Predicted Growth of Two-Dimensional Topological Insulator Thin Films of III-V Compounds on Si(111) Substrate

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We have carried out systematic first-principles electronic structure computations of growth of ultrathin films of compounds of group III (B, Al, In, Ga, and Tl) with group V (N, P, As, Sb, and Bi) elements on Si(111) substrate, including effects of hydrogenation. Two bilayers (BLs) of AlBi, InBi, GaBi, TlAs, and TlSb are found to support a topological phase over a wide range of strains, in addition to BBi, TlN, and TlBi which can be driven into the nontrivial phase via strain. A large band gap of 134 meV is identified in hydrogenated 2 BL film of InBi. One and two BL films of GaBi and 2 BL films of InBi and TlAs on Si(111) surface possess nontrivial phases with a band gap as large as 121 meV in the case of 2 BL film of GaBi. Persistence of the nontrivial phase upon hydrogenations in the III-V thin films suggests that these films are suitable for growing on various substrates.

Topological insulators (TIs) in general, and the two-dimensional (2D) quantum spin Hall insulators in particular, have been receiving increasing attention in the last few years in both theoretical and experimental studies. These materials support conducting edge states in 2D and conducting surface states in 3D, even though their bulk states are insulating. These unique properties make topological insulator materials well suited for spintronics, quantum computing, and other applications due to the robustness of their edge/surface states against backscattering. In fact, a variety of atomically thin films in the buckled honeycomb structure of groups IV (Si, Ge, Sn)3–5, V (Bi, Sb, As)6–11, and III-V12–15 elements have been theoretically predicted to harbor topological insulating phases.

In order to be realized experimentally, however, a film must eventually be placed or grown on a suitable substrate. Effects of substrates, or environments more generally, can be simulated via hydrogenation or halogenation, and/or strains. Numerous studies attempting to explore such effects include work on films of silicene17–18, stanene19,20, Bi, Sb11–21, and group III-V compounds12–15. These studies demonstrate that substrates can be expected to induce substantial modifications in the electronic structures and band topologies, adding to the challenge of synthesizing films which support nontrivial topological states, especially films with band gaps large enough for room temperature applications.

Although the layer or thickness dependency of topological properties of thin films of group IV10 and V11,12,22 elements has been reported, we are not aware of a previous study delineating how nontrivial phases evolve in thin films of III-V compounds as the number of layers increases; all the important effects of substrate on the III-V films23–27 have also not been investigated. With this motivation, here we explore the crystal and electronic structures of hydrogenated III-V films using first-principles calculations. Nontrivial phases are predicted in 2 BL thick films of hydrogenated AlBi, GaBi, InBi, TlAs,
and TlSb, which are found to survive over a wide range of strains. BBi, TlN, and TlBi films support a nontrivial phase for certain values of strain. Nontrivial topological phases are also found in 1 and 2 BL films of GaBi as well as 2 BL films of InBi and TlAs on Si(111) substrate. For the 2 BL film of GaBi on Si(111), the band gap can be as large as 121 meV, well above the room-temperature thermal excitation energy. Si(111) would thus provide a viable substrate for growing the proposed topological III-V films.

Results
We assumed the investigated III-V films to be stacked along the [111] direction in zincblende (ZB) and wurtzite (WZ) structures. We define one BL as a III-V pair of layers in the buckled honeycomb structure. The 2 BL film can assume ZB and WZ as two possible structures. The top view of the atomic structure (1 × 1 unit cell is outlined) for a 2 BL film based on the ZB structure is shown in Fig. 1(a). The surface Brillouin zone is presented in Fig. 1(b). Side views of a 2 BL film in ZB and WZ are shown in Fig. 1(c,d), respectively. The band structures for the equilibrium crystal structures were calculated including the spin-orbit coupling. In order to ascertain the band topologies, we computed the $Z_2$ invariant following the method of ref. 28.

Previous studies12–14 have shown that the only 1 BL films of III-V compounds, which exhibit nontrivial phases, involve Bi from group V and Tl from group III. With this in mind, even though we investigated all 25 combinations of group III (B, Al, In, Ga, and Tl) and group V (N, P, As, Sb, and Bi) elements, we will focus on 2 BL films of Bi and Tl, many of which are 2D TIs in the freestanding case. The optimized structures of these nine 2 BL III-V films before and after hydrogenation are summarized in Table 1. Also included in Table 1 are the preferred structure, the system band gap (defined as the energy difference between the lowest conduction band and the highest valence band), and the $Z_2$ invariant, along with the bulk lattice constant, $a_0$, the optimized lattice constant, $a$, of the film, buckling distances in the upper ($d_1$) and lower ($d_2$) layer, and the distance ($D$) between the two layers in the 2 BL film. The hydrogenated 2 BL film of InBi is seen in Table 1 to possess the largest band gap of 134 meV at its equilibrium structure.

A reference to Table 1 shows that the unhydrogenated 2 BL films of AlBi, GaBi, and InBi are nontrivial semi-metals with $Z_2 = 1$ and a negative system gap. TlN, TlAs, and TlSb, in contrast, are nontrivial insulators with band gaps of 18 to 51 meV. Upon hydrogenation, only the TlN film changes from nontrivial to trivial phase, where this transition is partially driven by the 4% (3.739 Å to 3.9 Å) change in lattice constant. Since all of the 2 BL films in Table 1 are seen to prefer the ZB rather than the WZ structure around the equilibrium bulk lattice constant, for the remainder of this study, we will only consider the ZB structure.

In order to simulate the effects of the supporting substrate, nine hydrogenated films with ZB structure in Table 1 were further analyzed over a range of lateral strains around the equilibrium structures (0% strain); the results are summarized in Fig. 2. We see from Fig. 2(a) that the hydrogenated 2 BL films of TlAs, TlSb, AlBi, GaBi, and InBi maintain their nontrivial phase over a wide range of strains; in fact,
certain strain values yield even larger band gaps, see Fig. 2(b). The TlBi film, even though it is trivial phase at its equilibrium lattice constant, exhibits nontrivial phase at strain values greater than 2% and less than −8%. It is remarkable that the nontrivial phase is robust for selected hydrogenated III-V films in that it is maintained over a wide range of strains, suggesting that this nontrivial phase is more likely to be realized when the film is grown on a suitable substrate. Notably, this family of films harbors band gaps large enough for possible room temperature applications. InBi and GaBi films, for example, possess band gaps up to 0.4 eV under compressive strain of around −5%.

Turning to the question of practical realization of our proposed films, Si(111), may be a good candidate substrate to grow TlAs, AlBi, GaBi, and InBi films since the hydrogenated equilibrium lattice constants of these 2 BL films in \( \sqrt{3} \times \sqrt{3} \) supercell (7.85, 7.95, 7.93, and 8.44 Å) are close to the lattice constant (7.73 Å) of 2 × 2 Si(111); also, as noted already in connection with Fig. 2 above, GaBi and InBi films maintain their nontrivial topology over a wide range of strains, while TlAs and AlBi do so near their equilibrium lattice constants. Note that the \( \sqrt{3} \times \sqrt{3} \) surfaces of InBi and GaBi have lattice

| Material | Structure | Sys. Gap (meV) | \( Z_2 \) | \( a_0(\text{Å}) \) | \( a(\text{Å}) \) | \( d_1(\text{Å}) \) | \( d_2(\text{Å}) \) | \( D(\text{Å}) \) |
|----------|-----------|---------------|----------|----------------|--------------|----------------|--------------|-------------|
| BBi      | ZB        | −366          | 0        | 3.90           | 3.90         | 0.56           | 0.80         | 2.58        |
| AlBi     | ZB        | −118          | 1        | 4.83           | 4.56         | 0.78           | 0.85         | 2.98        |
| GaBi     | ZB        | −67           | 1        | 4.56           | 4.55         | 0.78           | 0.86         | 2.98        |
| InBi     | ZB        | −43           | 1        | 4.84           | 4.85         | 0.82           | 0.91         | 3.15        |
| TlN      | ZB        | 18            | 1        | 3.78           | 3.95         | 0.14           | 0.15         | 2.37        |
| TIP      | ZB        | −41           | 0        | 4.39           | 4.42         | 0.68           | 0.74         | 2.97        |
| TlAs     | ZB        | 51            | 1        | 4.53           | 4.56         | 0.73           | 0.82         | 3.02        |
| TlSb     | ZB        | 42            | 1        | 4.83           | 4.85         | 0.80           | 0.95         | 3.15        |
| TlBi     | ZB        | −59           | 0        | 4.96           | 4.98         | 0.75           | 0.96         | 3.19        |
| BBi      | ZB        | 13            | 0        | 3.90           | 3.93         | 0.70           | 0.73         | 2.40        |
| AlBi     | ZB        | 44            | 1        | 4.83           | 4.59         | 0.91           | 0.87         | 2.74        |
| GaBi     | ZB        | 99            | 1        | 4.56           | 4.58         | 0.91           | 0.86         | 2.73        |
| InBi     | ZB        | 134           | 1        | 4.84           | 4.87         | 0.99           | 0.91         | 2.90        |
| TlN      | ZB        | 41            | 0        | 3.81           | 3.74         | 0.92           | 0.84         | 2.25        |
| TIP      | ZB        | 78            | 0        | 4.39           | 4.38         | 0.96           | 0.90         | 2.61        |
| TlAs     | ZB        | 24            | 1        | 4.53           | 4.53         | 0.98           | 0.91         | 2.70        |
| TlSb     | ZB        | 12            | 1        | 4.83           | 4.81         | 1.00           | 0.96         | 2.88        |
| TlBi     | ZB        | 47            | 0        | 4.96           | 4.97         | 1.01           | 0.94         | 2.96        |

Table 1. Calculated equilibrium structure [zincblende (ZB)], system band gap defined as the energy difference between the lowest conduction level and the highest valence level, and the topological invariant \( Z_2 \) for nine 2 BL films of III-V compounds with and without hydrogenation. Other structural parameters given are: bulk lattice constant \( (a_0) \); lattice constant \( a \) of the 2 BL film; interlayer distance \( D \) in the 2 BL film; and the buckling heights \( d_1 \) and \( d_2 \) of the two layers. Distances \( D, d_1 \) and \( d_2 \) are also marked in Fig. 1.

Figure 2. (a) Evolution of the topological phase as a function of strain in selected hydrogenated 2 BL films, and (b) the corresponding system band gaps as a function of strain.
mismatches of $-8.41\%$ and $-2.52\%$ with respect to the $2 \times 2$ Si(111) surface, obtained by using $(a_{\text{Si}} - a_{\text{H}-V})/a_{\text{H}-V}$, where $a_{\text{Si}}$ and $a_{\text{H}-V}$ are the equilibrium lattice constants of $2 \times 2$ Si(111) and hydrogenated $\sqrt{3} \times \sqrt{3}$ 2 BL III-V film, respectively. In this connection, we further explored substrate effects by placing InBi and GaBi films on the Si(111) substrate. For this purpose, three Si(111) bilayers were used to simulate the substrate with the bottom Si(111) layer passivated with H atom. The Si atoms at the bottom bilayer and the passivating H atoms were fixed while all other atoms were allowed to relax. (In these calculations, a $\Gamma$-centered Monkhorst-Pack grid of $12 \times 12 \times 1$ in the 2D Brillouin zone of $\sqrt{3} \times \sqrt{3}$ buckled honeycomb was used.) Since III-V films contain two distinct surfaces, two different types of bonding with the substrate is possible. The Si(111) layer can bond either to the Bi layer or In/Ga atoms. Figure 3 presents the crystal and band structures for these two cases in which the Bi layer lies on (a) top or (d) below the Ga/In layer. The corresponding band structures for Bi on top of Ga (b) and In (c) and for Bi below Ga (e) and In (f) are also shown. Table 2 summarizes the main results by giving the total energy, the system energy gap, and the $Z_2$ invariant for 1 BL and 2 BL Ga/In-Bi, AlBi, and TlAs films on Si(111). For 2 BL Ga/In-Bi films, both cases support nontrivial topological insulator phase and a band gap [121 meV for GaBi-Si(111)] large enough for room-temperature applications. Notably, 1 BL films of GaBi or BiGa on Si(111) also exhibit a nontrivial topological phase. The transition to trivial from nontrivial phase of 1 BL film of InBi or BiIn on Si(111) is consistent with our previous work in which the hydrogenated 1 BL film of InBi was found to be trivial under $-4\%$ strain. Finally, we comment on the results for AlBi and TlAs films. As shown in Fig. 2(a), 2 BL film of AlBi becomes trivial below $-1\%$ strain, while TlAs film maintains the nontrivial phase for less than $1\%$ strain. [AlBi and TlAs have lattice mismatches of $-2.77\%$ and $-1.53\%$, respectively.] When placed on Si(111), only the TlAs film exhibits a nontrivial phase as expected in view of its lattice mismatch with Si(111), see also Fig. 2. We note that all 1 BL films of AlBi and TlAs films are found to be trivial.

Conclusions
We have presented a first-principles study of the crystal and electronic structures of freestanding and hydrogenated multilayers of III-V compounds. Two BL films of hydrogenated AlBi, GaBi, InBi, TlAs, and TlSb are found to harbor the nontrivial insulator phase. BBi, TTN, and TiBi films can be driven into the nontrivial topological phase via strain, although these films are in the trivial phase at their equilibrium structures. Hydrogenated 2 BL films of GaBi and InBi exhibit band gaps of $99\text{ meV}$ and $134\text{ meV}$, respectively. We have also explored the electronic structures and topological properties of 1 BL and 2 BL films of GaBi as well as 2 BL films of InBi and TlAs on a Si(111) substrate, and found a nontrivial phase with a large band gap of $121\text{ meV}$ in 2 BL films of GaBi. Our study suggests that III-V thin films can support nontrivial topological phases, which are robust against hydrogenation, strain and substrate effects, and would thus provide a viable materials platform for future room temperature applications.
Table 2. Total energy, system gap, and the topological invariant (Z₂) of 1 and 2 BL films of Ga/In-Bi, AlBi, and TlAs on Si(111). Z₂ is 1 for nontrivial and 0 for trivial band topology, while m denotes that the system is metallic.

| Material         | Total energy(eV) | System Gap(meV) | Z₂ |
|------------------|------------------|-----------------|-----|
| BiGa-Si(111)     | -196.514         | 37              | 1   |
| GaBi-Si(111)     | -197.146         | 121             | 1   |
| BiIn-Si(111)     | -193.410         | 44              | 1   |
| InBi-Si(111)     | -194.443         | -330            | 1   |
| AlBi-Si(111)     | -201.291         | -16             | m   |
| BiAl-Si(111)     | -200.415         | 178             | 0   |
| TiAs-Si(111)     | -192.820         | 76              | 1   |
| AsTl-Si(111)     | -194.200         | 158             | 0   |
| 2BL              |                  |                 |     |
| BiGa-Si(111)     | -174.793         | 68              | 1   |
| GaBi-Si(111)     | -175.324         | 84              | 1   |
| BiIn-Si(111)     | -173.291         | 445             | 0   |
| InBi-Si(111)     | -173.327         | 254             | 0   |
| AlBi-Si(111)     | -177.584         | 466             | 0   |
| BiAl-Si(111)     | -176.842         | 611             | 0   |
| TiAs-Si(111)     | -173.012         | 195             | 0   |
| AsTl-Si(111)     | -174.198         | 342             | 0   |

Methods

First-principles calculations were performed within the density functional theory (DFT) utilizing the generalized gradient approximation (GGA). Projector-augmented-wave (PAW) wave functions with an energy cut-off of 400 eV were used in the Vienna Ab-Initio Simulation Package (VASP). Atomic positions were optimized for each lattice constant value considered until the residual forces were no greater than 10⁻³ eV/Å. The criteria for convergence for self-consistent electronic structure was set at 10⁻⁶ eV. A vacuum layer of at least 20 Å along the z direction was used to simulate multilayer films. A Γ-centered Monkhorst-Pack grid of 18 × 18 × 1 was used for 2D integrations in the Brillouin zone of the 1 × 1 buckled honeycomb lattice.

References

1. Kane, C. L. & Mele, E. J. Z₂ Topological Order and the Quantum Spin Hall Effect. Phys. Rev. Lett. 95, 146802 (2005).
2. Hasan, M. Z. & Kane, C. L. Colloquium: Topological insulators. Rev. Mod. Phys. 82, 3045 (2010).
3. Liu, C. C., Feng, W. & Yao, Y. Quantum Spin Hall Effect in Silicene and Two-Dimensional Germanium. Phys. Rev. Lett. 107, 076802 (2011).
4. Tsai, W.-F. et al. Gated silicene as a tunable source of nearly 100% spin-polarized electrons. Nat. Commun. 4, 1500 (2013).
5. Liu, C. C., Jiang, H. & Yao, Y. Low-energy effective Hamiltonian involving spin-orbit coupling in silicene and two-dimensional germanium and tin. Phys. Rev. B 84, 195430 (2011).
6. Wada, M., Murakami, S., Freimuth, F. & Bihlmayer, G. Localized edge states in two-dimensional topological insulators: Ultrathin Bi films. Phys. Rev. B 83, 121310 (2011).
7. Huang, Z.-Q. et al. Nontrivial topological electronic structures in a single Bi(111) bilayer on different substrates: A first-principles study. Phys. Rev. B 88, 165301 (2013).
8. Liu, Z. et al. Stable Nontrivial Z₂ Topology in Ultrathin Bi(111) Films: A First-Principles Study. Phys. Rev. Lett. 107, 136805 (2011).
9. Chuang, F.-C. et al. Tunable topological electronic structures in Sb(111) bilayers: A first-principles study. Appl. Phys. Lett. 102, 022424 (2013).
10. Zhang, P., Liu, Z., Duan, W. H., Liu, F. & Wu, J. Topological and electronic transitions in a Sb(111) nanofilm: The interplay between quantum confinement and surface effect. Phys. Rev. B 85, 201410 (R) (2012).
11. Huang, Z.-H. et al. Strain driven topological phase transitions in atomically thin films of group IV and V elements in the honeycomb structures. New J. Phys. 16, 105018 (2014).
12. Chuang, F.-C. et al. Prediction of Large-Gap Two-Dimensional Topological Insulators Consisting of Bilayers of Group III Elements with Bi. Nano Lett. 14(5), 2505 (2014).
13. Crisostomo, C. P. et al. Robust Large-Gap Two-Dimensional Topological Insulators in Hydrogenated III-V Bilayers. Nano Lett. DOI: 10.1021/acs.nanolett.5b02293 (2015).
14. Li, L., Zhang, X., Chen, X. & Zhao, M. Giant Topological Nontrivial Band Gaps in Chloridized Gallium Bismuthide. Nano Lett. 15(2), 1296 (2015).
15. Zhao, M., Chen, X., Li, L. & Zhang, X. Driving a GaAs film to a large-gap topological insulator by tensile strain. Sci. Rep. 5, 8441 (2015).
16. Garcia, J. C., de Lima, D. B., Assali, L. V. C. & Justo, J. F. Group IV Graphene- and Graphane-Like Nanosheets. J. Phys. Chem. C 115, 13242 (2011).
17. Zhang, C. & Yan, S. First-Principles Study of Ferromagnetism in Two-Dimensional Silicene with Hydrogenation. J. Phys. Chem. C 116(6), 4163 (2012).
18. Wang, R., Wang, S. & Wu, X. The formation and electronic properties of hydrogenated bilayer silicene from first-principles. J. App. Phys. 116, 024303 (2014).
19. Xu, Y. et al. Large-Gap Quantum Spin Hall Insulators in Tin Films. Phys. Rev. Lett. 111, 136804 (2013).
20. Chou, B.-H. et al. Hydrogenated ultra-thin tin films predicted as two-dimensional topological insulators. New J. Phys. 16, 115008 (2014).
21. Hsu, C.-H. et al. The nontrivial electronic structure of Bi/Sb honeycombs on SiC(0001). New J. Phys. 17, 025005 (2015).
22. Liu, C. C. et al. Low-energy effective Hamiltonian for giant-gap quantum spin Hall insulators in honeycomb X-hydrize/halide (X=N-Bi) monolayers. Phys. Rev. B 90, 085431 (2014).
23. Song, Z. et al. Quantum Spin Hall Insulators of Bi/SbX (X = H, F, Cl, and Br) Monolayers with a Record Bulk Band Gap. NPG Asia Mat. 6, e147 (2014).
24. Chen, L. et al. Edge state modulation of bilayer Bi nanoribbons by atom adsorption. Phys. Chem. Chem. Phys. 16, 17206 (2014).
25. Ferhat, M. & Znaoui, A. Structural and electronic properties of III-V bismuth compounds. Phys. Rev. B 73, 115107 (2006).
26. Zhuang, H. L., Singh, A. K. & Hennig, R. G. Computational discovery of single-layer III-V materials. Phys. Rev. B 87, 165415 (2013).
27. Keen, B. et al. Growth Parameters for Thin Film InBi Grown by Molecular Beam Epitaxy. J. Electron. Mat. 43, 914 (2014).
28. Fukui, T. & Hatsugai, Y. Quantum spin Hall effect in three dimensional materials: Lattice computation of Z2 topological invariants and its application to Bi and Sb. J. Phys. Soc. Jpn. 76, 053702 (2007).
29. Monkhorst, H. J. & Pack, J. D. Special points for Brillouin-zone integrations. Phys. Rev. B 13, 5188 (1976).
30. Hohenberg, P. & Kohn, W. Inhomogeneous Electron Gas. Phys. Rev. 136, B864 (1964).
31. Kohn, W. & Sham, L. J. Self-Consistent Equations Including Exchange and Correlation Effects. Phys. Rev. 140, A1133 (1965).
32. Ceperley, D. M. & Alder B. J. Ground State of the Electron Gas by a Stochastic Method. Phys. Rev. Lett. 45, 566 (1980).
33. Perdew, J. P. & Zunger, A. Self-interaction correction to density-functional approximations for many-electron systems. Phys. Rev. B 23, 5048 (1981).
34. Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized gradient approximation made simple. Phys. Rev. Lett. 77, 3865 (1996).
35. Kresse, G. & Joubert, D. From ultrasoft pseudopotentials to the projector augmented-wave method. Phys. Rev. B 59, 1758 (1999).
36. Kresse, G. & Hafner. J. Ab initio molecular dynamics for liquid metals. Phys. Rev. B 47, 558 (1993).
37. Kresse, G. & Furthmüller J. Efficient iterative schemes for an initio total-energy calculations using plane-wave basis set. Phys. Rev. B 54, 11169 (1996).

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Author Contributions
F.C.C. conceived and initiated the study. L.Z.Y., C.P.C., C.C.Y. and S.M.L. performed calculations. Z.Q.H., C.H.H., H.L. and F.C.C. performed the analysis and contributed the discussions. C.P.C., Z.Q.H., C.H.H., F.C.C., H.L. and A.B. wrote the manuscript. All authors reviewed the manuscript.

Additional Information
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