Privacy-Preserving XGBoost Inference

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Abstract

Although machine learning (ML) is widely used for predictive tasks, there are important scenarios in which ML cannot be used or at least cannot achieve its full potential. A major barrier to adoption is the sensitive nature of predictive queries. Individual users may lack sufficiently rich datasets to train accurate models locally but also be unwilling to send sensitive queries to commercial services that vend such models. One central goal of privacy-preserving machine learning (PPML) is to enable users to submit encrypted queries to a remote ML service, receive encrypted results, and decrypt them locally. We aim at developing practical solutions for real-world privacy-preserving ML inference problems. In this paper, we propose a privacy-preserving XGBoost prediction algorithm, which we have implemented and evaluated empirically on AWS SageMaker. Experimental results indicate that our algorithm is efficient enough to be used in real ML production environments.

1 Introduction

Machine Learning (ML) plays an important role in daily life. Pervasive use of digital devices and networks produces massive amounts of data that are analyzed to reveal patterns and correlations that, in turn, are used to draw conclusions or make predictions. Diverse applications that make successful use of ML include market forecasting, service personalization, voice and facial recognition, autonomous driving, health diagnostics, education, and security analytics.

Clearly in tension with the utility of ML is the desire of individuals and organizations for data privacy. Both the input and the output of an ML prediction may be highly personal, confidential information and may be constrained by regulations. For example, students’ confidential educational records are governed by FERPA – the Family Educational Rights and Privacy Act. Organizations that produce valuable models may wish to sell access to them on a pay-per-prediction basis and must protect them as one would any valuable form of digital intellectual property. The need to maintain the privacy of data subjects, to protect intellectual property, and to keep commercially valuable instances and predictions confidential motivate the study of privacy-preserving machine learning (PPML).

Gentry has shown that one can perform arbitrary computations on encrypted data using fully homomorphic-encryption (FHE) [16]. In principle, FHE could fully resolve the tension between utility of ML and data-privacy requirements, but there are application scenarios in which it is prohibitively computationally expensive by orders of magnitude. In these scenarios, it is natural to seek specialized homomorphic-encryption (SHE) schemes that are more efficient. We provide one such scheme in this paper.

Extreme Gradient Boosting (XGBoost) [9] is an optimized, distributed, gradient-boosting ML framework designed to be highly efficient, flexible, and portable. It performs parallel tree boosting that solves many classification and regression problems quickly and accurately. For example, 17 of the

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34th Conference on Neural Information Processing Systems (NeurIPS 2020), Vancouver, Canada.
29 challenge-winning solutions published on Kaggle’s blog in 2015 used XGBoost\(^{29}\), Facebook uses it to predict click through on advertisements\(^{19}\), and it is very popular on Amazon’s managed-cloud ML platform SageMaker\(^2\).

We present PPXGBoost, a privacy-preserving XGBoost-prediction algorithm, in Section\(^2\). In Section\(^3\) we explain the security definition and the privacy properties that our algorithm achieves. Experimental results are given in Section\(^4\). Finally, we present open problems in Section\(^5\).

2 Privacy-preserving XGBoost

2.1 Preliminaries

XGBoost Upon receiving a training dataset, the XGBoost training algorithm produces an ML model in the form of a set \(\{T_i\}_{i=1}^M\) of classification and regression trees (CARTs). A CART is a generalization of a decision tree; while the latter produces a binary output, thus classifying each input query as a “yes” or “no” instance of the phenomenon under study, a CART assigns to each input query a (real) numerical score. Interpretation of scores is application-dependent.\(^3\) We use boldface lowercase letters, such as \(v\), to denote a vector of real numbers. If \(v\) is an input query, and \(\{y_i \leftarrow T_i(v)\}_{i=1}^M\) is the set of scores produced by the CARTs, then the final prediction (i.e., the overall score assigned to \(v\) by XGBoost) is typically \(y = \sum_{i=1}^M y_i\). Depending on the application, a softmax function may be applied to the \(y_i\) to obtain the final prediction, but we restrict attention to summation in this paper. A full explanation of XGBoost training and inference can be found in the original paper of Chen and Guestrin\(^9\).

Homomorphic encryption Homomorphic encryption is a form of encryption that can perform arbitrary computation on plaintext values while manipulating only ciphertexts. In this work, we use an additive SHE scheme. Specifically, let SHE = (Gen, Enc, Dec) be a public-key SHE that consists of three polynomial-time algorithms. Gen is a probabilistic algorithm that takes a security parameter \(k\) as input and returns a private and public key pair \((pk, sk)\). Enc is a probabilistic encryption algorithm that takes as input a public key \(pk\) and a message \(m\) and outputs a ciphertext. Dec is an algorithm that takes as input a private key \(sk\) and a ciphertext and returns the corresponding plaintext. In addition, SHE has an evaluation algorithm Eval that supports any number of additions over the plaintexts: \(\text{Enc}(pk, (m_1 + \cdots + m_n)) = \text{Eval}(+, \text{Enc}(pk, m_1), \ldots, \text{Enc}(pk, m_n))\).

Order-preserving encryption For \(A, B \subseteq \mathbb{N}\) with \(|A| \leq |B|\), a function \(f : A \rightarrow B\) is order-preserving if, for all \(i, j \in A\), \(f(i) > f(j)\) if and only if \(i > j\). We say that a symmetric encryption scheme \((\text{Gen}, \text{Enc}, \text{Dec})\) with plaintext and ciphertext spaces \(\mathcal{D}\) and \(\mathcal{R}\) is an order-preserving encryption (OPE) scheme if \(\text{Enc}(K, \cdot)\) is an order-preserving function from \(\mathcal{D}\) to \(\mathcal{R}\), for all \(K\) output by \(\text{Gen}(1^k)\). To make sense of the \(>\) relation in this context, elements of \(\mathcal{D}\) and \(\mathcal{R}\) are encoded as binary strings, which are then interpreted as numbers.

Throughout this paper, “polynomial” means “polynomial in the security parameter \(k\).” Formal definitions of these cryptographic concepts, including the Pseudorandom Function (PRF) family and semantic security can be found in\(^{23}\).

2.2 PPXGBoost inference algorithm

The PPXGBoost algorithm is given in Figure\(^1\). On the client side, there is an app with which a user encrypts queries and decrypts results. On the server side, there is a module called Proxy that runs in a trusted environment and is responsible for set up (i.e., creating, for each authorized user, an encrypted model and a set of cryptographic keys) and an ML module that evaluates the encrypted queries.

The inputs to the Setup phase are an XGBoost model \(\Omega\), a model hyper-parameter \(\alpha\), and a security parameter \(k\). During this phase, Proxy generates, for each authorized user, the keys \(K_1\) and \((pk, sk)\). \(K_1\) is the user’s key for the (symmetric-key) OPE scheme. \((pk, sk)\) is the user’s key pair for the (public-key) SHE scheme. Proxy then encrypts the node values in each CART \(T_i\) in \(\Omega\) to create an

\(^{2}\)https://aws.amazon.com/sagemaker/

\(^{3}\)This is one of the roles of the hyper-parameter \(\alpha\) referred to in Subsection 2.2.
```plaintext
Setup Phase:
Input: Plaintext model $\Omega$; Security parameter $k$; Model hyper-parameter $\alpha$.
Proxy computes:
- $K_1 \leftarrow \text{OPE.Gen}(1^k)$;
- $(pk, sk) \leftarrow \text{SHE.Gen}(1^k)$;
- Choose $f$ uniformly at random from $\mathcal{F}_k$ in the PRF family;
- Choose $K_2$ uniformly at random from $\{0,1\}^k$;
- For each CART $T_i \in \Omega$, construct $T'_i$ in EncML as follows:
  - $T'_i$ is structurally isomorphic to $T_i$. Let $\phi: T_i \rightarrow T'_i$ be an isomorphism;
  - For each internal node $x$ with value $v$ in $T_i$, assign the value $\text{OPE.Enc}(K_1, v)$ to $\phi(x)$;
  - For each leaf $z$ with value $y_i$ in $T_i$, assign the value $\text{SHE.Enc}(pk, y_i)$ to $\phi(z)$;
  - For each feature name $\ell$ used in $T_i$, create the corresponding feature pseudonym $\ell' \leftarrow f(K_2, \ell)$;
Proxy sends to ML Module: EncML;
Query Phase:
Input (to client): Query $q_i$.
- Client computes:
  - For each feature name $\ell$ in $q_i$, compute the corresponding feature pseudonym $\ell' \leftarrow f(K_2, l)$;
  - Encrypt the plaintext value: $q'_i \leftarrow \text{OPE.Enc}(K_1, q_i)$;
- Client sends to ML Module: $q'_i$;
- ML Module computes:
  - For each $T'_i \in$ EncML, evaluate $T'_i$ on $q'_i$ to obtain value $y'_i$;
  - Homomorphically sum the values: $\overset {\text{ML Module}} {y'} \leftarrow \text{SHE.Eval}(+, y'_1, \ldots, y'_n)$, where $n$ is the number of CARTs in EncML (note: this step is slightly different for computing softmax objective);
- ML Module sends to client: $y'$;
- Client decrypts the result: $y \leftarrow \text{SHE.Dec}(sk, y')$;
- Client interprets the result using the model hyper-parameter $\alpha$;
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Figure 1: PPXGBoost: A privacy-preserving XGBoost inference algorithm

encrypted CART $T'_i$ in this user’s encrypted model EncML. For each internal node in $T_i$ with value $x$, the value of the corresponding node in $T'_i$ is $\text{OPE.Enc}(K_1, x)$. (Vectors of values are encrypted and decrypted component-wise.) For each leaf in $T_i$ with value $y$, the value of the corresponding leaf in $T'_i$ is $\text{SHE.Enc}(pk, y)$. Finally, the proxy sends $K_1$, $K_2$, $f$, sk to the user’s client and sends EncML to the ML module.

In the Query phase, the client first encrypts its plaintext query $q_i$ with OPE, i.e., it computes $q'_i \leftarrow \text{OPE.Enc}(K_1, q_i)$. It sends $q'_i$ to the ML module, which evaluates each $T'_i$ in EncML on input $q'_i$ to obtain a value $y'_i$. The module computes $y' \leftarrow \text{SHE.Eval}(+, y'_1, \ldots, y'_n)$, where $n$ is the number of CARTs, and sends it to the client, which decrypts to obtain the final result $y \leftarrow \text{SHE.Dec}(sk, y')$.

The correctness of this scheme follows directly from the properties of OPE and SHE. Because $a > b$ if and only if $\text{OPE.Enc}(K_1, a) > \text{OPE.Enc}(K_1, b)$, for all $a, b$, and $K_1$, and the same $K_1$ is used to encrypt both queries and internal-node values in $\Omega$, an encrypted query will travel precisely the same path through each encrypted CART $T'_i$ that the corresponding plaintext query would have traveled through the corresponding plaintext CART $T_i$. Because the leaf values $y_i$ in $\Omega$ have been encrypted using the additively homomorphic encryption operation $\text{SHE.Enc}(pk, y_i)$, and sk is the decryption key that corresponds to pk, the plaintext $y$ corresponding to the ciphertext sum $y'$ is the sum of the individual plaintext values $y_i$ in leaves of $T_i$.

The proxy also chooses, for each authorized user, a function $f$ uniformly at random from $\mathcal{F}_k$ in the PRF family and a a key $K_2$ uniformly at random from $\{0,1\}^k$ for use with $f$. This function is used to generate pseudorandom “feature names” for vectors of queries and node values. We defer discussion of this aspect of the algorithm until the full paper.

Note that the plaintext $(\Omega, \alpha, k)$ can be used by a very large user population, but a unique, personalized encrypted model must be created for each individual user.

3 Privacy properties

Ideally, we would like a privacy-preserving inference algorithm to hide all information about the model, the queries, and the results from all adaptive probabilistic polynomial-time (PPT) adversaries.
For the Setup phase, this means that the adversary should be able to choose a sequence $M_1, M_2, \ldots, M_n$ of plaintext models, submit them to an oracle, and receive the corresponding sequence $M'_1, M'_2, \ldots, M'_n$ of encrypted models; it may choose the sequence adaptively in the sense that its choice of $M_i$ may depend upon the oracle’s answers $M'_1, \ldots, M'_{i-1}$. After this adaptive, chosen-plaintext, oracle-query phase, the adversary is presented with an encrypted model that it has not seen before, and it cannot infer anything about the corresponding plaintext model.

For the Query phase, this means that, for a fixed encrypted model $M'$, the adversary should be able to choose a sequence $q_1, q_2, \ldots, q_n$ of plaintext queries, submit them to an oracle, and receive the corresponding sequence $\sigma = (q'_1, r'_1), (q'_2, r'_2), \ldots, (q'_n, r'_n)$ of encrypted queries and encrypted results; once again, it may choose $q_i$ based on $\sigma_{i-1} = (q'_1, r'_1), \ldots, (q'_{i-1}, r'_{i-1})$. After this adaptive query phase, it cannot infer anything about the encrypted model; furthermore, when subsequently presented with additional pairs $(q'_{n+1}, r'_{n+1}), \ldots, (q'_{n+j}, r'_{n+j})$, it cannot infer anything about the corresponding plaintext queries or answers.

Known algorithms that achieve these ideal privacy properties are not efficient enough for practical use. As initiated in the work of Curtmola et al.\cite{curtmola2006privacy} and Chase and Kamara\cite{chase2010fully}, one can instead define acceptable leakage functions and devise efficient algorithms that provably leak only the values of these functions. In PPXGBoost, this information may be leaked to the ML module and any party that observes the inner workings of the ML module, the communication between Proxy and the ML module, or the communication between the client and the ML module.

Because of space limitations we give the main ideas of our formal security definitions, PPXGBoost’s privacy properties, and our security proof in Appendix\cite{appendix}

### 4 AWS SageMaker experiments

| DATASET                  | TIME | MODEL SIZE |
|--------------------------|------|------------|
|                          | XGBoost | PPXGBoost | XGBoost | PPXGBoost |
| Amazon Synthetic Data    | 1ms   | 0.43s      | 506KB   | 4.2MB     |
| Titanic                  | < 1ms | 0.32s      | 3KB     | 12KB      |
| US Census                | 1ms   | 0.49s      | 210KB   | 2.5MB     |

Table 1: PPXGBoost Performance

For our experiments on PPXGBoost, we implemented the cryptographic protocols in python3. We instantiated the PRF using HMAC, and we used Paillier encryption\cite{paillier1999public} for our additive SHE and Boldyreva et al.’s scheme\cite{boldyreva2008additive} for our OPE.

An overview of our system architecture can be found in Appendix\cite{appendix}. All of our experiments were run on AWS. The Setup phase is deployed in AWS Virtual Private Cloud\cite{amazonvpc} environment. The inference procedure is run on SageMaker using an ml.t2.large instance and the Amazon Elastic Container Service\cite{amazonecs}. Our experimental results are summarized in Table 1. We ran PPXGBoost on three different models derived from three different datasets. One data is synthetically generated based on Amazon’s dataset. The other two datasets are public datasets. On average, PPXGBoost inference is approximately $10^3$ times slower than the plaintext version of XGBoost. The size of encrypted models is between four and nine times larger than that of the plaintext models. The inference time includes the network traffic time. This performance is sufficient for many inference tasks currently done on smart phones that must query a remote server.

### 5 Open problems

Our initial version of PPXGBoost is still quite limited. Currently, we can support binary classifications and multiclass classification using the softmax objective. Future work includes support for more learning parameters in the privacy-preserving version. Moreover, in our algorithm, we leverage the order-preserving encryption scheme to support comparisons. Comparison on semantically

https://aws.amazon.com/vpc/  
https://aws.amazon.com/ecs/
encrypted data is computationally expensive, but we plan to investigate the use of secure multiparty computation for this purpose. In particular, we will explore the use of two non-colluding servers that execute secure comparison for each internal node in an encrypted CART.

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A System Architecture

As mentioned in the paper, we deploy PPXGBoost using AWS infrastructure. We set up an Amazon VPC environment for deploying the inference prototype. Amazon VPC environment allows the model provider to have a logically isolated section of the AWS Cloud, therefore; the PPXGBoost provider can have complete control over the virtual networking environment. The Proxy service is deployed in a trusted environment, similarly to Amazon’s Key Management Services (KMS). The ML module is run on the Amazon SageMaker platform, a fully managed machine learning service. The security of SageMaker its own relies on the traditional AWS’s security model including AWS Identity and Access Management (IAM), Amazon Macie, etc.

Figure 2: System architecture

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*see https://docs.aws.amazon.com/sagemaker/latest/dg/data-protection.html
Amazon SageMaker makes extensive use of Docker containers for build and runtime tasks. After the proxy produces an encrypted model EncML, we store EncML to an S3 bucket (with proper permission configuration). We package our inference algorithm using Amazon’s container service, Amazon ECS. When deploying the ML inference module, we upload the inference package in Amazon’s Elastic Container Repository and specify the encrypted model location in S3. We create an endpoint for this SageMaker instance to handle the encrypted queries. After the client receives a private key, the client can send an encrypted query by querying a SageMaker endpoint. The ML module computes the encrypted query and returns an encrypted result to the client.

B Privacy Definitions and Proof

At a high level, the security guarantee we require from privacy-preserving inference scheme is that:

1. given an encrypted ML model, no adversary can learn any information about the model; and
2. given the view of a polynomial number of Query executions for an adaptively generated sequence of queries \( q = (q_1, \ldots, q_m) \), no adversary can learn any partial information about either the model or \( q \).

Such a security notion can be difficult to achieve efficiently, so often one allows for some form of leakage. Following [10], this is usually formalized by parameterizing the security definition with leakage functions for each operation of the scheme which in this case include the Setup algorithm and Query protocol.

B.1 Security definition

In our description of what it means for \( \text{PPXGB} = (\text{Setup, Query}) \) to be secure, \( \mathcal{A} \) is a semi-honest adversary, \( \mathcal{S} \) is a simulator, \( \mathcal{L}_{\text{Setup}} \) and \( \mathcal{L}_{\text{Query}} \) are the leakage functions, and \( \sigma \) and \( \sigma_{i-1} \) are as defined above. The terms Ideal and Real are used as they are in the literature on searchable encryption [10].

Let \( \Omega \) and \( \alpha \) be an XGBoost model and hyper-parameter chosen by \( \mathcal{A} \). Let \( v \) be a polynomially bounded function of \( k \). We consider the following two randomized experiments.

**Real**\( \Omega, 1^k, \alpha \):

- Run the Setup protocol: \( (K, \text{EncML}) \leftarrow \text{Setup}(\Omega, 1^k, \alpha) \)
- Execute the Query protocol \( m = v(k) \) times. In these executions, Client (adaptively) chooses queries as well as performing its role in Figure [1] it chooses \( q_1 \) uniformly at random.
- Output the sequence \( \sigma = (q_1', r_1'), (q_2', r_2'), \ldots, (q_m', r_m') \) of encrypted queries and results.

**Ideal\( _{\mathcal{A}, \mathcal{S}} \mathcal{L}_{\text{Setup}}(\Omega), 1^k, \alpha \):

- Given \( \mathcal{L}_{\text{Setup}}(\Omega), 1^k \), and \( \alpha \), \( \mathcal{S} \) generates an encrypted model EncML and sends it to \( \mathcal{A} \).
- \( \mathcal{A} \) and \( \mathcal{S} \) conduct \( m = v(k) \) executions of the Query protocol, in which \( \mathcal{S} \) plays the role of Client by (adaptively) constructing a sequence \( (q_1, \ldots, q_m) \) of queries, and \( \mathcal{A} \) plays the role of the ML module. \( \mathcal{S} \) generates \( q_1 \) uniformly at random and uses \( \mathcal{L}_{\text{Query}}(\Omega, \sigma_{i-1}) \) to generate \( q_i, 2 \leq i \leq m \).
- Output the sequence \( \sigma = (q_1', r_1'), (q_2', r_2'), \ldots, (q_m', r_m') \) of encrypted queries and results.

The gist of our security definition is that a PPT observer cannot distinguish between outputs of the Real experiment, which runs the protocol in Figure [1] and the Ideal experiment, in which a simulator that knows the values of the leakage functions plays the role of the client and the adversary plays the role of the ML module. A distinguisher \( \mathcal{D} \) is an algorithm that plays a refereed game with the adversary. In each round of the game, the referee obtains \( \Omega \) and \( \alpha \) from \( \mathcal{A} \), runs either Real\( (\Omega, 1^k, \alpha) \) or Ideal\( _{\mathcal{A}, \mathcal{S}} \mathcal{L}_{\text{Setup}}(\Omega), 1^k, \alpha \), and shows the output of whichever experiment is run to the distinguisher.

Let \( w \) be a polynomially bounded function of \( k \). The entire distinguishing game proceeds as follows. Fix a security parameter \( k \). For \( w(k) \) rounds, \( \mathcal{D} \) may ask the referee to run either Real\( (\Omega, 1^k, \alpha) \) or Ideal\( _{\mathcal{A}, \mathcal{S}} \mathcal{L}_{\text{Setup}}(\Omega), 1^k, \alpha \) and show him the output. The referee then chooses \( b \in \{0, 1\} \) uniformly at random; if \( b = 0 \), it runs Real\( (\Omega, 1^k, \alpha) \), and, if \( b = 1 \), it runs Ideal\( _{\mathcal{A}, \mathcal{S}} \mathcal{L}_{\text{Setup}}(\Omega), 1^k, \alpha \).
It shows the output to $\mathcal{D}$, and $\mathcal{D}$ outputs its best guess $b'$ of the value of $b$. The *distinguisher’s advantage* in this game, which is a function of the security parameter $k$, is $\Pr[b = b'] - \frac{1}{2}$.

**Definition B.1.** We say that PPXGBoost is adaptively $(\mathcal{L}_{\text{Setup}}, \mathcal{L}_{\text{Query}})$-semantically secure if, for every PPT adversary $\mathcal{A}$, there exists a PPT simulator $\mathcal{S}$ for which every PPT distinguisher’s advantage is negligible in $k$.

### B.2 Leakage profile

We now describe the leakage functions that specify, in the sense of (10) (8), the information that PPXGBoost is willing to leak for the sake of efficiency.

**Setup leakage.** Recall that the Setup phase of PPXGBoost takes as one of its inputs a plaintext model $\Omega$ and gives as one of the outputs an encrypted model. The plaintext model consists of a set of CARTs. Setup leakage in PPXGBoost is a function $\mathcal{L}_{\text{Setup}}(\Omega)$ of the plaintext model; it consists of the number of CARTs in $\Omega$, the depth of each CART, and, for each internal node $w$ in each CART, which of $w$’s two children has the smaller value. Note that the numerical values of the nodes are not leaked; this is true of both internal nodes and leaves. In the high-level descriptions of Setup given in Section 2 and Figure 1, the entire structure of each CART is leaked, but, in practice, it is straightforward to pad each CART out to a complete binary tree of the appropriate depth without changing the results of the computation.

**Query leakage.** During the Query phase of PPXGBoost, the client and ML module exchange a sequence $\sigma = (q_1', r_1'), (q_2', r_2'), \ldots, (q_n', r_n')$ of encrypted queries and encrypted results. Query leakage in PPXGBoost is a function $\mathcal{L}_{\text{Query}}(\Omega, \sigma)$ of the plaintext model and this sequence. It consists of a query pattern and the set of paths that are traversed during the execution of the encrypted queries. For every encrypted query $q'$ in $\sigma$, this phase of PPXGBoost leaks the number of times it appears in $\sigma$ and where it appears; that is, for every $q'$, the query phase reveals the set of $i$, $1 \leq i \leq n$, such that $q_i' = q'$. In addition, for each $q_i'$ and each encrypted CART, the path from the root to a leaf in that CART that is traversed during the evaluation of $q_i'$ is leaked to the ML module and to any party that can observe the inner workings of this module while queries are executed. Note that the query pattern and set of paths is well defined for each prefix $\sigma_i$ of $\sigma$. Crucially, the decryptions of the queries and results are not leaked.

### B.3 Main idea and interpretation of the security proof

To prove that the only information leaked by PPXGBoost is $\mathcal{L}_{\text{Setup}}$ and $\mathcal{L}_{\text{Query}}$, we present a PPT algorithm that is given $1^k$, $\alpha$, $\mathcal{L}_{\text{Setup}}(\Omega)$, and $\mathcal{L}_{\text{Query}}(\Omega, \sigma)$ as input and simulates the behavior of PPXGBoost’s Setup and Query phases. We provide the main idea of the security proof here and defer the full proof to an expanded version of this paper.

Given $\mathcal{L}_{\text{Setup}}(\Omega)$, a simulator $\mathcal{S}$ can construct a set $\{T_i\}$ of CARTs with the required ordering of internal nodes by sampling random values from the co-domain of OPE. For the leaves, $\mathcal{S}$ assigns values chosen at random from the co-domain of SHE. Given $\mathcal{L}_{\text{Query}}(\Omega, \sigma)$, $\mathcal{S}$ follows, for each encrypted query, the appropriate paths in each $T_i$ that it constructed and returns the leaf value. The security properties of the OPE and SHE schemes ensure that the final predictions are not revealed.

### C Related work

Practical attacks on supervised learning systems that result in leakage of sensitive information about training datasets, models, or hyper-parameters can be found in, e.g., (14; 21; 38). Among proposals to mitigate those attacks, the majority focus on classification models, including decision trees (25), SVM classification (39), linear regression (11; 12; 37), logistic regression (13), and neural networks (30; 52; 56). Recently, a fast-growing number of works (e.g., (3; 29; 15; 18; 14; 3; 8; 15; 26; 12; 52; 17; 28; 24; 22)) have achieved strong security guarantees in this setting by providing concrete security definitions and provably secure protocols that use multiple cryptographic-computation techniques (32). Another research thread has focused on privacy-preserving federated learning (see, e.g., (4)), in which multiple mobile users update a global model by sharing aggregated updates to model parameters using a privacy-preserving, client-server protocol. Recently, Liu et al. (27) proposed a privacy-preserving boosting method for training XGBoost models in the federated-learning setting.