Analysis of Combined Pile Raft Foundations Based on a Static Load Test

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Abstract Combined pile raft foundations (CPRF) take into account the synergy of a raft with a group of piles in transferring the load to the ground. In many ground conditions, such foundations are optimal in both utilitarian and economic terms. Based on a literature review, it can be concluded that, despite the numerous extant calculation methods for the analysis of piled raft foundations, there is lack of research related to the possibility of using a load-settlement curve from a static pile test in the full range, in order to analyse the load-settlement curve of a pile working in a group under the raft. Furthermore, the current trend in the design of pile foundations, based on the static load test databases, encourages the formulation of methods using the results of the static pile test. These methods allow for analyses closer to the physical model. In this paper, the above research postulate was answered, formulating a mathematical model in which a particular emphasis was placed on the actual work of a single pile in the ground, taking into account the interaction among raft, piles and subsoil. The developed mathematical model was verified on the basis of the results of field research. For this purpose, the results of settlement of two tanks were used.

Keywords Combined Pile Raft Foundation, Settlement, Numerical Model

1. Introduction

The development of new methods for the analysis of combined pile raft foundations is aimed at increasing the accuracy of calculations and, consequently, their practical significance. Newly developed methods, and often programs based on them, should contribute in the decision-making process during the design and optimisation of structures. An integral part of choosing the final structural solution is the experience of the designers who are aided by the development of calculation methods. Therefore, being aware of the benefits of the synergy between foundation rafts and a group of piles in transmitting the load to the ground, both in utilitarian and economic terms, this article delves into one of these methods.

So far, many methods have been developed for the analysis of piled raft foundations, which can be divided into: simplified (Terzaghi&Peck [24], Poulos&Davis [17], Randolph [3,18]), approximate (Butterfield&Banerjee [1], El Gendy, Hanisch&Kany [4], Clancy&Randolph [3,5]) and detailed (Ottaviani [15], Katzenbach et al. [6,7], Reul&Randolph [19,20]). On the basis of the literature review, it can be concluded that an approach taking into account the non-linear characteristics of pile behaviour in the form of load-settlement curve from the static test of the pile with the analysis of mobilization of skin and base resistance has not yet been applied in the examination of piled raft foundations.

Moreover, it is worth noting that it is common practice to reduce field studies to the analysis of the work of a single pile on the basis of a static load test. It is important to develop a method using the results of the static test of a single pile to analyse the load-settlement curve of the pile working within the group under the raft. An additional advantage would be that the curve extrapolating the results of the load test would be used for the limit resistance. This would enable the determination of the foundation safety factors but also, if necessary, optimise the piling plan.

The presented article is based on the dissertation [2] of one of the authors of this paper. The aim is to present a method of analysing combined pile raft foundations using the static load test curve as a boundary condition of the solution. The way to achieve this is through the development of a mathematical model based on assumptions, which is systematically reviewed, and its application. The thesis put forward is that it is possible to use with sufficient accuracy, for practical purposes, the load-settlement curve from the static load test of a pile in full range to the analysis of the load-settlement curve of a pile occurring in a group of piles under the raft.
2. Mathematical Description of the Settlement of Combined Pile Raft Foundations

The mathematical model of the cooperation of a combined pile raft foundation with subsoil is based on the differential equation of the plate deflection surface on elastic supports (Figure 1), under the vertical load uniformly distributed on the surface [16]:

\[
\frac{\partial^4 s(x,y)}{\partial x^4} + 2\frac{\partial^4 s(x,y)}{\partial x^2 \partial y^2} + \frac{\partial^4 s(x,y)}{\partial y^4} = \frac{q_0(x,y)}{D_x(x,y)} - \frac{k(x,y)}{D_y(x,y)} s(x,y)
\]

Figure 1. Scheme of a plate on spring supports modelling subsoil and piles

The analysis of an elastic raft resting on subsoil and piles requires knowledge of the stiffness of the ground medium and the piles embedded in it. In order to determine this, information on the interaction between the elements forming the foundation is needed. In the studies conducted, this was expressed in the form of partial settlements obtained by appropriate integration of stress distribution in the subsoil. For this purpose, the raft is divided into elementary fields. At the centre of each field and piles, a calculation profile is placed. In each profile, the settlement of the subsoil and piles is the sum of the partial settlements generated by all fields and piles forming the foundation. The stiffness of the supports was determined as the ratio of contact stress of the elementary field on the subsoil or piles to the node settlement in the given profile.

The mathematical description is based on the following assumptions:

- flexible raft rests on elastic half-space subsoil and compressible piles
- non-linear reaction of pile under raft is the result of a static load test and the interaction between raft, piles and subsoil
- raft–subsoil contact pressure is the result of non-linear compounds describing the loss of stress in the ground based on Boussinesq’s theory and Meyer’s active zones
- magnitude of settlements results from the integration of stress distribution within the active zones, taking into account the stress state from the interaction of raft, piles and subsoil
- vertical load uniformly distributed on raft surface
- flexible raft rests on layered subsoil

The non-linear characteristics of operation of a single pile in the ground medium were described using the curve by Meyer and Kowalów (MK curve) [11], which approximates the results of a static pile test, in the form of:

\[
s(N_t) = C \cdot \frac{N_w}{\kappa} \left[ \left( 1 - \frac{N_t}{N_p} \right)^{\gamma} - 1 \right]
\]

The presented curve, after determining its characteristic parameters, i.e. the critical load of a pile \( N_w \) and two constants \( C \) and \( \kappa \), enables extrapolation of the load-settlement curve beyond the range of the static test of a pile to the critical load. In the mathematical description, the limit resistance should be understood as the load causing the settlement of the pile without changing its resistance.

The mobilization of resistance around a pile was determined on the basis of two uses of the MK curve [12,14], characterising the behaviour of a single pile in two different states. The first condition is typical for the static load test of a pile, taking into account the skin and base resistance, while the second condition only takes into account base resistance. The parameters of the first state curve were determined by the method of the smallest sum of squares [22]. The parameters of the curve of the second state were determined from the dependencies, in the form of:

\[
s(N_t) = \frac{C_i \cdot N_{p1}}{\kappa_i} \left[ \left( 1 - \frac{N_t}{N_{p1}} \right)^{\gamma_i} - 1 \right]
\]

which was adopted on the basis of Meyer's research, for \( E_p = 4q_{c,s} \) [9]:

\[
N_{p1} = \frac{1}{8\pi} E_p \cdot D^3 \left( \frac{h_p}{D} \right)^3
\]

\[
C_i = \frac{4}{3\pi \cdot E_p \cdot D}
\]

\[
\kappa_i = \frac{2}{3} \kappa
\]

Mobilization of the skin resistance of the pile was determined from the following dependency:

\[
T(s) = N_s(s) - N_t(s)
\]

The interaction among raft, piles and subsoil has been determined in the form of partial settlements (Figure 2). These were obtained by appropriate integration of stress distribution in the soil within the limits of active zones (Figure 3). The range of the active zone is understood as the subsoil layer that deforms under the applied load.
settlement of the field of the discrete raft

Figure 2. Partial settlement modelling interaction between raft, piles and subsoil

settlement of the pile

Figure 3. Stress distribution in subsoil including active zones [10]
Meyer's research shows that the range of the active zone of the mineral soil for the VSS static plate depends on the soil parameters and contact stress $\sigma_0$, according to relation [8]:

$$z_0 = \frac{1}{2} \cdot \gamma_0 \cdot \frac{1}{\ln \left( \frac{E_0}{\sigma_0} \right)} \cdot \frac{\sigma_0}{\gamma}$$  (8)

Settlement of the plate, taking into account the active zone $z_0$, is obtained from formula:

$$s = \frac{\sigma_0}{E_0} \cdot \frac{D \cdot z_0}{D + z_0}$$  (9)

The above formulae, in accordance with the results of research [8,13], were used in the calculation of spread and pile foundations. For pile foundations, the active zone is determined on the basis of the stress generated in the base of the pile. In the mathematical model, the range of active zones of slab and pile was determined from the following formulae respectively:

$$z_{01} = \frac{1}{2} \cdot \gamma_{01} \cdot \frac{1}{\ln \left( \frac{E_0}{q} \right)} \cdot \frac{q}{\gamma_s}$$  (10)

$$z_{02} = \frac{1}{2} \cdot \gamma_{02} \cdot \frac{1}{\ln \left( \frac{E_c}{q_c} \right)} \cdot \frac{q_c}{\gamma_q}$$  (11)

For embankment soils, the range of the active zone equals the entire thickness of anthropogenic soils. We also apply this rule to highly compressible subsoil layers. Therefore, partial settlement in its general form expresses the relationship:

$$s = \int_{z_t}^{z_0} \frac{\sigma_0}{E_0} dz$$  (12)

where $z_t, z_0$ are the limits of the active zone.

The following relationships describing the partial settlements have been determined to express the interaction among raft, piles and subsoil.

The settlement of the elementary field of the raft caused by the load applied on its own field was determined from relation (9), which for the layered subsoil depended on the location of the range of the active zone (Figure 4):

- for $z_{01} < h_1$, $h_1 > z_{01} = z_{010}(\sigma_{z=0})$

$$s_{z_{01}(0,h_1)} = \frac{\sigma_{z=0}}{E_1} \cdot \frac{D \cdot z_{010}}{D + z_{010}}$$  (13)

- for $z_{01} = h_1, h_1+h_2 > z_{01} = h_1+z_{011}(\sigma_{z=h_1})$

$$s_{z_{01}(h_1,h_1+h_2)} = \frac{\sigma_{z=h_1}}{E_1} \cdot \frac{D \cdot h_1}{D + h_1} + \frac{\sigma_{z=h_2}}{E_2} \cdot \frac{D \cdot z_{011}}{D + z_{011}}$$  (14)

- for $z_{01} = h_1+h_2 > z_{01} = h_1+h_2+z_{012}(\sigma_{z=h_1+h_2})$

$$s_{z_{01}(h_1+h_2)} = \frac{\sigma_{z=h_1}}{E_1} \cdot \frac{D \cdot h_1}{D + h_1} + \frac{\sigma_{z=h_2}}{E_2} \cdot \frac{D \cdot h_2}{D + h_2}$$

$$+ \frac{\sigma_{z=h_1+h_2}}{E_1} \cdot \frac{D \cdot z_{012}}{D + z_{012}}$$  (15)

\[\text{Figure 4. The distribution of stress in the ground under the discrete raft from the load of the self and the adjacent field}\]
The settlement of the elementary field of the raft caused by the adjacent field load (Figure 4) is determined from the Boussinesq formula [25]:

$$\sigma_s(Q) = \frac{3 \cdot Q \cdot z^3}{2 \pi \cdot R^3}, \quad R = \sqrt{x^2 + y^2 + z^2} \quad (16)$$

which for the layered subsoil is presented in the form:

- for $z_{01} < 0, h_1 > z_{01} = z_{010}(\sigma = 0)$

$$s_{z_{01}}(0, h) = \int_0^{h_1} \sigma_s(Q) dz = \frac{Q}{2 \pi \cdot E_1} \left[ 2 \cdot \frac{z^2}{L} + 2 \cdot \frac{h_1^2}{L} \right] + \ldots \quad (17)$$

- for $z_{01} > h_1 + h_2 \rightarrow z_{01} = h_1 + z_{011}(\sigma = h_1)$

$$s_{z_{01}}(h_1, h_1 + h_2) = \int_0^{h_1} \sigma_s(Q) dz + \int_{h_1}^{h_1 + h_2} \sigma_s(Q) dz = \ldots$$

$$= \frac{Q}{2 \pi \cdot E_1} \left[ 2 \cdot \frac{z^2}{L} + 2 \cdot \frac{h_1^2}{L} \right] + \ldots$$

$$+ \frac{Q}{2 \pi \cdot E_2} \left[ 3 \cdot \frac{h_1^2}{L} + 2 \cdot \frac{L^2}{L} \right] - \frac{3 \cdot (h_1 + z_{011})^2 + 2 \cdot \frac{L^2}{L}}{\sqrt{h_1 + z_{011}} + L^2} + \ldots$$

$$\quad (18)$$

The settlement of the pile caused by the load applied in the head was determined on the basis of the MK curve (2).

The settlement of the pile caused by the force generated in the base of the adjacent pile (Figure 2 and Figure 3) is conditional, i.e. it occurs when the difference in length between the piles is smaller than the range of the active pile zone:

- for $|h_p - h_p| \geq z_{02} \rightarrow s = 0$

$$s = \int_{h_p}^{z_{02}} \sigma_s(Q) dz = \ldots$$

$$= \frac{Q}{2 \pi \cdot E_y} \left[ 3 \cdot \frac{(h_p - h_p)^2}{L} + 3 \cdot \frac{z_{02}^2 + 2 \cdot L^2}{L} \right] \quad (21a)$$

The settlement of the pile caused by stress generated on the skin of the adjacent pile (Figure 2 and Figure 3) is given by formula:

$$s = \int_{h_p - h_p}^{z_{02}} \sigma_s(Q) dz = \ldots$$

$$= \frac{Q}{2 \pi \cdot E_y} \left[ 3 \cdot \frac{(h_p - h_p)^2}{L} + 3 \cdot \frac{z_{02}^2 + 2 \cdot L^2}{L} \right] \quad (21b)$$

The settlement of the pile caused by the load of the elementary field of the raft occurs when the pile length is smaller than the active zone of the raft (Figure 2 and Figure 3) and is expressed as a relation:

- for $h_p \geq z_{01} \rightarrow s = 0$

$$s = \int_{h_p}^{z_{01}} \sigma_s(Q) dz = \ldots$$

$$= \frac{Q}{2 \pi \cdot E_1} \left[ 2 \cdot \frac{z^2}{L} + 2 \cdot \frac{h_1^2}{L} \right] + \ldots$$

$$+ \frac{Q}{2 \pi \cdot E_2} \left[ 3 \cdot \frac{h_1^2}{L} + 2 \cdot \frac{L^2}{L} \right] - \frac{3 \cdot (h_1 + z_{011})^2 + 2 \cdot \frac{L^2}{L}}{\sqrt{h_1 + z_{011}} + L^2} + \ldots$$

$$\quad (22)$$

The settlement of the pile caused by the force generated in the pile base (Figure 2 and Figure 3) occurs when the range of the active zone of the pile is greater than its length and therefore:

- for $h_p \geq z_{02} \rightarrow s = 0$

$$s = \int_{h_p}^{z_{02}} \sigma_s(Q) dz = \ldots$$

$$= \frac{Q}{2 \pi \cdot E_y} \left[ 3 \cdot \frac{(h_p - h_p)^2}{L} + 3 \cdot \frac{z_{02}^2 + 2 \cdot L^2}{L} \right] \quad (23)$$

The settlement of the elementary field of the raft caused by the stress generated on the pile skin (Figure 2 and Figure 3) is given by formula:
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3. Solution of the Mathematical Model

Knowing the relationships describing the interaction between the elastic raft on the subsoil and the piles, the settlement of the subsoil and piles was determined according to formula:

\[
s = \int_0^{hp} \frac{\sigma_\tau(z)}{E_w} dz = \ldots
\]

\[
= \frac{3 \cdot \chi \cdot \varepsilon}{2\pi \cdot E_w} \left[ \ln \frac{z_{02} + \sqrt{z_{02}^2 + \left(\frac{L}{hp} + 1\right)^2}}{z_{02} + hp + \sqrt{z_{02}^2 + hp^2 + \left(\frac{L}{hp} + 1\right)^2}} \right] + \ldots
\]

\[
+ \frac{z_{02} + hp}{3\sqrt{(z_{02} + hp)^2 + L^2}} - \frac{z_{02}}{3\sqrt{z_{02}^2 + L^2}} + \ldots
\]

\[
+ \ln \left[ \frac{L}{\sqrt{hp^2 + L^2 - hp}} - \frac{hp}{3\sqrt{hp^2 + L^2}} \right]
\]

(24)

The proposed method is to determine the distribution of the contact stress of the raft and piles with the subsoil in such a way that the deflections of the raft calculated on the basis of differential equation (1) and the settlement of the subsoil with piles (25) were the same with the assumed accuracy. The above equation is solved using the numerical method.

In the mathematical model discussed above, the raft rests on elastic supports, modelling layered subsoil and piles, with the vertical stiffness of the supports expressed in the form:

\[
\begin{bmatrix} \{s_R\} \\ \{s_p\} \end{bmatrix} = \begin{bmatrix} WRR \end{bmatrix} \begin{bmatrix} 0 \\ WN_p \end{bmatrix} \begin{bmatrix} WN{R} \end{bmatrix} \begin{bmatrix} W\tau R \end{bmatrix} \begin{bmatrix} \{N_R\} \\ \{N_p\} \end{bmatrix} \begin{bmatrix} \{R_R\} \\ \{R_p\} \end{bmatrix} \begin{bmatrix} \{f_R\} \\ \{f_p\} \end{bmatrix}
\end{bmatrix}
\]

(25)

The developed mathematical model enables the analysis of the geotechnical conditions of piled raft foundations, taking into account the static load test curve as a boundary condition of the solution. The mathematical model enables the analysis of load distribution between the raft and piles, and the influence of piles on the reduction and equalisation of raft settlement for given geotechnical conditions.

4. Examples of Calculations

A review of the solutions obtained with the mathematical model in question was carried out for the combined pile raft foundation with five piles. The analysis was performed for two types of piles deposited in different soil conditions (Table 1 and Table 2).

The first pile is a non-displacement drilled pile (pile no. I), while the second pile is a driven pile (pile no. II).

Geometric data of piles:
- Pile no. I – \(hp=10.0\) m, \(D=0.60\) m
- Pile no. II – \(hp=13.5\) m, \(D=0.508\) m

| Table 1. Geotechnical parameters – pile no. I |
| Type of soil | Thickness of layer [m] | Young's modulus \(E_0\) [MPa] |
| silty clay | 3.0 | 7.0 |
| sandy silty clay | 6.5 | 24.6 |
| silty clay | – | 12.5 |

| Table 2. Geotechnical parameters – pile no. II |
| Type of soil | Thickness of layer [m] | Young's modulus \(E_0\) [MPa] |
| silty clay | 5.0 | 7.0 |
| fine sand | 7.0 | 56.4 |
| fine sand | – | 60.0 |

The results of the static load tests were used to determine the parameters of the MK curve, together with the mobilization of the skin and base resistances of the piles (Figure 5).

A review of the solution was carried out on the example of a 4.5×7.0 m raft, which rests on the subsoil and five piles. The locations are shown in Figure 6.

Figure 5. Skin and base resistance mobilization of piles

Figure 6. Scheme of the analysed foundation
4.1. Analysis of Settlement and Deflection of the Combined Pile Raft Foundation

The analysis of the impact of bending stiffness of the raft is presented in Figure 7 and Figure 8. The review of the obtained results also takes into account the type of pile expressed in the load-settlement relation. Based on the obtained results of raft settlement, it can be concluded that for a given location and pile spacing in a group, the reduction of raft stiffness affects the increase of the load transmitted by the central pile. This illustrates the largest settlement in the middle of the raft, which is also a result of the work of a given pile group. As expected, the increased stiffness of the raft contributed to the compensation of settlement and increased uniformity of the load of corner piles with the central pile. This results from the stress state in the ground medium, the reduction of deflection of the raft and, thus, the compensation of the settlement of the subsoil.

The factor influencing the settlement of the raft is, of course, piles. Their influence depends on the settlement of a given pile in the group under the impact of the load applied to the head, resulting from its location in the group, the load of the raft, and its bending stiffness in the given ground conditions.

4.2. Analysis of the Load-Settlement Curve of a Pile Working in a Group of Piles under the Raft

The calculations carried out allow us to state that the settlement of piles working in a group, taking into account the synergy of the raft, is different from that during a static load test. The reason for this phenomenon can be found in the stress state in the ground medium, resulting from the impact of individual piles on each other. The settlement of piles in a group depends, apart from the load applied to their heads, on their interaction, which affects their settlement as a whole (Figure 9 and Figure 10). In the analysed example, due to the range of the active zone of the raft, the raft–subsoil contact stress does not affect the settlement of the piles.

In this example, the central pile is more loaded, showing a greater settlement than the corner pile. Resistance around the central pile and, therefore, the stress generated by it in the ground medium, have a greater impact on the settlement of adjacent piles. This is reflected in the greater divergence in the settlement of corner piles compared with the settlement of a single pile.

4.3. Analysis of the Contribution of Piles in Transferring the Load

The analysis of load distribution between the raft and piles is inextricably linked to the type of piles and
geotechnical conditions. The share of piles in transferring the load to the subsoil is determined by the load-settlement curve of the piles and the bending stiffness of the raft, taking into account the geotechnical conditions. Figure 11 and Figure 12 show the impact of the pile type and the stiffness of the raft on the load distribution. The contribution of piles in transferring the load to the subsoil increases with the bending stiffness of the raft.

5. Application

The correctness of the assumptions of the mathematical model was based on the results of field research [21,23]. The research included geodetic monitoring of settlement of two tanks of the Sewage Treatment Plant Complex, i.e. the Emergency tank and Final cleaning tank (Figure 13 and Figure 14). The foundations of these tanks were designed and constructed as combined pile raft foundations and have diameters of 13 m and 17 m. The tanks were placed on CFA (Continuous Flight Augering) piles with diameters of \( \phi \) 400/600 mm and lengths of 9.5–12 m.

Three basic geotechnical layers were distinguished. Anthropogenic embankment occurs on the surface of the area. This embankment has been partially consolidated by the coal storage site that used to exist here. In the second layer, mainly clayey sands and sandy clays in a very soft state are found, with stratification of non-cohesive loose or medium-compacted soils. Below, in a separate third layer, silty clay and sandy silt exist in the firm and soft state boundary.

The analysed objects have geotechnical profiles (Table 3 and Table 4), with the results of static load tests made on the foundation raft plan of each tank (Figure 15).
Table 3. Geotechnical profile – Emergency tank [21,23]

| Layer number | Type of soil                          | Ground condition $I_d/A_d$ | Oedometric modulus $E_{oed}$ [MPa] |
|--------------|--------------------------------------|---------------------------|-----------------------------------|
| I            | Fill                                 | 0.3(0.5)                  | 20                                |
| IIb          | clayey sand, sandy clay              | 0.4                       | 18                                |
| IIa          | clayey sand, sandy clay              | 0.6                       | 18                                |
| IIc          | fine sand, medium sand               | ≤0.3                      | 42                                |
| IIa          | clayey sand, sandy clay              | 0.6                       | 20                                |
| IIIa         | silt                                 | 0.25                      | 35                                |
| IIlb         | silty clay, sandy silt               | 0.25                      | 22                                |
| IIle         | silty clay, silty sand               | 0.1                       | 31                                |

Table 4. Geotechnical profile – Final cleaning tank [21,23]

| Layer number | Type of soil                          | Ground condition $I_d/A_d$ | Oedometric modulus $E_{oed}$ [MPa] |
|--------------|--------------------------------------|---------------------------|-----------------------------------|
| I            | fill                                 | 0.3(0.5)                  | 20                                |
| IIId         | medium sand                          | 0.5                       | 100                               |
| IIa          | clayey sand                          | 0.6                       | 20                                |
| IIIb         | silty clay, silty sand               | 0.25                      | 22                                |
| IIle         | silty clay, silty sand               | 0.1                       | 31                                |

Figure 15. Results of the static load test of pile no. 21 of the Emergency tank and pile no. 37 of the Final cleaning tank [21]

Measuring benchmarks were installed on the tank foundations, located along the perimeter of the foundation raft. The settlement control was carried out during the water test. The obtained settlement results were used to verify the presented mathematical model. The comparison between calculated and measured settlements is presented in Figure 16 and Figure 17.
Measurements of geodetic settlements were located on the external outline of the foundation. On the basis of measurements made, uneven displacement of the two benchmarks of the Emergency tank can be observed, which could be due to local deterioration of ground conditions. The obtained results of settlement calculations and their significant compliance with the majority of measured values verify the correctness of the adopted assumptions.

On the basis of calculations made for the foundation of the Final cleaning tank, we can observe the largest settlements around the perimeter of the raft edge. This is due to the diversity of piles in the group, i.e. the external perimeter is made of piles with lower bearing capacity and stiffness compared to the piles inside the group. The above design assumption made it possible to reduce settlement in the central part of the raft. It should be noted that the parameters of the MK curve for piles located around the perimeter were estimated on the basis of the results of a load test of a pile inside a group. We do not have the results of the load test of the external pile, which affects the accuracy of the obtained results.

6. Discussion

The subject of the research was the analysis of the synergy of a raft with a group of piles in transferring vertical load to the ground.

During the implementation of the above task, a method of calculation of combined pile raft foundations based on the results of a static test pile load was proposed. The authors of the article believe that the proposed mathematical model, based on the results of the static load tests, has practical significance, taking into account the EuroCode 7 method of pile design on the basis of the results of static load tests. The EC7 standard also states that empirical and analytical methods of pile design require verification based on static tests. Therefore, given that the current trend in the design of piling works considers the use of databases of static load tests as important, the authors argue that it is imperative to develop methods based directly on the results of static pile tests.

The mathematical model presented in the paper also takes into account the interaction of raft, piles and subsoil. As a result of the calculations carried out, we obtained the settlement and deflection of the raft, and determined the load distribution transmitted by the raft and individual piles in the group.

7. Conclusions

On the basis of the developed mathematical model, the systematic review of the solution, and the calculation of the foundations, the following conclusions were formulated:

1. The presented mathematical model determines the relationship between the load and settlement of combined pile raft foundations. The presented solution introduces into the calculations of the load-settlement relationship from the static load test, which brings it closer to the physical model.
2. The solution of the mathematical model was obtained on the basis of numerical methods and boundary conditions, which result from the synergy of a raft with a group of piles.
3. The analysis and research results confirm that it is possible to use the load-settlement curve from the static pile test to analyse the load-settlement curve of a pile occurring in a pile group under the raft.
4. The contribution of piles in transferring the load is inextricably linked with the type of pile. The performance characteristics of the piles and raft determine the share of piles in the transmission of the load to the ground.
5. The contribution of piles in transferring the load increases as the load increases to a certain value, exceeding which initiates the process of reducing the share of piles in transferring the load to the ground. The reason for this phenomenon can be found in the non-linear characteristics of the pile work in the ground.

Notation

Latin letters

- $B$ – dimensions of foundation raft [m]
- $C$ – a constant value representing the aggregated soil reaction modulus [mm/kN]
- $D$ – pile diameter [m]
- $D_{b}$ – bending stiffness of the raft [kNm]
Greek letters

\[ \gamma \] – volume weight of ground [kN/m³]
\[ \gamma_n = 1, 2, 3 \text{ [kN/m³]} \]
\[ \gamma_q \] – volume weight of ground under pile base [kN/m³]
\[ \kappa \] – dimensionless constant
\[ \lambda \] – pile circumference [m]
\[ \nu \] – Poisson's ratio
\[ \sigma_{(…)} \] – vertical component of soil stress [kPa]
\[ \tau_{,t} \] – skin resistance of pile [kPa]
\[ \phi \] – angle of internal friction of ground [°]
\[ \phi_q \] – angle of internal friction of ground under pile [°]
\[ \phi_n \] – angle of internal friction of ground under pile base [°]

Matrix and vectors

\[ \{0\} \] – null matrix
\[ \{k_P\} \] – vector of vertical stiffness of elastic supports modelling piles
\[ \{k_R\} \] – vector of vertical stiffness of elastic supports modelling subsoil
\[ \{N_j\} \] – vector of base resistance of piles
\[ \{N_k\} \] – load applied to pile head
\[ \{Q_k\} \] – vector of quotients of load applied to pile heads in the area of elementary field
\[ \{R_k\} \] – vector of contact pressure of raft fields with subsoil
\[ \{s_P\} \] – vector of settlement of piles in the calculation profiles of raft fields
\[ \{s_R\} \] – vector of settlement of subsoil in the calculation profiles of raft fields
\[ \{t\} \] – vector of skin resistance of piles
\[ \{W_n, P\} \] – matrix of impact factors of base resistance of piles on the settlement of piles
\[ \{W_n, R\} \] – matrix of impact factors of base resistance of piles on the settlement of raft fields
\[ \{W, P\} \] – matrix of impact factors of load applied to pile heads on the settlement of piles
\[ \{W, R\} \] – matrix of impact factors of contact pressure of raft with subsoil on the settlement of piles
\[ \{W_T, R\} \] – matrix of impact factors of skin resistance of piles on the settlement of piles
\[ \{W_T\} \] – matrix of impact factors of skin resistance of piles on the settlement of raft fields

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