Abstract

This article reviews soft pneumatic actuators (SPAs) that are manufactured entirely via additive manufacturing methods. These actuators are known as four-dimensional (4D)-printed SPAs and can generate bending motions in response to either pressurized or vacuum (negative pressure) air stimulus after fabrication. They are characterized by geometrical and material factors that determine their motion trajectory, and the force they exert on manipulated soft objects in delicate applications such as food handling and non-invasive surgery. Here, we review various 3D printers and materials used for the fabrication of the pressurized air bending-type SPAs. The reported approaches for modeling and control of these actuators are presented and compared. General discussions, as well as future directions and challenges of these actuators, are given.

Keywords: soft pneumatic actuators; soft robots; 3D printing; 4D printing

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1. Introduction

Actuators are the devices that cause motion, which could be linear, rotary, or their combination, to move joints and body of the robot. There are several different types of actuators in soft robotics, which are classified in terms of their source of energy and structural materials, such as pneumatic (Yap, Ng, and Yeow 2016), hydraulic (Cacucciolo et al. 2019), liquid crystal (Roach et al. 2018), liquid metal (He, Zhou, et al. 2018), and ionic polymer actuators.
The soft actuators exert force upon mechanical changes in response to the various stimuli, such as pressure, electricity, heat, humidity, and light. The soft actuators exert force upon these stimuli, rolling, rotating, jumping, and digital-ness, including polymers, hydrogels, inks, food materials, stereolithography (SLA), fused deposition modelling (FDM), direct ink writing (DIW), selective laser sintering (SLS), and digital light processing (DLP). The two major practical applications of 4D printing are the 3D-printed soft pneumatic actuators (SPAs) and soft pneumatic robots producing mechanical motions in response to pressurized or vacuum (negative pressure) air stimulus. In comparison to hydraulic actuators, the pneumatic actuators are simpler and cleaner due to operation by air, and notably deliver more compliance because of the lower density and viscosity thus making it possible to be used in applications which require the working fluid to travel relatively fast through lumens with small diameters. These products have been ideally suited to 4D printing due to ease of fabrication by using elastomeric materials. The 3D/4D-printed SPAs generated sophisticated motions (highlighted in Fig. 1) in response to simple pressurized air input, including bending, rotating, twisting, jumping, rolling, and their combinations with effective control capability. Desirable properties such as flexibility, lightweight, large amplitude, and repeatability of motion, safety in a human-robot interactive environment, inexpensiveness and ease of fabrication, associated with these soft actuators could not be realized by using traditional robots. These unique attributes offered their implementations in industrial applications such as fruit harvesting, food packaging, space exploration, and non-invasive surgery. In this study, we focus on bending-type SPAs operating with pressurized air stimulus fabricated via different 3D printing technologies and materials. Fabrication of the 3D-printed SPAs could be conducted through various elastomeric materials and resins and 3D printing technologies. Thus far, the 3D-printed SPAs have been fabricated by Multi Jet Fusion (MJF), fused deposition modelling (FDM), direct ink writing (DIW), selective laser sintering (SLS), stereolithography (SLA), and digital light processing (DLP) which are discussed in detail.

The kinematics and dynamics modeling of the 3D-printed SPAs are different from the conventional rigid manipulators due to the properties of soft materials used in their fabrication. Therefore, recent studies have proposed new static, kinematic, and dynamic models for predicting the 3D-printed SPAs behavior, taking their body morphology, and the pressure system characteristics into consideration. Step-wise methods, including the analytical and finite element analysis (FEA) approaches, are reviewed and addressed here to demonstrate the relationship among the input pressure, geometry, material characteristics, and the bending curvature of 3D-printed SPAs.
The SPAs were initially developed because their passive compliance was desirable enough to tolerate the uncertainties that emerged while manipulating the delicate objects with various shapes and textures without the need for costly sensors and controllers. However, it has so far been challenging to accurately carry out pick and place tasks, especially on soft objects with variable shapes and orientations, without feedback information (Elgeneidy, Lohse, and Jackson 2018). Thus, equipping them with some level of sensing capabilities would lead to more controllable SPAs with enhanced functionality and a wider range of applications involving more complex manipulation tasks. The control of 3D/4D-printed SPAs is highly reliant on the integrated flexible electronics interfaces (Tan, Tran, and Chua 2016) and sensors (Zolfagharian, Kaynak, and Kouzani 2019). These components provide the necessary feedback information to help with the decision making of the manipulator without interfering with the compliance and morphology of a soft manipulator body (Zolfagharian et al. 2020). A broad range of chemical and biological sensors, which allow for more accurate and delicate manipulations, are also discussed in this study. Finally, appropriate control approaches for 3D/4D-printed bending-type SPAs are presented.

In light of the above discussion, the remainder of the paper is organized as follows: Section 2, is an overview of the fabrication of 3D/4D-printed bending soft pneumatic actuators. Section 3, presents analytical modeling for estimating the bending behavior of these actuators. Section 4, reviews different energy function methods in FEA of the 3D/4D-printed SPAs based on the materials used in their fabrications. Section 5, investigates control-based 3D/4D-printed SPAs. Section 6, discusses the current challenges of these actuators and suggests innovative research possibilities. Section 7 concludes the paper.
Fig. 2. Various applications of 3D/4D-printed SPAs; (a) food handling, reprinted from (Wang, Zhu, et al. 2017) with permission of Springer Nature open-access article distributed under the terms of the Creative Commons CC BY license; (b) rehabilitation, reprinted from (Keong and Hua 2018) with permission of John Wiley and Sons; (c) locomotion soft robot, reprinted from (Keong and Hua 2018) with permission of John Wiley and Sons.

2. Fabrication of 4D-printed bending-type soft pneumatic actuators

There have been extensive efforts on developing and testing soft pneumatic robots and actuators, the majority of which made by silicone elastomers, using molding and casting techniques (Batsuren and Yun 2019; Gorissen et al. 2017; Polygerinos et al. 2015; Mosadegh et al. 2014; Gorissen et al. 2014; Tolley et al. 2014; Sun, Song, and Paik 2013). Yet, there are some challenges associated with these methods including, intensive post-processing and labor, limited flexibility in design, and lack of repeatability in custom-made manufacturing with finely detailed features. It has been evident that the complexity involved in the structure of the soft actuators prolonged the fabrication time and complicated the procedure. However, additive manufacturing has been recently introduced as a promising approach for the fabrication of complex soft pneumatic robots and actuators with high resolution and repeatability. 3D printing has enabled producing elastomeric and thermoplastic materials under certain conditions. Different 3D printing technologies (highlighted in Fig. 3) have been employed for the fabrication of the current bending-type SPAs.
The DIW is an extrusion-based 3D printing approach where the liquid phase is dispensed out of a nozzle to fabricate a meso or micro-scale spatial actuator body layer by layer. This method enables the combinations of a broad range of materials and feasibility of multi-material printing while it is limited in the resolution and modification needed for two-stage materials curing, such as silicone. The DIW method was used to develop a moisture-cured silicone elastomer SPA with minimal voids, high strength, and elongation at break (Plott and Shih 2017). The process parameters were optimized to inhibit void formation during 3D/4D printing of the thin-wall silicone SPA. The developed SPA showed a reasonable fatigue life of over 30,000 cycles before failure (Plott and Shih 2017). A robotic soft actuator was 3D/4D-printed with programmable bioinspired architectures using photocurable resins by multi-material DIW (Schaffner et al. 2018). Tunable mechanical properties were achieved by adding vinyl-terminated silicones of different molecular weights to various silicone-based elastomers, namely Ecoflex 00-30, Dragonskin 30A, and Sylgard 184 (Schaffner et al. 2018). The capability of the DIW method in the combination of multi-material in this work led to the
development of the viscoelastic silicone inks to form variable stiffness elastomers to improve the control mechanism.

The FDM printers heat thermoplastic filaments to the melting point and then extrude them layer by layer to create 3D-SPAs. The FDM could accommodate a larger group of thermosetting elastomers while having the capability to simultaneously print different and multiple materials. The FDM is used as an effective additive manufacturing method in comparison with SLA, DLP, or SLS, mainly due to its inexpensive and repeatable process as well as much less post-processing requirements. A modified FDM printer was used to extrude EcoFlex 00-30 (Smooth-On) for developing the SPAs (Morrow, Hemleben, and Menguc 2016). The printed actuator was compared with the mold manufactured method. Though the initial feasibility of the method was confirmed, it was reported that the printed actuators significantly deviated from the desired features, particularly in the wall thickness, leading to lower bending deflection and the force output. A pneumatic finger-like SPA was developed in one step using the FDM method and Filaflex (Recreus) filament (Anver, Mutlu, and Alici 2017). The authors reported an average wall thickness of 0.64 mm. The low-cost SPA was 3D/4D-printed using the FDM technique and commercially available thermoplastic poly(urethane) (TPU), NinjaFlex (NinjaTek, PA) filament (Rosalia, Ang, and Yeow 2018; Yap, Ng, and Yeow 2016). The complex inner features without any supporting materials were utilized to devise the actuator with high force tip performance up to 80 N (Yap, Ng, and Yeow 2016). A minimum wall thickness of 1.2 mm reported for this actuator to operate fully airtight. The cyclic fatigue testing on the actuator demonstrated higher durability performance than the 3D-printed SPA developed by projection SLA (Peele et al. 2015). In another study, the Ninjaflex (NinjaTek, PA), with a shore hardness of 85A was used for developing 3D/4D-printed bellow-type SPA where the effects of number and size of the bellows on the curvature bending under the same input pressure were investigated (Keong and Hua 2018). Recently, a bioinspired fin-ray structure for increasing the conformal grasping of the 3D/4D-printed SPA was developed by using commercially available TPU NinjaFlex (NinjaTek, PA) (Tawk, Gao, et al. 2019). The 4D-printed soft gripper showed the enhanced capability of lifting objects with various shapes, stiffness, and textures. A recent modified 3D printing technology, named fused pellets printing (FPP), was developed to make a multi-material SPA with different components with various properties (Khondoker and Sameoto 2019). The SPA was made of optically transparent thermoplastic elastomer pellets of copolymer Kraton G1657 (styrene ethylene butylene styrene (SEBS), Kraton Corporation, USA) with 600% stretchability and rigid pellets of MM3520 (SMP Technologies Inc., Japan).

A combination of DIW and FDM methods was also devised to additively manufacture a composite SPA from silicone and thermoplastic elastomer (TPE) with potential applications in patient-specific and assistive biomedical devices (Ng et al. 2020), such as stent implant and less invasive surgery (Byrne et al. 2018). To achieve this a modified machine with a four-axis, combined FDM and paste extrusion head is required, which would be cumbersome to operate compared to the conventional extrusion-based DIW printers (Byrne et al. 2018).

The SLA is a resin-based 3D printing approach that is using photochemical processes to develop the SPAs with higher resolution and smoothness than the FDM method. However, it is limited to the smaller material library and is quite slow. One of the early fully 3D-printed soft pneumatic actuators was made by a digital mask projection SLA using elastomeric precursor (Spot-E resin, Spot-A Materials, Inc.) and with a thin layer of Sylgard 184 (PDMS)
adhered to the bottom surface as a polymerization inhibitor (Peele et al. 2015). The life-cycle of the elastomer was found to be 9 ± 3 cycles without failure under the performed fatigue test while it has shown a relatively low ultimate strain 1.40. A high resolution, ~50 μm, silicone-based elastomeric polydimethylsiloxane (PDMS) pneumatic channel was also fabricated using an SLA printer (Wallin et al. 2017). The actuator was featured with autonomic self-healing in sunlight. The same research team later developed a 4D-printed hydrogel-based poly-N-isopropylacrylamide (PNIPAm) and polyacrylamide (PAAm) SPA using multi-material SLA printing with the capability of perspiration at a higher temperature for self-regulating the desired bending (Mishra et al. 2020).

The SLS uses a laser as the power source to sinter and bind powdered plastic materials, such as polyamide, to create SPAs. Although the 3D/4D-printed SPAs made by SLS are benefiting from high strength and chemical resistance, this method is not suitable for developing the compact SPAs with complex geometries. A case study was performed on fabricating a single body air pressure actuator using the SLS for soft robotic hand application (Scharff et al. 2017). The actuator was 3D-printed using a flexible polyurethane like material to achieve the minimum wall thickness 1 mm. Removing the powder and purging the chamber at the end of printing were mentioned as the main challenges of using this method, impeding the design of various shapes, particularly at the corners of the chamber. Also, a SPA was 3D/4D-printed by using a powder mixture of glass fiber reinforced Nylon, stacking three soft bellow-type actuators using SLS 3D printing technology (Chen et al. 2019).

The PolyJet printing is a fast technique, which sprays the materials using different jetting heads to fabricate high-resolution SPAs. Complex geometries with thin walls could be achieved via this approach though suffering from poor mechanical properties compared with the FDM or SLS and more expensive. The PolyJet printing method was used for 4D printing of a multi-material finger-like SPA using Object350 Connex3 (Stratasys, Co., Ltd.) and rubber-like TangleBlack material for inflation chambers (Zhu et al. 2018). The wall thickness of the actuator was reported 0.03 mm while metamaterial design and variable stiffness designs, and glossy finish were featured in the work. In another similar study, a dual-material approach was utilized to develop a 3D/4D-printed SPA using the PolyJet method. The study compared the advantage of dual-material 4D printing of SPA with a single machine. It was revealed that the adverse balling effect of the soft body was reduced significantly in the dual-material printing. Also, a differential pressure three-chambered SPA was made by PolyJet method to increase the workspace of the actuator to a planar motion than a mere bending (Drotman et al. 2018). From a different perspective, a bellow-type pre-stressed SPA was 3D-printed, which functioned analogously to a vacuum SPA (Wang, Torigoe, and Hirai 2017). The actuator was fabricated by the Objet260 Connex3 printer (Stratasys, Co., Ltd.) and a combination of a rubber-like material, TangoPlus, and a hard material, VeroBlue. The novelty of this work was to develop a curled 3D-printed SPA that helps with more maneuverability for grasping tasks in fruit picking. The same group also developed a food handling soft gripper with the same printer and using a mixture of soft TangoBlack+ and hard polymeric, VeroWhite, materials (Wang, Chathuranga, and Hirai 2016). The pre-stressed layer was included in the design to create a larger initial opening space for grasping the foods in various sizes and shapes for packaging purposes. A PolyJet 3D printer (J750, Stratasys Ltd.) was also used to 3D/4D print a tunable stiffness SPA using Agilus30 (Wang, Zhu, et al. 2017). This study investigated the incorporation of VeroClear (Stratasys Ltd.) as shape memory polymer (SMP) to enhance the
functionality of the SPAs actuators to grasp arbitrary shapes objects in a broad range from 10 g to 1.5 kg (Zhang, Zhang, et al. 2019).

The DLP is another resin-based 3D printing method, like SLA, which uses light sources to fabricate SPAs. However, its difference with SLA is that the layers are all printed at the same time. The advantage of DLP systems in 3D/4D-printing of SPAs lies in constructing high-resolution features that could be directly printed and demand less post-processing steps. On the other hand, there are shortcomings in using DLP due to the limited number of commercial photo-curing silicone elastomers and small print volumes. A SPA was fabricated via a desktop DLP 3D printer and a mixture of TangoPlus FLX 930 and Rhodamine B resins (Ge et al. 2018). The printing process was reported to be completed in less than 30 minutes featuring a microactuator with a 0.2 mm wall thickness and 87.5 μm length. Miniature 3D/4D-printed SPAs were fabricated using the DLP-based multi-material printing technology for soft robotics. The manufacturing challenges caused by the void formation in millimeter scale were reported to be rectified through the appropriate selection of photo absorber, its concentration, layer thickness, exposure time to UV light, and their effects on the mechanical properties of the SPA (Zhang, Ng, et al. 2019). A highly stretchable ultraviolet curable resin was formulated by mixing epoxy aliphatic acrylate (EAA), and an aliphatic urethane diacrylate (AUD) and was printed using a DLP process for developing 4D-printed pneumatically actuated grippers (Patel et al. 2017). In a similar study, the stretchability and stiffness of a commercially available UV curable elastomer, TangoPlus, was modified, to withstand more than 1000 times of loading/unloading cycles (Hingorani et al. 2019). This was achieved by mixing two chemical additives, EAA as mono-acrylate based linear chain builder and AUD crosslinker. The outstanding stretchability of the introduced elastomer led to much larger bending deformation in the 3D/4D-printed soft actuator compared to other similar works. A photo resin made from bis(propylacrylamide)-poly(dimethylsiloxane) (PDMS-DMAA) was also used for DLP printing of soft pneumatic actuator with high elongations of up to 472% under tensile load (Thrasher, Schwartz, and Boydston 2017).

In general as highlighted in Table 1, the DIW has shown promising results for 3D/4D printing of SPAs with minimal voids, controlled variable stiffness, acceptable fatigue properties, and high strength and elongation at break compared to the DLP, SLS, SLA, and PolyJet techniques. The FDM approach showed higher fatigue durability performance than the 3D-printed SPA developed by projection SLA (Peele et al. 2015). SLA is not the best method in terms of achieving the minimum wall thickness, which hinders its capability for achieving higher bending deflection and blocking force. However, the SLA method has shown significant performance in the fabrication of high-resolution 3D/4D-printed SPAs despite its weakness in durability and limited life-cycle. This method, also, is suggested to be suitable for the actuators with self-healing properties. The SPAs made by the SLS method have shown higher strength compared to other 3D printing techniques but were not promising in the design of various complex geometries due to the purging difficulty of the chamber at the end of printing. Besides, the materials used in SLS are not elastomers but thermoplastics that could yield and plastically deform under bending. The PolyJet method has featured capability of multi-material, functionally graded, and glossy surface finish printing at a higher cost than DIW and FDM while suffering from poor mechanical properties compared with the FDM or SLS. The DLP is confirmed as the method of choice for miniaturized highly stretchable 3D/4D-printed micro SPAs, however, is not suitable for large volume and longer life-cycle SPA applications.
| 3D printer | Pros and Cons | Material | Reference |
|------------|---------------|----------|-----------|
| FDM        | +Inexpensive materials and printers | TPU NinjaFlex (NinjaTek, PA) | (Yap, Ng, and Yeow 2016) |
|            | +Commercial filaments | TPU (eSUeNeFlex, Shenzhen Esun Industrial Co., Ltd) | (Irawan, Ritonga, and Prastowo 2019) |
|            | -Limited to few filaments | TPU NinjaFlex (NinjaTek, PA) | (Rosalia, Ang, and Yeow 2018) |
|            | -Rough surface finish | TPU NinjaFlex (NinjaTek, PA) | (Low et al. 2017) |
|            |                         | Silicone (Dow Corning® 737) | (Keong and Hua 2018) |
|            |                         | EcoFlex 00-30 (Smooth-On) | (Plott and Shih 2017) |
|            |                         | Filaflex (Recreus) | (Morrow, Hemleben, and Menguc 2016) |
|            |                         | TPU NinjaFlex (NinjaTek, PA) | (Anver, Mutlu, and Alici 2017) |
|            |                         | TPU NinjaFlex (NinjaTek, PA) | (Yap, Ng, and Yeow 2016) |
|            |                         | TPU NinjaFlex (NinjaTek, PA) | (Irawan, Ritonga, and Prastowo 2019) |
|            |                         | TPU NinjaFlex (NinjaTek, PA) | (Rosalia, Ang, and Yeow 2018) |
|            |                         | Low resolution | (Low et al. 2017) |
|            |                         | Silicone (Ecoflex 00-30 A, Dragonskin 30A, and Sylgard 184) | (Schaffner et al. 2018) |
|            |                         | Silicone (Dragon Skin 10, Smooth-On Inc., Macungie, PA) | (Byrne et al. 2018) |
|            |                         | TPE (Ninjaflex, ink3D.ie, Dublin) | (Schaffner et al. 2018) |
|            |                         | Kraton GI657 (SEBS, Kraton Corporation, USA) | (Khondoker and Sameoto 2019) |
|            |                         | MM3520 (SMP Technologies Inc., Japan) | (Khondoker and Sameoto 2019) |
| DLP        | +Fast prototyping | Tangoplus FLX 930 and Rhodamine B | (Ge et al. 2018) |
|            | -Void formation | EAA and AUD | (Patel et al. 2017) |
|            | -Small print volume | TangoPlus, EAA and AUD | (Hingorani et al. 2019) |
|            |                         | TangoPlus and Ebecryl 113 | (Zhang, Ng, et al. 2019) |
| SLA        | +Adding fillers | Elastomeric precursor (Spot-E resin, Spot-A Materials, Inc.) | (Peele et al. 2015) |
|            | +High resolution | PNIPAm and PAAm | (Mishra et al. 2020) |
|            | -Small print volume | PDMS | (Wallin et al. 2017) |
| SLS        | +High strength | Polyurethane-TPU92A-1 | (Scharff et al. 2017) |
|            | -Difficult purging | PA12 (HP 3D Printer) | (Lau 2019) |
|            | -Shape constraints | PA12 (HP 3D Printer) | (Lau 2019) |
| MJF        | +Fast and high resolution | Tangle Black (Stratasys, Co., Ltd.) | (Zhu et al. 2018) |
|            | -Limited materials | Tango Black+ and Tango+ (Stratasys Co., Ltd.) | (Drotman et al. 2018) |
|            |                         | Tangleplus and VeroBlue (Stratasys, Co., Ltd.) | (Wang, Torigoe, and Hirai 2017) |
|            |                         | TangoBlack+ and VeroWhite (Stratasys, Co., Ltd.) | (Wang, Chathuranga, and Hirai 2016) |
|            |                         | VeroWhite+ and Agilus30 (Stratasys, Co., Ltd.) | (Du Pasquier et al. 2019) |
| PolyJet    | +Fast and high resolution | AR-G1L (Agilista, Keyence, Japan) | (Zhang, Zhu, et al. 2017) |
|            | -Poor mechanical properties | VeroClear (J750, Stratasys Ltd.) | (Zhang, Zhang, et al. 2019) |
3. Modeling of 3D/4D-printed bending-type soft pneumatic actuators

The two main types of bending-type SPAs are identified in the literature. The first group is made by one, or even grouping of two or three of antagonistic fiber-reinforced chambers that control the bending of the actuators through pressure difference between the chambers also called tubular fiber-reinforced actuators (Connolly, Walsh, and Bertoldi 2017; Zhou, Chen, and Wang 2017). However, the second group is designed based on pressurizing air chambers formed by an asymmetric cross-section, with the inextensible bottom layer and an extensible top layer, which converts the pressure change into bending toward the side with the higher bending stiffness, known as bellow-type SPAs (Tawk, Gao, et al. 2019). The pneumatic chambers introduced in these SPAs can protect the walls from excessive deformation and thus induce the development of reliability against failure in higher input pressure. The bellow-type SPAs have been mainly focused in 4D printing due to several reasons (Drotman et al. 2018; Yap, Ng, and Yeow 2016); for creating rapid motions by unfolding the bellows, undergoing less radial expansion, which in turn minimizes failure and improves the durability, achieving full bending at lower pressures, and higher speed.

The FEA approaches have been broadly used for simulating and modeling the SPA’s kinematics and dynamics, but, the computational burden associated with these methods to achieve accurate results is always a matter of disputation that does not deter the researchers from exploring the analytical models first. Hence, in this study too, the analytical modeling and underlying mechanics of 3D/4D-printed bending-type SPAs are initially presented.

3.1. Analytical kinematic model

There are have been several analytical modelings of 3D/4D-printed SPAs developed in the literature. A principal strain field method was developed to realize the target deformation of SPAs (Ding et al. 2019). The heuristic approach utilized in the study could be more beneficial in 3D/4D-printed SPAs where material distribution was incorporated into the optimization of the constraints of the pneumatic chambers to achieve the target deformation. An analytical model of a three-chambered bellow-type actuator, including the forward and inverse kinematics, was also developed to analyze the extended motion of such actuators in 3D space rather than the planar model (Drotman et al. 2018). A rapid kinematic modeling of microtube SPA was also developed based on the line-segment model and the multi-segment Euler-Bernoulli’s beam model with the claimed less computational burden than the FEA (Ji et al. 2019).

Among all the analytical models developed for relating the input pressure to the bending deflection of the SPAs, a straight forward model based on Euler-Bernoulli is presented here. Assuming the SPA has a uniform deformation under pressure input, the bending model shown in Fig. 4(a) could be developed (Zhong, Hou, and Dou 2019). Thus, the geometric relationship could be defined as follows:

\[
\alpha = \frac{\beta}{2}, \quad \beta = \frac{L}{R}, \quad L = L_0 + \Delta L
\]

where \(\alpha\) is the bending angle under pressure input, \(\beta\) is the central angle of the actuator arc, \(R\) is the bending radius, \(L\) is the axial length of the upper finger after deformation, \(\Delta L\) is the growth of the upper side, and \(M_i\) is the bending moment generated by input air. Referring to the Euler-Bernoulli law:
\[
\frac{M_i}{EI} = \frac{1}{R}
\]
(2)

where E and I are the modulus of elasticity and the second moment of area of the actuator’s cross-section, respectively. The corresponding force of the input pressure (P) that acts on the internal surfaces of the chamber is:

\[
F_i = PA_i
\]
(3)

where \(A_i\) is the cross-sectional area of the actuator. The axial elongation, \(\Delta L\), of the top surface generated by \(F_i\) can be obtained as:

\[
\Delta L = \frac{F_iL_s}{EA_c} = \frac{PA_iL_s}{EA_c}
\]
(4)

where \(L_s\) is the length of the chamber and the distance between adjacent chambers. The moment of the entire SPA produced by input pressure, acts into two different cross-sectional areas, as shown in Fig. 4(b). \(O\) is the location of the cavity centroid, \(N\) is the neutral axis location of the cross-section, and \(h_i\) is the effective distance between points \(O\) and \(N\). The internal compressed air acts on the point \(O\) generates a bending moment \(M_i\) to bend the actuator toward the bottom part at point \(N\). Thus, by combining formulas (1)-(4), the relationship between the bending angle \(\alpha\) and the input pressure value \(P\) could be calculated as:

\[
\alpha = \frac{L_0 + \Delta L}{2R} = \frac{A_i^2h_iL_s}{2E^2IA_c} p^2 + \frac{A_ih_iL_0}{2EI} p \\
= mp^2 + np
\]
(5)

where \(m\) and \(n\) could be attained via curve fitting from experimental data.

**Fig. 4.** (a) Bending angle of a 3D/4D-printed SPA (b) Cross-section view of the single and adjacent chambers. Reproduced from (Zhong, Hou, and Dou 2019) with the permission of Elsevier.

Kinematic modeling of SPA resembles a flexible manipulator with many degrees of freedom (DOF) and continuous deformation. Therefore, a simplified method based on the discrete rigid elements and transformation matrices were applied with acceptable accuracy (Zolfagharian et al. 2018; Zhong, Hou, and Dou 2019). Having calculated the bending angle of the actuator
corresponding to the input air pressure, the kinematic model of the actuator could be derived to find the deformation of the whole body. A simplified model could divide the actuator into \( q \) equal rigid links assuming a uniform pressure along with the pneumatic chambers and constant distances in the circular arc direction between the adjacent joints surface during deformation. Since the curvature mainly occurs in the gap between neighboring chambers, the joints surfaces are assumed at the midpoint between the adjacent chambers (Zhong, Hou, and Dou 2019).

\[ \phi_{ij} = \theta_i, \quad L_i = \frac{2S\sin\left(\frac{\phi_{ij}}{2}\right)}{\phi_{ij}} \]  \hfill (6)

Using the transformation matrices:

\[ ^{j-1}T_j = ^{0}T_1^{1}T_2^{j-1}T_j \]  \hfill (7)

where

\[ j^{-1}T_j = \begin{bmatrix} [R_{\theta_j}]_{(3\times3)} & [P]_{(3\times1)} \\ 0_{(3\times1)} & 1 \end{bmatrix} = \begin{bmatrix} \cos \theta_j & -\sin \theta_j & 0 & m_j \\ \sin \theta_j & \cos \theta_j & 0 & n_j \\ 0 & 0 & 1 & 0 \end{bmatrix}, \quad j = 1, \ldots, q \]  \hfill (8)

\( m_j \) and \( n_j \) are calculated as:

\[ m_j = \frac{S(\sin \theta_j)}{\theta_j}, \quad n_j = \frac{S(1-\cos \theta_j)}{\theta_j}, \quad j = 1, \ldots, q - 1. \]  \hfill (9)

Therefore, Eq. (8) could be rewritten as:

\[ j^{-1}T_j = [R_j \quad P_j \quad 0 \quad 1]^T \]  \hfill (10)

**Fig. 5.** Discrete rigid elements kinematic modeling of a 3D/4D-printed SPA.

The pneumatic actuator divided into \( q \) equal length 3D-printed soft chambers is shown in Fig. 5. From the simplified geometry shown in Fig. 5 the relationship between the arc length, \( S \), and the rigid link length of \( i^{th} \) chamber \( L_i \), is derived as:
where

\[ R_j = m_1 + \sum_{k=2}^{j-1} [m_k \cos(\theta_1 + \theta_2 + \cdots + \theta_k) - n_k \sin(\theta_1 + \theta_2 + \cdots + \theta_k)] \]

\[ P_j = n_1 + \sum_{k=2}^{j-1} [m_k \sin(\theta_1 + \theta_2 + \cdots + \theta_k) + n_k \cos(\theta_1 + \theta_2 + \cdots + \theta_k)] \]

\[ j = 3, \ldots, q. \] (11)

3.2. Geometrical parameters effects on the bending angle of soft pneumatic actuators

Bellow geometry is a key factor in characterizing the deflection of the SPAs that could be a luxury of 3D/4D-printed SPAs too. The common geometries of bellows and their analytical stiffness model for hard materials are broadly investigated in the past (highlighted in Fig. 6). However, more understanding of the relation between the SPA deflection and the bellow shape was revealed in recent studies (Lau 2019; Stano, Arleo, and Percoco 2020). Using both FEA and the experimental results, it was found that the U-shaped bellow outperformed the other geometries by far in terms of achieving the maximum deflection for the same input pressure (Lau 2019). The comparison results of the other bellow geometries were reported as:

\[ \delta_{U-shaped} > \delta_{Elliptical} > \delta_{Rectangular} > \delta_{Crimped-plates} > \delta_{S-shaped} > \delta_{Triangular} \]

(Lau 2019)

where \( \delta \) is the deflection of the SPA under the same input pressure.

In another study, different shapes of chambers were 3D printed and their effects on the bending angle of the SPAs were investigated (Stano, Arleo, and Percoco 2020). Experimental results revealed that the best bending performance was achieved by the R-type (highlighted in Fig. 7) design compared to others.

\[ \delta_R > \delta_S > \delta_D \cong \delta_B \]

(Stano, Arleo, and Percoco 2020)

The R- and S-type, respectively, exhibited the largest bending angles with little difference at the pressure range of 0-3 bar. However, the B- and D-type demonstrated smaller bending angles than R- and S-type. At pressures higher than 4 bar, however, the D-type out-raced the B-type. Generally, the authors related these different bending angles of the actuators to the alignment of the chamber walls with the airflow direction.
Fig. 6. Various geometries for linear bellow-type actuators, reproduced from (Wilson 1984) with permission of Elsevier.

Fig. 7. Different designs of 3D/4D-printed SPAs: (a) S-type, (b) B-type, (c) R-type, and (d) D-type, reproduced from (Stano, Arleo, and Percoco 2020) with permission of MDPI under the terms of the Creative Commons CC BY license.

Besides, the variation of SPAs deflection with the cross-section geometries was investigated (Hu et al. 2018). The comparison of results of the cross-section geometries was reported as:

\[ \delta_{\text{Honeycomb}} \equiv \delta_{\text{Rectangular}} \equiv \delta_{\text{Semi-circular}} > \delta_{\text{Circular}} \]

(Hu et al. 2018)

where \( \delta \) is the deflection of the SPA under the same input pressure. It was found that while the honeycomb, rectangular, and semi-circle cross-sections have led to the more or less the same
extent of deflection, the actuator with circular cross-section has been the last effective one in this regard.

The deflection of 3D/4D-printed SPAs is highly dependent on the design parameters of the chambers, including bellow gap, width, and wall thickness, and bottom layer thickness (Auysakul et al. 2020; Demir et al.; Sun et al. 2019). These relations have been studied earlier and the effects of these parameters are shown in Fig. 8 (Hu et al. 2018). It was observed that the deflection of the SPA has a parabolic correlation with bottom layer thickness. Also, it was shown that the deflection of the SPAs decreases with increasing the gap size and the wall thickness of chambers in the bellow. The wall thickness is a crucial variable in the design of 3D/4D-printed SPAs. A thin wall thickness leads to a lower life-cycle while a thick wall leads to a smaller bending angle under the same input pressure. Therefore, there should be a balanced design for an optimized value of the wall and bottom layer thickness to avoid the rupture while achieving the full bending of the SPAs. Therefore, simultaneous consideration of wall and bottom layer thickness is recommended at the design stage (Hu et al. 2018).

Fig. 8. The effects of different geometrical parameters on the bending angle of SPAs.

The effect of asymmetry on the bending of 3D/4D-printed SPAs was investigated (Dilibal, Sahin, and Celik 2018). It was found that the tapered design with gradually reduced height toward the tip, which bio-mimics the elephant trunk led to a more bending angle compared to non-tapered. It was also found that the height of the chamber could be optimized for the amount of material used to produce the same extent of deflection and tip force in the bellow type 3D/4D-printed SPA (Auysakul et al. 2020). The bending effects of SPAs under various cross-section ratios were investigated via non-linear FE simulations. The cross-section ratio was defined between the size of the first and last chamber width. It was reported that increasing the cross-section ratio increases the bending angle, conversely, a decrease in cross-section ratio results in significant bending angle reduction. The authors discussed that the cross-section ratio of SPAs could be optimized over the same length depending on the applications to obtain
optimal curvature for grasping different objects. A genetic algorithm (GA) optimization method was also used to find the optimum design of the actuator for the target task of grasping (Sun et al. 2019). A blend of analytical and FE modeling was proposed to design a SPA that matches the target trajectory by adjusting the design parameters (Sun et al. 2019).

### 3.3 Analytical blocking/tip force model

The effect of design parameters on the blocking/tip-force of 3D/4D-printed bending-type SPAs was investigated. The outcomes of the studies revealed that the decrease in both bellow wall thickness and sidewall thickness, as well as the increase in cross-sectional width, resulted in increased tip-force at the same input pressure (Yap, Ng, and Yeow 2016). The effect of the length of the 3D/4D-printed SPA on the blocking force at the tip was also proven to be directly proportional (Anver, Mutlu, and Alici 2017).

Besides, the effect of different design parameters, including width, length, bottom layer thickness, bellow wall thickness, number of chambers, and cross-section geometry (Anver, Mutlu, and Alici 2017) on the tip force of 3D/4D-printed SPAs was investigated (highlighted in Fig. 9). It was found that the tip force of the actuator increased with the increase of the width, length, and the number of chambers. However, the increase of the bottom layer thickness and bellow wall thickness reduce the tip force of the SPAs. Also, the variation of SPAs tip force with the cross-section geometries was investigated (Hu et al. 2018). The comparison results of the cross-section geometries were reported as follows:

\[ F_{\text{Triangle}} > F_{\text{Honeycom}} > F_{\text{Semi-circular}} \]

where \( F \) is the tip force of the SPA under the same input pressure.

---

**Fig. 9.** The effects of different geometrical parameters on the tip force of SPAs.

Also, it was reported that using the experimental measurement of the tip force the effective modulus of elasticity \( (EI) \) of the SPA could be found to later estimate the theoretical blocking/tip force of the SPA at different bending angles (Alici et al. 2018). Using (2) and (3), and knowing the flexural rigidity \( (EI) \) of the actuator at the given bending angle we have:
\[
\frac{M_B}{EI} = \frac{1}{R} = \frac{\theta}{L}
\]  

(12)

where \( M_B \) is the bending moment at the tip, \( R \) is the radius of curvature, \( L \) is the length of the actuator, and \( \theta \) is the bending angle. Knowing \( M_B = F_B L \), the blocking force or tip force of 3D/4D-printed SPAs could be theoretically written as:

\[
F_B = \frac{\theta EI}{L^2}
\]  

(13)

However, it is often impractical to find an accurate value of flexural rigidity for such systems, particularly for multi-material actuators (Alici et al. 2018). Therefore, usually, the experimental data is collected initially for flexural rigidity by rearranging (13) as:

\[
EI = \frac{L^2 F_B}{\theta}
\]  

(14)

Then the flexural rigidity will be used for tip force estimation.

4. Finite Element Analysis of 3D/4D-Printed Bending-type Soft Pneumatic Actuators

Hyperelastic materials with high flexibility and capability of withstanding large strains, such as silicone and thermoplastic elastomers, are the most common materials used in the fabrication of 3D/4D-printed SPAs (Moseley et al. 2016). These materials demonstrate rubber elasticity with quite large and reversible nonlinear deformation, several times of their initial length, under a relatively low force. Their mechanical behavior cannot be characterized by a constant elastic modulus (highlighted in Fig. 10). They possess incompressible characteristics, which makes them retain their overall volume under applied stress (Hu et al. 2018; Hu 2019). The mechanical behavior of hyperelastic materials is complex therefore warranting constitutive mathematical strain energy function models to be employed to predict their elastic behavior via tensile test experimental data (Rivlin 1948; Ogden 1972; Ponte Castaneda 1989; Gent 1996). To estimate the nonlinear large deformation of these materials using FEA various strain energy models were employed and compared (Drozdov 2007; Kim et al. 2012; Marckmann and Verron 2006). Yet, not a single best model was reported as the selection of the best model is subjective to the application, and the material used in the SPA. Isotopic hyperelasticity models, including, Arruda-Boyce (Arruda and Boyce 1993) and Blatz-Ko, (Blatz and Ko 1962) were developed based on the incompressible hyperelastic material response at the molecular scale, while other models, including Mooney-Rivlin (Rivlin 1948), Ogden (Ogden 1972), Neo-Hookean (Ponte Castaneda 1989), and Yeoh (Yeoh 1993) reflect the rubber-like behavior of these materials, known as extended-tube models. Further details of the comparison of these models are discussed in the following.
The energy is internally stored over the volume of a material element when it is deformed by an external load. This internal energy is related to material strain and is known as the strain-energy. Consider an object under tension, where a volume element of the object is subjected to uniaxial stress, \( \sigma \) (Galley, Knopf, and Kashkoush 2019). Assuming there is no energy loss, the stored strain energy, \( \Delta U(E) \) in the constant volume element could be calculated based on the external work as:

\[
\Delta U(E) = \frac{1}{2} \sigma \varepsilon \Delta V
\]  

(15)

where \( \varepsilon \) and \( \Delta V \) are the strain and volume change of element, respectively. Then, the strain energy density formula could be derived from (15) as:

\[
W(E) = \frac{\Delta U(E)}{\Delta V} = \frac{1}{2} \sigma \varepsilon
\]  

(16)

For a volume element subjected to three principal stresses, (16) could be rewritten such that each principal stress contributes a portion of the total strain-energy density as:

\[
W(E) = \frac{1}{2} \sigma_1 \varepsilon_1 + \frac{1}{2} \sigma_2 \varepsilon_2 + \frac{1}{2} \sigma_3 \varepsilon_3
\]  

(17)

Fig. 10. A schematic diagram of the difference in the stress-strain behavior between hyperelastic and linear elastic materials.

The hyperelastic nonlinear mechanical behavior of the elastomers commonly used in 3D/4D-printed SPAs are characterized in terms of strain energy density function by assuming the isotropic and incompressible behavior for rubber-like elastomers. Therefore, the strain energy density function, \( W(E) \), is dependent on strain invariants of Green deformation tensor, \( I_1, I_2, I_3 \), and is expressed as follows:

\[
W(E) = f(I_1, I_2, I_3)
\]  

(18)

where

\[
I_1 = \text{trace}(E) = \lambda_1^2 + \lambda_2^2 + \lambda_3^2
\]

\[
I_2 = \frac{1}{2} \left(\text{trace}(E)^2 + \text{trace}(E^2)\right) = \lambda_1^2 \lambda_2^2 + \lambda_2^2 \lambda_3^2 + \lambda_3^2 \lambda_1^2
\]
\[ I_3 = \det(E) = \lambda_1^2 \lambda_2^2 \lambda_3^2 \]

and

\[ \lambda_i = 1 + \epsilon_i \] (19)

The \( \lambda_1, \lambda_2, \lambda_3 \) are the principal stretch ratio of Cauchy-Green tensor, and \( \epsilon_i \) is the uniaxial strain. The strain-energy density function, \( W(E) \), in (17) is defined as a sum of two terms (Holzapfel 2010):

\[ W(E) = W_{iso}(\tilde{I}_1, \tilde{I}_2) + W_v(J) \] (20)

where the isochoric term, \( W_{iso} \), represents the energy needed to deform or distort the element while preserving volume, and the volumetric term, \( W_v \), represents the energy needed to change in volume of the element with no change in shape. Also, \( \tilde{I}_1 = I_1/J^2/3, \tilde{I}_2 = I_1/J^{4/3} \) and \( J = \sqrt{I_3} \) is the volume ratio for incompressible materials that is equal to 1.

The common strain energy formula utilized in FEA of SPAs are listed in Table 2, where \( C_{ij} \) and \( d_i \) are material constants related to shear and bulk moduli, respectively. The Yeoh model is a phenomenological model used for simulating large nonlinear deformation while fitting the mechanical behavior of other deformation modes, such as uniaxial compression and shear, according to the data of uniaxial tensile test (Yeoh 1993). The Yeoh model is founded on the negligible influence of strain tensor invariants \( I_2 \) on the strain energy for nearly incompressible materials. The Mooney-Rivlin model is one of the most popular strain energy density models that could be used for fitting the nonlinear stress-strain curves of a broad range of hyperelastic materials based on the principal strain invariants in two, three, five or nine parameter models (Mooney 1940). The Ogden model is developed and used to fit the non-linear stress-strain behavior of large strain materials like biological tissue based on three principal stretches where \( \tilde{\lambda}_i = J^{-1/3} \lambda_i \), and \( \mu_i \) and \( \alpha_i \) are temperature-dependent parameters of materials. The measurability of the principal stretches in Ogden is deemed its advantage over the Mooney-Rivlin model. The Neo-Hookean model is a particular case of the Ogden model by limiting the number of terms in strain energy function to 1 and the fitting parameter \( \alpha_i = 2 \) (Ponte Castaneda 1989). This model is used to fit into nonlinear materials with small strains where \( \mu \) is the initial shear modulus of the material and \( d \) is the material incompressibility parameter. The polynomial model is a phenomenological hyperelastic material model suitable for describing the behavior of filled elastomers (Forni, Martelli, and Dusi 1999). The Arruda-Boyce, also known as the eight-chain model, was developed based on the evaluation of a cubic volume element with eight chains and is another suitable model for incompressible elastomeric materials (Arruda and Boyce 1993; Boyce 1996). The Blatz and Ko is a compressible model developed for finite strain modeling of more foam-like rubbery materials (Blatz and Ko 1962).

Given the nature of 3D printing, the actuators could show anisotropic properties. Therefore, material properties, like Young’s modulus and Poisson’s ratio of 3D-printed dumbbell test specimens in different directions are commonly characterized using a uniaxial tensile test for FEA. Expectedly, the specimens printed longitudinally demonstrate the highest stress, while the transverse printed specimens experienced the lowest stress. In several studies, only the longitudinal tests results were used for the constitutive model fitting of hyperelastic materials since it was justified that in the bellow-type pneumatic actuators the majority of the strains
occurred in the longitudinal direction of the bellows of the actuators during actuation (Yap, Ng, and Yeow 2016). Then the curve fitting methods (highlighted in Fig. 11) available in FE packages, such as ANSYS and ABAQUS, are employed to find the material constants from the stress-strain experimental data to characterize nonlinear behavior of hyperelastic materials in 3D/4D-printed SPAs (highlighted in Figs. 11 and 12).

**Table 2.** Energy model formula applied for FEA of 3D/4D-printed SPAs.

| Energy Model                  | Formula                                                                                                                                 |
|-------------------------------|----------------------------------------------------------------------------------------------------------------------------------------|
| Yeoh (Yeoh 1993)              | $W = \sum_{i=1}^{3} C_{i0} (I_1 - 3)^i + \sum_{i=1}^{3} \frac{1}{d_i} (J - 1)^{2i}$  
Two-parameter incompressible material model: $W = C_{10} (I_1 - 3) + C_{20} (I_1 - 3)^2$ |
| Mooney-Rivlin (Mooney 1940)   | $W = \sum_{i,j=0}^{N} C_{ij} (I_1 - 3)^i (I_2 - 3)^j + \sum_{i=1}^{N} \frac{1}{d_i} (J - 1)^{2i}$  
Two-parameter incompressible material model: $W = C_{10} (I_1 - 3) + C_{01} (I_2 - 3)$  
Three-parameter incompressible material model: $W = C_{10} (I_1 - 3) + C_{01} (I_2 - 3) + C_{11} (I_1 - 3) (I_2 - 3)$  
Five-parameter incompressible material model: $W = C_{10} (I_1 - 3) + C_{01} (I_2 - 3) + C_{20} (I_1 - 3)^2 + C_{11} (I_1 - 3) (I_2 - 3) + C_{02} (I_2 - 3)^2$  
Nine-parameter incompressible material model: $W = C_{10} (I_1 - 3) + C_{01} (I_2 - 3) + C_{20} (I_1 - 3)^2 + C_{11} (I_1 - 3) (I_2 - 3) + C_{02} (I_2 - 3)^2 + C_{03} (I_2 - 3)^3$ |
| Polynomial (Forni, Martelli, and Dusi 1999) | $W = \sum_{i+j=1}^{N} C_{ij} (I_1 - 3)^i (I_2 - 3)^j + \sum_{i=1}^{N} \frac{1}{d_i} (J - 1)^{2i}$ |
| Ogden (Ogden 1972)            | $W = \sum_{i=1}^{N} \frac{2\mu_i}{d_i^2} \cdot (\lambda_1^{\alpha_i} + \lambda_2^{\alpha_i} + \lambda_3^{\alpha_i} - 3) + \sum_{i=1}^{N} \frac{1}{d_i} (J - 1)^{2i}$ |
| Neo-Hookean (Ponte Castaneda 1989) | $W = \frac{\mu}{2} (\lambda_1^2 + \lambda_2^2 + \lambda_3^2 - 3) + \frac{1}{d} (J - 1)^2$ |
| Arruda-Boyce (Arruda and Boyce 1993; Boyce 1996) | $W = \mu \left( \frac{I_1}{2} (I_1 - 3) + \frac{1}{20\lambda_1^2} (I_2^2 - 9) + \frac{11}{1050\lambda_1^2} (I_1^3 - 27) + \frac{19}{7000\lambda_1^2} (I_1^4 - 81) + \frac{590}{673750\lambda_1^2} (I_1^5 - 243) \right) + \frac{1}{d} \left( \frac{J^2 - 1}{2} - \ln J \right)$ |
| Blatz and Ko (Blatz and Ko 1962) | $W = \frac{\mu}{2} \left( \frac{I_2}{I_3} + 2\sqrt{I_3 - 5} \right)$ |
A list of different constitutive models used in the FEA of 3D/4D-printed SPAs in terms of different materials is compiled in Table 3. A comparative study of experimental and FEA results, including the Ogden, Yeoh, Mooney Rivlin, and Arruda-Boyce models demonstrated the outperformance of the Ogden model for the actuator made from FDM 3D-printed TPU filament (Yap, Ng, and Yeow 2016). In another study, where the four hyperelastic models, Arruda-Boyce, Neo-Hookean, Yeoh, Mooney-Rivlin, and Ogden utilized for the simulation of a 3D/4D-printed SPA using a thermoplastic elastomer, FilaFlex, it was reported that the Mooney-Rivlin model outperformed others (Hu 2019). The authors attributed the superior performance of the model to its ability to almost perfectly fit the experimental stress-strain curve with the smallest residual value. The combinations of the strain energy density function models were also utilized for the modeling of a composite 3D/4D-printed SPA where it was reported that the Ogden model was fitted for Dragon Skin-10 (Byrne et al. 2018) while the Polynomial model was selected for TPE (Ninjaflex, ink3D.ie, Dublin).

In a recent study, a new FEA method called “design and fabrication in the loop” was introduced to avoid extensive material tensile tests required for modelling the bending-type SPAs (Irawan, Ritonga, and Prastowo 2019) (highlighted in Fig. 12). The first order Yeoh model was employed with a focus on selecting the appropriate value of $C_{10}$ to obtain a closer prediction of experimental results. It was reported that the model and value of $C_{10}$ could not predict the behavior of SPAs with low deflections while the results were more accurate for bending angles
more than 130°. A 3rd order Yeoh model was also successfully implemented for the bending modeling of TPU made 3D/4D-printed SPA (Rosalia, Ang, and Yeow 2018). Different material models, including Mooney-Rivlin, Neo-Hookean, and Ogden were developed to obtain maximum consistency with experimental results of an additively manufactured SPA made of TPU (Dilibal, Sahin, and Celik 2018). It was reported that the Ogden material model predicted the closest result to the experimental bending motion of the SPA compared to the others in that study.

For modeling of a 3D/4D-printed SPA made from TangoBlack material, a three-parameter Mooney-Rivlin model was adopted to simulate the nonlinear elasticity. The model successfully implemented to identify the coefficients through the experimental results of plane strain tension tests. A 5-parameter Mooney-Rivlin model was also successfully utilized in ANSYS for simulating both bending angle and blocking/tip force of a fin-ray printed SPA made of NinjaFlex (Tawk, Gao, et al. 2019). Tetrahedral mesh elements were used in the study by defining the contact pair between the adjacent walls during the blocking/tip force simulation. Adding the passive fin-ray structure to the design was confirmed to improve the gripping capabilities of the gripper via both FEA and experiment results. The Mooney-Rivlin was also successfully used for FEA of 3D/4D-printed SPAs made via DLP technology (Zhang, Ng, et al. 2019) (Hingorani et al. 2019).

Overall, there is not one recipe serve all Energy models that could be recommended for FEA of the 3D/4D-printed SPAs. However, here we have summarized our investigations in terms of different models successfully achieved in terms of various hyperelastic materials used in the fabrications of these SPAs in Table 3. It is also shown that the Ogden has worked better than others in the FDM 3D-printed TPU filament SPA (Yap, Ng, and Yeow 2016) the first order fitting model of Yeoh was not successful in predicting the bending angle of less than 130° with the same material. Ogden has also modeled the SPAs made from Dragon Skin-10 (Byrne et al. 2018) while the Polynomial model perfectly worked for TPE (Ninjaflex, ink3D.ie, Dublin). Also, Mooney-Rivlin was the model that outperformed others for the FilaFlex (Hu 2019).

**Fig. 12.** The FEA of 3D/4D-printed SPAs with a different design, reproduced from (Irawan, Ritonga, and Prastowo 2019) with the permission of Elsevier.
Table 3. The FEA models used for 4D printing bending-type SPAs.

| Model                | FE Platform | Materials                                      | Reference                                      |
|----------------------|-------------|-----------------------------------------------|-----------------------------------------------|
| Mooney–Rivlin        | ABAQUS      | EAA and AUD                                   | (Patel et al. 2017)                           |
| Mooney–Rivlin        | ABAQUS      | TPU, NinjaFlex (NinjaTek, PA)                 | (Yap, Ng, and Yeow 2016)                      |
| Mooney–Rivlin        | ABAQUS      | TangoPlus and Ebecryl 113                     | (Zhang, Ng, et al. 2019)                      |
| Mooney–Rivlin        | ABAQUS      | TangoPlus, EAA and AUD                       | (Hingorani et al. 2019)                       |
| Mooney–Rivlin        | ANSYS       | Tangle Black (Connex3 Object350 Stratasys, Co., Ltd.) | (Wang, Ge, et al. 2017)                      |
| Mooney–Rivlin        | ANSYS       | TPU, NinjaFlex (NinjaTek, PA)                 | (Tawk, Gao, et al. 2019)                      |
| Mooney–Rivlin        | Marc Mentat | TPU                                           | (Dilibal, Sahin, and Celik 2018)              |
| Neo-Hookean          | ABAQUS      | Tangleoplus FLX 930 and Rhodamine B           | (Ge et al. 2018)                              |
| Neo-Hookean          | ABAQUS      | RTV-2 silicone rubber and PA12 nylon          | (Ding et al. 2019)                            |
| Neo-Hookean          | Marc Mentat | TPU                                           | (Dilibal, Sahin, and Celik 2018)              |
| Linear               | ABAQUS      | TPU (Ninjaflex, ink3D.ie, Dublin)             | (Yap, Ng, and Yeow 2016)                      |
| Linear               | ABAQUS      | TPE and Dragon Skin-10                        | (Byrne et al. 2018)                           |
| Linear               | ABAQUS      | VeroWhite+ and Agilus30 (Stratasys, Co., Ltd.)| (Du Pasquier et al. 2019)                     |
| Yeoh                 | ANSYS       | TPU (eSUNEflex, Shenzhen Esun Industrial Co., Ltd.) | (Irawan, Ritonga, and Prastowo 2019)         |
| Yeoh                 | ABAQUS      | TPU, NinjaFlex (NinjaTek, PA)                 | (Yap, Ng, and Yeow 2016)                      |
| Yeoh                 | ABAQUS      | TPU, NinjaFlex (NinjaTek, PA)                 | (Rosalia, Ang, and Yeow 2018)                |
| Yeoh                 | ABAQUS      | TPU, NinjaFlex (NinjaTek, PA)                 | (Keong and Hua 2018)                          |
| Yeoh                 | ABAQUS      | Silicone (Keyence© Agilista 3200®)            | (Manns, Morales, and Frohn 2018)             |
| Ogden                | ABAQUS      | TPU, NinjaFlex (NinjaTek, PA)                 | (Yap, Ng, and Yeow 2016)                      |
| Ogden                | ABAQUS      | Silicone (Dragon Skin 10, Smooth-On Inc., Macungie, PA) | (Byrne et al. 2018)                           |
| Ogden                | ABAQUS      | TPU (NinjaFlex, NinjaTek)                     | (Hainsworth et al. 2020)                      |
| Ogden                | Marc Mentat | TPU                                           | (Dilibal, Sahin, and Celik 2018)              |
| Arruda–Boyce         | ABAQUS      | TPU, NinjaFlex (NinjaTek, PA)                 | (Yap, Ng, and Yeow 2016)                      |
5. Control of 4D-printed Bending-type Soft Pneumatic Actuators

5.1. Integration of Sensors

The inherent flexibility and compliance morphology of 3D/4D-printed SPAs require the integration of non-conventional sensors for their control. Thus, there have been investigations on the development of stretchable curvature sensors with minimal impact on the compliance of SPAs. However, due to the nonlinear behavior of the elastomeric materials in different environmental conditions, such as temperature and humidity changes, other types of chemical and biological sensors are required too. Feedforward and feedback controllers were applied for the control of 3D/4D-printed SPAs (George Thuruthel et al. 2018). Providing feedback information required for closed-loop control of SPAs demand availability of sensory feedback instruments that could be realized either using external measurement devices, such as camera (Marchese, Katzschmann, and Rus 2014) electromagnetic sensor (Wang et al. 2014), optical sensor (Zhuang et al. 2018; Darzi and Park 2017) or integrated flexible sensors (Khosravani and Reinicke 2020a) that do not compromise the conformability of the SPAs (Low et al. 2017) (Elgeneidy et al. 2018).

To facilitate the use of 3D/4D-printed SPAs in real-world applications, curvature or strain sensing is required in the closed-loop control algorithm for measuring the bending. The curvature sensors were integrated into 3D/4D-printed SPAs for grasping and trajectory tracking of the actuators during bending. These sensors have been fabricated via various 3D printing approaches, such as DIW, FDM, and PolyJet, to be directly integrated into the SPAs. The integrated flexible sensors could be in the form of adding conductive fillers such as carbon nanotube (CNT) (Giffney et al. 2016) and multi-walled carbon nanotube (MWCNT) (Lee et al. 2018) to elastomer materials with the possibility of 3D printing. To find more understanding of the grasping dynamics between a SPA gripper and deformable objects, a curvature resistive sensor (Spectra Symbol) was integrated to the bottom of the gripper (Wang and Hirai 2016).

The slippage detection of the object during lift was achieved using the inserted flexible sensor. An integrated sensor for 3D/4D-printed SPA was directly fabricated using a multi-material 3D printer (Objet350, Stratasys Ltd., USA) and rubber-like, AgilusBlack, material for both actuation and self-power triboelectric curvature sensing (Zhu et al. 2020). The sensor was reported to measure a curvature up to 8.2 m−1 in a low-frequency rate of 0.06 Hz. A flexible sensor was directly 3D-printed and embedded into soft pneumatic gripper to enhance its both exteroceptive and interoceptive capabilities (Shih et al. 2019). The resistive sensor was co-fabricated with the soft gripper using a commercial Connex3 Objet350 multi-material 3D printer and directly integrated into a pneumatic gripper. The black resin containing carbon particles was used to produce conductivity required for the sensor traces. The tests demonstrated the capability of the sensor to differentiate between objects after grasping by the actuator.

To extend the capabilities of SPAs, tactile force-sensing could be employed for closed-loop control of SPAs for safe manipulation, shape recognition, texture Discrimination, and grasping in diverse applications (Sonar et al. 2020; Zhou et al. 2020). However, the state-of-the-art is to entirely automate the integration of sensors and actuators using readily available 3D printers (Hohimer et al. 2020; Elgeneidy et al. 2018).
Multiple haptic capabilities, including thermoceptive and proprioceptive sensing, were simultaneously embedded in a 3D/4D-printed somatosensitive SPA (Truby et al. 2018). Conductive ionogel was used as conductive ink showing an acceptable level of longevity and low hysteresis (Truby et al. 2019; Truby et al. 2018; Zolfagharian, Kaynak, and Kouzani 2019). An ionically conductive hydrogel was one of the earliest sensors made by the DIW technique for measuring the tactile external stimuli based on the capacitive principle (Robinson et al. 2015). The so-called capacitive skin was able to detect a compressive force of 2 N for feedback control purposes. In another study, an inexpensive, flexible force sensor was devised for measuring the grasping forces exerted on the actuators to provide feedback information (Low et al. 2017). The flexible force sensor was made of a composite of electrodes and piezoresistive fabric (LW-SLPA, Eeonyx, CA) through printing conductive ink on the polyethylene substrate (AgIC, Japan). A self-sensing SPA was developed by common FDM technology and using two materials, TPU (NinjaFlex, NinjaTek) and ProtoPasta, which is carbon black (CB) doped polylactic acid (PLA), with no human intervention during the fabrication (Hainsworth et al. 2020). The actuator has shown acceptable compliance for grasping while providing feedback information. In other studies, both pressure and position sensors were integrated into SPAs made of TPU (Yang and Chen 2017). The sensing principle was based on the volume resistivity changes of conductive elastomers made by the addition of CB conductive fillers to TPU.

The embedded strain sensors made of liquid metals, such as eutectic gallium–indium (EGaIn), are also common in highly compliant soft gripper applications where extremely high deformations accompanying actuation can damage conventional sensing devices such as strain gauges (Fang et al. 2019; White, Case, and Kramer 2017). The optical Fiber Bragg Grating (FBG) sensors could also be used for imparting tactile capability in SPAs (Bogue 2016; He, Zhu, et al. 2018) due to their thin geometry, low hysteresis, and high speed and robustness. These sensors detect strain by measuring shifts in the wavelength of the reflected light. But, their drawback is limitations in large deformations. The Hall Effect magnetic field sensors have been developed by embedding the magnetic particles into soft materials, such as silicon. These types of sensors could be suitable for 3D/4D-printed SPAs due to their remote sensing of curvature (Ozel et al. 2016; Ozel et al. 2015) as well as accurate contact force measurements (Mirzanejad and Agheli 2019; Wang et al. 2016).

Environmental sensors for measuring the temperature (Yamaguchi, Kashiwagi, et al. 2019), humidity (Maldonado et al. 2019), and other chemical substances (Raman, Cvetkovic, and Bashir 2017) could be integrated to 3D/4D-printed SPAs for the purposes, such as stiffness variable adjustments and control of uncertain conditions.

Different types of soft sensors suitable for 3D/4D-printed bending-type SPAs are listed in Table 4. The selection criteria of the sensors could be varied based on different applications. However, in general, the DIW and FDM printers have shown superior performance due to resistive and capacitive sensors being directly 3D-printed and integrated to the SPAs and also allowing for the use of a wide range of materials and composites. The DIW of conductive ionogel has shown promising longevity and low hysteresis performance. The strain sensors 3D-printed by EGaIn are mainly suitable for extremely high deformations actuation. The FBG sensors, though needing further assembly requirements, are low in hysteresis and have robust functionalities. Also, the Hall Effect magnetic field sensors are highly accurate for contact force measurements for remote sensing capability.
Fig. 13. Integrating sensors into 3D/4D-printed SPAs (a) conductive filler Polyjet 3D-printing, reproduced from (Shih et al. 2019) with permission of Frontiers under the terms of the Creative Commons CC BY license; (b) conductive filler FDM 3D printing, reproduced from (Elgeneidy et al. 2018) with permission of Frontiers under the terms of the Creative Commons CC BY license; (c) liquid metal DIW 3D printing (the scale is 6.25 mm), reproduced from (White, Case, and Kramer 2017) with permission of Elsevier; (d) soft magnetic force sensor DIW 3D printing, reproduced from (Mirzanejad and Agheli 2019) with permission of Elsevier.
Table 4. Different types of soft sensors suitable for 3D/4D-printed bending-type SPAs.

| Types                  | Applications                                      | Mechanisms                                      | Materials                          |
|------------------------|---------------------------------------------------|-------------------------------------------------|------------------------------------|
| Curvature/Strain        | Grasping, Trajectory tracking                     | Capacitive (Frutiger et al. 2015)               | Silicone                           |
|                        |                                                   | Resistive (Eijking, Sanders, and Krijnen 2017)   | TPU                               |
|                        |                                                   | Resistive (Elgeneidy et al. 2018)                | TPU/PLA                           |
|                        |                                                   | Resistive (Yang and Chen 2017)                  | TPU/CB                            |
|                        |                                                   | Liquid metal (White, Case, and Kramer 2017)     | Magnetite/ABS                      |
|                        |                                                   | Liquid metal (Fang et al. 2019; Yuan et al. 2019)| EGaIn/Ecoflex0050                 |
|                        |                                                   | Hall effect (van Tiem et al. 2015)              | Magnet/plastic laminate            |
|                        |                                                   | Hall effect (Ozel et al. 2016; Ozel et al. 2015)| Magnet/silicone                    |
|                        |                                                   | Optical waveguide (Wolfer et al. 2016)          | InkOrmo/InkEpo                     |
|                        |                                                   | Optical FBG (Wang et al. 2019)                  | Polyimide                          |
|                        |                                                   | Eddy current (Wallin, Pikul, and Shepherd 2018;| Copper/ABS                         |
|                        |                                                   | Jeranče, Bednar, and Stojanović 2013; Li et al. 2018) |                      |
| Tactile Force           | Safe manipulation, Shape sensing, Texture Discrimination, Different shapes grasping | Capacitive (Laszczak et al. 2015) (Robinson et al. 2015) | Ionic gel                          |
|                        |                                                   | Capacitive (Ou et al. 2016)                     | TPU                               |
|                        |                                                   | Resistive (Lee et al. 2018)                     | Tango+/MWCNT                      |
|                        |                                                   | Resistive (Yamaguchi, Arie, et al. 2019)        | Ag/conductive thread              |
|                        |                                                   | Piezoelectric (Yoshida et al. 2018)             | Tango Black                       |
|                        |                                                   | Piezo resistive (Mousavi et al. 2018)           | Cilia                             |
|                        |                                                   | Piezo resistive (Sankar et al. 2019)            | Fabric                            |
|                        |                                                   | Liquid metal (Lopes et al. 2018) (Fang et al. 2019) | EGaIn                         |
|                        |                                                   | Hall effect (Mirzanejad and Agheli 2019; Wang et al. 2016) | ABS/magnet                     |
|                        |                                                   | Optical FBG (Lin et al. 2016)                   | ABS/FBG                           |
| Temperature            | Variable stiffness                                | Capacitive (Wickberg et al. 2015)               | Nanocrystals                      |
|                        |                                                   | Thermistor (Yamaguchi, Kashiwagi, et al. 2019)   | Polyethylene terephthalate        |
| Humidity               | Classification                                    | Solvatochromic (Maldonado et al. 2019)         | 1D coordination polymer           |
| Environmental          | Detection                                         | Electrochemical (Raman, Cvetkovic, and Bashir 2017) | PEGDA                             |
|                        |                                                   | Electrochemical (Gaál et al. 2018)              | Graphene/PLA                      |
5.2. **Data-driven machine learning modeling and control**

The conventional approaches used for analytical kinematic modeling of 3D/4D-printed SPAs, including the piecewise constant curvature (PCC) (Webster III and Jones 2010), and other discrete rigid elements models (Zolfagharian et al. 2018; Zhong, Hou, and Dou 2019) were developed based on assumptions that are only valid for specific simplified designs of the actuators mainly used in the structured environments. However, these models are not favorable for dealing with the nonlinearity and time-variable parameters associated with 3D/4D-printed SPAs in their practical applications in unstructured environments. The FEA also has some intrinsic drawbacks, such as imprecise constitutive law of hyperelastic materials and computational cost which are unsatisfactory for the controller design. Therefore, the use of machine learning techniques could be a more effective and reasonable choice for kinematic modeling of these systems.

The dynamics modeling of SPAs is even more complex than kinematics where data-driven modeling could be applied for learning dynamic models (Thuruthel et al. 2018; Zolfagharian et al. 2020; Zolfagharian, Kaynak, and Kouzani 2019). To include nonlinearity and hysteresis that occur in unconstrained dynamic environments into the design of 3D/4D-printed SPAs, the constitutive law of material behavior, particularly a modified Kelvin–Voigt, model was incorporated into dynamic modeling to embody the visco-hyperelasticity of SPAs (Mustaza et al. 2019). The proposed model was validated using experimental data for accurately reflecting the nonlinear and hysteresis behavior of the SPA, which could be used for model-based feedback control.

The data-driven machine learning approach was also previously used for modeling the nonlinearity of the SPAs arising from variation in solenoid valve flow rates during pressurization and depressurization (Mohamed et al. 2020; Mosadegh et al. 2014). Such nonlinearity in addition to the multi-material combination in the manufacturing, and effects of other embedded components in the body of SPAs, could not be addressed merely by FEA, thus causing difficulty in the accurate bending control of 3D/4D-printed SPAs in practice. Therefore, higher control accuracy could be achieved in the empirical model using real-life data and integrated sensing capabilities of SPAs compared to FEA and analytical models.

The input pressure flow rate and its duration are the controllable parameters that could be regulated based on the desired output, which is the end-point position and tip force of the actuator. Hence, the model outlining the relationship between the input pressure and the bending angle response should be developed first. Thus, the pressure sensors connected to the pneumatic supply tubes and the integrated sensors are required for developing the data-driven model. One drawback of this approach is the high feedback noise level borne during the data acquisition of input pressure. This was significantly rectified by introducing a fixed volume syringe pneumatic air tank and a pneumatic resistor to damp the undesired oscillations as well as by applying a moving average digital filter (Elgeneidy, Lohse, and Jackson 2018). Having developed the data-driven model to estimate the bending angle based on the input pressure measurements, the closed-loop controller is required to meet the target bending angle.

The supervised learning, including linear regression and artificial neural network (ANN), models were commonly investigated on learning the inverse kinematics of SPAs (Elgeneidy, Lohse, and Jackson 2016; George Thuruthel et al. 2017; Thuruthel et al. 2019). The kinematics of SPAs, as discussed in the earlier section, is highly nonlinear in an unstructured environment...
due to hyperelastic material properties and design geometry. Thus, the ANN models could be employed to approximate the Jacobian function of SPAs (George Thuruthel et al. 2018). A comparison study of using both linear regression and ANN for predicting the bending angle of the SPA end-point was investigated (Elgeneidy, Lohse, and Jackson 2018). The authors reported that the ANN used in the study was able to reflect the nonlinearity in the response of SPA with higher accuracy than the linear regression model. The model used in their work was further utilized for finding the PID gains of the closed-loop controller to handle the external disturbances during the operation of the SPA. However, due to the nonlinearity of the 3D/4D-printed SPAs, the conventional PID controller might not be an ideal choice for dealing with the uncertainties of the system. Hence, cascade controllers with the incorporation of machine learning algorithms to tune the PID gains could be adopted for improving the accuracy of the end-point position tracking of SPA (Zhao, Zhong, and Fan 2015; Fan et al. 2015) (Zolfagharian, Valipour, and Ghasemi 2016). A nonlinear autoregressive-exogenous (NARX) observer, using wavelet and sigmoid networks was also developed in the form of an Extended Kalman Filter to predict the behavior of the SPA operating in an unstructured environment with minimum error (Loo et al. 2019). The schematic workflow for the data-driven modeling and control of 3D/4D-printed SPAs is illustrated in Fig. 14.

Fig. 14. (a) Data-driven modeling and, (b) closed-loop adaptive control of 3D/4D-printed SPAs.
6. Discussions, Challenges, and Future Directions

There is a range of commercially available photocurable elastomers, including EPU 40 (Carbon), Tangoplus (Stratasys), Formlab Flexible (Formlab), and Spot-E Elastic (SpotAMaterials). The reviewed custom-made photo resins could be studied for an optimized mass ratio of the photo absorber and the resin to obtain customized and enhanced mechanical properties for 3D/4D printing of SPA via the DLP method (Ge et al. 2018).

One major concern of bending SPA is the balling effect of the lower chamber, which occurs due to abrupt change of the contour shape and may lead to an exertion of excessive pressure and even cause bursting of the actuator. The balling effect in a soft robot essentially wastes energy on radial inflation when the energy needs to be exercised on longitudinal inflation. Using multi-material 3D/4D printing is a proven way to deal with this problem in the SPA (Wang, Ge, et al. 2017). In this approach, a material with a higher modulus of elasticity is printed at the bottom layer of the SPA without compromising the bottom wall thickness. However, reducing the balling effect comes at the expense of the magnitude of the bending angle.

Miniaturizing and scaling down the 3D/4D printed SPAs are highly desirable, particularly by adding the micrometer-size functionalities for practical applications in the manipulation of microscale delicate objects, e.g. cells. Yet, such feature should be scalable in all the key components of the SPAs, including the integrated sensors (Khosravani and Reinicke 2020a), flexible electronics (Nasiri and Khosravani 2020), and controllers (Zolfagharian et al. 2020). However, miniaturizing the SPAs is constrained by the resolution of 3D printers and challenges in 3D printing such as avoidance of microscale voids and channels.

The power source of 3D-printed SPAs is a major point of emphasis using compressors, particularly for wearable SPAs in performing high mobility demand tasks such as medical applications and rehabilitation (Adami and Seibel 2019). Such applications require small-scale pressure generation systems as compact, lightweight, and low noise as possible where alternative methods such as onboard pneumatic pressure generation methods using chemical reaction-based sources or combustible fuels could be considered instead of bulk and heavy industrial-sized compressors (Walker et al. 2020). However, various factors, including the energy density, flow capacity, and safety are implicated in the selection of the most suited pressure generation method. For instance, it was reported that the battery-powered micro compressors provided relatively high capacity, but their maximum pressure and flow rate were lower than the fluidic compressed tanks for soft robotics applications (Wehner et al. 2014).

Compressors are often used as the power source of 3D-printed SPAs, particularly for wearable SPAs in performing tasks that demand high mobility such as medical applications and rehabilitation (Adami and Seibel 2019). Such applications require small-scale pressure generation systems to be as compact, lightweight, and low noise as possible for which alternative methods such as on-board pneumatic pressure generation methods using chemical reaction-based sources or combustible fuels could be considered instead of bulk and heavy industrial-sized compressors (Walker et al. 2020). However, various factors, including the energy density, flow capacity, and safety are implicated in the selection of the most suitable pressure generation method. For instance, it was reported that the battery-powered micro compressors provided relatively high capacity, but their maximum pressure and flow rate were lower than the fluidic compressed tanks for soft robotics applications (Wehner et al.
Compact 3D/4D-printed SPAs could be developed with applications in soft mobile robots. The energy source of these printed soft robots could be supplied using onboard pneumatic pressure generation methods, such as microprocessors, pressurized gas tanks, chemical reactions, and phase change at the triple point which are shown to generate up to 500 kPa input pressure (Adami and Seibel 2019).

One of the important conditions for the sustainability of a product is the ability of the material used to be recycled at any time during its life cycle, such as during manufacturing, during use, and after product life. These recycling stages could be considered so that 3D-printed SPAs could be integrated into the recycling process (Nguyen and Seibel 2019). 3D/4D printing of custom-made SPAs could be justified in terms of their environmental impact due to utilization of green and recyclable materials, optimization of processing parameters, such as layer thickness and porosity during the 3D printing process, and to their reduced carbon-foot print and waste (Khosravani and Reinicke 2020b).

Out-of-plane deformation is understood as a drawback of current 3D/4D-printed SPAs. The twist-coupled bending or sideward slipping of SPAs during operation leads to unstable grasping. This issue could be further investigated in 4D printing with more consideration in the design and also on the localized stiffening of the structure of the SPA (Scharff et al. 2019).

A novel 3D printing manufacturing method was introduced with the incorporation of fiber weaving into an elastomeric material extrusion (Stalin et al. 2019). This provides a new manufacturing path for 4D printing a novel type of reinforced SPA that could be a mixture of both bellow-type and embedded fiber into the matrix of 3D-printed elastomer.

Recently a SPA was 4D-printed, which operates based on the self-exciting vibration principles. This actuator has shown vibrating capabilities without needing any valve which simplifies the structure for wider applications. The self-excitation feature of this actuator will further simplify the control and drive of 3D/4D-printed bending-type SPAs in mobile soft robots and microfluidics (Tani et al. 2020).

The grasping adaptability and stability of the 3D/4D-printed SPA could be further enhanced by introducing the variable stiffness capabilities by various means such as self-locking mechanism (Guo et al. 2020) or multi-material fabrication (Al-Rubaiai et al. 2019; Zhu et al. 2019; Du Pasquier et al. 2019). While the self-locking mechanism provides energy-saving and less valve control, a combination of 3D-printed sensors and multi-material fabrication using SMPs could be implemented to develop variable stiffness control of 3D/4D-printed SPAs (Al-Rubaiai et al. 2019; Fang et al. 2019).

The 3D/4D-printed SPAs are intrinsically soft and resilient to mechanical impacts, but at the expense of vulnerability to wear, puncture, and cut due to over pressurizing or contact with sharp objects. Although self-healing SPAs have already been investigated (Terryn et al. 2017), the 4D-printed SPAs with self-healing capability are rarely studied, and this could be a prospect future direction in 4D printing eco-friendly pneumatic soft robots. These SPAs could be recycled and reused while having a beneficial impact on the life span and reducing their ecological footprint.

The port-Hamiltonian model of 3D/4D-printed SPAs could bring more insights into the control-based modeling of these systems for practical applications in unstructured environments. A study of developing the port-Hamiltonian model for SPA has proved the
efficacy of this approach for designing and controlling a more energy-efficient task-oriented SPA (Chun et al. 2019; Ghasemi, Xiao, and Gao 2019).

Further investigations on the behavior of 3D/4D-printed SPAs could be conducted for uncertain environments, such as amphibious for the under-water grasping ability for floating objects (Hao et al. 2017; Sun, Wang, and Zhu 2020; Zhang et al. 2020). This could be investigated further with advanced multimodal sensors (Chen et al. 2020) and electronic skin (e-skin) (Shih et al. 2020; Fu et al. 2020). The FEA could be used in kinematic model development of SPAs where an adequately large amount of data is required to train the ANN (Runge, Wiese, and Raatz 2017).

There is an opportunity for further investigations on the two-way fluid-structure interaction (FSI) meshless methods for accurately simulating the bending behavior of the 3D/4D-printed SPAs rather than merely one-way structural hyperelastic models (Moon et al. 2020). The early study has revealed that FSI outperformed the conventional structural FEA in nonlinear bending behavior of SPAs, particularly in the large deformation analysis (Moon et al. 2020).

Despite successful utilization of the data-driven controller in the closed-loop control of 3D/4D-printed SPAs there are still challenges remaining in the high-frequency control bandwidth applications. The incorporation of the intrinsic controller via the morphological properties of voxels acting as zero-lag feedback controller during printing can broaden the control bandwidth for faster and more robust manipulations. The sparse sensing and uncertainty quantification could be incorporated via integration of 3D-printed sensors by optimising the locations of sensors to enhance controller performance. The incorporation of the morphological computation of materials into the controller account for the optimal placement of sensors to SPAs.

Currently, there are two different viewpoints on the control of soft manipulators (Shih et al. 2020). First, is the high-level control of the SPAs, like rigid manipulators and grippers, where a range of integrated soft sensors with low bandwidth, less than 50 Hz, and higher bandwidth, up to 400 Hz, are required to provide the tactile perception and vibration-induced information to avoid the slippage. The second view, however, is focusing more on proprioceptive feedback information on each volumetric pixel (voxel) of SPA to deliver low-level control tasks relying on the morphology of the SPA body, like the way octopus arm works. The final decision should be made to realize 3D/4D-printed SPAs that are safer for human-robots and are more aware of their environment.

7. Conclusion

The 3D-printed bending-type soft pneumatic actuators are the most common soft actuators that attracted the research community recently due to their unique characteristics such as custom-made automated manufacturing, compliance, lightweight, and safety in human-robot interactions as well as the ability to handle delicate items. This study provided a comprehensive guide to fabrication, modeling, and control of 3D/4D-printed SPAs thus far developed. Different types of materials and 3D printing techniques used for developing these actuators were reviewed. The analytical kinematic modeling for predicting the bending curvature and blocking force of the 3D/4D-printed SPAs was described. The FEA for dynamic modeling of hyperelastic materials and various energy functions, which broadly applied for SPAs were
discussed and the suitability of them was investigated based on common materials. The appropriate sensors that could be integrated into the 3D/4D-printed SPAs were analyzed. The control-based 4D printing of SPAs was presented and discussed. Finally, the current challenges were depicted and cutting-edge research avenues for starting new studies on 3D/4D-printed SPAs were highlighted.

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