AN UPPER LIMIT ON THE ALBEDO OF HD 209458B: DIRECT IMAGING PHOTOMETRY WITH THE MOST SATELLITE

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ABSTRACT

We present space-based photometry of the transiting exoplanetary system HD 209458 obtained with the Micro-variability and Oscillations of Stars (MOST) satellite, spanning 14 days and covering 4 transits and 4 secondary eclipses. The HD 209458 photometry was obtained in MOST’s lower precision direct imaging mode, which is used for targets in the brightness range 6.5 ≥ V ≥ 13. We describe the photometric reduction techniques for this mode of observing, in particular the corrections for stray earthshine. We do not detect the secondary eclipse in the MOST data, to a limit in depth of 0.053 mmag (1σ). We set a 1σ upper limit on the planet-star flux ratio of 4.88 × 10^−3 corresponding to a geometric albedo upper limit in the MOST bandpass (400–700 nm) of 0.25. The corresponding numbers at the 3σ level are 1.34 × 10^−4 and 0.68, respectively. HD 209458b is half as bright as Jupiter in the MOST bandpass. This low geometric albedo value is an important constraint for theoretical models of the HD 209458b atmosphere, in particular ruling out the presence of reflective clouds. A second MOST campaign on HD 209458 is expected to be sensitive to an exoplanet albedo as low as 0.13 (1σ), if the star does not become more intrinsically variable in the meantime.

Subject headings: planetary systems — stars: individual (HD 209458) — techniques: photometric

Online material: color figures

1. INTRODUCTION

Since the discovery of the giant planet orbiting 51 Pegasi (Mayor & Queloz 1995) a decade ago, and the subsequent detection of about 160 exoplanetary systems around solar-type stars, the task of acquiring information about the atmospheres of giant close-in planets has been particularly challenging. Observations of the transits of the exoplanet HD 209458b have revealed the presence of sodium in its atmosphere (Charbonneau et al. 2002) and a hydrogen cloud around it (Vidal-Madjar et al. 2003). The Spitzer infrared space telescope has detected the eclipse of HD 209458b in its thermal emission at 24 μm (Deming et al. 2005b), yielding a brightness temperature at that wavelength of 1130 ± 150 K.

We report here an attempt to detect the eclipse of HD 209458b (orbital period ~3.5 days) in reflected light at optical wavelengths, with photometry from the Micro-variability and Oscillations of Stars (MOST) satellite (Walker et al. 2003; Matthews et al. 2004). The reflected light signal from an exoplanet is sensitive to the composition of its atmosphere, as well as to the nature and filling factor of cloud particles suspended in that atmosphere (Seager et al. 2000; Green et al. 2003; Burrows et al. 2005). The proportion of scattered to absorbed radiation is critical to the

1 MOST is a Canadian Space Agency mission, operated jointly by Dynacon, Inc., and the Universities of Toronto and British Columbia, with assistance from the University of Vienna.

2 The Interactive Extrasolar Planets Catalog (J. Schneider, 2006), http://vo.obspm.fr/exoplanetes/encyclo/catalog-main.php.
planet’s energy balance, and hence an albedo measurement is key to understanding its atmosphere.

The MOST satellite houses a 15 cm optical telescope feeding a CCD photometer through a single broadband filter (350–750 nm), which is capable of sampling target stars up to 10 times per minute. From the vantage point of its 820 km high circular Sun-synchronous polar orbit with a period of 101.413 minutes, MOST can monitor stars nearly continuously for up to 8 weeks in a continuous viewing zone (CVZ) with a declination range of +36° $\leq \delta \leq -18°$. The satellite was designed to achieve photometric precision of a few parts per million (ppm) at frequencies greater than 1 mHz in the Fourier domain. The necessary photometric stability is achieved by projecting an extended image of the instrument pupil illuminated by the Primary Science target via one of an array of Fabry microlenses above the MOST Science CCD (a 1K × 1K E2V 47-20 detector). For exposure times up to 1 minute long and observing runs of at least 1 month, this Fabry imaging mode can reach the desired precision of about 1 ppm at frequencies greater than 1 mHz for stars brighter than $V \sim 6.5$.

Fainter stars can be monitored (simultaneously or independently of the Fabry imaging mode) in an open area of the Science CCD not covered by the 6 × 6 Fabry microlens array and its chromium field stop mask. In the direct imaging mode, defocused star images are projected, with a full width at half-maximum (FWHM) of about 2.5 pixels. (The focal plane scale of MOST is about 3" pixel$^{-1}$.) The photometric precision possible in the direct imaging mode is not as good as for the Fabry photometry, as direct imaging targets are fainter and more sensitive to CCD calibrations. However, the unprecedented duty cycle of the MOST observations and the thermal/mechanical stability of the instrument yield impressive results. The point-to-point precision of the photometry reported here is about 3 mmag for a 1.5 s exposure during low stray light conditions, with sampling rates as high as 10 exposures per minute and a duty cycle of 85% in 14 days of observation, where a duty cycle of 100% represents no loss of data acquisition.

Photometry of this quality and coverage represents a unique opportunity to explore the HD 209458 transiting system. The star is not too bright for the MOST direct imaging mode ($V = 7.65$), and it is well placed in the MOST CVZ, observable for up to about a month and a half. MOST data have many applications to this system: (1) accurate transit timing to refine the near-zero orbital eccentricity and check for effects of orbital precession, (2) studies of the shapes of transit ingress and egress to search for large moons around HD 209458b, (3) searching for transits of other smaller planets in the systems with different orbital periods, as predicted by some models to explain the dynamical stability of HD 209458b (e.g., Ida & Lin 2004), (4) revealing subtle intrinsic variability in the star HD 209458a and possible interactions with the close-in planet, and (5) detection of the eclipse of HD 209458b in optical light to directly measure the geometric albedo of the planet.

In this paper, we report on MOST observations and analysis for eclipse detection in this system. In the next two sections, we describe the data and the MOST direct imaging reduction scheme, as a reference for MOST direct imaging results published here and elsewhere. We then present the reduced photometry of HD 209458, the eclipse analysis, and the upper limit on the depth of the eclipse. We translate this into an upper limit on the optical albedo of the exoplanet, and discuss its implications in atmosphere and cloud models. Finally, we predict the impact of future planned MOST observations of HD 209458 and the potential for other known transiting exoplanet systems.

2. MOST DIRECT IMAGING PHOTOMETRY

MOST is a microsatellite (mass 54 kg, peak solar power 39 W) with limited onboard processing capability, memory, and downlink. Hence it is not possible to transfer the entire set of 1024 × 1024 pixels of the Science CCD to Earth at a rapid sampling rate and with an analog-to-digital conversion (ADC) of 14 bits (necessary to preserve variability information at the ppm level). Small segments of the CCD (“subrasters”) are stored, which contain key portions of the target field. This usually includes the Primary Science target Fabry image, 7 adjacent sky background Fabry images, and subrasters for dark and bias readings.

2.1. Data Format

There is also the option to sample several nearby secondary science targets in the direct imaging field (less than about 0.5° away), by placing subrasters of typical dimensions 20 × 20 pixels over those stars. These targets are automatically monitored with the same sampling as the primary Fabry imaging target. The Fabry image illuminates about 1500 pixels, while each direct image illuminates a point-spread function (PSF) out to a radius of several pixels. When simultaneously observing Fabry and direct imaging targets to avoid saturation, the direct imaging targets must be at least 5.5 mag fainter than the Fabry target. For example, for MOST’s first Primary Science target, Procyon, the $V = 8$ star HD 61199 was chosen for the direct imaging field and was discovered to be a multiperiodic δ Scuti pulsator (see Fig. 2c in Matthews et al. 2004) with a peak amplitude of about 1 mmag.

It is also possible to select a star as bright as $V = 6.5$ as the principal science target in the direct imaging field, without a brighter Fabry target. Then the exposure time and sampling rate can be optimized for the direct imaging target. This was the case for HD 209458 ($V = 7.7$).

When the binary data stream is transferred from the satellite, it is converted to a FITS format image. The layout is shown in Figure 1. The locations of each subraster in the MOST Science CCD (in x-y pixel coordinates) are specified in the FITS file header. Typically, the FITS file contains resolved subrasters for the Fabry image, 2–4 direct images and 1 dark. The header also contains the pixel sums for various bias and dark regions, as well as satellite and instrument telemetry (e.g., spacecraft attitude control data; CCD focal plane temperatures) to allow additional photometric calibrations on the ground. The data format is unique to MOST, which necessitated the development of custom software to handle and process MOST data. Examples of MOST raw data and a document describing the FITS file and header format in detail are available in the Public Data Archive at the MOST Mission Web site.3

2.2. Photometric Reduction

In general, the approach to reducing MOST direct imaging photometry is similar to ground-based CCD photometry, applying traditional aperture and PSF approaches to the subrasters. However, there are several aspects and challenges specific to MOST data. For example, the MOST instrument has no onboard calibration lamp for correction of pixel-to-pixel sensitivity variations (“flat-fielding”). In its orbit, MOST passes through a region of enhanced cosmic-ray flux known as the South Atlantic Anomaly (SAA). There are also phases of increased stray light from scattered earthshine that repeat regularly during each satellite orbit ($P = 101$ minutes).

3 See http://www.astro.ubc.ca/MOST.
2.2.1. Dark Correction

To lower cost and increase reliability, the MOST instrument has no moving parts, so there is no mechanical shutter that can cut off light to the entire CCD for dark measurements; exposures are ended by rapid charge transfer into a frame buffer on the CCD. Dark measurements are obtained from portions of the CCD shielded from light by a chromium mask above the focal plane.

One-dimensional dark current correction is done by using averages from these dark subrasters; the averages are computed on the satellite, and the full raster information is not available on the ground (to meet downlink limitations while maximizing the amount of stellar data available). The values for each dark region are weighted in the average by the number of pixels in each subraster. There are usually four dark measurements available. If any of these individual readings deviates strongly (by more than 3σ) from the mean (likely due to a particularly energetic cosmic-ray hit), then that value is discarded.

2.2.2. Flat-Field Corrections

The MOST instrument was designed to obtain fixed extended pupil images of a single bright target star through a Fabry microlens. In this way, the Fabry imaging measurements are insensitive to pointing wander of the satellite. The direct images, however, do reflect the pointing errors. In data from the satellite commissioning and its early scientific operations, pointing errors of up to about 10′ led to wander of the direct images of up to 3 pixels on the CCD. This made precision photometry vulnerable to uncalibrated sensitivity variations among adjacent pixels. The pointing performance of the satellite has been improved dramatically since its early operation, now consistently giving positional errors of about ±1″ ~ 0.3 pixel rms (see § 2.2.3).

Despite the lack of an onboard calibration lamp, it is possible to recover some flat-fielding information for each subraster by exploiting intervals of high stray light during certain orbital phases. Frames containing no detectable stars are chosen from the data set. Such frames can be obtained when the satellite is commanded to point to an “empty” field (with only stars much fainter than \( V = 13 \), or occasionally, when the satellite loses fine pointing and the stars wander outside their respective subrasters. During two weeks of observing, over which 50,000–100,000 individual exposures are typically obtained, about 2000–4000 flat-fielding frames are usually available from when the satellite loses fine pointing.

The stray light can produce a strong spatial gradient across the CCD, so a two-dimensional polynomial is fitted to all the available flat-fielding pixels and removed. For each subraster, the mean pixel value is measured and compared to each individual pixel value; a linear fit to the correlation is made. The slope of this relationship is the relative gain, and the zero point is the dark current. The relative pixel gains are found to vary by less than 2% across any individual subraster, with the standard deviation for any individual pixel less than 0.5%.

2.2.3. Star Detection and Centroiding

We employ two methods for star identification. The first method involves deconvolving the individual subrasters with a model PSF. The model PSF is created by registering subrasters containing stars and mapping the pixel values onto an over-sampled grid to create a model profile with twice the resolution of a real image. After deconvolution the strongest source is chosen as the target star for photometry. The second method starts by prompting the user to identify by eye stars on each subraster via a graphical interface, which is particularly useful for fields containing several stars.

Once the stars have been identified, centroids are computed by an intensity-weighted average on a 5 × 5 grid around each object of interest. On the first frame the centroids for all the stars are saved as a master grid used to check the positioning for all subsequent frames. After the first frame the strongest source is always selected using the deconvolution technique, and its position is calculated with intensity-weighted means. This is done for each subraster, and the offsets are compared to the master grid of centroids. If the position of a star varies by more than 2 pixels, then that centroid is corrected by using the average offset from the remaining objects. This correction is particularly important when cosmic rays interact with the detector and can mimic a stellar PSF, leading to the occasional spurious star identification.

The pointing performance of MOST has been dramatically improved since its original on-orbit commissioning, thanks to upgraded software and a better understanding of the mechanical performance of the reaction wheels in its attitude control system. In Figure 2 the distribution of pointing centroids for three fields observed from 2003 December to 2004 August are shown. The first is for the star HD 263551 in the field of \( \xi \) Geminorum (observed during 2003 December 20–28); the second, for HD 61199 in the field of primary target Procyon (2004 January 8–February 9); and the third, for HD 209458 itself (2004 August...
14–30). The standard deviation for each target in $x$ and $y$ pixel directions are (0.985, 1.945), (0.947, 1.837), and (0.309, 0.403), respectively. The substantial improvement in tracking stability has resulted in improved photometry precision as flat-fielding errors have become less relevant.

2.2.4. Stray Light and Background Determination

In order to remove the strong background gradients associated with stray light, a two-dimensional second-order polynomial is fitted to the subrasters based on the pixel coordinates on the CCD and subtracted. A “sky radius” is defined, centered on selected stars. Only pixels outside this radius are included in the polynomial fit, to minimize influence from stellar sources.

Once the gradient has been suppressed, the background level for each subraster is determined by rejecting pixels with levels more than 2.5 standard deviations from the median to eliminate cosmic-ray hits. The rejection of pixels is iterated until the median converges, and the background is defined as the mean of the remaining pixel set. The median is chosen for the calculation of the standard deviation, since the small subraster sizes limit the total number of pixels available for background determination, making the mean sensitive to errant values, mostly due to cosmic-ray events.

2.2.5. PSF Fitting and Adding Up the Starlight

After determination of the star positions and the background, the PSF for each star is fitted by either a Moffat profile (Moffat 1969) or a Gaussian function. In general it is found that the Moffat profile provides a better approximation of the PSF shape (even though it was designed to reproduce stellar images smeared by atmospheric seeing). The difference between a Gaussian and Moffat profile is that the wings of the latter fall off much more slowly, accounting for the scattering profile at large off-axis distances, whether in the Earth’s atmosphere or in space, including telescope optics. The PSF is computed independently for each subraster using the Levenberg-Marquardt approach (Press et al. 1992, p. 678) to find the best-fit parameters. The background level can be allowed to vary with the fit minimization procedure, but we find that better photometry is obtained by fixing the level as determined by the procedure outlined in § 2.2.4.

For data sets obtained early in the mission lifetime, when the tracking performance was not ideal, such as with ξ Gemini, multiple images of the same source can appear on the subraster. In these cases, once the initial PSF fit has been made, the fit is removed, and the residual image is deconvolved using a predetermined instrumental PSF. The strongest peak is then identified, and the original subraster data are fitted with both centroids. This process is iterated until the deconvolved image has no significant peaks.

Once the stellar source has been modeled, the total flux is estimated by using aperture photometry for the center of the model fit and using the model fit for the faint extended wings. For cases such as ξ Gemini, this step is important, as the aperture accounts for the smearing effects of pointing jitter not included in the model, and the model allows an estimation of stellar flux located outside the subraster. The FWHM of the PSF under good tracking is found to be about 2 pixels, but the stellar source can be easily traced out to a radius of 8 pixels, meaning that for large pointing deviations, a significant portion of flux can lie outside the subraster. With HD 209458, where the pointing accuracy is greatly improved, only the PSF model is necessary to determine the brightness of the source. The final magnitude is defined as

$$\text{mag} = 25.0 - 2.5 \log \left( \frac{F_p + F_a}{E_t} \right)$$

as the standard conversion between magnitude and flux, where $F_p$ is the flux in analog-to-digital units (ADU) measured from the PSF fit, $F_a$ is the flux residual inside a small aperture in ADU, $E_t$ is the exposure time in seconds, and $g$ is the gain in e⁻ ADU⁻¹. The zero point of 25 has been arbitrarily chosen.

2.2.6. Removal of Stray Light Effects

Once the instrumental photometry has been extracted, variable stray light effects must be removed. It was discovered that the background level determined in § 2.2.4 needs to be scaled to
propably remove the contribution from stray light. The cause of this effect may be because the two-dimensional fits (see § 2.2.4) are not sufficient. With the small number of subraster pixels, a higher order polynomial is not stable enough, and hence the estimation of the background level is not optimum. Regardless, it can be corrected. In Figure 3, the relationship between instrumental magnitude and the background level is shown. A fit is made between the stellar flux and the background level with either a polynomial or a cubic spline, depending on the complexity of the relationship. If the relationship is modeled with a cubic spline, then the original data are binned before the fit, with 500 data points per bin and a minimum bin width of 10 ADU per pixel. In most cases the peak-to-peak amplitude of stray light variations is reduced by this approach to a few ×0.1 mmag. It can be further reduced by techniques such as subtracting a running averaged background phased to the orbital period (Rucinski et al. 2004). The advantage of the simple approach taken here is that no prior knowledge of the orbital period is required, and the amplitude of the stray light component is allowed to vary from orbit to orbit with changes in the Earth’s albedo.

3. HD 209458

3.1. Observations

Observations of HD 209458 were made during 2004 August 14–30, as part of a relatively short trial run on this star. This star is accessible to MOST in its CVZ (see § 1) for approximately 45 days, but this was the first opportunity to test the direct imaging mode on an exoplanetary system target. The exposure time was 1.50 s (regulated to better than 1 μs). Sampling rates were varied. During most of the run, to stay within downlink margins for the MOST ground station network, data were collected at a rate of 5 per minute. For 15 hr centered on the predicted times of exoplanetary eclipse, the sampling rate was increased to 10 per minute. This improved our sensitivity to eclipses, while staying within the MOST onboard buffer capacity so no data would be lost in the event of a malfunction of one of the three ground stations.

There were data losses in the first third of the run due to crashes of the satellite’s control system (ACS) when subtle bugs in new software (which had operated smoothly during the previous month of observations on another target) manifested themselves. Once the problem was traced, the previous version of the software was uploaded to the satellite, and observations continued with only one brief interruption due to a cosmic-ray-induced crash. The overall duty cycle of the raw photometry is about 85%.

Near the solstices, the contributions of scattered earthshine (stray light) in the MOST focal plane reach their peak. For a bright Fabry imaging target, the stray light can be less than 1% of the stellar signal. For a fainter direct imaging target like HD 209458 (V ~ 7.7), there is an interval during each orbit where the stray light is high enough to seriously degrade the quality of the photometry. Whenever the background level exceeded 300 ADU pixel⁻¹ in an exposure, that measurement was excluded from the analysis. This represents about 25 minutes from each 101.413 minute orbit, reducing the total duty cycle to 53% but still providing thorough coverage of the times of transit and eclipse.

There is an unfortunate coincidence between the orbital period of the HD 209458 exoplanet around its parent star and the orbital period of the MOST satellite around the Earth. The ratio of the two periods is 50.049, so that over the 2 week span of the MOST observations, the satellite orbital period maintains rough phasing with the exoplanet ephemeris.

MOST was designed to be a nondifferential photometer in its Fabry mode, but in the direct imaging there can be other stars in the field appropriate as photometric comparisons. In the HD 209458 field, two other relatively bright stars were also monitored, HD 209346 (V = 8.33) and BD +18 4914 (V = 10.60) (see Table 1). Even the brighter of these two is almost 0.7 mag fainter than HD 209458, so differential photometry tends to add noise to the point-to-point scatter and degrade the sensitivity to eclipses. However, it does provide a check for slow instrumental and/or environmental drifts. It was noticed that the data for HD 209458 during JD 1693–1693.5 (JD 2,451,545.5) showed a slow trend that was not present in HD 209346. This change was approximately 0.005 mag. This could represent intrinsic variability in the star HD 209458a. Since we are interested in variations due to phase changes of the planet over the orbital period, one cannot fit the trend and restore the data without perturbing trends due to the planet, so it was excised from this analysis. This stretch of data did not overlap with a phase of transit or eclipse, thus its exclusion has minimal effect for detection of the secondary eclipse.

The reduced light curves for HD 209458 and HD 209346 are shown in Figures 4a and 4b. The primary transits in the HD 209458 system are obvious, as are the regular gaps during each satellite orbit in which data were removed due to high stray light.

Next, any residuals due to the orbital period where removed from both light curves by fitting an equation of the form

\[
mag = A_0 + \sum_{j=1}^{n} A_j \cos (j \omega t + \phi_j),
\]

where \(A_0\) is the mean magnitude, \(A_j\) and \(\phi_j\) are the amplitude and phase coefficients for the cosine series, \(\omega\) is \((2\pi\text{ per}\ \text{period})\), and \(n = 8\) was chosen to accommodate the nonsinusoidal shape of the stray light residuals. Long-term trends in the light curve for HD 209458 were removed by binning the comparison stars with 0.2 day bins and interpolating with a cubic spline. The last step was to fit a 1 cycle day⁻¹ variation in the data (peak-to-peak amplitude 1.3 mmag) in the data, likely due to the fact that the MOST satellite returns to a similar albedo feature on the Earth each day.
The final reduced data are presented in a phase diagram in Figure 4c, using the ephemeris for HD 209458b determined by Wittenmyer et al. (2005), with an exoplanetary period of 3.52474554 days. The “tire-track” pattern in the data is due to the intervals of high stray light subtracted from each MOST orbit and the near-harmonic relationship between the orbital periods of the exoplanet and the MOST satellite. Unfortunately, intervals of high stray light happened in this data set to coincide with the phases of ingress, minimum, and egress of the exoplanetary transits. The primary transit is obvious in Figure 4c; the range of phases of the secondary eclipse is marked in the figure.

4. UPPER LIMIT ON THE ECLIPSE

To search for evidence of an eclipse in the light curve, we apply a model of the light variations due to the reflected light of the exoplanet, which is shown schematically in Figure 5. We neglect any intrinsic variability of the star in this version of the model. During segment “A” of the phase diagram, the planet is totally eclipsed by the star, and the system has a total magnitude of $y_2$. As the planet moves in its orbit toward inferior conjunction at point “D” (middle of transit), the illuminated fraction of the planet disk decreases. The points of maximum brightness occur at phases $x_1$ and $x_2$, where the planet is almost fully illuminated; minimum brightness (outside of transit) occurs at phases $x_3$ and $x_4$, where we see the night side of the planet.

We can set up a simple model to approximate the expected phased light curve by a series of straight lines connecting the points $x_1$, $x_2$, $x_3$, and $x_4$. In reality these points should be connected by slowly varying curves, but our first-order approximation is valid considering the star-planet flux ratio is greater than 10,000.
where we have adopted the formalism of Gregory (2005, pp. 41–65). The term \( H \) is our hypothesis of interest, \( D \) is our data set, and \( I \) is our current state of knowledge. Starting with \( p(y_1, y_2|D, I) \), we obtain an expression for the probability of \( y_2 \) by marginalizing over \( y_1 \), giving us

\[
p(y_2|D, I) = \frac{p(y_2|I)}{p(D|I)} \int p(y_1|I)p(D|y_1, y_2, I) \, dy_1, \tag{7}
\]

where we have chosen a Jeffrey’s prior,

\[
p(y|I) = \frac{1}{y \ln(y_{\text{max}}/y_{\text{min}})} \tag{8}
\]

to give equal probability to all parameters, where \( y_{\text{min}} = -0.3 \) mmag and \( y_{\text{max}} = 0.3 \) for both \( y_1 \) and \( y_2 \). These were chosen based on the scatter seen in the binned phased light curve shown in Figure 4d. We repeated all calculations using a uniform prior and found no change in our results, as our parameter range is well constrained by the data set. Since the data set is well constrained, it should be noted that a maximum likelihood analysis will give similar results, as the probability distribution is not strongly affected by our prior. The likelihood function is given by

\[
p(D|y_1, y_2, I) = \exp(-\chi^2) \prod_{i=1}^{n} \frac{1}{\sqrt{2\pi\sigma_i}} e^{-\frac{1}{2}\left(\frac{d_i - f(x_i; y_1, y_2)}{\sigma_i}\right)^2}, \tag{9}
\]

where \( f(x; y_1, y_2) \) is given by equations (3)–(5), \( d_i \) are the observations, \( \sigma_i \) are the photometric errors for each observation, \( n \) is the number of observations, and the normalization factor is

\[
p(D|I) = \int \int p(y_1|I)p(y_2|I)p(D|y_1, y_2, I) \, dy_1 \, dy_2. \tag{11}
\]

Using all available data, except during high levels of earthshine, we find that \( y_2 - y_1 = -0.08 \pm 0.05 \) mmag (90% confidence), which would imply the system is getting brighter during the planetary eclipse. The confidence levels are plotted in Figure 6. In this analysis, we have not accounted for potential intrinsic variations in the star. To make our analysis less sensitive to longer term variability in the star, we restricted the data set to phases bracketing the eclipse, defining three bins of equal size: one extending from \( x_1 \) to \( x_2 \) and two other bins of equal size \((x_2 - x_1) \) adjacent to the eclipse. Our initial choice of \( x_1 \) and \( x_2 \) to occur in the data gaps also means that the new adjacent boundaries occur at data gaps. This means that each bin will have approximately the same signal-to-noise ratio. We then recalculated the probabilities for \( y_1 \) and \( y_2 \), which we plot in Figure 7 using 1, 2, and 3 \( \sigma \) confidence levels for a two-dimensional distribution. The best-fit parameters for the value of \( y_2 - y_1 \) are then obtained from the maximum of equation (7), where we have adjusted the mean of the data set so that \( y_1 \) is equal to zero. Our detection limits are summarized in Table 2. Our fit is consistent with no detection of an eclipse, but it does allow us to place an upper limit and confidence interval on the photometric depth of the eclipse. We also repeated our analysis via a \( \chi^2 \) minimization analysis. In this case one minimizes
equation (10), and we get a best fit for \( y_1/y_0 = 0.018 \) mmag. Thus our answers remain unchanged under this type of analysis, as our choice of prior does not strongly affect our probability distribution.

5. UPPER LIMIT ON THE ALBEDO OF HD 209458B

In this section we derive the upper limit on the planet-star flux ratio and convert it to an upper limit on the geometric albedo. We convert the secondary eclipse upper limit value from magnitudes to a planet-star flux ratio using the standard equation for the definition of magnitude,

\[
y_1/y_0 = 2.5 \log \left( \frac{F_p + F_*}{F_*} \right).
\]

We take the error on the secondary eclipse \( y_1/y_2 \) as the eclipse upper limit, because the scatter in the data is larger than the putative eclipse measurement. Table 2 lists the upper limit (derived in § 4) for different confidence levels. Here we work with the 1 \( \sigma \) (or 68.3% confidence level) eclipse upper limit value, which is 0.053 mmag.

Using the eclipse upper limit \( y_1/y_2 = 0.053 \) mmag, the planet-star flux ratio upper limit is

\[
F_p/F_* \leq 4.88 \times 10^{-5}.
\]

The albedo is a more intuitive form of the planet-star flux ratio, since it describes the fraction of stellar radiation that is scattered by the planet.

The geometric albedo, \( A_g \), is the quantity relevant to the MOST measurement. It is defined as the ratio of the planet’s luminosity at full phase to the luminosity from a Lambert disk\(^4\) with the same cross-sectional area as the planet, and is equivalent to the fraction of incident stellar radiation scattered in the direction of the observer for planetary full phase (if the stellar intensity is spatially uniform). The MOST measurement occurs over a range covering 7° on either side of full phase and is close enough to full phase that we use the geometric albedo terminology.\(^5\) This \( A_g \) is usually specified at a particular wavelength, so we use \( A_g^{\text{MOST}} \) for the geometric albedo integrated over the MOST bandpass (400–700 nm; see Table 3) and \( A_g^{\text{TOT}} \) for the geometric albedo integrated over all wavelengths.

The \( A_g \) is related to the planet-star flux ratio by

\[
\frac{F_p}{F_*} = A_g \left( \frac{R_p}{a} \right)^2,
\]

where \( R_p \) is the planetary radius, and \( a \) is the semimajor axis. Taking \( R_p = 1.35 \pm 0.06 R_J \) (Brown et al. 2001) and \( a = 0.046 \) AU

\(^5\) Strictly speaking \( A_g \) is defined only at full phase. However, the MOST measurements are close enough to full phase that we use this familiar term.

| TABLE 2 | ECLIPSE OF HD 209458b |
|--------|---------------------|
|        | PARAMETER | BEST FIT | CONFIDENCE LEVEL |  |
|        | \( y_1/y_0 \) (mmag) | 0.013 | 0.053 | 0.105 | 0.145 |
|        | \( F_p/F_* \) | \( 1.20 \times 10^{-5} \) | \( 4.88 \times 10^{-5} \) | \( 6.76 \times 10^{-5} \) | \( 1.34 \times 10^{-4} \) |
|        | \( A_g \) | 0.06 | 0.25 | 0.49 | 0.68 |

**Notes.**—Best-fit parameters for the eclipse of HD 209458b. The confidence levels correspond to the 1, 2, and 3 \( \sigma \) levels, respectively. The first row gives the ranges for the fit of \( y_1/y_0 \) in mmag. The second row gives the corresponding flux ratio of the planet to the star for the MOST bandpass calculated using eq. (12). The third row gives the geometric albedo \( A_g \) using eq. (14).

\(^4\) A Lambertian surface is an ideal, isotropic reflector at all wavelengths.
(Mazeh et al. 2000), \(A_{\text{gMOST}} \leq 0.25\). The 5% uncertainty in planet radius translates into a \(\sim 10\%\) uncertainty in \(A_{g}\). We therefore more accurately state our HD 209458b 1 \(\sigma\) geometric albedo upper limit as

\[
A_{g\text{MOST}} \leq 0.25 \left(\frac{3.15}{R_p}\right)^2. \quad (15)
\]

6. DISCUSSION

HD 209458b’s geometric albedo of \(\leq 0.25\) is a relatively low value. The solar system giant planet albedos in the MOST bandpass are \(\gtrsim 0.4\), with Jupiter’s value 0.5 (computed from data in Karkoschka 1998; see Table 4). HD 209458b is therefore less than half as bright as Jupiter at the MOST wavelengths.

The solar system giant planets all have bright cloud decks (water ice or ammonia ice), which cause them to be bright in the MOST bandpass. HD 209458b is an order of magnitude hotter than Jupiter, far too hot for water or ammonia clouds to be present. HD 209458b may have clouds in its atmosphere, but composed of high-temperature condensates such as silicates or solid iron, instead of ices. Clouds at high altitude are consistent with previous observations of the HD 209458b atmosphere, including a primary transit low sodium absorption (Charbonneau et al. 2002), a primary transit CO nondetection (Deming et al. 2005a), and a secondary eclipse nondetection of H\(_2\)O at 2.2 \(\mu\)m (Richardson et al. 2003). If clouds are present in the HD 209458b atmosphere, the low \(A_{g\text{MOST}}\) rules out any bright clouds at high altitudes. Unlike ice clouds, high-temperature condensate clouds may be dark if they consist of small particles or are predominantly Fe (see Fig. 5 in Seager et al. 2000). If HD 209458b does not have clouds, strong sodium and potassium atomic absorption could be present on the day side and cause a low albedo in the MOST bandpass. While \(A_{g\text{MOST}}\) is not definitive, it is a key constraint on HD 209458b atmosphere models with specific regard to the thickness, altitude, composition, and particle size distribution of clouds. Our measurements are consistent with the results of Collier Cameron et al. (2002) and Leigh et al. (2003), who also find low albedo upper limits for the short period planetary companions of \(\upsilon\) And and HD 75289, which have orbital periods of 4.6 and 3.5 days, similar to HD 209458b.

With an upper limit determined for the measured geometric albedo a natural question is can we estimate the Bond albedo? The Bond albedo, \(A_B\), is the total radiation reflected from the planet compared to the total incident radiation, i.e., the total amount of radiation reflected in all directions integrated over all wavelengths. The \(A_B\) is an important physical parameter because it specifies the amount of stellar radiation absorbed by the planet and hence the equilibrium temperature of the planet,

\[
T_{\text{eq}} = T_s \left(\frac{R_s}{2a}\right)^{1/4} \left[f(1-A_B)\right]^{1/4}, \quad (16)
\]

where \(R_s\) is the stellar radius, \(T_s\) is the stellar effective temperature, \(a\) is the semimajor axis, and \(A_B\) is the Bond albedo. Here, \(f\) is the proxy for atmospheric circulation, \(f = 1\) if the absorbed stellar radiation is redistributed evenly throughout the planet’s atmosphere (e.g., due to strong winds rapidly redistributing the heat) and \(f = 2\) if only the heated day side radiates the energy. Figure 8 shows \(T_{\text{eq}}\) for the HD 209458b parameters (\(T_s = 6000\ K, R_s = 1.18\ R_J,\) and \(a = 0.046\ AU;\)

| Planet          | MOST Bandpass | All Wavelengths | Bond Albedo |
|------------------|----------------|-----------------|-------------|
| HD 209458b       | \(\leq 0.25\) | ...             | ...         |
| Jupiter          | 0.50           | 0.274 \pm 0.013 | 0.343 \pm 0.032 |
| Saturn           | 0.47           | 0.242 \pm 0.012 | 0.342 \pm 0.030 |
| Uranus           | 0.43           | 0.208 \pm 0.048 | 0.290 \pm 0.051 |
| Neptune          | 0.38           | 0.25 \pm 0.02   | 0.31 \pm 0.04  |

Notes.—Albedo of HD 209458b compared to albedos of the solar system giant planets. Solar system planet geometric albedo in the MOST bandpass computed from Karkoschka (1998), and other solar system planet albedos from Voyager, Pioneer, and ground-based measurements described in Conrath et al. (1989).
Mazeh et al. 2000; Cody & Sasselov 2002). The top left quadrant represents our parameter range space based on 1 σ limits.

In principle $A_B$ could be measured for a transiting extrasolar planet if its brightness at all phases could be measured in a wavelength range that encompasses all the planet’s scattered light. However, HD 209458 is too faint for such a measurement by MOST, and MOST’s bandpass has a cutoff at 0.7 μm (Table 3). Nevertheless, we estimate an $A_B$ upper limit for HD 209458b, based on the solar system planet albedos, the $A_{g\text{TOT}}/A_B$ relation, and model atmosphere considerations.

The solar system giant planets all have $A_B > A_{g\text{TOT}}$, as illustrated in Figure 9. This can be understood by considering a Lambertian planet, with $A_B = 1$; $A_{g\text{TOT}}$ would then have to be <1, since $A_g$ includes only the radiation scattered back toward the observer. More precisely, for a Lambert sphere $A_B = 1.5 A_{g\text{TOT}}$ (Lambert’s law is the dotted line in Fig. 9). Under the reasonable assumption that HD 209458b is a gas giant planet with a thick atmosphere and no reflecting surface, we can confine our attention to the very general theoretical case described by a semi-infinite atmosphere model. In this case the physically relevant albedo parameter space in Figure 9 is bound by the dashed and dotted lines, $0.67 < A_{g\text{TOT}}/A_B < 1$ (e.g., Sobolev 1975). Indeed, the solar system giant planet albedos comply (Conrath et al. 1989; reproduced in Table 4). Therefore, under the simplest case assumptions about the atmosphere of HD 209458b, we can use the isotropic scattering limit (dotted line) in order to derive an upper limit on its $A_B$. Multilayer atmosphere models and other complications can produce geometric albedos below that limit by no more than ~10% (see Sobolev 1975).

One further assumption is required in order to estimate HD 209458b’s $A_B$ from the $A_{g\text{MOST}}$ upper limit, $A_{g\text{TOT}} = A_{g\text{MOST}}$. We first note that $A_{g\text{TOT}} < A_{g\text{MOST}}$ for solar system planets because of strong CH4 absorption redward of the MOST bandpass but blueward of the wavelength where their thermal emission dominates over scattered radiation. HD 209458b is an order of magnitude hotter than the solar system giant planets and should differ. If HD 209458b were a blackbody emitter, its thermal emission would peak around 2–5 μm (depending on its actual equilibrium temperature). HD 209348b, however, is expected to deviate significantly from a blackbody. Near-IR molecular absorption could induce thermal emission at as short a wavelength as 0.8 or 0.9 μm (see Seager et al. 2005 and references therein). In low geometric albedo models, the thermal emission could dominate over scattered radiation at such a short wavelength and $A_{g\text{TOT}} \approx A_{g\text{MOST}}$ is not too unreasonable. With $A_{g\text{TOT}}$ and the 0.67 < $A_{g\text{TOT}}/A_B < 1$ argument (Fig. 9), we estimate for HD 209458b that $A_B \leq 0.375$.

From equation (16) this value of $A_B$ gives $T_{eq} > 1300$ K. In Figure 8 we show how this estimated $A_B$ value together with the Spitzer MIPS 24 μm brightness temperature measurement of 1130 K (Deming et al. 2005a) constrain the overall $T_{eq}$ of HD 209458b.

A more robust $A_B$ estimate requires detailed model computations, beyond the scope of this paper. Because of a wide viable parameter space (Seager et al. 2005, and references therein), however, more data are required before a definitive HD 209458b model atmosphere can be computed. Indeed, strong H2O near-IR absorption has not yet been detected (Richardson et al. 2003; Seager et al. 2005). Upcoming data, including Spitzer programs for secondary eclipse thermal emission measurements (photometry from 3.5 to 8 μm and spectra from 7.4 to 14.5 μm) and Hubble Space Telescope (HST) primary transit data analysis for H2O absorption (T. Brown 2005, private communication) will help constrain models and thus the $A_B$ estimate.

In summary, MOST has observed HD 209458 for 14 days, and we have derived an upper limit on the planet-star flux ratio of $4.88 \times 10^{-3}$, corresponding to a geometric albedo of ≤0.25 at the 1 σ level. These numbers at the 3 σ level are $1.34 \times 10^{-3}$ and 0.68, respectively. During a second HD 209458b observing...
campaign 3 times longer than the one described in this paper, \textit{MOST} will either detect the secondary eclipse or put a significant limit on it to a geometric albedo of 0.13 (1σ) or 0.34 (3σ). As the only existing constraint on scattered light from HD 209458b, the \textit{MOST} geometric albedo upper limit will play a pivotal role in constraining HD 209458b atmosphere interpretations.

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