H1 Diffractive Structure Function Measurements and QCD Fits
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Measurements of diffractive structure functions in $ep$ collisions and diffractive parton densities extracted from QCD fits are presented.

1. DIFFRACTION AT HERA

At the HERA $ep$ collider the diffractive quark structure of the proton is probed with a point-like photon (Fig. 1). The virtuality of the photon is denoted by $Q^2$ and sets the hard scale of the interaction. Diffraction is characterised by an elastically scattered proton which loses only a small fraction $x_P$ of its initial beam momentum. These events are selected experimentally by detecting the proton at small scattering angles (roman pot detectors) or by requiring a large empty area in the detector between the outgoing proton and the hadronic system $X$ produced in the interaction (rapidity gap). The squared 4-momentum $t$ transferred at the proton vertex can be measured by tagging the proton. For the rapidity gap method, which accesses a much larger event sample, the cross section has to be integrated over $|t| < 1$ GeV$^2$ and in $\approx 10\%$ of the events the proton is excited into a hadronic system of small mass $< 1.6$ GeV. The two methods give the same results when compared in the same kinematic range.

In a picture which depicts diffraction as a two step process, the proton exchanges a diffractive object (often called the pomeron) with momentum fraction $x_P$, and the quark struck by the photon carries a fraction $\beta$ of the momentum of the diffractive exchange. Additional kinematic variables are Bjorken-$x = \frac{x}{1-x}$ and the inelasticity $y = Q^2/(sx)$ where $s$ is the $ep$ centre-of-mass energy squared.

The cross section is proportional to the combination of two structure functions:

$$\sigma \propto F_2^D - YF_L^D \equiv \sigma_r^D, \quad (1)$$

where $Y = \frac{y^2}{1+(1-y)^2}$ is a kinematic factor resulting from the difference of the fluxes of transversely and longitudinally polarised photons from the electron. $F_2^D$ is proportional to the diffractive $\gamma^*p$ cross section, whereas $F_L^D$ is related only to the part induced by longitudinal photons. The factor $Y$ is sizable at large values of $y$ and in most of the phase space measured so far, $F_L^D$ is a small correction.

2. FACTORIZATION IN DIFFRACTION

The diffractive structure functions have been proven to factorise into diffractive parton densities $f_i^P$ of the proton convoluted with ordinary
photon-parton scattering cross sections $\hat{\sigma}^\gamma i$ [1]:

$$F_2^D = \sum_i f_i^D \otimes \hat{\sigma}^\gamma i,$$

(2)

where the sum runs over all partons. This factorisation formula holds for large enough scales at leading twist and applies also to $F_L^D$. The diffractive parton densities obey the standard QCD evolution equations and can be determined from fits to structure function data.

3. EXPERIMENTAL RESULTS

3.1. Dependence on $t$

The $t$ dependence of the cross section has the form $d\sigma/dt \propto e^{bt}$ with a slope parameter $b \approx 5$ to 7 GeV$^{-2}$ which at the present level of precision does not depend on $x_F$ as shown in Fig. 2 [2].

![Figure 2](image-url)

Figure 2. The slope parameter $b$ from fits to the diffractive $ep$ cross section $d\sigma/dt \propto e^{bt}$ for different values of $x_F$.

3.2. Dependence on $x_F$

The reduced diffractive cross section is shown in Fig. 3 as a function of $x_F$ in bins of $\beta$ and $Q^2$. The measurements are obtained using a rapidity gap selection and cover a large kinematic range $Q^2 = 1.5$ to 1600 GeV$^2$ [3,4]. The collected event sample statistics do not allow an extraction of diffractive parton densities at fixed values of $x_F$. Instead, the $x_F$ and $t$ dependence of the PDFs are parameterised in a so-called flux factor $f_F$:

$$f_i^D(\beta, Q^2, x_F, t) = f_F(x_F, t) f_i^D(\beta, Q^2)$$

(3)

with $f_F(x_F, t) = e^{bt}x_F^{1-2\alpha_F(t)}$, where $\alpha_F(t) = \alpha_F(0) + \alpha_F'(t)$ is the linear pomeron Regge trajectory. This flux factor approach is consistent with the data within the present uncertainties for $x_F < 0.01$. At larger $x_F$ values, a second term has to be introduced which can be interpreted as reggeon exchange:

$$\sigma^D = f_F \left( F_2^D + Y F_L^D \right) + f_R \left( F_2^R + Y F_L^R \right).$$

(4)

This is illustrated in Fig. 4 where the cross section is well described by $f_F$ alone for $x_F < 0.01$. A fit to the data gives an intercept $\alpha_F(0) = 1.17^{+0.07}_{-0.05}$.
which is larger than 1.08 as obtained for the soft pomeron in hadron-hadron collisions.

Figure 4. The $x_F$ dependence of the reduced diffractive cross section for low and high $\beta$ compared with the H1 2002 NLO QCD fit.

3.3. Scaling Properties and $\beta$ dependence

The $Q^2$ and $\beta$ dependences of the diffractive cross section are shown in Figs. 5 and 6 in a kinematic range ($y < 0.6$, $x_F < 0.01$) where to good approximation $\sigma_{D} = F_2^D$ and the reggeon term is negligible. The shown data points display the pure $\beta$ and $Q^2$ dependences of the structure function $F_2^D$, kinematic effects related to $x_F$ and $t$ have been corrected by dividing the cross section by $f_\gamma$. In Fig. 5, the structure function displays approximate scaling for $\beta = 2/3$. For lower values the data exhibit scaling violations which are driven by a large gluonic component in the diffractive exchange. The structure function depends only weakly on $\beta$ as shown in Fig. 6.

3.4. Diffractive parton densities

The H1 Collaboration has extracted diffractive parton densities from QCD fits to the diffractive structure function data. The $x_F$ and $t$ dependence of the PDFs is given by the flux factor as discussed in Sec. 3.2. The $\beta$ dependences of the quark and gluon densities are parameterised at a starting scale $Q_0^2 = 3$ GeV$^2$ and are evolved to the measured $Q^2$ values using the DGLAP equations [5]. The best fit is shown in Figs. 3–6 and describes the measurements very well. The corresponding parameterisations for the NLO and LO quark and gluon densities are shown in Fig. 7. The gluon carries $\approx 75\%$ of the momentum of the diffractive exchange. The error band around the NLO densities includes experimental (inner band) and model uncertainties (outer band) which have been propagated to the PDFs. The gluon density is known to better than $30\%$ up to fractional momenta $z \approx 0.5$, but is poorly known at large $z$. These densities have been used to predict diffractive final state cross sections such as dijet and heavy flavour production at HERA [6] and at the Tevatron [3].

3.5. Ratio of diffractive to inclusive cross section

The ratio of the diffractive to the inclusive cross section at the same $x = \beta x_F$ is shown in Fig. 8 for $x_F = 0.01$ as a function of $Q^2$. For this particular $x_F$ and the corresponding gap size, the diffractive contribution amounts to $2$–$3\%$ of the inclusive cross section. The ratio is flat for $\beta < 0.6$ indicating a similar QCD evolution of the inclusive and the diffractive structure functions away from the kinematic limit $\beta = 1$ [3].

3.6. Charged current cross section

Diffractive processes which occur via $W$ boson exchange instead of photon exchange have been
measured by H1 using events with missing transverse energy which is carried away by the neutrino [7]. The ratio of the diffractive to the inclusive charged current cross section was measured to be $2.5\% \pm 1.0\%$ for $x_F < 0.05$. The cross section as a function of $\beta$ is shown in Fig. 9. It is well described by a leading order Monte Carlo prediction which is based on the diffractive parton densities extracted in neutral current processes.

4. CONCLUSIONS

Diffractive structure functions have been measured by the H1 Collaboration to unprecedented precision. The data are consistent with QCD factorisation and diffractive parton densities have been extracted in QCD evolution fits. The gluon component carries $\approx 75\%$ of the momentum of the diffractive exchange. QCD factorisation was tested in diffractive charged current interactions where predictions based on the neutral current PDFs are in good agreement with the measured cross section. Diffractive and inclusive deep-inelastic $ep$ scattering were shown to evolve similarly with the hard QCD scale.

Figure 6. The diffractive structure function $F_D^{2}$ as a function of $\beta$ compared with the H1 2002 NLO QCD fit. The $x_F$ dependence has been divided out.

Figure 7. The H1 diffractive quark and gluon densities as extracted in a QCD fit to structure function data.

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Figure 8. The ratio of diffractive to inclusive $ep$ scattering cross sections as a function of $Q^2$ at $x_P = 0.01$ for different values of $x = \beta x_P$.

Figure 9. The diffractive charged current cross section as a function of the momentum fraction $\beta$ compared with a LO prediction based on the LO diffractive parton densities of Fig. 7.