From High-Level Modeling Towards Efficient and Trustworthy Circuits

Abstract. Behavior-Interaction-Priority (BIP) is a layered embedded system design and verification framework that provides separation of functionality, synchronization, and priority concerns to simplify system design and to establish correctness by construction. The framework comes with a runtime engine and a suite of verification tools that uses D-Finder and NuSMV as model checkers. In this paper we provide a method and a supporting tool that takes a BIP system and a set of invariants and computes a reduced sequential circuit with a system-specific scheduler and with a designated output that is true when the invariants hold. Our method uses ABC, a sequential circuit synthesis and verification framework to (1) generate an efficient FPGA implementation of the system, and to (2) verify the system and debug it in case a counterexample was found. Moreover we generate a concurrent C implementation of the circuit that can be directly used as a simulator. We evaluated our method with two large systems and our results outperform those possible with existing techniques.

1 Introduction

In recent years, embedded systems have witnessed a large expansion, especially with the emergence of automotive electronics, mobile and control devices. An embedded system is a composition of heterogeneous intellectual property (IP) components. Figure 1 shows a typical flow of the composition process where the components are specified as imperative programs, finite state machines (FSM), labeled transition systems (LTS), data flow networks, and discrete event based circuits. Computations in embedded systems are subject
to several physical and architectural constraints that render the separation between software and hardware design impractical [23]. The partitioning task, often done manually, decides whether a component is to be implemented as a programmed process or as a realtime logic circuit. A plethora of software, behavioral, and logic compilation and synthesis techniques are used in the process [19].

The Behavior-Interaction-Priority (BIP) framework is a Component-Based System (CBS) design framework that uses a dedicated language and tool-set to support a rigorous and layered design flow for embedded systems. BIP allows to build complex systems by coordinating the behavior of a set of atomic components [5]. BIP makes use of (1) the DFinder [8] compositional and incremental verification tool-set, and (2) the NuSMV [17] model checker, to check the correctness of BIP systems. However, DFinder [7] does not handle data transfer between components, and it does not support checking for invariants other than deadlock freedom. Additionally, for complex systems, NuSMV often suffers from the state space explosion problem [37], and fails to perform its verification tasks.

ABC [13] is a transformation-based verification (TBV) [26] framework that operates on And-Inverter Graphs (AIG); semi-canonical Boolean netlists with memory elements, and iteratively and synergistically employs powerful reduction, abstraction and decision algorithms such as retiming [26], redundancy removal [30,27,11,1], logic rewriting [10], interpolation [29], and localization [39], symbolic model checking, bounded model checking, induction, interpolation, circuit SAT solving, and target enlargement [31,32,24,6,28].

In this paper, we present a method and a supporting tool (BipSV) for embedded system synthesis, runtime verification, and model checking with a cycle based execution model. The method leverages transformation-based synthesis and verification techniques as follows.

1. The method takes a BIP system and a set of invariants and generates an AIG circuit with an output therein that is true iff the system is deadlock free, and satisfies the system invariants. The method passes the generated AIG circuit to ABC for verification. ABC either proves correctness or produces a counter example where the system violates an invariant. This enabled us to find defects and prove systems that were not possible using DFinder and NuSMV.
2. The supporting tool BipSV provides a debugging mechanism where the counter example is mapped back to the original BIP system. The debugging tool is integrated with a wave form visualization tool [15].
3. The method generates an FPGA implementation of the BIP system with a system-specific execution framework. The FPGA implementation is passed to ABC synthesis reduction algorithms which reduce the area and the critical time of the FPGA implementation by removing latches and logic gates. To the best our knowledge, we are the first to synthesize a BIP system directly into an FPGA.
4. The method generates a concurrent C implementation that simulates the BIP system with a system-specific execution framework.

BIP uses a runtime engine to simulate its execution semantic. The main loop of the engine consists of the following steps:

1. Each atomic component sends to the engine its current location.
2. The engine enumerates the list of interactions in the system, selects the enabled ones based on the current location of the atomic components and eliminates the ones with low priority.
3. The engine non-deterministically selects an interaction out of the enabled interactions.
4. Finally, the engine notifies the corresponding components and schedule their transitions for execution.

We differ in that, the system specific scheduler is a bit vector of interactions directly embedded in the implementation. The interaction bit vector evaluates in real-time and directly depends on the locations and
the values of the variables of the input system. The system specific execution framework empirically reduces the space and time requirements for the C simulation and the FPGA execution.

Several frameworks for the design and verification of embedded systems exist. We briefly introduce them here and discuss and compare to them later in Section 7. Metropolis [219] is a design framework that takes a Metropolis Meta Model (MMM) description of an embedded system and generates a SystemC [34] based simulator of the system. It has also a path to SIS [36] which is a synthesis predecessor tool of ABC, and a path to SPIN for model checking [25]. SystemC [34] in turn is a design framework based on C++ that allows system components to communicate through ports, interfaces, and channels. Extensions to SystemC such as ForSyDe [35] restrict the expressiveness to enable formal verification tools to handle the system. In brief, our method supports the synthesis, model checking, and runtime verification concerns of embedded systems using tool independent semantics across the three concerns by embedding the execution model of the embedded system in the generated systems for each concern. This allows for simple debugging and design flow cycle iterations. Furthermore, the use of AIG circuits for synthesis and model checking allows our method to leverage the mature and rich literature of logic synthesis techniques.

The remainder of this paper is organized as follows. In Section 2, we recall the necessary concepts of the BIP framework. Section 3 defines one loop program (OLP). Section 4 formalizes sequential circuit and shows how to translate a sequential circuit into OLP. Section 5 shows how to translate a BIP system into OLP. Section 6 describes BipSV, a full implementation of our framework and some benchmarks. Section 7 discusses related work. Section 8 draws some conclusions and perspectives.

2 BIP - Behavior Interaction Priority

We recall the necessary concepts of the BIP framework [5]. BIP allows to construct systems by superposing three layers of design: Behavior, Interaction, and Priority. The behavior layer consists of a set of atomic components represented by transition systems. The interaction layer provides the collaboration between components. Interactions are described using sets of ports. The priority layer is used to specify scheduling policies applied to the interaction layer, given by a strict partial order on interactions.

2.1 Component-based Construction

BIP offers primitives and constructs for designing and composing complex behaviors from atomic components. Atomic components are Labeled Transition Systems (LTS) extended with C functions and data. Transitions are labeled with sets of communication ports. Composite components are obtained from atomic components by specifying interactions and priorities.

Atomic Components. An atomic component is endowed with a finite set of local variables $X$ taking values in a domain $Data$. Atomic components synchronize and exchange data with each others through ports.

Definition 1 (Port). A port $p[x_p]$, where $x_p \subseteq X$, is defined by a port identifier $p$ and some data variables in a set $x_p$ (referred to as the support set). We denote by $p.X$ the set of variables assigned to the port $p$, that is, $x_p$.

Definition 2 (Atomic component). An atomic component $B$ is defined as a tuple $(P, L, T, X, \{g_T\}_{T \in T}, \{f_T\}_{T \in T})$, where:

- $(P, L, T)$ is an LTS over a set of ports $P$. $L$ is a set of control locations and $T \subseteq L \times P \times L$ is a set of transitions.
The semantics of the atomic component

Definition 3 (Semantics of Atomic Components). The semantics of an atomic component is an LTS over configurations with the port \( p \rightarrow \tau \) for each transition \( \tau \in T \):

- \( g_{\tau} \) is a Boolean condition over \( X \): the guard of \( \tau \),
- \( f_{\tau} = \{(x, f^x(X)) \mid x \in X\} \) where \( (x, f^x(X)) \in f_{\tau} \) expresses the assignment statement \( x := f^x(X) \) updating \( x \) with the value of the expression \( f^x(X) \).

For \( \tau = (l, p, l') \in T \) a transition of the internal LTS, \( l \) (resp. \( l' \)) is referred to as the source (resp. destination) location and \( p \) is a port through which an interaction with another component can take place. Moreover, a transition \( \tau = (l, p, l') \in T \) in the internal LTS involves a transition in the atomic component of the form \( (l, p, g_{\tau}, f_{\tau}, l') \) which can be executed only if the guard \( g_{\tau} \) evaluates to \( \text{true} \), and \( f_{\tau} \) is a computation step: a set of assignments to local variables in \( X \).

In the sequel we use the dot notation. Given a transition \( \tau = (l, p, g_{\tau}, f_{\tau}, l') \), \( \tau.\text{src} \), \( \tau.\text{port} \), \( \tau.\text{guard} \), \( \tau.\text{func} \), and \( \tau.\text{dest} \) denote \( l \), \( p \), \( g_{\tau} \), \( f_{\tau} \), and \( l' \), respectively. Also, the set of variables used in a transition is defined as \( \varphi(f_{\tau}) = \{x \in X \mid x := f^x(X) \in f_{\tau}\} \). Given an atomic component \( B \), \( B.P \) denotes the set of ports of the atomic component \( B \), \( B.L \) denotes its set of locations, etc.

Given a set \( X \) of variables, we denote by \( X \) the set of valuations defined on \( X \). Formally, \( X = \{\sigma : X \rightarrow \text{Data}\} \), where \( \text{Data} \) is the set of all values possibly taken by variables in \( X \).

Semantics of Atomic Components. The semantics of an atomic component is an LTS over configurations and ports, formally defined as follows:

Definition 3 (Semantics of Atomic Components). The semantics of the atomic component \( B = (P, L, T, X, \{g_{\tau}\}_{\tau \in T}, \{f_{\tau}\}_{\tau \in T}) \) is defined as the labeled transition system \( S_B = (Q_B, P_B, T_B) \), where:

- \( Q_B = L \times X \), where \( X \) denotes the set of valuations on \( X \),
- \( P_B = P \times X \) denotes the set of labels, that is, ports augmented with valuations of variables,
- \( T_B \) is the set of transitions defined as follows. \( T_B = \{(l', p', v_p), (l, v) \in Q_B \times P_B \times Q_B \mid \exists \tau = (l', p[l_p], l) \in T : g_{\tau}(v') \land v = f_{\tau}(v'/v_p)\} \), where \( v_p \) is a valuation of the variables of \( p \).

A configuration is a pair \( (l, v) \in Q_B \) where \( l \in L \) is a control location, \( v \in X \) is a valuation of the variables in \( X \). The evolution of configurations \( (l', v') \xrightarrow{p[v_p]} (l, v) \), where \( v_p \) is a valuation of the variables attached to the port \( p \), is possible if there exists a transition \( (l', p[l_x_p], g_{\tau}, f_{\tau}, l) \), such that \( g_{\tau}(v') = \text{true} \). As a result, the valuation \( v' \) of variables is modified to \( v = f_{\tau}(v'/v_p) \).

Creating composite components. Assuming some available atomic components \( B_1, \ldots, B_n \), we show how to connect the components in the set \( \{B_i\}_{i \in I} \) with \( I \subseteq [1, n] \) using an interaction. An interaction \( a \) is used to specify the sets of ports that have to be jointly executed.

Definition 4 (Interaction). An interaction \( a \) is a tuple \( (P_a, G_a, F_a) \), where:

- \( P_a \subseteq \cup_{i=1}^n B_i.P \) is a nonempty set of ports that contains at most one port of every component, that is, \( \forall i : 1 \leq i \leq n : |B_i.P \cap P_a| \leq 1 \). We denote by \( X_a = \cup_{p \in P_a} p.X \) the set of variables available to \( a \),
- \( G_a : X_a \rightarrow \{\text{true}, \text{false}\} \) is a guard,
- \( F_a : X_a \rightarrow X_a \) is an update function.

\( P_a \) is the set of connected ports called the support set of \( a \). For each \( i \in I \), \( x_i \) is a set of variables associated with the port \( p_i \).
**Definition 5 (Composite Component).** A composite component is defined from a set of available atomic components \( \{B_i\}_{i \in I} \) and a set of interactions \( \gamma = \{a_j\}_{j \in J} \). The connection of the components in \( \{B_i\}_{i \in I} \) using the set \( \gamma \) of connectors is denoted by \( \gamma(\{B_i\}_{i \in I}) \).

**Definition 6 (Semantics of Composite Components).** A state \( q \) of a composite component \( \gamma(\{B_1, \ldots, B_n\}) \), where \( \gamma \) connects the \( B_i \)'s for \( i \in [1, n] \), is an \( n \)-tuple \( q = (q_1, \ldots, q_n) \) where \( q_i = (l_i, v_i) \) is a state of \( B_i \). Thus, the semantics of \( \gamma(\{B_1, \ldots, B_n\}) \) is precisely defined as the labeled transition system \( S = (Q, \gamma, \rightarrow) \), where:

- \( Q = B_1 \times \ldots \times B_n, Q \),
- \( \rightarrow \) is the least set of transitions satisfying the following rule:

\[
\forall i \in I : q_i \xrightarrow{p_i(v_i)} q'_i \land v_i = F^i_a(\{v_i\}_{i \in I}) \quad \forall i \notin I : q_i = q'_i
\]

\[
(q_1, \ldots, q_n) \xrightarrow{a} (q'_1, \ldots, q'_n)
\]

where \( v_{p_i} \) denotes the valuation of the variables attached to the port \( p_i \) and \( F^i_a \) is the partial function derived from \( F_a \) restricted to the variables associated with \( p_i \).

The meaning of the above rule is the following: if there exists an interaction \( a \) such that all its ports are enabled in the current state and its guard evaluates to \( true \), then the interaction can be fired. When \( a \) is fired, all involved components evolve according to the interaction and uninvolved components remain in the same state.

Notice that several distinct interactions can be enabled at the same time, thus introducing nondeterminism in the product behavior. One can add priorities to reduce non-determinism. In this case, one of the interactions with the highest priority is chosen non-deterministically.\footnote{The BIP engine implementing this semantics chooses one interaction at random, when faced with several enabled interactions.}

**Definition 7 (Priority).** Let \( S = (Q, \gamma, \rightarrow) \) be the behavior of the composite component \( \gamma(\{B_1, \ldots, B_n\}) \). A priority model \( \pi \) is a strict partial order on the set of interactions \( A \). Given a priority model \( \pi \), we abbreviate \( (a, a') \in \pi \) by \( a \preceq \pi a' \) or \( a \prec \pi a' \) when clear from the context. Adding the priority model \( \pi \) over \( \gamma(\{B_1, \ldots, B_n\}) \) defines a new composite component \( \pi(\gamma(\{B_1, \ldots, B_n\})) \) noted \( \pi(S) \) and whose behavior is defined by \( (Q, \gamma, \rightarrow, \pi) \), where \( \rightarrow, \pi \) is the least set of transitions satisfying the following rule:

\[
q \xrightarrow{a} q' \quad \neg(\exists a' \in A, \exists q'' \in Q : a \prec \pi a' \land q \xrightarrow{a'} q'')
\]

An interaction \( a \) is enabled in \( \pi(S) \) whenever \( a \) is enabled in \( S \) and \( a \) is maximal according to \( \pi \) among the active interactions in \( S \).

Finally, we consider systems defined as a parallel composition of components together with an initial state.

**Definition 8 (System).** A BIP system \( S \) is a tuple \( (B, Init, v) \) where \( B \) is a composite component, \( Init \in B_1 \times \ldots \times B_n, L \) is the initial state of \( B \), and \( v \in X^{Init} \) where \( X^{Init} \subseteq \bigcup_{i=1}^n B_i \times X \).

Given a port \( p \) from the system \( S \), we denote by (1) \( interaction(p) \) to be the set of interactions that are connected to \( p \); (2) \( component(p) \) to be the component to which the port \( p \) belongs; (3) \( transitions(p) \) to be the set of transitions labeled by \( p \).
3 One loop program (OLP)

A one loop program (OLP) ranges over boolean, integer and array variables. A variable can be either a register denoting a memory element or a wire denoting a functional macro. An OLP starts with the variable declarations followed by the wire variable definitions. Then memory variables are initialized simultaneously using the do-together construct. After initialization, an infinite loop keeps updating the value of the memory variables simultaneously. The listings in Figure 2 shows the syntax of an OLP.

The wires are defined in a list of assignment statements wiredef-list. Each wire can be the target of at most one assignment statement. If a wire is not assigned then it is a non-deterministic primary input with a new non-deterministic value at each iteration of the loop.

The list of statements init-list assigns initial values to the register variables. All the assignment statements within init-list execute simultaneously as indicated with the do-together construct.

Similarly, the next-list list of statements updates the values of the register variables.

Each assignment statement has a left hand side target term which is either a variable or an access operator to an array element. The right hand side of an assignment is a combinational expression ranging over the program variables, Boolean and arithmetic operators, and a ternary choice operator. The ternary choice \((a? b : c)\) returns \(b\) if \(a\) is true and \(c\) otherwise.

```plaintext
| decl-list |
|-----------|
| wiredef-list |
| do-together { |
| init-list |
| while (true) { |
| do-together { |
| next-list |
| } |
|
| } |
```

type: bool | int | bool[NUM] | int[NUM];
declaration: wire type id; | type id;
expr: term | uop expr| expr bop expr | expr ? expr : expr;
term: id | id[expr];

decl-list: declaration+
wiredef-list: (term = expr)*
init-list: (term = expr)*
next-list: (term = expr)*

Fig. 2. OLP Syntax

4 Sequential Circuit

The ABC synthesis and model checker reasons about And-Inverted-Graph representation of a sequential circuit.

**Definition 9 (Sequential circuit).** A sequential circuit is a tuple \(((V, E), G, O)\). The pair \((V, E)\) represents a directed graph on vertices \(V\) and edges \(E \subseteq V \times V\) where \(E\) is a totally ordered relation. The function \(G : V \rightarrow \text{types}\) maps vertices to types. There are three disjoint types: primary inputs, bit-registers (which we often simply refer to as registers), and logical gates. Registers have designated initial values, as well as next-state functions. Gates describe logical functions such as the conjunction or disjunction of other vertices. A subset \(O\) of \(V\) is specified as the primary outputs of \(V\). We will denote the set of primary input variables by \(I\), and the set of bit-register variables by \(R\).
Definition 10 (Fanins). We define the direct fanins of a gate $u$ to be $\{v \mid (v, u) \in E\}$ the set of source vertices connected to $u$ in $E$. We call the support of $u \{v \mid (v \in I \lor v \in R) \land (v, u) \in *E\}$ all source vertices in $R$ or $I$ that are connected to $u$ with $*E$, the transitive closure of $E$.

For the sequential circuit to be syntactically well-formed, vertices in $I$ should have no fanins, vertices in $R$ should have 2 fanins (the next-state function and the initial-value function of that register), and every cycle in the sequential circuit should contain at least one vertex from $R$. The initial-value functions of $R$ shall have no registers in their support. All sequential circuits we consider will be well-formed.

The ABC analyzer reasons about And-Inverted-Graph (AIG) sequential circuits which are sequential circuits with only NAND gates restricted to have 2 fanins. Since NAND is functionally complete, this is not a limitation.

4.1 Semantics of sequential circuits

Definition 11 (State). A state is a Boolean valuation to vertices in $R$.

Definition 12 (Trace). A trace is a mapping $t : V \times \mathbb{N} \rightarrow \mathbb{B}$ that assigns a valuation to all vertices in $V$ across time steps denoted as indexes from $\mathbb{N}$. The mapping must be consistent with $E$ and $G$ as follows. Term $u_j$ denotes the source vertex of the $j$-th incoming edge to $v$, implying that $(u_j, v) \in E$. The value of gate $v$ at time $i$ in trace $t$ is denoted by $t(v,i)$.

$$t(v,i) = \begin{cases} s_v^i & : v \in I \text{ with sampled value } s_v^i \\ t(u_1,0) & : v \in R, i = 0, u_1 := \text{ initial-state of } v \\ t(u_2, i - 1) & : v \in R, i > 0, u_2 := \text{ next-state of } v \\ G_v(t(u_1,i),...,t(u_n,i)) & : v \text{ is a combinational gate with function } G_v \end{cases}$$

The semantics of a sequential circuit are defined with respect to semantical traces. Given an input valuation sequence and an initial state, the resulting trace is a sequence of Boolean valuations to all vertices in $V$ which is consistent with the Boolean functions of the gates. We will refer to the transition from one valuation to the next as a step. A node in the circuit is justifiable if there is an input sequence which when applied to an initial state will result in that node taking value true. A node in the circuit is valid if its negation is not justifiable. We will refer to targets and invariants in the circuit; these are simply vertices in the circuit whose justifiability and validity is of interest respectively. A sequential circuit can naturally be associated with a finite state machine (FSM), which is a graph on the states. However, the circuit is very different from its FSM; among other differences, it is exponentially more succinct in almost all cases of interest [14].

4.2 Translation from OLP to AIG circuits

The translation of an OLP into an AIG circuit first constructs registers, wires, and primary input variables for each OLP variable. It then recursively traverses the right hand side of the assignment statements in wiredef-list, init-list, and next-list to build corresponding combinational circuits. It connects the outputs of the combinational circuits built for the init-list and next-list assignment expressions to the initial value and next state value input pins of the corresponding registers, respectively. Finally, it connects the outputs of the combinational circuits built for the wiredef-list to the wires referring to the variables declared as wire variables in decl-list.
Variables. We consider each variable not declared as a wire in `decl-list`. We instantiate a corresponding vector of AIG registers with an adequate bit width. The width of the bit vector can be selected by the user, or can be set to match the default width of the declared type. Typically the default values for the bit width are 32 bits for an integer, one bit for a Boolean, and a finite two dimensional bit vector for an array. In our case, and for OLP programs generated from BIP systems, we will not have arrays of register variables and we will only have fixed size arrays of Boolean wires as discussed in Section . We consider variables declared as wires in `decl-list` and that do not have a corresponding assignment statement in `wiredef-list` as non-deterministic. For each non-deterministic variable we instantiate a corresponding vector of primary inputs with an adequate bit-width. We consider variables declared as wires in `decl-list` with a corresponding assignment statement in `wiredef-list` as functional macros. For each functional macro we instantiate a vector of identity gates (a sequence of two negation gates) where the fanouts correspond to the wire variable and the fanins correspond to the expression defining the wire variable in `wiredef-list`. We denote the gates corresponding to each variable by the function `vargates`.

Assignment statements. We consider each assignment statement in `wiredef-list`, `init-list`, and `next-list` and traverse the right hand side expressions of each assignment with the `traverse` routine. The traversal of an expression runs recursively. If the expression refers to a variable `v` (base case), then the traversal returns `vargates(v)`. If the expression is a logical, conditional, or arithmetic expression, then the `library` routine looks it up in a complete table of circuits with the adequate bit width. For example, if the expression is a ternary conditional statement of the form `b?e1:e2`, then `library` instantiates a multiplexer, connects its two data fanins to the nodes corresponding to `e1` and `e2`, connects its control fanins to the nodes corresponding to `b`, and returns its fanouts.

Connections. Finally, we connect the nodes corresponding to the right hand side expressions of the assignment statements in the `init-list` and `next-list` expressions to the initial value and next value fanins of the corresponding register gates, respectively. We connect the nodes corresponding to the right hand side expressions of the assignment statements in the `wiredef-list` expressions to the fanins of the corresponding wire identity gates.
5 BIP to OLP

Given a BIP system $S = (B, \text{Init}, v)$, BIPSV calls function BIP-to-OLP to translate $S$ into an OLP program with its own customized execution engine. It calls four functions that fill decl-list, wiredef-list, init-list, next-list. All these function use the append call to add code fragments to lists.

\begin{verbatim}
BIP-to-OLP(B, Init, v)
generateDeclarationList()
generateWireDefList()
generateInitList()
generateNextList()
\end{verbatim}

Function generateDeclarationList() fills decl-list as follows. It creates three arrays of wires to denote interaction semantics. Array $ie$ elements denote whether all logical constraints except priority rules are met for a given interaction. Array $ip$ elements denote whether a given interaction is enabled after applying priority rules. Array $is$ elements denote whether an enabled interaction is selected for execution. Currently, one interaction is selected to avoid executing conflicting interactions. Two interactions are conflicting if they involve same components. The $selector$ wire is a non-deterministic primary input that is used to select one of the enabled interactions. The $cycle$ boolean register is used to denote whether the system is executing actions corresponding to either interaction or transition. The function also declares two wires ($B_i.p_j.e$ and $B_i.p_j.s$) for each port $p_j$. Wire $B_i.p_j.e$ denotes whether the port is enabled and wire $B_i.p_j.s$ denotes whether the port is selected by the interaction for execution. Moreover, for each component $B_i$ the function declares a register variable $B_i.\ell$ denoting the current location of $B_i$. Similarly, the function declares a variable register $B_i.x_j$ for each variable $x_j$ in component $B_i$.

\begin{verbatim}
generateDeclarationList()
// interaction enablement wires
append wire bool ie[J] to decl-list
// interaction priority wires
append wire bool ip[J] to decl-list
// interaction selected wires
append wire bool is[J] to decl-list
// non-deterministic priority selector wire
append wire int selector to decl-list
// cycle denotes transition or interaction mode
append bool cycle to decl-list

foreach i ∈ [1..I]
  foreach j ∈ [1..|B_i.P|]
    // port enablement
    append wire bool B_i.p_j.e to decl-list
    // port selected
    append wire bool B_i.p_j.s to decl-list
  endfor

// location registers
append int B_i.\ell to decl-list

foreach j ∈ [1..|B_i.X|]
  // variable registers
  append int B_i.x_j to decl-list
endfor
\end{verbatim}

Function generateWireDefList() fills wiredef-list with functional macro definitions as follows. The enable wire $B_i.p_j.e$ is true when there exists a transition $\tau$ labeled with port $p$, its source ($\tau.src$) is the current location ($B_i.\ell$), and its guard is true.
Array element $ie[j]$ corresponding to interaction $a_j$ is evaluated to true when the guard of $a_j$ is true and all its ports are enabled. Array element $ip[j]$ is evaluated to true when $ie[j]$ is true and $a_j$ has higher priority than other enabled interactions. Array element $is[j]$ is evaluated to true when $ip[j]$ is true either $a_j$ is selected (selector equals to $j$) or the selected interaction is not enabled and $j$ is the first enabled interaction greater with an index greater than $j$. The use of non-deterministic selector is added for fairness. The selected wire $B_i.p_j.s$ is true when there exists a selected interaction $a_k$ (i.e., $is[k]$ is true) involving $B_i.p_j$.

| generateWireDefList() |
|------------------------|
| // iterate over components |
| foreach $i \in [1..I]$ |
| // iterate over component ports |
| foreach $j \in [1..|B_i.P|]$ |
| append $B_i.p_j.e := \bigvee_{\tau \in \text{transitions}(B_i.p_j)} \tau.\text{guard} \land B_i.\ell = \tau.\text{src}$ to wiredef-list |
| endfor |
| endfor |
| // iterate over interactions |
| foreach $j \in [1..|B_i.P|]$ |
| append $ie[j] := a_j.\text{guard} \land \bigwedge_{p \in B_i.P} \text{component}(p).p.e$ to wiredef-list |
| append $ip[j] := ie[j] \land (\forall k \neq j : ie[k] \Rightarrow a_k < a_j)$ to wiredef-list |
| append $is[j] := ip[j] \land (\text{selector} = j \lor (\neg\text{selector} \land \forall k > j : \neg ip[k])$ to wiredef-list |
| endfor |
| // iterate over components |
| foreach $i \in [1..I]$ |
| // iterate over component ports |
| foreach $j \in [1..|B_i.P|]$ |
| append $B_i.p_j.s := \bigvee_{a_k \in \text{interactions}(B_i.p_j)} is[k]$ to wiredef-list |
| endfor |
| endfor |

Function generateInitList() fills init-list with initial value definitions taken from Init for location variables ($B_i.\ell$) and $v$ for component variables ($B_i.x_j$). Register variable cycle is initialized to zero to denote an interaction execution mode.

| generateInitList() |
|-------------------|
| // initialize to interaction mode |
| append cycle := 0 to init-list |
| foreach $i \in [1..I]$ |
| append $B_i.\ell := \text{Init}.B_i$ to init-list |
| foreach $j \in [1..|B_i.X|]$ |
| // $v$ is the initial valuation |
| append $B_i.x_j := v(B_i.x_j)$ to init-list |
| endfor |
| endfor |

Function generateNextList() fills next-list with the next state value definitions of register variables. Each component variable can be modified either in an interaction action or in a transition action. The value of variable cycle makes this distinction.

In the interaction mode (cycle equals to zero), the function considers each assignment statement $\sigma$ from the action of interaction $a_j$. The function appends a conditional clause requiring the $a_k$ to be selected for execution so that the target variable $B_i.x_j$ of $\sigma$ is assigned to the expression of $\sigma.\text{expr}$ ($\sigma.\text{expr}$). The sequence of conditional clauses form a nested ternary conditional expressions where the last expression retains the previous value of the variable.

Similarly, in the transition mode (cycle equals to one), the function considers each assignment statement $\sigma$ from the action of transition $\tau$. The function appends a conditional clause requiring the port of the
transition $\tau$ to be selected for execution and the location of the component to be equal to the source of the transition. The target variable $B_i.x_j$ of $\sigma$ is assigned to the expression of $\sigma(\sigma.expr)$.

In the transition mode, the function considers the current location of each component $B_i.\ell$ and appends a conditional clause requiring the transition source to be equal to the current location and the port of the transition to be selected. The expression corresponding to the conditional clause updates the current location to be the destination of the transition ($\tau.dest$). In the interaction mode, the location retains its value. Finally, the $cycle$ variable is toggled.

```java
generateNextList()
// iterate over components - interaction-mode
for i ∈ [1..|I|]
    // iterate over variables, where $B_i.X = \{x_1, ..., l|B_i.X\}$
    for j ∈ [1..|B_i.X|]
        // interaction mode
        append $B_i.x_j := cycle = 0? to var-st
        // iterate over interaction assignments
        foreach $\sigma \in a_k.action$
            if ($B_i.x_j = $\sigma.term$)
                append is[k]?$\sigma.expr : to var-st
        endfor
    endfor
// iterate over component transitions - transition-mode
append $B_i.\ell := cycle = 0? B_i.\ell : to loc-st$
foreach $\tau \in B_i.T$
    // iterate over transition assignments
    foreach $\sigma \in \tau.action$
        if ($B_i.x_j = $\sigma.term$)
            append ($B_i.port(\tau).s \land \tau.src = B_i.\ell)?$\sigma.expr : to var-st
        endif
    endfor
append ($B_i.port(\tau).s \land \tau.src = B_i.\ell)?$\tau.dest : to loc-st
append $B_i.x_j to var-st$
append var-st to next-list
append $B_i.\ell to loc-st$
append loc-st to next-list
endfor
// switch cycle
append cycle := ¬cycle to next-list
endfor
```

5.1 Illustrative Example

Figure [3] shows a traffic light controller system modeled in BIP. It is composed of two atomic components, timer and light. The timer counts the amount of time for which the light must stay in a specific state (i.e. a specific color of the light). The light component determines the color of the traffic light. Additionally, it informs the timer about the amount of time to spend in each location through a data transfer on the interaction between the two components.
\[
[t \leq n] \quad t := t + 1
\]

\[
[t \geq n] \quad \text{done} \quad t := 0
\]

\[
[\text{true}] \quad \text{done}.n := \text{done}.m
\]

\[
\text{done}
\]

\[
\text{done}
\]

\[
\text{done}
\]

\[
[\text{true}] \quad m := 5
\]

\[
\text{done}
\]

\[
\text{done}
\]

\[
\text{done}
\]

\[
\text{done}
\]

\[
G
\]

\[
R
\]

\[
Y
\]

Fig. 3. Traffic light in BIP

Figure 4 shows OLP code generated that corresponds to the traffic light controller BIP system shown in Figure 3.

5.2 One cycle optimization

Recall that an interaction specifies a strong synchronization among its involved components. Data transfer can take place during such synchronization. The operational semantic of BIP requires to (1) first execute data transfer of the selected interaction and then (2) execute the functions of the corresponding transitions of atomic components. For this, in the above translation, we used \(\text{cycle}\) boolean register to denote whether the system is executing actions corresponding to either interaction or transition. However, in some cases data transfers of all interactions modify some variables that are not assigned in the corresponding transitions of those interactions. This can be detected by doing a static data dependency between interactions and their transitions. This may drastically improve the performance of the system since data transfers as well as functions of transitions may be executed in one cycle. Note that, our implementation supports this optimization.

6 Implementation and Evaluation

6.1 BipSV

\textit{BipSV} is a Java implementation of the translation from BIP to OLP described in Section 5 and, is part of the BIP distribution [38].

\textit{BipSV} takes as input a BIP system and a set of invariants and generates the corresponding OLP program with a system-specific execution framework. The OLP program can be directly compiled for runtime verification (simulation) where primary inputs are set to random values at each iteration. The resulting binary can be concurrent by replacing the \texttt{do-together} construct with the corresponding openmp directives.

For sequential synthesis, we synthesize an AIG circuit that can be used as an FPGA implementation of the system and pass it to ABC. We use ABC synthesis and reduction algorithms to reduce the area and the critical time of the AIG circuit by removing latches and logic gates using techniques such as retiming [26], redundancy removal [30,27,11,1], logic rewriting [10], interpolation [29], and localization [39]. The reduced AIG circuit is equivalent to the original circuit and can be used as a reduced FPGA implementation.

For verification, ABC uses the sequential synthesis techniques above to reduce the AIG circuit and render it amenable for decision algorithms. Then ABC uses decision algorithms such as symbolic model
Fig. 4. Sample of OLP generated code of traffic light system
checking, bounded model checking, induction, interpolation, circuit SAT solving, and target enlargement \([31,32,24,6,28]\) to verify the correctness of the circuit with respect to the BIP system invariants. It either proves correctness or produces a counter example where the system violates the property. *BipSV* provides a debugging mechanism where the counter example is mapped back to the original BIP system. The debugging tool is integrated with waveform visualization tool \([15]\).

*BipSV* is equipped with a command line interface that accepts a set of configuration options. It takes the name of the input BIP file and optional flags.

```
java -jar bip-to-abc.jar [options] input.bip output.abc [property.txt]
```

We evaluated *BipSV* against two industrial benchmarks, an *Automatic Teller Machine* (ATM) \([16]\) and the *Quorum* consensus protocol \([22]\). We report on the size of the generated AIGs before and after reduction, and on the time taken by the ABC solver to reduce and verify the benchmarks. We compare the results for the verification of the ATM benchmark with the NuSMV \([17]\) model checker.

### 6.2 The ATM benchmark

Automatic Teller Machine (ATM) is a computerized system that provides financial services for users in a public space. Figure 5 shows a structured BIP model of an ATM system adapted from the description provided in \([16]\). The system is composed of four atomic components: (1) the User (2) the ATM (3) the Bank Validation and (4) the Bank Transaction. ATM component handles all interactions between the users and the bank. No communication between the users and the bank is allowed.

The ATM starts from an idle location and waits for the user to insert the card and enter the confidential code. The user has 5 time units to enter the code before the counter expires and the card is ejected by the ATM. Once the code is entered, the ATM checks with the bank validation unit for the correctness of the code. If the code is invalid, the card is ejected and no transaction occurs. If the code is valid, the ATM waits for the user to enter the desired amount of money for the transaction. The time-out for entering the amount of money is of 6 time units.

Once the user enters the desired transaction amount, the ATM checks with the bank whether the transaction is allowed or not by communicating with the bank transaction unit. If the transaction is approved, the money is transferred to the user and the card is ejected. If the transaction is rejected, the user is notified and
the card is ejected. In all cases, the ATM goes back to the idle location waiting for any additional users. In our model, we assume the presence of a single bank and multiple ATMs and users.

Table 1 shows the improvement obtained by using *Bip*SV to verify the deadlock freedom of the ATM system, as compared to using the NuSMV model checker [17]. The first column of the table shows the number of clients and ATMs in the system. The table contains the number of latches, AND gates and logic levels in the AIG generated by *Bip*SV before and after applying reduction techniques, respectively. We report on the verification time taken by the ABC solver to check the generated AIG, and the total taken to perform both synthesis (reduction) and verification, in addition to the time taken by NuSMV to perform verification.

With the increase in the number of users and ATMs in the system, *Bip*SV outperforms NuSMV in terms of total verification time, reaching a speedup of 5.6 for 4 users and ATMs. Additionally, *Bip*SV allows developers to make use of several reduction techniques that are able to reach an average of 50% reduction in the size of the AIG. Note that for 2 ATMs and users, NuSMV outperforms *Bip*SV. This is due to the fact that when performing verification, ABC tries multiple verification and reduction algorithms before reaching a conclusive result. However, the advantage that *Bip*SV presents can be clearly seen for larger number of ATMs and users.

| ATMs | latches | AND-gates | levels | latches | AND-gates | levels | BipSV | NuSMV |
|------|---------|-----------|--------|---------|-----------|--------|-------|-------|
| 2    | 78      | 2308      | 125    | 37      | 552       | 25     | 26.1  | 1.4   |
| 3    | 102     | 3689      | 197    | 50      | 804       | 29     | 32.65 | 142.6 |
| 4    | 146     | 5669      | 234    | 63      | 1036      | 29     | 597   | 3361  |

Table 1. ATM results

6.3 The Quorum protocol

The *Quorum* protocol is a consensus protocol proposed in [22] as complementary to the Paxos consensus protocol [21] under perfect channel conditions. *Consensus* allows a set of communicating processes (clients and servers in our case) to agree on a common value. Each of clients proposes a value and receives a common decision value. The authors in [22] propose to use Quorum when no failures occur (perfect channel conditions) and Paxos when less than half of the servers may fail.

The Quorum protocol operates as follows.

1. Upon proposal, a client $c$ broadcasts its proposed value $v$ to all servers. It also saves $v$ in its local memory and starts a local time $t_c$.
2. When a server receives a value $v$ from a client $c$, it performs the following check.
   - If it has not sent any accept messages, it sends an accept message $accept(v)$ to the client $c$.
   - If it has already accepted value $v'$, it sends an accept message $accept(v')$ to the client $c$.
3. If a client $c$ receives two different accept messages, it switches to the backup phase $switch - backup(proposal_c)$.
4. If a client $c$ receives the same accept messages $accept(v)$ from all the servers, it decides on the value $v$.
5. If a client’s timer $t_c$ expires, it waits for at least one accept message $accept(v')$ from a server, or chooses a value $v'$ from an already received $accept(v')$ message, and then switches to the backup phase with the value $v'$.
6. The backup phase is an implementation of the Paxos algorithm. Quorum in this case has decided that the channel is not perfect.
### Table 2. Quorum results

| Design | Original latches | Original AND-gates | Original levels | After reduction latches | After reduction AND-gates | After reduction levels | Time (s) | BipSV | NuSMV |
|--------|------------------|---------------------|-----------------|-------------------------|---------------------------|------------------------|----------|--------|--------|
| 2-2-e  | 264              | 3508                | 101             | 65                      | 923                       | 51                     | 0.78     |        | 526    |
| 2-2-v  | 264              | 3614                | 105             | 66                      | 641                       | 29                     | 240.6    |        | 526    |
| 4-2-e  | 390              | 6305                | 145             | 117                     | 1129                      | 50                     | 0.24     | memory-out |        |
| 4-2-v  | 390              | 6453                | 151             | 117                     | 1170                      | 30                     | 58 hours | memory-out |        |

We implemented the Quorum protocol in BIP, and we used *BipSV* to verify two invariants as defined in [22].

1. **Invariant 1**: If a client $c$ decides on a value $v$, then all clients $c' \neq c$ that have switched, either before or after $c$, switch with the value $v$.
2. **Invariant 2**: If a client $c$ decides on a value $v$, then all clients $c' \neq c$ who decide, do so with the same value $v$.

Table 2 shows the results of using *BipSV* to verify the Quorum protocol for 2 and 4 clients with 2 servers. The designs are indexed as `num_clients-num_servers-status` where `num_clients` is the number of clients, `num_servers` is the number of servers and `status` is either valid (`v`) or erroneous (`e`). A valid design contains no design bugs, while an erroneous design is injected with a bug. We report on the size of the AIG in terms of number of latches, number of AND gates and logic levels before and after applying reduction algorithms.

Using ABC’s synthesis and reduction algorithms, *BipSV* was able to reduce the size of the generated AIGs for all designs by a factor larger than 50%. Furthermore, *BipSV* was able to give conclusive results about all four designs, unlike NuSMV which failed to give any decision about the designs having 4 clients and 2 servers. For example, *BipSV* found a counter example for the erroneous design having 4 clients and 2 servers in 0.24 sec while NuSMV failed to do so. Figure 6 shows a snippet of the generated counter example for the erroneous design, visualized using the Gtkwave [15] waveform viewer. The variables presented in the counterexample are the current control locations and the value of the variables of the different components in the design. Red arrows points to the values that implies a violation of the invariant.

![Fig. 6. Visualization of a counter example using Gtkwave](image_url)

We implemented the Quorum protocol in BIP, and we used *BipSV* to verify two invariants as defined in [22].
7 Related work

The overlap between software and hardware design in embedded systems creates more challenges for verification and code generation.

SystemC [34] is a modeling platform based on C++ that provides design abstractions at the Register Transfer Level (RTL), behavior, and system levels. It aims at providing a common design environment for embedded system design and hardware-software co-design. SystemC designers write their systems in C++ using SystemC class libraries that provide implementations for hardware specific objects such as concurrent modules, synchronization constructs, and clocks. Therefore the input systems can be compiled using standard C++ compilers to generate binaries for simulation. SystemC allows for the communication between different components of a system through the usage of ports, interfaces and channels.

Metropolis [2,19] is an embedded system design platform based on formal modeling and separation of concerns for an effective design process. A Metropolis process is a sequence of events representing functionality, and different processes communicate via ports of interfaces. An interface includes methods that processes can use to communicate. Metropolis uses SIS for synthesis, SystemC and Ptolemy for runtime verification, and SPIN for model checking. While BIP separates behavior from interaction (synchronization and communication) to simplify correctness by construction and compositional verification, Metropolis separates communication from behavior (computation) and leaves synchronization highly coupled within each of them.

The BIP framework differs from SystemC in that it presents a dedicated language and supporting toolset that describes the behavior of individual system components as symbolic LTS. Communication between components in BIP is ensured through ports and interactions. BIP operates at a higher level than SystemC and does not provide support for circuit level constructs.

Verification techniques for SystemC and BIP make use of symbolic model checking tools. NuSMV2 [17] is a symbolic model checker that employs both SAT and BDD based model checking techniques. It processes an input describing the logical system design as a finite state machine, and a set of specifications expressed in LTL, Computational Tree Logic (CTL) and Property Specification Language (PSL). Given a system $S$ and a set of specifications $P$, NuSMV2 first flattens $S$ and $P$ by resolving all module instantiations and creating modules and processes, thus generating one synchronous design. It then performs a Boolean encoding step to eliminate all scalar variables, arithmetic and set operations and thus encode them as Boolean functions.

The work in [33] uses constraint based programming to compute an executable MPI based parallel simulator of an embedded and cyber-physical system written in ForSyDe [35]. ForSyDe is a library of SystemC based parametrized system components with strict constraint specifications and a blocking write FIFO queue modeling a Kan network. The instants of the ForSyDe components are processes that communicate only through signals.

The work in [3] introduces a model checking methodology for LTL specifications of embedded system written in DIVINE [4] over a total store order (TSO) of memory elements. Our method assumes a similarly relaxed memory model since it adopts a cycle based execution model where updated memory values are observable at the next cycle.

In order to avoid the state space explosion problem, NuSMV2 performs a cone of influence reduction [9] step in order to eliminate non-needed parts of the flattened model and specifications. The cone of influence reduction abstraction technique aims at simplifying the model in hand by only referring to variables that are of interest to the verification procedure, i.e. variables that influence the specifications to check [18].

DFinder [8] is an automated verification tool for checking invariants on systems described in the BIP language. Given a BIP system $S$ and an invariant $I$, DFinder operates compositionally and iteratively to compute invariants $X$ of the interactions and the atomic components of $S$. It then uses the Yices Satisfiability
Modulo Theory (SMT) solver [20] to check for the validity of the formula $X \land \neg I = \text{false}$. Additionally, DFinder checks the deadlock freedom of $S$ by building an invariant $I_d$ that represents the states of $S$ in which no interactions are enabled, i.e., a deadlock occurs. It then checks the for the formula $X \land I_d = \text{false}$, i.e., none of the deadlock states are reachable in $S$.

Techniques based on symbolic model checking for the verification of BIP designs suffer from the state space explosion problem, and often fail to scale with the size and the complexity of the systems. On the other hand, DFinder does not handle data transfer between atomic components, thus limiting the range of practical applications on which it can be applied. Our technique handles data transfers and uses the wide range of synthesis and reduction algorithms provided by ABC to effectively reduce the size and the complexity of the verification problem. Most of these algorithms have no counterpart in symbolic model checking.

Unlike all the methods described above, our method leverages the same semantics for FPGA synthesis, model checking, and runtime verification (simulation).

8 Conclusion and Future Work

In this paper we present a method for embedded system synthesis, runtime verification, and model checking with supporting tools for the BIP framework. The method takes a BIP system and generates a concurrent C program with a system specific scheduler embedded therein. The concurrent C program serves as a software runtime verification simulator for the BIP system. The method then take the concurrent C program and generates an AIG circuit which is an FPGA implementation of the BIP system. The method applies synthesis reduction techniques using the ABC framework to simplify and reduce the AIG circuit into a smaller and a less complex circuit that can be readily implemented with an FPGA. The method passes the reduced AIG circuit with a designated output that is $\text{true}$ when the BIP system invariants are $\text{true}$ to ABC proof and model checking algorithms. In case ABC finds a counterexample, the methods maps the values from the counterexample to the original ABC system and provides the user with a debug visualization tool. We successfully used the system to verify and debug medium and large case studies.

Currently, the system specific scheduler makes conservative decisions to avoid interaction conflicts. Two interactions are conflicting if they share a port or they are using conflicting ports of the same component. An important extension is to allow parallel execution of non-conflicting interactions using techniques presented in [12].

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