Abstract—Distributed software-defined networks (SDN), consisting of multiple inter-connected network domains, each managed by one SDN controller, is an emerging networking architecture that offers balanced centralized control and distributed operations. Under such networking paradigm, most existing works focus on designing sophisticated controller-synchronization strategies to improve joint controller-decision-making for inter-domain routing. However, there is still a lack of fundamental understanding of how the performance of distributed SDN is related to network attributes, thus impossible to justify the necessity of complicated strategies. In this regard, we analyze and quantify the performance enhancement of distributed SDN architectures, influenced by intra-/inter-domain synchronization levels and network structural properties. Based on a generic weighted network model, we establish analytical methods for performance estimation under four synchronization scenarios with increasing synchronization cost. Moreover, two of these synchronization scenarios correspond to extreme cases, i.e., minimum/maximum synchronization, which are, therefore, capable of bounding the performance of distributed SDN with any given synchronization levels. Our theoretical results reveal how network performance is related to synchronization levels and inter-domain connections, the accuracy of which are confirmed by simulations based on both real and synthetic networks. To the best of our knowledge, this is the first work quantifying the performance of distributed SDN analytically, which provides fundamental guidance for future SDN protocol designs and performance estimation.

I. INTRODUCTION

Software-Defined Networking (SDN) [1] [2] [3] [4], an emerging networking architecture, significantly improves the network performance due to its programmable network management, easy reconfiguration, and on-demand resource allocation, which has therefore attracted considerable research interests. One key attribute that differentiates SDN from classical networks is the separation of the SDN’s data and control plane. Specifically, in SDN, all control functionalities are implemented and abstracted on the control plane for operational decision making, e.g., flow construction and resource allocation, while the data plane only passively executes the instructions received from the control plane. For a typical SDN architecture, all network decisions are made in the control plane by a control entity, called SDN controller, in a centralized manner. Since the centralized SDN controller has the full knowledge of network status, it is able to make the global optimal decision. Yet, such centralized control suffers from major scalability issues. In particular, as a network grows, the number of flow requests and operational constraints are likely to increase exponentially. Such high computation and communication requirements may impose substantial burden on the SDN controller, potentially resulting in significant performance degradation (e.g., delays) or even network failures.

In this regard, distributed SDN is proposed [5] [6] [7] [8] [9] [10] to balance the centralized and distributed control. Specifically, a distributed SDN network is composed of a set of subnetworks, referred to as domains, each managed by an independent SDN controller. Moreover, each domain contains several gateways connecting to some other domains; such inter-connected domains then form the distributed SDN architecture. In the distributed SDN, if the controllers do not communicate with each other regarding the network status of their own domains, then the distributed SDN is reduced to the classical multi-AS (Autonomous Systems) network, where the network flows are managed by IGP and BGP protocols. Nevertheless, in the distributed SDN architecture, controllers are expected to exchange information via proactively probing or passive listening. Such additional status information at each controller, called the synchronized information, can assist in enhancing decision making for inter-domain tasks. As a special case, when each controller knows the network status in all other domains, i.e., complete synchronization, then all controllers can jointly act as a logically centralized controller, which effectively is the same as the centralized SDN structure as all network decisions are globally optimal. These observations imply that the network performance, e.g., the constructed inter-domain path length, relies heavily on the inter-controller synchronization level. Since complete synchronization among controllers will incur high synchronization costs especially in large networks, practical distributed SDN networks are likely to be able to afford only partial inter-domain synchronization.

Under partial synchronization, most existing works focus on promoting the inter-domain synchronization so that the final decision making approaches optimality. For instance,
information sharing algorithms are proposed in [7], [8] for negotiating common traffic policies among various domains. Similarly, efficient frameworks are designed in [9], [10], aiming to facilitate inter-domain routing selection via fine-grained network status exchanges. However, one fundamental question regarding the distributed SDN architecture has generally been ignored: How does the network performance in distributed SDN relate to network synchronization levels and structural properties? It is possible that under certain network conditions, e.g., the number of gateways and their connections to external domains, the benefit of increasing the synchronization level is only marginal. Without such fundamental understanding, it is impossible to justify why a complicated mechanism for information sharing or flow construction is necessary in distributed SDN. We, therefore, investigate this unsolved yet critical problem in the distributed SDN paradigm, with the goal to quantify its performance under any given network conditions.

In this paper, we propose a network model to capture intra- and inter-domain connections and non-uniform edge weights in distributed SDN. Such network model is generic in that it only requires degree/weight distribution and the number of gateways in each domain as the input parameters, i.e., it is independent of any specific graph models. Based on this network model, we then derive analytical expressions of the network performance, focusing on characterizing the average length (see further discussion in section II-E) of the constructed paths with respect to (w.r.t.) random flow requests. Such performance metric is investigated under four canonical synchronization levels, ranging from the minimum to the complete (maximum) synchronization that experience increasing synchronization costs. If a given synchronization scenario cannot be described by any of these four cases, then its performance can always be bounded by our analytical results corresponding to the two extreme cases (i.e., maximum/minimum synchronization). Analytical results reveal that the performance metric is a logarithmic function of the network structural parameters even under the minimum synchronization level. Moreover, the performance gain declines with the increasing synchronization level and the number of gateways. To validate the accuracy of the derived analytical expressions, they are compared against evaluation results using both real and synthetic networks.

A. Related Work

The flexibility and scalability of the distributed SDN architecture have stimulated many research efforts in this area. In particular, the feasibility of deploying SDN-based mechanisms incrementally to current BGP-glued Internet is considered in [6], where routing control planes of multiple domains are outsourced to form centralized control planes for optimizing routing decisions. Similarly, [11] explores the problem of SDN upgrade in ISP (Internet Service Provider) networks under the constraint of migration costs. In addition, protocols and systems, such as HyperFlow [12] and ONOS [13] are proposed to realize logically centralized but physically distributed SDN architecture. Devflow [14] and Kandoo [15] are designed to reduce the overheads introduced by the interaction between control and data planes. Moreover, DIFANE [16] and Fibbing [17] are conceived for limiting the level of centralization and addressing robustness issues, respectively. From industry research community, Google’s B4 [18] and Espresso [19], and Facebook’s Edge Fabric [19] are developed to address routing-related challenges in the Internet using SDN-based techniques. However, most of these works are experiment-based without providing any rigorous mathematical analysis or theoretical guarantees, which therefore motivate us to investigate distributed SDN from the fundamental analytical perspective.

Since all theoretical results in this paper are obtained based on a weighted graph model, our work is also related to the area of graphical analysis of complex networks. However, most works in these areas are performed on certain graph models and constrained to specific graph properties, e.g., clustering [20], small-world effect [21], community structure [22], network motif [23], scale-free [24], etc. In contrast, our network model is substantially generalized with the most relaxed input parameters, i.e., degree and edge distributions. On the other hand, models in [21], [25]–[27] are purely randomized, which cannot differentiate intra- and inter-domain links in the context of distributed SDN. Finally, our work is most related to [28] and [29] as they also consider a layered-network model. However, the objectives in these papers are the analysis of transport networks and navigation strategies, which are substantially different from our problem. In this paper, we overcome these drawbacks to establish analytical results upon a generic network model that captures all key parameters and synchronization levels in distributed SDN.

B. Summary of Contributions

Our main contributions are five-fold.

1) We propose a generic two-layer network model capturing intra- and inter-domain connections, and edge weights;

2) On top of the network model in 1), we study the average length of constructed paths (APL) as the performance metric, and develop the analytical expression (a logarithmic function) of the APL under the minimum synchronization level. This result serves as an upper bound of the performance metric;

3) We derive a mathematical expression of the APL when the synchronization level is between the minimum and maximal synchronizations. These expressions give fine-grained quantification on how the performance metric relates to the incremental synchronization changes;

4) We establish an analytical expression of the APL for the maximum synchronization scenario, where all domains are synchronized with each other, i.e., complete synchronization. The theoretical result under such synchronization level provides a lower bound of the performance metric;

5) All of above theoretical results are evaluated using real and synthetic networks, both of which confirm their high accuracy as well as their capability in providing new insights into performance changes over various network conditions.

In this paper, we do not intend to design improved inter-domain routing mechanisms, and thus only basic and typical routing strategies are employed for theoretical analysis under
each of the synchronization scenarios. To the best of our knowledge, this is the first work that studies distributed SDN from the analytical perspective. The significance of these results is that they lay a strong theoretical foundation for the research community in distributed SDN.

The rest of the paper is organized as follows. Section II formulates the problem. Sections III–VI present analytical results for four different synchronization scenarios, respectively. Evaluations of the derived analytical expressions are conducted in Section VII. Finally, Section VIII concludes the paper.

II. PROBLEM FORMULATION

A. Network Model

We formulate the distributed SDN network as an undirected graph according to a two-layer network model (Fig. 1), where the top-layer abstracts the inter-domain connections, and under such constraints, the bottom-layer characterizes physical connections among all network elements. Specifically, the top-layer is a graph consisting of $m$ vertices, where each vertex represents a domain in the distributed SDN. These $m$ vertices are connected via undirected links according to a given inter-domain degree distribution, which refers to the distribution of the number of neighboring domains of an arbitrary domain. The top-layer graph, denoted by $G_d = (V_d, E_d)$ ($V_d/E_d$: set of vertices/edges in $G_d$, $|V_d| = m$), is called domain-wise topology in the sequel. The existence of an edge in $E_d$ connecting two vertices $v_1, v_2 \in V_d$ in the domain-wise topology implies that the two network domains corresponding to $v_1$ and $v_2$ are connected. Based on this domain-wise topology, we next construct the physical network in the bottom-layer. In particular, each of the $m$ domains in $G_d$ corresponds to an undirected graph with $n$ nodes in the bottom-layer; these $n$ nodes are connected following a given intra-domain degree distribution, which is the distribution of the number of neighboring nodes of an arbitrary node within the same domain $\beta$. We also assume that such intra-domain degrees across all domains are independently and identically distributed (i.i.d.). The graph of each domain is referred to as intra-domain topology. Then for each $e \in E_d$ with end-points corresponding to domains $A_i$ and $A_j$, we (i) randomly select two nodes $w_1$ from $A_i$ and $w_2$ from $A_j$ and connect these two nodes if link $w_1w_2$ does not exist, and (ii) repeat such link construction process between $A_i$ and $A_j$ $\beta$ times. By this link construction process, the bottom-layer network topology $G = (V, E)$ is therefore formed (i.e., set of nodes/links in $G$, $|V| = mn$); see Fig. 1 for illustrations. In each domain, nodes having connections to other domains are called gateways. Note that the above process indicates that the $i$-th selected link may overlap with existing links (i.e., the same end-points); therefore, parameter $\beta$ represents the maximum number of links between any two domains. Hence, if two domains, each with $n$ nodes, are connected in the domain-wise topology, then the expected number of links connecting these two domains is $n^2 \left(1 - \left(1 - \frac{1}{m}\right)^\beta\right)$. Without loss of generality, we assume that all inter/intra-domain topologies are connected graphs.

In addition, we also associate weights to links to capture the corresponding cost, e.g., computation, storage and/or communication cost, used for flow constructions. Specifically, we assume intra-domain link weights across all domains are non-negative and i.i.d.. In real distributed SDN environment, unlike the potential wireless links within a domain, inter-domain gateway-to-gateway links are likely to be wired with high bandwidth, thus more stable. In this regard, we characterize all inter-domain link weights by a non-negative constant $C$. Furthermore, without loss of generality, we assume $C = 1$; all theoretical results in this paper can be trivially extended to other values of $C$.

Discussions: Our two-layer network model is generic in that the inputs can be any degree and edge distributions; such distributions can be empirical or extracted from real networks of interest. Moreover, we do not require inter-domain degree and intra-domain degree to follow the same distribution.

B. SDN Data and Control Plane

Thus far, we have only discussed the graphical properties of the distributed SDN networks. One critical aspect of SDN that differentiates it from other networks is the separation of the data and control planes, which are formulated as follows.

1) Data Plane: We exploit graph $G$ generated by the two-layer network model in Section II-A to represent the data plane of the distributed SDN. Specifically, a node/link exists in $G$ if and only if it can be used for data transmission in the network.

2) Control Plane: We assume that in this two-layer network model, each domain contains one SDN controller that carries out control operations and facilitates information sharing. Each SDN controller can be one or a collection of intra-domain nodes that are equipped with the controlling functionality (i.e., in-band control) or external controlling entities operating on top of a network domain (i.e., out-of-band control). SDN controllers together with all inter/intra-domain controlling channels form a control plane.

In such network structure, to construct a path between a pair of source and destination nodes (only unicast is considered in this paper), the corresponding routing path is determined by the controllers in the source, destination, and all intermediate domains collectively. However, the performance of the
constructed paths may vary, depending on the network status information at each involved controller.

Remark: We do not specify the locations of SDN controllers, as they do not affect our theoretical analysis. For the same reason, we do not explicitly visualize the control plane in Fig. 1 or the rest of this paper.

C. Synchronization Among SDN Controllers

As discussed, synchronization levels among SDN controllers directly affects the quality of the constructed paths. We now formally define synchronization among SDN controllers.

Definition 1. Domain $A_i$ is synchronized with domain $A_j$ if and only if the SDN controller in $A_i$ knows the shortest distance (measured by the accumulated weight of shortest path) between any two gateways in $A_j$.

By Definition 1 it is clear there exist exponentially many synchronization levels, i.e., which domains are synchronized with which other domains. However, in real networks, it is usually the case that synchronization difficulty is high when two SDN controllers are far apart. In this paper, we study the following synchronization scenarios, sorted by their corresponding synchronization costs. A synchronization scenario corresponds to a specific set of synchronization levels in all domains.

(a) Minimum Synchronization (MS): MS corresponds to the minimal synchronization level. Under MS, no domains synchronize with any other domains. As a result, each controller only knows its own intra-domain topology and the domain-wise topology, but has no knowledge of its intra-domain link weights. This scenario captures IGP routing protocols that do not take into account any link weights but select routes purely based on the hop count (e.g., Routing Information Protocol (RIPv2)). Note that MS corresponds to the minimum network knowledge that is always available in scenarios in (b–d);

(b) Self-domain Synchronization (SS): In addition to the available knowledge provided by MS, each controller with SS knows nothing more except for the intra-domain link weights (not the distribution) in its own domain. With this additional information, one controller can find the optimal intra-domain path for any intra-domain flow request;

(c) Partial Synchronization (PS): PS refers to any synchronization level that is between SS and the following complete synchronization (CS);

(d) Complete Synchronization (CS): under CS, every pair of domains $A_i$ and $A_j$ synchronize with each other. As such, there is effectively one logically centralized controller, which can make globally optimal decisions. Among all these synchronization scenarios, CS experiences the highest synchronization cost.

Objective: Suppose (i) each network realization following the two-layer network model exists with the same probability, and (ii) the source-destination node pair belonging to two different domains in an arbitrary network realization following the two-layer network model, as the performance metric. APL is a natural generalized performance metric, as link weights can always be manipulated to reflect different routing objectives. Formally, our research objective is:

Objective: Suppose (i) each network realization following the two-layer network model exists with the same probability, and (ii) the source-destination node pair belonging to two different domains in an arbitrary network realization following the two-layer network model, as the performance metric. APL is a natural generalized performance metric, as link weights can always be manipulated to reflect different routing objectives. Formally, our research objective is:

Remark: It is important to notice that our two-layer network model is a random graph model, i.e., there exist multiple network realizations satisfying the same set of input parameters. Therefore, APL is an expected value over not only random source/destination node pairs but also random network realizations. All our theoretical results on APL are based on the given network parameters (e.g., degree and weight distributions) rather than a specific network realization.
### TABLE I: Main Notations.

| Symbol | Meaning |
|--------|---------|
| $n$    | number of nodes in a domain |
| $m$    | number of domains in the network |
| $\beta$ | maximum number of edges connecting two domains |
| $l$    | average shortest path length between a non-gateway and the closest gateway in a domain |
| $\Delta$ | average shortest domain-wise path length between two arbitrary domains |
| $D$    | random variable representing the shortest distance between two random nodes in a domain |
| $D^{(\beta)}_k$ | random variable representing the APL between two arbitrary nodes in the end-domains of a bus network of length $k$ |
| $M^{(\beta)}_k$ | random variable representing the APL between an arbitrary node in one domain and the closest gateway (connecting to external domains) in the other end-domain of a bus network of length $k$ |
| $L^{(\beta)}_k$ | expectation of random variable $D^{(\beta)}_k$ |

### III. AVERAGE PATH LENGTH UNDER MINIMUM SYNCHRONIZATION

In this section, we study the APL under MS, for which we describe the corresponding routing mechanism and then present its performance analysis. For ease of presentation, we first introduce the following definitions and notations.

**Definition 2.** 1) In the domain-wise topology $G_d$, the vertex corresponding to domain $A$ in $G$ is denoted by $\vartheta(A)$;

2) Given a pair of source and destination nodes $v_1$ and $v_2$ with $v_1 \in A_1$, $v_2 \in A_2$, and $A_1 \neq A_2$, the domain-wise path w.r.t. $v_1$ and $v_2$ is a path in $G_d$ starting at vertex $\vartheta(A_1)$ and terminating at vertex $\vartheta(A_2)$;

3) The shortest path between node $v$ and set $S$ is the shortest path in set $\{P_v: \text{shortest path between node } v \text{ and node } s, s \in S\}$.

**A. Routing Mechanism under MS (RMMS)**

A path between two nodes $v_1$ and $v_2$ can be constructed in the following way, called Routing Mechanism under MS (RMMS), which is similar to the BGP for inter-domain routing and the IGP for intra-domain routing:\footnote{Note that BGP routing policies typically reflects the commercial agreements among the domains. For generality purpose, we do not consider these factors in our routing mechanisms.}

(i) Select the shortest domain-wise path w.r.t. $v_1$ and $v_2$, which goes through vertices $\vartheta(A_1), \vartheta(A_2), \ldots, \vartheta(A_q)$ in $G_d (v_1 \in A_1, v_2 \in A_q)$, with ties (if any) broken arbitrarily. In other words, no domain-wise path from $\vartheta(A_1)$ to $\vartheta(A_q)$ traverses less than $q$ domains.

(ii) In domain $A_i$, let $w$ be (i) the source node $v_1$ if $i = 1$, or (ii) the starting point (also known as ingress node) selected by the controller in $A_{i-1}$ if $i \geq 2$. In addition, let (i) set $S = \{v_2\}$ if $i = q$, or (ii) $S = \{g: g \text{ is a gateway that has a link connecting to } A_{i+1}\}$ if $i < q - 1$. Then the controller in $A_i$ selects the shortest path $P_i$ in terms of the number of hops (link weights are not available, thus not considered) with ties broken randomly, from node $w$ to set $S$ using only nodes and links in $A_i$. Let $s' \in S$ denote the end-point of $P_i$. If $i \leq q - 1$, then the controller in $A_i$ further appends a random node $u \in \{w: w \in A_{i+1}, s'w \in G\}$ to path $P_i$, thus forming path $P'_i$ ($u$ is then the ingress node in $A_{i+1}$); otherwise $P'_i = P_i$.

(iii) The final end-to-end path $P$ connecting $v_1$ and $v_2$ is

$$P = P'_1 + P'_2 + \ldots + P'_q; \quad (1)$$

see Fig. 2 for the example.

**B. APL under Minimum Synchronization (MS)**

With RMMS, we are now ready to analyze APL for MS. The basic idea is that we first compute the average domain-wise path length w.r.t. two arbitrary source/destination nodes. Then in a domain-wise path with such average length, we calculate the average number of hops in each traversed domain, and add them together to get the final estimation of APL for MS. To this end, we first present the results in the existing work\footnote{This is similar to several IGPs, such as Open Shortest Path First (OSPF), RIP, RIPv2, and Intermediate System to Intermediate System (IS-IS) [24].} that can assist our mathematical analysis.

**Proposition 3.**\footnote{In an undirected graph $H$ with $n_0$ vertices and the vertex degree satisfying a given distribution, let $x_i$ be the average number of vertices that are $i$-hop away from a random vertex in $H$. Suppose all edge weights are 1, and $x_2 \gg x_1$. Then}

1) $x_i = (x_2/x_1)^{i-1} x_1$; \quad (2)

2) $\text{APL in } H$ is

$$\text{log}(n_0/x_1)/\text{log}(x_2/x_1) + 1. \quad (3)$$

In our two-layer model, the top-layer graph $G_d$ (domain-wise topology with $m$ vertices) itself is a random graph following a given domain-wise degree distribution. Therefore, similar to\footnote{In [27], we know that the average value of $q$ in (1) is $\Delta + 1$. If we further know the average length of $P'_q$ associated}, let $z'_i$ denote the average number of vertices that are $i$-hop away from a random vertex in $G_d$. For two arbitrary nodes $v_1$ and $v_2$ with $v_1 \in A_1$, $v_2 \in A_q$, and $A_1 \neq A_q$, let $\Delta$ denote the average number of hops of the shortest domain-wise path from vertex $\vartheta(A_1)$ to vertex $\vartheta(A_q)$ in $G_d$. Then according to\footnote{Note that BGP routing policies typically reflect the commercial agreements among the domains. For generality purpose, we do not consider these factors in our routing mechanisms.} (3), we have

$$\Delta = \text{log}(m/z'_1)/\text{log}(z'_2/z'_1) + 1, \quad (4)$$

assuming $z'_2 \gg z'_1$.

With\footnote{In [24], we know that the average value of $q$ in (1) is $\Delta + 1$. If we further know the average length of $P'_q$ associated}, we know that the average number of hops of the constructed path is $\text{log}(m/z'_1)/\text{log}(z'_2/z'_1) + 1$, implying that the APL for MS is

$$\text{APL for MS} = \text{APL for MS}, \quad (5)$$

Fig. 2: Path construction under RMMS w.r.t. $v_1$ and $v_2$, whose shortest domain-wise path traverses $A_1$, $A_2$, $A_4$, and $A_4$. Then $P_1 = v_1abc, P_2 = v_1cd, P_3 = ef, P_4 = ghv_2$. The constructed path is $P' = P_1 + P_2 + P_3 + P_4$, denoted by dotted line segments.
with the traversed domain \( A_i \), then we can estimate the APL of \( \mathcal{P} \). To this end, let \( |P| \) denote the number of hops on path \( \mathcal{P} \). Then according to (4), \( |P| = |P'_1| + |P'_2| + \ldots + |P'_{\Delta+1}| \), where \( q \) is replaced by its expectation \( \Delta + 1 \), and \( |P'_i| \) is a random variable. The expectation of \( |P| \) is

\[
E[|P|] = E[|P'_1| + |P'_2| + \ldots + |P'_{\Delta+1}|] = E[|P'_1|] + E[|P'_2|] + \ldots + E[|P'_{\Delta+1}|].
\]

(5)

According to the path construction procedure for MS, \( E[|P'_1|] = E[|P'_2|] = \ldots = E[|P'_{\Delta+1}|] \) for two reasons. First, all domains have the same statistical properties. Second, in each domain \( A_i \) (\( i \leq \Delta \)), the routing mechanism selects a gateway (from a candidate set) that is closest to the ingress node. By contrast, in domain \( A_{\Delta+1} \), the routing mechanism only selects the shortest path from the ingress node to a single node \( v_2 \), i.e., the destination. Thus, (5) can be simplified as

\[
E[|P|] = \Delta \cdot E[|P'_1|] + E[|P'_{\Delta+1}|].
\]

(6)

In a domain \( A \) with \( n \) intra-domain nodes, let \( z_i \) denote the average number of intra-domain nodes that are \( i \)-hop (\( i \geq 1 \)) away from an arbitrary node \( v (v \in \mathcal{A}) \). Then again by (3), we have

\[
E[|P'_{\Delta+1}|] = \frac{\log(n/z_1)}{\log(z_2/z_1)} + 1,
\]

(7)

assuming \( z_2 \gg z_1 \). Hence, to compute \( E[|P|] \) in (6), it suffices to consider only \( E[|P'_1|] \) associated with domain \( A_1 \).

We first compute the distribution of the distance between two random nodes within the same domain, called \( \text{INTER-DOMAIN DISTANCE DISTRIBUTION} \). Therefore, the routing mechanism under SS is almost the same as RMMS, except that each controller selects the shortest intra-domain path in terms of the accumulated link weight.

To analyze APL under SS, we need to combine the distributions of link weights and the number of hops into a new distance distribution for capturing APL. Here is the sketch of our analytical methodology.

**Sketch of Analytical Methodology:**

a) We first compute the distribution of the distance between two random nodes within the same domain, called \( \text{INTER-DOMAIN DISTANCE DISTRIBUTION} \).

We can determine the APL of \( P'_i \) for \( i = 1, 2, \ldots, q \). Since the domain-wise path is selected the same way as that under MS, again we have that the expected value of \( q \) is \( \Delta + 1 \).

b) The expression in (1) remains valid. Therefore, we need to determine the APL of \( P'_i \) for \( i = 1, 2, \ldots, q \). Since the domain-wise path is selected the same way as that under MS, again we have that the expected value of \( q \) is \( \Delta + 1 \).

c) As all controllers involved in the path construction process follow the same procedure, similar to (3), it suffices to only quantify the APL of \( P'_1 \) and \( P'_{\Delta+1} \) using the intra-domain distance distribution derived in a).

Based this methodology, we next discuss the details.
A. Intra-Domain Distance Distribution

In one domain, consider a path with $\lambda$ links. Let $W_1, W_2, \ldots, W_\lambda$ be i.i.d. random variables of link weights on this path with the probability density functions (pdf) being $f_{W_1}(x) = f_{W_2}(x) = \ldots = f_{W_\lambda}(x)$. Define random variable $W_\lambda := \sum_{i=1}^{\lambda} W_i$ as the accumulated weight on this path. Then the pdf of $W_\lambda$ is the convolution of the pdfs of $W_1, W_2, \ldots, W_\lambda$, i.e., $f_{W_\lambda}(x) = f_{W_1}(x) \ast f_{W_2}(x) \ast \ldots \ast f_{W_\lambda}(x)$. By the principle in mixture distribution [35], we still need to know the probability $p_{W_\lambda}$ of the shortest path (in terms of weights) between two random nodes containing $\lambda$ links. By the concept of $z_i$ we defined in the analysis of MS, we know that $p_{W_\lambda}$ is proportional to $z_\lambda$; therefore, by normalization, we get $p_{W_\lambda} = z_\lambda/n$. Note that when $\lambda = 0$, $z_0 = 1$ and the cumulative distribution function (cdf) of $W_0$ is a unit step function [36]. Let random variable $D$ be the shortest distance (in terms of overall weights) between two random nodes in one domain, with the pdf being $f_D(x)$, i.e., intra-domain distance distribution. Then by mixture distribution, $f_D(x)$ can be estimated as follows.  

$$f_D(x) = \sum_{i=0}^{h_{\text{max}}} p_{W_i} f_{W_i}(x) = \sum_{i=0}^{h_{\text{max}}} \frac{z_i}{n} f_{W_i}(x),$$  

(12)  

where $h_{\text{max}} := \arg \max_i z_i$ s.t. $\sum_{i=0}^{h_{\text{max}}} z_i \leq n$. Hence, the APL between two nodes in one domain is  

$$E[D] = \int_{x=0}^{+\infty} x f_D(x).$$  

(13)  

B. Domain-wise Path

Though SS and MS represent different synchronization levels, the corresponding domain-wise paths are exactly the same w.r.t. a pair of source and destination nodes in a given network. Thus, the end-to-end path construction can still be captured by (11). By (10), again, we have $q$ in (11) equals $\Delta + 1$. Let $L(P)$ be the end-to-end accumulated weight (i.e., length) of path $P$, which is a random variable. Then the expectation of $L(P)$, i.e., the APL for SS, denoted by $L_{ss}$ is  

$$L_{ss} = E[L(P)] = E[L(P_1') + L(P_2') + \ldots + L(P_{\Delta+1}')]$$  

(14)  

which is more complicated as the link weight can be of any distribution. Substituting (4), (18), and (13) into (14), we get the expression of $L_{ss}$.

C. Distance from a Node to the Closest Gateway

Let random variable $M(\beta)$ denote the shortest distance from an arbitrary node $w$ to the closest gateway in the candidate gateway set $S$ within a domain with the inter-domain connection parameter $\beta$, where $S$ contains all gateways connecting to the same neighboring domain. Recall that in our two-layer model, gateways are randomly selected. Therefore, let $D_1, D_2, \ldots, D_\beta$ be i.i.d. random variables, denoting the shortest distance between two random nodes in a domain with the same pdf as $D$ in (12). We have

$$M(\beta) = \min(D_1, D_2, \ldots, D_\beta),$$  

(15)  

and $L(P_1') = M(\beta) + 1$ as $P_1'$ terminates at domain $A_2$. As a special case, when $\beta = 1$, i.e., $\exists$ only one gateway in $S$, then $M(\beta) = D$. When $\beta > 1$, the probability $\Pr(M(\beta) \leq d) = \Pr(\min(D_1, D_2, \ldots, D_\beta) \leq d)$, i.e., at least one of $\{D_i\}_{i=1}^\beta$ is smaller than or equal to $d$. Therefore, let $F_D(x)$ be the cdf of $D$, and $F_{M(\beta)}(x)$ be the cdf of $M(\beta)$. Then  

$$F_{M(\beta)}(x) = 1 - (1 - F_D(x))^\beta.$$  

(16)  

Therefore, the pdf of $M(\beta)$ is  

$$f_{M(\beta)}(x) = \begin{cases} (1 - F_D(x))^\beta & \text{for } x \geq 1, \\ 1 - (1 - F_D(0))^\beta & \text{for } x = 0. \end{cases}$$  

(17)  

With (17), we derive  

$$E[L(P_1')] = E[M(\beta)] + 1 = \int_{x=0}^{+\infty} x f_{M(\beta)}(x) + 1.$$  

(18)  

B. Routing Mechanism under PS (RMPS)

Under the above partial synchronization model, we now describe a basic routing mechanism under PS, RMPS.

(i) Since $PS \neq CS$, similar to RMMS, for the given two nodes $v_1$ and $v_2$, RMPS first selects the shortest domain-wise path $P(v_1, v_2)$, which goes through vertices $\partial(A_1), \partial(A_2), \ldots, \partial(A_q)$ in $G_d$ ($v_1 \in A_1, v_2 \in A_q$), with ties (if any) broken randomly.

(ii) Following the direction from $\partial(A_1)$ to $\partial(A_q)$, RMPS partitions $P(v_1, v_2)$ into $[q/\tau]$ non-overlapping sub-paths $\{A_i\}$, where vertices $\partial(A_{(i-1)} \tau + 1), \partial(A_{i \tau + 2}), \ldots, \partial(A_{i \tau + 2})$.
Routing clusters 1 and 2

\( q = 4, \tau = 2 \), the dotted line segments represent constructed path

\[ A \rightarrow P \rightarrow A \rightarrow P \rightarrow A \]

(iii) Viewing each routing cluster as a whole “domain”, path segments are constructed in each routing cluster similar to step (ii) of RMMS, except that paths are computed based on link weights. Let \( S_i' \) be the constructed path segment by controllers in routing cluster \( i \). Note that similar to RMMS, \( S_i' \) is the concatenation of path \( S_i \) within routing cluster \( i \) and a link connecting to routing cluster \( i + 1 \) when \( i < [q/\tau] \);

(iv) The final end-to-end path \( P \) connecting \( v_1 \) and \( v_2 \) is

\[ P = S_1' + S_2' + \ldots + S_{[q/\tau]'} \].

Remark: RMPS provides a basic path construction method for the PS scenario. Note that though domains in different routing clusters may synchronize with each other (e.g., domains \( A_2 \) and \( A_3 \) in Fig. 3), the synchronized information may not be used under RMPS. We acknowledge that there may exist other routing algorithms with better performance. However, our intention here is not to design an optimal routing mechanism for PS. Instead, our goal is to quantify the performance of a given routing mechanism for PS, for which we select RMPS as a representative routing mechanism to analyze.

C. APL under Partial Synchronization (PS)

To compute APL incurred by RMPS under PS, denoted by \( L_{ps} \), we first consider APL w.r.t. two nodes with their shortest domain-wise path traversing exactly \( \lfloor q/\tau \rfloor \) vertices, denoted by \( L_{ps}^0 \). Similar to (6), we know from (19) that \( E[S_1] = E[S_2] = \ldots = E[S_{\lfloor q/\tau \rfloor}] \). Therefore, it suffices to determine \( E[S_1] \) and \( E[S_{\lfloor q/\tau \rfloor}] \). For ease of presentation, we introduce the concept of bus networks.

Definition 4. A bus network of length \( k \), a special graph following the two-layer network model, consists of \( k \) domains, where its domain-wise topology is a connected line graph (i.e., a special tree with each vertex having at most one child).

In a bus network of length \( k \) with the involved domains labelled as \( A_1, A_2, \ldots, A_k \), let random variable \( D_k \) denote the length of the shortest path between two arbitrary nodes \( v_1 \in A_i \) and \( v_2 \in A_j \). In the domain-wise topology, let \( M_k \) be the length of the shortest path between an arbitrary node \( v_1 \in A_i \) and the closest gateway in \( A_i \) connecting to domains outside this bus network. Hence, to determine \( E[S_1] \) and \( E[S_{\lfloor q/\tau \rfloor}] \), we only need to compute \( E[M] \) and \( E[D_k] \). Thus, we define random variable \( X := D_k + \min \{M, k\} + 1 \). Let \( X_1, X_2, \ldots, X_k \) be i.i.d. random variables following the same distribution as \( X \). Then similar to (15), we have

\[ D_k^* = \min(X_1, X_2, \ldots, X_k) \]

where \( D_k^* = D \). Analogously, let \( Y := D_k + \min \{Y_1, Y_2, \ldots, Y_k\} + 1 \) be i.i.d. random variables following the same distribution as \( Y \). Then \( M_k = \min(Y_1, Y_2, \ldots, Y_k) \), where \( M_k = \min(Y_1, Y_2, \ldots, Y_k) \) is defined in (15). Then following the same method in (16–18), \( E[M^*_k] \) and \( E[M_k] \) are computable. Note that it is expensive to compute \( D_k^* \) and \( M_k \), as they are defined in a recursive way; more efficient computation methods are discussed in Section VI.

Next, depending on the value of \( q \), we have

\[ L_{ps} = \begin{cases} \left( \frac{q}{\tau} - 1 \right) \cdot (E[M^*_k] + 1) + E[D_k^*] & \text{if } \theta = 0; \\ \frac{q}{\tau} \cdot (E[M^*_k] + 1) + E[D_k^*] & \text{if } \theta > 0. \end{cases} \]

where \( \theta = q \mod \tau \). Recall that two arbitrary nodes with their domain-wise path length containing \( q \) vertices happen with probability being approximately \( \frac{z}{z-1/m} \). Therefore, \( L_{ps} = \sum_{i=1}^{n} h_{i} + L_{ps} \), where \( h_{i} = \max \{z_1, z_2, \ldots, z_{n}\} \) s.t. \( L_{ps} = \sum_{i=1}^{n} h_{i} \leq m \).

VI. AVERAGE PATH LENGTH UNDER COMPLETE SYNCHRONIZATION

For complete synchronization (CS), all SDN domains are synchronized, which is equivalent to the case where there exists a logical centralized controller in the network. Therefore, the routing mechanism for CS is simple, and all controllers make the unanimous global optimal decisions. Since CS represents the best synchronization level, the following analytical results also serve as a performance bound that no routing mechanisms for any synchronization levels can exceed.

Given two arbitrary nodes \( v_1 \) and \( v_2 \), suppose the shortest domain-wise path \( P^* \) w.r.t. \( v_1 \) and \( v_2 \) contains \( k \) vertices in the domain-wise topology. If \( P^* \) corresponds to the shortest path between \( v_1 \) and \( v_2 \), then the APL under CS can be easily obtained as we have derived a method to compute \( E[D_k] \), the APL w.r.t. two random nodes at the end-domains in a bus network of length \( k \), in Section V. However, for the global shortest path \( P^* \), it is possible that \( P^* \) visits more than \( k \) domains while experiencing a shorter end-to-end path length. We, therefore, derive the properties of \( E[D_k] \) and examine how it is related to \( P^* \). Let \( L_k(\beta) := E[D_k] \). Then

**Theorem 5.** For the two-layer network model, \( L_k(\beta) < L_{k+1}(\beta) \) when \( k \geq 3 \).

**Proof:** Consider two bus networks of length \( k \) and \( k + 1 \), whose domains are labelled as \( A_1, A_2, \ldots, A_k \) and \( B_1, B_2, \ldots, B_k+1 \), respectively. Let \( V_i(\mathcal{C}) \) (\( V_{out}(\mathcal{C}) \)) be the set of gateways in domain \( \mathcal{C} \) connecting to domain \( \mathcal{C}_{i-1} \)
(C_{i+1}). Without loss of generality, we assume that A_1 = B_1 and A_k = A_{k+1}. This implies that V_{out}(A_1) = V_{out}(B_1) and V_{in}(A_k) = V_{in}(B_{k+1}). Therefore, L_k(\beta) and L_{k-1}(\beta) are determined by the pair-wise distance between V_{out}(A_1) and V_{in}(A_k), and V_{out}(B_1) and V_{in}(B_{k+1}), respectively. When k ≥ 3, there exist at least one domain, called middle domain, apart from the end-domains in a bus network. Since all middle domains have the same statistical parameters, each middle domain offers the same probability of finding a path with certain APL in that domain. Furthermore, more middle domains introduce more inter-domain edges. Thus, there is no higher possibility of finding a shorter route due to the presence of more middle domains. Therefore, more middle domains result in higher expectation of pair-wise distance between V_{out}(B_1) and V_{in}(B_{k+1}).

Theorem 5 reveals a property of L_k(\beta) that is vital to our analysis, i.e., a longer domain-wise path incurs higher end-to-end path weight if the shortest domain-wise path between two nodes contains at least three vertices. Note that in Theorem 5 there are two uncovered cases. First, k = 1. Since we are not interested in determining APL for two random nodes within the same domain, this case is ignored. Second, k = 2. From numerical results, we observe that L_2(\beta) may be slightly greater than L_3(\beta) when \beta satisfies certain conditions. Nevertheless, the case that two random nodes residing in two neighboring domains only happen with probability z'_1/m, which can be ignored as z'_2 ≫ z'_1 and m is large. Next, based on Theorem 5 the following two corollaries on L_k(\beta) can be deduced, which always hold irrespective of the values of k.

**Corollary 6.** For the two-layer network model, L_{k+1}(1) − L_k(1) = E[D] + 1.

*Proof:* When \beta = 1, L_k(1) = \mathbb{E}[D^{(1)}_k] = k\mathbb{E}[D] + k - 1, and L_{k+1}(1) = \mathbb{E}[D^{(1)}_{k+1}] = (k + 1)\mathbb{E}[D] + k. Therefore, L_{k+1}(1) − L_k(1) = \mathbb{E}[D^{(1)}_{k+1}] - \mathbb{E}[D^{(1)}_k] = \mathbb{E}[D] + 1. □

**Corollary 7.** For the two-layer network model, \lim_{\beta \to \infty} (L_{k+1}(\beta) − L_k(\beta)) = 1.

*Proof:* In a bus network with k domains A_1, A_2, ..., A_k, when \beta → \infty, every node in domain A_i directly connects to all nodes in domain A_{i+1} (i ≤ k − 1). As a result, the APL within each domain on a bus network is 0. Thus, the APL is the sum weight of all traversed inter-domain edges, which is k for L_{k+1}(\beta) and k − 1 for L_k(\beta). □

Note that one implicit assumption for Theorem 5 is that the domain-wise path associated with the constructed path is a simple path, i.e., a path without repeated vertices. To show that visiting more domains cannot construct a shorter end-to-end path, we still need to prove that visiting one domain more than once is also disadvantageous. To this end, we define L'_k(\beta) which is similar to L_k(\beta) except that the corresponding domain-wise path contains repeated vertices.

**Corollary 8.** For the two-layer network model, L_k(\beta) < L'_{k'}(\beta) for k' > k.

### A. Efficient Computation of E[D(\beta)]

The computation of L_{CS} in [22] relies on E[D(\beta)]. Since D(\beta) is defined in a recursive way, it is expensive to compute the exact value of E[D(\beta)]. As such, we establish an efficient strategy to estimate E[D(\beta)]. Specifically, let D_1, D_2, ..., D_k denote i.i.d. random variables following the same distribution as D. Then we define random variable \(Z^{(k)} := \sum_{i=1}^{k} D_i + k - 1\). For the two-layer network model, when the length of the bus network is increased by 1, the number of path options w.r.t. two random nodes at the end-domains grows \beta-fold. Therefore, let \(Z^{(k)}_1, Z^{(k)}_2, ..., Z^{(k)}_{\beta-1}\) be i.i.d. random variables following the same distribution as \(Z^{(k)}\). Define \(\tilde{D}(\beta) := \min(Z^{(k)}_1, Z^{(k)}_2, ..., Z^{(k)}_{\beta-1})\). We then use E[\tilde{D}(\beta)] to approximate E[D(\beta)]. Such efficient approximation method is accurate, which is discussed in the following section.
VII. Evaluations

To evaluate our analytical results of distributed SDN for various synchronization scenarios, we conduct a series of experiments on network topologies generated from both real and synthetic datasets. The focus in this section is two-fold. First, we validate the accuracy of the derived $L_{MS}$, $L_{SS}$, $L_{PS}$, and $L_{CS}$. We compare these theoretical results with the actual APLs collected from the above networks. Second, we aim to understand to what extent synchronization levels and network structures affect APLs, i.e., to justify the benefit of the synchronization cost and the network structural design.

A. Network Realizations

1) Network Topologies Based on Real Datasets: To generate network topologies based on real datasets, we need the degree distributions as the input. Specifically, we use the real datasets collected by the University of Oregon Route Views Project (Routeview project) [37], the Rocketfuel project [38], and the CAIDA project [39] for input degree distributions.

Given a specific degree distribution, one graph realization is generated in the following way: We assign each vertex (the total number of vertices is given) a target degree according to the degree distribution. We then select two vertices randomly and add an edge between them; the number of edges added w.r.t. each vertex is then recorded. If the degree target w.r.t. a vertex is met, this vertex will not be selected again to connect with other vertices. Such process repeats until all vertices reach their degree targets.

2) Network Topologies Based on Synthetic Models: We select Barabási-Albert [26] and Erdős-Rényi [25] models to generate network topologies.

(a) Barabási-Albert (BA) model: BA model starts with a small connected graph of a few nodes/edges. Then, we sequentially add new nodes in the following way: For each new node $v$, we connect $v$ to $g$ existing nodes such that the probability of connecting to node $w$ is proportional to the degree of $w$. If the number of existing nodes is smaller than $g$, then $v$ connects to all existing nodes. Vertex degree for the BA model follows a near power-law distribution. BA graphs can be used to model many naturally occurring networks, e.g., Internet and social networks.

(b) Erdős-Rényi (ER) model: For the ER model, the graph is generated by independently adding an edge between two nodes with a fixed probability $p$. The result is a purely random topology where all graphs with an equal number of links/edges are equally likely to be selected. Vertex degree under ER follows a binomial distribution.

Then, intra- and inter-domain topologies are generated based on the above network realization methods; see VII-B for details.

Remark: It should be noted that the above network realizations are only for the evaluation purpose. Our developed analytical results are generic, and are not restricted to any specific topological conditions.

B. Evaluation Settings

Three evaluation cases are studied: (i) Case 1, where we use degree distribution extracted from data collected on March 31, 2001 by the Routeview project to generate intra-domain topology. The inter-domain degree distribution used is based on AS27524 in CAIDA; (ii) Case 2, where the intra-domain degree distribution is calculated from AS1239 in the Rocketfuel project, and the inter-domain degree distribution is also based on AS27524 in CAIDA; (iii) Case 3, where all intra-domain topologies are BA graphs and the inter-domain topology is an ER graph. For each case, the two-layer network consists of 100 domains, each containing 200 nodes, i.e., $m = 100$ and $n = 200$. For a given $\beta$, 30 two-layer networks are realized. In each network realization, 50 source-destination pairs (in different domains) are randomly selected to construct paths between them with MS, SS, PS, and CS. In addition, for PS, two special cases, i.e., $\tau = 2$ and $\tau = 3$, are studied to compare against other synchronization scenarios. It should be noted that these settings are determined arbitrarily, as our analytical model does not require the input degree distributions to have certain patterns/properties.

C. Evaluation Results

The simulated APL averaged over all network realizations and source-destination node pairs are reported in Fig. 5(a)-(c), each of the evaluation cases, respectively. In these figures, each curve is also accompanied by our developed theoretical performance estimation.

1) Accuracy of the Theoretical Results: Evaluations of various real/synthetic networks in Fig. 5 confirm the high accuracy of our theoretical results in predicting the performance metric APL in distributed SDN networks. Specifically, the simulation curves can be closely approximated by the theoretical results for all values of $\beta$ and synchronization scenarios. Moreover, the theoretical results for PS and CS are obtained by the efficient computation method in Section VI-A. Fig. 5 shows that even such simplified method for approximating $L_k(\beta)$ exhibits high accuracy. Intuitively, this is because the process of establishing inter-domain connections in our network model is purely random, which enables us to use $\beta^{k-1}$ (see Section VI-A for details) to estimate the number of route options between two random nodes in the end-domains of a bus network of length $k$.

2) APL Variations for Different Synchronization Levels and Structural Parameters: Fig. 5 confirms that the APL in distributed SDN is related to the amount of information available to the controllers, i.e., synchronization levels. As expected, higher synchronization levels is superior in reducing APLs. In particular, APL for CS corresponds to the minimum APL that is achievable in all cases, i.e., a lower bound. By contrast, the results for MS act as an upper bound due to the minimum intra-/inter-domain information availability. Since the APL for
MS is expressed as a logarithmic function \( \beta \), Fig. 5 shows that even with the minimum synchronization level, APL is still significantly smaller than the network size (20,000 nodes in total) when all edge weights are at least 1. Fig. 5 shows that comparing to MS, the APL reduction for CS can be up to 60%. Moreover, comparing to MS, only intra-domain link weight information is available to SS. Nevertheless, such additional information is able to reduce APL by up to 50%. However, when more synchronized information is available, the reduction in APL starts to reduce (i.e., diminishing return). In particular, for PS, comparing against the case of \( \tau = 2 \), the APL reduction for \( \tau = 3 \) is rather minimal, especially when \( \beta \) is small. Consequently, it is expected that with the increase of \( \tau \), the benefit to cost ratio declines sharply. Finally, as \( \beta \) is a structural parameter, we observe that the network performance improves when \( \beta \) increases. This is intuitive as a large \( \beta \) directly renders the probability of finding a shorter route to be notably high, as there exist more inter-domain connections available for the routing mechanisms to choose from. Furthermore, Fig. 5 also demonstrates that APL converges to a certain value when \( \beta \) is large, which can be explained by Corollary [1].

In summary, these evaluation results reveal that in distributed SDN, the performance improvement space is only marginal when the network exhibits high synchronization level and contains a large number of gateways in each domain. Such constraints need to be addressed in practical network design and optimizations.

**VIII. CONCLUSIONS**

We have studied the performance of distributed SDN networks for different inter-domain synchronization levels and network structural properties from the analytical perspective. For this goal, a generic network model is first proposed to capture key attributes in distributed SDN networks. Based on this model, we have developed analytical results to quantify the performance of the constructed paths for four canonical synchronization scenarios. Extensive simulations on both real and synthetic networks show that our developed analytical results exhibit high accuracy while also providing significant insights into the relationship between the network performance and operational tradeoffs, which are vital to future network architecture and protocol design.

**REFERENCES**

[1] N. McKeown, “Software-defined networks and the maturing of the Internet,” The Institution of Engineering and Technology, 2014. [Online]. Available: https://tv.thiet.org/?video=5447

[2] D. Kreutz, F. M. Ramos, P. E. Verissimo, C. E. Rothenberg, S. Azodolmolky, and S. Uhlig, “Software-defined networking: A comprehensive survey,” Proceedings of the IEEE, vol. 103, no. 1, pp. 14–76, 2015.

[3] B. A. A. Nunes, M. Mendonca, X.-N. Nguyen, K. Obraczka, and T. Turletti, “A survey of software-defined networking: Past, present, and future of programmable networks,” IEEE Communications Surveys & Tutorials, vol. 16, no. 3, pp. 1617–1634, 2014.

[4] M. Casado, M. J. Freedman, J. Pettit, J. Luo, N. McKeown, and S. Shenker, “Ethane: Taking control of the enterprise,” in ACM SIGCOMM Computer Communication Review, vol. 37, no. 4, 2007, pp. 1–12.

[5] A. Gupta, L. Vanbever, M. Shahbaz, S. P. Donovan, B. Schlinker, N. Feamster, J. Rexford, S. Shenker, R. Clark, and E. Katz-Bassett, “SDX: A software defined internet exchange,” ACM SIGCOMM Computer Communication Review, vol. 44, no. 4, pp. 551–562, 2015.

[6] V. Kotronis, X. Dimitropoulos, and B. Ager, “Outsourcing the routing control logic: Better Internet routing based on SDN principles,” in ACM HotNets-XI, 2012.

[7] V. Kotronis, R. Klöti, M. Rost, P. Georgopoulos, S. B. Ager, S. Schmid, and X. Dimitropoulos, “Stitching inter-domain paths over IXPs,” in ACM SOSR, 2016.

[8] G. Petropoulos, F. Sardis, S. Spirou, and T. Mahmoodi, “Software-defined inter-networking; Enabling coordinated QoS control across the Internet,” in IEEE ICT, 2016.

[9] Z. Chen, J. Bi, Y. Fu, Y. Wang, and A. Xu, “Mlv: A multi-dimension routing information exchange mechanism for inter-domain SDN,” in IEEE ICNP, 2015.

[10] P. Thai and J. C. de Oliveira, “Decoupling policy from routing with software defined interdomain management: Interdomain routing for SDN-based networks,” in IEEE ICCCN, 2013.

[11] K. Poularakis, G. Josifidis, G. Saridakis, and L. Tassulas, “One step at a time: Optimizing SDN upgrades in ISP networks,” in IEEE INFOCOM, 2017.

[12] A. Tootoonchian and Y. Ganjali, “Hyperflow: A distributed control plane for openflow,” in Proceedings of the 2010 internet network management conference on Research on enterprise networking, 2010, pp. 3–3.

[13] P. Berde, M. Gerola, J. Hart, Y. Higuchi, M. Kobayashi, T. Koide, B. Lantz, B. O’Connor, P. Radoslavov, W. Snow et al., “One step towards an open, distributed SDN OS,” in ACM HotSDN, 2014.

[14] A. R. Curtis, J. C. Mogul, J. Tournilhes, P. Yalagandula, P. Sharma, and S. Banerjee, “Devflow: Scaling flow management for high-performance networks,” ACM SIGCOMM Computer Communication Review, vol. 41, no. 4, pp. 254–265, 2011.

[15] S. Hassas Yeganeh and Y. Ganjali, “Kandoor: a framework for efficient and scalable offloading of control applications,” in Proceedings of the first workshop on Hot topics in software defined networks. ACM, 2012, pp. 19–24.
[16] M. Yu, J. Rexford, M. J. Freedman, and J. Wang, “Scalable flow-based networking with DIFANE,” ACM SIGCOMM Computer Communication Review, vol. 40, no. 4, pp. 351–362, 2010.

[17] S. Visicchio, O. Tilmans, L. Vanbever, and J. Rexford, “Central control over distributed routing,” ACM SIGCOMM Computer Communication Review, vol. 45, no. 4, pp. 43–56, 2015.

[18] S. Jain, A. Kumar, S. Mandal, J. Ong, L. Poutievski, A. Singh, S. Venkata, J. Wanderer, J. Zhou, M. Zhu et al., “B4: Experience with a globally-deployed software defined WAN,” ACM SIGCOMM Computer Communication Review, vol. 43, no. 4, pp. 3–14, 2013.

[19] K.-K. Yap, M. Motiwala, J. Rahe, S. Padgett, M. Holliman, G. Baldus, M. Hines, T. Kim, A. Narayanan, A. Jain et al., “Taking the edge off with espress: Scale, reliability and programmability for global internet peering,” in ACM SIGCOMM, 2017.

[20] G. Szabó, M. Alava, and J. Kertész, “Structural transitions in scale-free networks,” Physical Review E, vol. 67, no. 5, p. 056102, 2003.

[21] D. J. Watts and S. H. Strogatz, “Collective dynamics of small-world networks,” Nature, vol. 393, no. 6684, pp. 440–442, 1998.

[22] M. Girvan and M. E. Newman, “Community structure in social and biological networks,” Proceedings of the national academy of sciences, vol. 99, no. 12, pp. 7821–7826, 2002.

[23] R. Milo, S. Shen-Orr, S. Itzkovitz, N. Kashtan, D. Chklovskii, and U. Alon, “Network motifs: Simple building blocks of complex networks,” Science, vol. 298, no. 5594, pp. 824–827, 2002.

[24] A. L. Barabási, “Scale-free networks: A decade and beyond,” Science, vol. 325, no. 5939, pp. 412–413, 2009.

[25] P. Erdős and A. Rényi, “On the evolution of random graphs,” Publ. Math. Inst. Hung. Acad. Sci, vol. 5, no. 1, pp. 17–60, 1960.

[26] A.-L. Barabási and R. Albert, “Emergence of scaling in random networks,” Science, vol. 286, no. 5439, pp. 509–512, 1999.

[27] M. E. Newman, S. H. Strogatz, and D. J. Watts, “Random graphs with arbitrary degree distributions and their applications,” Physical review E, vol. 64, no. 2, p. 026118, 2001.

[28] A. Aleta, S. Meloni, and Y. Moreno, “A multilayer perspective for the analysis of urban transportation systems,” Scientific reports, vol. 7, p. 44359, 2017.

[29] Q. Guo, E. Cozzo, Z. Zheng, and Y. Moreno, “Levy random walks on multiplex networks,” Scientific reports, vol. 6, 2016.

[30] L. Schiff, S. Schmid, and P. Kuznetsov, “In-band synchronization for distributed SDN control planes,” SIGCOMM Comput. Commun. Rev., vol. 46, no. 1, pp. 37–43, Jan. 2016.

[31] N. Feamster, J. Rexford, and E. Zegura, “The road to SDN: An intellectual history of programmable networks,” SIGCOMM Comput. Commun. Rev., vol. 44, no. 2, pp. 87–98, Apr. 2014.

[32] T. Bates, E. Chen, and R. Chandra, “BGP route reflection: An alternative to full mesh internal BGP (IBGP),” Internet Requests for Comments, RFC Editor, RFC 4456, 2006. [Online]. Available: http://www.rfc-editor.org/rfc/rfc4456.txt.

[33] R. Chandra, P. Traina, and T. Li, “BGP communities attribute,” Tech. Rep., 1996.

[34] V. Vetriselvan, P. R. Patil, and M. Mahendran, “Survey on the RIP, OSPF, EIGRP routing protocols,” International Journal of Computer Science and Information Technologies, vol. 5, no. 2, pp. 1058–1065, 2014.

[35] B. S. Everitt, Mixture Distributions. Wiley Online Library, 1985.

[36] R. Bracewell, “Heaviside’s unit step function,” The Fourier Transform and Its Applications, pp. 61-65, 2000.

[37] “University of Oregon route views project,” University of Oregon, 2005. [Online]. Available: http://www.routeviews.org/.

[38] “Rocketfuel: An ISP topology mapping engine,” University of Washington, 2002. [Online]. Available: http://www.cs.washington.edu/research/networking/rocketfuel/interactive/.

[39] “Center for applied Internet data analysis (CAIDA),” CAIDA, 2017. [Online]. Available: http://www.caida.org/home/.