Size-structure dynamics of mixed versus pure forest stands

Hans Pretzsch* and Gerhard Schütze

Chair for Forest Growth and Yield Science. Centre of Life and Food Sciences Weihenstephan. Technische Universität München. Hans-Carl-von-Carlowitz-Platz, 2. D-85354 Freising, Germany

Abstract

Mixed species forests are presently on the advance and widely held to provide many ecosystem functions and services better than pure stands. Recent studies well explored species mixing effects at the individual tree or stand level. However, the link between individual and stand level which is represented by the size-structure dynamics of stands, is still hardly understood.

Aim of this study: The objective was to analyse how species mixing modifies the size-structure dynamics of mixed compared with pure forest stands.

Area of the study: The study was carried out in Southern Germany.

Material and methods: We selected 11 long-term experiments comprising 129 plots of un-thinned or just lightly thinned pure and mixed stands of European beech [Fagus sylvatica (L.)] and analysed their size structure dynamics.

Main results: Based on the Gini coefficient, skewness and kurtosis we show how mixing with Norway spruce [Picea abies (L.) Karst] and sessile oak [Quercus petraea (Matt.) Liebl.] modifies the size-structure dynamics of European beech. The size distribution of beech in mixture mostly lags behind the pure stand, is more size-asymmetric, and the mortality shifts from the smaller diameter classes further to the taller trees than in pure stands.

Research highlights: The revealed changes of the size-structure dynamics of beech in mixed versus pure stands result from a modification of both growth partitioning and self-thinning. We draw conclusions of the reduced size growth and size equality of beech in mixed versus pure stands for forest management planning and perspectives for forest research.

Key words: species selection effect; true mixing effect; morphological plasticity; size-distribution; growth partitioning between trees; mode of mortality; European beech [Fagus sylvatica (L.)]; Norway spruce [Picea abies (L.) Karst]; sessile oak [Quercus petraea (Matt.) Liebl.].

Introduction

Mixed species forests are presently on the advance as they are widely held to provide many ecosystem functions and services better than pure stands. Recent studies well explored species mixing effects at the individual tree level (Río et al., 2014a,b; Webster & Lorimer, 2003) and at the stand level (Morin et al., 2011; Piotto, 2007). However, the link between individual and stand level, the way how species mixing modifies the growth partitioning between the trees in a stand and their size-structure dynamics, is still hardly understood.

Forest dynamics is often conceptualized at stand level by sum and mean values, at the collective level by tree size distributions, or at tree and organ level by the individuals’ structure and growth. Each approach reveals special insights, not attainable at the levels abo-
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The focus of this analysis is on beech and its interaction with admixed species such as Norway spruce and sessile oak. In Central Europe European beech has an overwhelming competition superiority compared to other native trees species, in particular in its physiological optimum under mild climatic conditions and on fertile soils which are well supplied with water. On such sites European beech would probably cover more than 2/3 of the Central European forest area (Bohn et al., 2003). However, since human influence on European forests, beech has been severely decimated by clearings for agricultural land or, during the last centuries, by replacing them in the forest by faster and straighter growing conifers such as spruce, fir, or pine species (Mantel, 1961). Presently, beech is strongly on the advance and becoming the pillar of close-to-nature forestry in the central European lowland, where it once dominated (Pretzsch et al., 2010, 2013). There, its cultivation in mixed-species stands elucidates and recalls its high competitiveness. In the long term added species such as oak, pine, or spruce could hardly persist without being supported by tending or thinning.

Behind different size distributions in pure and neighbouring mixed stands may be a simple species ‘selection effect’ or a ‘true mixing effect’. As we are mainly interested in the true mixing effect we use Fig. 1 to illustrate how to distinguish between both. Suppose the tree size distribution of species 1 and 2 in the pure stand are $D_1$ and $D_2$, then the weighted mean of both distributions in case of a 50:50 mixture is $D_{1,2}$ (left column from top to bottom). So, if the diameter distribution of a mixed stand of both species would resemble $D_{1,2}$, it would of course differ from $D_1$ and $D_2$, but it is simply the weighted mean of both. And as it simply results from the species selection it is called the “selection effect”. Any true mixing effects can be revealed by comparing $D_i$ of species 1 in the pure stand with the size distribution, $D_{i,(1,2)}$, of the same species in mixture (top row). In this model example the distribution of species 1 in the mixed stand is ahead of the pure stand but similar in shape. Size development of species 2, $D_{(1,2)}$ in mixture is slower and its distribution is wider, more left shallow, and right-steep compared with its distribution $D_2$ in the pure stand (central row). For both comparisons the size distributions in mixture are scaled up to unit area of 1 hectare by the species’ mixing portions ($m_1$ and $m_2$); in this example we assume a fifty-fifty mixture. The size superiority of $D_{1,(1,2)}$ over $D_1$ and their different shapes reveal true mixing effects.

A true mixing effect also becomes obvious at stand level by considerable differences between the expected distribution $\hat{D}_{1,2} = D_1 \times m_1 + D_2 \times m_2$ (weighted mean of pure stands) and the observed distribution of the mixed stand $D_{1,2}$ (bottom row).
So far, evidence of changes of the size-structure dynamics in mixed compared with pure stands is very limited as this requires long-term plots of equally treated pure and mixed stands in close neighbourhood. We use such data from pure and mixed plots of long-term experiments in South Germany, with some of them surveyed since more than 100 years, for scrutiny of differences at species level \( D_{1(2)} \) vs. \( D_{1(1,2)} \). We analyse (i) how mixing modifies the species specific shape of the tree size-distribution, (ii) how mixing modifies the growth partitioning between the trees compared with the partitioning in neighbouring pure stands, and (iii) whether species mixing modifies the mode of mortality in terms of size-distribution of the removed trees.

**Material and methods**

**Material**

As the focus was on effects of species mixing on the size-structure dynamics of European beech we included only fully stocked or at most moderately thinned stands, as they reflect the best the species specific behaviour. The study is based on more or less even-aged pure and mixed stands. As empirical basis we selected 11 long-term experiments in Germany in pure and mixed stands of European beech and sessile oak and European beech and Norway spruce (Table 1). The experiments MIT 101, ZWI 111, WIE 114, WAB 105 and WAB 106 cover only one stand development phase each. The age series NOR 811, FRE 813, SON 814, ROT 801, SWE 803, and KEH 804 cover pure and mixed stands at varies stand development phases. Some of the in total 129 plots were excluded due to their small size, admixture of additional species, or damages by windthrow or bark beetle. Out of in total 129 plots we selected \( n = 68 \) pairs of beech in mixed and pure stands, \( n = 41 \) pairs of spruce, and \( 32 \) pairs of oak in mixed and pure stands. The dataset represents the growing conditions of a rather broad time span (1905-2012) range of stand ages (31-238 years) and mainly experiments from central and southeast of Germany. Table 1 summarizes basic characteristics of the plots, for more detailed information see Matyssek et al. (2012, pp: 243-271) and Pretzsch (2009), Pretzsch et al. (2010, 2013) who used the same experiments for analyzing mixing effects at tree and stand level.

**Methods**

Skewness, kurtosis and other measures for characterizing diameter distributions

For comparing the tree diameter distribution of mixed versus pure stands we use measures such as arithmetic mean diameter, minimum and maximum diameter, diameter range (max-min), and standard deviation of the breast height diameter. For analyzing any differences in the shape of the respective distributions we use the skewness.

![Figure 1. Schematic representation of the comparison between pure and mixed stands’ tree diameter distribution and revelation of true mixing effects. At species level size distributions \( D_1 \) and \( D_2 \) of species in pure stands can be compared with the respective distributions \( D_{1(2)} \) and \( D_{1(1,2)} \) in neighbouring mixed stands (top and centre row). For scrutiny of mixing effect at whole stand level the weighted mean of both pure stand distributions \( \hat{D}_{1,2} \) can be compared with the observed whole stand distribution \( D_{1,2} \) (bottom row). Differences between the reference distributions (black) and the observed size distribution (grey) indicate inter-specific interactions and true mixing effects.](image)
In case of symmetric distribution skew = 0. Suppose an observed diameter distribution is equipped with many small trees and a low number of tall ones it is left-steep (right shallow) and yields skew > 0. If the distribution is equipped with many tall trees but small are rare it is right-steep (left shallow). Skew is useful for characterizing the effect of any kind of thinnings (including self-thinning and alien-thinning in unmanaged stands) on the shape of the distribution.

Furthermore we calculated the kurtosis

\[ \text{kurt} = \frac{\sum_{i=1}^{n} [(x_i - \bar{x})/s]^4}{n} - 3 \]

which characterizes the degree of concentration of tree sizes around the mean. If the concentration resembles the Gaussian normal distribution, kurt = 0. Stronger concentrations around the mean (peaked shapes) are indicates by kurt > 0, lower concentrations (shallow shapes) yield kurt < 0. The kurtosis is appropriate for characterizing the degree of restriction of a species by intra- and inter-specific competition.

For the further evaluation it is important to notice that both skewness and kurtosis are invariant to linear transformation, i.e., if the tree diameter distribution of a species occupying a certain portion of the mixed stand is scaled up to 1 ha, the skewness and kurtosis remain unchanged.

Table 1. Overview of the 11 long-term experiments and 129 plots included in this study. All listed experiments provide plots in pure as well as mixed stands and enable a comparison between the species performance in mixed versus pure stand at a given site.

| Experiments | Species                | Plots | Survey | Age (years) | Coordinates | Site characteristics |
|-------------|------------------------|-------|--------|-------------|-------------|----------------------|
|             |                        |       | First  | Last        | E long.     | N lat.   | Geology | Substrate |
| MIT 101     | Spruce/beech           | 3     | 1934   | 1955        | 78          | 12.17    | 49.95   | Basalt | Loam     |
| ZWI 111     | Spruce/beech           | 3     | 1954   | 2002        | 126         | 13.31    | 49.07   | Gneiss | Loam     |
| WIE 114     | Spruce/beech           | 3     | 1950   | 2006        | 121         | 10.58    | 51.64   | Schist | Sandy loam |
| NOR 811     | Spruce/beech           | 15    | 1997   | 2008        | 47-126      | 11.53    | 50.35   | Graywacke | Sandy loam |
| FRE 813     | Spruce/beech           | 18    | 1994   | 2012        | 55-168      | 11.40    | 48.25   | Tertiary | Loam     |
| SON 814     | Spruce/beech           | 24    | 2000   | 2011        | 62-142      | 10.46    | 47.52   | Moraine | Loam     |
| WAB 105     | Oak/beech              | 3     | 1951   | 2007        | 105         | 9.87     | 49.71   | Limestone | Loam     |
| WAB 106     | Oak/beech              | 3     | 1951   | 2007        | 116         | 9.86     | 49.68   | Limestone | Loam     |
| ROT 801     | Oak/beech              | 18    | 1994   | 2009        | 47-238      | 9.26     | 49.57   | Sandstone | Sand     |
| SWE 803     | Oak/beech              | 18    | 1995   | 2005        | 31-186      | 10.30    | 50.26   | Keuper  | Loam     |
| KEH 804     | Oak/beech              | 21    | 1996   | 2008        | 46-158      | 11.78    | 48.93   | Marl    | Loam     |

Species: spruce, Norway spruce; beech, European beech, oak, sessile oak; range of stand age: lowest stand age at the first survey and highest stand age at the last survey.

Coefficient by Gini and curve by Lorenz for characterizing the size and growth hierarchy

The coefficient by Gini and curve by Lorenz can be used for quantifying the size or growth hierarchy between the trees in forest stands (see de Camino, 1976; Kramer, 1988, p: 82). We use as a loan from economics the Gini coefficient, GC,

\[ GC = \frac{\sum_{i=1}^{n} \sum_{j=1}^{n} |x_i - x_j|}{2n(n-1) \times \bar{x}} \]

for quantifying the relative distribution of tree volume (GC_v) and volume growth (GC_g), respectively, between the trees in mixed versus pure stands. Variables x_i and x_j denote size or growth (or other tree characteristics) for the i'th, respectively the j'th tree in the stand with i = 1…n trees. GC = 0.0 applies for a very homogeneous distribution of the respective tree variable, e.g. maximum equality of size or growth distribution. The higher GC, the stronger the inequality of size or growth between the trees (Fig. 2a,b). The curves of the cumulative distributions in Fig. 2b together with the sketched stands reflect the inequality of size which can cause also an inequality of growth.

Application to mixed and pure stands can reveal how mixing modifies the hierarchy between the trees in a population, e.g., whether species mixing can favour the growth distribution towards small understory trees compared with pure stands. The Lorenz curve, known for analysing the inequality of income in hu-
man populations, can be used for visualizing the inequality of growth in forest stands. The larger the area between the bisector line (maximum equality) and the observed Lorenz curve, the stronger the inequality, and the higher GC. The GC is equivalent to the grey coloured area between the Lorenz curve and the bisector line (grey area in relation to the total area of the square) multiplied by 2 (see Fig. 2a).

**Size-growth relationship for quantifying the size symmetry respectively asymmetry**

Size growth plotted over size (Fig. 2c) reveals the inter-individual competition and growth partitioning between the trees in a stand (Schwinning & Weiner, 1998; Wichmann, 2001, 2002). A steeper slope indicates a stronger concentration of growth rates and resources on tall trees in the stand. Shallow size growth-size-relationships are assumed to prevail under limitation by below-ground resources (water and mineral nutrients), as they are mobile, diffuse quickly and are difficult to preempt by larger individuals. Strongly increasing size growth-size-relationships mean that larger individuals obtain a disproportionately higher share of resources and growth. This mode of growth-size relationship can be expected on high quality sites, where light is the limiting factor and pre-empted by the larger individuals (Weiner, 1990).

The growth-size slope might be suitable for indication of inter-individual growth allocation patterns and their dependency on species mixture. In the model example (Fig. 2c) mixing strongly improves the growth of smaller trees, while the taller trees have just small benefits. The differences can be quantified by the intercept a and slope b resulting from fitting the relationship between diameter growth and diameter to a linear model.

**Ratio between the diameter of the removal and total stand for characterizing the mode of mortality**

Based on the mean tree diameter of the removal stand, d_{removal}, and the remaining stand, d_{remain}, the ratio d_{rel} = d_{removal}/d_{remain} characterizes the size of the removal in relation to the remaining trees (Fig. 3). Notice, that latter is a schematic figure with simplified assumptions of the mean diameter of the remaining and removal trees and of the shape of the distributions. The higher the d_{rel} values the taller are the removed trees in relation to the remaining stand. Thinning from below or self-thinning befalls mainly small trees with d_{removal} < d_{remain} and yields ratios of d_{rel} < 1. In case of a schematic thinning the size of the mean size of the removal and remaining trees would be equal, and d_{rel} 1 (range d_{rel} = 0.9-1.1). Thinning from above means tree elimination from the right side and yields d_{rel} > 1, e.g., selective thinning eliminates 1-2 of the strongest competitors of each future crop tree (range d_{rel} = 0.8-1.2). Comparison between a species d_{rel} in the mixed with the neighbouring pure stand may reveal how mixing superimposes the self-thinning process in the pure.
stand which normally reduces the tree number from the left side of the tree size distribution.

Results

Table 2 gives an overview of the size-structure dynamics in mixed versus pure stands. While the scattergrams (Figs. 4-7) reflect the observed size-structure variables and correspond with the arithmetic means in columns “mixed” and “pure” in Table 2, the test for differences is based on the pair-wise ratios mixed/pure given in column “mixed/pure” of Table 2.

Notice, that in the columns “mixed” and “pure” we report the species specific arithmetic means of all n observations within the respective groups. In the column “mixed/pure”, in contrast, we report the mean of the ratio resulting from the pair-wise division of the characteristic of the mixed stand by the respective value of the neighbouring pure stand. The mean of the ratios is not necessarily equal to the ratio of the means. Pair-wise comparison is more informative and in the following used for testing any differences.

Effect of species mixing on tree size-distribution

A species’ frequency distribution in a mixed stand compared with the neighbouring pure stand reveals whether and how the species adapts to mixing by slowing down or accelerating growth (shifts of the mean size), occupying the dominant or rather subdominant tree classes (changes of skewness), or getting decimated or decimating members of the same or alien species (change of kurtosis).

Fig. 4 reflects how the mean tree volume, \( \bar{v}_{\text{mean}} \), comes off in mixed versus pure stands for (a) beech and (b) spruce and oak. Observations (small symbols) close to the bisector line indicate similar behaviour in mixed and pure stands, while deviations indicate true mixing effects. Large symbols indicate mean values. The higher Gini coefficient for tree volume of beech in mixed stands compared with pure stands indicates a more unequal distribution of standing stock in favor of the tall trees (Fig. 5a). GCv of spruce and oak remain rather unaffected by mixture (Fig. 5b).

Table 2 shows that the mean diameter, \( \bar{d}_{\text{mean}} \), as well as mean tree volume, \( \bar{v}_{\text{mean}} \), of beeches in mixture with spruce or oak are significantly \( (p < 0.05) \) smaller than in neighbouring pure stands. Norway spruce and sessile oak, in contrast, are about 12-30\% ahead in mixed versus neighbouring pure stands. Neither skewness nor kurtosis are significantly modified by mixing.

Growth distribution between trees in mixed compared with pure stands

The mode of growth partitioning between the trees of different sizes in a stand determines its size-structure dynamics. For scrutiny whether mixed stands differ in
the mode of growth partitioning we use the Gini coefficient for tree volume growth, GCiv, and the intercept a and slope b of the id-d-relationship fitted to a linear model.

**Table 2.** Overview of the differences between mixed and pure stands in terms of size distribution, size-growth relationship, and mode of mortality. The columns “mixed” and “pure” report the species specific arithmetic means of all n observations within the respective groups. The column “mixed/pure”, in contrast, shows the mean of the ratio resulting from the pair-wise division of the characteristic of the mixed stand by the respective value of the neighbouring pure stand. Bold ratios indicate significant ($p < 0.05$) differences between the species behaviour in mixed versus pure stands.

| Variable | European beech | Norway spruce | Sessile oak |
|----------|----------------|---------------|-------------|
|          | Mixed Pure Mixed/pure | Mixed Pure Mixed/pure | Mixed Pure Mixed/pure |
| n        | 68 68 68 | 41 41 41 | 32 32 32 |
| dmean (cm) | 26.5 29.1 0.92 ± 0.08 | 37.2 33.2 1.12 ± 0.03 | 25.0 24.6 1.03 ± 0.05 |
| Vmean (m^3) | 0.89 1.05 0.82 ± 0.12 | 1.08 1.41 1.30 ± 0.08 | 0.62 0.59 1.13 ± 0.15 |
| dmin (cm) | 14.6 15.2 1.08 ± 0.14 | 25.8 21.0 1.27 ± 0.11 | 17.7 17.0 1.07 ± 0.07 |
| dmax (cm) | 49.0 43.6 0.96 ± 0.07 | 49.4 46.4 1.07 ± 0.04 | 35.9 33.7 1.08 ± 0.06 |
| s_d (cm) | 74.7 79.3 1.05 ± 0.10 | 73.6 64.5 1.17 ± 0.09 | 46.5 41.5 1.13 ± 0.13 |
| skew | -0.017 0.144 -3.82 ± 5.06 | -0.283 -0.284 1.30 ± 1.33 | 0.31 -0.25 -12.02 ± 19.78 |
| Kurt | 0.18 0.16 1.27 ± 0.15 | 0.12 0.11 1.11 ± 0.18 | 0.79 0.47 1.40 ± 0.46 |
| GCv | 0.44 0.39 1.17 ± 0.11 | 0.35 0.34 1.06 ± 0.16 | 0.46 0.37 1.17 ± 0.15 |
| GCiv | 0.27 -0.65 0.74 ± 1.10 | -2.10 -2.22 0.51 ± 1.00 | -0.64 -1.18 -0.65 ± 3.16 |
| a | 0.024 0.014 2.02 ± 0.96 | 1.04 0.02 1.04 ± 0.22 | 1.28 0.02 1.29 ± 0.78 |
| b | 0.82 0.73 1.20 ± 0.09 | 0.75 0.74 1.03 ± 0.10 | 0.78 0.79 1.0 ± 0.08 |

Number of stands analyzed, n; arithmetic mean diameter, dmean; arithmetic mean tree volume, Vmean; minimum and maximum tree diameter, dmin respectively dmax; standard deviation of tree diameter, s_d; skewness and kurtosis of tree diameter distribution, skew respectively kurt; Gini coefficient of tree volume, GCv; Gini coefficient of tree volume increment GCiv; intercept and slope of the id-d-relationship, a respectively b; mode of mortality, drel=dremoval/dremaining.

Fig. 6 shows the coefficient of Gini, GCv, for the distribution of tree volume growth in mixed versus pure stands for (a) beech and (b) spruce and oak. In ca-

**Figure 4.** Mean tree volume, vmean, in mixed versus pure stands for (a) beech and (b) oak and spruce. Observations close to the bisector line indicate similar behaviour for mixed and pure stands, while deviations indicate true mixing effects. (a) Response of beech to admixture of oak is represented by empty circles, its response to spruce by filled circles. The large black circle indicates the mean relationship for beech in mixed versus pure stands. (b) Response of oak to the admixture of beech is represented by rectangles and the response of spruce to beech by triangles. The large black rectangle and triangles indicates the mean relationship for oak respectively spruce in mixed versus pure stands.
In the mixed stands, the mean GCiv values often lie above the bisector line, while the corresponding values for spruce and oak remain rather unmodified by mixing.

Table 2 reflects that both the Gini coefficient and slope of the id-d-relationship indicate a significant increase of the size-asymmetry in mixed versus pure stands for beech, i.e. an increase of the size hierarchy in mixed compared with pure stands. Except the GCiv value of sessile oak, the other species are not significantly modified in their size-structure dynamics by the admixture of beech.

Figure 5. Coefficient of Gini, GCiv, for the distribution of tree volume in mixed versus pure stands for (a) beech and (b) oak and spruce. Observations close to the bisector line indicate similar behaviour for mixed and pure stands, while deviations indicate true mixing effects. (a) Response of beech to admixture of oak is represented by empty circles, its response to spruce by filled circles. The large black circle indicates the mean relationship for beech in mixed versus pure stands. (b) Response of oak to the admixture of beech is represented by rectangles and the response of spruce to beech by triangles. The large black rectangle and triangles indicates the mean relationship for oak respectively spruce in mixed versus pure stands.

Figure 6. Coefficient of Gini, GCiv, for the distribution of tree volume growth in mixed versus pure stands for (a) beech and (b) oak and spruce. Observations close to the bisector line indicate similar behaviour for mixed and pure stands, while deviations indicate true mixing effects. (a) Response of beech to admixture of oak is represented by empty circles, its response to spruce by filled circles. The large black circle indicates the mean relationship for beech in mixed versus pure stands. (b) Response of oak to the admixture of beech is represented by rectangles and the response of spruce to beech by triangles. The large black rectangle and triangles indicates the mean relationship for oak respectively spruce in mixed versus pure stands.
Mode of tree mortality in mixed versus pure stands

The significantly higher ratio $d_{rel}$ of beech in mixture compared with monocultures (Table 2, Fig. 7a) indicates that the associated tree species exert an alien-thinning effect from above. The mean $d_{rel}$ ratio of the removal beeches in the mixed stand is about 10% higher ($d_{rel} \approx 0.83$ versus $d_{rel} \approx 0.73$) than in monoculture, i.e., mortality reaches wider into the right branch of the tree size distribution in mixed stands compared with pure stands. In the analysed even-aged mixed stands Norway spruce and Sessile oak are ahead in size growth (Fig. 4b) and obviously able to slow down the growth and reduce the number of beeches during early stand development.

In contrast, the $d_{rel}$ of Norway spruce and Sessile oak is not significantly modified by mixing (Fig. 7b). As shown in Fig. 4a the mean tree size growth of Norway spruce and Sessile oak can be fostered by mixing. However, the presence of beech does not significantly modify the removal-ratio of Norway spruce and Sessile oak. Their $d_{rel}$ values indicate a thinning-from-below effect which is rather equal in mixed and pure stands ($d_{rel} \approx 0.75$). Table 2 underlines that significantly ($p < 0.05$) exceeds 1.0 and indicates the mortality shifts from the smaller diameter classes further to the taller trees in mixed stands.

Discussion

Studies of mixing effects at stand level, e.g., analyses of over- and underyielding at the species or stand level on the basis of sum values (productivity, standing stock) or mean tree attributes (mean tree diameter or volume) may reveal the relevance of mixing effects in terms of stand productivity gains, but not evidence of the underlying reactions (Pretzsch et al., 2010, 2013). They do not reveal, e.g., whether modified stand density, growth partitioning in favour of higher or lower size classes, or a combination of both is behind effects found at stand level.

In contrast, studying of mixing effects at the individual tree level may deliver valuable insight how trees change their crown allometry (Dieler & Pretzsch, 2013), growth (Webster & Lorimer, 2003), and root-shoot-relationship (Schmid & Kazda, 2001) in mixed versus pure stands. However, the relevance of such findings for any productivity gains at species or stand level remains mostly unclear as the effects are rarely up-scaled from individual level to unit area. Up-scaling from individual tree level to the species or stand level has to take into account how general the observed reactions at organ or tree level are (variation between trees of different sizes) and how often the individual trees occur (frequency of the trees in different size classes).
Research into the size-structure dynamics can link findings at individual tree and stand level and thus contribute to tracing effects of species mixing, thinning, fertilization from tree to stand level (Hara, 1993; Webster & Lorimer, 2003). Tracing mixing effects from stand level to individual tree level via analyses of size-structure dynamics concerns also forest practice. It makes a big difference regarding assortment yield, whether a species increases the productivity by higher survival, growth of many small but non-merchantable trees or by growth distribution in favour of more valuable tall trees by both alien-thinning and growth acceleration. By taking into account both the modification of the frequency distribution (tree number per size class) and the growth-size relationship (growth rate depending on size) it becomes possible to reveal whether mixing modifies the size distribution, the growth rate at given sizes, or both. The size-structure approach may solve the apparently contradictory findings that mixing may strongly affect the growth of dominant trees in mixed compared to pure stands but hardly changes the stand productivity in total.

Changes of the frequency distribution or negative mixing reactions of smaller trees may counteract or even cancel the reactions observed at the subset of dominant trees. Behind a neutral effect of productivity at stand level, in contrast, may be hidden a higher density of smaller trees which have a lower growth rate so that the mixed stand may come off equal to the pure stand but may differ considerably in size-structure (Binkley et al., 2006). Size-structure dynamics reveals on the one hand the reaction at tree level for trees of different sizes (quality of the mixing effect) and on the other hand the frequency of such individuals in mixed versus pure stands (quantity of the effect); both together (product of change of growth and frequency of such changes) yields the mixing effect at stand level.

The focus of this study is on the behavior of beech in mixed compared with pure stands. European beech is a late-successional species which would finally dominate on many sites in Central Europe as it can endure strong competition by other species in the early state of stand development (Ellenberg and Leuschner, 2010, p: 102, 288). Its behaviour during the rotation of 100-120 years, which is much shorter than its natural lifespan of 300-500 years, is relevant for both ecological and forest management. On most sites growth of beech is, especially in the early phase of stand development, much slower than spruce or oak so that beech temporarily falls behind when mixed with them (Mitscherlich, 1970, pp: 98 and 115-122). Our study reflects this by the smaller mean size of beech in mixed stands.

Based on the relationship between cumulative tree growth and cumulative tree mass Binkley (2004) and Binkley et al. (2006) distinguish the following four phases growth dominance in stand development: In Phase 1 of the stand development, when open-grown trees have only little competition, the cumulative growth can be proportional to the cumulative mass and thus $GC = 0$ (see Fig. 2b). In Phase 2, when larger trees get more dominant and suppress the growth of smaller neighbours, the cumulative growth increases progressively with cumulative mass and thus $GC > 1.0$ (see Fig. 2b). The Gini coefficients $GC_v$ and $GC_w$ of our experimental plots are mostly considerably lower than 1.0 and indicate that according to Binkley (2004) they are in Phase 2 of growth dominance in stand development. With increasing stand age a declining growth dominance of larger trees may cause a return to a proportional relationship between cumulative tree growth and cumulative tree mass (Phase 3) or even a reverse growth dominance (Phase 4) when smaller trees get superior to taller trees (Binkley, 2004).

The equality of the size distribution between the trees in a stand is increased by thinning from below and reduced by thinning from above (Kramer, 1988, p: 82). Growing in community with spruce and oak obviously increases the inequality of beech comparable with the effect of thinning-from above. Behind this tendency of beech towards inequality is the growth allocation in favour of taller trees, reflected by coefficient $GC_w$ and the id-d-relationship which are significantly higher in mixed versus pure stands. Because of the much more advanced concentration of growth on the taller stand members, the mean diameter of the removed beeches in relation the remaining ones is higher in mixed versus pure stands. This is the result of a stronger self- and alien-thinning effect and considered as one component of the “biological automation” in complex versus homogeneous stands (e.g., Knoke, 2009), in addition to natural regeneration and mechanical stability. Norway spruce and sessile oak are often ahead in size growth in the early and middle phase of stand development but show no significant changes regarding the parameters of the size-growth relationship, $GC_v$ and $GC_w$.

Its high shade tolerance and crown plasticity (Dieler & Pretzsch, 2013) nevertheless enables beech
to persist and often finally dominate the admixed species in the late phase of stand development. However, in order to achieve economically usable stem dimensions in reasonable rotation times, beech needs strong competition release by active thinning from above in order to compensate its size inferiority to neighbouring species in the early stand development phase (Wiedemann, 1951, p: 146).

Fig. 8 summarizes in a schematic representation the accelerated forward shift of the size of Norway spruce and sessile oak in mixture (species 1) as well as their slowing down effect on beech (species 2). In the analyzed temperate forests, where mainly light is limiting individual tree growth, the effect of mixing on size-structure dynamics can be conceptualized as shown in Fig. 8. In most cases one of the two even-aged species is ahead of the other regarding size development (in Figure 8 species 1 is ahead of species 2). We speculate that the leading species is often more light demanding and quicker in growth, while the slower species is often more shade tolerant. Then mixing can modify the size distribution compared with pure stands by accelerating the growth of dominant trees, e.g., by triggering their above ground growth in order to keep a given hierarchical status (Kennel, 1965). Species 2 which is behind the size growth of species 1 may cause a thinning-from-below effect on species 1 by out-competing smaller population members of species 1. In contrast, species 1 may reduce species 2 similar to a thinning-from-above effect.

So far, we analyzed the size-structure dynamics in order to better understand mixed-species stand development compared with pure stands. For forest practice the modification of the frequency distribution by mixing towards taller trees of the leading species (Norway spruce, sessile oak) and less small-sized and more uniform individuals in case of the beech may cause an improvement of the assortment yield, even when productivity at stand level may remain unchanged. Further comparison of the frequency distribution of species in mixed and pure stands may be extended to proxies of wood quality such as ratios of h/d or cd/d which may decrease and cl/h, which may increase wood quality (tree height, h; tree diameter, d; crown diameter, cd; crown length, cl). Frequency distributions of latter proxy variables of tree wood quality enable an integrated view on the effect of species mixing on both quality (quality aspects such as distortion, knottness, wood density, stiffness, and strength) and quantity effect (number of trees with respective qualities) of the produced wood and potential wood products.

**Conclusions**

The size distribution of beech in mixture mostly lags behind the pure stand, is more size-asymmetric, and the mortality shifts from the smaller diameter classes further to the taller trees than in pure stands. In contrast, the mixing effect of beech on the size size-structure dynamics of spruce and oak is much less pronounced. In this study the community of mixed tree species was conceptualized by its size-structure dynamics. As the species’ roles in a given mixture becomes most obvious in unmanaged stands where silvicultural operations do not superimpose natural dynamics we included just unmanaged or moderately thinned stands into this study. We showed how the size distribution, the growth distributions between the trees, and their mortality in mixed stands differs from the respective patterns and processes in pure stands. The analysis yielded promising results, though based on a rather limited number of available pure and mixed stands. Future application to a broader set of triplets covering different species combinations, stand density levels and site conditions may lead to a refined understanding of how mixing modifies the size-structure dynamics.
Classical measures such as skewness, kurtosis, standard deviation hardly provided further insight into mixing effects as they probably are too insensitive for characterizing shape modifications. Further studies should use more data material and more detailed methods. Analyzing the diameter distribution by its percentiles or by the parameters of the Weibull distribution (Bailey & Dell, 1973; Zutter et al., 1986) may contribute to further analyses of mixing effects. Both broader data and more appropriate quantification of the size-structure may enable even better insight into the effect of species mixing on the frequency distribution at species level, their interplay, and the resulting frequency distribution at stand level.

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References

Assmann E, 1970. The principles of forest yield study. Pergamon Press, Oxford, New York, 506 pp.
Bailey RL, Dell TR, 1973. Quantifying diameter distributions with the Weibull function. Forest Science 19(2): 97-104.
Binkley D, 2004. A hypothesis about the interaction of tree dominance and stand production through stand development. Forest ecology and management 190(2): 265-271.
Binkley D, Kashian DM, Boyden S, Kaye MW, Bradford JB, Arthur MA, Fornwalt PJ, Ryna MG, 2006. Patterns of growth dominance in forests of the Rocky Mountains, USA. Forest ecology and management 236(2): 193-201.
Bohn U, Gollup G, Hettwer C, Neuhäusova Z, Schlüter H, 2003. Map of the Natural Vegetation of Europe, scale 1: 2.5 million. Federal Agency for Nature Conservation, Bonn-Bad Godesberg.
Buongiorno J, Dahir S, Lu HC, Lin CR, 1994. Tree size diversity and economic returns in uneven-aged forest stands. Forest Science 40(1): 83-103.
Coomes DA, Allen RB, 2007. Mortality and tree-size distributions in natural mixed-age forests. Journal of Ecology 95(1): 27-40.
Camino R de, 1976. Zur Bestimmung der Bestandeshomogenität. Allgemeine Forst- und Jagdzeitung 147: 54-58.
Dieter J, Pretzsch H, 2013. Morphological plasticity of European beech (Fagus sylvatica L.) in pure and mixed-species stands. For Ecol Manage 295: 97-108.
Ellenberg H, Leuschner C, 2010. Vegetation Mitteleuropas mit den Alpen in ökologischer, dynamischer und historischer Sicht. Eugen Umler, Stuttgart, Germany.
Enquist BJ, West GB, Brown JH, 2009. Extension and evaluations of a general quantitative theory of forest structure and dynamics. PNAS 106(17): 7046-7051.
Franz F, 1965. Ermittlung von Schätzwerten der natürlichen Grundfläche mit Hilfe ertragskundlicher Bestimmungsgrößen des verbleibenden Bestandes. Forstw Cbl 84: 357-386.
Gadow K von, 1987. Untersuchungen zur Konstruktion von Wuchsmodellen für schnellwüchsige Plantagenbaumarten. Forstl Forschungsber München, Germany. 77, 147 pp.
Haight RG, Brodie JD, Adams DM, 1985. Optimizing the sequence of diameter distributions and selection harvests for uneven-aged stand management. Forest Science 31(2): 451-462.
Hara T, 1993. Mode of competition and size-structure dynamics in plant communities. Plant Species Biol 8: 75-84.
Kennel R, 1965. Untersuchungen über die Leistung von Fichte und Buche im Rein- und Mischbestand. Allgemeine Forst- und Jagdzeitung 136: 149-161, 173-189.
Knöke Th, 2009. Zur finanziellen Attraktivität von Dauerwaldwirtschaft und Überführung: eine Literaturanalyse. Schweiz Z Forstw 160(6): 152-161.
Kramer H, 1988. Waldwachstumslehre. Paul Parey, Hamburg, Berlin, Germany. 374 pp.
Mantel W, 1961. Wald und Forst. Wechselbeziehungen zwischen Natur und Wirtschaft, Rowohlt’s deutsche Enzyklopädie, Rowohlt, Hamburg, Germany.
Matyssek R, Schnyder H, Ößwald W, Ernst D, Munch JCh, Pretzsch H, 2012. Growth and defence on Plants, Ecological Studies 220, Springer, Heidelberg, New York, USA. 470 pp.
Mitscherlich G, 1970. Wald, Wachstum und Umwelt. 1. Wald, Wachstum und Umwelt. JD Sauerländer’s Verlag, Frankfurt am Main, Germany. 142 pp.
Morin X, Fauhe L, Scherer-Lorenzen M, Bugmann H, 2011. Tree species richness promotes productivity in temperate forests through strong complementarity between niches. Ecology Letters 14(12): 1211-1219.
Müller J, Brandl R, Buchner J, Pretzsch H, Seifert S, Strätz C, Veith M, Fenton B, 2013. From ground to above canopy – Bat activity in mature forests is driven by vegetation density and height. For Ecol and Manage 306: 179-184.
Murray DM, Gadow K von, 1991. Relationships between the diameter distributions before and after thinning. Forest Science 37(2): 552-559.
Nguyen TT, Biber P, Pretzsch H, 2012. Analysis and management of stand dynamics of Vietnamese dipterocarp forests by applying a dynamic growth model. Annals of forest science 69(5): 581-601.
Piotto D, 2007. A meta-analysis comparing tree growth in monocultures and mixed plantations. For Ecol Manage 255: 781-786.

Pretzsch H, 1998. Structural diversity as a result of silvicultural operations. Lesnictví-Forestry 44(10): 429-439.

Pretzsch H, 2009. Forest dynamics, growth and yield, From measurement to model. Springer, Berlin, Heidelberg, Germany.

Pretzsch H, 2014. Canopy space filling and tree crown morphology in mixed-species stands compared with monocultures. For Ecol Manage, 327: 251-264.

Pretzsch H, 2010. Zur Verteilung des Zuwachses zwischen den Bäumen eines Bestandes und Abhängigkeit des Verteilungsschlüssels von den Standortbedingungen. Allg Forst- u. -Ztg 181(1/2): 4-13.

Pretzsch H, Block J, Dieler J, Dong PH, Kohnle U, Nagel J, Spellmann H, Zingg A, 2010. Comparison between the productivity of pure and mixed stands of Norway spruce and European beech along an ecological gradient. Annals of Forest Science 67: 1-12.

Pretzsch H, Bielak K, Block J, Bruchwald A, Dieler J, Ehrhart HP, Kohnle U, Nagel J, Spellmann H, Zasada M, Zingg A, 2013. Productivity of mixed versus pure stands of oak [Quercus petraea (Matt.) Liebl. and Quercus robur L.] and European beech (Fagus sylvatica L.) along an ecological gradient. European Journal of Forest Research, 132(2): 263-280.

Preußler T, 1981. Ertragskundliche Merkmale oberbayerischer Bergmischwald-Verjüngungsbestände auf kalkalpinen Standorten im Forstamt Kreuth. Forstwissenschaftliches Centralblatt 100(1): 313-345.

Prodan M, 1951. Messung der Waldbestände. JD Sauerländer’s Verlag, Frankfurt am Main, Germany. 260 pp.

Rio M del, Schütze S, Pretzsch H, 2014b. Analyzing size-symmetric vs. size-asymmetric and intra vs. inter-specific competition in beech (Fagus sylvatica L.) mixed stands. For Ecol Manage 325: 90-98.

Schmid I, Kazda M, 2001. Vertical and radial growth of coarse roots in pure and mixed stands of Fagus sylvatica and Picea abies. Can J For Res 31: 539-546.

Schwinning S, Weiner S, 1998. Mechanisms determining the degree of size asymmetry in competition among plants. Oecologia 113: 447-455.

Webster CR, Lorimer CG, 2003. Comparative growing space efficiency of four tree species in mixed conifer-hardwood forests. For Ecol Manage 177(1): 361-377.

Weiner J, 1990. Asymmetric competition in plant populations. Trends Ecol Evol 5: 360-364.

Wenk G, Antanaitis V, Šmelko Š, 1990. Waldertragslehre. VEB Deutscher Landwirtschaftsverlag, Berlin, Germany. 448 pp.

West GB, Enquist BJ, Brown JH, 2009. A general quantitative theory of forest structure and dynamics. PNAS 106(17): 7040-7045.

Westphal C, Tremer N, Oheimb G, von, Hansen J, Gadow K von, Härdtle W, 2006. Is the reverse J-shaped diameter distribution universally applicable in European virgin beech forests? For Ecol Manage 223: 75-83.

Wiedemann E., 1951. Ertragskundliche und waldbauliche Grundlagen der Forstwirtschaft. JD Sauerländer’s Verlag, Frankfurt am Main, Germany. 346 pp.

Zhang C, Wei Y, Zhao X, Gadow K von, 2013. Spatial characteristics of tree diameter distributions in a temperate old-growth forest. PLoS ONE 8(3): e58983.

Zöhrer F, 1969. Ausgleich von Häufigkeitsverteilungen mit Hilfe der Beta-Funktion. Forstarchiv 40(3): 37-42.

Zutter BR, Oderwald RG, Murphy PA, Farrar JRRM, 1986. Characterizing diameter distributions with modified data types and forms of the Weibull distribution. For Sci 31(1): 37-48.