The puzzling spectrum of HD 94509
Sounding out the extremes of Be shell star spectral morphology

C. R. Cowley\textsuperscript{1}, N. Przybilla\textsuperscript{2}, and S. Hubrig\textsuperscript{3}

\textsuperscript{1} Department of Astronomy, University of Michigan, Ann Arbor, MI 48109-1042, USA e-mail: cowley@umich.edu
\textsuperscript{2} Institut für Astro- und Teilchenphysik, Technikerstr. 25/8, A-6020 Innsbruck, Austria e-mail: Norbert.Przybilla@uibk.ac.at
\textsuperscript{3} Leibnitz-Institut für Astrophysik, Potsdam (AIP), An der Sternwarte 16, 14482, Potsdam, Germany e-mail: shubrig@aip.de

Received; accepted

ABSTRACT

Context. The spectral features of HD 94509 are highly unusual, adding an extreme to the zoo of Be and shell stars. The shell dominates the spectrum, showing lines typical for spectral types mid-A to early-F, while the presence of a late/mid B-type central star is indicated by photospheric hydrogen line wings and helium lines. Numerous metallic absorption lines have broad wings but taper to narrow cores. They cannot be fit by Voigt profiles.

Aims. To describe and illustrate unusual spectral features of this star, and make rough calculations to estimate physical conditions and abundances in the shell. Furthermore, the central star is characterized.

Methods. We assume mean conditions for the shell. An electron density estimate is made from the Inglis-Teller formula. Excitation temperatures and column densities for Fe\textsuperscript{i} and Fe\textsuperscript{ii} are derived from curves of growth. The neutral H column density is estimated from high Paschen members. The column densities are compared with calculations made with the photoionization code Cloudy. Atmospheric parameters of the central star are constrained employing non-LTE spectrum synthesis.

Results. Overall chemical abundances are close to solar. Column densities of the dominant ions of several elements, as well as excitation temperatures and the mean electron density are well accounted for by a simple model. Several features, including the degree of ionization, are less well described.

Conclusions. HD 94509 is a Be star with a stable shell, close to the terminal-age main sequence. The dynamical state of the shell and the unusually shaped, but symmetric line profiles, require a separate study.

Key words. Stars: emission-line, Be – Stars: individual: HD 94509 – Stars: peculiar

1. Introduction

The unusual nature of the spectrum of HD 94509 was noted during a search of the ESO archive for possible Herbig Ae/Be stars. Simbad lists HD 94509 as a Be star, while Houk & Cowley (1975) call it Bp SHELL, with the remark that it has strong typ-

1.2. Observations

The study is based primarily on UVES archive spectra of HD 94509 obtained with the dichroic beam splitter DIC-2 in blue and red arms on 16 March 2009. The high-resolution spectrograph UVES (Ultraviolet and Visual Echelle Spectrograph, Dekker et al. 2000) is installed at the VLT-8m (ESO/Paranal, Chile). Our wavelength coverage is 3750–4985, and 5682–9460 Å. The resolving power is $R = \lambda/\Delta\lambda \approx 40,000$, due to the use of a wide slit. The signal-to-noise ($S/N$) varies but was typically about 330 in the blue and 250 in the visual.
Fig. 1. Comparison of the spectrum of HD 94509 (lower curve) with a FEROS spectrum of \( \alpha \) Aqr (B7-B8 IV-V, upper curve), a prototype Be shell star, for a selection of strategic lines. The most prominent features are identified. Both spectra were rv-corrected to the laboratory restframe.

We also used an ESO archive FEROS spectrum (\( R = 48,000 \), \( S/N \approx 120 \)) obtained on 7 June 2009, covering the wavelength range from 3666 to 8700 Å. FEROS (Fiber-fed Extended Range Optical Spectrograph, Kaufer et al. 1999) is a high-resolution, \( \text{É} \text{chelle} \) spectrograph operated at ESO in La Silla, Chile and installed at the MPIA 2.2m telescope. Both UVES and FEROS spectra were examined for spectral variations. The FEROS spectrum was also useful for features (e.g. Ba \( \text{II} \) \( \lambda 4934 \)) that were in UVES order gaps. Additionally, an X-Shooter spectrum of HD 94509 from 5 February 2010 was retrieved from the ESO archive. X-Shooter (Vernet et al. 2011) is installed at VLT-8m (ESO/Paranal, Chile) and is the first of the second generation instruments at VLT. The resolution and noise level of this spectrum was considerably lower than those of the UVES and FEROS spectra. We only used the X-Shooter data to look for spectral variations.

Figure 1 shows a comparison of the spectrum of HD 94509 with that of \( \alpha \) Aqr (HD 209409, B7-B8 V-IV), a prototype Be shell star, for a selection of strategic lines. While some similarities in the Balmer and He \( \text{I} \) lines are seen, the richness of the metallic-line spectrum and the peculiar line profile shapes stand out, and – to our knowledge – are unreported for any other star so far. Note that \( \alpha \) Aqr shows sharp line cores originating from the shell in a few of the strongest Fe \( \text{II} \) lines, e.g. \( \lambda 4924 \).

CL discuss three absorption lines in the neighborhood of the broad He\( \text{I} \) line \( \lambda 6678 \), which they tentatively identify as Fe \( \text{II} \) \( \lambda 6677.989 \), Ca\( \text{I} \) \( \lambda 6690.628 \), and Ca\( \text{I} \) \( \lambda 6717.681 \), with velocity shifts of \( -45 \), \( -35 \), and \( -7 \) km s\( ^{-1} \). Their Fig. 20 shows wavelength shifts at three epochs, best seen in the strongest feature.

The upper part of CL’s Fig. 20 closely resembles our spectra, shown in detail in Fig. 2. The broad He\( \text{I} \) absorption is apparent. We can plausibly identify the sharper absorptions as lines of Fe\( \text{II} \) and Ti\( \text{II} \) with the radial velocity of the other metallic lines of the shell. Interestingly, \( \lambda 6677 \) of Fe\( \text{II} \) does not appear in the current National Institute of Standards and Technology (NIST) list, though it is in the Multiplet Tables, and in the Vienna Atomic Line Database (VALD). G. Nave of NIST (private...
communication) suggests it is masked in her spectra by an argon line. Our material does not indicate the presence of another star, or another shell with a relative radial velocity shift. We can, of course, not exclude a stage of variability at an epoch not covered by our spectra.

2.2. The metallic lines

Figure 3 is typical of the stronger metallic-line profiles. A rough fit to the observed line is possible with a $10 \times$ solar abundance and a standard model atmosphere see Sect. 3 for details on the modelling. However, the wings require an impossibly large enhancement of the damping, by a factor of $6 \times 10^4$. The dark gray (blue online) rotational profile used a $10 \times$ solar iron abundance, with $V \cdot \sin(i) = 100 \text{ km s}^{-1}$ and standard Stark broadening.

The somewhat rectangular shape of the profiles with rounded bottoms, of the latter star may be rather closely matched by a model with appropriate microturbulent and rotational broadening.

Figure 3 is typical of the stronger metallic-line profiles. A rough fit to the observed line is possible with a $10 \times$ solar abundance and a standard model atmosphere see Sect. 3 for details on the modelling. However, the wings require an impossibly large enhancement of the damping, by a factor of $6 \times 10^4$. The figure also shows a calculated profile based on a $V \cdot \sin(i)$ of $100 \text{ km s}^{-1}$ and standard Stark broadening.

The stronger metallic-line profiles of HD 94509 gracefully taper to cores as sharp as the instrumental resolution allows. The profiles merge with the continuum in what resemble Lorentz wings. The profiles are very symmetrical, with little or no indication of a wind, or velocity asymmetry within the zone in which they are formed.

A broader view of the $\lambda 4233$-region is shown in Fig. 4. The richness of the HD 94509 spectrum is comparable to that of the F3 Ia supergiant HD 74180, and not common among shell stars, cf. Fig. 1. Note we do not imply that HD 94509 is a composite containing such a star. Dilution indicators, discussed below (Section 4.1), show that the metallic-line spectrum of HD 94509 is not photospheric. But a few stable shell stars (Gulliver 1981) may have similar spectra. Merrill (1952) shows a microphotometer tracing for HD 193182, whose spectrum is surely rich in metal lines. We have been unable to find a digital, high-resolution spectrum that would allow us to make a close comparison of the line shapes.

A few of the strong metallic lines show broad emission shoulders as well as relatively narrow, deep absorption. An example is the Fe ii emission, $\lambda 6516: a^5S_2 - a^5D_2$ in Multiplet 40 (Moore 1945). Multiplet 42 of Fe ii ($\lambda \lambda 4924, 5018, \text{ and } 5169$) is commonly in emission in many peculiar spectra (Be, Herbig

---

4. Note that the effective temperature $T_{\text{eff}}$ and surface gravity log $g$ of the model are chosen here for illustrative purposes only – the line is not formed in the atmosphere of the central star, but in the shell.
Fig. 6. The base, or full width of Fe ii absorption lines shows a definite correlation with the line depths. For 31 points, the Pearson correlation coefficient is 0.674; the significance, or probability of no correlation is $3 \times 10^{-5}$.

Fig. 7. The Paschen line, P12, shows the sharp core of the shell and the broad-line morphology of the central source. Overlayed are rotational profiles for 0 (dark gray, or blue) and 260 km s$^{-1}$ (light gray, or red). Two Ni lines are seen to the violet of P12. See the text for details.

2.3. The hydrogen lines

The Balmer lines are highly symmetrical. Both H\(\alpha\) and H\(\beta\) have double emission peaks of equal intensity, see Fig. 1. The central absorption cores yield velocities that closely agree with the metallic-line absorption. The central reversals of both H\(\alpha\) and H\(\beta\) are very deep, while the cores of H\(\gamma\) through H\(\epsilon\) are virtually black. Our spectra extend from H\(\alpha\) to H\(\iota\) or H10, and none of the core wavelengths deviate from the laboratory positions by more than 0.04 Å. For such broad profiles, this may easily be attributed to measuring error. The mean deviation for the 9 lower Balmer cores from that expected from the metallic cores is 0.0033 Å. The symmetry of both the hydrogen and metallic absorption cores is indicative of “negligible line-of-sight velocities” in the absorbing shell (cf. Rivinius et al. 2006).

The non-LTE calculations of P12 shown in Fig. 7 were made with a 14000 K, log $g$ = 3.5 model, assuming an additional continuum equal to a factor of 0.2 times the stellar continuum. Theoretical plots are for $V \cdot \sin(i) = 0$ and 260 km s$^{-1}$. As the Stark-broadened wings of P12 are of stellar origin (only the sharp line core originates in the shell), this may be viewed in support of the atmospheric parameters chosen for the central star (Sect. 6.1). The same applies to other hydrogen lines, also the Balmer lines from H\(\gamma\) (see Fig. 8) to the higher series members. A continuum contribution of 0.12 times the central star’s photospheric continuum was adopted for H\(\gamma\), meeting the expectation of a decreasing ratio towards the blue. Note, however, that the true amount of dilution of the underlying spectrum is uncertain.

2.4. The helium lines

The He i lines are broad and shallow, unlike the metal lines. They can be matched by rotationally-broadened line profiles, except for cases with metal line blends (see e.g. Fig. 2). This is indication for a stellar atmospheric origin of these lines. They can be fit using atmospheric parameters as adopted for the central star (Sect. 6.1), and a solar helium abundance. Figure 9 shows the example of the line He i $\lambda$5875, assuming an additional continuum from the shell equal to a factor of 0.15 times the stellar continuum, intermediate between the two values adopted for the hydrogen Balmer and Paschen line above. A rotational velocity of $\sim 260$ km s$^{-1}$ is indicated, in consistency with the typical picture of shell star, where the metallic absorption is superimposed on the spectrum of a rapidly rotating central star.

Table 1. Apparent rotational velocities (half widths) in km s$^{-1}$. Emission lines marked with an asterisk. An average is given for the Ca ii infrared triplet.

| Spectrum | Wavelength (Å) | $V \cdot \sin(i)$ |
|----------|----------------|------------------|
| He i     | 5876           | 255              |
| He i     | 6678           | 299              |
| Si ii    | 6347, 6371     | 245              |
| Ca ii (IRT)$^*$ | 8500-8660 | 225              |
| Ave. 31 Fe ii | 3783-7516 | 99±33sd           |
| Fe ii$^*$ | 6516           | 214              |
| K i      | 7699           | 114              |

Notes. $^*$ The width measurement is of emission shoulders.

The non-LTE calculations of P12 shown in Fig. 7 were made with a 14000 K, log $g$ = 3.5 model, assuming an additional continuum equal to a factor of 0.2 times the stellar continuum. Theoretical plots are for $V \cdot \sin(i) = 0$ and 260 km s$^{-1}$. As the Stark-broadened wings of P12 are of stellar origin (only the sharp line core originates in the shell), this may be viewed in support of the atmospheric parameters chosen for the central star (Sect. 6.1). The same applies to other hydrogen lines, also the Balmer lines from H\(\gamma\) (see Fig. 8) to the higher series members. A continuum contribution of 0.12 times the central star’s photospheric continuum was adopted for H\(\gamma\), meeting the expectation of a decreasing ratio towards the blue. Note, however, that the true amount of dilution of the underlying spectrum is uncertain.
2.5. Additional remarks

Estimates of the putative $V \cdot \sin(i)$ may be made from the (half) base widths of both additional emission and absorption lines. Uncertainties in these values depend on the line width measurements, whose accuracies are discussed in Section 2.2.

While the metallic spectrum is predominantly absorption, a few lines show "emission shoulders". Table 1 summarizes the measurements, yielding the following picture. The lines originating from the highest excitation potentials (i.e. the He I lines) indicate the highest apparent rotational velocities, of about $250 - 300 \text{ km s}^{-1}$. This should correspond to the rotational velocity of the central star, which is in line with a typical $V \cdot \sin(i)$ that ranges from $200$ to $450 \text{ km s}^{-1}$ for the central component of shell stars (Rivinius et al. 2006). Slightly lower velocities are obtained from the emission shoulders of spectral lines, which arise from the faster-spinning inner parts of the disk. Then, even lower rotational velocities are found for the metallic absorption lines, which involve low-excitation levels and indicate the formation in the slower-rotating outer parts of the disk.

Finally, we note that several broad and shallow features are seen in the spectrum. These coincide in wavelength with several of the typically most pronounced diffuse interstellar bands (DIBs). In particular $\lambda 5780.45, 6283.86$ and $6613.62$ are present, but shifted by $\sim +17 \text{ km s}^{-1}$ relative to the intrinsic spectrum of HD 94509. This is consistent with the findings from the sodium D and calcium H and K lines (see Sect. 3).

3. Characterization of the central star

While the overall spectrum is dominated by shell photospheric absorption and emission, a small number of features are of shell photospheric origin, as indicated in the last section: the wings of several hydrogen lines and He I lines. Photospheric metal lines unaffected by disk absorption cannot be identified unambiguously. These lines do not provide sufficient information for a fully-fledged quantitative analysis, but allow an estimate of the atmospheric parameters. A $T_{\text{eff}} = 14,000 \text{ K}$ and $\log g = 3.5$, solar helium abundance and $V \cdot \sin(i) = 260 \text{ km s}^{-1}$ seems a proper choice, but cannot be considered precise. The presence of He I lines set a lower boundary of the temperature to $\sim 11,000 \text{ K}$. However, this would require an enhanced helium abundance, which is unlikely in view of evolution models for rotating stars that do not predict a noticeable increase of the surface helium values even at critical rotation in the relevant mass range (Brott et al. 2011, Georgy et al. 2013). The wings of the hydrogen lines provide additional information on the effective temperature, but are subject to temperature-gravity degeneracy. Calculations with the ionization code CLOUDY (see Section 6) show that the He emission strength would be too large for a higher temperature than the one adopted.

The adopted gravity value implies that the star is in an advanced stage of the main-sequence evolution, consistent with theoretical considerations (e.g. Granada et al. 2013). Note that the light from the central star – as a consequence of the fast rotation and the shadowing by the disk seen equator-on (i.e. $i = 90^\circ$) – is dominated by the hotter and slower-rotating polar caps. Consequently, our above-mentioned parameters are likely upper values for the non-uniform $T_{\text{eff}}$- and $\log g$- distribution over the rotationally-flattened stellar surface, while the rotational velocity is a lower limit (e.g. Towsend et al. 2004, Fremat et al. 2005). The metallicity of the star seems close to solar, or compatible with the present-day cosmic abundance standard (Nieva & Przybilla 2012), as indicated by the analysis of the shell (see Sect. 6).

We employed a hybrid non-LTE approach for our stellar photospheric line-formation calculations, which has been successfully used before in a similar temperature regime to the one studied here (Przybilla et al. 2006, Nieva & Przybilla 2007). Plane-parallel, hydrostatic and homogeneous LTE model atmospheres were computed with the code ATLAS9 (Kurucz 1991). Then, non-LTE line-formation computations were performed with the codes DETAIL and SURFACE (Giddings 1981, Butler & Giddings 1985, both updated and improved). DETAIL calculates atomic-level populations by solving the coupled radiative transfer and statistical equilibrium equations, and SURFACE computes the formal solution using realistic line-broadening functions. We employed model atoms of Przybilla & Butler (2004) for hydrogen, of Przybilla (2005) for He, and of Becker (1998) for Fe II.

We note that the model calculations are intended to illustrate the plausibility of our parameter choices, but are well aware that this approach is suited to address the complex phenomenology of a Be (shell) star only coarsely. We also note that similar approaches are nevertheless employed for quantitative Be star analyses (e.g. Levenhagen & Leister 2004, Dunstall et al. 2011).
Table 2. Electron densities \( \log(N_e) \)

| constant | \( n = 41 \) | \( n = 42 \) |
|----------|-------------|-------------|
| 23.26    | 11.16       | 11.08       |
| 23.49    | 11.40       | 11.32       |

4. Physical conditions in the shell

4.1. Dilution indicators

A general characteristic of shell stars is the relative enhancement of second spectra (from ions) relative to first (from neutrals), when compared with the spectra of dwarfs or normal giants. This may be attributed to the low electron pressure in the shell, which will be discussed in more detail below (cf. Sect. 4.2). A second characteristic, discussed in numerous papers and reviews by Struve (e.g. Struve 1951), is the weakness of certain lines which he called “dilution indicators”. Specifically, Struve called attention to lines of Si II \( \lambda \lambda 3853-3862 \), 4128-4130, and Mg II 4481. He noted that the lower levels of the dilution indicators were connected to the ground level by strong permitted transitions. Most absorption lines of Fe II and Ti II arise from levels of the same parity as the ground term, and are thus metastable.

We illustrate this in Fig. 10 where lines in HD 94509 and the supergiant Deneb are shown. The latter spectrum is the one described by Schiller & Przybilla (2008). Generally, the metallic lines in HD 94509 are significantly stronger than in Deneb, but this is not the case for Struve’s dilution indicators.

4.2. Electron density

A depth-dependent model of the shell of HD 94509 is beyond the scope of the present work. We attempt to determine mean conditions for the shell as a whole, making use of techniques common for normal stellar atmospheres prior to the use of numerical modeling.

Our high-resolution spectra do not include the Balmer limit, but the Paschen limit is clearly seen. The line P41 was measured, but P42 was not, and an inspection of the spectrum reveals no obvious feature between P41 and three moderate N \( i \) lines. A well-established interpretation of the termination of a one-electron line series is that overlapping Stark wings merge so individual features are no longer seen (Inglis & Teller 1939, henceforth, IT). A simple derivation of the formula may be found in Cowley (1970), where it is assumed that protons and electrons contribute equally to the line merging, unlike IT. If the last Paschen line is Pn, then

\[
\log(N_e) = \log(N_p) = 23.26 - 7.5 \log(n),
\]

where \( N_e \) and \( N_p \) are the electron and proton number densities, respectively. Varshni (1978) uses the constant 23.49 rather than 23.26. Let us put \( n = 41 \) and 42 into Eq. 1. Results are shown in Table 2. We conclude that a mean logarithmic electron density of the shell is 11.2 \( \pm 0.5 \).

4.3. The shell temperature

4.3.1. Fe II

We know from the dilution indicators that there can be no single temperature that will describe the excitation and ionization within the shell. Nevertheless, the ionization and excitation may be approximately estimated from measurements of the line strengths. These estimates will be subject to clarification by models of the shell. We have worked primarily with the second spectra of metallic lines: Sc II, Ti II, Cr II, Fe II, and Ni II. The Fe II spectrum is by far best suited for our purposes, both because of its richness and the detail of its treatment by the versatile program CLOUDY (c13.03, Ferland et al. 2013, cf. Sect. 6.1).

The unusual shape of the Fe II (and other metallic line) profiles means that measurements of equivalent widths \( W_A \) require special care. Our general approach in abundance work is to fit metal lines with Voigt profiles. However, the \( \alpha = \gamma/(2\Delta l_D) \) is usually small, typically 0.01 to 0.1, so the profiles are not far from Gaussian. Such a low \( \alpha \)-value is completely unsuitable for HD 94509. For the lines with profiles that are not too deep, we could make tolerable fits using \( \alpha = 5 \), virtually Lorentzian profiles. Core and wings of the stronger (deeper) lines could not be fit by any Voigt profile. All of the profiles were also fit with small line segments, so for many lines we could compare the results (Fig. 11). We adopted simple means for all pairs of measurements.

One may estimate an overall excitation temperature by plotting \( \log(W_A/\lambda) \) vs. \( \log(gf/\lambda) - (5040/T) \cdot \chi \), where \( \chi \) is the lower excitation potential of the absorption line. One adopts the temperature \( T \) as the value that gives the minimum separation of lines with different \( \chi \). We illustrate this determination using reliable Fe II \( gf \)-values, from Meléndez & Barbáru (2009, cf. also Adelman 2014). Figure 12 shows the adopted fit, using \( \theta = 5040/T = 0.55 \), or \( T_{exe} = 9164 \pm 170 \text{K} \). The uncertainty is derived from trial plots with \( \theta = 0.55 \) and 0.56, which were judged marginally acceptable.

4.3.2. Fe I and Ti II

Other atomic species with enough measurable (mostly unblended) lines to allow a credible curve of growth are Fe I and Ti II. Results are gathered in Table 3; uncertainty estimates, explained in 4.5.1, are significantly larger for Ti II and Fe I, which have fewer lines than Fe II.
The column density of an absorber follows from the relation for weak lines with equivalent widths \( W^* \):

\[
W^* = \frac{\pi e^2}{mc^2} \chi N_n f_{\text{num}}.
\]

(2)

Here, \( N_n \) is the number (per cm\(^2\), column density) in the lower energy level, in the absorbing shell. We have assumed the metal line absorption arises entirely in the shell. In this context we note that the central star has a spectral type in the late/mid-B range and it is unlikely to find chemical peculiarities, as the fast rotation inhibits the CP phenomenon because of rotationally-driven hydrodynamical mixing. Therefore, one may expect the only features of iron-group species present in the stellar spectrum to be weak Fe \( \text{II} \) lines. At most, these stellar lines contribute a few percent to the measured equivalent widths, i.e. they are indeed negligible. In fact the presence of strong unusually-shaped features of e.g. Sc \( \text{II} \), Ti \( \text{II} \), Cr \( \text{II} \), Fe \( \text{I} \) and Ni \( \text{II} \) makes the spectrum appear so unusual.

4.4.1. Fe \( \text{II} \)

One may estimate from Fig. 12 that lines as strong as 250 mÅ \((\log(W/\lambda + 6 = 1.7, \text{ for } 5000 \text{ Å})\) are still on the linear part of the curve of growth. Let us make the provisional assumption that iron is predominantly first ionized, neglecting Fe \( \text{I} \) and Fe \( \text{III} \).

Using the Boltzmann formula, with \( u(T) \) the partition function of Fe \( ^+ \), and using logarithms, this may be written to give the column density of all Fe \( ^+ \) for each line. With \( \theta \equiv 5040/T, \) and the lower excitation energy \( \chi_n \), we have

\[
\log[N(Fe^+)] = \log(W^*/\lambda) + 12.053 - \log(g f \lambda) + \log(u(T)) + \theta \chi_n.
\]

(3)

We work out the column densities for Fe \( ^+ \) using Eq. 3 for the Fe \( \text{II} \) lines shown in Tab. 4. The average value (of the logarithms) of the last column is 18.77±0.19.

4.4.2. Neutral iron

While the Fe \( \text{I} \) lines are less numerous than those of Fe \( \text{II} \), a number of them may be measured, and analyzed in a similar manner.

### Table 4. Calculation of column densities for Fe \(^+\). Dimensions are given for the arguments of the logarithmic quantities.

| \( \lambda \) (Å) | \( \chi \) (eV) | \( \log(g f \lambda) \) | \( \log(W/\lambda) \) | \( \log[N(Fe^+)] \) |
|-----------------|---------|----------------|----------------|----------------|
| 3873.76         | 2.43    | -0.88          | 1.72           | 15.52          |
| 3983.96         | 2.73    | -1.02          | 1.45           | 15.54          |
| 4118.55         | 3.63    | 0.22           | 1.88           | 15.20          |
| 4309.37         | 2.95    | -1.19          | 1.83           | 16.15          |
| 4442.34         | 2.20    | -1.26          | 1.18           | 15.11          |
| 4593.12         | 2.18    | -1.28          | 1.48           | 15.42          |
| 4666.55         | 2.83    | -0.60          | 1.69           | 15.32          |
| 4746.02         | 2.84    | -0.82          | 1.52           | 15.37          |
| 4944.56         | 2.20    | -1.14          | 1.62           | 15.43          |
| 8688.63         | 2.18    | -1.21          | 1.96           | 15.26          |

Oscillator strengths for Fe \( \text{I} \) are from Fuhr & Wiese (2006). Table 5 presents the results. The average of the logarithms for the last column is 15.41±0.35.

### Table 5. Calculation of column densities for neutral Fe or Fe \(^+\). The format is the same as for Table 4.

| \( \lambda \) (Å) | \( \chi \) (eV) | \( \log(g f \lambda) \) | \( \log(W/\lambda) \) | \( \log[N(Fe)] \) |
|-----------------|---------|----------------|----------------|----------------|
| 3873.76         | 2.43    | -0.88          | 1.72           | 15.52          |
| 3983.96         | 2.73    | -1.02          | 1.45           | 15.54          |
| 4118.55         | 3.63    | 0.22           | 1.88           | 15.20          |
| 4309.37         | 2.95    | -1.19          | 1.83           | 16.15          |
| 4442.34         | 2.20    | -1.26          | 1.18           | 15.11          |
| 4593.12         | 2.18    | -1.28          | 1.48           | 15.42          |
| 4666.55         | 2.83    | -0.60          | 1.69           | 15.32          |
| 4746.02         | 2.84    | -0.82          | 1.52           | 15.37          |
| 4944.56         | 2.20    | -1.14          | 1.62           | 15.43          |
| 8688.63         | 2.18    | -1.21          | 1.96           | 15.26          |

average 15.33±0.35 (sd)

4.4.3. Sc \( \text{II} \), Ti \( \text{II} \), Cr \( \text{II} \), and Ni \( \text{II} \)

Column densities have been estimated for other species, using the Fe \( \text{II} \) curve of growth to choose “weak” lines or estimate saturation corrections. Results are discussed in Sect. 6.4 below. These are uncertain by at least a factor of three because of the difficulty in estimating the contributions from the wings, especially in the case where wings from different lines overlap. Non-LTE effects are also expected, as can be seen from the more detailed results for Fe \( \text{II} \) available from CLOUDY (cf. Sect. 6.3).

A resume of observed and theoretical column densities may be found in Sect. 6. Relevant data are presented in Table A.1 in Appendix A.
4.4.4. Hydrogen

The highest Paschen lines (those that have no contribution from the central star) may be used to make a crude estimate of the column density $N_3$, of hydrogen in the $n = 3$ level. Measurements of equivalent widths were made using the segmented fits described above. With Eq. (2) we obtain values of $N_3$ that would apply as if the lines were unsaturated. In the ideal case, discussed in the classical text of Unsöld (1955), we would expect values of $N_3$ to increase, as the lines become optically thin, and then to decrease as the lines blend together, so their entire width is not measured.

The last column of Table 6 decreases as $n$ increases, as expected. We do not see a decrease due to saturation for the smaller $n$. However, the variation from P30 to the last visible line, P42, is not large, so the uncertainty is comparable to other approximations made herein. We adopt log($N_3$) = 15.3.

5. Qualitative chemistry of the circumstellar envelope or shell

Of the lighter elements, hydrogen is well represented by the features described previously. We see broad absorption from He I $\lambda\lambda$5876 and 6678, and most of the bluer optical lines, but this is from the underlying stellar spectrum. There is no sign of emission in the He I features. There is also not a hint of absorption or emission at the position of the Li I resonance lines near $\lambda\lambda$6708 – which is expected because any lithium initially present would be transported to deeper layers of the stellar envelope due to rotationally-induced mixing, and destroyed by nuclear reactions. This applies in a similar manner to beryllium and boron (relevant lines are located outside the available spectra). Absorption near $\lambda\lambda$9062 and 9112 could be due to C I in Multiplet 3. No C II lines were noted. A number of absorptions due to N I were identified in the near infrared. Several of these appear in Figs. 1 and 7. The sharp cores of the N I lines are indicative of absorption from the shell. Neutral oxygen lines from the shell are the strong infrared triplet $\lambda\lambda\lambda$7772, 7774, and 7775 and the line $\lambda\lambda$8446 (see Fig. 1).

The D lines of sodium are strong. Each line is double, with the deeper component having the stellar radial velocity, with the strong, second component shifted to the red by 17.3 km s$^{-1}$, likely being of interstellar origin (an analogous situation is seen in the calcium H and K lines). Several lines of Mg I are identified including the b-lines, which have the broad wings and sharp cores of the shell. The usually strong Mg II $\lambda\lambda$4481 is severely weakened as noted earlier. The Al I resonance doublet is present, but weak. No Si I lines were identified, but Si II lines are present in addition to the dilution indicators mentioned in Sect. 6.1. The violet component of the K I resonance pair, $\lambda\lambda$7665 is obscured by water-vapor absorption, but $\lambda\lambda$7699 is unblended and strong ($W_I \approx 500$ mÅ), see Fig. 1. The 3d elements Ca-Ni are all well represented, but heavier elements are weak or absent altogether, similar to the situation in a supergiant spectrum at comparable temperature.

An analysis by wavelength coincidence statistics (WCS) reveals meager evidence for the presence of neutron addition elements. Even the Sr II resonance lines, $\lambda\lambda$4077 and 4215 are weak and blended. Neither of the Ba II resonance lines, $\lambda\lambda$4554 and 4934 show more than a possibility of absorption near their positions. This need not imply an underabundance of Ba or Sr as we anticipate significant double ionization of these two elements. Zr II may be weakly present, but there is no evidence for Y II.

6. A model using CLOUDY

6.1. Details

It is clear that the conditions in the shell cannot be well described by local thermodynamic equilibrium (LTE). We have therefore used the versatile photoionization code CLOUDY (Ferland et al. 2013) to broaden our analysis. Ideally, we would run CLOUDY as a subroutine, and try to minimize deviations of its predictions against our measurements. Such an approach is beyond the scope of the present work. We have limited ourselves to trial and error comparisons of selected measurements or derived quantities, assuming default solar abundances (Asplund et al. 2009, Scott et al. 2015a, Grevesse et al. 2015).

The stellar background is from a Kurucz (1991) ATLAS9 model. Details, and some relevant quantities are collected in Table 7. Properties for the $T_{\text{eff}} = 14,000$ K main sequence star were chosen with the help of data from Torres et al. (2013). We report results here for a cylindrical geometry described in the documentation for CLOUDY (Hazy-1, Sect. 9.6). Similar results were obtained with a spherical geometry with the same parameters apart from the cylinder height.

It is possible to obtain column densities for any one of 371 individual levels of Fe +. Our models used 256 levels, to save computing time. We may obtain an “excitation temperature” from these column densities that should be comparable to the values derived by the empirical curves of growth from Ti II, Fe I, and Fe II. This is shown in Fig. 19.
Recall that the empirical results for Fe II and Ti II were 
~9164 K, while that for Fe I was 7750 K. Theoretical and empirical results are summarized in Table 8. The "empirical" entries for neutral and ionized hydrogen are described as semi-empirical and shown inside brackets. While the IT formula allows us to estimate a mean electron density (cm$^{-3}$), we can only infer a column density indirectly. The entry for H$^+$ in Table 8 comes from taking the product of the IT electron density and multiplying by the physical thickness of the model, to obtain a column density. We assume the column density of protons is reasonably approximated by the electron column density thus obtained.

We have an empirical estimate of the column density only for the $n = 3$ level of neutral hydrogen. We need a temperature to convert this to a column density for all levels of hydrogen, using the Boltzmann formula. There is no obvious empirical value to use; indeed, because of the non-LTE conditions the meaning of any temperature so chosen is strictly limited to the Boltzmann formula and the relevant level populations. If we simply define a $T_{ex}$ as that value giving the column densities $N_e$(H) and $N$(H), the adopted CLOUDY model gives $5040/T_{ex} = 0.69$. Recall the empirical values of $\theta$ from Fe I and Fe II were 0.65 and 0.55. The entry for H$^+$ in Table 8 was obtained using $\theta = 0.69$, and the empirical log($N_e$(H)) = 15.3.

Let us assume (Hanuschik 1996) that Be and shell stars have "disks that are intrinsically identical." Then our basic parameters from Table 8 should be comparable with those estimated for Be stars. These stars display a variety of characteristics, summarized by Slettebak and Smith (2000). The stellar types range from late O (X Per) to late B ($\beta$ CMi). The disks are typically 5 to 20 stellar radii, with temperatures of 10 000K, and electron densities of $10^{10}$ to $10^{13}$ per cm. Our values for $N_e$, $T$, and radii agree well with these values.

6.2. Comments

The dominant species, e.g. Fe$^+$, are predicted reasonably well by the model. For column and particle densities in Table 8, apart from neutral iron, the rms deviations of the empirical from the 9 model values is 0.33 dex, or a factor of 2.1. Neutral iron is an order of magnitude or more stronger than the predictions. If we include neutral iron, the rms deviation is 0.42 dex. A cooler central star could reduce this discrepancy, but the broad He I absorptions would then be difficult to explain. It does not help the ionization discrepancy to move the cloud out by a factor of 10. Higher or lower overall densities were also tried, with appropriate adjustments of the absorption path lengths.

We note that the treatment of complex atoms of the iron group by CLOUDY, apart from Fe II, does not involve multi-level models. In view of this approximate treatment, we do not consider the discrepancy with the Fe I column density to be serious in the context of the present study.

7. Conclusions

HD 94509 is a shell star with an unusually stable shell, posing an extreme in the zoo of Be star spectral morphology. We have not been able to account for the unusual shapes of the metallic absorption lines. However a simple model of the shell can predict the total absorption from H I, the electron density, and column densities of the dominant ions. Near-solar elemental abundances are found. The lowest Balmer lines have deep cores and symmetrical emissions. The cores of H y through H e are virtually black, indicating the shell must cover the stellar disk.

Acknowledgements. CRC thanks Howard Bond, Francis Fekel, and George Wallerstein for comments on samples of the HD 94509 spectrum. Advice and help from J. Hernandez and numerous Michigan colleagues is gratefully acknowledged. We thank Gillian Nave of NIST for clarification of a question regarding the Fe II spectrum. We thank R. Oudmaijer for comments on his reduction of the X-Shooter spectrum. This research has used the SIMBAD database, operated at CDS, Strasbourg, France. We made extensive use of the VALD atomic data base (Kupka et al. 2000), as well as the NIST online Atomic Spectroscopy Data Center (Kramida et al. 2013). Spectra were obtained from the ESO Science Archive Facility under request number SHUBRI/2955, and CCOW-LEY/101986.

References

Adelman, S. J. 2014, PASP, 126, 505
Asplund, M., Grevesse, N., Sauval, A. J. & Scott, P. 2009, ARA&A, 47, 481
Becker, S. R. 1998, ASP Conf. Ser., 131, 137
Brott, I., de Mink, S. E., Cantiello, M., et al. 2011, A&A, 530, A115
Butler, K. & Giddings, J. R. 1985, in Newsletter of Analysis of Astronomical Spectra, No. 9 (Univ. London)
Corporon, P. & Lagrange, A.-M. 1999, A&A, 136, 429 (CL)

5 http://vald.astro.univie.ac.at/~vald/php/vald.php
6 http://www.nist.gov/pml/data/index.cfm

Table 8. Comparison of various empirical results with corresponding quantities from the model using solar abundances. Numerical values without units are logarithms of column densities (cm$^{-2}$). Neutral species are indicated by a superscript ‘0’. Parenthesized numbers indicate the number of lines used. Values in square brackets are semi-empirical (see text).

| Species | Model | Empirical |
|---------|-------|-----------|
| H0     | 23.30 | [22.8]    |
| H+     | 23.15 | [23.5]    |
| N(I)(H)| 15.83 | 15.3      |
| log($N_e$(cm$^{-3}$)) | 10.99 | 11.2 |
| Sc+    | 14.54 | 15.2(2)   |
| Ti+    | 16.43 | 16.8(5)   |
| Cr+    | 17.11 | 17.2(4)   |
| Fe0    | 14.25 | 15.4(13)  |
| Fe+    | 18.98 | 18.8(16)  |
| Ni+    | 17.74 | 17.6(4)   |
| $T_{ex}$(K) | 11134 | 9164 |
| $W$(Hα)(Å) | 28    | 24     |
Appendix A: Data on iron group elements

Table A.1. Data for lines used for column densities of elements other than iron. References are to the oscillator strength source.

| Wavelength [Å] | χ (eV) | log(gf) | Wj (mÅ) |
|----------------|--------|---------|---------|
| 4246.82        | 0.315  | 0.242   | 616     |
| 4400.49        | 0.605  | −0.536  | 304     |
| 4415.56        | 0.595  | −0.668  | 491     |
| 4420.67        | 0.618  | −2.273  | 20      |
| 4025.13        | 0.61   | −2.34   | 310     |
| 4028.34        | 1.89   | −0.96   | 318     |
| 4227.35        | 1.13   | −2.24   | 169     |
| 4287.87        | 1.08   | −1.82   | 250     |
| 4290.22        | 1.17   | −0.85   | 455     |
| 4300.05        | 1.18   | −0.44   | 532     |
| 4312.86        | 1.18   | −1.10   | 434     |
| 4391.03        | 1.23   | −2.28   | 166     |
| 4398.29        | 1.22   | −2.78   | 86      |
| 4399.77        | 1.24   | −1.19   | 414     |
| 4411.93        | 1.22   | −2.52   | 98      |
| 4432.11        | 1.24   | −2.81   | 47      |
| 4441.73        | 1.18   | −2.27   | 190     |
| 4443.79        | 1.08   | −0.72   | 430     |
| 4450.48        | 1.08   | −1.52   | 418     |
| 4464.45        | 1.16   | 1.81    | 276     |
| 4468.51        | 1.13   | −0.60   | 506     |
| 4501.27        | 1.12   | −0.77   | 568     |
| 4518.33        | 1.08   | −2.91   | 91      |

Table A.2. Data on lines used for column densities of elements other than iron. References are to the oscillator strength source.

| Wavelength [Å] | χ (eV) | log(gf) | Wj (mÅ) |
|----------------|--------|---------|---------|
| 4195.42        | 5.32   | −1.95   | 41      |
| 4242.36        | 3.87   | −1.17   | 324     |
| 4558.66        | 4.07   | −0.656  | 616     |
| 4588.20        | 4.07   | −0.627  | 545     |
| 4634.07        | 0.47   | −0.980  | 454     |
| 4812.34        | 3.86   | −1.800  | 341     |
| 4824.13        | 3.87   | −0.920  | 500     |
| 4836.23        | 3.86   | −2.25   | 137     |
| 4041.47        | 4.03   | −2.41   | 58      |
| 4067.03        | 4.03   | −1.83   | 269     |
| 4244.78        | 3.86   | −3.10   | 17      |
| 4362.10        | 4.03   | −2.70   | 59      |

Cru, Nilsson et al. (2006)

Ni II (2014)

| Wavelength [Å] | χ (eV) | log(gf) | Wj (mÅ) |
|----------------|--------|---------|---------|
| 3615.10        | 2.41   | −0.92   | 500     |
| 3716.43        | 3.86   | −2.25   | 137     |

Cru, Nilsson et al. (2006)

Ni II (2014)