Wide-Gamut and Polarization-Independent Structural Color at Optical Sub-diffraction-Limit Spatial Resolution Based on Uncoupled LSPPs

Jiancun Zhao 1,2, Xiaochang Yu 1,2, Kui Zhou 1,2, Xiaoming Yang 1,2 and Yiting Yu 1,2*

Abstract
The decreasing pixel size of digital image sensors for high-resolution imaging brings a great challenge for the matching color filters. Currently, the conventional dye color filters with pixel size of several microns set a fundamental limit for the imaging resolution. Here, we put forward a kind of structural color filter with circular nanohole-nanodisk hybrid nanostructure arrays at sub-diffraction-limit spatial resolution based on the uncoupled localized surface plasmon polaritons (LSPPs). Due to the uncoupled LSPPs taking effect, the pixel could generate an individual color even though operating as a single element. The pixel size for the minimum color filtering is as small as 180 × 180 nm 2, translating into printing pixels at a resolution of ~ 141,000 dots per inch (dpi). In addition, through both the experimental and numerical investigations, the structural color thus generated exhibits wide color gamut, large viewing angle, and polarization independence. These results indicate that the proposed structural color can have enormous potential for diverse applications in nanoscale optical filters, microscale images for security purposes, and high-density optical data storage.

Keywords: Structural color, Wide color gamut, Sub-diffraction-limit resolution, Uncoupled LSPP effect, Large viewing angle, Polarization independence

Introduction
Digital image sensors, which have been widely used for photography, video imaging, and machine vision, are advancing toward the direction of miniaturization and high resolution. It brings a great challenge for the conventional optical elements such as color filters to improve the spatial resolution [1]. An ultrahigh-resolution digital image sensor with imaging unit size of 50 nm by vertical nanorod arrays was demonstrated in 2015 [2], while the unit size of traditional color filter mainly fabricated by organic dye polymers or chemical pigments was as large as several micrometers. Thus, one color filter unit will cover several imaging units and cause a loss to the imaging resolution, which could not meet the demand for the future high-resolution imaging [3].

Recently, color filtering based on structural colors provides an alternative method to control light spatially [4–6]. The structural color is mainly based on the interaction between light and various nanostructures rather than materials, so it is capable to generate much smaller pixel sizes than the pixels achieved today in image sensors [7–11]. Abbe’s classical diffraction limit states that the minimum resolvable distance between two closely spaced objects is at best half the wavelength used for imaging in visible light [12]. Since the discovery of extraordinary optical transmission (EOT) phenomenon in 1998 [13], plasmonic effects have been widely used for designing structural color filters (SCFs), providing a possibility for the color filter to realize a spatial resolution reaching the sub-diffraction limit [14–17]. At present, many kinds of SCFs have been reported with a variety of plasmonic nanostructures [18], such as periodic subwavelength
nanohole arrays [19–21], plasmonic nanodisks [22–24], hybrid nanohole-nanodisk structures [25–28], and subwavelength metal gratings [29–32]. For the applications of SCFs in image sensors, the small pixel size, wide color gamut, large viewing angle, and polarization independence are the major issues to be addressed. Burgos et al. exhibited a kind of plasmonic SCFs based on the periodic metallic subwavelength hole arrays. The colors were set by the periodicity of plasmonic building blocks due to the coupling effect, resulting in micrometer-sized pixels [33]. Structural colors generated from all-dielectric metasurfaces with a high refractive index and low loss offer high saturation and high efficiency [34, 35]. Sun et al. presented a kind of all-dielectric structural color generated by the electric and magnetic resonances in TiO$_2$ metasurfaces. However, the distinct colors could only be observed when the metasurface was reduced to around 1.6 μm [36], Horie et al. reported a kind of transmissive color filters based on periodical subwavelength silicon nanoholes that could replace conventional dye-based color filters used in backside-illuminated CMOS image sensor technologies. Nevertheless, its pixel size could only be shrunk down to nearly 1 μm and only had an insensitive response to $a \pm 20^\circ$ angular range [37]. Yang et al. introduced a kind of reflective color filter based on asymmetric Fabry-Perot cavities, which could get a minimum pixel size of 500 nm [38]. Zeng et al. demonstrated a kind of plasmonic subtractive color filter based on the one dimensional (1D) nanogratings patterned in a single optically thin Ag film, generating extremely small pixel size close to the optical diffraction limit due to the short-range interactions of surface plasmon polaritons (SPPs). However, it was sensitive to the incident polarization [39]. Kumar et al. presented an approach for full-color printing by encoding color information into Ag/Au nanodisks raised above a holey backreflector. The color thus generated was preserved even as individual pixels of $250 \times 250 \text{nm}^2$, enabling color printing at a resolution of ~ 100,000 dpi, close to the diffraction-limited resolution [40]. Small (tens of nanometers) isolated semiconductor nanostructures can be used to generate the scattering colors; however, they do not scatter strongly enough to be viewed plainly in a bright-field reflection microscope [41].

Here, we propose a kind of structural color with circular nanohole-nanodisk hybrid nanostructure arrays based on the uncoupled localized surface plasmon polaritons (LSPPs), obtaining an individual color pixel size of $180 \times 180 \text{nm}^2$, corresponding to a spatial resolution of ~141, 000 dpi. In addition, the structural color thus generated reveals a wide color gamut with a large viewing angle and strong polarization insensitive property. An illustrative color palette is obtained by changing the geometrical parameters of the hybrid nanostructures, including the primary component colors of cyan, magenta, and yellow (CMY). The simulation results demonstrate that the realized colors exhibit a large angular invariant feature up to ± 40°. Moreover, the circular shape of nanostructures makes the demonstrated structural color reveal a strong polarization independence. Furthermore, due to the uncoupled LSPPs taking effect in light field modulation, the individual color pixel can be generated even though operating as a single element, resulting in the achievement of sub-diffraction-limit resolution. As a proof-of-concept demonstration, an image containing colorful letters is printed by the suggested nanostructures.

**Methods**

The proposed plasmonic structural colors are reflective square-lattice circular nanodisk-nanohole hybrid nanostructure arrays on silicon substrate, as shown in Fig. 1a. The 25 nm Ag was directly evaporated onto the 120 nm polymethyl methacrylate (PMMA) pillars with 1 nm Cr as the adhesion layer. Here, silicon was selected as the substrate due to its high conductivity, which is convenient for the electron-beam lithography (EBL) fabrication. Ag was specifically chosen as the metallic layer due to its low extinction coefficient. Furthermore, its inherent formation of a thin (~ 2–3 nm) oxide layer (Ag$_2$O) that will cause a slight shift in the spectra, but it has a little effect on the structural color performance [17].

Figure 1b shows the schematics of the fabrication process for the nanostructures as suggested. Firstly, the electron-beam resist PMMA with the thickness of 120 nm was spin-coated onto the silicon substrate (Fig. 1b-i). And then, the PMMA nanopillar templates were exposed by the NanoBeam Limited nB5 system with an accelerating voltage of 100 kV and a beam current of 100 pA. The development process was performed by immersing the sample in methyl isobutyl ketone (MIBK) solution at 25 °C for 2 min, followed by rinsing in isopropl alcohol (IPA) for 2 min. Finally, the sample was blow-dried under a steady stream of N$_2$ (Fig. 1b-ii). And then, an adhesion layer of Cr (1 nm) and an Ag film (25 nm) were deposited by an e-beam evaporator system (Fig. 1b-iii). Figure 1c shows the SEM images of the ultimately achieved circular nanodisk-nanohole hybrid structure array.

**Results and Discussion**

**Wide Color Gamut**

Figure 2a displays a palette of experimentally reflected colors obtained by changing the diameter $D$ and period $P$ of the nanostructure arrays. Corresponding positions of these colors are plotted in the CIE 1931 color space, as shown in Fig. 2b, which confirms the capability for achieving the main CMY colors ranging from cyan to magenta to yellow. The reflectivity is then characterized
using the NOVA-EX spectrometer established on the microscopic system (Olympus-BX53) with the illuminating wavelength ranging from 400 to 800 nm. The reflection signals are collected by an objective lens (MPlanFL N, NA = 0.9, 100×). Figure 2c presents the experimental reflective spectra of the samples, the valleys redshift as \( D \) varies from 70 to 110 nm. Moreover, for the same structures, the simulated reflective spectra obtained by the finite-difference time-domain (FDTD) method shown in Fig. 2d are in qualitative agreement with the corresponding experimental results, where valleys redshift with the increasing \( D \). However, it still exists a little difference due to the shape and size deviations from nanofabrication, and the refractive indices, as well as the thicknesses in the experiment, could be slightly different from those used in the simulation. The contour maps of the experimental reflective spectra plotted in Fig. 2e, f demonstrate that the impact of period \( P \) on spectral modulation is fairly small, while the diameter \( D \) plays a dominant role for the spectral control, which is different from the situation where the period is the main factor reported in other common literatures [19–21, 33, 36, 37]. And this property makes it possible to define colors with only one single nanostructure.

**Physical Mechanism**

It is known that the optical properties of periodical nanostructures are largely dependent on the distance between nanostructures, especially when the distance is relatively small. This is because the coupling effect associated with the hybridization of the dipole or higher multipolar plasmons between nanostructures lead to variations in the collective plasmon energy [26, 42, 43]. However, the coupling effect limits the pixel size, and sometimes causes the non-negligible resonant peak shift or peak split, thus leading to unexpected color generation [17]. Due to the short propagation distance of short-range surface plasmon polaritons (SRSPPs) and small decay length of LSPPs, as the separation increases, the coupling effect becomes weaker, and interactions between neighboring nanostructures become negligible [23]. Hence, in order to avoid the coupling effect and
achieve a kind of structural color reached to the sub-diffraction-limit resolution, the space between nanoparticles must be large enough and the size of the unit cell should be less than the diffraction-limited size.

In order to analyze the underlying physical mechanism of the color filtering effect, the nanostructure arrays with large and small inter-particle distances have been analyzed by using the FDTD method. Figure 3 presents the simulated electric field ($|E|^2$) distribution results at reflective valleys and long incident wavelength of 600 nm, respectively. For the structure with a large inter-particle distance, no matter at short (Fig. 3a) or long (Fig. 3b) incident wavelength, the strong electric-field intensity distributions are both merely confined at the edges of the nanodisks and nanoholes, demonstrating that there is nearly no coupling LSPPs existing. In comparison, for the structure with a small inter-particle distance, as shown in Fig. 3c, the electric-field intensity...
confined on the Ag/Air interface demonstrates that it exists the SRSPPs coupling effect at short incident wavelength. And in Fig. 3d, the electric-field intensity limited in the gap between nanodisks illustrates that there is a strong LSPPs coupling effect at long incident wavelength. Therefore, when the distance is small, both the LSPPs and the SRSPPs coupling effect are in charge of light field modulation, while for the structure with a larger distance, there is nearly no coupling effect.

In our design, the inter-particle distance is large enough to avoid the coupling effect, so the observed colors in Fig. 2a are mainly modulated by the uncoupled LSPP modes. The property of LSPP mode is relevant to the shape and size of the nanoparticles [44–46]; thus, the resonant wavelength of the designed structure is mainly controlled by the diameters of the nanostructure (shown in Fig. 2f). And due to the uncoupling effects, the reflective valleys stay almost unchanged as the period increases, corresponding with the experimental results shown in Fig. 2e.

**Polarization Independence and Large Viewing Angle**

Both polarization independence and large viewing angle are necessary for the color filter in image sensing applications. Considering the circular shape of the nanostructure is symmetric along the x and y directions, it can be concluded that the proposed structural color is polarization independent. To investigate the viewing angle effect, the reflective spectra under various incident light angles have been analyzed by the FDTD method. The simulation model is built based on the schematic diagram shown in Fig. 1a. And the Broadband Fixed Angle Source Technique (BFAST) is used. The complex refractive indices of the material for simulations are based on the data from Palik in the material library of the software. The simulated results for both p-polarization and s-polarization shown in Fig. 4a, b illustrate that the reflective spectra almost keep invariant with the incident angle up to ± 40°, demonstrating a large viewing angle.

**Super High Resolution**

Owing to the uncoupled LSPPs, our design offers a kind of high spatial resolution structural color with pixel size at optical sub-diffraction limit. To verify the achievement of super high resolution, a set of resolution test structures are fabricated. The checkered patterns consisting of nanostructures with 5 × 5, 5 × 4, …, 2 × 1, 1 × 1 arrays with size of P = 180 nm, and D = 80 nm are shown in Fig. 5a (a bright-field microscope optical image (left) and an SEM image (right)). As expected, in Fig. 5a-i, the arrays with only one nanostructure can still generate the magenta color, even though it is a single pixel without periodicity. The individual magenta pixel with a unit cell area of 180 × 180 nm² demonstrates that this structure could form a pixel of color on a 180-nm-pitch grid and reach to a super high resolution of ~ 141,000 dpi.
The designed color pixels for subwavelength printing applications are demonstrated by showing microscopic colorful letters with sub-diffraction-limit pixel resolution. We printed the letters of “Nature, Science” with the corresponding structural colors, as shown in Fig. 5b-ii. Figure 5b-i, b-iii shows the SEM images of the regions outlined in Fig. 5b-ii. In Fig. 5b-ii, the top point on the letter “i” can be clearly visible, once again proving that even a single nanostructure can act as a color element. This feature gives rise to print resolution at the single-nanostructure level, which could provide extremely high spatial resolution for applications in high-density optical data storage and microscale images for security purposes.

Conclusions
In conclusion, the structural color at optical sub-diffraction-limit spatial resolution generated by the circular nanohole-nanodisk hybrid structure arrays is introduced, which exhibits the wide color gamut, large viewing angle, and strong polarization independence. Due to the uncoupled LSPPs taking effect, the color pixel sizes can reach to $180 \times 180 \text{ nm}^2$, exhibiting a high resolution up to ~ 141,000 dpi. And by simply changing the geometrical parameters of the nanostructure, the demonstrated structural color can span the whole CMY color system. Moreover, the simulation results demonstrate that the structural color exhibits a high angular tolerance up to $\pm 40^\circ$. Furthermore, this structure has the advantage of individual color generation at a sub-diffraction-limit pixel. As a proof-of-concept demonstration, a colorful letter image has been acquired with this structure. The proposed plasmonic structural color thus generated has the potential for applications in nanoscale color filters to satisfy the demand about super-high-resolution imaging, and could be used for security purposes, and high-density optical data storage.

Abbreviations
BFAST: Broadband Fixed Angle Source Technique; CMY: Cyan, magenta, yellow; dpi: Dots per inch; EBL: Electron-beam lithography; EOT: Extraordinary optical transmission; FDTD: Finite-difference time-domain; IPA: Isopropyl alcohol; LSPPs: Localized surface plasmon polaritons; MIBK: Methyl isobutyl ketone; PMMA: Polymethyl methacrylate; SCFs: Structural color filters; SPPs: Surface plasmon polaritons; SRSPPs: Short-range surface plasmon polaritons

Acknowledgements
We would like to thank the Analytical & Testing Center of Northwestern Polytechnical University for the EBL fabrication.

Authors’ Contributions
The idea of the study was conceived by YY. JZ carried out the numerical stimulation and wrote the manuscript. XY and KZ performed the experiment. XY and JZ contributed to the discussion of the results. All the authors have read and approved the final manuscript.

Funding
The National Natural Science Foundation of China (51622309), the Joint Fund for the Equipment Pre-research of Space Science and Technology (6141B06240205), the 111 Project (B13044), and the Innovation Foundation for Doctor Dissertation of Northwestern Polytechnical University (CX201830).
References

1. Chen Q, Hu X, Wen L, Yu Y, Cumming DRS (2016) Nanophotonic image sensors. Small 12:4922–4935
2. Jiang C, Song J (2015) An ultrahigh-resolution digital image sensor with pixel size of 50 nm by vertical nanorod arrays. Adv Mater 27(30):4454–4460
3. Catrysse PB, Wandell BA (2005) Roadmap for CMOS image sensors: Moore meets Planck and Sommerfeld. Proc SPIE - IS &T 5678:1–13
4. Chen Q, Das D, Chitnis D, Walls K, Drysdale TD, Collins S, Cumming DRS (2012) A CMOS image sensor integrated with plasmonic colour filters. Plasmonics 7:695–699
5. Nagasaki Y, Suzuki M, Takahara J (2017) All-dielectric dual-color pixel with subwavelength resolution. Nano Lett 17(12):7500–7506
6. Frey L, Parren P, Rabj J, Pellec P, Héralt D, Marty M, Michailos J (2011) Color filters including infrared cut-off integrated on CMOS image sensor. Opt Express 19(14):13073–13080
7. Dumanli AG, Savin T (2016) Recent advances in the biomimicry of structural colours. Chem Soc Rev 45:6698–6742
8. Roberts AS, Pors A, Albrekten O, Bozhevolnyi SI (2014) Subwavelength optical transmission through sub-wavelength hole arrays. Nature 391:667–670
9. Yokogawa S, Burgos SP, Atwater HA (2012) Plasmonic color filters for CMOS sensor. Nanoscale Res Lett 7:695
10. Yu P, Benteiro LV, Huang Y, Wu J, Fu L, Tan HHT, Jagadish C, Wiedenmann GP, Govorov AQ, Wang Z (2019) Broadband metamerism absorbers. Adv Opt Mater 7:1800995
11. Zhao J, Gao B, Li H, Yu Y, Yang X, Yu Y (2017) Biomimetic plasmonic color filters generated by the single-layer coaxial honeycomb nanostripe arrays. J Nanophotonics 11(3):036020
12. Li Y, Yue W, Chen ZX, Gao BQ, Fu XQ, Zhang CW, Li ZM (2018) Large-area structural color filtering capitalizing on nanoporous metal- dielectric-metal configuration. Nanoscale Res Lett 13:1217
13. Inoue D, Miura A, Nomura T, Fujiwara H, Sato K, Ikeda N, Tsuya D, Sugimoto Y, Kaido Y (2011) Polarization independent visible color filter comprising an aluminum film with surface-plasmon enhanced transmission through a subwavelength array of holes. Appl Phys Lett 98:093113
14. Yang C, Hong L, Shen W, Zhang Y, Liu X, Zhen H (2013) Design of reflective color filters with high angular tolerance by particle swarm optimization method. Opt Express 21(8):9315–9323
15. Ye M, Sun L, Hu X, Shi B, Zeng B, Wang L, Zhao J, Yang S, Tai R, Fecht HU, Jiang JZ, Zhang DX (2015) Angle-insensitive plasmonic color filters with randomly distributed silver nanodisks. Opt Lett 40(21):4979–4982
16. Si G, Zhao Y, Lv J, Lu M, Wang F, Liu H, Xiang N, Huang TJ, Danner AJ, Teng J, Liu YJ (2013) Reflective plasmonic color filters based on lithographically patterned silver nanorod arrays. Nanoscale 5:6243–6248
17. Zhao J, Yu X, Yang X, Xiang Q, Duan H, Yu Y (2017) Polarization independent subtractive color printing based on ultrathin hexagonal nanodisk-nanohole hybrid structure arrays. Opt Express 25(19):23157–23164
18. Wu QJ, Jia H, Xu XL, Sun LB, Wang LS, Yang SM, Tai RZ, Fecht HJ, Wang LQ, Zhang DX, Jiang JZ (2017) Plasmonic reflection color filters with metallic random nanostructures. Nanotechnol 28:085203
19. Mudachari R, Tanaka T (2017) Up scalable full colour plasmonic pixels with controllable hue, brightness and saturation. Sci Rep 7:1199
20. Zhao J, Yu X, Yang X, Tee CA, Yuan W, Yu Y (2019) Polarization-independent and high-efficiency broadband optical absorber in visible light based on nanostructured germanium arrays. Opt Lett 44:963–966
21. Koirala J, Shrestha VR, Park CS, Lee SS, Choi DY (2017) Polarization-controlled broad color palette based on an ultrathin one-dimensional resonant grating structure. Sci Rep 7:40073
22. Kaplan AF, Xu T, Guo L (2011) High efficiency resonance-based spectrum filters with tunable transmission bandwidth fabricated using nanoimprint lithography. Appl Phys Lett 99:143111
23. Park CH, Yoon YT, Shrestha VR, Park CS, Lee SS, Kim ES (2013) Electrically tunable color filter based on a polarization-tailed nano-photonic dichroic resonator featuring an asymmetric subwavelength grating. Opt Express 21(23):28783–28793
24. Shen C, Díaz-Rubio A, Li J, Cummer SA (2018) A surface impedance-based three-channel acoustic metasurface retroreflector. Appl Phys Lett 112:183503
25. Burgos SP, Yokogawa S, Atwater HA (2013) Color imaging via nearest neighbor hole coupling in plasmonic color filters integrated onto a complimentary metal-oxide semiconductor image sensor. ACS Nano 7(11):10038–10047
26. Yang B, Liu W, Li Z, Cheng H, Chen S, Tian J. Polarization-sensitive structural colors with hue-and-saturation tuning based on all-dielectric nanopixels. Adv Opt Mater. 2018;6:1701009.
27. Li J, Liu C, Wu T, Liu Y, Wang Y, Yu Z, Ye H, Yu L (2019) Efficient polarization beam splitter based on all-dielectric metasurface. Nano Res 14:34
28. Sun S, Zhou Z, Zhang C, Gao Y, Duan Z, Xiao S, Song Q (2017) All-dielectric full-color printing with TiO2 metasurfaces. ACS Nano 11(5):4445–4452
29. Horie Y, Han S, Lee JY, Kim J, Kim Y, Arbabi A, Shin C, Shi L, Arbabi E, Kamali SM, Lee HS, Hwang S, Faraon A (2017) Visible wavelength color filters using dielectric subwavelength gratings for backside-illuminated CMOS image sensor technologies. Nano Lett 17(5):3159–3164
30. Yang Z, Zhou Y, Chen Y, Wang Y, Dai P, Zhang Z, Duan H (2016) Reflective color filters and monochromatic color printing based on asymmetric Fabry-Perot cavities using nickel as a broadband absorber. Adv Opt Mater 4(8):1196–1202
31. Zeng B, Gao Y, Bartoli FJ (2013) Ultrathin nanostructured metals for highly transmissive plasmonic subtractive color filters. Sci Rep 3:2840
32. Kumar K, Duan H, Hegde RS, Koh SCW, Wei J, Yang JK (2012) Printing colour at the optical diffraction limit. Nat Nanotechnol 7(9):557–561
33. Kuznetsov AI, Miroshnichenko AE, Brongersma ML, Kivshar YS, Luk Brongersma SH, Rivas JG (2011) Universal scaling of the figure of merit of plasmonic sensors. ACS Nano 5:5151–5157
34. Rajeeva BB, Lin L, Zheng Y (2018) Design and applications of lattice plasmonic sensors. ACS Nano 5:5151–5157
35. Genet C, Ebbesen TW (2007) Light in tiny holes. Nature 445:39
36. Willets KA, Duyne RPV (2007) Localized surface plasmon resonance spectroscopy and sensing. Annu Rev Phys Chem 58:267–297
37. Barnes WL, Dereux A, Ebbesen TW (2003) Surface plasmon subwavelength optics. Nature 424:842–840
38. Offermans P, Schaafsma MC, Rodriguez SRK, Zhang Y, Crego-Calama M, Brongersma ML, Duan H, Yariv A, Mulvaney P, Prawer S (2013) Filling schemes at submicron scale: development of submicron sized plasmonic colour filters. Sci Rep 3:6742
39. Zhang DX, Jiang JZ, Zhang HY, Chen Y, Gao Y, Liu P, Xia H, Liu B, Wu Q, Wang Y, Li Z, Liu Y, et al. Nanoscale Research Letters 14:214
40. Ganesan K, Tomljenovic-Hanic S, Kandasamy S, Skafidas E, Neshev DN, Mulvaney P, Roberts A, Prawer S (2013) Filling schemes at submicron scale: development of submicron sized plasmonic colour filters. Sci Rep 3:6742
41. Kuznetsov AI, Miroshnichenko AE, Brongersma ML, Kivshar YS, Luk Brongersma SH, Rivas JG (2011) Universal scaling of the figure of merit of plasmonic sensors. ACS Nano 5:5151–5157
42. Genet C, Ebbesen TW (2007) Light in tiny holes. Nature 445:39–46

Publisher’s Note
Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.