On the Radial Metallicity Gradient and Radial Migration Effect of the Galactic Disk

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Abstract

We study the radial metallicity gradient $\Delta[M/H]/\Delta R_g$ as a function of $[\text{Mg}/\text{Fe}]$ and $[Z]$ with the help of a guiding radius based on the Apache Point Observatory Galactic Evolution Experiment and Gaia and then analyze the radial migration effect on the radial metallicity gradient and metallicity-rotation gradient between the Galactic thin and thick disks. The derived trend of gradient $\Delta[M/H]/\Delta R_g$ versus $[\text{Mg}/\text{Fe}]$ shows a transition at $[\text{Mg}/\text{Fe}] \sim 0.18$ dex, below which the gradient is negative and varies a little as $[\text{Mg}/\text{Fe}]$ increases; however, it changes sharply in $[\text{Mg}/\text{Fe}]$ ranges of 0.16-0.18, above which the gradient increases linearly with increasing $[\text{Mg}/\text{Fe}]$, being a positive value $[\text{Mg}/\text{Fe}] \gtrsim 0.22$ dex. These positive gradients in the high-$[\text{Mg}/\text{Fe}]$ populations are found at $[Z] < 0.8$ kpc, and there are nearly no gradients toward higher $[Z]$. By comparing the metallicity distributions, the radial metallicity gradients $\Delta[M/H]/\Delta R$, and the metallicity-rotation gradients between the total sample and $[R - R_g] < 2$ kpc subsample (or $[R - R_g] > 2$ kpc subsample), we find that, for the thick disk, blurring flattens the gradient $\Delta[M/H]/\Delta R$ and favors metal-poor high-eccentricity stars. These stars are responsible for the measured positive metallicity-rotation gradient of the thick disk.

Key words: Galaxy: abundances – Galaxy: disk – Galaxy: evolution – Galaxy: formation

1. Introduction

The Milky Way disk has been suggested to host a thick disk, in addition to its thin disk, based on the results of geometric decomposition works (e.g., Gilmore & Reid 1983; Jurić et al. 2008; Jia et al. 2014). Generally, the thick disk is thought to be old as the thin disk (e.g., Bensby et al. 2005; Yoachim & Dalcanton 2008). Other age-related properties, such as $\alpha$-element abundances (e.g., Fuhrmann 1998; Bensby et al. 2003, 2005; Reddy et al. 2006; Haywood 2008; Adibekyan et al. 2011) and kinematics (Chiba & Beers 2000; Gilmore et al. 2002; Yoachim & Dalcanton 2005), are also found to be different from the thin disk. Although the formation mechanism of the thick disk is still debated, four kinds of scenarios are widely known so far: heating (e.g., Quinn et al. 1993), accretion (e.g., Abadi et al. 2003), a gas-rich merger (e.g., Brook et al. 2004; Broumaud et al. 2009), and radial migration (e.g., Schönrich & Binney 2009). In particular, the last one has attracted much attention because it could be triggered by the well-known non-axisymmetric structures of the Milky Way disk (such as spiral arms and bars). On the other hand, radial migration would alter the disk structure and chemical composition through churning (stars changing angular momentum) and blurring (stars conserving their angular momentum, Schönrich & Binney 2009), which makes the interpretation of the observational results complicated. In this respect, the study on the radial metallicity gradient, which records the enrichment history of stellar abundances at a given radial location, provides a good way to disentangle the radial migration effect on the chemical evolution of the Galactic disk.

The radial metallicity gradient has been well studied in previous works based on a variety of stellar tracers. Önal Tas et al. (2016) gave a detailed summary in their Table 1, where the thin disk has a negative gradient and the thick disk shows a flat or even positive gradient. Moreover, the overall disk gradient was found to gradually flattens toward high $[Z]$, which is proposed to be driven mainly by radial migration (Schönrich & McMillan 2017). Interestingly, the metallicity-rotation gradient is also found to be negative for the thin disk but positive for the thick disk (e.g., Adibekyan et al. 2013; Allende Prieto et al. 2016), which is also linked with the radial metallicity gradient. It has been suggested that the negative (positive) metallicity-rotation gradients is driven by the negative (positive) radial metallicity gradient for thin (thick) disk stars due to blurring effect (Vera-Ciro et al. 2014; Allende Prieto et al. 2016; Schönrich & McMillan 2017). In this case, a thick disk star born in the inner disk with epicyclic motion would tend to be metal poor due to the positive radial metallicity gradient. Meanwhile, its current location in the solar neighborhood is near the orbit’s apo-center and thus tends to rotate slower. This naturally results in a positive metallicity-rotation gradient for thick disk stars. Supporting this scenario, Toyouchi & Chiba (2014) reported that the measured radial metallicity gradients for $\alpha$-enhanced (thick disk) populations are positive.

Note that Toyouchi & Chiba (2014) adopted the guiding radius $R_g$ instead of current Galactocentric distance $R$, since the gradient, if measured with $R$, likely suffers from the radial migration effect and the usage of the guiding radius $R_g$ can diminish the blurring effect. However, the elemental abundances in Toyouchi & Chiba (2014) are based on low-resolution spectra of the Sloan Digital Sky Survey (SDSS), and distances are based on photometric methods. These can be greatly improved using recently released high-quality data. Investigating the radial metallicity gradient by taking into account the guiding radius and the metallicity-rotation gradients based on accurate elemental abundances and radial velocity from high-resolution spectra provided by the Apache Point Observatory Galactic Evolution Experiment (APOGEE, Majewski et al. 2017) survey is of much interest. Additionally, the wealth astrometric information from Gaia (Gaia Collaboration et al. 2016) enables us to perform a statistical analysis on the radial metallicity gradient with the aid of the guiding radius. Specifically, we aim to derive the radial metallicity gradient as
a function of $[\text{Mg/Fe}]$ and $|Z|$ and analyze the effect of radial migration on the radial metallicity gradient and metallicity-rotation gradient between the Galactic thin and thick disks.

2. Data

APOGEE is a high-resolution ($R \sim 22,500$), near-infrared H-band (1.5–1.7 $\mu$m) spectroscopic survey targeting red giants selected with a cut of $(J - K)_{0} \geq 0.5$ (Zasowski et al. 2013). It provides precise radial velocities, stellar parameters, and elemental abundances through self-designed pipelines (Holtzman et al. 2015; Nidever et al. 2015; García Pérez et al. 2016). Recently, the second Gaia data release (DR2, Gaia Collaboration et al. 2018) provides parallaxes (distances) and proper motions for billions of stars, which contains most stars in the APOGEE/SDSS DR14 survey (Abolfathi et al. 2018). Our sample of stars is selected by cross-matching between APOGEE DR14 and Gaia DR2.

The distances in Galactic cylindrical coordinates $R$ and $Z$ are calculated using parallaxes from Gaia DR2, and we adopt the solar position of 8.0 kpc (Reid 1993). The spatial velocities $(U,V,W)$ in left-hand Cartesian coordinates are calculated from radial velocities from APOGEE DR14, with the distances and proper motions from Gaia DR2. In the calculation, we restrict stars with the relative error of parallax less than 20% to most stars. We correct the solar motion with respect to the local standard of rest of $(U,V,W)_{0} = (-10.00, +5.25, +7.17)$ (Dehnen & Binney 1998) and adopt coordinate transformation to obtain the cylindrical coordinate velocities $V_{r}$ and $V_{\phi}$. The orbital parameters, peri-center ($R_{p}$), apo-center ($R_{a}$), and eccentricity ($e = (R_{a} - R_{p})/(R_{a} + R_{p})$) are calculated with galpy (Bovy 2015) under the potential of MWPotential2014.

Then, the guiding radius ($R_{g}$), at which the minimum of effective potential occurs, is calculated under this potential through the following equation:

$$\frac{V_{\text{circ}}^{2}}{R_{g}} = \frac{L_{\phi}^{2}}{R_{g}^{3}},$$

where $V_{\text{circ}}$ is the circular velocity in this potential and $L_{\phi}$ is the angular momentum, which is a constant of motion in axisymmetric potential. The guiding radius identifies the radius of the circular orbit with an angular momentum of $L_{\phi}$. From the probability point of view, this radius better represents the Galactocentric distance at which a star was born than $R$ since many stars do not have circular orbits (Boeche et al. 2013). We then expect that a star with $R - R_{g} > 0$ ($R - R_{g} < 0$) has moved outward (inward) to the current location after it was born. In addition, we exclude stars with $[\text{M/H}]$ of less than $-1.0$ dex and stars with a total velocity of more than 150 km s$^{-1}$ to diminish the contamination from the halo. We also exclude stars at the fields of $(l, |b|) < (10^\circ, 10^\circ)$ to remove bulge stars. Finally, we have 147,794 stars for the following analysis. The $R$ versus $|Z|$ plane and the $T_{\text{eff}}$ versus log $g$ diagram of the sample are shown in Figure 1. This sample comprises giants with effective temperatures in the range of 3500–5600 K, and it covers a wide spatial range of $2 < R < 15$ kpc and $0 < |Z| < 5$ kpc.

Figure 1. Top panel: the spatial distribution of the sample stars in the Galactic cylindrical coordinate. Bottom panel: the $T_{\text{eff}}$ vs. log $g$ diagram for the sample stars.

3. Analysis and Results

3.1. Radial Metallicity Gradient as a Function of $[\text{Mg/Fe}]$

In order to investigate the variation of metallicity gradient with $[\text{Mg/Fe}]$, we illustrate the $R_{g}$ versus $[\text{Mg/Fe}]$ diagrams for 21 $[\text{Mg/Fe}]$ bins in Figure 2. The bin size is arbitrarily set so that enough stars can be used for the statistical analysis. In every $[\text{Mg/Fe}]$ bin, we first divide $R_{g}$ into 50 equal-length intervals and then adjust adjacent intervals to ensure the number of stars in every final interval is larger than 20. In Figure 2, black dots indicate the means of metallicities, and the corresponding error bars represent the standard deviations of the means. Then, we adopt a linear regression to the dots in every $[\text{Mg/Fe}]$ bin and obtain the radial metallicity gradient. The resulting gradient varies from $-0.045$ dex/kpc to $+0.030$ dex/kpc as $[\text{Mg/Fe}]$ increases from $-0.20$ to $+0.40$ dex, which is illustrated in Figure 3. Figure 3 shows that the gradient for the low-$[\text{Mg/Fe}]$ population with $[\text{Mg/Fe}] < 0.16$ dex is negative and varies slightly as $[\text{Mg/Fe}]$ increases. Then, the gradient changes sharply at $[\text{Mg/Fe}]$ around 0.18 dex, after which the gradient for the high-$[\text{Mg/Fe}]$ population rises steadily and becomes positive at $[\text{Mg/Fe}] \geq 0.22$. The absolute values of Pearson correlation coefficients are larger than 0.67 with the $p$ values less than 0.001 for bins of $[\text{Mg/Fe}] \leq 0.18$ dex and bins of $[\text{Mg/Fe}] \geq 0.26$ dex, indicating strong evidence of correlations between metallicity and $R_{g}$. For the middle $[\text{Mg/Fe}]$ bin of 0.24-0.26 dex, the coefficient is of 0.39 with a $p$ value of 0.017, indicating evidence of correlation between metallicity and $R_{g}$. However, for the $[\text{Mg/Fe}]$ bins of 0.18-0.24 dex, the coefficients are in the range of 0.16-0.22 with the $p$ values larger than 0.1, indicating no significant evidence for such correlations. Note that the blue arrow in Figure 3 indicates a transition of the radial metallicity gradient at $[\text{Mg/Fe}] \sim 0.18$. In light of the fact that $[\text{Mg/Fe}]$ is a proxy for age, this transition implies the separation between the thick disk and the thin disk because the former is typically older than the latter. In short, the thick disk that is represented
by stars with $\text{[Mg/Fe]} \geq 0.18$ has a linear trend in the gradient versus the $\text{[Mg/Fe]}$ plane, and the thin disk characterized by $\text{[Mg/Fe]} < 0.18$ appears to be relatively complicated. This difference indicates that the thin disk and the thick disk are distinct stellar populations.

Our data is consistent with the results summarized in Table 1 of Önal Tas et al. (2016) in which the thin disk has a negative radial metallicity gradient, whereas the thick disk has a flat or positive gradient. But the measured values of radial metallicity gradients for thick disk stars are very different in the literature, varying from a positive gradient (Carrell et al. 2012; Casagrande et al. 2012; Önal Tas et al. 2016) to nearly no gradient (Cheng et al. 2012; Boeche et al. 2013, 2014; Mikolaitis et al. 2014; Plevere et al. 2015; Xiang et al. 2015; Anders et al. 2017) and even a negative gradient (Hayden et al. 2014). These discrepancies may be caused by the sample biases. As pointed out in Anders et al. (2017), the gradient could depend on, e.g., the sample’s spatial location, age distributions, insufficient statistics, and selection biases. These factors are hardly to qualify among the works, and thus it is not easy to compare our results with other observational works based on a different data sample and different tracers. Instead, we prefer to compare our results with theoretical works. In this respect, Kawata et al. (2018) performed $N$-body simulations to the APOGEE data and found that the initial radial metallicity gradient of the thick disk progenitor should not be negative, but should be either flat or even positive. Moreover, some Galactic chemical evolution models (e.g., Chiappini et al. 2001; Schönrich & McMillan 2017) suggest that the inside-out formation of the Galaxy gives a positive radial gradient for thick disk stars. Our results support these theoretical works by providing evidence that the radial metallicity gradient of the Galactic disk depends on the $\text{[Mg/Fe]}$ ratio, and the thick disk has a flat or positive radial metallicity gradient.

3.2. The Radial Metallicity Gradients at Different $|Z|$ Intervals

It is interesting to investigate the dependence of the relation between the radial metallicity gradient and the $\text{[Mg/Fe]}$ ratio.
on $|Z|$ in light of the fact that the thin and thick disks dominate at different $|Z|$ ranges. For this purpose, we split $|Z|$ into six bins: $|Z| < 0.2$ kpc, $0.2 < |Z| < 0.5$ kpc, $0.5 < |Z| < 0.8$ kpc, $0.8 < |Z| < 1.1$ kpc, $1.1 < |Z| < 1.5$ kpc, and $|Z| > 1.5$ kpc. The relations of radial metallicity gradients versus [Mg/Fe] ratios at different $|Z|$ bins are presented in Figure 4. It shows that the negative gradient for the low-[Mg/Fe] sequence remains in all $|Z|$ bins, while the positive radial metallicity gradient of the high-[Mg/Fe] sequence with [Mg/Fe] $> 0.18$ dex only exists at $|Z| < 0.8$ kpc, and there is nearly no gradient in larger $|Z|$ bins. It should be noted that this trend disagrees with the result in Toyouchi & Chiba (2014), who found that the positive gradient is nearly unchanged as $|Z|$ increases (see their Figure 4).

3.3. Radial Metallicity Gradient between the Thin and the Thick Disks

It may be too simple to separate the thin disk and the thick disk based on the [Mg/Fe] ratio at 0.18 dex only. We adopt a conventional way to divide them in the chemical plane, as shown in Figure 5. A separation adopted in the high-resolution study by Adibekyan et al. (2011) is illustrated by the yellow line. It is clear that this separation is inappropriate for this work. Instead, we adopt a varying [Mg/Fe] ratio as a function of [M/H] by passing the three points of $(-1.0, 0.18)$, $(-0.4, 0.18)$, and $(-0.6, 0.8)$ in the [M/H] versus [Mg/Fe] diagram, which is presented by a black solid line in Figure 5. We shift this line by 0.02 dex in [Mg/Fe] upward (red dash line) and downward (blue dash line) in order to examine if the derived result depends on the separation criterion between the thin and thick disk. Note that the red line defines a relatively clean thick disk star population, and the blue line separates a relatively clean thin disk star population.

Based on the new separations, similar procedures are adopted to derive the radial metallicity gradient as functions of [Mg/Fe] for the thin disk and the thick disk populations in Figure 6. From the top panel to the bottom panel, the results correspond to the separations represented by the black, red, and blue lines, respectively. Compared with Figure 3, a prominent feature of the top panel of this figure is that the thick disk presents a flat gradient at the low-[Mg/Fe] end and then subsequently rises linearly to the high-[Mg/Fe] end. Similar features also hold in the middle panel that correspond to a...
separation containing a relatively clean sample of thick disk stars. However, the bottom panel shows that the flat gradients in the [Mg/Fe] range of 0.12–0.18 dex for the thick disk have been affected by pollution of thin disk stars and appear negative at [Mg/Fe] \sim 0.17 dex. This suggests that adopting an improper chemical definition of the thick disk would affect the derived radial metallicity gradient. Besides, we notice an interesting feature, which is that the gradient of the thin disk seems to transit continuously into the thick disk by following the linearly rising trend. This feature somewhat coincides with the finding that the structural parameters smoothly transit in the chemical plane (Bovy et al. 2012, 2016).

3.4. Radial Migration Effect

One superiority of using the guiding radius to derive radial metallicity gradient is that it can diminish the blurring effect as it conserves the angular momentum. We expect that the quantity of \( R - R_g \) could somewhat reflect the radial migration effect, and this quantity would be a simple and first approximation to help us disentangle how the radial migration affect the observation results. We assume that a subsample of stars with \( |R - R_g| < 2 \) kpc would suffer little from the radial migration effect (blurring), and the remaining subsample with \( |R - R_g| > 2 \) kpc is supposed to include the migration stars. In light of this, we expect that the footprint of the radial migration effect can be traced by comparing the results derived from the \( |R - R_g| < 2 \) kpc subsample (or \( |R - R_g| > 2 \) kpc subsample) and the total sample. We note that the stars with \( |R - R_g| > 2 \) kpc tend to move on highly eccentric orbits. We first investigate the differences in the metallicity distributions between the subsample of \( |R - R_g| > 2 \) kpc and the total sample for the thin disk and the thick disk in Figure 7. In the top panel of this figure, metal-poor stars are over-populated in the \( |R - R_g| > 2 \) kpc sample compared to the total sample. This implies that the migration favors the metal-poor for thick disk population, while the bottom panel shows that the metallicity distributions are similar between these two samples, which means that the migration does not play a significant role in shaping the thin disk’s metallicity distribution.

Second, we compare the radial metallicity gradients \( \Delta \text{[M/H]} / \Delta R \) between the \( |R - R_g| < 2 \) kpc subsample and the total sample using Galactocentric distance \( R \). We find that the thin disk gives a similar negative gradient between these two samples. However, the gradient \( \Delta \text{[M/H]} / \Delta R \) in the thick disk becomes flat, changing from 0.016 \pm 0.003 dex/kpc to 0.006 \pm 0.003 dex/kpc when moving from the \( |R - R_g| < 2 \) kpc subsample to the total sample. Considering the total sample contains migration stars with \( |R - R_g| > 2 \) kpc, this is evidence that radial migration flattens the radial metallicity gradient \( \Delta \text{[M/H]} / \Delta R \).

Finally, we investigate the differences in the metallicity-rotation gradients between the \( |R - R_g| < 2 \) kpc subsample and the total sample in Figure 8. The total sample gives a positive gradient of 26.5 km s\(^{-1}\) dex\(^{-1}\) and a negative gradient of \(-6.4 \text{ km s}^{-1} \text{ dex}^{-1}\) for thick disk and thin disk, respectively. However, the gradient changes from 26.5 km s\(^{-1}\) dex\(^{-1}\) to 3.8 km s\(^{-1}\) dex\(^{-1}\) when using \( |R - R_g| < 2 \) kpc subsample for the thick disk, which is close to the gradient of \(-6.4 \text{ km s}^{-1} \text{ dex}^{-1}\) for the thin disk. Note that the only difference between these two samples is the absence of some metal-poor stars with high eccentricity in the \( |R - R_g| < 2 \) kpc subsample. Therefore, the change in the metallicity-rotation gradient for the thick disk implies that the metal-poor high-eccentricity stars are responsible for the thick disk’s positive \( \Delta V / \Delta \text{[M/H]} \). This is an observational signature in which blurring contributes to the positive metallicity-rotation gradient of the thick disk.

4. Implications on the Formation and Evolution of the Disk

Before we discuss the implications of our results on the formation and evolution of the disk, we note that the usage of
the guiding radius, rather than the Galactocentric distance $R$, may introduce a bias against metal-rich inner disk stars that move on nearly circular orbits, as proposed by Boeche et al. (2013). This bias arises only when the eccentricity of the star is not well-sampled at small $R_e$. Due to the large sample size in our work provided by APOGEE and Gaia, the eccentricities are well-sampled at $R_e \gtrsim 4$ kpc, and even at smaller $R_e$, a fraction of low-eccentricity stars still exist. In view of this, we expect this bias would not affect much on our measured radial metallicity gradients. Moreover, in the small $R_e$ region, the potential missing stars are supposed to be, on average, metal-rich (Boeche et al. 2013) and should have relatively low-[Mg/Fe] ratios, thus we consider this bias in particular has less effect on the thick disk (high-[Mg/Fe] star population).

The variations of the radial metallicity gradient with [Mg/Fe] and $|Z|$ provide a way to infer the star formation history of the disk. As shown in Figures 3 and 6, the thin disk shows a negative radial metallicity gradient, whereas the thick disk presents flat and positive gradients. The negative gradient of the thin disk is usually understood as a natural result of the inside-out formation scenario (e.g., Chiappini et al. 2001), i.e., the star formation rate is higher in the inner disk than the outer disk. The positive gradient of the thick disk can also be achieved in this scenario under reasonable assumptions, which was recently suggested by Schönrich & McMillan (2017). They showed an example of the achieved positive radial metallicity gradient for star-forming gas by adopting high central gas-loss rates and re-accretion of one quarter of the lost enriched material in conjunction with the inside-out formation.

However, the results presented in Section 3.2 suggest that the positive radial metallicity gradients of the thick disk only exist in $|Z| < 0.8$ kpc, and the gradients found to be flattened at larger $|Z|$ intervals complicates this formation scenario. These features seems to be reconciled with the upside-down disk formation fashion (e.g., Bird et al. 2013), i.e., stars first forming in a geometrically thick layer and then in thinner layers. A recent work from Kawata et al. (2018) suggested that the thick disk forming in an upside-down fashion could have a different initial radial metallicity gradient, even including a negative one, and then the effect of the inside-out formation produced an overall flat or positive gradient when the formation was completed. Another work by Fragkoudi et al. (2017) supports this argument. They suggested that the inner disk star populations arose from an interstellar medium that has a mostly flat radial metallicity gradient forming in an upside-down fashion. These works support a picture where the Galactic disk formed in an inside-out and upside-down fashion, in which stars first formed in the thick layer (or larger $|Z|$) had flat radial metallicity gradients, and the subsequently formed stars in the thin layer (smaller $|Z|$) obtained their positive gradients through the inside-out formation fashion, thus the gradients are positive at low $|Z|$ and flat at larger $|Z|$. Therefore, our results can be understood from the inside-out and upside-down disk formation scenario.

5. Summary and Conclusions

In this work, we investigate the radial metallicity gradient between the thin and thick disks, with the help of the guiding radius, and analyze the effect of radial migration on the derived radial metallicity gradient and the metallicity-rotation gradient based on a large and high precision data from Gaia and APOGEE. To infer the Galactic disk formation history, we derive the radial metallicity gradient $\Delta[M/H]/\Delta R_g$ as a function of [Mg/Fe] and $|Z|$. We find that the radial metallicity gradient of the low-[Mg/Fe] population ($\text{[Mg/Fe]} < 0.16$ dex) is negative and has small variations with [Mg/Fe], and this gradient changes sharply until [Mg/Fe] reaches 0.18 dex, after which the gradient rises linearly and becomes positive at [Mg/Fe] $\geq 0.22$. The positive gradients in the high-[Mg/Fe] population are found to limit at $|Z| < 0.8$ kpc only, and there is nearly no gradient toward higher $|Z|$. The above results imply that the Galactic disk formed in an inside-out and upside-down fashion. Moreover, the different trends of $\Delta[M/H]/\Delta R_g$ versus [Mg/Fe] between the thick disk and thin disk, which are characterized by the high-[Mg/Fe] population ($\text{[Mg/Fe]} > 0.18$ dex) and the low-[Mg/Fe] population ($\text{[Mg/Fe]} < 0.18$ dex), respectively, indicate that the transition between them occurs at [Mg/Fe] $\sim 0.18$ dex. With a more specific division of the thin and thick disks in the chemical plane, we still find that the trends of $\Delta[M/H]/\Delta R_g$ versus [Mg/Fe] are rather different between the thin and thick disks, which indicates that the thin disk and thick disk are two distinct star populations. In the meantime, the thick disk clearly presented a flat or positive gradients depending on the [Mg/Fe] ratio.

In order to study the radial migration effect, we adopt a quantity, $|R - R_e|$, to reflect the blurring effect since blurring does not change on $R_e$ but does on $R$. A subsample with $|R - R_e| < 2$ kpc is thought to suffer not from the blurring effect, and the remaining subsample with $|R - R_e| > 2$ kpc is considered to contain migration stars. By comparing the metallicity distributions, the radial metallicity gradients $\Delta[M/H]/\Delta R$, and the metallicity-rotation gradients between the total sample and the alternative two above sub-samples, we find that blurring process flattens the gradient $\Delta[M/H]/\Delta R$ and favors metal-poor and high-eccentricity stars for the thick disk. These stars are responsible for the measured positive metallicity-rotation gradient in the thick disk.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure8}
\caption{Metallicity-rotation diagram for the total sample (marked by squares) and the $|R - R_e| < 2$ kpc subsample (marked by crosses). The thick disk stars are highlighted with black lines to better illustrate the change in the gradient $\Delta V_r/\Delta [M/H]$.}
\end{figure}
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