Conflicting Bundles: Adapting Architectures Towards the Improved Training of Deep Neural Networks

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Abstract

Designing neural network architectures is a challenging task and knowing which specific layers of a model must be adapted to improve the performance is almost a mystery. In this paper, we introduce a novel theory and metric to identify layers that decrease the test accuracy of the trained models, this identification is done as early as at the beginning of training. In the worst-case, such a layer could lead to a network that can not be trained at all. More precisely, we identified those layers that worsen the performance because they produce conflicting training bundles as we show in our novel theoretical analysis, complemented by our extensive empirical studies. Based on these findings, a novel algorithm is introduced to remove performance decreasing layers automatically. Architectures found by this algorithm achieve a competitive accuracy when compared against the state-of-the-art architectures. While keeping such high accuracy, our approach drastically reduces memory consumption and inference time for different computer vision tasks.

1. Introduction

The training of deep neural networks is a complex and challenging task [8], one that can be achieved by better initialization strategies [4, 6], activation functions [3, 19], regularization methods [11, 26] and network architectures [7, 22, 27, 29]. Designing good architectures is still a mystery and often done through trial and error approaches or exhaustive grid searches. A test accuracy map is shown in fig. 1 for 176 different fully connected neural networks trained on Mnist. The expressivity of networks grows exponentially with depth [23, 24], but it can be seen that the optimal architecture w.r.t test accuracy that is also trainable depends on a good balance between width and depth [29]. Searching through many different architectures this way to find a good configuration is not an option for real-world applications as too many possible configurations exist and the time required to train and evaluate each alternative is usually too long [28]. We introduce the conflicting training bundle problem in this paper and we can prove theoretically and experimentally that conflicting bundles worsen the performance of neural network models. The red line in fig. 1 is a boundary that separates all models that are trained without conflicting bundles (below the line) and all models that induce conflicting bundles during training (above the line). We are able to locate layers that induce conflicting bundles already at the beginning of the training by evaluating only the deepest network for each width as we motivate later in the paper. Therefore, our method to find this boundary is computationally very cheap and the analysis of conflicting bundles will (1) help researchers to create new or improve state-of-the-art network architectures (2) help to create novel neural architecture search (NAS) algorithms and (3) explain effects from a new theoretical perspective and hopefully inspire new research. The problem that we discovered is described next.

Figure 1: Test accuracy of different neural networks trained on Mnist together with the boundary that separates networks that induce conflicting training bundles.
1.1. The conflicting training bundle problem

The output of a neural network is calculated by successively propagating inputs forward through all hidden layers. Those calculations are executed on a CPU or GPU and therefore, all output values of a layer are represented with finite resolution such as float32. Consequently, two outputs that are only slightly different (less than the minimum resolution of float), are equal on a CPU or GPU. We found that weights are adjusted in wrong directions during training, leading to a worsened overall performance of the model, if any hidden layer produces the same output vector for two input examples with different labels. Therefore, we call two samples bundled if the same output w.r.t. the floating point resolution is produced for both inputs after passing through some hidden layer of the network and conflicting if both samples are labeled differently. The layer that bundles the samples, called the conflicting layer, can be precisely determined and therefore architectures can either manually or automatically be adapted as we demonstrate in this paper.

1.2. Outline

In section 2, the theory of conflicting training bundles is introduced. We show theoretically that the accuracy decreases if conflicting bundles appear during training and that in the worst-case scenario the network cannot learn from data. In that same section, we introduce a novel metric to quantify and to detect the precise layer that produces conflicting training bundles. In the experimental section 3, we evaluate many different types of networks: Under tightly controlled settings conflicting training bundles are produced, and the effects are studied. Then, the evolution of conflicting bundles is studied for each training epoch and layer. Fully connected networks, VGG nets and ResNets are tested on different datasets. Finally, a novel NAS algorithm to tackle conflicting training bundles is introduced and compared against the best ResNet found through a grid search. A discussion and inspiration for future research are given in section 4.

1.3. Related work

Different optimization problems have already been the subject of study. LeCun et al. [16] has shown that careful initialization of the weights of neural networks has a significant effect on the training process. Methods to initialize weights avoid vanishing information during forward-propagation and also avoid vanishing- or exploding gradients during backward propagation [4, 6, 8, 14, 18]. Very deep networks are difficult to optimize, even when variance-preserving initialization methods are used [27]. Solutions to overcome this problem include highway networks [27] that allow for the unimpeded information flow across several layers, or residual learning [7] among others. Historical developments and optimization problems that can occur during the training of neural networks are extensively described and summarized by the seminal survey of Schmidhuber [25] and the book of Goodfellow et al. [5].

To the best of our knowledge, we are the first that precisely locate and quantify the conflicting training bundles problem. Nevertheless, a closely related work published by Kamimura and Takeuchi [12] describes that information of original input patterns is lost in higher layers by going through multiple layer transformations and compressions. They also claimed that convolutional neural networks do not suffer from this problem probably due to the high dimensionality of hidden features. In this paper, we study layers in the network hierarchy where as much information vanishes such that two different inputs are represented equally when passed through this layer. We also show that this problem indeed arises for convolutional neural networks that distinguish our paper clearly from the work of Kamimura and Takeuchi [12].

Another closely related work is from Balduzzi et al. [2] which proved that the correlation between gradients in fully connected networks with \( L \) layers decay exponentially with \( 1/2^L \). The correlation decreases only with \( 1/\sqrt{L} \) if residual connections are used. Therefore, they concluded that residual networks are easier to train than fully connected networks. Shattered gradients are independent of the width (theorem 1 of [2]) and therefore, the pattern shown in fig. 1 can not be fully described. On the other hand, we show in this paper that conflicting training bundles depend on the depth and the width. To ensure that conflicting bundles do not shutter gradients, we directly evaluate gradients in section 3.2. The fact that conflicting bundles occur for very shallow networks rules out the vanishing- or exploding gradients [9] and we conclude that this is a new type of problem. We also want to mention that related work mainly analyses gradients. Conflicting bundles are analyzed after each layer during forward-propagation which allows to precisely detect the layer that induces the problem.

2. A theory of conflicting training bundles

In this section, our theory of conflicting training bundles is introduced. The focus is on classification problems for simplicity, although the idea of conflicting training bundles can also be applied to e.g. regression problems. Let’s consider a training set \( S \in \mathcal{X} \times \mathcal{Y} \) that contains objects from a specific domain \( \mathcal{X} \) along with its labels \( \mathcal{Y} \). Labels \( y \in \mathcal{Y} \) are one-hot encoded and the dimensionality of labels is \( N_y \). If the input to a layer of a neural network is of dimension \( m \) and output of dimension \( n \), we use weight matrices \( W \in \mathbb{R}^{n \times m} \) and bias terms \( b \in \mathbb{R}^{n \times 1} \) to calculate the output. The output of a specific layer \( l \in \{1, \ldots, L\} \) for a network with \( L \) layers is a vector \( a^{(l+1)}(x_i) = f \left( W^{(l)} a^{(l)} + b^{(l)} \right) \) for some input
We call the bundle that contains conflicting samples is called a conflicting bundle.

2.1. Fully conflicting bundle

Networks are trained with fully conflicting bundles or conditions to derive the negative effects that arise when neural output layer is per definition not included.

In the non-linearity of some hidden layer bundled, if the same output is produced for both inputs after layer

Definition 1. Two samples \( x_i, x_j \in \mathcal{X} \) are bundled by layer \( l \), if \( a_i^{(l+1)} = a_j^{(l+1)} \) for the current configuration of learnable parameters.

Definition 2. Two samples \( x_i, x_j \in \mathcal{X} \) are conflicting, if \( y_i \neq y_j \) and there exists some layer \( l \in \{1, ..., L\} \) that bundles \( x_i \) and \( x_j \). We call layer \( l \) the conflicting layer for \( x_i \) and \( x_j \).

Two different input examples \( x_i \) and \( x_j \) are therefore bundled, if the same output is produced for both inputs after the non-linearity of some hidden layer \( l \) is applied. The output layer is per definition not included.

Definition 3. A bundle \( D^i_l \) contains all samples \( x \in \mathcal{B} \) that are bundled after layer \( l \) and the set of all bundles \( D^i = \{D^i_1, D^i_2, ..., D^i_L\} \) with \( 1 \leq k \leq |\mathcal{B}| \) ensure that \( \forall i \neq j : D^i_1 \cap D^i_2 = \emptyset \) and \( D^i_1 \cup D^i_2 \cup ... \cup D^i_L = \mathcal{B} \). A bundle that contains conflicting samples is called a conflicting bundle. We call the bundle \( D^i_1 \) of the special case \( D^i = \{D^i_1\} \) a fully conflicting bundle.

Per definition, a conflicting bundle contains at least two samples with different labels. A fully conflicting bundle contains all samples of a mini-batch and therefore all samples are conflicting. We will now make use of the definitions to derive the negative effects that arise when neural networks are trained with fully conflicting bundles or conflicting bundles in general.

2.2. Conflicting bundles

We now relax the assumption that a fully conflicting bundle occurs and study the gradient if some conflicting bundles occur (see definition 3):

\[
\frac{\partial J}{\partial W^{(L)}} = \frac{1}{|\mathcal{B}|} \sum_{D \in \mathcal{D}^L} \left( |D| h_D - \sum_{i=1}^{|D|} y_i \right) a_D^{(L)T}
\]

\[
= \frac{1}{|\mathcal{B}|} \sum_{D \in \mathcal{D}^L} \left( |D| h_D - \hat{y}_D \right) a_D^{(L)T}
\]

Compared to the fully conflicting bundle case, where labels disappeared, labels are still included in the calculation of the gradient. But it can also be seen that for the same output \( h_D \) different labels are grouped into a single \( \hat{y}_D \). Therefore, we assume that the effect of conflicting bundles is similar to the effect of noisy labels for which it is well known that the model performance is worsened \[11\]. This leads us to the following hypothesis that will be extensively evaluated in the experimental section 3.

Hypothesis 2. If conflicting bundles occur during training the performance of the trained model is worsened.

To check the correctness of hypothesis 1 and hypothesis 2 we have to be able to detect situations where conflicting bundles occur. Therefore, a metric to quantify conflicting bundles is introduced next.

\[1\] This assumption can be easily removed by shifting derivations.
2.3. Conflicting bundle metric

To measure whether two samples \(x_i\) and \(x_j\) are bundled by layer \(l\) we must check if \(a_i^{(l+1)} = a_j^{(l+1)}\) (definition 1). As already mentioned the finite resolution of floating point values must be considered when calculated on a GPU or CPU. Therefore, it makes a difference whether the vectors are used during forward- or backpropagation: During backpropagation, \(a_i\) vectors are scaled by the learning rate \(\alpha\) and \(1/|B|\) before they are subtracted from the weights. Therefore, it is possible that very small values that are different during forward propagation are bundled during backpropagation due to the finite resolution of floating point values.

To consider this, we approximate definition 1 with
\[
\frac{\alpha}{|B|} \|a_i^{(l+1)} - a_j^{(l+1)}\|_\infty \leq \gamma
\]
(1)
where \(\gamma\) is the currently smallest possible resolution that is supported by the floating-point representation of the GPU or CPU (\(\gamma \approx 10^{-8}\)). Note that eq. (1) depends only on the output of the layer such that this metric can be used for any type of layers such as fully connected, convolutional, pooling or others.

A bundle \(D_i^l\) (definition 3) is then the set of all vectors that are equal according to eq. (1). We are mainly interested in conflicting bundles and to quantify how conflicting a single bundle \(D_i \in D^l\) at training step \(t\) and layer \(l\) is, we make use of the entropy \(H^l(t, D_i)\) with:
\[
H^l(t, D_i) = -\sum_{n=1}^{N_c} p(n) \ln (p(n) + \epsilon)
\]
(2)
where \(p(n)\) represents the probability that samples of class \(n\) occur in bundle \(D_i\) and \(\epsilon\) is an arbitrarily small value ensuring numerical stability. The entropy \(H^l(t, D_i)\) is large if bundle \(D_i\) created by layer \(l\) contains many examples with different labels and \(H^l(t, D_i)\) is small if examples have the same label.

To measure the entropy of all bundles, the size of each bundle must be also considered, because a large conflicting bundle \(D_1\) affects the training more than a small conflicting bundle \(D_2\). Therefore, we consider the bundle size of each bundle to report the bundle entropy at training step \(t\) for layer \(l\) with:
\[
H^l(t) = \frac{1}{|B|} \sum_{D_i \in D^l} |D_i| \cdot H^l(t, D_i)
\]
(3)
If only one sample or samples of the same class are included in a bundle, \(H^l(t)\) is zero. If a fully conflicting bundle occurs then \(H^L = \ln(N_c)\).

To be able to check the correctness of hypothesis 1 and hypothesis 2, we must detect whether conflicts occur during training. Therefore, we evaluate \(H^l(t)\) after multiple time steps and report an average value of the bundle entropy that occurred during training. We call this metric the bundle entropy \(H^l\). If not explicitly mentioned we call \(H^L\) of the last hidden layer \(L\) the bundle entropy. It is important to mention that the bundle entropy \(H^L > 0\) iff at least two samples with different labels are bundled during training.

3. Experimental evaluation

In section 2 we hypothesized that if conflicts occur, the test loss increases (hypothesis 2) and in the extreme case all labels are ignored (hypothesis 1). In this section, we evaluate whether conflicting bundles occur during the training of SOTA methods and if the effects are as hypothesized.

3.1. Setup

The theory of conflicting bundles should be a new starting point for research into several directions to improve the state-of-the-art, but the focus of this work is to introduce and shed light on the problem itself and not to fine-tune state-of-the-art methods or architectures. Therefore, we suggest the following setup as a starting-point for discussions:

**Training.** We refer to networks that are built only with fully connected layers as fully connected networks, networks as introduced by He et al. [7] residual neural network (ResNet) and we call the same network without residual connections VGG net. State-of-the-art datasets [10, 13, 15, 20], and random data augmentation is used to evaluate conflicting bundles under real conditions: We normalize and randomly crop, flip (except for Mnist) and adapt the brightness of images. ReLU activations are used and therefore weights are initialized with the HE initializer [6] to avoid vanishing or exploding gradients. To minimize the cross-entropy loss we use the state-of-the-art optimizer Ranger (RAdam [17] + Lookahead [31]) with a mini-batch size of 64, a learning rate of 0.001, weight decay of 0.01. ResNets and VGG nets are trained for 120 epochs and the fully connected networks for 50 epochs. The source uses TensorFlow Version 2.2.0 [1] and is available on GitHub [8]. Training is executed on a multi-GPU cluster, one GPU is used to measure conflicting bundles. All experiments are also implemented and designed to be executable on smaller systems with a single GPU.

**Evaluation.** The test accuracy is averaged over the last 5 epochs to exclude outliers. We estimate conflicting bundles through a random subset of the training set \(B \subseteq \mathcal{X}\) with \(|B| = 2048\) to speed up computations and we found empirically that this number of samples is large enough to rep-
(a) No conflicting bundle
balanced dataset.
(b) Fully conflicting bundle
training with balanced dataset
(c) Fully conflicting bundle
training with imbalanced dataset
Figure 2: Experiment with a toy dataset and manually initialized weights to produce a fully conflicting bundle for balanced
and imbalanced datasets and to check if gradients resemble white noise.

Figure 3: White noise of shattered gradients \[\text{[2]}\] compared
with gradients of the conflicting training bundle problem.

represent the bundle entropy. To calculate bundles we created
a vectorized function that iterates only once overall \(x \in B\)
such that this calculation can also be done on small hardware setups with e.g. only one GPU. Therefore, the complexity to evaluate all layers is \(O(|B| \times L)\). It is important
to mention that examples of the training data and not the
test data are used to measure conflicting training bundles,
as those examples are used to adjust the weights of the network.

3.2. Training with a fully conflicting bundle

To evaluate whether training with fully conflicting bundles
saddle at a region where all neurons fire with a constant
value as predicted in hypothesis \(1\) we compare the training
of a neural network with and without a fully conflicting bundle
under controlled settings. The fully conflicting bundle
is produced in a setup where the conditions can be tightly
controlled through manual weight initialization. We use a
toy dataset with two classes (class one if \(x_i < 0.5\), class
two otherwise) and 1k training examples for a network with
ReLU activations, two layers and two neurons per layer fol-
lowed by softmax and cross-entropy loss function. The re-

results are shown in fig. \(2\).

At first, we confirmed in fig. \(2a\) that this network can
solve the problem with a training accuracy of \(\approx 1.0\) if
weights are initialized such that no fully conflicting bundle
is produced. For the training shown in fig. \(2b\) we initialized
weights such that a fully conflicting bundle is produced. It
can be seen that for this weight configuration each output
neuron fires with a constant value of \(1/N\) after 50
epochs as predicted by hypothesis \(1\). In fig. \(2c\) the network
is trained under fully conflicting bundles together with an
imbalanced dataset such that 66% of the training examples
are of class one and 33% are of class two. As claimed in sec-
tion 2.1 each neuron reflects the imbalance of the dataset
because neuron one fires with a constant value of 0.66. The
gradient amplitude of the training without conflicting bun-
dles (fig. \(2a\)) and with conflicting bundles (fig. \(2b\), fig. \(2c\))
is similar at the beginning of the training process, ruling out
the gradient vanishing or exploding problem. Also, the net-
works have only two layers such that this problem would
not arise. We also compared the shattered gradient problem
with the gradients of fully conflicting training bundles in
fig. \(3\) and can rule out that both problems are the same be-
cause gradients of conflicting bundles are highly correlated
with its input.

We executed this first experiment under controlled set-
tings and therefore we continue with the HE initializer \(6\),
larger fully connected networks and the Mnist dataset.

3.3. Fully connected networks

The test accuracy of more than a hundred fully connected
networks together with the conflicting boundary is already
shown in fig. \(1\). In this section, we study the bundle en-
tropy and the number of bundles that occur during training
in more detail by analyzing each training epoch and layer
of different fully connected networks trained on Mnist. Results are shown in fig. 4 and fig. 5.

In fig. 4a we can see the training of two shallow networks with width 10 and 25. First of all, the number of conflicts mainly increases as we ascend the hierarchy of the network indicating that subsequent layers can not fully solve conflicts. Therefore, it can be concluded that the number of conflicting training bundles increases as the depth of the network increases. Comparing width 10 and width 25 of fig. 4a shows that conflicts occur much earlier in the architecture if the dimensionality of hidden features is smaller. This explains the pattern of the test-accuracy shown in fig. 5. Also, if conflicting bundles occur during training, conflicts can only slowly be resolved as the training proceeds. This motivates why we are able to create the boundary of fig. 1 already at the beginning of the training. Two deeper networks with 150 layers are analyzed in fig. 4b and fig. 4c. For both widths conflicting bundles occur during training, but for a width of 10 it can be seen that a fully conflicting bundle occurs because \( H^L(t) \approx 2.3 \). Therefore, conflicts are never resolved and we also confirmed that the accuracy is not better than chance as claimed in hypothesis 1. Interestingly, if we compare fig. 4a and fig. 4b it can be concluded that for a fixed width, the position where conflicting layers occur is similar between different depths. For example the first conflicting layer for width 25 is layer 19 for both, \( L = 25 \) and \( L = 150 \). Therefore, it is sufficient to only evaluate the deepest network to find the conflicting boundary in fig. 1. The correlation of the bundle entropy and test accuracy is evaluated in fig. 5. It can be seen that the bundle entropy \( H^L \) is negatively correlated with the test accuracy. This further supports our hypothesis 2 that conflicting bundles worsen the test accuracy of neural networks.

One natural question that arises from this section is, whether conflicts also occur for computer vision tasks and convolutional layers because hidden features are high dimensional.

### 3.4. VGG nets

In this section, conflicting bundles are evaluated for different VGG nets and different datasets to further support hypothesis 1 and hypothesis 2 experimentally. The network is trained without residual connections and the results are shown in fig. 6a. The bundle entropy of each time step \( H^L(t) \) for a network with 100 layers trained on Imagenette is shown in fig. 6b.

For small networks with only four layers, the model suffers from underfitting and therefore the test accuracy is lower. From 10 to 40 layers, the test accuracy is largest and the bundle entropy is also zero indicating no conflicting bundles during training. After 40 layers for Cifar (and 60 layers for Imagenette), the bundle entropy \( H^L \) increases...
as the depth increases. The test accuracy decreases as the bundle entropy increases which supports hypothesis 2. For 120 layers the entropy is approximately 2.3 (max. possible entropy for 10 classes is 2.35) indicating a fully conflicting bundle and therefore the accuracy is also not better than chance as hypothesized in hypothesis 1. Previous work already reported that the test accuracy decreases when training very deep convolutional networks [2, 7, 27]. We are now able to relate this behavior additionally to conflicting bundles. Another interesting observation is that weights are initialized correctly because at the beginning of the training the bundle entropy is zero as shown in fig. 6a and conflicting bundles occur after the first epochs of training. We conclude that weight initialization is very important, but conflicts can also occur even when weights are initialized correctly and the probability for conflicting layers increases with each layer that is added to the architecture also for very high dimensional features such as images.

It is well known that residual connections reduce the shattered gradient problem and we have seen in section 3.2 and section 3.3 that shattered gradients are different than conflicting bundles. Therefore the question of whether residual connections also solve the conflicting bundle problem is still an open one and analyzed next.

### 3.5. Residual neural networks

To evaluate whether residual connections solve conflicts, we trained residual networks with different depths on different datasets. It can be seen in fig. 6c that the bundle entropy is zero for all network depths and datasets, thus it can be concluded that conflicts are solved by residual connections and therefore, the training of very deep convolutional networks is possible. Also, the accuracy is high for all different residual networks which further supports hypothesis 2. He et al. [7] already showed that residual networks are easier to optimize and our conflicting bundle theory explains this fact from a new perspective.

We further evaluate how residual connections bypass conflicting layers from a theoretical viewpoint: Let’s consider layer \( l \) producing conflicts for \( x_i \) and \( x_j \) without any residual connection. We call this the intermediate conflicting output \( d^{(l)} \) (which is the same for \( x_i \) and \( x_j \) as it is assumed to be conflicting). The output for inputs \( x_i \) and \( x_j \) of the layer which adds a residual connection \( r^{(l)}(x) \) is \( a^{(l+1)}(x) = r^{(l)}(x) + d^{(l)} \). The residual \( r^{(l)}(x) \) is the identity mapping [7] and therefore it can be shown that the function \( a^{(l+1)}(x) \) is bijective for inputs \( x_i \) and \( x_j \). Definition 1 is violated because \( a^{(l+1)}(x_i) \neq a^{(l+1)}(x_j) \) and the conflict is resolved. This analysis shows how residual connections solve conflicts. But, it is also important to mention that this analysis not proved the absence of conflicts in general. For example, if the intermediate layer is exactly the negative identity function, the output \( a^{(l+1)}(x) \) is constantly zero and therefore, conflicting. On the other hand, He et al. [7] already showed that it is hard to learn the identity function and therefore we assume that the aforementioned special case never happens in practice. This is backed by the results shown in fig. 6c because the bundle entropy is always zero.

Another important insight of this theoretical analysis is that conflicting layers that are bypassed with residual connections represent only a linear mapping, because \( a^{(l+1)}(x) = r^{(l)}(x) + d^{(l)} \). Therefore, we assume that the test accuracy of correctly pruned networks (w.r.t conflicting layers) is not significantly worse than its residual counterpart which is evaluated next.

### 3.6. Auto-tuning the network depth

The pruning algorithm that we propose searches for the conflicting boundary as shown in fig. 1 for a given input dimensionality and prunes afterwards the network to ensure
Table 1: Comparison of test accuracy, memory consumption (based on checkpoint size) and inference time.

| Dataset    | Name  | Layers | Accuracy [%] | Mem. [MB] | Time / Step [ms] |
|------------|-------|--------|--------------|-----------|------------------|
| Imagenette | ResNet| 50     | 85.6 ± 0.8   | 116       | 310              |
|            | Auto-tune | 24 ± 1.6 | 84.7 ± 0.1   | 63 ± 6.0  | 200 ± 0.0        |
| Cifar      | ResNet| 76     | 85.7 ± 0.4   | 178       | 130              |
|            | Auto-tune | 19 ± 0.9 | 85.3 ± 0.4   | 53 ± 1.0  | 48 ± 2.5         |
| Svhn       | ResNet| 50     | 95.4 ± 0.1   | 116       | 90               |
|            | Auto-tune | 19 ± 0.9 | 95.1 ± 0.1   | 54 ± 0.5  | 46 ± 1.8         |
| Mnist      | ResNet| 50     | 99.4 ± 0.0   | 116       | 88               |
|            | Auto-tune | 17 ± 1  | 99.3 ± 0.5   | 54 ± 2.1  | 40 ± 0.0         |

that no conflicting bundles occur during training. This is implemented as follows: First, the largest network from section 3.4 with 120 layers is trained for at least one epoch (see fig. 6b). Then the first layer \( t \) with \( H^t(t) > 0 \) and all subsequent layers of the same type (specified in [7]) are removed from the architecture following the findings of section 3.3. Due to this pruning, also the dimensionality between two layers changes and therefore we restart the training with the new pruned architecture rather than continuing the training to avoid dimensionality problems. A restart additionally helps in terms of accuracy, because the network is trained for one epoch with conflicting bundles such that weights of the network are adjusted into wrong directions. This process is repeated until no conflicting layer can be found and the network is successfully trained.

To provide a fair comparison, we compare the pruned network found by the auto-tune algorithm against the ResNet which produced the highest accuracy (section 3.5). To evaluate whether a similar accuracy can be achieved for other datasets, the Svhn [20] and Mnist [15] dataset are included and trained on ResNet-50 as this depth produced good results in section 3.5. Note that each experiment is executed three times and the mean and standard deviation are reported in table 1. From our experimental evaluation, we observed that the auto-tune algorithm changed the architecture at most three times before the final pruned network was found and the architecture was changed after the first and before the second epoch. Therefore, this automatic depth selection process is computationally very efficient as it took only three epochs of training to select the architecture. The number of layers found by the auto-tune algorithm is within the optimal region w.r.t. test accuracy as shown in fig. 6a and the depth increases as its input dimensionality increases similar to the findings from section 3.3. Interestingly, the number of layers also corresponds with the studies of Veit et al. [30] which shows that paths in ResNets are only 10-34 layers deep. From table 1 it can also be concluded that the test accuracy of networks without conflicting layers are competitive when compared to its residual counterpart, but the inference time and the memory consumption is drastically reduced because fewer layers are used.

4. Discussion and future work

In this paper, we have shown that conflicting training bundles decrease the test accuracy of trained models or lead to networks that can not be trained at all. We have shown that the number of conflicting training bundles increases, as the dimensionality of hidden features decreases or the depth of the network increases. We demonstrated that this also happens for computer vision tasks where hidden features are very high dimensional and we proved that residual connections solve conflicts. The mapping from an input to its output of a conflicting layer bypassed with a residual connection is only linear and therefore, the pruning of those layers should lead to competitive test accuracy when compared to its residual counterpart. We introduced a novel NAS algorithm to remove conflicting layers and confirmed that the accuracy is maintained while the computational power and memory consumption is drastically reduced.

For future work, it would be interesting to study how conflicting layers can be directly fixed rather than removed from the architecture. The analysis of section 3.5 suggests to use a different approach than residual connections, because they force a linear mapping from inputs to outputs. Another promising direction of research would be to study if novel data-augmentation strategies or intelligent sampling of mini-batches could help to avoid conflicting bundles during training. Another interesting topic to study would be to evaluate whether a coarser resolution of floating point representations bundles samples with a higher probability. To correctly evaluate this hypothesis, it must be considered that the resolution \( \gamma \) is already included in the metric that we propose because this biases the metric into the hypothesized direction.

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