On the Incidence Rate of Blazhko Stars

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Abstract. In a recent paper (Kovacs 2018) we examined the incidence rate of the modulated RR Lyrae stars by using the data from Campaigns 01−04 of the Kepler K2 mission. We found an observed rate of \( \sim 90\% \), implying near 100\% underlying rate, after correcting for detection bias due to observational noise. In this work we extend the sample to Campaign 08 and check the reliability of our earlier estimate. We get the same high rate, stressing the importance of full time series modeling (including systematics) in searching for shallow signals in the presence of large amplitude variabilities.

1. Introduction

It is not easy to find an astrophysical phenomenon with as little clue to the physical nature of the cause of the phenomenon as the (quasi)periodic modulation of the light curves RR Lyrae stars (or, as commonly known, the Blazhko effect – Blažko 1907). Although several ideas have been suggested, none of them succeeded, likely because of the missing underlying physics in those ideas – see Kolláth in these proceedings and also earlier reviews of Kovacs (2016) and Smolec (2016). Under this circumstance, most of the works in this field focus on further analyses of observational data to spark some workable idea. In this purely experimental approach various studies aim for finding new frequency components, establishing relations among the observed parameters (e.g., Skarka et al. 2020) and derive accurate population parameters, such as incidence rates. In this work we follow the latter thread by extending our earlier work on the incidence rate of Blazhko stars (Kovacs 2018).

2. Method of Analysis

The hunt for transiting extrasolar planets has revolutionized the analysis of photometric time series. Considering the small signals to be searched for, filtering out systematic effects both from the ground- and space-based observations has become of vital importance. Many methods have been developed primarily for transiting planet search, e.g., TFA, SysRem, PDC, SFF, EVEREST, respectively, by Kovács et al. (2005), Tamuz et al. (2005), Stumpe et al. (2012), Vanderburg & Johnson (2014), Luger et al. (2018). However, only a few of these were extended to general variability search (Aigrain et al. 2016), primarily because of the difficulties encountered in separating the instrumental and environmental systematics from the underlying astrophysical signal. In particular, except for the very recent study by Plachy et al. (2019), all previous investigations on the Blazhko phenomenon have been carried out on datasets using Simple Aperture
Photometry (SAP) for the space data (Benkő et al. 2014) and standard ensemble photometry for the ground-based data (e.g., analyses performed on the OGLE database – see Prudil & Skarka 2017).

The main reason why standard methods (e.g., SFF by Vanderburg & Johnson 2014) are not applicable to variable stars with dominating large amplitude variations is that these methods employ the “null-signal” assumption. Although inclusion of Gaussian process models has been proven to be a useful way of conserving stellar variability (Aigrain et al. 2016), here we resort to another approach, we have already employed in our pilot survey on Blazhko stars in fields C01-C04 of the K2 mission (Kovacs 2018).

\[ D = \sum_{i=1}^{N} [T(i) - F(i)]^2 \]

\[ F(i) = a_0 + \sum_{j=1}^{N_{\text{max}}} a_j U_j(i) + \sum_{k=1}^{N_{\text{FUR}}} b_k S_k(i) + c_k C_k(i) \]

As briefly summarized in Fig. 1, the observed signal is represented by the sum of two distinct components: i) the large amplitude pulsation, modelled by the Fourier series \( \{ b_k, c_k \} \) and ii) systematics, estimated by the linear combination of the time series \( \{ U_j(i) \} \). This latter set may include other photometric time series from the same field (or, the combinations thereof – often referred to as cotrending vectors – e.g., Stumpe et al. 2012) and stellar image parameters (e.g., positions on the CCD chip). While using cotrending vectors enables us to grab the common features of the light variation (the very essence of systematics), the image parameters help to disentangle those variations in the stellar flux that have their origin in the peculiarities of the given stellar image (Bakos et al. 2010). For cotrending time series we select bright stars uniformly distributed throughout the field of the campaign under scrutiny. Whenever available, the cotrending set is extended by the pixel coordinates of the image center.

Because the pulsation frequency is known only approximately from the direct analysis of the SAP data, we need to perform an iterative search to make the frequency determination more accurate. This procedure serves to avoid artificial remnant power in the residuals, that could be incorrectly identified as a modulation component. The multistep procedure is depicted in Fig. 2. In the final grand fit (step 9) we also include the newly found small amplitude components to minimize the effect of incomplete signal modeling. The main interest of this paper is step 8, the search for additional frequency components, and, in particular, the search for those components that are close to the pulsation frequency (and its harmonics).

\footnote{That is, there is no underlying variation, except for the brief moments of the transit events.}
3. Results

By following the RR Lyrae list of Molnár et al. (2018), as in our former study, we gathered the publicly available items from the NASA Exoplanet Archive\(^2\). We relied mostly on the database stored in the ExoFOP section of the site by Petigura et al. (2015) (see also Aigrain et al. 2016). When the target was missing in the ExoFOP section, but it was available through the Kepler pipeline (Smith et al. 2012), we used this latter set. In both cases only the respective raw (i.e., SAP) fluxes were used with TFA for correcting systematics. As in our earlier work, the classification of the variables was based on the residual frequency spectra: a star was declared as a Blazhko variable, if there was one or more significant peaks in the residual spectrum near the fundamental frequency.

| Field | \(N_{\text{tot}}\) | \(N_{\text{RRab}}\) | \(N_{\text{BL}}\) | \(N_{\text{nonBL}}\) | \(N_{\text{BL}}/N_{\text{RRab}}\) |
|-------|------------------|------------------|------------------|------------------|------------------|
| 01    | 14               | 14               | 9                | 5                | 0.64             |
| 02    | 57               | 57               | 52               | 5                | 0.91             |
| 03    | 62               | 62               | 59               | 3                | 0.95             |
| 04    | 56               | 33               | 30               | 3                | 0.91             |
| 05    | 57               | 57               | 52               | 5                | 0.91             |
| 06    | 142              | 107              | 99               | 8                | 0.93             |
| **07** | **353**          | **235**          | **184**          | **51**           | **0.78**         |
| 08    | 47               | 46               | 44               | 2                | 0.96             |
| **Sum:** | **788**          | **611**          | **529**          | **82**           | **0.87**         |

**Notes:** \(N_{\text{tot}}\): Total number of RRab stars from the list of Molnár et al. (2018); \(N_{\text{RRab}}\): Actual number of RRab stars publicly available from the NASA Exoplanet Archive; \(N_{\text{BL}}\): Number of Blazhko stars; \(N_{\text{nonBL}}\): Number of non-Blazhko stars (single period or other). Campaign 07 is highlighted because of the low Blazhko rate – see text.

\(^2\)https://exoplanetarchive.ipac.caltech.edu/
The campaign-by-campaign incidence rates are shown in Table 1. We missed certain targets from the list of Molnár et al. (2018), because they were not included in the publicly available databases. Nevertheless, this study is based on four times larger sample than our pilot survey (Kovacs 2018), yielding statistically more significant estimate of the high incidence rate of the Blazhko effect. The field of C07 has apparently a low rate, but this is likely due to the overabundance of faint, blended targets associated with the Sagittarius dwarf galaxy.

![Figure 3: Residual Fourier spectra of a star from two overlapping campaigns. Spectra of the residuals after subtracting the variation corresponding to the monoperiodic pulsation are shown. Insets are zoomed near the fundamental frequency $\nu_0$. Interestingly, the modulation power is higher at the harmonics of $\nu_0$. The panels on the right show the systematics-filtered light curves (the magnitude zero point is arbitrary). The object was classified as a non-Blazhko variable by Plachy et al. (2019) – see text for possible reasons.](image)

In recent paper, Plachy et al. (2019) claim a more traditional observed rate of $\sim$ 50%, based on the analysis of the fields of C03–C06. Although we did not make a star-by-star comparison between their and our results, the following examples are aimed for the illustration of the possible sources of the discrepancy.

Figure 3 shows an example for a target of short modulation period, that was misclassified likely because of the poor performance of the K2SC detrending algorithm in this particular case. Figure 4, on the other hand, shows the frequency spectra of two stars from their Fig. 12. We guess that in these cases K2SC might have over-fitted the data and eliminated the small amplitude of the long period modulation. We

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3The 3rd star shown in their figure is not accessible from the public archives used in our work.
also note that their classification (Plachy, private communication) have multiple components (including the less sensitive O-C analysis), that leads to the de-selection of many candidates that otherwise show signatures of modulation in the frequency spectra.

Figure 4.: Fourier spectra of two stars classified as non-Blazhko variables by Plachy et al. (2019). Figure setting is the same as in Fig. 3. High-frequency peaks above 8 c/d are aliases (via the half hour sampling) of the higher (16th and up) harmonics left in the time series. The heights of the side lobes are ~ 5 and ~ 0.5 ppt for 206333750 and 210697426, respectively.

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References

Aigrain, S., Parviainen, H., & Pope, B. J. S. 2016, MNRAS, 459, 2408
Bakos, G. A., Torres, G., Pál, Á., et al. 2010, ApJ, 710, 1724
Benkő, J. M., Plachy, E., Szabó, R., et al. 2014, ApJS, 213, 31
Blažko, S. 1907, Astronomische Nachrichten, 175, 325
Kovács, G., Bakos, G., & Noyes, R. W. 2005, MNRAS, 356, 557
Kovács, G. 2016, Communications of the Konkoly Observatory Hungary, 105, 61
Kovács, G. 2018, A&A, 614, L4
Luger, R., Kruse, E., Foreman-Mackey, D., et al. 2018, AJ, 156, 99
Molnár, L., Plachy, E., Juhász, Á., et al. 2018, A&A, 620, A127
Petigura, E. A., Schlieder, J. E., Crossfield, I. J. M., et al. 2015, ApJ, 811, 102
Plachy, E., Molnár, L., Bódi, Á., et al. 2019, ApJS, 244, 32
Prudil, Z., & Skarka, M. 2017, MNRAS, 466, 2602
Skarka, M., Prudil, Z., & Jurcsik, J. 2020, MNRAS, 494, 1237
Smith, J. C., Stumpe, M. C., Van Cleve, J. E., et al. 2012, PASP, 124, 1000
Smolec, R. 2016, 37th Meeting of the Polish Astronomical Society, 22
Stumpe, M. C., Smith, J. C., Van Cleve, J. E., et al. 2012, PASP, 124, 985
Tamuz, O., Mazeh, T., & Zucker, S. 2005, MNRAS, 356, 1466
Vanderburg, A., & Johnson, J. A. 2014, PASP, 126, 948