To gain better understanding of the stabilizing interactions between metal ions and DNA quadruplexes, dispersion-corrected density functional theory (DFT-D) based calculations were performed on double-, triple- and four-layer guanine tetrads interacting with alkali metal cations. All computations were performed in aqueous solution that mimics artificial supramolecular conditions where guanine bases assemble into stacked quartets as well as biological environments in which telomeric quadruplexes are formed. To facilitate the computations on these significant larger systems, optimization of the DFT description was performed first by evaluating the performance of partial reduced basis sets. Analysis of the stabilizing interactions between alkali cations and the DNA bases in double and triple-layer guanine quadruplex DNA reproduced the experimental affinity trend of the order Li$^+$ < Rb$^+$ < Na$^+$ < K$^+$. The desolvation and the size of alkali metal cations are thought to be responsible for the order of affinity. Nevertheless, for the alkali metal cation species individually, the magnitude of the bond energy stays equal for binding as first, second or third cation in double, triple and four-layer guanine quadruplexes, respectively. This is the result of an interplay between a decreasingly stabilizing interaction energy and increasingly stabilizing solvation effects, along the consecutive binding events. This diminished interaction energy is the result of destabilizing electrostatic repulsion between the hosted alkali metal cations. This work emphasizes the stabilizing effect of aqueous solvent on large highly charged biomolecules.

1. Introduction

DNA sequences that are purine rich and contain runs of guanine (G) bases can form non-duplex four-stranded structures that are called guanine quadruplexes (GQs) (Fig. 1). $^1$–$^5$ GQs consist of stacked guanine quartets with alkali cations between the layers and occur in crucial regulatory regions of the human genome, such as telomeres and promotor regions. The guanine quartet (G₄) layers consists of four guanine bases assembled through Hoogsteen-type hydrogen bonding (Fig. 1a). The stabilization of GQ structures in telomeric regions has been shown to interfere with the activity of the enzyme telomerase, offering a tool to control the mechanism of elongation of telomeric ends that is related to cell senescence and therefore proliferation. On the other hand, the formation of GQ structures in telomeric and promotor regions of numerous genes can down-regulate transcription and suppress oncogene expression. Therefore, GQs have been considered as an attractive target for anticancer drug design.$^6$–$^9$ This potential therapeutic application has led to a new field devoted to the design of (metallo)organic compounds that selectively interact, promote and stabilize the GQ folding.$^{10}$–$^{12}$

However, in order to rationally design these so-called GQ-ligands, it is crucial to fully understand the physical principles behind the formation of GQs and the role of the alkali cations in the stabilization of these structures.

Previous work by Fonseca Guerra et al.$^{13}$, $^{14}$ has shown that the hydrogen bonding in G₄ relies on cooperativity. These synergistic effects originate from charge separation occurring upon hydrogen bonding, due to donor–acceptor interactions of the σ-electron system.$^{15}$ It contradicts previous assumptions that the enhancement of the hydrogen bonds was solely caused by resonance of the π-electrons. In addition, Fonseca Guerra and co-workers demonstrated that although the presence of alkali metal cations between the G₄ layers weakens the hydrogen bonds, the synergy remains in telomeric structures.$^{16}$–$^{19}$

The alkali metal cation that is located between two quartets was long believed to generate cation–dipole interactions with the eight interacting guanines and thereupon reducing the repulsion of the central oxygen atoms.$^{20}$–$^{22}$ This would enhance the hydrogen bonding strength and stabilize the GQ formation.
This idea was rationalized by the presence of significant negative charge located at the central cavity of the G₄. In 2016, work by Zaccaria et al. revealed that the central cation is not needed to reduce repulsion between the oxygen atoms, but rather provides additional stability of the quadruplex by electrostatic and donor–acceptor interactions between the oxygens and the cation. Later work showed that inclusion of the metal cation into the quadruplex significantly lowers the Gibbs free energy of formation of the cationic species compared to the formation of the empty scaffold. This led to the insight that the actual need for the cation is to overcome the entropic penalty. Gu and Leszczynski.29

Guanine quadruplexes can host different alkali metal cations, and many experimental studies have revealed an overall affinity sequence of K⁺ > Na⁺, Rb⁺ ≫ Li⁺, Cs⁺ in water.25-27 Research has been devoted to finding an explanation of this affinity trend.28-30 Williamson et al. suggested in 1989 that the overserved ion specificity was related to the snug fit of the alkali cations into the cavity of the quadruplex, thus the size of the cations. Later, Hud and co-workers claimed that the Gibbs free energy of solvation of the alkali metal cations was the determining factor, since cations have to be desolvated completely before they can access the inner channel of GQs. This idea was supported by the theoretical work of Gu and Leszczynski.29

Zaccaria et al. showed that both the ionic radius, as well as the Gibbs free energy of solvation, are of equal importance in determining the order of cation affinity in GQ structures. These results were obtained from extensive computational analysis of the electronic properties of double-layer GQ structures interacting with the different alkali metal cations. These computations were based on dispersion-corrected density functional theory (DFT-D). The study of Zaccaria and co-workers involved double-layer quadruplexes (Fig. 1c). However, natural occurring GQ structures can be encountered as multiple stacks of G₄, Therefore, we have investigated if our previous results and conclusions can be extended to larger systems which include interactions between adjacent cations.

In this work we investigate the electronic interactions of double, triple and four-layer GQ structures (with and without sugar-phosphate backbone) with the different alkali metal cations in aqueous solution by computational analysis using DFT-D based calculations. To facilitate the computations on these significant larger systems, optimization of the DFT description was performed at first by evaluating the performance of partial reduced basis sets. In case of the triple-layer systems, the computational geometries involve quadruplex structures occupied by one potassium cation, to which a second alkali metal cation is introduced. The four-layer GQ comprises a structure hosting three potassium cations. The calculations simulate the situation of quadruplexes under supramolecular and biological conditions in aqueous solution.

2. Computational methods

2.1 General procedure

All the calculations were performed using the Amsterdam Density Functional (ADF) program (ADF2017.103). Geometry optimizations and stationary point energy calculations were based on dispersion-corrected relativistic density functional theory at the ZORA-BLYP-D3(BJ) level of theory. A TZP basis set was used for the description of the alkali metal cations and the guanine bases, whereas DZ was used as basis set for the sugar phosphate backbone. Our benchmark study revealed that the usage of these smaller basis sets is justified (see Section 3.1 and ES1 Fig. S1 and S2). The use of the BLYP exchange functional in combination with D3 London dispersion correction with Becke–Johnson damping was supported by previous computational work on guanine quadruplexes that demonstrated that this description results in reliable geometries and trends in line with experiment. In addition, Sedlak et al. showed that BLYP-D3(BJ) outperforms semi-empirical functionals, such as M06-2X, in terms of accuracy:cost ratio for the description of non-covalent interactions. Because of this combination of high accuracy and low computational costs, BLYP-D3(BJ) was used in this work.

No geometrical constraints were imposed on the optimized geometries. This also applied to the guanine quadruplexes without backbone (129 atoms (2-layer), 194 atoms (3-layer) and 259 atoms (4-layer)) and the guanine quadruplex with
backbone (265 atoms (2-layer) and 402 atoms (3-layer)). The guanine quadruplexes in this work are parallel stranded right-handed GQ structures with anti-glycosidic torsion angles at all guanines. Biological GQ structures are also constituted by loop regions with dangling nucleobases. However, dangling nucleobases do not have significant influence on binding properties of the shielded interior of the quadruplex and are therefore omitted in the model systems.

Optimized geometries of the double-layer GQ structures at the ZORA-BLYP-D3 (Bj)/TZ2P level of theory of Zaccaria et al. were used as starting point for the calculations of the triple-layer systems.\(^{23,24}\) Solvent effects in water have been taken into account with the conductor-like screening model (COSMO), as implemented in the ADF program.\(^{36,44–46}\) Radii of the cations have been determined by reproduction of the guanine monomer.\(^{40}\) To compare the results led to more reliable geometry optimizations when the Solvent-Excluding-Surface (SES) method was implemented in COSMO (Delley cavity construction instead of the shielded interior of the quadruplex and are therefore omitted in the model systems.

The preparation energy, \(\Delta E_{\text{prep}}\), of the triple-layer guanine quadruplex structures is defined by eqn (1a) and (1b), for the GQ without and with sugar-phosphate backbone, respectively (see also Fig. 2).

\[
\Delta E_{\text{prep}} = E(G) - E(G^\ast) - E(M^\ast) \\
\Delta E_{\text{prep}} = E(GQ) - 4E(G) - E(K^\ast) - E(M^\ast)
\]

\(E(G)\) is the energy of the separately optimized geometry of the guanine monomer. \(E(GG)\) refers to the energy of the optimized guanosine trimer, wherein the sugar-phosphate backbone is neutralized by \(H^+\) as counterion (Fig. 1b). Zaccaria et al. found that neutralization with \(H^+\) gives the same affinity trend as with neutralization with \(Na^+\).\(^{21}\)\(E(M^\ast)\) denotes the energy of the central alkali metal cation (i.e. \(Li^+, Na^+, K^+\) or \(Rb^+\)). \(E(G_4–K^+–G_4–[\ ]–G_4)\) and \(E(GQ–K^+–M^\ast)\) are the energies of the triple-layer GQs, without and with backbone, in the optimal geometry.

2.2 Bond energy analysis

The bond energy between the second alkali metal cation and the triple-layer GQ structures, with one cavity occupied by \(K^+\) and one empty cavity, is formulated by eqn (2a) and (2b) for the guanine quadruplexes without \((G_4)\) and with backbone \((GQ)\), respectively (see also Fig. 3).

\[
\Delta E_{\text{bond}} = E(G_4–K^+–G_4–M^\ast–G_4)_{\text{aq}} - E(G_4–K^+–G_4–[]–G_4)_{\text{aq}} - E(M^\ast)_{\text{aq}} \\
\Delta E_{\text{bond}} = E(GQ–K^+–M^\ast)_{\text{aq}} - E(GQ–K^+–[\ ])_{\text{aq}} - E(M^\ast)_{\text{aq}}
\]

In these equations \(E(G_4–K^+–G_4–M^\ast–G_4)_{\text{aq}}\) and \(E(GQ–K^+–M^\ast)_{\text{aq}}\) are the energies of the in water optimized triple-layer GQs, without and with backbone, occupied by one potassium cation and another alkali metal cation (\(M^\ast = Li^+, Na^+, K^+\) or \(Rb^+\)). \(E(G_4–K^+–G_4–[\ ]–G_4)_{\text{aq}}\) and \(E(GQ–K^+–[\ ])_{\text{aq}}\) denote the energies of the optimized triple-layer GQs in water, without and with backbone, occupied by one potassium cation.

In order to understand the different components that determine the trend in bond energy (i.e. cation affinity) the bond energy was partitioned as formulated by eqn (3) (see also Fig. 3).

\[
\Delta E_{\text{bond}} = \Delta E_{\text{desolv}} + \Delta E_{\text{prep}} + \Delta E_{\text{int}} + \Delta E_{\text{solv}}
\]

The desolvation (\(\Delta E_{\text{desolv}}\)) and solvation energy (\(\Delta E_{\text{solv}}\)) can be computed by taking the energy difference between the solvated structure and the gas phase single-point calculation of the solvated optimized geometry (see eqn (4) and (5)). The subscript ‘aq’ indicates calculations performed with COSMO, whereas the subscript ‘gas’ refers to gas phase calculations.

\[
\Delta E_{\text{desolv}} = E(G_4–K^+–G_4–[\ ]–G_4)_{\text{gas}} - E(G_4–K^+–G_4–[]–G_4)_{\text{gas}} + E(M^\ast)_{\text{gas}} - E(M^\ast)_{\text{aq}}
\]

\[
\Delta E_{\text{desolv}} = E(GQ–K^+–[\ ])_{\text{gas}} - E(GQ–K^+–[\ ])_{\text{aq}} + E(M^\ast)_{\text{gas}} - E(M^\ast)_{\text{aq}}
\]

\[
\Delta E_{\text{solv}} = E(G_4–K^+–G_4–M^\ast–G_4)_{\text{aq}} - E(G_4–K^+–G_4–M^\ast–G_4)_{\text{gas}}
\]

\[
\Delta E_{\text{solv}} = E(GQ–K^+–M^\ast)_{\text{aq}} - E(GQ–K^+–M^\ast)_{\text{gas}}
\]

The preparation energy (\(\Delta E_{\text{prep}}\)) is the energy required to deform the solvated state geometry of the triple-layer GQ structure, with one cavity occupied by \(K^+\) and one empty cavity, \(G_4–K^+–G_4–[\ ]–G_4\) or \(GQ–K^+–[\ ]\) to the geometry it acquires when it interacts with the second alkali metal cation, but calculated in the gas phase (see Fig. 3). The values of the preparation have been checked to be almost phase independent.

Fig. 2 Definition of the formation energy (\(\Delta E_{\text{form}}\)) of the triple-layer guanine quadruplex structures without \((G_4, \text{top scheme})\) and with sugar-phosphate backbone \((GQ, \text{bottom scheme})\).
This approximation can be made since the interaction of the alkali metal cation occurs on the interior of the quadruplex cavity, which is shielded from the solvent by the guanine bases and sugar-phosphate backbone. In addition, it assumed that the negatively charged central cavity prevents entering of water molecules.

The interaction energy is further decomposed based on the Kohn–Sham molecular orbital theory using a quantitative energy decomposition analysis (EDA), which divides the total interaction energy ($\Delta E_{\text{int}}$) into electrostatic interaction ($\Delta V_{\text{elstat}}$), Pauli repulsion ($\Delta E_{\text{Pauli}}$), orbital interaction ($\Delta E_{\text{oi}}$) and dispersion correction ($\Delta E_{\text{disp}}$) components (eqn (7)).

$$\Delta E_{\text{int}} = \Delta V_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{oi}} + \Delta E_{\text{disp}} \quad (7)$$

The Voronoi deformation density (VDD) method allows analysis of the electronic redistributions within polyatomic fragments when a chemical bond is formed between these molecular fragments. \cite{48, 49} The VDD atomic charges ($DQ_{M^+}$) have been calculated for the second alkali metal cations in the central cavity of the triple-layer quadruplex (GQ–K+–M+). $DQ_{M^+}$ is computed as the (numerical) integral of the deformation density ($\Delta \rho(r)$) in the volume of the Voronoi cell of cation $M^+$ associated with the formation of the triple-layer quadruplex from the quadruplex hosting one K+ and the second metal cation (see eqn (8)). The Voronoi cell of $M^+$ is the space defined by the bond midplanes on and perpendicular to all bond axes between nucleus $M^+$ and its neighbouring nuclei.

$$\Delta Q_{M^+} = -\int_{\text{Cell}} \left( \rho_{\text{GQ–K+–M+}}(r) - \rho_{\text{GQ–K+–}}(r) - \rho_{M^+}(r) \right) dr \quad (8)$$

$\Delta Q_{M^+}$ is an indication for the number of electrons that flows into ($\Delta Q_{M^+} < 0$) or out of ($\Delta Q_{M^+} > 0$) the Voronoi cell of $M^+$ as result of the interaction of $M^+$ with GQ–K+[ ]. Cell is the Voronoi Cell of $M^+$ in GQ–K+[ ].
3. Results and discussion

3.1 Basis set dependency

Since DNA-based systems, especially including metals, encounter many non-covalent interactions, the use of triple-zeta (or larger) basis sets is often recommended when studying these systems. However, in these large (supramolecular) biomolecules, large basis sets can make the calculations too expensive. Therefore, smaller basis sets, which would combine high computational speed and accuracy, are preferred. The performance of the basis sets SZ, DZ, DZP, TZP and TZ2P and combinations of these for different regions of the quadruplexes were screened by stationary point calculations on the optimized double-layer GQ geometries at the ZORA-BLYP-D3(BJ)/TZ2P level of theory of Zaccaria et al. (see ESI† Fig. S1 and S2). By comparing the obtained energies with the energy of the TZ2P calculation, the most promising (i.e. lowest computational cost, with sufficient accuracy (≤1 kcal mol\(^{-1}\) deviation)) basis set combination was selected. The results show that usage of different basis sets within the ring system of the guanine base, leads to significant errors in calculated energies (ESI† Fig. S1). This result is in accordance to the results found by Fonseca Guerra et al. in 1999. In this work it was found that hydrogen bonding is not a local effect, but affects the distributions of the σ and π electrons throughout the whole DNA base. The results of this work show that the basis set combination using TZP for the guanine bases and K\(^+\), in combination with a DZ basis set for the sugar–phosphate backbone gives a \(\Delta E_{\text{form}}\) within the 1 kcal mol\(^{-1}\) deviation range and seems to be sufficient to describe quadruplexes (Table 1 and ESI† Fig. S2). To validate this, the performance of the TZP/DZ basis set combination was examined in a geometry optimization of GQ–K\(^+\). The results of these calculations are depicted in Table 1. Both the energy and the geometrical parameters are in good accordance with the by TZ2P obtained results. Nevertheless, the average calculation time per cycle is almost three times shorter. Therefore, using the TZP/DZ basis set combination is likely to significantly reduce the calculation time on DNA based systems, compared to the conventional TZ2P basis set, while maintaining the required computational accuracy. The TZP/DZ basis set combination was used in the calculations of the quadruplexes throughout this work.

3.2 Structure and energy of formation

Previous results by Zaccaria et al. showed that the double-layer quadruplexes preferably facilitate the hosting of K\(^+\) and that the order of affinity can be explained by the size of the alkali metal cation and the desolvation energy. Because of improvement of the implicit solvation model in the newer ADF version, the energies and structures of the double-layer GQs were recalculated in this work. To study the interaction between a second alkali metal cations in the by one K\(^+\) occupied triple-layer guanine quadruplex, two additional model systems have been studied computationally: G\(_4\)-K\(^+\)-G\(_4\)-M\(^+\)-G\(_4\) and GQ-K\(^+\)-M\(^+\) (see Fig. 1 and Fig. 4). The latter system also includes the sugar-phosphate backbone which is neutralized by H\(^+\) as counterion. The energy of formation (\(\Delta E_{\text{form}}\), eqn (1)) and geometrical parameters of the double and triple-layer GQs are listed in Table 2. The most stable complexes (i.e. most negative \(\Delta E_{\text{form}}\)) are the quadruplexes facilitating only K\(^+\). For example, the GQ-K\(^+\)-M\(^+\) system with M\(^+\) = K\(^+\) is most stable, followed by Na\(^+\) (+2.2 kcal mol\(^{-1}\)), Rb\(^+\) (+4 kcal mol\(^{-1}\)) and Li\(^+\) (+13 kcal mol\(^{-1}\)). These results are consistent with experimental findings and the computational results found by Zaccaria et al. for the double-layer quadruplexes. Thus, from Table 2 it can be concluded that also for the triple-layer quadruplexes, the trend in affinity follows the order K\(^+\) > Na\(^+\) > Rb\(^+\) > Li\(^+\). Although, improvement of the computational order of affinity is obtained by the more realistic system with backbone, the same trend was found for the simplified quadruplexes without backbone (G\(_4\)), but with smaller energy differences for the different cations. This justifies the usage of quadruplex systems without backbone for the study of cation-quadruplex interactions. This, together with the reduced computational costs, by using a smaller basis set (see Section 3.1 and ESI† Fig. S2 and Table 1), opens up possibilities to study larger multi-layer systems. It should be noted that for the G\(_4\)-K\(^+\)-G\(_4\)-M\(^+\)-G\(_4\) system, the order of Na\(^+\) and K\(^+\) is reversed by a small energy difference of 0.5 kcal mol\(^{-1}\). Since the experimental energy difference for Na\(^+\) and K\(^+\) is only a few kcal mol\(^{-1}\), small deviations in geometry due to the lack of the rigidity of the backbone, can already reverse the trend. The computed values of the distance between the metal cation (M\(^+\)) and the surrounding oxygen atoms (d[O-M\(^+\)]) are close to the experimental values and the values computed for the double-layered systems. Also, the average distance (\(R\)) between the upper and lower oxygen atoms and the hydrogen bond distances do not change significantly upon introduction of a third guanine layer.

3.3 Partitioning of the bond energy

In order to explain the computed trends in cation affinity for the triple-layer systems and identify differences compared to the double-layers GQs, the bond energy (\(\Delta E_{\text{bond}}\)) was partitioned into different terms (see eqn (3)). Solvation effects that

\[
\begin{align*}
\Delta E_{\text{form}} &= \Delta E_{\text{geometrical opt.}} + \Delta E_{\text{electronic contrib.}} + \Delta E_{\text{solvation}} \\
\Delta E_{\text{geometrical opt.}} &= \Delta E_{\text{formation}}^{0} + \Delta E_{\text{desolvation}} \\
\Delta E_{\text{electronic contrib.}} &= \Delta E_{\text{electronic}} \\
\Delta E_{\text{solvation}} &= \Delta E_{\text{solvation}}^{0} + \Delta E_{\text{interaction}}
\end{align*}
\]

\(\Delta E_{\text{formation}}^{0}\) corresponds to the energy of formation of the free cations, \(\Delta E_{\text{desolvation}}\) to the desolvation energy. The latter includes both, the desolvation of the solvent around the free cations and the desolvation of the cation bound to the quadruplex. The interaction term \(\Delta E_{\text{interaction}}\) is the difference in the electronic properties of the cation bound and free within the quadruplex.
may contribute to the observed trend can be studied computationally by the terms $\Delta E_{\text{desolv}}$ and $\Delta E_{\text{solv}}$ (eqn (4) and (5)). Furthermore, the effect of the size of the second alkali cation can be determined by the preparation energy term ($\Delta E_{\text{prep}}$, eqn (3)) and stabilizing interactions between the cation and the quadruplex scaffold by the interaction energy ($\Delta E_{\text{int}}$, eqn (6) and (7)).

Fig. 4 Structures of $G_4-K^+-[G_4]-G_4-K^+-[G_4]-G_4-M^+-[G_4]-G_4-K^+-[M^+]$ and $GQ-K^+-[M^+]$ where $M^+$ is an alkali metal cation. The $G_4$ structures were optimized at the ZORA-BLYP-D3(BJ)/TZP level of theory and the $GQ$ structures at the ZORA-BLYP-D3(BJ)/TZP/DZ level of theory with COSMO to simulate water. The difference in the average $z$-coordinate of the upper and lower oxygen atoms ($R$, in Å), as measure for the interplanar distance of adjacent guanine quartets, is displayed.
case of Li+, since Li+ lies in the center of one of the quartets.

\[ \text{GQ–K+–GQ–K+–GQ} \]

The preparation energy does not vary much for the different interaction energies, compensated by a large desolvation energy. The preparation energy is likely to be larger for cations with more favourable coordination to the negatively charged oxygen atoms. The second alkali metal cation is expected to be smaller when the alkali cation fits well into the central cavity of the scaffold. The cavity should shrink. This leads to a higher preparation energy than in the case of the larger cations (K+ and Na+), which give rise to less distortion of the empty cavity. For the guanine bases to interact with the smaller cations (Li+ and Na+), the cavity should shrink. This leads to a higher preparation energy than in the case of the larger cations (K+ and Rb+), which give rise to less distortion of the empty cavity.

In all cases, the bond energy is mainly the sum of a strong interaction energy, compensated by a large desolvation energy. The preparation energy does not vary much for the different cations and decreases upon increasing the size of the cation. This trend can be explained by looking at the cation–oxygen distance (\(d[O–M^+]\)) and interplanar distance (\(R\)) (Table 2) that determine the size of the cavity hosting the second cation. The values of the geometrical parameters \(d[O–M^+]\) and \(R\) come closer to the values of the empty cavity going from Li+ to Rb+.

Table 3 and graphically presented for the quadruplexes with backbone (GQ) in Fig. 5. In Fig. 5 the solid lines represent the results found in this study for the three-layer quadruplex systems, whereas the dashed lines represent the results found for the double-layered quadruplexes.

In all cases, the bond energy is mainly the sum of a strong interaction energy, compensated by a large desolvation energy. The preparation energy does not vary much for the different cations and decreases upon increasing the size of the cation. This trend can be explained by looking at the cation–oxygen distance (\(d[O–M^+]\)) and interplanar distance (\(R\)) (Table 2) that determine the size of the cavity hosting the second cation. The values of the geometrical parameters \(d[O–M^+]\) and \(R\) come closer to the values of the empty cavity going from Li+ to Rb+.

For the guanine bases to interact with the smaller cations (Li+ and Na+), the cavity should shrunk. This leads to a higher preparation energy than in the case of the larger cations (K+ and Rb+), which give rise to less distortion of the empty cavity.

To investigate the contributions of geometrical effects and solvation effects, the sum of the interaction and preparation energy (\(\Delta E_{\text{int}} + \Delta E_{\text{prep}}\)) is displayed in Table 3, as well as the sum of the solvation and desolvation energy (\(\Delta E_{\text{solv}} + \Delta E_{\text{desolv}}\)).
The former combination follows almost the exact same trend as the interaction energy alone. Table 3 shows that both summations are of counteracting and almost of equal importance to the order of cation affinity, resulting in small differences in bonding energy for the different alkali cations. The results of the double-layer GQs in Table 3 are consistent with the results found by Zaccaria et al.23 With this we would like to emphasize that the improved COSMO version results in different absolute interactions than in the case of $1^+$ species. It must be examined in more polarization of the solvent and thereupon to stronger destabilizing effects of alkali cations in the double and triple-layer guanine quadruplexes (Fig. 5). Remarkably, the magnitude of the bond energy decreases only little, going from the first to the second binding event. That the overall bond energy stays approximately the same for the first and second binding event of alkali metal cations of the same kind is the result of two counteracting effects: (1) the interaction energy ($\Delta E_{\text{int}}$) is less stabilizing for the interaction of the second metal cation ($M^+$) with the cavity of the GQ than for the first metal cation; (2) the sum of solvation effects ($\Delta E_{\text{desolv}} + \Delta E_{\text{solv}}$) is less destabilizing for the second binding event. The latter is because the stabilizing $\Delta E_{\text{solv}}$ term increases more than the destabilizing $\Delta E_{\text{desolv}}$ term, going from the first to the second binding cation. In other words, the gain in solvation energy ($\Delta E_{\text{solv}}$) for going from a GQ of charge $1^+$ (GQ–$M^+$) to $2^+$ (GQ–$K^+–M^+$) is larger, than the increase of desolvation energy ($\Delta E_{\text{desolv}}$) for going from an neutral GQ (GQ–[ ]) to a positively charged species (GQ–$K^+–[ ]$). This can be explained by the fact that in the $2^+$ species the charge is more localized, resulting in more polarization of the solvent and thereupon to stronger interactions than in the case of $1^+$ species. It must be examined if this effect will be even stronger in highly charged systems ($3^+$, $4^+$, etc.).

### 3.4 Energy decomposition analysis

The previous section showed that the desolvation energy and the size of the cation contribute equally to the bond energy of the alkali metal cations in the double and triple-layer guanine quadruplexes. The bond energy stays equal for binding a second metal cation, although a less stabilizing interaction energy was observed going from the double to the triple-layer quadruplexes. In order to get a better understanding of the reason why the interaction energy is less stabilizing for the second binding event, $\Delta E_{\text{int}}$ is decomposed into physically meaningful terms (see eqn (7), Table 4 and Fig. 6). The interaction energy terms follow the same trend for both the guanine quadruplexes with and without sugar-phosphate backbone. The results of the systems with sugar-phosphate backbone (GQ) are graphically presented in Fig. 6.

From Fig. 6, it can be seen that the significant drop in interaction energy going from Na$^+$ to K$^+$ is due to the increase in Pauli repulsion that increases by almost 20 kcal mol$^{-1}$. We want to emphasize this counterintuitive observation that K$^+$ results in less deformation of the GQ, although it is accompanied by a higher Pauli repulsion than Na$^+$. From the energy decomposition analysis (EDA) follows that the bonding interaction of the second alkali cation to GQ–K$^+–[ ]$ is a combination of mainly electrostatic interaction, followed by orbital interaction and dispersion. These trends are also in line with the results found by Zaccaria et al.23 In fact, the trendlines of the energy terms $\Delta E_{\text{Pauli}}, \Delta E_{\text{elstat}}$ and $\Delta E_{\text{disp}}$ do exactly overlap for the double- and triple-layered GQs. It turns out that only the decrease in electrostatic interaction ($\Delta V_{\text{elstat}}$) is responsible for the observed decrease in interaction energy in the second binding event.

The observed decrease in electrostatic interaction ($\Delta V_{\text{elstat}}$) for binding of the second alkali cation can be the result of the repulsion between the two present cations in the quadruplex or the diminished electron density available on middle guanine quartet to bind the second cation. The presence of the first potassium ion in GQ–K$^+–[ ]$ leads to extraction of electron density from the oxygen atoms. Thereupon, the oxygen atoms in the middle guanine quartet layer of GQ–K$^+–M^+$ are likely to become less electronegative, potentially leading to a smaller bond formation energy for GQ–K$^+–M^+$. The observed decrease in electrostatic interaction ($\Delta V_{\text{elstat}}$) is responsible for the observed decrease in interaction energy in the second binding event.

| System | $M^+$ | $\Delta E_{\text{int}}$ | $\Delta V_{\text{elstat}}$ | $\Delta E_{\text{Pauli}}$ | $\Delta E_{\text{elstat}}$ | $\Delta E_{\text{disp}}$ |
|--------|------|------------------|-----------------|-----------------|-----------------|-----------------|
| G$_4$–M$^+$–G$_4$ | Li$^+$ | −159.4 | −108.2 | 11.6 | −54.8 | −8.0 |
| | Na$^+$ | −150.0 | −105.3 | 11.2 | −43.0 | −12.9 |
| | K$^+$ | −127.2 | −102.1 | 30.9 | −40.8 | −15.2 |
| | Rb$^+$ | −114.3 | −96.0 | 36.6 | −38.4 | −16.5 |
| | Li$^+$ | −163.6 | −111.0 | 12.9 | −58.0 | −7.4 |
| | Na$^+$ | −154.2 | −106.8 | 10.3 | −44.6 | −13.1 |
| | K$^+$ | −133.1 | −103.6 | 28.4 | −42.3 | −15.6 |
| | Rb$^+$ | −121.5 | −99.2 | 34.8 | −40.1 | −16.9 |
| G$_4$–K$^+–M^+$–G$_4$ | Li$^+$ | −119.1 | −66.0 | 11.7 | −56.1 | −8.7 |
| | Na$^+$ | −105.2 | −58.6 | 11.8 | −45.3 | −14.9 |
| | K$^+$ | −81.3 | −51.3 | 30.9 | −42.7 | −18.2 |
| | Rb$^+$ | −68.2 | −46.7 | 37.1 | −40.3 | −18.2 |

$^{a}$ All energies were computed with the DFT-D method at the ZORA-BLYP-D3(BJ)/TZP (G$_4$) or at the ZORA-BLYP-D3(BJ)/TZP/DZ (GQ) level of theory.
due to less stabilizing electrostatic interaction with the second alkali cation $M^+$. In order to identify the effect of electron depletion of the middle guanine stack upon binding of the first alkali cation, it was examined whether there is diminished charge-transfer from the guanine bases to the second metal cation. Therefore, the VDD change in atomic charge to the second metal cation ($\Delta Q_{M^+}$) was calculated for the triple-layer GQs and compared to the values found for the two-layer GQs (eqn (8) and Table 5). As presented in Table 5, the charge-transfer interaction between the GQ and the second cation is equal to the values found for binding of the first alkali cation in two-layer GQ. This indicates that there is sufficient electron density left on the middle guanine quartet to donate the same number of electrons to the second cation. This observation is supported by the overlapping of $\Delta E_{\text{elstat}}$ (green lines in Fig. 6) for the binding of the first and second cation in the double-layer and triple-layer GQ systems, respectively.

To investigate the contribution of repulsive interactions as cause of the diminished electrostatic interaction, an EDA of the interaction energy between the two alkali cations in GQ–$K^+–M^+$ was performed at the inter-atomic distance within the GQ (see Table 6). The results demonstrate that a large destabilizing interaction is present between the alkali cations in the quadruplex with interaction energies of ca. +80 kcal mol$^{-1}$. Table 6 shows that this destabilizing interaction is almost exclusively due to repulsive electrostatic interactions between the two cations. The electrostatic interaction is less stabilizing by approximately $40$ kcal mol$^{-1}$ ($\Delta V_{\text{elstat}}$) for all the different cations in GQ–$K^–M^+$ compared to the two-layered quadruplexes (see difference in $\Delta V_{\text{elstat}}$ in Fig. 6 for the triple-layer (solid line) and double-layer GQ (dashed line)). Therefore, it is expected that the large repulsive interaction energy between the two alkali cations contributes significantly to the observed decrease in bond energy of the second alkali metal cation but is reduced by electronic shielding of the guanine bases.

Note that the trend in electrostatic repulsion among the different alkali metal cations is related to the distance between $K^+$ and the second alkali metal cation in the geometry of GQ–$K^–M^+$. It can be concluded that the strong repulsive interaction between the two alkali metal cations, as found by the results in Table 6, accounts for the decrease in interaction energy of the second binding event in guanine quadruplex systems, rather than electron depletion of the middle guanine layer. This would suggest that in even larger multi-layer guanine quadruplexes, where each cation is adjacent to two other cations, the interaction energy for hosting alkali cations would decrease even further. These results question the role of alkali metal cations in the stabilization of multi-layer guanine quadruplex DNA and whether each cavity hosts an alkali metal cation or that rather an alternating pattern of empty and occupied is preferred. The decreasing importance of the alkali metal cations for the stability of multi-layer quadruplexes is in line with the results find by Kotlyar et al. In this work they report G$_4$ DNA wires in the absence of alkali cations that show equal stability as the cation containing G$_4$ structures reported in literature. The high stability is probably the result of the much greater length of these structures.

### 3.5 Four-layer guanine quadruplexes

In order to see if the interaction energy for binding a third $K^+$ ion would decrease even further, a four-layer GQ without sugar-phosphate backbone hosting three $K^+$ ions was examined ($G_3–K^–G_3–K^–G_3–G_3$). The usage of quadruplexes without sugar–phosphate backbone was justified by the previous results of this work. The bond energy ($\Delta E_{\text{bond}}$) of the third $K^+$ ion was partitioned into different terms in the same way as was done for the triple-layer and double-layer systems (Fig. 7). It was found

| Table 5 | VDD change in atomic charge ($\Delta Q_{M^+}$, in electrons) to the alkali metal cation in the triple and double layer quadruplexes$^a$ |
|---------|---------------------------------------------------------------------------------------------------|
| $M^+$   | $\Delta Q_{M^+}$ (GQ–$K^–M^+$) | $\Delta Q_{M^+}$ (GQ–$M^+$)$^b$ |
| Li$^+$  | −0.146 | −0.142 |
| Na$^+$  | −0.085 | −0.079 |
| K$^+$   | −0.059 | −0.058 |
| Rb$^+$  | −0.054 | −0.054 |

$^a$ VDD charges were computed with the DFT-D method at the ZORA-BLYP-D3(BJ)/TZP/DZ level of theory.

### Table 6 | Energy decomposition analysis (in kcal mol$^{-1}$) of the interaction between the two alkali cations in GQ–$K^–M^+$

| $M^+$ | $\Delta E_{\text{elstat}}$ | $\Delta V_{\text{elstat}}$ | $\Delta E_{\text{Pauli}}$ | $\Delta E_{\text{vdisp}}$ | $\Delta V_{\text{elstat}}$ |
|-------|------------------|------------------|------------------|------------------|------------------|
| Li$^+$ | 61.8 68.5 0.0 | −0.3 | −6.4 | 34.2 | 48.5 |
| Na$^+$ | 88.1 90.2 0.0 | −0.9 | −1.2 | 42.6 | 36.8 |
| K$^+$ | 86.2 88.7 0.1 | −1.5 | −1.2 | 44.2 | 37.5 |
| Rb$^+$ | 83.4 86.1 0.2 | −1.7 | −1.1 | 39.5 | 38.5 |

$^a$ All energies were computed with the DFT-D method at the ZORA-BLYP-D3(BJ)/TZP(DZ) level of theory. $^b$ Difference in the electrostatic interaction component of the bond energy of GQ–$K^–M^+$ vs. the two-layer GQ–$M^+$ of Zaccaria et al. (see Fig. 6). $^c$ Distance (in Å) between $K^+$ and the second alkali metal cation in GQ–$K^–M^+$. 

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**Fig. 6** Energy decomposition of the interaction energy (in kcal mol$^{-1}$) between the alkali metal cations (M$^+$) and GQ–[ ] (dashed lines) and GQ–K$^+–[ ]$ (solid lines).
again that the bond energy stays approximately equal for binding of the third cation.

In Fig. 7 the preparation energy stays the same, but the interaction energy decreases for each binding event. In addition, the contribution of solvation effects becomes more significant following this trend. The stabilizing solvation energy increases faster than the destabilizing desolvation energy with each binding event, resulting in an equalized bond energy.

The interaction energy is further decomposed into physically meaningful terms for consecutive binding events in G4–K+–G4, G4–K+–G4–K+–G4 and G4–K+–G4–K+–G4–K+–G4 (see eqn (7) and Fig. 8). Fig. 8 shows that the energy terms ΔE_{Pauli}, ΔE_{oi} and ΔE_{disp} stay the same for the subsequent binding events of K+ in double- and triple- and four-layer quadruplexes. It is only the decrease in electrostatic interaction (ΔV_{elstat}) that is responsible for the observed decrease in interaction energy in sequel binding events. These results show that electrostatic repulsion operates not only locally, but operates also over long range distances.

4. Conclusions

Alkali metal cations are found to stabilize the assembly of guanine quadruplexes in nature. In this work, the alkali metal cation affinity of double-, triple- and four-layer guanine quadruplexes was studied using dispersion-corrected density functional theory (DFT-D). The computational results show an increasing stabilizing interaction of the order Li<sub>+</sub> < Rb<sub>+</sub> < Na<sub>+</sub> < K<sub>+</sub> for the double and triple-layer quadruplexes, which is in agreement with the experimental order of affinity.

Partitioning of the bond energy between the alkali cation and the cavity of the quadruplexes, showed that the desolvation energy and the size of the cation are of equal importance to the trend. Descending the first group of the periodic table shows a decrease of the desolvation energy of the cation, and a decrease of the attractive interaction between the cation and the quadruplex. Simultaneously, hosting of the larger cations diminishes the deformation of the empty quadruplex cavity. These effects result together in a minimum of the bond energy for K+.

The magnitude of the bond energy stays approximately the same for the subsequent binding events of a first, second and third cation in double, triple and four-layer guanine quadruplexes, respectively. Although the interaction energy decreases for each binding event, the contribution of solvation effects becomes more significant following this trend. The stabilizing solvation energy increases faster than the destabilizing desolvation energy with each binding event, resulting in an equalized bond energy.

Decomposition of the interaction energy into physically meaningful terms showed that electrostatic repulsion between the hosted metal cations is responsible for the diminished interaction energy. This work demonstrates that solvent effects become of increasing importance for the stabilization of highly charged multi-layer guanine quadruplex DNA.

Conflicts of interest

There are no conflicts to declare.

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References

1 S. Neidle and S. Balasubramanian, Quadruplex Nucleic Acids, Royal Society of Chemistry, Cambridge, 2006.
2 M. L. Bochman, K. Paeschke and V. A. Zakian, Nat. Rev. Genet., 2012, 13, 770–780.
3 R. Hänsel-Hertsch, M. Di Antonio and S. Balasubramanian, Nat. Rev. Mol. Cell Biol., 2017, 18, 279–284.
4 J. T. Davis, Angew. Chem., Int. Ed., 2004, 43, 668–698.
5 E. Henderson, C. C. Hardin, S. K. Walk, I. Tinoco and E. H. Blackburn, Cell, 1987, 51, 899–908.
