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Characterization of the low-temperature properties of a simplified protein model

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Prompted by results that showed that a simple protein model, the frustrated Gō model, appears to exhibit a transition reminiscent of the protein dynamical transition, we examine the validity of this model to describe the low-temperature properties of proteins. First, we examine equilibrium fluctuations. We calculate its incoherent neutron-scattering structure factor and show that it can be well described by a theory using the one-phonon approximation. By performing an inherent structure analysis, we assess the transitions among energy states at low temperatures. Then, we examine nonequilibrium fluctuations after a sudden cooling of the protein. We investigate the violation of the fluctuation-dissipation theorem in order to analyze the protein glass transition. We find that the effective temperature of the quenched protein deviates from the temperature of the thermostat, however it relaxes towards the actual temperature with an Arrhenius behavior as the waiting time increases. These results of the equilibrium and nonequilibrium studies converge to the conclusion that the apparent dynamical transition of this coarse-grained model cannot be attributed to a glassy behavior.

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I. INTRODUCTION

Proteins are fascinating molecules due to their ability to play many roles in biological systems. Their functions often involve complex configurational changes. Therefore the familiar aphorism that “form is function” should rather be replaced by a view of the “dynamic personalities of proteins” [1]. This is why proteins are also intriguing for theoreticians because they provide a variety of yet unsolved questions. Besides the dynamics of protein folding, the rise in the time averaged mean square fluctuation ⟨Δr²⟩ occurring at temperatures around ≈200 K, sometimes called the “protein dynamic transition” [2–4], is arguably the most considerable candidate in the search of unifying principles in protein dynamics. Protein studies lead to the concept of energy landscape [5,6]. According to this viewpoint a protein is a system which explores a complex landscape in a highly multidimensional space and some of its properties can be related to an incomplete exploration of the phase space. The protein glass transition, in which the protein appears to “freeze” when it is cooled down to about 200 K, is among them. Protein folding too can be related to this energy landscape. The famous kinetic limitation known as the Levinthal paradox, associated to the difficulty to find the native state among a huge number of possible configurations, is partly solved by the concept of a funneled landscape which provides a bias towards the native state.

These considerations suggest that the dynamics of the exploration of protein phase space deserves investigation, particularly at low temperature where the dynamic transition occurs. But, in spite of remarkable experimental progress which allows us to “watch protein in action in real time at atomic resolution” [1], experimental studies at this level of detail are nevertheless extremely difficult. Further understanding from models can help in analyzing the observations and developing new concepts. However, studies involving computer modeling to study the dynamics of protein fluctuations are not trivial either because the range of time scales involved is very large. This is why many mesoscale models, which describe the protein at scales that are larger than the atom, have been proposed. Yet, their validity to adequately describe the qualitative features of a real protein glass remains to be tested.

In this paper we examine a model with an intermediate level of complexity. This frustrated Gō model [7,8] is an off-lattice model showing fluctuations at a large range of time scales. It is though simple enough to allow the investigation of time scales which can be up to 10⁹ times larger than the time scales of small amplitude vibrations at the atomic level. The model, which includes a slight frustration in the dihedral angle potential which does not assume a minimum for the positions of the experimentally determined structure, exhibits a much richer behavior than a standard Gō model. Besides folding one observes a rise of fluctuations above a specific temperature, analogous to a dynamical transition [9,10], and the coexistence of two folded states. This model has been widely used and it is therefore important to assess to what extent it can describe the qualitative features of protein dynamics beyond the analysis of folding for which it was originally designed. This is why we focus our attention on its low-temperature properties in an attempt to determine if a fairly simple model can provide some insight on the protein dynamical transition. The purpose of the present article is to clarify the origin of the transition in the computer model, and to determine similarities and differences with respect to experimental observations. Although the calculations are performed with a specific model, the methods are more general and even raise some questions for experiments, especially concerning the nonequilibrium properties.

This article is organized as follows. The numerical findings relating to the “dynamical transition” from previous studies [9,10] are presented in Sec. II. As a very large body of experimental studies of protein dynamics emanates from neutron scattering experiments, it is rational to seek a connection between theory and experiment by studying the most relevant experimental observable for dynamics, the incoherent structure factor (ISF). We calculate the ISF from molecular dynamics simulations of the model in Sec. III. We show that its main features can be well reproduced by a
II. A DYNAMICAL TRANSITION IN A SIMPLE PROTEIN MODEL?

Following earlier studies [9–11] we chose to study a small protein containing the most common types of secondary structure elements (α helix, β sheets, and loops), protein G, the B1 domain of immunoglobulin binding protein [12] (Protein Data Bank code 2GB1). It contains 56 residues, with one α helix and four β strands forming a β sheet. We describe it by an off-lattice Gō model with a slight frustration which represents its geometry in terms of a single particle per residue, centered at the location of each Cα carbon in the experimentally determined tertiary structure. The interactions between these residues do not distinguish between the types of amino acids. Details on the simulation process and the parametrization of the model are presented in the Appendix. In spite of its simplicity, this model appears to exhibit properties which are reminiscent of the protein dynamical transition. This shows up when one examines the temperature dependence of its mean-squared fluctuations [9] by calculating the variance $\Delta r^2$ of the residue distances to the center of mass as a function of temperature, defined by

$$\Delta r^2 = \frac{1}{N} \sum_{i=1}^{N} (r_{i0}^2 - r_{00}^2).$$  

Here, $N$ denotes the number of residues, and $r_{i0}$ is distance of residue $i$ with respect to the instantaneous center of of mass. The average $\overline{A}$ of the observable $A(t)$ is the time average $\overline{A} = \frac{1}{T} \int_0^T dt \, A(t)$. The variances of 20 trajectories (Langevin dynamics simulations, each $3 \times 10^7$ time units long) were averaged for each temperature point ($\langle \cdot \rangle$ denotes the average over independent initial conditions).

Figure 1 shows the evolution of $\langle \Delta r^2 \rangle$ as a function of temperature. It exhibits a crossover in the fluctuations in the temperature range $T/T_f = [0.4, 0.5]$ resembling the transition observed for hydrated proteins in neutron scattering and Mössbauer spectroscopy experiments [2–4], the so-called dynamical transition. Above $T/T_f = 0.4$, the fluctuations increase quickly with temperature whereas a smaller, linear, growth is observed below. One may wonder whether the complexity of the protein structure, reflected by the Gō model, is sufficient to lead to a dynamical transition or whether, notwithstanding the resemblance of the onset of fluctuations in the present model and the experimentally determined transition, different physical and not necessarily related events may contribute to the curves which by coincidence look similar. One can already note that, for a folding temperature in the range 330–350 K, the range 0.4–0.5 $T/T_f$ corresponds to 132–175 K, lower than the experimentally observed transition occurring around 180–200 K. If it had been confirmed the observation of a dynamical transition in a fairly simple protein model would have been very useful to shine a new light on this transition which is still not fully understood. It is generally agreed that it is hydration dependent [13], but still different directions for a microscopic interpretation are being pursued, suggesting the existence [14] or nonexistence [15] of a transition in the solvent coinciding at the dynamical transition temperature. Recently, a completely different mechanism based on percolation theory for the hydration layer has been proposed [16]. The precise nature of the interaction between the solvent and proteins, and the driving factor behind the transition, hence still remain to be understood. The dynamical transition has often been called the protein glass transition due to its similarity with some physical properties of structural glasses at low temperatures. In particular, it was pointed out that, for both glasses and protein solutions, the transition goes along with a crossover towards nonexponential relaxation rates at low temperatures. The comparison is however vague since the glass transition itself and notably its mechanism are ongoing subjects of research and debate.

Our goal in this paper is to clarify the origin of the numerically observed transition, which moreover gives hints on the possibilities and limits of protein computer models.

III. ANALYSIS OF THE INCOHERENT STRUCTURE FACTOR

If computer models of proteins are to be useful they must go beyond a simple determination of the dynamics of the atoms,
and make the link with experimental observations. This is particularly important for the “dynamical transition” because its nature in a real protein is not known at the level of the atomic trajectories. It is only observed indirectly through the signals provided by experiments. Therefore a valid analysis of the transition observed in the computer model must examine it in the same context, i.e., determine its consequences on the experimental observations.

Along with NMR and Mössbauer spectroscopy, neutron scattering methods have been among the most versatile and valuable tools to provide insight on the internal motion of proteins [17,18]. Indeed, the thermal neutron wavelength being of the order of Å and the kinetic energy of the order of meVs, neutrons provide an adequate probe matching the length and frequency scales of atomic motion in proteins. An aspect brought forward in the discussion of the dynamical transition frequency scales of atomic motion in proteins. An aspect.

In neutron scattering the vibrational and conformational changes in proteins appear as a quasielastic contribution to the double-differential scattering cross section which gives the probability of finding a neutron in the solid angle element which contains crucial information about the dynamics of a monochromatic beam of neutrons with incident energy exchange $dE$ after scattering. The total cross section of the experiment is obtained by integration over all angles and energies. Neglecting magnetic interaction and only considering the short-range nuclear forces, the isotropic scattering is characterized by a single parameter $b_i$, the scattering length of the atomic species $i$ [20], which can be a complex number with a nonvanishing imaginary part accounting for absorption of the neutron. If one defines the average over different spin states $b_{coh} = |\langle b \rangle|$ as the coherent scattering length, and the root-mean-square deviation $\Delta b = \sqrt{\langle |b|^2 \rangle - |\langle b \rangle|^2}$ as the incoherent scattering length, the double-differential cross section arising from the scattering of a monochromatic beam of neutrons with incident wave vector $k_0$ and final wave vector $k$ by $N$ nuclei of the sample can be expressed as [20]

$$\frac{d^2\sigma}{d\Omega dE} = \frac{N}{\hbar} \frac{|k|}{|k_0|} (b_{coh}^2) S_{coh}(q,\omega),$$

$$+ \frac{N}{\hbar} \frac{|k|}{|k_0|} (b_{inc}^2) S_{inc}(q,\omega),$$

where $q = k - k_0$ is the wave vector transfer in the scattering process and $r_i$ denote the time-dependent positions of the sample nuclei and the coherent and incoherent dynamical structure factors are

$$S_{coh}(q,\omega) = \frac{1}{2\pi N} \sum_{i,j} \int_{-\infty}^{\infty} dt \ e^{-i\omega t} \langle e^{-i q (r_j(t) - r_i(0))} \rangle,$$

$$S_{inc}(q,\omega) = \frac{1}{2\pi N} \sum_{i,j} \int_{-\infty}^{\infty} dt \ e^{-i\omega t} \langle e^{-i q (r_j(t) - r_i(0))} \rangle.$$
different conformational substates. anharmonic dynamics involving several minima associated to 

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T/T_f different curves, from bottom to top, correspond to the temperatures offset to avoid the overlap of curves at different temperatures. The shows a magnification of the structure factor in the low frequency 

thermostat). The unit of time has been converted to absolute units 

using the approximate conversion factor 1 t.u. = 

leads to a broadening and a shift of these modes until they 

amplitude and the structure becomes flexible.

The analysis of the incoherent structure factor has shown 

the alignment procedure can efficiently eliminate contributions 

trajectories. At low temperatures when fluctuations are small, 

does not preserve the total momentum of the system. The 

additional technical difficulties because Langevin dynamics 

the spectra remains the same as the one shown on Fig.2(b). 

A further analysis can be carried out to determine whether 

the low-temperature behavior of the protein model shows 

a complex glassy behavior or simply the properties of an 

harmonic network made of multiple bonds. The picture of a rough energy landscape of a protein with many minima 

separated by barriers of different height does not exclude 

the possibility that, in the low-temperature range, the system behaves as if it were in thermal equilibrium in a single 

minimum of this multidimensional space. This would be the 

case if the time scale to cross the energy barrier separating this minimum from its neighbor basins were longer than the 

observation time (both in numerical or real experiments). In 

this case, it should be possible to describe the low-temperature behavior of the protein in terms of a set of normal modes. To determine if this is true for the Gō model that we study, one can compare the spectrum obtained from thermalized numerical simulations at low temperature (low temperature curves on Fig. 2) with the calculation of the structure factor in terms of phonon modes, in the spirit of the study performed in Ref. [23] for the analysis of inelastic neutron scattering data of staphylococcal nuclease at 25 K on an all-atom protein model. 

The theoretical basis for a quantitative comparison is an 

approximate expression of the quantum-mechanical structure factor \( S(q, \omega) \) in the so-called one-phonon limit which only 

accounts for single quantum process in the scattering events 

assuming harmonic dynamics of the nuclei. In this approxi-

mation, the incoherent structure factor can be written as

\[
S_{\text{inc}}(q, \omega) = \sum_i \sum_\lambda \frac{b_i^2 e^{\frac{\hbar \omega_i}{2}} e^{-2 W_i(q) \beta} |\hat{e}_i(q e_{\lambda,i})|^2}{[4m_i \omega_i \sinh(\beta \hbar \omega_i/2)]^{-1} \delta(\omega - \omega_i)}. 
\]  

Here, the indices \( i \) and \( \lambda \) denote the atom and normal modes indices respectively. \( e_{\lambda,i} \) is the subvector relating to the coordinates of particle \( i \) of the normal mode vector associated to index \( \lambda \). \( W_i(q) \) denotes the Debye-Waller factor, which in the quantum calculation of harmonic motion reads [23]

\[
W_i(q) = \sum_\lambda \frac{\hbar |q e_{\lambda,i}|^2}{m_i \omega_\lambda} [2n(\omega_\lambda) + 1], 
\]  

\( n(\omega) \) being the Bose factor associated to the energy level \( \omega \).

For the calculations of the structure factor in the Gō model within this approximation, we average \( S_{\text{inc}}(q, \omega) \) on a shell of \( q \) vectors by transforming the Cartesian coordinate vector \( (q_x, q_y, q_z) \) into spherical coordinates 

\[
\text{inc} 
\]  

B. Structure factor from normal mode analysis in the one phonon approximation

FIG. 2. (Color online) Incoherent structure factor \( S_{\text{inc}}(q = 4 \ \AA^{-1}, \omega) \) as a function of temperature for protein G (Nosé-Hoover thermostat). The unit of time has been converted to absolute units using the approximate conversion factor 1 t.u. = 0.1 ps. Panel (a) shows a magnification of the structure factor in the low frequency range. The structure factors in this panel have been shifted with an offset to avoid the overlap of curves at different temperatures. The different curves, from bottom to top, correspond to the temperatures \( T/T_f \) listed on the side of each panel.

The analysis of the incoherent structure factor has shown that the low-temperature dynamics of the Gō model is dominated by harmonic contributions. An increase of temperature leads to a broadening and a shift of these modes until they eventually become continuously distributed. However, for both strong and weak coupling to the heat bath, no distinct change of behavior can be detected within the temperature range \( T/T_f = [0.4, 0.5] \) in which Fig. 1 shows an apparent dynamical transition. Instead, the numerical results suggest a continuous increase of anharmonic dynamics, and the absence of a dynamical transition in this model, even though, in the range \( T/T_f = [0.4, 0.5] \), the peaks of the structure factor in the Nosé-Hoover simulations broaden significantly. In the lowest temperature range the structure factor does not show any contribution reminiscent of a Boson peak.
The freezing of the dynamics of a protein at temperatures below the "dynamic transition" is also described as a "glass transition." This leads naturally to consider an energy landscape with many metastable states, also called "inherent states" in the vocabulary of glass transitions. In Refs. [9,11] we showed that the thermodynamics of a protein can be well described in terms of its inherent structure landscape, i.e., a reduced energy landscape which does not describe the complete energy surface but only its minima. This picture is valid at all temperatures, including around the folding transition and above. For our present purpose of characterizing the low-temperature properties of a protein and probe its possible relation with a glassy behavior, it is therefore useful to examine how the protein explores its inherent structure landscape in the vicinity of the dynamic transition. Here, we shall try to find how the number of populated minima changes with temperature around the transition region $T/T_f = [0.4,0.5]$ for the Gō model of protein $G$, and which conformational changes can be associated to these inherent structures.

For three selected temperatures $T_1 = 0.275$ T$_f$, $T_2 = 0.39$ T$_f$, $T_3 = 0.482$ T$_f$ shown in Fig. 1, we generated ten trajectories from independent equilibrated initial conditions for $2 \times 10^6$ reduced time units using the Nosé-Hoover thermostat. Along each trajectory, a minimization was performed every
The width of the circles is proportional to $1/2 \log(w)$ where $w$ is the total number of occurrences of a given minimum. 

$2 \times 10^4$ time units such as to yield $N_m = 20\,000$ minima for each temperature point. In the classification of these minima and their graphical representation, we only keep those minima which have been visited at least two times within the $N_m$ minima, which lead to discard less than ten events from the total number of counts. Most of the counts are concentrated on a small number of inherent structures. In Fig. 4, we show the relative populations of the inherent structures on a two-dimensional subspace spanned by the inherent structure energy and the structural difference with the experimental structure measured by the dissimilarity factor [10,24]. The radius of the circles centered at the location of the minima on this plane is set proportional to $1/2 \log(w)$ where $w$ is the absolute number of counts of this minimum along the trajectories. This definition is necessary to allow the graphical representation on the plane, however, it may visually mask that linear differences in the radii translate into exponential differences of the frequency of visit of the minimum. As an example, the minima $\alpha_0, \alpha_4, \alpha_2, \alpha_3$ have the occupation probabilities $p(\alpha_0) = w(\alpha_0)/N_m \approx 92\%$, $p(\alpha_1) \approx 8\%$, $p(\alpha_2) \approx 0.1\%$, and $p(\alpha_3) \approx 0.02\%$ at $T = T_f$.

From Fig. 4, we notice that already at $T_1$ more than one minimum is populated though the global minimum $\alpha_0$ is dominant. In these figures, lines are drawn between minima that are connected along the trajectory, i.e., that form a sequence of events. It should however be noted that since the sampling frequency is low, it cannot be excluded that an intermediate corresponding to an additional connection line is skipped. Connections between all minima may therefore exist even though they did not appear in the sequences observed in this study. Moving to higher temperatures $T_2$ and $T_3$, a larger number of minima which are both higher in energy and structural dissimilarity appear. As the temperature rises, their population numbers become more important, as can be seen, e.g., by inspection of the radii of the block $\alpha_4-\alpha_7$ in Fig. 4. To obtain a physical picture of the conformational changes associated with these minima, it is useful to align their coordinates onto the coordinates of the global minimum. The results of such an alignment are shown in Fig. 5. In this figure, the coordinates of the effective Gō-model particles located at the positions of the $C_\alpha$ atoms for each amino acid are drawn in red color. One notices that the conformational changes associated to $\alpha_1-\alpha_3$ are small. It is interesting to notice that these small changes already appear in the range of temperatures where the rise in fluctuations seems to grow still linearly with the temperature. The next higher minima involve in particular a reorientation of a turn within the $\beta$ sheets of a protein. The temperature range at which these minima start to be populated coincides with the transition region revealed by the mean-distance displacement $\langle \Delta x^2 \rangle$, suggesting that the anharmonic motion required to make transitions between the basins of these minima is at its origin.

We again observe that the dynamic transition region does not exhibit any particular change of behavior that could deserve the name of “transition,” but rather a gradual evolution which gets noticeable in the range $T/T_f = [0.4,0.5]$. In the next section we use a nonequilibrium approach to reveal whether the dynamics below the transition range can be characterized as “glassy” or not.
V. TEST OF THE FLUCTUATION-DISSIPATION THEOREM (FDT)—A NONEQUILIBRIUM APPROACH

An alternative approach to study the low-temperature transition, for which equilibrium simulations take a significant amount of computer time, consists in the test of the response of the protein to external perturbations. Rather than waiting a long time to see rare fluctuations dominating the average fluctuation at low temperatures, the system is driven out of equilibrium on purpose to either observe the relaxation back to equilibrium and its associated structural changes, or the response to a continuous perturbation to be compared to fluctuations at equilibrium.

The fluctuation-dissipation theorem (FDT) relates the response to small perturbations and the correlations of fluctuations at thermal equilibrium for a given system. In the past years, the theorem and its extensions have become a useful tool to characterize glassy dynamics in a large variety of complex systems [25]. For glasses below the glass transition temperature, the equilibrium relaxation time scales are very large so that thermal equilibrium is out of reach [26]. Consequently, the FDT cannot be expected to hold in these situations, and the response functions and correlation functions depend not only on time, but also on the initial conditions.

In our studies we start from a given initial condition and put the system in contact with a thermostat during a waiting time \( t_w \). The end of the waiting time is selected as the origin of time \( t = 0 \) for our investigation. If \( t_w \) is large enough (strictly speaking \( t_w \to \infty \)) the system is in equilibrium at \( t = 0 \). We denote the Hamiltonian of the unperturbed system \( H_0 \), which under a small linear perturbation of the order \( \epsilon(t) \) acting on an observable \( B(t) \) becomes

\[
H = H_0 - \epsilon(t)B(t),
\]

where for \( \epsilon = 0 \) we recover the unperturbed system. For any observable \( A(t) \), we accordingly define the two ensemble averages \( \langle A(t) \rangle_0^{t_w} \) and \( \langle A(t) \rangle_\epsilon^{t_w} \) where the index references the average with respect to the unperturbed or perturbed system respectively and the exponent \( t_\epsilon \) indicates how long the system was equilibrated before the start of the investigation. The correlation function in the unperturbed system relating the observables \( A(t), B(t') \) at two instances of time \( t, t' \) is defined by

\[
C_{AB}(t,t') = \langle A(t)B(t') \rangle_0^{t_w} - \langle A(t) \rangle_0^{t_w} \cdot \langle B(t') \rangle_0^{t_w}.
\]

The susceptibility \( \chi_{AB}(t) \), which measures the time-integrated response of the of the observable \( A(t) \) at the instant \( t \) to the perturbation \( \epsilon(t') \) at the instant \( t' \), reads

\[
\chi_{AB}(t) = \int_{t_0}^{t} dt' \frac{\delta \langle A(t) \rangle_\epsilon^{t_w}}{\delta \epsilon(t')}.
\]

The index \( B \) in the susceptibility indicates that the response is measured with respect to the perturbation arising from the application of \( B(t) \), and the lower bound \( t_0 \) of the integral indicates the instant of time at which the perturbation has been switched on.

The integrated form of the FDT states that the correlations and the integrated response are proportional and related by the system temperature at equilibrium,

\[
\chi_{AB}(t) = \frac{1}{k_B T} \Delta C \quad \text{with}
\]

\[
\Delta C = [C_{AB}(t,t) - C_{AB}(t,0)].
\]

In the linear response regime for a sufficiently small and constant field \( \epsilon \), the susceptibility can be approximated as

\[
\chi_{AB}(t) \approx \frac{\langle A(t) \rangle_\epsilon^{t_w} - \langle A(t) \rangle_0^{t_w}}{\epsilon}
\]

such that in practice, verifying the FDT accounts for the comparison of observables on both perturbed and unperturbed trajectories. The basic steps for a numerical experiment aiming to verify the FDT can be summarized as follows:

(i) Initialize two identical systems 1 and 2, 1 to be simulated with and 2 without perturbation.

(ii) Equilibrate both systems without perturbation during \( t_w \).

(iii) At time \( t_0 \) (in practice \( t_0 = 0 \), i.e., immediately after the end of the equilibration period) switch on the perturbation for system 1 and acquire data for both systems for a finite time \( t_{\text{FDT}} \).

(iv) Repeat the calculation over a large number of initial conditions to yield the ensemble averages \( \langle \gamma \rangle_0^{t_w} \) and \( \langle \gamma \rangle_\epsilon^{t_w} \); combine the data according to Eq. (11).

The protocol may be modified to include an external perturbation which breaks the translational invariance in time. For instance the initial state can result from a quench from a high to a low temperature. Then the system is only equilibrated for a short time \( t_w \) before the perturbation in the Hamiltonian is switched on. In this case the distribution of the realizations of the initial conditions is not the equilibrium distribution so that the correlation function defined by Eq. (9) depends on the two times \( t \) and \( t' \) and not only on their difference.

A. Simulation at constant temperature

This case corresponds to \( t_w \to \infty \). In our calculations we start from an initial condition which as been thermalized for at least 5000 time units. The first step is to make an appropriate choice for the perturbative potential \( \epsilon(t)B(t) \). An earlier application of the FDT to a protein model [27] has used the perturbative term

\[
\epsilon(t)B(t) = \epsilon \sum_{i=1}^{N} \cos(k y_i),
\]

where \( k \) is a scalar, \( y_i \) is the \( y \) coordinate of amino acid \( i \), and \( \epsilon \neq 0 \) for \( t > t_0 \) a constant. This perturbation is invariant neither by a translation of the system nor by its rotation. Although this does not invalidate the FDT, this choice poses some problems for the accuracy of the calculations because, even in the absence of internal dynamics of the protein, the perturbation varies as the molecules diffuse in space or rotate.
To avoid this difficulty we selected the perturbation

$$W := -\epsilon B(t) = -\epsilon \sum_{i=1,\ldots,28} \cos(k r_{i,28}),$$

(14)

where \(r_{i,28}\) is the distance between amino acid \(i\) and the amino acid 28 which has been chosen as a reference point within the protein because it is located near the middle of the amino-acid chain. Such a potential only depends on the internal state of the molecule, while it remains unaffected by its position in space.

To test the FDT for the Gô model of protein \(G\) using Eqs. (11) and (12), we add this potential \(W\) to the potential energy \(V\) of the model and we select \(A(t) = B(t)\). The thermal fluctuations are described with the same Langevin dynamics as previously.

We switch on the perturbation for the equilibrated protein model and record 50,000–400,000 trajectories (depending on the value of \(\epsilon\) of duration 2000 time units for temperatures in the range \(T/T_f = [0.275, 0.826]\) covering both the low-temperature domain and the approach of the folding transition of the protein. The perturbation prefactors chosen in this first set of simulations were \(\epsilon = 0.05\) and \(\epsilon = 0.005\), and the wave number of the cosine term was \(k = 2\pi/10\).

Figure 6 shows the evolution of the relation between the susceptibility and the variation of the correlation function \(\Delta C = C_{AB}(t,t) - C_{AB}(t,0)\). The straight lines represent the slopes expected from the FDT. One notices that, for \(\epsilon = 0.05\), at \(T = 0.826 T_f\), in the long term the value of \(\chi/\Delta C\) stabilizes around a value which is away from the expected value \(1/k_BT\). From a first glance, this result is reminiscent of the properties of a glass driven out of equilibrium. In this context, the deviation from the slope expected from the FDT is interpreted as the existence of an "effective temperature" for non-equilibrium systems. For the case studied here, finding an effective temperature would be surprising as the results are obtained from measurements on a thermalized protein model, i.e., a system in a state of thermal equilibrium. How is it then possible to explain the apparent deviation from the FDT? The calculations performed with \(\epsilon = 0.005\) give the clue because they show that the deviation appeared because the perturbation was too large and outside of the linear response regime assumed to calculate the susceptibility because for this lower value of \(\epsilon\) the deviation has vanished.

If one computes the average value of the perturbation energy \(\langle W \rangle\) and compares it to the protein average energy \(\langle E(U) \rangle\), for the case shown in Fig. 6, \(\epsilon = 0.05\), one finds \(\langle W \rangle/\langle E(U) \rangle = 1.3 \times 10^{-2}\). This is small, but, at temperatures which approach \(T_f\) the protein is a highly deformable object and even a small perturbation can bring it out of the linear response regime. This shows up by a rise of \(\chi\) versus time for \(\epsilon = 0.05\). At low temperatures the protein is more rigid and therefore more resilient to perturbations. The insets in Fig. 6 show that for \(\epsilon = 0.05\) the calculations find that the fluctuation-dissipation relation at \(T = 0.275 T_f\) is almost perfectly verified although a very small deviation can still be detected for this value of \(\epsilon = 0.05\). Therefore a careful choice of parameters is necessary to test the FDT under controlled conditions. In particular, the perturbation needs to be carefully chosen to only probe the internal dynamics and not to dominate them.

**B. Simulation of quenching**

A typical signature of a glassy system is its aging after a perturbation. In the context of the protein “glass transition,” one can therefore expect to detect a slow evolution of the system as a function of the time after which it has been brought to the glassy state. This is usually tested in quenching experiments, which can be investigated by a sharp temperature drop in the numerical simulations. Our calculations start from an equilibrium state at high temperature \(T = 1.40 T_f\), which is abruptly cooled at a temperature \(T_q\) below the temperature of the dynamical transition studied in the previous sections. The model protein is then maintained at this temperature \(T_q\) by a Langevin thermostat. After a waiting time \(t_w\), we start recording the properties of the system over a time interval \(t_{\text{DFT}} = 25,000\) units of time (t.u.) to probe the fluctuation dissipation relation. In order to avoid nonlinear effects we use a small value of \(\epsilon = 0.005\). For such a weak perturbation, the response is weak compared to thermal fluctuations and a large number of realizations (50,000 or more) is necessary to achieve reliable statistical averages. To properly probe the phase space of the model, these averages must be made over different starting configurations before quenching. This is achieved by starting the simulations from a given initial condition properly thermalized at \(T = 1.40 T_f\) in a preliminary calculation. Then we run a short simulation at this initial temperature, during
FIG. 7. (Color online) Time evolution of the energy above the ground state, in units of $k_B T_f$, after a temperature jump from $T = 1.4 T_f$ to $T = 0.367 T_f$ for two different waiting times $t_w$, indicated in the title of each panel. The figure shows the evolution of the energy for 15 realizations (corresponding to the different colors) for the time $t_{FDT} = 25 000$ t.u.

which the unfolded conformations change widely from a run to another with different random forces because at high temperatures the fluctuations of the protein are very large. The conformations reached after this short high-$T$ thermalization are the conformations which are then quenched to $T_q$, for the FDT analysis.

Typical results are shown on Figs. 7 and 8 for two values of $t_w$. The time evolution of the energy shows that, after the waiting time $t_w$, even for the largest value $t_w = 50 000$ t.u. the model protein is still very far from equilibrium because its energy is well above the ground state energy (chosen as the reference energy $0$). This nonequilibrium situation sometimes leads to rapid energy drops, generally accompanied by a decrease of the dissimilarity with the native state, which superimpose to random fluctuations which have to be expected for this system in contact with a thermal bath. As expected the sharp variations of the conformations are more noticeable for the shortest waiting time. Figure 8 shows that, while for small values of $\Delta C = [C_{AB}(t, t) - C_{AB}(t, 0)]$, which also correspond to shorter times after we start to collect the data for the FDT test, the variation of $\chi_{AB}(t)$ versus $\Delta C$ follows the curve given by the FDT relation, then at larger $\Delta C$ the curve shows a significant deviation from the slope $1/T$. The effective temperature is larger for short waiting times after the quench and decreases when $t_w$ increases. This should be expected because, in the limit $t_w \to \infty$ we should have $T_{eff} \to T$ when the system reaches equilibrium.

It is not surprising to find a deviation from the FDT behavior after a strong quench of the protein model because we put the system very far from equilibrium. Therefore the observation of an effective temperature that differs from the actual temperature of the system is not a sufficient indication to conclude at the existence of a glassy state of the protein model. What is important is the time scale at which the system tends to equilibrium and how it depends on temperature. To study this we have performed a systematic study of the variation of $T_{eff}(t_w, T)$ as a function of the waiting time $t_w$ and temperature $T$, at the temperatures...
$T = 0.1875 T_f$, $T = 0.2752 T_f$, $T = 0.3670 T_f$, $T = 0.4128 T_f$, and $T = 0.4817 T_f$. The temperature domain that we can study numerically is limited both from below and from above. At the lowest temperatures the relaxation of the system is very slow so that $t_w$ must be strongly increased. Moreover the speed at which the protein model explores its phase space by moving from an inherent structure to another becomes very low and statistically significant data cannot be obtained without a large increase of $t_{FDT}$. Running enough calculations to get a good average on the realizations becomes unpractical. As discussed above, at high temperatures the protein becomes “soft” so that one quickly leaves the linearity domain of the FDT, unless the applied perturbation becomes very small. But then the large thermal fluctuations reduce the signal to noise ratio. Therefore the advantage of faster relaxation times at high temperature is whipped out by the need to make statistical averages over a much larger number of realizations. However, the temperature range over which one can get statistically significant results overlaps the number of realizations. However, the temperature range over which the model appear to grow faster (Fig. 1) so that one could expect to observe a change in the properties of the system at this temperature, if it existed.

At a given temperature $T$ we have defined a relaxation time $\tau(T)$ by assuming that the effective temperature relaxes exponentially towards the actual temperature according to

$$\left( \frac{T_{\text{eff}}}{T} - 1 \right) \propto \exp \left( - \frac{t_w}{\tau(T)} \right). \quad (15)$$

Figure 9 shows that this assumption is well verified by the numerical calculations. It should however be noticed that, for the longest waiting times, we may observe a large deviation from the exponential decay, as shown in Fig. 9 for the results at $T = 0.4128 T_f$. We attribute this to the limitations of our observations because, when the system has sufficiently relaxed so that its effective temperature approaches the actual temperature, all subsequent relaxations become extremely slow and may exceed the observation time $t_{FDT}$ above which the fluctuations of the model appear to grow faster (Fig. 1) so that one could expect to observe a change in the properties of the system at this temperature, if it existed.

FIG. 9. Variation of the effective temperature $T_{\text{eff}}$ as a function of the waiting time $t_w$ at two temperatures, $T = 0.2572 T_f$ (open circles) and $T = 0.4128 T_f$ (closed squares). The figure shows $\ln(T_{\text{eff}}/T - 1)$ vs $t_w$. The lines show a linear fit that takes into account the error bars on the determination of $T_{\text{eff}}$ determined as explained in the caption of Fig. 8. Such a fit determines $\tau(T)$ and its the standard deviation. For $T = 0.4128 T_f$, the point corresponding to the largest value of $t_w$ is not included in the fit (see the discussion in the text).

Figure 10 shows the variation of $\tau(T)$ with temperature, in logarithmic scale, versus $T_f/T$. It shows that, except for the value at the lowest temperature $T = 0.1875 T_f$, i.e., $T_f/T = 5.45$, within the numerical errors evaluated at each stage of our calculation, the relaxation time obeys a standard Arrhenius relation

$$\tau(T) = \tau_0 \exp \left( \frac{E_a}{T} \right) \quad (16)$$

with an activation energy $E_a/(k_B T_f) = 0.5668 \pm 0.1799$. At the lowest temperature, the relaxation temperature estimated from the Arrhenius law is $\tau(T = 0.1875 T_f) \approx 100000$ t.u. so that calculations with $t_w \gg 100000$ as well as $t_{FDT} \gg 100000$ would be necessary, which is unpractical. However, the observed deviation from Arrhenius law at low $T$ cannot be attributed to a low-temperature glass transition because such a transition would lead to a relaxation time larger than predicted by the Arrhenius relation, while we observe the opposite. In any case the Arrhenius relation is well verified for a temperature range which overlaps the temperature $T \approx 0.45 T_f$, i.e., $T_f/T \approx 2.22$, above which dynamical simulations suggested a possible increase of the fluctuations (Fig. 1). Therefore the relaxation of the protein model after a quench appears to follow
a standard activated process, with an activation energy of the order of \(0.57k_BT_f\), without any sign of a glassy behavior. These observations can be compared with other studies of the fluctuations of the same Go model of protein \(G\) \([9,28]\). Paper \([9]\) investigated the fluctuation \textit{in equilibrium} below the folding temperature \(T_f\). In these conditions, the numerical simulations of a protein which is near its native state detect small, up and down, jumps of the dissimilarity factor, which, in any case, stays very low \((d \approx 0.06\) for the equilibrium temperature \(T = 0.55T_f\)) but switches between values that differ by \(\approx 0.01\). In its equilibrium state the protein may jump from an inherent structure to another but these fluctuations are much slower than the one that we observed shorter after a temperature quench because they occur on a time scale of the order of \(10^7\) t.u. Their activation energy had been found to be \(E_B = 6.2T_f\), i.e., much higher than the activation energy \(E_a\) that characterizes the relaxation of the effective temperature that we measured. Those results are not in contradiction because they correspond to fundamentally different phenomena. The nonequilibrium fluctuations that we discuss in the present paper appear because the potential energy surface has minima on the side of the “funnel” that leads to the native state. Such minima, corresponding to protein structures which are not fully folded, can temporarily trap the protein in intermediate states. However the lifetime of these structures which are not fully folded, can temporarily trap the protein in intermediate states. However the lifetime of these high-energy minima is only of the order of \(10^7\) t.u., i.e., they are short lived compared to the residence time of the protein in an inherent structure close to the native state. When the protein escapes from one of these high-energy minima we observe an energy drop, as shown in Fig. 7.

The study that we presented here is neither a study of the protein near equilibrium, nor an investigation of the full folding process which also occurs on much longer time scales \((\text{typically }10^7–10^8\text{ t.u.})\) as observed in Refs. \([9]\) and \([28]\). Therefore the activation energy \(E_a\) is also different from the energy barrier for folding. For the same reason the effective temperature after the quench \(T_{\text{eff}}\) should not be confused with the configurational temperature \(T_{\text{cnf}}\) defined in Ref. \([28]\) which relates the entropy and energy of the inherent structures during folding. \(T_{\text{cnf}}\) gives a global view of the phase space explored during folding, and it evolves with a characteristic time of \(10^7–10^8\) t.u. as the folding itself. Compared to these scales, the FDT analysis that we presented here appears as a snapshot of the strongly nonequilibrium state created after a fast quench. It offers a new view of the time evolution of the protein model, which completes the ones which had been presented earlier.

VI. DISCUSSION

The starting point of our study has been the numerical observation of a low-temperature transition in a simplified protein model resembling the experimentally observed dynamical transition in hydrated protein samples. This suggested that, in spite of its simplicity, the frustrated Go model could be used not only to study the folding of proteins but also their dynamics in the low-temperature range, opening the way for an exploration of the glassy behavior of proteins.

We have therefore used different approaches to further characterize the properties of the protein model in the low-temperature range. Thermalized molecular dynamics simulations have been used to calculate the incoherent structure factor than one could expect to observe for the protein. It shows peaks that broaden as temperature increases, suggesting that the dynamics of the protein model is dominated by harmonic or weakly anharmonic vibrations. This has been confirmed by the calculation of the structure factor in the one-phonon approximation. All the main features of the structure factor obtained by simulations, such as the peak positions and even the power law decay of the amplitude of the modes with frequency, are well reproduced. In the low-temperature range, the dynamics of the protein appears to occur in a single energy well of its highly multidimensional energy landscape. Of course this is no longer true when the temperature increases.

By analyzing the population of the inherent structures, we have shown that, in the temperature range of the dynamical transition, there is a continuous increase of the number of states which are visited by the protein. The transition seems to be continuous, and it is likely that numerical observations suggesting a sudden increase may have the origin in the limited statistics due to finite time observation. Indeed, as shown for the example of protein \(G\), the conformational transitions become extremely slow at low temperatures, such that the waiting time between the jumps between conformations may exceed the numerical (or the experimental) observation time. It is this breakdown of the ergodic hypothesis together with the observation of nonexponential relaxation rates which may have led to the emergence of the terminology “protein glass transition” in analogy to the phenomenology of glasses.

Nonequilibrium studies allowed us to systematically probe a possible glassy behavior by searching for violations of the fluctuation-dissipation theorem. First we have shown that these calculations must be carried out with care because apparent violations are possible, even when the system is in equilibrium, due to nonlinearities in the response. Except at very low temperatures they can be observed even for perturbations as low as 1% of the potential energy of the system. Once this artifact is eliminated by the choice of a sufficiently small perturbative potential, we have shown that, after a sudden quench from an unfolded state to a very low temperature \(T_G\), one does observe a violation of the FDT in the protein model, analogous to what is found in glasses. The quenched protein is characterized by an effective temperature \(T_{\text{eff}} > T_G\), but the relaxation of the model towards equilibrium, deduced from the evolution of the effective temperature \(T_{\text{eff}}\) as a function of the waiting time after the quench, follows a standard Arrhenius behavior, even when the temperature crosses the value \(T \approx 0.45T_f\) at which dynamical simulations appeared to show a change in the amplitude of the fluctuations.

Although one cannot formally exclude that the results could be different for other protein structures or other simplified protein models, this work concludes that a coarse-grain model such as the Go model is too simple to describe the complex behavior of protein \(G\) and particularly its glass transition. Indeed such a model does not include a real solvent, which plays an important role in experiments. The thermostat used in the molecular dynamics simulations only partially models the effect of the surrounding of the protein. The apparent numerical transition previously observed for protein \(G\) may simply be related to finite-time observations of the activation of structural transitions which appears in a particularly long
time scale for proteins. This is an obvious limitation of molecular dynamics calculations, but this could also sound as a warning to experimentalists. Indeed experiments can access much longer time scales. But they also deal with real systems which are much more complex than the Gō model. In these systems relaxations may become very long, so that the experimental observation of a transition could actually face the same limitations as the numerical simulations. Such a “time window” interpretation has also been brought forward for the experimentally observed dynamical transition, suggesting that the transition may in fact depend on the energy resolution, and thus, on the time resolution of the spectrometer [29]. In this respect, as shown by our nonequilibrium studies to test the validity of the FDT, such measurements, if they could be performed for a protein, should tell us a lot about the true nature of the “glass transition” of proteins.

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APPENDIX: SIMULATION AND UNITS

The forcefield and the parametrization of the simplified Gō model are presented in [9,10]. In a standard Gō model the potential energy is written in such a way that the experimental energy state is the minimal energy state. We use here a weakly frustrated Gō model for which the dihedral angle potential does not assume a minimum in the reference position defined by the experimentally resolved structure: it favors angles close to π/4 and 3π/4 irrespective of the secondary structure element (helix, sheet, turn) the amino acid belongs to. This source of additional “frustration” affects the dynamics and thermodynamics of the model, leading to a more realistic representation [10]. This feature introduces additional complexity in the model because, besides its ground state corresponding to the experimental structure, the frustrated model exhibits another funnel for folding, which leads to a second structure which is almost a mirror image of the ground state, but has a significantly higher energy (Fig. 11).

To control temperature in the molecular dynamics simulations, several types of numerical thermostats were used. Most of the calculations use underdamped Langevin simulations [30,31] with a time step dt = 0.1 t.u. and friction constants in the range γ = 0.01, 0.025. The mass of all the residues is assumed to be equal to m = 10. Some calculations were also performed with the multithermostat Nose-Hoover algorithm using the specifications defined in [32].

For simulation purposes, the variables in the Gō model are chosen dimensionless (reduced units). Lengths are expressed in units of ʽt is 1 meaning that reduced temperatures are expressed in absolute units. It is possible to estimate the energy scale of the model by comparing the reduced folding temperature of the Gō model with a realistic order of magnitude of the folding temperature T′ f in units of K and setting

\[
k_B T_f = \tilde{\epsilon} k_B T_f,
\]

where the variables on the left-hand side are given in SI units (T′ f is the estimate of the folding temperature), and unprimed variables are written in reduced units; ʽ is the required energy scale in units of J to match between both. In our calculations k_B = 1 (meaning that reduced temperatures are expressed in reduced energy units) and T_f = 0.218 is deduced from equilibrium simulations. Then a simple dimensional analysis gives the time unit of the model as ʽ \( t = \sqrt{\frac{m \tilde{\epsilon}}{k_B T_f}} \). One arrives at an estimated time unit of ʽ \( t \approx 0.1 \) ps. In the paper we refer to ʽ \( t \approx 0.1 \) ps as the unit of time (t.u.) for the simulations of the Gō model, keeping in mind that this can merely be seen as an order of magnitude in view of the approximations that lead to this number.

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