Bioprocess Monitoring: A Moving Horizon
Estimation Experimental Application

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Abstract: Microbial fermentation processes are most often described by nonlinear time-varying dynamics, which require the implementation of nonlinear state estimators to infer unmeasured metabolites in the cultivation process. Among the various nonlinear available estimator strategies, the Moving Horizon Estimator (MHE) is an on-line optimization approach that easily allows to enforce hard constraints, an important feature that helps to avoid unfeasible concentrations. In this work we implemented an MHE by using experimental data from a fed-batch cultivation process of Corynebacterium glutamicum. Available real-time measurements of biomass and CO₂ formation were used to infer sugar concentrations by combining the available measurements with a simple Monod model. We found that the MHE was able to estimate all the three variables of interest, including the unmeasured sugar concentrations, during the entire fed-batch cultivation process. Moreover, we show that the estimates are accurate in comparison to the reference offline samples. This work demonstrates the benefits of MHE as a soft sensor that can monitor bioprocesses in real-time.

Keywords: Estimation and control in biological systems, Parameter and state estimation, Monitoring, Optimization

1. INTRODUCTION

Automation of biological processes is limited due to the unavailability of on-line measurement devices that can quantify variables of interest. The lack of sensors can be circumvented by implementing state estimators that enable to monitor the process in real-time. These state estimators are dependent on mathematical models (Rao, 2000) that represent the system in a simplified manner (i.e. Monod growth model). Different applications of nonlinear estimation techniques, including Extended Kalman Filters (EKF), Particle Filters (PF) and Unscented Kalman Filters (UKF), are available, as reported in Tuveri et al. (2021). However, those applications are all based on recursive Bayesian estimators, which approximate the posterior conditional probability density function (pdf) using measurements available at the current sampling instant.

Differently from them, optimization-based methods such as the Moving Horizon Estimator (MHE) use a moving window of past data (Robertson et al., 1996; Rawlings and Bakshi, 2006; Bavdekar et al., 2013; Ali et al., 2015). Most importantly, from a practical point of view and in contrast to the recursive Bayesian estimators, the MHE has:

- the ability to explicitly incorporate bound constraints in states and parameters;
- the possibility to easily handle multi-rate measurements;
- higher computational times (CPU times).

Indeed, MHE has the ability to explicitly incorporate physical constraints on states and parameters, and disturbances in the form of time-varying parameters can be added as extra degrees of freedom in the optimization (Robertson et al., 1996; Rao et al., 2005; Kühl et al., 2011). On the other hand, the EKFs or UKFs methods require strategies like clipping (Haseltine and Rawlings, 2005) or other optimization-based methods (Kolás et al., 2009; Tuveri et al., 2021) to avoid the estimation of negative concentrations. Additionally, time-varying parameters and disturbances have to be included as additional states, without the possibility to constrain them within predefined boundaries. Moreover, many real-time systems incorporate measurement devices with various sampling rates and times. For instance, whereas some absorbance probes sample every 10 seconds, sugar measurements by high performance liquid chromatography (HPLC) can be acquired every 30-60 minutes. The MHE, by considering a window of past measurements, is of interest in the case of such multi-rate measurements (Elsheikh et al., 2021), since it easily allows to place them in an adequate position within the time horizon. For those reasons, the MHE is a promising approach within bioprocesses.

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The continuously increasing interest in real-time optimal control has brought advances in nonlinear Model Predictive Control (MPC) algorithms and consequently in MHE methods (Findiesen et al., 2007). Indeed, even though fewer results are available in the literature about MHE, it can be seen as the dual of Model Predictive Control (MPC), since they both share moving horizon approach and dynamic optimization. The pioneering work of Kühl et al. (2011) in fact, transferred a fast real-time iteration approach developed for NMPC to MHE, contributing to its feasibility in real-time.

Although some in-silico applications within bioprocess monitoring are available (Raissi et al., 2005; Valipour and Ricardez-Sandoval, 2021; Bae et al., 2021; Elsheikh et al., 2021), the implementation of MHE combined with experimental data is almost non-existent and, to the best of our knowledge, it was only presented by Goffaux and Wouwer (2008). In Goffaux and Wouwer (2008) the authors present a robust receding horizon approach in the case of uncertain parameters, by selecting the worst parameter realization in a min-max optimization approach. To reduce the high computational demand, model linearization and monotonicity assumptions are required. Differently from the implementation in Goffaux and Wouwer (2008), our approach does not require linearisation or monotonicity of the model, parameter realisation is considered nominal and model uncertainty is a free variable minimized in the cost function. In order to demonstrate the benefits of MHE in bioprocess monitoring, we present an implementation of MHE using real experimental data of a fed-batch bacterial cultivation of Corynebacterium glutamicum, previously presented in Tuveri et al. (2021). The estimation performance obtained here by the MHE is accurate with respect to the off-line samples. Moreover, we demonstrate the incorporation of hard state constraints directly in the optimization formulation. This is an important advantage when the practitioner needs to avoid nonphysical estimates (i.e. negative concentrations).

2. INPUT AND OUTPUTS

The on-line output measurements were collected every 60 seconds and used by the estimator to measure biomass, volume and CO₂ respectively and to infer the unmeasured glucose composition. Signals from the absorbance probe were obtained in concentration units (0.05 - 4 CU) and then converted to g/L (cell dry weight, CDW) using a calibration curve as follows.

\[
\begin{align*}
\text{CU} & \geq 0.9: \\
\text{CDW}_{\text{CU}} & = 22.187 \cdot \text{CU} - 5.0991 \\
\text{CU} & < 0.9: \\
\text{CDW}_{\text{CU}} & = 11.124 \cdot \text{CU} + 0.66116
\end{align*}
\]

On-line CO₂ signals were obtained as measure of the composition in the outflow (0%-25%). The volume was calculated by integrating on-line the signals from the pumps, taking into account also the amount of volume taken for the off-line samples (8 mL/sample). The feeding profile is reported in Fig. 1. From here on we will define the two different phases as batch (from zero to the start of the feeding) and fed-batch or second batch (from the feeding on). More information about measurements and experimental setup are reported in Tuveri et al. (2021).

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3. SYSTEM MODEL

The dynamics are modelled by using simple Monod kinetics for growth on glucose as fed-batch process (Eq. 1), with the addition of linear cell death (Tuveri et al., 2021), where the state vector is defined by \( x(t) = [V(t), X(t), S(t), CO_2(t)] \) and the input vector by \( u = [F_{in}(t)] \). From here on we will drop the time-dependent notation for simplicity. The states \( V, X, S \) and \( CO_2 \) are respectively volume, biomass, substrate and carbon dioxide. \( F_{in} \) is the inflow of glucose with concentration \( S_{in} \) (100g/L), while \( q_{air} \) is the inflow of air (2 NL/min).

\[
\begin{align*}
\frac{dV}{dt} &= F_{in} \\
\frac{dX}{dt} &= -\frac{F_{in}}{V} X + \mu_{max} \frac{S}{X+S} X - k_{d} X \\
\frac{dS}{dt} &= \frac{F_{in}}{V} (S_{in} - S) - \mu_{max} \frac{S}{X+S} X \\
\frac{dCO_2}{dt} &= \mu_{max} \frac{S}{X+S} Y_{XCO_2} - q_{air} CO_2
\end{align*}
\]

The parameters are \( \mu_{max}, K_{S}, k_{d}, Y_{XS} \) and \( Y_{XCO_2} \) (Table 1). Those parameters were obtained using a nonlinear least-squares data fitting algorithm (lsqnonlin, Matlab) by a dedicated experiment (Tuveri et al., 2021).

| Parameter       | Description                     | Value      | Unit       | Std. Dev. |
|-----------------|---------------------------------|------------|------------|-----------|
| \( \mu_{max} \) | Maximum growth rate             | 0.19445    | h⁻¹        | 3.25 · 10⁻⁶ |
| \( K_{S} \)     | Monod growth constant           | 0.007      | g · L⁻¹    | 3.92 · 10⁻⁶ |
| \( k_{d} \)     | Death rate constant             | 0.006      | h⁻¹        | 4.49 · 10⁻⁶ |
| \( Y_{XS} \)    | S from X yield                  | 0.42042    | g · g⁻¹    | 3.58 · 10⁻⁶ |
| \( Y_{XCO_2} \) | CO₂ from X yield                | 0.54908    | g · g⁻¹    | 2.22 · 10⁻⁶ |

The covariance matrix for the parameters is calculated through the Fisher Information Matrix (FIM) as in Tuveri et al. (2021), where also structural identifiability and local observability for the system were positively assessed.

4. MOVING HORIZON ESTIMATION

The MHE estimates the states using past measurements at specific time points in the horizon \( T = T_N - T_L \), where \( T_N \) represents the current time and \( T_L \) the starting point of the horizon. The time horizon is then discretized according to the sampling rate.

The dynamics of the process (Eq. 1) are described by a set of ordinary differential equations (ODEs):

\[
\begin{align*}
\dot{x} &= f(x, u, w) \\
y &= h(x)
\end{align*}
\]
Fig. 2. The figure reports the MHE implementation, where the red dashed line represents the cost function (Eq. 6) and the blue dashed-dotted line its constraints. Measurements are given to both arrival and measurement error cost, while the measurement error covariance matrix is calculated at every iteration to weight for the model noise.

By discretizing it, we obtain:

\[ x_{k+1} = F(x_k, u_k, w_k) \]  
\[ y_k = h(x_k) \]  

where \( k \) denotes the sampling time \( t_k \) and \( w_k \) is a random variable.

The MHE problem (Kühl et al., 2011; Andersson et al., 2016) consists in finding the states and their noise obtained by solving the following constrained least-squares optimization problem:

\[
\min_{x_L, w_L} \left( \|\hat{x}_L - x_L\|^2_{P_L} + \sum_{i=1}^{N} \|y_i - h(x_i)\|^2_{V_i} + \sum_{i=L}^{N-1} \|w_i\|^2_{W_i} \right) \\
\text{s.t.} \quad x_{i+1} = F(x_i, u_i, w_i), \quad i = L, \ldots, N-1 \\
\quad x_i \geq x_{\text{min}}, \quad i = L, \ldots, N
\]  

(6)

The states \( x_i \) are constrained with \( x_{\text{min}} = [0, 0, 0, 0] \) as a lower bound, to avoid negative (unfeasible) concentrations. Following the work of Kühl et al. (2011), we define:

\[
P_L = P^{-1/2}, \quad V = R^{-1/2}, \quad W_k = Q_k^{-1/2}
\]  

(7)

and consider \( \|b\|^2_B = b^T B b \). The first term of the optimization (Eq. 6) is the arrival cost \( \Gamma \), which summarises the effect of measurements previous to the estimation horizon (up to \( t_L \)) and it is updated by single QR-factorization as in Kühl et al. (2011). The term \( \hat{x}_L \) (Eq. 6) represents the optimal estimate of \( x_L \).

The matrices \( P, R \) and \( Q_k \) (Eq. 7) are defined respectively as error, measurement noise and process noise covariances (Tuveri et al., 2021). Moreover, to take into account different process dynamics (Elsheikh et al., 2021), the process noise covariance \( Q_k \) is updated as in Tuveri et al. (2021). However since MHE, differently from EKF and UKF, takes into account several past measurements within the horizon \( T \), the corresponding process noise covariance matrix \( Q_k \) is used for each sampling time \( (k) \) within the horizon. Along the optimization horizon (30 min), states \((x_i)\) and process noise \((w_i)\) are optimized using the information from the mechanistic model and the outputs (1 min sampling rate). The implementation of the MHE is illustrated in Fig. 2. To transform the continuous time model, we apply three point Legendre collocation on finite elements. The Nonlinear Programming (NLP) problem was solved using IPOPT (Wächter and Biegler, 2006) embedded in CasADi (Andersson et al., 2019).

4.1 Arrival Cost Update

Several approaches can be used to calculate the arrival cost. An interesting review on different arrival cost schemes and how they can effect the stability of the MHE is presented in Elsheikh et al. (2021). Here we describe the QR-factorization approach employed in this work, which approximates the arrival cost to a quadratic term that is updated before each new horizon (Kühl et al., 2011). Although the QR-factorisation is a linearised technique as the EKF, it also holds all the numerical properties of the square-root Kalman Filter and the influence of past information can only grow within the limits of the process noise covariance \( Q_k \) (Kühl et al., 2011).

When we shift the horizon to a new start point at \( t_{L+1} \), the arrival cost would ideally be defined as:

\[
\Gamma(x_{L+1}) = \min_{x_L} \left( \|\hat{x}_L - x_L\|^2_{P_L} + \|y_L - h(x_L)\|^2_{V_L} + \|w_L\|^2_{W_L} \right) \\
\text{s.t.} \quad x_{L+1} = F(x_L, u_L, w_L)
\]  

(8)

However, since \( x_{L+1} \) is described by a nonlinear function, we do not have an analytical expression for the ideal arrival cost \( \Gamma \). For obtaining an explicit solution of Eq. 8, some approximations are carried out. First, we define the term \( x(t_{L+1}|x_L) \) as the solution of the ODEs (Eq. 4) in the interval from \( t \in [t_L, t_{L+1}] \) with \( x_L \) as initial value. By linearizing \( x(t_{L+1}|x_L) \) around the best available estimate \( x^* \), we obtain:

\[
x(t_{L+1}|x_L) \approx x(t_{L+1}|x^*) + A \cdot (x_L - x^*)
\]  

(9)

where \( \hat{x} := x(t_{L+1}|x^*) - Ax^* \) and matrix \( A \) is the derivative of \( x(t_{L+1}|x_L) \) with respect to \( x_L \):

\[
A = \frac{\partial F(x_L, u_L)}{\partial x_L} \bigg|_{x^*}
\]

Since in this case \( h(x_L) \) is linear, we can represent it as \( h(x_L) = H x_L \), where \( H \) is a selector matrix. This way it becomes possible to solve, analytically, Eq. 8 by rewriting it as:

\[
\min_{x_L} \left[ \frac{P_L(\hat{x}_L - x_L)}{V(y_L - H x_L)} + \frac{W_L(x_{L+1} - \hat{x} - A x_L)}{2} \right]^2
\]

(10)

and transforming it using QR-factorization:
The QR-factorization decomposes the matrix in the objective function (Eq. 10) into the product of an orthogonal matrix $Q$ and an upper triangular matrix $R$ (Elsheikh et al., 2021). From Eq. 11, we then obtain an equivalent problem of the form:

$$
\min_{x_L} \left\| \begin{pmatrix} \gamma_1 \\ \gamma_2 \\ \gamma_3 \end{pmatrix} + R_1 R_{12} x_L \right\|_2^2 \quad (12)
$$

The analytical solution of this problem (Eq. 12) results in the approximated quadratic expression for the arrival cost:

$$
\Gamma'(x_{L+1}) = \|\gamma_3\|^2 + \|\gamma_2 + R_2 x_{L+1}\|^2 \quad (13)
$$

Since the first term of Eq. 13 is given, the arrival cost updates are given by:

$$
\hat{x}_{L+1} = -R_2^{-1} \gamma_2, \quad P_{L+1} = R_2 \quad (14)
$$

4.2 Moving Horizon Estimation Setup

The filter receives the signals from the sensors every 60 seconds. The states and the input of the system are defined in Section 3, while the measured outputs are:

$$
y = [V CDW CO_2]^T \quad (15)
$$

The initial states are given by:

$$
x_0 = [1.5 1.2 20 0]^T
$$

with initial covariance matrix:

$$
P_0^+ = \begin{bmatrix}
2.09 \times 10^{-8} & 0 & 0 & 0 \\
0 & 1.10 \times 10^{-5} & 0 & 0 \\
0 & 0 & 1.09 \times 10^{-4} & 0 \\
0 & 2.17 \times 10^{-5} & 0 & 0
\end{bmatrix}
$$

and measurement noise covariance matrix $R$:

$$
R = \begin{bmatrix}
10^{-2} & 0 & 0 & 0 \\
0 & 10^{-1} & 0 & 0 \\
0 & 0 & 10^{-3} & 0 \\
0 & 0 & 0 & 10^{-3}
\end{bmatrix}
$$

The process noise covariance matrix $Q_k$ was tuned as in Tuveri et al. (2021), where $G_k$ is the Jacobian with respect to the model noise vector $w$:

$$
G_k = \frac{\partial f(x,u,w)}{\partial w}
$$

and $Q_k$ is obtained as:

$$
Q_k = G_k \cdot Q_w \cdot G_k^T \quad (16)
$$

With $Q_w$ defined as the covariance matrix of the noise $w$:

$$
Q_w = \text{diag} \left[ \sigma_{\mu_{\max}}^2, \sigma_d^2, \sigma_{S}^2, \sigma_{X_{CO_2}}^2, \sigma_{Y_{CO}}^2, \sigma_{X_{CDW}}^2, \sigma_{\mu_{\max}}^2, \sigma_{X_{CO_2}}^2 \right]
$$

The values of $Q_w$ are reported in Table 2. The values are kept equal to those reported in Tuveri et al. (2021), except the values for $\sigma_Y^2$ and $\sigma_{CO_2}^2$, which have been modified as they are considered tuning parameters. The additive noise terms on the states are added to prevent the process noise covariance $Q_k$ from being zero or indefinite whenever the substrate is depleted. To compensate for unmodelled dynamics, the values of $\sigma_Y^2$ and $\sigma_{X_{CO_2}}^2$ (Table 2) are increased, once the feeding phase is started and then kept constant thereafter.

Table 2. Variances ($\sigma_i^2$) of additive noise ($w_i$) in parameters and states. The parameters variance is obtained from Table 1. These values are kept constant until the second batch phase (Fed-batch values), when the values of $\sigma_{\mu_{\max}}^2$ and $\sigma_{Y_{X_{CO_2}}}^2$ are increased to compensate for the unmodelled dynamics.

| Parameter | Additive noise | Batch | Fed-batch |
|-----------|----------------|-------|-----------|
| $\mu_{\max}$ | $1.05 \times 10^{-11}$ | - | - |
| $K_S$ | $1.54 \times 10^{-11}$ | $3.38 \times 10^{-2}$ | - |
| $k_d$ | $2.02 \times 10^{-11}$ | - | - |
| $Y_{CDW}$ | $1.28 \times 10^{-11}$ | - | - |
| $Y_{X_{CO_2}}$ | $4.91 \times 10^{-12}$ | $4.91 \times 10^{-2}$ | - |
| $V$ | $1 \times 10^{-1}$ | - | - |
| $X$ | $1 \times 10^{-2}$ | - | - |
| $S$ | $1 \times 10^{-2}$ | - | - |
| $CO_2$ | $1 \times 10^{-1}$ | - | - |

5. RESULTS

In this section, the estimation results (Fig. 3) for the system presented in Sec. 3 obtained by the application of the MHE with incorporation of state constraints (Sec. 4) are presented. The parameters were tuned as was presented in Sec. 4.2, while the time horizon was 30 minutes. As was reported in Tuveri et al. (2021), intracellular metabolic changes (e.g. byproduct formation) during the batch and the feeding phases was not accounted for by the simple Monod model (because these changes are not entirely mapped), resulting in discrepancy between the model and the real dynamics. The results we obtained here (Fig. 3) are accurate with respect to the off-line measurements. The state estimator accurately follows the sugar consumption after adaptation of the tuning to the changes in metabolism due to high glucose feeding.

5.1 State Estimates

Using the MHE described in Sec. 4, we estimated with good accuracy the unmeasured glucose, following the changes in its concentrations also under high model mismatch (Fig. 3). It can be seen that the model predictions present a discrepancy compared to the off-line values. This is visible in both the first and the second (after feeding) batch. Despite these poor model predictions, the MHE improves the estimates by using the available information on the measurements.

Firstly, the off-line measurements of biomass are based on cell dry-weight, and are usually inaccurate due to manual sampling that exhibit high variance, e.g. at time $t = 8$ (Fig. 3a). The MHE, relying on the on-line OD high frequency measurements, estimated the biomass accurately compared to these off-line measurements, and at the same time corrected the biased biomass model prediction. Secondly, the consumption of the unmeasured sugars was well captured by the estimator, compared to the highly accurate sugar measurements (HPLC), even under high model-mismatch. Notably, the estimator could capture the change of sugar consumption rate after the feeding phase when we increased the parameters variance in the process noise covariance matrix $Q_k$. Thirdly, the model predictions for the $CO_2$ present the largest error. The $CO_2$ model predictions present a delay in the first
As it was presented previously (Elsheikh et al., 2021), due to steady-state offsets (Kühl et al., 2011). As it was presented previously (Elsheikh et al., 2021), due


can be achieved by the application of recursive Bayesian estimation in the optimization problem. Indeed, tuning needs to be done after the frequency of the output measurements is defined. In our case we selected a sampling rate of 60 seconds as in Tuveri et al. (2021) and a relatively short horizon (30 minutes). We found that a short sampling interval combined with a sufficient horizon length improves the performance of the MHE, consistent with what reported in Schei (2008), where the author states that it is desirable to choose short sampling times intervals and a long data window. This is also consistent with what was reported in Haseltine and Rawlings (2005). Here the authors state that for short time horizons there is the possibility that the data within the horizon can not overcome the biasing of the arrival cost approximation. The tuning of the MHE presents therefore a compromise between performance and computational requirement (Schei, 2008), since longer time horizons imply a bigger optimization problem. However, the time it took to solve our optimization problem was in the interval 0.05 to 1 seconds, well within the time update interval (60 seconds).

1) The tuning of the parameters $R$ and $Q_k$ weights differently the contribution of measurements and model information in the optimization problem. Indeed, tuning needs to be done after the frequency of the output measurements is defined. In our case we selected a sampling rate of 60 seconds as in Tuveri et al. (2021) and a relatively short horizon (30 minutes). We found that a short sampling interval combined with a sufficient horizon length improves the performance of the MHE, consistent with what reported in Schei (2008), where the author states that it is desirable to choose short sampling times intervals and a long data window. This is also consistent with what was reported in Haseltine and Rawlings (2005). Here the authors state that for short time horizons there is the possibility that the data within the horizon can not overcome the biasing of the arrival cost approximation. The tuning of the MHE presents therefore a compromise between performance and computational requirement (Schei, 2008), since longer time horizons imply a bigger optimization problem. However, the time it took to solve our optimization problem was in the interval 0.05 to 1 seconds, well within the time update interval (60 seconds).

2) Model mismatch can deteriorate the optimal solution, leading to steady-state offsets (Kühl et al., 2011). As it was presented previously (Elsheikh et al., 2021), due...
to the complexity of biological systems, model mismatch is often encountered in bioprocesses and it cannot be simply handled by a proper design of Qk. Moreover, as already presented in Tuveri et al. (2021), the system under consideration presents a high model mismatch due to sudden metabolic changes after an exposure of the bacteria to high glucose concentration following an oxygen deprivation period. There are two possible remedies to this problem. One is to consider the system with unknown non-Gaussian uncertainties (through the use of a Gaussian mixture model) as was recently presented in Valipour and Ricardez-Sandoval (2022). Indeed the authors show how their approach is effective in cases involving either unexpected process or measurement (e.g. sensor drift) noises. The other is to include model parameters as decision variables in the optimization problem (Bae et al., 2021). Interestingly, the optimization problem will adapt the model (by adapting the parameter values) during the metabolic change periods. The inclusion of parameters as decision variables in the optimization problem may not only reduce the time for the practitioner to manually tune the MHE by trial and error, but also reveal possible changes in metabolic behaviors, leading to more robust models. However, if this is not coupled with a proper choice of parameter selection to optimize, it may lead to an ill-conditioned problem with over-fitted parameters, as previously discussed in Bae et al. (2021). This will be however part of further investigations.

6. CONCLUSION

This work presents the implementation of an MHE for the estimation of biomass, glucose concentrations and CO₂ formation in a fed-batch cultivation process. We reported here the efficacy of the MHE as an alternative state estimator in bioprocesses, demonstrating its advantage under necessity of hard state constraints. We showed that although the results were accurate with respect to the off-line measurements, simple tuning could not fully compensate for unmodelled dynamics. As a future work, the MHE has the potential to serve as a powerful tool that can both estimate the states in real-time and allow an adaptive parameter estimation. This will enable the detection of changes in metabolic behaviours and, as a consequence, the basis for more robust model predictions.

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