Generation of a **Conjoint Surface Plasmon** by an Infrared Nano-antenna Array

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Localized surface plasmons (LSP) excited by optical fields have many potential applications resulting from their ability in detecting ultra-small, ambient refractive index change. Current methods using surface nano-patterning by means of lithography have given rise to LSP of limited propagation and interaction lengths, meaning that practical applications remain challenging. This paper de-
scribes a new all-optical method of generating LSP by means of a carefully fabricated low dimensional nano-structured material by using a direct-write photochemical lithography. It is shown that the resulting array of localized surface plasmons combine or “Conjoin” to have an unprecedented large interaction length, via coupled evanescent fields, giving rise to superior spectral sensitivities; several orders of magnitude better than those quoted elsewhere and reaching $6\times10^3$ nm/RIU in the aqueous regime and $10^4$ nm/RIU in the gaseous regime. Numerical modeling was performed that showed this design of plasmonic platform is capable of producing sensitivities of $10^5$-$10^6$ nm/RIU.

We believe the results achieved in this investigation show that a unique conjoint surface plasmon operational mode will significantly impact areas of interest, such as single molecular dynamics, drug delivery systems etc.

1. Introduction

Localized Surface Plasmons (LSPs) are damped collective free-electron oscillations, which can be generated on the surface of a nano-patterned metal when excited by electromagnetic radiation over a wide wavelength range. The field patterns of LSPs are extremely sensitive to optical parameters, such as changes in the refractive index (RI) surrounding the structured metal surface. This has led to intensive studies of the behavior of LSPs, with a view to exploiting their significant potential in various applications. For example, as sensors,\cite{1} for surface enhanced spectroscopy,\cite{2} in photonic circuits,\cite{3} within medical diagnostics/therapeutics and for monitoring real-time label-free biomolecular kinetics.\cite{4,5} The LSPs exhibit low loss, high penetration depth and a large spatially extended evanescent field. In the infrared spectrum they are exploited in biological and molecular fingerprinting identification for medical diagnostics,\cite{6} biochemistry and environmental sensing.\cite{7,8}

More recently, researchers are beginning to see the potential important role for plasmonics in optoelectronics and telecommunications.\cite{9,10}

It is well known that the dynamics of LSPs can be strongly influenced by subtle changes in the properties of any nano-patterned metal surface, e.g. surface roughness, re-scattering losses, along with other losses from the conversion of the surface plasmons into radiative bulk waves, leading to
a prominent spectral shift of the LSPs resonances. Furthermore, the spatial distribution of the LSPs’ evanescent field extends into the surrounding medium that defines their propagation and interaction length, and these two factors govern the spectral sensitivity of LSPs. To date, various types of surface patterns and geometries have been investigated in order to enhance LSPs’ sensitivity, including nano-spheres and nano-wells.\textsuperscript{[11,12]} There remains, however, one major obstacle the LSP propagation distance places a limit on the potential of having ultra-high spectral sensing sensitivities. To overcome this limitation, researchers since the 1970s have been investigating a myriad of surface structures, including metal nano-antennae to enhance the optical properties (including extending the propagation distance and the interaction length of the LSPs).\textsuperscript{[12]} Furthermore, research into the properties of LSPs and their generation has gathered significant momentum in recent years,\textsuperscript{[13]} because of the LSPs’ quantum size effect resulting from discrete electron bands and the intrinsic ability to produce significantly stronger and confined electromagnetic fields supporting highly efficient LSP resonance.\textsuperscript{[14]} These advances have led to applications, such as direct conversion of light to electrical power,\textsuperscript{[15]} metamaterials,\textsuperscript{[16]} optical switches,\textsuperscript{[13]} and sensors.\textsuperscript{[17]} The latter offers the abundant potential of low cost sensing with 1 pico-mole detection limits for certain bio-applications.\textsuperscript{[18]} Nano-antenna devices are strong contenders as ultra-sensitive sensors.\textsuperscript{[19]} The complexity in fabrication, however, currently hinders their development.\textsuperscript{[20,21]}

In this work, we use a thin-film deposition technique (sputtering) followed by a direct-write UV-chemically induced geometric inscription technique to produce a large, long-range ordered array of nano-antennae on a composite film coated planar surface. We discover in our investigations that the fabricated plasmonic platforms create infrared LSP evanescent fields that overlap with the evanescent field generated by adjacent nano-antennae within the array; moreover these fields are strongly coupled. This creates coupled evanescent fields from adjacent nano-antennae that spans over the entire array of the nano-antenna, thereby resulting in a “collective” evanescent field created by the individual nano-antenna within the array. This “collective field” can be visualized has a distinct mode of operation over the nano-antennae array, an assembly of LSP that can be thought of as a

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single conjoint surface plasmon. This new mode of operation of the surface plasmon are distinctively different from previously reported LSPs, whether they are conventional, damped, short-range, long-range and localized. Furthermore, the nano-antennae within the array have long range repeatability on the order of 1cm, thus the adjacent LSPs can couple to each other across the entire surface area of the nano-antenna array. Such long range ordered nano-antennae array with mutually coupled LSPs produces an effective interaction length on scale of few millimeters, which is 2 to 3 orders of magnitude higher than that of the conventional/typical LSP. Therefore, as the single nano-antenna’s LSPs is perturbed, this perturbation propagates across the nano-antennae array.

This distinctive feature leads to some of the highest spectral sensing sensitivities reported to date, exceeding $10^4 \, \text{nm/RIU}$ in the gaseous index regime and $6 \times 10^3 \, \text{nm/RIU}$ in the aqueous index regime. Firstly, experimental results presented in this paper. Secondly, to explain the spectral behavior observed two modeling approaches have been used. To establish that these nano-antenna arrays produce LSPs resonances and the resonances polarization dependence as experimentally observed with these devices. We used a conventional analytical model that uses the measured dimensions of Pt nano-antennae array to calculate spectral location of resonances of LSPs. The analytical approach yields LSPs resonances in the same spectral location and predicts their tunability over a large spectral range for a single plasmonic device/sensor with polarization dependence. The issue with the analytical approach is that it fails to predict the experimental spectral index sensitivities. To predict these spectral index sensing sensitivities and to explain the mechanism that produces such high sensitivities a second modeling approach using numerical Finite Element Method (FEM) was implemented. The FEM model showed reasonable agreement with regards to sensing sensitivities. In addition, the FEM model produced data that was used to understand the mechanism behind the high sensitivities, through the mutually coupled LSPs by investigating the spatial extension of their evanescent fields generated by the surface plasmons, which is perpendicular to the surface of the nano-antenna. These mutually coupled evanescent fields creates a homogenous field extending over the array of nano-antennae.

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The findings reported here also show possibly new direction to achieve further sensitivity enhancement. The FEM modeling has shown that the spectral sensitivity can potentially reach ultra-high values up-to $10^5$-$10^6$ nm/RIU in the aqueous regime. The authors have already used this optical phenomenon, in conjunction with gold-thiol immobilized bio-recognition molecule, a bisphenol-A aptamer.[22] The combination of this optical platform working with this aptamer has produced a detection scheme capable of sensing the presence of small molecules. In this particular case, bishenol-A (size 228 Da), yielding a limit of detection of 330 atto-molars.[22]

2. Results
The 2-dimensional nano-structured, optical-plasmonic platform devices possess a long-range order on the scale of ~1 centimeter. This is realized in a two-stage process; step-one, the fabrication of a multi-layered thin film/coating on the supporting waveguide (studied using planar BK7 substrates and used with D-shaped single mode optical fiber as the optical waveguide) are fabricated using RF sputtering machine. The sputtering machine deposited three different materials onto a supporting substrate/waveguide. These materials are thin films of germanium (48nm), silicon dioxide (48nm) and a metal over-lay coating that could be of various thicknesses, depending upon the metal used, which creates a planar structure. Step two, the fabrication of the 2-dimensional nano-structure produced by UV photo-bleaching;[23] this is a chemical reaction between UV irradiance and the germanium/germanium oxide. This is a standard reaction used to fabricate Bragg gratings in optical fibers; more detail on the entire fabrication process steps is given in the experimental and method section of this paper. There are two physical mechanisms occurring with regards the illumination of the germanium material by UV radiation. Firstly, a redox reaction occurring specifically at Ge=O/Ge-O bonds resulting in a change in the electron density that modifies the permittivity, and so the refractive index at that location. Secondly, the elasto-optic effect,[24] which creates additional changes to the refractive index in the material due to a “geometric spatial compaction” of the material itself, resulting in stress within the material. This 'compaction' mechanism results in the physical for-
formation of 2-dimensional nano-structures on the supporting substrate surface, from the initial planar metal (gold) overlay (prior to UV illumination) to a situation where the metal is located at the vertices of the corrugation, thereby creating metal (gold) nano-antennae surrounded by air and SiO$_2$ after the UV processing, (Figure 1). The net effect is the creation of an array of parallel gold nano-antennae on the surface, with a repeatable scale on the order of one centimeter.

**Figure 1.** Surface profile characteristics of the fabricated samples. a) An AFM scan showing typical regions of pristine coating without UV-laser irradiation and UV-laser exposed area with nano-
structuring. The arrows shows the two directions to evaluate spatial frequencies b) A high spatial resolution AFM scan showing the detail of the surface topology associated with each of the individual nano-antennas. The zoomed inset depicts the fine structures inside the nano-antenna. c, d) describe typical variation of the spatial frequencies along an individual nano-antenna and across the nano-antennas respectively. e) A typical microscopic image of the processed BK7 glass. f) An AFM of a typical nano-antennae array on a planar 200 µm-thick BK7 substrate, along with a cross-section line profile of the AFM. g) Conceptual illustration of the mechanism of the optical conjoined surface plasmonic array. h) Schematic of the fabrication procedure and materials used (Ge-SiO$_2$-Pt) for the plasmonic devices. Note: in all the cases, coating layers from bottom to top are 48 nm germanium, 48 nm silicon dioxide, and 32 nm gold respectively.

Atomic force microscopic (AFM) measurements, shown in Figure 1a and Figure 1b, reveal that the surface topology of the mechanically lapped and coated D-shaped fiber, after UV-irradiance through a phase mask. The coating layers from bottom to top are germanium, silicon dioxide and the metal overlay. The corresponding film thicknesses are inter-related and chosen to maximize the surface plasmon field; further details of the fabrication process are given in the Supporting Information section. Noticeably, the surface features small striped elements (nano-antennae) with a mean width of 110±10 nm and a typical length of 10±0.5 µm. They form an array with a predominant period of 520±10 nm and a typical array length of 1 cm to 2 cm.

The zoomed AFM image further reveals a twisted, rope-like nano-antenna structure with a defined orientation. Fast Fourier transform (FFT) analysis performed along an individual nano-antenna and on cross-sections between nano-antennas is shown in Figure 1c and Figure 1d, respectively. It reveals fundamental periods of 0.54 µm and 1.02 µm across the corrugations, which is consistent with the 1.02 µm fundamental period of the phase mask used when irradiating with UV irradiance. The fundamental period along an individual antenna is 0.29 µm. It is the direct result of the focused UV-laser beam passing through the phase mask and generating a 3-dimensional fringe pattern on
the sample. The “twisted rope-like” shape is hence associated with the germanium on exposure to the highest UV light intensity. This pattern is more predominant if the fiber samples are not parallel to the phase mask. We noted that the planar BK7 glass with the same coating produces similar surface topological profiles to the aforementioned coated D-shaped fiber, as shown in Figure 1e and Figure 1f. The length of a single nano-antenna in this case is ~30 µm, with an overall scale of the patterned region of 2 cm. Furthermore, regularity/repeatability of the surface structures on the planar sample can be seen from a typical cross-sectional line profile of an AFM image in Figure 1f. A closer inspection of Figure 1f shows an envelope function in the amplitude/height of the surface corrugations. Performing a FFT on a typical cross-section line profile of an AFM map detected dominant harmonics with periods of 0.54 µm, 1.02 µm and 1.54 µm, which suggests that there is mixing of residual zeroth order with the +1st orders of the phase mask causing multiple beam mixing. Figure 1g illustrates the concept of the conjoined surface plasmons, showing a typical localized surface plasmon that is generated and propagates along individual nano-antenna within the array. In addition, Figure 1g shows the spatial extension of the perpendicular electric evanescent field generated by the surface plasmons at the surface of the nano-antenna and that there is significant overlap between the electric field generated from a single nano-antenna to its adjacent nano-antenna.

We investigate first the LSP-induced polarization responsivity of the nano-patterned D-shaped fiber in air at room temperature and at one atmosphere pressure, using the configuration shown in Figure 2. A broadband light source is linearly polarized and the polarization state of the light is controlled that is used to optically illuminate the sensing platform and its LSPs. The optical transmission spectra of the sensing platform which includes the excitation resonances of the LSP is monitored using an approach similar to a previous report.

In order to measure the spectral index sensitivity of the LSP sensing platform, the D-shaped optical fiber is held in a V-groove on an aluminum plate mounted on an optical table that acts as a heat sink to maintain a constant temperature of 23 °C throughout the experiment, see Figure 2a. The LSP sensor is subsequently immersed in a series of certified refractive index liquids (Cargille-Sacher
Laboratories Inc, quoted accuracy of ± 0.0002). The low refractive index spectral sensitivity characterization is performed by a series of gas-exposure measurements using the alkane gases; these being methane, ethane, propane and butane.

Each of these gases are delivered separately via a gas manifold to a sealed chamber having a total volume of 3 liters (additional 2 liters for feed and exhaust pipes) as shown in Figure 2b. More details of the characterization apparatus and procedure are given in the Supporting Information section.

![Figure 2](image)

**Figure 2.** Schematic experimental apparatus used to characterize the spectral response of LSP. a) Measurement facilities for liquid environment characterization. b) Experimental setup under pure gas condition. Note: an optimized maximum optical strength LSP resonance in the transmission spectrum was set as the starting point from a broadband light with controlled polarization.

The typical optical spectral response of the sensing platform based upon the D-shaped fiber to the change of azimuthal polarization angle in air before and after UV-inscription, is shown in **Figure 3**. The maximum optical strength of the LSP resonance is defined as the maximum extinction band in the optical transmission spectra of the sensing platform. Note that before UV-irradiation, the three overlay coating on the D-shaped fiber only supports conventional surface plasmons (SPs), whereas
after the UV-inscription the corrugated nano-structures are capable of supporting LSPs. In our results, the zero azimuthal angle polarization is defined as the angle corresponding to the maximum optical coupling to the SPs, i.e., the minimum transmission optical power. It is known that the dispersion relation of the LSPs is different to that of conventional SPs. Furthermore, that the polarization sensitivity of LSPs is higher than that of conventional SPs. The results in Figure 3 show almost an order of magnitude increase in polarization sensitivity for the LSPs compared to the conventional SPs, from 1.0 nm/degree to 7.3 nm/degree and the corresponding optical strength sensitivity is greatly enhanced, from 0.7 dB/degree to 5.3 dB/degree, following the UV processing. We observe that when the azimuthal polarization angle is varied from 40º to 170º, both spectral and optical strength sensitivity is low; this is regardless of UV-laser processing, see the unshaded region of Figure 3.

**Figure 3.** Typical optical spectral response of the surface plasmon with regard to polarization before and after UV-processing. a) The spectral response of conventional SP. b) The spectral response of LSP. Note: shaded areas are high sensitivity regions.
The RI spectral sensitivity of the sensing platforms yields higher sensitivities for gaseous and liquid regimes after UV-laser processing. This is expected due to the change in the surface topology from a planar metal overlay to an array of nano-antennae. Furthermore, maximum RI sensitivities for the two metals used for the overlay were at different RI regimes, which is expected due to their different optical properties. Figure 4a to 4h show the response in the aqueous and gaseous RI regime for two types of metal overlay, i.e. platinum and gold, the spectral wavelength shifts and thus the spectral sensitivity are determined by using a centroid method, more details given in Supporting Information section.

**Figure 4.** Typical RI spectral shifts for two sensing platforms consisting of Ge-SiO2-Pt (GSP) and Ge-SiO2-Au (GSA) multi-layer coatings in the aqueous and gaseous regime. a) Experimentally recorded spectra of the GSP before and b) after UV-laser processing. c) The obtained spectral sensitivity and optical strength of the GSP platform before and after UV-laser processing. d) Experimentally recorded spectra of the GSA platform before and e) after UV-laser processing. f) The obtained spectral sensitivity and optical strength of the GSA platform before and after UV-laser processing.
Typical RI spectral responses for Ge-SiO2-Pt (GSP) in the alkane gases regime. g) Experimentally recorded transmission spectra and (h) the obtained spectral index sensitivity.

The surface topology of the sensing platform dramatically modifies the plasmonic spectral behavior and sensitivity in response to changes in the surrounding RI. By altering the composition of the supporting metallic thin film, we can manipulate the surrounding index range in which a plasmon can be generated. For instance, in the aqueous regime, the variation of the transmission spectra for the platinum metal overlay coating as a function of surrounding RI, before and after UV-laser processing, are shown in Figure 4a and 4b, respectively. The spectral sensitivity extracted from these spectra increases slightly from $(2 ~ 3) \times 10^3$ nm/RIU to $(4 ~ 6) \times 10^3$ nm/RIU (Figure 4c) upon UV-laser processing. To obtain the maximum spectral sensitivity in the aqueous regime, the platinum metal overlay coating is replaced with gold due to the fact that optical properties of Au deliver a higher spectral sensitivity, as ascertained from the modeling. Figure 4d and 4e show how the transmission spectrum of the surface plasmon sensing platform changes using the gold overlay platform with respect to the surrounding RI. Similarly, Figure 4f shows the spectral response: wavelength shift and change in optical strength of the gold overlay device, before and after UV processing. Remarkably, the gold overlay produces a significant increase in sensitivity from an initial value around 100 nm/RIU to as much as $15 \times 10^3$ nm/RIU following UV processing. This value is among the highest sensitivities reported in literatures in the aqueous index regime.$^{[5,22,27]}$

The same experimental characterization was performed on devices for other applications and reported elsewhere.$^{[5,22-28]}$ A dramatic RI sensitivity increase, however, can be found in the gas regime from a typical value of $\sim 300$ nm/RIU to $(4$ to $30) \times 10^3$ nm/RIU after UV processing,$^{[25]}$ which has been utilized in detecting CO$_2$ and CH$_4$ via monitoring the changes in permittivity of carbon nanotubes and zinc oxide, respectively, due to oxidization/reduction chemical reactions.$^{[25,28]}$ An example of our plasmonic sensing platform operating in the gas regime, after UV processing, is shown in Figure 4g and 4h using the alkane gases. This yields typical sensitivity values of $11 \times 10^3$ nm/RIU.

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nm/RIU and 5.5×10³ dB/RIU with spectral noise having a standard deviation of \( \Delta \lambda_{\text{error}} = 0.12 \) nm and 0.1 dB. There are two important parameters that can be deduced from these results, the resolution defined as \( \Delta \lambda_{\text{error}}/(\text{refractive index sensitivity}; S_{\lambda B}) \) and the limit of detection (LOD). Note that LOD is dependent on the interrogation scheme, the light source spectral width, and the noise bandwidth of the measurement system. The LOD can be expressed in terms of standard deviation of the sensor noise output \( \Delta \lambda_{\text{error}} \), bulk sensitivity defined as \( S_{\lambda B} = \Delta \lambda / \Delta n \), and bandwidth of the spectral transmission feature of the surface plasmons resonance \( \Delta \lambda_{\text{feature}} \). Furthermore, there are 1000 discrete spectral data points per spectral scan (using an Agilent optical spectrum analyzer) across the resonant peak which yields a LOD=\( \sqrt{(2\cdot(\Delta \lambda_{\text{feature}}+\Delta \lambda_{\text{error}}))/1000})S_{\lambda B} \). The full-width at half-maximum of bandwidth resonances for the results given above is 34 nm. Thus yielding a gas index resolution of 2.2 ×10⁻⁵ RIU and 9.1×10⁻⁶ RIU with LOD of 4.8 ×10⁻⁵ RIU and 2.4 ×10⁻⁵ RIU for intensity and wavelength, respectively. Higher sensitivities are obtained using the same fabrication process for plasmonic sensing platform with a top-layer of platinum/zinc oxide yielding a wavelength spectral RI sensitivity of 1.5×10⁵ nm/RIU and spectral bandwidth of 70 nm and with 0.06 nm standard deviation of noise yielding a maximum index resolution of 4.0×10⁻⁷ RIU in the gaseous regime.[28]

3. Modeling

To understand the underlying mechanism responsible for the experimental observations and to explain the ultra-high spectral sensitivities with respect to the refractive index of surrounding medium, two theoretical approaches were used. Firstly, via a combination of a conventional and well established analytical model to predict the extinction spectrum of the constituent metal composite components of the nano-antenna as a function of wavelength[29] along with the effective dielectric medium, the Bruggeman effective medium approach[30] to estimate of their effective dielectric constants. This analytical modeling approach when used with spatial measurements of the constituent components of the nano-antenna that are referred to as “nano-blocks” yields reasonable agreement with
the polarization dependence and the spectral tunability of the LSPs excitation resonances in the transmission spectrum of the sensing platform observed experimentally, see Figure 5. The assumptions and approximation used in the analytical modeling approach are given in the *supplementary information*. In Figure 5a, shows the excitation of the LSPs given by the differing major and minor axes dimensions of the nano-blocks; Y and X. The definition of these two parameters can be seen in Figure 1b. The weakness of the analytical approach was in the prediction of spectral index sensitivities of the LSPs are too small by at least an order of magnitude, an example is shown in Figure 5c. This method yielding sensitivities from 600 to 800 nm/RIU. In an attempt to replicate the observed experimental the ultra-high spectral index sensitivities a numerical modeling approach as established.

**Figure 5.** Analytical modeling of the LSP spectral responses. (a) Typical calculated spectral shifts of the extinction of the LSP as a function of the spatial geometry and size of the nano-blocks, using the measured variation in the minor and major axes, for a Ge-SiO2-Au tri-layer with a surrounding index of 1. (b) Typical experimentally measured plasmon resonances, produced by varying the polarization of illuminating irradiance. (c) Typical calculated RI sensitivity using minor and major axis values of 290 nm and 150 nm, respectively.

To theoretically replicate the experimentally observed index spectral sensitivities a second modeling approach is used. A Finite Element Method (FEM) model was constructed consisting of twelve nano-antennas (total length of 6 µm) representing a small section of our sensing platform. The FEM...
is based upon the commercial software package COMSOL Multiphysics. The direction of the illuminating light is parallel to the stacking direction of this array, the excitation port being on the left-hand side with mesh size varying from 1.21×10^{10} to 6.04×10^{8} with a maximum element growth rate of 1.17 and full vector solution. This model is evaluated over a range of wavelengths from 1250 nm to 1750 nm, where the wavelength dependent optical constants of the materials are incorporated for gold, silicon dioxide and germanium, according to the literature.\textsuperscript{[31]} Figure 6 shows an example of the electric field $E_x$ and magnetic field $H_z$ generated in the simulations. Firstly, the amplitude of the E-field is shown, in Figure 6a, this shows that E-fields overlap to adjacent nano-antenna. This overlap will affect the excitation of the electrons in each nano-antenna, thus creating coupling between the surface plasmons. This coupling to adjacent nano-antennae is more pronounced in the x-component of the E-field and that there is a collective coupling across the array, see Figure 6b. Furthermore, the majority of the $H_z$ field associated with SP lies above the surface of the coating, see Figure 6c. Therefore, the propagation /interaction length of the SP has less dependency upon the roughness of the surface,\textsuperscript{[32,33]} producing a long interaction length with the surrounding medium. Effectively, this antenna array, when optically irradiated in the infrared, creates infrared LSPs that are coupled and yielding an effective conjoint surface plasmon with an interaction length spanning over the entire array.
Figure 6. Numerical modeling of a section of the nano-antennae array generated conjoined LSP. FEM model showing the three major components, a) the overall amplitude of electric field, b) the x-component of the electric field c) the z-component of the magnetic field at a wavelength of 1550nm with a surrounding RI of 1.36. The physical dimensions are those measured experimentally using atomic force microscopy. d) Calculated real part of refractive index for the dispersion relationship of the various orders of LSPs (1, 2, 3, 5, 11, 13, 18, 23). e) Zoom-in plot for the 4 higher orders. f) Real part of the effective index of the surface plasmons, as a function of the surrounding

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medium’s refractive index. g) Theoretical estimation of the spectral sensitivity of the surface plasmons, as a function of plasmon order.

There are two factors that can be evaluated from the FEM numerical model that can be used to predict the ultra-high spectral index sensitivities that have been found experimentally (that yield ultra-low detection limits when used in conjunction with a bio-recognition molecule).\textsuperscript{5,23} Firstly, the dispersion of the LSPs over the wavelength range of interest from 1250 nm to 1750 nm is calculated from the results of FEM model run at a series of wavelength from 1250nm to 1750nm at increments of 50nm. From this series of FEM simulations the effective propagation constant of surface plasmons is extracted at the various wavelength yielding $\Delta n_{LSR}/\Delta \lambda$. The authors would like to point out that the optical constants of the materials used in the FEM simulations at the various wavelengths came from the open literature.\textsuperscript{31} The results from the series of runs of the FEM model are shown in Figure 6d and 6e. Secondly, we show the effective propagation constant of surface plasmons as a function of the surrounding RI ($\Delta n_{LSR}/\Delta n_s$) at a specific wavelength $\lambda_t$, again, a series of FEM simulations were run over various refractive indices from 1.30 to 1.39 at all the wavelengths of interest; from 1250nm to 1750nm; the example is shown in Figure 6f at a wavelength of 1550nm.

The first approximation for spectral index sensitivity is given by $\left(\Delta \lambda / \Delta n_s \right)|_{\lambda_t} = \left( \Delta n_{LSR}/\Delta \lambda \right) \cdot \left( \Delta n_{LSR}/\Delta n_s \right)|_{\lambda_t}$ for each of the individual surface plasmons under the assumption that the dispersion relationship is linear around wavelength $\lambda_t$. Note that this basic model serves to estimate an overall magnitude for the anticipated sensitivity. Our numerically calculated sensitivities plotted in Figure 6g show a reasonable qualitative agreement with the experimental results for the mid-range values LSP order 11 to 13, with values ranging between $10^3$ to $10^4$ nm/RIU.

To understand the physical mechanism that creates these ultra-high spectral index sensitivities observed experimentally and the results obtained from the FEM numerical modeling the propagation length needs to be inspected.

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The FEM mode solutions for the propagation constants $\beta$ are complex, thus describing a mode’s effective wavelength and attenuation as it propagates. The propagation length is defined as the distance a mode travels along the metal/medium interface; along the nano-antenna before decaying to $e^{-1}$ of its original power, this is defined as $L_y = 1/2\text{Im}(\beta)$, assuming the radiative loss are small compared to intrinsic loss. The spatial location/extension of the $E_z$ field and the overall amplitude of the E field spanning the array of nano-antennae producing a conjoint surface plasmon, lies above the surface and thus surface roughness is not significant. Moreover, the spatial location of the associated $H_z$ field, lies above the surface, again, indicating low-loss. These E/H fields are the perpendicular evanescent field to surface plasmon direction of travel along the each nano-antenna. These perpendicular evanescent fields have an interaction length (decaying to $e^{-1}$ of its original power) of 0.97 $\mu$m this distance is greater than the distance between adjacent antennae which is 0.52 $\mu$m. These dimensions with respect to the size and spacing of individual nano-antenna and the overlap with the perpendicular evanescent fields, are visualized in Figure 7a. Furthermore, the “twisted rope like” nano-antennae have a greater variation in the normal to their surface, thus perpendicular evanescent fields produced by an individual antenna occupy a greater volume of the wave vector space that is able to excitation/effect neighboring nano-antenna than a cylindrical-like nano-antenna; this is shown conceptual in Figure 7b.
Figure 7. The physical characteristics of the LSPs calculated from the FEM numerical model and determined experimentally. a) The schematic cross section view of the spatial extension of the evanescent field generated by the surface plasmons. b) conceptual illustration of the generation of evanescent field on the “twisted rope” surface of the nano-antennae c) and d). Effective propagation lengths of conjoined surface plasmon across the array (order 13) obtained from the FEM numerical modelling as a function of refractive index along with a fixed wavelength of 1550nm and as wavelength with a fixed refractive index of 1.36 over the array of nano-antennae respectively. e) Exper-
mentally determined propagation lengths along the nano-antennae for metals gold and platinum as a function refractive index, respectively. f) Coupling coefficients between adjacent evanescent fields on the nano-antennae.

Thus individual perpendicular evanescent fields created by the surface plamson on a nano-antenna will overlap with adjacent nano-antenna that effects the surface plasmon generation and its own perpendicular evanescent fields. Creating a single collective response to an event on the order of a few millimeters, that is, combining a section of the array’s surface plasmons to produce a conjoint/overlay response of a number of individual surface plasmons. An example of the interaction length for as a function of wavelength and as the surrounding refractive index in the infrared spectrum is shown in Figure 7b and 7c. Inspecting Figure 7b and 7c, we note the increasing propagation length with increasing wavelength is the same as conventional SP behavior, but opposite to the variation with increasing RI. In this case, as the ambient surrounding RI increases there is no energy flow increase in the metal due to the fact that the conjoint surface plasmon is above the surface and effectively there's no increase in the damping effect. The numerical results are compared to the experimentally determined propagation lengths of the surface plasmons along the nano-antennae using the inverse proportionality relationship between propagation length and bandwidth of the SPR (Figure 6e). For both metals used yielded propagation lengths of ranging from 0.7 µm to 1.2 µm over the range of RI used in the experiments. These experimental surface plasmon propagation length values are typical for the size of the nano-blocks within each nano-antenna. Moreover, these results are consistent with conventional LSPs having a decreasing propagation length with increasing RI. The interaction length/evanescent field generated by the surface plasmons propagating along the nano-antennae, which spatially extends perpendicularly from the surface of the nano-antennae, can be calculated from the material constants. The two materials form the metal–dielectric interface at a given wavelength, with the RI of the surrounding medium given by

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Where $\varepsilon_i(\lambda)$ is the dielectric constant for either gold or platinum and $n_s(\lambda)$ is the medium’s RI as a function of wavelength. Using the values given in the reference$^{31}$ yielded interaction length/evanescent field with spatial extensions from 0.85 $\mu$m to 0.95 $\mu$m for gold nano-antennae over RI range of 1.3 to 1.38 and 0.48 $\mu$m to 0.63 $\mu$m for platinum nano-antennae over a RI range of 1.0 to 1.35. What this means is that the extension of the perpendicular evanescent field is larger than the separation of the individual nano-antenna, visualized in Figure 7a and Figure 1e. The visualization of the overlap suggests coupling. Therefore, the coupling efficiency between adjacent fields and nano-antennae was investigated for the array at wavelengths range 1250nm to 1750nm. To estimate the coupling coefficients several measured physical attributes of the nano-antennae needs to be used, such as, the spatial dimensions and using the assumption that the significant contribution to the excitation of the surface plasmon and thus the extinction spectrum is caused by irradiance absorption.$^{36}$ Individual nano-antennae are composed of smaller nano-blocks considering each of three axis of nano-blocks dependently the coupling coefficients can be estimated between adjacent nano-antennas given by $C_{abs,i} \approx k \text{Im}[\alpha_i]$. Where $\alpha_i$ is polarizability of the principle axis $i$ and is given by $\alpha_i = 4\pi abc(\varepsilon_m(\lambda) - \varepsilon_s(\lambda))/3L_i(\varepsilon_m(\lambda) - \varepsilon_s(\lambda)) + 3\varepsilon_s(\lambda))$, where $a$, $b$ and $c$ are the values of the principle axis of the nano-antenna, which is assumed to be a cylindrical shape $a = b = 0.11 \mu$m and c = 30 $\mu$m. The permittivity values $\varepsilon_m(\lambda)$ is for the supporting metal of the surface plasmon and $\varepsilon_s(\lambda)$ is the dispersion relationship of the surrounding medium. The parameter $L_i$ is the form factor for the particular axis $i$ with $L_a = \frac{1-\xi^2}{\xi^2}\left[\frac{1}{2\xi}\ln(1 + \xi/1 - \xi) - 1\right]$ and $L_b = L_c = \frac{1}{2}(1 - L_a)$, where the parameter $\xi$ is defined as $\xi = \sqrt{1 - (b/a)^2}$, producing coupling coefficient values from 0.15 $\mu$m$^2$ to 0.42 $\mu$m$^2$ for this plasmonic platform. These are comparable values to other nanostructures with strong coupling,$^{36,37}$ see Figure 7e. Thus, the conjoint plasmon is a type of strongly coupled “collective” surface plasmon. Therefore, as the evanescent field generated by a single nano-antenna is perturbed, the adjacent field is also affected due to the
strong coupling. Thus the perturbation travels across the nano-antenna array, yielding an effective propagation across the array. Furthermore, this mechanism works with an array that has long-range order, from a few hundred micrometers to millimeters, for which part of the array can be seen in Figure 1e. It is known that the spectral sensitivity and wavelength shift are directly related to the degree of overlap integral of the evanescent fields in the sensing volume, which in turn is proportional to the interaction volume.\textsuperscript{[36,37]} Additionally there is also significantly increased interaction of the perpendicular evanescent field of the coupled adjacent surface plasmons. The net effect of the aforementioned three factors is to yield an effective ultra-long propagation length travelling across and perpendicular to the nano-antennae. This leads to the experimentally observed significant increase in spectral sensitivity. Given that the shape and size of the individual elements of a nano-antenna play an important role in the dispersion of the plasmons, the sign of the wavelength shift may be reversed from this model.

4. Discussion & Conclusion

In comparison with the quoted values\textsuperscript{[38]}, our experimentally determined RI spectral sensitivities obtained from our unique sensing platform are amongst the highest in the aqueous index regime (1.36 to 1.38) with sensitivity ranging from 4 to $6\times10^3$ nm/RIU.\textsuperscript{[5,22]} Moreover, the measured values are also amongst the highest in the gaseous index regime (1.0001 to 1.0015), from 5.5 to $15\times10^3$ nm/RIU,\textsuperscript{[25,26,28]} with figure-of-merit varying from 150 to 330.\textsuperscript{[28]} The performance of this LSP sensing platform are compared to similar supporting substrates (optical fibre), see Table 1.
Inspecting Table 1, we observe that for the sensing platform reported here, sensitivities are approximately $3 \times 10^4$ to $1.5 \times 10^5$ nm/RIU in the gaseous regime from 1.0002 to 1.0014 that are ultra-high sensitivities. To make comparable comparisons to alternative sensing platforms one needs to compare similar index regimes. Table 1 compares the aqueous index regime from 1.3 to 1.39, for which observe some of the highest reported sensitivities, approximately $10^4$ nm/RIU [45].

The sensitivities listed in the Table 1 are estimated from the data reported in the research article. Our basic numerical model offers realistic agreement with the experimental observations, offering further insight on the mechanism responsible for the experimental observed ultra-high sensitivities.

The modeling also predicts that when optimized, this platform can offer spectral sensitivities ranging in excess of $10^5$ nm/RIU, in the aqueous index regime. The aforementioned sensitivities can be achieved by further fine tuning the fabrication technique in two ways. Firstly, we require a reduction in the irregularities that can be perceived as “effective roughness” in the array topologies.\cite{32, 33}

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This would improve the repeatability of individual nano-antenna, which in turn improves the coupling of the LSPs. Furthermore, a decrease in this effective roughness would increase the interaction length (perpendicular evanescent field) and thus increase the sensitivity. Secondly, improving the uniformity and controllability of the dimensions of the individual nano-antennae yields greater effective excitation of the higher modes, due to the fact that shape and size of the nano-antenna dominates the excitation of the SPs.\textsuperscript{[48]} When assuming similar standard deviation of noise within the sensor, the scheme yields typical RI resolution of $4.0 \times 10^{-8}$ RIU (by improvements in the interrogation scheme) and higher in the aqueous index regime. Investigations are underway to predict the correct optical illumination requirements and refinement of the shape of the nano-antenna to have an optimized coupling efficiency to higher order SPs, thereby yielding even higher sensitivities. The flexibility of this direct-write fabrication procedure (on any substrates with flat surfaces) offers the opportunity to produce more complex nano-pattern surface structures.

In conclusion, we have proposed and demonstrated a new mode of operation for surface plasmons to create a \textit{collective state of a number} of LSP or an \textit{effective conjoint surface plasmon} spanning over a section of the sensing array. We have shown theoretically and experimentally that there is a significant increase the interaction length (perpendicular evanescent field or referred to as the scattered radiation field) of LSP due to strong coupling between adjacent nano-antennae. In addition, the “\textit{conjoint surface plasmon mode}” exists due to the close proximity of other nano-antennae and the surface topologies of the “nano-blocks” within each nano-antennae at the wavelength of excitation. These physical attributes of the nano-antennae result in strong coupling between the spatial location of the SP. Furthermore, the fact that nano-antenna arrays have long range ordering and have low effective roughness yielded the ultra-high sensitivities. Furthermore, comparing this mode operation to plasmonic surface lattice resonances\textsuperscript{49}, the resonances are much narrower than the observed LSPs in these experiments. In addition, and more importantly, that the spectral index sensitivity of the plasmonic surface lattice resonances are much less (~400 nm/RIU) which is more than order of magnitude less than the purposed \textit{conjoint surface plasmon}. Moreover, considering
using the near-field or far-field diffractive coupling effects as the mechanism for the observed surface plasmons would produce a narrowing of the bandwidth of the resonance of the surface plasmon which is not observed experimentally. Also the diffractive coupling effect can produce a splitting of the surface plasmon resonances in transmission spectra which isn’t observed in the experiments conducted, examples are shown in Figure 4.

This unique operational mode of SPs has great potential to make direct experimental observations and help answer more fundamental questions on the physical dynamics of proteins and the opportunities to explore the mutual interaction between biological components and surfaces.\textsuperscript{[50]} Such operational mode may also offer the real possibility of many new applications, such as, the experimental real-time study of single bimolecular binding kinetics, detection of ultra-low concentration (below the \textit{fM} level) of proteins and small molecules for the early diagnosis of various diseases.\textsuperscript{[51,52]}

5. **Experimental and Method Section**

**Fabrication of the optical sensing platform**

Initially, the formation of structures via the interaction of the germanium oxides on exposure to UV laser illumination were investigated using planar substrates. A thin film coating of germanium with a thickness of 48 nm was deposited upon a BK7 glass substrate with a thickness of 150 \( \mu \)m. The reason for using a thickness of 48 nm of germanium comes from the previous work\textsuperscript{[39]} and the results have been published elsewhere\textsuperscript{53}. Furthermore, this effect is utilized in the formation of multi-layered, 2-dimensional nano-structured films that support the localized surface plasmons. The multi-layered thin films consisted of three different materials (germanium (48nm), silicon dioxide (48nm) and metal over layer coating of varying thickness (Pt; 28nm), (Au; 32nm), (Ag; 32nm) producing a planar surface. For ease of interrogation of the surface plasmon a D-shaped single mode optical fiber as the optical waveguide and supporting substrate. The D-shaped fibers were fabricated from a standard telecoms optical fiber (SMF28) by mechanically lapping and polishing the optical fiber with the flat area 3 microns from the core/cladding interface (Phoenix Photonics Ltd, UK).
The thin films of germanium and other thin films were deposited using an RF sputtering machine (Nordico 6 inch RF/DC 3 target excitation machine, Nordiko 6, Nordiko Technical Services Limited, Havant, Hampshire, UK).

Secondly, the germanium-coated planar substrates were mounted, aligned and exposed to various intensities of 244 nm laser light. Note that the opto-mechanical arrangement of the apparatus is the same as used for the UV laser inscription of optical fiber gratings\textsuperscript{[54]}. The UV light source is an Argon ion, continuous wave laser (INNOVA Sabre Coherent Inc.) producing 500 mW at 244 nm. The laser beam is focused along the line of travel of the air-bearing stage (using a plano-convex lens with a focal length of 80 mm) and then passed through a phase mask (period of 1.018 µm, a QPS phase mask). The beam is focused perpendicularly to the line of travel of the air-bearing stage (Aerotech Inc.) with further alignment of beam to be constantly focused on the surface of the sample (using an additional plano-convex lens having focal length of 80 mm). A schematic of the coating process to realize the low dimensional nanostructure is shown in Figure 1h.

**Supporting Information**

Supporting Information is available from the Wiley Online Library or from the author.
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Conflict of Interest
The authors declare no conflict of interest

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A highly sensitive localized surface plasmon sensing platform has been reported. By using direct UV writing method, an array of nano-antennae has been formed on the top of an optical waveguide. In contrary to both conventional and localized surface plasmon operational mode, a novel ‘conjoint surface plasmon’ mechanism has been identified.