Towards Reduced Instruction Sets for Synchronization

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Abstract

Contrary to common belief, a recent work by Ellen, Gelashvili, Shavit, and Zhu has shown that computability does not require multicore architectures to support “strong” synchronization instructions like compare-and-swap, as opposed to combinations of “weaker” instructions like decrement and multiply. However, this is the status quo, and in turn, most efficient concurrent data-structures heavily rely on compare-and-swap (e.g. for swinging pointers and in general, conflict resolution).

We show that this need not be the case, by designing and implementing a concurrent linearizable Log data-structure (also known as a History object), supporting two operations: append(item), which appends the item to the log, and get-log(), which returns the appended items so far, in order. Readers are wait-free and writers are lock-free, and this data-structure can be used in a lock-free universal construction to implement any concurrent object with a given sequential specification. Our implementation uses atomic read, xor, decrement, and fetch-and-increment instructions supported on X86 architectures, and provides similar performance to a compare-and-swap-based solution on today’s hardware. This raises a fundamental question about minimal set of synchronization instructions that the architectures have to support.

1 Introduction

In order to develop efficient concurrent algorithms and data-structures in multiprocessor systems, processes that take steps asynchronously need to coordinate their actions. In shared memory systems, this is accomplished by applying hardware-supported low-level atomic instructions to memory locations. An atomic instruction takes effect as a single indivisible step. The most natural and universally supported instructions are read and write, as these are useful even in uniprocessors to store and load data from memory.

A concurrent implementation is wait-free, if any process that takes infinitely many steps completes infinitely many operation invocations. An implementation is lock-free if
in any infinite execution infinitely many operations are completed. The celebrated FLP impossibility result \cite{FLP85} implies that in a system equipped with only \textit{read} and \textit{write} instructions, there is no deterministic algorithm to solve binary lock-free/wait-free consensus among \( n \geq 2 \) processes. Binary consensus is a synchronization task where processes start with input bits, and must agree on an output bit that was an input to one of the processes. For one-shot tasks like consensus, wait-freedom and lock-freedom are equivalent.

Herlihy’s Consensus Hierarchy \cite{Her91} takes the FLP result further. It assigns a \textit{consensus number} to each object, namely, the number of processes for which there is a wait-free binary consensus algorithm using only instances of this object and read-write registers. An object with a higher consensus number is hence a more powerful tool for synchronization. Moreover, Herlihy showed that consensus is a fundamental synchronization task, by developing a universal construction which allows \( n \) processes to wait-free implement any object with a sequential specification, provided that they can solve consensus among themselves.

Herlihy’s hierarchy is simple, elegant and, for many years, has been our best explanation of synchronization power. It provides an intuitive explanation as to why, for instance, the \texttt{compare-and-swap} instruction can be viewed “stronger” than \texttt{fetch-and-increment}, as the consensus number of a \texttt{Compare-and-Swap} object is \( n \), while the consensus number of \texttt{Fetch-and-Increment} is 2.

However, key to this hierarchy is treating synchronization instructions as distinct objects, an approach that is far from the real-world, where multiprocessors do let processes apply supported atomic instructions to arbitrary memory locations. In fact, a recent work by Ellen et al. \cite{EGSZ16} has shown that a combination of instructions like \texttt{decrement} and \texttt{multiply-by-n}, whose corresponding objects have consensus number 1 in Herlihy’s hierarchy, when applied to the same memory location, allows solving wait-free consensus for \( n \) processes. Thus, in terms of computability, a combination of instructions traditionally viewed as “weak” can be as powerful as a \texttt{compare-and-swap} instruction, for instance.

The practical question is whether we can really replace a \texttt{compare-and-swap} instruction in concurrent algorithms and data-structures with a combination of weaker instructions. This might seem improbable for two reasons. First, \texttt{compare-and-swap} is ubiquitous in practice and used heavily for various tasks like swinging a pointer. Second, the protocol given by Ellen et al. solves only binary \( n \)-process consensus. It is not clear how to use it for implementing complex concurrent objects, as utilizing Herlihy’s universal construction is not a practical solution. On the optimistic side, there exists a concurrent queue implementation based on \texttt{fetch-and-add} that outperforms \texttt{compare-and-swap}-based alternatives \cite{MA13}. Both a \texttt{Queue} and a \texttt{Fetch-and-Add} object have consensus number 2, and this construction does not “circumvent” Herlihy’s hierarchy by applying different non-trivial synchronization instructions to the same location. Indeed, we are not aware of any practical construction that relies on applying different instructions to the same location.

As a proof of concept, we develop a lock-free universal construction using only \texttt{read}, \texttt{xor}, \texttt{decrement}, and \texttt{fetch-and-increment} instructions. The construction could be made wait-free by standard helping techniques. In particular, we implement a \texttt{Log} object \cite{BMW+13}. 

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(also known as a History object \cite{Dav04}), which supports high-level operations \texttt{get-log()} and \texttt{append(item)}, and is linearizable \cite{HW90} to the sequential specification that \texttt{get-log()} returns all previously appended items in order. This interface can be used to agree on a simulated object state, and thus, provides the universal construction \cite{Her91}. In practice, we require a \texttt{get-log()} for each thread to return a suffix of items after the last \texttt{get-log()} by this thread. We design a lock-free \texttt{Log} with wait-free readers, which performs as well as a \texttt{compare-and-swap}-based solution on modern hardware.

In our construction, we could replace both \texttt{fetch-and-increment} and \texttt{decrement} with the atomic \texttt{fetch-and-add} instruction, reducing the instruction set size even further.

\section{Algorithm}

We work in the bounded concurrency model where at most \(n\) processes will ever access the \texttt{Log} implementation. The object is implemented by a single \texttt{fetch-and-increment}-based counter \(C\), and an array \(A\) of \(b\)-bit integers on which the hardware supports atomic \texttt{xor} and \texttt{decrement} instructions. We assume that \(A\) is unbounded. Otherwise, processes can use \(A\) to agree on the next array \(A'\) to continue the construction. \(C\) and the elements of \(A\) are initialized by 0. We call an array location \texttt{invalid} if it contains a negative value, i.e., if its most significant bit is 1, \texttt{empty} if it contains value 0, and \texttt{valid} otherwise. The least significant \(m = \lceil \log_2(n+1) \rceil\) bits are \textit{contention bits} and have a special importance to the algorithm. The remaining \(b - m - 1\) bits are used to store items. See Figure 1 for illustration.

For every array location, at most one process will ever attempt to record a \((b - m - 1)\)-bit item, and at most \(n - 1\) processes will attempt to invalidate this location. No process will try to record to or invalidate the same location twice. In order to record item \(x\), a process invokes \texttt{xor}(\(x'\)), where \(x'\) is \(x\) shifted by \(m\) bits to the left, plus \(2^m - 1\geq n\), i.e., the contention bits set to 1. To invalidate a location, a process calls a \texttt{decrement}. The following properties hold:

1. After a \texttt{xor} or \texttt{decrement} is performed on a location, no \texttt{read} on it ever returns 0.

2. If a \texttt{xor} is performed first, no later \texttt{read} returns an invalid value. Ignoring the most significant bit, the next most significant \(b - m - 1\) bits contain the item recorded by \texttt{xor}.

3. If a \texttt{decrement} is performed first, then all values returned by later \texttt{reads} are invalid.

A \texttt{xor} instruction \textit{fails to record an item} if it is performed after a decrement.
To implement a \texttt{get-log()} operation, process \( p \) starts at index \( i = 0 \), and keeps reading the values of \( A[i] \) and incrementing \( i \) until it encounters an empty location \( A[i] = 0 \). By the above properties, from every valid location \( A[j] \), it can extract the item \( x_j \) recorded by a \texttt{xor}, and it returns an ordered list of all such items \((x_{i_1}, x_{i_2}, \ldots, x_{i_k})\). In practice, we require \( p \) to return only a suffix of items appended after the last \texttt{get-log()} invocation by \( p \). This can be accomplished by keeping \( i \) in static memory instead of initializing it to 0 in every invocation. To make \texttt{get-log} wait-free, \( p \) first performs \( l = C.read() \). Then, if \( i \) becomes equal to \( l \) during the traversal, it stops and returns the items extracted so far.

To implement \texttt{append}(\( x \)), process \( p \) starts by \( \ell = C.fetch-and-increment() \). Then it attempts to record item \( x \) in \( A[\ell] \) using an atomic \texttt{xor} instruction. If it fails to record an item, the process does another \texttt{fetch-and-increment} and attempts \texttt{xor} at that location, and so on, until it is able to successfully record \( x \). Suppose this location is \( A[\ell'] \). Then \( p \) iterates from \( j = \ell' - 1 \) down to \( j = 0 \), reading each \( A[j] \), and if \( A[j] \) is empty, performing a \texttt{decrement} on it. Afterwards, process \( p \) can safely return.

\texttt{fetch-and-increment} guarantees that each location is \texttt{xored} at most once, and it can be \texttt{decremented} at most \( n - 1 \) times, once by each process that did not \texttt{xor}. As a practical optimization, each process can store the maximum \( \ell' \) from its previous \texttt{append} operations and only iterate down to \( \ell' \) in the next invocation (all locations with lower indices will be non-empty). Our implementation of \texttt{append} is lock-free, because if an operation takes steps and does not terminate it must be repeatedly failing to record items in locations. This only happens if other \texttt{xor} operations successfully record their items and invalidate these locations.

At any time \( t \) during the execution, let us denote by \( f(t) \) as the maximum index such that, \( A[f(t)] \) is valid and \( A[j] \) is non-empty for all \( j \leq f(t) \). By the first property \( f(t) \) is non-decreasing, i.e., for \( t' > t \) we have \( f(t') \geq f(t) \). We linearize an \texttt{append}(\( x \)) operation by \( p \) that records \( x \) at location \( A[\ell] \) at the smallest \( t \) where \( f(t) \geq \ell \). This happens during the operation by \( p \), as when \( p \) starts \texttt{append}(\( x \)), \( A[\ell] \) is empty, and when \( p \) finishes, \( A[0] \neq 0, \ldots, A[\ell - 1] \neq 0 \) and \( A[\ell] \) is valid. Next, we show how to linearize \texttt{get-log()}.

Consider a \texttt{get-log()} operation with the latest returned item \( x_\ell \) extracted from \( A[\ell] \). We show by contradiction that the execution interval of this \texttt{get-log()} must contain time \( t \) such that \( f(t) = \ell \). We then linearize \texttt{get-log()} at the smallest such \( t \). It is an easy exercise to deal with the case when multiple operations are linearized at exactly the same point by slightly perturbing linearization points to enforce the correct ordering. Suppose the \texttt{get-log()} operation extracts \( x_\ell \) from \( A[\ell] \) at time \( T \). \( f(T) \geq \ell \) as \texttt{get-log()} stops at an empty index, and by the contradiction assumption we must have \( \ell' = f(T) > \ell \). \texttt{get-log()} then reaches valid location \( A[\ell'] \) and extracts an item \( x_{\ell'} \) from it, contradicting the definition of \( x_\ell \).

We implemented the algorithm on X86 processor and with 32 threads. It gave the same performance as an implementation that used \texttt{compare-and-swap} for recording items and invalidating locations. It turns out that in today’s architectures, the cost of supporting \texttt{compare-and-swap} is not significantly higher than that of supporting \texttt{xor} or \texttt{decrement}. This may or may not be the case in future Processing-in-Memory architectures [PAC+97].
Finding a compact set of synchronization instructions that, when supported, is equally powerful as the set of instructions used today is an important question to establish in future research.

References

[BMW+13] Mahesh Balakrishnan, Dahlia Malkhi, Ted Wobber, Ming Wu, Vijayan Prabhakaran, Michael Wei, John D Davis, Sriram Rao, Tao Zou, and Aviad Zuck. Tango: Distributed data structures over a shared log. In Proceedings of the 24th ACM Symposium on Operating Systems Principles, SOSP ’13, pages 325–340, 2013.

[Dav04] Matei David. Wait-free linearizable queue implementations, 2004.

[EGSZ16] Faith Ellen, Rati Gelashvili, Nir Shavit, and Leqi Zhu. A complexity-based hierarchy for multiprocessor synchronization: [extended abstract]. In Proceedings of the 35th ACM Symposium on Principles of Distributed Computing, 2016.

[FLP85] Michael J Fischer, Nancy A Lynch, and Michael S Paterson. Impossibility of distributed consensus with one faulty process. Journal of the ACM (JACM), 32(2):374–382, 1985.

[Her91] Maurice Herlihy. Wait-free synchronization. ACM Transactions on Programming Languages and Systems, 1991.

[HW90] Maurice Herlihy and Jeannette Wing. Linearizability: A correctness condition for concurrent objects. ACM Transactions on Programming Languages and Systems (TOPLAS), 12(3):463–492, 1990.

[MA13] Adam Morrison and Yehuda Afek. Fast concurrent queues for x86 processors. In Proceedings of the 18th ACM SIGPLAN Symposium on Principles and Practice of Parallel Programming, volume 48 of PPoPP ’13, pages 103–112, 2013.

[PAC+97] David Patterson, Thomas Anderson, Neal Cardwell, Richard Fromm, Kimberly Keeton, Christoforos Kozyrakis, Randi Thomas, and Katherine Yelick. A case for intelligent ram. IEEE Micro, 17(2):34–44, 1997.