Pulsar current revisited

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ABSTRACT

The pulsar current, in the \( P - \dot{P} \) plane where \( P \) is the pulsar period and \( \dot{P} \) is the period derivative, is used as a supposedly ‘model-free’ way to estimate the pulsar birthrate from statistical data on pulsars. We reconsider the derivation of the kinetic equation on which this is based, and argue that the interpretation of the pulsar current is strongly model dependent, being sensitive to the form of the assumed evolution law for pulsars. We discuss the case where the trajectory of a pulsar is assumed to be of the form \( \dot{P} = K P^{2-n} \) with \( K \) and \( n \) constant, and show that (except for \( n = 2 \)) one needs to introduce a pseudo-source term in order to infer the birthrate from the pulsar current. We illustrate the effect of this pseudo-source term using pulsar data to estimate the birthrate for different choices of \( n \). We define and discuss an alternative ‘potential’ class of evolution laws for which this complication is avoided due to the pseudo-source term being identically zero.

Key words: stars: magnetic field – pulsars: general – stars: statistics.

1 INTRODUCTION

The pulsar current is used to derive constraints on the birth of pulsars from the statistical distribution, \( N_P(P, \dot{P}) \), of the population of pulsars in the \( P - \dot{P} \) plane (Fig. 1), where \( P \) is the period and \( \dot{P} \) is the period derivative. Individual pulsars move along trajectories on the \( P - \dot{P} \) plane, becoming observable (‘birth’) at some point and disappearing from observation (‘death’) at some other point. In a steady state there should be a constant flow of pulsars in the \( P - \dot{P} \) plane from the region where they are born to the region where they die. This flow is referred to as the pulsar current (Phinney & Blandford 1981; Vivekanand & Narayan 1981; Deshpande, Ramachandran & Srinivasan 1995), which is defined as the integral over \( \dot{P} \) of \( J_P = \dot{P} N_P(P, \dot{P}) \). In a standard model (Lyne, Manchester & Taylor 1985), all pulsars are thought to be born in supernovae with short initial periods. The expected pulsar current should increase as a function of \( P \), reaching a plateau at \( P \sim P_0 \), with \( P_0 \) corresponding to the maximum period at birth, followed by decline at large \( P \) as pulsars die. The birthrate is proportional to the height of the plateau. An early analysis using the pulsar current technique indicated a step-like increase in the pulsar current at around \( P = 0.5 \) s (Vivekanand & Narayan 1981), implying significant injection at relatively large \( P \), and also at relatively high magnetic fields (\( B \geq 10^{12} \) G). However, Lorimer et al. (1993) found no strong evidence for injection at such relatively long periods. A more recent analysis (Vranesevic et al. 2004) suggests that up to 40 per cent of all pulsars are born with periods in the range 0.1–0.5 s, and that over half the pulsars are born with magnetic fields \( \geq 2.5 \times 10^{12} \) G. From the latest pulsar current analysis, Keane & Kramer (2008) found that the inferred birthrate is not obviously consistent with the supernova rate.

In this paper we reconsider the formal basis for the pulsar current technique, questioning the view that it is ‘model free.’ The formal basis for the pulsar current technique can be understood in terms of an analogy between the evolution of pulsars and the evolution of a one-dimensional (1D) dynamical system (Phinney & Blandford 1981). The period, \( P \), plays the role of a generalized coordinate, and the period derivative, \( \dot{P} \), plays the role of a generalized velocity. The evolution of pulsars may be described by a force law, which can be written as \( \dot{P} = f(P, \dot{P}) \), and the solution of this equation gives the trajectory (the path of an individual pulsar in the \( P - \dot{P} \) plane), which depends on the specific function \( f(P, \dot{P}) \), and on an arbitrary constant of integration that can be different for different pulsars. Some examples were given by Phinney & Blandford (1981). Here we choose a widely favoured (‘constant-\( n \)’) model, in which pulsars are assumed to evolve such that they have a constant braking index, \( n \), to illustrate our arguments.

The conventional interpretation of the pulsar current relies on two assumptions. One assumption is that all pulsars evolve according to the same law, and that this law depends only on \( P \) and \( \dot{P} \). The requirement that the evolution depend only on \( P \) and \( \dot{P} \) implies that it must not depend on any additional pulsar variable, such as a changing magnetic field, \( B \), or a changing angle, \( \alpha \), between the rotation and magnetic axes. This requires that pulsars with the same \( P \) and \( \dot{P} \) must have the same \( P \) and the same \( n \). This assumption seems inconsistent with glitching, involving discontinuous changes in \( P \), and other non-systematic changes observed in pulsar timing.
2.2 Pulsar current

The flow of pulsars through a vertical line in the $P - \dot{P}$ plane is interpreted as the pulsar current. The pulsar current is conventionally interpreted as a 'fluid' flow, where the fluid density corresponds to the distribution function for pulsars. These are described by the three terms in the kinetic equation.

\[ \frac{d}{dt} N_P(P, \dot{P}, t) = S_\text{birth}(P, \dot{P}) - S_\text{death}(P, \dot{P}) + S_\text{passage}(P, \dot{P}, t), \]

where $S_\text{birth}(P, \dot{P})$ and $S_\text{death}(P, \dot{P})$ are the rates, per unit time and per unit area of the $P - \dot{P}$ plane, that pulsars are born and die, respectively.

According to the rules of partial differentiation, the time derivative of $N_P(P, \dot{P}, t)$ on the left-hand side of (1) is given by

\[ \frac{d}{dt} N_P(P, \dot{P}, t) = \frac{\partial N_P(P, \dot{P}, t)}{\partial t} + \dot{P} \frac{\partial N_P(P, \dot{P}, t)}{\partial \dot{P}}. \]
is interpreted as the pulsar current. \((J_p(P, \dot{P}))\) is often referred to as the pulsar current, but it is actually the current density in a localized range of \(P\). The integral over \(P\) of

\[
\frac{\partial J_p(P, \dot{P})}{\partial P} = S_b(P, \dot{P}) - S_d(P, \dot{P})
\]

then expresses conservation of pulsars. This allows one to infer properties of the source term, \(S_b(P, \dot{P})\) describing birth of pulsars, and the sink term, \(S_d(P, \dot{P})\) describing death of pulsars, from the statistical distribution of pulsars on the \(P = \dot{P}\) plane.

### 2.3 Pseudo-source term

The kinetic equation (3) differs from that obtained by combining (2) and (1) in that the factors \(P\) and \(\dot{P}\) are inside the respective derivatives. To derive (3) from (2), one needs to move \(P\) and \(\dot{P}\) inside the respective derivatives. Assuming that \(P\) and \(\dot{P}\) are the independent variables, which is implicit in the use of the \(P = \dot{P}\) plane, the first of these is trivial. For the evolution law \(\dot{P} = f(P, \dot{P})\) assumed by Phinney & Blandford (1981), the second introduces an extra term, which we move to the right-hand side and interpret as a pseudo-source term,

\[
S_p(P, \dot{P}) = \frac{\partial f(P, \dot{P})}{\partial P} N_p(P, \dot{P}).
\]

The right-hand side of equation (5) is then replaced by \(S_b(P, \dot{P}) - S_d(P, \dot{P}) - S_p(P, \dot{P})\). In order to interpret information on the birthrate of pulsars from statistical data, one needs to calculate the additional term (equation 6). We discuss the effect of this term on the interpretation of the pulsar current for evolution at fixed \(n\) in the next section. We then argue that there is little evidence for the actual form of the pulsar evolution equation, that any model involves an ad hoc assumption and that a sensible criterion to adopt in choosing an evolution equation is that the pseudo-force term is absent.

### 3 OBSERVATIONAL RESULTS

The effect of the pseudo-source term on the interpretation of the pulsar current is explored in this section for the widely favoured model of evolution at fixed \(n\). This corresponds to \(f(P, \dot{P}) = (2 - n)\dot{P}^2/P\) in equation (6). The main qualitative point we make is that the use of the pulsar current is model dependent, with the explicit dependence on the model appearing through the pseudo-source term.

#### 3.1 Pseudo-source term for different values of \(n\)

We revisited our standard pulsar current analysis (Vranesevic et al. 2004) by including the pseudo-source term in our calculation. In the following analysis we used 1438 non-recycled pulsars that were predominantly discovered by the Parkes pulsar surveys, of which all are obtained from public pulsar catalogue at http://www.atnf.csiro.au/research/pulsar/psrcat. We accurately modelled the sensitivity threshold of the multibeam survey and used this model to compute the pulsar birth rate. To simulate the uncertainties in the data, rather than choosing a fixed braking index, we chose \(n\) randomly distributed about a mean, ranging from 1 to 5, and then calculated the pulsar current, with the same radio luminosity threshold, Galactic electron density and beaming models as for the conventional pulsar current approach (Vranesevic et al. 2004; Fig. 2). In Fig. 3 we plot the standard pulsar current together with two revisited pulsar currents, denoting their corresponding pulsar birthrates. There are substantial differences in currents corresponding to different values in \(n\). For \(n > 2\), \(S_p(P, \dot{P})\) is negative, which reduces the pulsar current, implying that the neglect of the pseudo-source term leads to an underestimate of the current. For \(n < 2\), \(S_p(P, \dot{P})\) is positive, implying that the neglect of the pseudo-source term leads to an overestimate of the current.

Our simulations for different runs of braking index are shown on Figs 4(a)–(c). Each plot displays two histograms, the revisited pulsar current on the left-hand side and its corresponding histogram of randomly chosen braking indices on the right-hand side. Matching birthrate and average braking index with its standard deviation are displayed on each histogram. The effect of the assumed value of \(n\) on the estimated birthrate for given data can be seen from the plots: \(n < 2\) (\(n > 2\)) the inferred birthrate is higher (lower) than when the pseudo-source term is neglected.
3.2 Measured braking indices

Lyne (2004) and Livingstone, Kaspi & Gavriil (2005) reported braking index measurements for six young pulsars (Crab, B0540−69, Vela, J1119−6127, B1509−58 and J1846−0258). Five have an unambiguous measurements of \( n \), via phase-coherent timing, and these are marked by a star in Table 1. We show their implied trajectories in the \( P - \dot{P} \) plane by arrows in Fig. 1.

There are only a few pulsars that are potential candidates for accurate measurement of \( n \), which requires that they satisfy the following. First they must spin-down sufficiently quickly to allow a useful measurement of \( \dot{P} \). Secondly, the position of the pulsar should be accurately known at the \( \sim 1\)-arcsec level. Thirdly, the spin-down must not be seriously affected by glitches, sudden spin-ups of the pulsar or timing noise. Typically, glitches begin to seriously affect smooth spin-down at characteristic ages of \( \sim 5-10 \) kyr (McKenna & Lyne 1990; Marshall et al. 2004). Thus many of the pulsars that may spin-down fast enough for a measurement of \( n \) are irretrievably contaminated by glitches (Shemar & Lyne 1996; Wang et al. 2001). Timing noise varies from object to object, is roughly correlated with spin-down rate (Arzoumanian et al. 1994) and can prevent a measurement of \( n \) in a finite data set in an unpredictable way. All six trajectories have \( n < 3 \), three of them have upward slopes (\( n < 2 \)) and none of them is directed towards the main body of pulsars. These data do not support the constant-\( n \)-model, which requires the same value of \( n \) for all pulsars at all \( P, \dot{P} \).

4 ALTERNATIVE EVOLUTION LAWS

For the pulsar current to be a well-defined concept, there must be a universal law of the form \( \dot{P} = f(P, \dot{P}) \) obeyed by all pulsars. This is clearly not the case. For the pulsar current to be a useful concept, such an evolution law must apply at least in some average sense for all pulsars. The constant-\( n \) evolution law assumed in the previous section, although widely favoured, is essentially ad hoc. In this section we introduce a general (Lagrangian) formalism that assumes that there is a unique evolution law but makes no assumptions on its form. We use this formalism to identify a simpler class of evolution models that we refer to as potential models.

4.1 Specific models

Before introducing a general theory for a possible pulsar evolution model, we summarize the models that underlie the discussion in the previous section.

4.1.1 Vacuum dipole model

The vacuum dipole model has a contradictory status in pulsar physics. One the one hand, it is the basis of our interpretation of pulsars, notably \( B \sin \alpha \propto (P \dot{P})^{1/2} \), and it is the only model for which the evolution is well determined. On the other hand, the model is clearly inapplicable to actual pulsars, and the actual evolution is inconsistent with observations. The constant \( n = 3 \) model is often assumed to describe evolution in the vacuum dipole, but this is incorrect.

The model is that a (structureless, point) rotating magnetic dipole in vacuo radiates electromagnetic radiation that escapes to infinity, carrying off energy and angular momentum. The loss of energy causes \( P \) to increase on a characteristic spin-down time-scale, and the torque causes \( \sin \alpha \) to decrease, implying that the rotation and
magnetic axes tend to align on the spin-down time-scale Michel
(1991). The braking index is \( n = 3 + 2 \cot^2 \alpha \) (Michel 1991),
which is always greater than 3 and which increases as \( \sin \alpha \) decreases.

This vacuum-dipole model, at least in its simplest form, is unac-
ceptable for pulsars. The putative electromagnetic radiation has a
frequency equal to the rotation frequency of the pulsar, well below
the plasma frequency in the pulsar wind and in the ISM, and
it cannot escape to infinity, as the model requires. The model predicts
that the magnetic and rotation axes align on the spin-down time-
scale. There is a theoretical argument that the structure of the star
may slow the alignment (Goldreich 1970), and there is evidence
for older pulsars having smaller of values of \( \sin \alpha \) (Weltevrede &
Johnston 2008), but the prediction of the model itself is inconsistent
with pulsar data.

4.1.2 The \( n = 3 \) model

The constant \( n = 3 \) model is often confused with the vacuum dipole
model. In the \( n = 3 \) model, it is assumed that the evolution of
pulsars is at constant \( B \sin \alpha \), and this is combined with the vacuum
dipole model so that the assumption becomes evolution at constant
\( PP \). Note that this is inconsistent with the actual vacuum dipole
model, which implies systematically decreasing \( \sin \alpha \). Thus, the
basic assumption in the constant \( n = 3 \) model is that the trajectory
of pulsars in the \( P - \dot{P} \) is of the form \( \dot{P} = K/P \), where \( K \) is a
constant. The force law implied by this relation is \( \ddot{P} = -P^2/P \) and
this implies a braking index
\[
\frac{d}{dt} = 2 - P \frac{P}{P^2} \tag{7}
\]
equal to 3. Although a vacuum model modified by assuming \( B \sin \alpha \)
remains constant is widely favoured, it is not supported by any
detailed theory for the evolution.

4.1.3 \( n = \text{constant} \) model

Another model that is used widely is based on the assumption that
the braking index is constant but not necessarily equal to 3; we
refer to this as the \( n = \text{constant} \) model. According to equation (7),
\( n = \text{constant} \) implies \( \dot{P} = (2 - n)P^2/P \), and integrating this equation
leads to the trajectory \( \dot{P} = K P^{2-n} \), where \( K \) is a constant. This
is the model used for illustrative purposes in the previous section.

However, the assumption \( n = \text{constant} \) on which it is based is also
not supported by any detailed theory for the evolution, and should
be regarded as ad hoc.

4.1.4 Potential models

Granted that one needs to make an ad hoc assumption in choosing a
possible universal law governing pulsar evolution in \( P - \dot{P} \), it is
desirable to choose a law that does not introduce unnecessary
complications. As shown in detail above, the \( n = \text{constant} \) model
leads to the need to include a pseudo-source term in the interpreta-
tion of the pulsar current. A model that avoids this complication is
one in which \( \dot{P} \) depends only on \( P \). We refer to this as a potential
model. The law is written in the form \( \ddot{P} = -C(P) \), where \( C(P) \)
is the potential in the theory developed below. This theory is also
not supported by any detailed theory for the evolution, and is also
ad hoc. However, a potential model has the advantage of being the
simplest model, and the best justification for it is that one should
explore the simplest model first.

4.2 Lagrangian formulation

In a Lagrangian formulation of dynamics the independent variables
are the generalized coordinates and generalized velocities. In the
present case, the generalized coordinate is identified as \( P \) and the
generalized velocity as \( \dot{P} \). A Lagrangian, \( L(P, \dot{P}) \) may be identified
by requiring that the Euler–Lagrange equation
\[
\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{P}} \right) - \frac{\partial L}{\partial P} = 0, \tag{8}
\]
reproduce the equation of motion.

Consider the evolution law (Phinney & Blandford 1981)
\[
\dot{P} = \frac{(2 - n)P^2}{P} - \frac{\dot{P}}{\tau}. \tag{9}
\]
This has a Lagrangian counterpart for \( \tau \to \infty \). The relevant
Lagrangian is a particular case of
\[
L(P, \dot{P}) = \frac{1}{2} A(P) \dot{P}^2 + B(P) \dot{P} - C(P), \tag{10}
\]
for which equation (8) implies
\[
\dot{P} = -\frac{A(P) \dot{P}^2 - C(P)}{2A(P)}. \tag{11}
\]
where the prime denotes a derivative in $P$. The form (9) is reproduced for $A(P) = P^{-2(n-\alpha)}$, $C(P) = 0$.

The trajectory of a pulsar in $P - \dot{P}$ space is found by solving the equation of motion. This is facilitated by noting the analogy with a one-dimensional particle in a potential, with $A(P)$ playing the role of the mass and $C(P)$ playing the role of the potential energy. The energy-integral (sum of kinetic and potential energies equals a constant) gives

$$\frac{1}{2}A(P)\dot{P}^2 + C(P) = E,$$

where $E$ is a constant of integration (the counterpart of the energy).

A second integral gives

$$\int dP \left( \frac{A(P)}{E - C(P)} \right)^{1/2} = 2^{1/2}t.$$

The example considered by Phinney & Blandford (1981) is reproduced by writing $E = (1/2)v^2, x = vt$.

### 4.3 Potential models

There is no pseudo-source term in the kinetic equation for a Lagrangian of the form (10) with $A(P) = 1$. The generalized momenta, $\partial L/\partial \dot{P}$, is then equal to the generalized velocity, so that the $P - \dot{P}$ is a phase space in the sense required for Liouville’s theorem to apply. In this case, equation (11) gives

$$\ddot{P} = -C(P),$$

and equations (12), and (13) apply with $A(P) = 1$. The braking index in this model is

$$n = 2 - \frac{\dot{P}P}{\dot{P}^2} = 2 + \frac{PC(C)}{2[E - C(P)]}.$$

A simple limiting case is $E \gg C(P)$, when the evolution law reduces to $\dot{P} \approx$ constant, with a braking index $n \approx 2$.

In these two examples of evolution laws, the trajectories of individual pulsars depend on a constant of integration, which depends on the particular pulsar. For trajectories of the form $\dot{P} = KP^{2-n}$ this constant is $K$, and for the potential law (equation 12), the constant is $E$. For any given law, the constant of integration is determined for a particular pulsar by the values of $P$ and $\dot{P}$ at birth, and the subsequent evolution is determined by equation (12) with $E$ fixed, but different for different pulsars.

### 5 DISCUSSION AND CONCLUSIONS

The theory for the pulsar current is based on the assumption that there is a universal evolution law for pulsars, and that it depends only on $P$ and $\dot{P}$. This requirement is not satisfied, with glitching and other random changes implying that the trajectory of at least some pulsars on the $P - \dot{P}$ plane is influenced by other effects. Nevertheless, it is possible that the evolution of all pulsars does follow a universal law in some average sense, and this would suffice to justify the pulsar current technique. Assuming there is an average universal evolution law that applies to all pulsars, it is clear that we have little information on what this law is. A constant-$n$ law has been used widely in the literature. We assume this law in Section 3, argue that such a law invalidates a conventional pulsar current analysis, and show how the error can be corrected by introducing a pseudo-source term. We argue that there is no theoretical basis for a constant-$n$ law, and that the complication it introduces through pseudo-source term makes it an undesirable choice for the form of the evolution law. We argue that the choice of a potential law for the evolution avoids the complication of a model-dependent pseudo-source term.

We discuss evolution laws in Section 4. We comment on the misconception that a constant $n = 3$ law corresponds to the vacuum dipole model, whereas it actually corresponds to a hybrid model, with $B \sin \alpha \propto (P \dot{P})^{1/2}$ determined by the energy-loss rate in the vacuum dipole model, and with $B \sin \alpha$ assumed constant. The actual vacuum dipole model implies that $\sin \alpha$ decreases (alignment of the magnetic and rotational axes) on the spin-down time-scale, and this does not occur. The vacuum dipole model is not applicable to actual pulsars, for this and other reasons. A general class of evolution models is developed in Section 4; this class includes the constant-$n$ model, with $\dot{P} = (2-n)P^{2-n}$, and potential models, with $\dot{P} = -C(P)$, where $C(P)$ is the potential. The evolution law is integrated to find the trajectory of the pulsar in $P - \dot{P}$ space. The trajectory can be written as $\dot{P} = KP^{2-n}$ for a constant-$n$ model, and as $\dot{P} = \sqrt{2(E - C(P))^{1/2}}$ for a potential model. The trajectory depends on a constant of integration, which is different for different pulsars. A physical model for the evolution is required to give a physical interpretation to such constants of integration. In the constant $n = 3$ model, the constant $K$ is proportional to $B \sin \alpha$, but there is no obvious interpretation of $K$ for other models with constant $n \neq 3$. A physical basis for a specific potential model is required to give a physical interpretation to $E$.

Assuming a potential law opens up a new way of thinking about the evolution of pulsars in the $P - \dot{P}$ plane. In our formulation the potential, $C(P)$, is an arbitrary function of $P$. By exploring different choices of $C(P)$ one can ask what choice (if any) best fits the data. Although we do not attempt to do this here, we speculate briefly on one implication. Suppose that the ‘potential energy’ is much smaller than the ‘kinetic energy’ $|C(P)| \ll (1/2)\dot{P}^2$. Then all trajectories have $\dot{P} \approx$ constant, implying a braking index $n \approx 2$. The measured values of $n$ include $n < 2$ and $n > 2$, which could be interpreted either according to equation (15), requiring $C(P) < 0$ and $C(P) > 0$, respectively, or interpreted as random variations about an average universal $n \approx 2$ for young pulsars. Perhaps average braking indices can be estimated for a large number of pulsars over a wide range of $P$, as suggested by Johnston & Galloway (1999) for example. If such an estimation of $n$ shows some systematic trend with $P$, equation (15) would provide some constraint on the possible form for $C(P)$. With such data one should be able to draw conclusions on whether simple examples of potential law are consistent with observations; simple models include $C(P) \propto P^a$ with $a > 0$ and $C(P) \propto -P^{-b}$ with $b > 0$. If there is no systematic trend, even in an average sense, this would cast serious doubt on the validity of the pulsar current technique, and conclusions drawn using it.

In conclusion, the pulsar current approach is not ‘model free’ and its interpretation depends on assumptions made about the form of the evolution law for pulsars. The theory depends on this law being universal, and although this is clearly not the case in an exact sense, it may be the case in some average sense. In modelling such an average law, the constant-$n$ assumption should be abandoned, and a ‘potential’ law should be the preferred choice on which to base future discussions.

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