Time-correlated single-photon counting (TCSPC) has been the gold standard for fluorescence lifetime imaging (FLIM) techniques due to its high signal-to-noise ratio and high temporal resolution. The sensor system’s temporal instrument response function (IRF) should be considered in the deconvolution procedure to extract the real fluorescence decay to compensate for the distortion on measured decays contributed by the system imperfections. However, to measure the instrument response function is not trivial, and the measurement setup is different from measuring the real fluorescence. On the other hand, automatic synthetic IRFs can be directly derived from the recorded decay profiles and provide appropriate accuracy. This paper proposed and examined a synthetic IRF strategy. Compared with traditional automatic synthetic IRFs, the new proposed automatic synthetic IRF shows a broader dynamic range and better accuracy. To evaluate its performance, we examined simulated data using nonlinear least square deconvolution based on both the Levenberg-Marquardt algorithm and the Laguerre expansion method for bi-exponential fluorescence decays. Furthermore, experimental FLIM data of cells were also analyzed using the proposed synthetic IRF. The results from both the simulated data and experimental FLIM data show that the proposed synthetic IRF has a better performance compared to traditional synthetic IRFs. Our work provides a faster and precise method to obtain IRF, which may find various FLIM-based applications.

Keywords: time-resolved imaging, photon counting, deconvolution, fluorescence microscopy, instrument response function

1 INTRODUCTION

Fluorescence lifetime imaging (FLIM) has become a versatile and powerful analytical tool for biomedical applications. Compared with fluorescence intensity imaging, FLIM is not only less susceptible to experimental artifacts in excitation/detection setups, optical paths, or fluorophore concentrations, but can also provide abundant cellular information [1–4]. FLIM offers a unique route for probing and visualizing intracellular physical parameters such as temperature, pH, O2, and ion...
of specimens like NAD(P)H, which has multiexponential decays with short lifetime components. In real experiments, the IRF signal is often hard to be detected because the quantum yield of fast decay fluorophores is low. Another drawback is that the spectral ranges of the dyes are limited. It is reported that the emission spectra of dyes with short fluorescence lifetimes only exist at the range larger than about 525 nm [20]. For example, the emission spectrum of pinacyanol iodide starts from 550 nm, and that of Allura Red is from 550 nm to 750 nm [16, 19]. No dye has been found with an emission spectrum covering all visible wavelengths. Therefore, it is difficult to find suitable dyes for every spectra window of interest. For a two-photon FLIM system, some other IRF measurement techniques based on Hyper-Rayleigh scattering (HRS) or second harmonic generation (SHG) have been proposed [21–23]. For example, the plasmon-enhanced gold luminescence can yield a wide-range ultrafast second-harmonic HRS signal, which can be used as a calibration sample for IRF measurements for a multiphoton FLIM system [22]. The second harmonic signal generated on the surface of urea crystals, potassium dihydrogen phosphate crystals or collagen fibers is also widely applied to measure the IRF [23]. However, there are still many restrictions that limit their performances. The HRS or SHG signals are easily corrupted by many artificial reflected or scattered signals in optical systems within the instrument.

Furthermore, the wavelengths of both HRS and SHG signals are only half of the excitation wavelength. Emission filters are required to ensure that signals are detected. For a multispectral FLIM system with multiple detectors, the situation becomes much more complex as the whole optical path should be rearranged to allow all detectors to detect signals effectively. Strictly speaking, the entire experimental setup should exactly keep the same with that for fluorescence lifetime measurements, or the measured IRF would be inaccurate. But this is difficult or impossible for many practical FLIM systems. Additionally, some detectors, especially for SPAD, have a wavelength-dependent temporal response known as the color effect [1]. In this case, the HRS or SHG signals cannot be used as the IRF should be measured within the same spectra with the fluorescence signals. Measurements of IRF increase experimental complexity and burden. What is worse, for some clinic or in-vivo FLIM-based applications, the IRF cannot be measured. Hence, it is desirable to directly extract the IRF information from the recorded decay profiles without extra measurements. One method uses synthetic gaussian or single exponential decay function to approximate to IRF by adjusting its width and position to give the best fit to the fluorescence decay signal. Such a method shows good precision and a wide dynamic range that can resolve lifetimes close to the FWHM of the IRF. However, one critical drawback for TCSPC FLIM is time-consuming curve-fitting analysis. It becomes worse for the synthetic IRF due to an extra fitting and optimization to determine the synthetic function pixel by pixel. Another method uses an automatic synthetic IRF or differential synthetic IRF, widely adopted in commercial FLIM data analysis software, e.g., SPCI mage (Becker and Hickl, Berlin, Germany). The calculation procedure of such a synthetic IRF can be divided into two steps: 1) the rising edge of the recorded decay profile is fitted with a
suitable function $R(t)$; 2) the synthetic IRF is then calculated as $dR(t)/dt$ [24]. The synthetic IRF has been proved to yield precise fitting results in a deconvolution procedure. Nevertheless, the dynamic range of the synthetic IRF is limited. To obtain acceptable fitting results, the lifetimes of fluorescence signals should be several times longer than the FWHM of the IRF; otherwise, the analysis will be heavily biased. In this work, we proposed a new strategy to generate synthetic IRFs. This newly proposed synthetic IRF is directly extracted from the recorded summed decay histogram of all pixels, which has advantages: a broader dynamic range and higher accuracy. Bi-exponential fluorescence decay models were used in deconvolution procedures for more general FLIM-FRET applications. For better quantitatively evaluations, simulated data was analyzed using a nonlinear least square deconvolution algorithm. Moreover, we also examined the fast deconvolution method’s deconvolution performance based on the Laguerre expansion with the proposed synthetic IRF. The real experimental FLIM-FRET data obtained from the two-photon FLIM system were further analyzed and compared using different automatic synthetic IRFs.

2 THEORY AND METHOD

For simplification, considering a single exponential decay $f(t) = e^{\alpha t}$. In order to evaluate $i(t)$ from $y(t)$, one can obtain the equation by performing both sides of Eq. 2 with the Laplace transform:

$$I(s) = Y(s)/F(s) = sY(s) + \frac{1}{\tau} Y(s) \quad (3)$$

where $Y(s), F(s)$, and $I(s)$ are the Laplace transform pairs of $y(t), f(t)$, and $i(t)$, respectively. $s$ is a complex-valued number. By performing the inverse Laplace transform on Eq. 3, The temporal IRF $i(t)$ is then expressed as

$$i(t) = \frac{dy(t)}{dt} + \frac{1}{\tau} y(t) \quad (4)$$

If the lifetime is large enough, the second item on the right side of Eq. 4 can be neglected, and the IRF can be directly estimated from the measured decay. This only holds for decay components with lifetimes much larger than the FWHM of IRF. However, if the lifetime is close to the FWHM of IRF, the estimated IRF is significantly shortened, which biases the calculated lifetimes toward longer values. As for multieponential decays, since the overall decay is the linear combination of single exponential decays described in Eq. 1, the conclusion is also suitable for this situation. Thus, a compensation method needs to be proposed to extend the applied range of a synthetic IRF.

A series of noiseless decay curves with different lifetimes and their corresponding synthetic IRFs were analyzed to investigate the effect of a fast decay component on the synthetic IRF. A Gaussian function approximates the IRF with a typical FWHM, $w = 300$ ps, referred to as “the true IRF”, $i_0(t)$. The measured decays were then generated by convolving single exponential decays with $i_0(t)$ with 256 time-bins over a range of 10 ns. The synthetic IRF $i_s(t)$ was obtained by calculating the measured decays’ difference and setting the negative values to zero. Figure 1A shows the measured decays with three different lifetimes and their corresponding synthetic IRFs ($i_s(t)$). It is evident that as the lifetime $\tau$ increases, the difference between $i_s(t)$ and $i_0(t)$ diminishes as Eq. 4 suggests. On the contrary, when $\tau$ is approximate to $w$, for example, $\tau = 2w$, the FWHM of $i_s(t)$ is noticeably smaller than that of $i_0(t)$. The results agree well with the above theoretical analysis. Another essential feature is that the fast decay components have more influence on the descending edge of the $i_s(t)$, which accounts for the significant contribution to the decrement of the FWHM in $i_s(t)$. For a smaller $\tau$, the descending edge of $i_s(t)$ has a steeper slope. On the contrary, the rising edge almost keeps unchanged as $\tau$ changes from $2w$ to $10w$. To compensate for the influence of the fast decay component, one possible approach is to use the mirror symmetry of the rising edge to replace the descending edge. The new synthetic IRF can be then referred to as the mirror-symmetric synthetic IRF and denoted by $i_m(t)$, which is calculated by

$$i_m(t) = \frac{dy}{dt}u(t_0 - t) + \frac{dy(t_0 - t)}{dt}u(t - t_0) \quad (5)$$

where $t_0$ is the peak position of the $i_s(t)$ and $u(t)$ is the step function. Figure 1B shows the relative error of FWHM. The relative error is defined as $|w_i - w|/w \times 100$ where $w_i$ is the FWHM of $i_s(t)$ or $i_m(t)$. From Figure 1B, the error of $i_s(t)$ shows an exponential increase when $\tau/w$ moves toward 1. In contrast, $i_m(t)$ offers better performance. The error is much smaller than that of $i_s(t)$ within the whole dynamic range. Even when the lifetime is the same as the FWHM of the IRF ($\tau = w$), the error is still less than 10%. The precise evaluation of the IRF leads to better fitting results in the deconvolution procedure. Moreover, the dynamic range of the proposed IRF can be extended for faster decay components with a lifetime close to the FWHM of the IRF.

3 SIMULATIONS ON FLUORESCENCE LIFETIME IMAGING IMAGES

To compare the deconvolution performances of the two synthetic IRFs $i_s(t)$ and $i_m(t)$, both synthetic IRFs were tested with simulated TCSPC data. It is possible to calculate the bias accurately, and standard deviation since all simulated decays’ parameters are already known. As shown in Eqs 1, 2, different synthetic IRFs are applied in the deconvolution procedure of TCSPC data with a various number of decay components. Here a bi-exponential decay with fast and slow decay components is considered. A bi-exponential decay model has broad applications and can be used to describe the quenched and unquenched states of fluorophores, the decays of endogenous fluorophores, and FRET donors, to name just a few [12]. A bi-exponential decay model is defined as

$$f(t) = ae^{-\alpha_1 t} + (1 - a)e^{-\alpha_2 t} \quad (6)$$
where $\tau_1$ and $\tau_2$ are the two different lifetimes and $a$ is the proportion ($0 < a < 1$). The synthetic measured decays can then be generated by convolving $f(t)$ and the pre-defined real IRF $y(t)$

$$y(t_m) = \sum_{k=0}^{m} i_m (t_m - t_k) f(t_k) + \epsilon_m \quad m = 1, 2, \ldots, 256$$

Here the observation window is $T = 10$ ns with 256 time-channels, and $\epsilon$ is the additive Poisson noise. $i_m(t)$ has a Gaussian profile with $w = 300$ ps. In the simulations, a series of TCSPC FLIM images with $100 \times 100$ pixels were generated, and the total photon count per pixel within the observation window was assumed to be $N_c$. $\tau_2$ is the longer lifetime and fixed at $2.8$ ns, whereas $\tau_1$ is a short lifetime varying from $0.2$ to $1.0$ ns. The proportion $a$ ranges from $0.2$ to $0.8$ with a $0.2$ step interval. Figures 2A,C show two examples of the simulated FLIM images' intensity map. The parameters in (a) and (b) are $a = 0.6$, $\tau_1 = 0.8$ ns, $\tau_2 = 2.8$ ns, and $N_c = 10,000$ for (A) and $a = 0.2$, $\tau_1 = 0.4$ ns, $\tau_2 = 2.8$, and $N_c = 5000$ for (C). (B,D) are the corresponding phasor plots of (A,C). (E) Normalized intensity plots for $Y(t)$ and the single decay in a pixel in (A). Generated synthetic IRF's using the total decay are depicted in dash lines.

The corresponding phasor plots of (a) and (c) are shown in (b) and (d), respectively. In the phasor plots, the real and imaginary parts of the Fourier transform of the decay profile correspond to the horizontal and vertical coordinates, respectively. And the fluorescence decay detected in each pixel can be projected to a single point on a phasor plot [25–27]. In Figures 2B,D, the projected point of a single exponential decay is located on the semicircle, whereas that of a bi-exponential is located on the straight line between two different lifetimes. For a FLIM image with a relative lower $N_c$, the points are spread within a larger area, indicating that the noise has a pronounced effect on the decay profiles. The traditional method to estimate IRF is computationally complicated and inaccurate because the peak position varies due to the noise and jitter. Here, we propose a new approach to extract the IRF based on the measured FLIM images obtained by a single-channel scanning sensor: we estimated the IRF by summing all pixels' histograms together. Since the SNR of the Poisson noise is proportional to the photon count, the total decay can be regarded as a noise-free decay curve and is used for calculating the synthetic IRF. As shown in Figure 2E, the summed decay of all pixels, $Y(t)$, and a decay in a pixel in

![FIGURE 1](image1.png) (A) Decay curves with different lifetimes and their synthetic IRFs. (B) Errors for $i_m(t)$ and $i_m(t)$ when $\tau_1/w$ is changing from 1 to 10.

![FIGURE 2](image2.png) (A) Simulated FLIM images with $a = 0.6$, $\tau_1 = 0.8$ ns, $\tau_2 = 2.8$ ns, and $N_c = 10,000$ for (A) and $a = 0.2$, $\tau_1 = 0.4$ ns, $\tau_2 = 2.8$, and $N_c = 5000$ for (C). (B,D) are the corresponding phasor plots of (A,C). (E) Normalized intensity plots for $Y(t)$ and the single decay in a pixel in (A). Generated synthetic IRF's using the total decay are depicted in dash lines.
were intendedly set to a high value so that the decay curves 106. For better comparing im(t) parameters is lower than that of deconvolution is worse for τ even reaches 100% when Y then obtained from Frontiers in Physics | www.frontiersin.org March 2021 | Volume 9 | Article 635645

Firstly, the nonlinear least-squares deconvolution (NLSD) based on the Levenberg-Marquardt algorithm was applied for recovering the parameters of the decays in Eq. 6. Figures 3A,C,E show the bias plots (Δa/Δa, Δτ/Δτ1 and Δτ/Δτ2) of the deconvolution fitting results using i(t) and im(t) with Nc = 106. For better comparing i(t) and im(t), the photon counts were intendedly set to a high value so that the decay curves are less affected by noise. As a reference, a, τ1 and τ2 were also calculated using the true IRF, i(t), for each pixel. The calculated a, τ1 and τ2 using i(t) have a larger bias within the whole dynamic range. When using i(t), Δa/Δa is generally larger than 10% and even reaches 100% when τ1 is closed to 0.2 or 1 ns. The situation is worse for τ2, where Δτ/Δτ1 is around 100% for all cases, indicating that i(t) cannot be used for resolving τ1. i(t) also failed to estimate τ2 when τ2 is close to 1 ns. In contrast, Δa/Δa, Δτ/Δτ1 and Δτ/Δτ2 are generally less than 1% using im(t). As for im(t), the biases are significantly reduced. The bias for all three parameters is lower than that of i(t). In particular, the bias of τ2 for im(t) is the same as that of i(t).

Figures 3B,D,F show the corresponding precision F-value = (σg/g·Nc)0.5 (g = a, τ1, or τ2) plots for (a) (c) and (e), respectively, where σg is the standard deviation of g [28, 29]. For the ideal condition, F = 1. For most realistic FLIM analysis, F >> 1. The F-values for a, τ1 and τ2 using i(t) are in general larger than those using im(t) or i(t). Surprisingly, the F-values for im(t) and i(t) are nearly the same throughout the whole dynamic range. It also shows that using im(t) instead of i(t), the instability effect of the synthetic IRF on the deconvolution procedure can be eliminated.

The deconvolution performances of i(t) and im(t) under relatively low photon counts were also assessed. For many applications such as real-time FLIM imaging for investigating cell dynamics or high-throughput screening, the acquisition time is usually kept low, resulting in low photon counts in pixels. Figures 4A–F show the bias, and F-value plots for simulated fluorescence decays with Nc = 5000 in each pixel. In this case, the noise considerably distorts the decay curve. As shown in Figures 4A,C,E, all three IRFs yield worse bias performances compared with those shown in Figure 3. Also, the gaps between the bias plots for all three parameters decrease, showing that in low photon counts, the deconvolution procedure becomes insensitive to the differences between IRFs. Nevertheless, im(t) still shows better performances to resolve τ2 when τ1 is smaller than 1 ns. For determining τ2, im(t) also yields similar performances with i(t). Moreover, im(t) has similar precision performances with i(t), showing smaller F-values for all variables.
compared with those of $i_n(t)$. On the other hand, $i_f(t)$ can yield an extremely large $F$-value for resolving $\tau_2$. Therefore, it demonstrates that $i_m(t)$ can provide a better estimation of the true IRF.

Although NLSD fitting routines have been widely used for FLIM analysis, they still have intrinsic limitations. They are usually time-consuming and computationally intensive. Moreover, they are prone to overfitting problems when the fluorescence signal is heavily contaminated by noise. An alternative fast least-squares deconvolution based on Laguerre expansion (LSD-LE) was recently developed [30–34]. LSD-LE has been proven to be a robust and effective method showing much faster deconvolution speed than traditional methods. It also shows superior sensitivity in disease diagnoses. In brief, Eqs. 2, 6 can be rewritten in discrete forms:

$$y(k) = \sum_{i=1}^{k} i(k-i)f(i) + \epsilon(k), k = 1, 2, \ldots, N$$

$$f(k) = ae^{-(k-1)t_1} + (1-a)e^{-(k-1)t_2}$$

where $t_i$ is the time bin width. LSD-LE expands the fluorescence single $f(t)$ onto an ordered set of orthonormal Laguerre basis functions $b(k; \alpha)$ as:

$$\hat{f}(k) = \sum_{l=0}^{L} c_l b_l(k; \alpha)$$

where $L$ is the Laguerre dimension and $\alpha (0<\alpha < 1)$ is the scale parameter of LBF, and $c_l$ is the $l$th expansion coefficient. The $l$th discrete LBF is defined as:

$$b_l(k; \alpha) = \frac{\alpha(k-1)(1-\alpha)}{2} \sum_{i=0}^{L-1} (-1)^{i} \binom{k}{i} \binom{L-1}{i} (1-a)^i$$

Under the Laguerre expansion, Eq. 9 becomes:

$$y(k) = \sum_{l=0}^{L} \sum_{i=0}^{L} c_l i(k-i)b_l(i; \alpha) + \epsilon_k$$

Equation 12 is the Laguerre expansion form of the fluorescence signal, which can be linearly parameterized by the expansion coefficient $c_l$. Also, the normalized sum of squared errors (NSSE) is defined as:

$$NSSE = \frac{||\hat{f} - f||^2}{||f||^2}$$

To obtain the expansion coefficient $c_l$, the expansion of the fluorescence signal with LBFs becomes a fitting problem where NSSE reaches its minimal value. We would like to assess how $i_f(t)$ behaves in Eq. 13. Therefore, the constrained LSD-LE is applied to recover the decay parameters using synthetic IRFs and the true

![Figure 4](https://www.frontiersin.org)
IRF [30]. The LBF parameters were set as the optimized value as $(\alpha, L) = (0.92,16)$ [32]. The total photon counts in each pixel are $N_c = 5000$. The normalized bias and $F$-value plots are shown in Figures 5A–F. Not surprisingly, $i_m(t)$ still has the worse performance (larger bias and $F$-value). It is unable to estimate $\tau_1$ robustly. Meanwhile, it fails to recover $\tau_2$ when $\tau_1$ approaches 1 ns. $i_m(t)$ has almost the same deconvolution results with the true IRF $i(t)$ in terms of the bias and $F$-value. It further demonstrates that compensating the descending edge of synthetic IRF is an effective way to improve the precision and the applied lifetime range of the synthetic IRF.

4 EXPERIMENTAL FLUORESCENCE LIFETIME IMAGING-FÖSTER RESONANCE ENERGY TRANSFER DATA ANALYSIS

To evaluate the performances of the new automatic synthetic IRF in real experiments, FLIM-FRET imaging data of tSA201 cells transfected with eCFP-eYFP (enhanced green fluorescent protein and enhanced cyan fluorescent protein) pair were investigated. FLIM-FRET is a well-established technique for studying protein-protein interactions within a nanometer scale. FRET refers to the non-radiative energy transfer between an excited fluorescent molecule (the donor) and a non-excited different fluorescent molecule (the acceptor) when they are close, which leads to the shortening the donor lifetime. The eCFP-eYFP pair is the most widely used donor-acceptor pair in various in-vitro or in-vivo FRET applications. The lifetimes of the eCFP-eYFP pair with/without FRET are known priorly, thus serving as a reference to evaluate the FRET between interacting proteins. Here the FLIM-FRET technique was used to assess the proximity of interacting proteins.

A two-photon FLIM system including a confocal microscope (LSM 510, Carl Zeiss), a femtosecond Ti: sapphire laser modulated source (Chameleon, Coherent) with excitation wavelength 800 nm, and the TCS acquisition system (SPC-830, Becker and Hickl GmbH) was used to obtain IRF and FLIM data. The exciting laser source’s duration is less than 200 fs, and the repetition rate is 80 MHz. The bin width of the TCS is 0.039 ns, and each measured histogram contains 256 time bins. Firstly, the IRF of the system was measured using the SHG signal from the urea ((NH₂)₂CO) microcrystal. A thin layer of urea crystal obtained from air-dry concentrated urea droplet was placed on a microscope slide and was covered by a coverslip. The emitted SHG signal was then collected by a photomultiplier (PCM-100, Becker & Hickl GmbH) after passing through a ×63 water-immersion objective lens (N.A. = 1.0) and a

![FIGURE 5 | (A,C,E) Normalized bias plots for $a$, $\tau_1$ and $\tau_2$ when $N_c = 5000$ using LSD-LE method with $(\alpha, L) = (0.92,16)$. The corresponding $F$-value plots are depicted in (B,D,F).](attachment:image.png)
650 nm short-pass filter. The emitted fluorescence signals from the cell samples were also collected using the same system except that a 535–590 nm bandpass filter was used.

The tSA201 cells were grown to 60% confluence on 13 mm glass coverslips located in 24 well plates. The cells were transfected with hP2Y12-eCFP or co-transfected with hP2Y12-eCFP and hP2Y1-eYFP. After 48 h of transfection, the cells on the coverslips were washed once gently with PBS followed by fixation with ice-cold methanol for 10 min at room temperature. Then they were washed 3 times with PBS before they were mounted on to glass microscope slides with Mowiol. The microscope slides were then stored in the dark at room temperature overnight to allow the coverslips to dry, then held at 4°C for later use.

The analyzed results of tSA201 cells with co-transfected eYFP are shown in Figure 6. The eYFPs work as acceptors and their lifetimes increase when FRET occurs. Figure 6A shows the grey-scale fluorescence intensity image. Although the fluorescence intensity can be an indicator of FRET, it is susceptible to photobleaching and spectral cross-talk in FRET pairs, thus greatly limiting its application range in real scenarios. From the intensity image, it is difficult to evaluate the FRET among cells. The summed histogram \( Y(t) \) of all pixels and the measured IRF \( i_r(t) \) are shown in Figure 6B, in which \( i_r(t) \) has already been aligned with the rising edge of \( Y(t) \). Two synthetic IRFs \( i_s(t) \) and \( i_m(t) \) derived from \( Y(t) \) are shown in lines with markers. The main peaks of synthetic IRFs are well agreed with the measured IRF. However, the pre-pulse in \( i_r(t) \) is quite short in the log-scale plot because the negative part of \( i_r(t) \) is truncated to zero. This problem is mitigated by replacing the descending edge by the rising edge in \( i_m(t) \). The FWHM of \( i_m(t) \) is nearly the same with \( i_r(t) \). It is worth noting that there are many complex sub-structures of after-pulse in \( i_r(t) \), caused by ion-feedback in the PMT. However, the amplitudes of these after-pulses are two orders in the magnitude smaller than the peak of \( i_r(t) \); therefore, the effect of these after-pulses can be neglected.
Figures 6C–F shows \( \tau_1, \tau_2, a \) and \( \tau_{\text{amp-ave}} \) images for the bi-exponential model using the experimental IRF \( i(t) \) and constrained LSD-LE method with \( (\alpha, L) = (0.92, 16) \). The \( \tau_{\text{amp-ave}} \) is the amplitude-average lifetime defined as \( \tau_{\text{amp-ave}} = a\tau_1 + (1-a)\tau_2 \). The shorter lifetime \( \tau_1 \) and longer lifetime \( \tau_2 \) are depicted in Figures 6C,D, respectively. A better contrast can be observed from these two figures. The image of the proportion \( a \) is shown in Figure 6E, which is typically used to calculate the FRET efficiency. One remarkable phenomenon that can be observed from the image is the proportion \( a \) at the edges of the cells is relatively smaller than the surrounding, which is attributed to the lifetime of eYFP becoming longer due to a higher FRET efficiency. As a comparison, Figure 6F shows the amplitude-weighted average lifetime, from which we can observe the changed lifetime in the range of the whole cells.

To compare the deconvolution performances of \( i_a(t) \) and \( i_{\text{amp}}(t) \) with that of \( i(t) \), the corresponding lifetime images for two automatic synthetic IRFs were calculated. For a better comparison, the scatter plots of \( \tau_1, \tau_2 \) and two kinds of average lifetimes named amplitude-weighted average lifetime \( (\tau_{\text{amp-ave}}) \) and intensity-weighted average lifetime \( (\tau_{\text{int-ave}}) \) vs. \( a \) are shown in Figures 7A–D, respectively. \( \tau_{\text{int-ave}} \) is also taken into consideration, defined as \( \tau_{\text{int-ave}} = [a\tau_1^2 + (1-a)\tau_2^2]/[a\tau_1 + (1-a)\tau_2] \). For \( \tau_1 \) and \( \tau_2 \) in Figures 7A,B, it is easy to see that the lifetime distributions obtained from \( i(t) \) (dots with blue “+” marker) are significantly different from that of \( i_a(t) \) (green “.” marker). The clusters obtained by \( i_{\text{amp}}(t) \) and \( i(t) \) are discernible. It demonstrates that the deconvolution results using \( i_a(t) \) can lead to a large bias compared to the results using \( i(t) \) and a wrong interpretation of the data. For example, for \( \tau_1 \) with sub-nanosecond lifetime, \( \alpha \) should be less than 0.8 according to the \( i(t) \) deconvolution results. Still, the results using \( i_a(t) \) leads to large dots distributions at \( \alpha > 0.8 \) (top left corner in Figure 7A). This problem also happens for \( \tau_2 \). On the other hand, for the proposed synthetic IRF \( i_{\text{int}}(t) \), the cluster shape of the data is almost identical with that of \( i(t) \), indicating that \( i_{\text{int}}(t) \) is more suitable for recovering the real parameters. As for the average lifetimes \( \tau_{\text{amp-ave}} \) and \( \tau_{\text{int-ave}} \) in Figures 7C,D, interestingly, the cluster shapes of three IRFs are similar, but the deviation of the results with \( i(t) \) from the other two is still noticeable. Compared to the cluster for \( i(t) \), the overall clusters for \( i_a(t) \) have a larger distribution range. Additionally, \( i_{\text{int}}(t) \) can yield an obvious artificial cluster at \( \alpha = 0 \), which is eliminated for \( i_{\text{int}}(t) \). Hence, it is safe to prove that \( i_{\text{int}}(t) \) shows superior deconvolution performances than \( i(t) \). It is worth noting that, for lifetimes down to or even smaller than the FWHM of the IRF, for example, the gold nanoparticles used as the biomarkers, both the synthetic IRFs would lead to a large deviation as shown in Figure 1B. Therefore, synthetic IRFs are not suitable for deconvolution analysis. Although our synthetic can well approximate the true IRF, it does not consider the pre-pulse and sub-structure after the main peak of IRF. However, both only cause negligible effects in TCSPC measurements because their magnitudes are generally two orders smaller than the main peak.

5 CONCLUSION

In conclusion, we proposed a strategy for obtaining the synthetic IRF of TCSPC based FLIM experiments. Compared to the simple differential synthetic IRF, the dynamic range of the mirror-symmetric synthetic IRF is significantly expanded. Even when the lifetime is close to the FWHM of the system’s true IRF, the proposed synthetic IRF can resolve the lifetime with high accuracy. At the same time, the accuracy is also much improved.
in the whole dynamic range. The proposed synthetic IRF was also applied to analyze bi-exponential decays with simulated data using both nonlinear least-square deconvolution and Laguerre expansion methods. The results show that the mirror-symmetric synthetic IRF has higher accuracy and a lower standard deviation. Additionally, the proposed synthetic IRF can resolve the more extended lifetime component in the whole dynamic range, unattainable in the simple differential synthetic IRF. We further investigated the proposed synthetic IRF with the real experimental FLIM-FRET data. Both simulated and experimental data show that the proposed synthetic IRF has superior performance than traditional synthetic IRF.

DATA AVAILABILITY STATEMENT
The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

REFERENCES
1. Lakowicz JR. Principles of fluorescence spectroscopy. Boston, MA: Springer (2006).
2. Datta R, Heaster TM, Sharick JT, Gillette AA, Skala MC. Fluorescence lifetime imaging microscopy: fundamentals and advances in instrumentation, analysis, and applications. J Biomed Opt (2020) 25(7):1. doi:10.1117/1.JBO.25.7.071203
3. Suhling K, Hirvonen LM, Levitt JA, Chung P-H, Tregidgo C, Le Marois A, et al. Fluorescence lifetime imaging (FLIM): basic concepts and some recent developments. Med Phys (2015) 27:3–40. doi:10.1118/1.4854680
4. Ngziachristos V. Going deeper than microscopy: the optical imaging Frontier in biology. Nat Methods (2010) 7(8):603–14. doi:10.1038/nmeth.1483
5. Bower AJ, Sorrells JE, Li J, Marjanovic M, Barkalifa R, Boppart SA. Tracking metabolic dynamics of apoptosis with high-speed two-photon fluorescence lifetime imaging microscopy. Biomed 10(12):6408–21. doi:10.1368/BOE.10.060408
6. Okabe K, Inada N, Gota C, Harada Y, Funatsu T, Uchiyama S. Intracellular temperature mapping with a fluorescent polynamic thermometer and fluorescence lifetime imaging microscopy. Nat Commun (2012) 3(1):795. doi:10.1038/ncomms1714
7. Sagolla K, Löhmansröben HG, Hille C. Time-resolved fluorescence microscopy for quantitative Ca2+ imaging in living cells. Anal Bioanal Chem (2013) 405(26):8525–37. doi:10.1007/s00216-013-7290-6
8. Schmitt FJ, Thaa B, Junghans C, Vitali M, Veit M, Friedrich T. eGFP-pHsens as a highly sensitive fluorophore for cellular pH determination by fluorescence lifetime imaging microscopy (FLIM). Biochim Biophys Acta Bioenerg (2014) 1837(9):1581–93. doi:10.1016/j.bbabi.2014.04.003
9. Lukina MM, Shimolina LV, Kiselev NM, Zagainov VE, Komarov DV, Zagayanova EV, et al. Interrogation of tumor metabolism in tissue samples ex vivo using fluorescence lifetime imaging of NAD(P)H. Methods Appl Fluoresc (2020) 8(1):014002. doi:10.1088/2050-6120/ab4ed8
10. Shivalingam A, Izquierdo MA, Le Marois A, Vyšniauskas A, Suhling K, Kuimova MK, et al. The interactions between a small molecule and G-quadruplexes are visualized by fluorescence lifetime imaging microscopy. Nat Commun (2015) 6(1):6178. doi:10.1038/ncomms9178
11. Tardif C, Nadeau G, Labrecque S, Côté D, Lavioe-Cardinial F. Fluorescence lifetime imaging nanoscopy for measuring Förster resonance energy transfer in cellular nanodomains. Neurophoton (2019) 6(1):015002. doi:10.1177/2398821018805424
12. Sparks K, Kondo H, Hooper S, Munro L, Kennedy G, Dunby C, et al. Heterogeneity in tumor chromatin-doxorubicin binding revealed by in vivo fluorescence lifetime imaging confocal endomicroscopy. Nat Commun (2018) 9(1):2662. doi:10.1038/s41467-018-04820-6

AUTHOR CONTRIBUTIONS
DX proposed the conceptualization and wrote the manuscript. MS and MC cultured and prepared the cell samples. NS and YC provided fluorescence lifetime imaging data and analysis. DL provided supervision and manuscript reviewing and editing. All authors reviewed the final manuscript.

FUNDING
The authors would like to acknowledge the Medical Research Scotland (1179-2017), Photon Force, Ltd., and the Engineering and Physical Sciences Research Council (EP/L01596X/1) for supporting this project. Photon Force supports the use of SPAD cameras in our project. The funder was not involved in the study design, collection, analysis, interpretation of data, the writing of this article or the decision to submit it for publication.
26. Ranjit S, Malacrida L, Jameson DM, Gratton E. Fit-free analysis of fluorescence lifetime imaging data using the phasor approach. *Nat Protoc* (2018) 13(9): 1979–2004. doi:10.1038/s41596-018-0026-5

27. Stringari C, Cinquin A, Cinquin O, Digman MA, Donovan PJ, Gratton E. Phasor approach to fluorescence lifetime microscopy distinguishes different metabolic states of germ cells in a live tissue. *Proc Natl Acad Sci USA* (2011) 108(33):13582–7. doi:10.1073/pnas.1108161108

28. Gerritsen HC, Asselbergs MA, Agronskaia AV, Van Sark WG. Fluorescence lifetime imaging in scanning microscopes: acquisition speed, photon economy and lifetime resolution. *J Microsc* (2002) 206(3):218–24. doi:10.1046/j.1365-2818.2002.01031.x

29. Li DD, Ameer-Beg S, Arlt J, Tyndall D, Walker R, Matthews DR, et al. Time-domain fluorescence lifetime imaging techniques suitable for solid-state imaging sensor arrays. *Sensors (Basel)* (2012) 12(5):5650–69. doi:10.3390/s120505650

30. Jo JA, Fang Q, Marcu L. Ultrafast method for the analysis of fluorescence lifetime imaging microscopy data based on the Laguerre expansion technique. *IEEE J Sel Top Quantum Electron* (2005) 11(4):835–45. doi:10.1109/JSTQE.2005.857685

31. Jo JA, Fang Q, Papaioannou T, Marcu L. Fast model-free deconvolution of fluorescence decay for analysis of biological systems. *J Biomed Opt* (2004) 9(4):743–52. doi:10.1117/1.1752919

32. Liu J, Sun Y, Qi J, Marcu L. A novel method for fast and robust estimation of fluorescence decay dynamics using constrained least-squares deconvolution with Laguerre expansion. *Phys Med Biol* (2012) 57(4):843–65. doi:10.1088/0031-9155/57/4/843

33. Pande P, Jo JA. Automated analysis of fluorescence lifetime imaging microscopy (FLIM) data based on the Laguerre deconvolution method. *IEEE Trans Biomed Eng* (2011) 58(1):172–81. doi:10.1109/TBME.2010.2084086

34. Zhang Y, Chen Y, Chen Y, Li DD. Optimizing Laguerre expansion based deconvolution methods for analysing bi-exponential fluorescence lifetime images. *Opt Express* (2016) 24(13):13894–905. doi:10.1364/OE.24.013894

**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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