Abstract—Using only electro-optic modulators, we generate a 41-line 10-GHz Gaussian-shaped optical frequency comb. We use this comb to demonstrate apodized microwave photonic filters with greater than 43-dB sidelobe suppression without the need for a pulse shaper.

Index Terms—Microwave photonics, optical signal processing, phase modulation, filters.

I. INTRODUCTION

Phase modulated continuous-wave (CW) laser frequency combs have seen wide use in various applications such as wavelength division multiplexing (WDM) networks [1], optical arbitrary waveform generation (O-AWG) [2], and rapid arbitrary millimeter wave generation [3]. Using such optical frequency comb as a multiple carrier optical source offers new potential for achieving complex and tunable microwave photonic filters [4]. References [5] and [6] used a line-by-line pulse shaper to manipulate the amplitudes of individual spectral lines to obtain a carefully apodized Gaussian shape for achieving clean passband shapes with large sidelobe suppression, and also demonstrated a novel mechanism that allows tuning of the filter largely independent of passband shape. In reference [5], the initial comb has an irregular power spectrum. However reference [6] starts with our newly developed comb with record flatness and a large number of lines (38-lines within 1-dB variation out of a total 61 lines [7]), which eases pulse shaper requirements for implementation of high quality RF photonic filters. Although the generation of flat-topped optical frequency combs [8] [9] has drawn much attention, little work has been done to directly generate Gaussian-shaped optical frequency combs. In one report, Hisatake et al. demonstrated Gaussian-shaped comb generation based on spatial convolution of a slit and a periodically moving optical spot in a system based on electro-optic deflectors [10]. Here we introduce for the first time a directly generated 10-GHz Gaussian-shaped comb using only electro-optic modulators without the need for a pulse shaper. Therefore the implementation of RF photonic filters is much simplified, with lower optical loss and higher signal to noise ratio. In our current experiment, by employing a 41-line 10 GHz spaced directly generated Gaussian-shaped comb (37 lines closely matched to a Gaussian shape across a dynamic range of 20 dB), we implement filters with 43.2 dB sidelobe suppression. The results are improved over that reported in [5] and [6] and with a much more compact set-up.

II. PRINCIPLE OF MICROWAVE PHOTONIC FILTERS

![Fig. 1. Experimental setup for Gaussian-shaped comb generation. TA: tunable amplifier; VA: variable attenuator; PS: phase shifter; red dashed module: quasi-quadratic phase generation.](image)

Fig. 1 shows the experimental setup of the 10-GHz Gaussian-shaped comb generator, which consists of three IMs and two PMs. We operate the RF oscillator at 10 GHz. At 10 GHz, the $V_{\pi}$ is ~9 V for the IM’s and ~3 V for the PM’s. The RF voltages delivered to IM1 and IM2 are both 0.5 $V_{\pi}$ zero to peak, and the RF voltage to IM3 is $V_{\pi}$. We cascade two phase modulators at their maximum RF input power (30 dBm) to double the total modulation index seen by the pulse and increase the number of comb lines.

The Gaussian-shaped comb generation mechanism is based on time-to-frequency mapping theory, where quadratic and periodic temporal phase causes the spectral envelope to mimic the input intensity profile to the phase modulators [11] [12] [13]. So for generating a Gaussian-shaped comb, the following two requirements should be met:

(i) Apply a quadratic phase. Applying a purely quadratic, periodic temporal phase is difficult, so here we apply a “quasi-quadratic” phase by combining the first and second harmonic of the sinusoidal drive signal with a power ratio of 24-dB and phase shift of 180° selected to suppress the 4th order term of the cosine expansion of the phase - refer to the red dashed box in Fig. 1. This substantially improves the
approximation to the target quadratic phase profile [7].

(ii) Generate a Gaussian-shaped pulse. IM1 and IM2 are both biased at 0.5 V with RF drive amplitude 0.5 V. IM3 is biased at 0 (maximum transmission) with RF drive amplitude V. We can get a flat-topped pulse with a series combination of IM1 and IM2 (without the black module in Fig. 1) and a very close approximation to a Gaussian pulse with the series combination of all three IMs as shown in Fig. 2(a). After applying the quasi-quadratic phase as described in (i), modeling indicates it is possible to obtain flat-topped or Gaussian-shaped combs as shown in Fig. 2 (b)-(c).

\[
H(\omega_{RF}) \propto \sum_{n=0}^{N-1} e^{i n D 2\pi f_{RF}}
\]

where \(N\) is the total number of the taps, \(e^{i} \) is the optical intensity of the \(n^\text{th}\) tap, \(D\) is the fiber dispersion, \(\Delta f\) is the repetition frequency of the optical comb, \(10 \text{ GHz}\) in our experiment, \(D 2\pi\Delta f\) is the tap delay between two adjacent taps, 96-ps in our experiment. The free spectral range (FSR) is the inverse of the tap delay, which can be tuned by changing the length of DCF.

IV. EXPERIMENTAL RESULTS

Fig. 4 shows the experimental results. First, we turn off TA3 (in Fig. 1). Fig. 4(a) shows a 50-line 10-GHz flat-topped optical frequency comb spectrum measured at the photodiode (in Fig. 3). After turning on TA3, Fig. 4(b) shows a 41-line 10-GHz Gaussian-shaped optical frequency comb spectrum measured at the photodiode; the EDFA is adjusted to set the average power at the photodiode to 4.3 dBm, as used with the flat-topped comb. The standard deviation of the comb line amplitudes from a best-fit Gaussian profile is 0.42 dB for the central 37 lines and 0.26 dB for the central 35 lines, with an excellent match over 37 spectral lines across a 20-dB dynamic range. After applying the comb to our filter setup, we measured the filter transfer function with a network analyzer. We compare our experimental results with simulations that include an RF calibration factor which accounts for cable loss, modulator transfer function and the photodiode frequency response (high frequency roll-off). The RF calibration data can be obtained by measuring the link frequency response without the dispersion compensating fiber [5]. Fig. 4(c) shows the measured (blue) and simulated (red, after calibration) filter transfer functions using the flat-topped comb. At baseband, the filter has a 3-dB bandwidth of 100 MHz, with 18.1 dB sidelobe suppression. Modeling (based on the measured optical power spectrum) indicates the filter has a 3-dB bandwidth of 115 MHz and 230 MHz with 14.4 dB and 15.43 dB sidelobe suppression at the baseband and passband respectively, in very close agreements with our experiment. Fig. 4(d) shows the measured (blue) and simulated (red, after calibration) filter transfer functions using the above Gaussian-shaped comb. At the baseband, the filter has a 3-dB bandwidth of 120 MHz, with 43.2 dB sidelobe suppression.
The 10.4 GHz passband has a 3-dB bandwidth of 330 MHz with 35.3 dB sidelobe suppression. Modeling indicates the filter has a 3-dB bandwidth of 165 MHz and 330 MHz with 41.1 dB and 34.9 dB sidelobe suppression at baseband and the passband respectively, in very close agreements with our experiment. The filter FSR is determined by the length of DCF fiber. In our experiment, the filter FSRRs with both comb shapes are 10.4 GHz in accordance with the 96-ps tap delays. By adding or decreasing the length of DCF we can change FSR, red-shifting or blue-shifting the filter pass band frequency accordingly.

V. CONCLUSION

For the first time, we introduce a 10-GHz Gaussian-shaped optical frequency comb generation (37 lines across a 20 dB dynamic range out of a total 41 lines) using only electro-optic modulators. Based on this directly generated Gaussian-shaped optical frequency comb, we demonstrate 43.2 dB high sidelobe suppression microwave photonic filters. Because a line-by-line pulse shaper is no longer required, the experimental implementation is greatly simplified. The filter FSR can be tuned by changing the length of DCF. Also our directly generated Gaussian-shaped comb is fully compatible with the novel tuning approach, based on varying optical delay in an interferometer structure, demonstrated in [5] [6].

ACKNOWLEDGMENT

We would like to thank Dr. Victor Torres-Company and Dr. Li Xu for valuable discussions.

REFERENCES

[1] N. Takachio, H. Suzuki, M. Fujiwara, J. Kani, K. Iwatsuki, H. Yamada, T. Shibata, and T. Kitoh, “Wide area gigabit access network based on 12.5 GHz spaced 256 channel super-dense WDM technologies,” Electron. Lett., vol. 37, no. 5, pp. 309–311, 2001.
[2] Z. Jiang, C. B. Huang, D. E. Leaird, and A. M. Weiner, “Optical arbitrary waveform processing of more than 100 spectral comb lines,” Nature Photon. 1, 463-467 (2007).
[3] C.-B. Huang, D. E. Leaird, A. M. Weiner, “Time-multiplexed photonically enabled radio-frequency arbitrary waveform generation with 100 ps transitions,” Opt. Lett., vol. 32, no. 22, pp. 3242-3244, 2007.
[4] J. Capmany, B. Ortega, D. Pastor, and S. Sales, “Discrete-time optical processing of microwave signals,” J. Lightwave Technol. 23, 702- (2005)
[5] E. Hamidi, D. E. Leaird, and A. M. Weiner, “Tunable programmable microwave photonic filters based on an optical frequency comb,” IEEE Transactions on Microwave Theory and Techniques, vol. 58 , no. 11, Nov. 2010.
[6] E. Hamid, R. Wu, V. R. Supradeepa, C. M. Long, D. E. Leaird, and A. M. Weiner, “Tunable radio frequency photonic filter based on intensity modulation of optical combs,” IEEE International Topical Meeting on Microwave Photonics, Montréal, Canada, October 5-9, 2010
[7] Rui Wu, V. R. Supradeepa, Christopher M. Long, Daniel E. Leaird, and Andrew M. Weiner, "Generation of very flat optical frequency combs from continuous-wave lasers using cascaded intensity and phase modulators driven by tailored radio frequency waveforms," Opt. Lett. 35, 2324-2326 (2010)
[8] T. Yamamoto, T. Komukai, K. Suzuki, and A. Takada, "Multicarrier light source with flattened spectrum using phase modulators and dispersion medium," Lightwave Technol. 27, 4297-4305(2009)
[9] T. Sakamoto, T. Kawanishi, and M. Itatsumi, "Widely wavelength-tunable ultra-flat frequency comb generation using conventional dual-drive Mach-Zehnder modulator," Electron. Lett. vol. 43, no. 19, pp 1039-1040, (2007)
[10] S. Hisatake, K. Tada, and T. Nagatsuma, “Generation of an optical frequency comb with a Gaussian spectrum using a linear time-to-space mapping system,” Opt. Express 18, 4748-4757 (2010)
[11] V. Torres-Company, J. Lancis, and P. Andrews, “Lossless equalization of frequency combs,” Opt. Lett. 33, 1822-1824 (2008)
[12] J. Azana, “Time-to-frequency conversion using a single time lens”, Opt. Comm. vol 217, pp. 205-209 (2003)
[13] J. Howe and C. Xu, “Ultrafast optical signal processing based upon space-time dualities,” J. Lightwave Technol. 24, 2649- (2006)