Photoelectron shake-ups as a probe of molecular symmetry: 4d XPS analysis of $I_3^-$ in solution†

Jesper Norell, ‡∗a Gilbert Grell, ‡b Oliver Kühn, ‡b Michael Odelius ‡a, ‡b and Sergey I. Bokarev ‡a, ‡b

A combination of multi-configurational restricted active space calculations with a Dyson orbital formalism has been applied for accurate simulations of 4d photo-electron spectra of the $I_3^-$ molecular ion. The analysis based on the occupation numbers of natural orbitals allowed to predict and rationalize the spectral fingerprints of solvent-induced nuclear asymmetry. In particular, it demonstrates how the nuclear asymmetry directly causes an increase of shake-up intensity. The relative intensity of shake-up and main features of the I 4d XPS spectrum could therefore serve as a simplified experimental observable of structural asymmetry, complementary to changes in the shape of the main spectral features.

1 Introduction

Photoelectron spectroscopy is one of the most powerful and widely applied experimental methods for studies of electronic structure of matter, which in the X-ray regime (XPS), by targeting of core-levels, constitutes an element-specific local probe around distinct atomic sites in molecules and complex materials.1 With the development of new delivering systems such as liquid jets combined with improved X-ray sources, XPS studies in the liquid phase have become increasingly viable to investigate the effects of solute–solvent interactions in e.g. electrolyte solutions2,3 and at liquid interfaces.4 Robust and detailed analysis of such experiments, however, often demands comparison to accurate theoretical simulations of spectra. Here, a crucial point is to predict and identify spectral signatures that are characteristic and yet readily detected in measurements, in addition to assigning and rationalizing the spectral features to facilitate an understanding of the underlying chemical and spectroscopic mechanisms.

As an important component in dye-sensitized solar cells, the electronic, structural and dynamic properties of $I_3^-$ in solution have been studied in great detail both with experimental5–7 and theoretical methods.8–12 These studies all demonstrate how the structure of the molecular ion and, in particular, its degree of nuclear asymmetry can be directly correlated with the varied strength of solvent–solute interaction in different solutions. In aqueous solution, the strong hydrogen bonding drives large amplitude asymmetrical stretches and charge localization, leading to an electronic structure more akin to an $I_2\cdot\cdot\cdot I^-$ configuration. The influence of hydrogen bonding is less pronounced in, e.g., ethanol and acetonitrile where the charge stays fairly delocalized over the whole moiety, [I–I–I]–, and structural symmetry is comparatively preserved. In previous work11,12 it has been demonstrated how the solvent-induced nuclear asymmetry may be evidenced from altered features of the main signal in 4d XPS measurements. Thus, $I_3^-$ constitutes an ideal model system to explore not only the possible effects of nuclear asymmetry on electrochemical functionality, but also its interplay with XPS intensities.

Due to a recent implementation by Grell et al.13 both main and shake-up XPS intensities can now be simulated within a Dyson orbital formalism with orbitals derived from the multi-configurational second order perturbation theory restricted active space method (RASPT2)14,15 that can account for the multitude of effects that may influence spectral intensities such as: various types of chemical bonding, multi-configurational character of states, dynamic correlation, scalar relativistic effects, and spin–orbit coupling. The development thereby directly enables extension of previous $I_3^-$ studies, with simulations of XPS spectra at an accuracy level that motivates theoretical predictions for possible future approval by experimental measurements. Complementarily, we also demonstrate in the current work how a framework for assignment and analysis, based on the multi-configurational Dyson orbital, may be conveniently formulated in terms of occupation numbers of the natural orbitals, to rationalize the predicted spectral trends.

‡ Department of Physics, AlbaNova University Center, Stockholm University, SE-106 91 Stockholm, Sweden. E-mail: jesper.norell@physik.su.se
† Electronic supplementary information (ESI) available: Motivation of sudden approximation via ezDyson 3.0 integration, extended definition of occupation numbers, multiplicity-decomposed spectrum, and the full set of relevant molecular orbitals. See DOI: 10.1039/c8cp02530d
2 Computational details

2.1 Molecular geometries

To study the principal influence of nuclear asymmetry on \( {I_3}^+ \) 4d XPS, spectral simulations were performed and compared for a symmetric and an asymmetrically stretched geometry. The symmetric geometry (representing \([I-I-I]\) as in e.g. EtOH solution) with 2.91 Å I-I bond lengths corresponds to a CASPT2(16,9) \( {I_3}^+ \) \([g]\) optimization.\(^7\) The linear asymmetric geometry (representing \(I_2\cdot\cdot\cdotI\)) with I-I bonds of 3.37 Å and 2.82 Å was chosen to have the largest asymmetric stretch among structures found in a number of previous molecular dynamic simulations of aqueous LiI\(_3\) solution.\(^11\)

2.2 Electronic structure calculations

The electronic wave function of the initial electronic state of \( {I_3}^- \) and the final core-ionized states of the neutral \( {I_3} \) were calculated on the RASSCF\(^{14} \) and RASPT\(^{15} \) levels, as implemented in the Molcas 8.0 program package.\(^16\) A RAS(15, 3; 34 e\(^-\), 1 h\(^+\)) active space was employed as illustrated in Fig. 1, i.e. 15 orbitals in the RAS1 space (one hole is allowed) and 3 orbitals in the RAS2 space (full CI) with a total of 34 active electrons (33 for the final states). The calculations were performed without explicit use of symmetry, a separate orbital constraint was, however, applied to the 15 4d orbitals to exclude orbital rotation with other occupied valence orbitals. Thereby, we ensure core-rather than valence-excitation in the final state calculation. Solvent effects, beyond their impact on the nuclear geometry, were not included in the calculations; previous work has, however, demonstrated the effects of explicit water solvation to mainly result in additional broadening and altered absolute shift of the XPS spectrum.\(^14\)

For the molecular ion \( {I_3}^- \) (i.e. the initial states of the XPS process), both the singlet ground state and the first triplet spin-free (pure multiplicity) states were calculated. For the neutral molecule \( {I_3} \) (i.e. the final states of the XPS process), all possible spin-free states were calculated within the state averaging formalism, namely 143 doublets (135 core-ionized) and 46 quartets (45 core-ionized). Subsequent multi-state RASPT2 calculations were carried out with an imaginary shift of 0.2 Hartree to accelerate convergence. For the doublet \( {I_3}^- \) calculations of the asymmetric geometry, the 10 states with highest energy were excluded from the multi-state RASPT2 due to the intruder states problems; this does not significantly affect the results as these states anyway fail outside the XPS energy range analyzed in the current work. Scalar relativistic effects were included via a Douglas–Kroll (DK) Hamiltonian\(^{17,18} \) and the relativistically contracted ANO-RCC-VTZP\(^{19} \) basis set. Spin–orbit coupling was included through the restricted active space state interaction (RASSI) method,\(^{20,21} \) via atomic mean field integrals\(^{22} \) with the electron repulsion integrals approximated through a density-fitting procedure.\(^{23-25} \)

2.3 XPS intensities

XPS intensities were obtained within a Dyson orbital (DO) formalism, as described in detail in previous work.\(^13\) In short, for the initial state \( i \) and final bound state of the ionized system \( f \) with the respective \( N \) and \( N - 1 \)-electron wave functions \( \psi_i^N \) and \( \psi_f^{N-1} \), the electron photoelectron matrix element can be written as

\[
D_{fi} = \langle \psi_f^{N-1} | \hat{d} | \psi_i^N \rangle = \langle \psi_f^1 \rangle | \hat{d} | \phi_{fi}^{DO} \rangle. \tag{1}
\]

Here, \( \psi_f^1 \) is the photo-electron wave function (k its momentum), \( \hat{d} \) the electronic dipole operator, and \( \phi_{fi}^{DO} \) stands for the one-electron DO

\[
\phi_{fi}^{DO} (x_N) = \sqrt{N} \int \psi_f^{N-1} (x_1, x_2, \ldots, x_{N-1})
\times \psi_i^1 (x_1, x_2, \ldots, x_N) \, dx_1 \, dx_2 \ldots \, dx_{N-1} \tag{2}
\]

that (after normalization) formally corresponds to the wave function of the photo-electron prior to the ionization. With \( \phi_{fi}^{DO} \) obtained from the quantum chemical calculation the spectral intensity of the transition \( i \rightarrow f \) is proportional to \( |D_{fi}|^2 \).

The results of the current work are all obtained within the sudden approximation (SA) where the energy (and thus k) dependence of \( \psi_f^1 \) is neglected to obtain

\[
|D_{fi}|^2 = \langle |\psi_f^1(k)| \hat{d} |\phi_{fi}^{DO} \rangle^2 \propto ||\phi_{fi}^{DO}||^2 \tag{3}
\]

where the proportionality constant is taken to be the same for all transitions.

The SA is well justified for our present comparison to experiments performed with 600 eV photon energies as shown
in ESI,† Section S1. This fact allowed us to avoid the most demanding step of computing transition matrix elements with continuum functions. We emphasize, however, that the approximation cannot be trivially assumed to hold equally well for other systems and binding energy ranges. Therefore, we advocate a case by case validation also in future studies.

All XPS transitions were shifted by 2.9 eV (1.5 eV at RASSCF level) and rescaled to align the main feature of the spectrum for the symmetric geometry to the experiment. The discrete XPS intensities from the calculations were convoluted with a Gaussian function with full-width-half-maximum of 1.1 eV, previously shown to yield good agreement with experiments. 11

2.4 Assignment and analysis

The DO formalism constitutes a convenient framework for assigning XPS transitions within a molecular orbital picture. The multi-configurational DO carries information both about the photo-electron and shake-up excitations in the molecular system, as may be expressed in terms of occupation numbers of the natural orbitals. For a multi-configurational state \( \Psi_f \), an occupation vector

\[
\mathbf{n}_f = (\text{occ}_1(\phi_1), \text{occ}_2(\phi_2), \ldots, \text{occ}_M(\phi_M))
\]  

may be defined from the occupation numbers of the \( M \) active molecular orbitals \( \{\phi_i\} \), where the components sum to the total number of active electrons. Similarly, an occupation-like vector

\[
\mathbf{n}^{DO}_f = (|\langle \phi_1 | \text{DO} \rangle|, |\langle \phi_2 | \text{DO} \rangle|, \ldots, |\langle \phi_M | \text{DO} \rangle|)
\]  

may be defined for the normalized DO, which carries information about the contributions of different active orbitals \( \{\phi_i\} \) to the photo-electron prior to the ionization, where the components instead sum to one. In other words, in a description accounting for electron correlation, the normalized DO corresponds to a quasiparticle, with a wave function being a superposition of initial state active molecular orbitals. Due to electron correlation (i.e. multi-configurational character of the initial and/or final states), ionization may additionally be accompanied by electronic shake-up (and shake-down) excitations in the molecular system as expressed in the residual occupation vector

\[
n^{res}_i = n^{DO}_i - n^n_i.
\]  

In a frozen-orbital approximation, the residual occupation is the zero vector for main lines (single-electron ionization). In contrast, for shake-up transitions it contains the occupation change due to the electronic excitations accompanying one-electron ionization. In the present case, with a multi-configurational self-consistent field method, both the DO and residual occupations are additionally affected by the orbital relaxation upon photo-ionization, i.e. the basis of orbitals \( \{\phi_i\} \) may differ for the initial and final states. Consequently, occupation number analysis is complicated by the possible differences in orbital bases for the \( I_3^- \) and \( I_3 \) species. As shown below, this effect is mainly seen for the asymmetric geometry.

3 Results and discussion

3.1 Comparison to experimental spectra

In Fig. 2(a), the spectra of the symmetric and asymmetric geometries simulated at the RASPT2 level are compared to the reported experimental \( I_3^- \) 4d signal in EtOH solution. 11 Firstly, comparison of the symmetric geometry and the experiment shows that the simulation protocol accurately reproduces both the main and shake-up features. Secondly, comparison of the XPS for symmetric and asymmetric geometries indicates the influence of solvent-induced nuclear asymmetry: while the peak positions are quite similar for both geometries, the asymmetry manifests itself in the changes in shape of the main peaks positions are quite similar for both geometries, the asymmetry manifests itself in the changes in shape of the main peaks positions are quite similar for both geometries, the asymmetry manifests itself in the changes in shape of the main...
features and the increased shake-up intensity. The spectral features are assigned and the observed trends are rationalized through occupation number analysis in Section 3.2.

In the available experimental studies for EtOH and aqueous solutions aiming at the analysis of the main signal, Li was used as a counter ion. As the Li 1s direct ionization spectrally overlaps with the I 4d shake-up features, the Li 1s signal had to be subtracted from the total measured spectrum to obtain the I 4d signal, as presented for EtOH in Fig. 2. In aqueous solution, further subtraction of I $^1$ and I $^3$ signal components was also necessary. This leaves too large uncertainties for a quantitative comparison, as indicated by the highly differing overlaps with the I3 and I2 signal components.

For the asymmetric geometry there are instead 10 stable circumstances enabled by, aimed also at shake-up analysis, may be performed under more aqueous solution and hope that potential future experiments, therefore refrain from direct comparison of our simulations to aqueous solutions aiming at the analysis of the main signal, 11 Li$^+$ was used as a counter ion. As the Li 1s direct ionization spectrally overlaps with the I 4d shake-up features, the Li 1s signal had to be subtracted from the total measured spectrum to obtain the I 4d signal, as presented for EtOH in Fig. 2. In aqueous solution, further subtraction of I $^1$ and I $^3$ signal components was also necessary. This leaves too large uncertainties for a quantitative comparison, as indicated by the highly differing overlaps with the I3 and I2 signal components.

We therefore refrain from direct comparison of our simulations to aqueous solution and hope that potential future experiments, aimed also at shake-up analysis, may be performed under more stable circumstances enabled by, e.g., a different choice of counter ion and I$^+$/I$^-$ ratio.

For comparison to the RASPT2 results, XPS spectra were also simulated directly from the RASSCF electronic states; the results for the symmetric geometry are shown in Fig. 2(a). While the main features of the spectra are nearly identical at the two levels of theory, the shake-up features are highly over-estimated both in terms of intensity and energetic distance from the main features. The effect can therefore be ascribed to the limited account for electron correlation provided by the active space. However, the current RASSCF calculations cannot be straightforwardly improved through inclusion of further valence orbitals, due to the already high computational cost of the setup with 15 $\times$ 4d core-orbitals that is necessary to describe the XPS process. The accurate simulation and analysis of shake-up features is thereby directly enabled by the multi-configurational second order perturbation theory and would not be possible at reduced computational level.

3.2 XPS assignment and occupation number analysis

The XPS features obtained at RASPT2 level for the symmetric and asymmetric geometry are assigned and rationalized through occupation number analysis, as visualized in Fig. 3. The DO (n$^0_{\text{DO}}$) and residual occupations (n$^0_{\text{res}}$) (see eqn (6)) are shown in the panels in the left (a and c) and right (b and d) columns, respectively. Upper row of panels (a and b) corresponds to the symmetric and lower row (c and d) to the asymmetric geometries. In each panel, the respective occupation vector for a particular transition energy (x-axis) represents a vertical slice. Different segments of these slices (y-axis) correspond to the active molecular orbitals.

Important for the analysis of spectral changes is to distinguish between different types of orbitals. The 15 $\times$ 4d orbitals can be grouped together based on their atomic site localization, with representative examples shown in Fig. 1. We denote them as 10 $\times$ central 4d(c) and 5 $\times$ terminal 4d(t) for the symmetric geometry. For the asymmetric geometry there are instead 5 $\times$ ionic orbitals 4d(i) localized on I $^+$, and 5 $\times$ central 4d(c) and 5 $\times$ terminal 4d(t) orbitals of I $^-$. Crucial for the current work is also an understanding of shake-up effects due to 5p $\rightarrow$ 5p valence excitations. Three combinations of symmetrized 5p orbitals are present for the symmetric geometry, which we denote as bonding 5p$^z$ (HOMO), non-bonding 5p$^x$ (HOMO-1) and anti-bonding 5p$^y$ (HOMO-2). Note that the inversion symmetry parity labels ‘g’ and ‘u’ are only applicable for the symmetric geometry. For the asymmetric geometry, the 5p orbitals instead form a non-bonding orbital 5p$^z$ on the I $^-$ ion, and the bonding 5p$^z$ and anti-bonding 5p$^y$ combinations for the I $^+$ moiety.

For the symmetric geometry, the main features of the 4d spectrum can be assigned to ionization from orbitals localized mainly on either the terminal 4d(t) or central 4d(c) sites in accordance with previous calculations. Each type of orbital gives rise to two features separated by spin–orbit splitting of 1.6 eV between the 4d$^{3/2}$ and 4d$^{5/2}$ levels, seen as two parallel vertical lines in the occupations (Fig. 3a) near −53.6 eV and −55.2 eV (terminal) and, respectively, near −55.1 eV and −56.7 eV (central). The overlap of transitions near −55 eV gives effectively rise to three main features in the spectrum. Further, two distinct shake-up features are found near −59.3 eV and −60.8 eV. As can be seen from the DO occupations (Fig. 3a), only ionization from the terminal sites is involved in these transitions; their intrinsic energy splitting is the same spin-orbit splitting as for the main features, while their distance from the main peaks is the result of the 5pn$^z$ (HOMO) to 5p$^y$ (LUMO) shake-up excitation that can be confidently assigned from the clear transfer of occupation between these two orbitals in the associated residual occupations (Fig. 3b). The assignment can be rationalized through an inversion-symmetry argument previously given for the I 3d XPS spectrum of triiodide by Arbman et al. that emphasizes the crucial impact of nuclear and electronic symmetry on shake-up features: shake-up excitation from gerade to ungerade orbitals is symmetry forbidden to occur together with ionization from central site orbitals, due to their gerade symmetry. The shake-up excitation is, however, allowed in combination with core-ionization at the terminal sites, as localization of the core-hole to either terminal site breaks the electronic symmetry in the final state. Shake-up features associated with central site ionization are instead seen at much lower intensity near −65.1 eV and −66.7 eV, i.e. at energies associated with the 5p$^z$ (HOMO−4) to 5p$^y$ (LUMO) excitation of parity-conserving ungerade to ungerade character.

Main feature assignments at the asymmetric geometry are also well described by the previous grouping of 4d orbitals. Assignment from the DO occupations (Fig. 3c) evidences dominant photo-ionization from the ionic site 4d(i) at 1.3 eV to 2.0 eV higher (−53.4 eV and −55.0 eV) rather than from the terminal 4d(t) (−54.8 eV and −56.3 eV) and central site 4d(c) (−55.4 eV and 56.9 eV), as explained by localization of surplus negative charge on the I $^-$ site. The single exception is a weak feature (less than 0.05 of maximal intensity) near −51.6 eV, ascribed to ionization from the central site 4d(c), rationalized in ESI, S2.3. We note that while the characters and the order of the 5p orbitals are essentially preserved upon ionization in the symmetric geometry, this is not the case for the asymmetric geometry. Hence, we conclude that the frozen orbital approximation (initially assumed
Occupation number analysis (for occupation number analysis) is clearly violated. This is a crucial aspect for the assignment of the shake-up excitations. As can be seen from the full set of orbitals for both the $I_3^-$ and $I_1$ species shown in the ESI,† Section S1 and Fig. S3, the ionic $5n^0$ orbitals (HOMO) and bonding $5\sigma^2$ (HOMO−7) orbitals permute their order, and the ionic orbital relaxes from an anti-bonding to bonding character towards the $I_2$ part, upon photo-ionization. This type of difference in orbital bases invalidates a straightforward comparison of initial and final states, and thereby makes simple characterization of shake-ups transitions in terms of e.g. HOMO, LUMO, etc. impossible. The effect is clearly seen in the residual occupations (Fig. 3d), with strong contributions present even within the nominal main peaks of the spectrum. Nevertheless, the intense shake-up features near −59.0 eV and −60.6 eV can be clearly associated with ionization from all three sites, based on their DO occupations (Fig. 3c), which are expressed exclusively in the initial state orbital basis. Thus, the symmetry limitations introduced for these features in the symmetric geometry are lifted, which directly explains their increased absolute intensity.

Based on comparison and rationalization of the symmetric and asymmetric spectra, it is clear that the degree of nuclear asymmetry is directly reflected in the relative intensity of main and shake-up features: integrating the XPS intensities between $−50$ eV to $−57.5$ eV (main features) and, respectively, $−57.5$ eV to $−62$ eV (shake-up features) one obtains the two highly different ratios of 9.6% for shake-up-to-main intensity ratio in the symmetric spectrum and 24.2% in the asymmetric spectrum. This theoretical prediction thus suggests a single scalar observable evidencing solvent-induced nuclear asymmetry in the $I_3^-$ ion. It could be conveniently extracted from experimentally measured 4d XPS spectra given an appropriate choice of counter ion. This simplifies the analysis otherwise often based on a complete comparison of spectral features.
4 Conclusion

In summary, our RASPT2 calculations combined with a DO formalism can accurately reproduce $1s^{-1}4d$ XPS spectra, which allows us to predict the influence of nuclear asymmetry on XPS intensities and, in particular, shake-up features. Based on an analysis of natural orbital occupation numbers, we assign an increased shake-up intensity upon asymmetric stretching to result from the break-down of inversion-symmetry dependent selection rules for XPS transitions. The ratio of shake-up-to-main feature intensities could thereby serve as a simple scalar quantity to measure nuclear asymmetry in $1s^{-1}$ with 4d XPS. This example demonstrates how the high accuracy of RASPT2 calculations can be utilized for theoretical predictions of XPS spectra, and motivates future experimental measurements of $1s^{-1}$ in solution to further elucidate the influence of solvent-induced symmetry breaking.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

JN and MO acknowledge financial support from the Helmholtz Virtual Institute VI419 “Dynamic Pathways in Multidimensional Landscapes”. MO also acknowledges financial support from the Swedish Research Council (Contract 2015-03956) and the Swedish Energy Agency (Contract 2017-00679). SIB acknowledges financial support from Deutsche Forschungsgemeinschaft (Grant No. BO 4915/1-1). We thank Ida Josefsson for stimulating and productive discussions.

References

1 K. Siegbahn, C. Nordling and A. Fahlman, ESCA, atomic, molecular and solid state structure studied by means of electron spectroscopy, Almqvist and wicksell tecnological review, 1967.
2 B. Winter and M. Faubel, Chem. Rev., 2006, 106, 1176–1211.
3 R. Golnak, S. I. Bokarev, R. Seidel, J. Xiao, G. Grell, K. Atak, I. Unger, S. Thürmer, S. G. Aziz, O. Kühn, B. Winter and E. F. Aziz, Sci. Rep., 2016, 6, 24659.
4 O. Björnholm, M. H. Hansen, A. Hodgson, L.-M. Liu, D. T. Limmer, A. Michaelides, P. Pedevilla, J. Rossmeisl, H. Shen, G. Tocci, E. Tyrode, M.-M. Walz, J. Werner and H. Bluhm, Chem. Rev., 2016, 116, 7698–7726.
5 A. E. Johnson and A. B. Myers, J. Phys. Chem., 1996, 100, 7778–7788.
6 K. H. Kim, J. H. Lee, J. Kim, S. Nozawa, T. Sato, A. Tomita, K. Ichiyanagi, H. Ki, J. Kim, S.-i. Adachi and H. Ihee, Phys. Rev. Lett., 2013, 110, 165505.
7 S. K. Eriksson, I. Josefsson, N. Ottosson, G. Öhrwall, O. Björnholm, H. Siegbahn, A. Hagfeldt, M. Odelius and H. Rensmo, J. Phys. Chem. B, 2014, 118, 3164–3174.
8 C. Margulis, D. Coker and R. Lynden-Bell, Chem. Phys. Lett., 2001, 341, 557–560.
9 F. S. Zhang and R. M. Lynden-Bell, Phys. Rev. Lett., 2003, 90, 185505.
10 C. Margulis, D. Coker and R. Lynden-Bell, J. Chem. Phys., 2001, 114, 367–376.
11 I. Josefsson, S. K. Eriksson, N. Ottosson, G. Öhrwall, H. Siegbahn, A. Hagfeldt, H. Rensmo, O. Björnholm and M. Odelius, Phys. Chem. Chem. Phys., 2013, 15, 20189–20196.
12 N. K. Jena, I. Josefsson, S. K. Eriksson, A. Hagfeldt, H. Siegbahn, O. Björnholm, H. Rensmo and M. Odelius, Chem. – Eur. J., 2015, 21, 4049–4055.
13 G. Grell, S. I. Bokarev, B. Winter, R. Seidel, E. F. Aziz, S. G. Aziz and O. Kühn, J. Chem. Phys., 2015, 143, 074104.
14 P. A. Malmqvist, A. Rendell and B. O. Roos, J. Phys. Chem., 1990, 94, 5477–5482.
15 P. A. Malmqvist, K. Pierloot, A. R. M. Shahi, C. J. Cramer and L. Gagliardi, J. Chem. Phys., 2008, 128, 204109.
16 F. Aquilante, J. Autschbach, R. K. Carlson, L. F. Chibotaru, M. G. Delcey, L. De Vico, I. Fdez Galván, N. Ferré, L. M. Frutos, L. Gagliardi, M. Garavelli, A. Giussani, C. E. Hoyer, G. Li Manni, H. Lischka, D. Ma, P. A. Malmqvist, T. Müller, A. Nenov, M. Olivucci, T. B. Pedersen, D. Peng, F. Plaßler, B. Pritchard, M. Reiher, I. Rivalta, I. Schapiro, J. Segarra-Martí, M. Stenrup, D. G. Truhlar, L. Ungur, A. Valentinzi, S. Vancolle, V. Veryazov, V. P. Vysootskiy, O. Weingart, F. Zapata and R. Lindh, J. Comput. Chem., 2016, 37, 506–541.
17 M. Douglas and N. M. Kroll, Ann. Phys., 1974, 82, 89–155.
18 B. A. Hess, Phys. Rev. A: At., Mol., Opt. Phys., 1986, 33, 3742–3748.
19 B. O. Roos, R. Lindh, P. Å. Malmqvist, V. Veryazov and P. O. Widmark, J. Phys. Chem. A, 2004, 108, 2851–2858.
20 P.-Å. Malmqvist and B. O. Roos, Chem. Phys. Lett., 1989, 155, 189–194.
21 P. Å. Malmqvist, B. O. Roos and B. Schimmelpennig, Chem. Phys. Lett., 2002, 357, 230–240.
22 B. A. Hess, C. M. Marian, U. Wahlgren and O. Gropen, Chem. Phys. Lett., 1996, 251, 365–371.
23 F. Aquilante, T. B. Pedersen and R. Lindh, J. Chem. Phys., 2007, 126, 194106.
24 F. Aquilante, P.-Å. Malmqvist, T. B. Pedersen, A. Ghosh and B. O. Roos, J. Chem. Theory Comput., 2008, 4, 694–702.
25 J. Boström, M. G. Delcey, F. Aquilante, L. Serrano-Andrés, T. B. Pedersen and R. Lindh, J. Chem. Theory Comput., 2010, 6, 747–754.
26 M. Arman, S. Holmberg, M. Lundholm, H. Siegbahn, O. Gropen and U. Wahlgren, Chem. Phys., 1983, 81, 113–119.