“Slow” Radio Bursts from Galactic Magnetars?

Bing Zhang

Department of Physics and Astronomy, University of Nevada, Las Vegas, Las Vegas, NV 89154, USA; zhang@physics.unlv.edu

Received 2020 November 19; revised 2020 December 10; accepted 2020 December 22; published 2021 January 21

Abstract

Recently, one fast radio burst (FRB), FRB 200428, was detected from the Galactic magnetar soft gamma-ray repeater (SGR) J1935+2154 during one X-ray burst. This suggests that magnetars can make FRBs. On the other hand, the majority of X-ray bursts from SGR J1935+2154 are not associated with FRBs. One possible reason for such rarity of FRB–SGR–burst associations is that the FRB emission is much more narrowly beamed than the SGR–burst emission. If such an interpretation is correct, one would expect to detect radio bursts with viewing angles somewhat outside the narrow emission beam. These “slow” radio bursts (SRBs) would have broader widths and lower flux densities due to the smaller Doppler factor involved. We derive two “closure relations” to judge whether a long, less luminous radio burst could be an SRB. The 2.2 s, 308 Jy ms, \( \sim 111 \) MHz radio burst detected from SGR J1935+2154 by the BSA/LPI radio telescope may be such an SRB. The \( \sim 2 \) ms, 60 mJy ms faint burst detected by the Five-hundred-meter Aperture Spherical radio Telescope from the same source could be also an SRB if the corresponding FRB has a narrow spectrum. If the FRB beam is narrow, there should be many more SRBs than FRBs from Galactic magnetars. The lack of detection of abundant SRBs from magnetars would disfavor the hypothesis that all SGR–bursts are associated with narrow-beam FRBs.

Key words: Radio transient sources – Magnetars

1. Introduction

The detection of a 1.5 MJy ms fast radio burst (FRB) in the Milky Way galaxy, i.e., FRB 200428 (Bochenek et al. 2020; CHIME/FRB Collaboration et al. 2020) in association with a bright X-ray burst (Li et al. 2020; Mereghetti et al. 2020; Ridnaia et al. 2020; Tavani et al. 2020) from the magnetar SGR J1935+2154, established the magnetar origin of at least some, probably all, FRBs (Popov & Postnov 2010; Kulkarni et al. 2014; Lyubarsky 2014; Katz 2016; Beloborodov 2017; Kumar et al. 2017; Metzger et al. 2017; Yang & Zhang 2018; Lu et al. 2020; Margalit et al. 2020; Wadiasingh et al. 2020; Yang et al. 2020b; Zhang 2020). On the other hand, deep monitoring of SGR J1935+2154 by the Five-hundred-meter Aperture Spherical radio Telescope (FAST; Lin et al. 2020) suggested that the FRB–SGR–burst associations are rather rare. During an active phase of SGR J1935+2154 when 29 other X-ray bursts were emitted from the source, no single FRB-like event was detected. Whereas whether the FRB-associated X-ray burst is physically special is still subject to debate (e.g., Li et al. 2020; Yang et al. 2020a; Younes et al. 2020), one plausible possibility is that the FRB emission is much more narrowly beamed than the SGR–burst emission (Lin et al. 2020).

Within this picture, an FRB can be detected only when the narrow beam points toward Earth. Outside the FRB “jet,” due to the rapid drop of the Doppler factor, one would expect that the flux drops rapidly, the spectrum becomes softer, and the duration becomes longer. These off-beam events are not likely detectable from cosmological FRB sources. However, in view of the huge specific fluence of FRB 200428, it is entirely possible that some off-axis, longer, and softer bursts from Galactic magnetars such as SGR J1935+2154 can be detected above the sensitivity thresholds of the available radio telescopes. We define these events as “slow” radio bursts (SRBs) and study their properties in this Letter.

2. On-beam FRB versus Off-beam SRB

FRB emission models from magnetars invoke either magnetospheres (Kumar et al. 2017; Yang & Zhang 2018; Lu et al. 2020; Wadiasingh et al. 2020; Yang et al. 2020b) or relativistic shocks (Lyubarsky 2014; Beloborodov 2017, 2020; Metzger et al. 2017, 2019; Margalit et al. 2020) to produce FRBs. Both types of models invoke a relativistically moving plasma to produce FRB emission (Zhang 2020, and references therein). Regardless of the emission site, here we consider a relativistically moving conical jet with bulk Lorentz factor \( \Gamma \) (and dimensionless speed \( \beta \)) and half opening angle \( \theta_j \). Considering an observer at a viewing angle \( \theta \) from the jet axis, in general one can define the Doppler factor

\[
D(\theta) = \begin{cases} 
D_{\text{on}} = \frac{1}{(1 - \beta \cos(\Delta \theta))}, & \theta \leq \theta_j, \\
D_{\text{off}} = \frac{1}{(1 - \beta \cos(\Delta \theta))}, & \theta > \theta_j, 
\end{cases}
\]

(1)

where \( \Delta \theta = \theta - \theta_j \). The Doppler factor makes a connection between comoving-frame quantities (primed) and the observer-frame quantities (e.g., Zhang 2018)

\[
\nu = D \nu', \\
\Delta t = D^{-1} \Delta t', \\
L_\nu = D^3 L_\nu',
\]

(2)

where \( \nu \) is the emission frequency, \( \Delta t \) is the emission duration, and \( L_\nu \) is the isotropic-equivalent specific luminosity. The last equation makes use of the point-source assumption, which is justified for FRB sources.

We compare the observed properties of two observers, one on-beam observer with \( \theta \leq \theta_j \) and \( D = D_{\text{on}} \) and another off-beam observer with \( \theta > \theta_j \) and \( D = D_{\text{off}} \). Defining a Doppler
factor ratio
\[ \mathcal{R}_D = \frac{D_{\text{on}}}{D_{\text{off}}} > 1 \] (3)
and assuming that the comoving-frame parameters are the same for on-beam and off-beam observers, one can write down the relationships of the properties of an on-beam FRB and an off-beam SRB.

Let us consider a radio burst with comoving-frame FWHM of \( \nu^w \) and specific luminosity power-law spectrum
\[ L'_\nu(\nu') = L'_\nu(\nu'_0) \left( \frac{\nu'}{\nu'_0} \right)^{-\alpha} \] (4)
at the burst peak time, where \( \nu'_0 \) is a characteristic frequency and \( \alpha \) is the spectral index. Consider an off-axis observer observing at \( \nu_2 \) and an on-axis observer observing at \( \nu_1 \), the ratio between the specific luminosities of the two observers reads
\[ \frac{L^\text{off}(\nu_2)}{L^\text{on}(\nu_1)} = \frac{L'_\nu(\nu'_0)}{L'_\nu(\nu'_0)} \left( \frac{\nu_2}{\nu_1} \right)^{-\alpha} = \mathcal{R}_D^{-\alpha} \left( \frac{\nu_2}{\nu_1} \right)^{-\alpha}. \] (5)

Noticing
\[ \frac{\nu^\text{off}}{\nu^\text{on}} = \mathcal{R}_D \] (6)
and considering that the specific luminosity ratio is proportional to the specific flux ratio, we finally get a "closure relation" among the ratios of specific fluxes \( \mathcal{F}_\nu \), width \( w \), and the observing frequency \( \nu \) between an off-axis SRB and an on-axis FRB:
\[ \left( \frac{\mathcal{F}_\nu^\text{SRB}}{\mathcal{F}_\nu^\text{FRB}} \right) \left( \frac{w^\text{SRB}}{w^\text{FRB}} \right)^{2+\alpha} \left( \frac{\nu^\text{SRB}}{\nu^\text{FRB}} \right)^\alpha = 1, \] (7)
where
\[ \mathcal{F}_\nu^\text{SRB} = L'_\nu(\nu_1) w^\text{on} / 4\pi d_L^2, \quad \mathcal{F}_\nu^\text{FRB} = L'_\nu(\nu_2) w^\text{off} / 4\pi d_L^2, \]
\[ w^\text{SRB} = w^\text{off}, \quad w^\text{FRB} = w^\text{on}, \]
\[ \nu^\text{SRB} = \nu_2, \quad \nu^\text{FRB} = \nu_1. \]

This relation can be used to determine whether a long-duration, low-fluence burst could be the off-beam version of an FRB.

The closure relation (7) makes the assumption of a power-law spectrum for FRBs and depends on the spectral index \( \alpha \). The true FRB spectral shape is not well measured. In any case, in the narrow band where FRBs are detected, some FRBs show a power-law spectrum, but with a wide range of spectral indices, e.g., \( \alpha = 4 \pm 1 \) for the Lorimer burst (Lorimer et al. 2007), \( \alpha = 7.8 \pm 0.4 \) for FRB 110523 (Masui et al. 2015), \( \alpha = -0.3 \pm 0.9 \) for FRB 131104 (Ravi et al. 2015), and \( \alpha \) ranging from -10.4 to +13.6 for FRB 121102 (Spitler et al. 2016).

There is evidence that at least some FRB spectra may be narrow (Spitler et al. 2016). The closure relation (7) also relies on the assumption that the FRB spectra extend to a high-enough frequency in the rest frame, so that the same index still applies for off-beam events. If the FRB spectrum is curved and intrinsically narrow, the closure relation could be more complicated. As an example, we consider a rest-frame Gaussian-like spectrum, i.e.,
\[ L'_\nu(\nu') = L'_\nu(\nu'_0) \exp \left[ -\frac{1}{2} \left( \frac{\nu' - \nu'_0}{\delta\nu'} \right)^2 \right]. \] (8)
where \( \nu'_0 \) and \( \delta\nu' \) are the center frequency and the characteristic width of the spectrum, respectively. For a narrow spectrum, one has \( \delta\nu' \ll \nu'_0 \). For an FRB with specific fluence \( \mathcal{F}_\nu^\text{FRB} \), intrinsic width \( w^\text{FRB} \), and observing frequency at \( \nu_1 \), one may assume \( \nu_1 = D_{\text{on}} \nu'_0 = \nu^\text{FRB} \) and \( \delta\nu_{\text{on}} = D_{\text{on}} \delta\nu' = \delta\nu^\text{FRB} \). An SRB observed at a large viewing angle would satisfy a more complicated closure relation (see the Appendix)
\[ \left( \frac{\mathcal{F}_\nu^\text{SRB}}{\mathcal{F}_\nu^\text{FRB}} \right) \left( \frac{w^\text{SRB}}{w^\text{FRB}} \right)^{2} \times \exp \left[ \frac{1}{2} \left( \frac{\nu^\text{SRB}}{\delta\nu^\text{SRB}} \right)^2 \right] = 1. \] (9)
If \( \delta\nu^\text{SRB} \ll \nu^\text{FRB} \), specific fluence drops significantly if the frequency is beyond the width of the line spectrum at an off-beam angle. Rapid variability is expected for such narrow-spectrum FRBs (Beniamini & Kumar 2020).

3. SRB Properties and Case Studies

From Equations (7) and (9), one may predict the properties of an SRB based on known properties of an FRB. A typical FRB with a specific fluence 1 Jy ms at a 100 Mpc cosmological distance would have a specific fluence of 100 MJy ms at a typical Galactic distance of 10 kpc. Assuming the same telescope (\( \nu^\text{SRB} = \nu^\text{FRB} \)) and for a power-law spectrum, one gets the SRB width longer than the FRB width by a factor of \( 10^{\alpha/2+\alpha} \) if it also has a specific fluence of 1 Jy ms level. This would make the burst duration of the order of 1 s for \( \alpha = 1 \) and even 10 s for a flat spectrum burst. So the main characteristic of an SRB is its "slow" nature. By definition in Equation (3), the discussion of an SRB is only relevant when its width is longer than its corresponding FRB.

Below we discuss several interesting radio bursts detected from SGR J1935+2154 and their compliance with the SRB closure relations.

3.1. The BSA/LPI Burst

The BSA/LPI radio telescope at Pushchino Radio Astronomy Observatory, Russia, detected one radio burst from SGR J1935+2154 at 2020 September 2 UTC 18:14:59 at 111 MHz with a 2.5 MHz band (Rodin & Fedorova 2020). The dispersion measure (DM) is in general consistent with the DM measured from other radio telescopes (Bochenek et al. 2020; CHIME/FRB Collaboration et al. 2020; Zhang et al. 2020; Zhu et al. 2020). The burst has a measured pulse width of 2.2 s, a flux density of 140 mJy, and a specific fluence 308 Jy ms with an observing frequency of 111 MHz. The intrinsic width is \( \sim 340 \) ms after correcting for the scattering and instrumental effects (A. Rodin 2020, private communication). We test the SRB hypothesis by setting \( \mathcal{F}_\nu^\text{SRB} \approx 308 \) Jy ms, \( w^\text{SRB} \approx 0.34 \) s, and \( \nu^\text{SRB} = 111 \) MHz. We test the closure relations against two reference FRBs: (1) Reference FRB-1 as a typical cosmological FRB with \( \mathcal{F}_\nu^\text{FRB} \approx 100 \) MJy ms, \( w^\text{FRB} \approx 1 \) ms, and \( \nu^\text{FRB} \approx 1.2 \) GHz if it were detected in the Milky Way; and (2) Reference FRB-2 as FRB 200428 itself, with
In order to detect an SRB with specific fluence above the telescope’s sensitivity threshold, the viewing angle should not be too far outside the FRB jet cone. The maximum viewing angle $\theta_{max}$ depends on the typical $\Gamma$ and $\theta_j$ of the FRB emitter as well as the shape of the FRB spectrum. For simplicity, we consider the same telescope to detect FRBs and SRBs so that $\nu_{SRB} = \nu_{FRB}$. The maximum viewing angle $\alpha$ for FRBs is $\theta_{max} - \theta_j$, at which $\nu_{FRB}$ equals the fluence sensitivity threshold $\nu_{th}$ of the telescope. For simplicity, we consider a power-law spectrum. Making use of Equations (6) and (11), Equation (7) can be then rewritten as

$$\beta \cos(\Delta\theta_{max}) = 1 - \frac{1}{2\Gamma^2} \left( \frac{\nu_{FRB}}{\nu_{th}} \right)^{\frac{1}{2}}.$$  

(10)

For $\Gamma \gg 1$ ($\beta \approx (1 - 1/2\Gamma^2)$) and $\theta_{max} \ll 1$, this can be reduced to

$$\Delta\theta_{max} \approx 1 - \frac{1}{\Gamma^2} \left( \frac{\nu_{FRB}}{\nu_{th}} \right)^{\frac{1}{2}}.$$  

(11)

where $\xi = (\nu_{FRB}/\nu_{th})^{\frac{1}{4}}$. One has $\xi \approx 100$ for $\alpha = 0$ and $\xi \approx 10$ for $\alpha = 2$. The small angle approximation is valid only when $\Gamma \gg 10$ or $\Gamma \ll 10$ in the respective cases.

The solid angle ratio between detectable Galactic SRBs and FRBs can be estimated as

$$\frac{R_{\Delta\Omega} \Omega_{SRB}}{\Omega_{FRB}} \approx \pi \left[ (\theta_j + \Delta\theta_{max})^2 - \theta_j^2 \right] \nu_{th}^2,$$

$$= \left( \frac{\Delta\theta_{max}}{\theta_j} \right)^2 + 2 \left( \frac{\Delta\theta_{max}}{\theta_j} \right),$$

$$= \left( \frac{\xi}{\Gamma \theta_j} \right)^2 + 2 \left( \frac{\xi}{\Gamma \theta_j} \right).$$  

(12)

This is also the ratio of event rates of the detectable SRBs and FRBs from Galactic magnetars. One can see that for wide-beam FRBs with $\theta_j \gg \xi/\Gamma$, which is relevant for relativistic shock models, the Galactic SRB rate would not be higher than the Galactic FRB rate. However, for narrow beams $\theta_j \ll \xi/\Gamma$, which is more relevant for a magnetospheric origin of FRBs, there should be many more SRBs than FRBs if the beaming interpretation of the FRB paucity is valid. If detailed data analyses suggest that SRBs are not as abundant as FRBs from Galactic magnetars, it may suggest either of the following two scenarios. First, the FRB beams may be very wide, which could be consistent with the models invoking emission beyond the magnetar light cylinder. Such models, on the other hand, face the challenge of interpreting diverse polarization angle variations from some repeating FRBs (Luo et al. 2020; Zhang 2020). Alternatively, if FRB emission indeed originates from narrow beams within magnetar magnetospheres, the lack of detection of abundant SRBs would suggest that the rarity of FRB–SRB–burst associations is likely intrinsic, i.e., the SGR–...
burst that makes FRB 200428 was physically distinct from other SGR–bursts (Li et al. 2020; Yang et al. 2020a; Younes et al. 2020).

5. Conclusions and Discussion

We have discussed a type of radio burst from Galactic magnetars that could be FRBs viewed off-beam. These bursts, dubbed SRBs, could have much longer durations and lower specific fluences than FRBs because of their smaller Doppler factors than on-beam FRBs. We derive two “closure relations”, Equations (7) and (9), among the ratios of burst specific fluence, width, and observing frequency between SRBs and FRBs, which could be used to judge whether a radio burst is an SRB. We show that the 2.2 s long, 111 MHz radio burst detected from SGR J1935+2154 by the BSA/LPI radio telescope (Rodin & Fedorova 2020) could be interpreted as an SRB. The weak FAST burst (Zhang et al. 2020) may be also interpreted as an SRB if the corresponding FRB has a narrow, Gaussian-like spectral shape.

We estimate the relative event rates of Galactic SRBs with respect to Galactic FRBs. The rate of Galactic SRBs could be much higher than that of Galactic FRBs if all SGR–bursts are associated with narrow-beam FRBs (Lin et al. 2020). A systematic search for SRBs from SGR J1935+2154 and other Galactic magnetars can place important constraints on this hypothesis. The lack of detection of abundant Galactic SRBs would rule out the hypothesis that all SGR X-ray bursts are associated with narrow-beam FRBs. Identifications of SRBs from Galactic magnetars, on the other hand, would confirm the beaming nature of FRBs and allow direct constraints on the physical parameters of the FRB emitters.

SRBs may not be only produced by Galactic magnetars. If other sources in the Milky Way can make Galactic FRBs and be detected by future wide-field radio telescope arrays, SRBs may also be generated from those objects based on the same reasoning discussed here.

The author thanks Alexander Rodin for clarifying the observational details of the BSA/LPI radio burst, Yuan-Pei Yang and Yun-Wei Yu for comments, and an anonymous referee for helpful suggestions.

Appendix

Derivation of Equation (9)

With a Gaussian-like spectrum in Equation (8), one can derive

\[
\frac{\mathcal{D}_{\text{off}}}{\mathcal{D}_{\text{on}}} = \frac{\mathcal{D}_{\text{off}}}{\mathcal{D}_{\text{on}}} \exp \left[ -\frac{1}{2} \left( \frac{\nu_2 - \nu_{0\text{off}}}{\Delta \nu_{\text{off}}} \right)^2 \right] = \frac{\mathcal{D}_{\text{off}}}{\mathcal{D}_{\text{on}}} \exp \left[ -\frac{1}{2} \left( \frac{\nu_2 - \nu_{0\text{off}}}{\Delta \nu_{\text{off}}} \right)^2 \right] \quad (A1)
\]

For an FRB, one can assume that the observing frequency is right at the center frequency of the spectrum, i.e., \( \nu_2' = \nu_0' \).

Equation (A1) now becomes

\[
\frac{L_{\text{off}}(\nu_2)}{L_{\text{on}}(\nu_1)} = \mathcal{R} \mathcal{D}^3 \exp \left[ -\frac{1}{2} \left( \frac{\nu_2 - \nu_{0\text{off}}}{\Delta \nu_{\text{off}}} \right)^2 \right] = \mathcal{R} \mathcal{D}^3 \exp \left[ -\frac{1}{2} \left( \frac{\nu_2 - \nu_{0\text{off}}}{\Delta \nu_{\text{off}}} \right)^2 \right] = \mathcal{R} \mathcal{D}^3 \exp \left[ -\frac{1}{2} \left( \frac{\nu_2}{\Delta \nu_{\text{on}}} \right)^2 \left( \mathcal{R} \mathcal{D}^3 \frac{\nu_2}{\nu_1} - 1 \right)^2 \right]. \quad (A2)
\]

Following the same logic of deriving Equation (7), one can then derive Equation (9).