Dynamics of surface evolution in semiconductor thin films grown from a chemical bath

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Dynamics of surface evolution in CdS thin films grown by chemical bath deposition technique has been studied from time sequence of atomic force micrographs. Detailed scaling analysis of surface fluctuation in real and Fourier space yielded characteristic exponents $\alpha_{loc} = 0.78 \pm 0.07$, $\alpha = 2.20 \pm 0.08$, $\alpha_s = 1.49 \pm 0.22$, $\beta = 0.86 \pm 0.05$ and $\beta_{loc} = 0.43 \pm 0.10$, which are very different from those predicted by the local growth models and are not related to any known universality classes. The observed anomalous scaling pattern, characterized by power law scaling dependence of interface width on deposition time differently at local and global scale, with rapid roughening of the growth front has been discussed to arise as a consequence of a nonlocal effect in the form of diffusional instability.

Recent developments in scaling invariance and universality have led to a growing interest in kinetic roughening theory with special attention being paid to studies on roughness evolution in thin films grown under far-from-equilibrium conditions\(^1\)\(^-4\). The study of evolving surfaces provides insight to the fundamental growth dynamics and enables one to control the roughness of the films. Such a study is of high technological relevance in that roughness of thin films in multilayer structures affects electrical, optical, mechanical and catalytic properties, and hence, determines the eventual performance of devices\(^5\)\(^-7\).

Typically roughness of a surface evolves as a consequence of simultaneous atomic scale processes such as direct addition of atoms on the growing surface from the surrounding, removal of atoms from the surface and motion of atoms along the surface or diffusive mass transport due to an existing or increasing chemical potential gradient\(^8\). The surfaces in many non-equilibrium growth models such as random surface recrystallization in the Eden model or ballistic aggregation are self-affining fractal which are described by the Kardar–Parisi–Zhang (KPZ) equation\(^9\)

$$\frac{\partial h(x, t)}{\partial t} = \nu \nabla^2 h(x, t) + \frac{\lambda}{2} |h(x, t)|^\beta + \eta$$

where $\nu$ accounts for the surface tension, $\lambda$ is an "excess velocity" in the growth, and $\eta$ is white noise. The self-affine patterns that the film surfaces develop into can be analyzed by the scaling properties of the surface fluctuations\(^10\). A number of applications of the KPZ equation were suggested based on the comparison of scaling exponents of surface roughness\(^1\).

The self-affine roughness is widely characterized by engaging it to a dynamic scaling form wherein the root mean square of the fluctuations of the surface height i.e. the interface width $w$ defined as $w(r, t) = \langle |h(r, t) - \langle h(r, t) \rangle|^\beta \rangle^{1/\beta}$, where $h$ is the surface height and $\langle \ldots \rangle_w$ is spatial averaging in a system of size $L$ and $r \leq L$, evolves following a simple dynamic scaling known as Family–Vicsek relation:

$$w(r, t) = t^{\alpha} f \left( \frac{r}{t^{\beta}} \right)$$

where the scaling function behaves as $f(u) = \text{constant}$ and $u^\alpha$ for $u \gg 1$ and $u \ll 1$, respectively, $\alpha$ and $\beta$ are the roughness and growth exponents respectively. The set of exponents corresponds to a specific universality class and is suggestive of the underlying mechanism that governs the evolution of roughness. Equation (2) suggests that for small $r$ (i.e. $r \ll t^{\beta_0}$), $w$ is independent of deposition time $t$ and scales as $r^\beta$, and independent of $r$ for large $r$ when it scales as $t^\beta$. The crossover between these two behaviors occurs at $r = \xi$, the lateral correlation length.

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which signifies the distance at which the surface features are no longer correlated. The correlation length scales as
\[ \xi \sim t^{1/z} \]
where the dynamic exponent is defined as \( z = \alpha/\beta \).

Although the roughening process during growth of thin films is microscopically diverse and complex in nature, a number of studies on growth of thin films have revealed that the interface roughness follows the Family-Vicsek scaling ansatz. However, in recent years, many experimental and theoretical studies have reported scaling patterns very different from that predicted by the Eq. (2)\(^{11-22}\). In such cases, growth models with different exponents at long (global/saturated) and short (local) length scales have been suggested. While the global width \( w(L,t) \) still follows the Family-Vicsek scaling relation (Eq. (2)), the local width is represented by the anomalous scaling ansatz:

\[
w(r, t) = \begin{cases} 
t^{\beta*} r^\alpha_{\text{loc}}, & \text{if } r \ll \xi \ll L \\
t^\beta, & \text{if } r \gg \xi 
\end{cases}
\]

where \( \alpha_{\text{loc}} \) is the local roughness exponent and \( \beta* \) is the anomalous growth exponent indicating the time dependence of the local width at length scales smaller than \( \xi \) and is given by \( \beta - \beta_{\text{loc}} = (\alpha - \alpha_{\text{loc}})/z \). The time dependence of \( w(r, t) \) through the term \( t^{\beta*} \) is the crucial signature of the anomaly in the scaling behaviour.

Although extensive studies have been carried out, the understanding of the surface dynamics of thin films is far from complete, as evident from the wide scatter in the experimentally determined scaling exponents for a given technique\(^4\). In particular, growth mechanisms in films by chemical bath deposition (CBD) technique on the lines of the dynamic scaling theory has not been explored, in spite of the fact that the CBD has been established as one of the most preferred techniques for cost effective large area deposition of semiconductor thin films\(^{23}\). This work is the first ever study of dynamics of surface evolution in compound semiconductor thin films grown by the CBD film.

We have investigated roughening of CdS thin films which were grown from an ammonia free chemical bath. Over the years, CdS thin films have emerged as a binary semiconductor of high technological importance and have found applications in photovoltaics, lasers, non-linear optical devices, etc\(^{24-26}\). Using the kinetic roughening analysis, we show an anomalous scaling pattern of the growth front of the chemical bath deposited CdS films. It is expected that this work will provide important clues for the complex changes of kinetic roughening that occur during the formation of CBD thin films.

**Results and Discussion**

Figure 1 shows typical surface morphology of the films of increasing deposition times. A granular structure with even sized grains, typical of polycrystalline thin films is observed at all stages of film growth. From the images, both surface roughening and coarsening process are evident, which is supported from the time sequences of scanned profile of the surfaces wherein the vertical and lateral stretch of the particles increased with the increase in deposition time.

The growth dynamics and whether roughening of the growth front follows any scaling pattern were assessed from the height-height correlation function \( G(r, t) \) defined as \( G(r, t) = \langle (h(\mathbf{r}, t) - \langle h(\mathbf{r}, t) \rangle)^2 \rangle \) for each film, which are presented in Fig. 2. \( G(r, t) \) shows a power law dependence on \( r \) for small length scales and remains saturated at large \( r \) values for films of varying deposition times. More importantly, the curves were up-shifted as deposition time increased at all length scales. This, however, is in contrast with the systems following the Family-Vicsek relation, wherein \( G(r, t) \sim [w(r, t)]^2 \) exhibit behaviors typical of self-affine interfaces: \( G(r, t) \) scales as \( G(r, t) \sim r^{\beta*} \) for \( r \ll \xi \) and becomes constant for \( r \gg \xi \). The up-lifting of the curves at small length scales indicates

![Figure 1. 2μm × 2μm AFM images of CBD CdS thin films grown under identical experimental conditions for different durations and the corresponding line profiles across the scan areas.](image-url)
the time dependence of $G(r, t)$ and hence, the anomaly in the scaling pattern. Consequently, $G(r, t)$ is expected to follow the scaling relation as given in Eq. (3), i.e.,

$$G(r, t) = \begin{cases} r^{2+\beta z} & \text{if } r \ll \xi \\ t^{2z} & \text{if } r \gg \xi \end{cases}$$

(4)

The dynamic exponent $z$ was estimated from the time dependent variation of the correlation length $\xi$, which was accurately determined from the relation $\Gamma(r = \xi)/\Gamma(r = 0) = e^{-1}$ after computing the auto-correlation function $\Gamma(r, t)$ from the AFM images corresponding to different deposition times (not shown here)\textsuperscript{27}. The plot of the variation of $\xi$ with deposition time (Fig. 3(a)) reveals the scaling of $\xi$ as $\xi \sim t^{1/z}$ with $1/z = 0.46 \pm 0.06$. The global and local surface widths were estimated from the height-height correlation functions as per Eq. (4) and are shown as function of deposition time in Fig. 3(b). Both global and local surface widths show a power-law dependence on growth time, typical of anomalous dynamic scaling patterns. The least-square linear fits to the data points yield that the
global surface width grew with $\beta = 0.86 \pm 0.05$, much faster than the random deposition limit of stochastic roughening ($\beta = 0.5$). The local surface width, on the other hand increased less rapidly at $\beta_{loc} = \beta - \beta^* = 0.43 \pm 0.10$. The fact $\beta^* \neq 0$ confirms the anomalous scaling pattern in the system. The global roughness exponent $\alpha = \beta z$ is calculated to be $1.87 \pm 0.35$. The observed rapid roughening of the CBD film surface characterized by a high $\beta$ value is similar to the cases of films grown by sputtering22.

The consistency of our analysis was verified by collapsing the height-height correlation functions obtained for films of different growth times. As Eq. (4) indicates, the plot of curves $G(r, t)/r^{2\alpha}$ versus $t^{\beta/\alpha}$ for all growth times should collapse, with the slopes in small and high arguments being equal to $m_1 = -2(\alpha - \alpha_{loc})$ and $m_2 = -2\alpha$, respectively. We show in Fig. 4 that all data points collapse into a single curve confirming the integrity of the general dynamic scaling theory as given in Eq. (4). The slope of the curve in small and high arguments was found to be $m_1 = -2.36$ and $m_2 = -3.79$, respectively. It is noted that $m_1 \neq 0$ implies $\alpha \neq \alpha_{loc}$ and therefore, the anomalous scaling behavior in our system. Using the values of $m_1$ and $m_2$, $\alpha_{loc}$ was calculated to be 0.69, which is close to the value $0.78 \pm 0.07$ calculated from the slope of the $G(r, t)$ vs $r$ curves (Fig. 2) for $r \ll \xi$ as per Eq. (4).

More insight into the dynamics of the roughening process in our system was gained from the plot of the power spectral density (PSD) functions for films of different deposition times, as shown in Fig. 5. All PSD curves show two distinct regimes: the power law $k$ dependence in the high-$k$ regime crosses over to a $k$-independent regime at
led to rapid roughening of the surfaces (i.e., with a high $\beta$). Films, shadowing arising due to the angular spread of the impinging particles works as a nonlocal effect, which indicates a new class and electrodeposition techniques, the obtained values of the exponents indicate significant deviation from classes based on local growth models, suggesting that nonlocal effect plays an important role in the evolution of growth front of the chemical bath deposited thin films. In the light of previous studies on electroless and electrodeposited films, the present results indicate that nonlocal effects in the form of diffusional instability should be incorporated in the models to further our understanding of growth mechanism of the films.

**Methods**

The precursor solution was prepared by sequential addition of 25 ml of 0.1 M cadmium chloride (Loba Chemie, India, 99.0%), 20 ml of 1 M sodium citrate (Loba Chemie, India, 98.0%), 5 ml of 1 M potassium hydroxide (Loba Chemie, India, 85.0%) and 20 ml of buffer (NaOH) pH = 10 (Loba Chemie, India, 98.0%) in a beaker. The solution was added with DI water to complete a total volume of 90 ml. The bath temperature was increased from room temperature and after reaching a bath temperature of 40 °C, 10 ml of 1 M thiourea (Loba Chemie, India, 99.0%) was added. The deposition temperature was maintained at 40 °C. The glass substrate was kept vertical in the beaker. A homogeneous layer with dark yellow color and with good adhesion to substrate of thicknesses depending on deposition time was obtained. After the deposition, the films were taken out of the bath and washed in DI water ultrasonically to remove the loosely adhered particles on the film and finally dried in air.

The surface topography of the films were studied in detail by atomic force microscopy (AFM) using a NT-MDT-NTEGRA PRIMA system. The images were acquired in air at room temperature in tapping mode of operation and at 256 × 256 pixels. Images were recorded at least at four different points on the sample surfaces and the results were consistent.

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Author Contributions

I.G. performed the experiments including sample preparation and AFM measurements, contributed in analyzing the results and writing the manuscript. B.C.M. supervised this study, designed theoretical and experimental strategies, and contributed in analyzing/interpreting experimental data and in writing the manuscript.

Additional Information

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