A series-resonant inverter with extended topology and pulse-density-modulation control for induction heating applications

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ABSTRACT
This paper presents a series-resonant inverter (SRI) with an extended topology using a pulse-density modulation (PDM) control method. Theoretical analysis shows that the use of the SRI with extended topology and the PDM control (extended PDM-SRI) allows reducing the fluctuation of the SRI output current by more than 40% at the quality factor of 5 compared to a conventional SRI with the traditional PDM control. To eliminate drawbacks of the extended PDM-SRI, specificities of PDM switching sequences to ensure the zero-voltage-switching (ZVS) operation are discussed in detail, and a solution to the voltage imbalance across the capacitors of the extended topology is proposed. Simulation analysis of the extended PDM-SRI confirmed the effectiveness of using the proposed solutions to eliminate the drawbacks. The feasibility of the proposed SRI is confirmed by testing on a 2.2 kW experimental setup.

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1. INTRODUCTION
Recently, the pulse-density modulation (PDM) control method [1]–[6] has been widely applied as a transistor converter current control method for many applications such as induction heating [1], [2], [7]–[10] and many others [3]–[6], [11]–[13]. In comparison with other control methods, such as pulse-width modulation, pulse-frequency modulation (PFM), or phase-shift control, the PDM control in the converters of induction heating equipment based on a series-resonant inverter (SRI) allows SRI transistors to operate with zero-voltage switching (ZVS) and quasi-zero-current switching (quasi-ZCS). As a result, high-frequency switching operation can be performed, switching losses and a surge voltage can be reduced, and the structure of induction heating equipment can be simplified. Despite the advantages of this method for the SRI, using the PDM control also has disadvantages; the main is that the amplitude of the SRI output current fluctuates. The fluctuation influences the maximum current through the SRI transistors, the maximum voltage across the resonant capacitor, and the required dead-time between the control signals of the SRI transistors. And the lower the value of the quality factor of a resonant circuit is, the higher the fluctuation is.

The basic idea of the PDM control method is that the SRI produces injection and free-wheeling intervals [7]–[9]. The output current is regulated by varying the duration of these intervals. In the traditional PDM control the duration of the injection and free-wheeling intervals is an integer multiple of the SRI output voltage period. The same pulse density and different amplitude fluctuations can be achieved with regular and irregular PDM controls [14]–[16]. The use of the irregular PDM control compared to the regular one allows to obtain lower fluctuations, but they are still significant.
In order to reduce the amplitude fluctuations and make the PDM control method more suitable for the SRI with a low value of a load quality factor, various enhanced PDM controls have been proposed [1], [2], [3], [6], [17], [18]. The general idea of these controls is that the duration of both the injection and free-wheeling intervals or just the injection interval is an integer multiple of the half-period of the SRI output voltage. When both the injection and free-wheeling intervals are integers multiple of half-period of the SRI output voltage, the voltage contains a direct current (DC) component [1]–[3]. This is not very suitable if a matching transformer is required, because a magnetizing current appears in the matching transformer due to the DC component. To avoid the influence of this component, Esteve et al. [1] used a blocking capacitor. But there also appears an unbalance in the inverter transistors’ switching loss. To avoid this unbalance, both half-bridges must operate alternatively during each enhanced PDM period. The switching sequence of the enhanced PDM can be further evenly distributed; this results in an additional reduction in current fluctuations [6], [17]. In both cases, the sign of the DC-component will alternate depending on the voltage sequence; as a result, the blocking capacitor will not be effective, and as a consequence, the matching transformer must be rated for a frequency lower than the operating one. When only the injection interval is an integer multiple of half-period of the voltage, the voltage does not contain the DC component. Still, fluctuations are not significantly lower compared to the traditional PDM control method [18].

Combined control methods based on the PDM control have been proposed [19]–[22]. A hybrid control method based on the PDM and PFM controls has been proposed for corona discharge treatment [19]. This method uses the regular PDM control, so if being applied in SRIs for induction heating applications, the amplitude fluctuations of the current will be significant. Shen et al. in [20], Namadmalan [21], the authors used the phase-shift and PDM controls for SRIs, where former acts between PDM patterns to provide more continuous/smooth power regulation. However, the mentioned method does not allow reducing the amplitude fluctuations. Herasymenko in [22], another combined control method based on the phase-shift and PDM controls is proposed. In this method, the current regulation for pulse density in the range from 0.5 to 1 is provided by only the traditional PDM control, and in the range from 0 to 0.5 – by the phase-shift control and the constant pulse density (equal to 0.5) of the PDM pattern. Disadvantages of this approach are that the use of the phase-shift control method increases the switch losses of the SRI transistors and besides, the amplitude fluctuations in the range from 0 to 0.5 are not reduced.

Another control method of the SRI output current, close to the PDM control method, is the odd (3rd or 5th) harmonic operation [21], [23], [24]. The advantage of this method is lower commutation losses in the SRI transistors. But in this case, the frequency of the SRI output voltage is three, five, or more times less than the resonance one. Thus, the size of the matching transformer is significantly larger compared to the case when the PDM control method is used. In addition, the amplitude fluctuations are larger compared to the irregular PDM control.

One more approach to reducing the fluctuation is the use of a modular converter, which is based on series or parallel connection of inverters, with the interleaved or stepped PDM control methods [3], [25]–[28]. In the case of using the interleaved PDM control, each channel of the converter has the same PDM pattern, but there is a time-shift between them, which influences the fluctuation [25]–[28]. In the case of using the stepped PDM control, the modulation begins to act only in one of the converter channels, and the modulation signals of other channels are 0 and/or 1 [28]. Compared to the single-channel SRI, the modular converter must have at least two channels, so more transistors are required; the constructions of the modular converter and the matching transformer are more complex, larger in dimensions, and finally, the modular converter costs more.

The SRI with extended topology and the PDM control method (extended PDM-SRI) has been presented in our primary work [29]. The present paper expands on previous research and proposes solutions to problems associated with the drawbacks mentioned in the primary work. The main contributions of this paper are summarized being as: 1) This article improves and enhances the theoretical analysis of the extended PDM-SRI, in particular through a deeper discussion of the amplitude fluctuations of the SRI output current. 2) Drawbacks of diodes reverse-recovery problems and voltage imbalance across capacitors mentioned in [29] are discussed, and solutions of these problems are proposed. 3) Simulation analysis of the extended PDM-SRI was carried out to verify the proposed solutions. The validity of the theoretical and simulation analysis is verified by a 2.2 kW experimental setup of the discussed extended PDM-SRI.

2. THEORETICAL BASIS
2.1. Induction heating equipment configuration
A typical configuration of induction heating equipment consists of a diode full-bridge rectifier, a DC-filter, a transistor inverter, a matching transformer, a control system, and a current transformer (CT). Figure 1. A load (an induction coil with a workpiece) of an induction heating system can be represented by the series-equivalent circuit model with an equivalent inductor \( L_{eq} \) and an equivalent resistor \( R_{eq} \); the model

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represents inductances of the workpiece, the induction coil, the gap, and resistances of the workpiece and the induction coil [30], [31]. The values of these parameters depend on geometries and materials of the induction coil and workpiece, and the operating frequency of the SRI. To obtain a series-resonant circuit, a capacitor \( C_r \) is usually connected in series with the secondary winding of the matching transformer and the load.

![Figure 1. Typical configuration of induction heating equipment](image)

Typically, the PDM control method is used in inverters with the full-bridge topology, because with this topology it is possible to obtain the injection and free-wheeling intervals [1], [2], [7]–[9]. This control method is also suitable in inverters with the half-bridge topology [10]. In this case the PDM-SRI produces two intervals: an injection one with a square-wave ac-voltage equal to half the SRI input voltage, and a rejection one, when the resonant circuit energy is transmitted to the capacitors of the half-bridge topology. As a consequence, the amplitude fluctuations of the SRI output current are higher.

**2.2. Pulse-density modulation-series-resonant inverter with extended topology**

To reduce the amplitude fluctuations of the PDM-SRI output current \( i_o \) it is expedient to combine operation modes of full-bridge and half-bridge inverters [29]. For this purpose, the extended inverter topology is used, which combines topologies of full-bridge and half-bridge inverters [29], [32], [33]. The extended inverter topology consists of switching devices (Q1–Q4) of the full-bridge topology, two capacitors \( (C_1 \text{ and } C_2) \) of equal values of the half-bridge topology, and an additional bi-directional switch Figure 2. The capacitors are series-connected across the DC source \( (V_d) \), and the SRI input voltage \( V_d \) is split by these capacitors into two equal sources with a voltage of \( V_d/2 \). The bi-directional switch is implemented with two back-to-back connected transistors (Q5 and Q6) in a typical source configuration. This switch is connected between the center tap of the series-connected capacitors and the center tap of the transistors Q3 and Q4; it is used to separate the operating modes of the full-bridge and half-bridge inverters. The secondary components of the matching transformer (inductor \( L_{eq} \), resistor \( R_{eq} \) and resonant capacitor \( C_r \)) are reflected to the primary side and represented as \( R, L, \) and \( C \), respectively.

![Figure 2. Inverter with the extended topology and the secondary components of the matching transformer reflected to the primary side](image)

The eight topological stages of the extended PDM-SRI are shown in Figure 3. With these stages, four modes of operation for the extended PDM-SRI can be obtained: Mode 1–stages 1 and 2 are used to produce the injection interval \( (T_A) \) during which the inverter acts as a square-wave ac-voltage source with the amplitude \( V_d \) for \( m \) cycles of the period \( T_O \) of the SRI output voltage \( V_{oS} \); Mode 2–stages 3 and 4 are used to produce the injection interval \( (T_C) \) during which the inverter acts as a square-wave ac-voltage source with the amplitude \( V_d/2 \) for \( l \) cycles of \( T_O \); Mode 3–stages 5 and/or 6 are used to produce the free-wheeling interval \( (T_B) \) during which the inverter acts as a zero-voltage source for \( n \) cycles of \( T_O \); Mode 4–stages 7 and 8 are used to produce the rejection interval during which the energy of the resonant circuit is transmitted to \( V_d \) source.
To reduce the amplitude fluctuations of $i_o$, it is expedient to combine mode 1 with mode 2, and mode 2 with mode 3, where mode 2 acts as an intermediate link between modes 1 and 3. It is not necessary to use mode 4 because when this mode is combined with modes 1 or 2, the amplitude fluctuations are higher compared to combining mode 3 with modes 1 or 2. Combining mode 4 with mode 3 is unreasonable; since both stages 5 and 6 ensure a zero-voltage state, it is sufficient to use only one of them to create mode 3.

Figure 4 shows the PDM control principle for the extended PDM-SRI: case I – $T_A$ is combined with $T_C$; Case II – $T_C$ is combined with $T_B$. The duration $T_M$ of the PDM sequence can be expressed as:

$$T_M = kT_O = \begin{cases} (T_A + T_C) = (m+l)T_O & \text{(in Case I)} \\ (T_C + T_B) = (l+n)T_O & \text{(in Case II)} \end{cases} \quad (1)$$

where $k$ is the number of cycles of $T_O$ during $T_M$. The value of $k$ may be constant for all PDM patterns of the regular and irregular PDM [9], [16], or it can be inconstant [12], [25].

The frequency of PDM sequences is given by:

$$f_{PDM} = 1/T_M. \quad (2)$$

For the extended PDM-SRI, the pulse density $D$ of PDM patterns can be expressed as:

$$D = \begin{cases} (T_A + T_C/2)/T_M = (m + 0.5l)/k & \text{(in Case I)} \\ (T_C/2)/T_M = 0.5l/k & \text{(in Case II)} \end{cases}. \quad (3)$$

2.3. Analysis of extended pulse-density modulation-series-resonant inverter output current

Typically, the SRI operates slightly above the resonant frequency to provide ZVS. But to simplify the mathematical analysis, the following two assumptions are made: the SRI operates at the resonant...
frequency \( \omega_o = 1/\sqrt{LC} \), and the quality factor \( Q \) of the resonant circuit is high enough to neglect higher harmonics in \( v_o \). In this case \( v_o \) can be represented is being as:

\[
v_o(t) = V_i \sin(\omega_o t) \tag{4}
\]

where \( V_i \) is the first harmonic amplitude of \( v_o \) (\( V_i = 4V_d/\pi \) during \( T_A \), \( V_i = 2V_d/\pi \) during \( T_C \), and \( V_i = 0 \) during \( T_B \)). In a steady-state operation, when the extended PDM-SRI operates only in mode 1, the output current \( i_o \) is given by:

\[
i_o(t) = I_m \sin(\omega_o t) \tag{5}
\]

where \( I_m \) is the maximum current amplitude in the case of \( D = 1 \), and is given by:

\[
I_m = \frac{4V_d}{\pi R} \tag{6}
\]

in case I – combination \( T_A \) and \( T_C \) Figure 4, the output current \( i_o \) is given by:

\[
i_o(t) = \begin{cases} 
    I_m \sin(\omega_o t) \left( 1 - \frac{1 - e^{-\frac{T_C}{T}}} {1 - e^{-\frac{T}{T}}} \right) & (0 \leq t \leq T_A) \\
    I_m \sin(\omega_o t) \left( 1 + \frac{1 - e^{-\frac{T_A}{T}}} {1 - e^{-\frac{T}{T}}} \right) & (0 \leq t \leq T_C),
\end{cases} \tag{7}
\]

where \( \tau \) is the time constant of the envelope of \( i_o \), and is given by:

\[
\tau = \frac{2L}{R} = \frac{2Q}{\omega_o}; \tag{8}
\]

when the extended PDM-SRI operates only in mode 3, the output current \( i_o \) is given by:

\[
i_o(t) = \frac{I_m}{2} \sin(\omega_o t); \tag{9}
\]

in case II – combination \( T_C \) and \( T_B \) Figure 4, the output current \( i_o \) is given by:

\[
i_o(t) = \begin{cases} 
    I_m \sin(\omega_o t) \left( 1 - \frac{1 - e^{-\frac{T_B}{T}}} {1 - e^{-\frac{T}{T}}} \right) & (0 \leq t \leq T_C) \\
    I_m \sin(\omega_o t) \left( 1 + \frac{1 - e^{-\frac{T_B}{T}}} {1 - e^{-\frac{T}{T}}} \right) & (0 \leq t \leq T_B).
\end{cases} \tag{10}
\]

It is convenient to submit \( \tau \) through the PDM parameters \( m, l, n, k \), and the quality factor \( Q \). In this way, (7) is given by:

\[
i_o(t) = \begin{cases} 
    I_m \sin(\omega_o t) \left( 1 - \frac{1 - e^{-\frac{\pi}{Q}} \frac{\pi}{Q_o}} {1 - e^{-\frac{\pi}{Q_o}}} \right) & (0 \leq t \leq T_A) \\
    I_m \sin(\omega_o t) \left( 1 + \frac{1 - e^{-\frac{\pi}{Q}} \frac{\pi}{Q_o}} {1 - e^{-\frac{\pi}{Q_o}}} \right) & (0 \leq t \leq T_C),
\end{cases} \tag{11}
\]

and (10) is given by:

\[
i_o(t) = \begin{cases} 
    I_m \sin(\omega_o t) \left( 1 - \frac{1 - e^{-\frac{\pi}{Q}} \frac{\pi}{Q_o}} {1 - e^{-\frac{\pi}{Q_o}}} \right) & (0 \leq t \leq T_C) \\
    I_m \sin(\omega_o t) \left( 1 + \frac{1 - e^{-\frac{\pi}{Q}} \frac{\pi}{Q_o}} {1 - e^{-\frac{\pi}{Q_o}}} \right) & (0 \leq t \leq T_B).
\end{cases} \tag{12}
\]

2.4. Analysis of extended pulse-density modulation-series-resonant inverter output power

The average output power is given by [1], [9]:

\[
\text{avg power} = \frac{1}{2} \cdot \frac{\pi}{Q_o} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q} \cdot \frac{1}{2} \cdot \frac{\pi}{Q}.
\]
where $\phi$ is the phase-shift between the fundamental frequencies of $v_o$ and $i_o$, and $i_E(t)$ is the envelope of the resonant current; in case I $i_E(t)$ is given by:

$$i_E(t) = \begin{cases} 
I_m \left(1 - \frac{1}{2} \frac{e^{-\frac{\pi}{Q_o} t}}{1 - e^{-\frac{\pi}{Q_o} t}}\right) & (0 \leq t \leq T_a) \\
I_m \left(1 + \frac{1}{2} \frac{e^{-\frac{\pi}{Q_o} t}}{1 - e^{-\frac{\pi}{Q_o} t}}\right) & (0 \leq t \leq T_c),
\end{cases}$$

and in case II it is given by:

$$i_E(t) = \begin{cases} 
I_m \left(1 - \frac{1}{2} \frac{e^{-\frac{\pi}{Q_o} t}}{1 - e^{-\frac{\pi}{Q_o} t}}\right) & (0 \leq t \leq T_c) \\
I_m \left(\frac{1}{2} \frac{e^{-\frac{\pi}{Q_o} t}}{1 - e^{-\frac{\pi}{Q_o} t}}\right) & (0 \leq t \leq T_b).
\end{cases}$$

If $\tau \neq 1/\omega_o$, (13) changes into the following equation:

$$P = \frac{2V_1}{\pi} \cos(\phi) \frac{1}{T_M} \int_0^{T_M} i_E(t) dt.$$  \hspace{1cm} (16)

The average output power can be calculated through the PDM parameters and $Q$ is being as:

- in the case of full power ($D = 1$), when the SRI operates as a conventional full-bridge SRI
  $$P = P_{max} = \frac{2}{\pi} V_d I_m \cos(\phi);$$  \hspace{1cm} (17)

- in case I
  $$P = P_{max} \frac{k - 0.5l}{k};$$  \hspace{1cm} (18)

- in the case of $D = 0.5$, when the SRI operates as a conventional half-bridge SRI
  $$P = \frac{1}{\pi} V_d I_m \cos(\phi);$$  \hspace{1cm} (19)

- in case II
  $$P = P_{max} \frac{k}{2} \left[1 + \frac{Q}{k} - \frac{\pi^2}{\pi^2 - 1} \right] \approx P_{max} \frac{0.5l}{k}.$$  \hspace{1cm} (20)

### 2.5. Amplitude fluctuation

The fluctuation of $i_o$ can be estimated in two ways: by the peak-to-peak value of the envelope $i_E$ of $i_o$ [1], and by the absolute peak-to-peak value of the amplitude of $i_o$ [29]. It is convenient to estimate the fluctuation by the peak-to-peak value of $i_E$ since there are only one maximal value $i_{E_{max}}$ and one minimal value $i_{E_{min}}$ of $i_E$ within $T_M$ Figure 4. Thus, the fluctuation can be estimated as the difference between $i_{E_{max}}$ and $i_{E_{min}}$ [1]. The normalized value of the fluctuation by $i_E$ is given by:

$$\Delta I_E^k = \frac{i_{E_{max}} - i_{E_{min}}}{I_m} = \begin{cases} 
\frac{1}{2} \frac{1 + e^{-\frac{\pi}{Q_o} t} - e^{-\frac{\pi}{Q_o} t}}{1 - e^{-\frac{\pi}{Q_o} t}} & (in \ case \ I) \\
\frac{1}{2} \frac{1 + e^{-\frac{\pi}{Q_o} t} - e^{-\frac{\pi}{Q_o} t}}{1 - e^{-\frac{\pi}{Q_o} t}} & (in \ case \ II).
\end{cases}$$  \hspace{1cm} (21)
The disadvantage of this approach is that the real absolute peak-to-peak value of the amplitude fluctuation is somewhat less. That is due to the fact that the maximal and minimal amplitudes of $i_O$ are at points that differ from the points of $I^*_\text{max}$ and $I^*_\text{min}$. Figure 4. Let’s consider the estimation of the fluctuation by the absolute peak-to-peak value of the amplitude of $i_O$. The maximal and minimal values of the current amplitude can be found for both active modes of the extended PDM-SRI Figure 4. Assuming that the exponential part of $i_O$ does not significantly affect the sinusoidal one during one half-period of $T_0$, the minimum amplitude value $I^*_\text{min}$ and the maximum amplitude value $I^*_\text{max}$ of $i_O$ can be determined for case I from (11) and for case II from (12) at points corresponding to 0.25 $T_0$ after the beginning and until the end of the active modes. The normalized minimum and maximum current amplitudes are given by:

- in case I

$$I^*_{\text{max}} = \left| \frac{i_O(T_0 - 0.25T_0)}{I_m} \right| = 1 - \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}},$$  

(22)

$$I^*_{\text{min}} = \left| \frac{i_O(0.25T_0)}{I_m} \right| = 1 - \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}},$$  

(23)

$$I^*_{\text{max}} = \left| \frac{i_O(0.25T_0)}{I_m} \right| = \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}},$$  

(24)

$$I^*_{\text{min}} = \left| \frac{i_O(T_0 - 0.25T_0)}{I_m} \right| = 1 - \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}};$$  

(25)

- in case II

$$I^*_{\text{max}} = \left| \frac{i_O(T_0 - 0.25T_0)}{I_m} \right| = \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}},$$  

(26)

$$I^*_{\text{min}} = \left| \frac{i_O(0.25T_0)}{I_m} \right| = \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}},$$  

(27)

$$I^*_{\text{max}} = \left| \frac{i_O(0.25T_0)}{I_m} \right| = \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}},$$  

(28)

$$I^*_{\text{min}} = \left| \frac{i_O(T_0 - 0.25T_0)}{I_m} \right| = \frac{1}{2} \left[ 1 - e^\frac{-\pi}{\tilde{\nu}} \right] e^{\frac{\pi}{\tilde{\nu}}};$$  

(29)

In this way, the normalized absolute peak-to-peak current amplitude fluctuation $\Delta I^*_m$ is given by:

$$\Delta I^*_m = \begin{cases} \max \{I^*_{\text{max}}, I^*_{\text{max}}\} - \min \{I^*_{\text{min}}, I^*_{\text{min}}\} & \text{(in Case I)} \\ \max \{I^*_{\text{min}}, I^*_{\text{min}}\} - \min \{I^*_{\text{max}}, I^*_{\text{max}}\} & \text{(in Case II)} \end{cases}$$  

(30)

The disadvantage of this approach is that it is necessary to determine which of the maximum amplitudes is higher and which of the minimum ones is lower. Figure 5 shows the relationship between the
fluctuation and the pulse density $D$, as well as the effectiveness $\eta$ of fluctuations reducing at various values of $Q$, which are obtained for the envelope of current Figure 5(a) and peak-to-peak current Figure 5(b). The effectiveness shows the relative reducing $\Delta I^*_{\text{E}}$ and $\Delta I^*_m$ when using the considered PDM-SRI with the extended topology compared to the PDM-SRI with the full-bridge topology at the same values of $D$, and is given by:

$$\eta = \frac{[\Delta I^*(D) \text{, full-bridge SRI}] - [\Delta I^*(D) \text{, extended SRI}]}{[\Delta I^*(D) \text{, full-bridge SRI}]} \times 100\% \quad (31)$$

Figure 5. Relationships comparing between the fluctuation and the effectiveness as functions of $D$ for different values of $Q$: (a) by envelope of current; (b) by peak-to-peak current.

The effectiveness $\eta$ exceeds 50% and reaches 100% at $D = 0.5$, as shown in Figure 5. The combinations of the PDM parameters used to calculate $\Delta I^*$ are given in Table 1. For the sake of simplicity, the PDM patterns were chosen with inconstant values of $k$, since otherwise PDM patterns with the irregular PDM and constant values of $k$ may contain different values of the PDM parameters within one $T_{\text{M}}$, which complicates the determination of $\Delta I^*$.

| Table 1. Values of PDM parameters |
|-----------------------------------|
| **Full-bridge topology** | $m$ | $n$ | $k$ | $D$ | $l$ | $n$ | $k$ | **Extended topology** |
|---|---|---|---|---|---|---|---|---|
| 16 | - | 16 | 1* | 8 | - | - | 8 | 16 |
| 15 | 1 | 16 | 0.94 | 7 | 1 | - | 8 | 15 |
| 11 | 1 | 12 | 0.92 | 5 | 1 | - | 6 | 11 |
| 7 | 1 | 8 | 0.875 | 3 | 1 | - | 4 | 7 |
| 5 | 1 | 6 | 0.83 | 2 | 1 | - | 3 | 5 |
| 3 | 1 | 4 | 0.75 | 1 | 1 | - | 2 | 3 |
| 2 | 1 | 3 | 0.67 | 1 | 2 | - | 3 | 2 |
| 1 | 1 | 2 | 0.5* | - | 1 | - | 1 | 1 |
| 1 | 2 | 3 | 0.33 | - | 2 | 1 | 3 | 1 |
| 1 | 3 | 4 | 0.25 | - | 1 | 1 | 2 | 1 |
| 1 | 5 | 6 | 0.17 | - | 1 | 2 | 3 | 1 |
| 1 | 7 | 8 | 0.125 | - | 1 | 3 | 4 | 1 |
| 1 | 11 | 12 | 0.08 | - | 1 | 5 | 6 | 1 |
| - | 16 | 16 | 0* | - | - | 8 | 8 | - |

*For these $D$ (except for $D = 0.5$ for the full-bridge topology) $v_0$ does not have two intervals, and the amplitude does not fluctuate. Thus, $\Delta I^*_{\text{E}}$ is considered equal 0, and $I_{\text{min}}$ equal to the amplitude of $i_0$.
When the PDM control method is used, the current control is limited by the available combinations of the PDM parameters. The control system monitors the change in the feedback signal between $i_O$ and the level of the current task signal, and being based on the feedback level, selects the appropriate combination of the PDM parameters to provide the required value of $D$. However, when the required value of $D$ cannot be realized with one of the available PDM combination, the control system will change two nearby PDM combinations whose values of $D$ are the closest to the desired one Figure 6. Thus, for $D_i < D < D_{i+1}$ (where $D_i$ and $D_{i+1}$ are two adjacent values of the pulse density which are the closest to the desired one and can be realized by the available PDM combinations) the amplitude fluctuation level will be determined by the action of the two PDM combinations and can be approximately defined is being as:

$$\Delta I_m^i = I^i_{\text{max}}(D_{i+1}) - I^i_{\text{max}}(D_i).$$

(32)

Figure 7 illustrates similar charts to Figure 5, but for the case when the fluctuation is determined by (32). As can be seen, at a low value of $Q = 5$, the effectiveness $\eta$ of fluctuations reducing is more than 40%.

![Figure 6. Output current waveform in case of cycling between two nearby combinations of the PDM parameters](image)

![Figure 7. Relationship between the fluctuation and pulse density at $Q$ of 5 and 20, and the effectiveness of fluctuations reducing](image)
2.6. Minimal current amplitude

In order to avoid non-ZVS operations of the SRI transistors, it is necessary to set a certain value of dead-time \( T_{DT} \) between the control signals of the SRI transistors. The value of \( T_{DT} \) depends, amongst other things, on the current amplitude value \([7–9]\). Thus, on the one hand, \( T_{DT} \) can be set constant and must be enough to ensure ZVS under different values of the parameters on which it depends. On the other hand, it can be changeable \([31]\). In the case of a low value of \( Q \), dynamically changing the value of \( T_{DT} \) is a complex task and requires high-speed mathematical calculation as well as measurements of current and voltage parameters with high accuracy. In the case of the constant \( T_{DT} \), the minimal current amplitude is important and the current fluctuation influences this amplitude value.

Let’s consider how using the proposed extended PDM-SRI allows increasing the minimal current amplitude compared to the full-bridge SRI with the traditional PDM control method. Figure 8 shows the difference between normalized values of \( I_{\text{min}} \) for the same \( D \) and \( Q = 5 \) for the mentioned above SRIs. As can be seen, if the current regulation is limited by values of \( D \) in the range of 0.25 to 1, the minimum amplitude value can be doubled. Thus, it is possible to reduce the value of \( T_{DT} \), and as a consequence, the switching losses will be lower. Or, if the dead-time value does not change, the range of \( D \) can be extended by 8.5%.

![Figure 8. Relationship between the minimal current amplitude and pulse density at \( Q = 5 \)](image)

3. METHOD

3.1. Drawbacks of extended pulse-density modulation-series-resonant inverter and proposed solutions

Figure 9 shows the SRI with extended topology, where \( C_S \) is the total capacitance of the snubber capacitor and the parasitic capacitances of the transistors. The main drawback of the extended PDM-SRI presented in \([29]\) is the problem of reverse-recovery of a transistor body-diode. This problem arises in two cases Figure 10: 1) when mode 1 is changed to mode 2, and 2) when mode 3 is changed to mode 2. Let’s consider it more deeply (in both cases mentioned, mode 2 is implemented using only stage 5).

![Figure 9. The extended SRI with \( C_S \)](image)

3.1.1. Reverse recovery problem

In case 1 Figure 10 (a), the extended PDM-SRI operates slightly above the resonance frequency. In mode 1 the SRI operates like a conventional full-bridge inverter. There is a certain dead-time \( T_{DT} \) between the control signals of the transistors to prevent shoot-through-current. During \( T_{DT} \), \( C_S \) are fully recharged until the next pair of transistors turns-on. After recharging \( C_S \), a pair of body-diodes starts to work and the switching of the transistors occurs with ZVS. At the end of mode 1, the bi-directional switch is turned-on within \( T_{DT} \). At this moment, one of the active diodes is supplied with half of the inverter input voltage from the capacitor of the half-bridge inverter topology, and as a result of this, the shoot-through-current flows through the circuit \( D_2-D_5-Q_6 \).
In case II Figure 10 (b), at the end of mode 3 we have a similar situation to the previous one. After recharging $C_s$ a pair of the body-diodes works, and the bi-directional switch is turned-on, resulting in a shoot-through-current flowing through the circuit $D_3-D_5-Q_6$. In addition, it is possible to provide that the bi-directional switch would be switched after a current zero-crossing. But in this case, the shoot-through-current will flow through the circuit $D_3-D_5-Q_6$. Therefore, this is not a solution to the problem.

![Figure 10. Switching sequence of the extended PDM-SRI with the diode reverse recovery problem (a) case I and (b) case II](image)

**3.1.2. Solution of reverse recovery problem**

In the described extended topology, the bi-directional switch is implemented with two back-to-back connected transistors ($Q_5$, $Q_6$) in a typical source configuration. A solution to the reverse recovery problem can be found through the change in the control signal of the bi-directional switch. In this way, the control signals $Q_5$ and $Q_6$ of transistors $Q_5$ and $Q_6$ are different, therefore the bi-directional switch will be seen below as two independent transistors $Q_5$ and $Q_6$. So, Figure 11 (a) shows the switching sequence of the extended PDM-SRI without the diode reverse recovery problem in case I, and Figure 11 (b) for case II, respectively.

![Figure 11. Switching sequence of the extended PDM-SRI without the diode reverse recovery problem (a) case I and (b) case II](image)

Both for cases I and II during the diode operation interval (at the end of mode 1 in case I and at the end of mode 3 in case II), it is expedient to turn-on only one of these transistors—the transistor $Q_5$. Since $Q_6$ is still turned-off, there is no problem with the reverse recovery of a transistor body-diode. At the end of the diode operation interval, the current flow changes, and $i_D$ flows through $Q_1$, $Q_6$, and $D_6$. As it is depicted in Figure 11, within this interval, after $C_s$ is recharged, $Q_6$ must be turned-on. Such a change in the control signals of $Q_5$ and $Q_6$ is sufficient to avoid the reverse recovery problem caused by the common control signal $Q_{5,6}$ of the bi-directional switch.
3.1.3. Voltage imbalance across capacitors

The second drawback mentioned in [29] is the voltage imbalance across the capacitors $C_1$ and $C_2$. This is caused that during mode 2 different currents flow through $C_1$ and $C_2$, which leads to an increase in voltage across one of the capacitors and a decrease across the other. In case I the envelope of $i_o$ falls during mode 2, causing the voltage across $C_1$ to decrease and the voltage across $C_2$ to increase. But in case II the envelope of $i_o$ rises during mode 2, causing the opposite situation—the voltage across $C_1$ increases, and the voltage across $C_2$ decreases. Therefore, it becomes necessary to balance the capacitor voltages.

3.1.4. Voltage imbalance across capacitors

A simple solution to this problem is to use the Delon circuit (a bridge voltage doubler circuit), because there is no need to use controlled devices. In this case it is necessary to use two diodes, a transformer and, as an option, a resistor connected as it is shown in Figure 12. The balancing resistor is used as an inrush current limiter and can generally be neglected due to the resistance of the transformer windings of the balancing circuit. Thus, when the voltage across one of the capacitors is higher than the other one, the energy of that capacitor will be transferred to the other one.

In case II during modes 1 and 2, the input voltage of the balancing transformer is half-wave symmetrical due to the pattern sequences of the control signals, and its frequency is equal to the frequency of $v_{O}$. However, when mode 3 is implemented using only stage 5, the input voltage of the balancing transformer will be asymmetrical and the effectiveness of the balancing circuit will be less. Thus, to avoid the asymmetrical voltage, it is reasonable to use mode 3 implemented using stage 5 within one $T_M$, and to use mode 3 implemented using stage 6 within the next $T_M$. But in this case, when mode 2 is changed to mode 3, the reverse recovery problem arises, similar to the one when mode 3 is changed to mode 2, and the shoot-through-current flows through the circuit $Q_3$-$D_4$. Thus, to avoid this current, $Q_1$ must switch when the direction of $i_o$ changes and $D_3$ starts to operate. The resulting sequence of control signals $Q_1$-$Q_4$ ensuring the ZVS operation of the extended PDM-SRI transistors in case II is shown in Figure 13. In such a way, in case II there is no reverse recovery problem, the input voltage of the balancing transformer will be symmetrical, and its period will be $(2k - 1)$ times more than the period $T_o$.

3.2. Simulation results

The extended PDM-SRI has been modeled in the MATLAB/Simulink environment. Simulations are carried out for the two mentioned above cases of combining the operation modes of the extended PDM-SRI. Figure 14 shows waveforms of the output voltage $v_O$ and output current $i_O$, as well as voltages $v_{C1}$, $v_{C2}$ across $C_1$ and $C_2$, the current through $Q_4$, and the current $i_{Q5}$, $i_{Q6}$ through the bi-directional switch, when the
mentioned in section 5 drawbacks are present: Figure 14 (a) for case I and Figure 14 (b) for case II. It can be seen in Figure 14 (a) that in case I \(V_{C1}\) decreases, and \(V_{C2}\) increases during the modeling process, but in case II there is the opposite situation, as it is shown in Figure 14 (b). In both case I and case II the shoot-through-current flows through the switch devices \(Q_4-Q_6\). Figure 15 shows waveforms for the case when the control signals were changed in accordance with the ones proposed in section 5, and the mentioned above balancing circuit was used Figure 15 (a) for case I and Figure 15 (b) for case II. It can be seen that these changes in the control signals are sufficient to ensure the ZVS operation of the SRI transistors and to avoid the shoot-through-current. In general, there is no imbalance of the voltages \(V_{C1}\) and \(V_{C2}\) both in case I and in case II, and \(V_{C1}\) and \(V_{C2}\) fluctuate only slightly owing to \(C_1\) and \(C_2\) charging and recharging.

![Figure 14](image1.png)

(a) case I and (b) case II

![Figure 15](image2.png)

(a) case I and (b) case II

Figure 14. Waveforms obtained as a result of the simulation when the mentioned drawbacks are present

Figure 15. Waveforms obtained as a result of the simulation when the mentioned drawbacks are absent

(a) case I and (b) case II
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4. RESULTS AND DISCUSSION

4.1. Experimental setup

The proposed PDM-SRI with the extended topology was verified using an experimental setup with a rated power of 2.2 kW Figure 18. The structure of the experimental setup is consistent with Figure 1. Discrete 650 V, 21 A SiC MOSFETs (SCT3120ALGC11) in the TO-247-3 package were chosen as switching devices of the extended PDM-SRI.

Figure 18. The experimental 2.2 kW setup

Two main tasks of the experimental setup control system are the generation of the above-described switching sequences and phase synchronization between $v_O$ and $i_O$ for performing ZVS during the SRI operating. Therefore, the STM32G474RCT6 microcontroller (MC) of the STM32 G4-series was chosen for its ability to generate up to ten PWM signals by its high-resolution timer (HRTIM) [34], [35]. A schematic depiction of the control system structure is shown in Figure 19.

Figure 19. Control system structure based on the microcontroller of the STM32G4 series

Apart from the MC, the control system consists of a current sensor, a current zero-crossing detector, a D-type flip-flop, a logical block, a block of measuring the average rectified value (ARV) of $i_O$, an operational amplifier, and drivers of the transistors. During operation, the MC changes the PDM combination according to the error signal produced by the operational amplifier. The output signal of the current sensor is used to determine the zero-crossing and average rectified value of $i_O$ by the zero-crossing detector and the block of measuring the ARV, respectively. The phase synchronization is based on a phase-locked-loop (PLL) technique that tracks the phase shift between $v_O$ and $i_O$. For this, two signals from the zero-crossing detector and the MC are fed to the D-type flip-flop. Based on the signal from the D-type flip-flop, the MC changes the operating frequency. The HRTIM generates six control signals and one shifted signal for phase synchronization. This shifted signal avoids the use of a compensator to eliminate propagation delay between the HRTIM control signals and $v_O$. The logical block is used to completely turn off all the SRI transistors of the converter (in case of an inactive state or in case of an emergency).

The HRTIM has to generate six control signals, which differ depending on the operation modes of the extended PDM-SRI and sequencing of changes in the acting PDM combinations. Figure 20 shows the control drive sequences generated by HRTIM for various cases of the PDM combinations. In the presented...
implementation, slave timers A, B, C, E, and the master timer of the HRTIM are used. The master timer handles the frequency control. Thus, the counters of the slave timers are reset on the master period.

To ensure all of the PDM combinations shown in Table 1, HRTIM must generate at least twelve control drive sequence shapes: six in the case of \(0.5 \leq D \leq 1\) Figure 20 (a) and six more in the case of \(0 \leq D \leq 0.5\) Figure 20 (b). A kind of shapes the HRTIM has to generate will depend on the sequence of changing the PDM combinations. Thus, the shapes of the control drive sequence of the same PDM combination may differ.

![Diagram](image)

**Figure 20.** Shape variants of the control drive sequences (a) in case of \(0.5 \leq D \leq 1\) and (b) in case of \(0 \leq D < 0.5\)

### 4.2. Experimental waveforms

Figure 21 shows the experimental \(v_o\) and \(i_o\) waveforms of a full-power \((D = 1)\) in the steady-state operation obtained by the setup. Experimental waveforms of \(v_o\) and \(i_o\) in case of using the extended PDM-SRI versus the full-bridge PDM-SRI for different \(D\) values are showed in Figure 22 (seen in Appendix). Figures 22 (a)-(c) on the left side show experimental waveforms for the extended PDM-SRI in the case of combining modes 1 and 2, when \(D = 0.83\), \(D = 0.75\), and \(D = 0.67\), respectively. Figure 22 (d) on the left side shows experimental waveforms in the case of modes 2, when \(D = 0.5\) (the SRI operates as a conventional half-bridge inverter). Figure 22 (e) on the left side shows experimental waveforms for the extended PDM-SRI in the case of combining modes 2 and 3, when \(D = 0.33\). On the right side of Figure 22 experimental waveforms for the full-bridge PDM-SRI, respectively for the same \(D\) value of the extended PDM-SRI, are shown. The operating frequency of the SRI was close to 34 kHz. Figure 23 shows the relationship between the current amplitude fluctuation and the output power when using the proposed PDM-SRI versus the full-bridge SRI with the traditional PDM. The fluctuation was calculated from the waveforms of \(i_o\). The \(Q\) value during the experiments was close to 6.

The resulting waveforms are fully in line with expectations. Since different shapes are required based on the sequence of changing the PDM combinations, different sequences have been stored in the MC memory for the same pulse density, and MC choses the appropriate sequence being based on the change of \(D\). So, there is no problem with changing the sequence. Through ongoing experiments, the \(T_{DT}\) value was kept constant. To reduce the switching losses in the inverter transistors, the \(T_{DT}\) value must be changeable [31]. Owing to fluctuations, changing the \(T_{DT}\) every \(T_o\) is challenging. On the other hand, the required \(T_{DT}\) value can only be determined for the minimal current amplitude. But calculating it correctly and promptly at a low \(Q\) value is a complex task.

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avoid inrush current during start-up, the initial frequency of the extended PDM-SRI was 50 kHz. During the start-up process, it is possible to obtain the non-ZVS operation of the extended PDM-SRI if the time shift in the control signals of \( Q_1 \) and/or \( Q_6 \) is too small, as shown in Figure 24(a). On the other hand, in a wide range of operating frequencies, it is also possible to obtain non-ZVS if the time shift is too large. Therefore, the time shift was set dynamically variable and equal to a quarter of the actual \( T_0 \). For this case, in Figures 24(b) and 24(c) the waveforms of \( v_o \) and \( i_o \) within the start-up process and in the steady-state operation, respectively, are shown. In both cases, the extended PDM-SRI operates with ZVS.

![Figure 21. Experimental waveforms of \( v_o \) and \( i_o \) in case of full-power operation (\( D = 1 \)).](image1)

![Figure 22. Relationship between the fluctuation and the output power](image2)

![Figure 23. Relationship between the fluctuation and the output power](image3)

![Figure 24. Waveforms of \( v_o \) and \( i_o \) at a low input voltage of the extended PDM-SRI (\( V_d = 70 \) V) (a) within start-up process and under non-ZVS condition; constant time shift in \( Q_6/Q_3 \), (b) within start-up process and under ZVS condition; dynamically variable time shift in \( Q_6/Q_3 \), and (c) in steady-state operation and under ZVS condition; dynamically variable time shift in \( Q_6/Q_3 \).](image4)

In general, the experimental results confirm the feasibility and performance of the proposed extended PDM-SRI. It is also worth noting the significant size of the balancing transformer due to the low frequency of its input voltage at low values of \( D \). In the experimental setup, the size was close to half the size of the matching transformer. To reduce the dimension of the balancing transformer, it is possible for \( D < 0.5 \) to use the PFM control method instead of the PDM one. In this case, the input voltage frequency of the balancing transformer will be equal to that of the matching one. Furthermore, one diode of the balancing circuit will be needless. Moreover, there will be no amplitude fluctuations of the SRI current. On the other hand, the dynamic losses in the SRI transistors will be higher.

5. CONCLUSION

The extended PDM-SRI for induction heating applications which is proposed and analyzed in the paper, has serious advantages in comparison with other types of PDM-SRIs. Such kind of the extended PDM-SRI allows to reduce the fluctuation of the SRI output current compared to the traditional PDM-SRI or reduces the number of required switching devices compared to a modular converter, which is based at least on two inverters connected in series, with an interleaved or a stepped PDM control method. A PDM control method and soft-switching operation of the proposed SRI were theoretically analyzed, explained, and verified with simulation. The experimental setup of a 2.2 kW extended PDM-SRI has confirmed its feasibility.
APPENDIX

Figure 22. Experimental waveforms of $t_{00}$ and $i_{0}$ in case of using the extended PDM-SRI versus the full-bridge PDM-SRI (a) in case of $D = 0.83$, (b) in case of $D = 0.75$, (c) in case of $D = 0.67$, (d) in case of $D = 0.5$ and (e) in case of $D = 0.33$
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