A Lagrangian Perspective on Stable Water Isotopes During the West African Monsoon

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Abstract We present a Lagrangian framework for identifying mechanisms that control the isotopic composition of mid-tropospheric water vapor in the Sahel region during the West African Monsoon 2016. In this region mixing between contrasting air masses, strong convective activity, as well as surface and rain evaporation lead to high variability in the distribution of stable water isotopologues. Using backward trajectories based on high-resolution isotope-enabled model data, we obtain information not only about the source regions of Sahelian air masses, but also about the evolution of H2O and its isotopologue D2O (expressed as δD) along the pathways of individual air parcels. We sort the full trajectory ensemble into groups with similar transport pathways and hydro-meteorological properties, such as precipitation and relative humidity, and investigate the evolution of the corresponding paired [H2O, δD] distributions. The use of idealized process curves in the [H2O, δD] phase space allows us to attribute isotopic changes to contributions from (a) air mass mixing, (b) Rayleigh condensation during convection, and (c) microphysical processes depleting the vapor beyond the Rayleigh prediction, i.e., partial rain evaporation in unsaturated and isotopic equilibration in saturated conditions. Different combinations of these processes along the trajectory ensembles are found to determine the final isotopic composition in the Sahelian troposphere during the monsoon. The presented Lagrangian framework is a powerful tool for interpreting tropospheric water vapor distributions. In the future, it will be applied to satellite observations of [H2O, δD] over Africa and other regions in order to better quantify characteristics of the hydrological cycle.

1. Introduction

The meteorology and hydrology of West Africa is dominated by the complex West African Monsoon (WAM) system (Fink et al., 2017). The onset of the WAM is characterized by a shift of maximum rainfall from the Guinea Coast to the Sahel (Fitzpatrick et al., 2015; Sultan & Janicot, 2003), where the rainfall is crucial for the livelihoods of the local population in terms of water resources. During the Sahelian rainy season from July to September, the moist southwesternly monsoon flow from the tropical Atlantic encounters the dry northeasterly Harmattan winds along the so-called Intertropical Discontinuity (ITD), a sharp air mass boundary characterized by large contrasts in humidity, temperature, vertical stability, and dust content. The temperature difference leads to a marked thermal wind maximum at around 600 hPa and 15°N, the African easterly jet (AEJ) (Cook, 1999; Wu et al., 2009). Large-scale subsidence and occasional extratropical mid-level dry intrusions from northern Africa (Roca et al., 2005) enhance the dryness on the poleward side of the ITD. In the environment of the ITD, strong convective instability and vertical wind shear support the development of highly organized, long-lived Mesoscale Convective Systems (MCSs; Fink & Reiner, 2003). When the mid-level dry air overrides the low-level moist monsoonal air, strong downdrafts and rain evaporation occur, which favor the formation of surface cold pools and ultimately result in intense air mass mixing.

The complex interactions of large-scale dynamical with small-scale convective and microphysical processes lead to a substantial spatio-temporal variability in the tropospheric moisture budget over the Sahel, which is still poorly understood (Bielli et al., 2010; Meynadier, Bock, Guichard, et al., 2010; Meynadier, Bock,
During the last decades, the analysis of stable water isotopologues in atmospheric water vapor and precipitation has been established as a powerful tool for investigating atmospheric moisture pathways. As each water isotopologue (hereafter referred to as water isotope) is associated with characteristic water vapor pressures and diffusivities, the ratios of different isotopes are altered during phase changes. The ratio $R$ between the heavier water isotope HDO against the lighter H$_2$O is given as $\delta D = 1000 \times (R/R_0 - 1)$ in $\%$. Several studies have emphasized the potential of the paired analysis of H$_2$O and $\delta D$, as this allows for evaluating effects of different moisture processes on tropospheric water vapor, such as air mass mixing (González et al., 2016; Lacour et al., 2017; Noone et al., 2011), condensation (Noone, 2012; Schneider et al., 2016), rain evaporation (Field et al., 2010; Worden et al., 2007), and deep convection (Bolot et al., 2013; Lacour et al., 2018). In this context, Noone (2012) derived a theoretical framework for characterizing the variability between H$_2$O and $\delta D$ by means of idealized process curves in the [H$_2$O, $\delta D$] phase space that describe effects of mixing (Gedzelman, 1988; Keeling, 1958), and cloud and rain microphysics (Ciais & Jouzel, 1994; Dansgaard, 1964; Merlivat & Jouzel, 1979; Rayleigh, 1902). Even though some of these simple models (e.g., the Rayleigh distillation for cloud formation) implicitly involve the Lagrangian perspective, the theoretical framework of Noone (2012) has never been explicitly applied in combination with air parcel trajectories and their isotope signals.

So far only few studies have investigated tropospheric distributions of stable water isotopes during the WAM. For instance, by using local rainfall samples and laser-based water vapor measurements, the impact of monsoon convection on isotope abundances was analyzed (Risi, Bony, Vimeux, Chong, & Descroix, 2010; Risi, Bony, Vimeux, Descroix, et al., 2008; Tremoy et al., 2012, 2014). A model-based approach to understand the Sahelian water budget was conducted by Risi, Bony, Vimeux, Frankenberg, et al. (2010), who underlined the strong influence of large-scale subsidence and convective activity to the isotopic variability in vapor and rain over the Sahel. However, this study concluded that the quantification of convective processes still remains a key challenge.

Recently, a novel data set of paired distributions of mid-tropospheric H$_2$O and $\delta D$ (also referred to as [H$_2$O, $\delta D$] pairs) was generated by using remote sensing data from the satellite sensor Metop/IASI (Diekmann et al., 2021; Schneider et al., 2021). Due to its high resolution in space (horizontal pixel size of 12 km, sensitive to $\delta D$ variations between 2 and 7 km) and time (global coverage of cloud-free scenes twice per day, between October 2014 and June 2019), this data set provides promising new opportunities for investigating the isotopic composition in the mid-troposphere, globally and in regions of particular interest such as West Africa. However, the challenge to take full benefit of this new wealth of information lies in the fact that individual scenes give snapshot distributions of the current atmospheric state without direct information on the processes that have led to the measured composition, particularly as different combinations of processes can lead to similar distributions in [H$_2$O, $\delta D$].

To overcome this challenge and aid the interpretation of Metop/IASI or similar data, we here develop a new Lagrangian framework for attributing signals in paired [H$_2$O, $\delta D$] distributions to underlying processes. For this purpose, we analyze the evolution of meteorological conditions, including isotope variables, along the atmospheric pathways of backward trajectories in order to understand the physical causes of air mass characteristics found in selected target regions.

As an exemplary case study to demonstrate the power of our new framework, we have selected the WAM period of 2016, for which the DACCIWA (Dynamics-Aerosol-Chemistry-Cloud Interactions in West Africa) measurement campaign elaborated an extensive meteorological documentation (Knippertz et al., 2017). As basis for the trajectory calculation we use the regional isotope-enabled model COSMO$_{iso}$ (see Section 3.1) that was run in a convection-permitting setup in order to account for the complex meteorology of the region Gervois, et al., 2010). The lack of a dense operational measurement network further hampers a detailed analysis of Sahelian moisture and its sources (Parker et al., 2008). Consistent with this, both weather forecasts (Vogel et al., 2018) and climate projections (Roehrig et al., 2013) show large uncertainties over the Sahel. Through teleconnections (e.g., Bielli et al., 2010), the poor performance of numerical models over West Africa can even negatively affect forecasts over the adjacent Atlantic and Europe (Pante & Knippertz, 2019). Given the enormous socio-economic importance of Sahelian rainfall, new approaches to better understand and quantify moisture processes in this region are urgently needed.
Using the isoCOSMO output, we apply the Lagrangian analysis tool LAGRANTO (see Section 3.2) to compute 7-day backward trajectories from the Sahelian mid-troposphere and to trace moisture diagnostics along individual trajectories. This paves the way for categorizing the temporal evolution of the \( \{\overset{2}{H}E, \overset{\delta}{D}\} \) signals along the trajectories based on the underlying meteorological conditions. In this manner, we can examine, whether and under which conditions the theoretical process curves of mixing and microphysical processes from Noone (2012) are representative for the isotopic evolution along the trajectories, and to which extent they can explain the general isotopic evolution in the Sahelian mid-troposphere during the monsoon season 2016.

In Section 2, we give a short overview about idealized process signals in paired \( \{\overset{2}{H}E, \overset{\delta}{D}\} \) distributions. Section 3 describes our modeling approach based on isoCOSMO, LAGRANTO, and the applied process-attribution method. In Section 4, we analyze the isotopic composition of the Sahelian troposphere during the WAM season 2016. Finally, Section 5 wraps up the results and gives an outlook on future work.

2. Signature of Different Moist Processes in \( \{\overset{2}{H}E, \overset{\delta}{D}\} \) Pair Distributions

Throughout the last decades, the paired analysis of stable water isotopes has proven highly valuable for retrieving information about atmospheric moisture processes (e.g., Eckstein et al., 2018; Graf et al., 2019; Noone et al., 2011; Schneider et al., 2016; Worden et al., 2007). As a theoretical basis for interpreting paired distributions of \( \overset{2}{H}E \) (given in volume mixing ratios) and \( \overset{\delta}{D} \) in water vapor, Noone (2012) compiled a set of idealized process curves to describe how different tropospheric moisture processes are reflected in the \( \{\overset{2}{H}E, \overset{\delta}{D}\} \) phase space. In our work, we concentrate on the process curves that govern the isotopic variability in the Sahelian troposphere during the West African Monsoon, as summarized in Figure 1. This section provides the theoretical background for the individual process curves, for which model-based evidence will be given in the course of this study.

First, let’s assume that two air parcels with the specific moisture contents \( q_{0} \) and \( q_{1} \) and the isotopic compositions \( \overset{\delta}{D}_{0} \) and \( \overset{\delta}{D}_{1} \) mix without fractionation (i.e., no phase changes during the mixing). The mixed moisture composition \( q_{m} \) and \( \overset{\delta}{D}_{m} \) then result as follows:

\[
q_{m} = f q_{0} + (1-f) q_{1}
\]

\[
\overset{\delta}{D}_{m} = \frac{f q_{0} \overset{\delta}{D}_{0} + (1-f) q_{1} \overset{\delta}{D}_{1}}{q_{m}}
\]
with \( f \) indicating the relative contribution of the two air masses (Noone et al., 2011). Note that we use the subscript \( v \) for the vapor phase and \( c \) for the condensate throughout the paper. Later, we will distinguish between different categories of condensate, namely rain \((r)\), snow \((s)\), liquid \((l)\) and ice \((i)\) clouds. While \( q_v \) exhibits linear mixing, \( \delta D_c \) follows a hyperbolic curve, as the ratio between light and heavy isotopes is dominated by the moister air mass (Noone, 2012). The position of the hyperbolic curve in the \([H_2O, \delta D_c]\) diagram is determined by the isotopic composition of the moist and dry end members. For instance, Figure 1a shows the mixing curves for a dry mixing process, where the dry end member is located at very low H$_2$O and \( \delta D_c \) (orange curve), and for a moist mixing process with both end members \((x_1\) and \(x_2)\) being relatively moist (blue curve). The dry mixing curve is representative for air masses that originate from dry regions of the upper troposphere (mixing member \(x_2\)) and become more humid while they are subsiding into lower altitudes (mixing member \(x_1\)), whereas the moist mixing curve illustrates a near-surface moistening due to surface evaporation (see Sections 4.2 and 4.4.1).

Second, if microphysical processes induce a phase change of atmospheric water, fractionation between H$_2$O and HDO occurs. Since the HDO molecule has higher binding energies in the condensed phase than H$_2$O, the two isotopes have different water vapor pressures leading to equilibrium fractionation (Bigeleisen, 1961; Urey, 1947). Additionally, differences in molecular mass leads to non-equilibrium fractionation due to differing diffusivities. The former refers to a reversible isotope separation under thermodynamic equilibrium between a condensate (isotopic ratio \( R_c \)) and the ambient vapor (isotopic ratio \( R_v \)) according to the fractionation factor:

\[
\alpha_{eq,c} = \frac{R_c}{R_v}
\]  

The values for \( \alpha_{eq,c} \) vary with temperature as also the saturation vapor pressure does. They were determined for liquid and ice condensation during various laboratory studies (e.g., Horita & Wesolowski, 1994; Majoube, 1971; Merlivat & Nief, 1967). Non-equilibrium fractionation is assumed to occur in addition to equilibrium fractionation for processes that enforce a fast isotope flux between vapor and liquid, for instance when ventilated or unsaturated conditions prevail.

A simple framework for the isotopic fractionation in a precipitating air parcel is the Rayleigh distillation process (Dansgaard, 1964; Rayleigh, 1902). In this model, a moist adiabatic ascent is assumed with immediate removal of the condensate (Johnson et al., 2001). As soon as the dew point temperature is reached, condensation begins and condensate forms from ambient vapor under equilibrium conditions. While this process enriches the condensate with heavy isotopes, the ambient vapor gets depleted according to

\[
\ln \left( \frac{R_v}{R_{v,0}} \right) = (\alpha_{eq} - 1) \ln \left( \frac{q_v}{q_{v,0}} \right)
\]  

The conditions at the starting point of the ascent are defined by \( q_{v,0} \) and the isotopic ratio \( R_{v,0} \). For condensation above the frost point (263 K, according to Noone, 2012 and Ciais & Jouzel, 1994) the liquid fractionation factor (3) is used and at colder temperatures, the factor over ice is applied. A typical Rayleigh line for convective condensation over West Africa is shown in green in Figure 1b (see Sections 4.2 and 4.4.2).

If a liquid hydrometeor falls into unsaturated air, evaporation takes place and acts as a reversed distillation process (Bony et al., 2008). If the evaporated fraction of the rain drop is large, then this process has an enriching effect on the surrounding water vapor (e.g., Risi et al., 2021; Tremoy et al., 2014). In contrast, if the evaporated fraction is small (i.e., partial evaporation), this leads to a depletion in \( \delta D_c \), as lighter isotopes evaporate preferentially (Risi, Bony, & Vimeux, 2008; Lee & Fung, 2008; Noone, 2012). While enriching the rain water, the ambient vapor content increases due to the input of relatively more depleted evaporated rain water. If both partial rain evaporation and Rayleigh condensation occur at the same time, this leads to a drop to below the Rayleigh curve in the \([H_2O, \delta D_c]\) space (Dansgaard, 1964; Rozanski et al., 1992) and creates a so-called Super-Rayleigh signal, representing a Rayleigh process with an increased fractionation factor (Noone, 2012):

\[
\alpha > \alpha_{eq}
\]  

Starting at different positions on the Rayleigh curve, this creates the signals indicated by magenta lines in Figure 1b. According to Noone (2012), the Super-Rayleigh hypothesis excludes cases, where either the
evaporated fractions of the falling rain drops are large, such that the evaporative enrichment effects prevail, or where rain evaporation does not coincide with condensation processes. However, as will be shown in Sections 4.2 and 4.4.3, the chosen Super-Rayleigh curves in Figure 1b are useful to characterize the COSMOiso data and allow to identify effects of rain evaporation in mid-levels (4–6 km) and near-surface sub-cloud areas (0–1.5 km).

In saturated conditions \((RH = 100\%)\), equilibrium exchange of water molecules between vapor and liquid may affect their isotopic compositions, because saturation does not necessarily imply that an equilibrium between liquid and vapor is reached immediately for HDO as well. Particularly in the case of a fast process such as during the fall of a droplet, the isotope composition of the vapor can be altered by equilibrium exchange with the falling droplet. If an isotopic disequilibrium between the ambient air \((\delta D, \delta \text{D})\) and the rain drop \(\delta \text{Dr}E\) exists, an HDO flux works toward equilibrating both phases (Lawrence et al., 2004; Stewart, 1975). For instance, if rain drops with low \(\delta D\) fall through saturated areas with a relatively more enriched vapor, a net isotopic flux from the vapor to the condensate occurs, while \(\delta \text{Dr}E\) remains constant. This leads to a lowering of \(\delta \text{Dr}E\) at constant \(q_r\). A mathematical demonstration of the depleting effect of isotopic equilibration on \(\delta \text{Dr}\) due to the interaction with more depleted rain drops is given in Appendix A. Throughout this study we show that thereby \([\text{H}_2\text{O}, \delta \text{D}]\) signals develop that lie below the Rayleigh curve and correlate with the Super-Rayleigh curves computed for partial evaporation according to Noone (2012) (see magenta lines in Figure 1 and discussions in Section 4.4.3).

The disequilibrium between rain and vapor can be approximated as follows (e.g., Aemisegger et al., 2015; Graf et al., 2019; Tremoy et al., 2014):

\[
\delta D_{v,eq} = \delta D_v - \delta D_{v,eq} = \delta D_r - [\alpha_{\text{eq}}(\delta D_r + 1000) - 1000] \tag{6}
\]

\(\delta D_{v,eq}\) is the isotopic composition that the vapor would have if it were in isotopic equilibrium with the rain drop (subscript \(r\) stands for rain). In a saturated and equilibrated state, \(\delta D_{v,eq}\) tends toward 0\%, whereas partial rain evaporation (both equilibrium and non-equilibrium fractionation) generates a negative disequilibrium.

3. Data and Methods

In this section, we introduce the model data and trajectory tool that we use to calculate the backward trajectories for the Sahelian mid-troposphere during the WAM season 2016, and explain the process-attribution strategy.

3.1. The Isotope-Enabled Model COSMOiso

COSMOiso is the isotope-enabled version of the non-hydrostatic limited-area weather and climate model COSMO (Steppeler et al., 2003) and is documented in detail in Pfahl et al. (2012). As a regional model that is fed by boundary data from a global model, it efficiently enables simulations with high spatio-temporal resolutions at convective-resolving scales. It incorporates the fractionating processes of HDO and \(\text{H}_2\text{O}\) within its whole hydrological cycle (Pfahl et al., 2012). Fractionation is assumed whenever phase changes occur that involve the vapor phase. A one-moment microphysical scheme is used and the isotopic composition is calculated for water vapor, liquid and ice clouds as well as rain and snow. For this purpose, it includes the fractionation schemes of Stewart (1975) for rain evaporation and Jouzel and Merlivat (1984) for snow formation. Further, it uses the isotope-enabled multi-layer soil moisture scheme TERRAiso for fractionating soil evaporation and non-fractionating plant transpiration (Christner et al., 2018). Fractionation during ocean evaporation is represented by the Craig-Gordon-model (Craig & Gordon, 1965).

Here we use data from a COSMOiso simulation with a focus on West Africa during the WAM season 2016. The simulation period is chosen to match the DACCIWA campaign (01 June–31 July 2016, Knippertz et al., 2017) and the model output frequency was set to 1 hr. Data provided by the global isotope-enabled model ECHAM5iso (Wernert et al., 2011) are used as initial and boundary data as well as for a spectral nudging of the horizontal wind fields above 850 hPa. This serves to keep the meteorology close to reality, as the ECHAM5iso simulation was nudged to ERA-interim reanalyses provided by the European Center for Medium Range Weather Forecasts (ECMWF). The model domain of the COSMOiso simulation is chosen such
2020 is a non-precipitating scheme of 2020 per time step on average), the trajectory is assumed to be non-precipitating. An individual 3.1 (corresponding to 1.18 2013), the trajectory data point is classified as precipitating, if the specific content (Nieto et al., 2016). Further, a trajectory will be classified as precipitating, if the rain content per time step on average). Analogously, if the summed up rain content is lower than 0.2 g/kg (corresponding to 1.18 10^{-3}gkg^{-1} per time step on average), the trajectory is assumed to be non-precipitating. An individual trajectory data point is classified as precipitating, if the specific content (q_r for rain, q_s for snow) is at least 10^{-3}g

that it covers the dominant moisture source regions of the WAM (see Figure 2). The model configuration has 40 vertical hybrid levels between the surface and 22.7 km and a horizontal grid spacing of 14 km (similar to the horizontal pixel size of Metop/IASI data, Diekmann et al., 2021). Vergara-Temprado et al. (2020) stated that for a horizontal grid spacing below 25 km switching off the convection parameterization, such that convection is explicitly simulated by the dynamical core of the model and the convective precipitation is determined by the microphysical scheme, leads to overall better results than increasing the horizontal resolution. Specifically when simulating the WAM, various studies reported significant improvements when using explicit convection (Berthou et al., 2019; Crook et al., 2019; Marsham et al., 2013; Martínez & Chaboureau, 2018; Maurer et al., 2017; Pante & Knippertz, 2019). Additionally, the shallow convection parameterization in COSMO is a non-precipitating scheme (similar to most shallow convection schemes) and does currently not include the water isotope physics. Therefore we decided not to use a parameterization for deep and shallow convection despite the relatively coarse grid spacing of 14 km, with the aim to have as few as possible non-resolved processes influencing the isotope and water budget.

3.2. The Trajectory Tool LAGRANTO

LAGRANTO is a Lagrangian analysis tool that allows calculating backward and forward air trajectories based on 3D wind fields and tracing physical variables along individual trajectories by interpolating model fields onto the trajectory path (Sprenger & Wernli, 2015; Wernli & Davies, 1997). Using the COSMO data from Section 3.1 as input, we calculate backward trajectories starting from the Sahelian mid-troposphere during the WAM season 2016. In accordance with the typical residence time of atmospheric water the trajectory length is set to 7 days (Sodemann, 2020). This implies that each trajectory contains 169 time steps, that is, one initialization step plus 24 time integration steps per day. Trajectories are started daily at 09 and 21 UTC from 08 June to 30 July 2016, at 575 and 625 hPa (corresponding to around 4.8 and 4.1 km) and for approximately every 1° within the domain from 13°–17°N, 8°W–8°E (see Figure 2). If in the following not explicitly mentioned, all trajectories from both starting altitudes and both starting times are analyzed. In total, this results in 12,720 trajectories. In addition to various meteorological variables, we trace the specific contents q_r of H_2O and HDO in vapor, sedimenting (rain and snow) and non-sedimenting condensates (liquid and ice clouds). As the trajectory setup is chosen with respect to the characteristics of the remotely sensed [H_2O, δD] data from Metop/IASI (peak of vertical sensitivity smoothed around 600 hPa, local overpass times around 09.30 and 21.30, results given as volume mixing ratios; see Diekmann et al., 2021), we convert q_r for H_2O and HDO into volume mixing ratios (ppmv) and calculate δD, along each trajectory. We will refer to the starting point (first calculation step, day 0) as the target time and to the last calculation step (day –7) as the trajectory origin.

3.3. Trajectory Sorting

For a meaningful interpretation of the full ensemble of 12,720 trajectories, the trajectories will be sorted according to geographical and meteorological criteria along their atmospheric pathways. By considering the geographical position and altitude of the trajectory origins, we aim to build clusters that represent the dominant transport patterns of the WAM (Niang et al., 2020). As transport is an important control factor for atmospheric moisture, such a dynamical clustering will give a useful first overview of the characteristic moisture evolution of the defined clusters (Nieto et al., 2006; Salih et al., 2015; Sy et al., 2018).

Further, a trajectory will be classified as precipitating, if the rain content q_r summed up over all 169 time steps of a trajectory pathway exceeds the arbitrarily chosen threshold of 2 g/kg (corresponding to 1.18 10^{-2}gkg^{-1} per time step on average). Analogously, if the summed up rain content is lower than 0.2 g/kg (corresponding to 1.18 10^{-3}gkg^{-1} per time step on average), the trajectory is assumed to be non-precipitating. An individual trajectory data point is classified as precipitating, if the specific content (q_r for rain, q_s for snow) is at least 10^{-3}g.
kg$^{-1}$. If both $q_r$ and $q_t$ fulfill this criterion, this precipitation is viewed as mixed-phase. Following the moisture source attribution of Sodemann et al. (2008), we attribute a moisture uptake along a trajectory to surface evaporation if the corresponding trajectory altitude $z_{bl}$ is below the boundary layer height $z_{bl}$. As models tend to underestimate the boundary layer height, Sodemann et al. (2008) recommended for this purpose a scaling of $z_{bl}$ with a factor of 1.5.

3.4. Trajectory-Based Process Attribution of $\{\text{H}_2\text{O}, \delta\text{D}\}$ Pairs

The aim of this work is to establish a framework for interpreting the isotopic composition in a region of interest with regard to moist processes occurring during the transport of air masses arriving in this region. For this purpose, we develop a process attribution procedure by considering temporal changes not only in $\text{H}_2\text{O}$ (as performed in Dütsch et al., 2018), but also in $\delta\text{D}$, thereby making use of the additional isotope information. The general concept behind our Lagrangian process attribution procedure is the following:

1. Definition of processes of interest that shall be identified in the $\{\text{H}_2\text{O}, \delta\text{D}\}$ phase space
2. Categorization of trajectories or individual segments along trajectories that correspond to the processes of interest
3. Interpretation of the isotopic composition in the region of interest by means of the categorized trajectories

We will use the idealized process curves of Figure 1 describing effects of air mass mixing, Rayleigh condensation, and Super-Rayleigh signals as the processes of interest (step 1). To illustrate the plausibility of those curves, we will first evaluate them against the isotopic evolution along three characteristic example trajectories. Then, following Section 3.3, we sort the trajectories into dominant transport patterns and evaluate their $\{\text{H}_2\text{O}, \delta\text{D}\}$ signals in order to link segments of trajectories to the proposed process curves (step 2). In turn, this provides statistical information of the relative process occurrence frequencies within the full trajectory ensemble, which eventually facilitates an improved interpretation of the isotopic composition in the target region and the atmospheric processes that determine this composition (step 3).

4. Lagrangian Analysis of the Sahelian Troposphere

In this section, we apply the proposed Lagrangian process attribution procedure to $\{\text{H}_2\text{O}, \delta\text{D}\}$ pair distributions in the Sahelian troposphere during the WAM 2016. We refer to the terminology of Knippertz et al. (2017), where the early monsoon period in 2016 was classified based on the difference of averaged precipitation between the Sahel and the Guinean coastal zone. During the pre-onset stage (Phase 1, 01–21 June 2016) the rainfall maximum lied over the Guinea Coast. The shift to the Sahel initiated the post-onset phase (Phase 2, 22 June–20 July 2016). In Phase 3 (21–26 July 2016) an unusual westerly regime formed and caused widespread precipitation over large parts of West Africa, while the circulation returned to undisturbed monsoon conditions in Phase 4 (27–31 July 2016). As both Phases 3 and 4 consist only of a few days, we merge them in the following in order to obtain a reasonable data ensemble size.

4.1. Average $\{\text{H}_2\text{O}, \delta\text{D}\}$ Development Along the West African Monsoon

Figure 3 emphasizes the added value of $\delta\text{D}$ compared to traditional humidity measures. It shows the average $\{\text{H}_2\text{O}, \delta\text{D}\}$ behavior over the Sahel at 600 hPa during the three monsoon stages, as given by the COSMO$_{uc}$ grid point values in the considered domain. The $\{\text{H}_2\text{O}, \delta\text{D}\}$ pair data are summarized by normalized two-dimensional histogram contours (calculated according to Eckstein et al., 2018).

While $\text{H}_2\text{O}$ remains within a similar data range throughout the whole period, $\delta\text{D}$ reveals a change with time. In particular, the development of the monsoon circulation in Phase 2 coincides with a shift of $\delta\text{D}$ toward markedly lower values. The very wet Phases 3 and 4 show a shift to higher moisture content and lower $\delta\text{D}$ with respect to Phase 2. Therefore, this figure suggests that there may be moist processes whose effects can be observed more clearly in the paired $\{\text{H}_2\text{O}, \delta\text{D}\}$ phase space than in individual $\text{H}_2\text{O}$ distributions. In this context, the backward trajectories serve to understand the mechanisms controlling the $\{\text{H}_2\text{O}, \delta\text{D}\}$ variability, as they shed light on the history of the air masses arriving at the target region.
4.2. Isotopic Process Attribution Along Single Trajectories

As a first step of the Lagrangian process analysis, we choose three individual trajectories from the full trajectory ensemble, each representing specific rain conditions: T1 as non-precipitating trajectory, T2 as trajectory with the summed up $q_r$ between 0.2 and 2 gkg$^{-1}$ and T3 as precipitating trajectory (see Section 3.3). We analyze their [$H_2O$, $\delta D_v$] evolution to demonstrate how the idealized process curves from Figure 1 can be interpreted for individual air parcels. The target dates of T1, T2 and T3 are 09 UTC 05 July, 21 UTC 23 June and 09 UTC July 19, 2016. Figure 4 provides an overview of the properties of the chosen trajectories. The dominant mixing and microphysical processes along the trajectories are identified according to the temporal evolution of [$H_2O$, $\delta D_v$] pairs and depending on the occurrence of hydrometeors. Arrows and markers illustrate the corresponding temporal evolutions in the [$H_2O$, $\delta D_v$] phase space.

The first trajectory T1 does not show any significant precipitation along its pathway. It starts with a relatively dry signature at around 2.5 km above the Mediterranean Sea near Sicily (Point 1) and then crosses the Libyan coast (Point 2, Figure 4a). During this time the trajectory moistens and enriches due to ocean evaporation. Therefore, in Figure 4d the [$H_2O$, $\delta D_v$] pairs follow the moist mixing line according to the blue arrow from marker 1 to 2. After this, dehydration sets in over the dry North African desert areas. At 30°N, T1 experiences a strong lifting to 4 km, probably as result of the interaction of the SHL and the local topography of the Haggard mountains (surface altitudes up to 2 km, see Figure 2), where it mixes with dryer mid-tropospheric air and moves southwestward (see marker “x” in Figure 4a). As a consequence, precipitation forms and depletes the trajectory of its heavy isotopes in the vapor phase following a clear Rayleigh signature (green arrow from 2 to 3 in Figure 4e). Thereafter, the air parcel appears to leave the convective cell and weak mixing with drier surrounding air occurs (orange arrow, from 3 to 4).

T2 (middle column in Figure 4) represents a trajectory with both strong mixing and precipitating effects. It originates in the lower troposphere ($z_{ns} \sim 3$ km) over the Gulf of Guinea and exhibits moistening and enrichment, while subsiding below 1 km and taking course toward the Guinea Coast. This moistening is associated with surface evaporation, while the trajectory penetrates into the boundary layer (Figure 4h). This leads to an enrichment following the moist mixing line (see blue arrow from marker 1 to 2, in Figure 4e) and results in higher moisture contents than for T1. Over the Sahel, a local convection event (see precipitation patterns in Figure 4b) lifts the trajectory abruptly from ~1–6 km altitude (see marker “x” in Figure 4b). As a consequence, precipitation forms and depletes the trajectory of its heavy isotopes in the vapor phase following a clear Rayleigh signature (green arrow from 2 to 3 in Figure 4e). Thereafter, the air parcel appears to leave the convective cell and weak mixing with drier surrounding air occurs (orange arrow, from 3 to 4).
leading to a less steep evolution than a pure Rayleigh process would imply. From 4 to 5, a slight moistening due to mixing appears (blue arrow), as the trajectory subsides down to \( \approx 4.5 \) km.

For the third, precipitating trajectory T3 (right column in Figure 4) the starting point is already associated with very moist and isotopically enriched conditions, as it is located near the surface of the tropical Atlantic \( \approx 200 \text{ m} \) and is therefore strongly affected by surface evaporation over the relatively warm waters southwest of West Africa. After reaching the West African land mass, the trajectory crosses a westward propagating squall line (see precipitation patterns and marker “x” in Figure 4c). Large rain drops fall through the air parcel, while the air parcel remains constantly at an altitude in the range of 1–2 km, hence without being lifted by convection. This suggests that this rain formed at higher altitudes and fell from

Figure 4. Overview of the trajectories T1, T2, and T3. (a–c) show the geometrical pathways, color-coded with altitude. The black framed circle marks the trajectory origin. The black shades indicate areas with a rainfall >2 mm hr\(^{-1}\) during the trajectory step marked with x. (d–f) show the evolution in the \( [\text{H}_2\text{O}, \delta\text{D}] \) phase space. The main variations between characteristic signals (marked with numbers) are illustrated with arrows (arrow colors according to Figure 1). (f–h) show the time series of the altitude \( (z_{\text{tra}}) \), boundary layer height \( (z_{\text{bl}}) \), rain \( (q_r) \) and snow content \( (q_s) \), \( \text{H}_2\text{O} \) and \( \delta\text{D} \) along the respective trajectory.
above into the considered air parcel. While H$_2$O decreases slightly, but still remains high during this event, $\delta$D$_2$ shows a sharp drop by more than 50 ‰ (Figure 4f, magenta arrow from marker 1 to 2). This depletion is stronger than would be predicted using the Rayleigh model and thus penetrates into the Super-Rayleigh regime. The hypothesis is that these depleted and slightly drier trajectory data are a result of an isotopically processed cold pool associated with the squall line marked by "$x$" in Figure 4c. Afterward, along its northeastward path over the Sahel, the trajectory enriches, likely due to surface evapotranspiration (blue arrow from 2 to 3), until it finally interacts with a second squall line and exhibits once again an isotopic pull toward the Super-Rayleigh regime (magenta arrow from 3 to 4). However, at this time the air parcel is lifted to 4 km and changes its flow direction by 180°, consistent with the easterly wind component of the AEJ and the southwestward propagation of the observed squall line. A subsequent enrichment (blue arrow from 4 to 5) defines the isotopic composition for the injection into a further convective updraft, which is part of the southwestward propagated squall line system observed at the trajectory points 3 and 4 and where the occurrence of snow particles (Figure 4i) is accompanied by Super-Rayleigh signals (magenta arrow from 5 to 6).

In summary, the analysis of the selected trajectories reveals that, by using the theoretical process curves from Figure 1, the temporal evolution of [H$_2$O, $\delta$D$_2$] pairs along air parcels can be divided into moist and dry mixing, drying and depletion due to Rayleigh condensation, and processes that deplete the vapor beyond the prediction by the Rayleigh model. Only by considering the whole isotopic history of an air parcel, it is possible to fully explain its target position in the [H$_2$O, $\delta$D$_2$] phase space.

4.3. Identification of Dominant Transport Patterns

In the next step, the aim is to test the usefulness of the idealized process curves for interpreting larger trajectory ensembles during the monsoon period 2016. Therefore, as discussed in Section 3.4, we first sort the full ensemble of 12,720 trajectories into meteorologically meaningful clusters of trajectories that experience a similar moisture history. Taking into account the characteristic regions of the trajectory origins as well as the relative position of origin altitude against target altitude, we roughly distinguish between rising (R1 to R3) and subsiding (S1 and S2) transport clusters (see Section 3.3). Their main averaged properties (see Figures 5 and 6) are briefly characterized:

R1. This cluster represents the southerly monsoon inflow (dark red trajectories in Figure 5), originating from the lower troposphere over the Gulf of Guinea with high contents of H$_2$O and $\delta$D$_2$ (see Figures 6c and 6d). It advances on an anticyclonic path toward the Sahel, where it is lifted into the middle troposphere due to moist convection (see Figure 6a; Marsham et al., 2013). This ascent into colder and dryer regions is associated with intense precipitation (Figures 6e and 6f), leading to a strong depletion in $\delta$D$_2$ (Figure 6d).

R2. The orange trajectories in Figure 5 indicate the subtropical Atlantic low-level inflow with the trade winds that get deflected eastward toward the Sahel as a response to the Saharan heat low (Lavaysse et al., 2009; Nieto et al., 2006). Its initial moisture is lower than for R1, but increases during the transport over the Atlantic (Figures 6c and 6d). Similar to R1, it experiences a convective lifting over the Sahel (Figure 6a), but ends up with more enriched $\delta$D$_2$.

R3. The trajectories in yellow (Figure 5) originate in the lower troposphere over the Mediterranean Sea and follow the Etesian winds toward the African continent (Tyrulis & Lelieveld, 2013). Over North Africa, this cluster moves along the eastern side of the Atlas mountains and then feeds the relatively dry Harmattan (Hall & Peyrillé, 2006). As the surface evaporation over North Africa is small, there is hardly any change in moisture (Figure 6c) as well as no significant contribution to the Sahelian precipitation (Figures 6e and 6f). At the target location, it shows $\delta$D$_2$ values similar to R2 (Figure 6d).

S1. The African Easterly Jet inflow is represented by the dark blue trajectories (Figure 5). It is characterized by a low-latitude easterly flow that transports dry air masses from the upper troposphere (Figure 6a) from East Africa down to the Sahelian mid-troposphere (Cook, 1999; Sy et al., 2018). Through deep tropical convection, frozen precipitation falls into the AEJ (Figure 6f). During its subsiding path into moister tropospheric regions, H$_2$O and $\delta$D$_2$ increase and converge toward the values of R1 (Figures 6c and 6d).

S2. The cyan trajectory ensemble in Figure 5 describes extratropical mid-level dry intrusions, which feed into the anticyclonic circulation above the Saharan surface heat low (Cook, 1999; Lavaysse et al., 2009).
As this flow originates from the mid-latitude upper troposphere, it reveals very low moisture contents (Roca et al., 2005), even lower than for S1 (Figures 6c and 6d). During its subsiding transition toward the Sahel (Figure 6a), moistening and enrichment takes place. Several studies have documented similar abundances of relatively high moisture contents over Saharan regions (González et al., 2016; Schneider et al., 2016), where moisture advected from adjacent sea basins (e.g., North Atlantic and Mediterranean Sea) converges at low levels (Dahinden et al., 2021). This moist air is then lifted by dry convection during the day in the SHL and thereby moistens S2 (Figure 6b). At its target position, the $\delta D_{vE}$ of S2 resembles the values of the rising extratropical clusters (R2 and R3).

Figure 7a shows the relative contributions of each transport cluster to the target region as a function of time. The clusters represent together up to 90% of the air transported into the Sahelian mid-troposphere. The unclassified trajectories mainly originate above the West African continent with no characteristic large-scale transport. Even though the relative contribution of the monsoon inflow (R1) is comparably low in terms of number of trajectories (<10%), it is nonetheless the major driver of precipitation for the Sahel during the post-onset stage (Phase 2, e.g., compared to R2 in Figure 7b). The pre-onset Phase 1 shows marked fluctuations associated with synoptic-scale disturbances described in Knippertz et al. (2017), leading to single rainfall events during June (e.g., Maranan et al., 2019). As the monsoon has not fully developed yet, the fraction of trajectories from the subtropical Atlantic (R2) is higher than in the other Phases (Figure 7a). The actual monsoon onset is characterized by a breakdown and then re-establishment of the AEJ as indicated by the dark blue trajectories S1. The fraction of monsoon trajectories in Phase 2 clearly increases compared to Phase 1 and precipitation events are now more frequent (Figure 7b). Finally, the unusual flow situation during Phase 3 (and to a lesser extent Phase 4) is reflected in a clear shift of the fractions of transport clusters.
Figure 6. Averaged time series for the transport clusters R1 (dark red), R2 (orange), R3 (yellow), S1 (dark blue) and S2 (cyan). Shown are (a) the trajectory altitude, (b) boundary layer height ($1.5 z_0$), (c) $H_2O$, (d) $\delta D$, (e) rain content $q_r$, and (f) snow content $q_s$. For (e and f), a running mean over 6 time steps is used. To underline the daily cycles, in particular for the boundary layer height, only the trajectories with the same starting time of 09 UTC at the Sahelian mid-troposphere are herein considered.

Figure 7. Time series of (a) the relative contribution of each transport cluster to the total amount of trajectories arriving every 12 hr in the target region in the Sahelian free troposphere. The monsoon stages described in Knippertz et al. (2017) are separated by dashed lines. (b) Rain water content accumulated along the last 12 hr of each trajectory before arriving in the target region and averaged over each cluster.
Extratropical intrusions almost disappear entirely with a surge in AEJ inflow. The monsoon inflow, which causes marked precipitation events, increases at the expense of the Harmattan inflow.

In summary, the trajectory clustering according to their source regions reflects well the major transport contributions for the Sahelian troposphere during the monsoon season 2016. The clusters separate the trajectories into rising and subsiding transport patterns that bring moist and dry air masses to West Africa from different regions.

4.4. Isotopic Process Attribution Along Transport Clusters

In this section, we investigate the importance of different processes along the transport clusters presented in Section 4.3. We address the question to which extent and for which meteorological conditions the mixing, Rayleigh, and Super-Rayleigh process curves from Figure 1 are useful to explain the isotopic signals along the transport clusters. As these clusters are most representative during the active monsoon (see Figure 7), we focus in the following on trajectories during the post-onset stage (Phase 2).

4.4.1. Importance of Mixing Processes

As discussed in Section 4.2, air mass mixing plays a crucial role for the isotopic evolution along a trajectory, in particular if no rain processes occur. Therefore, to extract pure mixing effects in the $\{\delta^{2}H, \deltaD\}$ phase space, we select all non-precipitating trajectories (see Section 3.3).

Figure 8 shows the $\{\delta^{2}H, \deltaD\}$ pair data along the non-precipitating trajectories for each transport cluster. Even though the rising clusters R1 and R2 show on average strong occurrences of precipitation along their pathways (see Figure 6e), still non-precipitating trajectories appear for both (7% and 56%). The non-precipitating trajectories of R1, R2, and R3 show clear isotopic signals toward the moist mixing line. Moisture uptake from ocean evaporation and continental evapotranspiration represents a very moist mixing member and is opposed to the relatively dry conditions in the free troposphere. For instance, the non-precipitating trajectories in the monsoon cluster R1 (only 7%) start with very moist and enriched values above the Gulf of Guinea and subsequently mix with the drier and more depleted mid-tropospheric air masses while they...
advance over West Africa. Similar mixing structures are apparent for the Atlantic inflow (R2) and the Harmattan (R3), with substantially larger numbers of non-precipitating trajectories (56% and 84%, respectively). As their initial moisture is much more variable than for R1, both moistening and drying occurs along the non-precipitating trajectories of the R2 and R3, closely following the moist mixing curve.

For the subsiding clusters S1 (AEJ) and S2 (extratropical intrusions), the non-precipitating trajectories are predominant (∼90%). As they typically originate in the upper troposphere, their starting points constitute very dry and depleted end members, while in this case the mid-tropospheric air masses act as moister end members. Thus, during the subsidence of S1 and S2 strong signals along the dry mixing curve develop, until the moisture approaches values similar to the target moisture of the rising trajectories.

In summary, even though the non-precipitating trajectories of the rising and subsiding transport clusters start with significantly different isotopic signals, mixing homogenizes to first order their \(\{^{2}H, \delta D\}_v\) pairs when arriving over the Sahel. Dehydration and moistening along the respective trajectories is well described by the theoretical moist and dry mixing curves.

### 4.4.2. Importance of Rayleigh Processes

To identify Rayleigh processes along the transport clusters, we now focus on the precipitating trajectories (see Section 3.3). Here, we consider only the transport clusters R1 and R2, because only these two clusters include trajectories that exhibit a significant rain amount and therefore fulfill the rain criterion (see Figure 7b).

In addition to signatures along the moist mixing curve, a clear Rayleigh signal is evident for both clusters (see Figure 9). In particular during the last 24 hr before arrival, when the convection peaks, the \(\{^{2}H, \delta D\}_v\) pairs are distributed along the theoretical Rayleigh curve and indicate a depletion that cannot be explained with the mixing curves alone. Additionally, also values appear below the Rayleigh curve. Either this is due to further Rayleigh processes with initial conditions that lead to Rayleigh curves that are shifted toward lower \(\delta D\) values (which is rather unlikely, since the plotted Rayleigh curve is already chosen for relatively high surface temperature and relative humidity, see Figure 1), or there are processes that lead to an enhanced depletion and create signals in the Super-Rayleigh area, as documented for trajectory T3 in Section 4.2.

### 4.4.3. Importance of Super-Rayleigh Processes

This section sheds light upon the Super-Rayleigh signatures in the \(\{^{2}H, \delta D\}_v\) pair distributions that develop during the precipitating ascent of the monsoon flow (R1) into the Sahelian mid-troposphere.

For this purpose, we take the precipitating trajectories of R1 and further classify the precipitating points of the corresponding trajectories based on the altitude and phase of the precipitation. Following the precipitation thresholds of Section 3.3, a distinction is made for frozen \(q_f\), mixed-phase \(q_m\) and \(q_f\), and mid- and low-level liquid \(q_l\) precipitation. The respective altitude ranges are shown in Figure 10. While the low-level liquid class represents the near-surface and mostly sub-cloud rain, the other precipitation classes can go along with liquid or frozen clouds (Figure 10c). Further, we distinguish between saturated (\(RH \geq 99\%\))
and unsaturated (RH ≤ 90%) conditions of the ambient vapor (Figures 11a–11d). In line with the saturation adjustment of COSMOiso, the unsaturated data points are cloud-free (near-cloud points may exhibit minor cloud contents due to the 3D interpolation when tracing $c_{eq}$ and $i_{eq}$ along the trajectories).

Figures 11a and 11e depict the trajectory points with frozen precipitation $s_{eq}$, with only few corresponding data points appearing within the chosen axis range of the $\{2H E, \delta D\}$ plot. These snow particles are assumed to have formed at high altitudes, for instance within the deep convective parts of MCSs, and fall through the trajectories on their way down. As sublimation is assumed not to fractionate, the isotopic composition of the ambient vapor gathers around the Rayleigh condensation curve with no significant Super-Rayleigh signals.

If these snow particles fall into the melting zone, where the air temperature is around ~0°C, an area of mixed-phase precipitation develops (Figures 11b and 11f). The melting process itself is non-fractionating, but it initiates fractionating interactions between the newly formed liquid drops and the ambient vapor. The contours in the $\{2H E, \delta D\}$ phase space reveal that for both saturated and unsaturated conditions Super-Rayleigh signatures appear. Even in saturated conditions an isotopic flux can occur and equilibrate the

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**Figure 10.** Classification of precipitating segments along the precipitating trajectories of R1. (a) Shows snow content $s_{eq}$ plotted against the trajectory altitude and (b) the respective rain content $r_{eq}$. The dark gray scatter indicate the data points, where the respective precipitation content exceeds $10^{-5}$ g kg$^{-1}$. In (c), liquid and frozen cloud water contents are plotted against trajectory altitude.

**Figure 11.** $\{2H E, \delta D\}$ pair distributions of water vapor for the different classes of precipitating segments within the transport cluster R1, further separated according to relative humidity. (a–d) relative humidity against trajectory altitude with black (golden) dots indicating saturated (unsaturated) conditions. The gray dots show all data points within R1. (e–h) display the contours that summarize 95% of the $\{2H E, \delta D\}$ pair data of the ambient water vapor for the saturated (black) and unsaturated (golden) points in the different precipitation classes.
rain drops with the ambient vapor. In case of sub-saturation, rain evaporation can take place. Both effects have the potential to further deplete the water vapor (see Section 2) and may thus explain the depleted Super-Rayleigh signatures inside the melting zone.

During the sedimentation of the liquid drops through a convective system, the Super-Rayleigh signatures are less pronounced for the saturated trajectory points, but still remarkable for unsaturated and cloud-free conditions (Figures 11c and 11g). This depletion results, for instance, from rain evaporation in the unsaturated area below the stratiform cloud shield of a squall line.

Figures 11d and 11h show the trajectory points, where rain drops occur near the surface and below the convective cloud base. Here, the air parcels are mostly unsaturated and indicate sharp tendencies toward the Super-Rayleigh area. In agreement with Risi, Bony, and Vimeux (2008), this hints toward effects of subcloud rain evaporation in unsaturated downdrafts.

To further improve the distinction between contributions of rain evaporation and isotopic equilibration, we analyze the degree of isotopic disequilibrium \( \delta D_{\text{v,deq}} \) between the vapor and the liquid condensate (see Equation 6). Figures 12a–12c show the distribution of \( \delta D_{\text{v,deq}} \) in the \([\text{H}_2\text{O}, \delta D_{\text{v}}]\) phase space for all precipitating trajectory points of the precipitation classes from Figure 10 with liquid hydrometeors. Even though the \([\text{H}_2\text{O}, \delta D_{\text{v}}]\) pair distributions for negative, low, and positive disequilibrium are highly similar (Figures 12a–12c), the corresponding histograms of \( \delta D_{\text{v,deq}} \) show fundamental differences (Figures 12d–12f).

In the melting zone, we observe a strong imbalance toward positive values of \( \delta D_{\text{v,deq}} \) that is, the vapor in equilibrium with the rain drops would be more depleted than the actual vapor (Figure 12d). These rain drops have formed from melting snow and therefore reflect the isotopic composition at the condensation altitudes of the snow particles. Within deep convective systems, condensation can occur up to the tropopause level, imprinting highly depleted signatures on the precipitation (e.g., Celle-Jeanton et al., 2004; Lawrence & Gedzelman, 1996; Lawrence et al., 2004; Lee & Fung, 2008; Risi, Bony, & Vimeux, 2008). If saturated conditions prevail at lower altitudes, the fall of this precipitation with low \( \delta D_{\text{v}} \) through a region with relatively higher \( \delta D_{\text{v}} \) induces an equilibrating isotopic flux from the vapor to rain. This decreases \( \delta D_{\text{v}} \), while \( \text{H}_2\text{O} \) remains constant, contributing to the development of Super-Rayleigh signals within the melting zone (Figure 12a). With decreasing height, the histogram of \( \delta D_{\text{v,deq}} \) shifts to lower values (Figure 12e).
while equilibration and rain evaporation proceed and reduce the grade of disequilibrium (see Section 2). Eventually, in the sub-cloud zone the imbalance in $\delta_{D_{v\text{-eq}}}$ changes sign (Figure 12f), featuring equilibrium vapor from precipitation with a higher $\delta D$ than the sub-cloud vapor. As here unsaturated conditions prevail (Figures 11h), rain evaporation is strongly enhanced, leading to an enrichment of heavy isotopes in the rain drops and as a consequence to negative $\delta_{D_{v\text{-eq}}}$.

Figures 11 and 12 reveal another interesting feature with more enriched values toward the mixing curves (at around $-150\%$). In particular for the mid-level liquid precipitation, a clear mixing signal stands out that correlates with sub-saturation (Figures 11g) and negative disequilibrium (Figure 12b). We suspect that this feature is a result of synoptic-scale intrusions that transport dry and depleted air masses as rear-to-front flow into a convective system (Kurita, 2013).

In summary, to account for the Super-Rayleigh signals in water vapor in the presence of precipitation, it is not sufficient to think of an isolated process but rather to consider the full interaction of microphysical processes that occur within and around a convective cell. The depletion due to Rayleigh condensation during the convective updraft is superposed by additional depleting contributions of evaporation and equilibration of the falling rain drops. However, the two Super-Rayleigh lines marked in the $\{H_2O, \delta D_{v}\}$ phase space constitute rough bounds for the Super-Rayleigh area, as they frame the altitude range, where interactions between vapor and liquid precipitation can occur (from the melting zone to the surface).

### 4.5. Understanding $\{H_2O, \delta D_{v}\}$ Pair Distributions Over the Target Region

In the discussion of Figure 3 we have already noted that COSMO$_{iso}$ simulates markedly different isotopic distributions in the Sahelian free troposphere during the three monsoon phases documented in Knippertz et al. (2017) (see Section 4.1). By combining the attributed signals in the $\{H_2O, \delta D_{v}\}$ phase space along the transport clusters, we can now examine to which extent mixing and microphysical processes along the trajectory pathways explain the temporal evolution of the $\{H_2O, \delta D_{v}\}$ distributions in the target region, that is, the Sahelian free troposphere. To this end, Figure 13 shows the same two-dimensional histogram contours for $\{H_2O, \delta D_{v}\}$ pairs as in Figure 3 but now separated by the trajectory transport cluster. In other words, Figure 13 includes the data of each transport cluster at the corresponding trajectory starting points over the target region Sahel, whereas Figure 3 refers to the grid point data of COSMO$_{iso}$ over the Sahel. As a reference, results for the five transport clusters combined are also provided (Figures 13g–13i).

A direct comparison to Figure 3 reveals that the $\{H_2O, \delta D_{v}\}$ pairs of the full trajectory ensemble in the target region (Figure 13) are in line with the full COSMO$_{iso}$ grid point values (Figures 13g–13i). During the pre-onset stage (Phase 1) the $\{H_2O, \delta D_{v}\}$ distribution is governed by (mostly dry) mixing processes between moister and drier air masses that converge along the ITD. After the monsoon onset (Phase 2), convective processes (i.e., condensation, evaporation, and diffusive equilibration of rain drops) prevail and lead to a strong shift of $\delta D_{v}$ toward the Rayleigh and Super-Rayleigh areas. This shift can temporally be enhanced during particularly wet monsoon periods (Phase 3 and 4). As the contours of the full trajectory ensemble result from contributions of each transport cluster (Figure 7), their individual inspection allows for further disentangling the isotopic variability during the monsoon.

During the pre-onset stage (Phase 1; left column in Figure 13) all clusters reveal robust and similar isotopic signals along the mixing curves. Despite the significantly different mixing history of the rising (R1, R2 and R3) and the subsiding (S1 and S2) clusters, two-way mixing harmonizes their $\{H_2O, \delta D_{v}\}$ pairs in the Sahelian troposphere. Only within the monsoon inflow (R1, red contours) occasional convective events create departures from the mixing curves toward the Rayleigh and Super-Rayleigh lines. The dominating extratropical intrusion cluster S2 (cyan contours, 1079 trajectories) agrees well with R2 and R3 but with a tendency toward drier and more depleted air. In contrast, the AEJ cluster S1 (dark blue contours) shows mild indications of both mixing along the dry mixing line and toward the Rayleigh and Super-Rayleigh area. Consequently, the contours for all trajectories combined are dominated by mixing along the moist mixing curve.

With the transition to the post-onset stage (Phase 2; middle column in Figure 13), the frequent convection over the Sahel causes a general shift from relatively enriched air toward lower $\delta D_{v}$, while $H_2O$ remains high. The condensation processes associated with the monsoon convection pushes the $\{H_2O, \delta D_{v}\}$
pair distributions of R1 and R2 toward the Rayleigh line. Additionally, the increased convection enhances effects such as diffusive equilibration and partial rain evaporation. Since we here consider data in the free troposphere, that is, in the melting zone of falling snow particles, strong isotopic signals develop for R1 and R2 toward the lower Super-Rayleigh line. Because of the strong relation of monsoon precipitation with the air masses transported by the AEJ (Niang et al., 2020; Sy et al., 2018), the isotopic composition of cluster S1 merges with the signals of R1. By contrast, the northwesterly subtropical clusters R3 (Harmattan) and S2 (extratropical mid-level dry intrusions) remain around the mixing curves with only slight tendencies toward the Rayleigh curve. This emphasizes the existence of a subtropical mixing barrier that hinders the isotopic exchange between subtropical and tropical transport clusters as discussed in Yang and Pierrehumbert (1994) and Niang et al. (2020). The resulting contrast between the effects of mixing and microphysical processes are well represented in the contours of the full ensemble.

Finally, in the unusually wet Phases 3 and 4 (right column in Figure 13) the Sahelian free troposphere remains overall moist, but also becomes even more isotopically depleted. The monsoon inflow (R1) and the AEJ inflow (S1) further drop to lower $\delta D$, as convective processes increase and foster Rayleigh and Super-Rayleigh signatures. During this period convection is so widespread that also the sub-tropical clusters R3 and S2 show indications of reduced mixing and increased Rayleigh signals. As already shown in Figure 7, the low-level Atlantic inflow cluster R2 is not present during these phases (Knippertz et al., 2017). The isotopic composition of all trajectories clearly reflects the shift from the mixing to the Rayleigh line with a marked extension toward the Super-Rayleigh area.

To summarize, the comparison of the $\{\text{H}_2\text{O}, \delta D\}$ pairs of the transport clusters from Figure 13 against the COSMO$_{iso}$ grid point values from Figure 3 reveals that the identified process curves along different transport
pathways provide a useful framework for better understanding the actual evolution of the isotopic composition in the Sahelian mid-troposphere during the WAM.

5. Conclusions

The aim of our Lagrangian process attribution procedure is to provide a framework for interpreting the isotopic composition of tropospheric moisture in a chosen target region by means of individual moisture pathways. In this procedure, we trace the evolution of paired distributions of H$_2$O and $\delta$D$_O$ along backward trajectories. Analyzing the two-dimensional $\{H_2O, \delta D\}$ phase space, a separation of effects due to mixing and precipitation processes (condensation, evaporation, and equilibration) is possible by following the theoretical process curves of Noone (2012). They usually refer to single processes occurring along idealized air parcel trajectories. However, an application of these curves that explicitly identifies processes occurring along actual trajectories has never been done so far.

As a showcase for our Lagrangian process attribution, we demonstrate how the interpretation of mid-tropospheric $\{H_2O, \delta D\}$ pair data over the Sahel during the West African Monsoon season 2016 can be improved by considering the past transport pathways and moist processes of inflowing air masses. For this purpose, we use data from a high-resolution, convection-permitting COSMO$_{lu}$ simulation and compute Lagrangian backward trajectories started from the Sahelian mid-troposphere. By analyzing the $\{H_2O, \delta D\}$ evolution along individual trajectories as well as clusters of trajectories, we identify characteristic effects of: (a) mixing of moist air masses that were enriched due to surface evaporation and moist advection with subsiding air masses that transport dry and depleted signals from the upper troposphere or from higher latitudes; (b) condensation associated with convection that follow the Rayleigh model; (c) partial rain evaporation and isotope equilibration of rain drops formed from melting snow that both lead to a depletion of water vapor beyond the Rayleigh prediction, thereby accounting for the so-called Super-Rayleigh area. This complements earlier work from Worden et al. (2007) and Risi, Bony, Vimeux, Chong, and Descroix (2010), who attributed the enhanced depletion in tropical mid-level water vapor to rain evaporation and dry mixing.

In summary, the combination of the aforementioned processes, which are closely connected with the dominant transport pathways over West Africa, ultimately determine the prevailing signals in $\{H_2O, \delta D\}$ pairs in the Sahelian mid-troposphere at a given time.

This kind of Lagrangian process attribution is a valuable foundation for future studies, as it can be flexibly adapted to any region and time period. It holds great potential for an improved interpretation of tropospheric water vapor measurements and for an evaluation of numerical models. While here the analysis has been performed based only on model data, in ongoing studies, the authors examine the potential of comparing the here presented model-based results with remotely sensed Metop/IASI $\{H_2O,\delta D\}$ pair data for the Sahelian troposphere across different time scales. Further, this study lays the meteorological foundation for the development of an improved clustering method that automatically groups trajectories with similar geographical and isotopic properties. As this would require the consideration of multiple dimensions (e.g., three spatial coordinates, time coordinate, H$_2$O and $\delta$D), sophisticated clustering algorithms are needed. An approach addressing this challenge is discussed in Ertl et al. (2021) based on the trajectory ensemble from this study. Such an analysis has the potential of generating quantitative information about the occurrence of specific processes along trajectory ensembles and therefore better estimating their impact on $\{H_2O, \delta D\}$ values in specific air masses.

In a long-term perspective, we are confident that careful synergistic analyses combining in-situ and satellite measurements with model simulations and process attribution can improve the general understanding of the hydrological cycle and its representation in weather and climate models.

Appendix A: Depletion of $\delta$D, Due to Isotopic Equilibration With Falling Rain

This appendix provides mathematical evidence that isotopic equilibration between falling rain drops and relatively enriched water vapor in saturated conditions has a depleting effect on $\delta$D$_O$ in the ambient air.
Following the definitions from Section 2, the ratio between the specific water contents of HDO and H2O in rain \((x = r)\) and vapor \((x = v)\) is

\[
R_x = \frac{q_x^D}{q_x}; \quad R_{x,eq} = \frac{q_{x,eq}^D}{q_{x,eq}}
\]  

(A1)

with \(q_x^D\) and \(q_x\) referring to the initial, isotopically non-equilibrated state and \(q_{x,eq}^D\) and \(q_{x,eq}\) denoting the water contents after isotopic equilibration. Analogous to Equation 3, the equilibrium fractionation factor for the equilibrated states is

\[
\alpha_{eq} = \frac{R_{v,eq}}{R_{v,eq}}
\]  

(A2)

In saturated conditions there is no net exchange of H2O between the rain drop and the ambient water vapor, that is, \(q_x = q_{x,eq}\). However, as saturation does not automatically also that HDO is in equilibrium, an isotopic flux may be enforced between the rain drop and the vapor that fulfills following criterion:

\[
q_x^D + q_r^D = q_{x,eq}^D + q_{v,eq}^D
\]  

(A3)

Combining Equations A1–A3 yields

\[
R_{v,eq} = \frac{1}{\alpha_{eq}} R_{v,eq} = \frac{1}{\alpha_{eq} q_r} \left( q_x^D + q_r^D - q_{x,eq}^D \right)
\]  

(A4)

\[
= \frac{1}{\alpha_{eq}} \left( \frac{1}{q_r} \left( R_v + \frac{q_x}{q_r} (R_r - R_{v,eq}) \right) \right)
\]  

(A5)

and after further rewriting this results in the following expression:

\[
\frac{R_{v,eq}}{R_v} = \frac{R_v + q_x}{\alpha_{eq} + q_r} \frac{q_r}{q_r}
\]  

(A6)

Equation A6 relates the ratio of the isotopic composition in the vapor between the equilibrated \((R'_{v,eq})\) and non-equilibrated \((R_v)\) state to the ratio of the initial, non-equilibrated isotopic compositions of the falling rain drop \((R_r)\) and the vapor \((R_v)\). As the rain drops form typically further aloft from more depleted vapor, \(R_v\) is in this case lower than \(R_{v,eq}\). Therefore, we can assume that the ratio of \(R_v\) and \(R_{v,eq}\) is lower than \(\alpha_{eq}\), such that Equation A6 results in

\[
\frac{R_{v,eq}}{R_v} < 1
\]  

(A7)

That is, the vapor in equilibrium with the more depleted rain drop is more depleted in \(\delta D\) than the non-equilibrated vapor. This shows that isotopic equilibration can account for an enhanced depletion in \(\delta D\), while H2O remains unaffected.

**Data Availability Statement**

Simulations were conducted at the Swiss National Supercomputing Centre (CSCS). The trajectory data can be accessed via the DOI: 10.35097/469 (Diekmann & de Vries, 2021).

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