Surface stress of graphene layers supported on soft substrate

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We obtain the surface stress of a single layer and multilayers of graphene supported on silicone substrates by measuring the deformation of the graphene-covered substrates induced by the surface tension of liquid droplets together with the Neumann’s triangle concept. We find that the surface stress of the graphene-covered substrate is significantly larger than that of the bare substrate, and it increases with increasing graphene layers, and finally reaches a constant value of about 120 mN/m on three and more layers of graphene. This work demonstrates that the apparent surface stress of graphene-substrate systems can be tuned by the substrate and the graphene layers. The surface stress and the tuning effect of the substrate on it may have applications in design and characterization of graphene-based ultra-sensitive sensors and other devices. Moreover, the method may also be used to measure the surface stress of other ultrathin films supported on soft substrates.

Surface stress of solids, which connects the macroscopic properties of solids and the chemical bonding state at a surface or an interface¹–³, plays an important role in many surface phenomena such as elastic moduli of nanoscale materials⁴–⁶, surface reconstruction of metals⁷,⁸, shape transitions of nanoparticles⁹, surface diffusion, epitaxial growth¹⁰, self-assembled domain patterns¹¹, deformation of nanoporous materials¹²,¹³, bending of layered cantilevers¹⁴,¹⁵, contacts of soft matters¹⁶, and stiffening of solids by surface stress¹⁷,¹⁸. Another important surface property is surface energy, and the relation between surface stress and surface energy is elaborated in many papers²,³,⁴. Graphene is a typical two-dimensional or surface material¹⁹,²⁰. In many applications, graphene layers are supported on a substrate²¹, such as graphene-based electrodes²²,²³, solar cells²⁴, and artificial actuators²⁵. Thus, the surface properties of graphene layers and the effect of the underlying substrates on their surface properties have significant implications in design of graphene-based devices, and thus attracted much attention²⁶–³⁰. For example, graphene layers supported on soft substrates, by converting the deformation of the layered system under lateral loading into electronic signals, can make ultra-sensitive flexible tactile sensors attaining the lowest human pressure perception³¹–³³. Surface stress and interface stress can be principal factors in determining the deformation of nanoscale films and multilayers³⁴,³⁵,³⁶, and thus, control of their effect is regarded as “the core of design and construction of ultra-sensitive mechanical sensors”³⁷. Mechanical deformation also affects the electronic structure of graphene³⁸,³⁹. However, to our knowledge, there is no report about the apparent surface stress of graphene supported on substrates. Moreover, graphene is the thinnest material ever found⁴⁰. When combining it with a substrate, one may study the relative contribution of the atomic layers of the substrate beneath the thin membrane to the apparent surface stress of the membrane-substrate composite system.

Nevertheless, the effects of surface stresses are not notable in normal conditions, and therefore, direct experimental measurement of the value of surface stress of solids has remained a challenge for a long time. The reported surface stress of solids is mostly based on theoretical calculations³⁵. The available surface stress that has been obtained from experiments is confined to soft polymers, such as silicone³⁶,⁴⁰,⁴¹, which has an elasto-capillary length γ/E of several tens of microns, where γ is the surface stress and E is the Young’s modulus of the solid⁴². Recent research reveals that, when a liquid droplet contacts a soft elastic substrate, a deformed microscopic region will emerge at the vicinity of the contact line, and the shape of this region can be used to calculate the surface stress directly⁴⁰,⁴¹.

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Results
Deformation influenced by graphene. In this Article, we investigate the apparent surface stress of graphene supported on silicone substrates (Fig. 1), by extending the method recently developed by Style et al.\textsuperscript{40}, who measured the surface stress of pure silicone based on the deformation of the substrate induced by a liquid droplet. Here, graphene layers were supported on two kinds of soft silicone, i.e., one type of polydimethylsiloxane with a high softness (PDMS) and another type of highly elastic silicone gel of CY52-276A/B (CY52-276) (See Methods for details). Two kinds of liquid, i.e., glycerol and liquid paraffin, were used to induce the deformation of the substrates by the surface tension (Fig. 1a) (Supplementary information). We embedded fluorescent beads on the surface of the soft silicone substrate to trace the deformation. Figure 1b shows the positions of the embedded fluorescent beads located on the surface of a silicone substrate of PDMS that is covered by one layer of graphene and deformed by a glycerol droplet, where the surface profile can be obtained by extracting the centre of each fluorescent bead\textsuperscript{40,43}. Figure 2(a,b) show the extracted surface profiles of bare and one layer graphene-covered PDMS substrates of different thicknesses under glycerol droplets (See Supplementary information for the results of liquid paraffin). The height of the profile is determined by the vertical component of the liquid surface tension\textsuperscript{43–45}. When focusing on the profile of the contact line region in Fig. 2(a,b), and, in particular, the close-up of this region in Fig. 2(c,d), we find that for a given substrate and liquid, all the scattered points collapse into a cusp region, as discovered for pure silicone substrates\textsuperscript{40}, irrespective of the substrate thickness and the existence of graphene. Theoretically, the thickness only influences the deformation of the substrate that is many micrometers away from the contact line, and does not influence the angle of the cusp which can be determined from a region near the contact line. Using the method of Style et al.\textsuperscript{40}, we can calculate the angle of the cusp. Both of the two types of liquids cause a larger cusp angle on the graphene-covered substrate than that on the bare counterpart (Supplementary information). For example, the cusp angle of the bare PDMS substrate caused by a glycerol droplet is $94.9^\circ \pm 2.4^\circ$, whereas that of the substrate covered by one layer of graphene increases to $124.0^\circ \pm 0.3^\circ$.

Model of deformation with graphene membrane coverage. The similar deformation profiles and cusp shapes caused by liquid droplets near the contact lines on the bare and graphene-covered substrates imply that the same rule governs the deformation. Because graphene is the stiffest material ever found\textsuperscript{46,47}, the increase in the cusp angle of the graphene-covered substrate may be a consequence of the joint effect of the mechanical reinforcement of graphene and the surface stress. Therefore, we generalize the model of Jerison et al.\textsuperscript{43} for a pure substrate to a substrate covered by a graphene membrane to single out the effect of the surface stress (schema shown in Fig. 3a). As the deformation caused by a liquid droplet is significantly smaller than the contact radius of the droplet on the substrate, we employ a two-dimensional elasticity model to analyze the substrate deformation\textsuperscript{43}. Introduce the Airy stress function $\phi$ that satisfies the biharmonic equation:

$$\nabla^2 \phi = \left( \frac{\partial^2 \phi}{\partial r^2} + \frac{\partial^2 \phi}{\partial z^2} \right) \left( \frac{\partial^2 \phi}{\partial r^2} + \frac{\partial^2 \phi}{\partial z^2} \right) \phi = 0$$

(1)

where $r$ and $z$ represent the radial and vertical coordinates from the position of the contact line on the surface of the substrate, respectively. The stress and strain of the substrate can be found in ref. 48. Graphene is modeled...
as a membrane for its thickness is ultra-small compared to other length scales of the system. The deformation of graphene can be described by

$$\frac{E_g h_g}{1 - \nu_g^2} \frac{\partial^2 u(r)}{\partial r^2} = -q(r)$$

(2)

where $u(r)$ is the displacement in the horizontal direction; $q(r)$ is the interface stress between graphene and the substrate; $E_g$, $h_g$, and $\nu_g$ are the Young’s modulus, the thickness, and the Poisson’s ratio of graphene, respectively. Using the continuity conditions of the displacements and stresses at the interface of graphene and the substrate, this problem can be solved analytically based on the Fourier transform procedure (Supplementary information and ref. 48). Figure 3b displays the profiles of the deformed surfaces calculated from the above theory. Without considering the surface stress of the solid, the displacement is singular at the contact line no matter how stiff the membrane is, as characterized by the classical Boussinesq solution. Thus, the mechanical reinforcement of the graphene membrane shows little effect on the deformation pattern.

Figure 2. Surface profiles near the contact line. (a,b) are the deformation profiles induced by a glycerol droplet on a bare silicone substrate of PDMS and a substrate covered by one layer of graphene (1LG), respectively. The cusp regions of the substrates with different thicknesses (shown in different colours) are aligned to the origin point ($z=0$). (c,d) are the close-ups of the cusp regions in (a,b), with the dashed lines showing the extracted cusp angles.
Surface stress of substrate covered by one layer of graphene. Following the method developed in ref. 40, which is based on the Neumann's triangle concept that the surface stress of the solid, the interface stress between the liquid and solid, and the surface tension of the liquid are in equilibrium at the contact point, we extract the surface/interface stress through

\[
\gamma_{s} = \frac{1}{2} \left( \sin \frac{\varphi}{2} \cos \frac{\varphi}{2} + \cos \frac{\varphi}{2} \right) \gamma_{l}
\]

\[
\gamma_{d} = \frac{1}{2} \left( \sin \frac{\varphi}{2} \cos \frac{\varphi}{2} - \cos \frac{\varphi}{2} \right) \gamma_{l}
\]

where \(\gamma_{s}\) is the interface stress between the liquid and solid; \(\gamma_{l}\) is the liquid surface tension; \(\theta\) is the cusp angle; and \(\varphi\) is the contact angle (Supplementary information). The surface stress of pristine CY52-276 that is obtained with glycerol is 42.8 \(\pm\) 1.4 mN/m, which is close to the value 42 mN/m measured by Park et al.\textsuperscript{41}. The values of the surface stress of the pristine PDMS that are obtained with glycerol and liquid paraffin are 34.1 \(\pm\) 1.6 mN/m and 31.8 \(\pm\) 1.2 mN/m, respectively, in good agreement with each other. The surface stress of one layer graphene-covered PDMS which is obtained with glycerol is 58.4 \(\pm\) 1.1 mN/m, whereas that obtained with liquid paraffin is 60.6 \(\pm\) 3.1 mN/m. These values are consistent, and significantly larger than the value of the corresponding bare substrate.

Model of deformation with surface stress of solid. We use the extracted surface stress in the model developed above to describe the deformation profile. Assuming \(\gamma_{s} = \gamma_{d}\), the linearized tensile stress \(\sigma_{zz}(r,0)\) in the vertical direction can be related to the vertical deformation \(v(r,0)\) as\textsuperscript{43,44}

\[
\sigma_{zz}(r,0) = \gamma_{l} \frac{\partial^2 v(r,0)}{\partial r^2}
\]

This problem can be solved analytically (Supplementary information). Figure 4 shows the profiles of the deformed surfaces calculated from the above theory including the surface stress. The singularity of the
displacement at the contact line is removed when considering the effect of the surface stress (Fig. 4a), as for pure silicone. The theory also gives a region near the contact line whose profile can be fitted by a cusp with an open angle (the insert of Fig. 4a). Figure 4b displays the measured deformation profile induced by a glycerol droplet standing on a substrate covered by one layer of graphene (scattered black dots), and the analytical solutions with (red line) and without (green line) the surface stress. The theoretical model incorporating the measured surface stress provides a good quantitative description of the out-of-plane deformation of the graphene-covered substrate, as found for pure substrates.

Surface stress of single layer graphene and multilayer graphene supported on substrate. The single layer graphene we used above is polycrystal at the millimeter scale and it contains grain boundaries. Using the same method, we measure the surface stress of a centimeter-sized single crystal of a single layer of graphene. Shown in Fig. 5, the surface stress of the single crystal graphene supported on PDMS is $57.9 \pm 3.2 \text{ mN/m}$, which is very close to $58.4 \pm 1.1 \text{ mN/m}$ of the polycrystal graphene. This behaviour is similar to the finding that the stiffness of polycrystal graphene is close to that of single crystal graphene.

Next, we study the surface stress of multilayer graphene supported on a substrate. Here multilayers are obtained by two methods. The first one is the widely used layer-by-layer transfer method, which can precisely control the layers of graphene and is referred to as “stacked” graphene in Fig. 5. The second method is direct transfer of grown multilayer graphene (referred to as “grown” in Fig. 5), which would guarantee the standard Bernal stacking of graphene. The interface stresses at the graphene-silicone interface and between the graphene layers are found well below the interface strengths. Thus, the graphene layers will neither separate from the substrate, nor from each other, in the experiments. Figure 5 shows the extracted surface stress of substrates covered by different numbers of layers of graphene. The surface stress of the stacked multilayer graphene supported on PDMS is comparable with that of the grown multilayer graphene for the cases of two layers and 3~5 layers. Increasing graphene layers enhances the surface stress, and finally the surface stress reaches an asymptotic value when the substrate is covered by three layers of graphene. The surface stress of multilayer graphene is thickness-dependent, which is similar to the surface energy of graphene that is related to the substrate and thickness. The asymptotic values of the surface stress of the multilayer graphene supported on PDMS and CY52-276 are consistent and are about $120 \text{ mN/m}$ measured with glycerol.

Discussion
In this study, we extracted the surface stress using the method developed in ref. 40 which assumes that the cusp orientation is symmetric and perpendicular to the surface of the substrate. Recently, by using the X-ray...
microscopy, Park et al. found that, in general, the cusp induced by the surface stress at the three-phase contact line may be bent to form an asymmetric tip. Based on the geometry of the cusp measured by X-ray microscopy, Park et al. found that the surface stress of CY52-276 is 42 mN/m, which is close to the value 42.8 ± 1.4 mN/m we obtained with glycerol. On the other hand, Park et al. pointed out that for systems with γ ≈ γ (that is, φ ≈ 90°), the cusp profile is approximately symmetric, except its tip. Thus, the model of Style et al. may provide a reasonably accurate prediction for the solid surface stress when the contact angle is close to 90°. In our experiments, the graphene-covered substrates have a much stronger resistance to the applied liquid surface tension than bare silicone. The contact angle of glycerol on these substrates is very close to 90° (about 98°, Supplementary information). Therefore, the model of Style et al. can be used to extract the surface stress of the graphene-covered substrates, and the values of the surface stress of the graphene-covered substrates we obtained with glycerol droplets can be deemed to be reasonably accurate. However, the applicability of the experiment and the model is based on the condition that the layered system can support the applied force while still keeping the interface well bonded, which is true in this study. If the interface bonding is very weak such that debonding or sliding takes place under the action of the droplet, the experiment and the model will not be applicable.

The surface stress reaches a constant value on three and more layers of graphene because the surface stress is mainly contributed by the three atomic layers near the surface, which constitutes a direct experimental confirmation of the general theoretical result that the contribution to the surface stress is mainly from the surface atomic layer and two layers under it. Nevertheless, the increase of the surface stress with increasing layers of graphene on the substrate demonstrates that the substrate plays an important role.

In conclusion, by measuring the deformation of substrates induced by the surface tension of liquid droplets, we find that the graphene-covered soft substrates have similar deformation profiles to that of the bare substrate, while the deformation magnitude is significantly reduced. The theoretical model that includes the effect of surface stress can remove the singularity of the deformation and thus agrees with the experimental measurement. Based on the Neumann’s triangle concept, we extract the surface stress of bare and graphene-covered substrates. The apparent surface stress of one layer graphene supported on the silicone substrate (PDMS) is 58.4 ± 1.1 mN/m, measured with glycerol, and is 60.6 ± 3.1 mN/m obtained with liquid paraffin. This apparent surface stress increases with the number of the graphene layers, and eventually reaches a value of ~120 mN/m on three and more layers of graphene. The results reveal that the contribution to the surface stress of multilayer graphene is mainly from the three layers in the vicinity of the surface. This work provides a basic parameter of supported multilayer graphene, which is the commonly used structure in graphene-based devices. The method may also be used to measure the surface stress of other ultrathin films supported on soft substrates.

Methods

Fabrication of silicone substrate. Two kinds of soft silicone, i.e., polydimethylsiloxane (PDMS, Sylgard 184, Dow Corning) and CY52-276 (Dow Corning), were used in our experiments. The soft PDMS samples were prepared by spin-coating the oligomer with a base-curing ratio 75:1 on clean smooth glass slides for 1 min at different speeds (1000, 3000 and 5000 rpm). After curing at 75 °C for 6 hours, we obtained soft silicone substrates of different thicknesses (70μm, 30μm and 16μm). The estimated Young’s modulus of the gel is ~2 kPa. Following
a procedure similar to that reported by Style et al.16, we fabricated another soft silicone substrate of CY52-276. The Young's modulus of this kind of gel is ~3 kPa16. As PDMS is mainly used in this study, in the Article and in the Supplementary information, soft silicone refers to PDMS-based soft silicone unless CY52-276 is explicitly mentioned.

To obtain the topography of the substrates, we physically attached fluorescent nanobeads (carboxylated Yellow-Green Fluospheres of 200 nm diameter, Invitrogen) to the substrates. Each 180 μm × 180 μm square field of view contained ~2000 fluorescent beads, which covered a total area fraction of no more than 0.002. For PDMS surfaces fabricated by spin coating, the root-mean-square roughness is always less than 2 nm59, and should have little effect on the accuracy of the measured deformation.

Transfer of graphene. The graphene samples we used were from three sources: the commercially available polycrystal single layer graphene, chemical vapor deposition (CVD) multilayer graphene (two layers and 3–5 layers) on a copper foil (ACS Materials, USA), and single crystal single layer CVD graphene on copper that was provided by the research group of Dr Dong Wang of the Institute of Chemistry of the Chinese Academy of Sciences, who and his co-workers recently developed a facile atmospheric pressure CVD method to grow centimeter-sized single-crystal graphene on copper foil59. The graphene on copper was first cut at a proper size (approximately 2 centimeters). The backside graphene was removed by oxygen plasma (100 w for 3 minutes). To obtain continuous covered graphene, it is important to press a flat copper foil on a flat substrate26–28. Then the graphene-covered side of the copper foil was attached to the substrate that had embedded fluorescent beads gently to avoid damaging the soft substrate. The copper foil was etched by ammonium peroxydisulfate with a concentration of 0.5 M for ~30 minutes. Then the substrate with graphene coverage was washed in pure water for 3 times.

The multilayer graphene-covered silicone was prepared by two ways. Firstly, for as-grown multilayer graphene, the graphene-covered substrate was obtained by direct transfer of as-grown multilayer graphene onto the silicone substrate as mentioned above. Here, we chose two layer as-grown graphene and 3–5 layer as-grown graphene (Characterization of graphene is shown in the Supplementary information) in our experiment. Secondly, single layers of graphene were transferred onto a copper foil layer-by-layer, following the standard wetting transfer procedure59. Subsequently, the silicone substrate was attached to the copper foil covered by the multilayer graphene stack, and the copper was etched by the same procedure as above.

In the Article and in the Supplementary information, the single layer graphene will refer to the polycrystal single layer graphene that was purchased from ACS Materials (USA) unless an explicit statement is made to the single crystal single layer graphene of Li et al.26.

Measurement of deformation profiles. We followed the method in ref. 40. A spinning disk confocal microscope (PerkinElmer, mounted on a Nikon Ti Eclipse inverted microscope with an oil immersion 40X objective and numerical aperture (NA) = 1.3) was employed to image the beads. We used two kinds of liquid droplet, glycerol and liquid paraffin, to induce the deformation. Three-dimensional image stacks of the fluorescent tracer particles were acquired less than 20 seconds after a liquid droplet became stabilized on a substrate. The positions of the nanobeads were then extracted by Gaussian fits and azimuthally collapsed to radial surface profiles under each droplet.

References
1. Sander, D. Surface Stress: Implications and measurements. *Carr. Opin. Solid State Mater. Sci.* 7, 51–57 (2003).
2. Haiss, W. Surface stress of clean and adsorbate-covered solids. *Rep. Prog. Phys.* 64, 591–648 (2001).
3. Cammarata, R. C. & Sieradzki, K. Surface and interface stresses. *Annu. Rev. Mater. Sci.* 24, 215–234 (1994).
4. Dingreville, R. & Qu, J. Surface free energy and its effect on the elastic behavior of nano-sized particles, wires and films. *J. Mech. Phys. Solids* 53, 1827–1854 (2005).
5. Duan, H. L., Wang, J., Huang, Z. P. & Karihaloo, B. L. Size-dependent effective elastic constants of solids containing nano-inhomogeneities with interface stress. *J. Mech. Phys. Solids* 53, 1574–1596 (2005).
6. Diao, J., Gall, K. & Dunn, M. L. Surface-stress-induced phase transformation in metal nanowires. *Nat. Mater.* 2, 656–660 (2003).
7. Ibach, H. The role of surface stress in reconstruction, epitaxial growth and stabilization of mesoscopic structures. *Surf. Sci. Rep.* 29, 195–263 (1997).
8. Roy, A. et al. Wrinkling of atomic planes in ultrathin Au nanowires. *Nano Lett.* 14, 4859–4866 (2014).
9. Sun, J. et al. Liquid-like pseudoelasticity of sub-10-nm crystalline silver particles. *Nat. Mater.* 13, 1007–1012 (2014).
10. Lysenko, O., Stepanyuk, V., Hergert, W. & Kirschner, J. Mesoscopic relaxation in homeopetaxial metal growth. *Phys. Rev. Lett.* 89, 126101 (2002).
11. Monroy, F. & Langevin, D. Direct experimental observation of the crossover from capillary to elastic surface waves on soft gels. *Phys. Rev. Lett.* 81, 3167–3170 (1998).
12. Weissmuller, J. et al. Charge-induced reversible strain in a metal. *Science* 300, 312–315 (2003).
13. Jin, H. J. & Weissmuller, J. A material with electrically tunable strength and flow stress. *Science* 332, 1179–1182 (2011).
14. Kramer, D., Viswanath, R. N. & Weissmuller, J. Surface-stress induced macroscopic bending of nanoporous gold cantilevers. *Nano Lett.* 4, 793–796 (2004).
15. Weissmuller, J. & Duan, H. L. Cantilever bending with rough surfaces. *Phys. Rev. Lett.* 101, 146102 (2008).
16. Style, R. W., Hyland, C., Boltyansky, R., Wettlaufer, J. S. & Dufresne, E. R. Surface tension and contact with soft elastic solids. *Nat. Commun.* 4, 2728 (2013).
17. Style, R. W. et al. Stiffening solids with liquid inclusions. *Nat. Phys.* 11, 82–87 (2014).
18. Style, R. W., Wettlaufer, J. S. & Dufresne, E. R.Surface tension and the mechanics of liquid inclusions in compliant solids. *Soft Matter* 11, 672–679 (2015).
19. Novoselov, K. S. et al. A roadmap for graphene. *Nature* 490, 192–200 (2012).
20. Geim, A. K. & Grigorieva, I. V. Van der Waals heterostructures. *Nature* 499, 419–425 (2013).
21. Ciaudo, A., Melchionna, M., Marchesan, S. & Prato, M. The covalent functionalization of graphene onsubstrates. *Angew. Chem. Int. Ed.* 54, 10734–10750 (2015).
22. Bae, S. et al. Roll-to-roll production of 30-inch graphene films for transparent electrodes. *Nat. Nanotechnol.* 5, 574–578 (2010).
23. Zang, J. F. et al. Multifunctionality and control of the crumpling and unfolding of large-area graphene. Nat. Mater. 12, 321–325 (2013).
24. Wang, Y., Tong, S. W., Xu, X. F., Ozylizmaz, B. & Loh, K. P. Interface engineering of layer-by-layer stacked graphene anodes for high-performance organic solar cells. Adv. Mater. 23, 1514–1518 (2011).
25. Nguyen, N. N. et al. Atomically thin epitaxial template for organic crystal growth using graphene with controlled surface wettability. Nano Lett. 15, 2474–2484 (2015).
26. Song, Y. et al. Role of interfacial oxide in high-efficiency graphene-silicon schottky barrier solar cells. Nano Lett. 15, 2104–2110 (2015).
27. Schumacher, S. et al. The backside of graphene: manipulating adsorption by intercalation. Nano Lett. 13, 5013–5019 (2013).
28. Goldfain, M. D. et al. Tuning and persistent switching of graphene plasmons on a ferroelectric substrate. Nano Lett. 15, 4859–4864 (2015).
29. LaKiGio, M. et al. Graphene on a hydrophobic substrate: doping reduction and hysteresis suppression under ambient conditions. Nano Lett. 10, 1149–1153 (2010).
30. Raj, R., Maroo, S. C. & Wang, E. N. Wettability of graphene. Nano Lett. 13, 1509–1515 (2013).
31. Chuu, S., Kim, Y., Jung, H. & Park, W. A flexible graphene touch sensor in the general human touch range. Appl. Phys. Lett. 105, 041907 (2014).
32. Chuu, S., Kim, Y., Oh, H. S., Bae, G. & Park, W. A highly sensitive pressure sensor using a double-layered graphene structure for tactile sensing. Nanoscale 7, 11652–11659 (2015).
33. Zhu, B. et al. Microstructured graphene arrays for highly sensitive flexible tactile sensors. Small 10, 3625–3631 (2014).
34. Cammarata, R. C. & Sieradzki, K. Surface stress effects on the critical film thickness for epitaxy. Appl. Phys. Lett. 55, 1197 (1989).
35. Cammarata, R. C. Surface and interface stress effects in thin-films. Prog. Surf. Sci. 46, 1–38 (1994).
36. Lachut, M. J. & Sader, J. E. Effect of surface stress on the stiffness of cantilever plates. Phys. Rev. Lett. 99, 206102 (2007).
37. Pereira, V. M., Castro Neto, A. H. & Peres, N. M. R. Tight-binding approach to uniaxial strain in graphene. Phys. Rev. B 80, 045401 (2009).
38. Yoon, D., Son, Y.-W. & Cheong, H. Strain-dependent splitting of the double-resonance raman scattering band in graphene. Phys. Rev. Lett. 106, 155502 (2011).
39. Castro Neto, A. H., Peres, N. M. R., Novoselov, K. S. & Geim, A. K. The electronic properties of graphene. Rev. Mod. Phys. 81, 109–162 (2009).
40. Style, R. W. et al. Universal deformation of soft substrates near a contact line and the direct measurement of solid surface stresses. Phys. Rev. Lett. 110, 066103 (2013).
41. Park, S. J. et al. Visualization of asymmetric wetting ridges on soft solids with X-ray microscopy. Nat. Commun. 5, 4369 (2014).
42. Nadermann, N., Hui, C. Y. & Jagota, A. Solid surface tension measured by a liquid drop under a solid film. Proc. Natl. Acad. Sci. USA 110, 10541–10545 (2013).
43. Jerison, E. R., Xu, Y., Wilen, L. A. & Dufresne, E. R. Deformation of an elastic substrate by a three-phase contact line. Phys. Rev. Lett. 106, 186103 (2011).
44. Style, R. W. & Dufresne, E. R. Static wetting on deformable substrates, from liquids to soft solids. Soft Matter 8, 7177 (2012).
45. Yu, Y. S. & Zhao, Y. P. Elastic deformation of soft membrane with finite thickness induced by a sessile liquid droplet. J. Colloid Interface Sci. 339, 489–494 (2009).
46. Lee, C., Wei, X., Kysar, J. W. & Hone, J. Measurement of the elastic properties and intrinsic strength of monolayer graphene. Science 321, 385–388 (2008).
47. Lee, G. H. et al. High-strength chemical-vapor-deposited graphene and grain boundaries. Science 340, 1073–1076 (2013).
48. Gupta, P. K. & Walowit, J. A. Contact stresses between an elastic cylinder and a layered elastic solid. J. Lubr. Tech. - T. Asme 96, 250–257 (1974).
49. King, R. B. & Oussilvan, T. C. Sliding contact stresses in a two-dimensional layered elastic half-space. Int. J. Solids Struct. 23, 581–597 (1987).
50. Li, J. et al. Facile growth of centimeter-sized single-crystal graphene on copper foil at atmospheric pressure. J. Mater. Chem. C 3, 1530–1535 (2015).
51. Rafiei, J. et al. Wetting transparency of graphene. Nat. Mater. 11, 217–222 (2012).
52. Shih, C. J., Strano, M. S. & Blankschtein, D. Wetting translucency of graphene. Nat. Mater. 12, 866–869 (2013).
53. Chen, L. Q., Bonaccorso, E. & Shanahan, M. E. R. Inertial to viscoelastic transition in early drop spreading on soft surfaces. Langmuir 29, 1893–1898 (2013).
54. Chen, L., Auernhammer, G. K. & Bonaccorso, E. Short time wetting dynamics on soft surfaces. Soft Matter 7, 9084 (2011).
55. Sokuler, M. et al. The softer the better: fast condensation on soft surfaces. Langmuir 26, 1544–1547 (2010).
56. Chen, X. D. et al. High-quality and efficient transfer of large-area graphene films onto different substrates. Carbon 56, 271–278 (2013).
57. Kim, K. S. et al. Large-scale pattern growth of graphene films for stretchable transparent electrodes. Nature 457, 706–710 (2009).
58. Martins, L. G. et al. Direct transfer of graphene onto flexible substrates. Proc. Natl. Acad. Sci. USA 110, 17762–17767 (2013).
59. Lin, Y. C. et al. Clean transfer of graphene for isolation and suspension. Acc Nano 5, 2362–2368 (2011).

Acknowledgements
The authors thank the National Natural Science Foundation of China (Grants 11225208 and 11521202) and National Basic Research Program of China (2013CB933702). We also thank Dr. Dong Wang and Mr. Jing Li (Institute of Chemistry, Chinese Academy of Sciences) for providing the single crystal graphene, and Dr Mario Lanza (Soochow University, China) and Dr Xiaoding Wei (Northwestern University, USA) for helpful discussions.

Author Contributions
F.D., C.Y.X. and J.X.W. designed the research; F.D. performed the experiment; F.D., J.Y.H., H.L.D., C.Y.X. and J.X.W. analysed the model and data; and F.D., J.Y.H., C.Y.X. and J.X.W. wrote the paper.

Additional Information
Supplementary information accompanies this paper at http://www.nature.com/srep

Competing financial interests: The authors declare no competing financial interests.

How to cite this article: Du, F. et al. Surface stress of graphene layers supported on soft substrate. Sci. Rep. 6, 25653; doi: 10.1038/srep25653 (2016).
