1. Introduction

For rock-based engineering projects, the damage characteristic of rocks is quite important. Furthermore, attentions must be paid to the initial damage point of rocks in these rock engineering projects, such as high-level radioactive wastes (HLW) disposal [13], hydropower stations [17], subways [10], soft-rock engineering [1], deep-buried tunnels [19], and mining engineering [11], to name a few. In general, the damage point is an inherent property of rock under single loading, independent of loading conditions. This point marks the beginning of rock damage, indicating subsequent crack formation and propagation, and is of great practical significance.

An increasing number of scholars have examined the damage point of rocks using laboratory tests. Brace et al. [2] monitored the volume variation of rock specimens. They thought that when rock was damaged, its volumetric strain would present nonlinear volume expansion, instead of linear development. Thus, the end point of linear volumetric strain is regarded as the damage point of rocks, and the solution process is shown in Figure 1(a). This method expresses clear physical meaning and convenient application, but the results are deeply influenced by the coordinate scale and discrete data. Taking the volumetric strain in Figure 1(a) as example, it is difficult to determine the No. 1 point, or the No. 2 point is the target point in the partial enlarged Figure 1(b). The confirmation of end point is subjective and arbitrariness. Lajtai [8] thought that the nonlinear lateral strain meant cracks expansion, so he took the beginning point of nonlinear growth in the axial stress-lateral strain curve as damage point (as shown in Figure 2(a)). Compared with the method proposed by Brace, the lateral strain method is much easier and more intuitive. However, it is undeniable that the lateral strain method also has some subjective factors and errors, and the same problem will affect the accuracy of the result. As the enlarged crack volumetric curve shown in Figure 2(b), there will also be some deviations in the determination results under different data curve scales, the initial damage point can be confirmed as point 1, and the other damage point can be selected as point 3 in Figure 2(b). Martin and Chandler [12] conducted a large number of triaxial compression tests on granite samples from mine-by tunnel in Canada. By summarizing the strength relationship of granite samples, they proposed that the stress when the crack volume strain is not zero at first could be treated as the damage point. The accuracy of calculation through this method is largely dependent on the accuracy of elastic
modulus and Poisson’s ratio of rock, and there are still errors in the calculation of elastic modulus and Poisson’s ratio, which also makes this method highly subjective. Studies show that the failure process of rocks is accompanied by the release of acoustic emission (AE) signals. Through monitoring the AE signal strength, the damage process of rocks can be visually obtained. Therefore, various studies on rock stress are carried out by acoustic emission monitoring. Eberhardt et al. [4] identified the crack initiation and propagation thresholds in brittle rock by AE monitoring; Ganne and Vervoort [5] confirmed the effect of stress path on pre-peak damage with AE method; Nejati and Ghazvini [15] studied the brittleness effect during rock fatigue damage process by employing AE equipment; Kim et al. [7] carried out a comparative evaluation of stress-strain and AE methods for quantitative damage assessments of brittle; Zhao et al. [23] analyzed the rock damage characteristics based on the AE monitoring data. It is assumed that the first AE count mutation corresponds to the damage point of rock. AE techniques provide scientific method for exploring rock fracture process, but this method still has subjective errors, noise interference, and absence of theoretical basis [21]. The initial AE records during loading can be related to the setting of loading platens on the specimen, machine displacement, instrument vibration, and other influence factors. It is difficult to determine which AE count is the correct index which corresponds to the damage point of rock.

In order to avoid the shortage of the above methods, a new step cyclic loading test was designed. Some scholars have conducted experiments on rocks under cyclic loading. Yang et al. [18] studied the mechanical property of sandstone post-peak under the cyclic loading and unloading; Zhang et al. [20] carried out the lab tests on damage characteristics of sandstone subjected to pre-peak and post-peak cyclic loading; Munoz and Taheri [14] analyzed the post-peak deformability parameters of rocks under cyclic loading. These studies can provide good experimental ideas and schemes for reference. In this paper, taking advantage of
MTS815 rock experimental equipment, the step cyclic loading tests with increasing stress were conducted on deep granite from Sanshandao Gold Mine, China. And, a more accurate initial damage point under confining pressures of 10 MPa, 20 MPa, and 30 MPa was confirmed. The calculated initial damage points are much more scientific and intuitive, which provides a new method for the study on rock mechanics in deep mining engineering.

2. Testing Scheme

2.1. Granite Samples and Basic Parameters. In the tests, the rock specimen is granite, drilled from -895 level of Sanshandao Gold Mine (Shandong Province, China), with the mineral composition of quartz, anorthose, biotite, and alkali feldspar. The density of rock samples is 2.72 g/cm³, and the porosity is 0.59%. All the rock samples were cut from a whole block rockmass without any obvious cracks. According to the proposed approach of ISRM [6], the allowed deviation of roughness at the two ends for the specimen is ±0.05 mm, and the allowed perpendicularity deviation is ±0.25°. In the tests, 36 standard rock samples with 50 mm diameter and 100 mm height were acquired, as shown in Figure 3.

2.2. Experimental Installation. In the step cyclic loading tests, the MTS 815 testing system was adopted, as shown in Figure 4. For this MTS 815 testing system, the maximum axial loading can reach 2700 kN, and the maximum confining pressure is 140 MPa. The strain of rock samples could be monitored by the axial and lateral extensometers, with the largest testing ranges of 5 mm and 8 mm in axial and lateral direction, respectively. And, during the loading process, to avoid the effect of hydraulic oil, the heat shrinkable tube was employed to encircle the granite sample. At the same time, the lubricant was spread on the two ends of samples to decrease the ends’ effect.

2.3. Experimental Design. Firstly, to obtain the basic strength and other mechanical parameters of granite, a set of triaxial compressive tests with different confining pressures (10 MPa, 20 MPa, and 30 MPa) were carried out. During the tests, the AE event will be monitored by AE instrument, and the key parameters of AE instrument related to the measurement are shown in Table 1. The obtained stress thresholds can be conducted for the comparative analysis with next ascending step cyclic loading testing results. The testing programs are as follows: apply the confining pressure to design value, with the loading rate of 0.25 MPa/s; apply axial loading until the granite specimen is completely damaged; the axial loading is controlled by deformation at 0.024 mm/min. The stress and strain data were recorded during the whole testing process. The testing results are listed in Table 2.

Secondly, to evaluate the effect degree of cyclic loading on the rock strength and to confirm the initial value of next ascending step cyclic loading tests, two kinds of cyclic loading tests up to 20% peak strength and 40% peak strength were implemented. A large number of studies showed that the ratio of crack initiation stress to peak stress is about or a little bigger than 40% peak strength [3], so the 40% cyclic loading tests could give an approximate threshold of ascending step cyclic loading tests. For the 20% cyclic loading test, its results can verify whether specimens in 40% cyclic loading test are always in the elastic stage. The testing programs are as follows: apply the confining pressure to design value, with the loading rate of 0.25 MPa/s; apply axial loading to a certain value (about 20% $\sigma_p$ or 40% $\sigma_p$) with the loading rate of 0.5 kN/s; unload to 2 MPa at the same rate (0.5 kN/s); repeat the above cyclic steps 5 times for one sample and record the stress and strain data during the whole testing process. The loading process is shown in Figure 5(a). The testing data is listed in Table 3.

Thirdly, based on the above confirmed initial range of the elastic stage, the ascending step cyclic loading tests were conducted, to determine the accurate initial damage point of deep granite. In the increasing process of loading, if the endpoint of two cyclic curves is different, it is considered that the samples are damaged. The detailed testing program is as follows: apply the confining pressure to design value, with the loading rate of 0.25 MPa/s; apply axial loading from about 40% $\sigma_p$, with the loading rate of 0.5 kN/s; unload to 2 MPa at the same rate (0.5 kN/s); repeat this cyclic loading process with ascending axial loading (about 42%, 44%, 46% $\sigma_p$, …, respectively), as shown in Figure 5(b); in this cyclic process, monitor the stress and strain data; if the end point of two cyclic process are different, apply axial loading with 0.024 mm/min, until the granite specimen is completely damaged. The detailed testing data is listed in Table 4.

3. Testing Results and Data Analysis

After the triaxial compression tests under three confining pressures (10 MPa, 20 MPa, and 30 MPa), the stress-strain curves are shown in Figure 6.

The triaxial compression strength of deep granite samples can be acquired from Figure 6. The detailed values are shown in Table 2. And, the typical corresponding AE data was shown in Figure 7. After data analyzing, the initial crack stress thresholds are 153 MPa, 186 MPa, and 215 MPa for the confining pressure of 10 MPa, 20 MPa, and 30 MPa, respectively.

In addition, by analyzing the stress-strain curves, the elasticity modulus can also be calculated following the method in Figure 8. Here, the elasticity modulus values are 73.06 GPa, 76.35 GPa, and 78.94 GPa, respectively, with computational formula in the ISRM suggestion method [6]:

$$E = \frac{\sigma_{l,\text{begin}} - \sigma_{l,\text{end}}}{\epsilon_{l,\text{begin}} - \epsilon_{l,\text{end}}}$$

where $E$ is the elasticity modulus, $\sigma_{l,\text{begin}}$ and $\sigma_{l,\text{end}}$ are the beginning and ending values of stress in linear stress-strain curve segment, and $\epsilon_{l,\text{begin}}$ and $\epsilon_{l,\text{end}}$ are the beginning and ending values of strain in linear stress-strain curve segment.

The triaxial compressive tests provide basic mechanical parameters of granite samples. Following the testing program in Table 3 and Figure 5(a), 6 groups of loading and
unloading tests with 20% \( \sigma_P \) and 40% \( \sigma_P \) fixed values and 10 MPa, 20 MPa, and 30 MPa confining pressures were carried out. Here, the typical stress-strain curves are drawn in Figure 9.

As exhibited in Figure 9, after 5 times loading and unloading process cycles, for all testing conditions, the unloading curves all show good overlap, which means there is not any fatigue damage after 5 cycles, and the whole testing processes are all under elastic status. It also indicates that the initial damage point of granite must occur over 40% \( \sigma_P \). These tests' results give guidance for the next ascending step cyclic tests.

After confirming the approximate range of initial damage point, 3 groups ascending cyclic loading tests were carried out, with loading conditions over 40% \( \sigma_P \). After the test, the stress and strain curves of step cyclic loading tests with different confining pressure could be obtained. Taking 10 MPa confining pressure testing data as example, the data processing step is shown in Figure 10.

As shown in Figure 10, based on the testing data, the step cyclic loading curve of stress and strain could be fitted and is shown in Figure 10(a). During the step cyclic loading tests, if the two unloading curves begin to separate, meaning that the input energy supplied by MTS 815 testing system is consumed by the rock samples, it can be assumed that the granite sample begins to enter damage status from this stress. So, the unloading curve which begins to separate was the target unloading curve (the pink curve in Figure 10(b)); also, the corresponding loading curve could be found (the red curve in Figure 10(c)). To acquire accurate damage threshold, the key segment data of target loading curve was obtained and fitted separately, as shown in Figure 10(d). In Figure 10(d), since the rock sample began to damage, the stress-strain curve would no longer be linear; there would be a turning point, which is the initial damage point. Under 10 MPa confining pressure, the turning point appears at 147 MPa stress value.

Other stress-strain curves with 20 MPa and 30 MPa confining pressure are illustrated in Figures 11(a) and 11(b), respectively.
From Figures 10 and 11, the peak strengths under different confining pressure are 311 MPa, 408 MPa, and 472 MPa, which are almost the same with that of the aforementioned triaxial compression testing results (328 MPa, 402 MPa, and 461 MPa, as shown in Figure 6). The slight errors maybe produced by the instrument, testing process, or different granite samples. These good verified results also testify that the cyclic loading process produce no effect on the strength characteristics of granite. After calculation with the method shown in Figure 10, the initial damage stress thresholds confirmed by cyclic tests are shown in Table 5. The initial damage points are 47.2% $\sigma_P$ for 10 MPa, 44.4% $\sigma_P$ for 20 MPa, and 43.8% $\sigma_P$ for 30 MPa, respectively.

4. Discussion

The initial damage points confirmed by the step cyclic loading method show that the turning stress of initial damage is about 45% peak strength on average. It is similar to the crack initiation thresholds for shale by Li et al. [9] and Beishan granite by Zhao et al [22] confirmed by the AE...
And, the testing result in this paper presents a little decrease with the increasing of confining pressure. To verify and analyze the step cyclic testing data, the AE testing results are also listed in Table 5.

As shown in Table 5, the stress values determined by two testing methods (initial damage stress by cyclic test and initial crack stress by the AE method) are not far apart under the same confining pressure, and the percentage of difference is below 5%. However, the results confirmed by cyclic loading tests have much clearer physical meaning and less error of the combination of two instruments. Therefore, the cyclic testing method has more credibility than the AE monitoring method.

![Stress-strain curves under three different confining pressures.](image)

**Figure 6:** Stress-strain curves under three different confining pressures.

![Typical AE monitoring data and stress-strain curve.](image)

**Figure 7:** Typical AE monitoring data and stress-strain curve: (a) AE monitoring data and stress-strain curves; (b) AE data and corresponding initial crack stress thresholds.

![Schematic diagram for elasticity modulus calculation.](image)

**Figure 8:** The schematic diagram for elasticity modulus calculation.
Figure 9: Typical stress-strain curves under different fixed values and confining pressures: (a) 20%σP and 10 MPa; (b) 40%σP and 10 MPa; (c) 20%σP and 20 MPa; (d) 40%σP and 20 MPa; (e) 20%σP and 30 MPa; (f) 40%σP and 30 MPa.
Figure 10: Data processing step of damage threshold with 10 MPa confining pressure: (a) the stress-strain curves in ascending step cyclic loading under 10 MPa confining pressure; (b) target unloading curve evaluated process; (c) target loading curve evaluated process; (d) initial damage point evaluated process.
5. Conclusions

The initial damage point of rock is an important parameter in rock-based engineering. In this paper, by employing a series of scientific laboratory tests, a much more accurate and intuitive initial damage point of deep granite from Sanshandao Gold Mine was confirmed, which provides a new method and scientific data for the study on rock mechanics in deep mining.

Through triaxial compression tests, the peak strength, elasticity modulus, and other basic mechanical parameters of granite samples were acquired. On this basis, cyclic loading tests with 20% peak strength and 40% peak strength were carried out. Results show that, under these stress conditions, all the specimens are under elastic status, and the initial damage point of granite must occur over 40% \( \sigma_P \).

Finally, taking advantage of ascending step cyclic loading tests, the accurate initial damage points of deep granite were acquired. The exact values are 47.2% \( \sigma_P \) for 10 MPa, 44.4% \( \sigma_P \) for 20 MPa, and 43.8% \( \sigma_P \) for 30 MPa, respectively. The testing results show that the turning stress of initial damage is about 45% peak strength on average, and it presents a little decrease with the increasing of confining pressure.

Data Availability

All data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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