Fatigue cracks in aluminum alloys structures detection using electromagnetic sensors array

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Abstract. The paper presents the architecture of a new type of electromagnetic sensor in 2D structure designed and made in order to estimate the location of a discontinuity below the surface of a conductive material. The use of 2D emission reception architecture in configuration of 5x5 identical reception sensors excited by a surrounding emission coil is proposed. The analysis follows the way in which one or more linear fatigue cracks that intersect can affect the eddy current answers and the electromotive force induced in the reception coils. The study of the dependence of the field distribution on the number and position of the reception coils against the discontinuity was carried out using FDTD. Spatial resolution has been improved using a known super resolution algorithm. The 2D structure was tested for the detection of subsurface discontinuities induced in Al2024 samples subjected to cyclic loading.

1. Introduction
The aluminum’s lightweight, strength, and high resistance to corrosion has been demonstrated since the man's first attempt to fly [1]. Also, the aluminum has been chosen for the cylinder block and other engine parts the first airship of Wright brothers, using an aluminum alloy which had been heat-strengthened, a discovery that positioned aluminum’s dominance in aerospace engineering [2].

Nowadays, Aluminum alloys take the first place in nonferrous materials as both production and usage.

By the year 2025, the global demand will be 80 million metric tons, so, the aerospace industry is increasingly looking at recycled alloys and new types of Al alloys are developed for the structure of aircrafts. Aluminum alloys have good machinability and surface finish capabilities, a high strength material of adequate workability.

The return of aluminum in the “lights of stage” is due to its possible combination with rare earths elements that improve the physical and chemical properties.

The phase composition and phase transformations during solidification and thermal treatments are still hard to follows for aluminum alloys [3,4]. Numerous phase diagrams were developed till now [5], but for multicomponent alloys system they are difficult to be found. Because aluminum alloys are the most used material for structures in aerospace and automotive industry, their behavior before and after production must be determined [6]. Critical structures, such as airframes, wings, need quality control
and careful maintenance [7] in order to avoid fatigue cracks leading to structural failure. The occurring of dislocations ordering leads to cyclic plastic deformation location and further to fatigue cracks appearing. The microstructure drives this process and is connected to distribution and displacing of dislocations. Al–Si–Mg type 2024 alloy is widely used in aircraft structural applications due to their moderate strength, lightweight, wear resistance, and good corrosion resistance [8]. In aircrafts, the parts are joined by rivets and bolts. During functioning of the structure, due to vibration, surface damage and cracking at the contact interface can occurs [9]. Under the cyclic loading, it leads to unexpected failure due to fatigue. The cracks are due to plastic deformation (hole expansion around fasteners or rivets).

Multiple testing methods have proven their effectiveness in the detection of different defects and damages in Al alloy structures. The most used are based on ultrasonic C-scan inspections but without the sizing ability for different crack depth to sample thickness ratios [10], thermoelastic stress analysis (TSA), acoustic emission (AE) with aim to detect the growth of small cracks [11], digital image correlation (DIC), electronic speckle pattern interferometry (ESPI), electrical resistance and strain gauges described in [12], as different destructive methods to measure damage defined as the effective surfacic density of micro-cracks. Electromagnetic methods using different type of sensors were suggested for detection of corrosion beneath (including material loss) [13] and moisture within paint coatings on aircraft aluminum alloys [14]. New advances in eddy current sensors provide the detection superficial flaws with more accuracy, in [15] being presented a new type of eddy currents sensor, and specific electronics for automated mechanized scanning and analysis software. For ideal cracks placed on surface or subsurface, using eddy current method, requires only knowledge of the crack's depth. Generally, pulsed methods are also able of probing deeper into the material than the conventional eddy current methods [9], but the signals in pulsed methods are recorded in the time domain and not on an impedance plane diagram [16].

The dimensions of the aluminum alloy parts (rivets, nuts, bolts), as well as the places where these are used in aircrafts, made that the testing methods shall use miniaturized sensors or arrays of sensors in order to improve the resolution of testing and to reduce the signal post processing time.

The paper presents a 2D architecture in configuration of 5x5 identical reception sensors in order to detect and characterize fatigue cracks into slab of Al–Si–Mg alloy usually used in aircraft components. The array allows the rapid measurements of the studied samples and signal post processing is carried out using a superresolution algorithm in order to increase the spatial resolution.

2. Studied samples

Samples were machined from a thick sheet of Al 2024 alloy with chemical composition according to [17], in the shape of dog bone for tensile testing (Figure 1).

![Figure 1. Studied samples: a) for ultrasound measuring; b) for fatigue testing.](image)

The alloy take part from series Al2024, Si and Mg providing substantial increases in strength, facilitates precipitation hardening, reduce ductility and corrosion resistance [18].

The elastic properties of the sample’s elastic modulus E, Shear modulus G and Poisson ratio ν were determined by ultrasound pitch-catch procedure [19], measuring longitudinal $C_L$ and transversal $C_T$ velocities in different points on the both faces of the samples (Table 1).
Table 1. Studied samples characteristics determined by ultrasound measurements [19]

| Sample | $\rho$ [g/cm$^3$] | $C_L$ [m/s] | $C_T$ [m/s] | $\nu$ | $E$ [GPa] | $G$ [GPa] |
|--------|-----------------|-----------|-----------|------|---------|---------|
| Al 1   | 2.772           | 7657      | 2775      | 0.33 | 74.21   | 21.24   |
| Al 2   | 2.778           | 7516      | 2867      | 0.33 | 71.34   | 22.8    |

The emission ultrasound sensor is applied on a face of the sample over a Perspex® delay line with 20 mm height. A G5KB GE sensor (General Electric Measurement & Control, USA) with a central frequency of 5 MHz is been used for the measurement of the longitudinal ultrasound velocity. For the transversal velocity, a MB4Y GE sensor is used, with a central frequency of 4 MHz. The emission impulses are delivered by a PR 5077 Square Wave Pulser Receiver Panametrics which also receive the measured signal, amplifies and forward it to digital oscilloscope for reading and acquiring (Figure 2).

Figure 2. Ultrasound measurement set-up

Fatigue tests have been performed according to standard ASTM B646 – Fracture toughness testing of aluminum alloys [20] by using the system for the analysis of the fatigue behavior of the structures, Series 1451, K22305 (manufacturer Walter & Bai – Switzerland) at Transylvania University of Brasov, under cyclic loading using a test frequency of 2 Hz at room temperature. The amplitude of loading was 150MPa determined by strain gauge according to [20], until the fatigue cracks appears opened at the surface detected by a camera that records the crack evolution over time. Once the crack has appeared, the residual fatigue life can be determined according to Paris’s law [21, 22]

$$\frac{da}{DN} = C(\Delta K)^m$$

where $N$ are the cycles number, $C=1.1\times10^{10}$ and $m=2.589$ are materials constants obtained at fatigue testing, $\Delta K$ is the amplitude of stress intensity factor, thus $N = \int_0^{a_c} \frac{1}{C(\Delta K)^m} da$, $a_0$ is the initial length of the crack and $a_c$ is the critical length.

3. 2D architecture of sensors
The experience gained in the construction and testing of linear eddy current sensor used for emphasizing the surface discontinuities in conductive materials [23, 24] leads to development of a 2D sensors able to detect and locate the flaws with a minimum of steps in scanning the inspected surfaces.

Consider a 2D structure of sensors array [25] with one rectangular emission coil placed parallel with the surface to be inspected, driven by an alternative current that assures the electromagnetic field scattered into conductive material.

The geometry has been simulated stating from the Green dyadic functions and the methods of integral volume [26]. The architecture has been designed as configurable, able to interrogate also only few reception coils by programming the data acquisition board. The 5x5 identical reception coils form...
an array, each line can work independently [27], and can be simultaneous interrogated by a multiplexer (figure 3).

![Figure 3. Scheme of the sensors array.](image)

The reception coils have inner and outer diameters 2r_i = 0.64mm and respective 2r_e = 0.8mm, 2mm height and 20turns. A multiplexing internal system reduces the mutual inductance and calculates the effective time for interrogation of the coils. The reception coils detect the field created by the emission coil and scattered by the discontinuities from the sample, the system measuring the recaptioned signals both in amplitude and phase.

4. Modeling and simulation of array behavior

Finite-difference time-domain offer a solution for the sensor’s electromagnetic excitation at high frequencies. Using the system presented in Figure 3, using XFDTD software, the behavior of the architecture has been simulated. The FDTD algorithm is used as instrument for numerical evaluation in space and time of induced currents into Al2024 specimen. FDTD finds approximate solutions of Maxwell equations in differential forms, the discretization using the central difference through 30 approximations to the space and time partial derivatives. The equations are implemented in the software and solved in a cyclic manner: the electric field vector components in a volume of space are solved in time, the magnetic field vector components in the same spatial volume are successively solved. The process is repeated until the desired EM field state as transient or steady-state is fulfilled. Using the Fourier transform, the FDTD method covers a range of frequency in a single simulation.

The field decrease exponential in time inside the material, being scattered by the discontinuity. Thus, a gradient along z axis will appear, allowing the identification of electric/magnetic field location of the peaks, corresponding to the position of discontinuity under the reception coils. Using FDTD for analysis of array layout, it is possible to test the design data implemented in simulation as well as the eventually improvement of geometrical elements and the performance of the axial gradient system taking into consideration the electromagnetic fields obtained in modelling. FDTD has been used at low frequency of the electric and magnetic field generated by the architecture presented in Figure 3. The discretization of the computational problem is given by ∆x, ∆y, ∆z and corresponding, the permittivity, the permeability and the conductivity defined in the center of the Yee cell [28].

The Yee’s cell represents is the building block of the FDTD method [29], where the electric and magnetic fields are defined at discrete points, each electric field component is located a half-cell width from the origin. Using the same coordinate system as for the array design, the fields are manifesting in the center of each coil in the array. The scanning of the surface is made in “leap-frog” style, the step being equal with the width of the array. A current source represented by the emission coil creates the excitation field, being scattered into the sample, and the intensity was 0.1A at 130kHz frequency.

The differences of the electric and magnetic field amplitudes received by the array in the presence of the sample with fatigue crack are presented in Figure 4. The amplitudes of the fields are different for each location of the coils in the array and is in function of the location of discontinuity under certain coils, the amplitude being reduced at a distance larger than 3 times the minimum distance between the coils.
The FDTD method allows the calculation of electromagnetic field generated into a small space, impossible to be carried out with analytical methods. The perfect matched layers boundary conditions in FDTD simulation allow a high accuracy of the results. Despite the fact that there are 5x5 coils, the interaction of each can be represented as a transfer of energy towards free space. The electromagnetic waves have a good distribution, each responding separately when each coil has a certain position toward the inspected surface. Also, the simulation allows the better choice of the architecture’s sensors dimensions and layout to improve array’s resolution.

5. Signal processing scheme

For the start the reception coils was considered that form a linear array and is used for scanning over the fatigue crack. Using the direction of propagation method, the resolution of the sensors is improved [Error! Bookmark not defined.30]. The reception signals can be written as a vector

\[ x_i = a_i e^{j \psi_i}, \quad i = 1, \ldots, M \]

(2)

where \( M \) is the number of reception coils, \( a_1 \ldots a_M \) and \( \psi_1 \ldots \psi_M \) are the amplitudes and phases of induced electromotive force for each element, and \( j \) is the unit imaginary number.

In order to locate discontinuities, the array manifold should be free of ambiguity [31]. Thus, the system won’t be able to discern between two discontinuities placed at different distance that give the same response, emphasizing them as only one discontinuity. For one discontinuity, first rank ambiguity can appear [30]. The first rank ambiguity can be avoided by a weighting vector \( w \), which linear combines the output signal from the sensor array into single output signal \( y \)[32]

\[ y = xw^H \]

(3)

where superscript \( H \) denotes the Hermitic [i.e., conjugate-transpose] operation and the sensitivity distribution of a sensor array must be a cosine function. Thus, the maximum sensitivity occurs at the center of the array while on the boundary this is null. Each coil has been sampled in 12 intervals. The sensitivity at the center depends on the amplitude and phase of the current circulating in the emission coil when the array is placed over a good region. The power of a signal received by the array is proportional to the

\[ P \sim |y|^2 \]

(4)

and the normalized response array [NRA] is defined as

\[ \text{NRA}[\text{dB}] = 10 \log_{10} \frac{P - P_0}{P_0} \]

(5)
where $P_0$ is the power at a reference point

$$P_0 \sim |y_0|^2$$

and $y_0$ is the reference output array signal measured from a defect-free region. The normalized response array can be used to estimate the location of discontinuities. Figure 5 presents the amplitude and the phase of the signal received by the linear eddy current sensors at the scanning over a notch, when the notch is found by the coil #3 and #4 from the array.

It can be shown that the presence of a notch under a specific coil can be emphasized. The signal processing scheme can be adapted to a sensor array by modelling the operation with dyadic Green’s functions and obtaining the weight vector for different positions of the notch under specific reception coils from the array [25].

### 6. Experimental results

The experimental set-up is presented in Figure 6. The incident magnetic field is assured by an emission coil, a rectangular frame with 6x6mm sides, having 100 turns. The emission coil is fed by a function generator WW1074 Tabor Ltd. The signal is amplified by Power amplifier RF A1012 AG-T&C Power Conversion Inc. The reception coils are connected to a multiplexor, which significantly increases the number of sensors that can be measured by a datalogger, improving also the scanning time.

The output signal is amplified, the reference signal being in the same phase with the input current into the emission coil. The amplifier delivers both the amplitude and the phase of the induced electromotive force [33]. The interrogation of reception coils is correlated with the scanning steps and speed, in order to have enough time for the temporary buffer to be emptied. The received signal is forwarded to the PC. The displacement system, the emission system and the reception part are controlled by codes developed in Matlab. The sample is displaced under the fixed sensor array with a XY scanning system, Newmark USA.

The electromagnetic image of the scanned surface has been obtained by postprocessing of the signals acquired by each coil in each scanning point, using a sub encoding reconstruction algorithm and multiple coil scheme [34]. The image reconstruction starts at the first scanning step with the set of
received signals using a low number of phase-encoding gradient steps. Applying Fourier transforms, aliased component images are obtained. Now, the signals are processed as images taking into account that each pixel in an aliased image is a superposition of multiple pixels [35, 36].

Figure 7 presents the response of sensors array at the scanning of studied sample, after signal post processing. It can be shown the presence of the crack under reception coils 3.3 and 3.4 (middle row).

![Figure 7](image_url)

**Figure 7.** The response of the sensor array at the scanning over the fatigue crack in the sample

The length of a crack is evaluated upon the largest signals delivered by the reception coils at the crack’s edge, meaning that the crack is directly evaluated from the spatial distance between the centers of two reception coils whose signals are clearly maximal. Initial results of applying the algorithm to the array data allows the localization of the fatigue cracks.

7. **Conclusions**

The paper presents a new type of electromagnetic sensors array, emission reception type. The model and the simulation of the 2D architecture are developed in order to extract the characteristic signal due to the presence of discontinuities under the surface of the studied specimen. The study of the dependence of the field distribution on the number and position of the reception coils against the discontinuity was carried out using FDTD. The 2D architecture has been designed and experimental test have been carried out in order to verify the possibility to obtain the distinct answer of each reception coil to a certain position of the discontinuity. The presented results show that the electromagnetic signal obtained by simulation coincides with the experimental one, suggesting that the 2D structure can assure the scan in leapfrog step of the surface with small dimensions, précising the location of the discontinuity. Further tests will be complete after more loading cycles by complementary methods as acoustic emission and validated by destructive tests.

8. **References**

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