STAR FORMATION IN TWO LUMINOUS SPIRAL GALAXIES

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ABSTRACT

We examined star formation in two very luminous ($M_V = -22$ to $-23$) Sc-type spiral galaxies, NGC 801 and UGC 2885, using ultra-deep Hα images. We combine these Hα images with $UBV$ and Two-Micron All-Sky Survey $JHK$ images and H1 maps to explore the star formation characteristics of disk galaxies at high luminosity. Hα traces star formation in these galaxies to 4–6 disk scale lengths, but the lack of detection of Hα further out is likely due to the loss of Lyman continuum photons. Considering gravitational instabilities alone, we find that the gas and stars in the outer regions are marginally stable in an average sense, but considering dissipative gas and radial and azimuthal forcing, the outer regions are marginally unstable to forming spiral arms. Star formation is taking place in spiral arms, which are regions of locally higher gas densities. Furthermore, we have traced smooth exponential stellar disks over four magnitudes in $V$-band surface brightness and 4–6 disk scale lengths, in spite of a highly variable gravitational instability parameter. Thus, gravitational instability thresholds do not seem relevant to the stellar disk. One possibility for creating an exponential disk is that the molecular cloud densities and star formation rates have exponential profiles and this fact forces the stellar disk to build up such a profile. Another possibility is that the stellar disk is continuously adjusted to an exponential shape regardless of the star formation profile, for example, through global dynamical processes that scatter stars. However, such scattering processes are only known to operate in spiral systems, in which case they cannot explain the same dilemma of smooth exponential disks observed in dwarf irregular galaxies.

Key words: galaxies: individual (NGC 801, UGC 2885) – galaxies: spiral – galaxies: star formation

Online-only material: supplemental data

1. INTRODUCTION

In the Milky Way, we see that stars form from clouds of molecular H2 and that there is a correlation between the locations of molecular clouds and the newly minted young stars. Presumably, the molecular clouds form from atomic gas, but what are the conditions for clouds to form in a particular region? Star formation in the inner regions of spiral galaxies is usually attributed to gravitational instabilities following Toomre’s (1964) condition for collapse (Quirk 1972; Kennicutt 1989). However, this condition does not explain star formation in the outer parts of spiral galaxies or in dwarf irregular galaxies (dIrr) where the gas appears to be more stable. Furthermore, empirical relationships between gas and star formation (Kennicutt et al. 2007; Bigiel et al. 2008) become less predictive in dwarfs and the outer parts of spirals where the range in star formation rates (SFRs) is large for a given total gas density (Bigiel et al. 2010; Barnes et al. 2012; D. Ficut-Vicas, in preparation).

Yet, stellar disks are traced to extraordinarily large radii, well outside the accompanying gas disks (see, for example, Ferguson et al. 1998; Ferguson & Johnson 2001; Bland-Hawthorn et al. 2005; Carraro et al. 2010; Vlajić et al. 2011; Eufrazio et al. 2013), and young stars are found in these outer disks. Stars younger than <0.5 Gyr are traced to eight disk scale lengths in NGC 2403 (Barker et al. 2012) and 10 inner disk scale lengths in M33 (Grossi et al. 2011). In NGC 7793 (Radburn-Smith et al. 2012), M33 (Grossi et al. 2011), M83 (Bigiel et al. 2010), CIG96 (Espada et al. 2011), several other spiral galaxies (Barnes et al. 2012), and several dIrrs (Hunter et al. 2011), star formation continues in the outer parts down to an H1 column density of a few $M_⊙$ pc$^{-2}$ or less. GALEX has revealed UV-bright stellar complexes in M83 to 7 kpc (Thilker et al. 2005). Even in dwarf galaxies, like the Large Magellanic Cloud, young stars (<a few gigayears old) are found to eight disk scale lengths (Saha et al. 2010).

Here, we discuss star formation in two of the most luminous and massive Sc-type galaxies in the nearby universe (Burstein et al. 1982). These galaxies, NGC 801 and UGC 2885, were originally observed as part of a study of the rotation curves of spirals by Rubin et al. (1980). We obtained extremely deep Hα images of these galaxies in order to trace H1 regions into the outer disk. These data were originally taken for the purpose of extending the optical rotation curves further out into the disk, but here we use them as tracers of star formation. Characteristics of the galaxies are given in Table 1. We combine the Hα data with $UBV$ and Two-Micron All-Sky Survey (2MASS) $JHK$ images to trace the stellar populations and H1 maps that reveal the atomic gas. With these data, we examine the star formation properties of the galaxies. How far out can we trace star-forming regions? How does the star formation activity compare with the density of gas? Are these very luminous galaxies different compared to less luminous spirals, and how do their outer disks compare with low luminosity dwarf galaxies? And, what do the data tell us about the disk assembly of luminous spirals?
Table 1

| Parameter          | NGC 801  | UGC 2885 |
|--------------------|----------|----------|
| \( D \) (Mpc)\(^a\) | 79.4     | 79.1     |
| Center (h m s, deg arcmin arcsec; J2000)\(^b\) | 2:03:45.4 38:15:32 | 3:53:02.5 35:35:22 |
| P.A. (deg)\(^b\) | −28      | 47.5     |
| \( b/a \)\(^c\) | 0.24     | 0.33     |
| Incl (deg)\(^b\) | 82       | 74       |
| \( E(B - V) \)\(^c\) | 0.042    | 0.176    |
| \( E(B - V) \)\(^f\) | 0.18     | 0.15     |
| \( M_V \)\(^d\) | −21.99 ± 0.005 | −22.71 ± 0.007 |
| \( R_{1/2} \) (kpc)\(^f\) | 15.4     | 22.2     |
| \( R_{25} \) (kpc)\(^f\) | 17.3     | 22.2     |
| \( R_D \) (kpc)\(^b\) | 14.14 ± 0.52 | 12.05 ± 0.41 |
| \( \mu_0^V \) (mag arcsec\(^{-2}\))\(^h\) | 23.09 ± 0.14 | 21.26 ± 0.15 |
| \( \log L_{HI} \) (erg s\(^{-1}\))\(^i\) | 41.6     | 41.5     |
| \( \log SFR_{HI} \) (M\(_\odot\) yr\(^{-1}\))\(^j\) | 0.50     | 0.41     |

Notes.

\(^a\) Determined from \( V_{GRS} \), taken from NED and assuming a Hubble constant of 75 km s\(^{-1}\) Mpc\(^{-1}\).

\(^b\) Determined from the V-band image. The inclination assumes an intrinsic \( b/a \) of 0.2.

\(^c\) Foreground reddening \( E(B - V) \) from Schlafly & Finkbeiner (2011). Internal reddening \( E(B - V) \) from Prescott et al. (2007) for star-forming regions.

\(^d\) The FWHM of stars in the H\(_\alpha\) images is about two pixels, and we used the same parameters for surface photometry as were used for the broad-band imaging.

\(^e\) Half-light radius of galaxy in the V-band, not corrected for extinction.

\(^f\) Radius of the galaxy at a B-band isophote of 25 mag arcsec\(^{-2}\) before the extinction correction was applied.

\(^g\) Disk scale length determined from the fit to the outer disk V-band surface photometry.

\(^h\) Central surface brightness of the stellar disk from the fit to the outer disk V-band surface photometry.

\(^i\) Integrated H\(_\alpha\) luminosity, corrected for extinction using the value appropriate for \( R_{1/2} \). This value has also been corrected for [N\(_II\)] emission in the filter bandpass (see Section 3.3.1).

\(^j\) Integrated SFR determined from \( L_{HI} \) using the formula of Kennicutt (1998; see Section 3.3.3).

2. OBSERVATIONS AND DATA

2.1. H\(_\alpha\) Imaging

Deep H\(_\alpha\) images were obtained 2007 November 6–12 using the T2KB 2048 × 2048 direct imaging CCD on the 2.1 m telescope at Kitt Peak National Observatory (KPNO). For the on-band filter, we used KPNO #1495, which has a passband center at 6691 Å and a FWHM of 78 Å. We used filter #1564 for the off-band (stellar continuum). The off-band filter is centered at 6618 Å with a FWHM of 74 Å. The pixel scale was 0.304 pixel\(^{-1}\) for a field of view of 10.4. We used observations of the flat-field screen in the dome to correct for pixel-to-pixel variations. We also observed spectrophotometric standard stars at several airmasses to correct for extinction by Earth’s atmosphere and to transform counts in the H\(_\alpha\) images to erg s\(^{-1}\) cm\(^{-2}\). The FWHM of stars on the H\(_\alpha\) images are 1′.5 for NGC 801 and 1′.3 for UGC 2885.

For the galaxies, the observing sequence was on-band, H\(_\alpha\), H\(_\beta\), off-band, H\(_\alpha\), H\(_\beta\), off-band, and so forth. Each exposure was 1800 s. There were 24 H\(_\alpha\) images of NGC 801 and 28 of UGC 2885 for a total on-band exposure time of 12 and 14 hr, respectively. All images were shifted and scaled to match one of the H\(_\alpha\) images for each galaxy. The off-band images were also shifted and scaled to the on-band image in order to subtract the stellar continuum. The final H\(_\alpha\) image of NGC 801 has a stellar FWHM of 1′.4, and that of UGC 2885 has a stellar FWHM of 1′.3. The H\(_\alpha\) image was geometrically transformed to match the scale and orientation of the V-band image so that we could use the same parameters for surface photometry as were used for the broad-band imaging.

The rms in the sky-subtracted, edited H\(_\alpha\) images is (3–4) × 10\(^{-18}\) erg s\(^{-1}\) cm\(^{-2}\). Thus, the rms includes the sky-subtraction and residuals due to editing foreground stars. This rms translates to about 3 × 10\(^{36}\) erg s\(^{-1}\) pixel\(^{-1}\) at the distance of these galaxies. The FWHM of stars in the H\(_\alpha\) images is about two pixels, and the area covered is about three pixels. Thus, an unresolved H\(_\alpha\) region at a level of one rms would have a luminosity of about 9 × 10\(^{36}\) erg s\(^{-1}\), approximately one Orion nebula (Kennicutt 1984).

2.2. UBV Imaging

UBV images of NGC 801 and UGC 2885 were obtained 2010 December 1 and 27–28 with an e2v 2048 × 2048 CCD on the Lowell 1.1 m Hall telescope. The CCD was binned 2×2 for a pixel scale of 0.74. Exposure times were 600 s in \( V \), 1200 s in \( B \), and 1800 s in \( U \). We obtained 10/6/4 exposures in \( V/B/U \) of NGC 801 for total exposure times of 1.7/2.0/2.0 hr, respectively. For UGC 2885 we have 10/7/6 exposures in \( V/B/U \) for total exposure times of 1.7/2.3/3.0 hr, respectively. We used observations of the twilight sky to remove pixel-to-pixel variations across the CCD. We also observed Landolt (1992) standard stars for photometric calibrations. The rms in
the $U$-band calibration is 0.042 mag, for $B$ it is 0.036 mag, and for $V$ it is 0.028 mag. Stars in the final $V$-band image of NGC 801 have a FWHM of 1.9 and stars in the UGC 2885 image have a FWHM of 2.4.

All of the images in a given filter were aligned, scaled, and averaged to produce a single final image. The $B$-band image was also shifted to match the $V$-band image and the $U$-band was geometrically transformed to match the $V$-band image. Foreground stars and background objects were edited from the images and the non-galaxy portion of the CCD images were fit to determine the two-dimensional background using MSFURFIT in the Image Reduction and Analysis Facility (IRAF). The background was subtracted from the image to produce a sky-subtracted image ready for surface photometry. The center of the galaxy, the position angle (P.A.) of its major axis, and its minor-to-major axis ratio $b/a$ were measured from an outer isophote in the $V$-band image. The center of the galaxy was determined from a radial profile of the nucleus/bulge.

2.3. JHK Imaging

We obtained $JHK$ images of the galaxies from the 2MASS online archives of the All-Sky Release Survey Atlas. Before performing surface photometry, we geometrically transformed the $JHK$ images to match the scale and orientation of the $V$-band image, and, as for the other images, edited non-galaxy objects from the image, fit the two-dimensional background, and subtracted it from the images. The FWHMs of stars in the frames were $2^{′}.4$–$2^{′}.5$ in the NGC 801 images and $2^{′}.7$–$2^{′}.8$ in the UGC 2885 images. The 2MASS images come with calibration information in their headers. These images are not very deep, but they give us the $JHK$ colors of the central regions of the galaxies.

We also examined the Spitzer $3.6$ μm images of these galaxies, but the field of view was too small to allow adequate sky subtraction. Hence, the $3.6$ μm photometry was unreliable.

2.4. $H\,\text{I}$-line Data

$H\,\text{I}$-line data were available for both galaxies from the archives of the Westerbork Synthesis Radio Telescope (WSRT). NGC 801 was observed as part of the Westerbork Observations of Neutral Hydrogen in Irregular and Spiral Galaxies (WHISP; see van der Hulst et al. 2001) project and the data were provided to us. The beam size is $16^{′}.1 \times 27^{′}.0$, and the channel separation and spectral resolution is $8.25$ km s$^{-1}$. The map cubes are $512 \times 512$ pixels and each pixel is $5^{′}.0$. The rms noise in a channel map of the data cube is $0.73$ mJy beam$^{-1}$. From the data cube, we determine a total flux of $20.96$ Jy km s$^{-1}$, corresponding to an $H\,\text{I}$ mass of $3.0 \times 10^{10}$ $M_{\odot}$. This mass is similar to the $H\,\text{I}$ mass of $2.6 \times 10^{10}$ $M_{\odot}$, corrected for distance, given by the WHISP project (http://www.astro.rug.nl/~whisp/).

UGC 2885 was observed with the WSRT in 2004 in two runs with a total on-source integration time of 24 hr. The total bandwidth was 10 MHz with a number of 1024 channels, centered on the $H\,\text{I}$ line of UGC 2885. We used two parallel-handled polarization products without online Hanning smoothing. The data underwent a standard data reduction with the Miriad software package (Sault et al. 1995). The data were flagged, and a primary bandpass calibration was applied. After that, an iterative self-calibration on the continuum image was performed to correct the frequency-independent gains. The data were Hanning-smoothed, continuum-subtracted, gridded and inverted using a set of different weighting schemes, and subsequently deconvolved employing the CLEAN algorithm. For the CLEAN algorithm, we used an iterative approach in which we successively decreased the cutoff level and increased “clean regions,” restricting CLEAN to certain areas in the single planes of the cubes. For this study, a data cube employing a Robust weighting of 0.0 without averaging in frequency was found to be most suitable. The resulting spatial resolution is $22^{′}.3$–$13^{′}.6$ (half-power beam width), the channel width is $2.06$ km s$^{-1}$, and the rms noise is $0.63$ mJy beam$^{-1}$. The adopted data cube has a size of $256 \times 256$ pixels and a pixel size of $4^{′}.0$. From this data cube, we determined the total $H\,\text{I}$ flux of UGC 2885 to be $28.3$ Jy km s$^{-1}$, which corresponds to an $H\,\text{I}$ mass of $4.2 \times 10^{10}$ $M_{\odot}$.

Note that there is another galaxy in the field of view of the NGC 801 map. The galaxy, NGC 797, to the southwest of NGC 801, has a recessional velocity that is $110$ km s$^{-1}$ smaller than the recessional velocity of NGC 801. The two galaxies are $215$ kpc apart at a distance of $79.4$ Mpc. NGC 797 is classed as an SAB(s)a by de Vaucouleurs et al. (1991). The integrated $H\,\text{I}$ map showing both galaxies is displayed in Figure 1. From here on, only the region immediately around NGC 801 will be shown.

3. ANALYSIS

3.1. Surface Photometry

The $V$-band, $H\alpha$, and integrated $H\,\text{I}$ images of NGC 801 and UGC 2885 are shown in Figures 2 and 3. Both galaxies are seen fairly edge-on; their inclinations are $74^{°}$ and $82^{°}$, respectively.

\footnote{IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.}
We performed azimuthally averaged surface photometry on the $UBVJHK$ and $H\alpha$ images using ELLIPSE in IRAF. We began with the edited, sky-subtracted images, all geometrically transformed to match the scale and orientation of the $V$-band image, and used the parameters derived from the $V$-band image to define the ellipse shape and orientation (see Table 1). We held the center, P.A. of the major axis, and ellipticity of successive ellipses constant and used a step size of 14".8 for the semi-major axis. The annular surface photometry was determined by subtracting two adjacent ellipses and dividing by the area in the annulus.

Although we edited the images of foreground and background objects, there were some artifacts from nearby bright stars or fainter stars within the galaxy image that were masked. UGC 2885, in particular, has a bright star to the northeast of the galaxy center, so much of that half of the galaxy had to be masked. Masked regions were replaced with the average photometry in the annulus. The azimuthally averaged surface photometry, not corrected for reddening, is shown in Figures 4 and 5.

Similar to the stellar photometry, we determined the $HI$ surface densities from the integrated $HI$ maps using the Groningen Image Processing System (Vogelaar & Terlouw 2001). The ellipse parameters and step size were the same as those for the optical and near-IR images.

3.2. Extinction and Reddening

Correcting the surface photometry for extinction due to dust includes foreground reddening due to the Milky Way $E(B-V)_f$ and reddening internal to the galaxy $E(B-V)_i$. The total reddening $E(B-V)$ is the sum of these two components. For $E(B-V)_f$, we use the values given in the NASA/IPAC Extragalactic Database (NED) for the recalibration of the Schlegel et al. (1998) values by Schlafly & Finkbeiner (2011). The $E(B-V)_f$ values are given in Table 1. To correct for

Figure 2. Images of NGC 801. All images show the same field of view. Upper left: $V$-band shown in false-color as the logarithm in order to allow inner details to be seen. Upper right: $H\alpha$ image with stellar continuum subtracted to leave only nebular emission. Lower left: integrated $HI$ map in false-color with contours superposed. The beam size is 16".1 $\times$ 27".0. Lower right: $H\alpha$ image with integrated $HI$ contours superposed. The contours begin at 4.2 $\times$ 10$^{19}$ cm$^{-2}$ and increase in steps of 5.2 $\times$ 10$^{19}$ cm$^{-2}$. The locations of distant $HI$ regions are marked.
the foreground extinction, we use the Cardelli et al. (1989) extinction law that was determined for the Milky Way:

$$A_{V,i} = 3.1 \times E(B-V)_f,$$
$$E(U-B)_f = 0.69 \times E(B-V)_f,$$
$$E(J-H)_f = 0.27 \times E(B-V)_f,$$
$$E(H-K)_f = 0.23 \times E(B-V)_f,$$
$$E(V-J)_f = 2.14 \times E(B-V)_f.$$

We have no direct measurements of $E(B-V)_i$ for our galaxies, so we estimate values from observations of other galaxies in the literature. One complication is that extinction may be a function of galaxy luminosity (Wang & Heckman 1996) and in spirals it changes with radius, decreasing toward the outer disk (Huizinga & van Albada 1992). We began with the work of Prescott et al. (2007), a study of star-forming regions in galaxies observed as part of the Spitzer Infrared Nearby Galaxies Survey (SINGS). Fitting their Figure 12, we have that the internal $V$-band extinction of star-forming nebulae is

$$\log A_{V,i}^{H_\alpha} = 0.45 - 0.67 \times (R/R_{25}).$$

The Prescott et al. (2007) data only extend to $R/R_{25} = 1.4$, so we extrapolate this value to $R/R_{25} = 3$ for our data. The values from Prescott et al. (2007) were determined for star-forming regions, and are appropriate for our $H\alpha$ photometry of H\textsc{ii} regions. We adopt $A_{V,i}^{H_\alpha} = 0.82 A_{V,i}^{H_\alpha}$, which Prescott et al. took from Calzetti et al. (2000).

We expect field stars to suffer from less extinction than star-forming regions in dense clouds, and so for the field stars we turn to the extinction law of Calzetti et al. (1994, 2000). This extinction law was determined specifically for the stellar continuum integrated over large regions in starburst galaxies. Our spirals are not strictly speaking “starburst” systems, but they are actively forming stars. For scaling the extinction law, $E(B-V)_i^*$, we use the observation that the reddening of the stars is related to that of the ionized gas in star-forming regions, on average, as $E(B-V)_i^* = 0.44 \pm 0.03 E(B-V)_i^{H\alpha}$ (Calzetti

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**Figure 3.** Images of UGC 2885. All images show the same field of view. Upper left: V-band shown in false-color as the logarithm in order to allow inner details to be seen. Upper right: H\textalpha image with stellar continuum subtracted to leave only nebular emission. Artifacts due to poor subtraction of saturated stars are marked. Lower left: integrated H\textit{i} map in false-color with contours superposed. The beam size is $22.2'\times13.58'$. Lower right: H\textalpha image with integrated H\textit{i} contours superposed. The contours begin at $4.2 \times 10^{19}$ cm$^{-2}$ and increase in steps of $5.2 \times 10^{20}$ cm$^{-2}$, as for NGC 801. The location of distant H\textsc{ii} regions are marked.
There is no emission in the third to last annulus (60 kpc radius) in the profile. The photometry has not been corrected for reddening.

Figure 4. Surface photometry and colors of NGC 801 from UBVJHK and Hα images. The photometry has not been corrected for reddening. $R_{25}$ is the radius of the galaxy at the $B$-band surface brightness of 25 mag arcsec$^{-2}$.

(Supplemental data for this figure are available in the online journal.)

Figure 5. Surface photometry and colors of UGC 2885 from UBVJHK and Hα images. There is no emission in the third to last annulus (60 kpc radius) in the azimuthally average Hα profile. The photometry has not been corrected for reddening. $R_{25}$ is the radius of the galaxy at the $B$-band surface brightness of 25 mag arcsec$^{-2}$.

(Supplemental data for this figure are available in the online journal.)

Figure 6. Internal reddening $E(B-V)$ as a function of radius, adopted and extrapolated from Prescott et al. (2007). This reddening is appropriate for H II regions, and hence our Hα observations. For the field stars, we adopt a scaling factor of 0.44 times $E(B-V)$, for the H II regions (Calzetti 1997). Thus, we use the $A_{V,H}^\text{II}$ determined from Prescott et al. (2007) for the ionized gas, divide that by $R_V = 4.05$ (Calzetti et al. 2000) to obtain $E(B-V)_H^\text{II}$, and multiply that by 0.44 to obtain $E(B-V)_V^\text{II}$. The Calzetti et al. extinction law can then be used to correct the photometry of the stellar populations in the various broad-band filters:

$$A_{V,J}^\ast = 4.05 \times E(B-V)_V^\ast, \quad E(U-B)_V^\ast = 0.95 \times E(B-V)_V^\ast, \quad E(J-H)_V^\ast = 0.57 \times E(B-V)_V^\ast, \quad E(H-K)_V^\ast = 0.43 \times E(B-V)_V^\ast, \quad \text{and} \quad E(V-J)_V^\ast = 0.97 \times E(B-V)_V^\ast.$$

$E(B-V)_V^\ast$ and $E(B-V)_H^\ast$ are shown as a function of radius in Figure 6. From these relations, we have that $E(B-V)_V^\ast$ is $\sim$0.7 mag in the centers of the galaxies and drops to 0.01 at $R/R_{25} = 3$.

For integrated photometry, we use the $E(B-V)_V^\ast$ and $E(B-V)_H^\ast$ appropriate to the $V$-band half-light radius $R_{1/2}$ of the galaxy. $R_{1/2}$ was determined before any reddening correction was applied. These values are given in Table 1.

Figure 7 shows the integrated $UBV$ and $JHK$ colors of NGC 801 and UGC 2885 in color–color diagrams. We also show $(U-B)_0$ and $(B-V)_0$ averages by spiral morphological type from de Vaucouleurs & de Vaucouleurs (1972), and the uncertainties are the spread in colors for each type. The arrow shows the reddening vector for $E(B-V) = 0.1$. NGC 801 and UGC 2885 are redder than other Sc-type galaxies, comparable instead to Sb-type galaxies. For $(H-K)_0$ versus $(J-H)_0$, we show the average for spiral disks from Holwerda et al. (2005) and the uncertainties are the range of values in the average colors. The arrow is the reddening vector for $E(J-H) = 0.1$. NGC 801 and UGC 2885 are redder than most other spirals in these colors too, but within the range of values seen.

The azimuthally averaged surface photometry, corrected for reddening, is shown in Figures 8 and 9. In the top panel, $\log \Sigma_{H\alpha}$ and $\mu_V$ are plotted as a function of radius. The logarithmic interval is equal to the magnitude interval that is plotted, so that the shapes of the profiles of the two quantities $\log \Sigma_{H\alpha}$ and $\mu_V$ can be compared directly.
For NGC 801, the V-band surface photometry $\mu_V$ is high in the center, presumably due to the central bulge. Beyond 20 kpc, $\mu_V$ can be fit with a two-component exponential with an upbending outer part. The inner component fits $R = 20–40$ kpc and the outer component fits $R = 40–60$ kpc, shown in Figure 8 as a dotted line and a solid line, respectively. The inner component is fit with a disk scale length $R_D$ of $10.5 \pm 0.4$ kpc and a central surface brightness $\mu_v^0$ of $22.0 \pm 0.1$ mag arcsec$^{-2}$. A fit to the outer disk yields a disk scale length $R_D$ of $14.1 \pm 0.5$ kpc and a central surface brightness of $23.1 \pm 0.1$ mag arcsec$^{-2}$. The two components cross at a break radius of 39.4 kpc and a surface brightness of 26.1 mag arcsec$^{-2}$. Because we emphasize the outer disk here, we use the disk scale length of the outer surface brightness component.

We see that $\Sigma_{H\alpha}$ drops like $\mu_v$ with radius until a radius of 26 kpc, and then it declines faster. $H\alpha$ ends where the V surface photometry ends. The V-band image is not particularly deep, so it is possible that $\mu_v$ continues to lower surface brightness levels, but the $H\alpha$ exposure is deep and it is unlikely that $H\alpha$ would be detected much further out. In NGC 801, the $(B - V)_0$ and $(U - B)_0$ colors are red in the center and get slightly (~0.15 mag) bluer to a radius of about 25 kpc, approximately the same radius where the $H\alpha$ surface brightness begins to decline faster than $\mu_v$. Beyond that radius, $(B - V)_0$ stays constant within the uncertainties and $(U - B)_0$ gets slightly (~0.16 mag) redder. There are only two annuli with JHK colors, but they are red and within the uncertainties constant over that limited radius range.

For UGC 2885, there is a small excess of $\mu_v$ in the inner 8.5 kpc, but beyond that we see an exponential disk. The disk scale length is $12.0 \pm 0.4$ kpc and $\mu_v^0$ is $21.3 \pm 0.1$ mag in V. Here, we see that $\Sigma_{H\alpha}$ is low in the center, and then from 8.5 kpc outward it declines with radius like $\mu_v$. $H\alpha$ emission is traced to 74 kpc, similar to $\mu_v$, which is traced to 71 kpc. The colors $(B - V)_0$ and $(U - B)_0$ are red in the center and get bluer (~0.25, 0.23 mag) with radius to 31 kpc. Beyond that radius, the colors stay approximately constant within the uncertainties, although the $(U - B)_0$ color exhibits a 0.1 mag offset to the red. There are only two annuli with JHK colors, but the colors are red in the center, and in $(H - K)_0$ and $(V - J)_0$ the colors are a bit redder in the second annulus compared to the first.
3.3. Determining Star Formation Rates

We use Hα to determine the SFRs in NGC 801 and UGC 2885 using the formula of Kennicutt (1998). However, first we must correct the flux measured in the Hα filter for the contribution by [N ii]λ6548+6583 emission. We must also correct the SFR formula for the metallicity of the stars since the output of ionizing photons changes with metallicity for a given stellar mass.

3.3.1. [N ii] Correction

The Hα filter bandpass includes [N ii]λ6548 and [N ii]λ6584, and we need to subtract the contribution of [N ii] from the total flux in order to derive the pure Hα emission. First, all three emission lines are located on the flat part of the transmission curve of the filter. This fact means that there is no difference in the transmission of the different emission lines, and we need only correct for the intrinsic relative fluxes of the emission lines. Second, from the Hα survey of James et al. (2005), five spirals give a global average ratio Hα/[N ii] of 0.82, where [N ii] is the sum of the emission from λ6548 and λ6583. So, we multiply our Hα fluxes by 0.82 to correct for [N ii] emission.

3.3.2. Metallicity

Spiral galaxies typically exhibit abundance gradients with radius. For NGC 801 and UGC 2885, we adopt M81’s oxygen abundance gradient as given by Patterson et al. (2012): −0.117 ± 0.073 dex R−2. M81 has an integrated M2 of −20.8, so it is less luminous than NGC 801 and UGC 2885 by a factor of 3–6. However, Henry & Worthey (1999) argue that abundance gradients in spirals are independent of the absolute magnitude of the galaxy when the gradient is expressed in terms of radius normalized to R25. We use Patterson’s “KK04” gradient, determined from four data sets, which has the advantage that the oxygen abundance 12+log (O/H) at the center is 9.0. This value is close to the maximum 12+log (O/H) of 8.9 found by Pilyugin et al. (2007) at the centers of luminous (MB ≃ −22.5) spirals. Therefore, we adopted 12 + log (O/H) = 9.0–0.12(R/R25) as the oxygen abundance as a function of radius in our spirals. This relation is shown in Figure 10. 12 + log (O/H) starts at 9.0 in the center and drops to 8.58, 78% solar, at R/R25 = 3.5. We use a solar oxygen abundance of 8.69 (Asplund et al. 2009).

3.3.3. The SFR Formula

To convert ΣHα in units of erg s−1 pc−2, as shown in Figures 8 and 9, to ΣSFR, in units of M⊙ yr−1 kpc−2, we begin with the formula of Kennicutt (1998): SFRHα(M⊙ yr−1) = 7.9 × 10−22 LHα( erg s−1 ). We multiply the Hα surface density by 0.82 to remove [N ii] and then adjust the formula for the deviation of the metallicity from solar, the abundance that Kennicutt used. For the latter, we use the synthesis models of STARBURST99 (Leitherer et al. 1999), with constant SFR and a Salpeter (1955) stellar initial mass function. Their Figure 78, which gives the number of photons below 912 Å, enables us to find the average flux of ionizing photons per second from a stellar population relative to that at solar and so to modify Kennicutt’s Hα formula as a function of Z from twice solar to below solar. The correction factor at twice solar metallicity is 1.18 and at 40% solar is 0.87. We interpolate to determine the correction factor for the metallicity at a given radius. The derived ΣSFR,Hα values for NGC 801 and UGC 2885 are shown in Figure 11.

Integrated SFRs use the oxygen abundance at the half-light radius to determine the SFR formula. For both galaxies, the oxygen abundance at the half-light radius is approximately
where the formula for converting Hα emission in the third to last azimuthally averaged annulus (60 kpc radius); hence, there is a discontinuity in the SFRHα mass in stars. Because the figure is shown in Figure 12. We also compute the current surface density of the stellar mass Σ∗ in units of $M_\odot$ pc$^{-2}$, as shown in Figures 13 and 14.

4. DISCUSSION

4.1. Extent of Hα Emission

The extent of Hα emission in our two galaxies was determined by eye in the continuum-subtracted images. The furthest emission we detected in NGC 801 to the north of the galaxy has a surface brightness of $10 \times 10^{-18} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ arcsec}^{-2}$. In UGC 2885, the faintest region we traced to the southwest has an Hα surface brightness of $5 \times 10^{-18} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ arcsec}^{-2}$. This value represents the faintest surface brightness we could probably identify as a distinct region.

In NGC 801, the Hα disk extends further to the northwest than to the southeast, and the furthest discrete H II region that we can identify is found at a radius of $\sim 55$ kpc. The southeast H II regions only extend to 43 kpc. The local $\Sigma_{\text{H}II}$ is $1 \times 10^{21} \text{ atoms cm}^{-2}$ at the radius of the most distant H II region. This HI column density is integrated along the line of sight for a highly inclined disk. Multiplying by the cosine of the inclination, 82°, to convert to the perpendicular surface density, we get $1.4 \times 10^{20} \text{ cm}^{-2} = 1.5 \ M_\odot \text{ pc}^{-2}$ including He and heavy elements. The outer H II regions in NGC 801 fall along the extensions of spiral arms. That star formation, even in the outer disks of spirals, is generally found associated with spiral arms seems to be a general feature of spiral galaxies (Ferguson et al. 1998; Thilker et al. 2007; Barnes et al. 2012). Outer star formation in dIrr galaxies, by contrast, is not in spiral arms, but in local clumps of high gas surface density (Hunter 1982; Hunter & Gallagher 1986).

On the northeast end of the disk of UGC 2885 there is an arc of H II regions, probably the end of a spiral arm, the tip of which is 68 kpc from the galactic center. The local $\Sigma_{\text{H}II}$ there is $2 \times 10^{21} \text{ atoms cm}^{-2}$, which corresponds to $6.0 \ M_\odot \text{ pc}^{-2}$ after correcting for inclination and heavy elements. On the southwest side of the galaxy, there are two possible faint detached H II regions at 60 kpc and 74 kpc. Off the major axis, there is a region to the southeast of center located at a de-projected...
radius of 74 kpc. These detached regions are located at Σ_II of 8 × 10^{20} atoms cm^{-2} (2.4 M_☉ pc^{-2} face-on).

In Figures 13 and 14, we show the azimuthally averaged Hα-based SFR densities, Σ_{SFR,Hα}, along with Σ_II, as well as the stellar mass surface density Σ_*. We see that the Σ_{SFR,Hα} drops four dex in NGC 801 from the center to a value of 10^{-4} M_☉ yr^{-1} kpc^{-2} at a radius of 60 kpc. In UGC 2885, Σ_{SFR,Hα} drops 1.5 dex to a value of 10^{-3} M_☉ yr^{-1} kpc^{-2} at 54 kpc. These very low Σ_{SFR,Hα} values in the outer disks are comparable to those seen in less luminous Sab- to Sd-type outer disks (Barnes et al. 2012) and in the outer disks (3–5 kpc radius) of dwarf galaxies (Hunter et al. 2011).

Some of the drop in Hα at large radii could be from a loss of Lyman continuum photons from the vicinity of star formation (Beckman et al. 2000; but see Lee et al. 2011; Hunter et al. 2010; Pellegrini et al. 2012). If we re-write the Strömgren relation as

\[ nR_S = (3S/(4\pi R_S\alpha))^{1/2} \]  

(1)

for an ambient density n, Strömgren radius R_S, stellar ionization rate S, and Case B recombination rate α, then the critical column density for trapping Lyman continuum radiation from an O-type star with S = 10^{49} s^{-1}, considering α ∼ 2.6 × 10^{-13} cm^{2} s^{-1} (Osterbrock 1989) and R_S = 100 R_2 pc, is:

\[ nR_{S,\text{crit}} = 1.7 \times 10^{-10} R_2^{-1/2} \text{ cm}^{-2} = 1.9 R_2^{-1/2} M_\odot \text{ pc}^{-2}. \]  

(2)

To consider the possible loss of Lyman continuum photons from a region of star formation, the column density through a critical Strömgren diameter, 2nR_{S,\text{crit}}, should be compared to the local average gas column density measured perpendicular in the disk. Equation (2) suggests that the critical value for trapping is 4 M_☉ pc^{-2} or less for a single O-type star, especially if R_2 gets large in a disk flare. In fact, the most distant H II regions in our galaxies have local Σ_II at about this limit or less. This result suggests we could be missing other H II regions at these galactocentric distances and certainly missing those much further out. As a result, our estimates of SFRs from outer disk Hα should be considered lower limits.

The loss of ionizing radiation at extremely low Σ_II is in addition to the loss studied by Relaño et al. (2012) that is for visible H II regions. These authors found that shell H II regions have lower Hα compared to FUV than compact regions, indicating up to a 25% loss of ionization in the shell phase. If Σ_II is as low as ∼2 M_☉ pc^{-2}, however, then even these visible H II regions should be difficult to see. First, there should be a loss of radiation from the disk because the Strömgren radius is larger than the scale height, which is the condition for the critical disk column density derived above.

Second, the emission from the fully ionized disk itself will be difficult to see because the emission measure is low. This fully ionized emission measure depends on the gas column density and scale height. The scale height is α^2 / π G Σ_{total} for a velocity dispersion σ and a total mass column density in gas and stars Σ_{total}. We assume σ = 10 km s^{-1} and take the total column densities from Figures 13 and 14. For NGC 801 at the outer annulus in the azimuthally averaged surface photometry, R ∼ 60 kpc, Σ_{total} = 0.6 M_☉ pc^{-2}, which gives a scale height of 13.1 kpc. For UGC 2885 at its outer annulus for Hα detection, R ∼ 71 kpc, Σ_{total} ∼ 1.3 M_☉ pc^{-2} and the scale height is 5.7 kpc.

The full disk thicknesses are twice these scale heights. If we take the measured Σ_{gas} = 0.45 M_☉ pc^{-2} at this radius in NGC 801 and correct for Hα and heavy elements, then the average H I density over the full thickness is 0.00052 cm^{-3} and the emission measure would be 0.0069 cm pc if the disk is completely ionized. Similarly, for UGC 2885, where Σ_{gas} = 1.18 M_☉ pc^{-2}, the density and emission measure would be 0.0031 cm^{-3} and 0.11 cm^{6} pc, respectively. Emission measures in Hα convert to Σ_{Hα} as shown in Figures 4, 5, 8, and 9 according to the equation:

\[ Σ_{Hα} (\text{erg s}^{-1} \text{ pc}^{-2}) = 7.7 \times 10^{30} \text{EM (cm}^{6} \text{ pc}), \]  

(3)

so the full-disk emission measures at the outer radii of the H II regions in these two galaxies convert to log-luminosity densities of log Σ_{Hα} = 28.7 for NGC 801 and 29.9 for UGC 2885. In fact, these values are close to the minimum average luminosity densities for Hα at the outer radii of these galaxies (Figures 8 and 9). We conclude again that we are probably missing Hα emission and underestimating the Hα SFR near the edges of these galaxies.

In NGC 801, we see that Σ_{SFR,Hα} decreases with radius in the inner region like the surface density of the stellar mass even though the excess mass in the center is due to the galaxy bulge. Beyond a radius of 25 kpc, Σ_{SFR,Hα} drops faster than Σ_. This type of behavior is seen in other spirals as well (Christlein et al. 2010). However, beyond 25 kpc the H I gas surface density is...
about four times the stellar surface density and they both drop at nearly the same rate as far as our data trace the stars. Beyond our V-band image, the gas continues to decrease gently.

In the center of UGC 2885, there is a dip in the value of $\Sigma_{\text{SFR,He}}$. Beyond about 15 kpc radius, the azimuthally averaged $\Sigma_{\text{SFR,He}}$ falls, more or less, like the surface density of the mass in stars, until 48 kpc. Beyond that radius, $\Sigma_{\text{SFR,He}}$ drops more rapidly than $\Sigma$, until both stars and Hα emission are no longer detected at a radius of 71 kpc. At a radius of about 30 kpc, the Hα and stellar mass surface densities are equal, and beyond that the stellar mass surface density drops more steeply than the gas surface density, which continues to decrease gently, as in NGC 801. This lack of a correlation between outer disk star formation and outer disk gas is also evident in galaxies with large Hα disks studied by Wang et al. (2013) and J. Wang et al. (in preparation).

In NGC 801 and UGC 2885, we trace Hα emission as far out as we trace V-band starlight. However, it is possible that young stars might be detectable in FUV emission even beyond where Hα emission ends, since in outer disks UV light from young massive stars traces recent star formation more easily than Hα emission from nebulae (as discussed above and see, for example, Thilker et al. 2005, 2007; Boissier et al. 2007). Unfortunately, FUV images of these galaxies do not exist.

4.2. Radial Trends in SFRs

In Figure 12 we show the ratio of current ($\lesssim$10 Myr) SFR to the lifetime averaged SFR necessary to form the mass in stars, $\text{SFR}_{\text{He}}/\text{SFR}_{\text{V}}$, over 4–6 disk scale lengths. We find that the ratio is near unity in the central regions of NGC 801, to a radius of 1.8$R_D$. Beyond that in NGC 801 and everywhere in UGC 2885, the current SFR is significantly lower than the lifetime-averaged rate. For NGC 801, the ratio drops to 0.09 at a radius of 4$R_D$. For UGC 2885 the ratio is quite low ($\sim$0.01) in the center, rises to a high value of 0.6 at a radius of 2.6$R_D$, and then drops slowly to a value of 0.07 at a radius of 6$R_D$. Some of the drop in the perceived SFR in the far outer regions could be from a loss of sensitivity to very faint Hα regions there, considering that the Hα column density is comparable to or lower than the critical value (Equation (2)) for trapping ionization in the nearby ambient medium.

In a deep imaging study of five dIrr galaxies, we found a different situation (Hunter et al. 2011). In three of the dwarfs, the ratio of current to lifetime-average SFR was roughly unity at all radii. In the other two galaxies, the ratio was of order 0.1, so the current SFR was low compared to the past average. This low ratio is comparable to the maximum values in NGC 801 and UGC 2885. So, compared to dwarfs, these luminous spirals have formed much more of their stellar mass in the past than they are adding today.

The trends in NGC 801 and UGC 2885 are different from the general relationship seen in some spirals, as well. In a large sample of spirals, Ryder & Dopita (1994) found that the disk scale length in Hα is much longer than that in the V-band, and the V-band scale length is longer than that of the I-band surface photometry. Similarly, Chang et al. (2012) found in one gas-rich spiral that the recent SFR relative to the lifetime average increases as one moved to the outer disk. These types of observations are interpreted as evidence for an inside-out disk assembly model (e.g., Larson 1976; Chiappini et al. 1997; Mo et al. 1998; Naab & Ostriker 2006).

In UGC 2885, the inner part of the galaxy appears to be dominated by older stars while the outer disk is relatively younger, consistent in a general sense with inside-out growth. On the other hand, the current SFR drops relative to the lifetime average beyond a radius of 2.5$R_D$. So, while the outer disk is younger than the central regions overall, the outer disk becomes more and more dominated by older stars with increasing radius. In NGC 801, however, the inner disk exhibits a constant SFR and then the current SFR drops steadily in the outer disk, beyond a radius of 2$R_D$, compared to the lifetime average. This finding implies that the outer disk is relatively older than the inner disk, counter to inside-out disk growth models.

Youchim et al. (2012) also find mixed star formation profiles in a sample of six nearby spirals: half are dominated by an older stellar population beyond a break in the surface brightness profile, which the authors interpret as evidence for radial migration of older stars. Other studies have also found evidence for extended old stellar disks (see, for example, Ferguson & Johnson 2001; Vlajić et al. 2009). The other half of the Youchim et al. sample shows no significant change in the stellar population in the outer disk. Thus, there does not seem to be a universal star formation profile among spirals (see also Roediger et al. 2012).

The decrease in the ratio of current to past star formation in the outer regions of our galaxies, particularly in NGC 801, contradicts our expectation from the lack of a $B-V$ color gradient, which is shown in Figures 8 and 9. We seem to require some radial migration of stars to make the color gradients flat (e.g., Roškar et al. 2008a, 2008b).

4.3. The Toomre Model

Toomre (1964) calculated the dispersion relation of self-gravitating waves in a thin rotating stellar disk and found a minimum velocity dispersion in the radial direction for stability. This critical velocity dispersion has found popular use in star formation models when it is re-written as a critical column density for gas $\Sigma_{\text{crit}}$. If the gas column density is greater than $\Sigma_{\text{crit}}$, then the model suggests star formation is active because of widespread instabilities. To check this model, we calculated $\Sigma_{\text{crit}}$ as a function of radius for our galaxies using the rotation curves in Rubin et al. (1980). $\Sigma_{\text{crit}}$ depends on the rotation curve through the epicyclic frequency $\kappa$: $\Sigma_{\text{crit}} = \kappa^2 g/\pi G$ for a gas velocity dispersion $\sigma_g$. We assume $\sigma_g = 10$ km s$^{-1}$, a typical spiral galaxy gaseous velocity dispersion (Tamburro et al. 2009).

We also assume that the velocity dispersion is independent of radius, although there is evidence that the velocity dispersion is lower in outer spiral disks (Kauffmann & Sancisi 1993; Tamburro et al. 2009). The effect of lowering the velocity dispersion would be to decrease $\Sigma_{\text{crit}}$, making the gas proportionally more unstable to gravitational instabilities. The ratios of the observed $\Sigma_{\text{gas}}$ to $\Sigma_{\text{crit}}$ are shown for our two galaxies in Figure 15.

In the conventional instability model (e.g., Kennicutt 1989), stars should form at a greater rate where $\Sigma_{\text{gas}}/\Sigma_{\text{crit}}$ is higher. This fact is approximately true for our galaxies, too. In both cases, the ratio of the observed $\Sigma_{\text{gas}}$ to $\Sigma_{\text{crit}}$ is low in the center, climbs to a peak at mid-radius, and then drops in the outer disk. The radius at which $\Sigma_{\text{gas}}/\Sigma_{\text{crit}}$ begins to drop rapidly (1.8–2.5$R_D$) is also the same radius at which the current SFR drops relative to the integrated past SFR (Figure 12). However, this pattern is usually found in exponential disks with flat rotation curves, because then $\Sigma_{\text{gas}}/\Sigma_{\text{crit}} \propto R \exp(-R/R_D)$ for a constant velocity dispersion regardless of star formation, and this function has the same general rising and falling shape as the observed profile. The low values of $\Sigma_{\text{gas}}/\Sigma_{\text{crit}}$ in the centers of our galaxies could be from a high $\kappa$, a lack of gas, or the presence of molecules...
that are not included in $\Sigma_{\text{gas}}$. The maximum value of the ratio in NGC 801 is 0.7 and in UGC 2885 it is 0.6. At these peaks, the gas is close to the original Toomre (1964) critical density. However, at the maximum radius where H II regions are detected, the ratio is 0.2 in both NGC 801 and UGC 2885, which is far into the conventionally stable regime (see also the spirals in Barnes et al. 2012).

The low values of $\Sigma_{\text{gas}}/\Sigma_{\text{crit}}$ in the outer regions mean that stars are forming in gas that is sub-critical in the usual sense. This result is similar to the situation in the outer disks of dIrr galaxies, even though the average H I column densities where the last H II regions are found in our spirals are higher than those in the outer disks of dwarfs by a factor of 10 (Hunter et al. 2011). Clearly, it is not the H I column density alone that determines where stars form (but see Bigiel et al. 2010).

We also see no threshold or shift in the SFR at some characteristic $\Sigma_{\text{gas}}/\Sigma_{\text{crit}}$. The underlying stellar disk has a smooth, extended exponential profile, with no significant features at some radius where the SFR or disk instability may be changing properties. If this exponential disk reflects the past history of star formation, then there is no evident threshold.

The stability of galaxy disks is more complicated than what can be captured by this one-dimensional model, however. Stars contribute to the instability, the disk thickness impedes the instability, gas dissipation promotes the instability, and spirals that fragment into self-gravitating clouds can still form in sub-threshold conditions.

A combined gas+star disk is more unstable than a pure gas disk (Toomre 1964; Jog & Solomon 1984). Romeo & Wiegert (2011) suggest an effective $Q_{\text{eff}}$ given by:

$$Q_{\text{eff}} = \left( \frac{W}{T_s Q_s} + \frac{1}{T_g Q_g} \right)^{-1},$$

in the likely case where $T_s Q_s > T_g Q_g$, which means that the stellar disk alone is more stable than the gaseous disk alone. Here, $T = 0.8 + 0.7 \sigma_\|/\sigma_\perp$ is a thickness correction for gas or stars with velocity dispersions $\sigma$ in the perpendicular ($\|\$) or radial ($R$) directions. Romeo and Wiegert suggest $\sigma_\|/\sigma_\perp = 0.6$ for stars and 1 for gas, producing $T_s = 1.22$ and $T_g = 1.5$. Also, $W = 2 \sigma_\|/\sigma_\|^2_{\|} + \sigma_\|^2_{\perp}$. The quantities $T$ and $W$ depend only on the ratios of velocity dispersions, so a decrease with radius in these dispersions will not affect the results of this discussion.

As for the dispersion in $\Sigma_{\text{crit}}$, the values used in $Q_s$, $Q_g$, and $W$ are radial components.

Note that $Q_{\text{eff}} < 1$ becomes the instability condition for a two-fluid thick disk, replacing $Q_s < 1$, or equivalently, $\Sigma_{\text{gas}}/\Sigma_{\text{crit}} > 1$, for the thin disk model discussed above. Thus, we can convert $Q_{\text{eff}}$ to a threshold two-fluid gas column density for thick disks, $\Sigma_{\text{crit,2F, thick}}$, by setting $Q_{\text{eff}} = 1$ in Equation (4).

We write the one-fluid critical value for infinitely thin disks that we have been using as $\Sigma_{\text{crit,1F, thin}} = \kappa_\| \sigma_\|^2_{\|}/(\pi G)$. Then, inverting Equation (4) and substituting for $W$, we obtain:

$$\Sigma_{\text{crit,2F, thick}} = \Sigma_{\text{crit,1F, thin}} T_g \left( \frac{2 \Sigma_{\text{star}} T_g}{1 + \sigma_\|^2_{\|}/\sigma_\|^2_{\perp}} \right).$$

Using the above values for the thickness corrections, $T$, we obtain a ratio of observed gas column density to the critical, two-fluid, thick disk column density

$$\frac{\Sigma_{\text{H}I+\text{He}}}{\Sigma_{\text{crit,2F, thick}}} = \frac{\Sigma_{\text{H}I+\text{He}}}{\Sigma_{\text{H}I+\text{He}}/\Sigma_{\text{crit,1F, thin}}} \times \frac{1.5 - 0.492 T_g}{\Sigma_{\text{crit,1F, thin}}}.$$

where we have assumed $\sigma_\|/\sigma_\perp = 2$. Figures 13 and 14 suggest that in the outer disks of our two spiral galaxies, $\Sigma_{\text{star}} \sim \Sigma_{\text{gas}}/4$, and Figure 15 indicates that $\Sigma_{\text{H}I+\text{He}}/\Sigma_{\text{crit,1F, thin}} \sim 0.2$ or less there. Thus, $\Sigma_{\text{star}}/\Sigma_{\text{crit,1F, thin}} \sim 0.05$, and for this value, the denominator becomes 1.47. Then:

$$\frac{\Sigma_{\text{H}I+\text{He}}}{\Sigma_{\text{crit,2F, thick}}} \sim 0.68 \frac{\Sigma_{\text{H}I+\text{He}}}{\Sigma_{\text{crit,1F, thin}}}.$$

This result means that the two-fluid thick disk is more stable than the one-fluid thin disk considered in Figure 15, primarily because of thickness effects, even with the presence of stars. The outer disk is therefore 30% more stable than indicated in Figure 15.

Energy dissipation changes this picture, however. Two-component star-gas thick disks with turbulent gas dissipation (Elmegreen 2011) are more unstable than two-fluid thick disks that follow the Toomre model, which for gas, assumes an isothermal fluid. For typical conditions in galaxies, instabilities that create star-forming clouds in turbulent gas can occur with average gas column densities as low as 30%–50% of the Romeo & Wiegert (2011) critical value given above. This range assumes that turbulent energy dissipates on timescales between one and two crossing times over the length of the self-gravitational perturbation, and this range furthermore assumes a ratio of velocity dispersions $\sigma_\|/\sigma_\perp$ between one and five. Lower $\sigma_\|/\sigma_\perp$ and faster dissipation relative to a crossing time correspond to lower critical gas column densities in the two-fluid case; i.e., these conditions correspond to greater instability. This factor of two or three increase in the ratio of the observed $\Sigma_{\text{H}I+\text{He}}$ to the threshold column density, now with dissipation included, is still not enough to bring us to an unstable regime in the far outer parts, however.

So far, all of these gravitational instability models apply only to the radial direction, and the instabilities make only rings spaced by the Jeans length. Before a disk becomes this unstable because of radial forcing alone, it becomes unstable to the formation of spiral arms by a combination of radial and azimuthal forcing. Spiral arm formation should always be viewed as the first step in star formation when a disk has shear (which spiral galaxies have but dIrr galaxies do not). Clouds should not be expected to form directly from the

Figure 15. Ratio of H I+He gas surface density to critical gas density predicted by the gravitational instability model of Toomre (1964) vs. radius in units of disk scale length.

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interstellar medium in random places, but they should form as condensations in the spiral arms.

The stability condition for combined radial and azimuthal forcing was written in terms of an effective $Q$ parameter by Lau & Bertin (1978) and Bertin et al. (1989; see also Julian & Toomre 1966):

$$Q_{\text{eff}} = \left( \frac{1}{Q^2} + \frac{J^2 Q^4}{4} \right)^{-1/2},$$

where $J$ is a parameter such that:

$$\frac{J^2 Q^4}{4} = (q_i Q)^2 \left( \frac{2 \Omega}{\kappa} \right)^2 \left( \frac{d \ln \Omega}{d \ln R} \right) \sim 2 (q_i Q)^2,$$

for a rotation rate $\Omega$ and dimensionless azimuthal wavenumber $q_i = 2 \pi \sigma / (\lambda_i \kappa)$ at a wavelength $\lambda_i$. The factor of two in the last expression is for a flat rotation curve. If there are $m$ spiral arms in the azimuthal direction, then $q_i = \sigma m / (\pi \kappa R)$, and if we write $Q = \sigma \kappa / (\pi G \Sigma)$ in the usual way, then $q_i Q = \sigma^2 m / (\pi G \Sigma R) \sim H_m / R$ for a scale height $H$. Condition (8) was applied to disk stability and star formation by Zasov & Lau & Bertin (1978) and Bertin et al. (1989; see also Julian & Toomre 1966):

$$\frac{J^2 Q^4}{4} = (q_i Q)^2 \left( \frac{2 \Omega}{\kappa} \right)^2 \left( \frac{d \ln \Omega}{d \ln R} \right) \sim 2 (q_i Q)^2,$$

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$$\frac{J^2 Q^4}{4} = (q_i Q)^2 \left( \frac{2 \Omega}{\kappa} \right)^2 \left( \frac{d \ln \Omega}{d \ln R} \right) \sim 2 (q_i Q)^2,$$

for a rotation rate $\Omega$ and dimensionless azimuthal wavenumber $q_i = 2 \pi \sigma / (\lambda_i \kappa)$ at a wavelength $\lambda_i$. The factor of two in the last expression is for a flat rotation curve. If there are $m$ spiral arms in the azimuthal direction, then $q_i = \sigma m / (\pi \kappa R)$, and if we write $Q = \sigma \kappa / (\pi G \Sigma)$ in the usual way, then $q_i Q = \sigma^2 m / (\pi G \Sigma R) \sim H_m / R$ for a scale height $H$. Condition (8) was applied to disk stability and star formation by Zasov & Lau & Bertin (1978) and Bertin et al. (1989; see also Julian & Toomre 1966):

$$\frac{J^2 Q^4}{4} = (q_i Q)^2 \left( \frac{2 \Omega}{\kappa} \right)^2 \left( \frac{d \ln \Omega}{d \ln R} \right) \sim 2 (q_i Q)^2,$$

for a rotation rate $\Omega$ and dimensionless azimuthal wavenumber $q_i = 2 \pi \sigma / (\lambda_i \kappa)$ at a wavelength $\lambda_i$. The factor of two in the last expression is for a flat rotation curve. If there are $m$ spiral arms in the azimuthal direction, then $q_i = \sigma m / (\pi \kappa R)$, and if we write $Q = \sigma \kappa / (\pi G \Sigma)$ in the usual way, then $q_i Q = \sigma^2 m / (\pi G \Sigma R) \sim H_m / R$ for a scale height $H$. Condition (8) was applied to disk stability and star formation by Zasov & Lau & Bertin (1978) and Bertin et al. (1989; see also Julian & Toomre 1966):

$$\frac{J^2 Q^4}{4} = (q_i Q)^2 \left( \frac{2 \Omega}{\kappa} \right)^2 \left( \frac{d \ln \Omega}{d \ln R} \right) \sim 2 (q_i Q)^2,$$
because the dynamical time is longer in the outer part, another order of magnitude is because the total gas surface density is lower in the outer part, and a third order of magnitude is because the fraction of the gas that is molecular is lower in the outer part if the $\Sigma_{\text{SFR}}$ is proportional to the molecular column density.

It seems baffling how the average SFR can maintain such a precise exponential disk for over four magnitudes in both dIrr galaxies and these spiral galaxies. This result is especially puzzling when the molecular fraction is only a small part of the gas: how do molecular clouds forming at extremely low rates know what the rest of the galaxy is doing? The orbit time varies with radius like a power law ($1/R$) while the perpendicular oscillation time or disk crossing time, which is approximately the turbulent dissipation time, increases exponentially with radius for a fixed velocity dispersion. In the inner disk, the perpendicular crossing time is much less than the orbit time, but in the outer disk these times are about the same. The Toomre model has a characteristic timescale comparable to the epicyclic time, which is about the orbit time, whereas cloud formation that combines gas dissipation and local stellar dynamics has a timescale somewhat between the orbit and crossing times. If these times vary separately with radius, then how do the cloud formation rate and internal cloud evolution rate combine to give a SFR that ends up precisely exponential?

If only the perpendicular crossing time mattered for star formation, because the most important processes are governed by dissipation, for example, then the exponential can be self-sustaining: once the disk has an exponential dependence on radius, then the perpendicular crossing time is exponential, and star formation following this crossing time would also be exponential. This situation could be stabilized in the short term by feedback, which puffs up the disk when the SFR is too high and makes the crossing time longer. But it would seem to be unstable in the long term for a given average velocity dispersion because a high SFR in some annulus would make the disk relatively dense there, and this effect would lower the local crossing time and speed up the star formation, making the disk even denser. Subsequent smoothing by stellar spirals (Sellwood & Binney 2002) could recover the original exponential. The same instability would seem to arise in more detailed models, such as those by Ostriker et al. (2010), in which the $\Sigma_{\text{SFR}}$ Scales with the gas column density multiplied by the square root of the local midplane stellar volume density. If the long-term SFR increases with background stellar density, then the exponential profile would seem to be unstable.

We are left with a choice between two puzzling models: (1) the molecular cloud and star formation rate profiles have an exponential profile independent of the underlying stars and this rate profile forces the stellar disk to build up such a profile too, or, (2) the stellar disk is continuously adjusted to an exponential shape regardless of the star formation profile, and then star formation tends to follow the existing stars for dynamical reasons and occasional sequential triggering (Shi et al. 2011). However, the latter seems more reasonable at the present time because global dynamical processes can be imagined that scatter the stars and keep the disk globally exponential. Stellar waves might have this effect (Roškar et al. 2008a), although dIrrs have extended exponentials with no obvious waves. Initial conditions that are exponential (Mestel 1963; van der Kruit 1987) do not help solve this problem because in the present models of galaxy formation, disk mass is added by gas accretion over a long period of time with in situ star formation playing a decisive role in the distribution of new stars. In both of these models, the star formation profile does not follow the gas in the outer parts, which is mostly H\textsc{i}.

5. CONCLUSIONS

We have examined star formation in two very luminous ($M_V = -22$ to $-23$) Sc-type spiral galaxies, NGC 801 and UGC 2885, using ultra-deep H\textsc{a} images. We combine these images with $UBV$ and $2MASS$ $JHK$ images and H\textsc{i} maps to explore the star formation characteristics of disk galaxies at high luminosity.

H\textsc{i} traces star formation in these galaxies to 4–6 disk scale lengths. We find that the most distant H\textsc{i} regions are found at the tips of spiral arms: at radii of $3.9R_D$ and $5.6R_D$ and local H\textsc{i} densities of $1.5 M_\odot \text{pc}^{-2}$ and $6 M_\odot \text{pc}^{-2}$, for NGC 801 and UGC 2885, respectively. In UGC 2885, there are also a few identifiable detached H\textsc{i} regions as far out as $6.1R_D$.

Except in the center ($R < 1.8R_D$) of NGC 801, the azimuthally averaged current SFR is lower than the SFR necessary to form the stellar mass over the lifetime of the galaxy and the current SFR is particularly low in the outer disks. However, the decrease in current SFR relative to that in the past is not consistent with the relatively constant colors in the outer disks. The lack of detection of H\textsc{a} further out is likely due to loss of Lyman continuum photons, and stellar migration processes may also be important in populating the outer disk.

The gas in the outer regions is marginally stable to gravitational instabilities in an average sense, and star formation is taking place in regions of locally higher gas densities, namely, spiral arms. The traditional Toomre (1964) gravitational instability parameter $Q$ is everywhere larger than unity, implying a stable gas. However, when we include the stellar disk thickness with dissipative gas and both radial and azimuthal forcing ($Q_{\text{eff}}$), the outer regions become marginally unstable to forming spiral arms. Star formation occurs in these arms with higher local densities than the surrounding average. Generally, spirals grow at higher $Q$ than the radial stability threshold, so the spirals are the primary instability, from which star formation follows at the locally increased densities in the arms.

We have traced smooth exponential stellar disks over four magnitudes in V-band surface brightness and 4–6 disk scale lengths, in spite of a highly variable gravitational instability parameter. Thus, gravitational instability thresholds do not seem relevant to the stellar disk. One possibility for creating an exponential disk is that the star formation activity has an exponential profile and this fact forces the stellar disk to build up such a profile too. Another possibility is that the stellar disk is continuously adjusted to an exponential shape regardless of the star formation profile. The latter could be due to global dynamical processes that scatter the stars. However, the known scattering processes only operate in spiral systems and cannot explain the same situation of smooth exponential disks observed in dIrr galaxies. Perhaps clumps in dIrr galaxies play the role of scattering centers to make the disks exponential (Hunter et al. 2011; Elmegreen & Struck 2013).

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