Evolution of Disc Thickness in Simulated High-Redshift Galaxies

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ABSTRACT
We study the growth of stellar discs of Milky Way-sized galaxies using a suite of cosmological simulations. We calculate the half-mass axis lengths and axis ratios of stellar populations split by age in galaxies with stellar mass $M_*=10^7-10^{10} M_\odot$ at redshifts $z > 1.5$. We find that in our simulations stars always form in relatively thin discs, and at ages below 100 Myr are contained within half-mass height $z_{1/2} \sim 0.1$ kpc and short-to-long axis ratio $z_{1/2}/x_{1/2} \sim 0.15$. Disc thickness increases with the age of stellar population, reaching median $z_{1/2} \sim 0.8$ kpc and $z_{1/2}/x_{1/2} \sim 0.6$ for stars older than 500 Myr. We trace the same group of stars over the simulation snapshots and show explicitly that their intrinsic shape grows more spheroidal over time. We identify a new mechanism that contributes to the observed disc thickness: rapid changes in the orientation of the galactic plane mix the configuration of young stars. The frequently mentioned "upside-down" formation scenario of galactic discs, which posits that young stars form in already thick discs at high redshift, may be missing this additional mechanism of quick disc inflation. The actual formation of stars within a fairly thin plane is consistent with the correspondingly flat configuration of dense molecular gas that fuels star formation.

Key words: galaxies: formation — galaxies: high redshift — galaxies: kinematics and dynamics — galaxies: star formation — galaxies: structure

1 INTRODUCTION

The stellar disc of the Milky Way (MW) galaxy shows two distinct geometric components, the thin disc and the thick disc, with characteristic scale heights ~0.3 kpc and 0.9 kpc, respectively (Juric et al. 2008). Similar thin disc plus thick disc structure is also observed in other nearby galaxies (e.g. Reddy et al. 2006; Yoachim & Dalcanton 2008a,b). The MW thin and thick discs differ in chemical abundances (Bensby et al. 2005) – the thin disc being more metal rich with lower [$\alpha$/Fe], and the thick disc being more metal poor with higher [$\alpha$/Fe] – suggesting that the thin disc is mainly composed of relatively young stars, while the thick disc mainly of old stars. The typically quoted axis ratios of the thin and thick discs are ~ 0.1 and 0.4, respectively (e.g., Bovy & Rix 2013; Bensby et al. 2011). Results of massive spectroscopic surveys such as APOGEE suggested that instead of a clear separation between the thin and thick discs, the MW structure may be better described by a superposition of many mono-abundance populations, each with a single exponential scale height and scale length (Bovy et al. 2012, 2016). For older populations, indicated by lower metallicity and enhanced [$\alpha$/Fe], the scale heights monotonically increase with age (from ~200 pc to 1 kpc), while the scale lengths decrease (from ~4.5 kpc to 2 kpc).

The disc structure has also been studied at high redshift. Unlike the regular thin discs seen at low redshift, high-redshift galaxies show thick discs which are often clumpy (e.g. Elmegreen et al. 2007; Overzier et al. 2010; Swinbank et al. 2010). Chain and spiral galaxies in the Hubble Space Telescope (HST) Ultra Deep Field have the ratio of scale height to radial scale length ~ 1/3 (Elmegreen & Elmegreen 2006). Elmegreen et al. (2017) found the scale heights of galaxies in the HST Frontier Fields Parallels to increase with galaxy mass and decrease with redshift. They noted that clump regions have smaller scale height, and that the thick disc is observed best between the clumps, with a larger scale height. The overall evolution of galaxy shape appears to transform galaxies from prolate and spheroidal shapes at high redshift to thin discs at low redshift (Law et al. 2012; van der Wel et al. 2014; Zhang et al. 2019).

Current cosmological simulations successfully reproduce the observations that the present day distribution of young stars is thinner than that of old stars, and that galaxy discs are thicker at high redshift (e.g. Bird et al. 2013; Pillepich et al. 2019; Buck et al. 2020). However, the origin of such a transition from thick to thin discs, and how stars form in thick discs at high redshift, is still actively debated.

There are several scenarios that attempt to explain the formation of thick discs. One posits that the old stellar populations formed thick and kinematically hot at high redshift (e.g. Tutukov et al. 2000; Bird et al. 2013; Stinson et al. 2013), as mono-age or mono-abundance populations in simulations show thicker and shorter discs at birth. Other scenarios suggest that stars always form in thin discs and are heated to larger heights because of scattering by massive clumps (Bournaud et al. 2009; Comeron et al. 2011, 2014;
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Beraldo e Silva et al. (2020) or radial migration (Schönrich & Binney 2009; Loebman et al. 2011). The third type of studies suggest that thick discs are related to galaxy mergers, including heating of a thin disc in a merger, direct accretion of stars from satellite galaxies, and star formation in merging gas-rich systems (e.g. Reddy et al. 2006). Considering that mergers are more frequent at high redshift, these scenarios may lead to thicker discs of old stellar populations.

In this paper, we revisit the evolution of galactic disc thickness with stellar age, taking advantage of a recent suite of cosmological simulations of MW-sized galaxies with ultrahigh resolution. We test whether young stars actually form in thin discs and how quickly the scale height grows with stellar age. In Section 2 we describe the simulations and how we calculate the shape of the simulated galaxies. We present the evolution of thickness of our simulated galaxies with stellar age in Section 3. We compare our results with observations and other simulations and discuss the factors that contribute to the thickening of galactic discs in Section 4, and present our conclusions in Section 5.

2 SHAPE OF HIGH-REDSHIFT GALAXIES

2.1 Simulation Suite

We use a suite of cosmological simulations run with the Adaptive Refinement Tree (ART) code (Kravtsov et al. 1997; Kravtsov 1999, 2003; Rudd et al. 2008) and described in Li et al. (2018) and Meng et al. (2019). All runs start with the same initial conditions in a periodic box of 4 comoving Mpc, producing a main halo with total mass $M_{200} \sim 10^{12} M_\odot$ at $z = 0$, similar to that of the MW. The ART code uses adaptive mesh refinement to reach higher spatial resolution in dense regions. The lowest resolution is set by the root grid, which has $128^3$ cells. This sets the dark matter particle mass $m_{\text{DM}} \approx 10^7 M_\odot$. The finest refinement level is adjusted in runtime to keep the physical size of gas cells on that level between 3 and 6 pc. Because of strong stellar feedback, few cells remain at this finest refinement level and the typical spatial resolution of molecular gas is 36-63 pc.

The simulations include three-dimensional radiative transfer using the Optically Thin Variable Eddington Tensor approximation (Gnedin & Abel 2001) of ionizing and ultraviolet (UV) radiation from stars (Gnedin 2014) and the extragalactic UV background (Haardt & Madau 2001), non-equilibrium chemical network that calculates the ionization states of hydrogen and helium, and phenomenological molecular hydrogen formation and destruction (Gnedin & Kravtsov 2011). The simulations incorporate a subgrid-scale model for unresolved gas turbulence (Schmidt et al. 2014; Semenov et al. 2016). Star formation is implemented with the continuous cluster formation (CCF) algorithm (Li et al. 2017), where each stellar particle represents a star cluster that forms at a local density peak and grows its mass via accretion of gas and star formation until feedback of its own stars terminates the growth. The feedback recipe includes early radiative and stellar wind feedback, as well as a supernova (SN) remnant feedback model (Martizzi et al. 2015; Semenov et al. 2016). The momentum feedback of the SN remnant model is boosted by a factor $f_{\text{boost}} = 5$ to compensate for the underestimation due to numerical discreteness of the isolated SN model and to match the star formation history expected from abundance matching. The simulations include several runs with different values of the local star formation efficiency (SFE) per free-fall time, which ranges from $\epsilon_{\text{ff}} = 10\%$ to 200\%. For a full description of the star formation and feedback recipe, see Li et al. (2017, 2018) and Li & Gnedin (2019).

The simulations are run to $z \approx 1.5$. The high-redshift galaxies in our simulations are turbulent and irregular. They show prolate shape and contain clumps of young stars, consistent with the observed high-redshift clumpy galaxies. We remind the reader that these galaxies are unlike the regular galaxies at low redshift with a thin rotating disc and central bulge. Instead, the high-redshift galaxies are rather more irregular and dominated by turbulence.

Apart from the fiducial runs with $f_{\text{boost}} = 5$, our simulation suite also includes a weaker feedback run with $f_{\text{boost}} = 3$. The weaker feedback run produces a much higher stellar mass than expected from abundance matching and has a thin rotating disc even at high redshift. We do not consider that run as realistic and exclude it from analysis in this paper. More details about the structure of our simulated galaxies are given in Meng et al. (2019) and Meng & Gnedin (2020).

In this paper we analyze four runs that used different values of $\epsilon_{\text{ff}}$. The number after “SFE” in the run name corresponds to the percentage of local $\epsilon_{\text{ff}}$. At redshifts $z \approx 2 - 5$, there is one main galaxy and several smaller galaxies. We investigate the structure of the main galaxy and other isolated galaxies with stellar mass above $10^7 M_\odot$.

2.2 Measurements of galaxy shape

To measure galaxy shape, first we need to define the extent of a central galaxy and eliminate possible effects of satellites and galaxy mergers. For this purpose we calculate galaxy properties in a sphere centered on the galaxy center with radius 10 kpc for $z < 5$ galaxies, and 5 kpc for $z > 5$ galaxies. This covers most of the stellar distribution of our galaxies.

We examined the robustness of this choice by evaluating several alternative radial cuts. We determined the stellar extent of the galaxies by identifying a local minimum $r_{\text{min}}$ in the spherically-averaged mass profile $M(r)/dr$. If the profile decreases with $r$ and then begins to increase again, it means there is another stellar structure such as a satellite galaxy. We use $r_{\text{min}}$ as one of alternative radial cuts. The median of these radii is about 10 kpc for $z < 5$ galaxies, and 5 kpc for $z > 5$ galaxies, which informs our final choice. The other alternative we tried is 20 kpc for $z < 5$ galaxies, and 10 kpc for $z > 5$ galaxies, which is close to the extent of the largest galaxies in high-redshift observations (e.g. Elmegreen et al. 2017).

We found that for most of our simulated galaxies, choosing different maximum radius has little effect on the determination of galaxy orientation or stellar scale lengths along all axes. Using these alternative radial cuts results in the median fractional difference in the half-axis lengths smaller than 0.1 dex, and the orientation of the majority of galaxies changes by less than 1 degree.

We study all isolated (also referred to as central to their dark matter halo) galaxies, which are located outside of virial radii of other galaxies. The number of stellar particles in a galaxy ranges from a few hundred for galaxies with $M_\ast \sim 10^7 M_\odot$ to several million for galaxies with $M_\ast \sim 10^{10} M_\odot$. We require galaxies to have $M_\ast > 10^7 M_\odot$ so that they contain at least 100 stellar particles for the shape analysis to be reliable.

For the purpose of comparison with observational samples, different stages in the evolution of a given simulated galaxy can be considered uncorrelated if they are separated by a long enough time. We choose the separation between simulation snapshots based on the dynamical time calculated at the typical largest extent of stellar distribution, which is $R/V_{\text{circ}} \sim 60 - 100$ Myr. We wish to use the snapshots separated by at least two dynamical times. The time
Figure 1. Stellar mass of simulated galaxies vs. cosmic time and redshift in the simulation snapshots selected for analysis. In addition to the main galaxy, each snapshot contains several smaller isolated galaxies.

Figure 2. Intrinsic axis ratios of stellar populations of different age. Points with error bars show the median and interquartile ranges of stars in a given age bin for all galaxies in our sample. For most galaxies, the stellar distribution transitions from prolate to more spheroidal shape as stellar age increases.

interval between our snapshots is $\sim 150$ Myr at $z < 5$ and $\sim 100$ Myr at higher redshift, thus we select one in every two snapshots. This results in separation of $200 - 300$ Myr between the analyzed epochs.

We show the galaxy stellar mass and cosmic time of our sample in Figure 1. Each point corresponds to an isolated galaxy at a selected snapshot. One can see two relatively large galaxies and several smaller galaxies at these epochs.

High-redshift galaxies often show irregular shapes unlike axisymmetric discs observed at low redshift, and they are often dominated by turbulent motions instead of rotation. Therefore, following Meng et al. (2019) we use the shape tensor (Zemp et al. 2011) to determine the orientation of our simulated galaxies:

$$I = \sum_{k,i,j} M_k r_{k,i} r_{k,j} \mathbf{e}_i \otimes \mathbf{e}_j,$$

where $M_k$ is the mass of $k$-th stellar particle, $r_{k,i}$ are its coordinates in the galactocentric reference frame ($i = 1, 2, 3$), and $\mathbf{e}_i$ are the three unit vectors of the coordinate axes. The tensor can be diagonalized by a rotation matrix to obtain the principal moments of inertia $I_1 \geq I_2 \geq I_3$. From these we calculate the axis ratios $b/a$ and $c/a$.

Figure 3. Disc half-mass height of stellar populations split by age. Galaxies in the four runs are shown by the same symbols as in Figure 1. Lines show median values of $z_{1/2}$ in bins of galaxy mass. For the youngest stars the disc height increases with galaxy mass, but at ages above 100 Myr the median height is independent of mass.

For all subsequent analysis we fix a single orientation for a given galaxy, as it would be assigned in observation. We choose the plane orientation based on the shape tensor of stars younger than 100 Myr, because they contribute most of the observable rest-frame UV light. We then transform the coordinates of stellar particles into the new coordinates given by the adopted orientation.

We use half-mass axis lengths to describe the thickness of different components of our galaxies. The half-mass axis length is calculated as the length that contains half the cumulative mass along a given direction: $M(|x| < x_{1/2}) = \frac{1}{2} M_{\text{tot}}$, where $x$, $y$, and $z$
correspond to the long, middle, and short axes. We use $z_{1/2}/x_{1/2}$ as a proxy for the ratio of scale height to scale length, and refer to it as "disc thickness". Note here we use "disc thickness" only to describe the thickening of stellar distributions as in observations. We do not distinguish between a flattened stellar distribution or a rotationally-supported disc.

In previous papers (Meng et al. 2019; Meng & Gnedin 2020) where we studied the relation between the star formation rate and interstellar medium, we defined galaxy plane as the orientation of the short axis of the shape tensor of neutral gas. Here we use the definition based on stars to match the observations of high-redshift stellar populations. We checked the difference in these two definitions of galaxy orientation: the median difference is about 30° for all galaxies in our sample. For the most massive galaxies, the difference is smaller, with a median of 16°.

### 3 EVOLUTION OF DISC THICKNESS

For a more detailed analysis of the thickness of stellar populations, we group stars into more fine age bins: <30 Myr, 30–100 Myr, 100–300 Myr, 300–500 Myr, >500 Myr. We then calculate the half-mass length for each age bin in the three established coordinate directions.

First we explore whether the thickness of stellar discs depends on galaxy mass, which itself increases over time. Figure 3 shows the half-mass height $z_{1/2}$ for stellar populations of different age. Each galaxy is represented by five small points corresponding to the half-mass height monotonically increasing with age of the stellar population. We describe it in more detail in the following plots. Any dependence on galaxy stellar mass is much less obvious. There may be a slight trend for the height of the youngest stars to increase with mass, but not for stars older than 100 Myr. Considering that the low-mass galaxies contain fewer than $10^3$ stellar particles, and even less in a given age bin, this trend may not be significant.

Figure 4 shows disc thickness as the ratio of the short to long axis lengths $z_{1/2}/x_{1/2}$. Similar to the half-mass height, the thickness also increases with the age of the stellar populations. The only possible exception is with the two youngest age bins, which show more scatter and variation at the low mass end. This is because the orientation we choose to define the disc plane is based on the shape of stars younger than 100 Myr, which includes both age bins. This definition automatically minimizes the thickness of both stellar populations. Depending on stellar mass and specific star formation history, either the < 30 Myr bin or the 30-100 Myr bin may display a thinner disc. Therefore, we find little difference in all of our results between these two bins.

A small fraction of points lie above the line $z_{1/2} = x_{1/2}$. As our disc orientation minimizes the thickness of stars younger than 100 Myr, some older stellar populations that formed in a very different orientation may show $z_{1/2} > x_{1/2}$. This includes even one of the younger age bins (<30 Myr or 30–100 Myr) for a few galaxies. Our definition of the disc orientation guarantees that at least one of the younger bins will have $z_{1/2}/x_{1/2} < 1$, and for majority of the galaxies both bins do. However, a few cases with rapidly precessing disc plane show the other young bin with $z_{1/2} > x_{1/2}$. The rapid precession of the plane of young stars is illustrated later in Figure 8. Such precession may be caused by the clumping of star forming regions and the cycles of gas infall and expansion due to strong stellar feedback.

For the oldest bin with age >500 Myr the ratio $z_{1/2}/x_{1/2}$ decreases slightly with increasing stellar mass, from about 0.75 at $M_\star \sim 10^7 M_\odot$ to about 0.5 at $M_\star > 10^9 M_\odot$. A linear fit between $\log(z_{1/2}/x_{1/2})$ and $\log M_\star$ has a slope of -0.102 ±0.023. Thus disc thickening appears to be more pronounced for the older stars in dwarf galaxies. Still the trend is weak and does not appear to be related to the velocity dispersion of gas from which the stars form. We find the median ratio of the velocity dispersion to galaxy circular velocity is roughly constant $\sigma_r/v_\text{circ} \approx 0.6$ at all galaxy masses. The more likely cause of higher $z_{1/2}/x_{1/2}$ in dwarf galaxies is just the small number of young stellar particles, which leads to a more stochastic galaxy orientation.

Both the disc height and thickness increase with stellar age. Figure 5 illustrates this explicitly for the half-mass height. Instead of individual points for each galaxy’s populations, vertical errorbars indicate the interquartile range of the galaxy distribution. Diamonds show the median values for all galaxies in our sample in a given age bin. We can see that the disc thickness clearly increases from ~0.1 kpc at formation to ~0.8 kpc after 1 Gyr. The scatter in the galaxy sample is approximately constant at 0.15–0.2 kpc, although it appears larger for younger ages due to the logarithmic scale.

Similarly, Figure 6 shows that the half-mass ratio $z_{1/2}/x_{1/2}$ steadily increases with stellar age. Young stars always form in relatively thin discs with $z_{1/2}/x_{1/2} \leq 0.2$, while after several hundred Myr the stars occupy significantly thicker shapes with $z_{1/2}/x_{1/2} \approx 0.6$. Some runs have $z_{1/2}/x_{1/2}$ larger in the first age bin than in the second, again because the galaxy orientation is based on all stars younger than 100 Myr. Overall, both young stellar populations appear to occupy a similarly thin disc. As in the previous plots, there is no clear difference for the simulations with different adopted SFE.

We provide the medians and interquartile ranges of $z_{1/2}/x_{1/2}$ for stellar populations of different age in Table 1.

To study the evolution of thickness of individual stellar populations, we trace the shape of the same group of stars through

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**Figure 4.** Ratio of the short to long axes, split by stellar age. Symbols are as in Figure 3. The median disc thickness shows little variation with galaxy mass.
time. We choose all stars younger than 100 Myr within 10 kpc from galaxy center, for galaxies in the redshift range \( z = 2 - 4.6 \). We follow these same stars in all consecutive snapshots and calculate the intrinsic half-mass axis ratio, in the coordinate frame defined by their own shape tensor. Note that this is different from the previous plots where the orientation of all stars is defined by the shape tensor of stars younger than 100 Myr at that snapshot. We choose the intrinsic orientation for this calculation because the galaxy orientation changes over time, and simple misalignment with current plane may lead to thicker inferred shape of the tracked stars. We stop tracking the stars when their host galaxies merge into larger halos, since mergers significantly alter the original shape of the stellar distribution.

Figure 7 shows the resulting distribution for all selected populations. In total we have stellar groups selected from 118 independent galaxy snapshots. We only include groups with at least 100 stellar particles to be able to calculate the shape reliably. The stellar populations start from median age of \( \sim 50 \) Myr and are traced in every consecutive snapshot after selection. The median value of \( z_{1/2}/x_{1/2} \) increases from 0.15 when the stars are youngest to about 0.5 after 2 Gyr. The thickening of their distribution is unambiguous. This process saturates after 1-2 Gyr and therefore it is easy to miss in studies that have coarser time resolution. We do not find any dependence in this evolution on galaxy mass. Note that in Figure 7 the ratio \( z_{1/2}/x_{1/2} \) is measured in the coordinate system defined by the shape tensor of the same stars that we trace. If instead \( z_{1/2}/x_{1/2} \) is measured in the orientation of the galaxy defined by young stars in each snapshot, the median of \( z_{1/2}/x_{1/2} \) will increase to 0.5 in 1 Gyr, and further to 0.58 in 2 Gyr. This is because different stellar populations do not always align. We describe the orientation of different stellar populations in more detail in Figure 8.

### 4 DISCUSSION

#### 4.1 Comparison with observations of high-redshift galaxies

When galaxies are observed edge-on, their vertical heights can be directly measured. At \( z > 1.5 \), optical and near infrared wavebands correspond to the rest-frame UV, which is contributed mostly by young stars. Elmegreen & Elmegreen (2006) fitted the vertical profiles of galaxies in HST UDF with the functional form

\[
\text{sech}^2 \left( \frac{z}{z_0} \right) = 4 \left[ \exp \left( \frac{z}{z_0} \right) + \exp \left( -\frac{z}{z_0} \right) \right]^2,
\]

where the half-light height \( z_{1/2} \) is related to the scale height \( z_0 \) by \( z_{1/2} = 0.55 z_0 \). Their results show that the half-light height of clumpy galaxies in the F850LP band to be \( z_{1/2} = 0.5 \pm 0.2 \) kpc. This is larger than the thickness of the youngest stellar population of our galaxies: 0.1 – 0.2 kpc. Similarly, Elmegreen et al. (2017) measured the \( \text{sech}^2 \) scale height of the high-redshift galaxy discs in the HST Frontier Fields Parallels. They divided the galaxies into spiral type and clumpy (or "chain") type, and found that spiral galaxies are only present at \( z < 1.5 \). Since our simulated galaxies are at \( z \geq 1.5 \) and appear clumpy, we compare our results to the clumpy/chain galaxies. For these systems Elmegreen et al. (2017) find that the height is smaller for the star-forming clumps and larger in the interclump regions. They interpret it as the clumps representing the thin disc, while the interclump regions being more similar to the thick disc.
the average scale height quantifies the thin disc and the maximum scale height in each galaxy quantifies the thick disc. The median of the average half-light height of the clumpy galaxies in the redshift range 1.5-2.5 is $z_{1/2} = 0.35 \pm 0.13$ kpc. This is closer to, but still larger than, the median half-mass height of the youngest stars in our simulated galaxies (see Figure 3). Note that the observational sample includes more massive galaxies than in our simulations, from $10^9 M_\odot$ up to $10^{10.7} M_\odot$, whereas our sample is below $10^{9.8} M_\odot$. In the Elmegreen et al. (2017) sample the disc height strongly increases with galaxy mass, which may partly account for the larger median values in the observational sample. In contrast, the median of the maximum heights is even higher at $0.58 \pm 0.24$ kpc, well above our results.

Although stars form in relative thin configuration in our simulated high-redshift galaxies, this configuration is still somewhat thicker than local star-forming discs, which typically have axis ratios below 0.15. As a comparison, in our simulations the median short-to-long axis ratio of young stars is 0.15-0.2. High-redshift observations directly support thicker star-forming discs. For example, Reshetnikov et al. (2003) find that in the Hubble Deep Field galaxies the ratio of disc scale height to scale length increases by a factor of at least 1.5 from low redshift to $z > 1$. Elmegreen & Elmegreen (2006) quote the mean ratio of the radial half-length between clumps to $\text{sech}^2$ scale height to be $3.4 \pm 1.6$, which corresponds to $z_{1/2}/x_{1/2} \gtrsim 0.16$, although exact conversion is not possible. This ratio is similar to that for young stars in our simulated galaxies.

Besides the direct way of measuring the thickness of edge-on discs, there are also studies of shapes of high-redshift galaxies with other orientations. If galaxies are randomly projected on the sky, the observed shape distribution can be modeled to infer the intrinsic 3D shape distribution. Elmegreen et al. (2005) found the intrinsic thickness of spiral galaxy discs in the HST UDF to be $\pm 0.2-0.3$. Other studies divide high-redshift galaxies into mass and redshift bins and reconstruct the shape distribution for each bin to analyse the evolution of intrinsic galaxy shapes. These studies found that high-redshift galaxies are more prolate or spheroidal than oblate (e.g. Law et al., 2012), and that the prolate fraction decreases with decreasing redshift and increasing galaxy mass (e.g. van der Wel et al. 2014; Zhang et al. 2019). For the mass and redshift range that best matches our simulated galaxies, $M_*=10^9 - 10^{11} M_\odot$ and $z = 1.5 - 3.6$, Law et al. (2012) found galaxy minor/major and intermediate/major axis ratios $c/a \sim 0.3$ and $b/a \sim 0.7$. Zhang et al. (2019) give the average ratios $c/a \sim 0.3$ and $b/a \sim 0.5$ for galaxies with mass $10^{9.0-9.5} M_\odot$ at $1.5 < z < 2.5$. This puts the intrinsic shape of observed high-redshift galaxies in the prolate regime, similar to our simulated galaxies.

Elmegreen et al. (2017) also find the scale height of the most massive ($M_*=10^{9.5-10^{10.5}} M_\odot$) clumpy galaxies to increase with galaxy mass and decreasing redshift. This trend is present for the youngest stars in our galaxies (Figure 3).

### 4.2 Comparison with simulations

Numerical simulations have also investigated the evolution of disc thickness. For example, the Illustris TNG50 simulation suite has a much larger number of galaxies but lower spatial resolution (100-300 pc) than our simulations. In TNG50 the half-light height of star-forming galaxies with $M_*=10^9 - 10^{10} M_\odot$ in the rest-frame V band at $z = 2$ is 200-400 pc (Pillepich et al., 2019). Since the V band light is produced by stars of a wide range of age, this result should be compared to our age bins up to 500 Myr. Indeed, it agrees with the height of 100-500 Myr old stars in our galaxies. Pillepich et al. (2019) define disc thickness somewhat differently from us, as the ratio of the half-mass height to the 2D circularized half-mass radius, $z_{1/2}/r_{1/2}$, but the difference should be limited to tens of percent. For galaxies in the mass range $10^9 - 10^{10} M_\odot$ at $z = 1.5 - 2$, the ratio $z_{1/2}/r_{1/2}$ ranges from 0.15 to 0.35. More massive galaxies, with $10^9 - 10^{10} M_\odot$, are significantly less thick: $z_{1/2}/r_{1/2} \approx 0.1 - 0.2$. While these values are comparable to the average thickness of the 100-300 Myr old populations in our galaxies, we do not find as
strong a dependence on galaxy mass. This difference may provide a useful observational test of the models.

The TNG50 results were not split by stellar age, but they provide another measure of height for the Hα emitting gas, which is a proxy for star formation rate and may indicate future location of very young stars. In all the TNG50 galaxies the height of the Hα gas is consistently smaller than that of the V-band stars, which indicates the age trend that we described above for our results.

In addition to measuring the disc height and length, Pillepich et al. (2019) studied the intrinsic shape of the stellar distribution in elliptical shells. They find that elongated (or prolate) galaxies are more common at higher redshift and lower galaxy mass: at $z > 2$ about half of the galaxies with $M_*=10^9-10^{10}M_\odot$ have prolate shapes while the other half show spheroidal shapes. It is similar to our results (Figure 2) for the $>100$ Myr old stars. None of the TNG50 stellar distributions are as prolate as our young stars ($<100$ Myr old). The only comparably small values of $b/a$ are shown by the distribution of Hα emitting gas, which may be a proxy for the very young stars. Therefore it is possible that in the TNG50 simulation stars also form only in thin discs. A more direct investigation of this trend would be desirable.

In other suite of Vela simulations, Ceverino et al. (2015) investigated the shape of high-redshift galaxies by fitting an ellipsoid to the 3D isodensity surface around the half-mass radius. They show one example of a galaxy at $z=2.2$ with $M_*=10^9M_\odot$ that has the axis lengths of the stellar distribution equal to $(a, b, c) = (2.2, 0.76, 0.67)$ kpc. Both the short axis length and the short-to-long axis ratio are similar to our results (Figure 2).

A number of simulation studies favor the "upside-down" formation scenario for galactic discs, wherein stars form in thick discs at high redshift with a kinematically "hot" configuration, and then in progressively thinner discs at lower redshift. For example, Buck et al. (2020) used the NIHAO-UHD simulations of isolated MW-sized galaxies to investigate the evolution of height of stellar populations split in age bins of $\Delta t = 2$ Gyr. They find that the exponential scale heights at birth decrease with stellar age, i.e. the "upside-down" formation. They also find that the scale heights at present day are larger than at those birth. This suggests that the disc thickness today is set partly at the time of formation and partly by subsequent secular heating. Note that unlike our globally measured $z_{1/2}$, Buck et al. (2020) excluded the central galaxy and calculated the exponential scale height in the radial range $2 < R < 25$ kpc. The numbers they find for $\sim10$ Gyr old stars (i.e. formation at $z \sim 1$) are $z_d = 0.8 - 1.5$ kpc, which correspond to the half-mass height $z_{1/2} = 2 z_d$, $2 \approx 0.5 - 1.0$ kpc. This is within the range of thickness of the oldest stars in our galaxies. However, these estimates are likely to be incorrectly classified as "at birth". Buck et al. (2020) choose wide age bins of $\Delta t = 2$ Gyr, during which the disc orientation can evolve significantly as shown by our results, and therefore the stellar thickness may already be artificially inflated. This is supported by inspecting their Figs. 13 and 14, which show 3 of 5 galaxies with larger scale height than scale length "at birth" for stars older than 10 Gyr. This confirms the disc precession which hides the actual thickness of the star-forming disc. A finer time resolution is required to uncover the trend indicated by our results.

Other simulation studies that favor the "upside-down" disc formation scenario also take wide 1-2 Gyr age bins for mono-age stellar populations (e.g. Bird et al. 2013; Stinson et al. 2013; Ma et al. 2017; Navarro et al. 2018). They consistently find that old stars form in structures that are radially compact and relatively thick, while younger stars form in progressively larger, thinner, and colder configurations. We show that this cannot be used as confirmation of the "upside-down" scenario. The stars could either form in actually thicker discs or form in thin discs and get quickly displaced from the changing midplane. This is especially important at high redshift where more frequent mergers may change the galaxy orientation more often. Only tracing the stellar population from the very young stars can distinguish between these two cases. For example, a recent paper by Bird et al. (2020) analysed the upside-down formation scenario in simulated galaxies with smaller time intervals (50 Myr), illustrating both effects of the disc forming kinematically hotter at high redshift, and the stars being heated after birth. Since their analysis covers later epochs ($z < 1.5$) than our simulations and quantities only the velocity dispersion instead of disc thickness, we cannot make a direct comparison with their results.

4.3 On the cause of thickening of galactic discs

There are many physical mechanisms that lead to real thickening of galactic discs with fixed orientation. Classic papers by Spitzer & Schwarzschild (1951) and Spitzer & Schwarzschild (1953) pointed out that gravitational scattering by massive gas clouds could increase the velocity dispersion of stars in the galactic plane, especially considering differential galactic rotation. Lacey (1984) generalized the calculation by considering the vertical motion of stars and found that the velocity dispersion increases steadily while the shape of the velocity ellipsoid remains fixed. More recently, Bournaud et al. (2009) found that secular internal processes, such as gravitational instabilities and scattering by large clumps, lead to increased but constant disc height over galactocentric radius, while galaxy mergers lead to flaring of discs at large radii. Grand et al. (2016) showed the galactic bar and tidal perturbations from satellites to be responsible for most of the disc heating at $z \leq 1$ in the Auriga simulations.

In addition to these real processes, we have identified another important, and possibly dominant, mechanism leading to apparently larger axis ratios of high-redshift galaxies. It is the rapidly changing orientation of the disc midplane. For example, the intrinsic axis ratio for the same stellar population 1 Gyr since birth is only $0.4$ (Figure 7), while the observable axis ratio for the oldest stars with the median age 800 Myr is already $\sim0.6$ (Figure 6). The difference comes from the different definitions of the galaxy orientation. In observations, only one orientation exists in the plane of the sky, and because of redshifting of starlight, it is defined by the distribution of blue young stars. Because of rapid midplane precession, this orientation may not align with the intrinsic orientation of older populations and artificially inflate the measured thickness.

Figure 8 illustrates the precession of the disc plane directly. The angle between the short axis of the configuration of tracked stars for Figure 7 and the short axis defined by the current young stars rises up to $\sim 20^\circ$ in less than 200 Myr and then oscillates around those values. The path of individual galaxies has a much wider variation than the interquartile trend, as illustrated by two cases in the figure.

The median angle offset is noticeably larger for low-mass galaxies, $M_* < 10^9M_\odot$. Less massive galaxies are more easily affected by accretion and mergers which can change the disc orientation. Also, the determination of the plane is more stochastic for low-mass galaxies simply because of the smaller number of stellar particles.

Overall, the plane precession is a significant contributor to the thicker appearance of high-redshift discs. Investigation of such offset at lower redshifts will be important for disentangling this effect from the real disc expansion by secular and external heating. Unfortunately, our current simulation suite does not extend beyond

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z ≈ 1.5. We plan to investigate this issue with new simulations in progress and encourage other groups with available simulations to look into it as well.

5 CONCLUSIONS

We investigated the thickening of high-redshift galaxy discs using a suite of ultrahigh-resolution cosmological simulations. We selected a galaxy sample with stellar mass $M_* = 10^7 - 10^{10} M_\odot$ at redshifts $z \geq 1.5$. We calculated the half-mass disc height and the axis ratio for stellar populations split into narrow age bins, from < 30 Myr to > 500 Myr. The main results are summarized below:

- Using the shape tensor, we find the intrinsic 3D shape of high-redshift galaxies to be prolate or elongated, unlike the local axisymmetric discs. Stars younger than 100 Myr are confined to a thin disc plane and then rapidly expand away from the current disc plane.

- The disc plane in observations of high-redshift galaxies is defined as a plane precession effect. We plan to address these issues with upcoming galaxy formation simulations.

- In future studies it will be desirable to quantify the effect of disc precession using other simulations and at lower redshift. Since the mixing of stellar populations is rapid, with the timescale less than 200 Myr, this will require correspondingly high temporal resolution of the analyzed stellar populations. Previous studies advocating the "upside-down" disc formation scenario lacked sufficient time resolution to detect the plane precession effect. We plan to address issues with upcoming galaxy formation simulations.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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