Reconstruction of images in non-scanned confocal microscope (NSCM) using speckle imaging

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Abstract

Background: The common formation of images in CSLM assumes mechanically scanned object placed in the common short focus of the objective lenses of the microscope, while in the arrangement under study, the scanning of the object is realized by placing a diffuser behind the collimating lens. A model is suggested in the formation of images in Confocal Scanning Laser Microscope (CSLM) using non-scanned object. Since the illumination and detection are coherent, the obtained image is constructed from the simple product of the Resultant Point Spread Function (RPSF) modulated by the diffuser spread over the object transparency. Hence, the product of the object and the image of the diffuser replace the mechanical scanning of the object.

Results: Reconstructed images using this novel arrangement of CNSM are presented using mammographic X-ray image.

Conclusions: Convolution of the RPSF and the object is realized by the spreading of the diffuser image over the object. A coherent detector captures the whole image affected by a noisy diffused function. It is noted that image processing is necessary to improve noisy images making use of filtration techniques.

Keywords: Non-scanned object, Resultant Point Spread Function, Confocal microscopy, Image processing and filtration

1 Background
The ordinary confocal laser scanning microscope (CSLM) described early by Sheppard et al. [1–12] assumes mechanical scanning of the object placed in the common short focus of the objective lenses of the microscope. Coherent illumination is realized using laser beam, and coherent detection is realized by using pinhole detector to construct the image point by point where the mechanical scanning is synchronized with the electronic scanning during the detection. The detected signal is amplified and localized on CRO. Previous studies [13–18] showed an improvement in the lateral resolution using different modulated apertures. A linear, quadratic, combination of linear–quadratic [12], Gaussian and other modulated apertures is considered, while optimization of axial resolution in confocal imaging using annular pupils is investigated in [10]. Recently, a modified Hamming aperture is used in the formation of images in confocal microscope and the lateral resolution is computed from the Point Spread Function (PSF) and compared with the corresponding resolution in case of uniform apertures [19]. Confocal microscope can provide images of thick pieces of tissues which are optically sliced, instead of using microtome. Hence, out-of-focus light is rejected, and a thin section of the tissue is obtained. Applications of confocal microscope are basically in research laboratory; however, its
application in clinical settings has been also reported [20–26].

In this study, we are interested to form images using non-scanned confocal microscope making using diffuser placed behind the collimating lens instead of using a grating [18].

2 Methods

A collimated beam from He–Ne laser is obtained using spatially filtered techniques as shown in Fig. 1. The collimated parallel beam is incident on the confocal arrangement of the microscope where a diffuser is placed behind the collimating objective lens $L$. In this arrangement, we assume stationary object where the mechanical scanning is replaced by the image of the diffuser. Hence, the object is covered by the image of the diffuser convoluted by the Point Spread Function corresponding to the 1st objective lens. The following steps for the formation of images using non-scanned object are summarized as follows:

1. Consider unit amplitude of coherent radiation incident upon the diffuser placed in contact with the collimating lens $L$. The diffuser is represented by a randomly distributed function $d(x_1, y_1)$ and obstructed by the 1st aperture $P(x_1, y_1)$. Then the transmitted complex amplitude is represented as follows:

$$A(x_1, y_1) = d(x_1, y_1) \cdot P(x_1, y_1)$$

where $P(x_1, y_1) = 1$: for $|\rho| \leq 1$ \hspace{1cm} (1)

$= 0$; otherwise

$\rho$: is the radial coordinate in the aperture plane of the collimating lens $L$.

And $d(x_1, y_1) = \text{rand}(x_1, y_1)$.

2. In the back focal plane of the collimating lens $L$, we get by applying the F.T. upon Eq. (1), the following:

$$\tilde{A}(u, v) = \text{F.T.}\{d(x_1, y_1) \cdot P(x, y)\} = \tilde{d}(u, v) \otimes h(u, v)$$

(2)

3. For simplicity, assume the F.T. corresponding to the collimating lens is replaced by a Dirac–delta function where the illumination is considered coherent. Hence, Eq. (2) is approximately given as:

$$\tilde{A}(u, v) = \tilde{d}(u, v) \otimes \delta(u, v) = \tilde{d}(u, v)$$

(3)

4. In the focal plane of the 1st objective lens limited by the aperture $P_1(u, v)$ where the transparency of the object is placed in $(x, y)$ plane, we apply the $\text{F.T}^{-1}$. upon Eq. (3) to get the following:

$$B(x, y) = \text{F.T}^{-1}\{\tilde{d}(u, v) \cdot P_1(u, v)\} = d(x, y) \otimes h_1(x, y)$$

(4)

5. The 2nd objective is shown conjugate to the 1st objective where the pupil aperture $P_2(u, v)$ is shown in front of the 2nd objective. The Point Spread Function is equal to that shown for the 1st objective is formed in the common short focus where the object is located. Consequently, the object transparency $g(x, y)$ is multiplied by both the PSF’s but convoluted with the diffuser covering the non-scanned object. Hence, we get the following multiplication in the object plane of transmitted complex amplitude $C(x, y)$:

$$C(x, y) = [d(x, y) \otimes h_1(x, y)] \cdot h_2(x, y) \cdot g(x, y)$$

(5)

Fig. 1 Confocal microscopic imaging of non-scanned object using a diffuser placed in front of the lens $L$. The two microscope objectives are $L_1$ and $L_2$. The image of the diffuser spreads over the object in its plane.
6. The detected intensity is represented as the modulus square of the complex amplitude $C(x, y)$, represented as follows:

$$I(x, y) = |d(x, y) \otimes h_1(x, y)| \cdot h_2(x, y) \cdot g(x, y)|^2$$  \hfill (6)

7. Since the convolution product of the diffuser and the PSF corresponding to the 1st objective lens of aperture $P_1(x, y)$ gives truncated image of the diffuser convoluted by the 1st objective PSF formed in the object plane $(x, y)$, then we can write the complex amplitude corresponding to the modulated diffuser image as follows:

$$d_{\text{mod.}}(x, y) = d(x, y) \otimes h_1(x, y)$$  \hfill (7)

Substituting from (7) in (6), the detected intensity is rewritten as follows:

$$I(x, y) = |d_{\text{mod.}}(x, y) \cdot h_2(x, y) \cdot g(x, y)|^2$$  \hfill (8)

Or using equation (6), we get the following convolution:

$$I(x, y) = |g(x, y) \cdot d(x, y) \otimes h_1(x, y)h_2(x, y)|^2$$  \hfill (9)

Consequently, the detected image intensity is simply affected by the PSF corresponding to the 2nd objective, while the PSF corresponding to the 1st objective is convoluted with the diffuser image giving the modulated diffuser. Hence, the whole image is formed without the object scanning since it is integrated by the modulated diffuser. The Resultant Point Spread Function (RPSF) is computed from the product of the PSF corresponding to each objective and written as follows:

$$h_r(x, y) = h_1(x, y)h_2(x, y)$$  \hfill (10)

8. Finally, the coherent extended detector is required to capture the whole image covered by the randomly distributed function.

9. Image processing is necessary to extract an improved image.

### 3 Results

The input mammographic image used in the processing is shown in Fig. 2.

We construct random diffuser $d(u, v)$, of dimensions $512 \times 512$ pixels as shown in Fig. 3. It is placed in front of the collimating lens $L$. This diffuser incident upon a circular aperture of diameter 128 pixels is given in Fig. 4. The PSF corresponding to the aperture of the collimating lens convoluted with the Fourier spectrum of the diffuser is shown in Fig. 5. It is called modulated speckle pattern since the FT of the diffuser is named ordinary speckle assuming high numerical aperture (NA).

The modulated speckle pattern shown in Fig. 5 is truncated by the 1st microscope objective is shown in Fig. 6.

The FT of the modulated speckle multiplied by the transmittance from 1st objective of the microscope will give the image of the diffuser convoluted by the PSF of the 1st objective located in the object plane as shown in Fig. 7. The modulus square of the multiplication of the above convolution with the object and the PSF corresponding to the 2nd objective forming the detected
A noisy image is shown in Fig. 8a. The detected images in absence of the diffuser are shown as in Fig. 8b for aperture radius $= 128$ pixels, while Fig. 8c shows the image for aperture radius $= 16$ pixels. The figures from 2 up to 8 represent images of two-dimensional matrix of $512 \times 512$ pixels starting from $(0,0)$ in the upper left corner and ending with $(512, 512)$ in the lower right corner.

4 Discussion
The proposal of NSCM using a diffuser gives reconstructed images in the detection plane affected by the diffuser noise. The reconstructed image may be improved by filtration technique. This new arrangement of NSCM is compared with the ordinary confocal microscope provided with the mechanical scanning of the object placed in the confocal plane of the objectives. It is shown equal resolution in both cases with and without diffuser. The different confocal microscope arrangements gave equal values of resolution since the Resultant Point Spread Function (RPSF) is only dependent on the objectives and the laser beam of wavelength $\lambda$. It is computed from the PSF corresponding to each objective lens represented by Eq. (10). The PSF corresponding to uniform circular aperture has the known Airy disc [2].

It is shown a noisy image affected by the diffuser as in Fig. 8a, of resolution dependent on the PSF corresponding
to the objectives. The detected intensity for greater radius (128 pixels) shown in Fig. 8b has better resolution than that shown in Fig. 8c for smaller radius = 16 pixels. This is attributed to the inverse relation between resolution and the aperture radius for certain focal length which is determined from the spatial radial cutoff in the focal plane. The PSF using uniform circular aperture versus radial distance in the Fourier plane is plotted as in Fig. 9. The cutoff values computed to represent resolution are as follows:

The cutoff radial distance \( r_c = 0.5039 \, \mu m \) for aperture radius = 16 pixels, while \( r_c = 0.06 \, \mu m \) for aperture radius = 128 pixels. Another values of cutoff are given as follows: \( r_c = 0.2581 \, \mu m \) for aperture radius = 32 pixels, and \( r_c = 0.1352 \, \mu m \) for aperture radius = 64 pixels. It is shown inverse relation between the cut-off value \( r_c \) and the aperture radius as expected from the resolution limit, assuming monochromatic light for the microscope illumination of wavelength \( \lambda \). The theoretical resolution limit is given by: resolution limit = \( \frac{\lambda}{2a} \).

Consequently, the highly resolved images are obtained for sharper PSF hence lower cutoff value as shown in Fig. 8b.

5 Conclusions
A confocal microscope based on substituting the mechanical scanning of the object by the image of the diffuser formed in the object plane. The diffuser is placed before the collimating lens of the spatial filter. Hence, speckle pattern is formed in the back focal plane of the collimating lens which is the Fourier transform of the transmitted diffuser. Then, operating the inverse Fourier transform upon the 1st objective lens limited by the aperture \( P_1 \) to get the convolution of the diffuser image and the PSF corresponding to the 1st objective. This convolution product is formed in the object plane. Consequently, the detected intensity is computed from the multiplication of the object with the diffuser convoluted with the PSF corresponding to both microscope objectives. The detected image is affected by a noise originated from the
diffuser, which can be removed by filtering techniques. Concerning the image resolution using diffuser or in absence of it, we insist upon its dependence upon the aperture radius as outlined in results and discussion.

The potential work of NSCM is to test the confocal microscope, while the object placed in the common short focus of both objectives is fixed and assuming the scanning realized by either diffuser or grating.

Abbreviations

NSCM: Non-Scanned Confocal Microscope; CSLM: Confocal Scanning Laser Microscope; PSF: Point Spread Function; RPSF: Resultant Point Spread Function; ⊗: Symbol for convolution operation; F.T.: Fourier transform integral and its inverse F.T.\(^{-1}\); NA: Numerical aperture corresponding to an objective lens.

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Authors’ contributions

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Fig. 9 The PSF using uniform circular aperture of radius = 16 pixels. The cutoff radial distance \( r_c \) = 0.5039 µm as shown in the curve.

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