The Role of Epsilon Near Zero and Hot Electrons in Enhanced Dynamic THz Emission from Nonlinear Metasurfaces

Eviatar Minerbi,* Symeon Sideris, Jacob B. Khurgin, and Tal Ellenbogen

ABSTRACT: We study theoretically and experimentally the nonlinear THz emission from plasmonic metasurfaces and show that a thin indium-tin oxide (ITO) film significantly affects the nonlinear dynamics of the system. Specifically, the presence of the ITO film leads to 2 orders of magnitude stronger THz emission compared to a metasurface on glass. It also shows a different power law, signifying different dominant emission mechanisms. In addition, we find that the hot-electron dynamics in the system strongly modify the coupling between the plasmonic metasurface and the free electrons in the ITO at the picosecond time scale. This results in striking dynamic THz emission phenomena that were not observed to date. Specifically, we show that the generated THz pulse can be shortened in time and thus broadened in frequency with twice the bandwidth compared to previous studies and to an uncoupled system. Our findings open the door to design efficient and dynamic metasurface THz emitters.

KEYWORDS: epsilon near zero (ENZ), terahertz (THz), ITO, hot electrons, dynamic metasurface

Recently, surprisingly efficient THz emission following femtosecond laser excitation of nonlinear plasmonic metasurfaces has been reported. The magnitude of the field emitted from an ultrathin gold metasurface was shown to be comparable to that emitted from an orders of magnitude thicker zinc telluride (ZnTe) nonlinear crystal. Taking advantage of this effect, metasurfaces allowing phase control for generation of spatiotemporally tailored THz wavepackets have been demonstrated. However, the underlying physical mechanisms that enable such efficient THz emission are still not fully understood. Several processes, such as ponderomotive acceleration of photoejected electrons, either by multiphoton ionization or tunneling ionization, as well as optical rectification (OR) were proposed as the dominant mechanisms in the THz emission. Yet, a deeper understanding is still required to fully account for all the observations.

In many works that study THz emission from plasmonic metasurfaces, the metasurfaces are fabricated on thin ITO films, which are commonly used in the electron beam lithography process. Until recently, this layer was generally disregarded, and the nonlinear emission was considered to arise solely from the plasmonic nanostructures. However, the permittivity of ITO changes its sign from positive to negative in the near-infrared (NIR) region. It is also tunable and can be shifted up to the mid-infrared range by annealing in various atmospheric oxygen environments. This zero-crossing point coincides with the excitation wavelengths of some of the studied nonlinear metasurfaces and their resonant response. It was shown that at the epsilon near zero (ENZ) region, ITO as well as other materials possess strong optical nonlinearities and exhibit unusual properties, thus make promising candidates for new applications in both linear and nonlinear optics. A plethora of enhanced nonlinear effects were demonstrated in ITO films, such as second-harmonic generation (SHG), high harmonic generation, a nonlinear Kerr effect, and very recently also THz generation. However, since the amplification of the nonlinear effects is attributed to the enhancement of the normal component of the electric field at the ENZ region, they can only be observed when pumped at oblique incidence. To circumvent this constraint, hybrid metasurfaces constructed from plasmonic nanoantennas coupled to the ENZ material were designed and showed remarkably large second- and third-order nonlinearities.

Here, we study the role of ITO and hot-electron dynamics in the THz emission from nonlinear plasmonic metasurfaces. To get better insight, we compare the emission from gold split ring resonator array (SRRs) metasurfaces, fabricated on a thin layer...
(~20 nm) of ITO (referred to as SRR-ITO throughout this work) and on a bare SiO$_2$ substrate (referred to as SRR-Glass). Figure 1a illustrates the unit cell structure. More details on the fabrication process along with SEM images of the fabricated samples are given in the Supplementary Notes 1 and 2.

We start by characterizing the linear response of the samples. Figure 1(b,c) presents the polarized transmission spectra of the SRR-ITO and SRR-Glass samples, respectively. It can be seen that the SRR-Glass metasurface exhibits one resonance at $\lambda_{\text{res}} \approx$ 1500 nm when irradiated along the base of the SRRs ($E_{\text{in}} \hat{x}$) and no resonance when excited along the arms ($E_{\text{in}} \hat{y}$).

On the other hand, the SRR-ITO metasurface exhibits two resonances at 1240 and 1550 nm for $\hat{x}$-polarized illumination and a single-resonance dip around 1400 nm for $\hat{y}$-polarized illumination.

Figure 2. Nonlinear emission comparison between SRR-ITO and SRR-Glass metasurfaces. (a) Experimental setup. Ti:Sapp - Amplified titanium sapphire laser. OPA - Optical parametric amplifier. FM - Flip mirror. SP - Short pass. ZnTe - 0.5 mm (110-cut) crystal. WP - Wollaston prism. BPD - Balanced photodiode. (b) Time domain spectroscopy measurement of the THz signal emitted from SRR-ITO (magenta) and SRR-Glass (blue) under the same pumping conditions with an average power of 30 mW. (c) Emission spectrum from SRR-ITO and SRR-Glass metasurfaces. (d) Intensity of the THz signal generated from an SRR-ITO (magenta) and SRR-Glass metasurfaces (X5, blue) as a function of pump power. Dashed lines represent quadratic (black) and $x^4$ (red) fits. (e) Intensity of SH signal generated from an SRR-ITO metasurface (magenta) and from an SRR-Glass metasurface (blue). Dashed black lines represent a quadratic fit.

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The dependence of the generated THz intensity on the pumping power from the different samples reveals some unique properties, as shown in Figure 2d. First, it can be seen that the thin ITO film enhances the THz intensity up to 2 orders of magnitude (for a pumping power of 30 mW). In addition, the power law dependencies of the THz emission from metasurfaces on glass and ITO are different. This can be attributed to different dominant THz generation mechanisms in the two cases. The SRR-Glass sample shows a fourth power ($x^4$) dependency, which can be explained by ponderomotive acceleration of photoexcited electrons as was previously proposed. On the other hand, in the case of SRR-ITO, we observe a quadratic power dependence for up to ~40 mW pump power. This suggests a second-order nonlinear process, optical rectification, as has been previously suggested, and settles the disagreement between the previous reports (see also supplementary of ref 1).

At higher pumping power of the SRR-ITO sample, saturation is observed (Figure 2d). This saturation behavior is reversible and may point on dynamic effects involved in the generation process. To verify that these observations are unique to the THz emission, we also measured the second-harmonic generation from the samples. The results of the SHG measurements are shown in Figure 2e. In both samples, the intensity of the generated SH exhibits a quadratic dependence on the pump power, as expected. In addition, the SRR-ITO metasurface enhances the SH generation compared to SRR-Glass (up to ~4 fold), which agrees with previous reports. This comparison shows that the ITO plays a more dominant role in the THz enhancement and may be explained by the large intrinsic nonlinearities arising from hot carriers in the THz regime that far exceed the fast nonlinearities in ITO.

In order to explain the unique observations of the emission from the coupled SRR-ITO metasurface, we consider a nonlinear hydrodynamic model, which treats the electrons in the material as a fluid that obeys Euler’s equation. Using this model, we describe the second-order nonlinearity that arises in the metal nanoparticles as well as in the ITO layer (see Supplementary Note 4). The nonlinear currents generated by the OR act as the driving source of the THz emission.

Using this method, we are able to correctly predict the spectrum of the emitted field at low pumping powers, as presented in Figure 3a, as well as the quadratic power dependence (Figure 3b). We note that the spectrum predicted using this method does not depend on the pumping power and remains unchanged (thus referred to as “static model”). In addition, since this model only describes the OR process, it shows a quadratic power dependence and does not capture the saturation observed in Figure 2d.

Moreover, the simulations of the system confirm that the strong THz emission recorded is due to the existence of the thin ITO layer rather than solely by the gold nanoparticles as was considered in previous studies. This large enhancement originates from the OR process in the ITO-SRR metasurface. The free carriers in the ITO are subject to strong asymmetric driving fields in the system, which are enhanced by field confinement, due to the SRRs and due to excitation wavelengths where the permittivity is near zero (see Supplementary Notes 5 and 6). Furthermore, the SRRs couple to the ITO to enable emission at normal incidence illumination.

Next, we examine more carefully the THz emission from the SRR-ITO sample. We see that pumping at either $\hat{x}$ or $\hat{y}$ polarizations result in strong THz emission (see Supplementary Note 7). Figure 4 shows the generated signal when pumped with a fundamental wavelength of $\lambda_p = 1300$ nm (Figure 4a,c) and $\lambda_p = 1500$ nm (Figure 4b,d). The temporal and spectral shape of the pulse remains unchanged while pumping the weakly coupled resonance along $\hat{y}$ (see Supplementary Notes 8 and 9). However, pumping the strongly coupled resonance along $\hat{x}$ results in shortening of the THz pulse and a broadening of the emitted THz bandwidth (Figure 4c,d). We measured a broadening of up to twice the bandwidth compared to previous studies and to
the weakly coupled system \((E_y)\). In addition, pumping the strongly coupled system results not only in shorter pulses when increasing the pumping power, but the pulse shape changes as well. Also, pumping at different wavelengths generates a different THz signal. This behavior may be explained by a phase difference between THz signals generated by short and long wavelengths (further explanation is given in Supplementary Note 8).

To understand the saturation in the THz generated at high pumping powers and broadening of the spectrum, we take into account temporal dynamics that occur due to hot-electron generation in the ITO (see the schematic illustration in Figure 5a). The semiclassical two-temperature model (TTM) is used to calculate the spatiotemporal temperature distribution of the hot electrons in the gold nanoparticle and in the ITO layer together with their energy transfer to the lattice. In this model, the pumping NIR ultrashort laser excites the electrons, which then thermalize and also transfer the heat to the lattice. As a result of the fast electron and lattice heating, the effective mass changes due to the nonparabolicity of the conduction band. This leads to fast changes of the plasma frequency and the permittivity of the ITO. Therefore, the optical response is temporally changed at the sub-picosecond time scale. We account for this temporal thermo-optical change by altering the permittivity \(\epsilon(T_e, T_l)\), which is dependent on the electrons \((T_e)\) and lattice \((T_l)\) temperatures (see Supplementary Notes 10–13 for more details on the theoretical model). These thermo-optical modifications dynamically change the coupling between the SRR resonance and the ITO ENZ mode, and therefore are evident for \(x\)-polarized excitation. Finally, the observed spectrum is highly dependent on the optical properties of the metasurface, which determine the frequencies that will radiate to the far field. Therefore, since the ultrafast heating process occurs at the subpicosecond time scale, the generated THz pulse is affected, thus resulting in the significant

![Figure 4](image_url)

**Figure 4.** THz signal dynamics. (a) TDS measurements of the emitted THz signal when pumped at 40 mW with a wavelength of \(\lambda_p = 1300\) nm and (b) \(\lambda_p = 1500\) nm. The red line represents pumping along the base of the SRRs (\(x\)-polarization), and the black line represents pumping along the arms (\(y\)-polarization). The arrow marks the time of the THz cycle for \(x\)-polarized pumping. (c,d) Emission spectrum at different pumping powers for (c) \(\lambda_p = 1300\) nm and (d) \(\lambda_p = 1500\) nm for \(P = 10\) (blue), \(P = 30\) (green), \(P = 40\) mW (red). The dashed black line represents the static THz spectrum generated by the weakly coupled system (\(y\)-polarization).

![Figure 5](image_url)

**Figure 5.** Theoretical model. (a) Illustration of the dynamical model. The ultrafast electron dynamics consist of photoexcitation by the IR pump pulse, hot-electron redistribution, thermalization by electron–electron scattering, and heat transfer to the lattice via electron–phonon scattering. The electron and lattice temperatures affect the optical properties of the system. The dynamic system then relaxes back to its static state in the picosecond time scale. The dashed line represents the parabolic conduction band. (b) Intensity of THz signal as a function of pumping power simulated with the dynamic model (light blue). The dashed black line represents a quadratic fit. (c) Simulated emission spectra for pumping wavelengths of \(\lambda_p = 1300\) nm and (d) \(\lambda_p = 1500\) nm at pumping powers of 5 mW (blue), 35 mW (green), and 65 mW (red).
broadening of the emission spectrum. On the other hand, the generated SH is an almost instantaneous process and therefore remains unchanged by the delayed temporal dynamics. Using full wave simulations with a finite element method commercially available software, we are able to reproduce the saturation behavior shown in Figure 2d. We show in Figure 2b that the quadratic power dependence of the THz emission observed at low pumping powers saturates at increasing powers when the heating effects become dominant. Saturation occurs due to a combined effect of a shift in the ENZ point and increase of the heated electron effective mass with pumping power, which reduces the strength of the ITO response due to a reduction in mobility. In addition, our framework also captures the broadening of the spectrum at increasing powers. Simulations of the generated THz spectrum when pumping the strongly coupled system are presented in Figure 5c,d and are in good agreement with the measurements (Figure 4c,d, respectively). Results for pumping the weakly coupled system are shown in the Supporting Information and agree with the measured results as well.

In conclusion, we have shown that the strong THz emission from plasmonic metasurfaces is due to a thin film of ITO. This ~20 nm thin layer enhances the THz emission by up to 2 orders of magnitude. In addition, we have shown that the strongly coupled SRR-ITO metasurface exhibits previously unreported dynamic phenomena. Specifically, broadening of the generated THz spectrum by a factor of 2 compared to previous reports and to an uncoupled system. To account for this behavior, we developed a dynamic theoretical framework which combines the hydrodynamic model as the source of the nonlinear THz emission with electron and lattice temperature-dependent permittivity. We see that our model agrees well the experimental results. These concepts unveil the fine fundamental physical dynamics of THz emission from nonlinear plasmonic metasurfaces. In addition, our work can advance the field toward efficient, active, integrated, and ultracompact optical elements for generating and controlling THz radiation.

**ASSOCIATED CONTENT**

**Supporting Information**
The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.2c01400.

1. Sample fabrication method; 2. Linear response; 3. Measurement setup; 4. Hydodynamic model; 5. Field enhancement in ITO layer; 6. SRRs and ITO contribution to THz generation; 7. THz dependence on pump polarization; 8. THz dynamics—time domain; 9. THz dynamics—frequency domain; 10. ITO nonparabolicity parameters; 11. Temperature-dependent effective mass; 12. Two-temperature model; 13. Thermo-optic response (PDF)

**AUTHOR INFORMATION**

**Corresponding Author**

Eviatar Minerbi — Department of Physical Electronics, School of Electrical Engineering, Tel-Aviv University, Tel-Aviv 6997801, Israel; Center for Light-Matter Interaction, Tel-Aviv University, Tel-Aviv 6779801, Israel; Raymond and Beverly Sackler Faculty of Exact Sciences, School of Physics & Astronomy, Tel-Aviv University, Tel-Aviv 6779801, Israel; orcid.org/0000-0002-1874-4919; Email: minerbi@mail.tau.ac.il

**Authors**

Symeon Sideris — Department of Physical Electronics, School of Electrical Engineering, Tel-Aviv University, Tel Aviv 6997801, Israel; Center for Light-Matter Interaction, Tel-Aviv University, Tel-Aviv 6779801, Israel

Jacob B. Khurgin — Department of Electrical and Computer Engineering, Johns Hopkins University, Baltimore, Maryland 21218, United States; orcid.org/0000-0003-0725-8736

Tal Ellenbogen — Department of Physical Electronics, School of Electrical Engineering, Tel-Aviv University, Tel Aviv 6997801, Israel; Center for Light-Matter Interaction, Tel-Aviv University, Tel-Aviv 6779801, Israel

Complete contact information is available at: https://pubs.acs.org/10.1021/acs.nanolett.2c01400

**Notes**
The authors declare no competing financial interest.

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