X-ray imaging of chemically active valence electrons during a pericyclic reaction

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Time-resolved imaging of chemically active valence electron densities is a long-sought goal, as these electrons dictate the course of chemical reactions. However, X-ray scattering is always dominated by the core and inert valence electrons, making time-resolved X-ray imaging of chemically active valence electron densities extremely challenging. Here we demonstrate an effective and robust method, which emphasizes the information encoded in weakly scattered photons, to image chemically active valence electron densities. The degenerate Cope rearrangement of semibullvalene, a pericyclic reaction, is used as an example to visually illustrate our approach. Our work also provides experimental access to the long-standing problem of synchronous versus asynchronous bond formation and breaking during pericyclic reactions.

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or over a century, X-ray and electron scattering have been indispensable in studying the structure of matter with atomic-scale spatial resolution. Thanks to enormous technological progress, it is now becoming possible to generate tunable, intense, ultrashort X-ray \(^1\)–\(^3\) and electron pulses\(^4,5\), adding femtosecond temporal resolution to structural analysis. These pulses promise to provide time-resolved snapshots of physical, chemical and biological processes in individual molecules\(^6\)–\(^8\). Atoms in molecules are glued together by valence electrons, which undergo ultrafast rearrangements during the formation and breaking of chemical bonds. Thus, the ability to follow the flow of valence electron density is paramount for ‘filming their motion’, and, ultimately, better understanding and controlling chemical reactions. The remarkable properties of modern ultrashort X-ray and electron pulses seem to offer a natural way for extending static scattering techniques into the domain of ultrafast electronic processes.

However, X-ray scattering from valence electrons is very weak in comparison with that from core electrons. The valence electron density contributes only a very small fraction to the total scattering pattern. Moreover, typically only a small fraction of the valence electron density participates actively in chemical reactions. These factors make use of X-ray scattering for time-resolved imaging of changes in chemically relevant parts of the valence electron density during complex chemical reactions extremely challenging. One way to circumvent the low sensitivity of X-ray scattering to valence electrons, proposed over four decades ago, is to use nonlinear X-ray scattering\(^9\). In a recent experiment, sum and difference frequency generation in the X-ray domain have been used to determine the valence electron density of diamond in real space, for a particular orientation\(^10\).

However, realizing the time-resolved version of nonlinear X-ray scattering requires the triad of two optical and one ultrashort X-ray pulse with controlled variable time-delays between all three, by no means an easy task. Another option is to focus on the temporal behaviour of Bragg peaks. This approach has been successfully applied to imaging valence electron density in refs 6,11,12. However, it is limited to crystals, and requires subtracting of the total electron density at time zero from those at successive times, that is, the analysis of density differences.

Here we describe an effective and robust approach that allows us to extract changes of that part of the total electron density directly related to bond making and bond breaking during chemical reactions, that is, chemically active valence electron density, from the overall X-ray scattering pattern, which itself is dominated by the core electrons. This allows us to image the flow of valence electrons in space and time during a chemical reaction and thus solve one of the major problems, which has hampered the progress of time-resolved imaging of chemical reactions. Of course, many other experimental challenges remain, including better control of pump-probe jitter, better detectors, improved signal-to-noise ratios and so on. Our approach works in both the condensed and the gas phase, giving access to valence electron rearrangements in individual molecules. We illustrate our approach using the example of a very general pericyclic reaction—the degenerate Cope rearrangement of semibullvalene, sketched in Fig. 1. Our example also addresses another important and long-debated issue: is the breaking of old bonds during pericyclic reactions synchronous with the formation of new bonds? We show that our method distinguishes these two alternatives.

**Results**

**The degenerate Cope rearrangement of semibullvalene.**

Figure 1a shows effective reaction paths for the degenerate Cope rearrangement. In general, the reaction path strongly depends on the preparation of the reactants. Depending on the reactant energy, the Cope rearrangement can proceed by tunnelling (path 1) or over the barrier (path 2). Such alternative pathways are ubiquitous in many chemical reactions. They invariably trigger the question about synchronous versus asynchronous bond breaking and formation, debated over many decades for such pericyclic reactions\(^13\)–\(^19\). So far, the debate has been purely theoretical.

Recent quantum mechanical \(ab\ initio\) calculations for the Cope rearrangement of semibullvalene in the electronic ground state predicted that the synchronicity of the underlying electronic bond-to-bond fluxes depends on the energy (temperature) of the reactants\(^16,17\). Synchronous bond formation and breaking was predicted for tunnelling, which is the dominant pathway at low energies (temperatures). In contrast, asynchronous bond breaking and formation was predicted for the over-the-barrier pathway, typical for high excitation energies (high temperatures). In this case, there should be a time-delay between the breaking of the old and the formation of the new bonds. Initiating pericyclic
reactions at different excitation energies is possible using ultrashort optical pulses: down-chirped pump-dump and photoimpulsive methods have been proposed and experimentally demonstrated\textsuperscript{20,21}.

**Imaging via time-resolved X-ray scattering.** To simulate the time-resolved scattering pattern to image the Cope rearrangement, we have used the following expression for the differential scattering probability\textsuperscript{22–24}

\[
\frac{dP}{d\Omega} = \frac{d\sigma_{th}}{d\Omega} \int dt \ j_x(t) \left\langle \frac{\mathcal{X}(\mathbf{r}, \tau)}{\mathcal{X}(\mathbf{r}, \tau)} \right\rangle \left|\int d^3r \rho(r; \mathbf{R}) e^{iQr} \right|^2 \mathcal{X}(\mathbf{R}, \tau).
\]

(1)

Here, \(d\sigma_{th}/d\Omega\) is the Thomson scattering cross-section, \(j_x(t)\) is the fluence of the incident X-ray pulse at time \(t\), \(\mathcal{X}(\mathbf{R}, \tau)\) corresponds to the nuclear wave packet with \(\mathbf{R}\) denoting the set of nuclear coordinates with \(\tau\) as the pump-probe delay-time, \(\rho(r; \mathbf{R})\) is the electronic density with \(r\) as electronic coordinate and \(\mathbf{Q}\) is proportional to the momentum transfer of the scattered X-ray. \(\rho(r; \mathbf{R})\) is evaluated using quantum chemical calculations based on the density functional theory using the B3LYP functional with the cc-pVTZ basis sets by means of the MOLPRO program package\textsuperscript{25}. The time-dependent nuclear Schrödinger equation is solved to compute the time evolution of \(\mathcal{X}(\mathbf{r}, \tau)\) along the reaction coordinate \(\xi\) describing the direct path from the reactant to the product as shown in Fig. 1a. Comparison with high-level \textit{ab initio} methods shows that (i) the structures and energies along \(\xi\) are accurate in the present calculations and (ii) asynchronous bond making and breaking is a stable phenomenon, irrespective of the actual reaction path over the barrier\textsuperscript{26}. The mean total energy along \(\xi\) for the reaction over the barrier is set to 1.25 eV, well above the potential barrier of 0.36 eV, and well below the first excited electronic state, which is about 4 eV higher in energy according to TDDFT calculation with the B3LYP functional using the 6-31G* basis sets\textsuperscript{27}. Consequently, the dynamics along \(\xi\) is essentially decoupled from the other degrees of freedom\textsuperscript{28} and the
reaction is well described within the Born–Oppenheimer approximation. For the calculation of the scattering patterns, an incident X-ray pulse with 20 keV photon energy and the detection of photons scattered up to 60° is assumed, yielding $Q_{\text{max}} = 10 \text{ Å}^{-1}$. The total scattering patterns encode the ground-state electron density. The excited electronic states and the electronic current density do not contribute to the total scattering pattern\(^{22–24,29,30}\).

**Figure 3 | Density differences for the Cope rearrangement of semibullvalene.** The total electron density at time zero is subtracted from the electron densities at later delay times during the course of the reaction via (a) tunnelling, and (b) for the over-the-barrier reaction. The density differences are presented in the $y–z$ plane at pump-probe delay times T/4, T/2, 3T/4 and T.

**Imaging chemically active electrons.** In theoretical analysis of chemical bonding, topological analysis\(^{33–36}\) or a partitioning of the total electronic density based on localized molecular orbitals\(^{37,38}\) is typically used. In refs 16–18 such analyses enabled the prediction of synchronous versus asynchronous bond making and bond breaking, c.f. Fig. 1b. Specifically, the total electronic density was partitioned into a core electron density $\rho_{\text{core}}(r; R)$ (which accounts for the 16 carbon core electrons), a pericyclic electron density $\rho_{\text{peri}}(r; R)$ (which accounts for the six electrons associated with the mutation of the Lewis structure for the reactant into that of the product) and a density of the remaining valence electrons $\rho_{\text{oval}} (r; R)$, such that $\rho(r; R) = \rho_{\text{core}}(r; R) + \rho_{\text{peri}}(r; R) + \rho_{\text{oval}} (r; R)$. Although the pericyclic density has been established as a powerful theoretical tool for the analysis of pericyclic reactions, as well as to access the underlying bond-to-bond fluxes, no method exists to observe this quantity experimentally.

We now demonstrate how the chemically active valence electron densities, which carry invaluable information about chemical reactions and hence electronic bond-to-bond fluxes, can be directly accessed from the full scattering patterns: although there is no strict separation of the contributions from the core, inert valence and the chemically active valence electrons to the total scattering pattern, their relative contributions might be different in different regions of the $Q$-space. The delocalized valence electrons scatter weakly and should show their fingerprints mostly in the low $Q$-region of the scattering pattern. The well-localized core electrons, on the other hand, scatter strongly and contribute across the full scattering pattern. For the Cope rearrangement of semibullvalene, representing a whole range of pericyclic reactions, the chemically active valence electrons can indeed be brought to the fore to a remarkable extent by restricting the reconstruction to the relatively small momentum transfer,
The electron densities are in the $Q$ electrons according to the Lewis structures (cf. Fig. 1b). The reconstruction of the densities is performed using scattering intensity information up to Cope rearrangement of semibullvalene via tunnelling. ($T$ for tunnelling and the over-the-barrier reaction at times $0$, $T/4$, $T/2$, $3T/4$ and $T$). $p_{\text{peri}}(r, R)$ accounts for the six rearranging valence electrons according to the Lewis structures (cf. Fig. 1b). The reconstruction of the densities is performed using scattering intensity information up to $Q_{\text{limited}} = 3.4 \, \text{Å}^{-1}$ from the full time-resolved scattering patterns as shown in Fig. 2. The electron density is given in units of number of electrons per Å$^2$.

Figure 4 | Reconstructed valence electron densities and the pericyclic electron densities. (a) Reconstructed valence electron densities obtained via the restricted $Q$-reconstruction method, and (b) the pericyclic electron densities ($p_{\text{peri}}(r, R)$) obtained via partitioning the total electron densities for the Cope rearrangement of semibullvalene via tunnelling. (c) Reconstructed valence electron densities, and (d) $p_{\text{peri}}(r, R)$ for the over-the-barrier reaction. The electron densities are in the $y$–$z$ plane at pump-probe delay times $0$, $T/4$, $T/2$, $3T/4$ and $T$.

Figure 4 shows that the hitherto dominant contribution from the core and inert valence electrons has been considerably diminished, while the contribution of the hitherto hidden chemically active electrons has been considerably increased. We observe that the reconstructed electron densities have more strength than $p_{\text{peri}}(r, R)$, which indicate that the reconstructed electron densities contain the contributions from pericyclic electrons as well as from other valence and core electrons, whereas $p_{\text{peri}}(r, R)$ contains the contributions from pericyclic electrons alone. However, the reconstructed electron densities are in excellent agreement with $p_{\text{peri}}(r, R)$, which provides direct insight into the reaction mechanism. We note that the restricted $Q$-reconstruction method is analogous to fourier filtering techniques of image analysis with a low-pass square-shaped.

The retrieved electron densities in the $y$–$z$ plane, using the restricted $Q$-region information, are presented in Fig. 4a,c for tunnelling and the over-the-barrier reaction, respectively. For comparison, the modelled pericyclic electron densities ($p_{\text{peri}}(r, R)$) for tunnelling and the over-the-barrier reaction at times $0$, $T/4$, $T/2$, $3T/4$ and $T$ are shown in Fig. 4b,d, respectively. A value of $Q_{\text{limited}}$ equal to $3.4 \, \text{Å}^{-1}$ is used for the retrieval of electron densities using restricted-$Q$ fourier transform, for Fig. 4a,c. To ensure robust reconstruction, we have varied $Q_{\text{limited}}$ and find that the key features of the reconstructed densities are present for $Q_{\text{limited}}$ ranging from 3 to $4.5 \, \text{Å}^{-1}$. For an illustration of the robustness of the results, the reader is referred to Supplementary Fig. 4.
filter. In particular, the ‘ringing’ in the retrieved electron densities is related to the sharp edge of the square filter. Typically, a low-pass filter blurs the image. Here, however, this blurring is beneficial: we see that it brings out the chemically active electron density. Regarding the applicability of our method, the key requirement is the ability to measure wide-angle scattering pattern up to $Q_{\text{max}}$, which enables atomic-scale spatial resolution and faithful reconstruction of the lost phase of the scattering pattern using a phase-retrieval algorithm.

**Discussion**

The issue of synchronous versus asynchronous bond formation and breakage can indeed be addressed using the reconstructed electron densities. The reconstructed electron densities for the reaction intermediate at $T/2$ show that in the tunnelling case, the reaction is synchronous, whereas it is indeed asynchronous in the over-the-barrier case. At $T/2$, the electronic flux out of the old bond, centred around $z = -1 \text{ Å}$ and $y = 0 \text{ Å}$, is larger for the over-the-barrier reaction than for tunnelling (disconnected and connected black contours in the vicinity of the old bond, respectively). At the same time, the flux into the new bond, centred around $z = 1 \text{ Å}$ and $y = 0 \text{ Å}$, is smaller for the over-the-barrier reaction as compared with the tunnelling scenario.

In conclusion, using the degenerate Cope rearrangement of semibullvalene as an example, we have demonstrated a powerful approach to retrieve valence electron density from the full time-resolved scattering pattern using the restricted $Q$-reconstruction method. The phase of the scattering pattern needed for the reconstruction can be obtained from the full, unrestricted-$Q$ scattering pattern. Our approach enables us to image the instants of bond formation and breakage during chemical processes and resolve experimentally the long-standing debate of synchronous versus asynchronous bond formation and breakage during chemical processes. Of course, our approach also applies for imaging chemically active valence electron densities in static structures and non-adiabatic chemical reactions.

The notion of quantum fluxes along with their respective densities for the Cope rearrangement of semibullvalene proceeds for temperatures below 40 K by coherent tunnelling involving the lowest doublet of nuclear eigenstates within $T = 970$ K. Hence, the nuclear density $|\rho(r, \mathbf{R})|^2$ for tunnelling consists essentially of two parts representing the reactant and the product, centred at $\mathbf{R}_a$ and $\mathbf{R}_b$, respectively, superimposed according to

$$\rho(r, \mathbf{R}) = N \sum_{i} |\Phi(r, \mathbf{R})|^2 \delta_{\mathbf{R}_a} - \mathbf{R} + \delta_{\mathbf{R}_b} - \mathbf{R},$$

where $\rho$ denotes the Dirac distribution. Inserting equation (4) into equation (3) and performing the integration yields the time-dependent electron density for the tunnelling scenario. For the reaction over the barrier, the time-dependent nuclear Schrödinger equation is solved to compute the time evolution of $\psi(t, \mathbf{R})$ along the reaction coordinate $\zeta$, describing the direct path from the reactant to the product corresponding to synchronous nuclear motion. The underlying potential energy surface and the corresponding electron densities are evaluated at the $32\text{LYP/cc-pVTZ}$ level of theory employing the Moplo program package, yielding excellent agreement with high-level multi-reference ab initio calculations. The mean total energy along $\zeta$ is set to 1.25 eV, well above the potential barrier of 0.36 eV. Consequently, the dynamics along $\zeta$ is essentially decoupled from the other degrees of freedom. It shall be added that asynchronous bond making and bond breaking in the reaction over the barrier is a stable phenomenon in the investigated pericyclic reaction, which is even more pronounced when deviating from the direct path as shown in refs 18,26.

**Retrieval of chemically active valence electron densities**

The full time-resolved scattering pattern provides only the scattering amplitude while the phase is lost in the measured scattering signal. There exists a variety of phase-retrieval procedures to reconstruct the phase from the scattering amplitude and therefore reconstruct the total electron density of crystalline and non-crystalline samples. In the present case, we have used the HIO algorithm, based on iterative fourier transformations, back and forth between the momentum space and real space. Combining the retrieved phase and the scattering amplitude, the total electron densities for the Cope rearrangement of semibullvalene can be reconstructed in the present case by performing two-dimensional fourier transformation over the extended $Q$-range equal to $Q_{\text{max}} = 10^{-1} \text{ Å}^{-1}$. For the reconstruction of the chemically active electron density, the two-dimensional fourier transformation for the restricted range of the photon-momentum transfer, that is, $|Q_{\text{zonal}}| = 3.4 \text{ Å}^{-1}$ is performed. The reader is referred to Supplementary Figs 2 and 3 for a detailed discussion of our implementation of the HIO algorithm.

To ensure the robustness of our approach for the retrieval of chemically active valence electron densities, the range of $|Q_{\text{zonal}}|$ is varied from 3 to 4.5 $\text{ Å}^{-1}$, and the key features of the retrieved electron densities are present within this range of $|Q_{\text{zonal}}|$. The reader is referred to Supplementary Fig. 4 for the corresponding illustrations.

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