A Scenario of Heavy but Visible Baryonic Dark Matter

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ABSTRACT: We consider a model in which dark matter is a composite baryon of a dark sector governed by $SU(3)$ gauge theory, with vector-like quarks also charged under $U(1)_Y$. The model provides simple answer to the dark matter stability problem: it is a result of the accidental dark baryon number conservation. And with an analogy to QCD, all physical quantities of the dark matter can be calculated by rescaling the QCD experimental results. According to the thermal freeze-out mechanism the mass of the dark matter is predicted to be $O(100)$ TeV in order to achieve a correct relic abundance. Such heavy dark matter is in general hard for detection due to small dark matter number density in the universe. However, dark baryon number in our model is not necessarily strictly preserved thanks to operators suppressed by the Planck scale, and such decay operator results in a decay lifetime marginal to the current detection bound. We show our model with $O(10^{27})$ s dark matter decay lifetime can explain the AMS-02 anti-proton data, if it is experimentally interpreted as an access, although some theoretical uncertainty may weaken its significance. We also investigate other phenomena of this model such as the extragalactic gamma ray and neutrino signatures.
1 Introduction

A lot of particle physics candidates have been worked out for dark matter (DM), which takes about 26% of the energy density of our universe \(^1\). All of the models have, at least after tuning to certain parameters, to explain some basic facts of DM such as its stability, weakness of its interaction with the standard model (SM) matter, its relic abundance and so on. Mainly motivated by the stability problem, we revisit the composite DM model, in which DM is a baryonic or antibaryonic composite particle in a hidden strong gauge interaction, or the technibaryon DM which has a long history \(^2\)–\(^4\) (see more recent similar works \(^5\)–\(^10\), and more generally the references in \(^10\)).

In the simplest put our composite DM model is a copy of quantum chromodynamics (QCD) at different scale. Some hidden strong gauge group at certain scales has exactly the same QCD phenomena of color confinement and chiral symmetry breaking, they contain fermionic dark baryons as composite bound states in totally antisymmetric representation. In particular we will see that our model also has an \(SU(3)\) strong gauge group, which will be introduced below. Protected by the accidental baryon number, the QCD proton is stable empirically, even if the theory is promoted to the grand unified theory (GUT) and proton decay is allowed. The stability of (the lightest) dark baryon is similarly guaranteed, as a consequence of the accidental dark baryon number conservation.

Within baryonic DM models there are still a lot of possibilities, and some of the models are actually difficult to test. If the dark sector and the SM sector are connected
only by some portal particle, then the typical interaction between the two sectors may be too weak to see (e.g. the direct detection cross section). Moreover, for reproducing the correct relic abundance we would like to stick to the simplest assumptions that the DM is a thermal relic (as well as implicitly the dark baryon antibaryon are symmetric in number). However, in the following we will see that the repetition of the QCD exactly provides us a tool to calculate the thermal freeze out cross section, and the DM mass is therefore determined to be $\mathcal{O}(100)$ TeV \cite{6-10}. Such high scale DM mass implies a very small DM number density in the universe, and suppressing any DM event rates such as direct detection and annihilation, making it invisible. In particular, we have checked that even with the largest possible annihilation cross section of the $s$ wave unitarity bound, the most optimistic NFW DM profile and large exposure time assumptions, next generation gamma ray indirect detection experiment such as the CTA still cannot probe/constrain such a high scale DM candidate from the galaxy center, similar to \cite{11}.

Still we manage to test our model. Instead of connecting the two sectors with a portal, we consider the following criteria \cite{8} that, while the dark baryon itself must carry no net SM charges for being sufficiently weakly interacting with the visible sector, the vector-like quarks in the hidden sector are charged under some SM gauge groups of $SU(3)_c \times SU(2)_L \times U(1)_Y$. And the second problem of being too heavy on the other hand weakens the DM stability if it is not absolute, eventually enhance the decay rate to a detectable level as a benefit. For our benchmark $SU(3)_{hid} \times SU(2)_R \times U(1)_{B-L}$ model the decay spectrum can be determined and the decay rate happens to be marginal to the current bound, which eventually makes the model testable. For example we compare our model prediction of DM decay against the preliminary AMS-02 antiproton data, as well as checking with the Fermi extragalactic gamma ray and the IceCube neutrino data. In all, (unlike many early work) we have provided answers to every aspect of DM physics, by building a model which is simple, and detectable or falsifiable in the near future.

This paper is structured as followed. Section 2 is a quick check of the stability in more details. In Section 3 we discuss the rescaling calculation of the DM annihilation cross section, and eventually show the DM mass scale of 150 TeV. Next Section 4 is devoted to the discussion of the specific gauge group choice, in which an $O(10^{27})$ $s$ decay life time is estimated and the $SU(3)_{hid} \times SU(2)_R \times U(1)_{B-L}$ is justified, with discussion of constraints (such as the one from the big bang nucleosynthesis) for various scales implicitly in the model building. We check the recent AMS-02 antiproton data with the decay life time as a major test of the model in Section 5, as well as check other constraints such as the extragalactic gamma ray and neutrino flux. At last we conclude in Section 6.

2 The Dark Matter Stability

The solution of DM stability, or suppression of any possible decay operators by composite-ness, still allows a range of hidden gauge groups. Suppose the hidden strong gauge group is an $SU(N)$ gauge group, with $N$ an odd number for baryon to be a fermion. The dark baryon is in the totally antisymmetric representation of $N$ dark quarks, and as the proton decay in GUT the effective decay operator is at least $N + 1$ fermions times together, with
the new “1” being some (not necessarily to be new, as we will see) “lepton”. To be overall mass dimension 4 we need high scale Λ suppression of power $\left(\frac{3}{2}(N+1) - 4\right)$. In such analysis the DM has an decay width of order

$$\Gamma \sim m_\chi^{3N-4}/\Lambda^{3N-5}. \quad (2.1)$$

This hidden strong gauge group has no relation with the postulated GUT in the visible sector, so the first choice of the large scale is the Planck scale. Then we can see that even for a minimal $N = 3$, the DM can be stable enough. However, the choice of $N = 3$ will actually turn out to be tricky and interesting, as shown in Section 4.

Further comment is that we expect this dimension-6 $QQQL$ operator for $N = 3$ gives leading contribution to DM decay, simply because given the dimension of $3 \times \frac{3}{2}$ (with $\frac{3}{2}$ being the quark dimension) which must appear as a whole in any possible decay operator, it is unable to construct any operator with even lower dimension. Within the framework of dimension-6 $QQQL$ operator the decay process exactly resembles the QCD proton decay, and the lattice calculation of the QCD proton decay matrix element can be rescaled to give results in the dark sector, given that the lepton $L$ mass are much lower. Specific choice such as whether the $L$ is charged or neutral will depend on the model building, which will be addressed in Section 4. Apparently going to even higher dimensions there are various operator choices such as just adding powers of the SM $H^\dagger H$ to the operator, but they will have much more suppressed decay contributions and are irrelevant.

3 Dark Matter Annihilation and Mass

Due to the strong dynamics nature there is no way to calculate from the first principle the annihilation cross section of baryons with antibaryons at the low velocity regime. A useful first approximation is given by the unitarity bound [12]

$$\sigma v_{\text{rel}} \simeq \frac{4\pi(2\ell + 1)}{m_B^2 v_{\text{rel}}}. \quad (3.1)$$

This unitarity bound can be obtained by solving a nonrelativistic Schrodinger equation, with a complex potential to decrease the exiting wave amplitude. Achieving the unitarity bound corresponds to a vanishing exiting $\ell$ partial wave, which is a result of alignment of the potential configuration. Potential scattering is nonperturbative in nature, in the Feynman diagram point of view messenger particles are repeatedly exchanged, forming ladder diagrams. And enhancement of the hard scattering/annihilation process are taken into account in this way, recovering the Sommerfeld enhancement [13, 14].

The approximation of Eq. (3.1) is indeed supported by the real QCD experiments. In the low velocity regime higher partial waves are suppressed by powers of velocity, leading to a general $s$ wave domination if it is not forbidden by symmetries. However for a thermal freeze out velocity of $v_{\text{rel}} \simeq 0.4$, the $s$ wave may be further assisted by a $p$ wave or even higher partial waves. In Fig. 1 we see from experimental results that the annihilation cross section is indeed higher than $s$ wave unitarity bound by a factor of a few, due to mainly
Figure 1. The QCD measurement of baryon antibaryon annihilation cross section $\sigma v$ in the low relative velocity region. At higher relative velocity $\sigma v$ will exceed the $s$ wave or the $(s + p)$ wave unitarity bound. $\bar{p}p$ data are taken from [15–18], and $\bar{n}p$ data are taken from [19, 20].

the $p$ wave contributions. A significant $p$ wave contribution same to our case has already been shown in [20].

In Eq. (3.1) the true QCD annihilation cross section scales as $m_B^{-2}$ with $m_B$ the QCD baryon mass, while the $2\ell + 1$ adopt an effective value of about two to four (note that the annihilation remains rather constant with variation of relativity velocity in Eq. (3.1), which means the effective $2\ell + 1$ has a rough scaling with $v_{rel}$, to cancel the $v_{rel}$ dependence). If it is applied to the dark sector baryon antibaryon annihilation the same effective $2\ell + 1$ should be kept, difference is only in replacing the QCD baryon mass (about 1 GeV) by the dark baryon/antibaryon mass. Namely the DM annihilation cross section is just a rescaling of the QCD annihilation cross section

$$\sigma_{v_{rel}}^{DM}(m_\chi) = \sigma_{v_{rel}}^{QCD} \times \left(\frac{1 \text{ GeV}}{m_\chi}\right)^2,$$

(3.2)

where $\sigma_{v_{rel}}^{QCD}$ is the averaged value of purple and blue points in the Fig. 1. In the following we will see that our benchmark model is also based on the $SU(3)$ strong gauge group; and we are taking implicitly that the current quark mass is at least one order smaller than the baryon mass, making the chiral symmetry breaking effect small as the QCD. In such case the effective theory can be approximated by only one scale, which is the QCD scale of typical baryon mass for the real QCD, and the dark baryon mass for the dark sector$^1$. Thus the strong dynamics of the dark sector is quite similar to the real QCD case, and we expect the rescaling calculation to be very good.

$^1$The other scales introduced in Section 4.2,4.3 has nothing to do with the annihilation.
The thermal freeze out mechanism is the most elegant way to reproduce the observed relic abundance, in which we only set the DM annihilation cross section to the famous $3 \times 10^{-26} \text{ cm}^3 \text{s}^{-1}$, corresponding to $\Omega_{\chi} h^2 \simeq 0.12$. When we do this to the baryonic dark sector we get

$$m_\chi \simeq 150 \text{ TeV}. \quad (3.3)$$

Here we make a few comments and comparisons on the result, which is crucial to the following analysis. This number is larger than the literature value of the $s$ wave unitarity bound of the DM mass in thermal freeze out, which calculated from Eq. (12) of [12] is about 86 TeV for a Dirac fermion. Note that the latter number is assuming a freeze out relative velocity of about $0.4c$. In Fig. 1 at such relative velocity we can read the true baryonic annihilation cross section is almost four times larger than the $s$ wave unitarity bound, so a further factor of two difference of DM mass can be understood. The discussion for higher partial waves in [12] is implicitly assuming that one partial wave will dominate the total annihilation cross section. This assumption fails for a strong dynamics system such as the QCD case, which has already been shown in Fig. 1 for the real QCD. Still in the same small relative velocity regime due to the strong dynamics nature many partial waves contribute to the annihilation amplitude and possibly interfere with each other, in that case the implicitly omitted $2\ell + 1$ factor in [12] makes a difference.

4 The Benchmark $SU(3)_{\text{hid}} \times SU(2)_R \times U(1)_{B-L}$ Dark Matter Model

4.1 The Hidden Gauge Group

The high scale of DM does provide one advantage, that the increase of decay width from Eq. (2.1) makes better chance of its detection in the decay channel. We start with checking $N = 3$, a reduced Planck scale\(^2\) square suppression and the dark baryon mass of 150 TeV.

Eq. (2.1) gives

$$\Gamma \simeq m_\chi^5/\Lambda_{Pl}^4 \approx (150 \times 10^3)^5/(2.4 \times 10^{18})^4 = 2.3 \times 10^{-48} \text{ GeV},$$

which corresponds to a decay life time of $2.9 \times 10^{23} \text{ s}$. This estimation has already revealed an amazing coincidence, that the minimal model leads to a decay life time close to the current observational limit.

We can use lattice calculation of the GUT proton decay to further improve the estimation. Rescaling Eq. (10) of [21] of such calculation gives further significant corrections of an extra factor of $1/(32\pi)$ from the phase space, and another $10^{-2}$ or so as the lattice calculated matrix element amplitude square of $W_0^2 \simeq (0.1 \text{ GeV}^2)^2$ divided by the QCD proton mass to the fourth. Putting altogether the decay life time is a few times $10^{27} \text{ s}$.

The choice of hidden gauge group of $SU(3)$ has additional benefit, of further justifying the previous rescaling of the annihilation calculation. The real QCD has strong gauge group of $SU(3)_c$, or baryon consisting three quarks. The choice of $SU(3)_{\text{hid}}$ also preserves this structure, which is expected to minimize the uncertainty of our ignorance of strong

\(^2\)Here we use the reduced Planck scale $(8\pi G)^{-\frac{1}{4}} = 2.4 \times 10^{18} \text{ GeV}$ rather than the Planck scale $G^{-\frac{1}{4}} = 1.2 \times 10^{19} \text{ GeV}$. The reduced Planck scale appears naturally in supergravity theory of particle physics. The Planck scale, on the other hand, already gives too low a decay rate.
dynamics, making the rescaling the most reliable compared with other choices of the strong
gauge group.

4.2 Introduction of the SU(2)_R × U(1)_{B−L}

Let’s take a look at other aspects of the minimal SU(3)_{hid} model. The requirement that it is also charged under some SM gauge group is minimally satisfied for the SM U(1)_Y group, and that will induce the SM electromagnetic interactions and the current quarks will be SM electromagnetically charged. To further build our model we refer to the most common way of extension of the U(1)_Y in beyond SM model building, namely the SU(2)_R × U(1)_{B−L} → U(1)_Y left-right symmetry model, which also gives the neutrino masses. An SU(2)_R gauge group behaves as the counterpart of the SU(2)_L isospin, and the U(1) before this breaking becomes B − L. The hidden quarks are postulated to be in the doublet representation of SU(2)_R.

| Gauge | SU(3)_H | SU(3)_c | SU(2)_R | SU(2)_L | U(1)_{B−L} |
|-------|---------|---------|---------|---------|------------|
| Φ     | 1       | 1       | 3       | 1       | +1         |

| New Particle | | | | | |
|--------------|--------------|--------------|------------|
| Q_L          | 3            | 1            | 2          | 1 + 1/3   |
| Q_R          | 3            | 1            | 2          | 1 + 1/3   |
| H            | 1            | 1            | 2          | 2         |
| q_L          | 1            | 3            | 1          | 2 + 1/3   |
| q_R          | 1            | 3            | 2          | 1 + 1/3   |
| l_L          | 1            | 1            | 1          | 2 − 1/3   |
| l_R          | 1            | 1            | 2          | 1 − 1/3   |

Table 1. The particle content and their quantum numbers.

Going back to the minimal dimension-6 decay operator Q_R Q_R Q_R l_R, the “lepton” is also in the doublet representation of SU(2)_R. Actually it can be identified as the SM right handed charged lepton, which is also promoted by the beyond SM SU(2)_R. The model is shown in Table 1. Here we also introduce an SU(2)_R triplet Φ, which gets some large vacuum expectation value to break the SU(2)_R, and gives large masses to the SU(2)_R W boson and the right handed neutrino [22]. The right handed neutrino mass scale is postulated to be determined by the natural seesaw mechanism, or much larger than the DM scale of 150 TeV, so the ℓ_R could only be the charged right handed lepton, in order not to be kinetically forbidden. We do not expect forbidden of right handed neutrino decay channels significantly affects the estimation of the DM life time.

At the level of the elementary particle our model can be summarized as the renormalizable Lagrangian

\[ \mathcal{L} = \mathcal{L}_{LR} - (\lambda^{T}_R \bar{\epsilon}_L \Phi \ell_R + h.c) \]

\[ - \frac{1}{4} G_{\mu \nu}^{a} G^{\mu \nu} - \frac{1}{4} W_{\mu \nu}^{a} W^{a \mu \nu} - \frac{1}{4} F_{\mu \nu} F^{\mu \nu} \]

\[ + \bar{Q}_L (i D - M) Q_L + \bar{Q}_R (i D - M) Q_R + (D_{\mu} \Phi)^{T} D^{\mu} \Phi. \]

(4.1)
The $\mathcal{L}_{LR}$ is the left-right symmetric extension of the SM, and we write the allowed neutrino Majorana mass terms separately. Note the $\epsilon = i\sigma^2 = (-1,1)$ in the $SU(2)$ contraction, and in this matrix basis $\langle \Phi \rangle = (\nu \nu)$. Each covariant derivative can be read from Table 1.

Note that if we choose the SM $SU(2)_L$ rather than the $SU(2)_R$ for the dark quark, then the dark baryon is also charged under the SM $SU(2)_L$. This still suits the definition of “WIMP”, but the scattering with ordinary matter in direct detection will have charge induced $W^\pm$ scattering rather than the current dipole induced photon scattering as the leading one, and we do not consider this situation in our scenario.

4.3 The Mass Splitting between Dark Neutron and Proton

After the introduction of $SU(2)_R$, the baryonic DM candidate is also promoted into doublet. The dark neutron is the DM candidate. The dark proton need to be heavier than the dark neutron, and after thermal freeze out decay early enough to it.

Dimensional analysis suggests such decay has a width of $\Gamma \propto \Delta m^5/m_W^4$ [23], where $m_W$ is the SM (or $SU(2)_R$) $W$ boson mass for real QCD (or the dark sector), and $\Delta m$ is the mass difference between the SM (or dark) proton and neutron. The simple requirement that the dark proton to dark neutron decay life time is before the big bang nucleosynthesis ($\lesssim 1$ s) corresponds to a constraint of

$$\Delta m \gtrsim 0.22 \left( \frac{m_{W_R}}{10^8 \text{ GeV}} \right)^4 \text{ TeV},$$

which is obtained by rescaling the QCD free neutron to proton decay.

The mass difference between the dark proton and the dark neutron comes in two ways: One is the electromagnetic radiative self energy correction which applies only to charged proton. The other is the current quark mass differences. In real QCD the two happen to cancel with each other, with the latter the dominant one which makes neutron heavier. However in our dark baryonic sector the two can be additive. The radiative self energy correction will contribute a fixed mass splitting of about 0.1% of the baryon mass, which alone will be sufficient for a light $m_{W_R} < 10^8$ GeV or a low seesaw scale, nothing else is needed.

On the other hand, for a heavy $m_{W_R}$ the radiative self energy correction is not enough, and the current quark mass splitting shall be the dominant source of mass differences between dark neutron and proton. In our setup it can be generated by the dimension-5 operator $\bar{Q} \Phi^\dagger \Phi Q$, in which the vacuum expectation value of $\Phi$ indeed makes the “up type” dark quark as well as the dark neutron heavier (viz. we give a theory for the up-down current quark mass splitting which is unexplained in QCD). Assuming the $SU(2)_R$ coupling is order one, the vacuum expectation value of $\Phi$ is expected to be at the same order of $m_{W_R}$. Here we need to introduce a new effective suppression scale $\Lambda'$ for the dimension-5 operator. In Fig. 2 we plot the $m_{W_R}$ vs. $\Delta m$ with several $\Lambda'$s. We can see that the big bang nucleosynthesis constraint only exclude some region of $\Lambda' \gtrsim 10^{14}$ GeV, even when the $\Delta m$ is reasonably small.
Figure 2. The big bang nucleosynthesis constraint of $\tau \lesssim 1$ s (shaded region excluded), on the dark neutron proton mass splitting $\Delta m = 0.15 \text{ TeV} + m_W^2/\Lambda'$ (electromagnetic radiative self energy correction plus current quark mass splitting from dimension-5 operator) with $m_W$.

### 4.4 The Dark QCD Spectrum

In addition to the baryonic new particles in the dark sector possibly there are also mesonic new particles. Among them the most interesting ones will be the lightest, which are the pseudo Nambu-Goldstone (pNG) bosons\(^3\). Corresponding to the QCD pions in the hypothetical proton decay, they can be the other decay product of the dark neutron except for the right hand charged leptons. Like the SM pions they are not stable either, the charged one can decay through a virtual $W_R$ into SM fermions, with the chirality flipping mechanism making the top bottom pair the dominant channel, and the neutral one will dominantly decay into photon pairs through anomalous triangle diagram.

In real QCD the pion mass is determined by the Gell-Mann-Oakes-Renner relation \(^{[24]}\) from the partially conserved axial current principle

$$m_\pi^2 = -\frac{(m_u + m_d)}{f_\pi^2}\langle\bar{q}q\rangle$$

(4.3)

In our dark QCD with the baryonic particle scale of 150 TeV, we expect the $-\langle\bar{q}q\rangle/f_\pi^2$ also at the scale of hundred TeVs. The current quark mass is a complete free parameter, making the dark pNG pion mass also a free parameter. On the experimental side, the charged component of the dark pion should decay through a virtual $W_R$ which is exactly like the QCD pion decay through a virtual SM $W$, and chirality flipping mechanism makes the $t_R\bar{b}_R$ channel the dominant one. However the usual searches for $W'^\pm \rightarrow tb$ (or the $H'^\pm \rightarrow tb$ which shares the same final state) assumes a singly produced $\Pi'^\pm$, and in our model the dark pion should be produced in pairs by a very energetic gamma. Since searches for the top and bottom dijets in pairs have not been performed in this topology, and the

\(^3\)We assume some other broken symmetry to protect this Nambu-Goldstone bosons from having large masses. Note that one cannot equate the $SU(2)_R$ as the isospin $SU(2)_L$ in real QCD the chiral breaking of which leads to the QCD pion, for the quarks in our scaled-up QCD are vector-like.
production is through electroweak process which is very suppressed compared to a QCD process, there is essentially no experimental constraint.

We also expect other mesons in the spectrum which differ in discrete quantum numbers, such as the dark $\eta$ meson, the $\rho$ meson, the $\omega$ meson and so on. Without a universal understanding of the spectrum in strong dynamics we do not know the exact mass comparison with the dark neutron, so we will ignore their contribution in the dark neutron decay.

5 DM Decay Detectibility

Next we will compare the theoretical prediction of the $\mathcal{O}(10^{27} \text{ s})$ DM decay life time to current and future experiments, to see whether they are detectable. We find that the AMS-02 preliminary antiproton data indeed favors an $\mathcal{O}(10^{27} \text{ s})$ DM decay life time, and it does not exceed the Fermi EGB bound and the IceCube neutrino bound. As a benchmark we ignore all the SM particle mass including the top quark which are much smaller, and choose the dark pion mass to be $1/10$ of the dark baryon mass or 15 TeV. We want to emphasize that it should not be taken as a rigorous data driven fit.

Except for the three DM indirect detections, we found direct detection experiments are also constraining and complementary. Our result agrees with [10] and we would like to redirect reader to their paper but not repeat it here.

5.1 Proton and Antiproton ratio

The dark neutron will decay through the proton decay like chain of $N \rightarrow \ell^+_R \Pi^- \rightarrow \ell^+_R \ell^- R \Pi^- \rightarrow \ell^+_R \ell^- R \bar{t} \bar{b}$ as discussed before. The neutral decay mode of replacing the $\ell^+_R$ by the (on-shell) right hand antineutrino is kinematically forbidden. The branching ratio for $\ell^+$ is assumed equal for three families. The same but every particle replaced by antiparticle decay chain applies to dark antineutron.

For the most interesting decay product of top quark, the energy distribution can be determined analytically in the sequential two body decay. With $m_{\Pi} = 15$ TeV fixed the charged lepton has a fixed energy of $E_\ell = (m^2_{\chi} - m^2_{\Pi})/(2m_\chi) = 74.25$ TeV, and the top and bottom will be evenly distributed in the energy region from $E_{\text{qmin}} = \frac{1}{2} (E_{\Pi} - \sqrt{E^2_{\Pi} - m^2_{\Pi}})$ to $E_{\text{qmax}} = \frac{1}{2} (E_{\Pi} + \sqrt{E^2_{\Pi} - m^2_{\Pi}})$, where $E_{\Pi} = (m^2_{\chi} + m^2_{\Pi})/(2m_\chi) = 75.75$ TeV. All the prompt decay spectra are then calculated by

$$
\frac{dN_i}{dE} = \sum_{q=t,b} \int_{E_{\text{qmin}}}^{E_{\text{qmax}}} \frac{dE_q}{E^2_{\Pi} - m^2_{\Pi}} \left( \frac{dN_i}{dE} \right)'_q (m_\chi = E_q)
+ \frac{1}{3} \sum_{\ell=\ell^+} \left( \frac{dN_i}{dE} \right)'_\ell (m_\chi = E_\ell),
$$

(5.1)

where the primed $\frac{dN_i}{dE}$ are taken from the PPCP4 [25] for $i = p\bar{p}, e^+e^-, \gamma$ and so on. 4

4The PPCP4 cosmic ray spectrum calculation is only available for unpolarized primary quarks, but in
The antiproton prediction are shown in Fig. 3, to the AMS-02 preliminary antiproton data [26] which shows a slight excess but still can be viewed as consistent with background. In this work we use the the NFW halo profile and the MAX/MED propagation parameters [27, 28] for antiproton, as argued recently in [29] that the MED is less favored by isotopic abundance data from AMS-02, but for completeness we still leave our prediction for MED on the right panel. The background is taken from [30]. Considering $K > 10$ GeV, the best-fit DM decay time is $\tau = 2.4 \times 10^{27}$ second for MAX and $\tau = 4.5 \times 10^{26}$ second for MED. The chi-square improvement of $(\chi^2_{\text{Sum}} - \chi^2_{\text{Secondary}})/\text{d.o.f.}$ can achieve 19.97/17 (66.29/17) for MAX (MED).

We have checked that varying the dark pion mass (e.g., by a factor of two) has negligible effect on the spectrum (Eq. 5.1), as well as the experimental statistical strength. The result always holds as long as the dark pion mass is much smaller than the dark matter mass.

5.2 Extragalactic Gamma Ray and Neutrino

The EGB\(^5\) prediction comparing with the Fermi-LAT 4 year data [33] are shown in Fig. 4. We ignored the local DM decay contribution such as that from our Milky Way, only working for redshift $z_{\text{min}} = 10^{-4}$ to $z_{\text{max}} = 2$ where the gamma ray is effectively cut off by the optical

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\(^5\)In [31] it is pointed out that the most stringent gamma ray limit for decaying DM is from the angular cross-correlation of low-redshift sources, but the improvement, c.f. [32], seems weaker in our high energy region.
depth for all interested energy. We also ignore the contribution from inverse Compton scattering of our charged decay product with the CMB photons, which is less important in our interested high energy region and makes the result conservative. The gamma ray flux can be described by

$$\frac{d\Phi_\gamma}{dE} = \frac{c}{4\pi m_\chi\tau_\chi} \int_{z_{\text{min}}}^{z_{\text{max}}} dz e^{-\tau(z,E)} \frac{dN_\gamma}{dE}(E^z),$$

(5.2)

where $H(z) \simeq H_0 \sqrt{(\Omega_{\chi} + \Omega_b)(1+z)^4 + \Omega_\Lambda}$ is the Hubble function and the data of $H_0, \Omega_0, \Omega_\chi, \Omega_b, \Omega_\Lambda$ and critical density $\rho_c$ are taken from [34]. The redshifted photon energy $E$ measured at earth is related to the initial energy of $E^z = E(1+z)$ at production, and the optical depth suppression $e^{-\tau(z,E)}$ is taken of the min UV case in PPC4 [25]. For the background we use a power law with cutoff, ignoring possible astrophysical sources such as blazars, star-forming galaxies [35], and misaligned active galactic nuclei [36, 37].

In general we find an $O(10^{27})$ s decay life time is consistent with the Fermi EGB gamma ray data. For example, with $\tau = 2.4 \times 10^{27}$ s favored by the AMS-02 antiproton data with MAX propagation, our model prediction is well below the Fermi EGB gamma ray data. On the other hand, the $\tau = 4.5 \times 10^{26}$ s favored by antiproton data with MED propagation is almost excluded, but still barely allowed if including the 2σ error band of the antiproton data.

Also the $O(10^{27})$ s decay life time is allowed in the neutrino channel. There is no recent isotropic neutrino data in our desired energy regime, so we use an extrapolation fitted

\footnote{In our model we cannot have primary SM neutrinos and all produced SM neutrinos are secondary, and their energy should be much smaller than the DM scale of 150 TeV, so unable to account the IceCube 100 TeV to PeV neutrino signals.}
from the IceCube neutrino data at an even higher energy spectrum [39], assuming a single unbroken power law and equal neutrino fluxes of all flavors. In the right panel of Fig. 4, it is shown that the $O(10^{27})$ s decay life time is at least two orders below the current IceCube neutrino extrapolated bound.

6 Summary

We have proposed a new scenario of baryonic DM based on a strong hidden $SU(3)$ gauge group, which also connects to the visible sector through the $SU(2)_R \times U(1)_{B-L}$ gauge group. This composite gauge group is primarily motivated by the DM stability consideration, but the hypothetical Planck scale suppressed decay can induce interesting possible signals while the connection sector $SU(2)_R \times U(1)_{B-L}$ is added.

In the minimal model building we introduce the following scales

- The DM or the dark baryon mass scale of 150 TeV, which is determined by rescaling the real QCD baryon antibaryon annihilation cross section to the “WIMP miracle” cross section.
- The dark pion mass scale which is much lower.
- The $SU(2)_R$ breaking scale, which is free but appears in the natural seesaw mechanism.
- The optional free effective suppression scale of the dimension-5 operator.

We find that theoretical estimation and fitting to recent preliminary AMS-02 antiproton data are both consistent with a decay life time of a few $10^{27}$ s. Although being heavy, our DM model has a perspective of detection in the near future.

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References

[1] P. A. R. Ade et al. [Planck Collaboration], arXiv:1502.01589 [astro-ph.CO].
[2] S. Nussinov, Phys. Lett. B 165, 55 (1985).
[3] R. S. Chivukula and T. P. Walker, Nucl. Phys. B 329, 445 (1990).
[4] S. M. Barr, R. S. Chivukula and E. Farhi, Phys. Lett. B 241, 387 (1990).
[5] S. B. Gudnason, C. Kouvaris and F. Sannino, Phys. Rev. D 74, 095008 (2006) [hep-ph/0608055].
[6] H. Murayama and J. Shu, Phys. Lett. B 686, 162 (2010) [arXiv:0905.1720 [hep-ph]].
[7] T. Hambye and M. H. G. Tytgat, Phys. Lett. B 683, 39 (2010) [arXiv:0907.1007 [hep-ph]].
[8] K. Hamaguchi, E. Nakamura, S. Shirai and T. T. Yanagida, JHEP 1004, 119 (2010) [arXiv:0912.1683 [hep-ph]].
[9] O. Antipin, M. Redi and A. Strumia, JHEP 1501, 157 (2015) [arXiv:1410.1817 [hep-ph]].
[10] O. Antipin, M. Redi, A. Strumia and E. Vigiani, JHEP 1507, 039 (2015) [arXiv:1503.08749 [hep-ph]].
[11] A. Ibarra, A. S. Lamperstorfer, S. López-Gehler, M. Pato and G. Bertone, JCAP 1509, no. 09, 048 (2015) Erratum: [JCAP 1606, no. 06, E02 (2016)] [arXiv:1503.06797 [astro-ph.HE]].
[12] K. Griest and M. Kamionkowski, Phys. Rev. Lett. 64, 615 (1990).
[13] J. Hisano, S. Matsumoto and M. M. Nojiri, Phys. Rev. Lett. 92, 031303 (2004);
[14] J. Hisano, S. Matsumoto, M. M. Nojiri and O. Saito, Phys. Rev. D 71, 063528 (2005).
[15] W. Bruckner, B. Cujec, H. Dobbeling, K. Dworschak, F. Guttnner, H. Kneis, S. Majewski and M. Nomachi et al., Z. Phys. A 335, 217 (1990).
[16] A. Bertin et al. [OBELIX Collaboration], Phys. Lett. B 369, 77 (1996).
[17] A. Benedettini et al. [OBELIX Collaboration], Nucl. Phys. Proc. Suppl. 56, 58 (1997).
[18] A. Zenoni, A. Bianconi, F. Bocci, G. Bonomi, M. Corradini, A. Donzella, E. Lodi Rizzini and L. Venturelli et al., Phys. Lett. B 461, 405 (1999).
[19] T. Armstrong et al. [BROOKHAVEN-HOUSTON- PENNSYLVANIA STATE-RICE Collaboration], Phys. Rev. D 36, 659 (1987).
[20] A. Bertin et al. [OBELIX Collaboration], Nucl. Phys. Proc. Suppl. 56, 227 (1997).
[21] Y. Aoki, E. Shintani and A. Soni, Phys. Rev. D 89, no. 1, 014505 (2014) [arXiv:1304.7424 [hep-lat]].
[22] M. Fukugita, T. T. Yanagida, “Physics of Neutrinos: And Applications to Astrophysics”.
[23] D. H. Wilkinson, Nucl. Phys. A 377, 474 (1982).
[24] M. Gell-Mann, R. J. Oakes and B. Renner, Phys. Rev. 175, 2195 (1968).
[25] M. Cirelli, G. Corcella, A. Hektor, G. Hutsi, M. Kadastik, P. Panci, M. Raidal and F. Sala et al., JCAP 1103, 051 (2011) [JCAP 1210, E01 (2012)] [arXiv:1012.4515 [hep-ph], arXiv:1012.4515 [hep-ph]].
[26] AMS-02 Collaboration, Talks at the ‘AMS Days at CERN’, 15-17, April, 2015.
[27] F. Donato, N. Fornengo, D. Maurin, P. Salati and R. Tailliet, Phys. Rev. D 69, 063501 (2004) [astro-ph/0306207].
[28] T. Delahaye, R. Lineros, F. Donato, N. Fornengo and P. Salati, Phys. Rev. D 77, 063527 (2008) [arXiv:0712.2312 [astro-ph]].
[29] R. Kappl, A. Reinert and M. W. Winkler, arXiv:1506.04145 [astro-ph.HE].
[30] G. Giesen, M. Boudaud, Y. Genolini, V. Poulin, M. Cirelli, P. Salati and P. D. Serpico, arXiv:1504.04276 [astro-ph.HE].
[31] M. Regis, J. Q. Xia, A. Cuoco, E. Branchini, N. Fornengo and M. Viel, arXiv:1503.05922 [astro-ph.CO].

[32] S. Ando and K. Ishiwata, JCAP 1505, no. 05, 024 (2015) [arXiv:1502.02007 [astro-ph.CO]].

[33] M. Ackermann et al. [Fermi-LAT Collaboration], arXiv:1501.05464 [astro-ph.CO].

[34] P. A. R. Ade et al. [Planck Collaboration], Astron. Astrophys. 571, A16 (2014) doi:10.1051/0004-6361/201321591 [arXiv:1303.5076 [astro-ph.CO]].

[35] M. Ackermann et al. [Fermi-LAT Collaboration], Astrophys. J. 755, 164 (2012) [arXiv:1206.1346 [astro-ph.HE]].

[36] M. Di Mauro, F. Calore, F. Donato, M. Ajello and L. Latronico, Astrophys. J. 780, 161 (2014) [arXiv:1304.0908 [astro-ph.HE]].

[37] Y. Inoue, Astrophys. J. 733, 66 (2011) [arXiv:1103.3946 [astro-ph.HE]].

[38] M. G. Aartsen et al. [IceCube Collaboration], Phys. Rev. D 91, no. 2, 022001 (2015) doi:10.1103/PhysRevD.91.022001 [arXiv:1410.1749 [astro-ph.HE]].

[39] M. G. Aartsen et al. [IceCube Collaboration], Phys. Rev. Lett. 113, 101101 (2014) doi:10.1103/PhysRevLett.113.101101 [arXiv:1405.5303 [astro-ph.HE]].