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Excluding Light Gluinos from $Z$ decays

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Abstract

We reanalyze the constraints on light gluinos ($m_{\tilde{g}} \leq 5$ GeV/$c^2$) from the hadronic $Z$ decays into four jets. We find that the published OPAL data from the 1991 and 1992 runs exclude a light gluino with mass $\lesssim 1.5$ GeV/$c^2$ at more than 90% confidence level. This limit depends little on assumptions about the gluino fragmentation and the definition of the gluino mass. The exclusion confidence level is shown as a function of the mass. A future projection is briefly discussed. We also discuss quantitatively how the distributions in the Bengtsson-Zerwas and the modified Nachtmann-Reiter angles change due to the finite bottom quark or gluino mass.

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Supersymmetry is one of the primary targets of extensive searches at various collider experiments, most importantly at CERN $e^+e^-$ collider LEP and Fermilab $p\bar{p}$ collider Tevatron [1]. Negative searches at these and previous colliders have already put significant constraints on the parameter space of low-energy supersymmetry. However, a light gluino below the few GeV mass range has surprisingly weak experimental constraints as emphasized recently by various authors [2, 3, 4] (see, however, an opposing view [5]). It is an extremely important task to verify or exclude a gluino in this light window experimentally. While the Tevatron Run II is expected to extend the reach of heavy gluinos up to a few hundred GeV, little effort is devoted to definitively exclude or verify the light gluino window. On the other hand, a careful reexamination of the existent data may reveal an overlooked constraint on a light gluino; this is our motivation to study the existent data in detail.

We reanalyzed published data on $Z$ decays into four jets [6, 7, 8, 9, 10, 11], and find that they already exclude a gluino lighter than 1.5 GeV/$c^2$ at more than 90% confidence level. Since the published results use only 1991 and 1992 data, it is conceivable that the currently available data, if analyzed properly, could put a much more significant constraint on a light gluino. We hope our result urges the experimental groups to analyze the whole data set including a possible light gluino.

Let us briefly review the existent constraints on a light gluino (see [3, 12] for more details). The negative searches at beam dump experiments have excluded a light gluino which decays inside the detector into photino, which in turn interacts with the neutrino detector. However, a gluino tends to leave the detector without decaying if the squark mass is above a few hundred GeV/$c^2$ [13, 14]. Even if the gluino decays, the photino interacts very weakly in this case and cannot be detected. If the gluino does not decay, it forms bound states such as gluinoball $\tilde{g}\tilde{g}$, glueballino $\bar{g}\bar{g}$ or baryon-like states, especially $uds\bar{g}$ [15]. Other states are likely to decay into these neutral bound states, and searches for exotic charged hadrons may not apply unless a charged gluino bound state decays only weakly. One the other hand, the mass region above 1.5 GeV/$c^2$ and below 4 GeV/$c^2$ is excluded from quarkonium decay $\Upsilon \rightarrow \gamma \eta_g$, where $\eta_g$ is the pseudo-scalar gluinoball, independent of the gluino lifetime [16, 3]. Whether the bound extends to lower masses is controversial because of the applicability of perturbative QCD calculations [16]. The mass range above 4 GeV/$c^2$ is expected to give a shorter lifetime and is excluded by a negative search for events with missing energy at UA1
The authors of [18] claim that the limit from UA1 extends down to 3 GeV/c². In any case, the least constrained region is the mass range below 1.5 GeV/c², where the gluino is relatively stable so that it does not decay inside detectors. This is our window of interest in this letter.

We would like to emphasize that the best method to exclude the gluino mass range below 1.5 GeV/c² is to use inclusive processes rather than searching for specific bound states with certain decay modes. The latter search would heavily depend on assumptions such as the mass spectrum of various gluino bound states and their decay modes and decay lifetimes. One would have to design experiments and put constraints with all possible theoretical assumptions on gluino bound states in order to exclude the light gluino definitively. On the other hand, the constraints would be much less sensitive to theoretical assumptions if they were based on inclusive processes where perturbative QCD is applicable. There are several possibilities pointed out in the literature along this line. The most popular one is to study the effect of light gluinos in the running of the QCD coupling constant αs. It was even pointed out that the values of αs from higher energy measurements tend to be higher than those extrapolated from lower energies using QCD with the ordinary quark flavors, and the data actually prefer the existence of a light gluino to compensate the slight discrepancy [2, 19, 20]. However, this issue remains controversial [21, 22, 23]. Even though the discrepancy between low-energy and high-energy measurements is diminishing [24], still the data are not precise enough to exclude or verify a light gluino definitively. The second one is its effect on the Altarelli–Parisi evolution of the nucleon structure functions [25, 26]. Unfortunately the effect is too small to be tested using the present experimental data. It might be that the more recent HERA data could improve the situation, but making a definite statement on the existence of a light gluino appears to be difficult. The third one is to study the angular correlations in so-called “3+1” jet events at HERA [27]. However, the effect of the light gluino was found to be negligible. The final one which we employ in this letter is the study of four jet correlations in e⁺e⁻ collisions [28, 23, 29]. Previous studies did not find significant constraints, but given the size of the current LEP data, we find this to be the most promising direction.

The only data we use in this letter are studies of QCD color factors [9, 10, 11]. The experimental groups at LEP have performed impressive analyses of the hadronic Z decays into four jets, extracting QCD color factors C_A/C_F and T_F/C_F [30] from jet angular distributions, to confirm SU(3) as
the QCD gauge group and five light quark flavors. The angular distributions of $q\bar{q}q\bar{q}$ final state differ from those of $q\bar{q}gg$, where $q$ refers to a generic quark and $g$ to a gluon. Three angles are commonly used in four-jet analyses: the Bengtsson–Zerwas (BZ) angle $\chi_{BZ}$ [31], the modified Nachtmann–Reiter (NR) angle $\theta'_{NR}$ [32], and the opening angle of the two less energetic jets $\alpha_{34}$. If there exists a light gluino $\tilde{g}$, the final state $q\bar{q}g\tilde{g}$ also contributes to the $Z$ decays into four jets. The angular distributions of $q\bar{q}g\tilde{g}$ would be identical to those of $q\bar{q}q\bar{q}$. Therefore, a possible light gluino would change the extracted $T_F/C_F$ but not $C_A/C_F$. Apart from the mass effects, $T_F/C_F$ should increase by a factor of $(5 + 3)/5$, because the gluino is a color-octet and counts effectively as three additional massless quarks. Note that these analyses do not use the overall rate of four-jet events since it is sensitive to the choice of $\alpha_s$ in the absence of next-leading order calculations. So far the experimental analysis which used the highest statistics is the one by OPAL [11], which also briefly discussed constraints on a light gluino. They found that the light gluino is barely outside the 68% confidence level contour and decided the data did not put a significant constraint.

However, we find the previous analyses not carefully designed to study the effect of a light gluino because of the following reason. When one discusses a possible light gluino, QCD with the color group SU(3) should be assumed. Given overwhelming experimental evidences of QCD, it is not wise to, for instance, vary the number of colors $N_c = 3$ when one studies the effect of a particle (light gluino) added to QCD. Therefore, we must fix the QCD color factor $C_A/C_F$ to be that of the SU(3) group, $9/4$. Second, we already know that there are five quark flavors $u, d, s, c$ and $b$, which appear in $Z$ hadronic decays. When one puts constraints on an additional contribution from a light gluino, one should not vary the number of flavors below 5, or equivalently, $T_F/C_F$ below $3/8$. The only LEP paper which analyzed data in a way close to this spirit, and put an upper bound on possible additional $q\bar{q}q\bar{q}$-type final states, is the one from OPAL [7]; but it used very limited statistics. All more recent papers [9, 10, 11] varied both $C_A/C_F$ and $T_F/C_F$ without constraints. By reanalyzing data with these constraints we can put a much more significant bound on a light gluino than reported. Actually, fixing the group to be SU(3) ($C_A/C_F = 9/4$) has the greatest impact on the confidence level, while restricting $T_F/C_F \geq 3/8$ has a much smaller effect (actually it makes the significance worse). We further include the finite mass of the bottom quark in the analysis which slightly improves the significance.
Figure 1: Extracted QCD color factors from the OPAL analysis [11]. The shown $\chi^2$ values correspond to 39.3%, 68% and 95% confidence levels with two degrees of freedom. We impose the constraint $C_A/C_F = 9/4$ (vertical solid line) and limit ourselves to the unshaded region ($T_F/C_F \geq 3/8$) in order to put constraints on a possible light gluino contribution to the four-jet events from $Z$ decays. See the text for more details.

Overall, a massless gluino is excluded already better than at 90% confidence level by the OPAL 1991 and 1992 data only [11].

Let us start from the reported contour on the $C_A/C_F$, $T_F/C_F$ plane, shown in Fig. 1. We fix $C_A/C_F = 9/4$ because of the philosophy of our study stated above. Since one-dimensional $\chi^2$ distributions have much higher confidence levels than two-dimensional ones, this change improves the significance of the data drastically. From their $\chi^2$ contours, we minimized $\chi^2$ with fixed $C_A/C_F = 9/4$, and defined $\Delta \chi^2$ relative to the $\chi^2$ at the minimum ($T_F/C_F = 0.36$). The confidence levels are calculated using a one-dimensional $\chi^2$ distribution with $\Delta \chi^2$ defined in this manner. This is a conservative choice because $\Delta \chi^2 < \chi^2$. We obtain $T_F/C_F = 0.36 \pm 0.15$ with fixed $C_A/C_F$. If one had used this central value and the standard deviation, a massless gluino would be excluded at 95% confidence level. However, we
also need to impose another constraint, \( T_F/C_F \geq 3/8 \), which can be easily taken into account. The standard method is to use the Gaussian distribution only in the physical region, and scale the normalization of the distribution so that the total probability in the physical region becomes unity. Since the central value is very close to the theoretical value of the QCD, this effectively increases the probability of allowing light gluinos by a factor of two; numerically the confidence level is 88%.

Finally, we study the effect of the finite mass of the bottom quark and gluinos on the extracted \( T_F/C_F \). The authors of [33] studied the effect of the finite mass of quarks on the four-jet rates. They also looked at the angular distributions and reported there were little changes. Even though it is true that the distributions do not change drastically, they gradually become similar to those of \( q\bar{q}gg \) final state as one increases the mass of the quark, and hence the extracted \( T_F/C_F \) from the fit to the distributions has a relatively large effect due to the finite mass of the bottom quark. The papers [9, 10] do not take this effect into account at all. The OPAL experiment [11] used parton level event generators by the authors of [33] and [29] to study the effect. They have found a surprisingly large effect: the bottom quark contribution to \( T_F/C_F \) was about one half of a massless quark at \( y_{cut} = 0.03 \). We confirmed their estimate in a detailed parton-level calculation based on that done in [34], neglecting the interference between primary and secondary quarks. This approximation is known to be better than a few percent. On the other hand, this approximation has the clear advantage of enabling us to distinguish primary and secondary quarks unambiguously. Our code employs helicity amplitude technique using the HELAS package [35], which made it straight-forward to incorporate finite masses in the four-jet distributions.

The finite mass affects the extracted \( T_F/C_F \) in two ways. First, the rate of producing secondary massive quarks is suppressed compared to the massless case as shown with the solid line in Fig. 2. For instance, there is about 20% suppression with \( m_q = 5 \text{ GeV}/c^2 \) and \( y_{cut} = 0.03 \). This result is consistent with [33]. The mass of the primary quark has little effect on the rate: only a 6% suppression for \( m_q = 5 \text{ GeV}/c^2 \). We also checked that the distributions in BZ and NR angles with a massive primary quark are indistinguishable from the massless case. These observations are consistent with naive expectations, because the primary quarks are much more energetic than the secondary ones and hence the mass effect is suppressed by \( m^2/E^2 \). We therefore neglect the finite mass of primary quarks hereafter. Second, the NR and BZ angle
distributions gradually approach those of the $q\bar{q}gg$ final state as one increases the mass of the secondary quarks. We are not aware of detailed analyses of these distributions with massive quarks in the literature. The distributions are shown in Fig. 3 normalized so that the total area below the curve is unity, in order for the effect on the rate and that on the distribution to be clearly separated. We fit the distributions as linear combinations of $q\bar{q}gg$ and massless $qqqq$ distributions to determine the effective TFICF, in order to mimic the experimental analyses. The fit is surprisingly good; we checked this for quark masses between 0 and 5 GeV/$c^2$. Combined with the reduction in the rate, the net effect of the finite mass of secondary quarks is shown in Fig. 2. With $m_b = 5$ GeV/$c^2$ for secondary bottom quarks, the overall rate of $q\bar{q}b\bar{b}$ final state is reduced to 82.5%, while the fit to angular distributions gives a $T_F/C_F$ reduced to 76.4% (BZ) or 85.5% (NR) compared to that of a massless quark flavor (3/8), on top of the reduction in the rate. In total, secondary bottom quarks contribute to $T_F/C_F$ as $3/8 \times 0.630$ or $3/8 \times 0.705$, which is not a negligible suppression. The extracted $T_F/C_F$ from the data is an average of $T_F/C_F$ from five flavors. The reported $T_F/C_F$ in [11] includes a
Figure 3: The distributions in BZ and NR angles of the $q\bar{q}q\bar{q}$ final state where the secondary quark has a mass of 5 GeV/c$^2$. They can be fit extremely well as a linear combination of massless $q\bar{q}q\bar{q}$ and $q\bar{g}gg$ distributions. We used $y_{\text{cut}} = 0.03$ and $\sqrt{s} = m_Zc^2$.

correction to compensate the apparent suppression due to the finite bottom quark mass. Such a correction in turn effectively enhances the additional contribution from gluinos by a factor of $5/(4 + 0.630)$ or $5/(4 + 0.705)$. Note that this slight enhancement effect does not change significantly even when one varies $m_b$ from 4 to 5 GeV/c$^2$, as can be seen in Fig. 2.

The actual OPAL analysis [11] fits the data in the three dimensional space spanned by BZ, NR and $\alpha_{34}$ angles after bin-by-bin systematic corrections from Monte Carlo simulations. Such an analysis is beyond the scope of this letter. We assume that the total effect of the finite mass is somewhere between the effects on BZ or NR angles since $\alpha_{34}$ is not as effective in extracting $T_F/C_F$. As it is clear from Fig. 3, fits to distributions of massive quarks give apparent additional contributions to $q\bar{g}gg$ and hence $C_A/C_F$. They are completely negligible, however, compared to the size of the true $q\bar{g}gg$ which is about one order of magnitude larger than the sum of all $q\bar{q}q\bar{q}$ final states, and hence we will neglect such contributions hereafter.

Given the above considerations, we can now present the exclusion confidence levels on a light gluino for varying gluino masses in Fig. 4. For both
curves, we used $m_b = 5$ GeV/$c^2$ and used the effective $T_F/C_F$ extracted from the fits to BZ and NR angles. The finite mass effect of the gluino is treated in the same manner. First of all, it is clear that the finite mass effect which we studied depends little on the choice of BZ or NR angles, and hence we believe it mimics the true experimental fits (which use BZ, NR and $\alpha_{34}$ angles simultaneously in a three-dimensional fit with 295 bins) quite well. Second, the confidence level is extremely flat up to 2 GeV/$c^2$. This implies that we do not need to worry about complication due to non-perturbative dynamics in defining the gluino mass [36]. The lower bound of $\simeq 1.5$ GeV/$c^2$ at 90% confidence level is already in the perturbative region. It is quite likely that the gluino mass relevant to this analysis is a running mass defined at the scale $Q^2 \sim y_{\text{cut}} m_Z^2$ [37]. It is then straightforward to convert the bound to the on-shell gluino mass: the lower bound of $\tilde{m}_\tilde{g}(0.03m_Z^2) = 1.5$ GeV/$c^2$ in the $\overline{\text{MS}}$ scheme corresponds to $m_{\text{pole}}(\tilde{g}) = 2.8$ GeV/$c^2$.

We would like to comment that the clever jet reconstruction method used in the OPAL analysis [11] is particularly suited for the study of light gluinos in four-jet events. They did not scale the measured jet energies by an overall ratio $E_{\text{vis}}/m_Z$, as done traditionally in similar analyses, but instead used the
angular information of the jets to calculate the energy of each jet using energy and momentum conservation. This method avoids uncertainties in the gluino fragmentation. Since it is not well understood how a gluino fragments, one should use a similar method to avoid dependence on assumptions about the gluino fragmentation in future studies.

One may worry that the lack of next-leading-order calculations makes the interpretation of the bound somewhat ambiguous. We do not believe that higher order corrections can modify the angular distributions of $q\bar{q}gg$ to exactly mimic additional contributions from $q\bar{q}q\bar{q}$-type, and cause a systematic bias in the extracted $T_F/C_F$. The excellent agreement between the matrix element calculation and data found in [11] supports this claim; next-leading-order calculations are, however, necessary to justify it. It is also desirable to compare different Monte Carlo programs, while only JETSET was used in recent experimental papers [9, 10, 11].

Finally, it is worth emphasizing that the result in this letter is based on the 1991 and 1992 OPAL data with 1.1M hadronic Z's [11]. The statistical and systematic uncertainties are comparable in their paper. Given the current size of the LEP data, which is more than an order of magnitude larger, the statistical uncertainty should reduce substantially once all of the data has been analyzed. This change alone could drastically improve the sensitivity to the light gluino in four-jet events. On the other hand, it is not obvious how systematic uncertainties can be further reduced. The largest systematic uncertainty originates in the bin-by-bin acceptance corrections which needed to be done before performing a fit in BZ, NR, and the opening angle space. It is not clear how this uncertainty can be reduced if one employs the same method. Perhaps choosing larger values of $y_{\text{cut}}$ reduces the uncertainty while reducing the statistics at the same time. There could be an optimal choice of $y_{\text{cut}}$ for this particular purpose. Some of the other large systematic uncertainties are specific to the OPAL experiment and could be reduced by averaging results from all four experiments. In any case, there is no doubt that we can expect a better result from the currently available data set.

In summary, we reanalyzed the published OPAL 1991 and 1992 data on the QCD color factors [11] to constrain possible additional contributions to four-jet events in $Z$ decays due to $q\bar{q}g\bar{g}$ final states. The main difference from the original OPAL study is to fix $C_A/C_F = 9/4$ as required by QCD. We further imposed $T_F/C_F \geq 3/8$ and treated the finite mass effects of both the bottom quark and the gluino carefully. We find that a light gluino with
a mass below 1.5 GeV/c² is excluded at better than 90% confidence level. The result is insensitive to assumptions about the gluino fragmentation, its lifetime, what bound state it forms, and the definition of its mass. We believe that the currently available data set is much more sensitive to a possible additional contribution from the light gluino. As a by-product of this analysis, we discussed the effect of finite bottom quark mass on BZ and NR distributions in detail, which is not negligible when extracting QCD color factors at current precisions.

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[37] We thank J. Ellis for discussions on this point.
