Molecular Laser-Cooling in a Dynamically Tunable Repulsive Optical Trap

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Recent work with laser-cooled molecules in attractive optical traps has shown that the differential AC Stark shifts arising from the trap light itself can become problematic, limiting collisional shielding efficiencies, rotational coherence times, and laser-cooling temperatures. In this work, we explore trapping and laser-cooling of CaF molecules in a ring-shaped repulsive optical trap. The observed dependences of loss rates on temperature and barrier height show characteristic behavior of repulsive traps and indicate strongly suppressed average AC Stark shifts. Within the trap, we find that Λ-enhanced gray molasses cooling is effective, producing similar minimum temperatures as those obtained in free space. By combining in-trap laser cooling with dynamical reshaping of the trap, we also present a method that allows highly efficient and rapid transfer from molecular magneto-optical traps into conventional attractive optical traps, which has been an outstanding challenge for experiments to date. Notably, our method could allow nearly lossless transfer over millisecond timescales.

Ultracold polar molecules, with their rich structure and long-range dipolar interactions, have been proposed as an ideal platform for many applications ranging from quantum simulation and information processing to precision measurement [1–4]. These possibilities have led to intense experimental efforts to produce, cool and control molecules, with many advances along the way. In particular, the approach of direct laser-cooling has seen tremendous progress in the past few years. Starting with the first molecular magneto-optical traps (MOTs) [5–8], direct laser-cooling promises to be a versatile and efficient route into the ultracold regime for a large variety of molecules [9–14]. Many potential applications for molecules require conservative trapping in the absence of resonant light, motivating recent work on magnetic trapping [15] and optical dipole trapping using off-resonant light [16–18]. To date, attractive optical traps have been used and sub-Doppler cooling has been shown to remain somewhat effective in these traps. This has enabled preparation of samples with record phase-space densities and also high-fidelity detection of optically trapped molecules [17–19]. Nevertheless, the large AC Stark shifts that give rise to trapping can themselves be problematic. For example, differential AC Stark shifts between internal states are thought to limit in-trap laser-cooling temperatures [17, 19, 20], coherence times between rotational states [21], and the effectiveness of shielding molecular samples from inelastic collisions [22]. In attractive optical traps, molecules preferentially occupy regions with high trap light intensity and hence experience near-maximal AC Stark shifts. In contrast, molecules in repulsive traps experience minimal AC Stark shifts, since they reside in areas of minimal light intensity.

In addition to reducing differential AC Stark shifts, repulsive optical potentials also aid in preparing large optically trapped samples, crucial for many applications. In experiments to date, the mismatch in trap volume between attractive optical traps (typically ~ 100 μm

**FIG. 1.** (a) Experimental Setup. The ring-shaped repulsive optical trap is shown in green. An attractive optical dipole trap (red) formed from a focused Gaussian beam runs along the ring trap axis. Molecules are detected by imaging along the same axis. (b) Intensity distribution of the ring trap with radius set to \( r_0 = 160(10) \) μm. (c) Model potential used to describe the repulsive trap. (d) Energy level diagram of CaF with relevant levels and transitions shown.

due to limitations in laser power) and the initial MOTs (mm-sized) have limited transfer fractions to well below unity [17–19]. Since repulsive optical potentials can be more power-efficient, larger trap volumes are possible given the same absolute AC polarizabilities. In particular, for an attractive trap formed from a single laser beam, the power required for a given trap depth scales with the cross-sectional area of the laser beam, while for a ring-shaped repulsive trap, the required power scales with the circumference.

These two benefits, smaller AC Stark shifts and larger trap volumes, motivate exploring trapping of laser-cooled molecules with repulsive optical potentials. In this work, we demonstrate 2D-trapping and laser-cooling of CaF molecules in a near-detuned repulsive optical barrier. The starting point for this work is a Λ-cooled cloud of
CaF molecules in the \(|X, v = 0, N = 1\) rotational manifold at zero magnetic field [23]. In brief, a DC-MOT [24] of CaF molecules is loaded from a cryogenic buffer gas beam (CBGB) [25] that is slowed via chirped slowing [26, 27]. The MOT is subsequently compressed by ramping down the MOT beam powers and ramping up the magnetic field gradient. The magnetic field is then switched off and \(\Lambda\)-enhanced gray molasses cooling is turned on for 10 ms. The \(\Lambda\)-cooling light has a single photon detuning of \(\Delta = 26\) MHz and contains two hyperfine components addressing the \(|J = 1/2, F = 1\rangle\) and \(|J = 3/2, F = 2\rangle\) states. The \(\Lambda\)-cooled cloud consists of \(4.5 \times 10^4\) molecules at a temperature of \(\sim 10\) \(\mu\)K, and has a Gaussian diameter \((2\sigma)\) of 1.2(1) mm.

The ring-shaped repulsive optical trapping potential is generated using a laser beam with light blue-detuned by \(\Delta_t = 108\) GHz from the \(X^2\Sigma^+(v = 0, N = 1) \rightarrow B^2\Sigma^+(v = 0, N = 0)\) transition. The ring size is dynamically tunable using two liquid lenses over ms timescales [23]. To a good approximation, the potential is axially invariant in the region explored by the molecules. In addition, the lack of thermalization over the experimental timescales implies that only the radial dynamics are relevant and the situation is effectively 2-dimensional. Since the molecular temperature \(k_B T\) is much lower than the barrier height \(U_0\), the potential explored by the molecules is well-approximated by

\[
U(r) = \begin{cases} 
0, & r \leq r_0 \\
\alpha (r - r_0)\sigma^*, & r > r_0, 
\end{cases}
\]

where \(\alpha \gg 1\) (Fig. 1(c)).

In optical traps, undesirable effects such as differential AC Stark shifts and heating are proportional to the trap light intensity. Since the off-resonant photon scattering rate is also proportional to the light intensity, one can use the trap-averaged photon scattering rate \(\langle \Gamma_{sc}\rangle_{\text{trap}}\) as a figure-of-merit. For a thermal ensemble in an attractive trap, \(\langle \Gamma_{sc}\rangle_{\text{trap}} \propto V\), where \(V\) is the trap depth. In contrast, for a repulsive trap, the scaling of \(\langle \Gamma_{sc}\rangle_{\text{trap}}\) with barrier height is geometry-dependent. For the ring-shaped barrier explored here, \(\langle \Gamma_{sc}\rangle_{\text{trap}}\) is approximately linear with \(T\) and independent of barrier height:

\[
\langle \Gamma_{sc}\rangle_{\text{trap}} \propto \frac{\int dr U(r)e^{-U(r)/(k_B T)}}{\int dr e^{-U(r)/(k_B T)}} \propto T \left( \frac{T}{a} \right)^{O(1/a)} \quad (2)
\]

Photon scattering and therefore differential Stark shifts can therefore be strongly suppressed at low temperatures. We note in passing that similar scaling laws for other repulsive trap geometries have previously been derived in work with ultracold atoms [28].

To observe these scalings, we first characterize trap heating and loss, which serve as probes for \(\langle \Gamma_{sc}\rangle_{\text{trap}}\). Molecules are transferred from the \(\Lambda\)-cooled cloud into a conventional attractive optical dipole trap (ODT) concentric with the ring trap. The ODT is generated using a single laser beam at 1064 nm focused to a Gaussian waist of \(60(7)\) \(\mu\)m, much smaller than the repulsive ring radius, and retro-reflected to form a 1D lattice (Fig. 1(a)). Subsequently, the cooling light is switched off and untrapped molecules fall away over 50 ms. The molecules are then released into the repulsive ring trap, which has radius \(r_0 = 160(10)\) \(\mu\)m and a barrier height of \(U_0/k_B = 240(30)\) \(\mu\)K. Subsequently, a 2 ms \(\Lambda\)-cooling pulse recools the cloud to \(10(1)\) \(\mu\)K. After holding the sample in the trap for time \(t\), the number and the temperature \(T\) are measured. We measure a \(1/e\) lifetime of \(42(3)\) ms, but find no observable temperature increase over this timescale (Fig. 2(a,b)).

At first sight, the lack of significant heating seems to contradict Eq. (2), which predicts \(T \propto T\) and hence exponentially increasing temperatures. Our observations are nevertheless consistent with theory when one takes into account rotational loss due to Raman scattering, which is also proportional to \(\langle \Gamma_{sc}\rangle_{\text{trap}}\). Specifically in our case, molecules off-resonantly excited to \(|B, v = 0, N = 0\rangle\) always return to \(|X, v = 0, N = 1\rangle\) and experience recoil heating, but molecules excited to \(|B, v = 0, N = 2\rangle\) are lost from detection if they decay to \(|X, v = 0, N = 3\rangle\). One therefore expects a rotational loss rate \(\sim \langle \Gamma_{sc}\rangle_{\text{trap}}\). On the other hand, photon scattering imparts kinetic energy at a rate of \(\sim \langle \Gamma_{sc}\rangle_{\text{trap}} E_R\), where \(E_R = h^2 k^2/(2m) = k_B \times 0.58\) \(\mu\)K is the recoil energy, and \(k\) is the trapping light wavevector. Since the initial temperature \((10\) \(\mu\)K) is well above \(E_R/k_B\), molecules are rotationally lost before significant heating occurs. This generically holds true in far-detuned optical traps when temperatures are well above \(E_R/k_B\), a regime reached in many laser-cooling experiments.

The observed loss rate is therefore a proxy for \(\langle \Gamma_{sc}\rangle_{\text{trap}}\), and should therefore be linear in temperature \(T\) and independent of barrier height \(U_0\), in accordance with Eq. (2). To observe the temperature dependence, we vary the molecular temperature between \(9.4(3)\) \(\mu\)K and...
61(4) µK by adjusting the cooling parameters during a 2 ms Λ-cooling pulse following trap loading. Indeed, we find that the 1/e loss rate $\gamma$ increases linearly with $T$ with an offset at $T = 0$ (Fig. 2(c)). The $T = 0$ offset could arise from residual light on the interior of the ring and other loss mechanisms such as collisions with background gas and leaked resonant light. We note that the observed loss rates are $\sim 10^{-2} \Gamma_{sc,max}$, where $\Gamma_{sc,max}$ is the theoretically predicted loss rate at the peak barrier intensity [23]. Since the average AC Stark shifts are also proportional to $\langle \Gamma_{sc} \rangle_{trap}$, this indicates that they are strongly suppressed compared to an attractive trap with a similar depth and absolute polarizability.

We next probe the dependence of $\langle \Gamma_{sc} \rangle_{trap}$ on barrier height $U_0$. We begin with molecules at 10(1) µK within the barrier, and then suddenly change the barrier height $U_0/k_B$ to a value between 50 µK and 230 µK. As shown in Fig. 2(d), the loss rates increase slightly with $U_0$. This generally agrees with Eq. (2), which predicts $\gamma$ to be largely independent of $U_0$, in stark contrast to the linear scaling found in attractive traps ($\gamma \propto V$). The small increase in loss rate with $U_0$ likely arises from residual light within the ring.

Having explored the dependences of loss and heating on $T$ and $U_0$, we next investigate whether laser-cooling, specifically Λ-cooling, continues to be effective within the repulsive barrier. Because of the suppressed AC Stark shifts, one could expect in-trap laser-cooling to perform similarly as in free space, in contrast to attractive optical traps where significant AC Stark shifts can affect the effectiveness of Λ-cooling by destabilizing the coherent dark states involved. This should be true on timescales shorter than the transit time $\tau_t$ of a molecule across the trap ($\tau_t = r_0/\sqrt{2k_BT/m} \approx 1 - 3$ ms). On longer timescales, the effectiveness of in-trap Λ-cooling is not guaranteed. The repulsive trap light can lead to heating and loss in several ways. First, the electronically excited state could experience opposite AC Stark shifts and the molecules could become untrapped when they reach the ring. Second, strong differential Stark shifts could convert Λ-cooling into Λ-heating. In our case, these are non-negligible, since $\Delta \approx 5B$, where $B \approx 20$ GHz is the rotational constant. Third, multi-photon processes involving the repulsive trap light in combination with the cooling light can also lead to heating or loss.

To characterize in-trap Λ-cooling, we compare temperatures obtained in free space to those obtained in-trap following identical laser-cooling pulses. Molecules are loaded from the Λ-cooled cloud into the ring trap by subsequently switching the trap on, which ensures that the in-ring molecules are in contact with the repulsive light. Subsequently, we wait 30 ms for untrapped molecules to fall away. A 5 ms Λ-cooling pulse with various detunings $\Delta$ and intensities $I$ is then applied, both with or without the ring present. The temperature is then measured via time-of-flight expansion. Over the explored range of Λ-cooling parameters, we observe no significant difference between temperatures obtained in-trap ($T_{FS}$) and those obtained in free space ($T_{FS}$) (Fig. 3(a)). Notably, the minimum temperature reached in the trap is similar to that obtained in free-space. To investigate whether additional heating processes involving trap light are present, we plot the ratio $\kappa = T_{trap}/T_{FS}$ as a function of the cooling light intensity $I$ (Fig. 3(b)), and observe no dependence. This rules out any significant heating contributions from processes involving both cooling light and trapping light, since an incoherent process with $n$ photons of cooling light would show $I^n$ dependence.

We next examine whether laser-cooling leads to additional losses for the trapped molecules. We compare the $1/e$ lifetimes $\tau$ of the trapped molecules with and without Λ-cooling light, and find $\tau = 57(1)$ ms and $\tau = 40(1)$ ms respectively. These are much longer than the transit time $\tau_t$, which indicate that in-trap cooling does not lead to additional losses compared to trapping alone. We note in passing that we obtain lifetimes up to 100 ms when the repulsive barrier light is further detuned [23].

In the last part of this work, we illustrate how repulsive optical traps can be used to transfer molecules from a MOT into an optical trap with high efficiency. In past experiments, the size mismatch of typical optical traps with MOTs have been a limiting factor in achieving high transfer fractions. Although Λ-cooling-assisted optical loading helps by enlarging the capture volume beyond the bare size of the optical trap, the highest observed transfer fractions have been limited to $\sim 5\%$ to date [17]. As mentioned earlier, repulsive traps with a suitable geometry are more power-efficient than their attractive counterparts, and can therefore be made much larger. To illustrate this, we set the repulsive ring radius to $r_0 = 414(2) \mu$m (barrier height $U_i/k_B = 65(1)$ µK) to maximize the spatial overlap with the Λ-cooled cloud, which is similar in size to the initial MOT. The ring trap is switched on following initial Λ-cooling, after which we wait 21 ms for any transient dynamics to damp out. We subsequently image the molecular cloud in-situ using a 250 µs imaging pulse with resonant light. Despite blurring from the imaging process [23], we observe a clear...
boundary between trapped and untrapped molecules, and find that 27(3)% of the molecules are captured into the repulsive trap (Fig. 4(b)).

Despite its advantage of achieving large trap volumes with limited laser power, the ring-shaped geometry has a drawback. Since the molecule density is set by the ring size, in-trap laser-cooling produces negligible density enhancement, unlike in Gaussian-shaped attractive traps where density is strongly enhanced at lower temperatures [16–19]. To benefit from both the large capture volume of the repulsive trap and the density enhancement offered by a conventional attractive ODT, we implement the following two-step transfer scheme. After initial transfer into the large volume ring trap, we compress the trap in the presence of laser-cooling by dynamically tuning the ring size. The compressed samples are then loaded into an attractive ODT. With better mode-matching offered by trap compression, high transfer fractions can be achieved.

In detail, we switch on the repulsive ring with initial radius $r_i = 414(2) \mu$m and barrier height $U_i/k_B = 65(1) \mu$K. Subsequently, the radius is smoothly compressed to $r_f = 160(10) \mu$m and the barrier height is ramped to $U_f/k_B = 240(30) \mu$K over 21 ms (Fig. 4(a)) [23]. In-situ images show rising densities throughout compression (Fig. 4(b,c,d,e)). In addition, we find that $T$ remains constant at its initial value of $T_i \approx 10 \mu$K [23]. This indicates sufficient cooling, since in the absence of cooling, compression-induced heating would lead to a final temperature $T_f \geq \alpha T_i$, where the lower bound is for an adiabatic ramp and $\alpha = r_i^2/r_f(t)^2$ is the compression ratio.

To transfer molecules from the repulsive trap into the much smaller attractive ODT, we switch on the attractive trap in the presence of $\Lambda$-cooling light. Fig. 4(f) shows the transfer fraction $f = N_{\text{ODT}}/N_{\text{SD}}$ as a function of transfer time $t$, where $N_{\text{SD}}$ is the initial molecule number in the $\Lambda$-cooled cloud measured within the same experimental sequence. The transfer fraction initially rises and then saturates, with both the loading rate and the saturated transfer fraction increasing with compression. Since the initial loading rate $R_0 = N_{\text{ODT}}(t = 0)/N_{\text{SD}}$ is proportional to the initial density, the normalized initial loading rate $\eta = R_0(\alpha)/R_0(\alpha = 1)$ directly measures the density enhancement. As shown in Fig. 4(g), we observe a peak enhancement factor of 6 and find that $\eta \approx \alpha$, consistent with the geometric expectation from the reduced ring area. At maximum compression ($\alpha \approx 6$), rapid saturation times around 10 ms are observed, much faster than the $\sim 100$ ms times previously reported [17–19]. We also observe highly efficient transfer, with 45(5)% of the repulsively trapped molecules transferred into the attractive ODT. This corresponds to an overall transfer efficiency of 12(2)% from the $\Lambda$-cooled cloud, and a total of $5.4(5) \times 10^3$ molecules in the attractive ODT.

Although the loading rate is enhanced six-fold by trap compression, the final trapped number is enhanced two-fold. We believe that the overall transfer efficiency is likely limited by the number initially captured in the repulsive trap. We estimate that the transfer fraction is consistent with the observed lifetimes in the repulsive trap, which can be increased with faster compression. Theoretically, we find that the compression rate $\dot{r}/r$ can in fact be as fast as the cooling rate $T/\dot{T}$ [23]. Based on the observed and theoretically predicted sub-Doppler cooling timescales of $\approx 100 \mu$s [16, 29–31], sub-ms-scale compression, much faster than the 21 ms used here, is in principle possible.

In conclusion, we have explored trapping and laser-cooling of molecules in a near-detuned repulsive optical potential. We find rotational loss, rather than heating, to be the dominant feature at laser-cooling temperatures. Loss measurements reveal temperature and power dependences characteristic of repulsive traps, consistent with strongly suppressed off-resonant photon scattering rates and average AC Stark shifts. In addition, despite using repulsive light detuned by only a few rotational spacings, we find that in-trap $\Lambda$-cooling performs similarly as in free space, and find no evidence of additional losses due to the trapping light. By combining laser-cooling with dynamical reshaping of a repulsive trap, we have also presented a new method that rapidly transfers laser-cooled molecules into optical traps with record efficiencies. With

![Fig. 4](image-url)
improvements such as faster compression and more optimal trap shaping, our method could allow nearly lossless transfer of molecules from MOTs into optical traps, overcoming an outstanding challenge in experiments to date.

Looking ahead, laser-cooling in dynamically tunable repulsive traps could be useful in a variety of future explorations, such as evaporative cooling. The shielding of molecules from collisional loss is expected to be much more effective due to suppressed differential Stark shifts [22], and dynamical compression can offer high starting densities. The work here could also guide the development of bottle-beam optical tweezers [32] for molecules, where internal state decoherence caused by differential AC Stark shifts could be suppressed [21]. Methods shown in this work could also be useful for precision measurement experiments with trapped and laser-cooled molecules [4]. Repulsive ring traps could suppress effects due to trap inhomogeneity, and dynamic trap decompression could be used to lower molecular densities and temperatures, thereby reducing systematic effects that arise from Doppler shifts and molecular interactions.

Y.L. and C.M.H. contributed equally to this work.

[1] A. Micheli, G. K. Brennen, and P. Zoller, Nature Physics 2, 341 (2006).
[2] L. D. Carr, D. DeMille, R. V. Krems, and J. Ye, New Journal of Physics 11, 055049 (2009).
[3] J. A. Blackmore, L. Caldwell, P. D. Gregory, E. M. Bridge, R. Sawant, J. Aldegunde, J. Mur-Petit, D. Jaksch, J. M. Hutson, B. E. Sauer, M. R. Tarbutt, and S. L. Cornish, Quantum Science and Technology 4, 014010 (2018).
[4] B. L. Augenbraun, Z. D. Lasner, A. Frenett, H. Sawaoka, C. Miller, T. C. Steimle, and J. M. Doyle, New Journal of Physics 22, 022003 (2020).
[5] J. F. Barry, D. J. McCarron, E. B. Norrgard, M. H. Steinke, and D. DeMille, Nature 512, 286 (2014).
[6] S. Truppe, H. J. Williams, M. Hambach, L. Caldwell, N. J. Fitch, E. A. Hinds, B. E. Sauer, and M. R. Tarbutt, Nature Physics 13, 1173 (2017).
[7] L. Anderegg, B. L. Augenbraun, E. Chae, B. Hemmerling, N. R. Hutzler, A. Ravi, A. Collopy, J. Ye, W. Ketterle, and J. M. Doyle, Phys. Rev. Lett. 119, 103201 (2017).
[8] A. L. Collopy, S. Ding, Y. Wu, I. A. Finneran, L. Anderegg, B. L. Augenbraun, J. M. Doyle, and J. Ye, Phys. Rev. Lett. 121, 213201 (2018).
[9] I. Kozyryev, L. Baum, K. Matsuda, B. L. Augenbraun, L. Anderegg, A. P. Sedlack, and J. M. Doyle, Physical review letters 118, 173201 (2017).
[10] J. Lim, J. R. Almond, M. A. Trigatzis, J. A. Devlin, N. J. Fitch, B. E. Sauer, M. R. Tarbutt, and E. A. Hinds, Phys. Rev. Lett. 120, 123201 (2018).
[11] D. Mitra, N. B. Vilas, C. Hallas, L. Anderegg, B. L. Augenbraun, L. Baum, C. Miller, S. Raval, and J. M. Doyle, Science 369, 1366 (2020).
[12] B. L. Augenbraun, J. M. Doyle, T. Zelevinsky, and I. Kozyryev, Phys. Rev. X 10, 031022 (2020).
[13] L. Baum, N. B. Vilas, C. Hallas, B. L. Augenbraun, S. Raval, D. Mitra, and J. M. Doyle, Physical Review A 103, 043411 (2021).
[14] X. Alauze, J. Lim, M. Trigatzis, S. Swarbrick, F. Collings, N. Fitch, B. Sauer, and M. Tarbutt, Quantum Science and Technology 6, 044005 (2021).
[15] H. J. Williams, L. Caldwell, N. J. Fitch, S. Truppe, J. Rodewald, E. A. Hinds, B. E. Sauer, and M. R. Tarbutt, Phys. Rev. Lett. 120, 163201 (2018).
[16] L. Anderegg, B. L. Augenbraun, Y. Bao, S. Burchesky, L. W. Cheuk, W. Ketterle, and J. M. Doyle, Nature Physics 14, 890 (2018).
[17] T. K. Langin, V. Jorapur, Y. Zhu, Q. Wang, and D. DeMille, arXiv:2106.06622 (2021).
[18] Y. Wu, J. J. Burau, K. Mehling, J. Ye, and S. Ding, arXiv:2107.06422 (2021).
[19] L. W. Cheuk, L. Anderegg, B. L. Augenbraun, Y. Bao, S. Burchesky, W. Ketterle, and J. M. Doyle, Phys. Rev. Lett. 121, 083201 (2018).
[20] L. Caldwell and M. Tarbutt, Physical Review Research 2, 013251 (2020).
[21] S. Burchesky, L. Anderegg, Y. Bao, S. S. Yu, E. Chae, W. Ketterle, K.-K. Ni, and J. M. Doyle, arXiv:2105.15199 (2021).
[22] L. Anderegg, S. Burchesky, Y. Bao, S. S. Yu, T. Karman, E. Chae, K.-K. Ni, W. Ketterle, and J. M. Doyle, Science 373, 779 (2021).
[23] See Supplemental Material.
[24] M. R. Tarbutt and T. C. Steimle, Phys. Rev. A 92, 053401 (2015).
[25] N. R. Hutzler, H.-I. Lu, and J. M. Doyle, Chem. Rev. 112, 4803 (2012).
[26] S. Truppe, H. J. Williams, N. J. Fitch, M. Hambach, T. E. Wall, E. A. Hinds, B. E. Sauer, and M. R. Tarbutt, New Journal of Physics 19, 022001 (2017).
[27] C. M. Holland, Y. Lu, and L. W. Cheuk, New Journal of Physics 23, 033028 (2021).
[28] N. Friedman, A. Kaplan, and N. Davidson, Advances in Atomic Molecular and Optical Physics 48, 99 (2002).
[29] J. Devlin and M. Tarbutt, New Journal of Physics 18, 123017 (2016).
[30] L. Caldwell, J. A. Devlin, H. J. Williams, N. J. Fitch, E. A. Hinds, B. E. Sauer, and M. R. Tarbutt, Phys. Rev. Lett. 123, 033202 (2019).
[31] S. Ding, Y. Wu, I. A. Finneran, J. J. Burau, and J. Ye, Phys. Rev. X 10, 021049 (2020).
[32] D. Barredo, V. Lienhard, P. Scholl, S. de Léséleuc, T. Boulier, A. Browaeys, and T. Lahaye, Phys. Rev. Lett. 124, 023201 (2020).
I. EXPERIMENTAL APPARATUS AND PREPARATION OF MOLECULAR SAMPLES

A. Apparatus Overview

Our apparatus consist of three parts, a cryogenic chamber used to produce a molecular beam, an intermediate chamber, and a main chamber where laser-cooling and trapping occurs (Fig. S1(a)). The three chambers are connected in series by differential pumping tubes. During the experiment, the cryogenic chamber has a typical pressure of $\sim 1 \times 10^{-9}$ Torr, while the intermediate and main chambers are held at ultra high vacuum pressures (UHV) of $\sim 3 \times 10^{-10}$ Torr and $\sim 1 \times 10^{-10}$ Torr, respectively.

Laser beams used for laser-slowing, magneto-optical trapping, sub-Doppler cooling and fluorescent imaging enter the chamber from a variety of paths. The main cooling light ($X^2\Sigma^+(v = 0, N = 1) \rightarrow A^2\Pi_{1/2}(v = 0, N = 0)$) used for magneto-optical trapping and Λ-cooling/imaging enter along the $x, y, z$ axes. Also, the first vibrational repumping light ($X^2\Sigma^+(v = 1, N = 1) \rightarrow A^2\Pi_{1/2}(v = 0, N = 0)$) is also sent along these paths. The slowing light ($X^2\Sigma^+(v = 0, N = 1) \rightarrow B^2\Sigma^+(v = 0, J = 1/2, +)$) and three vibrational repumpers ($X^2\Sigma^+(v = 1, 2, 3, N = 1) \rightarrow A^2\Pi_{1/2}(v = 0, N = 0)$) enter along the molecular beam axis $x'$, which is oriented 45 degrees to the $x, y$ axes (Fig. S1(b)).

For our work here, we detect molecules by measuring their fluorescence as they cycle on the $X$-$A$ transition. This fluorescence is imaged along the imaging path ($y'$ axis) onto an EMCCD camera. The repulsive ring trap propagates along the imaging path and is mostly filtered out with a dichroic mirror before reaching the camera. The attractive optical dipole trap is also sent in along this same axis using a dichroic mirror, but propagates opposite to the imaging path.

B. Molecular Source

Our experimental sequence begins with the generation of a cryogenic buffer gas beam (CBGB) of CaF molecules with significant population in the laser-coolable $X^2\Sigma^+(v = 0, N = 1)$ manifold [1]. In detail, a Ca target is ablated using a pulsed Nd:YAG laser (frequency doubled to 532 nm) in the presence of $^4$He and SF$_6$ inside a buffer gas cell held at 3.5 K. A subsequent chemical reaction produces CaF molecules [2], which are cooled via collisions with the $^4$He gas, producing a bright beam of CaF molecules with a mean forward velocity of 150 to 180 m/s. We typically flow 1 sccm of $^4$He and 0.05 sccm of SF$_6$ into the cell.
C. Chirped Laser Slowing of Molecular Beam

The CBGB of molecules are then slowed via chirped slowing to near zero velocity using a counter-propagating laser beam addressing the rotationally closed \(X^2\Sigma^+(v = 0, N = 1) \rightarrow B^2\Sigma^+(v = 0, N = 0)\) transition (\(\lambda = 531.0\, \text{nm}\)) [3]. To address the four hyperfine manifolds in order to obtain photon cycling, we engineer the required frequency spectrum using a high-bandwidth fiberized electro-optical modulator (EOM) combined with a computer generated holography (CGH) technique [4]. To slow molecules, the frequency of the cooling light is continuously chirped to stay on resonance with decelerating molecules. The slowing light is turned on to 2 to 3 ms following laser ablation, and is initially red-detuned by \(\approx 500\, \text{MHz}\). Its frequency is then ramped linearly to resonance over 4.7 ms. This sequence maximizes the slow molecular population (within the MOT capture velocity) at the center of our UHV chamber, which is centered 80 cm from the exit aperture of our buffer gas cell.

To repump molecules that vibrationally decay into the \(v = 1, 2, 3\) manifolds during the slowing process, we combine our slowing light with three vibrational repumpers addressing the \(X^2\Sigma^+(v = 1, N = 1) \rightarrow A^2\Pi_{1/2}(v = 0, J = 1/2, +)\) (\(\lambda = 628.6\, \text{nm}\)), \(X^2\Sigma^+(v = 2, N = 1) \rightarrow A^2\Pi_{1/2}(v = 1, J = 1/2, p = +)\) (\(\lambda = 628.1\, \text{nm}\)), and \(X^2\Sigma^+(v = 3, N = 1) \rightarrow A^2\Pi_{1/2}(v = 2, J = 1/2, p = +)\) (\(\lambda = 627.7\, \text{nm}\)) transitions. The frequencies of the \(v = 1, 2\) repumpers are also ramped during chirped slowing. Frequency sidebands addressing the ground state hyperfine levels are imprinted using free-space resonant EOMs at a modulation frequency of \(f = 25\, \text{MHz}\) with modulation indices of \(\beta = 3.2(2)\) and \(\beta = 3.8(2)\) for \(v = 1\) and \(v = 2, 3\) repumpers, respectively. The slowing beam and repumping beams all have diameters of \(\sim 10\, \text{mm}\), and their powers are 880 mW for slowing, 290 mW for \(v = 1, 35\, \text{mW for} v = 2,\) and \(3\, \text{mW for} v = 3.\)

D. Magneto-Optical Trapping and Compression

The slowed molecules are then loaded into a DC magneto-optical trap (MOT) operating on the \(X^2\Sigma^+(v = 0, N = 1) \rightarrow A^2\Pi_{1/2}(v = 0, J = 1/2, +)\) transition (\(\lambda = 606.3\, \text{nm}\)) [5]. The MOT light is red-detuned from resonance (\(\Delta = -5.5\, \text{MHz}\)) and sidebands addressing the four ground state hyperfine components are generated using acousto-optical modulators (AOMs). In addition to the main MOT cooling light, the MOT beams also contain \(v = 1\) light. The MOT beams are sent into the chamber along 3 orthogonal axes (\(x', y'\) and \(z\)) and retro-reflected. During MOT loading, the \(v = 1\) light along the slowing path is turned off, but \(v = 2\) and \(v = 3\) light remain on.

During slowing, the axial magnetic field gradient is initially set to 26 G/cm, and the MOT beams are kept on with a power of 22 mW (single-beam, single-axis). Initially, each MOT beam contain hyperfine components with single-axis single-pass powers of 9.4 mW, 5.5 mW, 1.8 mW, 5.3 mW for \(F = 2, F = 1^+, F = 0,\) and \(F = 1^-\), respectively, and has a beam diameter of \(\sim 1\, \text{cm}\). The \(v = 1\) repump light has a single-axis single-pass power of 41 mW. After loading molecules into the MOT for 5 ms, we compress the MOT by ramping the magnetic gradient to 106 G/cm over 10 ms, while simultaneously lowering the MOT beam power from 22 mW to 2 mW. The power balance between the hyperfine components is unchanged during MOT compression.

E. A-Enhanced Gray Molasses Cooling

After the MOT is compressed, the magnetic field is switched off, and we perform A-enhanced gray molasses cooling [6]. The MOT frequency is jumped to a single-photon detuning of \(\Delta = 21\, \text{MHz}\), the \(F = 1^+, 0\) components are turned off, and the \(F = 2, 1^-\) components are set to be on two-photon resonance. The \(v = 1, 2, 3\) repumpers remain unchanged from the MOT configuration. For optimal A-cooling, we null the magnetic field using three pairs of bias coils.

To optimize the density and temperature of the molecular samples, we specifically use the following sequence. Molecules are first cooled for 1 ms at a single-photon detuning \(\Delta = 21\, \text{MHz}\), hyperfine ratio \(R_{2,1} = P_{F = 2}/P_{F = 1} = 0.66\), and total single-axis single-pass power of \(P_{\lambda} = 9.75\, \text{mW}\). These values are then ramped over the next ms to the final configuration of \(\Delta = 26\, \text{MHz}\), \(R_{2,1} = 0.67\), \(P_{\lambda} = 0.94\, \text{mW}\) and are held constant for the subsequent 8 ms. This procedure generates a molecular cloud containing \(\sim 4.5 \times 10^4\) molecules at \(10(1) \,\mu\text{K}\) with a Gaussian diameter (\(2\sigma\)) of 1.2(1) mm. This is the starting point of the work described in the main text.

II. Generating Attractive and Repulsive Optical Potentials

A. Attractive Optical Dipole Trap (ODT)

We form a single-beam attractive optical dipole trap (ODT) using \(\lambda = 1064\, \text{nm}\) light. The light passes through a 2-axis acousto-optical deflector (2D-AOD), which allows fast switching, location control, and intensity stabilization of the trapping beam. The single trap beam has a maximum power of 25 W and is focused to a waist of \(60(7)\, \mu\text{m}\), providing a single-pass trap depth of \(V_0/k_B = 170(30)\, \mu\text{K}\). To maximize the total trap depth, the beam is retro-reflected to form a 1D lattice.

B. Repulsive Ring Trap

The repulsive ring trap is generated using light blue-detuned from the \(X^2\Sigma^+(v = 0, N = 1) \rightarrow B^2\Sigma^+(v = 1, 2, 3)\) transitions. To this end, three repump light frequencies are ramped during chirped slowing.

\[\lambda = 628.6\, \text{nm} \quad \lambda = 628.1\, \text{nm} \quad \lambda = 627.7\, \text{nm}\]
0, \( N = 0 \) transition (\( \lambda = 531 \) nm). This light is generated via a DBR seed laser at \( \lambda = 1061.8 \) nm, which is amplified and frequency doubled. We shape this light into a variable-size ring beam with the setup shown in Fig. S1(b). In detail, a ring beam is first generated using an axicon lens, and subsequently passes through a chrome ring mask that is imaged using a telescope with variable magnification onto the molecules. The telescope comprises a pair of liquid lenses (Optotune EL-10-30-C-VIS-LD) whose focal lengths can be adjusted from \( f = 200 \) mm to \( 100 \) mm over ms timescales.

C. Ring Trap Compression Sequence

The compression sequence used in this work has a duration of 21 ms. Exemplary images showing the intensity distributions are shown in Fig. S2. The evolution of the ring radius, the barrier height, and their respective fractional variations are shown in Fig. S3 as a function of time along the compression sequence. During the compression sequence, the mean ring radius decreases from \( 413(2) \) \( \mu \)m to \( 160(10) \) \( \mu \)m while its fractional standard deviation \( \delta r_0/r_0 \) increases from 2% to 10%. The mean barrier height increases from \( U_0/k_B = 65(1) \) \( \mu \)K to \( U_0/k_B = 230(40) \) \( \mu \)K while its fractional standard deviation \( \delta U_0/U_0 \) varies between 10% and 25%. Exemplary images are shown at various times along the compression sequence in Fig. S2.

D. Ring Trap Characterization

To characterize the repulsive ring potential, we directly measure the trap light intensity distribution using a camera placed at an equivalent imaging plane. The camera is triggered at different points during the ring compression sequence, allowing us to also characterize any transient features.

Since the ring shape slightly deviates from circular due to ring-generation imperfections, we use the following an-
Fig. S4. (a) Exemplary curves showing maximum average counts versus rotation angle for a ring size of 160(10) µm for a few measurements. (b) Exemplary curves showing extracted radius versus rotation angle for a ring size of 160(10) µm.

To estimate the barrier height, we discard the left half of the 1D distribution from above, and the maximum intensity is recorded. We then extract the maximum intensity versus rotational angle, which is then converted to a barrier height via the theoretically calculated polarizability. Typically, we observe 10% to 25% variation \( \delta U_0/U_0 \) (fractional standard deviation) as a function of angle (Fig. S4). The mean barrier height reported in the main text is the average across all angles, while the error bar is obtained from the variation of this mean value across multiple measurements.

III. DETECTION METHODS AND THERMOMETRY

A. Imaging Methods and Procedure

We use two methods of fluorescent imaging on the \( X-A \) transition: \( \Lambda \)-imaging (\( \Delta \Lambda = 25.5 \text{ MHz} \)) \cite{6} and resonant imaging. For in-ring lifetime measurements with and without laser-cooling, a 100 ms \( \Lambda \)-imaging pulse is used. For lifetime measurements in Fig. 2(a, c) and Fig. S7, a 50 ms \( \Lambda \)-imaging pulse is used. For the normalizing image used in Fig. 2(d) and Fig. 4(f), a 20 ms \( \Lambda \)-imaging pulse is used (see Section II D for details concerning count normalization).

We find that both methods have significant effects on the spatial distribution of molecules in free-space at the 10's of µm scale, with resonant imaging performing better for the same signal-to-noise. We thus primarily use resonant imaging when measuring the spatial distribution of molecules. During resonant imaging, the detuning is set to \( \Delta = 0 \text{ MHz} \) and all hyperfine components are present. We use a 500 µs long imaging pulse when performing time-of-flight thermometry measurements in Fig. 2(b, c) and Fig. 3(a). We use a 250 µs resonant imaging for the in-situ images shown in Fig. 1(a) and Fig. 4(b, c, d, e).

To quantify the effect of imaging, we release molecules from the attractive ODT and image them using the two
methods for a variable time $t$. The molecules are initially loaded into the attractive ODT, after which the ODT is turned off immediately before the start of the imaging light exposure. As shown in Fig. S6, the squared width grows linearly with time under both imaging configurations, indicative of diffusive behavior.

Note that for Fig. 4(b, c, d), due to a large background from the repulsive barrier, the repulsive beam is kept off during resonant imaging. The observed images therefore suffer diffusive blurring, which becomes especially significant as the compression is increased and the ring becomes smaller.

B. Number Count Normalization

To reduce the effect of molecule number fluctuations, we use a normalization procedure implemented using a four-image sequence comprising two pairs of images (each with a signal and background). The signal image of the first pair records fluorescence during the initial $\Lambda$-cooling pulse following MOT loading. The signal image of the second pair is the measurement of interest. The background image of each pair is taken under identical light configuration to that of the signal image and is used for background subtraction. Hence, the first image pair can be used to monitor and correct for molecule number fluctuations.

C. Camera Count Calibration

To extract the conversion factor between camera counts and molecule number, we measure the photon scattering rate in both the $\Lambda$-imaging and resonant imaging configurations. We first measure the lifetime of the initial $\Lambda$-cooled cloud under each configuration, but with the $v = 2, 3$ repumpers turned off. Using published values of branching ratios [7, 8], we then deduce the photon scattering rate. By combining these measurements with the detection efficiency of our camera and losses along our imaging path, we obtain a conversion factor from camera counts to molecule number for the various imaging configurations.

D. Time-of-Flight Thermometry

We measure the temperature of our molecular samples using time-of-flight expansion. We fit an integrated cut across each of the camera axes ($x', z$) to a 1D Gaussian curve. The squared Gaussian width $\sigma^2$ of each axis is then plotted against the effective time of flight $t_{\text{TOF}}$, which takes into account the finite imaging duration. These data are fit to a linear model $\sigma^2 = c_1 t_{\text{TOF}}^2 + c_0$, and the slope $c_1$ is converted to a temperature via $T = mc_1/k_B$. The geometric mean of the extracted temperatures along the two axes ($T = \sqrt{T_{x'} T_z}$) is reported for all measurements. Note that this method is exact when both the initial spatial distribution and any blurring during imaging is described by convolution with a Gaussian kernel. These conditions are true of a good approximation for our system.

IV. SCALING LAWS FOR PHOTON SCATTERING IN A RING TRAP

In this section, we derive the scaling laws mentioned in the main text. We assume an ideal model for a repulsive ring trap, where $U(r)$ is given by

$$U(r) = 0, \quad r < r_0$$
$$U(r) = a(r - r_0)^\alpha, \quad r > r_0$$

For a thermal ensemble, the average potential experienced by a molecule can be computed via

$$\langle U \rangle_{\text{trap}} = \frac{1}{Z} \frac{2\pi}{r_z^2} \int r dr U(r) \exp \left[ \frac{-U(r)}{k_B T} \right]$$

$$= \frac{2\pi r_0^2}{Z} \xi \frac{\Gamma \left( \frac{2 + \frac{1}{\alpha}}{\alpha + 1} \right)}{\Gamma \left( \frac{2 + \frac{2}{\alpha}}{\alpha + 2} \right)} k_B T$$
where \( \xi = k_B T/(a r_0^a) \) and the partition function \( Z \) is given by

\[
Z = 2\pi \int r^2 dr U(r) \exp \left[ \frac{-U(r)}{k_B T} \right] = 2\pi r_0^2 \left[ \frac{1}{2} + \xi^2 \left( \frac{1}{\alpha} + 1 \right) + \frac{1}{2} \xi \left( \frac{1}{\alpha} + 2 \right) \right].
\]

In the limit of a small ring interior \( (r_0 \to 0) \), one finds that

\[
\langle U \rangle_{\text{trap}} = \frac{2k_B T}{\alpha},
\]

which is independent of the overall trap potential height, \( \alpha \).

We next consider the opposite limit of a large ring interior. By large, we mean that the spatial extent in the barrier region due to finite temperature \( T \) is small compared to the interior size \( r_0 \). In other words, the parameter \( \xi = k_B T/(a r_0^a) \ll 1 \). In this limit,

\[
\langle U \rangle_{\text{trap}} = \frac{2k_B T}{\alpha} \left[ \frac{\Gamma (3 + \frac{1}{\alpha})}{2\alpha + 1} + \frac{\Gamma (3 + \frac{2}{\alpha})}{2\alpha + 2} \right] (k_B T)^2.
\]

In the limit of a small ring interior \( (r_0 \to 0) \), one finds that

\[
\langle U^2 \rangle_{\text{trap}} = \frac{2(k_B T)^2(2 + \alpha)}{\alpha},
\]

which is again independent of the overall trap potential height, \( \alpha \). In the opposite limit \( \xi \ll 1 \),

\[
\langle U^2 \rangle_{\text{trap}} = \frac{2(k_B T)^2}{\alpha} \left[ \frac{\Gamma (2 + \frac{1}{\alpha})}{\alpha} \xi + O(\xi^2) \right].
\]

To lowest order, \( \langle U \rangle_{\text{trap}} \propto T^{2+1/\alpha} a^{-1/\alpha} \). In the limit of a steep wall \( (\alpha \to \infty) \), \( \langle U \rangle_{\text{trap}} \) is again independent of the overall trap potential height, \( a \), but now exhibits quadratic temperature dependence.

V. OPTICAL DIPOLE POTENTIAL AND PHOTON SCATTERING IN REPULSIVE OPTICAL TRAPS

A. Analytic Expressions for Heating and Rotational Loss Rates

In this section, we derive analytic expressions for the optical dipole potential, heating rate, and rotational cycling loss rate due to near-resonant rotational levels in the \( B^2\Sigma^+ \) excited state manifold. The trap detunings explored are in the +10-100 GHz range from the transitions to \( B(v = 0, N = 0) \) and \( B(v = 0, N = 2) \), which are the only two \( B^2\Sigma^+ \) rotational manifolds with non-vanishing dipole matrix elements with the \( X^2\Sigma^+ \) ground state manifold. Since we are near-detuned from these lines, we ignore other vibrational levels (\( \sim \) THz away) and electronic levels (\( \sim \) 100 THz away). Our derivations do not take into account hyperfine structure, namely take into account spin-rotational structure, and approximate the spin-rotational splitting to be small compared to the detuning.

Under the rotating-wave approximation (counter-rotating term is negligible since we are near-detuned), the optical dipole potential is given by

\[
U(r) = -\frac{\pi e^2 \Gamma_B f_{00}}{6\omega_X^3 B} \left[ \frac{1}{\omega_{10} - \omega} + \frac{2}{\omega_{12} - \omega} \right] I(r),
\]

where \( I(r) \) is the intensity, \( \omega_{10} \) is the angular frequency of the \( X(v = 0, N = 1) \) \( \rightarrow B(v = 0, N = 0) \) transition, \( \omega_{12} \) is the angular frequency of the \( X(v = 0, N = 1) \) \( \rightarrow B(v = 0, N = 2) \) transition, \( \Gamma_B \) is the excited state decay rate of the \( B \) state, and \( f_{00} = 0.998 \) is the vibrational Franck-Condon factor.

Due to parity and angular momentum selection rules, off-resonant photon scattering can only populate the \( B(v = 0, N = 0) \) and \( B(v = 0, N = 2) \) states. While molecules excited to the \( B(v = 0, N = 0) \) states predomnantly return to the initial \( X(v = 0, N = 1) \) manifold, molecules excited to the \( B(v = 0, N = 2) \) can decay into either \( X(v = 0, N = 1) \) or \( X(v = 0N = 3) \) manifold with significant probability, the latter of which will be observed as loss.

We can thus compute two different photon scattering rates, the rotation-preserving (cycling heating) photon scattering rate and the rotation-changing photon scattering rate. Ignoring the counter-rotating term, we find that the cycling heating rate \( \Gamma_h \) for \( N = 1 \) is

\[
\Gamma_h(r) = \frac{\pi e^2 \omega_X^3 \Gamma_B^2 f_{00}}{3\omega_X^6 B} \left[ \frac{1}{(\omega_{10} - \omega)^2} + \frac{4/5}{(\omega_{12} - \omega)^2} \right] I(r),
\]

and that the rotation-changing scattering rate \( \Gamma_r \) for \( N = 1 \) is

\[
\Gamma_r(r) = \frac{\pi e^2 \omega_X^3}{3\omega_X^6 B} \left( \frac{2/5}{(\omega_{12} - \omega)^2} \right) \Gamma_B^2 f_{00} I(r).
\]
B. Loss Rate versus Trap Detuning

As we reasoned in the main text, rotational loss, rather than heating beyond the barrier height, is the dominant loss mechanism. Since the suppression of photon-scattering in a blue-detuned trap can be understood as molecules spending less time in regions of high trap light intensity, the observed rotational loss should still be proportional to $\Gamma_r$, derived above, albeit with a suppression factor if the peak intensity $I$ is used.

Fig. S7 shows the measured trap loss rates as a function of trap laser detuning $\Delta t$. The photon loss rate is found to decay slower than the expected $1/\Delta t^2$. We believe this is due to spectral imperfections in the trap laser, which can drive two-photon transitions that incoherently transfer molecules from $N = 1$ to $N = 3$. Over a bandwidth of 250 GHz about the carrier, the trap laser is expected to have a decaying broadband pedestal at the $-40$ to $-60$ dB level. As shown in Fig. S7, we can approximately reproduce the observed loss rate dependence by taking into account these incoherent two-photon processes. Note that the theoretical curves in Fig. S7 are only for illustrative purposes, since the two-photon contribution is highly sensitive to the exact shape of the broadband pedestal, which we are unable to measure with the required resolution. In Fig. S7, the laser is assumed to have a flat broadband pedestal.

Note that the two-photon losses should scale as $T^{2+1/\alpha} \approx T^2$, as we derived above. We believe that at the detuning of $\Delta t = 108$ GHz used, single-photon loss dominates over two-photon loss since the measured loss rate does not reveal strong quadratic dependence on $T$.

VI. HEATING TIMESCALE VERSUS TIMESCALE FOR ROTATIONAL LOSS

During laser-cooling, spontaneous emission leads to velocity-space diffusion, which leads to heating. The velocity variance thus evolves as

$$\frac{d \langle v^2 \rangle}{dt} = C\Gamma_h (\Delta v)^2$$

(6)

where $\Delta v = \frac{\hbar k}{m}$ is the recoil velocity due to a resonant photon, and $C$ is a constant of order unity. It follows that the kinetic energy $K$ evolves as

$$\dot{K} = \frac{m d \langle v^2 \rangle}{dt} = C\Gamma_h E_R$$

(7)

where $E_R = \frac{\hbar^2 k^2}{2m}$, $k = 2\pi/\lambda$ with $\lambda = 531$ nm for the $X$-$B$ transition. Hence, we expect significant heating (compared to the initial temperature $T$) to occur over a timescale $\frac{1}{\Gamma_r}k_B T/E_R$. In our system, the recoil temperature is only $E_R/k_B = 0.58 \mu K$ while $T \approx 10 \mu K$, implying that the timescale for significant heating is much longer than $1/\Gamma_r$. Since the rotational loss photon scattering rate and cycling photon scattering rate are comparable ($\Gamma_h \sim \Gamma_r$), we expect rotational loss to become significant much earlier than heating at laser-cooling temperatures.

VII. LASER-COOLING FOR DYNAMICAL TRAP COMPRESSION

A. Bounds on the Required Cooling Rate

To estimate how laser-cooling affects dynamic trap compression, we derive both minimum and maximum bounds on the cooling rate. The problem can be modeled by a particle of mass $m$ subject to a damping acceleration of the form $a_{\text{damp}} = -\beta \ddot{x}$, and a time-dependent force due to a moving optical barrier. The damping coefficient, $\beta$, can be recast as a cooling rate, since velocity damping leads to negative power out of the molecular sample at a rate $-\beta m v_b^2$.

For simplicity, we consider the situation in 1D. For concreteness, suppose the particle is positioned to the right of a barrier that is moving to the right at a speed $v_b$. On the right slope of the barrier, the barrier provides a maximum force $F_{b,\text{max}}$ at its steepest point. Transforming to the frame moving with the barrier, the equation of motion at the point of maximum force reads

$$\ddot{x} = -\beta v_b + a_{b,\text{max}}.$$  

(8)

where $a_{b,\text{max}} = F_{b,\text{max}}/m$. The condition that the particle remains confined to the right, $\dot{x} \geq 0$, sets an upper bound $\beta_{\text{max}}$ for the damping coefficient

$$\beta \leq \beta_{\text{max}} = \frac{a_{b,\text{max}}}{v_b}.$$  

(9)
We can also provide a bound for $\beta$ from below subject to the following conditions. In order to minimize barrier height requirements, we would like enough cooling such that the temperature remains constant throughout the compression. The minimum temperature increase can be found by requiring the phase space density (and hence entropy) of the sample to be constant. This corresponds to adiabatically compressing the sample. In the absence of damping, for an $n$-dimensional isotropic sample of initial radius $r_i$ and temperature $T_i$, the final temperature $T_f$ is given by

$$T_f = T_i \left( \frac{r_i}{r_f} \right)^2. \quad (10)$$

The adiabatic rate of kinetic energy increase $\dot{K}$ is thus

$$\dot{K} = k_B \dot{T} = -2k_B T \frac{\dot{T}}{r}. \quad (11)$$

Assuming the damping is large enough to counteract the adiabatic heating, the gas remains at a fixed temperature, and the maximum rate of internal energy increase is

$$k_B \dot{T}_{\text{max}} = -k_B T i \frac{2v_b}{r_f}. \quad (10)$$

For a 2D gas, we can relate the cooling rate to the damping coefficient via

$$k_b \dot{T} = -\beta m v^2 = 2\beta k_b T, \quad (12)$$

where the last equality follows from the equipartition theorem. Equating the rate of internal energy increase (Eq. 11) and decrease (Eq. 12), we obtain a lower bound for the damping rate $\beta_{\text{min}}$.

$$\beta \geq \beta_{\text{min}} = \frac{v_b}{r_f}. \quad (13)$$

We next estimate these bounds in our system. Using the measured ring profile and the approximate ramp time, we find $\beta_{\text{min}} \approx 100 \text{ s}^{-1}$ and $\beta_{\text{max}} \approx 10^{10} \text{ s}^{-1}$. The typical cooling timescales observed for $\Lambda$-cooling in CaF [10] and YO [11] are on the order of 0.1 ms, giving $\beta \sim 10^4 \text{ s}^{-1}$, comfortably within these bounds. In fact, these cooling rates are high enough such that the compression sequence used in this work could be sped up more than tenfold without significant heating.

### B. Molecular Temperature During Trap Compression

To verify that the cooling rate offered by in-trap $\Lambda$-cooling is sufficient, we measure the temperature of the molecules at various points of the compression sequence. In detail, we first load the molecules into the ring trap from the $\Lambda$-cooled cloud and immediately apply the 21 ms compression ramp is carried out in the presence of $\Lambda$-cooling. The ramp however is truncated at various earlier times $t$. Subsequently, the cooling light is turned off, and the untrapped molecules outside the ring fall away over 20 ms. The temperature of the remaining molecules are then measured via time-of-flight expansion. As shown in Fig. S8, we observe that the temperature remains unchanged at the initial temperature of 10 $\mu$K throughout the ramp. This verifies that indeed $\beta$ is large enough to counteract heating that arises from compression.

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[1] N. R. Hutzler, H.-I. Lu, and J. M. Doyle, Chem. Rev. 112, 4803 (2012).
[2] S. Truppe, M. Hambach, S. M. Skoff, N. E. Bulleid, J. S. Bumby, R. J. Hendricks, E. A. Hinds, B. E. Sauer, and M. R. Tarbutt, Journal of Modern Optics 65, 648 (2018).
[3] S. Truppe, H. J. Williams, N. J. Fitch, M. Hambach, T. E. Wall, E. A. Hinds, B. E. Sauer, and M. R. Tarbutt, New Journal of Physics 19, 022001 (2017).
[4] C. M. Holland, Y. Lu, and L. W. Cheuk, New Journal of Physics 23, 033028 (2021).
[5] M. R. Tarbutt and T. C. Steimle, Phys. Rev. A 92, 053401 (2015).
[6] L. W. Cheuk, L. Anderegg, B. L. Augenbraun, Y. Bao, S. Burchesky, W. Ketterle, and J. M. Doyle, Phys. Rev. Lett. 121, 083201 (2018).
[7] M. Pelegrini, C. S. Vivasquara, O. Roberto-Neto, F. R. Ornellas, and F. B. Machado, Brazilian journal of physics 35, 950 (2005).
[8] T. Wall, J. Kanem, J. Hudson, B. Sauer, D. Cho, M. Boshier, E. Hinds, and M. Tarbutt, Physical Review A 78, 062509 (2008).
[9] N. Friedman, A. Kaplan, and N. Davidson, Advances in Atomic Molecular and Optical Physics 48, 99 (2002).

[10] L. Anderegg, B. L. Augenbraun, Y. Bao, S. Burchesky, L. W. Cheuk, W. Ketterle, and J. M. Doyle, Nature Physics 14, 890 (2018).

[11] S. Ding, Y. Wu, I. A. Finneran, J. J. Burau, and J. Ye, Phys. Rev. X 10, 021049 (2020).