Flux-sum analysis identifies metabolite targets for strain improvement

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Abstract 

Background: Rational design of microbial strains for enhanced cellular physiology through in silico analysis has been reported in many metabolic engineering studies. Such in silico techniques typically involve the analysis of a metabolic model describing the metabolic and physiological states under various perturbed conditions, thereby identifying genetic targets to be manipulated for strain improvement. More often than not, the activation/inhibition of multiple reactions is necessary to produce a predicted change for improvement of cellular properties or states. However, as it is more computationally cumbersome to simulate all possible combinations of reaction perturbations, it is desirable to consider alternative techniques for identifying such metabolic engineering targets.

Results: In this study, we present the modified version of previously developed metabolite-centric approach, also known as flux-sum analysis (FSA), for identifying metabolic engineering targets. Utility of FSA was demonstrated by applying it to Escherichia coli, as case studies, for enhancing ethanol and succinate production, and reducing acetate formation. Interestingly, most of the identified metabolites correspond to gene targets that have been experimentally validated in previous works on E. coli strain improvement. A notable example is that pyruvate, the metabolite target for enhancing succinate production, was found to be associated with multiple reaction targets that were only identifiable through more computationally expensive means. In addition, detailed analysis of the flux-sum perturbed conditions also provided valuable insights into how previous metabolic engineering strategies have been successful in enhancing cellular physiology.

Conclusions: The application of FSA under the flux balance framework can identify novel metabolic engineering targets from the metabolite-centric perspective. Therefore, the current approach opens up a new research avenue for rational design and engineering of industrial microbes in the field of systems metabolic engineering.

Keywords: Flux-sum, Constraints-based flux Analysis, Genome-scale metabolic modeling, Metabolic engineering, Strain design

Background

Previous microbial engineering for strain improvement was largely based on biological intuition and/or trial-and-error methods, such as random mutagenesis. However, with the recent advent of high-throughput experimental technologies and improved in silico modeling capabilities, there is growing interest in the application of the systems biology approach to metabolic engineering studies [1–3]. Notably, genome-scale metabolic models (GEMs) provide a convenient and cost-effective platform for systems biologists to carry out metabolic perturbation studies in silico and rationalize findings from high-throughput experiments. This practical utility consequently fueled the reconstruction of over 100 GEMs representing the metabolic organization of various organisms across all three domains of life [4, 5].

Specifically, in silico analysis of GEMs enables us to achieve the following goals: (1) interpreting high-throughput omics data, (2) aiding design of metabolic engineering strategies, (3) generating new testable hypotheses to gain knowledge of the biological system, (4) investigating inter-cellular and inter-species interactions and (5) understanding of complex genotype-phenotype relationships leading to discovery of emergent properties.
Among these, the successful application of GEM analysis to aid cellular metabolic engineering has been consistently reported in numerous studies ranging from simple *in silico* simulation of gene deletions [10, 11], to more sophisticated computational techniques such as OptKnock [12], OptReg [13], OptStrain [14], OptGene [15], flux response analysis [16], RobustKnock [17], flux scanning based on enforced objective flux [18], OptForce [19] and most recently, cofactor modification analysis [20] for identifying valid gene knockout, up-, down-regulation and cofactor engineering targets (see [21] for thorough review). These *in silico* methods share the common theme of identifying suitable genetically and environmentally perturbed conditions by optimizing the cellular objective, typically cell growth, under mass balance, reaction reversibility and flux capacity constraints. Basically, such a constraints-based technique mimics the wet-lab genetic engineering experiments by imposing relevant constraints on the metabolic reaction fluxes and can thus be considered “reaction-centric”. However, more often than not, these techniques have encountered the computational issue of combinatorial explosion due to consideration of multiple reaction perturbations. Hence, to deal with this limitation, an alternative method is needed to further expand our *in silico* capability of multiple reaction targets identification.

Recognizing that many metabolites are involved in multiple reactions, a “metabolite-centric” approach can potentially find individual metabolite targets implicating some combination of reaction flux constraints. In this way, the metabolite-centric flux-sum analysis (FSA) was initially utilized to evaluate the structural and evolutionary properties of cellular metabolism in *E. coli* [22, 23]. Later, the same concept was successfully utilized to compare and contrast the metabolic capabilities of *Z. mobilis* and *E. coli* [24]. Nonetheless, its potential applicability of identifying metabolic engineering targets for strain improvement remains unexamined. Therefore, in this study, we demonstrate the efficacy of FSA by applying it to *Escherichia coli* for increasing succinate and ethanol production, and reducing acetate formation as case studies.

**Results**

**Flux-sum analysis for identifying metabolic engineering targets**

In this work, we harness the previously presented computational technique, flux-sum analysis [22], to identify metabolite targets that will “force” the overproduction of desirable by-products or the reduction in formation of undesirable metabolites upon the attenuation or intensification of metabolite turnover, also known as “flux-sum”. The concept of “forcing” the desired metabolic behavior is similar to a previous study [19]. Briefly, first, the conventional constraints-based flux analysis problem is solved with biomass maximization as objective and the wild-type flux-sum of all metabolites are calculated as a reference. Second, the minimal and maximal flux-sum values of each metabolite are computed to determine the allowable range for attenuation and intensification from the reference state, respectively. Next, a MILP problem is sequentially solved for all metabolites to attain the maximum cell growth at various flux-sum perturbations between the calculated minimal and maximal values. Finally, using this growth values as additional minimum biomass production constraint, the same optimization problem is again solved for all metabolites to investigate whether the perturbation of a particular metabolite’s flux-sum improves the desired target compound production or not (see Methods). To demonstrate the applicability of this proposed framework, we apply it to the *E. coli* genome-scale metabolic model, thereby identifying the possible metabolite attenuation/intensification targets which can enhance the production of ethanol/succinate, and reduce the formation of toxic acetate. The list of identified best metabolite targets are summarized in Table 1 and will continue to examine each case in detail to gain a better understanding of their effects on cellular metabolism (see Additional file 1 for the target compound production profile under flux-sum perturbation of metabolites presented in Table 1).

**Ethanol production under flux-sum attenuation**

The flux-sums of individual metabolites are attenuated to investigate their effects on ethanol production. The ethanol production profile (Fig. 1) generated by FSA revealed that the attenuation of acetate and acetylphosphate flux-sums can “force” ethanol production rates to increase. It has also been demonstrated in previous experimental studies that deletion of the phosphate acetyltransferase gene (*pta*) resulted in improved ethanol production rate [25, 26]. The identification of acetate and acetylphosphate as flux-sum attenuation targets for ethanol overproduction is also an example of how parallel pathways compete for same carbon flux where the perturbation of one can positively favor the other (Fig. 2). This is similar to the previously identified essential metabolites located along parallel biosynthetic pathways which could cause sub-optimal distribution of metabolic fluxes and attenuated cell growth when their flux-sums were perturbed [22].

Another flux-sum attenuation target identified by FSA for the ethanol production is formate. Generally, acetyl-CoA in a cell can be synthesized in two ways. The pyruvate formate lyase (PFL) reaction yields acetyl-CoA and formate as the co-product. Another alternative is the pyruvate dehydrogenase (PDH) reaction that generates acetyl-CoA, CO₂ and NADH. Therefore, attenuating
formate flux-sum promotes acetyl-CoA formation through the PDH reaction, leading to increased NADH generation, which in turn drives the NADH-consuming alcohol dehydrogenase (ALCD) reaction towards ethanol production. Interestingly, it has been reported that a high flux through PDH can increase ethanol yield [27]. Hence, the construction of a PFL-repressed and PDH-overexpressed E. coli strain can be explored in future experimental validation to further improve ethanol production.

| Table 1 List of metabolic engineering targets |
|---------------------------------------------|
| Objective | Target metabolites | Flux-sum perturbation | Experimental validation |
| Enhance ethanol production | Acetate | Attenuation | [25, 26] |
| | Acetylphosphate | Attenuation | [25, 26] |
| | Formate | Attenuation | N.A. |
| | 6-Phospho-D-gluconate | Intensification | N.A. |
| | Erythrose 4-phosphate | Intensification | N.A. |
| | 5,10-Methylenetetrahydrofolate | Intensification | N.A. |
| | Sedoheptulose 7-phosphate | Intensification | N.A. |
| Enhance succinate production | Pyruvate | Attenuation | [11] |
| | Glyoxylate | Intensification | [30, 31] |
| | Menaquinone/menaquinol | Intensification | N.A. |
| Minimize acetate production | Acetate | Attenuation | [34, 35] |
| | Acetylphosphate | Attenuation | [34, 35] |
| | 3-Phosphoglycerate | Intensification | N.A. |
| | 4-Methyl-2-oxopentanoate | Intensification | N.A. |
| | Isocitrate | Intensification | [36] |
| | Lactate | Intensification | [34] |
| | Ribulose 5-phosphate | Intensification | N.A. |
| | Succinic semialdehyde | Intensification | N.A. |

Ethanol production under flux-sum intensification
Flux-sum intensification analysis identified several target metabolites such as 6-phospho-D-gluconate, erythrose-4-phosphate, ribulose-5-phosphate, sedoheptulose-7-phosphate and xylulose-5-phosphate that can improve ethanol production. Clearly, these metabolites are predominantly active in the NADPH-generating pentose phosphate pathway (PPP). Hence, flux-sum intensification of such metabolites will increase the formation of NADPH, which can be re-oxidized to NADP via the soluble NAD transhydrogenase (UdhA) reaction and simultaneously regenerate NADH. The elevated NADH regeneration rate can thus improve ethanol production. However, the in vivo activity of UdhA has been reported to be low [28] and this scenario of increased NADPH regeneration will most likely cause its accumulation that can possibly cause growth inhibition. Therefore, the simultaneous overexpression of UdhA and flux-sum intensification of PPP metabolites by overexpressing the glucose-6-phosphate dehydrogenase and gluconate dehydrogenase will be a promising strategy to increase ethanol production without the inhibitory effect.

Another target identified by the flux-sum intensification analysis is 5,10-methylenetetrahydrofolate (MLTHF), a key metabolite in folate metabolism. Examination of metabolic reactions involving MLTHF revealed that the metabolite can only be formed by glycine hydroxymethyltransferase reaction and the glycine cleavage reaction, where the latter reaction is coupled with NADH regeneration.
Furthermore, FSA predicts that fluxes through both the reactions can be increased when MLTHF flux-sum is intensified. Thus, such a metabolic perturbation will have a positive effect on the ethanol-producing pathway which requires NADH as the co-substrate.

### Pyruvate decarboxylase insertion alters ethanol production profile

In previous metabolic engineering studies, it has been reported that the insertion of pyruvate decarboxylase (PDC) and alcohol dehydrogenase II genes can significantly improve ethanol production [29]. We can mimic this metabolic engineering strategy by inserting the PDC reaction into the GEM of *E. coli*, iAF1260 model and increasing ALCD flux, which is also equivalent to intensification of acetaldehyde flux-sum. Our simulation has shown that the intensification of acetaldehyde flux-sum in the wild-type *E. coli* GEM without the PDC reaction did not result in consistently increasing ethanol production. Thus, we carried out flux-sum intensification on the modified GEM of *E. coli* with the PDC reaction to further understand how PDC insertion can influence the ethanol production profile.

The new simulation results indeed show that addition of PDC reaction to the metabolic network improved the ethanol production profile under acetaldehyde flux-sum intensification (Fig. 3). In addition, a slightly higher cell growth rate can be achieved when the PDC reaction is available. This phenomenon of enhanced ethanol production due to such a metabolic engineering strategy can be understood by examining the reactions originating from pyruvate to acetaldehyde (Fig. 4). Wild-type conversion of pyruvate to acetaldehyde occurs via PDH or PFL, and then acetaldehyde dehydrogenase (ACALD). The addition of PDC allows the engineered *E. coli* strain to directly convert the pyruvate into acetaldehyde directly without forming the acetyl-CoA intermediate. Such direct conversion may positively assist the ethanol production as it circumvents the possible limitations which are associated with CoA regeneration in the ACALD step. Interestingly, intensification of acetaldehyde flux-sum beyond a certain point in wild-type decreases the ethanol production as the excess acetaldehyde gets converted into acetate via aldehyde dehydrogenase and then into acetyl-CoA via phosphotransacetylase (PTA) and acetate kinase (ACK), forming a cycle.

### Succinate production under flux-sum attenuation

Similar to the ethanol production case, we apply FSA to identify metabolite targets for strain improvement in the aspect of succinate production. The corresponding profile under metabolite flux-sum attenuation upon glucose uptake indicated that pyruvate is the only metabolite which can be targeted for enhancing succinate production (Fig. 5). This result has also been experimentally confirmed, demonstrating the improvement of succinate production through the reduction of total metabolic fluxes towards pyruvate by knocking out the genes of pyruvate-forming enzymes [11]. Moreover, our simulation also shows that succinate production can be negatively affected when pyruvate flux-sum is excessively high.
attenuated (Fig. 5). Thus, we will further examine the corresponding flux distribution to gain a better understanding of how pyruvate flux-sum perturbation can alter the cellular metabolism.

Under the anaerobic condition, succinate dehydrogenase reaction is not utilized since oxygen is unavailable to regenerate the electron acceptor ubiquinone. Hence, instead of producing NAD through the ubiquinone-dependent NADH dehydrogenase reaction, NAD regeneration occurs mainly via ethanol-producing ACALD and ALCD reactions, which are part of the mixed acid fermentation pathway. Thus, by examining this pathway, we will attempt to explain how pyruvate flux-sum attenuation can lead to enhanced succinate production. From Fig. 2, it is clear that pyruvate is the precursor for acetate, ethanol, lactate and formate and synthesis. Pyruvate formation via the pyruvate kinase (PYK) and phosphoenolpyruvate/glucose phosphotransferase system (PTS) competes for the metabolic fluxes that could potentially flow towards succinate formation. Hence, attenuating pyruvate flux-sum favors the redirection of metabolic fluxes at the phosphoenolpyruvate branch towards succinate synthesis. Since pyruvate flux-sum attenuation also causes a concomitant decrease in NAD regeneration by LDH, ACALD and ALCD, the metabolic flux is preferably channeled towards succinate-producing fumarate reductase (FRD), where the NAD shortage can be compensated by the coupling of FRD with the menaquinone-dependent NADH dehydrogenase reaction. Therefore, the substitution of LDH, ACALD and ALCD by FRD as the major NAD regenerator can increase the succinate production under pyruvate flux-sum attenuation as depicted by the right section of the succinate production profile (Fig. 5). For the same reason, it may be possible that the in vivo deletion of ptsG and pykFA have given rise to more than eight-fold increase in succinate yield [11].

On the other hand, the left section of the profile (Fig. 5) can be explained by realizing that pyruvate flux-sum attenuation is also accompanied by decreased ATP regeneration due to lower ACK and pyruvate kinase (PYK) fluxes. Hence, when ATP regeneration is attenuated below the threshold which affects glucose uptake, we immediately observe a decrease in succinate productivity, thus explaining the triangular shaped succinate production profile under pyruvate flux-sum attenuation.

**Succinate production under flux-sum intensification**

Flux-sum intensification analysis allowed us to observe the increase in succinate production when the flux-sum of several metabolites involved in redox reactions and the glyoxylate pathway were intensified. As the succinate-forming FRD consumes menaquinol to produce menaquinone, flux-sum intensification of such metabolites is expected to directly promote succinate production. It should be noted that the iAF1260 model accounts for two species of menaquinones, demethylmenaquinone-8 and menaquinone-8, which were thus detected as potential targets for flux-sum intensification.

In the case of glyoxylate flux-sum intensification, its perturbation effect was understood by examining the TCA cycle with glyoxylate bypass. Under anaerobic condition, the metabolic flux through the TCA cycle is low: energy (ATP) is mainly regenerated by substrate-level phosphorylation rather than oxidative phosphorylation. Thus, increasing glyoxylate flux-sum will force a redistribution of fluxes away from the ethanol production pathway towards the TCA cycle. Consequently, the role of ACALD and ALCD in the ethanol production pathway as the major NAD regenerator is replaced by the succinate-producing FRD in the TCA cycle, similar to the metabolic state observed under pyruvate flux-sum attenuation. This strategy has also been demonstrated in a previous experimental study whereby the deletion of iclR, a repressor of the glyoxylate bypass operon aceBAK [30], increased glyoxylate pathway utilization and enhanced succinate production yield of more than eight fold [31].
Minimizing acetate secretion under flux-sum perturbation

From the viewpoint of strain improvement, acetate secretion is usually undesirable as it inhibits cell growth and biochemical production [32, 33]. Hence, metabolite flux-sum perturbations for reducing acetate secretion will be of interest in this section. For flux-sum attenuation, only metabolites directly involved in acetate formation pathway, such as acetyl-CoA and acetylphosphate, were identified as targets. Previous experimental studies have also validated that the knockout of acetate kinase (ackA) or pta, which is equivalent to attenuating acetylphosphate flux-sum, can effectively reduce acetate formation [34, 35].

On the other hand, for flux-sum intensification, we identified about 30 potential metabolite targets, some of which are shown in Table 1. These metabolites were found to be mostly present in parallel biosynthetic pathways that compete with the acetate pathway for the same precursors. Thus, intensifying the flux-sum of key metabolites in these pathways may deprive the acetate pathway of metabolic fluxes, leading to reduced acetate formation. Examples of these metabolites include lactate from mixed acid fermentation pathway, isocitrate from TCA cycle, and ribulose 5-phosphate from the pentose phosphate pathway and 4-methyl-2-oxopentanoate from the leucine biosynthetic pathway. Some of these perturbation strategies to reduce acetate production have also been verified experimentally, e.g. isocitrate flux-sum intensification through deregulation of isocitrate lyase [36] and lactate flux-sum intensification by overexpression of lactate dehydrogenase [34].

An interesting and novel flux-sum intensification target for reducing acetate formation is 3-phosphoglycerate (3PG). As 3PG is an upstream precursor required for producing acetate, it is unexpected that increasing its turnover rate will attenuate acetate production. However, further examination of the flux distribution indicated that as the 3PG flux-sum increases, the pathway for glyoxylate catabolic process becomes activated. In short, glyoxylate catabolic process begins the synthesis of glyoxylate from 3PG. Since 3PG is a precursor for serine biosynthesis, the utilization of the glyoxylate metabolic pathway redistributes the fluxes such that cell growth is lowered. Consequently, the decrease of both energy requirement and resources for acetate synthesis leads to less flux through acetate kinase. Interestingly, a concomitant production of succinate was also observed as a result of glyoxylate bypass utilization. Thus, the intensification of 3PG flux-sum via overexpression of glyoxylate catabolic process can be a desirable metabolic engineering strategy for reducing acetate formation and increasing succinate production.

Discussion

Recently, the application of flux-sum to a strain improvement study for vanillin production in S. cerevisiae was reported [37]. In that study, FSA was used to compute the minimum metabolite turnover which reflects the lower bound for the degree of resource allocation required to achieve a particular metabolic state. Subsequently, FSA was demonstrated to be a useful evaluation tool that provides insight into the cellular metabolism of engineered microbial strains from the metabolite perspective. Since the flux-sum concept can characterize resource distribution to various metabolites within the network, the application of FSA can be systematically utilized to identify metabolic engineering targets, rather than being used only as a supplementary tool to understand cellular metabolism. Accordingly, herein, we have proposed a systematic workflow to identify metabolic engineering targets using the FSA approach and demonstrated its applicability by applying it to E. coli for enhancing ethanol and succinate production, and reducing acetate formation. In general, this procedure can be simply applied to any other organism of interest whose genome-scale metabolic model is readily available. For example, we also applied the proposed FSA to S. cerevisiae using the iMM904 model [38] for succinate overproduction case and identified glyoxylate and acetyl-CoA as intensification and ethanol as attenuation targets, respectively (see Additional file 2 for details). Notably, the glyoxylate intensification strategy is very similar to the one identified in E. coli where the redirection of carbon flux towards glyoxylate cycle instead of the TCA cycle is beneficial for succinate overproduction. Collectively, such results reveal that the utilization of glyoxylate cycle could be a global strategy for succinate overproduction across different organisms.

The metabolic engineering targets identified using the metabolite-centric technique can be equivalent to the reaction targets obtained by the gene deletion-based approach. Thus, we compared the results of current work with that of OptKnock, OptReg and OptForce algorithms for the succinate overproduction case [19] to examine the uniqueness of the metabolite targets. Such comparison between reaction and metabolite targets revealed that although there are some comparable ones, not all the metabolites have an equivalent reaction(s) candidate (Table 2). For example, OptKnock consistently identified the deletion of PTAr and ACKr, corresponding to the attenuation of acetylphosphate and acetate, respectively. Similarly, the deletion/downregulation of PFL, as identified by OptKnock, OptReg and OptForce also correspond very well with the formate attenuation. Moreover, the overexpression of citrate synthase and aconitase in conjunction with the isocitrate dehydrogenase deletion may be an equivalent strategy to
augment the glyoxylate pool as identified by FSA. However, despite such comparable results, the pyruvate flux-sum attenuation for succinate overproduction does not have many equivalent targets in reaction-centric algorithms, except PYK deletion, which is presumably due to pyruvate’s association with multiple reactions. Intensification of menaquinol/menaquinone is unique target identified by FSA which does not have equivalent reaction-centric targets. Such results clearly demonstrate the efficacy of FSA in identifying novel metabolite targets that could only have been found via the multiple reaction deletion analysis. In this sense, FSA can be considered as a useful tool to circumvent the much higher computational cost of perturbing the large number of reaction flux combinations. Nonetheless, the flux-sum analysis method is not completely superior to conventional gene/reaction deletion analysis as we have also identified unique reaction targets using the latter method. Such examples include the downregulation of malate dehydrogenase (MDH) identified by OptForce, which prevents the malate from getting converted into oxaloacetate and redirects the flux towards fumarate, and then to succinate. Hence, we propose FSA as a complementary procedure within the general constraints-based flux analysis framework for strain improvement studies.

While using FSA for metabolic engineering, following the identification of metabolite targets, we envisage two different approaches to manipulate the flux-sum of target metabolites. The first approach could be based on the genetic engineering of genes around the target metabolite in the metabolic network. For example, in order to intensify the 6-phospho-D-gluconate production levels, we can either overexpress the corresponding biosynthetic gene, glucose-6-phosphate dehydrogenase (zwf) or forcefully reroute excess carbon flux into the desired pentose phosphate pathway by deleting the phosphofructokinase (pgi) genes from the parallel glycolytic pathway. In the second approach, more intuitive strategies such as the use of antimetabolites or co-feeding of certain pathway intermediates in the culture media could possibly restrict or enhance the target metabolites’ turnover rates. Although the use of such compounds to manipulate the flux-sum of a particular metabolite has never been attempted before, it could still be an interesting option to explore.

Conclusion
In this study, we successfully identified potential metabolite targets that can enhance the cellular physiology of E. coli using the FSA method developed in our previous work [22]. The original FSA framework was modified to elucidate changes in cellular metabolism under flux-sum perturbation, leading to the identification of metabolic engineering targets for strain improvement. The in silico simulation presented results that were highly consistent with previous wet-lab experimental observations, and also novel findings that could be validated in future works. In addition, comparison with reaction targets identified by
conventional gene/reaction deletion analysis shows that FSA has the capability to identify unique metabolite targets. Thus, the application of FSA complemented with conventional gene deletion analysis will provide researchers with a wider choice of potential metabolic engineering targets for strain improvement, which will be beneficial to the field of systems metabolic engineering.

**Methods**

**Constraints-based flux analysis**

Constraints-based flux analysis is an *in silico* method that simulates cellular metabolism such that a hypothetical cellular objective, usually cell growth, is maximized under stoichiometric and reaction capacity constraints [39–41]. The mathematical formulation is in the form of a linear programming (LP) problem as follows:

\[
\text{max } Z_i = \sum_j c_j v_j 
\]

Subject to:

\[
\sum_j S_{ij} v_j = 0 \\
0 \leq v_j \leq \beta_j
\]

where \(c_j\) is the coefficient of the desired cellular objective to be maximized, \(v_j\) is the flux of reaction \(j\) and \(S_{ij}\) indicates the stoichiometric coefficient of metabolite \(i\) involved in reaction \(j\). Values of \(\alpha_i\) and \(\beta_i\) can be specified based on experimental measurements or any hypothetical flux perturbation. Solving Eq. (1) by setting \(Z_i\) to be equal to cell growth rate, without any flux perturbation constraint, yields the wild-type (WT) metabolic flux distribution.

**Quantification of metabolite flux-sum**

Conventional constraints-based flux analysis does not provide a means to quantify the degree of individual metabolite utilization. Hence, we introduced the flux-sum concept to quantify metabolite turnover rates [22, 23]. Under the steady-state flux balanced condition, the consumption and generation rates for any metabolite are equal.

\[
\text{i.e. } \sum_j |S_{ij}v_j|_{\text{consumption}} = \sum_j |S_{ij}v_j|_{\text{generation}}
\]

Thus, the flux-sum of any intermediate metabolite \(i\), \(\Phi_i\), can be calculated as half the sum of the absolute rate of all reactions consuming or producing the metabolite:

\[
\Phi_i = 0.5 \sum_j |S_{ij}v_j| 
\]

Unlike the mathematical formulation of the basic constraints-based flux analysis, the flux-sum expression is nonlinear due to the modulus operator and directly imposing constraints on the flux-sum expression will result in a nonlinear problem. Hence, additional constraints are introduced to recast the problem to a linear integer form as discussed previously [22]:

\[
\Phi_i = 0.5 \sum_j (g_{ij}^+ + g_{ij}^-)
\]

where \(S_{ij}v_j = g_{ij}^+ - g_{ij}^-\)

\[
g_{ij}^+ \geq 0 \quad g_{ij}^- \geq 0
\]

\[
g_{ij}^+ \leq I_{ij}^+ \cdot M \quad g_{ij}^- \leq I_{ij}^- \cdot M
\]

\[
I_{ij}^+ \in \{0, 1\} \quad I_{ij}^- \in \{0, 1\}
\]

\[
I_{ij}^+ + I_{ij}^- = 1
\]

The positive variables, \(g_{ij}^+\) and \(g_{ij}^-\), refer to the generation and consumption components of metabolite \(i\) due to reaction \(j\), respectively. Binary variables, \(I_{ij}^+\) and \(I_{ij}^-\), serve as switches to turn the generation and consumption on and off such that only one of the component is active, affected by the \(I_{ij}^+ + I_{ij}^- = 1\) constraint. Big \(M\) can be an arbitrarily large flux value, e.g. 1000 mmol/gDCW-hr.

**Flux-sum analysis for identifying metabolic engineering targets**

To identify the attenuation and intensification metabolite targets which lead to the enhanced production of desired compound, we first need to quantify the flux-sum of all metabolites in the wild-type strain. This can be determined by first solving the constraints-based flux analysis problem (Eq. 1) with biomass maximization as objective, and then substituting the resulting flux distribution into Eq. (2). Next, we need to solve the below mentioned MILP problem to identify the flux-sum maxima and minima to determine the feasible ranges of individual metabolite flux-sum such that they can be attenuated or intensified within this limit:

\[
\text{max/min } \Phi_i = 0.5 \sum_j (g_{ij}^+ + g_{ij}^-) \text{ for fiven metabolite } i
\]

Subject to:

\[
\sum_j S_{ij}v_j = 0 \\
0 \leq v_j \leq \beta_j
\]

\[
S_{ij}v_j = g_{ij}^+ - g_{ij}^- \\
g_{ij}^+ \geq 0 \quad g_{ij}^- \geq 0
\]
to investigate the effects of flux-sum attenuation/intensification targets for succinate overproduction in Saccharomyces cerevisiae.

Implementation of flux-sum analysis

The FSA procedure is applied to the iAF1260 metabolic model of *E. coli* [42] to investigate the effects of flux-sum perturbation on ethanol, succinate and acetate production. All *in silico* simulations were carried out based on a glucose uptake rate of 1 g/gDCW-hr, such that all flux values can also be interpreted as yield in mmol/g glucose or g/g glucose. Since by-product formation in *E. coli* typically occurs under the anaerobic condition, we also constrained oxygen uptake rate to zero. All the optimization problems were solved using the GAMS IDE software version 22.4 [43] with IBM ILOG CPLEX solver.

Additional files

- **Additional file 1:** Ethanol, acetate and succinate production profiles in *Escherichia coli* under metabolite flux-sum attenuation/intensification. (DOC 129 kb).
- **Additional file 2:** Attenuation/intensification targets for succinate overproduction in *Saccharomyces cerevisiae*. (DOC 62 kb).

Competing interests

The authors declare that they have no competing interests.
Authors’ contributions
ML, TYK, BKSC, SYL and DL conceived and designed the in silico study. ML and BKSC performed the computational simulations and drafted the manuscript. ML, SYL and DL revised the manuscript. All authors read and approved the final manuscript.

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