RELATIONAL ANALYSIS OF THE FRAUCHIGER–RENNER PARADOX AND EXISTENCE OF RECORDS FROM THE PAST

MARIJN WAAIJER & JAN VAN NEERVEN

Abstract. We present an analysis of the Frauchiger–Renner Gedankenexperiment from the point of view of the relational interpretation of quantum mechanics. Our analysis indicates that the paradox obtained by Frauchiger and Renner arises from a combination of allowing self-measurement and reasoning about other agent’s knowledge in the past without validation by surviving records. A by-product of our analysis is an interaction-free detection scheme for the existence of records from the past.

1. Introduction

In their recent paper [9], Frauchiger and Renner propose an interesting Gedankenexperiment which can be thought of as an extension of (Deutsch’s [6] extension of) the classical Wigner’s Friend paradox [18]. It describes a protocol involving two labs, \( L \) and \( L' \), operated by the ‘friends’ \( F \) and \( F' \), respectively. A spin \( \frac{1}{2} \)-particle \( S \), whose state is determined by a quantum coin \( R \), is prepared in lab \( L \) and sent to \( L' \). Subsequently the labs \( L \) and \( L' \) are measured, in suitably chosen bases, by two ‘Wigners’ \( W \) and \( W' \). Frauchiger and Renner argue that, with probability one, \( W \) will arrive at contradictory measurement outcomes if one simultaneously accepts

(Q) quantum mechanics: the rules of quantum mechanics apply to all agents;
(C) consistency: if agent \( A \) has established that “I am certain that agent \( B \) is certain that \( x = \xi \) at time \( t' \)”, then agent \( A \) can conclude that “I am certain that \( x = \xi \) at time \( t \)”.

On the basis of the paradox it is argued in [9] that (Q) and (C) are incompatible with the ‘single world assumption’ (S) that measurement outcomes are unique. Although there is no explicit reference to the time at which \( A \) has established his/her statement, scrutinising the arguments one finds that this could be a time different from \( t \). In fact, the following more precise version of (C) is actually used: if agent \( A \) has established at time \( t_0 \) that “I am certain that agent \( B \) will be certain that \( x = \xi \) at time \( t_1 \geq t_0 \)”, then at time \( t_0 \) agent \( A \) can conclude that “I am certain that \( x = \xi \) at time \( t_0 \)”.

The Frauchiger–Renner paradox has provoked intense discussion and has been analysed from various points of view [1, 3, 4, 5, 10, 13, 14, 17]. The aim of this note

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is to analyse and resolve it from the point of view of Rovelli’s relational interpretation of quantum mechanics (RQM)\(^1\) [15] (see also [8, 12, 16]). RQM is inspired by general covariance considerations in quantum gravity and extrapolates the lessons learnt from relativity, which teaches us that ‘time’ and ‘space’ are observer dependent, to quantum mechanics by arguing that also the notion of ‘state’ should be considered observer-dependent. In this view, physics is the study of consistency of the records that different observers give of the observed phenomena. These observers are allowed to have different accounts as to what their records mean and how they should be interpreted. Thus RQM keeps metaphysics and ontology to the barest minimum, based on the consistency of reports of different observers, while preserving a notion of objective reality making scientific exchange possible and meaningful. An instructive example of how this works in the case of the EPR paradox has been worked out in [16], where the tenets of RQM are eloquently summarised:

“In RQM, physical reality is taken to be formed by the individual quantum events (facts) through which interacting systems (objects) affect one another. Quantum events are therefore assumed to exist only in interactions and (this is the central point) the character of each quantum event is only relative to the system involved in the interaction. In particular, which properties any given system \(S\) has is only relative to a physical system \(A\) that interacts with \(S\) and is affected by these properties.

If \(A\) can keep track of the sequence of her past interactions with \(S\), then \(A\) has information about \(S\), in the sense that \(S\) and \(A\)’s degrees of freedom are correlated. According to RQM, this relational information exhausts the content of any observer’s description of the physical world.”

An essential point of our analysis is therefore to consider the experiment from the perspective of each agent separately, carefully keeping track of who knows what at what time, and to base all inferences exclusively on the available information at the given moment from the perspective taken. The conclusions of our analysis are twofold and may be stated as follows.

1. The Gedankenexperiment reveals no conflict between (Q) and the following restricted version (C\(_{\text{pres}}\)) of (C):
   - If at time \(t_1\) agent \(A\) has established that “I am certain that agent \(B\) is certain at time \(t\) that \(x = \xi\) at time \(t\), then at time \(t\) agent \(A\) can conclude that “I am certain that \(x = \xi\) at time \(t\).”
   (cf. Subsection 5.1.)

2. Two steps in the derivation of the Frauchiger–Renner paradox require self-descriptions, by the friends \(F\) and \(F\) respectively, and one step relies on inferences about the past of quantum mechanical systems that keep no records of their history. (cf. Subsection 5.2.)

3. The very existence of records of the measurements by \(F\) and \(F\) can lead to different predictions of certain measurement outcomes. (cf. Subsection 5.3.)

\(^1\)Such an analysis has already been carried out in [19], but we were unable to understand various points in the reasoning. Moreover the conclusions of this paper differ from ours. We leave it to the reader to decide about the merits of each approach.
It is claimed in [9] (see Table 4) that in RQM one has to sacrifice (C). However, conclusion (2) exhibits the use of implicit schemes of reasoning in [9] which are not permitted in RQM, rendering the claim unwarranted. Within different interpretations of quantum mechanics, objections in the same spirit as (2) have been put forward in [13, 17] (self-measurement) and [10] (ambiguity of the past).

Conclusion (3) is a variation on the Elitzur–Vaidman interaction-free detection scheme. It has the interesting additional feature that the records, once created, have no interaction whatsoever with the rest of the system and can nevertheless be detected. We consider this one of the main contributions of this note.

The remainder of the paper is organised as follows. In Section 2 we describe the Gedankenexperiment and summarise the main steps in the reasoning in [9]. In Section 3 we begin our analysis of the experiment in the framework of RQM by first leaving out the public announcements of the Wigners. The full experiment is analysed in Section 4. The main conclusion is that the accounts about the outcome of the experiment given by the various agents from their perspectives agree at all points with the account of an external observer. In that sense, there is no paradox at all. In the final Section 5 we critically examine the individual steps in the Frauchiger–Renner argument within the RQM formalism. This leads to the three conclusions stated above.

2. Description of the Gedankenexperiment

Following the notation of [9] we will begin by describing the Gedankenexperiment. It involves four agents: two ‘Wigners’ (W and W) and two ‘friends’ (F and F). The four agents agree beforehand on a protocol which is repeatedly run until the halting condition specified in the last step is reached. Each run consists of the following steps.

0. At \( t = 0 \) the following step has been completed: \( \overline{F} \) prepares a quantum coin \( R \) in the following superposition of the ‘tail’ and ‘head’ states:

\[
|t\rangle_R = \sqrt{\frac{2}{3}} |t\rangle_R + \sqrt{\frac{1}{3}} |h\rangle_R
\]

and measures it in the \( \{|t\rangle_R, |h\rangle_R\} \) basis. If the outcome is ‘tail’, \( \overline{F} \) sends a spin-\( \frac{1}{2} \) particle \( S \) to \( F \) in superposition state \( \frac{1}{\sqrt{2}} |\uparrow\rangle_S + \frac{1}{\sqrt{2}} |\downarrow\rangle_S \); if the outcome is ‘head’, she sends the particle in state \( |\downarrow\rangle_S \).

1. At \( t = 1 \) the following steps have been completed: \( F \) measures \( S \) in the \( \{|\uparrow\rangle_S, |\downarrow\rangle_S\} \) basis.

2. At \( t = 2 \) the following steps have been completed: \( \overline{W} \) measures the lab \( \overline{L} = \{R, \overline{F}\} \) in an orthonormal basis containing \( |\overline{ok}\rangle_{\overline{L}} \) and \( |\overline{fail}\rangle_{\overline{L}} \), where

\[
|\overline{ok}\rangle_{\overline{L}} := \frac{1}{\sqrt{2}} |h\rangle_R |h\rangle_{\overline{F}} - \frac{1}{\sqrt{2}} |t\rangle_R |t\rangle_{\overline{F}}
\]

\[
|\overline{fail}\rangle_{\overline{L}} := \frac{1}{\sqrt{2}} |h\rangle_R |h\rangle_{\overline{F}} + \frac{1}{\sqrt{2}} |t\rangle_R |t\rangle_{\overline{F}}
\]

and announces the result to everyone.
At \( t = 3 \) the following steps have been completed: \( W \) measures the lab
\( L = \{S, F\} \) in an orthonormal basis containing \( |\text{ok}\rangle_W \) and \( |\text{fail}\rangle_W \), where
\[
|\text{ok}\rangle_L := \frac{1}{\sqrt{2}} |\downarrow\rangle_S |\downarrow\rangle_F - \frac{1}{\sqrt{2}} |\uparrow\rangle_S |\uparrow\rangle_F,
\]
\[
|\text{fail}\rangle_L := \frac{1}{\sqrt{2}} |\downarrow\rangle_S |\downarrow\rangle_F + \frac{1}{\sqrt{2}} |\uparrow\rangle_S |\uparrow\rangle_F
\]
and announces the result to everyone. If \( \overline{W} \) and \( W \) have both announced
‘ok’ (the halting condition) the experiment is halted; otherwise, the protocol
is repeated.

An easy computation, reproduced below, shows that from the perspective of a fifth
external observer \( C \), in each run the halting condition is reached with probability
\( \frac{1}{12} \). It is also shown below that \( \overline{W} \) and \( W \) reach the same conclusion from their
perspectives. Therefore, \( \overline{W} \) and \( W \) agree with \( C \) that with probability one the
halting condition will be eventually met.

It should be mentioned that [9] only assumes measurements by \( \overline{W} \) and \( W \) in
orthonormal bases containing \( |\text{ok}\rangle_{\overline{W}} \) and \( |\text{ok}\rangle_W \), respectively, and that the agents
announce ‘fail’ in all cases when their measurement differs from ‘ok’. Our slightly
stronger assumption, where \( |\text{fail}\rangle_{\overline{W}} \) and \( |\text{fail}\rangle_L \) are explicitly added to the bases,
has the advantage of allowing simple explicit computations and does not affect the
conclusions of our analysis.

2.1. The paradox. Of interest is what happens in the final run of the experiment
which leads to the halting condition. In [9] it is argued that if one simultaneously
accepts the hypotheses (Q) and (C) introduced earlier, then the following assertions
hold simultaneously:

- in each run, with probability \( \frac{1}{12} \) both \( W \) and \( \overline{W} \) measure ‘ok’.
- in the final run \( W \) is certain to announce ‘fail’.

The assertion implies that with probability one the halting condition will be eventually
reached. By definition, in that round \( \overline{W} \) and \( W \) announce ‘ok’. This contradicts
the second assertion.

The argument by Frauchiger and Renner leading to the second conclusion can
be summarised in four main steps as follows:

(i) If \( F \) measures ‘tail’ at \( t = 0 \), she sends the particle in state
\( \frac{1}{\sqrt{2}} |\uparrow\rangle_S + \frac{1}{\sqrt{2}} |\downarrow\rangle_S \),
and infers that \( W \) will announce ‘fail’.

(ii) If \( F \) measures ‘up’ at \( t = 1 \), she is certain that \( F \) must have measured ‘tail’
at \( t = 0 \). Because of (i) and the consistency hypothesis (C), \( F \) therefore is certain
that \( W \) will announce ‘fail’.

(iii) If \( \overline{W} \) measures ‘ok’ at time \( t = 2 \), he infers that \( F \) must have measured the
spin to be ‘up’ at \( t = 1 \). Because of (ii), \( \overline{W} \) is then certain that \( F \) is certain that
\( W \) will announce ‘fail’. Hence by (C), \( \overline{W} \) is certain that \( W \) will announce ‘fail’.

(iv) If \( W \) hears \( \overline{W} \) announce ‘ok’ at time \( t = 2 \), so by (iii) \( W \) is certain that \( \overline{W} \) is
certain that \( W \) will announce ‘fail’. Hence by (C), \( W \) is certain to announce ‘fail’.

Here we just reproduced the main steps; for the intermediate reasoning leading to
them we refer to the original paper. An analysis from the point of view taken in
the present paper is given in the final section. There, we will argue that each of the
steps (i), (ii), (iii) is problematic: the first two because of self-reference problems
and (iii) because it involves beliefs about the past in the absence of records which need revision in the presence of records.

3. RELATIONAL ANALYSIS OF A MODIFIED GEDANKENEXPERIMENT

Before analysing the Gedankenexperiment as originally proposed by Frauchiger and Renner, we introduce a minor modification to their protocol. In the modified protocol, instead of announcing the outcome of his measurement right away, $W$ keeps it secret until the end of the run. This has the obvious advantage that no assumptions need to be made as to how the other agents should interpret the information that can be inferred from $W$’s announcement and how it affects their descriptions of the experiment. All we assume is hypothesis (Q), according to which the agents may use the rules of quantum mechanics to describe the experiment from their vantage points. Any conclusions drawn from this scenario will of course remain valid in the original Frauchiger–Renner scenario, which we consider in the next section.

We will analyse the modified Gedankenexperiment from the points of view of the agents $W$, $F$, and the external observer $C$ separately. From the points of view of $F$ and $F$ a complete analysis of the experiment is not possible: When $F$ attempts to describe the joint state of $R$, $S$, $F$, $W$, and $W$, she will run into difficulties describing $W$’s measurement of her lab $L = \{R\, F\}$, of which she is part. Describing $L$ from the view of $F$ amounts to letting $F$ perform a self-measurement; but this is to be avoided [2, 11]. Likewise, $F$ will not be able to describe the measurement by $W$ of her lab $L = \{S\, F\}$ of which she is part.

3.1. THE POINT OF VIEW OF $F$. We start by analysing $F$’s perspective until $W$ is about to perform his measurement.

We assume that $F$’s measurement of $R$ results in ‘tail’ (the case of ‘head’ being of no interest here). After the spin particle has been prepared, at time $t = 0$, $F$ describes the joint state of $R$, $S$, $F$, $W$, and $W$ as follows:

$$
|\Psi_I^{F,t=0}_{RFSTW} = |t\rangle_R |0\rangle_F \left( \frac{1}{\sqrt{2}} |\uparrow\rangle_S + \frac{1}{\sqrt{2}} |\downarrow\rangle_S \right) |0\rangle_W |0\rangle_W ,
$$

where $|0\rangle$ denote ready-to-measure states. Now $F$ measures the spin of $S$. According to $F$ this entangles the states of $S$ and $F$. The resulting joint state will be described by $F$ as

$$
|\Psi_I^{F,t=1}_{RFSTW} = |t\rangle_R \left( \frac{1}{\sqrt{2}} |\uparrow\rangle_F |\uparrow\rangle_S + \frac{1}{\sqrt{2}} |\downarrow\rangle_F |\downarrow\rangle_S \right) |0\rangle_W |0\rangle_W = |t\rangle_R |\text{fail}\rangle_L |0\rangle_W |0\rangle_W .
$$

At this point, $W$ measures the lab $L = \{R\, F\}$. The present formalism does not permit $F$ to make any prediction about $W$’s findings because $F$’s state is not included $F$’s description of the experiment.

3.2. THE POINT OF VIEW OF $W$. Next we analyse $W$’s perspective until $W$ is about to perform his measurement.
Once $R$ has been prepared and measured by $\overline{F}$ and the spin particle has been prepared, at time $t = 0$ $F$ describes the joint state of $R$, $\overline{F}$, $S$, $\overline{W}$, and $W$ as follows:

\begin{equation}
\Psi_{RFS\overline{W}W}^{F,t=0} = \left(\sqrt{\frac{2}{3}} |t\rangle_R |t\rangle_F \left(\frac{1}{\sqrt{2}} |\uparrow\rangle_S + \frac{1}{\sqrt{2}} |\downarrow\rangle_S\right) + \frac{1}{\sqrt{3}} |h\rangle_R |h\rangle_F |\downarrow\rangle_S\right) |0\rangle_F |0\rangle_W.
\end{equation}

Now $F$ measures the spin state of $S$.

If she finds $S$ to be ‘up’, the probability of which she evaluated beforehand (at $t = 0$) to be $\frac{1}{3}$, at $t = 1$ she describes the new state as

\begin{equation}
\Psi_{RFS\overline{W}W}^{F,t=1} = |t\rangle_R |t\rangle_F |\uparrow\rangle_S |0\rangle_W |0\rangle_W.
\end{equation}

Consequently she is certain that measuring $R$ and $\overline{F}$ at $t = 1$ would both result in ‘up’. Still assuming she found $S$ to be ‘up’, right after $\overline{W}$’s measurement she describes the new state as follows:

\begin{equation}
\Psi_{RFS\overline{W}W}^{F,t=2} = \left(\frac{1}{\sqrt{2}} |\text{fail}\rangle_F - \frac{1}{\sqrt{2}} |\text{ok}\rangle_F\right) |\uparrow\rangle_S |0\rangle_W |0\rangle_W.
\end{equation}

She concludes that with probability $\frac{1}{3} \times \frac{1}{3} = \frac{1}{9}$, $\overline{W}$ will have measured ‘ok’. Here she is forced to stop her analysis: At $t = 3$ her lab, of which she herself is part, is going to be measured by $W$.

In conclusion,

Before each run, $F$ evaluates the probability that $\overline{W}$ will report ‘ok’ to be $\frac{1}{6}$.

### 3.3. The point of view of $\overline{W}$

The first few steps are similar: after preparing and measuring $R$ and preparing $S$, at $t = 0$ $\overline{W}$ describes the joint state of $R$, $\overline{F}$, $S$, $F$ and $W$ as

\begin{equation}
\Psi_{RFS\overline{W}W}^{\overline{W},t=0} = \left(\frac{1}{\sqrt{3}} |t\rangle_R |t\rangle_F (|\uparrow\rangle_S + |\downarrow\rangle_S) + \frac{1}{\sqrt{3}} |h\rangle_R |h\rangle_F |\downarrow\rangle_S\right) |0\rangle_F |0\rangle_W.
\end{equation}

Then the spin particle $S$ is measured by $F$. At $t = 1$, $\overline{W}$ describes the resulting state as

\begin{equation}
\begin{align*}
\Psi_{RFS\overline{W}W}^{\overline{W},t=1} &= \left(\frac{1}{\sqrt{3}} |t\rangle_R |t\rangle_F (|\uparrow\rangle_S |\uparrow\rangle_F + |\downarrow\rangle_S |\downarrow\rangle_F) + \frac{1}{\sqrt{3}} |h\rangle_R |h\rangle_F |\downarrow\rangle_S |\downarrow\rangle_F\right) |0\rangle_W \\
&= \left(\frac{1}{\sqrt{3}} \left(\frac{1}{\sqrt{2}} |\text{fail}\rangle_F - \frac{1}{\sqrt{2}} |\text{ok}\rangle_F\right) (|\uparrow\rangle_S |\uparrow\rangle_F + |\downarrow\rangle_S |\downarrow\rangle_F) + \frac{1}{\sqrt{3}} \left(\frac{1}{\sqrt{2}} |\text{fail}\rangle_F + \frac{1}{\sqrt{2}} |\text{ok}\rangle_F\right) |\downarrow\rangle_S |\downarrow\rangle_F\right) |0\rangle_W \\
&= \left(\frac{1}{\sqrt{6}} |\text{fail}\rangle_F (|\uparrow\rangle_S |\uparrow\rangle_F + \frac{\sqrt{2}}{3} |\downarrow\rangle_S |\downarrow\rangle_F) - \frac{1}{\sqrt{6}} |\text{ok}\rangle_F |\downarrow\rangle_S |\uparrow\rangle_F\right) |0\rangle_W.
\end{align*}
\end{equation}

At this point, $\overline{W}$ measures the lab $\overline{F} = \{R, F\}$. We are interested in the scenario that $\overline{W}$ measures ‘ok’ which, on the basis of (7), he expects to happen with
probability \( \frac{1}{6} \). In that scenario, at \( t = 2 \) he describes the new state as

\[
|\Psi\rangle^{WF, t=2}_{RF SFW} = |\text{ok}\rangle_T (|\uparrow\rangle_S |\uparrow\rangle_F) |0\rangle_W.
\]

Rewriting (8) as

\[
|\text{ok}\rangle_T \left( \frac{1}{\sqrt{2}} |\text{fail}\rangle_L - \frac{1}{\sqrt{2}} |\text{ok}\rangle_L \right) |0\rangle_W,
\]

\( WF \) infers that if he measures ‘ok’, then \( W \) will report ‘ok’ with probability \( \frac{1}{2} \). Now knowing \( W \)’s outcome, at \( t = 3 \) he will describe the state by

\[
|\Psi\rangle^{WF, t=3}_{RF SFW} = |\text{ok}\rangle_T \left( \frac{1}{\sqrt{2}} |\text{fail}\rangle_L |\text{fail}\rangle_W - \frac{1}{\sqrt{2}} |\text{ok}\rangle_L |\text{ok}\rangle_W \right),
\]

In conclusion,

Before each run, \( WF \) evaluates the probability that he will report ‘ok’ to be \( \frac{1}{6} \), and that if that happens the probability that \( W \) will report ‘ok’ is \( \frac{1}{2} \). Consequently, \( WF \) expects that with probability \( \frac{11}{12} \), both he and \( W \) will report ‘ok’.

3.4. The point of view of \( W \). The step \( t = 0 \) is similar as for \( WF \) and is skipped. After the spin particle \( S \) has been created by \( F \) and measured by \( F \), \( W \) describes the joint state of \( R, F, S, F, \) and \( WF \) by

\[
|\Psi\rangle^{WF, t=1}_{RF SFW} = \left( \frac{1}{\sqrt{3}} |\uparrow\rangle_R |\uparrow\rangle_T (|\uparrow\rangle_S |\uparrow\rangle_F + |\downarrow\rangle_S |\downarrow\rangle_F) + \frac{1}{\sqrt{3}} |\downarrow\rangle_R |\downarrow\rangle_T (|\downarrow\rangle_S |\downarrow\rangle_F + |\uparrow\rangle_S |\uparrow\rangle_F) \right) |0\rangle_{TF}.
\]

(11)

\[
= \left( \frac{1}{\sqrt{3}} \left( |\text{fail}\rangle_T \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} |\text{ok}\rangle_T \right) (|\uparrow\rangle_S |\uparrow\rangle_F + |\downarrow\rangle_S |\downarrow\rangle_F) + \frac{1}{\sqrt{3}} \left( |\text{fail}\rangle_T \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} |\text{ok}\rangle_T \right) |\downarrow\rangle_S |\downarrow\rangle_F) |\text{fail}\rangle_T |\text{fail}\rangle_W - \frac{1}{\sqrt{6}} |\text{ok}\rangle_T |\text{ok}\rangle_T |\uparrow\rangle_S |\uparrow\rangle_F |0\rangle_{TF} \right).
\]

At this point, \( WF \) measures the lab \( T \). From the point of view of \( W \) this leads to the description

\[
|\Psi\rangle^{WF, t=2}_{RF SFW} = |\text{fail}\rangle_T \left( \frac{1}{\sqrt{6}} |\uparrow\rangle_S |\uparrow\rangle_F + \sqrt{\frac{2}{3}} |\downarrow\rangle_S |\downarrow\rangle_F \right) |\text{fail}\rangle_W - \frac{1}{\sqrt{6}} |\text{ok}\rangle_T |\text{ok}\rangle_T |\uparrow\rangle_S |\uparrow\rangle_F |\text{ok}\rangle_W.
\]
The preceding formula can be rewritten as
\begin{equation}
|\text{fail}\rangle_{T}\left(\frac{1}{\sqrt{6}}|\text{fail}\rangle_{L} - \frac{1}{\sqrt{2}}|\text{ok}\rangle_{L}\right) + \sqrt{\frac{2}{3}}\left(\frac{1}{\sqrt{2}}|\text{fail}\rangle_{L} + \frac{1}{\sqrt{2}}|\text{ok}\rangle_{L}\right) |\text{fail}\rangle_{W}
- \frac{1}{\sqrt{6}}|\text{ok}\rangle_{T}\left(\frac{1}{\sqrt{2}}|\text{fail}\rangle_{L} - \frac{1}{\sqrt{2}}|\text{ok}\rangle_{L}\right) |\text{ok}\rangle_{W}
= |\text{fail}\rangle_{T}\left(\frac{3}{4}|\text{fail}\rangle_{L} + \frac{1}{\sqrt{12}}|\text{ok}\rangle_{L}\right) |\text{fail}\rangle_{W}
- \frac{1}{\sqrt{6}}|\text{ok}\rangle_{T}\left(\frac{1}{\sqrt{2}}|\text{fail}\rangle_{L} - \frac{1}{\sqrt{2}}|\text{ok}\rangle_{L}\right) |\text{ok}\rangle_{W}.
\end{equation}

On the basis of this, \(W\) expects with probability \(\frac{1}{12}\) that both he and \(\overline{W}\) are going to report ‘ok’. Also, \(W\) expects \(\overline{W}\) to announce ‘ok’ with probability \(\frac{1}{12} + \frac{1}{12} = \frac{1}{6}\). Not knowing \(\overline{W}\)’s outcome, upon measuring ‘ok’ \(W\) will describe the new state as
\begin{equation}
|\Psi\rangle^{W,t=3}_{RFSF\overline{W}} = \left(\frac{1}{\sqrt{2}}|\text{fail}\rangle_{T}|\text{fail}\rangle_{W} + \frac{1}{\sqrt{2}}|\text{ok}\rangle_{T}|\text{ok}\rangle_{W}\right) |\text{ok}\rangle_{L}.
\end{equation}

In conclusion,

Before each run, \(W\) evaluates the probability that \(\overline{W}\) will report ‘ok’ to be \(\frac{1}{6}\), and the probability that both \(\overline{W}\) and \(W\) will report ‘ok’ to be \(\frac{1}{12}\).

3.5. The external point of view. We now take the point of view of an external observer \(C\) (Charlie), who only receives the measurement outcomes of \(\overline{W}\) and \(W\) but not from \(\overline{F}\) and \(F\) (in this respect \(C\) is different from the ‘super-observer’ of [10]).

When \(F\) measures \(S\), at \(t = 1\) the observer \(C\) describes the joint state of \(R, \overline{F}, S, F, \overline{W}, \) and \(W\) as
\begin{equation}
|\Psi\rangle^{C,t=1}_{RFSSF\overline{W}W} = \frac{1}{\sqrt{3}}\left(|\uparrow\rangle_{S}|\uparrow\rangle_{F} + |\downarrow\rangle_{S}|\downarrow\rangle_{F}\right) + |h\rangle_{R}|h\rangle_{\overline{F}} |\downarrow\rangle_{S} |\downarrow\rangle_{F}\right) \left(|0\rangle_{\overline{W}} |0\rangle_{W}\right).
\end{equation}

Next \(\overline{W}\) measures \(T\). At \(t = 2\) \(C\) describes the result as
\begin{equation}
|\Psi\rangle^{C,t=2}_{RFSSF\overline{W}W} = \left(|\text{fail}\rangle_{T}\left(\frac{1}{\sqrt{6}}|\uparrow\rangle_{S} |\uparrow\rangle_{F} + \sqrt{\frac{2}{3}} |\downarrow\rangle_{S} |\downarrow\rangle_{F}\right) |\text{fail}\rangle_{W}
- \frac{1}{\sqrt{6}}|\text{ok}\rangle_{T}|\uparrow\rangle_{S} |\uparrow\rangle_{F} |\text{ok}\rangle_{W}\right) |0\rangle_{W}.
\end{equation}

On the basis of this, \(C\) expects that \(\overline{W}\) will announce ‘ok’ with probability \(\frac{1}{6}\).

Then \(W\) performs his measurement and, arguing as in (13), \(C\) updates his description to
\begin{equation}
|\Psi\rangle^{C,t=3}_{RFSSF\overline{W}W} = |\text{fail}\rangle_{T}\left(\frac{3}{4}|\text{fail}\rangle_{L} |\text{fail}\rangle_{W} + \frac{1}{\sqrt{12}}|\text{ok}\rangle_{L} |\text{ok}\rangle_{W}\right) |\text{fail}\rangle_{W}
- \frac{1}{\sqrt{6}}|\text{ok}\rangle_{T}\left(\frac{1}{\sqrt{2}}|\text{fail}\rangle_{L} |\text{fail}\rangle_{W} - \frac{1}{\sqrt{2}}|\text{ok}\rangle_{L} |\text{ok}\rangle_{W}\right) |\text{ok}\rangle_{W}.
\end{equation}

On the basis of this, \(C\) expects that with probability \(\frac{1}{12}\) both \(\overline{W}\) and \(W\) report ‘ok’. We reach the following conclusion:
Before each run, $C$ evaluates the probability that $\overline{W}$ will report ‘ok’ to be $\frac{1}{6}$, and the probability that both $\overline{W}$ and $W$ will report ‘ok’ to be $\frac{1}{12}$.

4. RELATIONAL ANALYSIS OF THE Frauchiger–Renner GEDANKENEXPERIMENT

In the original Gedankenexperiment, $\overline{W}$ announces the outcome of his measurement before $W$ performs his measurement. From this announcement, he and the other agents are able to deduce various bits of new information. For instance, when $\overline{W}$ measures ‘ok’, in view of (8) he is certain that a measurement of $S$ would give ‘up’, and the other agents are certain at that point that $\overline{W}$ is certain that a measurement of $S$ would give ‘up’. In contrast to our analysis up to this point, in order to analyse how $\overline{W}$’s announcement affects everyone’s analysis we will accept the following principle:

**Hypothesis** ($C_{\text{pres}}$) (“Shared knowledge of the present”): If, at time $t = k$, agent $A$ is certain that agent $B$ is certain that a measurement of the system $X$ at that moment would result in the value $x$, then at $t = k$ agent $A$ is certain that a measurement of the system $X$ at that moment would result in the value $x$.

This hypothesis allows $A$ to infer new information from announcements made by $B$. Since $B$ could make his announcement by entering a written record in a notebook which he could pass for inspection to $A$, even from the relational point of view it is reasonable to accept this hypothesis. It reflects the way we do science and is reasonable on epistemological grounds in that it offers the possibility to check our beliefs by actually performing a measurement of $X$ at $t = k$ (although admittedly this may change our description of the state and we may not be able to resume the experiment in its original state).

Let us first take the perspective of $\overline{W}$ and assume that he measures ‘ok’. He then describes the state of $R, F, S, F, W$ by (8), i.e.,

$$|\Psi\rangle_{W,t=2} = |\text{ok}\rangle_T |\uparrow\rangle_S |\uparrow\rangle_F |0\rangle_W.$$  

When $W$ also reports ‘ok’, $\overline{W}$ uses hypothesis ($C_{\text{pres}}$) to update his description at $t = 3$ to

$$|\Psi\rangle_{W,t=3} = |\text{ok}\rangle_T |\text{ok}\rangle_L |\text{ok}\rangle_W.$$  

From this he concludes that a measurement of $S$ and $F$ at $t = 3$ will give ‘up’ and ‘down’ with equal probability $\frac{1}{2}$.

From the perspective of $W$, when $\overline{W}$ announces ‘ok’, hypothesis ($C_{\text{pres}}$) allows him to update (12) and (13) to

$$|\Psi\rangle_{RFSFW} = - |\uparrow\rangle_S |\uparrow\rangle_F |\text{ok}\rangle_T |\text{ok}\rangle_W$$

$$= - \left( \frac{1}{\sqrt{2}} |\text{fail}\rangle_L - \frac{1}{\sqrt{2}} |\text{ok}\rangle_L \right) |\text{ok}\rangle_T |\text{ok}\rangle_W.$$  

In the event $W$ also measures ‘ok’, he updates his perspective to

$$|\Psi\rangle_{RFSFW} = |\text{ok}\rangle_L |\text{ok}\rangle_T |\text{ok}\rangle_W$$

and therefore $W$ will be convinced that a measurement of $S$ at $t = 3$ would result in ‘up’ and ‘down’ with equal probability $\frac{1}{2}$.
Similarly, upon hearing the announcement ‘ok’ from $\overline{W}$, the external observer $C$ uses ($C_{\text{pres}}$) to update (16) to

$$\langle \Psi \rangle_{t=2}^{C,R,F,S,W} = - |\uparrow\rangle_F |\overline{\text{ok}}\rangle_T |\overline{\text{ok}}\rangle_W |0\rangle_W,$$

and, when $W$ also announces ‘ok’, he uses hypothesis ($C_{\text{pres}}$) once more to arrive at

$$\langle \Psi \rangle_{t=3}^{C,R,F,S,W} = |\text{ok}\rangle_L |\overline{\text{ok}}\rangle_T |\overline{\text{ok}}\rangle_W |\text{ok}\rangle_W.$$

Accepting ($C_{\text{pres}}$) we reach the following conclusion:

If $\overline{W}$ announces ‘ok’, at $t = 2$ the agents $\overline{W}$, $W$, and $C$ expect that if they were to measure $S$ this would result in ‘up’. At $t = 2$ they also expect that $W$ will measure ‘ok’ with probability $\frac{1}{2}$. In that scenario, at $t = 3$ they expect to find $S$ in states ‘up’ and ‘down’ with probability $\frac{1}{2}$.

Inspecting various conclusions in this section and the previous one, no Frauchiger–Renner paradox has arisen so far.

5. DISCUSSION

Our analysis of the original Frauchiger–Renner Gedankenexperiment in Section 4, as well as that of the modified version studied in Section 3, reveals that in all three scenarios the involved agents provide consistent records about the various issues at stake. Thus the Gedankenexperiment reveals no inconsistency between hypothesis (Q) on the validity of quantum mechanics and hypothesis ($C_{\text{pres}}$) on sharing knowledge about the present.

Let us now revisit the steps (i), (ii), (iii) of Frauchiger and Renner’s analysis.

5.1. Discussion of steps (i) and (ii): Being measured. Frauchiger and Renner claim (see statement $F^0_{\text{fail}}$ in Box 3 in [9]) that by (Q),

“If $F$ measures ‘tail’, at $t = 0$ $F$ is certain that $W$ will announce ‘fail’ at $t = 3’.”

This is step (i) in the sketch of their argument given in Subsection 2.1. From the relational point of view this reasoning is problematic for reasons of self-reference: $\overline{F}$ is part of the lab that is being measured by $\overline{W}$ at time $t = 2$ and consequently she is not able to describe this measurement from her point of view. Because of this, she is unable to make predictions about the joint state of $R$, $S$, $F$, $\overline{W}$, and $W$ at times $t \geq 2$.

One could try to get around this by agreeing to consider $\overline{W}$ and $W$ as external agents and permit $\overline{F}$ to keep track of the joint state of $R$, $S$, and $F$ only. Let us analyse what happens from $\overline{F}$’s perspective in this “subplot” assuming her measurement of $R$ has given ‘tail’. Arguing as in (2), at time $t = 1$ (and then also at time $t = 2$, since $\overline{W}$ is no longer in the plot) she describes the joint state of $R$, $S$, and $F$ as

$$\langle \Psi \rangle^{\overline{F},t=1}_{R,S,F} = \langle \Psi \rangle^{\overline{F},t=2}_{R,S,F} = |t\rangle_R \left( \frac{1}{\sqrt{2}} |\uparrow\rangle_F |\uparrow\rangle_S + \frac{1}{\sqrt{2}} |\downarrow\rangle_F |\downarrow\rangle_S \right) = |t\rangle_R |\text{fail}\rangle_L.$$
On the basis of this, $F$ could argue at $t = 1$ that $W$ will announce ‘fail’ at $t = 3$ (and thus obtain the Frauchiger–Renner paradox). It is not clear, however, how $F$ could arrive at this conclusion on the basis of (Q). Indeed, because she cannot model $W$’s actions, she cannot use (Q) to argue why they can be left out from the plot.

Statement $F_n^{02}$ is used in [9] to deduce that if $F$ finds ‘up’, then $F$ is certain at $t = 1$ that $W$ will observe ‘fail’ at $t = 3$ (see statement $F_n^{14}$ on Box 3 in [9]). This is step (ii) in the sketch of their argument given in Subsection 2.1. It suffers from the same self-reference problem: the formalism does not permit $F$ to describe $W$’s measurement on the lab of which $F$ herself is part. Near the end of the next subsection we will show that the conclusions drawn from $F_n^{14}$ are actually invalid.

5.2. Discussion of step (iii): Knowing the past. Steps (ii) and (iii) of the Frauchiger–Renner argument employ assertions of the following format:

\[ \text{If at time } t \text{ agent } A \text{ knows } p, \text{ then at time } t \text{ agent } A \text{ is certain that } \text{agent } B \text{ knew } q \text{ at time } t' \leq t. \]

Are assertions of this type to be admitted in scientific reasoning? If taken literally they belong to the domain of metaphysics, for one cannot check their truth (at least not under (Q)) by time travelling back to $t = k$ and asking $B$ if he really knew. They can only be made into meaningful and testable statements if there are surviving records of $B$’s thoughts, for instance in the form of an entry in a notebook authored by $B$ at $t = k$. The notebook can be accepted by $A$ at time $t = l$ to be a reflection of $B$’s thoughts at time $t = k$. In this process the metaphysical statement “$A$ is certain that $B$ knew $q$ at time $t = k$” is reinterpreted as the scientific statement “$A$ inspects $B$’s notebook at time $t = l$ and finds the entry $q$”.

Frauchiger and Renner employ assertions of the above format in a non-trivial way in at least two places, namely in their derivations of steps (ii) and (iii), through the statements $F_n^{12}$ and $W_n^{22}$ (cited below) in Table 3 of [9] respectively. If one gives these statements an operational meaning by equipping the agents with notebooks and re-interpreting the statements accordingly, it turns out that that $F_n^{12}$ can indeed be justified, in the sense that one arrives at the same statement on the basis of the written records, but $W_n^{22}$ cannot: a different conclusion is reached on the basis of these records.

Let us now turn to the mathematical details and begin with a look at the first line of step (ii):

Statement $F_n^{12}$: If $F$ measures ‘up’, then at $t = 1$ she is certain that $F$ must have measured ‘tail’ at $t = 0$.

This is statement $F_n^{12}$ in Table 3 of [9] and is of the format discussed above. We have seen that, upon measuring $S$ to be ‘up’, agent $F$ updates her description of the system to (4), i.e.,

\[ |\Psi\rangle_{RFSW} = |t\rangle_R |t\rangle_F |\uparrow\rangle_S |0\rangle_W |0\rangle_W. \]

Hence she is certain that if she herself were to measure $R$ at time $t = 1$ the outcome would be ‘tail’. The statement that, on the basis of this, she is certain that $F$ must have measured ‘tail’ at $t = 0$ is only meaningful in the presence of a surviving record of $F$’s measurement. As an aside, notice that the particle $S$ itself cannot play the role of this record: for if it could, it would serve also as a record when $F$ measures...
This provides the justification of $F$’s description of the system is given by
\begin{equation}
|\Psi_{F, t=1}^{F, t=1} \rangle_{\overline{N} \overline{F} \overline{S} \overline{W} W} = \left( \frac{1}{\sqrt{2}} |t_R \rangle_{\overline{F}} |tF \rangle_{\overline{F}} \right) \left( |\downarrow \rangle_{F} |0 \rangle_{W} + |\uparrow \rangle_{F} |1 \rangle_{W} \right) = |\text{fail} \rangle_{\overline{F}} |\downarrow \rangle_{S} |0 \rangle_{W} |0 \rangle_{W},
\end{equation}
and nothing can be recovered from it about $F$’s measurement of $R$ at $t = 0$.

Thus we propose to extend the protocol by introducing a notebook $\overline{N}$ in which $F$ writes down the result of her measurement at $t = 0$. (Likewise, $F$ needs a notebook $N$ in step (iii); see below). The assertion that $F$ is certain that $\overline{F}$ must have measured ‘tail’ at $t = 0$ can then be taken to mean that $\overline{F}$ is certain that an inspection of the notebook $\overline{N}$ at time $t = 1$ will reveal that it contains the entry ‘tail’ (cf. the interpretation of the Gedankenexperiment from the point of view of QBism in [9]).

Redoing the derivation of (4) with the notebook $\overline{N}$ added we arrive at
\begin{equation}
|\Psi_{\overline{N} \overline{F}, t=1}^{\overline{F}, t=1} \rangle_{\overline{F} \overline{S} \overline{W} W} = |t_{\overline{F}} \rangle_{\overline{F}} |tF \rangle_{\overline{F}} |\uparrow \rangle_{S} |0 \rangle_{W} |0 \rangle_{W}.
\end{equation}
This provides the justification of $F^{n;2}$.

Turning to the analysis of step (iii), consider the statement
\begin{equation}
\text{Statement } \overline{W}^{n;2}: \text{ If } \overline{W} \text{ measures ‘up’, then at } t = 2 \text{ he is certain that } F \text{ must have measured ‘up’ at } t = 1.
\end{equation}
This is statement $\overline{W}^{n;2}$ in Table 3 of [9] and again it is of the format discussed at the beginning of this subsection. Providing $\overline{F}$ and $F$ with notebooks $\overline{N}$ and $N$, the description at time $t = 1$ given by $\overline{W}$ becomes
\begin{equation}
|\Psi_{\overline{N} \overline{F}, t=1}^{\overline{F}, t=1} \rangle_{\overline{F} \overline{N} \overline{S} \overline{F} W} = \left( \frac{1}{\sqrt{3}} |t_{\overline{N}} \rangle_{\overline{F}} |t \rangle_{\overline{F}} \left( |\uparrow \rangle_{F} |\uparrow \rangle_{S} |F \rangle + |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle \right) + \frac{1}{\sqrt{3}} |\text{ok} \rangle_{\overline{F}} |\downarrow \rangle_{S} |F \rangle \right) |0 \rangle_{W} = \left( \frac{1}{\sqrt{6}} |\downarrow \rangle_{\overline{F}} \left( \frac{1}{\sqrt{2}} |\text{fail} \rangle_{\overline{F}} - \frac{1}{\sqrt{2}} |\text{ok} \rangle_{\overline{F}} \right) \left( |\uparrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle + \frac{1}{\sqrt{3}} \left( |t_{\overline{N}} \rangle_{\overline{F}} + |\text{ok} \rangle_{\overline{F}} \right) \left( |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle - \frac{1}{\sqrt{3}} \left( |t_{\overline{F}} \rangle_{\overline{F}} |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle - \frac{1}{\sqrt{3}} \left( |t_{\overline{F}} \rangle_{\overline{F}} |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle \right) \right) |0 \rangle_{W}.
\end{equation}
If the subsequent measurement of $\overline{F}$ gives ‘ok’, at $t = 2$ he updates this to
\begin{equation}
|\Psi_{\overline{N} \overline{F}, t=2}^{\overline{F}, t=2} \rangle_{\overline{N} \overline{F} \overline{S} \overline{F} W} = \left( \frac{1}{\sqrt{3}} \left( |h_{\overline{N}} \rangle_{\overline{F}} - |t_{\overline{N}} \rangle_{\overline{F}} \right) |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle - \frac{1}{\sqrt{3}} \left( |t_{\overline{F}} \rangle_{\overline{F}} |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle \right) \right) |0 \rangle_{W}.
\end{equation}
Note the difference with (8), i.e.,
\begin{equation}
|\Psi_{\overline{N} \overline{F}, t=2}^{\overline{F}, t=2} \rangle_{\overline{N} \overline{F} \overline{S} \overline{F} W} = \left( \frac{1}{\sqrt{3}} \left( |h_{\overline{N}} \rangle_{\overline{F}} - |t_{\overline{N}} \rangle_{\overline{F}} \right) |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle - \frac{1}{\sqrt{3}} \left( |t_{\overline{F}} \rangle_{\overline{F}} |\downarrow \rangle_{F} |\downarrow \rangle_{S} |F \rangle \right) \right) |0 \rangle_{W}.
\end{equation}
where the analogous term to the first term on the right-hand side of (29) disappeared by cancellation. Due to the presence of $F$’s notebook $N$, this cancellation doesn’t happen in (29) and $\overline{W}$ can no longer be sure that $F$’s notebook $N$ contains the entry ‘up’. In this testable sense, he therefore he cannot claim to “be certain at $t = 2$ that $F$ must have measured ‘up’ at $t = 1$”.

This means that $\overline{W}^{n:22}$ is false if it is interpreted as a testable statement about the enlarged system that keeps records. We take the point of view that this is the only meaningful interpretation of $\overline{W}^{n:22}$. One could try to maintain the validity of $\overline{W}^{n:22}$ as a true statement about the original system without notebooks while at the same time accepting (29) as a true statement about the enlarged system with notebooks. But in the absence of records $\overline{W}^{n:22}$ becomes a metaphysical statement. The labs $L$ and $L$ are entangled at the moment of $W$’s measurement (from $W$’s perspective, by (7)), and therefore the measurement of $L$ is in fact a measurement of the joint system comprised of $L$ and $L$ which erases the memory that $L$ and $L$ held about the state of $S$ at time $t = 1$. At $t = 2$, $\overline{W}$ has no way of testing the truth of $\overline{W}^{n:22}$ by performing measurements on $L$ and $L$. All that (8) and (30) tell us is that $\overline{W}$ is certain that if he were to measure $S$ at time $t = 2$ he would find ‘up’.

We conclude the analysis with a final remark about (29). It is of interest to note that the non-cancellation disappears if only $F$ is allowed to keep a notebook. Apparently, the existence of recorded information about $R$ makes all the difference, even though statement $\overline{W}^{n:22}$ contains no reference to $R$ whatsoever. But if only $F$ gets a notebook we run into problems in the earlier analysis of step (ii) where we needed $F$’s notebook to interpret statement $F^{n:12}$. One and only one protocol should describe the entire experiment, and therefore we are forced to equip both $F$ and $F$ with notebooks.

5.3. Interaction-free detection of records. Comparison of (29) and (30) reveals a deeper issue. What does $\overline{W}$ expect to see if he were to enter lab $L$ and measure $S$ at $t = 2$? In the original system without notebooks he is certain to find ‘up’, while in the enlarged system with notebooks the probability of finding ‘up’ is down to $\frac{1}{3}$! Apparently the mere existence of the records influences the outcome. Puzzling as this seems, one has to keep in mind that we are comparing statements about different quantum mechanical systems.

This conundrum can be formulated as an interaction-free detection in the spirit of [7]. Suppose that, after agreeing on the Frauchiger–Renner protocol (part of the agreement being that no notebooks will be kept), $F$ decides to cheat, takes a hidden notebook from her pocket, and records the outcome secretly. When $\overline{W}$ measures $S$ at $t = 2$ he is convinced that (30) gives the correct description and therefore expects to see ‘up’ with probability one. Much to his surprise, this happens only in one third of the rounds; in two thirds of the rounds he measures ‘down’. Then he realises that the secret use of a notebook by $F$ would lead to (29) and, therefore, that he was able to detect the existence of the secret record inside lab $L$ by performing measurements inside lab $L$.

5.4. Conclusion. From the point of view of RQM the Frauchiger–Renner paradox disappears. All beliefs that various agents have at given moments time are consistent with those of an external observer. The ‘paradox’ arises from a combination of
implicit use of self-measurements and reasoning on the basis of inferences about the past which do not stand up if records are kept. In the final subsection we showed that the Frauchiger–Renner Gedankenexperiment provides an instance where the mere existence of records influences the probabilities of measurement outcomes.

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References

[1] Baumann, V., Hansen, A., & Wolf, S. The measurement problem is the measurement problem is the measurement problem. arXiv:1611.01111.
[2] Breuer, T. (1993). The impossibility of accurate state self-measurements. Philosophy of Science, 62: 197-214.
[3] Brukner, C. (2018). A no-go theorem for observer-independent facts. Entropy 20: 350.
[4] Bub, J. (2017). Why Bohr Was (Mostly) Right. arXiv:1711.01604.
[5] Bub, J. (2018). In defense of a “single-world” interpretation of quantum mechanics. Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics.
[6] Deutsch, D. (1985). Quantum theory as a universal physical theory. Int. J. Theor. Phys. 24: 1-41.
[7] Elitzur, A. C., & Vaidman, L. (1993). Quantum mechanical interaction-free measurements. Foundations of Physics, 23(7), 987-997.
[8] Fraassen, B. C. van (2010). Rovelli’s world. Foundations of Physics, 40(4), 390-417.
[9] Frauchiger, D., & Renner, R. (2018). Quantum theory cannot consistently describe the use of itself. Nature communications, 9(1), 3711.
[10] Laloe, F (2018). Can quantum mechanics be considered consistent? A discussion of Frauchinger and Renner’s argument. arXiv:1802.06396.
[11] Laudisa, F. (2001). The EPR Argument in a Relational Interpretation of Quantum Mechanics. Foundations of Physics Letters, 14: 119-132.
[12] Laudisa, F., & Rovelli, C. (2010). Relational quantum mechanics. Stanford Encyclopedia of Philosophy.
[13] Lazaroñici, D., & Hubert, M. (2018). How Quantum Mechanics can consistently describe the use of itself. arXiv:1809.08070.
[14] Rafaño, A. (2018). Decoherence allows quantum theory to describe the use of itself. arXiv:1810.07065.
[15] Rovelli, C. (1996). Relational quantum mechanics. International Journal of Theoretical Physics, 35(8), 1637-1678.
[16] Smerlak, M., & Rovelli, C. (2007). Relational EPR. Foundations of Physics, 37(3), 427-445.
[17] Sudbery, A. (2017). Single-world theory of the extended Wigner’s friend experiment. Foundations of Physics, 47(5): 658-669.
[18] Wigner, E. (1961). Remarks on the mind-body question. In: Good, I. (ed.) The Scientist Speculates. Heinemann, London.
[19] Yang, J. M. (2018). Consistent Descriptions of Quantum Measurement. arXiv:1812.00985.