A New Force Field for OH$^-$ for Computing Thermodynamic and Transport Properties of H$_2$ and O$_2$ in Aqueous NaOH and KOH Solutions

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1. INTRODUCTION

Modeling aqueous alkaline solutions is of interest for a broad array of manufacturing and separation processes. Aqueous alkaline solutions containing potassium hydroxide (KOH) and sodium hydroxide (NaOH) are often used for electrolysis and in fuel cells due to their high ionic conductivities and low cost. NaOH and KOH have solubilities exceeding 18 mol/kg in water at 293 K (and above) and significantly influence the thermophysical properties of the solution. The interplay between different thermophysical properties (e.g., densities, viscosities, and ionic conductivities) of aqueous NaOH and KOH solutions influences the product gas purity, and the energy (and Faradaic) efficiency of alkaline-water electrolyzers. Knowledge of the thermodynamic and transport properties of hydrogen (H$_2$) and oxygen (O$_2$) gas in aqueous NaOH and KOH solutions is therefore highly relevant for optimization and process design of electrolyzers.

Modeling electrolyte systems is a challenging endeavor because of the strong long-range ionic interactions, which make the solutions highly nonideal. Electrolyte solutions are commonly modeled using semiempirical equations of state and molecular based simulations. Semiempirical equations provide a rapid and convenient method for the prediction of thermophysical properties. The quality of these equations depends on the availability of accurate experimental and simulation data. For aqueous alkaline solutions, experimental data for self-diffusivities and solubilities of H$_2$ and O$_2$ at high concentrations (above 4 mol/kg), temperatures (323–373 K), and pressures (above 50 bar) is lacking, especially in the case of aqueous NaOH solutions. These temperatures (ca. 353 K) and concentrations (4–12 mol/kg electrolyte solution) are especially relevant for alkaline electrolyzers. Molecular simulations (i.e., molecular dynamics (MD) and Monte Carlo (MC)) can be used as a complementary approach to experiments to provide insight at conditions for which experimental data are limited and difficult to obtain due to high temperatures, pressures, and the
corrosiveness of the solution (in case of strong alkaline solutions).

Molecular simulations of electrolyte systems can be studied using either ab initio simulations or force-field-based methods.\textsuperscript{1,3,2,3} Ab initio simulations have the potential to more accurately describe the structure and solvation of the ions,\textsuperscript{4,3,2,2,4} but these simulations are computationally expensive and are limited to systems comprising hundreds of atoms for time scales of the order of pico-seconds. To precisely calculate transport properties of fluids, long simulations of several nanoseconds are essential.\textsuperscript{24,35} To account for ion–ion and ion–water interactions at high electrolyte concentrations, water molecules need to be modeled explicitly,\textsuperscript{16,3} which makes the calculations more costly. To overcome both the time and system-size restrictions of ab initio calculations, force-field-based methods are usually preferred for large-scale production of thermophysical data.

Force fields for aqueous electrolytes can be polarizable or nonpolarizable.\textsuperscript{38-41} The nonpolarizable TIP4P/2005 water model\textsuperscript{42} has proven to be quite suitable for predicting densities, viscosities, and self-diffusivities of water.\textsuperscript{32-44} In an attempt to model the effective charge screening that occurs in electrolyte solutions, ions are modeled as scaled charges in nonpolarizable force fields.\textsuperscript{1} Prior research has demonstrated that the use of scaled charges significantly helps in capturing the correct dynamics of ions.\textsuperscript{38,43-45} Scaled charge models for ions such as Na\textsuperscript{+}, K\textsuperscript{+}, and Cl\textsuperscript{−} have been developed by Zeron et al. (the so-called Madrid-2019 force field)\textsuperscript{38,47} and used in combination with the TIP4P/2005 water model.\textsuperscript{38} These force fields yield reasonable predictions for densities, dynamic viscosities, and self-diffusivities of aqueous electrolytes with a scaled charge of 0.85 for concentrations up to 4 mol/kg salt.\textsuperscript{38} However, the dynamic viscosities computed using the Madrid-2019 force field deviate from experiments at higher molalities. To address this, Vega and co-workers have developed a new force field called the Madrid-Transport with a scaled charge of 0.75.\textsuperscript{47} This force field can accurately predict dynamic viscosities of aqueous NaCl and KCl solutions up to their solubility limit.\textsuperscript{47} Despite the importance of alkaline systems, there is no Madrid-force field for OH\textsuperscript{−} to accurately predict densities and dynamic viscosities of aqueous NaOH and KOH systems. Existing OH\textsuperscript{−} force fields are often used to simulate the solvation energy\textsuperscript{48-50} and structure,\textsuperscript{51-56} and cannot be used directly in combination with the TIP4P/2005 water model and the Madrid-force fields\textsuperscript{38,47} for Na\textsuperscript{+} and K\textsuperscript{+} ions as they do not use scaled charges of -0.85 or -0.75.

Here, we propose several nonpolarizable two-site OH\textsuperscript{−} force fields with scaled charges of -0.85 and -0.75, respectively. One of the newly proposed OH\textsuperscript{−} force fields with a scaled charge of -0.75 yields accurate predictions for both densities and dynamic viscosities of aqueous NaOH and KOH solutions for concentrations ranging from 0 to 8 mol/kg, at temperatures ranging from 298 to 353 K. We use this force field to compute the self-diffusivities of H\textsubscript{2} and O\textsubscript{2} in aqueous NaOH and KOH solutions using MD. Solubilities of these gases as functions of concentrations, and temperatures, and pressures are computed using Continuous Fractional Component Monte Carlo (CFCMC) simulations.\textsuperscript{57-59} Our data, obtained from molecular simulations, are compared to available experimental data on H\textsubscript{2} and O\textsubscript{2} in KOH solutions. Our simulations can adequately describe the trends observed in experiments for variations in both concentration and temperature. The self-diffusivities and solubilities of H\textsubscript{2} and O\textsubscript{2} in NaOH and KOH solutions are then fitted to semiempirical engineering equations. These engineering equations can be used for process modeling, and for optimizing electrolyzers and fuel cells.\textsuperscript{12}

This paper is organized as follows. In section 2, details on the force fields are provided, and the molecular simulation (MD and MC) techniques are explained. In section 3, force field optimization of OH\textsuperscript{−} is discussed, and the results for viscosities, H\textsubscript{2} and O\textsubscript{2} self-diffusivities, and solubilities at temperatures ranging from 298 to 353 K are provided. Our conclusions are summarized in section 4.

2. METHODOLOGY

2.1. Force Fields. The four-site TIP4P/2005 water model is used in all simulations.\textsuperscript{12} This model can accurately describe the densities and transport properties of pure H\textsubscript{2}O and of gases dissolved in H\textsubscript{2}O for a wide range of conditions.\textsuperscript{31,42-44,61} The two-site Bohn model\textsuperscript{62} is used for modeling O\textsubscript{2}. For H\textsubscript{2}, the single-site Vrabec model\textsuperscript{63} and the three-site Marx model\textsuperscript{65,66} are used. These force fields for H\textsubscript{2} and O\textsubscript{2} have shown to accurately describe gas diffusivities in pure water at various pressures and temperatures.\textsuperscript{31} The single-site H\textsubscript{2} Vrabec model is less computationally demanding (no bonds or angles) than the three-site Marx model and yields similar self-diffusivities in pure TIP4P/2005 water (see Figure S1). This force field is used for computing self-diffusivities of H\textsubscript{2} in NaOH and KOH solutions. The Marx model yields significantly more accurate H\textsubscript{2} solubilities than the Vrabec model in pure TIP4P/2005 water (see Figure S1) and is used for computing H\textsubscript{2} solubilities in NaOH and KOH solutions. For the K\textsuperscript{+} and Na\textsuperscript{+} ions, the Madrid-Transport (+0.75)\textsuperscript{47} and Madrid-2019 (+0.85)\textsuperscript{38} force fields are used (parameters listed in Table 1). For OH\textsuperscript{−}, several force fields are proposed in this work. The details for OH\textsuperscript{−} force field are discussed in section 3.1. All force fields considered in this work are rigid. All interaction parameters for the TIP4P/2005 water, H\textsubscript{2}O and O\textsubscript{2} models are provided in the Supporting Information (Tables S1–S3). The Lennard-Jones (LJ) and Coulombic interactions are considered for modeling the intermolecular interactions. The Lorentz–Berthelot mixing rules\textsuperscript{5,6} are applied for all mixtures, with the exception of [Na/K – H\textsubscript{2}O] LJ interactions as specified in this table.

| Force Field | Na+ | K+ |
|-------------|-----|-----|
| Madrid-2019 | 0.85 | 0.75 |
| Madrid-Transport | 1.77 | 2.38 |
| | 2.1737 | 2.3014 |
| | 95.42 | 168.43 |
| | 2.60838 | 2.89040 |

Table 1. Force Field Parameters for the Na\textsuperscript{+} and K\textsuperscript{+} Models Used (Madrid-2019\textsuperscript{38} and Madrid-Transport\textsuperscript{47})

2.2. MD Simulations. MD simulations are carried out as implemented in the open-source Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS).\textsuperscript{67} The Verlet algorithm,\textsuperscript{68} with a time step of 1 fs, is used for integrating the
equations of motion. Periodic boundary conditions are imposed in all directions. For H$_2$O, O$_2$, and OH$^-$, the SHAKE algorithm in LAMMPS$^{67,69}$ is used to fix the bond lengths (and the bond angle of H$_2$O). Analytic tail corrections for energies and pressures are applied to the LJ part of the potential. The cutoff radius for both LJ and Coulombic potentials is set to 10 Å. The particle–particle–particle-mesh (PPPM)$^{66,70}$ method is used for long-range electrostatic interactions with a relative error of 10$^{-5}$.

The OCTP tool$^1$ is used in LAMMPS to calculate the transport properties. The simulations are initially equilibrated in the NPT and NVT ensembles for a period of ca. 2 ns. Production runs (in NVT) of 10–50 ns are used to calculate dynamic viscosities and self-diffusivities. To obtain an ensemble mean and a standard deviation, each calculation is repeated 5 times with a different random seed for the initial velocity. The Nose–Hoover thermostat and barostat$^{66,72,73}$ are used, with a coupling constant of 100 and 1000 fs, respectively. The modifications of the Nose–Hoover for rigid bodies, proposed by Kamberaj,$^{74}$ are used in LAMMPS. The densities and transport properties are calculated in a simulation box containing 700 H$_2$O molecules. The corresponding numbers of NaOH and KOH molecules, in combination with the respective molarities are provided in Tables S4 and S5. All NaOH and KOH molecules, in combination with the respective molarities are provided in Tables S4 and S5. All MC simulations are performed using the open-source Brick-CFCMC software.$^6$ Temperatures of 298, 323, 333, 343, and 353 K, at H$_2$ and O$_2$ pressures of 1, 50, and 100 bar.

To calculate the excess chemical potentials and solubilities of H$_2$ and O$_2$, “fractional” molecules are introduced. In contrast to “whole” or normal molecules, the interactions of “fractional” molecules with other molecules are scaled with a continuous order parameter $\lambda$ (in the range of $[0, 1]$).$^{57,86}$ $\lambda = 0$ indicates no interactions between the fractional and whole molecules (ideal gas), while $\lambda = 1$ indicates full interactions, corresponding to a “whole” or normal/unscaled molecule. For more details regarding the scaling of the interactions of fractional molecules the reader is referred to refs 87–89. A single fractional molecule of H$_2$ (and O$_2$) is used to calculate the excess chemical potentials of the respective molecules in the solution. All other molecules in the simulation are whole molecules. The Wang–Landau algorithm$^{90,91}$ is used to construct a biasing weight function for $\lambda$ ($W(\lambda)$). The biasing weight function helps in overcoming possible energy barriers in $\lambda$-space, to ensure a flat observed probability distribution.$^{83}$ 100 bins are used to obtain a histogram of $\lambda$ values, thereby computing the probability of occurrence for each $\lambda$ value. The Boltzmann average of any parameter ($A$) can be computed using

$$\langle A \rangle_{\text{Boltzmann}} = \frac{\langle A \exp[-W(\lambda)] \rangle}{\langle \exp[-W(\lambda)] \rangle}$$  \hspace{1cm} (2)

The infinite dilution excess chemical potential ($\mu^{\infty,0}$) can be related to the Boltzmann sampled probability distribution of $\lambda$ ($p(\lambda)$) using$^{57,83}$

$$\mu^{\infty,0} = -k_B T \ln \frac{p(\lambda = 1)}{p(\lambda = 0)}$$  \hspace{1cm} (3)

where $p(\lambda = 1)$ and $p(\lambda = 0)$ are the Boltzmann sampled probability distribution of $\lambda$ at 1 and 0, respectively. The molarity based Henry coefficient ($H$) is defined as$^{83}$

$$H = \lim_{\lambda \to 0} \frac{f_i}{m_i/m_0}$$  \hspace{1cm} (4)\n
in which $f_i$ is the fugacity of a solute in the gas phase, $m_i$ is the molarity of the gas in the solution (mol/L), and $m_0$ is set to 1 mol/L. The infinite dilution excess chemical potential of H$_2$ and O$_2$ can be related to the molarity based Henry coefficient using$^{83}$

$$H = m_0 RT \exp \left[ \frac{\mu^{\infty,0}}{k_B T} \right]$$  \hspace{1cm} (5)

where $R$ is the universal gas constant. For all simulations, 4 × 10$^6$ equilibrium cycles are carried out followed by 4 × 10$^6$ production cycles. A cycle refers to N number of trial moves, with N corresponding to the total number of molecules, with a minimum of 20. Trial moves are selected with the following probabilities: 1% volume changes, 35% translations, 29% rotations, 25% $\lambda$ changes, and 10% reinsertions of the fractional molecules at random locations inside the simulation box. The maximum displacements for volume changes, molecule translations, rotations, and $\lambda$ changes are adjusted to obtain ca. 50% acceptance of trial moves. For each condition (concentration, temperature, pressure), 20 independent simulations are performed. The final Boltzmann probability distributions of $\lambda$ are averaged in blocks of 4 to obtain 5 independent averaged distributions. For all averaged distribu-
tions, the excess chemical potentials and Henry coefficients are calculated to obtain a mean value and the standard deviation. All the raw data for the MD and MC simulations are shown in Tables S6–S11.

3. RESULTS AND DISCUSSION

3.1. Force Field Optimization. To construct accurate models for aqueous NaOH and KOH solutions, four different two-site OH\(^{−}\) (i.e., OH\(^{−}\) and H\(^{+}\)) force fields are considered (FF1–FF4) combined with the TIP4P/2005 water\(^{42}\) and the Madrid-2019\(^{38}\) or Madrid-Transport\(^{39}\) force fields for Na\(^{+}\) and K\(^{+}\). These force fields and their corresponding parameters are listed in Table 2. For all OH\(^{−}\) models, the O–H bond length is set to 0.98 Å, similar to the works of refs 52 and 53. FF1, FF3, and FF4 have a total scaled charge \(q_{\text{OO}}\) of −0.75 on OH\(^{−}\), while FF2 has a total scaled charge of −0.85. These force fields are used in combination with the Madrid-Transport (+0.75)\(^{47}\) and Madrid-2019 (+0.85)\(^{38}\) Na\(^{+}\) and K\(^{+}\) models such that the total charge of NaOH and KOH clusters becomes 0. The charge of OH\(^{−}\) is distributed on the O \(q_{\text{O}}\) and H \(q_{\text{H}}\) atom. For FF1 and FF2, the charges on the O and H atoms have the same ratios as in the work by Botti et al. on the structure of concentrated NaOH solutions.\(^{52}\) The charge distributions of the FF3 and FF4 models are based on Quantum Theory of Atoms in Molecules (QTAIM) calculations for OH\(^{−}\), which have indicated that the O atom can have an unscaled charge of −1.4 to −1.3.\(^{92}\) For this reason, for the FF3 and FF4 models, the charge on the O atom is set to −1.4 × 0.75 and −1.3 × 0.75, respectively. The charge on the H atom \(q_{\text{H}}\) is set such that \(q_{\text{O}} + q_{\text{H}} = q_{\text{OO}}\). For each force field, the Lennard-Jones \(\sigma\) parameter of the O atom \(\sigma_{\text{OO}}\) is adjusted based on the experimental densities of aqueous NaOH and KOH solutions.\(^{10,93,94}\)

Figure 1 shows the variation of densities as functions of electrolyte concentrations for both NaOH and KOH. By adjusting the value of \(\sigma_{\text{OO}}\), it is possible to obtain an excellent agreement for all the different models. All the densities obtained deviate less than 2% from experimental fits found in literature. A larger negative charge on O \(q_{\text{O}}\) results in a larger optimum \(\sigma_{\text{OO}}\) parameter, to counteract the strong attractive Coulombic interactions. The experimental fits of Olsson\(^{24}\) (for densities and viscosities of aqueous NaOH), Gilliam\(^{93}\) (densities of aqueous KOH), and Guo\(^{95}\) (viscosities of aqueous KOH) are used and shown as lines in Figure 1.

The dynamic viscosities of aqueous NaOH and KOH solutions calculated using FF1–FF4 are shown in Figure 2. It can be observed that the choice of the total charge \(q_{\text{OO}}\) and the resulting \(\sigma_{\text{OO}}\) has a significant influence on the viscosities, especially at higher concentrations in which the influence of ion–ion interactions become more important. The influence of ion size on the viscosities and densities is shown in Figure S2. In case of FF2 (with \(q_{\text{OO}} = −0.85\)), the dynamic viscosity is overestimated by more than a factor 3 compared to the experimental fit for the highest concentration of NaOH. For aqueous KOH, the FF2 model overestimates the dynamic viscosity by around 40% at the highest concentration of KOH. The FF1, FF3, and FF4 models with \(q_{\text{OO}} = −0.75\) show a much better agreement with the experimental fit. The findings of the Madrid-Transport model for aqueous NaCl and KCl solutions\(^{47}\) also show that a scaled charge of 0.75 leads to better predictions of transport properties (especially at concentrations above 4 mol/kg salt) compared to a scaled charge of 0.85. Overall, the FF1 model shows the best agreement with the experimental viscosities and densities. For this reason, only the results of the FF1 model will be used and discussed further in this work.

### Table 2. Force Field Parameters for OH\(^{−}\)

| Model | \(q_{\text{O}}/|e|\) | \(q_{\text{H}}/|e|\) | \(q_{\text{O}}\) | \(k_{\text{b}}/\text{k}\) | \(q_{\text{O}}\) | \(k_{\text{b}}/\text{k}\) |
|-------|-----------------|-----------------|--------|--------|--------|--------|
| FF1   | −1.2181         | +0.4681         | −0.75  | 3.65   | 30.19  | 1.443  | 22.13  |
| FF2   | −1.3805         | +0.5305         | −0.85  | 3.85   | 30.19  | 1.443  | 22.13  |
| FF3   | −1.0500         | +0.3000         | −0.75  | 3.55   | 30.19  | 1.443  | 22.13  |
| FF4   | −0.9750         | +0.2250         | −0.75  | 3.45   | 30.19  | 1.443  | 22.13  |

The bond length of O–H is set to 0.98 Å. For all models, the \(\sigma\) parameter of the O atom \(\sigma_{\text{OO}}\) results in a larger optimum \(\sigma_{\text{OO}}\) parameter, to counteract the strong attractive Coulombic interactions. The experimental fits of Olsson\(^{24}\) (for densities and viscosities of aqueous NaOH), Gilliam\(^{93}\) (densities of aqueous KOH), and Guo\(^{95}\) (viscosities of aqueous KOH) are used and shown as lines in Figure 1.

![Figure 1](https://doi.org/10.1021/acs.jpcb.2c06381)

**Figure 1.** Densities at 298 K and 1 bar as functions of the electrolyte concentrations for (a) NaOH and (b) KOH. Four different OH\(^{−}\) force fields are considered (FF1–FF4) and compared to experimental fits (shown as lines) of Olsson\(^{94}\) (for NaOH) and Gilliam\(^{10,93}\) (for KOH). The different parameters used for all the force fields are listed in Table 2.
The radial distribution functions (RDFs) for anion−\(O_W\) and cation−\(O_W\) are shown in Figure 3. The RDFs for the anion−anion, anion−cation, and cation−cation are shown in Figure S3. Based on the RDFs, the hydration numbers (\(n_{\text{hyd}}\)) are calculated using

\[
 n_{\text{hyd}} = 4 \pi \rho_w \int_0^{r_{\text{min}}} g_w(r) r^2 \, dr \tag{6}
\]

where \(g_w\) is the anion/cation−\(O_W\) RDF, \(r\) is the radial distance, \(r_{\text{min}}\) is the position of the first minimum in the RDF, and \(\rho_w\) is the number density of water in the solution. Our results show a first peak at approximately 2.13 and 2.79 Å for \(Na^+−O_W\) and \(K^+−O_W\), respectively. The cation hydration numbers are 4.9 and 7.2 for \(Na^+\) and \(K^+\), respectively, at a molality of 5 mol/kg (corresponding to a molarity of 4.98 mol/L for \(NaOH\), and 4.68 mol/L for \(KOH\)). Crystallization of ions is not observed for all our MD simulations of 10−50 ns based on the RDFs.

Experimental and simulation results in literature suggest a first RDF peak at approximately 2.4−2.5 Å for \(Na^+−O_W\) and 2.7−2.8 Å for \(K^+−O_W\). The reported hydration numbers (in the first shell) are in the ranges of 4−8 and 6−8 for \(Na^+\) and \(K^+\), respectively. For \(OH^-\), the results show a first peak at approximately 2.75 Å for \(OH^-−O_W\), with hydration numbers of 4.8 and 5.9 for \(KOH\) and \(NaOH\), respectively, at a molality of 5 mol/kg. Other molecular simulations in literature report a first peak ranging from 2.3 to
The combined Car–Parrinello MD and X-ray diffraction studies of Megyes et al. for aqueous NaOH report a OH$^-$–O$_W$ distance ranging from 2.65 to 2.70 Å, with hydration numbers ranging from 3 to 5.

Overall, our force field results show agreement with other studies, albeit slightly overpredicting the first OH$^-$–O$_W$ peak and the hydration. The self-diffusivities of NaOH and KOH are listed in Table 3. Even though for Na$^+$ and K$^+$ the self-diffusivities at infinite dilution are close, this is not the case for OH$^-$ (underestimated by a factor ca. 5). For reasonable values of $\sigma$$_{OO}$, $\epsilon$$_{OO}$, and $q$$_O$, we could not obtain OH$^-$ self-diffusivities close to the values reported by experiments without causing significant deviations from experimental densities and viscosities. This result is expected as classical OH$^-$ models cannot capture the details of the solvation of OH$^-$ in water and the proton transfer mechanism, which lead to anomalously high OH$^-$ mobilities as discussed by Tuckerman et al.$^{43,45}$ As such, our model, similarly to other classical force fields, is not suitable for predicting OH$^-$ diffusivities of NaOH and KOH. Since electrical conductivities vastly depend on the mobility of the OH$^-$ ions in the solution, the new OH$^-$ model presented here is unable to accurately predict electrical conductivities of aqueous NaOH and KOH solutions. Although our classical force field cannot capture the proton transfer mechanism, it can correctly predict the dynamic viscosities of the electrolyte solutions. As the aim of this study is to study the transport properties and solubilities of H$_2$ and O$_2$ gas in aqueous NaOH and KOH electrolytes, correct predictions of densities and viscosities are sufficient. Developing an OH$^-$ force field by taking into account the proton transfer mechanism and accurate OH$^-$ mobilities is beyond the scope of this work as quantum mechanical based force fields will be required.

### 3.2. Densities and Viscosities

It is important to show that the NaOH and KOH models (FF1 OH$^-$ model, and the Madrid-Transport models of Na$^+$, and K$^+$)$^{47}$ can accurately predict the temperature-dependence of densities and viscosities. Figure 4 shows the densities and viscosities at different temperatures for both NaOH and KOH solutions. The agreement between MD simulations and experimental fits is excellent for aqueous KOH. For aqueous NaOH solutions, the results of densities are overestimated by ca. 2% and for dynamic viscosities by ca. 20% at the highest concentration (molality 8 mol/kg). Despite this, the trends of densities and
viscosities for variations of electrolyte concentration and temperature are well-predicted by the MD simulations using the new force fields. Densities and viscosities show a much weaker dependence on pressure (in the range of 1 to 100 bar) compared to temperature (in the range of 298 to 353 K) due to the incompressibility of the liquid phase. The variations of densities and viscosities as a function of pressure are shown in Figure S4.

3.3. Self-Diffusivities of \( \text{H}_2 \) and \( \text{O}_2 \) in Aqueous NaOH and KOH.

The finite size-corrected self-diffusivities (using eq 1) of \( \text{H}_2 \) and \( \text{O}_2 \) in aqueous NaOH and KOH solutions calculated using MD simulations at various temperatures are shown in Figure 5. The results obtained by our MD simulations for the KOH solution are compared to the experimental data of Tham et al.\textsuperscript{27,99} at different temperatures, i.e., 298, 333, and 353 K. For \( \text{H}_2 \) self-diffusivities, our results are in quantitative agreement with the results of Tham et al.\textsuperscript{27,99} The increase in \( \text{H}_2 \) and \( \text{O}_2 \) diffusivities at higher temperatures are well-predicted. These trends are linked to the decrease of the dynamic viscosities of the solutions, which the MD simulations capture correctly. In our simulations for \( \text{O}_2 \).

![Figure 5](https://doi.org/10.1021/acs.jpcb.2c06381)

**Figure 5.** \( \text{H}_2 \) (a, c) and \( \text{O}_2 \) (b, d) self-diffusivities as functions of KOH (a, b) and NaOH (c, d) concentrations at different temperatures (298, 333, and 353 K) at 1 bar. For diffusivities of \( \text{H}_2 \) and \( \text{O}_2 \) in the KOH solution, the experimental data of Tham et al.\textsuperscript{27,99} at 298 (red), 333 (blue), and 353 K (purple) are fitted using eq 4 and shown in (a) and (b) as lines. The fitting coefficients of these data are shown in Table 4. The experimental diffusivities of \( \text{O}_2 \) in NaOH solution at 296 K (black) provided by Zhang et al.\textsuperscript{14} are plotted as points. The FF1 OH\textsuperscript{−} model, in combination with the TIP4P/2005 water model,\textsuperscript{42} the Bohn O\textsubscript{2} model,\textsuperscript{62} the Vrabec H\textsubscript{2} model,\textsuperscript{63} and the Madrid-Transport Na\textsuperscript{+} and K\textsuperscript{+} models,\textsuperscript{47} is used for the MD simulations.

**Table 4. Fitting Parameters for eq 7 for \( \text{H}_2 \) and \( \text{O}_2 \) Self-Diffusivities in Aqueous NaOH and KOH Solutions**\textsuperscript{a}

|           | \( a_0 \) (in units of \( 10^{-11} \text{ m}^2/\text{s} \)) | \( a_1 \) (in units of \( 10^{-12} \text{ m}^2/\text{s} \) (L/mol)) | \( a_2 \) (in units of \( 10^{-13} \text{ m}^2/\text{s} \) (L/mol)^2) | \( a_3 \) (in units of \( 10^{-14} \text{ m}^2/\text{s} \) (L/mol)^3) | \( a_4 \) (in units of \( 10^{-2} \text{ K}^{-1} \)) |
|-----------|-------------------------------------------------|-------------------------------------------------|-------------------------------------------------|-------------------------------------------------|-------------------------------------------------|
| \( \text{H}_2 \)−KOH (exp) | 0.4066 | −0.5903 | 0.4748 | −0.1421 | 2.288 |
| \( \text{O}_2 \)−KOH (exp) | 0.2625 | −0.5124 | 0.4345 | −0.1278 | 2.201 |
| \( \text{H}_2 \)−KOH (MD) | 3.844 | −5.006 | 3.686 | −1.511 | 1.606 |
| \( \text{O}_2 \)−KOH (MD) | 1.511 | −2.092 | 2.483 | −1.743 | 1.701 |
| \( \text{H}_2 \)−NaOH (MD) | 3.344 | −5.725 | 4.649 | −2.103 | 1.648 |
| \( \text{O}_2 \)−NaOH (MD) | 1.313 | −2.105 | 1.604 | −0.7482 | 1.743 |

\textsuperscript{a}The values for \( a_0 \), \( a_1 \), \( a_2 \), \( a_3 \), and \( a_4 \) are shown for both the MD simulations obtained in this work (range of validity: 0-8 mol/L, 298-353 K), and the experimental work of Tham et al. (at 298, 333, and 353 K) for \( \text{H}_2 \) and \( \text{O}_2 \) diffusion coefficient in KOH solutions (range of validity: 0-14 mol/L). The FF1 OH\textsuperscript{−} model, in combination with the TIP4P/2005 water model, the Bohn O\textsubscript{2} model, the Vrabec H\textsubscript{2} model, and the Madrid-Transport Na\textsuperscript{+} and K\textsuperscript{+} models is used for the MD simulations.
the decay in the self-diffusivities with respect to variations of KOH concentrations are underpredicted with respect to the experimental data. Zhang et al.\textsuperscript{14} report experimental O\textsubscript{2} diffusivities in aqueous NaOH at 296 K. Although the results of Zhang et al.\textsuperscript{14} for O\textsubscript{2} diffusivity at 1 mol/L NaOH is in agreement to ours, at 2 mol/L their results show a sharp decrease of the O\textsubscript{2} diffusivities by approximately a factor 1/3 with respect to diffusivities at 1 mol/L NaOH.\textsuperscript{14} This sharp decline is not observed in our calculations. However, the current force field models have managed to qualitatively predict the trends for a wide concentration (0–8 mol/kg) and temperature (298–353 K) range. For H\textsubscript{2} self-diffusivities in aqueous NaOH no experimental data at these different temperatures are found. Thus, our simulations serve as a first prediction for these data.

The simulations results (at 298, 323, 333, 343, and 353 K) in this work (shown in Figure S5), and the experimental data of Tham et al. (at 298, 333, and 353 K)\textsuperscript{27,99} are fitted to an engineering equation with an Arrhenius-inspired term for temperature variations:

\[ D_i = (a_0 + a_1 C + a_2 C^2 + a_3 C^3) \exp(a_4 T) \]  

**Figure 6.** H\textsubscript{2} (a, c) and O\textsubscript{2} (b, d) solubilities as functions of KOH (a, b) and NaOH (c, d) concentrations at different temperatures of 298, and 333 K at 1 bar. For solubilities of H\textsubscript{2} and O\textsubscript{2} in KOH solutions, the experimental data of Walker et al.\textsuperscript{99} at 298 (red), and 333 K (blue) is fitted using eq 8 and shown in (a) and (b) as lines. The fitting coefficients are shown in Table 5. For H\textsubscript{2} and O\textsubscript{2} solubilities in NaOH solutions, the Sechenov model\textsuperscript{100,101} (using the parameters provided by Weisenberger et al.\textsuperscript{101}), and the experimental solubilities in pure water\textsuperscript{99} are used to obtain the experimental fits, which are shown as lines. The FF1 OH\textsuperscript{−} model, in combination with the TIP4P/2005 water model,\textsuperscript{42} the Bohn O\textsubscript{2} model,\textsuperscript{62} the Marx H\textsubscript{2} model,\textsuperscript{64} and the Madrid-Transport Na\textsuperscript{+} and K\textsuperscript{+} models,\textsuperscript{47} is used for the MC simulations.

**Table 5. Fitting Parameters for eq 8 for the H\textsubscript{2} and O\textsubscript{2} Solubilities (mol/L) in NaOH and KOH Solution**\textsuperscript{a}

|          | f_0   | f_1   | f_2   | f_3   | f_4   |
|----------|-------|-------|-------|-------|-------|
| H\textsubscript{2}–KOH (expt) | −1.944 | −3.167 | 9.517 | −5.337 | 8.078 |
| O\textsubscript{2}–KOH (expt) | −5.712 | 5.854 | 16.961 | −8.993 | 12.494 |
| H\textsubscript{2}–KOH (MC) | −5.468 | 10.077 | 4.874 | −2.526 | 3.773 |
| O\textsubscript{2}–KOH (MC) | −5.670 | 8.889 | 13.935 | −7.331 | 10.218 |
| H\textsubscript{2}–NaOH (MC) | −4.749 | 7.241 | 4.874 | −2.526 | 3.773 |
| O\textsubscript{2}–NaOH (MC) | −4.093 | 4.057 | 13.935 | −7.331 | 10.218 |

\textsuperscript{a}The values for f_0 (10\textsuperscript{−1} (L/mol)), f_1 (10\textsuperscript{−4} (L/mol K\textsuperscript{−1})), f_2 (10\textsuperscript{−3} (mol/L)), f_3 (10\textsuperscript{−5} (mol/L K\textsuperscript{−1})), and f_4 (10\textsuperscript{−8} (mol/L K\textsuperscript{−1})) are shown for both the MC simulations obtained in this work (range of validity: 0–8 mol/L, 298–353 K), and the experimental work of Walker et al. (at 298, 333, and 353 K) for H\textsubscript{2} and O\textsubscript{2} solubilities in KOH solutions (range of validity: 0–14 mol/L). The FF1 OH– model, in combination with the TIP4P/2005 water model, the Bohn O\textsubscript{2} model, the Marx H\textsubscript{2} model, and the Madrid-Transport Na\textsuperscript{+} and K\textsuperscript{+} models, is used for the MC simulations.
where $D$ is the self-diffusivity of $H_2$ and $O_2$ in NaOH and KOH solutions, $a_j$ are fitting constants, $C$ is the electrolyte concentration (in mol/L), and $T$ is the temperature (in K). All fitting parameters for $H_2$ and $O_2$ in the aqueous NaOH and KOH solutions are listed in Table 4. Equation 7 provides an excellent fit for both the simulation results found in this work and the experimental data of Tham et al. as shown in Figure S5.

3.4. Solubilities of $H_2$ and $O_2$ in Aqueous NaOH and KOH. In Figure 6, the $H_2$ and $O_2$ solubilities obtained using CFCMC calculations are shown as functions of NaOH and KOH concentrations. In this figure, only the results at 298 and 333 K are shown as solubilities (especially at higher electrolyte concentrations) vary only weakly in the temperature range of 298–353 K. The solubilities of $H_2$ and $O_2$ at 298, 323, 333, and 353 K are shown in Figure S7.

As a comparison the experimental data provided by Walker et al. on the solubilities of $H_2$ and $O_2$ in aqueous KOH are fitted and plotted in Figure 6a,b. This experimental data are also in agreement with the experiments of Davis et al. for $O_2$ solubilities (at 298 and 333 K) and with the Sechenov model. The Sechenov model is an empirical model, which predicts the salting out effect at different temperatures (273–363 K) and electrolyte concentrations. For NaOH, our data are compared to the Sechenov model as direct experimental data at these two temperatures are not available. Zhang et al. report solubilities of $O_2$ in aqueous NaOH at 296 K. Our simulations show agreement with data and experimental fits for both $H_2$ and $O_2$. Both the salting out phenomena and the temperature trends are captured by our simulations. At low electrolyte concentrations (below 2 mol/L), increasing the temperature from 298 to 333 K leads to slightly lower $H_2$ and $O_2$ solubilities. At higher molarities, the solubilities become less dependent on the temperature and the concentration of the salts dominate the solubilities. The simulations results and experimental data of Walker et al. for $H_2$ and $O_2$ solubilities in aqueous KOH and NaOH are fitted to a Sechenov-based engineering equation:

$$\ln\left(\frac{C_G}{C_{G,0}}\right) = (f_0 + f_1 T)C$$

(8)

where $C_G$ and $C_{G,0}$ are the solubility of the gas in the electrolyte and pure water at 1 bar, respectively. $f_0$ and $f_1$ are fitting constants. The temperature dependence of the parameter $C_{G,0}$ can be fitted as

$$C_{G,0} = f_2 + f_3 T + f_4 T^2$$

(9)

where $f_2, f_3, f_4$ are additional fitting parameters. The optimized fitting parameters for MC simulations in this work and the experimental data of Walker et al. for $H_2$ and $O_2$ solubilities are shown in Table 5. Equation 8 provides an excellent fit for both the simulation results found in this work and the experimental data present in the literature, as shown in Figure S7.

4. CONCLUSIONS

The self-diffusivities and solubilities of $H_2$ and $O_2$ in aqueous NaOH and KOH solutions are modeled using MD and CFCMC simulations. A new two-site nonpolarizable OH− force field (FF1 model) is proposed with a scaled charge of −0.75, which matches with the TIP4P/2005 water and the Madrid-Transport models for Na$^+$ and K$^+$. Although our classical force field cannot capture the proton transfer mechanism, which influences the OH$^-$ diffusivities, it can predict the densities, dynamic viscosities, and the salting out of $H_2$ and $O_2$ in aqueous NaOH and KOH solutions. Excellent agreement is observed between simulation and experimental data for both densities and dynamic viscosities of NaOH and KOH for a concentration range of 0–6 mol/kg and a temperature range of 298–353 K. This model is used to generate self-diffusivity and solubility data for $H_2$ and $O_2$ in aqueous NaOH and KOH solutions for a temperature range of 298–353 K and a concentration range of 0–8 mol/kg. The computed data and existing experimental results are used to fit engineering equations. The obtained data and engineering equations can be used for process modeling and optimizing electrolyzers and fuel cells.
The authors declare no competing financial interest.

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REFERENCES

(1) Panagiotopoulos, A. Z. Simulations of activities, solubilities, transport properties, and nucleation rates for aqueous electrolyte solutions. J. Chem. Phys. 2020, 153, 010903.
(2) Hellström, M.; Behler, J. Structure of aqueous NaOH solutions: insights from neural-network-based molecular dynamics simulations. Phys. Chem. Chem. Phys. 2017, 19, 82–96.
(3) Bodner, M.; Hofer, A.; Hacker, V. H. generation from alkaline electrolyzer. Wiley Interdisciplinary Reviews: Energy and Environment 2015, 4, 365–381.
(4) David, M.; Ocampo-Martinez, C.; Sánchez-Peña, R. Advances in alkaline water electrolyzers: A review. Journal of Energy Storage 2019, 23, 392–403.
(5) Solovyev, V.; Shevchenko, A.; Zipunnikov, M.; Kotenko, A.; Khim, N. T.; Tri, B. D.; Hai, T. T. Development of high pressure membraneless alkaline electrolyzer. Int. J. Hydrogen Energy 2022, 47, 6975–6985.
(6) Ulleberg, Ø. Modeling of advanced alkaline electrolyzers: a system simulation approach. Int. J. Hydrogen Energy 2003, 28, 21–33.
(7) Merle, G.; Wessling, M.; Nijmeijer, K. Anion exchange membranes for alkaline fuel cells: A review. J. Membr. Sci. 2011, 377, 1–35.
(8) Solubility table of compounds in water at temperature. https://www.sigmaaldrich.com/NL/en/support/calculators-and-apps/solubility-table-compounds-water-temperature (Accessed Sep. 6, 2022).
(9) Potassium hydroxide. https://webwiser.nlm.nih.gov/substance?substanceId=401& (Accessed Sep. 6, 2022).
(10) Le Bideau, D.; Mandin, P.; Benbouzid, M.; Kim, M.; Sellier, M. Review of necessary thermophysical properties and their sensitivities with temperature and electrolyte mass fractions for alkaline water electrolysis multiphysics modelling. Int. J. Hydrogen Energy 2019, 44, 4553–4569.
(11) Zarghami, A.; Deen, N.; Vreman, A. CFD modeling of multiphase flow in an alkaline water electrolyzer. Chem. Eng. Sci. 2020, 227, 115926.
(12) Haug, P.; Kreitz, B.; Koj, M.; Turek, T. Process modelling of an alkaline water electrolyzer. Int. J. Hydrogen Energy 2017, 42, 15689–15707.
(13) Haug, P.; Koj, M.; Turek, T. Influence of process conditions on gas purity in alkaline water electrolysis. Int. J. Hydrogen Energy 2017, 42, 9406–9418.
(14) Zhang, C.; Fan, F.-R. F.; Bard, A. J. Electrochemistry of oxygen in concentrated NaOH solutions: solubility, diffusion coefficients, and superoxide formation. J. Am. Chem. Soc. 2009, 131, 177–181.
(15) Rowland, D.; Köngsberger, E.; Hefer, G.; May, P. M. Aqueous electrolyte solution modelling: Some limitations of the Pitzer equations. Appl. Geochem. 2015, 55, 170–183.
(16) Kontogeorgis, G. M.; Maribo-Mogensen, B.; Thomsen, K. The Debye-Hückel theory and its importance in modeling electrolyte solutions. Fluid Phase Equilib. 2018, 462, 130–152.
(17) Walker, P. J.; Liang, X.; Kontogeorgis, G. M. Importance of the Relative Static Permittivity in electrolyte SAFT-VR Mie Equations of State. Fluid Phase Equilib. 2022, 551, 113256.
(18) Costa Reis, M. Current Trends in Predictive Methods and Electrolyte Equations of State. ACS Omega 2022, 7, 16847.
(19) Maribo-Mogensen, B.; Thomsen, K.; Kontogeorgis, G. M. An electrolyte CPA equation of state for mixed solvent electrolytes. AIChE J. 2015, 61, 2933–2950.
(20) Nikolaïdis, I. K.; Novák, N.; Kontogeorgis, G. M.; Economou, I. G. Rigorous Phase Equilibrium Calculation Methods for Strong Electrolyte Solutions: The Isothermal Flash. Fluid Phase Equilib. 2022, 558, 113441.
(21) Kontogeorgis, G. M.; Schluijkjer, A.; Olsen, M. D.; Maribo-Mogensen, B.; Thomsen, K.; von Solms, N.; Liang, X. A Review of Electrolyte Equations of State with Emphasis on Those Based on Cubic and Cubic-Plus-Association (CPA) Models. Int. J. Thermophys. 2022, 43, 54.
(22) Novak, N.; Kontogeorgis, G. M.; Castier, M.; Economou, I. G. Modeling of Gas Solubility in Aqueous Electrolyte Solutions with the eSAFT-VR Mie Equation of State. Ind. Eng. Chem. Res. 2021, 60, 15327–15342.
(23) Jiang, H.; Mester, Z.; Moultos, O. A.; Economou, I. G.; Panagiotopoulos, A. Z. Thermodynamic and Transport Properties of H2O + NaCl from Polarizable Force Fields. J. Chem. Theory Comput. 2015, 11, 3802–3810.
(24) Orozco, G. A.; Moultos, O. A.; Jiang, H.; Economou, I. G.; Panagiotopoulos, A. Z. Molecular simulation of thermodynamic and transport properties for the H2O+NaCl system. J. Chem. Phys. 2014, 141, 234507.
(25) Sarabi, S. H.; Panagiotopoulos, A. Z. Activity Coefficients and Solubilities of NaCl in Water—Methanol Solutions from Molecular Dynamics Simulations. J. Phys. Chem. B 2022, 126, 2891–2898.
(26) Zhang, C.; Yue, S.; Panagiotopoulos, A. Z.; Klein, M. L.; Wu, X. Dissolving salt is not equivalent to applying a pressure on water. Nat. Commun. 2022, 13, 822.
(27) Tham, M. J.; Walker, R. D., Jr.; Gubbins, K. E. Diffusion of oxygen and hydrogen in aqueous potassium hydroxide solutions. J. Phys. Chem. 1970, 74, 1747–1751.
(28) Tjarks, G.; Merget, J.; Stolten. *Hydrogen Science and Engineering: Materials, Processes, Systems and Technology*; John Wiley & Sons, Ltd., 2016; Chapter 14, pp 309–330.

(29) Manabe, A.; Kashiwase, M.; Hashimoto, T.; Hayashida, T.; Kato, A.; Hirao, K.; Shimomura, I.; Nagashima, I. Basic study of alkaline water electrolysis. *Electrochem. Acta* 2013, 100, 249–256.

(30) Bidault, F.; Brett, D.; Middleton, P.; Brandon, N. Review of gas diffusion cathodes for alkaline fuel cells. *J. Power Sources* 2009, 187, 39–48.

(31) Tsimpanogiannis, I. N.; Maity, S.; Celebi, A. T.; Moultos, O. A. Engineering Model for Predicting the Intradiffusion Coefficients of Hydrogen and Oxygen in Vapor, Liquid, and Supercritical Water based on Molecular Dynamics Simulations. *Journal of Chemical & Engineering Data* 2021, 66, 3226–3244.

(32) Chen, B.; Ivanov, I.; Park, J. M.; Parrinello, M.; Klein, M. L. Solvation Structure and Mobility Mechanism of OH⁻: A Car-Parrinello Molecular Dynamics Investigation of Alkaline Solutions. *J. Phys. Chem. B* 2002, 106, 12006–12016.

(33) Megyes, T.; Bálint, S.; Grósz, T.; Radnai, T.; Bakó, I.; Sipos, P. The structure of aqueous sodium hydroxide solutions: A combined solution x-ray diffraction and simulation study. *J. Chem. Phys.* 2008, 128, 044501.

(34) Tuckerman, M. E.; Chandra, A.; Marx, D. Structure and dynamics of OH⁻(aq). *Acc. Chem. Res.* 2006, 39, 151–158.

(35) Guevara-Carrion, G.; Nieto-Draghi, C.; Vrabec, J.; Hesse, H. Prediction of Transport Properties by Molecular Simulation: Methanol and Ethanol and Their Mixture. *J. Phys. Chem. B* 2008, 112, 16664–16674.

(36) Ghaffari, A.; Rahbar-Kelishami, A. MD simulation and evaluation of the self-diffusion coefficients in aqueous NaCl solutions at different temperatures and concentrations. *J. Mol. Liq.* 2013, 187, 238–245.

(37) Saravi, S. H.; Panagiotopoulos, A. Z. Individual Ion Activity Coefficients in Aqueous Electrolytes from Explicit-Water Molecular Dynamics Simulations. *J. Phys. Chem. B* 2021, 125, 8511–8521.

(38) Zeron, I.; Abascal, J.; Vega, C. A force field of Li⁺, Na⁺, K⁺, Mg²⁺, Ca²⁺, Cl⁻, and SO₄²⁻ in aqueous solution based on the TIP4P/2005 water model and scaled charges for the ions. *J. Chem. Phys.* 2008, 151, 134504.

(39) Jiang, H.; Moultos, O. A.; Economou, I. G.; Panagiotopoulos, A. Z. Hydrogen-Bonding Polarizable Intermolecular Potential Model for Water. *J. Phys. Chem. B* 2016, 120, 12358–12370.

(40) Jiang, H.; Moultos, O. A.; Economou, I. G.; Panagiotopoulos, A. Z. Gaussian-Charge Polarizable and Nonpolarizable Models for Water. *J. Chem. Phys.* 2016, 144, 114501.

(41) Abascal, J. L.; Vega, C. A general purpose model for the condensed phases of water: TIP4P/2005. *J. Chem. Phys.* 2005, 123, 234505.

(42) Abascal, J. L.; Vega, C. Widom line and the liquid–liquid critical point for the TIP4P/2005 water model. *J. Chem. Phys.* 2010, 133, 234502.

(43) Tsimpanogiannis, I. N.; Moultos, O. A.; Franco, L. F. M.; Spera, M. B. M.; Erdős, M.; Economou, I. G. Self-diffusion coefficient of bulk and confined water: a critical review of classical molecular simulation studies. *Mol. Simul.* 2019, 45, 425–453.

(44) Blazquez, S.; Conde, M. M.; Abascal, J. L. F.; Vega, C. The Madrid-2019 force field for electrolytes in water using TIP4P/2005 and scaled charges: Extension to the ions F⁻, Br⁻, I⁻, Rb⁺, and Cs⁺. *J. Chem. Phys.* 2022, 156, 044505.

(45) Kann, Z.; Skinner, J. A scaled-ionic-charge simulation model that reproduces enhanced and suppressed water diffusion in aqueous salt solutions. *J. Chem. Phys.* 2014, 141, 104507.

(46) Blazquez, S.; Conde, M. M.; Vega, C.2023, in preparation.

(47) Bonthuis, D. J.; Mamakulov, S. I.; Netz, R. R. Optimization of classical nonpolarizable force fields for OH⁻ and H₂O⁺. *J. Chem. Phys.* 2016, 144, 104503.
concentrations and temperatures. J. Chem. Phys. 2007, 127, 339–346.

(87) Poursaiedesfahani, A.; Hens, R.; Rahbari, A.; Ramdin, M.; Dubbeldam, D.; Vlugt, T. J. H. Efficient application of Continuous Fractional Component Monte Carlo in the reaction ensemble. J. Chem. Theory Comput. 2017, 13, 4452–4466.

(88) Rahbari, A.; Hens, R.; Dubbeldam, D.; Vlugt, T. J. H. Improving the accuracy of computing chemical potentials in CFCMC simulations. Mol. Phys. 2019, 117, 3493–3508.

(89) Rahbari, A.; Hens, R.; Jamali, S.; Ramdin, M.; Dubbeldam, D.; Vlugt, T. J. H. Effect of truncating electrostatic interactions on predicting thermodynamic properties of water–methanol systems. Mol. Simul. 2019, 45, 336–350.

(90) Wang, F.; Landau, D. P. Efficient multiple-range random walk algorithm to calculate the density of states. Phys. Rev. Lett. 2001, 86, 2050.

(91) Poulain, P.; Calvo, F.; Antoine, R.; Broyer, M.; Dugourd, P. Performances of Wang-Landau algorithm for continuous systems. Phys. Rev. E 2006, 73, 056704.

(92) Heidar-Zadeh, F.; Ayers, P. W.; Verstraeten, T.; Vinogradov, I.; Vöhlinger-Martinez, E.; Bultinck, P. Information-Theoretic Approaches to Atoms-in-Molecules: Hirshfeld Family of Partitioning Schemes. J. Phys. Chem. A 2018, 122, 4219–4245.

(93) Gilliam, R.; Graydon, J.; Kirk, D.; Thorpe, S. A review of specific conductivities of potassium hydroxide solutions for various concentrations and temperatures. Int. J. Hydrogen Energy 2007, 32, 359–364.

(94) Olsson, J.; Jernqvist, Å.; Åly, G. Thermophysical properties of aqueous NaOH-H₂O solutions at high concentrations. Int. J. Thermophys. 1997, 18, 779–793.

(95) Guo, Y.; Xu, H.; Guo, F.; Zheng, S.; Zhang, Y. Density and viscosity of aqueous solution of K₂CrO₄/KOH mixed electrolytes. Transactions of Nonferrous Metals Society of China 2010, 20, s32–s36.

(96) Marcus, Y. Ionic radii in aqueous solutions. Chem. Rev. 1988, 88, 1475–1498.

(97) Yuan-Hui, L.; Gregory, S. Diffusion of ions in sea water and in deep-sea sediments. Geochim. Cosmochim. Acta 1974, 38, 703–714.

(98) Tuckerman, M.; Laasonen, K.; Sprik, M.; Parrinello, M. Ab Initio Molecular Dynamics Simulation of the Solvation and Transport of H₂O⁺ and OH⁻ Ions in Water. J. Phys. Chem. 1995, 99, 5749–5752.

(99) Walker, R. D., Jr. Study of Gas Solubilities and Transport Properties in Fuel Cell Electrolytes; Technical Report; Florida University, Gainesville, FL, 1971.

(100) Setschenow, J. Über die konstitution der salzlö serungen auf grund ihres verhaltens zu kohlensaure. Z. Phys. Chem. 1889, 4, 117–125.

(101) Weisenberger, S.; Schumpe, A. Estimation of gas solubilities in salt solutions at temperatures from 273 to 363 K. AIChE J. 1996, 42, 298–300.

(102) Davis, R.; Horvath, G.; Tobias, C. The solubility and diffusion coefficient of oxygen in potassium hydroxide solutions. Electrochim. Acta 1967, 12, 287–297.

(103) Shoos, S.; Walker, R. D., Jr; Gubbins, K. Salting out of nonpolar gases in aqueous potassium hydroxide solutions. J. Phys. Chem. 1969, 73, 312–317.

(104) Ruesch, P.; Amile, R. Solubility of hydrogen in potassium hydroxide and sulfuric acid. Salting-out and hydration. J. Phys. Chem. 1966, 70, 718–723.