Research on cluster overlap and non-overlap region for 5G-IoV networks with NOMA

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\textbf{Abstract}

As a multi hop self-organizing network, wireless sensor network has the ability to cooperatively sense, collect and process the information of the sensed objects. The applications of WCN in 5G-based Internet of Vehicles (5G-IoV), using information fusion and intelligent information processing technologies, can obtain more reliable and accurate detection parameters, which has been widely concerned. However, the massive connectivity and information exchange in 5G-IoV pose great challenges to the bandwidth efficiency. In order to overcome these issues in 5G-IoV networks, a performance enhanced scheme based on non-orthogonal multiple access (NOMA) is proposed. In the proposed scheme, different vehicle locations are respectively discussed, i.e., whether in the overlap region of cluster head vehicles (CHVs). In particular, different to conventional works, each receiving node only decodes the desired signal to avoid performance loss provided from the poor channel quality limitation. On the other hand, all CHVs decode-and-forward new superposition coded signals with new power allocation factors, while that the maximum ratio combining is utilized at receivers to further improve the ergodic sum-rate (SR) and probability of conflict. The closed-form expressions of ergodic SR for our proposed scheme are analyzed under the independent Rayleigh fading channels. Numerical results corroborating our theoretical analysis show that the superposition coded signal transmission scheme applied to the proposed NOMA-IoV improves the ergodic SR performance significantly compared with the existing works, especially for the high signal-to-noise region.

\textbf{Keywords:} Wireless sensor network (WSN), Non-orthogonal multiple access (NOMA), 5G-Internet of Vehicles (IoV), Ergodic sum-rate, Cluster overlap region

\section{Introduction}

In recent years, traffic safety, travel efficiency, environmental protection and other issues caused by the growing number of cars have become particularly prominent, which results in the research and development of related fields of Internet of Vehicles (IoVs) concerning \cite{1, 2}. The IoV is based on the intranet and mobile Internet, which integrates the Global Position System (GPS), sensors, radio frequency identification (RFID), data mining, automatic control and other related technologies \cite{3}. According to the agreed architecture, communication protocol and data interaction standard, it is in the process of the vehicle-X(X: vehicle, road, pedestrian, Internet) interaction to realize the integrated network of intelligent traffic management, intelligent dynamic information...
service and vehicle intelligent control. Moreover, the IoV is a typical application of the Internet of Things (IoT) [4] technology in the field of transportation system with the core as Vehicle to Everything (V2X) wireless communication technology [5, 6]. With the help of V2X wireless communication technology, IoVs can not only break through the technical bottleneck of single vehicle in intelligent development, but also intuitively improve the intelligent level and automatic driving ability of the Internet connected vehicles [7]. In particular, V2X provides the traffic efficiency enhancement, driving experience improvement, the new business form of the intelligent and comfortable, safe, energy-saving and efficient comprehensive services. In addition, the mainstream technology of V2X communication includes Dedicated Short Range Communication (DSRC) technology [8], and Cellular V2X (C-V2X) technology based on the cellular mobile communication system. Currently, the C-V2X technology is mainly based on LTE-V2X technology [9–11], which evolves to the 5th generation mobile communication (5G)-based V2X technology in the future. Specifically, the vehicle clustering has been utilized to reduce the complexity of V2X communications that would ultimately improve road traffic efficiency.

On the other hand, with the rapid development of 5G, in the face of the explosive growth of network demands in the future wireless communications, 5G mobile network considers the wireless transmission technologies that can further explore the potential of spectrum efficiency improvement, i.e., large-scale antenna technology, millimeter wave communication, ultra-density network, non-orthogonal multiple access, etc. [12]. In order to meet the massive access and ultra-high capacity demands of 5G network, non-orthogonal multiple access (NOMA) [13, 14] technology is considered as the most critical technology in the next generation of mobile communication. Based on the multi-user information theory, NOMA technology can further improve the number of users’ connections by introducing new dimensions such as power and code domains with the existing physical resources, providing more channel capacity than the conventional orthogonal multiple access (OMA) [15–17].

It is known that NOMA technology can not only meet the requirements of higher spectrum efficiency, but also satisfy the user fairness condition. Therefore, it is serving as a potential technology for the future beyond 5G (5GB) and the 6th generation wireless communication (6G) system [18, 19]. Therefore, the combination of NOMA technology in vehicle network enables multiple vehicles to transmit information by sharing the same channel simultaneously, thus alleviating resource conflicts such as limited transmission capacity and unpredictable transmission delay in 5G-V2X communications. The basic idea of NOMA is to use non-orthogonal transmission at the transmitter, introduce interference information actively and realize correct demodulation at the receiver via the successive interference cancellation (SIC). Even that the receiver using SIC technology is more complex, it can achieve a higher spectrum efficiency. In fact, the core idea of NOMA technology is to increase spectrum efficiency at the acceptable cost of receiver complexity [20]. With the in-depth study of 5G and continuous improvement of chip processing capacity, the processing complexity of the receiver has significantly improved, which leads to that NOMA technology inevitably becomes a hot topic in academia.

With above observations, in this paper, NOMA is introduced to the 5G-IoV networks with two adjacent cluster head vehicles (CHVs) to satisfy the spectrum efficiency and
massive connectivities requirements. Particularly, since the overall performance of the system is limited by the poor channel [21], at the CHVs, only the desired signals for the vehicles will be decoded and forwarded. We further discuss the effects of different vehicle locations: (1) the vehicle is in the overlap region of the CHVs; (2) the vehicle is not in the overlap region of the CHVs, which means that multiple CHVs can support the service or not. For our proposed NOMA-IoV networks, all the CHVs will forward the new superposition coded signals to the vehicles in the served region to further improve the ergodic sum-rate (SR) of the system. These motivate us to investigate the proposed NOMA-IoV system with multiple CHVs. The following are the key contributions of this paper:

- In order to further improve the ergodic SR, we comprehensively investigate the NOMA-IoV networks with two CHVs. Different to the conventional NOMA scheme, after receptions, the CHVs only decode-and-forward (DF) the desired signals to the vehicles, in the meanwhile, the maximum ratio combining (MRC) is also utilized to improve the performance. To the best of our knowledge, combining NOMA-V2X networks with overlap region discussion has not been considered so far, which is more general and challenging.
- The closed-form solutions of the ergodic SR for the proposed schemes at the high transmit signal-to-noise ratio (SNR) region are derived with a negligible performance loss. It is worth noting that, there are few works that focus on the 2-stage superposed transmission for multiple CHVs NOMA-V2X networks, since it is hard to obtain the exact expression of the ergodic SR. Furthermore, the theoretical results are shown to highly agree with the simulation results, especially in the high SNR region.
- By means of numerical results, both analytically and numerically, we compare the proposed NOMA-IoV schemes with the TDMA scheme in terms of ergodic SR. It is shown that the proposed NOMA-IoV with the overlap region service scheme outperforms the TDMA and existing NOMA schemes significantly.

The rest of this paper is organized as follows. Related work is first introduced in Sect. 2. In Sect. 3, we present the proposed model and corresponding problems. The performance of proposed NOMA-IoV in terms of the ergodic SR is analyzed in Sect. 4 including the overlap, non-overlap and conventional NOMA schemes. Section 5 contains the system simulation conditions and results. This paper is concluded in Sect. 6.

2 Related work
In recent years, adopting NOMA in vehicle network has became a popular research hot-spot. In [22], the author studied the potential capacity of NOMA in the V2X scenario and difficulties in the next generation communication. From the unicast system, a spectrum resource allocation scheme based on NOMA is proposed, which is extended to the broadcast system. Based on this, the authors in [23] investigate the key problems of interference management and handover in 5G vehicle communication system with NOMA. Moreover, in order to improve the spectrum efficiency of 5G vehicle communication system based on NOMA and adapt to traffic load conditions and high mobility, a hierarchical power control scheme is proposed to realize joint optimization of cell
correlation and power control. In [24], the power allocation of heterogeneous vehicle communication with NOMA under non-ideal channel estimation is studied, where the influence of channel estimation error caused by high mobility in vehicle communication on the realization of effective power distribution and link reliability is demonstrated. In addition, a NOMA-V2X network with spatial multiplexing permission is proposed in [25], which can be efficiently solved by a constructed interference hypergraph. However, the interference model in [25] only considers whether the interference exceeds a fixed threshold and ignores the impact of the interference level, which is difficult to reflect the real interference environment. It is known that, due to the real-time change of road traffic, the vehicle network is dynamic leading to the problem of network topology instability. According to this, in [26], a clustering method is proposed to make the network topology hierarchical and scalable by establishing the connectivity graph between the nodes of the vehicle network. To support data distribution and reduce the complexity of end-to-end (E2E) communication through the cluster head node, the authors in [27] investigate an efficient cluster selection scheme. This clustering method has been widely used in V2X communication to improve the performance of vehicle network [28, 29]. Since that the expansion of vehicle network leads to a huge increase in energy consumption, the power control is an effective way to reduce power consumption without reducing the connectivity and coverage of vehicle networks [30]. In order to balance the power allocation among the cluster heads and further improve the throughput of the downlink, the power control method is used in V2X communication. On the other hand, as mentioned above, NOMA has developed power domain multiplexing to meet the requirements of a higher overload transmission [22]. Based on this, some researchers have studied the power control scheme in 5G-IoV communication with NOMA [23, 31].

Clearly, the above discussed researches show that NOMA-enabled V2X communication will be a trend in the future, for its potential to improve spectrum efficiency, and the ability for the effective resource management. However, the interference management problems in the NOMA-aided vehicle communication scenario still need to be excavated, i.e., how to use vehicle clustering to reduce the complexity of V2X communication effectively to improve road traffic efficiency; how to balance the power allocation between CHVs; how to improve the downlink throughput with NOMA power control method. One can conclude that this will be a new and meaningful research direction to propose effective solutions to the above problems to improve the system performance.

### 3 Methods

In this paper, we focus on the downlink transfer scheme for NOMA-IoV system involving one base station (BS), two cluster head vehicles and three vehicles as shown in Fig. 1, where all the nodes are equipped with a single antenna with perfect channel state information (CSI) and half duplex transmission protocol. Two kinds of vehicles locations are considered, i.e., one is that the vehicle (V1) is located in the overlap region of two CHVs, the other is that the vehicle (V1) is not located in the overlap region. The other vehicles can only receive the signals from the corresponding CHVs. Let $h_{\mu}$, for $\mu \in \{B_1, B_2, (v_1, U_1), (v_1, U_2), (v_2, U_1), (v_2, U_3)\}$, denote the independent Rayleigh fading channels from the BS to CHV1 and CHV2, from CHV1 to V1 and V2, and from CHV2 to V1 and V3, with the average powers as $\alpha_{B_1}, \alpha_{B_2}, \alpha_{v_1, U_1}, \alpha_{v_1, U_2}, \alpha_{v_2, U_1}, \alpha_{v_2, U_2}$. 
\( \alpha \nu_2, \Upsilon_1 \) and \( \alpha \nu_2, \Upsilon_3 \), respectively. We further assume that the two CHVs not only represent power domain differences between users, but also facilitate collaborative NOMA analysis and deployment. Therefore, the power distribution of two CHVs is sufficient to illustrate the key aspects of power distribution between vehicles, while avoiding unnecessary complications. Note that although we limit ourselves to two CHVs, the proposed approach can be easily extended to a multi-CHVs scenarios. It is also considered that the decode-and-forward (DF) scheme is adopted at each CHV.

It is worth noting that, due to the dense topology of the IoV network, when multiple CHVs (i.e., CHV1 and CHV2) are assigned the same time-frequency resource, those vehicle located in the overlap region of two adjacent CHVs has serious conflicts. In the traditional OMA case, a conflicting vehicle is likely to be unable to decode multiple CHV signals due to severe interference, resulting in additional retransmission delays. In order to reduce the probability of conflict and transmission delay, and consider the non-orthogonal allocation of wireless resources, a sub-channel can be simultaneously occupied by multiple CHVs. The data rate of the CHV-vehicle link can be increased compared to OMA schemes, and the vehicle for each collision is more likely to decode the received superposition coded signals using SIC technology. This can reduce the data conflicts and increase the number of users supported by the system.

With above descriptions, the superposition coded signal sent by the BS to these two CHVs can be denoted as

\[
S = \sqrt{a_1} P_B x_1 + \sqrt{a_2} P_B x_2 + \sqrt{a_3} P_B x_3, \tag{1}
\]

where \( a_i \), for \( i \in \{1, 2, 3\} \), is the power allocation coefficient with \( a_1 > a_2 > a_3 \) and \( \sum_3 a_i = 1 \), and \( x_i \) is intended for the transmitted NOMA information at the BS satisfied \( E[|x_i|^2] = 1 \). Moreover, we clarify that all the power allocation factors used in this paper are nonnegative. In our proposed scheme, each transmission involves two time slots. At the first time slot, the BS transmits the NOMA signal \( S \) to CHVs, therefore, the received signals at CHV1 and CHV2 are respectively given by

\[
y_{B_1}^{(1)} = h_{B_1} S + n_1, \tag{2}
\]

and
where $h_{Bi}$, for $i = \{1, 2\}$, is the Rayleigh fading channel coefficient from BS to $i$-th CHV following the complex Gaussian distribution with the mean of zero and the variance of $\sigma_{Bi}^2$, i.e., $h_{Bi} \sim CN(0, \sigma_{Bi}^2)$, and $n_1$ and $n_2$ are the AWGN with variance $N_0$ at CHV1 and CHV2, respectively. After receptions, CHVs will immediately decode the received superposition signal following the NOMA decoding principle, i.e., decode the symbol with higher power allocation factor first by treating the one with lower power allocation, and then cancel it to decode another one. Therefore, the received SINR for $x_1$ can be obtained from

$$\gamma_{Bj}^{(x_1)} = \frac{|h_{Bj}|^2 a_1 \rho}{|h_{Bj}|^2 (a_2 + a_3) \rho + 1},$$

for $j \in \{1, 2\}$, where $\rho = \frac{P_B}{N_0}$ denotes the transmit SNR at the BS. It is clear that the desired signals for the users in CHV1 served region are $\{x_1, x_2\}$, while that the desired signals for the users in CHV2 served region are $\{x_1, x_3\}$. In this assumption, we consider that CHV1 will only decode $\{x_1, x_2\}$, and CHV2 will decode $\{x_1, x_2, x_3\}$ following NOMA decoding principle with the received SNRs for $x_2$ and $x_3$ as

$$\gamma_{B1}^{(x_2)} = \frac{|h_{B1}|^2 a_2 \rho}{|h_{B1}|^2 a_3 \rho + 1},$$

and

$$\gamma_{B2}^{(x_3)} = \frac{|h_{B2}|^2 a_2 \rho}{|h_{B2}|^2 a_3 \rho + 1}, \quad \gamma_{B2}^{(x_3)} = |h_{B2}|^2 a_3 \rho.$$

It worth noting that, only decode the desired signals in CHVs is resealable and practical. Because of that, on one hand the undesired signals will not be forwarded to the vehicles, on the other hand, it may limit the system performance due to the overall performance is restricted by the poor channel coefficient. During the second time slot, CHVs forward new superposition coded signals to the users in the corresponding served region. For simplicity, we assume that the signal $\sqrt{b_1} x_1 + \sqrt{b_2} x_2$ will be forwarded by CHV1 with $b_1 + b_2 = 1$, and $\sqrt{c_1} x_1 + \sqrt{c_2} x_3$ will be forwarded by CHV2 with $c_1 + c_2 = 1$, where $b_i$ and $c_i$, for $i \in \{1, 2\}$, are new power allocation factors. In this time slot, without loss of generality, there are two kinds of situations that are: 1) V1 is in the overlap region, 2) V1 is not in the overlap region. In following subsections, we will discuss these two situations in details for a better readability.

### 3.1 Overlap case

In this case, the V1 is in the overlap region, leading to that it will receive two superposition coded signals from both of CHV1 and CHV2. And hence, the received signals at V1 can be written as

$$y_{B1}^{(1)} = h_{B1} S + n_1,$$

5
\[
\gamma_{dl}^{(V1)} = \left( b_1 h_{v_1,u1} + \sqrt{c_1 h_{v_2,u1}} \right) \sqrt{P_C x_1} + \sqrt{b_2 P_C h_{v_1,u1} x_2} + \sqrt{c_2 P_C h_{v_2,u1} x_3} + n_{u1},
\]

(7)

where \( P_C \) is the transmit power at CHV1 and CHV2, while \( n_{u1} \) is the AWGN at V1. We further consider that MRC is adopted as V1 to further improve the system performance, therefore, the effective received SNRs for \( x_1, x_2 \) and \( x_3 \) can be respectively presented as

\[
\gamma_{V1}^{(x_1)} = \frac{|h_{v_1,u1}|^2 b_1 \rho}{|h_{v1,u1}|^2 b_2 \rho + 1} + \frac{|h_{v2,u1}|^2 c_1 \rho}{|h_{v2,u1}|^2 c_2 \rho + 1},
\]

(8)

\[
\gamma_{V1}^{(x_2)} = |h_{v1,u1}|^2 b_2 \rho \quad \text{and} \quad \gamma_{V1}^{(x_3)} = |h_{v2,u1}|^2 c_2 \rho,
\]

(9)

where \( \rho = \frac{P_C}{b_0} \). From Eq. (10), it is easy to see that, if the channels \( h_{v1,u1} \) and \( h_{v2,u1} \) are very weak, that may results in a serious performance limitation when calculating ergodic SR. Therefore, in our proposed scheme, the SIC is only used to decode the desired signal, i.e., only decode \( x_1 \). In the meanwhile that, the received signals at V2 and V3 are given as

\[
\gamma_{dl}^{(V2)} = \sqrt{b_1 P_C h_{v_1,u2} x_1} + \sqrt{b_2 P_C h_{v_1,u2} x_2} + n_{u2},
\]

(10)

with the corresponding received SNRs for \( x_1 \) and \( x_2 \) as

\[
\gamma_{V2}^{(x_1)} = \frac{|h_{v1,u2}|^2 b_1 \rho}{|h_{v1,u2}|^2 b_2 \rho + 1}
\]

and

\[
\gamma_{V2}^{(x_2)} = |h_{v1,u2}|^2 b_2 \rho,
\]

(11)

with the corresponding received SNRs for \( x_1 \) and \( x_3 \) as

\[
\gamma_{V3}^{(x_1)} = \frac{|h_{v2,u3}|^2 c_1 \rho}{|h_{v2,u3}|^2 c_2 \rho + 1}
\]

and

\[
\gamma_{V3}^{(x_3)} = |h_{v2,u3}|^2 c_2 \rho,
\]

where \( n_{u_i} \), for \( i \in \{1, 2\} \), denotes the AWGN at \( V_i \). Remarkably, even that \( x_1 \) is not the desired signal for V2 and V3, however, in order to strictly follow the NOMA decoding principle, \( x_2 \) and \( x_3 \) should be decoded after \( x_1 \) decoded by adopting SIC. With above observations, the overall effective received SNRs for \( x_1, x_2 \) and \( x_3 \) in our proposed overlap system can be respectively written as

\[
\gamma^{(x_1)} = \min \left( \gamma_{B_1}^{(x_1)}, \gamma_{B_2}^{(x_1)}, \gamma_{V1}^{(x_1)}, \gamma_{V2}^{(x_1)}, \gamma_{V3}^{(x_1)} \right),
\]

\[
\gamma^{(x_2)} = \min \left( \gamma_{B_1}^{(x_2)}, \gamma_{B_2}^{(x_2)}, \gamma_{V2}^{(x_2)} \right),
\]

\[
\gamma^{(x_3)} = \min \left( \gamma_{B_2}^{(x_3)}, \gamma_{V3}^{(x_3)} \right).
\]

### 3.2 Non-overlap case

In this case, we assume that V1 is in the CHV1 serviceable region, and out of service from CHV2. Since the receptions for CHV1, CHV2, V2 and V3 are similar to the ones in overlap situation, we omit them. In this manner, it will only receive the signal transmitted from CHV1 as:

\[
\gamma_{\text{non}}^{(V1)} = \sqrt{b_1 h_{v_1,u1} \sqrt{P_C x_1} + \sqrt{c_2 P_C h_{v_2,u1} x_2} + n_{u1}},
\]

(12)

with the corresponding received SNRs for \( x_1 \) and \( x_2 \) as
\[ \xi^{(x_1)}_{V1} = \frac{|h_{V1, U1}|^2 b_1 \rho}{|h_{V1, U1}|^2 b_2 \rho + 1}, \]  

(13)

and

\[ \xi^{(x_2)}_{V1} = |h_{V1, U1}|^2 b_2 \rho. \]  

(14)

Similar to the overlap case, \( x_2 \) will not be decoded. Therefore, the overall effective received SNRs for \( x_1, x_2 \) and \( x_3 \) in the non-overlap system can be respectively written as

\[ \xi^{(x_1)} = \min \left( \frac{1}{\xi^{(x_1)}_{V1}}, \frac{1}{\xi^{(x_1)}_{V2}}, \frac{1}{\xi^{(x_1)}_{V3}} \right), \]

\[ \xi^{(x_2)} = \gamma^{(x_2)} \quad \text{and} \quad \xi^{(x_3)} = \gamma^{(x_3)}. \]

In conventional NOMA scheme, after receptions, all the CHVs will immediately decode the received signals, i.e., \( x_1, x_2 \) and \( x_3 \), and then forward the signals to vehicles. On the other hand, the V1 and V2 will also decode the all received signals.

4 Ergodic sum-rate analysis for the proposed NOMA-IoV networks

In this section, the overall performance of the ergodic SR and outage probability for our proposed NOMA-IoV networks are analyzed to show the advantages of our proposed schemes, where the V1 are with different locations, i.e., in the overlap region and non-overlap region.

4.1 Overlap case

Letting \( \beta_{\mu} = |h_{\mu}|^2 \) for \( \mu \in \{B_1, B_2, (v_1, U_1), (v_2, U_1), (v_2, U_2)\} \), we have

\[ \mathcal{X} = \min \left( \frac{\beta_{B_1} a_1 \rho}{2 \beta_{B_1} a_2 \rho + 1}, \frac{\beta_{B_2} a_1 \rho}{2 \beta_{B_2} a_2 \rho + 1}, \frac{\beta_{V1, U1} b_1 \rho}{2 \beta_{V1, U1} b_2 \rho + 1}, \frac{\beta_{V2, U1} c_1 \rho}{2 \beta_{V2, U1} c_2 \rho + 1}, \frac{\beta_{V1, U2} b_1 \rho}{2 \beta_{V1, U2} b_2 \rho + 1}, \frac{\beta_{V2, U2} b_1 \rho}{2 \beta_{V2, U2} b_2 \rho + 1} \right). \]

(15)

Based on above equation, the complementary cumulative distribution function (CCDF) of \( \mathcal{X} \) can be obtained from

\[ T_{\mathcal{X}}(x) = \Pr \left\{ \frac{\beta_{B_1} a_1 \rho}{\beta_{B_1} (a_2 + a_3) \rho + 1} > x, \frac{\beta_{B_2} a_1 \rho}{\beta_{B_2} (a_2 + a_3) \rho + 1} > x, \frac{\beta_{V1, U1} b_1 \rho}{\beta_{V1, U1} b_2 \rho + 1} > x, \frac{\beta_{V2, U1} c_1 \rho}{\beta_{V2, U1} c_2 \rho + 1} > x \right\}. \]

(17)

Noting that the CCDF of \( \beta_{\mu} = e^{-\frac{x}{\mu}} \), when \( x < \min \left\{ \frac{a_1}{a_2 + a_3}, \frac{b_1}{b_2} \right\} \), (17) can be approximately represented as

\[ T_{\mathcal{X}}(x) \approx T_{B_1} \left( \frac{x}{(a_1 - (a_2 + a_3)x) \rho} \right) T_{B_2} \left( \frac{x}{(a_1 - (a_2 + a_3)x) \rho} \right) T_{V1, U1} \left( \frac{x}{(b_1 - b_2 x) \rho} \right) \times T_{V2, U2} \left( \frac{x}{(b_1 - b_2 x) \rho} \right) T_{V1, U1} \left( \frac{x - c_1}{C_2 \rho} \right) \]

\[ = e^{-\frac{x}{(a_1 - (a_2 + a_3)x) \rho} - \frac{x}{(a_1 - (a_2 + a_3)x) \rho} - \frac{x}{(a_1 - (a_2 + a_3)x) \rho} - \frac{x}{(b_1 - b_2 x) \rho} - \frac{x - c_1}{C_2 \rho}}, \]

(16)
where, for the first term, we approximate \( \frac{\beta_{\nu_1} b_1 \rho}{\beta_{\nu_1} b_1 \rho + 1} + \frac{\beta_{\nu_2} c_1 \rho}{\beta_{\nu_2} c_2 \rho + 1} \approx \frac{\beta_{\nu_1} b_1 \rho}{\beta_{\nu_1} b_1 \rho + 1} + \frac{c_1}{c_2} \) by considering the high transmit SNR, since it is difficult to obtain the exact closed-form expression of \( Y_{V_1}^{(x_1)} \).

Denote \( Y = \min \left( Y_{B_1}^{(x_2)}, Y_{B_2}^{(x_2)}, Y_{V_2}^{(x_2)} \right) \), and hence the CCDF of \( Y \) for \( x_2 \) can be obtained from

\[
F_Y(y) = \Pr \left( \frac{\beta_{B_2} a_2 \rho}{\beta_{B_2} a_3 \rho + 1} > y, \frac{\beta_{B_2} a_2 \rho}{\beta_{B_2} a_3 \rho + 1} > y, \frac{\beta_{\nu_1} b_2 \rho}{\beta_{\nu_1} b_2 \rho + 1} > y \right)
\]

\[
= e^{-\frac{(\alpha_2 - \beta_2 \rho)y}{\rho_{B_2} a_2 b_2 \rho + 1} - \frac{(\alpha_2 - \beta_2 \rho)y}{\rho_{B_2} a_3 b_2 \rho + 1}}
\]

(17)

On the other hand, denoting \( Z = \min \left( Y_{B_2}^{(x_2)}, Y_{V_3}^{(x_2)} \right) \), we have the closed-form expression for \( Z \) as:

\[
F_Z(z) = \Pr \left( \frac{\beta_{B_2} a_3 \rho}{\beta_{B_2} a_3 \rho + 1} > z, \frac{\beta_{\nu_2} c_2 \rho}{\beta_{\nu_2} c_2 \rho + 1} > z \right)
\]

\[
= e^{-\frac{z}{\rho_{B_2} a_2 b_2 \rho + 1} - \frac{z}{\rho_{B_2} a_3 b_2 \rho + 1}}
\]

(18)

After introducing the equalities

\[
\int_0^\infty \log_2(1 + x) f_X(x) dx = \frac{1}{\ln 2} \int_0^\infty \frac{1 - F(x)}{1 + x} dx,
\]

(19)

and

\[
\int_0^\infty e^{-\mu x} dx = e^{\mu \beta} \left[ Ei(-\mu u - \mu \beta) - Ei(-\mu \beta) \right],
\]

(20)

[32, Eq. (3.352.1)], where \( Ei(\cdot) \) means the exponential integral function. Since that the closed-form expression of ergodic rate for \( x_1 \) is quite difficult, we focus on the high transmit SNR case, i.e., \( \rho \gg 1 \). In addition, for simplicity, we further assume that \( a_1 < b_1 \) due to that there exists three signals in \( X \) and only two in \( Y \). Therefore, when \( x < \min \left\{ \frac{a_1}{a_1 + b_1}, \frac{b_1}{a_1 + b_1} + \frac{c_1}{c_2} \right\} = \min \left\{ \frac{a_1}{1-a_1}, \frac{b_1}{1-b_1} \right\} = \frac{a_1}{1-a_1} \), the ergodic rate for \( x_1 \) in the overlap case can be respectively written as

\[
C_{ol}^{(x_1)} \approx \frac{1}{2 \ln 2} \int_0^{\frac{a_1}{1-a_1}} \frac{e^{-\frac{\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}}}}{1 + x} dx
\]

\[
\begin{cases}
\frac{1}{\ln 2} \left[ e^{\frac{\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}}} Ei \left( \frac{-\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}} \right) - e^{\frac{\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}}} Ei \left( \frac{-\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}} \right) \right], & \text{for } a_1 = b_1 \\
\frac{b_1}{\ln 2} \left[ e^{\frac{\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}}} Ei \left( \frac{-\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}} \right) - e^{\frac{\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}}} Ei \left( \frac{-\alpha_1}{\rho_{B_1} + \rho_{B_2} + \rho_{V_1}} \right) \right], & \text{for } a_1 \neq b_1
\end{cases}
\]

where \( A = \frac{A_0}{\alpha_1} + \frac{1}{\alpha_2} \) and \( B = \frac{1}{\alpha_1 \mu_1} + \frac{1}{\alpha_1 \mu_2} + \frac{1}{\alpha_2 \mu_3} \) for the case \( x > \frac{a_1}{1-a_1} \), \( C_{ol}^{(x_1)} = 0 \) always holds. For \( x_2 \), we have
where \( (22) \) follows the condition \( x < \frac{a_2}{a_3} \), otherwise \( C_{ol}^{(x_2)} = 0 \). In the meanwhile, the ergodic rate in closed form for \( x_3 \) can be obtained from

\[
C_{ol}^{(x_3)} = \frac{1}{2\ln2} e^{\frac{a_2}{\rho B_2} + a_3 \rho v_2, U_3} e^{-\frac{a_3}{\rho B_2}} b_2 \rho v_1, U_1 \left[ \text{Ei} \left( \frac{a_2}{\rho B_2} + \frac{a_3}{\rho v_1, U_1} \right) - \text{Ei} \left( \frac{a_2}{\rho B_2} + \frac{a_3}{\rho v_1, U_1} \right) \right].
\]

Finally, the ergodic SR for the proposed overlap scheme can be expressed as

\[
C_{sum,ol} = C_{ol}^{(x_1)} + C_{ol}^{(x_2)} + C_{ol}^{(x_3)}.
\]

For non-overlap case, it is clear that the analysis results for the non-overlap case will follow the received SNRs as shown in \( \xi^{(x_1)} \), \( \xi^{(x_2)} \) and \( \xi^{(x_3)} \). There is only one difference between the proposed two cases that are \( \xi^{(x_1)} \gamma^{-1} \) and \( \gamma^{(x_1)} \). Therefore, for simplicity and better readability, in the manuscript, we omitted them.

5 Results and discussion

5.1 Numerical results

In this section, we show the numerical results in terms of ergodic SR to demonstrate the performance of the proposed NOMA-IoV system. The numerical results are averaged over 100,000 channel realizations with Rayleigh fading. In following figures, we use “Simulation” to denote the simulation results, while the “Analysis” is used to presented the analytical results. The simulation set up is given as follows: \( \alpha v_1, U_1 = 1, \alpha v_1, U_2 = 10, \alpha v_2, U_1 = 1, \alpha v_2, U_2 = 10, a_1 = 0.7, a_2 = 0.2, a_3 = 0.1, b_1 = 0.7, b_2 = 0.3 \) and \( c_1 = c_2 = 0.5 \).

Figure 2 depicts the ergodic SR performance of our proposed NOMA-IoV scheme versus the transmit SNR, where two channel coefficient setups are considered: (1) \( \alpha B_1 = 1, \alpha B_2 = 10; \) (2) \( \alpha B_1 = 10, \alpha B_2 = 1 \). The motivations for these two groups depend on the effect of CHV1 and CHV2, since that the poor channel quality will limit to a significantly performance limitation. As shown in Fig. 2, it is easy to see that our proposed scheme for both overlap and non-overlap cases overwhelm that of the conventional NOMA scheme, due to that the undesired signals for the V2 and V2 will not be decoded. With the growing SNRs, our proposed scheme illustrate more obvious advantages. In addition, it is also shown that, for our proposed NOMA-IoV scheme, the overlap case is better than the non-overlap case at the low SNR region, and these two cases are almost same at the high SNR region. This is reasonable, because of that, when \( \rho \) goes to infinity, the influence of the channel quality to the system performance will be weak replaced by the SNR. Moreover, it is clear that the simulation results tightly fit the analysis results especially in the high SNR region, which verifies our theoretical analysis. It is worth noting that, we approximate Eqs. (16) and (17) by considering the high transmit
SNR, since it is difficult to obtain the exact closed-form expression of $\gamma(x_1)$. On one hand, the approximation is only used partial of Eq. (15) as $\frac{B_{v_1}U_1c_1}{B_{v_1}U_1c_2\rho+1} \sim \frac{c_1}{c_2}$. On the other hand, as shown in numerical results, there is a good match between the simulation and analysis results, especially at high SNR region. Therefore, these illustrates that the performance loss provided from the approximation is negligible.

Figure 3 shows the ergodic SR performance of the overlap case for our proposed NOMA-IoV scheme with respect to the average channel power $\alpha_\varsigma$, for $\varsigma \in \{(v_1, U_1), (v_1, U_2), B_1, B_2\}$. In these subfigures, we also consider the different SNR conditions, i.e., $\rho = \{10, 15, 20, 25\}$ dB. All the subfigures depict that, even that $\alpha_{B_1}$ has the maximum impact on the system, the ergodic SR performance with respect to it are always the smallest from low to high SNRs. This is reasonable, because of that, with Eq. (15), it is easy to see if the channel coefficient is smaller, the results for the received SNR will change fast. According to the simulation set up, we have defined $\alpha_{B_1}$ as a smallest one for another one is greater (without loss of generality). Particularly, the ergodic sum-rate has varying degrees of improvements for all the cases. In addition, the $\alpha_{v_1, U_1}$ provides the maximum ergodic SR in every situations, especially at low SNR region. For high SNR case, $\alpha_\varsigma$ shows similar results, except $\alpha_{B_1}$.

Figure 4 illustrates the ergodic SR performance of the overlap case for our proposed NOMA-IoV system versus the power allocation factors $a_1$ and $b_1$, where we have fixed
\( \alpha_{B1} = 1 \), \( \alpha_{B2} = 10 \), and \( \alpha_3 = 0.01 \). Different transmit SNRs are considered including \( \rho = \{5, 10, 15, 20\} \) dB, respectively. Clearly, for all subfigures, the maximum ergodic SR will be achieved for a value of \( a_1 \) close to “1” while \( b_1 \) closed to “0.5”; due to that, for the greater \( a_1 \), similar \( b_1 \) and \( b_2 \), i.e., \( \{b_1, b_2\} \) close to 0.5 with \( b_1 + b_2 = 1 \), the maximum received SNRs in Eq. (15) will be achieved. To sum up, the ergodic SR of the proposed NOMA-IoV provides an outstanding advantage over the conventional NOMA one, and the overlap case achieves better performance than the non-overlap case at a low SNR region.

5.2 Discussion
For the conventional NOMA scheme, after receptions from BS, CHV1 and CHV2 will simultaneously decode the received signals, and then forward them to V1, V2 and V3. However, if the receiving node decode the signal transmitted via a very poor channel, and these decoded signals are not the the demands (the desired signal) of V1, V2 and V3, that will lead to a significantly performance limitation. Moreover, in conventional NOMA scheme, V1, V2 and V3 will also decode all the received signal without considering the demands, resulting in a further performance loss. Therefore, different from conventional works, we focus on the demands of vehicles to avoid the
disadvantages discussed above. Finally, the decoding elements for our proposed overlap scheme and conventional NOMA scheme are respectively shown as Table 1 in details.

**6 Conclusions**

In this paper, a novel NOMA-IoV scheme was investigated with different vehicle locations considering the overlap and non-overlap region for CHVs. Different to conventional NOMA schemes, the CHVs only decoded the desired signals for the vehicles in next hop to avoid the system performance loss. Adopting MRC, the vehicle in overlap region received signals from CHV1 and CHV2 resulting in a significantly ergodic rate improvement. Moreover, the theoretical derivations have been shown to highly agree
with the simulation results, especially at the high SNR region. By means of the numerical results, our proposed NOMA-IoV scheme has been shown to exhibit a better SR behavior than the conventional NOMA scheme. Moreover, in our proposed scheme, the ergodic SR for the overlap case is better than the non-overlap case at the low SNR, and is similar at high SNR. Our future concerns will be the joint optimization on the power allocations at BS and CHVs.

Abbreviations
(NOMA): Non-orthogonal multiple access; (OMA): Orthogonal multiple access; (SIC): Successive interference cancellation; (MRC): Maximum ratio combining; (SR): Sum-rate; (PA): Power allocation; (TDMA): Time-division multiple access; (CSI): Channel state information; (DF): Decode-and-forward; (AWGN): Additive white Gaussian noise; (BS): Base station; (CHV): Cluster head vehicle.

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Authors' contributions
J. Gu, W. Duan, and G. Zhang conceived and designed the study. J. Gu and W. Duan performed the simulations. J. Gu and G. Zhang wrote the paper. W. Duan, and G. Zhang reviewed and edited the manuscript. All authors read and approved the final manuscript.

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Availability of data and materials
The authors declare that all the data and materials in this manuscript are available. In addition, a MATLAB tool has been used to simulate our concept.

Declaration
Competing interests
The authors declare that they have no competing interests.

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