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Gold and US sectoral stocks during COVID-19 pandemic

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ARTICLE INFO

JEL classification:
C58
G11
Z30

Keywords:
Stocks
Hedging effectiveness
COVID-19 pandemic

ABSTRACT

In this study, we examine the hedging relationship between gold and US sectoral stocks during the COVID-19 pandemic. We employ a multivariate volatility framework, which accounts for salient features of the series in the computation of optimal weights and optimal hedging ratios. We find evidence of hedging effectiveness between gold and sectoral stocks, albeit with lower performance, during the pandemic. Overall, including gold in a stock portfolio could provide a valuable asset class that can improve the risk-adjusted performance of stocks during the COVID-19 pandemic. In addition, we find that the estimated portfolio weights and hedge ratios are sensitive to structural breaks, and ignoring the breaks can lead to overestimation of the hedging effectiveness of gold for US sectoral stocks. Since the analysis involves sectoral stock data, we believe that any investor in the US stock market that seeks to maximize risk-adjusted returns is likely to find the results useful when making investment decisions during the pandemic.

1. Introduction

The literature on the response of financial markets, including the stock market, to the COVID-19 pandemic is fast growing, owing to its grave consequences. Several studies have examined the impact of the pandemic on financial markets (see for example, Ali et al., 2020; Al-Awadhi et al., 2020; Baig et al., 2020; Haroon and Rizvi, 2020a,b; He et al., 2020; Li et al., 2020; Narayan et al., 2020a,b; Mishra et al., 2020; Phan and Narayan, 2020; Prabheesh et al., 2020; Salisu and Akanni, 2020; Salisu et al., 2020a,b; Salisu and Sikiru, 2020; Salisu and Vo, 2020; Sharma, 2020; Zhang et al., 2020; Sikiru and Salisu, 2021; among others) and the evidence suggests a negative impact; consequently, the need to hedge against the risk associated with the pandemic becomes crucial. This is the motivation for our study. In response to this challenge, we consider gold to be a potential asset that can serve as a good hedge for stocks against the pandemic risk. The pioneering studies on the gold-stocks nexus (see for instance, McDonald and Solnik, 1977; Sherman, 1979).
1982; Jaffe, 1989; Chua et al., 1990) indeed support the inclusion of gold in the equities portfolio for the benefits of portfolio diversification and downside risk management.\textsuperscript{3,4} This continues to be emphasised in the recent literature with pieces of evidence of negative or low correlation of gold in the investment portfolio containing stocks (see for example, Joy, 2011; Reboredo, 2013; Beckmann et al., 2015; Bredin et al., 2015). This strand of the literature also finds support in the conceptual arguments, which suggest stock market hedging qualities of gold when its return is shown to be negative or uncorrelated with the stocks prices (or returns) (see Baur and Lucey, 2010; Baur and McDermott, 2011; Zagaglia and Marzo, 2013).\textsuperscript{5} In the class of traditional hedging assets, Shahzad et al. (2020), while not particularly considering the COVID-19 pandemic, have shown that gold offers more effective hedging benefits for G7 stock indices.

During pandemics, the search for alternative, safe assets is more critical than it is during tranquil periods, given the associated high uncertainties and the need to minimize downside investment risks (see Reboredo and Ugolini, 2017; Godil et al., 2020). The second motivation for situating the study in the context of the COVID-19 pandemic is hinged on previous incidences that have shown that stock market fundamentals were influenced by the SARS & Ebola Virus pandemics (see Chen et al., 2009; Ichev and Marinč, 2018). The third comes on the heels of the negative impacts of the COVID-19 pandemic on the global stock indices\textsuperscript{6} and the US in particular (see Akhtaruzzaman et al., 2020; Ji et al., 2020; Shehzad et al., 2020) for relevant statistics showing that the major US indices (the DJIA and S&P 500) dropped by around 30 % and the stock market hit four historic circuit breakers during this period). The fourth motivation is against the backdrop of the literature, which suggests that the ability of gold to function as a justifiable hedge may be constrained during crises when the stock market volatility is exceptionally high,\textsuperscript{7} which is currently observed to be the case as a result of the COVID-19 pandemic (see Hood and Malik, 2013; Baumöhl and Lyocsa, 2017; Shehzad et al., 2020).

This study focuses on the US sectoral stocks due to the pre- eminent posture of the US in the global economy and its highly developed financial market which attracts international investors to seek solace during periods of high market volatility (see for instance, Forbes, 2010; Gau and Wu, 2017; Yunus, 2020). This is theoretically argued in the International Capital Asset Pricing Model (I-CAPM), which allows investors to move their investments across national boundaries in search of international portfolio diversification in response to crises in one or more domestic markets (Guesmi and Nguyen, 2014; Adewuyi et al., 2019). Further, the sectoral analysis of stocks is important in the search for diversification benefits because of information transmission and diffusion of policy decisions across different classes of assets and markets (see Ciner et al., 2013; Baumöhl and Lyocsa, 2017). Further motivation for sectoral analysis emanates from the arguments of Haroon and Rizvi (2020b) in their sectoral analysis of effects of panic news on stocks, where they observe that aggregation hinders heterogeneous profiling of stock market fundamentals. Hence, sectoral analysis may reveal that the different sectors behave differently to the hedging behaviour of gold (see Akhtaruzzaman et al., 2020).\textsuperscript{8}

In line with the extant literature on hedging, we construct a multivariate generalized autoregressive conditional heteroscedastic (MGARCH), which allows for time-variation in the analysis of hedging relationship (see for example, Arouri and Nguyen, 2010; Arouri et al., 2011a,b, 2012; Salisu and Mobolaji, 2013; Salisu and Oloko, 2015). Since there are alternative variants of the MGARCH model, we conduct relevant preliminary tests to determine the appropriate model. In addition to the outcome of these tests, the chosen methodology tends to offer superior hedging effectiveness performance relative to other competing models such as Vector Autoregressive model and its variants (see Lypny and Powalla, 1998; Lee et al., 2005; Sultan and Hasan, 2008; Yang and Lai, 2009).

Next to this background, we offer some preliminary analyses in Section 2 to determine the appropriate model for analyses; In Section 3, we evaluate the relative hedging effectiveness of gold for stock in order to mitigate the risk associated with the COVID-19 pandemic, while Section 4 concludes the paper.

2. Methodology

2.1. Data and pre-tests

In line with our study objectives, our data for sectoral stocks for the US and gold prices cover the period January 02, 2019 to July 27, 2020. The sample period is partitioned into three: (i) full sample, (ii) pre-COVID, and (ii) post-COVID. The pre-COVID sample covers the period before the emergence of COVID-19, that is, between January and December, 2019; while the COVID sample covers the period since the outbreak of the COVID-19 pandemic, starting from January 2020. The full sample on the other hand combines both the pre- COVID and during COVID samples.

The sectoral stocks are captured using the Standard and Poor’s (S&P) 500 sectoral stock indices, which consist of eleven primary stock sectors: Basic Materials, Consumer discretionary, Consumer staples, Energy, Financials, Health care, Industrials, Information

\textsuperscript{3} See relevant theoretical justification in the Capital Asset Pricing Models (Tobin, 1958; Markowitz, 1959; Ross, 1976).

\textsuperscript{4} A review of relevant studies on the gold-stocks hedging relationship is well documented in Shahzad et al. (2020).

\textsuperscript{5} In addition to gold serving stock market hedging purposes, gold aids policy makers in their efforts at financial stability by keeping gold reserves to defend the domestic currency (see Mensi et al., 2015).

\textsuperscript{6} A recent paper by Al-Awadhi et al. (2020) on the Chinese stock market shows that growth in COVID-19 reported cases and deaths negatively affects stock returns of companies.

\textsuperscript{7} Other justification is that increased speculation in gold during this period could destroy its hedging power (see Baur and Glover, 2012).

\textsuperscript{8} Generally, studies have shown that the response of sectoral stocks to macroeconomic fundamentals or risks may differ (see Bampinas and Panagiotidis, 2016; Rooyen and Jones, 2019) and therefore, using the aggregate stocks will not only undermine this salient attribute of sectoral sectors but may also lead to wrong conclusions about the response of stocks to the hedging potential of gold market.
Technology, Real estate, Telecommunication, and Utilities. Each of the indices measures the performance of the stocks of US firms in each of the sectors under consideration. In addition to the sectoral classification, we also include the overall S&P500 index to evaluate the hedging effectiveness of gold on the overall equity. Daily data on the sectoral stock series are freely downloadable from the www.investing.com online database, while data on gold prices is obtained from the Federal Economic Reserve Database (https://fred.stlouisfed.org/series). Start and end periods are January 02, 2019 and July 17, 2020 respectively.

The descriptive statistics (mean and standard deviation) for the considered series and their returns are summarized in Table 1. While the mean values are positive for virtually all the sectors with the exception of energy sector over the full sample, however, they are only positive for the non-essential consumer goods and services (i.e. consumer discretionary), health care, materials, and technology sectors during the covid-19 period. By implication, the average returns in the four latter sectors suggest improved performance during the COVID-19 period, while the remaining seven sectors, including the tourism sector on the average experienced decline in their stock performance since the outbreak of the pandemic.

In addition, the standard deviation, which depicts how volatile the stock return series are, shows that the oil & gas sector stocks returns exhibit more volatility than all other sectors while both the health care and telecommunication sectors have the least standard deviation values, and thus less volatile stock returns. Additionally, we offer some graphical evaluation of the co-movements between gold and each of the sectoral stock indices (see Fig. 1) and they show evidence of a shift in their trends after the outbreak of the pandemic. This further validates the need to conduct distinct analyses for the pandemic period in order to fully understand its

![Fig. 1. Co-movements between gold and sectoral stock indices.](image_url)

### Table 1
Descriptive statistics for gold and stock returns.

| Sectoral stock returns | Mean | Standard Deviation |
|------------------------|------|--------------------|
|                        | Full sample | Pre-Covid | During-Covid | Full sample | Pre-Covid | During-Covid |
| Consumer discretionary  | 0.0918 | 0.0890 | 0.0882 | 1.7241 | 0.9093 | 2.6094 |
| Consumer staples       | 0.0528 | 0.0873 | -0.0019 | 1.4503 | 0.6796 | 2.2434 |
| Energy                | -0.1063 | 0.0212 | -0.3384 | 2.8996 | 1.2072 | 4.5564 |
| Financials            | 0.0005 | 0.0991 | -0.1804 | 2.3220 | 0.9703 | 3.6471 |
| Health care           | 0.0564 | 0.0737 | 0.0250 | 1.6013 | 0.8424 | 2.4263 |
| Industrials           | 0.0285 | 0.0929 | -0.0978 | 2.0488 | 0.9875 | 3.1504 |
| Information technology| 0.1386 | 0.1560 | 0.0966 | 2.0860 | 1.1394 | 3.1316 |
| Materials             | 0.0532 | 0.0770 | 0.0203 | 1.9733 | 0.9869 | 3.0186 |
| Real estate           | 0.0380 | 0.0979 | -0.0581 | 2.0663 | 0.7844 | 2.8383 |
| Telecom services      | 0.0174 | 0.0123 | 0.0221 | 1.6805 | 0.9684 | 2.4888 |
| Utilities             | 0.0347 | 0.0871 | -0.0479 | 1.9727 | 0.7186 | 3.1472 |
| S&P 500               | 0.0647 | 0.1006 | -0.0040 | 1.7706 | 0.7878 | 2.7615 |
| Gold                  | 0.0941 | 0.0563 | 0.1593 | 1.0381 | 0.7902 | 1.4508 |

Note: The stock returns series for the different sectors are used in the computation of the descriptive analyses.

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9 This is the most recent coverage at the time of preparing the first draft of this article.
10 All the data are transformed to returns series in the main analysis as a way of ensuring stationarity of the series.
Table 2  
Conditional Heteroscedasticity, Autocorrelation and Asymmetry Tests (Full sample)\(^a\).

| Conditional Heteroscedasticity and Autocorrelation | Asymmetry and CCC | Model Choice |
|---------------------------------------------------|-------------------|--------------|
| ARCH LM (5) | ARCH LM (10) | LB(5) | LB(10) | LB\(^2\)(5) | LB\(^2\)(10) | Sign bias | Negative bias | Positive bias | Joint bias | E-S test |
| Gold | 13.22*** | 10.14*** | 4.70 (0.32) | 23.25*** | 93.48*** | 209.9*** | 0.890 | 0.574 | 0.232 | 0.840 | 0.003 | Asymmetric |
| SP500 | 26.83*** | 17.25*** | 17.66*** | 73.10*** | 193.3*** | 362.7*** | 2.438** | 0.472 | 0.446 | 9.418** | (0.998) | CCC |
| Consumer discretionary | 32.25*** | 23.85*** | 19.07*** | 64.05*** | 160.5*** | 248.6*** | 2.268** | 0.571 | 0.271 | 7.784* | 0.043 | Asymmetric |
| Consumer staples | 28.04*** | 23.03*** | 23.37*** | 73.88*** | 217.8*** | 418.5*** | 0.820 | 0.574 | 0.909 | 7.965** | 0.024 | CCC |
| Energy | 16.10*** | 11.59*** | 12.32** | 64.36*** | 189.2*** | 0.890 | 0.574 | 0.232 | 0.840 | 0.003 | Asymmetric |
| Financials | 27.84*** | 15.03*** | 21.78*** | 75.12*** | 262.9*** | 433.3*** | 0.820 | 0.574 | 0.909 | 7.965** | 0.024 | CCC |
| Health care | 36.40*** | 25.11*** | 18.17*** | 76.06*** | 265.6*** | 539.0*** | 1.284 | 1.035 | 0.750 | 7.965** | 0.024 | CCC |
| Industrials | 35.45*** | 22.61*** | 20.19*** | 75.78*** | 275.4*** | 477.7*** | 2.415 | 0.422 | 0.820 | 0.909 | 0.024 | CCC |
| Information technology | 19.06*** | 13.90*** | 5.24 (0.26) | 49.25*** | 142.6*** | 282.3*** | 2.869*** | 0.843 | 0.084 | 10.68** | 0.002 | Asymmetric |
| Materials | 26.47*** | 16.39*** | 21.48*** | 75.22*** | 204.6*** | 368.0*** | 1.472 | 0.401 | 0.109 | 4.298 | 1.518 | CCC |
| Real estate | 29.58*** | 16.15*** | 36.96*** | 70.71*** | 205.1*** | 328.3*** | 2.483*** | 0.202 | 0.834 | 7.057* | 2.703 | Asymmetric |
| Telecom services | 18.04*** | 11.11*** | 6.64 (0.16) | 43.39*** | 134.2*** | 217.6*** | 3.131*** | 0.923 | 0.499 | 11.57*** | 0.106 | Asymmetric |
| Utilities | 75.40*** | 48.57*** | 42.15*** | 97.26*** | 496.6*** | 819.4*** | 2.412** | 0.066 | 0.206 | 9.076** | 0.140 | Asymmetric |

Note: The ARCH LM tests refer to the Engle (1982) test for conditional heteroscedasticity while the LB and LB\(^2\) imply the Ljung-Box tests for autocorrelations involving the standardized residuals in levels and squared standardized residuals respectively. The null hypothesis for the ARCH LM test is that the series has no ARCH effects (that is, it is not volatile) while LB test for null hypothesis is that the series is not serially correlated; ES test denotes the Engle-Sheppard constant conditional correlation (CCC) \(\chi^2\) test; the computed probability values are in parentheses.  
\(^a\) The results of these pre-tests for pre-covid and covid samples are not reported here for want of space but could be provided upon request.
peculiarities relative to the period before it and possible hedging options to mitigate its adverse effects on the stock markets.

As a precondition in standard empirical research, we conduct some pre-tests to validate our choice of multivariate volatility model, on the one hand and whether to allow for constant or dynamic correlation as well as asymmetric effect in the model, on the other hand. These tests include the serial correlation, which is carried out using the Ljung-Box Q-statistics and the conditional heteroscedasticity using the ARCH-LM test. In addition, we evaluate whether asymmetric effects exist, as well as the constant conditional correlation tests. The asymmetry test is carried out using the Engle and Ng sign and bias tests, while the Engle-Sheppard test is used to evaluate the presence or otherwise, of constant conditional correlation (CCC). The results are summarised in Table 2. The ARCH-LM tests indicate the rejection of the null hypothesis of no ARCH effects for all the series under consideration, implying that the stock returns exhibit conditional heteroscedasticity; hence, capturing such effects is essential when modelling their returns. Complementarily, the Ljung-Box tests also confirm the presence of serial correlation in the return series for all the sectors and therefore the inclusion of lagged terms of the return series in the mean and variance equations (as demonstrated in the immediate section) is justified.

The Engle-Ng sign and joint sign bias tests which evaluate whether there is evidence of significant asymmetric effects in the relationship between gold and sectoral stock returns are also summarised in Table 2. Both tests confirm significant asymmetric effect for the overall US stocks using the S&P 500 index. In addition, six sectors of the eleven sectoral categorisation reveal evidence of statistically significant asymmetric effects. These sectors are: consumer discretionary, health care, information technology, real estate, telecommunication services, and utilities. On the other hand, the five other sectors (consumer staples, energy, financials, industrials and materials) exhibit symmetric effects. The Engle-Sheppard test is not significant across all the sectors except health care and by implication, the assumption of constant conditional correlations between each of the sectoral stocks and gold stock is valid. On the other hand, the health care stock returns exhibit a dynamic conditional correlation with gold stock returns and same is captured in the return series in the mean and variance equations (as demonstrated in the immediate section) is justified.

Lastly, we account for structural breaks in the volatility analysis to enhance the model precision. A number of studies have suggested the need to account for structural breaks in addition to controlling for volatility when dealing with high frequency series such as those used in this paper (see Narayan and Liu, 2011, 2015; Salisu et al., 2016; Salisu and Adeleke, 2016). The assumption that GARCH processes are stationary may cause problems during periods where structural breaks are present, which can render the GARCH assumptions invalid (Babikir et al., 2012). Besides, failure to account for such breaks has grim consequences, and can particularly lead to sizeable upward biases in the degree of persistence in estimated GARCH models.\textsuperscript{11} The effects of ignoring structural breaks have been found to affect the optimal weights, hedge ratios and hedge effectiveness (see Babikir et al., 2012; Mongi and Dhouha, 2016). Therefore, we account for structural breaks by following a three-step procedure. First, we determine the presence of structural breaks in each of the series using the Bai and Perron (2003) multiple break tests. The number of breaks and break dates for each of the series is summarized in Table 3 for full sample, pre-covid sample and covid sample. The second step requires regressing each of the sectoral stocks and gold return series on dummy variables constructed for the identified break dummies, that is, \( r_{it} = \theta + \sum_{j=1}^{N} \tau_j D_{ij} + \nu_{it} \) where \( D_{ij} = 1 \) for each \( j \) and zero otherwise, where \( j \) is the number of breaks up to \( N \). In the third step, we determine the break-adjusted returns \( (r_{it}^D) \) which is estimated as \( r_{it}^D = r_{it} - \left( \hat{\theta} + \sum_{j=1}^{N} \hat{\tau}_j D_{ij} \right) \) or simply \( r_{it}^D = \tilde{\nu}_{it} \). The estimated break-adjusted return series \( (r_{it}^D) \) is thereafter

\textsuperscript{11} For robustness purposes, we estimated the appropriate model VARMA GARCH model for each of the US sectoral stock returns while ignoring structural breaks. The estimated optimal portfolio weights and hedge ratios are provided in the appendix section (Tables A1 and A2). We find that ignoring structural breaks may over-estimate the optimal weights and hedging effectiveness of gold for US stocks.
used in the returns and volatility modelling as discussed in the next section.

3. The model and results

3.1. The model

One of the prominent instruments for modelling interdependencies among financial time series with and without asymmetric shock effects in the empirical literature is the VARMA–GARCH\textsuperscript{12} model (see Salisu and Mobolaji, 2013; Salisu and Oloko, 2015; Caporale et al., 2017). We employ the VARMA-CCC-GARCH model and the DCC variant model (Ling and McAleer, 2003), following the results of the preliminary tests discussed in the preceding section. The preference for the model lies in its ability to capture both the symmetric and asymmetric effects that could exist in the asset returns, which structurally the CCC\textsuperscript{13} model, including its dynamic variant (the DCC model), may not capture (McAleer et al., 2009).\textsuperscript{14} The mean equations for the gold and stock series are respectively given as:

\begin{align}
  r_t^G &= \phi^G + \delta^G r_{t-1}^G + \lambda^G r_{t-1}^S + \epsilon_t^G \\
  r_t^S &= \phi^S + \delta^S r_{t-1}^S + \lambda^G \epsilon_{t-1}^G + \epsilon_t^S
\end{align}

(1)

(2)

where \(r_t^G\) and \(r_t^S\) are return series, with \(G\) and \(S\) denoting gold and sectoral stocks, respectively. The parameter \(\phi\) denotes the constant term and \(\delta\) is for the lagged own-return series and \(\lambda\) denotes the coefficient on the lagged cross-returns and measures cross-return spillovers between the two markets; \(\epsilon_t\) is for the identically distributed errors while the superscripts denote gold and sectoral stocks, respectively. The parameter \(\rho\) denotes the constant correlations. The conditional variance and covariance estimates are crucial for the computation of the optimal weights and hedge ratios. The optimal portfolio weight (OPW) establishes the proportion of an asset pair that could form an investment portfolio to ensure optimality. For example, the significant volatility spillover between gold returns and any of the sectoral stock returns is an indication that investment in both assets is volatile and susceptible to risk and uncertainty. To circumvent or reduce such risks, investors need to engage in hedging, by investing in future contracts while not jeopardising their expected returns. In line with the works of Kroner and Ng (1998); Arouri et al. (2011b); Salisu and Mobolaji (2013) and Salisu and Oloko (2015), the optimal portfolio weight of holding the two assets in an investment portfolio is constructed using the conditional variance and covariance estimates as given in Eqs. (3) and (4) and it could be expressed as:

\begin{equation}
  \sigma^G_{GS,j} = \frac{h_t^G - h_t^{GS}}{h_t^G - 2h_t^{GS} + h_t^S} 
\end{equation}

(6)

and,

\begin{equation}
  \sigma^G_{GS,j} = \begin{cases} 
  0, & \text{if } \sigma^G_{GS,j} < 0 \\
  \sigma^G_{GS,j}, & \text{if } 0 < \sigma^G_{GS,j} \leq 1 \\
  1, & \text{if } \sigma^G_{GS,j} > 1 
\end{cases}
\end{equation}

(7)

\textsuperscript{12} VARMA-GARCH denotes Vector Autoregressive Moving Average-Generalized Autoregressive Conditional Heteroscedasticity.

\textsuperscript{13} CCC denotes Constant Conditional Correlations

\textsuperscript{14} Ling and McAleer (2003) provide the estimation procedure, including the structural and statistical properties of the model which covers both the necessary and sufficient conditions. Returns, shock and volatility spillovers are evaluated using conditional mean and conditional variance equations specified within a bivariate framework (see also Salisu and Oloko, 2015).

\textsuperscript{15} The asymmetric version of the model includes own asymmetric effects as part of the independent variables in Eqs. (3) and (4) and this is given as \(r_t^G \epsilon_{t-1}^G + r_t^S \epsilon_{t-1}^S\) for gold and stock conditional variance equations, respectively.
where $\omega_{GS}^*$, $t$ denotes the weight of gold asset in a one-dollar gold/stock combination in an investment portfolio at time $t$. The term $h_{GS}^*$ is the conditional covariance between the gold and stock returns at time $t$. Consequently, the optimal weight of the gold stocks in the two assets class considered can be evaluated using 1

\[ \omega_{GS}^*, t \]

In addition, we construct the optimal hedge ratio (OHR) following Kroner and Sultan (1993), who accordingly considered a portfolio of two assets and concluded that the risk of the investment portfolio is minimised if a long position of one dollar in stocks can be hedged by a short position of $\alpha_t$ dollars in the gold stock. The formulation of the OHR between gold and stock returns is defined as:

\[ \alpha_{GS}^*, t = \frac{h_{GS}^*}{h_G^*} \]  

where $\alpha_{GS}^*, t$ is the optimal hedge ratio between gold and each of the sectoral sectors. The estimated results are discussed in the next section. However, given our objective of evaluating the hedging effectiveness of the sector stocks, we only report results for the optimal portfolio weights and hedge ratios between gold and stock returns.

### 3.2. Results

Our objective is to evaluate the effectiveness of gold as a hedge or safe haven for US sectoral stocks, particularly during pandemics. It has been well established in the literature that gold is an effective diversifier for financial assets including common stocks. In line with the proposition of Kumar (2014), the risk in taking a long position in stock assets can be offset by taking a short position in an alternative asset such as gold. The optimal portfolio weights and hedge ratios are summarised in Tables 4 and 5 respectively. Both the portfolio weights and hedge ratios are obtained using the estimates of the conditional variance and covariance from the estimation of the main model. The estimated optimal portfolio weights show positive portfolio weights of gold assets in a portfolio combination of

\[ \begin{array}{c|c|c|c}
& \text{Full sample} & \text{Pre-Covid} & \text{During-Covid} \\
\hline
\text{S&P 500} & 0.2755 & 0.3953 & 0.2864 \\
\text{Consumer discretionary} & 0.2919 & 0.4475 & 0.1835 \\
\text{Consumer staples} & 0.4109 & 0.6441 & 0.4746 \\
\text{Energy} & 0.1489 & 0.5026 & 0.1161 \\
\text{Financials} & 0.3037 & 0.4727 & 0.3678 \\
\text{Health care} & 0.3186 & 0.4346 & 0.6330 \\
\text{Industrials} & 0.3241 & 0.3842 & 0.1889 \\
\text{Information technology} & 0.2507 & 0.4484 & 0.2136 \\
\text{Materials} & 0.2373 & 0.2394 & 0.4484 \\
\text{Real estate} & 0.2723 & 0.5363 & 0.1794 \\
\text{Telecom services} & 0.3095 & 0.3958 & 0.2025 \\
\text{Utilities} & 0.3759 & 0.5239 & 0.2915 \\
\end{array} \]

Notes: The table reports average optimal portfolio weights in a gold-stock asset portfolio.

\[ \begin{array}{c|c|c|c}
& \text{Full sample} & \text{Pre-Covid} & \text{During-Covid} \\
\hline
\text{S&P 500} & -0.3204 & -0.2480 & -0.0064 \\
\text{Consumer discretionary} & -0.3333 & -0.2285 & -0.2141 \\
\text{Consumer staples} & 0.0357 & 0.0081 & 0.0987 \\
\text{Energy} & -0.4417 & 0.1287 & 0.0130 \\
\text{Financials} & -0.3817 & -0.3297 & -0.0830 \\
\text{Health care} & 0.1011 & -0.2398 & -0.2057 \\
\text{Industrials} & -0.2287 & -0.3344 & -0.1065 \\
\text{Information technology} & -0.3457 & -0.2032 & -0.1708 \\
\text{Materials} & -0.2315 & -0.2317 & 0.0174 \\
\text{Real estate} & 0.1597 & 0.1409 & -0.0048 \\
\text{Telecom services} & -0.2524 & -0.2431 & -0.1506 \\
\text{Utilities} & 0.1881 & 0.1886 & 0.1779 \\
\end{array} \]

Notes: The table reports average optimal hedge ratios in a gold-stock asset portfolio.

\[ \begin{equation}
\alpha_{GS}^*, t = \frac{h_{GS}^*}{h_G^*}
\end{equation} \]  

The results of VARMA-GARCH models are not reported here for want of space but could be made available upon request.
gold and stock assets. For example, the estimated results show that for the overall US stocks (S&P 500), the optimal portfolio weight is 0.2755; however for the sub-samples, we find that in a unit of gold-stock portfolio, the proportion of gold to be held in such portfolio combination is about 39.53% before the outbreak of COVID-19 but declined to about 28.6% afterwards (during the pandemic).

The optimal portfolio weights during-COVID period are less than the pre-COVID era (see Table 4). However, the OPW differs across sectors for the three sample periods considered, supporting the arguments that different sectors behave differently to the gold hedging (see Akhtaruzzaman et al., 2020). For example, while 37% of gold/stock portfolio should be invested in financial stocks during-COVID period, the energy sector should attract just about 12%. The remaining 63% and 88% of the portfolio are expected to be invested in gold for the financial and energy sectors respectively. While the results show that gold has continued to perform its traditional role as a safe haven against decline in US stocks, the optimal portfolio weights may not be unconnected with the increase in stock market volatilities brought about as a result of the pandemic which could have eroded investors’ confidence, and increased uncertainties (Justin, 2020). These uncertainties in the market environment may have further left investors unsure how to respond to the unprecedented shocks and delay in their investment rebalancing options to curtail the risks associated with volatile markets.

Similar to our findings, Baur and Lucey (2010) empirically establish that during extreme stock market conditions such as the 2007/2008 global financial crisis and in volatile periods such as during war, gold market still acts as a safe haven for equities. In addition, Ciner et al. (2013) using time rolling regressions to investigate time-varying safe-haven relations, also find the safe-haven status of gold versus US equities between 1990 and 2010 to range between 18% and 89%, with the average value at 59%.

The optimal hedge ratios in a gold - US stock portfolio combination are summarised in Table 5. The estimated hedge ratios show negative values between gold returns and US stock returns, both at aggregate and sectoral levels. As established in Baur and Lucey (2010), the negative correlation between two assets within a given portfolio indicates hedging. However, as similar to the optimal portfolio weight results discussed above, the optimal hedge ratios also show that the hedging effectiveness of gold for stocks declined (in absolute term) during the COVID-19 period across all the sectors considered relative to those obtained for the pre-covid sample. These findings corroborate the similar diminishing effectiveness of gold against US stocks reported in Kumar (2014) and Shrydeh et al. (2019). For instance, Kumar (2014) finds that a stock-gold portfolio provides better diversification benefits than holding just stock portfolios. On the other hand, Shrydeh et al. (2019) suggest that gold hedging effectiveness against US stocks tends to diminish during a crisis era. Besides, a hedge may sometimes not retain the property of minimizing losses in periods of market turbulence since it may exhibit a positive correlation with another asset during such periods.

4. Robustness

As a robustness check, we extend the empirical analyses by evaluating the hedging effectiveness of gold for the US sectoral stocks before and after the declaration of COVID-19 as a global pandemic. The World Health Organisation (WHO) declared COVID-19 a pandemic on March 11, 2020, following its alarming spread and severity across countries (WHO, 2020). Addressing the media in his opening remarks, the WHO Director-General emphasised one of the implications of declaring the virus as a pandemic is that it can stoke up fear and panic. Therefore, we categorized the COVID-19 sample period into epidemic and pandemic periods. The estimated optimal portfolio weights and optimal hedge ratios are summarised in Table 6.

Notes: OPW indicates average optimal portfolio weights, while OHR denotes the optimal hedge ratios in a gold-stock asset portfolio. Epidemic period denotes the periods before the COVID-19 was declared as a global pandemic by the WHO, while pandemic period is the period after the declaration.
The OPW results confirm the main estimation results using the COVID-19 sample. The analysis using the post-pandemic declaration data further supports our main findings that gold provides a safe-haven against declining stock performance, although the performance is mixed across different sectors. Besides, the optimal hedge ratios support the main estimation that gold provides effective hedge for US stocks during the epidemic period. However, the performance diminishes in the pandemic period as previously noted. Overall, the results provide supportive evidence of gold effectiveness as a suitable hedge for US stocks, although the magnitude and unprecedented nature of COVID-19 reveal a reduction in the hedging performance between the epidemic and pandemic periods.

5. Conclusion

The main objective of this study is to examine the portfolio designs and hedging effectiveness in gold and US aggregate and sectoral stocks, especially with the outbreak of COVID-19. In the paper, both the symmetric and asymmetric versions of the VARMA-CCC-GARCH model, determined based on formal pre-tests, are used to estimate the conditional variance and covariances required for the hedging analysis. We evaluate the impact of the COVID-19 pandemic, partitioning the full data into the pre-covid and covid samples. We also test and account for structural breaks, a presence of which could lead to sizeable upward biases in the degree of persistence in estimated GARCH models and the overestimation of the portfolio weights and hedging effectiveness. Overall, our results suggest that including gold in a stock portfolio could provide a valuable asset class that can improve stock risk-adjusted-performance. Our findings further suggest that the shocks associated with the unprecedented emergence of COVID-19 may have increased investors’ uncertainties in responding to market shocks, leading to delay in their investment rebalancing options. This is reflected with the declining optimal portfolio weights and hedge ratios in the crisis period, with further empirical support in the robustness check, wherein we partitioned the COVID-19 sample into epidemic and pandemic samples. Finally, we believe that our findings will have a far-reaching impact, given the fact that we utilize sectoral stock data covering virtually all the sectors of the US economy. Therefore, any investor in the US stock market seeking to maximize risk-adjusted returns is likely to find the results useful when making investment decisions during the pandemic. Future studies that extend our analysis to other precious metals will further enrich the literature on the subject.

Author contributions

Afees A. Salisu: Conceptualization, Methodology, Formal Analysis, Software, Writing - Original Draft, Reviewing & Editing.
Xuan Vinh Vo: Conceptualization, Data curation, Results validation, Reviewing & Editing, Funding acquisition, Project administration.
Brian Lucey: Conceptualization, Results validation, Reviewing & Editing, Supervision, Project administration.

Declaration of Competing Interest

The authors declare that there are no conflicts of interest.

Acknowledgments

The authors wish to acknowledge the helpful suggestions received from the anonymous reviewers and the guest editor for the special issue on COVID FIN MKTS. The funding received from the University of Economics Ho Chi Minh City with the paper reference IBR_RF155 is acknowledged and appreciated. The usual disclaimer applies.

Appendix A

Table A1

|                         | Full sample | Pre-Covid | Post-Covid |
|-------------------------|-------------|-----------|------------|
| S&P 500                 | 0.3698      | 0.5037    | 0.2947     |
| Consumer discretionary  | 0.3181      | 0.4662    | 0.1894     |
| Consumer staples        | 0.5505      | 0.5322    | 0.4948     |
| Energy                  | 0.1972      | 0.1953    | 0.1034     |
| Financials              | 0.3512      | 0.4441    | 0.3739     |
| Health care             | 0.4156      | 0.4379    | 0.3902     |
| Industrials             | 0.3640      | 0.3789    | 0.2565     |
| Information technology  | 0.2208      | 0.4417    | 0.2082     |
| Materials               | 0.3163      | 0.5136    | 0.3525     |
| Real estate             | 0.4307      | 0.5388    | 0.2075     |
| Telecom services        | 0.3397      | 0.3793    | 0.3286     |
| Utilities               | 0.3458      | 0.5267    | 0.3032     |

Notes: The table reports average optimal portfolio weights in a gold-stock asset portfolio.
Table A2
Optimal hedge ratios between gold and stocks returns (before SB).

|                    | Full sample | Pre-Covid | Post-Covid |
|--------------------|-------------|-----------|------------|
| S&P 500            | -0.2518     | -0.1526   | -0.0768    |
| Consumer discretionary | -0.3080     | -0.2171   | -0.1944    |
| Consumer staples    | 0.0213      | 0.0223    | 0.0899     |
| Energy             | -0.3873     | -0.5693   | -0.0406    |
| Financials         | -0.3174     | -0.3609   | 0.0959     |
| Health care        | -0.0753     | -0.2399   | 0.1428     |
| Industrials        | -0.2333     | -0.3279   | -0.1639    |
| Information technology | -0.3089    | -0.2185   | -0.1220    |
| Materials          | -0.1656     | -0.1592   | 0.0474     |
| Real estate        | 0.1247      | 0.1692    | -0.0192    |
| Telecom services   | -0.2317     | -0.2224   | -0.0500    |
| Utilities          | 0.2035      | 0.1855    | 0.2088     |

Notes: The table reports average optimal hedge ratios in a gold-stock asset portfolio.

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