Anisotropic splitting of intersubband spin plasmons in quantum wells with bulk and structural inversion asymmetry

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In semiconductor heterostructures, bulk and structural inversion asymmetry and spin-orbit coupling induce a $k$-dependent spin splitting of valence and conduction subbands, which can be viewed as being caused by momentum-dependent crystal magnetic fields. This paper studies the influence of these effective magnetic fields on the intersubband spin dynamics in an asymmetric $n$-type GaAs/Al$_0.3$Ga$_0.7$As quantum well. We calculate the dispersions of intersubband spin plasmons using linear response theory. The so-called D’yakonov-Perel’ decoherence mechanism is inactive for collective intersubband excitations, i.e., crystal magnetic fields do not lead to decoherence of spin plasmons. Instead, we predict that the main signature of bulk and structural inversion asymmetry in intersubband spin dynamics is a three-fold, anisotropic splitting of the spin plasmon dispersion.

The importance of many-body effects is pointed out, and conditions for experimental observation with inelastic light scattering are discussed.

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I. INTRODUCTION

The field of spintronics is based on the concept of exploiting the spin degree of freedom of carriers to develop new features and functionalities for solid-state devices. Many of the proposed new applications rely, in one form or another, on manipulating nonequilibrium spin coherence. Two characteristic times, $T_1$ and $T_2$, provide a quantitative measure for the magnitude and persistence of spin coherence: $T_1$ describes the return to equilibrium of a non-equilibrium spin population, and $T_2$ measures the decay of transverse spin order.

In this paper, we consider electronic spin dynamics in quantum wells not within one but between two subbands (we will limit the discussion here to conduction subbands). One motivation for this work is that intersubband (ISB) charge dynamics in quantum wells is currently of great experimental and theoretical interest since electronic ISB transitions are the basis of a variety of new devices operating in the terahertz frequency regime, such as detectors, modulators and quantum cascade lasers. In view of this, it seems worthwhile to explore ISB spin dynamics as a possible route towards novel applications in the terahertz regime.

Characteristic times for ISB dynamics are also referred to as $T_1$ and $T_2$, whether or not decay of spin coherence is involved. Population decay from an excited to a lower conduction subband is characterized by an ISB relaxation time $T_{1}^{\text{ISB}}$, and loss of coherence of collective ISB excitations is measured by a decoherence time $T_{2}^{\text{ISB}}$. Much has been learned recently about ISB charge-density excitations (CDE’s, also called charge plasmons). The two characteristic times were measured experimentally for CDE’s in quantum wells and were found to differ substantially at low temperatures, $T_{2}^{\text{ISB}}$ being three orders of magnitude smaller than $T_{1}^{\text{ISB}}$. The reason is that CDE relaxation characterized by $T_{1}^{\text{ISB}}$ proceeds mainly via phonon emission and is thus slowed down by an energy bottleneck for acoustic phonons with small momenta and all optical phonons.

In contrast to $T_{1}^{\text{ISB}}$, decoherence ($T_{2}^{\text{ISB}}$) of collective ISB CDE’s in quantum wells is determined by a complex interplay of a variety of different scattering mechanisms, whose relative importance is not $a$ priori obvious. In recent experimental and theoretical work, it was found that the linewidth of (homogeneously broadened) ISB charge plasmons in a wide GaAs/Al$_0.3$Ga$_0.7$As quantum well (where phonon scattering is not important) is determined mainly by interface roughness and electronic many-body effects.

The question now arises which physical mechanisms govern the decoherence of ISB spin-density excitations (SDE’s, or spin plasmons). Near room temperature the intrasubband electron spin decoherence in semiconductors is to a large extent determined by the D’yakonov-Perel’ mechanism which involves spin precession of carriers with finite crystal momentum $k$ in an effective $k$-dependent crystal magnetic field in inversion-asymmetric materials and implies $T_1$ and $T_2$ are comparable. Using this theory, Lau et al. achieved good agreement with experimental spin decoherence times, without including electron-electron interactions (see also Refs. 25, 26). Thus, it is clear that crystal magnetic fields are a fundamentally important factor in determining $T_1$ and $T_2$ in intrasubband spin dynamics. However, the role of the crystal magnetic fields for $T_{1}^{\text{ISB}}$ and $T_{2}^{\text{ISB}}$ has so far remained an open question.

This paper addresses the influence of the $k$-dependent crystal magnetic field in semiconductor quantum wells on ISB spin plasmons. Building on a formal framework in-
introduced previously, we use (time-dependent) density functional theory to describe static and dynamic many-body effects. We extend our previous result that due to their collective nature the ISB spin plasmons are robust against D’yakonov-Perel’ decoherence. The main reason for this suppression is that the k-averaged effect of the crystal magnetic field vanishes for an electron occupation function symmetric in k, due to time-reversal invariance. This result was previously reported only for Rashba effective magnetic fields, and we now include effective magnetic fields arising from both bulk inversion asymmetry and Rashba effects.

The general structure of the ISB plasmon dispersions consists of a CDE branch above and three SDE branches below the region of single-particle excitations. In the absence of any magnetic fields, the three SDE branches (one longitudinal, two transverse) are degenerate. As we will show, the crystal magnetic field further splits the three SDE dispersion relations in an anisotropic way. We will predict that this effect should be observable with inelastic light scattering techniques. We mention that similar predictions were made, based on Fermi liquid theory, by Mal’shukov et al., who discussed ISB spin dynamics for model III-V quantum wells without including the Rashba effect. In the present paper, we will consider a realistic, asymmetrically doped GaAs/AlGaAs quantum well system that features an interesting interplay between bulk and structural inversion asymmetry.

This paper is organized as follows. In Section II we calculate the electronic ground state in modulation-doped quantum well conduction subbands, including spin-orbit coupling and many-body effects. In Section III we use a linear response formalism for the spin-density matrix, based on time-dependent density functional theory, to calculate the ISB plasmon dispersions. We also discuss possibilities for experimental observation of the spin plasmons with inelastic light scattering. Section IV contains our conclusions.

II. CONDUCTION SUBBAND SPIN SPLITTING IN QUANTUM WELLS

The first step is to calculate the momentum-dependent spin splitting of conduction subbands in a quantum well in the presence of bulk inversion asymmetry (BIA) and structural inversion asymmetry (SIA) or Rashba effect. A detailed account of the method is given in Ref. The use of a 2 × 2 conduction subband Hamiltonian, which can be obtained by reduction from a multi-band k · p Hamiltonian in a standard way. This results in the following two-component form of the electron wavefunction for the jth subband:

$$\psi_{j\|}(r) = e^{i\mathbf{iq}_j \cdot \mathbf{r}} \begin{pmatrix} \psi_{j\|}(\mathbf{q}_j, z) \\ \psi_{j\perp}(\mathbf{q}_j, z) \end{pmatrix},$$

where $\mathbf{r}_\|$ and $\mathbf{q}_\|$ are in-plane position and wave vectors, and $z$ is the direction of growth of the quantum well. The envelope functions $\psi_{j\sigma}$ are obtained from a two-component effective-mass Kohn-Sham equation, which in its most general form reads as follows:

$$\sum_{\beta=\uparrow, \downarrow} \left( \hbar \delta_{\alpha\beta} + v_{\alpha\beta}^{\text{ext}}(z) + H_{\alpha\beta}^{\text{so}}(z) + v_{\alpha\beta}^{\text{xc}}(z) \right) \hat{\psi}_{j\beta}(\mathbf{q}_\|, z) = E_j a_{\|j} \hat{\psi}_{j\alpha}(\mathbf{q}_\|, z),$$

where $\alpha = \uparrow, \downarrow$, and

$$\hat{h} = -\frac{d}{dz} \frac{\hbar^2}{2m^*(z)} \frac{d}{dz} + \frac{\hbar^2 q^2_{\|}}{2m^*(z)} + v_{\text{conf}}(z) + v_H(z).$$

We use here the simplifying assumption of energy-independent effective masses $m^*$, which is sufficient for the GaAs/AlGaAs system studied in this paper. $v_{\text{conf}}(z)$ is the confining bare quantum well potential (e.g., a square well). The Hartree potential $v_H(z)$ describes the classical Coulomb potential due to the electron ground-state density $n(z)$ and to the density of positive donor impurities $n_i(z)$:

$$\frac{d^2 v_H(z)}{dz^2} = -4\pi e^2 [n(z) - n_i(z)].$$

where $e^* = e/\sqrt{\epsilon}$ is the effective charge (the static dielectric constant is taken as $\epsilon = 13$ throughout the system).

In this paper, we consider the case without any externally applied static electric or magnetic fields, so that $v_{\alpha\beta}^{\text{ext}}(z) = 0$. As a consequence, the exchange-correlation (xc) potential becomes diagonal in the spins: $v_{\alpha\beta}^{\text{xc}}(z) = v_{\text{xc}}(z) \delta_{\alpha\beta}$. We take a standard local-density approximation (LDA) for $v_{\text{xc}}(z)$.

Intrinsic conduction band spin splitting is caused by spin-orbit interaction, but may originate from various sources. In the following, we will consider BIA and SIA contributions: $H_{\alpha\beta}^{\text{so}} = H_{\text{BIA}}^{\alpha\beta} + H_{\text{SIA}}^{\alpha\beta}$. The BIA term depends on the direction of growth of the quantum well which we here take along [001].

The spin-orbit Hamiltonian can be written as

$$\hat{H}_{\text{so}} = \sigma \cdot \mathbf{B}_{\text{eff}},$$

where $\sigma$ is the vector of the Pauli spin matrices, and $\mathbf{B}_{\text{eff}}$ acts as an in-plane effective magnetic field. Some simplification is achieved using a perturbative treatment and one arrives at

$$\mathbf{B}_{\text{eff}} = \begin{pmatrix} (\gamma)q_x q_y - (\gamma z^2)q_y + (\alpha)q_y \\ - (\gamma)q_y q_x^2 + (\gamma z^2)q_y - (\alpha)q_x \end{pmatrix}. $$

This leads to

$$\hat{H}_{\uparrow\uparrow}^{\text{so}} = \hat{H}_{\downarrow\downarrow}^{\text{so}} = 0, \quad \hat{H}_{\uparrow\downarrow}^{\text{so}} = (\hat{H}_{\text{BIA}}^{\alpha\beta})^\dagger = h\Omega,$$

where

$$h\Omega = (\gamma)q_x q_y (q_x + iq_y) - (\gamma z^2)(q_x + iq_y) + (\alpha)(q_y + iq_x).$$


γ and α are material parameters determining the BIA and SIA effects, and are position dependent in a quantum well. Thus, we have
\[
\langle \gamma \rangle = \int dz \gamma(z) |\psi_j(z)|^2 ,
\]
(9)
the analogous definition for \( \langle \alpha \rangle \), and
\[
\langle \gamma \alpha \rangle^2 = - \int dz \psi_j(z) \frac{d}{dz} \gamma(z) \frac{d}{dz} \psi_j(z) .
\]
(10)
(notice the dependence on the subband index \( j \)). Several authors\cite{43,44,45,46,47,48} have pointed out the importance of a proper treatment of the discontinuities at the left and right quantum well interfaces, \( z = z_{L,R} \). Thus, we take
\[
- \langle \gamma \alpha \rangle^2 = \int dz \psi_j(z) \frac{d}{dz} \gamma(z) \frac{d}{dz} \psi_j(z) + \Gamma_L \psi_j(z_L) + \Gamma_R \psi_j(z_R).
\]
(11)
where the prime on the integral means that infinitesimal regions around the interfaces are excluded in the integration, and the jumps \( \Gamma_{L,R} \) are defined as
\[
\Gamma_{L,R} = \left[ \gamma(z) \frac{d\psi_j(z)}{dz} \right]_{z_{L,R}} - \left[ \gamma(z) \frac{d\psi_j(z)}{dz} \right]_{z_{L,R}} .
\]
(12)
A similar treatment is carried out for the jumps in \( \langle \alpha \rangle \), where the Rashba coefficient \( \alpha \) is given as
\[
\alpha = \frac{d}{dz} \frac{\hbar^2}{2m^*} \left[ \frac{\Delta}{3E_g + 2\Delta} - \frac{(\varepsilon_j - V)}{E_g} \frac{(2E_g + \Delta^2)}{(3E_g + 2\Delta)} \right] .
\]
(13)
where \( V = v_{\text{conf}} + v_{\text{H}} + v_{\text{xc}} \) is the total potential, and the \( j \)th subband energy \( \varepsilon_j \) is defined as the energy above the minimum of \( V \) inside the quantum well (\( z_L < z < z_R \)). We take a conduction band offset of \( 257.6 \) meV between GaAs and Al\(_{0.3}\)Ga\(_{0.7}\)As. All other material parameters determining γ and α are summarized in Table I.

| Material       | \( E_g \) (eV) | \( \Delta \) (eV) | \( \gamma \) (eV Å\(^3\)) | \( m^* \) |
|----------------|----------------|-----------------|----------------|--------|
| GaAs           | 1.519          | 0.34            | 24.12          | 0.067  |
| Al\(_{0.3}\)Ga\(_{0.7}\)As | 1.921          | 0.322           | 18.03          | 0.092  |

FIG. 1: Total potential \( V \) and conduction subband levels \( \varepsilon_j \) of an asymmetrically doped \( 180 \) Å GaAs/Al\(_{0.3}\)Ga\(_{0.7}\)As quantum well, with electron density \( N_s = 8 \times 10^{13} \) cm\(^{-2}\). The dashed line indicates the conduction band Fermi level.

where we replaced the subband index \( i \) by the pair of indices \( \{s_j\} \), such that \( s = (-1)^i \) and \( j = (i + 1)/2 \) for \( i \) odd and \( j = i/2 \) for \( i \) even. In the absence of the off-diagonal terms in Eq. (14), i.e. for inversion symmetry and hence spin degeneracy at each \( q_{||} \), \( j \) simply labels the spin-degenerate pairs, and \( s \) labels the eigenfunctions within each pair.

The \( \varphi_j(z) \) are the solutions of a spin-independent effective-mass Kohn-Sham equation:
\[
\left[ - \frac{d}{dz} \frac{\hbar^2}{2m^*} \frac{d}{dz} + v_{\text{conf}} + v_{\text{H}} + v_{\text{xc}} \right] \varphi_j = \varepsilon_j \varphi_j ,
\]
(17)
where \( \varepsilon_j \) are the energy levels of the associated, doubly degenerate, parabolic subbands. The presence of the off-diagonal BIA and SIA terms in Eq. (14), however, lifts the spin degeneracy for \( q_{||} \neq 0 \). Ignoring the slight non-parabolicity that comes from the \( z \)-dependence of \( m^* \), we obtain
\[
E_{sjq_{||}} = \varepsilon_j + \frac{q_{||}^2}{2m^*} + sh|\Omega| , \quad s = \pm 1 ,
\]
(18)
for the energy eigenvalues associated with the solutions \( \{\Omega\} \) of Eq. (14), where \( m^* \) is the GaAs effective mass.

Fig. 1 shows the conduction band edge and subband levels of an asymmetrically doped, \( 180 \) Å wide, \( [001] \)-grown GaAs/Al\(_{0.3}\)Ga\(_{0.7}\)As quantum well. The carrier sheet density is taken as \( N_s = 8 \times 10^{13} \) cm\(^{-2}\), and the same number of positive donor impurities is evenly distributed between 50Å < \( z < 200 \) Å, which defines \( n_i(z) \) in Eq. (4). It is seen from the figure that only the lowest subband is occupied.

The conduction subband splitting in the same quantum well system was studied before by Jusserand et al.\cite{38} using intrasubband Raman scattering, and theoretically by Wissinger et al.\cite{39} using more sophisticated \( 8 \times 8 \) and \( 14 \times 14 \) band models. Our results, obtained with the
can be seen how magnitude as well as direction of
for the first and second subband of our quantum well. It
strongly depend on the in-plane momentum
of Fig. 1, for in-plane momenta
[110], and 0.20 meV along
[100], 0.23 meV along

The lowest conduction subband at the Fermi level, where
the crystal magnetic field in the lowest subband is dominated by the
Rashba effect, whereas the second (lowest unoccupied)
subband is dominated by the Dresselhaus bulk term.

III. INTERSUBBAND SPIN DYNAMICS

A. Formal framework

Having calculated the subband energy levels and envelope functions, we now consider ISB excitations. Formal basis is the linear response theory for the spin-density matrix that was developed earlier. ISB charge and spin plasmons emerge as solutions of the response equation corresponding to collective CDE’s and SDE’s.

We denote the first-order change of the spin-density matrix by \( n^{(1)}_{\sigma\sigma'}(k, z, \omega) \), and define

\[
\begin{align*}
  m_j^{(1)}(k_z) = \frac{1}{2}\text{Tr}[\sigma_j \pi^{(1)}_{\sigma}(k_z)], \\
  j = 0, 1, 2, 3,
\end{align*}
\]

where \( \sigma_0 \) is the 2 \times 2 unit matrix, and \( \sigma_1, \sigma_2, \sigma_3 \) are the Pauli matrices. \( m_0^{(1)} = n^{(1)}_{\uparrow\uparrow} + n^{(1)}_{\downarrow\downarrow} \) describes a collective CDE, and \( m_3^{(1)} = n^{(1)}_{\uparrow\downarrow} - n^{(1)}_{\downarrow\uparrow} \) is a longitudinal SDE with respect to the z-axis. In terms of this choice of global spin quantization, \( m_1^{(1)} = n^{(1)}_{\uparrow\downarrow} + n^{(1)}_{\downarrow\uparrow} \)
and \( m_2^{(1)} = i(n^{(1)}_{\uparrow\downarrow} - n^{(1)}_{\downarrow\uparrow}) \) appear as transverse SDE’s (or spin-flip excitations).

The spin-density-matrix response \( n^{(1)}_{\sigma\sigma'} \) couples to spin-dependent potentials \( \epsilon^{(1)}_{\sigma} \), which we can again combine as

\[
V^{(1)}_j = \frac{1}{2}\text{Tr}[\sigma_j \pi^{(1)}_{\sigma}(k_z, \omega)].
\]

Thus, the CDE couples to an oscillating electric field polarized along the z-direction, associated with \( V^{(1)}_z \). The longitudinal SDE is excited by an oscillating magnetic field along z associated with \( V^{(1)}_3 \), and the transverse SDE’s are excited by oscillating magnetic fields along x and y, associated with \( V^{(1)}_1 \) and \( V^{(1)}_2 \), respectively. We will discuss the corresponding selection rules for inelastic light scattering below.

In terms of these quantities, the linear response equation takes on the following 4 \times 4 matrix form:

\[
m_j^{(1)}(k_z, \omega) = \sum_{k=0}^{3} \int dz' \Pi_{jk}^{\text{KS}}(k_z, z, z', \omega) V^{(1)}_k(k_z, z', \omega).
\]

(19)

\( \Pi_{jk}^{\text{KS}} \) is the non-interacting (Kohn-Sham) charge-spin response function, which was given in Appendix B of Ref. 28. The \( V^{(1)}_k \), in turn, are sums of external perturbations and linearized Hartree and xc terms:

\[
V^{(1)}_k(k_z, z, \omega) = V^{\text{ext}}_k(k_z, z, \omega) + \sum_{l=0}^{3} \int dz' \left[ \frac{2\pi e^2}{\hbar^2} \right] e^{-k_{l||} z - z'} \delta_{kl} \delta_{l0} + \int f_{kl}(k_z, z', \omega) m_j^{(1)}(k_z, z', \omega).
\]

(20)
The xc kernels $f^{\sigma}_{kl}F^{\sigma}$ are given in Appendix A of Ref. 28. Eq. 19 can be rewritten formally exactly as

$$m_{j}^{(1)}(k_{||},z,\omega) = \sum_{k=0}^{3} dz' \Pi_{jk}(k_{||},z,z',\omega)V_{k}^{\text{ext}}(k_{||},z',\omega),$$

which defines the full charge-spin response function:

$$\Pi = \frac{\Pi_{\text{KS}}}{1 - \Pi_{\text{KS}}F^{\text{Hxc}}}. \quad (22)$$

The elements of the matrix $F^{\text{Hxc}}$ are given by

$$F_{kl}^{\text{Hxc}}(k_{||},z,z',\omega) = \frac{2\pi e^{2}}{k_{||}} e^{-k_{||}|z-z'|}\delta_{k0}\delta_{00} + \bar{f}_{kl}^{\text{ext}}(k_{||},z,z',\omega). \quad (23)$$

The poles of $\Pi_{\text{KS}}$ yield the single-particle excitation spectrum, whereas the poles of $\Pi$ are the charge and spin plasmons.

Experimental observation of ISB plasmons can be achieved with various methods of optical spectroscopy. Consider the following expression:

$$\bar{\Pi}_{jk}(k_{||},\omega) = \int dz \int d z' z z' \Pi_{jk}(k_{||},z,z',\omega), \quad (24)$$

which entails the proper ISB dipole selection rules for interaction of the quantum well carriers with electromagnetic waves. CDE’s can be observed using photoabsorption spectroscopy, inelastic light scattering, or inelastic light scattering in the so-called polarized geometry, with cross sections given in both cases by

$$\sigma_{c}(k_{||},\omega) \sim \text{Im} \; \Pi_{00}(k_{||},\omega). \quad (25)$$

SDE’s, on the other hand, are seen with inelastic light scattering in the depolarized geometry, with cross sections

$$\sigma_{s}(k_{||},\omega) \sim \text{Im} \; \sum_{i,j=1}^{3} p_{i} \bar{\Pi}_{ij}(k_{||},\omega) p_{j}^{*}. \quad (26)$$

This expression implies orthogonal polarization vectors of the incident and scattered light, $\vec{e}_{i,s}$, through $\hat{P} = \vec{e}_{i} \times \vec{e}_{s}$. We also note that no definite selection rules exist for incoherent single-particle excitations which thus show up in both $\sigma_{c}$ and $\sigma_{s}$.

Finite linewidths of collective CDE’s and SDE’s in weakly disordered systems enter through the structure of $\Pi_{ij}$; either in the form of phenomenological scattering times (which can essentially be put in by hand), or through microscopic approaches such as the memory-function formalism. In the following, however, we will not be concerned with dissipation mechanisms such as impurity, interface roughness, phonon or electron-electron scattering.

The direction of the plasmon wave vector is taken along the so-called $[100]$. Despite the presence of the crystal magnetic field, the spin plasmons emerge as distinct collective excitations, i.e. sharp lines with long lifetimes (limited to a maximum wave vector transfer of $k_{\parallel} \sim 0.002 \text{Å}^{-1}$, by rotating the sample with respect to the incident and detected wavevector of the light.

The shaded region indicates the particle-hole continuum: if the collective modes enter this region, they rapidly decay into incoherent single-particle excitations (Landau damping). The CDE lies above the single-particle region, and the SDE’s lie below. We mention that in inelastic light scattering experiments, ISB plasmon dispersions can be measured up to a maximum wave vector transfer of $k_{\parallel} \sim 0.002 \text{Å}^{-1}$, by rotating the sample with respect to the incident and detected wavevector of the light.

B. Results and Discussion

Fig. 4 shows the wave vector dispersions of the CDE and the SDE in our GaAs/Al$_{0.3}$Ga$_{0.7}$As quantum well. The direction of the plasmon wave vector is taken along $[100]$. The overall qualitative picture of the ISB plasmon dispersions is well known. The shaded region indicates the particle-hole continuum: if the collective modes enter this region, they rapidly decay into incoherent single-particle excitations (Landau damping). The CDE lies above the single-particle region, and the SDE’s lie below. We mention that in inelastic light scattering experiments, ISB plasmon dispersions can be measured up to a maximum wave vector transfer of $k_{\parallel} \sim 0.002 \text{Å}^{-1}$, by rotating the sample with respect to the incident and detected wavevector of the light.

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Despite the presence of the crystal magnetic field (Fig. 3), the spin plasmons emerge as distinct collective excitations, i.e. sharp lines with long lifetimes (limited...
only by other scattering mechanisms such as impurities or phonons). Thus, the D'yakonov-Perel' decoherence mechanism does not directly affect the spin plasmon lifetimes. However, the crystal magnetic fields cause a broadening of the particle-hole continuum, as evident from its finite width at \( k_\parallel = 0 \) (a similar effect would be caused by including band-nonparabolicity\(^\text{(a)}\)). This broadening of the particle-hole continuum has an indirect effect on the spin plasmon lifetimes, in the sense that it may slightly enhance the effectiveness of extrinsic or phonon scattering. Notice that in our system the plasmon frequencies are comparable to the LO phonon frequency in GaAs (35.6 meV). In practice, a somewhat wider quantum well may thus be preferable to reduce line broadening due to phonon scattering.

A much more pronounced signature of the BIA and SIA crystal magnetic fields appears in the spin plasmon dispersions themselves, in the form of a splitting into three branches, for finite in-plane wave vector. This is shown in detail in Fig. 5, where \( \Delta \omega \) denotes the difference of the spin plasmon frequencies with and without the crystal magnetic fields (in the latter case, the three spin plasmon branches – one longitudinal and two transverse – are identical). We denote the three branches by \( m_+^{(1)} \), \( m_\parallel^{(1)} \), and \( m_-^{(1)} \). The \( m_+^{(1)} \) branch has an essentially flat dispersion, after passing through an avoided crossing for small \( k_x \). The splitting between \( m_+^{(1)} \) and \( m_-^{(1)} \) is very nearly linear in \( k_\parallel \), and reaches values of about 0.3 meV shortly before the \( m_-^{(1)} \) branch enters the particle-hole continuum.

The splitting of the spin plasmon dispersions turns out to be highly anisotropic, as shown in Fig. 6b for in-plane wave vectors of magnitude \( k_\parallel = 0.0005 \text{ Å}^{-1} \) and different directions. The radial distance between the three concentric curves represents the splitting between \( m_+^{(1)} \), \( m_\parallel^{(1)} \), and \( m_-^{(1)} \). The splitting is maximal (0.22 meV) along the [1\( \bar{1} \)0] and [110] directions, and minimal (0.06 meV) along [1\( \bar{1} \)0] and [110]. In the latter cases, we observe an avoided crossing between the \( m_+^{(1)} \) and \( m_-^{(1)} \) branches.

The selection rules for inelastic light scattering, see Eq. \( \text{(28)} \), are tied to the polarizations of the three spin plasmon modes. Figs. 6a-d illustrate the polarization of the \( m_+^{(1)} \) branch for different directions of \( k_\parallel \). In the case of (b) both SIA and BIA (which corresponds to Fig. 6a), (c) SIA only, and (d) BIA only. In the limiting cases (c) and (d) \( (\text{SIA and BIA only}) \), the direction of this effective field is determined by the difference of the crystal magnetic fields of the first and second subband, \( \Delta \mathbf{B}_{\text{eff}}(\mathbf{k}_\parallel) \sim \mathbf{B}_{\text{eff},2}(\mathbf{q}_\parallel + \mathbf{k}_\parallel) - \mathbf{B}_{\text{eff},1}(\mathbf{q}_\parallel) \). Case (b) (both SIA and BIA) is more subtle since \( \mathbf{B}_{\text{eff},2} - \mathbf{B}_{\text{eff},1} \) now depends on both \( \mathbf{k}_\parallel \) and \( \mathbf{q}_\parallel \). Of course, a uniform \( \Delta \mathbf{B}_{\text{eff}}(\mathbf{k}_\parallel) \) can still be defined from the polarization and the splitting of the \( m_+^{(1)} \) and \( m_-^{(1)} \) modes. Compensating the \( \mathbf{q}_\parallel \)-dependence of \( \mathbf{B}_{\text{eff},2} - \mathbf{B}_{\text{eff},1} \) therefore requires an additional, \( \mathbf{q}_\parallel \)-dependent contribution to \( \Delta \mathbf{B}_{\text{eff}}(\mathbf{k}_\parallel) \), which is provided by collective (dynamical xc) effects.

**IV. CONCLUSIONS**

In this paper, we have studied ISB spin dynamics in a quantum well in the presence of bulk and structural inversion asymmetry (BIA and SIA). We have found that there is a unique signature of inversion asymmetry and spin-orbit coupling: the ISB spin plasmons exhibit a three-fold splitting. The magnitude of this splitting depends both on the magnitude and orientation of
the in-plane wave vector associated with the spin plasmons. As a result of the interplay of BIA and SIA, we find a pronounced anisotropy of the ISB spin plasmon splitting. This anisotropy is of a different nature than the anisotropy that was previously seen in the spin-flip Raman spectra of intra-subband spin excitations (see Fig. 2), since it arises from the difference of the crystal magnetic fields of two subbands. Thus, the predicted anisotropic ISB spin plasmon spin splitting should be a sensitive test for many-body theories of electronic and spin excitations in semiconductor nanostructures.

Another conclusion of this paper points to the dominant role of collective effects in the ISB dynamics in quantum wells. It turns out that the D'yakonov-Perel’ decoherence mechanism is not effective in limiting the lifetime of ISB spin plasmons, which are expected to be rather long-lived in the absence of other efficient scattering mechanisms. In our previous paper, we had come to the same conclusion for the more specialized case of Rashba splitting only. We have, therefore, extended that result in this paper to both BIA and SIA.

In the materials considered here (GaAs/Al$_0.3$Ga$_0.7$As), the effects of spin-orbit coupling are relatively weak compared to other materials such as InAs or AlSb, which can be expected to produce a much more pronounced spin plasmon splitting. In those cases, however, the $2 \times 2$ conduction band Hamiltonian used in this paper can no longer be expected to be accurate enough: for instance, band nonparabolicity will become important. Thus, a more detailed treatment of band structure will be needed, which will be the subject of future studies.

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