Cosmological Reionization

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In popular cosmological scenarios, some time beyond a redshift of 10, stars within protogalaxies created the first heavy elements; these systems, together perhaps with an early population of quasars, generated the ultraviolet radiation and mechanical energy that reheated and reionized the cosmos. The history of the Universe during and soon after these crucial formative stages is recorded in the all-pervading intergalactic medium (IGM), which contains most of the ordinary baryonic material left over from the big bang. Throughout the epoch of structure formation, the IGM becomes clumpy and acquires peculiar motions under the influence of gravity, and acts as a source for the gas that gets accreted, cools, and forms stars within galaxies, and as a sink for the metal enriched material, energy, and radiation which they eject.

Keywords: diffuse radiation – intergalactic medium – radiative transfer

1. Introduction

At epochs corresponding to $z \sim 1000$ the intergalactic medium (IGM) is expected to recombine and remain neutral until sources of radiation and heat develop that are capable of reionizing it. The detection of transmitted flux shortward of the Ly$\alpha$ wavelength in the spectra of sources at $z \sim 5$ implies that the hydrogen component of this IGM was ionized at even higher redshifts. There is some evidence that the double reionization of helium may have occurred later, but this is still controversial. It appears then that substantial sources of ultraviolet photons and mechanical energy were already present when the Universe was less than 7% of its current age, perhaps quasars and/or young star-forming galaxies: an episode of pre-galactic star formation may provide a possible explanation for the widespread existence of heavy elements (like carbon, oxygen, and silicon) in the IGM, while the integrated radiation emitted from quasars is likely responsible for the reionization of the intergalactic helium. Establishing the epoch of reionization and reheating is crucial for determining its impact on several key cosmological issues, from the role reionization plays in allowing protogalactic objects to cool and make stars, to determining the small-scale structure in the temperature fluctuations of the cosmic microwave background. Conversely, probing the reionization epoch may provide a means for constraining competing models for the formation of cosmic structures, and of detecting the onset of the first generation of stars, galaxies, and black holes in the Universe.
2. The transition from a neutral to an ionized Universe

Popular cosmological models predict that most of the intergalactic hydrogen was reionized by the first generation of stars or accreting black holes at \( z = 7 - 15 \). One should note, however, that while numerical N-body+hydrodynamical simulations have convincingly shown that the IGM is expected to fragment into structures at early times in cold dark matter (CDM) cosmogonies (e.g. Cen et al. 1994; Zhang, Anninos, & Norman 1995; Hernquist et al. 1996), the same simulations are much less able to predict the efficiency with which the first gravitationally collapsed objects lit up the Universe at the end of the ‘dark age’ (Rees, this volume).

(a) Photo- versus collisional ionization

The scenario that has received the most theoretical studies is one where hydrogen is photoionized by the UV radiation emitted either by quasars or by stars with masses \( \gtrsim 10 \, M_\odot \), rather than ionized by collisions with electrons heated up by, e.g. supernova-driven winds from early pregalactic (‘Pop III’) objects. In the former case a high degree of ionization requires about \( 13.6 \times (1 + t/t_{\text{rec}}) \) eV per hydrogen atom, where \( t_{\text{rec}} \) is the volume-averaged hydrogen recombination timescale, \( t/t_{\text{rec}} \) being much greater than unity already at \( z \approx 10 \) according to the numerical simulations of Gnedin & Ostriker (1997), and Gnedin (2000). Collisional ionization to a neutral fraction of only few parts in \( 10^5 \) requires a comparable energy input, i.e. an IGM temperature close to \( 10^5 \) K or about 25 eV per atom.

Massive stars will deposit both radiative and mechanical energy into the interstellar medium of Pop III objects. A complex network of ‘feedback’ mechanisms is likely at work in these systems, as the gas in shallow potential is more easily blown away thereby quenching further star formation (Mac Low & Ferrara 1999), and the blastwaves produced by supernova explosions reheat the surrounding intergalactic gas and enrich it with newly formed heavy elements and dust. It is therefore difficult to establish whether an early input of mechanical energy will actually play a major role in determining the thermal and ionization state of the IGM on large scales (Tegmark, Silk, & Evrard 1993). What can be easily shown is that, during the evolution of a ‘typical’ stellar population, more energy is lost in ultraviolet radiation than in mechanical form. This is because in nuclear burning from zero to solar metallicity (\( Z_\odot = 0.02 \)), the energy radiated per baryon is \( 0.02 \times 0.007 \times m_{\text{H}^2} \); about one third of it goes into H-ionizing photons. The same massive stars that dominate the UV light also explode as supernovae (SNe), returning most of the metals to the interstellar medium and injecting about \( 10^{51} \) ergs per event in kinetic energy. For a Salpeter initial mass function (IMF), one has about one SN every 150 \( M_\odot \) of baryons that forms stars. The mass fraction in mechanical energy is then approximately \( 4 \times 10^{-6} \), ten times lower than the fraction released in photons above 1 ryd.

The relative importance of photoionization versus shock ionization will depend, however, on the efficiency with which radiation and mechanical energy actually escape into the IGM. Consider, for example, the case of an early generation of halos with circular speed \( v_c = 50 \, \text{km} \, \text{s}^{-1} \), corresponding in top-hat spherical collapse to a virial temperature \( T_v = 0.5 \mu m_p v_c^2/k \approx 10^{5.3} \) K and halo mass \( M = 0.1 v_c^3/GH \approx \).
In these systems rapid cooling by atomic hydrogen can take place and a significant fraction, $f\Omega_B$, of their total mass may be converted into stars over a dynamical timescale (here $\Omega_B$ is the baryon density parameter). For $f = 0.05$, $\Omega_B h^2 = 0.02$, and $h = 0.5$, the explosive output of 50,000 SNe would inject an energy $E_0 \approx 10^{55.7}$ ergs. The hot gas will escape its host, shock the IGM, and eventually form a cosmological blast wave. If the explosion occurs at cosmic time $t = 4 \times 10^8$ yr, corresponding in the adopted cosmology (EdS with $h = 0.5$) to $z = 9$, at time $\Delta t = 0.2t$ after the event the proper radius of the (adiabatic) shock is given by the standard Sedov-Taylor self-similar solution,

$$R_s \approx \left( \frac{12\pi GE_0}{\Omega_B} \right)^{1/5} t^{2/5} \Delta t^{2/5} \approx 23 \text{ kpc}. \quad (1)$$

At this instant the shock velocity relative to the Hubble flow is

$$v_s \approx 2R_s/\Delta t \approx 110 \text{ km s}^{-1}, \quad (2)$$

still much higher than the escape velocity from the halo. The gas temperature just behind the shock front is $T_s = 3\mu m_p v_s^2/16k \approx 4 \times 10^5$ K, more than enough to efficiently ionize all the incoming hydrogen. At these redshifts, it is the onset of Compton cooling off cosmic microwave background photons that ends the adiabatic stage of blast wave propagation. According to the Press-Schechter formalism, the comoving abundance of collapsed dark halos with mass $M = 10^9 h^{-1} M_\odot$ at $z = 9$ is $d\ln n/d\ln M \sim 5 h^3 \text{ Mpc}^{-3}$, corresponding to a mean proper distance between neighboring halos of $\sim 40 h^{-1}$ kpc, and to a total mass density parameter of order 0.02. With the assumed star formation efficiency, only a small fraction, about one percent, of the stars seen today would have to be formed at these early epochs. Still, our simple analysis shows that the blast waves from such a population of pregalactic objects could overlap with large enough velocities to initially drive the intergalalactic medium to a significantly higher adiabat, $T \gtrsim 10^5$ K, than expected from photoionization, and pollute the entire IGM with metal-enriched material. A lower density of sources – which would therefore have to originate from higher amplitude peaks – would suffice if the typical efficiency of star formation were larger than assumed here.

Quasar-driven blast waves ($E_0 \gtrsim 10^{60}$ ergs) are instead quite inefficient at ionizing the IGM, since much of the initial explosion energy is lost into the collisionless component (Voit 1996). They would also be too rare to fill the IGM without violating the COBE limit on the $y$-distortion of the microwave background.

### (b) Cosmological H II regions

In the following sections we will focus our attention to the photoionization of the IGM, i.e. we will assume that UV photons from an early generation of stars and/or quasars are the main source of energy for the reionization and reheating of the Universe, and that star formation and quasar activity occurs in collapsed galaxy halos. The process then begins as individual sources start to generate expanding H II regions in the surrounding IGM; throughout an H II region, H is ionized and He is either singly or doubly ionized. As more and more sources of ultraviolet

† This assumes an Einstein-de Sitter (EdS) Universe with $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$. 

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radiation switch on, the ionized volume grows in size while the neutral phase shrinks. Reionization is completed when the H II regions overlap, and every point in the intergalactic space gets exposed for the first time to a nearly uniform Lyman-continuum (Lyc) background.

When an isolated point source of ionizing radiation turns on, an ionization (I) front separating the H II and H I regions propagates into the neutral gas, and the proper volume $V_I$ of the ionized zone grows according to the equation

$$\frac{dV_I}{dt} - 3HV_I = \frac{\dot{N}_{\text{ion}}}{\bar{n}_H} - \frac{V_I}{\bar{t}_{\text{rec}}}$$  \hspace{1cm} (3)

(Shapiro & Giroux 1987), where $\dot{N}_{\text{ion}}$ is the number of ionizing photons emitted by the central source per unit time, $\bar{n}_H(0) = 1.7 \times 10^{-7} \left(\Omega_B h^2/0.02\right) \text{ cm}^{-3}$ is today’s mean hydrogen density, and all other symbols have their usual meaning. Most photons travel freely in the ionized gas, and are absorbed in a transition layer. In the case of stellar sources the I-front is quite sharp, and the degree of ionization changes on a short distance of the order of the mean free path for an ionizing photon.

When $\bar{t}_{\text{rec}} \ll t$, the growth of the H II region is slowed down by recombinations in the highly inhomogeneous IGM, and its evolution can be decoupled from the Hubble expansion. Just like in the static case, the ionized bubble then fills its time-varying Strömgren sphere after a few recombination timescales,

$$V_I = \frac{\dot{N}_{\text{ion}} \bar{t}_{\text{rec}}}{\bar{n}_H} \left(1 - e^{-t/\bar{t}_{\text{rec}}} \right).$$  \hspace{1cm} (4)

While the volume that is ionized depends on the luminosity of the central source, the time it takes to produce an ionization-bounded region is only a function of $\bar{t}_{\text{rec}}$.

In the presence of a population of ionizing sources, the transition from a neutral IGM to one that is almost fully ionized can be statistically described by the evolution with redshift of the volume filling factor (or porosity) $Q$ of H II, He II, and He III regions. The radiation emitted by spatially clustered stellar-like and quasar-like sources – the number densities and luminosities of which may change rapidly as a function of redshift – coupled with absorption processes in a medium that becomes more and more clumpy owing to the non-linear collapse of structures (Figure 1), all determine the complex topology of neutral and ionized zones in the Universe (Gnedin 2000; Ciardi et al. 2000; Abel, Norman, & Madau 1999). When $Q \ll 1$ and the radiation sources are randomly distributed, the ionized regions are spatially isolated, every UV photon is absorbed somewhere in the IGM, and the UV radiation field is highly inhomogeneous. As $Q$ grows, the crossing of ionization fronts becomes more and more common, until percolation occurs at $Q = 1$.

Since the mean free path of Lyc radiation is always much smaller than the horizon (this is also true after ‘overlapping’ because of the residual H I still present in the Ly$\alpha$ forest clouds and the Lyman-limit systems), the filling factor of cosmological H II regions is equal at any given time $t$ to the total number of ionizing photons emitted per hydrogen atom by all radiation sources present at earlier epochs, $\int_0^t \dot{n}_{\text{ion}} dt/\bar{n}_H$, minus the total number of radiative recombinations per atom, $\int_0^t Q dt/\bar{t}_{\text{rec}}$. This statement reflects the simple fact that every ultraviolet photon that is emitted is either absorbed by a newly ionized hydrogen atom or by a
Figure 1. Simulating the reionization of the Universe: propagation of an ionization front in a $128^3$ cosmological density field. A ‘mini-quasar’ emitting $5 \times 10^{53}$ ionizing photons s$^{-1}$ was turned on at the densest cell, in a virialized halo of total mass $10^{11} M_{\odot}$. The box length is 2.4 comoving Mpc. The solid contours give the position of the front at 0.15, 0.25, 0.38, and 0.57 Myr after the quasar has switched on at $z = 7$. The underlying greyscale image indicates the initial H I density field. (From Abel et al. 1999.)

recombining one. Differentiating one gets

$$\frac{dQ}{dt} = \frac{\dot{n}_{\text{ion}}}{\bar{n}_H} - \frac{Q}{t_{\text{rec}}}$$  \hspace{1cm} (5)

(Madau, Haardt, & Rees 1999). It is this differential equation – and its equivalent for expanding helium zones – that statistically describes the transition from a neutral Universe to a fully ionized one independently, for a given UV photon emissivity per unit cosmological volume $\dot{n}_{\text{ion}}$, of the complex and possibly short-lived emission histories of individual radiation sources, e.g. on whether their comoving space density is constant or varies with cosmic time. Initially, when the filling factor is $\ll 1$, recombinations can be neglected and the ionized volume increases at a rate fixed solely by the ratio $\dot{n}_{\text{ion}}/\bar{n}_H$. As time goes on and more and more Lyc photons are emitted, radiative recombinations become important and slow down the growth of the ionized volume, until $Q$ reaches unity, the recombination term saturates, and reionization is finally completed (except for the high density regions far from any source which are only gradually eaten away, Miralda-Escudé, Haehnelt, & Rees 2000). In the limit of a fast recombining IGM ($t_{\text{rec}} \ll t$), one can neglect the derivative on the left-hand side of equation (5) and derive

$$Q \lesssim \frac{\dot{n}_{\text{ion}}}{\bar{n}_H} t_{\text{rec}},$$  \hspace{1cm} (6)

i.e. the volume filling factor of ionized bubbles must be less (or equal) to the number of Lyc photons emitted per hydrogen atom in one recombination time. In other
words, because of radiative recombinations, only a fraction $\bar{t}_{\text{rec}}/t \ll 1$ of the photons emitted above 1 ryd is actually used to ionize new IGM material. The Universe is completely reionized when

$$\dot{n}_{\text{ion}} \bar{t}_{\text{rec}} \gtrsim \bar{n}_{\text{H}},$$

i.e. when emission rate of ultraviolet photons exceeds the mean rate of recombinations.

(c) A clumpy Universe

The simplest way to treat reionization in an inhomogeneous medium is in terms of a clumping factor that increases the effective gas recombination rate. In this case the volume-averaged recombination time is

$$\bar{t}_{\text{rec}} = [(1 + 2\chi)n_{\rho}\alpha_{B}C]^{-1} = 0.06 \text{ Gyr} \left(\frac{\Omega_{B}h^{2}}{0.02}\right)^{-1} \left(\frac{1 + z}{10}\right)^{-3} \frac{\bar{n}_{\text{H}}}{\bar{n}_{\rho}} C_{10}^{-1},$$

where $\alpha_{B}$ is the recombination coefficient to the excited states of hydrogen (at an assumed gas temperature of $10^{4}$ K), $\chi$ the helium to hydrogen abundance ratio, and the factor $C \equiv \langle n_{\rho}^{2}\rangle/\bar{n}_{\rho}^{2} > 1$ takes into account the degree of clumpiness of photoionized regions (hereafter $C_{10} \equiv C/10$). If ionized gas with density $n_{\rho}$ filled uniformly a fraction $1/C$ of the available volume, the rest being empty space, the mean square density would be $\langle n_{\rho}^{2}\rangle = n_{\rho}^{2}/C = \bar{n}_{\rho}^{2}C$. More in general, if $f_{m}$ is the fraction of baryonic mass in photoionized gas at an overdensity $\delta$ relative to the mean, and the remaining (underdense) medium is distributed uniformly, then the fractional volume occupied by the denser component is

$$f_{v} = f_{m}/\delta,$$

the density of the diffuse component is

$$\bar{n}_{\rho} = \frac{1 - f_{m}}{1 - f_{v}},$$

and the recombination rate is larger than that of a homogeneous Universe by the factor

$$C = f_{m}\delta + \frac{(1 - f_{m})^{2}}{1 - f_{v}}$$

(e.g. Chiu & Ostriker 1999; Valageas & Silk 1999). It is difficult to estimate the clumping factor accurately. According to hydrodynamics simulations of structure formation in the IGM (within the framework of CDM-dominated cosmologies), Lyα forest clouds with moderate overdensities, $5 \lesssim \delta \lesssim 10$, occupy a fraction of the available volume which is too small for them to dominate the clumping at high redshifts (e.g. Zhang et al. 1998; Theuns et al. 1998). In hierarchical clustering models, it is the virialized gas (with $\delta \approx 180$ if one ignores the slope of the density profile) in dark matter halos with temperatures $\lesssim 10^{4}$ K (masses $M \lesssim 10^{7} h^{-1} M_{\odot}$) which will plausibly boost the recombination rate by large factors as soon as the collapsed mass fraction exceeds 0.5%. Halos or halo cores which are dense and thick enough to be self-shielded from UV radiation will stay neutral and will not contribute to the recombination rate. This is also true of gas in more massive
Reionization

halos, which will be virialized to higher temperatures and ionized by collisions with thermal electrons. With a large comoving space density at \( z = 9 \) of \( \frac{dn}{d\ln M} \sim 1000 \ h^3 \text{Mpc}^{-3} \), corresponding to a mean proper distance of only \( \sim 6 \ h^{-1} \text{kpc} \), and to a mass fraction of 0.04, halos with \( T_v \approx 10^4 \text{K} \) will contribute significantly, \( f_{m\delta} \approx 7 \), to the clumping. Recent calculations by Benson et al. (2000), which instead include all halos with \( T_v > 10^4 \text{K} \) and adopt an isothermal density profile with a flat core, give \( C \approx 30 \) already at \( z = 9 \). Because of finite resolution effects, numerical simulations may underestimate clumping: in those of Gnedin & Ostriker (1997), for example, \( C \) rises above unity at \( z \gtrsim 20 \), and grows to \( C \sim 10 \) (40) at \( z \approx 9 \) (5).

It is important to note that the use of the volume-averaged clumping factor in the recombination timescale is only justified when the size of the \( \text{H} \text{II} \) regions is much larger compared to the scale of the clumping, so that the effect of many halos within the ionized volume can be averaged over. This will be a good approximation either at late epochs, when the \( \text{H} \text{II} \) zones have had time to grow (or when overlapping ionized regions from an ensemble of sources are able to proper sample the small-scale density fluctuations), or at earlier epochs if the ionized bubbles are produced by more luminous sources like quasars or the stars within halos collapsing from high-\( \sigma \) peaks. As mentioned above, the mean free path between halos having \( T_v \approx 10^4 \text{K} \) is \( \lambda \sim 6 \ h^{-1} \text{kpc} \) at \( z = 9 \), but their virial radius is only \( r_v \approx 0.4 \ h^{-1} \text{kpc} \). It is only on scales greater than \( \lambda^3/r_v^2 \approx 2 \ h^{-1} \text{Mpc} \) that the clumping can then be averaged over, and the covering factor of halos within the Strömgren sphere exceeds unity.

3. Sources of UV photons

(a) Quasars

In recent years, several optical surveys (Warren, Hewett, & Osmer 1994; Schmidt, Schneider, & Gunn 1995; Kennefick, Djorgovski, & de Carvalho 1995) have consistently provided evidence for a turnover in the QSO counts. The space density of radio-loud quasars also appears to decrease strongly for \( z > 3 \) (Shaver et al. 1996), suggesting that the turnover is indeed real and not an effect on optically-selected QSOs induced by dust along the line of sight. The density of optically bright and flat-spectrum radio-loud quasars has a relatively flat maximum at \( 1.8 \lesssim z \lesssim 2.8 \), and declines gradually at higher redshifts (Figure 2).

The QSO emission rate of hydrogen Lyc photons per unit comoving volume, \( \dot{N}_Q \), is also shown in Figure 2. The procedure adopted to derive this quantity implies a large correction for incompleteness at high-\( z \). With a fit to the quasar luminosity function (LF) which goes as \( \phi(L) \propto L^{-\beta} \), with \( \beta = 1.64 \) at the faint end (Pei 1995), the contribution to the emissivity converges rather slowly, as \( L^{0.36} \). At \( z = 4 \), for example, the blue magnitude at the break of the LF is \( M_* \approx -25.4 \), comparable or slightly fainter than the limit of current high-\( z \) QSO surveys. While a large fraction, about 90\% at \( z = 4 \) and even higher at earlier epochs, of the ionizing emissivity shown in the figure is therefore produced by quasars that have not been actually observed, and are assumed to be present based on an extrapolation from lower redshifts, it is also fair to ask whether an excess of low-luminosity QSOs, relative to the best-fit LF, could actually boost the estimated Lyc emissivity at early epochs. The interest in models where the quasar LF significantly steepens...
Figure 2. **Left**: comoving space density of bright QSOs as a function of redshift. The data points with error bars are taken from different optical and radio surveys (see Madau, Haardt, & Rees 1999 for details). **Right**: comoving emission rate of hydrogen Lyc photons (solid line) from QSOs, compared to the comoving rate of recombinations, $n_{HI}(0)/\dot{n}_{rec}$ (dashed lines) in an IGM with gas clumping factor $C = 20, 30, 40$). An EdS cosmology with $\Omega_B h^2 = 0.02$ and $h = 0.5$ has been assumed. Models based on photoionization by quasar sources appear to fall short at $z \approx 5$. The data points show the estimated contribution from Lyman-break galaxies at $z \approx 3$ and $4$, assuming that the fraction of Lyc photons which escapes the dense H I layers into the galaxy halos and the IGM is 50%.

with lookback time, and therefore predict many more QSOs at faint magnitudes than the extrapolation of Pei’s (1995) fitting functions, stems from recent claims of a strong linear correlation between bulge and observed black hole masses (Magorrian et al. 1998), linked to the steep mass function of dark matter haloes predicted by hierarchical cosmogonies (e.g. Haehnelt, Natarajan, & Rees 1998; Haiman & Loeb 1998). As discussed by Haiman, Madau, & Loeb (1999), the space density of low-luminosity quasars at high-$z$ is constrained by the observed lack of red, unresolved faint objects in the Hubble Deep Field (HDF). Down to a 50% completeness limit of $V_{AB} = 29.6$ ($I_{AB} = 28.6$), no $z > 4$ quasar candidates have actually been found by Conti et al. (1999); by contrast, about 10 objects would be predicted by a QSO evolution model characterized by a steep LF with slope $\beta = 2$ and a comoving space density that remains constant above $z = 2.5$ instead of dropping (Figure 3), and chosen to boost the emission rate of ultraviolet photons at $z \sim 5$ by a factor of 5. A large population of faint AGNs at high-$z$ would still be consistent with the data if, at these faint magnitude levels and high image resolution, the host galaxies of active nuclei could actually be resolved by the Hubble Space Telescope.

**(b) Star-forming galaxies**

Galaxies with ongoing star-formation are another obvious source of Lyc photons. The recent progress in our understanding of faint galaxy data made possible by the identification of star-forming galaxies at $2 \lesssim z \lesssim 4$ in ground-based surveys and in the HDF has provided new clues to the long-standing issue of whether galaxies
Figure 3. Theoretical number-magnitude relation of quasars in the redshift range $4.0 < z < 5.5$. The **solid line** shows the prediction for a ‘standard’ QSO model, one in which the faint end of the QSO luminosity function has slope $\beta = 1.64$ and tracks the turnover observed in the space density of bright quasars at $z \gtrsim 3$. The **dashed line** shows the increased number of sources expected in the case of a steeper, $\beta = 2$, luminosity function and a comoving space density that stays constant above $z = 2.5$. The latter evolution scenario provides, within the errors, enough UV photons to keep the Universe ionized at $z \approx 5$, but appears to be inconsistent with the lack of red, faint stellar objects observed in the Hubble Deep Field.

at high redshifts can provide a significant contribution to the ionizing background flux. Since the rest-frame UV continuum at 1500 Å (redshifted into the visible band for a source at $z \approx 3$) is dominated by the same short-lived, massive stars which are responsible for the emission of photons shortward of the Lyman edge, the needed conversion factor, about one Lyc photon every 10 photons at 1500 Å, is fairly insensitive to the assumed IMF and is independent of the galaxy history for $t > 10^{7.3}$ yr.

Composite ultraviolet luminosity functions of Lyman-break galaxies (LBG) at $z \approx 3$ and $z \approx 4$ have been recently derived by Steidel et al. (1999). They are based on a large catalog of spectroscopically and photometrically selected galaxies from the ground-based and HDF samples, and span about a factor of 40 in luminosity from the faint to the bright end. Integrating these LF over all luminosities $L > 0.1 L^*$, and using the conversion $L(1500)/L(912) \approx 6$ valid for a Salpeter mass function and constant star formation rate, we derive for the comoving emissivities at 1 ryd the values of $9 \pm 2 \times 10^{25} h \text{ ergs s}^{-1} \text{ Hz}^{-1} \text{ Mpc}^{-3}$ at $z \approx 3$, and $7 \pm 2 \times 10^{25} h \text{ ergs s}^{-1} \text{ Hz}^{-1} \text{ Mpc}^{-3}$ at $z \approx 4$, about 4 times higher than the estimated quasar contribution at $z = 3$. These numbers do not include any correction for local H i absorption (since the color excess $E_{912-1500}$ is expected to be small, dust extinction can probably be neglected in correcting from observed rest-frame far-
UV to the Lyman edge. The data points plotted in Figure 2 assumes a value of \( f_{\text{esc}} = 0.5 \) for the unknown fraction of Lyc photons which escapes the dense sites of star formation (not included in our clumping factor) into the halos and the intergalactic space. Note that, at \( z = 3 \), Lyman-break galaxies radiate more ionizing photons than QSOs for \( f_{\text{esc}} \gtrsim 25\% \).

4. Implications

(a) First light

We have seen in the previous sections that, in the approximation the clumping can be averaged over, only the photons emitted within one recombination timescale can actually be used to ionize new material. As \( t_{\text{rec}} \ll t \) at high redshifts, it is possible to compute using equation (7) a critical value for the photon emission rate per unit cosmological comoving volume at a given epoch, \( N_c \), independently of the (unknown) previous emission history of the Universe: only rates above this value will provide enough UV photons to keep the IGM ionized at that epoch. Equation (7) can then be rewritten as

\[
N_c(z) = \frac{n_H(0)}{t_{\text{rec}}(z)} = (10^{51.4} \text{ s}^{-1} \text{ Mpc}^{-3}) C_{10} \left( \frac{1 + z_{10}}{10} \right)^3 \left( \frac{\Omega_B h^2}{0.02} \right)^2. \tag{12}
\]

The uncertainty on this value is difficult to estimate, as it depends on the clumping factor and the nucleosynthesis constrained baryon density. It is interesting to convert this rate into a ‘minimum’ star formation rate per unit (comoving) volume, \( \dot{\rho}_* \) (for \( \Omega_B h^2 = 0.02 \)):

\[
\dot{\rho}_* \approx \frac{N_c \times 10^{-53.1}}{f_{\text{esc}}} \approx (0.12 \text{ M}_\odot \text{ yr}^{-1} \text{ Mpc}^{-3}) \left( \frac{0.5}{f_{\text{esc}}} \right) C_{10} \left( \frac{1 + z_{10}}{10} \right)^3. \tag{13}
\]

(The conversion factor can be understood by noting that, for each 1 M\(_\odot\) of stars formed, 8% goes into massive stars with \( M > 20 M_\odot \) that dominate the Lyc luminosity of a stellar population. At the end of the C-burning phase, roughly half of the initial mass is converted into helium and carbon, with a mass fraction released as radiation of 0.007. About 25% of the energy radiated away goes into Lyc photons of mean energy 20 eV. For each 1 M\(_\odot\) of stars formed every year, we then expect 0.08 \times 0.5 \times 0.007 \times 0.25 \times M_\odot c^2/20 \text{ eV yr} \sim 10^{53} \text{ photons s}^{-1} \text{ to be emitted shortward of 1 ryd}.)

Taken at face value, equations (12) and (13) have perhaps a surprising implication. In a inhomogeneous Universe, early reionization at \( z \sim 9 \) requires an ionizing emissivity which is comparable or larger than that radiated by QSOs at the peak of their activity, \( z \approx 3 \). In a similar manner, photoionization by massive stars can only play a role if the star formation density at this epoch were significantly larger than the value directly ‘observed’ (i.e. uncorrected for dust reddening) at \( z = 2 \) (Madau, Pozzetti, & Dickinson 1998).

(b) Delayed He II reionization

Because of its higher ionization potential and the steep spectra of UV radiation sources, the most abundant (by a factor \( \sim 100 \)) absorbing ion in the post-reionization Universe is not H i but He ii. The importance of intergalactic helium
Figure 4. The evolution of the He \textsc{iii} filling factor as a function of redshift in an inhomogeneous Universe where photoionization is dominated by QSOs turning over at $z \gtrsim 3$. From right to left, the three curves assume a constant clumping factor of $C = 10, 20, \text{ and } 30$. The QSO photon spectrum is assumed to vary as $\nu^{-2.8}$ shortward of the hydrogen Lyman edge. Note how the ionization of He \textsc{ii} is never completed before $z = 3$ in models with $C \geq 10$.

In the context of this study stems from the possibility of detecting the effect of ‘incomplete’ He \textsc{ii} reionization in the spectra of $z \sim 3$ quasars as, depending on the clumpiness of the IGM (Madau & Meiksin 1994), the photoionization of singly ionized helium may be delayed until much later than for H \textsc{i}.

Since H \textsc{i} and He \textsc{i} do not absorb a significant fraction of $h\nu > 54.4$ eV photons, the problem of He \textsc{ii} reionization can be decoupled from that of other ionizations, and the equivalent of equation (5) for expanding He \textsc{iii} regions becomes

$$\frac{dQ}{dt} = \frac{\dot{n}_{\text{ion4}}}{\bar{n}_{\text{He}}} - \frac{Q}{\bar{t}_{\text{HeIII}}},$$

where $\dot{n}_{\text{ion4}}$ now includes only photons above 4 ryd, and $\bar{t}_{\text{HeIII}}$ is 6.5 times shorter than the hydrogen recombination timescale if ionized hydrogen and doubly ionized helium have similar clumping factors. It is interesting to note that, if the intrinsic photon spectrum of ionizing sources has slope $\dot{n}(\nu) \propto \nu^{-2.8}$, the first terms on

\[\dagger\] This last assumption appears, however, rather dubious: the reason is that self-shielding of He \textsc{ii} Lyc radiation occurs at much lower hydrogen columns than self-shielding of photons at 1 ryd (by about a factor of S/2, where the spectral ‘softness’ S is the the ratio of the radiation flux at the hydrogen Lyman edge to the flux at 4 ryd), and self-shielded gas will remain neutral and not add to the recombination rate. Ionized hydrogen may then be more clumpy than doubly ionized helium.

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the right-hand side of equations (5) and (14) are actually equal, and a significant
delay between the complete overlapping of H II and He III regions can only arise
if recombinations are important. This effect is illustrated in Figure 4, where the
expected evolution of the He III filling factor (obtained by numerical integration
of eq. 14) is plotted for a QSO-photoionization model with a source decline at
high redshifts: He II reionization is never completed before z = 3 in models with
C $\gtrsim$ 10. A significant contribution to the UV background at 4 ryd from massive
stars, which could push the helium reionization epoch to higher redshifts, has been
traditionally ruled out on the basis that the ratio between the number of He II and
H I Ly photons emitted from low-metallicity starbursts is only about two percent
(Leitherer & Heckman 1995), five times smaller than in typical QSO spectra. It has
been recently pointed out by Tumlinson & Shull (2000), however, that metal-free
stars exhibit higher effective temperatures and dramatically harder stellar spectra,
particularly in the He II continuum. This enhanced He-ionizing capabilities of Pop
III stars could have interesting implications for reionization.

To date, various studies of the HeII Ly$\alpha$ forest in the spectra of distant QSOs
(Hogan, Anderson, & Rugers 1997; Reimers et al. 1997; Heap et al. 2000) have
revealed patchy absorption with low He II opacity ‘voids’ alternating several Mpc
sized regions with vanishing flux. These observations suggest that helium absorption
does not increase smoothly with lookback time, but rather in the abrupt manner
expected in the final stages of inhomogeneous reionization by quasar sources. Ra-
diative transfer effects during He II reionization could affect the thermal history
of the IGM (Abel & Haehnelt 1999, Efstathiou, this volume). Here it is impor-
tant to remark that, while delayed He II reionization in a clumpy Universe appears
to be naturally linked to the observed decline in the space density of quasars be-
yond z $\sim$ 3, the complete overlapping of He III regions occurs instead much earlier
(z $\gg$ 5) in models that predict many more faint QSOs at high redshifts (Haiman
& Loeb 1998).

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References
Abel, T., & Haehnelt, M. G. 1999, ApJ, 520, L13
Abel, T., Norman, M. L., & Madau, P. 1999, ApJ, 523, 66
Benson, A. J., Nusser, A., Sugiyama, N., & Lacey, C. G. 2000, MNRAS, submitted
Cen, R., Miralda-Escudé, J., Ostriker, J. P., & Rauch, M. 1994, ApJ, 437, L9
Chiu, W. A., & Ostriker, J. P. 1999, ApJ, submitted
Ciardi, B., Ferrara, A., Governato, F., Jenkins, A. 2000, MNRAS, in press
Conti, A., Kennefick, J. D., Martini, P., & Osmer, P. S. 1999, AJ, 117, 645
Gnedin, N. Y. 2000, ApJ, in press
Gnedin, N. Y., & Ostriker, J. P. 1997, ApJ, 486, 581
Haehnelt, M. G., Natarajan, P., & Rees, M. J. 1998, MNRAS, 300, 817
Haiman, Z., & Loeb, A. 1998, ApJ, 503, 505
Haiman, Z., Madau, P., & Loeb, A. 1999, ApJ, 514, 535
Heap, S. R., et al. 2000, ApJ, in press
Hernquist, L., Katz, N., Weinberg, D. H., & Miralda-Escudé, J. 1996, ApJ, 457, L51
Hogan, C. J., Anderson, S. F., & Rugers, M. H. 1997, AJ, 113, 1495
Kennefick, J. D., Djorgovski, S. G., & de Carvalho, R. R. 1995, AJ, 110, 2553
Leitherer, C., & Heckman, T. M. 1995, ApJS, 96, 9
Mac Low, M.-M., & Ferrara, A. 1999, ApJ, 513, 142
Madau, P., Haardt, F., & Rees, M. J. 1999, ApJ, 514, 648
Madau, P., & Meiksin, A. 1994, ApJ, 433, L53
Madau, P., Pozzetti, L., & Dickinson, M. E. 1998, ApJ, 498, 106
Magorrian, J., et al. 1998, AJ, 115, 2285
Miralda-Escudé, Haehnelt, & Rees 2000, ApJ, 530, 1
Pei, Y. C. 1995, ApJ, 438, 623
Reimers, D., Köhler, S., Wisotzki, L., Groote, D., Rodriguez-Pascual, P., & Wamsteker, W. 1997, A&A, 327, 890
Schmidt, M., Schneider, D. P., & Gunn, J. E. 1995, AJ, 110, 68
Shapiro, P. R., & Giroux, M. L. 1987, ApJ, 321, L107
Shaver, P. A., Wall, J. V., Kellerman, K. I., Jackson, C. A., & Hawkins, M. R. S. 1996, Nature, 384, 439
Steidel, C. C., Adelberger, K. L., Giavalisco, M., Dickinson, M., & Pettini, M. 1999, ApJ, 519, 1
Tegmark, M., Silk, J., & Evrard, A. 1993, ApJ, 417, 54
Theuns, T., Leonard, A., Efstathiou, G., Pearce, F. R., & Thomas, P. A. 1998, MNRAS, 301, 478
Tumlinson, J., & Shull, J. M. 2000, ApJ, 528, 65
Valageas, P., & Silk, J. 1999, A&A, 347, 1
Voit, G. M. 1996, ApJ, 465, 548
Warren, S. J., Hewett, P. C., & Osmer, P. S. 1994, ApJ, 421, 412
Zhang, Y., Anninos, P., & Norman, M. L. 1995, ApJ, 453, L57
Zhang, Y., Meiksin, A., Anninos, P., & Norman, M. L. 1998, ApJ, 495, 63