The interplay of strong Coulomb interactions and of topology is currently under intense scrutiny in various condensed matter and atomic systems. One example of this interplay is the phase competition of fractional quantum Hall states and the Wigner solid in the two-dimensional electron gas. Here we report a Wigner solid at $\nu = 1.79$ and its melting due to fractional correlations occurring at $\nu = 9/5$. This Wigner solid, that we call the reentrant integer quantum Hall Wigner solid, develops in a range of Landau level filling factors that is related by particle-hole symmetry to the so called reentrant Wigner solid. We thus find that the Wigner solid in the GaAs/AlGaAs system straddles the partial filling factor 1/5 not only at the lowest filling factors, but also near $\nu = 9/5$. Our results highlight the particle-hole symmetry as a fundamental symmetry of the extended family of Wigner solids and paint a complex picture of the competition of the Wigner solid with fractional quantum Hall states.
one of the most stunning effects of strong interactions is the formation of interaction-driven topological states, such as the fractional quantum Hall states (FQHSS) developing in clean two-dimensional electron gases (2DEGs)\(^1\). A fundamental symmetry that governs the fractional quantum Hall regime is the particle–hole symmetry\(^2\)–\(^4\). While particle–hole symmetry is commonly applied to the physics of the 2DEG, highly non-trivial aspects of this symmetry were not appreciated until recently. Indeed, particle–hole symmetry near the Fermi sea of composite fermions was found to have deep implications for the understanding of this Fermi sea\(^5\), and the examination of particle–hole symmetry for the even denominator FQHSS broadened concepts of topological order significantly\(^6\)–\(^11\).

Besides generating novel topological states, strong interactions in clean 2DEGs also order charge carriers into electron solids\(^12\),\(^13\). Due to the flat nature of energy bands at high magnetic fields, one way for electrons to minimize their Coulomb energy is through ordering into a triangular lattice called the Wigner solid (WS). The insulating phase at Landau level filling factors \(v<1/5\) forming in the 2DEG in GaAs/AlGaAs heterostructures has long been interpreted as a WS, often called the high-field WS (HFWS)\(^14\)–\(^18\). Results from a variety of experiments, such as nonlinear transport\(^19\)–\(^21\), noise\(^22\), dielectric constant measurement\(^23\), microwave spectroscopy\(^24\)–\(^26\), composite fermion commensuration oscillations\(^27\), and screening measurements\(^28\) have strengthened this interpretation. Since the HFWS and the terminal FQHSS at \(v=1/5\) form in the same range of magnetic fields, these two phases often display a competition that determines the structure of the phase diagram\(^14\)–\(^16\),\(^19\)–\(^20\),\(^23\).

Wigner crystallization in the 2DEG is energetically favored not only at \(v<1/5\) but also at other values of the filling factor. These WSs bear different names. For example, the WS that develops in the HFWS at \(v<1/5\) by ordering into a triangular lattice is called the Wigner solid (WS). The insulating phase at Landau level filling factors \(v<1/5\) forming in the 2DEG in GaAs/AlGaAs heterostructures has long been interpreted as a WS, often called the high-field WS (HFWS)\(^14\)–\(^18\). Results from a variety of experiments, such as nonlinear transport\(^19\)–\(^21\), noise\(^22\), dielectric constant measurement\(^23\), microwave spectroscopy\(^24\)–\(^26\), composite fermion commensuration oscillations\(^27\), and screening measurements\(^28\) have strengthened this interpretation. Since the HFWS and the terminal FQHSS at \(v=1/5\) form in the same range of magnetic fields, these two phases often display a competition that determines the structure of the phase diagram\(^14\)–\(^16\),\(^19\)–\(^20\),\(^23\).

Here, we report the observation of an electron solid near the filling factor \(v=1.79\) in clean 2DEGs confined to GaAs/AlGaAs hosts. The transport signatures of this phase, a vanishing magnetoresistance accompanied by a Hall resistance that is quantized to \(R_{xy}=h/2e^2\), allow us to infer that this electron solid is a WS. The WS at \(v=1.79\) develops near the IQHWS, but it is distinct from the latter. We, therefore, term this WS the reentrant IQHWS (RIQHWS). We find that the RIQHWS is related by particle–hole symmetry to the RWS that develops at high magnetic fields. This means that the elementary building blocks of the RIQHWS are quasiholes, rather than quasielectrons, and we establish that particle–hole symmetry is a fundamental symmetry that extends over the larger family of WSs. In addition, our observations reveal that the phase competition of the RIQHWS and an FQHS that forms nearby is a generic property for 2DEGs with strong interactions, which has an imprint on the wider phase diagram.

Results and discussion
Magnetotransport of our Sample 1 measured at \(T=12\) mK reveals a rich structure exhibiting various known ground states of the 2DEG. In Fig. 1 we identify a few prominent examples, such as the \(v=2\), \(3\), and \(4\) IQHS, several FQHSS, including a rich structure in the \(N=1\) Landau level\(^44\)–\(^46\). In addition, the \(v>4\) range is dominated by various electronic stripe and bubble phases\(^47\)–\(^51\). We focus our attention on the range of filling factors delimited by the \(v=2\) IQHS and the \(v=5/3\) FQHS, i.e., the region near \(B=7.25\) T. In this region in Fig. 1, we observe structures in the longitudinal magnetoresistance \(R_{xx}\).

The region \(5/3<v<2\) is shown in greater detail in Fig. 2. In the \(T=300\) mK magnetoresistance \(R_{xx}\) trace of Fig. 2, three local minima are signaling the development of FQHSS. One is at \(v=nh/eB=12/7\). Here, \(n\) is the electron density, \(B\) is the magnetic field, \(e\) is the electron charge, and \(h\) is Planck’s constant. A resistance minimum at \(v=12/7\) was attributed to an FQHSS\(^52\). In addition, in the \(T=300\) mK \(R_{xx}\) trace, there is another so far unreported resistance minimum at a higher filling factor \(v=9/5\). Hall resistance measurements at these two filling factors, \(v=12/7\) and \(v=9/5\), reveal inflections close to \(7h/12e^2\) and \(5h/9e^2\), respectively. These data are therefore suggestive of developing fractional correlations associated with FQHSS at \(v=12/7\) and 9/5. These and other Landau level filling factors of interest are marked in Fig. 2 by dashed vertical lines.

Observation of a collective insulator at \(v=1.79\) and its competition with the \(v=9/5\) FQHS. Even though at \(T=300\) mK we identified similar behavior at both \(v=12/7\) and 9/5, we find that the temperature evolution of the magnetoresistance at these two filling factors is very different. Indeed, as the temperature is

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**Fig. 1** Magnetoresistance \(R_{xx}\) and Hall resistance \(R_{xy}\) of Sample 1 over a broad range of magnetic fields \(B\). Traces are obtained at the temperature \(T=12\) mK. Numerical labels indicate notable Landau level filling factors \(v\). Structures of interest develop near \(B=7.25\) T, in the range of filling factors \(5/3<v<2\).
lowered from $T = 300$ mK, the inflection in the Hall resistance at $\nu = 12/7$ persists. As shown in Fig. 2, at the lowest temperature of $T = 12$ mK, $R_{xx}$ maintains its local minimum and $R_{xy}$ is quantized to $7h/12e^2$. However, $R_{xy}$ at this filling factor changes very little with temperature. This indicates a weak FQHS at $\nu = 12/7$. In contrast, the behavior near $\nu = 9/5$ is qualitatively different. The local minimum in $R_{xx}$ at $\nu = 9/5$ is still present at $T = 100$ mK, but it rides on a magnetoresistance background that rises with lowering the temperature. Indeed, as seen in Fig. 2, $R_{xx}$ near $\nu = 9/5$ at $T = 100$ mK is approximately doubled as compared to that at $T = 300$ mK. Furthermore, the local minimum in $R_{xx}$ at $\nu = 9/5$ is extremely weak at $T = 75$ mK and it is no longer present at $T < 75$ mK. We conclude that at temperatures $T \geq 75$ mK, our sample exhibits signs of fractional correlations at $\nu = 9/5$. However, at the lowest accessed temperatures, our sample does not support a fractional quantum Hall ground state at $\nu = 9/5$.

An unusual feature of the $T = 75$ mK $R_{xx}$ data is that there is a local minimum in $R_{xx}$ which, however, is at a distinctively different filling factor than $9/5$. This new minimum in $R_{xx}$, marked by arrows in Fig. 2, develops at $\nu = 1.79$. This filling factor is not a part of the standard sequence of fractional valued filling factors; therefore, the minimum in $R_{xx}$ at $\nu = 1.79$ most certainly cannot be associated with an FQHS. This conclusion is strengthened by our observations of the Hall resistance at $T \leq 75$ mK, which deviates significantly from any possible plateau values expected for an FQHS that may develop near $\nu = 1.79$. Instead, as the temperature is lowered, $R_{xx}$ at $\nu = 1.79$ gradually decreases towards $R_{xx} = 0$ and $R_{xy}$ becomes quantized to $R_{xy} = h/2e^2$. This is seen in the $T = 23$ mK and $T = 12$ mK traces shown in Fig. 2. Such a behavior signals collective localization, i.e., the development of an electron solid. In Fig. 2 we marked this electron solid at $\nu = 1.79$ with arrows. Since a similar transport signature is present along a perpendicular crystal direction, this electron solid is isotropic.

Relating the electron solid at $\nu = 1.79$ and the IQHWS. In order to understand the nature of the electron solid forming at $\nu = 1.79$, we recall that complex electron solids called electronic bubble phases form in high Landau levels. Bubble phases are a triangular lattice of electron bubbles, formed of electrons clustered together. The clustering of several electrons into a bubble is afforded by the nodal structure of the single electron wavefunction and it is consistent with the most recent experimental observations. The electronic wavefunction in the $N = 0$ Landau level does not have any nodes; therefore, among the electronic bubble phases, only the one-electron bubble phase may form, a phase that is identical to the WS. Other charge-ordered phases we have to consider are the ones constituted by quasiparticles of FQHSs, such as the WS of composite fermions. However, because the Hall resistance is not quantized to a fractional value, in our experiment we have no evidence of the formation of such quasiparticles at $\nu = 1.79$. Since our electron solid forms in the $N = 0$ Landau level, where multi-electron bubble phases are not expected, and since at $\nu = 1.79$ we have no evidence of quasiparticles of FQHSs, we identify the solid at this filling factor with a WS.

As discussed in the “Introduction,” WSs termed IQHWSs are known to form in the flanks of integer plateaus, specifically in the flanks of the $\nu = 2$ IQHS as well. IQHWSs form within the range of filling factors $0 < |\nu^*| < 1/5$, albeit the stability range is expected to be temperature and disorder dependent. Here, the partial filling factor near $\nu = 2$ is $\nu^* = \nu - 2$. The partial filling factor of the $\nu = 1.79$ WS is $|\nu^*| = 0.21$, which is clearly outside the range of formation of the IQHWS. Hence, the $\nu = 1.79$ WS forms at a larger quasiparticle density than the nearby IQHWS. When a ground state becomes unstable for a small range of parameters and then reappears, it is called a reentrant ground state. We will thus refer to the $\nu = 1.79$ WS as the RIQHWS.

Before further analysis, we check that the filling factor of the formation of the RIQHWS is independent of the experimental
The range of RIQHWS forms in the range $9/5 < |\nu| < 2/9$ and it is indeed related by the same $\nu \leftrightarrow 2 - \nu$ symmetry to the $1/5 < \nu < 2/9$ range of the RWS\textsuperscript{16}. This means that the RWS is a WS of electrons, whereas the RIQHWS is a WS of hole quasiparticles and both of these solids form in the same range of partial filling factors. The stability ranges of the various WSs, including that of the RIQHWS, and their symmetries are on display in Fig. 4. All WSs marked in this figure share the partial filling factor $|\nu^*| = 1/5$ and obey particle–hole symmetry. As a consequence, we found that the RIQHWS, the newest member of the WS family, together with other WSs, admit particle–hole symmetry as a fundamental property.

Our results find a natural explanation if one assumes that the IQHWS and the RIQHWS are part of the same monolithic WS phase. This monolithic WS phase straddles the filling factor $\nu = 9/5$, i.e., it is present on both sides of $\nu = 9/5$. The resistive peak in $R_{xx}$ seen at $\nu = 9/5$ in Fig. 3 and also in Fig. 2 at the four lowest temperatures is then due to melting of this WS due to remnant fractional correlations at this filling factor. The observed magnetotransport thus indicates a competition of two strongly correlated ground states: the WS and the $\nu = 9/5$ FQHS. Invoking such remnant correlations at $\nu = 9/5$ is not unreasonable since their effect may be observed in Fig. 2 as an incipient FQHS at $75 < T < 300$ mK. These fractional correlations in our sample are, however, not strong enough to allow the development of a fully quantized fractional quantum Hall ground state at $\nu = 9/5$. Indeed, according to data plotted in Fig. 3, $R_{xx}(\nu = 9/5) \neq 0$ and $R_{xy}(\nu = 9/5) \neq 5h/9e^2$ for both samples. $R_{xy}$ at $\nu = 9/5$ has a shoulder in Sample 2, but $R_{xy}(\nu = 9/5)$ is $3.4\%$ less than $5h/9e^2$. A similar situation was encountered in early experiments on low

![Fig. 3 Reentrant integer quantum Hall Wigner solids in a variable density sample and a sample of fixed density. a Waterfall plots of the magnetoresistance $R_{xx}$ and Hall resistance $R_{xy}$ as plotted against the inverse filling factor $1/\nu$ of Sample 1 as prepared at different electron densities. Measurements were performed at the temperature of $T = 12$ mK. b Magnetoresistance $R_{xx}$ and Hall resistance $R_{xy}$ as plotted against the inverse filling factor $1/\nu$ of Sample 2 of a fixed electron density. This density is significantly lower than that of Sample 1. Measurements were performed at the temperature of $T = 5.1$ mK. Labels on traces indicate electron densities $n$ in units of $10^{11}$ cm$^{-2}$. Vertical dashed lines mark locations and values of filling factors $\nu$ of interest and arrows mark the reentrant integer quantum Hall Wigner solid (RIQHWS). With the exception of traces at the highest density, traces for Sample 1 are shifted vertically upward for clarity.

Relating the electron solid at $\nu = 1.79$ and other WSs. Further insight on the nature of the RIQHWS may be gained from considering particle–hole symmetry, a fundamental symmetry of the Hamiltonian of electrons in two dimensions that connects ground states at different filling factors sharing the same absolute value of the partial filling factor $|\nu^*|^2$. The $2 - 1/5 < \nu < 2$ range of stability of the IQHWS and the range of stability $\nu < 1/5$ of the HFWS share the same range of partial filling factors $|\nu^*| < 1/5$. It is said that the IQHWS and the HFWS are linked by the $\nu \leftrightarrow 2 - \nu$ particle–hole symmetry, or HFWS $\leftrightarrow$ IQHWS. We notice that the RIQHWS and the RWS are also linked by particle–hole symmetry, i.e., RWS $\leftrightarrow$ RIQHWS. Indeed, the RIQHWS forms in the range $9/5 = 2 - 1/5 < \nu < 2 - 2/9 = 16/9$. The range of filling factors of $2 - 1/5 < \nu < 2 - 2/9$, the RIQHWS corresponds to partial fillings $1/5 < |\nu^*| < 2/9$ and it is indeed related by the same $\nu \leftrightarrow 2 - \nu$ symmetry to the $1/5 < \nu < 2/9$ range of the RWS\textsuperscript{16}. This means that the RWS is a WS of electrons, whereas the RIQHWS is a WS of hole quasiparticles and both of these solids form in the same range of partial filling factors. The stability ranges of the various WSs, including that of the RIQHWS, and their symmetries are on display in Fig. 4. All WSs marked in this figure straddle the partial filling factor $|\nu^*| = 1/5$ and obey particle–hole symmetry. As a consequence, we found that the RIQHWS, the newest member of the WS family, together with other WSs, admit particle–hole symmetry as a fundamental property.
mobility 2DEGs in which insulating behavior was seen on both sides of $\nu = 1/5$, i.e. in which both the HFWS and the RWS were present, but an FQHS at $\nu = 1/5$ between these WSs did not fully develop\cite{43,44}. Therefore our results show that the competition of WSs and the FQHS that they straddle is a generic feature of phase competition in regions where WSs form.

The WSs discussed so far form in the $N = 0$ orbital Landau level, i.e., in the $0 < \nu < 2$ range. We suggest that the above properties of the WS may be further extended even into the $N = 1$ Landau level. The IQHWS was known within the $2 < \nu < 2 + 1/5$ range\cite{31,34}, and in an earlier publication, a WS was found at $\nu = 2.21$, clearly confined to the $2 + 1/5 < \nu < 2 + 2/9$ range\cite{39,60}. For this WS $1/5 < |\nu^*| < 2/9$ and based on our arguments put forth earlier, we identify this WS at $\nu = 2.21$ with the RIQHWS. Furthermore, there is a monolithic WS phase in this region that straddles both sides of $\nu = 2 + 1/5$ FQHS and which is melted by the fractional correlations of this FQHS. This RIQHWS is related by particle–hole symmetry to both the RIQHWS at $\nu = 1.79$ and to the RWS, and it is included in the diagram shown in Fig. 4. We note that in Sample 1 this WS at $\nu = 2.21$ did not develop. The reason for this is unknown, but differences in density, mobility, different measurement temperatures, and a different background impurity profile due to the different growth chambers are possible culprits.

Most recently, electron solids in the $N = 0$ Landau level were also reported close to $\nu = 1$\cite{38,39}. Some of these are in the range of filling factors associated with the IQHWS. Others, such as the ones forming at $\nu = 0.78$ in a 42, 44\cite{38}, and a 65 nm quantum well sample\cite{39} develop at partial filling factor $|\nu^*| = 0.22$. These electron solids were first interpreted as WSs\cite{38}, and then later as exotic solids formed of composite fermions\cite{39}. The partial filling factor of these electron solids is stunningly close to that of the RIQHWS we found. One possibility is thus that these WSs are identical to the RIQHWS, particle–hole symmetric counterparts of the RWS. Nonetheless, the nature of these electron solids remains to be determined; softening of the short-range part of the effective electron–electron interaction that occurs in samples with wide quantum wells is known to tune the formation of electron solids and may stabilize various types of electronic solids.

A shared feature of the WSs in our electron samples is that they straddle the partial filling factor $|\nu^*| = 1/5$. In other systems, however, WSs may straddle other partial filling factors. For example, in two-dimensional hole gases (2DHGs), the WS straddles $\nu^* = \nu = 1/361$–63. This difference between 2DEGs and 2DHGs is attributed to the significantly larger ratio of the Coulomb interaction and Fermi energies in the latter\cite{61,62}. Furthermore, the WS in 2DEGs in very narrow quantum wells straddles $\nu = 1/364$ and WSs form in samples with added short-range disorder near $|\nu^*| = 1/365$. In yet other systems, phases associated with the WS may straddle more than just one FQHS. This is the case of a 2DEG realized in the ZnO/MgZnO system in which the WS was found to straddle several FQHS\cite{41}. These experiments suggest that disorder influences the range of stability of the WS and highlight that there is still much to be understood about disorder effects.

**Conclusions**

We reported complex features of the magnetoresistance at $\nu = 1.79$ in the $N = 0$ Landau level of two high-mobility 2DEGs confined to GaAs/AlGaAs. In contrast to similar transport features in high $N > 2$ Landau levels, the ground state at $\nu = 1.79$ is associated with a WS. Because of its proximity to the IQHWS, we named this WS the RIQHWS. Based on the stability region in the filling factor space, the RIQHWS and another RIQHWS reported at $\nu = 2.21$ in the $N = 1$ Landau level\cite{39,60} can both be understood as the particle–hole symmetric counterparts of the RWS. Our results indicate that WSs in the GaAs/AlGaAs system straddle the partial filling factor $|\nu^*| = 1/5$, that particle–hole symmetry of the WS is more pervasive than previously thought, and that this symmetry leads to competing WSs and FQHSs in unexpected parts of the phase diagram.

**Methods**

**Samples.** Sample 1 is a 2DEG confined to a 30 nm GaAs quantum well that is part of a GaAs/AlGaAs heterostructure. The density of this sample is $n = 3.05 \times 10^{11}$ cm$^{-2}$ and low-temperature mobility is $\mu = 3.2 \times 10^6$ cm$^2$/Vs. The 2DEG is doped in a superlattice. The sample state was prepared with illumination with a red light-emitting diode at 10 K according to a procedure described in ref. 66. Sample 2 is also a 2DEG confined to a GaAs/AlGaAs heterostructure, but differs in several aspects from Sample 1. It belongs to the most recent generation of high-mobility samples\cite{67}. Its density is significantly less than that of Sample 1, $n = 1.0 \times 10^{11}$ cm$^{-2}$, and its mobility is $\mu = 3.5 \times 10^6$ cm$^2$/Vs. The width of the confining quantum well in Sample 2 is 49 nm, significantly larger than that of Sample 1. We note that since the mobility of Sample 2 is very large, the second electric subband in this sample is not populated.

**Experimental techniques.** Magnetotransport measurements were performed in a van der Pauw sample geometry using the standard lock-in technique. The square-shaped samples have eight indium ohmic contacts placed in the corners and the middle of the sides. The excitation current used was 3 nA. Sample 1 was mounted in a vacuum on the copper tail of our dilution refrigerator, reaching the lowest estimated temperature of $T = 12$ mK. In contrast, Sample 2 was mounted inside a He-3 immersion cell, with the lowest bath temperature reached in our current measurement being $T = 3.1$ mK\cite{68}. In this setup, the electronic temperature follows closely that of the bath\cite{68}. For temperature measurements, a carbon thermometer was used\cite{69}, which below 100 mK was calibrated against a He-3 quartz tuning fork viscometer\cite{69}.

The density of Sample 1 was reduced from its maximum value by using a cold illumination procedure described in ref. 66. As a result of this process, sample parameters changed from $3.05 \times 10^{11}$ cm$^{-2}$ and $\mu = 3.2 \times 10^6$ cm$^2$/Vs to $2.70 \times 10^{13}$ cm$^{-2}$ and $\mu = 1.3 \times 10^6$ cm$^2$/Vs. We passed bursts of current of 1 µA through a red light-emitting diode for a duration of about 5 s, while the sample was kept near the base temperature of the refrigerator and at $B = 0$. For the illumination procedure, it is critical that the light beam covers the area of the sample uniformly. To achieve this, the diode faces the sample, it is centered onto the sample, and it is mounted at a distance of 1.5 cm from the sample.
Data availability
The data that support the findings of this study are available from the corresponding author upon request.

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**Author contributions**

V.S. and S.A.M. performed low-temperature transport measurements. L.N.P. and K.W.B. produced MBE-grown GaAs/AlGaAs samples and characterized them. V.S., S.A.M. and G.A.C. conceived the project, analyzed the data, and wrote the manuscript.

**Competing interests**

The authors declare no competing interests.

**Additional information**

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