Spin–valley locking in the normal state of a transition-metal dichalcogenide superconductor

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Metallic transition-metal dichalcogenides (TMDCs) are benchmark systems for studying and controlling intertwined electronic orders in solids, with superconductivity developing from a charge-density wave state. The interplay between such phases is thought to play a critical role in the unconventional superconductivity of cuprates, Fe-based and heavy-fermion systems, yet even for the more moderately-correlated TMDCs, their nature and origins have proved controversial. Here, we study a prototypical example, 2H-NbSe2, by spin- and angle-resolved photoemission and first-principles theory. We find that the normal state, from which its hallmark collective phases emerge, is characterized by quasiparticles whose spin is locked to their valley pseudospin. This results from a combination of strong spin–orbit interactions and local inversion symmetry breaking, while interlayer coupling further drives a rich three-dimensional momentum dependence of the underlying Fermi-surface spin texture. These findings necessitate a re-investigation of the nature of charge order and superconducting pairing in NbSe2 and related TMDCs.
n combination with broken structural inversion symmetry, spin–orbit coupling (SOC) provides a powerful route to stabilize spin-polarized electronic states without magnetism. This can give rise to electrically-tuneable spin splittings via the Rashba effect, promising new technological developments in spintronics\(^1\), and underpins the formation of spin-helical Dirac cones at the surfaces of topological insulators\(^2\). It is strongly desired to realize similar effects in systems where more pronounced electronic interactions drive the emergence of collective phases. In non-centrosymmetric superconductors, for example, spin-splitting driven by strong SOC is expected to induce a mixing of spin-triplet and singlet superconducting order parameters\(^3\), and offers potential for stabilizing topological superconductors\(^4\). Yet, identifying suitable candidate materials has proved a major challenge to date. Partly this is driven by a relative dearth of non-centrosymmetric metals, while for non-magnetic systems in which the centre of inversion is maintained, robust-spin degeneracies of their electronic states would typically be expected due to the dual constraints of time-reversal and inversion symmetry.

In contrast, we show here from spin- and angle-resolved photoemission (ARPES) measurements that the normal state of the centrosymmetric TMDC superconductor 2H-NbSe\(_2\) (hereafter denoted NbSe\(_2\)) hosts a strong layer- and momentum-dependent spin polarization of its electronic states at and in the vicinity of the Fermi level. We attribute this as a consequence of a recently-realized form of spin polarization that can emerge in globally centrosymmetric materials in which constituent structural units nonetheless break inversion symmetry\(^5\)–\(^7\). Together with first-principles calculations, we show how this drives a critical and complex interplay of interlayer interactions and SOC in NbSe\(_2\). This yields a rich underlying spin-polarized electronic landscape from which charge order and superconductivity emerge upon cooling.

### Results

**Bulk electronic properties of NbSe\(_2\).** We consider here exclusively the layered 2H polymorph (Fig. 1a). Each layer forms a graphene-like honeycomb structure with Nb occupying the A sublattice and two Se atoms situated on the B sublattice. These lie out of the basal plane, equidistant above and below the transition metal. The unit cell contains two such layers, stacked along the c-axis with 180° in-plane rotation. Our resistivity measurements (Fig. 1b) from single-crystal NbSe\(_2\) samples show a metallic temperature-dependence. They additionally exhibit a pronounced hump at a temperature of \(T_{\text{CDW}}\approx 33\) K indicative of charge-density wave (CDW) formation\(^8\), as well as a sharp superconducting transition at \(T_c \approx 7\) K. The corresponding normal-state Fermi surface is shown in Fig. 1c, as measured by ARPES. There are two barrel centred around each zone-corner \(K(K')\) point, which are strongly trigonally-warped. Two further barrels are centred at the \(\Gamma\) point, the inner of which is hexagonal, while the outer exhibits additional warping. From our first-principles density-functional theory (DFT) calculations, and consistent with previous studies\(^9\)–\(^11\), we assign all four of these Fermi surface sheets as being predominantly derived from Nb 4\(d\) orbitals. Additional spectral weight at the zone centre is evident in our ARPES measurements for selected photon energies, which we attribute as a fifth, highly three-dimensional, Fermi surface sheet of predominantly Se \(p_z\) orbital character.

This sheet also contributes diffuse filled-in intensity, due to the finite out-of-plane momentum (\(k_z\)) resolution of ARPES, close to the zone centre in measurements of the electronic dispersions along in-plane high-symmetry directions (Fig. 2a). The Nb-dominated states, on the other hand, yield clear spectral features close to their Fermi crossings. Kinks in their measured dispersion and a decrease in linewidth near the Fermi-level point to relatively strong electron–phonon coupling in this system\(^11\)–\(^13\). It is these Nb-derived states that are known to host the largest energy gaps at the Fermi level arising from the CDW and superconducting instabilities in this system\(^13\)–\(^16\), although the origins of these have proved highly controversial\(^8\)–\(^10\),\(^11\),\(^13\)–\(^22\).

To the best of our knowledge, all prior theoretical treatments assume these orders emerge from an electronic liquid of trivially spin-degenerate character. Indeed, standard expectations of group theory would say this must be the case for the centrosymmetric space group (P6\(_3\)/mmc) of 2H-NbSe\(_2\).

In contrast, we directly observe pronounced spin polarizations of the underlying electronic states in spin-resolved energy distribution curves (spin-EDCs, see Methods) measured along the \(\Gamma \rightarrow K\) direction, shown in Fig. 2c–f. Close to the saddle point of these bands (Fig. 2d), two clearly-separated peaks can be observed in spin-EDCs. The measured spin polarization is almost entirely out-of-plane (Fig. 2d and Supplementary Fig. 1), with a sign that reverses between the two bands. We attribute this as...
arising from local inversion symmetry breaking within the individual layers that make up the bulk crystal structure\(^5,6,23\). For sufficiently weak interlayer interactions (a point we return to below), pronounced SOC characteristic of the 4\(d\) transition metal can lift the spin degeneracy of the states localized within each layer, that thus strongly feel the local inversion asymmetry. A layer-dependent sign change of this spin polarization, mediated by the rotated-layer stacking of the bulk crystal structure, would act to restore overall spin degeneracy as required by global inversion and time-reversal symmetries. Nonetheless, the electronic states retain strong layer-resolved spin polarizations. Depth-averaging probes would largely be insensitive to these, but photoemission is a surface sensitive technique. Incoherent superposition of photoelectrons emitted from neighbouring layers of the unit cell would lead to some suppression of the measured spin polarization, while interference effects can further complicate this picture\(^5\). Nonetheless, the extreme surface sensitivity at the photon energies used here, with an inelastic mean free path on the order of the interlayer separation, renders us predominantly sensitive to the spin texture of the top-most layer of the unit cell.

Spin–valley locking. Our measurements show how such spin textures in NbSe\(_2\) persist up to the Fermi level. This is evident in spin-resolved EDCs along the \(\Gamma – K\) direction (Fig. 2c-f) as well as the spin polarization of EDCs and a Fermi-level momentum-distribution curve along the \(K – M – K’\) direction (Fig. 3). The latter clearly reveals how the spin polarization reverses sign for each pair of Fermi surface sheets centred on neighbouring \(K\) and \(K’\) points. This is a natural consequence of time-reversal symmetry. Here, this results in a coupling of the spin to the so-called valley index, the quantum number which distinguishes \(K\)– and \(K’\)-centred Fermi surfaces in NbSe\(_2\) (Fig. 3e). Such spin–valley coupling has recently been extensively investigated for the band extrema in monolayers of semi-conducting TMDCs\(^{24–26}\), where it has not only been shown to lead to new physics, such as a valley Hall effect\(^27\), but also to offer potential for devices exploiting the valley pseudospin\(^{28,29}\). Our observations here point to a pronounced role of spin–valley coupling also for the low-energy quasiparticle excitations of the metallic 2H-structured TMDCs.

Critically, it is from this spin-polarized Fermi sea that electron–hole and electron–electron pairing interactions drive the formation of CDW order and superconductivity. The largest CDW gaps in NbSe\(_2\) are located on the zone-corner spin–valley-locked Fermi surfaces\(^{13}\). The CDW wave vector is entirely in-plane\(^{30}\), making the hidden layer-dependent spin polarizations relevant. The underlying spin textures can also be expected to have important implications for superconductivity. Recent measurements on electrically gated MoS\(_2\), which is known to host a strong spin–valley locking in its band structure\(^{25,26}\), have found evidence for unconventional so-called Ising superconductivity\(^{31,32}\). In this, the pronounced spin–orbit field which induces the underlying spin texture of the electronic states pins the spin of Cooper pair electrons in the out-of-plane direction. This leads to upper critical fields dramatically exceeding the Pauli paramagnetic limit for a magnetic field applied within the \(ab\)-plane. Similar phenomenology has recently been reported for mono- and few-layer NbSe\(_2\) (ref. 33), entirely consistent with our direct observation of spin–valley locking in this compound.

In bulk NbSe\(_2\), the spin-layer locking, and also multi-band nature as compared to gated MoS\(_2\), raises further prospects for stabilizing a delicate balance between different pairing states. In the normal state, we find that the \(\Gamma\)-centred Fermi surface barrels, which are known to support a modulated superconducting gap in the bulk\(^{13,34}\), are also strongly spin-polarized along the \(\Gamma – K\) direction (Fig. 2c). Their spin polarization, however, is completely suppressed along \(\Gamma – M\) (Fig. 2b). Intriguingly, the largest superconducting gaps of this Fermi surface determined in Rahn et al.\(^{13}\) are located at the regions of strongest spin polarization evident here. Pronounced superconducting gaps are also known to occur on the zone-corner Fermi surfaces\(^{13,15,34}\), which as demonstrated above, host strong spin–valley locking even in the bulk. Given the pronounced influence of SOC, a mixing of spin-triplet and spin-singlet order parameters could potentially be expected\(^3\). Forming even pseudospin-singlet Cooper pairs from the strongly spin-polarized Fermi surfaces could necessitate a phase locking between the order parameter of neighbouring Fermi surface sheets. Moreover, the \(c\)-axis coherence length in NbSe\(_2\) is much greater than the interlayer separation\(^{35,36}\). This raises the tantalizing prospect that the inherent coupling between the spin and layer pseudospins reported here could be tuned to drive an instability to an odd-parity pair density-wave state, where the sign of the superconducting gap becomes tied to the layer index\(^{7,37}\). The proximity of bulk NbSe\(_2\) and similar compounds to such phases requires further theoretical exploration, and will depend sensitively on the relative importance of inter- and intra-band as well as interlayer pairing interactions.

Three-dimensional spin structure. Our DFT calculations (Fig. 4) already reveal a key role of interlayer interactions in mediating and controlling the underlying spin texture of the normal-state
bulk Fermi surface. The calculated spin polarization projected onto the first layer of the unit cell is shown throughout the full three-dimensional Brillouin zone in Fig. 4a,b. The momentum-dependent spin polarizations are determined by the effective spin–orbit field, $B_{so} = \beta(\nabla V \times \mathbf{k})$, where $\beta$ is a momentum-dependent scaling factor, $\nabla V$ is the net electrostatic potential gradient and $\mathbf{k}$ is the crystal momentum. The horizontal mirror symmetry of each NbSe$_2$ structural unit about the transition-metal plane ($\sigma_{h}$ of the D$_{sh}$ point group; Fig. 1a) ensures that $\nabla V$ is entirely within the $xy$ plane. Due to the 180° relative rotation of neighbouring NbSe$_2$ monolayers in the bulk crystal structure, $\nabla V$, and thus $B_{so}$ has opposite sign for successive layers in the unit cell. This causes the sign of the spin polarization to reverse at each momentum-space point when projected onto layer 2 versus layer 1 of the unit cell (Supplementary Fig. 3). This confirms that local inversion asymmetry within each NbSe$_2$ layer drives the formation of the spin-polarized states observed here.
For electronic states whose wavefunctions are completely delocalized over both layers of the unit cell, the spin–orbit field from each layer cancels. Such states are consequently unpolarized, restoring the conventional expectations for a centrosymmetric space group. This can be observed for the highly three-dimensional pancake-like Fermi surface at the Brillouin zone centre here. In contrast, for electronic states predominantly localized within individual layers of the unit cell, strong layer-dependent spin–orbit fields mediate large layer-resolved spin polarizations. This is ideally realized at the three-dimensional Brillouin zone boundary along \( k_z = \pi/c \). In a tight-binding picture, for this \( k_z \), interlayer hoppings within a unit cell and between neighbouring unit cells are out of phase with each other and thus cancel\(^{15}\). This can be directly visualized by comparing the dispersion of the electronic states along the \( \Gamma-M-K-\Gamma \) and A-L-H-A directions: neglecting SOC, a single fourfold degenerate band crosses the Fermi level in the \( k_z = \pi/c \) plane (Fig. 4c), whereas this is split into a pair of twofold degenerate bands by interlayer interactions for \( |k_z| < \pi/c \), as evident in Fig. 4d. With forbidden interlayer coupling, the electronic structure for the \( k_z = \pi/c \) plane is thus formally equivalent to that of an isolated monolayer. The spin–orbit field is consequently maximized, driving the largest (>90%) layer-dependent spin-polarizations. These are purely out-of-plane (Fig. 4a,b), as \((VV \times k)\) must lie entirely along \( z \) at the Brillouin zone boundary along \( k_z \). Along the A-L direction, however, a vertical mirror plane in the crystal structure forbids any out-of-plane component of \((VV \times k)\). The spin–orbit field must therefore be strictly zero along A-L. This enforces a touching, and hence spin degeneracy, of the zone-centre Fermi surface barrels along this direction, which are otherwise strongly spin-polarized throughout the \( k_z = \pi/c \) plane.

For other \( k_z \) through the Brillouin zone, the spin–orbit field strength can be partially suppressed by finite interlayer coupling. Moreover, the \( z \)-component of the momentum induces a non-zero component of \((VV \times k)\) in the \( xy \) plane. Together, this causes not only the magnitude of the Fermi surface spin polarization, but also its vectorial spin texture, to develop a strong dependence on both the in- and out-of-plane momentum, but also its vectorial spin texture, to develop a strong dependence on both the in- and out-of-plane momentum, and thus cancel\(^{10}\). This can be directly visualized by comparing the non-zero component of \((r)\) and \( (z) \) for the \( k_z = \pi/c \) plane (Fig. 4f) and points to the existence of such hidden in-plane spin textures is a unique property of the bulk compound. Indeed, the in-plane spin component goes strictly to zero at the Brillouin zone boundary along \( k_z \), enforced by symmetry, and recovering a monolayer-like purely out-of-plane spin texture for \( k_z = \pm \pi/c \). The bulk system thus hosts a rich intertwining of spin, orbital and layer degrees of freedom, mediating a three-dimensional nature of its spin texture that can be expected to further modulate its pairing interactions\(^{31}\).

**Discussion**

Taken together, our results show how the combination of interlayer hopping and intralayer inversion symmetry breaking can lead to particularly rich momentum-dependent spin textures of metallic TMDCs. Suppression of Fermi-surface spin polarization away from the Brillouin zone boundary along \( k_z \) will be reduced with decreased interlayer interactions. Indeed, upper critical fields, already known to exceed the Pauli limit for bulk NbSe\(_2\) (ref. 38), and dramatically enhanced in other 2H-TMDC superconductors as a function of increasing interlayer separation\(^{59}\). This points to a susceptibility of the bulk systems to Ising superconductivity similar to that recently observed in isolated monolayers\(^{33}\). The delicate balance between interlayer hopping and SOC strength in NbSe\(_2\) makes this an ideal material for understanding, and ultimately controlling the role of layer-dependent spin polarizations on the collective states and phases of transition-metal dichalcogenides.

**Methods**

**ARPES.** Spin-resolved ARPES measurements were performed at the I3 beamline of MAX IV Laboratory, Sweden, and ARPES measurements were performed using the I05 beamline of Diamond Light Source, UK. Measurements were performed at temperatures of 50–80 K using p-polarized synchrotron light. Scienta 84000 hemispherical electron analyzers were utilized for all measurements. This was additionally fitted with a mini-Mott detector scheme for the spin-ARPES measurements, configured to simultaneously probe the out-of-plane and in-plane (along the analyzer slit direction) component of the photoelectron spin\(^{37}\). The finite spin-detection efficiency was corrected using a Sherman function of \( S = 0.17 \) (ref. 40), and the spin-resolved EDCs determined according to\(^{21}\):

\[
I_{\uparrow}^{\downarrow} = I_{\uparrow}^{\downarrow}(1 \pm P_z)/2
\]

with \( i = (\downarrow, \uparrow) \), \( I_{\uparrow}^{\downarrow} \) the measured intensity on the individual detectors in the Mott scattering chamber, corrected by a relative detector efficiency calibration, and the total spin polarization,

\[
P_z = \left( I_{\uparrow} - I_{\downarrow} \right) / \left( I_{\uparrow} + I_{\downarrow} \right)
\]

with \( I_{\uparrow} = \left( I_{\uparrow}^{\downarrow} + I_{\uparrow}^{\uparrow} \right) \).

**Calculations.** DFT calculations including SOC were performed using the modified Becke–Johnson exchange potential and Perdew–Burke–Ernzerhof correlation functional implemented in the WIEN2K programme\(^{41}\). A \( 20 \times 20 \times 10 \) k-mesh was employed. The DFT results were downfolded using maximally localized Wannier functions\(^{42,44}\), employing Nb 4d orbitals and Se 5p orbitals as basis functions. The resulting tight-binding Hamiltonian allows a direct extraction of the spin and layer projections of the electronic structure.
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Acknowledgements
We thank M.R. Lees for assistance with the transport measurements and C. Howley, P. Wahl, A.P. Mackenzie, S. Lee and B. Braunecker for useful discussions. We gratefully acknowledge support from the Engineering and Physical Sciences Research Council, UK (work at St Andrews under Grant No. EP/I031014/1 and work at Warwick under Grant No. EP/M028771/1) and the International Max Planck partnership. P.D.C.K. acknowledges support from the Royal Society through a University Research Fellowship. M.S.B. was supported by the Grant-in-Aid for Scientific Research (S) (No. 24224009) from the Ministry of Education, Culture, Sports, Science and Technology (MEXT) of Japan. L.B., J.M.R. and V.S. acknowledge studentship funding from EPSRC through Grant Nos. EP/G03673X/1, EP/I050579/1 and EP/I015110/1, respectively. The experiments at MAX IV Laboratory were made possible through funding from the Swedish Research Council and the Knut and Alice Wallenberg Foundation. We also thank Diamond Light Source for access to beamline I05 (Proposal No. SI11383) that contributed to the results presented here.

Author contributions
The experimental data were measured by L.B., S.P.C., F.M., J.M.R., L.J.C-M., V.S., K.W.B.H., C.M.P., J.W.W. and P.D.C.K., and analyzed by L.B.; theoretical calculations were performed by M.S.B. G.B. synthesized the samples used in this study; M.L., C.M.P., T.B., T.K.K. and M.H. maintained the synchrotron ARPEX end stations and provided experimental support; P.D.C.K., M.S.B. and L.B. wrote the manuscript, with input and discussions from all co-authors; P.D.C.K. conceived the study and was responsible for overall project planning and direction.

Additional information
Supplementary Information accompanies this paper at http://www.nature.com/naturecommunications

Competing financial interests: The authors declare no competing financial interests.

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How to cite this article: Bawden, L. et al. Spin–valley locking in the normal state of a transition metal dichalcogenide superconductor. Nat. Commun. 7:11711 doi: 10.1038/ncomms11711 (2016).

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