The influence of geometry, surface character, and flexibility on the permeation of ions and water through biological pores

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Abstract
A hydrophobic constriction site can act as an efficient barrier to ion and water permeation if its diameter is less than the diameter of an ion’s first hydration shell. This hydrophobic gating mechanism is thought to operate in a number of ion channels, e.g. the nicotinic receptor, bacterial mechanosensitive channels (MscL and MscS) and perhaps in some potassium channels (e.g. KcsA, MthK and KvAP). Simplified pore models allow one to investigate the primary characteristics of a conduction pathway, namely its geometry (shape, pore length, and radius), the chemical character of the pore wall surface, and its local flexibility and surface roughness. Our extended (about 0.1 µs) molecular dynamic simulations show that a short hydrophobic pore is closed to water for radii smaller than 0.45 nm. By increasing the polarity of the pore wall (and thus reducing its hydrophobicity) the transition radius can be decreased until for hydrophilic pores liquid water is stable down to a radius comparable to a water molecule’s radius. Ions behave similarly but the transition from conducting to non-conducting pores is even steeper and occurs at a radius of 0.65 nm for hydrophobic pores. The presence of water vapour in a constriction zone indicates a barrier for ion permeation. A thermodynamic model can explain the behaviour of water in nanopores in terms of the surface tensions, which leads to a simple measure of ‘hydrophobicity’ in this context. Furthermore, increased local flexibility decreases the permeability of polar species. An increase in temperature has the same effect, and we hypothesize that both effects can be explained by a decrease in the effective solvent–surface attraction which in turn leads to an increase in the solvent–wall surface free energy.

Nomenclature

| MD | molecular dynamics |
| SPC | simple point charge water model |
| RMSD | root mean square deviation |
| nAChR | nicotinic acetylcholine receptor |
| MscS | mechanosensitive channel of small conductance (Escherichia coli) |
| MscL | mechanosensitive channel of large conductance (Mycobacterium tuberculosis) |
| KcsA | potassium channel (Streptomyces lividans) |
| KirBac1.1 | inward rectifier potassium channel (Burkholderia pseudomallei) |
| MthK | calcium-gated potassium channel (Methanobacterium thermoautotrophicum) |
| KvAP | voltage-dependent potassium channel (Aeropyrum pernix) |
| D2 | model pore containing two dipoles (amphipathic) |
| D4 | model pore containing four dipoles (hydrophilic) |
| TRP | transient receptor potential channel family |
KTN potassium transport, nucleotide binding domain
TRAP trp RNA-binding attenuation protein
Trp tryptophan
mRNA messenger RNA

1. Introduction

Although only about 3 nm thick, the membranes of living cells present an efficient barrier to polar substances such as water or ions. Transport of water and ions into and out of the cell is facilitated by specialized proteins. For molecules that move down their electro-osmotic gradients the proteins are ion channels [1] and water pores (aquaporins) [2]. They share common functional characteristics such as high specificity (for instance, the potassium channel KcsA prefers potassium ions over sodium ions, aquaporins allow the flow of water but not of ions or protons) and transport rates comparable to diffusion in bulk solution. Ion channels can also be switched (‘gated’) between an open (ion conducting) and closed (ion blocking) state by external signals such as changes in transmembrane voltage, binding of a ligand, mechanical stress etc.

In recent years a number of near atomic resolution structures of ion channels [3–10] and aquaporins [11–14] have been published. Based on these structures an atomistic understanding of the transport and gating properties is emerging. If we view transport proteins as molecular machines which are designed by evolution to perform selective and efficient transport that can be controlled, i.e. gated, then we can ask what the ‘building blocks’ of these machines are. This involves not only identification and structural characterization of the protein domains involved in gating, but also, at a more abstract level, understanding the underlying physical principles.

Here we address the questions: what are the physical properties that are important for the permeation of ions and water, and what is their effect? In particular we will focus on how the flow of ions and water can be controlled, i.e. we will investigate possible gating mechanisms. This interest is based on the observation that the putative gate in many known ion channel structures (in particular, the nicotinic acetylcholine receptor nAChR [10], the bacterial potassium channels KcsA [3] and KirBac1.1 [9], and the mechanosensitive channels MscL [4] and MscS [5]) is formed by a constriction made by hydrophobic residues. For example, the closed state nAChR structure displays an ion pathway which is still wide enough (radius $R \approx 0.31$ nm) to admit three water molecules (radius of a water molecule $r_w = 0.14$ nm) or one potassium ion ($r_K = 0.133$ nm) with half of its first hydration shell intact. It is somewhat surprising that a pore does not have to be completely physically occluded to prevent the flow of ions. On the other hand ions can readily move through the KcsA [3, 5] selectivity filter although its radius is less than 0.15 nm. When an ion enters the filter it has to shed its hydration shell at a high cost in free energy—the solvation free energy for a potassium ion is about $-320$ kJ mol$^{-1}$ [15]. The filter is lined by backbone oxygen atoms which coordinate the potassium ion and substitute for its hydration shell, thus reducing the desolvation barrier of $+320$ kJ mol$^{-1}$ to about $+12$ kJ mol$^{-1}$ [16]. The putative gates differ from the selectivity filter in that they are lined by hydrophobic residues. For nAChR [10, 17] and MscL [4, 18] it was already hypothesized that these residues cannot substitute for water molecules so that the energetic cost of desolvation prevents the passage of the ion.

It appears that the geometry of a pore (its radius, length and shape) and the chemical character of the pore wall have a great influence on the permeation of ions and water. In addition, local flexibility (i.e. fluctuations in the protein structure as opposed to concerted larger scale motions) of the pore lining might play a role, as seen in simulations of $K^+$ permeation through KcsA [16].

It seems difficult to comprehend the dynamical nature of transport phenomena from static crystal structures alone. Computational methods can be used to complement the experimentally observed picture. In particular, classical molecular dynamics (MD) can be used to investigate the behaviour of water or ionic solutions in the environment presented by a protein. This realistic environment, however, makes it difficult to disentangle the contributions of various pore properties. In order to be able to reduce the number of parameters simplified pore models can be designed to capture the characteristics in question [19–25]. We focus on the influence of geometry, pore wall character and flexibility.

In previous studies we investigated the behaviour of water in these ‘nanopores’. In particular, we found that below a critical radius liquid water becomes unstable in the pore and the pore is predominantly filled with water vapour [25]. We hypothesized that a pore environment which cannot sustain liquid water would also present a high energetic barrier to an ion [21]. Although it seems plausible that the absence of water would imply the absence of ions, it has not been demonstrated previously.

In this work we explicitly consider ions in model pores and explore dimensions, pore wall character and flexibility in more detail than in our previous work. We also present a simple thermodynamic model based on surface energies that explains the observed behaviour of water in hydrophobic pores.

2. Methods and theory

2.1. Model

The pore models were constructed as described previously [25]. Briefly, they consist of concentric rings of methane-like pseudo-atoms of van der Waals radius $0.195$ nm (figure 1). These are held in their equilibrium position by harmonic constraints with spring constant $k_o = 1000$ kJ mol$^{-1}$ nm$^{-2}$. A pore consists of two mouth regions (length $0.4$ nm, i.e. one layer of pseudo-atoms, and radius $1.0$ nm) at either end of the constriction site of length $L$ (varied between $0.4$ nm and $2.0$ nm) and radius $R$ (varied between $0.15$ nm and $1.0$ nm). The pore was embedded in a membrane mimetic, a slab of pseudo-atoms held on a cubic lattice with unit cell length $0.39$ nm with harmonic springs of strength $k_o$. Pores with a polar surface were created by placing partial charges of $\pm0.38e$ on atomic sites $0.2$ nm apart. The resulting dipole moments pointed parallel to the pore axis with a magnitude of
Figure 1. Simulation system: the solvent-accessible surface of a model pore with pore radius $R = 0.55\, \text{nm}$ is shown in light blue (parts of the pore close to the observer are removed for clarity). The pore is not completely hydrophobic due to two dipoles (red/blue) in the pore wall which have the same magnitude as the peptide bond dipole. Water molecules in the pore are depicted in licorice representation and as lines in the mouth region or the bulk (image created with VMD [27] and Raster3D [28]).

3.6 D each, which is comparable to the dipole moment of the peptide bond (about 3.7 D [26]).

2.2. Molecular dynamics

MD simulations were performed with GROMACS v3.1.4 [29] and the SPC water model [30]. The Lennard–Jones parameters for the interaction between a methane-like pseudo-atom and the water oxygen are $\epsilon_{CO} = 0.906\, 493\, \text{kJ mol}^{-1}$ and $\sigma_{CO} = 0.342\, 692\, \text{nm}$; parameters for sodium and chloride ions are taken from the GROMACS force field. The integration step was 2 fs and coordinates were saved every 2 ps. With periodic boundary conditions, long range electrostatic interactions were computed with a particle mesh Ewald method (real space cutoff 1 nm, grid spacing 0.15 nm, fourth-order interpolation [31]) while the short range van der Waals forces were calculated within a radius of 1 nm. This treatment of electrostatic effects is known to influence the permeation of ions, especially in narrow pores. These artefacts need to be accounted for in order to obtain quantitative predictions of ionic currents [32]. However, though most likely present in our case, too, they are less important because of our emphasis on principles and order-of-magnitude effects. The neighbourhood list (radius 1 nm) was updated every 10 steps. Weak coupling algorithms [33] were used to simulate at constant temperature ($T = 300\, \text{K}$, time constant 0.1 ps) and pressure ($P = 1\, \text{bar}$, compressibility $4.5 \times 10^{-5}\, \text{bar}^{-1}$, time constant 1 ps) with the $x$ and $y$ dimensions of the simulation cell held fixed at $4\, \text{nm}$. The total thickness of the water reservoir in the $z$-direction was 3.0 nm, ensuring bulk-like water behaviour far from the membrane mimetic. The initial system configuration was created by solvating the slab-embedded pore model with water. For simulations with ions, some water molecules were replaced with ions to reach the target concentration. Initially, there were always ions present in pores with $R \geq 0.4\, \text{nm}$. A typical simulation box measured $3.9 \times 3.9 \times 4.6\, \text{nm}^3$ and contained about 1500 water molecules and 280 pseudo-atoms (and between 25 to 28 Na\(^+\) and Cl\(^-\) ions each).

2.3. State-based analysis

We define discrete states by mapping equilibrium states of the whole system (snapshots from the MD equilibrium trajectory) onto numbers $\omega_i$. The same approach is used in statistical mechanics to map different microscopic states to one macroscopic state, characterized by the value of a state variable, here called $\omega$. This approach is used to label the two phase states that the pore water exhibits in our simulations. We either find liquid-filled pores or vapour-filled ones. Due to the small pore volumes ‘vapour’ typically refers to zero or one water molecule in the cavity. We use the density in the pore as an indicator of the phase state. As described previously [25] we assign the state using a Schmitt-trigger procedure [34] in order to avoid spurious state changes due to fluctuations from the interfacial region. When the water density $n(t)$ rises above 0.65 of the density of bulk water, $n_0$ ($n_0 = 1.0\, \text{g cm}^{-3}$ at $T = 300\, \text{K}$ and $P = 1\, \text{bar}$) the liquid state, i.e. $\omega = 1$, is assigned to the phase state at time $t$. When $n(t)$ drops below 0.25$n_0$ the vapour state ($\omega = 0$) is assigned. The pore in the liquid-filled state is termed ‘open’ because our simulations show that significant amounts of water pass through it; furthermore, we also demonstrate in this work that a pore that sustains a liquid environment potentially allows ions to permeate. A vapour-plugged pore, however, will prevent ion permeation and is said to be ‘closed’.

Liquid-filled pores and vapour-filled pores are assumed to be in equilibrium. The ‘openness’ or probability for the occurrence of the liquid, i.e. open, state is

$$\langle \omega \rangle = \frac{1}{T_{\text{sim}}} \int_0^{T_{\text{sim}}} \text{d}t \omega(t) = \frac{T_{\omega}}{T_{\text{sim}}},$$

where $T_{\text{sim}}$ denotes the total simulation time, $T_{\omega}$ the total time that the pore is open, whereas $T_c$ is the total time in the vapour or closed state. If $\langle \omega \rangle > \frac{1}{2}$ then equilibrium is on the side of liquid (and vapour is a metastable state), otherwise the stable phase state is vapour. The equilibrium is governed by the equilibrium constant

$$K(R) = \frac{T_c(R)}{T_{\omega}(R)} = \frac{T_{\text{sim}} - T_c(R)}{T_{\omega}(R)} = (\omega(R))^{-1} - 1,$$

which is trivially related to the openness. (Note that for $T_c = 0$ or $T_{\omega} = 0$ it is meaningless to compute $K$ because it indicates that the simulation time was too short to sample any state changes.)

2.4. Thermodynamic model for liquid–vapour equilibrium in pores

We investigate a subsystem of the whole simulation system comprising of the pore of volume $V = L\pi R^2$. The subsystem can exchange water molecules with the bulk water outside...
the pore, which acts as a particle reservoir at average chemical potential \( \mu \). \( \mu \) is implicitly determined by the constant average density of water in the bulk system, which in turn is prescribed by simulating at constant pressure. Hence we can use the grand potential \( \Omega(T, V, \mu) = -pV \) as the free energy to describe the subsystem in the closed and open state [24]. The equilibrium constant \( K \) is determined by the free energy difference between the closed (vapour) and open (liquid) state,

\[
\beta \Delta \Omega(R) = \beta[\Omega_{\text{v}}(R) - \Omega_{\text{l}}(R)] = -\ln K(R) = -\ln [(\omega(R))^{-1} - 1],
\]

using \( \beta = 1/k_B T \). Following [35], we write the free energy difference between the vapour and the liquid state with the corresponding surface contributions as

\[
\Delta \Omega(R) = \Omega_{\text{v}}(R) - \Omega_{\text{l}}(R) = -p_v(T, \mu) L \pi R^2 + 2 \pi R L \gamma_{\text{lv}} + 2 \pi R^2 \gamma_{\text{lw}} = -(p_l(T, \mu) L \pi R^2 + 2 \pi R L \gamma_{\text{lw}}). \tag{3}
\]

Here the index \( v \) indicates the solid pore wall, \( l \) the liquid, and \( v \) the vapour phase; for instance \( \gamma_{\text{lw}} \) is the surface tension or surface free energy per area of the liquid–vapour interface. The system is fairly close to bulk phase coexistence so we can expand the pressure \( p \) around the saturation chemical potential \( \mu_{\text{sat}}(T) \) in a Taylor series,

\[
p(T, \mu) = p(T, \mu_{\text{sat}}) + (\mu - \mu_{\text{sat}}) \left. \frac{\partial p(T, \mu)}{\partial \mu} \right|_{\mu=\mu_{\text{sat}}} + \cdots,
\]

where at saturation \( p(T, \mu_{\text{sat}}) = p_l(T, \mu_{\text{sat}}) \). This leads to a simple parabolic form for the free energy difference between the two states,

\[
\Delta \Omega(R) = [2 \gamma_{\text{lv}} + (\mu - \mu_{\text{sat}})(n_1(T, \mu_{\text{sat}}) - n_1(T, \mu_{\text{sat}})]) - n_1(T, \mu_{\text{sat}}) L \pi R^2 + 2 \pi L (\gamma_{\text{lw}} - \gamma_{\text{lw}}) R = 2 \gamma_{\text{lw}} + \frac{1}{2} \Delta \mu \Delta n_{\text{sat}} L \pi R^2 + 2 \pi L \Delta \gamma_{\text{lw}} R, \tag{4}
\]

where we define the distance of the state from saturation \( \Delta \mu := \mu - \mu_{\text{sat}} \), the difference in densities \( \Delta n_{\text{sat}} := n_1 - n_1 \) at saturation, and the difference in surface free energies of the two phases with the wall, \( \Delta \gamma := \gamma_{\text{lw}} - \gamma_{\text{lw}} \). The term \( \Delta \mu \Delta n_{\text{sat}} L \) is small for \( L < 10 \) nm as the system is close to phase coexistence (for \( L \approx 1 \) nm it is about \( 10^{-3} \) times smaller than \( \gamma_{\text{lw}} \approx 17 k_B T \) nm\(^{-2} \) when estimated from \( \Delta n_{\text{sat}} \Delta \mu L \approx \Delta P L \approx 1 \) bar \( \times L = 2.4 \times 10^{-3} k_B T \) nm\(^{-2} \times L, \ T = 300 \) K) and will be neglected. Only the difference between the surface energies enters the model so we express it as the contact angle \( \theta_e \), using the macroscopic definition from Young’s equation \( \gamma_{\text{lw}} + \frac{1}{2} \Delta \mu \Delta n_{\text{sat}} L \pi R^2 + 2 \pi L \Delta \gamma_{\text{lw}} R = \gamma_{\text{lv}} \cos \theta_e \) (see, for instance, [36]). Then equation (4) becomes

\[
\Delta \Omega(R, L, \theta_e) = 2 \pi R \gamma_{\text{lv}} (R + L \cos \theta_e). \tag{5}
\]

(equation (5) is similar to the simple model derived by Allen et al. [24] but it includes \( \gamma_{\text{lw}} \) and hence \( \theta_e \) instead of just \( \gamma_{\text{lw}} \)). For fixed pore length \( L \) and a given pore material, characterized by \( \theta_e \), the graph of \( \Delta \Omega(R) \) over the pore radius \( R \) describes a parabola containing the origin. Although it is not \textit{a priori} obvious that such a macroscopic treatment (equation (4) or (5)) of a nanoscale system is meaningful the MD results for the free energy difference presented in section 3.1 can be adequately explained within this model.

The connection between the model free energy \( \Delta \Omega(R) \) and the behaviour of the system as observed in MD simulations, i.e. the openness (\( \omega(R) \)), is established by inverting equation (2), yielding

\[
\langle \omega(R) \rangle = \frac{1}{1 + \exp(-\beta \Delta \Omega(R))}. \tag{6}
\]

For linear \( \Delta \Omega(R) \) this represents a sigmoidal curve but non-linear terms (as in equation (4)) change its shape considerably.

### 3. Results and discussion

First we investigate the behaviour of pure water in nanopores and quantify the influence of geometry, pore surface, and local flexibility on the equilibrium between liquid- and vapour-filled pores. Then simulations for a NaCl electrolyte are analysed and compared to the pure water case. The intention behind these studies is to explore more fully the ways in which a hydrophobic gate may be opened, and how other factors might modulate such hydrophobic gating. This is particularly important in the context of current models for the gating of nAChR [10, 37] which suggest that the transition between the closed and open states of the pore involves both an increase in pore radius and in polarity. We also note that recent discussion of the state (open versus closed) of MscS has suggested a hydrophobic gating mechanism [38], similar to that proposed for nAChR [21].

### 3.1. Pure water

A large number of simulations were run for water in model pores (total simulation time \( >5 \) \( \mu s \)) in order to investigate the influence of pore radius (0.15 nm \( \leq R \leq 1 \) nm) and pore surface character (hydrophobic versus amphipathic versus hydrophilic). Local flexibility (wall atom positional root mean square deviations (RMSDs) 0.03 nm \( \leq \rho \leq 0.192 \) nm) and temperature dependence in the range 273 K \( \leq T \leq 450 \) K were examined for a hydrophobic pore of \( R = 0.55 \) nm pore.

#### 3.1.1. Pore dimensions and surface character

The water density in short nanopores oscillates between liquid and vapour on a nanosecond time scale as seen in figure 2, a manifestation of capillary evaporation and condensation at the nanoscale [25]. In figure 3 the openness and the free energy difference \( \Delta \Omega \) between vapour and liquid states are shown for different pore surfaces. For hydrophobic and amphipathic pores a strong dependence of the pore state on the radius is apparent. The stable thermodynamic state switches from vapour \( (\Delta \Omega < 0 \) or \( \omega) < \frac{1}{2} \) to liquid \( (\Delta \Omega > 0 \) or \( \omega) > \frac{1}{2} \) at a critical radius \( R_c = -L \cos \theta_e \) (using \( \Delta \Omega(R_c) = 0 \) in equation (5)). \( R_c \) is 0.56 \pm 0.03 nm for the hydrophobic pore and 0.29 \pm 0.02 nm for the amphipathic one. The functional form equation (4) fits the data from the MD simulations (table 1) well (the continuous lines in figure 3). The coefficient of the quadratic term, \( \gamma_{\text{lv}} + \frac{1}{2} \Delta \mu \Delta n_{\text{sat}} L \), is positive and similar for both the hydrophobic and the amphipathic (two dipoles, abbreviated D2) pores (table 1), consistent with the model equation (4), which predicts this coefficient to be independent
Liquid–vapour oscillations of water in a $R = 0.65$ nm apolar pore (top panel) when bathed in a 1.3 M NaCl solution. As indicated by the number $N$ of ions within the pore, sodium (middle) and chloride ions (bottom) are only observed in the pore when there is also liquid water ($n/n_{bulk} \approx 0.8$) present. Permeation events are indicated by triangles; ions do not permeate the pore during the vapour phases.

Water in model pores. Left: openness ($\omega$) over radius. Right: free energy difference $\Delta \Omega$ (in $k_B T$) between vapour and liquid state. The grey region indicates radii smaller than the radius of a water molecule (0.14 nm). Data points are obtained from MD simulations with the errors estimated from block averages [39]. The continuous lines (——) are fits of the model (equation (4)) to the data points (right) or the openness computed from the model (equation (6)). The vertical line indicates the radius of the closed nAChR gate ($R = 0.31$ nm).

**Table 1.** Parameters of the thermodynamic model equation (4) fitted to the MD results and resulting contact angle $\theta_e$. Experimental values for $\gamma_{lv} = 72 \times 10^{-3}$ J m$^{-2} = 17 k_B T$ nm$^{-2}$ and $\theta_e \approx 118^\circ$ for water on a flat methyl (–CH$_3$) terminated self-assembled monolayer [40, 41] indicate that the simple thermodynamic model gives the right order of magnitude results. (All values at room temperature.)

| Pore surface character | $\gamma_{lv} + \frac{1}{2} \Delta \mu \Delta n_d L$ ($k_B T$ nm$^{-2}$) | $\Delta \gamma_{lw} = \gamma_{lw} - \gamma_{lw}$ ($k_B T$ nm$^{-2}$) | $\theta_e (^\circ)$ |
|------------------------|-----------------------------------------------------------|-------------------------------------------------|------------------|
| Bare CH$_3$            | 0 ‘Hydrophobic’                                           | $+10 \pm 1$                                    | $-7.2 \pm 0.2$   | 134 $\pm$ 3 |
| Two dipoles            | D2 ‘Amphipathic’                                          | $+8.2 \pm 0.5$                                 | $-3.0 \pm 0.2$   | 111 $\pm$ 2 |
| Four dipoles           | D4 ‘Hydrophilic’                                          | $+2.8 \pm 0.5$                                 | $+1.8 \pm 0.2$   | 51 $\pm$ 10 |

of the pore wall. For the polar pore (four dipoles, D4) the data are more ambiguous. Only if the first two data points at small radii are excluded from the fit as outliers is this coefficient positive (but still three times smaller than that for the less hydrophilic pores). The outliers show that a high density of local charges leads to a higher probability of the pore being liquid-filled than predicted by the macroscopic model, possibly indicating a shortcoming of the model to subsume inhomogeneous potentials into the surface tension terms. For our system parameters, the coefficient of the quadratic term is in fact dominated by the water liquid–vapour surface tension $\gamma_{lv}$ (see section 2.4) and hence we will use its value as an approximation to $\gamma_{lw} = \gamma_{lw} - \gamma_{lw}$. $\Delta \gamma_{lw}$, the difference in surface tensions between the wall and vapour or liquid, becomes more positive with increasing polarity of the pore wall. It effectively measures the hydrophobicity of the wall. This becomes even more apparent when the (macroscopic) contact angle $\cos \theta_e = \Delta \gamma_{lw}/\gamma_{lv}$ is formally computed (table 1). Macroscopically, a hydrophobic surface can be defined as one with $\theta_e > 90^\circ$. This allows us to call the apolar pore ($\theta_e = 134^\circ$) ‘hydrophobic’ compared to the ‘amphipathic’ pore D2 ($\theta_e = 111^\circ$); still hydrophobic but with some ‘hydrophilic’ patches. A ‘hydrophilic’ pore like the D4 system ($\theta_e \approx 51^\circ$) is characterized by $\Delta \gamma_{lw} > 0$ or $\theta_e < 90^\circ$ and liquid is always the preferred phase in the pore, regardless of $R$.

Experimental macroscopic contact angles $\theta_e$ for water on flat methyl (–CH$_3$) terminated self-assembled monolayers are reported up to 118° [40, 41]. A ‘microscopic contact angle’ of 135° ± 15° was calculated for a droplet of 90 water molecules.
Our model implies that for both nano- and mesoscale pores the cost of creating the liquid–vapour interface is the only force driving the filling of a hydrophobic pore. Little free energy $\Delta \mu \Delta n_p LRT^2$ is gained by creating a bulk-like liquid in the pore instead of vapour.

### Table 2. RMSD of wall atoms in flexible pore models of radius $R = 0.55$ nm and influence on the liquid–vapour equilibrium of water in the pore at $T = 300$ K.

| Restraint force constant $k$ ($10^2 k_BT$ nm$^{-2}$) | RMSD $\rho(k)$ ($10^{-1}$ nm) | $\langle \alpha \rangle$ | $\beta \Delta \Omega$ |
|-----------------------------------------------|-------------------------------|----------------------|-----------------|
| MD                                           | Theory                        | MD                   | MD               |
| 0.8                                          | 1.7 ± 0.3                     | 1.92                 | 0.001 ± 0.001   | −6.9 ± 1.0      |
| 2                                            | 1.0 ± 0.0                     | 1.22                 | 0.006 ± 0.005   | −5.1 ± 0.8      |
| 4                                            | 0.72 ± 0.02                   | 0.86                 | 0.291 ± 0.089   | −0.89 ± 0.43    |
| 8                                            | 0.52 ± 0.01                   | 0.61                 | 0.616 ± 0.097   | 0.47 ± 0.41     |
| 20                                           | 0.35 ± 0.01                   | 0.39                 | 0.755 ± 0.060   | 1.1 ± 0.3       |

Figure 4. Influence of flexibility on the liquid–vapour equilibrium. (a) For a hydrophobic $R = 0.55$ nm pore the harmonic restraint force constant $k$ of the pore wall atoms was varied, resulting in a range of RMSDs $\rho$, which shows the expected behaviour of thermic harmonic oscillators. The free energy difference $\Delta \Omega$ between liquid and vapour states of water in the pore shows strong dependence on the local flexibility $\rho$; rigid pores contain liquid water whereas flexible ones favour vapour. The effect cannot be explained by a reduction of the effective pore radius by $\rho$ alone (broken line $\cdots \cdots$ in (b)). All data at $T = 300$ K.

3.1.2. Local flexibility. The influence of local fluctuations in protein structure can be modelled by changing the harmonic spring constant $k$ that holds the pore wall atoms at their equilibrium positions. In a simplified picture of a harmonic oscillator with an average energy $k_BT/2$ per degree of freedom the RMSD $\rho$ is directly related to $k$ by $\rho(k) = \sqrt{(\Delta \rho_{\text{max}}) = \sqrt{3k_BT/k}}$. This simple model overestimates the measured RMSDs by only 10–20% (table 2), showing that the wall atoms behave like almost independent, thermally driven, harmonic oscillators (figure 4(a)). At a fixed radius, increasing the flexibility (smaller $k$, hence greater $\rho$) shifts the equilibrium towards vapour (figure 4). Conversely, a more rigid wall favours the condensation of water in the pore.

Thus, water does not ‘push away’ the pore walls to fill the pore but rather fluctuating pore walls appear to disfavour the formation of adjacent water layers. This effect cannot be explained with the assumption that the water molecules encounter a more narrow pore ‘on average’. Even if one assumes that the pore is narrowed by the RMSD of an atom down to an effective radius $R(k) = R_0 - \rho(k)$, the effect is still much stronger. When the thermodynamic model and the parameters for the hydrophobic pore (from table 1 where $k_s = 4 \times 10^2 k_BT$ nm$^{-2}$) are used to predict $\Delta \Omega(R(k))$ then the prediction compared to the simulation results underestimates the effect for the more flexible pores.
O Beckstein and M S P Sansom

Figure 5. Equilibrium densities of water (top row), sodium ions (middle) and chloride ions (bottom) in hydrophobic model pores of radii $R = 0.35$ nm to 0.75 nm; the NaCl bulk concentration is $1.3 \text{ mol l}^{-1}$. The narrow 0.35 nm pore mimics the closed gate of nAChR whereas the wide 0.65 nm pore approximates the open channel. Although wide enough to admit the ions physically, the narrow pore is effectively closed to ions (‘hydrophobic gating’). The membrane mimetic is located in the horizontal region which appears black, i.e. void of water, in all images.

3.2. NaCl electrolyte

As mentioned in the introduction it has been hypothesized that a local hydrophobic environment would present a significant desolvation barrier to ion permeation. Our simulations of model pores bathed in a 1.3 M NaCl solution exhibit a striking change in the behaviour of the ions for pore radii $R \geq 0.65$ nm. Figure 5 shows that in pores of comparable dimensions to the closed nAChR pore ($R = 0.35$ nm) ions have a vanishing probability of entering the pore, but at the open-state radius $R = 0.65$ nm the pore density rises to half the bulk value. The average density of ions in the centre of the pore (figure 6) also exhibits a sharp increase near $R = 0.65$ nm, similar to the behaviour of the openness (figure 3).

The radially averaged densities show two pronounced water layers with an interlayer distance $d = 0.3$ nm near the membrane mimetic. The ion exclusion zone stretches into the pore without interruption so that at $R = 0.65$ nm there is only a narrow channel of easily...
markedly at the critical radius and exhibits the highest density of ions. The core density increases density at $R$ and ions, the equilibrium flux $\Phi_0/R^2$ as MD simulations output the trajectories of water as the latter also requires rapid permeation of ions through a pore. As MD simulations output the trajectories of water and ions, the equilibrium flux $\Phi_0/R^2$, i.e. the total number of particles per nanosecond which completely permeate the pore, can be measured. Figure 7 shows $\Phi_0$ for ions and water molecules (both for water in a 1.3 M NaCl electrolyte and for pure water) in hydrophobic pores of varying radius on a logarithmic scale. Water flux is about three orders of magnitude larger than ion flux and increases rapidly with increasing radii while $R$ is smaller than the critical radius $R_c = 0.62$ nm. Beyond $R_c$ (when liquid becomes the stable phase) the slope in the logarithmic plot decreases from $15 \text{ nm}^{-1}$ to $2.4 \text{ nm}^{-1}$. The water current density $\Phi_0/R^2$ reaches a constant value of $300 \text{ ns}^{-1} \text{ nm}^{-2}$ so the increase for $R > R_c$ is only due to the increase in pore diameter. The increase for $R < R_c$ correlates with the openness (figure 3), indicating that the main contribution to the flux stems from the open-state periods [25]. The presence of ions slightly shifts $R_c$ from $0.56 \pm 0.03$ nm for pure water to $0.62 \pm 0.07$ nm for 1.3 M NaCl electrolyte. Qualitatively, this is explained by the increase of surface tension with ionic concentration [50]. This leads to a higher contact angle $\theta_e$ [51], which is also observed in our simulations where it increases from $134^\circ$ to $140^\circ$. Hence, $R_c = -L \cos \theta_e$ increases for electrolytes compared to pure water.

The total number of ions that successfully permeate the pore per nanosecond shows an increase over almost two orders of magnitude when the pore radius $R$ is increased from 0.6 nm to 0.65 nm. Thus the pore ‘opens’ at a radius much larger than the bare ionic radius. Ions permeate only when the pore is filled with liquid water (typical data in figure 2) and Na⁺ permeation events are not correlated with Cl⁻ ions passing through the pore.

Because the simulations are in thermodynamic equilibrium the net flux through the pore is zero for all $R$. In order to compare the MD equilibrium flux $\Phi_0$, which is determined by the intrinsic free energy barrier to ion permeation, to experimentally measured non-equilibrium fluxes $\Phi$ of ions of charge $q$ at a driving transmembrane voltage $V$ we employ rate theory and estimate

$$\Phi(V; R) = \Phi_0(R) \sinh \frac{qV}{2k_BT}. \quad (7)$$

For $R = 0.65$ nm, $V = 100 \text{ mV}$, $q = 1e$ and $T = 300 \text{ K}$ we obtain $\Phi \approx 1.2 \text{ ns}^{-1}$, which is 40 times larger than the experimental value of $0.03 \text{ ns}^{-1}$ for nAChR at 0.2 M ionic concentration (calculated from a conductance of ca. 45 pS [11]). The discrepancy between our estimate and the experimental data is not unexpected as equation (7) has only qualitative character. Furthermore, nAChR presents a more complex pore lining surface than the model pore, and if the difference in bath concentrations and access resistance was taken into account the discrepancy would likely be reduced by an order of magnitude. Nevertheless, the estimate demonstrates that the intrinsic barrier to ion permeation is small beyond the critical radius.

3.3. Sensing external parameters

In the simplest model of sensing a system exists in an equilibrium with two states. External stimuli shift the equilibrium which elicits a cellular response. For example, a temperature-sensing channel at normal temperature might be in the closed state. Elevated temperature shifts the equilibrium
to the open state and the influx of ions initiates a signalling cascade that terminates in the sensation of heat. However, the exact mechanisms of gating by temperature of, e.g., TRP channels remain obscure [52]. We tested the influence of temperature in the range from 273 K to 450 K on water in the $R = 0.55 \, \text{nm}$ hydrophobic pore (data points for $T > 373 \, \text{K}$ represent ‘supercritical’ water because the critical point for the SPC water model is close to $T = 373 \, \text{K}$). The free energy landscape of the water–pore system depends on the temperature (figure 8(a)). With increasing temperature the liquid state (i.e. near water bulk density) decreases in stability. Accordingly, the openness decreases with temperature so that the vapour state, i.e. the closed state, dominates at higher temperatures (figure 8(b)). The decrease in openness with increasing $T$ indicates that the difference of the wall surface tensions $\Delta \gamma_w$ must become even more negative, i.e. vapour in contact with the wall is increasingly favoured. The effect would be similar to the one discussed for increased flexibility of wall atoms as the major effect of temperature would be to smear out the interaction potential between water molecules and wall atoms. This example demonstrates in principle how an external signal, an increase in temperature from $T = 300 \, \text{K}$ to $330 \, \text{K}$, decreases the openness, and correspondingly the flux of water molecules, by a factor of 6.

4. Conclusions and outlook

We have explicitly demonstrated a hydrophobic gating mechanism for ions, using simplified hydrophobic pores as models for the closed gates of ion channels. There is a critical radius $R_c$ above which a pore becomes effectively permeable to water or ions. The radius $R_c \approx 0.56 \, \text{nm}$ for water and $R_c \approx 0.65 \, \text{nm}$ for ions, is much larger than the radius for a water molecule or a bare ion alone. This correlates nicely with the current view that the closed state structures of many ion channels contain gates formed by hydrophobic constriction sites. In nAChR the radius of the putative gate is 0.31 nm, 0.17 nm in MscL, and 0.13 nm in KcsA. Models of KcsA and of Kv channels in their open states, based on the MthK and KvAP structures respectively, have gate radii of about 0.6 nm [53], whereas the open-state nAChR structure opens up to about 0.65 nm. Our simulations show that the polarity of the pore wall can shift the critical radius considerably. This is reflected in the proposed gating mechanism of nAChR [37]. Not only does the radius of the constriction site increase but hydrophobic side chains are also rotated out of the pore to expose the more polar, i.e. hydrophilic, peptide backbone. By combining hydrophobic gating with a change in surface polarity only a moderate change in radius is required to obtain a large physiological effect. Changes in local flexibility may also modulate the gating behaviour. It is too early to ascertain their importance as such changes in flexibility have not been widely investigated experimentally for channels (or any other proteins). There are suggestions of possible regulatory roles of changes in flexibility in, e.g., KTN domains [54], and in the modulation of binding of TRAP protein to the Trp operon mRNA [55]. Temperature can also affect gating, in a fashion similar to local flexibility, but its direct effects seem too small to explain, for instance, the temperature sensitivity of TRP channels on their own.

A thermodynamic model based on surface energies fits remarkably well the data of the atomic-scale MD simulation, even for very small radii. Though such a macroscopic treatment is not a priori expected to give a satisfactory description of a microscopic system there are other examples as, for instance, classical nucleation theory, which shares some similarities with our and others’ models [24, 56]. It generally agrees quite well with experiments on the condensation of droplets from vapour, which implies that the use of macroscopic surface tension is valid even for droplets of radii of about 1 nm [57]. It appears that in this case water structure (i.e. a hydrogen bond network) is only important insofar as it is responsible for different wall–fluid surface tensions. Our results seem to corroborate the conclusions of [58] that two-state behaviour of water in pores should only require a cold
liquid close to phase coexistence and sufficiently different vapour–wall and liquid–wall surface tensions (which is, of course, where the ‘special’ properties of water reside in such a model).

We have sketched out principles of gating mechanisms in ion channels, based on model channels. Ion channels in nature display complex conformational dynamics in relationship to gating. There is a need for better single molecule methods for ion channels to probe these phenomena experimentally. Combined electrical and optical methods look promising in this respect [59] although considerable improvements in time resolution are still required. In the meantime there is a continued role for simulations and theory to enable us to bridge between static structure and dynamic function.

In addition to hydrophobic gating per se, our studies suggest the possible importance of gate flexibility in regulation of biological activity. The relationship between static structures, conformational change and intrinsic flexibility in relationship to proteins and signalling merits further active investigation. In a recent review of protein–protein interactions and conformational changes, Goh et al [60] conclude that there is increasing support for a pre-existing equilibrium model. In such a model, proteins exist in a population of conformations, with ligand binding leading to a change in the probability distribution of the ensemble. Some evidence in support of this has been obtained from recent simulation studies of ligand binding proteins (e.g. [61]) but further (single-molecule) experimental and computational studies of a wider range of proteins are needed to more firmly establish the general importance of changes in flexibility.

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Glossary

**Classical molecular dynamics.** A computational scheme to calculate the time evolution of a microscopic system that is treated in atomic detail. Interactions are parametrized through classical two-, three- or four-body potentials. A collection of these parameters is known as a ‘force field’. The dynamics are obtained by integrating Newton’s equations of motion.

**Gating.** An ion channel can exist in an ‘open’ state, which allows for ion permeation, and a ‘closed’ state, when ions cannot pass the channel’s gate and thus are prevented from crossing the membrane. Such a channel can be switched between states by external signals.

**Surface tension, surface free energy.** The free energy per area required to create an interface between two phases. It is always positive, i.e. it always costs free energy to create a surface compared to the homogeneous bulk phases.

**Contact angle.** The angle which is formed between the tangent on a droplet of liquid where it is in contact with the surface and the surface itself. The droplet is taken to be in equilibrium with its vapour. A surface material is called hydrophobic (‘water-hating’) when the contact angle with water is greater than 90° (the drop sits on the surface) and hydrophilic (‘water-loving’) when it is smaller (the drop resembles a pancake).

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