Noncollinear ferrielectricity and morphotropic phase boundary in monolayer GeS

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I. INTRODUCTION

Ferroelectric (FE) materials with spontaneous switchable electric polarization have been widely explored for their rich physics and broad applications [1–3]. However, for those mostly used FE perovskite oxides, the ferroelectricity is seriously suppressed when the material thickness decreases to ~1 nm, due to the strong depolarization field and surface effects [4,5], which limits the further miniaturization of devices.

Two-dimensional (2D) van der Waals polar materials provide the possibility to overcome this challenge and achieve atomic-scale applications [6,7]. Recently, many 2D FE materials, e.g., SnTe [8,9], CnInP2S6 [10,11], and SnS [12], have been obtained in experiments. More 2D FE materials were theoretically predicted [13–15]. In addition, antiferroelectricity with antiparallel electric dipoles was also found in MXene [16] and group V monolayers [17]. Besides these plain collinear dipole textures, noncollinear dipole order was also recently predicted in monolayers of dioxynhaldides (WO2Cl2 and MoO2Br2) [18]. This progress has opened an emerging field of 2D polar materials.

Despite these achievements, the physical understanding of 2D polarity remains in the early stage. Here a structural evolution diagram is established for monolayer GeS, which leads to a noncollinear ferrielectric δ phase energetically as stable as the ferroelectric α phase. Its ferrielectricity is induced by the phonon frustration, i.e., the competition between ferroelectric and antiferroelectric modes, providing more routes to tune its polarity. Besides its prominent properties such as large band gap, large polarization, and high Curie temperature, more interestingly, the morphotropic phase boundary between α and δ phases is highly possible, which is crucial to obtain giant piezoelectricity for lead-free applications.

II. RESULTS AND DISCUSSION

A. Origin of δ phase

In Ref. [25], the so-called α-GeS (space group No. 31, Pnma) was predicted, together with other α phases of the group IV-VI family. The α phase can be derived from the paraelectric (PE) parent phase (space group No. 129, P4/nmm), as shown in Fig. 1(a).

Using a $\sqrt{2} \times \sqrt{2}$ unit cell [constructed by the a-b vectors in Fig. 1(a)], the phonon spectrum of the PE phase has two (dual) main imaginary frequencies at the Brillouin center Γ point, as shown in Fig. 1(b). The duality comes from the tetragonal symmetry. As a result, a uniform in-plane displacement of all Ge atoms can occur along the (110) direction (i.e., the (100) direction of the primitive cell), leading to the FE α phase as predicted in Ref. [25], whose phonon spectrum shows its dynamic stability despite tiny imaginary frequencies at the Γ point, as shown in Fig. S1(d) in the Supplemental Material [35].
FIG. 1. (a) Structural evolution diagram of monolayer GeS. Center: the square PE structure as parent phase. The dynamic stable phases are four corner ones, which can be derived by condensing two branches of unstable phonon modes together. The edge ones, obtained by considering only one single branch of unstable phonon mode for each other, are dynamic unstable. For comparison among different phases, the base vectors $a-b$ are shown, while the minimal unit cells of PE and $\alpha$ phase are indicated by green rectangles. (b)–(e) The corresponding phonon spectra.
TABLE I. Comparison among different phases of 2D GeS monolayers. $a$ and $b$ are the in-plane lattice constants as defined in Fig. 1(a). $E_{coh}$ is the cohesive energy per atom with respect to isolated atoms. $P$ is the polarization. Our results of $P$ for $\alpha$-GeS and $\beta$-GeS monolayers are consistent with previous works [25,29]. The $\beta$ phase is not derived from the aforementioned square structure [29].

| Phase | $a$ (Å) | $b$ (Å) | $E_{coh}$ (eV/atom) | $P$ (pC/cm) |
|-------|---------|---------|---------------------|----------|
| PE    | 5.517   | 5.778   | 5.754               | 5.657    |
| $\alpha$ | 5.571   | 5.778   | 5.680               | 5.656    |
| $\delta$ | 3.5976  | 3.6216  | 3.6195              | 3.6087   |
| $h$   | 2.0       | 2.0       | 2.0               | 2.0       |
| $\beta$ | 0        | 4.81     | 2.73               | 0.195    |

However, besides the imaginary frequencies at the $\Gamma$ point, there are additional imaginary frequencies at the Brillouin edge $X/Y$ points, which indicate the antiferroelectric (AFE) distortions. Considering the $x$-$y$ duality from tetragonal symmetry, the FE and AFE orders can be along the $x$ or $y$ axis. However, the pure FE or AFE order along the $x$ or $y$ axis remains dynamic unstable, with residual imaginary frequencies [Figs. 1(c) and 1(d)]. Only the combination of two distortion modes can lead to stable phases. For example, the $\alpha$ phase can be considered as a combination of FE modes along the $x$ and $y$ axes. In this sense, the combination of the FE mode along the $x$ axis and the AFE mode along the $y$ axis (or vice versa) can lead to a new phase, i.e., the $\delta$-GeS (space group No. 29, Pca2$_1$) [36], which owns a noncollinear dipole texture, similar to the case of dioxydihalides [18]. Such $\delta$-GeS shares the identical geometry of $\delta$-phosphorene [34]. The phonon spectrum of $\delta$-GeS [Fig. 1(e)] indicates its dynamic stability. Furthermore, the combination between two AFE modes along the $x$ and $y$ axes can lead to one more exotic noncollinear dipole texture, i.e., the so-called haeckelite phase ($h$-GeS), which is also dynamic stable. The complete diagram of phase evolution is sketched in Fig. 1(a).

To further verify the stability of monolayer $\delta$-GeS, the cohesive energy is calculated, to compare with previously reported $\alpha$- and $\beta$-GeS [25,29]. As summarized in Table I, the cohesive energy of $\delta$-GeS is very close to that of $\alpha$-GeS, both of which are higher than those of $\beta$ phase and $h$ phase. Since the monolayer/few-layer $\alpha$-GeS had been experimentally realized [37,38], the predicted $\delta$-GeS should be also available, considering the proximate energy (only 2.1 meV/atom higher) [39]. Since the energy of $h$ phase is higher (12.9 meV/atom higher than $\alpha$ phase), in the following only the $\delta$ phase will be focused on.

The electronic band structure of monolayer $\delta$-GeS is shown in Fig. 2(a). The monolayer $\delta$-GeS is an insulator, with an indirect band gap (1.94 eV in PBE and 2.67 eV in HSE06), whereas the shapes of band dispersion are similar between PBE and HSE06. Such an appropriate band gap of $\delta$-GeS allows the switching of its polarization by external electric field.

The projected density of states (PDOS) is plotted in Fig. 2(b). There is significant hybridization between the Ge’s $s/p$ orbitals and S’s $p$ orbitals at the valence band maximum, while the conduction band minimum is mostly contributed by Ge’s $p$ orbitals. The Bader charge analysis suggests that 0.84 electron is transferred from Ge to S [40]. It is the interplay of both ionic and covalent bonding between Ge and S atoms that causes the lattice distortions in $\delta$-GeS [41], which is different from the driving force in WO$_2$Cl$_2$ and MoO$_2$Br$_2$ (the so-called $d^0$ rule) [18]. Such ionic and covalent bonding requires the structure of GeS satisfies the threefold bonding, i.e., each Ge bonds with three neighboring S and vice versa. All aforementioned stable phases fulfill this rule.

By taking the S framework as the reference, Ge ions in the other sublayer have the zigzag-type displacements in the $\delta$ phase. The displacements ($d$) along the $y$ axis [inset of Fig. 2(c)] are uniform, leading to a net FE polarization. Meanwhile, the displacements along the $x$ axis have opposite directions between neighboring Ge-S chains along the $x$ axis, i.e., with the AFE dipole order and thus zero net polarization. Using the standard Berry phase calculations [42], the FE polarization (along the $y$ axis) is estimated as 2.73 pC/cm [Fig. 2(c)] for $\delta$-GeS, which is lower than that of the FE $\alpha$ phase (as compared in Table I). If an effective thickness of monolayer $\delta$-GeS can be evaluated as the half of lattice constant $c$ in the $AB$ stacking bulk structure (i.e., 5.37 Å [35]), the 3D polarization is estimated as 50.8 $\mu$C/cm$^2$, about twice that of traditional FE perovskite BaTiO$_3$ (20–25 $\mu$C/cm$^2$) [43].

More interestingly, such ferrielectricity is robust against thermal fluctuation. We performed the $ab$ initio molecular dynamics (AIMD) simulation for a $\delta$-GeS monolayer to estimate its FiE transition temperature ($T_c$). The net polarization of $\delta$-GeS was calculated by the point charge model as a function of temperature, as shown Fig. 2(d). A distinct phase transition occurs around 500 K. This $T_c$ makes monolayer $\delta$-GeS attractive for room-temperature applications.
FIG. 3. (a) Double-well energy profiles for two FiE switching processes. The path I corresponds to the 180° in-plane flipping of dipoles, while the easier path II corresponds to the 83° in-plane rotation of dipoles. (b) The possible two paths for 90° rotation of the FiE domain obtained using the nudged elastic band method [44].

B. Domain switching and morphotropic phase boundary

In the following, the physics beyond a static FiE single domain will be studied, which is nontrivially interesting for monolayer δ-GeS.

First, for any polar material, the polarization switching is a key physical process. For the noncollinear FiE system, the switching paths are more interesting than those plain FE cases. As shown in Fig. 3(a), the 180° switching of net polarization can be achieved via two paths. Path II, with 83° in-plane rotation of local dipoles, can be easier than path I with direct 180° in-plane flip of local dipoles. This is a unique characteristic of the noncollinear FiE system.

Second, the 90° rotation of net polarization, i.e., the change between twin domains, can be realized via two paths, as shown in Fig. 3(b). Path I involves the h phase as the intermediate one, while path II involves the α phase. The energy barriers are close between these two paths (25 meV/f.u. vs 27 meV/f.u.), but path II owns a much lower energy saddle point.

Since the energies of α-GeS and δ-GeS are very proximate, their stability should be sensitive to stimulus, and thus tunable. As shown in Fig. 4, the energy of α-GeS will increase if the monoclinic distortion is suppressed. Then the δ phases will be the stabler one if the lattice is close to tetragonal, which can be realized by certain shearing strain conditions. The proximate energies and lattice constants, but different symmetries and polarizations, can lead to MPB between α and

FIG. 4. Strain modulated phase transition between the α and δ phases of monolayer GeS. By continuously tuning the monoclinic angle between vectors a-b (90° for the δ phase and 78.9° for the α phase), the energies of α and δ phase can be reversed. The intermediate framework is obtained using the linear interpolation between the optimized α and δ phases. When the monoclinic distortion is large enough, the δ phase decays to the α phase spontaneously.

FIG. 5. Phase coexistence in monolayer GeS. (a) The FE domain wall of δ-GeS is a strip of h phase. (b) The AFE domain wall of δ-GeS is a strip of α phase. Such domain walls, i.e., the phase coexistence, are stable during the structural relaxation. (c) Schematic of the coexistence of α and δ phases, with two strips of α phase, for example. (d) The width of α phase can change with energy barriers.

FIG. 5. Phase coexistence in monolayer GeS. (a) The FE domain wall of δ-GeS is a strip of h phase. (b) The AFE domain wall of δ-GeS is a strip of α phase. Such domain walls, i.e., the phase coexistence, are stable during the structural relaxation. (c) Schematic of the coexistence of α and δ phases, with two strips of α phase, for example. (d) The width of α phase can change with energy barriers.
\(\delta\) phases of monolayer GeS, which will be the origin of giant piezoelectric effect and many exotic collective effects.

The strain-dependent MPB will lead to possible phase coexistence, which is essential physics in many strongly correlated electronic systems [45] as well as relaxor ferroelectrics [46]. In fact, the domain walls in \(\delta\)-GeS can be a seed of phase coexistence. As shown in Figs. 5(a) and 5(b), the FE domain wall propagating along the \(b\) axis is just the \(h\) phase, while the AFE domain walls propagating along the \(a\) axis is just the \(\alpha\) phase. Both these domain walls are atomically sharp and stable during the structural relaxation. Since these two types of domain walls do not break the local threefold bonding character, the domain wall energies are not high: 26 meV/Å for the FE wall and 2 meV/Å for the AFE one, respectively.

The phase coexistence can occur in even larger scale. To demonstrate this issue, here a large supercell is constructed, with partial \(\alpha\) region and partial \(\delta\) region, as shown in Fig. 5(c). The stability of phase boundary can be estimated, as shown in Fig. 5(d). Such energy barriers make the MPB stable in monolayer GeS, which will not decompose forming calculations.

As mentioned before, according to the experience in 3D piezoelectric crystals and the related physical principles, it is well accepted that the MPB will enhance the piezoelectricity. Although the DFT method cannot directly calculate the piezoelectricity of the MPB system here, other numerical methods in larger scales, like the phase field model simulation, are encouraged to verify the enhanced piezoelectricity in the near future.

III. CONCLUSION

In summary, a frustration-induced noncollinear dipole order has been revealed in the ferrielectric \(\delta\)-GeS monolayer, which is as stable as the ferroelectric \(\alpha\)-GeS monolayer. Its prominent ferrielectric properties are attractive for experimental verifications and room-temperature applications. Furthermore, the competition between \(\alpha\) phase and \(\delta\) phase can be tuned by strain, and they can coexist with the morphotropic phase boundary. Our results can also be extended to other IV-VI two-dimensional polar systems, e.g., \(\delta\)-SnSe [30], which will significantly add value to low-dimensional materials.

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