Ways to increase the efficiency of detection of unmanned aerial vehicles by thermal imaging devices

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Abstract. The possibilities to increase the efficiency of detection of air objects due to the optimized choice of a functional area of an infrared range of electromagnetic waves are mathematically estimated. It is shown that there is a need to use receivers with maximum visibility in longer wavelengths, as well as the need to work in the "transparency windows" of the atmosphere. With low visibility, long-wavelength infrared thermal imaging devices are advantageous at long distances from objects. Devices with more shortwave sensitivity can be effective over short distances. Radar detection methods in many cases are not able to detect small objects with a low reflection coefficient, which is one of the reasons for the small effective scattering area. Known methods of observation using night vision devices and thermal imaging devices, having their advantages, are also ineffective in certain conditions. An attempt is made to combine the advantages of detecting aerial objects by the multi-position radar method with the advantages of thermal imaging devices. A method of illuminating air objects with infrared searchlights is proposed, which implies the presence of one or more geometrically spaced sources of infrared radiation with a working spectrum combined with areas of "windows of transparency" of the atmosphere and the maximum sensitivity of the thermal imager. In such conditions, the receiver registers the total signal of thermal radiation of the object and the reflected rays of searchlights. Remote control of the spotlight emission, on which the effective scattering area depends linearly, makes it possible to bring it to the level guaranteed with a high probability of detecting a small flying object.

1. Introduction

In recent years, observations of hostilities in various hotspots of the planet show that unmanned aerial vehicles are experiencing a real boom. High combat efficiency of unmanned aerial vehicles confirms it as one of the most important types of aircraft. As a result, the problem of airspace control has become more acute. Modern technologies used in small aircraft, such as unmanned aerial vehicles (UAVs), dramatically reduce their visibility. Special methods and surveillance systems are needed for timely detection of UAVs. UAVs are of small size and special geometry, have low engine power, are made of composite structural materials, which is expressed in small effective area of electromagnetic wave scattering (EWS), perform covert flights at medium, low and extremely low altitudes and are often invisible to radar systems (RS). In addition, RSs are quite structurally complex, cumbersome and at high power dangerous to humans, energy-intensive, and also unmasked. The use of traditional pulse RSs to increase the probability of detection of UAVs requires radical changes in their physical and technical parameters, and hence in the structural elements, which results in an increase in the cost of their production and maintenance. Multi-position radiolocation with a specific arrangement of radars and receivers is more effective for detecting small targets [1-6]. However, spaced multi-position systems have a major drawback – loss of functionality in the absence of radio communication. To reliably detect a UAV, it is necessary to maintain a continuous radar field over the controlled area at low and extremely low altitudes.
The low visibility of UAVs and the limited possibilities to detect radars encourage the search for the possibility of detection by other unmasking features.

2. Literature analysis
Still new models with various possibilities and characteristics regularly appear on the UAV market, which requires immediate development of the theory and practice of combating them [7-8].

Trends in the development of small aircraft, ways to increase the probability of detection by the main types of visibility are analyzed [9-12]. Professional analysis of methods to increase the efficiency of UAV detection by traditional radio equipment showed that they are associated with an increase in the number of RSs, increasing power consumption [13-15]. Thus, to increase the effective scattering surface, the methods of single-position and multi-position radar are combined, for which the appropriate channels of synchronized processing of own signals and signals from third-party transmitters are formed in the RS. However, the developed recommendations for the optimal use of these systems do not reduce the financial costs of their production and operation [16-18].

One of the unmasking features of a UAV is thermal infrared (IR) radiation, which is mainly emitted by the power plant of the flying object. The possibility to be detected depends on the temperature contrast between the object and the background, the radiation area, the emissivity of materials. The targets in the IR region of the EMS are observed using night vision devices (NVD) and thermal imaging devices (TID). Each of them has its advantages and disadvantages. The use of active-pulse optoelectronic devices increases the detection range, but unmask the observer. Such modern devices are complex in design and consume more energy [19-21].

Passive night vision devices are characterized by the covertness of reconnaissance surveillance and by their characteristics reach the theoretical limit of sensitivity [22-24]. Thermal imagers are inferior to night vision devices in resolution, but they can operate in complete darkness. Passive two-channel iconoptoelectronic systems are the most common for round-the-clock surveillance in poor visibility conditions [25-27].

Based on the problems of UAV detection, there is a need for a detailed study of the possibilities of increasing the detection efficiency in the IR range of EMS, the possibility of combining the methods of multi-position radar with the advantages of thermal imaging equipment.

2.1. Purpose of the paper.
Analyze possible mechanisms to increase the efficiency of detection of small aircraft TID.

3. Statement of the basic material

3.1. Optimization via the choice of the spectral section of the receiver sensitivity.
The efficiency of the system is its generalized functional property necessary to perform a certain task, which objectively expresses the degree of success in achieving the goal.

The signal-to-noise ratio at the output of the heat-sensitive radiation receiver is the physical and technical criterion of the efficiency of the TID observation.

The contrast of the thermal image of the object with temperature $T_o$ against the background with temperature $T_\phi$ is determined by difference signal $\Delta U$ [27-29]:

$$\Delta U_T = \frac{A_0\cdot A_0}{\pi L} \int_0^\infty \tau_w(\lambda) \cdot e^{-\alpha(\lambda)L} \cdot S_o(\lambda) \cdot \left[ e_o(\lambda)M(\lambda,T_0) - e_\phi(\lambda)M(\lambda,T_\phi) \right] d\lambda,$$

where $A_0$ – the area of the entrance pupil of the optical system;

$A_0$ – the area of the object of observation;

$\lambda$ – EMS length;

$\tau_w$ – spectral transmittance of the optical system;

$\alpha(\lambda)$ – the natural indicator of the attenuation of the atmosphere;
\( S_{a}(\lambda) \) – absolute voltage sensitivity of the radiation receiver;
\( L \) – the distance between the object and the optical system;
\( e_{o}(\lambda), e_{b}(\lambda) \) – the coefficients of the radiation of the object and the background, respectively;
\( M(\lambda, T_{o}), M(\lambda, T_{b}) \) – the spectral density of the radiation of an absolutely black body at the object temperature \( T_{o} \) and background temperature \( T_{b} \), respectively;
\[ M(\lambda, T) = c_{1}T^{3} \left[ \exp \left( \frac{c_{2}}{\lambda T} \right) - 1 \right]^{-1} \], where \( c_{1} = 3.74 \cdot 10^{-16} \text{W} \cdot \text{m}^{2} \); \( c_{2} = 1.439 \cdot 10^{-3} \text{m}^{2} \cdot \text{K} \).

Taking into account that \( S_{a}(\lambda) = d'_{a}(\lambda) \cdot \frac{U_{w}}{\sqrt{A_{r} \cdot \Delta f}} = d'_{a}(\lambda) \cdot D(\lambda) \cdot \frac{U_{w}}{\sqrt{A_{r} \cdot \Delta f}} \), expression (1) can be rewritten as follows:
\[ \Delta U_{r} = \frac{A_{r} \cdot A_{b} \cdot U_{w} \cdot D'_{a}(\lambda) \cdot \tau_{w}(\lambda) \cdot e^{-\alpha(\lambda)t}}{\pi \cdot L^{2} \cdot \sqrt{A_{r} \cdot \Delta f}} \cdot D(\lambda) \cdot \left[ e_{o}(\lambda) \cdot M(\lambda, T_{o}) - e_{b}(\lambda) \cdot M(\lambda, T_{b}) \right] d\lambda, \quad (2) \]

where \( d'_{a}(\lambda) \) – reduced detection ability, \( D'_{a}(\lambda) \) – its maximum value;
\( U_{w} \) – root-mean-square value of the noise;
\( \Delta f \) – equivalent noise bandwidth of the radiation receiver;
\( A_{r} \) – the area of the sensitive element of the receiver;
\( D(\lambda) = \frac{D'_{a}(\lambda)}{D'_{a}(\lambda)} \) – relative spectral detection ability.

To simplify the calculations, we make the following assumptions:
- integration \( \tau_{w}(\lambda) \) in expression (2) is substituted by an approximate value of the optical system transmittance integration coefficient \( \tau_{w} \);
- assume \( e_{o}(\lambda) = e_{b}(\lambda) = 1 \);
- relative spectral detection ability \( D(\lambda) \) is restricted by section \( \lambda \in [\lambda_{1}, \lambda_{2}] \) within the limits of which \( D(\lambda) = 1 \);
- at low differences between the object temperature \( T_{o} \) and background temperature \( T_{b} \) the difference in expression (2) can be changed by temperature differential [37-38]:
\[ d_{r} M(\lambda, T) = \frac{\partial M(\lambda, T)}{\partial T} dT \approx \frac{\partial M(\lambda, T)}{\partial T} \Delta T. \]

Then signal-to-noise relation \( q_{i} = \frac{\Delta U}{U_{w}} \) taking into account (2) will be of the form:
\[ q_{i}(\lambda) = \frac{A_{r} \cdot A_{b} \cdot \tau_{w} \cdot \Delta f \cdot \Delta \lambda}{\pi \cdot L^{2} \cdot \sqrt{A_{r} \cdot \Delta f}} \cdot \frac{\partial M(\lambda, T)}{\partial T} \cdot e^{-\alpha(\lambda)t} \cdot d\lambda, \quad (3) \]

The dependence of the attenuation natural indicator \( \alpha(\lambda) \) on EMS length at the molecular or aerosol mechanisms of scattering and absorption is interpreted by G. Mie’s known theory of radiation scattering in the turbid environment, which is based on the classical Maxwell's equations and is represented by rather complex mathematical expressions containing a number of special functions.
[30]. In this form, non-numerical integration in (3) is impossible. In practice, a somewhat approximate semi-empirical formula is used [31-33]:

$$\alpha(\lambda) = A \lambda^{-\beta}$$

(4)

where $$A = \frac{3.91}{S_M}(0.555)^\beta$$,

$$S_M$$ – meteorological visibility range, km.

In the general case the value of indicator $$\beta$$ and depends on the state of the atmosphere. Value $$\beta=4$$ corresponds to molecular (Rayleigh) scattering and in EMS IR-range is neglected small. Value $$\beta<4$$ corresponds to the attenuation of radiation due to absorption and scattering on aerosol particles of the atmosphere.

Value $$\beta$$ can be roughly compared with meteorological visibility $$S_M$$ according to the characteristics of the atmosphere in terms of the International Classification [34, 35]:

- the atmosphere is cloudless, very clear: $$S_M > 20 km$$, $$\beta \in (3.4);$$
- cloudless, clear: $$10 km \leq S_M \leq 20 km$$, $$\beta \in (2.3);$$
- noticeable haze, strong haze: $$2 km < S_M \leq 6 km$$, $$\beta \in (1.5);$$
- light fog: $$0.5 km < S_M < 1 km$$, $$\beta = 1;$$
- thick, continuous fog: $$0.05 km < S_M < 0.2 km$$, $$\beta \approx 0.$$  

In many cases dependence $$\beta = 0.585 \cdot S_M^{\frac{1}{2}}$$ is used, and under the conditions of moderate haze for $$\lambda \in (0.61 - 11.48) \mu m$$ indicator $$\beta \approx 0.7$$ [36, 37]. At operation sections $$\lambda \in [8 - 14] \mu m$$, where most TID function, dependence of $$\beta$$ on $$\lambda$$ is weak, therefore, without a great error, value $$\alpha(\lambda)$$ can be characterized by average value $$\bar{\alpha}$$ at interval $$\Delta \lambda = \lambda_2 - \lambda_1$$, taking into account (4) (Figure 1):

$$\bar{\alpha}(\lambda, \Delta \lambda) = \frac{1}{\lambda_2 - \lambda_1} \int_{\lambda_1}^{\lambda_2} \alpha(\lambda) d\lambda = \frac{A}{(1 - \beta) \cdot \Delta \lambda} \left[ \left( \lambda + \Delta \lambda \right)^{-\beta} - \left( \lambda - \Delta \lambda \right)^{-\beta} \right], \beta \neq 1.$$  

(5)

Then expression (3) will be of the form:

$$q_i(\lambda_i) = C_0 \cdot e^{-2(\lambda_i)\mu} \cdot \frac{\Delta T}{E_i} \cdot \frac{\lambda_i^{1/2}}{\tau_0} \cdot \frac{\partial M(\lambda, T)}{\partial T} d\lambda,$$

(6)

where $$C_0 = \frac{A_0 \cdot A_n \cdot \mathcal{D}_{max} \cdot \tau_0}{\pi \cdot \sqrt{A_0 \cdot \Delta f}}.$$  

In the range of temperatures $$(250 - 350)K$$ and wave lengths $$(1 - 15) \mu m$$ $$\exp\left(\frac{C_2}{\Lambda T}\right)$$ takes the value within limits $$\left(15 \cdot 10^{25}\right)$$. At lower temperatures, the exponent grows even more significantly. That is, in the range of functional lengths of EMS of thermal imagers of different generations, the spectral energy luminosity of the object and the background can be considered under the condition $$\exp\left(\frac{C_2}{\Lambda T}\right) >> 1,$$

which approximates Planck’s formula by Wine’s law and derivative in (6)

$$\frac{\partial M(\lambda, T)}{\partial T} \approx C_1 C_2 \cdot \exp\left(\frac{-C_1}{\Lambda T}\right)$$ (Figure 2).
Figure 1. Dependence of the average natural index of atmospheric attenuation on fixed beginning $\lambda_1$ of the section of TID thermal sensitivity (curve 1 – SM=0.2 km, $\beta$=1; curve 2 – SM=0.2 km, $\beta$=3; curve 3 – SM=10 km, $\beta$=1; curve 4 – SM=10 km, $\beta$=3).

Figure 2. Spectral density of energy luminosity according to Planck’s law (curve 1, 3 – solid) according to Wine’s law (curves 2, 4 – dotted) at $T=350^\circ K$ (curves 1, 2) and $T=273^\circ K$ (curves 3, 4).

Taking into account the above said, relation (6) is of the form:

$$q_i(\lambda_1, T, \Delta T, \Delta \lambda) = \frac{C_0 \cdot C_T \cdot T^3 \cdot \Delta T \cdot e^{-\sigma(\lambda)L}}{C_T^2 \cdot L^2} \sum_{n=1}^{\infty} (-1)^n \cdot e^{-x_n} \cdot (x_n^4 + 4x_n^3 + 12x_n^2 + 24x_n + 24),$$

(7)

where $x_n = \frac{C_2 \lambda_1}{\lambda_2}$, $\lambda_2 = \lambda_1 + \Delta \lambda$.

Figure 3. relation signal/noise at the output of TID receiver:

a) $T=273^\circ K; \Delta T=1^\circ K; L=3$ km

(b) curves 1, 2, 3 at $T=400^\circ K$

(1 – SM=30 km, $\beta$=3.5; curve 2 – SM=1 km, $\beta$=1; curve 3 – SM=0.2 km, $\beta$=0.7)

b) curves 1, 2, 3 at $T=400^\circ K$

c) $\beta$=0; $\Delta T=1^\circ K; SM=0.2$ km

(T=273$^\circ K$; curve 1 – L=0.3 km; curve 3 – L=0.5 km; curve 5 – L=1 km

T=400$^\circ K$; curve 2 – L=0.3 km; curve 4 – L=0.5 km).
As can be seen from Figure 3, the maximum signal-to-noise ratio at the output of the receiver is shifted to the long-wavelength section of the IR range with decreasing $\beta$, that is, with impaired visibility. At $\beta=0$ relation $q/C_0$ does not depend on $\lambda_i$, but its value at a distance of $L=3$ km is very small and it becomes significant only at distances $L \leq 0.2$ km. The higher the temperature of the object and the background is the more $\max q(\lambda_i)$ shifts into the short wavelength range. When temperature $T$ changes within the limits of 273ºK÷400ºK, and $S_u$ from 0.2 km to 30 km, max $q(\lambda_i)$ is within the limits $\sim (5\div12) \mu$m. That is, at high $T$ (and available $\Delta T$) objects can be detected by TID with receiver sensitivity in the range of $\lambda_i \sim 5 \mu$m. At low $T$ greater detection efficiency will be observed at longer operating waves. Fig. 3 illustrates the fact that with deterioration of visibility from $S_u \geq 20$ km to $S_u \leq 0.2$ km the probability of detecting objects for devices with short-wave sensitivity decreases and detection may not be possible at all, while for devices with long-wave sensitivity it may be most effective.

![Image](https://example.com/image.png)

**Figure 4.** Dependence of the detection range of the object by the thermal imager on the distance caused by the illumination curve $1 - L_T=0$; curve $2 - L_T=0.1$ km; curve $3 - L_T=0.3$ km; curve $4 - L_T=1$ km; curve $5 - L_T=5$ km.

3.2. *Optimization via the choice of the section of the atmosphere transmittance spectrum.*

When the TID operates with the sensitivity of the receivers, parts of the spectrum of which are combined with the "windows" of the transparency of the atmosphere, indicator $\alpha(\lambda)$ is small and can be neglected [17, 18]. In the case inequality $\alpha(\lambda) << L^{-1}$ is true and $\exp(-\alpha(\lambda) \cdot L) \approx 1$, signal-to-noise relation $q_2$ at the output of the receiver increases by $\exp(\alpha(\lambda) \cdot L)$ times.

3.3. "**Illumination**" of the observation zone by artificial sources of IR radiation.

Assume there are N IR ray diodes, whose operating wave lengths $\lambda_i$ are on the section of TID thermal sensitivity. Then signal-to-noise relation at the receiver output will increase by value of $q_{\text{for}}(r, \theta_i)$:

$$q_{\text{for}}(r, \theta_i) = C_0 \cdot \frac{\int_{\Delta \lambda} I(\lambda, \theta_i) \cdot \cos \theta_i \cdot \rho_i(\theta_i) \, d\lambda \cdot e^{-\alpha(\lambda) \cdot L \cdot r_i}}{L^2 r_i^2},$$

(8)

where $I(\lambda, \theta_i)$ – the spectral density of the radiant intensity of the i-th source;

$\rho_i(\theta_i)$ – the coefficient of infrared rays reflection from the object;

$\theta_i$ – the polar distance of the beam direction from the i-th source;

$r_i$ – the distance between the object of observation and the i-th radiation source.

In the general case, taking into account the "illumination", relation $q_i^*$ signal-to-noise is:

$$q_i^*(\lambda, T, \Delta T, \Delta \lambda, r, \theta_i) = q_i(\lambda, T, \Delta T, \Delta \lambda) + q_{\text{for}}(r, \theta_i).$$

(9)
When combining the spectral sensitivity of the receiver, the "transparency windows" of the atmosphere and the emission spectra of the ray diodes \( \alpha(\lambda) \ll L^{-1}, r_i^{-1} \) signal-to-noise relation \( q_s^2 \) is:

\[
q_s^2(\lambda, T, \Delta T, \Delta \lambda, r_i, \theta) = q_s^2(\hat{\lambda}, T, \Delta T, \Delta \lambda) + q_{2\text{nat}}(r_i, \theta),
\]

where \( q_{2\text{nat}}(r_i, \theta) = C_0 \cdot \sum_{i=1}^{n} \frac{I_r(\lambda) f(\theta) \cdot \cos \theta \cdot \rho(\theta)}{L^2} d\lambda \).

Without detailed calculation of \( q_{1\text{nath}} \) and \( q_{2\text{nath}} \), which is a separate problem, we can estimate the contribution of illumination to the detection range of an aircraft object. Solving equation (10) with respect to \( L \) at \( q_s^2 = 1 \), we have:

\[
L = \sqrt{L_T^2 + L_{\text{nat}}} ,
\]

where \( L_T = \left[ \frac{C_0 C_1 T^3 \cdot \Delta T \cdot \sum_{i=1}^{n} (-1)^i \cdot e^{-\lambda \cdot (x_i^4 + 4x_i^2 + 12x_i^2 + 24x_i + 24)}}{C_2} \right]^{1/2} \) – range of detection of TID object due to its thermal radiation without "illumination";

\[
L_{\text{nat}} = \left[ C_0 \cdot \sum_{i=1}^{n} \frac{I_r(\lambda, \theta) \cdot \cos \theta \cdot \rho(\theta)}{r_i^2} d\lambda \right]^{1/2} \] – increase in the detection range of the TID object due to additional "illumination" of the object (Figure 4).

It is easily seen that \( L_{\text{nat}} \) can vary widely, reaching a value predominant over \( L_T \) and can be the only factor in the detection of UAVs with low intrinsic thermal radiation. The detection range of the object can be increased by adjusting intensity \( I_r(\lambda) \). For the continuity of the detection zone, the searchlights are selected to the required power and pattern. Distance \( d \) between them is calculated based on the specified minimum height of the field overlap \( h_{\text{min}} \):

\[
d = 2h_{\text{min}} \cdot \tan \gamma ;
\]

where \( \gamma \) – the aperture angle of searchlight emission.

The active work of EMS sources is a factor in unmasking their positions, however, the placement of a significant number of infrared searchlights in a large area is at the same time a disorientation for enemy air reconnaissance.

The use of a large number of IR searchlights to illuminate UAVs operating in areas of the thermal sensitivity spectrum of TID and located over a large area is nothing more than an analogue of multi-position multistatic radar [36-44].

4. Conclusions.

1. With decreasing meteorological visibility \( S_w \) the maximum signal from the TID receiver is shifted to the long-wavelength part of the IR spectrum.

2. At low visibility \( (S_w \leq 0.2 \text{km}) \) TIDs with long-wavelength sensitivity in the IR range have advantages in object detection at long distances.

Surveillance devices with short-wave sensitivity in the IR range can be effective at short distances.

3. The use of infrared searchlights to illuminate the air surveillance zone, the combination of searchlight emission spectra, thermal sensitivity of TID and "windows of transparency" of the atmosphere can significantly increase the efficiency of UAV detection.
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