Energy, Economic, and Environmental Evaluation of a Proposed Solar-Wind Power On-grid System Using HOMER Pro®: A Case Study in Colombia

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Abstract: The electrical sector in the Caribbean region of Colombia is currently facing problems that affect its reliability. Many thermo-electric plants are required to fill the gap and ensure energy supply. This paper thus proposes a hybrid renewable energy generation plant that could supply a percentage of the total energy demand and reduce the environmental impact of conventional energy generation. The hybrid plant works with a photovoltaic (PV) system and wind turbine systems, connected in parallel with the grid to supply a renewable fraction of the total energy demand. The investigation was conducted in three steps: the first stage determined locations where the energy system was able to take advantage of renewable sources, the second identified a location that could work more efficiently from an economic perspective, and finally, the third step estimated the number of PV solar panels and wind turbines required to guarantee optimal functioning for this location using, as a main method of calculation, the software HOMER pro® for hybrid optimization with multiple energy resources. The proposed system is expected to not only limit environmental impacts but also decrease total costs of electric grid consumption from thermoelectric plants. The simulations helped identify Puerto Bolivar, Colombia, as the location where the hybrid plant made the best use of non-conventional resources of energy. However, Rancho Grande was found to offer the system more efficiency, while generating a considerable amount of energy at the lowest possible cost. An optimal combination was also obtained—441 PV arrays and 3 wind turbines, resulting in a net present cost (NPC) of $11.8 million and low CO₂ production of 244.1 tons per year.

Keywords: solar energy; wind energy; energy efficiency; environmental impact; economic evaluation; on-grid system; HOMER Pro software

1. Introduction

The continuous increase in greenhouse effects in the energy field [1,2], the potential danger that represents the future of this trend, and the continuous rise in this kind of energy production boost the development of new trends of energy generation (NTEG), which lead to energy transition [3–5]. NTEG will be independent of hydrocarbons and fossil fuels because research on clean energy acquisition
methods is on the rise, offering reliable solutions to the current problem [6,7]. Solar and wind energy systems are the most selected methods for clean energy production because of their viability and easy acquisition [8]. In 2006, the World Energy Outlook estimated that energy production could be duplicated in 25 years. Furthermore, the publication also expects a growth of 57% in renewable energy production [9]. The boost from new trends in renewable energy generation takes into consideration the current development of technologies that can be used to obtain energy from the movement of the sea waves, as well as ocean currents. There are other ways to obtain renewable energy, one of which is the photovoltaic (PV) system. Asia Pacific is estimated to remain the global PV leader in 2025 with the largest installed solar PV facility in the world [10]. The PV market has grown in both developed and developing countries, implying that renewable energy is a viable global resource. The world’s largest PV energy production from an installed plant is located in Pavagada solar park in India. The park, which can generate up to 2 GW, was fully functional in 2019 [11]. A report in the Journal of Geophysical Research estimated that the highest reachable capacity of wind energy around the world is approximately 72 million GW, which corresponds to 500% more than the energy consumption of every kind of power [12].

Hybrid energy, which is the use of different kinds of energy, is more efficient than conventional energy generation. The availability of wind energy in Colombia, combined with biomass energy, has had a significant influence on the Caribbean region [13]. The exploitation of this source of energy can be an excellent solution to the energy problems prevalent in the region [14]. This solution lies in the design of a hybrid renewable energy plant that has the capacity to use all the renewable energy resources existing in this region [15].

However, fossil fuels are still considered the main energy source in the region, although they cause considerable damage to the environment by the high generation of greenhouse gases [6,16]. The use of fossil fuels by “fracking” increases greenhouse gases and other gases like arsenic and mercury [10]. Greenhouse gas emissions increased by at least 70% in the period between the 1970s to the beginning of the 21st century, with the energy sector being the main responsible factor [17]. An analysis by the Oak Ridge National Laboratory (Tennessee, United States) on carbon dioxide emissions states that greenhouse gasses in Colombia increased from 16 megatons to 84 megatons (80%) in the 1960s to 2014; it was compared to Portugal, Finland, Chile, Austria, Sweden, Ireland, and Hungary [18].

At present, energy potential (wind and solar energy) in the Caribbean Colombian region is going to waste, more specifically in La Guajira department; these forms of renewable energy can help mitigate greenhouse emissions and increase electricity generation. With hybrid systems, operating costs are reduced because they do not require as much maintenance as conventional energy generation methods, and owing to a learning curve that helps people understand how this technology operates [19].

The Hybrid Optimization for Multiple Energy Resources (HOMER) software provides the necessary tools to establish different simulations with multiple energy resources [20] and study behavior over time. This enables the simulation of a hybrid power plant with twice or more renewable resources. This academic tool can be used to determinate viability from economic and environmental perspectives and/or energy generation systems. Therefore, HOMER is ideal for this research work.

The main contribution of this research is to highlight the renewable energy potential in the Caribbean region of Colombia (more specifically in La Guajira), showcase the possibilities to meet the growing energy demand, and offer renewable energy as a great solution to the region’s problems. The following sections of the paper are organized as follows. Section 2 provides the legal and regulatory framework for renewable energy projects, a description of the available sources in different locations of La Guajira, a scheme of the proposed system, and the planning undertaken for this research. Section 3 provides the theory and equations required to implement the study. Section 4 presents the results of the simulations with a complete analysis.
2. Contextualization and Required Information

This section highlights the Colombian policy associated with renewable integration in the electrical grid. It also gives geographical details of the different weather stations located in La Guajira, Colombia. The tables and graphs presented in this section contain relevant data obtained by the meteorological stations over 20 years. In addition, this research work’s planning process is described.

2.1. Political Context

Colombia has a legal and policy framework that helps justify the development of this research work; it is shown in Figure 1 [21]. It is important to note that the legal framework is responsible for establishing limits and penalties for all future projects. An essential point of the policy is to provide economic benefits for projects that meet their guidelines and contribute to the development of new trends—in this case, the energy sector. The benefits include reduction in taxes, such as the cost of importing energy generating devices from renewable sources, and return on investment in net income coming directly from the state. In some countries, the production of clean energy in homes is promoted through incentives for those who provide this type of resource as a surplus in the community power grid.

2.2. Energy System Scheme

The data were obtained from different meteorological stations located in La Guajira department, Colombia, as shown in Figure 2. There are nine stations dedicated to collecting temperature, wind speed, and solar radiation data. The data of pressure, relative humidity, and temperature in Figure 2 correspond to average yearly values.

In order to provide accurate results and establish the ideal location to use solar and wind energy, it was necessary to obtain data from each of the meteorological stations and pinpoint their specific locations [22].
After studying the problem mentioned in this study, the creation of a hybrid wind and solar power generation plant was proposed to tap into the energy potential (Figure 3). This plant is proposed to have wind turbines 80 m in rotor height and with output power of 1.5 MW each, and an inverter module system like the Goldwind PMDD 1.5 MW Wind turbine [23]. A set of PV arrays (1kW per array) with 4 PV modules of 250 W each and a converter module system were proposed to work together with the turbine’s wind power to take advantage of the high energy potential in the area. The map is divided into two different zones to establish areas influenced by wind speed and zones where potential renewable energy is higher and meteorological stations are located.

Figure 2. Geographic locations of the different meteorological stations in La Guajira, Colombia.

Figure 3. Proposed energy system scheme.
2.3. Planning

The investigation was carried out in three stages. The first stage involved the analysis of data collected from the weather stations over 10 years. The data concerning energy production and renewable fraction were studied without considering the costs on the system in an effort to estimate locations where renewable energy sources could be used in higher proportions.

The second stage sought to determine the most efficient location for a hybrid energy system that uses both wind and PV systems, working at the same time. This stage focuses on an economic perspective to study the results of total energy production, fraction of renewable energy, and aspects such as total net present cost (NPC) and CO$_2$ production to determine a location with optimal behavior.

The third stage determined the most efficient arrangement of wind and PV technologies working together, that is, the ideal number of wind turbines and PV panels depending on the energy demand and characteristics of the selected location. Finally, the grid power that the plant could develop, and its optimal composition was determined.

The first and second stages were calculated using simulations made in HOMER Pro software. The third stage used an optimization process through the MATLAB optimization function called Optimtool and the TOPSIS method for Pareto optimization. The data was used in the MATLAB curve fitting complement to determine the corresponding function for two main optimization objectives (energy cost and CO$_2$ emissions).

2.4. Renewable Energy Resource Data

Figure 4, and Tables 1 and 2 show the curves corresponding to wind speed in different locations at an altitude of 80 m with the corresponding temperature and solar radiation matrices for nine measurement points during a year, where AP means “Almirante Padilla” influence zone, and PB means “Puerto Bolivar” influence zone.

![Figure 4. Wind speed graph for different measurement points in La Guajira [13].](image-url)
Table 1. Temperature [°C] matrix for the different measurement points in La Guajira [22].

| Locations     | Jan. | Feb. | Mar. | Apr. | May | Jun. | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. |
|---------------|------|------|------|------|-----|------|------|------|------|------|------|------|
| Camp. Intercor| 26.9 | 27.3 | 28.2 | 28.5 | 28.6| 28.7 | 29.2 | 29.0 | 28.2 | 27.6 | 27.2 | 27.0 |
| Carraipa      | 25.9 | 26.3 | 27.0 | 27.7 | 27.9| 28.2 | 28.4 | 28.6 | 27.9 | 27.2 | 26.7 | 26.1 |
| La Mina       | 27.0 | 27.6 | 28.3 | 28.7 | 28.9| 29.3 | 29.5 | 29.4 | 28.4 | 27.7 | 27.3 | 26.9 |
| Manaure       | 27.8 | 27.8 | 27.9 | 28.4 | 29.1| 30.0 | 29.9 | 29.5 | 29.1 | 28.6 | 28.6 | 28.1 |
| Matitas       | 26.7 | 26.8 | 27.2 | 27.7 | 27.9| 28.8 | 28.9 | 28.4 | 27.7 | 27.1 | 27.1 | 26.6 |
| Nazareth      | 25.7 | 25.8 | 26.3 | 27.0 | 27.6| 28.0 | 27.9 | 28.5 | 28.5 | 27.8 | 27.1 | 26.2 |
| Puerto Bolivar| 27.0 | 26.9 | 27.4 | 28.2 | 29.0| 29.5 | 29.4 | 29.5 | 29.3 | 28.8 | 28.3 | 27.5 |
| Rancho Grande | 25.9 | 26.4 | 27.1 | 27.3 | 28.1| 28.7 | 28.3 | 28.3 | 28.3 | 27.7 | 27.7 | 27.2 |
| Urumita       | 27.3 | 28.0 | 28.4 | 28.5 | 27.9| 28.0 | 28.5 | 28.3 | 27.4 | 27.0 | 26.8 | 26.7 |

It is important to highlight the need to consider temperature in this case study. La Guajira, being a coast, is one of the warmest places in the Colombian territory. In addition, PV panels have a deficit when the temperature over them is too high. Furthermore, the physical properties of wind see a negative change with temperature increase. This reduces the amount of energy generated from PV arrays and wind turbines. Therefore, the temperature factor in the simulations was not considered, as it could represent possible incorrect results in this investigation.

2.5. Forecasting of Energy Demand

Thermoelectric plants are essential in the Colombian energy dispatch. However, large quantities of fossil fuels are required in thermoelectric plants, which means high and continuous operating costs, in addition to the high production of polluting gases and the legal consequences [24].

For this reason, it is necessary to implement a hybrid renewable energy generation plant that can replace a high percentage of the energy produced in thermoelectric plants. It would help in reducing the use of thermoelectric plants and facilitate their operation. If optimal operation of the hybrid plant is found, it could guarantee supply security and even enable selling of the remaining energy to the electric grid.

It was necessary to determine energy demands as a function of time, as shown in Figure 5. The energy that can be produced in thermoelectric plants is then compared with that produced by wind and solar systems. The effect of temperature is taken into account. Table 3 shows the parameters used in this research.
Figure 5. Seasonal profile of energy demand used in this study.

Table 3. Different parameters requested by HOMER Pro® for the specific economic and power calculations, where O&M means Operation & Maintenance and * indicates an estimated value.

| Parameter                        | Description                                                                 | Value      | Unit        |
|----------------------------------|------------------------------------------------------------------------------|------------|-------------|
| Grid power price *               | Price that the electric utility charges for energy purchased from the grid   | 0.2        | USD/kWh     |
| Simulation period                | Time considered for the study                                               | 10         | Years       |
| Annual scaled average            | Parameter used to scale the whole array of hourly data up or down           | 24,000     | kWh/day     |
| Pike                             | Energy top value                                                            | 1833.2     | kW          |
| Discount rate *                  | The rate considered to borrow money                                         | 8          | %           |
| Rate of inflation *              | The percentage at which money is devalued along time                        | 2          | %           |
| Wind turbine hub height          | Height of the rotor measured from the ground                                | 80         | Meters      |
| Grid CO₂ *                       | CO₂ emission factor of the energy generated by the grid                    | 0.1        | kg/kWh      |
| PV O&M cost per unit            | Operation and maintenance cost per PV unit                                  | 10         | USD/year    |
| Wind O&M cost per unit          | Operation and maintenance cost per wind turbine unit                        | 30,000     | USD/year    |

3. Methodology

3.1. Wind Speed Estimation

The Weibull probability distribution was implemented to estimate the most probable wind speed in different locations using maximum and minimum values. A random variable $x$ has a Weibull distribution if its probability density function is given as shown in Equation (1) [25].

$$f(x; \alpha, \theta) = \begin{cases} \frac{\alpha}{\theta} x^{\alpha-1} \exp\left(\frac{-x}{\theta}\right)^\alpha & x \geq 0 \\ 0 & x < 0 \end{cases}$$

(1)

The parameters $\alpha$ and $\theta$ [26] are estimated with experimental data. Depending on their values, Equation (1) can obtain the form of Equation (2), called the function of the probability density of the Rayleigh distribution:

$$f(x; \sigma^2) = \frac{x}{\sigma^2} \exp\left(\frac{-x^2}{2\sigma^2}\right) \quad x > 0$$

(2)
In this case study, the factors of the different types of distribution expressed monthly for the locations of Puerto Bolívar and Almirante Padilla are presented in Table 4. On the other hand, Figure 6 shows the different velocity distributions of wind speed.

Table 4. Multi-annual adjusted distributions of wind speed for Puerto Bolivar (PB) and Almirante Padilla (AP), from 2003 to 2013 [22].

| Distribution | Weibull PB | Weibull AP |
|--------------|------------|------------|
| Month        | Jan. | Feb. | Mar. | Apr. | May | Jun. | Jan. | Feb. | Mar. | Apr. | May | Jun. | Jan. | Feb. | Mar. | Apr. | May | Jun. |
| Form         | 3.62  | 3.94 | 4.03 | 3.84 | 3.06 | 3.63 | 1.84 | 2.05 | 1.87 | 1.89 | 20.88 |
| Scale        | 7.12  | 7.66 | 7.70 | 7.56 | 7.14 | 7.89 | 3.51 | 3.76 | 3.80 | 3.52 | 3.45 | 3.73 |
| Month        | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. |
| Form         | 3.88  | 3.06 | 2.31 | 2.21 | 2.61 | 3.11 | 2.14 | 1.75 | 1.69 | 1.77 | -    | 1.75 |
| Scale        | 8.11  | 7.13 | 5.73 | 5.11 | 5.44 | 6.42 | 4.02 | 3.31 | 2.68 | 2.48 | -    | 2.94 |

| Distribution | Rayleigh PB | Rayleigh AP |
|--------------|-------------|-------------|
| Month        | Jan. | Feb. | Mar. | Apr. | May | Jun. | Jan. | Feb. | Mar. | Apr. | May | Jun. | Jan. | Feb. | Mar. | Apr. | May | Jun. |
| Scale        | 6.64  | 6.94 | 7.15 | 7.04 | 6.71 | 7.37 | 3.66 | 3.74 | 3.76 | 3.64 | 3.55 | 3.67 |
| Lower threshold | 0.01 | 0.30 | 0.01 | 0.10 | 0.10 | 0.10 | −0.09 | 0.01 | 0.02 | −0.09 | −0.07 | 0.03 |
| Month        | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. |
| Scale        | 7.57  | 6.69 | 5.55 | 4.97 | 5.15 | 6.01 | 3.95 | 3.57 | 2.93 | 2.59 | -    | 3.13 |
| Lower threshold | 0.09 | 0.10 | 0.05 | 0.05 | 0.10 | 0.10 | 0.03 | −0.17 | −0.15 | −0.04 | -    | −0.10 |

Figure 6. Adjusted frequency distributions of wind speed for Puerto Bolivar, (A) January, (B) February; and Almirante Padilla, (C) January, and (D) February.

The data for wind velocity were taken at a height of 10 m. Hellman’s exponential law was used to determine the average wind velocity at any altitude:

\[ V_h = V_{10} \cdot (h/10)^\mu \]  

(3)

where, \( V_h \) is wind velocity at the required altitude \( h \), \( V_{10} \) is the wind velocity at altitude of 10 m, and \( \mu \) is the Hellman exponent, which varies with the roughness of the terrain [27]. These values were found to be 0.28 and 0.14 for the locations of Almirante Padilla and Puerto Bolivar airport, respectively [13].
3.2. HOMER Economic Analysis

In the principal cost analysis, total net present cost (NPC) and cost of energy (COE) are determined using Equation (4).

\[ \text{NPC} (\$) = \frac{\text{TAC}}{\text{CRF}} \]  

(4)

where, TAC is the total annualized cost and CRF is the capital return factor, calculated using Equation (5).

\[ \text{CRF} (\$) = i \cdot \left(1 + \frac{i}{N}\right)^N \]  

(5)

where, \( N \) is the number of years, and \( i \) is the annual range of real interest [%]. The cost of energy COE is the average unit cost of energy produced [\$/kWh], and is determined using Equation (6).

\[ \text{COE} (\$/kWh) = \frac{C_{\text{tot.ann}}}{E} \]  

(6)

where, \( C_{\text{tot.ann}} \) is the total annual cost, and \( E \) is the total energy consumption per year.

3.3. HOMER Estimation of the Output Power of PV Panels

Equation (7) is used to determine the output power of PV panels:

\[ P_{\text{PV}} = Y_{\text{PV}} \cdot f_{\text{PV}} \cdot \left( \frac{G_T}{G_{T,\text{STC}}} \right) \left[ 1 + \alpha_P \left( T_c - T_{c,\text{STC}} \right) \right] \]  

(7)

where, \( Y_{\text{PV}} \) is the nominal capacity of the panel matrix, \( f_{\text{PV}} \) is the reduction factor of the panels, \( G_T \) is the incident solar radiation in the PV matrix in the current time step, \( G_{T,\text{STC}} \) is the radiation incident in standard conditions, \( \alpha_P \) is the power temperature coefficient, \( T_c \) is the temperature of the PV cell in the current time step, and \( T_{c,\text{STC}} \) is the temperature of the PV cell under conditions of a standard test.

3.4. HOMER Estimation of the Output Power of Wind Turbines

Equation (8) is used to determine the output power of wind turbines.

\[ P_{\text{WTG}} = \left( \frac{\rho}{\rho_0} \right) P_{\text{WTG,STP}} \]  

(8)

where \( P_{\text{WTG}} \) is the output power of the wind turbine, \( P_{\text{WTG,STP}} \) is the output power of the wind turbine at standard conditions, \( \rho \) is the actual density of air, and \( \rho_0 \) is the density of air at standard conditions.

3.5. Curve Fitting and Multi-Objective Optimization of the Forecast

With tabulated data, curve fitting using regressions is necessary; thus, it is important to have the best mathematical function to make forecasts. Optimtool was thus implemented to create an optimization process using the previously found function and determine Pareto’s efficiency as a way of plotting the results. Pareto’s efficiency shows a set of solutions delimited by the values closest to the origin coordinate if it is a minimum optimization; or, on the contrary, if it is a maximum optimization, the solution is delimited with the farthest values. The study then proceeded to use the multiple criteria method called Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS) [28]. This method selects one of the values obtained in the Pareto efficiency, using the closest distance of any data from the lower vertex delimited by both ends of the graph. This technique uses the following equation:

\[ d_{ix} = \sqrt{\sum_{j=1}^{n} (t_{ij} - t_{xj})^2}, \quad i = 1, 2, \ldots, m \]  

\[ d_{iy} = \sqrt{\sum_{j=1}^{n} (t_{ij} - t_{yj})^2}, \quad i = 1, 2, \ldots, m \]  

(9)
where \(d_{ix}\) and \(d_{iy}\) are the distances from the selected point \(t_{ij}\) to the ideal positive point \(t_{xj}\), and the ideal negative point \(t_{yj}\), respectively.

The relative proximity to the ideal solution \((S_{iy})\) is determined by Equation (10):

\[
S_{iy} = \frac{d_{iy}}{(d_{iy} + d_{ix})} \quad 0 \leq S_{iy} \leq 1
\]  

This method allows to determine the best operating conditions for a system based on mathematical tools. However, it is also possible to achieve optimal conditions of power generation systems through advanced exergetic analysis, which are formulations based on the physical phenomena involved in each piece of equipment in the system [29,30].

4. Results and Discussions

This section presents the energy results, economic perspective, and multi-objective optimization.

4.1. Energy Results

Figure 7 shows the profile of the energy production obtained by PV systems, their nominal output power, and equivalent PV hours per year in multiple locations in La Guajira, Colombia. In this step, device replacement and capital costs are not considered, because the objective of this section is to evaluate the energy generation potential of the hybrid system.

Figure 7. Comparison between the rated power and energy production for the photovoltaic (PV) system.

Figure 7 shows that the most significant annual energy production is in the town of Urumita. However, this does not mean that Urumita is the best location. It is necessary to quantify the efficiency of the devices to determine an optimal location for the PV system. The fraction between the nominal PV power and the energy generated per year gives a specific number of hours for each location in one year. Therefore, it estimates how PV arrays take advantage of solar light during operation, which means that locations where PV arrays have the longer number of hours per year will take more advantage of solar radiation.

On the other hand, it is necessary to highlight that PV output power indicates the nominal power for all the set of PV arrays connected between them, which are made of 4 panels with 250 W each. On this basis, Puerto Bolívar was identified as the location where the system works with the highest number of hours, despite having less energy generation compared to the other locations. This means
that Puerto Bolívar is the best place to use our PV system. In percentage terms, the efficiency of this system is the fraction between the worked hours per year and the hours of one year, which gives an efficiency of 21.9%.

Subsequently, the optimal location for the wind system was determined. Considering that the use of wind turbines with hub height of 80 m and nominal power of 1.5 MW is fixed, a comparison was made between the number of wind turbines (given by the software for each location) and the energy production generated per year, which points towards the ideal location (Figure 8).

Figure 8. Comparison between the number of wind turbines and the annual energy production for each location.

Figure 8 shows six locations where the system considered five 1.5 MW turbines to reach the energy production plotted in the previous graphic for each location, while the other three only needed four turbines to reach a higher amount of energy. Thus, these three locations were analysed to find the area with the highest generation of wind power: Nazareth was identified as the location with 0.4% and 0.18% more wind power, compared to Puerto Bolívar and Rancho Grande, respectively.

After the best location for installation of the wind generation system was identified, the optimal general location was determined since the optimal sites for both types of devices are different. Therefore, it was necessary to analyse the percentage of renewable fraction present in each of the locations to identify which of these two locations generates the highest amount of renewable energy. The renewable fraction in a system is the ratio of the amount of clean energy produced and the total energy demand of our system.

Once the optimal location was determined, the parameters of the hybrid renewable energy generation plant were modified to increase power generation, resulting in a decrease in costs. Figure 9 shows that Nazareth, Puerto Bolivar, and Rancho Grande are the locations with the highest RF percentage to produce energy by renewable resources. However, these values have a minimal difference, which means that it is necessary to verify the second step of the simulation; this refers to an economic perspective to determine the optimal location.
4.2. Economic Perspective

The simulation requires capital and replacement costs for PV systems and wind turbines. A generic PV array (1 kW; $4 \times 250$ W) with a capital cost of USD 3000 and a replacement cost of USD 3000 was used. Generic wind turbines of 1.5 MW with a capital cost of USD 3,000,000 and a replacement cost of USD 3,000,000 were used. The effects of temperature were considered in the simulation.

Using generic energy demand based on the requirements of La Guajira department, simulation at this stage resulted in a single generic wind turbine for each location. Therefore, Figures 10 and 11 show the relationship of the number of PV panels with net present cost (NPC), total energy production, a fraction of renewable energy, and CO$_2$ emissions for the following locations: Nazareth, Port Bolivar, and Rancho Grande.

Figure 9. Comparison between the production and renewable fraction for each location.

Figure 10. Comparative results for Nazareth, Puerto Bolivar, and Rancho Grande: (A) PV units and net present cost, (B) comparison between PV units and total production.
Figure 10A shows that Nazareth and Rancho Grande are the locations where the NPC of the entire project, based on the number of PV panels implemented, is the lowest. Practically, the NPC for Nazareth and Rancho Grande are the same, which means that it is necessary to consider the following criteria to make the right decision about which place is optimal. In the town of Nazareth, the reason for total energy production and the number of PV panels is the lowest, compared to the localities of Rancho Grande and Puerto Bolivar. In addition, Figure 10B shows that the total energy production in Rancho Grande remains the best for at least 200 PV arrays. Another essential criterion considered was the renewable fraction. It is critical to highlight that a 1 PV device or 1 PV unit is equal to a 1 PV array for this simulation analysis.

Figure 11A shows that Nazareth and Rancho Grande have almost the same fraction values to produce energy by renewable energy, which are higher than those of Puerto Bolivar. This means that Puerto Bolivar is not the optimal place to implement a hybrid PV and wind power plant. Even if the location has good production values, its renewable fraction is the lowest, resulting in a high NPC.

The last criterion to study is the CO$_2$ emission produced by thermoelectric power plants and the acquisition of other non-renewable energy sources. Figure 11B shows that CO$_2$ emissions in Nazareth are lower than those of Rancho Grande when there are 110 PV arrays. For large numbers of PV units, lower CO$_2$ production is located in Rancho Grande, making it the best possible location.

4.3. Multi-Objective Optimization of Rancho Grande for Location of a Hybrid System

Considering that Rancho Grande was identified as the optimal location to implement a hybrid wind and PV system, the next stage sought to determine, through the optimization of multiple objectives, the most efficient combination of the number of PV devices and wind turbines.

Wind turbines in the range of 1 to 10 and the number of PV arrays in the range of 50 to 500 were implemented. A matrix was then developed for current NPC and CO$_2$ production based on PV devices and wind turbines.

A mathematical function for each criterion, NPC (Equation (11)) and CO$_2$ (Equation (12)), was determined using the MATLAB curve fitting tool. Figures 12 and 13 show the corresponding polynomial regressions with their respective functions.

\[
f_1(x, y) = 9.523 + 8.646 \times 10^{-6} x - 0.8988 y + 0.0006295 x y + 0.6652 y^2 - 8.478 \times 10^{-5} x y^2 - 0.06331 y^3 + 3.936 \times 10^{-6} x y^3 + 0.002267 y^4
\] (11)
These functions were useful in developing a MATLAB code for a multi-objective optimization process. Figure 12 shows the behavior of the NPC as a function of the PV devices and the wind units. It was necessary to use fourth-degree polynomial regression to obtain the minimum percentage of error, 0.0001%. Equation (11) is the mathematical function of the net present cost (NPC), where “x” is the number of PV units and “y” is the number of wind turbines.

Figure 13 shows the behavior of CO₂ production as a function of the number of wind units and PV devices. Equation (12) is the corresponding mathematical function for CO₂ emissions, where “x” is the number of PV units, and “y” is the number of wind turbines. As can be seen, the effect of PV devices on CO₂ production is negligible, compared to the wind unit.

The optimization was conducted considering Objective 1 (the current NPC), and Objective 2 (the production of CO₂) with the two functions mentioned above. The purpose was to minimize both criteria using Pareto’s efficiency. For each data of PV arrays and wind turbines, there are values of current NPC and CO₂ Production, as given in Table 5 (only a range of values was placed, since it can be more extensive).
Table 5. Data collected from previous multi-objective optimizations.

| Index | Population $f_1$ | Population $f_2$ | $f_1(x,y)$ | $f_2(x,y)$ |
|-------|------------------|------------------|------------|------------|
| 1     | 162.35           | 1.00             | 9.3208     | 424.2034   |
| 2     | 455.86           | 2.84             | 11.5792    | 250.6008   |
| 3     | 374.16           | 1.58             | 9.8313     | 342.0218   |
| 4     | 458.33           | 7.68             | 21.8166    | 169.9665   |
| 5     | 450.50           | 7.50             | 21.4097    | 171.6429   |
| 6     | 190.93           | 1.09             | 9.3685     | 411.2848   |
| 7     | 463.61           | 8.10             | 22.7594    | 166.4565   |
| 8     | 464.54           | 7.08             | 20.4920    | 174.8915   |
| 9     | 182.34           | 1.16             | 9.3980     | 402.9515   |
| 10    | 466.82           | 9.27             | 25.4634    | 159.7775   |
| 11    | 459.10           | 9.01             | 24.8412    | 160.7772   |
| 12    | 252.28           | 1.31             | 9.5272     | 380.0974   |
| 13    | 170.97           | 1.47             | 9.5804     | 370.2378   |
| 14    | 460.99           | 5.58             | 17.1489    | 188.2983   |
| 15    | 204.76           | 1.51             | 9.6331     | 363.7958   |
| 16    | 162.35           | 1.00             | 9.3208     | 424.2034   |
| 17    | 467.55           | 8.58             | 23.8424    | 162.9501   |
| 18    | 289.97           | 1.20             | 9.4879     | 388.5064   |
| 19    | 456.46           | 6.39             | 18.9383    | 181.0377   |
| 20    | 452.18           | 6.71             | 19.6354    | 178.4340   |
| 21    | 460.93           | 4.41             | 14.6000    | 203.6394   |
| 22    | 435.81           | 7.99             | 22.4599    | 167.9836   |
| 23    | 443.14           | 4.65             | 15.0778    | 200.5169   |
| 24    | 447.40           | 3.76             | 13.2597    | 218.3149   |
| 25    | 436.18           | 3.23             | 12.2364    | 235.6264   |
| 26    | 294.45           | 1.59             | 9.7729     | 348.1610   |
| 27    | 453.42           | 5.85             | 17.7357    | 185.9505   |
| 28    | 456.58           | 4.38             | 14.5426    | 204.2703   |
| 29    | 292.95           | 2.85             | 11.4068    | 260.6003   |
| 30    | 451.30           | 6.14             | 18.3635    | 183.4294   |
| 31    | 390.02           | 2.24             | 10.5965    | 288.6604   |
| 32    | 460.17           | 3.87             | 13.5000    | 214.7941   |
| 33    | 440.81           | 3.00             | 11.8483    | 244.0983   |
| 34    | 212.64           | 1.61             | 9.7231     | 353.2899   |
| 35    | 407.42           | 7.34             | 20.9747    | 174.1048   |
| 36    | 466.60           | 8.46             | 23.5835    | 163.7199   |
| 37    | 434.90           | 2.31             | 10.7404    | 280.7996   |
| 38    | 458.70           | 9.03             | 24.8764    | 160.7231   |
| 39    | 208.45           | 2.99             | 11.5348    | 259.4823   |
| 40    | 295.98           | 2.07             | 10.2843    | 307.6137   |
| 41    | 208.34           | 1.17             | 9.4170     | 399.9407   |
| 42    | 430.48           | 2.02             | 10.3587    | 300.6018   |
| 43    | 391.20           | 4.99             | 15.7236    | 197.8553   |
| 44    | 461.77           | 5.12             | 16.1006    | 193.4751   |
| 45    | 445.79           | 5.75             | 17.4817    | 187.2504   |
| 46    | 731.67           | 2.49             | 10.9957    | 270.3299   |
| 47    | 443.03           | 3.41             | 12.5793    | 228.9088   |
| 48    | 404.32           | 5.30             | 16.4306    | 193.4263   |
| 49    | 468.14           | 9.52             | 26.0469    | 159.4742   |
| 50    | 162.38           | 1.02             | 9.3261     | 422.2238   |

$f_1(x,y)$ and $f_2(x,y)$ from Table 5, which are the values for NPC and CO$_2$ production, respectively, were then plotted (Figure 14).
It is important to note that Table 5 shows values that are not feasible due to decimal values; for example, index 17 gives 8.58 wind turbines. Decimal values are out of range because it is impossible to install 8.58 wind turbines of 1.5 MW. When choosing the nearest integer values, a considerable error was generated. On the other hand, PV arrays do not have this problem because their units are high, making it possible to approximate decimals to the nearest integer.

For this reason, it was necessary to determine the index that has the nearest integer for wind turbine devices, with at least 0.01 difference of any integer, as shown in Table 6.

Table 6. Feasible values to consider as an option, obtained from Table 4.

| Index | PV Devices | Wind Units | NPC [million USD] | CO₂ Production [ton/yr] |
|-------|------------|------------|-------------------|------------------------|
| 1     | 162        | 1          | 9.3208            | 424.2034               |
| 11    | 459        | 9          | 24.8412           | 160.7772               |
| 22    | 436        | 8          | 22.4599           | 167.9836               |
| 33    | 441        | 3          | 11.5348           | 259.4823               |
| 39    | 208        | 3          | 11.5348           | 259.4823               |
| 43    | 391        | 5          | 15.7236           | 197.8553               |

While it is necessary to choose one of these values, it is important to note that all the previous data were optimal combinations, that is, data that is the best possible option for a specific number of selected devices. Figure 14 shows the locations of these indexes (in orange dots).

Figure 14 is a Pareto front composed of values of $f_1(x,y)$ and $f_2(x,y)$ shown in Table 5, which represents the net present cost (NPC) and CO₂ emissions, respectively. In addition, the characteristic equation is presented, where “x” is the number of PV arrays, and “y” is the number of wind turbines. Orange dots are the possible values given in Table 6, which represent specific configurations for the purposed hybrid plant. The ideal point is described as the interception of the vertical axis in the lowest value of CO₂ production with the horizontal axis in the lowest value of the Net Present Cost. The non-ideal point is described as the interception of the horizontal axis generated from the higher amount of CO₂ production with the vertical axis generated from the higher value of the Net Present Cost. Both ideal points are represented with red dots.

The next step is to implement the Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS) method, which states that the selected point (taken in Figure 14) should have the shortest geometric length from the positive ideal solution and the most extended geometric length from the perfect negative solution. This optimization method has been widely used to improve the thermal
and economic performance of energy systems [31–33]. Indexes 39 and 33 are the closest to the desired condition, as shown in Table 7.

Table 7. Results from TOPSIS analysis for index 33 and 39.

| Index | Dx     | Dy     | Sy     |
|-------|--------|--------|--------|
| 33    | 89.1292| 181.4544| 0.6706 |
| 39    | 104.5021| 166.1486| 0.6139 |

Equation (10) is used to choose between the two values. The index with the value of Sy closest to 1 is the right point. The index 33 is closer to 1, making it the best possible option; therefore, a total of 441 PV arrays (1764 modules of 250 W) and 3 wind turbines of 1.5 MW should be used, resulting in an estimated NPC cost of 11.8 million dollars, and estimated CO₂ emission of 244.1 tons per year.

In this way, the best parameters that offer minimum energy costs to the residents, minimum emissions of pollutant gases, and maintain a reasonable energy production rate are obtained.

5. Conclusions

In this paper, an optimization process was developed to install a hybrid PV and wind power plant in La Guajira, Colombia. The study was done in three stages, with specific characteristics and region conditions. The first stage focused on an energy perspective, where it was found that three of the nine measurement locations—Nazareth, Puerto Bolivar, and Rancho Grande—were the best locations to take advantage of the available energy with 95% percentage each to produce energy using renewable energy. The renewable fraction for the other locations was close to 87%.

The second stage focused on an economic perspective, considering prices and taxes. This stage was developed only for the three best locations, finally identifying Rancho Grande as the optimal place to set up a hybrid energy plant. This location had an advantage over other areas in terms of renewable fraction, total production, and estimated CO₂ reduction.

The third and final stage focused only on the town of Rancho Grande, intending to determine the optimal combination of PV panels and wind turbines. This stage identified, for the plant, an optimal combination of 441 PV units and 3 wind turbines, giving an estimated minimum NPC of $11.8 million, and low CO₂ production of 244.1 tons per year.

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