Search for the $\eta$ mesic $^3$He in the $pd \to dp\pi^0$ reaction with the WASA-at-COSY facility

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The excitation function for the $pd \rightarrow dp\eta^0$ reaction has been measured by WASA-at-COSY experiment with the aim of searching for $^3\text{He}-\eta$ mesic nuclei. The measurement in the vicinity of $\eta$ meson production was performed using a ramped proton beam. The data analysis and interpretation was carried out with the assumption that the $\eta$-mesic Helium decays via the formation of an intermediate $N^*$ (1535) resonance. No direct signal of the $\eta$-mesic nucleus is observed in the excitation function. We determine a new improved upper limit for the total cross section for the bound state production and decay in the $pd \rightarrow (^3\text{He}-\eta)_{\text{bound}} \rightarrow dp\eta^0$ process. It varies between 13 nb to 24 nb for the bound state with width in the range $\Gamma \in (5,50)$ MeV.

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I. INTRODUCTION

In this paper we present a new high statistics search for $^3\text{He}-\eta$ bound states with focus on the $pd \rightarrow dp\eta^0$ reaction. The measurement was performed using data from the WASA-at-COSY experiment at Forschungszentrum Jülich. Strong attractive interactions between the $\eta$ meson and nucleons mean that there is a chance to form $\eta$ meson bound states in nuclei [1]. If discovered in experiments, these mesic nuclei would be a new state of matter bound just by the strong interaction without electromagnetic Coulomb effects playing a role because of the zero electric charge of the $\eta$ meson. Early experiments with low statistics using photon [2, 3], pion [4], proton [5] or deuteron [6-8] beams gave hints for possible $\eta$ mesic bound states but no clear signal [9, 10]. The new results reported here are complementary to the recent $^3\text{He}-\eta$ bound state search using the $pd \rightarrow ^3\text{He}2\gamma$ and $pd \rightarrow ^3\text{He}6\gamma$ reactions and performed with the same experiment.

The key physical process involves a virtual $\eta$ meson produced in the $pd$ collision forming a bound state with the $^3\text{He}$ nucleus in which it is produced. The bound states might form by the attractive interaction, with finite width corresponding to the finite lifetime of the state due to the absorptive interaction with the nucleus. $\eta$ meson interactions with nucleons and nuclei are a topic of much experimental and theoretical interest. For recent reviews see [9-14].

Hints for possible $^3\text{He}$ helium bound states are inferred from the observation of strong interaction in the $\eta$ helium system. One finds a sharp rise in the cross section at threshold for $\eta$ production in photoproduction from $^3\text{He}$ [2, 15] and in the proton-deuteron reaction $dp \rightarrow ^3\text{He}\eta$ [16]. These observations may hint at a reduced $\eta$ effective mass in the nuclear medium, see e.g. [11].

Possible $\eta$-nucleus binding energies are related to the $\eta$-nucleus optical potential and to the value of $\eta$-nucleon scattering length $a_{\eta N}$ [17]. Phenomenological estimates for the real part of $a_{\eta N}$ are typically between 0.2 and 1 fm. $\eta$ bound states in helium require a large $\eta$-nucleon scattering length with real part greater than about 0.7–1.1 fm [18-20]. Recent calculations in the framework of optical potential [21], multi-body calculations [19], and pionless effective field theory [13] suggest a possible $^3\text{He}-\eta$ bound state.

The related system of $\eta'$-nucleus interactions is also a strong candidate for a meson-nucleus bound state. Recent measurements by the CBELSA/TAPS collaboration in Bonn using photoproduction of $\eta'$ mesons from a carbon target determined the $\eta'$-nucleus optical potential $V_{\text{opt}} = V + iw$ with the strength of the real part at nuclear matter density $\rho_0$ related to the meson’s effective mass shift $V = m^* - m = -37 \pm 10 \pm 10$ MeV and imaginary part $W = -10 \pm 2.5$ MeV at $\rho_0$ [22]. With the attractive real part of the potential greater than the imaginary part, this result has inspired a program of bound state searches with first results (ruling out much larger potential depths) reported in Ref. [23] and future more accurate measurements in planning. The $\eta'$ mass shift suggested by CBELSA/TAPS is very close to the prediction of the Quark Meson Coupling model, QMC, with mixing angle -20 degrees [24, 25] and consistent with $\eta'$-nucleon scattering length determinations from Bonn [20] and COSY-11 [27]. The QMC model predicts an $\eta$ nucleus potential depth about -100 MeV at $\rho_0$.

In May 2014 the experimental search for $\eta$ mesic $^3\text{He}$ nuclei was carried out using the WASA-at-COSY detection system [28-33] at Forschungszentrum Jülich in Germany colliding the COSY proton beam with a deuteron pellet target. The search for $\eta$-mesic bound states was performed considering two main predicted mechanisms for the $\eta$-mesic bound state decay, via the formation of an intermediate $N^*$ (1535) resonance and its decay into a nucleon pion pair (used in previous experimental studies) and via decay of $\eta$-meson still “orbiting” around the nucleus [34]. The bound state, if it exists, would be man-
FIG. 1: Model of the $^3$He-$\eta$ bound state production and decay in the $pd \rightarrow d\rho\pi^0$ reaction.

ifest as a resonance structure in the excitation function for the studied processes below the $pd \rightarrow ^3$He$\eta$ reaction threshold.

The mechanism of $\eta$-mesic $^3$He decay has been investigated recently for the first time by analysing the $pd \rightarrow ^3$He$2\gamma$ and $pd \rightarrow ^3$He$6\gamma$ reactions [35] assuming the theoretical model recently developed in [34]. The final excitation functions for both channels showed a slight indication of the signal from a possible bound state for $\Gamma > 20$ MeV and binding energies in the range from 0 to 15 MeV which is, however, covered by the systematic error. Therefore, drawing conclusions for the bound state existence in the considered mechanism was not possible.

The upper limit at the CL=90% obtained by fitting simultaneously excitation functions for both processes varied between 2 nb to 15 nb depending on the bound state parameters [35].

In this paper we present results of the search for $\eta$-mesic $^3$He in the $pd \rightarrow dp\pi^0$ reaction corresponding to the mechanism $pd \rightarrow (^3$He-$\eta)_{bound} \rightarrow N^*d \rightarrow pd\pi^0$ via excitation of the $N^*(1535)$ resonance – see Fig. 1 – with the $N^*(1535)$ coming with narrower momentum distribution compared to nucleons [36, 37].

Earlier bound state searches at COSY, assuming the above mechanism, focused on the reaction $dd \rightarrow ^4$He$N\pi$. The excitation functions determined around the threshold for $dd \rightarrow ^4$He$N\pi$ did not reveal a structure that could be interpreted as a narrow mesic nucleus [3, 38, 40]. Upper limits for the total cross sections for bound state production and decay in the processes $dd \rightarrow (^4$He-$\eta)_{bound} \rightarrow ^4$He$N\pi^0$ and $dd \rightarrow (^4$He-$\eta)_{bound} \rightarrow ^4$He$N\pi^-$ were deduced to be about 5 nb and 10 nb for the $NN^0$ and $p\pi^-$ channels, respectively [38]. The bound state production cross sections for $pd \rightarrow (^3$He-$\eta)_{bound}$ [41] are expected to be more than 20 times larger than for $dd \rightarrow (^4$He-$\eta)_{bound}$ [42].

II. EXPERIMENT

A. Measurement conditions

The high statistics experiment devoted to the search for $^3$He-$\eta$ mesic nuclei in the $pd \rightarrow d\rho\pi^0$ reaction was carried out with the WASA (Wide Angle Shower Apparatus) [16, 30-33] detection setup installed at the COSY accelerator [28, 29]. The WASA detector consisted of two main parts: the Forward Detector (FD) and Central Detector (CD) optimized for tagging the recoil particles and registering the meson decay products, respectively.

The measurement was performed changing the proton beam momentum very slowly and continuously around the $\eta$ production threshold in each acceleration cycle from 1.426 to 1.635 GeV/c, corresponding to the $^3$He excess energy range $Q \in (-70,30)$ MeV. The application of this so-called ramped beam technique allowed us to reduce the systematic uncertainties with respect to separate runs at fixed beam energies [8, 43].

Possible resonance-like structure below the $\eta$ production threshold associated with the $^3$He-$\eta$ bound state was searched for via measurement of the excitation function for the $pd \rightarrow d\rho\pi^0$ reaction.

B. $pd \rightarrow (^3$He-$\eta)_{bound} \rightarrow d\rho\pi^0$ events selection

The events corresponding to formation of $^3$He-$\eta$ bound states were selected with appropriate conditions based on the Monte Carlo simulation of the $pd \rightarrow (^3$He-$\eta)_{bound} \rightarrow d\rho\pi^0$ reaction. The considered kinematic mechanism of the process is presented schematically in Fig. 1. According to the scheme, the proton deuteron collision leads to the formation of a $^3$He nucleus bound with the $\eta$ meson via strong interactions. Then, the $\eta$ meson can be ab-
sorbed by one of the nucleons inside the helium exciting it to the \( N^*(1525) \) nucleon resonance until the resonance decays into a proton \( \pi^0 \) pair, with the pion subsequently decaying into two photons. This mechanism, with formation of an intermediate \( N^* \), was also assumed in the previous analyses \cite{35, 36, 37}. The simulation was performed using the \( N^* \) resonance momentum distribution in the \( N^*-d \) system determined recently by Kelkar et al. \cite{36, 37}. The distribution calculated for two different values of binding energy \( E_{N^*-d} = -0.33 \) MeV and \(-0.53 \) MeV is shown in Fig. 2 (red and green solid lines). It is much narrower compared to the Fermi momentum distribution of protons inside \(^3\)He \cite{14} (blue dotted line) which results from the fact that the \( N^* \) binding energy is smaller than the energy separation of proton in \(^3\)He.

![FIG. 2: Fermi momentum distribution of the \( N^* \) resonance in the \( N^*-d \) system for two different values of binding energy \( E_{N^*-d} = -0.33 \) MeV and \(-0.53 \) MeV (red and green solid lines, respectively) \cite{36, 37} and of protons inside \(^3\)He nucleus for the separation energy \( \sim 5.5 \) MeV (blue dotted line) \cite{14}.](image)

The deuteron in this process plays the role of a spectator. In the simulations it was assumed that the bound state has a resonance structure given by the Breit-Wigner distribution with fixed binding energy \( B_s \) and width \( \Gamma \):

\[
N(\sqrt{s_{pd}}) = \frac{\Gamma^2/4}{(\sqrt{s_{pd}} - (m_\eta + m_{^3He} - B_s))^2 + \Gamma^2/4},
\]

where \( \sqrt{s_{pd}} \) is the invariant mass of the colliding proton and deuteron and \( m_\eta + m_{^3He} - B_s \) is the bound state mass. The total invariant mass \( \sqrt{s_{pd}} \) was calculated based on the proton beam momentum \( p_{beam} \), which was generated with uniform probability density distribution in the range of \( p_{beam} \in (1.426, 1.635) \) GeV/c corresponding to the experimental beam ranging.

Events selection for the \( pd \rightarrow (^3\text{He}-\eta)_{\text{bound}} \rightarrow dp\pi^0 \) process started with particles identification in the Central Detector. Protons were identified based on the energy deposited in the Scintillator Electromagnetic Calorimeter (SEC) combined with the energy loss in the Plastic Scintillator Barrel (PSB), see Fig. 3.

The neutral pions \( \pi^0 \) were identified on the basis of the invariant mass of two photons originating from their decays and measured in the SEC (left upper panel of Fig. 3). Deuterons which were not directly registered in the experiment were identified via the missing mass technique. The events corresponding to \( \eta \)-mesic bound states were selected by applying cuts in the \( \pi^0 \)-proton opening angle in the c.m. frame \( \vartheta_{\pi^0,p} \) in the missing mass as well as in the deuteron momentum \( p_d \) distributions (see Fig. 4).

The spectra including experimental data and Monte-Carlo simulation for the signal and the dominant background \( pd \rightarrow dp\pi^0 \) process are presented in Fig. 4 with marked selection cuts.

The final number of selected events as a function of the excess energy \( Q \) for the \( pd \rightarrow dp\pi^0 \) reaction is shown in Fig. 5. The excess energy range \( Q \in (-70, 30) \) MeV was divided into 40 intervals, each of width 2.5 MeV.

![FIG. 3: Energy deposited in the Scintillator Electromagnetic Calorimeter (SEC) as a function of the energy loss in the Plastic Scintillator Barrel (PSB) for experimental data (upper panel) and simulations (lower panel). The area corresponding to selected protons is marked with a red line.](image)
FIG. 4: $\pi^0$ identification based on the two photon invariant mass spectrum (left upper panel), $\pi^0$-proton opening angle in the c.m. frame $\vartheta_{\pi^0,p}$ (right upper panel), deuteron identification based on the missing mass technique (left lower panel) and the deuteron momentum distribution in the laboratory frame $p_d$ (right lower panel). Data are shown as black crosses. Orange solid and blue dotted lines show the simulation of signal and background from $pd \rightarrow dp\pi^0$ reaction respectively, while the red vertical lines indicate the boundary of the applied selection cuts.
In order to determine the excitation function for the studied reaction the number of events in each excess energy interval has to be normalized by the integrated luminosity and corrected for the total efficiency. Since, during the beam ramping process the luminosity has varied due to the change of the beam-target overlap, the luminosity dependence on the excess energy \( L(Q) \) has been determined analysing the quasi-elastic proton\( \rightarrow \)proton scattering process based on the method described in \([45–47]\). For this purpose dedicated Monte Carlo simulation for \( pd \rightarrow ppm_{\text{spectator}} \) reaction has been performed assuming that the beam protons scatter on the protons in the deuteron target and the neutrons from the deuteron play a role of spectators. The target nucleons momenta were generated isotropically with Fermi momentum distribution derived from the Paris \([48]\) and the CDBonn potential models \([49]\), see Fig. 6.

In the analysis quasi-elastically scattered protons were searched for with the primary events selection condition of exactly one charged particle in the Forward Detector and one charged particle in the Central Detector. Proton identification in the Central Detector was based on the selection criterium shown in Fig. 3.

A part of the background from elastic \( pd \rightarrow pd \) scattering corresponding to deuterons was subtracted applying the criterium for polar angle \( \theta_{CD} \in (40, 100)^\circ \), while part corresponding to protons was eliminated by fitting the \( \theta_{CD} \) distribution for each interval of excess energy \( Q \) and polar angle \( \theta_{FD} \) with the sum of two Gaussian functions (see Fig. 7).

In order to determine the integrated luminosity the number of reconstructed events obtained from Monte Carlo simulation was weighted with the values of the differential cross section for the quasi-free proton-proton scattering, which is uniquely determined by the scattering angle and the total proton-proton collision energy. For the estimation of the differential cross-sections the data for elastic proton-proton scattering \([50–52]\) has been used (see left panel of Fig. 8). The integrated luminosity dependence on the excess energy is presented in right panel of Fig. 8 and its total value is equal to \( 2511 \pm 2(\text{stat.}) \pm 120(\text{syst.}) \pm 100(\text{norm.}) \text{ nb}^{-1} \), where the statistical, systematic and normalization errors are indicated, respectively \([47]\). In the calculations the shadowing effect equals 4.5% \([53]\) caused by the neutron shading the scattered protons. The total integrated luminosity is consistent within systematic and normalization errors with the luminosity determined for the current experiment based on two alternative methods presented in Refs. \([35, 54]\).

The Monte Carlo simulations for the \( pd \rightarrow \eta^0 \) process allowed one to determine detection and reconstruction efficiency as a function of the excess energy \( Q \). The obtained geometrical acceptance is equal to about 30% while the full efficiency including all applied selection criteria is about 9% (see Fig. 9).

### D. Upper limit of the total cross section

The final excitation function (Fig. 10) was obtained by correcting the number of events identified as \( pd \rightarrow \eta^0 \) for the efficiency (Fig. 9) and normalizing by the luminosity (right panel of Fig. 8). The excitation curve does not show any structure that could be interpreted as an indication for the \( \eta \)-mesic \( ^3\text{He} \).

Hence, the upper limit of the total cross-section for the \( ^3\text{He}-\eta \) bound state production and its decay to \( \eta^0 \) channel was evaluated. In order to quantitatively estimate the upper limit, a fit to the excitation function with a polynomial describing the background (first and second order) combined with a Breit-Wigner function (for the signal) was performed. In the fit the polynomial coefficients and the normalization of the Breit-Wigner amplitude were

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**FIG. 5:** The number of selected events for the \( pd \rightarrow d\pi^0 \) reaction after application of all selection criteria.

**FIG. 6:** Fermi momentum distribution of nucleons inside the deuteron for Paris (red line) \([48]\) and CDBonn (blue dotted line) \([49]\) potential models.
FIG. 7: Correlations between the polar angles of charged particles registered in the FD $\theta_{FD}$ and CD $\theta_{CD}$ obtained in the MC simulations for the $pd \rightarrow ppp_{spectator}$ (left upper panel) and $pd \rightarrow pd$ reactions (right upper panel), experimental data (left lower panel). Note that the 2D spectra are in logarithmic scale. The right lower panel shows an example of experimental distribution of $\theta_{CD}$ (black points), fitting function (cyan line), signal from $pd \rightarrow ppp_{spectator}$ reaction (orange area) and peak from background reaction $pd \rightarrow pd$ (purple area) for $Q \in (10, 12.5)$ MeV and $\theta_{FD} \in (15, 16)^\circ$. The applied cuts are marked with red lines.

FIG. 8: Left panel: differential cross sections for proton-proton elastic scattering as a function of the effective beam momentum for different values of the scattering angle $\theta^{cm}$ in the c.m. frame. Triangles show EDDA collaboration data [52]. Curves denote SAID calculations [50, 51]. The pink dotted line presents the distribution of the effective beam momentum obtained from simulations. Right panel: integrated luminosity calculated based on experimental data for quasifree $pd \rightarrow ppp_{spectator}$ reaction with statistical (black points) and systematic (red areas) errors fitted with third degree polynomial function (cyan line).
treated as free parameters, while the binding energy $B_s$ and the width $\Gamma$ were fixed in the range from $-40$ MeV to 0 MeV and from 5 MeV to 50 MeV, respectively. An example excitation function with the fit result for binding energy $-30$ MeV and width 15 MeV is presented in Fig. 10.

The obtained upper limit as a function of $B_s$ and $\Gamma$ is presented in Table I. It varies between 13 to 24 nb and depends mainly on the width of the bound state while it is not sensitive to the binding energy. The result for $B_s = -30$ MeV is shown in Fig. 11. The blue area denotes the systematic errors described in the next section. The obtained upper limit as a function of $B_s$ and $\Gamma$ is presented in Fig. 12.

The upper limit of the total cross section was determined based on the uncertainty of the amplitude obtained from the fit $\Delta \sigma_A$:

$$\sigma_{\text{upper}}^{CL=90\%}(B_s, \Gamma) = k \cdot \Delta \sigma_A,$$

where $k$ is the statistical factor equal to 1.64 corresponding to 90% confidence level (CL) as given by the Particle Data Group, PDG [55].

The upper limit obtained by averaging the results derived from fits with a background described by the linear and quadratic functions for different values of $B_s$ and $\Gamma$ is presented in Table I. It varies between 13 to 24 nb and depends mainly on the width of the bound state while it is not sensitive to the binding energy. The result for $B_s = -30$ MeV is shown in Fig. 11. The blue area denotes the systematic errors described in the next section.

![FIG. 9: Geometrical acceptance (blue triangles) and efficiency (orange circles) for the $pd \rightarrow (^3\text{He}-\eta)^{\text{bound}} \rightarrow dp\pi^0$ reaction as a function of excess energy Q.](image)

![FIG. 10: Experimental excitation function for the $pd \rightarrow (^3\text{He}-\eta)^{\text{bound}} \rightarrow dp\pi^0$ reaction as a function of excess energy Q.](image)

![FIG. 11: The upper limit at 90% confidence level of the total cross section for formation of the $^3\text{He}-\eta$ bound state and its decay via the $pd \rightarrow (^3\text{He}-\eta)^{\text{bound}} \rightarrow dp\pi^0$ reaction as a function of the width of the bound state.](image)

![TABLE I: The upper limit for the cross section for the bound state and its decay in the $pd \rightarrow (^3\text{He}-\eta)^{\text{bound}} \rightarrow dp\pi^0$ process, determined at the 90% confidence level. The values were obtained by fitting excitation curve with a Breit-Wigner function combined with the first and second order polynomial with different fixed bound state parameters, $B_s$ and $\Gamma$.](table)

| $B_s$, MeV | $\Gamma$, MeV | $\sigma_{\text{upper}}^{CL=90\%}$, nb | $B_s$, MeV | $\Gamma$, MeV | $\sigma_{\text{upper}}^{CL=90\%}$, nb |
|------------|---------------|-------------------------------|------------|---------------|-------------------------------|
| $-40$      | 5             | 19.74                         | $-20$      | 5             | 16.85                         |
| $-40$      | 10            | 16.08                         | $-20$      | 10            | 13.64                         |
| $-40$      | 20            | 15.61                         | $-20$      | 20            | 13.19                         |
| $-40$      | 30            | 17.35                         | $-30$      | 30            | 14.86                         |
| $-40$      | 40            | 20.14                         | $-40$      | 40            | 17.86                         |
| $-40$      | 50            | 23.67                         | $-50$      | 50            | 22.21                         |
| $-30$      | 5             | 17.91                         | $-10$      | 5             | 16.11                         |
| $-30$      | 10            | 14.34                         | $-10$      | 10            | 13.07                         |
| $-30$      | 20            | 13.49                         | $-10$      | 20            | 12.67                         |
| $-30$      | 30            | 14.66                         | $-30$      | 30            | 14.23                         |
| $-30$      | 40            | 16.85                         | $-40$      | 40            | 16.96                         |
| $-30$      | 50            | 19.92                         | $-50$      | 50            | 20.79                         |
E. Systematics

Systematic checks were performed just as in the previous analyses presented in Refs. [8, 38]. The upper limit of the total cross section in the pd → (³He-η)\text{bound} → dpπ⁰ reaction analysis is sensitive to the variation of the selection criteria, systematic error of the luminosity determination, and application of different theoretical models.

Changing the selection criteria applied in analysis within ±10% results in the systematic error of about 8.5%.

Overall, systematic and normalization errors of the luminosity determined based on the quasi-free pp reaction are equal to 4.8% and 4%, respectively, and are another contribution to the systematic uncertainty of the upper limit. The details of the luminosity analysis can be found in Ref. [47] (in Polish).

The description of the background with quadratic and linear functions introduces additional systematic uncertainty, which is estimated as

\[ \delta = \frac{\sigma_{\text{quad}} - \sigma_{\text{lin}}}{2} \]  

This systematic error changes from about 2% (for \( \Gamma = 5 \) MeV) to 24% (\( \Gamma = 50 \) MeV).

An important source of systematic errors comes from the assumption of the N* momentum distribution inside the ³He nucleus applied in the simulations. The current analysis was performed with the Fermi momentum distribution for N* determined for binding energy −0.53 MeV by Kelkar et al. [36, 37]. In addition, in this analysis the simulations were also performed assuming that the N* resonance in the c.m. frame moves with a momentum distribution similar to that of protons inside ³He [11] (see the blue dotted line in Fig. 2). The choice of the alternative model does not influence the experimental method but it affects the acceptance of the deuterons in the FD, which is connected with the fact that the momentum distribution of protons inside ³He is peaked at higher value with respect to the N* distribution in the N*-d system. It provides a systematic error of about 17%.

Adding the above-estimated contributions in quadrature we obtain the systematic uncertainty of the lower limit that varies from 20% to 31%. The systematic uncertainties are presented by the blue area in Fig. 11.

III. CONCLUSION

In order to search for evidence of the possible ³Heη bound state we performed measurements of the proton beam scattering on a deuteron target with the WASA-at-COSY detector. The analysis was based on the determination of the excitation function for the pd → dpπ⁰ process. The applied selection criteria were inferred from Monte-Carlo simulations based on the assumption that the N* resonance momentum in the N*×deuteron bound state is distributed according to the recent theoretical modelling in [36, 37].

A narrow resonance-like structure associated with an \( \eta \)-mesic ³He bound state was not observed. Therefore, the upper limit for the total cross sections for the pd → (³He-η)\text{bound} → dpπ⁰ process was estimated and varies from 13 to 24 nb depending on the bound state parameters \( B_s \in (0, 40) \) MeV and \( \Gamma \in (0, 50) \) MeV.

The upper limit obtained in this analysis for the pd → (³He-η)\text{bound} → dpπ⁰ reaction is about 3 times lower than the limit of 70 nb [7, 56] determined by the COSY-11 collaboration for the pd → (³He-η)\text{bound} → ³Heπ⁰ process. The limit about 24 nb found here compares with the total cross section for η meson production above threshold in dp collisions which is about 400 nb [33]. In dd collisions the limits obtained by the WASA-at-COSY Collaboration for the dd → ³Heπ⁰, dd → ³Heηπ⁻ processes (2.5–7 nb) [8, 38] compare with the total cross section 15 nb [57] for η production above threshold. These measurements provide an important constraint for models of He-η bound state production. Within the limits determined here, bound states predicted with \( \eta \)-nucleon scattering lengths about 1 fm remain a possibility.

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[1] Q. Haider and L. C. Liu, Phys. Lett. B 172 (1986) 257.
[2] F. Pheron et al., Phys. Lett. B 709 (2012) 21.
[3] V. A. Baskov et al., PoS Baldin-ISHEPP-XXI (2012) 102.
[4] R. E. Chrien et al., Phys. Rev. Lett. 60 (1988) 2595.
[5] A. Budzanowski et al., Phys. Rev. C 79 (2009) 012201.
[6] S. V. Afanasev et al., Phys. Part. Nucl. Lett. 8 (2011) 1073.
[7] P. Moskal and J. Smyrski, Acta Phys. Polon. B 41 (2010) 2281.
[8] P. Adlarson et al., Phys. Rev. C 87 (2013) 035204.
[9] N. G. Kelkar, K. P. Khemchandani, N. J. Upadhyay and B. K. Jain, Rept. Prog. Phys. 76 (2013) 066301.
[10] V. Metag, M. Nanova and E. Y. Paryev, Prog. Part. Nucl. Phys. 97 (2017) 199.
[11] S. D. Bass and P. Moskal, Rev. Mod. Phys. 91 (2019) 015003.
[12] B. Krusche and C. Wilkin, Prog. Part. Nucl. Phys. 80 (2014) 43.
[13] C. Wilkin, Eur. Phys. J. A 53 (2017) 114.
[14] M. Skurzok, arXiv:2004.13467 (2020).
[15] M. Nanova et al., Phys. Lett. B 772 (2018) 297.
[16] T. E. O. Ericson and W. Weise, Int. Ser. Monogr. Phys. 74, Oxford UP (1988).
[17] N. Barnea, B. Bazuk, E. Friedman and A. Gal, Phys. Lett. B 771 (2017) 297, Erratum: [Phys. Lett. B 775 (2017) 364].
[18] N. Barnea, E. Friedman and A. Gal, Nucl. Phys. A 968 (2017) 35.
[19] A. Fix and O. Kolesnikov, Phys. Lett. B 772 (2017) 663.
[20] J. J. Xie et al., Phys. Rev. C 95 (2017) 015202.
[21] M. Nanova et al., Phys. Lett. B 727 (2013) 417.
[22] Y. K. Tanaka et al., Phys. Rev. Lett. 117 (2016) 202501.
[23] S. D. Bass, A. W. Thomas, Phys. Lett. B 634 (2006) 368.
[24] S. D. Bass and A. W. Thomas, Acta Phys. Polon. B 45 (2014) 627.
[25] A. Anisovich et al., Phys. Lett. B 785 (2018) 626.
[26] E. Czerwinski et al., Phys. Rev. Lett. 113 (2014) 062004.
[27] R. Maier, Nucl. Instrum. Meth. A 390 (1997) 1.
[28] D. Prasuhn et al., IKP Annual Report (2006).