ABSTRACT  In this study, a memristor-based 2-DOF PI controller (2-DOF Mem-PI) was designed for the temperature profile tracking control of a model of heat flow experiment (HFE) setup. A simulation study is presented in which the performance of the designed controller is compared with a standard 2-DOF PI controller. Compared to 1-DOF control structures, 2-DOF controllers that include an extra adjustable parameter perform better in terms of response to disturbances and improving the transient response of the system. In addition, memristor-based controllers (Mem-PI and 2-DOF Mem-PI) and standard controllers (PI and 2-DOF PI) were compared and it was determined that because of the variable memristance value, the control structures containing memristors showed an adaptive feature. The simulation results demonstrated the success of the proposed controller in temperature profile reference tracking and showed the memristor to be applicable in nonlinear control structures.

INDEX TERMS  2-DOF PI controller, memristor, memristor-based controller, temperature profile control.

I. INTRODUCTION
Temperature and temperature control are important factors in different classes and processes of industrial production that should be taken into consideration, especially in terms of the safety of the production facility and product quality [1]. In practice, tracking the reference temperature profile, keeping the temperature at a set point, and controlling the distribution of the atmospheric temperature are the most common temperature control tasks encountered. Temperature reference tracking control is also important, as it requires flexible, stable, and adaptable control because of various control theory issues such as the operating environment, varying time constants, and disturbing external factors that can be seen in real systems. Ahn et al. introduced a new analytical tuning method for the fractional-order integral derivative (FO-ID) $I^{\alpha}D^{\beta}$ controller and applied it to analyze the heat flow in the obtained controller heat flow experiment (HFE) module. In addition, they presented comprehensive simulation results to demonstrate the practical and simple nature of the proposed new tuning rules [2]. Al-Saggaf et al. proposed a new model-based analytical design for fractional-order controllers. The efficiency and performance of this proposed method was demonstrated by simulations and on a heat flow platform experimentally [3]. In another study, a control design approach for input saturated linear systems was presented. Two practical applications in both a heat flow system and a liquid flow system were presented to verify the effectiveness of the proposed control design method. The effectiveness of the proposed approach was demonstrated by experimental results [4]. Hernandez-Perez et al. investigated the stabilization problem of the class of highly unstable time-delayed systems. In the control structure they proposed, a new control law called the PIf controller, consisting of a standard PI controller and a first-order low-pass filter, was used. The performance of the proposed controller was tested in a thermal flow assembly equipped with a time delay and a recycling path, and it was reported that an adequate performance had been achieved [5]. In order to obtain a generally acceptable process response, Nath et al. proposed
an automatic tuning scheme for the traditional internal model control - PID (IMC-PID) controller by changing the single setting parameter depending on the latest process operating conditions [6]. They also demonstrated the superiority of the proposed fuzzy rule-based automatic adjustment scheme with the results of real-time experiments on level and temperature control processes.

The proportional-integral / proportional-integral-derivative (PI/PI-D) controller structure is a control mechanism that has a wide range of uses such as in electronic devices, mechanical devices, and pneumatic systems, and for process control in different fields of industry [7], [8], [9], [10]. In addition, the advantages of the two-degree-of-freedom (2-DOF) control structure over the one-degree-of-freedom (1-DOF) control structure were stated by Horowitz [11]. The 2-DOF controller structure was developed for situations where a 1-DOF controller structure is insufficient. By adding the $\beta$ parameter to the controller structure, better performance is provided in terms of maintaining the output of the controller to disturbances and improving the transient response of the system. In recent years, there have been many studies based on different tuning and optimization algorithms proposed for 2-DOF control structures [12], [13], [14], [15], [16].

The memristor was first described by L. Chua in 1971 as a memory resistor and was produced by HP researchers in 2008 [17], [18]. The physically realized memristor quickly managed to attract the attention of researchers, but its application as a discrete circuit element has been delayed. However, researchers have realized many models and circuits by working on circuits that act as memristors [19], [20], [21], [22], [23], [24]. Recently, testing of the memristor has begun in the control field, and memristor-based controllers have been suggested by researchers [25], [26], [27], [28], [29], [30], [31], [32]. In applications such as variable gain and automatic gain control, the TiO$_2$ memristor model was used as the memristor model due to the simplified expressions and the same ideal physical behavior [33], [34], [35]. In particular, once controllers designed using memristor emulator circuits increase and production has begun, their use will be possible in the future.

In previous studies, unlike this study, 1-dof PI controller with memristor-based integrator circuit was designed and applied to the heat flow system [28]. In [30], a PD control structure was obtained with a memristor derivative circuit and applied to the ball and beam system. In [31], a sliding mode control approach was obtained by using a memristor-based derivative circuit and simulation results for speed control of BLDC motor were presented.

In this study, a novel memristor-based 2-DOF PI controller structure was proposed and a comparison was made between standard PI, standard 2-DOF PI, 1-DOF mem-PI and 2-DOF mem-PI controllers. The simulation model of Quanser’s heat flow experimental (HFE) setup was used to test the temperature profile tracking performance of the proposed controller and simulation results were presented.
indicates high resistance states, and D

The relationship between voltage and current recommended by the HP research group for a TiO2 memristor [18] is:

\[ V(t) = M_i(t) = \left[ R_{ON} \omega(t) \frac{D}{D} + R_{OFF} \left( 1 - \omega(t) \frac{D}{D} \right) \right] i(t) \]  

where \( \omega \) is the state variable of the device, \( M \) represents the memristance, \( R_{ON} \) indicates low resistance states, \( R_{OFF} \) indicates high resistance states, and \( D \) represent the total length of the TiO2 memristor, respectively.

The memristance value, which is directly dependent on the change of the \( \omega \) value, is defined as:

\[ \frac{d\omega(t)}{dt} = \mu_v \frac{R_{ON}}{D} i(t) \]  

where \( \mu_v \) is the mobility of the memristor [18]. The physical structure of the memristor is given in Figure 2.

IV. CONTROLLER DESIGN

A. 2-DOF PI CONTROLLER

Using the temperature profile tracking error based on the current temperature \( T \) and the desired temperature value \( T_d \), an error signal can be defined for the controller design as follows:

\[ e(t) = T_d(t) - T(t) \]  

The block diagram of the 2-DOF PI-based closed-loop control function for temperature profile tracking in the HFE simulation model is given in Figure 3.

B. MEMRISTOR-BASED INTEGRATOR

If this equation is rearranged,

\[ u(s) = K_p \left[ \beta T_d(s) - T(s) + \frac{1}{T_is} \left[ T_d(s) - T(s) \right] \right] \]  

is obtained, where \( e(s) \) is the error signal specified in (6).

C. MEMRISTOR-BASED 2-DOF PI CONTROLLER

If the integration process in the 2-DOF PI control structure given in Figure 3 is carried out with the memristor-based integrator circuit given in Figure 4, a memristor-based 2-DOF PI controller structure is obtained. A block diagram of the temperature profile tracking control of the HFE with the memristor-based 2-DOF PI (2-DOF Mem-PI) approach is given in Figure 5.

Using (4), (6), (9) and (10), the control signal \( u(s) \) in the proposed control structure can be written as follows:

\[ u(s) = K_p \left[ \beta T_d(s) - T(s) + \frac{1}{MC} \int_0^t e(\tau) \, d\tau \right] \]  

where \( C \) is capacitance and \( M \) represents the memristance.
\[ u(s) = K_P \left[ \beta T_d(s) - T(s) \right] \]

\[ + \frac{1}{R_{ON} \frac{d(t)}{dt} + R_{OFF} \left( 1 - \frac{d(t)}{dt} \right)} Cs \]

\[ \times \left\{ T_d(s) - T(s) \right\} \]

(12)

D. Determination of Controller Parameters

Parameters in the proposed control structure were determined using the multiple dominant pole method (MDPM) as in the study presented by Viteckova and Vitecek [40]. The definition of the HFE as a first-order plus time-delay (FOPTD) plant in the Quanser instruction manual is as follows [36]:

\[ Y(s) = \frac{K}{\tau s + 1} U(s) \]  

(13)

By solving the system of equations given in (14), adjustable controller parameters and multiple dominant poles \( \hat{s}_{p+1} \) can be obtained. The FOPTD system and the quasi-polynomial characteristic of the standard PI controller described in [38] are given in (15) and (16), respectively.

\[ \frac{d^jN(s)}{ds^j} = 0 \quad \text{for} \quad j = 0, 1, \ldots p \]  

(14)

\[ G(s) = \frac{K}{Ts + 1} e^{-Ls} \]  

(15)

\[ N(s) = \left( T_s^2 + s \right) e^{Ls} + KK_p \left( s + \frac{1}{T_I} \right) \]  

(16)

where \( p \) is the number of adjustable controller parameters, \( K \) is plant gain, \( L \) is time delay, \( K_P \) is controller gain, \( T_I \) is integral time, and \( N(s) \) is the quasipolynomial characteristic of the control system. The form of the standard PI controller adjusted with MDPM and the approximate control system transfer functions to be designed for a plant expressed as in (16) is given in (17) [40].

\[ C(s) = \frac{T_I s + 1}{\left( \frac{T_I}{|s|} s + 1 \right)} e^{-Ls} \]  

(17)

In Table-1 presented in [40], in light of (15) and (17), it is stated that for \( p = 2 \), two adjustable controller parameters \( \hat{K}_p \) and \( \hat{T}_I \) and triple dominant pole \( \hat{s}_3 \) values can be obtained as indicated below:

\[ \hat{s}_3 = -\frac{2}{L} - \frac{1}{LT} + \sqrt{\frac{2}{L^2} + \frac{1}{4T^2}} \]  

(18)

\[ \hat{K}_p = -\frac{1}{K} \left[ LT \hat{s}_3^3 + (2T + L) \hat{s}_3 + 1 \right] e^{L\hat{s}_3} \]  

(19)

\[ \hat{T}_I = -\frac{LT \hat{s}_3^3 + (2T + L) \hat{s}_3 + 1}{LT \hat{s}_3 + (2T + L) \hat{s}_3^2} \]  

(20)

\[ \hat{\beta} = \min \left\{ \frac{1}{\hat{T}_I \hat{s}_3}, 1 \right\} \]  

(21)

In the Quanser instruction manual, the values determined for the step response were \( K = 10 \), \( T = 5 \) s and \( L = 1 \) [36]. Considering these values, if (18), (19), (20), and (21) are solved, the parameters of the 2-DOF PI controller given in (8) are obtained:

\[ \hat{s}_3 = -0.6823 \quad \hat{K}_p = 0.2112 \]

\[ \hat{T}_I = 3.4668 \quad \hat{\beta} = 0.4228 \]

V. SIMULATION

In this study, the memristor model in the MATLAB (2016a)/Simulink Simscape model library was used. The \( R_{ON} \) and \( R_{OFF} \) resistance values in (4) are used as state-A and state-B resistors in the model parameter given in Figure 6. Considering the memristor model parameters and (10), it was determined that \( MC = T_I = \hat{T}_I \) and hence, \( C = 1.7334 \mu F \). The designed 2-DOF mem-PI controllers and the standard 2-DOF PI controllers were compared in terms of temperature profile tracking performance and the results are given in Figures 7-12. The reference temperature profile signal includes sudden and smooth changes.

In Figure 7, both controllers are seen to perform similarly in terms of time to reach the reference. However, the 2-DOF Mem-PI controller was more successful than the 2-DOF PI controller in terms of eliminating the error early on.

Figure 8 gives the control signals of the 2-DOF Mem-PI controller and the 2-DOF PI controller. Both control signals have a similar form, but the 2-DOF Mem-PI control signal is smoother than that of the 2-DOF PI.

Considering the previous study of [28], it was thought to examine the relationship between memristor-based controllers and classical controllers, and for this purpose, the temperature control of HFE for the same reference signal was tested with the standard 1-DOF PI, 1-DOF Mem-PI, standard 2-DOF PI, and 2-DOF Mem-PI controllers. The reference temperature profile tracking simulation results of these four controllers are given in Figure 9.
The graphic in Figure 9 shows that, regardless of whether the controller was standard or memristor-based, the 2-DOF control structures reached the reference earlier than the 1-DOF control structures. On the other hand, the memristor-based control structures (Mem-PI and 2-DOF Mem-PI) eliminated the error more quickly than the standard control structures (PI and 2-DOF PI). This is more clearly seen where the error signals are given in Figure 10.

Figure 11 gives the simulation results of the change of the memristance ($M$) value under the adjusted parameter values of the memristor used in the simulation study. During sudden
VI. DISCUSSIONS AND CONCLUSION
In practice, many control systems have a time delay within the closed loop of the system, which affects the stability of the system. The time delay for the heat flow system given in (15) was represented by $e^{-Ls}$, where $L$ is the time delay. One of the valid methods used to determine the effect of time delay on the relative stability of the feedback system is the Nyquist criterion. The Nyquist criterion remains valid for a time-delayed system, as the factor $e^{-Ls}$, which adds a phase shift to the frequency response without changing the magnitude curve, does not introduce any additional poles or zeros in the contour. Also, a time delay $e^{-Ls}$ introduces an additional phase delay in the feedback system and makes the system less stable. In the stability analysis of such systems, most analytical tools are considered and the transfer functions of the systems are defined by rational functions or a finite set of ordinary constant coefficient differential equations. The Padé approximation can be used to obtain a rational function approximation of the time delay. The Padé approximation uses a series expansion of the transcendental function $e^{-Ls}$ and matches as many coefficients as possible with a series expansion of a rational function of specified order. In practical applications of heat flow systems, time delay occurs. However, dead time and time delay are ignored in the model used in this study. In addition, stability analysis of the proposed controller was not performed.

In this study, 2-DOF PI controllers based on memristors were tested via HFE temperature profile tracking control and simulation results were presented. It was demonstrated that the memristor, known as the missing circuit element, can be applied in 2-DOF control structures. Results of this simulation study showed that the 2-DOF Mem-PI controller was successful in the temperature profile tracking control of the HFE. When Figure 9 was examined, it was observed that no overshoot occurred in all the compared controllers. Additionally, the 2-DOF control structures were faster in terms of reaching the reference compared to the 1-DOF control structures because of the extra adjustable parameter. As can be seen in Figure 9, 2-DOF control structures reached the reference approximately 1 second earlier than 1-DOF control structures. On the other hand, because they contained an extra parameter, the 2-DOF control structures were faster in eliminating error compared to the 1-DOF control structures. Figure 10 shows that the error elimination time of the 2-DOF PI controller is approximately 46% lower than the 1-DOF PI controller. Furthermore, the Mem-PI and 2-DOF Mem-PI controllers designed using a memristor were successful in eliminating error faster than the PI and 2-DOF PI standard controllers because of their variable memristance value. Depending on the voltage change of the error signal at the controller input, the resistance value of the memristor takes a value between the $R_{ON}$ and $R_{OFF}$ values. Therefore, an adaptation effect occurs in the system.

Future studies are planned to demonstrate the effectiveness of this simulation study, to test the proposed controller structure on a real system with a dead-time included system model, and to analyze the stability, sensitivity and frequency stability of the system.

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KAMIL ORMAN received the B.Sc. degree in electrical and electronics engineering from Selçuk University, in 1996, and the M.Sc. and Ph.D. degrees in electrical and electronics engineering from Atatürk University, in 2008 and 2018, respectively. He is currently working as an Assistant Professor with the Computer Engineering Department, Erzincan Binali Yıldırım University. His main research interests include control systems, nonlinear control, algorithms, robotic systems, and unmanned vehicles.

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