Application of the monte-carlo method for solving problem of acoustic radiation propagation along vertical paths in the atmosphere

Abstract

Difficulties of the analytical approach to a solution of the problem of acoustic radiation transfer through the outdoor atmosphere call for the application of numerical methods, from which the most promising, in our opinion, is the method of statistical simulation (Monte Carlo). This method allows sound scattering on refractive index fluctuations caused by wind and temperature in homogeneities to be correctly taken into account for the most realistic models of the propagation medium and geometrical parameters of the problem to be solved. A review of authors’ works devoted to the application of the Monte Carlo method to a solution of the problem of acoustic radiation transfer through the lower 500-meter layer of the plain-stratified turbulent atmosphere is presented in the report. The acoustic model of the atmosphere is considered, and the structure and special features of the computational algorithm of the Monte Carlo method are discussed. The influence of the outer scale of atmospheric turbulence on the distribution of the transmitted acoustic radiation intensity is investigated for sound frequencies in the range 1–4 kHz. Regional and seasonal variations of the contribution of multiple scattering to the transmitted radiation intensity as well as the effect of cloudiness and source altitude are investigated. The calculated dependences of the transmitted acoustic radiation intensity and of the multiple scattering contributions on the angle of source divergence and source altitude above the Earth’s surface are discussed. Calculations were performed for a point sound source and a source with a circular aperture and uniform and Gaussian radiation distributions. Good agreement of calculated values of the total sound attenuation with the available experimental data confirms the reliability of the results of statistical simulation. PACS: 43.28.-g; 43.28.+h

Keywords: atmospheric acoustics, monte-carlo method, statistical simulation, acoustic radiation transfer

Introduction

Investigations of sound propagation in the atmosphere are necessary for its prediction, finding direction to a sound source, and quantitative interpretation of results of acoustic sounding.¹ In the outdoor atmosphere, the sound propagation is influenced by a great number of factors, the main of which are the vertical atmospheric stratification, viscosity, turbulence, and angular beam divergence. Difficulties of analytical approach call for the application of numerical methods from which,³⁴ by our opinion, the Monte Carlo method first used in⁵ for statistical estimation of the multiple scattering contribution to the distribution of the transmitted acoustic radiation intensity over detector zones depending on the sound frequency and outer scale of atmospheric turbulence is most promising. This method allows sound scattering on the acoustic refractive index fluctuations caused by wind velocity and temperature in homogeneities to be taken into account for the most realistic models of the atmosphere and concrete geometry of numerical experiment.

Models of the atmosphere and calculations

The main results obtained by the authors can be found in⁶–¹² Calculations by the Monte Carlo method were performed for the acoustic model of the atmosphere based on the theoretical estimates of sound scattering by the atmospheric turbulence presented in¹² for the von Karman model of the spectra of atmospheric temperature and wind velocity fluctuations. In calculations of the vertical profiles of the acoustic absorption and scattering coefficients, the vertical profiles of the atmospheric temperature, pressure, and sound velocity were taken from the standard model of the mid-latitude summer atmosphere. Both conventional computational procedures¹³ and procedures developed in¹⁴–¹⁵ with allowance for the specifics of the interaction of sound with the atmosphere were used. The flow chart of the computational algorithm was presented in.¹⁶ Calculations were performed for a point source with coordinates $x = 0, y = 0, z = H_s$, where $0 \leq H_s \leq 35 m$, and a source with circular aperture 1 m in diameter and power of 1 W, sound frequencies $1000 Hz \leq F \leq 4000 Hz$, and the outer scale of atmospheric turbulence $L = 10–100 m$. The angle of source divergence was $\phi = 2.5^\circ – 25^\circ$. The receiver was placed at an altitude of 500 m. The radiation distribution over the horizontal plane of the detector depending on the distance $H$ from the vertical axis passing through the source (over the detector zones with $H = 10–100 m$ with a step of 10 m and then with a step of 50 m to $H = 500 m$) was estimated with allowance for the contribution of multiply scattered radiation. The acoustic radiation of the source propagated through the plane-parallel atmospheric layers with constant within these layers coefficients of classical, $\sigma_{cl}(j)$ and molecular absorption, $\sigma_{mol}(j)$ and scattering
on turbulent fluctuations of the temperature, $\sigma_T(j)$ and wind velocity, $\sigma_V(j)$ where $j = 1, \ldots, 25$. The 500-meter plain-stratified turbulent atmosphere was subdivided into 25 layers 20 m each. Calculations were performed on a personal computer for $10^5$–$10^7$ phonon histories that provided error in the range 3–10\%. Time of calculating the individual realization did not exceed 15 min.

**Results of numerical experiments**

As an example, Figure 1 shows the altitude dependence of the total attenuation coefficient $\sigma_{\text{tot}}(j) = \sigma_T(j) + \sigma_{\text{mol}}(j) + \sigma_P(j)$ and phonon survival probability $P_{\text{sc}}(j) = \sigma_T(j) / \sigma_{\text{tot}}(j)$ for frequencies in the range 1000-4000 Hz and outer scale of turbulence $L_0 = 80$ m (a) and the phonon scattering probability $P_{\text{sc}}(j) = \sigma_T(j) / \sigma_{\text{tot}}(j)$ (b). Results of calculations demonstrated that for a frequency of 2 kHz, most often used in sodars, the turbulent attenuation becomes comparable with the molecular absorption in the surface layer of the atmosphere already for $L_0 = 15$ m ($P_{\text{sc}} \geq 0.5$). For $L_0 = 80$ m, $P_{\text{sc}} > 0.56$ in the examined frequency range (Figure 1). In the surface layer, the total attenuation coefficient increases approximately by an order of magnitude when $L_0$ increases from 10 to 80 m.

**Figure 1** Altitude dependence of the total sound attenuation coefficient (a) and phonon survival probability (b) for frequencies $F=1000$–$4000$ Hz and outer scale of turbulence $L_0=80$ m.

**Figure 2** Normalized phase functions of sound scattering on temperature (a) and wind velocity fluctuations (b) for frequencies $F=1000$–$4000$ Hz and outer scale of turbulence $L_0 = 80$ m.

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of calculations demonstrated that their elongation in the forward direction increases with the outer scale of turbulence. Thus, the portion of radiation scattered in the forward direction increases by a factor of 15 when $L_0$ increases from 10 to 40 m; it increases by a factor of 63 for $L_0=80$ m. It should also be noted that good agreement of the calculated coefficients and scattering phase functions with the available experimental data was demonstrated.\textsuperscript{12}

Results of calculations by the Monte Carlo method of the total attenuation of acoustic radiation, in dB, for vertical sound propagation at frequencies of 2800 Hz (the dashed curve) and 4000 Hz (the solid curve) are shown in Figure 3. Symbols here show the results of measurements\textsuperscript{16} with a tethered balloon. Good agreement of the results of our calculations by the Monte Carlo method with the experimental data can be seen, which confirms the efficiency of the suggested computational algorithm.

The influence of the source aperture and the form of radiation distribution is illustrated by Figure 4 which shows the distributions of the transmitted ($I_{tr}$) and multiply scattered ($I_{msc}$) radiation intensities, in W/m$^2$, over the detector zones for the point sound source and the source with the circular aperture 1 m in diameter and uniform and Gaussian radiation distributions over the source aperture for $F=3000$ Hz, $\phi=2.5^\circ$, and $L_0=10$ m. From the figure it can be seen that the intensity of transmitted radiation in the first detector zone $I_{tr}(0^\circ,2.5^\circ)$ increases by 66–68% for the source with the circular aperture and Gaussian radiation distribution in comparison with the point source. For the source with the circular aperture and uniform radiation distribution, it remains almost unchanged.

Figure 5 from\textsuperscript{10} shows the dependence of the distribution of transmitted and multiply scattered radiation over the detector zones for frequencies of 1.7 and 4 kHz and angles of source divergence $\phi=5$ and $15^\circ$. Results of calculations demonstrate that for $F=1.7$ kHz, the contribution of multiple scattering to the transmitted radiation intensity increases with the outer scale from ~10% for $L_0=10$ m to ~90% for $L_0=80$ m; for $L_0=80$ m, the transmitted radiation intensity is almost completely determined by the contribution of multiple scattering. In this case, the sharp decrease of $I_{tr}$ is caused by the exit from the source radiation cone.

The contribution of multiple scattering within the source radiation cone increases from $4.710^{-7}$ to $4.3\cdot10^{-4}$ W/m$^2$, that is, by 89% when $L_0$ increases from 10 to 80 m. This increase in the multiple scattering contributions compensates for the corresponding decrease of the transmitted radiation intensity due to the increase in the outer scale of turbulence and, as can be seen from Figure 5A, $I_{tr}$ for $H<50$ m remains virtually independent of $L_0$.

The dependence of the transmitted radiation intensity for the first detector zone on the angle of source divergence is well described by a quadratic power-law dependence: $I_{tr}(0^\circ,\phi)=A\times\phi^{-2}$, where $I_{tr}$ is in W/m$^2$ and $\phi$ is in degrees. Thus, for $F=1000$, 2000, 3000 and 4000 Hz, $A=2.8\cdot10^{-3}, 1.4\cdot10^{-3}, 2.10^{-4}$ and $4\cdot10^{-4}$, respectively. When the angle of source divergence increases from 5 to $25^\circ$, $I_{tr}$ decreases by 96%, which confirms the necessity of application of massive protective shields in soundars.

Figure 6 from\textsuperscript{11} shows the calculated dependences of the multiple scattering contribution ($I_\text{msc}$) to the transmitted radiation intensity for

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure3.png}
\caption{Total sound attenuation for its vertical propagation. Here the dashed curve shows the results of calculations by the Monte Carlo method and closed triangles show the data measured\textsuperscript{11} with the ascending tethered balloon at $F=2800$ Hz; the solid curve shows the results of our calculations and closed diamonds show the data measured\textsuperscript{11} with the descending tethered balloon at $F=4000$ Hz.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure4.png}
\caption{Distributions of the intensity of transmitted ($I_{tr}$) and multiply scattered ($I_{msc}$) acoustic radiation over the detector zones for the point source and the source with circular aperture and uniform and Gaussian radiation distributions over the source aperture.}
\end{figure}
Figure 5 Distributions of the transmitted \( (I_{tr}, \text{W/m}^2) \) and multiply scattered radiation intensity \( (I_{msc}, \text{W/m}^2) \) over the detector zones for \( F = 1.7 \text{ kHz}, \phi = 5^\circ \) (a and c) and \( 15^\circ \) (b and d); \( F = 4 \text{ kHz}, \phi = 5^\circ \) (e and g) and \( 15^\circ \) (f and h) and indicated values of the outer scale of turbulence, in meters.

The first detector zone with radius \( H = 10 \text{ m} \) on the source altitude \( H_s \) for \( L_0 = 10 \) Figure 6(A) and 20 m Figure 6(B). Sound frequencies \( F \) are plotted on the y axis. From the figure it can be seen that the multiple scattering contribution essentially decreases as the source altitude increases from 5 to 20 m. With further increase in the source altitude, it changes only slightly. Therefore, the source altitude \( H_s = 20 \text{ m} \) can be recommended as optimal for acoustic sounding taking into account that the multiply scattered signal represents noise in the interpretation of the data of acoustic sounding.

The influence of cloudiness is illustrated by Figure 7 which shows...
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statistical estimates of the multiple scattering contribution, MRS, in %, to the transmitted radiation intensity for frequencies in the range 500–3000 Hz in clear and cloudy winter days (for the average relative surface air humidity in winter $u = 67$ and 81%.

Figure 6 Dependence of the multiple scattering contribution to the transmitted radiation intensity on the source altitude $H_s$ above the Earth’s surface for $L_0 = 10$ (A) and 20 m (B).

Figure 7 Contribution of multiple scattering to the transmitted acoustic radiation intensity in the first detector zone in clear and cloudy days for $H_s = 35$ m and $L_0 = 10$ (A) and 20 m (B).

Figure 8 Seasonal (winter-summer) variability of the multiple scattering contribution to the transmitted radiation intensity for the first detector zone, $H_s = 35$ m, and $L_0 = 20$ m.

From the figure it can be seen that for $L_0 = 20$ m and sound frequency of 3000 Hz, variations of the multiple scattering contribution caused by cloudiness are ~20%; moreover, the contribution of multiple scattering increases in cloudy days. To investigate seasonal variations of the multiple scattering contribution, calculations were performed with summer and winter standard mid-latitude models of the atmosphere. Results of calculations are shown in Figure 8.

From the figure it can be seen that in summer for $L_0 = 20$ m the contribution of multiple scattering to the transmitted radiation intensity is by 4–17% larger than in winter. In addition, the seasonal dependence is complex in character. For larger $L_0$ values, the seasonal dependence is intensified. For $L_0 = 5$ m, the difference does not exceed 4%; for $L_0 = 10$ m, it is 10% for the acoustic frequency $F = 2500$ Hz; and for $L_0 = 20$ m, it reaches 17%.

Conclusion

Statistical estimates of the regional variability of the multiple scattering contributions were obtained for Moscow and Novosibirsk.
It was established that in winter for $L_0=20\text{ m}$ and $F=3000\text{ Hz}$, the contribution of multiple scattering for the first detector zone was 34% for Moscow and 50% for Novosibirsk, which demonstrates its essential regional variability.

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**Conflicts of interest**

Authors declare there is no conflict of interest.

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