Predictions of diffusion rates of organic molecules in secondary organic aerosols using the Stokes-Einstein and fractional Stokes-Einstein relations

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Abstract. Information on the rate of diffusion of organic molecules within secondary organic aerosol (SOA) is needed to accurately predict the effects of SOA on climate and air quality. Often, researchers have predicted diffusion rates of organic molecules within SOA using measurements of viscosity and the Stokes-Einstein relation \(D \propto 1/\eta\) where \(D\) is the diffusion coefficient and \(\eta\) is viscosity. However, the accuracy of this relation for predicting diffusion in SOA remains uncertain. We measured diffusion coefficients over eight orders in magnitude in proxies of SOA including citric acid, sorbitol, and a sucrose-citric acid mixture. These results were combined with literature data to evaluate the Stokes-Einstein relation for predicting diffusion of organic molecules in SOA. Although almost all the data agrees with the Stokes-Einstein relation within a factor of ten, a fractional Stokes-Einstein relation \(D \propto C/\eta^t\) with \(t = 0.93\) and \(C = 1.66\) is a better model for predicting diffusion of organic molecules in the SOA proxies studied. In addition, based on the output from a chemical transport model, the Stokes-Einstein relation can over predict mixing times of organic molecules within SOA by as much as one order of magnitude at an altitude \(\sim 3\) km, compared to the fractional Stokes-Einstein relation with \(t = 0.93\) and \(C = 1.66\). These differences can be important for predicting growth, evaporation, and reaction rates of SOA in the middle and upper part of the troposphere. These results also have implications for other areas where diffusion of organic molecules within organic-water matrices is important.

1 Introduction

Atmospheric aerosols, suspensions of micrometer and sub-micrometer particles in the Earth’s atmosphere, modify climate by interacting with incoming solar radiation and by altering cloud formation and cloud properties (Stocker et al., 2013). These
Aerosols also negatively impact air quality and may facilitate the long-range transport of pollutants (Friedman et al., 2014; Mu et al., 2018; Shrivastava et al., 2017a; Vaden et al., 2011; Zelenyuk et al., 2012).

A large fraction of atmospheric aerosols are classified as secondary organic aerosol (SOA). SOA is formed in the atmosphere when volatile organic molecules, emitted from both anthropogenic and natural sources, are oxidized and partition to the particle phase (Ervens et al., 2011; Hallquist et al., 2009). The exact chemical composition of SOA remains uncertain; however, measurements have shown that SOA contains 1000s of different organic molecules and the average oxygen-to-carbon (O:C) ratio of organic molecules in SOA ranges from 0.3 – 1.0 or even higher (Aiken et al., 2008; Cappa and Wilson, 2012; Chen et al., 2009; DeCarlo et al., 2008; Ditto et al., 2018; Hawkins et al., 2010; Heald et al., 2010; Jimenez et al., 2009; Laskin et al., 2018; Ng et al., 2010; Nozière et al., 2015; Takahama et al., 2011; Tsimpidi et al., 2018). SOA also contains a range of organic functional groups including alcohols and carboxylic acids (Claeys et al., 2004, 2007; Edney et al., 2005; Fisseha et al., 2004; Glasius et al., 2000; Liu et al., 2011; Surratt et al., 2006).

In order to accurately predict the impacts of SOA on climate, air quality, and the long-range transport of pollutants, information on the rate of diffusion of organic molecules within SOA is needed. For example, predictions of SOA mass, which has major implications for climate and air quality, can vary by an order of magnitude when the molecular diffusion rate of organic molecules in SOA is varied (Shiraiwa and Seinfeld, 2012). Predictions of SOA particle size, which has implications for climate and visibility, also vary significantly in simulations as the diffusion rate of organic molecules is varied (Zaveri et al., 2014, 2018). Reactivity and photochemistry in SOA can also depend on diffusion rates (Davies and Wilson, 2015; Hinks et al., 2016; Lakey et al., 2016; Li et al., 2015; Lignell et al., 2014; Liu et al., 2018; Shiraiwa et al., 2011; Zhang et al., 2018; Zhou et al., 2013).

In some cases, diffusion rates of organic molecules in SOA have been measured or inferred from experiments (Abramson et al., 2013; Liu et al., 2016; Perraud et al., 2012; Ullmann et al., 2019; Ye et al., 2016). However, in most cases researchers have predicted diffusion rates of organic molecules within SOA using measurements of viscosities and the Stokes-Einstein relation (Booth et al., 2014; Hosny et al., 2013; Koop et al., 2011; Maclean et al., 2017; Power et al., 2013; Renbaum-Wolff et al., 2013; Shiraiwa et al., 2011; Song et al., 2015, 2016a). This is due to the development and application of several techniques which can measure viscosity of ambient aerosol or small volumes in the laboratory (Grayson et al., 2015; Pajunoja et al., 2014; Renbaum-Wolff et al., 2013; Song et al., 2016b; Virtanen et al., 2010). The Stokes-Einstein relation (Eq. 1) states that diffusion is inversely related to viscosity:

\[
D = \frac{kT}{6\pi \eta R_H}
\]

where \(D\) is the diffusion coefficient, \(k\) is the Boltzmann constant, \(T\) is the temperature in Kelvin, \(R_H\) is the hydrodynamic radius of the diffusing species, and \(\eta\) is the viscosity of the matrix. Until now, only a few studies have investigated the accuracy of the Stokes-Einstein relation for predicting diffusion coefficients of organic molecules in SOA, and almost all of these studies...
relied on sucrose as a proxy for SOA particles (Bastelberger et al., 2017; Chenyakin et al., 2017; Price et al., 2016). Sucrose was used as a proxy for SOA in these studies because 1) sucrose has an O:C ratio similar to that of highly oxidized components of SOA and 2) viscosity and diffusion data for sucrose existed in the literature (mainly from the food science literature, as well as from Power et al. (2013), who reported viscosities far outside the range of what had previously been reported. However, studies with other proxies of SOA are required to determine if the Stokes-Einstein relation can accurately represent the diffusion of organic molecules in SOA, and to more accurately predict the role of SOA in climate, air quality, and transport of pollutants (Reid et al., 2018; Shrivastava et al., 2017b).

In the following we expand on the previous studies with sucrose matrices by testing the Stokes-Einstein relation in the following proxies for SOA: 2-hydroxypropane-1,2,3-tricarboxylic acid (i.e. citric acid), 1,2,3,4,5,6-hexanol (i.e. sorbitol), and a mixture of citric acid and sucrose. These proxies have functional groups that have been identified in SOA, and O:C ratios similar to those ratios found in the most highly oxidized components of SOA in the atmosphere (1.16, 1.0, and 0.92 for citric acid, sorbitol, and sucrose respectively). To test the Stokes-Einstein relation, we first determined diffusion coefficients of fluorescent organic molecules as a function of water activity ($a_w$) in these SOA proxies using rectangular area fluorescence recovery after photobleaching (rFRAP; Deschout et al., 2010). Studies as a function of $a_w$ are critical because as the relative humidity (RH) changes in the atmosphere, $a_w$ (and hence water content) in SOA will change to maintain equilibrium with the gas phase. The diffusing organic molecules studied in this work were the fluorescent organic molecules rhodamine 6G and cresyl violet (Fig. S1). Details of the experiments are given in the Methods section. The measured diffusion coefficients are compared with predictions using literature viscosities (Rovelli et al., n.d.; Song et al., 2016b) and the Stokes-Einstein relation. The results from the current study are then combined with literature diffusion (Champion et al., 1997; Chenyakin et al., 2017; Price et al., 2016; Rampp et al., 2000; Ullmann et al., 2019) and viscosity (Fürst et al., 2002; Grayson et al., 2017; Green and Perry, 2007; Haynes, 2015; Lide, 2001; Migliori et al., 2007; Power et al., 2013; Quintas et al., 2006; Rovelli et al., n.d.; Swindells et al., 1958; Telis et al., 2007; Ullmann et al., 2019) data to assess the ability of the Stokes-Einstein relation to predict diffusion of organic molecules in atmospheric SOA. The ability of the fractional Stokes-Einstein relation (see below) to predict diffusion is also tested.

In addition to atmospheric applications, the results from this study have implications for other areas where diffusion of organic molecules within organic-water matrices is important, such as the cryopreservation of proteins (Cicerone and Douglas, 2012; Fox, 1995; Miller et al., 1998), the storage of food products (Champion et al., 1997; van der Sman and Meinders, 2013), and the viability of pharmaceutical formulations (Shamblin et al., 1999). The results also have implications for our understanding of the properties of deeply supercooled and supersaturated glass forming solutions, which are important for a wide range of applications and technologies (Angell, 1995; Debenedetti and Stillinger, 2001; Ediger, 2000).
2 Methods

2.1 Preparation of fluorescent organic-water films

The technique used here to measure diffusion coefficients required thin films containing the organic matrix (i.e. citric acid or sorbitol or a mixture of citric acid and sucrose), water, and trace amounts of the diffusing organic molecules (i.e. fluorescent organic molecules). Citric acid (≥ 99 % purity) and sorbitol (≥ 98 % purity) were purchased from Sigma-Aldrich and used as received. Rhodamine 6G chloride (≥ 99 % purity), and cresyl violet acetate (≥75 % purity) were purchased from Acros Organics and Santa Cruz Biotechnology respectively, and used as received. Solutions containing the organic matrix, water, and the diffusing molecules were prepared gravimetrically. 55 weight percent citric acid solutions and 30 weight percent sorbitol and sucrose-citric acid solutions were used to prepare the citric acid, sorbitol, and sucrose-citric acid thin films, respectively. A mass ratio of 60:40 sucrose to citric acid was used for the sucrose-citric acid matrix. The concentrations of rhodamine 6G and cresyl violet in the solutions were 0.06 mM and 0.08 mM, respectively. After the solutions were prepared gravimetrically, the solution s were passed through a 0.02 µm filter (Whatman™) to eliminate impurities. Droplets of the solution were placed on cleaned siliconized hydrophobic slides (Hampton Research), by either nebulizing the bulk solution or using the tip of a sterilized needle (BD PrecisionGlide Needle, BD, Franklin Lakes, NJ, USA). The generated droplets ranged in diameter from ~100 to ~1300 µm. After the droplets were located on the hydrophobic slides, the hydrophobic slides were placed inside sealed glass containers with a controlled water activity (a_w). The a_w was set by placing saturated inorganic salt solutions with known a_w values within the sealed glass containers. The a_w values used ranged from 0.14 to 0.86. When the a_w values were higher than 0.86 recovery times were too fast to measure with the rFRAP setup. When the a_w values were lower than 0.14 or 0.23, depending on the organic solute, solution droplets often crystallized. The slides holding the droplets were left inside the sealed glass containers for an extended period of time to allow the droplets to equilibrate with the surrounding a_w. The method used to calculate equilibration times is explained in Section S1, and conditioning times for all samples are given in Tables S1-S4. Experimental times for conditioning were a minimum of three times longer than calculated equilibration times.

After the droplets on the slides reached equilibrium with the a_w of the airspace over the salt solution, the sealed glass containers holding the slides and conditioned droplets were brought into a Glove Bag™ (Glas-Col). The a_w within the Glove Bag was controlled using a humidified flow of N_2 gas and monitored using a handheld hygrometer. The a_w within the Glove Bag™ was set to the same a_w as used to condition the droplets, to prevent the droplets from being exposed to an unknown and uncontrolled a_w. To form a thin film, aluminum spacers were placed on the siliconized glass slide holding the droplets, followed by another siliconized glass slide, which sandwiched the droplets and the aluminum spacers. The thickness of the aluminum spacers (30-50 µm) determined the thickness of the thin film. The two slides were sealed together by vacuum grease spread around the perimeter of one slide before sandwiching (see Fig. S2 in the Supplement for details).

The organic matrices were often supersaturated with respect to crystalline citric acid or sorbitol. Nevertheless, crystallization was not observed in most cases until a_w values ≤ 0.14 - 0.23, depending on the organic matrix, because the solutions were...
passed through a 0.02 µm filter and the glass slides used to make the thin films were covered with a hydrophobic coating. Filtration likely removed heterogeneous nuclei that could initiate crystallization and the hydrophobic coating reduced the ability of these surfaces to promote heterogeneous nucleation (Bodsworth et al., 2010; Pant et al., 2006; Price et al., 2014; Wheeler and Bertram, 2012). In the cases where crystallization was observed, determined using optical microscopy, the films were not used in rFRAP experiments. An image demonstrating the difference in appearance between crystallized and non-crystallized droplets is given in Figure S3.

2.2 Rectangular area fluorescence recovery after photobleaching (rFRAP) technique and extraction of diffusion coefficients

Diffusion coefficients were measured using the rFRAP technique reported by Deschout et al. (2010). The technique uses a confocal laser scanning microscope to photobleach fluorescent molecules in a specified volume of an organic thin film containing fluorescent molecules. The photobleaching event initially reduces the fluorescence intensity within the bleached volume. Afterward, the fluorescence intensity within the photobleached volume recovers due to the diffusion of fluorescent molecules from outside of the bleached region. From the time-dependent recovery of the fluorescence intensity, diffusion coefficients are determined. All diffusion coefficients reported here were measured at 295 ± 1 K.

The rFRAP experiments were performed on a Zeiss Axio Observer LSM 510MP laser scanning microscope with a 10X, 0.3 NA objective and a pinhole setting between 80 and 120 µm. Photobleaching and the subsequent acquisition of recovery images were done using a 543 nm helium–neon (HeNe) laser. The bleach parameters (e.g. laser intensity, iterations, laser speed) were varied for each experiment so that the fraction of fluorescent molecules being photobleached in the bleach region was about 30%. A photobleaching of about 30% was suggested by Deschout et al. (2010), who report that diffusion coefficients measured with the rFRAP technique are independent of the extent of photobleaching up to a bleach depth of 50%.

Bleached areas ranged from 20 µm² to 400 µm². The geometry of the photobleached region was a square with sides of length lₓ and lᵧ ranging from 4.5 to 20 µm. Smaller bleach areas were used in experiments where diffusion was slower in order to shorten recovery times. Chenyakin et al. (2017) showed that measured diffusion coefficients varied by less than the experimental uncertainty when the bleach area was varied from 1 µm² to 2500 µm² in sucrose-water films. Similarly, Deschout et al. (2010) demonstrated that diffusion coefficients varied by less than the experimental uncertainty when the bleach area was varied from approximately 4 µm² to 144 µm² in sucrose-water films. The images collected during a rFRAP experiment represent fluorescence intensities as a function of x and y coordinates, and are taken at regular time intervals after photobleaching. An example of images recorded during a rFRAP experiment are shown in Fig. S4. Every image taken following the photobleaching event is normalized relative to an image taken before photobleaching. To reduce noise, all images are downsized by averaging from a resolution of 512x512 pixels to 128x128 pixels.

The mathematical description of the fluorescence intensity as a function of position (x and y) and time (t) after photobleaching a rectangular area in a thin film, was given by Deschout et al. (2010):
\[ F(x,y,t) = \left[ 1 - \frac{K_0}{4} \left( \text{erf} \left( \frac{x \pm l_x}{2 \sqrt{r^2 + 4Dt}} \right) - \text{erf} \left( \frac{x \mp l_x}{2 \sqrt{r^2 + 4Dt}} \right) \right) \cdot \left( \text{erf} \left( \frac{y + l_y}{2 \sqrt{r^2 + 4Dt}} \right) - \text{erf} \left( \frac{y - l_y}{2 \sqrt{r^2 + 4Dt}} \right) \right) \right] \]  

(2)

where \( F(x,y,t) \) is the fluorescence intensity at position \( x \) and \( y \) after a time \( t \), \( F_0(x,y) \) corresponds to the initial intensity at position \( x \) and \( y \) before photobleaching, \( K_0 \) is related to the initial fraction of photobleached molecules in the bleach region, and \( l_x \) and \( l_y \) correspond to the size (length) of the bleach region in the \( x \) and \( y \) directions. The parameter \( r \) represents the resolution of the microscope, \( t \) is the time after photobleaching, and \( D \) is the diffusion coefficient.

The images collected during a rFRAP experiment were fit to Eq. (2) using a Matlab script (The Mathworks, Natick, MA, USA), with the terms \( K_0 \), and \( r^2 + 4Dt \) left as free parameters. An additional normalization factor was also left as a free parameter, and returned a value close to 1, since images recorded after photobleaching were normalized to the pre-bleach image before fitting. To determine the bleach width \( (l_x, l_y) \), Eq. (2) was fit to the first five images recorded after photobleaching a film with the bleach width \( (l_x, l_y) \) left as a free parameter. The bleach width returned by the fit to the first five frames was then used as input in Eq. (2) to analyze the full set of images.

From the fitting procedure, a value for \( r^2 + 4Dt \) was determined for each image, and was plotted as a function of time after photobleaching. A straight line was then fit to the \( r^2 + 4Dt \) vs. \( t \) plot, and from the slope of the line \( D \) was calculated. An example is shown in Fig. S5. As the intensity of the fluorescence in the bleached region recovers, the noise in the data become large relative to the difference in fluorescence intensity between the bleached and non-bleached regions (i.e. signal). To ensure we only use data with a reasonable signal to noise, images were not used if this signal was less than \( 3 \times \) the standard deviation of the noise.

Figure S6 shows a cross section of the fluorescence intensity along the \( x \) direction from the data in Fig. S4. To generate the cross-sectional view, at each position \( x \), the measured fluorescence intensity is averaged over the width of the photobleached region in the \( y \) direction (black squares). Also included in Fig. S6 are cross-sectional views of the calculated fluorescence intensity along the \( x \) direction generated from the fitting procedure (solid red lines). To generate the line, Eq. (2) was first fit to the images. The resulting fit was then averaged over the width of the photobleached region in the \( y \) direction. The good agreement between the measured cross section and the predicted cross section illustrates that Eq. (2) describes the rFRAP data well.

Equation (2) assumes that there is no net diffusion in the axial direction (i.e. \( z \)-direction). Deschout et al. (2010) have shown that Eq. (2) gives accurate diffusion coefficients when the numerical aperture of the microscope is low (≤ 0.45) and the thickness of the fluorescent films is small (≤ 120 μm), which is consistent with the numerical aperture of 0.30 and film thickness of 30–50 μm used here.
3 Results and Discussion

3.1 Diffusion coefficients of organic molecules in citric acid, sorbitol, and sucrose-citric acid matrices

The measured diffusion coefficients of organic molecules in matrices of citric acid, sorbitol, and sucrose-citric acid as a function of water activity ($a_w$) are shown in Fig. 1 (and listed in Tables S1-S4). The measured diffusion coefficients depend strongly on $a_w$ for all three proxies of SOA. As $a_w$ increases from 0.23 (0.14 in one case) to 0.86, diffusion coefficients increase by between five and eight orders of magnitude. This dependence on $a_w$ arises from the plasticizing influence of water on these matrices; as $a_w$ increases (and hence the water content increases) the viscosity decreases (Koop et al., 2011). In addition, the measured diffusion coefficients varied significantly from matrix to matrix at the same $a_w$ (Fig. 1). As an example, at $a_w = 0.23$ the diffusion coefficient of rhodamine 6G is about four orders of magnitude larger in citric acid compared to the sucrose-citric acid mixture.

We also considered the relationship between $\log(D) - \log(kT/6\pi R_H)$ and $\log(\eta)$, a comparison that allows the identification of deviations from the Stokes-Einstein relation (Fig. 2). By plotting $\log(D) - \log(kT/6\pi R_H)$ we account for differences in hydrodynamic radii of diffusing species and small differences in temperature (within a range of 6 K). The viscosity corresponding to each measured diffusion coefficient was determined from relationships between $a_w$ and viscosity developed from literature data (Figs. S7-S9). The solid line in Fig. 2 corresponds to the relationship between $\log(D) - \log(kT/6\pi R_H)$ and $\log(\eta)$ if the Stokes-Einstein relation (Eq. 1) is obeyed. Figure 2 shows that the diffusion coefficients of the fluorescent organic molecules depend strongly on viscosity, with the diffusion coefficients varying by approximately eight orders of magnitude as viscosity varied by eight orders of magnitude. If the uncertainties of the measurements are considered, all the data points except three (89 % of the data) are consistent with predictions from the Stokes-Einstein relation (meaning that the error bars on the measurements overlap with the solid line in Fig. 2) over eight orders of magnitude change in diffusion coefficients. This finding is remarkable considering the assumptions inherent in the Stokes-Einstein relation (e.g. the diffusing species is a hard sphere that experiences the fluid as a homogeneous continuum and no slip at the boundary of the diffusing species).

3.2 Comparison with relevant literature data

Previous studies have used sucrose to evaluate the ability of the Stokes-Einstein relation to predict diffusion coefficients of organic molecules in SOA (Bastelberger et al., 2017; Chenyakin et al., 2017; Price et al., 2016). In addition, a recent study (Ullmann et al., 2019) used SOA generated in the laboratory from the oxidation of limonene, subsequently exposed to NH$_3$ (g) (i.e. brown limonene SOA) to evaluate the Stokes-Einstein relation. Although studies with SOA generated in the laboratory are especially interesting, that previous study was limited to relatively low viscosities ($\leq 10^2$ Pa s), where a breakdown of the Stokes-Einstein relation is less expected. In Fig. 3a we have combined the results from the current study (i.e. the results from Fig. 2) with previous studies of diffusion and viscosity in sucrose and brown limonene SOA (Champion et al., 1997; Chenyakin et al., 2017; Price et al., 2016; Rampp et al., 2000; Ullmann et al., 2019). To be consistent with the current study, we have not...
included data in Fig. 3a if the diffusion coefficients and viscosities were measured at, or calculated using, temperatures outside the range of 292 – 298 K and if the radius of the diffusing molecule was smaller than to the radius of the molecules in the fluid matrix. Previous work has shown that the Stokes-Einstein relation is not applicable when the radius of the diffusing molecule is less than the radius of the matrix molecules, and those cases are beyond the scope of this work (Bastelberger et al., 2017; Davies and Wilson, 2016; Marshall et al., 2016; Power et al., 2013; Price et al., 2016; Shiraiwa et al., 2011). Additional details for the data shown in Fig. 3a are included in section S2 and Table S5.

Based on Fig. 3a the diffusion coefficients of the organic molecules in sucrose matrices and matrices consisting of SOA generated in the laboratory depend strongly on viscosity, similar to the results shown in Fig. 2. In addition, almost all the data agree with the Stokes-Einstein relation (solid line in Fig. 3a) within a factor of ten. This finding is in stark contrast with the diffusion of water in organic-water mixtures, where much larger deviations between measured and predicted diffusion coefficients were observed over the same viscosity range (Davies and Wilson, 2016; Marshall et al., 2016; Price et al., 2016).

In Fig. 3b, we show the differences between the measured values and the solid line in Fig. 3a as a function of viscosity. If the Stokes-Einstein relation describes the data well, these differences (i.e. residuals) should be scattered symmetrically about zero, while the magnitude of the residuals should be less than or equal to the uncertainty in the measurements. However, the residuals are skewed to be positive, especially as viscosity increases, with measured diffusion faster than expected based on the Stokes-Einstein relation. Figure 3b suggests that the Stokes-Einstein relation may not be the optimal model for predicting diffusion coefficients in SOA, particularly at high viscosities.

### 3.3 Fractional Stokes-Einstein relation

When deviation from the Stokes-Einstein relation has been observed in the past, a fractional Stokes-Einstein relation ($D \propto 1/\eta^t$, where $t$ is an empirical fit parameter) has often been used to quantify the relationship between diffusion and viscosity. For example, Price et al. (2016) showed that a fractional Stokes-Einstein relation can accurately represent the diffusion of sucrose in a sucrose matrix over a wide range of viscosities (from roughly $10^0 \rightarrow 10^6$ Pa s) with $t = 0.90$. Building on that work, the data in Fig. 3a were fit to the following fractional Stokes-Einstein relation:

$$D = C \frac{kT}{6\pi \eta^t R_H}$$

(3)

where $t$ and $C$ are empirical fit parameters. When fitting Eq. 3 to the data, we used the additional constraint that $\log(D) – \log(kT/6\pi R_H)$ equals 3 when the viscosity is $10^3$ Pa s, which is equivalent to assuming the Stokes-Einstein relation is valid at a viscosity of $10^3$ Pa s (roughly the viscosity of water). The best fit to the data (represented by the dashed line in Fig. 3a) resulted in a $t$ value of 0.93 and a $C$ value of 1.66.

In Fig. 3c, we plotted the difference between the measured values shown in Fig. 3a and the predicted values using the fractional Stokes-Einstein relation (dashed line in Fig. 3a). These residuals are more symmetrically scattered about zero compared to the residuals plotted in Fig. 3b. In addition, the sum-of-squared residuals ($r^2$) in Fig 3c was less than the sum-of-squared
residuals in Fig. 3b ($r^2 = 10.8$ compared to 19.7). This suggests that the fractional Stokes-Einstein relation with an exponent value of $t = 0.93$ and $C = 1.66$ may be the better model for predicting diffusion coefficients of organic molecules in SOA compared to the traditional Stokes-Einstein relation.

### 3.4 Implications for atmospheric mixing times

To investigate the atmospheric implications of these results, we considered the mixing times of organic molecules within SOA in the atmosphere as a function of viscosity using both the Stokes-Einstein relation (Eq. 1) and the fractional Stokes-Einstein relation (Eq. 3) with $t = 0.93$ and $C = 1.66$. Mixing times were calculated with the following equation (Seinfeld and Pandis, 2006; Shiraiwa et al., 2011):

$$
\tau_{\text{mix}} = \frac{d_p^2}{4\pi D} 
$$

where $\tau_{\text{mix}}$ is the characteristic mixing time, $d_p$ is the SOA particle diameter, and $D$ is the diffusion coefficient. $\tau_{\text{mix}}$ corresponds to the time at which the concentration of the diffusing molecules at the centre of the particle deviates by less than a factor of 1/e from the equilibrium concentration. We assumed a $d_p$ of 200 nm, which is roughly the median diameter in the volume distribution of ambient SOA (Martin et al., 2010; Pöschl et al., 2010; Riipinen et al., 2011). We assumed a value of 0.38 nm for $R_H$ based on literature values for molecular weight (175 g mol$^{-1}$; Huff Hartz et al., 2005) and the density (1.3 g cm$^{-3}$; Chen and Hopke, 2009; Saathoff et al., 2009) of SOA molecules, and assuming a spherical symmetry of the diffusing species.

Figure 4 shows the calculated mixing times of 200 nm particles as a function of the viscosity of the matrix. The mixing time of 1 hour is highlighted, since when calculating the growth and evaporation of SOA and the long-range transport of pollutants using chemical transport models, a mixing times of < 1 hour for organic molecules within SOA is often assumed (Hallquist et al., 2009). At a viscosity of 5 x 10$^6$ Pa s, the mixing time is > 1 hour based on the Stokes-Einstein relation, but remains < 1 hour based on the fractional Stokes-Einstein relation. Furthermore, at high viscosities > 5 x 10$^6$ Pa s, the mixing times predicted with the traditional Stokes-Einstein relation are at least a factor of 5 greater than those predicted with the fractional Stokes-Einstein relation.

Recently, Shiraiwa et al. (2017) estimated mixing times of organic molecules in SOA particles in the global atmosphere using the global chemistry climate model EMAC (Jöckel et al., 2006) and the organic module ORACLE (Tsimpidi et al., 2014). Glass transition temperatures of SOA compounds were predicted based on molar mass and the O:C ratio of SOA components, followed by predictions of viscosity. Diffusion coefficients and mixing times were predicted using the Stokes-Einstein relation. To further explore the implications of our results, we calculated mixing times of organic molecules in SOA globally using the same approach as Shiraiwa et al. (2017) and compared predictions using the Stokes-Einstein relation and predictions using the fractional Stokes-Einstein relation with $t = 0.93$ and $C = 1.66$. Shown in Fig. 5 are results from these calculations.

At all latitudes at the surface, the mixing times are well below the 1 hour often assumed in chemical transport models, regardless if the Stokes-Einstein relation or the fractional Stokes-Einstein relation is used (Fig. 5a). On the other hand, at an altitude of approximately 1.4 km, the latitudes where the mixing times exceed 1 hr will depend on whether the Stokes-Einstein
relation or fractional Stokes-Einstein relation is used (Fig. 5b). At an altitude of 3.2 km the mixing times are well above the 1-hour cut-off regardless of what relation is used, and the Stokes-Einstein relation can over predict mixing times of SOA particles by as much as one order of magnitude compared to the fractional Stokes-Einstein relation (Fig. 5c). A caveat is that the predictions at 3.2 km are based on viscosities higher than the viscosities studied in the current work. Hence, at 3.2 km the Stokes-Einstein and fractional Stokes-Einstein relations are being used outside the viscosity range tested here. Although experimentally challenging, additional studies are recommended to determine if the fractional Stokes-Einstein relation with $t = 0.93$ and $C = 1.66$ is able to accurately predict diffusion coefficients of organic molecules in proxies of SOA at viscosities higher than investigated in the current study.

4 Summary and Conclusions

We report measured diffusion coefficients of fluorescent organic molecules in a variety of SOA proxies. The reported diffusion coefficients varied by about eight orders of magnitude as the water activity in the SOA proxies varied from 0.23 (0.14 in one case) to 0.86. By combining the new diffusion coefficients with literature data, we have shown that, in almost all cases, the Stokes-Einstein relation correctly predicts diffusion coefficients of organic molecules in SOA proxies within a factor of ten. This finding is in stark contrast with the diffusion of water in SOA proxies, where much larger deviations between measured and predicted diffusion coefficients have been observed over the same viscosity range. Even though the Stokes-Einstein relation correctly predicts diffusion of organic molecules in the majority of cases within a factor of ten, a sum-of-squared residuals analysis shows that a fractional Stokes-Einstein relation with an exponent of $t = 0.93$ and $C = 1.66$ is a better model for predicting diffusion coefficients in SOA proxies, for the range of viscosities included in this study. This is consistent with earlier work that showed the fractional Stokes-Einstein relation is able to reproduce measured diffusion coefficients of sucrose in sucrose-water matrices. The fractional Stokes-Einstein relation predicts faster diffusion coefficients and therefore shorter mixing times of SOA particles in the atmosphere. At an altitude of ~3.2 km, the difference in mixing times predicted by the two relations is as much as one order of magnitude.

Authors contributions

EE performed the diffusion measurements. AMM, YL, APT, VAK, JL, and MS provided calculations of mixing times as a function of altitude and latitude. GR and JPR provided viscosity data. SK provided assistance with the diffusion measurements. EE and AKB conceived the study and wrote the manuscript. All authors contributed toward revising the manuscript. All authors read and approved the final manuscript.
Conflicts of interest

There are no conflicts of interest to declare.

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Figures

Figure 1. Measured diffusion coefficients of fluorescent organic molecules in various organic matrices as a function of water activity ($a_w$). X-error bars represent the uncertainty in the measured $a_w$ (0.025) and y-error bars correspond to two times the standard deviation in the diffusion measurements. Each data point is the average of a minimum of four measurements. Indicated in the legend are the fluorescent organic molecules studied and the corresponding matrices.
Figure 2. Plot of log (D) – log (kT/6πRH) as a function of log (η) for measurements shown in Fig. 1. Viscosities (η) were determined from relationships between viscosity and a_w (Figs. S7–S9). T corresponds to the experimental temperature and RH corresponds to the radius of each diffusing species (see Table S5). The x-error bars were calculated using the uncertainty in a_w at which the samples were conditioned (± 0.025) and uncertainties in the viscosity-a_w parameterizations. The y-error bars represent 2 times the standard deviation of the diffusion measurements. The black line represents the relationship between log (D) – log (kT/6πRH) and log (η) predicted by the Stokes-Einstein relation (slope = -1). Shown at the bottom of the figure are various substances and their approximate room temperature viscosities to provide context, as in Koop et al. (2011). The image of tar pitch is part of an image from the pitch drop experiment (image courtesy of Wikimedia Commons, GNU Free Documentation License, University of Queensland, John Mainstone).
Figure 3. a) Plot of \( \log(D) - \log(kT/6\pi R_H) \) as a function of \( \log(\eta) \) for new measurements reported in this work and literature data. Indicated in the legend are the diffusing organic molecules studied and the corresponding matrices. \( T \) corresponds to the experimental temperature of each diffusion measurement and \( R_H \) corresponds to the radius of each diffusing species (Section S2 and Table S5). The symbols represent measured data points. The solid line represents the relationship between \( \log(D) - \log(kT/6\pi R_H) \) and \( \log(\eta) \) predicted by the Stokes-Einstein relation, while the dashed line represents the relationship between \( \log(D) - \log(kT/6\pi R_H) \) and \( \log(\eta) \) predicted by a fractional Stokes-Einstein relation with slope = -0.93 and intercept 0.219 (equal to the log of the C value, 1.66). Panels b) and c) are plots of the differences (i.e. residuals) between measured and predicted values of \( \log(D) - \log(kT/6\pi R_H) \) using the Stokes-Einstein relation and the fractional Stokes-Einstein relation, respectively. The sum-of-squared residuals for the Stokes-Einstein relation is 19.7 and the sum-of-squared residuals for the fractional Stokes-Einstein relation is 10.8.
Figure 4. Mixing times of organic molecules within a 200 nm particle as a function of viscosity using the Stokes-Einstein relation (black line) and a fractional Stokes-Einstein relation (red line). The dashed lines indicate that the relations were extrapolated to viscosities beyond the tested range of viscosities (≥ 4 x 10^6 Pa s).
Figure 5. Mixing times (in hours) of organic molecules in 200 nm SOA particles at a) the surface, b) 850 hPa or ~1.4 km altitude, and c) 700 hPa or ~3.2 km altitude, using diffusion coefficients calculated with the Stokes-Einstein relation (solid black lines) and the fractional Stokes-Einstein relation (dashed black lines). A one-hour mixing time, which is often assumed in chemical transport models, is also indicated in each figure with a horizontal dotted line.

References

Abramson, E., Imre, D., Beránek, J., Wilson, J. and Zelenyuk, A.: Experimental determination of chemical diffusion within secondary organic aerosol particles., Phys. Chem. Chem. Phys., 15(8), 2983–2991, doi:10.1039/c2cp44013j, 2013.

Aiken, A. C., Decarlo, P. F., Kroll, J. H., Worsnop, D. R., Huffman, J. A., Docherty, K. S., Ulbrich, I. M., Mohr, C., Kimmel, J. R., Sueper, D., Sun, Y., Zhang, Q., Trimborn, A., Northway, M., Ziemann, P. J., Canagaratna, M. R., Onasch, T. B., Alfarra, M. R., Prevot, A. S. H., Dommen, J., Duplissy, J., Metzger, A., Baltensperger, U. and Jimenez, J. L.: O/C and OM/OC ratios of primary, secondary, and ambient organic aerosols with high-resolution time-of-flight aerosol mass spectrometry, Environ. Sci. Technol., 42(12), 4478–4485, doi:10.1021/es703009q, 2008.

Angell, C. A.: Formation of Glasses From Liquids and Biopolymers, Science, 267(5206), 1924–1935, doi:10.1126/science.267.5206.1924, 1995.

Bastelberger, S., Krieger, U. K., Luo, B. and Peter, T.: Diffusivity measurements of volatile organics in levitated viscous aerosol particles, Atmos. Chem. Phys., 17(13), 8453–8471, doi:10.5194/acp-17-8453-2017, 2017.

Bodsworth, A., Zobrist, B. and Bertram, A. K.: Inhibition of efflorescence in mixed organic-inorganic particles at temperatures less than 250 K., Phys. Chem. Chem. Phys., 12(38), 12259–12266, doi:10.1039/c0cp00572j, 2010.

Booth, A. M., Murphy, B., Riipinen, I., Percival, C. J. and Topping, D. O.: Connecting bulk viscosity measurements to kinetic limitations on attaining equilibrium for a model aerosol composition, Environ. Sci. Technol., 48(16), 9298–9305, doi:10.1021/es501705c, 2014.

Cappa, C. D. and Wilson, K. R.: Multi-generation gas-phase oxidation, equilibrium partitioning, and the formation and...
evolution of secondary organic aerosol, Atmos. Chem. Phys., 12(20), 9505–9528, doi:10.5194/acp-12-9505-2012, 2012.

Champion, D., Hervet, H., Blond, G., LeMeste, M. and Simatos, D.: Translational diffusion in sucrose solutions in the vicinity of their glass transition temperature, J. Phys. Chem. B., 101, 10674–10679, doi:10.1021/jp971899i, 1997.

Chen, Q., Farmer, D. K., Schneider, J., Zorn, S. R., Heald, C. L., Karl, T. G., Guenther, A., Allan, J. D., Robinson, N., Coe, H., Kimmel, J. R., Pauliquevis, T., Borrmann, S., Pöschl, U., Andreae, M. O., Artaxo, P., Jimenez, J. L. and Martin, S. T.: Mass spectral characterization of submicron biogenic organic particles in the Amazon Basin, Geophys. Res. Lett., 36(20), L20806, doi:10.1029/2009GL039880, 2009.

Chen, X. and Hopke, P. K.: Secondary organic aerosol from α-pinene ozonolysis in dynamic chamber system, Indoor Air, 19(4), 335–345, doi:10.1111/j.1600-0668.2009.00596.x, 2009.

Chenakin, Y., Ullmann, D. A., Evoy, E., Renbaum-Wolff, L., Kamal, S. and Bertram, A. K.: Diffusion coefficients of organic molecules in sucrose-water solutions and comparison with Stokes-Einstein predictions, Atmos. Chem. Phys., 17, 2423–2435, doi:10.5194/acp-17-2423-2017, 2017.

Cicerone, M. T. and Douglas, J. F.: Beta-Relaxation governs protein stability in sugar-glass matrices, Soft Matter, 8, 2983–2991, doi:10.1039/c2sm06979b, 2012.

Claeys, M., Graham, B., Vas, G., Wang, W., Vermeylen, R., Pashynska, V., Cafmeyer, J., Guyon, P., Andreae, M. O., Artaxo, P. and Maenhaut, W.: Formation of secondary organic aerosols through photooxidation of isoprene, Science, 303(5661), 1173–1176, doi:10.1126/science.1092805, 2004.

Claeys, M., Szmigielski, R., Kourtchev, I., Van Der Veken, P., Vermeylen, R., Maenhaut, W., Jaoui, M., Kleindienst, T. E., Lewandowski, M., Offenberg, J. H. and Edney, E. O.: Hydroxydicarboxylic acids: Markers for secondary organic aerosol from the photooxidation of α-pinene, Environ. Sci. Technol., 41(5), 1628–1634, doi:10.1021/es0620181, 2007.

Davies, J. F. and Wilson, K. R.: Nanoscale interfacial gradients formed by the reactive uptake of OH radicals onto viscous aerosol surfaces, Chem. Sci., 6(12), 7020–7027, doi:10.1039/c5sc02326b, 2015.

Davies, J. F. and Wilson, K. R.: Raman Spectroscopy of Isotopic Water Diffusion in Ultraviscous, Glassy, and Gel States in Aerosol by Use of Optical Tweezers, Anal. Chem., 88(4), 2361–2366, doi:10.1021/acs.analchem.5b04315, 2016.

Debenedetti, P. G. and Stillinger, F. H.: Supercooled liquids and the glass transition, Nature, 410, 259–267, doi:10.1038/35065704, 2001.

DeCarlo, P. F., Dunlea, E. J., Kimmel, J. R., Aiken, A. C., Sueper, D., Crounse, J., Wennberg, P. O., Emmons, L., Shinozuka, Y., Clarke, A., Zhou, J., Tomlinson, J., Collins, D. R., Knapp, D., Weinheimer, A. J., Montzka, D. D., Campos, T. and Jimenez, J. L.: Fast airborne aerosol size and chemistry measurements above Mexico City and Central Mexico during the MILAGRO campaign, Atmos. Chem. Phys., 8(14), 4027–4048, doi:10.5194/acp-8-4027-2008, 2008.

Deschout, H., Hagman, J., Fransson, S., Jonasson, J., Rudemo, M., Lorén, N. and Braeckmans, K.: Straightforward FRAP for quantitative diffusion measurements with a laser scanning microscope., Opt. Express, 18(22), 22886–22905, doi:10.1364/OE.18.022886, 2010.

Ditto, J. C., Barnes, E. B., Khare, P., Takeuchi, M., Joo, T., Bui, A. A. T., Lee-Taylor, J., Eris, G., Chen, Y., Aumont, B.,
Jimenez, J. L., Ng, N. L., Griffin, R. J. and Gentner, D. R.: An omnipresent diversity and variability in the chemical composition of atmospheric functionalized organic aerosol, Commun. Chem., 1(1), 75, doi:10.1038/s42004-018-0074-3, 2018.

Ediger, M. D.: Spatially Heterogeneous Dynamics in Supercooled Liquids, Annu. Rev. Phys. Chem., 51, 99–128, doi:10.1146/annurev.physchem.51.1.99, 2000.

Edney, E. O., Kleindienst, T. E., Jaoui, M., Lewandowski, M., Offenberg, J. H., Wang, W. and Claeys, M.: Formation of 2-methyltetrols and 2-methylglyceric acid in secondary organic aerosol from laboratory irradiated isoprene/NOX/SO2/air mixtures and their detection in ambient PM2.5 samples collected in the eastern United States, Atmos. Environ., 39(29), 5281–5289, doi:10.1016/j.atmosenv.2005.05.031, 2005.

Ervens, B., Turpin, B. J. and Weber, R. J.: Secondary organic aerosol formation in cloud droplets and aqueous particles (aqSOA): A review of laboratory, field and model studies, Atmos. Chem. Phys., 11(21), 11069–11102, doi:10.5194/acp-11-11069-2011, 2011.

Fisseha, R., Dommen, J., Sax, M., Paulsen, D., Kalberer, M., Maurer, R., Höfler, F., Weingartner, E. and Baltensperger, U.: Identification of organic acids in secondary organic aerosol and the corresponding gas phase from chamber experiments, Anal. Chem., 76(22), 6535–6540, doi:10.1021/ac048975f, 2004.

Först, P., Werner, F. and Delgado, A.: On the pressure dependence of the viscosity of aqueous sugar solutions, Rheol. Acta, 41(4), 369–374, doi:10.1007/s00397-002-0238-y, 2002.

Fox, K. C.: Putting Proteins Under Glass, Science, 267(5206), 1922–1923, doi:10.1126/science.7701317, 1995.

Friedman, C. L., Pierce, J. R. and Selin, N. E.: Assessing the influence of secondary organic versus primary carbonaceous aerosols on long-range atmospheric polycyclic aromatic hydrocarbon transport, Environ. Sci. Technol., 48(6), 3293–3302, doi:10.1021/es405219r, 2014.

Glasius, M., Lahaniati, M., Calogirou, A., Di Bella, D., Jensen, N. R., Hjorth, J., Kotzias, D. and Larsen, B. R.: Carboxylic acids in secondary aerosols from oxidation of cyclic monoterpenes by ozone, Environ. Sci. Technol., 34(6), 1001–1010, doi:10.1021/es990445r, 2000.

Grayson, J. W., Song, M., Sellier, M. and Bertram, A. K.: Validation of the poke-flow technique combined with simulations of fluid flow for determining viscosities in samples with small volumes and high viscosities, Atmos. Meas. Tech., 8(6), 2463–2472, doi:10.5194/amt-8-2463-2015, 2015.

Grayson, J. W., Evoy, E., Song, M., Chu, Y., Maclean, A., Nguyen, A., Upshur, M. A., Ebrahimi, M., Chan, C. K., Geiger, F. M., Thomson, R. J. and Bertram, A. K.: The effect of hydroxyl functional groups and molar mass on the viscosity of non-crystalline organic and organic-water particles, Atmos. Chem. Phys., 17(13), 8509–8524, doi:10.5194/acp-17-8509-2017, 2017.

Green, D. W. and Perry, R. H.: Perry’s Chemical Engineers’ Handbook, 8th ed., The McGraw-Hill Companies, New York, NY., 2007.

Hallquist, M., Wenger, J. C., Baltensperger, U., Rudich, Y., Simpson, D., Claeys, M., Dommen, J., Donahue, N. M., George, C., Goldstein, a. H., Hamilton, J. F., Herrmann, H., Hoffmann, T., Inumya, Y., Jang, M., Jenkin, M. E., Jimenez, J. L., Kiendler-
Scharr, A., Maenhaut, W., McFiggans, G., Mentel, T. F., Monod, A., Prévôt, A. S. H., Seinfeld, J. H., Surratt, J. D., Szmiğielski, R. and Wildt, J.: The formation, properties and impact of secondary organic aerosol: current and emerging issues, Atmos. Chem. Phys., 9(14), 5155–5236, doi:10.5194/acp-9-5155-2009, 2009.

Hawkins, L. N., Russell, L. M., Covert, D. S., Quinn, P. K. and Bates, T. S.: Carboxylic acids, sulfates, and organosulfates in processed continental organic aerosol over the southeast Pacific Ocean during VOCALS-REx 2008, J. Geophys. Res., 115, D13201, doi:10.1029/2009JD013276, 2010.

Haynes, W. M.: CRC Handbook of Chemistry and Physics, 96th ed., CRC Press/Taylor and Francis Group, Boca Raton, FL., 2015.

Heald, C. L., Kroll, J. H., Jimenez, J. L., Docherty, K. S., Decarlo, P. F., Aiken, A. C., Chen, Q., Martin, S. T., Farmer, D. K. and Artaxo, P.: A simplified description of the evolution of organic aerosol composition in the atmosphere, Geophys. Res. Lett., 37(8), L08803, doi:10.1029/2010GL042737, 2010.

Hinks, M. L., Brady, M. V., Lignell, H., Song, M., Grayson, J. W., Bertram, A., Lin, P., Laskin, A., Laskin, J. and Nizkorodov, S. A.: Effect of Viscosity on Photodegradation Rates in Complex Secondary Organic Aerosol Materials, Phys. Chem. Chem. Phys., 18(13), 8785–8793, doi:10.1039/C5CP05226B, 2016.

Hosny, N. A., Fitzgerald, C., Tong, C., Kalberer, M., Kuimova, M. K. and Pope, F. D.: Fluorescent lifetime imaging of atmospheric aerosols: a direct probe of aerosol viscosity, Faraday Discuss., 165, 343–356, doi:10.1039/c3fd00041a, 2013.

Huff Hartz, K. E., Rosenørn, T., Ferchak, S. R., Raymond, T. M., Bilde, M., Donahue, N. M. and Pandis, S. N.: Cloud condensation nuclei activation of monoterpene and sesquiterpene secondary organic aerosol, J. Geophys. Res. D Atmos., 110(14), 1–8, doi:10.1029/2004JD005754, 2005.

Jimenez, J. L., Canagaratna, M. R., Donahue, N. M., Prevot, A. S. H., Zhang, Q., Kroll, J. H., DeCarlo, P. F., Allan, J. D., Coe, H., Ng, N. L., Aiken, A. C., Docherty, K. S., Ulbrich, I. M., Grieshop, A. P., Robinson, A. L., Duplissy, J., Smith, J. D., Wilson, K. R., Lanz, V. A., Hueglin, C., Sun, Y. L., Tian, J., Laaksonen, A., Raatikainen, T., Rautiainen, J., Vaattovaara, P., Ehn, M., Kumala, M., Tomlinson, J. M., Collins, D. R., Cubison, M. J., Dunlea, E. J., Huffman, J. A., Onasch, T. B., Alfarra, M. R., Williams, P. I., Bower, K., Kondo, Y., Schneider, J., Drewnick, F., Borrmann, S., Weimer, S., Demerjian, K., Salcedo, D., Cottrell, L., Griffin, R., Takami, A., Miyoshi, T., Hatakeyama, S., Shimono, A., Sun, J. Y., Zhang, Y. M., Dzepina, K., Kimmel, J. R., Sueper, D., Jayne, J. T., Herndon, S. C., Trimborn, A. M., Williams, L. R., Wood, E. C., Middlebrook, A. M., Kolb, C. E., Baltensperger, U. and Worsnop, D. R.: Evolution of Organic Aerosols in the Atmosphere, Science, 326(5959), 1525–1529, doi:10.1126/science.1180353, 2009.

Jöckel, P., Tost, H., Pozzer, A., Brühl, C., Buchholz, J., Ganzeveld, L., Hoor, P., Kerkweg, A., Lawrence, M. G., Sander, R., Steil, B., Stiller, G., Tanarhte, M., Taraborrelli, D., van Aardenne, J. and Lelieveld, J.: The atmospheric chemistry general circulation model ECHAM5/MESy1: consistent simulation of ozone from the surface to the mesosphere, Atmos. Chem. Phys. Discuss., 6(4), 6957–7050, doi:10.5194/acp-6-5067-2006, 2006.

Koop, T., Bookhold, J., Shiraïwa, M. and Pöschl, U.: Glass transition and phase state of organic compounds: dependency on molecular properties and implications for secondary organic aerosols in the atmosphere, Phys. Chem. Chem. Phys., 13(43), 19.
Lakey, P. S. J., Berkemeier, T., Krapf, M., Dommen, J., Steimer, S. S., Whalley, L. K., Ingham, T., Baeza-Romero, M. T., Pöschl, U., Shiraiwa, M., Ammann, M. and Heard, D. E.: The effect of viscosity and diffusion on the HO2 uptake by sucrose and secondary organic aerosol particles, Atmos. Chem. Phys., 16(20), 13035–13047, doi:10.5194/acp-16-13035-2016, 2016.

Laskin, J., Laskin, A. and Nizkorodov, S. A.: Mass Spectrometry Analysis in Atmospheric Chemistry, Anal. Chem., 90(1), 516–189, doi:10.1021/acs.analchem.7b03429, 2018.

Li, Y. J., Liu, P., Gong, Z., Wang, Y., Bateman, A. P., Bergoend, C., Bertram, A. K. and Martin, S. T.: Chemical reactivity and liquid/nonliquid states of secondary organic material, Environ. Sci. Technol., 49(22), 13264–13274, doi:10.1021/acs.est.5b03392, 2015.

Laskin, J., Laskin, A. and Nizkorodov, S. A.: Exploring matrix effects on photochemistry of organic aerosols, Proc. Natl. Acad. Sci. U. S. A., 111(38), 13780–13785, doi:10.1073/pnas.1322106111, 2014.

Liu, P., Li, Y. J., Wang, Y., Gilles, M. K., Zaveri, R. A., Bertram, A. K. and Martin, S. T.: Lability of secondary organic particulate matter, Proc. Natl. Acad. Sci., 113(45), 12643–12648, doi:10.1073/pnas.160318113, 2016.

Liu, P., Li, Y. J., Wang, Y., Bateman, A. P., Zhang, Y., Gong, Z., Bertram, A. K. and Martin, S. T.: Highly Viscous States Affect the Browning of Atmospheric Organic Particulate Matter, ACS Cent. Sci., 4(2), 207–215, doi:10.1021/acscentsci.7b00452, 2018.

Liu, S., Day, D. A., Shields, J. E. and Russell, L. M.: Ozone-driven daytime formation of secondary organic aerosol containing carboxylic acid groups and alkane groups, Atmos. Chem. Phys., 11(16), 8321–8341, doi:10.5194/acp-11-8321-2011, 2011.

Maclean, A. M., Butenhoff, C. L., Grayson, J. W., Barsanti, K., Jimenez, J. L. and Bertram, A. K.: Mixing times of organic molecules within secondary organic aerosol particles: A global planetary boundary layer perspective, Atmos. Chem. Phys., 17(21), 13037–13048, doi:10.5194/acp-17-13037-2017, 2017.

Marshall, F. H., Miles, R. E. H., Song, Y.-C., Ohm, P. B., Power, R. M., Reid, J. P. and Dutcher, C. S.: Diffusion and reactivity in ultraviscous aerosol and the correlation with particle viscosity, Chem. Sci., 7(2), 1298–1308, doi:10.1039/C5SC03223G, 2016.

Martin, S. T., Andreae, M. O., Althausen, D., Artaxo, P., Baars, H., Borrmann, S., Chen, Q., Farmer, D. K., Guenther, A., Gunthe, S. S., Jimenez, J. L., Karl, T., Longo, K., Manzi, A., Müller, T., Pauliquevis, T., Petters, M. D., Prenni, A. J., Pöschl, U., Rizzo, L. V., Schneider, J., Smith, J. N., Swietlicki, E., Tota, J., Wang, J., Wiedensohler, A. and Zorn, S. R.: An overview of the Amazonian Aerosol Characterization Experiment 2008 (AMAZE-08), Atmos. Chem. Phys., 10(23), 11415–11438, doi:10.5194/acp-10-11415-2010, 2010.

Migliori, M., Gabriele, D., Di Sanzo, R., De Cindio, B. and Correra, S.: Viscosity of multicomponent solutions of simple and complex sugars in water, J. Chem. Eng. Data, 52, 1347–1353, doi:10.1021/je700062x, 2007.

Miller, D. P., Anderson, R. E. and De Pablo, J. J.: Stabilization of lactate dehydrogenase following freeze-thawing and vacuum-drying in the presence of trehalose and borate, Pharm. Res., 15(8), 1215–1221, doi:10.1023/A:1011987707515, 1998.
Mu, Q., Shiraiwa, M., Octaviani, M., Ma, N., Ding, A., Su, H., Lammel, G., Pöschl, U. and Cheng, Y.: Temperature effect on phase state and reactivity controls atmospheric multiphase chemistry and transport of PAHs, Sci. Adv., 4(3), doi:10.1126/sciadv.aap7314, 2018.

Ng, N. L., Canagaratna, M. R., Zhang, Q., Jimenez, J. L., Tian, J., Ulbrich, I. M., Kroll, J. H., Docherty, K. S., Chhabra, P. S., Bahreini, R., Murphy, S. M., Seinfeld, J. H., Hildenbrandt, L., Donahue, N. M., Decarlo, P. F., Lanz, V. A., Prévôt, A. S. H., Dinar, E., Rudich, Y. and Worsnop, D. R.: Organic aerosol components observed in Northern Hemispheric datasets from Aerosol Mass Spectrometry, Atmos. Chem. Phys., 10(10), 4625–4641, doi:10.5194/acp-10-4625-2010, 2010.

Nozière, B., Kalberer, M., Claeys, M., Allan, J., D’Anna, B., De Cesari, S., Finessi, E., Glasius, M., Grgić, I., Hamilton, J. F., Hoffmann, T., Inuma, Y., Jaoui, M., Kahnt, A., Kampa, C. J., Kourtchev, I., Maenhaut, W., Marsden, N., Saarikoski, S., Schnelle-Kreis, J., Surratt, J. D., Szidat, S., Szmigielski, R. and Wisthaler, A.: The Molecular Identification of Organic Compounds in the Atmosphere: State of the Art and Challenges, Chem. Rev., 115(10), 3919–3983, doi:10.1021/cr5003485, 2015.

Pajunoja, A., Malila, J., Hao, L., Joutsensaari, J., Lehtinen, K. E. J. and Virtanen, A.: Estimating the Viscosity Range of SOA Particles Based on Their Coalescence Time, Aerosol Sci. Technol., 48(2), doi:10.1080/02786826.2013.870325, 2014.

Pant, A., Parsons, M. T. and Bertram, A. K.: Crystallization of aqueous ammonium sulfate particles internally mixed with soot and kaolinite: Crystallization relative humidities and nucleation rates, J. Phys. Chem. A, 110(28), 8701–8709, doi:10.1021/jp060985s, 2006.

Perraud, V., Bruns, E. A., Ezell, M. J., Johnson, S. N., Yu, Y., Alexander, M. L., Zelenyuk, A., Imre, D., Chang, W. L., Dabdub, D., Pankow, J. F. and Finlayson-Pitts, B. J.: Nonequilibrium atmospheric secondary organic aerosol formation and growth, Proc. Natl. Acad. Sci. U. S. A., 109, 2836–2841, doi:10.1073/pnas.1119909109, 2012.

Pöschl, U., Martin, S. T., Sinha, B., Chen, Q., Gunthe, S. S., Huffman, J. A., Borrmann, S., Farmer, D. K., Garland, R. M., Helas, G., Jimenez, J. L., King, S. M., Manzi, A., Mikhailov, E., Pauliquevis, T., Petters, M. D., Prenni, A. J., Roldin, P., Rose, D., Schneider, J., Su, H., Zorn, S. R., Artaxo, P. and Andreae, M. O.: Rainforest Aerosols as Biogenic Nuclei of Clouds and Precipitation in the Amazon, Science, 329, 1513–1517, doi:10.1126/science.1191056, 2010.

Power, R. M., Simpson, S. H., Reid, J. P. and Hudson, A. J.: The transition from liquid to solid-like behaviour in ultrahigh viscosity aerosol particles, Chem. Sci., 4(6), 2597–2604, doi:10.1039/C3SC50682G, 2013.

Price, H. C., Murray, B. J., Mattsson, J., O’Sullivan, D., Wilson, T. W., Baustian, K. J. and Benning, L. G.: Quantifying water diffusion in high-viscosity and glassy aqueous solutions using a Raman isotope tracer method, Atmos. Chem. Phys. Discuss., 14, 3817–3830, doi:10.5194/acpd-13-29375-2013, 2014.

Price, H. C., Mattsson, J. and Murray, B. J.: Sucrose diffusion in aqueous solution, Phys. Chem. Chem. Phys., 18, 19207–19216, doi:10.1039/C6CP03238A, 2016.

Quintas, M., Brandão, T. R. S., Silva, C. L. M. and Cunha, R. L.: Rheology of supersaturated sucrose solutions, J. Food Eng., 77(4), 844–852, doi:10.1016/j.jfoodeng.2005.08.011, 2006.

Rampp, M., Buttersack, C. and Luedemann, H. D.: c,T-dependence of the viscosity and the self-diffusion coefficients in some
aqueous carbohydrate solutions, Carbohydr. Res., 328, 561–572, doi:10.1016/S0008-6215(00)00141-5, 2000.

Reid, J. P., Bertram, A. K., Topping, D. O., Laskin, A., Martin, S. T., Petters, M. D., Pope, F. D. and Rovelli, G.: The viscosity of atmospherically relevant organic particles, Nat. Commun., 9, 1–14, doi:10.1038/s41467-018-03027-z, 2018.

Renbaum-Wolff, L., Grayson, J. W., Bateman, A. P., Kuwata, M., Sellier, M., Murray, B. J., Shilling, J. E., Martin, S. T. and Bertram, A. K.: Viscosity of α-pinene secondary organic material and implications for particle growth and reactivity., Proc. Natl. Acad. Sci. U. S. A., 110(20), 8014–8019, doi:10.1073/pnas.1219548110, 2013.

Riipinen, I., Pierce, J. R., Yli-Juuti, T., Nieminen, T., Haekkinen, S., Ehn, M., Junninen, H., Lehtipalo, K., Petaejae, T., Slowik, J., Chang, R., Shantz, N. C., Abbatt, J., Leaitch, W. R., Kerminen, V. M., Worsnop, D. R., Pandis, S. N., Donahue, N. M. and Kulmala, M.: Organic condensation: A vital link connecting aerosol formation to cloud condensation nuclei (CCN) concentrations, Atmos. Chem. Phys., 11, 3865–3878, doi:10.5194/acp-11-3865-2011, 2011.

Rovelli, G., Song, Y. C., Maclean, A. M., Topping, D. O., Bertram, A. K. and Reid, J. P.: Comparison of Approaches for Measuring and Predicting the Viscosity of Ternary Component Aerosol Particles, Submitted to Anal. Chem., n.d.

Saathoff, H., Naumann, K.-H., Möhler, O., Jonsson, Å. M., Hallquist, M., Kiendler-Scharr, A., Mentel, T. F., Tillmann, R. and Schurath, U.: Temperature dependence of yields of secondary organic aerosols from the ozonolysis of α-pinene and limonene, Atmos. Chem. Phys. Discuss., https://doi.org/10.5194/acpd-8-15595-2008, 2009.

Seinfeld, J. H. and Pandis, S. N.: Atmospheric Chemistry and Physics: From Air Pollution to Climate Change, Wiley-Interscience, Hoboken, New Jersey., 2006.

Shamblin, S. L., Tang, X., Chang, L., Hancock, B. C. and Pikal, M. J.: Characterization of the time scales of molecular motion in pharmaceutically important glasses, J. Phys. Chem. B, 103(20), 4113–4121, doi:10.1021/jp983964+, 1999.

Shiraiwa, M. and Seinfeld, J. H.: Equilibration timescale of atmospheric secondary organic aerosol partitioning, Geophys. Res. Lett., 39(24), 1–6, doi:10.1029/2012GL054008, 2012.

Shiraiwa, M., Ammann, M., Koop, T. and Poschl, U.: Gas uptake and chemical aging of semisolid organic aerosol particles, Proc. Natl. Acad. Sci. U. S. A., 108(27), 11003–11008, doi:10.1073/pnas.1103045108, 2011.

Shiraiwa, M., Li, Y., Tsipmida, A. P., Karydis, V. A., Berkemeier, T., Pandis, S. N., Lelieveld, J., Koop, T. and Pöschl, U.: Global distribution of particle phase state in atmospheric secondary organic aerosols, Nat. Commun., 8, 1–7, doi:10.1038/ncomms15002, 2017.

Shrivastava, M., Lou, S., Zelenyuk, A., Easter, R. C., Corley, R. A., Thrall, B. D., Rasch, P. J., Fast, J. D., Massey Simonich, S. L., Shen, H. and Tao, S.: Global long-range transport and lung cancer risk from polycyclic aromatic hydrocarbons shielded by coatings of organic aerosol, Proc. Natl. Acad. Sci., 114(6), 1246–1251, doi:10.1073/pnas.1618475114, 2017.

Shrivastava, M., Cappa, C. D., Fan, J., Goldstein, A. H., Guenther, A. B., Jimenez, J. L., Kuang, C., Laskin, A., Martin, S. T., Ng, N. L., Petaja, T., Pierce, J. R., Rasch, P. J., Roldin, P., Seinfeld, J. H., Shilling, J., Smith, J. N., Thornton, J. A., Volkamer, R., Wang, J., Worsnop, D. R., Zaveri, R. A., Zelenyuk, A. and Zhang, Q.: Recent advances in understanding secondary organic aerosol: Implications for global climate forcing, Rev. Geophys., 55(2), 509–559, doi:10.1002/2016RG000540, 2017.

van der Sman, R. G. M. and Meinders, M. B. J.: Moisture diffusivity in food materials, Food Chem., 138, 1265–1274,
doi:http://dx.doi.org/10.1016/j.foodchem.2012.10.062, 2013.

Song, M., Liu, P. F., Hanna, S. J., Li, Y. J., Martin, S. T. and Bertram, A. K.: Relative humidity-dependent viscosities of isoprene-derived secondary organic material and atmospheric implications for isoprene-dominant forests, Atmos. Chem. Phys., 15(9), 5145–5159, doi:10.5194/acp-15-5145-2015, 2015.

Song, M., Liu, P. F., Hanna, S. J., Zaveri, R. A., Potter, K., You, Y., Martin, S. T. and Bertram, A. K.: Relative humidity-dependent viscosity of secondary organic material from toluene photo-oxidation and possible implications for organic particulate matter over megacities, Atmos. Chem. Phys., 16(14), 8817–8830, doi:10.5194/acp-16-8817-2016, 2016a.

Song, Y. C., Haddrell, A. E., Bzdek, B. R., Reid, J. P., Banan, T., Topping, D. O., Percival, C. and Cai, C.: Measurements and predictions of binary component aerosol particle viscosity, J. Phys. Chem. A, 120(41), 8123–8137, doi:10.1021/acs.jpca.6b07835, 2016b.

Stocker, T. F., Qin, D., Plattner, G.-K., Tignor, M. M., Allen, S. K., Boschung, J., Nauels, A., Xia, Y., Bex, V. and Midgely, P. M., Eds.: IPCC Climate Change 2013: The Physical Science Basis. Contribution of Working Group I to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change, Cambridge University Press, Cambridge, United Kingdom and New York, NY, USA., 2013.

Surratt, J. D., Murphy, S. M., Kroll, J. H., Ng, N. L., Hildebrandt, L., Sorooshian, A., Szmigielski, R., Vermeylen, R., Maenhaut, W., Claeyss, M., Flagan, R. C. and Seinfeld, J. H.: Chemical composition of secondary organic aerosol formed from the photooxidation of isoprene, J. Phys. Chem. A, 110(31), 9665–9690, doi:10.1021/jp061734m, 2006.

Surratt, J. D., Chan, A. W., Eddingsaas, N. C., Chan, M., Loza, C. L., Kwan, a J., Hersey, S. P., Flagan, R. C., Wennberg, P. O. and Seinfeld, J. H.: Reactive intermediates revealed in secondary organic aerosol formation from isoprene, Proc. Natl. Acad. Sci. U. S. A., 107(15), 6640–6645, doi:10.1073/pnas.0911114107, 2010.

Swindells, J. F., Snyder, C. F., Hardy, R. C. and Golden, P. E.: Viscosities of sucrose solutions at various temperatures: Tables of recalculated values., 1958.

Takahama, S., Schwartz, R. E., Russell, L. M., MacDonald, A. M., Sharma, S. and Leaitch, W. R.: Organic functional groups in aerosol particles from burning and non-burning forest emissions at a high-elevation mountain site, Atmos. Chem. Phys., 11(13), 6367–6386, doi:10.5194/acp-11-6367-2011, 2011.

Telis, V. R. N., Telis-Romero, J., Mazzotti, H. B. and Gabas, A. L.: Viscosity of aqueous carbohydrate solutions at different temperatures and concentrations, Int. J. Food Prop., 10(1), 185–195, doi:10.1080/10942910600673636, 2007.

Tsimpidi, A. P., Karydis, V. A., Pozzer, A., Pandis, S. N. and Lelieveld, J.: ORACLE (v1.0): Module to simulate the organic aerosol composition and evolution in the atmosphere, Geosci. Model Dev., 7(6), 3153–3172, doi:10.5194/gmd-7-3153-2014, 2014.

Tsimpidi, A. P., Karydis, V. A., Pozzer, A., Pandis, S. N. and Lelieveld, J.: ORACLE 2-D (v2.0): An efficient module to compute the volatility and oxygen content of organic aerosol with a global chemistry-climate model, Geosci. Model Dev., 11(8), 3369–3389, doi:10.5194/gmd-11-3369-2018, 2018.

Ullmann, D. A., Hinks, M. L., Maclean, A., Butenhoff, C., Grayson, J., Barsanti, K., Jimenez, J. L., Nizkorodov, S. A., Kamal,
S. and Bertram, A. K.: Viscosities, diffusion coefficients, and mixing times of intrinsic fluorescent organic molecules in brown limonene secondary organic aerosol and tests of the Stokes-Einstein equation, Atmos. Chem. Phys., 19, 1491–1503, doi:10.5194/acp-19-1491-2019, 2019.

Vaden, T. D., Imre, D., Beránek, J., Shrivastava, M. and Zelenyuk, A.: Evaporation kinetics and phase of laboratory and ambient secondary organic aerosol, Proc. Natl. Acad. Sci. U. S. A., 108(6), 2190–2195, doi:10.1073/pnas.1013391108, 2011.

Virtanen, A., Joutsensaari, J., Koop, T., Kannosto, J., Yli-Pirilä, P., Leskinen, J., Mäkelä, J. M., Holopainen, J. K., Pöschl, U., Kulmala, M., Worsnop, D. R. and Laaksonen, A.: An amorphous solid state of biogenic secondary organic aerosol particles, Nature, 467(7317), 824–827, doi:10.1038/nature09455, 2010.

Wheeler, M. J. and Bertram, A. K.: Deposition nucleation on mineral dust particles: A case against classical nucleation theory with the assumption of a single contact angle, Atmos. Chem. Phys., 12(2), 1189–1201, doi:10.5194/acp-12-1189-2012, 2012.

Ye, Q., Robinson, E. S., Ding, X., Ye, P., Sullivan, R. C. and Donahue, N. M.: Mixing of secondary organic aerosols versus relative humidity, Proc. Natl. Acad. Sci., 113(45), 12649–12654, doi:10.1073/pnas.1604536113, 2016.

Zaveri, R. A., Easter, R. C., Shilling, J. E. and Seinfeld, J. H.: Modeling kinetic partitioning of secondary organic aerosol and size distribution dynamics: Representing effects of volatility, phase state, and particle-phase reaction, Atmos. Chem. Phys., 14(10), 5153–5181, doi:10.5194/acp-14-5153-2014, 2014.

Zaveri, R. A., Shilling, J. E., Zelenyuk, A., Liu, J., Bell, D. M., D’Ambro, E. L., Gaston, C. J., Thornton, J. A., Laskin, A., Lin, P., Wilson, J., Easter, R. C., Wang, J., Bertram, A. K., Martin, S. T., Seinfeld, J. H. and Worsnop, D. R.: Growth Kinetics and Size Distribution Dynamics of Viscous Secondary Organic Aerosol, Environ. Sci. Technol., 52(3), 1191–1199, doi:10.1021/acs.est.7b04623, 2018.

Zelenyuk, A., Imre, D., Beránek, J., Abramson, E., Wilson, J. and Shrivastava, M.: Synergy between secondary organic aerosols and long-range transport of polycyclic aromatic hydrocarbons, Environ. Sci. Technol., 46(22), 12459–12466, doi:10.1021/es302743z, 2012.

Zhang, Y., Chen, Y., Lambe, A. T., Olson, N. E., Lei, Z., Craig, R. L., Zhang, Z., Gold, A., Onasch, T. B., Jayne, J. T., Worsnop, D. R., Gaston, C. J., Thornton, J. A., Vizuete, W., Ault, A. P. and Surratt, J. D.: Effect of the Aerosol-Phase State on Secondary Organic Aerosol Formation from the Reactive Uptake of Isoprene-Derived Epoxydiols (IEPOX), Environ. Sci. Technol. Lett., 5(3), 167–174, doi:10.1021/acs.estlett.8b00044, 2018.

Zhou, S., Shiraiwa, M., McWhinney, R. D., Pöschl, U. and Abbatt, J. P. D.: Kinetic limitations in gas-particle reactions arising from slow diffusion in secondary organic aerosol, Faraday Discuss., 165, 391, doi:10.1039/c3fd00030c, 2013.