Third Generation in Cascade Decays

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In supersymmetric models with gluinos $m(\tilde{g}) \sim 1000 – 2000$ GeV, new physics searches based on cascade decay products of the gluino are viable at the next run of the LHC. We investigate a scenario where the light stop is lighter than the gluino and both are lighter than all other squarks, and show that its signal can be established using multi-$b$-jet, multi-$W$ and/or multi lepton final state topologies. We then utilize both boosted and conventional jet topologies in the final state in conjunction with di-tau production as a probe of the stau-neutralino co-annihilation region responsible for the model’s dark matter content. This study is performed in the specific context of one such phenomenologically viable model named No-Scale $F$-$SU(5)$.

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I. INTRODUCTION

Weak-scale supersymmetry (SUSY) provides a leading candidate for physics beyond the Standard Model (SM), as it addresses the hierarchy problem, gives gauge coupling unification, and (in R-parity conserving models) provides a robust dark matter (DM) candidate. The search for colored superpartners at the Large Hadron Collider (LHC) has so far yielded null results. The exclusion limits on squark ($\tilde{q}$) and gluino ($\tilde{g}$) masses, when they are comparable, are approximately 1.5 TeV at 95% CL with 20 fb$^{-1}$ of integrated luminosity [1–4]. If the squarks are heavy, the gluino mass is constrained to be heavier than approximately 1.2 TeV at 95% CL with 20 fb$^{-1}$ of integrated luminosity [1–5].

There are many interesting scenarios where the squarks are heavy but the gluino mass is about a TeV or so. In this paper we probe one such scenario, i.e., No-Scale $F$-$SU(5)$ [6, 7]. In this model, the Higgs mass receives supplementary contributions from additional TeV scale vector-like fields [8], which may make it easier to obtain a Higgs mass near 126 GeV without tuning in the stop sector. The light stop $\tilde{t}_1$ is lighter than the gluino in this model, and by an amount that allows for on-shell decays with unity branching ratio for most of the viable parameter space. Similar types of mass spectra may also occur in large volume scenario models [9]. Once gluinos are produced, they may cascade via the stop into the (Wino-like) second lightest neutralino or light chargino, which then decay into the lightest neutralino via stau, e.g. $\chi_2^0 \to \tilde{\tau}_1 \tau \to \tau \tau \chi_1^0$. The potentially sizeable mass gap between the first and second neutralino will tend to impart a sizeable kinematic boost to the lead tau production, but the narrow conduit $\Delta M = M_{\chi_1^0} = M_{\chi_2^0}$ linking the stau and LSP may render the secondary tau rather soft, and hence more difficult to detect, barring inheritance of a substantive upstream boost. The dark matter content may be obtained thermally by stau and (Bino-like) light neutralino co-annihilation in the case of a small $\Delta M \approx 6$ GeV.

The final state of such a cascade contains $b$-quarks, $\tau$ leptons, missing transverse energy $E_T$, and also additional light flavor leptons. The scenario can be established by the presence of multiple $b$-quarks and leptons in the final state. Establishing the coannihilation element would require $b$'s and $\tau$'s in the final state, where $t\bar{t}$ is the dominant background for such a signal, also containing $b$'s, $\tau$'s and missing energy. In this paper we first try to establish the scenario from the multi-$b$-jets and leptons in the final state. Establishing the coannihilation element would require $b$’s and $\tau$’s in the final state, where $t\bar{t}$ is the dominant background for such a signal, also containing $b$’s, $\tau$’s and missing energy. In this paper we first try to establish the scenario from the multi-$b$-jets and leptons in the final state. Establishing the coannihilation element would require $b$’s and $\tau$’s in the final state, where $t\bar{t}$ is the dominant background for such a signal, also containing $b$’s, $\tau$’s and missing energy. In this paper we first try to establish the scenario from the multi-$b$-jets and leptons in the final state. Establishing the coannihilation element would require $b$’s and $\tau$’s in the final state, where $t\bar{t}$ is the dominant background for such a signal, also containing $b$’s, $\tau$’s and missing energy.
refer to as the “Conventional Event Topology”, the two leading jets $j_{1,2}$ in $|\eta| < 2.5$ carry very large transverse momenta $p_T > (400, 200)$ GeV. No vetoes on heavy flavor jets or light lepton flavors are enforced. We will demonstrate the cut flow optimization for all the selections, and calculate the signal to background ratios S/B. A methodology using the boosted event topology has been used in the context of stop searches recently [10] and is found to be very effective for background reduction. A variation of conventional topology has been prescribed in [11] with the requirement that the jets have to be non-$b$ jet to reduce the background. In our case study, however, the signal contains a large population of $b$-jets arising from decays of the on-shell stop, which makes controlling the $t\bar{t}$ background for establishing the coannihilation region more challenging.

The structure of the paper is as follows. In Section II, the model context is described for this work, followed by event generation and selection in Section III. The primary results and analysis are presented in Sections IV (establishment of the signal), V (di-tau event topologies), and VI (resolving the neutralino-stau system). Conclusions are given in Section VII.

II. NO-SCALE $\mathcal{F}$-SU(5) MODEL CONTEXT

In order to provide a specific context for long-chain cascades of the described type arising from the gluino decay when the squarks are heavy, this study will reference a class of well-defined models named No-Scale $\mathcal{F}$-SU(5) (see Ref. [6] and references therein), which combine (i) field content of the Flipped SU(5) grand unified theory (GUT), with (ii) a pair of hypothetical TeV-scale vector-like supermultiplets (“flippons”) of mass $M_V$ derivable within local F-Theory model building, and (iii) the boundary conditions of No-Scale Supergravity (SUGRA).

The signature collider characteristic of this model family is a light stop $t_1$, lighter than the gluino $\tilde{g}$, which is in turn lighter than all other squarks $\tilde{q}$. Lightness of the gluino is attributable to flippon-induced modifications to evolution of the renormalization group equations (RGEs), specifically a nullification at first-loop of the color-associated beta-function coefficient ($b_3 = 0$); these modifications simultaneously elevate the scale of secondary Flipped SU(5) × U(1)$_X$ gauge unification into adjacency with $M_{\text{Planck}}$, allowing for phenomenologically consistent implementation of the notoriously delicate No-Scale framework [12, 13]. The gluino to stop plus top decay $\tilde{g} \rightarrow t\bar{t}$ is on-shell, with a 100% branching ratio in the viable parameter space, and is associated with an extreme prevalence of hadronic jets [7].

The key phenomenological characteristic of this model is proportional rescaling at leading order of the full model spectrum with respect to only a single high scale dimensionful parameter, the unified gaugino mass $M_{1/2}$. The model is only logarithmically sensitive to the specific threshold scale $M_V$ at which the vector-like multiplets actively circulate in loops. Lower order facility is available to exchange small variations of $\tan \beta$, the ratio of up- and down-like Higgs vacuum expectation values, within a narrow range around 20 – 25 for a corresponding fluctuation in the stau-LSP mass gap $\Delta M$ between about 5 and 25 GeV. The neutralino LSP dark matter candidate is always dominantly Bino.

This model thereby provides a tightly constrained, yet realistic, testbed for a study of the described type, which may moreover exemplify a formally smooth transition between thermal and non-thermal dark matter scenarios. The $\mathcal{F}$-SU(5) SUSY spectrum for $M_{1/2} \sim 1$ TeV and $\Delta M \sim 6$ GeV is provided in Table I. This example is in the stau-neutralino coannihilation region, with thermal Bino dark matter providing the observed relic density. The selected mass range is in the vicinity of the exclusion boundary established data from the 7 and 8 TeV Large Hadron Collider (LHC) runs; commencement of collisions near the 14 TeV design energy will actively probe the $\mathcal{F}$-SU(5) construction at scales above $M_{1/2} = 1$ TeV. The technology to be described is generically applicable for all UV models that feature light gluinos, for example those based alternatively on the SO(10) GUT, and can be employed broadly in the next run of LHC.

![Table I: Spectrum (in GeV) for $M_{1/2} = 990$ GeV, $M_V = 8044$ GeV, $m_t = 174.4$ GeV, and $\tan \beta = 23.3$. Here, $\Omega_{\text{CDM}}h^2 = 0.1197$, the stau-LSP mass gap is $\Delta M = 6.4$ GeV, and the lightest neutralino is greater than 99% Bino. For other values of $M_{1/2}$, revisions to the complete SUSY spectrum may be very well approximated by a simple proportional rescaling. $\Delta M$ may be increased by slightly lowering $\tan \beta$, with minimal additional effect on the spectrum overall.](attachment:image)

III. EVENT GENERATION AND SELECTION

Numerical analysis of the parameter interdependencies in No-Scale $\mathcal{F}$-SU(5) is conducted with Suspect 2.34 [14], utilizing a proprietary codebase modification that incorporates the flippon-enhanced RGEs. Signal and standard model (SM) background Monte Carlo event samples, including parton showering and fast detector simulation, are generated via the standard MadGraph5/MadEvent [15], Pythia [16], PGS4 [17] chain. Subclassifications of SUSY two-body production channels, such as $gg, g\tilde{g}, gg, g\tilde{q}$, and etc., are individually simulated for a variety of $\mathcal{F}$-SU(5) benchmark configurations with 0, 1, or 2 hard jets (generated inclusively) at the matrix element level. There is some approximation here (at a level consistent with other technological and systematic limitations) associated with (for exam-
ple) the reembedding of certain diagrams for squark production with 0 jets into diagrams for gluino pair production with 2 jets. MADEVENT is configured, in conjunction with PYTHIA, to use MLM matching with kt jets in the “Shower kT” scheme, setting (ICKKW = 1), (XQUT = 200), (DRJJ = 0), (AUTO_P3J +MJJ = T), (Qicut ⇒ 200), and (SHOWERK = T). The PGS4 detector simulation employs a standard LHC-appropriate parameter card, with jet clustering performed using the anti-kt algorithm. Given the vital importance of hadronic tau reconstruction to this study, the somewhat dated “shrinking cone” algorithm native to PGS4 has been replaced by a customized treatment that applies a flat 60% detection efficiency (with a 1% fake rate) to tau objects itemized at the PYTHIA level; the invisible tau neutrino 4-momentum is appropriately subtracted. The algorithms for tagging of heavy flavor jets have also been customized, with curves selected for an efficiency around 70%, and the acceptance region in pseudo-rapidity for generic jet candidates has been extended to $|\eta| < 5.0$. Selection cuts are implemented on the detector-level event simulation within AEACuS 3.6 [18, 19]. Initial event selections for the various targeted final states are made very conservatively, to allow for subsequent optimization.

The strongest signal of new physics in a $m(\tilde{q}) > m(\tilde{t}_1)$ type model is expected in association with extremely long cascade decay chains, featuring a strong four $W$ plus four $b$ heavy flavor jet component [5]. Since the $W$ may decay leptonically (1/3 for three light generations) or hadronically (2/3 for two light generations times 3 colors), the final state will also be profused with soft leptons and multi-jets. In order to establish the signal, we therefore require at least two b-jets in all cases, while recording the net count of jets, leptons, di-leptons, and missing transverse energy $\not{E}_T$, expecting (i) that events with fewer leptons should have more jets, and (ii) that the dominant $t\bar{t} +$Jets background may likewise have large jet counts, but should not generally feature very large $\not{E}_T$ values. For $t\bar{t} +$Jets, charge conservation further implies that any dilepton production must be anti-correlated in sign, whereas the independent leptonic decay events are uncorrelated in flavor. The SUSY four $W + b$ signal may readily produce tri-leptons (category III), which are inaccessible, outside of fakes, to $t\bar{t} +$Jets; this category, which necessarily includes also a like-sign dilepton, should be intrinsically low background. Likewise, the orthogonal categorization of precisely two leptons (category II) with like sign should intrinsically suppress $t\bar{t} +$Jets, with residual fakes, sign-flips, etc., reduced by a requirement on missing transverse energy $\not{E}_T$. The remaining event subdivisions (category I), i.e. those with 0, 1, or 2 leptons, but no like-sign dilepton, will rely heavily on the missing energy cut for background reduction, but may also feature a much stronger net signal count. Opposite sign di-tau production, which is subsequently studied in detail, is a subset of this very broad event category (though the final jet requirements will ultimately be quite different).

In the $2j + 2\tau + \not{E}_T$ final state, which is vital to probing the question of dark matter coannihilation, we preliminarily select on (i) two or more isolated taus with $P_T > (40, 20)$ GeV in $|\eta| > 2.5$; (ii) two jets $j_{i,2}$ with $P_T > 20$ GeV in $|\eta| > 2.5$ for the conventional scenario, $OR$ two jets $j_{i,2}$ with $P_T > 20$ GeV, ($\eta_1 \times \eta_2 < 0$), and $|\eta_2 - \eta_1| > 3.5$ in $|\eta| > 5.0$ for the boosted scenario. More specifically, in the latter scenario, the pair satisfying these criteria that has the largest invariant mass is tagged, and additional jets interior to this pair are allowed. The AEACuS instructions (with comments) applicable to these selections (and to the computation and storage of other analysis parameters such as the $\not{E}_T$, jet kinematics, heavy flavor and light lepton counts, di-tau sign orientation, transverse momentum components, and invariant masses) are documented in Card A.

```
1 ******* cut_card.dat v3.6 *******
2 * DiTau, Jets and MET Searches
3 *** Object Reconstruction ****
4 OBJ_JET = PTM:20, PWM:(0,0.2,5)
5 # Jet candidates with P_T > 20 & |ETA| < 2.5
6 # OBJ_JET = PTM:20, PWM:(0,0.5,0)
7 # Alternative "VBF" Wide Jets for boosted scenario
8 OBJ_JET_001 = SRC:<000, CUT:(2,UNDEF,-1)
9 # Classifies Leading Jet Pair objects
10 # OBJ_JET_001 = SRC:<000, EFF:([-1,3,5,UNDEF],1)
11 # CUT:[2,UNDEF,-1] # Alternative "VBF" Topology
12 # for boosted scenario with Delta ETA > 3.5
13 OBJ_JET_002 = SRC:<001, CUT:[1,UNDEF,-1],
14 # Two isolated taus with P_T > 20
15 # OBJ_JET_003 = SRC:<001,-002>,
16 # OBJ_JET_004 = SRC:<002,003>, HFT:0.5, CUT:0
17 # Outputs Lead Jet kinematics
18 OBJ_JET = PTM:10, PWM:(0,0.2,5)
19 # Soft Leptons restricted in P_T and ETA
20 OBJ_JET_001 = SRC:<000, PTM:20, ENT:+3, SDR:[0.3,UNDEF,1],
21 CUT:[2,UNDEF,-1] # Two isolated taus with P_T > 20
22 # OBJ_JET_002 = SRC:<001, PTM:40, CUT:[1,UNDEF,-1],
23 # OBJ_JET_003 = Lead Tau has P_T > 40
24 OBJ_JET_004 = SRC:<001,-002>, OUT:PTM:004
25 # Object holds the Soft Tau (no cut)
26 OBJ_JET_000 = SRC:<000, PTM:40, ENT:+3, CUT:0
27 # Counts soft light leptons (no cut)
28 OBJ_DIL_001 = LEP:001, DLS:+1, CUT:0
29 # Counts Like Sign DiTaus (no cut)
30 OBJ_DIL_002 = LEP:001, DLS:-1, CUT:0
31 # Counts Opposite Sign DiTaus (no cut)
32 #對 Event Selection *******
33 EVT_MET = CUT:0
34 # Outputs Missing Energy (no cut)
35 EVT_DIL_001 = LEP:001, CUT:0
36 # Outputs DiTau Invariant Mass (no cut)
37 #******** cut_card.dat v3.6 *******
```

Card A: AEACuS instruction card for di-Tau, jets and missing transverse energy $\not{E}_T$ searches.

IV. ESTABLISHING THE $F$-SU(5) SIGNAL

The described 2 b-jet signal categories (I.III) have been established in Monte Carlo simulation. The results are little changed for a b-jet transverse momentum threshold of 40 GeV versus 80 GeV, so the more robust value of 80 is retained. The intuition that something like
interactions with b-quark and gluino transition (typically a 500 GeV to 750 GeV mass gap) are expected to be quite hard. Jets downstream from the stop decay also receive a substantial boost from the mass differential, and all downstream jets may inherit large kinematic boosts, even in decays with less phase space. Requiring $P_T > (400, 200)$ GeV facilitates very robust tagging on the leading jet pair, while dampening background (allowing a lower $E_T$ floor), and retaining excellent signal statistics. Jets 3 and 4 are well resolved at $P_T > 80$ GeV, consistent with the b-jet threshold, whereas any jets required beyond the leading four are better captured with softer threshold around $P_T^{4+} > 40$ GeV. With these cuts in place, the missing transverse energy $E_T$ threshold may be individually optimized for each category, as demonstrated in Figs. (1,2).

We will select $E_T > (700, 500, 300)$ GeV, respectively. The AEACuS instructions (with comments) applicable to the Category I final state selections are documented in Card B, and may be readily adapted for application to categories II or III.

The background is found in each case to be extraordinarily well controlled, with excellent signal retention. Categories III (tri-leptons) and II (like-sign di-leptons) appear to be observable up to about $M_{1/2} \sim 1200$ GeV, while the primary category I (all other events) may be probed beyond $M_{1/2} \sim 1400$ GeV, encompassing the majority, if not totality, of the $SU(5)$ model space. The gluino masses in these cases are on the order of 1600 and 1900 GeV, respectively. As demonstrated clearly in Fig. (1), the expected SUSY event yield is a strongly decaying function of $M_{1/2}$, which may be inverted in order to establish the global $SU(5)$ mass scale. Since the model is dominantly single parameter, the bulk properties of the spectrum are then fixed, and may be cross-correlated against alternatively designed event selections for consistency, such as the di-tau production channel to be elaborated subsequently.

In Fig. (3), we show that the signal is indeed more rich in heavy flavor jets than the background, even after considering b-fake rates. It should be recalled that these rates also receive a sizeable contribution from the hadronic decays of W to charm/strange. We also show the significance optimization for various $M_{1/2}$ values in $\geq 8$ jets $+ \geq 4$ b-jets $+ E_T$ final states. It is clear, in comparison to Fig. (1), that the stronger b-jet requirement allows for a softer $E_T$ cut, although this strategy is not necessarily a more favorable one.

In Fig. (4), we depict the density of hadronic W-bosons reconstructed with an invariant mass inside the 65 to 95 GeV window out of non-b tagged jets, after application of all the Category I cuts. In this limit, the signal is showing more W counts, although a trend toward under representing the expected prevalence of W’s has been observed. In the gluino pair production channel, at $M_{1/2} \sim 1$ TeV, two top/stop pairs are produced, and the stop will produce a top/neutralino with probability $p \sim 0.86$, or a bottom/chargino with probability $(1-p) \sim 0.14$, such that the expected density of top quarks is $2t \times (1-p)^2 + 3t \times 2p(1-p) + 4t \times p^3 \sim 3.7$, each of which should be associated with a final state W-boson. This has been validated in Monte Carlo at the generator level, although is apparently difficult to resolve at the detector level using elementary techniques. Several contributions to the W shortage are trivial, including exclusion of leptonic branching (the neutrino cannot be...
FIG. 2: Signal significance is evaluated as a function of the missing transverse energy $E_T$ cut for the like-sign dilepton (category II) and tri-lepton (category III) event topologies at a luminosity of 30 events per femtobarn. Two heavy-flavor tagged jets with $P_T > 80$ GeV are required, and the leading four jets (with or without a b-tag) must carry $P_T > (400, 200, 80, 80)$ GeV. For the like-sign dilepton categorization, two additional jets (for a total of 6) must carry $P_T > 40$ GeV.

FIG. 3: Distribution of $b$-jets retained after soft kinematic grooming in the background, the unified signal, and the isolated gluino pair production channel (left). The signal significance is evaluated as a function of the missing transverse energy $E_T$ for the Category I selections, adding a 4 $b$-jet requirement relative to the selection depicted in Fig. (1).

FIG. 4: Distribution of reconstructed hadronic $W$’s in the Category I $\geq 8$ jets with $\geq 2$ b-jets plus large $E_T$ final state for both signal and background.

decovolved from the large SUSY $E_T$ content), the likelihood of heavy flavor tagging for decays to charm/strange, limits on kinematic acceptance of jets, and smearing of the jet energy resolution. However, difficulty in clearly distinguishing the SUSY hadronic $W$ shape distribution from that of $t\bar{t}$ suggests that a more subtle agent is also at work. Specifically, it would seem to implicate the absorption of distinct partonic chains into combined fat jets, as is made more likely in a cascade environment with extremely high jet density, and also when decay products are highly boosted (collimated); it is likely that a jet substructure analysis [20, 21] would improve discrimination, but this will not be considered further here.
V. DI-TAU EVENT RESULTS AND ANALYSIS

Having established a strong third generation signal component in the prior section, we now turn attention to the question of stau/LSP coannihilation, via a focus on di-tau event production. Vector boson fusion (VBF) [22–24] is a key electroweak process capable of highlighting the light neutralino system at the four-vertex order. The VBF process is inherently suppressed, but may be emphasized by imposing an event topology that features highly boosted tagging jets with wide separation in pseudorapidity. Also, there are a large variety of strongly-interacting diagrams which may be considered VBF analogs that may likewise give rise to the described event topology, such as those exhibited in Fig. (5). Such diagrams cannot directly invoke the neutralino system, but may still probe the electroweak sector downstream, generating similar di-tau production via long-chain decay cascades, in association with a (potentially substantially) elevated net count of jets. By strength of the interaction and of numbers, such processes may residually swamp their electroweak analogs.

The signal significance metric $S/\sqrt{1+B}$ has been optimized as a function of the missing energy and transverse momenta of the two relevant jets for each of the two considered event topologies (boosted/conventional), with and without the application of light lepton and heavy flavor jet vetoes. This optimization, which is mildly luminosity and scale dependent, has been performed at an integrated luminosity of 30 events per fb, taking an $\mathcal{F}-SU(5)$ model benchmark with $M_{1/2} = 1000$ GeV and $\Delta M = 25$ GeV. Including a lepton veto hurts the significance ratio by about 30% for both event topologies. Including a $b$-jet veto hurts the boosted case by about 10%, but the conventional case by 20 or 30%. This latter difference may be traced in part to the fact that the boosted topology employs jets at large $\eta$ that cannot be tagged for heavy flavor, such that the veto is less harmful. Both results are consistent with the expectation that long cascades down the squark to gluino to stop to neutralino cascade may fork a large population of both light leptons and $b$-jets. The possibility of widening the jet pseudorapidity acceptance to $|\eta| < 5.0$ for the conventional event topology has also been examined, and found to be inconsequential with regards both to net signal efficiency and the optimization structure; this observation may be traced to the fact that the two leading jets in $P_T$ are not likely to exist at large pseudorapidity, as these conditions are anti-correlated.

For both scenarios, the most important cut is on missing energy, and values around 700 GeV work very well. In the conventional event topology, the signal significance at $L = 30/fb$ is moderately, though not greatly, enhanced by the addition of cuts on the leading jet transverse momenta $P_T$. This is because the background would already be well controlled by the $E_T$ cut alone and the “+1” regulator term is playing a deciding role in the denominator. Nevertheless signal is not much harmed by pushing the jet momenta substantially (a large $E_T$ will require large jet momenta) and background is thereby suppressed in a much more robust manner. This is supported by the Table II cut flow, presented in terms of the residual fb cross section. Specifically, the addition of a cut $P_T > (400, 200)$ reduces the background by about 150 times, but the signal by only about 2.5 times; this is prior to implementation of any $E_T$ cut whatsoever.

For the boosted event topology, increasing $P_T$ of the jets beyond the initial 20 GeV threshold is actually quite detrimental, almost immediately. Note in this case that the $E_T$ contribution may be balanced by more central non-tagged jets with much higher $P_T$. However, we are concerned that such soft jets are not realistic for tagging in a high pile-up environment, and instead adopt the more conservative bounds $P_T > (75, 50)$, sacrificing approximately two thirds of the signal in the process. The background drops by a similar, if slightly larger, factor close to five. Table II suggests that the hard jet cuts applied in the conventional event topology remove quite a bit less signal and quite a bit more background than the corresponding $\Delta \eta$ requirement imposed in the boosted topology; however, subsequent application of an identical
FIG. 6: Normalized signal and background distribution shapes are compared as a function of the missing transverse energy $E_T$ for the boosted and conventional event topologies.

TABLE II: Residual effective cross-section (fB) at various cut flow stages for the two described event topologies, as applied to the $M_{1/2} = 1000 \text{ GeV}$ $F$-SU(5) benchmark and the $t\bar{t}$ plus 2 Jets inclusive background at the LHC14. The production level cross sections and di-tau event selections are common to both scenarios. Energies and momenta are in GeV.

| Selection | $t\bar{t}$+Jets Signal |
|-----------|------------------------|
| Matched Production | 645,000 | 192 |
| 2 $\tau$’s, $P_T > (40, 20)$ | 2,230 | 10.1 |
| Conventional Event Topology | | |
| 2 Jets, $P_T > (400, 200)$ | 15 | 4.2 |
| $E_T > 700$ | 0.040 | 1.5 |
| Boosted Event Topology | | |
| 2 Jets, $\Delta \eta > 3.5$ & $P_T > (75, 50)$ | 88.1 | 0.78 |
| $E_T > 700$ | 0.005 | 0.21 |

$E_T > 700$ GeV cut on missing transverse energy devastates the boosted topology background component, while removing very little additional signal by comparison.

After all cuts, the signal and background expectations are both larger, by around 7 or 8 times, for the conventional event topology, but the signal to background ratio $S/B$ is essentially identical for the two event topologies. It should be emphasized that both scenarios, and especially the boosted event topology, present such stringent suppression of the $t\bar{t}$+jets background component, no more than about one event per 25 fB$^{-1}$ of data, that the statistical and systematic reliability of the analysis may become over stretched when extended to the detailed comparison of two extremely small values; nevertheless, the central message appears quite robust: backgrounds are extremely well controlled, and signal has a realistic chance to present itself.

Fig. (6) depicts the unity-normalized $t\bar{t}$+jets and $F$-SU(5) event densities as a function of missing transverse energy $E_T$ for both the boosted and conventional event topologies, with all other di-tau and jet cuts documented in Section I are imposed as a prerequisite.
into the extremely large missing energy domain. The boosted event topology does demonstrate a somewhat harder background suppression slope in the distribution tail. Moderate bin smoothing is applied here and in most subsequent plots.

Fig. (7) exhibits the integrated signal significance as a function of the missing transverse energy cut for the boosted and conventional event topologies. The metric \( S/\sqrt{1+B} \) is employed, comparing the count of signal events to the Gauss/Poisson fluctuation inherent to the background estimation, with the numeral 1 employed as a low-background regulator. A very mild scale dependence is observed, with lighter models favoring a bit less missing energy; this asymmetry is strongly accentuated when employing the alternative significance metric \( S/\sqrt{S+B} \), because lighter models generate a large quantity of signal events, which may exceed or retain parity with the background, such that significance scales with the signal square-root, disfavoring an over-strong cut. Optimization with regard \( S/\sqrt{S+B} \) is much less dependent upon the signal event scale, being driven instead primarily by background elimination, which becomes particularly pronounced in the vicinity of \( \mathbb{E}_T > 500 \sim 700 \) GeV. The apparent tendency of the boosted event topology to favor a lighter \( \mathbb{E}_T \) cut is attributable to the previously described reduction in net event counts associated with this scenario, such that the regulator term is dominant at moderate luminosities; nevertheless, the ratio \( S/B \) continues to benefit substantially from a harder cut.

![Event Selection Significance Ratio, \( \sqrt{s} = 14 \text{ TeV}, \mathcal{L} = 30 \text{ fb}^{-1} \)](image)

**Fig. 8:** The ratio of boosted to conventional signal to background ratios is displayed as a function of the gaugino scale parameter \( M_{1/2} \) for various \( \mathbb{E}_T \) cut thresholds.

Fig. (8) compares the boosted versus conventional signal to background ratios \( S/B \) as a function of the signal event scale for various common \( \mathbb{E}_T \) cuts. This ratio is observed to be comparable for both event topologies at a missing energy cut around 700 GeV, independent of the model scale.

Fig. (9) depicts the raw \( \mathcal{F}-SU(5) \) signal and \( t\bar{t} \) event counts for the boosted and conventional event topologies as a function of the gaugino scale parameter \( M_{1/2} \) for various values of the missing energy cut at an integrated luminosity of 300 events per femtobarn. A global suppression factor on the order of 10 is observed for application of the boosted event topology. A dramatic discrimination is observed in the relative impact of background (much stronger) and signal (much milder) suppression with increasing missing energy. For \( \mathbb{E}_T > 700 \) GeV, the \( \mathcal{F}-SU(5) \) signal counts exceed the \( t\bar{t} \) background counts for event scales across the viable model space, up to \( M_{1/2} = 1.5 \) TeV and beyond. A minimal signal count of more than 5 events is likewise maintained over this full scale range, even for the boosted topology. For a softer missing energy cut, e.g. \( \mathbb{E}_T > 300 \) GeV, the observed events are expected to become background dominated at a much lighter scale, as low as 1.0 TeV in this case.

**VI. THE NEUTRALINO-STAU SYSTEM**

The structure of the neutralino-stau mass hierarchy will be strongly imprinted upon the kinematic distribution of invariant masses \( M_{\tau\tau} \) for opposite-sign (OS) di-tau pairs \([11]\). After subtracting the density of like-sign (LS) pairs, which serve as a statistical estimator for the density and shape of unassociated opposite sign production, the invariant mass cutoff \( M_{\tau\tau}^{\text{max}} \) \([11]\) shown following may become visible, thereby providing a window into the nature of dark matter and its potential compatibility with thermal processes \([25, 26]\) that is largely orthogonal to other techniques.

\[
M_{\tau\tau}^{\text{max}} = M_{{\tilde{\chi}}^0_1} \sqrt{1 - \frac{M_{\tilde{\chi}_2}^2}{M_{\tilde{\chi}_1}^2}} \sqrt{1 - \frac{M_{\tilde{\chi}_1}^2}{M_{\tilde{\tau}_1}^2}}
\]

Fig. (10) depicts the opposite-sign (OS) minus like-sign (LS) di-tau invariant mass distribution shape in the conventional event topology after applying a missing energy cut of \( \mathbb{E}_T > 700 \) GeV. In the left-hand pane the universal gaugino mass \( M_{1/2} \) is varied as the stau-LSP mass gap \( \Delta M \equiv M_{\tilde{\tau}_1} - M_{\tilde{\chi}_1} \) is held fixed at 25 GeV. In the right-hand pane, the mass gap \( \Delta M \) is fluctuated while holding the gaugino mass \( M_{1/2} \) (approximately) constant. The distribution cutoff is visually extended in order to facilitate a numerical comparison with theoretical expectations, as in Table III. Fluctuation of this extension suggests a generic error on the order of 10 GeV in the limit of high statistics. Variation of the bin sizing and smoothing parameterization may induce a more or less comparably sized shift, to be combined in quadrature.

Table III examines the agreement between simulated data of a cascade-rich signal and the theoretical prediction from Eq. (1) for the di-tau invariant mass cutoff \( M_{\tau\tau}^{\text{max}} \). For a large mass gap \( \Delta M \approx 25 \) GeV, which implies a non-thermal mechanism for dilution of the Bino relic density, agreement is excellent. Ability to discern a well correlated cutoff persists for the background-
FIG. 9: Expected $F$-$SU(5)$ signal and $t\bar{t}$ background counts at a luminosity of 300 events per femtobarn are depicted for the boosted and conventional event topologies as a function of the gaugino scale parameter $M_{1/2}$ for various $E_T$ cut thresholds.

The tabulated elements, as well as Fig. (10), use oversampled data. In practice, the di-tau invariant mass peak is a difficult measurement requiring high luminosity. For the model samples under consideration, very little is resolvable at a luminosity of $30 \text{ fB}^{-1}$, but benchmarks in the vicinity of $M_{1/2} \sim 1 \text{ TeV}$ present a sufficient event count for peak resolution at 300 fB$^{-1}$. Reduction of the $E_T$ threshold substantially improves event yields, but makes discrimination from the background very difficult.

FIG. 10: The conventional event topology opposite-sign minus like-sign di-tau invariant mass $M_{\tau\tau}$ distribution shape is depicted for various gaugino mass $M_{1/2}$ scales and mass gaps $\Delta M \equiv M_{\tilde{\tau}_1} - M_{\tilde{\chi}_1}^{0}$.

A sharp decline is evident in the transverse momentum population of the softer tau, which is ostensibly associable with the phase space constricted secondary decay $\tilde{\tau}_1 \rightarrow \tilde{\chi}_1^0 + \tau$; this circumstance highlights the criticality of extending detection acceptance for hadronic tau candidates to as low a transverse momentum threshold as is technically possible, and at least to $P_T \sim 20 \text{ GeV}$. The transverse momentum distribution of the lead tau, which is expected to arise from the kinematically broad channel $\tilde{\chi}_2^0 \rightarrow \tilde{\tau}_1 + \tau$, is rather flat; a harder cut here, on the order that currently employed at $P_T > 40$, does not appear detrimental. The right-hand pane depicts the absolute distribution height of the soft tau element at a luminosity of 300 events per femtobarn for various values of $\Delta M$. As expected, this figure suggests that it is substantially more difficult (though not impossible) to effectively probe di-tau production in the case of a narrow stau-LSP mass gap; visibility of the daughter tau is more strongly dependent in this case upon a substantial upstream boosting of the parent stau.
stop the generation of a Higgs mass near 126 GeV. The light presence of additional vector like fields may contribute to 

$F_{\tilde{t}_{1}}$ have considered the No-Scale squark masses and sleptons are heavy. In particular, we 

mass is in the 1 to 2 TeV range, whereas the first two 

× in Fig. (10), where applicable. The “2 

tion. A dash is presented when the signal is highly unresolved 

The “With 

raps of $|\eta| < 5.0$ with an opposite hemisphere orientation ($\eta_1 \times \eta_2 < 0$), and an absolute separation in pseudorapidity of $|\eta_2 - \eta_1| > 3.5$. In the “Conventional Topol-

TABLE III: Comparison between theoretical prediction and Monte-Carlo observation of the opposite-sign minus like-sign di-tau invariant mass distribution cutoff for $\mathcal{F}$-SU(5) benchmarks with various gaugino mass $M_{1/2}$ and stau-LSP mass gap $\Delta M$ values. The “$M_{\tau\tau}^{\text{max}}$” value is computed by direct application of Eq. (1) to the associated spectrum. The “Visual” entry references the extrapolated linear descents plotted in Fig. (10), where applicable. The “2×Peak” value is established numerically, averaging over bin counts in the upper third of the corresponding histogram plots (after moderate bin smoothing to wash out noise peaks) and simply doubling the result. The “With $t\bar{t}$” column applies this same logic to the $\mathcal{F}$-SU(5) signal and $t\bar{t}$ + jets SM background combination. A dash is presented when the signal is highly unresolved relative to background. All entries are in units of GeV.

| $M_{1/2}$ | $\Delta M$ | $M_{\tau\tau}^{\text{max}}$ | Visual | 2×Peak | With $t\bar{t}$ |
|----------|----------|----------------|-------|--------|-------------|
| 850      | 25       | 153            | 155   | 155    | 154         |
| 1000     | 25       | 172            | 175   | 170    | 165         |
| 1200     | 25       | 193            | 195   | 196    | 178         |
| 1400     | 25       | 213            | 225   | 204    | -           |
| 821      | 15       | 123            | 135   | 135    | 139         |
| 1000     | 15       | 140            | 150   | 155    | 150         |
| 1400     | 16       | 172            | 175   | 183    | -           |
| 875      | 6        | 85             | 120   | 110    | 109         |
| 990      | 6        | 94             | 125   | 125    | 115         |
| 1400     | 6        | 111            | 155   | 145    | -           |

VII. DISCUSSION AND CONCLUSIONS

In this paper we address a scenario where the gluino mass is in the 1 to 2 TeV range, whereas the first two squark masses and sleptons are heavy. In particular, we have considered the No-Scale $\mathcal{F}$-SU(5) model, where the presence of additional vector like fields may contribute to the generation of a Higgs mass near 126 GeV. The light stop $\tilde{t}_1$ is lighter than the gluino in this model, which allows the gluino to decay on-shell into $\tilde{t}_1$. The lighter stop may then decay directly into a top plus lightest neutralino, or into a top plus (Wino-like) second lightest neutralino or bottom plus light chargino, which decay in turn to the lightest neutralino via stau. The dark matter content may be obtained thermally by stau and (Bino-like) light neutralino coannihilation in the case of a small $\Delta M \approx 6$ GeV. The final state of such a cascade contains multiple $b$-quarks, $W$’s, $\tau$ leptons and missing energy, and additional light flavor leptons, making $t\bar{t}$ the dominant background.

We first established the scenario from the multi-$b$, lepton and $W$’s, so that the existence of third generation can be surmised. We showed the signal can be differentiated from the leading background (where we considered $t\bar{t}$ + multijet production with a 1% $b$-fake rate) by demanding multiple jets, multiple $b$-quarks, and multiple $W$’s in the final state, in addition to very large missing transverse energy $E_T$. We calculated significances and showed that $M_{1/2}$ scales up to 1400 GeV ($M_\tilde{g} \sim 1900$ GeV) can be investigated at the 14 TeV LHC with a 30 fb$^{-1}$ luminosity, requiring 8 jets with 2 heavy flavor tags and $E_T > 700$ GeV. In the multi-lepton cases, we showed that a strategy requiring at least 6 jets with a like sign dilepton, or four jets with three leptons, can be utilized in conjunction with missing transverse energy to establish the model. We showed that $M_{1/2}$ up to around 1200 GeV ($M_\tilde{g} \sim 1600$ GeV) can be investigated in these channels at the 14 TeV LHC with a 30 fb$^{-1}$ luminosity; sensitivity may be extended to $M_{1/2} \sim 1300-1400$ GeV ($M_\tilde{g} \sim 1750-1900$ GeV) with a 300 fb$^{-1}$ luminosity.

We investigated the coannihilation region by considering two analysis routes, each of which require at least two $\tau$’s with $P_T > (40, 20)$ GeV in $|\eta| < 2.5$ and large missing energy. In the “Boosted Event Topology”, two tagging jets $j_{1,2}$ with $P_T > (75, 50)$ GeV were required in $|\eta| \leq 5.0$ with an opposite hemisphere orientation ($\eta_1 \times \eta_2 < 0$), and an absolute separation in pseudorapidity of $|\eta_2 - \eta_1| > 3.5$. In the “Conventional Topol-
ogy”, two leading jets $j_{1,2}$ in $|\eta| < 2.5$ carry very large transverse momenta $P_T > (400, 200)$ GeV. To retain the cascade signal, no vetoes on heavy flavor jets or light lepton flavors were enforced. We demonstrated the cut flow optimization that leads to these selections, and calculated the signal to background ratios $S/B$ for both routes. Both event topologies require a large $E_T$ cut around 700 GeV to reduce the background. After all cuts, the signal and background expectations are both larger, by around 7 or 8 times, for the conventional event topology, but the signal to background ratio $S/B$ is essentially identical for the two event topologies. With the optimized cuts, we investigated the small $\Delta M$ region and found that gaps of around 6 GeV can be probed for $M_{1/2} \sim 1000$ GeV ($M_3 \sim 1300$ GeV) at 300 fb$^{-1}$, although loss of the soft tau somewhat inhibits resolution of the invariant $M_{\tau\tau}^{\text{max}}$ mass in this case; the experimental prospects are improved for larger $\Delta M$ GeV (around 15-25 GeV).

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