Simulation: Early Detection of Brain Vessels Stroke by Applying Electromagnetic Waves Non-Invasively

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Abstract

Introduction: Early recognition of stroke with its two types Ischemic and Hemorrhagic, is one of the most crucial research points, commonly used methods are CT- (computerized tomography), and MRI- (Magnetic resonance imaging). These techniques cause a delay in the detection of the condition, which causes permanent disability. The main reason behind the fatal consequences of stroke is the delay of detection. Therefore, this research paper aims to early detection of the type of stroke without delay until the appropriate diagnosis of each type is made, and then the appropriate treatment without delay.

Method: Using a non-invasive and fast technique to determine the stroke type by wave, we simulate and design a vessel containing a liquid as a laminar flow with the same density and velocity of blood, and it was surrounded by a Homogenized multi-turn coil consisting of (n) turns to represent the magnetic field, using specific frequency (HZ) with Electrical field in coil current (A) to see the changing in magnetic flux density (MFD). Depending on the changes in MFD, the flow of blood in laminar flow can be affected by clotting (Ischemic) or Hemorrhagic (cutting) in our vessel designed. We have built three different scenarios to apply the technique which are: First: Normal Scenario (where the blood in vessel has no problem), second: clotting (ischemic, where the vessel blocked in specific three position) and third: cutting (Hemorrhagic, where the vessel cut in certain nine positions).

Results: This paper presents-through our own design-the studying of applying the electromagnetic waves on blood inside the vessel to detect the stroke type in our three scenarios (normal, ischemic three positions or hemorrhagic nine positions), Studying the magnetic field and laminar flow. This study covered in three areas. First: coil geometry analysis, Second: stationary, and Third: frequency domain. through the changes in Magnetic Flux Density -MFD- waves. The results were promising and distinct for distinguishing between the three scenarios which are normal, ischemic (3 positions) and hemorrhagic (9 positions) the results of MFD are: 0.09 to 3.3*10^-3, 0.08 to 3.15*10^-4, 0.15 to 6.2*10^-3 respectively.

Keywords— Stroke recognition, Brain Stroke, Non-Invasive stroke detection, Stroke simulation, Vessel modeling.

Introduction

In order to increase the impact of the study, a vital topic was chosen by thinking of a new method that saves the time required to identify the type of stroke [1-3] and provides many patients with the time needed for the treatment process so that complications and permanent disabilities do not occur due to this delay in discovery through the available technologies. Stroke is one of the research areas that need a lot of effort, as it dramatically affects the person who suffers from it. As is well known, stroke occurs when a blood vessel that feeds the brain gets blocked (ischemic stroke) or bursts (hemorrhagic stroke). Then that part of the brain cannot work, nor can the part of the body it controls. Stroke causes the death of more than six million people annually, while 70% of those who recover from it live the rest of their lives with permanent disability. The main reason behind the fatal consequences of stroke is the delay of detection. Predetecting of Stroke type: [Ischemic which is a clot in a vessel in the brain or Hemorrhagic which is
caused by bleeding in the brain) using scanning by CT (computerized tomography) [4,5] or MRI (Magnetic resonance imaging) [6-8]. These available techniques for stroke detection, despite their vast potentials, and apart from the continuous development, do not help in the early detection of a stroke to reduce death or permanent disability for millions of people. So, it has some delay in detecting the stroke type in many scenarios.

The main goal in this study is to predilect stroke by changing in waves MFD (Magnetic Flux Density), which is the amount of magnetic flux through a unit area taken perpendicular to the direction of magnetic flux, so, Magnetic Flux is the total number of magnetic field lines passing through a given area. In the magnetic flux formula $\mu$ is the permeability of the medium (material) where we are measure the fields.

We use simulation Multiphysics between our designed geometry as a model to represent the vessel and magnetic fields with laminar flow and frequency to determine fast detection of brain stroke by non-invasive technique [9-13]. This noninvasive technique Does not require physical interference such as CT and MRI as imaging devices available technique, it is provided. It requires shining electromagnetic waves at a certain distance from the artery according to the scenarios mentioned later, and then measuring the extent to which these waves change according to the situation, being Ischemic or Hemorrhagic. Through the changing in waves and depending on the changing of magnetic flux density in the vessel design [14-17]. This treatment is highly dependent on time and cost from symptom onset to administration.

This paper primarily aims to provide a novel technique for early stroke detection, which reduces the risk of death or permanent disability. The mechanism of the technique is non-invasive by matching the radiation waves of healthy and infected as well. By finding a relationship between frequency, electric current, the nature of the coil and the number of its coils, where the experiment was carried out on the model that was designed according to several criteria, The study concluded with precise results and easy to differentiate between the different types of stroke, and on the other hand, the normal state through the resulting change in three scenarios (Normal, Ischemic and Hemorrhagic) Stroke. In this way, which can be developed later to be a device that can contribute to the early detection of stroke, we have begun to move towards a new method that may significantly reduce the risk of stroke as much as possible.

**Model Construction**

Based on the shortcomings in the current methods of stroke detection and identification, the use of a scenario in a non-intrusive manner was addressed by designing our simulation model, then, applying electromagnetic waves [18,19], and measuring the change in results according to the three scenarios.

The model was designed- figure 1, using laminar flow [20-23] to represent the blood flow in venous, in normal Scenario, blood clotting in ischemic Scenario 2 through 3 positions, and vessel cut in hemorrhagic Scenario 3 through 9 positions. With a total of 13 models to represent all Scenarios with it is positions. The laminar flow in our designed model has defined the Inlet boundary condition as velocity ($u$), and the outlet boundary condition as pressure ($p$).

In addition, we surrounded this laminar flow by Homogenized multi-turn Coil as a conductor model that represent electromagnetic field [24-27]. The coil is Numeric, and coil magnetic vector potential is Quadratic, with current (A) to coil excitation as we need to see the Magnetic Flux Density MFD [28-32]. Our model is a Cartesian geometry $\{x, y, z\}$ with a main parameter listed in table 1.
# Table 1: Model Basic parameters

| Name                  | Value   | Description | Unit |
|-----------------------|---------|-------------|------|
| Frequency - F         | (10,15,20) | All          | Hz   |
| Relative permeability | 1       | Air Material parameter | μr   |
| Relative permittivity | 1       | Air Material parameter | Er   |
| Coil current          | (0.5,1,1.5) | Coil-MF | A    |
| Dynamic viscosity     | 1 Pa·s  | Core        | μ/μu |
| Reference temperature | 293.15[K] | Laminar Flow | T    |
| Reference pressure level | 1[atm]  | Laminar Flow |      |
| Blood Density- rho    | 1060 kg/ m³ | Laminar Flow | ρ    |
| Electrical conductivity | 0       | Air Material parameter |      |
| Number of turns       | (20,25) | Coil-MF | n    |
| Coil conductivity     | 6e7[S/m] | Coil-MF | σ(s/m) |
| Stabilization         | Automatic | Coil-MF |      |
| Relative permeability | 1e3     | Core       |      |
| Electrical conductivity | 0       | Core       |      |
| Relative permittivity | 1       | Core       |      |
| Velocity              | u       | (m/s)      |      |
| Pressure/ Absolute pressure | p       | (pa)      |      |
| Electric Field- D     | D = ε   |            |      |
| Magnetic Vector Potential | A       | Wb/m |      |
| Magnetic Insulation   | = n*A=0 |            |      |
| Coi l Multiplication factor | 1       | F_L |      |
| Coi l Area            | 1       | F_A |      |
| Coi l cross-section area | wire_rad²*pi | m² |      |
| Ratio of specific heats | Gamma 1.4 | 1 |      |

Matrix of our models designed as shown in the three scenarios is shown in figure 2 to show graphical vessel– Normal, clotting, and cut positions

![Graphical Representation](image_url)

**Methodology**

The researchers studied the multi-physics, which are (Magnetic fields and Laminar Flow) in the three areas: **First**: coil geometry analysis [33,34], **Second**: stationery [35-38], and **Third**: frequency domain [39-42].

In detailing the study there were many steps we will mention some of them. We started the study by compiling equations coil geometry analysis through magnetic vector potential and using a Linear solver with direct value in stationary solver1. Then we compile equation stationary 2 for magnetic vector potential with other dependent variables using Linear solver with Iterative value and Iterative solver value is FGMRS (flexible generalized minimum residual). The next step is to study stationary solver 3 for frequency domain using linear solver with iterative value, and
iterative solver value is BicGStab (biconjugate gradient stabilized iterative method)

Table 2: MFD norm for three scenarios in all positions designed in our models

| Scenario id | Name                                    | MFD- Magnetic Flux Density       |
|-------------|-----------------------------------------|----------------------------------|
| Scenario 1  | Normal blood flow                        | MFD = 0.09 to 3.3*10^-3          |
| Scenario 2  | Clotting: [3 positions - Position 1] Middle | MFD = 0.08 to 3.15*10^-4          |
| Scenario 2  | Clotting: [3 positions - Position 2] Above | MFD = 0.08 to 2.99*10^-4          |
| Scenario 2  | Clotting: [3 positions - Position 3] Down | MFD = 0.08 to 2.99*10^-4          |
| Scenario 3  | Cut: [9 positions - Position 1] Middle-Right | MFD = 0.18 to 6.91*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 2] Top-Right | MFD = 0.15 to 5.96*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 3] Down-Right | MFD = 0.17 to 6.69*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 4] Top-Left  | MFD = 0.59 to 6.89*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 5] Middle-Left | MFD = 0.16 to 5.82*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 6] Down-Left | MFD = 0.15 to 5.56*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 7] Top-Middle | MFD = 0.1 to 4.06*10^-3           |
| Scenario 3  | Cut: [9 positions - Position 8] Midle-Middle | MFD = 0.16 to 6.37*10^-3          |
| Scenario 3  | Cut: [9 positions - Position 9] Down-Middle | MFD = 0.15 to 5.82*10^-3          |

Our designed geometries for three scenarios to represent 14 different positions to measure the changing in MFD – Magnetic Flux Density [9], as described below:

**Domains and Boundaries specifications**

Figure below describe the Magnetic Fields Domains (1-14)

Figure below describe the Air Domains (1-7, 9-14)

Figure below describe the Core Domain (8)

Figure below describe the Ampere Low (Domains 1–5, 8–10, 12–13)

**Model Materials, Domains, and Boundaries**

Simulation notation of geometry (volume, surfaces, lines, and points) and processed "Entities" Domains, Boundaries, and if applicable edges and points. Common domain was used as mentioned below, with note some changes depending on the different Scenario and equations is applied in all scenarios.
density. And equation (2) $B = \nabla \times A$, where $B$ is the magnetic field, $A$ is the coil current, and equation (3) $J = \sigma E$, where $\sigma$ is the coil conductivity.

Magnetic Insulation (Boundaries 5–8, 29–30, 41, 46) with equation (4) $n \times A = 0$, Coil (Domains 6–7, 11, 14) using equation (5) $J = N l I / A_{coil}$, Geometry Analytics (Domains 6–7, 11, 14), Input (Boundary 13) for magnetic field see the figure 3, Laminar Flow (Domain 8) see the figure 4 with equations (6) $\rho \nabla (u) = 0$, Wall (Boundaries 22–23, 38, 47) using equation $U = 0$, Inlet (Boundary 24) see the figure 8 using equation $u = U_{in}$, Outlet (Boundary 25) see the figure 9 using equations (7) $\rho \nabla (u) + \nabla \rho = 0$, Wall (Boundary 24) see the figure 8 using equation $u = U_{in}$, Outlet (Boundary 25) see the figure 9 using equations (7) $\rho \nabla (u) + \nabla \rho = 0$.

With fluid properties equations (8) $\nabla \rho \nabla (u) + \nabla \rho = 0$.

Scenario 2: For clotting/Ischemic stroke which have three positions, Top (T), middle (M) and down (D) of vessel designed.

Magnetic fields (Domains 1–75), Air (Domain 1–6, 10–42, 44–73, 75), Core (Domains 7–9, 43, 74), Ampere Low (Domains 1–4, 7–41, 43–74) using equations (1) (2), (3), Magnetic Insulation (Boundaries 5–12, 14–25, 107–110, 112–116, 164–165, 168–169, 215, 217–220) using equation (4), Coil (Domains 5–6, 42, 75) using equation (5), Geometry Analytics (Domains 5–6, 42, 75), Input (Boundary 13), Laminar Flow (Domains 7–9, 43, 74) using equation (6), Wall (Boundaries 22–23, 32–33, 35–36, 41, 51–52, 83–84, 93, 99–103, 116, 121, 123, 132, 151, 160–161, 171, 174, 181, 191, 210, 212, 215), Inlet (Boundary 24), Outlet (Boundary 25) using equation (7).
Scenario 3: For cutting/ Hemorrhagic stroke which have nine positions, 3 Right (Top, middle and down), 3 Center (Top, middle and down), 3 Left (Top, middle and down). See the figures Figure 5, Figure 6, and Figure 7, respectively.

Magnetic fields (Domains 1–14), Air (Domains 1–7, 9–14), Core (Domain 8), Ampere Low (Domains 1–5, 8–10, 12–13) using equations (1) (2), (3), Magnetic Insulation (Boundaries 5–8, 29–30, 41, 46) using equation (4), Coil (Domains 6–7, 11, 14) using equation (5).

Geometry Analytics (Domains 6–7, 11, 14), Input (Boundary 13), Laminar Flow (Domain 8) using equation (6), Wall (Boundaries 22–23, 38, 47, 54–59), Inlet (Boundary 24), Outlet (Boundary 25) using equation (7).

In All three scenarios the stationary solver 1 with segregated 1 using termination technique with value iterations or tolerance, with the number of iterations 6, it had two segregated steps with linear solver with direct value.

The stationary 2 compiled the equations with dependent variables, with 150 as a maximum number of iterations and linear solver value is iterative, in addition, velocity u, pressure ρ, also using direct linear solver with the number of iteration value 2 for auxiliary space Maxwell (AMS) and direct solver value is PARDISO (Parallel Direct Sparse Solver for Clusters).

The stationary solver 3 is defined by the study step for frequency domain set at 15 HZ, and fully coupled linear solver with iterative value. In addition, iterative solver value is BicGStab (biconjugate gradient stabilized iterative method). in this section we have table 2 bellow that describing the results for all scenarios with it is all positions To ensure that our main parameters which are frequency F, Current A and Coil number of turns N, we tried to fix the current, and changing the values for coil turns and frequency, then fixing the frequency and change the current and coil current, and finally we fixed the coil turns and change the current and the frequency. And this is happened in many scenarios, we found that no change in MFD - Magnetic flux density norm results when we change the frequency. at the same time A and N fixed, table 3 show some results for normal Scenario, as the Magnetic flux density norm depend on / affected by the A and N only:

| #  | Frequency (F) | Current (A) | Coil (N) | MFD norm |
|----|---------------|-------------|----------|----------|
| 1  | 10 Hz         | 0.5 A       | 20       | 0.03 to 1.32*10^-3 |
| 2  | 15 Hz         | 0.5 A       | 20       | 0.03 to 1.32*10^-3 |
| 3  | 20 Hz         | 0.5 A       | 20       | 0.03 to 1.32*10^-3 |

While fixing the Current A, and increasing the coil turns N, in same Scenario and frequency is changes, the increase in coil N in effected by 0.3 in MFD norm, table 4 is showing some results:
In addition, the increasing of current (double 1 A) while frequency is changing and the coil N is fixed as shown in table 5, the MFD norm results became two times (double), and the results show that in 0.5 A the MFD value was 0.03 to $1.32 \times 10^{-3}$ and in 1 A the MFD value was 0.07 to $2.46 \times 10^{-3}$.

| #  | Frequency (F) | Current (A) | Coil (N) | MFD norm          |
|----|---------------|-------------|----------|-------------------|
| 4  | 10 Hz         | 0.5 A       | 25       | 0.04 to $1.65 \times 10^{-3}$ |
| 5  | 15 Hz         | 0.5 A       | 25       | 0.04 to $1.65 \times 10^{-3}$ |
| 6  | 20 Hz         | 0.5 A       | 25       | 0.04 to $1.65 \times 10^{-3}$ |

In addition, the increasing of current (double 1 A) while frequency is changing and the coil N is fixed as shown in table 5, the MFD norm results became two times (double), and the results show that in 0.5 A the MFD value was 0.03 to $1.32 \times 10^{-3}$ and in 1 A the MFD value was 0.07 to $2.46 \times 10^{-3}$.

| #  | Frequency (F) | Current (A) | Coil (N) | MFD norm          |
|----|---------------|-------------|----------|-------------------|
| 7  | 10 Hz         | 1 A         | 20       | 0.07 to $2.46 \times 10^{-3}$ |
| 8  | 15 Hz         | 1 A         | 20       | 0.07 to $2.46 \times 10^{-3}$ |
| 9  | 20 Hz         | 1 A         | 20       | 0.07 to $2.46 \times 10^{-3}$ |

By implementing 1.5 A, as shown in Table 6, the MFD norm results became three times when we used 0.5 A and this is mean that, the changing in frequency did not make any difference, while the increase in coil turns N is affecting the MFD value, also increasing the current A is very effective with N as they are the main effect of MFD norm value.

| #  | Frequency (F) | Current (A) | Coil (N) | MFD norm          |
|----|---------------|-------------|----------|-------------------|
| 10 | 10 Hz         | 1.5 A       | 20       | 0.1 to $3.96 \times 10^{-3}$ |
| 11 | 15 Hz         | 1.5 A       | 20       | 0.07 to $2.46 \times 10^{-3}$ |
| 12 | 20 Hz         | 1.5 A       | 20       | 0.07 to $2.46 \times 10^{-3}$ |
| 13 | 10 Hz         | 1.5 A       | 25       | 0.13 to $4.95 \times 10^{-3}$ |

Results

According to the results obtained in all scenarios, we found a clear difference and change in the shape of Magnetic Flux Density norm, and it is value, as we find the best differentiation between all scenarios, and we choose to study our model at frequency 15 Hz, current 1 A, and coil number of turns 25. results in table 2. The main scenarios result show that there are different values of the waves that can help us predict the stroke type through normal, clotting/Ischemic, and cutting/Hemorrhagic scenarios. The results represented in the figures below from figure 10 – 22 represent all scenarios respectively.

Table 6: Results for MFD, F is changing, A and N are fixed 1.5 A, 20 & 25 Turns
From the above-mentioned results, an average was extracted, where the scenario was $=0$, scenario $1 = 0.09$ to $0.0033$, scenario $2 = 0.08$ to $0.000315$, and scenario $3 = 0.15$ to $0.0062$. the results are graphically represented in figure 23.

Discussion

Through our approach to distinguishing stroke types in a non-invasive way, and according to the model that was designed which includes the base scenarios with a variety of positions, and by changing the basic values of the most influential parameters, the researchers found a solid indicator to approve that every Scenario has a different output in scenario exposure to radiation with low frequency. This help us to quickly define the stroke type and start the first step of medication that can help the patient because it is many times not appear as a result in MRI and we must wait for second scanning after 6 hours minimally, this may lead to a further deterioration of the condition and delay in its treatment, which causes common complications of the disease. Through this research, in the future we can design a hardware device using same software features we applied in this research to detect and measure magnetic field changes as a result of MFD and move this simulation work to be real to know the type and this is very cheap, fast, and safe in human real scenarios. And by calculating the average for every Scenario, we obtain a chart prove that we can determine and detect each stroke type and normal Scenario.

Conclusion

Considering the available medical devices that detect stroke, and according to what was mentioned in the delay of these devices in the early detection of stroke, and through the purpose of our research to present a new method that contributes to the early detection of stroke in a non-invasive way, where the results indicated a difference Significant change in electromagnetic waves in the first scenario, which is the normal state, the value of MFD was $0.09$ to $3.3\times10^{-3}$. The second scenario was ischemic at (3 positions) and the average of them for MFD equal to $0.08$ to $3.15\times10^{-4}$, And third scenario was haemorrhagic at (9 positions), and the average of them for MFD equal to $0.15$ to $6.2\times10^{-3}$.

This contribution provided by the research is a very important beginning for the development of the sector of available devices technologies to detect stroke in a simpler, faster and less expensive way, which may contribute to the development of these devices or their evolution towards a gradual adoption of the use of electromagnetic waves in the early detection or identification of stroke in order to be Determine the appropriate treatment.
faster or the emergence of alternative devices that contribute to this direction, which is what we hope for the future in our upcoming research.

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