Abstract: In this work, the photochemical treatment of a real municipal wastewater using a persulfate-driven photo-Fenton-like process was studied. The wastewater treatment efficiency was evaluated in terms of total carbon (TC), total organic carbon (TOC) and total nitrogen (TN) removal. Response surface methodology (RSM) in conjunction Box-Behnken design (BBD) and multilayer artificial neural network (ANN) have been utilized for the optimization of the treatment process. The effects of four independent factors such as reaction time, pH, $K_2S_2O_8$ concentration and $K_2S_2O_8/Fe^{2+}$ molar ratio on the TC, TOC and TN removal have been investigated. The process significant factors have been determined implementing Analysis of Variance (ANOVA). Both RSM and ANN accurately resulted in complete mineralization of TOC at the reaction time of 106.06 min, pH of 7.7, persulfate concentration of 30 mM and $K_2S_2O_8/Fe^{2+}$ molar ratio of 7.5 for RSM and at the reaction time of 104.93 min, pH of 7.7, persulfate concentration of 30 mM and $K_2S_2O_8/Fe^{2+}$ molar ratio of 9.57 for ANN. On the contrary, the attempts to find the optimal conditions for the maximum TC and TN removal using statistical, and neural network models were not successful.

Keywords: photo-Fenton-like process; municipal wastewater; persulfate oxidation; response surface methodology; Box-Behnken design; artificial neural network

1. Introduction

Municipal wastewater (MWW) is the second limitless source of water [1]. MWW mostly contains water (99.9%) with relatively small concentrations of suspended and dissolved organic and inorganic solids [2]. MWWs usually contain around 5% to 10% settleable suspended solids. They also contain approximately 1000 parts per million of dissolved and colloidal solids, most of which are organic in nature and usually difficult to remove with biological treatment [3]. The following organic compounds are present in MWW: carbohydrates, synthetic detergents, fats, proteins, lignin, soaps and their decomposition products, various natural and synthetic organic chemicals from the process industries [2]. Some of these compounds pose serious problems in biological treatment systems due to their resistance to biodegradation and/or toxic effects on microbial processes [4,5]. Municipal wastewater also comprises different inorganic substances from domestic and industrial sources, including several potentially toxic elements such as arsenic, cadmium, lead, mercury, etc. In addition, pathogenic viruses, bacteria, protozoa and helminths may be present in raw municipal wastewater and survive in the environment for long periods [6].
Recently, the effluents from municipal wastewater treatment plants (WWTPs) have been identified as a major source of emerging micropollutants, such as hormones, pharmaceuticals, and personal care products [7]. Despite their low concentration (from a few ng/L to several µg/L), they are resistant to biodegradation, since conventional WWTPs cannot provide a high rate of removal of micropollutants [8]. Strategies for removing these compounds from MWW are currently being discussed [9].

Advanced Oxidation Processes (AOPs) have been widely applied for the treatment of municipal wastewater [4]. AOPs using highly reactive hydroxyl radical (OH·) as the main oxidant were first proposed for the treatment of drinking water in the 1980s. Then AOPs were widely used to treat various types of wastewater since strong oxidants can easily degrade persistent organic contaminants and remove inorganic pollutants from wastewater [10].

In recent years, a new type of oxidizing agent has attracted the interest of researchers. \( \text{S}_2\text{O}_8^{2−} \) is a strong oxidizing agent with a standard oxidation potential \( (E^o) \) of 2.01 V [11]. It can form more powerful sulfate radicals \( \text{SO}_4^{•−} \) \( (E^o = 2.6 \text{ V}) \) after activation by heat, ultraviolet (UV) irradiation (Equation (1)), transition metals (Equation (2)), or elevated pH, and further initiate sulfate radical-based AOPs [12,13]. The mechanisms of activation of persulfate with elevated pH are still unclear [14]. The temperature for the thermal activation of persulfate ranges from 35 to 130 °C [14].

\[
\text{S}_2\text{O}_8^{2−} + \text{hv} \rightarrow 2\text{SO}_4^{•−} \tag{1}
\]

\[
\text{S}_2\text{O}_8^{2−} + \text{Fe}^{2+} \rightarrow \text{SO}_4^{•−} + \text{SO}_2^{−} + \text{Fe}^{3+} \tag{2}
\]

As seen in Equations (1) and (2), the metal activation method gives only a 50% yield of sulfate radicals, which is obtained by heating or UV-activated persulfate method with the same molar concentration of persulfate. Consequently, the metal activation method is theoretically ineffective. The most commonly used metals include ferrous (Fe (II)) and ferric (Fe (III)) ions [15].

Sulfate radicals, like hydroxyl radicals, are highly reactive species with a short lifetime, although both radicals have different reaction patterns. Hydroxyl radicals have a tendency to attach to C=C bonds or remove H from C–H bonds during their reactions with organic substances [16], while sulfate radicals tend to remove electrons from organic molecules, which are consequently converted into organic radical cations [10]. In addition, hydroxyl radicals can be generated from sulfate radicals via Equations (3)–(5) [17–19].

\[
\text{SO}_4^{•−} + \text{S}_2\text{O}_8^{2−} \rightarrow \text{SO}_2^{−} + \text{S}_2\text{O}_8^{•−} \tag{3}
\]

\[
\text{SO}_4^{•−} + \text{H}_2\text{O} \rightarrow \text{SO}_2^{−} + \text{H}^+ + \text{HO}^* \tag{4}
\]

\[
\text{SO}_4^{•−} + \text{OH}^− \rightarrow \text{SO}_2^{−} + \text{HO}^* \tag{5}
\]

Moreover, Equation (5) demonstrates that more hydroxyl radicals can be produced from sulfate radicals at alkaline conditions [10]. Unlike hydrogen peroxide \( (\text{H}_2\text{O}_2) \), persulfate can also oxidize some organic substances directly, without the participation of radical species [20].

Potassium persulfate (KPS) \( (\text{K}_2\text{S}_2\text{O}_8) \) has good stability at room temperature, it is inexpensive, and solid at ambient temperatures, making it easy to store and transport [21]. The technical benefits of persulfate-AOP over \( \text{H}_2\text{O}_2 \)-AOP include: (i) lower storage and transportation costs as a result of the availability of persulfate salts, (ii) higher achievable yields of radical formation, (iii) less dependence of the treatment efficiency on operating parameters, such as pH, initial peroxide loading, background constituents, and (iv) a wider range of available persulfate activation methods [20].

Velo-Gala et al. [19] studied the effectiveness of oxidation processes based on the application of UV radiation, UV/\( \text{H}_2\text{O}_2 \) and UV/\( \text{K}_2\text{S}_2\text{O}_8 \), for the degradation of sodium
diatrizoate in the aqueous medium. The UV/K$_2$S$_2$O$_8$ process was found to be more efficient than the UV/H$_2$O$_2$ system, with higher rate constants [19].

Yang et al. [22] investigated sulfate-based oxidation technologies for the defluorination of aqueous perfluorooctanesulfonate (PFOS). The defluorination efficiency of PFOS with different treatments corresponded to the following order: HT (hydrothermal)/K$_2$S$_2$O$_8$ > UV/K$_2$S$_2$O$_8$ > Fe$^{2+}$/K$_2$S$_2$O$_8$ > US (ultrasound)/K$_2$S$_2$O$_8$. The increase in the persulfate amount had a positive effect on the defluorination of PFOS [22].

Dbira et al. [23] found that the photo-Fenton process was more efficient for the tannic acid degradation in aqueous solution than the UV/persulfate system, concluding that hydroxyl radicals were stronger oxidizing agents than sulfate radicals.

Since iron-based heterogeneous catalysts activated with persulfate have received a lot of attention as a potentially advanced and sustainable water treatment system, Pervez et al. [24] employed a novel Fe$_3$O$_4$ impregnated graphene oxide (Fe$_3$O$_4$@GO)-activated persulfate (Fe$_3$O$_4$@GO+$K_2$S$_2$O$_8$) system for the efficient degradation of dye pollutants in real wastewater treatment.

Persulfate-based oxidation technologies were recently classified as realistic for full-scale application based on energy consumption values [25]. However, most of works have been conducted using synthetic wastewater or aqueous solutions [19,22,23], although real wastewaters include several inorganic (chlorides, bicarbonates, carbonates) and organic constituents that may have a scavenging effect on oxidative radicals [26]. Therefore, it is essential to examine the efficiency of the process in the case of real wastewaters.

The present study focused on the effectiveness of AOPs based on the application of iron salts, potassium persulfate, and UV radiation to treat real municipal wastewater. There are no published studies applying Fe$^{2+}$/S$_2$O$_8^{2-}$/UV process to treat wastewaters.

Response surface methodology (RSM) and artificial neural network (ANN) were used to optimize the photo-Fenton-like treatment of the MWW.

2. Results and Discussion
2.1. Regression Model Based on ANOVA

Table 1 shows the experimental design (Box-Behnken design) obtained from the software and the results of the experiments.

| Run | X1 | X2 | X3 | X4 | Molar Ratio | TC | TOC | TN | Predicted by RSM | Predicted by ANN |
|-----|----|----|----|----|-------------|----|-----|----|-----------------|-----------------|
| 1   | 60 | 5.35 | 30 | 10 | 10 | 56.35 | 45.79 | 9.42 | 54.77 | 46.43 | 34.86 | 56.33 | 46.19 | 9.43 |
| 2   | 100 | 3 | 30 | 10 | 10 | 50.80 | 27.98 | 10.87 | 48.18 | 34.35 | 15.79 | 50.73 | 27.75 | 11.37 |
| 3   | 140 | 5.35 | 20 | 7.5 | 7.5 | 60.69 | 58.06 | 6.97 | 57.54 | 60.27 | 26.40 | 60.67 | 58.23 | 6.98 |
| 4   | 100 | 3 | 10 | 7.5 | 10 | 68.35 | 53.03 | 6.35 | 65.51 | 58.62 | 30.66 | 68.28 | 53.17 | 6.52 |
| 5   | 140 | 3 | 20 | 10 | 10 | 58.50 | 46.89 | 6.63 | 64.53 | 52.78 | 14.46 | 58.65 | 46.58 | 6.28 |
| 6   | 140 | 5.35 | 30 | 10 | 10 | 71.31 | 73.9 | 10.05 | 63.57 | 65.80 | 15.49 | 71.29 | 73.83 | 10.03 |
| 7   | 100 | 5.35 | 20 | 10 | 10 | 50.96 | 55.74 | 35.66 | 47.52 | 55.87 | 45.65 | 47.77 | 55.96 | 45.62 |
| 8   | 100 | 3 | 20 | 10 | 10 | 39.86 | 76.27 | 5.07 | 37.30 | 69.55 | 12.25 | 39.82 | 76.12 | 5.07 |
| 9   | 100 | 5.35 | 20 | 10 | 10 | 47.17 | 59.64 | 46.13 | 47.52 | 55.87 | 45.65 | 47.77 | 55.96 | 45.62 |
| 10  | 60 | 5.35 | 20 | 7.5 | 7.5 | 68.24 | 46.06 | 8.13 | 64.30 | 49.37 | 28.64 | 68.04 | 46.81 | 8.07 |
| 11  | 60 | 3 | 20 | 10 | 10 | 65.61 | 24.68 | 39.52 | 66.28 | 25.72 | 26.26 | 65.55 | 24.81 | 39.47 |
| 12  | 60 | 5.35 | 10 | 10 | 10 | 57.39 | 56.96 | 21.4 | 63.29 | 57.82 | 17.70 | 57.59 | 56.56 | 21.51 |
| 13  | 140 | 5.35 | 20 | 10 | 12.5 | 61.69 | 63.61 | 53.35 | 60.46 | 59.94 | 44.94 | 61.37 | 63.21 | 53.32 |
| 14  | 100 | 7.7 | 20 | 10 | 10 | 46.36 | 72.34 | 11.49 | 46.99 | 74.68 | 39.83 | 46.28 | 72.12 | 11.30 |
| 15  | 100 | 3 | 20 | 7.5 | 7.5 | 60.63 | 37.45 | 46.66 | 58.16 | 38.51 | 20.06 | 60.61 | 37.27 | 46.68 |
| 16  | 140 | 7.7 | 20 | 10 | 10 | 49.32 | 67.99 | 21.08 | 55.67 | 68.90 | 20.50 | 49.34 | 67.85 | 21.07 |
| 17  | 100 | 3 | 20 | 12.5 | 10 | 57.51 | 55.8 | 51.61 | 58.75 | 52.85 | 54.42 | 57.50 | 55.57 | 51.56 |
| 18  | 100 | 5.35 | 20 | 10 | 10 | 44.44 | 52.23 | 55.15 | 47.52 | 58.57 | 45.65 | 47.77 | 55.96 | 45.62 |
Table 1. Cont.

| Run | Independent Variables | Time | pH | K₂S₂O₈, mM | Molar Ratio K₂S₂O₈/Fe²⁺ | X1 | X2 | X3 | X4 | Actual | Predicted by RSM | Predicted by ANN |
|-----|-----------------------|------|----|-------------|---------------------------|----|----|----|----|-------|------------------|------------------|
| 19  |                       | 100  | 7.7| 20          | 7.5                       | 55.07| 79.09| 33.43| 51.99| 85.45 | 32.36            | 55.01            |
| 20  |                       | 60   | 5.35| 20          | 12.5                      | 59.01| 55.83| 59.26| 56.98| 53.26 | 51.93            | 59.99            |
| 21  |                       | 100  | 5.35| 10          | 7.5                       | 46.11| 60.96| 23.24| 48.80| 55.44 | 45.31            | 51.99            |
| 22  |                       | 100  | 5.35| 30          | 12.5                      | 44.19| 53.94| 57.89| 48.52| 56.41 | 45.31            | 55.03            |
| 23  |                       | 60   | 7.7 | 20          | 10                        | 56.21| 60.96| 23.24| 48.80| 55.44 | 21.98            | 55.01            |
| 24  |                       | 100  | 5.35| 30          | 7.5                       | 44.19| 53.94| 57.89| 48.52| 56.41 | 45.31            | 55.03            |
| 25  |                       | 140  | 5.35| 10          | 10                        | 51.47| 65.26| 51.53| 51.21| 56.03 | 27.83            | 51.49            |

The outcome of the experiments was predicted using a second-order quadratic polynomial model [27], which was based on the relation between responses and variables (Equation (6)):

\[ Y = \beta_0 + \sum_{i=1}^{k} \beta_i x_i + \sum_{i<j}^{k} \beta_{ij} x_i x_j + \sum_{j=1}^{k} \beta_{jj} x_j^2 + \epsilon \]  

where \( Y \) is the outcome variable (TC, TOC, and TN removal, %); \( \beta_0 \) is a constant coefficient; \( \beta_i \) is a linear regression coefficient; \( \beta_{ij} \) is a quadratic regression coefficient; \( \beta_{jj} \) is an interactive regression coefficient; \( x_i \) and \( x_j \) are the coded variables; \( \epsilon \) is the random error.

The BBD models for TC, TOC, and TN removals obtained from Design-Expert software are presented in the following Equations (7)–(9):

TC removal (\%) = 251.2 - 1.743A - 15.09B - 8.20D + 0.00601A² + 0.683B² + 0.0106C² + 0.428D² + 0.0006A × B + 0.01305A × C + 0.0256A × D + 0.409B × C - 0.238B × D - 0.104C × D \hspace{1cm} (7)

TOC removal (\%) = -44.7 + 0.800A + 15.23B - 3.54C + 5.1D - 0.00114A² + 0.454B² + 0.0604C² + 0.384D² - 0.1105A × B + 0.01238A × C - 0.0105A × D + 0.499B × C - 1.068B × D - 0.281C × D \hspace{1cm} (8)

TN removal (\%) = -210 + 1.76A + 26.4B + 6.64C + 2.5D - 0.00767A² - 2.46B² - 0.0940C² + 0.74D² + 0.038A × B - 0.0184A × C - 0.012A × D + 0.368B × C - 1.14B × D - 0.288C × D \hspace{1cm} (9)

where A, B, C, and D represent reaction time (min), pH, K₂S₂O₈ concentration (mM), and K₂S₂O₈/Fe²⁺ molar ratio, respectively. According to the analysis of variance (ANOVA) for the response surface model, B, A², BC terms for TC removal, and A, B, C², AB, BC, CD terms for TOC removal were significant in equations (Figure S1). No terms for TN removal were considered significant due to the lack of fit of the model.

The normal probability versus residuals for TC, TOC, and TN removals are presented in Figure 1a–c, respectively. They show that the data for all three models follow approximately the normal probability distribution. The actual and predicted data (obtained from BBD models) for TC, TOC, and TN removals are shown in Figure 2a–c, respectively. According to these figures, there is a good agreement between actual and predicted data for TC and TOC removal. However, a straight line pattern cannot be observed in Figure 2c, which suggests that the regression quadratic model is not suitable for the TN removal.
Figure 1. Normal probability vs. internally studentized residuals values for (a) TC removal, (b) TOC removal, and (c) TN removal.

Figure 2. RSM predicted vs. actual values for (a) TC removal, (b) TOC removal, and (c) TN removal.
2.2. ANOVA Analysis

The adequacy of the model for TC, TOC, and TN removal by the photo-Fenton-like treatment was checked using the Analysis of Variance (ANOVA). The analysis includes the calculation and assessment of regression coefficients ($R^2$), $F$- and $p$-values. The results of ANOVA are summarized in Table 2.

Table 2. ANOVA results of the quadratic polynomial model for the photo-Fenton-like process of municipal wastewater.

| Removal | Source       | Sum of Squares | Degrees of Freedom | Mean Square | F-Value | $p$-Value |
|---------|--------------|----------------|--------------------|-------------|---------|-----------|
| TC      | Model        | 1344.37        | 14                 | 96.03       | 2.84    | 0.039     |
|         | Error        | 405.90         | 12                 | 33.83       |         |           |
|         | Lack of fit  | 384.45         | 10                 | 38.45       |         |           |
|         | Pure error   | 21.44          | 2                  | 10.72       |         |           |
|         | $R^2 = 0.7681$ |               |                    |             |         |           |
| TOC     | Model        | 6659.09        | 14                 | 475.65      | 11.64   | <0.0001   |
|         | Error        | 490.32         | 12                 | 40.86       |         |           |
|         | Lack of fit  | 462.84         | 10                 | 46.28       |         |           |
|         | Pure error   | 27.48          | 2                  | 13.74       |         |           |
|         | $R^2 = 0.9314$ |               |                    |             |         |           |
| TN      | Model        | 4664.4         | 14                 | 333.17      | 0.70    | 0.739     |
|         | Error        | 5697.3         | 12                 | 474.77      |         |           |
|         | Lack of fit  | 5507.3         | 10                 | 550.70      |         |           |
|         | Pure error   | 190.3          | 2                  | 95.14       |         |           |
|         | $R^2 = 0.4502$ |               |                    |             |         |           |

Regression coefficients are important parameters in the models. The $R^2$ values for TC, TOC, and TN removal were 0.7681, 0.9314, and 0.4502, respectively. The high values of $R^2$ (close to one) show the adequacy of the model to fit the experimental data. $R^2$ values for TC and TOC were considered satisfactory. However, regarding the TN removal, only 45% of the total variation could be explained by the model.

Generally, the model predictions are considered statistically significant when $p$-values are less than 0.05, while $p$-values more than 0.1 demonstrate that the model does not fit well the experimental observations [27]. $p$-values of TC and TOC removals were 0.039 and <0.0001, respectively, which implies that the models used are significant for both response variables. On the contrary, the $F$-value of 0.7 and the $p$-value of 0.739 calculated for the TN removal indicate that the model is not suitable for the TN removal response.

Overall, considering the obtained ANOVA results, the application of the quadratic polynomial model described the process well and can be used to optimize the process in terms of TC and TOC removals.

2.3. Three-Dimensional Plots for the RSM Regression Model

Three-dimensional surface plots demonstrate the interaction between the variables on the response. The graphical representation of the regression models for TC, TOC, and TN removals are shown in Figures 3–5, respectively.
and <0.0001, respectively, which implies that the models used are significant for both response variables. On the contrary, the F-value of 0.7 and the p-value of 0.739 calculated for the TN removal indicate that the model is not suitable for the TN removal response. Overall, considering the obtained ANOVA results, the application of the quadratic polynomial model described the process well and can be used to optimize the process in terms of TC and TOC removals.

2.3. Three-Dimensional Plots for the RSM Regression Model

Three-dimensional surface plots demonstrate the interaction between the variables on the response. The graphical representation of the regression models for TC, TOC, and TN removals are shown in Figures 3–5, respectively.

Figure 3. 3D plots of TC removal as a function: (a) reaction time (min) and pH, (b) reaction time (min) and K$_2$S$_2$O$_8$ concentration (mM), (c) reaction time and K$_2$S$_2$O$_8$/$\text{Fe}^{2+}$ molar ratio, (d) pH and K$_2$S$_2$O$_8$ concentration (mM), (e) pH and K$_2$S$_2$O$_8$/$\text{Fe}^{2+}$ molar ratio, (f) K$_2$S$_2$O$_8$ concentration (mM) and K$_2$S$_2$O$_8$/$\text{Fe}^{2+}$ molar ratio.
Figure 3. 3D plots of TC removal as a function: (a) reaction time (min) and pH, (b) reaction time (min) and K$_2$S$_2$O$_8$ concentration (mM), (c) reaction time and K$_2$S$_2$O$_8$/Fe$_2^+$ molar ratio, (d) pH and K$_2$S$_2$O$_8$ concentration (mM), (e) pH and K$_2$S$_2$O$_8$/Fe$_2^+$ molar ratio, (f) K$_2$S$_2$O$_8$ concentration (mM) and K$_2$S$_2$O$_8$/Fe$_2^+$ molar ratio.

Figure 4. 3D plots of TOC removal as a function: (a) reaction time (min) and pH, (b) reaction time (min) and K$_2$S$_2$O$_8$ concentration (mM), (c) reaction time and K$_2$S$_2$O$_8$/Fe$_2^+$ molar ratio, (d) pH and K$_2$S$_2$O$_8$ concentration (mM), (e) pH and K$_2$S$_2$O$_8$/Fe$_2^+$ molar ratio, (f) K$_2$S$_2$O$_8$ concentration (mM) and K$_2$S$_2$O$_8$/Fe$_2^+$ molar ratio.
Figure 5. 3D plots of TN removal as a function: (a) reaction time (min) and pH, (b) reaction time (min) and K$_2$S$_2$O$_8$ concentration (mM), (c) reaction time and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio, (d) pH and K$_2$S$_2$O$_8$ concentration (mM), (e) pH and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio, (f) K$_2$S$_2$O$_8$ concentration (mM) and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio.

Figure 3a shows the interaction between the reaction time and pH with the TC removal as a response. It is obvious that the increase in both pH and reaction time slightly decreased the TC removal. According to Figure 3b, TC removal decreased from 57.39% to 51.47% with time at 10 mM K$_2$S$_2$O$_8$ and increased from 56.35% to 71.31% at 30 mM K$_2$S$_2$O$_8$. A similar pattern can be observed from Figure 3c where the TC removal decreased over
time in the low range and increased at the high range of molar ratio. The interaction between pH and K$_2$S$_2$O$_8$ is shown in Figure 3d. The increment in K$_2$S$_2$O$_8$ concentration at acidic pH led to poorer TC removal from 68.35% to 50.80%, while at neutral pH it showed opposite behavior, increasing the TC removal from 39.86% to 60.79%. Figure 3e indicates the interaction between pH and molar ratio, where TC removal decreased with the pH increment at both low and high molar ratios. Figure 3f illustrates the interaction of oxidant concentration and molar ratio on the TC removal. TC removal increased with the K$_2$S$_2$O$_8$ increment at low molar ratio and decreased at high molar ratio.

According to Figure 4a, TOC removal increased with reaction time at acidic conditions and decreased at neutral pH. As shown in Figure 4b, TOC removal slightly increased over time in low ranges from 56.96% to 65.26%, and sharply increased with time from 45.79% at 60 min to 73.90% at 140 min and 30 mM K$_2$S$_2$O$_8$. Figure 4c shows the effects of the reaction time and molar ratio of K$_2$S$_2$O$_8$/Fe$^{2+}$ on TOC removal. The TOC removal increased with time at any range and the molar ratio enhancement slightly increased the TOC removal. Figure 4d shows the interaction between the pH and K$_2$S$_2$O$_8$ concentration. In fact, the increase in pH enhanced the TOC removal at any range. The increase in K$_2$S$_2$O$_8$ concentration decreased the TOC removal from 53.03% to 27.98% at acidic pH and increased the TOC removal from 76.27% to 98.15% at neutral pH. According to Figure 4e, the effect of pH was more important than the effect of K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio on the TOC removal. The TOC removal increased with pH enhancement from 37.45% to 79.09% at the molar ratio of 7.5 and decreased with the molar ratio enhancement from 79.09% to 72.34% at neutral pH. Figure 4f illustrates the interaction of K$_2$S$_2$O$_8$ concentration and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio on the TOC removal. The increase of molar ratio increased the TOC removal from 60.96% to 66.90% at the K$_2$S$_2$O$_8$ concentration of 10 mM. On the contrary, the molar ratio enhancement at the K$_2$S$_2$O$_8$ concentration of 30 mM decreased the TOC removal from 76.10% to 53.94%.

As it can be seen from Figure 5a–f, the increase in the reaction time, pH, and K$_2$S$_2$O$_8$ concentration enhanced the TN removal up to the optimum point. Moreover, the increase in the molar ratio of K$_2$S$_2$O$_8$/Fe$^{2+}$ increased the TN removal at any range of the reaction time, pH, and K$_2$S$_2$O$_8$ concentration.

### 2.4. Effective Parameters on the Photo-Fenton Like Process

#### 2.4.1. Effect of Reaction Time

The effect of reaction time was different for TC, TOC, and TN removal. As shown in Figures 4 and 5, the reaction time increment enhanced the TOC and TN removal. This is because the oxidation of organic compounds requires time for completion. Afterward, the removal of TOC and TN decreased after 106 and 98 min, respectively. In contrast, TC removal decreased with increasing reaction time. TC is the sum of total organic carbon (TOC) and total inorganic carbon (TIC). The removal of TIC occurred simultaneously which possibly decreased the optimum time needed for TC removal to 60 min.

#### 2.4.2. Effect of pH

The pH is the one of the crucial factors in the photo-Fenton-like process. The oxidation of organic compounds and production of oxidative radicals are controlled by the pH. In this work, the highest removals were achieved at a pH of 5.35 for 71.31% TC removal and 60.13% TN removal, and a pH of 7.7 for 100% TOC removal. Unlike the photo-Fenton process where hydrogen peroxide acts as an oxidant, persulfate-driven oxidation is less dependent on pH adjustment as persulfates decrease the pH during the reaction. This creates optimal working conditions for Fe$^{2+}$ due to the increased solubility [28].

#### 2.4.3. Effect of K$_2$S$_2$O$_8$ Concentration and K$_2$S$_2$O$_8$/Fe$^{2+}$ Molar Ratio

The reactions that occur during the persulfate-driven photo-Fenton-like process are shown in Equations (1)–(5) [18,19]. Peroxodisulfate ions (S$_2$O$_8^{2-}$) can be activated by
UV light and Fe$^{2+}$ to produce sulfate radicals (SO$_{4}^{*-}$) (Equations (1) and (2)). Furthermore, sulfate radicals are well known to generate peroxodisulfate and hydroxyl radicals (Equations (3)–(5)).

According to ANOVA results, K$_2$S$_2$O$_8$ concentration and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio significantly affected TC and TOC removals. As shown in Figure 3f, K$_2$S$_2$O$_8$ concentration increment decreased the TC removal from 46.11% to 45.98% at a low molar ratio and from 54.74% to 44.19% at a higher ratio. Therefore, the optimal values for TC removal were 10 mM K$_2$S$_2$O$_8$ and 12.5 K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio. In contrast, the interaction of K$_2$S$_2$O$_8$ and molar ratio with TOC removal occurred differently. TOC removal increased with the K$_2$S$_2$O$_8$ concentration increment from 60.96% to 76.10% at a low molar ratio and decreased from 66.90% to 53.94% at a high molar ratio. The optimal TOC removal parameters were 30 mM K$_2$S$_2$O$_8$ and the molar ratio of 7.5. This behavior was due to the consumption of sulfate radicals by excessive iron ions, which resulted in the formation of Fe$^{3+}$ and SO$_4^{2-}$ (Equation (10)) [29].

$$\text{SO}_{4}^{*-} + \text{Fe}^{2+} \rightarrow \text{SO}_{4}^{2-} + \text{Fe}^{3+}$$  \hspace{1cm} (10)

2.5. Modeling of TC, TOC, and TN Removal by ANN

The multilayer feed-forward ANN was developed for modeling the photo-Fenton-like process, where the BBD experimental matrix was used to train the ANN. The network had 4 input layers (time, pH, K$_2$S$_2$O$_8$ concentration, and molar ratio) and three output nodes (TC, TOC, and TN removals). The best predictor model was determined by Equation (14), which combined root mean square error (RMSE) and regression coefficients ($R^2$). The optimal number of nodes in the hidden layer was 20 (Tables S1–S3).

The configuration with 20 nodes in the hidden layer had high values of $R^2$ (close to 1) and low values of RMSE. The values predicted using optimal ANN are presented in Table 1. As it can be seen from Figure 6, the variance between actual and ANN predicted values was very low, which means that the ANN model has fitted the experimental data.
Table 1. As it can be seen from Figure 6, the variance between actual and ANN predicted values was very low, which means that the ANN model has fitted the experimental data.

Figure 6. ANN predicted vs. actual values for (a) TC removal, (b) TOC removal, and (c) TN removal.

2.6. Optimization and Validation

The optimum conditions for TC, TOC, and TN removal were obtained by the RSM and ANN (Table 3).
Table 3. Optimum conditions found by RSM and ANN, and experimental validation for TC, TOC, and TN removals.

| Method | Removals, % | Reaction Time (min) | pH | K$_2$S$_2$O$_8$, mM | Molar Ratio K$_2$S$_2$O$_8$/Fe$^{2+}$ | Actual | Predicted | Error |
|--------|-------------|---------------------|----|---------------------|---------------------------------|--------|-----------|-------|
| RSM    | TC          | 60                  | 3  | 10                  | 12.5                            | 52.78  | 84.24     | 31.46 |
|        | TOC         | 106.06              | 7.7| 30                  | 7.5                             | 100    | 100       | 0     |
|        | TN          | 97.98               | 4.33| 15.05              | 12.5                            | 56.29  | 63.87     | 7.58  |
| ANN    | TC          | 140                 | 5.21| 30                  | 10.17                           | 49.56  | 71.38     | 21.82 |
|        | TOC         | 104.93              | 7.7 | 30                  | 9.57                            | 100    | 98.7      | 1.3   |
|        | TN          | 71.46               | 4.2 | 17.59              | 12.5                            | 45.74  | 72.83     | 27.09 |

The optimum conditions for TC, TOC, and TN removal were obtained by the RSM and ANN. The optimum conditions for 100% TOC removal found by RSM were at pH of 7.7, the reaction time of 106.06 min, the concentration of K$_2$S$_2$O$_8$ 30 mM and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio of 7.5, while ANN predicted 98.7% removal of TOC at pH of 7.7, the reaction time of 104.93 min, the concentration of K$_2$S$_2$O$_8$ 30 mM and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio of 9.57. Experiments were conducted at these conditions and as can be seen from Table 3, there is a good agreement between actual and predicted data for TOC removal. On the contrary, both methods were unable to accurately predict the optimal conditions for TC and TN removal. This is due to the lack of fit of the models for TC and TOC, where regression coefficients were smaller than 0.8.

Formic and acetic acids were determined using ion chromatography. The organic carbon of the intermediates (OC$_{intermediates}$) and the mineralized organic carbon (OC$_{CO_2}$) after the photo-Fenton-like process was calculated using the following Equations (11) and (12):

\[
OC_{intermediates} = \text{final}(\text{TOC}_{overall} - \text{TOC}_{formic acid} - \text{TOC}_{acetic acid})
\]  
\[
OC_{CO_2} = \text{initial}\text{TOC}_{overall} - \text{final}\text{TOC}_{overall}
\]  

Table S4 summarizes the results of the calculation of the intermediates. RSM and ANN optimized experiments achieved complete mineralization. Moreover, it can be seen that after run #17 (pH of 7.7, reaction time of 60 min, concentration of K$_2$S$_2$O$_8$ 20 mM and K$_2$S$_2$O$_8$/Fe$^{2+}$ molar ratio of 10), the organic carbon consisted of acetic acid only. Even though complete mineralization of TOC has not been achieved after run 17, these conditions could be favorable for the time and resource economy.

3. Materials and Methods

3.1. Wastewater Source and Characteristics

The real municipal wastewater used in this study was collected from the local wastewater treatment plant “Astana Su Arması” (Nur-Sultan city, Kazakhstan). Wastewater samples with a volume of 20 L were collected and stored in a refrigerator at 4 °C before conducting experiments and further analysis. Prior to experiments, MWW was filtered through a glass microfiber filter paper with a porosity grade of 0.7 μm (Whatman, Grade GF/F) under vacuum (Diaphragm vacuum pump KNF Laboport®, N 811). Characteristics of the real municipal wastewater are shown in Table 4. Around 83% of carbon was inorganic.
Table 4. Characteristics of the used wastewater (No. of samples = 3).

| Parameter                     | Unit    | Value       |
|-------------------------------|---------|-------------|
| Chemical oxygen demand (COD)  | mg L⁻¹  | 33.5 ± 1.5  |
| Total carbon (TC)             | mg L⁻¹  | 118.5 ± 2.2 |
| Total organic carbon (TOC)    | mg L⁻¹  | 20.77 ± 1.7 |
| Total inorganic carbon (TIC)  | mg L⁻¹  | 98.03 ± 2.32|
| Total nitrogen (TN)           | mg L⁻¹  | 37.49 ± 2.55|
| pH                            | –       | 7.75 ± 0.34 |

3.2. Reagents and Supplies

Potassium persulfate K₂S₂O₈ (ACS reagent, ≥99%) purchased from Sigma-Aldrich was utilized as a source of sulfate radicals. Ammonium iron(II) sulfate hexahydrate (ACS reagent, 99% w/w) received from Fisher Chemical was used as a source of ferrous ions. Hydrochloric acid solution (1 M) prepared from hydrochloric acid (ACS reagent, 37% w/w) supplied by Sigma-Aldrich was used for pH adjustment. All chemicals were applied without further purification.

3.3. Experimental Setup and Procedure

All experiments were conducted in a batch photochemical reactor (Toption Instrument Co., Ltd., Xi’an, China), which is shown in Figure 7. A lamp with 30 W power, located inside the photoreactor, emitted UV irradiation of 254 nm. At each run, 400 mL of the MWW was poured into the reactor, and desired amounts of iron salt and potassium persulfate were added. Depending on the required conditions, the initial pH of the MWW was adjusted by a 1 M hydrochloric acid solution. The treated solution was continuously stirred with a magnetic stirrer. The start of the experiment was considered with the switch-on of the UV lamp. Aliquots from the reaction mixture were taken at the end of the experiments and sent directly to the analysis.

Figure 7. The experimental setup.
3.4. Analytical Methods

The treatment efficiency was assessed via TC/TIC/TOC/TN analyses, pH, and COD measurements. The TC/TIC/TOC/TN analyses were carried out using the Multi N/C 3100 instrument by Analytik Jena AG (Jena, Germany). The pH of samples was measured using a WTW pH meter inoLab Multi 9310 IDS. The COD concentration was recorded using the Hach DRB 200 dry thermostat reactor and Hach DR 3900 spectrophotometer without RFID technology.

In addition, ion chromatography (IC, the 930 Compact IC Flex supplied by Metrohm, Herisau, Switzerland) was used to determine the concentrations of acetic and formic acids in the initial wastewater and final solutions.

All samples were filtered before analyses by the PVDF membrane filters with a pore size of 0.45 µm (Whatman, Maidstone, UK, diameter 25 mm). Prior to IC analysis, the poultry wastewater was filtered through Agilent Technologies premium syringe filters with a 0.2 µm RC membrane (25 mm diameter).

The removal efficiency was calculated using Equation (13):

\[
\text{Removal} (\%) = \frac{C_0 - C_t}{C_0} \times 100, \tag{13}
\]

where \(C_t\) and \(C_0\) are final and initial concentrations.

3.5. Modelling Using RSM

The Design-Expert statistical software (version 13) was applied for the statistical analysis and optimization of experiments. A four-factor with three-level Box-Behnken Design (BBD) in conjunction with the response surface methodology (RSM) was employed to maximize total carbon (TC), total organic carbon (TOC), and total nitrogen (TN) removal in municipal wastewater treatment. The affecting parameters on the reaction chosen as independent variables were the reaction time (A), pH (B), \(K_2S_2O_8/Fe^{2+}\) molar ratio (C), and concentration of \(K_2S_2O_8\). The TC, TOC, and TN removals were chosen as responses (dependent variables) (Table 5). Each factor was coded at three levels (from −1 to +1).

Minitab software (version 19) was used to construct Pareto chart.

| Table 5. Independent variables and their levels. |
|-----------------------------------------------|
| Symbol | Factor | Levels of Variables |
|------- |------- |---------------------|
| A      | Reaction time (min) | −1 | 0 | +1 |
| B      | pH | 60 | 100 | 140 |
| C      | \(K_2S_2O_8/Fe^{2+}\) molar ratio | 3 | 5.35 | 7.7 |
| D      | Concentration (mM) | 7.5 | 10 | 12.5 |

3.6. Modelling Using ANN

The neural network module from the statistical software SAS JMP Pro 15 was used to train and validate the artificial neural network (ANN). The values of the parameters are shown in Table 6.
Table 6. Independent variables and their levels.

| Parameter                  | Value                                      |
|----------------------------|--------------------------------------------|
| Cross-validation k-fold methods (5 groups) |                                             |
| Hidden nodes               | 5 to 20                                    |
| Number of models           | 200                                        |
| Learning rate              | 0.1                                        |
| Penalty method             | squared                                    |
| Number of tours            | 4                                          |
| Transfer function          | Tanh ()                                    |

A fully connected ANN has been built using one hidden layer, which consisted of 5 to 20 nodes with Tan H sigmoid function [30]. The optimum number of hidden nodes was found by calculation of a specific score (E) with an equation that includes both regression coefficients ($R^2$) and root mean square error (RMSE) of training and validation models (Equation (14)) [31].

$$E = \left( \frac{R^2_{\text{training}} + R^2_{\text{validation}}}{\text{RMSE}_{\text{training}} + \text{RMSE}_{\text{validation}}} \right) \times 100,$$

(14)

4. Conclusions

Response surface methodology and artificial neural network have been utilized for the optimization of the photochemical treatment of municipal wastewater using the photo-Fenton-like process. According to the RSM, the optimum conditions for the highest TOC removal (100% both experimentally and statistically) were achieved at the reaction time of 106.06 min, pH of 7.7, persulfate concentration of 30 mM, and $K_2S_2O_8/Fe^{2+}$ molar ratio of 7.5. According to the ANN results, the optimum conditions for the highest TOC removal (100% experimentally and 98.7 theoretically) were obtained at the reaction time of 104.93 min, pH of 7.7, persulfate concentration of 30 mM, and $K_2S_2O_8/Fe^{2+}$ molar ratio of 9.57. Both RSM and ANN models inaccurately predicted optimum conditions for TC and TN removal. Thus, the conditions with the highest removal of TC (71.31%) and TN (60.13%) were observed at the reaction time of 140 min (for TC) and 100 min (for TN), pH of 5.35 (for both TC and TN), persulfate concentration of 30 mM (for TC) and 10 mM (for TN), $K_2S_2O_8/Fe^{2+}$ molar ratio of 10 (for TC) and 12.5 (for TN). ANOVA was able to indicate the significant parameters for the photo-Fenton-like process. Factors such as reaction time, pH, $K_2S_2O_8$, interactions between reaction time and pH, pH and $K_2S_2O_8$, and $K_2S_2O_8/Fe^{2+}$ molar ratio had a significant impact on TOC removal.

Supplementary Materials: The following are available online at https://www.mdpi.com/article/10.3390/catal11101206/s1, Table S1: $R^2$ and RMSE values for actual and predicted TC removal (%), Table S2: $R^2$ and RMSE values for actual and predicted TOC removal (%), Table S3: $R^2$ and RMSE values for actual and predicted TN removal (%), Table S4: The concentrations of formic acid, acetic acid, intermediates, and CO$_2$ expressed in organic carbon (OC) for each run, Figure S1. Pareto chart of the standardized effects (response is TOC removal (%); the reference line is at 2.18, $\alpha = 0.05$): (A) reaction time, (B) pH, (C) $K_2S_2O_8$, (D) $K_2S_2O_8/Fe^{2+}$.

Author Contributions: Conceptualization, Y.N.K. and S.G.P.; Data curation, Y.N.K. and V.Z.; Formal analysis, Y.N.K.; Funding acquisition, E.A. and S.G.P.; Investigation, Y.N.K. and A.M.; Methodology, Y.N.K. and A.M.; Project administration, E.A. and S.G.P.; Resources, E.A. and S.G.P.; Software, Y.N.K.; Supervision, S.G.P.; Validation, Y.N.K. and V.Z.; Visualization, Y.N.K.; Writing—original draft, Y.N.K. and A.M.; Writing—review & editing, Y.N.K., V.Z., E.A. and S.G.P. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the Nazarbayev University project “Cost-Effective Photo-catalysts for the Treatment of Wastewaters containing Emerging Pollutants”, Faculty development competitive research grants program for 2020–2022, Grant Number 240919FD3932 awarded to S.G. Poulopoulos.
Catalysts 2021, 11, 1206

Acknowledgments: The authors acknowledge funding support from Nazarbayev University. The technical support of Core Facilities of Nazarbayev University is greatly acknowledged.

Conflicts of Interest: The authors declare no conflict of interest.

References

1. Fane, A.G.; Tang, C.Y.; Wang, R. Membrane Technology for Water: Microfiltration, Ultrafiltration, Nanofiltration, and Reverse Osmosis. In *Treatise on Water Science*; Newnes Books-Elsevier: Amsterdam, The Netherlands, 2011; Volume 4, pp. 301–335, ISBN 9780444531933.

2. Pereira, L.S.; Duarte, E.; Fragoso, R. Water Use: Recycling and Desalination for Agriculture. In *Encyclopedia of Agriculture and Food Systems*; Elsevier: Amsterdam, The Netherlands, 2014.

3. Neta, P.; Madhavan, V.; Zemel, H.; Fessenden, R.W. Rate constants and mechanism of reaction of sulfate radical anion with aromatic compounds. *J. Am. Chem. Soc.* 1977, 99, 163–164. [CrossRef]

4. Waldemer, R.H.; Tratnyek, P.G.; Johnson, R.L.; Nurmi, J.T. Oxidation of chlorinated ethenes by heat-activated persulfate: Kinetics and products. *Environ. Sci. Technol.* 2007, 41, 1010–1015. [CrossRef]

5. Wang, Z.; Jiang, J.; Pang, S.; Zhou, Y.; Guan, C.; Gao, Y.; Li, J.; Yang, Y.; Qiu, W.; Jiang, C. Is Sulfate Radical Really Generated from Peroxydisulfate Activated by Iron(II) for Environmental Decontamination? *Environ. Sci. Technol.* 2018, 52, 11276–11284. [CrossRef]

6. Velo-Gala, I.; López-Peña, J.J.; Sánchez-Polo, M.; Rivera-Utrilla, J. Comparative study of oxidative degradation of sodium diatrizoate in aqueous solution by H₂O₂/Fe₂+, H₂O₂/Fe₃+, Fe (VI) and UV, H₂O₂/UV, K₂S₂O₈/UV. *Chem. Eng. J.* 2014, 241, 504–512. [CrossRef]

7. Yang, S.; Cheng, J.; Sun, J.; Hu, Y.; Liang, X. Defluorination of Aqueous Perfluoroctanesulfonate by Activated Persulfate Oxidation. *PloS ONE* 2013, 8, e74877. [CrossRef]

8. Díbira, S.; Bensalah, N.; Zagho, M.M.; Ennahoui, M.; Bedoui, A. Oxidative degradation of tannic acid in aqueous solution by UV/S₂O₈⁻ and UV/H₂O₂/Fe₂+ processes: A comparative study. *Appl. Sci.* 2019, 9, 156. [CrossRef]

9. Pervez, M.N.; He, W.; Zarra, T.; Naddeo, V.; Zhao, Y. New sustainable approach for the production of Fe₃O₄/Graphene oxide-activated persulfate system for dye removal in real wastewater. *Water* 2020, 12, 733. [CrossRef]

10. Miklos, D.B.; Remy, C.; Jekel, M.; Linden, K.G.; Dreves, J.E.; Hübner, U. Evaluation of advanced oxidation processes for water and wastewater treatment—A critical review. *Water Res.* 2018, 139, 118–131. [CrossRef] [PubMed]
26. Ioannidi, A.; Arvaniti, O.S.; Nika, M.-C.; Aalizadeh, R.; Thomaidis, N.S.; Mantzavinos, D.; Frontistis, Z. Removal of drug losartan in environmental aquatic matrices by heat-activated persulfate: Kinetics, transformation products and synergistic effects. *Chemosphere* **2022**, *287*, 131952. [CrossRef]

27. Davarnejad, R.; Nasiri, S. Slaughterhouse wastewater treatment using an advanced oxidation process: Optimization study. *Environ. Pollut.* **2017**, *223*, 1–10. [CrossRef] [PubMed]

28. Bello, M.M.; Abdul Raman, A.A.; Asghar, A. A review on approaches for addressing the limitations of Fenton oxidation for recalcitrant wastewater treatment. *Process. Saf. Environ. Prot.* **2019**, *126*, 119–140. [CrossRef]

29. Li, R.; Kong, J.; Liu, H.; Chen, P.; Liu, G.; Li, F.; Lv, W. A sulfate radical based ferrous-peroxydisulfate oxidative system for indomethacin degradation in aqueous solutions. *RSC Adv.* **2017**, *7*, 22802–22809. [CrossRef]

30. Saber, W.E.I.A.; El-Naggar, N.E.A.; El-Hersh, M.S.; El-khateeb, A.Y.; Elsayed, A.; Eldadamony, N.M.; Ghoniem, A.A. Rotatable central composite design versus artificial neural network for modeling biosorption of Cr6+ by the immobilized Pseudomonas alcaliphila NEWG-2. *Sci. Rep.* **2021**, *11*, 1717. [CrossRef] [PubMed]

31. Alves da Rocha, R.; Paiva, I.M.; Anjos, V.; Furtado, M.A.M.; Bell, M.J.V. Quantification of whey in fluid milk using confocal Raman microscopy and artificial neural network. *J. Dairy Sci.* **2015**, *98*, 3559–3567. [CrossRef] [PubMed]