Anisotropic layered Bi$_2$Te$_3$-In$_2$Te$_3$ composites: control of interface density for tuning of thermoelectric properties

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Layered (Bi$_{1-x}$In$_x$)$_2$Te$_3$-In$_2$Te$_3$ ($x = 0.075$) composites of pronounced anisotropy in structure and thermoelectric properties were produced by zone melting and subsequent coherent precipitation of In$_2$Te$_3$ from a (Bi$_{1-x}$In$_x$)$_2$Te$_3$ ($x > 0.075$) matrix. Employing solid state phase transformation, the Bi$_2$Te$_3$/In$_2$Te$_3$ interface density was tuned by modifying the driving force for In$_2$Te$_3$ precipitation. The structure-property relationship in this strongly anisotropic material is characterized thoroughly and systematically for the first time. Unexpectedly, with increasing Bi$_2$Te$_3$/In$_2$Te$_3$ interface density, an increase in electrical conductivity and a decrease in the absolute Seebeck coefficient were found. This is likely to be due to electron accumulation layers at the Bi$_2$Te$_3$/In$_2$Te$_3$ interfaces and the interplay of bipolar transport in Bi$_2$Te$_3$. Significantly improved thermoelectric properties of Bi$_2$Te$_3$-In$_2$Te$_3$ composites as compared to the single phase (Bi$_{1-x}$In$_x$)$_2$Te$_3$ solid solution are obtained.

Research on thermoelectrics has witnessed a renewal of interest with the drastic improvement of thermoelectric properties owing to nanoscaled structures, e.g. in thin film superlattice/quantum well multilayered structures$^{1-3}$. Although the drawbacks of thin film materials such as their small scale, high cost and processing difficulties restrict their practical application, their favorable properties have stimulated extensive research on preparing nanostructured materials by bulk processes. Examples are high temperature high pressure pressing or spark plasma sintering of nanoscale powder$^{4,5}$. Nanostructured materials prepared by bulk processes, which either contain nanometer sized grains or nanoscale precipitates, have been shown to exhibit a strongly enhanced thermoelectric performance. It is widely accepted that the enhancement is due to a high density of interfaces such as grain boundaries and heterophase interfaces$^{6-9}$. Under certain conditions, the interfaces in thermoelectric materials augmented the Seebeck coefficient and reduced thermal and electrical conductivity by energy filtering of charged carriers$^{10}$. Interfaces have on the other hand been found to induce an increase in electrical conductivity by selective scattering of lower mobility charged carriers by interfacial charged defects$^{11}$. The questions how the interface density on the nanoscale can be controlled and how it affects the transport properties are challenging from both the engineering and the scientific viewpoint.

Several traditional metallurgical methods have shown their potential to achieve nanoscaled structures and to generate interfaces that are beneficial for the thermoelectric properties$^{12-21}$. Physical processes such as eutectic reaction$^{12-15}$, solid state precipitation$^{16-19}$, and spinodal decomposition$^{20,21}$ have been exploited favorably and reproducibly. For clarifying structure-property relationships, the microstructural length scales can be varied systematically in a wide range by adjusting the processing parameters. For example, the lamellar spacing of the layered structure of PbTe and Sb$_2$Te$_3$ formed by the decomposition of Pb$_2$Sb$_6$Te$_11$ is controlled by the temperature and time of the decomposition process$^{16}$ and has been found to range from 30 nm at 200 °C to 200 nm at 500 °C.

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Up to present, the characterization of thermoelectric properties of lamellar thermoelectric materials generated by solidification/solid state phase transformation is either utterly lacking or carried out for isotropic materials prepared by conventional solidification processes. Recalling that lamellar structures formed via liquid/solid or solid state phase transformations exhibit preferential crystallographic orientations with respect to each other, a systematic analysis of the structure-property relationships should include the effects of anisotropy, and precise control of the lamellar growth direction should be attained in such materials, as e.g. by employing directional solidification techniques. In the present work, we apply a specially developed zone melting technique on Bi$_2$Te$_3$-In$_2$Te$_3$ samples, controlling the crystal orientation of the parent solid solution and the lamellar structure that is formed by solid state precipitation. The lamellar spacing is adjusted in a wide range by varying the supersaturation of the parent solid solution. Thoroughly characterized microstructural parameters are correlated with the thermoelectric performance for the first time. Suppression of bipolar transport and enhanced interface density contributed to an improved performance of the material.

**Experimental Synthesis.** Oriented (Bi,In)$_2$Te$_3$ (containing 3, 4, 6, and 7.5 at%In) solid solutions with the {001} plane being parallel to the growth axis were obtained by a seeding zone melting technique. This technique yields an especially uniform composition over the entire length of the zone melted region along the growth direction. More details on the control of macroscopic homogeneity via seeding zone melting can be found in ref. 22. Macroscopic homogeneity is a necessary precondition for the homogeneous distribution of precipitates and thus for a uniform thermoelectric performance of the bulk composite samples. The driving force for precipitation is temperature and concentration dependent, as can be directly seen in the pseudo-binary Bi$_2$Te$_3$-In$_2$Te$_3$ phase diagram according to previous work in the literature and our present work (Fig. 1). The blue lines illustrate the recently reported solidus and liquidus lines, based on which the concentration of the seed alloy for the seeding zone melting is selected. The seed alloys for 3, 4, 6 and 7.5 at% In are 7, 9, 12.5 and 13.5 at%In, respectively.

Samples with In concentrations of 4, 6 and 7.5 at% were vacuum sealed in quartz and isothermally annealed for the precipitation of In$_2$Te$_3$. Note that homogenization after seeding zone melting is not necessary, as a perfectly homogeneous crystal is generated. This reduces possible artifacts and the misinterpretation of measured values significantly. Considering the temperature dependent solubility of In in Bi$_2$Te$_3$, as illustrated by the red line in Fig. 1, a uniform annealing temperature (400 °C in the present work) was chosen for all samples, resulting in a uniform and identical In concentration in the Bi$_2$Te$_3$ matrix in all samples, but a different Bi$_2$Te$_3$/In$_2$Te$_3$ interface density. After annealing for 6 days, the sample was water quenched. Annealing for a longer time of up to 12 days was also performed, but no further change in microstructure and thermoelectric properties was observed. This confirms that 6 days are long enough to reach the equilibrium. The microstructure consists of micro-/nanoscaled Bi$_2$Te$_3$/In$_2$Te$_3$ (“BTIT”) lamellae of different spacing, depending on the initial In concentration. For simplification, all the BTIT composites are termed as BTIT-c with the initial In concentration c = 4, 6, 7.5, in at%In.

**Materials characterization.** The samples were prepared metallographically by grinding with a series of SiC papers up to a grit size of 4000, by polishing with 3 μm and 1 μm Al$_2$O$_3$ powder suspension, and finally polishing with 50 nm colloidal silica. The microstructure was observed using a scanning electron microscope (SEM) equipped with a backscattered electron (BSE) detector and energy dispersive X-ray (EDX) spectrometry. Thickness and volume fraction of the phases in the samples were analyzed using the image processing software Image J. X-ray diffraction (XRD) was used to characterize the constituent phase(s) of the sample. Thin sections of the specimens were examined in the transmission electron microscope (TEM, JEM 3010 - HR pole piece, JEOL). TEM samples were prepared by means of Focused Ion Beam (FIB) using an *in-situ* lift-out technique.
Measurement of thermoelectric properties was performed for all samples. Plates of $4 \times 4 \times 10$ mm$^2$ and $\varnothing 6 \times 1$ mm$^2$ were cut along and perpendicular to the growth direction, respectively. The electrical conductivity ($\sigma$) and Seebeck coefficient ($S$) were measured using the thermoelectric measurement system ZEM-3 in the temperature range from room temperature to 300°C. The equilibrium phase diagram [1] suggests that the temperature-dependent solubility may lead to microstructural changes during aforementioned measurement of the thermoelectric properties. For assuring the accumulated annealing effect (heating rate 1.5 K/min) during measurement on microstructure and properties, repeated measurements on one sample were performed. The measured properties during the second cycle are essentially the same as the first time, indicating the negligible changes within the measurement time. The thermal conductivity ($k_{\text{tot}}$) was calculated from the values of thermal diffusivity ($\alpha$), density ($\rho$) and specific heat ($C_p$) by the relationship $k = \alpha \rho C_p$, where $\alpha$ was measured using a laser flash system (Netzsch LFA-457), $\rho$ was measured by the Archimedes method, and $C_p$ was determined by a combination of the Dulong-Petit law and a differential scanning calorimeter (Netzsch STA-449FA). The measured values fall into the same range and are also consistent with the calculated values by the Dulong-Petit law. For each sample state, 3 samples prepared by the same experimental procedure were characterized with respect to their thermoelectric properties. All samples exhibited similar or identical temperature dependent Seebeck coefficients and thermal diffusivities. A maximum variation of $\pm 12\%$ of the measured electrical conductivity was observed, and average values were finally used in the present work. The variation of the measured heat capacities and thermal conductivities was $\pm 5\%$. The electronic contribution to the thermal conductivity ($k_e$) is determined from the electrical conductivity utilizing the Wiedemann-Franz law, $k_e = L_0 T$. From the total thermal conductivity $k_{\text{tot}}$, the electronic contribution ($k_e$) is subtracted, yielding $k_{\text{lat}}$, the lattice thermal conductivity $k_l$, plus further contributions, particularly the bipolar contribution $k_{\text{bip}}$.

Results and Discussion

Strong anisotropy in structure and thermoelectric properties of layered Bi$_2$Te$_3$-In$_2$Te$_3$. Figure 2 shows a typical morphology and the corresponding XRD pattern of an ingot after annealing. Over the width of the ingot, there are only a few grains (see Fig. 2(a)), all of them with the [001] plane parallel to the growth axis (see XRD patterns in Fig. 2c,f). The lamellar structures obtained after annealing also exhibit a preferential orientation of the lamellae along the growth direction, as shown in Fig. 2(b). The solidified sample is very sensitive to cleavage along the axis during the cutting process, as shown in Fig. 2(c,d), demonstrating the pronounced crystallographic anisotropy of the samples. The XRD pattern (Fig. 2(e,f)) confirm that the the Bi$_2$Te$_3$ grains grow in a preferential orientation perpendicular to the [001] direction. In$_2$Te$_3$ peaks also show the anisotropy, considering that all the visible peaks are indexed $(h k l)$ with $k = l$.

Since the samples produced by zone melting and precipitation exhibit pronounced microstructural anisotropy, also anisotropic thermoelectric properties are expected. Figure 3 shows the temperature dependence of the thermoelectric properties of the sample of which the initial In concentration is 7.5 at%In, i.e. BTIT-7.5, for measurements directions parallel (//) and perpendicular (⊥) to the crystal growth direction. The electrical conductivity $\sigma$, is nearly two orders of magnitude higher than $\sigma$⊥ for the whole temperature range (Fig. 3(a)). This anisotropy in conductivity is dramatically more pronounced than that generally expected for anisotropic single phase Bi$_2$Te$_3$, where the electrical conductivity $\sigma$⊥ is only 3...7 times larger than $\sigma$∥. For the Seebeck coefficient $S$, The negative values agree with the n-type transport behavior of Bi$_2$Te$_3$.[10,28] The decrease of $|S|$∥ with temperature has been assigned to mixed conduction of holes and electrons (bipolar conduction) in this temperature range due to the increasing number of thermally generated holes, considering the narrow band gap of (or below) 130 meV.[29] The bipolar contribution is also the reason for the increasing conductivity with increasing temperature (3a). As opposed to the strong anisotropy in the electrical conductivity, $|S|$∥ is only a little smaller than $|S|$⊥ and exhibits similar temperature dependence. The bright phase in Fig. 2(b) represents the (Bi, In)$_2$Te$_3$ phase, whose In concentration was measured as $\sim 3$ at%, and the black phase represents the In$_2$Te$_3$ phase with negligible Bi concentration. More details on the composition distribution across the two phases will be discussed in detail below.

The temperature dependence of the thermal conductivities in both directions is shown in Fig. 3(c). The thermal conductivity in the direction parallel to the growth direction $k_{\text{lat//}}$ is higher than $k_{\text{lat⊥}}$, reflecting also the anisotropy of the electrical conductivity. However, after subtracting the electronic contribution ($k_e = L_0 T$) from the total thermal conductivity, the remaining thermal conductivity $k_{\text{lat//}}$ becomes smaller than $k_{\text{lat⊥}}$. The value of the Lorenz number is not only dependent on charged carrier concentration and temperature, but also can be influenced by quantum well effects, which e.g. occurs in superlattice/quasi two thin film materials.[30,31] An accurate determination of the Lorenz number of all BTIT composites would require considerably more effort, i.e. the determination of the lattice thermal conductivity utilizing the Wiedemann-Franz law, $L_0 = \frac{k_e S}{\rho T}$, where the electrical conductivity $\sigma$⊥ is only 3...7 times larger than $\sigma$∥, and exhibits similar temperature dependence. The bright phase in Fig. 2(b) represents the (Bi, In)$_2$Te$_3$ phase, whose In concentration was measured as $\sim 3$ at%, and the black phase represents the In$_2$Te$_3$ phase with negligible Bi concentration. More details on the composition distribution across the two phases will be discussed in detail below.
drastically smaller than in the direction parallel to the growth direction, despite the lower thermal conductivity. This is mainly due to the drastically lower $\sigma_{\perp}$, as shown in Fig. 3(a).

Analytical models of the effective properties of layered $\text{Bi}_2\text{Te}_3$-$\text{In}_2\text{Te}_3$. When discussing the thermoelectric properties of BTIT, one has to keep in mind that the material is a two-phase composite material (see Fig. 2). Effective medium theory (EMT) and its generalized derivation (GEMT)\textsuperscript{37–39} have been used to predict the thermoelectric properties of composite materials where a randomly distributed secondary phase is embedded in a matrix\textsuperscript{40,41}. As to BTIT-7.5 in the present work, strong anisotropy effects in structure and thermoelectric properties were confirmed. Hence, it is most appropriate to use a parallel model\textsuperscript{42,43} to predict the transport properties along the layer orientation, and a series model\textsuperscript{42,43} for the properties perpendicular to the layer orientation. It is worth noting that effects of the interface density are not considered in all these models, which will be shown to be an essential limitation later in the discussion section.

The total Seebeck coefficient ($S$) as calculated by a mixture rule follows from the Seebeck coefficients of the two phases 1 and 2 by one of the relationships

$$f_1 \frac{k_1}{\sigma_1} + f_2 \frac{k_2}{\sigma_2} = 0 \quad \text{(EMT model)}$$

Figure 2. (a) Typical macroscopic structure of the Bi-In-Te samples; (b) BTIT lamellar structure in a longitudinal section, where the bright phase represents $\text{Bi}_2\text{Te}_3$ and the dark phase represents $\text{In}_2\text{Te}_3$; (c,d) cleaved interface; (e,f) XRD patterns.
Figure 3. Temperature dependence of (a) electrical conductivity $\sigma$, (b) Seebeck coefficient $S$, (c) thermal conductivity $k$, and (d) $\alpha T$ for BTIT-7.5 in the directions parallel ($//$) and perpendicular ($\perp$) to the crystal growth direction. Solid symbols are for parallel ($//$), open symbols for perpendicular ($\perp$).

$$f_1 \left( \frac{k_1}{\sigma} \right)^{1/t} - \left( \frac{k_1}{\sigma} \right)^{1/t} + f_2 \left( \frac{k_2}{\sigma} \right)^{1/t} - \left( \frac{k_2}{\sigma} \right)^{1/t} = 0 \text{ (GEMT model)}$$

(2)

$$S_{||} = \frac{S_1 \sigma_1 f_1 + S_2 \sigma_2 f_2}{\sigma_1 f_1 + \sigma_2 f_2} \text{ (parallel model, upper limit)}$$

(3)

$$S_{\perp} = \frac{S_1 k f_1 + S_2 k f_2}{k f_1 + k f_2} \text{ (series model, lower limit)}$$

(4)

and the total electrical conductivity ($\sigma$) should be a consequence of the conductivity of the individual phases following

$$f_1 \frac{\sigma_1 - \sigma_e}{\sigma_1 + 2\sigma_e} + f_2 \frac{\sigma_2 - \sigma_e}{\sigma_2 + 2\sigma_e} = 0 \text{ (EMT model)}$$

(5)

$$f_1 \frac{\left( \sigma_1 \right)^{1/t} - \left( \sigma_1 \right)^{1/t}}{\left( \sigma_1 \right)^{1/t} + A \left( \sigma_1 \right)^{1/t}} + f_2 \frac{\left( \sigma_2 \right)^{1/t} - \left( \sigma_2 \right)^{1/t}}{\left( \sigma_2 \right)^{1/t} + A \left( \sigma_2 \right)^{1/t}} = 0 \text{ (GEMT model)}$$

(6)

$$\sigma_{||} = \sigma_1 f_1 + \sigma_2 f_2 \text{ (parallel model, upper limit)}$$

(7)

$$\sigma_{\perp} = \frac{\sigma_1 \sigma_2}{\sigma_1 f_1 + \sigma_2 f_2} \text{ (series model, lower limit)}$$

(8)
where \( f \) is the volume fraction and \( k \) is the total thermal conductivity of the respective constituent phase, \( A \) is a constant that depends on the actual percolation threshold \( \varphi_c \) (of phase 2 in phase 1) through the equation \( A = (1 - \varphi_c)/\varphi_c \), \( t \) is a constant representing the asymmetry of the microstructure, and the subscripts 1, 2 and \( \parallel \) refer to Bi\(_2\)Te\(_3\), In\(_2\)Te\(_3\) and BTIT, respectively.\(^{37-39}\)

Irrespective of the chosen model, the calculated properties of a composite cannot exceed those of one of the constituents. The two phases in our material are substantially different in their thermoelectric properties. Bi\(_2\)Te\(_3\) with dissolved In is known to be n-type material for In concentrations ranging from 2...6.5 at\%\(^{27,28}\), with a conductivity in the order of \( 10^4 \Omega^{-1}\text{m}^{-1} \). In\(_2\)Te\(_3\) is a p-type material with a very low conductivity in the order of \( 10^{-5} \Omega^{-1}\text{m}^{-1} \). Since the In concentration in the Bi\(_2\)Te\(_3\) layers of BTIT is \( \sim\)3at\%, the experimental room temperature properties values for single phase Bi\(_2\)Te\(_3\), with 3at\%In, i.e. BT-3, are used for the calculation. A Seebeck coefficient of \( \sim\)114\(\mu\text{V K}^{-1}\), an electrical conductivity of \( 33 \times 10^3\text{S m}^{-1}\), and a thermal conductivity of \( 1.36\text{W m}^{-1}\text{K}^{-1}\) are used for the calculation. Since the In\(_2\)Te\(_3\) phase in BTIT samples is plate-like with thicknesses of 100...200 nm, the room temperature thermoelectric properties for In\(_2\)Te\(_3\) are taken from literature on In\(_2\)Te\(_3\) films.\(^{44-46}\) The Seebeck coefficient for In\(_2\)Te\(_3\), is set to 185\(\mu\text{V K}^{-1}\), the electrical conductivity to \( 5.6 \times 10^{-3}\text{S m}^{-1}\), and the thermal conductivity to \( 1.1\text{W m}^{-1}\text{K}^{-1}\).\(^{14,46}\)

When using the EMT or GEMT models to calculate the Seebeck coefficient of BTIT, equations (1) and (2) listed above do not work. The reason is that Bi\(_2\)Te\(_3\) is an n-type material with negative Seebeck coefficient, and In\(_2\)Te\(_3\) is a p-type material with a positive Seebeck coefficient. Considering the opposite contribution of Bi\(_2\)Te\(_3\) and In\(_2\)Te\(_3\) to the total Seebeck coefficient of the composite, the EMT/GEMT models need to be adapted, as shown below:

\[
\frac{k_1}{\varphi_1} - \frac{k_2}{\varphi_2} - f_2 \frac{k_2}{\varphi_1} + \frac{k_1}{\varphi_2} = 0 \quad \text{(EMT model)}
\]

\[
\frac{k_1}{\varphi_1}^{1/\nu} + A \frac{k_2}{\varphi_1}^{1/\nu} = 0 \quad \text{(GEMT model)}
\]

The calculation results for the properties of the BTIT composites at room temperature are plotted in Fig. 4 together with the measured values. In the direction perpendicular to the growth direction, the measured properties of BTIT-7.5 are very close to the calculations with the series model. The electrical conductivity in the direction perpendicular is dominated by In\(_2\)Te\(_3\) phase, see eq. (8), i.e. \( \sigma_\perp \approx \sigma_{\text{In}_2\text{Te}_3} \). BTIT-7.5 exhibits such a low electrical conductivity in the direction perpendicular to the growth direction (Fig. 3(a)). Due to the anisotropic microstructure, the transport properties along the growth direction should follow the parallel model and thus be dominated by the properties of Bi\(_2\)Te\(_3\), see eq (7), i.e. \( \sigma_\parallel \approx \sigma_{\text{Bi}_2\text{Te}_3} \) and eq. (3) \( S_\parallel \approx S_{\text{Bi}_2\text{Te}_3} \). However, the experimentally measured thermoelectric properties in the parallel direction (both \( \sigma_\parallel \) and \( S_\parallel \)) of BTIT-7.5 divert drastically from the calculated values. The measured \( S_\parallel \) values are close to the values calculated with the GEMT model (\( A = 1, t = 2 \)). All models suggest a decreasing \( \sigma_\parallel \) with increasing volume fraction of In\(_2\)Te\(_3\). However, the large difference between the calculated \( \sigma_\parallel \) and the measured \( \sigma_\parallel \) suggest that the Bi\(_2\)Te\(_3\)/In\(_2\)Te\(_3\) interfaces influence the thermoelectric properties in a more complex manner.

**Tuning of interface density in Bi\(_2\)Te\(_3\)/In\(_2\)Te\(_3\) via solid state phase transformation.** To get deeper insight into the effect of the Bi\(_2\)Te\(_3\)/In\(_2\)Te\(_3\) interfaces on the transport behavior of BTIT, the interface density in

Figure 4. Calculated dependence of room temperature (a) Seebeck coefficient and (b) electrical conductivity of BTIT on the volume fraction of In\(_2\)Te\(_3\).
BTIT was varied in a controlled way. Since the thermoelectric properties of Bi$_2$Te$_3$ are very sensitive to the composition, the Bi$_2$Te$_3$/In$_2$Te$_3$ interface density was modified by changing the supersaturation of the parent (Bi, In)$_2$Te$_3$ phase while maintaining the same annealing temperature, i.e. the same composition of each constituent phase. Figure 5 shows cross section microstructures of (Bi, In)$_2$Te$_3$ (4, 6, and 7.5 at% In) after precipitation annealing at 400 °C. For avoiding projection effects in the lamellar spacing measurements, microstructural analysis was performed in cross sections of the samples. The grey phase in Fig. 5 represents the (Bi, In)$_2$Te$_3$ phase with an identical In concentration of ~3 at% for all samples, and the black phase represents the In$_2$Te$_3$ phase with negligible Bi content. The composition distribution in each phase was determined in the TEM, as shown in Fig. 6. In each phase, the concentration of each element is homogeneous within the measurement scatter of EDX. Interestingly, a slight but significant variation in the Te concentration across Bi$_2$Te$_3$/In$_2$Te$_3$ interfaces is observed. The concentration of Te in the (Bi, In)$_2$Te$_3$ phase is a little higher than 60 at%, while the Te concentration in the In$_2$Te$_3$ phase is somewhat lower than 60 at%. Inhomogeneity and lattice misfit at heterophase interfaces have been demonstrated to cause transport processes across the interface and hence change the thermoelectric properties.

Figure 5. Microstructure of BTIT-c (c = 4, 6, 7.5 at% In), with the dark phase representing In$_2$Te$_3$, and the grey phase representing (Bi,In)$_2$Te$_3$ (~3at%In); (a) 4 at%In; (b) 6 at%In; (c) 7.5 at%In.

Figure 6. EDX composition analysis in the TEM across (Bi, In)$_2$Te$_3$ and In$_2$Te$_3$ layers; the HRTEM image in the inset illustrates the sharp (Bi, In)$_2$Te$_3$/In$_2$Te$_3$ interface.
performance. A high resolution TEM image of a Bi$_2$Te$_3$/In$_2$Te$_3$ interface is also shown in Fig. 6. Together with the EDX analysis, this confirms that there is no diffusion layer and that the Bi$_2$Te$_3$/In$_2$Te$_3$ interface is sharp and coherent. As can be clearly seen from Fig. 5, the volume fraction of In$_2$Te$_3$ increases and the lamellar spacing decreases with increasing In concentration. Simultaneously, the length of the In$_2$Te$_3$ plates increases. For all samples, the thickness of the In$_2$Te$_3$ plates is similar, in the order of ~100 to 200 nm. For BTIT-6, the lamellar spacing ranges from ~500 nm to ~3.5 μm, with the majority of lamellar spacings being in the size class ~1.2 μm. For BTIT-7.5, the lamellar spacing is smaller, ranging from ~200 nm to ~2 μm, and most of the lamellae have a spacing below 1 μm. For verifying that 6 days are enough for reaching thermodynamic equilibrium at 400°C, we compared the measured lamellar spacing values with the diffusion length, \( \delta = \sqrt{2D \tau} \), where \( D \) is the diffusion coefficient and \( \tau \) is the involved time scale. \( D \) is of the order of \( 10^{-12} \text{ m}^2 \text{s}^{-1} \), as found in previous work on the diffusion of metallic elements in Bi$_2$Te$_3$47–49. The calculated diffusion length in 6 days is 1440 μm, which is much larger than the observed spacing between neighboring In$_2$Te$_3$ precipitates for all BTIT samples. This in turn confirms that the equilibrium state at 400°C is reached. With the In concentration increasing from 4 to 7.5 at%, the volume fraction of In$_2$Te$_3$ after annealing was measured as 1.5 ± 0.5%, 7.3 ± 1.5% and 13.5 ± 1.5%, respectively. These values are consistent with those calculated by the lever rule based on the solubility of In in Bi$_2$Te$_3$ (3 at% at 400°C) and negligible solubility of Bi in In$_2$Te$_3$. In the present work, it can be seen from Fig. 5 that the increase in In$_2$Te$_3$ volume fraction mainly comes from the decrease of lamellar spacing rather than the increase in thickness of In$_2$Te$_3$.

**Correlation between the interface density and thermoelectric properties of Bi$_2$Te$_3$/In$_2$Te$_3$.** To get deeper insight into the physical transport mechanisms, the thermoelectric properties of the solid solution sample (BT-3 at%In) and the composite samples (BTIT-4, -6, -7.5 at%In) were characterized in the temperature range from room temperature to 300°C, see Fig. 7. Since the thermoelectric properties perpendicular to the growth direction are expected to be technologically uninteresting, as shown in Figs 3 and 4, only the properties parallel to the sample axis were studied. All samples exhibit a similar temperature dependence trend of the thermoelectric properties. Negative values of the Seebeck coefficient throughout the whole measured temperature range are found for all samples (Fig. 7(a)), indicating n-type transport behavior. With increasing temperature from room temperature to 300°C, the absolute value of the Seebeck coefficient \( |S| \) decreases, indicating mixed conduction or bipolar transport behavior29. The BT-3 sample shows the highest \( |S| \), but the lowest \( \sigma \) of all samples. With increasing volume fraction of In$_2$Te$_3$ and decreasing lamellar spacing, \( |S| \) decreases while \( \sigma \) increases. Since the conductivity of In$_2$Te$_3$ is much smaller than that of Bi$_2$Te$_3$, the increase of \( \sigma \) with increasing In$_2$Te$_3$ volume fraction is not straightforward to understand.

For qualitatively analyzing the possible reason for the increasing \( \sigma \), Hall tests at room temperature were performed on all the samples. The measured Hall coefficients of BTIT at room temperature are given in Table 1. The carrier concentration can be calculated from \( R_H \) via the equation \( R_H = A/ne \), where \( A \) is related to the anisotropy factor of the effective carrier mass and the Fermi energy levels50. However, the microstructure/property anisotropy and the existence of two types of material, p-type In$_2$Te$_3$ and n-type Bi$_2$Te$_3$ (i.e. the coexistence of both holes and electrons) make the accurate determination of \( A \) not straightforward. Due to a lack of detailed information, an approximation, \( R_H = 1/ne \), is used in our present work. We get qualitative information concerning the increase of the electrical conductivity with increasing BT/IT interface density, as listed in Table 1. The measured carrier concentration does not differ much between the samples. This indicates that the contribution of In$_2$Te$_3$ and the BT/IT interfaces to the carrier concentration is negligible. This is partly due to the very low room temperature hole concentration of In$_2$Te$_3$, 7.8 × 10^16 cm$^{-3}$, which is nearly 10 orders of magnitude lower than that of BT-3In. The increasing \( \sigma \) of BTIT with increasing In$_2$Te$_3$ volume fraction mainly comes from the increasing carrier mobility.

The total thermal conductivity shows a non-uniform trend: BTIT-4 and BTIT-6 exhibit a lower \( k_L \) than BT-3, and BTIT-7.5 exhibits a comparable \( k_L \) as BT-3, as shown in Fig. 7(d). After subtracting the electronic contribution, the thermal conductivity shows a clear trend in Fig. 7(e) – it distinctly decreases with increasing In$_2$Te$_3$ fraction. The remaining thermal conductivity after subtracting the electronic contribution contains the lattice thermal conductivity and the bipolar contribution. The pure lattice thermal conductivity should decrease with increasing temperature due to phonon-phonon interaction54. In contrast, the bipolar contribution increases due to the increasing number of electron/hole pairs. Thus, all samples show a significant bipolar contribution to the thermal conductivity (Fig. 7(e)), in agreement with the mixed conduction behavior of the Seebeck coefficient and the electrical conductivity. Nevertheless, \( k_L \) decreases with increasing In$_2$Te$_3$ fraction, and for BTIT-7.5 the overall temperature dependence is inverted from increasing to decreasing (Fig. 7(e)). This indicates the suppression of the bipolar contribution by a decreasing BT/IT lamellar spacing. Bipolar transport contributions are counterproductive for the thermoelectric properties, because they do not only increase the thermal conductivity, but also lower the Seebeck coefficient. Thus, BTIT-7.5 with the lowest bipolar contribution has the highest \( zT \) value, see Fig. 7(f).

**n-Bi$_2$Te$_3$/p-In$_2$Te$_3$ hetero-interface effects.** The enhanced \( zT \) values of BTIT are mainly attributed to the increased electrical conductivity and the resulting higher power factor. Bergman and Levy51 theoretically predicted the possibility of higher thermoelectric power factors than the power factors of the pure components in a composite consisting of two phases, especially for a parallel slabs microstructure. They pointed out that the \( zT \) value of a composite can never be beyond the highest value of one of the constituent components51. An enhancement of both power factor and thermoelectric figure of merit beyond those of the components in a two-phase composite was first experimentally found in SiGe-Si nanocomposites52,53. This enhancement is mainly attributed to a higher carrier mobility, which in turn is interpreted to be induced by inhomogeneous doping only in Si nanograins instead of uniform doping in both components52. Selective doping will certainly contribute to the
band engineering at the interface and may lead to charge transfer from one phase to the other one, which in turn can enhance \( zT \).

In the present work, the enhanced electrical conductivity (as a consequence of the higher carrier mobility, see Table 1) is the main reason for enhanced power factor and \( zT \). As for SiGe-Si\(^{32,33}\), band alignment and charge transfer across Bi\(_2\)Te\(_3\)/In\(_2\)Te\(_3\) interface was considered to be one of the possible reasons. A simple schematic illustration of the band diagram for an n-type (Bi,In)\(_2\)Te\(_3\)/p-In\(_2\)Te\(_3\) interface is proposed in the present work, see Fig. 8, in which the maximum work function for In\(_2\)Te\(_3\) and the minimum work function for Bi\(_2\)Te\(_3\) are used. For p-type In\(_2\)Te\(_3\), an electron affinity of 3.85 eV and a band gap of \( \sim 1.12 \) eV have been reported\(^{34}\). It is not straightforward

\[ \text{Table 1. Carrier concentration (n) and mobility (\( \mu \)) of the samples at room temperature (295 K).} \]

| Sample    | \( R_n (10^{-5} \text{m}^2 \text{A}^{-1} \text{s}^{-1}) \) | \( \sigma (10^5 \text{S m}^{-1}) \) | \( n (10^{19} \text{cm}^{-3}) \) | \( \mu (\text{cm}^2 \text{V}^{-1} \text{s}^{-1}) \) |
|-----------|---------------------------------------------------|----------------------------------|-------------------------------|----------------------------------|
| BT-3In    | \(-0.52\)                                         | 33                               | 1.20                          | 172                              |
| BTIT-4In  | \(-0.59\)                                         | 62.5                             | 1.12                          | 368                              |
| BTIT-6In  | \(-0.63\)                                         | 92                               | 1.0                           | 580                              |
| BTIT-7.5In| \(-0.55\)                                         | 175                              | 1.13                          | 963                              |

\[ \text{Figure 7. Temperature dependence of Seebeck coefficient } S (a), \text{ electrical conductivity } \sigma (b), \text{ power factor (c), thermal conductivity } k_{\text{tot}} (d), k_{\text{tot}} - k_{LB} (e), \text{ and } zT (f) \text{ of BT-3 and BTIT-4, -6, -7.5.} \]
to determine the Fermi level of In$_2$Te$_3$ in BTIT in the present work. In view of the p-type behavior, we assume a Fermi level close to the valence band. Then the work function ($W_F$) for In$_2$Te$_3$ ranges from 4.41 to 4.97 eV. As to n-type Bi$_2$Te$_3$ with 3 at% In, so far the band structure is not known and cannot be determined on the basis of the results in our present work. The recently reported band gap value, 0.08 eV, for Bi$_2$Te$_3$ with 4 at% In$^{55}$ was used in the present work. We assumed a same electron affinity (5.17 eV$^{56}$) as Bi$_2$Te$_3$. Considering the n-type transport behavior of (Bi,In)$_2$Te$_3$, a Fermi level at the same position of the conduction band is used. Even though the Fermi level of In$_2$Te$_3$ is higher than that of (Bi,In)$_2$Te$_3$ at the (Bi,In)$_2$Te$_3$/In$_2$Te$_3$ interface, the electrons tend to flow from In$_2$Te$_3$ to (Bi,In)$_2$Te$_3$ to balance the Fermi level at the contact, which in turns yields band bending. (Bi,In)$_2$Te$_3$ can then be expected to act as electron acceptor, and the formation of an electron accumulation layer close to the interface to In$_2$Te$_3$ can be safely assumed.

The Fermi levels of the two phases and the band offsets are crucial in the band alignment at the interface and the resulting charge transfer between the two phases. Experimentally, alloying/doping in each phase can induce a change of the Fermi level of each phase, and a change in the resulting band offset between the two phases. Moreover, thinking of the difference in the crystal structures of two phases, the lattice misfit and the resulting strain at the two-phase interface can affect the band alignment and then resulting charge transfer across the interface. These factors will lead to different band alignments and final properties$^{53}$. Only suitable doping can lead to good band alignment to ensure the desired charge transfer from one phase to another$^{53,57}$, which is an opportunity for enhanced $zT$ values.

In the present case, electron transfer across the BT/IT interface could lead to a change in the thermoelectric properties of the two phases, similarly as for the SiGe-Si nanocomposites$^{52,53}$. Calculations with the properties of the single separated phases (Bi,In)$_2$Te$_3$ and In$_2$Te$_3$ would necessarily lead to a deviation from the experimental data. With a modified charge distribution in the two components and thus a different electrical resistance of each phase, the enhancement of the conductivity of BTIT could probably be explained using the model in ref. 52. Our own simulation calculations suggest an accumulation layer that can also be regarded as a highly conductive third phase. Then, a three-phase model is more realistic for predicting the final properties. In this case, the highly conductive third phase leads to the increasing electrical conductivity with increasing Bi$_2$Te$_3$/In$_2$Te$_3$ interface density.

Band alignment at hetero-interfaces is regarded as one of the main reasons for enhanced electrical conductivity in two-phase nanocomposites, for example SiGe-Si$^{52,53}$ and ZnO:Al – ZnS thin films$^{58}$. As shown in Fig. 8, band bending at the Bi$_2$Te$_3$/In$_2$Te$_3$ interface may shift the Fermi level closer to the conduction band or even below the Fermi level (metal-like behavior). Such a metal-like surface state of Bi$_2$Te$_3$ may also be a possible reason for the increase of electrical conductivity with increasing BT/IT interface density. Together with the metal-like behavior at the BT/IT interfaces, a metal-like surface state of Bi$_2$Te$_3$ as a prominent example for a topological insulator$^{59,60}$.
may be another possible reason for the increase of electrical conductivity with increasing BT/IT interface density. Besides, In$_2$Te$_3$ was reported to exhibit a high room temperature carrier mobility, particularly a hole mobility of 1820 cm$^2$V$^{-1}$s$^{-1}$ and electron mobility of 2890 cm$^2$V$^{-1}$s$^{-1}$. Previous work on Cu$_2$Se-CuAgSe$_x$ indicates that the carrier mobility in each constituent phase plays a critical role for the electrical conductivity of the composite, especially when there is a big difference in the carrier mobility values between the phases.

Tentative Density Functional Theory (DFT) calculations with VASP (see e.g. ref. 62,63) using the Perdew-Burke-Ernzerhof exchange-correlation functional for a supercell built to reproduce the coherent BT/IT interface also predicted the possibility of a metal-like interface state. A crystallographic orientation between Bi$_2$Te$_3$ and In$_2$Te$_3$, of $\langle 2211 \rangle$ $\langle 3321 \rangle$ $< 1100 >$ $< 1100 >$ and $\langle 1111 \rangle$ $\langle 0001 \rangle$ and an adjusted band offset as in Fig. 8 were used. Metallic states localized on the Te atoms and on the neighboring In and Bi planes directly at the interface were observed. Generally, an extremely high carrier mobility in the vicinity of the interface is expected. The metal-like layer in the present work extends over a few atomic layers, which is not straightforward to detect experimentally. Metal-like conductivity originating from band alignment and charge transfer through the interface has been found in other systems, for example in LaAlO$_3$/SrTiO$_3$.

The enhanced electrical conductivity is likely to be due to band alignment and charge transfer across Bi$_2$Te$_3$/In$_2$Te$_3$ interface. The experimental strategy is promising to lead to pronounced high $\tau T$ values, if the interface of the experiments is exploited in combination with doping.

Conclusions

Metallurgical production methods exhibit high potential for generating high quality thermoelectric materials. In the present work, seeding zone melting and solid state precipitation were applied to produce n-type Bi$_2$Te$_3$-In$_2$Te$_3$ layered composites of pronounced anisotropy in structure and thermoelectric properties. The spacing of the Bi$_2$Te$_3$/In$_2$Te$_3$ layers and density of Bi$_2$Te$_3$/In$_2$Te$_3$ interfaces was tuned via the initial composition of the solid solution samples. Correlations between thermoelectric performance and microstructure were established. With increasing interface density, an increase in electrical conductivity and a decrease of bipolar transport properties lead to a substantial enhancement of $\tau T$. The enhanced electrical conductivity is likely to be due to band alignment and charge transfer across Bi$_2$Te$_3$/In$_2$Te$_3$ interface. The experimental strategy is promising to lead to pronounced high $\tau T$ values, if the interface of the experiments is exploited in combination with doping.

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Author Contributions
Markus Rettenmayr and Dongmei Liu conceived and initiated the study. Dongmei Liu and Xinzhong Li prepared all the samples and measured all the thermoelectric data. Roland Schmechel provided access to the temperature dependent thermoelectric characterization facilities. Pedro de Castro Borlido and Silvana Botti performed the DFT calculations. All the authors analyzed the data and wrote the manuscript.

Additional Information
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