Effects of high pressure on the electrical resistivity and dielectric properties of nanocrystalline SnO$_2$

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The electrical transport and structural properties of tin oxide nanoparticles under compression have been studied by in situ impedance measurements and synchrotron X-ray diffraction (XRD) up to 27.9 GPa. It was found that the conduction of SnO$_2$ can be improved significantly with compression. Abnormal variations in resistivity, relaxation frequency, and relative permittivity were observed at approximately 12.3 and 25.0 GPa, which can be attributed to pressure-induced tetragonal-orthorhombic-cubic structural transitions. The dielectric properties of the SnO$_2$ nanoparticles were found to be a function of pressure, and the dielectric response was dependent on frequency and pressure. The dielectric constant and loss tangent decreased with increasing frequency. Relaxation-type dielectric behaviour dominated at low frequencies. Whereas, modulus spectra indicated that charge carrier short-range motion dominated at high frequencies.

Transparent conductive oxides (TCOs) attract increasing attention in modern optoelectronic devices due to their large optical transparency and high electrical conductivity. SnO$_2$ is one of the widely used TCOs, with a bandgap $E_g$ of ~3.6 eV. It shows high electrical conductivity and optical transparency in the visible region, making it useful in optoelectronic devices such as flat panel displays, organic light emitting diodes, and transparent electrodes for solar cells. The crystal morphology of SnO$_2$ can considerably improve the performance of electronic devices, as exemplified by the SnO$_2$ nanomaterials that show larger electrical and optical variation than those of bulk SnO$_2$.

It is well known that the electrical transport of material plays a central role in the performance of optoelectronic devices. For SnO$_2$, studies of its conduction mechanism have provided possible routes for optimising nano-crystalline SnO$_2$-based devices. Various approaches have been proposed to enhance the electrical conductivity, including changing the grain size and chemical doping. Applying pressure compression has been shown to be one of the effective approaches to tuning the crystalline structure, the electrical structures and the electrical transport properties of materials, which inspired us to further explore the pressurisation of SnO$_2$. A previously reported observation indicated that with application of pressure, SnO$_2$ transforms from rutile (tetragonal structure with $P4_2/mnm$ symmetry) to a CaCl$_2$-type phase (orthorhombic structure with $Pnnm$ symmetry) under hydrostatic pressure or an $\alpha$-PbO$_2$-type phase (orthorhombic structure with $Pbcm$ symmetry) at ~12 GPa under non-hydrostatic pressure conditions. Both $\alpha$-PbO$_2$-type and CaCl$_2$-type phases were found to transform to a modified fluorite-type phase (cubic structure with $Pm-3$ symmetry) at with further compression up to 21 GPa.

How compression tunes the structural properties of SnO$_2$ has been well studied. However, very few works have focused on the effects of pressure on the electrical resistivity of SnO$_2$, which significantly precludes our understanding of the conduction mechanism of nanocrystalline SnO$_2$.

Since SnO$_2$ is a semiconducting dielectric material and widely applied in optoelectronic devices, its resistivity and dielectric properties are two important factors to characterize this material. For example, the resistance and dielectric change will affect the feature and efficiency of device, such as thermal loss, leakage current, refractive index, signal responding speed and so on. SnO$_2$ as a transparent conductive electrode material, the resistivity affects power conversion efficiency (PCE) of devices, while the dielectric affects light transmittance. The optimization of device development based on SnO$_2$ material requires a better understanding of the dielectric properties.

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Herein, we track the evolutions of electrical, structural, and dielectric properties of SnO\textsubscript{2} nanoparticles \textit{in situ} under compression using a combination of AC impedance spectroscopy and X-ray diffraction (XRD) experiments. The electrical and dielectric properties of nanocrystalline SnO\textsubscript{2} under compression have been well discussed.

**Methods**

Our sample is nanocrystalline SnO\textsubscript{2} powder (99.996%) purchased from Alfa Aesar Co. High pressure was obtained by a diamond anvil cell (DAC), with one pair of diamonds with a culet of 300 μm in diameter and a T-301 steel gasket. A 150 μm hole with was drilled in the centre of the indentation area. To insulate the metallic gasket and electrodes, the hole was covered with compressed alumina (Al\textsubscript{2}O\textsubscript{3}) and epoxy powders. Another hole with a diameter of 100 μm was then drilled in the centre of the compressed Al\textsubscript{2}O\textsubscript{3} for use as a sample chamber. Thin-film Mo electrodes were magnetically sputtered onto the diamond anvils, forming a pair of capacitance block-electrodes for electrical transport measurements. More detailed information about the configuration of the parallel plate was reported in previously\textsuperscript{21}. AC impedance spectroscopy measurements were conducted on a Solartron 1260 impedance analyser equipped with a Solartron 1296 dielectric interface with a frequency range from 10\textsuperscript{-1} to 10\textsuperscript{6} Hz. During the measurements, the DAC was shielded with a metal box to avoid any electromagnetic background and pseudo linear responses from the inner structure of the cell.

\textit{In situ} high-pressure XRD experiments were conducted at BL15U1 of the Shanghai Synchrotron Radiation Facility (SSRF) and BL4W2 of the Beijing Synchrotron Radiation Facility (BSRF), using angle-dispersive XRD mode (λ = 0.6199 Å). Argon was used as the pressure transmitting medium. The instrument parameters, including the distance between the sample and detector, were calibrated using a CeO\textsubscript{2} standard material. Ruby chips were loaded into the chamber near the sample to calibrate the pressure.

The first-principles calculations were performed based on the density functional theory and the pseudo potential method on the standard CASTEP program in the Material Studio package. The effects of electron—electron exchange correlation are depicted by CA-PZ functional in Local Density Approximation (LDA). The geometric optimization of the unit cell was conducted with the Broyden—Fletcher—Goldfarb—Shanno (BFGS) minimization algorithm. Integration in the Brillouin zone was performed by use of special k points generated with 7 × 7 × 11, 8 × 8 × 11, and 8 × 8 × 8 mesh parameter grids for the tetragonal, the orthorhombic, and the cubic phase, respectively. A plane-wave cutoff energy of 750 eV was set up for the two phases to guarantee the convergence of the enthalpy calculations.

**Results and Discussion**

**Impedance analysis.** The average grain size of SnO\textsubscript{2} nanoparticles is about 50 nm, and it is homogeneous. The scanning electron microscopy (SEM) pattern is shown in Supplementary Fig. 1. The complex impedance spectra of the SnO\textsubscript{2} nanoparticles at various compression pressures are shown in Fig. 1(a). A single semi-circular response corresponding to grain interiors is observed at every pressure. The components related to the grain boundaries and electrode effects were too weak compared with those of the grain contribution to be distinguished. With application of pressure, the semicircle related to the grain effect collapses considerably but the shape of the arcs remains unchanged.

The representations of the real and imaginary parts of the impedance are given as a function of angular frequency. The purpose is to evaluate the relaxation frequency of the most resistive contribution, which is related to the type and strength of the electrical relaxation in the SnO\textsubscript{2} nanoparticles. The dependences of the experimental values of $Z’$ and $Z''$ on angular frequency $\omega$ at different pressures are shown in Fig. 2(a) and (b), respectively. In the low frequency region, the amplitude of $Z’$ in Fig. 2(a) is typically higher at lower pressures. It then gradually decreases with increasing frequency and pressure, indicating an increase in the AC conductivity of the SnO\textsubscript{2} nanoparticles. In Fig. 2(a), the value of $Z’$ decreases with increasing frequency and attains a constant value at high frequencies at all pressures. Similar behaviour has been reported previously, which suggests a possible release of space charge, and a consequent lowering of the barrier properties in the SnO\textsubscript{2} nanoparticles\textsuperscript{22,23}.

Figure 2(b) shows that $Z''$ initially reaches a maximum value ($Z''_{\text{max}}$) and then decreases with increasing frequency at all measured pressures. The maximum appears when the hopping frequency of localised electrons is approximately equal to the frequency of the applied electric field. The average position of the maximum frequency at all measured pressures is shown in Fig. 1(a). A single semi-circular response corresponding to grain interiors is observed at every pressure. The components related to the grain boundaries and electrode effects were too weak compared with those of the grain contribution to be distinguished. With application of pressure, the semicircle related to the grain effect collapses considerably but the shape of the arcs remains unchanged.

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The AC conductivity $\sigma_{\text{AC}}$ of a material is represented by two parts: $\sigma(\omega) = \sigma’(\omega) + i \sigma”(\omega)$, in which $\sigma’(\omega) = 2\pi\varepsilon_0\sigma_{\text{DC}}\omega$ is the real part, and $\sigma”(\omega) = -2\pi\varepsilon_0\sigma’$ is the imaginary part. The AC conductivity of the SnO\textsubscript{2} nanoparticles as a function of frequency at different pressures is shown in Fig. 3(a). The conductivity pattern can be divided into two parts. At low frequencies, the AC conductivity is weakly frequency dependent at each pressure which corresponds to DC conductivity. At higher frequencies, the AC conductivity shows dispersion that is characteristic of $\omega^\alpha$. The phenomenon of the dispersion of conductivity generally obeys the power law relationship of Jonscher: $\sigma_{\text{AC}} = \sigma_{\text{DC}} + A\omega^\alpha$, where $\sigma_{\text{DC}}$ is the DC conductivity, $A$ is a complex proportionality constant and $\omega$ is the angular frequency. The exponent $S$ is a frequency-dependent parameter of value less than unity, and its dependence on pressure determines the conduction mechanism in the material\textsuperscript{27}. The variation of $S$ with pressure in Fig. 3(b) is limited to 0.6 < $S$ < 1 and $S$ decreases with the increase in pressure, which indicates a hopping conduction mechanism in the SnO\textsubscript{2} nanoparticles\textsuperscript{27–29}. The observed dispersion of conductivity with frequency and pressure is in general agreement with the prediction of the correlated barrier hopping (CBH) model\textsuperscript{27,30}. 

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To quantify the characteristic relaxation frequencies and electrical resistances of the SnO$_2$ nanoparticles, Nyquist plots have been modelled using the Z-view software package. As shown in the insert in Fig. 1(b), an equivalent circuit formed by the parallel combination of the resistance R and constant phase element (CPE) was used for this purpose. Fitting data for the resistance and relaxation frequency as a function of pressure are shown in Fig. 4. With increasing compression pressure, each parameter shows three linear regions with different slopes. The slope changes occur at 13.4 and 25.0 GPa. In fact, most anomalies of the electrical parameters usually coincide with crystal structure transition. To determine the correlation between the electrical transport properties and the structure of SnO$_2$ nanoparticles, we performed high pressure synchrotron XRD experiments.

Figure 5(a) shows the collected XRD data at different pressures. From 2.9 to 12.3 GPa, the XRD pattern of nanocrystalline SnO$_2$ is consistent with a high-crystallinity rutile structure (P4$_2$/mnm). At higher pressures, the (211) diffraction peak begins to split and broaden into the (101) and (200) reflections. This suggests that an orthorhombic phase is formed (i.e., a CaCl$_2$-type structure with space group Pnnm). No discontinuities in the relative volume and cell constant are observed, as shown in Fig. 5(b) and (c). This indicates that the phase transition could be second order. The diffraction pattern at 22.4 GPa shows a weak peak emerging between the strong (110) and (101) peaks of the rutile structure, indicating the onset of a phase transition in the SnO$_2$ nanoparticles. As the pressure increases, the intensities of peaks related to the rutile phase decrease, and the intensities of peaks originating from the new phase increase. The new peaks could be assigned to the high-pressure cubic fluorite (Pa3) phase, because of the typical characteristics of the cubic fluorite phase (Pa3) in the (111) direction. This conclusion is consistent with an earlier report\textsuperscript{[1]}\textsuperscript{[1]}. The changes in the electrical parameters at 13.4 and 25.0 GPa are therefore attributed to the rutile-to-CaCl$_2$ and CaCl$_2$-to-fluorite phase transitions, respectively. The rutile, CaCl$_2$ and fluorite structures are described in Fig. 5(d). Compared with the synchrotron XRD experiment, the transitions pressures shift approximately 1–3 GPa towards higher pressure, which can be attributed to the pressure transmitting medium. To avoid the introduction of additional effects, our electrical experiments did not use the pressure transmitting medium, but we used argon in the high-pressure synchrotron XRD experiment. Neglecting the pressure transmitting medium can give rise to deviatoric stresses at different pressures. The absence of a pressure-transmitting medium in an electrical experiment can cause deviatoric stress.

In general, the compression always causes an energy gap narrow effect and then results the conductivity increase of the compressed sample. For SnO$_2$, the situation is different. We have calculated the band gap of SnO$_2$.
at different phases (as shown in Fig. 6) and the pressure induced band gap broaden has been found at every phase. This result shows the intrinsic band gap change will result the conductivity decrease at every phase. The effect of band gap change on conductivity is negative. However, our experimental result shows that the conductivity of SnO$_2$ increases with pressure increasing.

Figure 2. The real $Z'$ (a) and imaginary $Z''$ (b) components of impedances as a function of the angular frequency, $\omega$, for the SnO$_2$ nanoparticles at different compression pressures.

Figure 3. (a) The AC conductivity $\sigma_{AC}$ versus frequency $f$ for SnO$_2$ nanoparticles at different compression pressures. (b) Variation of exponent $S$ with pressure.
According to the Arrhenius relationship, the relaxation frequency of the grain can be expressed by the following equation:

$$f = f_0 \exp(-H/k_B T)$$  \hspace{1cm} (1)

where $H$ represents the activation energy of the grain, and corresponds to the energy barrier that carriers pass over in the grain interior. $k_B$ is the Boltzmann constant, and $T$ is the temperature. Assuming that $f$ and $H$ are the only functions of pressure, and if $f_0$ remains constant, then:

$$d(\ln f)/dP = -(1/k_B T)(dH/dP)$$  \hspace{1cm} (2)

Linear fitting of the curve of $\ln f$ versus $P$ yields the pressure dependence of the activation energy $dH/dP$, as shown in Table 1. It is seen that the activation energy decreases with increasing pressure in the tetragonal and orthorhombic phases but slightly decreases in the cubic phase. The decrease in activation energy under pressure indicates that pressure plays an important role in decreasing the energy barriers, which consequently enhances the conductivity. The electrical conduction of semiconducting metal oxides such as SnO$_2$ and ZnO strongly depends upon lattice vacancies at oxygen sites$^{6,19}$. The conductivity may also result from the migration of charged particles of SnO$_2$, such as $O^-$, $O^2-$, and $O_2^-$, or the migration of oxygen defects across the grain interior. A pressure increase leads to an energy barrier decrease in the grain of the SnO$_2$ nanoparticles, which results in the resistance decrease shown in Fig. 4(a). Another reason for conductivity growing in SnO$_2$ with pressure increasing is due to the connectivity between neighbor grains in compressed SnO$_2$ nanoparticles is improved.

**Dielectric properties.** With the parallel-plate electrode model, the relative permittivity ($\varepsilon_r$) of the grain as a function of pressure is given by Eq. 3:

$$\varepsilon_r(P) = d/(2\pi Rf_0 S)$$  \hspace{1cm} (3)

where $d$ is the sample thickness, $\varepsilon_0$ is the vacuum permittivity, $S$ is the area of the electrode, and $f$ is the relaxation frequency of the grain. The change in $\varepsilon_r$ with increasing pressure is shown in Fig. 4(c). Two abnormal slope changes occur at 13.4 and 24.2 GPa. The high-pressure XRD experiments indicate that the SnO$_2$ nanoparticles are subjected to tetragonal-to-orthorhombic and orthorhombic-to-cubic phase transitions under high pressure. Therefore, the abnormal slope changes in Fig. 4(c) are attributed to these phase transitions. The relative permittivity is measured at a single relaxation frequency and is a static permittivity. The variation of relative permittivity under compression indicates that the dielectric performance of SnO$_2$ nanoparticles is modulated by pressure. The pressure makes the polarization rate of SnO$_2$ nanoparticles decrease, which is beneficial to its application in the micro-circuit integration.

The complex permittivity is measured in the alternating electric field which known as the dynamic permittivity. The complex dielectric constant ($\varepsilon'$) and dielectric loss ($\varepsilon''$) are determined from the following relationships:

$$\varepsilon' = Z'/[\omega C_0(Z'^2 + Z''^2)]$$  \hspace{1cm} (4)

$$\varepsilon'' = Z''/[\omega C_0(Z'^2 + Z''^2)]$$  \hspace{1cm} (5)
**Figure 5.** (a) XRD patterns of the SnO$_2$ nanoparticles at various compression pressures. (b) The relative volume of the SnO$_2$ nanoparticles as a function of compression pressure. (c) Cell constants of the SnO$_2$ nanoparticles as a function of compression pressure. (d) Crystal structures of the three high-pressure polymorphs of SnO$_2$ nanoparticles.

**Figure 6.** The band structure of (a) the tetragonal phase at 6 GPa and (b) the orthorhombic phase at 16 GPa, (c) the cubic phase at 26 GPa. (d) The pressure dependence of energy bandgap in three phases.
where $C_0$ is the vacuum capacitance of the cell.

Figure 7 shows the frequency dependences of $\varepsilon'$ and $\varepsilon''$ as functions of pressure. As seen, the dielectric constant $\varepsilon'$ of SnO$_2$ nanoparticles increases with pressure in all frequency regions. The dielectric behaviour is strongly related to their conduction mechanism$^{32,33}$. At higher pressure, the charge carrier mobility and the rate of hopping increase, hence, the dielectric polarisation increases, causing an increase in the dielectric constant. With increasing frequency, the charge carrier hopping cannot follow the alternating current which leads to a decrease polarisation. This type of polarization mechanism has been discussed by Aziz et al.$^{34}$.

$\varepsilon''$ is a measure of the dissipated energy in the dielectric material, due to the presence of an applied electric field. The evolution of $\varepsilon''$ as a function of frequency at different pressures is shown in Fig. 7(b). At low frequencies,

| Phase     | Pressure (GPa) | $dH/dP$ (meV/GPa) | Error (%) |
|-----------|----------------|-------------------|-----------|
| tetragonal| 0.8–12.6       | -2.84             | 0.228     |
| orthorhombic| 13.4–24.2   | -8.45             | 0.198     |
| cubic     | 25.0–27.9      | -0.941            | 2.745     |

Table 1. Pressure dependence of activation energy $dH/dP$ within the grain interior.

Figure 7. Dependence of the (a) dielectric constant $\varepsilon'$ and (b) dielectric loss $\varepsilon''$ on frequency $f$, as a function of compression pressure. (c) Variation in the dielectric loss tangent (tan&delta;) of the SnO$_2$ nanoparticles with frequency $f$, for different compression pressures.
ε″ decreases rapidly with increasing frequency and then becomes constant at higher frequencies. The fast decrease in ε″ at lower frequencies is attributed to space charge polarization in the pellet sample. ε″ is almost constant at higher frequencies, because of an inability to follow the applied external electric field. This type of polarization can be explained using the Maxwell-Wagner-Sillars theory of dielectric dispersions. The ε″ peak position shifts towards higher frequency with increasing pressure, showing that the relaxation process increases with the pressure. This could be because, as the pressure increases, the polar charge carriers are freer to orient, allowing them to adjust to the changing electric field.

Additional information that can be deduced from the loss tangent tanδ (tanδ = ε″/ε′), which is proportional to the amount of energy dissipated in a dielectric material. The variation of tanδ with frequency at different pressure is shown in Fig. 7(c). It can be seen that tanδ decreases rapidly at low frequencies, and becomes almost constant at high frequencies. This confirms that the Maxwell-Wagner relationship is responsible for the enhanced dielectric permittivity at low frequency. The decrease in tanδ at low frequencies suggests that the present SnO2 nanoparticles could be used in high frequency devices.

**Electric modulus analysis.** Investigating the form of the complex electric modulus M is another approach to exploring the electrical properties of the SnO2 nanoparticles. This approach can also magnify other effects present in the sample because of different relaxation time constants. The real (M′) and imaginary (M″) parts of the complex electric modulus were obtained from the impedance data in a conventional way according to the following equations:

\[ M' = \varepsilon C_0 Z' \]  
\[ M'' = \varepsilon C_0 Z'' \]  

M′ and M″ for our SnO2 nanoparticles at various compression pressures are shown in Fig. 8(a) and (b), respectively. In Fig. 8(a), M′ tends to zero at low frequencies, suggesting that the interface effect tends to be eliminated in the modulus representation. At high frequencies, M′ displays a maximum value corresponding to M′ max, which can be attributed to the phenomenon of conduction due to the mobility of charge carriers at a small distance. The plots in Fig. 8(b) are characterized by the presence of a relaxation peak. At lower frequencies, charge carriers can move freely over longer distances, up to a certain frequency (peak maximum). A further increase in frequency confines carriers to potential wells. Therefore, the region where the peak occurs indicates the transition from long-range to short-range mobility with increasing frequency.

Figure 8(c) shows the dielectric spectra of the normalized imaginary part of the electric modulus M″/M″ max as a function of the normalized frequency f/f max at different pressure. The data under different pressures overlap...
almost perfectly, except for their high-frequency tails. This indicates that all dynamic processes occurring on different time scales exhibit a distribution of relaxation times that is independent of compression pressure.

The combined plot of $M^*/M^*_{\text{max}}$ and $Z^*$ versus angular frequency can distinguish whether the short- or long-range movement of charge carriers dominates the relaxation process. Figure 8(d) shows plots of $M^*/M^*_{\text{max}}$ and $Z^*$ versus angular frequency, at a compression pressure of 12.6 GPa. The peak maxima of the two curves do not occur at the same frequency. This indicates that the relaxation process is dominated by the short range movement of charge carriers, and thus departs from ideal Debye-type behaviour.

Conclusions

The electric and dielectric properties of SnO$_2$ nanoparticles were investigated as a function of frequency and pressure. The pressure-induced structural phase transitions in the SnO$_2$ nanoparticles correspondingly change their electrical transport and dielectric properties. Complex impedance plots reveal only one semi-circular curve, which is attributed to the grain effect. The AC conductivity and electric modulus studies suggest hopping-type conduction in this system. Frequency-dependent AC conductivity data obey the universal power law at each compression pressure. The dielectric constant and dielectric loss factor decrease with increasing frequency and pressure, which can be interpreted by the Maxwell-Wagner-Sillars model. Furthermore, detailed studies of modulus spectra suggest that the SnO$_2$ nanoparticles exhibit a non-Debye type of relaxation mechanism. These findings hint at the potential of SnO$_2$ nanoparticles in dielectric applications.

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**Author Contributions**
C.G. conceived and designed the research; W.S., T.O., J.W., T.Q., G.Z., and X.Z. performed high-pressure in situ AC impedance measurements; W.S. performed high-pressure X-ray diffraction measurements; Y.H. and Y.M. refined the data; W.S. wrote the paper. All authors reviewed the manuscript.

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