Temperature has profound effects on a wide range of parameters of neural activity at various scales (Hodgkin and Katz, 1949). At the cell level, ionic currents, membrane potential, input resistance, action potential amplitude, duration and propagation, and synaptic transmission have all been shown to be affected by temperature variations (Hodgkin and Katz, 1949; Kullmann and Asztely, 1998; Volgushev et al., 2000a,b; Fujii et al., 2002). At mesoscopic scales of neural activity, temperature changes can steer network activity toward different functional regimes (Reig et al., 2010), affecting the duration, frequency and firing rate of activated states during slow frequency oscillations, and the ability to end these states (Compte et al., 2003). Temperature also has a substantial effect on chemical reaction rates (Swan, 1974), and affects the blood oxygen saturation level by changing haemoglobin affinity for oxygen (Guyton, 1987). Furthermore, cooling reduces metabolic processes (Esmann and Skou, 1988), and has been used to silence cortical areas to study their function (Uyeda and Fuster, 1967).

While from single cell to mesoscopic levels temperature can directly be measured, at the system level of non-invasive studies using electroencephalogram or functional magnetic resonance, it can only be estimated indirectly, using the temperature dependence of the magnetic resonance signal’s frequency (Hindman, 1966; Parker et al., 1983; Kuroda et al., 1996). Furthermore, a theoretical model of brain temperature (Yablonskiy et al., 2000; Sukstankii and Yablonskiy, 2006) allows inferring from functional magnetic resonance data that functional stimulation can induce local brain temperature fluctuations of up to ±1°C with respect to resting temperature, by locally changing the balance between metabolic heat production and heat removal by blood flow.

The potential impact of temperature modulations on functional brain activity is significant. Given a temperature effect on blood oxygen saturation levels of several percent/1°C (Guyton, 1987), and an estimated average brain van’t Hoff temperature coefficient Q10 (the factor by which a reaction rate increases for 10°C increases) of 2.3 (Swan, 1974), the observed temperature fluctuations may lead to sizeable changes in blood oxygen saturation levels and to >2% variations in chemical reaction rates.

Here we propose a way to directly quantify temperature from system-level brain recordings, and show how it can be used to characterize neural activity associated with cognitive function.

**TEMPERATURE AS A BRIDGE FROM RESTING TO TASK-RELATED BRAIN ACTIVITY**

Temperature is a physical quantity that measures the mean kinetic energy of matter’s particles motion. Its role is to control the energy transfer between the system and other ones to which it is thermally coupled. Temperature is an intensive property, i.e., it is shared by all the system’s constituents, and independent of system size. Together with potential and other types of particle energy, it contributes to the total internal energy within a substance.

Temperature is defined as the inverse of the entropy variation ΔS with respect to a variation of the energy ΔE, at fixed volume

$$-\frac{1}{T} = \left. \frac{\partial S}{\partial E} \right|_{V,N}$$

The inverse temperature $\beta = 1/T$ is, in essence, the cost, in entropy, of buying energy from the rest of the world (Sethna, 2006). At low temperatures, the system has few excited states and is relatively ordered; energy changes ΔE lead to large variations in the number of excited states, quantified by ΔS. High temperature corresponds to low sensitivity of entropy to variations in energy: the system is excited and disordered (Sornette, 2004).

A bona fide temperature ought to reflect heat flows and thermalization, i.e., how fluctuations relax to states in which the values of macroscopic quantities are stationary, universal with respect to differing initial conditions, and predictable (Cugliandolo et al., 1997a).

The notion of temperature is intimately related to that of equilibrium. Operationally, equilibrium is defined by the zeroth law of thermodynamics, which states that if two systems are in thermal equilibrium with a third one, they must be in thermal equilibrium with each other. The zeroth law allows using thermal equilibrium as an equivalence relationship on the set of thermally equilibrated systems, inducing a partition into subsets in mutual equilibrium. Temperature maps these subsets onto real numbers, with ordering and continuity properties.

Thermometers can be used to establish whether two systems will remain in thermal equilibrium when brought in contact. Thus, provided an appropriate thermometer can be devised, temperature...
can be used as a macroscopic collective variable describing the system, through which value its different subparts can be sorted.

**THERMOMETERS AND THE FLUCTUATION–DISSIPATION THEOREM**

A thermometer is a device, e.g. an oscillator, which when coupled to a given observable $X$, feels both its fluctuations in the absence of perturbations, measured by the two-time autocorrelation function $C_X(t, t') = \langle X(t) X(t') \rangle$, and the result of its own action on the system, proportional to the response function $R_X(t - t')$, i.e., how $X$ responds at time $t$ to a small perturbation at time $t'$ (Kurchan, 2005).

For a system at equilibrium, these two opposing effects give the correct energy, i.e., the one predicted by the equipartition theorem, for every thermometer energy, i.e., the one predicted by the two-time autocorrelation function in the absence of perturbations, measured by Equation (1).

**Fluctuation–dissipation far from equilibrium**

Brain fluctuations generically show properties typical of non-equilibrium systems. The relaxation time is considerably slower than exponential (Linkenkaer-Hansen et al., 2001; Buiatti et al., 2007; Ciuciu et al., 2012; Zilber et al., 2012). Brain activity is *weakly non-ergodic* (Bianco et al., 2007), i.e., all possible states remain accessible, but some require exceedingly long times to visit (Bouchaud, 1992), and undergoes *aging* (Barkai, 2003); i.e., contrary to equilibrium fluctuations, which are time homogeneous and for which both the correlation $C$ and the response function $R$ depend on $t = t - tw$ elapsed from the instant $tw$ at which a field is applied, these quantities separately depend on both $tw$ and $t$. Preliminary evidence suggests that brain fluctuations undergo a form of aging termed *renewal aging* (Bianco et al., 2007), the possible etiologies and phenomenologies of which are discussed in Godrèche and Luck (2001); Allegrini et al. (2003); Barkai (2003); West et al. (2008); Burov et al. (2010); Barkai et al. (2012); Lomholt et al. (2013); Schulz et al. (2013) and references therein. The importance of these studies for neuroscience is huge, not least because aging is evaluated for single realizations (rather than for group averages) and this is particularly important in a field where repetitions of the same experiment encounter intrinsic difficulties.

In the presence of complex fluctuations, the FDT does not hold in its classical form (Kubo, 1966), and an appropriate generalization needs to be found. Generalized FDTs have been proposed for aging fluctuations of various kinds (Cugliandolo et al., 1997b; Crisanti and Ritort, 2003; Pottier and Mauger, 2004), including renewal aging (Allegrini et al., 2007; Aquino et al., 2007).

Out of equilibrium, the equilibrium temperature $T$ no longer completely characterizes probability distributions for the system’s degrees of freedom, so that, for instance, the particles’ velocity and position distributions are no longer specified. Fast fluctuations thermalize to the bath temperature $T$ but slow modes do not, and the direction of heat flows is characterized by an *effective temperature* $T_{\text{eff}} > T$ (Kurchan, 2000). $T_{\text{eff}}$ is, in essence, what a thermometer responding on the time scale at which the system slowly reverts to equilibrium would measure (Cugliandolo et al., 1997a). For an aging system, a generalized FDT can be written as:

$$T_X(t, tw) = \frac{\partial C_X(t, tw)/\partial t}{R_X(t, tw)}$$

where $X(t, tw)$ is the fluctuation–dissipation ratio (FDR), and the ordinary FDT is recovered for $X = 1$ (Cugliandolo et al., 1997b). The time-dependent effective temperature $T_{\text{eff}}(t, tw) \propto T(t, tw)$ allows quantifying the distance to equilibrium, and the extent to which the FDT is violated, at a given scale of activity.

As the system ages, the number of dynamically accessible configurational states diminishes (Angell et al., 2000) and the corresponding $T_{\text{eff}}$ is higher than the equilibrium temperature $T$, whereas external stimuli, force the system out of equilibrium, *rejuvenating* it (Dupuis et al., 1999; Linkenkaer-Hansen et al., 2004). $T_{\text{eff}}$ counts the number of metastable states of the system in the same way as $T$ reflects the number of microstates at equilibrium (Martinez and Angell, 2001).

**Multi-thermalization and dynamic heterogeneity**

In an equilibrium system, any thermometer coupled to a part of the system reads the same temperature (Kurchan, 2005). In out-of-equilibrium systems, thermalization happens at widely different timescales simultaneously, within the same region of space. Correspondingly, the brain responds with avalanches spanning a broad range of scales when driven by changing external fields (Lundstrom et al., 2008).

Each timescale may be associated with its own FDR, containing information on the process relaxation, and $T_{\text{eff}}$ (Jack et al., 2006). A system can be at equilibrium on one scale and out of equilibrium on another, or may even be in equilibrium but show scale-dependent properties (Cugliandolo et al., 1997b;
Crisanti and Ritort, 2003). Measuring $T_{\text{eff}}$ at various scales allows understanding the relationship between spontaneous and stimulus-induced brain activity at each scale, and the extent to which each scale of brain activity deviates from equilibrium conditions, produces entropy etc.

Furthermore, at any given time, different regions in the brain relax at different rates. $T_{\text{eff}}$ can be used to estimate the degree of dynamical heterogeneity, i.e., of spatiotemporal fluctuations in the local dynamical behavior. This can be done by calculating the dynamic susceptibility $\chi_T(t) = \partial \langle C(t) \rangle / \partial T$ (Berthier et al., 2005).

**EVALUATING TEMPERATURE**

Functionally induced brain temperature changes and the associated spatiotemporal scales can be estimated using the model of brain temperature proposed in Yablonskiy et al. (2000); Sukstankii and Yablonskiy (2006).

For brain activity at rest, the local steady state temperature $T_0$ can be estimated by

$$T_0 = T_{\text{arterial}} + \frac{\Delta H^0 - \Delta H_b}{\rho B \cdot C_B} \cdot \frac{r\text{CMRO}_2}{r\text{CBF}}$$

where $T_{\text{arterial}}$ is arterial inflow temperature, $\Delta H^0$ the enthalpy generated by the reaction between oxygen and glucose, $\Delta H_b$ the energy used to release oxygen from haemoglobin, $\rho_B$ the blood heat density, $C_B$ the blood heat capacity, $r\text{CMRO}_2$ the regional oxygen metabolic rate, and $r\text{CBF}$ the regional cerebral blood flow (Yablonskiy et al., 2000).

Functional activity changes the oxygen extraction fraction $OEF = r\text{CMRO}_2/r\text{CBF}$. Since typically $r\text{CBF} > r\text{CMRO}_2$, $T$ the model predicts that local changes in temperature and in $r\text{CBF}$ always have opposite sign (Sukstankii and Yablonskiy, 2006).

The model estimates in the order of a few millimeters the characteristic length $\Delta$ of regions where temperature changes can be observed (Sukstankii and Yablonskiy, 2006).

Changes in global $\text{CBF}$ induce a temperature dynamics with a relaxation time $\tau_T = C_{\text{issue}}/(r\text{CBF} \cdot \rho B \cdot C_B)$. Estimates of $\tau_T \sim 40-60$ s (Sukstankii and Yablonskiy, 2006) indicate that for $t < \tau_T$, below the vascular response scale, measurements are out of equilibrium, $T$ is not well defined, and $T_{\text{eff}}$ should be estimated.

Importantly, the model provides quantitative indications on steady state temperature modulations, and the precision with which these can be evaluated, but says little on the fluctuations that these may undergo.

**EFFECTIVE TEMPERATURE IN REAL DATA**

$T_{\text{eff}}$ can be estimated empirically (Martin et al., 2001; Buisson et al., 2003; Hérisson and Ocío, 2004; Mizuno et al., 2007) using standard non-invasive recordings such as electroencephalography or functional brain imaging, respectively plotting the local electrical or BOLD signal amplitude $\chi (t, t')$ against $C_X(t, t')$, and regarding brain stimulation and more generally cognitive demands can be thought of as fields pushing brain activity away from equilibrium, so that the FDT no longer holds. For instance, $\chi$ can be elicited by trains of stimuli of measurable frequency distribution (Bianco et al., 2007).

For equilibrium systems, this would yield a straight line with slope $-1/T$. Out-of-equilibrium systems typically have a more complex, system-dependent $\chi - C_X$ relationship. For instance, multiscaling and aging lead to a non-linear $\chi - C_X$ plot (Crisanti and Ritort, 2003), and a corresponding spectrum of slopes.

The $T_{\text{eff}} (t, t_w)$ dependence on $t$ and $t_w$ helps determining aging properties and FDT violations (Hérisson and Ocío, 2004). The former can be studied by monitoring the time evolution of $C(t, t_w)$ vs. $(t, t_w + \tau)$, and by following the evolution of the linear response to a perturbation applied at $t_w$. Deviations from the FDT can be estimated by plotting $\chi (t, t_w)$ against the correlation for fixed $t_w$, varying $t$ from $t_w$ and infinity (Cugliandolo, 2011).

The estimated $T_{\text{eff}}$ can then be used to quantify the whole system’s dynamical heterogeneity by evaluating $\chi_T (t)$ with an appropriate ansatz (Berthier et al., 2005).

Depending on the recording technique, $T_{\text{eff}}$ could be estimated with a temporal precision ranging from the order of the temporal window within which correlations and responses are evaluated, up to $T_T$, in the tens of seconds range (Sukstankii and Yablonskiy, 2006), and a spatial one at least of the order of the characteristic length $\Delta$, of several millimeters (Parker et al., 1983).

**CONCLUSIONS**

We proposed a method to measure brain temperature from any kind of non-invasive recording, which takes into account the non-equilibrium, multiscale nature of brain activity.

Effective temperature can identify, at various spatial and temporal scales the non-equilibrium regime at which the brain is working.

Temperature can be treated not only as an order parameter i.e., as a collective variable describing brain activity, but also as a control parameter, steering it to various regimes. Intuitively, cognitive processes such as learning or reasoning may be characterized as thermally-guided searches within and modifications of a complex landscape (Sherrington, 1997, 2010).

One could observe how temperature varies during the execution of a cognitive task, and then how phase transitions may occur, using temperature as a control parameter and some other property of neural activity as the order parameter.

More generally, assessing temperature and thermal history enables both a dynamical characterization of brain activity and a complete reconstruction of its thermodynamics, affording neuroscientists a description of the object of their investigations with a sound physical basis.

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Received: 10 February 2014; paper pending published: 24 February 2014; accepted: 13 March 2014; published online: 27 March 2014.

Citation: Papo D (2014) Measuring brain temperature without a thermometer. *Front. Physiol.* 5:124. doi: 10.3389/fphys.2014.00124

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