Giant fine structure splitting of the bright exciton in a bulk MAPbBr$_3$ single crystal

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Exciton fine structure splitting in semiconductors reflects the underlying symmetry of the crystal and quantum confinement. Since the latter factor strongly enhances the exchange interaction, most work has focused on nanostructures. Here, we report on the first observation of the bright exciton fine structure splitting in a bulk semiconductor crystal, where the impact of quantum confinement can be specifically excluded, giving access to the intrinsic properties of the material. Detailed investigation of the exciton photoluminescence and reflection spectra of a bulk methylammonium lead tribromide single crystal reveals a zero magnetic field splitting as large as $\sim 200$µeV. This result provides an important starting point for the discussion of the origin of the large bright exciton fine structure observed in perovskite nanocrystals.

In an ideally pure semiconductor, the lowest energy electronic excitation is a bound electron-hole pair (exciton). The exchange interaction between electron and hole spins lifts the degeneracy between dark singlet and bright multiplet excitonic states producing a fine structure. The physics of the fine structure splitting (FSS) has been the subject of intense investigation$^{1-13}$, since it can be used for quantum logic$^{14}$, and wave function control$^{15}$. Moreover, the ability to control the FSS is essential to fabricate the efficient entangled photon sources$^{16-20}$ required for quantum teleportation$^{21}$, quantum communication$^{22}$, and quantum cryptography$^{23}$.

The pattern of excitonic states produced by the exchange interaction strongly depends on the symmetry of the system. In structures with sufficiently low symmetry, the degeneracy of the bright states should be completely lifted. However, in general, it is expected that the bright exciton FSS is much smaller than the bright–dark state splitting$^6$, which is typically a few tens of µeV in common inorganic semiconductors$^{24}$. Since the symmetry breaking is generally also small (or even absent), the bright exciton FSS has never been observed in any bulk semiconductor. In contrast, the bright exciton FSS is commonly observed in semiconductor nanostructures$^{1-8}$ where quantum confinement greatly enhances the exchange interaction and the symmetry is strongly broken by the anisotropic quantum confinement.

Recently, different theoretical models predict that the low symmetry of lead-halide perovskites in the orthorhombic phase should result in a significant bright exciton fine structure splitting. While there is no consensus about the origin of this phenomenon, which can result from the Rashba effect$^{25-27}$ or interplay of exchange interaction and crystal field$^{28-31}$, all of those predictions make lead halide perovskites a promising starting point to search for the elusive bright exciton FSS in bulk semiconductors.

Here, we report that indeed the bright exciton FSS can be observed in a high quality bulk MAPbBr$_3$ single crystal in which all the extrinsic sources of symmetry breaking and quantum confinement enhancement can be specifically excluded. Therefore our work constitutes an important base for further discussions of the intrinsic origin of exciton FSS in perovskite crystals. By means of detailed magneto-optical spectroscopy, we reveal the FSS of the exciton 1s transition with a splitting as large as $200$µeV. We show that the observed value can be reasonably explained by the recent model proposed in refs.$^{29,32}$ with parameters extracted from our experimental studies.

In lead-halide perovskites, the conduction and valence bands are built mainly from cationic Pb orbitals. Crucially, the valence band is built from s-like orbitals, while the conduction band is built from p-like orbitals$^{33-36}$. Strong spin-orbit coupling in the conduction band$^{33}$ splits the electron states with total angular momentum $J = 3/2$ (upper band) and $J = 1/2$ (lower band). Therefore, the band-edge exciton can be in one of four degenerate states: $|0_D⟩$ with zero total angular momentum, $J^{\text{exc}} = 0$, and three states $|Z⟩$ , $|\pm 1⟩$ with $J^{\text{exc}} = 1$ and $z$ components of angular momentum $J^{\text{exc}}_z = 0$ or $J^{\text{exc}}_z = \pm 1$ respectively.

In a cubic crystal, the exchange interaction splits the dark, $J^{\text{exc}} = 0$, exciton state from the triply degenerate bright, $J^{\text{exc}} = 1$, states. Depending on temperature, the
lead-halide perovskite crystal can be in a cubic, or tetragonal or orthorhombic phase. In the latter two phases, crystal field together with exchange interaction lifts the degeneracy of bright states. In the tetragonal phase, the bright exciton levels split into two degenerate $|\pm 1\rangle$ states, which couple to linearly (electric vector along $z$ direction) polarized light. The further symmetry reduction in the orthorhombic (low temperature) phase lifts the degeneracy of the $|\pm 1\rangle$ states resulting in symmetric andantisymmetric states $|X\rangle = (|1^+\rangle + |1^-\rangle)/\sqrt{2}$, $|Y\rangle = (|1^+\rangle - |1^-\rangle)/\sqrt{2}$, which couple to the two other linearly orthogonal polarizations of light, respectively. The expected fine structures of excitons in different crystallographic phases are summarized in figure 1.

Very recently, bright exciton FSS (in the range of few hundred $\mu$eV up to 1-2 meV) has been reported for lead halide perovskite nanocrystals. However it is not clear if the observed splitting is related only to the crystal field and exchange interaction or if it is enhanced or driven by the Rashba effect. Moreover, in nanocrystals one has to worry about possible contributions of anisotropic quantum confinement to the FSS or a surface enhancement of the Rashba effect. The significant variation in the size of bright exciton FSS observed in the nanocrystals indicates that the fine structure splittings in perovskites can be strongly affected by extrinsic contributions. This hinders the determination of the intrinsic properties of perovskite crystals, which are required to provide a starting point for the discussion of the origin of the large bright exciton fine structure splitting. Moreover, the random orientation of the nanocrystals, together with the presence of high temperature phases even at cryogenic temperatures, further complicates the interpretation of the exciton FSS.

The few mm by few mm single MAPbBr$_3$ crystal were prepared as reported for MAPbBr$_3$ in ref. Briefly, MABr (from Dyesol) and PbBr$_2$ (Sigma-Aldrich) salts were added to dimethyl formamide (DMF) to prepare a 1M solution. Formic acid (~40 $\mu$l/ml) was added to the above solution followed by a filtration with a 0.45 micron filter. The solution incubated at 55°C produced multiple seed crystals (~500$\mu$m). The seed crystals (which are single crystalline as we have used them for XRD characterisation) were collected and used as seed for the growth of mm size crystals where DMF solution has less amount of formic acid. Each seed produced only one large crystal and the number of large crystals were controlled by the number of seeds added. Namely the filtered solution was poured into a glass vial and a cleaned glass slide was placed at the bottom of the vial. A small seed (~500 $\mu$m) of MAPbBr$_3$ crystal was carefully placed on the glass slide. The glass vial was then incubated at ~55°C to produce the large MAPbBr$_3$ crystals of size 2 x 2 x 1 mm$^3$. The crystal was collected when the solution is still hot (~55°C) and preserved in chlorobenzene.

Before the measurements, the crystal were blow dried with a N$_2$ gun. The measurements were performed on the largest facet of the crystal.

The magnetic field measurements were performed in a cryofree split coil (up to 7 T) equipped with a variable temperature insert ($1.5 \sim 300$ K). The optical access to the sample was through quartz B optical windows. The white light used for the reflection studies was provided by a tungsten lamp. For the PL measurements the sample was excited using a 405 nm continuous wave (CW) laser with a power of 100$\mu$W. The PL and reflection measurement were performed in the Faraday geometry where the excitation beam or white light was directed onto the sample through a non-polarizing beam splitter and focused on the sample by a 20 cm focal length lens. The signal was collected by the same lens and dispersed by a 0.5 m long spectrometer with a 1800 groove/mm grating. The dispersed light was detected using a nitrogen cooled CCD camera. The polarization of the signal was analyzed using a broad band half wave or quarter wave plate and linear polarizer.

All our measurements have been performed in the low temperature orthorhombic phase (which was confirmed by temperature dependence of PL presented in SI). The macroPL and reflectance spectrum of the MAPbBr$_3$ crystal taken at $T = 1.5$ K are presented in figure 2(a). The PL spectrum (red curve) is dominated by a sharp feature at 2.245 eV with a 1.5 meV full width at half maximum (FWHM). In reflectance, in addition to the strong dispersive resonance observed for the 1s free exciton transition, a much weaker feature corresponding to the 2s free exciton state is observed on the high energy side (see expanded 20 curve). For the dispersive reflectance line shape the resonance position, indicated by the vertical black dash/dotted lines, corresponds to the maximum
slope.

The 1s and 2s states are separated by $\approx 11$ meV, consistent with an exciton binding energy $R_e^\pi \approx 14.5$ meV (assuming a hydrogenic model). This value of exciton binding energy is in good agreement with those reported previously. The dominant PL peak is red-shifted by $\approx 9$ meV with respect to the resonance observed in the reflectance spectrum. Furthermore, on the high energy side of the PL spectrum there is a relatively weak peak (see expanded x200 curve) at the same energy as the 1s excitonic transition observed in reflectance. Therefore, we attribute the strong PL emission to bound states (see also extended dissuasion in SI), and the small PL feature on the high energy side to the 1s free exciton emission.

Moreover two weak low energy peaks separated by about 5 meV and 9 meV from strongest PL peak can be observed. Such peaks have been already observed in CsPbBr$_3$ perovskite nanocrystals and attributed TO phonon replica. Interestingly the separation between first phonon replica from 1s excitonic peak is 14 meV which is also very close to effective energy of LO phonon reported for MAPbBr$_3$ crystals. The lowest energy bands can be attributed to phonon replicas of the bound and free exciton transitions.

Reflectance and PL spectra measured in a linear polarization basis are shown in figure 2(b,c). The energy shift of the energy bands can be attributed to phonon replicas of the lowest energy features in PL and reflectance. The strong PL emission 9 meV below the 1s transition (with no corresponding feature in reflectance) is assigned to bound exciton emission. (b) Reflectance spectrum measured in a linear polarization basis for two orthogonal polarizations. (c) Two linear orthogonally polarized components of PL spectra (dashed lines) together with PL spectra measured in linear polarization basis. For clarity the PL background has been subtracted.

Reflectance and PL spectra measured at $T = 1.5$ K. The 1s excitonic transition is observed in PL and both the 1s and 2s states can be identified in reflectance. The strong PL emission 9 meV below the 1s transition (with no corresponding feature in reflectance) is assigned to bound exciton emission. (b) Reflectance spectrum measured in a linear polarization basis for two orthogonal polarizations. (c) Two linear orthogonally polarized components of PL spectra (dashed lines) together with PL spectra measured in circular polarization basis. For clarity the PL background has been subtracted.

FIG. 2. PL (red line) and reflectance (blue line) spectra measured at $T = 1.5$ K. The 1s excitonic transition is observed in PL and both the 1s and 2s states can be identified in reflectance. The strong PL emission 9 meV below the 1s transition (with no corresponding feature in reflectance) is assigned to bound exciton emission. (b) Reflectance spectrum measured in a linear polarization basis for two orthogonal polarizations. (c) Two linear orthogonally polarized components of PL spectra (dashed lines) together with PL spectra measured in circular polarization basis. For clarity the PL background has been subtracted.

Slopes in the 1s and 2s states are separated by $\sim 11$ meV, consistent with an exciton binding energy $R_e^\pi \approx 14.5$ meV (assuming a hydrogenic model). This value of exciton binding energy is in good agreement with those reported previously. The dominant PL peak is red-shifted by $\sim 9$ meV with respect to the resonance observed in the reflectance spectrum. Furthermore, on the high energy side of the PL spectrum there is a relatively weak peak (see expanded x200 curve) at the same energy as the 1s excitonic transition observed in reflectance. Therefore, we attribute the strong PL emission to bound states (see also extended dissuasion in SI), and the small PL feature on the high energy side to the 1s free exciton emission.

Moreover, two weak low energy peaks separated by about 5 meV and 9 meV from strongest PL peak can be observed. Such peaks have been already observed in CsPbBr$_3$ perovskite nanocrystals and attributed TO phonon replica. Interestingly the separation between first phonon replica from 1s excitonic peak is 14 meV which is also very close to effective energy of LO phonon reported for MAPbBr$_3$ crystals. Therefore, the lowest energy bands can be attributed to phonon replicas of the bound and free exciton transitions.

Reflectance and PL spectra measured in a linear polarization basis are shown in figure 2(b,c). The energy shift between the orthogonal linear polarizations $\pi$ and $\sigma$, clearly visible in both PL and reflectance, is the smoking gun signature of the bright exciton FSS in a bulk crystal.

Before discussing in detail the zero magnetic field FSS, we present magneto-optical data taken in the Faraday configuration, which unambiguously demonstrates the free excitonic nature of the high energy PL feature. Figure 3(a) shows reflectance spectra measured for the two opposite circular polarizations $\sigma^1$ and $\sigma^2$ at 0 and 7 T magnetic field. The expected shift of the $\sigma^1$ and $\sigma^2$ components in magnetic field is clearly seen. To determine precisely the splitting of the $\sigma^1$ and $\sigma^2$ transition as a function of magnetic field we divide them by the zero field spectrum (see figure 3(b)). The ratioed spectra have a characteristic sharp feature with an amplitude and width which increase with the size of the energy shift. As the shape of the reflectance spectra are almost unchanged in magnetic field, the shift can be measured by fitting to the ratioed spectra by varying the shift between the spectra in

$$\frac{R_B(E)}{R_0(E)} \propto \frac{R_0(E + \Delta E)}{R_0(E)} ,$$

where $R_B(E)$ and $R_0(E)$ are reflectance spectra in magnetic field and at zero field and $\Delta E$ is the shift of the reflectance resonance in magnetic field. More details about fitting procedure can be found in the supplementary information. The fits, shown as solid lines figure 3(b), are in excellent agreement with the experimental data. This method allows us to precisely determine the shift of the exciton transition even at very low magnetic field and avoids having to model the reflection line shape.

The energy shift of the $\sigma^1$ and $\sigma^2$ transitions and the resulting Zeeman splitting and diamagnetic shift are summarized in figure 3(c,d). Fitting the splitting of the $\sigma^1$ and $\sigma^2$ features with $E_2 - E_1 = g\mu_B B$ (see figure 3(d)) gives $g = 2.6 \pm 0.1$, in agreement with the previously reported value. The diamagnetic shift is extracted by fitting the average behavior in field $(\sigma B^2 = (E_2 + E_1)/2)$, giving $\sigma = (3.4 \pm 0.1) \mu eVT^{-2}$ with a resulting exciton Bohr radius of $\approx 3.8$ nm and effective mass of $\mu = 0.185 m_0$. Finally, we compare the behavior of the exciton transitions in magneto-reflectance with the behavior of the corresponding 1s features in PL (broken lines figure 3(e))). The 1s PL feature shifts in exactly
FIG. 3. (a) $\sigma^1$ and $\sigma^2$ components of the reflectance spectrum measured at zero (black and gray curve) and 7 T (red and blue). (b) Reflectance spectrum at 1 T divided by the zero field spectra (open points) together with a fit using equation (1). (c) Shift of the $\sigma^1$ and $\sigma^2$ components as a function of magnetic field. (d) Determined Zeeman splitting (blue squares) and diamagnetic shift (red triangles) together with linear and quadratic fit, respectively. (e) Comparison of the reflectance shift with the PL spectra feature assigned to free exciton emission.

FIG. 4. (a) Shift of the reflectance resonance (open squares) and PL peak (open triangles) as a function of detection angle of linear polarization. For clarity, the PL data is shifted vertically by 100 $\mu$eV. The red lines are fits using a $\sin^2 \theta$ function. The same way as in the reflectance data, plotted in solid lines.

Two in-plane bright excitons should be linearly polarized and energetically separated (see also discussion in supplementary information). To confirm that the zero magnetic field spectrum is composed of two linearly polarized components and to precisely determine the splitting energy we have measured the energy shift versus the angle of the linear polarization in detection. The energy shift in reflectance (open squares) and PL (open triangles) shows the expected oscillatory behavior with the angle of the polarization analyser (see figure 4(a), where the PL data has been shifted vertically by 100$\mu$eV for clarity). The data is well described using $\delta \sin^2 (\phi + \phi_0)$ (red lines in figure 4(a)), where $\delta$ is the bright exciton FSS, $\phi$ is the angle of linear polarization detection and $\phi_0$ is a phase factor. Similar values of the zero field splitting are extracted from fitting the reflectance ($\delta \approx 197 \pm 7 \mu$eV) and PL ($\delta \approx 220 \pm 40 \mu$eV). A detailed discussion of uncertainty estimation can be found in the supplementary information.

Theoretically the quantitative evolution of exciton fine structure exchange splitting in different perovskite phases can be derived from symmetry considerations applied to the exciton picture. Recently this approach has been used to provide a relation between the band structure parameters and the bright exciton fine structure splitting. The observed splittings between exciton states with dipole moment along X, Y and Z can be ex-
pressed as

\[ \Delta_{XY} = 2J_b|\alpha^2 - \beta^2| \]

\[ \Delta_{XZ} = 2J_b|\beta^2 - \gamma^2| \]

\[ \Delta_{YZ} = 2J_b|\alpha^2 - \gamma^2| \]

where the \( J_b \) is an exchange integral and \( \alpha, \beta \) and \( \gamma \) are the weights of the Bloch wave functions of electrons in the orthorhombic crystal structure. The exchange integral \( J_b \) depends on the exciton Bohr radius and Kane energy \( E_{P_S} \), while \( \alpha, \beta \) and \( \gamma \) depend on the strength of the spin-orbit coupling and the crystal field (see detailed discussion in supplementary information).

From our magneto-optical measurements, we can extract the exciton Bohr radius (3.8 nm), the effective mass \( (\mu = 0.185) \) and the dielectric constant \( (\epsilon_r = 13.1) \) which lies between the accepted high (5.6-6.7) \cite{56-58} and low frequency (25-38) \cite{58,59} values. Such a discrepancy is typical for materials with smaller exciton radii \cite{60}. Unfortunately, the Kane energy \( E_{P_S} \) and \( \alpha \) and \( \beta \) parameters for MAPbBr\(_3\) are not well established. Taking into account that the spin orbit-coupling and crystal field are expected to be similar for fully inorganic and hybrid perovskites\cite{29,40} and that MAPbBr\(_3\) and CsPbBr\(_3\) have comparable band parameters\cite{61,62} we assume \( \alpha = 0.67 \) and \( \beta = 0.57 \) as in CsPbBr\(_3\)\cite{29}. The estimation of the Kane energy based on 4 and 40 band \( k \cdot p \) model gives \( E_{P_S} = 18.4 \) eV and 28.4 eV (see supplementary information for details and ref.\cite{30}). In the literature, one can also find values for the Kane energy in the range of 37.1 – 39.9 eV in the inorganic compounds CsPbX\(_3\) (X = I, Br, Cl)\cite{25,41}, although these would correspond to substantially lower effective mass values. The calculated value of the splitting between different excitonic states as a function of the Kane energy are presented in figure 5 for values of the dielectric constant in the range \( \epsilon_r = 5.6 - 13.1 \). The predicted splitting of the bright excitonic states is in the range of a few hundreds of \( \mu eV \) in agreement with the experimental observation. Since all axes are equivalent in the room temperature cubic phase the orientation of the crystal axis cannot be determined after the transition to the low temperature orthorhombic phase. The accepted range of Kane energies \( (\simeq 15-40 eV) \) is however sufficient to correspond well with the calculated splitting for any of the three possible alignments.

![FIG. 5. Calculated bright exciton fine structure splittings as a function of the Kane energy \( E_{P_S} \) for values of the dielectric constant \( \epsilon_r \) from 5.6 to 13.1 (see text for details). The red, blue and green colors corresponds to \( \Delta_{XY} \), \( \Delta_{XZ} \) and \( \Delta_{YZ} \) respectively. The experimentally observed splitting is indicated by the horizontal black line. The dashed lines indicate the estimated error for the reflectance measurements. Details of the calculations and numeric values of all used parameters can be found in supplementary information.](image)

![FIG. 6. (a) PL spectra measured at 7T in circular polarization basis (red and blue curves) and linear basis (dashed black curve). (b) Dependence of PL peak position as a function of magnetic field measured in linear (open squares) and circular (full squares) polarization basis. The black lines are calculated using the exchange Hamiltonian with parameters extracted from the reflectance measurements \( \delta = 197 \mu eV, g = 2.6 \) and \( \sigma = 3.4 \mu eV T^{-1} \). The grey curve corresponding to the linear basis is calculated with \( \delta = 0 \), i.e., neglecting the zero field splitting.](image)

We have also investigated the behaviour of the FSS in magnetic field. Figure 6(a) shows PL spectra measured at \( B = 7 T \) in circular and linear polarization basis. In the circular basis splitting between states corresponding to \( \sigma^1 \) and \( \sigma^2 \) components of the emission is clearly visible, while both components are observed simultaneously in the linear basis. The detailed evolution of the PL peaks in the circular and linear polarization basis is shown in Figure 6(b). The fine structure splitting of the 1s bright exciton in the orthorhombic phase, in the presence of magnetic field along the direction perpendicular
to the dipole moment orientation, can be described in the $|1^+\rangle, |1^-\rangle$ basis by the following Hamiltonian (see supplementary information and references$^{28,40}$):

$$H = \frac{1}{2} \left( \frac{g\mu_B B + 2\sigma B^2}{\delta} \delta - g\mu_B B + 2\sigma B^2 \right)$$

The corresponding eigenvalues and eigenstates are:

$$E_{Y/X} = \pm \frac{1}{2} \sqrt{(g\mu_B B)^2 + \sigma^2 + \sigma B^2}$$

$$|X/Y\rangle = A |+1\rangle + \left( -\frac{g\mu_B B}{\delta} \mp \sqrt{\frac{(g\mu_B B)^2}{\delta^2} + 1} \right) |-1\rangle$$

where $A$ is a field dependent normalizing constant. At zero magnetic field the energy difference between the states is equal to $\delta$ and the states couple to linearly polarized light (superposition of states $|\pm 1\rangle$). Increasing magnetic field induces a continuous change from linear polarization to circular polarization of the excitonic transitions in agreement with experiment (see figure 2(c)) and figure 6(a)). Finally, we compare the dependence of the PL peak position as a function of the magnetic field (see Fig. 6(b)) with the predictions of the exchange Hamiltonian (black lines) using the parameters extracted from reflectance studies, i.e., $\delta = 200\mu eV$, $g = 2.6$ and $\sigma = 3.4 eV T^{-1}$. The exchange Hamiltonian provides a full quantitative description of the data. At low magnetic field, the bright FSS is determined by the zero field splitting $\delta$, and with increasing magnetic field the transition energy is increasingly dominated by the Zeeman splitting.

It is worth to note that now one can find two interpretations of exciton states splitting in perovskite nanocrystals. One is solely based on crystal symmetry, exchange interaction and crystal field$^{28-31}$ while the other one recall also to Rashba effect to explain FSS in fully inorganic perovskite nanocrystals$^{25-27}$. The Rashba effect$^{25}$ is often invoked to explain several of the unique properties of the lead halide perovskites$^{49,63-66}$. Despite the obvious beauty of this idea, it nevertheless remains highly controversial. For instance, the Rashba effect requires a lack of inversion symmetry or a breaking of bulk inversion symmetry, not present in centrosymmetric perovskite crystals. It was proposed that the temporal symmetry breaking is provided by the cation motion, which leads to local polar fluctuation in mixed and fully inorganic perovskites$^{49,65,67}$. However, such vibrations of the cations should be absent at very low temperatures$^{67,68}$, used for all exciton fine structure studies to date. The absence of the Rashba effect in the orthorhombic phase is also consistent with circular photogalvanic measurements performed on the analogue MAPbI$_3$ compound$^{69}$.

Another source of symmetry breaking might be attributed to surface effects$^{48}$, which can be especially important for nanocrystals providing a possible explanation for the widely varying (200-1000$\mu eV$) bright exciton FSS observed in the CsPbBr$_3$ nanocrystals. However, in our case, both the optical methods used here, namely reflectivity and PL, probe the bulk properties of the crystal. The absorption coefficient in MAPbBr$_3$ is of the order of $\alpha = 10^5 cm^{-1}$ at a PL excitation wavelength of 405 nm which corresponds to an optical absorption depth of order of 100 nm. The exciton diffusion will further increase the volume sampled by the PL. At the energy of the excitonic reflectivity feature, the absorption depth has increased to approximately 300 nm. In the presence of a surface electric field, which could lead to some inhomogeneity, the sampling depth can fall to distances of order $\lambda/(4\pi n)$, where $n$ is the real part of the refractive index, giving an effective probing depth of a few tens of nm$^{70,71}$, which is, however, still large on the scale of the lattice and the exciton wavefunction ($\sim 4$ nm) or surface roughness ($\sim 10$ nm see SI for details). Nevertheless, PL and reflectivity give identical results (within experimental error) in sign and magnitude when sampling different regions of the crystal. Therefore, both techniques measure the same property, namely the fine structure splitting of the bulk free exciton, so the surface impact can be excluded.

Finally, according to models for the Rashba effect, the order of the bright and dark states should be reversed in fully inorganic perovskite nanocrystals$^{25,27}$ which seems to be in contrast to some of the experimental reports on the PL dynamics in inorganic perovskite nanocrystals$^{29,38,72,73}$ and recent direct observation of dark ground states in FAPbBr$_3$ nanocrystals$^{31}$. Given all above arguments and good quantitative agreement of theoretical prediction based only on crystal symmetry consideration suggest that the Rashba effect plays little role in MAPbBr$_3$ (and FAPbBr$_3$) crystal, at least at lowest temperature phases.

It should be noted however that the excitonic band parameters, in particular the reduced effective mass, $\mu$, are significantly different from those deduced at higher energy from the magnetic field dependence of the nearly free electron Landau levels for thin films$^{61}$. This discrepancy may be a hallmark of polronic effects in perovskites crystals$^{74-77}$. The effective mass extracted here comes from low field limit while previous report concentrate on free electron Landau levels observed in high field limit where the motion of carriers is decoupled from lattice vibration$^{60}$. Therefore previously extracted effective mass is lower than at low field limits. However, this aspect is beyond the scope of this work and will be the subject of further studies.

In summary, we have observed a significant bright exciton fine structure splitting $\delta = 197 \mu eV$ in bulk MAPbBr$_3$. This represents an important step in the understanding of the fine structure splitting in lead-halide perovskites and perovskite based nanostructures. Using a large single crystal, we are able to exclude the influence of surface, size and anisotropic confinement on the observed bright exciton FSS giving direct access to the intrinsic properties of the bulk MAPbBr$_3$. The observed split-
ting can be understood in the exciton picture combined with symmetry considerations. We show that, within this model, the observed splitting can be reasonably estimated based on band structure parameters derived from magneto-optical studies. Our work constitutes a firm base for further exciton fine structure studies in lead-halide perovskites. The presented results should provide valuable insight for future investigations of the different mechanisms that contribute to the exciton fine structure, such as confinement anisotropy or Rashba effect, in perovskite based nanostructures.

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