Search for $b \to u$ Transitions in $B^- \to (\bar{D}^0)K^-$ and $B^- \to (\bar{D}^0)K^-\gamma$

The BABAR Collaboration

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Abstract

We report on searches for $B^- \to (\bar{D}^0)K^-$ and $B^- \to (\bar{D}^0)K^-\gamma$, with $(\bar{D}^0) \to (\bar{D}^0)\pi^0$ or $(\bar{D}^0) \to (\bar{D}^0)\gamma$, and $(\bar{D}^0) \to K^+\pi^-$ (and charge conjugates). These final states, which we denote as $[K^+\pi^-]_D K^-$ and $[K^+\pi^-]_D^* K^-$, can be reached through the $b \to c$ transition $B^- \to D^{(*)0}K^-$ followed by the doubly Cabibbo-suppressed $D^0 \to K^+\pi^-$, or through the $b \to u$ transition $B^- \to D^{(*)0}K^-\gamma$ followed by the Cabibbo-favored $D^{0} \to K^+\pi^-$, or through interference of the two. Our results are based on 227 million $Y(4S) \to B\bar{B}$ decays collected with the BABAR detector at SLAC. We measure the ratios

$$\mathcal{R}_{K\pi} = \frac{\Gamma(B^+ \to [K^-\pi^+]_D K^+)}{\Gamma(B^+ \to [K^-\pi^+]_D K^+)} + \frac{\Gamma(B^- \to [K^+\pi^-]_D K^-)}{\Gamma(B^- \to [K^+\pi^-]_D K^-)} = 0.013 \pm 0.009,$$

$$\mathcal{R}^*_{K\pi,D\pi^0} = \frac{\Gamma(B^+ \to [K^-\pi^+]_D^{*+} D^{0*} K^+)}{\Gamma(B^+ \to [K^-\pi^+]_D^{*+} D^{0*} K^+)} + \frac{\Gamma(B^- \to [K^+\pi^-]_D^{*-} D^{0*} K^-)}{\Gamma(B^- \to [K^+\pi^-]_D^{*-} D^{0*} K^-)} = -0.001 \pm 0.006,$$

and

$$\mathcal{R}^*_{K\pi,D\pi^0} = \frac{\Gamma(B^+ \to [K^-\pi^+]_D^{*+} D^{0*} K^+)}{\Gamma(B^+ \to [K^-\pi^+]_D^{*+} D^{0*} K^+)} + \frac{\Gamma(B^- \to [K^+\pi^-]_D^{*-} D^{0*} K^-)}{\Gamma(B^- \to [K^+\pi^-]_D^{*-} D^{0*} K^-)} = 0.011 \pm 0.019.$$

We set $\mathcal{R}_{K\pi} < 0.030$ (90% C.L.) and from this limit we extract the amplitude ratio $r_B \equiv |A(B^- \to D^0K^-)/A(B^- \to D^0K^-)| < 0.23$ at the 90% confidence level. This limit is obtained with the most conservative assumptions on the values of the CKM angle $\gamma$ and the strong phases in the $B$ and $D$ decay amplitudes. From the measurements of $\mathcal{R}_{K\pi,D\pi^0}$ and $\mathcal{R}^*_{K\pi,D\gamma}$ we extract $r_{B}^2 \equiv |A(B^- \to D^0K^-)/A(B^- \to D^0K^-)|^2 = 4.6^{+15.2}_{-2.3} \times 10^{-3}$ and $r_{B}^2 < (0.16)^2$ at the 90% confidence level.

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1 INTRODUCTION

Following the discovery of $CP$ violation in $B$-meson decays and the measurement of the angle $\beta$ of the unitarity triangle [1] associated with the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix, focus has turned towards the measurements of the other angles $\alpha$ and $\gamma$. The angle $\gamma$ is $\text{arg}(-V^*_{ub}V_{ud}/V^*_{cb}V_{cd})$, where $V_{ij}$ are CKM matrix elements; in the Wolfenstein convention [2], $\gamma = \text{arg}(V^*_{ub})$.

Several proposed methods for measuring $\gamma$ exploit the interference between $B^- \to D^{(*)0}K^{(*)-}$ and $B^- \to \bar{D}^{(*)0}K^{(*)-}$ (Fig. 1) which occurs when the $D^{(*)0}$ and the $\bar{D}^{(*)0}$ decay to common final states, as first suggested in Ref. [3].

![Feynman diagrams](image)

Figure 1: Feynman diagrams for $B^- \to D^{(*)0}K^{(*)-}$ and $\bar{D}^{(*)0}K^{(*)-}$. The latter is CKM- and color-suppressed with respect to the former. The CKM and color suppression factors are expected to be roughly $|V_{ub}V^*_{cs}/V_{cb}V^*_{ts}| \approx 0.4$ and $1/3$ respectively.

As proposed in Ref. [4], we search for $B^- \to \bar{D}^0K^-$ and $B^- \to \bar{D}^{0*}K^-$, $\bar{D}^{0*} \to \bar{D}^{h_0}/\gamma$ followed by $\bar{D}^0 \to K^+\pi^-$, as well as the charge conjugate sequences. In these processes, the favored $B$ decay followed by the doubly CKM-suppressed $D$ decay interferes with the suppressed $B$ decay followed by the CKM-favored $D$ decay. The interference of the $b \to c$ and $b \to u$ amplitudes is sensitive to the relative weak phase $\gamma = \text{arg}(-V_{ub}V^*_{ub}/V_{cb}V^*_{ub})$.

We use the notation $B^- \to [h_1^+h_2^-]Dh_3^-$ (with each $h_i = \pi$ or $K$) for the decay chain $B^- \to \bar{D}^{0*}h_3^-$, $\bar{D}^{0*} \to h_1^+h_2^-$. For the closely related modes with a $D^{0*}$, we use the same notation with the subscript $D$ replaced by $D^*$. We also refer to $h_3$ as the bachelor $\pi$ or $K$.

In the decays of interest, the sign of the bachelor kaon is opposite to that of the kaon from $D$ decay. It is convenient to define ratios of rates between these decays and the similar decays where the two kaons have the same sign. The decays with same-sign kaons have much higher rate and proceed almost exclusively through the CKM-favored and color favored $B$ transition, followed by the Cabibbo-favored $D$-decay. The advantage in taking ratios is that most theoretical and experimental uncertainties cancel. Thus, ignoring the possible effects of $D$ mixing and taking into account the effective strong phase difference of $\pi$ between the $D^*$ decays in $D\gamma$ and $D\pi^0[5]$, we define the charge-specific ratios for $D$ and $D^*$ as:

$$
R_{K^\pm}^\pm = \frac{\Gamma([K^\mp\pi^\pm]_D K^\pm)}{\Gamma([K^\mp\pi^\pm]_{\bar{D}} K^\pm)} = r_B^2 + r_D^2 + 2r_Br_D \cos(\pm \gamma + \delta)
$$

(1)
and
\[
\mathcal{R}^{\pm}_{K\pi,D\pi^0} \equiv \frac{\Gamma([K^\mp\pi^\pm]_{D\pi^0}K^\mp)}{\Gamma([K^\mp\pi^\pm]_{D\pi^0}K^\mp)} = r_B^2 + r_D^2 + 2r_B r_D \cos(\pm \gamma + \delta^*) \quad \text{and} 
\]
(2)
\[
\mathcal{R}^{\pm}_{K\pi,D\gamma} \equiv \frac{\Gamma([K^\mp\pi^\pm]_{D\gamma}K^\mp)}{\Gamma([K^\mp\pi^\pm]_{D\gamma}K^\mp)} = r_B^2 + r_D^2 - 2r_B r_D \cos(\pm \gamma + \delta^*),
\]
(3)
where
\[
r_B \equiv \left| \frac{A(B^- \to \bar{D}^0 K^-)}{A(B^- \to D^0 K^-)} \right|,
\]
(4)
\[
r_B^* \equiv \left| \frac{A(B^- \to \bar{D}^0 K^-)}{A(B^- \to D^0 K^-)} \right|,
\]
(5)
\[
r_D \equiv \left| \frac{A(D^0 \to K^\mp\pi^-)}{A(D^0 \to K^-\pi^+)} \right| = 0.060 \pm 0.003 \quad [6],
\]
(6)
\[
\delta^{(*)} \equiv \delta_B^{(*)} + \delta_D,
\]
(7)
and \(\delta_B^{(*)}\) and \(\delta_D\) are strong phase differences between the two \(B\) and \(D\) decay amplitudes, respectively.

We also define the charge-integrated ratios:
\[
\mathcal{R}_{K\pi} \equiv \frac{\Gamma(B^- \to [K^+\pi^-]_{D}K^-) + \Gamma(B^+ \to [K^-\pi^+]_{D}K^+)}{\Gamma(B^- \to [K^-\pi^+]_{D}K^-) + \Gamma(B^+ \to [K^+\pi^-]_{D}K^+)}
\]
(8)
and
\[
\mathcal{R}^{*}_{K\pi, D\pi^0(D\gamma)} \equiv \frac{\Gamma(B^- \to [K^+\pi^-]_{D^*\pi^0(D\gamma)}K^-) + \Gamma(B^+ \to [K^-\pi^+]_{D^*\pi^0(D\gamma)}K^+)}{\Gamma(B^- \to [K^-\pi^+]_{D^*\pi^0(D\gamma)}K^-) + \Gamma(B^+ \to [K^+\pi^-]_{D^*\pi^0(D\gamma)}K^+)}.
\]
(9)
Then,
\[
\mathcal{R}_{K\pi} = \frac{\mathcal{R}^+_{K\pi} + \mathcal{R}^-_{K\pi}}{2} = r_B^2 + r_D^2 + 2r_B r_D \cos \gamma \cos \delta
\]
(10)
\[
\mathcal{R}^*_{K\pi, D\pi^0} = \frac{\mathcal{R}^+_{K\pi, D\pi^0} + \mathcal{R}^-_{K\pi, D\pi^0}}{2} = r_B^2 + r_D^2 - 2r_B r_D \cos \gamma \cos \delta^*,
\]
(11)
and
\[
\mathcal{R}^*_{K\pi, D\gamma} = \frac{\mathcal{R}^+_{K\pi, D\gamma} + \mathcal{R}^-_{K\pi, D\gamma}}{2} = r_B^2 + r_D^2 - 2r_B r_D \cos \gamma \cos \delta^*,
\]
(12)
assuming no \(CP\) violation in the normalization modes \([K^\mp\pi^\pm]_{D}K^\mp\) and \([K^\mp\pi^\pm]_{D^*}K^\mp\). In the following we use the notation \(R^*_{K\pi}\) when there is no need to refer specifically to \(R^*_{K\pi, D\pi^0}\) or \(R^*_{K\pi, D\gamma}\).

Since \(r_B^{(*)}\) is expected to be of the same order as \(r_D\), \(CP\) violation could manifest itself as a large difference between the charge-specific ratios \(\mathcal{R}^{(*)}_{K\pi}\) and \(\mathcal{R}^{(*)}_{K\pi}\). Measurements of these six ratios can be used to constrain \(\gamma\).

The value of \(r_B^{(*)}\) determines, in part, the level of interference between the diagrams of Fig. 1. In most techniques for measuring \(\gamma\), high values of \(r_B^{(*)}\) lead to larger interference and better sensitivity to \(\gamma\). As we will describe below, the measured \(\mathcal{R}^{(*)}_{K\pi}\) are consistent with zero in the current analysis. This allows us to set restrictive upper limits on \(r_B^{(*)}\), since \(\mathcal{R}^{(*)}_{K\pi}\) depend quadratically on \(r_B^{(*)}\).
In the Standard Model, $r_B^{(s)} = |V_{ub}V_{cs}^*/V_{cb}V_{us}^*|F_{cs} \approx 0.4F_{cs}$. The color-suppression factor $F_{cs} < 1$ accounts for the additional suppression, beyond that due to CKM factors, of $B^- \to \bar{D}^{(*)0}K^-$ relative to $B^- \to \bar{D}^{(*)0}K^-$. Naively, $F_{cs} = \frac{1}{r}$, which is the probability for the color of the quarks from the virtual $W$ in $B^- \to \bar{D}^{(*)0}K^-$ to match that of the other two quarks; see Fig. 1. Early estimates [7] of $F_{cs}$ were based on factorization and the then available experimental information on a number of $b \to c$ transitions. These estimates gave $F_{cs} \approx 0.22$, leading to $r_B^{(s)} \approx 0.09$. However, the recent observations and measurements [8] of color suppressed $B^- \to c$ decays ($B \to D^{(*)}h^0$; $h^0 = \pi^0, \rho^0, \omega, \eta, \eta'$) suggest that $F_{cs}$, and therefore $r_B^{(s)}$, could be larger.

In this paper we report on an update of our previous analysis of $B^- \to \bar{D}^{(*)0}K^-$ [9], and the first attempt to study $B^- \to \bar{D}^{(*)0}K^{-}$. The previous analysis was based on a sample of $B$-meson decays a factor of 1.9 smaller than used here, and resulted in an upper limit $R_{K\pi} < 0.026$ at the 90% confidence level. This in turn was translated into a limit $r_B < 0.22$, also at 90% C.L.. On the other hand, a study by the Belle collaboration [10] of $B^\pm \to \bar{D}^{(*)0}K^\pm$ and $B^\pm \to \bar{D}^{(*)0}K^\pm, \bar{D}^{(*)0} \to K_S\pi^+\pi^-$, favors rather large color suppressed amplitudes: $r_B = 0.26^{+0.11}_{-0.15}$ and $r_B = 0.26^{+0.20}_{-0.18}$.

2 THE \textbf{BaBar} DATASET

The results presented in this paper are based on $227 \times 10^6 \Upsilon(4S) \to B\bar{B}$ decays, corresponding to an integrated luminosity of 205 fb$^{-1}$. The data were collected between 1999 and 2004 with the \textit{BaBar} detector [11] at the PEP-II $B$ Factory at SLAC [12]. In addition, a 16 fb$^{-1}$ off-resonance data sample, with center-of-mass (CM) energy 40 MeV below the $\Upsilon(4S)$ resonance, is used to study backgrounds from continuum events, $e^+e^- \to q\bar{q}$ ($q = u, d, s, \text{ or } c$).

3 ANALYSIS METHOD

This work is an extension of our analysis from Ref. [9], which resulted in limits on $R_{K\pi} < 0.026$ and $r_B < 0.22$, as mentioned above. The main changes in the analysis are the following:

- The size of the dataset is increased from 120 to $227 \times 10^6 \Upsilon(4S) \to B\bar{B}$ decays.
- This analysis also includes the $B^\pm \to \bar{D}^{(*)0}K^\pm$ mode.
- The analysis requirements have been tightened in order to reduce backgrounds further.
- A few of the requirements in the previous analysis resulted in small differences in the efficiencies of the signal mode $B^\pm \to [K^\mp\pi^\mp]K^\pm$ and the normalization mode $B^\pm \to [K^\pm\pi^\mp]K^\pm$. These requirements have now been removed.

The analysis makes use of several samples from different decay modes. Throughout the following discussion we will refer to these modes using abbreviations that are summarized in Table 1.

The event selection is developed from studies of simulated $B\bar{B}$ and continuum events, and off-resonance data. A large on-resonance control sample of $D\pi$ and $D^{*}\pi$ events is used to validate several aspects of the simulation and analysis procedure.

The analysis strategy is the following:

1. The goal is to measure or set limits on the charge-integrated ratios $R_{K\pi}$ and $R_{K\pi}^{-}$.  

10
2. The first step consists in the application of a set of basic requirements to select possible candidate events, see Section 3.1.

3. After the basic requirements, the backgrounds are dominantly from continuum. These are significantly reduced using a neural network designed to distinguish between $B\bar{B}$ and continuum events, see Section 3.2.

4. After the neural network requirement, events are characterized by two kinematical variables that are customarily used when reconstructing $B$-meson decays at the $\Upsilon(4S)$. These variables are the energy-substituted mass, $\hat{m}_{ES} \equiv \sqrt{\left(\frac{s}{2} + \vec{p}_0 \cdot \vec{p}_B\right)^2/E_0^2 - \vec{p}_B^2}$ and energy difference $\Delta E \equiv E_B^2 - \frac{1}{2}\sqrt{s}$, where $E$ and $p$ are energy and momentum, the asterisk denotes the CM frame, the subscripts 0 and $B$ refer to the $\Upsilon(4S)$ and $B$ candidate, respectively, and $s$ is the square of the CM energy. For signal events $\hat{m}_{ES} = m_B$ and $\Delta E = 0$ within the resolution of about 2.5 and 20 MeV respectively (here $m_B$ is the known $B$ mass).

5. We then perform simultaneous fits to the final signal samples ($D\bar{K}$ and $D^*K$), the normalization samples ($DK$ and $D^*K$), and the control samples ($D\pi$ and $D^*\pi$) to extract $R_{K\pi}$ and $R_{K\pi}^*$, see Section 3.3. The fits are based on the reconstructed values of $\hat{m}_{ES}$ and $\Delta E$ in the various event samples.

6. Throughout the whole analysis chain, care is taken to treat the signal, normalization, and control samples in a consistent manner.

### 3.1 Basic Requirements

Charged kaon and pion candidates in the decay modes of interest must satisfy $K$ or $\pi$ identification criteria [13] that are typically 85% efficient, depending on momentum and polar angle. The misidentification rates are at the few percent level. The invariant mass of the $K\pi$ pair must be within 18.8 MeV (2.5$\sigma$) of the mean reconstructed $D^0$ mass. For modes with $\bar{D}^{*0} \rightarrow \bar{D}^0 \pi^0$ and $\bar{D}^{*0} \rightarrow \bar{D}^0 \gamma$ the mass difference $\Delta M$ between the $\bar{D}^{*0}$ and the $\bar{D}^0$ must be within 3.5 (3.5$\sigma$) and 13 (2$\sigma$) MeV, respectively, of the expectation for $\bar{D}^{*0}$ decays.

A major background arises from $DK$ and $D^*K$ decays where the $K$ and $\pi$ in the $D$ decay are misidentified as a $\pi$ and a $K$ respectively. When this happens, the decay could be reconstructed as a $D\bar{K}$ or $D^*K$ signal event. To eliminate this background, we recompute the invariant mass ($M_{\text{switch}}$) of the $h^+h^-$ pair in $\bar{D}^0 \rightarrow h^+h^-$ switching the particle identification assumptions ($\pi$ vs.
After these initial requirements, backgrounds are overwhelmingly from continuum events, especially $e^+e^-\rightarrow c\bar{c}$, with $\bar{c}\rightarrow D^0X$, $D^0\rightarrow K^+\pi^-$ and $c\rightarrow DX$, $D\rightarrow K^-Y$.

The continuum background is reduced by using neural network techniques. The neural network algorithms used for the $DK$ and $\bar{D}K$ modes are slightly different. First, we use for both modes a common neural network (NN) based on nine quantities that distinguish between continuum and $BB$ events. Then, for the $\bar{D}^*K$ mode only, we also take advantage of the fact that the signal is distributed as $\cos\theta_{D^*}$ for $D^*\rightarrow D\pi$ or $\sin^2\theta_{D^*}$ for $D^*\rightarrow D\gamma$, while the background is roughly independent of $\cos\theta_{D^*}$. Here $\theta_{D^*}$ is the decay angle of the $D^*$, i.e., the angle between the direction of the $D$ and the line of flight of the $D^*$ relative to the parent $B$, evaluated in the $D^*$ rest frame. Thus, we construct a second neural network, $NN'$, which takes as inputs the output of $NN$ and the value of $\cos\theta_{D^*}$. We then use as a selection requirement the output of $NN$ in the $\bar{D}K$ analysis and the output of $NN'$ in the $\bar{D}^*K$ analysis.

The nine variables used in defining $NN$ are the following:

1. A Fisher discriminant constructed from the quantities $L_0 = \sum_i p_i$ and $L_2 = \sum_i p_i \cos^2\theta_i$ calculated in the CM frame. Here, $p_i$ is the momentum and $\theta_i$ is the angle with respect to the thrust axis of the $B$ candidate of tracks and clusters not used to reconstruct the $B$ meson.

2. $|\cos\theta_T|$, where $\theta_T$ is the angle in the CM frame between the thrust axes of the $B$ candidate and the detected remainder of the event. The distribution of $|\cos\theta_T|$ is approximately flat for signal and strongly peaked at one for continuum background.

3. $\cos\theta_B$, where $\theta_B$ is the polar angle of the $B$ candidate in the CM frame. In this variable, the signal follows a $\sin^2\theta_B$ distribution, while the background is approximately uniform.

4. $\cos\theta_D^K$ where $\theta_D^K$ is the decay angle in $\bar{D}^0\rightarrow K\pi$.

5. $\cos\theta_B^K$, where $\theta_B^K$ is the decay angle in $B\rightarrow\bar{D}^0K$ or $B\rightarrow\bar{D}^{*0}K$.

6. The charge difference $\Delta Q$ between the sum of the charges of tracks in the $\bar{D}^0$ or $\bar{D}^{*0}$ hemisphere and the sum of the charges of the tracks in the opposite hemisphere excluding the tracks used in the reconstructed $B$. For signal, $\langle\Delta Q\rangle = 0$, whereas for the $c\bar{c}$ background $\langle\Delta Q\rangle \approx \frac{4}{3} \times Q_B$, where $Q_B$ is the charge of the $B$ candidate. The $\Delta Q$ RMS is 2.4.

7. $Q_B \cdot Q_K$, where $Q_K$ is the sum of the charges of all kaons not in the reconstructed $B$. In many signal events, there is a charged kaon among the decay products of the other $B$ in the event. The charge of this kaon tends to be highly correlated with the charge of the $B$. Thus, signal events tend to have $Q_B \cdot Q_K \leq -1$. On the other hand, most continuum events have no kaons outside of the reconstructed $B$, and therefore $Q_K = 0$.

8. The distance of closest approach between the bachelor track and the trajectory of the $\bar{D}^0$ This is consistent with zero for signal events, but can be larger in $c\bar{c}$ events.
9. The existence of a lepton (\(e\) or \(\mu\)) and the invariant mass \((m_{K\ell})\) of this lepton and the bachelor \(K\). Continuum events have fewer leptons than signal events. Furthermore, a large fraction of leptons in \(\bar{c}\bar{c}\) events are from \(D \rightarrow K\ell\nu\), where \(K\) is the bachelor kaon, so that \(m_{K\ell} < m_D\).

The neural networks (\(NN\) and \(NN'\)) are trained with simulated continuum and signal events. The distributions of the \(NN\) and \(NN'\) outputs for the control samples (\(D\pi\), \(D^*\pi\), and off resonance data), are compared with expectations from the Monte Carlo simulation in Figure 2. The agreement is satisfactory. We have also examined the distributions of all variables used in \(NN\) and \(NN'\), and found good agreement between the simulation and the data control samples.

Our final events selection requirement is \(NN > 0.5\) for \(\overline{D}K\) and \(NN' > 0.5\) for \(\overline{D}^*K\). In addition, to reduce the remaining \(B\overline{B}\) backgrounds, we also require \(\cos \theta_D^K > -0.75\). These requirements are about 40\% efficient on simulated signal events, and reject 98.5\% of the continuum background. Note, however, that we do not rely on the Monte Carlo simulation to estimate the efficiency of the neural net requirements. We apply the exact same requirements to the normalization modes \(\bar{D}K\) or \(\overline{D}^*K\). Then, in the extraction of \(R_{K\pi}\) and \(R_{\overline{K}\pi}\), the efficiencies of the overall selection cancels in the ratio.

### 3.3 Fitting for event yields and \(R_{K\pi}^{(s)}\)

The ratios \(R_{K\pi}\) and \(R_{\overline{K}\pi}^{(s)}\) are extracted from the ratios of the event yields in the \(m_{ES}\) distribution for the signal modes (\(\overline{D}K\) and \(\overline{D}^*K\)) and the normalization modes (\(DK\) and \(D^*K\)), while taking into account potential differences in efficiencies and backgrounds. All events must satisfy the requirements discussed above and have a \(\Delta E\) value consistent with zero within the resolution (\(-52\text{ MeV} < \Delta E < 44\text{ MeV}\)).

The \(m_{ES}\) distributions for \(\overline{D}K\) (signal mode) and \(DK\) (normalization mode) are fitted simultaneously. The fit parameter \(R_{K\pi}\) is given by \(R_{K\pi} \equiv c \cdot N_{\overline{D}K}/N_{DK}\), where \(N_{\overline{D}K}\) and \(N_{DK}\) are the fitted yields of \(\overline{D}K\) and \(DK\) events, and \(c\) is a correction factor, determined from Monte Carlo, for the ratio of efficiencies between the two modes. We find that this factor \(c\) is consistent with unity within the statistical accuracy of the simulation, \(c = 0.98 \pm 0.04\).

The \(m_{ES}\) distributions are modeled as the sum of a threshold combinatorial background function [15] and a Gaussian centered at \(m_B\). The parameters of the background function for the signal mode are constrained by a simultaneous fit of the \(m_{ES}\) distribution for events in the sideband of \(\Delta E\) (\(-120\text{ MeV} < \Delta E < 200\text{ MeV}\), excluding the \(\Delta E\) signal region defined above). The parameters of the Gaussian for the signal and normalization modes are constrained to be identical. The number of events in the Gaussian is \(N_{sig} + N_{peak}\), where \(N_{sig} = N_{DK}\) or \(N_{\overline{D}K}\) and \(N_{peak}\) is the number of background events expected to be distributed in the same way as the \(DK\) or \(\overline{D}K\) in \(m_{ES}\) ("peaking backgrounds").

There are two classes of peaking background events:

1. Charmless \(B\) decays, \(e.g., B^- \rightarrow K^+K^-\pi^+\). These are indistinguishable from the \(\overline{D}K\) signal if the \(K^-\pi^+\) pair happens to be consistent with the \(D\)-mass.

2. Events of the type \(B^- \rightarrow D^0\pi^- (D\pi)\), where the bachelor \(\pi^-\) is misidentified as a \(K^-\). When the \(D^0\) decays into \(K^-\pi^+ (K^+\pi^-)\), these events are indistinguishable in \(m_{ES}\) from \(DK\) (\(\overline{D}K\)), since \(m_{ES}\) is insensitive to particle identification assumptions.

\(^6\)In the \(D^*\) modes this correction factor is \(c = 0.97 \pm 0.05\) and \(c = 0.99 \pm 0.05\) for \(D^* \rightarrow D\pi^0\) and \(D^* \rightarrow D\gamma\) respectively.
Figure 2: Distributions of the continuum suppression neural network (NN and NN’) outputs for the three modes. Figures (a-c) show the expected distribution from signal events. The solid line histogram shows the distribution of simulated signal events, the histogram with error bars shows the distribution of $D^{(*)0}\pi$ control sample events with background subtracted using the $m_{ES}$ sideband. Figures (d-i) show the expected distribution for continuum background events. The solid line histogram shows the distribution of simulated continuum events and the histogram with errors show the distribution of off-resonance events. The $m_{ES}$ and $\Delta E$ requirements on the off-resonance and continuum Monte Carlo events have been kept loose to increase the statistics. Figures (g-i) show the distributions of figures (d-g) in log scale. Each Monte Carlo histogram is normalized to the area of the corresponding data histogram.
The amount of charmless background (1) is estimated directly from the data by performing a simultaneous fit to events in the sideband of the reconstructed $D$ mass. The $\Delta E$ distribution of the $D\pi$ background (2) is shifted by about $+50$ MeV due to the misidentification of the bachelor $\pi$ as a $K$. Since the $\Delta E$ resolution is of order 20 MeV, the $\Delta E$ requirement does not eliminate this background completely. The remaining $D\pi$ background after the $\Delta E$ requirement is estimated from a fit to the $\Delta E$ distribution of the $DK$ sample.

We fit the $\Delta E$ distribution of $DK$ candidates, with $m_{ES}$ within $3\sigma$ of $m_B$, to the sum of a $DK$ component, a $D\pi$ component, and a combinatorial component. The $D\pi$ sample, with the bachelor track identified as a pion, is used to constrain the shape of the $DK$ component in the $DK$ sample. The same sample of $D\pi$ events, but reconstructed as $DK$ events, is used to constrain the shape of the $D\pi$ background in the $DK$ sample. The fitted number of $D\pi$ background events in this sample that survive the $\Delta E$ requirements, which we denote as $N_{DK}^\pi$, is taken as the number of $D\pi$ background events in the fit to the $m_{ES}$ distribution of $DK$ events.

The $D\pi$ peaking background is much more important in the $DK$ (normalization) channel than in the $\bar{DK}$ (signal) channel. This is because in order to contribute to the signal channel, the $D^0$ has to decay into $K^+\pi^-$, and this mode is doubly Cabibbo-suppressed. For the $\bar{DK}$ (signal) sample, the contribution from the residual $D\pi$ peaking background in the $m_{ES}$ fit is estimated as $N_{\bar{DK}}^\pi = r_D^2 N_{DK}^\pi$, where $r_D = 0.060 \pm 0.003$ is the ratio of the doubly Cabibbo-suppressed to the Cabibbo-favored $D \to K\pi$ amplitudes (see Eq. 6), and $N_{DK}^\pi$ was defined above.

The complete procedure simultaneously fits seven distributions: the $m_{ES}$ distributions of $DK$ and $\bar{DK}$, the $\bar{DK}$ distributions in sidebands of $\Delta E$ and $m(D^0)$, the $\Delta E$ distribution of $DK$, and the $\Delta E$ distributions of $D\pi$ reconstructed as $D\pi$ and as $DK$. The fits are configured in such a way that $R_{K\pi}$ and $R_{K\pi}^*$ are explicit fit parameters. The advantage of this approach is that all uncertainties, including the uncertainties in the PDFs and the uncertainties in the background subtractions, are automatically correctly propagated in the statistical uncertainty reported by the fit.

The fit is performed separately for $\bar{DK}$, $\bar{DK}^*\to\bar{DK}^{0}$, and $D^*\to\bar{DK}$ and is identical for all three modes, except in the choice of parameterization for some signal and background components in the $\Delta E$ fits.

Systematic uncertainties in the detector efficiency cancel in the ratio. This cancellation has been verified by studies of simulated events, with a statistical precision of a few per-cent. The likelihood includes a Gaussian uncertainty term for this cancellation which is set by the statistical accuracy of the simulation. Other systematic uncertainties, e.g., the uncertainty in the parameter $r_D$ which is used to estimate the amount of peaking backgrounds from $D^{(*)}\pi$, are also included in the formulation of the likelihood.

The fit procedure has been extensively tested on sets of simulated events. It was found to provide an unbiased estimation of the parameters $R_{K\pi}$ and $R_{K\pi}^*$.

4 RESULTS

The results of the fits are displayed in Table 2 and Figs. 3, 4, 5, and 6. As is apparent from Fig. 6, we see no evidence for the $\bar{DK}$ modes and no significant evidence for the $DK$ mode.

For the $\bar{DK}$ mode we find $R_{K\pi} = 13^{+11}_{-9} \times 10^{-3}$; For the $D^*K$ mode we find $R_{K\pi}^* = -1^{+10}_{-6} \times 10^{-3}$ (for $D^* \to D\pi^0$) and $R_{K\pi}^{*0} = 11^{+13}_{-19} \times 10^{-3}$ (for $D^* \to D\gamma$). We estimate from a parameterized Monte Carlo study that the probability that an upward fluctuation of background events results in our observed value of $R_{K\pi}$ or larger is 7.5%.
Figure 3: $\Delta E$ distributions for normalization events ($DK$ and $D^*K$) with $m_{ES}$ within $3\sigma$ of $m_B$ with the fit model overlaid. (a) $DK$ events. (b) $D^*K$ events with $D^* \to D\pi^0$. (c) $D^*K$ events with $D^* \to D\gamma$. The dashed (dot-dashed) curves are the contributions from $D\pi$ or $D^*\pi$ ($DK$ or $D^*K$) events. The dotted curves are the contributions from other backgrounds, and the solid line is the total.

Table 2: Summary of fit results.

| Mode                              | $D^0 K$       | $D^0 K, D^* \to D\pi^0$ | $D^* K, D^* \to D\gamma$ |
|-----------------------------------|---------------|--------------------------|---------------------------|
| Ratio of rates, $R_{K\pi}$ or $R^*_{K\pi}$, $\times 10^{-3}$ | $R_{K\pi} = 13^{+11}_{-9}$ | $R^*_{K\pi} = -1^{+10}_{-6}$ | $R^*_{K\pi} = 11^{+19}_{-13}$ |
| No. of signal events              | 4.7$^{+4.0}_{-3.2}$ | 142$^{+17}_{-16}$ | 2.5$^{+18}_{-14}$ |
| No. of normalization events       | 356$^{+26}_{-26}$ | 101$^{+14}_{-14}$ | |
| No. of peaking charmless events   | 0.75$^{+1.3}_{-0.75}$ | 0.05$^{+0.7}_{-0.05}$ | |
| No. of peaking $D^{(*)}\pi$ ev. in sig. sample | 0.47$^{+0.04}_{-0.04}$ | 0.01$^{+0.03}_{-0.03}$ | |
| No. of peaking $D^{(*)}\pi$ ev. in norm. sample | 132$^{+10}_{-10}$ | 48$^{+6}_{-6}$ | |

We use our results to extract information on $r_B$ and $r_B^*$. In the case of decays into a $D^*/\overline{D^*}$ we can use equations 11 and 12 to write

$$r_B^* = \frac{R^*_{K\pi,D\pi^0} + R^*_{K\pi,D\gamma}}{2} - r_B^2. \quad (13)$$

Our results then give $r_B^2 = 4.6^{+15.2}_{-7.3} \times 10^{-3}$. The likelihood function for $r_B^2$ is shown in Figure 7. Based on this likelihood, we set an upper limit $r_B^2 < (0.16)^2$ at the 90% C.L. using a Bayesian method with a uniform prior for $r_B^2 > 0$.

In the case of decays into a $D/\overline{D}$, there are not enough information to extract the ratio $r_B$ without additional assumptions. Thus, we first extract an upper limit on the experimentally measured quantity $R_{K\pi}$. This is done starting from the likelihood as a function of $R_{K\pi}$ (see Figure 8) using a Bayesian method with a uniform prior for $R_{K\pi} > 0$. The limit is $R_{K\pi} < 0.030$ at 90% C.L.. Next, in Fig. 9 we show the dependence of $R_{K\pi}$ on $r_B$, together with our limit on $R_{K\pi}$. This dependence is shown allowing a $\pm 1\sigma$ variation on $r_D$, for the full range $0^\circ - 180^\circ$ for $\gamma$ and $\delta$, as well as with the restriction $48^\circ < \gamma < 73^\circ$ suggested by global CKM fits [16]. We use the
Figure 4: $m_{ES}$ distributions for normalization events ($DK$ and $D^*K$) with $\Delta E$ in the signal region with the fit model overlaid. (a) $DK$ events. (b) $D^*K$ events with $D^* \rightarrow D\pi^0$. (c) $D^*K$ events with $D^* \rightarrow D\gamma$. The dashed curves represent the backgrounds; these are mostly from $D\pi$ or $D^*\pi$, and also peak at the $B$-mass. As explained in the text, the size of the $D\pi$ and $D^*\pi$ backgrounds is constrained by the simultaneous fits to the distributions of Figure 3.

information displayed in this Figure to set an upper limit on $r_B$. The least restrictive limit on $r_B$ is computed assuming maximal destructive interference: $\gamma = 0^\circ, \delta = 180^\circ$ or $\gamma = 180^\circ, \delta = 0^\circ$. The limit is $r_B < 0.23$ at 90% C.L.
Figure 5: $m_{ES}$ distributions for $\bar{D}K$ and $\bar{D}^*K$ events with $K\pi$ mass in a sideband of the reconstructed $D$ mass and with $\Delta E$ in the signal region. These events are used to constrain the size of possible peaking backgrounds from charmless $B$-meson decays, i.e., decays without a $D$ in the final state. The fit model is overlaid. (a) $\bar{D}K$ events. (b) $\bar{D}^*K$ events with $D^* \rightarrow D\pi^0$. (c) $\bar{D}^*K$ events with $D^* \rightarrow D\gamma$. Note that the $K\pi$ mass range in the sideband selection is a factor of 2.7 larger than in the signal selection.

Figure 6: $m_{ES}$ distributions for candidate signal events with the fit model overlaid. (a) $\bar{D}K$ events. (b) $\bar{D}^*K$ events with $D^* \rightarrow D\pi^0$. (c) $\bar{D}^*K$ events with $D^* \rightarrow D\gamma$. 

18
Figure 7: Likelihood distribution (arbitrary units) for $r_B^{*2}$.

Figure 8: Likelihood distribution (arbitrary units) for $R_{K\pi}$.
Figure 9: Expectations for $R_{K\pi}$ and the number of signal events vs. $r_B$. Dark filled-in area: allowed region for any value of $\delta$, with a $\pm 1\sigma$ variation on $r_D$, and $48^\circ < \gamma < 73^\circ$. Hatched area: additional allowed regions with no constraint on $\gamma$. Note that the uncertainty on $r_D$ has a very small effect on the size of the allowed regions. The horizontal line represents the 90% C.L. limit $R_{K\pi} < 0.030$. The vertical dashed lines are drawn at $r_B = 0.209$, $r_B = 0.235$. They represent the 90% C.L. upper limits on $r_B$ with and without the constraint on $\gamma$. The light filled in areas represent the 68% C.L. regions corresponding to $R_{K\pi} = 0.013\pm0.011$.

5 SUMMARY

In summary, we find no significant evidence for the decays $B^\pm \rightarrow [K^\mp \pi^\pm]_D K^\pm$ and $B^\pm \rightarrow [K^\mp \pi^\pm]_{D^*} K^\pm$. We measure the ratios $R_{K\pi}$ of the rates for these modes and the favored modes $B^\pm \rightarrow [K^\mp \pi^\pm]_D K^\pm$ and $B^\pm \rightarrow [K^\mp \pi^\pm]_{D^*} K^\pm$ as $R_{K\pi} = 0.013\pm0.010$, $R^*_{K\pi,D\pi^0} = -0.001\pm0.006$ and $R^*_{K\pi,D\gamma} = 0.011\pm0.019$.

We use the results for $R^*_{K\pi,D\pi^0}$ and $R^*_{K\pi,D\gamma}$ to set a model independent limit $r_B^{B^\pm} \equiv |A(B^- \rightarrow D^0 K^-)/A(B^- \rightarrow D^0 K^-)|^2 < (0.16)^2$ at the 90% confidence level. We also set 90% C.L. limits on the ratio $R_{K\pi} < 0.030$ (90% C.L.). With the most conservative assumption on the values of $\gamma$ and of the strong phases in the $B$ and $D$ decays, this limit translates into a limit on the ratio of the magnitudes of the $B^- \rightarrow D^0 K^-$ and $B^- \rightarrow D^0 K^-$ amplitudes amplitude $r_B < 0.23$ at 90% C.L.. If $r_B$ and $r_B^*$ are small, as our analysis suggests, the suppression of the $b \rightarrow u$ amplitude will make the determination of $\gamma$ using methods based on the interference of the diagrams in Figure 1 difficult.

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