Collisions between equal sized ice grain agglomerates

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ABSTRACT

Context. Following the recent insight in the material structure of comets, protoplanetesimals are assumed to have low densities and to be highly porous agglomerates. It is still unclear if planetesimals can be formed from these objects by collisional growth.

Aims. Therefore, it is important to study numerically the collisional outcome from low velocity impacts of equal sized porous agglomerates which are too large to be examined in a laboratory experiment.

Methods. We use the Lagrangian particle method Smooth Particle Hydrodynamics to solve the equations that describe the dynamics of elastic and plastic bodies. Additionally, to account for the influence of porosity, we follow a previous developed equation of state and certain relations between the material strength and the relative density.

Results. Collisional growth seems possible for rather low collision velocities and particular material strengths. The remnants of collisions with impact parameters that are larger than 50% of the radius of the colliding objects tend to rotate. For small impact parameters, the colliding objects are effectively slowed down without a prominent compaction of the porous structure, which probably increases the possibility for growth. The protoplanetesimals, however, do not stick together for the most part of the employed material strengths.

Conclusions. An important issue in subsequent studies has to be the influence of rotation to collisional growth. Moreover, for realistic simulations of protoplanetesimals it is crucial to know the correct material parameters in more detail.

Key words. planetary systems: formation – planetary systems: protoplanetary discs

1. Introduction

The initial growth of particles in a protoplanetary disc is accomplished by sticking collisions. All solid objects in a planetary system are believed to have been developed from collisions between small dust particles with initial sizes of about 0.1 micron (Greenberg 1982). These collisions result from Brownian motion, gas turbulence in the disc and gas drag (Weidenschilling 1977; Voelck et al. 1982; Weidenschilling & Cuzzi 1993). It has been shown that even protoplanetesimals of equal mass might have rather high relative velocities due to different shapes and hence different gas resistances (Benz 2000), depending on the orbital distance to the protostar. Experimental data for collisional growth of macroscopic agglomerates with sizes extending the dm-regime are rather scarce. The formation of such macroscopic bodies from smaller dust grains was studied in detail by Ossenkopf (1993) and the fractal growth was modelled by Dominik & Tielens (1997) and Kempf et al. (1999). Generally, the dust particles stick together due to van-der-Waals forces. This growth process leads to (highly) porous agglomerates, a fact that was experimentally confirmed by Wurm & Blum (1998). These macroscopic agglomerates do not stick together as easily as tiny dust grains which only interact by van-der-Waals forces. Instead, aggregate compaction, fragmentation and disruption become important above a specific kinetic energy of the collision. The agglomerates can break and can be dispersed which eventually prevents a fast growth process or even further growth at all. It is now generally assumed that decimetre sized porous agglomerates can form rather quickly in the presolar nebula and the protoplanetary accretion disc (Poppe et al. 2000; Wurm & Blum 1998; Blum & Wurm 2000; Weidenschilling 2000). The critical bottleneck in the formation process of planetesimals lies however in the size range from about several decimetre to objects whose interaction is mainly dominated by gravitation, that is 1 to 10 km planetesimals. First studies to the collisional growth of brittle planetesimals with material strength were performed by Benz & Asphaug (1994, 1995, 1999) and Benz (2000). Their results indicate that the weakest bodies during collisions are in the size range from metres to around 100 m. Caused by the stronger interaction with the gas, metre sized bodies experience higher collision velocities and are also rather fragile objects and easily disrupted.

A better understood problem is the formation of planets from planetesimals. The formation of planetary embryos or cores has been investigated in a series of publications (Stewart & Wetherill 1998; Wetherill & Stewart 1989, 1993) with the application of a statistical approach to describe the evolution of a swarm of planetesimals around the star. Later, by the use of modern supercomputers, direct n-body simulations of a large number of planetesimals became feasible and yielded similar results (Kokubo & Ida 2000, 2002). Once planetary cores have formed, the terrestrial planets grow through collisions between them (Chambers & Wetherill 1998; Agnor et al. 1999; Kominami & Ida 2002). In this size regime, the collisional outcome is by far dominated by gravitational interactions (e.g., Agnor & Asphaug 2004).

One alternative to avoid the bottleneck at the metre length scale of the formation process of planetesimals is gravitational instability of the dust layer in the midplane of the protoplanetary accretion disc. This idea was suggested independently by Safronov (1969) and Goldreich & Ward (1973). For the solar nebula, Goldreich & Ward (1973) found gravitational clumping of the dust which forms clumps with radii of 10 km at 1 AU.
within 1000 years after the onset of the vertical settling of dust. However, it is still unclear and strongly discussed in the community whether the dust in the midplane can become gravitational unstable, because Kelvin-Helmholtz instability and turbulent motion of dust particles in the disc lead to significant velocity dispersions which may prevent the collapse (Cuzzi et al. 1993; Weidenschilling 2000; Youdin & Shu 2002; Youdin & Chiang 2004).

Therefore, collisional growth of metre sized bodies has to be studied in greater detail in order to investigate the mechanisms of planetesimal formation. Laboratory experiments of collisions between water ice objects (e.g., Bridges et al. 1996) have been restricted to smaller sizes (up to several cm) and low impact velocities (up to several cm/s). Thus, experiments have concentrated on the dependence of sticking forces from the frost-coating of the surfaces (Supulver et al. 1997) or on measuring restitution coefficients (Supulver et al. 1995).

Since real collisions between objects of metre size are not feasible yet in laboratory experiments, one has to resort to numerical simulations. Here, we employ the numerical Lagrangian particle method Smooth Particle Hydrodynamics (SPH) which was first introduced by Lucy (1977) and Gingold & Monaghan (1977) for modelling compressible flows in astrophysical problems. The method was extended to solid state mechanics in the beginning of the nineties by Libersky & Petschek (1990) and improved extensively in the following years (Libersky et al. 1997, Randles & Libersky 1996, Libersky et al. 1997). After Benz (2000) has applied the method successfully to simulations of low velocity collisions between brittle objects, Sirono (2004) used experimentally measured data to parametrise the compressive strength curve of icy grain agglomerates and derived a modified Murnaghan equation of state (see sect. 2) to simulate porous objects.

Recent astronomical investigations such as the Deep Impact mission (Lisse et al. 2006) and observations of comets (e.g., Lamy et al. 2006) yield strong indications for rather low densities of comets (the values range from 0.1 g/cm$^3$ to several tenths of g/cm$^3$ and still have some larger errors). This matches well with the idea of collisional growth of fractal porous dust agglomerates to planetesimals.

In order to extend the investigations by Sirono (2004), we apply his model to simulate the collisions between equal sized (ice) agglomerates with different impact parameters and also explore the influence of material properties to the simulation outcome. The outline of the paper is as follows: In the next section, we will present the physical model, that is the basic equations and material properties we assume. In sect. 3 we will discuss some numerical issues and in sect. 4 the setup of our simulations. We present our results in sect. 5 and finally draw some conclusions.

2. Physical Model

2.1. Basic Equations

The system of partial differential equations that describe the dynamics of an elastic solid body is given by three equations. The first is the continuity equation

$$\frac{d\rho}{dt} + \rho \frac{\partial v^\alpha}{\partial x^\alpha} = 0,\quad (1)$$

where $\rho$ denotes the density and $v$ the velocity and where the Einstein summation rule is applied. Greek indices denote the spatial coordinates and run from 1 to 3. The second equation in the system accounts for the conservation of momentum

$$\frac{dv^\alpha}{dt} = \frac{1}{\rho} \frac{\partial \sigma^{\alpha\beta}}{\partial x^\beta},\quad (2)$$

The stress tensor $\sigma$ is given by the pressure $p$ and the deviatoric stress tensor $S^{\alpha\beta}$ according to

$$\sigma^{\alpha\beta} = -p\delta^{\alpha\beta} + S^{\alpha\beta}.\quad (3)$$

In contrast to fluid dynamics, this set of partial differential conservation equations is not sufficient to describe the elastic body, since the time evolution of the deviatoric stress tensor is not yet specified. The missing relations are called the constitutive equations which describe the rheology of the body and relate the kinematic states of the body to the dynamic states. The elastic behaviour of a solid body can be described by Hooke’s law, which reads in three dimensions

$$S^{\alpha\beta} \sim 2\mu \left( \varepsilon^{\alpha\beta} - \frac{1}{3} \delta^{\alpha\beta} \varepsilon^{\gamma\gamma} \right),\quad (4)$$

where $\mu$ is the shear modulus of the material, and $\varepsilon^{\alpha\beta}$ denotes the strain tensor which is given by

$$\varepsilon^{\alpha\beta} = \frac{1}{2} \left( \frac{\partial x^\alpha}{\partial x^\prime\beta} + \frac{\partial x^\beta}{\partial x^\prime\alpha} \right).\quad (5)$$

Here, the primed coordinates denote the coordinates of the deformed body.

The stress rate has to be defined in a way that obeys the principle of frame invariance. There are various possibilities to achieve this. We follow the usual approach which is used for SPH codes (Benz & Asphaug 1994) and adopt the Jaumann rate form, where the time evolution of the deviatoric stress tensor can be expressed as

$$\frac{dS^{\alpha\beta}}{dt} = 2\mu \left( \varepsilon^{\alpha\beta} - \frac{1}{3} \delta^{\alpha\beta} \varepsilon^{\gamma\gamma} \right) + S^{\gamma\alpha} R^{\beta\gamma} + S^{\beta\gamma} R^{\alpha\gamma},\quad (6)$$

where $R^{\alpha\beta}$ denotes the rotation rate tensor

$$R^{\alpha\beta} = \frac{1}{2} \left( \frac{\partial v^\alpha}{\partial x^\beta} - \frac{\partial v^\beta}{\partial x^\alpha} \right),\quad (7)$$

and $\varepsilon^{\alpha\beta}$ the strain rate tensor

$$\varepsilon^{\alpha\beta} = \frac{1}{2} \left( \frac{\partial v^\alpha}{\partial x^\alpha} + \frac{\partial v^\beta}{\partial x^\beta} \right).\quad (8)$$

The closure of this set of equations is provided by the equation of state that relates the pressure $p$ to the density of the agglomerate. Here, we focus on porous objects and follow the semi-empirical approach by Sirono (2004). We use an extension of the Murnaghan equation of state which accounts for the change of porosity and reads

$$p(\varrho) = \left\{ \begin{array}{ll} K(\varrho_0)(\varrho/\varrho_0 - 1), & \varrho < \varrho_c, \\
\Sigma(\varrho), & \varrho \geq \varrho_c. \end{array} \right.\quad (9)$$

The quantity $\varrho_0$ is the reference density of an agglomerate at no external stress while $\varrho_0$ is the initial density of the porous agglomerate. Note that $\varrho_0$ is in general different to the initial density $\varrho_0$ of the porous agglomerate after the start of the simulation. The critical density $\varrho_c$ is a function of the reference density $\varrho_0$ and determines the state where the pressure reaches the compressive strength limit $\Sigma(\varrho)$. As soon as the pressure decreases, the
behaviour of the agglomerate is again elastic but with a different
ebulk modulus $K(q'_0)$ since the reference density has changed.
The slope of $K(q'_0)$ has to be known either by experimental data
or theoretical considerations. The tensile strength of the material
is determined accordingly and limits the tension for negative
pressure.

The sound speed of the agglomerate is given by the bulk
modulus of the agglomerate and the reference density according
to the relation

$$c(q'_0) = \sqrt{K(q'_0)/\rho'_0}.$$  \hspace{1cm} (10)

For plastic states when the pressure exceeds the compressive
strength of the material the sound speed is calculated according to

$$c(q) = \sqrt{\frac{d\Sigma(q)}{\rho_0}}.$$  \hspace{1cm} (11)

Sirono (2004) additionally uses an empirical damage model
for porous agglomerates which is based on the damage model for
brittle materials developed for SPH by Benz & Asphaug (1994,
1995). However, this model is only applicable for the simulation
of brittle fracture in rocks (Grady & Kipp 1980), and our test simulations show that the application of the damage model
to porous agglomerates does not yield reliable results since the
model also includes compressive damage effects. Because of
these considerations, we do not include any damage model in our
calculations and only consider the fragmentation due to plastic
flow.

3. Numerical Issues

Smooth Particle Hydrodynamics (SPH) is perfectly suitable for
the simulation of brittle and plastic materials. The continuum
of the solid body is discretised into mass packages which are
called particles. The particles move like point masses according
to the Lagrangian form of the equation of motion. They carry
all physical properties like mass, momentum and energy of the
part of the solid body they represent. The particles interact by
kernel interpolation during the simulation to exchange momentum
and energy. For a complete description of the method and its
features and qualities, we refer to two comprehensive review
articles (Benz 1993, Monaghan 1992).

In standard SPH, the velocity derivatives in eqs. (7) and (8)
for the determination of the rotation rate and the strain rate tensor
for particle $i$ are usually calculated according to

$$\frac{\partial \nu^\alpha_i}{\partial x^\beta_i} = \sum_j m_j \frac{\rho_j}{\rho_i} (v^\alpha_j - v^\alpha_i) \frac{\partial W^{ij}}{\partial x^\beta_i},$$  \hspace{1cm} (14)

where the sum runs over all interaction partners $j$ of particle $i$, and $W^{ij}$ denotes the kernel for the particular interaction.

This approach, however, leads to erroneous results and does not
conserve angular momentum due to the discretisation error
by particle disorder in simulations of solid bodies. This error can
be avoided by constructing and applying a correction tensor $C^{\rho\beta}$
according to

$$\frac{\partial \nu^\alpha_i}{\partial x^\beta_i} = \sum_j m_j \frac{\rho_j}{\rho_i} (v^\alpha_j - v^\alpha_i) \sum_\gamma \frac{\partial W^{ij}}{\partial x^\gamma_i} C^{\rho\beta} \delta^\gamma_\beta,$$  \hspace{1cm} (15)

where the correction tensor $C^{\rho\beta}$ is the inverse of

$$\sum_j m_j \frac{\rho_j}{\rho_i} (v^\alpha_j - v^\alpha_i) \sum_\gamma \frac{\partial W^{ij}}{\partial x^\gamma_i} = \delta^\rho_\beta.$$  \hspace{1cm} (16)

By applying this correction tensor first order consistency can be
constructed where the errors due to particle disorder cancel out
and the conservation of angular momentum is ensured. This is
similar to an approach that Bonet & Lok (1999) proposed for the
conservation of angular momentum, where all spatial derivatives are
corrected according to eq. (15). We have found however that it is
sufficient to correct only the rotation rate and the strain rate
tensor.

We additionally use the standard SPH artificial viscosity
(Monaghan & Gingold 1983) with $\alpha = 1$. However, in order to
reduce the viscous energy dissipation, we follow Sirono’s approach
and apply the artificial viscosity only when the approaching
relative velocity of two particles is larger than the sound speed in contrast to the standard case where the artificial viscos-
city acts always on approaching particles.

Our SPH code parasph (Hipp & Rosenstiel 2004) has been
successfully tested with some numerical standard tests such as
the collision of perfectly elastic rings (Sweege 1993, Monaghan
2000) and the simulations of ductile and brittle rods under
tension (Benz & Asphaug 1994, Gray et al. 2001). Additionally,
the Sirono model in the extended code has been checked carefully
(Schäfer 2005) and we have successfully reproduced the impact
result for the standard setup in Sirono (2004).
4. Setup

All collisions have been simulated in three dimensions. The setup of our calculations includes the following parameters: Two spherical ice agglomerates with the initial density \( \rho_0 = 0.1 \text{ g/cm}^3 \) and identical radius \( r = 1 \text{ m} \) collide at either 20 m/s or 10 m/s. The initial density implies an initial porosity of 90\%.

The density dependencies of compressive and tensile strengths are chosen according to Sirono (2004) to \( \Sigma(\rho) = \Sigma_0(\rho/\rho_0)^b \) and \( T(\rho) = T_0(\rho/\rho_0)^a \), and the bulk modulus is given by \( K(\rho) = K_0(\rho/\rho_0)^c \). We always assume the shear modulus is given by \( \mu = K/2 \). For the first simulations with impact velocity 20 m/s we use the basic setup values from Sirono and set \( K_0 = 6 \times 10^5 \text{ Pa} \), \( \Sigma_0 = 600 \text{ Pa} \), and \( T_0 = 6 \times 10^3 \text{ Pa} \). These are the values for which Sirono (and we) find perfect sticking behaviour for a smaller sphere impacting into a larger object (with a radii ratio of 10:3) at speed 10 m/s. The temperature implicitly assumed in this set of parameters corresponds to very cold ice, which is consistent with the simulation results where large deformations but hardly any compression is found. Since the probability of a head-on collision is low, we have additionally varied the impact parameter of the collision, \( b = 0.2, 0.4, 0.8, 1.2 \text{ m} \). The results of these simulations are shown in sect. 5.1.

To study the importance of realistic material properties, we have then varied the tensile and compressive strength parameters \( T_0 \) and \( \Sigma_0 \) in some of the 10 m/s head-on collisions and present these calculations in sect. 5.2. Reducing the impact velocity also allows to compare the influence of the latter.

5. Results

5.1. Varying impact parameter

As noted above, in this section we focus on the material parameters for which Sirono (2004) found perfect sticking for a collision with a projectile 3:10 smaller in radius than the target. Figs. 1-5 present the simulation outcome for five different impact parameters. The plots show the SPH particles with a colour-scale code for the density of each particle. As we are mainly interested in the final configuration of the impact after compression has ceased, the density is acting as a measure for any permanent compaction that may have taken place during the compression phase.

Each sphere consists of approximately 11 500 SPH particles which are initially placed on a tetrahedral grid to maximise the number of adjacent and interacting particles and thus to increase the resolution. The figures show the surface of the resulting objects after impact, as the particles are plotted opaque.

The first simulation (see fig. 1) demonstrates the behaviour during a head-on collision with impact parameter \( b = 0 \). In contrast to the sticking mechanism found by Sirono (2004) with the same material properties but different sizes, the two spheres do not penetrate. In fact, they undergo a large change in shape and the two spheres end up as flattened discs. Almost the entire kinetic energy of the impact is dissipated by plastic deformation, and ultimately the two discs are at rest in the barycentric system. Only some particles which were tossed outwards during the compression phase fly away at constant speed.

The picture slightly changes for the simulation with \( b = 0.2 \text{ m} \) (see fig. 2). As in the head-on collision, the two spheres transform into flattened discs with some separate particles floating away. In contrast to the head-on collision, the remnants of the spheres rotate slowly.

First major difference arises at the step from \( b = 0.2 \text{ m} \) to \( b = 0.4 \text{ m} \) (see fig. 3), when the spheres break up. Again, the spheres undergo a large plastic deformation during the compression phase and become strongly prolate. A small piece is quarried out of each object after the compression due to the strong tensile forces caused by rotation.

Even more smaller fragments emerge after the collision with impact parameter \( b = 0.8 \text{ m} \) (see fig. 4). However, now the largest remnants of the collision consist of two rotating half-spheres. The density of the half-spheres is exactly the density of the initial spheres. Essentially they have not been compacted.

The situation hardly changes for \( b = 1.2 \text{ m} \) (see fig. 5). Again, smaller fragments are tossed out from the spheres after the compaction phase. The two formed larger remnants have again the shape of half-spheres, slightly larger than in the simulation with \( b = 0.8 \text{ m} \). The rotation rate and the velocity of the half-spheres is larger than for smaller impact parameters.

\footnote{As in the printed version of this paper the figures have to be displayed in grey-scale, we refer the reader to the online-version for colour figures.}
The strong influence of the impact parameter $b$ on the change in kinetic energy with the respect to the centre of mass is shown in fig. 6, where the ratio $Q$ of the kinetic energy at the end of the simulation to the initial kinetic energy is plotted. In the case of the head-on collision, more than 99.7% of the initial kinetic energy has been dissipated during the plastic deformation phase.

The remnants (except for a few particles) of the collision are at rest. Although they do not stick together, their relative velocity is zero. Even for impact parameters $b = 0.2$ and $0.4$ m, the kinetic energy at the end is less than 10% of the initial kinetic energy. The spheres are effectively slowed down during the compression phase.

The situation changes for higher impact parameters. For $b = 0.8$ m less than 80% and for $b = 1.2$ m even less than 50% of the initial kinetic energy is lost due to the compression.

Interestingly, the density of the remnants after the simulation is basically the initial density for all studied impact parameters. Only some small areas in the contact region have a slightly higher density. The density in the interior of the objects does not differ distinctly from the density at the surfaces. Therefore only the latter is shown in the figures.

5.2. Varying material strength

Although Sirono (2004) has investigated the influence of the material strength on the collisional outcome, we have additionally studied the behaviour for our equal-sized agglomerates.

All simulations with varying material strengths are head-on collisions with a relative velocity of 10 m/s. The basic relations...
for the compressive and tensile strengths and the bulk modulus remain unchanged, only the coefficients $\Sigma_0$ and $T_0$ are varied.

The figures 7-10 show colour-scaled density plots of the particles at the end of each simulation. For the first of these simulations, we have used the same material properties as in sect. 5.1, $\Sigma_0 = 600 \text{ Pa}$ and $T_0 = 6 \times 10^3 \text{ Pa}$ (see fig. 7). Because the collision velocity is half the collision velocity from the simulation shown in fig. 1, the spheres do not experience the same drastic plastic deformation. In fact, they end up as two solid half spheres and no particles were pulled out of the spheres during the compression phase. Their relative velocity at the end are again vanishing. This picture changes drastically if the tensile strength coefficient $T_0$ is reduced by one order of magnitude to $600 \text{ Pa}$ (see fig. 8). Now the tensile forces are too weak to sustain the bodies during the contact phase. In the end, the two spheres stick together into a disc-like structure and many particles are ejected due to the fragmentation by plastic flow. Interestingly, if the compressive strength is augmented even further to $6 \times 10^4 \text{ Pa}$ (see fig. 9), the bodies become too elastic and do not stick.

The basic structure of the spheres is conserved, only in the impact contact region, the spheres are flattened. The objects rather bounce off from each other, losing some particles. A nearly fully elastic rebound of the spheres happens for $\Sigma_0 = T_0 = 6 \times 10^4 \text{ Pa}$ (see fig. 11).

Again, the density of the spheres does not change significantly. Although their shapes change notably, they are not compacted effectively and their porosities stay mainly unchanged.

6. Discussion

The simulations presented in this work extend the investigation of Sirono (2004) to collisions between equal-sized agglomerates. Sirono’s main results regarding collisional growth and stickiness conditions can be summarised in the following way: Porous agglomerates can grow by collisions if the tensile strength is larger than the compressive strength, the shear strength is larger than the compressive strength and the Mach number is lower than 0.04 for oblique impacts, which corresponds in our simulations to a maximum collision velocity of 3.1 m/s. Additionally, a damage restoration effect has to be included, otherwise the agglomerates are totally fragmented. Since we do not use the damage model from Sirono, there is no need for a restoration effect.
Our new simulations with varying impact parameters indicate that collisions with $b < 0.4$ lead to drastic shape deformations, the spheres finally form disc-like structures. Clearly, disc-like structures will withstand subsequent collisions even worse if the impact is perpendicular to the disc plane. On the other hand most (for head-on collisions nearly all) of the kinetic energy is lost, which possibly leads to lower collision velocities for following encounters, thus favouring growth in subsequent collisions. The change in shape is lower for larger impact parameters $b > 0.4$, where less kinetic energy is lost. However, agglomerates emerging from oblique collisions tend to rotate and eventually break if the tensile strength is not large enough. Then, plastic flow leads to fragmentation of agglomerates after the compression phase. However, the tensile strength of a realistic porous protoplanetesimal might be higher in orders of magnitude than assumed here.

One of the most striking simulation results is the missing compaction of the agglomerates. Although they are rather porous objects (with 90% porosity), their porosity does not change significantly during the impact. It is unclear, how the porosity in the agglomerates may be reduced and the bodies compacted. Probably, lower collision velocities and differing sizes of the colliding agglomerates lead to the incorporation of smaller bodies into large agglomerates, and a slight decrease of porosity. However, the velocity distribution of protoplanetesimals in the solar nebula at the Earth’s orbital distance ranges up to several tens of m/s. One collision at such a high speed might destroy previous growth entirely.

The varying material strength parameters which were investigated in the second series of simulations show the strong influence of the material properties on the collisional outcome. For the applied values we find the whole spectrum: sticking, no sticking but vanishing relative velocity, complete fragmentation, and elastic rebound. In contrast to Sirono’s results, the only simulation that results in sticking uses $\Sigma_d = T_0 > Y_0$. Moreover, since the Mach number of our simulations is 0.13 for the 10 m/s collisions and 0.26 for the 20 m/s collisions respectively, all simulations should lead to fragmentation according to Sirono’s results.

Altogether the results indicate that to prevent fragmentation, a large compressive strength may compensate a low tensile strength (see fig. 10) and vice versa (see fig. 7).

7. Conclusion

As long as we do not have more insight into realistic material properties of protoplanetesimals, it is cumbersome to give any accurate description about the formation of planetesimals by collisional growth. However, we have demonstrated that specific strength parameters can lead to growth and encourage the formation of planetesimals even for collisions of equal sized objects, where previous investigations have found destruction. Currently, it is a major topic to establish realistic material parameters of protoplanetesimals in laboratory experiments. Recent experimental data [Blum & Schräpler 2004; Wurm et al. 2005a,b] provide first insight in the properties of porous dust agglomerates which differ significantly from the properties applied in this study and may lead to further perception. We plan to recalibrate the existing SPH-model which was applied in this paper by performing comparison calculations of impact experiments. Thus, a realistic model for elastic and plastic behaviour of porous agglomerates will be developed.

Additionally, our studies indicate that rotation is an important unexplored effect which needs to be probed in more detail. A subsequent study will therefore focus on the collisions between rotating porous protoplanetesimals.

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