Strong Nonadditivity as a Key Structure–Activity Relationship Feature: Distinguishing Structural Changes from Assay Artifacts

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Supporting Information

ABSTRACT: Nonadditivity in protein—ligand affinity data represents highly instructive structure–activity relationship (SAR) features that indicate structural changes and have the potential to guide rational drug design. At the same time, nonadditivity is a challenge for both basic SAR analysis as well as many ligand-based data analysis techniques such as Free-Wilson Analysis and Matched Molecular Pair analysis, since linear substituent contribution models inherently assume additivity and thus do not work in such cases. While structural causes for nonadditivity have been analyzed anecdotally, no systematic approaches to interpret and use nonadditivity prospectively have been developed yet. In this contribution, we lay the statistical framework for systematic analysis of nonadditivity in a SAR series. First, we develop a general metric to quantify nonadditivity. Then, we demonstrate the non-negligible impact of experimental uncertainty that creates apparent nonadditivity, and we introduce techniques to handle experimental uncertainty. Finally, we analyze public SAR data sets for strong nonadditivity and use recourse to the original publications and available X-ray structures to find structural explanations for the nonadditivity observed. We find that all cases of strong nonadditivity (∆ΔpKi and ∆ΔpIC50 > 2.0 log units) with sufficient structural information to generate reasonable hypothesis involve changes in binding mode. With the appropriate statistical basis, nonadditivity analysis offers a variety of new attempts for various areas in computer-aided drug design, including the validation of scoring functions and free energy perturbation approaches, binding pocket classification, and novel features in SAR analysis tools.

INTRODUCTION

Nonadditivity in protein—ligand binding is the basic factor that complicates structure–activity relationship (SAR) analysis: If the effect of adding a specific substituent to position A depends on the presence of another substituent in position B, no simple SAR picture à la “the scaffold series requires a small hydrophobic substituent in position A” or “the scaffold series requires a donor in position B” can be drawn. Nonadditivity indicates that behind the simple 2D chemical drawings, there are more complex physical processes going on and molecular interaction types change due to the combination of substituents. It is tempting to interpret nonadditivity as some kind of interaction between the substituents, but which interaction types should we expect at which level of nonadditivity? Here we attempt to shed light on the chemical features that lead to nonadditivity and lay the statistical basis to systematically analyze nonadditivity in drug design.

So far, nonadditivity in drug design has only been analyzed anecdotally and for single SAR series. A lot of work on nonadditivity has come from the Klebe group at the University of Marburg: Klebe and co-workers have analyzed a series of thrombin inhibitors and found that a loss in residual mobility,
strongly beneficial effect on protein–ligand binding. Many of these cases can be rationalized with the methyl introducing a different conformation, which would lead to nonadditive effects for other substituents that upon introduction of the methyl point into different parts of the binding pocket. These examples indicate that nonadditivity should not be considered as a problem but rather as a key SAR feature that indicates changes in binding modes.

In biochemistry, additivity and cooperativity of ligand binding has been a long-standing topic.9–13 Cooperativity has extensively been studied for oxygen binding to hemoglobin, where the oxygen affinity of the four subunits depends on how many other subunits already have oxygen bound.14,15 In this system, there is a clear cooperative effect, since the hemoglobin ligands always bind to the same binding site in different subunits. In physical organic chemistry, nonadditivity as measured in chemical double mutant cycles has been used to quantify the interaction energy between functional groups.16–19 Key for the analysis of these experiments is that the relative orientation of the complexes remains the same for all complexes—only then differences in interaction energies can directly be interpreted as functional group interaction energies. For drug–protein complexes, this is rarely the case due to the complexity of the underlying macromolecular binding events.

Nonadditivity also poses problems to most automated SAR analysis approaches. Many approaches require additivity of functional group contributions: classic linear QSAR models, standard Matched Molecular Pair Analysis and Free-Wilson analysis approaches. Many approaches require additivity of functional group contributions: classic linear QSAR models, standard Matched Molecular Pair Analysis and Free-Wilson analysis approaches. These models may work on the subsets with much improved accuracy. However, achieving this goal requires an understanding of the factors that cause nonadditivity in structure–activity relationships.

In recent work, Klebe et al. have shown that flat SARs can contain strong nonadditivity in terms of the enthalpy–entropy profile.20,21 In this work, we focus on analyzing nonadditivity in the free energy of binding, since this still is the major criterion for ligand optimization. Further, understanding enthalpy–entropy effects is certainly more complex than understanding the free energy of binding, since small changes in protein conformations can have large effects on the enthalpy–entropy profile.22 Once the factors that drive entropy-enthalpy profiles are better understood, nonadditivity analysis can be extended to the entropy-enthalpy domain of molecular interactions.

The remaining paper is structured in three parts: First, we define the basics for the quantification of nonadditivity. Second, we theoretically analyze the impact of experimental uncertainty on the distribution of calculated nonadditivity on a whole SAR table and compare our findings to nonadditivity distributions observed in real data sets. This allows us to develop a tool to distinguish between real nonadditivity and artifacts from assay noise. Third, we analyze all well-characterized cases with strong nonadditivity, which are very unlikely to be caused by experimental uncertainty, on a structural level to develop an overview of the molecular origins of extreme nonadditivity.

## METHODS

### Assembly of Double Transformation Cycles

Nonadditivity can be determined from chemical double transformation cycles.17 Double transformation cycles consist of four molecules with the same scaffold and known binding affinity that are linked by two chemical transformations. A double transformation cycle is schematically shown in Figure 1.

If the effect of adding substituent B depends on the presence or absence of substituent A, the transformations are nonadditive. Nonadditivity can be quantified as the difference in change of affinity between adding substituent A in the presence and in the absence of substituent B. Since this is a closed thermodynamic cycle, it is the same as the difference of the change of affinity between adding substituent B in the presence and in the absence of substituent A. Mathematically, nonadditivity can be calculated as a single number according to

\[
\text{nonadditivity} = \Delta \Delta p\text{Activity} = \Delta p\text{Act}_{14} - \Delta p\text{Act}_{12} = \Delta p\text{Act}_{23} - \Delta p\text{Act}_{12}
\]

The sign of the nonadditivity will depend on the ordering of the molecules within the cycle. If the two transformations involve adding two substituents to a position where there has been a hydrogen before, the compound with the fewest heavy atoms can be placed in the upper left corner and the compound with the most heavy atoms in the lower right corner. Then, the sign of the calculated nonadditivity can be interpreted as positive or negative cooperativity. However, in general there will be a lot of transformations where one functional group is either moved or exchanged for another one. In such cases, there is no natural ordering within the cycles any more and the sign cannot be interpreted in terms of positive or negative cooperativity.

We implemented a python program that extracts all nonadditivity cycles from a given data set. It is based on

![Figure 1. Schematic view of a double transformation cycle. Each cycle consists of four molecules with a common scaffold and all possible combinations of changing two substituents A and B (here indicated in orange and blue). The activities of the individual compounds are pAct\_\_i; the activity differences between two compounds are denoted by ΔpAct\_\text{norm}.

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484
python and the RDKit implementation of the Matched Molecular Pair Analysis (MMPA) Algorithm by Hussain and Rea.6 The matched pairs are the basis for the cycles where matched pair transformation connects two similar molecules. The Hussain and Rea MMPA implementation also yields transformations where linkers are exchanged. For further analysis after creating the full set of cycles, we removed all linker exchanges where the number of heavy atoms between the connecting atoms changes, since those are very likely to change the ligand geometry and nonadditivity should be expected for those cases. Note that cycles are assembled in a way that all four compounds have been measured in the same assay and have the same activity type so that $p_{\text{Act} \text{meas}}$ is composed of a true value $p_{\text{Act} \text{true}}$ and some experimental uncertainty $\epsilon_{\text{uncertainty}}$.

\[
\begin{align*}
\text{nonadditivity} &= \Delta p_{\text{Act}_{3}} - \Delta p_{\text{Act}_{12}} \\
&= p_{\text{Act}_{3} \text{true}} + \epsilon_{\text{uncertainty},3} - p_{\text{Act}_{12} \text{true}} - \epsilon_{\text{uncertainty},1} \\
&= p_{\text{Act}_{3} \text{true}} + p_{\text{Act}_{12} \text{true}} + \epsilon_{\text{uncertainty},2} - \epsilon_{\text{uncertainty},2}
\end{align*}
\]

Assuming that the experimental uncertainty of each individual measurement is drawn from the same normal distribution

\[
\epsilon_{\text{uncertainty}} \sim N(\mu = 0, \sigma = 3\sigma_{\text{uncertainty}})
\]

the standard deviation of the contribution of the experimental uncertainties to the observed nonaddivities can be calculated using the addition rule for standard deviations (covariances need not be considered since the covariance between two random vectors is zero):

\[
\begin{align*}
\sigma_{\text{uncertainty–nonadditivity}} &= \sqrt{\sigma_{\text{uncertainty},1}^2 + \sigma_{\text{uncertainty},2}^2 + \sigma_{\text{uncertainty},3}^2 + \sigma_{\text{uncertainty},4}^2} \\
&= \sqrt{4\sigma_{\text{uncertainty},2}^2 + \sigma_{\text{uncertainty},1}^2 + \sigma_{\text{uncertainty},3}^2 + \sigma_{\text{uncertainty},4}^2} \\
&= \sqrt{4\sigma_{\text{uncertainty},2}^2}
\end{align*}
\]

The contribution of experimental uncertainty to the observed nonaddivities is thus twice as large as the contribution of the experimental uncertainty to the individually measured values. In order to quantitatively model the effect of experimental uncertainty, we need an estimate of the uncertainty of the individual activity values. Kramer et al. have previously estimated the experimental uncertainty of heterogeneous public $pK_{\ell}$ data to be 0.54 log units.31 For homogeneous $pK_{\ell}$ and $pIC_{50}$ data, the uncertainty has been estimated to be around 0.2 log units.32 These are rather general estimates that should be replaced by more assay-specific data if available. Since better estimates are not available for most of the published data, we will use an estimated experimental uncertainty of 0.2 log units in the remaining analysis. If future studies show that the real experimental uncertainty is higher or lower, the calculations done here can easily be adapted.

We implemented a program that automatically extracts all nonadditivity cycles from a given SAR table or all ligand data for a specific target from CHEMBL. This program can be found in the Supporting Information.

Structural figures have been produced using maestro,38 and statistical plots have been created with R.39

### RESULTS

We extracted nonadditivity cycles for all CHEMBL targets with more than 1000 ligands that either have a $K_{\ell}$ or $IC_{50}$ value assigned. Overall, this yielded 44 519 nonadditivity cycles for 157 targets. For 14 607 of those cycles, there is at least one co-crystal structure available where the ligand has a similarity of 0.6 or greater to one of the compounds in the cycle. The number of nonadditivity cycles per target differs greatly, which reflects the number of compounds, and the number of SAR analogs that have been tested experimentally.

Distribution of Nonadditivity within the CHEMBL SAR Data. With an experimental uncertainty of 0.2 log units, the nonadditivity distribution due to noise on a full SAR data sets is expected to look like a Gaussian distribution with a mean of zero and a standard deviation of 0.4 log units. Figure 2 shows the theoretical nonadditivity distribution due to experimental uncertainty, and the real distribution of nonaddivities of all double transformation cycles for cytochrome P450 3A4 (CYP3A4, 63 cycles), human ether-a-go-go related gene product (hERG, 132 cycles), and Factor Xa (hFXa, 24 cycles) $pK_{\ell}$ data, extracted from CHEMBL18.

Figure 2 shows that most of the observed nonadditivity of the CYP3A4, hERG, and Factor Xa data sets can be explained with experimental uncertainty. In particular, the major peak in the middle of all three distributions can fully be explained by experimental uncertainty. While there might be some real nonadditivity in the cycles making up the majority of the data, it is impossible to identify any nonadditivity due to the experimental uncertainty. Only in the tails of the distributions...
that deviate from the normal distribution, in particular for Factor Xa, there are some cycles that cannot be explained by experimental uncertainty.

As a nonadditivity analysis tool, the deviation from normality can be visualized with normal probability plots. In normal probability plots, the observed quantile distribution is compared to an expected quantile distribution from a normal distribution. Deviations from a normal distribution can be seen as points deviating from the diagonal line. Figure 3 shows normal probability plots for the observed nonadditivities of the CYP3A4 data and the Factor Xa data.

Figure 3 shows that while CYP3A4 nonadditivities fit quite well to a single normal distribution, stronger Factor Xa nonadditivities can clearly not be explained with a single normal distribution due to experimental uncertainty. Therefore, while there is statistical evidence for biochemical phenomena that lead to nonadditivity for Factor Xa data, there is little evidence for such phenomena in CYP3A4 Ki data, despite the apparent nonadditivity of some cycles at the extremes of the distribution.

Different targets show very different nonadditivity profiles. In Figure 4, we compare the nonadditivity profiles for MAO-B (1372 cycles), hERG, and MMP-2 (1538 cycles) data extracted from CHEMBL18.

Figure 4 shows that the nonadditivity profiles can differ a lot for different data sets. For MMP2, there is a very narrow central peak indicating perfect additivity of substituent contributions and many individual nonadditivities that do not follow a central Gaussian. On the other side, MAO-B nonadditivities follow a single very broad Gaussian. The differences in the central peaks may be explained by different experimental uncertainties due to different assay qualities. However, there might also be biochemical factors rooted in the nature of the different binding sites that lead to very different nonadditivity profiles. This raises the question how nonadditivity relates to promiscuity and the structure and dynamics of binding sites. Comparing the nature of the binding sites to the respective nonadditivity profiles may yield very important insights into binding site classes. Nonadditivity analysis provides the means to quantify those differences, which is not possible otherwise.
Structure-Based Analysis of Strong Nonadditivity. In the previous part, we have shown that only a small fraction of the nonadditivities should actually be interpreted, since we are not able to distinguish small nonadditivities from assay noise. In order to get an idea about the structural factors that cause nonadditivity, we decided to systematically inspect those double transformation cycles with strong nonadditivity and structural information. From the above prepared data set, we retained all cycles with a nonadditivity > 2.0 log units and at least one cocrystal structure with a ligand similarity TC > 0.95. We found that for our purpose of understanding structural factors that lead to nonadditivity, structural interpretation is hardly possible if the highest similarity is below 0.95. The threshold of 2.0 log units is motivated by the 5σ rule, which is often used in physics as threshold for real discoveries (for example in the first announcement of the discovery of the Higgs Boson): if the experimental uncertainty of the individual measurement is 0.2 log units, σ of the nonadditivity distribution due to noise is 0.4 log units, and 2.0 log units is 5σ. The probability of observing a 5σ event by chance is roughly one in 3.5 million.

Overall, this process yielded 79 cycles for 24 distinct scaffold series on 20 different targets. Upon further inspection, we removed nine different scaffold series for four different reasons: Four of those series contained covalently binding ligands. We decided not to interpret the binding data for those ligands, since we cannot be sure that the reported IC₅₀ data really represented equilibrium values. Three series were discarded due to errors in the data, including one of the covalently binding series. Two scaffold series were discarded since despite a TC of 0.95, the cocrystallized ligand was too different in the regions of interest to start generating any reasonable structural hypothesis. Finally, one series was discarded because of a discrepancy between the ligand published in the original publication and the model deposited at the PDB. We also checked the electron density for the ligand and the binding site of all X-ray structures where this was available and found sufficient electron density support for all modeled ligand poses analyzed in this contribution. A table summarizing all 79 cycles can be found in the Supporting Information.

We inspected the original publications and the PDB structures for the remaining 15 cycles to generate structural hypothesis that could explain the observed nonadditivity in SAR data. In five cases, the available X-ray structures showed that there can be alternative orientations of the central scaffold. Such findings imply that the ligands can completely reorient, depending on the substitution patterns. A complete reorientation of the scaffold can lead to strong nonadditivity, since the substituents then interact with completely different subpockets, yielding different contributions to the free energy of binding. Figure 5 shows an example for such a case: a set of estrogen receptor β ligands with an indenone scaffold, published by Malamas et al.⁴³

Here, the two highly nonadditive transformations are a shift of an aromatic hydroxy group by one position and an exchange of a thioethyl by a bromine. Shifting the hydroxy group on the thioethyl substituted indenone changes the pIC₅₀ by 1.28 log units, whereas the same hydroxy shift changes the pIC₅₀ on the bromine substituted scaffold by 1.07 log units in the other direction. From the same publication, there are also some more double transformation cycles with other similar scaffolds that show strong nonadditivity. The overlay of two estrogen receptor β X-ray structures (PDBID 1U3S⁴³ and 1U3Q⁴³)

with similar ligands that feature a benzisoxazole scaffold shows that the benzisoxazoles can be oriented in two completely different ways inside the binding pocket, as shown in Figure 6.

Figure 5. Double transformation cycle for 1H-inden-1-one derivatives binding to the estrogen β receptor.⁴³

Figure 6. Alternative orientation of two benzisoxazole-based estrogen receptor β ligands (ligand in 1U3S green, 1U3Q orange).
establish that the carboxylic acids show a two-state binding behavior, with the fast formation of a preequilibrium, followed by a slow inactivation. When the \( pK_a \) for the fast formation of the preequilibrium is measured separately (biprofen \( pK_a = 6.89 \), flubiprofen \( pK_a = 6.0 \)) and compared to the pIC\(_{50}\) values for the tertiary amides, the strong nonadditivity almost completely disappears. This shows that strong nonadditivity may not only indicate structural changes and concurrencies, but also identify assay anomalies that require deeper analysis.

### DISCUSSION

Nonadditivity is a key SAR feature that indicates important changes within the ligand series. Therefore, the analysis and interpretation of nonadditivity is a crucial step for rational drug design, which relies on three-dimensional rationalization of SAR. Up to now, nonadditivity has been analyzed anecdotally, but we believe that nonadditivity analysis should become a standard tool in the medicinal chemist’s toolbox. With the statistical basics introduced here to distinguish real nonadditivity from apparent nonadditivity due to assay noise, this is now possible in a statistically rigorous way.

In most situations, it is not possible to distinguish weak nonadditivity from assay noise—therefore, it is mandatory to compare the observed nonadditivity to the nonadditivity expected due to noise. Knowing the level of experimental uncertainty is crucial for nonadditivity analysis. Here, we assume a normally distributed experimental uncertainty with a standard deviation of 0.2 log units. While this probably overestimates the true uncertainty for very well established assays with many repeat measurements, in some cases it is surely also underestimates the true uncertainty. It is therefore very important to improve our understanding of experimental uncertainty by regular independent repeat measurements and a deeper scientific analysis of the roots of uncertainty. Once the uncertainty is known, normal probability plots can be a practical help in identifying the double transformation cycles that show real nonadditivity and deserve more detailed investigation.

Biochemically, there can be different phenomena that lead to nonadditivity in SAR data. In previous works, loss of residual mobility, nonadditive rearrangements in the water network, and intramolecular hydrogen bonds have been named among others. In our analysis of double transformation cycles with nonadditivities \( >2.0 \) log units, we found evidence that complete structural rearrangements and substituent interactions can explain ten out of the 15 cycles. In a recent study on a series of Endothiapepsin inhibitors, Klebe and co-workers showed that chemically closely related compounds can have rather different binding poses. Structural rearrangements can explain otherwise inconclusive SAR and might occur much more frequently than is usually expected. In the other five cases, the available X-ray structures do not give a clear hint toward a single biochemical reason that could explain these cases of extreme nonadditivity. This is not due to the absence of a good reason but most probably due to the absence of a convincing set of experimental or computational results that can explain the nonadditivity. It should also be kept in mind that the combination of transformations can have nonadditive effects on solubility, and impurities or degradation can also cause apparent nonadditivity. We cannot control such effects in this retrospective study and hope such reasons have been ruled out in literature data, but these basic quality control checks are among the first things to be done if possible.
| Target, PDB IDs | Scaffold | Transformations | Nonadditivity [log pActivity]: Structural Hypothesis |
|----------------|---------|----------------|-----------------------------------------------------|
| Dihydrofolate Reductase<sup>67</sup> 1BOZ, 1MVS, 1MVT | A = CH<sub>2</sub>N  
B = H<sub>2</sub>CH<sub>3</sub> | 2.85: Scaffold rearrangement in presence or absence of the acceptor nitrogen |
| CHK1<sup>68</sup> 2X0E, 2YER, 2YEX | A = NH<sub>2</sub>, S  
B = CH<sub>3</sub>, NH<sub>2</sub> | 2.78: Most probably complete reorientation along hinge region. There is one more strong nonadditivity cycle in the same SAR series |
| Estrogen β receptor<sup>63</sup> 1U3Q, 1U3S, 1U3R, 1X7B | A = Br; S-C<sub>2</sub>H<sub>5</sub>  
B = | 2.34: Discussed in main text, complete rearrangement of scaffold. |
| Thrombin<sup>5</sup> 4AX9, 4AYV, 4AYY | A = H, C<sub>3</sub>H<sub>5</sub>  
B = CH<sub>3</sub> | 3.08: Authors of original publication discuss two different binding modes. Competition of substituents for same subpocket. There are three more similar highly nonadditive cycles in the SAR series. |
| Factor Xa<sup>19</sup> 1LQD, 1LPZ | A = H, CH<sub>3</sub>  
B = | 2.02: Complete rearrangement of binding mode (S1 group and S4 group exchange) |
| Thrombin<sup>50</sup> 1ZGI | A = CH<sub>2</sub>N  
B = | 2.54: Most probably intramolecular hydrogen bond: substituent interaction. |
| CDK<sup>21</sup> 1psj,1pxh,1pxl,1pxm,1pxn,1pxo,1pxp,2c5n,2c5o,2c5v,2wev,2xmy,3sw4,3sw7,4bcck,4bcn,4bco,4bcp,4bcq,4ek8,4fkl,4k0 | A = OH, NO<sub>2</sub>  
B = H<sub>2</sub>CH<sub>3</sub> | 2.23: Substituents come quite close in the Xray structure. Also, the protein is quite flexible. It probably reacts differently to combinations of substituents. There is one more nonadditivity cycle in the same SAR series. |
Table 1. continued

| Target, PDB IDs | Scaffold | Transformations | Nonadditivity [log pActivity]: Structural Hypothesis |
|----------------|----------|----------------|-----------------------------------------------------|
| DPP IV<sup>6</sup> 3KWJ, 3KWF, 30C0 | ![Scaffold](image1) | A = H, CH₃  
B = H, CH₃ | 2.70: Discussed in text, competition of two substituents for the same binding pocket |
| BACE<sup>52</sup> 3IVH, 410H | ![Scaffold](image2) | A =  
B = ![Structure](image3) | 3.16: Intramolecular hydrogen bond with NH or combination size effect. |
| LCK Kinase<sup>53</sup> 20FV, 20G8 | ![Scaffold](image4) | A = H, CH₃  
B = H, Cl | 2.26: Ortho-Substituent changes torsional energy profile |
| Glycogen Synthase Kinase<sup>54</sup> 3L15 | ![Scaffold](image5) | A = H, OCH₃  
B = ![Structure](image6) | 2.29: Unclear. There is one more cycle with strong nonadditivity in the same SAR series |
| LCK Kinase<sup>53</sup> 20FV, 20G8 | ![Scaffold](image7) | A = H, CH₃  
B = CH₃ | 2.65: Unclear |
| Dihydrofolate Reductase<sup>55</sup> 2W3B, 1PD8, 1PD9 | ![Scaffold](image8) | A = NH₂, S  
B = ![Structure](image9) | 2.01: Unclear |
| MMP13<sup>56</sup> 317G, 317I | ![Scaffold](image10) | A =  
B = ![Structure](image11) | 2.39: Unclear |
There is a tight analogy between activity cliffs and cases with strong nonadditivity (which could also be called additivity cliffs): While activity cliffs indicate the formation of key interactions, strong nonadditivity indicates that key interactions are changing due to the presence/absence of other substituents. Strong nonadditivity is a 2D indicator for a dynamic 3D behavior. If the key substitutions that cause a change in conformation are properly understood, it possibly allows dividing a SAR data sets into subsets that have the same orientation inside the binding pocket.

Computational models could be of great help here, and future development of these can benefit from the strong nonadditivity examples: In order to be useful, FEP approaches should be able to model the strong nonadditivity, if direct or indirect substituent interactions are involved. Note that 2 log units nonadditivity, which at room temperature corresponds to an energy difference of roughly 2.8 kcal/mol in binding free energy, is way above 1 kcal/mol, which is often cited as the difference threshold that can be described by higher-level computational methods. If the scaffolds completely reorient, docking/scoring approaches should be able to predict the correct pose. From a different perspective, strong nonadditivity cycles represent ideal test cases for the validation and further development of scoring functions and FEP approaches, since the effects of a lot of interactions cancel out in the cycles and only very few interactions lead to major differences in affinity.

Free Wilson analysis does not work in the presence of strong nonadditivity, since it relies on the same contribution from the same substituent in all cases. If a ligand exposes the same substituent to different subpockets, based on the presence or absence of other substituents, the contribution to the free energy of binding may differ dramatically depending on the subpocket. However, if the reason for nonadditivity is understood and the SAR data sets can be divided in subgroups for the different binding modes, Free Wilson Analysis should work within the different subgroups. For example, a ligand could have two distinct orientations inside the binding site. This would show up as a bimodal distribution in the increments for substitutions in specific positions. If there are bimodal distributions for specific substituents and the partner substituents that cause a rearrangement are known, the overall data sets can be split into orientation A and orientation B and Free Wilson Analysis might then work again for the split sets. For such situations, the most important task will be to identify key substituents that trigger rearrangements of the binding pose.

Knowledge of the experimental uncertainty plays a central role in nonadditivity analysis, since uncertainty can cause a substantial amount of apparent nonadditivity, in particular if many double transformation cycles are analyzed. If the experimental uncertainty in the data is neglected or underestimated, there is a risk that structural reasons for nonadditivity are searched where in fact there are none. This leads to a waste of human and/or computational resources and data overinterpretation. The nonadditivity profile of specific targets contains features that may be very interesting for further analysis. On the one hand, it may be possible to estimate the experimental uncertainty of a set of experiments from the width of the central peak in the nonadditivity profile. This might be an elegant way to obtain this very important number, which can otherwise only be obtained from independently repeated measurements that are often not available. On the other hand, the nonadditivity profile may be characteristic for the

| Target, PDB IDs | Scaffold | Transformations | Nonadditivity [log pActivity]: Structural Hypothesis |
|----------------|---------|----------------|-----------------------------------------------------|
| PI3 Kinase p110-gamma subunit<sup>67</sup> | ![Scaffold](image) | 2.15: Unclear |
| 2V4L, 3ENE | ![Scaffold](image) | A = H, F |
| COX1<sup>58</sup> | ![Scaffold](image) | B = OH, NMe<sub>2</sub> |
| 1CQE, 1EQH, 2AYL | | 2.08: Discussed in text, binding kinetics |

Figure 9. (Flu-)biprofen derivatization into a tertiary amide leads to highly nonadditive SAR data.

Table 1. continued
nature of the binding site. In our analysis, promiscuous targets such as hERG and CYP3A4 show a lot less nonadditivity than for example Factor Xa or MMP2. Whether this is due to the fact that targets such as hERG or CYP3A4 have much more continuum-like binding sites that do not fit Ehrlich’s lock-and-key concept\cite{18} is a topic for future studies.

With the statistical basics defined in this work, nonadditivity can systematically be analyzed in SAR data sets. The more nonadditivity comes into the focus of SAR analysis, the more we will learn about structural features that cause nonadditivity. Most of the existing structural information for cycles with strong nonadditivity has been generated to explain the nonadditivity observed. However, in the other cases, strong nonadditivity is often not discussed in the primary publications, leaving a central part of the SAR unexplained. If automated nonadditivity analysis becomes a standard tool, the risk of leaving a central part of the SAR unexplained.

Most of the existing structural information for cycles with strong nonadditivity has been generated to explain the nonadditivity observed. However, in the other cases, strong nonadditivity is often not discussed in the primary publications, leaving a central part of the SAR unexplained. If automated nonadditivity analysis becomes a standard tool, the risk of missing key SAR information from nonadditivity cycles will be decreased. Following the $\sigma$ rule, we have here concentrated on those 15 cycles where we are very sure that we do not interpret assay noise. However, this threshold can probably be set at a lower point, revealing much more nonadditivity cycles with structural information which can give valuable information for rational drug design. With the growing number of data in X-ray structure and bioactivity databases, there will be even more possibilities for systematic nonadditivity analysis in the future.

\section{SUMMARY}

Strong nonadditivity is an important SAR feature that can provide hints toward structural rearrangements or substituent concurrences and interactions. Therefore, nonadditivity analysis is an integral part of the SAR analysis toolbox. Experimental uncertainty can have a strong impact on the observed nonadditivity. It needs to be taken into account when searching for strong nonadditivities, otherwise there is a non-negligible risk of overinterpreting assay artifacts.

We have analyzed double transformation cycles with nonadditivity $>2.0$ log units for which there was sufficient structural information available. For five cycles, we found that there is good evidence that a complete rearrangement of the ligand in the binding site causes the nonadditivity. For five other cycles, we found that there is good evidence that direct or indirect substituent interactions cause the observed nonadditivity. For the remaining five cycles, we did not find a clear structural hint toward what is going on, and further calculations and analyses need to be done to reveal the source of nonadditivity.

Since nonadditivity is such a fundamental and important SAR pattern, we expect that there will be a lot more detailed analyses about the biochemical sources of nonadditivity and how we can use them in future drug design. Herein, we provide the basic statistical and cheminformatic methods for further exploration of this emerging field in medicinal chemistry.

\section{ASSOCIATED CONTENT}

\subsection{Supporting Information}

Program used to generate the double transformation cycles and an excel sheet with all double transformation cycles. This material is available free of charge via the Internet at http://pubs.acs.org.

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\textbf{Notes}

The authors declare no competing financial interest.

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