A combined stretching–tilting mechanism produces negative, zero and positive linear thermal expansion in a semi-flexible Cd(II)–MOF†

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A novel semi-flexible Cd(II)-MOF has been synthesized and characterized by variable temperature powder and single-crystal X-ray diffraction. The material displays an unusual combination of thermal expansion (TE) i.e. negative, zero and positive, which is an extremely rare finding, especially for metal–organic frameworks as a result of a combined stretching–tilting mechanism.

Most solid materials expand along all directions upon heating – a phenomenon known as positive thermal expansion (PTE). The coefficients ($a_i$) of positive linear thermal expansion are usually in the order of about 20 MK$^{-1}$. However, in a few known instances specific mechanical phenomena or packing arrangements in the solid state lead to anomalous thermal expansion behavior such that extraordinarily large PTE ($>100$ MK$^{-1}$) or negative thermal expansion (NTE) occurs. Materials that possess geometric flexibility can undergo expansion along one particular direction, leading to contraction along the perpendicular directions (or vice versa) as a consequence of scissor- or hinge-like thermal responses. Several organic and metal-organic materials such as Ag$_3$[Co(CN)$_6$] and the Prussian blue analogues have been reported to possess large anisotropic thermal expansion coefficients. MOFs have recently attracted significant interest owing to their novel architectures as well as their potential applications as functional materials. Moreover, materials such as cyanide-bridged MOFs, HKUST-1 (Cu(n)-1,3,5-BTC)$^8$ and IRMOFs$^9$ display isotropic negative thermal expansion. A few magnetic materials exist in which increased thermal motion is negated by effects due to a change in the magnetic ordering, thus resulting in overall zero thermal expansion (ZTE) within a particular temperature range. We also note that some MOF are known to undergo combined PTE, NTE and ZTE based on either hinge or lattice fence mechanisms.$^{4b,c}$

Here we report the design and synthesis of a semi-flexible MOF $\{[\text{Cd(HBTC)}(\text{BPP})]_{1.5}\text{DMF.2H}_2\text{O}]_n(1)$ containing mono-protonated 1,3,5-benzenetricarboxylate (HBTC$^{2-}$) as the rigid part and 1,3-bis-(4-pyridyl)propane (BPP) as the flexible unit (Scheme 1). Crystallizes in the triclinic space group $P\overline{1}$. The asymmetric unit contains one Cd$^{2+}$ ion, one HBTC$^{2-}$ ligand, one BPP ligand, two water molecules and 1.5 disordered DMF molecules (Fig. 1).

Of the three carboxyl groups of BTC only two are deprotonated and they bind to the metal ion in chelate-bridging and chelating modes (Fig. S1, ESI†) to form a dinuclear Cd$_2$ secondary building unit. The BPP ligands coordinate to the Cd centers to form a Cd$_3$(BPP)$_2$ macrocyclic unit, which is approximately co-planar to the crystallographic $bc$ plane (Fig. S2, ESI†), whereas the aromatic ring of HBTC$^{2-}$ is oriented parallel to the crystallographic $ab$ plane. Thus the interconnected Cd$_3$BPP$_2$ macrocyclic units form a 2D layer parallel to (011). Each layer contains solvent-accessible channels.

![Scheme 1 Schematic representation of the synthetic procedure for 1.](image)

![Fig. 1 Thermal ellipsoid plot (50% probability) of the asymmetric unit of 1.](image)
along [100] with dimensions \(3.1 \times 9.7\ \text{Å}\) (taking into account the contributions of the van der Waals radii of the atoms). The channels are occupied by some of the disordered DMF and water molecules while the carboxylic acid group remains uncoordinated, forming O-H⋯O and C-H⋯O hydrogen bonding interactions (Fig. S3, ESI†) with the remaining water molecules and the BPP ligands. The overall 3D architecture of the framework has an \(\cdots\text{ABAB}\cdots\) stacking arrangement (Fig. 2) and the remaining DMF molecules occupy the interstitial positions between the layers.

In order to monitor temperature dependent structural changes, a variable-temperature single-crystal X-ray diffraction (VT-SCD) study was carried out. Starting at 100 K, intensity data were recorded at 20 K intervals; data collection above 260 K was not feasible owing to solvent loss and degradation of the single crystal. The variation of crystallographic axes and angles with temperature are shown in Fig. S4 and S5 (ESI†). Since \(\text{1}\) crystallizes in the triclinic crystal system, the coefficients of thermal expansion were calculated using the program PASCal.\(^{11}\)

The expansion coefficients along the three principal axes \(X_1\) along fractional coordinate vectors \((0.4920, 0.7734, -0.3997)\), \(X_2\) \((0.9134, -0.4041, 0.0480)\) and \(X_3\) \((0.0575, 0.1605, 0.9854)\) are \(-43.4(7), 2(1)\) and \(133(2)\) \(\text{MK}^{-1}\), respectively (Fig. 3 and 4). The volumetric thermal expansion coefficient \(\alpha_v = 91(2)\) \(\text{MK}^{-1}\) (Fig. S6, ESI†).

Expansion data obtained from PASCal were verified against data obtained from the program Win_strain\(^ {11}\) (see ESI†) and found to be in close agreement. Thus \(\text{1}\) displays NTE along \(X_1\), ZTE along \(X_2\) and PTE along \(X_3\) (Fig. 5).

The reversibility of the thermal expansion phenomenon was verified by determining the unit cell dimensions after rapid cooling to 100 K, heating back to 260 K and then cooling again to 100 K (100-R in the ESI†). The initial and final unit cell dimensions at 100 K were approximately equal, and the temperature cycling did not appear to cause significant degradation of the crystal mosaicity.

Using the VT-SCD data, temperature-dependent changes in the conformation of the framework were examined in order to elucidate the mechanism of this rare thermal expansion behavior. Upon heating, the \(\text{Cd}_2\text{BPP}_2\) macrocyclic unit undergoes expansion diagonally (d) across the macrocycle (\(\varepsilon_\text{d} = 104(1)\) \(\text{MK}^{-1}\)) as is evident from the elongation of the non-bonding distances \(\text{C15-C16}', \text{C12-C17}'\) and \(\text{N1}-\text{i1}\) (Table 1, Fig. 6, Fig. S7–S14, ESI†). The aliphatic unit of the BPP...
ligand (approximately parallel to X1) bends, as evidenced by an increase in the bond angle C15\cdots C16\cdots C17 and a decrease in the Cd1\cdots C16\cdots Cd10 non-bonding angles with increasing temperature. A decrease in the torsion angle N1\cdots C15\cdots C17\cdots N2 also occurs during this process (Table 2, Fig. 7). Concomitantly, the macrocyclic moiety tilts towards the c axis, thus leading to a decrease in the crystallographic angle \( \alpha \) with increasing temperature. In isolation, tilting would cause NTE along X1 and PTE along X3 while unidirectional stretching of the macrocycle would cause PTE along both principle axes X1 and X3. However, simultaneous stretching and tilting of the macrocycle (see ESI† Video) combine to enhance PTE along X3 (approximately along the c axis). The rigid HBTC\(^2\) units are approximately collinear to the principal axis X2 and, since they are largely unaffected by the variation in temperature, ZTE is observed along X2.

The O–H\cdots O hydrogen bonding interactions are sufficiently strong to preclude variation in the donor\cdots acceptor distances with temperature (Table S4, ESI†).

Variable temperature X-ray powder diffraction (VT-XRPD) was carried out to confirm the thermal expansion of the bulk material. Reflections corresponding to the Miller indices 00l shift towards lower 2\( \theta \) (\(^{\circ} \)) values with increasing temperature, confirming positive thermal expansion approximately along the c axis (along X3). Reflections with Miller indices hk0 show almost no shift with changing temperature (Fig. 8, Fig. S15 and S16, ESI†). Furthermore, the diffraction patterns also confirm reversibility of the thermal expansion phenomenon. The differential scanning calorimetric (DSC) thermogram of 1 precludes any possibility of a thermotropic phase transition (Fig. S17, ESI†) since no energetic events are observed during the thermal cycle (100–260 K).

To date, flexible materials that exhibit anisotropic thermal expansion behavior have undergone expansion (or contraction) along one axis with an associated compensation along the remaining two axes. These materials involve a ‘scissor/hinge’

### Table 1

| \( T/\text{K} \) | C15\cdots C16' (Å) | C12\cdots C17' (Å) | N1\cdots i1\( ^a \) (Å) |
|----------------|------------------|------------------|------------------|
| 100            | 7.672(4)         | 7.617(4)         | 4.152(2)         |
| 140            | 7.703(4)         | 7.640(4)         | 4.157(2)         |
| 180            | 7.747(4)         | 7.678(4)         | 4.174(2)         |
| 220            | 7.797(4)         | 7.713(4)         | 4.192(2)         |
| 260            | 7.844(4)         | 7.757(4)         | 4.213(2)         |

\( ^a \) i1 = Centroid of C18' C19' C20' N2' C21' C22'.

### Table 2

| \( T/\text{K} \) | \( y^a \) (\(^{\circ} \)) | \( \phi^a \) (\(^{\circ} \)) | \( \tau^c \) (\(^{\circ} \)) |
|----------------|------------------|------------------|------------------|
| 100            | 7.672(4)         | 7.617(4)         | 4.152(2)         |
| 140            | 7.703(4)         | 7.640(4)         | 4.157(2)         |
| 180            | 7.747(4)         | 7.678(4)         | 4.174(2)         |
| 220            | 7.797(4)         | 7.713(4)         | 4.192(2)         |
| 260            | 7.844(4)         | 7.757(4)         | 4.213(2)         |

\( ^a \) \( y = \) C15\cdots C16\cdots C17. \( ^b \) \( \phi = \) Cd1\cdots C16\cdots Cd10. \( ^c \) \( \tau = \) N1\cdots C15\cdots C17\cdots N2.
PTE along the 
and 
involving expansion of Zn
Similarly, the Zn-MOF recently reported by the same group 
anisotropic expansion facilitated by a scissor-type motion.

Fig. 8 Variable temperature XRPD patterns for 1

We thank the National Research Foundation and Department of Science and Technology (SARChI Program) for support of this work. PL also thanks the Claude Leon Foundation for financial support.

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