Credit scoring analysis using kernel discriminant

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Abstract. Credit scoring model is an important tool for reducing the risk of wrong decisions when granting credit facilities to applicants. This paper investigate the performance of kernel discriminant model in assessing customer credit risk. Kernel discriminant analysis is a non-parametric method which means that it does not require any assumptions about the probability distribution of the input. The main ingredient is a kernel that allows an efficient computation of Fisher discriminant. We use several kernel such as normal, epanechnikov, biweight, and triweight. The models accuracy was compared each other using data from a financial institution in Indonesia. The results show that kernel discriminant can be an alternative method that can be used to determine who is eligible for a credit loan. In the data we use, it shows that a normal kernel is relevant to be selected for credit scoring using kernel discriminant model. Sensitivity and specificity reach to 0.5556 and 0.5488 respectively.

1. Introduction
Effective credit risk assessment has become a very important factor for obtaining many advantages in credit market which can help financial institutions to grant credit to credit worthy customers and reject non-creditworthy customers [1]. The decision makers need some help to decide whether to grant credit or not for a credit applicant from some efficient and feasible tools [2]. Credit scoring is the most widely used techniques that help them to make credit granting decision. Credit scoring models play an important role in contemporary risk management practice. They contribute to the key requirement in loan approval process, which is to accurately and efficiently quantify the level of credit risk associated with a customer [3]. Credit scoring models help credit institutions evaluate credit applications with respect to customer characteristics such as age, income, and marital status [4]. Technically, credit scoring models classify loan clients to either good credit or bad credit [5].

A wide range of classification techniques have already been proposed in the credit scoring literature, including statistical methods, such as linear discriminant analysis and logistic regression and non-parametric models, such as decision trees, k-nearest neighbor, and nonparametric discriminant [6]. These models are categorized into parametric and non-parametric or data mining models [1]. Briefly, a parametric model presumes that the form of the model is known except for finitely many unknown parameters, whereas a non-parametric models only assumes that the model belongs to some infinite dimensional collection of functions [7]. Generally, linear discriminant analysis and logistic regression are categorized into parametric model and decision trees, k-nearest neighbor, and kernel discriminant are classified into nonparametric one.

In a discriminant analysis, the optimal Bayes rule is used to assign an object to the class with the largest posterior probability. This probability is the product of the prior and the density function of the input. But, the density functions are usually unknown in practice, and can be estimated from the training data set either parametrically or nonparametrically. In parametric approaches, the underlying...
population distributions are assumed to be known except for some unknown parameters. Consequently, the performance of a parametric discrimination rule largely depends on the validity of those parametric models [8]. Nonparametric classification techniques, however, are more flexible in nature and free from such parametric model assumptions. Kernel density estimation is a famous method for constructing nonparametric estimates of population densities. The use of kernel density estimates in discriminant analysis is quite popular in the existing literature ([9], [10], [11], [12]). The application of kernel methods for scoring credit scoring analysis is still rare. We are interested in using this method to classify credit customers based on the characteristics of the previous borrower.

The rest of this paper is organized as follows. In Section 2, we give a brief overview of kernel discriminant. The data used in this paper describe in Section 3. An empirical study of a credit from a financial institution and its results are presented in Section 4. Finally, conclusions are offered in Section 5.

2. Kernel Discriminant Analysis

This study aims to apply the kernel discriminant method for the purpose of classification of a prospective borrower as a good or bad borrower. Let \( x_1, \ldots, x_n \) is a random sample from population \( \Pi_t \), and \( x \) is an observation from population \( \Pi_t \) which has an unknown probability density function \( f_t(x) \). In this paper \( f_t(x) \) was estimated by \( \hat{f}_t(x) = \frac{1}{n_t} \sum_{i=1}^{n_t} K_t(x - x_i) \), where \( K_t(x) \) is a function defined by \( x \), a vector \( d \) dimensions. \( K_t(x) \) is called a kernel function of the population \( t \) [13]. Let \( z = x - x_i \), \( h \) is bandwidth value, \( d \) is the number of explanatory variables, \( V_t \) represent a covariance matrix of population \( t \), and \( t = 1, 2, \ldots, g \). Below are some kernels that frequently used:

a. Kernel Normal (mean 0, variance \( h^2 \cdot V_t \))
\[
K_t(z) = \frac{1}{c_0(t)} \exp\left(-0.5z^T V_t^{-1} z / h^2 \right)
\]
where \( c_0(t) = (2\pi)^{d/2} h^d |V_t|^{1/2} \)

b. Kernel Epanechnikov
\[
K_t(z) = \begin{cases} 
\frac{3}{4} \left(1 - \frac{z^T V_t^{-1} z}{h^2}\right), & \text{if } z^T V_t^{-1} z \leq h^2 \\
0, & \text{elsewhere}
\end{cases}
\]
where \( c_0(t) = \frac{d}{\pi^{d/2}} h^d |V_t|^{1/2} \)
\[
v_h(t) = \frac{d}{\pi^{d/2} h^d |V_t|^{1/2}}
\]
c. Kernel Biweight
\[
K_t(z) = \begin{cases} 
\frac{3}{4} \left(1 - \frac{z^T V_t z}{h^2}\right)^2, & \text{if } z^T V_t z \leq h^2 \\
0, & \text{elsewhere}
\end{cases}
\]
where \( c_2(t) = \frac{1}{4} c_1(t) \)

d. Kernel Triweight
\[ K_i(z) = \begin{cases} 
    c_3(t) \left(1 - z'V_i z / h^2\right)^3, & \text{if } z'V_i z \leq h^2 \\
    0, & \text{elsewhere}
\end{cases} 
\]

where \( c_3(t) = \left(1 + \frac{d}{6}\right)c_2(t) \).

An observation will be classified to population \( t \) if the posterior probability value in that population is greatest when compared to the posterior probability value in the other populations. The posterior probability of an observation \( x \) in population \( t \) is

\[ P(\Pi_i | x) = \frac{p_t \hat{f}_i(x)}{\sum_{i=1}^{g} p_t \hat{f}_i(x)} \]

which is defined by \( p_t = \frac{n_t}{\sum_{i=1}^{g} n_t} \).

### 3. Data And Methods

The data used in this paper come from a financial institution in Indonesia consisting 2075 clients of which 409 clients are categorized as bad customer which are debtors in July 2017. The financial institution dispurse a loans for purchasing a motorcycles. For the data set, a bad customer was defined as someone who had missed three consecutive months of payments. The data involve 8 continuous explanatory variables including amount principal, working experience, total income, price, down payment, installment, long repayment, and rate. The description of each variables and its unit of measure is shown in Table 1.

**Table 1. Variables used for building The credit scoring model**

| Variable          | Definition                                      |
|-------------------|-------------------------------------------------|
| Amount principal  | Amount principal of applicant in Rupiahs         |
| Total income      | Monthly income in Rupiahs                       |
| Working experience| Working experience of the applicant in years     |
| Price             | Price of motorcycle                             |
| Down payment      | Down payment for the purchase of motorcycles in Rupiahs |
| Installment       | Installment in Rupiahs                          |
| Long repayment    | Long repayment in month                         |
| Rate              | Rate in percent per month                       |

For this empirical study, we split the data into training set consisting of 80% and testing set for the rest. After specifying a kernel and executing the algorithm of the method, the accuracy of the method was calculated using sensitivity, specificity, percentage of correctly classified (PCC), and apparent error rate (APER). The formulas of the four measures of accuracy refer to the paper of Zhou, Lai, and Yu [1].

\[
\text{Sensitivity} = \frac{GG}{GG + GB} \\
\text{Specificity} = \frac{BB}{BB + BG} \\
\text{PCC} = \frac{GG + BB}{GG + GB + BB + BG}
\]
where GG represent the number of good customers that were classified as good by the classifier; GB represent the number of good customer that were mistakenly classified as bad; BB represent the number of correctly classified customer that belongs to class bad; BG represent the number of observed bad customer that were mistakenly classified as good. Good models should have high value on both sensitivity and specificity. But it is often not fulfilled, because there is a trade off between the values of both, when a model has a high sensitivity, it usually has low specificity. We chose a model whose sensitivity and specificity values did not differ large.

4. Results And Discussions
Tables 2 is statistical summaries of each good and bad customers based on 8 explanatory variables. The tables tell that the average of each variable on good customers shows tend to be better than bad customers. For example, the average of total monthly income of good customers reaches Rp 3785948.379 which is greater than the total revenue of bad customers whose value only reaches Rp 3390931.540. Furthermore, the mean of down payment from good customers reach Rp 3656439.226 which is greater than bad customers. Similar condition happen to other variables that indicate good customers has a positif individual performance. Tables 2 and 3 also show that there were a different variations in the independent variables involved in the analysis on both types of customers. Overall, variability of variables from good customers is greater than bad ones.

Table 2. Statistical summary of both good and bad customer

| Variables            | Good Customers | Bad Customers |
|----------------------|----------------|---------------|
| Amount principal     | 9268090.09     | 8609974.98    |
| Total income         | 3785948.379    | 3390931.54    |
| Working experience   | 8.659          | 7.71          |
| Price                | 11993838.73    | 10704745.36   |
| Down payment         | 3656439.226    | 3029413.203   |
| Installment          | 635646.459     | 563264.059    |
| Long repayment       | 20.993         | 21.191        |
| Rate                 | 21.367         | 21.913        |

In this paper we examine the performance of several kernels including normal, epanechnikov, biweight, and triweight in classifying credit status of customers. The main parameter of a kernel is a smoothing parameter or sometimes called a bandwidth. Each kernel has an optimal performance at a certain bandwidth value. In order to know the optimal bandwidth, we do by trying some values at a certain interval. Computations of nonparameteric discrimination using kernel were conducted using SAS. A good classifier should has a high value on both sensitivity and specificity.

Table 3 shows the performance of nonparametric discriminant using kernel Normal in assessing credit worthiness. We tried some bandwidth values at intervals (0,1]. It appears that at a bandwidth value of 0.4, nonparametric discriminant models with kernel Normal produce a sensitivity and specificity of 0.5556 and 0.5488 respectively. It means that customers whose credit status is good, by the model are classified as good reach to 55.56% while customers whose credit status is bad, by the model are classified as bad reach to 54.88%. The PCC and APER at bandwidth 0.4 respectively 0.5542 and 0.4458. For bandwidth values greater than 0.4 will produce a sensitivity greater than
0.5556 but the specificity value is lower than 0.5488. We did not try a bandwidth value greater than 1, because it would widen the gap between the sensitivity and specificity of the model.

Table 3. Accurrance of nonparametric discriminant using kernel normal

| Bandwidth | Sensitivity | Specificity | PCC  | APER  |
|-----------|-------------|-------------|------|-------|
| 1.0       | 0.2492      | 0.8659      | 0.3711 | 0.6289 |
| 0.6       | 0.4565      | 0.6829      | 0.5012 | 0.4988 |
| 0.5       | 0.5015      | 0.6341      | 0.5277 | 0.4723 |
| 0.4       | 0.5556      | 0.5488      | 0.5542 | 0.4458 |
| 0.3       | 0.6637      | 0.5000      | 0.6313 | 0.3687 |
| 0.2       | 0.7958      | 0.3537      | 0.7084 | 0.2916 |
| 0.1       | 0.8739      | 0.1951      | 0.7398 | 0.2602 |

Tables 4 describe the performance of Epanechnikov, biweight, and triweight kernels on bandwidth values at intervals [4,9]. At the interval, the kernel discriminant model shows unsatisfactory performance. For those kernels with bandwidth values at intervals [4,9] yields very low sensitivity and high specificity. This means that the three kernel functions on the bandwidth [4,9] are incapable of predicting a good consumer in paying credit as a good consumer according to the kernel discriminant model. In contrast, the kernel discriminant model using the epanechnikov, biweight, and triweight kernels has a high specificity value which indicates that it is able to predict poor consumers in paying credit as a bad consumer as well. Furthermore, the combination of kernel types and the bandwidth values also result in low PCC and high APER values. We did not try a bandwidth value that is less than 4, because it produces an unidentifiable classification of whether the customer is in good or bad credit status. We also did not try a bandwidth which is larger than 9, because the difference between sensitivity and specificity is getting bigger.

Table 4. Accurrance of nonparametric discriminant using kernel epanechnikov, biweight, and triweight

| Bandwidth | 4    | 5    | 6    | 7    | 8    | 9    |
|-----------|------|------|------|------|------|------|
| Epanechnikov |      |      |      |      |      |      |
| Sensitivity | 0.1652 | 0.1201 | 0.0781 | 0.0601 | 0.039 | 0.042 |
| Specificity | 0.9146 | 0.939 | 0.9512 | 0.9634 | 0.9756 | 0.9756 |
| PCC | 0.3133 | 0.2819 | 0.2506 | 0.2386 | 0.2241 | 0.2265 |
| APER | 0.6867 | 0.7181 | 0.7494 | 0.7614 | 0.7759 | 0.7735 |
| Biweight |      |      |      |      |      |      |
| Sensitivity | 0.1862 | 0.1291 | 0.0961 | 0.0751 | 0.0511 | 0.042 |
| Specificity | 0.878 | 0.9268 | 0.939 | 0.9512 | 0.9878 | 0.9756 |
| PCC | 0.3229 | 0.2867 | 0.2627 | 0.2482 | 0.2361 | 0.2265 |
| APER | 0.6771 | 0.7133 | 0.7373 | 0.7518 | 0.7639 | 0.7735 |
| Triweight |      |      |      |      |      |      |
| Sensitivity | 0.2102 | 0.1622 | 0.1141 | 0.0841 | 0.0691 | 0.0511 |
| Specificity | 0.8902 | 0.9268 | 0.9268 | 0.939 | 0.9634 | 0.9878 |
| PCC | 0.3446 | 0.2529 | 0.2747 | 0.253 | 0.2458 | 0.2361 |
| APER | 0.6554 | 0.7471 | 0.7253 | 0.747 | 0.7542 | 0.7639 |

5. Conclusions
Credit scoring has become an important task as financial industries can increase their benefits. This paper apply kernel discriminant model for evaluating credit applicants worthiness. We investigate the performance of several kernels in order to find a nonparametric discriminant model which good accurrance in classification. In our case, the results show that kernel discriminant can be an alternative
method that can be used to determine who is eligible for a credit loan. In the data we use, it shows that a normal kernel is relevant to be selected for credit scoring using kernel discriminant model. Sensitivity and specificity reach to 0.5556 and 0.5488 respectively. This such model is very required by a financial institutions for reducing the risk of wrong decisions when granting credit facilities. The objective of this model is to separate a credit applicants who is eligible and who isn't.

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