Selecting Target Range with Accurate Vital Sign Using Spatial Phase Coherency of FMCW Radar

Ho-Ik Choi 1, Woo-Jin Song 1, Heemang Song 2 and Hyun-Chool Shin 3,*

1 Department of Electrical Engineering, Pohang University of Science and Technology, Pohang 37673, Korea; chi1932@postech.ac.kr (H.-I.C.); wjsong@postech.ac.kr (W.-J.S.)
2 Department of Electronic Engineering, Soongsil University, Seoul 06978, Korea; songhm@soongsil.ac.kr
3 Department of Software Convergence, Soongsil University, Seoul 06978, Korea
* Correspondence: shinhc@ssu.ac.kr; Tel.: +82-02-828-7165

Abstract: Respiration and heartbeat are basic indicators of the physiological state of human beings. Frequency-modulated continuous wave (FMCW) radar can sense micro-displacement in the human body surface without contact, and is used for vital-sign (respiration and heartbeat) monitoring. For the extraction of vital-sign, it is essential to select the target range containing vital-sign information. In this paper, we exploit the coherency of phase in different range-bins of FMCW radar to effectively select the range-bins that contain accurate signals for remote monitoring of human respiration and heartbeat. To quantify coherency, the spatial phase coherency (SPC) index is introduced. The experimental results show that the SPC can select a range-bin containing more accurate vital-sign signals than conventional methods. This result demonstrates that the proposed method is accurate for monitoring of vital signs by using FMCW radar.

Keywords: FMCW radar; respiration; heartbeat; range selection; spatial phase coherency

1. Introduction

Respiration and heartbeat can provide the basic physiological state of human beings, and can be used as healthcare indicators or in clinical diagnosis [1–6]. Traditionally, stretch sensors [7], pneumotachographs [6,8], photoplethysmographs [9,10], and electrocardiographs [11,12] have been used to measure respiration and heartbeat. However, traditional monitoring sensors that are attached to the body can cause discomfort and restrict behavior. Radar can detect micro-displacement in the human body surface without contact [13–15], and this ability has been exploited for contactless monitoring of vital signs (VSs). Radar can monitor VSs continuously, and without contact, so the monitoring system has been applied in various applications such as medical care surveillance for severe burns or infectious diseases [16,17], driver assistance [18,19], sleep monitoring for sudden infant death syndrome, apnea detection [20–22], and homecare for the elderly [23–25]. In particular, frequency-modulated continuous wave (FMCW) radar, which has ranging capability, can spatially separate VSs from clutters [26,27]. Additionally, FMCW radar uses a millimeter-wave band, and therefore has the advantages of small sizes and low power consumption. Therefore, FMCW radar has been widely used for contactless monitoring of VSs [28–36].

Methods to extract VSs from the FMCW radar signal are generally divided into spectral analysis and range-bin selection [37–41]. The discrete Fourier transform (DFT) is mostly used for spectral analysis, which is a range analysis of the FMCW signal. The results of DFT at each range (or spectral) bin, namely magnitude and phase, contain information about displacement of the target. Information pertaining to respiration and heartbeat exists in specific range-bins, such as range-bins near the abdomen or thorax for respiration [39,42], and range-bins near the neck for heartbeat [43], so the range-bin that includes the VSs must be selected precisely. In conventional methods, the magnitude or phase in a single range-bin...
is used to search for the range-bin that includes the VSs [37–39], or signals in multiple range-bins are integrated [40]. The method in [37] uses the coherency between magnitude and phase as a criterion for range-bin selection, and therefore enables more accurate selection of range-bins that contain information about VSs, compared to the methods in [38–40], which exploit the extent of magnitude, phase fluctuation, or integrated phase. However, when inaccurate information on VSs may be selected. When a range-bin that contains inaccurate VS information is selected, the accuracy of the measurement of VSs degrades. Therefore, range-bin that contains accurate VS information must be selected exactly.

This paper introduces a range-bin selection criterion that exploits coherency of the phase in multiple range-bins to select a range-bin that contain an accurate VS signal. Considering the radar signal model, phase is preferred for measuring the VS displacement to magnitude. In addition, respiration and heartbeat occur in spatially-various parts of the body, so the displacement with vital periods observed simultaneously in various range-bins is expected to be respiration or heartbeat. Thus, spatial phase information is used for range-bin selection instead of using magnitude, as in [37,38]. A spatial phase coherency (SPC) index was devised to quantify the coherency between displacements in spatially different range-bins. Then, a pair of range-bins that had the highest SPC was selected for vital extraction. Experimental results demonstrate that the proposed method selects range-bins that contain more accurate respiration and heartbeat than the bins selected by using conventional methods.

2. Methods
2.1. FMCW Radar Signal Model

The FMCW radar transmits a radio wave that has linearly-increasing frequency. The transmitted signal is mixed with the received signal, then subjected to low-pass filtering, to obtain the intermediate frequency (IF) signal, \( x(t, n) \) [26,27]:

\[
x(t, n) = \sum_r M(t, r) \cdot \cos(2\pi \cdot f_r \cdot n + P(t, r)),
\]

where \( t \) is the scan time, \( n \) is the sampling time in a chirp, \( r \) is the range, \( f_r \) is the beat frequency, \( M(t, r) \) is the magnitude, and \( P(t, r) \) is the phase.

\( x(t, n) \) contains the range information in \( f_r \). DFT is applied to \( x(t, n) \) at each \( f_r \) to calculate \( M(t, r) \) and \( P(t, r) \), which contain displacement information of the target at \( r \). When a target exists in range-bin \( r \), the signal model in [37] for \( M(t, r) \) and \( P(t, r) \) are

\[
M(t, r) = \frac{M_0}{4\pi \cdot f_r \cdot r^2},
\]

\[
P(t, r) = \frac{4\pi \cdot f_c}{c} \cdot r,
\]

where \( M_0 \) is the baseline magnitude, \( f_c \) is the center frequency, and \( c \) is the lightspeed.

Moreover, with regard to the small displacement \( \Delta(t) \) in the target, the displacement affects \( M(t, r) \) and \( P(t, r) \), as

\[
M(t, r) = \frac{M_0}{4\pi \cdot (r + \Delta(t))},
\]

\[
P(t, r) = \frac{4\pi \cdot f_c}{c} \cdot (r + \Delta(t)).
\]

However, \( M(t, r) \) in (2) is valid for an isotropic antenna model. In general, radar uses directional antennas and \( M(t, r) \) should be modeled considering antenna gain \( G \), radar cross section \( \sigma \), and effective area \( A_e \) [44,45], as

\[
M(t, r) = \frac{M_0 \cdot \sqrt{G \cdot \sigma \cdot A_e}}{4\pi \cdot r^2}.
\]
According to the conventional studies [46,47], $\sigma$ changes by respiratory activity. Considering the results, $G$, $\sigma$, and $A_e$ in (4) could change by VS displacement, $\Delta(t)$. Therefore, $M(t,r)$ in (4) is difficult to describe for $\Delta(t)$ unlike in (3). Considering the model in (3) and (4), the relationship between $M(t,r)$ and $\Delta(t)$ is not clear, whereas $P(t,r)$ is linearly proportional to $\Delta(t)$. With regard to VS measurements, $\Delta(t)$ is the displacement of the body surface caused by respiration and heartbeat, and $P(t,r)$ measures displacement more precisely than $M(t,r)$ does.

### 2.2. Vital-Sign Measurement

Figure 1 shows the experimental settings for FMCW radar based VS measurements. As shown in Figure 1a, subjects comfortably sat on a chair facing the radar about 1 m apart. The distance between parts of body and the radar depends on the build of subjects, but generally distance to the abdomen was about 0.6~0.8 m, and distance to the neck was about 0.9~1.0 m. The FMCW radar used for recording was BTS60 [48] (bitsensing Inc., Seoul, Korea) shown in Figure 1b. To obtain ground truth of VSs, a Neulog Respiration Monitor Belt logger sensor (Neulog Inc., Rishon Lezion, Israel) was wrapped around the abdomen, and the ECG electrodes of a PolyG-A (Laxtha Inc., Daejeon, Korea) were attached to both wrists and the right ankle.

![Figure 1. Vital-sign measurement using FMCW radar. (a) Experimental settings for vital measurement; (b) FMCW radar.](image)

Figure 2 shows VS signals measured by FMCW radar. $M(t,r)$ and $P(t,r)$ for respiration and heartbeat are shown in Figure 2a,b. Because of high range-resolution of the radar, displacements in various parts of body are reflected in different range-bins. To identify the range-bin where the VS displacement exists, the temporal correlation coefficient [49] between $P(t,r)$ at each range-bin and referenced VS signals was calculated as shown in Figure 2c,d. According to the conventional studies, respiration can be measured near the abdomen or thorax [39,42], and heartbeat can be measured where the skin is thin, such as the neck [43]. In our experiments, the correlation between $P(t,r)$ and referenced respiration signal was high between 0.5 and 0.6 m, which is near the subject’s abdomen. The correlation between $P(t,r)$ and referenced heartbeat signal was high between 0.75 to 0.85 m which is near the subject’s neck.

In Figure 2e,f, the extracted VSs (respiration and the heartbeat) from various range bins corresponding to high and low correlation with referenced signals are compared. $P(t,r = 0.525, 0.550)$ m in Figure 2e is highly correlated with referenced respiration, but $M(t,r = 0.525, 0.550)$ m is not. $P(t,r = 0.775, 0.800)$ m in Figure 2f shows a high correlation with a referenced heartbeat; however, $M(t,r = 0.775, 0.800)$ m does not. At $r = 0.800$ m in Figure 2e and $r = 1.050$ m in Figure 2f, $M(t,r)$ nor $P(t,r)$ are associated with referenced VSs.

To summarize, respiration and heartbeat signals can be observed in multiple range-bins of $P(t,r)$, which is more accurate and reliable than $M(t,r)$. In addition, displacement of VSs exists in certain range-bins, so the range-bin that contains accurate displacement of VSs must be chosen.
2.3. Spatial Phase Coherency

To select the range-bins that contain displacement of VSs, we introduce a new method that selects range-bins by considering the coherency between $P(t, r)$ over multiple range-bins. As shown in Figure 2, displacement by VSs is spatially distributed in multiple range-bins, and the displacement is simultaneously observed in the $P(t, r)$ of the range-bins. Thus, the coherency between $P(t, r)$ in range-bins that contain VS displacement should be high. Coherency is our criterion for selecting a range-bin that contains vital information, and an SPC index to quantify coherency was devised, as in (5).

$$SPC(t, r, r') = \frac{\sum_{s=t-t_0}^{t} P(s, r) \cdot P(s, r')}{\sigma_P(r) \cdot \sigma_P(r')} \quad \text{for} \quad r \neq r', \quad (5)$$

where the mean of $P(t, r)$ over $t$ is eliminated beforehand, and $\sigma_P(r)$ is the standard deviation of $P(t, r)$.

Then, the pair of range-bins that have the highest SPC value are selected as the VS target range $r_T(t)$, as in (6):

$$r_T(t) = \arg \max_{\{r, r'\}} SPC(t, r, r'). \quad (6)$$
To test whether SPC could measure coherency, signals were generated and SPC was applied. Figure 3a shows generated $P(t, r)$. To generate $P(t, r)$, peak points of sinusoids were detected, the location of peak points were disordered by uniform noise, and the points were interpolated. From $r_1$ to $r_9$, the boundary of uniform distribution was expanded to generate further disorder. Figure 3b shows the SPC between $P(t, r_1)$ and $P(t, r)$ in other range-bins. As $P(t, r)$ was disordered from $r_2$ to $r_9$, the SPC decreased.

Figure 3. Generated signal and SPC. (a) Generated $P(t, r)$, and (b) SPC with respect to $P(t, r_1)$.

As shown in Figure 4, SPC was applied to a real FMCW radar signal shown in Figure 4a,b and the capability of SPC in selecting the range-bins that contain vital information was tested. Figure 4c,d shows the calculated SPC. The SPCs for respiration and heartbeat were high for range-bins where $P(t, r)$ was spatially coherent such as $0.50 \leq r \leq 0.60$ m in Figure 4a, and $r = 0.75 \leq r \leq 0.85$ m in Figure 4b. In addition, maximum SPC at each range-bin was compared to the correlation coefficient between $P(t, r)$ and referenced VSs. The SPC and correlation coefficient represented similar trends over the range, and both indices had maximum values at the same range-bin. Figure 4e,f shows $M(t, r)$ and $P(t, r)$ in the pair of range-bins that had the highest SPC. For respiration, $P(t, r_{R1})$ and $P(t, r_{R2})$ in Figure 4e are coherent, and are in proportion with the referenced respiration. For heartbeat, $P(t, r_{H1})$ and $P(t, r_{H2})$ in Figure 4f are coherent, and are proportional to the referenced heartbeat. However, the $M(t, r)$ in the same range-bins does not show VS displacement.

To summarize, displacement by VSs was represented in several range-bins of $P(t, r)$; accurate respiration and heartbeat signals were extracted by selecting a pair of range-bins that had the highest SPC.
Figure 4. SPC and extracted vital-sign signals. (a,b) $M(t,r)$ and $P(t,r)$ for respiration and heartbeat, (c,d) SPCs, for respiration and heartbeat, and (e,f) extracted respiration and heartbeat.

3. Results

3.1. Data Acquisition

The radar and referenced VS signals of 20 subjects (15 men and 5 women) were recorded. The subjects sat on a chair facing the radar apart about 1 m. Depending on subjects, the distance between body parts and radar can be varied. However, the distance to the abdomen was generally 0.6−0.8 m and the distance to the neck was 0.9−1.0 m. Thus, we set the searching boundary of the target range bin to 0.5−1.2 m. Each subject was well informed about the entire process and purpose of recording, and agreed to the recording. All subjects had normal vital rates, and rested for least 5 min before the recording process. The recording lasted 2 min for each subject.

3.2. Computation Process

The recorded data were processed using MATLAB R2015a (MathWorks Inc., Natick, MA, USA). $M(t,r)$ and $P(t,r)$ were calculated using the built-in fast Fourier transform
function, and the Hamming window was applied to \( x(t, n) \) to prevent spectral distortion. To reconstruct the continuous phase variation, phase unwrapping was applied to \( P(t, r) \). To reduce the time complexity, the boundary of the human target was set by reference to the variance of \( M(t, r) \); this process suppresses stationary clutter [50]. Then, considering that normal adults’ respiratory rate is \( 14 \sim 20 \) respiration per minute (RPM), and heart rate is \( 60 \sim 100 \) beats per minute (BPM) [51, 52], \( P(t, r) \) inside the boundary, was filtered at \( 0.1 \sim 0.4 \) Hz for respiration, and \( 0.8 \sim 1.7 \) Hz for heartbeat. For each pair of range-bins, the SPC was calculated and \( r_T(t) \) was selected. Then, \( P(t, r) \) in the selected range-bins was averaged to calculate vital rates using the zero-crossing detection [53]. The vital rates were represented as RPM for respiration and BPM for heartbeat. For continuous monitoring of vital rates, they were extracted every second using \( t_0 = 15 \) s of time-windowed data. For comparison with conventional methods, the vital rates of conventional methods were calculated in the same way as the proposed method, except for the range-bin selection. Conventional methods were implemented as followed equations. The method in [37] selects a range-bin, which has the highest coherency between magnitude and phase, as

\[
 r_T(t) = \arg \max_r \frac{\sum_{i=t-t_0}^t M(s, r) \cdot P(s, r)}{\sigma_M(r) \cdot \sigma_P(r)},
\]

where \( \sigma_M(r) \) is the standard deviation of \( M(t, r) \).

The method in [38] selects a range-bin, which has the maximum magnitude of range-profile considering the reflected power from the target as in (8). The range profile, \( X(t, r_k) \) is calculated by Fourier transform as in (9)

\[
 r_T(t) = \arg \max_r \left\| \sum_{s=t-t_0}^t X(s, r) \right\| 
\]

\[
 X(t, r_k) = \sum_{n=0}^{N-1} x(t, n) \cdot \exp \left( -j \cdot \frac{2\pi \cdot k \cdot n}{N} \right),
\]

where \( r_k = \frac{k}{BW} \cdot k \) for \( k = 0, \ldots, N - 1 \), and \( BW \) is bandwidth and \( N \) is the number of samples in a chirp.

The method in [39] selects a range-bin, which has the maximum phase fluctuation as

\[
 r_T(t) = \arg \max_r \sum_{s=t-t_0}^t P^2(s, r),
\]

where DC offset of \( P(t, r) \) is removed in advance.

The method in [40] uses a range-integrated phase, \( \hat{P}(t) \) for VS measurements as

\[
 \hat{P}(t) = \angle \sum_r X(t, r)
\]

### 3.3. Vital-Sign Accuracy

The accuracy of the VSs in the range-bins that was selected by the proposed and conventional methods were examined and compared.

Figure 5 shows extracted VS signals depending on range-bin selection methods. As shown in Figure 5, the proposed method selected the pair of range-bins for which showed the coherency and correlations between \( \hat{P}(t, r) \) and referenced VSs were high. However, in the same range-bins, \( M(t, r = 0.975, 1.000) \) m in Figure 5a and \( M(t, r = 1.175, 1.120) \) m in Figure 5d do not represent respiration or heartbeat, although \( M(t, r = 1.150, 1.175) \) m in Figure 5b and \( M(t, r = 0.800) \) m in Figure 5c are proportional to referenced heartbeat or respiration. Although \( M(t, r) \) represented vital displacement as in Figure 5b,c, \( M(t, r) \) was not reliable in measuring VS displacement as in Figure 5a,d. Consequently, the accuracy of VSs extracted by method in [37] varied among the subjects. Furthermore, both \( M(t, r) \)
and $P(t, r)$ of methods in [38–40] had inaccurate information about both respiration and heartbeat considering the correlation with the reference.

Figure 5. Extracted vital signs. (a,b) Extracted respiration and heartbeat signals for subject#1, and (c,d) extracted respiration and heartbeat signals for subject#2.
Figures 6 and 7 show the results of continuous vital monitoring using the proposed method for 20 subjects. For most subjects, the estimated VS rates were consistent with the reference. However, due to the unexpected body movements or spectral overlapping of respiration and heart rhythms, there were some subjects whose estimated VS rates show large variation from the reference data at some time points.

Figure 6. Comparison of the extracted respiration rate using the proposed method with the referenced ground truth for 20 subjects.
Figure 7. Comparison of the extracted heart rate using the proposed method with the referenced ground truth for 20 subjects.
For each subject, 105 vital rates were obtained and 2100 vital rates were totally obtained from the all subjects. Figure 8 depicts scatter plots of the estimated vital rates compared to the ground truth. Diagonal patterns are observed in the scatter plots of the proposed method, indicating that estimated vital rates are close to the ground truth. Moreover, we evaluated the accuracy of the estimated vital-sign rates as the mean error $\epsilon$, correctness $\phi$, and correlation coefficient $\rho$ with ground truth for the various time window, $t_0$ as shown in Figure 9.

The $\epsilon$ measures averaged absolute difference between estimated vital rates and ground truth, as in (12):

$$
\epsilon = \frac{1}{K} \sum_{i=1}^{K} |x_i - y_i|,
$$

where $K = 2100$ is total number of vital rates, $x$ is estimated vital rates, and $y$ is referenced vital rates.

The $\phi$ calculates the proportion of the estimated vital rates of which the error compared to the ground truth is within the boundaries $[37,40]$, as in (13).

$$
\phi = \frac{100}{K} \sum_{i=1}^{K} I(|x_i - y_i| < \text{thr}),
$$

where $I(\text{statement}) = \begin{cases} 1 & \text{if statement = true} \\ 0 & \text{if statement = false} \end{cases}$, $\text{thr} = 2$ RPM for respiration and $\text{thr} = 5$ BPM for heartbeat.

The $\rho$ measures the correlation between the estimated vital rates and ground truth [49], as in (14):

$$
\rho = \frac{\sum_{i=1}^{K} (x_i - \mu_x)(y_i - \mu_y)}{\sigma_x \cdot \sigma_y},
$$

where $\mu_x$ and $\mu_y$ are mean of $x$ and $y$, and $\sigma_x$ and $\sigma_y$ are standard deviation of $x$ and $y$.

For both respiration and heartbeat, the vital rates extracted from the proposed method show higher accuracy than conventional methods with respect to $\epsilon$, $\phi$, and $\rho$ regardless of length of the time window.

![Figure 8. Comparison of radar based vital rates with reference. (a) Respiration rate, and (b) heart rate.](image-url)
4. Discussion

SPC was introduced to select a range-bin containing accurate VS displacement, and VS signals were extracted from $P(t, r)$ in a selected pair of range-bins that had the highest SPC. The range-bins selected by the proposed method had more accurate VS displacement than those selected by the conventional methods. For some subjects, estimated vital rates deviated at some time intervals due to the unknown artifacts, presumably caused by body motion, respiration harmonics, or subject dependency. For future works, the range-bin tracking logic [54,55] or the cancellation of respiration harmonic [56] can be applied to improve the stability of VS monitoring. Moreover, considering the FMCW radar is widely used for multi-target monitoring because of its ranging capability, the proposed SPC needs to be expanded to multi-target VS monitoring.

5. Conclusions

Depending on the range-bin selection, the accuracy of the extracted respiration and heartbeat varied. To select an appropriate range-bin that contains accurate VS signals, a range-bin selection method that used SPC was proposed. The method utilized spatial information of the phase, which is more reliable than the magnitude in VS monitoring. In experimental results, the accuracy of VS extraction for 20 subjects was shown. The range-bins that had the highest SPC contained accurate vital information. Furthermore, the proposed method selected the range-bins that contain more accurate-respiration and heartbeat signals than the bins selected by conventional methods. Quantitative evaluations of $\epsilon$, $\sigma$, and $\rho$, demonstrated that the proposed method was superior to the conventional methods. The proposed method can extract accurate VS signals from the FMCW radar signal, and therefore will be useful for applications in healthcare monitoring.

Although the proposed method selected the range-bins that contain more accurate-respiration and heartbeat signals than the bins selected by conventional methods, the results were obtained from the situation when subjects sat on a chair facing the radar apart about 1 m. For the rigorous quantification of the performance, the proposed method needs to be evaluated with freely moving subjects located at various distances.
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