A STATISTICAL STUDY OF TRANSVERSE OSCILLATIONS IN A QUIESCENT PROMINENCE

A. Hillier 1 , R. J. Morton 2 , and R. Erdélyi 3

1 Kwasan and Hida Observatories, Kyoto University, Kyoto 607-8471, Japan; andrew@kwasan.kyoto-u.ac.jp
2 Mathematics and Information Science, Northumbria University, Pandon Building, Camden Street, Newcastle upon Tyne NE1 1ST, UK
3 Solar Physics and Space Plasma Research Centre (SP 2 RC), University of Sheffield, Hicks Building, Hounsfield Road, Sheffield S3 7RH, UK

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ABSTRACT

The launch of the Hinode satellite has allowed for seeing-free observations at high-resolution and high-cadence making it well suited to study the dynamics of quiescent prominences. In recent years it has become clear that quiescent prominences support small-amplitude transverse oscillations, however, sample sizes are usually too small for general conclusions to be drawn. We remedy this by providing a statistical study of transverse oscillations in vertical prominence threads. Over a 4 hr period of observations it was possible to measure the properties of 3436 waves, finding periods from 50 to 6000 s with typical velocity amplitudes ranging between 0.2 and 23 km s⁻¹. The large number of observed waves allows the determination of the frequency dependence of the wave properties and derivation of the velocity power spectrum for the transverse waves. For frequencies less than 7 mHz, the frequency dependence of the velocity power is consistent with the velocity power spectra generated from observations of the horizontal motions of magnetic elements in the photosphere, suggesting that the prominence transverse waves are driven by photospheric motions. However, at higher frequencies the two distributions significantly diverge, with relatively more power found at higher frequencies in the prominence oscillations. These results highlight that waves over a large frequency range are ubiquitous in prominences, and that a significant amount of the wave energy is found at higher frequency.

Key words: magnetohydrodynamics (MHD) – Sun: filaments, prominences – waves

Online-only material: color figure

1. INTRODUCTION

Prominences are cool (~10,000 K—Tandberg-Hanssen 1995), dense structures (3–6×10¹⁸ cm⁻³—Hirayama 1986) that are observed in the corona above the limb. On disk, prominences are observed as dark absorption structures called filaments. To support the dense prominence material above the solar surface against gravity, classically it has been the curvature of the magnetic field, creating an upward directed magnetic tension force, that is invoked to counteract the gravitational force (Kippenhahn & Schlüter 1957; Kuperus & Raadu 1974).

There has been a long history of observation of periodic phenomena in both filaments and prominences (e.g., Moreton & Ramsey 1960). We focus here on the transverse displacement of the fine-scale threads that make up the prominence, although longitudinal motions are also well-documented (Vršnak et al. 2007; Tripathi et al. 2009). Typically, the observed transverse waves are separated into two categories: large-amplitude and small-amplitude oscillations (Oliver & Ballester 2002; Arregui et al. 2012). The large-amplitude oscillations are characterized as being excited by a flare blast wave, generally with velocity amplitudes >20 km s⁻¹ (Okamoto et al. 2004; Isobe et al. 2007; Hershaw et al. 2011; Gosain & Foullon 2012). The large-amplitude waves typically show damped sinusoidal motion, similar to that seen in flare-excited kink waves in coronal loops (e.g., White & Verwichte 2012).

The small-amplitude waves (velocity amplitudes ≤10 km s⁻¹; e.g., Okamoto et al. 2007; Lin et al. 2007, 2009; Berger et al. 2008; Schmieder et al. 2010), in contrast, are assumed to be unrelated to flaring activity, although the mechanism(s) that excites these waves still remains a mystery. Ning et al. (2009) suggested that the observed waves could be driven by the three and five minute oscillations typically associated with acoustic/slow magnetohydrodynamic (MHD) perturbations in the photosphere and low corona. This suggestion was made as the observed periods were in the range 210–525 s. However, the authors only provide details of 13 periodic waves, so it is hard to draw any conclusions about the excitation mechanism from such a small number of events.

One mechanism that is frequently suggested for the excitation of transverse waves is the convective motions of photospheric granules. However, the focus is usually directed toward the heating of the solar atmosphere or solar wind acceleration (e.g., Cranmer & van Ballegooijen 2005). Wave excitation by convective motions is occasionally named as being a source of the filament/prominence waves (e.g., Engvold 2008) but, to the best of our knowledge, this idea does not seem to have pursued further. It would be a logical way to excite the waves and is pervasive in models for generating transverse waves in the chromosphere/corona (e.g., Cranmer & van Ballegooijen 2005; Matsumoto & Shibata 2010; Fedun et al. 2011; Vigeesh et al. 2012).

In this Letter, we provide the first statistical study of small-amplitude transverse waves in a quiescent prominence. The measurements allow for the determination of frequency dependent trends in wave properties and for the derivation of the associated velocity power spectrum for the transverse waves. The implications in terms of excitation mechanisms, and the potential role of waves in prominence dynamics are discussed.

2. OBSERVATIONS AND ANALYSIS OF THREAD OSCILLATIONS

2.1. Hinode SOT Hα Observations

The data was obtained by the Hinode Solar Optical Telescope (SOT; Suematsu et al. 2008) on 2007 August 8 between
To observe the transverse displacements of the prominence threads, a total of 21 slits, of length 54 arcsec, were placed horizontally over the prominence with a separation of 0.83 arcsec, apart from the topmost four slits that are spaced at double this separation. To increase the position accuracy of the slit pixels, the data pixels were divided into approximately three sub-pixels when constructing the slit. Examples of the slits are given in Figure 1. Stacking the individual slits in time, time–distance diagrams are constructed that show clearly sinusoidal transverse displacements of the threads with a range of periods and amplitudes (see, e.g., Figure 2).

To analyze the observed oscillatory motion in the time–distance diagrams, we locate and track the center of the threads using a technique similar to that described in Morton et al. (2013a). For each time-slice of each slit, any time series of peaks that contains 20 points or more is kept, the rest are discarded. The time series for the peaks of each thread are compared to the time–distance diagrams to remove any false positives. Further, the data is checked to see if any two time series trace the same thread and can be joined together. Any gaps in the time series are filled by linearly interpolating between the data points at the beginning and end of the gap and finding the peaks closest to the interpolated line.

An example time–distance diagram is shown in panel (a) of Figure 2, with the over-plotted black lines showing the traced threads. To highlight the threads and their transverse motions, panel (b) shows an unsharpened mask version of the data in panel (a). Running this routine on the 21 slits, the temporal evolution of a total of 3141 sections of the vertical threads of the prominence were traced. It should be noted that we use the phrase “sections of the vertical threads” because it is not possible to trace all threads for the duration they appear in the time–distance plots because of ambiguities that result from the crossing of two threads.

2.3. Fitting of Oscillations

Before performing a sinusoidal fit to the data, it is necessary to remove any trends. To do this, the data is split into its intrinsic mode functions using empirical mode decomposition (EMD; e.g., Terradas et al. 2004). This method can be viewed as a multi-pass filter that empirically decomposes the time series data into separate frequency bands. The lowest frequency component of an oscillation is subtracted from the time series, removing the trend from the data. The highest frequency fluctuations are also removed under the assumption that they are created by noise. This process limits the smallest fluctuations that can be fit to periods of \( \geq 50 \) s.
Figure 2. Results of the wave tracking routine. Panel (a) displays the time–distance diagram for slit number 17 (counting from the bottom slit in Figure 1) with the over-plotted black lines showing the position of the traced threads. Panel (b) shows an unsharp masked view of the same slit. The threads and their associated transverse motions are clearly evident.

Figure 3. Panels (a-i) to (d-i) display four examples of threads with their centers traced by black lines (dashed lines show the trend of each thread found through application of EMD). The panels (a-ii) to (d-ii) show plots of the detrended curve (solid line), the fit to the initial curve (dashed line) and a combination of the original fit and the residual fit (dot-dash line). Any remaining oscillations present are fitted using the following function:

$$F(t) = A_0 \exp\left(\frac{2\pi t}{P_0(1 + Ct)} + S\right),$$

where $A_0$ is the initial displacement amplitude of the oscillation, $\tau$ is the amplification/damping time, $P_0$ is the initial period, $C$ is the linear increase/decrease of the oscillation period and $S$ is the phase. This fitting function has been employed by Gosain & Foullon (2012), where the term allowing the change in period with time was found to be of importance in accurately determining the period of oscillations. Four examples of threads that have been fitted are shown in Figure 3. The velocity amplitude of the transverse waves is calculated using $V = 2\pi A_0 / P_0$.\hfill 3
3. STATISTICS OF TRANSVERSE PROMINENCE OSCILLATIONS

Using the techniques described in the previous section, a total of 3436 oscillations each of more than one and a half periods were analyzed. The accumulated statistics for the displacement amplitude, period and velocity amplitude are displayed in histograms in Figure 4. The waves have displacement amplitudes ranging from 19 to 1400 km, periods of 50–6000 s, and velocity amplitudes of 0.2–23 km s$^{-1}$. The histograms also reveal that measured events are dominated by the waves with displacement amplitudes <200 km, periods <300 s, and velocity amplitudes <5 km s$^{-1}$. The histogram for the frequency of events for different velocities shows that the peak frequency occurs at approximately $V = 1–2$ km s$^{-1}$.

Figure 5 shows plots of (a) the displacement amplitude against the period, (b) the velocity amplitude against the period, and (c) the synthesized velocity power spectrum density ($V(v)^2/v$) as a function of frequency ($v = 1/P$). In panels (a) and (b) the contour plot shows the density of the results, with the plus marks showing the positions of the outliers in regions with few points. For panels (a) and (b) the straight lines show fitted power laws. The power laws found are (a) $A_0 = 10^{0.93±0.02} P_0^{0.74±0.04}$ and (b) $V = 10^{0.96±0.02} P_0^{0.25±0.04}$. The observations and the analysis technique come with constraints on the minimum period (50 s) and minimum displacement amplitude (19 km) we are able to measure. These constraints also affect the minimum measurable velocity amplitude. The respective constraints are over-plotted in each plot (dash triple dot).

The data points plotted in Figure 5(c) were obtained by binning the data into log-frequency bins of width log $v$ ∼ 0.15. Any bin with less than 30 events was amalgamated with a neighboring bin. The data for each frequency bin was binned into log-power spectrum bins, the size of the bin was varied to some degree due to the different number of events in each frequency bin but was generally kept to be approximately 0.15. The histogram of the binned power spectrum density for each frequency bin was then fitted with a Gaussian distribution, with the central peak of the Gaussian distribution taken as the center of the probability density function of the data. The errors bars show two times the standard error of the fit (i.e., $σ/\sqrt{N}$ where $σ$ is the standard deviation of the results and $N$ is the number of bins). The position of the data points along the frequency axis and the range (horizontal bars) were determined by the mean and the standard deviation of the data points in the frequency bin.

Figure 4. Histograms showing the frequency as a function of displacement amplitude ($A_0$), period ($P_0$) and velocity amplitude ($V$). All histograms are plotted with a log-log scale to allow the ranges to be clearly observable. Only oscillations that display >1.5 periods are included in the analysis.

The Gaussian distribution provides a very good representation of the distribution of the power spectrum density in each frequency bins, implying that the data is log-normally distributed. The triple dot-dash lines show the observational limits of the study.

Perhaps most interestingly, in Figure 5(c), we over-plot the measured photospheric power spectra derived from granulation (solid line—Matsumoto & Kitai 2010—multiplied by a factor of $10^{1.1}$) and from magnetic bright point motions (dashed line—Chitta et al. 2012—multiplied by a factor of $10^{1.4}$), which have been shown to correspond to the motion of concentrations of magnetic flux both observationally (e.g., Berger & Title 1996) and numerically (e.g., Schüssler et al. 2003; Shelyag et al. 2004). Note, the photospheric velocity power is scaled upward to allow for a direct comparison. The difference in magnitude of velocity power between the photosphere and the prominence is a reflection on the increase in velocity amplitudes of waves with height, namely due to lower values of magnetic field strength and density in the prominence than in the photosphere, i.e., the increase in Alfvén speed.

The distribution of the synthesized power spectrum for the prominence waves and the observed photospheric power spectra show a number of similarities and differences. The power distribution for low-frequency waves can be seen to closely follow the photospheric power spectra, although, for higher frequencies (greater than 7 mHz), the distributions diverge.

4. IMPLICATIONS FOR PROMINENCE ENERGETICS

We present here the largest study to date of transverse waves supported by vertical quiescent prominence threads in a single prominence, measuring 3436 periodic motions, which allows us to draw general conclusions about the properties of transverse waves in prominences. First, we can confidently state that both the displacement amplitude and velocity amplitude are functions of period. The variation in displacement amplitude and velocity amplitude with period appear to qualitatively agree with results found from large-scale studies of transverse waves in chromospheric fibrils (Morton et al. 2013a, 2013b).

Second, and perhaps most interestingly, we can hypothesize about the excitation mechanism of the prominence waves. The horizontal motions of the photosphere has long been conjectured to be the driver of incompressible waves including prominence waves, however, no direct evidence of this has been provided by observations. In Figure 5(c) we compare the velocity power spectrum of the observed transverse oscillations.
with the velocity power spectrum of horizontal photospheric granular motions and horizontal magnetic bright point motions. There are also slight differences between the power spectra derived in Matsumoto & Kitai (2010) and Chitta et al. (2012), e.g., magnitudes of the velocity power, but the profile is very similar. After scaling the photospheric distributions, it is clear that the velocity power spectrum of the prominence waves correlates well with the photospheric power spectra for \( f < 7 \) mHz. We suggest this result provides evidence for the horizontal motions being the driver of prominence waves. However, further information (e.g., study of phase spectra) is required to attribute full causality to the horizontal motions. There is no evidence for enhanced power at three or five minutes, potentially ruling out \( p \)-modes as the main driving mechanism.

One further interesting point of note is that the prominence waves show greater velocity power in the high-frequency range than the photospheric spectra. A similar result was found for the analysis of fibrils in the solar chromosphere by Morton et al. (2013b), implying that the position of the break in the power law (found to be approximately 5 mHz in Matsumoto & Kitai 2010) could be at higher frequencies in many cases or that the chromosphere processes the energy in such a way that the higher frequency component is enhanced relative to the lower frequency component. Either way, the existence of the relatively enhanced power at high frequencies should be of great interest for studying the transport of energy by waves from the photosphere to the corona. We note that the results in this Letter cannot rule out that local instabilities in a prominence, e.g., the convective continuum instability (Blokkland & Keppens 2011), driving some of the observed prominence oscillations.

The prospect that the photospheric motions are driving the observed prominence waves raises a number of questions regarding wave propagation through the lower solar atmosphere. What causes the deviation from the photospheric power spectra at higher frequencies, be it an enhancement at higher frequencies or a sink reducing the power at lower frequencies, and why the power of the velocity power spectra for frequencies \(<7 \) mHz remains unaffected after propagation through the chromosphere both need to be understood. Studies show that wave spectra can be modified due to mode conversion (e.g., Carlsson & Bogdan 2006; Fedun et al. 2011) at altitudes where the plasma \( \beta \) equals unity or due to reflection from strong gradients in plasma quantities present in the transition region (e.g., Cranmer & van Ballegooijen 2005; Fedun et al. 2011). However, the physical processes involved are complex, meaning simulations of wave propagation from the photosphere to the prominence are likely required to answer such questions.

Finally, we pick up on a comment by van Ballegooijen & Cranmer (2010) related to prominences, namely, “Others have suggested that . . . the plasma is supported by MHD waves. However, relatively high frequencies and wave amplitudes are required, and it is unclear why such waves would not lead to strong heating of the plasma.” Here we demonstrate that the prominence plasma does indeed support numerous MHD waves over a wide frequency range, with velocity power comparable to those seen in chromospheric fine structure (Morton et al. 2012), who suggest that the chromospheric waves have an energy flux capable of maintaining a heated atmosphere. The following questions then naturally arises: what happens to the wave energy observed in prominence fine-structure? If the MHD waves are suitable for the heating of the solar atmosphere, why does the prominence plasma not display evidence for strong heating? At present we cannot answer these questions but they are clearly a future challenge for that models of prominences should aim to answer.

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