L - I_R = -\frac{2\pi e^2}{\hbar} I_0 \text{Im}[x^{01} y^{10}] \delta - \frac{2\pi e}{hc} I_0 \text{Im}[m_x^{01} x^{10} + m_y^{01} y^{10}] \delta \]

(4)

where \( x^{01} = \langle 0 | x | 1 \rangle \) and \( m_x^{01} = \langle 0 | m_x | 1 \rangle \) represent the electric and magnetic transition dipoles, respectively, and \( I_0 = |E_0|^2 \). We note \( \mathbf{m} = (m_x, m_y, m_z) \), \( \mathbf{r} = (x, y, z) \) and \( \delta \) for the same \( \delta \)-function in Eq. 3. The second term in Eq. 4 is routinely employed to understand CD, CP-PL or CP-EL for organic/inorganic systems and has been called natural chiroptical activity\textsuperscript{35}. Because it corresponds to interaction with the electric and magnetic fields of light, this term involves both electric and magnetic transition dipoles. We call it the normal circular polarization effect (NCPE) in the following. In chiral organic molecules, the OAM change in the transition is zero because TRS forces the net OAM of \( |0, 1\rangle \) to be zero. Due to the conservation of angular momentum, the total spin angular momenta of all emitted photons sum to zero. Because counter-propagating photons emitted are equal in probability, they carry opposite spins, i.e., they share the same handedness. Thus, the handedness of CP emission is free from the emission direction in the case of NCPE, as observed in PL and EL reported in other chiral emissive systems\textsuperscript{18,27–29}.

The first term in Eq. 4 corresponds to the dipole interaction with light electric field. If \( |0, 1\rangle \) respect TRS, this term is exactly zero. Additionally, a similar term corresponds to the Berry-curvature-induced\textsuperscript{36} anomalous Hall effect\textsuperscript{37} in solid crystals and also vanishes if TRS appears. Therefore, the first term was generally ignored when studying organic molecules. It was referred to as the magnetic CD\textsuperscript{38,39} in absorption of magnetic materials or in an external magnetic field. However, if electrons and holes carry finite velocities before recombination, the first term cannot be naively neglected. In other words, the current flow can induce magnetization, more specifically the
orbital magnetization as we will show. The nonequilibrium phase breaks TRS in chiral molecules. We refer to the first term as the anomalous circular polarization effect (ACPE) here. In such a case, ACPE may contribute more to the net circular polarization than NCPE because the electric field is much stronger than magnetic field for light.

Now we discuss the TRS-breaking of $|0, 1\rangle$ in the presence of current flow. The electron wave function $|\psi\rangle$ in a molecule, for example, a sine function like profile (see Fig. 3), can be considered as the superposition of two counter-propagating plane waves, $|\psi\rangle = |\psi^+\rangle + |\psi^-\rangle$, where $|\psi^{\pm}\rangle$ propagate along $\pm z$ directions, and $|\psi^+\rangle = |\psi^-\rangle^*$ because TRS allows $|\psi\rangle$ to be real valued. If an electron picks up a velocity along $\pm z$ due to a charge current, its wave function reduces from $|\psi\rangle$ to $|\psi^{\pm}\rangle$. We point out that $|\psi^{\pm}\rangle$ themselves violate TRS, although $|\psi\rangle$ does not.

Next, $|\psi^{\pm}\rangle$ carry opposite OAM ($\pm l$). We can generally describe a positive-moving plane wave by $|\psi^+\rangle = A(\rho, z)e^{i\phi + ikz}$, where $A(\rho, z)$ is a general coefficient depending on $z$ and the radial distance $\rho$, $k$ is the momentum, and $l = 0, \pm 1, \pm 2 \ldots$ represents OAM. $|\psi^+\rangle$ is a plane wave with vortex-like wave front if $l \neq 0$ and reduces to a normal plane wave for $l = 0$. The inversion or mirror reflection (e.g. $z \rightarrow -z$) forces $l = 0$. In a chiral system, $l \neq 0$ generically holds. It is obvious that $|\psi^-\rangle$ with $-k$ carries opposite OAM $-l$ because $|\psi^+\rangle = |\psi^-\rangle^*$. Such orbital($l$)-momentum($k$) locking represents the wave function topology, in which the parallel or antiparallel $l - k$ relation is controlled by the molecular chirality.

The ACPE term in Eq. 4 is equivalent to the OAM shift in the transition $^{38-40} \Delta l = \langle \hat{L}_z \rangle = x^{01}p^{10}_y - y^{01}p^{10}_x$, where $\hat{L}_z = xp_y - yp_x$ is the OAM operator (see more information in Supplementary
Figure 3: Illustration of orbital-momentum locking and anomalous circular polarization effect. (a) The wave function ($\psi$) of a chiral molecule (represented by the helical chain below) can be regarded superposition of counterpropagating plane waves, $\psi^\pm$. (b)-(c) $\psi^\pm$ carry opposite orbital angular momenta (OAM) ($\pm l$), i.e. $\psi^\pm$ share the same chirality. The black arrow represents the propagating direction ($k$). The vortex-like wave front is shown to indicate $l$. (d) Normal circular polarized emission from the excited state $|1\rangle$ to ground state $|0\rangle$, where $|0, 1\rangle$ carry zero OAM. The angular momentum transfer in the transition $\Delta l = 0$, leading to the same handedness in emitted lights along opposite directions. “e” and “h” represent electron and hole, respectively. (e)-(f) Anomalous circular polarized emission from $|1^+\rangle$ to $|0^+\rangle$ ($|1^-\rangle$ to $|0^-\rangle$), where $|0^+, 1^\pm\rangle$ ($|0^-, 1^-\rangle$) carry finite OAM. Because $\Delta l$ is finite, oppositely emitted lights carry the same spin and exhibit opposite handedness.
Information). In the presence of current along $-z$, we need replace $|0^+\rangle (|1^+\rangle)$ for $|0\rangle (|1\rangle)$ to evaluate the ACPE in Eq. 4. In this case, $\Delta l$ is nonzero in the optical transition from $|1^+\rangle$ to $|0^+\rangle$, both of which carry finite OAM, as illustrated in Fig. 3. In addition, reversing current leads to $-\Delta l$. We note that $\Delta l$ is gauge invariant although $l$ of a given band depends on the specific gauge.

For a photon with a positive spin angular momentum, it is defined as right-handed CP light if it travels along $+z$ and as the left-handed CP light if along $-z$. Therefore, the finite angular momentum, which is transferred from OAM of electrons/holes to spin of photons ($S = +\Delta l$), forces that the handedness of CP light relies on the emission direction. Overall, the orbital-momentum locking eventually leads to the current direction- and emission-direction dependencies of CP-EL, fully consistent with our experiments.

Furthermore, we quantitatively estimate the ACPE and NCPE for the chiral F8BT polymer assembly by \textit{ab initio} calculations. It is challenging to refine the accurate atomic structure of such chiral aggregates. Without losing generality, we simulate chiral stacking of F8BT molecules and focus on the intermolecular chirality that is associated with the dominant charge transport direction along the layered packing structure (noted as $z$ axis here)\textsuperscript{41}. Although $|0, 1\rangle$ can be generally many-body wave functions, we use the highest occupied molecule orbital (HOMO) and lowest unoccupied molecule orbital (LUMO) to represent $|0\rangle$ and $|1\rangle$, respectively, by ignoring higher-order corrections (like the distortion in excited states) in the calculations. As shown in Figure 4, two layer stacking with a counter-clockwise twisting angle $30^\circ$ reshapes HOMO and LUMO wave functions dramatically compared to a single layer of molecule. By calculating the ACPE involving the $+z$
Figure 4: The chirality and circular polarized emission for stacking two F8BT molecules with a twisted angle. (a) The total charge density distribution for the HOMO ($|0\rangle$) and LUMO ($|1\rangle$) states calculated by density functional theory. (b) Schematics of transition from $|1^+\rangle$ to $|0^+\rangle$. (c) The phase distribution $l\phi$ in the $xy$ plane for a vortex-like plane wave $e^{i(l\phi \pm kz)}$. The $l$ is deduced from the phase winding number counterclockwise along the dashed circle. $|0^\pm, 1^\pm\rangle$ with $\pm k$ exhibit $\pm l$, showing the orbital-momentum locking.
moving HOMO and LUMO, we obtain a large dissymmetry factor $|g_{EL}| = 0.48$ ($0.44$) for two (three) layer stacking, which is in the same order of magnitude as experimental $g_{EL}$. The OAM can be evaluated from the phase winding number in the $xy$ plane, verifying the orbital-momentum locking in $|0^\pm\rangle$ and $|1^\pm\rangle$. Because $|0, 1\rangle$ is usually composed by many plane waves, the total value of $l$ is unnecessarily an integer. Better knowledge on the molecular arrangement of chiral polymer assemblies will help improve the prediction power of calculations in the future work.

Additionally, the current-induced magnetization in our experiments is relevant to the orbital rather than spin of electronic states. If electron-spin polarization matters, it would require substantial spin-orbit coupling (SOC) in the device. We know that these organic polymers made of light elements exhibit negligible SOC. Despite that metal electrodes may include heavy elements, the circular polarization rate remains the same for Al, Ag and Au electrodes with largely varied SOC (Fig. S6). Thus, the role of electron spin is negligible in the light emission process. The ACPE is caused by the chirality-induced orbital polarization, different from the chirality-induced spin selectivity effect discussed in literature\textsuperscript{8}. Our experiment demonstrates a significant consequence of the electron orbital effect in chiral materials. Here, the electron OAM is indicated by the the handedness flip of CP light (spin flip of light) as reversing the current flow (e.g., see Figs. 1c-d).

In summary, we report an anomalous phenomenon where the handedness of CP light emission depends on the emission direction. This effect enables us to design unconventional CP-OLED devices with large $g_{EL}$ and immune from the back-electrode reflection. We highlight that the orbit-momentum locking causing ACPE is strongly associated with the charge transport mode in
the polymer systems and therefore suggest the following design principles for further development of CP-OLEDs with strong CP-EL. To ensure the entire stack of molecular assemblies exhibit strong ACPE, the emissive sites have to be strongly coupled with chiral transport sites or ideally within the same sites as in our polymer systems. If charge carriers are independently transported, such as in host materials, then they get scattered to random adjacent chiral emissive sites, the net momentum and OAM will be quenched and only NCPE will appear. In this case, CP-EL can no longer be considered as the same origin as CP-PL and circular dichroism where no charge transport and current flows exist.

We propose an ACPE that involves finite angular momentum transfer in the optical transition. Because ACPE and NCPE come from the first and second-order optical transitions in Eq. 4, ACPE is often much larger than NCPE when TRS is broken. We highlight that the unusual TRS-breaking in ACPE is driven by the nonequilibrium orbital magnetization, which originates in the chiral orbital nature in wave functions. In CP-OLED, such orbital magnetization is caused by the current flow (rather than static magnetization), the impact of which was ignore and unexplored for almost 200 years research of chiral materials\textsuperscript{42}. Our work reveals an intriguing unification of chirality in seemingly unrelated aspects: structure geometry, electronic topology, and the handedness of CP light.
Methods

Samples: \([P]\)-aza[6]helicene was synthesized as previously reported\(^{23}\) and separated using preparative chiral HPLC.

Thin-film and device fabrication: The cleaning process for all substrates (fused silica and prepatterned ITO glass, Thin Film Devices Inc., 20 ohms/sq) involved rinsing in an ultrasonic bath with acetone, isopropyl alcohol (IPA), Hellmanex III (Sigma-Aldrich), and deionized water for 30 min. These were transferred to a plasma asher for 3 min at 80 W and 50 W before spin-coating for fused silica and prepatterned ITO, respectively. F8BT and aza[6]helicene were dissolved in toluene to a concentration of 30 mg/mL and blended to form a 10% aza[6]helicene solution. About 130 nm thick emissive layer can be achieved by dynamically spin-coating at 2300 rpms for 1 min. Chiral samples were annealed for 10 min in a nitrogen atmosphere (glovebox, < 0.1 ppm of \(\text{H}_2\text{O}\), < 0.1 ppm of \(\text{O}_2\)). Dynamic coating ensures strong chiroptical activity is achieved without giving too thick films, compared to previous studies\(^{14,23}\). Organic film thicknesses was monitored using a Dektak 150 surface profiler and the metal thickness was used as displayed from QCM monitor. Circular dichroism measurements were performed using a Chirascan (Applied Photophysics) spectrophotometer.

CP-EL: Left-handed and right-handed CP emission spectra were collected using a combination of linear polarizer and zero-order quarter-wave plate (546 nm, Thorlabs) placed before detectors. The device is driven by a constant current of 1 mA (pixel area = 0.045 cm\(^2\)). The dissymmetry factor \(g\) in the EL spectra was calculated from the equation \(g = 2(I_L - I_R)/(I_L + I_R), \mid g \mid \leq 2\). Here,
$I_L$ and $I_R$ are the left-handed and right-handed emission intensities. EL spectra from the PLED were recorded using an Ocean Optics USB 2000 charge-coupled spectrophotometer. All CP-EL measurements are carried out after measuring with only a linear polarizer to ensure negligible linear polarization or random polarization, which should be considered in all CP emission measurements.

**Conventional devices:** Poly(3,4-ethylenedioxythiophene):poly(styrenesulfonate) (PEDOT:PSS) (H.C. Starck GmbH) (55 nm) was dynamically spin-coated on cleaned ITO substrate with a spin speed of 2500 rpms for 1 min. [P]-aza[6]helicene-blended F8BT deposition was the same as for the thin film studies, followed by the thermal evaporation of a 10 nm TPBi (Sigma-Aldrich), 10 nm Ca layer (Sigma-Aldrich), capped by an Al (99.99%, Kurt J. Lesker Company Ltd.) layer up to 100 nm on the organic layer under a vacuum level of $1 \times 10^{-7}$ mbar. Conventional device structure: ITO/PEDOT:PSS/TFB/ F8BT:[P]-aza[6]helicen/TPBi/Ca/Al.

**Inverted devices:** The ZnO is deposited on the cleaned ITO by a sol–gel method which has been described elsewhere followed by a PEIE (30 wt % in water, Sigma-Aldrich) rinsing step. Then, [P]-aza[6]helicene-blended F8BT was dynamically spin-coated onto ZnO/PEIE. Afterward, 25 nm TCTA (97% Sigma-Aldrich), MoOx (99.97%, Sigma-Aldrich) and Au (99.99%, Kurt J. Lesker Company Ltd.) up to 120 nm were thermally evaporated onto the organic layer under vacuum level of $1 \times 10^{-7}$ mbar. Inverted device structure: ITO/ZnO/PEIE/ F8BT:[P]-aza[6]helicene/TCTA/MoOx/Au.

**Ab initio calculations:** The electronic wave functions and charge densities of F8BT chiral assemblies were calculated by the density-functional theory (DFT) implemented in the Vienna ab initio Simulation Package (VASP). The generalized gradient approximation (GGA) was used for
the exchange-correlation functionals. F8BT molecules were stacked along the $z$ axis in a twisted manner. The molecular cluster model included at least 10 Å vacuum distances along all directions. An energy cutoff of 400 eV was used for the plane wave basis. The total number of plane waves is about $4 \times 10^5$. We note the plane wave by wave vector $\mathbf{G} = (G_x, G_y, G_z)$. In the plane wave basis, for example, the wave function of HOMO, $\langle 0 \rangle$, can be expressed as:

$$
\langle 0 \rangle = \sum_{G_z} \phi_0(G_z) e^{iG_z z},
$$

$$
\langle 0^{\pm} \rangle = \sum_{G_z>0/G_z<0} \phi_0(G_z) e^{iG_z z},
$$

where $\phi_0(G_z) = \sum_{G_x,G_y} c_0^G e^{i(G_x x + G_y y)}$ and $c_0^G$ is the plane wave coefficient extracted directly from DFT wave functions. The charge density is $\rho_0 = |\langle 0 \rangle|^2$. Besides $G_z$, the phase of the $G_z$ propagating wave in Fig. 4 is $\arg \phi_0(G_z)$. Under electrical current along $-z$, the CP electric dipole transition amplitudes are calculated as:

$$
I_{R/L}(\omega) \propto \left| \langle 0^+ | x \pm iy | 1^+ \rangle \right|^2 \delta(\epsilon_1 - \epsilon_0 - \hbar \omega)
$$

$$
= \int d\mathbf{r} \sum_{G_z>0} \sum_{G_z>0} \phi_0^*(G_z') (x \pm iy) \phi_1(G_z) e^{i(G_z - G_z') z} \left| \delta(\epsilon_1 - \epsilon_0 - \hbar \omega) \right|^2
$$

$$
= \sum_{G_z} \sum_{G_y} \sum_{G_z>0} c_1^G \left( \frac{\partial c_0^G}{\partial G_x} \pm i \frac{\partial c_0^G}{\partial G_y} \right)^* \delta(\epsilon_1 - \epsilon_0 - \hbar \omega),
$$

where $^*$ represents taking complex conjugate. One can analyze the symmetry constrain on CP emission from Eq. (6). If inversion symmetry is present, then $c_0^{1,1}_G = p_{0,1} c_{-G}^{0,1}$ with $p_{0,1} = \pm 1$ refers to the parity eigenvalue of $|0\rangle$ or $|1\rangle$. On the other hand the time-reversal symmetry requires that $c_0^{1,1}_G = (c_{-G}^{0,1})^*$. Thus, if inversion and time-reversal symmetries exist simultaneously, the coefficient $c_0^{1,1}_G$ is purely real (imaginary) for the parity even (odd) state. Therefore, $I_R = I_L$ always holds according to Eq. (6). When inversion is broken, the circular polarization ($I_R \neq I_L$) can appear.
Supplementary Information

Table S1 Summary of reported $g_{PL}$ and $g_{EL}$.

Scheme S1 Molecular structures of materials in Figure 2 analysis.

Figure S1 Absorption and circular dichroism spectra.

Figure S2 PL and absorption dissymmetry factor measured from opposite direction.

Figure S3 Detailed CP-EL spectra of semi-transparent inverted CP-OLEDs.

Figure S4 Detailed CP-EL spectra of semi-transparent conventional CP-OLEDs.

Figure S5 Detailed CP-EL spectra of inverted CP-OLEDs with different reflective electrode.

Section S1 Electric and Magnetic Dipoles in Plane-Wave Basis

Section S2 CP and Orbital Angular Momentum (OAM)

References and Notes

Acknowledgements: Dedication: To the memory of Professor Alasdair James Campbell (1961-2021). L.W. would like to thank Prof. Alasdair Campbell and Prof. Jenny Nelson for useful discussions at Imperial College London. L.W. would like to thank Prof. Feng Gao (Linköping University) for the support during his transition period from Imperial College London to Linköping University. B.Y. acknowledges the financial support by the MINERVA Stiftung with the funds from the BMBF of the Federal Republic of Germany and the European Research Council (ERC Consolidator Grant “NonlinearTopo”, No. 815869). L.W. and M.J.F. would like to thank Cambridge
Display Technology Limited (company number 02672530) for providing the F8BT polymers. L.W. and M.J.F. would like to acknowledge EPSRC research grants EP/P000525/1, EP/L016702/1 and EP/R00188X/1.

**Competing Interests:** The authors declare the following competing financial interest(s): M.J.F. is an inventor on a patent concerning chiral blend materials (WO2014016611).

**Data and materials availability:** All data needed to evaluate the conclusions in the paper are present in the paper and/or the Supplementary Materials. Additional data related to this paper can be requested from the authors.

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Table S1: Summary of reported $g_{PL}$ and $g_{EL}$.

| Emissive layer         | Category            | $|g_{PL}|$ | $|g_{EL}|$ | Comment               |
|------------------------|---------------------|----------|----------|-----------------------|
| F8BT$^1$               | Polyfluorene        | 0.21     | 0.65     |                       |
| F8BT$^2$               | Polyfluorene        | 0.21     | 0.48     |                       |
| PFO crystalline$^3$    | Polyfluorene        | 0.21     | 0.42     |                       |
| PFO beta-phase$^3$     | Polyfluorene        | 0.39     | 0.44     |                       |
| CsEu((-)hfbc)$_4$      | Lanthanide complex  | 1.21     | 0.15     | Used for Figure 2b analysis |
| $M$-Pt$^5$             | Phosphorescent      | $4.9 \times 10^{-3}$ | $1.1 \times 10^{-3}$ | Used for Figure 2b analysis |
| $\Delta$-fac-Ir(ppy)$_3$ $^6$ | Phosphorescent | $3.15 \times 10^{-3}$ | $2.8 \times 10^{-4}$ |                       |
| $\Delta$-Ir(ppy)$_2$(acac)$^6$ | Phosphorescent | $1.33 \times 10^{-3}$ | $3.1 \times 10^{-4}$ |                       |
| $\Delta$-(tfpqz)$_2$Ir(R-L$_2$)$^7$ | Phosphorescent | $9 \times 10^{-4}$ | $5 \times 10^{-4}$ |                       |
| $\Delta$-Ir(dfppy)$_2$(S-sdpp)$^8$ | Phosphorescent | $1.7 \times 10^{-3}$ | $2.1 \times 10^{-3}$ |                       |
| $\Delta$-Ir(dfppy)$_2$(R-sdpp)$^8$ | Phosphorescent | $1.2 \times 10^{-3}$ | $2.1 \times 10^{-3}$ |                       |
| $P$-Pt$^9$             | Phosphorescent      | $4 \times 10^{-3}$ | $1.3 \times 10^{-3}$ |                       |
| $(R)$-BN-CF$^{10}$     | TADF                | $1.2 \times 10^{-3}$ | $2.1 \times 10^{-3}$ |                       |
| Compound               | Type   | TADF 1   | TADF 2   |
|-----------------------|--------|---------|---------|
| (S)-CPDCz\textsuperscript{11} | TADF   | $3.7 \times 10^{-4}$ | $5.5 \times 10^{-4}$ |
| (S)-CPDCB\textsuperscript{11} | TADF   | $5.8 \times 10^{-4}$ | $8.6 \times 10^{-4}$ |
| (R)-OBN-DPA\textsuperscript{12} | TADF   | $2.52 \times 10^{-3}$ | $2.3 \times 10^{-3}$ |
| (R)-OBN-Cz\textsuperscript{13} | TADF   | $1.4 \times 10^{-3}$ | $2.3 \times 10^{-3}$ |
| (R)-ODQPXZ\textsuperscript{14} | TADF   | $4.6 \times 10^{-4}$ | $6.0 \times 10^{-4}$ |
| (S)-SFST\textsuperscript{15} | TADF   | $4 \times 10^{-3}$ | $1.3 \times 10^{-3}$ |
| (S,S)-CPAD\textsuperscript{16} | TADF   | $2.5 \times 10^{-3}$ | $1.8 \times 10^{-3}$ |
| (S,S)-CAI-Cz\textsuperscript{17} | TADF   | $1.1 \times 10^{-3}$ | $1.7 \times 10^{-3}$ |

Scheme S1: Molecular structures of CsEu((-)hfbc)\textsubscript{4} and \textit{M-Pt} for Figure 2 analysis
Figure S1: Absorption (left) and circular dichroism (right) spectra of F8BT:[P]-aza[6]helicene thermally annealed (TA) films.

Figure S2: $g_{abs}$ (left) and $g_{PL}$ (right) spectra of F8BT:[P]-aza[6]helicene thermally annealed (TA) films measured from opposite direction.
Figure S3: Detailed CP-EL spectra of semi-transparent inverted CP-OLEDs. Device structure:

ITO/ZnO/PEIE/ F8BT:[P]-aza[6]helicene/TCTA/MoOx/Au (x nm)
Figure S4: Detailed CP-EL spectra of semi-transparent conventional CP-OLEDs.

ITO/PEDOT:PSS/TFB/ F8BT:[P]-aza[6]helicene/TPBi/Ca/Al (x nm)
Figure S5: Detailed CP-EL spectra of inverted CP-OLEDs with different reflective electrode.

ITO/ZnO/PEIE/ F8BT:[P]-aza[6]helicene/TCTA/MoOx/Ag (or Al) (120 nm)
In this section we explicitly derive the expressions of electric and magnetic transition dipoles in terms of the coefficients of plane-wave basis. The wavefunctions of HOMO/LUMO, i.e. $\psi_{0,1}$ can be expanded in the series of plane-wave functions as:

$$
|0, 1\rangle = \sum_G c_G^{0,1} e^{iG \cdot r} = |0^0, 1^0\rangle + |0^+, 1^+\rangle + |0^-, 1^-\rangle,
$$

where:

$$
|0^0, 1^0\rangle = \sum_G c_G^{0,1} e^{iG \cdot r} \bigg|_{G_z=0} = \sum_G c_G^{0,1} e^{iG \cdot r},
$$

$$
|0^+, 1^+\rangle = \sum_G c_G^{0,1} e^{iG \cdot r} \bigg|_{G_z>0} = \sum_G c_G^{0,1} e^{iG \cdot r},
$$

$$
|0^-, 1^-\rangle = \sum_G c_G^{0,1} e^{iG \cdot r} \bigg|_{G_z<0} = \sum_G c_G^{0,1} e^{iG \cdot r}.
$$

The electric dipole $\langle 0^+ | r_\alpha | 1^+ \rangle$ can be derived as:

$$
\langle 0^+ | r_\alpha | 1^+ \rangle = \int dr \left( \psi_0^{+\ast} r_\alpha \psi_1^{+\ast} \right)
$$

$$
= \int dr \sum_{G'}^{+} \sum_{G}^{+} \left( c_G^{0} r_\alpha c_G^{1} e^{i(G-G') \cdot r} \right)
$$

$$
= \sum_{G'}^{+} \sum_{G}^{+} \left( c_G^{0} c_G^{1} \left( i \frac{\partial}{\partial G_\alpha} \right) \right) \int dr \ e^{i(G-G') \cdot r}
$$

$$
= -i(2\pi)^3 \sum_{G'}^{+} \sum_{G}^{+} \left( c_G^{0} c_G^{1} \frac{\partial \delta(G-G')}{\partial G_\alpha} \right)
$$

$$
= -i(2\pi)^3 \sum_{G}^{+} c_G^{1} \left( \frac{\partial c_G^{0}}{\partial G_\alpha} \right),
$$

where two identities

$$
\int dr \ e^{i(G-G') \cdot r} = (2\pi)^3 \delta(G-G'),
$$

$$
\sum_{G'} f(G') \frac{\partial \delta(G-G')}{\partial \lambda} = \frac{\partial f(G')}{\partial \lambda},
$$

(S3)
have been used. The magnetic dipole $\langle 0^+|m_\alpha|1^+ \rangle$ can be similarly derived as:

$$\langle 0^+|m_\alpha|1^+ \rangle = \frac{e}{2m_e} \langle 0^+|L_\alpha|1^+ \rangle$$

$$= \frac{e\hbar}{2m_e} \sum_{G'}^+ \sum_{G} (c^0_{G'})^* c^1_{G} \left( G_y \frac{\partial}{\partial G_x} - G_x \frac{\partial}{\partial G_y} \right) \int d\mathbf{r} \ e^{i(G-G') \cdot \mathbf{r}} \tag{S4}$$

$$= -i(2\pi)^3 \frac{e\hbar}{2m_e} \sum_{G} c^1_{G} \left( G_y \frac{\partial}{\partial G_x} - G_x \frac{\partial}{\partial G_y} \right)^*.$$

The electric or magnetic dipole itself depends on the gauge choice of $|0\rangle$ and $|1\rangle$ but the products $x^{01}y^{10}$ and $r^{01} \cdot m^{10}$ is gauge independent.

### S2 CP and Orbital Angular Momentum (OAM)

In this section we relate the CP to an OAM-like quantity. The intensity difference between (right- and left- handed) circularly polarized light can be rewritten as:

$$I_L - I_R = -\frac{2\pi e^2}{\hbar} \text{Im}\left[x^{01}y^{10}\right] \delta(\varepsilon_1 - \varepsilon_0 - \hbar\omega)$$

$$= i\frac{\pi e^2}{\hbar} \left[ \langle 0| x | 1 \rangle \langle 1| y | 0 \rangle - (x \leftrightarrow y) \right] \delta(\varepsilon_1 - \varepsilon_0 - \hbar\omega)$$

$$= i\frac{\pi e^2}{\hbar} \left[ \langle 0| x | 1 \rangle \frac{-i\hbar \langle 1| p_y | 0 \rangle}{m_e(\varepsilon_1 - \varepsilon_0)} - (x \leftrightarrow y) \right] \delta(\varepsilon_1 - \varepsilon_0 - \hbar\omega)$$

$$= \frac{\pi e^2}{m_e\hbar\omega} \langle L^1_z \rangle_0 \delta(\varepsilon_1 - \varepsilon_0 - \hbar\omega) \tag{S5}$$

where $\langle L^1_z \rangle_0 = \langle 0| x | 1 \rangle \langle 1| p_y | 0 \rangle - \langle 0| y | 1 \rangle \langle 1| p_x | 0 \rangle$ is an OAM-like variable and $\langle \cdots \rangle_0$ means the expectation value at state $|0\rangle$. It should be noted that Eq. (S5) is a gauge-invariant form of CP-EL which is different from the gauge-dependent magnetic dipole $m^{01}_z$ or $m^{00}_z$ in Eq. (S4).
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