Constraining Galaxy Haloes from the Dispersion and Scattering of Fast Radio Bursts and Pulsars

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ABSTRACT

Fast radio bursts (FRBs) can be scattered by ionized gas in their local environments, host galaxies, intervening galaxies along their lines-of-sight, the intergalactic medium, and the Milky Way. The relative contributions of these different media depend on their geometric configuration and the internal properties of the gas. When these relative contributions are well understood, FRB scattering is a powerful probe of density fluctuations along the line-of-sight. The precise scattering measurements for FRB 121102 and FRB 180916 allow us to place an upper limit on the amount of scattering contributed by the Milky Way halo to these FRBs. The scattering time \( \tau \propto (\tilde{F} \times \text{DM}^2) A_\tau \), where DM is the dispersion measure, \( \tilde{F} \) quantifies electron density variations with \( \tilde{F} = 0 \) for a smooth medium, and the dimensionless constant \( A_\tau \) quantifies the difference between the mean scattering delay and the \( 1/e \) scattering time typically measured. A likelihood analysis of the observed scattering and halo DM constraints finds that \( \tilde{F} \) is at least an order of magnitude smaller in the halo than in the Galactic disk. The maximum pulse broadening from the halo is \( \tau \lesssim 12 \mu \text{s} \) at 1 GHz. We compare our analysis of the Milky Way halo with other galaxy haloes by placing limits on the scattering contributions from haloes intersecting the lines-of-sight to FRB 181112 and FRB 191108. Our results are consistent with haloes making negligible or very small contributions to the scattering times of these FRBs.

Keywords: galaxy: haloes — Galaxy: disk — ISM: structure — scattering — turbulence — stars: neutron

1. INTRODUCTION

Fast radio bursts (FRBs) propagate from as far as \( \sim \)Gpc distances through their local environments, the interstellar medium (ISM) and circumgalactic medium (CGM) of their host galaxy, the intergalactic medium (IGM) and any intervening galaxies or galaxy haloes, the halo and ISM of the Milky Way, and finally through the interplanetary medium (IPM) of our Solar System before arriving at the detector. Along their journey they experience dispersion and multi-path propagation from free electrons along the line-of-sight (LoS). The dispersion measure DM = \( \int n_e dl / (1+z) \), where \( n_e \) is the electron density and \( z \) is the redshift. Most FRBs are extragalactic and have DM much larger than the expected contribution from our Galaxy, with the single possible exception being the Galactic magnetar source SGR 1935+2154 (Bochenek et al. 2020; The CHIME/FRB Collaboration et al. 2020). Many studies of FRB propagation have focused on the “DM budget,” constraining the relative contributions of intervening media to the total observed FRB DM, with particular attention paid to determining the DM contribution of the IGM, which in principle can be used to estimate the distance to an FRB without a redshift (e.g., Dolag et al. 2015; Pol et al. 2019). For FRBs with redshifts the subsequent intergalactic DM(\( z \)) relationship can be used to measure the cosmic baryon density, as was first empirically demonstrated by Macquart et al. (2020). Arguably the least constrained DM contribution to FRBs is that of their host galaxies, which has been estimated in only one case using Balmer line observations (Tendulkar et al. 2017).

Understanding FRB propagation requires study of not just dispersion but also scattering. Bursts propagate along multiple ray paths due to electron density fluctuations, which leads to detectable chromatic effects like pulse broadening, scintillation, and angular broadening. These effects are respectively characterized by a temporal delay \( \tau \), frequency bandwidth \( \Delta \nu_d \), and full width at half maximum (FWHM) of the scattered image \( \theta_d \). Scattering effects generally reduce FRB detectability, obscure burst substructure, or produce multiple images of the burst, and may contaminate emission signatures imprinted on the signal at the source (e.g., Cordes et al. 2017; Hessels et al. 2019; Day et al. 2020). On the
other hand, scattering effects can also be used to resolve the emission region of the source (Simard & Ravi 2020) and to constrain properties of the source’s local environment (for a review of FRB scattering see Petroff et al. 2019; Cordes & Chatterjee 2019). Since the relationship between $\tau$ and DM is known for Galactic pulsars (e.g., Ramachandran et al. 1997; Bhat et al. 2004; Krishnakumar et al. 2015; Cordes et al. 2016), it is a promising basis for estimating the DM contributions of FRB host galaxies based on measurements of $\tau$ (Cordes et al., in prep). In order to use scattering measurements for these applications, we need to assess how intervening media contribute to the observed scattering (i.e., a “scattering budget”). To disentangle any scattering effects intrinsic to the host galaxy or intervening galaxies, we need to accurately constrain the scattering contribution of the Milky Way.

Broadly speaking, an FRB will encounter ionized gas in two main structural components of the Milky Way, the Galactic disk and the halo. The Galactic disk consists of both a thin disk, which has a scale height of about 100 pc and contains the spiral arms and most of the Galaxy’s star formation (e.g., Cordes & Lazio 2002), and the thick disk, which has a scale height of about 1.6 kpc and is dominated by the more diffuse, warm ($T \sim 10^4$ K) ionized medium (e.g., Ocker et al. 2020). The halo gas is thought to be dominated by the hot ($T \sim 10^6$ K) ionized medium, and most of this hot gas is contained within 300 kpc of the Galactic center (e.g., Faerman et al. 2017). While the DMs and scattering measurements of Galactic pulsars and pulsars in the Magellanic Clouds predominantly trace plasma in the thin and thick disks, extragalactic sources like FRBs are also sensitive to gas in the halo.

In this paper we assess the contribution of galaxy haloes to the scattering of FRBs. We demonstrate how scattering measurements of FRBs can be interpreted in terms of the internal properties of the scattering media, and apply this formalism to galaxy haloes intervening LoS to FRBs. We first assess scattering from the Milky Way halo using two case studies: FRB 121102 and FRB 180916. These FRBs have the most comprehensive, precise scattering measurements currently available, in addition to highly precise localizations and host galaxy associations. Due to their location close to the Galactic plane, the emission from these sources samples both the outer spiral arm of the Galaxy and the Galactic thick disk, and the scattering observed for these FRBs is broadly consistent with the scattering expected from the spiral arm and disk. Only a minimal amount of scattering is allowed from the Galactic halo along these LoS, thus providing an upper limit on the halo’s scattering contribution. We then extrapolate this analysis to two FRBs that pass through haloes other than those of their host galaxies and the Milky Way, FRB 181112 and FRB 191108.

In Section 2 we summarize the formalism relating electron density fluctuations and the observables $\tau$, DM, $\Delta \nu_d$, and $\theta_d$, and describe our model for the scattering contribution of the Galactic halo. A new measurement of the fluctuation parameter of the Galactic thick disk is made in Section 3.1 using Galactic pulsars. An overview of the scattering measurements for FRB 121102 and FRB 180916 is given in Section 3.2, including an updated constraint on the scintillation bandwidth for FRB 121102 and a comparison of the scattering predictions made by Galactic electron density models NE2001 (Cordes & Lazio 2002, 2003) and YMW16 (Yao et al. 2017). The FRB scattering constraints are used to place an upper limit on the fluctuation parameter of the Galactic halo in Section 3.3. A brief comparison of the FRB-derived limit with scattering observed towards the Magellanic Clouds is given in Section 3.4 and scattering constraints for intervening galaxy haloes are discussed in Section 4.

2. MODELING

2.1. Electron Density Fluctuations and Scattering

We characterize the relationship between electron density fluctuations and scattering of radio emission using an ionized cloudlet model in which clumps of gas in the medium have a volume filling factor $f$, internal density fluctuations with variance $\epsilon^2 = \langle (\delta n_e)^2 \rangle / n_e^2$, and cloud-to-cloud variations described by $\zeta = \langle n_e^2 \rangle / \langle n_e \rangle^2$, where $n_e$ is the local, volume-averaged mean electron density (Cordes et al. 1991; Cordes & Lazio 2002, 2003). We assume that internal fluctuations follow a power-law wavenumber spectrum of the form (Coles et al. 1987) $P_{nm}(q) = C_n^2 q^{-\beta} \exp(-(ql_i/2\pi)^2)$ that extends over a wavenumber range $2\pi/l_o \leq q \lesssim 2\pi/l_i$ defined by the outer and inner scales, $l_o$, $l_i$, respectively. We adopt a wavenumber index $\beta = 11/3$ that corresponds to a Kolmogorov spectrum. Typically, $l_i \ll l_o$, but their magnitudes depend on the physical mechanisms driving and dissipating turbulence, which vary between different regions of the ISM.

Multipath propagation broadens pulses by a characteristic time $\tau$ that we relate to DM and other quantities. For a medium with homogeneous properties, the scattering time in Euclidean space is $\tau(DM, \nu) = K_\gamma A_\gamma \nu^{-4} F_{G\text{scatt}} \text{DM}^2$ (Cordes et al. 2016). The coefficient $K_\gamma = \Gamma(7/6) c^3 r_e^2 / 4$, where $c$ is the speed of light and $r_e$ is the classic electron radius, while the factor $A_\gamma \lesssim 1$ scales the mean delay to the $1/e$ delay that is typically estimated from pulse shapes. Because $A_\gamma$ is medium dependent, we include it in relevant expressions symbolically rather than adopting a specific value. The scattering efficacy is determined by the fluctuation parameter $F = \zeta \epsilon^2 / f(l_i^2) / 1/3$ combined with a dimensionless geometric factor, $G_{\text{scatt}}$, discussed below.

Evaluation with DM in pc cm$^{-3}$, the observation frequency $\nu$ in GHz, the outer scale in pc units, and the inner
scale in km, $\bar{F}$ has units pc$^{-2/3}$ km$^{-1/3}$ and
\[
\tau(\Delta \nu, \nu, z) \approx 48.03 \mu s \times A_\nu \bar{F} \frac{\text{DM}^2}{(1 + z)^{3/2}} \left[ \frac{2d_{\delta}d_{\delta0}}{L_{\delta0}} \right].
\] (2)

If the layer’s DM could be measured, it would be smaller by a factor $(1 + z)^{-1}$ in the observer’s frame.

The pulse broadening time is related to the scintillation bandwidth $\Delta \nu_{\delta}$ through the uncertainty principle $2\pi \tau \Delta \nu_{\delta} = C_1$, where $C_1 = 1$ for a homogeneous medium and $C_1 = 1.16$ for a Kolmogorov medium (Cordes & Rickett 1998). Multipath propagation is also manifested as angular broadening, $\theta_\delta$, defined as the FWHM of the scattered image of a point source. The angular and pulse broadening induced by a thin screen are related to the distance between the observer and screen, which will be discussed further in Section 3.2.1.

Measurements of $\tau$, $\Delta \nu_{\delta}$, and $\theta_\delta$ can include both extragalactic and Galactic components. We use the notation $\tau_{\text{MW}, a}$, $\tau_{\text{MW}, b}$, and $\tau_{h}$ to refer to scattering contributed by the Galactic disk (excluding the halo), the Galactic halo, and intervening haloes, respectively, and an equivalent notation for DM. To convert between $\Delta \nu_{\delta}$ and $\tau$ we adopt $C_1 = 1$. Wherever we use the notation $\tau$ and $\theta_\delta$ we refer to the 1/e delay and FWHM of the autocorrelation function that are typically measured.

### 2.2. Electron Density Model for the Galactic Halo

Models of the Milky Way halo based on X-ray emission and oxygen absorption lines depict a dark matter halo permeated by hot ($T \sim 10^7$ K) gas with a virial radius between 200 and 300 kpc (e.g., Prochaska & Zheng 2019; Yamasaki & Totani 2020; Keating & Pen 2020). Based on these models, the average DM contribution of the hot gas halo to FRBs is about 50 pc cm$^{-3}$, which implies a mean electron density $n_e \sim 10^{-4}$ cm$^{-3}$. However, the DM contribution of the Milky Way halo is still not very well constrained. Keating & Pen (2020) compare the range of DM$_{\text{MW}, h}$ predicted by various halo models with the XMM-Newton soft X-ray background (Henley & Shelton 2013) and find that the range of DM$_{\text{MW}, h}$ consistent with the XMM-Newton background spans over an order of magnitude and could be as small as about 10 pc cm$^{-3}$. Using a sample of DMs from 83 FRBs and 371 pulsars, Platts et al. (2020) place a conservative upper limit on DM$_{\text{MW}, h} < 123$ pc cm$^{-3}$, with an average value of DM$_{\text{MW}, h} \approx 60$ pc cm$^{-3}$.

Most models of the hot gas halo adopt a spherical density profile, but Yamasaki & Totani (2020) and Kaaret et al. (2020) argue that a disk component with a scale height of about 2 kpc and a radial scale length of about 5 kpc should be added to the spherical halo based on the directional dependence of emission measure found in Suzaku and HaloSat X-ray observations (Nakashima et al. 2018; Kaaret et al. 2020). In such a combined disk-spherical halo model, the disk would account for most of the observed X-ray emission attributed to the halo, while the diffuse, extended, spherical halo contains most of the baryonic mass. Kaaret et al. (2020) also suggest that significant, patchy variations may exist in the halo gas on scales $\sim 400$ pc. The physical scales of the disk models fit to these recent X-ray observations are similar to the spatial scale of the warm ionized medium in the Galactic disk, and several orders of magnitude smaller than the spatial scales ($\sim 100$ s of kpc) typical of spherical halo models. Whether such a disk component should really be attributed to the circumgalactic medium and not to the ISM of the Galactic disk is unclear.

We use the Prochaska & Zheng (PZ19) modified Navarro-Frenk-White (mNFW) profile to model the halo density. The mNFW profile adjusts the NFW profile’s matter density cusp at the Galactic center with a more physical roll-off, giving a matter density of
\[
\rho(y) = \frac{\rho_0}{y^{1+\alpha}(y_0 + y)^{2+\alpha}},
\] (3)
where $y = K_c \times (r/r_{200})$, $r$ is radial distance from the Galactic center, and $r_{200}$ is the virial radius within which the average density is 200 times the cosmological critical density. The characteristic matter density $\rho_0$ is found by dividing the total mass of the halo by the volume within the
surements of $\tau$ by the fluctuation parameter $\tilde{\tau}$ traces the same plasma that gives rise to dispersion, weighted in a way, is shown in Figure 1.

The maximum DM contribution of the halo predicted by the model is $63 \text{ pc cm}^{-3}$, similar to the predictions of other halo density models for lines of sight to the Galactic antecenter (e.g., Platts et al. 2020; Yamasaki & Totani 2020; Keating & Pen 2020).

The concentration parameter $K_c$ depends on the galaxy mass; e.g., $K_c = 7.7$ for a total Milky Way halo mass $M = 1.5 \times 10^{12} M_\odot$, and can range from $K_c = 13$ for $M = 10^{10} M_\odot$ to $K_c = 5$ for $M = 10^{11} M_\odot$ for redshifts $z < 0.1$ (Navarro et al. 1997). Like PZ19, we assume that $75\%$ of the baryonic mass in a galaxy is in the halo ($f_b = 0.75$), and the fraction of the total matter density that is baryonic is $\Omega_b/\Omega_m$, the ratio of the baryonic matter density to the total matter density ($\Omega_b/\Omega_m = 0.16$ today). If $f_b$ is smaller, then the electron density and the predicted scattering from a halo will be smaller.

The electron density profile of the halo is

$$n_e(r) \approx 0.86 f_b \times (\Omega_b/\Omega_m) \rho(r) \frac{\sigma(r)}{m_p} U(r),$$

where $m_p$ is the proton mass and we have assumed a gas of fully ionized hydrogen and helium. The function $U(r) = (1/2) \{1 - \text{tanh}[r - r_c]/w \}$ imposes an explicit integration limit at a radius $r_c = 2 r_{200}$ over a region of width $w = 20 \text{ kpc}$ so as to avoid sharp truncation of the model. Our implementation of the PZ19 model, evaluated for the Milky Way, is shown in Figure 1.

2.3. Scattering from the Galactic Halo

Generally speaking, scattering from the Galactic halo traces the same plasma that gives rise to dispersion, weighted by the fluctuation parameter $\tilde{F}$. To constrain $\tilde{F}$ from measurements of $\tau$ and $\theta_d$, we approximate the total scattering as a sum of two components: one from the disk and spiral arms of the Milky Way, which we denote with the subscript (MW, $d$), and one from the Galactic halo, which we denote with the subscript (MW, $h$). The total $\tau$ and $\theta_d$ predicted by the model are therefore

$$\tau_{\text{MW}} = \tau_{\text{MW},d} + \tau_{\text{MW},h}$$

and

$$\theta_{\text{MW},d} = \sqrt{\theta_{\text{MW},d}^2 + \theta_{\text{MW},h}^2}$$

We adopt the NE2001 predictions for the MW components and model the halo components using Equations 1 and 9. The composite parameter $A_r(\tilde{F} \times \text{DM}^2)_{\text{MW},h}$ is constrained by maximizing the likelihood function

$$L((\tilde{F} \times \text{DM}^2)_{\text{MW},h}|\tau_j) = \prod_j N(\tau_{\text{total},j} - \tau_{\text{obs},j}, \sigma_{\tau,j}^2)$$

using measurements $\tau_{\text{obs},j}$ and $\theta_{\text{obs},j}$. The variance of the likelihood function $\sigma_{\tau,j}^2$ is taken from the measurement uncertainties, where we implicitly assume that measurements of $\tau$ and $\theta_d$ are sufficiently approximated by Gaussian PDFs. An estimate of $\tilde{F}_{\text{MW},h}$ can then be obtained by assuming a given halo density profile or constructing a PDF for $\text{DM}_{\text{MW},h}$, and adopting a value for $A_r$.

3. THE MILKY WAY HALO

In order to determine how the Milky Way halo (and in turn other galaxy haloes) contributes to the scattering of FRBs, we must constrain the scattering contribution of the Galactic disk. In the following sections, we first determine the amount of scattering that can occur in the thick disk of the Galaxy using the distribution of pulsar scattering measurements and DMs at high Galactic latitudes. We then compare the scattering measurements of FRB 121102 and FRB 180916 to the scattering expected from the Galactic disk using NE2001, and explain discrepancies between the scattering predictions of the NE2001 and YMW16 Galactic disk models. Finally, in Section 3.3, we constrain the scattering contribution of the Galactic halo, followed by discussion of scattering constraints from pulsars in the Magellanic Clouds.

3.1. Scattering from the Thick Disk

Most currently known FRBs lie at high Galactic latitudes, and their LoS through the Galaxy predominantly sample the thick disk, which has a mean density at mid-plane of 0.015 cm$^{-3}$ and a scale height $\approx 1.6$ kpc (Ocker et al. 2020). The distribution of $\tau$/DM$^2$ for Galactic pulsars with measurements of $\tau$ (Cordes et al. 2016, and references therein) and DM and other parameters from Manchester et al. (2005)\footnotemark[1]
yields a direct constraint on $\tilde{F}$: $\tau/\text{DM}^2 \approx (16 \text{ ms}) A_\nu \tilde{F}$, for $\nu = 1 \text{ GHz}$ and $G_{\text{scatt}} = 1/3$ for sources embedded in the scattering medium. The distribution of $\tilde{F}$ for all Galactic pulsars, assuming $A_\nu \approx 1$, is shown in Figure 2. For the pulsars above $|20^\circ|$ Galactic latitude, the mean value of $\tau/\text{DM}^2$ from a logarithmic fit is $(5.3^{+5.3}_{-3.3}) \times 10^{-8} \text{ ms pc}^{-2} \text{ cm}^6$, which yields $\tilde{F} \approx (3 \pm 2) \times 10^{-3} \text{ pc}^{-2/3} \text{ km}^{-1/3}$. The value of $\tilde{F}$ based on high-latitude pulsars is consistent with the related $F = l^{1/3} F$ factor used in the NE2001 model for scattering in the thick disk.

A structural enhancement to radio scattering for LoS below $|20^\circ|$ is reflected in the distribution of $\tau/\text{DM}^2$ shown in Figure 2, which shows a multiple orders of magnitude increase in $\tilde{F}$ at low latitudes, with the largest values of $\tilde{F}$ dominating LoS to the Galactic center. This latitudinal and longitudinal dependence of $\tilde{F}$ is directly responsible for the “hockey-stick” relation between $\tau$ and DM for Galactic pulsars, in which high-DM pulsars lying close to the Galactic plane and towards the Galactic center have a much steeper dependence on DM than pulsars lying high above the Galactic plane or towards the Galactic anti-center (e.g., Bhat et al. 2004; Krishnakumar et al. 2015; Cordes et al. 2016). The implications of the directional dependence of $\tilde{F}$ for FRB LoS are discussed further in Section 3.2.3.

For the many FRBs in high Galactic latitude directions, the Galactic disk has a virtually undetectable contribution to the observed pulse broadening. The DM contribution of the thick disk is about $(23.5 \times \csc(|b|)) \text{ pc cm}^{-3}$, which varies negligibly with latitude for $|b| > 20^\circ$ (Ocker et al. 2020). The pulse broadening at 1 GHz expected from the thick disk therefore ranges from $\tau < 0.25 \mu\text{s}$ at $|b| = 20^\circ$ to $\tau < 29 \text{ ns}$ at $|b| = 90^\circ$. As discussed in the following section, scattering from the Galactic thin disk and spiral arms increases dramatically for FRB LoS close to the Galactic plane.

### 3.2. Scattering Constraints for Two FRB Case Studies

Unlike Galactic pulsars, for which the scintillation bandwidth and pulse broadening both result from the same electrons and conform to the uncertainty relation $2\pi \Delta \nu_d \tau_d = C_1$, some FRBs indicate that two scattering media are involved. In these cases, the scintillation bandwidth is consistent with diffraction interstellar scintillation caused by foreground Galactic turbulence while the pulse broadening also has contributions from an extragalactic scattering medium (Masui et al. 2015; Gajjar et al. 2018; Cordes & Chatterjee 2019). Here we analyze the Galactic scintillations of two FRBs with highly precise scattering measurements in order to place constraints on any scattering in the Galactic halo.

#### 3.2.1. FRB 121102

FRB 121102 currently has the most comprehensive set of scattering constraints on an FRB source so far, with scintil-
lation bandwidths $\Delta \nu_{d} = 58.1 \pm 2.3$ kHz at 1.65 GHz (Hessels et al. 2019), 5 MHz at 4.5 GHz (Michilli et al. 2018), 6.4 $\pm$ 1.4 MHz at 4.85 GHz (Spitler et al. 2018), and 10 $-$ 50 MHz between 5 and 8 GHz (Gajjar et al. 2018). All of these scintillation bandwidth measurements are assembled in Figure 3, along with a power-law fit to the data using linear least squares that gives a mean value $\Delta \nu_{d} = 3.8_{-2.5}^{+1.5}$ kHz at 1 GHz.

FRB 121102 also has a pulse broadening time upper limit of $\tau < 9.6$ ms at 500 MHz (Josephy et al. 2019), and angular broadening $\theta_{d} = 2 \pm 1$ mas at 1.7 GHz and $\theta_{d} \sim 0.4 - 0.5$ mas at 5 GHz, which was measured in the Marcote et al. (2017) high-resolution VLBI study of the FRB and its persistent radio counterpart. These angular diameters are consistent with those reported in Chatterjee et al. (2017) and with the NE2001 prediction. The scattering measurements are shown in Table 1 and are referenced to 1 GHz assuming $\tau \propto \nu^{-4}$ frequency scaling.

The NE2001 angular broadening and scintillation bandwidth predictions for FRB 121102 are broadly consistent with the corresponding empirical constraints (see Table 1). In NE2001, the scattering for this LoS is dominated by an outer spiral arm located 2 kpc away and by the thick disk, which extends out to 17 kpc from the Galactic center (Cordes & Lazio 2002). The $C_{\phi}^2$, electron density, and DM predicted by NE2001 along the LoS to FRB 121102 are shown in Figure 4. Modeling of the anti-center direction in NE2001 is independent of our analysis and is based on DM and scattering measurements of Galactic pulsars in the same general direction and upper bounds on the angular scattering of extragalactic sources. The NE2001 model parameters were constrained through a likelihood analysis of these measurements, which revealed that the fluctuation parameter was smaller for LoS that probe the outer Galaxy compared to the inner Galaxy (Lazio & Cordes 1998). This result required that the thick disk component of NE2001 have a smaller fluctuation parameter compared to the thin disk and spiral arm components that are relevant to LoS through the inner Galaxy.

Since the measured $\Delta \nu_{d}$ and $\theta_{d}$ for FRB 121102 are broadly consistent with the predicted amount of scattering from the Galactic disk, we use $\Delta \nu_{d}$ and $\theta_{d}$ to estimate the effective distance to the dominant scattering material. For thin-screen scattering of a source located at a distance $d_{so}$ from the observer, the scattering diameter $\theta_{s}$ is related to the observed angular broadening by

$$\theta_{d} \sim \theta_{s}(d_{so}/d_{so}) = \theta_{s}
\left(1 - \frac{d_{lo}}{d_{so}}\right),$$

where $d_{so}$ is the source-to-screen distance and $d_{lo}$ is the screen-to-observer distance. The scattering diameter is related to the pulse broadening delay by $\tau \approx A_{\nu}d_{so}(d_{dl}/d_{so})(1 - d_{dl}/d_{so})\theta_{s}^{2}/8(\ln 2)c$ (Cordes & Chatterjee 2019). For a thin screen near the observer and an extragalactic source, $d_{lo} \ll d_{dl}$, giving $\theta_{d} \approx \theta_{s}$ and

$$\theta_{d} \approx \left(\frac{4(\ln 2)A_{\nu}c}{\pi \Delta \nu_{d} d_{lo}}\right)^{1/2}.$$  \hspace{1cm} (9)

The scattering screen location can thus be directly estimated from measurements of $\theta_{d}$ and $\Delta \nu_{d}$.

Assuming that the same Galactic scattering material gives rise to both the angular broadening and the scintillation of FRB 121102, Equation 9 implies the scattering material has an effective distance $d_{lo} \approx 2.3$ kpc from the observer (assuming $A_{\nu} \approx 1$), which is consistent with the distance to the spiral arm, as shown in Figure 4. A numerical joint-probability analysis of the uncertainties in $\Delta \nu_{d}$ and $\theta_{d}$, assuming both quantities follow normal distributions, allows the screen to be as close as 1.6 kpc or as far as 5.5 kpc (corresponding to the 15% and 85% confidence intervals). Figure 5 shows a comparison of the relationship between $\theta_{d}$ and $d_{lo}$ for a thin screen and the measured $\theta_{d}$ from Marcote et al. (2017). Given that there is no known HII region along the LoS to FRB 121102, the most likely effective screen is in fact the spiral arm.

The scintillation bandwidth implies a pulse broadening contribution from the Milky Way disk and spiral arms $\tau_{MW,d} \approx 0.04 \pm 0.02$ ms at 1 GHz. The upper limit on $\tau$ measured by Josephy et al. (2019) is an order of magnitude larger than the $\tau_{MW,d}$ inferred from $\Delta \nu_{d}$. Any additional scattering beyond the Galactic contribution is more likely from the host galaxy due to the lack of intervening galaxies along the LoS, and the small amount of scattering expected from the IGM (Macquart & Koay 2013; Zhu & Feng 2020).

### 3.2.2. FRB 180916

The scattering constraints for FRB 180916 consist of a scintillation bandwidth $\Delta \nu_{d} = 59 \pm 13$ kHz at 1.7 GHz (Marcote et al. 2020) and a pulse broadening upper limit $\tau < 1.7$ ms at 350 MHz (Chawla et al. 2020). The $\Delta \nu_{d}$ and $\tau$ upper limit are entirely consistent with each other, so we again use $\Delta \nu_{d}$ and the inferred $\tau_{MW,d}$ for the rest of the analysis due to its higher precision. Based on $\Delta \nu_{d}$, $\tau_{MW,d} = 0.023 \pm 0.005$ ms at 1 GHz. As with FRB 121102 the NE2001 scattering predictions for this LoS are consistent with the empirical constraints to within the model’s uncertainty, suggesting that the Galactic halo has a small ($\lesssim \mu$s level) contribution to the observed scattering.

### 3.2.3. Comparison with YMW16 Scattering Predictions

The YMW16 model significantly overestimates the scattering of FRB 121102 and FRB 180916. The DM and scattering predictions for these FRBs are shown in Table 1. Evaluating YMW16 for FRB 121102 using the IGM mode gives $\log(\tau) = -3.074$ with $\tau$ in seconds, implying $\tau = 0.84$ ms.
at 1 GHz, corresponding to $\Delta\nu_d \approx 0.2 \, \text{kHz}$, about 50 times smaller than the NE2001 value. Compared to the measured scattering, the nominal output of the YMW16 model overestimates the scattering toward FRB 121102 by a factor of 28 to 35 (depending on whether a $\nu^{-4}$ or $\nu^{-4.4}$ scaling is used). Moreover, combining the measured $\theta_d$ with the YMW16 estimate for $\tau$ implies a scattering screen distance $\sim 500$ kpc, beyond any local Galactic structure that could reasonably account for the scattering. For FRB 180916, YMW16 also overestimates $\tau$ to be 0.42 ms at 1 GHz, implying a scintillation bandwidth of 0.4 kHz at 1 GHz.

The discrepancies between the observed scattering and the YMW16 predictions are due to several important factors. Unlike NE2001, YMW16 does not explicitly model electron density fluctuations. Instead, it calculates DM for a given LoS and then uses the $\tau$–DM relation based on Galactic pulsars to predict $\tau$. In using the $\tau$–DM relation, the YMW16 model incorrectly adjusts for the scattering of extragalactic bursts. The waves from extragalactic bursts are essentially planar when they reach the Galaxy, which means they are scattered from wider angles than diverging spherical waves from a Galactic pulsar would be. The differences between plane and spherical wave scattering are discussed in detail for FRBs in Cordes et al. (2016). The YMW16 model accounts for this difference by reducing the Galactic prediction of $\tau$ by a factor of two, when geometric weighting of the mean-square scattering angle implies that the Galactic scattering prediction should really be larger by a factor of three to apply to extragalactic FRBs (see Eq. 10 in Cordes et al. 2016). This implies that values for $\tau$ in the output of YMW16 should be multiplied by a factor of six, which means that the model’s overestimation of the scattering is really by a factor of 170 to 208 when one only considers the correction for planar wave scattering.

YMW16 may also overestimate the Galactic contribution to DMs of extragalactic sources viewed in the Galactic anticenter direction (and perhaps other low-latitude directions) because it significantly overestimates the observed DM distribution of Galactic pulsars that NE2001 is based on. In YMW16, the dominant DM contributions to extragalactic sources in this direction are from the thick disk and from the spiral arms exterior to the solar circle. Together these yield DM values of 287 pc cm$^{-3}$ and 243 pc cm$^{-3}$ for FRB 121102 and FRB 180916, respectively. These DM pre-
dictions are over 50% and 20% larger for each FRB than the NE2001 values, which may be due to overestimation of the densities or characteristic length scales of the outer spiral arm and thick disk components.

The primary cause for YMW16’s scattering overprediction is that the part of the pulsar-derived \( \tau - \text{DM} \) relation that applies to large values of DM should not be used for directions toward the Galactic anti-center. The \( \tau - \text{DM} \) relation has the empirical form (Cordes et al. 2016)

\[
\tau = (2.98 \times 10^{-7} \text{ ms}) \text{DM}^{1.4} (1 + 3.55 \times 10^{-5} \text{DM}^{3.1})
\]

based on a fit to pulsar scattering data available through 2016. Similar fits were previously done by Ramachandran et al. (1997), Bhat et al. (2004), and Krishnakumar et al. (2015). It scales as \( \text{DM}^{1.4} \) for DM \( \lesssim 30 \) pc cm\(^{-3}\) and as \( \text{DM}^{4.5} \) for DM \( \gtrsim 100 \) pc cm\(^{-3}\).

The YMW16 model uses Krishnakumar’s model for 327 MHz scattering times scaled to 1 GHz by a factor \( (0.327)^4 \), giving \( \tau = (4.1 \times 10^{-8} \text{ ms}) \text{DM}^{2.2} (1 + 0.00194 \times \text{DM}^2) \). This scaling law is in reasonable agreement with the expression in Equation 10 except at very low DM values. The Krishnakumar scaling law adopted the Ramachandran et al. (1997) approach of fixing the leading DM exponent to 2.2, which is based on the assumption that the relatively local ISM is uniform. This assumption is imperfect given our knowledge of the Local Bubble and other shells and voids in the local ISM. The steep \( \tau \propto \text{DM}^{4.2} \) to 4.5 scaling for Galactic pulsars is from LoS that probe the inner Galaxy, where the larger star formation rate leads to a higher supernova rate that evidently affects the turbulence in the HII gas, and results in a larger \( F \), as shown in Section 3.1.

If the YMW16 model were to use instead the shallow part of the \( \tau - \text{DM} \) relation, \( \tau \propto \text{DM}^{2.2} \) to 1.4, which is more typical of LoS through the outer Galaxy, its scattering time estimates would be smaller by a factor of \(~ 1.94 \times 10^{-3} \times (287)^2 \sim 160 \) or \(~ 3.55 \times 10^{-5} \times (287)^{3.1} \sim 1500 \), depending on which \( \tau - \text{DM} \) relation is used (and using FRB 121102 as an example). These overestimation factors could be considerably smaller if smaller DM values were used. While there is a considerable range of values for the overestimation factor based on the uncertainties in the empirical scaling law, it is reasonable to conclude that the high-DM part of the \( \tau - \text{DM} \) relation should not be used for the anti-center FRBs.

### 3.3. Fluctuation Parameter of the Galactic Halo

The measurements of \( \tau \) and \( \theta_d \) for FRBs 121102 and 180916, combined with the scattering predictions of NE2001, yield a maximum likelihood estimate for the pulse.

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**Figure 4.** Galactic DM, electron density \( n_e \), and \( C_n^2 \) contribution predicted by NE2001 for FRB 121102. The maximum DM (excluding the Galactic halo) is 188 pc cm\(^{-3}\). The sharp changes in \( n_e \) and \( C_n^2 \) between 0 and 0.3 kpc are due to structure in the local ISM. The shaded grey region indicates the distance to the scattering screen derived from a numerical joint-probability analysis of the measured scattering constraints for FRB 121102; see Figure 5.

**Figure 5.** Scattering diameter vs. effective distance. The blue band indicates the angular diameter \( \theta_d = 2 \pm 1 \) mas (1\( \sigma \) errors) from Marcote et al. (2017). The green band is the predicted angular diameter for a thin-screen that matches the least-square fit to scintillation bandwidth measurements and the uncertainties at \( \pm 1\sigma \). All values are expressed at 1.7 GHz. A numerical joint-probability estimate constraining the overlap of the green and blue regions gives a screen distance \( d_{lo} \approx 2.3^{+0.2}_{-0.7} \) kpc.
broadening contribution of the Milky Way halo (see Equation 7). The 95% upper confidence interval yields \((F \times D^2)_{\text{MW},h} < 250/A_\tau \text{ pc}^{4/3} \text{ km}^{-1/3} \text{ cm}^{-1/3}\). The maximum amount of pulse broadening expected from the Galactic halo is therefore \(\tau_{\text{MW},h} < 12 \mu s\) at 1 GHz, which is comparable to the scattering expected from the Galactic disk for LoS towards the Galactic anti-center or at higher Galactic latitudes.

Based on the broad range of \(D_{\text{MW},h}\) currently consistent with the empirical and modeled constraints (see Section 2.2), we construct a Gaussian probability density function (PDF) for \(\overline{D}_{\text{MW},h}\) with a mean of 60 pc cm\(^{-3}\) and \(\sigma_{\text{DM}} = 18\) pc cm\(^{-3}\). Combining this PDF with the maximum likelihood estimate for \((F \times D^2)_{\text{MW},h}\) yields an upper limit \(\overline{F}_{\text{MW},h} < 0.03/A_\tau \text{ pc}^{-2/3} \text{ km}^{-1/3}\). While \(A_\tau\) is probably about 1, if \(A_\tau\) is as small as 1/6 then \(\overline{F}_{\text{MW},h}\) could be up to 6 times larger.

This estimate of \(\overline{F}_{\text{MW},h}\) is based on just two LoS towards the Galactic anti-center, and it is unclear how much \(\overline{F}_{\text{MW},h}\) will vary between different LoS through the halo. Given that sources viewed through the inner Galaxy (near \(b = 0^\circ\)) are more heavily scattered, it is unlikely that estimates of \(\overline{F}_{\text{MW},h}\) will be obtainable for LoS that intersect the halo through the inner Galaxy. However, FRB 121102, FRB 180916, and most of the FRBs detected at higher latitudes do not show evidence of any intense scattering regions that might be associated with the halo (e.g., Qiu et al. 2020), suggesting that extremely scattered FRBs would be outliers and not representative of the Galactic halo’s large-scale properties. All FRBs are ultimately viewed through not only the Galactic halo but also the haloes of their host galaxies and, in some cases, the haloes of intervening galaxies. Given the observed variations in scattering between different LoS through the Milky Way, it appears most likely that the heaviest scattered FRBs will be viewed through scattering regions within galaxy disks rather than haloes, and extrapolating our analysis to a larger sample of FRBs will require determining whether observed variations in \(F\) are due to variations between galaxy haloes, disks, or the sources’ local environments. In the following sections, we compare the Milky Way halo scattering contribution inferred from FRBs 121102 and 180916 to scattering observed from the Magellanic Clouds and galaxy haloes intervening LoS to FRBs.

### 3.4. Constraints from Pulsars in the Magellanic Clouds

At distances of 50 to 60 kpc and latitudes around \(-30^\circ\), pulsar radio emission from the Large and Small Magellanic Clouds (LMC/SMC) mostly samples the Galactic thick disk and a much smaller path length through the Galactic halo than FRBs. So far, twenty-three radio pulsars have been found in the LMC and seven in the SMC (e.g., McConnell et al. 1991; Crawford et al. 2001; Manchester et al. 2006; Ridley et al. 2013; Titus et al. 2019). Very few scattering measurements exist for these LoS. PSR B0540−69 in the LMC has a DM of 146.5 pc cm\(^{-3}\) and was measured to have a pulse broadening time \(\tau = 0.4\) ms at 1.4 GHz (Johnston & Romani 2003). The Galactic contribution to DM and scattering predicted by NE2001 towards this pulsar are \(D_{\text{NE2001}} = 55\) pc cm\(^{-3}\), and \(\tau_{\text{NE2001}} = 0.3 \times 10^{-3}\) ms at 1 GHz. Based on this DM estimate, the pulsar DM receives a contribution of about 92 pc cm\(^{-3}\) from the LMC and the Galactic halo. The lowest DMs of pulsars in the LMC have been used to estimate the DM contribution of the halo to be about 15 pc cm\(^{-3}\) for pulsars in the LMC (Yamasaki & Totani 2020), which suggests that the LMC contributes about 77 pc cm\(^{-3}\) to the DM of B0540−69.

The scattering observed towards B0540−69 is far in excess of the predicted scattering from the Galactic disk. Since B0540−69 not only lies within the LMC but also within a supernova remnant, it is reasonable to assume that most of the scattering is contributed by material within the LMC. Using the upper limit \(\overline{F}_{\text{MW},h} < 0.03/A_\tau \text{ pc}^{-2/3} \text{ km}^{-1/3}\) and \(\overline{D}_{\text{MW},h} = 15\) pc cm\(^{-3}\) yields \(\tau_{\text{MW},h} < 0.1\) ms at 1.4 GHz for this LoS, which is too small to explain the observed scattering. If we instead combine \(\tau = 0.4\) ms at 1.4 GHz and the estimated \(\overline{D}_{\text{LMC}} = 77\) pc cm\(^{-3}\), we find \(\overline{F}_{\text{LMC}} = 16/A_\tau \text{ pc}^{-2/3} \text{ km}^{-1/3}\). More scattering measurements for LMC and SMC pulsars are needed to better constrain the fluctuation parameters of the LMC and SMC, which in turn will improve our understanding of interstellar plasma in these satellite galaxies.

### 4. Constraints on Intervening Haloes along Lines of Sight to FRBs

As of this paper, two FRBs are found to pass through galactic haloes other than those of their host galaxies and the Milky Way: FRB 181112, which passes within 30 kpc of the galaxy DES J214923.89−525810.43, otherwise known as FG−181112 (Prochaska et al. 2019), and FRB 191108, which passes about 18 kpc from the center of M33 and 185 kpc from M31 (Connor et al. 2020). Both FRBs have measurements of \(\tau\) which are somewhat constraining.

#### 4.1. FRB 181112

FRB 181112 was initially found to have \(\tau < 40\) \(\mu s\) at 1.3 GHz by Prochaska et al. (2019); follow-up analysis of the ASKAP filterbank data and higher time resolution data for this burst yielded independent estimates of \(\tau < 0.55\) ms (Qiu et al. 2020) and \(\tau \approx 21 \pm 1\) ms (Cho et al. 2020) at 1.3 GHz. We adopt the last value for our analysis, with the caveat that the authors report skepticism that the data is best fit by a pulse broadening tail following the usual frequency dependence expected from scattering in a cold plasma, and that the measured decorrelation bandwidth of the burst spectrum is
in tension with the pulse broadening fit (for a full discussion, see Section 4 of Cho et al. 2020).

We first place an upper limit on \( (\tilde{F} \times \Delta M^2)_i \), for FG−181112 by assuming that the intervening halo may contribute up to all of the observed scattering of FRB 181112. The halo density profile (Equation 4) is re-scaled to the lens redshift (\( z_{\text{lens}} \approx 0.36 \)) and evaluated at the impact parameter \( R_{\perp} = 29 \) kpc. Prochaska et al. (2019) constrain the mass of the intervening halo to be \( M_{\text{halo}}^{\text{FG−181112}} \approx 10^{12.3} M_\odot \). Again assuming a physical extent to the halo of 2\( r_\text{200} \) gives a path length through the halo \( L \approx 930 \) kpc. The observed scattering \( \tau \approx 21 \) \( \mu \text{s} \) is the maximum amount of scattering that could be contributed by the halo, i.e., \( \tau_{\text{dm}} < 21 \mu \text{s} \) at 1.3 GHz, which yields \( (\tilde{F} \times \Delta M^2)_i / \text{pc cm}^{-3} \approx 13 / A_r \) \( \text{pc}^{-4/3} \text{cm}^{-1/3} \), using Equation 2.

Assuming the halo density profile where \( y_0 = \alpha = 2 \) gives \( \Delta M_{\text{halo}} \approx 135 \) \( \text{pc cm}^{-3} \) in the frame of the intervening galaxy. This DM estimate for the halo is similar to the estimate of 122 \( \text{pc cm}^{-3} \) from Prochaska et al. (2019), but as they note, the DM contribution is highly sensitive to the assumed density profile and could be significantly smaller if the physical extent and/or the baryonic fraction of the halo are smaller. This DM estimate yields \( \tilde{F}_i / \text{pc cm}^{-3} \approx (7 \times 10^{-4}) / A_r \) \( \text{pc}^{-2/3} \text{cm}^{-1/3} \). If the DM contribution of the intervening halo is smaller, then \( \tilde{F}_i \) could be up to an order of magnitude larger. The observed DM of the FRB is broadly consistent with the estimated DM contributions of the Milky Way, host galaxy, and IGM alone (Prochaska et al. 2019), so the uncertainty in \( \Delta M_{\text{halo}} \) remains the greatest source of uncertainty in deconstructing \( \tilde{F} \). Both estimates of \( (\tilde{F} \times \Delta M^2)_i \) and \( \tilde{F}_i \) for FRB 181112 are within the upper limits for the Milky Way halo.

### 4.2. FRB 191108

FRB 191108 passes through both the M31 and M33 haloes and has a source redshift upper limit \( z \lesssim 0.5 \) based on DM. Connor et al. (2020) report an upper limit of 80 \( \mu \text{s} \) on the intrinsic pulse width and scattering time at 1.37 GHz, but they demonstrate that this limit is likely biased by dispersion smearing. Connor et al. (2020) also report 25% intensity modulations at a decorrelation bandwidth \( \sim 40 \) MHz. This decorrelation bandwidth may be attributable to scattering in the M33 halo and/or in the host galaxy (for a full discussion, see Section 3.4 of Connor et al. 2020).

Re-scaling our galactic halo density profile using halo masses \( M_{\text{halo}}^{\text{M33}} \approx 5 \times 10^{11} M_\odot \) and \( M_{\text{halo}}^{\text{M31}} \approx 1.5 \times 10^{12} M_\odot \) yields a total DM contribution from both haloes of about 110 \( \text{pc cm}^{-3} \), nearly two times larger than the DM contribution estimated by Connor et al. (2020), who use a generic model for the M33 and M31 haloes from Prochaska & Zheng (2019) based on the same galaxy masses. We assume that the density profiles are independent; if there are dynamical interactions between the haloes then these may slightly modify the overall density distribution along the LoS, but it is unclear how turbulence in the plasma would be affected, if at all. Since the impact parameter of 18 kpc for M33 is significantly smaller than the 185 kpc for M31, M33 dominates the predicted DM contribution to FRB 191108 (with \( \Delta M_{\text{halo}} \approx 90 \) \( \text{pc cm}^{-3} \)), and therefore is more likely than M31 to also dominate the scattering.

If we were to assume that \( \Delta\nu_{\text{d}} \approx 40 \) MHz (at 1.37 GHz, which translates to \( \tau \approx 4 \) ns) is attributable to scattering in the M33 halo, then we get \( (\tilde{F} \times \Delta M^2)_i \approx 0.23 / A_r \text{pc}^{-4/3} \text{cm}^{-1/3} \text{cm}^{-1/3} \) for \( z_{\text{host}} = 0.5 \). A smaller source red-shift would increase \( d_{\text{LOS}} / d_{\text{host}} \), resulting in an even smaller value of \( (\tilde{F} \times \Delta M^2)_i \). For a halo DM contribution of about 90 \( \text{pc cm}^{-3} \) this estimate of \( (\tilde{F} \times \Delta M^2)_i \) yields \( \tilde{F}_i \approx (2.7 \times 10^{-5}) / A_r \text{pc}^{-2/3} \text{cm}^{-1/3} \), which is three orders of magnitude smaller than the upper limit we infer for the Milky Way halo. Using a smaller \( \Delta M_{\text{halo}} \approx 50 \text{pc cm}^{-3} \) increases \( \tilde{F} \) to \( \tilde{F}_i \approx (9 \times 10^{-5}) / A_r \text{pc}^{-2/3} \text{cm}^{-1/3} \). Generally speaking, if \( \tilde{F} \) is about a factor of 10 larger, then the pulse broadening from the halo would be 10 times larger and the scintillation bandwidth 10 times smaller. On the other hand, if M31 were to contribute more significantly to the DM then \( \tilde{F}_i \) would be smaller than our estimate. While there is a range of reasonable values for \( \tilde{F}_i \), it appears that scattering in the M33 halo is negligible.

Connor et al. (2020) use a different approach to evaluate the scattering of FRB 191108. They estimate a scattering angle from the decorrelation bandwidth in order to obtain an estimate of the diffractive scale and rms electron density fluctuations in the halo. Making assumptions about the outer scale and the relationship between the mean density and rms density fluctuations, they find a mean electron density for the halo that is larger than expected, and conclude that if the scattering occurs in M33, then it is more likely from cool clumps of gas embedded in the hot, extended halo. Prochaska et al. (2019) use a similar methodology to estimate a mean density for the halo of FG−181112. Rather than make an indirect estimate of \( n_e \) in each halo, our analysis yields a direct constraint on \( (\tilde{F} \times \Delta M^2)_i \) from observable quantities. The corresponding estimates of \( \tilde{F} \) are sufficient to demonstrate that very little scattering occurs along either of these FRB LoS through the galaxy haloes. Further deconstructing \( \tilde{F} \) will require more information about the outer and inner scales of turbulence, which may differ from halo to halo.

### 5. DISCUSSION

We present a straightforward methodology for constraining the internal electron density fluctuations of galaxy haloes using FRB scattering measurements. The pulse broadening time \( \tau \propto \tilde{F} \times \Delta M^2 \), where the fluctuation parameter \( \tilde{F} \)
quantifies the amount of scattering per unit DM and is directly related to the density fluctuation statistics. We analyze two case studies, FRB 121102 and FRB 180916, and find their scattering measurements to be largely consistent with the predicted scattering from the Galactic disk and spiral arms, plus a small or negligible contribution from the Galactic halo. A likelihood analysis of their scintillation bandwidths and angular broadening places an upper limit on the product of the Galactic halo DM and fluctuation parameter \((\bar{F} \times \Delta M^2)_{MW,h} < 250/A_\tau \text{ pc}^{4/3} \text{ km}^{-1/3} \text{ cm}^{-1/3}\), where \(A_\tau\) is the dimensionless constant relating the mean scattering time to the \(1/e\) time of a scattered pulse. This estimate can be used to calculate the pulse broadening delay induced by electron density fluctuations in the halo, independent of any assumptions about the electron density distribution of the Galactic halo. The upper limit on \((\bar{F} \times \Delta M^2)_{MW,h}\) implies a maximum amount of pulse broadening from the Galactic halo \(\tau_{MW,h} < 12 \mu s\) at 1 GHz.

While the DM contribution of the Milky Way halo to FRB DMs is still poorly constrained, we adopt a Gaussian PDF for the observed DM of the halo to estimate \(\bar{F}_{MW,h} < 0.03/A_\tau \text{ pc}^{-2/3} \text{ km}^{-1/3}\). We compare this to the fluctuation parameter of the Galactic thick disk using the distribution of \(\tau/DM^2\) for all Galactic pulsars at high Galactic latitudes with pulse broadening measurements. We measure the fluctuation parameter of the thick disk to be \(\bar{F}_{\text{disk}}^{\text{thick}} = (3\pm2) \times 10^{-3} \text{ pc}^{-2/3} \text{ km}^{-1/3}\), about an order of magnitude smaller than the halo upper limit. At high Galactic latitudes, the thick disk will only cause a scattering delay on the order of tens of nanoseconds at 1 GHz. Larger samples of FRBs and continued X-ray observations of the Galactic halo will refine our understanding of the DM contribution of the halo and may modify our current constraint on \(\bar{F}_{MW,h}\), which is only based on two LoS through the halo. While we assume for simplicity that the density distribution of the halo is spherically symmetric, \(\bar{F}_{MW,h}\) and \(DM_{MW,h}\) will vary between different LoS through the halo, and an extension of our analysis to a larger sample of FRBs may yield a more constraining limit on the average fluctuation parameter of the halo.

Extrapolating the scattering formalism we use for the Galactic halo to intervening galaxies, we examine two examples of FRBs propagating through intervening haloes, FRB 181112 and FRB 191108. The observed upper limits on each halo’s contribution to \(\tau\) are \(\tau_{h,h} < 21 \mu s\) at 1.3 GHz for FRB 181112 (Cho et al. 2020) and \(\tau_{h,i} < 36 \mu s\) at 1.37 GHz for FRB 191108 (Connor et al. 2020). We find \((\bar{F} \times \Delta M^2)_{h,h} < 13/A_\tau \text{ pc}^{4/3} \text{ km}^{-1/3} \text{ cm}^{-1/3}\) for FRB 181112 and \((\bar{F} \times \Delta M^2)_{h,i} < 0.2/A_\tau \text{ pc}^{4/3} \text{ km}^{-1/3} \text{ cm}^{-1/3}\) for FRB 191108. Both estimates fall within the upper limit for the Milky Way halo, and all of these haloes have small to negligible scattering contributions for the FRBs considered in this paper.

We also model the DM contribution of each intervening halo to find nominal constraints on \(\bar{F}\). The values of \(\bar{F}\) from our analysis of FRB 181112, FRB 191108, the LMC, the Galactic halo, the Galactic thick disk, and the values of \(\bar{F}\) used in NE2001 for the Galactic anti-center and inner Galaxy are all assembled in Figure 6. The uncertainties associated with the conversion factor \(A_\tau\) and the halo DMs are also shown. The values of \(\bar{F}\) for M33, FG–181112, the Galactic halo, and the LMC are essentially point estimates because they are based on individual sources, while the estimates provided for the Galactic thick disk, anti-center, and inner Galaxy are based on the population of Galactic pulsars. Broadly speaking, the \(\bar{F}\) limit for the Galactic halo is similar to that of the disk and spiral arms in the anti-center direction, and is about an order of magnitude larger than the fluctuation parameter of the thick disk. The value of \(\bar{F}\) for the LMC is similar to that of the inner Milky Way because it is based on the pulse broadening of B0540–69, which lies within a supernova remnant and hence within an enhanced scattering region. Our estimates of \(\bar{F}_{h,h}\) for both FRB 181112 and FRB 191108 indicate that very little scattering occurs in the haloes intervening their LoS.
The fluctuation parameter is directly related to the inner and outer scales of turbulence as $\bar{F} \propto (\zeta \epsilon^2 / f) (l_{w} l_{o})^{-1/3}$, where $\zeta$ and $\epsilon$ respectively describe changes in the mean density between different gas cloudlets and the variance of the density fluctuations within cloudlets. While the inner and outer scales in the Galactic warm ionized medium (WIM) are constrained by pulsar measurements to be on the order of $100 \lesssim l_i \lesssim 1000 \text{ km}$ and $l_o \gtrsim 10 \text{ pc}$ (Spangler & Gwinn 1990; Armstrong et al. 1995; Bhat et al. 2004; Rickett et al. 2009), the corresponding scales in hot halo gas are probably much larger. Given the size of the halo, $l_o$ could be on the order of tens of kpc. The inner scale could also be larger if it is related to the proton gyroradius and the magnetic field strength is smaller in the halo than in the disk, which is probably the case given that the rotation measures of extragalactic sources tend to be larger closer to the Galactic plane (Han 2017). Given that $f$, $l_o$, and $l_i$ are all probably larger in the halo than in the disk, we would expect $\bar{F}_{\text{MW,h}}$ to be much smaller than $\bar{F}_{\text{disk}}$. If we further expect the Milky Way halo to be similar to other galaxy haloes like FG–181112 and M33, then $\bar{F}_{\text{MW,h}}$ would likely be less than $10^{-3} \text{ pc}^{-2/3} \text{ km}^{-1/3}$. However, our current constraints allow $\bar{F}$ to be larger in the halo than in the disk, which suggests that the upper limit for $\bar{F}_{\text{MW,h}}$ is not constraining enough to make any further conclusions about $\zeta$, $\epsilon^2$, $f$, $l_o$, and $l_i$ in the halo.

On the other hand, quasar absorption studies of the CGM of other galaxies (mostly at redshifts $z \gtrsim 2$) indicate the presence of $\sim 10^4 \text{ K}$ gas (Hennawi et al. 2015; Lau et al. 2016; McCourt et al. 2018), suggesting that the CGM is a two-phase medium consisting of warm gas clumps embedded in a hot ($10^6 \text{ K}$) medium (McCourt et al. 2018). Using a cloudlet model based on the simulations of McCourt et al. (2018), Vedantham & Phinney (2019) demonstrate that a clumpy CGM could significantly scatter FRBs. Our empirical constraints on $\bar{F}$ are largely independent of any assumptions about the physical properties of the scattering medium. We assume a halo density model to estimate the DM contribution of a halo, although mapping of ionized and neutral high-velocity clouds in the Galactic CGM indicates that the DM is likely dominated by the hot gas (Prochaska & Zheng 2019). As a composite parameter, $\bar{F}$ is insensitive to a broad range of assumptions about gas temperature or clumps, and could serve as an independent test of the two-phase model for the CGM. In a clumpy, cooler CGM, the inner and outer scales of turbulence would be similar to those in the WIM and $f \ll 1$, and $\bar{F}$ would be larger than it would be in a hot medium with a larger filling factor and scale size. Adopting fiducial values of $\epsilon^2 = \zeta = 1$, $f \sim 10^{-4}$ (the value used by Vedantham & Phinney (2019)), $l_i \sim 100 \text{ km}$, and $l_o \sim 10 \text{ pc}$ gives $\bar{F} \sim 500 \text{ pc}^{-2/3} \text{ km}^{-1/3}$. This estimate is orders of magnitude larger than our results for the Galactic halo and the foreground haloes of FRBs 181112 and 191108, suggesting that halo gas probed by these LoS is either not dominated by cooler clumps, or that $f$, $l_o$, and $l_i$ are significantly different in the clumpy CGM than otherwise assumed by McCourt et al. (2018) and Vedantham & Phinney (2019).

A more stringent comparison of hot gas in the halo and the WIM will require a larger sample of precise FRB scattering measurements. Regardless, the nominal range of $\bar{F}$ constrained for the Galactic halo and the haloes intervening FRB 181112 and FRB 191108 demonstrate the range of internal properties that different galaxy haloes can have. A broader sample of FRB scattering measurements with intervening halo associations will expand this range and may potentially reveal an interesting diversity of galaxy haloes.

Many more FRBs with intervening galaxy haloes will likely be discovered in the near future. In these cases, the amount of scattering to be expected from the intervening haloes will depend not only on the fluctuation parameter $\bar{F}$ and DM of the halo, but also on the relative distances between the source, halo, and observer, and the effective path length through the halo. Depending on the relative configuration, an intervening halo may amplify the amount of scattering seen in FRB experiences by factors of 100 or more relative to the amount of scattering expected from the Milky Way halo. However, plausibly attributing scattering to an intervening halo will still require careful consideration of the FRB host galaxy, which in many cases may be the dominant source of FRB scattering.

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