1 Introduction

Blazars are extragalactic objects with a relativistic jet pointing at us. They often emit most of their electromagnetic output in the γ-ray band, and they are the most numerous class of extragalactic objects detected by the Large Area Telescope (LAT) onboard the Fermi satellite [67] and by on ground Cherenkov telescopes (see [46] for a review). These relatively recent γ-ray data improved the knowledge of the basic properties of blazars, even if, as usually happens, new open issues appeared. Perhaps one of the most puzzling is where, in the jet, most of the luminosity is produced. As discussed below we have conflicting evidences, and suggestions ranging from 0.1 to 10 parsecs.

Another long debated issue is the real existence of a blazar sequence, in which low power blazars are characterized by a Spectral Energy Distribution (SED) with two broad hump peaking respectively in the UV–soft X–ray band, and leave the accretion disk emission unhidden. For them, we can easily and confidently find the black hole mass and accretion rate. Therefore a very promising line of research concerns the hunt of heavy black holes at redshifts greater than 4. The physical motivation is twofold: on one hand discovering a blazar (whose jet is aligned with our line of sight) with a heavy black hole implies the existence of hundreds of similar black holes with jets pointing elsewhere. Discovering a single blazar at $z \sim 6$ with a black hole mass $M > 10^9 M_\odot$ implies the existence of 450–(Γ/15)$^2$ black holes with the same mass. This outnumber the known heavy black holes in radio–quiet quasars at the same redshift (there are ~30 radio–quiet quasars with a spectroscopic redshift $z > 6$ listed in NED, http://ned.ipac.caltech.edu).

The second point concerns the growth of spinning black holes. It is likely, in fact, that relativistic jets are associated with fast spinning holes. In these systems the accretion disk is very radiatively efficient (disk luminosity

Abstract. The Fermi and Swift satellites, together with ground based Cherenkov telescopes, has greatly improved our knowledge of blazars, namely Flat Spectrum Radio Quasars and BL Lac objects, since all but the most powerful emit most of their electromagnetic output at γ-ray energies, while the very powerful blazars emit mostly in the hard X–ray region of the spectrum. Often they show coordinated variability at different frequencies, suggesting that in these cases the same population of electrons is at work, in a single zone of the jet. The location of this region along the jet is a matter of debate. The jet power correlates with the mass accretion rate, with jets existing at all values of disk luminosities, measured in Eddington units, sampled so far. The most powerful blazars show clear evidence of the emission from their disks, and this has revived methods of finding the black hole mass and accretion rate by modelling a disk spectrum to the data. Being so luminous, blazars can be detected also at very high redshift, and therefore are a useful tool to explore the far universe. One interesting line of research concerns how heavy are their black holes at high redshifts. If we associate the presence of a relativistic jets with a fastly spinning black hole, then we naively expect that the accretion efficiency is larger than for non–spinning holes. As a consequence, the black hole mass in jetted systems should grow at a slower rate. In turn, this would imply that, at high redshifts, the heaviest black holes should be in radio–quiet quasars. We instead have evidences of the opposite, challenging our simple ideas of how a black hole grows.
Figure 1. All blazar SED detected in the first three months of operations divided according to their luminosity in the LAT band (0.1–100 GeV): \( \log L_\gamma < 45.5 \) (blue); \( 45.5 \log L_\gamma < 46.5 \) (green); \( 46.5 < \log L_\gamma < 47.5 \) (red); \( \log L_\gamma > 48 \) (black). Solid lines are the phenomenological models in [26], that divided the blazars according to their radio luminosity, assumed to be a good tracer of the bolometric one. Luminosities in erg s\(^{-1}\).\( L_d = \eta \dot{M} c^2 \), with \( \eta \geq 0.1 \) up to \( \eta = 0.3 \); [98]). For this accreting Kerr holes, the Eddington luminosity is reached with a a smaller \( \dot{M} \) than for a Schwarzschild hole. As a consequence an Eddington limited black hole grows at a slower rate, and cannot reach \( 10^9 M_\odot \) at \( z > 4 \). But we do see jetted sources with heavy black holes at \( z > 4 \).

2.1 Interpretation

The blazar sequence was interpreted by [29] as the result of the different amount of radiative cooling in different sources. Low power sources are BL Lac objects, with weak or absent broad emission lines. Being less powerful, their jet presumably carries a weaker magnetic field. The main emission mechanisms are synchrotron and self Compton. Since the cooling is limited, electrons can attain high energies, and they preferentially produce high frequency radiation. As a result, the produced SED is “blue” (namely, the synchrotron peak is at UV or soft X–ray frequencies, while the high energy peak can reach the TeV band. These blazars are also called High frequency BL Lacs, or HBL, by [68]). By increasing the total luminosity, we have objects with strong broad emission lines, and presumably jets with stronger magnetic fields. Cooling is more severe, and the electron energies are smaller. The peak frequencies of the two humps shift to the “red” (sub–mm for the synchrotron, MeV for the Compton. These are called Low frequency BL Lacs, orLBL, by [68]). At the same time, the electrons can scatter seed photons not only produced internally in the jet (i.e., their own synchrotron photons), but also the seeds coming externally (disk, broad line region, torus). The enhanced abundance of seed photons makes the scattering process more important, and the high energy bump is then dominant. This can be demonstrated by applying simple, one–zone, synchrotron + inverse Compton (leptonic) models to blazar samples (for the alternative hadronic models, and a nice comparison between leptonic and hadronic jet models, see [18]).
one relates the energy of the electrons emitting at the peak of the SED with the total (magnetic plus radiative) energy density as seen in the comoving frame, one finds a strong correlation, shown in Fig. 4: high electron energies are possible only if the energy densities are small. This confirms the idea that the blazar sequence is a by–product of the different amount of radiative cooling.

In [24] we divided blazars according to their radio luminosity, thought to be a good tracer of the bolometric one. Now, with the advent of the Fermi satellite, we can divide blazars according to their \(γ\)-ray luminosity in the LAT band \([0.1–100 \text{ GeV}]\). The result is shown in Fig. 1 and agrees remarkably well with the phenomenological solid curves proposed 15 years ago. There is a discrepancy between the phenomenological models and the \(γ\)-ray data at intermediate luminosities, but this can easily be explained remembering that the phenomenological models were built when only the brightest (and more luminous) \(γ\)-ray blazars were known. The conclusion is that Fermi fully confirms the existence of the blazar sequence.

On the other hand, the number of Fermi sources with a featureless spectrum (thus of unknown redshift) is large. These could be genuine BL Lacs without emission lines or FSRQs whose continuum is so beamed to hide the broad emission lines. Many of these sources have a flat \(γ\)-ray spectrum \((α < 1 \text{ when } F_γ \propto ν^{−α})\). As shown by Fig. 4 (empty blue circles), sources with flat \(γ\)-ray spectra are preferentially BL Lacs. If they are at \(z = 4\), then there is a population of BL Lac objects that is very powerful, and nevertheless have a “blue” spectrum. This would contradict the blazar sequence. Rau et al. (2012) [74] succeeded to put limits on the redshifts of these objects, by using the GROND instrument (giving 7 photometric data simultaneously, from near infrared to optical) together with UVOT (onboard Swift) giving 6 optical–UV photometric data. If a source is at high–z, the intervening material imprints absorption features in the spectrum (Lyman–α forest and edge) that can be used to estimate a photometric redshift. Fig. 3 reports the results: the green diamond (with a black dot) correspond to the sources with \(γ\)-ray features that can be used to estimate a photometric redshift, \(z_\text{max}\), the limit at which the host galaxy should be visible.

![Figure 3. The energy spectral index \(α_γ\) as measured by Fermi as a function of their \([0.1–10 \text{ GeV}]\) (rest frame) luminosity. Red points are FSRQs, blue circles are BL Lacs. The sources studied in [74] are plotted with larger symbols if the redshift is determined (spectroscopically or photometrically). Sources with only an upper limit for the photometric redshifts are plotted assuming a luminosity the upper limit as the maximum redshift, and \(z_\text{max} = 0.3\) as the minimum (this corresponds approximately to the limit at which the host galaxy should be visible).](image)

### 2.2 Dividing FSRQs and BL Lacs

As mentioned in the introduction, the traditional division between FSRQs and BL Lacs is based on the EW of the broad emission lines. Furthermore, the parent population (i.e. the misaligned counterparts) of FSRQs is made by powerful FR II radio–galaxies, while the parents of BL Lacs are low power FR I radio-galaxies. There are however several exceptions to this rule, and intermediate objects exist. Furthermore, according to [79] there is a continuity between BL Lac and FSRQs in the MgII line luminosity with no clear separation of blazars in the two subclasses.

In investigating the 4 sources with the flat \(γ\)-ray spectra and the measured photometric redshift, [38] concluded that they are FSRQs with relatively weak accretion disk luminosity and with a strongly boosted jet continuum. The energy \(γ\)–peak of the relevant electrons of these sources is shown in Fig. 2. They well agree with the general correlation, but lie in the “blue part” (high \(γ\)–peak), where usually we find low power BL Lacs. Another example is the blazar PMN J2345–1555: it is usually characterized by a “red” spectrum, but during a flaring episode, it became “blue”. This was interpreted by [39] as a change in the location of the dissipation region along the jet, where most of the flux is produced: usually it is within the broad line region (BLR), where the presence of broad line photons ensures a large radiation energy density and thus a small \(γ\)–peak and a red spectrum. Occasionally, the dissipation region may move beyond the BLR: there the decreased radiation energy density let the electrons reach large \(γ\)–peak (Fig. 2), making the spectrum blue.
more, since there are estimates of the black hole mass for a good fraction of the sample, we could also see at which $L_{\text{BLR}}/L_{\text{edd}}$ there is the divide between BL Lacs and FSRQs. We found a value $L_{\text{BLR}}/L_{\text{edd}} \approx 5 \times 10^{-4}$, as shown in Fig. 4. Since the disk luminosity $L_d \sim 10^{-2} L_{\text{BLR}}$, this is in good agreement with the value suggested earlier by [31] on the basis of the BL Lac/FSRQs division in the $\alpha_{\gamma}-L_{\alpha}$ plane, and by [51] on the basis of the FR I/FR II division in the radio power – galaxy bulge optical luminosity plane.

2.3 Accretion and the blazar sequence

For what discussed above, we can draw the conclusion that the jet power in blazars correlates with the accretion rate of their accretion disks. Since we also know the black hole masses of several blazars, we can also say that: i) the blazar' divide occurs at $L_d \sim 10^{-2} L_{\text{edd}}$; ii) jets are present for all $L_d/L_{\text{edd}}$ we can measure, i.e. from below $L_d/L_{\text{edd}} \sim 10^{-4}$ to 1. In addition, the jet power often exceeds the disk luminosity ([21], [36]). We can envisage two scenarios for explaining the FSRQs/BL Lac divide:

1. At the critical luminosity $L_d \sim 10^{-2} L_{\text{edd}}$, the disk accretion changes nature, from being radiatively efficient to radiatively inefficient. In other words the efficiency $\eta$ in $L_d = \eta M c^2$ is constant ($\eta \sim 0.1$) for $L_d \geq 10^{-2} L_{\text{edd}}$, while it decreases for lower values [65], [66]. The disk becomes geometrically thick as the result of inefficient proton cooling, since electrons and protons are decoupled, and protons remain hot. The main radiation mechanism in these conditions are cyclo–sychrotron, bremsstrahlung and inverse Compton scattering [57]: the amount of UV photons to ionize the clouds of the BLR decreases dramatically. Emission lines then becomes very weak or even absent. The power of the jet, however, continues to be proportional to $M$. If in this regime $L_d \propto M^2$, as suggested by [68], then $P_{\text{jet}}/L_d \propto M$.

2. The divide between radiatively efficient and inefficient disks might occur at values of $L_d/L_{\text{edd}}$ smaller than $10^{-2}$. Sharma et al. (2007) [82], indeed, suggest a smooth transition around $10^{-2}$. In this case there is not a sharp decrease of the UV ionizing radiation, and weak broad emission lines continue to be produced. The ionizing luminosity, however, correlates with the size of the BLR $R_{\text{BLR}}$ (as $R_{\text{BLR}} \propto L^{1/5}$), so in these sources $R_{\text{BLR}}$ is small, and it is very likely that the jet produces most of its non–thermal luminosity beyond $R_{\text{BLR}}$. This could explain why broad lines are visible even in BL Lac itself or in Mkn 421 and Mkn 501 [63, 89].

3 One–zone model?

In the early and mid ‘80s it was thought that the observed non–thermal luminosity was produced all along an inhomogeneous jet ([64], [53], [28], see [72] for a revival) with magnetic field and particle density that were power law functions of the distance from the black hole. As a consequence, the flux at different frequencies was produced mainly at different jet locations, with different variability timescales. The high energy hump of the SED was not yet discovered, and 3C 273 was the only quasar detected in $\gamma$–rays (by the COS–B satellite, [13]). When EGRET discovered that blazars were strong $\gamma$–ray emitters as a class [45], it was also discovered that the optical, the X–ray and the $\gamma$–ray fluxes often varied simultaneously, shifting the “inhomogeneous jet” paradigm to the simpler “one–zone” model. Having fewer parameters, this model played a crucial role for our understanding of jets, and this is the reason of its success.

However, we should not forget that this model adopts a drastic simplification: after all we do see, also in the radio VLBI maps, that the jet is composed of several distinct knots, and it is therefore very likely that also on the sub–pc scale there is more than one zone contributing to the observed flux, even if a single one may dominate in one particular frequency range. These sub–components could vary independently, and possibly have a lifetime comparable to the light crossing time, since the cooling time (both radiative and adiabatic) of their radiating particles is short. At any given time, we may see one or more than one component. Since the locations of these components will be different, their size will also be different, as well as their magnetic field and the amount of the external radiation they see.
we assumed: $M = 10^8M_\odot$, $L_\odot = 10^{39}$ erg s$^{-1}$, $z = 3$ and $\Gamma = \min[15, (R_{\text{dis}}/3R_0)^{1/2}]$. $U'_\gamma$: magnetic energy density; $U'_\text{BLR}$: radiation coming directly from the disk, assumed to be a standard Shakura–Sunyaev disk [34]; $U'_\text{BLR}$ and $U'_{\text{IR}}$: contribution from the BLR and the molecular torus, respectively; $U'_C$: contribution from the X-ray corona emission; $U'_\text{CMB}$: contributions from the Cosmic Microwave Background. The grey vertical lines indicate the distances used to construct the SEDs shown in Fig. 5.

3.1 Location of the main emission region

In [34], we studied how the different radiation energy densities change as a function of the distance $R_{\text{dis}}$ from the black hole. This is illustrated in Fig. 5. This figure shows the energy densities as observed in the comoving frame of a jet that is accelerating (as $\Gamma \propto R^{1/2}$, see e.g. [102]) in its inner part, until it acquires a final value of $\Gamma$. Beyond the BLR the line seed photons are seen from behind, and are more and more de–beamed as the distance increases. This makes $U'_{\text{BLR}}$ to decrease faster than $R^{-2}$. In analogy with radio–quiet quasars, we calculate the contribution to the external radiation energy density of a molecular torus, intercepting a substantial fraction of the disk luminosity and re–emitting it in the IR [34]. The distance from the black hole of this structure is much larger than $R_{\text{BLR}}$ and the corresponding $U'_{\text{IR}}$ is smaller. For the magnetic field, we simply assume that the Poynting flux $L_B \propto R_{\text{dis}}^{-1} \Gamma^2 B^2$ carried by the jet is a constant fraction of the jet total power. For a constant $\Gamma$ this implies $B \propto R_{\text{dis}}^{-1}$. At large distances (i.e. several kpc away) the dominant contribution to the external radiation energy density becomes the Cosmic Microwave Background (CMB), with a corresponding $U'_{\text{CMB}} \propto \Gamma^2(1+z)^4$. These simple and reasonable scalings play a major role in shaping the SED. In fact, for different $R_{\text{dis}}$, i.e. the location where the jet transforms part of its power into radiation, the ratio $U'_{\gamma}/U'_{\text{CMB}} \approx L_{\text{jet}}/L_{\text{syn}}$ is very different. The Compton dominance, defined as the ratio between the inverse Compton to synchrotron luminosities, $L_{\text{C}}/L_{\text{syn}}$, is maximized at specific distances. To better illustrate this point, we have labelled in Fig. 7 the distances $R_{\text{dis}}$ of maximum Compton dominance (labelled 2 and 4). We expect $L_{\text{C}}/L_{\text{syn}} \sim 1$ at the distances labelled 1, 3 and 5. A synchrotron dominated SED is expected only beyond point 5, with a minimum Compton dominance at distance 6. Beyond that, if the jet continues to remain relativistic with the same $\Gamma$, $U'_{\text{CMB}}$ takes over and $L_{\text{C}}/L_{\text{syn}} \gg 1$ again. Going back to Fig. 5 we can calculate the SED resulting from dissipation at different $R_{\text{dis}}$, with the following recipe:

1. we calculate the SED each decade of $R_{\text{dis}}$, from $R_{\text{dis}} = 10^3R_0$ to $10^9R_0$ (one per decade). The injected electron luminosity is $P'_{\gamma} = 10^{38}$ erg s$^{-1}$ for $R_{\text{dis}} = 10^9R_0$ and is reduced by a factor 3 each decade. The particle distribution has always the same $\gamma_{\text{min}} = 100$, while $\gamma_{\text{max}}$ increases by a factor 3 each decade starting from $\gamma_{\text{max}} = 10^3$ for $R_{\text{dis}} = 10^9R_0$. The shown spectra neglect the absorption of the high energy flux due to the IR–opt–UV cosmic background. The numbers correspond to the same numbers of Fig. 5. The thicker black line is the sum of all the SEDs. The grey line at radio frequencies indicates $F(\nu) \propto \nu^0$. The flux is calculated assuming $z = 3$. Adapted from [34].
100 and $\gamma_{\text{max}} \propto R_{\text{diss}}^{1/2}$, starting from $\gamma_{\text{max}} = 10^3$ at $R_{\text{diss}} = 10^3 R_S$;

4. the Poynting flux remains constant after the acceleration region. This implies $B^2 \Gamma^2 R_{\text{diss}}^2 = \text{const}$;

5. the particle distribution is calculated through the continuity equation at a time equal to the light crossing time which is also the dynamical time, namely the time required to double the size of the source. Continuous injection of relativistic particles, radiative cooling and electron–positron pair production are accounted for.

With the above prescriptions, the density $n$ of the relativistic particles scales approximately as $n \propto R_{\text{diss}}^2$ while $B \propto R_{\text{diss}}^{-1}$. If the jet were continuous, and not fragmented into several blobs, we would obtain a flat radio spectrum, with a self-absorption frequency scaling as $R_{\text{diss}}^{-1}$. The sum of the emission of our discrete components (black thick line in Fig. 4) is not far from this, as can be appreciated comparing with the grey oblique line indicating a $F(\nu) \propto \nu^0$ spectrum. The SEDs in Fig. 5 show a great diversity and a non–monotonic behavior, but this is in agreement with the $U''_{\text{rad}}/U''_B$ ratio shown in Fig. 5. Particularly interesting is the fact that $\gamma$–ray spectrum in the GeV band is dominated by the innermost emitting zone, while the X–ray flux receives the contributions from the first 3 zones. This would imply a variability of the GeV flux more pronounced and faster than the X–ray flux, in agreement with what observed in powerful blazars where the [0.3–10 keV] flux is produced by the inverse Compton process. In these examples, the synchrotron self–Compton process is unimportant for all SEDs but the number 4, which is the one with the smallest Compton dominance. At larger distances, in fact, $U''_{\text{CMB}}$ becomes larger than $U''_B$ and the Compton dominance increases again. These large regions of the jet emit most of their flux in the MeV–TeV band.

To conclude this section, note that the most efficient location to produce the largest amount of $\gamma$–rays is at $10^3$ and around $10^4$ Schwarzschild radii, corresponding to 0.1 and 1 pc. In these two locations there is the largest amount of seed photons and the maximum $\Gamma$. At smaller radii the disk radiation may be even larger, but the beaming is modest, at larger radii the broad lines or the IR photons coming from the torus are seen coming from the back, and are not boosted any longer.

This apparently reasonable conclusion is challenged by two facts. The first is that in some sources there is a correlation between the radio flares, the switch in polarization angle and the occurrence of $\gamma$–ray flares (see, e.g. [51], [63]), suggesting that also the $\gamma$–ray emission originates in a region more than one parsec away from the black hole. The second issue is the variability of the TeV emission, which in some source is embarrassingly fast, as discussed below.

![Figure 7](https://example.com/figure7.png) 

**Figure 7.** Similar to Fig. 5 to illustrate the distances where the largest and the smallest Compton dominance are predicted. The used parameters are for PMN J2345–1555, the FSRQs that became “blue” during a flare [39]. The numbers next to the circles and arrows correspond to the location where $U''_B$ is equal to the dominant form of radiation energy density (points 1, 3 and 5), and where instead the ratio between the radiative and magnetic energy density is maximized (arrows 2, 4) leading to the maximum expected Compton dominance. Arrow 6 corresponds instead to a synchrotron dominated SED.

### 3.2 Fast TeV variability, a puzzle

Ground based Cherenkov telescopes collect enough photons to study fast variability of bright blazars, even on timescales of minutes. And they did discover that the TeV flux is sometimes varying on these timescales, which is the shortest observed at any wavelength. The BL Lac objects Mkn 501 ($\tau = 0.0336$) and PKS 2155–304 ($\tau = 0.116$) showed variations on $t_{\text{var}} = 3–5$ minutes of their TeV flux [4], [4]. This challenged models in which the minimum variability timescales is related to the light crossing time of the Schwarzschild radius of the black hole of the system (see e.g. [11]), and strongly suggested that the region emitting these ultrafast TeV flares is very compact, smaller than the distance light travels in one year. Nevertheless the location of this TeV emitting region could still be at $R_{\text{diss}} \sim 10^3 R_S$, where we think that most of the dissipation is taking place. In this case we have a “jet in a jet”, or rather “needle in a jet” scenario, where the compact TeV emitting zone is immersed in a larger and active jet zone, and can use the seed synchrotron photons produced by the larger region to produce the TeV flux. This is allowed by the absence, in these BL Lac objects, of broad emission lines: while helping the very production of MeV–GeV photons (because they are used as seeds for Compton scatterings), the line photons act as killers of $\gamma$–rays above...
a few tens of GeV, through photon–photon collisions (see e.g. [55], [91] and [73]).

According to the above idea, FSRQs (with prominent emission lines) should not be strong TeV emitters, and instead a few of them are. Up to now we know 3 TeV (\(\gamma\) = 0.36) [105], and PKS 1222+216 (\(z = 0.431\)) [10]. To these sources one can add PKS B1424–418 (\(z = 1.52\)), not detected in the TeV band, but with photons above tens of GeV detected by Fermi [95] varying on a ~day timescale.

PKS 1222+216 doubled its TeV flux in just 10 minutes, constraining the emitting region size to be \(R < \frac{c t_{\text{var}}}{\delta/(1+z)} \approx 5 \times 10^{14}(6/20)\) cm (\(\delta\) is the relativistic Doppler factor). This is an extremely compact region, and yet cannot be located within the BLR, whose photons would absorb the emission above ~20 GeV. The TeV emitting region must be located outside. This remains true even if the BLR has a flattened geometry (as suggested by e.g. [84]; [49]; and [24]), as shown in [96].

At \(R > R_{\text{BLR}}\) the radiation field is dominated by the thermal radiation of the dusty torus [16] and the opacity is smaller. We must conclude that the varying TeV emitting region is both small and very distant from the black hole. It is a bullet (or a bomb) with a milli–pc size at a distance of more than a pc. Ideas to explain it involve strong collimation and focusing of the flow (e.g. [88]; [19]; [64] or complex reconnection events [42], or the existence of new particles, like axions: in this case high energy photons could be produced within the BLR, be converted into axions, insensitive to \(\gamma\)–\(\gamma\) → e± processes, and converted again into photons at large distances [94].

### 3.3 Tentative summary

Most of the time and in most of the sources, there is one preferred location in the jet where most of the jet bolometric luminosity is produced, from the IR to the \(\gamma\)–rays. Usually this is within the BLR, at \(~10^5R_\odot\), rarely beyond. This can be proved by the presence of a break at \(~10\) GeV due to \(\gamma\)–\(\gamma\) → e±e± [73] in bright \(\gamma\)–ray FSRQs with enough photons above 10 GeV. Other emitting regions are however likely. Even if their bolometric output is less, they may significantly contribute to the flux in specific bands, especially in the soft X–rays and the optical.

Sometimes much smaller jet regions become active, not only at a distance \(~10^3R_\odot\) from the black hole, but also much further out. The ratio between the distance and their size can approach \(10^5\) (i.e. one parsec over a milli–parsec). The geometry and the emission processes of these regions is an open issue. However we can infer that their spectrum is peaked at high \(\gamma\)–ray energies, since we never saw extremely fast variability at other well–sampled frequencies, such as soft X–rays.

The presence of sub–jet regions is also inferred by the X–ray emission observed by the \textit{Chandra} satellite at hundreds of kpc away from the nucleus (see e.g. [85] for review). This emission is interpreted as inverse Compton scattering of relativistic electrons off the CMB photons, requiring the jet to have a bulk Lorentz factor of \(~10\) also at that distances. The radiative cooling time of the emitting electrons is very long, and also the adiabatic cooling timescale is long if one assumes that the emission comes from a blob with a radius equal to the entire cross section of the jet. If so, the X–ray knot should be resolved by \textit{Chandra}, and instead it is not. A solution to this puzzle is that the emitting size is much smaller than the cross sectional radius of the jet, to let the emitting electrons lose energy by adiabatic losses before they cross the jet [50].

### 4 Black hole masses of blazars

#### 4.1 Virial methods

Virial methods have become popular to measure the black hole mass. They are based on the assumption that gravity controls the velocity of the clouds of the BLR. Through reverberation mapping ([15]; [71]) one estimates \(M_{BLR}\), while the Full Width Half Maximum (FWHM) of the broad lines is associated to the velocity \(v_{BLR}\) of the clouds (\(v_{BLR} = f \cdot \text{FWHM}\), with \(f\) of order unity). The black hole mass is found through \(M = M_{BLR} v_{BLR}^2 / G\). The number of AGN with a BLR size measured directly through reverberation mapping is very small, but good correlations exist between \(M_{BLR}\) and the ionizing luminosity of the accretion disk ([52]; [12]), or to the monochromatic disk luminosity at specific frequencies (with the implicit assumption that the disk spectrum does not greatly change from one object to the other). A single spectrum then allows to measure both the FWHM of the line and the ionizing disk luminosity, and then the black hole mass. The uncertainty of these estimates is large, of the order of 0.5–0.6 dex [101], [70]. In addition, there may be systematic uncertainties related to the BLR geometry ([23]; [24]) and the role of radiation pressure [54]. This large uncertainty is one of the reasons why there is still a debate about the difference in black hole masses in radio–loud and radio–quiet sources. A correlation between black hole mass and radio–loudness was claimed by [27] and [54], but instead [108] found that both the radio–quiet and radio–loud AGN span the same range of black hole mass, with no evidence for a correlation between radio loudness and black hole mass. However, [22], taking into account radiation pressure to compute the virial black hole masses, recently found that \(M > 10^8 M_\odot\) is required to produce a radio–loud AGN.

#### 4.2 Accretion disk fitting

This was the first method (in the 80s) to measure the black hole mass and the accretion rate in quasars [84], [58], but was not widely used thereafter (see [20] for a critical discussion). A revival of this method occurred recently, mainly because i) the availability of large sample of distant quasars: often this allows to observe directly the redshifted peak of the accretion disk emission in the optical; ii) the better knowledge of the different components contributing to the IR–UV spectrum of a typical quasar; iii) the realization that even when the peak emission is not seen, the broad lines can give an estimate of the total disk luminosity. The latter point is particularly useful for blazars, where...
the accretion disk continuum can receive a substantial contribution from the non-thermal jet component.

The simplest disk model to fit the accretion disk spectrum is the Shakura & Sunjaev [80] model. It assumes a Schwarzschild black hole, a geometrically thin, optically thick disk that emits as a blackbody at each radius. Although these assumptions appear rather crude at first sight, they are not as bad as they seem [20], and can give a good estimate of the black hole mass of the object. The uncertainty associated to this method depends on the data quality: if the peak of the disk emission is visible, then the uncertainty on the black hole mass is less than a factor 2.

4.3 Blazars and accretion disk emission

Powerful blazars are “red”, with a synchrotron component peaking in the sub-mm band and steep in the IR–optical. This leaves their accretion disk component “naked”, and well visible. To illustrate this point, Fig. 8 shows the SED of PKS 0836+710 (z = 2.17). The labels indicate the different components: the dashed black line correspond to the accretion disk, the IR torus and the X–ray corona emissions; the green solid line is the synchrotron component, the long dashed grey line is the SSC contribution, and the dot–dashed grey line is the EC component, dominating the high energy hump. The disk emission component, and its peak, are clearly visible. In these cases it is possible to derive \( M \sim 3 \times 10^9 M_\odot \), and \( \dot{L}_d \sim 2 \times 10^{47} \) erg s\(^{-1}\), nearly half the Eddington luminosity \([35]\). This source is present in the catalog of Fermi sources that collects sources detected during the first 2 years of the mission, [5], but not in the 1LAC (first year, [2]), not in the LBAS (first 3 months, [1]), even if it is one of the most powerful blazar. On the contrary, it has been detected during the 3–years survey of the BAT instrument onboard Swift [7].

Fig. 9 shows the SED of the second most distant blazar known, B2 1023+25, at \( z = 5.3 \), selected as a blazar candidate because of its radio brightness and large radio–loudness, and soon after confirmed as a blazar by Swift X–ray observation in the 0.3–10 keV band [78]. Although the received X–ray photons were a few, they suggest a large flux and a hard spectrum, two signatures of a blazar. B2 1023+25 was selected within the ~ 8,800 square degrees covered both by the SDSS (Sloan Digital Sky Survey) and FIRST (Radio Images of the Sky at Twenty-Centimeters). It implies the existence of other ~3 similar blazars (all sky) and then ~1800 intrinsically similar blazars, but misaligned (all sky). The fact that its black hole mass is \( M \sim 3 \times 10^9 M_\odot \) implies the existence of other ~1800 black holes in jetted sources as heavy as that at the same redshift. At \( z \sim 5.3 \), the Universe was only one billion years old. Through these numbers one can understand why the search for heavy black holes in blazars can help the study of black formation and growth at high redshift, even challenging similar studies based on searches of radio–quiet objects.
4.4 Early and heavy black holes

According to the blazar sequence, and to the evidences gathered so far, powerful blazars emit most of their luminosity in the high energy hump, which peaks between 1 and 10 MeV. Being so powerful, these blazars can be detected also at high redshifts, and thus shed light on the far Universe. The two main instruments best suited to find blazars at high redshifts are BAT (15–150 keV), onboard Swift and LAT (0.1–100 GeV), onboard Fermi. The INTEGRAL satellite is somewhat more sensitive than BAT in the same energy range, but a significant fraction of the exposure time is dedicated to observations of sources in the Galactic plane, while BAT, which follows Gamma Ray Bursts, is observing more uniformly the entire sky.

BAT, after the first 3 years of operations, detected 38 blazars. 10 of them have \( z > 2 \). Of these, 5 have \( z > 3 \). LAT instead detected 31 blazars at \( z > 2 \) in two years, but only 2 have \( z > 3 \). These numbers, albeit small, already suggest that the hard X–ray band is more efficient than the GeV band to find out high–redshift powerful blazars. In [35] and [103] we have considered all 10 BAT blazars at \( z > 2 \), finding that all of them have black hole masses \( M > 10^9 M_\odot \), and all of them have a [15–55 keV] luminosity greater than \( 1.5 \times 10^{47} \text{ erg s}^{-1} \). The latter point allowed to associate the luminosity function of BAT blazars in [7] to the mass function of heavy (i.e. \( M > 10^9 M_\odot \)) and active (\( L_\gamma > 0.1 L_{\text{Edd}}^\gamma \)) black holes. Conservatively, we have also modified the luminosity function in [7] adding an exponential cut above \( z = 4 \), where [7] had no data. In the 4–5 redshift bin, however, we have 4 serendipitously discovered blazars with \( M > 10^9 M_\odot \) [104], [47], [109] and [110], and two blazars at \( z > 5 \): one is the most distant blazar known, Q0906+6930 at \( z=5.47 \), [75] (green pentagon in Fig. 10) and the other is the recently discovered blazar B2 1023+25 [78], which was discovered through a selection within the SDSS+FIRST survey (yellow pentagon).

For each detected blazar, there must be other 2\( T^2 = 450(1/15^2) \) other sources pointing away from us, and we have adopted \( \Gamma = 15 \) as the typical bulk Lorentz factor of the relativistic jets [46]. The result showed that the mass function of heavy black holes, as a function of redshift, had a peak at \( z \sim 4 \) (see the red stripe in Fig. 10). This was surprising, since the mass function of heavy and active black holes in radio–quiet objects has a peak at \( z \sim 2 \) (blue lines in Fig. 10). However, for the jetted sources, we had considered only BAT blazars. There could be the possibility that many more heavy and active black holes could be revealed by LAT, possibly preferentially at \( z \sim 2 \), to re–establish a symmetry with radio–quiet objects. But when the \( \gamma–\text{ray} \) luminosity function was derived by [48], we could calculate the mass function of heavy and active black holes of LAT blazars, which is illustrated in Fig. 10 by the green stripe [48]. There are too few LAT blazars with heavy and active black holes to shift the peak from \( z \sim 4 \) to \( z \sim 2 \). We must therefore take this result seriously. We are led to conclude that most massive black holes forms at two epochs: in jetted sources they form earlier (\( z \sim 4 \)) than in radio–quiet objects (\( z \sim 2 \)).

As a consequence of the two different formation epochs, the ratio of radio–loud to quiet sources with a heavy black hole is strongly evolving. We stress that this refers only to those sources hosting a black hole with \( M > 10^9 M_\odot \), not to the entire population of quasars.

4.5 Black hole growth and spin

It is popular to associate the presence of a relativistic jet with a black hole spinning rapidly. In fact, the rotational energy of the hole can be an important source of power for the jet ([14], [97]). This led to the idea that the radio–loud/radio–quiet dichotomy is associated to the value of the spin ([107], [57]). Since for spinning black holes the innermost stable orbit moves inward as the spin increases, the accretion efficiency also increases, to reach a theoretical maximum of \( \eta = 0.42 \) for a dimensionless spin value.
Accretion starts at rate as a function of time (bottom axis) and redshift (top axis).

Figure 11. The mass of a black hole accreting at the Eddington rate as a function of time (bottom axis) and redshift (top axis). Accretion starts at $z = 20$ onto a black hole seed of $10^4 M_\odot$, $10^5 M_\odot$, or $10^6 M_\odot$, with different efficiencies, as labeled. The horizontal line marks one billion solar masses. The larger $\eta_d$, the smaller the amount of accreted mass needed to produce a given luminosity, and the longer the black hole growing time. If part of the accretion energy goes into launching a jet, however, $\eta_d < \eta$ and the growth time decreases. From [40].

\( M = \eta M c^2 \), where $M$ is the mass accretion rate. However, [98] pointed out that if the disk is emitting, there is a torque exerted by the photons on the hole, inhibiting it to spin with $\omega = 1$. The maximum value is $a = 0.998$, corresponding to a maximum $\eta = 0.3$. This means that, with respect to a Schwarzschild black hole with $\eta \sim 0.06$, a maximally spinning hole allows to reach the Eddington luminosity with 1/5 of the accretion rate. As a consequence, if accretion is Eddington limited, the spinning black hole will grow at a slower rate. This simple argument leads to a crucial problem: if jets are associated to large spins, their black holes grow at a slower rate than the hole in radio-quiet quasars. At high redshifts, there should be no jetted sources with a large black hole mass. Quite the opposite of what observed.

Fig. 11 illustrates the point. It assumes that the black hole starts to accrete at $z = 20$ with a seed mass of $10^5$, $10^4$ or $10^3 M_\odot$, and accretes at the Eddington rate with an accretion efficiency $\eta_d = 0.3$ (red solid lines) or $\eta_d = 0.1$ (green dot–dashed lines). If $\eta = 0.3$, the black hole mass reaches $10^5 M_\odot$ at $z = 2$ for a $10^5 M_\odot$ seed, and at $z = 4$ for a $10^4 M_\odot$ seed. Even a very large black hole seed is not enough to account for what we see: a black hole mass exceeding $10^5 M_\odot$ in a jetted source at $z = 5.3$. We conclude that one of the assumptions usually made to calculate the black hole growth must be wrong.

In [40] we suggested a possible way out of this problem, by considering the possibility that the gravitational energy of the accreted matter does not entirely heat up the disk, but it is partly used to amplify the magnetic field that can act as a catalyst for the jet formation and acceleration. In other words, for a given accretion rate, the produced disk luminosity is smaller, because it corresponds to a fraction of the total efficiency. Following [50] (see also [61]), the global efficiency $\eta$ is the sum of two terms, one for the generated magnetic field ($\eta_B$), and the other for the disk luminosity ($\eta_d$):

\[
\eta \equiv \eta_B + \eta_d.
\]

A rapidly spinning hole can have $\eta = 0.3$, but the fraction of the gravitational energy going to heat the disk could correspond to $\eta_d < 0.3$. As a consequence, the black hole grows faster, doubling its mass on a Salpeter time [76], which is now modified in [40]:

\[
t_s = \frac{M}{\dot{M}} = \frac{\eta_d}{1 - \eta_d} \frac{\sigma v c}{4 \pi G M_p} \frac{L_{Edd}}{L_d}
\]

If $\eta_d$ becomes small because a fraction of the energy goes to amplify the magnetic field, then the Salpeter time becomes smaller and the black hole can grow faster. This is illustrated in Fig. 11 by the dashed blue lines, that assume $\eta_d = 0.1$ and $\eta = 0.3$. In this case even Kerr holes with maximum spin and large total efficiency can grow fast enough to reach $M = 10^8 M_\odot$ at redshifts larger than 5.

The above hypothesis is not implying that accretion is directly the only responsible for powering the jet. Most of the jet power can still come from the rotational energy of the hole. But this energy, to be extracted efficiently enough, needs large magnetic fields. These are amplified using part of the gravitational accretion energy.

5 Summary and conclusions

- **Blazar sequence so far confirmed by Fermi** — Fermi blazars observed up to now, with known redshift, obey the phenomenological blazar sequence. Studies in the optical–UV of featureless Fermi blazars succeeded in setting an upper limit to their redshift through the absence of Lyman–$\alpha$ absorption. As a corollary, all blazars observed by Fermi are at $z < 4$.
- **Blazar divide** — Blazars can be divided into low power BL Lacs and high power FSRQs. This parallels the division in FR I and FR II radio–galaxies. This division could be the result of a change of the accretion regime: from radiative inefficient to efficient disks, at a dividing disk luminosity approximately 1% of the Eddington one.
- **One zone vs multizone vs continuous jets** — Most jets usually emit most of their luminosity in a single region at $\sim 10^3$ Schwarzschild radii. It is very likely that there are other emitting regions of the jet, contributing to a lesser extent in terms of bolometric luminosity, but that can give important contributions in selected frequency ranges. In addition, sometimes there are compact regions of the jet, much smaller than the cross section radius of the jet itself, that emit, preferentially at $\gamma$-ray energies, a strong and fast varying flux. These are required...
by the fast varying TeV emission in (line emitting) FS-RQs. The emitting region of this radiation should be located beyond the BLR.

- **Accretion disks and blazars** — The most powerful blazars have a “red” non–thermal SED, that leaves unhidden the accretion disk emission. Its luminosity, and frequency peak, give both $M$ and $M$ with an uncertainty often smaller than virial methods. This allowed to study the disk and jet power as a function of the Eddington luminosity. Relativistic extragalactic jets are present for all $L_d/L_{Edd}$ values we can sample. The jet power and the disk luminosity correlate. This implies that jets and accretion must correlate. On the other hand, often the jet power is larger than the disk luminosity, implying that accretion cannot be the only driver of jets. We believe that accretion amplifies the magnetic field close to the Schwarzschild radius. This field can then extract the rotational energy of the hole.

- **Heavy and early black holes** — Blazars are powerful and can be seen at large redshifts, so they can probe the far Universe. Since the disk emission is clearly visible in very powerful blazars, we can measure the black hole mass of these object at large redshifts. For each source classified as blazars, with a viewing angle less than $1/\Gamma$, there are other $2\Gamma^2$ similar sources pointing elsewhere. This makes the hunt for high-\(z\) blazars risky (they are a few), but rewarding.

- **Two formation epochs of heavy black holes?** — Powerful blazars emit most of their power at high energies, in the hard X–rays and in the $\gamma$–ray band. For the very powerful, the hard X–ray band is closer to their frequency peak than the $[0.1–10\text{ GeV}]$ $\gamma$–ray band. Hard X–ray surveys are then most productive to find high–\(\gamma\) blazars. Studying their hard X–ray luminosity function, and converting it to a black hole mass function, one finds that active ($L_d > 0.1 L_{Edd}$) black holes with a mass in excess of a billion solar masses have a peak in their space density at $z \sim 4$. This does not change by adding blazars coming from the Fermi satellite survey. This contrasts with active and massive black holes in radio-quiet quasars, whose space density peaks at $z \sim 2$. We conclude that there are two formation epochs of heavy black holes, and that jets help the early growth of black holes (or there is a selection effect at action).

- **Black hole growth and spin** — If the presence of a jet is associated to a fast black hole spin, and therefore to a large accretion efficiency, we expect that jetted sources accreting at the Eddington limit need more time to grow that their radio–quiet counterpart. And yet they are discovered at very large redshift. This could imply that the global accretion efficiency is in fact the sum of two parts, corresponding to two way of transforming the available gravitational energy: one goes to heat the disk, and the other to amplify the magnetic field, that in turn helps to extract the rotational energy of spining holes.

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