Stress Analysis of Steel Plate Girders Subjected to Patch Loading in Elastoplastic Domain

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Abstract: This paper considers the stress analysis of steel I girders subjected to patch loading for different lengths of load. Behavior of the girders under the patch loading or uniformly distributed load on the flange and in the plane of web represents complex stability and elastic-plastic problem. The geometric and material non-linearities that exist, also affect the behavior of the girder. A better knowledge of girder behavior is important in order to achieve a more economical and a safer design. In addition to the limit load analysis, the stress analysis is of particular interest. The results from the experiment were used and were compared with the results obtained by modeling the girders in the ANSYS software.

Keywords: elastic-plasticity; limit load analysis; patch loading; steel plate girders; stress analysis

1 INTRODUCTION

The behavior of welded plate girders subjected to patch load or partially distributed load on the flange in the plane of a web (see Fig. 1) represents a complex stability and elastic-plastic problem. Numerous researches during past decades in this field indicate the main parameters that influence the behavior of plate girder subjected to patch loading: thickness of the web, size of the flange, distance of vertical stiffeners, distance of the longitudinal stiffeners from the upper flange of the girder, yield stresses of the parts of the girder, distribution length of the subjected load, value of the bending moment etc. Both geometric and material non-linearities appear and they influence the behavior of the girder. This paper represents a continuation of the research presented in [1].

The research conducted in this paper is related to the stress state analysis of plate girders, which was not considered in the previous paper. In further text, we will briefly describe the problems and basic elements of our research.

The experimental results by N. Marković are taken as the basis for solving these problems [2].

Girder analysis in computer program ANSYS was done in accordance with the experimental model [3]. The girders were set with the same initial geometrical imperfections of the web as those on the experimental model. Within the numerical analysis, six different material models with different σ-ε curves were considered. In accordance with the standards EN 1993-1-5 [4] numerical modeling of these girder models was performed.

Girder behavior in a nonlinear area is observed, especially in terms of stress state analysis until the ultimate strength is reached, with buckling in the zone where loading is applied.

Also, the cases of stress state occurring in the girders with and without longitudinal stiffening and the cases when the length of loading is 5.0 cm or 15.0 cm were analyzed.

Geometrical imperfections of the girders are taken into consideration.

We compared the stress analysis based on the experimental model and the stress analysis obtained by computer modeling of the same model of the girder.

Because of the complexity of this problem, which involves the spatial system, the problem of stability, i.e. the buckling of the web, the appearance of plastic zones before the appearance of buckling and long before the collapse of the girder, a complete theoretical solution does not yet exist.

2 EXPERIMENTAL MODEL

Data from the experimental research of Dr. Nenad Markovic were used in the research [2]. These data were used to compare with the data obtained in the software program.

Four cases of girders with the same span (s = 50 cm) and the same height (h = 50 cm) were treated. Two types of girders have longitudinal stiffeners and the other two types of girders do not have a longitudinal stiffener. The application of the load was to the upper flange along the entire width. The load application length is 5.0 cm for two types of girders, and 15.0 cm for the other two types of girders. The considered girder of series "A" is presented in Fig. 1 with characteristic notations and the dimensions are shown in Tab. 1.

![Figure 1 Model geometry [1]](image)

| Girder | s | h | lfl | bfl | tfl | h1 | l1 | hst | tst |
|-------|---|---|-----|-----|-----|----|----|-----|-----|
| A1    | 50.0 | 50.0 | 0.4 | 12.0 | 0.8 | 15.0 | 3.0 | 0.8 | 10.0 |
| A2    | 50.0 | 50.0 | 0.4 | 12.0 | 0.8 | 5.0  | 0   | 0   | 0   |
| A3    | 50.0 | 50.0 | 0.4 | 12.0 | 0.8 | 15.0 | 0   | 0   | 0   |
| A4    | 50.0 | 50.0 | 0.4 | 12.0 | 0.8 | 5.0  | 0   | 0.8 | 10.0 |

Table 1 Girder model-geometrical characteristics [1]
A closed frame was designed for the purposes of the experiment. A hydraulic press was used to apply the load step by step. The cessation of the load increase was performed with the achievement of the ultimate load, but the increase of deformations is caused without further increase of the load. During this process, a visible buckling of a part of the upper zone of the vertical web appeared (see Fig. 2).

Material characteristics were tested and the calculated results were used for creation on nonlinear material models. The steel coupons taken from the webs of the girders which did not sustain permanent deformation were examined by N. Marković. The testing was performed in the Innovation center of the Faculty of Technology and Metallurgy of Belgrade in 2013 in order to determine mechanical properties of steel sheets according to the SRPS EN ISO 6892-1:2012 standard.

3 NUMERICAL MODELING OF GIRDERS AND FORMATION OF MATERIAL MODELS WITHIN THE NONLINEAR ANALYSIS

In order to obtain the most accurate results, girder modeling was fully adapted to the experimental models. Numerical modeling was calculated in computer program ANSYS [3].

The girder modeling included: setting of material characteristics, setting the adequate geometry of the girder, the geometric imperfections of the ribs were also entered, setting boundary conditions, setting of loads according to the experimental models, selection of appropriate finite element mesh size, setting other parameters relevant to the analysis.

Numerical models are designed to best describe experimental models.

In a numerical analysis, it is of great importance to set the appropriate material behavior parameters in a proper way. Material imperfections of the girder are in most cases related to errors during fabrication and to other reasons. It can be said that material imperfections, in fact, occur, due to the residual stresses in the material, so they must be calculated in the initial state of the girder.

Based on the data from laboratory tests the \(\sigma-\varepsilon\) diagram in Fig. 4 is obtained. The diagram corresponds to one of the coupons.

Shear strains were calculated from the measured strains at the points where the strain gauge rosettes were placed. The position of the strain gauges was on both sides of the web or loaded flange. This allows calculating membrane stresses and bending stresses. Normal stresses in the horizontal (longitudinal direction) \(\sigma_x\), vertical (transversal) direction \(\sigma_y\) and shear stresses were calculated. On the basis of these values, the main stresses \(\sigma_1\) and \(\sigma_2\) and their directions were determined.
EN1993-1-5 [5] as well as \( E_t = E/100 \) for the additional analysis were used.

In addition, we used a multi-linear curve recommended by BSK07 (Swedish regulations) [6]. The modulus of elasticity of material is \( E = 210 \) MPa and the Poisson's coefficient is \( \nu = 0.3 \). Based on von-Mises condition in the frame of the theory of plasticity we use material models on the isotropic rule (for more information, see [1]).

Geometry of the girder was assigned according to the experimental models. The initial geometrical imperfections of the model, measured in the experiment, were designed on the girder web. Imperfections were previously measured during the experiment. The flanges and stiffeners were designed without imperfections.

The loading was applied to the girder in the same manner as in the experiment.

The load was applied in six steps. With each of the different types of girders, the load increment differed, regarding the expected value of ultimate load in accordance with the experimental data. In this way it is possible to monitor the flow of variation of stress and strain state in the girder.

Starting from the size of the finite element mesh, we chose a certain element size. As these elements were made smaller and smaller, as the mesh was refined, the computed solution would approach the true solution. Our criterion was to achieve a difference between two iterations less than 5%. In that way, we perform discretization of the mesh of the finite element. The adopted size of the finite element was 1.5 cm. The finite elements of the type "SOLID 186" were defined by twenty nodes. It was very convenient for nonlinear analysis [3].

4 STRESS STATE VARIATION UNTIL GIRDER ULTIMATE LOAD CAPACITY IS REACHED

The problem of local buckling is very complex [7]. During loading of the girder, still in the elastic zone, the first to occur are the deformations on the lower part of the web under the longitudinal stiffening. With the further increase of the force, the deformation on the upper part of the web between the loaded flange and longitudinal stiffening continues. Such a combination of stresses is formed that the plasticity condition is reached. Approaching to the ultimate load, buckling in the upper part of the web becomes more prominent, only to become dominant when the ultimate load capacity is reached. After that, with small force increased increments, this buckling increases uncontrollably and the girder fails in that zone. After unloading of the girder, residual plastic deformations remain, which are more prominent in the upper part of the web.

We consider that the ultimate load capacity is reached when the solution starts to diverge. In this case, sudden deformations occur on the girder and the girder loses stability.

The value of the force at which the girder loses stability is taken as the ultimate load capacity. For the obtained value of the ultimate load, the stress reaches the maximum value and then abruptly declines [8].

In Fig. 7 we can see a diagram of increasing force and von Mises stresses for \( A_1 \) up to the ultimate load. The tensile strength of material is \( f_u = 449.6 \) MPa. In the same figure we can see that already from the load of 92.96 kN at certain points the yielding stresses are reached \( (f_y = 329.97 \) MPa). The highest value of von Mises stress is 440.59 MPa.

In Fig. 8 we can see von-Mises stresses for type of \( A_1 \) girder.

The remaining cases are treated similarly. Stress state for the \( A_2 \) girder is presented in Fig. 9 and Fig. 10. At the
force of 131.9 kN (60.8 % of ultimate load) yielding stress is reached at certain points, and the highest value of von-Mises stress of 446.65 MPa (tensile strength $f_u = 449.6$ MPa), is reached at the ultimate load of 216.92 kN (see Fig. 9).

In Fig. 12 is presented the status of von-Mises stresses for the ultimate load value of 188.5 kN.

The A7 girder achieves plastic phase in certain points at the load value of 192.86 kN when yield stress is reached, which is 70.39 % of the limit load value. After reaching the limit load of 274 kN, the corresponding stress value is 425.41 MPa.

As in the previous cases, for the girder A3, after reaching the ultimate load (188.5 kN) the stress value is the highest and amounts to 436.98 MPa (tensile strength $f_u = 449.6$ MPa), and for the load of 95.697 kN (50.77% of the limit value) the yield stress is reached in certain points (see Fig. 11 and Fig. 12).

In Fig. 13 is presented the status of von-Mises stresses for the ultimate load value of 274 kN.

Characteristic locations of the strain gauges applied to girder webs (all type of girders), which are experimentally tested are presented in Fig. 15, Fig. 16 and Fig. 17. Dimensions are in cm.
For each of the girders, stress diagrams in characteristic points are determined. In that process, the ultimate load values and stress and strain diagrams of each of four cases of girders are determined for six material models: multi-linear curve which is obtained after the curve obtained by the testing (see Fig. 5) and according to the recommendations in EN1993-1-5, multi-linear curve according to the recommendations in Swedish regulations BSK07 [6], bilinear curve with tangent modulus $E_t = E/10000$ (according to the recommendations in EN1993-1-5), bilinear curve with $E_t = E/1000$ for additional research, bilinear curve with tangent modulus $E_t = E/100$ (according to the recommendations in EN1993-1-5 [5]), see Fig. 6.

The obtained results in numerical simulations of the girder model are compared to the results of the corresponding models from the experiment.

In the following diagrams are presented the $\sigma_x$ and $\sigma_z$ stress values in characteristic points in which the strain gauges were placed, at the front side of web, during the experiment. What is presented, are the stresses for the A3 girder for different material models (see Fig. 18).

For the A1 girder, the results are compared. The ultimate load for the girder with imperfections is 178.174 kN, and the value of the ultimate load in the experiment is 165 kN. The obtained stress values on the appropriate measuring places are presented in Fig. 19.

Stress values $\sigma_x$ and $\sigma_z$, for the girder $A_2$ at certain measuring places (see Fig. 16) are presented in Fig. 20. The ultimate load capacity for the $A_2$ girder is 215 kN according to the experiment, and 216.9275 kN via the numerical simulation.

For the $A_3$ girder the stress values $\sigma_x$ and $\sigma_z$ are presented also with the increase of forces (see Fig. 21). The ultimate load capacity during numerical simulation for the girder with geometrical imperfections is 188.5 kN and in the experiment it is 183 kN. The stress values exceeding tensile strength values need not be taken into consideration ($f_u = 449.6$ MPa).

In Fig. 22 are presented the stress diagrams $\sigma_x$ and $\sigma_z$ for the girder $A_7$ and measuring place 1. The ultimate load capacity for the girder with geometrical imperfections is 274 kN. In the experiment the ultimate load obtained is 255 kN.
An analysis of the obtained results of stress values revealed certain deviations in the values obtained experimentally and through numerical simulation. Within the numerical models, for the reasons of modeling simplification, the following were ignored: impacts of imperfections of flanges and stiffening, impacts of welds between the flanges and webs and stiffeners and webs; mean values of yield stress $f_y$ and tensile strength $f_u$ are considered, etc. It is assumed that taking of those initial geometrical imperfections does not produce considerably better results, so they can be ignored in this case in the numerical modeling. The following must be emphasized: during numerical simulations of the model, the form, character and flow of deformation development and buckling are identical as in the experiment, and for each sample with which the comparison was made, too, which is presented in the paper [1]. Also, a better agreement of the stress values of the girders with longitudinal stiffeners, $A_3$ and $A_7$ is observed.

6 CONCLUSION

The assessment of the measured strains used for obtaining the stress state, along with other results of undertaken measuring confirmed that the behavior of the girder web exposed to patch loading represents a complex problem of stability in an elastic-plastic zone, with early development of plasticizing.

During the nonlinear numerical simulation of the experiments, the stresses in the characteristic points for all cases of girders are calculated, at the places where strain gauges were placed in the previously described experiment (see Fig. 15, Fig. 16 and Fig. 17). Strain gauges were placed on the front and back side of the girder web, and on the basis of the obtained strain values the stress values in $x$ and $z$ directions are calculated.

It is determined, that in the zone where the load was applied the yield stresses on the web were reached before the ultimate load, without a notable deformation in that zone of the web.

By analyzing the obtained data, it is found that the onset of plasticization occurs at 58.5% of the ultimate load. This is the average value for all types of the girders.

The deformations which occur in this case do not need to be considerable. This provided data on the plastic reserve possessed by the girder.

This suggests that for every structure, two combinations need to be analyzed:
1) Girder made of high-grade steel, with higher-yield strength and with a slender web.
2) Girder made of lower-grade steel, with a thick web.
The presented MKE analyses in numerical simulation provide finding a cost-efficient design with a high reliability.

The stress values are compared for different material models, for individual measuring points, and within each of those diagrams, for the sake of analysis there is one diagram which corresponds to the experimental results and it is designated as "experiment". The stresses exceeding the value of tensile strength ($f_t = 449.6$ MPa) are not presented in the diagrams.

Due to their complexity and non-existing comprehensive solutions, the problem of patch loading is not a closed book. It is topical, as attested by increasing number of papers, doctoral dissertations, changes of European codes and propositions for their amendments [9-11].

From the previous statements, it is concluded that there is a satisfactory agreement of the established numerical models of these researches with experimental models. These researches cannot provide all the answers, but these tests and potential for new tests and different models can contribute to explanation of this complex problem. This provides potential for new testing of behavior of such or different girder models using numerical simulation. The tests which are conducted, in this manner, facilitate performing of girder analyses which would indirectly contribute to adoption of correct approaches to obtaining of theoretical results, for instance, with the aim of analyzing failure mechanisms in a non-elastic zone (see [12-14]).

Also, there is potential for further analysis of many parameters, changes of girder geometry, testing of girders with openings in the web, as well as application of new materials for whole girders or their parts.

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