Reaction mechanism between Cu(II)-enolate complex and O\textsubscript{2} as a test case for methodology used in DFT computational studies

Agnieszka Stańczak\textsuperscript{1,2} · Anna Miłaczewska\textsuperscript{3} · Tomasz Borowski\textsuperscript{3}  

Received: 30 November 2018 / Accepted: 15 March 2019 / Published online: 24 April 2019
© The Author(s) 2019

Abstract
The reaction mechanism of an intricate oxidation reaction of chlorodiketonate ligand of mononuclear Cu(II) complex was studied computationally employing five different models that differ in: a) basis set, b) the way that solvent corrections are included, and c) DFT functional. Qualitative and quantitative comparison of structures and enthalpy reaction profiles enabled us to assess how sensitive they are to the changes in computational methodology.

Keywords
Enolate · Dioxygen · PCM · Homolytic · Heterolytic bond cleavage

Introduction
Using quantum chemistry methods to model (bio)inorganic reaction mechanisms for systems involving first row transition metals (TM) is a challenging task. First, such systems involve coordination bonds that are difficult to describe quantitatively with robust DFT methods. Second, electronic configurations with open 3d shells often result in several spin states that are close in energy and a so-called multi state reactivity may emerge [1]. Finally, the metal ion(s) may be redox active, and hence may promote radical mechanisms aside from the heterolytic processes. Even though recent years have witnessed major breakthroughs in the development of very promising post-HF methods, such as DMRG-CASPT2 or local CCSD(T) methods [2, 3], their computational cost still remains relatively high when they are used with adequate one-electron basis sets. Therefore, it is foreseen that much less demanding DFT methods will continue to be widely used for geometry optimizations and energy calculations, whereas these more advanced post-HF methods will be employed to compute accurate electronic energies for (selected) structures optimized with DFT.

Embarking on a DFT computational study on a reaction mechanism for a TM system necessitates taking several decisions on the computational methodology, including which density functional and which basis set shall be used for geometry optimization and which for energies or weather a solvent model shall be applied during optimization or rather it suffices to use it only as an energy correction for structures optimized in vacuum.

To assess to what extent such particular decisions may affect conclusions one draws from computational results, we did a small yet systematic case study for a synthetic mononuclear copper(II)-chloroenolate complex, for which congruent experimental and computational results are already available [4, 5]. This system has several particularly attractive features concerning testing variations of computational methodology. First, it is a mononuclear system of size that is not prohibitively large, so both double and triple-zeta one electron basis sets may be tested for geometry optimization and frequency calculations. Second, the reaction between this complex and dioxygen features several plausible yet different reaction types, i.e., reduction of dioxygen to peroxy species, nucleophilic substitution as a prelude to heterolytic O–O cleavage, and heterolytic and homolytic O–O bond cleavage.
accompanying oxidation of chlorine, aliphatic or aromatic carbons. Finally, experimental results are available and they can be used as a reference point when assessing various computational methodologies.

The model system is a cationic chelate complex of Cu(II) with 6-Ph₂TPA and PhC(O)CCIC(O)Ph chlorodiketonate as ligands (S), or its derivative with one chloride anion bound in the first coordination shell of copper (S_cl, see Scheme 1). Results of previous computational investigations on the mechanism of the reaction between these complexes and dioxygen have already been published, yet for the sake of completeness the key findings are summarized here. Thus, the X-ray crystal structure of a salt with Cu(II) complex as a cation and ClO₄⁻ as an anion is known [4]. In acetonitrile, the reaction between S and O₂ proceeds with an initial slow lag phase that can be eliminated by addition of catalytic amounts of chloride salts.

Crystal structure of S_cl is not available, yet UV-vis and EPR spectroscopic data together with the DFT optimized structure suggest that chloride anion coordinates Cu in a complex with distorted square pyramidal geometry. The composition of the final reaction mixture is the same as the one obtained in an independent reaction between NaOCl, diphenylpropanetrione (triketone), and [(6-Ph₂TPA)Cu(CH₃CN)](ClO₄)₂, which strongly indicates that triketone and hypochlorite are formed as reactive intermediates in the initial stage of the reaction [5].

From the DFT results obtained for the parent compound S, it follows that in the first step of the reaction one of the oxygen atoms of the chloroenolate detaches from Cu(II) making a place for dioxygen; O₂ binds first to copper and then to the central carbon (C2) of the enolate. Thus, formed peroxo-bridged intermediate P subsequently undergoes a remarkable and concerted, yet asynchronous transformation, whereby first, the oxygen atom proximal to copper (O1) makes an SN₂ type nucleophilic attack on C2 expelling Cl⁻ and second, this liberated chloride anion attacks a strained 3-membered CO₂ ring cleaving the O–O bond heterolitically and forming an adduct between hypochlorite and triketone (T). The two barriers connected with TS₁ and TS₂ are substantial and comparable in size. The reaction between S_cl and O₂ proceeds in a similar way, yet the presence of Cl ligand changes the mechanism of the second step, as in TS₂_cl the oxygen atom O1 is attacked by Cl₂, which elicits O–O cleavage and dissociation of Cl₁ as Cl⁻. Both barriers, connected with TS₁_cl and TS₂_cl, are substantially lower than for the parent compound lacking the chloride ligand, which successfully explains the catalytic effect exerted by the chloride ion.

Two alternative pathways were found for the decay of the peroxo intermediate P_Cl (Scheme 2).

First, the O–O bond may be cleaved homolytically via TS₂_Cl_homol. Second, instead of oxidizing Cl₂, one of the phenyl appendages of the 6-Ph₂TPA ligand may be oxidized to

---

Scheme 1 Mechanisms for the initial stage of oxidation of S or S_cl formulated on the basis of a joined experimental and computational study [5]
arene oxide ($\text{Cl}_2\text{Ph}$). In the original study, both of these processes involved barriers higher than that connected with $\text{TS2}_{\text{Cl}}$; however, the latter reaction was also found for the parent compound $\text{P}$, and in this case $\text{TS2}_{\text{Ph}}$ was lower in energy than $\text{TS2}$.

In this study we re-examined the above summarized mechanisms using several variations of the computational methodology originally applied to this system. From comparison of the results we were able to draw several conclusions that, in our opinion, will be useful when one considers a similar project.

### Computational details

Three one-electron basis sets were used in this study. BS1 of double-$\zeta$ quality consisted of LANL2DZ basis and an effective core potential for Cu and 6-31G basis for other elements. BS2 of triple-$\zeta$ quality for the key atoms combining lacv3p + basis for Cu, 6-311G* for Cl, N, O, and three central carbon atoms of chlorodiketonate and 6-31G for other carbon and all hydrogen atoms. BS1 or BS2 were used for geometry optimization, frequency calculations, and computation of solvent effects. The final electronic energies were computed with BS3, which combined the lacv3p + basis for copper with cc-pVTZ(−f) basis for other elements.

Three hybrid density functionals were used for computations: B3LYP [6], TPSSh [7], and $\omega$B97XD [8]. All three were combined with the D2 dispersion correction [9]; in the case of $\omega$B97XD the D2 correction is included in the functional formula. For B3LYP and TPSSh, the final electronic energy, which was computed with BS3 basis set, was combined with the D3 dispersion correction obtained with the DFT-D3 program [10].

Solvent (acetonitrile) effects were computed with the polarizable continuum model using the integral equation formalism (IEFPCM). Computations were done with the spin-unrestricted formalism using Gaussian 09 [11].

For species with antiferromagnetic coupling between unpaired electrons, the electronic energy was corrected with the procedure proposed by Yamaguchi and co-workers [12].

All reported values combine: electronic energy computed with BS3, Yamaguchi correction, if applicable, D3 correction for the appropriate functional or D2 built-in $\omega$B97XD, solvent effects computed either as single point corrections or used also for geometry optimization, and zero point and thermal corrections to enthalpy computed with the harmonic approximation at the same level of theory as used for geometry optimization.

The results taken from the previous study are used as a reference and are labeled as B3LYP-D3/BS3//B3LYP-D2/BS1 [5]. In previous work, although the TPSSh functional was used, it was only to compute electronic energies for geometries of stationary points that were optimized at the B3LYP-D2/BS1 level; such energy profiles were very similar to those obtained with B3LYP only. In the present work, the TPSSh functional is used both to optimize geometries and compute final energies; hence, the results and conclusions may be different than from previous work.

In the model abbreviated by B3LYP-D3/BS3//B3LYP-D2,PCM/BS1, the PCM method was used both for geometry optimization and the final enthalpy calculations. In the model B3LYP-D3/BS3//B3LYP-D2/BS2 the larger basis set (BS2) was used for geometry optimization and harmonic analysis. Two other models differ from the reference one in the functional used and are labeled with TPSSh-D3/BS3//TPSSh-D2/BS1 and $\omega$B97XD/BS3//$\omega$B97XD/BS1, respectively.

### Results and discussion

The representative enthalpy reaction profile, computed with the B3LYP-D3/BS3//B3LYP-D2/BS2 model, is presented in Fig. 1, and profiles computed with other models can be found in Supporting information. Relative enthalpy values obtained for all models are gathered in Table 1, whereas Table 2 presents key interatomic distances for stationary points along the reaction coordinates.

Concerning the qualitative aspects, all of the enthalpy profiles computed with different models reproduce the catalytic effect introduced by the chloride ligand, as the barriers connected with $\text{TS1}_{\text{Cl}}$ and $\text{TS2}_{\text{Cl}}$ are markedly lower than those.
corresponding to TS1 and TS2. Similarly, for all models the first elementary step, i.e., S → P, is more exothermic when Cl is bound in the first coordination shell of Cu(II), whereas TCl_homo is the least stable of all products. Relative stability of other products is somewhat less preserved among the models. However, some trends may be noticed, as for almost all models TCl_Ph is the lowest enthalpy product; the exception is the TPSSh-D3/BS3//TPSSh-D2/BS1 model, for which the most stable product is TPh, with TCl_Ph being the second most stable. Relative barrier heights for various decay channels of the peroxo species P indicate that for the parent system TPh would be the most easily accessible product for all models except the TPSSh-D3/BS3//TPSSh-D2/BS1 model, for which T is predicted to be produced with the lowest barrier. Analogous analysis for the channels starting at PCl shows that TCl is the kinetically preferred product for all models except TPSSh-D3/BS3//TPSSh-D2/BS1, for which TCl_homo is accessible with the lowest barrier. The latter prediction when confronted with the experimental observation of identical reaction outcomes from reactions starting with S/O2 or triketone/ClO− may suggest that the TPSSh-D3/BS3//TPSSh-D2/BS1 model probably incorrectly favors the homolytic O–O bond cleavage over the heterolytic process leading to ClO−.

Comparison of the reaction enthalpy profiles obtained with the B3LYP-D3/BS3//B3LYP-D2/BS1 and B3LYP-D3/BS3//B3LYP-D2,PCM/BS1 models shows that qualitatively the reaction landscape does not change when the PCM model of the solvent is also used for geometry optimization. Similar conclusions can be drawn with respect to the effect of using a larger basis set (BS2) for geometry optimization, cf. enthalpy profiles obtained with the B3LYP-D3/BS3//B3LYP-D2/BS1 and B3LYP-D3/BS3//B3LYP-D2/BS2 models.

Comparing qualitative features of the enthalpy profiles computed with the three different hybrid functionals enables one to conclude that the choice of the functional affects the computed landscape more than using a bigger basis set or solvent model for geometry optimization. The most important differences can be noticed for the decay of the peroxo intermediate. One difference has already been mentioned above, i.e., the TPSSh model predicts the lowest barrier for homolytic O–O cleavage starting from PCl. Another qualitative difference is that for the parent system the lowest barrier for decay

**Table 1** Relative enthalpy values computed for elementary steps along the reaction coordinates

| Reaction step | ΔH [kcal mol⁻¹] |
|---------------|-----------------|
| S → TS1       | 25.9 28.8 27.9 30.3 34.2 |
| S → P         | -9.8 -7.7 -8.3 -6.1 -5.9    |
| P → TS2       | 24.7 22.9 22.3 22.9 26.9    |
| P → T         | -15.5 -15.7 -19.4 -16.2 -18.6 |
| P → TS2ph     | 19.8 20.8 21.7 17.9 31.4    |
| P → TPh       | -21.2 -21.5 -19.9 -22.2 -22.7 |
| SCl → TS1Cl   | 16.9 18.2 14.5 21.0 24.3    |
| SCl → PCl     | -17.2 -15.9 -19.5 -9.0 -14.6 |
| PCl → TS2Cl   | 11.6 12.2 13.6 17.5 18.9    |
| PCl → TCl     | -7.7 -9.7 -10.1 0.3 -1.5    |
| PCl → TS2ph   | 23.1 22.3 24.8 23.0 35.7    |
| PCl → TClPh   | -19.2 -22.6 -16.8 -15.4 -20.1 |
| PCl → TClhomo | 17.4 n.d. 22.9 13.5 33.5  |
| PCl → TCl     | 11.6 10.4 15.5 8.1 23.0    |

**Fig. 1** Reaction enthalpy profile computed with the B3LYP-D3/BS3//B3LYP-D2/BS1 model
Table 2  Key bond lengths [Å] for selected optimized stationary points. The values are reported in the following order: B3LYP-D3/BS3/B3LYP-D2/BS1, B3LYP-D3/BS3/B3LYP-D2/PCM/BS1, B3LYP-D3/BS3/B3LYP-D2/BS2, TPSSh-D3/BS3/TPSSh-D2/BS1, ωB97XD/BS3/ωB97XD/BS1. Standard deviations are in brackets.

| Species       | Cu-O | O1-O2 | O2-C2 (O1-C2) | C2-C1 | O1-CX | Cl1-O2 (Cl2-O3) | Cu-C1 |
|---------------|------|-------|---------------|-------|-------|-----------------|-------|
| TS1           | 1.97; 1.97; 1.97; 1.97 | 1.34; 1.35; 1.28; 1.28 | 2.37; 2.44; 2.33; 2.61; 2.18 [0.16] | 1.80; 1.81; 1.73; 1.73 | 2.95; 3.06; 3.03; 3.03 | – | – |
| P             | 1.93; 1.93 [0.01] | 1.51; 1.52; 1.44; 1.44 | 1.40; 1.38; 1.37; 1.40; 1.39 [0.01] | 1.94; 1.98; 1.85; 1.85 | 2.88; 2.92; 2.98; 2.98 | 2.75; 2.76; 2.67; 2.75; 2.71 | – |
| TS2           | 2.01; 2.06; 2.05 | 1.68; 1.61; 1.50; 1.50 | 1.37 (1.72); 1.39 (1.70); 1.35 (1.62); 1.38 | 2.55; 2.64; 2.53; 2.37 | 2.84; 2.83; 2.90; 2.90 | 2.57; 2.80; 2.81; 2.53; 2.79 | – |
| T             | 1.94; 1.96; 1.92; 1.92 | 2.24; 2.24; 2.20; 2.20 | 1.53 (1.37); 1.54 (1.37); 1.47 (1.34); 1.51 | 2.91; 2.94; 2.76; 2.76 | – | 1.86; 1.87; 1.75; 1.88; 1.82 | – |
| TS2Ph         | 1.97; 1.98; 1.94; 1.94 | 2.03; 1.93; 2.02; 2.02 | 1.33; 1.30; 1.33; 1.33 [0.02] | 2.08; 2.27; 1.96; 1.96 | 1.84; 1.94; 1.85; 1.85 | – | – |
| PPh           | 1.95; 2.00 [0.02] | 2.04; 2.02; 2.04; 2.04 | 1.31; 1.28; 1.30; 1.33 [0.02] | 2.19; 2.48; 2.03; 2.03 | 1.50; 1.51; 1.46; 1.46 | – | – |
| TS2Cl         | 2.03; 2.02; 2.03 | 1.35; 1.36; 1.29; 1.29 | 2.27; 2.34; 2.25; 2.25 [0.13] | 1.82; 1.82; 1.75; 1.75 | 3.00; 3.05; 3.11; 3.11 | – | – |
| PCl           | 1.94; 1.93; 1.93; 1.93 | 1.53; 1.53; 1.46; 1.46 | 1.37; 1.35; 1.35; 1.38 [0.02] | 2.00; 2.14; 1.92; 1.92 | 3.12; 3.14; 3.20; 3.20 | (2.93); (2.89); (2.94); (2.94) | 2.36; 2.39; 2.31; 2.31 |
| TS2Cl         | 1.92; 1.95; 1.90; 1.90 | 2.31; 2.01; 2.08; 2.08 | 1.27; 1.26; 1.24; 1.28; 1.26 [0.02] | 2.50; 2.88; 2.45; 2.45 | – | (1.94); (2.08); (1.98); (1.98) | 2.72; 2.46; 2.39; 2.39 |
| TCl           | 1.91; 1.91; 1.90; 1.90 | 2.94; 2.88; 2.96; 2.96 | 1.29; 1.26; 1.25; 1.32; 1.29 [0.03] | 2.47; 2.91; 2.46; 2.46 | – | (1.84); (1.84); (1.71); (1.85); (1.82) [0.06] | 2.76; 2.49 [0.17] |
| TS2Cl_homo    | 1.98; 1.98; 1.96; 1.96 | 2.01; 1.85; 2.02; 2.02 | 1.30; 1.30; 1.26; 1.30; 1.31 [0.02] | 2.24; 2.35; 2.13; 2.13 | 1.84; 1.99; 1.85; 1.85 | – | 2.57; 4.85; 2.42; 2.42 |
| TCl_homo      | 1.99; 1.98 [0.01] | 2.00; 1.96 [0.07] | – | 2.19; 2.07 [0.11] | 1.80; 1.83 [0.07] | – | 2.49; 3.09 [1.02] |
| TS2Cl_homo    | 1.89; 1.86; 1.90; 1.90 | 2.54; 2.20; 2.11; 2.11 | 1.26; 1.24; 1.30; 1.29 [0.03] | 2.26; 2.17; 2.21; 2.21 | 2.81; 3.08 [0.11] | 1.52; 1.52; 1.48; 1.48 | – |
| TCl_homo      | 1.91 [0.02] | 2.36 [0.19] | – | 2.05 [0.09] | – | – | 2.33; 2.36; 2.27; 2.27 |
| TCl_homo      | 1.89; 1.90; 1.86; 1.86 | 2.85; 2.88; 2.84; 2.84 | 1.24; 1.22; 1.20; 1.25; 1.27 [0.03] | 2.36; 2.56; 2.26; 2.26 | – | – | 2.36; 2.41; 2.33; 2.33 |
| TCl_homo      | 1.88; 1.88 [0.02] | 3.87; 3.12 [0.44] | – | 2.31; 2.06 [0.18] | – | – | 2.37; 2.35 [0.03] |
of the P species varies with the functional, i.e., in the case of B3LYP or TPSSh it is connected with TS2_pC, whereas ωB97XD prefers TS2. Unfortunately, at present there are no experimental data to discriminate between these two alternatives, and both of them lead to generation of catalytic Cl⁻.

More quantitative comparison between the different computational models may be based on the numeric data gathered in Tables 1 and 2. From the enthalpy values (Table 1), one can notice that certain reaction energies and activation barriers are relatively insensitive to the variations of the methodology (differences within 5 kcal mol⁻¹), i.e., P → TS2, P → T, P → TS2_pC. On the other hand, several other barriers and reaction enthalpy values vary dramatically (differences above 10 kcal mol⁻¹) with the model, i.e., SCl → TS1_pC, SCl → P_sC, P_Cl → T_sC, P_Cl → TS2_pC, P_Cl → TS2_sC_homo, and P_Cl → T_sC_homo. Notably, the former set includes exclusively the reaction step for the parent system, whereas the latter set exclusively the derivative with Cu-bound Cl⁻, which might indicate that the presence of inorganic chloride makes the energy of the system more variable with the computational method used. Importantly, most of this variability comes from the change of the density functional. Indeed, if one compares the relative enthalpy values obtained with the three models based on the B3LYP functional, the differences are in almost all cases less than 5 kcal mol⁻¹, with the exceptions of P_Cl → T_sC_pC, P_Cl → TS2_sC_homo, and P_Cl → T_sC_homo, where the spread is 5.8, 5.5, and 5.1 kcal mol⁻¹, respectively. Nevertheless, including the solvent model or using a larger basis set in the optimization step affects both energies and geometries quite noticeably; hence, whenever it is practically feasible, it is recommended to use these more complete methods.

From analysis of key inter-atomic distances gathered in Table 2 and view of superimposed optimized structures (Fig. S1 and S2), it can be inferred that bond lengths and overall conformation of complexes may vary quite substantially with the computational method used. A larger geometrical variance seems to be correlated with a larger spread of energies. For example, one can compare TS2 and TS2_sC, i.e., two transition states for similar chemical transformations that proceed somewhat differently. For TS2 the variance of critical bond lengths, measured by standard deviation, is 0.08 Å for the O₁–O₂ bond, 0.06 Å for the C₂–Cl₁ bond, and 0.14 Å for the O₂–Cl₁ bond. For TS2_sC, the corresponding values are 0.14 Å for O₁–O₂, 0.19 Å for Cl₁–Cl₂, and 0.06 Å for O₁–Cl₂, i.e., larger for two out of three critical bonds. For the preceding species, i.e., P and P_sC, the variance of bond lengths is very comparable. The spread of computed values of enthalpy of activation are 4.6 and 7.3 kcal mol⁻¹ for TS2 and TS2_sC, respectively. Another example is T_sC_homo, which is characterized by large variability of bond lengths and for which the relative stability, measured by enthalpy of the P_Cl → T_sC_homo step, spans a range of 22.0 kcal mol⁻¹.

Conclusions

Stationary points defining coordinates of several elementary reactions were optimized, and their relative enthalpy values were computed with the use of five computational models. From the comparison of the reaction enthalpy profiles, one can conclude that using a basis set of triple-zeta quality or a PCM solvent model (acetonitrile) for geometry optimization causes the relative values to change by less than 6 kcal mol⁻¹. On the other hand, changing the functional, even within the hybrid subfamily, brings about more pronounced changes in relative enthalpy values, such that the predicted kinetically preferred product changes. In addition, a correlation between variability of the key bond lengths and enthalpy variance was noticed. In the context of the mechanisms of the reaction between S and O₂, the TPSSh-D3/BS3//TPSSh-D2/BS1 model is likely at odds with the available experimental data, since it predicts a kinetic preference for homolytic O–O bond cleavage, whereas the experimental evidence supports a process leading to triketone/hypochlorite, presumably via a heterolytic pathway.

Acknowledgments

This research was funded in part by the statutory research fund of ICSC PAS. This research was supported in part by PL-Grid Infrastructure. Computations were performed in the AGH Cyfronet Supercomputer Centre.

Open Access

This article is distributed under the terms of the Creative Commons Attribution 4.0 International License (http://creativecommons.org/licenses/by/4.0/), which permits unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.

References

1. Sam P. de Visser, François Ogliaro, Nathan Harris and, Shaik S (2001) Multi-state epoxidation of ethene by cytochrome P450: a quantum chemical study. J Am Chem Soc. https://doi.org/10.1021/ja003544+. 1
2. Werner H-J, Schütz M (2011) An efficient local coupled cluster method for accurate thermochemistry of large systems. J Chem Phys 135:144116. https://doi.org/10.1063/1.3641642 2
3. Nakatani N, Guo S (2017) Density matrix renormalization group (DMRG) method as a common tool for large active-space CASSCF/CASPT2 calculations. J Chem Phys 146:094116. https://doi.org/10.1063/1.4976644 3
4. Allpress CJ, Milacewicz A, Borowski T et al (2014) Halide-promoted Dioxygenolysis of a carbon–carbon bond by a copper(II) Diketone complex. J Am Chem Soc 136:7821–7824. https://doi.org/10.1021/ja502577b 4
5. Saraf SL, Milacewicz A, Borowski T et al (2016) Anion effects in oxidative aliphatic carbon–carbon bond cleavage reactions of Cu(II) chlorodiketone complexes. Inorg Chem 55:6916–6928. https://doi.org/10.1021/acs.inorgchem.6b00456 5
6. Becke AD (1993) Density-functional thermochemistry. III. The role of exact exchange. J Chem Phys 98:5648–5652. https://doi.org/10.1063/1.464913

7. Tao J, Perdew JP, Staroverov VN, Scuseria GE (2003) Climbing the density functional ladder: nonempirical meta–generalized gradient approximation designed for molecules and solids. Phys Rev Lett 91:146401. https://doi.org/10.1103/PhysRevLett.91.146401

8. Chai J-D, Head-Gordon M (2008) Long-range corrected hybrid density functionals with damped atom–atom dispersion corrections. Phys Chem Chem Phys 10:6615. https://doi.org/10.1039/b810189b

9. Grimme S (2006) Semiempirical GGA-type density functional constructed with a long-range dispersion correction. J Comput Chem 27:1787–1799. https://doi.org/10.1002/jcc.20495

10. Grimme S, Antony J, Ehrlich S, Krieg H (2010) A consistent and accurate ab initio parametrization of density functional dispersion correction (DFT-D) for the 94 elements H–Pu. J Chem Phys 132:154104. https://doi.org/10.1063/1.3382344

11. Frisch MJ, Trucks GW, Schlegel HB et al (2009) Gaussian 09, revision B.01. Gaussian, Inc., Wallingford

12. Yamaguchi K, Jensen F, Dorigo A, Houk KN (1988) A spin correction procedure for unrestricted Hartree-Fock and Möller-Plesset wavefunctions for singlet diradicals and polyradicals. Chem Phys Lett 149:537–542. https://doi.org/10.1016/0009-2614(88)80378-6

Publisher’s note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.