Research Article

Intelligent Monitoring of Multistory Buildings under Unknown Earthquake Excitation by a Wireless Sensor Network

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Abstract

It is necessary to investigate techniques for monitoring structures under unknown earthquakes. For this purpose, an algorithm is proposed in this paper for the identification of structures and excitation of multi-story shear buildings with limited measurements of structural responses. The equation of motion of a multi-story shear building under ground motion is established in the absolute co-ordinate system, while the multi-story building is decomposed into substructures. A novel two-step Kalman estimator approach, which is not available in the previous literature, is proposed for the identification substructures and unknown ground motion with less computational effort. Then, for the purpose of intelligent structural monitoring, a new wireless sensor network is developed in this paper. The designed wireless sensor network has a two-level cluster-tree architecture. Hardware designs of the sensor unit and the cluster head are presented; especially the cluster head contains a low power digital signal processor with strong computing capacity. Thus, the wireless sensor network has the unique feature offers distributed computing at group level. Finally, the proposed algorithm is embedded into the wireless sensor network for intelligent structural monitoring and an experimental test shows the technique is effective for intelligent monitoring of multi-story buildings under unknown earthquakes.

1. Introduction

In the past decades, many structural identification and structural damage detection algorithms have been proposed, for example, see [1, 2]. Since some structural external excitations such as earthquakes or wind forces cannot be accurately measured under actual operating conditions, it is necessary to investigate algorithms for structural identification and damage detection under unknown earthquake excitation. Also, in structural health monitoring, the knowledge of external excitation is very useful for the safety evolution of structures.

Identification of structural parameters and unknown external excitation has been investigated by some researchers, for example, Wang and Haldar [3] developed iterative least squares approaches to identify simultaneously the structural parameters and ground motion of an earthquake. Chen and Li [4] proposed a statistical average algorithm for simultaneous estimation of structural parameters and earthquake-induced ground motion. Yang et al. presented several methods including extended Kalman filter with unknown excitation inputs (EKF-UI) [5] and the sequential nonlinear least square estimation (SNLSE) [6] for the identification of structural parameters as well as the unmeasured excitation inputs. However, the aforementioned identification approaches are based on the equation of motion established in the relative coordinate system for earthquake-excited structures. Since the absolute structural responses other than the relative structural responses are often measured in practice, there is a limitation for these approaches to be implemented in practice if the ground motion is unknown. Thus, Zhao et al. [7, 8] proposed hybrid identification methods for multistory buildings with unknown ground motion, in which the equation of motion of an n-story shear building subject to unknown ground motion is established in the absolute coordinate system. However, their methods request the measurements of all structural responses including the displacement, velocity, and acceleration responses. In practice, it is highly desirable to deploy as few sensors as possible [9, 10]. So, it is essential
to explore efficient algorithms which utilize only a limited numbers of measured responses of structures subject to unknown (unmeasured) earthquake excitation.

Extended Kalman filter (EKF) has been studied and shown to be a useful tool for structural identification with limited measurements of structural response [11, 12], but EKF approach requires that excitation inputs are measured [5]. Also, in the extended state vector, unknown structural parameters are included as an augmented vector. Hence the size of the extended state vector and the corresponding state equation are quite large [13]. If the order of the EKF is \(2n + m\) (\(n = \) number of structural DOFs, \(m = \) number of unknown structural parameters), the computational effort of the EKF is on the order of \((2n + m)^3\) [14]. An EKF with high order suffers from not only long computational time and may lead to divergent behavior for a large number of unknown parameters as identification is an inverted problem. It has been demonstrated that EKF is sensitive to initial estimates of the parameters and exhibit divergent behavior for large numbers of parameters to be estimated [15]. Also, such estimation requires large computation effort and storages, which can hardly be implemented by the microprocessors in the wireless sensor network. To remove the above drawbacks of the current EKF approaches, a two-step Kalman estimator approach, which is not available in the previous literature, is proposed in this paper. The numbers of unknown parameters to be estimated in each step are reduced. Then, unknown external excitations are estimated via the least squares estimation. So, the proposed algorithm identifies structural parameters and unknown excitation in a sequential manner, which simplifies the identification problem and reduces both the computational effort and storages compared with other approaches [5, 6].

For the identification of a large number of unknown parameters in large size structural systems, the computational efforts increase tremendously. Consequently, substructural identification approaches are used, in which a large size structure is decomposed into smaller size substructures with fewer unknown parameters [16–19]. The proposed identification algorithm is extended to large size multistory shear buildings by dividing buildings into small size substructures. In the absolute coordinate system, the unknown groundmotion input is applied on the 1st floor of the building as an unknown external force. For each substructure above the 1st floor, substructure is identified by the two-step Kalman estimator approach; for the substructure containing the 1st floor, Zhao et al. [7, 8] demonstrated that this substructural parameters and the ground motion cannot be uniquely identified. Herein, an algorithm is proposed in which substructural responses and parameters are identified by the proposed two-step Kalman estimator and the structural eigenvalue equation. Then, the unknown ground motion is estimated subsequently by least squares estimation and the Newmark-\(\beta\) method.

Therefore, the proposed algorithm enables distributed identification of substructures in multistory shear buildings with less computational effort and storage compared with other existing algorithms. It is suitable for the purpose of intelligent structural monitoring as it can be implemented into the computation core of a wireless sensor network (WSN) which has limited computation storage and capacity. So far, some innovative WSNs have been developed in recent years for intelligent structural monitoring [20–26]. Besides the merit of avoiding the problem of the extensive lengths of wires compared with the traditional wire-based monitoring system, another important virtue of a WSN is that it offers distributed data processing and computation capacity, which is particularly useful for the implementation of algorithms for intelligent structural monitoring [20, 27–29]. Since wireless communication consumes a large amount of energy, approaches which require transmission of long-time history records to the central server should be avoided. One of the efficient strategies is to embed data processing and analysis algorithms in the wireless sensor’s microprocessor and then just transmit small amount of useful results wirelessly. The embedded algorithms enable a WSN autonomously analyze data, which grants the network with “intelligent” characteristics. So far, some intelligent WSNs have been established [20, 21, 26–29], but most of data processing and analysis are designed at sensor level. Moreover, many WSNs require deploying a large number of sensors. Hierarchical clustering is considered as an efficient way to facilitate the operation of such networks and minimize the energy consumption [30–32]. In this paper, a hierarchical wireless sensor network is established [33, 34]. The distributed sensors are grouped into clusters, in which a cluster head is assigned to each cluster to control the communication in the allocated cluster. A cluster head not only serves as a router of the network but also possesses computational capabilities with the data collected from the sensor nodes in the cluster. Hardware designs of the sensor unit and the cluster head are presented, especially each cluster head has a low power digital signal processor (DSP) with strong computing capacity. This is the distinguishing unique feature of the proposed WSN different from other WSNs. Therefore, the proposed WSN provides parallel computation resources at group level, which is particularly useful for the implementation of substructure identification as the clusters in WSN match with substructures.

Finally, based on the advantages of the proposed distributed structural identification algorithm and the designed new WSN, intelligent monitoring of multistory buildings under unknown earthquake excitation can be conducted by embedding the proposed algorithm into the cluster heads of the designed WSN. To evaluate the performance of the proposed technique, experimental examination is demonstrated by shake table test of a scaled 8-story shear building under unknown ground motion.

2. Algorithm for the Identification of Building under Unknown Earthquake Excitation

Consider an \(n\)-story shear building subject to earthquake-induced ground motion as shown in Figure 1(a). It is well known that the equation of motion of the building with relative to the ground motion structure can be written as

\[
M\ddot{x}(t) + C\dot{x}(t) + Kx(t) = -M\ddot{x}_g(t),
\]
where $x(t)$, $\dot{x}(t)$, and $\ddot{x}(t)$, are vectors of displacements, velocity, and acceleration responses, respectively; $\ddot{x}_g(t)$ is the unknown earthquake-induced ground motion, $\mathbf{M}$, $\mathbf{C}$, and $\mathbf{K}$ are the mass, damping, and stiffness matrices of the building, respectively, and $\mathbf{I}$ is an unit vector. Usually, the mass of a building can be estimated with accuracy based on its geometry and material information.

2.1. Equation of Motion in the Absolute Coordinate System.
In practice, it is hard to accurately measure earthquake-induced ground motion under actual operating conditions, so $\ddot{x}_g(t)$ in (1) is unknown. As structural dynamic responses are usually measured by deploying some accelerometers, only limited absolute acceleration responses of the building can be measured. Then, (1) can be rewritten in the absolute coordinate system as

$$\mathbf{M}\ddot{\mathbf{x}}_a(t) + \mathbf{C}\ddot{\mathbf{x}}_a(t) + \mathbf{K}\mathbf{x}_a(t) = \mathbf{C}\dot{\mathbf{x}}_g(t) + \mathbf{K}\ddot{\mathbf{x}}_g(t),$$

where $\ddot{x}_a(t)$, $\ddot{x}_a(t)$, and $\mathbf{x}_a(t)$ are the absolute responses of structural acceleration, velocity, and displacement, respectively; $\ddot{x}_g(t)$ and $\mathbf{x}_g(t)$ are the velocity and displacement of ground motion, respectively.

Without the loss of generality, damping matrix of the building can be assumed as

$$\mathbf{C} = a_1\mathbf{M} + a_2\mathbf{K},$$

where $a_1$ and $a_2$ are two Rayleigh damping coefficients which depend on structural damping ratios and frequencies.

For a shear building, its stiffness matrix $\mathbf{K}$ is in the form as

$$\mathbf{K} = \begin{bmatrix} k_1 + k_2 & -k_2 & 0 & \cdots & 0 & 0 & 0 \\ -k_2 & k_2 + k_3 & -k_3 & \cdots & 0 & 0 & 0 \\ 0 & \cdots & \cdots & \cdots & 0 & 0 & 0 \\ 0 & \cdots & -k_i & k_i + k_{i+1} & -k_{i+1} & 0 & 0 \\ 0 & 0 & 0 & \cdots & \cdots & \cdots & 0 \\ 0 & 0 & 0 & 0 & -k_{n-1} & k_n & -k_n \\ 0 & 0 & 0 & 0 & 0 & -k_n & k_n \end{bmatrix},$$

that is in the absolute coordinate system, the building is excited on the 1st floor by an external force due to ground motion as shown in Figure 1(b). Since the ground motion is not measured, the external force is unknown.

2.2. Substructure Approach. If the story number $n$ is not small, the number of unknown parameters is quite large. Direct identification of the whole building requires a large computation effort and storages. Moreover, as an inverse problem, direct identification of a large number of unknown parameters can lead to the problems of ill-condition and computational divergent. Consequently, substructural identification approaches are used, in which a large size structure is decomposed into smaller size substructures with fewer
unknown parameters [16–19]. The multistory building is divided into \( m \) substructure as shown in Figure 2(a).

2.3. A Two-Step Kalman Estimator for the Identification of Substructure under Known Excitation. For substructure \( m \) (Sub. \( m \)) at the top of the building as shown in Figure 2(a), the equation of motion of the substructure with relative to the motion of its bottom floor (4th floor) can be written as

\[
M_m \ddot{x}_m^+ (t) + (a_1 M_m + a_2 K_m) \dot{x}_m^+ (t) + K_m x_m^+ (t)
= -M_m I_m \dot{x}_m (t),
\]

in which \( x_m^+ (t), \dot{x}_m^+ (t), \) and \( \ddot{x}_m^+ (t) \) are the relative acceleration, velocity, and displacement response vector of substructure \( m \), respectively, \( M_m \) and \( K_m \) are the mass and stiffness matrices of the substructure, respectively, \( \dot{x}_m (t) \) is the measured absolute acceleration response of the 4th floor, and \( I_m \) is a \( n \)-dimension unit vector as shown in Figure 2(b).

In (7), \( \dot{x}_m (t) \) is measured, so substructure \( m \) is excited by a known excitation. Introducing the state vector \( X_m^* = [x_m^* x_m^*]^{T} \), one can transform (7) into a state equation, that is,

\[
\dot{X}_m^* = \begin{bmatrix} \dot{x}_m^* \\ I \dot{x}_m - M_m \left[ (a_1 M_m + a_2 K_m) \dot{x}_m^+ (t) + K_m x_m^+ (t) \right] \end{bmatrix} = g(X_m^*, \theta_m, \dot{x}_m),
\]

(8)

in which \( \theta_m \) denotes the stiffness and damping parametric vector of the substructure.

Some sensors are deployed on the substructure to measure the response signals. Usually acceleration signals are measured and the observation vector of the substructure can be expressed in the discretized form as

\[
y_m [k] = D_m X_m^+[k] + v_m[k]
= h_m (X_m^+[k], \theta_m[k], \dot{x}_m[k]) + v_m[k],
\]

(9)

in which \( y_m[k] \) is the observation vector (measured relative acceleration responses) in the \( m \)th substructure at time \( t = k \times \Delta t \) with \( \Delta t \) being the sampling time step, \( X_m^+[k], \theta_m[k] \) and \( \dot{x}_m[k] \) are the corresponding discretized values at time \( t = k \times \Delta t \), \( D_m \) is the matrix associated with the locations of accelerometers in the concerned substructure, \( v_m \) is the measured noise vector, and

\[
h_m (X_m^+[k], \theta_m[k], \dot{x}_m[k])
= D_m \left[ -I \dot{x}_m[k] - M_m \left[ (a_1 M_m + a_2 K_m) \dot{x}_m^+ [k] + K_m x_m^+ [k] \right] \right].
\]

(10)

Extended Kalman filter (EKF) has been shown to be useful for structural identification with limited response outputs [11, 12], but in the EKF approach, the extended state vector includes the augmented unknown structural parameters. Structural state vector and the parametric vector are estimated simultaneously [13, 14]. Such estimation requires large computation effort and storages, which can hardly be implemented even by the DSP of a cluster head in the designed wireless sensor network. To remove these drawbacks of the EKF approaches, a two-step Kalman estimator approach, which is not available in the previous literature, is proposed in this paper.

In the first step, substructural response state vector is considered as an implicit function of the structural parameters. Then the discretized observation equation can be rewritten as

\[
y_m[k] = h_m (X_m^+[\theta_m[k]], \theta_m[k], \dot{x}_m[k]) + v_m[k].
\]

(11)

Assume \( \hat{\theta}_m[k | k - 1] \) is the estimated value of \( \theta_m[k] \) at time \( t = (k - 1) \Delta t \), \( h_m (X_m^+[\theta_m[k]], \theta_m[k], \dot{x}_m[k]) \), which is a nonlinear function of unknown parametric vector \( \theta_m \), can be linearized around \( \hat{\theta}_m[k | k - 1] \) through Taylor expansion, that is,

\[
h_m (X_m^+[\theta_m[k]], \theta_m[k], \dot{x}_m[k])
= h_m (X_m^+[\hat{\theta}_m[k | k - 1]], \hat{\theta}_m[k | k - 1], \dot{x}_m[k])
+ H_m[k] (\theta_m[k] - \hat{\theta}_m[k | k - 1]),
\]

(12)

where \( H_m[k] \) is derived based on the chain rule of partial differentiation as

\[
H_m[k] = H_{m,\theta}[k] + H_{m,X}[k] X_m^+[\theta_m[k]],
\]

(13)

\[
H_{m,\theta}[k] = \frac{\partial h_m}{\partial \theta_m} \bigg|_{\theta_m = \hat{\theta}_m[k | k - 1]};
\]

(14)

\[
H_{m,X}[k] = \frac{\partial h_m}{\partial X_m^+} \bigg|_{\theta_m = \hat{\theta}_m[k | k - 1]};
\]

(15)

\[
X_m^+[\theta_m[k]] = \frac{\partial X_m^+}{\partial \theta_m} \bigg|_{\theta_m = \hat{\theta}_m[k | k - 1]}.
\]

Then, the recursive solution for the parametric vector can be estimated based on Kalman estimator, which has been widely used in the field of structural control, as

\[
\hat{\theta}_m[k | k] = \hat{\theta}_m[k | k - 1] + K_{m,\theta}[k]
\]

\[
\times \left[ y_m[k] - h (X_m^+[\hat{\theta}_m[k | k - 1]], \hat{\theta}_m[k | k - 1], \dot{x}_m[k]) \right],
\]

(16)

in which \( K_{m,\theta}[k] \) is the Kalman gain matrix for \( \theta_m \) given by

\[
K_{m,\theta}[k] = P_{m,\theta}[k] H_m^+[k] \left( H_m^+[k] P_{m,\theta}[k] H_m^+[k] + R_\theta[k] \right)^{-1},
\]

(17)

and \( P_{m,\theta}[k] \) is given by

\[
P_{m,\theta}[k] = (I - K_{m,\theta}[k] H_m^+[k]) P_{m,\theta}[k - 1].
\]
In the second step, recursive solution for the substructural state vector is estimated by Kalman estimator after the recursive solution for the substructural parametric vector $\theta_m$

$$\hat{X}_m^*[k + 1 | k] = \hat{X}_m^*[k + 1 | k] + K_{mx}[k] \times \left[ y_m[k] - h_m(\hat{X}_m^*[k | k - 1], \hat{\theta}_m[k | k - 1], \hat{x}_m[k]) \right],$$

(18)

where

$$K_{mx}[k] = \frac{\partial X^*_m}{\partial \theta_m} \bigg|_{\hat{\theta}_m = \hat{\theta}_m[k | k - 1]}$$

is the Kalman gain matrix for state vector $X^*_m$.

For the estimation of the partial differentiation $\frac{\partial X^*_m}{\partial \theta_m}[k] = \frac{\partial \hat{X}_m^*[k | k - 1]}{\partial \theta_m}$, the direct differentiation method (DDM) is utilized in this paper. Differentiating both sides of (8) with respect to $\theta_m$, one can derive the equation for $X_{m,\theta}$ as

$$X_{m,\theta} = \frac{\partial g(X_m^*(\theta_m), \theta_m, \hat{x}_m)}{\partial \theta_m} = g(X_{m,\theta}, X_m^*(\theta_m), \theta_m).$$

(20)

Then,

$$X_{m,\theta}^*[k + 1 | k] = X_{m,\theta}^*[k | k - 1] + \int_{k\Delta t}^{(k+1)\Delta t} g(X_{m,\theta}, X_m^*(\theta_m), \hat{x}_m) dt.$$

(21)

Thus, the substructural relative responses and parameters in substructure $m$ can be identified by the proposed two-step Kalman estimator approach.

For the next substructure $m - 1$ (Sub. $m - 1$) of the building in Figure 2(a), the equation of motion of the substructure with relative to the motion of its bottom floor (jth floor) can be written as

$$M_{m-1} \ddot{x}_{m-1}^*(t) + (a_1 M_{m-1} + a_2 K_{m-1}) \dot{x}_{m-1}^*(t) + K_{m-1} x_{m-1}^*(t) = -M_{m-1} \ddot{x}_j(t) + k_{j1} x_{m-1}^*(t) + a_2 k_{j1} x_{m1}^*(t),$$

(22)

in which, $\ddot{x}_{m-1}^*(t)$, $\dot{x}_{m-1}^*(t)$, and $x_{m-1}^*(t)$ are the relative acceleration, velocity, and displacement response vector of substructure $m - 1$, respectively, $\ddot{x}_j(t)$ is the measured absolute acceleration response of the jth floor in the substructure, $\ddot{x}_{m1}^*(t)$ and $\dot{x}_{m1}^*(t)$ are the relative displacement and velocity responses of the 1st floor in substructure $m$ in Figure 2(b), that is, the relative displacement and velocity.
responses between the \( (r + 1) \)th and \( r \)th floors in the whole building in Figure 2(a).

As \( k_{j+1}, x_{m1}^*(t) \), and \( x_{n1}^*(t) \) have been indentified from the above identification of substructure \( m \), substructure \( m - 1 \) is also excited by a known excitation as shown in Figure 2(b). Therefore, the above two-step Kalman estimator approach can be used for the identification of the substructure state and parameters.

Analogously, for other substructures, above substructure 1 (Sub. 1) in Figure 2 can be identified sequentially by the proposed two-step Kalman estimator for the substructure under known excitation.

Thus, for the identification of substructure under known excitation, a two-step Kalman estimator is proposed in this paper. Recursive solutions for the substructural parameters and state vector are derived sequentially. Such solutions are not available in the previous literature. The numbers of unknown parameters to be estimated in each step are greatly reduced, which not only saves computational effort and storage but also avoids the difficulty of computational divergent in the inverse problem.

2.4 Identification of Substructure under Unknown Excitation.

For substructure 1 (Sub. 1) of the building in Figure 2, the equation of motion can be extracted from (6) as

\[
M_1 \ddot{x}_1^*(t) + (a_1 M_1 + a_2 K) \ddot{x}_1^*(t) + K x_1^*(t) = K e_{x_1}(t) + a_2 k_1 x_1^*(t) + k_1 x_1^*(t) + \begin{bmatrix} a_2 k_1 x_1^*(t) + k_1 x_1^*(t) \end{bmatrix} \theta_{(n-1) \times 1},
\]

(23)

in which \( \ddot{x}_1^*(t), \dddot{x}_1^*(t), \) and \( x_1^*(t) \) are the absolute acceleration, velocity, and displacement response vector of substructure 1, respectively, \( x_{21}^*(t) \) and \( x_{31}^*(t) \) are the relative displacement and velocity responses of the 1st floor in substructure 2, that is, the relative displacement and velocity responses between the \( (e + 1) \)th and \( e \)th floors in the whole building.

As \( \ddot{x}_1^*(t) \) and \( \dddot{x}_1^*(t) \) are unknown, substructure 1 is excited by both known an excitation on the \( e \)th floor and an unknown excitation on its 1st floor. Zhao et al. [7, 8] demonstrated through a multistory shear building that the 1st story stiffness \( k_1 \) and the unknown ground motion cannot be uniquely identified when the absolute forced structural response time histories are used directly. Therefore, the term containing \( k_1 \) in (23) is shifted to the right side and (23) is rewritten as

\[
M_1 \ddot{x}_1^*(t) + (a_1 M_1 + a_2 K_1) \dddot{x}_1^*(t) + K_1 x_1^*(t) = B_1 f_1 + B_1^\prime f_1^\prime,
\]

(24)

where \( K_1 \) is the stiffness matrix of the substructure 1 without \( k_1 \),

\[
f_1 = k_{e+1} x_{21}^*(t) + a_2 k_{e+1} x_{31}^*(t),
\]

(25a)

\[
f_1^\prime = a_2 k_1 x_1^*(t) + k_1 x_1^*(t) - a_2 k_1 x_{11}^*(t) - k_1 x_{11}^*(t),
\]

(25b)

\( x_{21}^*(t) \) and \( x_{31}^*(t) \) are the absolute velocity and displacement at the 1st floor level, respectively, and \( B_1 \) and \( B_1^\prime \) are the location vector of the known and unknown external forces, respectively.

For the identification of the unknown external excitation on the 1st floor of the building due to unknown ground motion, as shown in Figure 2(b), it is necessary to deploy a sensor on the 1st floor to measure its absolute acceleration response. The discretized observation equation in substructure 1 can be written as

\[
y_1[k] = h_1(x^*_1(\theta_1[k]), \theta_1[k]) + G_1 f_1 + G_1^\prime f_1^\prime,
\]

(26)

in which

\[
\begin{align*}
&h_1(x^*_1(\theta_1[k]), \theta_1[k]) = -D_1 M_1^{-1} \{ (a_1 M_1 + a_2 K_1) \dddot{x}_1^*(t) + K_1 x_1^*(t) \}; \\
& G_1 = D_1 M_1^{-1} B_1, \quad G_1^\prime = D_1 M_1^{-1} B_1^\prime,
\end{align*}
\]

and \( D_1 \) is the matrix associated with the locations of accelerometers in substructure 1.

Substructural state vector and parameters above the 1st floor can be identified by the proposed two-step Kalman estimator approach. Then, recursive solution for the unknown external excitation \( f_1^\prime \) can be obtained by least squares estimation approach as

\[
\begin{align*}
&\hat{f}_1^\prime[k + 1 | k + 1] = \left[G_1^\prime (G_1^\prime)^T \right]^{-1} (G_1^\prime)^T \\
& \quad \times \{ y_1[k + 1] - h_1(\hat{x}_1^*(\theta[k + 1 | k]), \theta[k + 1 | k]) - G_1 f_1[k + 1] \}
\end{align*}
\]

(28)

In order to estimate \( k_1 \), frequency spectra of the measured acceleration response are analyzed to obtain the vibration frequencies of the building. With an estimated value of the frequency of the building and its frequency equation as follows:

\[
|K - \omega^2 M| = 0,
\]

(29)

\( k_1 \) can be estimated based on the expansion of the determinant of matrix \( A = K - \omega^2 M \) and the formulation of the stiffness matrix \( K \) by (4), that is,

\[
det(A) = (k_1 + k_2 - \omega^2 m_1) A_{11} - k_2 A_{12} = 0,
\]

(30)

where \( A_{11} \) and \( A_{12} \) are the two determinants of the complementary submatrices (cofactors) of the two element in the 1st row of matrix \( A \), respectively.

With the recursive estimation of unknown external excitation \( f_1^\prime(t) \) and the estimated value of \( k_1 \), the unknown ground motion can be estimated from (25b) utilization the Newmark-\( \beta \) method for solving a first-order differentiation
The following recursive estimations can be derived by the Newmark-β method:

\[
\hat{x}_g[k+1] = \frac{1}{\beta \Delta t^2} \left( x_g[k+1] - x_g[k] \right) - \frac{1}{\beta \Delta t} \hat{x}_g[k] - \left( \frac{1}{2\beta} - 1 \right) \dot{x}_g[k],
\]

\[
\hat{x}_g[k+1] = \frac{\gamma}{\beta \Delta t} \left( x_g[k+1] - x_g[k] \right) + \left( 1 - \frac{\gamma}{\beta} \right) \hat{x}_g[k] + \left( 1 - \frac{\gamma}{2\beta} \right) \dot{x}_g[k] \Delta t.
\]

Inserting (31b) into (25b), one can obtain

\[
\left( a_2 k_1 + k_1 \right) \hat{x}_g[k + 1 | k + 1] = \hat{f}_d^s[k + 1 | k + 1] + a_2 k_1 \hat{x}_g[k + 1 | k] + k_1 \hat{x}_g^a[k + 1 | k]
\]

\[
+ a_2 k_1 \left( \frac{\gamma}{\beta \Delta t} \hat{x}_g[k | k] - \left( 1 - \frac{\gamma}{\beta} \right) \hat{x}_g[k | k] \right) \Delta t
\]

\[
- \left( 1 - \frac{\gamma}{2\beta} \right) \dot{x}_g[k | k] \Delta t.
\]

Thus, the recursive estimated values of the unknown ground motion are obtained by (31a),(31b), and (32).

It is noted that the proposed identification algorithm for substructure under unknown excitation is based on the Kalman estimator approach instead of the conventional Kalman filter approach in other identification algorithms. In the sequential Kalman estimator for the state vector and least squares estimation of the unknown excitation inputs, state vector at time \( t = (k + 1) \times \Delta t \) is initially estimated given the observation signals \( (y[1], y[2], \ldots, y[k]) \). Then, the unknown excitation at time \( t = (k + 1) \times \Delta t \) is estimated. On the other hand, in the Kalman filter approach, estimation of extended state vector at time \( t = (k + 1) \times \Delta t \) needs the observation signals \( (y[1], y[2], \ldots, y[k+1]) \), which contain the unknown excitation at time \( t = (k + 1) \times \Delta t \). Superiority of the algorithm based on Kalman estimator is obvious over the conventional Kalman filter approach for the identification of structural parameter under unknown excitation, which is the advantage of the proposed algorithm.

In summary, the proposed algorithm can identify structural parameters and unknown excitation in a sequential manner, which simplifies the identification problem and reduces both the computational effort and storages compared with other existing work.

After the identification of structural parameters of the building, structural damage can be detected from the changes of structural parameters, especially from the degradation of the identified stiffness parameters.

3. The New Wireless Sensor Network

Recently, a new wireless sensor network (WSN) has been designed by the authors. Some lab and in field experiment tests on the accuracy of data acquisition, time synchronization of measurement data and other capabilities of the wireless sensor units validated that the designed wireless sensor network possesses favorable performances of data collection, transmission, and distributed computation [34].

3.1. Topology of the New WSN. Many sensor networks require deploying many sensors and the transmission of recorded data via long distance. Hierarchical clustering is generally considered as an efficient and scalable way to facilitate the management and operation of such networks and minimize the total energy consumption for prolonged lifetime [33, 34]. In this paper, a two-level cluster-tree network topology is proposed for the wireless sensor network as shown in Figure 3. A large-size structure can be divided into substructures. The distributed sensor units deployed in a substructure are grouped into a cluster. A cluster head is assigned to each cluster to coordinate the sensors in its cluster and to collect data from them during monitoring. Communication between the distributed sensor units with their corresponding cluster head forms the lower level and the network of cluster heads forms the upper level as shown in Figure 3. In wireless communication, the relationship between power consumption \( E \) and communication distance \( d \) is

\[
E = kd^\alpha,
\]

where \( k \) and \( \alpha \) are constants that depend upon the nature of the sensor.
in which $2 \leq n \leq 4$. This means with the increase of communication distance, power consumption has a sharp increase. A cluster head not only serves as a router of the network messages but also possesses computational capabilities with the data collected from the sensor nodes in the cluster. Sensors in a cluster transmit recorded data in a single hop communications to the cluster head. Then, only calculation results by the cluster head are transmitted via the upper level routing. This avoids the transmission of raw data from a sensor node over long distance, which is of great help to decrease power consumption of sensor units as shown by (33).

In the designed WSN, wireless communication is based on the Zigbee communication protocol built on the IEEE802.15.4 wireless communication standard [35]. IEEE802.15.4 standard is intended to provide the most energy efficient wireless communication protocol available. It also offers a standardized wireless interface for wireless sensor networks, thereby ensuring compatibility between wireless sensor platforms with different designs and functionalities. Thus, while an immediate benefit of IEEE 802.15.4 is its low power consumption, a potentially greater benefit is that it offers a common protocol for wireless sensor networks.

The proposed wireless sensor network topology provides parallel computation between the substructures, which is useful for the implementation of computational algorithms for structural health monitoring. This is the unique feature of the proposed WSN different from other WSNs currently available. Finally, a center node combines the function of a cluster head with additional computational capabilities can be used for the final decision on structural health monitoring.

3.2. Hardware Design. Figure 4(a) shows the overall hardware design of the wireless sensor unit. The sensor unit mainly consists of six functional modules: (1) sensor interface; (2) signal conditioning; (3) sensor signal digitization; (4) computational core; (5) wireless communication; (6) battery management. To package the selected hardware components into a compact wireless sensor prototype, a two-layer printed circuit board was designed and fabricated. As shown in Figure 4(b), all electrical components are surface mounted to the printed circuit board. Most of the designs of the above six main modules are similar to those in other wireless sensors. Only the distinguishing features in
the hardware structure of the proposed wireless sensor are introduced herein.

Compared with other commercial wireless sensors, the Chipcon CC2430 is selected as the wireless transceiver in this design. The chip, named CC2430, released by Texas Instrument Corporation and is a true System-on-Chip (SoC) solution specifically tailored for 2.4 GHz IEEE 802.15.4 and ZigBee applications [36]. The CC2430 combines the excellent performance of the leading CC2420 RF transceiver with an industry-standard enhanced 8051 MCU, 32/64/128 KB flash memory, 8 KB RAM and many other powerful features. It has various operating modes and features of extra low consumption. When the microcontroller runs at 32 MHz, the CC2430 only consumes 25 mA for receiving and 27 mA for transmitting, while 0.3 μA current consumed in standby mode. Its short transition time between operating modes further ensure low power consumption. All these features make CC2430 highly suitable for the applications where ultra low power consumption is required.

In the computation core, a low-cost, low-power 8-bit Atmel AVR microcontroller (ATmega 128) is selected for the sensor unit. The microcontroller has 128 KB of ROM and 4 KB of SRAM is integrated with the microcontroller; however, this amount of SRAM is insufficient to store all the collected data. An additional 128 kB of SRAM (Cypress CY62128B) is interfaced with the microcontroller for the storage of sensor data. This microcontroller, together with certain internal and external memories, provides the capability of onboard data interrogation at the sensor level.

The hardware structure of a cluster head in the designed wireless sensor network is similar to that of a sensor unit except that its computational core is replaced by a TMS320C5409 digital signal processor (DSP) as shown in Figure 5(a). The attractive feature of TMS320VC5509A is the extra low power consumption compared with its strong computing ability. The TMS320VC5509A, a 16-bit fixed-point digital signal processor (DSP) produced by Texas Instrument Corporation, is based on the TMS320C55x DSP generation CPU processor core. The C55x CPU provides two multiply-accumulate (MAC) units, each capable of 17-bit × 17-bit multiplication in a single cycle. The clock rate of this chip is up to 200 MHz and its power consumption is only 0.5 mW/MIPS in full-speed operation while in lowest power mode is 0.05 mW/MIPS. The TMS320VC5509A also provides rich on-chip resources and peripheral set, such as 128 k*16-Bit on-Chip RAM, 64 k Bytes ROM, Two 20-Bit
the proposed algorithm into the new wireless sensor network. The proposed algorithm for distributed structural identification is coded in C language and embedded into the cluster heads and sensor nodes in the wireless sensor network, which grants the wireless sensor network with “intelligent” characteristics.

As shown in Figure 6, a multistory shear building is divided into \( m \) substructures in such a manner each substructural interface responses are measured by accelerometers. A corresponding WSN with \( m \) clusters is established in which sensors (s) and cluster heads (ch) are used to record some acceleration responses of the building under unknown earthquake excitation. Intelligent identification starts from substructure \( m \) at the top of the building. Sensors (s) in the substructure \( m \) transmit reordered acceleration responses to its cluster head (ch) in which the proposed two-step Kalman estimator algorithm is embedded to identify the substructural conditions and send the calculation results of structural parameters and substructural interaction force to the following substructure \( m - 1 \). Then, substructural state vector and parameters in substructure \( m - 1 \) are identified by the embedded algorithm in the cluster head (ch) and the identification results are sent to the lower substructure cluster head (ch). Such identification progress is performed sequentially till the 2nd substructure/cluster head. In the 1st substructure, each sensor node is embedded with the peak-picking (PP) algorithm to estimate the natural frequencies of the building based on the frequency response functions (FRFs) of recorded data by executing the embedded fast Fourier transform (FFT) algorithm \([28, 29]\). Then, each sensor node transmits both the recorded acceleration time history and the estimated natural frequencies of the building to the cluster head, where the embedded algorithm for identification of substructure under unknown excitation is executed to identify substructural parameters above the 1st floor, the unknown excitation on the 1st floor, the 1st story stiffness and the unknown ground motion based on the algorithm in Section 3.2. Finally identification results of structural parameters and unknown earthquake excitation are transmitted to the central PC, where a final decision on the monitoring of the building can be made, for example, structural damage is detected by tracking the degrading of the identified values of story stiffness parameters.

It is noted that in the proposed technique by the WSN, each sensor node transmits its recorded data to its cluster head nearby instead of direct to the central PC. Also, each cluster head just transmits its calculation results to its adjacent cluster head. Thus, the transmission of recorded data over long distance is avoided, which greatly reduced the power consumption in data transmission.

4.2. Experimental Validation. To assess the performance of the proposed technique for intelligent monitoring of multistory building under unknown earthquake excitation by the wireless sensing network, an eight-story shear type building in lab under shake table test is selected as an experimental example. As shown in Figure 7(a), the steel structure model behaves as a lumped mass shear building
because the building’s floors are constructed by rigid beams. The connection of the column-beam is shown in Figure 7(b). The structure model is mounted on a small size shake table which induces 1940 N-S El-Centro earthquake ground motion to the structure, but this ground motion is not unmeasured. Six light PCB accelerometers are deployed on the 1st, 3rd, 4th, 5th 6th and 8th floors to measure structural absolute acceleration responses of at the corresponding floor levels, respectively. Structural damage is simulated by replacing the flexible columns with thinner ones as shown in Figure 7(b), which results in the reduction of corresponding story stiffness $k_i$ ($i = 1, 2, \ldots, 8$). In the experiment,
structural damage is assumed to occur in the 5th story which leads to the reduction of $k_5$.

As shown in Figure 8, the building is divided into two substructures with floors 1–4 being the 1st substructure and floors 5–8 being the second one. The upper substructure is subject to the measured acceleration $\ddot{x}_a(t)$ while the lower substructure is excited by both the interface force and the unknown excitation due to unknown ground motion. Topology of the wireless sensor network is also shown in Figure 8. In each substructure, the deployed sensor nodes are grouped into a cluster. Each cluster is assigned with a cluster head (ch) to collect data from the sensor nodes during vibration. Based on the proposed technique described in above section, the identification results of story stiffness parameters and the unknown earthquake excitation are sent to the central server (PC).

Figure 9 indicates the results of the identified story stiffness parameters of the undamaged building shown in the PC server while the identified earthquake excitation results (solid line) are compared with the actual ground motion (dotted line) in Figure 10. For the ease of replacement of columns, each column is connected to the rigid beam by two screws at each ends, as shown in Figure 7(b). Thus, the structure model is not an ideal shear-type building, so there is certain difference between the identified story stiffness values and those of the analytical shear building model. From the comparison in Figure 9, it is noted that the proposed technique can identify unknown earthquake excitation with good accuracy.

Figure 11 indicates the identified story stiffness parameters of the damaged building shown in the central PC. By comparing the identification results of the story stiffness parameters shown in Figures 9 and 11, a final decision of structural damage detection can be made in the central PC. It is clearly shown that the proposed technique can autonomously detect structural damage based on the degrading of identified values of element stiffness parameters of $k_5$.

Although a small size 8-story structure model is used as an experimental test, the experiment results demonstrate the strategy and performance of the proposed technique.

5. Conclusions

In this paper, a technique is proposed for intelligent monitoring of multistory building under unknown earthquake excitation by a new wireless sensor network. Original contributions of the paper include: first, an algorithm is proposed for distributed structural identification detection with limited output measurements. It requires fewer structural output measurements compared with previous approaches. The algorithm is based on a proposed two step Kalman estimator for the identification of structural parameters and least squares estimation for unknown excitation. It cannot only identify structural parameters and unknown excitation in a sequential manner but also reduce both computational effort and storages compared with other existing work. Such straightforward derivation and analytical solutions are not available in the previous literature. Then, a new wireless sensor network with a two-level cluster-tree architecture is proposed. The distributed sensors are grouped into a cluster, in which a cluster head consists of a low power DSP with strong computing capacity. Thus, it provides parallel computation resources at group level, which is a particularly useful feature for the implementation of algorithm for intelligent structural health monitoring compared with other WSNs. Finally, intelligent monitoring of multistory building under unknown earthquake excitation is implemented by embedding the proposed algorithm into the new WSN. Such a technique is not available in the previous literature. A lab experimental test demonstrates that the proposed technique
is effective for intelligent identification of structural parameters, excitation and structural damage of multistory shear buildings with limited measurements of structural responses.

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