Initiation of the Non-metallic Inclusions Influenced by Slag-Metal Reactions in Ti-Containing Ferritic Stainless Steel

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Laboratory experiment and thermodynamic calculation for the Ti-containing 24 mass pct Cr ferritic stainless steel with a CaO-SiO₂-Al₂O₃-MgO system slag were performed to investigate the effect of slag addition on the inclusion characteristics in molten steel. The morphology, composition, and size evolution of inclusions in steel samples were analyzed in three-dimensional by the electrolytic extraction method and in two-dimensional by the automatic analysis method. The results showed that the Ti content significantly decreased after the slag addition. However, the change of the Si content showed an opposite tendency. The decrease of the Ti content in steel was due to the reduction of SiO₂ and Al₂O₃ in the slag by dissolved Ti in steel. An increase of the TiO₂ content in the slag can decrease the Ti loss in steel based on the slag-steel kinetic analysis. The total O content in the steel melt decreased from 62 to 26 ppm, and the steel cleanliness was improved, since the number density of inclusions decreased after the slag refining. The results of a kinetic analysis showed that the rate-determining step of the oxidation of Ti in the steel and the reduction of SiO₂ in the slag were the mass transfer on the slag side. In addition, high TiO₂-containing inclusions were found to be transformed to Cr₂O₃-TiO₂-Al₂O₃ and Cr₂O₃-TiO₂-SiO₂ system inclusions after the slag addition. The Al₂O₃ contents in inclusions increased while the TiO₂ contents decreased with time. However, there were some amount of high melting point inclusions with high Al₂O₃ content, which were not what we expected. When plotted on logarithmic scales, the mole ratio $X_{Al_{2}O_{3}}/(X_{Ti_{2}O_{3}} \cdot X_{Cr_{2}O_{3}})$ values of the inclusions were expressed as a linear function of the $a_{Al}^2/(a_{Ti}^2 \cdot a_{Cr}^2 \cdot a_{O}^3)$ values of the steel melts with a slope of unity, which was theoretically expected.

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I. INTRODUCTION

TITANIUM-CONTAINING ferritic stainless steels are widely used in various applications which require both high-temperature mechanical properties and excellent oxidation and corrosion resistance in an aggressive environment.[1] However, the presence of non-metallic inclusions, i.e., titanium oxides and nitrides, caused by the alloy addition can seriously affect the production process as well as the quality of the final steel products, for example, clogging of the submerged entry nozzle.[2,3] Normally, inclusions need to be removed or modified to achieve the optimal steel properties. The objective of inclusion modification techniques is to convert the existing solid inclusions to liquid inclusions that can be removed by coalescence and floatation.[4,5] Further, liquid inclusions would be easy to deform thus preventing failure during casting and rolling.[6-8] Therefore, it is crucial to control the formation of oxide inclusions in Ti-containing stainless steel during the steelmaking process.

For inclusions in Ti-stabilized ferritic stainless steels, many studies focused on the behaviour of Al₂O₃, Al₂O₃-TiO₂, MgO-Al₂O₃-TiO₂ and TiN inclusions at different refining and casting stages.[1,9,10] Calcium treatment of Ti-bearing inclusions in steel contributes
to the production of high-quality steel with fewer defects caused by inclusions. \cite{12} Li et al.,\cite{9, 13} and Chen et al.\cite{14} have shown that a small amount of Ca in Al-killed Ti-bearing stainless steel effectively modified Al<sub>2</sub>O<sub>3</sub>-TiO<sub>x</sub> inclusions into liquid oxides and reduced the stability of the spinel by modifying the solid Al<sub>2</sub>O<sub>3</sub> inclusions into liquid calcium aluminates. Seo et al.\cite{15} investigated the effect of the Ca and Ti addition sequence on the inclusion behavior in Al-killed Ti-bearing stainless steels. They reported that a Ca treatment after the Ti addition was not an effective way to minimize the spinel formation. However, a Ca treatment before the Ti addition efficiently prevented the formation of MgAl<sub>2</sub>O<sub>4</sub> spinel because of the depletion of available Al<sub>2</sub>O<sub>3</sub> by the earlier Ca operation. Kruger et al.\cite{10} also investigated the effect of a Ca treatment on the modification of oxide inclusions in Ti-containing 24 mass pct Cr stainless steel. They reported that a Ca treatment before the Ti addition efficiently prevented the formation of MgAl<sub>2</sub>O<sub>4</sub> spinel because of the depletion of available Al<sub>2</sub>O<sub>3</sub> by the earlier Ca operation. Kruer et al.\cite{11} investigated the effect of Ca treatment on the modification of oxide inclusions in Ti-containing 24 mass pct Cr stainless steel. They reported that a Ca treatment before the Ti addition efficiently prevented the formation of MgAl<sub>2</sub>O<sub>4</sub> spinel because of the depletion of available Al<sub>2</sub>O<sub>3</sub> by the earlier Ca operation. Kruger et al.\cite{12} investigated the effect of the Ca and Ti addition sequence on the inclusion behavior in Al-killed Ti-bearing stainless steels. They reported that a Ca treatment after the Ti addition was not an effective way to minimize the spinel formation. However, a Ca treatment before the Ti addition efficiently prevented the formation of MgAl<sub>2</sub>O<sub>4</sub> spinel because of the depletion of available Al<sub>2</sub>O<sub>3</sub> by the earlier Ca operation. Kruger et al.\cite{13} reported that the spinel inclusions were modified to spherical dual-phase spinel-liquid matrix inclusions by Ca treatment in a Ti-stabilized 11 mass pct Cr (409) stainless steel, which eliminated the clogging of SEN for this grade. In summary, these studies have investigated the effect of a Ca treatment on the modification of inclusions in molten steel.

Meanwhile, it is well known that the refining slag having a proper composition and excellent physico-chemical properties can effectively modify and remove the inclusions.\cite{16-23} It is a significant advantage that a good contact between metal and slag makes the steel chemically refined.\cite{24} Park et al.\cite{25} investigated the effect of CaO-Al<sub>2</sub>O<sub>3</sub>-MgO slags on the formation of MgO-Al<sub>2</sub>O<sub>3</sub> inclusions in a Si deoxidized 16 mass pct Cr ferritic stainless steel. They found that the MgO-rich spinel solid solutions were formed in the steel melt equilibrated with the highly basic slags saturated by MgO or MgO. Later, Park et al.\cite{26} also investigated the equilibrium between CaO-SiO<sub>2</sub>-MgO-Al<sub>2</sub>O<sub>3</sub>-CaF<sub>2</sub> (TiO<sub>2</sub>) slag and a Si deoxidized Ti-stabilized ferritic stainless steel containing 11 mass pct Cr. They reported that the inclusions in the steel melt equilibrated with the basic slags were located in the spinel+liquid multiphase region, while those in equilibrium with the less basic slags were located in the fully liquid region. Kim et al.\cite{27} investigated the formation of complex oxide inclusions in Al-Ti deoxidized 304 stainless steel. They concluded that a decrease in the slag basicity was the most effective way to reduce the crystallization of the harmful CaO-TiO<sub>2</sub> phase in inclusions. Li et al.\cite{28} investigated the effect of CaO-MgO-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub>-CaF<sub>2</sub> slags containing different CaF<sub>2</sub> contents on the inclusion characteristics in an Al deoxidized Ti-stabilized 20 mass pct Cr stainless steel. They concluded that the lower the CaF<sub>2</sub> content in slag, the lower MgO content of inclusions in steel, which made most of the inclusions located in or close to the liquid phase field.

High basicity slags have commonly been used in Al-killed steels to reach a high cleanliness and inclusions having low melting temperature.\cite{28-30} Nevertheless, the effect of slag on the high TiO<sub>x</sub> contained inclusions in Ti-containing stainless steel has been under discussion. Therefore, in the present study, the refractory-slag-metal reaction experiments were performed to investigate the effect of the CaO-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub>-MgO slag on the evolution of oxide inclusions in Ti-containing 24 mass pct Cr stainless steel.

II. METHODOLOGY

A. Experimental Procedures

The experiment was carried out using a high-frequency induction furnace, which is shown in Figure 1(a). The quartz reaction chamber was initially evacuated using a mechanical rotary pump prior to performing the experiments; the chamber was subsequently filled with a highly purified Ar-3 pct H<sub>2</sub> gas mixture controlled using a mass flow controller. Impurities in the Ar–H<sub>2</sub> gas mixture were removed by passing the gas through Drierite (W.A. Hammond Drierite Co. Ltd., Xenia, OH), silica gel, and Mg turnings at 723 K (450 °C). The quartz reaction chamber was subsequently filled with a refractory mixture (99.9 pct purity, 60 × 50 × 120 mm) with a graphite heater for induction heating; the heater was surrounded by insulation. The experimental temperature was 1873 K (1600 °C), which was controlled within ± 2 K (2 °C) using a B-type (Pt-30Rh/Pt-6Rh, mass pct) thermocouple and a proportional integral differential controller. After the temperature was stabilized for 30 min, 85 g FeCr alloy was added through the quartz tube (14 × 12 × 500 mm) under an Ar-3 pct H<sub>2</sub> atmosphere. The chemical compositions of the steel and FeCr alloy are shown in Table I.

Several steel samples were taken after the FeCr addition, and the inclusion characterization results were reported elsewhere.\cite{31} After 30 min of the alloy addition, sample S0 was taken from the molten steel using a quartz tube (ID = 4 mm). Thereafter, 50 g slag was added on the surface of molten steel under an Ar-3 pct H<sub>2</sub> atmosphere. The slag was prepared by melting reagent grades of SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, MgO and CaO in advance in a vertical resistance tube furnace under a purified Ar atmosphere. Here, CaO was obtained from a reagent grade of CaCO<sub>3</sub>, which was calcined at 1273 K (1000 °C) for 12 hours. Then, steel samples were taken at predetermined times after the slag addition (S1-5 min, S2-15 min, S3-25 min) and rapidly quenched in water. Slag samples were also taken using stainless steel rods at the predetermined times (Slag 1-5 min, Slag 2-15 min, Slag 3-25 min), as shown in Figure 1(b).

B. Analysis and Characterization

The chemical compositions of the steel and slag samples were determined using inductively coupled plasma atomic emission spectrometry (ICP-AES, ACROS, SPECTRO) and X-ray fluorescence spectroscopy (XRF, Bruker, model S4 Explorer). The oxygen and nitrogen contents were determined by using a LECO combustion analyzer. Three-dimensional observations using the electrolytic extraction method were used to observe the exact morphology and composition of inclusions in the steel samples. For this experiment, a 10 pct AA solution (10 pct acetylacetone,
1 pct tetramethylammonium chloride, and methanol) was used as the electrolyte, and a 750 mA current was applied for 3 h. The extracted inclusions were filtered out by using a vacuum pump and laid on a membrane filter with a pore size of 0.1 μm. Once completely dried, the filter was coated with platinum. Next, the inclusions on the filter were investigated using field emission scanning electron microscopy analysis (FESEM; TESCAN model MIRA 3) with an energy-dispersive X-ray spectroscope (EDS). Besides, the characterization of inclusions in two-dimensional, i.e., number density, size and composition, in the steel samples was performed using the automated inclusion analysis system. The following settings were applied: accelerating voltage 20 KV, magnification 500 times and a 1 μm limit diameter for inclusion detection in a 10 mm² area.

III. RESULTS AND DISCUSSION

A. Characterization of Inclusions

SEM images of typical inclusions found in the samples before and after the slag addition are shown in Figure 2. To get stable TiOₓ and TiOₓ-CrOₓ based inclusions, FeCr alloys were added into the Ti-containing steels. The inclusion characteristics can be found from previous work,[31] where Ti₂O₃ and Cr₂O₃ were chosen to represent the Ti oxide and Cr oxide in inclusions. Before the slag addition, the main inclusions were TiO₂-CrO₂ based systems containing a small amount of Al₂O₃ content. It should be pointed out that the TiO₂-Cr₂O₃ based inclusions have rarely been reported before. They can further be divided into two groups based on their morphologies and compositions: irregular shapes with lower Cr₂O₃ contents (Figure 2(a)) and globular shapes with higher Cr₂O₃ contents (Figure 2(b)). In addition, a small number of spherical TiO₂-Cr₂O₃-SiO₂ inclusions (Figure 2(c)) were also observed.

In sample S1 taken after 5 min of the slag addition, the number of inclusions significantly increased due to the slag-steel reactions. A relatively larger amount of inclusions were located together on the film filters, as shown in Figure 2(d). The original TiO₂-Cr₂O₃ based inclusions with different morphologies (Figure 2(e) and (f)) still existed. Besides, spherical (Figure 2(g)) TiO₂-Cr₂O₃-Al₂O₃ inclusions were observed, which had higher Al₂O₃ contents compared to the TiO₂-Cr₂O₃ based inclusions. The corresponding elemental mappings of these TiO₂-Cr₂O₃-Al₂O₃ inclusions are shown in Figure 3(a).

It is of interest to note that dual-phase TiO₂-Cr₂O₃-SiO₂ inclusions were commonly observed in this sample, where the Al₂O₃ content was less than 5 mass pct. They consisted of a dark grey phase having higher Si contents and a light grey phase with lower Si contents (Figures 2(h) and (i)). In addition, some dark phases contained TiO₂, Cr₂O₃, SiO₂ and Al₂O₃ four components (Figure 2(j)). The elemental mappings of the typical dual-phase TiO₂-Cr₂O₃-SiO₂ inclusions are shown in Figures 3(b) through (d). Homogenous spherical TiO₂-Cr₂O₃-SiO₂ inclusions were also found (Figure 2(k)), the elemental mappings are shown in Figure 3(e). Moreover, spherical complex TiO₂-Cr₂O₃-SiO₂-Al₂O₃ inclusions were observed (Figure 2(l)). In addition, they were found in all the following samples.
In sample S2 taken after 15 min of the slag addition, the number of inclusions significantly reduced, which is discussed in detail in Figure 5 later. Moreover, most irregular shaped Ti₂O₃-Cr₂O₃ based inclusions disappeared and were transformed into spherical (Figure 2(m)) and polygonal (Figure 2(n)) Ti₂O₃-Cr₂O₃-Al₂O₃ inclusions. Specifically, the polygonal type consisted of a homogeneous one and a heterogeneous one containing higher Al₂O₃ contents in the center. Their mappings results are shown in Figures 3(f) and (g). In addition, spherical complex Ti₂O₃-Cr₂O₃-SiO₂-Al₂O₃ inclusions (Figure 2(o)) were more commonly observed than Ti₂O₃-Cr₂O₃-SiO₂ inclusions. It should be noted that the Ti₂O₃-Cr₂O₃-SiO₂-Al₂O₃ inclusions started to form in sample S1 (5 min) and that the Al₂O₃ contents in these inclusions obviously increased with time. In the final sample S3 taken after 25 min of the slag addition, the types of inclusions were similar to those found in sample S2, but with some composition changes.

To investigate the evolution of inclusions, the compositions of inclusions in different samples were projected onto the CrOₓ-TiO₂-Al₂O₃ and CrOₓ-TiO₂-SiO₂ ternary phase diagrams, as shown in Figure 4. The phase diagrams were calculated with the aid of FactSage 7.1.
software using the FactPS and FToxid databases at 1873 K (1600 °C) and p(O₂) = 10⁻¹⁵ atm, which was calculated based on the measured oxygen content. The details of the calculation to determine the oxygen partial pressure in the present system is given elsewhere. It can be seen from Figure 4(a) that the main compositions of inclusions are concentrated in the single liquid and Ti₂O₃ + liquid regions before the slag addition. After 5 min of the slag addition (S1), the number of inclusions significantly increases, as shown in Figure 4(b). The majority of inclusions are located in the single liquid region. The Ti₂O₃ contents slightly decrease while the Al₂O₃ contents in inclusions are higher than those in sample S0 (Figure 4(a)). In sample S2 (15 min), the Al₂O₃ contents in inclusions continue to increase and there are very few inclusions in the Ti₂O₃ + liquid region (Figure 4(c)). The tendency is more obvious as most of the inclusions move towards the Al₂O₃ + liquid region in sample S3 (Figure 4(d)). Therefore, the slag addition has a great effect on the transformations of inclusions.

The composition distributions of homogeneous and multiphase Ti₂O₃-Cr₂O₃-SiO₂ inclusions in all four samples are presented in Figure 4(e). As can be seen, most of the inclusions are located in the single liquid phase region. Also, a small number of inclusions with higher SiO₂ contents are located in the SiO₂ + liquid region, which corresponds to the high SiO₂ phase in the multiphase inclusions. However, it should be noted that the automatic two-dimensional SEM analysis only resolves one point composition of each inclusion. Thus, there might be more multiphase inclusions present. In terms of the homogeneous Ti₂O₃-Cr₂O₃-SiO₂-Al₂O₃ inclusions (Figure 4(f)), the Al₂O₃ contents in these inclusions are first grouped with the Cr₂O₃ contents and then their compositions are projected onto the CrOₓ-Ti₂O₃-SiO₂ ternary phase diagram. Most of the inclusions are located in the liquid area, and their composition distributions overlapped to some extent. Moreover, the Cr₂O₃ + Al₂O₃ contents obviously increase and the Ti₂O₃ contents decrease with time.

Fig. 3—Element mappings of typical inclusions (a) spherical Ti₂O₃-Cr₂O₃-Al₂O₃ inclusions, (b) through (d) multiphase Ti₂O₃-Cr₂O₃-SiO₂ inclusions, (e) homogenous Ti₂O₃-Cr₂O₃-SiO₂ inclusions, (f) and (g) polygonal Ti₂O₃-Cr₂O₃-Al₂O₃ inclusions.
The number density and area fraction variations of different types of inclusions show similar tendency, which are illustrated in Figure 5. Before the slag addition (S0), the major type is the Ti$_2$O$_3$-Cr$_2$O$_3$-Al$_2$O$_3$ system inclusions. After 5 min of the slag addition (S1), the number of this type of inclusions has increased by about 5 times. A large number of inclusions have been formed due to the slag-steel reactions. Thereafter, their number continues to decrease with time due to the inclusion floatation and absorption of inclusions by slag. Finally, their number approximately reduces by half in sample S3 (25 min) compared to that in sample S0 before the slag addition.

The number of Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions (multi-phase and homogeneous) also greatly increases in sample S1. The number density of Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions is almost twice more than that of Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions. In sample S2, the reduction of the number density of Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions is much greater than that of
Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions. This might be attributed to the fact that some Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions have been transformed into Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions. This tendency continues with time and the Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions are more dominant in the SiO$_2$ containing inclusions in the final sample S3.

The effect of the slag addition on the average compositions and sizes of Ti$_2$O$_3$-Cr$_2$O$_3$-Al$_2$O$_3$ and Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions is shown in Figure 6. The Al$_2$O$_3$ contents in Ti$_2$O$_3$-Cr$_2$O$_3$-Al$_2$O$_3$ inclusions significantly increase from 10 to 42 mass pct, while the Ti$_2$O$_3$ and Cr$_2$O$_3$ contents decrease after the slag additions. These results indicate that the oxides of Ti$_2$O$_3$ and Cr$_2$O$_3$ are reduced by dissolved Al. The composition change of Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions shows a similar tendency to that of Ti$_2$O$_3$-Cr$_2$O$_3$-Al$_2$O$_3$ inclusions. The final Al$_2$O$_3$ contents in the Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions reach about 30 mass pct, and the Ti$_2$O$_3$ and SiO$_2$ contents slightly decrease. The composition distributions of this type of inclusions move towards the Cr$_2$O$_3$ + Al$_2$O$_3$ corner with time (Figure 4(f)) and these are primarily due to the increase of the Al$_2$O$_3$ contents. The average sizes of these two types of inclusions first increase and reach a peak at 15 min and then decrease. Their final sizes have similar values of approximately 1.2 (±0.3) μm.

B. Slag-Steel Reactions

1. Composition change of molten steel and slag

After the slag addition, it took about 3 min for the slag to be fully melted, as shown in Figure 7. The compositions of the initial premelted slag, and the slag and steel samples taken at different times are shown in Table II and Figure 8. A high basicity ((CaO)/(SiO$_2$) = 6) MgO saturated slag was used in the present study. After the slag addition, the CaO and SiO$_2$ contents slightly decreased, while the Al$_2$O$_3$ content increased (but not significant) with time. It should be noted that titanium oxide generated after the slag-steel reactions continuously increased with time, indicating the oxidation of Ti in the steel. Here, the titanium oxide is assumed to be TiO$_2$ for the sake of simplicity. In terms of the steel compositions, the Ti content significantly decreased while the Al content only gradually decreased with time. The Si content showed an increasing tendency with time but with a small fluctuation, which increased
greatly during the first 5 min. The total O content decreased from 62 to 26 ppm after the slag addition, which indicated that the cleanliness of the steel had been improved due to the slag refining. The changes in the slag and steel compositions were due to the slag-steel reactions.

The activities of the slag components at the initial and final compositions were calculated with an aid of FactSage 7.1 software using the FToxide database, the results are shown in Figure 9. The activity of CaO decreases with time, whereas the activities of Al2O3, SiO2 and TiO2 all increase with time. Besides, the activity of Al2O3 is much higher than those of SiO2 and TiO2. This can be explained by the fact that the TiO2 in the slag is an acidic oxide which has a strong affinity with CaO. Thus, the activity of CaO decreases with an increased TiO2 content. Therefore, the relative attraction between SiO2, Al2O3 and CaO decreases, which further increases the SiO2 and Al2O3 activity.[32] Therefore, the activity changes of slag component not simply depend on their compositions, but also the attractive force between different components. The activity changes of the slag components have a significant influence on the Al, Ti and Si contents in the steel melts.

During the refining process of Ti-bearing stainless steel, the slag-steel reaction could lead to the loss of titanium in molten steel.[27,33] The SiO2 and Al2O3 in slag can react with Ti in molten steel according to Eqs. [1] and [4], which would cause a loss of Ti in steel.[10,27,32,34] Moreover, considering the mass balance of the decrease of SiO2 and the increase of TiO2 in the slag, both reactions happened in the present study. Also, the increase of Al2O3 in the slag might be due to the reaction between SiO2 in the slag and Al in the molten steel based on Eq. [7].

\[
[Ti] + (SiO_2) = (TiO_2) + [Si]
\]  

where \(a_{TiO_2}, a_{SiO_2}\) and \(a_{AlO_3}\) are the activities of TiO2, SiO2 and Al2O3 in the slag; \(f_{Ti}, f_{Si}\) and \(f_{Al}\) are the Hennian activity coefficients of Ti, Si and Al in the steel.

![Fig. 7—Melting process of slag during the experiment.](image)

According to Eqs. [3], [6] and [9], the dependence of the composition ratios of steel on the activity ratios of slag in different samples can be calculated, as shown in Figure 10. Based on Eq. [3], the increase of log([TiO2]/[SiO2]) in the slag could cause an increase of log([%Ti]/[%Si]) in the molten steel. This, in turn, can result in higher Ti contents and lower Si contents in the steel melt. It indicates that an increased TiO2 activity can lead to a higher Ti content in the steel melt, which is also obtained in the following kinetics analysis. However, it should be pointed out that the increased TiO2 activity should be obtained in the original slag before

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**Table II. Compositions of the Steel and Slag Samples Investigated in the Present Study**

| Sample | [Ti, Pct] | [Si, Pct] | [Al, Pct] | [O, ppm] | CaO | Al2O3 | MgO | SiO2 | TiO2 |
|--------|-----------|-----------|-----------|---------|-----|-------|-----|------|------|
| S0     | 0.13      | 0.20      | 0.01      | 62      | 53.2| 31.4  | 6.4 | 9    | 0    |
| S1     | 0.03      | 0.28      | 0.01      | 45      | 51.7| 31.7  | 6.4 | 8.6  | 1.6  |
| S2     | 0.03      | 0.26      | 0.01      | 34      | 49.9| 32.7  | 6.9 | 7.8  | 2.7  |
| S3     | 0.02      | 0.28      | 0.01      | 27      | 48.0| 34.1  | 7.5 | 7.3  | 3.1  |
the slag-steel reactions. The measured values of log\(\frac{\%\text{Ti}}{\%\text{Si}}\) decrease when the log\(\frac{a_{\text{TiO}_2}}{a_{\text{SiO}_2}}\) of slag increases, which is due to the fact that the TiO\(_2\) is formed after the slag-steel reactions in the present study (Figure 10(a)). Similarly, in the case of Eq. [6], the decrease of log\(\frac{a_{\text{Al}_2\text{O}_3}}{a_{\text{TiO}_2}}\) slag could cause a decrease of log\(\frac{\%\text{Al}}{\%\text{Ti}}\) in the molten steel, but the experimental results also showed the opposite tendency (Figure 10(b)). Moreover, both the Al and Ti contents decreased with time as shown in Figure 8(b). Therefore, the reduction of the Ti content was greater than that of Al in the molten steel, which indicated that Eq. [4] might not be the main reaction. The decrease of log\(\frac{a_{\text{Al}_2\text{O}_3}}{a_{\text{SiO}_2}}\) of slag could cause a decrease of log\(\frac{\%\text{Al}}{\%\text{Si}}\) in the molten steel according to Eq. [9], where a similar tendency of the measured values of log\(\frac{\%\text{Al}}{\%\text{Si}}\) was obtained as shown in Figure 10(c). Based on these discussions, the final steel composition changes depend on these coupled reactions.

C. Kinetics of Slag-Steel Reactions

The coupled-reaction model and two film theory have frequently been applied to describe the kinetics of slag-steel reactions.\(^{30,32,35,36}\) It is assumed that the concentrations of Al\(_2\)O\(_3\), TiO\(_2\), SiO\(_2\) in the slag side and Al, Ti, Si and O in the steel show respective concentration gradients in the boundary film layer at the slag-steel interface, and have reached a thermodynamic equilibrium at the interface, as shown in Figure 11.

In the present study, the reactions [10], [12] and [14] were simultaneously considered to take place at the slag-steel interface. Assuming that these reactions occur rapidly during the present conditions, and local equilibrium reaches at the slag-steel interface. The corresponding equilibrium constants \(K\) for each reaction can be calculated.\(^{37-39}\) To simplify the computation, AlO\(_{1.5}\) is used. Apparent equilibrium constant \(B_i\) can be expressed by Eq. [16].
Fig. 10—Dependence of the composition ratios of steel on the activity ratios of slag (a) log($a_{TiO_2}/a_{SiO_2}$) to log($[\%Ti]/[\%Si]$), (b) log($a_{Al_2O_3}/a_{TiO_2}$) to log($[\%Al]^{\#}/[\%Ti]^{\#}$) and (c) log($a_{Al_2O_3}/a_{SiO_2}$) to log($[\%Al]^{\#}/[\%Si]^{\#}$).

Fig. 11—The schematic diagram for the reaction between slag and steel.

\[
[Al] + 1.5[O] = (AlO_{1.5}) \quad [10]
\]

\[
\log K_{10} = \log \frac{a_{AlO_{1.5}}}{a_{Al} \cdot a_{O}^{1.5}} = \log \frac{\gamma_{AlO_{1.5}} a_{AlO_{1.5}}}{f_{Al} \cdot [\%Al]^{2} \cdot f_{O}^{0.5} \cdot [\%O]^{1.5}} = \frac{32000}{T} - 10.29
\]

\[
[Ti] + 2[O] = (TiO_2) \quad [12]
\]

\[
\log K_{12} = \log \frac{a_{TiO_2}}{a_{Ti} \cdot a_{O}^{2}} = \log \frac{\gamma_{TiO_2} a_{TiO_2}}{f_{Ti} \cdot [\%Ti]^{\#} \cdot f_{O}^{2} \cdot [\%O]^{2\#}} = \frac{34458}{T} - 11.96
\]
\[ [\text{Si}] + 2[\text{O}] = (\text{SiO}_2) \]  \[ [14] \]

\[
\log K_{14} = \log \frac{a^e_{\text{SiO}_2}}{a^e_{\text{Si}}} = \log \frac{f_{\text{Si}}}{[\% \text{Si}]} \cdot \frac{f^2_{\text{O}}}{[\% \text{O}]}^2
\]

\[
= \frac{24600}{T} - 8.4 \tag{15} \]

\[
B_i = \left( \frac{[\% M_i O_n]^*}{[\% M]^*} \right) \cdot \frac{f_i \cdot K_i \cdot M_{M,O_n} \cdot \sum (\frac{[\% M_i O_n]}{M_{M,O_n}})}{\gamma M_i O_n} \tag{16} \]

\[
\log f_i = \sum (\epsilon_i^f [\% f] + r_i^f [\% f]^2) \tag{17} \]

where \( a_i \) is the activity of element \( i \) in the metal, \( f_i \) is the Henrian activity coefficient of element \( i \) referred to 1 pct standard state with mass percentage [%] as the concentration unit, which can be calculated by the classical Wagner formulation [17], using the first-order (\( \epsilon_i^f \)) and second-order (\( r_i^f \)) interaction parameters, which are listed in Table III. \( M_{M,O_n} \) and \( \gamma M_{i O_n} \) are the molecular weight and activity coefficient of \( M_i O_n \) in slag. \([\% M] \) and \( [\% M_i O_n] \) are the mass concentration of element \( i \) in steel and \( M_i O_n \) in slag.

Because the rates of the chemical reactions involving the respective component at the slag-steel interface are extremely large. Thus, mass transfer is the rate-determining step, which can be controlled by the mass transfer of metal in the steel side and slag component in the slag side. Therefore, the respective mass transfer resistance of metal (\( R_{M_i} \)) and slag component (\( R_{M_i O_n} \)) can be expressed by Eq. [18], which can express the controlling step in the reactions. During the transfer of component \( i \) from molten steel to slag, the flux density should be constant, this can be expressed by Eq. [19]. The modified mass transfer coefficients can be illustrated by Eqs. [20] and [21]. Therefore, the flux density of Al, Ti, Si and O can be derived by combing Eqs. [22] through [25].

### Table III. Interaction Parameters Used in the Present Study[10,36,40]

| \( \epsilon_i^f/\epsilon_i^f \) | Cr  | Si   | Mn   | Al   | Ti     | N    | O    |
|-------------------------|-----|------|------|------|-------|------|------|
| O                       | –0.032 | –0.066  | –0.037  | –1.17 (–0.01) | –0.54 (0.039) | 0.043  | –0.17  |
| Ti                      | 0.055  | –0.025 | –0.043 | 0.024 | 0.042 (–0.001) | 2.04  | 1.8  |
| Al                      | 0.03  | 0.056 | 0.035 | 0.043 | 0.016 | 0.033 | 1.98 (39.82) |
| Si                      | –0.021 | 0.1 | –0.007 | 0.058 | –0.013 | 0.11 | –0.12 |
transfer coefficients of element \( i \) and \( M_iO_n \) in slag (m/s), and \( M_i \) is molecular weight of element \( i \) in steel.

The oxygen activity \( a_{O_2} \) at the slag-steel interface can be determined by Eq. [26]. Then, the concentrations of each element in the metal as a function of time can be calculated by Eq. [27] when the calculated \( a_{O_2} \) value is 2.6 ppm. The parameters used in the calculations can be found in Table IV.

\[
1.5J_{Al} + 2J_{Ti} + 2J_{Si} - J_O = 0 \quad [26]
\]

\[
- \frac{d[\%i]}{dt} = k_{i,m} \cdot \frac{A}{V_m} ([\%i] - [\%i]^*) \quad [27]
\]

Figure 12(a) shows the measured and calculated results of the concentrations of Ti, Si, and Al in the steel as a function of time. It can be seen that the Si and Ti contents change more drastically during the first 5 min than during a later stage. Moreover, the calculated results of the contents of Al, Si, and Ti in the molten steel show relatively good agreement with the experimental results. Based on Eq. [18], the mass transfer resistance of the respective components on the slag side can be obtained. The calculated values for mass transfer resistances of \( Al_2O_3 \), \( TiO_2 \) and \( SiO_2 \) are 0.23, 44 and \( 2.3 \times 10^4 \) m\(^2\)/s/kg, respectively. The mass transfer resistance in molten steel is 0.71 m\(^2\)/s/kg. Therefore, the rate-determining step of the oxidation of Ti in the steel and the reduction of \( SiO_2 \) in the slag are the mass transfer on the slag side. Thus, the Ti content change can be expressed by Eq. [28].

\[
\frac{d[\%Ti]}{dt} = k_{Ti,m} \cdot \frac{A}{V_m} (\frac{\langle TiO_2 \rangle - \langle TiO_2^* \rangle}{2}) \quad [28]
\]

It is indicated that the Ti content change depends on the difference between the \( TiO_2 \) content in the slag and the \( TiO_2^* \) value at the slag-steel interface. According to a previous work,\([32]\) an increased \( TiO_2 \) content in slag can prevent a loss of titanium by the reaction of dissolved Ti in steel with alumina and silica in slag. Therefore, different \( TiO_2 \) contents in the original slag were considered, and the corresponding oxygen activity \( a_{O_2} \) values were calculated by Eq. [26]. It should be pointed out that this calculation was simply performed by increasing the \( TiO_2 \) content while keeping the proportion of other slag components unchanged. As a result, the Ti content change can be calculated by Eq. [27] when an \( a_{O_2} \) value is obtained. The calculated results are shown in Figure 12(b). As can be clearly seen that an increased \( TiO_2 \) content in the original slag results in a less decreased Ti content in the melt. This can be explained by the fact that a higher \( TiO_2 \) content in the slag can suppress reactions [1] and [4] to the right. From another point of view, the activities of \( SiO_2 \) and \( Al_2O_3 \) decrease with an increased \( TiO_2 \) content. Thus, reactions [1] and [4] become weakened due to the lower activities of \( SiO_2 \) and \( Al_2O_3 \) on the left side of the

Table IV. The Values of the Parameters Used in the Present Study

| Parameter                          | Value             | Parameter                          | Value             |
|------------------------------------|-------------------|------------------------------------|-------------------|
| Mass transfer coefficient of Al, Si, Ti and O in steel | \( 2 \times 10^{-4} \) m/s\([30]\) | Density of steel, \( \rho_{steel} \) | 7000 kg/m\(^3\)\([41]\) |
| Mass transfer coefficient of \( Al_2O_3 \), TiO\(_2\) in slag | \( 1 \times 10^{-5} \) m/s\([30]\) | Density of slag, \( \rho_{slag} \) | 3000 kg/m\(^3\)\([41]\) |
| Mass transfer coefficient of \( SiO_2 \) in slag | \( 2 \times 10^{-6} \) m/s\([30]\) | Weight of steel, \( W_{steel} \) | 500 g |
| Reaction area between the steel and slag, A | \( \pi \cdot (0.025)^2 \) m\(^2\) | Weight of slag, \( W_{slag} \) | 50 g |

Fig. 12—Measured changes of Ti, Si and Al contents in steel melt compared with those calculated values (a) and calculated Ti contents as a function of the \( TiO_2 \) content in slag (b).
reactions. Therefore, TiO\textsubscript{2} or complex inclusions containing TiO\textsubscript{2} due to the reactions between Ti and SiO\textsubscript{2} and Al\textsubscript{2}O\textsubscript{3} will be reduced. It was reported that there was an optimum TiO\textsubscript{2} content of about 8 mass pct due to the different combining affinity between TiO\textsubscript{2} and other components.\textsuperscript{[32]} However, because this kind of experimental work was not carried out in the present study, future work needs to investigate the optimum slag composition to get a low Ti loss in the steel melt.

D. Thermodynamic Calculations of Inclusion Formations

The effect of the activity of alumina in the slag on the mole fraction of alumina in the inclusions is shown in Figure 13. The mole fraction of Al\textsubscript{2}O\textsubscript{3} in both Ti\textsubscript{2}O\textsubscript{3}-Cr\textsubscript{2}O\textsubscript{3}-Al\textsubscript{2}O\textsubscript{3} and Ti\textsubscript{2}O\textsubscript{3}-Cr\textsubscript{2}O\textsubscript{3}-SiO\textsubscript{2}-Al\textsubscript{2}O\textsubscript{3} inclusions (log $X_{\text{Al}_2\text{O}_3}$) increases linearly with an increased activity of Al\textsubscript{2}O\textsubscript{3} (log $a_{\text{Al}_2\text{O}_3}$) in the slag. However, it is of interest to note that the slopes of the lines are 1.4 (r\textsuperscript{2} = 0.99) and 2.1 (r\textsuperscript{2} = 0.98) in the Ti\textsubscript{2}O\textsubscript{3}-Cr\textsubscript{2}O\textsubscript{3}-Al\textsubscript{2}O\textsubscript{3} and Ti\textsubscript{2}O\textsubscript{3}-Cr\textsubscript{2}O\textsubscript{3}-SiO\textsubscript{2}-Al\textsubscript{2}O\textsubscript{3} inclusions, respectively. This indicates that the stability of Al\textsubscript{2}O\textsubscript{3} in the inclusions could significantly be affected by the reactions between slags and steel melts. Moreover, the average content changes of Al\textsubscript{2}O\textsubscript{3} in both types of inclusions during the same period are nearly the same (as shown in Figure 6), while the presence of SiO\textsubscript{2} has a larger effect on the activity coefficient of alumina in the inclusions.

After the slag addition, the Ti\textsubscript{2}O\textsubscript{3} and Cr\textsubscript{2}O\textsubscript{3} contents decreased in the Ti\textsubscript{2}O\textsubscript{3}-Cr\textsubscript{2}O\textsubscript{3}-Al\textsubscript{2}O\textsubscript{3} inclusions. This might be due to the fact that they were reduced by dissolved Al in the steel melts based on Eqs. [29] and [31].\textsuperscript{[39,40,42]} Thus, the composition of inclusions can be deduced as a function of the activities of Al, Ti, Cr and O as given in Eq. [33] and [34].

\[ 2[\text{Al}] + (\text{Ti}_2\text{O}_3)_{\text{inclusion}} = (\text{Al}_2\text{O}_3)_{\text{inclusion}} + 2[\text{Ti}] \]  \hspace{1cm} [29]

\[ \log K_{29} = \log \frac{a_{\text{Al}}^2 \cdot a_{\text{Ti}_2\text{O}_3}}{a_{\text{Al}_2\text{O}_3} \cdot a_{\text{Ti}_2\text{O}_3}} = \frac{870}{T} - 1.44 \]  \hspace{1cm} [30]

\[ 2[\text{Al}] + (\text{Cr}_2\text{O}_3)_{\text{inclusion}} = (\text{Al}_2\text{O}_3)_{\text{inclusion}} + 2[\text{Cr}] \]  \hspace{1cm} [31]

\[ \log K_{31} = \log \frac{a_{\text{Al}}^2 \cdot a_{\text{Cr}_2\text{O}_3}}{a_{\text{Cr}_2\text{O}_3} \cdot a_{\text{Al}_2\text{O}_3}} = \frac{9100}{T} + 4.48 \]  \hspace{1cm} [32]

\[ \log \frac{X_{\text{Al}_2\text{O}_3}}{X_{\text{Ti}_2\text{O}_3}} = \frac{\log a_{\text{Al}}^2}{\log a_{\text{Ti}_2\text{O}_3}} - \log \frac{\gamma_{\text{Al}_2\text{O}_3}}{\gamma_{\text{Ti}_2\text{O}_3}} + \log K \]  \hspace{1cm} [33]

\[ \log \frac{X_{\text{Al}_2\text{O}_3}}{X_{\text{Cr}_2\text{O}_3}} = \frac{\log a_{\text{Al}}^2}{\log a_{\text{Cr}_2\text{O}_3}} - \log \frac{\gamma_{\text{Al}_2\text{O}_3}}{\gamma_{\text{Cr}_2\text{O}_3}} + \log K \]  \hspace{1cm} [34]

where $a_i$ denotes the activity of component $i$ in steel, $X_{MO}$ and $\gamma_{MO}$ are the mole fraction and the activity coefficient of MO in the inclusions.

Therefore, it can be expected that on a logarithmic scale the mole ratios of the inclusion components are in direct proportion to the logarithmic activity ratios of Al, Ti, Cr and O in the steel melts with a slope of unity, by assuming that the activity coefficient ratio $\gamma_{\text{Al}_2\text{O}_3}/\gamma_{\text{Ti}_2\text{O}_3}$ and $\gamma_{\text{Al}_2\text{O}_3}/(\gamma_{\text{Ti}_2\text{O}_3} \cdot \gamma_{\text{Cr}_2\text{O}_3})$ in Eqs. [33] and [34] would not be significantly affected by the compositions at a fixed temperature. Their relationships are given in Figure 14. The log($X_{\text{Al}_2\text{O}_3}/X_{\text{Ti}_2\text{O}_3}$) and log($X_{\text{Al}_2\text{O}_3}/(X_{\text{Ti}_2\text{O}_3} \cdot X_{\text{Cr}_2\text{O}_3})$) values of the inclusions increase linearly by increasing log($a_{\text{Al}}^2/a_{\text{Ti}_2\text{O}_3}^2$) and log($a_{\text{Al}}^2/a_{\text{Cr}_2\text{O}_3}^2$) values, respectively. However, it is of interest that the slope of the line for Eq. [33] is about 0.81 (R\textsuperscript{2} = 0.88), which is smaller than the expected value of unity. Whereas the slope of the line for Eq. [34] is 1.04 (R\textsuperscript{2} = 0.99), which is very close to unity as expected. This difference means that both Ti\textsubscript{2}O\textsubscript{3} and Cr\textsubscript{2}O\textsubscript{3} in the inclusions are simultaneously reduced by dissolved Al, which is in good agreement with the experimental results. The transformation tendency of the Ti\textsubscript{2}O\textsubscript{3}-Cr\textsubscript{2}O\textsubscript{3}-Al\textsubscript{2}O\textsubscript{3} inclusions can be predicted from the thermodynamics of Al, Ti, Cr and O in the steel melts.\textsuperscript{[10,25,43]}

In terms of the SiO\textsubscript{2}-containing inclusions, the typical multiphase and homogeneous inclusions formed after the slag additions have been mentioned in Figure 2. These inclusions were spherical in shape but with varied Si-Ti-Cr contents. Figure 15 shows possible evolutions of these SiO\textsubscript{2}-containing inclusions after the slag additions. The dissolved Si content increased in the melt after the slag additions, which originated from the
reduction products of the slag-steel reactions as discussed before. They reacted with the Ti$_2$O$_3$-Cr$_2$O$_3$ inclusions to form a Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ phase, resulting in the formation of multiphase inclusions. The oxide inclusions transformed by gaining SiO$_2$ and losing Ti$_2$O$_3$, Cr$_2$O$_3$ or both can be expressed by Eqs. [35] and [36]. In addition, the drop in the Ti content was higher than the Cr content in the inclusions, which suggested that Si reduced Ti$_2$O$_3$ more severely than Cr$_2$O$_3$.

In terms of the multiphase inclusions, they can be divided into two groups: type 1 containing Ti$_2$O$_3$-Cr$_2$O$_3$ and Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ two different phases and type 2 containing a Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ phase and a SiO$_2$-rich SiO$_2$-Cr$_2$O$_3$-(Cr$_2$O$_3$) phase. The compositions of the Ti$_2$O$_3$-Cr$_2$O$_3$ and Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ phases are located in the liquid phase region, while those of the SiO$_2$-rich phases are located in the SiO$_2$+liquid region and they have higher melting points. In type 1 inclusions, Si in the steel continually reacted with the Ti$_2$O$_3$-Cr$_2$O$_3$ inclusions and were then transformed into type 3 homogeneous Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions. This was also applied to the Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ phases in type 2 inclusions. Moreover, the SiO$_2$-rich phases in type 2 inclusions were attributed to the enrichment of Si. Thereafter, the higher chemical potential of Si in the SiO$_2$-rich phases may have resulted in the diffusion of Si into the low melting Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ phases. Conversely, the Ti and Cr contents in the low melting phases diffused into the SiO$_2$-rich phases. When the diffusion reached a certain extent, a distinct interface between the low melting phases and SiO$_2$-rich phases disappeared and spherical homogeneous type 3 Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions were formed. Further, due to the increased activity of Al$_2$O$_3$ in the slag, the Ti$_2$O$_3$, Cr$_2$O$_3$, and also SiO$_2$ contents in the inclusions were simultaneously reduced by dissolved Al in the steel melts based on the Eqs. [29], [31] and [37]. Finally, some Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$ inclusions were transformed into spherical complex Ti$_2$O$_3$-Cr$_2$O$_3$-SiO$_2$-Al$_2$O$_3$ inclusions.
2(Cr₂O₃)\text{inclusion} + 3[Si] = 3(SiO₂)\text{inclusion} + 4[Cr] \Delta G_{35}^{0} = -26806 - 1347 \text{J/mol} \ [35] \\
2([Ti]₂O₃)\text{inclusion} + 3[Si] = 3(SiO₂)\text{inclusion} + 4[Ti] \Delta G_{36}^{0} = 288371 - 17.37 \text{T J/mol} \ [36] \\
3(SiO₂)\text{inclusion} + 4[Al] = 2(Al₂O₃)\text{inclusion} + 3[Si] \Delta G_{37}^{0} = -321670 - 37.5 \text{T J/mol} \ [37] 

IV. CONCLUSIONS

In the present study, the equilibration between a CaO-SiO₂-Al₂O₃-MgO slag and a Ti-containing ferritic stainless steel melt was investigated at 1873 K (1600 °C) to clarify the effect of the slag composition on the modification of high Ti₂O₃-containing inclusions. Moreover, the slag-steel reaction was investigated from the viewpoint of kinetics. The following conclusions were obtained.

1. The total O content greatly decreased from 62 ppm to 26 ppm after the slag addition. High Ti₂O₃-containing inclusions were transformed to Ti₂O₃-Cr₂O₃-Al₂O₃ and Ti₂O₃-Cr₂O₃-SiO₂ two system liquid inclusions after the slag addition. The number density of inclusions decreased to a lower level than that before the slag addition.

2. The mole fraction of Al₂O₃ in both Ti₂O₃-Cr₂O₃-Al₂O₃ and Ti₂O₃-Cr₂O₃-SiO₂-Al₂O₃ inclusions increases linearly with an increased activity of Al₂O₃ (log \(X_{Al_2O_3} = \log A_{Al_2O_3} \)) in the slag. The Al₂O₃ content in both inclusion types obviously increased with time. The log [\(X_{Al_2O_3}/(X_{Ti_2O_3} \cdot X_{Cr_2O_3})\)] values of the inclusions were expressed as a linear function of log [\(A_{Al_2O_3}/(A_{Ti_2O_3} \cdot A_{Cr_2O_3} \cdot A_{O})\)] values of the steel melts with a slope of unity, which was theoretically expected.

3. The slag-steel reactions have a great effect on the slag and steel compositions, where the Ti content greatly decreased and TiO₂ generated in the slag. Based on the kinetic analysis, the rate-determining step of the oxidation of Ti in the steel and the reduction of SiO₂ in the slag are the mass transfer on the slag side. The addition of some amount of TiO₂ in the slag can prevent a loss of Ti in the steel melt.

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