Mathematical Model of HIV superinfection dynamics and R5 to X4 switch

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Abstract

During the HIV infection several quasispecies of the virus arise, which are able to use different coreceptors, in particular the CCR5 and CXCR4 coreceptors (R5 and X4 phenotypes, respectively). The switch in coreceptor usage has been correlated with a faster progression of the disease to the AIDS phase. As several pharmaceutical companies are starting large phase III trials for R5 and X4 drugs, models are needed to predict the co-evolutionary and competitive dynamics of virus strains. We present a model of HIV early infection which describes the dynamics of R5 quasispecies and a model of HIV late infection which describes the R5 to X4 switch. We report the following findings: after superinfection or coinfection, quasispecies dynamics has time scales of several months and becomes even slower at low number of CD4\(^+\) T cells. The curve of CD4\(^+\) T cells decreases, during AIDS late stage, and can be described taking into account the X4 related Tumor Necrosis Factor dynamics. Phylogenetic inference of chemokine receptors suggests that viral mutational pathway may generate R5 variants able to interact with chemokine receptors different from CXCR4. This may explain the massive signaling disruptions in the immune system observed during AIDS late stages and may have relevance for vaccination and therapy.

\textbf{Key words:} HIV, viral dynamics, quasispecies, coinfection, superinfection
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1 Introduction

Human immunodeficiency virus type 1 (HIV-1) infection is characterized by the progressive loss of CD4+ T cells. Infection by most strains of HIV-1 requires interaction with CD4 and a chemokine receptor, either CXCR4 or CCR5. During early stages of HIV-1 infection, viral isolates most often use CCR5 to enter cells and are known as R5 HIV-1. Later in the course of HIV-1 infection, viruses that use CXCR4 in addition to CCR5 (R5X4) or CXCR4 alone (X4 variants) emerge in about 50% patients (switch virus patients) [30,22]. These strains are syncytium-inducing and are capable of infecting not only memory T lymphocytes but also naïve CD4+ T cells and thymocytes through the CXCR4 coreceptor. The switch to use of CXCR4 has been linked to an increased virulence and with progression to AIDS, probably through the formation of cell syncytia and killing of T cell precursors. X4 HIV strains are rarely, if ever, transmitted, even when the donor predominantly carries X4 virus. CXCR4 is expressed on a majority of CD4+ T cells and thymocytes, whereas only about 5 to 25% of mature T cells and 1 to 5% of thymocytes express detectable levels of CCR5 on the cell surface [23]. It is noteworthy that X4 HIV strains stimulate the production of cellular factor called Tumor Necrosis Factor (TNF), which is associated with immune hyperstimulation, a state often implicated in T-cell depletion [25]. TNF seems able to both inhibit the replication of R5 HIV strains while having no effect on X4 HIV and to down regulate the number of CCR5 co-receptors that appear on the surface of T-cells [41].

A powerful concept in understanding HIV variability and its consequences is that of quasispecies [17]. Quasispecies are the combined result of mutations and recombination, that originate variability, and of co-infection (simultaneous infection), superinfection (delayed secondary infection) and selection, that keep variability low. HIV-1-infected individuals show heterogeneous viral populations of related genomes best described as viral quasispecies [7]. Infact, the infection capacity of mutants may vary, and also their speed of replication [39]. Moreover, since the number of targets (the substrate) is limited, fitter clones tend to eliminate less fit mutants, which are subsequently regenerated by the mutation mechanism [16]. While mutations are an essential ingredient for exploring the genetic space in the search for the fitness maximum, they also lowers the average fitness of the strain, that generally is formed by a cloud of mutants around the fitness maximum, the quasispecies. It’s worth noting that, for a given fitness landscape, there is a maximum tolerable mutation rate above which the quasispecies structure is lost (error threshold [17]).

The use of mathematical models is an insightful and essential complement to in vivo and in vitro experimental design and interpretation. Indeed mathematical models of HIV dynamics have proven valuable in understanding the mechanisms of many of the observed features of the progression of the HIV infection [27,10,9,15,55,42,54,51]. With the incorporation of accurate stoichiometries, gene expression levels and detailed kinetic information, from bioinformatics of sequence analysis and molecular
dynamics, mathematical models will be even more effective in predicting time and space patterns and the effects of drug therapy.

Here we address the issue of studying the coevolutive and competitive dynamics of different strains of HIV-1 virus also leading to the R5 to X4 phenotype switching. In doing this in the next section we introduce two models: a quasispecies model for R5 phase in which several R5 strains appear by mutations, co-infection and super-infection. In the limit of 1 quasispecies we are able to find the same values observed experimentally and in other models (most notably Perelson’s standard model). We test the model in the scenarios of co-infection and superinfection using parameters derived from biological literature. The second model focuses on the R5 to X4 shift and the hyperstimulation of T cell precursors through TNF. We are able to describe the decreasing dynamics of CD4+ after the appearance of X4 strains and make predictions on the HAART results in coinfection and superinfection scenarios at different times of the disease progression. We make use of phylogenetic models of the amino acid sequences of the human and mice chemokine receptor families to investigate the mutational pathway underlying the switching from different chemokine receptors. Finally we find that the switch from R5 to X4 may allow the HIV to bind to other chemokine receptors.

2 Models

2.1 A model of the early R5 phase

In someone who is newly infected by HIV, several variants of the virus, called R5, are often the only kind of virus that can be found. A meaningful way to model strain mutations, coinfection and superinfection is to extend Perelson’s standard model [42] to multiple strains and incorporate immune response to R5 quasi species amplification (in the following termed QSR5 model). The R5 quasispecies dynamics can be described by the following set of equations:

\begin{align}
\dot{T}_i &= \left( \lambda_i + \sum_k \gamma_{ik}^{(T)} I_k T_i \right) \left( 1 - \frac{1}{K} \sum_i T_i \right) - \left( \delta_T + \sum_k \beta_k V_k \right) T_i, \\
\dot{I}_k &= \left( \sum_{k'} \mu_{kk'} \beta_{k'} V_{k'} \right) \left( \sum_i T_i \right) - \left( \delta_I + \sum_i \gamma_{ki}^{(I)} T_i \right) I_k, \\
\dot{V}_k &= \pi I_k - \left( c + \sum_i \gamma_{ki}^{(V)} T_i \right) V_k.
\end{align}

The following cell types are considered: T-helper (CD4+) cells carrying the CCR5 co-receptor responding to virus strain \( i \), \( (T_i) \); T cells infected by virus strain \( k \), \( (I_k) \);
k strains of R5 virus, (V_k). We have thus assumed that viral strain k are identified by just one epitope, which is then displayed on the surface of the T cell of class k, and that a T cell of class i can be activated at least by one CD4+ T cell carrying the epitope k, which is specific of the viral strain k. The indices i (k) range from 1 to N_i (N_k), and in the following we have used N_i = N_k = N.

In Equation (1) T cells are generated through two mechanisms: the bone-marrow source (and selection in the thymus) and the duplication of T cell strains activated upon the recognition with an antigen carrying cell that may be even an infected one. We modeled T cells activation as a logistic term mimicking the global carrying capacity of immune system [5].

The death-rate term is composed by a natural death rate proportional to the population, and by the infection rate of T cells due to any viral strain. The term \( \sum_k \beta_k V_k T_i \) and the sum over \( T_i \) in the I cell birth rate reproduce the infection probability, that is the same irrespective of the T class. As a cell become infected it does no more contribute to the immune response.

Equation (2) describes the infection dynamics. The two death rate parameters account for the decrease of the infected cells due to cellular death and after the action of T-killer cells (CD8+). Even if there are clear experimental evidences that CD4+ cells decrease during the late HIV infection stages and in the AIDS state, as far as the asymptomatic phase of the infection is concerned, the parameter \( \delta^I \) may be assumed as a constant, medical literature referred, value.

The \( \mu_{kk'} \) term is responsible of the mutation process affecting the phenotype, essential for the formation of new quasispecies. The choice of a mutation rate of the order of \( 10^{-5} \) is based on considering only those non-synonymous mutations that alter the phenotype (protein structure) [5].

In Equation (3) the virus replicative dynamics is described. The birth rate term is proportional to the virus “budding” numerosity while the viral death rate parameters depend on the rate of natural death and accounts for the recognition of virus by B cells.

It’s worth noting that B-cells and T-killer cells are only implicitly included in the model in order to reduce the dimensionality without loosing too many details. We assume that these responses are fast enough to be at equilibrium and they are just proportional to the abundance of (cognate) T helper cells.

The three \( \gamma \) parameters \( \gamma^{(T)} \), \( \gamma^{(I)} \) and \( \gamma^{(V)} \) are matrices describing the interactions between cells and/or cells and viruses, i.e. who will interact with whom, in terms of geometry and strength of the interaction. It is thus possible to consider which strains of the virus are recognized and with which accuracy, and the same for the action of T-killer cells and B-cells. It is also worth noting that \( \gamma^{(T)}_{1i} \) is the most important determinant of the viral fitness [5].
Fig. 1. Schematic description of the model for the switching from R5 to X4 viral phenotype. Naïve T-cells, $U$, are generated at constant rate $N_U$ and removed at rate $\delta^U$. They give birth to differentiated, uninfected T-cells, $T$. These in turn are removed at constant rate $\delta^T$ and become infected as they interact with the virus. Infected T-cells, $I$, die at rate $\delta^I$ and contribute to the budding of viral particles, $V$, that are cleared out at rate $c$. As soon as the X4 phenotype arise, the production of the TNF starts, proportional to the X4 concentration and contribute to the clearance of naïve T-cells, via the $\delta_f^U$ parameter.

2.2 Modeling the transition R5 to X4

In about half of the people who develop advanced HIV disease, the virus begins to use another co-receptor called CXCR4 (X4 viral phenotype). The shift to using CXCR4 is considered a bad sign because it is often accompanied by a dramatic increase in the rate of T-cell depletion. The inability of the thymus to efficiently compensate for even a relatively small loss of naïve T cells may be a key factor for CD4+ T cells depletion and AIDS progression. We hypothesize that it may not be exhaustion of homeostatic responses, but rather thymic homeostatic inability along with gradual wasting of T cell supplies through hyperactivation of the immune system that lead to CD4 depletion in HIV-1 infection. We here introduce a modified version of the previous model, that considers only CD4 dynamics. Neither B nor CD8+ T cells are explicitly modeled and the space that now is considered is that of different phenotypes of the virus (we term this model R5toX4 model). Under those
| Parameter                                      | Symbol | Value | Units of Meas. |
|------------------------------------------------|--------|-------|---------------|
| Production of immature T cells                 | $N_U$  | 100   | cell/µl $t^{-1}$ |
| Death rate of immature T cells                 | $\delta_U$ | 0.1   | $t^{-1}$       |
| Death rate of immature T cells upon the interaction with TNF | $\delta_U F$ | $10^{-5}$ | µl/cell $t^{-1}$ |
| Decreasing infectivity of R5 phenotype due to TNF | $k_{R5}$ | 10$^{-7}$ | (µl/cell)$^2$ $t^{-1}$ |
| Increasing infectivity of R5 phenotype due to TNF | $k_{X4}$ | 10$^{-7}$ | (µl/cell)$^2$ $t^{-1}$ |
| Increasing death rate of immature T cells due to TNF | $\delta_I X_4$ | 0.0005 | µl/cell $t^{-1}$ |
| Rate of production of TNF                      | $k_F$  | 0.0001 | $t^{-1}$       |

Table 1
Model for the R5 to X4 phenotypic switch: a summary of the additional parameters introduced. The value of the other parameters are medical literature referred, see also [8].

assumptions we may focus on the appearance of X4 viruses and on their subsequent interaction with R5 strains.

\[
\frac{dU}{dt} = N_U - \delta^U U - \delta_U F U F \tag{4}
\]
\[
\frac{dT_i}{dt} = \delta^U U - \left( \sum_k \beta_k V_k \right) T_i - \delta^T T_i \tag{5}
\]
\[
\frac{dI_k}{dt} = \left( \sum_{k'} \mu_{kk'} \beta_k V_{k'} \right) \left( \sum_i T_i \right) - \delta^I I \tag{6}
\]
\[
\frac{dV_k}{dt} = \pi I_k - c V_k \tag{7}
\]
\[
\frac{dF}{dt} = k_F \sum_{k \in X4} V_k \tag{8}
\]

In the equations above, the variables modeled are the pool of immature CD4+ T cells, $U$, the different strains of uninfected and infected T cells ($T$ and $I$, respectively), HIV virus, $V$, and the concentration of TNF, $F$. A schematic view of the model is depicted in Fig.1. The value of the parameters introduced with respect to the R5 model are summarized in Table 2.2.

In particular, Equation (4) describes the constant production of immature T cells by the thymus $N_U$ and their turning into mature T cells at rate $\delta^U$. If X4 viruses are present, upon the interaction with TNF, immature T-cells are cleared at fixed rate $\delta^U F$.

Equation (5) describes how uninfected mature T cells of strain $i$ are produced at fixed rate $\delta^U$ by the pool of immature T cells. Those cells, upon the interaction with any strain of the virus, $V_k$, become infected at rate $\beta_k = \beta \ \forall k$. The infectiousness parameter, $\beta$, is not constant over time, but depends on the interplay between R5 and X4 viruses. In particular, due to the presence of TNF, the infectivity of R5 strains is reduced ($\beta_{R5}(t) = \beta - k_{R5} F(t)$), while the one of X4 viruses increases, with constant of proportionality $k_{X4}$ ($\beta_{X4}(t) = \beta + k_{X4} F(t)$), mimicking the cell
syncytium effect induced by the TNF molecule.

Equation (6) describes the infection of mature T-cells. Infected T-cells of strain $k$ arise upon the interaction of a virus of strain $k$ with any of the mature T-cell strains. The infected cells, in turn, are cleared out at a rate $\delta^I$. When TNF is released, this value increases linearly with constant $\delta^I_{X4}$, $\delta^I(t) = \delta^I + \delta^I_{X4} F(t)$.

Equation (7) is close to that in the R5 quasispecies model, a part from different viral phenotypes being here considered.

Finally, in Equation (8), we model the dynamics of accumulation of TNF by assuming the increase in TNF level to be proportional, via the constant $k_F$, to the total concentration of X4 viruses present.

2.3 Investigating the mutational pathway from R5 to X4

In our model we represent the different phenotypes by using a linear strain space, see for instance [20,34] for similar assumptions. The strain space is ordered in terms of phenotype similarity. This assumption is justified if the phenotypes are determined by few viral protein functional determinants which are both independent and differ only few DNA bases, i.e. few mutations can change one determinant into another.

Although we are aware of the several recent works on HIV mutational dynamics and phylogenetic assessments, we thought that a meaningful way to estimate the mutational pathways between R5 and X4 seen is to use phylogenetic inference on chemokine receptor families. The assessment of phylogenies using likelihood framework depends on the choice of an evolutionary model [53]. We computed the maximum likelihood (ML) analysis of the CRs data set under different models of evolution: [12], JTT [29], WAG [52]. We used these models considering the incorporation of the amino acid frequencies of the chemokine data sets, (‘+$F$’), and the heterogeneity of the rates of evolution, implemented using a gamma distribution (‘+$\Gamma$’ [56,57].

3 Results

We have first extended Perelson’s standard model [42] to incorporate different antigen recognition abilities by the immune system and coexistence dynamics of different R5 strains of HIV virus. Our approach is a mean field one, i.e. we investigate the average quantities of these molecular species [43,32,24,1,19]. Then, we have modified the model to describe features of the latent phase of the infection, i.e. the R5 to X4 switch and the hyperstimulation of the T cell precursors through the TNF.
response to the first inoculum has completed and the virus has established a chronic or to a global constraints (the $K$ also Fig. 2. Moreover, in the presence of coupling among strains, due to competition phenotype, mutations are necessary to populate the other strains of the virus, see superinfection, respectively. We considered the first viral inoculum to happen at time $t=0$ in plot (a) and $t=3000$ in plot (b); the y-axis on the right shows the interaction strength (dashed line) between T cells and virus phenotypes (x-axis).

3.1 Amplification of R5 strains: mutation, co-infection and super-infection

Recent works have shown that HIV quasispecies may compete [11] and cooperate [59] and that persistence of the initial or ancestor quasispecies is a good indicator for disease progression [4]. Burch and Chao [8] have stressed that the evolution of an RNA virus is determined by its mutational neighborhood. As the phenotype divergence among viral strains arises from differences in selection pressure, these differences may lead, for instance, to a higher infection rate. Since the competition is through the immune system response and given that the phase space of antigen recognition is not homogeneously covered [14], the HIV high mutation rate allows the quasispecies to find regions with weak immune response. This competition may lead to speciation of viral strains.

If we consider the model of the early phase of the infection, the evolution of T cells abundances in a scenario of quasispecies is shown in Fig. 2a. As the asymptotic state of our model is a fixed point, the asymptotic distribution is insensitive of the initial conditions, and the strains corresponding to higher fitness are more abundant (see inset of Fig. 2b). However, one should consider that this asymptotic state may be reached after such a long time that it may be outside any practical scenario of the progression of a disease. The role of mutations in the transitory regime is quite particular. First of all, starting from the first inoculum at time $t = 0$ on the zeroth phenotype, mutations are necessary to populate the other strains of the virus, see also Fig. 2. Moreover, in the presence of coupling among strains, due to competition or to a global constraints (the $K$ parameter), the specific form of mutations does not play a fundamental role, see also Ref. [3].

Figs. 3a and 3b report the results of short time and long term viral coevolution after superinfection, respectively. We considered the first viral inoculum to happen at time $t = 0$, with the superinfection event occurring at time $t = 20$, when the immune response to the first inoculum has completed and the virus has established a chronic
Fig. 3. Viral counts, $V$, during a superinfection scenario. We set $N=5$ and no mutation is considered, thus $\mu=0$. (a) A slow mounting of the second viral infection ($\square$), having time scale of several months, is observed. In (b) a compromised immune system is considered. The time for the second strain to reach the same abundance of the first-infecting strain ($\Diamond$) is greater than in (a).

infection. After the second inoculum the model exhibits a short transient, followed by a slow mounting of the second infection. Due to the resulting low dynamics, the time needed by the second quasispecies to reach the same level of the other amounts to several months (Fig. 3a), and represents another example of a slow relaxation toward a fixed-point equilibrium. We may also take into consideration the progression of the disease, characterized by a compromised immune system, assuming, as a first approximation, a lower number of T cells, i.e. a lower value of $\lambda$, with respect to the previous scenario. In this case the strain corresponding to the second inoculum requires much longer time to reach the same abundances of the first strain (Fig. 3b).

If we consider HAART therapy, is interesting to address the question of what happens if a patient suddenly stops the drugs treatment. During HAART virus load in blood declines, but the virus is not definitively eradicated. At the same time T cells recover and their concentration arise towards the stationary state corresponding to the low-level concentration of the virus. As the treatment is interrupted, virus level begins to increase again. Something similar to a second, delayed infection, occurs. It’s worth noting that, if more than one viral strain is present, as in the case of a coinfected or superinfected patient, the second infection may lead to a different asymptotic dominant strain. Infact the growth velocities of the different phenotypes of the virus depend both on the concentration of uninfected T cells and on the fitness of the different strains. Thus a more aggressive strain or one with a weaker recognition by the immune system may take advantage of the interruption of the drugs treatment and of the renewed infection, leading to an acceleration of the disease.
Fig. 4. Speciation of virus quasispecies and uninfected T cells dynamics after competitive superinfection at four different times: $t = 0$ (a), $t = 4.5$ (b), $t = 5.25$ (c) and $t = 5.75$ (d). Virus strain 15 is present at time $t = 0$, while strain 5 is inoculated at time $t = 1$. Mutation rate $\mu = 10^{-4}$ and non-uniform interaction strength as in Fig. 2. The dashed line represents the abundances of T cells targeting each viral phenotype, represented as vertical stems.

Finally we have studied how the co-evolutionary and competitive dynamics of viral strains, mediated by the immune response, may lead to the formation of new viral quasispecies. In Fig. 4 we consider a phenotypic space of 25 strains and the first inoculum is at phenotype 15 (Fig. 4a), followed by a delayed inoculum at phenotype 5 at time $t = 1$. We account for the differences in recognition ability of viral antigens by T cells by using a non-uniform interaction strength which favor the central phenotypes. The immune system does not discriminate among similar phenotypes, thus inducing a competition among neighboring strains. The result of this induced competition is the separation of the original quasispecies into two clusters (quasispeciation), Fig. 4b. However the immune system response continues to change in time (Figs. 4c-d), resulting into a complex coevolution with viral populations.

### 3.2 R5 to X4 switch

We studied the coevolutive dynamics leading to X4 strain appearance by successive mutations of the ancestor R5 strain. The stimulated production of TNF regulate the interactions between immune response and the virus and between the different strains of HIV virus. The results of these interactions are a decline in T-cells level, leading to the AIDS phase of the disease, and the decline in levels of viruses using the R5 coreceptor. In Fig. 5 the temporal evolution of the infection is shown, with the appearance of the X4 strain, and the successive decline in T-cells abundances.
Fig. 5. Time evolution of the concentrations of uninfected T-cells (◇) and viruses (+), during R5 to X4 switch, occurring at time $t \approx 900$. The time of appearance of the X4 strains depends on the mutation rate and on the phenotypic distance between R5 and X4 viruses. After the appearance of the X4 phenotype a continuous slow decline in CD4+ T-cells level leads to AIDS phase (CD4 counts below 200cells/ml). We set $\mu \approx 0.001$ and $d_P \approx 5$.

Fig. 6. The efficacy of HAART therapy may be disrupted by a sudden interruption in drugs treatment. If time has passed for mutations to populate the R5 strains closer to the X4 phenotypes, an earlier appearance of X4 strains may occur. Uninfected T-cells (◇) and viruses (+). Parameters as in Fig. 5.

The time at which the phenotypic switch occurs depends both on the mutation rate $\mu$ and on the phenotypic distance between R5 and X4 strains, $d_P$. Once experimental data are known, it’s possible to tune the model parameters to their corresponding biological values. Moreover, to get a better insight on the range of variability of the time of appearance of X4 phenotype, a sensitivity analysis for varying values of the $\mu$ and $d_P$ parameters is still possible.

In Fig. 6 we considered HAART treatment, which is usually able to decrease the concentration of the virus in the blood and delay the X4 appearance. The use of this model suggests a possible scenario in the case of a sudden interruption in the
Fig. 7. CD4+ T-cells concentration during HIV-1 super-infection by a R5 viral strain. Different signs represent: evolution without superinfection, (◊); superinfection occurring at time $t = 100$ and 400, (+) and (□), respectively. For a superinfection event occurring after the R5 to X4 switching the dynamics is qualitatively the same as for a single infection, (◊). If the second delayed infection occurs before the R5 to X4 switching, the time of appearance of X4 viruses may be shorter, when the superinfecting strain is closer to the X4 phenotypes, (+, □). Parameters as in Fig. 5.

therapy. If the different R5 strains experience the same selection pressure, as soon as the therapy is stopped, the X4 strain may appear sooner. In fact during the treatment the concentration of the different strains of R5 viruses is kept to a very low level while T-cell abundances increase. As the therapy is interrupted, all the strains give rise to a renewed infection, but now also the strains closer to the X4 co-receptor using viruses are populated, and a mutation leading to an X4 strain occurs sooner.

We have finally studied the influence of switching co-receptor usage in superinfection dynamics. In Fig. 7 we show T-cells dynamics for different times of the superinfection event. We may observe that if the superinfection occurs after the appearance of the X4, the new R5 strain does not have any effect on T-cells behavior. On the other hand is worth noting that if the new R5 inoculum take place before the X4 appearance, this may speed up the switching to the X4 phenotype if the new strain is mutationally close to the X4.

### 3.3 Investigating the mutational pathway between R5 and X4

Research into HIV dynamics has much to gain from investigating the evolution of chemokine co-receptor usage. Although CCR5 and CXCR4 are the major coreceptors used by HIV-1 a number of chemokine receptors display coreceptor activities in vitro. Several other chemokine receptors, possibly not present on the T cell membrane, may act as targets. To date, a number of human receptors, specific for these chemokine subfamilies, have been described, though many receptors are still unassigned. Several viruses, for example Epstein-Barr, Cytomegalovirus, and Herpes Samiri, contain
functional homologous to human CRs, an indication that such viruses may use these receptors to subvert the effects of host chemokines [38]. Cells different from CD4 and CD8, such as macrophages, express lower levels of CD4, CCR5, and CXCR4 on the cell surface compared with CD4+ T cells [33,40,50], and low levels of these receptors expressed on macaque macrophages can restrict infection of some non-M-tropic R5 HIV-1 and X4 simian immunodeficiency virus (SIV) strains [6,37].
Fundamental to the evolutionary approach is the representation of the evolution of sequences along lineages of evolutionary trees, as these trees describe the complex patterns of dependence amongst sequences that are caused by their common ancestry [52,48,21].

The ML tree, obtained using the JTT+$F+\Gamma$ model of evolution, is shown in Figure 8. The topology clearly shows that the CCR family is not homogeneous: CCR6, CCR7, CCR9 and CCR10 are separated from the other CCRs; in particular, CCR10 clusters with CXCRs; CXCR4 and CXCR6 do not cluster with the CXCRs. The tree shows that there are many mutational steps between CCR5 and CXCR4. The phylogeny suggests that the mutations that allow the virus env to cover a wide phenotypic distance from R5 to X4, may also lead to visit other receptors. Since the external loops of CRs contain the binding specificities and have higher rates of evolution than internal loops and transmembrane segments [46], the tree Fig. 9 shows a relative...
longer mutational pathway between CCR5 and CXCR4 with respect to pathway linking CCR5 to other receptors.

4 Discussion

The worldwide presence of several strains of the HIV virus and their often simultaneous presence within a patient, due to the increased frequency of multiple infections, are the remarkable features of HIV pandemia. For example, HIV-1 exists as several groups, subdivided in growing number of subtypes which are slightly predominant in different geographical regions [58]. HIV-1-infected CD4+ T cells isolated from the spleens of two individuals were recently shown to harbor anywhere between one and eight proviruses, with an average of three to four proviruses per cell [13]. Mutations, recombinations and selection pressure cause the appearance of quasispecies [17].

The interest in HIV quasispecies is motivated by concern about developing strain specific drugs. Quasispecies are likely the key for understanding the emerging infectious diseases and has implications for transmission, public health counseling, treatment and vaccine development. Moreover, the observed co-evolutionary dynamics of virus and immune response opens the way to the challenging possibility of the introduction or modulation of a quasispecies to be used in therapy against an already present aggressive strain, as experimented by Snell and colleagues [47]. The authors showed that the introduction of an engineered virus can achieve HIV load reduction of 92% and recovery of host cells to 17% of their normal levels (see also the mathematical model in Ref. [44]).

Different drug treatments can alter the population of quasispecies. Will R5 blocking drugs cause HIV to start using X4? And will that be worse than letting the R5-using virus stay around along at its own, slower, but no less dangerous activity?

We first presented a model of the within-patience persistence of HIV quasispecies, by extending to multiple strain the Perelson’s standard model [42]. This approach allows to incorporate coevolutive and competitive dynamics resulting from the different strains of HIV virus and different antigen recognition abilities by the immune system considered. Our model shows that the time evolution of the competition between quasispecies is slow and has time scales of several months.

Recent works show that TNF is a prognostic marker for the progression of HIV disease [25,26]. We focused on both the inability of the thymus to efficiently compensate for even a relatively small loss of T cells precursors and on the role of TNF in regulating the interactions between the different strains of HIV virus. The second model we have introduced shows that keeping low the concentration of TNF, both the depletion of T-cells precursors repertoire and the R5 overcome by X4 strains slow down.
Phylogenetic inference of chemokine receptors shows that there are several mutational patterns linking CCR5 to several receptors that have the same branch length of that from CCR5 to CXCR4. There is a massive abundance of signaling disruptions in the immune systems during AIDS progression, particularly after the transition R5 to X4. These disruptions may be due to variants of the virus which bind other chemokine receptors. This hypothesis also suggests that R5-late strains in not-X4 AIDS, which are known to be different from R5 early strains, may have accumulated mutations enabling them to interact with other chemokine receptors. Therefore, our model suggests the sooner the HAART the better, because the presence of a large number of R5 will increase the mutational spectra in R5 strains (late R5) and the probability of getting closer to the binding specificities of other chemokine receptors.

The large effect of TNF on T cells dynamics described by our model, suggests the benefit of a TNF buffering therapy. It is known that the dynamics of TNF is related to the dynamics of TNF-related apoptosis-inducing ligand (TRAIL). In this model we consider constant the concentration of TRAIL [26] and we do not consider many other important players such as Rantes.

Our models represent also a general framework to investigate intermittency or switching dominance of strains and the arising of new dominant strains during different phases of therapy; how superinfection will evolve in case of replacement of drug-resistant virus with a drug-sensitive virus and acquisition of highly divergent viruses of different strains; to investigate whether antiviral treatment may increase susceptibility to superinfection by decreasing antigen load.

Work in progress focuses on refining the ”R5toX4” model by incorporating the dynamics for TRAIL and comparing our results with those of Ribeiro and colleagues [45] who have presented a model of R5 to X4 switch based on the hypothesis that X4 and R5 viruses have a preferential tropism for naïve and memory T cells, respectively.

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