A solid state source of photon triplets based on quantum dot molecules

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Producing advanced quantum states of light is a priority in quantum information technologies. In this context, experimental realizations of multipartite photon states would enable improved tests of the foundations of quantum mechanics as well as implementations of complex quantum optical networks and protocols. It is favourable to directly generate these states using solid state systems, for simpler handling and the promise of reversible transfer of quantum information between stationary and flying qubits. Here we use the ground states of two optically active coupled quantum dots to directly produce photon triplets. The formation of a triexciton in these ground states leads to a triple cascade recombination and sequential emission of three photons with strong correlations. We record 65.62 photon triplets per minute under continuous-wave pumping, surpassing rates of earlier reported sources. Our structure and data pave the way towards implementing multipartite photon entanglement and multi-qubit readout schemes in solid state devices.

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With the rise of quantum technologies, generalized quantum key distribution protocols based on multiparticle entangled states could be stepping stones towards realizing real-world quantum networks. While remarkable progress has been made on creating single photons and entangled photon pairs, multiparticle correlated photon states are usually produced in purely optical systems by postselection techniques or cascading, with extremely low efficiency and exponentially poor scaling. The most widespread technique for generating multiparticle photon correlations relies on spontaneous parametric down conversion (SPDC) with low conversion efficiency and restricted scalability, which limits its production rate and applications. Moreover, in order to generate multiparticle correlated photons, most schemes based on SPDC use the interference of photon pairs created by independent Poissonian sources and post-select the favoured subset of output photon states, which significantly adds to the probabilistic nature of the process and the uncorrelated background light.

In contrast, quantum dots offer the most practical route in building scalable quantum architectures and their efficiency reaches almost unity per excitation pulse, enabling high count rates. The ground state of a single quantum dot host at most two bright excitons, a biexciton, which can be controlled coherently to produce correlated photon pairs in a so-called cascade recombination process. Thus the creation of multiparticle photon correlations in a single quantum dot requires exploiting energetically higher shells and phonon-mediated processes under heavy pumping, which lead to inevitable dephasing, line broadening and poor photon correlation visibility. The coupled s shells of a quantum dot molecule (QDM), however, render additional excitonic states suitable for increasing the number of correlated photons possibly using coherent schemes. The wavefunctions of photogenerated excitons localized in the QDM s shells are coupled via molecular hybridization and Coulomb interactions, thus the radiative recombination of such molecular excitons will naturally prepare correlated photons. The hybridization of carrier wavefunctions in a QDM is a strong function of the interplay between dot composition and interdot spacing. Nanowire-embedded quantum dots offer controllable size and composition, which enable engineering of the QDM interdot coupling and its spectral properties. In addition, the core-shell structure alleviates the propagation and extraction of the optical modes that carry photons and promises more efficient detection of the photons emitted from higher-order excitons, which is a requisite in our photon correlation measurements.

In the following, we demonstrate the creation of photon triplets using a QDM positioned inside an epitaxially-grown photonic nanowire. The photoluminescence (PL) spectrum of our QDM shows two sets of resonances governed by the QDM material and size. We identify these resonances by conducting a series of power-dependent and time-resolved spectroscopy experiments along with magneto-photoluminescence and photon correlation measurements. We observe a clear bunching–antibunching pattern when the photon correlations between each pair of triexciton, biexciton and exciton resonances are measured, which implies the emission of a photon triplet through a triexciton recombination process. Employing the molecular s shells of the QDM aids us in achieving a far better photon correlation visibility than previous attempts in single quantum dots. The photon-triplet-emission rate is estimated by conducting triple coincidence experiments in both continuous-wave and pulsed excitation regimes, showing a remarkable improvement compared to the creation of triplets in SPDC-based schemes. A realization of photon triplets from a triexciton forming in a QDM serves as an elementary step for the direct generation of multiphoton entanglement, which has so far been limited to photon pairs in solid state systems.

Results

QDM structure. Our QDM is composed of two InAs$_x$P$_{1-x}$ segments ($x \approx 0.15$ and 0.25) embedded inside an InP photonic nanowire that incorporates core and cladding regions (Fig. 1a). The thick cladding of 250 nm in diameter aids funnelling the QDM emission into the fundamental HE$_1$ mode to be guided out toward the collection optics. The cladding is gently tapered at its apex to improve the photon extraction efficiency (Fig. 1b). The molecule contains two $h_D \approx 2.5$–3 nm thick and $D_{NW} \approx 18$ nm in diameter dots as confirmed by transmission electron microscopy imaging (Fig. 1c). The growth of the second dot QD$_R$ is seemingly influenced by the strain field caused by the formation of the first dot QD$_L$ during the molecular beam epitaxy process, giving rise to some compositional asymmetry of the molecule. Notice that even though the hybridization energy itself can exceed several tens of meV in strongly coupled double dots, an important part of the s-shell splitting in the molecule studied here is induced by the above material composition change. Such an inherent asymmetry aids the localization of the heavy hole wavefunctions mainly inside the two individual dots rather than evenly spread throughout the molecule. The similarity of dot and barrier compositions however leads to a comparatively weaker localization of the electron, and its orbital partially diffuses into the neighbouring dot. An interdot spacing of $\approx 8$–10 nm was initially targeted in the vapour–liquid–solid growth mode; however, the arsenic tailing in our dots possibly reduces the effective separation down to $\approx 7$ nm. Considering the low arsenic concentration ($0.15 < x < 0.25$) of the dot segments, a thinner spacing would lift the barrier and aid the delocalization of electrons, or would promote the directional nonresonant tunnelling in the QDM, whereas a larger spacing would impair the electron hybridization and interdot coupling. The yield of finding a suitable QDM in our investigated samples was 10%.

Spectroscopy measurements and interdot coupling. In our experiment, the formation of a triexciton in the QDM entails the photogeneration of a biexciton (XX) in one quantum dot (QD$_L$) along with an exciton (X) in the neighbouring dot (QD$_R$) under continuous optical pumping. The predominant coupling mechanism among the two dots can be explained either via the wavefunction hybridization and Coulomb interactions, or the direct energy transfer of excitons (Förster process), or nonresonant phonon-assisted tunnelling. The direct transfer of excitons is caused by long-range Coulomb interactions and typically occurs if the interdot energy splitting is small, at most a few meV. As shown later, the energy detuning of the constituent quantum dots is several tens of millielectronvolts in our molecule because of its structural asymmetry, hence the direct exciton transfer has a negligible impact on the interdot coupling here. Moreover, the nonresonant tunnelling of carriers in QDMs is a function of the phonon spectral density, thus depends on the wavefunction overlap and particularly the energy difference of the states involved in the transition. This implies that any carrier tunnelling between the two detuned s shells of the constituent quantum dots in our QDM would require multiple acoustic phonon processes. We will later demonstrate that nonresonant tunnelling plays a minor role in the interdot communication here, and therefore wavefunction correlation must be the primary source of coupling. The studied QDM shows two distinguished high energy (HE) and low energy (LE) sets of spectral resonances at $\approx 894$ nm and...
dependence on the pump power. Inset: The nanowires are site-controlled allowing excellent isolation of QDM spectrum from inhomogeneous broadening. The scale bar is 1 \mu m.

To understand the possible effect of nonresonant carrier tunnelling, we performed a time-resolved micro-PL experiment on the present QDM and another double dot, DD2, with identical single dot specifications, but an increased interdot spacing of over 30 nm to eliminate the coupling. The lifetime of the single exciton \( X_{\text{L}} \) of the QDM was measured at \( \tau_d = 2.8 \pm 0.2 \) ns (a similar value can be inferred by comparing the \( X_{\text{L}}X_{\text{R}} \) and \( X_{\text{R}} \) lifetimes as shown in Supplementary Note 4), whereas the \( X_{\text{L}} \) resonance of DD2 lasted \( \tau_r = 2.5 \pm 0.2 \) ns. In general, the decay time \( \tau_d \) of the exciton \( X_{\text{L}} \) in a molecule, where nonresonant tunnelling from \( QD_L \) to \( QD_R \) continuously takes place, is given by \( 1/\tau_d = 1/\tau_r + 1/\tau_t \), where \( \tau_r \) is the exciton radiative lifetime and \( 1/\tau_t \) is the tunnelling rate. The fact that \( \tau_d \) and \( \tau_r \) are comparable within the accuracy of our experiment suggests that the impact of nonresonant tunnelling between the \( s \) shells of our QDM is negligible and perhaps a reverse mechanism exists between the \( s \) shell of \( QD_L \) and the nearby \( d \) shells of \( QD_R \) appearing at slightly higher energies in the spectrum. The nonresonant electron tunnelling is however enhanced at a small enough spacing (\( d < 3 \) nm), where the barrier is lifted and \( QD_L \) is steadily emptied showing weak PL intensity (see Supplementary Note 2). The above observations indicate that the coupling in our QDM forms primarily via the hybridization of electron wavefunctions.
Triple coincidence experiments. The true character of \(XX_1X_R\), \(X_1X_R\) and \(X_R\) were fully identified by conducting a series of magneto-photoluminescence measurements to confirm that the Zeeman splitting of their spin fine structure comply with the theoretically predicted values, as presented in Supplementary Note 3. The next step was to measure the second-order autocorrelation function of each individual resonance and the cross-correlation functions between various pairings (\(a, b\)) of distinct resonances (\(t_{ab} = t_{Dx} - t_{D\beta}\) denotes the delay time between photon detections by detectors \(D_x\) and \(D_\beta\)). These correlations can provide insight into the coupling strength and the nature of the lines. An autocorrelation experiment on every QDM resonance in our sample verified their low multiphoton emission probability by featuring an antibunching dip at \(t = 0\). Among all possible cross-correlations of QDM resonances, the ones measured between \(XX_1X_R\), \(X_1X_R\) and \(X_R\) are of highest interest for the photon triplet characterization. A triplet state comprising temporally correlated photons \(\lambda_1, \lambda_2, \lambda_3\) originates from a triple sequential cascade in the QDM (Fig. 1d). In our correlation setup illustrated in Supplementary Note 1, a diffraction grating separates the \(XX_1X_R\), \(X_1X_R\) and \(X_R\) photons towards the detectors \(D_1\), \(D_2\) and \(D_3\). All cross-correlations \(g^{(2)}(\tau)\) of the above three resonances feature an asymmetric bunching-antibunching behaviour as expected for cascade transitions (Fig. 2a–c). The cross-correlations between \(XX_1X_R\) (or \(X_1X_R\)) and \(X_R\) are fitted with \(g^{(2)}(\tau)=1-ae^{(t_{\text{fit}})/\tau_0}\) resulting in \(g^{(2)}(0^-) = 0.71 (0.59)\), that is, considerably smaller than unity, which indicates that the system is indeed a molecule rather than two separate dots. Here, the non-zero level of correlation at \(t = 0^-\) can be explained by, first, the temporal dynamics of the transitions, which depends on the ratio between their pumping rate \(W_p\) and decay rates \(\Gamma_X\) as further scrutinized in Supplementary Note 4 (increasing \(W_p/\Gamma_X\) lifts the antibunching floor and suppresses the bunching peak); second, the parasitic background caused by the phonon sideband of the neighbouring weak spectral lines or stacking fault states. The effect of such background noise is more pronounced in cases where photons from the LE set contribute to the correlations, because they are collected by a fibre with a twice larger core that also collects more background emission (see Methods). Similarly, the cross-correlations between the remaining pairings of LE and HE resonances featured similar above antibunching characteristics, in contrast to the cross-correlations of our comparison double quantum dot DD2, which showed no signs of antibunching.
To prove that the QDM actually emits a photon triplet, we conducted a triple coincidence experiment by sending detector pulses D1 (as Start), D2 (as Stop1) and D3 (as Stop 2) into a time-tagging device. The time-resolved (512 ps wide bins) histogram versus $\tau_{21}$ and $\tau_{31}$ contains the fully random contribution due to uncorrelated photons (319 counts) plus the sum (618.6 counts) of the three contributions that derive from two correlated photons and a third accidental one. We observe a large number of threefold coincidences in the vicinity of zero time delay (Fig. 2d) above the uncorrelated and partially correlated events. We recorded 20,744 photon counts in total (including 8,932 random background counts) integrated in 3 h in the coincidence window of $\tau_{21} \in [-0.768, 1.28]$ ns and $\tau_{31} \in [-1.28, 2.304]$ ns (see Fig. 2e). To ensure that the photon triplet generation rate is not overestimated, we subtract all the random or partially correlated events, which leaves us with 11,812 photon triplets corresponding to an average detection rate of 65.62 triplets per minute. We estimate that only 0.023% of all photon triplets could be detected because of the low detection efficiency of our detectors, $\eta_D = \eta_D1 = \eta_D2 = \eta_D3$ ($\eta_D1 = 25\%$, $\eta_D2 = 25\%$ and $\eta_D3 = 15\%$ at the respective wavelengths), along with non-ideal extraction efficiency $\eta_E = 46\%$ (see Methods), fibre coupling efficiency ($\eta_f = 85\%$) and grating efficiency ($\eta_g = 75\%$). The above photon triplet rate is, to the best of our knowledge, the highest recorded rate exceeding the values reported for direct generation of photon triplets via cascaded SPDC under continuous wave pumping.

In general, the bunching peak $\rho_{XX}^{(2)}(0^+)$ of a cascade decreases with the excitation rate, because the ratio of true cascade events versus individual excitations becomes less favourable, as has been observed in regular biexciton–exciton cascades of single quantum dots. We examined this behaviour by applying increasing levels of pump power while recording the cross-correlations between the triexciton and the other two resonances (see Fig. 3a,b). The measurements were conducted in a regime where the PL intensity to background ratio hardly changed, thus the variation in the bunching peak was mainly a function of the ratio between the excitation rate $W_p$ and transition lifetimes ($1/\tau_X$). The difference between the bunching visibility of $XX_1X_R - X_1X_R$ and $XX_1X_R - X_R$ cross-correlations in Fig. 3a,b also originates from the inequality of this ratio, $W_p/\Gamma_X$, in the $XX_1X_R$ and $X_R$ resonances, together with their unequal PL intensity measured by the silicon avalanche photodiodes at different wavelengths (see Methods). The suppression of the bunching visibility with increasing excitation power agrees with the results of our theoretical model based on the time propagation matrix method, as explained in Supplementary Note 4, and reconfirms the cascaded nature of the selected transitions.

Finally, we demonstrated the formation of the triexciton and creation of photon triplets under pulsed excitation. For this purpose, the QDM was pumped non-resonantly with 2.6 ps pulses at 820 nm in the same cross-correlation setup used for the cw pumping regime (see Methods). Figure 3c illustrates the triple coincidence counts versus $\tau_{21}$ and $\tau_{31}$ measured in 80 min, featuring a central peak located at ($\tau_{21} = 0$, $\tau_{31} = 0$) and a 2D grid of side peaks with a temporal period of 12.5 ns, equal to the pulse cycle. The coincidence peaks in this histogram have contributions from fully and partially correlated events as previously identified in the cw regime. The central coincidence peak comprises all above contributions along with the fully correlated photon triplets occurring after the first excitation pulse. The side peaks primarily result from the fully accidental and partially correlated events taking place between consecutive pulse excitations. We estimated the maximum number of partially correlated events at the side peaks to be 114 counts, and thus all the counts above this level and within a 5 ns window (≈ $\tau_{XX}X_R + \tau_{XX}X_1 + \tau_{XX}$) around the central peak were considered as true photon triplet counts, that is 363 photon triplets in 80 min (4.53 triplets per min). The lower rate of photon triplet generation here, as compared to the cw regime, could be attributed to the lower average cw-equivalent power, which essentially reduces the number of photogenerated carriers in the higher shells that eventually feed the ground state of the molecule within less than 1 ns. Moreover, in our method of calculation, the number of detection events considered genuine photon triplet counts is also a function of the ratio between the pulsed laser repetition rate and $\tau_{XX}X_R$, $\tau_{XX}X_1$ or $\tau_{XX}$, because longer lifetimes increase the probability of photon correlation between, e.g., $X_R$ and re-excited $XX_1X_R$ or $X_1X_R$ from consecutive cycles. We predict that under coherent excitation, the background noise and the amplitude of the side peaks would drastically drop and the maximum triplet count rate would increase up to 17 kHz at the given efficiencies. Nevertheless, the above rate still tops the rates of direct photon

**Figure 3** | Bunching visibility and triple coincidence counts under pulsed excitation. (a,b) Normalized cross-correlations of the $XX_1X_R$ resonance with the $X_1X_R$ and $X_R$ resonances measured at eight increasing power densities starting from 220 mW mm$^{-2}$. The histograms are colour-coded according to the applied pumping levels. (c) The triple coincidence histogram measured in 80 min plotted versus $\tau_{21}$ and $\tau_{31}$ and linearly interpolated with a colour-mapped surface. The blue plane, at 114 counts, indicates the threshold level separating genuine photon triplet counts from the partially correlated photon counts.
triplet generation employing SPDC under pulsed pumping by an order of magnitude.\(^\text{37}\)

**Discussion**

Creating entangled photon triplets, as opposed to time correlated ones, remains as the next-step study goal to our present observations. The prospects of tripartite photon entanglement include, but are not limited to, multipartite quantum secret sharing, other quantum communication protocols,\(^\text{38,39}\) and third party cryptography. As a relevant example, tripartite time-bin entanglement\(^\text{40}\) could be realized using the spin states of a triexciton bound in a QDM. Time-bin encoding has a clear benefit for long distance quantum communication through optical fibres because the relative phase between each two pulses with a few nanosecond temporal spacing is merely susceptible to a medium varying faster than this timescale. Implementing this kind of entanglement in a QDM, however, demands resonant pumping of the triexciton to encode the laser phase onto the emitted photon triplet in a relatively depolarization-free process.\(^\text{16}\) In contrast to incoherent, pulsed excitation, almost susceptible to a medium varying faster than this timescale. Incoherent, pulsed excitation is merely optical fibres because the relative phase between each two pulses with a few nanosecond temporal spacing is merely susceptible to a medium varying faster than this timescale.

\[ T = \frac{1}{\sqrt{2}} \left( \begin{array}{cc} 1 & 1 \\ -1 & 1 \\ 1 & -1 \end{array} \right), \quad \{ \uparrow \uparrow \downarrow \} \ ( \{ \uparrow \downarrow \uparrow \} \) denote the electron (heavy hole) spin localized in the left (L) or the right (R) quantum dot. \( S_L, S_R \) could then decay to the \( \{ S_L, S_R \} \) \( \{ \uparrow \downarrow, \downarrow \uparrow \} \) biexciton states, followed by a second and eventually a third transition to \( S_L, S_R \) and the ground state \( S_L \) (see Supplementary Note 6 for the detailed diagram). These transition paths provide four sets of triple decays emitting three polarized photons \( H_1H_2H_3, V_1V_2H_3, H_1H_2V_3 \) and \( V_1V_2V_3 \) in the H and V linear basis, either of which could be used, for example, to create Greenberger–Horne–Zeilinger\(^\text{10}\) time-bin entangled photon triplets. Here, the coherent pumping of the triexciton is feasible through either employing three different coloured lasers in resonance with the transitions of interest or pumping virtual levels.\(^\text{16}\) In either case, the output pulse of the lasers would be split into two pulses, early \((e)\) and late \((l)\). At sufficiently low pumping powers, a triexciton is formed by either the early or late pulse and the wavefunction of the three emitted photons can be represented as \( 1/\sqrt{2} (e_1e_2e_3 + e^{i\phi}l_1l_2l_3) \). \( \phi \) is the phase of the sum in the pumping interferometers, which will be added to the phases of the three analysing interferometers in a time-bin measurement.

At first glance, our rather low emission rate of photon triplets under the incoherent pulsed excitation regime might imply an inefficient generation of entangled photon triplets using QDMs. However, we predict a drastic improvement of the photon triplet counts under resonant excitation due to the profound suppression of background noise and accidental coincidences. In this case, the triplet generation rate is approximately given by \( \eta_{\text{exc}} \eta_{\text{p}} \eta_{\text{D2}} \eta_{\text{D3}} \eta_{\text{NS4}} \eta_{\text{NS5}} \eta_{\text{NS6}} \eta_{\text{NS7}} \eta_{\text{NS8}} \eta_{\text{NS9}} \eta_{\text{NS10}} \), where \( \eta_{\text{p}} \) denotes the pulse repetition rate, and \( \eta_{\text{exc}} \) is the excitation probability of the triexciton, which can potentially reach up to 90% with an optimized pulse length as previously demonstrated for the biexciton.\(^\text{41}\) Under such circumstances, improving the detection efficiency, for example, by employing near-ideal superconducting nanowire photodetectors,\(^\text{42}\) or enhancing the light extraction efficiency, by embedding a reflective layer under the nanowire base,\(^\text{21}\) could potentially boost the integrated triplet counts by two orders of magnitude.

In conclusion, we have demonstrated that a triexciton bound in a QDM can originate time-ordered photon triplets in a cascaded process. We expect to improve the triplet generation rate by reducing the inter-dot energy splitting, deterministic coherent pulsed excitation of the triexciton to reduce the background, and enhanced collection efficiency. Triple excitons forming in the s shells of a QDM should, in principle, benefit from far better coherence properties than \( p \)-shell excitons in single quantum dots, because their coherence time \( T_2 \) is not subject to the dephasing caused by the \( p \)-to-\( s \) phonon scattering relaxation. The necessity of populating higher shells in single quantum dots also requires strong optical pumping, which further adds to the spectral diffusion and the photon decoherence problem. The inhomogeneous broadening observed in our current QDM samples, however, arises from the stacking faults in the nanowire, which function as efficient charge traps and cause the spectral wandering.\(^\text{43}\) The density of such stacking faults is expected to be reduced by improving the molecular beam epitaxy growth conditions at higher temperatures (500°C) in the near future. With the earlier demonstration of multiple dot-based quantum key distribution,\(^\text{44}\) our device facilitates the implementation of multiparty quantum secret sharing on integrated semiconductor chips.

**Methods**

**Nanowire-QDM fabrication.** The InP nanowires with embedded InAs\(^\text{p}\) quantum dots are grown using selective-area vapour–liquid–solid epitaxy. The nanowires are grown on an SO\(_2\)-patterned (111)B InP substrate. The pattern consists of circular holes defined using electron-beam lithography and hydrofluoric acid wet-etch. A single gold particle is deposited in each hole using self-aligned lift-off process, with the size of the particle determined by the hole size and the thickness of the deposited gold. We employ chemical beam epitaxy with trimethylindium and pre-cracked PH\(_3\) and AS\(_3\) sources. The growth temperature is 420°C. Two growth modes are utilized to grow a nanowire core, which defines the quantum dots, and a shell, which defines the cladding of photonic nanowire.

The nanowire core is grown under a reduced PH\(_3\) flow resulting in an untapered InP nanowire with a diameter corresponding to the gold catalyst particle, typically 20 nm in this work. The nanowire core is pure phase wurtzite with less than 1 stacking fault per micrometre.\(^\text{20}\) The double InAs\(^\text{p}\) quantum dots are grown by switching the group \( V \) species from phosphorous to arsenic to grow the first dot, switching back to phosphorous to grow the InP spacer, then switching back to arsenic to grow the second dot while maintaining a constant flux of trimethylindium. Samples were dot-doped with quantum-wire emission between 2.5 and 3 ps, and with spacer times of 10, 15, and 60 s. The interdot spacing for a given growth time between dots depends on the core diameter due to a diameter-dependent growth rate.\(^\text{45}\) By using a diameter-dependent growth model,\(^\text{45}\) we calculate an interdot separation of 8–20 nm for core diameters of 18–24 nm. Details of the spacer-dependent interdot coupling are beyond the scope of this work and will be published elsewhere. The spacer of QDM studied here is 10–7 nm that provides the optimum coupling. The nanowire shell is grown by increasing the PH\(_3\) flow rate by a factor of three, which reduces the indium adatom migration length and promotes deposition on the nanowire sidewall facets. The shell is grown to reach base diameters of 250 nm, resulting in nanowires with heights of \( \sim \) 10 μm and tapers of \( \sim \) 2°.

**Optical experiments.** The sample is cooled down to 6 K in a customized and thermally stabilized liquid-helium continuous-flow cryostat. The QDM is nonresonantly excited either by a cw or a ps-pulsed Ti:Sapphire laser at 820 nm with 8.4 ps (or 2.6 ps for the cross-correlation measurement) pulse duration (80 MHz repetition rate) slightly above the wurtzite InP band gap 1.49 eV (832 nm) and the donor–acceptor recombination level 1.44 eV (861 nm). We excite the QDM via a separate objective rather than the collecting objective even though this is not reflected in the setup schematic in Supplementary Note 1. The molecule luminescence is collected using an objective lens with a numerical aperture of 0.7 and dispersed by grating monochromators with a spectral resolution of \( \sim 0.01 \) nm to split the spectral lines and send the respective photons into separate avalanche photodiodes (APD). APDs are identical with 300 ps temporal resolution and \( \geq 25\% \) (\( \geq 15\% \)) detection efficiency at 893 nm (940 nm). The combination of spectrometer and charge coupled device camera enables performing \textit{in situ} spectroscopy during the recording of counts in the correlation measurement setup (composed of APDs and ps time-tagging module). Only two APDs register the photon counts to conduct the autocorrelation and the conventional dual-channel cross-correlation analysis, whereas all the three APDs are in use for the triple coincidence experiment. In the dual-channel correlation measurements, the HE set
resonances are cross-correlated utilizing two 5 μm core optical fibres for photon collection. In the triple coincidence experiment, we collected from the LE set using a single mode fibre with 9 μm core optimized for the telecommunication wavelength, which operates as a multimode fibre at 940 nm. The multimode character improves the collection efficiency without the requirement for an optimized mode matching. However, owing to the small core radius the background light picked up from X0 is suppressed and the antibunching dip in the triple coincidence histogram is improved compared to the 125 μm core multimode fibre. To estimate the extraction efficiency of the nanowire, we calculate the probability of a bieexciton-exciton coincidence $\eta_{\text{E}2\text{X}1}$ from the dual-channel cross-correlation histogram to be 0.54%, which yields $\eta_{\text{E}2\text{X}1} = 46\%$. To produce the detector-dependent cross-correlation histograms in the cw excitation mode, we started from 220 mW mm$^{-2}$ (with 4 μm spot size and the excitation objective tilted 22° from the optical table axis) and raised the pump power to linearly increase the indirect bieexciton luminescence $X0X0$. Therefore, the pump power scales up approximately in a quadratic fashion until the $X0X0$ resonance is saturated. To resolve the associated lifetimes, the QDM is heavily pumped within each pulse using the Ti:Sapphire laser in a way that its resulting spectrum exactly resembles the one under cw excitation. In the triple coincidence experiment under pulsed excitation, the pumping power was adjusted to 40 μW (with 2.6 ps pulse duration), which translates to a peak intensity of 905 mW mm$^{-2}$. The temporal resolution of the detectors D1, D2 and D3 was set to 512 ps. The laser spot size was approximately 7.5 μm on the sample (measured perpendicular to the beam, which was aligned under an angle of approximately 50° with respect to the nanowire axis). For the magneto-optical measurements the setup remains unchanged except that the cryostat is replaced by a continuous flow exchange gas cryostat with a T split-pair superconducting magnet. The QDM was excited co-linearly to the collection through the collection objective with a Ti:Sapphire laser. For the mixed Voigt-Faraday (tilted) configuration the sample was rotated 12° inside the cryostat.

Data availability. The data that support the findings of this study are available from the corresponding author upon request.

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Author contributions
M.K. conceived the idea and developed the theory. M.K. and D.D. designed the QDM. D.D., J.L., X.W.P. and F.P. fabricated the nanowire-QDMs. M.K., A.P. and T.H. designed the photon statistics experiments. T.H., A.P. and M.P. accomplished the photon correlation measurements. M.K., A.P. and B.L. designed the magneto-optical measurements conducted by A.P., P.T. and M.P. T.H., A.P. and M.P. compiled the data and M.K. carried out the data analysis and wrote the manuscript with feedback from all co-authors. G.W. and H.M. supervised the project and contributed to the manuscript.
