Molecules with ALMA at Planet-forming Scales. XX. The Massive Disk around GM Aurigae

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Abstract

Gas mass remains one of the most difficult protoplanetary disk properties to constrain. With much of the protoplanetary disk too cold for the main gas constituent, H2, to emit, alternative tracers such as dust, CO, or the H2 isotopologue HD are used. However, relying on disk mass measurements from any single tracer requires assumptions about the tracer’s abundance relative to H2 and the disk temperature structure. Using new Atacama Large Millimeter/submillimeter Array (ALMA) observations from the Molecules with ALMA at Planet-forming Scales (MAPS) ALMA Large Program as well as archival ALMA observations, we construct a disk physical/chemical model of the protoplanetary disk GM Aur. Our model is in good agreement with the spatially resolved CO isotopologue emission from 11 rotational transitions with spatial resolution ranging from 0”15 to 0”46 (24–73 au at 159 pc) and the spatially unresolved HD J = 1–0 detection from Herschel. Our best-fit model favors a cold protoplanetary disk with a total gas mass of approximately 0.2 $M_\odot$, a factor of 10 reduction in CO gas inside roughly 100 au and a factor of 100 reduction outside of 100 au. Despite its large mass, the disk appears to be on the whole gravitationally stable based on the calculated Toomre Q parameter. However, the region between 70 and 100 au, corresponding to one of the millimeter dust rings, is close to being unstable based on the calculated Toomre Q of <1.7. This paper is part of the MAPS special issue of the Astrophysical Journal Supplement.

Unified Astronomy Thesaurus concepts: Protoplanetary disks (1300); Astrochemistry (75)

1. Introduction

Protoplanetary disk mass is a fundamental property influencing virtually all aspects of the disk’s evolution and the resulting planetary system. It sets a limit on the mass available to forming planets and determines the mechanisms that shape the final system architecture. Gravitational instability (GI) in a protoplanetary disk can result in the formation of massive companions at separations of hundreds of astronomical units from the central star (Boss 1997). Gravitational collapse at early stages results in the formation of close multiple-star systems (Tobin et al. 2018). In other cases, GI can result in the formation of massive planets at wide separation, such as the giant planets proposed to exist in the HD 163296 disk (Isella et al. 2016; Liu et al. 2018; Pinte et al. 2018; Teague et al. 2018).

In a recent study of the HD 163296 system, Booth et al. (2019) found a total disk mass of 0.31 $M_\odot$ based on observations of the optically thin CO isotopologue $^{13}$C$^1$O. They further found that the disk currently is stable against gravitational collapse, though they noted the disk may have been more massive, and thus unstable, in the past, having had ample time to accrete mass onto...
the central star. Analysis of the HL Tau disk using the same $^{13}$C$^{17}$O transition indicates this much younger system surrounded by a residual envelope has a lower total disk mass of 0.2 $M_\odot$ but is likely unstable at radii of 50–110 au (Booth & Ilee 2020), spanning several of the rings and dark bands observed in the millimeter continuum (ALMA Partnership et al. 2015).

Disk gas mass remains one of the most difficult parameters to constrain. This is because the dominant gas component, $H_2$, does not readily emit throughout most of the disk due to its lack of a permanent dipole moment. Instead, trace species such as CO and dust are used to extrapolate to a total gas mass. However, each tracer relies on assumptions that may not be applicable to protoplanetary disks (see Bergin & Williams 2017 for a review).

Converting dust continuum emission to a total dust mass requires assumptions about the grain size distribution, dust composition, scattering, and dust temperature. The dust mass is often then converted to a gas mass assuming a gas-to-dust mass ratio of 100, as measured for the interstellar medium (ISM). However, several processes can change the derived ratio, including differential radial drift for grains of different sizes, dust growth beyond the observable range, accretion onto the central star, and photoevaporative winds. Additionally, observations show that the gas disk often extends far beyond the millimeter dust grains (Guilloteau & Dutrey 1998; Najita & Bergin 2018; Facchini et al. 2019; Trapman et al. 2019).

CO column densities derived from optically thin emission can be converted into a total gas mass assuming a $H_2$/CO ratio of $\sim 10^{-4}$ based on ISM values and correcting for the effects of CO freeze-out in the cold disk midplane and CO photodissociation in the surface layers (Miotello et al. 2014; Williams & Best 2014). However, surveys of protoplanetary disks consistently find a discrepancy between dust-derived and CO-derived disk gas masses, with CO-based measurements generally indicating a lower mass (Ansdell et al. 2016; Long et al. 2017). One potential explanation is that gas-phase CO abundance is further reduced by processes beyond freeze-out and photodissociation, resulting in an underestimate of the total gas. These processes could be physical, such as vertical mixing, which preferentially traps CO in the cold disk midplane (Xu et al. 2017; Krijt et al. 2018), or chemical, with CO processed into other, less emissive species in either the gas or ice (Yu et al. 2016; Bosman et al. 2018; Eistrup et al. 2018; Schwarz et al. 2018).

Alternative tracers are needed to determine the true gas mass in protoplanetary disks. One approach is to use the outer radius of dust emission at different wavelengths to constrain the rate of radial drift (Powell et al. 2017). Masses derived using this technique are significantly larger than those derived from dust or CO line emission (Powell et al. 2019). However, as this analysis does not yet consider the disk substructure, which would impact drift timescales, these values are likely upper limits to the true gas mass.

Another approach is to derive the $H_2$ mass from observations of the $H_2$ isotopologue HD. The HD/$H_2$ ratio of $3 \times 10^{-5}$ is not subject to the same processes that can change the CO/$H_2$ and gas-to-dust mass ratios (Linsky 1998). The HD $J = 1$–0 transition has been detected in three protoplanetary disks using the Herschel Space Observatory, including the Molecules with ALMA at Planet-forming Scales (MAPS) target GM Aur (Bergin et al. 2013; McClure et al. 2016). Upper limits exist for an additional 19 systems (McClure et al. 2016; Kama et al. 2020).

Initial analysis of HD detections has yielded large disk gas masses, more in line with those derived from dust than with those derived from CO (McClure et al. 2016; Trapman et al. 2017). However, the range of disk masses consistent with the observed HD emission strength can be quite large, in some cases spanning more than an order of magnitude. This is due to the strong degeneracy between HD abundance and gas temperature in contributing to the observed HD emission strength. Further, due to the high $J = 1$ upper-state energy, the ground-state transition of HD does not emit at temperatures lower than roughly 20 K (Bergin et al. 2013). Knowledge of the gas temperature structure in the disk from, e.g., spatially resolved CO observations can reduce the uncertainty on the HD-derived gas mass from over an order of magnitude to approximately a factor of two (Trapman et al. 2017).

Subsequent analysis of HD toward one source, TW Hya, has used observations of CO isotopologs to constrain the gas temperature and, when combined with HD, the gas mass (Favre et al. 2013; Schwarz et al. 2016; Zhang et al. 2017). Key results include the fact that HD emits primarily within the inner 20 au of the TW Hya disk, with a gas-to-dust mass ratio of 140 in this region, and a CO/$H_2$ abundance ranging from $< 10^{-6}$ in the outer disk to greater than $10^{-5}$ inside the CO snowline, indicating an overall depletion of gas-phase CO in TW Hya as compared to ISM values. Additionally, Calahan et al. (2021b) demonstrated a wide range of CO abundance and total gas mass are able to reproduce the observed CO emission profiles, while the additional constraint of the HD line provides a way to break this degeneracy.

In this paper we focus on the disk around GM Aur. GM Aur is a 1.1 $M_\odot$ star hosting a well-known transition disk at a distance of 159 pc (Calvet et al. 2005; Hughes et al. 2009; Gaia Collaboration et al. 2018; Macías et al. 2018). We use the CO isotopologue observations of GM Aur from the Atacama Large Millimeter/submillimeter Array (ALMA) Large Program MAPS, along with the HD detection from Herschel, archival ALMA CO observations, and data on the spectral energy distribution (SED) to construct a 2D thermochemical model of the gas density, temperature, and CO abundance in the GM Aur disk. The observations and data reduction process are summarized in Section 2. Section 3 describes the modeling framework used to fit the data. In Section 4 we present the results of our modeling study. In Section 5 we discuss what our results reveal about the gas mass, temperature, and CO abundance in the GM Aur disk. Finally, our conclusions are summarized in Section 6.

2. Observations and Data Reduction

This study uses the CO isotopologue emission toward GM Aur as part of the MAPS Large Program, covering the $^{13}$CO, $^{13}$C$^{18}$O, and $^{17}$O $J = 1$–0 transitions in Band 3 and the $^{12}$CO, $^{13}$CO, and $^{18}$O $J = 2$–1 transitions in Band 6. The full details of the calibration and imaging processes are described in Öberg et al. (2021) and Czekala et al. (2021), respectively. Additionally, we augment these data with CO isotopologs in Band 7 and Band 9 from the ALMA Cycle 4 program 2016.1.00565.S (PI: K. Schwarz), targeting the $^{13}$CO and $^{13}$CO $J = 3$–2 and $^{13}$CO, $^{17}$CO, and $^{17}$O $J = 6$–5 transitions. Observations were obtained in Band 7 on 2016 November 11 with 42 antennas. Observations were obtained in Band 9 on
2018 August 18 with 48 antennas. The continuum data associated with the Band 7 observations was previously analyzed by Macías et al. (2018).

Initial calibration of the archival Band 7 and 9 data was carried out by ALMA/NAASC staff using standard procedures. Additionally, phase and amplitude self-calibration were performed in each band using the continuum visibilities. The fixvis task was used to correct the phase center of each data set. Imaging was performed in CASA 5.4 using the imaging scripts developed by Czekala et al. (2021). The channel widths used in the imaging are 0.2 km s\(^{-1}\) in Band 7 and 0.3 km s\(^{-1}\) in Band 9. The properties of the final CLEAN images, with a robust weighting of 0.5, are given in Table 1 and the moment 0 maps are shown in Figure 1. All lines are detected, including the associated with the Band 7 observations was previously performed in each band using the continuum visibilities.

### Table 1

| Molecular Transition | Beam \((\theta \times \phi, \text{deg})\) | rms \((\text{mJy beam}^{-1})\) | Channel Spacing \((\text{km s}^{-1})\) | Program ID |
|----------------------|-------------------------------|-----------------|------------------|-------------|
| C\(^{18}\)O \(J = 1-0\) | \((0.30 \times 0.30, 75.0)\) | 0.514 | 0.5 | 2018.1.01055.L |
| \(^{13}\)CO \(J = 1-0\) | \((0.30 \times 0.30, 81.1)\) | 0.498 | 0.5 | 2018.1.01055.L |
| C\(^{17}\)O \(J = 1-0, F = \frac{3}{2}, \frac{1}{2}\) | \((0.30 \times 0.30, -29.8)\) | 0.629 | 0.5 | 2018.1.01055.L |
| C\(^{17}\)O \(J = 1-0, F = \frac{3}{2}, \frac{3}{2}\) | \((0.30 \times 0.30, -29.8)\) | 0.629 | 0.5 | 2018.1.01055.L |
| C\(^{18}\)O \(J = 2-1\) | \((0.15 \times 0.15, 54.8)\) | 0.484 | 0.2 | 2018.1.01055.L |
| \(^{13}\)CO \(J = 2-1\) | \((0.15 \times 0.15, 72.4)\) | 0.660 | 0.2 | 2018.1.01055.L |
| CO \(J = 2-1\) | \((0.15 \times 0.15, 66.3)\) | 0.730 | 0.2 | 2018.1.01055.L |
| C\(^{18}\)O \(J = 3-2\) | \((0.37 \times 0.27, 6.7)\) | 9.2 | 0.2 | 2016.1.00565.S |
| C\(^{17}\)O \(J = 3-2\) | \((0.38 \times 0.27, 7.5)\) | 8.3 | 0.2 | 2016.1.00565.S |
| C\(^{18}\)O \(J = 6-5\) | \((0.46 \times 0.26, 3.8)\) | 48.7 | 0.3 | 2016.1.00565.S |
| \(^{13}\)CO \(J = 6-5\) | \((0.46 \times 0.26, 3.7)\) | 56.1 | 0.3 | 2016.1.00565.S |
| C\(^{17}\)O \(J = 6-5\) | \((0.45 \times 0.26, 4.7)\) | 57.1 | 0.3 | 2016.1.00565.S |

3. Methods

3.1. Physical Model

Our physical disk model is based on an axisymmetric viscously evolving disk (Lynden-Bell & Pringle 1974; Andrews et al. 2011). The surface densities of both gas and dust are described by

\[
\Sigma(R) = \sum_c \left( \frac{R_c}{R} \right)^{\gamma - 2} \exp \left[ -\left( \frac{R}{R_c} \right)^2 \right].
\]

where \(\Sigma_c / e\) is the surface density at a characteristic radius \(R_c\). The 2D density distribution is then

\[
\rho(R, Z) = \frac{\Sigma}{\sqrt{2\pi} R \rho h} \exp \left[ -\frac{1}{2} \left( \frac{Z}{h} \right)^2 \right].
\]

The scale height \(h\) varies as a function of the radius such that

\[
h(R) = h_{\text{ref}} \left( \frac{R}{R_{\text{ref}}} \right)^{\psi}.
\]

where \(h_{\text{ref}}\) is the characteristic scale height at a radius \(R_{\text{ref}}\) and \(\psi\) is the power-law index characterizing disk flaring. Our disk includes three populations of matter: gas, small grains, and large grains. The small grains are well mixed with the gas, i.e., they have the same scale height, and follow the same surface density profile. The scale height of the large grains is smaller than that of the gas and small grains to mimic vertical settling. Further, while the gas and small grains vary smoothly, the large-grain surface density includes several depleted regions corresponding to the gaps seen in continuum emission (Huang et al. 2020). For our large-grain model we start with the surface density profile from the model of Macías et al. (2018). This model includes rings and gaps and was able to reproduce both the millimeter- and centimeter-continuum emission. The initial large-grain distribution is then adjusted as described by Zhang et al. (2021).

3.2. SED Fitting

Our initial values for the disk model were determined by fitting the SED. The general procedure for modeling the SEDs of all MAPS sources is described in detail by Zhang et al. (2021) and we use the same dust surface density models for GM Aur as in that work. Briefly, data is fit using RADMC-3D (Dullemond et al. 2012). The large grains range in size from 0.005 \(\mu\)m to 1 mm with an MRN distribution \(n(a) \propto a^{-3.5}\) (Mathis et al. 1977) and use the standard dust opacities from Birnstiel et al. (2018), who assumed dust composed of 20% H\(_2\)O ice, 32.9% astronomical silicates, 7.4% troilite, and 39.7% refractory organics by mass. This differs from the 38% graphite and 62% silicate composition used in previous SED modeling of GM Aur (Espaillat et al. 2011), necessitating some modification of the dust surface density profile from Macías et al. (2018). The small grains have a size range of 0.005 to 1 \(\mu\)m with an MRN distribution and are assumed to be composed of equal parts silicates and refractory organics by mass. At large scale heights, where most of the dust mass is in small grains, models suggest water is removed from grains via photodesorption (Hogerheijde et al. 2011). For a given large- and small-grain distribution, we used RADMC-3D to compare our model to the observed SED and ALMA continuum image.

3.3. Thermochemical Models

After using the SED to constrain the dust distribution we pass our disk density model to the 2D thermochemical modeling code RAC2D to model the molecular line emission. RAC2D self-consistently computes the chemistry as well as the
evolving balance between heating and cooling in the disk. The modeling framework is described in detail by Du & Bergin (2014). For each model run \textsc{Rac2D} first calculates the dust thermal structure, cosmic-ray attenuation, and radiation field, taking into account photon scatter and absorption. We assume a cosmic-ray ionization rate at the disk surface of \(1.38 \times 10^{-18}\) s\(^{-1}\) per H\(_2\), consistent with cosmic-ray modulation by stellar winds (Cleeves et al. 2013). The chemical evolution and gas temperature structure are then solved simultaneously.

The chemical network is based on the gas-phase network from the UMIST 2006 database (Woodall et al. 2007) and the grain surface network of Hasegawa et al. (1992). We consider a total of 5830 reactions among 484 species. The chemical network includes two-body gas-phase reactions, photodissociation (including Ly\(\alpha\) dissociation of H\(_2\)O and OH), adsorption of species onto grain surfaces, thermal desorption, UV photodesorption, and cosmic-ray-induced desorption, as well as a limited network of two-body grain surface reactions. The default initial chemical composition is given in Table 2.

The chemistry is run for 1 Myr. The main consequence of changing the run time is the amount of chemical processing of CO that takes place, as the gas and dust temperatures converge on much shorter timescales. However, we adjust our initial CO abundance in order to match the observed CO line emission profiles, as described in Section 3.4. Thus, the decision on how long to run the chemistry does not impact our final results.

Line radiative transfer calculations assuming local thermal equilibrium are also carried out using \textsc{Rac2D}. Line and continuum emission are modeled together using the source properties in Table 3. The resulting image cubes are then continuum-subtracted and convolved with an elliptical Gaussian beam with the same size.
and orientation as the corresponding observation before comparison to the observations. By treating the dust continuum and line emission simultaneously, we account for any extinction of the line emission by the dust. Our chemical network is not fractionated to include species such as $^{13}$C, $^{18}$O, and deuterium. Instead, isotopologue emission profiles are generated assuming $^{13}$C/$^{12}$C $= 69$, $^{18}$O/$^{16}$O $= 557$, $^{17}$O/$^{16}$O $= 3.6$, and $D/H = 1.5 \times 10^{-5}$ as measured in the local ISM (Linsky 1998; Wilson 1999).

### 3.4. Parameter Study

The mass in dust is constrained by the continuum imaging and the SED. In attempting to fit the line emission we limit our parameter study to the total gas mass and the variables that determine the gas and dust density distribution: $\gamma$, $R_e$, $h_{\text{ref}}$, and $\psi$, as well as the initial CO abundance and the gas temperature in the inner disk, as discussed in Section 4. In total we generate 145 unique models. The range of parameters considered is given in Table 4. Due to the long run times required for each model, it is unrealistic to use a systematic parameter study using, e.g., a Markov Chain Monte Carlo method to find the best-fit model. Instead, parameters are changed one at a time in order to achieve a reasonable fit.

We modify the CO abundance before modeling the chemistry, in contrast with the CO abundance study of Zhang et al. (2021), who modified the CO abundance after modeling the chemistry. Because RAC2D includes line processes when calculating the gas temperature, our choice to remove CO initially impacts the gas temperature structure and, by extension, the strength of the HD $J = 1-0$ emission. In constructing our initial model we use the same disk parameters as the best-fit model of Zhang et al. (2021). Initially, we use the CO depletion profile of Zhang et al. (2021). We then run additional thermochemical models with the depletion profile multiplied by a constant factor ranging from 0.1 to 2. To quantify how well a given model fits the data we calculate the reduced $\chi^2$ for the CO isotopologue emission radial profiles, comparing the model and observed emission at half beam spacing. We construct a new initial CO abundance profile taking the best fit based on the reduced $\chi^2$ at each radius. This model, using an updated CO abundance profile but otherwise using the same parameters as the best-fit model from Zhang et al. (2021), serves as our initial model.

To constrain the model in the vertical direction we compare the extracted emission surfaces from the observations and models for the $^{18}$O $J = 2-1$, $^{13}$CO $J = 2-1$, $^{12}$CO $J = 2-1$, and $^{17}$CO $J = 3-2$ lines. The signal-to-noise ratios of the other transitions are too low to meaningfully constrain the emission height. Emission surfaces for both the observations and the models are extracted with the Python package disksurf, using the method presented by Pinte et al. (2018).

### Table 3

| Source Properties | Value | Reference |
|-------------------|-------|-----------|
| Distance (pc) | 159 | Gaia Collaboration et al. (2018) |
| $i$ (deg) | 53.2 | Huang et al. (2020) |
| P.A. (deg) | 57.2 | Huang et al. (2020) |
| $T_{\text{eff}}$ (K) | 4550 | Espaillat et al. (2011) |
| $M_e$ ($M_\odot$) | 1.1 | Macías et al. (2018) |
| $R_e$ ($R_\odot$) | 1.9 | Macías et al. (2018) |

### Table 4

| Range of Parameter Values Considered | Gas | Small Dust | Large Dust |
|-------------------------------------|-----|------------|------------|
| Mass ($M_\odot$) | 0.02–0.41 | $1.03 \times 10^{-4}$ | $5.94 \times 10^{-4}$ |
| $\psi$ | $1-2$ | $1-2$ | $1-2$ |
| $\gamma$ | 0.3–1.5 | 0.3–1.5 | $\ldots$ |
| $R_e$ (au) | 100–176 | $100-176$ | $\ldots$ |
| $h_{\text{ref}}$ (au) | 5–12 | 5–12 | 0.75–12 |
| $R_m$ (au) | 0.5–27 | $\ldots$ | $\ldots$ |
| CO/H | $7 \times 10^{-7}$–$1.4 \times 10^{-3}$ | $\ldots$ | $\ldots$ |

### Note.

$^a$ The $\psi$ for the gas and small grains are varied together, while the $\psi$ for the large grains is changed independently.

### Table 5

| Gas and Dust Population Parameters: Initial Model Values | Gas | Small Dust | Large Dust |
|---------------------------------------------------------|-----|------------|------------|
| Mass ($M_\odot$) | 0.2 | $1.03 \times 10^{-4}$ | $5.94 \times 10^{-4}$ |
| $\psi$ | 1.35 | 1.35 | 1.35 |
| $\gamma$ | 1.0 | 1.0 | 1.0 |
| $R_e$ (au) | 176 | 111 | $\ldots$ |
| $R_m$ (au) | 100 | 100 | 100 |
| $h_{\text{ref}}$ (au) | 7.5 | 7.5 | 3.75 |
| $R_m$ (au) | 1.0 | 1.0 | 34 |
| $R_m$ (au) | 650 | 650 | 310 |

The parameters for our initial model, based on the best-fit model of Zhang et al. (2021), are given in Table 5. This model fits the radial intensity profiles for the majority of the observed lines within $1\sigma$ outside of 160 au (1") (Figure 2). Inside 160 au, the model underpredicts the line flux for nearly all transitions. The integrated HD $J = 1-0$ flux in our initial model is $1.9 \times 10^{-18}$ W m$^{-2}$ compared to the observed $2.5 \pm 0.5 \times 10^{-18}$ W m$^{-2}$, just below the $1\sigma$ uncertainty. In the outer disk the model emission surfaces for the $^{13}$CO lines are below the $1\sigma$ uncertainty of the surfaces derived from observations, while for CO$^{18}$O the model over predicts the emission surface (Figure 3).

To raise outer-disk emission surfaces in our model, we modify the surface density profile of the gas and small grains by changing $R_e$ and $\gamma$, thus shifting more mass to larger radii, and modify the disk flaring by adjusting $\psi$. We also consider models with varying total gas mass (see Table 4) but find that holding the gas mass at 0.2 $M_\odot$ provides the best fit to the data. After adjusting the gas surface density, we modify the initial CO depletion profile as described in Section 3.4 in order to match the observed radial emission profiles. The resulting model brings the CO$^{18}$O $2-1$, $^{13}$CO $2-1$, and $^{13}$CO $3-2$ model emission surfaces within the $1\sigma$ uncertainty of the surfaces derived from observations throughout much of the disk (Figure 3). Further, the model HD flux increases from $1.9 \times 10^{-18}$ W m$^{-2}$ in our initial model to

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27 https://github.com/richteague/disksurf
In the inner disk the model underpredicts the strength of the $^{12}$CO 2–1 emission by a factor of 2.6, while providing a reasonable fit to the emission from the less abundant CO isotopologs (Figure 4). The emission surface profiles derived from observations show that $^{12}$CO emission originates from higher in the disk than the other lines. To fit the $^{12}$CO $J = 2–1$ emission in the inner disk we increase the temperature inside 32 au and for $Z/R > 0.1$. Increasing the gas temperature by a factor of 10 in this region, from several tens of kelvin to several hundred kelvin, greatly improves the agreement between the model $^{12}$CO $J = 2–1$ emission and the observations without significantly increasing emission from the other lines (Figure 5). Possible sources of this extra heating are discussed below. Increasing the temperature in the inner disk has a negligible effect on the model HD flux. This model, with an increased temperature in the inner disk, provides the best fit to the data. The input values for our best-fit model are shown in Table 6 and the 2D hydrogen gas distribution, dust temperature, and gas temperature are shown in Figure 6. However, because of our sparsely sampled parameter space we cannot rule out the possibility of other model solutions fitting the data equally well.

In order to match the $^{12}$CO 2–1 flux in the inner disk, we need to increase the gas temperature in the surface layers of the inner disk. The primary source of dust heating in RAC2D is radiation from the central star. The gas temperature is initially assumed to be the same as the dust temperature and allowed to evolve due to a number of heating and cooling processes, including photoelectric heating, endothermic and exothermic chemical reactions, and viscous dissipation (Du & Bergin 2014). However, in the surface layers of the inner disk photoelectric heating of polycyclic aromatic hydrocarbons (PAHs) can be an important contributor to the local gas temperature (Kamp & Dullemond 2004; Woitke et al. 2016). While heating by PAHs is included in RAC2D, the PAH abundance in the disk surface layers is uncertain. We assume a PAH abundance relative to H of $1.6 \times 10^{-7}$ (Du & Bergin 2014). A higher PAH abundance could result in increased photoelectric heating and thus in a warmer disk surface.

Alternatively, mechanical heating mechanisms such as stellar winds and accretion onto the central star can raise the temperature of the inner disk. When including mechanical heating, both Glassgold et al. (2004) and Najita & Ádámkovics (2017) found temperatures of several hundred kelvin for vertical column densities equivalent to those in the region of our model where we artificially increase the temperature, though these models looked at full disks without a large central dust cavity as seen in the GM Aur disk. Calahan et al. (2021a) also found that their RAC2D model requires additional heating to match the observed $^{12}$CO $J = 2–1$ flux in the HD 163296 disk inside 32 au, further suggesting that underprediction of emission in the surface layers of the inner disk is due to limitations in the code.

![Figure 2](image-url)
4.1. CO Abundance

Figure 7 shows the CO abundance relative to H$_2$ as a function of height and radius in our best-fit model. CO is effectively frozen out from the gas near the midplane from 75 to 250 au. Outside the millimeter dust disk, the gas temperature remains below the CO freeze-out temperature. However, nonthermal desorption by UV photons allows some CO to remain in the gas (e.g., Öberg et al. 2015). In the region directly above the CO freeze-out layer, gas-phase CO has been converted into CO$_2$ ice (e.g., Reboussin et al. 2015; Bosman et al. 2018). Closer to the disk surface, where the temperature exceeds the CO$_2$ freeze-out temperature, CO remains in the gas.

Figure 8 compares the CO depletion profile after evolution of the chemistry in our best-fit model for 1 Myr to that found by Zhang et al. (2021). Both results follow the general trend of a roughly constant, high level of CO depletion outside of roughly 100 au, with the inner disk less depleted in CO. The location of the midplane CO snowline in our model, here defined as where the CO gas and ice abundances are equal, is 31 au, consistent with the derived CO snowline of 30 ± 5 au from Zhang et al. (2021). Our model has greater CO depletion inside 200 au, as well as a more abrupt return of CO in the inner disk compared to the Zhang et al. (2021) results. The abrupt change in the CO column is due to the conversion of CO gas into CO$_2$ ice and CH$_4$ ice near the midplane at roughly 90–150 au, which is not seen to the same extent in the Zhang et al. (2021) model. Given that the two approaches remove CO from the disk at different points in the modeling process, and that this work attempts to match a greater number of observations, some variation is to be expected.

5. Discussion

5.1. 2D Temperature and CO Distribution

Figure 9 shows the 2D gas temperature distribution in a subset of our models with the derived temperatures for the $^{12}$CO $J=2$–1, $^{13}$CO $J=2$–1, and $^{13}$CO $J=3$–2 surfaces overplotted. C$^{18}$O $J=2$–1 is not included as this emission is optically thin and thus is not a good temperature tracer. The temperature extraction follows the same process described by Law et al. (2021). Briefly, the gas temperature is determined from the peak surface brightness at a given radius for the non-continuum-subtracted line image cubes using the full Planck function and assuming the line emission is optically thick. Using non-continuum-subtracted data to measure the temperature ensures the temperature is not underestimated in the case of optically thick dust emission (Weaver et al. 2018). In the
layers traced by the $^{13}$CO $J = 2–1$ and $J = 3–2$ lines our best-fit model temperature is in reasonable agreement with the data, with the model gas temperature varying by less than 10 K from the measured temperature at most radii (Figure 10).

However, at larger heights our model is over two times warmer than the temperature measured from the $^{12}$CO $J = 2–1$ emission surface. Past models of CO emission in protoplanetary disks have cooled the upper layers of the disk by increasing dust settling (McClure et al. 2016; Calahan et al. 2021a). We test this solution by decreasing the scale height of the small dust grains in our model. Decreasing the small-grain scale height from 7.5 to 5 au does in fact decrease the gas temperature in some regions of the disk, particularly in the upper layers beyond 400 au (Figure 9). However, the regions traced by CO emission are warmer in this model, increasing the discrepancy between the model and the observations (Figure 10).

An alternative explanation is that the upper layers of the disk are warmer and more CO-rich than we assume in our models. If material is falling onto the disk from a residual cloud or envelope—the favored explanation for the nonaxisymmetric features seen in $^{12}$CO $J = 2–1$ (Huang et al. 2014)—the infalling material is expected to produce shock heating (Sakai et al. 2014). This heating will enhance the gas temperature in the surface layers from which $^{12}$CO emits. Additionally, the infalling material is unlikely to have undergone much chemical processing, and thus will have a CO/H$_2$ abundance ratio similar to that of the dense ISM. While the amount of CO supplied to the disk by a residual envelope is likely to be small, the combination of increased temperature and elevated CO/H$_2$ could result in some $^{12}$CO emission originating closer to the disk surface.

5.2. Mass Traced by HD and Comparison to Previous Work

Figure 11 shows the distribution of the HD emission in our best-fit model. Seventy-five percent of the HD emission originates from the inner 100 au. In particular, the hot, low-density gas inside the millimeter dust inner radius at 32 au contributes a non-negligible amount to the HD flux. In comparison, only 47% of the total disk gas mass is inside 100 au. Since HD does not readily emit at temperatures less than $\sim$20 K, much of the disk beyond 100 au is not well traced by the HD $J = 1–0$ emission. There may be more mass in the outer disk than accounted for in our best-fit model. Additional analysis, e.g., using CS emission (Teague et al. 2018), is needed to better constrain the gas density in the outer disk.

Previous analysis of HD detection by McClure et al. (2016) in GM Aur constrains the disk gas mass to 0.025–0.204 $M_\odot$. Based on analysis of the millimeter and centimeter continuum, Macías et al. (2018) found a total dust mass of 2 $M_\odot$. Assuming a gas-to-dust mass ratio of 100, this corresponds to a total gas mass of 0.19 $M_\odot$, at the high end of the range given by McClure et al. (2016). Trapman et al. (2017) reanalyzed the HD detection in GM Aur by comparing to the HD line flux in a grid of generic 2D thermochemical models. They constrained the mass of the GM Aur disk to between 0.01 $M_\odot$ and a few.
tenths of a solar mass. Woitke et al. (2019) have also built a model of the GM Aur disk as part of the DIANA project. Their model based on the observed SED has a total disk mass of 0.11 $M_\odot$ and also reasonably reproduces the observed total flux of the 63 $\mu$m [OI] line as well as the $^{13}$CO 2–1 and HCO$^+$ 3–2 lines. Their final model, independent of the SED fit and based on Submillimeter Array (SMA) observations of the $^{12}$CO $J = 2–1$ line, has a disk mass of $3.3 \times 10^{-2} M_\odot$.

Our best-fit model has a total gas mass of 0.2 $M_\odot$, consistent with the upper limits of previous works. This high value comes in part from our overall low disk temperature, needed to match the gas temperature from CO observations. Additionally,
previous works have set the outer radius of the disk to 250–300 au. Here we set the disk outer radius to 650 au based on the observed extent of the $^{12}\text{CO}$ 2–1 emission, though less than 3% of the total gas mass is outside of 300 au.

### 5.3. Disk Stability

The stability of a rotating disk against gravitational collapse is often characterized using the Toomre $Q$ parameter (Toomre 1964):

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

where $c_s$ is the gas sound speed assuming the midplane gas temperature, $\Omega$ is the Keplerian angular velocity of the disk, and $\Sigma$ is the total gas+dust surface density. For a geometrically thin disk $Q \sim 1$ is needed for density perturbations to develop. However, numerical simulations demonstrate that instabilities can develop for $Q < 1.7$ in systems not well approximated by a geometrically thin disk (Helled et al. 2014). Figure 12 shows the Toomre $Q$ radial profile using values from our best-fit disk model.

Our calculated $Q$ value for GM Aur is greater than 1.7 throughout much of the disk. In the outer disk, where spiral-like features are seen in the $^{12}\text{CO}$ 2–1 emission, our calculated $Q$ is extremely high, ranging from $\sim$7 at 250 au to $\sim$700 at 500 au. The two values in our model that determine $Q$ are temperature and surface density. Without changing the surface density, the midplane temperature at 250 au would need to be unrealistically low, $\sim$1 K, to reach a $Q$ of 1.7.

As discussed in the previous section, HD detection does not constrain the gas surface density in the outer disk. The model surface density would need to be increased by a factor of four at 250 au to reach a $Q$ of 1.7 while holding the temperature constant. Zhang et al. (2021) note that for four of the five MAPS sources, including GM Aur, the CO column density profiles are very shallow, consistent with a viscously evolving disk. This supports the conclusion of Huang et al. (2021), who argue against the nonaxisymmetric features seen in $^{12}\text{CO}$ $J = 2$–1 being driven exclusively by disk instability based on the kinematics.

However, $Q$ dips below 1.7 from 70 to 100 au, corresponding to the location of one of the bright rings seen in the continuum. The concentration of large dust grains in this region increases the disk opacity and thus decreases the temperature of both the gas and the dust. This lower temperature, in turn, results in a lower sound speed and thus in a lower Toomre $Q$ value. The presence of dust rings and gaps can lower the midplane temperature by several kelvin as compared to a disk with a smoothly varying surface density profile (Facchini et al. 2018; van der Marel et al. 2018; Alarcón et al. 2020; Calahan et al. 2021).

The dip in Toomre $Q$ in our model is due entirely to an overdensity of dust. Our model is able to fit the CO emission profiles in this region without a corresponding increase in the gas density. Decreasing the disk surface density to 88% of our assumed value between 70 and 100 au would bring the dust ring into a gravitationally stable regime. Alternatively, a warmer temperature than assumed would also lead to a higher $Q$. Between 70 and 100 au our model midplane temperature is $\sim$12 K. The temperature derived from the observed $^{13}\text{CO}$ 2–1 line is $\sim$22 K and can be considered an upper limit on the midplane temperature. We use the temperature from $^{13}\text{CO}$ because $^{18}\text{O}$ is optically thin at these radii and therefore not a good tracer of temperature. Taking the midplane temperature to
be 22 K increases the $Q$ value to 2.0. Interestingly, recent smoothed particle hydrodynamics modeling shows that a migrating planet can increase the local disk temperature, suppressing spiral-structure development and stabilizing the disk (Rowther et al. 2020).

GI is thought to primarily manifest as nonaxisymmetric features. Previous analysis of the continuum disk emission at far-UV wavelengths does not indicate any such features in the 70–120 au range (Hornbeck et al. 2016). No nonaxisymmetric substructure is seen in the CO emission profiles in this region. However, the intensity of the bright continuum ring at 40 au at 7 mm shows a low signal-to-noise ($\sim-2\sigma$) asymmetry (Macgas et al. 2018). While the ring at 84 au is not detected at 7 mm with high enough sensitivity to enable a similar analysis, Huang et al. (2020) note that the 84 au ring is nonaxisymmetric at 1.1 mm. The ring appears wider along the major axis of the disk, which as Huang et al. (2020) demonstrate is unlikely to be an imaging artifact; instead the variation can be attributed to either a nonaxisymmetric or a vertical structure within the ring.

An interesting point of comparison is the HL Tau disk, which, though less evolved than GM Aur, has a similar total gas mass and a region of instability centered on a dust gap (Booth & Ilee 2020). A spiral structure is also seen in the HCO$^+$ $J = 3-2$ emission toward HL Tau (Yen et al. 2019). While this spiral structure was originally attributed to the infalling envelope, Booth & Ilee (2020) note that the feature could also be associated with the region of instability in the disk. Conversely, observations of HCO$^+$ $J = 3-2$ toward GM Aur do not appear to deviate substantially from Keplerian rotation (Huang et al. 2020). It is possible that the GM Aur disk is in the process of stabilizing after a period of infall or planet formation. Given the limitations of using Toomre $Q$ to determine the stability of a non–geometrically thin disk, a more detailed study of the kinematics is required to determine the stability of the GM Aur disk from 70 to 100 au.

6. Summary and Conclusions

In this work we use observations of CO isotopologs in the GM Aur disk taken as part of the MAPS ALMA Large Program along with archival observations of CO from ALMA and HD from Herschel to build a model of the disk gas density.
and temperature structure. Based on our results we conclude the following:

1. Much of the disk (32% by mass) is cooler than 20 K. As such the HD emission only traces the inner 200 au, while the gas disk extends to 650 au based on observations of $^{12}$CO.

2. We constrain the gas mass of the GM Aur disk to $\sim 0.2 M_\odot$. While the total mass in the outer disk remains somewhat uncertain, only 15% of the mass in our best-fit model is beyond 200 au. Any variation in mass in the outer disk will likely have only a small effect on the total disk mass.

3. The CO gas abundance relative to H$_2$ is reduced by approximately one order of magnitude with respect to the ISM values inside 100 au and by two orders of magnitude outside 100 au. This is consistent with the analysis of Zhang et al. (2021). Our model also shows CO gas returning to the midplane outside of the millimeter dust disk due to nonthermal desorption.

4. Based on the calculated Toomre $Q$ parameter, the outer disk appears stable against gravitational collapse. However, $Q$ dips into the unstable regime between 70 and 100 au, corresponding to the second bright ring seen in millimeter dust emission. While there is some evidence for nonaxisymmetric features in the dust continuum at these radii, a more detailed study is needed to determine if the GM Aur disk is gravitationally unstable.
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Software: analysisUtils (https://casuguides.nrao.edu/index.php/Analysis_Utilsities), Astropy (Astropy Collaboration et al. 2013), CASA (McMullin et al. 2007), disksurf (https://github.com/richtega/disksurf), Matplotlib (Hunter 2007), NumPy (van der Walt et al. 2011), RAC2D (Du & Bergin 2014), RADMC-3D, (Dullemond et al. 2012), SciPy (Jones et al. 2001).

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