Biomechanical properties of masticatory balance in cases with RPDs—The influence of preferred and nonpreferred chewing side: A pilot study

Lydia Eberhard | Stefan Rues | Lea Bach | Jürgen Lenz | Hans J. Schindler

Abstract

Objectives: Removable partial dentures (RPDs) are inserted with the aim to restore masticatory function. There is however inconsistent evidence supporting the alleged improvements, posterior occlusal contacts being one of the decisive factors. We hypothesized that the distribution of abutment teeth in RPDs influences masticatory performance and functional parameters. To evaluate the masticatory performance and functional parameters in patients with a RPD using a single mathematical parameter (tilting index [TI]) for both jaws that predicts biomechanical behavior on the basis of the distribution of abutment teeth.

Materials and Methods: Masticatory performance was measured in patients wearing long-time adapted RPDs using the standardized test food optocal, yielding the mean particle size ($X_{50}$). Mastication on the preferred and nonpreferred chewing sides was analyzed. Total muscle work (TMW) was calculated using bipolar electromyographic recordings of the masseter and anterior temporalis muscle. Functional parameters were subjected to multiple linear regression analysis including $X_{50}$ as a dependent variable and functional units (FU), the number of teeth, bite forces, and sagittal and frontal components of TI ($TI_{\alpha}$ and $TI_{\beta}$) as independent variables.

Results: When the preferred chewing side was tested, none of the investigated parameters correlated significantly with $X_{50}$. In contrast, chewing on the nonpreferred side was correlated significantly with performance for most variables ($p < .05$). This means that increased dental support improved chewing performance with RPDs under these conditions.

Conclusions: In well-adapted RPDs, the distribution of abutment teeth as expressed by the tilting index seems to be of subordinate importance for masticatory performance.

Keywords: bite force, chewing performance, EMG, RPD, $X_{50}$ value
1 INTRODUCTION

With a rapid increase in life expectancy, the number of partially dentate patients is also growing. In particular, caries and periodontal diseases lead to tooth loss and/or shortened dental arches. Depending on the number and location of lost teeth, removable partial denture (RPD) is used to restore masticatory function, aesthetics, and phonetics. Previous studies have shown that the masticatory performance of patients with RPD is less than for fully dentate subjects (Ikebe et al., 2012). Above all, gender, bite force, location of remaining teeth, and the number of functional units (FU) affect the masticatory performance of patients with RPD (Tumrasvin et al., 2006).

Studies on the biomechanical effects of incorporated RPD have furnished divergent results, depending on the measure of performance used and the number of lost teeth. It has been reported that patients with an extremely shortened dental arch have a poor masticatory performance, which can be improved by wearing a removable partial denture (Arce-Tumbay et al., 2011). In contrast, other studies found that RPD has no effect on masticatory performance if the premolar regions are intact (Ikebe et al., 2011; Peyron et al., 2004).

For patients with unilateral shortened dental arches, the correlation between bite force and masticatory performance is stronger on the dentate side (Tumrasvin et al., 2005), and the greatest correlation between masticatory performance and bite force is observed for the first molar region (Lujan-Climent et al., 2008). It can generally be stated that the decrease in masticatory performance among elderly patients is mainly caused by tooth loss, and less by reduced bite force and muscle forces (Ikebe et al., 2011; Peyron et al., 2004).

Monitoring of electric muscle activity (EMG) reveals that symmetrical activation of the masticatory muscles improves chewing performance (Garrett et al., 1995) and that the duration of EMG activity during the chewing cycle is inversely proportional to the stability of the dentition (Baïkhi et al., 1993). It has, furthermore, been reported that EMG activity (area under the curve, or integral) during chewing of foods of different hardness is not significantly different for elderly people with full dentition and young subjects. This means that the elderly are still able to adapt excellently in the submaximum range of muscle activation, despite the loss of maximum bite-force capacity (Peyron et al., 2004). Reduced chewing performance of the elderly might be caused by tooth wear, which reduces the biomechanical effectiveness of the teeth (Giannakopoulos et al., 2014).

In previous work, biomechanical conditions that affect the chewing performance of partially edentulous patients have been studied by use of classic measures, for example, the “Kennedy” or “Eichner” classification (Ikebe et al., 2010; Rehmann et al., 2015), which characterize linear, triangular, and quadrangular dental support conditions as well as FU (Figure 1).

Essential physiological data for the masticatory system, in particular EMG and bite force measurements, have also been used to determine the neuromuscular effect of tooth loss on the functional behavior of the system. Criteria for evaluation of the biomechanical balance of prostheses on the basis of the arrangement of the residual teeth and other support elements for both jaws, by use of a single model, are not available. Such an approach might enable more consistent grading of the biomechanical conditions for prosthetic reconstructions, and, more importantly, better characterization of the biomechanical balance. Additional basic condition in this context represents the adaptability of the neuromuscular system. The target for a realistic assessment of the neuromuscular capacity of the masticatory system is unquestionably the physiology of mastication. Mastication is a complex process involving food breakdown, moistening and dilution in saliva, bolus formation, and swallowing. Masticatory performance was proposed to be the result of two processes: selection of food particles and breakage (Lucas & Luke, 1983). These processes are fundamentally dependent on learned motor patterns, and both should be reflected by the method of testing experimental performance. Commonly, the masticatory performance is investigated in the short term after the incorporation of dentures. However, this experimental design cannot picture the realistic chewing performance after long-term motor adaptation. Previous investigations substantiated the adaptability of the jaw motor system and have also shown that the motor behavior adapts to new motor tasks by training (Hellmann et al., 2011). This adaptation needs a certain time (Goia et al., 2010). In this context, it can be supposed that in the fully adapted chewing system the nonpreferred chewing side, which is challenged by unfamiliar chewing, may respond with different performance.

The purpose of this investigation was twofold. First, it correlates the masticatory performance of partially dentate subjects wearing RPD for more than 3 years with two variables, the distribution of

![Figure 1](https://example.com/figure1.png)

**FIGURE 1** Categories of denture support according to the distribution of abutment teeth. (a) Linear, (b) triangular, and (c) quadrangular
individual abutment teeth in the maxilla and mandible, by means of a mathematical model specifically developed to enable estimation of the biomechanical properties of both jaws. Second, the gained data on the preferred chewing side were compared with those when patients chewed on the nonpreferred chewing sides. We hypothesized that the distribution of individual abutment teeth in the maxilla and mandible would substantially affect masticatory performance under both conditions. As an additional goal, EMG and bite force was also measured, and classic variables, for example, FU and the number of teeth, were determined to enable an analysis of their correlation with performance on the preferred and nonpreferred chewing sides.

2 | MATERIALS AND METHODS

2.1 | Subjects

Twenty-nine patients (mean age 65.8 ± 8.8 years, 21 female; 8 male) with telescopic RPD participated in the study. The prostheses were incorporated for at least 3 years. Participants underwent a conventional clinical examination used for prosthetodontic cases.

The study included 58 jaws and 366 telescopes (166 in the upper and 200 in the lower jaw) distributed with no side preferences. In Table 1 the distribution of the different support conditions is categorized.

The study was approved by the Ethics Committee of the University Medical Center, Heidelberg (S-570/2014) and all patients gave their written consent to the experiments.

2.2 | Biomechanical model

Traditional classification schemes, for example, the “Eichner” or “Kennedy” classification, cannot give a correct indication of mutual support for maxillae and mandibles containing teeth in different positions. For further clarification of this issue, we developed a biomechanical model that quantifies the static equivalence of support conditions in the maxilla and mandible. The occlusal plane (OP) is modeled by a rigid plate. The teeth are modeled by springs that are attached perpendicular to the OP (index i was used for all parameters associated with the maxilla whereas index j indicated an association with the mandible) at their respective positions (including missing teeth). For mathematical analysis, a Cartesian coordinate system is chosen, which lies in the OP with x and z pointing in the anterior and vertical directions, respectively (Figure 2).

Ideally, the occlusal plane and the positions of the teeth are determined for each patient individually. Uniform geometry can, however, be used as a simplification. In both cases, the appropriate stiffness of each spring is chosen in accordance with the local support of the respective partial dentures (tooth, implant, and gingiva). In our biomechanical model, we included mechanical support up to the positions of the second molars (each 14 teeth tooth positions for maxilla and mandible). The model can contain any number of theoretical support positions, for example, n = 16 if positions of the wisdom teeth should be included.

To evaluate the equivalence of the support present in the maxilla and mandible, the position of the rigid plate is fixed and all spring ends are moved by a distance Δz toward the OP, thus introducing prestress into the system. When the plate is released, it will move to a new position of equilibrium, depending on the support. This position will usually be displaced and twisted compared with the original position. The mathematical basics of the model are summarized in the appendix.

Tilting of the rigid plate (α: tilt in the x-direction, β: tilt in the y-direction) is appropriate for evaluation of the equivalence of the spatial distribution of the support elements for both jaws. Under the action of spatially equivalent support in the maxilla and mandible, conditions in the maxilla and mandible. The occlusal plane (OP) is modeled by a rigid plate. The teeth are modeled by springs that are attached perpendicular to the OP (index i was used for all parameters associated with the maxilla whereas index j indicated an association with the mandible) at their respective positions (including missing teeth). For mathematical analysis, a Cartesian coordinate system is chosen, which lies in the OP with x and z pointing in the anterior and vertical directions, respectively (Figure 2).

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| Support       | Upper jaw | Lower jaw | Both jaws | Single jaw | Total |
|---------------|-----------|-----------|-----------|------------|-------|
| Punctual      | 3         | 3         | 1         | 4          | 6     |
| Linear        | 11        | 12        | 4         | 15         | 23    |
| Triangular    | 8         | 6         | 2         | 10         | 14    |
| Quadrangular  | 1         | 1         | 0         | 2          | 2     |
| Full dentition| 5         | 6         | 0         | 11         | 11    |
| Complete denture | 1      | 1         | 0         | 2          | 2     |

Note: The number of patients with respective support is depicted.
the plate remains in the horizontal position. The more the situations in the maxilla and mandible differ from this state, the larger becomes the tilting, that is, more unfavorable is the static situation of the system. The vertical displacement at the position of the resultant force in each jaw \( z_{rf} \) is a measure of total stiffness differences of the supports in the maxilla and mandible and will always be oriented toward the more resilient side.

Clinically, the algebraic signs of the three variables are possibly misleading; absolute values of \( |z_{rf}|, |\alpha|, \) and \( |\beta| \) should therefore be used. In statistical analysis of the results from this study, however, only the TI, \( |\alpha|, \) and \( |\beta| \) were analyzed whereas the effect of total stiffness differences (corresponding with \( z_{rf} \)) was not taken into account.

### 2.3 Masticatory performance

After completing a test cycle, the patients performed three different masticatory performance tests. Each test entailed 15 chewing strokes for habitual and unilateral chewing on the right and left sides of the jaw. Habitual chewing was repeated two times. Standardized artificial test food (Optocal) was used (Pocztaruk Rde et al., 2008) and 17 5.6-mm cubes formed a portion. Optosil, plaster, alginate, vaseline, and toothpaste were blended in a standardized mixing ratio. The hardness and texture of Optocal make it similar to natural test food, but it can also be chewed by patients wearing a prosthesis (Pocztaruk Rde et al., 2008; Slagter et al., 1993) and it has been used in previous studies (Eberhard et al., 2018).

In this context, habitual chewing enabled the identification of the preferred chewing side. To identify the preferred chewing side, three methods were employed. First, total muscle work (TMW) ratios were used. The side that showed greater muscle activity (TMW) was determined to be the preferred chewing side. Similar methods were applied by Yamasaki et al. (2016) and Ratnasari et al. (2011). Second, observation by an examiner was used as an indicator. Finally, the patients were interviewed and their preferred chewing side was documented. Related to this, other studies have used a questionnaire or a visual analog scale to document the subjective preferred chewing side (Diernberger et al., 2008; Rovira-Lastra et al., 2016).

It is known that EMG activity is greater on the preferred chewing side during deliberate unilateral chewing (Stohler, 1986). Thus, muscle activity for habitual chewing and deliberate unilateral chewing were compared, and the greater activity was chosen. This pattern is reflected in the measurements from all three performance tests; usually, it is most pronounced during habitual chewing. The activity of the masseter muscle was decisive for determining the chewing side, because this muscle is mainly responsible for the power stroke, whereas the temporalis muscle is more important for the coordination of movements and positioning of the mandible. This is also in agreement with Yamasaki et al. (2015), in which masseter activity was used to determine the actual chewing side.

For silicone test food, the standard approach is to determine the weight of the particles retained by sieves and to curve-fit the cumulative weight by the use of the Rosin–Rammler equation. In the present study, in contrast to classical sieving methods, optical scanning analysis methods for measuring masticatory performance were used (Eberhard et al., 2012). The approximate weight distributions were determined by the use of the Rosin–Rammler equation and by a least-squares method (Olthoff et al., 1984; Rosin & Rammler, 1933; Slagter et al., 1993), by use of a MatLab tool (MatLab tool "Rosin Rammler diagram v 1.0" by Ivan Brezani, 2010). The Rosin–Rammler function used was:

![Figure 3](image-url)
In this equation, \( Q \) represents the volume percentage of the particles with a size smaller than \( X \). \( X_{50} \) is the median particle size or the size of the theoretical sieve through which 50% of the volume of particles can pass. The variable \( b \) represents the broadness of the size distribution. A high \( X_{50} \)-value means that the chewing performance is poor. The particle size is overall large. A low value, on the other hand, means that the particles are quite small and the chewing performance is good (Mowlana et al., 1994; Speksnijder et al., 2009; van der Bilt et al., 1993).

2.4 | Electromyography

The electromyographic activity of the chewing muscles was recorded by use of Ag/AgCl bipolar surface electrodes (Noraxon, Scottsdale, Arizona, USA). After cleaning the skin with alcohol (70%), electrodes were placed on both sides of the middle part of the masseter and on the anterior temporalis. The reference electrode was positioned on the neck over the seventh vertebra. The EMG signals were differentially amplified (MP100, Acquire 3.9.1 software; Biopac, Santa Barbara, CA, USA), recorded at a sampling rate of 1500 Hz, saved on a personal computer, and band-pass-filtered (10–700 Hz) off-line.

2.5 | Bite force measurement

Bite force was measured with a recently available bitefork (BiteFork; ViMes, Igel, Germany). The two functionally separated sensors of the instrument were placed between prefabricated bite blocks individualized with silicone impression material and positioned between the second premolars and first molars (Figure 4). This configuration enabled simultaneous but separate force recordings for the left and right sides of the jaw. The sampled data were saved on a personal computer for further analysis.

2.6 | Experimental procedure

After the installation of the EMG recording device, the three masticatory performance tests were conducted in one session. First, the subjects performed three maximum bites in maximum intercuspatation. After a test cycle for habitual chewing to familiarize them with the procedure, subjects were asked to chew habitually, followed by chewing on the right side and, finally, on the left side. Habitual chewing was used to identify the preferred chewing side and was repeated two times. Under each condition, 15 chewing cycles were performed. The minced food was spat out and the mouth was rinsed with water to collect all the particles in a filter bag.

The bitefork was adjusted with silicone impression material. Initially, while holding the bitefork in the mouth and stabilizing it by hand, the patient was asked to bite on the bite blocks and to perform some bites to become familiar with the feedback device. If the subject was able to control the bite force by watching a bar on the feedback screen, he/she was asked to bite three times with 50, 100, and 150 N on the device.

2.7 | Data analysis

The collected and dried chewed artificial test food was scanned and analyzed by use of a validated procedure (Eberhard et al., 2012). \( X_{50} \) values were calculated by use of the Rosin–Rammler algorithm. The EMG data were analyzed by use of AcqKnowledge 3.9.1 software and a semiautomatic Matlab program. Root mean square (RMS) normalized recordings adjusted to maximum biting EMG were used to compute the area under the curve (integral) of the EMG bursts. TMW for all bilaterally measured muscles was summed for the 15 chewing cycles and analyzed. The ratios of side-specific TMW (SMW) for the preferred and nonpreferred chewing sides were also analyzed. Bite force recordings were evaluated separately for each side of the jaw.

The tilting indices \( TI_{\alpha} \) and \( TI_{\beta} \) categorize the overall biomechanical balance of the jaws for the respective RPD-reconstructed dentition. The number of remaining teeth was also counted, and documented as totals for the preferred and nonpreferred chewing sides for each subject. In the same way, FU (antagonistically contacting teeth) for each person were matched with the chewing sides.

To achieve a realistic comparison of the functional data with the remaining dentition, all analyzed recordings were adjusted in relation to the preferred or nonpreferred chewing side (e.g., the EMG data for
left-side chewers were interchanged in comparison with those for the right-side chewers). Means and standard deviations (SD) were calculated for all results.

2.8 | Statistics

Spearman correlation was used to analyze correlations between the variables $X_{50}$, TI, TMW, FU, bite forces, and the number of teeth. Multiple linear regression analysis was also used. Preferred and nonpreferred chewing sides were analyzed separately. Chewing side differences for TMW, SMW ratios, and bite forces were tested by repeated-measures analysis of variance. The level of significance was set at $p < .05$.

2.9 | Ethical approval

All procedures performed in studies involving human participants were in accordance with the ethical standards of the institutional review board and with the 1964 Helsinki declaration and its later amendments.

3 | RESULTS

A broad distribution of the total number of remaining teeth was observed for the maxillae and mandibles; the minimum was three and the maximum 20 (Figure 5). The findings revealed that 22 of the subjects chewed preferentially on the right and seven on the left. The

![Figure 5: Histogram showing the frequency of the numbers of teeth remaining for all the participants.](image)

values obtained for TI $\alpha$ and TI $\beta$ are listed in Table 2; high and low values represent the most unfavorable and favorable cases, respectively. FU could be detected for 16 subjects but were absent in 13.

The $X_{50}$ values presented in Table 3 ranged from 0.50 to 4.82 mm; high scores are indicative of relatively poor and low scores for relatively good performance, respectively. The $X_{50}$ values for the nonpreferred chewing side were smaller than those for the preferred side but did not differ significantly ($p = .68$). Values of $X_{50}$ and the tilting index $\beta$ (tilting around a sagittal axis) were significantly positively correlated ($r = .36, p = .05$) for chewing on the nonpreferred side (Table 4). No significant correlation ($r = -.04, p = .85$) with TI $\beta$ was observed for the preferred chewing side, however. Correlations between $X_{50}$ and TI $\alpha$ values of both preferred and nonpreferred chewing sides were not significant ($r = .17, p = .39$ and $r = .23, p = .51$, respectively) (Table 4).

On the preferred chewing side, the mean number of teeth was 6.52 (SD = 2.6); on the nonpreferred side the mean was 6.10 (SD = 2.7). A significant negative correlation was observed for the total number of teeth and the $X_{50}$ values for both the preferred and nonpreferred chewing sides ($r = -.42, p = .03$ and $r = -.37, p = .05$).

A significant negative correlation was observed between TMW and $X_{50}$ for the preferred chewing side ($r = -.37, p = .05$), but not for the nonpreferred chewing side ($r = -.33, p = .08$, Table 4). TMW values (integrals) for both conditions (Table 5) were not significantly different, however ($p = .24$). The SMW ratios for the preferred (mean = 1.5, SD = 0.3) and nonpreferred (mean = 1.1, SD = 0.3) chewing sides differed significantly ($p < .0001$).

None of the bite forces for the preferred and nonpreferred chewing sides correlated significantly with the $X_{50}$ values ($p > .05$), and no significant differences between bite forces for either side were found for any force level (Table 6).

Multiple linear regression analysis for the preferred chewing side revealed no significant contribution of any independent variable to the variability of the dependent variable $X_{50}$. For the nonpreferred chewing side, in contrast, TI $\alpha$, TI $\beta$, TMW, and FU, in particular, explained 33.3% of the variability, with significant contributions ($p < .05$) (Table 7).

### Table 2

| TI $\alpha$ and TI $\beta$ (n = 29) |
|----------------------------------|
| T | Min. | Max. | Mean | SD  |
|---|------|------|------|-----|
| $\alpha$ | 0.03 | 2.21 | 0.83 | 0.59 |
| $\beta$  | 0.00 | 1.30 | 0.50 | 0.40 |

Abbreviation: TI, tilting indices.

### Table 3

| $X_{50}$ values for preferred and nonpreferred chewing sides, n = 29 (in mm) |
|--------------------------------------------------|
| T | Min. | Max. | Mean | SD  |
|---|------|------|------|-----|
| Preferred | 0.5  | 4.82 | 2.96 | 1.11 |
| Nonpreferred | 0.87 | 4.76 | 3.03 | 1.11 |
The objective of this study was to quantify the functional effects of different abutment teeth distributions for a sample of patients restored with RPDs that had been worn for at least 3 years. The performance of the nonpreferred chewing side was assumed to correspond to a nonadapted situation, for instance, a condition immediately after tooth loss or a short-term response after modifying static tooth distribution in the context of various prosthetic reconstruction techniques. In the context of this study, we refer to adaptation in a general sense as the reaction of the organism to an alteration of internal or environmental conditions. Several physiological variables were included in the statistical analysis. For the preferred chewing side, the main result of this investigation is that—on the basis of the rather small data set of this pilot study—masticatory performance correlates neither with a static biomechanical balance of the restored chewing system, characterized by the TI nor with the number of FU, the number of teeth, TMW, or bite force. A small, nonsignificant influence on the number of functional units can be seen on the preferred chewing side as well. We assume that in a larger patient collective, this effect might be more pronounced. Even so, for long-term adapted RPD and the preferred chewing side static biomechanical variables seem to be of subordinate significance for performance.

In contrast, if the nonpreferred chewing side is used by the patients, the static balance of restorations, characterized by the TI, the FU, and the number of teeth, correlate significantly with X50 values. The TIα, representing the tilting of the denture in the sagittal plane, is of greater importance than the TIβ, referring to the frontal plane. Summed up, the distribution of abutment teeth has a significant effect on the nonpreferred side. We would attribute this effect to the unfamiliarity of this condition to the patient. The lower TMW indicates that patients may have exerted greater caution when chewing on the nonpreferred side. As their masticatory performance tends to increase over an adaptation period (Giannakopoulos et al., 2017), we assume that in an unfamiliar situation, the influence of the distribution of abutment teeth is higher in proportion to overriding factors and thus produces a significant result. It can be argued, whether this unfamiliar situation is generalizable to nonadapted states as described above (e.g., new dentures). To validate this claim, longitudinal studies involving a change in the number of abutment teeth would have to be performed.

On the basis of our findings, the initially stated hypothesis that specific distributions of abutment teeth of RPDs in the maxilla and mandible significantly affect masticatory performance must be rejected for the adapted restored jaw.

The results do, however, support the notion that for adapted neuromuscular systems motor control strategies are adjusted in such a way as to enable them to perform with the best available biomechanical effectiveness. This may imply that, in the long term, the masticatory system does not correspond to static loading conditions in intercuspation, as is generally assumed.

This is also supported by the findings that the ratios of SMW (i.e., working side vs. balancing side; 1.5 for chewing on the preferred side vs. 1.1 for chewing on the nonpreferred side) differ significantly under both chewing conditions; this was not observed for the TMW values. The ratios for the preferred side correspond well to those for natural dentition during unilateral chewing (Proschel & Morneburg, 2010). In the context of our study, it must be considered that during chewing the food bolus is placed unilaterally between the opposing jaws, resulting in bite forces substantially different from those of symmetrical static loading of the dentition or prosthetic reconstruction. Thus, our results challenge a mechanistic approach that is still commonly used for the prediction of the denture dynamics of reconstructions.

Several limitations of this study must be considered. First, the study sample was relatively small and the genders were unequally distributed (this issue should be considered in future investigations). The broad range of abutment teeth distribution may, however, have

### Table 4: Correlations of X50 for preferred and nonpreferred chewing side

|          | TIα | | TIβ | | Total number of teeth | | Number of functional units | | Total muscle work |
|----------|-----|---|-----|---|---------------------|---|---------------------|---|------------------|
| X50      | .17 | .39 | .04 | .85 | .42 | .03 | .47 | .01 | .37 | .05 |
| X50      | .23 | .51 | .36 | .05 | .37 | .05 | .09 | .61 | .33 | .08 |

### Table 5: Total muscle work (TMW, mVs) for preferred and nonpreferred chewing sides, n = 29

|          | Min. | Max. | Mean | SD |
|----------|------|------|------|----|
| Preferred | 0.05 | 0.21 | 0.1  | 0.03 |
| Nonpreferred | 0.04 | 0.13 | 0.08 | 0.03 |

### Table 6: Bite force for preferred and nonpreferred chewing sides at 50, 100, and 150 N, n = 29

| Bite force (N) | Chewing side | Mean | SD |
|---------------|--------------|------|----|
| 50            | Preferred    | 23.84| 11.50|
|               | Nonpreferred | 23.02| 11.39|
| 100           | Preferred    | 45.37| 21.54|
|               | Nonpreferred | 48.39| 20.78|
| 150           | Preferred    | 71.16| 33.15|
|               | Nonpreferred | 67.00| 33.74|

### 4 Discussion

The performance of the nonpreferred chewing side was assumed to correspond to a nonadapted situation, for instance, a condition immediately after tooth loss or a short-term response after modifying static tooth distribution in the context of various prosthetic reconstruction techniques. In the context of this study, we refer to adaptation in a general sense as the reaction of the organism to an alteration of internal or environmental conditions. Several physiological variables were included in the statistical analysis. For the preferred chewing side, the main result of this investigation is that—on the basis of the rather small data set of this pilot study—masticatory performance correlates neither with a static biomechanical balance of the restored chewing system, characterized by the TI nor with the number of FU, the number of teeth, TMW, or bite force. A small, nonsignificant influence on the number of functional units can be seen on the preferred chewing side as well. We assume that in a larger patient collective, this effect might be more pronounced. Even so, for long-term adapted RPD and the preferred chewing side static biomechanical variables seem to be of subordinate significance for performance.

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Several limitations of this study must be considered. First, the study sample was relatively small and the genders were unequally distributed (this issue should be considered in future investigations). The broad range of abutment teeth distribution may, however, have...
balanced this possible limitation. Second, all patients were restored with telescopic RPD, which usually ensures a better balance of the denture than the use of clasps. This has consequences for the generalizability of our results. One significant open question also remains unanswered—the overwhelming dominance of preferred right side chewing. The finding is in agreement with population-based studies (Diernberger et al., 2008) but cannot be explained for our sample on the basis of varying biomechanical conditions because no significant differences between either number of teeth or FU were observed for the preferred and nonpreferred chewing sides. Intraorally, there were no signs of laterality. Other aspects of laterality, such as handedness or eye or ear preference, were not examined. However, studies have shown that there is only a weak positive relationship between the preferred chewing side and other signs of laterality (handness, eye, ear) (Barcellos et al., 2012). Obviously, simple biomechanical principles seem not to explain this problem. It might be speculated, however, that previous neuromuscular engrams, controlling the complex chewing process, are essential basics for neuromuscular control of this unconscious decision-making.

It might be argued that the TI, based on the static behavior of the combined jaws, may not be of substantial benefit for estimating the real dynamic conditions in function. However, the results for chewing on the nonpreferred side show that the parameter is sensitive enough to model an effect. Under these conditions the $X_{50}$ values are significantly affected by tooth distribution; they also specify an unfavorable distribution as a tilt around the x-axis (angle $\beta$). The clinical correlate to this observation would be, for example, the common case of the unfavorable dynamics of free-end saddles (Preston, 2007). The adapted long-term biomechanical behavior is not predictable by the use of any of the functional variables analyzed, however.

As outlined above, our new biomechanical model describes the static equivalence of both jaw situations in maximum intercusption and uses the tilt after loading of the combined system as a measure of inequality. A biomechanical description with the help of a continuous mathematical parameter, comprising both jaws, has not previously been available. It is the first attempt to use the distribution of teeth in both jaws as a predictor of the biomechanical balance of the compromised masticatory system. The fact that there are no significant results when the patients were chewing on their habitual chewing side suggests that static considerations that are based on the Eichner- or Kennedy-Classification should be re-evaluated. When the chewing process is viewed as an asymmetrical movement, it is obvious that a complex procedure such as stabilizing a denture cannot be described with simple static designs. Many treatment plans still follow the idea that only a symmetrical chewing pattern results in good chewing performance. This concept has to be refuted: The chewing process can be regarded as an interaction between acquired neuromuscular patterns, the innate preference for one chewing side, and external conditions. For the first phase of usage after the incorporation of RPD the model might enable the prediction of the quality of performance of the masticatory system. Future investigations must, however, replicate the results of this investigation and validate this new model for cases analyzed before and immediately after the prosthetic restoration of patients. When planning a new restoration, the patient’s tooth status could be entered into a software mask based on our mathematical model. The resulting tilting indices show what kind of tilt and torsion

---

**TABLE 7** Multiple linear regression analysis for preferred side (PS) and nonpreferred side (NPS)

| Independent variables | Regression coefficient | SE | Sig. | CI lower | CI upper | $R^2$ |
|-----------------------|------------------------|----|-----|----------|----------|------|
| **Preferred side**    |                        |    |     |          |          |      |
| Constant              | 3.19                   | 1.21| 0.02| 0.67     | 5.72     | .15  |
| Bite force            | .015                   | 0.011| 0.18| −0.01    | 0.04     |      |
| $TI_{\alpha}$         | .29                    | 0.37| 0.44| −0.48    | 1.06     |      |
| $TI_{\beta}$          | −.16                   | 0.57| 0.78| −1.35    | 1.03     |      |
| Functional units (PS) | −.41                   | 0.21| 0.06| −0.85    | 0.02     |      |
| Number of teeth (PS)  | .01                    | 0.11| 0.97| −0.22    | 0.23     |      |
| **Nonpreferred side** |                        |    |     |          |          |      |
| Constant              | 3.51                   | 0.96| 0.001| 1.53     | 5.50     | .33  |
| Bite force            | −.01                   | 0.01| 0.41| −0.03    | 0.01     |      |
| $TI_{\alpha}$         | .85                    | 0.34| 0.02| 0.15     | 1.54     |      |
| $TI_{\beta}$          | 1.08                   | 0.51| 0.04| 0.03     | 2.13     |      |
| Functional units (NPS)| .39                    | 0.18| 0.04| 0.01     | 0.76     |      |
| Number of teeth (NPS) | −.28                   | 0.10| 0.01| −0.49    | −0.06    |      |
can be expected for the planned denture or prosthesis immediately after incorporation. Based on these results, the dentist could decide to add another implant or abutment tooth to achieve a smaller tilting index and greater stability. A major advantage of the developed model is that the tilting index can be calculated individually for each patient time-saving and efficient.

On the basis of this pilot study, and despite its inherent limitations, it might also be of future interest to evaluate the previously preferred chewing side of patients, to enable comparison of this preference with the preferred chewing side in long-term use, in particular, because for the human population and all age groups chewing side preference seems to be normal behavior (Barcellos et al., 2012; Nayak et al., 2016; Nissan et al., 2004). For future planning of RPD, this information might be of benefit for obtaining recommendations for placing additional load-bearing structures (i.e., implants) in the jaws for immediate optimum chewing performance or in patients with a known history of bruxism, to better distribute the generated pathophysiological forces. However, prospective studies have to prove these conceptual hypotheses.

AUTHOR CONTRIBUTIONS

Lydia Eberhard, Stefan Rues, Jürgen Lenz and Hans J. Schindler contributed to study design. Lea Bach and Lydia Eberhard contributed to data acquisition. Lydia Eberhard, Lea Bach, Stefan Rues and Hans J. Schindler contributed to data analysis. All authors contributed to the drafting of the manuscript and approved the final version.

ACKNOWLEDGMENTS

This investigation was conducted as part of a thesis. The first and second authors contributed equally to this study. The work received no funding.

CONFLICTS OF INTEREST

The authors declare no conflicts of interest.

INFORMED CONSENT

Informed consent was obtained from all individual participants included in the study.

DATA AVAILABILITY STATEMENT

Supporting Information, such as raw data, is available from the corresponding author upon reasonable request.

ORCID

Lydia Eberhard http://orcid.org/0000-0003-4755-7730
Stefan Rues http://orcid.org/0000-0001-9515-4405

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How to cite this article: Eberhard, L., Rues, S., Bach, L., Lenz, J., & Schindler, H. J. (2022). Biomechanical properties of masticatory balance in cases with RPDs—The influence of preferred and nonpreferred chewing side: A pilot study. Clinical and Experimental Dental Research, 8, 912–922. https://doi.org/10.1002/cre2.576

APPENDIX

The spring forces acting on the rigid plate are given by the expressions:

\[ F_{x, i} = -k_i (z_i + \Delta z) = -f_i \kappa_{\text{tooth}} (z_i + \Delta z) \]

and for the mandible:

\[ F_{z, i} = -k_j (z_j - \Delta z) = -f_j \kappa_{\text{tooth}} (z_j - \Delta z), \]

where \( k_{ij} \) denote spring stiffness and \( z_{ij} \) the displacements from their respective rest positions of the spring ends fixed to the plate. By introducing a reference stiffness, here the stiffness \( \kappa_{\text{tooth}} \) of a tooth, all spring constants \( k_{ij} \) can be specified as values \( f_{ij} \) proportional to this reference stiffness.

In the new state of equilibrium (Figure 3a), the components of all forces and moments acting on the plate must sum to zero:

\[ \sum F_x = 0 \text{ is automatically fulfilled} \]
\[ \sum F_z = 0 \text{ is automatically fulfilled} \]
\[ \sum F_{x, i} = \sum_{i=1}^{14} F_{x, i} = \sum_{j=1}^{14} F_{x, j} \]
\[ \sum M_y = \sum_{i=1}^{14} \gamma_i F_{x, i} + \sum_{j=1}^{14} \gamma_j F_{x, j} \]
\[ \sum M_z = \sum_{i=1}^{14} \xi_i F_{x, i} + \sum_{j=1}^{14} \xi_j F_{x, j} \]
\[ \sum M_x = 0 \text{ is automatically fulfilled} \]

All contact points of the springs are located on the plate, that is, in a plane, displaced and tilted into a new equilibrium position relative to the initial position. This new state of equilibrium is characterized by three variables:

- the displacement, \( z_0 \), of the rigid plate at the origin, 0, of the coordinate system,
the gradient \( m_x \) of the plate in the \( x \)-direction,
- the gradient \( m_y \) of the plate in the \( y \)-direction.

All deflections must therefore fulfill the side condition:

\[
z_{ij} = z_0 + m_x x_{ij} + m_y y_{ij}
\]

Thus, the system of equations can be rewritten in the form:

\[
\begin{bmatrix}
A_{11} & \ldots & A_{13} \\
\vdots & \ddots & \vdots \\
A_{31} & \ldots & A_{33}
\end{bmatrix}
\begin{bmatrix}
z_{0}/\Delta z \\
\vdots \\
z_{y}/\Delta z
\end{bmatrix}
= \begin{bmatrix}
-\sum_{i=1}^{14} f_i + \sum_{j=1}^{14} f_j \\
-\sum_{i=1}^{14} y_i f_i + \sum_{j=1}^{14} y_j f_j \\
-\sum_{i=1}^{14} x_i f_i + \sum_{j=1}^{14} x_j f_j
\end{bmatrix}
\]

where:

\[
A_{11} = \sum_{i=1}^{14} f_i + \sum_{j=1}^{14} f_j \\
A_{12} = \sum_{i=1}^{14} f_i x_i + \sum_{j=1}^{14} f_j y_j \\
A_{13} = \sum_{i=1}^{14} f_i y_i \\
A_{21} = \sum_{i=1}^{14} y_i f_i \\
A_{22} = \sum_{i=1}^{14} y_i f_i x_i + \sum_{j=1}^{14} y_j f_j \\
A_{23} = \sum_{i=1}^{14} y_i f_i x_i \\
A_{31} = \sum_{i=1}^{14} x_i f_i \\
A_{32} = \sum_{i=1}^{14} x_i f_i x_i + \sum_{j=1}^{14} x_j f_j \\
A_{33} = \sum_{i=1}^{14} x_i f_i x_i + \sum_{j=1}^{14} x_j f_j y_j
\]

The system of equations shows that \( z_0, m_x, \) and \( m_y \) are proportional to the auxiliary quantity \( \Delta z \) and can therefore be scaled with \( \Delta z \). The behavior of the system does not, furthermore, depend on the reference stiffness \( k_{\text{tooth}} \), but only on the stiffness ratios \( f_{ij} \).

By means of the inverse, \( A^{-1} \), of matrix \( A \) the unknown scaled variables can be calculated rather easily:

\[
\begin{bmatrix}
z_0/\Delta z \\
m_x/\Delta z \\
m_y/\Delta z
\end{bmatrix}
= A^{-1}
\begin{bmatrix}
-\sum_{i=1}^{14} f_i + \sum_{j=1}^{14} f_j \\
-\sum_{i=1}^{14} y_i f_i + \sum_{j=1}^{14} y_j f_j \\
-\sum_{i=1}^{14} x_i f_i + \sum_{j=1}^{14} x_j f_j
\end{bmatrix}
\]

To avoid normalized variables the deflection \( \Delta z = 1 \text{ mm} \) is chosen in the discussion below.

Because the position of the coordinate system within the occlusal plane can be chosen arbitrarily, the deflection \( z_0 \) is not a specifically meaningful mechanical variable. Thus, the translation \( z_{rt} \) (Figure 3b) at the position of the line of action of the resulting forces \((x_{rt}, y_{rt})\) in the maxilla (which is identical to that in the mandible)

\[
z_{rt} = z_0 + m_x x_{rt} + m_y y_{rt}
\]

is introduced with:

\[
x_{rt} = \sum_{i=1}^{14} f_i (x_i + \Delta z) x_i / \sum_{i=1}^{14} f_i (x_i + \Delta z) \quad \text{and}
\]

\[
y_{rt} = \sum_{i=1}^{14} f_i (x_i + \Delta z) y_i / \sum_{i=1}^{14} f_i (x_i + \Delta z)
\]

\( z_{rt} \) is zero if the overall stiffnesses in the maxilla and mandible are equal. If the overall stiffnesses are different, the translation \( |z_{rt}| \) is directed toward the more resilient side.

Furthermore, instead of the use of gradients \( m_x, m_y \) describing the incline of the new equilibrium position in \( x \) - and \( y \)-direction, angles associated with these gradients \( \alpha \) and \( \beta \) can be specified:

\[
\alpha = \tan^{-1} m_y (\Delta z = 1 \text{ mm}) \quad \text{(corresponds to rotation around the } y \text{-axis)},
\]

\[
\beta = \tan^{-1} m_x (\Delta z = 1 \text{ mm}) \quad \text{(corresponds to rotation around the } x \text{-axis)}.
\]

To summarize, the equilibrium state of the plate (after prestressing with \( \Delta z = 1 \text{ mm} \)) can be described by use of the set of variables \( z_{rt}, \alpha, \) and \( \beta \).