Study of hadronic transitions between $\Upsilon$ states and observation of $\Upsilon(4S) \to \eta\Upsilon(1S)$ decay

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We present a study of hadronic transitions between $T(mS)$ ($m = 4, 3, 2$) and $T(nS)$ ($n = 2, 1$) resonances based on $347.5\,fb^{-1}$ of data taken with the BABAR detector at the PEP-II storage rings. We report the first observation of $\Gamma(4S) \to \eta T(1S)$ decay with a branching fraction $B(\Gamma(4S) \to \eta T(1S)) = (1.96 \pm 0.06_{\text{stat}} \pm 0.09_{\text{syst}}) \times 10^{-4}$ and measure the ratio of partial widths $\Gamma(\Gamma(4S) \to \eta T(1S))/\Gamma(\Gamma(4S) \to \pi^+\pi^- T(1S)) = 2.41 \pm 0.40_{\text{stat}} \pm 0.12_{\text{syst}}$. We set 90% CL upper limits on the ratios $\Gamma(T(2S) \to \eta T(1S))/\Gamma(T(2S) \to \pi^+\pi^- T(1S)) < 5.2 \times 10^{-3}$ and $\Gamma(T(3S) \to \eta T(1S))/\Gamma(T(3S) \to \pi^+\pi^- T(1S)) < 1.9 \times 10^{-7}$. We also present new measurements.
of the ratios \( \Gamma(Y(4S) \to \pi^+\pi^- Y(2S))/\Gamma(Y(4S) \to \pi^+\pi^- Y(1S)) = 1.16 \pm 0.16 \text{stat} \pm 0.14 \text{sys} \) and
\( \Gamma(Y(3S) \to \pi^+\pi^- Y(2S))/\Gamma(Y(3S) \to \pi^+\pi^- Y(1S)) = 0.577 \pm 0.026 \text{stat} \pm 0.060 \text{sys} \).

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I. INTRODUCTION

Hadronic transitions between bound states of heavy quarkonia \cite{1} are generally studied using the QCD multipole expansion model (QCDME) \cite{2}. This succeeds in explaining the relative rates of the \( \psi(2S) \to \eta J/\psi \) and \( \psi(2S) \to \pi\pi J/\psi \) transitions and the \( \pi \) invariant mass distributions in \( \psi(2S) \to \pi\pi J/\psi \), \( Y(2S) \to \pi\pi Y(1S) \), \( Y(3S) \to \pi\pi Y(2S) \) and the recently observed \( Y(4S) \to \pi^+\pi^- Y(1S) \) decays \cite{3, 4}. Until recently the only feature that QCDME could not explain was the dipion invariant mass distribution in the \( Y(3S) \to \pi\pi Y(1S) \) transition \cite{5}, for which a number of possible explanations have been proposed \cite{6}. The dipion invariant mass distribution in the \( Y(4S) \to \pi^+\pi^- Y(2S) \) \cite{3} is also in disagreement with the QCDME prediction and was not predicted either by the alternative explanations proposed for the \( Y(3S) \to \pi^+\pi^- Y(1S) \). This implies that additional experimental input is needed to understand hadronic transitions. In QCDME the gluon radiation from a heavy \( q\bar{q} \) bound state is calculated in terms of chromo-electric and chromo-magnetic fields, in analogy to electromagnetism. Transitions between colorless hadrons require the emission of at least two gluons. The \( Y(mS) \to \pi\pi Y(nS) \) transitions \( (m^3S_1 \to \pi\pi n^3S_1 \) in spectroscopic notation \cite{7}) are E1E1, i.e. transitions where both gluons are in an E1 state. The decays \( Y(mS) \to \eta\eta Y(nS) \) \( (m^3S_1 \to \eta \eta n^3S_1) \) proceed either via E1M2 or M1M1 transitions; the E1M2 transition is expected to dominate. The \( b\bar{b} \) system offers unique opportunities: there are five known \( m^3S_1 \to \pi\pi n^3S_1 \) transitions and also four kinematically allowed transitions involving an \( \eta \) meson. Of the latter only the \( Y(2S) \to \eta Y(1S) \) has been recently observed by CLEO \cite{8}, with a branching fraction \( B(Y(2S) \to \eta Y(1S)) = (2.1^{+0.7}_{-0.6} \pm 0.5) \times 10^{-4}. \)

In this paper we present improved measurements of the \( Y(4S) \to Y(nS) \) transitions, a search for \( Y(mS) \to \eta Y(1S) \) and new measurements of \( Y(3S) \to \pi^+\pi^- Y(nS) \) and \( Y(2S) \to \pi^+\pi^- Y(1S) \) partial widths. We also measure the ratios of partial widths \( \Gamma(Y(mS) \to \eta Y(1S))/\Gamma(Y(mS) \to \pi^+\pi^- Y(1S)) \) and \( \Gamma(Y(mS) \to \pi^+\pi^- Y(2S))/\Gamma(Y(mS) \to \pi^+\pi^- Y(1S)) \) \( (m = 3, 4) \), for which a number of systematic uncertainties cancel.

The \( Y(mS) \to \pi^+\pi^- Y(nS) \) and \( Y(mS) \to \eta Y(nS) \) transitions, denoted by \( mS \to \pi\pi nS \) and \( mS \to \eta nS \), respectively, are studied by reconstructing the \( Y(nS) \) mesons via their leptonic decay to \( \mu^+\mu^- \) or \( e^+e^- \). The \( \eta \) meson is reconstructed via its \( \pi^+\pi^-\pi^0 \) decay. With the choice of this particular \( \eta \) decay mode all final states contain the same charged particles, resulting in larger cancellations of the systematic uncertainties for the ratios of partial widths. Events where the \( \eta \) decays to \( \gamma\gamma \) are not considered in this work because the \( \ell\ell\gamma \) final state has a smaller signal-to-background ratio than the \( \ell^+\ell^-\pi^+\pi^-\pi^0 \) final state.

II. DATA SAMPLES AND DETECTOR

We search for \( Y(4S) \) hadronic transitions using a sample of \( (383.2 \pm 4.2) \times 10^6 \ Y(4S) \) decays corresponding to an integrated luminosity, \( L_{\text{int}} \), of 347.5 fb\(^{-1}\) acquired near the peak of the \( Y(4S) \) resonance ("on-peak"), nominal center-of-mass energy, \( \sqrt{s} \) of about 10.58 GeV with the BaBar detector at the PEP-II asymmetric-energy \( e^+e^- \) storage rings at SLAC. In addition, a data sample corresponding to \( L_{\text{off}} = 36.0 \) fb\(^{-1}\), collected approximately 40 MeV below the resonance ("off-peak") is used to study some of the backgrounds. Decays of \( Y(3S) \) and \( Y(2S) \) are studied in events recorded "on-peak" and selected with an initial state radiation (ISR) photon. The ISR photon, preferentially emitted at small angle along the beam direction, is not required to be detected.

The BaBar detector is described in detail elsewhere \cite{9}. Charged-particle momenta are measured in a tracking system consisting of a five-layer double-sided silicon vertex tracker (SVT) and a 40-layer central drift chamber (DCH), both embedded in a 1.5-T axial magnetic field. Charged-particle identification is based on the specific energy loss measured in the SVT and DCH, and on a measurement of the photons produced in the fused-silica bars of the ring-imaging Cherenkov detector (DIRC). A CsI(Tl) electromagnetic calorimeter (EMC) is used to detect and identify photons and electrons, while muons are identified in the instrumented flux return of the magnet (IFR).

Simulated Monte Carlo (MC) events are generated using the EvtGen package \cite{10}. The angular distribution of generated dilepton decays incorporates the \( Y(nS) \) polarization, while dipion transitions are generated according to phase space. In the simulation of \( mS \to \eta \ 1S \) we use the angular distribution dictated by the quantum numbers for a vector decay to a pseudoscalar and a vector. Secondary photon emission is taken into account.

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in the simulation of $\Upsilon(mS)$ produced in ISR. Simulated events are passed through a detector simulation based on GEANT4 [11], and analyzed in the same manner as data.

### III. EVENT SELECTION

The events of interest have a lepton pair from the decay of the $\Upsilon(nS)$ resonance of invariant mass, $M_{\ell\ell}$, compatible with the known mass values of the $\Upsilon(nS)$ [12], $M(nS)$, and a pair of oppositely charged pions.

The signature for $mS \rightarrow \pi\pi nS$ transition events is an invariant mass difference $\Delta M = M_{\pi\pi nS} - M_{\ell\ell}$ compatible with the difference of the masses of the two $\Upsilon$ resonances, $M(mS) - M(nS)$, where $M_{\pi\pi nS}$ is the $\pi^+\pi^-\ell^+\ell^-$ invariant mass.

The $mS \rightarrow \eta nS$ events have two additional photons from the $\pi^0$ decay, a $\pi^+\pi^-\pi^0$ invariant mass, $m_{\pi\pi\eta}$, compatible with the known $\eta$ mass, $M(\eta)$, and an invariant mass difference, $\Delta M_{\eta} = M_{\eta nS} - M_{\ell\ell} - m_{\pi\pi}$ compatible with $M(mS) - M(nS) - M(\eta)$, where $M_{\eta nS}$ is the $\pi^+\pi^-\eta\ell^+\ell^-$ invariant mass.

The r.m.s. widths of the reconstructed $M_{\ell\ell}$, $M_{\pi\pi\eta}$, $\Delta M$, and $\Delta M_{\eta}$ distributions are of the order of 75 MeV/$c^2$, 12 MeV/$c^2$, 7 MeV/$c^2$ and 10 MeV/$c^2$, respectively.

Events in the data sample with $M_{\ell\ell}$ within 350 MeV/$c^2$ of the known $M(nS)$ values and $\Delta M$ within 60 MeV/$c^2$ of the values expected for any of the $mS \rightarrow \pi\pi nS$ transitions were not examined until the event selection criteria were finalized. Events outside these regions were used to understand the background. Simulated MC events were used to model the signal.

Candidate events have at least 4 charged tracks with a polar angle $\theta$ within the fiducial volume of the tracking system ($0.41 < \theta < 2.54$ rad). Each lepton candidate is required to have a center-of-mass momentum between 4.20 GeV/c and 5.25 GeV/c. At least one of the muons of $\Upsilon(nS) \rightarrow \mu^+\mu^-$ candidates must be compatible with the muon hypothesis based on the energy deposited in the EMC and the hit pattern in the IFR along the track trajectory. Similarly at least one of the electrons of $\Upsilon(nS) \rightarrow e^+e^-$ candidates must be compatible with the electron hypothesis based on the energy deposit in the EMC, the ratio of energy in the EMC to the track momentum, and the energy loss in the detector material. We require $M_{\mu\mu}[M_{ee}]$ to be within $\pm200 [-350, +200]$ MeV/$c^2$ of the nominal $\Upsilon(1S)$ or $\Upsilon(2S)$ mass. The asymmetric cut in the $e^+e^-$ sample is due to bremsstrahlung, which causes a long tail in the reconstructed $M_{ee}$ distribution at low invariant masses and that is partially recovered by an algorithm that combines the energy of electron tracks with the energy of nearby photons.

Pairs of oppositely charged tracks, not identified as electrons and whose Cherenkov angle in the DIRC, when measured, is within 3$\sigma$ of the value expected for a pion, are selected to form a dipion candidate. The dilepton and the dipion are constrained to a common vertex and the vertex fit is required to have a $\chi^2$ probability larger than $10^{-3}$.

A large fraction of the remaining background is due to $e^+e^-\gamma$ and $\mu^+\mu^-\gamma$ events where a photon converts in the detector material and the leptons are reconstructed as pions. To reduce this background we reject events where the opening angle of the charged pion candidates in the laboratory reference frame has $\cos(\theta_{p+} + \pi^-) > 0.95$, or where the invariant mass of the charged tracks associated with the pion candidates, calculated assuming the $e^\pm$ mass hypothesis, satisfies $m_{\text{conv}} < 50$ MeV/$c^2$. The distribution of $M_{\ell\ell}$ vs $\Delta M$ for candidate events after the preliminary selection is shown in Fig. 1.

In the case of $\Upsilon(4S) \rightarrow \Upsilon(nS)$ transitions the back-
TABLE I: Selection efficiencies for all studied transitions, separately for \( \Upsilon(nS) \rightarrow \mu^+\mu^- \) and \( e^+e^- \) as determined by MC simulation. For the \( mS \rightarrow \pi^+\pi^-nS \) transitions we quote both the efficiency averaged over phase space, \( \varepsilon_{PS} \), and the effective efficiency, \( \varepsilon_{eff} \), calculated according to Eq. 3.

| Transition       | Selection efficiency (%) | \( \varepsilon_{PS} \) | \( \varepsilon_{eff} \) | \( \varepsilon_{PS} \) | \( \varepsilon_{eff} \) |
|------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| \( 2S \rightarrow \pi\pi 1S \) | \( 34.46 \pm 0.05, 36.62 \pm 0.08 \) | \( 11.17 \pm 0.03, 11.45 \pm 0.14 \) | \( 32.69 \pm 0.05, 34.18 \pm 0.20 \) | \( 24.48 \pm 0.05, 23.96 \pm 0.24 \) | \( 41.23 \pm 0.23, 42.4 \pm 1.2 \) | \( 19.04 \pm 0.18, 19.7 \pm 2.4 \) |
| \( 3S \rightarrow \pi\pi 1S \) | \( 14.76 \pm 0.04, 17.2 \pm 0.6 \) | \( \approx 0 \) | \( 8.25 \pm 0.22, 30.2 \pm 0.8 \) | \( 6.17 \pm 0.12, 7.9 \pm 3.4 \) | \( 8.25 \pm 0.22, 30.2 \pm 0.8 \) | \( 6.17 \pm 0.12, 7.9 \pm 3.4 \) |

The \( \Delta M \) distributions of events in the final sample for the \( mS \rightarrow \pi^+\pi^-nS \) transitions are shown in Fig. 2.

We determine the efficiency corrected signal yield for the \( mS \rightarrow \pi^+\pi^-nS \) transitions without any assumption on the angular distributions of the decays. We divide the \( 2S \rightarrow \pi^+\pi^-1S \) and \( 3S \rightarrow \pi^+\pi^-1S \) samples into \( 10 \times 6 \) bins of \( m_{\pi\pi} \) and \( \cos \theta_h \), where \( m_{\pi\pi} \) is the \( \pi^+\pi^- \) invariant mass and \( \theta_h \) is the helicity angle of the \( \pi^+ \), defined as the angle between the \( \pi^+ \) direction in the \( \pi^+ \) rest frame and the \( \pi^+ \) direction in the candidate \( \Upsilon(mS) \) rest frame.

The signal yield in each bin is determined by a fit to the \( \Delta M \) distribution, by maximizing the unbinned extended likelihood to the sum of a background probability density function (PDF) and a signal PDF. The signal PDF is parametrized by a Voigtian function (convolution of a Lorentzian with a Gaussian function), that is found to describe well the measured \( \Delta M \) distribution for simulated events. The background is parametrized by a linear function. The resolution parameters for the signal PDF are fixed to the values determined by the simulation, thus the free parameters in the fits for bin \( i \) are: \( \Delta M_{i,\text{sig}}^\text{peak} \), the peak position of the signal distribution, \( N_{i,\text{sig}}^\text{corr} \), and \( N_{i,\text{bkg}}^\text{corr} \), the number of signal and background events, and the background shape parameters. The efficiency corrected signal yield for each \( mS \rightarrow \pi\pi\eta \) transition is then obtained as

\[ N_{\text{corr}} = \sum_{i=1}^{n\text{bins}} N_{i,\text{corr}} / \varepsilon_i, \]

where \( n\text{bins} \) is the number of bins (60 or 24) and \( \varepsilon_i \) is the efficiency in each bin determined from MC simulation.

### IV. SIGNAL YIELDS

#### IV. A. \( \Upsilon(mS) \rightarrow \pi^+\pi^-\Upsilon(nS) \)

The \( \Delta M \) distributions of events in the final sample for the \( mS \rightarrow \pi^+\pi^-nS \) transitions are shown in Fig. 2.

We determine the efficiency corrected signal yield for the \( mS \rightarrow \pi^+\pi^-nS \) transitions without any assumption on the angular distributions of the decays. We divide the \( 2S \rightarrow \pi^+\pi^-1S \) and \( 3S \rightarrow \pi^+\pi^-1S \) samples into \( 10 \times 6 \) bins of \( m_{\pi\pi} \) and \( \cos \theta_h \), where \( m_{\pi\pi} \) is the \( \pi^+\pi^- \) invariant mass and \( \theta_h \) is the helicity angle of the \( \pi^+ \), defined as the angle between the \( \pi^+ \) direction in the \( \pi^+ \) rest frame and the \( \pi^+ \) direction in the candidate \( \Upsilon(mS) \) rest frame.

#### IV. B. \( \Upsilon(mS) \rightarrow \eta\Upsilon(1S) \)

Figure 3 shows the \( m_{3\pi} \) vs \( \Delta M_0 \) distributions for events selected as \( mS \rightarrow \eta 1S \) candidates. The widths of the signal boxes have been chosen as \( \approx \pm 3\sigma \) in both variables based on MC simulation: \( |m_{3\pi} - m_{\eta}| < 35 \text{ MeV}/c^2 \) and \( |M(mS) - M(1S) - M(\eta) - \Delta M_0| < 30 \text{ MeV}/c^2 \). For the \( 2S \rightarrow \eta 1S \) transition we require \( \Delta M_0 < 30 \text{ MeV}/c^2 \) because the signal for this transition is expected close to the kinematic limit.

The numbers of candidates in the \( 2S \rightarrow \eta 1S \) and \( 3S \rightarrow \eta 1S \) signal boxes, shown in Table II, are compatible with the backgrounds extrapolated from the sidebands defined in Fig. 3. Thus, we have no signal for the \( 2S \rightarrow \eta 1S \) and \( 3S \rightarrow \eta 1S \) transitions.

We observe 56 candidates for the \( 4S \rightarrow \eta 1S \) transition in the “on-peak” data sample, and no candidates in the “off-peak” data sample. We test the hypothesis that the
Maximum likelihood fits to $\Delta M_{\mu\mu}$ and $\Delta M_{e\mu}$ based on the integrated luminosities of the two samples.

We obtain the ability to serve $\eta\Upsilon$ and "off-peak" samples by calculating the binomial probability $P$ of observing respectively 56 and 0 events for a binomial coefficient of $p = L_{\text{int}}^{\text{on}}/(L_{\text{int}}^{\text{on}} + L_{\text{off}}^{\text{on}}) = 0.905$, based on the integrated luminosities of the two samples. We obtain $P = 4 \times 10^{-3}$ and thus we attribute the observed $\eta \Upsilon(1S)$ events to $\Upsilon(4S)$ decays.

The event yields for the $4S \rightarrow \eta 1S$ transition in the $ee$ and $\mu\mu$ final states are determined by unbinned extended maximum likelihood fits to the $\Delta M_\eta$ distribution of the sample of events in Fig. 3 having $m_{3\pi}$ within 35 MeV/$c^2$ of the known $\eta$ mass. The signal PDF is parametrized by a Voigtian function, with resolution parameters fixed to the values determined from MC events, while the background is assumed to be constant. The free parameters in the fits are: $\Delta M_\eta^{\text{sig}}$, the peak position of the signal distribution, $N_\text{sig}$ and $N_{\text{bkg}}$, the number of signal and background events. The efficiency and acceptance are determined from MC samples. The fits are shown in Fig. 4. The significance, estimated from the likelihood
TABLE II: Results for the products of partial widths and branching fractions for the $\Upsilon(mS)$ hadronic transitions. $N_{\text{cand}}$ is the number of candidates in the signal box, $N_{\text{bck}}$ is the number of background events from the fit or estimated from data sidebands as described in the text, $N_{\text{corr}}$ is the efficiency-corrected number of signal events. The first error is statistical, the second is systematic. All upper limits are 90% CL.

| Transition                                                                 | Our Measurement | $N_{\text{cand}}$ | $N_{\text{bck}}$ | $N_{\text{corr}}$ |
|----------------------------------------------------------------------------|-----------------|-------------------|------------------|------------------|
| $\Gamma_{\mu\mu}(2S) \times B(\Upsilon(2S) \to \pi^+\pi^-) \times B(\Upsilon(1S) \to \mu^+\mu^-)$ | (meV) 2582 ± 28 ± 94 | 9036          | 156 ± 11         | 24319 ± 268      |
| $\Gamma_{\mu\mu}(2S) \times B(\Upsilon(2S) \to \pi^+\pi^-) \times B(\Upsilon(1S) \to e^+e^-)$ | (meV) 2618 ± 60 ± 97 | 3139          | 230 ± 9          | 25202 ± 574      |
| $\Gamma_{\mu\mu}(2S) \times B(\Upsilon(2S) \to \eta(1S) \times B(\Upsilon(1S) \to \mu^+\mu^-) \times B(\eta \to \pi^+\pi^-)$ | (meV) < 3.1     | 0              | 2.5 ± 1.1        | < 28             |
| $\Gamma_{\mu\mu}(3S) \times B(\Upsilon(3S) \to \pi^+\pi^-) \times B(\Upsilon(1S) \to \mu^+\mu^-)$ | (meV) 457 ± 8 ± 18 | 4198          | 207 ± 10         | 9945 ± 174       |
| $\Gamma_{\mu\mu}(3S) \times B(\Upsilon(3S) \to \pi^+\pi^-) \times B(\Upsilon(1S) \to e^+e^-)$ | (meV) 441 ± 12 ± 18 | 3604          | 1234 ± 20        | 9821 ± 261       |
| $\Gamma_{\mu\mu}(3S) \times B(\Upsilon(3S) \to \pi^+\pi^-) \times B(\Upsilon(2S) \to e^+e^-)$ | (meV) 206 ± 11 ± 12 | 975           | 180 ± 21         | 4477 ± 241       |
| $\Gamma_{\mu\mu}(3S) \times B(\Upsilon(3S) \to \eta(1S)) \times B(\Upsilon(1S) \to \mu^+\mu^-) \times B(\eta \to \pi^+\pi^-)$ | (meV) < 2.0     | 1              | 0.8 ± 0.4        | < 41             |
| $\Gamma_{\mu\mu}(3S) \times B(\Upsilon(3S) \to \eta(1S)) \times B(\Upsilon(1S) \to e^+e^-) \times B(\eta \to \pi^+\pi^-)$ | (meV) < 9.6     | 4              | 2.8 ± 0.8        | < 210            |
| $B(\Upsilon(4S) \rightarrow \pi^+\pi^-) \times B(\Upsilon(1S) \rightarrow \mu^+\mu^-)$ | ($10^{-6}$) 1.99 ± 0.16 ± 0.07 | 687             | 375 ± 11         | 739 ± 60          |
| $B(\Upsilon(4S) \rightarrow \pi^+\pi^-) \times B(\Upsilon(1S) \rightarrow e^+e^-)$ | ($10^{-6}$) 1.76 ± 0.15 ± 0.06 | 1057          | 934 ± 17         | 676 ± 397         |
| $B(\Upsilon(4S) \rightarrow \pi^+\pi^-) \times B(\Upsilon(2S) \rightarrow \mu^+\mu^-)$ | ($10^{-6}$) 1.65 ± 0.21 ± 0.11 | 377             | 204 ± 8          | 615 ± 78          |
| $B(\Upsilon(4S) \rightarrow \pi^+\pi^-) \times B(\Upsilon(2S) \rightarrow e^+e^-)$ | ($10^{-6}$) 1.76 ± 0.13 ± 0.11 | 251             | 206 ± 8          | 660 ± 392         |
| $B(\Upsilon(4S) \rightarrow \eta(1S)) \times B(\Upsilon(1S) \rightarrow \mu^+\mu^-) \times B(\eta \to \pi^+\pi^-)$ | ($10^{-6}$) 1.08 ± 0.17 ± 0.05 | 40              | 0.2 ± 0.4        | 387 ± 60          |
| $B(\Upsilon(4S) \rightarrow \eta(1S)) \times B(\Upsilon(1S) \rightarrow e^+e^-) \times B(\eta \to \pi^+\pi^-)$ | ($10^{-6}$) 1.15 ± 0.29 ± 0.05 | 16              | 0.7 ± 0.6        | 424 ± 106         |

FIG. 3: Distributions of $m_{3S}$ vs $\Delta M_{\eta}$ for the $mS \to \eta$ 1S transitions studied. Crosses are for the $T(1S) \to e^+e^-$ sample and dots are for the $T(1S) \to \mu^+\mu^-$ sample. Solid lines delimit the signal box region. Dashed lines delimit the sideband regions used for background extrapolation. The signal box for the $2S \to \eta$ 1S transition (top left) is at the boundary of the kinematically allowed region of $\Delta M_{\eta}$ and only one sideband can be defined.

The 90% CL upper limits on the signal yields for the $3S \to \eta$ 1S and $2S \to \eta$ 1S transitions are conservatively estimated from the numbers of events in the signal boxes, taking into account the uncertainties in the efficiencies [13]. The background level in the $\mu^+\mu^-$ sample is negligible, and background subtraction in the $e^+e^-$ sample, which also has a lower efficiency, would not affect the result.

V. SYSTEMATIC UNCERTAINTIES

We have considered a number of possible sources of systematic uncertainties, in addition to the number of $\Upsilon(4S)$ [15] and the calculated luminosity for ISR events.
TABLE III: Sources of systematic uncertainties on partial widths or branching fractions and ratios of partial widths, separated into errors that cancel in ratios, errors due to lepton identification (ID) and invariant mass that are common to all transitions, but differ for electrons and muons, and errors that are specific to individual decay modes. All errors are relative and given in percent. We also list the corrections applied to account for differences between data and simulation.

| Source | data/MC | $\mathcal{T}(2S) \rightarrow \pi\pi\Upsilon(1S)$ | $\mathcal{T}(3S) \rightarrow \pi\pi\Upsilon(1S)$ | $\mathcal{T}(4S) \rightarrow \pi\pi\Upsilon(1S)$ |
|--------|--------|---------------------------------|---------------------------------|---------------------------------|
| Number of $\Upsilon(4S)$ | – | – | – | 1.1 |
| ISR luminosity | 3.0 | 3.0 | – | – |
| Tracking | 1.0 | 1.0 | – | 1.0 |
| Selection | 0.3 | 0.3 | – | 0.3 |
| $p_{\text{cand}}$ cut | 0.3 | 0.3 | – | 0.3 |

Systematic errors associated to lepton identification or invariant mass (%)

| Source | 1.025 | 0.6 | 0.6 | 0.6 |
|--------|-------|-----|-----|-----|
| Muon ID | 1.006 | 0.2 | 0.2 | 0.2 |
| $M(\mu^+\mu^-)$ cut | 1.011 | 0.7 | 0.7 | 0.7 |
| Electron ID | 0.998 | 0.5 | 0.5 | 0.5 |
| $M(e^+e^-)$ cut | | | | |

Systematic errors specific to each mode (%)

| Source | 1.033 | 3.6 | 3.6 | 3.6 |
|--------|-------|-----|-----|-----|
| $\pi^0$ efficiency | 0.3 | 1.7 | 4.7 | 2.6 |
| Acceptance | 1.6 | 1.6 | 1.6 | 1.6 |
| Fitting | 3.7 | 4.1 | 5.1 | 3.5 |
| Total $e^+e^-$ (%) | 3.7 | 5.1 | 4.0 | 5.9 |
| Total $\mu^+\mu^-$ (%) | 3.7 | 5.1 | 5.1 | 3.5 |
| Total on ratios (%) | – | 4.3 | 5.5 | 4.6 |

VI. RESULTS

The products of branching fractions and partial widths for each transition are given Table II. They are determined from the efficiency-corrected yield in each mode, after correcting for small differences between data and MC samples and taking into account the number of $\Upsilon(4S)$ or the equivalent ISR luminosity, $\mathcal{L}$. For a narrow vector resonance produced in ISR

$$\mathcal{L} = L_{\text{int}} \frac{12\pi^2}{M(mS)s} W \left( s, 1 - \frac{M^2(mS)}{s} \right)$$

where the QED “radiator” function $W(s, x)$ is calculated to second order following [16–18].

Averaging the results from the $e^+e^-$ and the $\mu^+\mu^-$ final states, taking into account the common systematic errors, and using the world average values of $B(\eta \rightarrow \pi^+\pi^-\pi^0)$ and $B(\eta \rightarrow \ell^+\ell^-)$ [12] we obtain the partial widths and ratios of partial widths listed in Table IV. In this Table, we also compare our results to the values expected for each quantity based on previous measurements of $\Upsilon(2S)$ widths and branching fractions. The measured values of the $\Upsilon(2S)$ and $\Upsilon(3S)$ total widths are used to derive the theoretical expectations for branching fractions from the predicted partial widths in [2].
on a fraction of the current sample [3]. Part of the difference in the central values is due to the different methods used to determine the acceptance, which was calculated in our previous paper assuming a phase-space distribution in the $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(nS)$ decay. The efficiency is not uniform over the Dalitz plot, thus the impact on the central value between the two methods depends on the angular distributions peculiar of each transition. The difference can be estimated by comparing the value of the phase-space averaged efficiencies $\varepsilon_{PS}$, and the effective efficiencies $\varepsilon_{eff}$ calculated from the observed event yields in each region of the Dalitz plot

$$\varepsilon_{eff} = \frac{\sum N_i^{s i g}}{\sum N_i^{s i g}/\varepsilon_i}.$$ \hspace{1cm} (3)

Notice that the uncertainty in the calculated effective efficiency is due to the statistical uncertainty in the event yield. As shown in Table I the effective efficiency for $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S)$, when the $\Upsilon(1S)$ decays to $\mu^+\mu^-$, is $\sim 7\%$ larger than the value estimated using a phase-space distribution. Accounting for this difference, the results presented here are statistically compatible with the ones previously reported.

From our result we derive new values for $B(\Upsilon(3S,2S) \rightarrow \pi^+\pi^-\Upsilon(1S))$ that are of comparable precision to the previous world averages, and compatible with them. The value of $B(\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(2S))$ derived from our measurement has an error that is smaller than the current world average.

### VII. Conclusions

We have presented a study of hadronic transitions between the $\Upsilon$ states: new measurements of the branching fractions $B(\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S,2S))$, $B(\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(2S))$, $B(\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(1S))$ which have smaller errors than current world averages, and new measurements of $B(\Upsilon(3S,2S) \rightarrow \pi^+\pi^-\Upsilon(1S))$ whose precision is comparable to present world averages. We have also presented measurements of the ratios of partial widths $\Gamma(\Upsilon(mS) \rightarrow \pi^+\pi^-\Upsilon(2S))/\Gamma(\Upsilon(mS) \rightarrow \pi^+\pi^-\Upsilon(1S))$ ($m = 3, 4$) where a number of systematic uncertainties cancel. Our results for the branching fractions of the $\Upsilon(2S)$ and $\Upsilon(3S) \rightarrow \eta\Upsilon(1S)$ transitions represent improvements over the current published upper limits, and are compatible with the recent results from CLEO [8]: $B(\Upsilon(2S) \rightarrow \eta\Upsilon(1S)) = (2.1^{+0.7}_{-0.6} \pm 0.5) \times 10^{-4}$, $B(\Upsilon(3S) \rightarrow \eta\Upsilon(1S)) < 2.9 \times 10^{-4}$ at 90\% CL.

We observe a significant number of $\eta\Upsilon(1S)$ candidates at the formation energy of the $\Upsilon(4S)$. We can exclude the hypothesis that they are due to continuum $e^+e^- \rightarrow \eta\Upsilon(1S)$ with a probability of 99.6\% and we attribute them to $\Upsilon(4S)$ decays. The branching fraction for the $\Upsilon(4S) \rightarrow \eta\Upsilon(1S)$ decay is larger than the branching fraction for $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S)$, which is unexpected when compared to all other known charmonium and bottomonium transitions. There are no predictions for this specific decay mode. In the QCDME calculation for hadronic transitions, the effect of the nodes in the wave functions in the overlap integrals be-
between the initial and final states and the intermediate states can be large for radial excitations. But even that should not significantly affect the ratio of partial widths $\Gamma(\Upsilon(4S) \rightarrow \eta\Upsilon(1S))/\Gamma(\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S))$, at least if the $\Upsilon(4S) \rightarrow \eta\Upsilon(1S)$ transition is E1M2 [2]. It is possible that accidental cancellations suppress the E1M2 term with respect to M1M1, or perhaps QCDME becomes unreliable for higher gluon momenta. These results, together with the recent CLEO measurement of the matrix elements in $\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(1S,2S)$ and $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$ transitions [19], could provide a tool to understand the hadronic transitions better.

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[1] For a recent review on heavy quarkonia, see N. Brambilla et al. [Quarkonium Working Group], arXiv:hep-ph/0412158.
[2] Y. P. Kuang, Front. Phys. China 1, 19 (2006) and references therein.
[3] B. Aubert et al. [BABAR Collaboration], Phys. Rev. Lett. 96, 232001 (2006).
[4] A. Sokolov et al. [Belle Collaboration], Phys. Rev. D 75, 071103 (2007).
[5] F. Butler et al. [CLEO Collaboration], Phys. Rev. D 49, 40 (1994).
[6] P. Moxhay, Phys. Rev. D 39, 3497 (1989); H. Y. Zhou and Y. P. Kuang, Phys. Rev. D 44, 756 (1991); F. K. Guo, P. N. Shen, H. C. Chiang and R. G. Ping, Nucl. Phys. A 761, 269 (2005); V. V. Anisovich, D. V. Bugg, A. V. Sarantsev and B. S. Zou, Phys. Rev. D 51, 4619 (1995); M. Uehara, Prog. Theor. Phys. 109, 265 (2003); H. W. Ke, J. Tang, X. Q. Hao and X. Q. Li, Phys. Rev. D 76, 074035 (2007).
[7] In the rest of the paper $m = 4,3,2$ and $n = 2,1$ unless specified otherwise.
[8] Q. He et al. [CLEO Collaboration], arXiv:0806.3027 [hep-ex].
[9] B. Aubert et al. [BABAR Collaboration], Nucl. Instrum. Meth. Phys. Res., Sect. A 479, 1 (2002).
[10] D. J. Lange, Nucl. Instrum. Meth. Phys. Res., Sect. A 462, 152 (2001).
[11] S. Agostinelli et al., Nucl. Instrum. Meth. Phys. Res., Sect. A 506, 250 (2003).
[12] W. M. Yao et al. [Particle Data Group], J. Phys. G 33 (2006) 1 and 2007 partial update for the 2008 edition available on the PDG WWW pages http://pdg.lbl.gov/.
[13] R. Barlow, Comput. Phys. Commun. 149, 97 (2002).
[14] E. Eichten, S. Godfrey, H. Mahlke and J. L. Rosner, arXiv:hep-ph/0701208.
[15] B. Aubert et al. [BABAR Collaboration], Phys. Rev. D 67, 032002 (2003) [arXiv:hep-ex/0207097].
[16] M. Benayoun, S. I. Eidelman, V. N. Ivanchenko and Z. K. Silagadze, Mod. Phys. Lett. A 14, 2605 (1999).
[17] G. Bonneau and F. Martin, Nucl. Phys. B 27, 381 (1971).
[18] V. N. Baier, V. S. Fadin and V. A. Khoze, Nucl. Phys. B 65, 381 (1973).
[19] D. Cronin-Hennessy et al., [CLEO Collaboration] Phys. Rev. D 76, 072001 (2007).