Kaon interferometric probes of space-time evolution in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV

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Bose-Einstein correlations of charged kaons are used to probe Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV and are compared to charged pion probes, which have a larger hadronic scattering cross section. Three dimensional Gaussian source radii are extracted, along with a one-dimensional kaon emission source function. The centrality dependences of the three Gaussian radii are well described by a single linear function of $N_{\text{part}}$ with zero intercept. Imaging analysis shows a deviation from a Gaussian tail at $r > \sim 10$ fm, although the bulk emission at lower radius is well-described by a Gaussian. The presence of a non-Gaussian tail in the kaon source reaffirms that the particle emission region in a heavy ion collision is extended, and that similar measurements with pions are not solely due to the decay of long-lived resonances.
Experiments at the Relativistic Heavy Ion Collider (RHIC) at Brookhaven National Laboratory have revealed that collisions of Au ions at $\sqrt{s_{NN}} = 200$ GeV produce a new form of matter which is opaque to jets and exhibits anisotropic flow consistent with perfect fluid hydrodynamics \[1, 2\]. Studies of the space-time evolution of the collisions are needed to elucidate the properties of the hot, dense, and strongly interacting matter, probe the time scale and degree of thermalization, and investigate the order of the deconfinement phase transition.

Two-particle interferometry, also known as HBT after the radio astronomers R. Hanbury Brown and R.Q. Twiss \[3\], is a powerful tool for measuring the space-time extent of particle-emitting sources. In elementary particle and nuclear physics, enhanced production of like-sign pions with small relative momenta was discovered experimentally and explained by the Bose-Einstein symmetrisation of identical bosons \[4\]. Correlations are produced by the combination of quantum mechanical interference of identical particles and strong and/or electromagnetic final state interactions such as Coulomb repulsion for same-sign charged pairs. HBT radii refer to Gaussian measures of source sizes on the femtometer scale.

Although the traditional HBT analyses are constrained by the assumption of a Gaussian distribution of particle emission, recent detailed measurements of pion emission sources using an imaging technique show a non-Gaussian structure for the two-particle source region above $\sim 20$ fm \[5\], suggesting the possibility that decays of long-lived resonances or a temporal component of the source contribute to the non-Gaussian tails \[6\]. While charged pions are strongly affected by rescattering among hadrons and decays of hadronic resonances, charged kaons have smaller rescattering cross sections than charged pions ($\sigma_{K^-N} < \sigma_{\pi^-N}$) and are less affected by resonance decays. Until recently, no full hydrodynamic calculation has accurately predicted particle spectra and HBT radii for pions, and none can simultaneously describe the momentum asymmetry measurements of flow. The measurement of the kaon source structure herein add an important new constraint to address this “HBT puzzle” \[7, 8\].

An angle-averaged one-dimensional Gaussian measurement of correlations of neutral kaons by STAR \[9\] suggests that the transverse mass dependence for neutral kaons and charged pions falls on one universal curve. In this paper, 3D Gaussian HBT correlations of like-sign kaons are presented in three transverse momentum bins for $0.3 < p_T < 1.5$ GeV/c and three collision centrality bins. The resulting HBT radius parameters for kaons are compared to those of like-sign pion pairs \[10\]. In addition we present 1D emission source functions for charged kaons in relativistic heavy-ion collisions.

This analysis of 2004 data from the PHENIX detector \[11\] uses $\sim 600$ million minimum bias events, which are triggered by the coincidence of the Beam-Beam Counters (BBC) and Zero-Degree Calorimeters (ZDC) with collision vertex $|z| < 30$ cm. A Monte Carlo Glauber model \[12\] is used to match the observed BBC and ZDC distributions and to bin the data according to the number of nucleons participating in the collisions, $N_{\text{part}}$.

Charged kaons are tracked and identified using the drift chamber (DC), pad chambers (PC1,PC3) and PbSc Electromagnetic Calorimeters (EMCal) to cover pseudorapidity $|\eta| < 0.35$ and azimuthal angle $\Delta \phi = \pi/2$ ($\Delta \phi = \pi/4$) in one (and the other) central arm. A track model provides a 3-dimensional trajectory and momentum vector for charged particles based on DC and PC1 information with a momentum resolution of $\delta p/p \approx 0.7\% \pm 1.0\% \times p$ (GeV/c). Backgrounds are reduced by requiring $2 \sigma$ position match between track projections and EMCal hits, and $3 \sigma$ match for PC3. Kaons are separated from pions up to $p_T \sim 0.9$ GeV/c using timing information from BBC and EMC. Particles at higher $p_T$ that fall within $2 \sigma$ of the ideal mass-squared for kaons but $\geq 3 \sigma$ away from the peak for pions or (anti-)protons are identified as kaons. The contamination level is $\sim 4\%$ from pions, and $\sim 1\%$ from protons at $p_T \sim 1.5$ GeV/c.

The correlation function is experimentally measured as $C_2(q) = A(q)/B(q)$ where $A(q)$ is the relative momentum ($q$) distribution of actual pairs obtained by all possible combinations of pairs within the same events and $B(q)$ is the background pair distribution from mixed events. Two-track detection inefficiencies for charged kaons that traverse the DC and EMCal in close proximity have been carefully studied with Monte-Carlo detector simulation and the actual pair distribution is corrected by the MC efficiency factors. After pair selection cuts to remove track splitting and merging (see \[10\] for details), $\sim 15$ million positive kaon pairs and 14 million negative kaon pairs remain.

To measure multi-dimension source sizes, $q$ is decomposed into standard “side-out-long” axes \[13\]: for which $q_{\text{long}}$ is parallel to the beam axis, $q_{\text{out}}$ is parallel to the transverse momentum of the pair ($k_T = (p_{T1} + p_{T2})/2$), and $q_{\text{side}}$ is orthogonal to both $q_{\text{long}}$ and $q_{\text{out}}$. This analysis is performed in the Longitudinally Co-Moving System (LCMS) defined as $p_{Tz} = -p_{2z}$. For the treatment of charged kaons emitted away from the central region (core), we adopt an effective core-halo Coulomb correction, proposed by Bowler and Sinyukov \[14\], in which the 3D Gaussian fit function is given by

$$C_2 = C_2^{\text{core}} + C_2^{\text{halo}} = \left[ \lambda (1 + G) \right] F_C + [1 - \lambda], \quad (1)$$

where the Coulomb correlation function $F_C$ is iteratively evaluated from the Coulomb wave function of kaon pairs.
assuming a spherical Gaussian source. The Gaussian correlation function in the side-out-long decomposition is determined by

\[ G = \exp \left( -R_{\text{side}}^2 \sigma_{\text{side}}^2 - R_{\text{out}}^2 \sigma_{\text{out}}^2 - R_{\text{long}}^2 \sigma_{\text{long}}^2 \right). \]  

The systematic error estimate incorporates a contribution from the Coulomb interaction of the source halo using a prescription developed by Maj and Mrowczynski. The fitted \( R_{\text{side}} \) and \( R_{\text{long}} \) are Gaussian measures of the spatial lengths of homogeneity, where particles of similar momenta are emitted, in the transverse and longitudinal directions at freeze-out. \( R_{\text{out}} \) contains a contribution from the duration of the particle emission in addition to the spatial length. Note that an out-long cross-term vanishes in the expression for \( G \) for our \( |y| < 0.35 \) acceptance at midrapidity. The fitted \( \lambda \) is empirically defined and includes contributions from mis-identified particles \((1-f)^2\) along with components of the source that are not well resolved by the Gaussian fit.

Figure 1 shows the 3D correlation function of charged kaons without the Coulomb correction measured for \( 0.3 < k_T < 1.5 \text{ GeV}/c \) at \( 0 - 30\% \) centrality in Au+Au collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \) and the fit with Eq. (1). Separate fits to the \( 2K^+ \) and \( 2K^- \) correlation functions were performed, yielding consistent results for all \( k_T \) and centrality bins.

Panels (a)-(e) in Fig. 2 show the HBT radius parameters of charged kaons for \( 0.3 < k_T < 1.5 \text{ GeV}/c \) as functions of \( N_{\text{part}}^{1/3} \), which is proportional to the transverse radius of the initial collision volume. Similar to pions, kaon radii are well described by linear functions of \( N_{\text{part}}^{1/3} \). Because initial fits yielded slopes that were consistent for all radii and intercepts that were consistent with zero, the all three radii were fit to a single linear function with zero intercept: \( R_i = p_i + N_{\text{part}}^{1/3} \), with \( p_i = 0.51 \pm 0.01 \) and \( \chi^2/\text{ndf} = 14.6/8 \). We note that similar fits to the pion radii yield non-zero intercepts. Although pions and kaons are measured in a similar \( k_T \) range \((0.2 < k_T < 2.0 \text{ GeV}/c \) for pions\), the higher transverse mass \((m_T = \sqrt{k_T^2 + m^2})\) for kaons \((\langle m_T \rangle \sim 0.89 \text{ GeV}/c^2\) than for pions \((\langle m_T \rangle \sim 0.47 \text{ GeV}/c^2\) leads to smaller radii, as expected from \( m_T \) scaling.

Panels (f)-(j) in Fig. 2 show the \( m_T \) dependence of the radius parameters for kaons in 3 different \( m_T \) bins at \( 0 - 30\% \) centrality, compared with pions [10]. HBT radii are quite consistent at the same \( m_T \), clearly indicating that the radii follow \( m_T \) scaling. The \( R_{\text{out}}/R_{\text{side}} \) ratio
for kaons is \( \sim 1.0-1.2 \) which is consistent with the value for pions at low \( m_T \). Kaon HBT results from a 2D+1 hybrid, hydrodynamic + UrQMD calculation (open circles) \( ^{22} \) show slightly larger sideways radii than the data, and the outwards and longitudinal components are too large by a factor of 2-3. A more recent 1D+1 hybrid calculation \( ^{23} \) for kaons (open squares), which assumes flat rapidity distribution and axial symmetry, compares more favorably, matching all radii to within systematic and statistical errors. This calculation incorporates pre-equilibrium flow and a lattice-inspired equation of state, which are two features lacking in earlier calculations of HBT radii. Although promising, these theoretical results remain to be verified with full 3D+1 calculations that can also reproduce the elliptic flow.

Recent femtoscopic measurements \( ^{5,6} \), which use an imaging technique \( ^{24} \) revealed that the emission source function of charged pions has a non-Gaussian tail which cannot be resolved with traditional Gaussian fitting techniques. In the imaging scheme, the correlation function is expressed by the Koonin-Pratt equation \( ^{25,26} \)

\[
C_2(\mathbf{q}) - 1 = \int dr K(\mathbf{q}, \mathbf{r}) S(\mathbf{r}),
\]

where the kernel \( K(\mathbf{q}, \mathbf{r}) \) is the relative wave function as \( |\Phi_\mathbf{q}(\mathbf{r})|^2 - 1 \) that describes the propagation of pairs emitted with relative separation \( \mathbf{r} \) and relative momentum \( \mathbf{q} \) in the Pair Center-of-Mass System (PCMS). \( S(\mathbf{r}) \) is the emission source function of pairs.

The filled squares in Fig. 3(a) show the 1D kaon correlation as a function of the invariant relative momentum of the pair \( q_{inv} = \sqrt{(p_1 - p_2)^2/2} \). The 1D source function \( S(\mathbf{r}) \) imaged from \( C_2(q_{inv}) \) is shown by filled circles in Fig. 3(b).

In this analysis, input parameters that govern the imaging procedure \( ^{24} \) were selected to minimize the \( \chi^2 \) between the data and the restored \( C_2(q_{inv})(\chi^2/ndf \sim 1) \), shown by open circles in Fig. 3(a). The solid curve shows the traditional Gaussian source function, obtained by angle-averaging the 3D HBT radius parameters (\( \lambda, R_{side}, R_{out}, R_{long} \)) in the PCMS frame, the same frame in which the imaging is performed.

The imaged \( S(\mathbf{r}) \) exhibits a non-Gaussian tail at \( r \gtrsim 10 \) fm. This excess corresponds to the deficit in the \( q_{inv} \lesssim 20 \) MeV/c region of the angle-averaged Gaussian curve of Fig. 3(a), and is also visible in the 3D Gaussian slices in Fig. 4. The \( S(\mathbf{r}) \) for pions in the same \( k_T \) range shows a similar trend. The deviation from a Gaussian in the shape of the \( S(\mathbf{r}) \) indicates that the particle emission region is extended, and a similar non-Gaussian tail in the pion source is not solely the result of long lived resonance decays such as the \( \omega \), although a less prominent contribution from the \( K^* \) is likely. The observation of a more substantial non-Gaussian tail for kaons than for pions is qualitatively consistent with a hadronic resonance cascade model with a time dependent tail for an expanding source, in which the larger mean free path for kaons leads to an extended emission region \( ^{23,28} \). Detailed measurements with 3D HBT imaging of kaons, or 1D imaging of more species probing different hadronic cross sections will determine contributions from other kinetic effects to \( S(\mathbf{r}) \).

In summary, we have measured Bose-Einstein correlation functions of charged kaon pairs in Au+Au collisions at \( \sqrt{s_{NN}} = 200 \) GeV. The 3D HBT radii \( R_{side} \) and \( R_{long} \) are consistent for pions and kaons at the same \( N_{part} \) and \( m_T \). The 1D emission source function for kaons extracted by imaging shows a non-Gaussian tail at distances greater
than 10 fm. This tail represents a direct measurement of the 1D length of homogeneity of the particle emission source and is not due primarily to resonance decays.

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