Determination of the contributions of degenerate and non-degenerate

two-photon absorption response in silicon avalanche photodiode for

infrared photon detection

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Abstract:

The study of non-linear interactions in semiconductor photo-electronic devices to achieve effective and fast photon identification is an ongoing and important task. We investigated the specific contribution of degenerate and non-degenerate two-photon absorption (D-TPA and ND-TPA) response in silicon avalanche photodiode (Si-APD) for infrared photon detection at room temperature. We experimentally demonstrated that when the two laser pulses overlapped, the average D-TPA quantum detection efficiencies at 1800 nm, and that at 1550 nm were measured as $3.3 \times 10^{-16}$ counts$\cdot$pulse$/$photon$^2$, $4.3 \times 10^{-15}$ counts$\cdot$pulse$/$photon$^2$, respectively. And the ND-TPA quantum detection efficiency of 1800 nm and 1550 nm was measured to be $7.9 \times 10^{-16}$ counts$\cdot$pulse$/$photon$^2$. This study provides a solution for the practical infrared photon detection devices based on TPA effect in Si-APDs.

Keywords: degenerate and non-degenerate two-photon absorption, infrared photon detection, silicon avalanche photodiode.

1. Introduction

Since the invention of the transistor more than half a century ago, semiconductor devices have been revolutionizing our daily lives, such as computers, smartphones, virtual reality devices and so forth. The photo-electronic devices such as photodetectors have become increasingly important by supporting various modern techniques. And recently, non-linear optical devices begin to develop vigorously to convert the infrared light to the visible regime or vice versa because the main information carrier in the
optical cable network is in the infrared but detectors of infrared light is not as good as its counterpart for the visible regime [1,2]. Especially, in the fiber-based quantum cryptography where the information is encoded with single photons at the telecom wavelengths, different infrared single-photon detectors are developed including single-photon frequency upconversion detectors [3-5]. Moreover, non-linear optical devices based on high-order transitions between energy levels such as two-photon absorption (TPA) effect enables ultra-fast signal processing [6-8].

Non-linear optical equipment are commonly based on frequency-upconversion or TPA effect to achieve rapid infrared light signal processing and detection. The frequency upconversion scheme is based on the sum-frequency generation process where the wavelength of the signal photons is transformed into the shorter wavelength region with the preservation of all the quantum characteristics and the upconverted photons finally impinge on the active area of a silicon-based detector for detection [9,10]. However, in the frequency upconversion system, special nonlinear crystals are designed and cut to fulfill the phase-matching conditions by adjusting the tilting angle and the operation temperature to maintain the momentum conservation for a high conversion efficiency [11-14]. At the same time, the TPA effect caused by the free electron in a semiconductor photodetector that absorbs two photons simultaneously, thereby achieving a transition from the ground state to the excited state and releasing a photoelectron by returning to the ground state can also be used for the detection of infrared photons [15,16]. For example, in a Si-avalanche photodiode (Si-APD) or other detector, the electron-hole pairs are created by TPA of the infrared photons and give
rise to a photo-avalanche pulse output directly [17,18]. Infrared photon detection based on TPA effect has many advantages over the frequency upconversion scheme since the TPA effect is not constrained by the phase matching, and can provide a wide operating spectral range, making the TPA scheme cheap and easy to integrate with other devices. In addition, the induced photocurrent of TPA is almost insensitive to the polarization state of the incident light.

In the TPA process, if the energies of the two absorbed photons are the same, it is the so-called the degenerate two-photon absorption (D-TPA), otherwise it is the so-called the non-degenerate two-photon absorption (ND-TPA). The TPA effect of semiconductors has been studied in different materials and structures. It has been experimentally demonstrated that the TPA effect can lead to an enhancement factor up to 100-1,000 in direct-bandgap semiconductors [6]. The extremely ND-TPA in GaN photodiodes is utilized to perform scanned imaging of three-dimensional structures by infrared femtosecond laser pulse illumination [19]. The TPA effect in the commercial In$_{0.81}$Ga$_{0.19}$As photodetector has been investigated to extend the nonlinear optical response to 4500 nm [20]. In addition, the nanostructured indium phosphide (InP) photodiode has been designed to detect the infrared light at room temperature using ND-TPA, and owing to the nanostructure, the photocurrent shows a gain of 24 with respect to the bulk response of InP [21]. The TPA effect has also been considered in silicon materials. For instance, a full band structure of TPA in bulk silicon has been theoretically calculated [22], and the D-TPA and Kerr coefficient of bulk Si for wavelength at 850 nm to 2200 nm has been measured in the experiment [23]. But the
specific contribution value of D-TPA and ND-TPA effects in silicon photodetectors for infrared light detection has not been investigated so far as we known.

In this paper, we determined the contribution of D-TPA and ND-TPA effects for infrared light detection in the Si-APD single-photon detector at room temperature. When two beams of different wavelengths were casting on the active area of the detector with temporal separation, we got that the quantum detection efficiency of D-TPA at 1800 nm and 1550 nm was about $3.2 \times 10^{-16}$ counts•pulse/photon$^2$ and $4.8 \times 10^{-15}$ counts•pulse/photon$^2$, respectively. And when the two pulses coincided in time and space, the average quantum detection efficiency for the ND-TPA of 1800 and 1550 nm was measured as $7.9 \times 10^{-16}$ counts•pulse/photon$^2$. This research has further broadened our understanding of the TPA effect in the silicon-based photo-electronics devices, and will promote the development of infrared photon detection via TPA in Si-APDs in extended applications.

2. Methods and Experimental
In the experiment, we used an ultrabroadband fiber laser to study the D-TPA and ND-TPA induced photon counting in the Si-APD. The experimental setup is sketched in Fig.1 (a). The spectrum of the ultrabroadband fiber laser covered from 1200 nm to 1900 nm. The laser was passively mode-locked at a repetition rate of 55 MHz with a 10 ps pulse duration. The average output power was up to the mW level. A beam splitter was used to split the output laser into two beams. In one beam (Beam A), we used a germanium window to select the spectrum around 1800 nm as shown in Fig.1(b), while in the other beam (Beam B), a band-pass filter was inserted to select the spectrum around 1550 nm.
around 1550 nm as shown in Fig.1(c). Two variable intensity attenuators were placed in each beam to adjust the incident photon fluxes. Then the two beams were combined by a dichroic mirror, and coupled into a fiber collimator by a lens. The photons from the combined beam were captured by a fiber-coupled single-photon detector based on Si-APD (SPCM-780-14-FC, Excelitas Tech.). The diameter of the active area of the Si-APD was about 180 μm. The photon flux incident to the Si-APD was evaluated according to the laser power and the transmittance loss of the two beams independently.

The photon-active area of the Si-APD functioned by the p-n junction of silicon, which band gap energy is 1.12 eV. According to the wavelengths of the two in beams in our experiment, we have

\[ h\omega_A, h\omega_B < E_g < 2h\omega_A, 2h\omega_B, \]

where the \( E_g \) is the bandgap energy, \( \omega_A \) and \( \omega_B \) are the optical frequencies of Beam A and Beam B, respectively. Because both photon energies were lower than the band gap of silicon, it is impossible for the Si-APD to effectively respond those infrared photons over 1100 nm by the single-photon absorption. Therefore, the Si-APD has to absorb at least two photons to trigger a photo-induced avalanche output pulse, indicating the occurrence of the two- or three-photon absorption effects. But the efficiency of three-photon absorption is much smaller than that of the TPA. So we can attribute the detection of the infrared photons in Si-APD to the TPA effect alone. Since the two beams of different optical frequencies were incident on the Si-APD simultaneously, besides the D-TPA, the ND-TPA may also happen.
3. Result and discussion

In the semiconductor, the ND-TPA effect can be described according to the coupled-wave equation [24]

$$\frac{dI_1}{dz} = -2\alpha_2(\omega_1; \omega_2)I_1I_2,$$

(2)

$$\frac{dI_2}{dz} = -2\alpha_2(\omega_1; \omega_2)I_1I_2,$$

(3)

where $I_1$ and $I_2$ are the intensities of the incident light at the optical frequencies of $\omega_1$ and $\omega_2$, respectively. And the TPA coefficient $\alpha_2$ is governed by the scattering matrix formalism with two parabolic bands in Ref [24]

$$\alpha_2(\omega_1; \omega_2) = K \frac{E_p}{n_1n_2E_g^3} F_2\left(\frac{\hbar\omega_1}{E_g}; \frac{\hbar\omega_2}{E_g}\right),$$

(4)

where $E_p$ is the Kane energy parameter, $E_g$ is the bandgap energy, $n_1$, $n_2$ are the refractive indices of the material at $\omega_1$, and $\omega_2$, respectively, and $K$ is a material independent parameter. And the function $F_2$ is written as

$$F_2(x; x') = \frac{(x + x' - 1)^2}{2^7x_1x_2^2}\left(\frac{1}{x_1} + \frac{1}{x_2}\right)^2.$$

(5)

Firstly, we studied the D-TPA in Si-APD, which means $\omega_1 = \omega_2$ in Eq.(1). In the experiment, the two beams were incident on the Si-APD independently and we recorded the photon-counting rate as a function of the incident photon flux of Beam A and Beam B as shown in Fig.2. In a semiclassical approach, the photon counting rate of the Si-APD depends on the square of the incident photon flux as
\[ C = \eta \langle N \rangle^2, \]  
(6)

where \( \eta \) represents the quantum detection efficiency by the TPA effect and \( \langle N \rangle \) is the photon flux of the incident light.

Fig. 2 Photon-counting rate as a function of the incident photon flux with a single beam at 1800 nm (a) and 1550 nm (b), respectively.

In D-TPA, the TPA response is a quadratic function of the incident light intensity. The slope of the logarithmic plots are 2.08 and 2.16 in Fig. 2 (a), and (b) respectively, which shows that the detector’s response depends quadratically on the incident photon flux both at 1800 nm and 1550 nm. We can conclude that the Si-APD’s response at these two wavelengths is dominated by the TPA effect. But note that in the measurement at 1800 nm, the incident photon flux ranges from \( 0.3 \times 10^6 \) to \( 2.8 \times 10^6 \) photons/pulse. Meanwhile, in the measurement at 1550 nm, the incident photon flux ranges from \( 0.06 \times 10^6 \) to \( 0.7 \times 10^6 \) photons/pulse. The photon counting rates were at the same level. The big difference is caused by the TPA coefficient \( \alpha_2 \) of the Si-APD at the two wavelengths.
Fig. 3 Photon counting rate as a function of the relative delay between the two beams. The red spots and the blue spots are the counting rate of the D-TPA of 1800 nm and 1550 nm, respectively. The pink triangle spots are the sum of the both D-TPA effect. And the blue triangle spots are the counting rate of the TPA of two beams.

Then, we tuned the VAs to adjust the photon counting rate of Beam A and B at about 135 kHz and 125 kHz, respectively. Both beams were injected to the detector but the pulse trains from the two were with a temporal delay much longer than the laser pulse duration. As shown in Fig. 3, the two endpoints of the total photon counting rate represented by the blue triangles are the same as the sum from the two beams by the purple inverted triangles, showing that the Si-APD’s response was from the TPA of each beam if the two pulses did not overlap each other. The photon counting rate is about 260 kHz, which was almost the same as the sum of that from the two beams. Tuning the time delay between the two beams, the total counting rate of the Si-APD increased and reached a maximum when the two beams were temporally overlapped. This increase in the photon counting rate was considerably caused by the ND-TPA.
Similar to the principle of an optical autocorrelator, when the phase difference between the two beams was zero, ND-TPA got a maximum of 325 kHz. The full-width at half maximum of the curve is 14.2 ps, in good agreement with the laser pulse duration of 10 ps with \( t = \sqrt{2}\tau \), where \( t \) is the measured cross-correlation width and \( \tau \) is the laser pulse duration.

\[
C = \eta_{AB}\langle N_A \rangle \langle N_B \rangle + \eta_A \langle N_A \rangle^2 + \eta_B \langle N_B \rangle^2 ,
\]  

(7)
where $\eta_{AB}, \eta_A, \eta_B$ represent the quantum detection efficiency by the ND-TPA effect, D-TPA of Beam A, and D-TPA of Beam B respectively. And $<N_A>$ and $<N_B>$ are the photon fluxes of Beam A and Beam B, respectively. We adjusted the incident photon fluxes by the two VAs while keeping a certain total photon counting rate ranging from 27 kHz to 160 kHz as shown in Fig.4(a). By fitting the curves in Fig.4(a) according to Eq.(7), we get

$$\eta_{AB} = (7.9 \pm 1.5) \times 10^{-16} \text{ counts \cdot pulse/photon}^2,$$

$$\eta_A = (3.3 \pm 0.1) \times 10^{-16} \text{ counts \cdot pulse/photon}^2, \quad (8)$$

$$\eta_B = (4.3 \pm 0.26) \times 10^{-15} \text{ counts \cdot pulse/photon}^2.$$

Meanwhile, the D-TPA quantum detection efficiency were determined by recording the photon counting rates when the delay between the two beams was far from zero. The incident photon fluxes were recorded in the same way as in the ND-TPA measurement. All the curves are in a quarter ellipse shape obeying

$$C' = \eta_A <N_A>^2 + \eta_B <N_B>^2. \quad (9)$$

And by fitting the curves in Fig.4(b), we get

$$\eta_A = (3.2 \pm 0.2) \times 10^{-16} \text{ counts \cdot pulse/photon}^2,$$

$$\eta_B = (4.8 \pm 0.12) \times 10^{-15} \text{ counts \cdot pulse/photon}^2, \quad (10)$$

which are almost the same as those in Eq.(8). We can conclude that the quantum detection efficiency of D-TPA keeps the same in the presence of ND-TPA.
The spectral dependence of the TPA efficiency is expected to be different for indirect gap semiconductor as compared with that of the direct-gap semiconductors. According to Ref [25], the D-TPA coefficient has a maximum slightly above the indirect bandgap, at $\hbar \omega \approx \left(7/6\right)E_g$. Accordingly, the wavelength of the photon is at about 954 nm. As the wavelength increases, the D-TPA efficiency decreases [23]. The D-TPA quantum detection efficiency at 1800 nm was measured to be more than one order smaller than that at 1550 nm in our experiment. Meanwhile, the ND-TPA efficiency was not equal to the D-TPA efficiency at either wavelength of 1800 nm and 1550 nm. And there was no direct relation between the ND-TPA efficiency and the D-TPA efficiencies of the two beams at different wavelengths.

4. Conclusion

In summary, we experimentally determined the specific contribution of D-TPA and ND-TPA effects at two different wavelengths of 1800 nm and 1550 nm for infrared light detection in the Si-APD single-photon detector at room temperature. The quantum detection efficiencies of D-TPA at 1800 nm and 1550 nm were measured to be about $3.2 \times 10^{-16}$ counts•pulse/photon$^2$ and $4.8 \times 10^{-15}$ counts•pulse/photon$^2$, respectively, and they kept the same in the presence of ND-TPA. Meanwhile the quantum detection efficiency of ND-TPA of 1550 nm and 1800 nm was measured to be $7.9 \times 10^{-16}$ counts•pulse/photon$^2$. The TPA effect in photon detectors has shown great potential in many applications. Owing to the advantages of infrared photon detection based on TPA effect over the frequency upconversion scheme, we believe that high efficiency TPA
quantum detectors of silicon-based optoelectronic devices will be developed in the near future for various applications.
Declarations

Availability of data and materials

The datasets used and/or analyzed during the current study are available from the corresponding author on reasonable request.

Competing interests

The authors declare that they have no competing interests.

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Authors’ contributions

Guangjian Xu, and Qucheng Miao conducted experiment and wrote the manuscript. Xinyi Ren and Ming Yan built the laser source. Haifeng Pan, Xiuliang Chen and Guang Wu designed the data collection system and analyzed the data. E Wu designed the experiment, analyzed the data and wrote the manuscript.

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