Computational modelling of cambium activity provides a regulatory framework for simulating radial plant growth

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Keywords: cambium, radial plant growth, PXY, CLE41, cellular model, VirtualLeaf

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Abstract

Precise organization of growing structures is a fundamental problem in developmental biology. In plants, radial growth is mediated by the cambium, a stem cell niche continuously producing wood (xylem) and bast (phloem) in a strictly bidirectional manner. While this process contributes large parts to terrestrial biomass, cambium dynamics eludes direct experimental access due to obstacles in live cell imaging. Here, we present a cell-based computational model visualizing cambium activity and integrating the function of central cambium regulators. Performing iterative comparisons of plant and model anatomies, we conclude that an intercellular signaling module consisting of the receptor-like kinase PXY and its ligand CLE41 constitutes a minimal framework sufficient for instructing tissue organization. Employing genetically encoded markers for different cambium domains in backgrounds with altered PXY/CLE41 activity, we furthermore propose that the module is part of a larger regulatory circuit using the phloem as a morphogenetic center. Our model highlights the importance of intercellular communication along the radial sequence of tissues within the cambium area and shows that a limited number of factors is sufficient to create a stable bidirectional tissue production.
Introduction

Stem cells in plants are crucial for their longevity and usually maintained in meristems, special cellular environment constituting maintaining niches [1]. At key positions in the plant body, we find distinct types of meristems that maintain their activity throughout a plant’s life cycle. Shoot and root apical meristems (SAM, RAM) are located at the tips of shoots and roots, respectively, driving longitudinal growth and the formation of primary tissue anatomy in these organs. Moreover, lateral meristems organized in cylindrical domains at the periphery of shoots and roots execute their thickening. The cambium is the most prominent among these lateral meristems [2]. Cambium cells are embedded in and produce two distinct vascular tissues in opposite directions by periclinal cell divisions: the xylem (wood) and phloem (bast) [3]. These tissues carry out fundamental physiological functions: long-distance transport of water and nutrients in case of the xylem and translocation of sugars and a multitude of signaling molecules in the case of the phloem. Based on its tightly controlled bidirectionality of tissue production and bipartite organization, the cambium is a paradigm for bifacial stem cell niches found across different kingdoms of life [2, 4]. However, although the cambium plays this instructive role for stem cell biology, a dynamic view on its activity is missing due to its inaccessibility for live cell imaging.

Balancing proliferation and differentiation within meristems is essential. In the SAM and the RAM this balance is maintained via interaction between the pool of stem cells and the organizing center (OC) and the quiescent center (QC), respectively, where the rate of cell division is relatively low. Both domains form a niche within the meristem instructing surrounding stem cells via regulatory feedback loops [5-9]. In comparison to apical meristems, functional characterization of cambium domains was performed.
only very recently. During their passage from stem cells to fully differentiated xylem cells, early xylem cells instruct radial patterning of the cambium including stem cell activity and, thus, similar to the OC in the SAM, fulfil this role only transiently [10]. In addition to influence from the early xylem, phloem-derived DNA-BINDING ONE ZINC FINGER (DOF) transcription factors designated as PHLOEM EARLY DOFs (PEARs) move to cambium stem cells and stimulate their proliferation in a non-cell autonomous manner [11]. Supported by genetically encoded lineage tracing experiments which showed that cell divisions are restricted to a narrow domain, and most likely to individual bifacial stem cells, located in the central cambium [10, 12, 13], these findings defined functional cambium domains and started to reveal their reciprocal communication.

Another central and well-established mechanism regulating cambium activity in the reference plant Arabidopsis thaliana and beyond [14-17] is the action of a receptor-ligand pair formed by the plasma membrane-bound receptor-like kinase PHLOEM INTERCALATED WITH XYLEM (PXY, also known as TDR) and the secreted CLAVATA3/ESR-RELATED 41 (CLE41) and CLE44 peptides. Like the PEAR proteins [11], CLE41 and CLE44 are expressed in the phloem and thought to travel to the dividing cells in the cambium area expressing PXY [15, 18]. Direct binding of CLE41 to PXY [18-20] promotes the expression of the transcription factor WUSCHEL RELATED HOMEBOX 4 (WOX4) [21], which, in turn, is crucial for maintaining the capacity of cells to proliferate [14, 21, 22]. At the same time, the PXY/CLE41 module is reported to repress xylem differentiation in a WOX4-independent manner [21, 23]. In this context, PXY stimulates the activity of glycogen synthase kinase 3 proteins (GSK3s), like BRASSINOSTEROID-INSENSITIVE 2 (BIN2) [23]. BIN2, in turn,
represses the transcriptional regulator BRI1-EMS SUPPRESSOR 1 (BES1), which mediates BR signaling and promotes xylem differentiation [23, 24]. Under the hypothesis of a dual role in regulating stem cell activity and xylem differentiation, PXY is predominantly expressed in the proximal cambium zone oriented toward the xylem containing bifacial cambium stem cells but also cells determined for xylem development [12, 25].

Distally to the PXY expression domain-oriented toward the phloem, the closest homolog to PXY, the receptor-like kinase MORE LATERAL GROWTH 1 (MOL1) represses cambium activity [26, 27]. Although their extracellular domains are highly similar, PXY and MOL1 cannot functionally replace each other, indicating that MOL1 activity does not depend on CLE41/44 peptides and that distinct signaling loops act in the proximal and the distal cambium domain [27]. The latter conclusion is also supported by the finding that the AUXIN RESPONSE FACTOR5 (ARF5) is expressed in the proximal cambium and promotes the transition from stem cells to xylem cells by directly dampening WOX4 activity [25, 28]. ARF5 activity is enhanced by phosphorylation through the GSK3 BIN2-LIKE 1 (BIL1) which, in contrast to other GSK3s [23], is inhibited by the PXY/CLE41 module [28].

Because the role of several communication cascades between different cambium-related tissues is beginning to emerge, it is vital to generate an integrated and dynamic view on their combined impact on cambium activity and patterning. Here, we present a dynamic, cell-based model [29] of the cambium integrating the functions of PXY, CLE41, and putative phloem-derived signals into a modelling framework. Thereby, we are able to reproduce anatomical features of the cambium in a dynamic manner and
as revealed by informative cambium markers. Our model allows studying the cambium as a dynamic system comprised of multiple interacting factors, and the effects of those factors on cell division, patterning and differentiation.
Results

Establishing a dynamic cambium model

To explore the functional dynamics of cambium activity, we sought to create a dynamic 2D recapitulation of radial plant growth. To do so, we first produced a simplified stereotypic 2D-representation of a plant growth axis displaying a secondary anatomy by employing VirtualLeaf – a framework specially designed for cell-based modeling of plant tissue growth [30]. To avoid confusion, we referred to factors within the model by an asterisk: e.g., GENE – referred to the plant gene, whereas GENE* referred to its model counterpart. Within the model we defined three cell types: Cells designated as cambium*, cells present in the center referred to as xylem*, and cells present distally to the cambium* designated as phloem* (Fig. 1A). We then defined rules determining cell* behavior: i) all cells* grew until they reached a size specific for each cell type, ii) cambium cells* divided when they exceeded a certain size, iii) cambium cells* changed their identity into xylem* or phloem* depending on the conditions described below. All chemical-like factors* implemented in the model had manually chosen cell* type-specific production and degradation rates.

To implement context-dependent regulation of cambial cell division and differentiation, we took advantage of the PXY/CLE41 signaling module [18, 21]. Phloem cells* produced a factor designated as CLE41* able to diffuse passively from cell to cell, whereas cambium cells* produced a non-diffusing factor designated as PXY*. Recapitulating the CLE41-dependent function of PXY, we considered the following reaction:

\[ \text{CLE41}^* + \text{PXY}^* \rightarrow \text{PXY}_{active}^* \] (1)
Thereby, the presence of both CLE41* and PXY* in a cell turned PXY* into PXY-active*. For cambium cells* we described the PXY*-CLE41* interaction by the following equations:

\[
\frac{d}{dt} [PXY_{active}] = [PXY][CLE41] - \text{degradation}_{PXY} [PXY_{active}] \tag{2}
\]

\[
\frac{d}{dt} [PXY] = \frac{\text{production}_{PXY}}{(1+\text{suppressRate}_{PXY}[PXY_{active}])} - [PXY][CLE41] - \text{degradation}_{PXY} [PXY] \tag{3}
\]

\[
\frac{d}{dt} [CLE41] = \text{diffusion}_{CLE41} - [PXY][CLE41] - \text{degradation}_{CLE41} [CLE41] \tag{4}
\]

In these equations, [X] denoted the concentration of the respective factor in each cell. Since PXY-CLE41 signaling was reported to negatively regulate PXY expression [15], we assumed that the production rate of PXY* is inversely dependent on [PXY-active*]. Therefore, the higher [PXY-active*] there was in a given cell*, the less PXY* was produced (equation 3). To integrate PXY/CLE41-dependent regulation of cell proliferation, we let cambium cells* divide only when [PXY-active*] exceeded a certain threshold. Thereby, the proliferation of cambium cells* was dependent on both, locally produced PXY* and CLE41* produced in the phloem*. To instruct the differentiation of cambium cells*, we took advantage of the observation that the PXY/CLE41 module represses xylem differentiation [18, 23]. Consequently, we instructed cambium cells* to change their identity into xylem* as soon as they reached a certain size and [PXY-active*] was low.

In the resulting Model 1, the growing structure maintained a circular pool of dividing cambium cells* with a high concentration of PXY-active* while producing xylem cells* toward the center of the organ (Fig. 1B, Movie 1A, Movie 1B, Movie 1C). As expected,
when cambium cells* were displaced to the proximal side of the cambium*, they stopped dividing likely due to low [PXY-active*] (Fig. 1C, Movie 1C) allowing them to reach a size sufficient for xylem* differentiation. Cell* division rates were highest close to CLE41* producing phloem cells (Fig. 1C-F, Movie 1B, Movie 1C). Moreover, as expected due to the negative effect of PXY-active* on the production of PXY*, [PXY*] was particularly low in the distal cambium* region (Movie 1A, Fig. 1B, E, F). This pattern was reminiscent of the exclusive activity of the \( \text{PXY} \) promoter in the proximal cambium area observed previously [12, 27]. Thus, although phloem was not produced, with maintaining a circular domain of cambium cells* and cell* proliferation and with promoting xylem* production, Model 1 was able to recapitulate several central features of the active cambium.

The combination of \( \text{PXY} \) and \( \text{SMXL5} \) promoter reporters visualizes cambium anatomy

To identify rules for phloem formation, we took advantage of findings obtained using the \( \text{PXYpro:CYAN FLUORESCENT PROTEIN (PXYpro:CFP)} \) and \( \text{SUPPRESSOR OF MAX2-LIKE 5pro:YELLOW FLUORESCENT PROTEIN (SMLX5pro:YFP)} \) markers, recently established read-outs for cambium anatomy [12]. \( \text{PXYpro:CFP} \) and \( \text{SMXL5pro:YFP} \) markers label the proximal and distal cambium domain, respectively, and are therefore indicative of the bipartite cambium organization [12]. A transgene expressing the fluorescent mCherry protein under the control of the Histone 4 promoter (\( \text{H4pro:mCherry} \)) as an approximate marker for cell divisions [31, 32], confirmed similar rates of cell proliferation along both domains [12] and revealed that \( \text{H4pro:mCherry} \) positive cells are present equally in \( \text{PXYpro:CFP} \) and \( \text{SMXL5pro:YFP} \) positive regions with the center of activity at the interface of both domains (Fig. 2E and F, Fig. S1).
To computationally recapitulate the observed pattern of cell division rates, we introduced a factor inhibiting cell divisions in the distal layers of the cambium. Such a factor was reminiscent of the receptor-like kinase MOL1 which, similarly to SMXL5, is expressed distally to PXY expressing cells and suppresses cambial cell divisions [27]. Because cells in the distal cambium region were characterized by high levels of PXY-active (Fig. 1B, D), we used this positional feature to introduce a local inhibition of cell division and, at the same time, to instruct phloem formation. Therefore, we modified the rule for cell differentiation such that when a cambium cell reached a specific size, it differentiated into xylem if [PXY-active] was low and into phloem when [active-PXY] was high. Thereby, our model followed a classical 'French flag' principle of development according to which concentration gradients of diffusible morphogens pattern surrounding tissues [33]. It is worth noting that the combined effect of CLE41 on cell proliferation, on phloem specification and on [PXY] may also be achieved by distinct phloem-derived factors mediating these effects individually.

Computational implementation of these rules (Model 2A) resulted in a descending gradient of cell division rates in the distal cambium domain likely due to high levels of PXY-active (Fig. 3A-D, Movie 2A, Movie 2B, Movie 2C). The cell division rate was highest in the proximal cambium domain defined by high [PXY] (Fig. 3D, Movie 2D). Also, not only xylem but also phloem was continuously produced and the fate of cambium cells was dependent on their position relative to the differentiated tissues. In the central cambium domain cells proliferated and constantly replenished the stem cell pool (Figure 3B, Movie 2A, Movie 2B, Movie 2C). Thus, by incorporating relatively simple rules, Model 2A was able to recapitulate major cambium features, including
phloem formation. Moreover, in qualitative terms, the resulting anatomy reproduced the anatomy of a mature Arabidopsis hypocotyl (Fig. 3A, B).

**Model of cambium dynamics offers an explanation for the effect of ectopic CLE41 expression**

To estimate the predictive power of Model 2, we tested its capacity to simulate the effects of experimental perturbation of cambium regulation. Ectopic expression of CLE41 by employing the *IRREGULAR XYLEM 3/CELLULOSE SYNTHASE CATALYTIC SUBUNIT 7* (*IRX3/CESA7*) promoter which is active in cells undergoing secondary cell wall deposition [34-36] substantially alters hypocotyl anatomy [15]. This effect was confirmed when *PXYpro:CFP/SMXL5pro:YFP* activities were analyzed in a plant line carrying also an *IRX3pro:CLE41* transgene (Fig. 4A). The *PXYpro:CFP* activity domain had a cylindrical shape surrounding the xylem in plants with a wild type background (Fig. 3A), while in the presence of the *IRX3pro:CLE41* transgene, *PXYpro:CFP* activity surrounded a reduced overall number of differentiated xylem cells and was present in irregularly shaped patches distributed over the whole cross-section (Fig. 4A). Moreover, we observed regions without *PXYpro:CFP* activity in proximal hypocotyl regions where *SMXL5pro:YFP* was active (Fig. 4A). Besides, a substantial part of *SMXL5pro:YFP* activity was detected in the distal regions of the hypocotyl forming islands of irregular shape sometimes intermingled with *PXYpro:CFP* activity (Fig. 4A). This activity pattern was in contrast to the one found in plants without the *IRX3pro:CLE41* transgene where *SMXL5pro:YFP* reporter activity surrounded the *PXYpro:CFP* expression domain only from the distal side (Fig. 3A). These results indicated that not only the radial anatomy of the hypocotyl [15] but also the cambium organization itself depends on the site of CLE41 production.
For a computational simulation of the effect of the \textit{IRX3pro:CLE41} transgene, we instructed xylem cells to produce CLE41 at the same rate as phloem cells (Model 2B). Although in this case xylem formation was initially repressed possibly due to high levels of PXY-active in all cambium cells (Fig. 4B, Movie 3A, Movie 3B, Movie 3C), new xylem cells were formed as soon as the distance between existing xylem and phloem cells became large enough such that CLE41 levels and, in turn, PXY-active dropped to permissive levels (Fig. 4C, Movie 3A, Movie 3B, Movie 3C). New phloem cells were produced close to existing phloem and xylem cells likely due to high levels of PXY-active (Fig. 4C, Movie 3D). As a result, Model 2B produced a similar disruption in cambium organization, as observed in \textit{IRX3pro:CLE41} plants (Movie 3A, Movie 3B, Movie 3C, Fig. 4D). Zones with both high [PXY-active] and low [PXY], which were found in the distal cambium in Model 2A (Fig. 3B), appeared in the organ center together with individual xylem cells (Fig. 4D). Moreover, in addition to being produced in distal regions, new phloem cells were produced in the central areas of the organ as demonstrated previously for \textit{IXR3pro:CLE41} plants [15]. Thus, rules determining cambium polarity implemented in Model 2 were sufficient to partly simulate organ anatomy found in wild type and \textit{IXR3pro:CLE41} genetic backgrounds.

However, a discrepancy between model structure and the \textit{in planta} situation was suggested when we compared a model with reduced PXY activity with \textit{pxy} mutants carrying the \textit{PXYpro:CFP} and \textit{SMXL5pro:YFP} reporters. In \textit{pxy} mutants the xylem tissue did not have a cylindrical shape, but was instead clustered in radial sectors showing \textit{PXYpro:CFP} and \textit{SMXL5pro:YFP} activity at their distal ends, whereas regions in between those sectors had little to no xylem (Fig. 4E). PXY promoter reporter activity
was observed distally to xylem sectors, whereas the SMXL5 promoter activity was as usual present distally to the PXY activity domain. Interestingly, the radial dimension of the PXYpro:CFP expression domain was not expanded in relation to the SMXL5pro:YFP domain and both domains were still completely distinct (Fig. 4E). This discrepancy indicated that, in contrast to our assumption, the CLE41-PXY signaling module did not restrict PXY promoter activity in the distal cambium. The discrepancy between Model 2 and the situation in plants was confirmed when we completely eliminated PXY* activity from our model (Model 2C). As expected, this resulted in the absence of growth due to the full dependence of cell* divisions on the PXY* function, clearly being at odds with the phenotype of pxy mutants (Fig. 4E). Even a computational reduction of PXY* activity (Model 2D) did not result in a split of the continuous cambium domain* but abolished phloem* formation and increased the production of xylem (Fig. 4F). Also, in contrast to the situation in the pxy mutant, the size ratio of the PXY* and active-PXY* domains was increased under conditions with reduced PXY* activity (Fig. 4E, F). Moreover, quantification of xylem vessels, xylem fibers and xylem parenchyma in sections from wild type and pxy mutant hypocotyls by automated image segmentation revealed that the total number of xylem cells and the number of xylem vessels was comparable (Fig. 4G-I). In contrast, the number of cells classified as fibers was substantially reduced in pxy mutants whereas the number of cells classified as parenchyma was increased (Fig. 4G-I). These results suggested that during radial growth, PXY promotes the formation of xylem fibers, while the formation of xylem vessels and the total number of cambium-derived cells produced proximally is hardly PXY-dependent.
Multiple phloem-derived factors determine cambium activity

Our observations prompted us to reconsider some features of our model and to extend the ‘French flag’ approach. Because the production rate of cells produced proximally by the cambium was not PXY-dependent, we made xylem* formation independent from the control of PXY-active*. Instead, cambium cells* differentiated into xylem* cells when they reached a specific size and, at the same time, expressed PXY* as a positional feature. To allow maintenance of active cambium cells* in the absence of PXY*, we introduced a second phloem*-derived factor (PF), reminiscent of the PEAR transcription factors identified recently [11]. PF stimulated cell* divisions by promoting the production of a division factor (DF) in cambium cells* and in phloem parenchyma* (Fig. 5A, see below). Cambium cells divided only if the concentration of DF exceeded a threshold value. DF production was at the same time stimulated by PXY-active* as its only effect in cambium cells (Fig. 5A). Thereby, cambial cell* divisions were dependent on the combined influence of PXY-active* and their proximity to phloem poles.

DF production was, thus, determined as follows:

\[
\frac{d}{dt}[DF] = diffusion_{DF} + \frac{production_{DF}[Stimuli]}{(k + [PF^*] + [PXY-active^*])} - degradation_{DF}
\]

(5)

Where k stands for an empirically defined coefficient.

Based on the strong association of xylem sectors with developing phloem cells (Fig. 4E), we further hypothesized that the formation of those sectors in pxy mutants was dependent on the heterogeneity of cell type distribution in the phloem. Therefore,
phloem cells* from the previous models were split into two cell types – phloem-parenchyma* and phloem-poles* (Fig. 5A). To achieve the dispersed pattern of phloem poles, cambium*-derived cells* fulfilling the criteria to differentiate into phloem (see above), differentiated into phloem poles by default, unless inhibited by PF, which was specifically produced in pole cells*. Thereby, phloem-poles* suppressed phloem-pole* formation in their vicinity, expected to result in a patchy pattern of phloem poles as observed in planta [37]. It is worth noting that CLE41* was still produced in both phloem poles* and phloem parenchyma* but with a higher rate in phloem poles*. To further achieve PXY*-independent cambium subdomain separation, phloem-parenchyma* and phloem-poles* were set to express another diffusive signal (RP) which suppressed PXY* expression in cambium* cells, the role that was played by PXY-active* before (Fig. 5A). Importantly, cell divisions in the distal cambium were not actively repressed anymore but were exclusively dependent on cell size and the level of DF.

Computational application of these principles (Model 3A) resulted again in the establishment of two cambium* subdomains – the distal subdomain which was characterized by high concentrations of DF and the proximal subdomain characterized by high PXY* concentration (Fig. 5B-D, Movie 4A, Movie 4B). Distally, the cambium* produced phloem-parenchyma* cells from which phloem-poles* were continuously formed with a pattern resembling the patchy phloem pattern observed in plants (Fig. 5B) [37]. Interestingly, the localization of PF production mainly in phloem poles* resulted in increased DF levels in the vicinity of those poles and, as expected, in locally increased cell* division rates (Movie 4C, Movie 4D). This observation was reminiscent of the activity of the cell division marker *H4pro:mCherry* in patches of cells distally to
the immediate cambium area where also the SMXL5pro:YFP reporter was active and which presumably contained developing phloem cells (Fig. S1).

By instructing CLE41* production also in xylem cells*, we simulated CLE41-misexpression by the IRX3 promoter (Model 3B, Movie 5A, Movie 5B, Movie 5C, Movie 5D, Fig. 5E). CLE41* interacted with PXY* on the proximal cambium* border, which resulted in ectopic DF production and phloem-parenchyma* formation in the proximal hypocotyl* regions (Fig. 5E). Still, xylem cells* were formed, generating a patchy xylem* pattern resembling the xylem configuration found in IRX3pro:CLE41 plants (Movie 5A, Fig. 4A, Fig. 5E). Eliminating PXY* (Model 3C) generated a patchy outline of the distal cambium* subdomain (Movie 6A, Movie 6B, Movie 6C, Movie 6D, Fig. 5F) likely because in cambium cells* at a certain distance from phloem poles*, PXY* was usually the main trigger of cell* divisions whereas PF was also influential next to phloem poles*. Thus, by introducing both a PXY*-independent pathway stimulating cambium* proliferation and dependence of cell* proliferation on the distance to phloem poles*, we were able to simulate important features of the pxy mutant phenotype (Fig. 4E, Fig. 5F). Collectively, we concluded that we established a cambium model with sufficient power and robustness to simulate major genetic perturbations of cambium regulation.

To incorporate realistic tissue ratios and unbiased parameter identification, we next performed an automated parameter search using a previous characterization of Arabidopsis hypocotyl anatomy [37] as a criterion for parameter selection. To this end, we instructed our search algorithm to aim for a tissue ratio of 20, 15 and 65 % for cambium*, xylem*, and phloem cell* number, respectively. Performing 4000
simulations resulted in a set of parameters (Table S1) producing a more realistic tissue anatomy than we achieved by our manually selected set before (Fig. 5G). Thus, by taking real tissue anatomy as a guideline, we were able to establish a model with a more realistic outline.
Discussion

Growth and development of multicellular organisms are complex non-linear processes whose dynamics and network properties are not possible to predict only based on information on their individual building blocks and their one-to-one interactions. The rather simple cellular outline along the radial axes of organs, growth in only two dimensions, and the recent identification of central functional properties [10-12], make radial plant growth an attractive target for a systematic approach to reveal its intriguing dynamics. Here, we developed a computational representation of radial plant growth using the VirtualLeaf framework [30] which can recapitulate fundamental features of this process and integrates the PXY/CLE41 module as one central element for cambium patterning and maintenance of tissue domains.

Using positional information mediated by morphogenetic gradients of diffusible chemicals to pattern growing structures is a classical concept in developmental biology [33, 38, 39]. In a first approach, we used the PXY/CLE41 module to generate such a gradient instructing cambium cells* to differentiate into xylem cells*, to proliferate or to differentiate into phloem cells*. Repression of cell division in the distal cambium was achieved by implementing an adverse effect of PXY-signaling* on PXY* production. Together, this setup was able to maintain stable radial tissue organization during radial growth and established a maximum of cell division rates in the cambium center as observed by experimental means [12]. Thus, we conclude that cambium organization and radial patterning of plant growth axes can be maintained by a distinct pattern of radially acting morphogens. Such a role was initially proposed for auxin whose differential distribution, however, seems to be rather a result of tissue patterning than being instructive [40].
In contrast to our expectations, though, the amount of proximal tissue production during radial plant growth did not depend on the function of \textit{PXY}. Automated image analysis including object classification revealed that neither the number of cells produced toward the organ center nor the number of vessel elements did change in a \textit{pxy} mutant background but rather the ratio between parenchyma and fiber cells. Therefore, in contrast to a negative effect of \textit{PXY}/\textit{CLE41} signaling on vessel formation in vascular bundles in leaves [18, 23], vessel formation during radial plant growth is \textit{PXY}/\textit{CLE41}-independent. Instead, fiber formation is positively associated with the \textit{PXY}/\textit{CLE41} module. These observations indicated that xylem formation is unlikely to be instructed by \textit{PXY}/\textit{CLE41} signaling alone but that additional signals are required.

Moreover, the application of markers visualizing cambium organization showed that \textit{PXY}-deficiency leads to the absence of an organized cambium in some regions of the hypocotyl whereas in other areas, the cambium is maintained. Since such areas are regularly spaced, factors acting in parallel to \textit{PXY}/\textit{CLE41} also carrying spatial information may be responsible for this pattern. Although ethylene signaling was reported to fulfill the first criterion, spatial specificity does not seem to be a characteristic property of ethylene signaling [41]. In contrast, PEAR transcription factors are phloem-derived and stimulate the proliferation of cambium stem cells presumably in a \textit{PXY}/\textit{CLE41}-independent manner [11] and, thus, may act similarly to the PF* factor we introduced in our model. The \textit{ERECTA}/\textit{EPIDERMAL PATTERNING FACTOR-LIKE} (ER/EPFL) receptor-ligand pathway acting in concert with the \textit{PXY}/\textit{CLE41} module [42, 43] represents another candidate for playing such a role. In addition, \textit{CLE45} was recently proposed to be expressed in developing sieve elements,
the conducting units of the phloem, and repress the establishment of sieve element identity in their immediate environment [44]. The PF* factor in our model combines features of these phloem-derived molecules.

In addition to the phloem sending out instructive signals, early xylem cells have been identified recently to act as an organizing center of cambium patterning [10]. Although this finding seems to be at odds with our claim that phloem-derived signals are sufficient for cambium organization, it is important to consider that we, for example, ignored upstream regulation of postulated factors like PXY* or CLE41* which obviously depends on positional information. Thus, reciprocal and interconnected gradients of regulators along the radial sequence of tissues may be essential for establishing and maintaining cambium organization, including xylem-derived signals.

In this context, it is interesting to note that we deliberately excluded the transition from the initially bisymmetric tissue conformation to a concentric tissue organization as occurring in hypocotyls and roots [10, 37] from our simulations. Our rationale was that the rather complex change in tissue anatomy during the transition from a primary to a secondary conformation in the hypocotyl required more assumptions in our model and would have spoiled the advantages of a relatively simple anatomy for generating a cell-based computational model. Moreover, the differences in primary anatomy of shoots and roots before the onset of radial plant growth [10, 32] would have required different cellular outlines for both cases and, thus, would have hampered the generality of our approach. Interestingly, when starting with a concentric anatomy of tissues, the circular shape of the organ* was maintained and no additional mechanism ensuring organ circularity had to be postulated. The maintenance of the circularity of the entire organ*
during its expansion was an emerging property of a radial domain of cell proliferation. However, it is likely that more peripheral tissues like the epidermis or the periderm [45], which we did not consider in our model, influence organ shape *in planta*.

We envision that the model presented in this study allows recapitulating qualitative and quantitative variation in radial plant growth found in different mutants and when comparing different dicotyledonous species [46]. Remarkable features like the establishment of concentric cambium rings often found in the order of Caryophyllales [47] or ‘phloem wedges’ found, among others, in the Bignonieae genus [48] may be recapitulated by modifying parameters chosen in the model or by the invention of novel factors. Moreover, the model may help to predict targets of environmental stimuli inducing changes of cambium activity like seasonal changes [49] or mechanical perturbation [50], allowing the generation of testable hypotheses. Thus, our dynamic model will be a useful tool for investigating a process not possible to observe in real time and partly develops over exceptionally long periods.
Material and Methods

Plant material and growth conditions

Arabidopsis thaliana (L.) Heynh. plants of Columbia-0 accession were used for all experiments and grown as described previously [22]. pxy-4 (SALK_009542, N800038) mutants were ordered from the Nottingham Arabidopsis Stock Centre (NASC). Plant lines carrying IRX3pro:CLE41 and 35Spro:CLE41 transgenes [15] were kindly provided by Peter Etchells (Durham University, UK). PXYpro:ECFP-ER (pPS19) and SMXL5pro:EYFP-ER (pJA24) reporter lines were described previously [51, 52].

Generation of the H4pro:mCherry transgene

The H4pro:mCherry-ER (pMS77) vector was generated using pGreen0029 [53] as a backbone. The 5’ and 3’ promoter regions of the H4 gene were first amplified using genomic DNA as a template using the primers H4for2/H4rev2 (5’-actaggtacctagtgttgctgcaagtgacac-3’/5’-actagaattcttgatgcatttttcagcgaagattaatgattttatc-3’) and H4for3/H4for3 (5’-actagtacagttatatctctcagggcagactgacaaagctgataaagtgaac-3’/5’-actagcggccgaaagctgataaaattggaac-3’), respectively. The resulting DNA fragments were cloned into KpnI/NotI restriction sites of pGreen0029 resulting in pMS76. Next, the mCherry reporter sequence was fused to target signals for the endoplasmatic reticulum [54] and cloned into Nsil/PstI sites generated between the two promoter fragments.
Confocal microscopy

Confocal microscopy of hypocotyls was performed as described before [22]. Hypocotyls were isolated and cleaned from surrounding leaf material using razor blades (Classic Wilkinson, Germany). The cleaned hypocotyls were mounted in 7% low melting point agar (Sigma-Aldrich, St. Louis, MO, USA) in water and 200 μm sections were taken using a vibratome (Leica VT1000 S). For analyzing the fluorescent markers, the following microscopes were used: LSM 880, LSM 780 microscope (Zeiss, Germany) and Leica SP5 (Germany). Different fluorescence protein signals were collected in different tracks. YFP was excited at 514 nm and emission was collected at 522-542 nm. CFP was excited at 458 nm and the signal emission was collected at 469-490 nm. The propidium iodide-derived signal was excited at 561 nm and emission was detected at 620-670 nm. mCherry was excited at 561 nm and emission was detected at 600 - 650 nm.

Histology

Histological analyses of the stem were performed as described previously [51]. All samples whose histology was compared were grown in parallel.

Ilastik cell type counting

The xylem area was cropped manually from histological images of wild type and pxy mutant. The Ilastik toolkit [55] was used for image segmentation and cell type classification (https://www.ilastik.org). With a training set, the pixel classification workflow was trained to distinguish cell walls from the background. After segmentation, the object classifier was then trained to split the resulting objects into four groups - xylem vessels, xylem fibers, xylem parenchyma, and unclassified objects. The
resulting classifier was then applied to all cropped images. For each image, cell type
data were extracted using python.

**VirtualLeaf simulations**

Simulations were performed as recommended previously [30]. To be able to see
established models in action, the VirtualLeaf software was installed according to the
following instructions described in the supplementary information and as described
previously [56]. All simulations within Model 1, Model 2, and Model 3, respectively,
were conducted for the same VirtualLeaf time duration. For each of the models
described in this paper, we provide code files in the “model_codes” folder found at
https://github.com/kergakerga/cambium_models.

**Splitting the result of VirtualLeaf simulations into bins**

After a VirtualLeaf simulation was completed, the resulting xml template was stored.
To analyze the distribution of chemicals* in such a template along the radial axis, we
produced a python script named “Cambium_bins_calculation.ipnb”. Within the script, it
was possible to indicate the path to the xml file, and the script produced two .csv files
– one with a table containing data about each cell and another with information about
averages across the requested bin number.

**Parameter optimization**

In order to optimize the parameters of our model we took advantage of the “Hyperopt”
python library [57]. To extract cell numbers in each tissue after each simulation, we
built a python script able to run VirtualLeaf simulations automatically using a distinct
set of parameters as input. After every simulation, the script counted the number of
cells belonging to each cell type and computed their relative proportion. To use
Hyperopt, we needed to design a score function and the parameter space. The score function should contain information about the optimization goals - during the parameter search, Hyperopt will attempt to minimize this function. The parameter space contains an interval for each parameter from which the parameter value can be chosen. Based on *in planta* observations [37], we defined that the simulation should result in 20% cambium, 15% xylem, and 65% phloem cells. Thus, we created this score function: 
\[(c-20)^2 + (x-15)^2 + (p-65)^2 + (t/3000 \times 100)^2\], where c, x, and p were the relative amount of cambium, xylem, and phloem cells, respectively. We added the total number of cells (t) to the score function to encourage model growth during the parameter search. This function had lower values when the result of a simulation was closer to the desired issue proportions. To define the parameter search space, we used parameter values found during the model creation procedure. We designed a search space for each parameter around the value which was manually found using the following criterion: 
Manually found Value / 3 < Search space values < Manually found Value * 3. As we were interested in obtaining simulations with an active cambium we discarded simulations that resulted in hypocotyls* with less than 300 cells* in total and with cambium cells less than 30.
Acknowledgements

We thank Peter Etchells (Durham University, UK) for providing seed material, Karin Grünwald and Martina Laaber-Schwarz (both GMI, Vienna, Austria) for technical assistance and Dongbo Shi, Eva-Sophie Wallner and Vadir López-Salmerón for comments on the experimental strategy and the manuscript. We also thank Claudiu Antonovici (University of Leiden, The Netherlands) for help in setting up the VirtualLeaf platform. This work was supported by the Deutsche Forschungsgemeinschaft (DFG) through the Research Unit FOR2581 ‘Plant Morphodynamics, grant GR2104/4-1 and a Heisenberg Professorship (GR2104/5-2) to T.G.. The work by B.H.M. was initiated at Centrum Wiskunde & Informatica (CWI), Amsterdam, The Netherlands. R.M. and B.H.M. thank CWI for providing a CWI Internship to B.H.M. and for hosting I.L..

Author Contributions

Conceived and designed the experiments: IL, BHM, RM, TG. Performed the experiments: IL, BHM, AZ, NG. Analysed the data: IL, BHM, AZ. Wrote the paper: IL, TG.

Conflict of Interest

The authors have no conflicts of interest to declare.
Supplementary Information Items

Figure S1: Visualization of H4 promoter activity within cambium subdomains

Table S1: Parameter values and chemicals

Supplementary Methods: Instructions for implementing VirtualLeaf models

Movie 1A: Model 1 output, visualizing xylem (red) and phloem (purple), and accumulation of PXY* (blue) and PXY-active* (green)

Movie 1B: Model 1 output, visualizing CLE41* (yellow) accumulation

Movie 1C: Model 1 output, visualizing cell divisions (red)

Movie 2A: Model 2A output, visualizing xylem (red) and phloem (purple), and accumulation of PXY* (blue) and PXY-active* (green)

Movie 2B: Model 2A output, visualizing CLE41* (yellow) accumulation

Movie 2C: Model 2A output, visualizing cell divisions (red)

Movie 2D: Model 2A output, visualizing cell divisions (red) together with PXY* (blue) and PXY-active* (green) accumulation

Movie 3A: Model 2B output, visualizing xylem (red) and phloem (purple), and accumulation of PXY* (blue), and PXY-active* (green)

Movie 3B: Model 2B output, visualizing CLE41* (yellow) accumulation

Movie 3C: Model 2B output, visualizing cell divisions (red)

Movie 3D: Model 2B output, visualizing accumulation of PXY* (blue) and PXY-active* (green)
Movie 4A: Model 3A output, visualizing xylem (red), phloem parenchyma (light purple), and phloem poles (dark purple), and accumulation of PXY* (blue) and the division chemical (DF)* (green)

Movie 4B: Model 3A output, visualizing CLE41* (yellow) accumulation

Movie 4C: Model 3A output, visualizing cell divisions (red)

Movie 4D: Model 3A output, visualizing accumulation of PXY* (blue) and the division chemical (DF)* (green)

Movie 5A: Model 3B output, visualizing xylem (red), phloem parenchyma (light purple), and phloem poles (dark purple), and accumulation of PXY* (blue) and the division chemical (DF)* (green)

Movie 5B: Model 3B output, visualizing CLE41* (yellow) accumulation

Movie 5C: Model 3B output, visualizing cell divisions (red)

Movie 5D: Model 3B output, visualizing accumulation of PXY* (blue) and the division chemical (DF)* (green)

Movie 6A: Model 3C output, visualizing xylem (red), phloem parenchyma (light purple), and phloem poles (dark purple), and accumulation of PXY* (blue) and the division chemical (DF)* (green)

Movie 6B: Model 3C output, visualizing CLE41* (yellow) accumulation

Movie 6C: Model 3C output, visualizing cell divisions (red)

Movie 6D: Model 3C output, visualizing accumulation of PXY* (blue) and the division chemical (DF)* (green)
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Figure 1. Initial model generation. (A) Tissue template used to run VirtualLeaf simulations. Phloem* is depicted in purple, xylem* in red. Cambium* cells are colored according to their levels of PXY* and PXY-active*. Cambium* is colored in blue due to the initial level of PXY*. (B) Output of simulation using Model 1. (C) Visualization of cell division rates within the output shown in (B). Dividing cells are marked by a red color which fades over time. (D) Visualization of CLE41* levels within the output shown in (B). (E) Sorting cells* within the output shown in (B) into bins based on how far their centers are from the center of the hypocotyl*. Different colors represent different bins. (F) Visualization of the relative chemical levels and division rates in different bins shown in (E). Each chemical’s bin average is calculated and then expressed as a percentage of the maximum bin value of the chemical. Bin colors along the x-axis correspond to the colors of bins in (E).
Figure 2. Visualization of \textit{H4} promoter activity within cambium subdomains. (A-F)
\textit{PXYpro:CFP} (blue) and \textit{SMXL5pro:YFP} (green) activities mark proximal (A) and distal (B) cambium subdomains, respectively, and show only a small overlap (D, arrows). The overlap of signals from the \textit{H4pro:mCherry} (red) (C) and proximal (E) and distal (F) cambium markers indicate the presence of cell in the S-phase in both subdomains. Arrows point to the same position in each picture. Scale bars: 50 \textmu m.
Figure 3. Implementing phloem formation into the model. (A) Cross-section of a wild type hypocotyl expressing PXYpro:CFP (blue) and SMXL5pro:YFP (green). Cell walls are stained by propidium iodide, mainly visualizing xylem (red). Only a quarter of the hypocotyl is shown with the center in the bottom right corner. Scale bar: 100 μm. (B) Output of simulation using Model 2A. Unlike Model 1, Model 2A produces new phloem* cells. (C) Sorting cells* within the output shown in (B) into bins. (D) Visualization of the relative chemical levels and division rates in different bins shown in (C). Bin label colors along the x-axis correspond to the colors of bins shown in (C).
Figure 4. Comparing the effect of perturbing cambium activity in the model and in plants. (A) Cross-section of a hypocotyl carrying PXYpro:CFP (blue), SMXL5pro:YFP (green) markers, and the IRX3pro:CLE41 transgene. Cell walls are stained by propidium iodide visualizing mostly xylem (red). Arrowheads point to proximal hypocotyl regions where SMXL5pro:YFP activity is found. Arrows indicate distal regions with SMXL5pro:YFP activity. Cell walls are stained by propidium iodide visualizing mostly xylem (red). Only a quarter of the hypocotyl is shown with the center in the bottom right corner. Scale bar: 100 μm. (B) First frames of Model 2B simulations. Due to the expression of CLE41* by xylem* cells, high levels of PXY-active* are generated around xylem cells* already at this early stage. (C) Intermediate frames of Model 2B simulations. Newly formed xylem cells* express CLE41* and produce high levels of PXY-active* next to them (white arrowheads). (D) The final result of Model 2B simulations. Zones of PXY* (blue) and PXY-active*(green) are intermixed, xylem* cells are scattered, and phloem* cells are present in proximal areas of the hypocotyl*. (E) Cross-section of a pxy mutant hypocotyl carrying PXYpro:CFP (blue) and SMXL5pro:YFP (green) markers, stained by propidium iodide (red). The xylem shows a ray-like structure. Only a quarter of the hypocotyl is shown with the center in the bottom right corner. Scale bar: 100 μm. (F) Final result of Model 2C simulations. Reducing PXY* levels leads to similar results as produced by Model 1 (Figure 1B) where only xylem* is produced. (G, H) Comparison of histological cross-sections of a wild type (G) and a pxy (H) mutant hypocotyl, including cell type classification produced by ilastik. The ilastik classifier module was trained to identify xylem vessels (red), fibers (green), and parenchyma (purple), unclassified objects are shown in yellow. (I) Comparison of the number of xylem vessels, fibers and parenchyma cells found in wild type (blue) and pxy mutants (purple). Welch’s t test was performed comparing wild-type and pxy mutants for the different cell types (n = 11-13). ***p < 0.0001, *p < 0.05. Lines indicate means with a 95 % confidence interval.
**Figure 5. An extended model for simulating genetic perturbations.** (A) Regulatory network proposed based on experimental observations. (B) Result of the simulation run for Model 3A. This model implements the network interactions described in (A). (C) Outline of cell bins for the results of Model 3A, as shown in (B). (D) Visualization of the relative levels of chemicals and division rates in different bins. Bin colors along the x-axis correspond to the bin colors in (C) (E) Output of Model 3B simulation. Ectopic CLE41* expression was achieved by letting xylem cells* produce CLE41*. (F) Output of Model 3C. Simulation of the pxy mutant was achieved by removing the stimulation of DF* production by PXY* and hence by removing the effect of PXY* on cell division and cambium* subdomain patterning. Because of the network structure, PXY* can be eliminated from Model 3 without letting the model collapse (Fig. 4F) but reproducing the pxy mutant phenotype observed in adult hypocotyls (Fig. 4E). (G) Comparison of numbers and proportions of distinct cells* in the initial tissue template (as shown in Fig. 1A, in green) with the final model output before the automated parameter search (as shown in Figure 5B, in blue) and the model output after the parameter search (in orange). In yellow, values found for wild type (Col-0) hypocotyls 20 days after germination [37] are depicted.
Figure S1. Visualization of *H4* promoter activity within cambium subdomains. (A-F) *PXYpro:CFP* and *SMXL5pro:YFP* mark proximal (A) and distal (B) cambium subdomains, respectively. *H4pro:mCherry* (C) is used as a marker for cells in the S-phase. The overlay of signals of *H4pro:mCherry* and proximal (E) and distal (F) cambium markers indicates cell division in both subdomains. Scale bars: 100 μm.
### Table S1: Parameters and chemicals

| index | function                                                                 | before search | after search |
|-------|--------------------------------------------------------------------------|---------------|--------------|
| k0    | chemical 6 limit above which parenchyma cell can divide                  | 1.00E-04      | 9.28E-05     |
| k1    | xylem max cell size                                                      | 1.00E+00      | 1.43E+00     |
| k2    | not used                                                                 | 1.00E+01      | 1.87E+01     |
| k3    | not used                                                                 | 2.30E+00      | 6.05E+00     |
| k4    | chemical 5 limit below which parenchyma can convert to phloem pole      | 1.00E-06      | 1.80E-06     |
| k5    | chemical 6 limit above which cambium cell can turn into parenchyma      | 2.40E-02      | 6.53E-02     |
| k6    | chemical 6 limit above which cambium cell can divide                     | 1.00E-04      | 6.27E-05     |
| k7    | phloem parenchyma max cell size                                          | 3.00E+00      | 8.38E+00     |
| k8    | size above which parenchyma is converted to phloem poles                | 1.50E+00      | 1.55E+00     |
| k9    | phloem pole max cell size                                                | 3.00E+00      | 5.83E+00     |
| k10   | cambium cell max cell size                                               | 2.30E+00      | 4.62E+00     |
| k11   | cambium cell size limit above which it can convert to xylem             | 1.90E+00      | 1.20E+00     |
| k12   | chemical 1 limit above which cambium cell can convert into xylem        | 8.00E+00      | 7.82E+00     |
| k13   | rate of how much chemical 4 supress expression of pxy                    | 1.00E+02      | 2.87E+02     |
| k14   | not used                                                                 | 4.80E+01      | 5.51E+01     |
| k15   | cell size above which parenchyma cell can divide                         | 1.00E+00      | 6.70E-01     |
| k16   | cell size above which cambium cell can divide                            | 1.00E+00      | 8.19E-01     |
| k17   | defines saturation curve for chemical 6 (so chemical 6 concetration is restricted from above) | 1.42E-02      | 2.35E-02     |
| k18   | defines saturation curve for chemical 6 (so chemical 6 concetration is restricted from above) | 1.39E+01      | 3.44E+01     |
| k19   | cle41 production rate in phloem parenchyma                              | 1.00E-01      | 1.01E-01     |
| k20   | cle41 production rate in phloem poles                                    | 1.00E+00      | 1.87E+00     |
| k21   | rate of how much input pxy makes in stimulating production of chemical 6 (rate 0 would be pxy mutant) | 1.00E+02      | 1.43E+02     |

#### Chemicals

| Chemical | Description |
|----------|-------------|
| 0        | cle41       |
| 1        | pxy free    |
| 2        | pxy active  |
| 3        | PROMOTES DIVISION CHEMICAL (COMES FROM PHLOEM POLES) |
| 4        | SUPRESSES PXY EXPRESSION (COMES FROM ALL PHLOEM CELLS) |
| 5        | SUPRESSES PHLOEM POLE FORMATION (COMES FROM PHLOEM POLES) |
| 6        | DIVISION CHEMICAL |
Supplemental Methods:

Instructions for implementing VirtualLeaf models

To be able to see established models in action, the VirtualLeaf software should be installed according to the following instructions and as described previously [1]. There are three files to be installed to view a model. For each model described in this paper, we provide these three files in the “model_codes” folder found at https://github.com/kergakerga/cambium_models.

1. Model.h

This is a c++ header file containing a line with the following structure: “this:virtual QString DefaultLeafML(void) {return QString("hypo7.xml");}”. The line indicates where VirtualLeaf should search for an xml file that describes the structure of the tissue template (called “leaf”) used for the model to run upon. In this particular example, the name of the xml template is “hypo7.xml”. VirtualLeaf will go to the folder in which you installed the software and will look for this file in the subfolder “../data/leaves”. In our case, a Windows machine was used. Therefore, the full path looked like this: “C:\VirtualLeaf-v1.0-src\data\leaves” and this folder contained a file “hypo7.xml”. Please note that paths will be different depending on the operating system being used.

2. Model.cpp

A c++ file containing the model algorithm to reproduce the output described in this study. A formal description of each model was given within the main text.
3. Leaf.xml

A file containing the description of a tissue template as described before [2]. The software uses this file to construct a tissue template and to run a given model.

In order to run or modify a provided model, follow the following instructions.

a. Create a new model with the desired name (e.g. “my_cool_model”) as described [2].

b. After a new model was created, there should be a folder “../src/my_cool_model” in your VirtualLeaf folder. In our case, the full path looked like this: “C:\VirtualLeaf-v1.0-src\src\TutorialCode\my_cool_model”.

c. In your “../src/TutorialCode/my_cool_model” folder locate “my_cool_model.h” and “my_cool_model.cpp” files. Using a text editor replace the content of those files by the content of the respective files from the model you are interested in (files provided in this paper are called “uncoupleCle.h” and “uncoupleCle.cpp”). Please note that you should only replace the content of the files and not the files themselves. After you have completed this step, your files should still be named “my_cool_model.h” and “my_cool_model.cpp”.

d. Open the files “my_cool_model.h” and “my_cool_model.cpp” using a text editor and replace every instance of “uncoupleCle” by “my_cool_model” in the text. Save the changes.

e. Locate the “../data/leaves” folder and add the provided xml file defining the tissue template (in our case, the tissue template is called “hypo7.xml”). The resulting full path to the file had the following structure in our case: “C:\VirtualLeaf-v1.0-src\data\leaves\hypo7.xml”.

f. Compile the model as described [2]. In our case, we used a qt-console, switched to the folder with the model (make sure your VL is not running): “C:\VirtualLeaf-v1.0-src\src\TutorialCode\my_cool_model” and run “set MAKE=mingw32-make” and
“mingw32-make”. Please note that each time you introduce changes into the code, you should recompile the model.

**g.** Now you can run VirtualLeaf. Go to the “../bin’ folder and run the “VirtualLeaf” file. In our case the full path looked like this: “C:\VirtualLeaf-v1.0-src\bin\VirtualLeaf”.

The new model will appear under the “Models” section with the corresponding name. Please note that the name of the model that will be shown is not the same as “my_cool_model”. Instead, it will show whichever name was indicated in the “my_cool_model.cpp” file in this line: // specify the name of your model here; return QString( “Model 1 - pxy only” )”. In this case, there will be a new model called “Model 1 - pxy only” in the VirtualLeaf folder under the “Models” section.

**Literature**

1. Merks, R.M., and Guravage, M.A. (2013). Building simulation models of developing plant organs using VirtualLeaf. Methods Mol Biol 959, 333-352.
2. Merks, R.M., Guravage, M., Inze, D., and Beemster, G.T. (2011). VirtualLeaf: an open-source framework for cell-based modeling of plant tissue growth and development. Plant physiology 155, 656-666.