Design and Performance of Microstrip Diplexers: A Review

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Abstract—The radiofrequency microstrip diplexers are widely demanded nowadays by modern wireless communication systems. Hence, several types of previously reported microstrip diplexers are reviewed and investigated in this work. Microstrip diplexers are three ports devices used for separating desired signals and delivering them through two (or more) different channels. The diplexers are investigated in three categories of dual-channel bandpass-bandpass diplexers, multichannel diplexers, and lowpass-bandpass diplexers. The investigated multi-channel diplexers include a number of four-channel, six-channel, and eight-channel diplexers. Due to the hard design process, the number of reported diplexers with more than four channels is limited. The layout structures and theory design methods of the previously reported diplexers are studied. Moreover, their size and performance are compared while some explanations about their advantages and disadvantages are presented. This comparison includes insertion loss, return loss, fractional bandwidths, isolation, selectivity, and gaps between channels.

Index Terms—Microstrip, Diplexer, Bandpass-bandpass, Lowpass-bandpass, Multichannel.

I. INTRODUCTION

High-performance and compact microstrip devices are strongly demanded by modern telecommunication and wireless networks. These microstrip devices are microstrip filters, couplers, diplexers, multiplexers, power dividers, and sometimes low-noise amplifiers (Noori and Rezaei, 2017; Shen and Che, 2020; Salehi and Noori, 2014; Chen, et al., 2019; Rezaei and Noori, 2018; Salehi, et al., 2016). A microstrip diplexer is a passive three-port device for frequency-domain multiplexing. It usually consists of two filters which are integrated by a junction circuit (Feng, et al., 2017; Huang, et al., 2016). The signal can be transmitted to the other two ports through a common port connected to the junction circuit (Rezaei, et al., 2019). Each diplexer has two channels working at two frequencies for the specific applications. For examples, the proposed diplexer in Yang, et al., 2014, has been designed for 4G application while the introduced diplexer in Noori and Rezaei, 2017, has been designed for IEEE 802.16 and 802.20 WiMAX technology and wireless applications. When the channels are close together, the diplexer can be employed for frequency division duplex (FDD) scheme (Peng and Chiang, 2015). However, in this case, improving the insertion loss and isolation between channels is hard (Noori and Rezaei, 2017). The diplexers can be formed by two bandpass filters (BPF), which are bandpass-bandpass diplexers (BBDs) (Jun-Mei, et al., 2016; Chinig, et al., 2015; Guan, et al., 2014; Chen, et al., 2015; Xiao, et al., 2015; Rezaei and Noori, 2018; Sasipriya and Aparna, 2018; Rezaei and Noori, 2018). Some of BBDs have two channels (Deng, et al., 2013; Noori and Rezaei, 2017; Rezaei, et al., 2017; Feng, et al., 2014; Chinig, et al., 2015; Salehi, et al., 2016; Chen, et al., 2006; Cheng, et al., 2013; Chinig, 2017; Wang, et al., 2016) named dual-channel diplexers. However, some have more than two channels. The multiplexers have more than three ports and more than two channels (Heng, et al., 2014), but multi-channel diplexers have only three ports with the channel numbers more than two (Liu, et al., 2017; Lee, et al., 2016; Wu, et al., 2013; Lai and Jeng, 2005; Hsu, et al., 2016). Since ultra-wideband has traditional applications in non-cooperative radar, some of diplexers have been designed with wide channels.
The wideband diplexer can use a very low energy level for short-range and high-bandwidth communications. On the other hand, a number of diplexers have narrow channels (Salehi, et al., 2016). They are suitable for multi-channel long-range RF communication systems (Noori and Rezaei, 2018; Yahya, et al., 2019). The stopband rejection of a high-performance diplexer must be wide with low harmonic level (Yahya, et al., 2019; Bukuru, et al., 2015; Rezaei, et al., 2019). Nevertheless, many designers did not give attention to attenuate the harmonics (Rezaei, et al., 2019; Rezaei, et al., 2019). Other types of diplexers are lowpass-bandpass diplexers (LBDs), which have been formed by a lowpass filter (LPF), BPF, and junction circuit (Rezaei, et al., 2019; Deng and Tsai, 2013; Rayatzadeh and Molouadian, 2019; Heshmati and Roshani, 2018; Capstick, 1999; Hayati, et al., 2019). An important factor related to the diplexer performance is the high selectivity. However, some of the diplexer designers did not improve the selectivity (Rezaei, et al., 2019; Bui, et al., 2017) while the others could design the diplexers with high-frequency selectivity at both channels (Rezaei and Noori, 2018; Lobato-Morales, et al., 2012). A well-designed diplexer must have low loss and high isolation between channels. For example, a microstrip diplexer that reported in Ghafari and Afsahi, 2019, has relatively a good isolation but large measured insertion and return losses at both channels. Furthermore, a diplexer with flat passbands has low time distortion, which is an advantage.

In this work, several kinds of microstrip diplexers are reviewed. The structures and performance of these diplexers are studied to find the best structures with high performance and small size. Moreover, the mathematical methods of analyzing some structures have been reviewed. The Frequency response and overall size of the introduced diplexers are compared in the following categories: Dual-channel BBDs, multichannel bandpass diplexers, and LBDs.

II. DUAL-CHANNEL BBDs

The majority designed diplexers for the wireless communication market are the dual-channel BBDs. Usually, to design this type of diplexer, the designers use two similar BPF but with different overall dimensions. Each filter should create only one passband. Therefore, to design a dual-channel diplexer, we need two single-mode resonators. Several structures have been proposed to design the dual-band passband diplexers (Feng, et al., 2017; Huang, et al., 2016; Rezaei, et al., 2019; Yang, et al., 2014; Noori and Rezaei, 2017; Peng and Chiang, 2015; Jun-Mei, et al., 2016; Chinig, et al., 2015; Guan, et al., 2014; Chen, et al., 2015; Xiao, et al., 2015; Rezaei and Noori, 2018; Sasipriya and Aparna, 2018; Rezaei and Noori, 2018; Deng, et al., 2013; Noori and Rezaei, 2017; Rezaei, et al., 2017; Feng, et al., 2014; Chinig, et al., 2015; Salehi, et al., 2016; Chen, et al., 2006; Cheng, et al., 2013; Chinig, 2017; Wang, et al., 2016). To achieve a high performance, different mathematical methods have been used. Some of the layout configurations of diplexers with a summary of their design methods are presented in Table I. In addition to the presented layout, some lumped elements have been used (Feng, et al., 2017). Due to the symmetric structures, the even/odd modes analysis has been performed (Feng, et al., 2017; Huang, et al., 2016; Yang, et al., 2014; Guan, et al., 2014; Rezaei and Noori, 2018; Sasipriya and Aparna, 2018; Rezaei and Noori, 2018). The even/odd input admittances ($Y_{me}$ and $Y_{mo}$) have been calculated to obtain the coupling coefficient $k_{12}$ according to the following formula (Feng, et al., 2017):

$$k_{12} = \frac{\text{Im}[Y_{me}(\omega_e)]}{\text{Im}[Y_{me}(\omega_o)]}; \quad Y_{11} = \frac{Y_{me} + Y_{ma}}{2}, \quad Y_{12} = \frac{Y_{me} - Y_{ma}}{2} \quad (1)$$

Where $\omega_e$ and $\omega_o$ are angular resonance frequencies. As mentioned in Feng, et al., 2017, the coupling factor is strongly affected by the gap between resonators. Accordingly, another way to realize $k_{12}$ is by selecting the gap between the resonators and coupling sections. For analyzing the symmetrical resonators (Huang, et al., 2016; Yang, et al., 2014; Guan, et al., 2014; Liu, et al., 2017), the even and odd modes resonance frequencies $f_{\text{even}}$ and $f_{\text{odd}}$ are expressed as:

$$f_{\text{odd}} = \frac{(2n-1)c}{2L_1\sqrt{\varepsilon_{\text{eff}}}} \quad \text{and} \quad f_{\text{even}} = \frac{nc}{(L_1 + 2L_2)\sqrt{\varepsilon_{\text{eff}}}} \quad (2)$$

Where $\varepsilon_{\text{eff}}$ is the effective dielectric constant and $c$ is the speed of light in free space. The physical length of half circuit under odd-mode and even mode excitations are depicted by $L_1$ and $L_2$, respectively. As depicted in Table II, the resonators (Huang, et al., 2016; Yang, et al., 2014) are similar where they are loaded by similar T-shape stubs. On the other hand, they used (2) to calculate the even/odd mode resonance frequencies. However, they have different junction circuits.

The meandrous lines have been coupled to realize a microstrip diplexer (Rezaei, et al., 2019; Chinig, 2017; Bukuru, et al., 2015), but they are implemented on different substrates. To analyze some resonators, the ABCD matrixes have been calculated (Salehi and Noori, 2014; Noori and Abiri, 2016; Rezaei, et al., 2019; Noori and Rezaei, 2017; Noori and Rezaei, 2017). Using the ABCD matrix (Rezaei, et al., 2019), $S_{11}$ and $Z$ matrix have been calculated. Then for having the lowest insertion loss, the value of $S_{11}$ is obtained. On the other hand, based on the value of $Z_{11}$, the resonance condition is obtained. Finally, by combining the equations, the values of the physical lengths at a target resonance frequency are obtained. Meanwhile, Noori and Rezaei (2017) calculated the reflection coefficient based on the ABCD matrix to obtain the condition of good isolation. However, due to its special structure, it could not improve the isolation between channels. The transmission matrix (Noori and Rezaei, 2017) is utilized based on an equivalent LC circuit of a basic resonator. It is utilized for calculating the values of the unknown stubs dimensions. As shown in Table I, the simple structure (Jun-Mei, et al., 2016) is analyzed by calculating the external quality factors corresponding to source and load ($Q_{e,o}$ and $Q_{e,N+1}$) using the coupling coefficients ($M_{0,1}$ and $M_{e,N+1}$) as follows:

$$Q_{e,o} = \frac{M_{0,1}^2}{1 + M_{0,1}^2} \quad \text{and} \quad Q_{e,N+1} = \frac{M_{e,N+1}^2}{1 + M_{e,N+1}^2} \quad (3)$$

Where $Q_{e,o}$ and $Q_{e,N+1}$ are the external quality factors at the source and load. The expression (3) is used for obtaining the proper values of $M_{0,1}$ and $M_{e,N+1}$ in the circuit (Jun-Mei, et al., 2016).
### Layout Configuration, Substrate, and Theory Method of the Dual-channel BBDs. $\varepsilon_r$ is the Substrate Relative Dielectric Constant and $h$ is the Substrate Height

| Refs. | Diplexer structure | Substrate | Theory method |
|-------|--------------------|-----------|---------------|
| (Feng, et al., 2017) | ![Diplexer](image1.png) | $\varepsilon_r=2.65$  
$h=0.508$ mm | 1. Calculating the even/odd modes admittances ($Y_{ee}$ and $Y_{oo}$)  
2. Calculating the coupling coefficient |
| (Huang, et al., 2016) | Rogers RO4003C  
$\varepsilon_r=3.55$  
$h=0.508$ mm | Finding the fundamental odd and even modes resonant frequencies |
| (Rezaei, et al., 2019) | RT_Duroid_5880  
$\varepsilon_r=2.2$  
$h=0.787$ mm | 1. Calculating the ABCD matrix  
2. Calculating $S_{21}$ and $Z$ matrix from ABCD matrix  
3. Calculating the resonance frequency from $Z$ matrix |
| (Yang, et al., 2014) |  
$\varepsilon_r=3.5$  
$h=0.8$ mm | Finding the fundamental odd and even modes resonant frequencies |
| (Noori and Rezaei, 2017) | RT_Duroid_5880  
$\varepsilon_r=2.2$  
$h=0.787$ mm | 1. Calculating the transmission matrix  
2. Calculating the reflection coefficient  
3. Finding a method to obtain better isolation between two channels |
| (Jun-Mei, et al., 2016) |  
$\varepsilon_r=2.55$  
$h=0.8$ mm | 1. Calculating the external quality factors  
2. Tuning the space between coupled lines based on quality factors |
| (Chinig, et al., 2015) |  
$\varepsilon_r=4.4$  
$h=1.58$ mm | 1. Even and odd modes analysis by calculating the input admittance  
2. Calculating the desired frequency ratio of harmonic from the input admittance |
| (Guan, et al., 2014) |  
$\varepsilon_r=3.5$  
$h=0.8$ mm | Calculating the even and odd modes of resonance frequencies |
| (Chen, et al., 2015) |  
$\varepsilon_r=10.8$  
$h=0.653$ mm | Finding the resonance condition based on the equivalent circuit of quarter resonator |

(Contd...)
TABLE I

(Continued)

| Refs.            | Diplexer structure | Substrate         | Theory method                                                                 |
|------------------|--------------------|-------------------|-------------------------------------------------------------------------------|
| (Chen, et al., 2015) | ![Diplexer Structure](image1.png) | RT_Duroid_5880  $e=2.2$  $h=0.787$ mm | 1. Proposing an equivalent $Lc$ model of the resonator |
| (Sasipriya and Aparna, 2018) | ![Diplexer Structure](image2.png) | RT_Duroid_5880  $e=2.2$  $h=0.787$ mm | 1. Proposing an equivalent $Lc$ model of the resonator |

BBDS: Bandpass-bandpass diplexers

TABLE II

Performance Comparison among Different Reported BBDS

| Refs.            | IL1, IL2 (dB) | RL1, RL2 (dB) | Size ($l_{i,j}^2$) | Isolation (dB) | $f_{oc}, f_{oc}$ (GHz) | $f_n/f_o$ (GHz) | FBW1, FBW2 (%) |
|------------------|--------------|--------------|-------------------|----------------|------------------------|----------------|---------------|
| (Feng, et al., 2017) | 1.4, 3.4     | 15, 20       | 0.089             | 45             | 1.05, 1.87             | 1.78           | 6.1, 4        |
| (Huang, et al., 2016) | 1, 0.9      | Better than 20 | 0.127             | 30             | 2.3, 2.72             | 1.18           | 6.1, 5.8      |
| (Rezaei, et al., 2019) | 0.36, 0.44  | Better than 23.7 | 0.028             | 23             | 2.88, 3.29             | 1.14           | ---           |
| (Yang, et al., 2014) | ---          | ---          | 0.082             | 30             | 2.35, 2.59             | 1.10           | 6.89, 6.5     |
| (Nouroi and Rezaei, 2017) | 0.6, 0.9    | 11.3, 12.4   | 0.076*            | 13.8           | 2.6, 2.6               | 2.30           | ---           |
| (Peng and Chiang, 2015) | 2.1, 2.1    | Better than 20 | 0.07             | 20             | 1.75, 1.85             | 1.06           | 5, 5          |
| (Jun-Mei, et al., 2016) | 2.2, 2.1    | 11.9, 12     | 0.064             | 30             | 1.82, 2.41             | 1.32           | 2.8, 1.9      |
| (Ching, et al., 2015) | 2.2, 2.2    | Better than 16 | ---              | 21             | 1.8, 2.45              | 1.36           | 8.7, 6.6      |
| (Guang, et al., 2014) | 1.2, 1.5    | ---          | 0.137             | 35             | 1.95, 2.14             | 1.10           | 3.59, 3.27    |
| (Chen, et al., 2015) | 1.83, 1.52  | ---          | 0.705             | 26             | 1.1, 1.13              | 1.18           | 8.9, 2.2      |
| (Xiao, et al., 2015) | 1.43, 1.59  | ---          | 0.282             | 42             | 2.44, 3.52             | 1.44           | ---           |
| (Rezaei and Noori, 2018) | 0.14, 0.16  | 18.5, 20     | 0.022             | 34             | 1.8, 2.4               | 1.33           | 11.7, 11      |
| (Rezaei and Noori, 2018) | 0.28, 0.29  | 21.2, 24.3   | 0.010             | 30             | 0.8, 0.9              | 1.12           | 3.2, 3.2      |
| (Deng, et al., 2013) | 3, 3        | Better than 10.3 | 0.073             | 37.5           | 3.5, 5.8              | 1.93           | 80, 5         |
| (Nouroi and Rezaei, 2017) | 0.2, 0.4    | 15, 16.8     | 0.09*             | 19.8           | 2.36, 4               | 1.69           | ---           |
| (Rezaei, et al., 2017) | 0.18, 0.39  | 27.1, 27.6   | 0.075             | 20.55          | 2.4, 2.79             | 1.15           | ---           |
| (Feng, et al., 2014) | ---         | Better than 20 | 0.32*             | 30             | 1.84, 2.41             | 1.3            | 6.6, 2         |
| (Ching, et al., 2015) | 2.24, 2.16  | Better than 29 | 0.13*             | 21             | 1.8, 2.45             | 1.36           | ---           |
| (Salehi, et al., 2016) | 1.5, 1.3    | Better than 21 | 0.087*            | 30             | 2.3, 2.55             | 1.10           | 3.6, 3.4      |
| (Chen, et al., 2006) | 2.8, 3.2    | 16, 17       | ---              | 30             | 1.5, 1.75*             | 1.16           | 3.8, 3.3      |
| (Cheng, et al., 2013) | 2.86, 3.04  | Better than 20 | 0.688             | 40             | 8, 9                   | 1.12           | ---           |
| (Ching, 2017) | 2.6, 2.4    | 35, 33       | 0.079*            | 24.4           | 1.7, 2.49             | 1.46           | 2.6, 5.1*     |
| (Wang, et al., 2016) | 0.4, 0.3    | Better than 13 | 0.488             | 70             | 9.9, 10.02             | 1.01           | 0.65*, 0.65* |
| (Yahya, et al., 2019) | 0.85, 0.8   | 15.7, 24     | 0.047             | 21             | 2.85, 2.72             | 1.05           | ---           |
| (Bukuru, et al., 2015) | 1.35, 1.31  | 15, 20       | 0.05              | 25             | 3.65, 5.2              | 1.42           | 8.2, 7.69     |
| (Rezaei, et al., 2019) | 0.25, 0.26  | 18.45, 17.47 | 0.038             | 24             | 2.12, 3.94             | 1.85           | ---           |
| (Rezaei, et al., 2019) | 0.10, 0.16  | 33, 22       | 0.054             | 22             | 1.6, 2.1               | 1.31           | 16.8, 11      |
| (Bui, et al., 2017) | 0.4, 0.42   | better than 20 | 0.095             | ---             | 1.8, 2.45             | 2.36           | ---           |
| (Rezaei and Noori, 2018) | 0.21, 0.21  | 32, 25       | 0.018             | 40             | 1.1, 1.3               | 1.3            | 4.6, 4.6      |

* : Approximated values. BBDS: Bandpass-bandpass diplexers

\[
Q_{c,o} = \frac{1}{\text{FBW} M_{c,0}^2} \quad (3)
\]

\[
Q_{c,y+1} = \frac{1}{\text{FBW} M_{c,N,y+1}^2}
\]

Where $M_{c,y+1}$ is the coupling coefficient and fractional bandwidth (FBW) is the FBW. Finally, the space between coupled lines is tuned based on quality factors. The resonator analysis presented by Guan, et al. (2014) and Rezaei, et al. (2017) has been performed by calculating the extra quality factor ($Q_e$) as defined by the following equation:

\[
Q_e = \frac{2f_o}{(\Delta f)_{3dB} 10^{\frac{-IL}{20}}}
\]

Where $f_o$, IL, and $(\Delta f)_{3dB}$ are resonance frequency in GHz, insertion loss in dB, and $-3$dB bandwidth, respectively. Proposing an approximated $LC$ circuit is a method to analyze the resonator structure. Fig. 1 presents some resonators with their approximated equivalent $LC$ circuit proposed in Noori and Rezaei, 2017; Rezaei and Noori, 2018; Rezaei and Noori, 2018; Salehi, et al., 2016; Rezaei, et al., 2019. Since the effects of steps in widths and bent are negligible
at the frequencies lower than 10 GHz, the equivalent lumped elements of these sections are removed. The patch cells are replaced by capacitors, and thin stubs are presented by inductors. As depicted in Fig. 1, the effect of coupling between microstrip lines is replaced by some capacitors. Using these LC circuits, it can be easy to calculate the resonance frequencies, ABCD matrix, input impedance/admittance, and even/odd modes analysis.

A well-designed diplexer must be compact with low loss, sharp roll-off, attenuated harmonics, and high isolation. The simulated and measured frequency responses of dual-channel BBDs in (Huang, et al., 2016; Jun-Mei, et al., 2016; Guan, et al., 2014; Cheng, et al., 2013) are presented in Figs. 2(a)-(d), respectively. As presented in Fig. 2, the parameters $S_{21}$ and $S_{31}$ show the transition between common port (1) and other ports, while the isolation between channels is depicted by $S_{23}$. However, they could not improve the selectivity while the harmonics did not suppress.

The size and performance of designed dual-band BBDs are compared in Table II. In this table; RL is the return loss, and $f_{1}$ and $f_{2}$ are the resonance frequencies of the first and second channels, respectively. As presented in Table II, the lowest insertion losses at both channels are achieved in Rezaei and Noori, 2018, while the best return losses are obtained in Chinig, et al., 2015. The overall sizes of the reported diplexers are presented in $\lambda_{g}$, where $\lambda_{g}$ is the guided wavelength calculated at the lower resonance frequencies. The comparison results show that the most compact dual-band BBD is designed in Rezaei and Noori, 2018, with the overall size of 0.01 $\lambda_{g}$. Another important factor in the diplexer design is the isolation between channels where the highest isolation (70 dB) is achieved in Wang, et al., 2016. When the channels are close together, the diplexer can be used for FDD applications. Nevertheless, having a small gap between channels leads to increase in the loss and decrease the isolation. Accordingly, the diplexer with $f_{2}/f_{1} \leq 1.1$ has been less designed. As shown in Table II, only the proposed diplexer in Wang, et al., 2016, could reach $f_{2}/f_{1} = 1.01$, but it could not improve the common port return loss at both channels. The narrowband and wideband diplexers can be identified from the presented FBWs in Table II. A diplexer with FBW1 = 2.8% and FBW2 = 1.9% is designed in Jun-Mei, et al., 2016, where it can be used for long-range RF communication systems. However, having narrow channels increases the group delay that leads to time distortion. On the other hand, a diplexer with 80% first channel FBW is designed in Deng, et al., 2013, which is suitable for ultra-wideband applications.

### III. Multichannel BBDs

Another type of diplexer is multichannel BBDs. Quad-channel diplexers are a type of BBDs which is the most reported one. The quad-channel diplexers have three ports similar to dual-band BBDs, but with four channels. They are suitable for multichannel communication systems. The special applications of dual and multichannel diplexers are related to their resonance frequencies. For example, a diplexer with resonance frequencies at 2.4 GHz and 5.2 GHz is appropriate for wireless local area networks (WLAN) while a diplexer with an operational frequency at 1.8 GHz is suitable for GSM applications (Rezaei and Noori, 2018). The
Quad-band diplexers are usually composed of two dual-band BPF and a junction circuit. The sizes of this type of diplexer are usually larger than dual-band BBDs. The layout structure, substrate properties, and theory method of the quad-band bandpass diplexers are summarized in Table III.

As illustrated in Table III, the microstrip spiral cells with inductance features have been utilized to design quad-band bandpass diplexers (Heng, et al., 2014; Liu, et al., 2017). They are integrated by murderous microstrip lines. The spiral cells have the advantage of being compact, but the junction circuits (Heng, et al., 2014; Liu, et al., 2017) occupy large implementation areas. When we decrease the gap between spiral cells, they will be coupled to each other. The coupling between them creates some small coupling capacitors. Therefore, the inductor and capacitors can create passbands easily. The quad-band diplexer reported by Heng, et al. (2014) is designed based on proposing an LC circuit and finding the coupling coefficients. However, in Liu, et al., 2017, the even and odd modes resonance frequencies have been calculated as functions of $\varepsilon_{\text{eff}}$ and light speed $c$. This diplexer is designed using BPF. Then, the coupling coefficient from the simulated $S$-parameters is extracted by:

$$M = (f_{o2}^2 - f_{o1}^2) / (f_{o2}^2 + f_{o1}^2)$$

(5)

Where $f_{o1}$ and $f_{o2}$ represent the lower and higher resonance frequencies of the proposed filter. To design a microstrip four-channel diplexer in Lee, et al., 2016, the step impedance cells have been used. In this work, the design method is based on the calculation of the resonance frequencies of step impedance sections without mathematical formulas. Coupled open loops have been integrated on RT/Duroid 5880 substrate with $\varepsilon_r = 2.2$ and $h = 0.787$ mm to realize a four-channel diplexer in Wu, et al., 2013. In the loop structures, low impedance sections are utilized. The analysis of this structure is performed based on finding the impedance ratio of the low impedance section. Furthermore, similar to the proposed diplexer in Lee, et al., 2016, the coupling coefficients are obtained from the two resonant modes based on (5) using the full-wave electromagnetic simulator.

Coupled hairpins have been integrated in Hsu, et al., 2016, to obtain a microstrip diplexer with four passbands. This diplexer is designed based on finding the coupling coefficient as functions of the distance between resonators without mathematical formulas. To obtain a four channel diplexer in Noori and Rezaei, 2018, two similar dual-band BPF with
different dimensions have been designed and analyzed. For this purpose, first, an approximated $LC$ model of the basic resonator is presented. Then, the input impedance of the $LC$ circuit is extracted. Finally, an angular resonance frequency is calculated when the input impedance is zero. In this case, the dimensions can be tuned based on a target resonance frequency when the equations show the resonator behavior. The basic resonator and its approximated $LC$ circuit (Noori and Rezaei, 2018) are presented in Fig. 3. As shown in Fig. 3, the open ends and feed lines are replaced by the capacitors $C_o$ and $C_f$, respectively.

Similar to the dual-band BBDSs, a high-performance quad-band bandpass diplexer must have low loss, high-frequency selectivity, suppressed harmonics, high isolation, and low group delay. The frequency response of the quad-band bandpass diplexers (Liu, et al., 2017; Lee, et al., 2016; Hsu, et al., 2016; Noori and Rezaei, 2018) is presented in Figs. 4(a)-(d), respectively. Advanced design system full-
A wave EM simulator has been used to simulate the reported diplexers. As depicted in Fig. 4, the selectivity of the proposed diplexer (Liu, et al., 2017) is poor where the other quad-band diplexers (Lee, et al., 2016; Hsu, et al., 2016; Noori and Rezaei, 2018) could improve the frequency selectivity. However, the proposed diplexer (Lee, et al., 2016) has low selectivity at its last channel. On the other hand, any of them could not attenuate the harmonics after the last channel.

The channels with 1% up to 3% FBW are narrowband (Yu and Chang, 1998). However, a narrowband BPF with 0.5% FBW is proposed (Chen, et al., 2015). As shown in Fig. 4d, the reported diplexer by Noori and Rezaei (2018) has very narrow channels with 1.2%, 1.96%, 1.15%, and 1.09% FBWs. The narrow channels of this diplexer give a good resistance against interference. The size and performance of the previously reported quad-channel diplexers are compared. The comparison results are listed in Table IV. The resonance frequency of the quad-channel diplexers at the 1st, 2nd, 3rd, and 4th channels are presented by $f_{o1}$, $f_{o2}$, $f_{o3}$, and $f_{o4}$. As written in Table IV, the lowest insertion losses of quad-band diplexers are obtained (Liu, et al., 2017) while the best return losses are obtained (Noori and Rezaei, 2018). Getting high isolation between channels, when we have more number of channels is harder. The highest isolation of quad-channel diplexers is 55 dB, which is obtained (Heng, et al., 2014). Meanwhile, the introduced diplexer (Rezaei, et al., 2019) has the minimum overall size of $0.025 \lambda_g^2$ in comparison with the other reported quad-channel diplexers. Among multichannel diplexers, quad-channel diplexers are more designed. However, based on the tri-band unit cell, a six-channel diplexer is proposed in Ghafari and Afsahi, 2019. It operates at 3.4 GHz, 3.7 GHz, 5.6 GHz, 6 GHz, 7 GHz, and 7.6 GHz, which is suitable for wireless and WiMAX applications. Meanwhile, an eight-channel microstrip diplexer with a size of $0.1 \lambda_g^2$ is presented in Tu and Hung, 2014. It is designed using coupled closed loops with different widths. The channels of this diplexer are relatively narrow, with isolation between channels better than 29 dB. High selectivity and attenuated harmonics are the advantages of this work.

| Refs. | ILs (dB) | RLs (dB) | Isolation (dB) | $f_{o1}$, $f_{o2}$, $f_{o3}$, $f_{o4}$ (GHz) | Size ($\lambda_g^2$) | FBWs (%) |
|-------|---------|---------|---------------|---------------------------------|-----------------|---------|
| (Heng, et al., 2014) | 0.4, 0.33, 0.35, 0.45 | 19, 19, 19, 20 | 55 | 2.8, 2.81, 2.82, 2.83 | 1.17 | 0.2, 0.2, 0.2, 0.2 |
| (Liu, et al., 2017) | 0.24, 0.15, 0.18, 0.28 | --- | --- | 50 | 1.9, 2.15, 2.3, 2.5 | 0.037 | 0.44, 0.65, 0.45, 0.75 |
| (Lee, et al., 2016) | 1.38, 1.6, 1.52, 1.8 | --- | 44.8 | 1.92, 2.45, 5.25, 5.81 | 0.962 | 7.8, 6.5, 4, 3.4 |
| (Wu, et al., 2013) | 0.8, 1, 0.7, 1.5 | --- | --- | 30 | 1.5, 2, 2.4, 3.5 | 0.078 | 8, 4, 6, 2 |
| (Lai and Jeng, 2005) | --- | 10, 10, 7.75, 7.75 | 10 | 2.52, 4.02, 5.48, 7.13 | 0.22 | --- |
| (Hsu, et al., 2016) | 2, 1.5, 2, 2.5 | >13 dB | 29 | 0.9, 1.5, 2.4, 3.5 | 0.042 | 4.3, 4.6, 3.3, 4 |
| (Noori and Rezaei, 2018) | 0.5, 0.38, 0.53, 0.58 | 20, 21, 25, 22 | 30 | 1.67, 2.54, 3.45, 4.57 | 0.029 | 1.2, 1.96, 1.15, 1.09 |
| (Rezaei, et al., 2019) | 0.59, 0.41, 0.45, 0.73 | 12.9, 21.6, 16.7, 12.6 | 23 | 2.07, 2.37, 3.94, 4.49 | 0.025 | --- |

* Approximated values. BBDS: Bandpass-bandpass diplexers

Fig. 4. Simulated and measured frequency response of four-channel diplexers: (a) (Liu, et al., 2017), (b) (Lee, et al., 2016), (c) (Hsu, et al., 2016), and (d) (Noori and Rezaei, 2018).
IV. LBDS

The microstrip LBDS are composed of microstrip LPF, BPF, and junction circuit. As mentioned earlier, to achieve a BBD, designing a bandpass resonator was enough. Then, the designed resonator is used to obtain two BPF to use in the diplexer structure.

However, it is necessary to design two bandpass and lowpass resonators to achieve a LBD. The LPF must have high performance with small normalized size. One advantage of a diplexer is its novel structure.

A novel LBD is designed (Rezaei, et al., 2019) for WLAN and WiMAX applications. It is implemented on RT/Duroid 5880 substrate. It includes a novel LPF composed of the patch and thin cells, a BPF, and a small junction circuit. For designing the lowpass section, first, a simple microstrip cell is simulated. Then, it is expanded and simulated step by step so that a very sharp lowpass channel is created. The passband channel of this diplexer is designed based on proposing a basic resonator and its equivalent LC circuit. Then, the even and odd modes of angular resonance

| Refs. | Diplexer structure | Substrate | Theory method |
|-------|--------------------|-----------|---------------|
| (Rezaei, et al., 2019) | [Image] RT/Duroid 5880 | $\varepsilon_r=2.2$ $h=0.787$ mm | 1. Proposing an $Lc$ model for the basic bandpass resonator 2. Calculating the angular even/odd modes resonance frequencies from $Lc$ circuit |
| (Deng and Tsai, 2013) | [Image] Rogers RO4003C | $\varepsilon_r=3.55$ $h=1.524$ mm | Calculating of the electric lengths of the shunt open stub and high-impedance transmission line of the LPF |
| (Heshmati and Roshani, 2018) | [Image] RO4003C | $\varepsilon_r=3.38$ $h=0.813$ mm | Optimization method without mathematical analysis |
| (Capstick, 1999) | [Image] RT/Duroid 5880 | $\varepsilon_r=2.2$ $h=0.38$ mm | Designing the LPF for 50Ω stub λ/4 long at the center frequency of the bandpass filter |
| (Hayati, et al., 2019) | [Image] RT/Duroid 6002 | $\varepsilon_r=2.93$ $h=30$ mil | 1. Proposing $Lc$ circuits for the LPF and BPF 2. Calculating ABCD matrix of the LPF 3. Finding a method to create a lowpass channel 4. Calculating an angular resonance frequency of the BPF |

LBDs: Lowpass-bandpass diplexers, LPF: Lowpass filter, BPF: Bandpass filters
frequencies of the LC model are calculated. Furthermore, a method to attenuate the harmonics is performed similarly to the proposed method (Salehi and Noori, 2015). In this method, all resonance frequencies have been calculated, where the resonance frequency is the main and the others are harmonics. To attenuate these harmonics, the undesirable resonance frequencies and main resonance frequency are set equal. Layout configuration, substrate type, and summarized theory method of the previous reported LBDs are presented in Table V. As depicted in Table V, the use of coupled microstrip cells in the lowpass sections is not essential. However, the engraved patch cells are utilized (Heshmati and Roshani, 2018; Hayati, et al., 2019). The U-shape cells are coupled to create the bandpass channel (Deng and Tsai, 2013), whereas the bandpass channel (Capstick, 1999) is formed by the simple coupled lines. In (Deng and Tsai, 2013), an equivalent circuit model of the proposed LBD is presented. The LPF utilized (Deng and Tsai, 2013) is fifth-order while the electric lengths of the shunt open stub ($\theta$) and series high-impedance transmission line ($\theta_s$) are calculated as follows:

$$
\theta_i = \tan^{-1}(2\pi f_c C_i Z_f) \quad \text{for } i = 1, 3, 5
$$

$$
\theta_s = \sin^{-1}\left(\frac{2\pi f_s L_s}{Z_s}\right) \quad \text{for } K = 2, 4
$$

Where $f_c$ is the cutoff frequency of the LPF, $C_i$ and $L_s$ are the required lumped capacitors and inductors, respectively. The parameters $Z_i$ and $Z_s$ are the characteristic impedances. The proposed LBD (Heshmati and Roshani, 2018) is realized based on an optimization method without mathematical analysis. In Capstick, 1999; first, a lowpass prototype is created with the first capacitor $C_1$ defined as follows:

$$
C_1 = \frac{\pi f_c}{2f_c^2 Z}
$$

Where $f_c$, $f_o$, and $Z$ are the LPF cutoff frequency, the BPF center frequency, and the stub impedance, respectively. Then, the lowpass prototype is transformed into microstrip using the method outlined (Capstick, 1994). After that, a Chebyshev BPF is designed and connected to the LPF. To design the LBD in Hayati, et al., 2019, a perfect mathematical method

| Refs. | IL1, IL2 (dB) | RL1, RL2 (dB) | Size ($\lambda_g^2$) | Isolation (dB) | $f_c/f_o$ (GHz) | $f/f_o$ (GHz) |
|-------|--------------|--------------|---------------------|----------------|----------------|--------------|
| (Rezaei, et al., 2019) | 0.15, 0.18 | 18.2, 41.4 | 0.036 | 26 | 2.4, 4.2 | 1.75 |
| (Deng and Tsai, 2013) | 0.25, 2.42 | 15, 15 | 0.49 | 35 | 1.5, 2.4 | 1.6 |
| (Rayatzadeh and Moloudian, 2019) | 0.2, 0.8 | --- | --- | 30 | 1, 2.4 | 2.4 |
| (Heshmati and Roshani, 2018) | 0.25, 0.58 | 15, 30 | 0.046 | 35 | 1, 2.4 | 2.4 |
| (Capstick, 1999) | 1, 4.8 | --- | --- | 30 | 0.6, 2.4 | 4 |
| (Hayati, et al., 2019) | 0.12, 0.10 | 19.2, 36 | 0.03 | 20 | 1.88, 3.56 | 1.89 |

*: Approximated values. LBD: Lowpass-bandpass diplexers
is done to design both lowpass and bandpass sections. The approximated equivalent LC models of both lowpass and bandpass resonators are proposed. Then, using the LC circuits, the ABCD matrix for the LPF and the resonance for the bandpass resonator are calculated and analyzed to find the behavior of the device and better tuning the physical dimensions.

The frequency response of the LBDs is depicted in Figs. 5(a)-(d) (Rezaei, et al., 2019; Deng and Tsai, 2013; Capstick, 1999; Hayati, et al., 2019). As shown in Fig. 5, the designed LBDs (Rezaei, et al., 2019; Hayati, et al., 2019) have the advantage of high selectivity, whereas in (Deng and Tsai, 2013; Capstick, 1999) there are poor roll-off at the lowpass channels.

Moreover, the proposed diplexer (Capstick, 1999) could not attenuate the harmonics. Totally, the best selectivity and suppressed harmonics are obtained (Hayati, et al., 2019). The size and performance of the previous reported LBDs are compared in Table VI. In Table VI, IL and RL are the insertion and return losses where the indexes 1 and 2 are related to the lowpass and bandpass channels, respectively. The lowpass channel cutoff frequency and bandpass channel resonance frequency are shown with $f_L$ and $f_R$, respectively. As written in Table VI, the best insertion and return losses are achieved (Hayati, et al., 2019) while it occupies the most compact area $0.03λ^2$. The highest isolation between channels and the smallest gap between channels are obtained (Deng and Tsai, 2013) by victimizing the overall size so that it has the largest size $(0.49λ)^2$.

V. Conclusion

Several types of microstrip diplexers are studied in this work. The structures and mathematical design methods of these diplexers are reviewed. The reviewed microstrip diplexers are dual-band BBD, LBDs, and multichannel diplexers. Some of the design methods of these works were based on proposing an equivalent LC circuit. Therefore, we presented and explained some proposed LC models of the resonator layouts. The mathematical equations presented in some works were explained too. The layout configurations of the previously reported works with their used substrates were shown and described. The performance of the reviewed diplexers in terms of losses, isolation, selectivity, harmonics, isolation, and the gap between channels is compared. We believe that this review paper may serve a useful guide for researchers who are interested in microstrip diplexers design.

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