Direct measurement of key exciton properties: Energy, dynamics, and spatial distribution of the wave function

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Abstract: Excitons, Coulomb-bound electron–hole pairs, are the fundamental excitations governing the optoelectronic properties of semiconductors. Although optical signatures of excitons have been studied extensively, experimental access to the excitonic wave function itself has been elusive. Using multidimensional photoemission spectroscopy, we present a momentum-, energy-, and time-resolved perspective on excitons in the layered semiconductor WSe2. By tuning the excitation wavelength, we determine the energy–momentum signature of bright exciton formation and its difference from conventional single-particle excited states. The multidimensional data allow to retrieve fundamental exciton properties like the binding energy and the exciton–lattice coupling and to reconstruct the real-space excitonic distribution function via Fourier transform. All quantities are in excellent agreement with microscopic calculations. Our approach provides a full characterization of the exciton properties and is applicable to bright and dark excitons in semiconducting materials, heterostructures, and devices.

Key points:
- The full life cycle of excitons is recorded with time- and angle-resolved photoemission spectroscopy.
- The real-space distribution of the excitonic wave function is visualized.
- Direct measurement of the exciton-phonon interaction.

KEYWORDS condensed matter physics, exciton physics, many-body physics, quasi-particle interactions, semiconductors, time-resolved photoemission spectroscopy, ultrafast dynamics

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Excitons, bound electron–hole quasi-particles carrying energy and momentum but no net charge, are fundamental excitations of semiconductors and insulators arising from light–matter interaction [1]. An initial excitonic polarization induced by a light field (often referred to as coherent excitons and, e.g., detected by optical absorption spectroscopy) rapidly loses coherence with the driving field and dephases into a population of incoherent excitonic states [2, 3]. The generated excitons propagate in solid-state materials through diffusion [4, 5] and eventually release their energy, for example, in the form of luminescence (photon), lattice excitation (phonon), or dissociation into single-charged quasi-particles [6–9]. Understanding exciton physics is of capital importance for advanced photonic and optoelectronic applications including photocatalysts. Layered transition metal dichalcogenide (TMDC) semiconductors exhibit rich exciton physics even at room temperature due to strong Coulomb interaction [10]. Excitons in TMDCs feature large oscillator strength [11] and their inter- and intraband dynamics have been extensively investigated [12–14]. Moreover, strong spin–orbit coupling and broken inversion symmetry in each crystalline trilayer lead to a locking between spin, valley, and layer degrees of freedom, which started a surge of valley physics studies [15–17].

A large portion of the research on excitonic phenomena in TMDCs adopts optical spectroscopic techniques [10, 12, 14–16, 18–21], which only access bright excitonic transitions with near-zero momentum transfer. Although techniques such as time-resolved THz spectroscopy also allow probing optically dark excitons via internal quantum transitions [13], finite-momentum excitons that lie outside the radiative light cone remain inaccessible to such methods. This limitation is overcome by time- and angle-resolved photoemission spectroscopy (trARPES), a spectroscopic tool accessing excited states, including excitons, in energy–momentum space and on ultrafast time scales [17, 22–24]. Here, we reveal the characteristics of the excitonic wave function in the photoemission signal of the prototypical layered TMDC semiconductor 2H-WSe2 and establish that all fundamental exciton properties are encoded in the trARPES signal’s energy, time, and momentum dimensions: the exciton binding energy, its self-energy as measure of the exciton–lattice coupling, as well as the real-space distribution of the excitonic wave function.

Figure 1a depicts the experimental scheme of trARPES employing femtosecond near-infrared pump and extreme ultraviolet (XUV) probe pulses combined with two types of photoelectron analyzers: a hemispherical analyzer (HA) and a time-of-flight momentum microscope (MM). The whole setup allows us to measure the three-dimensional (3D) time-dependent electronic structure in a given energy–momentum-plane with high counting statistics using the HA, and alternatively resolve both in-plane momentum directions yielding a four-dimensional (4D) photoemission signal \( \{E_{\text{kin}}, k_x, k_y, t\} \) of the entire valence band with the MM [21, 25]. Figure 1b–d and e–g show snapshots of the 3D and 4D data with 1.55 eV excitation, respectively, at three selected time delays: (i) prior to optical excitation, showing the ground-state band structure of WSe2 from the Brillouin zone (BZ) center \( \Gamma \) (only shown in the MM data) to the BZ boundary K points (b and e); (ii) upon optical excitation resonant with the A exciton absorption (the first excitonic state), featuring excited-state signal at the K and \( \Sigma \) valleys (c and f); and (iii) at \( t = 100 \text{ fs} \) after optical excitation, with excited-state signal mostly at the \( \Sigma \) valleys (d and g).

In the following, we identify the excitonic features in the excited state photoemission signal and quantify the exciton properties retrieved from the energy, time, and momentum dimensions of the 4D trARPES signal.

PHOTOEMISSION SIGNATURE OF EXCITONS

During the photoemission of an electron bound in an exciton, the electron–hole interaction diminishes, that is, the exciton breaks up, as a single-particle photoelectron is detected while a single-particle hole is left behind in the material [23]. To identify the signature of the excitonic electron–hole interaction in photoemission spectroscopy, we compare the signal of excitons with that of single-particle excited states. For generating excitons, we excite with 1.55 eV photons (1/e² bandwidth = 43 meV), in resonance with the low-energy side of the A-excitonic absorption of bulk WSe2 [12]. Figure 2a shows the excited-state signal integrated in the first 25 fs after pump–probe overlap. The data reveal a vertical transition at the K point through an excited-state signal localized in energy and momentum. In contrast, the above-band-gap excitation with 3.1 eV photon energy generates a population higher in the conduction band, which rapidly redistributes to all bands and valleys of the lower conduction band (the equivalent scenario applies to the holes in the valence band). Figure 2b shows this excited state signal in the K valley 100 fs after excitation, where carriers have redistributed in energy and momentum. This signal resembles the dispersion of a single-particle band with an effective mass of \( m^* = 0.55 \text{ m}_e \), in good agreement with electronic band structure calculations [26]. The energetic positions of the excitonic and single-particle states at the K point are determined as the center of mass of the energy distribution curves (EDCs), see Figure 2b. The excited-state signal upon resonant excitation of the A exciton is centered 100 ± 3 meV below the center of the single-particle band. Such a signal below the single-particle band has been predicted as photoemission signature of excitons and the energy difference can be associated with the exciton binding energy \( E_b \) [2, 3, 9, 27]. A calculation of the A-exciton binding energy in bilayer WSe2 based on the screened Keldysh-like potential (see the Supporting Information for details) yields \( E_b = 91.3 \text{ meV} \), in very good agreement with the experimental value. It is important to note that we retrieve the exciton binding energy directly from measuring the absolute energies of many-body and single-particle states with a single photoemission experiment, in contrast to combining different experimental methods [18] or by comparing photoemission signals with electronic structure calculations [24]. The observation that the excitonic binding energy is measurable as energy loss of the photoelectron confirms that the hole final states indeed are identical to single-particle holes, which further implies that the localized hole of the exciton transforms to Bloch-like single-particle states during the photoemission process.
FIGURE 1  Multidimensional photoemission spectroscopy of excitons in WSe$_2$: (a) Using near-infrared (1.55 eV) or UV (3.1 eV) pump and XUV probe (21.7 eV), we performed trARPES measurements in bulk WSe$_2$ with two types of photoelectron detectors: hemispherical analyzer (HA) or time-of-flight momentum microscope (MM). (b) With the HA, the equilibrium band structure in a finite momentum window is found at negative pump–probe delay, $t = -100$ fs, showing the spin–orbit split valence bands near the K-points. Upon 1.55 eV excitation, the excited state dynamics, that is, the intervalley scattering from K to $\Sigma$ valley, are representatively shown in (c) $t = 0$ fs and (d) $t = 100$ fs. (e) Four-dimensional (4D) band structure mapping, $I(E, k_x, k_y, t)$, with the MM showing the band dispersion within the whole Brillouin zone from its center $\Gamma$ to the K valleys at its corners. The same evolution of the excited state is shown for (f) $t = 0$ fs and (g) $t = 100$ fs, respectively. All the excited states signal are scaled for clarity.

FIGURE 2  Signatures of excitons versus quasi-free carriers in trARPES. (a) Upon the arrival of the pump photons at $\hbar\omega = 1.55$ eV, the excited states at K and $\Sigma$ are populated. During the pump–probe overlap, sideband replica of the two topmost valence bands, VB1 and VB2, are visible (highlighted by the green dashed lines). Inset: schematic of the bright exciton at the K valley and dark exciton at the $\Sigma$ valley. (b) Using the above-band-gap pump at 3.1 eV, the parabolic dispersion of the conduction band at the K valley is clearly observed. As shown in the energy distribution curves (EDCs) at K (right panel), the single-particle (3.1 eV pump photon energy; blue) is $\Delta E \approx 100$ meV higher than the excitonic signal at 1.66 eV (1.55 eV pump photon energy; red). The excited state signals are scaled for clarity.
To set the stage for discussing the exciton dynamics, we emphasize a signal appearing as replicas of the upper (VB1) and lower (VB2) spin–orbit split valence bands in Figure 2a shifted by the photon energy $\hbar \omega$. This signal only appears during temporal pump–probe overlap and we attribute it to a photon-dressed electronic state due to coherent coupling to the optical driving field. As the employed s-polarized pump light (polarization parallel to the sample surface) suppresses scattering into the optical driving field, the experimental configuration selectively probes the coherent excitonic polarization induced by the pump field [2, 3, 28].

**FORMATION AND DECAY DYNAMICS OF BRIGHT EXCITONS**

The bright A excitons at the K point are not the lowest energy excitons in WSe$_2$ but can relax their energy further by scattering in momentum space. We extract the quasi-particle dynamics within three regions of interest (ROIs) from the trARPES data in Figure 2a, representing the coherent excitonic replica of VB1, the excitonic state at the K valley, and the $\Sigma$ valley population. The respective time traces in Figure 3a reflect three types of quasi-particle dynamics: the dephasing of the coherent excitonic polarization (black), the buildup and relaxation of a bright exciton population at K (blue), and the carrier accumulation of dark states at $\Sigma$ (yellow).

The observed carrier dynamics imply the following microscopic processes as sketched in Figure 3b. First, the interaction of the initial valence band state $|i\rangle$ with the near-resonant optical light field creates a coherent excitonic polarization (dashed line), which quickly dephases into an optically bright exciton population $|n\rangle$, offset by the pump detuning $\Delta_p$. The decoherence process occurs with the pure dephasing time $T_2^\text{ex}$. These bright excitons undergo rapid scattering into the optically dark $\Sigma$-point state $|s\rangle$ on the time scale $T_1$. We model these processes and the photoemission signals from these states into the continuum final states $|f\rangle$ and $|g\rangle$ using a five-level extension to the optical Bloch equations (OBEs; see the Supporting Information). Based on a multivariate least-squares fitting procedure, we are able to describe the dynamics of coherent and incoherent exciton contributions, obtaining a coherent exciton dephasing time of $T_2^\text{ex} = 17 \pm 9$ fs and a population lifetime for the bright A-exciton population of $T_1 = 18 \pm 4$ fs. The extracted dephasing time corresponds well to microscopic calculations [14, 31].

To evaluate the mechanism governing the bright exciton scattering, we performed ab initio calculations of the single-particle self-energy of WSe$_2$. At low excitation densities, the electron self-energy is dominated by electron–phonon interaction that is computed using density functional perturbation theory, taking into account the electronic screening of the lattice motion (see the Supporting Information). The imaginary part of the momentum-resolved self-energy is shown in Figure 3c encoded by the color scale. From the calculation, we obtain $\text{Im}(\Sigma_{\text{el-ph}}) = 13.1$ meV at the conduction band minimum and $\text{Im}(\Sigma_{\text{h-ph}}) = 2.6$ meV at the valence band maximum of the K valleys. Although a rigorous description of exciton–phonon coupling requires treatment on the basis of excitonic eigenstates, in the weak coupling limit, that is, small self-energy renormalization due to the electron–hole interaction, the exciton–phonon self-energy is dominated by its incoherent contribution [32]. In this case, the exciton–phonon interaction can be approximated as sum of the single-particle-phonon interactions. Our calculated value $\text{Im}(\Sigma_{\text{el-ph}}) + \text{Im}(\Sigma_{\text{h-ph}}) = 16$ meV agrees with the experimental exciton self-energy $\text{Im}(\Sigma_{\text{ex}}) = 18 \pm 4.8$ meV determined according to $\text{Im}(\Sigma_{\text{ex}}) = \hbar/(2T_1)$. This agreement with theory shows that the exciton lifetime provides a
quantitative measure of the strength of its interaction with the lattice and supports the assumption of a dominating incoherent self-energy contribution.

**MOMENTUM- AND REAL-SPACE DISTRIBUTION OF A EXCITONS**

Our 4D trARPES data not only provide the energy–momentum dynamics of excitons, but also contain direct amplitude information about exciton wave functions. In Figure 4a, we display the early-time excited-state momentum distribution \( I(k_x, k_y, t = 0 \text{ fs}) \) of the K valleys, by integrating in energy over the conduction band. Signals from other valleys are filtered out in order to focus on the A excitons (see the Supporting Information). The total photoemission intensity is proportional to the squared transition dipole matrix element, 

\[ |M_{jk}|^2 = |\langle \psi_f | A \cdot p | \psi_i \rangle|^2, \]

which connects the initial state wave function \( \psi_i \) to the photoemission final state \( \psi_f \), via the polarization operator \( A \cdot p \). Here, \( A \) is the vector potential of the light field and \( p \) is the momentum operator. Within the plane wave approximation (PWA) for the final state, the matrix element takes the following form:

\[ |M_{ji}|^2 \propto |A \cdot k|^2 \left| e^{ik \cdot r} |\psi_j\rangle \right|^2, \]  

where \( k \) is the wave vector of the photoionized electron. According to Equation (1), the matrix element is proportional to the amplitude of the Fourier transform (FT) of the initial state wave function. Therefore, the momentum distribution of the photoemission signal \( I(k_x, k_y) \) can be used to retrieve the real-space probability density of the electron contribution to the two-particle excitonic wave function, that is, the modulus-squared wave function \( I(r_x, r_y) \), with a suitable assumption for the missing phase information.

A similar reconstruction of electronic wave functions from ARPES spectra has been previously demonstrated for occupied molecular orbitals in the ground state of crystalline organic films and chemisorbed molecular monolayers [33, 34]. Here, we extend this technique into the time domain and apply it to reconstruct the excitonic wave function in WSe₂. Assuming a constant phase profile across the BZ as a lower-limit wave function extension (see the Supporting Information), we retrieve the exciton probability density via two-dimensional FT as shown in Figure 4a and b. The reconstruction exhibits a broad isotropic real-space exciton distribution carrying high-frequency oscillations, corresponding to the hexagonal periodic lattice structure of WSe₂. To resolve the isotropic exciton wave function envelope more clearly, the one-dimensional real-space carrier distribution without the oscillatory pattern is shown in Figure 4d, obtained by FT of only one of the six K valleys.
valleys, yielding a value of $r_{\text{WSe}_2}^{\text{exp}} = 1.74 \pm 0.2$ nm for the excitonic Bohr radius.

To verify the method of reconstructing excitonic wave functions, we performed microscopic calculations of trARPES spectra. The momentum-resolved description of the exciton is based on a many-particle treatment of the Coulomb interaction between electron–hole pairs and the exciton–phonon scattering dynamics [3] (see the Supporting Information). The momentum distributions of the bright K excitons calculated within the PWA for the final state is shown in Figure 4c. We find very good agreement to the experimental momentum distribution curve (MDC) taken along the dashed line in Figure 4a, supporting our assumption that the trARPES spectrum contains the fingerprints of the excitonic wave function and justifying the use of the PWA. Furthermore, the calculated real-space exciton distribution in Figure 4d shows good agreement to our experimental results, yielding a very similar excitonic Bohr radius of $r_{\text{WSe}_2}^{\text{theo}} = 1.78$ nm. This agreement demonstrates the consistency of the experimentally retrieved exciton binding energy and Bohr radius and additionally suggests the validity of the assumption of a constant phase, which provides the FT-limited (lower bound) exciton distribution. Although the excitonic Bloch state is invariant under global and valley-dependent phase renormalization, we find that valley-local phase variations in momentum space can lead to broadening of the exciton probability distribution. In the Supporting Information, we reconstruct the real-space exciton density distribution with nonconstant intervalley and intravalley phase profiles, where we find a broadened exciton distribution in the case of an intravalley varying phase. Therefore, we note here that the real-space reconstruction of the exciton density with a constant phase is suitable for topologically trivial solid-state wave functions. However, the winding of the phase in topologically nontrivial materials leads to an additional expansion of the carrier density distribution, requiring explicit momentum-dependent phase information. In general, the phase of the excitonic wave function might additionally be reconstructed through iterative phase retrieval algorithms [35]. We envision that future developments will allow retrieving the phase as well as orbital information of excitonic wave functions by utilizing dichroic observables [36–38] in trARPES.

In this work, we provide a comprehensive experimental characterization of an excitonic state with trARPES. The interactions governing the formation of this prototypical many-body state are observable as energy renormalization in comparison to single-particle states, while its interaction strength with other quasi-particles is reflected in the excited state’s lifetime. These quantities are intimately connected to the real and imaginary parts of the many-body state’s self-energy and our approach establishes experimental access to these elusive quantities. Moreover, we retrieve real-space information of the excitons by FT of its momentum distribution, establishing the measurement of wave function properties of transient many-body states with 4D photoemission spectroscopy. Our approach is applicable to all exciton species occurring in a wide range of inorganic and organic semiconductors, van der Waals heterostructures, and devices. Its extension to other many-body quasi-particles in solids appears straightforward.

NOTE ADDED IN PROOF
Recently, Man et al. applied a similar approach for retrieving real-space information of excitons with time- and angle-resolved photoemission spectroscopy. Man MKL, Madeo J, Sahoo C, et al., Sci. Adv. 2021;7:eabc0192.

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AUTHOR CONTRIBUTIONS
Shuo Dong: Data curation (Lead); Formal analysis (Equal); Investigation (Lead); Methodology (Equal); Validation (Equal); Writing – original draft (Lead); Writing – review and editing (Equal), Michele Puppin: Data curation (Equal); Formal analysis (Equal); Investigation (Equal); Methodology (Equal); Writing – review and editing (Equal), Tommaso Pincelli: Data curation (Equal); Formal analysis (Equal); Investigation (Equal); Methodology (Equal); Software (Lead); Writing – review and editing (Equal), Samuel Beaulieu: Formal analysis (Equal); Investigation (Equal); Methodology (Equal); Software (Lead); Writing – review and editing (Equal), Dominik Christiansen: Investigation (Equal); Methodology (Equal); Software (Lead); Writing – review and editing (Equal), Hannes Hübener: Formal analysis (Equal); Investigation (Equal); Writing – review and editing (Equal), Christopher Nicholson: Investigation (Supporting); Methodology (Equal); Writing – review and editing (Equal), Rui Patrick Xian: Formal analysis (Equal); Software (Lead); Writing – review and editing (Equal), Maciej Dendzik: Investigation (Equal); Methodology (Equal); Writing – review and editing (Equal), Yoav William Windsor: Methodology (Equal); Malte Selig: Investigation (Equal); Methodology (Equal); Writing – review and editing (Equal), Ermin Malic: Methodology (Supporting), Angel Rubio: Funding acquisition (Equal); Methodology (Equal); Resources (Equal); Supervision (Equal); Writing – review and editing (Equal), Andreas Knorr: Conceptualization (Equal); Funding acquisition (Equal); Methodology (Equal); Project administration (Equal); Resources (Equal); Supervision (Lead); Validation (Equal); Writing – review and editing (Equal).
CONFLICT OF INTEREST
The authors declare no conflict of interest.

DATA AVAILABILITY STATEMENT
We provide the full experimental dataset as well as the details of the data analysis on the data repository Zenodo (https://doi.org/10.5281/zenodo.4739195). Also, we provide the source code of our data analytics on GitHub (https://github.com/mpes-kit).

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SUPPORTING INFORMATION
Additional supporting information may be found online in the Supporting Information section at the end of the article.

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