Double Neutron Star Populations and Formation Channels

Jeff J. Andrews1,2,3,4 and Ilya Mandel2,3,4

1 Niels Bohr Institute, University of Copenhagen, Blegdamsvej 17, DK-2100 Copenhagen, Denmark; jeff.andrews@nbi.ku.dk
2 Monash Centre for Astrophysics, School of Physics and Astronomy, Monash University, Clayton, VIC 3800, Australia; ilya.mandel@monash.edu
3 OzGrav: The ARC Center of Excellence for Gravitational Wave Discovery, Australia
4 Birmingham Institute for Gravitational Wave Astronomy and School of Physics and Astronomy, University of Birmingham, Birmingham B15 2TT, UK

Received 2019 April 29; revised 2019 July 1; accepted 2019 July 3; published 2019 July 18

Abstract

In the past five years, the number of known double neutron stars (DNSs) in the Milky Way has roughly doubled. We argue that the observed sample can be split into three distinct subpopulations based on their orbital characteristics: (i) short-period, low-eccentricity binaries; (ii) wide binaries; and (iii) short-period, high-eccentricity binaries. These subpopulations also exhibit distinct spin period and spindown rate properties. We focus on subpopulation (iii), which contains the Hulse–Taylor binary. Contrary to previous analysis, we demonstrate that, if they are the product of isolated binary evolution, the $P_{\text{orb}}$ and $e$ distribution of these systems requires that the second-born NSs must have been formed with small natal kicks ($<25 \, \text{km s}^{-1}$) and have pre-SN masses narrowly distributed around $3.2 \, M_\odot$. These constraints challenge binary evolution theory and further predict closely aligned spin and orbital axes, inconsistent with the Hulse–Taylor binary’s measured spin–orbit misalignment angle of $\approx 20^\circ$. Motivated by the similarity of these DNSs to B1217+11C, a DNS residing in the globular cluster M15, we argue that this subpopulation is consistent with being formed in, and then ejected from, globular clusters. This scenario provides a pathway for the formation and merger of DNSs in stellar environments without recent star formation, as observed in the host galaxy population of short gamma-ray bursts and the recent detection by LIGO of a merging DNS in an old stellar population.

Key words: binaries: close – stars: neutron – supernovae: general

1. Introduction

Shortly after the discovery of the first double neutron star (DNS), the Hulse–Taylor binary (B1913+16; Hulse & Taylor 1975), theorists derived evolutionary sequences describing the formation of these exotic systems in isolated stellar binaries (Flannery & van den Heuvel 1975; Webbink 1975). Their evolution typically involves a complex interplay of multiple mass transfer phases (both stable and unstable), two supernovae, and the effects of mass loss, tides, and rotation (Srivivasan & van den Heuvel 1982; Bhattacharya & van den Heuvel 1991; Tauris & van den Heuvel 2006). The canonical evolutionary sequence is described in detail in Tauris et al. (2017, and references therein). As pulsar surveys began to find more NS binaries, including several DNSs, it was realized that, although extraordinary, the Hulse–Taylor binary was by no means unique.

Stellar binary theory has progressed along with the expanding sample of Milky Way DNSs. Using binary population synthesis, a technique that evolves a population of high-mass binaries sampled from a distribution of initial conditions, studies generated synthetic DNS populations to uncover the properties of these systems, often with a focus on the rates of DNS mergers (Tutukov & Yungelson 1993; Portegies Zwart & Yungelson 1998; Belczynski & Bulik 1999). This technique is able to reproduce the broad characteristics of DNS populations (Portegies Zwart & Yungelson 1998; Oslowski et al. 2011; Andrews et al. 2015; Kruckow et al. 2018; Shao & Li 2018; Vigna-Gomez et al. 2018). The predictions of these studies were largely borne out with the recent detection of a merging DNS in gravitational waves by LIGO, GW170817, along with its electromagnetic counterpart (Abbott et al. 2017).

On the other hand, the detailed properties of DNS populations modeled with binary population synthesis do not always match the observed Galactic systems. Models predict too many systems with high eccentricity relative to observations (Ihm et al. 2006; Chruslinska et al. 2017), underpredict DNS masses (Vigna-Gomez et al. 2018), and predict lower DNS merger rates than the point estimate based on the single gravitational-wave observation to date (Belczynski et al. 2018; although a single fortuitous detection is by no means implausible given the predicted range of merger rates).

With recent observational efforts, there are now 17 known DNSs in the Milky Way field. In Section 2 we demonstrate that the current sample clusters into three subpopulations, and we describe their general characteristics. In Sections 3 and 4 we outline two separate formation scenarios, demonstrating that the short-period, high-eccentricity subpopulation is best explained through dynamical formation. We end with a discussion of our results and conclusions in Section 5.

2. DNS Subpopulations

Figures 1 and 2 show the orbital period ($P_{\text{orb}}$), eccentricity ($e$), spin period ($P_{\text{spin}}$), and spin period derivative ($\dot{P}_{\text{spin}}$) distributions of the current sample of 17 DNSs in the Milky Way field, along with the two known systems in globular clusters. The $P_{\text{orb}}-e$ distribution shows that systems with orbital periods $P_{\text{orb}} \lesssim 1$ day exhibit a gap in eccentricity at $e \approx 0.4$. We apply an agglomerative clustering algorithm (Pedregosa et al. 2011) to the $P_{\text{orb}}-e$ distribution of field DNSs to split the systems into three subpopulations. We highlight the clustering in Figures 1 and 2 using separate colors and plot symbols: subpopulation (i) contains binaries with small eccentricities that merge within a Hubble time; subpopulation (ii) consists of widely separated systems that do not merge...
within a Hubble time; and subpopulation (iii) includes binaries with orbital periods short enough to merge within a Hubble time but having eccentricities tightly clustered around 0.6. Clustering analysis formally associates the long-period, high-eccentricity system J1811–1736 with subpopulation (iii), but we opt to group it with the other long-period systems. We list the sample of known DNSs, their properties, and their associated subpopulations in Table 1.

Since they define the shape and size of the orbit, $P_{\text{orb}}$ and $e$ are sensitive indicators of the prior dynamical evolution of the system; differences in this space are indicative of differences in SN dynamics and mass transfer sequences (Andrews & Mandel 2019). At the same time, pulsars in binary systems occupy different regions in $P_{\text{spin}}^2$-$P_{\text{spin}}$ space depending principally on their accretion histories; pulsars that have accreted more mass during formation tend to achieve faster spin periods while simultaneously burying their magnetic field and spin axes.

3. Isolated Binary Evolution

We first consider the formation of DNSs through isolated binary evolution. The $P_{\text{orb}}$ and $e$ distribution of a population of DNSs resulting from isolated binary evolution is determined by the (distributions of) orbital separations before the second SN

### Notes.

* Tauris et al. (2017) and references therein.
* Unconfirmed DNS. The DNS nature of several other systems is based principally on their nonzero eccentricities. In some cases, dynamical formation may allow NS–WD systems with nonzero eccentricities.
* Stovall et al. (2018).
* Martinez et al. (2017).
* Lynch et al. (2018).
* Cameron et al. (2018).
(a), pre-SN He-star masses ($M_{\text{He}}$), SN kick velocities ($v_k$), and to a lesser extent, the systems’ post-SN evolution driven by the emission of gravitational waves (Andrews & Zezas 2019). This simplicity is due to the fact that pre-SN orbits are expected to be circular and SN kicks are assumed to be isotropically distributed in the orbital frame.

Figure 1 shows a clear gap in the observed eccentricity distribution ($0.3 < e < 0.6$) separating subpopulations (i) and (iii). In the top left panel of Figure 3, we compare the known Galactic DNSs with the predictions for isolated binary evolution from the binary population synthesis model of Vigna-Gómez et al. (2018, their fiducial model; gray points) for the population of DNSs immediately after the second SN. In the bottom left panel, we show the population after 100 Myr of orbital circularization and decay due to general relativity (GR). While Figure 3 shows that the population synthesis results can account for any individual DNS system, they predict a large number of systems within the observed eccentricity gap. Other binary population synthesis codes (e.g., Andrews et al. 2015; Kruckow et al. 2018) predict similar distributions.

We focus on the second supernova during DNS formation in order to understand the physical reason behind these population synthesis results. Using the equations for supernova dynamics from Hills (1983), we can calculate the post-SN distribution of $P_{\text{orb}}$ and $e$, given pre-SN $a$, $M_{\text{He}}$, and $v_k$ (see also Kalogera 1996; Tauris & Takens 1998; Andrews & Zezas 2019). For orbital modeling, we assume that all NSs have a mass of $1.4 M_\odot$.

BROADLY speaking, eccentricity in previously circular binaries can be produced by a combination of two types of kicks. The first are natal kicks imparted to the proto-NS upon collapse, responsible for the few hundred km s$^{-1}$ velocities of single pulsars in the Milky Way (Hobbs et al. 2005). Larger natal kicks tend to produce systems with higher eccentricities, provided they stay bound. The second, so-called “Blauuw” kicks (Blauuw 1961) are due to instantaneous mass loss that is symmetric in the frame of the collapsing object, but asymmetric in the binary’s center-of-mass frame. The eccentricity imparted to a circular binary by the Blauuw kick depends only on the fraction of the binary’s mass lost during the SN, with the post-SN eccentricity given by the ratio of the mass lost to the remaining binary mass (the binary is disrupted if this ratio exceeds 1).

By studying the evolution of massive post-common-envelope binaries comprised of an NS with a helium-main-sequence companion, Tauris et al. (2013, 2015) showed that binary evolution theory predicts that systems with small Blauuw kicks ought to also receive small natal kicks; upon expansion after the He-main-sequence, the system will enter a second phase of mass transfer, which reduces the mass of the secondary’s helium envelope to $\lesssim 0.5 M_\odot$. When this ultra-stripped core explodes in an SN, there is little mass loss and limited asymmetry, yielding small natal and Blauuw kicks consistent with subpopulation (i).

On the other hand, to reproduce systems through this channel with eccentricities $e \sim 0.6$, such as those observed in subpopulation (iii), the pre-SN binaries must have either large natal kicks, large Blauuw kicks, or both. In the top, middle left panel of Figure 3, we show the post-SN orbital distributions assuming a log-normal pre-SN orbital separation distribution (centered on $1 R_\odot$, with a standard deviation of 0.2 in log-space), a $3.2 M_\odot$ pre-SN He-star, and a kick velocity of either 25 km s$^{-1}$ (gray contours) or 125 km s$^{-1}$ (open contours). Comparison between the two sets of contours demonstrates the well-known effect that large kick velocities produce post-SN distributions with large spreads in eccentricity. The bottom, middle left panel of the same figure demonstrates that this conclusion is unaltered after GR circularization and orbital decay (using the equations from Peters 1964) have taken place.
Previous studies analyzing the detailed formation of the Hulse–Taylor binary through isolated binary evolution consistently suggested that it was formed with a kick velocity \( \geq 100 \text{ km s}^{-1} \) (Wang et al. 2006; Wong et al. 2010; Tauris et al. 2017). However, our results in Figure 3 indicate that systems formed with these large kicks ought to span a large eccentricity range, not form a cluster with \( e \approx 0.6 \) like the three systems comprising subpopulation (iii). Unless the observed sample is not representative of the overall Milky Way population (through either observational bias or small number statistics), we conclude that subpopulations (i) and (iii) likely form through distinct evolutionary channels. We consider this our acting hypothesis throughout the remainder of this work.

The second column of panels in Figure 3 shows how the tight clustering in subpopulation (iii) can be reproduced with \( v_k \approx 25 \text{ km s}^{-1} \) and \( M_{\text{He}} \approx 3.2 M_\odot \). In the third column of panels in Figure 3, using the same distribution of pre-SN a as was used in the second column of panels and a kick velocity of 25 km s\(^{-1}\), we generate separate distributions of post-SN orbits for \( M_{\text{He}} = 1.7, 2.3, 2.9, \) and \( 3.5 M_\odot \). These distributions all produce eccentricities either too small or too large for the observed systems.

Although only three systems comprise subpopulation (iii), the middle two columns in Figure 3 show that—assuming formation through isolated binary evolution—in order to explain the observed clustering, the second-born NSs in subpopulation (iii) systems must have kick velocities significantly less than 100 km s\(^{-1}\) (larger kick velocities produce a DNS distribution spanning too wide a range of orbital separations and eccentricities) and a finely tuned distribution of \( M_{\text{He}} \) near 3.2 \( M_\odot \). We stress that this requirement arises from the need to statistically match the full population of observed DNSs in \( P_{\text{orb}}-e \) space, meaning both a high probability of producing observed systems and a low probability of producing systems in regions of the parameter space where there are no observations.

Our conclusions about the formation of subpopulation (iii) challenge our understanding of isolated binary evolution. With a pre-SN mass of 3.2 \( M_\odot \), whatever mechanism (e.g., Janka 2017) causes the large natal kicks in single pulsars is unlikely to be suppressed. Furthermore, even if supernovae can produce low natal kicks from 3.2 \( M_\odot \) He-stars, some aspect of binary evolution must produce pre-SN orbits at a separation of \( \sim 1 R_\odot \) with He-star masses of \( \lesssim 2 M_\odot \) (to explain subpopulation (i)) and \( \approx 3.2 M_\odot \) (to explain subpopulation (iii)), but no binaries with intermediate masses.

4. Dynamical Formation

Although DNS dynamical formation has been largely ignored in recent years (although see Grindlay et al. 2006; Lee et al. 2010), there are two known DNSs that reside in globular clusters: B2127+11C in M15 (Anderson et al. 1990) and J1807−2500 in NGC 6544 (Lynch et al. 2012). Figures 1 and 2 show that one of these, B2127+11C, has \( P_{\text{orb}}, e, P_{\text{spin}}, \) and \( \dot{P}_{\text{spin}} \) similar to the three field DNSs forming subpopulation (iii). Either these similarities are coincidental or suggestive of a common evolutionary channel, in which case subpopulation (iii) systems would have been formed in a dense stellar environment such as a globular cluster, then dynamically kicked into the Milky Way field.\(^8\)

Provided the stellar cluster is largely devoid of black holes, which may decouple through the Spitzer instability and then be dynamically ejected (Spitzer 1969; but see, e.g., Morscher et al. 2013), NSs will be the most massive objects in a cluster older than \( \sim 5 \text{ Gyr} \). Subsequent mass segregation will cause the NSs to occupy the center of the cluster, where a series of capture, exchange, and flyby interactions will form NS binaries. On average, these interactions harden binaries, which sample a thermal eccentricity distribution, \( P(e) = 2e \) (Heggie 1975). This process continues until one of three things happens: (a) the binary runs out of objects to interact with (the interaction timescale becomes longer than the age of the universe: \( \tau_{\text{interaction}} > \tau_{\text{Hubble}} \)), leaving the binary “frozen” in the cluster; (b) GR-driven evolution takes over as the dominant force for tightening the binary (\( \tau_{\text{GW}} < \tau_{\text{interaction}} \)), in which case a DNS will merge within the cluster; or (c) the binary is ejected from the cluster because the momentum recoil kick from the last interaction exceeds the cluster’s escape velocity \( v_{\text{esc}} \), in which case a dynamically formed DNSs will be thrown into the Milky Way field.

These key timescales and their scalings with cluster properties are illustrated in Figure 4. We adopt fiducial parameters taken from dynamical models of the expanded core of M15, the host of B2127+11C (Dull et al. 1997): a central density \( n = 2.5 \times 10^7 \text{ pc}^{-3} \), a velocity dispersion \( v_{\text{disp}} = 10 \text{ km s}^{-1} \), and an escape velocity \( v_{\text{esc}} = 50 \text{ km s}^{-1} \), and assume an average interloper mass \( m = 1.4 M_\odot \). As in our isolated binary models, we assume a NS mass of \( 1.4 M_\odot \). Comparison of the various timescales in Figure 4 shows that dynamical interactions will drive a DNS to smaller orbital separations, until it is ejected from the cluster with an average separation \( a_{\text{ejection}} \approx 3.5 R_\odot \) (vertical dashed line).

The ejection of such tight DNSs can only occur in clusters that have sufficiently high escape velocities and interaction timescales shorter than the age of the universe. This likely requires core-collapsed clusters, such as M15, as somewhat less dense and less massive globular clusters are likely to form DNSs at wider separations (J1807−2500 is such a system), if at all.

Dynamically formed binaries are likely to have high eccentricities (Heggie 1975); however, since \( \tau_{\text{GW}} \sim (1 - e^2)^{7/2} \), the highest eccentricity systems will evolve and merge first. This is illustrated in the right panels of Figure 3, where we assume a log-normal separation distribution for ejected binaries (\( \mu = 0.45, \sigma = 0.1 \) in log-space in units of \( R_\odot \)) and a thermal eccentricity distribution. We then give every system a random birth time uniformly chosen in the last 100 Myr (the characteristic ages of the subpopulation (iii) systems are all between 100 and 150 Myr). The contours in the bottom right panel of Figure 3 show the distribution of these systems in \( P_{\text{orb}}-e \) space after GR orbital circularization and decay. The close match between the contours and the subpopulation (iii) DNSs suggests that dynamical evolution can in principle yield tight clustering in \( P_{\text{orb}}-e \) space.

---

8. Phinney & Sigurdsson (1991) propose this formation scenario for the Hulse–Taylor binary.
The Astrophysical Journal Letters, 880:L8 (6pp), 2019 July 20

Andrews & Mandel

5. Discussion and Conclusions

While some of the physics involved in binary evolution is complex and uncertain, the last two stages of DNS formation—the dynamical effect of the supernova on the orbit and the subsequent orbital decay due to gravitational radiation—involve well-understood physical processes. In this work, using the 17 known DNSs in the Milky Way field, we focus on the last two stages of DNS evolution and explore the conditions of the pre-SN DNS progenitors. Based on the observed systems’ $P_{\text{orb}}$, $e$, $P_{\text{spin}}$, and $P_{\text{pin}}$, we find that the distribution of systems may split into as many as three subpopulations. We focus on subpopulation (iii) systems, characterized by large eccentricities and small orbital separations. If formed through isolated binary evolution, we find that subpopulation (iii) would require relatively massive He-star progenitors $M_{\text{He}} \approx 3.2 M_\odot$, receiving small SN natal kicks ($v_k \approx 25 \text{ km s}^{-1}$). Larger kick velocities cannot reproduce the tight cluster of DNSs in $P_{\text{orb}}$–$e$ space, while even modestly altered He-star masses predict DNSs with either smaller or larger eccentricities.

Using additional information from the measured spin–orbit misalignment angle ($\approx 20^\circ$; Kramer 1998) and the position and velocity of the system in the Galaxy (using a dispersion measure–derived distance of $8.3 \pm 1.4 \text{kpc}$; previous works on DNS formation have consistently argued that the Hulse–Taylor binary (a member of subpopulation (iii)) requires a natal kick velocity of several hundred km s$^{-1}$ (e.g., Wong et al. 2010; Tauris et al. 2017). In particular, the spin–orbit misalignment angle of $\approx 20^\circ$ is inconsistent with a low SN kick velocity. This inconsistency reinforces our analysis in Section 3, which suggests that conventional binary evolution theory cannot simultaneously explain the low kicks and high He-star masses that we find best reproduces subpopulation (iii) in $P_{\text{orb}}$–$e$ space.

We emphasize that previous binary population synthesis studies find that the Hulse–Taylor binary is at the short-period edge of a steeply declining distribution in $P_{\text{orb}}$–$e$ space (Andrews et al. 2015; Kruckow et al. 2018; Vigna-Gómez et al. 2018). Furthermore, none of these studies predict a gap in the eccentricity distribution of DNSs between 0.3 and 0.6. Either future observations will fill in the gap in short-period DNSs for $0.3 < e < 0.6$, or an alternative formation scenario is required.

Based on their similarities with B2127+11C, a known DNS found in a globular cluster, we argue that subpopulation (iii) DNSs in the field may have been dynamically formed in a dense stellar environment, such as a globular cluster, and kicked out into the field. We find that the birth cluster should be characterized by a high central density of at least a few million objects per pc$^3$ and an escape velocity $>50 \text{ km s}^{-1}$—a combination best achieved at the centers of collapsed-core globular clusters such as M15.

Detailed simulations will need to address several challenges to this scenario. Black holes, which would otherwise readily substitute into DNS binaries, must be predominantly ejected from the cluster before the present epoch. Additionally, the pulsar had to be recycled, then substituted into a DNS binary, and finally ejected from the cluster within the $<150 \text{ Myr}$ characteristic age of subpopulation (iii) systems, which would seemingly require a very high interaction rate (see Grindlay et al. 2006); though the last two steps could be combined if a pulsar in a tight low-mass X-ray binary interacted with an NS. Furthermore, the three subpopulation (iii) binaries are all found within a few degrees of the Galactic plane, which, taken at face value, appears to be inconsistent with the orbits of globular clusters in the Milky Way; however, given that pulsar searches tend to narrowly focus on the Galactic plane, even systems ejected from globular clusters may be more likely to be observed when crossing the plane. Finally, the young characteristic ages and relatively short merger times of subpopulation (iii) binaries could indicate that implausibly large formation rates would be needed to explain their prevalence in the Milky Way field. Nevertheless, the existence of B2127+11C in the collapsed-core cluster M15 suggests that this formation channel indeed occurs, possibly providing a nonnegligible contribution to the overall rate of DNS mergers. Since dynamical formation predicts no correlation between the spin and orbital axes, measurements of the spin–orbit misalignment angles for more DNSs in subpopulation (iii) will help discern between different formation scenarios.

Regardless of their exact formation channel, the short merger times of subpopulation (iii) DNSs, combined with their young ($<150 \text{ Myr}$) characteristic ages, have profound implications. If they are formed through isolated binary evolution, the short delay times between formation and merger of subpopulation (iii) systems potentially provide a route to the $r$-process enrichment of globular clusters and ultra-faint dwarf galaxies (Ji et al. 2016). While isolated binary evolution also produces some DNSs with long delay times (Kruckow et al. 2018; Vigna-Gómez et al. 2018), if subpopulation (iii) systems are formed dynamically in old globular clusters many Gyr after a

---

9 Deller et al. (2018) recently published a VLBI parallax measurement placing the system at a distance of 4.1 kpc; this new distance halves both the Hulse–Taylor binary’s height off the Galactic plane, and its peculiar velocity.

10 Note, however, that characteristic ages may be a poor proxy for the true age of recycled pulsars, especially those coming from globular clusters, where the pulsar may have undergone several accretion phases.
star formation episode, they will naturally explain the abundance of DNS mergers and short gamma-ray bursts in non-star-forming galaxies (Grindlay et al. 2006), potentially including NGC 4993, the host galaxy of the recently detected DNS merger GW170817 (Abbott et al. 2017).

We thank Kyle Kremer, Claire Ye, Carl Rodriguez, Michele Trenti, and Thomas Tauris for useful discussions. We additionally thank the referee for comments and suggestions that greatly improved the quality of the manuscript. J.J.A. acknowledges support by the Danish National Research Foundation (DNRF132).

ORCID iDs

Jeff J. Andrews https://orcid.org/0000-0001-5261-3923
Ilya Mandel https://orcid.org/0000-0002-6134-8946

References

Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017, PhRvL, 119, 161101
Alpar, M. A., Cheng, A. F., Ruderman, M. A., & Shaham, J. 1982, Natur, 300, 728
Anderson, S. B., Gorham, P. W., Kulkarni, S. R., Prince, T. A., & Wolszczan, A. 1990, Natur, 346, 42
Andrews, J. J., Farr, W. M., Kalogera, V., & Willems, B. 2015, ApJ, 801, 32
Andrews, J. J., & Zezas, A. 2019, MNRAS, 486, 3213
Belczynski, K., Askar, A., Arca-Sedda, M., et al. 2018, A&A, 615, A91
Belczyński, K., & Bulik, T. 1999, A&A, 346, 91
Bhattacharya, D., & van den Heuvel, E. P. J. 1991, PhR, 203, 1
Blaauw, A. 1961, BAN, 15, 265
Bray, J. C., & Eldridge, J. J. 2018, MNRAS, 480, 5657
Cameron, A. D., Champion, D. J., Kramer, M., et al. 2018, MNRAS, 475, L57
Chruslinska, M., Belczynski, K., Bulik, T., & Gladysz, W. 2017, A&A, 67, 37
Dettler, A. T., Weisberg, J. M., Nicc, D. J., & Chatterjee, S. 2018, ApJ, 862, 139
Dull, J. D., Cohn, H. N., Lugger, P. M., et al. 1997, ApJ, 481, 267
Flannery, B. P., & van den Heuvel, E. P. J. 1975, A&A, 39, 61
Grindlay, J., Portegies Zwart, S., & McMillan, S. 2006, NatPh, 2, 116
Heggie, D. C. 1975, MNRAS, 173, 729
Hills, J. G. 1983, ApJ, 267, 322
Hobbs, G., Lorimer, D. R., Lyne, A. G., & Kramer, M. 2005, MNRAS, 360, 974
Hulse, R. A., & Taylor, J. H. 1975, ApJL, 195, L51
Ihm, C. M., Kalogera, V., & Belczynski, K. 2006, ApJ, 652, 540
Janka, H.-T. 2017, ApJ, 837, 84
Ji, A. P., Frebel, A., Chiti, A., & Simon, J. D. 2016, Natur, 531, 610
Kalogera, V. 1996, ApJ, 471, 322
Kramer, M. 1998, ApJ, 509, 856
Kruckow, M. U., Tauris, T. M., Langer, N., et al. 2018, MNRAS, 481, 1908
Lee, W. H., Ramirez-Ruiz, E., & van de Ven, G. 2010, ApJ, 720, 953
Lynch, R. S., Freire, P. C. C., Ransom, S. M., & Jacoby, B. A. 2012, ApJ, 745, 109
Lynch, R. S., Swiggum, J. K., Kondratiev, V. I., et al. 2018, ApJ, 859, 93
Martinéz, J. G., Stovall, K., Freire, P. C. C., & Portegies Zwart, S. F. 2017, ApJL, 851, L29
Morscher, M., Umbreit, S., Farr, W. M., & Rasio, F. A. 2013, ApJL, 763, L15
Olsoski, S., Bulik, T., Gondek-Rosińska, D., & Belczyński, K. 2011, MNRAS, 413, 461
Pedregosa, F., Varoquaux, G., Gramfort, A., et al. 2011, J. Mach. Learn. Res., 12, 2825
Peters, P. C. 1964, PhRv, 136, 1224
Phinney, E. S., & Sigurdsson, S. 1991, Natur, 349, 220
Portegies Zwart, S. F., & Yungelson, L. R. 1998, A&A, 332, 173
Radhakrishnan, V., & Srinivasan, G. 1982, CSci, 51, 1096
Shao, Y., & Li, X.-D. 2018, ApJ, 867, 124
Spitzer, L., Jr. 1969, ApJL, 158, L139
Srinivasan, G., & van den Heuvel, E. P. J. 1982, A&A, 108, 143
Stovall, K., Freire, P. C. C., Chatterjee, S., et al. 2018, ApJL, 854, L22
Tauris, T. M., Kramer, M., Freire, P. C. C., et al. 2017, ApJ, 846, 170
Tauris, T. M., Langer, N., Moriya, T. J., et al. 2013, ApJL, 778, L23
Tauris, T. M., Langer, N., & Podsialwoski, P. 2015, MNRAS, 451, 2123
Tauris, T. M., & Takens, R. J. 1998, A&A, 330, 1047
Tauris, T. M., & van den Heuvel, E. P. J. 2006, in Formation and Evolution of Compact Stellar X-ray Sources, ed. W. H. G. Lewin & M. van der Klis (Cambridge: Cambridge Univ. Press), 623
Tutukov, A. V., & Yungelson, L. R. 1993, MNRAS, 260, 675
Vigna-Gómez, A., Neijssel, C. J., Stevenson, S., et al. 2018, arXiv:1805.07974
Wang, C., Lai, D., & Han, J. L. 2006, ApJ, 639, 1007
Webbink, R. F. 1975, A&A, 41, 1
Wong, T.-W., Willems, B., & Kalogera, V. 2010, ApJ, 721, 1689