Implementation of Two-Stream Emission Model for L-Band Retrievals on the Tibetan Plateau

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Abstract: This study assesses the suitability of the two-stream microwave emission model in simulating brightness temperature ($T_B$) and retrieving liquid water content ($\theta_L$) at L-band in combination with the four-phase dielectric model for both thawed and frozen soil. Both single (SCA) and double (DCA) channel algorithms are adopted using both ground-based ELBARA-III and spaceborne SMAP measurements conducted in a Tibetan grassland site. The ELBARA-III measured $T_B$ are smaller than the SMAP measurements in the warm season due to a lower value of average $\theta_L$ presented within the ELBARA-III footprint. The two-stream emission model configured with SMAP vegetation and surface roughness parameterization underestimates both ELBARA-III and SMAP measured $T_B$ at horizontal polarization in the cold season, and overestimates the vertical polarized measurements ($T_V$) in the warm season. Implementation of a new surface roughness and vegetation parameterization resolves above deficiency, and the simulations capture better largescale SMAP measurements in comparison to these performed for the ELBARA-III footprint. The dynamics of in situ $\theta_L$ are better reproduced by retrievals using the SCA based on $T_V$ measurements (SCA-V), whereby the SCA-V retrievals using the SMAP ascending overpass measurements shows the best results with an unbiased root-mean-square error (ubRMSE) of 0.035 m$^3$ m$^{-3}$ that outperforms the SMAP mission specification.

Keywords: Soil Moisture Active Passive (SMAP); L-band microwave radiometry; thawed and frozen soil conditions; liquid water content; grassland; Tibetan Plateau

1. Introduction

Passive microwave remote sensing at L-band (1-2 GHz) is recognized as one of the most useful approaches for worldwide monitoring of surface soil moisture and freeze–thaw state [1,2]. Two currently operating satellite missions, i.e., the SMOS (Soil Moisture and Ocean Salinity) and SMAP (Soil Moisture Active Passive) launched, respectively, in 2009 by the European Space Agency (ESA) and in 2015 by the National Aeronautic and Space Administration (NASA), all use this technology to map global soil moisture. In the meantime, numerous studies have been devoted over the past decade to improve parameterizations of the commonly used $\tau-\omega$ microwave emission model [3] and retrieval of soil moisture by these two missions [2,4,5].

The $\tau-\omega$ microwave emission model includes radiative components from both vegetation canopy and soil surface, whereby the vegetation canopy is generally treated as a single homogeneous “soft layer” [6,7]. This model is a zero-order solution of the microwave radiative transfer equations, which generally neglects multiple reflections between vegetation canopy and underground soil surface and does not follow the Kirchhoff’s law [8]. In addition, the $\tau-\omega$ microwave emission model also neglects the multiple scattering processes in the vegetation canopy that is inadequate to represent canopy volume scattering [9–11]. To resolve this problem, a common way is to calibrate
the vegetation parameters, i.e., the single-scattering albedo $\omega$ and vegetation optical depth $\tau$, to match brightness temperature ($T_w$) measurements [12,13] or simulations produced by numerical models [11,14–16]. As such, Kurum [17] showed that the canopy volume scattering can be accounted for by using the equivalent/effective vegetation parameters, and thus the first-order solution of microwave radiative transfer equations can be appropriately reproduced by the zero-order $\tau$-$\omega$ model. However, calibration of the $\tau$-$\omega$ model generally requires spaceborne, aircraft- or ground-based $T_w$ measurements, and the calibration also needs a network of in situ measurements across different climate and vegetation types with the assumption that the calibrated parameters can be applied to other similar geographical regions [9].

On the other hand, higher-order solution of the microwave radiative transfer equations has been developed to overcome the abovementioned deficiencies of zero-order $\tau$-$\omega$ emission model [6,9]. For instance, a two-stream emission model has recently been developed by Schwank et al. [6] according to the framework of MEMLS (Microwave Emission Model of Layered Snowpacks) model [18,19]. It’s shown that the two-stream emission model that considers multiple scattering and reflection is physically more correct than the $\tau$-$\omega$ microwave emission model, whereby the “soft layer” assumption is removed [6]. Li et al. [7] and Schwank et al. [6] have recently compared the performances of two-stream and $\tau$-$\omega$ emission models in simulating the $T_w$ and retrieving soil moisture using ground-based and spaceborne measurements at local and global scales, respectively. The results have demonstrated the potential of replacing the $\tau$-$\omega$ model with the two-stream microwave emission model in the soil moisture retrieval algorithms due to its better performance. Specifically, the formulation of the single layer two-stream microwave emission model is as simple as the $\tau$-$\omega$ emission model, whereby the former is also applicable to snow condition [20,21] that makes it possible to implement a single microwave emission model for applications to different land conditions [7]. However, the performance of the two-stream microwave emission model for its application to frozen ground is still unknown, whereby the frozen ground is widely presented in the northern hemisphere, i.e., covers more than 50% of the land in the winter [22–24].

However, most of the currently widely used soil dielectric models, i.e., the semi-empirical models proposed by Mironov et al. [25] and Dobson et al. [26], are only applicable to thawed soil condition. To date, there are three soil dielectric models that can be applicable to both thawed and frozen soil conditions, i.e., modified versions of abovementioned Dobson [27] and Mironov [28] models and the four-phase dielectric model [29,30]. Mironov [28] demonstrated that their model provides a better estimate of soil permittivity in comparison to the model of Zhang et al. [27]. Recently, Zheng et al. [31] have shown that the four-phase dielectric mixing model is more suitable for simulating the $T_w$ on the Tibetan Plateau via comparing the performance of the above three soil dielectric models. The $T_w$ simulations are also sensitive to the vegetation and surface roughness parameterizations. The semi-empirical model proposed by Wang and Choudhury [32] has often been implemented to account for the impact of surface roughness, which adopts three parameters, namely, $Q$ represents the impact of polarization mixing, $h$ accounts for the increase/decrease in reflectivity affected by the surface roughness, and $N$ represents the angular dependence of reflectivity. On the other hand, the extinction and scattering effects of vegetation are usually expressed by the optical depth $\tau$ and effective scattering albedo $\omega$ [33]. In the baseline soil moisture retrieval algorithm of the SMAP mission, the $h$ and $\tau$ are, respectively, linearly correlated to the RMS height ($s$) and vegetation water content (VWC), the $Q$ is assumed to be zero, and $\omega$ is defined for specific vegetation types [34]. Recent studies [35–37] have suggested that the $Q$ is non-zero, and the empirical power-law relationship developed by Wigneron et al. [13] has also been widely implemented in the literature [35,36,38]. Recently, Zheng et al. [16,39] indicated that the SMAP algorithm overestimates the effect of vegetation canopy and underestimates the impact of surface roughness over the
Tibetan Plateau, and a new parameterization has thus been proposed to address these problems. Similar findings have also been reported by Chaubell et al. [40].

In this study, we expand the application of the two-stream microwave emission model to both thawed and frozen soil conditions by incorporating the four-phase dielectric mixing model. Its performance in simulating L-band $T_{\text{w}}$ and retrieving liquid water content ($\theta_{\text{hiq}}$) has been tested using both spaceborne SMAP and ground-based ELBARA-III radiometry measured $T_{\text{w}}$ conducted in a Tibetan grassland site. The impact of different surface roughness and vegetation parameterizations on the $T_{\text{w}}$ simulation is also assessed, and the $\theta_{\text{hiq}}$ is retrieved using both single (SCA) and double (DCA) channel algorithms. In Section 2, we show the simultaneous SMAP and ELBARA-III $T_{\text{w}}$ measurements, and Section 3 outlines the two-stream microwave emission model as well as the thereon-based $\theta_{\text{hiq}}$ retrieval algorithms. The comparative analysis of SMAP and ELBARA-III $T_{\text{w}}$ measurements and their relationships with in situ $\theta_{\text{hiq}}$ are presented in Section 4. Impacts of surface roughness and vegetation parameterizations on the $T_{\text{w}}$ simulations and $\theta_{\text{hiq}}$ retrievals based on SMAP and ELBARA-III measured $T_{\text{w}}$ are investigated in Section 4 as well. The findings are summarized in the Section 5.

2. Study Area and Observations

2.1. Maqu Station

The Maqu soil moisture (SM) monitoring network is located within the Yellow River source region on the northeastern part of the Tibetan Plateau (Figure 1). The Maqu network is configured with about 30 SM profile monitoring sites, which was chosen as one of the calibration/validation sites by the SMAP scientific team for evaluating the SMAP soil moisture retrievals [41]. The dominant land cover is alpine meadows, and the soil type is generally dominated by silt loam, whereby the average sand and clay percentage are about 30% and 10%, and the average bulk density ($\rho_b$) is about 1 g cm$^{-3}$ [16]. The elevations vary from 3400 to 3800 m.

Each monitoring site records readings of SM at different soil depths ranging from 5 to 80 cm every 15 min using the Decagon 5TM probes. In the air, the 5TM sensors integrate a volume of 715 mL around the prong, with a maximum distance of 6 cm from the center of the sensor. In the soil, the zone of influence ranges from 3 to 4 cm from the middle prong of the 5TM sensors [42]. To further improve the measured accuracy of in situ soil liquid water contents $\theta_{\text{hiq}}$ derived from the 5TM capacitance measurements, Dente et al. [43] have developed several calibration functions for specific soil types found across the Maqu area. Detailed description of the Maqu SM network is referred to Zheng et al. [44] and Zhang et al. [45].
2.2. ELBARA-III Field Site

For the purpose of evaluating the SMOS and SMAP measurements over the Tibetan Plateau, the L-band ELBARA-III radiometer [46] was setup within the Maqu in situ SM monitoring network (Figure 1) in January, 2016 [47,48]. The ELBARA-III radiometer has been deployed on a tower with 4.8 m height above the ground, and the beam waist of the antenna is about 6.5 m height. Both horizontal ($T_b^h$) and vertical ($T_b^v$) polarized $T_b^r$ of ground have been measured for incidence angles ranging from 40° to 70° in steps of 5° every 30 min. Concurrent to the $T_b^r$ measurements, next to the radiometer tower SM and soil temperature (SMST) profiles have been measured by the STM probes as well, and micrometeorological measurements have also been performed in the field site. An additional description of the ELBARA-III observation site and the abovementioned in situ measurements was outlined by Zheng et al. [47,48].
2.3. SMAP Products

The SMAP satellite mission led by the NASA has been launched in January 2015, which is configured with an L-band (1.41 GHz) radiometer and an L-band (1.26 GHz) radar. The radar ceased operations in July 2015, while the radiometer continues to work and provides a spatial extent of about 40 km with off-nadir incidence angle $\psi \approx 40^\circ$ as expected.

Latest versions of Level 1C radiometer product and Level 2 radiometer SM product are utilized in this study, which is gridd ed on a 36 km Equal-Area Scalable Earth-2 (EASE2) grid and is available at https://nsidc.org/data/smap/smap-data.html (accessed on January 2022). A centered validation grid pixel has been defined by the SMAP scientific team for the Maqu SM monitoring network to address the uncertainties related to the spatial mismatch between the SMAP soil moisture retrievals and the in situ references [41]. In Figure 1, it can be noted that the ELBARA-III monitoring station is placed at the upper right part of the SMAP validation grid. The $T^\psi$ measurements of SMAP during both ascending (6 PM) and descending (6 AM) overpasses are used in this study, and the data during the period from August 2016 to July 2017 are extracted for the validation grid pixel. There are about 360 SMAP measurements that are available for the presented research.

Both SMAP and ELBARA-III measured $T^\psi$ and the corresponding footprint average $\theta_{\text{iq}}$ used in this study is provided as Supplementary Material. Please find the supplementary Table S1 for the details.

3. Methods

3.1. Two-Stream Microwave Emission Model

The two-stream emission model developed by Schwank et al. [6] is implemented to simulate the land surface emission in this study:

$$
T^p_B = T^p_G \cdot e^p_s + T^p_V \cdot e^p_v + T^p_{\text{sky}} \cdot e^p_{\text{sky}},
$$

(1)

$$
e^p_s = \gamma_s (1 - r^p) / (1 - r^p r_\gamma),
$$

(2)

$$
e^p_v = (1 - r_\gamma - \gamma_s)(1 - r^p r_\gamma + r^p \gamma_s) / (1 - r^p r_\gamma),
$$

(3)

$$
e^p_{\text{sky}} = 1 - e^p_s - e^p_v,
$$

(4)

$$
\gamma_s = \frac{2 \cdot \exp(\tau \sqrt{1 - \omega^2 / \cos \psi}) \cdot [1 - \omega^2 + \sqrt{1 - \omega^2}]}{\exp(2 \tau \sqrt{1 - \omega^2 / \cos \psi}) \cdot [2 - \omega^2 + 2 \sqrt{1 - \omega^2} - \omega^2]},
$$

(5)

$$
r^p_\gamma = \frac{\omega \cdot [\exp(2 \tau \sqrt{1 - \omega^2 / \cos \psi}) - 1] \cdot [1 + \sqrt{1 - \omega^2}]}{\exp(2 \tau \sqrt{1 - \omega^2 / \cos \psi}) \cdot [2 - \omega^2 + 2 \sqrt{1 - \omega^2} - \omega^2]},
$$

(6)

where $p$ indicates the polarization of microwave emission ($p = H$, horizontal; $p = V$, vertical), $T^p_G$, $T^p_V$, and $T^p_{\text{sky}}$ are the effective vegetation and soil temperature (K), $T^p_{\text{sky}}$ represents the sky brightness temperature (K), $e^p_s, e^p_v$, and $e^p_{\text{sky}}$ are emissivity (-) of soil, vegetation and sky, $r_\gamma$ represents the vegetation reflectivity (-), $\gamma_s$ represents the transmissivity of vegetation canopy (-), $r^p$ represents the rough soil reflectivity (-), $\omega$ represents the effective scattering albedo (-), $\tau$ represents the vegetation optical depth (-), and $\psi$ is the incidence (observation) angle (-). The $T^p_{\text{sky}}$ can be estimated by an empirical approach using air temperature and elevation as input [49], which is ignored in this study due to the fact that its value is very small at L-band ($\approx 5$ K) [6].

The estimation of $r^p$ is formulated as [50]:

$$
r^p = [(1 - Q) \cdot r^p_s + Q \cdot r^p_v] \cdot \exp(-h \cdot \cos \psi),
$$

(7)
where \( q \) indicates the polarization of microwave emission (\( q = H \), horizontal; \( q = V \), vertical), \( r_s\) and \( r_i \) are the specular reflection coefficients (-), \( N \) represents the angular effect on the reflectivity (-), \( h \) takes into account the intensity effect (-), and \( Q \) refers to the impact of polarization mixing (-). The \( r_s\) and \( r_i \) are estimated by the Fresnel’s equations [33] using the effective soil permittivity \( \varepsilon_s \) as input:

\[
\begin{align*}
 r_s^H &= \frac{\cos \psi - \sqrt{\varepsilon_s - \sin^2 \psi}}{\cos \psi + \sqrt{\varepsilon_s - \sin^2 \psi}}, \\
 r_s^V &= \frac{\varepsilon_s \cos \psi - \sqrt{\varepsilon_s - \sin^2 \psi}}{\varepsilon_s \cos \psi + \sqrt{\varepsilon_s - \sin^2 \psi}},
\end{align*}
\]

(8)

(9)

The soil permittivity \( \varepsilon_s \) (\( \varepsilon_s = \varepsilon_s' + i \varepsilon_s'' \)) of the thawed or frozen soil condition is simulated by the four-phase soil dielectric model as [30,31,51]:

\[
\varepsilon_s^\eta = \left( \theta - \theta_s^\eta \right) \varepsilon_{air}^\eta + \theta_s^\eta \varepsilon_w^\eta + \left( \theta - \theta_s^\eta \right) \varepsilon_{ice}^\eta + \left( 1 - \theta_s^\eta \right) \varepsilon_{matrix}^\eta,
\]

(10)

where \( \theta_s^\eta \) represents the porosity (m\(^3\) m\(^{-3}\)), \( \theta \) represents the soil total water content (m\(^3\) m\(^{-3}\)) that derived from the in situ \( \theta_{air} \) (m\(^3\) m\(^{-3}\)) as in Zheng et al. [52]. The exponent \( \eta \) is specified as 0.5, and the complex permittivity of ice, dry soil matrix and air are taken from Schwank et al. [30] as \( \varepsilon_{ice} = 3.2 + i0.1 \), \( \varepsilon_{matrix} = 5.5 + i0.2 \) and \( \varepsilon_{air} = 1 \). The complex permittivity of liquid water (\( \varepsilon_{w} \)) is computed using the Dobson et al. [26] model as in Zheng et al. [47].

During the SMAP overpass (6 PM or 6 AM), it’s reasonable to assume that the near-surface vegetation and air are in thermal equilibrium with \( T_s \approx T_c \), which can be represented by the effective soil temperature \( T_{eff} \). Here, we compute \( T_{eff} \) according to Choudhury et al. [53] from available in situ SMST information as:

\[
T_{eff} = \int_0^\infty T_s(z) \alpha(z) \exp \left[ - \int_0^z \alpha(z')dz' \right] dz,
\]

(11)

\[
\alpha(z) = \frac{4\pi}{\lambda} \cdot \text{Im} \left( \sqrt{\varepsilon_s} \right),
\]

(12)

where \( \lambda \) is the vacuum wavelength (cm), \( T_s(z) \) is the soil temperature (K), and \( \alpha(z) \) is the attenuation coefficient (-) at soil depth \( z \).

In this study, the surface roughness parameter \( N \) in Equation (7) and vegetation parameter \( \omega \) in Equations (5) and (6) are set equal to 2 and 0.05 as the SMAP retrieval algorithm [34] for grassland, and two parameterizations are adopted to estimate the parameters \( \tau \) in Equations (5) and (6), as well as \( h \) and \( Q \) in Equation (7). One is to implement the parameterization adopted by the SMAP retrieval algorithm [34] (hereafter “SMAP parameterization”) as:

\[
\tau = b \cdot VWC,
\]

(13)

\[
VWC = 1.9134 \cdot \text{NDVI}^2 - 0.3215 \cdot \text{NDVI} \quad + 1.5 \cdot (\text{NDVI} - 0.1) / (1 - 0.1)
\]

(14)

\[
h = 0.01 \cdot s,
\]

(15)

\[
Q = 0,
\]

(16)

where NDVI refers to the normalized difference vegetation index (-), VWC refers to the vegetation water content (-), and \( s \) represents the standard deviation of surface roughness height (mm). The parameters \( b \) and \( s \) are set equal to 0.13 (-) and 15.6 mm as the SMAP
retrieval algorithm [34] for grassland, which lead to the value of 0.156 for the \( h \) according to Equation (15).

The other is to implement the new vegetation and surface roughness parameterization newly developed by Zheng et al. [16,39] (hereafter “Zheng’s parameterization”) which showed that the SMAP parameterization underestimates the impact of surface roughness and overestimates the effect of vegetation in the Tibetan grassland and desert ecosystems:

\[ \tau = 0.025 \cdot \text{LAI}, \]  
\[ h = \left( \frac{0.9437 \cdot s}{0.8865 \cdot s + 2.2913} \right)^6, \]  
\[ Q = 0.1771 \cdot h, \]  

where LAI is the leaf area index (m² m⁻²), \( s \) is also set equal to 15.6 mm as the SMAP retrieval algorithm [34] for grassland, which leads to values of 0.58 and 0.1 for the \( h \) and \( Q \) according to Equations (18) and (19).

The needed NDVI and LAI in this study are obtained from the MODIS MOD13A2 [54] and MOD15A2 [55] products, respectively. Figure 2 presents the time series of vegetation optical depth \( \tau \) estimated by the SMAP and Zheng’s parameterizations for the SMAP descending overpass from August 2016 and July 2017 that is consistent with both SMAP and ELBARA-III measurements. The \( \tau \) estimates, based on the SMAP parameterization, are considerably larger than those computed by the new parameterization of Zheng et al. [16]. On the contrary, Zheng’s parameterization tends to produce larger values of \( Q \) and \( h \) in comparison to SMAP parameterization, i.e., 0.1 vs. 0 for the \( Q \), and 0.58 vs. 0.156 for the \( h \).

To help the reader understand how the two-stream emission model is implemented with either SMAP or Zheng’s vegetation and surface roughness parameterization to simulate the \( T_{\delta v} \), a sample computation is provided as Supplementary Material. Please find the supplementary Table S2 for the details.

![Figure 2](image.png)

**Figure 2.** Time series of \( \tau \) estimates derived from SMAP and Zheng’s parameterizations between August 2016 and July 2017 for the SMAP descending overpass.

### 3.2. Soil Liquid Water Content Retrieval Algorithms

Both the single channel soil moisture retrieval algorithm (SCA) using either the \( T_{\delta h} \) (SCA-H) or \( T_{\delta v} \) (SCA-V) measurements and double channel algorithm (DCA) using both \( T_{\delta v} \) and \( T_{\delta h} \) measurements implemented by the SMAP retrieval algorithm [34] are adopted to retrieve the \( \theta_{\text{liq}} \) in this study for both thawed and frozen soil conditions. The two-stream emission model is adopted for the forward land emission modelling with the implementation of the four-phase soil dielectric model (see Section 3.1), whereby the better performance of vegetation and surface roughness parameterization (SMAP or...
Zheng’s parameterization) is implemented to estimate the parameters \( \tau, h, \) and \( Q \). Additional information about the SCA and DCA retrieval approaches is referred to O’Neill et al. [34].

4. Results

4.1. Comparisons between SMAP and ELBERA-III \( T_\psi \) Observations

Figure 3 presents the time series of \( T_{B1}^{hi} \) and \( T_\psi \) measurements collected by the SMAP and ELBERA-III radiometer at the observation angle \( \psi \) of 40\(^\circ\). The SMAP measurements performed between August 2016 and July 2017 during both ascending and descending overpasses are considered, and the ELBERA-III measurements closest to the overpasses of SMAP are extracted for the comparison. The data gap noted for the ELBERA-III measurements is caused by power supply failures. Figure 3 also presents the statistical errors estimated between the SMAP and ELBERA-III measurements, which includes the root-mean-square error (RMSE), bias, unbiased RMSE (ubRMSE) and Pearson product moment correlation coefficient (R). Figure 4 further shows the spatial \( \theta_{\text{liq}} \) averages at 5 cm soil depth taken from the in situ data collected within the footprints of ELBERA-III and SMAP measurements (Figure 1). The error statistics estimated between the in situ \( \theta_{\text{liq}} \) representative of the ELBERA-III and the SMAP footprints are shown in Figure 4 as well.

The \( \theta_{\text{liq}} \) dynamics of the ELBERA-III and SMAP footprints are comparable to each other (Figure 4). Pearson’s correlation coefficient R between the two in situ \( \theta_{\text{liq}} \) averages is high (\( R \geq 0.96 \)) during the SMAP overpasses. In general, the soil is unfrozen and wet from May to October (i.e., warm season), while it appears as frozen and dry between November and April (i.e., cold season). In the warm season, the average \( \theta_{\text{liq}} \) of the ELBERA-III footprint is generally smaller than that within the SMAP footprint, which is due to the fact that the soil porosity and water holding capacity are higher within the SMAP footprint caused by larger organic matter contents found in the soil [43,44]. Comparison of Figures 3 and 4 shows that both ELBERA-III and SMAP measured dynamics of \( T_\psi \) generally follow the \( \theta_{\text{liq}} \) variations in the warm season, whereby the \( T_\psi \) increase with decreasing \( \theta_{\text{liq}} \) (e.g., July 2017) and vice versa (e.g., September 2016). In the cold season, the \( \theta_{\text{liq}} \) sharply decreases due to soil freezing between November and February that results in the increase in \( T_\psi \), while thawing of soil ice between February and April leads to increase in \( \theta_{\text{liq}} \) and thus a decrease in \( T_\psi \). Generally, the SMAP and ELBERA-III measured \( T_\psi \) show high correlation as indicated by \( R \geq 0.87 \) except for the \( T_{B1}^{hi} \) during the SMAP descending overpass (Figure 3a). In addition, the ELBERA-III measured \( T_\psi \) are generally larger than the SMAP measurements between June and October due to the fact that \( \theta_{\text{liq}} \) of ELBERA-III footprint is smaller than that of SMAP footprint.

![Figure 3: Time series of \( T_{B1}^{hi} \) and \( T_\psi \) measurements.](image)

![Figure 4: Spatial \( \theta_{\text{liq}} \) averages within footprints.](image)
4.2. Relations between $T_b^v$ and $\theta_{lh}$ Observations

Figure 5 shows the relations of the $T_b^h$ (left panel), $T_b^v$ (middle panel) and polarization ratio (PR = ($T_b^v - T_b^h$)/($T_b^v + T_b^h$), right panel) extracted from the ELBRA-III and SMAP measurements at $\psi = 40^\circ$ versus the corresponding footprint averaged $\theta_{lh}$. The analysis is conducted for the cold (November–April) and warm (May–October) seasons during the SMAP descending (top panel) and ascending overpasses (bottom panel) between 2016 and 2017, respectively. The corresponding R are also shown in Figure 5. Compared to the ELBRA-III measurements, the $T_b^h$, $T_b^v$ and PR obtained from the SMAP measurements show higher correlations with footprint averaged $\theta_{lh}$ for both cold and warm periods during both SMAP descending and ascending overpasses as indicated by smaller scatters and thus higher R values (Figure 5).

The correlations between both ELBRA-III and SMAP measured $T_b^v$ and the footprint averaged $\theta_{lh}$ in the warm season are best explained by a linear function, with $R^2$ values larger than 0.81 during both SMAP descending and ascending overpasses. In contrast, the largest scatter is found for the plot with the ELBRA-III derived PR versus the footprint averaged $\theta_{lh}$. In the cold season, the SMAP measurements (i.e., $T_b^h$, $T_b^v$ and PR) are better linked to the $\theta_{lh}$ measurements during the SMAP ascending overpass, while the ELBRA-III measurements show better agreement with the in situ $\theta_{lh}$ during the SMAP descending overpass. In general, higher $R^2$ values are found between both SMAP and ELBRA-III measured $T_b^h$ and the $\theta_{lh}$ measurements in the cold period, and the relationship between SMAP measured $T_b^v$ and the in situ $\theta_{lh}$ shows the highest $R^2$ value during the SMAP ascending overpass.
4.3. Brightness Temperature Simulation

To investigate the performance of the two-stream emission model and its sensitivity to different vegetation and surface roughness parameterizations, two simulations are performed with the two-stream model using either the SMAP (Sim1) or Zheng’s (Sim2) parameterization (see Section 3.1). The SMST input data are specified as the arithmetic average of in situ data collected within either the ELBRA-III or the SMAP footprint (Section 2) closest to the SMAP overpasses for matching the $T_{b}^{\upsilon}$ simulations with either the SMAP or the ELBRA-III measurements.

Figure 6 shows the time series of SMAP $T_{b}^{\upsilon}$ measurements and simulations produced from both Sim1 and Sim2 performed for the SMAP footprint between August 2016 and July 2017 for the SMAP descending and ascending overpasses. The corresponding statistical errors estimated between the measured and simulated $T_{b}^{\upsilon}$ are provided in Table 1. The SMAP $T_{b}^{\upsilon}$ measurements are underestimated by the two-stream microwave emission model configured with the vegetation and surface roughness parameterizations of SMAP mission (Sim1) for the cold season (November–April), and the SMAP measured $T_{b}^{\upsilon}$ are overestimated for the warm season (June–October). These discrepancies are strongly reduced when using Zheng’s surface roughness and vegetation parameterizations within the two-stream model (Sim2). Particularly, the ubRMSE errors are reduced by, on average, about 44% and 29% for the $T_{b}^{h}$ and $T_{b}^{\upsilon}$. This demonstrates that the impact of surface roughness is underestimated by the Sim1 based on the SMAP parameterizations with the implementation of lower values of $Q$ and $h$, and the vegetation effect is overestimated due to the usage of higher $\tau$ values (Figure 2) in accordance with the findings of Zheng et al. [16]. In addition, it can be noted that both Sim1 and Sim2 underestimate the SMAP measured $T_{b}^{h}$ and $T_{b}^{\upsilon}$ for the transition seasons with soil thawing from March and April and soil freezing between October and November and during the SMAP descending overpass. However, such underestimations disappeared in the SMAP ascending overpass. The SMAP $T_{b}^{\upsilon}$ measurements are better captured by both Sim1 and Sim2 in terms of error statistics in comparison to the $T_{b}^{h}$ simulation due to the higher correlation with the measured $\theta_{liq}$ as shown in Section 4.2.
Figure 7 further shows the time series of ELBARA-III $T_{\psi}$ measurements and simulations for the off-nadir angle $\psi = 40^\circ$ produced by both Sim1 and Sim2 performed for the ELBARA-III footprint during the SMAP overpasses. The corresponding statistical errors estimated between the ELBARA-III measured and simulated $T_{\psi}$ are given in Table 2. Similar to the SMAP case, the Sim2 reduces the $T_{\psi}^{H}$ underestimation between November and February and the $T_{\psi}^{V}$ overestimation between June and October noted for the Sim1. In addition, the ELBARA-III measured $T_{\psi}^{V}$ are better captured in comparison to the $T_{\psi}^{H}$ simulation. However, it should be noted that both $T_{\psi}^{H}$ and $T_{\psi}^{V}$ are still underestimated between January and February, which is most probably due to the fact that the $\theta_{\text{liq}}$ measurement at 5 cm soil depth do not necessarily represent well the ELBARA-III sensing depth as reported by Zheng et al. [47,48]. Such underestimations are not found in the simulations performed with Sim2 for the large-scale SMAP $T_{\psi}$ measurements, which is consistent with the better agreements noted between SMAP measurements and the in situ $\theta_{\text{liq}}$ (see Section 4.2).

![Figure 6](image_url)

**Figure 6.** Time series of the SMAP (a,c) $T_{\psi}^{H}$ and (b,d) $T_{\psi}^{V}$ measurements and simulations performed for the SMAP footprint during the SMAP descending (a,b) and ascending (c,d) overpasses between August 2016 and July 2017. Sim1: two-stream emission model configured with SMAP parameterization; Sim2: Zheng’s parameterization.
Figure 7. Time series of the ELBARA-III (a,c) $T_{BH}$ and (b,d) $T_{BV}$ measurements and simulations performed for the ELBARA-III footprint during the SMAP descending (a,b) and ascending (c,d) overpasses between August 2016 and July 2017. Sim1: two-stream emission model configured with SMAP parameterization; Sim2: Zheng’s parameterization.

Table 1. Error statistics estimated between the SMAP measured and simulated $T_B$ performed for the SMAP footprint between August 2016 and July 2017 for the SMAP ascending and descending overpasses. Sim1: SMAP parameterization; Sim2: Zheng’s parameterization.

| Simulations | $T_{BH}$ ubRMSE (K) | Bias (K) | RMSE (K) | R | $T_{BV}$ ubRMSE (K) | Bias (K) | RMSE (K) | R |
|-------------|---------------------|---------|----------|---|---------------------|---------|----------|---|
|             |                     |         |          |   |                     |         |          |   |
| Descending  |         |         |          |   |         |         |          |   |
| Sim1        | 16.88              | -11.86  | 20.63    | 0.70 | -2.56              | 11.54   | 0.79     |
| Sim2        | 9.23               | -6.29   | 11.17    | 0.90 | -4.25              | 9.10    | 0.90     |
|             |         |         |          |   |         |         |          |   |
| Ascending   |         |         |          |   |         |         |          |   |
| Sim1        | 14.50              | -6.60   | 15.93    | 0.78 | -2.56              | 7.42    | 0.89     |
| Sim2        | 8.35               | -0.27   | 8.35     | 0.93 | -0.91              | 5.26    | 0.94     |

Table 2. Error statistics estimated between the ELBARA-III measured and simulated $T_B$ performed for the ELBARA-III footprint between August 2016 and July 2017 for the SMAP ascending and descending overpasses. Sim1: SMAP parameterization; Sim2: Zheng’s parameterization.

| Simulations | $T_{BH}$ ubRMSE (K) | Bias (K) | RMSE (K) | R | $T_{BV}$ ubRMSE (K) | Bias (K) | RMSE (K) | R |
|-------------|---------------------|---------|----------|---|---------------------|---------|----------|---|
|             |                     |         |          |   |                     |         |          |   |
| Descending  |         |         |          |   |         |         |          |   |
| Sim1        | 12.72              | -6.82   | 14.43    | 0.81 | 1.19               | 9.11    | 0.80     |
| Sim2        | 12.29              | -1.76   | 12.41    | 0.83 | -0.43              | 7.09    | 0.88     |
|             |         |         |          |   |         |         |          |   |
| Ascending   |         |         |          |   |         |         |          |   |
4.4. Soil Liquid Water Content Retrieval

The two-stream emission model configured with the four-phase soil dielectric model (see Section 3.1) is adopted by the SCA-V, SCA-H and DCA algorithms (see Section 3.2) to retrieve the $\theta_{hiq}$, whereby Zheng's vegetation and surface roughness parameterization is implemented to estimate the parameters $\tau$, $h$, and $Q$ due to its better performance (see Section 4.3). Both ELBARA-III and SMAP measured $T_w^{\text{at}}$ and $T_w^{\text{v}}$ during both ascending and descending overpasses are used to retrieve the $\theta_{hiq}$ for both cold and warm periods, and the in situ $\theta_{hiq}$ representative of both ELBARA-III and SMAP footprints measured at 5 cm depth are utilized to identify the optimum retrievals.

Figure 8a,b show the time series of in situ $\theta_{hiq}$ representative of SMAP footprint (black line) and the retrieved $\theta_{hiq}$ obtained by the SCA-V, SCA-H and DCA algorithms (colored lines) based on the SMAP $T_w^{\text{v}}$ measurements during the period between August 2016 and July 2017 for the descending and ascending overpasses, respectively. Corresponding statistical errors estimated between the $\theta_{hiq}$ measurements and retrievals are given in Table 3. For the comparison purpose, the $\theta_{hiq}$ retrieval derived from the SMAP radiometer soil moisture product (see Section 2.3) is also presented in Figure 8 (orange line). It can be found that the SMAP $\theta_{hiq}$ retrieval is only available for the warm season since the adopted soil dielectric mixing model developed by Mironov et al. [25] is only suitable for thawed soil condition. On the contrary, the SCA-V, SCA-H and DCA approaches configured with the four-phase soil dielectric mixing model are able to retrieve $\theta_{hiq}$ for both cold and warm periods in this study. In general, the retrieved $\theta_{hiq}$ obtained by the SCA-V, SCA-H and DCA approaches based on the SMAP $T_w^{\text{v}}$ measurements are comparable to each other, which capture well both magnitudes and dynamics of in situ $\theta_{hiq}$ representative of SMAP footprint for both warm and cold seasons during both descending and ascending overpasses. In addition, all the $\theta_{hiq}$ retrievals produced in this study are better than the SMAP $\theta_{hiq}$ product, and the latter tends to underestimate the $\theta_{hiq}$ measurements due to poorer performance of SMAP default vegetation and surface roughness parameterizations (Section 4.3). It can be noted that all the $\theta_{hiq}$ retrievals including SMAP product underestimate the $\theta_{hiq}$ measurements for the transition seasons with soil thawing from March and April and soil freezing between October and November during the descending overpass due to underestimations of both $T_w^{\text{at}}$ and $T_w^{\text{v}}$ simulations (see Figure 6). Such underestimations, however, disappeared in the SMAP ascending overpass for the $\theta_{hiq}$ retrievals produced in this study. The reason can be that the spatial heterogeneity of soil freezing is not fully represented by the measured $\theta_{hiq}$ representative of SMAP footprint as also given in Zheng et al. [16]. The error statistics shown in Table 3 reflect the better performance of $\theta_{hiq}$ retrievals obtained with the SCA-V than with SCA-H or DCA especially during the ascending overpass as indicated by lower RMSE and ubRMSE values. This finding supports the use of the SCA-V approach as the baseline soil moisture retrieval algorithm of the SMAP mission [36] for the Tibetan environments. Notably, the SCA-V gives the best $\theta_{hiq}$ retrievals that match the average $\theta_{hiq}$ measurements of the SMAP footprint, especially when the SMAP $T_w^{\text{v}}$ measured during the ascending overpass are used. For these circumstances, an $\text{ubRMSE} = 0.035 \text{ m}^3 \text{ m}^{-3}$ is produced, which outperforms the mission goal of SMAP with an expected $\text{ubRMSE}$ of 0.04 $\text{ m}^3 \text{ m}^{-3}$ [4]. This indicates that the SMAP $T_w^{\text{v}}$ measurements during the ascending overpass can be the better choice to retrieve the $\theta_{hiq}$ for both warm and cold periods using the SCA-V approach.

Figure 9 further shows the time series of measured $\theta_{hiq}$ representative of ELBARA-III footprint (black line) and retrieved $\theta_{hiq}$ obtained by the three SM retrieval algorithms (colored lines) using the ELBARA-III measured $T_w^{\text{v}}$ at the observation angle of 40°. Corresponding statistical errors estimated between the measured $\theta_{hiq}$ and associated retrievals are also provided in Table 3. As in the case for the retrievals using the SMAP $T_w^{\text{v}}$ measurements, the SCA-V algorithm also outperforms the two other methods (i.e., DCA

|     | Sim1 | 0.97 | 18.34 | 18.36 | 0.76 | 10.56 | 3.76 | 11.21 | 0.80 |
|-----|-----|------|-------|-------|------|-------|------|-------|-----|
|     | Sim2 | 0.674 | 19.88 | 0.78 | 9.67 | 2.51 | 9.99 | 0.85 |
and SCA-H) in retrieving the \( \theta_{liq} \) using the ELBARA-III measurements for both warm and cold seasons during both descending and ascending overpasses as indicated by lower values of bias, RMSE and ubRMSE and higher R values. In comparison to the \( \theta_{liq} \) retrievals produced based on the SMAP measured \( T_w \), the retrievals produced using the ELBARA-III measurements show poorer performance during the transition seasons with soil thawing (e.g., March and April) and freezing (e.g., October and November). Particularly, the \( \theta_{liq} \) retrievals tend to largely overestimate the in situ \( \theta_{liq} \) representative of ELBARA-III footprint between March and April, which can be related to the thawing of the snowpack that would affect the ELBARA-III measurements.

**Figure 8.** Time series of average \( \theta_{liq} \) measurements of SMAP footprint and retrievals obtained by the SCA-V, SCA-H and DCA algorithms based on the SMAP measured \( T_w \) for the (a) descending and (b) ascending overpasses between August 2016 and July 2017. The \( \theta_{liq} \) retrieval derived from the SMAP SM product is also shown.

**Figure 9.** Time series of average \( \theta_{liq} \) measurements of ELBARA-III footprint and retrievals obtained by the SCA-V, SCA-H and DCA algorithms based on the ELBARA-III measured \( T_w \) measurements for the (a) descending and (b) ascending overpasses between August 2016 and July 2017.

**Table 3.** Statistical errors estimated between the in situ average \( \theta_{liq} \) and retrievals obtained by the SCA-V, SCA-H and DCA algorithms using either the ELBARA-III or SMAP measured \( T_w \) during the ascending and descending overpasses between August 2016 and July 2017.

| Retrievals | SMAP Footprint | ELBARA Footprint |
|------------|----------------|------------------|
|            | ubRMSE (m\(^3\) m\(^{-3}\)) | Bias (m\(^3\) m\(^{-3}\)) | RMSE (m\(^3\) m\(^{-3}\)) | R | ubRMSE (m\(^3\) m\(^{-3}\)) | Bias (m\(^3\) m\(^{-3}\)) | RMSE (m\(^3\) m\(^{-3}\)) | R |
| Descending |                  |                  |                  | |                  |                  |                  | |
| SCA-V      | 0.053           | -0.025           | 0.059           | 0.91     | 0.045           | -0.003           | 0.045           | 0.90 |
| SCA-H      | 0.055           | -0.032           | 0.064           | 0.90     | 0.070           | -0.011           | 0.070           | 0.76 |
| DCA        | 0.051           | -0.027           | 0.057           | 0.92     | 0.053           | -0.009           | 0.054           | 0.85 |
| Ascending  |                  |                  |                  | |                  |                  |                  | |
| SCA-V      | 0.035           | -0.005           | 0.035           | 0.95     | 0.063           | 0.021           | 0.067           | 0.84 |
5. Conclusions

This study investigates the performance of the two-stream microwave emission model in simulating L-band $T_\nu$ and retrieving $\theta_{liq}$ in combination with the four-phase dielectric model for both thawed and frozen soils on the Tibetan Plateau. Both single (SCA) and double (DCA) channel algorithms are adopted using both ground-based ELBARA-III and spaceborne SMAP measurements conducted in a Tibetan grassland site. Intercomparison between the time variations of ELBARA-III and SMAP $T_\nu$ measurements demonstrates that high correlations ($R \geq 0.87$) are found between both measurements, though the footprints are obviously distinct for the spaceborne SMAP and ground-based ELBARA-III measurements. The SMAP measured $T_\nu$ are generally lower than the ELBARA-III measurements between June and October, which are associated with the distinct variations of in situ average $\theta_{liq}$ found across the ELBARA-III and SMAP footprints. In addition, the analysis of relations between the $T_\nu$ measurements and in situ average $\theta_{liq}$ reveals that (i) SMAP $T_\nu$ measurements are better responding to the in situ $\theta_{liq}$ compared to the ELBARA-III measured $T_\nu$, and (ii) the in situ $\theta_{liq}$ explains better the $T_\nu$ measurements during the warm period from May to October, while $T_{liq}^H$ measurements are more consistently varying with the in situ $\theta_{liq}$ in the cold period between November and April.

It is found that the two-stream microwave emission model configured with the default vegetation and surface roughness parameterization of SMAP mission underestimates both ELBARA-III and SMAP measured $T_{liq}^H$ in the cold season and overestimates the $T_{liq}^V$ measurements in the warm season. The above deficiencies are largely reduced by adopting the new parameterization proposed by Zheng et al. [16], which employs higher values for the roughness parameters ($Q$ and $h$) and lower values for the vegetation parameter $\tau$. It can also be found that the SMAP measured $T_\nu$ are better reproduced with the new parameterization in comparison to the simulations performed for the ELBARA-III footprint, and the simulation of $T_{liq}^H$ outperforms that of $T_{liq}^H$.

In addition, it is found that all the $\theta_{liq}$ retrievals produced using the SMAP measured $T_\nu$ in this study capture well the in situ $\theta_{liq}$ representative of SMAP footprint and are consistently better than the SMAP product. The $\theta_{liq}$ retrievals produced using the ELBARA-III measurements show poorer performance in comparison to those generated based on the SMAP measurements. The SCA-V algorithm outperforms both DCA and SCA-H methods in retrieving the $\theta_{liq}$ which supports implementing the SCA-V method as the baseline soil moisture retrieval algorithm for the SMAP mission. Notably, the $\theta_{liq}$ retrievals using the SCA-V based on the SMAP $T_{liq}^V$ measured during the ascending overpass gives the best results (ubRMSE = 0.035 m$^3$ m$^{-3}$), which is also better than the specified goal of ubRMSE = 0.04 m$^3$ m$^{-3}$ for the SMAP mission.

This study shows the potential of using a two-stream model configured with the four-phase soil dielectric model for simulating L-band $T_\nu$ and retrieving $\theta_{liq}$ for both thawed and frozen soil conditions. It’s also noted that the SCA-V algorithm configured with the SMAP measured $T_{liq}^V$ during the ascending overpass is able to produce reliable $\theta_{liq}$ retrievals in a Tibetan meadow ecosystem. These findings are crucial for improving emission simulation and $\theta_{liq}$ retrievals at the L-band in cold regions such as the Tibetan Plateau. However, additional work is still needed to investigate and test the performance of the proposed method for its application in other areas. Recently, Li et al. [7] have implemented the two-stream model to simulate the $T_\nu$ and retrieve soil moisture using SMOS measurements at a global scale, which provides an excellent reference to extend the application of the method proposed in this study. For example, the soil dielectric model, and the adopted vegetation and surface roughness parameterization for grassland used by Li et al. [7] can be directly replaced by the four-phase soil dielectric model and new parameterization proposed in this study to improve its performance in a cold region.
such as the Tibetan Plateau. The needed SMST data can be taken from the reanalysis data such as the ECMWF model simulations carried out by Li et al. [7].

**Supplementary Materials:** The following are available online at www.mdpi.com/article/10.3390/rs14030494/s1, supplementary Table S1: Measurements of brightness temperature and liquid soil water content; supplementary Table S2: Sample computation for implementing the two-stream model with SMAP or Zheng’s parameterization.

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