Nanoscale magnetic field imaging for 2D materials

Review Article

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Imaging weak magnetic field patterns on the nanometer-scale and its application to 2D materials

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Abstract

Nanometer-scale imaging of magnetization and current density is the key to deciphering the mechanisms behind a variety of new and poorly understood condensed matter phenomena. The recently discovered correlated states hosted in atomically layered materials such as twisted bilayer graphene or van der Waals heterostructures are noteworthy examples. Manifestations of these states range from superconductivity, to highly insulating states, to magnetism. Their fragility and susceptibility to spatial inhomogeneities limits their macroscopic manifestation and complicates conventional transport or magnetization measurements, which integrate over an entire sample. In contrast, techniques for imaging weak magnetic field patterns with high spatial resolution overcome inhomogeneity by measuring the local fields produced by magnetization and current density. Already, such imaging techniques have shown the vulnerability of correlated states in twisted bilayer graphene to twist-angle disorder and revealed the complex current flows in quantum Hall edge states. Here, we review the state-of-the-art techniques most amenable to the investigation of such systems, because they combine the highest magnetic field sensitivity with the highest spatial resolution and are minimally invasive: magnetic force microscopy, scanning superconducting quantum interference device microscopy, and scanning nitrogen-vacancy center microscopy. We compare the capabilities of these techniques, their required operating conditions, and assess their suitability to different types of source contrast, in particular magnetization and current density. Finally, we focus on the prospects for improving each technique and speculate on its potential impact, especially in the rapidly growing field of two-dimensional materials.

Introduction

In the early 1800s, images of the stray magnetic fields around permanent magnets and current-carrying wires made with tiny iron filings played a crucial role in the development of the theory of electromagnetism. Today, magnetic imaging techniques continue to provide invaluable insights well beyond producing pretty pictures. They shed light on magnetization patterns, spin configurations, and current distributions, which are invisible in optical or topographic images. Unlike bulk measurements of transport, magnetization, susceptibility, or heat capacity, they provide microscopic information about length-scales, inhomogeneity, and interactions. This kind of local information is proving crucial

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in ongoing efforts to understand and harness an emerging class of two-dimensional (2D) van der Waals (vdW) materials and their heterostructures.

The demonstration of the first graphene device in 2004 [1] launched the field of 2D and layered materials. Graphene itself, however, represents just one of manifold atomically thin vdW materials with a variety of compositions and crystal structures. Furthermore, heterostructures of these materials can be engineered, due to the weak vdW interactions that typically dominate their interlayer coupling: these interactions allow the stacking and twisting of individual atomically thin layers without lattice mismatch adversely affecting the quality of the structure. This flexibility in both material choice and structure design has led to the synthesis and fabrication of 2D materials with a range of properties than span those of insulators, semiconductors, and metals.

Recent observations of correlation phenomena such as superconductivity, Mott insulating states, and magnetically ordered states in such materials are particularly intriguing and are just beginning to be understood. Such macroscopic manifestations of quantum mechanics are sensitive to the local environment. In many cases, nanometer-scale spatial resolution is required to investigate and identify the conditions for their emergence. As a result, there is now an urgent need for sensitive and high-resolution imaging to zero-in on the nanometer-scale mechanisms behind these phenomena. In particular, the techniques most adept at tackling this problem are scanning probe microscopies (SPMs) designed to map subtle magnetic field patterns non-invasively. In 2D systems, such maps can be used to image magnetization configurations and charge transport, giving crucial local information on quantum phases, including on the spatial variation of order parameters, the presence of domains, and the role of defects.

In the last few decades, the development of magnetic imaging technologies has been driven by applications in magnetic storage and information processing. The need to understand magnetostatics and dynamics on the nanometer-scale and with high temporal resolution has led to powerful optical, electron, x-ray, and scanning probe microscopies. There are a number of excellent reviews on these techniques and their myriad applications [2–7]. Most of these techniques, however, are not suitable for resolving the weak contrast produced by both magnetization and current density in atomically thin vdW materials.

This Technical Review focuses on the subset of state-of-the-art techniques best equipped for this timely task. Scanning superconducting quantum interference device (SQUID) microscopy has already demonstrated its ability to map superconducting currents [8] and magnetization [9] in magic-angle twisted bilayer graphene (MATBG) or quantum Hall edge channels in mono-layer graphene [10,11]. Scanning nitrogen-vacancy (NV) center microscopy has been used to image layer-dependent magnetization in Cr-based vdW magnets [12–14], as well as hydrodynamic electron flow in graphene [15,16] and WTe$_2$ [17]. Sensitive forms of magnetic force microscopy (MFM), including dissipation microscopy and nanowire (NW) MFM [18,19], are also poised to make an impact.

We treat these techniques in the following, briefly explaining how each works and specifying its magnetic sensitivity and spatial resolution limits. We also touch on the process of reconstructing spatial maps of measured magnetic field into images of magnetic moment or current. Finally, we compare the different microscopies and speculate on which is most suitable for which type of contrast and how each might best be applied in measurements of 2D materials.
Figure 1: Recent SPM measurements of magnetic field on 2D systems. On the left are measurements carried out by SSM (clockwise from top left): [8–10]; on the right by SNVM (clockwise from top): [12,13,15]. Measurements show magnetic field due both to magnetization and current density.

Imaging magnetization and current
Mapping magnetization patterns is important for investigations of magnetic domains, antiferromagnetism, magnetic skyrmion phases, and the spin-Hall effect. Measurements directly sensitive to magnetization include synchrotron-based x-ray techniques, neutron diffraction, and electron polarization techniques. For most, the tiny total magnetic moment of atomically-thin materials complicates their application to 2D systems. Particularly sensitive techniques such as magneto-optic microscopy and spin-polarized scanning tunneling microscopy have been used to reveal layer-dependent magnetism in flakes of CrI$_3$ [20] and films of CrBr$_3$, grown by molecular beam epitaxy [21], respectively. However, the spatial resolution of magneto-optical techniques is limited to the micrometer-scale and interference effects can obscure magnetic signals in thin samples. SP-STM requires atomically-clean conducting surfaces, which can often only be obtained by thermal annealing. Because many magnetic vdW materials are volatile at high temperatures, this step is sometimes not possible. Magnetic imaging via the magnetic circular dichroism of x-ray photoemission electron microscopy has not yet been applied to 2D systems. Nevertheless, its sensitivity should be sufficient to resolve single layer magnetism [22]. Huang et al. provide a recent survey on the application of magnetization-sensitive techniques to 2D materials and especially to 2D magnets [23].
Here, we consider techniques capable of mapping magnetic stray field, because they are applicable to a wider set of phenomena than direct magnetization imaging. Stray fields are produced not only by magnetization patterns, but also by current distributions. Transport imaging can be used to visualize local disorder, bulk and edge effects, electron guiding and lensing, topological currents, viscous electron flow, microscopic Meissner currents, and the flow and pinning of superconducting vortices. Common methods of mapping field include the use of fine magnetic powders as demonstrated by Bitter, Lorentz microscopy, electron holography, and a number of SPM techniques. Those most applicable to 2D systems, for their combination of high spatial resolution and high magnetic field sensitivity, are MFM, scanning SQUID microscopy (SSM), and scanning NV center microscopy (SNVM).

Although, in general, a map of magnetic field cannot be reconstructed into a map of the source current or magnetization distribution, under certain boundary conditions the source can be uniquely determined. In particular, for 2D structures such as 2D materials, patterned circuits, thin films, or semiconductor electron and hole gases, a spatial map of a single magnetic field component can be used to fully reconstruct the source current or out-of-plane magnetization distribution. Since some of the most interesting and elusive effects are observed over length-scales of less than 1 µm and with currents less than 1 µA or magnetizations of few µB/nm², techniques are required with both nanometer-scale spatial resolution and a sensitivity to fields smaller than a µT.

Figure 2: Schematic showing the principal magnetic imaging techniques and sources of magnetic field discussed in this review.
Imaging weak magnetic field patterns with high spatial resolution

In SPM, high spatial resolution is achieved by minimizing both sensor size and its distance from the sample. High sensitivity is obtained by maximizing signal-to-noise ratio for the magnetic signal of interest and the fundamental noise of the measurement. In evaluating the sensitivity of different techniques to magnetic contrast, we follow Kirtley [24] and consider their response to two idealized sources of magnetic field: a magnetic dipole moment and a line of current. This procedure allows us to assess and compare the sensitivity of each technique to magnetization and current density in a sample below.

Magnetic force microscopy

Working principle and conditions

Near surfaces, the most common technique for imaging magnetic fields with high spatial resolution is MFM, which was introduced in the late 1980s as a natural extension of atomic force microscopy [25,26]. Contrast results from the magnetostatic interaction between the stray magnetic fields of a sample and the magnetic tip of a mechanically compliant scanning probe. The vibration frequency and amplitude of a cantilever probe, whose tip has been coated with a ferromagnetic film, are recorded as the probe is scanned above a sample. The response typically depends on a gradient of the stray field. Although some simplifying assumptions can often be made, extracting exact magnetic field maps from MFM images involves a deconvolution requiring knowledge of the shape and magnetization configuration of the tip.

MFM is possible under a wide variety of conditions, including in air, liquid, vacuum, and over a broad range of temperatures. As shown in Fig. 3, a MFM system consists of the cantilever, piezoelectric positioners for moving the sample, and a setup for detecting cantilever motion, usually by optical deflection or interferometry. Scan areas are typically in the range of a few micrometers on a side and take several minutes. The cantilever’s mechanical frequency, typically a few hundred kHz, sets the upper limit on the speed of the dynamics that can be measured. In fact, measurement bandwidths are limited to tens of Hz due to the linewidth of the mechanical resonance or the speed of the phase-locked loop used for determining the cantilever’s frequency.

Cantilevers are typically made from Si, SiO$_2$, or Si$_3$N$_4$ and their tips are coated with a magnetic film of Co or Ni. Because cantilevers are optimized to probe surfaces on the atomic-scale, they are designed to have spring constants around 1 N/m, which is smaller but on the order of spring constant of an atomic bond at the surface of a solid. As a result, conventional MFM can have extremely high spatial resolution, down to 10 nm [27,28] at cryogenic temperatures and in vacuum, but more typically from 30 to 100 nm. This large spring constant, however, makes MFM responsive only to strong magnetic field modulations on the order of tens of T/(m Hz$^{1/2}$) (few $\mu$T over 100 nm measured in 1 s). It is, therefore, well-suited for the measurement of highly magnetized samples, however, ineffective for detecting the weak stray fields produced by subtle magnetization patterns or Biot-Savart fields of currents flowing through nanometer-scale devices.

The advent of cantilever probes consisting of individual nanowires (NWs) [29,30] or even carbon nanotubes [31] have given researchers access to much smaller force transducers. This reduction in size implies both a better force sensitivity and potentially a finer spatial resolution [32]. Sensitivity to small forces provides the ability to detect weak magnetic fields and therefore to image subtle magnetic patterns; tiny concentrated magnetic tips have the potential to achieve nanometer-scale spatial resolution, while also reducing the invasiveness of the tip on the sample under investigation.

NWs have been demonstrated to maintain force sensitivities around 1 aN/Hz$^{1/2}$ near sample surfaces (within 100 nm) when operated in high vacuum and at cryogenic temperatures, due to extremely low
noncontact friction [33]. In recent proof-of-principle experiments, both magnet-tipped NWs and fully magnetic NWs were shown to be sensitive to magnetic field gradients of just a few mT/(m Hz\(^{1/2}\)) [10] and a few nT/Hz\(^{1/2}\) [19], respectively. These are the gradients and fields produced by tens of \(\mu_B/\text{Hz}^{1/2}\), where \(\mu_B\) is a Bohr magneton, or several nA/Hz\(^{1/2}\) of flowing current, each at a distance a hundred or so nanometers.

**Sensitivity to different types of contrast**

Depending on the type of transducer and its tip, MFM maps magnetic field or magnetic field gradients. The ultimate noise limiting these measurements is thermal noise acting on the transducer. Such noise causes random fluctuations in the measured vibration amplitude and frequency. As shown in Box 1, thermal noise sets a minimum measurable magnetic field or field gradient, depending on the measurement type and the magnetization configuration of the tip. For example, a frequency shift measurement of a conventional MFM transducer [34] has a thermal limit at 4 K to static gradients of \((\partial \mathbf{B} / \partial r)_{\text{min}} \approx 30 \text{ T/(m Hz}^{1/2}\)). Recently demonstrated NW MFM has a thermal limit for the same measurement that is about 1000 times smaller [19].

**Box 1: MFM**

Force microscopy contrast is generated by the interaction of a cantilever tip with the sample underneath. By monitoring the vibration amplitude, one can measure tip-sample forces at the cantilever resonance frequency, while by monitoring the vibration frequency, one can measure static tip-sample force gradients. The ultimate noise limiting these measurements is the thermal (Brownian) motion of the cantilever. Thermal noise sets a minimum measurable resonant force \(F_{\text{min}} = \sqrt{4 k_B T \Gamma}\) in an amplitude measurement and a minimum measurable static force gradient \((\partial F / \partial r)_{\text{min}} = 1 / \sqrt{4 k_BT \Gamma}\) in a frequency measurement, where \(k_B\) is the Boltzmann constant, \(T\) is the temperature, \(\Gamma\) is the mechanical dissipation, \(r_{\text{rms}}\) is the cantilever oscillation amplitude, and \(\hat{r}\) indicates the direction of cantilever oscillation.

In MFM, the magnetic tip transduces a magnetic field profile into a force profile. This interaction can often be approximated using a point-probe model, in which an effective magnetic multipole – including a monopole \(q\) and a dipole \(\mathbf{m}\) – represents the magnetization distribution of the tip. A magnetic field profile \(\mathbf{B}\) then produces a magnetic force acting on the cantilever given by \(\mathbf{F}_{\text{MFM}} = q \mathbf{B} \cdot \hat{r} + \nabla(\mathbf{m} \cdot \mathbf{B}) \cdot \hat{r}\). Note that, in most cases, the contribution of the torque generated by \(\mathbf{B}\) is negligible. For conventional MFM, where the tip-sample interaction can be approximated by a pure magnetic monopole, this results in a minimum measurable resonant magnetic field \(B_{\text{min}} = 1 / q \sqrt{4 k_BT \Gamma}\) and a minimum measurable static magnetic field gradient \((\partial B / \partial r)_{\text{min}} = 1 / q r_{\text{rms}} \sqrt{4 k_BT \Gamma}\).

Purely dipolar tips, such as those on the ends of some NWs [18], are sensitive to a further spatial derivative of the magnetic field, compared to monopolar tips. Similar expressions can be written limiting those measurements.

By comparing the thermal noise background to the expected magnetic field or field gradient from a single Bohr magneton \(\mu_B\) or a line or current \(I\), as calculated in Box 2, we can assess the sensitivity of MFM. For example, conventional MFM scanning 50 nm above a sample is sensitive to frequency shifts equivalent to a magnetic moment of a few thousand \(\mu_B/\text{Hz}^{1/2}\) or currents of a few mA/Hz\(^{1/2}\) [34]. The same type of measurement carried out with newly demonstrated NW MFM probes 100 nm above a sample is about 100 times more sensitive to each type of contrast [18,19]. Estimates of sensitivity to magnetic moment and current as a function of probe-sample spacing are shown in Figs. 4 a) and b).
It should be noted that the thermal limit on frequency measurements is rarely reached in practice. Most frequency measurements are limited by other noise sources, such as temperature variations, adsorption-desorption noise, or other microscopic mechanisms intrinsic to the resonator, that are typically an order of magnitude larger [35]. On the other hand, measurements of resonant oscillation amplitude, which are sensitive to modulations at the mechanical frequency of the sensor (typically in the 100 kHz regime), are often thermally limited. In such measurements, conventional MFM cantilevers can be sensitive to a few hundred $\mu_B/Hz^{1/2}$ or a few hundred nA/Hz$^{1/2}$, while NW MFM transducers reach down to a few $\mu_B/Hz^{1/2}$ or a few nA/Hz$^{1/2}$.

**Box 2: Magnetic field sources**

The magnetic field of a magnetic moment $m$ at distance $r$ is given by $B_m = \frac{\mu_0}{4\pi r^3} \left(\frac{3(m \cdot r)r}{r^2} - m\right)$ and the magnetic field of a line of current $I$ is given by $B_I = \frac{\mu_0 I \times r}{2\pi r^2}$, where $\mu_0$ is the vacuum permeability.

Using these two equations, we can express the various quantities measured by our scanning probe sensors as a function of tip-sample spacing in terms of $\mu_B$ of magnetic moment or $A$ of current. For example, for SNVM measuring the $z$-component of the stray magnetic field, the maximum measurable signal from a single $\mu_B$ moment pointing along the $z$-direction at a tip-sample spacing $z$ is $B_{\mu_B z} = \frac{\mu_0 \mu_B}{2\pi z^3}$, while the maximum from a line of current $I$ flowing in the plane is $B_{I,z} = \frac{\mu_0 I}{4\pi z}$. Similar expressions can be written for the maximum magnetic flux in the $z$-direction from the same moment and current measured by SSM: $\Phi_{\mu_B z} = \frac{\mu_0 \mu_B R^2}{2(2z^2+R^2)^{3/2}}$, where $R$ is the SQUID radius and $\Phi_{I,z} = \frac{\mu_0 D}{4\pi} \ln \left(\frac{D^2+4z^2+D\sqrt{D^2+4z^2}}{D^2+4z^2-D\sqrt{D^2+4z^2}}\right)$, where $D$ is the length of one side of a square SQUID loop (to simplify the calculation, the current is integrated over a square rather than a circular loop). The corresponding maximum static magnetic field gradients measured by standard MFM are: $\frac{\partial B_{\mu_B z}}{\partial z} = \frac{3\mu_0 \mu_B}{2\pi z^4}$ and $\frac{\partial B_{I,z}}{\partial z} = \frac{3\sqrt{3} \mu_0 I}{16\pi z^2}$.

**Applications to 2D materials**

Despite the lack of conventional MFM studies on 2D materials, researchers are starting to employ high-sensitivity MFM probes to visualize correlated states in 2D systems via frequency shift maps, which can ultimately be reconstructed in current density or magnetization contrast. Such images would be particularly useful for measuring the spatial localization of flowing currents, as in edge states, and for the determination of length scales such as magnetic domain sizes and coherence lengths. Visualizing current flow in MATBG [36] and WeTe$_3$ [37,38] while they are electrostatically tuned into their superconducting states, would help reveal the origin of this superconductivity and whether or not it is topological. NW MFM may also help provide direct evidence for magnetism in 2D magnets or even in the 2D semiconductor, monolayer MoS$_2$ [39,40]. Optical spectroscopy has provided evidence of a high-field spin-polarized state in this material, however, confirmation of its presence via a direct measurement of magnetic field has not yet been possible. NW MFM’s high sensitivity and ability to operate in high-field conditions make it promising for such an investigation.

MFM can also be used to map dissipation in a sample by measuring the power required to maintain a constant oscillation amplitude. This type of contrast maps the energy transfer between the tip and the sample and provides excellent contrast for nanometer-scale magnetic structure [41]. Since energy dissipation plays a central role in the breakdown of topological protection, it may provide important contrast in spatial studies of strongly correlated states in 2D vdW materials. Dissipation contrast has been used to observe superconducting [42] and bulk structural phase transitions [43], as well as the local density of states. 2D materials engineering allows for the fabrication of devices, in which a variety
of different physical phases can be accessed by the application of a gate voltage. Local measurements of dissipation via MFM could be an important tool for making spatial maps of the transitions between those states.

Figure 3: Representative schematic diagrams for the field-sensitive SPMs most applicable to 2D systems for their combination of high spatial resolution and high magnetic field sensitivity. From top to bottom these are NW MFM, SSM via SOT, and SNVM. In the bottom portion, each diagram shows
a sample mounted on a movable stage, actuated by piezoelectric positioners. For scale, the white sample-holder in each diagram is 12 x 12 mm in lateral size. Above this sample, is the scanning probe along with its corresponding readout scheme. Insets show zoomed-in views of each probe, which more clearly depict the detection schemes. For NW MFM, in red, incident from the right, we see the focused laser light used for interferometric detection of the NW’s flexural motion. For the SSM, we see the mechanically-coupled tuning fork used for tip-sample distance control. For the SNVM, in green, incident from above, we see focused laser light for NV excitation.

Scanning SQUID microscopy

Working principle and conditions

Taking advantage of a SQUID’s extreme sensitivity to magnetic flux, SSM was first realized in the early 1980s [44]. Contrast results from the magnetic flux threading through a superconducting loop that is interrupted by at least one JJ. The SQUID’s critical current is periodic in this flux – given by the magnetic field integrated over the area of the loop \(\Phi_z = \int B \cdot dA\) – with a period given by the flux quantum \(\Phi_0\). By applying the appropriate current bias, one can detect voltages across the SQUID which correspond to changes in magnetic field threading the SQUID loop corresponding to factions of a \(\Phi_0\), typically down to \(10^{-6} \Phi_0/\hbar^2/2\). For imaging applications, a DC SQUID with two JJs is most often used. This loop – or a pick-up loop inductively coupled to it – is scanned above a target sample in order to map the magnetic field profile. The loop’s size is minimized in order to optimize spatial resolution. SQUIDs operate only below a superconducting transition temperature, which is typically below 10 K, but can be above the temperature of liquid nitrogen (77 K) for some high-T\(_c\) superconductors.

As shown in Fig. 3, an SSM system consists of the SQUID sensor or pick-up loop and piezoelectric positioners for moving the sample. In high-sensitivity and high-resolution applications, these elements are in a cryostat and in vacuum. Precise control of the sensor-sample distance can be achieved, for example, by coupling it to a micromechanical tuning fork [45,46]. As in MFM, scan areas are in the micrometer range and take several minutes. The SQUID sets the system’s ultimate bandwidth, which can be in the GHz range, however stray capacitance, cabling, and detection electronics typically limit the bandwidth to tens of MHz or below.

As imaging resolution has improved from the micrometer- down into the nanometer-scale, a number of strategies have been employed to realize ever-smaller sensors, which simultaneously retain high magnetic flux sensitivity and can be scanned in close proximity to a sample. One strategy has involved miniaturizing the pick-up loop of a conventional SQUID and placing it at the extreme corner of the chip where it can come close to a sample. The most advanced of such devices use a loop with a 200-nm inner diameter to achieve sub-micrometer imaging resolution and a sensitivity of 130 nT/Hz\(^{1/2}\) [47]. Although this design has the advantage of allowing for susceptibility measurements, the size of the sensor and minimum distance from the sample, which together determine the imaging resolution, are limited by the complex fabrication process. In the last decade, this limitation has been addressed through the development of SQUID-on-tip (SOT) sensors, consisting of a SQUID fabricated by shadow evaporation or directional sputtering of a metallic superconductor directly on the end of a pulled quartz tip [48,49]. This process has resulted in scanning SQUID sensors with diameters down to 50 nm, 100 nm imaging resolution, and a sensitivity of 5 nT/Hz\(^{1/2}\) [50].

Sensitivity to different types of contrast

The noise limiting the measurement of magnetic flux in a SQUID arises from several sources including Johnson noise, shot noise, 1/f noise, and quantum noise [24]. For SQUIDs smaller than 1 \(\mu\)m and at frequencies high enough to avoid 1/f noise, quantum noise sets the fundamental limit on detectable flux to be \(\Phi_Q = (\hbar L)^{1/2}\), where \(\hbar\) is Planck’s constant and \(L\) is the loop inductance [24,51,52]. State-
of-the-art SOT sensors made from Pb combine the highest flux sensitivity with the smallest sensor
size. In the white-noise limit (measured in the kHz range), sensors with 50 nm diameter reach \( \Phi_{\text{min}} = 50 \, \mu \Phi_0/\text{Hz}^{1/2} \), which is about 4 times larger than \( \Phi_0 \) [50]. Near DC (measured in the Hz range), where
the same sensor is limited by 1/f noise, \( \Phi_{\text{min}} \) is about 10 times larger. In these devices, \( L \) is dominated
by kinetic rather than geometric inductance. For this reason, optimizing material parameters for low
kinetic inductance provides the best route for improving \( \Phi_{\text{min}} \).

What this sensitivity means in terms of magnetization or current sources requires knowing the tip-
sample spacing. Using the best 50-nm-diameter SOT at a spacing of 50 nm – closer approach than the
characteristic sensor size does not improve spatial resolution – the white noise level is equivalent to
the field of a few \( \mu \Phi_0/\text{Hz}^{1/2} \) or a few tens of nA/Hz^{1/2}, while at DC the device is ten times less sensitive.
Again, such estimates are shown as a function of probe-sample spacing in Figs. 4 a) and b).

**Applications to 2D materials**

SSM has already been successfully used to image current density via local measurements of Biot-
Savart fields. In particular, maps of the flow of equilibrium currents in graphene made using SOT
probes revealed the topological and non-topological components of edge currents in the quantum
Hall state [10]. The non-topological currents, which are of opposite polarity to the topological
currents, were predicted theoretically [53], but are not typically considered because they do not affect
conventional transport measurements [54]. In fact, although previous SPM experiments, including
Kelvin probe [55], scanning single-electron transistor [56], and scanning capacitance [57], revealed the
presence of compressible and incompressible regions, non-topological currents were never observed.
This new insight into the microscopic make-up of orbital currents in the quantum Hall systems was
made possible by the SSM’s sensitivity to tiny magnetic fields. Similar images of equilibrium currents
in MATBG, revealed the twist-angle disorder in these samples with a resolution and over an extent
not possible by other techniques [8]. In those experiments, SSM also provided a direct correlation
between the degree of disorder and the presence of correlated states, including superconductivity. In
another set of measurements, SSM with the same kind of SOT sensor found evidence for orbital
magnetism in twisted bilayer graphene [9]. Images of the weak orbital magnetization and the
presence of micrometer-scale domains, both of which have not been previously observed, were –
once again – made possible by the technique’s sensitivity to magnetic field combined with its spatial
resolution.

Given the SOT’s exquisite sensitivity to local temperature, such probes can also be applied to measure
local sources of dissipation, as was demonstrated in experiments on graphene [58,59]. Similar
scanning probe measurements of magnetic field and dissipation could be carried out on other moiré
systems, including twisted transition metal dichalcogenides and twisted multi-layer graphene. These
systems are also predicted to host a variety of correlated states, including superconductivity, Mott
insulating states, magnetic states, and Wigner crystal states [60].

**Scanning NV center microscopy**

**Working principle and conditions**

Following proposals in 2008 pointing out its potential for high-resolution, high-sensitivity magnetic
field imaging [61,62], the last decade has seen a flurry of activity in the development of SNVM. In this
scheme, NV centers, which are optically addressable electronic defect spins in diamond, are used as
scanning single-spin sensors. Magnetic field measurements are carried out via optically-detected
magnetic resonance (ODMR) spectroscopy, where the EPR spectrum of the NV is recorded by
simultaneous microwave excitation and optical readout of the defect’s spin state as the probe is
scanned in close proximity to the sample surface. Thanks to the technique of single-molecule
fluorescence, these experiments can be performed on a single spin [63]. The magnetic field sensitivity results from a Zeeman shift of the spin resonances. In the regime of a weak orthogonal component of an external magnetic field, the field component parallel to the NV symmetry axis leads to a linear shift of the \( m_s = \pm 1 \) spin states with a proportionality given by the free-electron gyromagnetic ratio \( \gamma = 2\pi \times 28 \text{ GHz/T} \) [64]. The ODMR spectrum is measured as a change in optical intensity as a function of continuous-wave or pulsed microwave excitation [65]. Other forms of contrast include ODMR quenching in magnetic fields larger than 10 mT due to energy-level mixing by the off-axis field component [66,67] and spin relaxometry [83]. The latter probes high-frequency fluctuations near the NV resonance (GHz range) and allows for the investigation of magnetic fluctuations and spin waves in ferromagnets [68–70]. Further, dynamical decoupling techniques can be used to perform frequency spectroscopy in the kHz-MHz range [71,72].

In scanning probe applications, as shown in Fig. 3, the NV center is hosted within a crystalline diamond nanopillar and scanned over the sample of interest [61,73]. State-of-the-art diamond probes are engineered with shallow NV centers, which are implanted at depths around 10 nm [74], in order to minimize the distance between the NV center and the sample and thus to optimize both sensitivity and spatial resolution. However, in most SNVM literature, the NV stand-off distance is 50 to 100 nm, indicating that NV centers may be deeper than expected. As in MFM and SSM, the sample is scanned below the probe, usually using piezoelectric positioners, while precise distance control is achieved by coupling to a micromechanical tuning fork. An objective lens above the probe is used to optically excite the NV center and to detect its fluorescence.

Using advanced sensing protocols and sequences of microwave and laser pulses, scanning NV center microscopes have achieved field sensitivities down to a few \( \mu \text{T}/\text{Hz}^{1/2} \) [75] for DC signals and around 100 nT/Hz\(^{1/2} \) [17] for AC signals. The best resolutions reported for scanning setups are between 15 and 25 nm [76,77], although resolution better than 10 nm should ultimately be possible for optimized scanning tips with very shallow NV centers. On top of high sensitivity and spatial resolution, scanning NV microscopy offers additional benefits: a large temperature range — including room temperature — a quantitative measurement of the magnetic field that is intrinsically calibrated via natural constants, vector sensitivity, and a number of spin manipulation protocols for performing spectroscopy from DC to GHz signal frequencies.

These advantages notwithstanding, scanning NV microscopy remains challenging at high fields due to the high microwave frequencies (10s to 100s of GHz) required to actuate the sensor electron spin, and the spin-level mixing for magnetic fields that are not aligned with the NV symmetry axis [66,67]. Although NV center detection has been reported below 1 K, experiments at cryogenic temperatures are hampered by reduced photoluminescence contrast and poor charge stability. Furthermore, the required optical and microwave excitation sometimes poses a limit on the possible samples, since it can perturb materials such as direct-band-gap semiconductors, nanomagnets, and fragile biological structures.

**Sensitivity to different types of contrast**

SNVM is typically limited by photon shot noise from the optical readout, and can be expressed by a simple signal-to-noise formula typical for optical magnetometry [78]. Specifically, the magnetic sensitivity of the scanning NV magnetometer is determined by a combination of the spin dephasing or decoherence time \( T_2 \), the optical contrast \( \varepsilon \) and the maximum photon count rate \( I_0 \). A generic estimate for the minimum detectable magnetic field is given by \( B_{\text{min}} \approx \gamma \varepsilon \sqrt{I_0 t_{\text{acq}} T_2} \), where \( \gamma \) is the gyromagnetic ratio and \( t_{\text{acq}} \) is the photon integration time. Using typical values (\( \varepsilon = 0.2, \ I_0 = 200 \text{ kC/s}, \ t_{\text{acq}} = 300 \text{ ns}, \ T_2 = T_2^* = 1.5 \text{ ms} \)), the minimum detectable field is about 1 \( \mu \text{T}/\text{Hz}^{1/2} \) for...
pulsed operation and 10 μT/Hz<sup>1/2</sup> for continuous-wave operation. Recent SNVM experiments have shown state-of-the-art pulsed sensitivity of 100 nT/Hz<sup>1/2</sup> [17]. In the future, the sensitivity can be improved by extending T<sub>2</sub> using isotopically-purified (free of <sup>13</sup>C) material [79] and AC magnetometry techniques [80], improving the contrast through alternative readout schemes [81], and improving the count rate by photonic shaping [82,83].

If we assume the best demonstrated pulsed sensitivity and a 25 nm NV-sample distance, SNVM is sensitive to one μB/Hz<sup>1/2</sup> or a few tens of nA/Hz<sup>1/2</sup>. Fig. 2 shows such sensitivity estimates for some of the best SNVM as a function of probe-sample spacing.

Applications to 2D materials

SNVM has been applied to image magnetization in the 2D ferromagnets [12–14] and current flow in graphene [15,16,84] and layered semimetals [17]. Given SNVM’s particularly high sensitivity to magnetic moment, the technique is particularly suited for mapping magnetism in vdW magnets to distinguish domain structure, quantify the strength of the magnetism, and confirm its origin. The ability to distinguish the magnetism of single atomic layers, as first shown in CrI<sub>3</sub> [12] and later in CrBr<sub>3</sub> [13] and CrTe<sub>2</sub> [14], is crucial for investigating the effect of each layer in vdW heterostructures. The ability of SNVM to retain high sensitivity at room temperature and under ambient conditions makes it applicable to magnetic systems with potential practical application in spintronic devices. Sub-micrometer spatial resolution also distinguishes SNVM from optical techniques such a Kerr effect [20,85] and magnetic circular dichroism microscopy [86,87], allowing it to resolve, for example, domain walls pinned by defects [13]. Moreover, its ability to quantitatively measure stray field allows the mapping of local 2D magnetization with a precision not possible via optical techniques. High-frequency sensing with SNVM [88] may also be useful for investigating magnonic excitations in 2D magnets.

Although current mapping at temperatures below 4 K, such as required for studies of superconductivity in 2D materials, is still challenging, SNVM is ideal for experiments across a broad and higher temperature range. In fact, researchers have used SNVM to map hydrodynamic flow in graphene [15] and WTe<sub>2</sub> [17], which is strongest at intermediate temperatures. The ability to measure current flow over a wide range of temperatures, allowed, in both of these systems, the observation of a crossover from diffusive to viscous electron transport. In WTe<sub>2</sub>, SNVM revealed as an unexpected temperature dependence, indicating that strong electron-electron interactions are likely phonon-mediated. Similar studies could be carried out in a plethora of other 2D systems, in which viscous electron transport may dominate under certain conditions.
Figure 4: Comparing sensitivity and resolution. Plots comparing the sensitivity to magnetic moment (a) and current (b) of the 3 magnetic imaging techniques under the most favorable conditions, i.e. in vacuum and at liquid helium temperatures. We use parameters from van Schendel et al. for conventional MFM [34], Mattiat et al. for NW MFM [19], Vasyukov et al. for SSM [50], and Vool et al. for SNVM [17]. MFM and NW MFM sensitivities are based on frequency shift measurements at DC, while SNVM and SSM sensitivities are based on AC measurements usually in the tens of kHz range. (c) Plot showing the characteristic length and magnetic field noise of state-of-the-art scanning magnetic probes under ideal conditions, i.e. in vacuum and at liquid helium temperatures. The characteristic length sets the scale of the possible spatial resolution. Diagonal lines show the sensitivity required to measure the labelled magnetic moments and currents. Data points correspond to state-of-the-art SPMs demonstrated in the corresponding reference: 1, van Schendel et al. [34]; 2, Mattiat et al. [19]; 3, Vasyukov et al. [50]; 4, Kirtley et al. [24]; 5, Jeffery et al. [89]; 6, Vool et al. [17]. (d) Sensitivity as a function of feature size, expressed as the ratio between the feature’s spatial wavelength $\lambda$ and the probe-sample spacing $z$. (Solid lines) Magnetic field imaging is most sensitive to spatially large current features (red) and to magnetization features (blue) with a size similar to the probe-sample spacing $z$. (Dashed lines) Magnetic gradient imaging shifts the maximum sensitivity towards smaller feature size.

Comparison between techniques

Having quantified the sensitivity of MFM, SSM, and SNVM to magnetic moment and electrical current, we can now discern which techniques are best suited for mapping which type of contrast. Fig. 4 a) and b) show the sensitivity of all techniques to the magnetic field profile produced by a magnetic moment and a line of current as a function of probe-sample spacing. In the case of conventional and NW MFM, we refer to thermal limit of frequency shift measurements, which applies to DC or low-frequency measurements. In the other two cases, we use the minimum flux and field noise achieved in these devices in AC measurements in the tens of kHz range.
|                          | MFM (conventional) [27,28,34,90] | MFM (NW) [19] | SSM (susceptometer) [47] | SSM (SOT) [50] | SNVM [17,75–77] |
|--------------------------|----------------------------------|----------------|--------------------------|----------------|-----------------|
| Sensor size              | 10-100 nm                        | 100 nm         | 0.5 µm                  | 50 nm          | < 1 nm          |
| Sensor stand-off         | 10-100 nm                        | 50 nm          | 330 nm                  | 25 nm          | 50 nm           |
| Spatial resolution       | 10-100 nm                        | 100 nm         | 0.5 µm                  | 100 nm         | 15-25 nm        |
| DC sensitivity           | 10-100 µT/(Hz)^{1/2}             | 3 nT/(Hz)^{1/2} | 660 nT/(Hz)^{1/2}      | 50 nT/(Hz)^{1/2} | 4 µT/(Hz)^{1/2} |
| AC sensitivity           | 170 nT/(Hz)^{1/2}                | 3 nT/(Hz)^{1/2} | 130 nT/(Hz)^{1/2}      | 5 nT/(Hz)^{1/2} | 100 nT/(Hz)^{1/2} |
| Operating field          | < 10 T                           | < 10 T         | < 30 mT                 | < 1.2 T        | < 100s mT       |
| Operating temp.          | < 500 K                          | < 300 K        | < 9 K                   | < 7 K          | < 600 K         |

Table 1: Parameters for state-of-the-art magnetic SPM combining the highest-sensitivity with the highest resolution, based on the devices discussed in the cited references. Values shown in gray represent estimates based on the properties of the sensors, which have not yet been experimentally confirmed.

Together with sensor size, probe-sample spacing sets the spatial resolution of an SPM technique. Depending on the type of contrast, this spacing also strongly affects sensitivity. SSM sensitivity is not shown closer than 10 nm, because sensors are difficult to operate closer without a catastrophic crash. MFM sensitivity is not shown closer than 50 nm and NW MFM is not shown closer than 100 nm, because the point-probe approximation breaks down at tip-sample spacings smaller than the tip size and non-contact friction starts to dominate the force noise [91]. Also, at such close spacing, the stray field produced by the MFM tip at the sample is often invasive. Since SNVM can essentially be operated in contact with the sample, we plot its sensitivity down to 1 nm of probe-sample spacing.

Depending on tip-sample spacing, either SNVM or SSM have the highest sensitivity to magnetic moment. SSM appears best for tip-sample distances larger than 25 nm, while SNVM is better for closer approach. Conventional MFM is the least sensitive, while NW MFM is competitive with the other techniques. While very promising, NW MFM tip size must be reduced from state-of-the-art diameters of 100 nm in order for the technique to become competitive in high spatial resolution imaging of magnetic moment.

Among proven techniques, SSM is most sensitive to current. While conventional MFM is the least sensitive, NW MFM appears to surpass all techniques between 500 and 50 nm. Once again, for spatial resolutions better than 10 nm SNVM appears to be the best choice.

Fig. 4 c) provides another way to compare the three techniques, by showing the characteristic length of each sensor (its size in one dimension) together with its sensitivity to magnetic field. We plot a few
state-of-the-art sensors of each type and give an approximate idea of each technique’s operating regime. The characteristic length of a sensor not only sets its ultimate spatial resolution, but also sets the optimum probe-sample spacing, since closer approach is either impossible or does not improve sensitivity. Diagonal lines represent the combined probe-sample spacing and field noise required to achieve a certain sensitivity to magnetic moment or current.

Fig. 4 c) makes clear that SNVM has the smallest characteristic length, due to the atomic-scale of the NV center and the possibility to implant NVs with long coherence times just 10 nm from the surface of a scanning probe. This makes SNVM the technique of choice for spatial resolution under 25 nm and for the detection of small magnetizations. Because the magnetic field produced by a magnetic moment drops of with the inverse cube of the probe-sample distance, a small sensor able to work in close proximity to the sample is crucial for this type of contrast.

Fig. 4 c) also shows that SSM has the highest field sensitivity, but that it comes at the expense of large sensor size. While conventional MFM appears too insensitive to measure weak magnetization or current density, the increased force sensitivity of NW MFM makes it competitive with the other two techniques. In fact, for the measurement of currents, where spatial resolutions better than 100 nm are not required, SSM and NW MFM are the best techniques. Because Biot-Savart fields fall off only with the inverse power of the probe-sample spacing, a small sensor is not as important in current measurements as it is in magnetization measurements.

Aside from their sensitivity and resolution, each technique has properties making it more or less advantageous for certain samples. The strongly magnetic tip of an MFM can produces tens of mT of magnetic field on a sample 50 nm away. This field can in turn perturb the sample, potentially altering its state. SNVM requires the excitation of the probe with visible laser light. This optical excitation can perturb optically active samples below the probe. On the other hand, the stray fields due to the Meissner effect on an SSM probe are nearly negligible, making these sensors minimally invasive. SSM, however, is the most limited from the environmental point of view, functioning only at temperatures below the superconducting transition of the SQUID, typically below 10 K. Both MFM and SNVM function at a wide range of temperatures and pressures. SSM must also work below its critical field, which for state-of-the-art SOTs can be as high as a few T. SNVM is also limited in field, in that the frequency of the microwaves used to address the NV center scale linearly with field and become impractically high above 1 T.

Reconstruction of magnetization or current from field images

Since magnetic field microscopy techniques do not directly image the current or magnetization pattern, but rather their stray field, the question arises whether and how the former may be reconstructed from a stray field map. The relation between stray field and current density is governed by the Biot-Savart law that, via the concept of bound currents, can also be applied to magnetization.

Work in the late eighties by Roth [92] and Beardsley [93] established a framework to compute the stray fields of two-dimensional current density $J(x,y)$ and two-dimensional magnetization patterns $M(x,y)$, respectively. The same work also specified the conditions, in which a reconstruction of $J$ and $M$ is possible. In particular, they showed that three-dimensional current densities and magnetization patterns do not produce a unique magnetic stray field pattern, and can therefore not be determined by stray field imaging. Further, even an arbitrary two-dimensional magnetization pattern does not possess a unique stray field because the divergence-free part of $M$ does not generate an external stray field and is left arbitrary [93]. A rigorous solution, on the other hand, exists for two-dimensional
current densities \( \mathbf{J} = (J_x, J_y, 0) \) and out-of-plane magnetized films \( \mathbf{M} = (0,0,M_z) \). It has further been shown that this solution can be extended to thick films if the magnetization, or current density, is uniform through the thickness [76]. As a consequence, magnetic field imaging is especially useful for analyzing 2D systems and thin-film devices.

Magnetic field maps do not reproduce all current or magnetization features with the same sensitivity. Looking at the mechanics of the reconstruction, shown in Box 3, it becomes clear that features smaller than the probe-sample spacing \( z \) produce negligible magnetic field at the sensor location, because stray fields decay exponentially with distance from the surface. The decay length is given by \( \lambda/2\pi \), where \( \lambda \) is the spatial wavelength of the current or magnetization feature, as shown in Fig. 4 d). Interestingly, large features compared to the probe-sample spacing, i.e. large \( \lambda/z \), produce a strong signal for currents, but not for magnetization.

Imaging magnetic field gradients rather than magnetic fields, allows one to push the maximum sensitivity towards smaller feature size. Magnetic gradient detection is the standard mode for MFM, but can also be implemented for SSM and SNVM by a mechanical oscillation of the sensor [10,61]. Using lock-in techniques to demodulate the resulting signal can also significantly reduce noise through spectral filtering. Gradient detection is especially attractive for imaging currents, because the magnetic gradient image closely resembles the current density image, so that no reconstruction is needed [10]. For SNVM, gradient imaging is attractive because it upconverts DC signals to AC where much more sensitive magnetometry protocols are available [61,80].

**Box 3: Reconstruction of current density and magnetization from a magnetic field image**

The current density \( \mathbf{J} = (J_x, J_y) \) and in-plane magnetization \( M_z \) of a two-dimensional sample can be conveniently reconstructed from a magnetic field image by expressing the Biot-Savart law in \( k \)-space. Assume that we image in a plane at distance \( z \) above the sample, the magnetic stray field, in \( k \)-space is given by: \( B_z(k_x,k_y,z) = ig(k,z)[\frac{k_y}{k} \int_x(k_x,k_y) - \frac{k_x}{k} \int_y(k_x,k_y)] \), where \( g(k,z) = \frac{1}{z} \mu_0de^{−kz} \) is a transfer function with \( d \ll z \) being the film thickness, \( k_x \) and \( k_y \) are the \( k \)-vectors, and \( k = (k_x^2 + k_y^2)^{1/2} \). Similar expressions can be derived for \( B_x \) and \( B_y \) as well as for \( d \geq z \) [76,92]. To reconstruct the current density from a magnetic field map, the relation is inverted: \( J_x(k_x,k_y) = -\frac{(i\kappa W B_z(k_x,k_y,z))}{kg(k,z)} \) and \( J_y(k_x,k_y) = -\frac{(i\kappa W B_z(k_x,k_y,z))}{kg(k,z)} \), where \( W \) is a window function, whose cut-off wavelength is adjusted to suppress high-frequency noise. Different choices for the window function have been reported in the literature, including Hann and rectangular and Tikhonov-based windows. The cut-off wavelength typically is of order \( z \). An expression for reconstructing \( \mathbf{J} \) from an arbitrary \( B \)-field component is given in [76].

Similar expressions can be derived for reconstructing an out-of-plane magnetization \( M_z \) or to reconstruct magnetic gradient images. To reconstruct \( M_z \), note that \( \mathbf{J} = \nabla \times \mathbf{M} \), and therefore: \( B_z(k_x,k_y) = kg(k,z)M_z(k_x,k_y) \) for the forward problem as well as \( M_z(k_x,k_y) = \frac{W B_z(k_x,k_y,z)}{kg(k,z)} \) for the reverse problem. To reconstruct a magnetic gradient image, the transfer function incurs an additional factor of \( k \) due to the derivative.

**Prospects for improvement**

Improving MFM sensitivity requires stronger magnetic tips or transducers with better force sensitivity. Up to an order of magnitude in force sensitivity could be gained by using optimized NW transducers. MFM cantilevers have recently been realized with spring constants in the hundreds of mN/m and...
mechanical quality factors above $10^6$, resulting in nearly 100 times more sensitivity than conventional transducers. In general, however, improving the sensitivity of a mechanical transducer is achieved by reducing its size [94], as in recent work on NW MFM. Another route to improve magnetic field sensitivity is to increase the magnetic moment and size of MFM tips. This gain, however, comes at the cost of reducing spatial resolution and increasing the perturbative effect of the probes, which now produce larger stray fields at the sample.

The spatial resolution of the MFM could be improved by utilizing the sharpest possible magnetic tips. Extensive work has been done in this area in the context of conventional MFM, achieving spatial resolutions down to 10 nm [95–98]. Such work could be extended to high-force-sensitivity NW MFM. Smaller tips, however, have reduced magnetic moment and, consequently, a worse sensitivity to magnetic field profiles. In order to maintain high sensitivity, in general, the reduction in tip size should be accompanied with a reduction in transducer size.

Improvements in SSM field sensitivity could come from a reduction in the SQUID inductance. Given that this quantity is dominated by kinetic inductance in state-of-the-art devices, optimizing the superconducting material from which the device is made could be a fruitful pursuit. Further reduction of the characteristic size of SSM probes is difficult to imagine. SOT probes have been fabricated with diameters just under 50 nm. Reducing this size further would make the device size similar to the thickness of the deposited superconducting film, complicating much of the process, on which the fabrication is based. SQUIDs with feature sizes of only a few nanometers have been fabricated in YBCO using a focused ion beam of He [99], raising the possibility of devices that are an order of magnitude smaller and potentially work at liquid nitrogen temperature. Nevertheless, significant work remains to be done before such devices can be integrated onto scanning probes.

In order to reduce the characteristic length scale of SNVM, a number of researchers have focused on simultaneously reducing the implantation depth of NV centers and maintaining their coherence properties. Implantation depths of less than 3 nm have been reported combined with greater than 10 µs coherence times [100], giving a perspective of better than 10 nm imaging resolution combined with sub-10 nT/Hz$^{1/2}$ sensitivity. So far, however, most reported stand-off distances remain between 50 and 100 nm and the best magnetic field sensitivities at 100 nT/Hz$^{1/2}$ and significant work may be needed to reduce either figure of merit.

Conclusion

The confluence of substantial improvements in nanometer-scale magnetic imaging with the advent of engineered 2D materials creates the perfect opportunity to gain new insight into the physics of correlated states in condensed matter. The unprecedented control provided by layer-by-layer material engineering gives physicists a vast playground on which to test theories on superconductivity, magnetism, and other correlated phenomena. With this control, however, comes sensitivity to disorder and inhomogeneity. In such a fragile environment, local measurements – with sensors whose characteristic size is smaller than the length scale of the disorder – are essential for making sense of the system. For this reason, SPM techniques will become ever more important tools in this growing field, perhaps only losing traction, once fabrication techniques have been honed and substantially improved.

There are a number of SPM techniques, which have emerged as important tools for the investigation of 2D systems. Conventional atomic force microscopy has been used extensively for topographic characterization of 2D materials. In graphene, scanning single electron transistors have been used to
map the local density of states [101] and for imaging hydrodynamic flow [102]. Scanning gate microscopy has been used to image localized states [103] and scanning microwave impedance microscopy for visualizing the structural details of moiré lattices [104]. Electronic properties of 2D transition metal dichalcogenides have also been studied by scanning tunnelling microscopy [105]. Scanning near-field optical microscopy has even been used to measure polaritonic response in graphene-hexagonal boron nitride heterostructures [106].

As discussed in this review, among these SPM techniques, those involving non-invasive magnetic field imaging are particularly suited to investigating the correlated states present in 2D systems, because of their ability to map both current and out-of-plane magnetization. Given the high sensitivity and spatial resolution required to investigate correlated states in 2D materials, it is important to choose the appropriate magnetic SPM for the physical system under investigation. The different scaling of magnetization and current contrast with probe-sample spacing and the different physical quantities that are measured by various magnetic SPM make certain techniques more amenable to certain systems. We hope to have provided some insight in this regard, both to experimentalists wanting to apply magnetic SPM to 2D systems and to physicists working on the next generation of magnetic imaging techniques.

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