The bounce of the body in hopping, running and trotting: different machines with the same motor

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The bouncing mechanism of human running is characterized by a shorter duration of the brake after ‘landing’ compared with a longer duration of the push before ‘takeoff’. This landing–takeoff asymmetry has been thought to be a consequence of the force–velocity relation of the muscle, resulting in a greater force exerted during stretching after landing and a lower force developed during shortening before takeoff. However, the asymmetric lever system of the human foot during stance may also be the cause. Here, we measure the landing–takeoff asymmetry in bouncing steps of running, hopping and trotting animals using diverse lever systems. We find that the duration of the push exceeds that of the brake in all the animals, indicating that the different lever systems comply with the basic property of muscle to resist stretching with a force greater than that developed during shortening. In addition, results show both the landing–takeoff asymmetry and the mass-specific vertical stiffness to be greater in small animals than in large animals. We suggest that the landing–takeoff asymmetry is an index of a lack of elasticity, which increases with increasing the role of muscle relative to that of tendon within muscle–tendon units.

Keywords: locomotion; running; hopping; trotting; landing–takeoff asymmetry; muscle force–velocity relation

1. INTRODUCTION

A landing–takeoff asymmetry has been described in the apparently elastic bounce of the body during human running. In each bounce, some of the mechanical energy of the centre of mass of the body is absorbed by muscle–tendon units during the brake and successively restored during the push. In a symmetric elastic system, the duration of the brake equals that of the push. This was found not to be true in human running. The rebound is asymmetric: at low and intermediate running speeds the difference in force may not be the consequence of the

The force–velocity relation of muscle however is not the only candidate to be considered as a cause of the landing–takeoff asymmetry. As Professor McNeill Alexander pointed out in conversation (personal communication, 5 July 2006), the different length of the moment arms between heel and ankle, operating before takeoff (push; Carrier et al. 1994), is shorter than that exerted during the brake, when muscle–tendon units are stretched. In other words, the force performing negative work during the brake of the body after landing is greater than the force performing positive work during the push before takeoff. A force during negative work greater than during positive work is consistent with the force–velocity relation of muscle contractile component (i.e. with the basic property of muscle to resist stretching with a force greater than that developed during shortening). Therefore, the landing–takeoff asymmetry in human running has been considered to be a consequence of the asymmetry of the force–velocity relation of muscle (Cavagna 2006).

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force–velocity relation of muscle, but would be the consequence of the asymmetric lever system, which would then be the initial cause of the landing–takeoff asymmetry. The question therefore arises: what is the cause of the landing–takeoff asymmetry in human running? The motor, the machine or both?

It has been shown that the bouncing mechanism of running initially described for humans (Cavagna et al. 1964) also applies to hopping mammals, running birds and trotting quadrupeds (Cavagna et al. 1977). These animals use a machine (lever system) to promote locomotion which differs from that of humans. In particular, hopping kangaroos and springhares, running birds and trotting quadrupeds land with the digits first, contrary to humans who commonly run with a heel strike. In this study, we re-analyse the bounce of the body in these animals to determine the effect of their different lever systems on the landing–takeoff asymmetry.

We hypothesize that a persistence of the landing–takeoff asymmetry found in humans would indicate that the different machines comply with the basic property of muscle to resist stretching with a force greater than during shortening. In addition we relate the landing–takeoff asymmetry to the mass-specific vertical stiffness measured in animals of different sizes exhibiting different step frequencies and different natural frequencies of their bouncing system.

2. MATERIAL AND METHODS

(a) Subjects and experimental procedure
We re-analysed 136 records, previously obtained by Cavagna et al. (1977), of the vertical and forward velocity changes of the centre of mass of the body during hopping, running and trotting on a force platform sensitive to the vertical and forward component of the force exerted by the feet on its surface. The vertical and forward velocity changes were obtained during the experiments of Cavagna et al. (1977) by analogical integration of the platform signals made simultaneously with the animal run. Data in table 1 derive from measurements made in 31 records of two kangaroos (Macropus rufus, about 20 kg each) and 26 of a springhare (Pedetes cafer, 2.5 kg) during hopping; 12 records of two wild turkeys (Meleagris gallopavo, about 7 kg) and 13 of a rhea (Rhea americana, 22.3 kg) during running; and 28 records of two dogs (Canis familiaris, weighing 5 and 17.6 kg), 14 of a monkey (Macaca speciosa, weighing 3.1 kg) and 12 of two rams (Ovis musimon, weighing approx. 60 and 85 kg) during trotting. The characteristics of the platform and the principle of the method followed to process the platform’s signals are described in detail in previous studies (Cavagna 1975; Cavagna et al. 2008). Analytical procedures used in this study are described briefly below.

(b) From velocity changes to mechanical energy of the centre of mass
The velocity change records were interpolated every 8–9 ms (KALEIDAGRAPH v. 4.03) to reduce a high-frequency noise present in the magnetic substrate we recovered. A compromise was searched between the reduction of the noise and the reduction of the points available for the analysis. The interpolated curve was analysed by means of custom LabView software (National Instruments, Austin, TX, USA, v. 7.1) to measure the instantaneous vertical velocity \( V_{v}(t) \) and forward velocity \( V_{f}(t) \) of the centre of mass, the kinetic energy of vertical motion \( E_{k,v}(t) = 0.5M_{b}V_{f}(t)^{2} \) (where \( M_{b} \) is the mass of the body), the kinetic energy of forward motion \( E_{k,f}(t) = 0.5M_{b}V_{v}(t)^{2} \), the gravitational potential energy \( E_{g}(t) = M_{b}gS_{z}(t) \) (where \( S_{z}(t) \) is the vertical displacement of the centre of mass obtained by integration of the vertical velocity, and \( g \) the acceleration of gravity), and the total mechanical energy \( E_{cm}(t) = E_{k,v}(t) + E_{k,f}(t) + E_{g}(t) \) (figure 1). The work done at each step against gravity, \( W_{g} \), to sustain the forward velocity changes, \( W_{DF} \), and the total mechanical energy changes of the centre of mass, \( W_{cm} \), were measured from the \( E_{g}(t) \), \( E_{k,v}(t) \) and \( E_{cm}(t) \) records, respectively. Positive values of the energy changes gave positive work, negative values gave negative work. In a perfect steady run on the level, the ratio between the absolute values of positive and negative work done in an integer number of steps should be equal to one. The regularity of the selected steps was therefore assessed from the ratio between positive and negative work. Initially, steps where \( 0.5 < W_{DF}/W_{cm} < 1.5 \) were used for analysis. Experimental values were as follows \( (n = 167) \): \( W_{DF}/W_{cm} = 1.021 \pm 0.116 \) and \( W_{DF}/W_{cm} = 1.019 \pm 0.166 \) and \( W_{DF}/W_{cm} = 1.017 \pm 0.113 \). Subsequently, steps where \( 0.75 < W_{DF}/W_{cm} < 1.25 \) were used for analysis. Experimental values were as follows \( (n = 136) \): \( W_{DF}/W_{cm} = 1.015 \pm 0.095 \), \( W_{DF}/W_{cm} = 1.010 \pm 0.120 \), \( W_{DF}/W_{cm} = 1.014 \pm 0.084 \). Data in figure 2 and table 1, obtained from measurements made on the 136-record sample, do not differ appreciably from those made on the 167-record sample.

(c) Measurement of the landing–takeoff asymmetry
As described in §1, the landing–takeoff asymmetry is revealed by the duration of the push, \( t_{push} \), being greater than that of the brake, \( t_{brake} \). The ratio \( t_{push}/t_{brake} \) was therefore taken as a measure of the landing–takeoff asymmetry (figure 2; table 1). Push and brake durations were measured from the increment and the decrement, respectively, of the total mechanical energy of the centre of mass, \( E_{cm} \) (black curve in figure 1).

The difficulty in measuring the increment \( (t_{push}) \) and the decrement \( (t_{brake}) \) of \( E_{cm} \) is mainly due to the blunt attainment of the \( E_{cm} \) plateau. In order to make this transition more sharp, the derivative \( dE_{cm}/dt \) was made. This procedure did succeed in making the transition to the \( E_{cm} \) plateau more clear, but resulted in a noise of the \( dE_{cm}/dt \) below the ideal line, where \( dE_{cm}/dt \) was below the upper line, without crossing the noise, was automatically taken by the program as \( t_{push} \), whereas the time interval during which \( dE_{cm}/dt \) was below the horizontal line, without crossing the noise, was taken as \( t_{brake} \) (Cavagna 2006). However, as pointed out by Cavagna (2006), this procedure is inconvenient in underestimating both \( t_{push} \) and \( t_{brake} \). In fact a fraction of the time interval during which \( dE_{cm}/dt \) was indeed above and below the ideal line, where \( dE_{cm}/dt \approx 0 \), was missed to avoid crossing the noise of the \( dE_{cm}/dt \) record during the \( E_{cm} \) plateau. The error is obviously larger the greater the noise, and the noise is larger the smaller the animal. An improvement of the method previously used was therefore applied in this study, by measuring push and brake durations as the time intervals during which \( dE_{cm}/dt \) was respectively above and below the mean of the data points comprised between the two reference levels (not above and below
Figure 1. Mechanical energy of the centre of mass of the body during steps of hopping, running and trotting animals at the indicated speeds. Left column, larger animals; right column, smaller animals. In each panel the curves show the gravitational potential energy ($E_p$, blue), the kinetic energy of vertical motion ($E_{kv}$, red), the kinetic energy of forward motion ($E_{kf}$, brown), the kinetic energy of motion in the sagittal plane ($E_k = E_{kv} + E_{kf}$, green) and the total translational energy of the centre of mass of the body in the sagittal plane ($E_{cm} = E_p + E_k$, black). The interrupted vertical lines through the peaks of $E_{kv}$ indicate the instants of static equilibrium position when the bouncing system is loaded with a vertical force equal to body weight. The red horizontal bars indicate the time during which positive external work is done, $t_{push}$ (increment of $E_{cm}$), whereas the blue horizontal bars indicate the time during which negative external work is done, $t_{brake}$ (decrement of $E_{cm}$). The gap between red and blue bars indicates the duration of the aerial time (when present). The landing–takeoff asymmetry, indicated by $t_{push} > t_{brake}$, measures the discrepancy from an elastic rebound where $t_{push} = t_{brake}$.
the two reference levels as previously made). This procedure requested manual instead of automatic measure of $t_{\text{push}}$ and $t_{\text{brake}}$ in 11 of the 136 records analysed. In most trotting steps it was not possible to detect a fraction of the step, where \( \frac{dE_{\text{cm}}}{dt} = 0 \) and the two reference levels were superposed. In this case, both $t_{\text{push}}$ and $t_{\text{brake}}$ were automatically measured by the software as the number of data points respectively above and below the superposed reference levels.

(d) Vertical stiffness
The mass-specific vertical stiffness, $k/M_b$, is given by the slope of the relationship between vertical acceleration and vertical displacement of the centre of mass in the range corresponding to the amplitude of the oscillation of the spring–mass system, i.e. from its equilibrium position (vertical acceleration $= 1g$) to its maximal deformation (Cavagna et al. 1988). In this study we measured the maximal upward acceleration $A_{\text{v,\,max,\,up}}$ of the centre of mass of the body, attained at the lowest point of its trajectory, and the vertical displacement of the centre of mass $S_{\text{ce}}$ from the lowest point to the equilibrium position. The vertical acceleration was deduced from the time derivative of the vertical velocity, whereas the vertical displacement was obtained by integration of the vertical velocity. The mass-specific vertical stiffness is given by:

$$k = \frac{\Delta A_v}{\Delta S_{\text{ce}}},$$

where $\Delta A_v$ is the change in vertical acceleration and $\Delta S_{\text{ce}}$ is the change in vertical displacement from the equilibrium position to the lowest point of the trajectory.
### Table 1

| Animal | Mass (kg) | $t_{\text{push}}$ (s) | $t_{\text{brake}}$ (s) | $L_0$ (Hz) | $f_{\text{spring}}$ (Hz) | $v_{\text{max}, \text{up}}$ (m/s) | $W_{\text{eff}}$ | \(k/M\) | \(f_p\) | \(\text{step}\) |
|--------|----------|---------------------|---------------------|----------|---------------------|---------------------|--------|--------|--------|--------|
| kangaroo | 20.4 ± 0.05 | 0.095 ± 0.017 | 0.088 ± 0.013 | 4.01 ± 0.52 | 2.17 ± 0.14 | 0.017 ± 0.019 | 0.118 ± 0.012 | 0.099 ± 0.011 | 1.091 | 2.19 |
| springhare | 22.4 ± 0.3 | 0.094 ± 0.014 | 1.292 ± 0.19 | 2.64 ± 0.05 | 4.30 ± 0.05 | 0.017 ± 0.019 | 0.120 ± 0.012 | 0.099 ± 0.011 | 1.091 | 2.19 |
| turkey | 7.2 ± 0.2 | 0.094 ± 0.014 | 1.292 ± 0.19 | 2.64 ± 0.05 | 4.30 ± 0.05 | 0.017 ± 0.019 | 0.120 ± 0.012 | 0.099 ± 0.011 | 1.091 | 2.19 |
| monkey | 17.6 ± 0.2 | 0.094 ± 0.014 | 1.292 ± 0.19 | 2.64 ± 0.05 | 4.30 ± 0.05 | 0.017 ± 0.019 | 0.120 ± 0.012 | 0.099 ± 0.011 | 1.091 | 2.19 |
| rams | 76.2 ± 11.4 | 0.094 ± 0.014 | 1.292 ± 0.19 | 2.64 ± 0.05 | 4.30 ± 0.05 | 0.017 ± 0.019 | 0.120 ± 0.012 | 0.099 ± 0.011 | 1.091 | 2.19 |
| dogs | 18.0 ± 0.2 | 0.094 ± 0.014 | 1.292 ± 0.19 | 2.64 ± 0.05 | 4.30 ± 0.05 | 0.017 ± 0.019 | 0.120 ± 0.012 | 0.099 ± 0.011 | 1.091 | 2.19 |

The physiological meaning of the landing–takeoff asymmetry in the animal bounce is evidenced, as described below, by a comparison with a purely elastic rebound of the mechanical energy attained by the centre of mass. The landing–takeoff asymmetry of the bounce increases with increasing ratio \(\frac{t_{\text{push}}}{t_{\text{brake}}}\) which is given in table 1 together with the mass-specific vertical stiffness of the bouncing system \(k/M_0\). Both \(t_{\text{push}}/t_{\text{brake}}\) and \(k/M_0\) are greater in the animals of smaller size and body weight, suggesting that the landing–takeoff asymmetry of the bounce increases with the stiffness of the bouncing system.

The mechanical energy of the centre of mass at the equilibrium position during the descent equals the mechanical energy of the spring–mass system loaded with a vertical force equal to body weight (Blickhan 1989) and can be conveniently used as reference points for a comparison with an elastic system.
the lift. This is because the kinetic and gravitational potential energy of the centre of mass is stored during the descent as elastic potential energy and converted without loss back into kinetic and gravitational potential energy attaining the same value during the lift. Figure 1 shows that this condition is approached in the bounce of a kangaroo.

The rebound of the body in the animals showing a large landing–takeoff asymmetry, i.e. a large ratio $t_{\text{push}}/t_{\text{brake}}$ differs drastically from an elastic rebound. Consider, for example, the running turkey in figure 1, which shows the greatest landing–takeoff asymmetry. The intersection of the interrupted lines with the $E_{cm}$ curve in figure 1 shows that the mechanical energy during the lift is less than the mechanical energy during the fall, indicating that some losses occur in the stretch–shorten cycle of muscle–tendon units. During the stretch, these losses are expected to occur due to cross-bridge detachment if muscle, instead of tendon, is forcibly lengthened (i.e. if tendons are stiffer than muscle). Due to these losses, some energy must be added to complete the lift of the centre of mass and to accelerate it forwards to the velocity attained before the brake. This additional energy must derive from the active muscular contraction, which, according to the force–velocity relation of the contractile component, is characterized by a lower force developed during shortening. This lower force necessarily requires more time to restore the momentum lost during stretching when the force is higher, thus explaining why $t_{\text{push}} > t_{\text{brake}}$. According to this analysis, therefore, the landing–takeoff asymmetry is a measure of the lack of elasticity in the rebound of the body and is expected to increase with increasing contribution of muscle relative to tendon in the stretch–shorten cycle of muscle–tendon units. In fact contracting muscle exhibits a large hysteresis in its stretch–shorten cycle, whereas a very low hysteresis is found in the stretch–shorten cycle of tendons (Alexander 2002).

The ‘elastic’ mechanism suggested above may not be the only cause of the landing–takeoff asymmetry in the animal bounce. Given the large number of limb and trunk muscles that produce, absorb and re-distribute energy within the limbs and body during the bounce, it is possible that antagonistic work done by muscles against others may contribute to the observed landing–takeoff asymmetry.

4. DISCUSSION
(a) Different machines with the same motor
Locomotion is carried on in the animals of this study and in humans with a large diversity in the anatomy and geometry of their machines (i.e. of the lever systems, which promote forward movement of the body). The different machines serve different tasks and are used differently during the step. For example, whereas in human running landing takes place on the heel and takeoff from the front of the foot, in running in birds landing takes place on the front of the foot far from the ankle, which is shifted upwards relative to the ground. Thanks to this geometry the digits of birds, instead of the knee, occupy a front position when the legs are flexed against the body during the flight and are ready to grasp support at landing. In hopping and trotting also, contact with the ground takes place with the front of the foot. In hopping, a long duration of the aerial phase is required to allow repositioning of the same two feet over which each bounce takes place, whereas in trotting a minimal, often absent, aerial phase is inserted between bounces on two (front–back) feet of opposite sides of the body. The characteristics of the environment may also modify the anatomy of the locomotor’s machine. Differences in hind limb anatomy and in hopping mechanics have been found in two species of wallabies inhabiting different environments (McGowan et al. 2008). Other examples could be given showing how different machines evolved differently in order to fulfil different requirements in different surroundings and are used differently during locomotion because of their different geometries and structure.

In contrast with the large diversities mentioned above, the motor operating the different machines remained largely the same throughout evolution, maintaining, from frog to humans, its basic property to resist stretching with a force greater than that developed during shortening, as described by the force–velocity relation of muscle contractile component.

The finding that the landing–takeoff asymmetry of the animals of this study takes place always in one direction (i.e. with $t_{\text{push}} > t_{\text{brake}}$), never the reverse, in spite of the diverse geometries of the lever systems involved, body mass and step frequencies, strongly suggests that the different machines are used to comply with the asymmetric response of their motor during negative and positive work performance. This requirement results in a trend of the $E_{cm}$ curve (rounded attainment of plateau and sharp departure from plateau) that is very similar in the 7 kg turkey of figure 1 running at 12 km h$^{-1}$, a 73 kg human running at 13.5 km h$^{-1}$ (see fig. 1 of Cavagna 2006), in spite of more than a tenfold difference attained by $E_{cm}$ during the step (approx. 40 J in the turkey and 600 J in the human) and of the striking difference of the two locomotors’ machines.

(b) Factors affecting the elastic storage mechanism
In human running the landing–takeoff asymmetry (i.e. the ratio $t_{\text{push}}/t_{\text{brake}}$) decreases with speed: above 14 km h$^{-1}$ $t_{\text{push}}/t_{\text{brake}}$ as expected in an elastic rebound (Cavagna 2006). This finding has been explained as an increase of muscle activation with speed privileging the role of tendons relative to muscle within muscle–tendon units. If muscle activation is so high that muscle does not yield during stretching and is held isometric, as some studies suggest (Roberts et al. 1997; Biewener et al. 1998), the whole of the length change will be taken up by the tendon, the response of the muscle–tendon unit will approach that of an elastic structure and the landing–takeoff asymmetry would disappear. This mechanism may conveniently apply to kangaroo hopping, which approaches an elastic rebound (i.e. $t_{\text{push}} > t_{\text{brake}}$), with most of the length change taken up by tendons (Biewener et al. 1998). This is consistent with the high force that must be developed by the muscle to attain the high upward acceleration we measured in these animals (table 1). Furthermore, the efficiency of external work production in kangaroos (Cavagna et al. 1977) increases with speed, suggesting an improved elastic storage and recovery as the force exerted on the ground increases.

It has been shown that force enhancement following muscle stretch has a transient character—that is, it disappears rapidly at the end of stretching and, with it, the
elastic energy stored within tendons and other undamped elastic elements (Cavagna et al. 1986). This transient character of elastic storage and recovery may contribute to the observed decrease of the landing–takeoff asymmetry with running speed in humans.

However, important exceptions indicate that other factors must be taken into account when comparing different groups of subjects. For example, the landing–takeoff asymmetry is greater in the springhare than in the kangaroo in spite of a similarly high upward acceleration (table 1). On the other hand, the landing–takeoff asymmetry is almost nil in the rams, which show the lowest upward acceleration (table 1).

One factor, found in humans, is age: during running the landing–takeoff asymmetry is greater in old subjects than in young subjects, suggesting a less elastic rebound in the elderly (Cavagna et al. 2008).

Another factor is size. Data in table 1 suggest that the landing–takeoff asymmetry is greater in small than in large animals. The hypothesis that small animals are unable to use an elastic storage mechanism during the bouncing step as efficiently as large animals do was put forward on the basis that the efficiency of the transformation of metabolic energy into mechanical work is less in small than in large animals (Heglund et al. 1982).

The efficiency of the transformation of metabolic energy into external work is given in table 1 for some of the animals (mean of the lowest and highest values of the curves in fig. 10 of Cavagna et al. 1977). It can be seen that a larger landing–takeoff asymmetry in the smaller animals (i.e. a greater ratio $\tau_{\text{land}}/\tau_{\text{take}}$), is associated with a lower metabolic efficiency, supporting the hypothesis that the landing–takeoff asymmetry is a measure of a lack of elasticity in the bouncing step. Both metabolic inefficiency and landing–takeoff asymmetry independently show that elastic energy storage is less efficient in small animals.

It has been suggested that the elastic storage mechanism is lower in small animals because their tendons are relatively thicker than those of large animals. This was measured by comparing small kangaroo rats with large kangaroos (Biewener et al. 1981) and calculated from measurements of muscle and tendon dimensions in kangaroos (Bennett & Taylor 1995) and quadrupedal mammals (Alexander et al. 1981; Pollock & Shadwick 1994). This hypothesis is consistent with the present findings, showing that the landing–takeoff asymmetry (i.e. the deviation from an elastic bounce) is associated in the smaller animals with a greater stiffness of the system (table 1). The greater mass-specific vertical stiffness in small animals implies a greater natural frequency of the bouncing system $f_0 = (1/2\pi)\left(\sqrt{l/M_{\text{eff}}}/h\right)$, which in turn is bound to a greater step frequency (table 1). More steps (i.e. a greater step frequency) are required to cover a given distance in the animals of smaller dimensions. This requires a greater frequency of the bouncing system (i.e. a greater mass-specific vertical stiffness), with the drawback of a less efficient elastic rebound, resulting in a greater landing–takeoff asymmetry.

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