Microphysics in GRB central engine

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We study the structure and evolution of the accreting plasma in gamma ray burst central engines. The models are based on the general relativistic MHD simulations. The nuclear equation of state adequate for dense and degenerate plasma, is incorporated to the numerical scheme instead of a simple polytropic EOS. Plasma is cooled by neutrinos and energy is extracted from the rotating BH by magnetic fields. We discuss our results in the frame of the observable GRBs, and speculate about the origin of variability in the GRB jet emission. We also discuss the possible contribution from the heavy elements synthesized in winds from GRB engines to the kilonova emission.

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1. Introduction

The observed gamma ray bursts, which are generally grouped into two categories, namely the long and the short events, present a large variety of time profiles and variability of emission. Some of them consist of multiple peaks, while some present only a single fast rise and exponential decay in the prompt gamma ray lightcurve. Also, the energetics involved in the explosions, albeit it is enormously large in comparison with any other known cosmic events, may differ by several orders of magnitude depending on the burst, which is inferred by their fluence detected with gamma-ray instruments.

There are several unknown factors that might be responsible for this variety, which are intrinsically related to the physics of jets, such as the efficiency of gamma ray production in the internal shocks, or the efficiency of conversion between accretion and jet powers. Nevertheless, it is the accretion onto a black hole, which acts here and drives the explosion, with the gravitational potential energy being the most efficient mechanism of energy generation that we know.

To build a satisfactory model of the gamma ray burst central engine, like in all other cases where accretion processes are studied, we need to solve the set of basic equations of hydrodynamics: the continuity, energy and momentum conservation equations. These can be treated with various simplifying assumptions, such as the spherical or axial symmetry, or the prescription for the angular momentum transport with a so-called $\alpha$-disk model, which mimics the MHD turbulence. We can also work out a stationary solution, before solving for a time-dependent evolution of the flow. All of these assumptions did work reasonably well in the context of accreting black holes in persistent sources, such as X-ray binaries or centers of active galaxies. They were also used in the early works devoted to the GRB central engine modeling, and, to some extent, are still used in the GRB context.

What actually makes a difference between the black hole accretion process that occurs in GRB engines and all the other accreting black holes, is the microphysics of the plasma. Due to the extremely transient nature of events, and hence a huge accretion rate (which makes about one Solar mass to be swallowed by the black hole in a timescale of one second), the gas is very dense and hot, so that the onset the nuclear reactions occurs. Under the condition of $\beta$-equilibrium, the processes of electron and positron capture on nucleons, or electron-positron pair annihilation, lead to the efficient production of neutrinos. These neutrinos carry the energy and provide a cooling mechanism to the disk plasma, which is otherwise completely opaque to photons. Also, heavier elements, starting from Helium nuclei, are synthesized within the disk, as well as in the winds launched from its surface. These winds, possibly supported by the centrifugal force, but mainly magnetically- and neutrino- driven, may then provide a site for nucleosynthesis of heavy nuclei via the r-process. In this way, they provide a chemical enrichment to the circum-burst medium, and they may act as a source of power to the emission of 'kilonovae', which are driven by the radioactive decay of unstable nuclei.

2. Relativistic MHD model of gamma ray burst engine activity

We based our simulations on the High Accuracy Relativistic Magnetohydrodynamics code HARM [1] which provides solver for continuity and energy-momentum conservation equations in
GR:

\[ \nabla_\mu (\rho u^\mu) = 0 \quad \nabla_\mu T^{\mu\nu} = 0 \]

where the energy tensor contains electromagnetic and gas parts:

\[ T^{\mu\nu} = T^{\mu\nu}_{\text{gas}} + T^{\mu\nu}_{\text{EM}} \]

\[ T^{\mu\nu}_{\text{gas}} = \rho hu^\mu u^\nu + pg^{\mu\nu} = (\rho + u + p)u^\mu u^\nu + pg^{\mu\nu} \]

\[ T^{\mu\nu}_{\text{EM}} = b^2 u^\mu u^\nu + \frac{1}{2} b^2 g^{\mu\nu} - b^\mu b^\nu; \quad b^\mu = u_\nu F^{\mu\nu} \]

Here \( u^\mu \) is four-velocity of gas, \( u \) is internal energy density, and \( b^\mu = \frac{1}{2} e^{\nu\rho\sigma} u_\nu F_{\rho\sigma} \) and \( F \) is the electromagnetic stress tensor. Note that in the force-free approximation, \( E_\nu = u_\mu F^{\mu\nu} = 0 \).

In the simulations presented here in Fig. 1, the assumed initial condition invoked the relativistic equilibrium torus in the potential of a Kerr black hole, as described by [2]. In addition, the initial seed poloidal magnetic field, with \( A_\phi = (\rho/\rho_{\text{max}}) \), was imposed, and normalized with \( \beta = P_{\text{gas}}/P_{\text{mag}} = 50 \).

![Figure 1: Distribution of magnetic field lines, the gas to magnetic pressure ratio (left), neutrino emissivity (middle), and electron fraction (right), in the innermost 40 gravitational radii from the black hole. The evolved state of the flow is plotted at time \( t=2000 \, M \), after the initial conditions have been relaxed. This model global parameters adopt the black hole mass of \( 3 \, M_\odot \), its spin of \( a = 0.98 \), and disk mass is \( 0.1 \, M_\odot \).]

We observe that the field is advected with gas under the BH horizon and close to the poles, the mass density is low while the magnetic pressure is high. The black hole rotation helps launching the GRB jets in two ways.

The mass-energy is dragged with the flow under the black hole horizon, and it will provide a source of power to the relativistic jets, which are accelerated to the ultrarelativistic speeds. At large distances from the engine, they become transparent to photons and are the sites of gamma ray production.
We can evaluate the radial energy flux that is threading the black hole horizon, and define in this way the power of the Blandford-Znajek process:

\[ \dot{E} \equiv 2\pi \int_0^\pi d\theta \sqrt{-g} F_E \]

where \( F_E \equiv -T' \). This can be subdivided into a matter \( F_E^{(MA)} \) and electromagnetic \( F_E^{(EM)} \) part, although in the force-free limit the matter part vanishes [3]. This power scales with the black hole spin parameter, and in our simulations, for \( a = 0.98 \), we obtained the luminosity of the Blandford-Znajek process on the order of \( 10^{53} \) erg/s.

A similar order of magnitude is obtained via integration of the neutrino emissivities over the volume in our simulation. Also in this case, the results scale with the black hole spin, as the conditions in the plasma surrounding the fastly rotating black hole produce mode dense and hotter disks and hence are brighter in neutrinos. The emissivities are computed from the balance of nuclear reactions, which act on partially degenerate and relativistic species: free protons, neutrons, electrons and positrons. The contributions to the pressure and internal energy from all these species, which constitute the Fermi gas, are calculated numerically and updated consistently at every time step during the dynamical simulation (see [5] for the EOS details, and [6] for the details of numerical scheme and the GR MHD scheme implementation).

### 3. Synthesis of heavy elements in the engine under statistical equilibrium

We studied the synthesis of heavy nuclides in the plasma accreting onto the black hole in the GRB engine, or ejected in the winds from accretion torus. The physical parameters of the system, such as the black hole mass, its spin, and mass of the disk, shape the profiles of temperature and density in the torus. Exemplary distributions of these quantities, within the 500 gravitational radii from the black hole, are shown in Figure 2. In these calculations, we assume the conditions of nuclear statistical equilibrium, and the number density ratio of protons to neutrons achieves a steady state value. This so called ’electron fraction’ is then used to establish the rates of nuclear reactions, which together with the temperature and density profiles on our grid, are taken as an input for the reactions network. The latter is performed via the postprocessing of the results, and the currently used computational package is taken from [http://webnucleo.org](http://webnucleo.org). The computational methods are described in detail in the literature [7].

The nucleosynthesis results in abundant appearance of lightest isotopes, i.e., Helium, Lithium, and Beryllium, and then also the elements which mass numbers peak around \( \sim 80 \). It gives therefore the first peak of nuclides synthesized in the r-process. The subsequent second and third peaks will be produced via neutron capture, in the dynamical ejecta from the disk, at large distances. In the results presented in Figure 3 we observe the presence of a second peak at \( A \sim 120 \).
Microphysics in GRB central engine

Agnieszka Janiuk

Figure 2: Distribution of density (left) and temperature (right) in the accretion inflow and outflow, up to the distance of 500 gravitational radii from the black hole. The flow contains a small torus in the GRB engine, and a wind. The evolved state of the torus is taken at time \( t = 2000 \) M, after the initial conditions were relaxed. The outflow material reaches already the outer boundary, but at moderate altitudes. Global parameters of the model are \( M_{\text{BH}} = 3M_\odot \), \( a = 0.6 \), \( M_{\text{disk}} = 0.1M_\odot \).

Figure 3: Relative mass fraction of nuclei synthesized in the flow around a black hole in the GRB engine, i.e. torus and its wind. The parameters of the model are \( M_{\text{BH}} = 3M_\odot \), and \( M_{\text{disk}} = 0.1M_\odot \). Three lines mark the results obtained for a range of black hole spins, \( a = 0.6, 0.8, \) and \( a = 0.9 \).

Here, we show the distributions of isotopes that are produced in the surface layers of accretion disk, and within the outflowing gas. The conditions in the nuclear matter allow for abundant production of nuclei such as \( ^{28}\text{Si}, ^{32}\text{P}, ^{36}\text{Cl}, ^{40}\text{Ca}, \) and \( ^{44}\text{Ti} \). As the Figure show, the amount of \( ^{56}\text{Ni} \), peaks at almost 100\% regardless of the value of the black hole spin. All the other elements are about 100 times less abundant. The abundance of elements at around \( A = 80 \) (\( ^{76}\text{Cu}, ^{78}\text{Zn}, ^{80}\text{Se}, ^{82}\text{Ge}, ^{84}\text{Ga} \)), depends slightly on the value of the black hole spin, and is the largest for a maximally rotating hole (spin 0.98, model E). The elements present at around \( A = 120 \), i.e., \( ^{118}\text{Kr}, ^{120}\text{Sr}, ^{122}\text{Zr} \), are synthesized also in this model, and their abundance is not sensitive to the BH spin value. The model does not predict the third r-process peak at \( A \sim 200 \), which would require us to go beyond the equilibrium nucleosynthesis and follow the dynamical ejecta, with the extrapolation of the particle trajectories outside the computational domain. This is postponed to the future work.
4. Variability of the pulses in short GRB engine due to the magnetic barrier

In the previous simulations we focused on modeling the structure of torus that accretes onto the black hole in GRB engine. The detailed microphysics was introduced into the dynamical simulations, however these models assumed a moderately low magnetic field, normalized with the gas to magnetic pressure ratio of $\beta = 50$, and with an initial poloidal configuration. The magnetic field lines traced the constant density isolines in the torus. In the last part of our study we present the study of magnetic field influence on the resulting jet outflows and their variability.

Here we adopt a simplified, polytropic equation of state in the gas, with the index of $4/3$, which is relevant to describe the flow consisting of relativistic particles. The degeneracy of species is now neglected. However, we allow for an extremely high magnetisation ($\beta = 3 \times 10^{-3}$). For comparison, we present also the results for an almost completely thermally dominated flow ($\beta = 3 \times 10^{18}$).

![Figure 4: Time profiles of the ejected pulses in the extremely highly magnetized (right) and very mildly magnetized (left) central engines. The evolved state of the torus is taken at time $t=1600$ M after the initial conditions were relaxed. The global parameters of the flow are black hole mass $3 M_\odot$ and its spin is $a = 0.9$.](image)

The main focus is now given to the time variability of blobs ejected along the rotation axis of the black hole (a Kerr hole with a spin of $a = 0.9$ was adopted here), which is quantified by the value of their Lorentz factor. The thermally dominated and magnetically dominated models presented in Fig. 4 yield the $\Delta t_{\text{blobs}}$ on the order of $4.9 \times 10^{-3}$ sec, and $5.9 \times 10^{-4}$ sec, respectively. Also, the lower $\beta$ parameter produces higher Lorentz factors of the jets. This result provides a quantitative way to estimate the magnitude of magnetic field of the progenitor, basing on the observed profiles of the GRB lightcurve. We note here that, due to the significant acceleration our outflow achieves, it was necessary to consider a gamma barrier and test different values to exclude any implication on the launched jet variability. The selected value is $\gamma_{\text{max}} = 50$ and is common for all models. Going beyond this limitation is the subject of our future study.

5. Conclusions

A reliable model of the process leading to the high energy emission in the GRB jets requires detailed modeling of the central engine that is at the base of GRB and drives the jets. This is
done in our simulations by self-consistently solving the equations of General Relativistic magneto-hydrodynamics. In this way we are able to quantify the conditions sufficient for the appearance of magnetically driven jets, and also for the uncollimated winds (outflows) from the engine. We also argue for the neutrino-antineutrino annihilation process being comparable in its efficiency of driving the jets to the well-established Blandford-Znajek mechanism.

By postprocessing of our results, we are aiming to quantify the amounts of heavy nuclei produced in the GRB engine and its outflows ejecta. In addition to the a possible detection of heavy nuclei and their radioactive decay signal in the afterglows, the variability of prompt GRB emission is the main and direct observable. Both these quantities link our modeling to the observable GRB sources.

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References

[1] C.F. Gammie, J.C. McKinney, G. Toth, *HARM: A Numerical Scheme for General Relativistic Magnetohydrodynamics* ApJ 589 444 (2003)

[2] L.G. Fishbone, V. Moncrief, *Relativistic fluid disks in orbit around Kerr black holes* ApJ 207 962 (1976)

[3] J.C. McKinney, C.F. Gammie, *A Measurement of the Electromagnetic Luminosity of a Kerr Black Hole* ApJ 611 977 (2004)

[4] A. Janiuk, P. Mioduszewski, M.A. Moscibrodzka, *Accretion and Outflow from a Magnetized, Neutrino Cooled Torus around the Gamma-Ray Burst Central Engine*, ApJ 776 105 (2013)

[5] A. Janiuk, Y.-F. Yuan, R. Perna, T. DiMatteo, *Instabilities in the Time-Dependent Neutrino Disk in Gamma-Ray Bursts*, ApJ 664 1011 (2007)

[6] A. Janiuk, *Microphysics in the Gamma-Ray Burst Central Engine*, ApJ 837 39 (2017)

[7] G. Wallerstein et al., *Synthesis of the elements in stars: forty years of progress*, Rev. Mod. Phys. 69 995 (1997)