An excellent deep-ultraviolet birefringent material based on \([\text{BO}_2]\)\(_\infty\) infinite chains

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**Abstract**

Birefringent materials play indispensable roles in modulating the polarization of light and are vital in the laser science and technology. Currently, the design of birefringent materials operating in the deep-ultraviolet region (DUV, \(\lambda \leq 200\) nm) is still a great challenge. In this work, we developed a new DUV birefringent crystal LiBO\(_2\) based on \([\text{BO}_2]\)\(_\infty\) infinite chains in the Li-B-O system, which simultaneously achieves the shortest UV cutoff edge (164 nm) and the largest birefringence (\(\simeq 0.168\) at 266 nm) among all the reported borate-based DUV birefringent materials. Single crystals of LiBO\(_2\) with dimensions up to \(\varnothing 55 \times 34\) mm\(^3\) were grown by the Czochralski method, providing access to large-sized single crystal with low cost. Moreover, it has a high laser damage threshold and stable physicochemical properties. These outstanding characters unambiguously support that LiBO\(_2\) can be an excellent birefringent material for DUV application.

**Introduction**

Birefringent crystals are important materials in modern laser and polarization technology owing to their vital function to modulate the polarization of light\(^1\)–\(^5\). Various birefringent crystals including YVO\(_4\), \(\text{TiO}_2\), \(\text{LiNbO}_3\), \(\text{CaCO}_3\), and \(\alpha\)-Ba\(_2\)B\(_4\)O\(_6\) (\(\alpha\)-BBO)\(^10\) are commercially available to fabricate optical devices operating over the wavelength regions from ultraviolet (UV) to mid-infrared (mid-IR). Nowadays, the deep-ultraviolet (DUV, \(\lambda \leq 200\) nm) laser technology has been greatly accelerated due to the significant advancements of nonlinear optical (NLO) crystals\(^11\)–\(^18\) and laser frequency conversion techniques, that enable the output wavelengths below 200 nm\(^19\)–\(^22\). Consequently, the demand for polarization devices based on DUV birefringent crystals is extremely urgent. In general, two prerequisites should preferably be combined for a DUV birefringent crystal. First, the UV cutoff edge \((\lambda_{\text{cutoff}})\) should be as short as possible to achieve wide transparent range and high transmittance in the DUV region. A relatively high \(\lambda_{\text{cutoff}}\) would result in a narrow DUV transparent range (from \(\lambda_{\text{cutoff}}\) to 200 nm), besides, the transmittance in the spectral range that is close to \(\lambda_{\text{cutoff}}\) would be low, therefore, the working spectral range is limited\(^23\)–\(^24\). Second, a sufficient birefringence is preferred. A small birefringence leads to a small beam splitting angle of the polarizing prism, which is not conducive to the compactness of the whole device\(^25\). In addition, from a viewpoint of application, other requirements should include high laser damage threshold (LDT), stable physicochemical properties, and suitable for large size crystal growth, etc.\(^26\)–\(^28\). However, few commercial birefringent crystals can satisfy the requirements simultaneously, and the exploration of high performance DUV birefringent materials is still a great challenge.

Borate is one of the best material systems to explore DUV birefringent crystals\(^29\)–\(^33\). Specifically, the strong covalent B–O bonds are ideal for the transmission of DUV light and the \([\text{BO}_3]\) units with sp\(^3\) hybridization possess large polarizability anisotropy, of which the coplanar alignment is conducive to large birefringence\(^34\). Besides the commercial \(\alpha\)-BBO crystal, some other birefringent crystals based on different...
anionic groups of [BO$_3$]$^{35-}$, [B$_2$O$_5$]$^{36-}$, or [B$_3$O$_6$]$^{37-40}$ were reported. In our previous work, we proposed that the [BO$_2$]$^{\infty}$ infinite chain composed of corner-connected [BO$_3$] units can serve as an optimal functional unit for DUV birefringent materials design. A [BO$_2$]$^{\infty}$-based alkaline-earth metal borate, Ca(BO$_2$)$_2$, possessing both large birefringence and wide band gap was developed$^{41}$. With the in-depth study of the [BO$_2$]$^{\infty}$-based crystals, we realized that the Li-B-O system is even superior because of the following reasons: (i) Li has the largest electronegativity among alkali- and alkaline earth-metals, thus a shorter UV cutoff edge can be expected. (ii) Lithium borate, such as the famous NLO crystal LiB$_3$O$_5$ (LBO)$^{42,43}$, usually possesses desired high LDT that is important for practical applications. (iii) Lithium borates have a low melting point, which can make it easy to grow crystal. (iv) The small ionic radius of Li is beneficial to increase the [BO$_3$] density and thereby enhance the birefringence.

Guided by these ideas, we successfully developed a new [BO$_2$]$^{\infty}$-based birefringent crystal LiBO$_2$, which pushes the thresholds of $\lambda_{cutoff}$ to 164 nm and a birefringence to larger than 0.168 at 266 nm, achieving the best among all the reported borate-based DUV birefringent crystals. The theoretical analyses reveal that good coplanarity of the [BO$_2$]$^{\infty}$ chains (i.e., a small dihedral angle (DA) between adjacent [BO$_3$] planes), as well as the large density of the [BO$_3$] units leads to the large birefringence. Intriguingly, LiBO$_2$ is a congruent melting compound with a relatively low melting point, and does not exhibit first-order phase transition, which make it easier for growing large crystal. Moreover, the crystal has a high LDT and good physicochemical stability as well as a low production cost. These excellent attributes suggest that LiBO$_2$ is a superb birefringent material working in the DUV region.

Fig. 1 Thermal property, as-grown single crystals, and transmittance spectra of LiBO$_2$. a TG-DSC curves of LiBO$_2$. b As-grown LiBO$_2$ crystal via top-seeded growth method from the stoichiometric melt (top) and the theoretical morphology viewed along b-axis (bottom). c As-grown LiBO$_2$ crystal via the Czochralski method using [010]-oriented seed. d Transmission spectra of LiBO$_2$. e Comparison of transmission spectra of LiBO$_2$ and $\alpha$-BBO.
Results

The thermal study of LiBO$_2$ is shown in Fig. 1a. TG curve shows that there is scarcely any weight loss in the temperature up to 900 °C. Meanwhile, an endothermic peak at 845 °C and an exothermic peak at 722 °C are observed from the heating and cooling curves, respectively, which do not show any evidence of a first-order phase transition. The powder X-ray diffraction (XRD) pattern of the solidified melt agrees with that of the initial LiBO$_2$ powder (Fig. S1). These results indicate the congruent melting feature of LiBO$_2$, therefore, large single crystals, in principle, can be grown from stoichiometric melts. Figure 1b shows a LiBO$_2$ crystal grown from the stoichiometric melt by the top-seeded growth method. The distinguishable crystal facets are (100) and (001), which are in accordance with the predicted growth morphology according to the Bravais–Friedel and Donnay–Harker (BFDH) theory.\textsuperscript{44} Subsequently, colorless, high optical quality LiBO$_2$ crystal with sizes up to Ø55 × 34 mm$^3$ (Fig. 1c) was grown via the Czochralski method after a series of growth parameters optimizations within a short development period. It is worth to note that the crystal growth does not require a vacuum or inert atmosphere as the cases of MgF$_2$ and YVO$_4$ while the growth temperature is much lower than those of α-BBO and Ca(BO$_2$)$_2$.\textsuperscript{31,45–47} The relatively low growth temperature can not only reduce thermal stress induced defects and shorten the growth cycle, but also avoid many severe growth conditions such as high-power furnace and expensive iridium crucible, etc. Moreover, since there is no phase transition during the growth process, it is easier to obtain a large single crystal than α-BBO which suffers a first-order phase transition during the cooling process. Accordingly, the growth of LiBO$_2$ can be relatively efficient, cheaper, and easier.

The transmittance measurement of LiBO$_2$ (0.3 mm-thick plate, without coating) shows a wide transparency region of 164–3480 nm, and the transmittance at 193 nm is higher than 80% (Fig. 1d), which indicates that the application of LiBO$_2$ can cover a broad spectral region from DUV to near-IR. To further confirm the DUV transparent capacity, α-BBO was measured for comparison under the same condition (2 mm-thick plates, without coating). From Fig. 1e, we can clearly see that both crystals show high optical transmittance from 220 to 300 nm, in contrast, the transmittance of LiBO$_2$ below 200 nm is significantly higher than that of α-BBO (e.g., 75.3 % vs. 9.7 % at 193 nm). We would highlight that its superior DUV transparent range (164–200 nm) can cover multiple coherent light wavelengths of great interest (e.g., 177, 193 nm) for various applications including high resolution photoelectron spectroscopy and photolithography.

A (001) plate of LiBO$_2$ was employed to evaluate the refractive indices and their dispersion via the prism coupling method. The refractive indices values at 405, 514, 636, 965, and 1547 nm are summarized in Table S1, where $n_a$ represents the refractive index perpendicular to the $b$-axis in the (001) plane. The included angle between $d'$ direction and the $a$-axis of the crystal is 25.07 ° according to the symmetry of LiBO$_2$. Since LiBO$_2$ crystallizes in the monoclinic system, only crystallographic $b$-axis coincides with one of the optical principal axes ($x$, $y$, $z$, corresponding to dielectric principal axes), while both $a$- and $c$-axes have a certain angle with other two optical principal axes of the crystal. Therefore, the real birefringence ($\Delta n = n_z - n_c$) of the crystal should be larger than the current experimental values ($\Delta n' = n_a - n_c$) because $n_z$ should be close to but larger than $n_a$, while $n_c$ should be close to but smaller than $n_c$ in the case of LiBO$_2$. Nonetheless, the experimental data were fitted to the following Sellmeier equations to preliminarily evaluate the birefringence of LiBO$_2$ in a broader wavelength range,

\[
\begin{align*}
\frac{n_a^2}{\lambda^2} &= 2.567041 + \frac{0.020843}{\lambda^2 + 0.004167} + 0.0007501^2 \\
\frac{n_b^2}{\lambda^2} &= 2.553004 + \frac{0.019078}{\lambda^2 + 0.002827} - 0.0091091^2 \\
\frac{n_c^2}{\lambda^2} &= 2.159205 + \frac{0.011337}{\lambda^2 + 0.006320} + 0.0021351^2
\end{align*}
\]

where $\lambda$ is the wavelength expressed in micrometer. As shown in Fig. 2a, the difference between $n_a$ and $n_c$ is pretty large, $\Delta n' = n_a - n_c = 0.168–0.135$, in the wavelength range from 266 to 1064 nm. Figure 2b shows the comparison of LiBO$_2$ with other borate-based DUV birefringent crystals.\textsuperscript{33,35–41} The results indicate that LiBO$_2$ possesses the shortest DUV cutoff edge and the largest birefringence simultaneously.

LDT is one of the most important parameters of a birefringent crystal for practical use. The LDT measurements (1064 nm, 10 ns, 10 Hz) of high optical quality LiBO$_2$ and α-BBO crystals under the same conditions show that the LDT of LiBO$_2$ is about 2.3 times higher than that of α-BBO. As the resistance ability to laser damage for the crystal is significantly dependent on the quality of the crystal, the higher LDT can be anticipated when the crystal quality is further improved in the future.

A (001) plate of LiBO$_2$ was exposed in the air at room temperature for one month to test the chemical stability. After that, the transparency and weight did not change, indicating that LiBO$_2$ is stable in air and has good chemical stability. Mechanical hardness measurement on a (001) plate shows a Vickers hardness of 192 (HV0.3, 10 s), corresponding to a Mohs hardness of 3.3. This moderate hardness is beneficial for processing.

The DUV transparent capacity along with the large birefringence of LiBO$_2$ thus makes it an attractive
candidate to design DUV Glan-type polarizer, which has been first realized in Ca(BO$_2$)$_2$ by our group$^{41}$. Here we proposed a feasible design scheme for Glan polarizer based on LiBO$_2$ crystal. As shown in Fig. 3a, the Glan polarizer is composed of two identical rectangular prisms. Considering the convenience for prism cutting and fabricating, the triangle base of the prism could be (001) face, which is a cleavage plane that is relatively easy to be obtained from the as-grown crystal. Besides, bc-plane that is perpendicular to (001) face can be selected as the face of normal incidence, in which the difference of refractive indices along two polarized directions (b and c), $n_b - n_c$, is large enough in LiBO$_2$ for Glan-type polarizer design. The hypotenuse lateral face of the left prism is for the selective transmission of the polarized light beams: the polarized light along b-axis would be totally reflected while only the polarized light along c-axis can transmit through the adjacent prism when the apex angle of the prism is appropriate. The critical angle for total internal reflection is determined by the following equation:

$$i_c = \arcsin(1/n_1),$$

where $n_1$ is the refractive index along the polarized direction. To fulfill the requirement of DUV applications for LiBO$_2$, we calculated the corresponding $i_c$ for polarization along b- and c-axes in a wavelength ranging from 165 to 200 nm. In LiBO$_2$ crystal, the apex angle ($\theta$) of the prism should meet the condition as follows: 35.28° < $\theta$ < 39.26°, in the working spectral range of 165~200 nm. Note that the obtained tolerance range of
Ca(BO₂)₂ (0.1225 at 1064 nm).

3.72° (Fig. 4a), which is smaller than that of Ca(BO₂)₂

geometrically linked to form infinite [BO₂]∞ chains with different dihedral angles. The number of [BO₃] groups were chosen from 1 to 15 in the calculation. Structural models for Ca(BO₂)₂, NbMoBO₆ and KBe₂B₃O₇ are retrieved from Refs.41,56,57, respectively. Total and partial density of states (DOS) of LiBO₂. In addition, the density of [BO₃] units of LiBO₂ (26.86 per O atom) which is positively correlated to the birefringence (Fig. 4b), which is comparable to the experimental value (Δn’ = 0.168 at 266 nm). Figure 4f illustrates the electron density difference of LiBO₂ which clearly shows the electron distribution that can be attributed to the formation of B–O bonds. Response electron distribution anisotropy (REDA) analysis 49,50 was also performed to examine the contribution of the anionic groups. The bonding electron density difference (Δρ) of the structural units, i.e., [BO₂]∞ chains and [LiO₄] tetrahedra, along the optical principal axes were calculated. From Table 1, we can see that the [BO₂]∞ chains are the primary source of birefringence (~80%), which verify the effectiveness of our design strategy of DUV birefringent crystals using [BO₂]∞ chains.

In order to further understand the relationship between the structure and optical properties, first principles calculations were carried out. LiBO₂ has a direct band gap as illustrated in Fig. 4c. The total and partial densities of states (DOS) show that O-2p and B-2p states determine the valence band top and conduction band bottom (Fig. 4d), indicating that the band gap of LiBO₂ is dominated by [BO₃] units, that is, [BO₂]∞ chains. The birefringence (Δn) of LiBO₂ is calculated based on the relation between the wavelength and refractive index. Results show that LiBO₂ is a negative biaxial crystal (nₓ < nᵧ < nᵧ < nᵧ), and the calculated birefringence is as high as 0.166 at 266 nm (Fig. 4e), which is comparable to the experimental value (Δn’ = 0.168 at 266 nm). Figure 4f illustrates the electron density difference of LiBO₂ which clearly shows the electron distribution that can be attributed to the formation of B–O bonds. Response electron distribution anisotropy (REDA) analysis 49,50 was also performed to examine the contribution of the anionic groups. The bonding electron density difference (Δρ) of the structural units, i.e., [BO₂]∞ chains and [LiO₄] tetrahedra, along the optical principal axes were calculated. From Table 1, we can see that the [BO₂]∞ chains are the primary source of birefringence (~80%), which verify the effectiveness of our design strategy of DUV birefringent crystals using [BO₂]∞ chains.
Table 1  Bonding electron difference ($\Delta \rho$) of the bonds along the optical principal axes and contribution percent w (%) of the structural units that calculated by the response electron distribution anisotropy (REDA) model

| Units     | $\Delta \rho$ | w (%) |
|-----------|-------------|-------|
| [LiO$_4$] | 0.0118      | 20.6  |
| [BO$_3$]$^-$ | 0.0454      | 79.4  |
| Total     | 0.0572       | /     |

Discussion

In summary, we have successfully developed a new DUV birefringent crystal LiBO$_2$ by screening the alkali- and alkaline earth-metal borates with the optimal [BO$_3$]$^-$ infinite chains for achieving short DUV cutoff edge and large birefringence simultaneously. High-quality single crystals with maximum dimensions up to 55 x 34 mm$^3$ have been obtained. Comprehensive experimental and theoretical studies show that LiBO$_2$ exhibits both the largest birefringence (≥ 0.168 at 266 nm) and the shortest UV cutoff edge (164 nm) in comparison with other borate-based DUV birefringent materials. Moreover, it has a high LDT and stable physicochemical properties. Fascinatingly more, LiBO$_2$ crystal is easier in crystal growth attributed to its multiple merits including congruent melting, free of first-order phase transition, rather low melting point (845 °C) among birefringent crystals, and achievable growth in an open system with ambient air. In addition, LiBO$_2$ may have much lower production costs due to its low growth temperature, high production yields, and inexpensive raw materials. These outstanding characteristics clearly suggest that LiBO$_2$ is an excellent DUV birefringent material. Future work will focus on the machining of prisms to evaluate the refractive index dispersion using the minimum deviation technique, as well as the design, manufacturing and assessment of polarizing devices.

Materials and methods

Synthesis, crystal growth and structure detection

Polycrystalline powder of LiBO$_2$ was prepared by a conventional high temperature solid-state reaction method. A stoichiometric mixture of Li$_2$CO$_3$ and B$_2$O$_3$ was loaded into a platinum crucible, and then preheated at 700 °C for 24 h to decompose the carbonates. The product was ground thoroughly, and then gradually heated to 750 °C and held at this temperature for 72 h with several intermediate grindings and mixings. The phase purity of the sample was confirmed by powder XRD (Fig. S1).

Initially, top-seeded growth method was adopted to grow LiBO$_2$ crystal for preliminary assessment of optical properties. A vertical-tube furnace equipped with heating element of resistance wire, pulling and rotating system and programmable controller was employed. During the growths, the rotation speed was 5–10 rpm. After several crystal growth cycles, transparent crystals with well-developed facets were obtained. Oriented seed crystal was separated from the as-grown crystal for the subsequent Czochralski growth.

Large LiBO$_2$ single crystals with higher optical qualities were grown by the Czochralski method using a furnace with RF heating. To compensate for the loss of B$_2$O$_3$ caused by the volatilization, 0.5 mol% excess of B$_2$O$_3$ was mixed with LiBO$_2$ powder for melt preparation. Seed crystals with different orientations were tried and [010]-oriented seeds were finally adopted to optimize other growth parameters. Typically, the applied pulling rate was 0.2–1 mm·h$^{-1}$ and the rotation rate was 2–5 rpm. The diameters of the grown crystals were carefully controlled by power adjustment based on the observation during the crystal growth. After the crystals grew to a desired size, they were pulled up and separated from the melt manually. Afterwards, the crystals were cooled to room temperature at a rate of 5–30 °C·h$^{-1}$. The crystal growth was performed in ambient air condition and does not require a vacuum or inert atmosphere.

A single crystal of LiBO$_2$ was selected for the structure determination by single-crystal XRD. The detailed method is presented in the Supplementary Information. Results show that LiBO$_2$ crystallizes into the monoclinic space group of $P2_1/c$ with lattice parameters of $a = 5.8529(8)$ Å, $b = 4.3461(7)$ Å, $c = 6.4630(9)$ Å, $\beta = 115.071(10)$ °, $Z = 4$ (Table S2), in accordance with the data reported by Zachariasen.

Thermal analysis

The thermal gravimetric analysis (TG) analysis and differential scanning calorimetry (DSC) of LiBO$_2$ were carried out on a simultaneous NETZSCH STA 449 F3 thermal analyzer instrument under a flowing N$_2$ atmosphere. The crushed single crystal was enclosed in a platinum crucible, heated from 40 to 900 °C, and then cooled to 200 °C at a rate of 5 °C·min$^{-1}$.

Transmittance spectra

Transmittance spectra were measured on single crystals by vacuum UV analytical spectrophotometer under vacuum conditions (140–200 nm), SolidSpec-3700DUV spectrophotometer in a nitrogen gas atmosphere (175–2600 nm) and SHIMADZU IRAffinity-1 Fourier transform infrared spectrometer in the air (2500–25000 nm).

Refractive indices determination

A (001) plate of LiBO$_2$ was used to measure the refractive indices at the wavelengths of 405, 514, 636, 965,
and 1547 nm, on the Metricon model 2010/M prism coupler (Metricon Co.) The accuracy of the measurements is estimated to be $2 \times 10^{-4}$. The refractive indices along $a'$- and $b$-axes direction were measured by using transverse electric mode which tests the refractive indices parallel to the crystal plane. The refractive indices along $c$-axis were tested using transverse magnetic mode which tests the refractive indices perpendicular to the crystal plane.

**Laser damage threshold**

The laser damage threshold of LiBO$_2$ single crystal was measured on a pulsed Q-switched Nd:YAG laser (1064 nm, 10 ns, 10 Hz). The incident plane is (001) face that was optically polished. A commercial $\alpha$-BBO crystal was measured under the same conditions for comparison. An optical convex lens was used to obtain the laser beam with a diameter of 1 mm. The damage was confirmed afterward by observing the irradiated sites under a microscope.

**Mechanical hardness**

The Vickers hardness of a LiBO$_2$ crystal with (001) face was measured using a DHV-1000 microhardness meter, with HV0.3 and a dwell time of 10 s. Five points were tested, and the average value was calculated as the final value. Mohs hardness (HM) was calculated from Vickers hardness (HV) by using the following equation: $HM = 0.675(HV)/1.3$.

**Numerical calculation**

The electronic structure and optical properties were calculated by employing CASTEP package based on density functional theory (DFT) with the norm-conserving pseudopotentials (NCPs). The exchange-correlation functionals were Perdew-Burke-Ernzerhof (PBE) functional within the generalized gradient approximation (GGA). The plane-wave energy cutoff was set at 750.0 eV. The $k$-point grid was generated as $4 \times 4 \times 3$ using the Monkhorst-Pack grid parameters. The empty bands were set as 3 times of valence bands for the calculation of the optical properties. Because GGA method underestimates the bandgap, the scissors operators were utilized to shift the conduction bands to agree with the experimental band gap values, and then the refractive indexes were obtained by the real part of the dielectric function on the base of the Kramers-Kronig transform. The polarizability anisotropy of anionic groups was calculated using DFT implemented by the Gaussian09 package. B3LYP (Becke, three-parameter, Lee-Yang-Parr) exchange-correlation functional with the Lee-Yang-Parr correlation functional at the 6-31G basis set in Gaussian was employed.

Birefringence is sensitive to the anisotropy of the response electron distribution, corresponding to REDA index $\zeta = \sum_i N_i Z_i \Delta \rho_i/(n_i E_o)$. of the anionic groups contained in the same crystal, where $N_i$ is the coordination number of the nearest neighbor cations to the anion, $E_o$ is the optical bandgap, $\Delta \rho_i = \rho_{max} - \rho_{min}$, $\rho_{max}$ and $\rho_{min}$ are the maximum and minimum of the covalent electron density of the covalent bond on the optical principal axes of a crystal, and $n_i$ is the minimum refractive index.

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**Author contributions**

All authors contributed to the preparation of the manuscript. F.Z. and X.C. proposed the concept, designed the experiments, grew the single crystals, and performed the experiments. M.Z. grew the single crystals and supported the characterizations. W.J. performed the theoretical calculations. S.H. supported the crystal growth. Z.Y. supervised the theoretical calculations. S.P. designed and supervised the study. All the authors discussed the results and commented on the manuscript.

**Competing interests**

The authors declare no competing interests.

**Supplementary information**

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