Heavy flavor suppression in a dynamical QCD medium with finite magnetic mass

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Abstract

Reliable predictions for jet quenching in ultra-relativistic heavy ion collisions require accurate computation of radiative energy loss. While all available energy loss calculations assume zero magnetic mass, in accordance with the one-loop perturbative calculations, different non-perturbative approaches report a non-zero magnetic mass at RHIC and LHC. We generalized the dynamical energy loss formalism, to consistently include a possibility for existence of non-zero magnetic screening. We show that this generalization indicates a fundamental constraint on electric to magnetic mass ratio, which appears to be supported by lattice QCD simulations. Jet suppression patterns, obtained from this newly developed generalization, show reasonable agreement with the available RHIC and LHC measurements.

Keywords: jet suppression, jet energy loss, magnetic mass, heavy quarks

1. Introduction

Jet suppression measurements at RHIC and LHC, and their comparison with theoretical predictions, provide a powerful tool for mapping the properties of a QCD medium created in ultra-relativistic heavy ion collisions [1]. This suppression results from the energy loss of high energy partons moving through the plasma [2]. Therefore, accurate calculations of jet energy loss mechanisms are essential for the reliable predictions of jet suppression.

In [3, 4], we developed a theoretical formalism for the calculation of radiative energy loss in realistic finite size dynamical QCD medium (see also a viewpoint [5]), which abolished a static approximation used in previous models (see e.g. [6, 7, 8]). In this proceedings, we will first provide a brief review of the developed dynamical energy loss formalism. We will then show that in the dynamical medium there are comparable contributions to the energy loss due to both longitudinally (electric) and transversely (magnetic) polarized gluons. Since we will see that the magnetic contribution is significant, we will next discuss how to introduce finite magnetic mass into our formalism. Finally, we will incorporate dynamical energy loss formalism and finite magnetic mass into numerical procedure, which we will use to obtain suppression predictions for RHIC and LHC experiments. Note that only the main results are presented here. For a more detailed version see [9, 10, 11], and references therein.

2. Radiative energy loss - electric and magnetic contributions

In [3, 4] we calculated the radiative jet energy loss in a finite size dynamical QCD medium. The formalism takes into account that the medium constituents are in reality dynamical, that is they are moving particles, and that the medium has finite size. This dynamical energy loss formalism abolished the previously widely used static approximation. The main result of the formalism is presented by the Eq. (1), which shows the expression for the dynamical
energy loss.

\[ \frac{\Delta E_{\text{rad}}}{E} = \frac{C_R \alpha_s}{\pi} \frac{L}{\lambda_{\text{dyn}}} \int \frac{d^2 k}{\pi} \frac{d^2 q}{\pi} v(q) \left[ 1 - \frac{\sin \left( \frac{(k+q)^2}{2} \right)}{\frac{(k+q)^2}{2\mu_E}} L \right] \frac{2(k+q)}{(k+q)^2 + \chi} \left( \frac{(k+q)}{(k+q)^2 + \chi} - \frac{k}{k^2 + \chi} \right) \]  

(1)

Here \( v(q) = \frac{\mu_E^2}{\pi^2 q^2 + \mu_E^4} \) is the effective crosssection in dynamical QCD medium, \( \mu_E \) is Debye screening mass, \( \lambda_{\text{dyn}} \equiv C_2(G)\alpha_s T = 3\alpha_s T \) is defined as “dynamical mean free path”, \( \alpha_s = \frac{e^2}{2\pi} \) is coupling constant and \( C_R = \frac{4}{3}, \) \( m_g = \mu_E/\sqrt{2} \) is the effective mass for gluons with hard momenta \( k \gtrsim T \), and \( \chi \equiv M^2 x^2 + m_g^2 \) where \( x \) is the longitudinal momentum fraction of the heavy quark carried away by the emitted gluon. We assume constant coupling \( g \).

Based on this expression, we can compute and compare the energy loss in the static and the dynamic case (see [4]), showing that in dynamical QCD medium the energy loss is significantly larger compared to the static case. Consequently, the question is what is the origin of such energy loss increase in the dynamical QCD medium? To address this question, it is useful to separate the energy loss to the magnetic and the electric contribution (for more details see [9]). Note that the electric contribution comes from the longitudinally polarized gluon exchanges, while the magnetic contribution comes from the transversely polarized gluon exchange. In [9] we showed that, in the dynamical case, there are both electric and magnetic contributions to the energy loss; on the contrary, in the static medium, there is only the electric contribution.

Figure 1: Left panel: Charm quark fractional radiative energy loss as a function of momentum for an assumed path length \( L = 5 \text{ fm} \) at RHIC (medium temperature \( T = 225 \text{ MeV} \)). Dotted and dashed curves correspond, respectively, to magnetic and electric contributions to the energy loss in a dynamical QCD medium, while dot-dashed curve corresponds to the energy loss in a static QCD medium (see [12]). Right panel: Ratio of magnetic and electric contributions to the radiative energy loss in a finite size dynamical QCD medium for light, charm and bottom quark (full, dot-dashed and dashed curve, respectively) at RHIC.

Since both electric and magnetic contributions are present in the dynamical QCD medium, in Fig. 1 we numerically investigate relative importance of these two contributions. We see that the magnitude of the magnetic and electric contributions are comparable to each other, and they are moreover comparable to the static energy loss. Therefore, we can conclude that the reason for a significant increase of the radiative energy loss in dynamical medium is due to existence of additional magnetic contribution.

3. Magnetic mass and energy loss

In the previous section, we showed that magnetic contribution to the dynamical energy loss is important, which opens a question on how this contribution depends on the value of magnetic mass. That is, HTL preturbative QCD, which we used to develop the energy loss formalism, assumes that magnetic mass is equal to zero. On the other hand, different non-perturbative approaches (see e.g. [13]) suggest a non-zero magnetic mass at RHIC and LHC. Since magnetic contribution to the energy loss depends on magnetic mass, two questions emerge: First, can magnetic mass be consistently included in the dynamical energy loss calculations, and if yes, how this inclusion would modify the energy loss results?

To address the above questions, we generalized the dynamical energy loss formalism to the case of finite magnetic mass. From our analysis in [10] follows that finite magnetic mass modifies only the effective crosssection in Eq. (1) to
Figure 2: Charm quark fractional radiative energy loss as a function of momentum for path length of $L = 5$ fm. Full curve corresponds to the case when magnetic mass is zero. Gray band corresponds to the energy loss when magnetic mass is non-zero (i.e. $0.4 < \mu_M/\mu_E < 0.6$). For left panel, we assume a medium of temperature $T = 225$ MeV and constant coupling $\alpha_S = 0.3$ (“RHIC conditions”). For right panel, we assume a medium of temperature $T = 290$ MeV and constant coupling $\alpha_S = 0.25$ (“LHC conditions”).

the following expression:

$$ v(q) = \frac{\mu_E^2 - \mu_M^2}{(q^2 + \mu_E^2)(q^2 + \mu_M^2)} $$

Furthermore, it is interesting that inclusion of the finite magnetic mass leads to an important physical constraint on the magnetic mass value. From Eq. (2) (see also [10]), it follows that, if magnetic mass is larger than electric mass, the quark jet would, overall, start to gain (instead of lose) energy in this type of plasma. Such energy gain would be in an apparent violation of the second law of thermodynamics, since it would involve a transfer of the energy of disordered motion of the medium constituents to the ordered motion of the jet. From this follows a simple constraint that it is not possible to create a plasma with magnetic mass larger than electric. It is interesting that this simple constraint is actually in agreement with the various non-perturbative approaches, which suggest that, at RHIC and LHC, $0.4 < \mu_M/\mu_E < 0.6$ (see [10] and references therein).

By using Eq. (2) in Fig. 2 we numerically explore what is the effect of introducing finite magnetic mass into energy loss calculations. We see that the introduction of the finite magnetic mass reduces the energy loss for 25% to 50% compared to the zero magnetic mass case.

4. Jet suppression at RHIC and LHC

Based on the developed dynamical energy loss for both zero magnetic value and for finite magnetic value, we now calculate suppression patterns for RHIC and LHC experiments (for more details, see [11]). In addition to taking into account the dynamical effect and the finite magnetic mass, our numerical procedure also includes multigluon [15] and pathlength fluctuations [16]. Multi-gluon fluctuations address the fact that energy loss is a distribution, while path length fluctuations address the fact that particles travel different paths in the medium.

In Fig. 3 we compare our suppression predictions with available experimental data from RHIC and LHC experiments. Left panel correspond to pions, while middle panel correspond to single electrons from RHIC 200 GeV Au+Au collisions. The right panel shows D meson suppression predictions for 2.76TeV Pb+Pb collisions at LHC. In all three panels, we see a reasonable agreement between our predictions and available experimental data, which is moreover robust with the introduction of the finite magnetic mass value. We can, therefore, conclude that introduction of the dynamical medium significantly improves the agreement between the predictions and experimental data.

5. Summary

In this proceedings, we first briefly reviewed the dynamical energy loss formalism, which abolishes the approximation of static medium. Since we showed that the magnetic contribution to the energy loss is important, we consequently generalized the dynamical energy loss to include a possibility of finite magnetic mass. This generalization suggests a
simple constraint on electric to magnetic mass ratio. We furthermore incorporated the dynamical formalism, together with the finite magnetic mass, into a numerical procedure for suppression predictions. The predictions for RHIC and LHC indicate a reasonable agreement of the dynamical energy loss formalism with the available data.

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References

[1] N. Brambilla et al., Preprint hep-ph/0412158 (2004).
[2] M. Guylassy, I. Vitev, X. N. Wang and B. W. Zhang, in Quark Gluon Plasma 3, edited by R. C. Hwa and X. N. Wang, p. 123 (World Scientific, Singapore, 2003)
[3] M. Djordjevic, Phys. Rev. C 80, 064909 (2009).
[4] M. Djordjevic and U. Heinz, Phys. Rev. Lett. 101, 022302 (2008).
[5] M. Gyulassy, Physics 2, 107 (2009).
[6] M. Gyulassy, P. Levai and I. Vitev, Nucl. Phys. B 594, 371 (2001).
[7] M. Gyulassy and X. N. Wang, Nucl. Phys. B 420, 583 (1994); X. N. Wang, M. Gyulassy and M. Plumer, Phys. Rev. D 51 (1995) 3436.
[8] U.A. Wiedemann, Nucl. Phys. B 588, 303 (2000); and Nucl. Phys. B 582, 409 (2000).
[9] M. Djordjevic, J. Phys. G G39 045007 (2012).
[10] M. Djordjevic and M. Djordjevic, Phys. Lett. B709 229 (2012).
[11] M. Djordjevic, Phys. Rev. C 85, 034904 (2012).
[12] M. Djordjevic and M. Gyulassy, Phys. Lett. B. 560, 37 (2003); and Nucl. Phys. A 733, 265 (2004).
[13] Yu. Maezawa et al. [WHOT-QCD Collaboration], Phys. Rev. D 81 091501 (2010); Yu. Maezawa et al. [WHOT-QCD Collaboration], PoS Lattice 194 (2008).
[14] B. Betz and M. Gyulassy, Phys. Rev. C 86 024903 (2012).
[15] M. Gyulassy, P. Levai and I. Vitev, Phys. Lett. B 538, 282 (2002).
[16] S. Wicks, W. Horowitz, M. Djordjevic and M. Gyulassy, Nucl. Phys. A 784, 426 (2007).
[17] A. Adare et al. [PHENIX collaboration], Phys. Rev. Lett. 101, 232301 (2008).
[18] A. Adare et al. [PHENIX collaboration], Phys. Rev. Lett. 98, 172301 (2007).
[19] B.I. Abelev et al. [STAR collaboration], Phys. Rev. C 80 044905 (2009).
[20] B.I. Abelev et al. [STAR collaboration], Phys. Rev. Lett. 98, 192301 (2007).
[21] B. Abelev, et al. [ALICE collaboration] arXiv:1203.2160