Optimizing the Parameters of A Physical Exercise Dose-Response Model
An Algorithmic Comparison

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ABSTRACT
The purpose of this research was to compare the robustness and performance of a local and global optimization algorithm applied to the problem of fitting the parameters of a non-linear dose-response model utilized in the field of exercise physiology. Traditionally, the parameters of dose-response models utilised in exercise physiology have been fit with non-linear least squares procedures in combination with local optimization algorithms. These algorithms have demonstrated limitations in their ability to converge on a globally optimal solution. This research purpose the use of an evolutionary computation based algorithm as an alternative method to fit a non-linear dose-response model. The results of our comparison over 1000 experimental runs demonstrated the superior performance of the evolutionary computation based algorithm to consistently achieve a more consistent model fit and holdout evaluation performance in comparison to the local search algorithm. This initial research would suggest that global evolutionary computation based optimization algorithms are a fast and more robust alternative to local optimization algorithms when fitting the parameters of non-linear dose-response models.

CCS CONCEPTS
• Applied computing → Health care information systems;

KEYWORDS
Intelligent Systems In Sport, Athletic Training, Model Fitting, Differential Evolution

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space effectively but also to focus the area from which it started the exploration. The rationale for this procedure was to perform a closer comparison of the algorithms when the search process is initiated from a similar area of the search space and a randomly initialised area as is the case in the unseeded DE algorithm [1]. This process was repeated 1000 times using a new set of random initial parameter values during each experimental run. To test the fit of the optimized models an open-source data set consisting of 166 exercise training sessions and observed responses was used [3, 8].

3 RESULTS

The mean±SD model fit coefficient of determination ($R^2$) scores are as follows: DE ($M = 0.997, SD = 0.00$), DE-Seeded ($M = 0.976, SD = 0.070$), L-BFGS ($M = 0.877, SD = 0.201$). Figure 1 displays the loss scores (sum of the squared errors) between the predicted and observed response variables over the 1000 experimental runs using a hold out data. The results of a one-way analysis of variance (ANOVA) test comparing the fitted R-Squared scores are: $F_{\text{statistic}} = 264.71, \ p < 0.001$, while the results of an ANOVA test using a hold out data set mean loss scores are: $F_{\text{statistic}} = 90.07, \ p < 0.001$. These results would suggested that there is significant difference in the performance of the algorithms at an $\alpha = 0.05$.

![Figure 1: Sum of the squared errors between the fitted model predicted and observed response variables](image1)

Figure 2 displays the distribution of the optimization process run time for each algorithm during the experimental runs. The results demonstrate that the DE and DE seeded algorithm consistently achieve a strong model fit and low hold out set prediction error. The L-BFGS algorithm displayed higher variance and worse performance across the experimental runs.

![Figure 2: Process Running Time](image2)

4 CONCLUSIONS & FUTURE WORK

In this paper, we set out to compare the performance and robustness of a local versus global optimization algorithm when fitting the parameters of a non-linear dose-response model. Based on our observations we found that the differential evolution global algorithm is capable of repeatedly finding optimal model parameter values demonstrated by strong model fits and performances on a holdout data set. The local search L-BFGS algorithm displayed low robustness to varying initial parameter settings and had inferior performances when predicting response values on a holdout data set. A seeded version of the differential evolution algorithm displayed the best overall performance across all measures. These result would suggest that when fitting a dose-response model, of the similar type to that used in this research, a differential evolutionary algorithm seeded with reasonable initial parameters may provide a fast, robust and high performing alternative to local search algorithms such as L-BFGS. Future work should be conducted to confirm these findings using a wider set of algorithmic settings and variants, as well as larger more diverse real-world data sets.

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