Graph Learning for Anomaly Analytics: Algorithms, Applications, and Challenges

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Anomaly analytics is a popular and vital task in various research contexts that has been studied for several decades. At the same time, deep learning has shown its capacity in solving many graph-based tasks, like node classification, link prediction, and graph classification. Recently, many studies are extending graph learning models for solving anomaly analytics problems, resulting in beneficial advances in graph-based anomaly analytics techniques. In this survey, we provide a comprehensive overview of graph learning methods for anomaly analytics tasks. We classify them into four categories based on their model architectures, namely graph convolutional network, graph attention network, graph autoencoder, and other graph learning models. The differences between these methods are also compared in a systematic manner. Furthermore, we outline several graph-based anomaly analytics applications across various domains in the real world. Finally, we discuss five potential future research directions in this rapidly growing field.

CCS Concepts:
- General and reference → Surveys and overviews;
- Theory of computation → Theory and algorithms for application domains;
- Computing methodologies → Neural networks;

Additional Key Words and Phrases: Anomaly analytics, anomaly detection, graph learning, graph neural networks, deep learning

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1 INTRODUCTION

Anomalies, which are also known as outliers, commonly exist in various real-world networks [12], such as fake reviews in opinion networks [120], fake news in social networks [118], outlier members in collaboration networks [94, 117], flash crowds in traffic networks [50], socially selfish nodes in mobile networks [109], and network intrusions in computer networks [24]. The exploration of
anomaly detection research dates back to the 1960s, and it has been a popular research field for several decades [35]. With the increasing demand and broad applications in different domains, anomaly analytic plays an increasingly important role in various communities such as data mining and machine learning.

With the advancement of deep learning, graph learning is proposed subsequently, which is coined for deep learning–based models that are applied into graph-structured data [111, 127]. Due to its convincing performance and explainability, recent years have witnessed, in varied disciplines, an increasing number of studies focusing on anomaly detection and prediction tasks by utilizing deep graph models [99, 136], which is not limited to shallow embedding such as random walks [40, 110]. As a unique non-Euclidean data structure, graphs are able to represent entities and their relationships in different kinds of scenarios. However, this research direction faces several inevitable problem complexities to all detection methods when applying deep learning and artificial intelligence in real-world networks [57, 104].

- **Irregularity of graph structure.** Unlike other regular structured data, such as text, sequences, and images, nodes in a graph are unordered and can have distinct neighborhoods, which makes the structure of graphs irregular. Therefore, some traditional deep learning architectures cannot be directly applied, such as convolution and pooling operation in convolutional neural networks [72].
- **Heterogeneous anomaly classes.** The types of nodes and links are generally not unitary in a graph, which leads to the emergence of heterogeneous information networks (HINs). HINs usually incorporate more complex information among entities and relationships, especially those containing different modalities [85], which are very important in identifying different types of anomalies in a specific graph.
- **Scalability to real-world networks.** Nowadays, real-world networks such as social networks are composed of millions or even billions of nodes, edges, and attribute information [112]. This kind of large-scale network definitely increases computational complexity. Therefore, it is imperative to devise scalable models having a linear time complexity with respect to the graph size.
- **Label scarcity.** Compared with manually generated graph data, there are mainly two reasons for the sparsity of real-world networks. The first one is the scale-free network structure nature that the degree of nodes in most real-world networks follows long-tailed distribution [122]. The other one is limited by the collection technology and privacy protection in the process of crawling data. Moreover, due to the lack of labeled datasets, devising unsupervised anomaly detection models is becoming important.
- **Diverse types of anomalies.** Several types of anomalies have been explored such as node, edge, subgraph, and path (shown in Figure 2). Node anomalies are entities that show anomalous behaviours in the whole graph compared with other nodes, e.g., users who spread fake news in social networks. Other types of anomalies have similar concepts and their own real-world applications. Here subgraph anomaly is difficult to detect, because the individual nodes could show normal behaviours when extracted from an anomalous subgraph.

There have been a line of deep anomaly detection research demonstrating significantly better performance than conventional models on solving the above-mentioned challenges. Despite the fact that the adopted technologies vary from Graph Convolution Networks (GCNs) to Graph AutoEncoder (GAEs), most methods focus on detecting or predicting an anomaly in a specific situation due to the complexity of existing anomalies. To the best of our knowledge, little attention has been devoted to summarizing these methods in a comprehensive way and clearly analyzing how they are applied to solve real-world application scenarios.
1.1 Related Surveys and Novelty

There are several surveys related to our work. Zamini et al. [121] summarized the anomaly detection techniques in four real-world application scenarios, namely banking, wireless sensor networks, social networks, and healthcare. Akoglu et al. [3] reviewed the anomaly detection methods using graph metric-based techniques. Ranshous et al. [78] only focused on anomaly detection methods in dynamic networks, while Bilgin et al. [8] briefly reviewed some non-deep learning methods of detecting anomalies in dynamic networks. Both Chalapathy et al. [11] and Pang et al. [75] concentrated on deep learning enabled anomaly detection in different kinds of data, which is not limited to graph data. Reference [67] reviewed the contemporary deep learning methods for graph anomaly detection and categorized existing work according to the anomalous graph objects. Actually, there are also some surveys that focused on introducing the main concepts and frameworks of Graph Neural Networks (GNNs) [108, 136] and divided the corresponding methods according to the type of GNN models. Inspired by this classification strategy, we also divided the graph learning models in terms of the model type when introducing the specific anomaly detection tasks. However, the main focus of our survey and GNN survey are totally different in spite of the similar classification strategy.

This work is different from previous studies in that we aim to summarize the graph learning methods systematically and comprehensively for detecting anomalies in various graphs, ranging from homogeneous to heterogeneous, non-attributed to attributed, undirected to directed, rather than focusing on only one specific kind of graph. To fill this gap, we divide the existing methods into four categories based on their model architectures and training strategies: GCNs, Graph Attention Networks (GATs), GAEs, and other GNN-based methods (shown in Figure 1). The main characteristics of these methods are compared and summarized in Table 1. The characteristics of these basic models are briefly introduced in Section 2. In summary, the contributions of this work are outlined as follows:

- A systematic summarization and comparison of graph learning methods for anomaly analytics is presented. Specifically, we delineate their capabilities in addressing the existing problem complexities among all categories of the methods.
- An overview of major anomaly analysis tasks in various application domains is given.
- Insights into future research directions in this field are provided.

1.2 Organization

The rest of this survey is structured as follows. Section 2 presents the notations and preliminaries of graph learning models, which will be used in the subsequent sections. The anomaly analytics methods are reviewed in Sections 3 to 6. In Section 7, we outline several real-world applications.
Table 1. Summary of Graph Learning Models in Detecting and Predicting Anomalies

| Type   | Method       | Graph Type       | Anomaly Type | Dataset                  | Application                       |
|--------|--------------|------------------|--------------|--------------------------|-----------------------------------|
| GCN    | GEM [62]     | HIN              | Node         | Karate, Dolphin, Jazz, US Power grid, Ego-Facebook\(^1\) | Malicious account                 |
|        | GCNSI [26]   | Undirected network | Node         | Cora, PubMed, PolBlog [76] | Rumor source detection            |
|        | GAS [54]     | HIN              | Node\&Edge   | BlogCatalog [102], Flickr [89], ACM [88] | —                                 |
|        | SpecAE [56]  | Attributed networks | Node         | —                        | Spam review detection             |
|        | DOMINANT [22] | Attributed networks | Node         | —                        | —                                 |
|        | GCNwithMRF [107] | Directed graph | Node         | TwitterSH [53], iKS-10KN [115] | Social spammer detection          |
|        | Bi-GCN [7]   | —                | Edge         | Weibo [65], Twitter [66] | Rumor detection                   |
|        | GCAN [63]    | Weighted graph   | Node         | Twitter                  | Fake news detection               |
|        | TPC-GCN [133] | HIN              | Node         | Weibo [65], Reddit [37]  | Controversy detection             |
|        | AANE [29]    | —                | Edge         | Disney, Enron\(^7\)      | —                                 |
|        | HMGN [141]   | Vanilla graph    | Node         | —                        | Fraud invitation                  |
|        | GraphRH [126] | Bipartite Graph  | Node         | Yelp [79], Amazon [70]   | —                                 |
|        | AddiGraph [136] | Dynamic graph | Edge         | UC [73], Digg [18]       | —                                 |
|        | ST-GCN [58]  | ST Graph         | Graph        | Shanghai tech [64]       | Anomalous action                  |
|        | SpecAE [56]  | Temporal Graph   | Node         | UCL, Digg [18]           | —                                 |
|        | ANEMONE [45] | —                | Node         | Cora, Citeseer, PubMed   | —                                 |
|        | CoLA [60]    | Attributed network | Node         | [102], [89], [88]        | —                                 |
|        | GCAD [15]    | Attributed network | Node         | Aminer, MAS, Alpha, Yelp | —                                 |
| GAT    | HAGNE [100]  | Vanities graph   | Graph        | —                        | Unknown malware                   |
|        | HACULI [41]  | Attributed HINs  | Node         | —                        | Cash-out user detection           |
|        | SemiGNN [95] | Multiview graph  | Node         | —                        | Financial fraud                   |
|        | AA-HGNN [81] | HINs             | Node         | BuzzFeed\(^4\)           | Fake news detection               |
|        | mHGNN [32]   | Attributed HINs  | Subgraph     | —                        | Illicit traded product            |
|        | GLN [19]     | Directed graph   | Node         | SWaT [69], WADI [1]      | Anomalous sensors                 |
|        | TGBULLY [34] | Temporal graph   | Subgraph     | Instagram [39], Vine [77] | Cyberbullying detection           |
|        | TADDY [61]   | Dynamic graph    | Node         | Email\(^*\), AS-Topology\(^*\) | —                                 |
| GAE    | AEHE [31]    | HINs             | Path         | ACM [68]                 | Co-authored event                 |
|        | AEGIS [22]   | Attributed networks | Node         | BlogCatalog, Flickr, ACM | —                                 |
|        | DONE [6]     | Attributed network | Node         | Cora, Citeseer, PubMed\(^8\) | —                                 |
|        | DeepSphere [90] | Dynamic networks | Node         | NYC taxi trip\(^*\), HERMEVENT [20] | —                                 |
|        | UCD [17]     | Attributed networks | -            | Instagram [39], Vine [77] | Cyberbullying detection           |
|        | SL-GAD [10]  | Attributed network | Node         | Cora, Citeseer, PubMed\(^7\) | —                                 |
|        | Other        | Bipartite graph  | Node         | Bitcoin-Alpha [52], Tencent-Weibo [44] | —                                 |
|        | CARE [27]    | Multi-relation graph | Node         | Yelp, Amazon             | Camouflaged fraudsters            |
|        | Meta-GDN [23] | Cross-network    | Node         | PubMed [83], Reddit [36] | —                                 |
|        | GAAN [15]    | Attributed network | Node         | BlogCatalog, Flickr, ACM | —                                 |
|        | MAHINDER [134] | Multi-view HINs | Node         | —                        | Financial defaulter               |

\(^1\)http://www-personal.umich.edu/~mejn/netdata/ & http://snap.stanford.edu/.
\(^2\)https://www.ipd.kit.edu/~muellere/consub/.
\(^3\)https://www.cs.cmu.edu/~./enron/.
\(^4\)https://github.com/KaiDMML/FakeNewsNet/tree/old-version.
\(^5\)http://networkrepository.com/email-dnc.
\(^6\)http://networkrepository.com/tech-as-topology.
\(^7\)https://linqs.org/datasets/.
\(^8\)https://portal.311.nyc.gov/.
of anomaly analytics that can be solved with deep graph models and discuss some future research directions and challenges in Section 8. Finally, we briefly conclude this survey in Section 9.

2 NOTATIONS AND PRELIMINARIES

2.1 Notations

A graph is represented as $G = (V, E)$, where $V = \{v_1, \ldots, v_n\}$ is a set of $n$ nodes and $E \subseteq V \times V$ is a set of $m$ edges between nodes. A graph may have different types, such as weighted or unweighted, directed or undirected. Here, if a graph is directed, then $e_{ij} = (v_i, v_j) \in E$ denotes an edge pointing from $v_i$ to $v_j$. The neighborhood set of a node $v_i$ is defined as $N(v_i) = \{v_j \in V | (v_i, v_j) \in E\}$. The adjacency matrix of a graph is a $n \times n$ matrix, which is denoted as $A$. We use $A(i, \cdot), A(\cdot, j), A(i, j)$ to denote the $i$th row, $j$th column, and an element of $A$, respectively. For an unweighted graph, the element of its adjacency matrix is defined as

$$A(i, j) = \begin{cases} 1 & \text{if } e_{ij} \in E \\ 0 & \text{otherwise} \end{cases}. \quad (1)$$

For a weighted graph, $A(i, j)$ is defined as the weight of edge $e_{ij}$. A graph may have node attributes $X^V$ and edge attributes $X^E$, where $X^V$ is the node attributes matrix and $X^E$ is the edge attributes matrix, respectively. If the feature matrix is used as $X$ for convenience, then the default setting $X$ refers to node attributes matrix. Functions are marked with curly braces, e.g., $\mathcal{F}(\cdot)$.

Throughout this article, we use bold uppercase characters to denote matrices and bold lowercase characters to represent vectors, like a matrix $A$ and a vector $a$. Unless particularly specified, the notations used in this article are illustrated in Table 2. Then, we provide a formal definition and

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**Table 2. Commonly Used Notations**

| Notations | Descriptions |
|-----------|--------------|
| $G = (V, E)$ | A graph. |
| $N(v)$ | The neighbors of a node $v$. |
| $A$ | The graph adjacency matrix. |
| $D$ | The diagonal degree matrix. |
| $X$ | The graph feature matrix. |
| $D_{ii} = \sum_{j=1}^{n} A_{ij}$ | The degree of node $i$. |
| $L = D - A$ | The Laplacian matrix. |
| $U$ | The eigenvector matrix of Laplacian matrix. |
| $\Lambda$ | The eigenvalue matrix of Laplacian matrix. |
| $A^T$ | The transpose of the matrix $A$. |
| $A^n$ | The $n$th power of $A$. |
| $H^{(l)}$ | The hidden representation in the $l$th layer. |
| $W$ | The weight parameter matrix. |
| $b$ | The bias parameter vector. |
| $Z$ | The generated node embedding matrix. |
| $\Theta$ | Learnable parameters. |
| $\| \cdot \|$ | The concatenation of two vectors. |
| $| \cdot |$ | The length of a set. |

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1 Graph and network are used interchangeably in this article.
Fig. 2. Illustration of the whole process of detecting anomalies in graph data with deep graph models. The models are mainly divided into two parts according to whether anomaly score is calculated by latent representation or directly generated by end-to-end models. There are mainly four types of graph anomalies, namely node, edge, (sub)graph, and path anomaly.

brief introduction of some predefined matrices to better understand the concepts described in this article.

2.2 Preliminaries

Given an undirected graph, the Laplacian matrix is defined as $L = D - A$, where $D \in \mathbb{R}^{n \times n}$ is a diagonal degree matrix with $D_{ii} = \sum_{j=1}^{n} A_{ij}$. $L = Q\Lambda Q^T$ denotes eigendecomposition, where $\Lambda \in \mathbb{R}^{n \times n}$ is a diagonal matrix of eigenvalues in ascending order and $Q \in \mathbb{R}^{n \times n}$ is composed of corresponding eigenvectors. The element $P(i, j)$ of transition matrix $P = D^{-1}A$ represents the probability of a random walk from node $v_i$ to node $v_j$.

As mentioned previously, this survey aims to introduce existing research on graph anomaly detection and prediction. A graph is an abstract data type consisting of a set of nodes (a.k.a. vertices) representing entities, with edges between nodes representing relations or connections. Anomalies in graph data fall into four main categories: node anomaly, edge anomaly, path anomaly, and (sub)graph anomaly. The whole process of detecting anomalies with deep graph models is briefly illustrated in Figure 2.

When learning a deep model on graphs for anomaly analytics tasks, we divide the models into four categories based on their model architectures and training strategies. Here we briefly introduce the process and potential mechanism of these graph neural network models.

- **GCNs.** Considering that graphs lack a grid structure like image and text, it is impractical to directly apply standard convolution operation on graphs. Graph convolution is generally divided into two categories, spectral convolution, which performs Fourier transform on graph signals, and spatial convolution, which learns structural information by aggregating node neighbors [106]. The graph signal $X$ in spectral methods is filtered by

$$Z = f(X, A) = \tilde{D}^{-\frac{1}{2}} \tilde{A} \tilde{D}^{-\frac{1}{2}} X \Theta,$$

(2)

where $\Theta$ is a matrix of learnable parameters and $Z$ is the convolved signal matrix. In addition, the equation of learning node representation of node $i$ in a GCN can be written as

$$h_i = \sigma \left( \sum_{j \in N(v_i)} \alpha_{ij} Wh_j \right),$$

(3)
where $W$ is weight matrix to be learned and $\alpha_{ij}$ is set as 1 in GCN. The calculation formula of $\alpha_{ij}$ will be introduced in GAT.

- **GATs.** It is acknowledged that spatial convolution is to aggregate features from node neighbors to update the hidden state of this node in the next layer. The aggregation operation could be (weighted) summarization, averaging, and maximization. GAT is a special type of spatial convolution methods. Although some spatial methods also consider the node importance and allocate a predefined weight for every neighbor, a Graph Attention Network is proposed so that the weight of nodes can be learned automatically by applying the attention mechanism to neighbors in the model [92]. The influence $\alpha_{ij}$ of node $v_j$ on node $v_i$ in GAT is calculated as

$$\alpha_{ij} = \frac{\exp(\sigma(a^T[W_h_i \parallel W_h_j]))}{\sum_{k \in N(i)} \exp(\sigma(a^T[W_h_i \parallel W_h_k]))}.$$  \hspace{1cm} (4)

Here $a$ denotes a weight vector and the symbol $\parallel$ is the concatenation operation on two vectors.

- **GAE.** Graph autoencoder is a popular model used in unsupervised learning tasks [4, 30]. Similarly to the general autoencoder model, GAE is composed of an encoder compressing the sparse node vector (input) into a low-dimensional representation through learning node structural features and a decoder reconstructing the dense vector into a high-dimensional vector similar to the input as much as possible. Based on this mechanism, an essential part of loss function in GAE models is to minimize the difference between the input and output vectors:

$$\min_{\Theta} L_2 = \|A - \hat{A}\|_2 + \|X - \hat{X}\|_2,$$  \hspace{1cm} (5)

where $A$ and $X$ are the input node adjacency and attribute matrix, and $\hat{A}$ and $\hat{X}$ are the reconstructed node structure and attribute matrix. It should be noted that the encoder could be any kind of neural network like Multilayer Perceptron (MLP), Recurrent Neural Network (RNN), and GCN. Therefore, there are a line of anomaly detection methods combining GAE and GCN. We refer readers to References [127] for more details about deep graph models and their applications.

### 3 GCN-BASED METHODS

As the most popular structure among the deep graph models, GCNs can learn and generate node embeddings through the operation of convolution, which refers to the process of aggregating information from the nodes’ local neighborhoods. In this section, we introduce the GCN-based anomaly detection and prediction methods, which is also the most popular model type among all anomaly analytics models. The methods are divided into two classifications according to whether the methods are devised for specific anomaly detection tasks or not, namely, general models and task-driven models. A toy model of how anomalous users are detected in social networks with spatial convolution operation is shown in Figure 3. The main characteristics of these methods are summarized in Table 3.

#### 3.1 General Models

In Reference [56], the authors defined two types of node anomaly according to its global location and topological network structure, named global anomaly and community anomaly, respectively. When learning global anomaly node embeddings, an autoencoder is applied to extract node attributes $X$. As for community anomaly representation, the authors designed a convolutional encoder and deconvolutional decoder networks based on their neighborhoods. Then, the anomalous node could be detected by measuring the embedding’s energy in the Gaussian Mixture Model.
Fig. 3. An illustration of applying spatial convolution operation in anomalous user detection in social networks, where nodes are affected only by their immediate neighbors. Both attribute feature and structure feature could be learned with a GCN model to get the final anomaly ranking list.

Table 3. A Comparison of the GCN-based Models

| Sec. | Method          | Type   | Convolution | Characteristic          |
|------|-----------------|--------|-------------|-------------------------|
| 3.1  | SpecAE [56]     | Spectral | —           | AutoEncoder             |
|      | DOMINANT [22]   | Spatial | First-order | —                       |
|      | DeepAD [139]    | Spatial | First-order | —                       |
|      | AANE [29]       | Spatial | First-order | —                       |
|      | AddGraph [130]  | Spatial | First-order | GRU + Attention         |
|      | ANEMONE [45]    | Spatial | First-order | Contrastive learning    |
|      | CoLA [60]       | Spatial | First-order | Contrastive learning    |
|      | GCCAD [13]      | Spatial | First-order | Contrastive learning    |
| 3.2  | GEM [62]        | Spatial | First-order | Attention mechanism     |
|      | GCNSI [26]      | Spectral | First-order | Semi-supervised learning|
|      | GAS [54]        | Spatial | First-order | Attention mechanism     |
|      | Bi-GCN [7]      | Spectral | Polynomial | DropEdge                |
|      | GCAN [63]       | Spatial | First-order | —                       |
|      | TPC-GCN [133]   | Spatial | First-order | —                       |
|      | HMGNN [141]     | Spatial | First-order | Adversarial learning + Attention |
|      | GCNwithMRF [107]| Spatial | First-order | —                       |
|      | GraphRfi [126]  | Spatial | First-order | Attention mechanism     |
|      | TSN [132]       | Spatial | First-order | —                       |
|      | ST-GCAE [68]    | Spatial | First-order | Attention mechanism     |

Similarly, Ding et al. [22] and Zhu et al. [139] proposed to learn node embeddings by combining AutoEncoder with Graph Convolutional Networks in attributed networks. Specifically, the encoder module extends the operation of convolution in the spectral domain and learns a layerwise new latent representation. Then, the structure reconstruction decoder $\mathbf{A} - \hat{\mathbf{A}}$ and attribute reconstruction decoder $\mathbf{X} - \hat{\mathbf{X}}$ are jointly learned to compute the anomaly score, which can be formulated as

$$\text{score}(v_i) = (1 - \alpha)\|\mathbf{a}_{i} - \hat{\mathbf{a}}_{i}\|_2 + \alpha\|\mathbf{x}_{i} - \hat{\mathbf{x}}_{i}\|_2,$$

where $\alpha$ is a hyper-parameter balancing the importance of reconstructed structure and attribute information.

Instead of detecting anomalous nodes, Duan et al. [29] generated node embeddings by combining GAE and GCN to detect anomalous links. They assumed that a link with a lower value of predicted presence probability is regarded as anomalous, which is calculated as

$$\mathbf{P}_{u,v} < \text{MEAN}_ {v' \in N_u} \mathbf{P}_{u,v'} - \mu \cdot \text{STD}_ {v' \in N_u} \mathbf{P}_{u,v'},$$
where MEAN and STD represent the mean and standard operations, respectively, and $\mu$ is a parameter. $P$ is the predicted presence probability matrix.

In Reference [130], the authors aimed to incorporate all possible features in the proposed framework AddGraph, including structural, content, and temporal features. In AddGraph, they used a GCN incorporating content and structural features, with an attention-based Gated Recurrent Unit (GRU), which can combine short-term and long-term states. After obtaining the hidden states of nodes at timestamp $t$, the anomalous score of an edge is computed as

$$F(i, j, w) = w \cdot \sigma(\beta \cdot (\|a \odot h_i + b \odot h_j\|_2^2 - \mu)),$$

where $h_i$ and $h_j$ are the hidden states of the $i$th node and $j$th node, respectively. Other characteristics are parameters to be adjusted. $a$ and $b$ are parameters to optimize the output layer, and $\beta$ and $\mu$ are hyper-parameters.

Jin et al. [45] leveraged a multi-scale contrastive learning technique to capture node anomalies in multiple scales. ANEMONE simultaneously performs patch- and context-level contrastive learning via two GCN models. Anomaly is identified by leveraging the statistics of multi-round contrastive scores.

Similarly, Liu et al. [60] also proposed to detect node anomalies in attributed network in a contrastive learning way. The objective of their model CoLA is to discriminate the agreement between the elements within the selected instance pairs, which is finally used to calculate the anomalous scores of nodes. The difference between CoLA and ANEMONE is the process of sampling. CoLA selected the local subgraph including the target node as positive sample, while local graph without target node is negative sample.

Differing from existing graph contrastive learning frameworks for GNN pre-training, Chen et al. [13] performed contrastive learning in a supervised learning way. In other words, the negative samples are constrained to anomalous nodes instead of being constructed according to some rules. Considering that the bottleneck of anomaly detection tasks is the lack of sufficient anomaly labels, they proposed to construct pseudo anomalies via corrupting the original graph.

### 3.2 Task-driven Models

To detect malicious account at a mobile cashless payment platform, Liu et al. [62] jointly learned the topology of a heterogeneous graph and the features of local structures of the nodes. Specifically, they constructed “homogeneous connected subgraph” based on an assumption that an edge $(i, i')$ is added if both account $i$ and $i'$ login to the same device in the original heterogeneous graph. This subgraph is composed of only accounts as nodes. The function to learn the embeddings of nodes is defined as

$$H^{(l+1)} \leftarrow \sigma(X \cdot W + \sum_{d=1}^{[D]} softmax(\alpha_d) \cdot A^{(d)} \cdot H^{(l)} \cdot V_d),$$

where $[D]$ is the number of subgraphs extracted from the original graph and $V_d$ is a parameter controlling the shape of the function. Moreover, an attention mechanism is also utilized in the learning process of different types of subgraphs, i.e., $softmax(\alpha_d) = \frac{\exp \alpha_d}{\sum_i \exp \alpha_i}$, and $\alpha = [\alpha_1, \ldots, \alpha_{[D]}]^T$ is a free parameter to be learned.

Based on an assumption that representing nodes with the information of its neighbors will effectively improve the performance of the source node detection task, Dong et al. [26] designed a model GCNSI to locate multiple rumor sources without prior knowledge of the underlying propagation model. This model learns node embeddings by adopting convolution in the spectral domain, which considers its multi-hop neighbors’ information. The propagation strategy of GCNSI is modified based on LPSI [105].
Concerning the task of spam review detection, Li et al. [54] aimed to capture the local context and global context of a comment. The proposed model GAS simultaneously integrates a heterogeneous bipartite graph and a homogeneous comment graph. The comment edge embedding in bipartite graph is to aggregate the hidden states of three variables in the previous layer, i.e., the edge itself and its linked two nodes:

\[
H^l_e = \sigma \left( W^l_E \cdot AGG^l_E \left( H^{l-1}_e, H^{l-1}_{U(e)}, H^{l-1}_{I(e)} \right) \right),
\]

where

\[
AGG^l_E \left( H^{l-1}_e, H^{l-1}_{U(e)}, H^{l-1}_{I(e)} \right) = H^{l-1}_e \left\| H^{l-1}_{U(e)} \left\| H^{l-1}_{I(e)} \right. \right. 
\]

Here \( U(e) \) and \( I(e) \) are user node set and item node set linked by edge \( e \), respectively. Similarly, the user and item embedding are calculated in the same way and the comment embedding in the comment graph can be obtained from a general GCN model. Finally, the classification result \( y \) can be calculated according to

\[
y = \text{classifier}(z_i \parallel z_u \parallel z_c \parallel p_c),
\]

where \( z_i, z_u, \) and \( z_c \) are item, user, and comment embeddings obtained from bipartite graph, and \( p_c \) is the comment embedding from comment graph, respectively.

With the aim of detecting a rumor on social media, Bian et al. [7] proposed a top-down GCN (TD-GCN) to model the rumor propagation features and a bottom-up GCN (BU-GCN) to model the rumor dispersion features, respectively. The node representations are learned over a two-layer GCN:

\[
H^{TD}_1 \leftarrow \sigma \left( \hat{A}^{TD}XW^{TD}_0 \right),
\]

\[
H^{TD}_2 \leftarrow \sigma \left( \hat{A}^{TD}H^{TD}_1W^{TD}_1 \right),
\]

where \( H^{TD}_1 \) and \( H^{TD}_2 \) refer to the two-layer hidden features of the TD-GCN. The bottom-up features of BU-GCN are calculated in the same manner as Equations (13) and (14), while the adjacency matrix should be transposed.

Another similar topic in social media is fake news detection. Lu et al. [63] aimed to model the interactions among users by creating a propagation graph as a part of the proposed model. The propagation graph \( G_t = (U_t, E_t) \) is constructed by the set of users \( U_t \) who share or retweet the topic \( s_t \), and the edge is weighted by the cosine similarity between the feature vectors of users. Then, the user embeddings will be learned by a GCN model based on this weighted propagation graph. Similarly, Zhong et al. [133] created a Topic-Post-Comment graph for target posts in the task of controversy detection, where the nodes represent topic, post, or comment, and the edges refer to the corresponding interactions between two nodes. The node representations are obtained through a two-layer GCN, the same as Equations (13) and (14).

As the first application of deep graph model in the task of fraud invitation detection, Zhu et al. [141] proposed HMGNN model by dividing the whole network into \( |D| \) mini-graphs, which were represented by hypernodes. The hypergraph is generated by adding edges between mini-graphs. Based on this graph, the convolution for hypernodes is defined as

\[
H^{l+1} \leftarrow \sigma \left( X_hU^l + \sum_{d \in D} ATT_d \left( \hat{A}^d_hH^lW^l_d + b^l_d \right) \right),
\]

where \( ATT_d \) is the attention mechanism and \( U^l \) are free parameters to be trained. Here \( H^0 = [X; X^1_h; \ldots; X^{[D]}_h] \) is the initial representation of the whole graph that concatenates the feature matrix of normal- and hyper- nodes.
To detect social spammers in a semi-supervised way, Wu et al. [107] combined GCNs and Markov Random Field (MRF) on directed social networks. The layerwise propagation rule of GCN is defined as

$$H^{(l+1)} = \sigma \left( D^{-1/2} A H^{(l)} W^{(l)} + D^{-1/2} A_b H^{(l)} W^{(l)}_o + \tilde{D}^{-1/2} A_b \tilde{D}^{-1/2} H^{(l)} W^{(l)}_b \right),$$

where $A_i$, $A_o$, and $A_b$ are three types of adjacency matrices constructed according to three different definitions of neighbors. Considering that different characteristics of pairwise nodes can have different influences on social networks, the authors proposed to use MRF modeling for the joint probability distribution of users’ identities. The MRF is formulated as a RNN in this article to perform multi-step inference when computing the posterior distribution.

Since deliberately inserting fake feedback will cause the recommender system bias to the malicious users’ favor, Zhang et al. [126] presented a GCN-based user representation learning framework to perform robust recommendation and fraudster detection in a unified way. Given a weighted bipartite rating graph $G = (U \cup V, E)$, GCN is adopted to capture topological neighborhood information and side information of nodes. The user and item embedding are calculated as

$$z_u = \sigma(W \cdot AGG(h_k, \forall k \in N(u)) + b),$$

$$z_v = \sigma(W \cdot AGG(h_q, \forall q \in N(v)) + b),$$

where $h_k$ and $h_q$ are the neighbor information for each node. Here the attention mechanism is incorporated into the aggregation function.

It is acknowledged that noisy labels will influence the results of anomaly detection algorithms to some degree. Then, instead of directly generating latent representations, Zhong et al. [132] designed a GCN-based model to correct noisy labels before detecting anomalous actions in videos. Here the feature similarity graph is constructed with nodes denoting snippets and edges referring to the similarity between two snippets. Another temporal consistency graph module is directly built upon the temporal structure of a video.

Pose estimation is the first step of detecting anomalous actions in videos, and the extracted poses can be embedded by deep graph models. In Reference [68], the authors proposed spatio-temporal graph convolution block, which is composed of a spatial-attention graph convolution, a temporal convolution, and a batch normalization. The generated latent vector is fed into a cluster layer to obtain a normality score. Here the normality score is calculated by a Dirichlet Process Mixture Model for evaluating the distribution of proportional data.

### 3.3 Discussion

As it can be found from the GCN-based anomaly detection models we have discussed above, the modern GCN model could learn both local and global structure features of a graph with convolution and pooling operations. To improve the training efficiency when imposing GCN on large-scale graphs, neighborhood samplings and layerwise samplings are two common strategies to deal with the phenomenon that some nodes have high degrees (too many neighbors). In addition to node and edge anomaly, a characteristic of GCN is that it is more suitable to detect (sub)graph or group anomaly when compared with other GNN models.

The aforementioned models mostly focus on learning node features and graph structures, ignoring another important element consisting of a graph, i.e., edge. In some real-world networks, edges generally contain abundant information, such as edge types and corresponding attributes, which could play a key role in anomaly detection tasks. Therefore, incorporating edge features into graph anomaly detection models could be considered as a future work [14]. Besides, although applying...
GCN to an inductive setting is verified \cite{36}, conducting inductive GCN for graphs without explicit features remains an open problem.

\section{GAT-BASED METHODS}

In deep graph models, the weights of node neighbors are defined as an equal or default setting. However, the importance of neighbors is mostly different in terms of their attribute and structural features. Motivated by the attention mechanism, Velivckovic et al. \cite{92} proposed a GAT by applying the attention mechanism to the spatial convolution operation of GCN. A toy example of how attention mechanism is applied into cyberbullying detection is shown in Figure 4. In this section, we summarize and introduce the anomaly analytics algorithms using graph attention networks. The methods are divided into two subsections in terms of the anomaly type, i.e., node anomaly detection and (sub)graph anomaly detection. The main characteristics of these methods are summarized in Table 4.

\subsection{Node Anomaly Detection}

To detect anomalous nodes in an Attributed Heterogeneous Information Network, Hu et al. \cite{41} applied feature and path attention mechanism to differentiate the importance of meta-paths as well as attribute information. As a basic analysis tool for heterogeneous graph, a meta-path captures the proximity among multiple nodes from a specific semantic perspective, which could be seen as a high-order structure. For example, the meta path “Author-Paper-Author” describes that two authors collaborated with each other in a particular paper. The feature attention of neighbor node $i$ on node $u$ in path $\rho$ is calculated as

$$\hat{\alpha}_{u,i}^\rho = \frac{\exp(\alpha_{u,i}^\rho)}{\sum_{j=1}^{K} \exp(\alpha_{u,j}^\rho)}.$$  \hspace{1cm} (19)

The attention weight of path $\rho$ for node $u$ is defined as

$$\beta_{u,\rho} = \frac{\exp(z^\rho \cdot \tilde{f}_u^C)}{\sum_{\rho' \in \mathcal{Z}} \exp(z^{\rho'} \cdot \tilde{f}_u^C)}.$$  \hspace{1cm} (20)

Here $z^\rho$ is the attention vector of meta-path $\rho$ and $\tilde{f}_u^C$ is the collection of user representations w.r.t. all meta-paths. The cash-out probability (i.e., anomalous score) is calculated via a regression layer with a sigmoid unit.

To detect user fraud in financial networks, Wang et al. \cite{95} designed a hierarchical attention structure in graph neural network from node-level attention to view-level attention when generating graph embeddings. View-attention mechanism is applied to fuse multiple views of data information into user embeddings. Finally, a softmax function is used on the representations of the embedding layer to get the classification result.

In Reference \cite{81}, the authors constructed a news-oriented heterogeneous information network with nodes of creators, subjects, and articles, and two links of write and belong-to. Based on this network, they proposed AA-HGNN to solve the problem of fake news detection. From the perspective of node-level attention, the model first aggregates the importance of the same-type neighbors for each news node and generates an integrated embedding of schema node. By using a transformation matrix, the embeddings of the nodes can be mapped into the same dimension. The logistic regression layer works as the classification layer to generate the detection results.

To give direct explanations like how anomalies deviate from normal behaviors, Reference \cite{19} proposed to use graph attention mechanism to predict the future behavior of a node. The anomaly score of node $i$ is defined as the difference between the expected behavior and observed behavior.
Fig. 4. An illustration of how attention mechanism is applied into cyberbullying detection. Each comment is first encoded by a RNN framework as the initial vector, and the comments are constructed as a temporal graph where nodes represent user comments and edges represent time intervals between two comments. Then, the attention mechanism is applied to learn the temporal information among these comments for final anomaly detection.

| Method          | Attention Level | Objective Function               | Other Characteristics                   |
|-----------------|-----------------|----------------------------------|-----------------------------------------|
| HAGNE [100]     | node & path     | Error sum of squares             | Siamese network for graph matching      |
| HACUD [41]      | feature & path  | Maximum likelihood estimation     | Hierarchical attention mechanism        |
| mHGNN [32]      | node            | Cross-entropy                    | Metagraph-guided neighbor search        |
| SemiGNN [95]    | node & view     | Cross-entropy + Structure similarity | Semi-supervised learning               |
| AA-HGNN [81]    | node & schema   | Cross-entropy                     | Adversarial active learning             |
| GDN [19]        | node            | Mean squared error               | Graph deviation scoring                 |
| TGBULLY [34]    | node            | —                                | Temporal graph interaction learning     |
| MAHINDER [134]  | node & path     | Cross-entropy                    | —                                       |

at time $t$,

$$
\text{Err}_i(t) = \left| \hat{s}_i(t) - \tilde{s}_i(t) \right|.
\tag{21}
$$

For session-level cyberbullying detection, the final embedding is fed into a single-layer dense network and predict its label.

In financial default user detection over online credit payment service, Zhong et al. [134] devised a meta-path-based encoder to capture local structural feature of nodes and links. The path representation is defined as the concatenation of node and link embeddings. Moreover, attention mechanism is applied to capture different importance of nodes/links of a path. After modeling the node and link interactions above, the learned representation is fed into several fully connected neural networks and a regression layer with a sigmoid unit for anomaly classification.

4.2 (Sub)graph Anomaly Detection

Wang et al. [100] proposed HAGNE to detect unknown malicious programs in computer systems. Instead of setting one-hop nodes as neighbors, the authors construct a contextual neighborhood
set by searching for meta-paths. Then, three kinds of aggregators are applied to generate graph embeddings based on the generated meta-path set \( \mathcal{M} = \{M_1, M_2, \ldots, M_{|\mathcal{M}|}\} \), namely, node-wise attentional neural aggregator, which is defined as

\[
\mathbf{h}_v^{(i)(k)} = AGG_{\text{node}} \left( \mathbf{h}_v^{(i)(k-1)}, \{\mathbf{h}_u^{(k-1)}\}_{u \in \mathcal{N}_i} \right),
\]

(22)

where \( i \in \{1, 2, \ldots, |\mathcal{M}|\} \), \( k \in \{1, 2, \ldots, K\} \) denotes the layer index, and \( \mathbf{h}_v^{(i)(k)} \) is the feature vector of node \( v \) at the \( k \)th layer in meta-path \( M_i \); layerwise dense-connected neural aggregator, which is inspired by DENSENET [42]:

\[
\mathbf{h}_v^{(i)(K+1)} = AGG_{\text{layer}} \left( \mathbf{h}_v^{(0)}, \mathbf{h}_v^{(1)}, \ldots, \mathbf{h}_v^{(K)} \right),
\]

(23)

and pathwise attentional neural aggregator, whose attentional weight is defined as

\[
\alpha_{ij} = \frac{\exp \left( \sigma \left( b \left( \mathbf{W}_b \mathbf{h}_v^{(i)(K+1)} \| \mathbf{W}_b \mathbf{h}_u^{(j)(K+1)} \right) \right) \right)}{\sum_{j' \in |\mathcal{M}|} \exp \left( \sigma \left( b \left( \mathbf{W}_b \mathbf{h}_v^{(i)(K+1)} \| \mathbf{W}_b \mathbf{h}_{v'}^{(j')(K+1)} \right) \right) \right)}.
\]

(24)

Then, the graph embedding can be calculated from the joint representation of all meta-paths:

\[
\mathbf{h}_G = AGG_{\text{path}} = \sum_{i=1}^{|\mathcal{M}|} ATT \left( \mathbf{h}_v^{(i)(K+1)} \right) \mathbf{h}_v^{(i)(K+1)}.
\]

(25)

Graph matching is used to measure the anomalous level of a program [80]. An alert will be triggered if the highest similarity score among all the existing programs is below the threshold. The similarity score is calculated as

\[
\text{Sim}(G_{i(1)}, G_{i(2)}) = \frac{\mathbf{h}_{G_{i(1)}} \cdot \mathbf{h}_{G_{i(2)}}}{\|\mathbf{h}_{G_{i(1)}}\| \cdot \|\mathbf{h}_{G_{i(2)}}\|}.
\]

(26)

Subsequently, Fan et al. [32] identified the illicit traded product in underground market with a similar process. After constructing the neighbors set by the meta path-based method, the authors applied an attention mechanism to learn product and buyer embeddings, respectively. Finally, their embeddings are generated by concatenating each embedding based on a specific metagraph.

Social media contains multi-modal information such as comment, user, time, and history. Ge et al. [34] proposed to use temporal graph interaction learning module as a building block to detect cyberbullying in social networks. In this work, the authors incorporated GATs to automatically aggregate information from neighbor nodes to the central node in a temporal graph. Edge in the temporal graph denotes time dynamics, and the weight of the node pair \((i, j)\) is defined as

\[
\alpha(z_i, z_j, t_i, t_j) = \tanh((\mathbf{W}_o z_i)^T z_j + \mathbf{W}_t (t_j - t_i)).
\]

(27)

### 4.3 Discussion

As we have explained, GAT is a branch of GCN. To improve GCN, GAT-based methods are separated as a unique section in which the importance of different neighbors on the central node is considered. The difference between these two sections is that the utilized traditional attention mechanism of Section 4 is only applied on nodes, while models in Section 3 are either using attention mechanism on other parts of the framework or using simple GCN function without any attention mechanism.
Table 5. A Comparison Among Different GAE-based Models

| Method   | Type                | Objective Function                        | Other Characteristics       |
|----------|---------------------|--------------------------------------------|-----------------------------|
| AEHE [31]| GAE                | Cross-entropy+L2-reconstruction            | Negative sampling           |
| AEGIS [21]| GAE+GAN            | Cross-entropy                             | GDN Encoder                 |
| DONE [6]  | GAE+Discriminator   | L2-reconstruction+Cross entropy            | Adversarial learning        |
| DeepSphere [90] | GAE+LSTM         | L2-reconstruction                         | Hypersphere learning        |
| UCD [17]  | GAE+GCN            | L2-reconstruction                         | Attention mechanism         |

Fig. 5. An illustration of combining GAE with contrastive learning for anomalous academic’s detection in heterogeneous networks. After selecting a target node, the second step is to sample positive and negative instances from the network for contrastive learning. Then, different kinds of nodes are encoded with different encoders and a common decoder. The encoder aims to learn structure and attribute feature of nodes and generate low-dimensional vectors, and the decoder aims to reconstruct the input vector as similar as possible. The anomaly score is calculated by combining the discrimination score generated by the discriminator and the reconstruction loss generated by the AutoEncoder.

5 GAE-BASED METHODS

GAE is an unsupervised structure to generate low-dimensional representations, with the aim of minimizing the loss between the input of encoder and the output of decoder [91]. In this section, we present the GAE-based algorithms that are applied to anomaly analytics. The methods are classified into three types according to the training and learning schema, namely, General AutoEncoder, Adversarial Training, and Hypersphere Learning. The main characteristics of these methods are summarized in Table 5. In Figure 5, we present a GAE-based model for detecting anomalous citation behaviors in a heterogeneous network.

5.1 General AutoEncoder

Only considering the structure of a heterogeneous network is not sufficient for abnormal event detection due to the sparsity of a network. Fan et al. [31] proposed AEHE to learn both attribute embedding and the second-order structure-preserving node embedding. The heterogeneous attribute embedding of a node is generated by a MLP component, which consists of two hidden layers with ReLU as the activation function. As for the second-order structure embedding, the authors constructed a homogeneous graph by extracting symmetry meta-paths. Autoencoder is used to model the neighborhood structures, which is composed by an encoder

\[ r'_i = \sigma \left( W_i \cdot s'_i + b_i \right), \]
and a decoder,
\[ \hat{s}_t^i = \sigma \left( \hat{W}_t^i \cdot r_t^i + \hat{b}_t^i \right), \]  

(29)

where \( r_t^i \) is the latent representation of entity \( a_t^i \), and \( \hat{s}_t^i \) is the reconstructed representation of \( s_t^i \). It should be noted that \( s_t^i \) is the \( i \)th row of the adjacency matrix, not just a node feature vector.

Research has shown that human behaviors reflect self-selection bias and peer influence in online social networks, which is closely associated with cyberbullying behaviors [33]. In this regard, Cheng et al. [17] used a GCN encoder and an inner product decoder to learn a latent matrix \( Z \) by minimizing the following reconstruction error:
\[ F(v_i) = \| A - \hat{A} \|^2_2, \]  

(30)

where \( \hat{A} = \sigma(ZZ^T) \) and \( Z = \text{GCN}(X, A) \). Then, the anomalous session could be detected by measuring the embedding’s energy in the Gaussian Mixture Model, which follows [56].

### 5.2 Adversarial Training

Adversarial methods such as Generative Adversarial Network (GAN) and adversarial attacks are popular in the machine learning community in recent years. In Reference [74], the authors incorporated an adversarial training scheme into GAEs as an additional regularization term. Motivated by this work, Ding et al. [21] proposed AEGIS to learn anomaly-aware node representations through graph differentiation networks (GDNs) for inductive anomaly detection. AEGIS is composed of a GAE to learn node embeddings for training new networks, and a GAN to calculate the anomaly scores of nodes. The autoencoder network is built with the graph differentiative layers. Specifically, a GDN layer has a hierarchical attention structure from node level,
\[ h^{(l)}_i = \sigma \left( W_1 h^{(l-1)}_i + \sum_{j \in N_i} \alpha_{ij} W_2 \Delta^{(l-1)}_{i,j} \right), \]  

(31)

where \( \Delta_{i,j} \) denotes the embedding difference between nodes \( i \) and \( j \); and neighbor level,
\[ h^l_i = \sum_{k=1}^K \rho_i^k h^{(l,k)}_i. \]  

(32)

Finally, the anomaly score of node \( i \) is computed according to the output of a discriminator:
\[ \text{score}(z_i) = 1 - D(z_i'). \]  

(33)

In real-world networks, community outliers deviate significantly from other nodes in the same community in terms of link structures and attributes. To alleviate the influence of these outliers and generate robust node embeddings, Bandyopadhyay et al. [6] mapped every vertex to a low-dimensional vector and detected outliers via a deep autoencoder-based architecture. Moreover, the authors introduced adversarial learning for outlier resistant network embedding. Here a discriminator is combined with two parallel autoencoders to align the embeddings in terms of link structure and node attributes.

### 5.3 Hypersphere Learning

Inspired by hypersphere learning, Wang et al. [101] proposed One-Class Graph Neural Network (OCGNN) with the aim of minimizing the volume of a hypersphere that encloses normal nodes as much as possible. Then, the nodes out of the hypersphere are regarded as abnormal.

With the aim of identifying anomalous sample cases and nested anomalies within the anomalous tensors, Teng et al. [90] proposed DeepSphere by incorporating hypersphere learning into a LSTM Autoencoder model in a mutual supportive manner. Here, attention mechanism is also applied to differentiate and aggregate different neighbors. The motivation of DeepSphere is that the learned
Fig. 6. The GAN-based anomaly detection model is composed of three main parts: a Generator sampling similar node attributes, an Encoder generating low-dimensional node representations, and a Discriminator differentiating real nodes embeddings from generated nodes embeddings.

representations at large distance from the outside of hypersphere are regarded as anomalous, while the ones with small distances from the inside of the hypersphere tend to be normal.

5.4 Discussion
GAE is the most popular model in tackling unsupervised graph learning tasks, which can only consider the structural patterns by using graph adjacency matrix. However, GCN-based models are semi-supervised and could capture both node attributes and graph structures. Despite the different architectures between GAE and GCN, existing research have shown that it is possible to combine them together in a unified framework [9]. When applying GCN as the encoder, GAE could be applied to the inductive learning settings where node attributes are incorporated. Considering that the aim of GAE is to reconstruct the input embedding as similar as possible, it should be cautious when selecting the appropriate similarity metrics that have significant influence on subsequent anomaly detection results.

6 OTHER METHODS
Apart from the deep graph models mentioned above, there are many other popular deep learning models that can be used for anomaly analytics tasks, such as Generative Adversarial Methods [96], Meta-learning [135], and Graph Reinforcement Learning [25]. In this section, we summarize these different deep graph models that are utilized to solve anomaly analytics tasks. The process of detecting anomalies with a GAN is shown in Figure 6. The main characteristics of these methods are summarized in Table 6.

6.1 GAN-based Methods
With the rapid growth of research in GAN for high-dimensional data distribution approximation, Chen et al. [15] proposed to detect anomalies with a Generative Adversarial Attributed Network (GAAN), which is composed of three parts: a Generator sampling similar node attributes, an Encoder generating low-dimensional node representations, and a Discriminator differentiating real nodes embeddings from generated nodes embeddings. The anomalous score is defined based on a context reconstruction loss $L_G$ and a structure discriminator loss $L_D$,}

$$
\mathcal{F}(v_i) = \alpha L_G(v_i) + (1 - \alpha) L_D(v_i),
$$

(34)
Table 6. A Comparison Among Other Deep Graph Models

| Method               | Method/Problem Innovation                      |
|----------------------|------------------------------------------------|
| GAAN [15]            | Generative adversarial network                 |
| GAL [129]            | New loss function                              |
| CARE-GNN [27]        | Reinforcement learning                         |
| Meta-GDN [23]        | Cross-network meta-learning                    |
| OCGNN [101]          | One-Class graph neural network                 |
| MAHINDER [134]       | Financial default user detection over online credit payment service |

where $\mathcal{L}_G(v_i) = \|x_i - x'_i\|_2$, and $\mathcal{L}_D(v_i)$ is defined as

$$
\mathcal{L}_D(v_i) = \sum_{j=1}^{n} A_{ij} \cdot \sigma(\hat{A}_{ij}, 1) / \sum_{j=1}^{n} A_{ij}.
$$

(35)

Larger value of $\mathcal{F}(v_i)$ indicates the node $v_i$ is more likely to be anomalous.

6.2 Reinforcement Learning-based Method

In Reference [129], the authors divided the graph anomaly detection tasks into two classifications, i.e., outlier detection and unexpected dense block detection. When applying graph learning models to generate embeddings of nodes, a new loss function was designed as

$$
\mathcal{L}(u) = \mathbb{E}_{u_i \sim U_{u_i}, u_+ \sim U_{u_+}} \max\{0, g(u, u_+) - g(u, u) + \Delta y_u\},
$$

(36)

where $\Delta y_u = \frac{C}{n_{yu}} \cdot g()$ is a function to denote the similarity of the representations between any two user nodes. Here $U_{u_i}$ denotes the set of user nodes that has the same label as $u$, $U_{u_+}$ refers to $U \setminus U_{u_i}$, and $n_{yu} = |U_{u_+}|$. The construction of sets $U_{u_i}$ and $U_{u_+}$ have different strategies for corresponding tasks. It is impractical to exactly detect camouflaged fraudsters with graph learning detectors. Dou et al. [27] proposed three neural models to enhance the deep graph models against two kinds of camouflages, i.e., feature camouflage and relationship camouflage. Because camouflaged nodes should be filtered when selecting similarity-aware neighbors, a reinforcement learning process is formulated as a Bernoulli Multiarmed Bandit to find the optimal thresholds. The reward mechanism of epoch $e$ is defined as

$$
R\left(p_r^{(l)}, a_r^{(l)}\right)^{(e)} = \begin{cases} +1, & G(D_r^{(l)})^{(e-1)} - G(D_r^{(l)})^{(e)} \geq 0 \\ -1, & G(D_r^{(l)})^{(e-1)} - G(D_r^{(l)})^{(e)} < 0 \end{cases}.
$$

(37)

Here $G(D_r^{(l)})^{(e)}$ refers to the average neighbor distances for relationship $r$ at the $l$th layer for epoch $e$. If the average distance of newly selected neighbors at epoch $e$ is less than that of epoch $e - 1$, then the reward is positive.

6.3 Few-shot Learning-based Method

To investigate the novel problem of few-shot network anomaly detection under the cross-network setting, Ding et al. [23] designed a new graph learning architecture, namely GDNs. GDN in this article is composed of three key building blocks: an encoder to generate node embeddings, an abnormality valuator to compute the anomaly score of nodes, and a deviation loss for optimization. Concretely, the GDN model can be formally represented as

$$
\mathcal{F}_O(A, X) = \mathcal{F}_O(\mathcal{F}_O(A, X)),
$$

(38)
which directly maps the input network to anomaly scores (scalar). After detecting anomalies in arbitrary networks, a meta-learner is learned to initialize GDN from multiple auxiliary networks, which possesses the ability to distill comprehensive knowledge of anomalies.

6.4 Discussion

There are also many other neural network structures and learning strategies being applied to detect graph anomalies, such as adversarial learning and reinforcement learning. Considering that the number of these methods is relatively less, we summarize all these methods into one section instead of different sections. Other aspects of common deep graph learning models include but are not limited to graph reinforcement learning and graph adversarial learning.

It is well known that the advantage of reinforcement learning is to actively learn from the feedback. In graph anomaly detection tasks, reinforcement learning could help in optimal selection of neighbors and aggregating them together for more informative node embeddings. Adversarial methods have shown its capacity in generating realistic entities, which improve the detection performance of anomalies that are hardly reconstructed from the latent space. However, this kind of anomaly detection methods faces multiple problems during the training process, such as failure to converge and mode collapse.

7 APPLICATIONS

Thus far, we have reviewed different graph learning methods in anomaly analytics tasks. In this section, we briefly introduce their applications in different kinds of networks.

7.1 Fake News

With the rapid growth of the Internet, social media provides a platform for people to participate and discuss online news more conveniently, like communicating news without the physical distance barrier among individuals and acquiring news at an unprecedented rate. In general, fake news in social media is defined as the verifiably false information that is generated by malicious users or social bots intentionally, with the aim of misleading the public. There have been research showing that fake news spread more quickly and broadly than true news [93].

Detecting fake news, especially at an early stage, is complex and challenging due to the characteristics of fake news. Various types of information are integrated when designing detection strategies, including news-related and social-related features [138]. Among the whole process of detection algorithms, extracting information from network-based features is a procedure to improve the performance of detection results. In social media, users form different kinds of networks in terms of interests, topics, and relations. For example, Reference [71] proposed a heterogeneous graph to incorporate all major social actors and their interactions into node representations, which is constructed by user, news, and sources. Other types of networks also exist, for instance, co-occurrence network indicating user engagements, friendship network showing the following relationships, and diffusion network tracking the source of fake news. We refer readers to References [86, 137] for more information about the research on fake news.

7.2 Cyberbullying

Based on the definition of bullying, cyberbullying is, by extension, defined as an aggressive act intentionally carried out by a group or individual using an electronic device, against people who cannot easily defend themselves. Research have shown that cyberbullying is quite prevalent on social media with 54% of young people reportedly cyberbullied on Facebook [82]. Apart from the traditional research using merely content-based features, recent years have witnessed a proliferation of research focusing on incorporating network-based features (e.g., number of friends, uploads,
likes, and so on) in detection systems [87]. For example, Cheng et al. [16] refined the cyberbullying detection problem within a multi-modal context. Then, the problem is a process of multiple modalities exploited in a collaborative fashion.

### 7.3 Fake Reviews
Rating platforms require aggregating a large-scale collection of user reviews and ratings about items (e.g., products, movies, or other users), which play a central role in deciding what service to purchase, restaurant to patronize, and movie to watch, to name but a few. However, fraudulent users give fake ratings and even malicious reviews out of personal interest or prejudice. Therefore, it is necessary to detect such users and eliminate the influence of malicious competition among peers on rating systems.

The algorithm of detecting fraudulent users is formulated as a process to calculate the trustworthiness of a user and its ratings. Networks used in this line of research are diverse, ranging from homogeneous to heterogeneous, such as user-product bipartite network with signed edges [2], homogeneous co-review graph with weighted or unweighted edges [47], and a bipartite rating graph with directed and weighted edges [51].

### 7.4 Electrical Grid
A power grid, also known as an electrical grid, can be constructed as a graph, with nodes denoting generators and edges indicating power lines. Several research questions about anomaly detection or prediction need to be solved in an electrical system. For example, when an electrical component has failed or is going to fail, how could we detect or predict it accurately? Another more challenging problem is to determine the locations of a limited budget of sensors, then it is easier to detect and predict grid anomalies in advance.

Existing anomaly detection algorithms mainly focus on graph theory-based measures instead of graph learning methods. For example, Hooi et al. [38] detected sensor-level anomalies by designing detectors for three common types of anomalies, and constructed an optimization strategy for sensor placement, with the aim of maximizing the probability of detecting an anomaly. Li et al. [55] proposed an index to measure the distance between each past graph and the current graph, thereby generating anomaly scores of a graph in a specific timestamp.

### 7.5 Financial Defaulter
Despite the huge benefits created by online financial services to the society, we have been witnessing a huge growth in financial frauds. The types of frauds in financial scenarios include cash-out behaviors [41], insurance fraud [95], and default users [134]. These frauds severely damage the security of users and service providers, which is a serious problem that needs to be solved.

In financial systems, users engage in interactions and have multiple sources of information. These data form a large multi-view network that conventional methods cannot fully exploit. By integrating the features of various kinds of objects and their interactions, Reference [41] aims to identify whether a user is a cash-out user or not. Default user is defined as a user who is likely to fail to make required payments on time in the future [134]. Hence, these kinds of research questions are generally formulated as binary classification problems.

### 7.6 Anomalous Citations and Co-authors
In the context of big scholarly data, the concept of Academic Social Networks (ASNs) is created. ASNs are complex heterogeneous networks formed by academic entities and their relationships [49], such as co-authorship network, co-citation network, and co-word network. Among
these complex relationships and interactions, abnormal academic behaviors (e.g., citations and collaborations) commonly and implicitly exist in different kinds of ASNs [5].

In References [46], the authors proposed five heuristic rules to define five types of anomalous citation from the perspective of journal-level citation count. Another kind of anomalous citation is defined in terms of citation context, which is identified by analyzing the context similarity between two publications. As for academic collaboration, Fan et al. [31] analyzed the author-paper-author meta-path (co-authorship) to discover rare pattern events in a heterogeneous information network, where each event is denoted by a specific meta-path. To detect anomalous citations, Liu et al. [58] first applied transfer learning to automatically identify unmarked citation purposes and then, applied a deep graph learning framework for anomalous citation detection.

7.7 Urban Computing and Mobile Sensing
In the process of constructing a smart city, urban anomalies like traffic congestion widely occur and sometimes it may bring serious environmental, economic, and social threats to the public [125]. To prevent tragedies, the use of smart devices and sensors to detect urban anomalies is of great value. Since the urban data are collected in real time through mobile devices or distributed sensors, they are generally modeled as spatial-temporal graphs that have timesteps and location tags.

The emergence of urban big data inspired many novel research on anomaly detection and prediction, such as air quality prediction [131], traffic speed prediction [114], and crime detection [103]. By modeling the urban data as a global cross-region hypergraph, Reference [113] proposed to encode crime dependent representations and spatial temporal dynamics for crime prediction. As for intelligent transportation system, Reference [98] proposed a model based on integration of a modified GCN and LSTM to predict anomaly distribution and duration.

8 FUTURE DIRECTIONS
There are several ongoing or future research directions that are worthy of discussion. In this section, we summarize five potential research directions of anomaly analytics on graph data.

8.1 Anomaly Detection on Graphs with Complex Types
Most of the existing research focus on detecting anomalies on simple graphs, while real-world networks are more complicated and have different types, such as heterogeneous graph with multiple node types [123, 128], spatio-temporal graph evolving with time [43], and hypergraph with relations not limited to pairwise relations [97]. Detecting and predicting anomalies on these complex graphs involve technical challenges. For example, as nodes and links that are representing entities and relationships in real-world networks are constantly evolving over time, anomalous entities/relationships might sometimes present normal behaviors as other entities in static networks. This will decrease the accuracy of anomaly detection methods [8]. So, how to model the temporal characteristic of dynamic networks and update real-time graph embeddings remain as important challenges. As for heterogeneous graph anomaly detection, how to incorporate both attribute and structure information of various types of nodes and edges into the graph learning model is a key problem [100]. Therefore, anomaly detection and prediction on complex graphs is still a potential research direction need to be further explored.

8.2 Interpretable and Robust Anomaly Detection Algorithms
Despite the fact that representation learning methods relieve much of the cost of handling features manually, a major limitation of current graph embedding approaches is the lack of interpretability. Unlike the general tasks, an interpretable model for anomaly analytics can help people to understand the results, thereby avoiding the potential model risks and human bias. Apart from result
visualization and benchmark evaluation, efforts must be devoted to improving the interpretability of graph learning methods from the perspective of neural network structures. Interpretable models for anomaly analytics can be presented clearly and are likely to be accepted by the public. For example, Reference [71] could identify which neighbor of an anomalous node influenced most by differentiating the edge weights generated by the attention mechanism. Moreover, it is acknowledged that adversarial attacks will influence the model’s accuracy and performance. Therefore, how to enhance the robustness of a model is another challenge. Several studies regarding interpretability and robustness can be found in References [28, 116, 140].

8.3 Anomalous Subgraph Detection
Recent years have substantially witnessed superior performance on detecting point anomalies, while users in real-world tend to carry out abnormal behaviors in groups, such as spreading rumors and telecommunications fraud. Apart from this, graph data have diverse structures and forms, while existing methods are not available for all situations. Methods regarding group or subgraph anomaly detection have been less explored [119], especially for complex network structures like hypergraph and multi-modal graph.

8.4 Novel Applications of Anomaly Prediction
While most of the works we reviewed aim to detect existing anomalies, there are still significant works to be done in predicting anomalies in advance. For example, predicting traffic jams ahead of time in transportation networks can help people map out another travel route and avoid congestion situations [48]. Therefore, developing representation learning frameworks that are truly appropriate to anomaly prediction settings in a timely manner is necessary to prevent accidents, huge financial loss, or even deaths.

As a special data structure, graphs are often employed as an auxiliary tool to combine with many research fields, such as biology, chemistry, and social science. Considering that anomalies are defined quite different in various scenarios, domain knowledge is thereby necessary when applying anomaly prediction models into novel applications.

8.5 Fairness in Anomaly Analysis
Recent years have witnessed a surge of attention in fair machine learning models [59]. Consequently, several fairness metrics have been proposed as the constraints of objective function in various machine learning models to guarantee the equality of the prediction results. As for anomaly detection tasks, whether users can trust the detection results of the models is still a significant problem [124]. It is due to the fact that incorrect anomaly detection results may sometimes lead to serious consequences, such as wrong object detection when dealing with criminals and fraudsters. In Reference [84], the authors formally defined fairness-aware outlier detection problem and proposed a model to satisfy the fairness criteria. However, fairness on graph anomaly detection is still of concern and deserve further attention.

9 CONCLUSION
In this survey, we comprehensively reviewed anomaly analytics methods using graph learning models. The algorithms are divided into four classifications: graph convolutional network-based methods, graph attention network-based methods, graph autoencoder-based methods, and other graph learning models. A thorough comparison and summarization of these methods are provided in this article. Then, we enumerated and briefly introduced several real-world applications of graph anomaly analytics. Finally, we discussed five future research directions when applying deep learning methods into graph anomaly analytics.
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