New CMB spectral distortion constraints on decaying dark matter with full evolution of electromagnetic cascades before recombination

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Current constraints on energy injection in the form of energetic particles before the epoch of recombination using CMB spectral distortions assume that all energy goes into $y$ and $\mu$-type distortions. We revisit these constraints with exact calculations of the spectral distortions by evolving the electromagnetic cascades. The actual spectral distortion differs in shape and amplitude from the $y$-type distortion and depends on the energy and nature of injected particles. The constraints on the energy injection processes such as dark matter decay can be relaxed by as much as a factor of 5.

Introduction.–– In the standard ΛCDM cosmology, the cosmic microwave background (CMB) has an almost perfect blackbody spectrum, a consequence of almost complete thermal equilibrium in the early Universe. Any deviation from equilibrium in the CMB spectrum is exponentially suppressed at redshifts $z \gtrsim 2 \times 10^6$ [1, 2]. The Planck spectrum once created is preserved by the expansion of the Universe. At redshifts $z \lesssim 2 \times 10^6$, it is no longer possible to restore the equilibrium disturbed by, for example, injection of energetic standard model particles such as photons, electrons and positrons. It therefore becomes possible to create deviations in the CMB from a Planck spectrum. By observing these spectral distortions of the CMB, we can learn about the physical processes which injected energy into the CMB at $z \gtrsim 2 \times 10^6$. The high entropy per baryon in our Universe, quantified by the photon-to-baryon number density ratio ($\sim 10^9$), means that the recombination dynamics is controlled by the energetic photons in the Wien tail of the Planck spectrum with the recombination starting only when the temperature of the CMB is more than a factor of 30 smaller than the Lyman-α energy [3, 4]. As a result, the recombining and subsequent Universe, with most neutral atoms in the ground state, is optically thin to the bulk of the photons in the CMB since they are at energies much smaller compared to the energy of the first excited state of neutral atoms. The CMB spectral distortions, and the information about the energy injection processes in the early Universe, are therefore preserved through recombination and are observable today.

The measurement of the CMB monopole spectrum in 1990s by the Far Infrared Absolute Spectrometer (FIRAS) onboard Cosmic Background Explorer (COBE) satellite [4, 5] remains the best constraint on the deviation of the CMB monopole spectrum from a blackbody until today. The COBE-FIRAS data has been used by numerous authors to constrain many exotic as well as standard model energy injection processes in the early Universe (e.g. [6–11], see [12] for a review). Almost all calculations until now have assumed that the injected energy ends up heating the electrons [1, 3, 13–17] irrespectively of the initial energy or nature of the injected particles. The Compton scattering of CMB photons on heated electrons produces $y$-type distortions which then thermalize to $i$-type and $\mu$-type (Bose-Einstein spectrum) distortions [10]. We will call $y$, $i$ and $\mu$-type distortions collectively as $yim$-distortions and the assumption that all energy goes into heat or $yim$-distortions as the $yim$-approximation. The amplitude of the $yim$-distortions depends on the amount of energy injected while the shape depends on the redshift of energy injection, with departure from the $y$-type distortion becoming important at $z \gtrsim 10^4$.

We have recently shown that this simple picture of $yim$-distortions is incorrect [18]. In particular, when the energy is injected in the form of standard model particles, with energy much greater than the average energy of the CMB photons, not all of the energy goes into the $yim$-distortions as is usually assumed. A significant fraction of energy is lost by the particles as they collide with the background electrons, ions and photons and make their way down in energy towards thermalization with the background. The Compton scattering of relativistic electrons, produced in the cascade, with the CMB results in spectral distortions with distinctly different shape and amplitude compared to the $yim$-distortions. We call these distortions non-thermal relativistic or $ntr$-type spectral distortions. The shape and amplitude of the $ntr$-type spectral distortions depend on the energy, type and redshift of injected particles [18]. In particular, a fraction of the energy goes into the high frequency Wien tail of the spectral distortions resulting in decrease in the amplitude of the distortions in the main observable CMB frequency range compared to the $yim$-approximation. We therefore expect significant corrections to the existing constraints on energy injection scenarios in the early Universe.

A particularly interesting scenario which injects energetic particles is decay of unstable dark matter particles. The dark matter direct detection experiments, looking for Weakly Interacting Massive Particles (WIMPS) have so far not yielded any detection and the allowed parameter space for WIMPs is gradually being ruled out. This has motivated physicists to look beyond the simplest thermal WIMP models. One way around the direct de-
tection constraints is Super-WIMPs (SWIMP), where instead of producing the usual lightest stable particle in the theory in a beyond standard model theory like supersymmetry or Kaluza-Klein models, the thermally produced WIMP is the next-to-lightest particle which then decays to the lightest stable particle of the theory with the right abundance needed for dark matter halos \cite{10,19}. For a review of dark matter models, see \cite{21}. We can escape the direct detection constraints if the lightest particle, which would become sensitive to the dark matter mass, is a SWIMP. We could in general have additional unstable particles which were produced in the early Universe, with lifetime of few years to hundreds of thousands of years, which would decay not into SWIMPs + standard model particles but completely into standard model particles. More generally, we would like to constrain energy injection in the form of different standard model particles over the entire history of the Universe and look for deviations from standard cosmology as a probe of beyond standard model physics. Another interesting example of energy injection in the form of energetic photons and other particles is from evaporating primordial black holes \cite{21} or from accreting primordial black holes \cite{22,24}. We note that there are examples of long lived composite particles in the standard cosmology. During the big bang nucleosynthesis, tritium (\(^9\)H) and beryllium (\(^7\)Be) are produced which decay to stable isotopes of helium (\(^3\)He) and lithium (\(^7\)Li) at redshifts of \(z_{\text{7Be}} = 3 \times 10^3\) and \(z_{\text{7Li}} = 2.5 \times 10^5\) respectively injecting energy into the CMB \cite{24}. Unfortunately the abundance of these elements in our Universe is too low for the resulting spectral distortions to be observable.

We use Planck \cite{24} ΛCDM cosmological parameters for all calculations and parameterize the injected energy, \(\rho_X\), as a fraction of CDM dark matter density, \(f_X = \rho_X/\rho_{\text{CDM}}\), where \(\rho_{\text{CDM}}\) is the ΛCDM (non-decaying) dark matter density. When we consider only \(yim\)-distortions, \(f_X\) and lifetime \(\tau_X\) of the corresponding redshift \(z_X\) are the only parameters that need to be considered. With the explicit evolution of electromagnetic cascades, the spectral distortions and constraints in addition become sensitive to the dark matter mass, \(m_X\), as well as the decay channel or the initial spectrum of photons, electrons and positrons injected in the decay.

**Electromagnetic cascades in the expanding Universe.**— In this Letter, we explicitly follow the electromagnetic cascade to calculate the \(ntr\) part of the distortion while keeping track of energy that is lost to heat to calculate the \(yim\)-type contribution to the total CMB spectral distortion resulting from the injection of energetic particles. When using COBE-FIRAS data, previous authors have approximated the full distortion with a \(\mu\)-type or \(\mu\)-type distortion \cite{3,11}. We note that even in the all energy going to heat approximation there is a small difference between the \(\gamma\) - and \(\mu\)-distortion from the actual \(yim\)-distortion for \(10^4 \lesssim z \lesssim 2 \times 10^5\) \cite{10}. We evolve even the heat contribution to the spectral distortions with Kompaneets equation \cite{27} getting correctly the intermediate or \(i\)-type part of the distortion and use the actual \(yim\) and \(ntr\)-distortions for our COBE constraints.

At high redshifts \((z \gtrsim 2 \times 10^5)\), the Compton scattering process is very efficient and any initial distortion, including the \(ntr\)-type, thermalizes to a Bose-Einstein spectrum or \(\mu\)-distortion irrespective of energy and type of injected particles \cite{16}. At \(z \lesssim 2 \times 10^5\), kinetic equilibrium is no longer possible and we must follow the full particle cascade to correctly calculate the final distortion. We divide the energy range of interest into energy bins for each particle (e.g. photons, electrons and positrons). The problem of electromagnetic cascade is then cast as a system of ordinary differential equations describing the flow of particles between different energy bins. This system can then be solved using the inductive approach \cite{28,30}. Staring with an initial high energy particle, the electromagnetic cascade proceeds by sharing the total energy with more and more background particles, quickly multiplying the number of energetic particles (i.e. with energy \(\mu\) much greater than the background electrons and photons). Since, the energy cascade is one-way (i.e. higher to low energy), solution for a given energy bin only depends on the cascade solution for the lower energy bins. Therefore, starting with the lowest energy bins, we can solve for populations of higher and higher energy bins in the cascade. Details of our numerical codes implementing the above method are described in detail in \cite{18}.

In an ionized universe, the most important scattering process for low energy electrons (\(\lesssim \text{keV}\)) is Coulomb scattering and results in thermalization of the electron with most of its energy going to heat or \(yim\)-type distortions. The dominant energy loss mechanism for a relativistic electron or positron is elastic scattering (inverse Compton) with the CMB. Once a positron becomes non-relativistic it annihilates with a background electron to give two 511 keV photons. The injection of a positron is therefore, to a very good approximation, equivalent to an electron with same initial kinetic energy and two 511 keV photons. Since, the energy loss rates for electrons and positrons are extremely rapid compared to Hubble scale, they deposit their energy instantaneously \cite{18,28}.

For photons, the relevant scattering processes are Compton scattering, pair production and photon-photon elastic scattering. For most of the relevant energy range, the energy loss rate for photons is comparable to the Hubble rate. Therefore, we evolve the photon spectrum with background expansion taken into account. The most important process which determines the shape of the spectral distortion is elastic or Compton scattering of photons and electrons. Energetic photons produce energetic electrons and energetic electrons produce energetic photons by Compton scattering. The cycle repeats until the electrons start losing energy by Coulomb scattering to heat or loss of energy by photons in Compton scatter-
FIG. 1: Ratio of energy density deposited as heat with respect to CMB energy density for varying \( z_X \) and \( f_X = 0.0003 \) for dark matter decay into electron-positron pair.

Spectral distortions from dark matter decay into photons and electron-positron pairs. — We can write the energy density \( (E) \) injection rate for particle decay as

\[
\frac{dE}{dt} = \frac{f_X \rho_{DM}}{\tau_X} \exp(-t/\tau_X) \tag{1}
\]

where \( \tau_X \) is the particle decay lifetime and \( z_X \) is the redshift at proper time \( t = \tau_X \), \( \rho_{DM}(z) = (1+z)^3 \rho_{DM}(z = 0) \) is the non-decaying dark matter energy density at redshift \( z \) and \( f_X \) is ratio of the initial energy density of decaying dark matter to that of the non-decaying component.

We plot the energy density deposited as heat per logarithmic redshift interval as a fraction of the CMB energy density \( (\rho_c) \) with full evolution of particle cascades in Fig. 1 and compare it with the “yim-approximation” i.e. instantaneous deposition of all energy as heat for \( f_X = 0.0003 \). There is a clear time delay between energy injection and deposition as heat in the exact calculation and there is a bias in the temporal information also in the yim-approximation.

In Fig. 2 we plot the spectral distortions for dark matter decaying to two monochromatic photons and compare our exact calculations with the spectral distortion in the yim-approximation, the latter being insensitive to the mass of dark matter. In the exact calculation we find that the amplitude of the distortion is very sensitive to the mass of the dark matter, especially at low redshifts. The difference in shape is most evident in the high frequency tail of the spectral distortion. As we increase the redshift, the sensitivity to the initial dark matter mass decreases and the exact spectral distortion becomes closer to the yim-approximation, the two becoming indistinguishable and close to a Bose-Einstein spectrum (\( \mu \)-distortion) at \( z_X \gtrsim 2 \times 10^5 \).

We use COBE-FIRAS data \( ^8 \), publicly available on the NASA LAMBDA website, \(^1\) to constrain the fraction of dark matter that can decay as a function of decay redshift \( z_X \). We use the same procedure that was used by \( ^8 \) for the \( \mu \)-type distortion and simultaneously fit the spectral distortion from decay, a temperature shift and the galactic spectrum given in Table 4 of \( ^8 \) to the COBE-FIRAS monopole residuals. We do not find any positive detection and plot 95% upper limits for \( f_X \) in Fig. 3 for dark matter decaying to monochromatic photons and electron-positron pairs. We also show constraints in the yim-approximation.

If we assume that all energy goes into the spectral distortion with fixed shape, e.g. a \( \mu \)-type distortion, then the amplitude of the distortion will just be proportional to \( f_X \rho_{DM}/\rho_c \propto f_X/(1+z_X) \). At higher redshifts the decay of same amount of dark matter will give a smaller distortion because the energy density of CMB is higher by a factor of \( (1+z_X) \). For a given sensitivity of the experiment, the constraints on \( f_X \) become weaker with redshift, \( \propto (1+z_X) \), with some correction because the decay does not happen instantaneously. This is what we see in the curve labeled yim-approximation. Since we take into account that the distortion at \( z \lesssim 2 \times 10^5 \) is not exactly \( \mu \) but \( i \)-type and becomes \( y \)-type at \( z \sim 10^4 \), there is small departure from this linear relation. For our exact calculation, explicitly evolving the electromagnetic cascade, there is dramatic departure from the yim-approximation, with the difference of a factor of 4.7 for electron-positron channel for \( m_X \approx 4 \) MeV and a factor of 4.1 for the photon channel for \( m_X \approx 3 \) MeV at \( z_X \approx 5000 \) or dark matter lifetime \( \tau_X = 8 \times 10^{11} \) s. As we

\(^1\) https://lambda.gsfc.nasa.gov/product/cobe/firas_products.cfm
FIG. 2: Spectral distortions for dark matter decay into monochromatic photons for different $m_X$ and $z_X$ and constant $f_X = 0.0003$.

FIG. 3: 95% COBE-FIRAS upper limits on $f_X$ for different $m_X$ as a function of decay redshift $z_X$. Also shown is the constraint in the $yim$-approximation.

FIG. 4: 95% COBE-FIRAS limits on $f_X$ for decay into electron-positron pairs (left) and photons (right).
go to higher redshifts, the constraints become closer to the \( yim \)-approximation as Compton scattering become more efficient in reprocessing the energy trying to establish a Bose-Einstein spectrum. The constraints in particular are very sensitive to the mass of the decaying particle.

We show the complete constraints from full evolution of electromagnetic cascades in the \( m_X - z_X, \tau_X \) plane in Fig. 4 for decay to photons and electron-positron pairs. The colour scale represents the 95\% upper limits on \( f_X \) from COBE-FIRAS data. In the \( yim \)-approximation there will be no sensitivity to \( m_X \) and the isocontours of \( f_X \) would all be vertical lines. This is what we see at high redshifts, where \( yim \)-approximation holds. At lower redshifts the spectral distortions and hence the constraints become sensitive to \( m_X \). The cyclic nature of electromagnetic cascades, as discussed above, is reflected in oscillation in the isocontours in the \( m_X \) direction. At \( z \approx 2 \times 10^8 \) the photon creation processes double Compton scattering and bremsstrahlung, become important suppressing the spectral distortions \([1, 2]\) and weakening the constraints. We have taken this suppression into account using the blackbody visibility function from \([4]\).

**Conclusions:**– We have derived new upper limits on dark matter decay in the early Universe from COBE-FIRAS measurements of the CMB monopole spectrum. We explicitly evolve the electromagnetic cascades resulting from dark matter decay into photons and electron-positron pairs, calculate the resulting spectral distortions in the CMB band and use these to constrain the dark matter decay into these two channels. Previous COBE constraints have assumed that all energy from decay goes into heat and gives \( y \)-type and \( \mu \)-type distortions and were therefore blind to the decay channel. We show that these approximations fail at low redshifts, \( z_X \lesssim 2 \times 10^5 \) or dark matter lifetimes \( \tau_X \gtrsim 6 \times 10^8 \) s. In addition, the spectral distortions, and hence the constraints, are sensitive to the dark matter mass. Our results show that the decay channels are important for spectral distortions, just as they are important for the CMB recombination history for larger lifetimes \([31, 32]\). This work motivates a more comprehensive study, in the future, taking into account different decay channels motivated by different particle physics models in specific cosmological scenarios such as in \([11]\). Future experiment like Primordial Inflation Explorer (PIXIE) \([34]\) would have a sensitivity of 3-4 orders of magnitude better than COBE-FIRAS \([32]\) and may discover distortions from new physics in the early Universe. Accurate calculations of spectral distortions by explicitly evolving the electromagnetic cascades would be crucial in interpretation of such a future detection.

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