Cosmology of the DFSZ axino

Kyu Jung Bae*, Eung Jin Chun†† and Sang Hui Im∗†

aDepartment of Physics, KAIST, Daejeon 305-701, Korea
bKorea Institute for Advanced Study, Seoul 130-722, Korea

Abstract

We study the cosmological impact of the supersymmetric DFSZ axion model. Extending recent works, we first provide a comprehensive analysis of thermal production of the DFSZ axino considering all the possible scattering, decay and inverse decay processes depending on various mass parameters and the reheat temperature. Although it is hard for the DFSZ axino to be in thermal equilibrium, its coupling is still large enough to generate huge axino population which can turn into overabundant neutralino density. We examine the neutralino parameter space to identify the dark matter property depending on the Peccei-Quinn scale. As the Peccei-Quinn scale becomes higher resulting in longer axino lifetime, the neutralino dark matter appears in a lighter Higgsino-like LSP region or a more restricted Bino-like LSP region allowing a resonant annihilation through a CP-odd Higgs boson to meet stronger reannihilation.

* kyujung.bae@kaist.ac.kr
†† ejchun@kias.re.kr
‡‡ shim@muon.kaist.ac.kr
I. INTRODUCTION

The most attractive solution to the strong CP problem would be to introduce the axion, a pseudo-Goldstone boson of the Peccei-Quinn (PQ) symmetry which is supposed to be broken at \( v_{PQ} = 10^9 - 10^{12} \) GeV \[1\]. The axion solution can be realized typically in two ways: (i) the KSVZ model assuming a heavy quark at an intermediate scale \( \lessapprox v_{PQ} \) \[2\]; (ii) the DFSZ model extending the Higgs sector with PQ charged singlet fields \[3\]. In the supersymmetric extension of the axion models, the presence of the axino \( \tilde{a} \), the fermionic partner of the axion, can change dramatically the property of dark matter.

First of all, the axino can be the lightest supersymmetric particle (LSP) in \( R \)-parity conserving models. The axino in the KSVZ model decouples at a very high temperature and thus it must be very light (\( m_{\tilde{a}} \sim 0.1 \) keV) to become a viable dark matter candidate \[4\]. In the gravity mediated supersymmetry breaking scheme, such a light axino mass could be arranged although it is generic to have the axino mass of order of the gravitino mass, \( 10^2 - 10^3 \) GeV \[5–7\]. In the DFSZ model or in the KSVZ model with lower reheat temperature, the axino may never be in thermal equilibrium, but thermal regeneration (the axino production from the scattering, decay and inverse decay of thermal particles) becomes an important source of the cosmic axino abundance \[8–14\]. Although suppressed by the intermediate PQ symmetry breaking scale, \( v_{PQ} \), the axino interactions turn out to be efficient enough to generate a huge number of axinos unless the reheat temperature is much lower than the weak scale.

If the axino has a typical mass in the range of \( 10^2 - 10^3 \) GeV and the reheat temperature is above the electroweak scale, the axino cannot be dark matter as its thermal population easily overcloses the Universe. Then, it has to decay into the LSP dark matter such as the usual neutralino LSP \[12, 15, 16\] or gravitino \[17\]. Since the axino lifetime is suppressed by \( v_{PQ}^2 \), the axino decay may occur very late to produce the neutralino dark matter after its freeze-out causing overabundant neutralino density. This problem can be evaded if \( v_{PQ} \) takes its lower value to render the axino decay before the neutralino freeze-out, otherwise the neutralino LSP must have a large annihilation cross-section to allow a sufficient reannihilation \[15\].

The thermal axino production in the KSVZ model has been studied extensively taking a simple assumption of the effective QCD interaction below the PQ scale \[9–11\] and more carefully considering a general situation \[13\]. Axino couplings in the DFSZ model are dif-
ferent from those in the KSVZ model and their impact on the thermal axino production has
been considered recently in Refs. [12–14]. In this paper, we provide more general analysis
of the DFSZ axino abundance including the scattering, decay and inverse decay processes.
Then, we explore the Bino-Higgsino dark matter parameter region depending on the PQ
symmetry breaking scale.

The paper is organized as follows. In Section 2, we describe the supersymmetric DFSZ
model to derive the dominant axino couplings. In Section 3, the DFSZ axino abundances
coming from various channels are calculated and compared with each other. Since the
DFSZ axinos are overproduced as far as the reheat temperature is above the weak scale, we
investigate its impact on the neutralino dark matter property by taking some benchmark
parameter points in Section 4. We conclude in Section 5.

II. AXINO COUPLINGS IN THE SUPERSYMMETRIC DFSZ MODEL

One of the hierarchy problems in the minimal supersymmetric standard model is the
µ problem: “why the Higgs bilinear parameter, µ, sits at the TeV scale?” This problem
can be nicely resolved in connection with the axion solution of the strong CP problem à la
Kim-Nilles [18]. Extending the Higgs sector with

\[ W_{DFSZ} = \lambda_H \frac{P^2}{M_P} H_u H_d, \]

where \( M_P \) is the reduced Planck mass, one can introduce the PQ symmetry under which
the Higgs doublet superfields \( H_{u,d} \) and the gauge singlet field \( P \) are charged. In order to
break the PQ symmetry, one can introduce a PQ sector like

\[ W_{PQ} = \lambda_S S \left( P Q - \frac{v_{PQ}^2}{2} \right) \]

which will lead to \( \langle P \rangle \sim \langle Q \rangle \sim v_{PQ}/\sqrt{2} \). One can then get an appropriate µ term: \( \mu = \lambda_H \langle P \rangle^2 / M_P \). This is nothing but the supersymmetric realization of the DFSZ axion model [3]. In this scheme, the axion supermultiplet is a combination of mostly \( P \) and \( Q \), and a small

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mixture of $H_u$ and $H_d$. Thus, the axino interaction is given by the axino-Higgs-Higgsino:

$$\mathcal{L}_{DFSZ} = c_H \frac{\mu}{v_{PQ}} \tilde{a} [H_u \tilde{H}_d + \tilde{H}_u H_d] + h.c. \quad (3)$$

And after the electroweak symmetry breaking, the axino-top-stop coupling induced by the axino-Higgsino mixing also becomes important:

$$\mathcal{L}_{DFSZ, top} = c_t \frac{m_t}{v_{PQ}} \tilde{a} [\tilde{t} \tilde{c} + \tilde{c} \tilde{t}] + h.c. \quad (4)$$

where $c_H$ and $c_t$ are order-one parameters depending on the PQ symmetry breaking sector and other couplings proportional to smaller quark or lepton masses are neglected. As the axino couplings are of order $\mu/v_{PQ} \lesssim 10^{-8}$, the axinos cannot be in thermal equilibrium but can be produced thermally by the scattering, decay and inverse decay coming from the couplings (3) and (4). For our numerical calculation of the thermal axino production in the next section, we will put $c_H = 2$ and $c_t = 2$, which corresponds to assigning the PQ charge 1 to each Higgs supermultiplet, respectively, with the PQ sector Eq. (2).\textsuperscript{1} Note that the axino-top-stop coupling arises only after the electroweak symmetry breaking and thus does not contribute to the thermal axino production if the temperature of the Universe is larger than the weak scale.

Let us now compare the DFSZ axino couplings to the KSVZ axino couplings. In the supersymmetic KSVZ model, one introduces a heavy quark pair $(X, X^c)$ carrying the PQ charge:

$$W_{KSVZ} = \lambda_X PXX^c \quad (5)$$

from which the heavy quark gets an intermediate mass, $M_X \sim \lambda_X v_{PQ}/\sqrt{2}$. Below the scale $M_X$, the axino gets an effective QCD interaction:

$$\mathcal{L}_{QCD} = \frac{g_s^2}{32\pi^2} \frac{1}{\sqrt{2}v_{PQ}} \tilde{a} \sigma^{\mu\nu} \tilde{g}^a G_{\mu\nu}^a + h.c., \quad (6)$$

from which the previous calculation of the KSVZ axino abundance was preformed \textsuperscript{9,11}\textsuperscript{1}. Note that the physically relevant parameter is $c_{H,t}/v_{PQ}$ so that $c_{H,t}$ also depends on the normalization convention on $v_{PQ}$. $c_t$ can be obtained from the axino-Higgsino mixing Eq. (27) with $\mu \gg m_{\tilde{a}}$.\textsuperscript{4}
to show that the axino relic density is proportional to the reheat temperature $T_R$ of the Universe. However, a recent study showed that such a $T_R$-dependence does not occur if $T_R$ is between $v_{PQ}$ and $M_X$ as the axino abundance is determined by the Yukawa coupling $\lambda_X \sim \sqrt{2}M_X/v_{PQ}$ and this property is applied to the DFSZ axino \[13\].

Let us recapitulate the result of Ref. [13] to show that the DFSZ axino abundance is independent of the reheat temperature. After the PQ symmetry breaking, we get the effective axino coupling with the Higgs and Higgsino fields (3) (which corresponds to the non-linear realization of the PQ symmetry with the parameter $c = 0$ in Ref. [13]). This leads to the 1PI axino-gaugino-gauge boson interaction of dimension 5 from the diagram in Fig. 1. The corresponding amplitude is given by

$$A = \frac{g^2}{16\pi^2\sqrt{2}v_{PQ}}c_H \int_0^1 dx \int_0^{1-x} dy \, \frac{2\mu^2\bar{u}(p_1 + p_2)\sigma_{\mu\nu}\gamma_5 u(p_1)\epsilon^{\mu}p_2'}{\mu^2 - [p_1^2x(1-x) + p_2^2y(1-y) + 2(p_1 \cdot p_2)xy]}$$  \hspace{1cm} (7)$$

for the axino and the $SU(2)$ gauge supermultiplet interaction. It is then easy to see the limiting behavior of the loop integral: $1/p^2$ if $|p| \gg \mu$, and $1/\mu^2$ if $\mu \gg |p|$ assuming $\mu \sim m_H$, which tells us that the axino production through the effective axion-gaugino-gauge boson interaction is suppressed by $\mu^2/T^2$ for $T > \mu$ if there is no other heavier gauge charged and PQ charged supermultiplet than the scale $\mu$, which is the case for the "pure" DFSZ models.\[3\]

In this case, the axino production will be determined by the tree level interaction Eq. (3) so that the DFSZ axino abundance becomes independent of $T_R$. Still if we assume some additional heavier gauge charged and PQ charged supermultiplet of some mass $M$ larger than the scale $\mu$, the axino production will be dominated by the effective interaction

\[2\] Note that a different claim was made in Ref. [14].

\[3\] We refer the “pure” DFSZ to the models where gauge charged and PQ charged particles are only among the MSSM particles, and the “mixed” DFSZ to the models containing exotic gauge charged and PQ charged supermultiplets in addition to the MSSM particles.
Eq. (6) between the energy scales $8\pi^2\mu$ and $M$ as can be seen in the table 1 of [13], and the axino abundance becomes proportional to $T_R$ in this regime as in the KSVZ case. Previous studies on the DFSZ axino production with the Eq. (6) as the dominant interaction at high reheat temperature effectively correspond to such “mixed” DFSZ models. In this paper, we consider the “pure” DFSZ case with the Higgs supermultiplet as the heaviest gauge charged and PQ charged supermultiplet. So while the DFSZ axino abundance is independent of $T_R$, the KSVZ axino abundance is proportional to $T_R$ and can be larger than the DFSZ axino abundance for larger $T_R$ [12].

Note that the axino effective interactions with $SU(2) \times U(1)$ gauge supermultiplets are obtained below the scale $\mu$ by integrating out the Higgs supermultiplets. In a similar way, the effective axino-gluino-gluon interaction (6) in the “pure” DFSZ model arises after integrating out the quark supermultiplet having the Yukawa coupling as in Eq. (4), along with its supersymmetric counterpart: the usual effective axion-gluon-gluon interaction solving the strong CP problem.

Another distinction of the DFSZ axino from the KSVZ axino comes from the lifetime calculated from the couplings (3) and (6), respectively. As was shown in Ref. [15], the thermal abundance of the KSVZ axino can dominate the energy density of the Universe for larger $v_{PQ}$. But the DFSZ axino lives shorter than the KSVZ axino and thus it always decays before it overdominates the Universe as will be discussed in Section IV.

III. THERMAL PRODUCTION OF THE DFSZ AXINO

Thermal production of the DFSZ axino has been computed previously considering the decay and inverse decay in Ref. [12] and the scattering involving the axino-Higgsino-Higgs coupling and gauge coupling of Higgs multiplet in Ref. [13] as depicted in Fig. 2. There are additional processes involving the top Yukawa coupling as depicted in Fig. 3 which can be potentially more important since the top Yukawa coupling is of order of unity. In this section, we combine all the possible processes to evaluate the axino yield for each channel. For the calculation, we take some benchmark points for the relevant particle masses including supersymmetry breaking effect both in the unbroken phase and in the broken phase of the electroweak symmetry.

In Fig. 4 the thermal axino number density $Y_\tilde{a} \equiv n_{\tilde{a}}/s$ per the entropy density is analyzed.
FIG. 2: Examples of scattering diagrams (considered in Fig. 3-7 of Ref. [13]) involving the axino-Higgs-Higgsino coupling and gauge couplings of the Higgs multiplet. There are also two other diagrams with supersymmetric gauge vertices and t, u-channel diagrams. All processes are included in the calculation.

FIG. 3: Examples of scattering diagrams involving the axino-Higgs-Higgsino coupling and top Yukawa coupling. There are also t, u-channel diagrams. All processes are included in the calculation.

for the benchmark points: $\mu = 1$ TeV, $m_{H_u} = 100$ GeV, $m_{H_d} = 500$ GeV, $m_{\tilde{t}} = 1.5$ TeV, and $m_{\tilde{a}} = 100$ GeV with $v_{PQ} = 10^{11}$ GeV. In this parameter space, the Higgsino decay $\tilde{H} \to H \tilde{a}$ is allowed to contribute to the thermal axino production in addition to the scattering processes from Fig. 2 and 3 (red line). As can be seen in the plot, three contributions are almost the same in the region of $T_R \gtrsim \mu$. In the slightly lower temperature, i.e. $T_R \lesssim \mu$, the decay contribution is about an order of magnitude larger than the others because scattering processes are doubly suppressed by the Boltzmann factor while decay process has only one Boltzmann suppression.

The second example is depicted in Fig. 5 for which we take the benchmark points: $\mu = 1$ TeV, $m_{H_u} = 100$ GeV, $m_{H_d} = 500$ GeV, $m_{\tilde{t}} = 300$ GeV, $m_{\tilde{a}} = 100$ GeV with $v_{PQ} = 10^{11}$ GeV. The only difference from the previous example is the stop mass. In this example, a

$^4 m_{H_u}$ and $m_{H_d}$ denote $(m_2^2 + |\mu|^2)^{1/2}$ and $(m_1^2 + |\mu|^2)^{1/2}$, where $m_2$ and $m_1$ are soft mass terms of $H_u$ and $H_d$, respectively.
FIG. 4: The axino yield from the scattering diagrams in Fig. 2 (blue line), the scattering diagrams in Fig. 3 (red line), and the decay $\tilde{H} \to H\tilde{a}$ (green line).

FIG. 5: Same as in Fig. 4 but with the parameter choice allowing a resonant axino production in the channel of Fig. 3(b)
small stop mass is considered to allow a resonant axino production in the channel $\tilde{t} + \tilde{t} \rightarrow \tilde{H} \rightarrow \tilde{a} + H$ (Fig. 3(b)). The resonant process can enhance the production cross section by factor of $1/Γ^2$, where $Γ$ is the decay rate of the intermediate particle, the Higgsino in this case. As the axino thermal production is obtained by integrating the cross section over $T = [0, T_R]$, such a resonance effect is averaged out by the width of the resonance, $Γ$, resulting in the enhancement of the axino yield by factor of $1/Γ$. In this example, we have a quite large decay rate of Higgsino, $Γ \sim 100$ GeV, leading to $μ/Γ \sim \mathcal{O}(10)$ enhancement for the resonant production channel. Thus, the corresponding scattering process dominates the others by about factor 4.

The third case, shown in Fig. 6 is for a heavy axino which can decay to a Higgs boson and a Higgsino: $m_{\tilde{a}} = 1$ TeV and $μ = 300$ GeV with the other parameters kept same as in the previous case. As one can see, the axino yield from the inverse decay is more or less the same as the decay contribution in the previous examples.

From the above calculation, one finds the axino yield $Y_{\tilde{a}} \sim 10^{-5}(10^{11}$ GeV/$v_{PQ})^2$ for each

\footnote{Our results in Figs. 4-6 are different from Fig. 3 of Ref. [14] showing $T_R$ dependence as remarked in Section II.}
allowed channel of scattering, decay or inverse decay as far as the reheat temperature above the electroweak scale ($T_R \gtrsim \mu$). In some cases, a resonant production can occur to enhance the axino yield in a certain scattering process. As a consequence, thermally produced axinos would severely overclose the Universe if they take a weak scale mass and are stable.

The thermal axino production can be effectively suppressed if the reheat temperature of the Universe is below the weak scale. In such a case, the relevant processes for axino production strongly depend on a specific mass spectrum with broken electroweak symmetry. For the purpose of our presentation, we will discuss only a representative behavior taking a simplified benchmark point. To this end, we assume that the stop, Wino and CP-odd Higgs are heavy enough ($\sim 1.5$ TeV) to be decoupled at low reheat temperature. Also we set $m_{\tilde{a}} = 500$ GeV which is taken to be the reference value in the next section discussing heavy axino decay. For the Higgsino mass, we choose $\mu = 1$ TeV allowing the decay $\tilde{H} \rightarrow h\tilde{a}$. Note also that the $\tilde{t} \rightarrow t\tilde{a}$ decay processes are possible. Fig. 7 shows the result for the axino yield in this benchmark point at low reheat temperature below 200 GeV. As we have observed in Fig. 4, the decay contribution from the Higgsino is dominant over the scattering

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6 In this calculation, we use the zero temperature value for the vacuum expectation value of the Higgs field $v = 174$ GeV.
contributions because of less Boltzmann suppression. On the other hand, the contribution from the stop decay is smaller because the process becomes available from the Higgsino-axino mixing by the electroweak symmetry breaking and thus involves the top mass \( m_t \) which is much smaller than \( \mu \) appearing in the Higgsino decay process. We can observe that all contributions become rapidly decreasing after the electroweak scale and drop down drastically below 50 GeV being heavily suppressed by the Boltzmann factors. Due to such a high Boltzmann suppression, the heavy axino can have a right dark matter density for \( T_R \sim 50 \text{ GeV} \).

IV. HEAVY AXINO DECAY AND NEUTRALINO DARK MATTER

In this section, we explore the cosmological impact of a heavy axino which cannot be the LSP and thus has to decay to a dark matter candidate which we assume to be a neutralino LSP. Such a scenario has been considered first in Ref. [15] for the case of the KSVZ axino and later in Ref. [12] for the case of the DFSZ axino. Generalizing the latter analysis, we examine the dark matter property depending on the neutralino parameter space and the PQ scale.

Depending on the mass spectrum, the axino can decay to a Higgsino and a Higgs, a Neutralino (Bino-like) and a photon, etc. We assume here, for simplicity and consistency with current experiment [21, 22], that all the squarks and sleptons are heavier than the Higgsino. One can consider two regimes of the axino mass as follows.

- For \( m_\tilde{a} > \mu \), the dominant decay process of the axino is
  \[
  \tilde{a} \rightarrow \tilde{H}^0 + H^0/Z \quad \text{or} \quad \tilde{H}^\pm + H^{\mp}/W^{\mp}
  \]
  (8)

  where \( H^0 \) stands for neutral Higgs states, i.e. \( h, H, \) or \( A \). This decay mode is due to the tree-level axino-Higgs-Higgsino coupling. If allowed, it will provide the most efficient axino decay.
For $m_{\tilde{a}} < \mu$, possible decay processes are

\begin{align}
\tilde{a} &\rightarrow \tilde{\chi} + \gamma \\
\tilde{a} &\rightarrow H^0/H^\mp + \tilde{H}^0*/\tilde{H}^{\pm*} \rightarrow H^0/H^\mp + H^0/Z/H^\mp/W^\mp + \tilde{\chi} \\
\tilde{a} &\rightarrow H^0 + \tilde{\chi} \\
\tilde{a} &\rightarrow Z + \tilde{\chi}
\end{align}

The first mode is due to the 1PI axino-photon-neutralino interaction. The second mode is a 3-body decay due to the tree-level axino-Higgs-Higgsino interaction. The third mode is a tree-level process due to the axino-Higgs-Higgsino coupling with the Higgsino-Bino and axino-Higgsino mixing. Finally the last one is a tree-level process due to the axino-Higgsino mixing.
Following the calculation described in Appendix, we compute the total decay rate in Fig. 8. Unlike the KSVZ case where the axino yield depends on the reheat temperature, the DFSZ axino yield is determined by the mass spectrum and can be parameterized by

\[ Y_\tilde{a} = 10^{-5} \xi \left( \frac{\mu}{\text{TeV}} \right)^2 \left( \frac{10^{11} \text{ GeV}}{v_{PQ}} \right)^2 \]  

if the reheat temperature is larger than the electroweak scale. Here \( \xi \) is an order-one quantity depending on the particle mass spectrum. Such abundant axinos will decay to yield overproduction of neutralinos which may thermalize or reannihilate depending on the axino lifetime. The axino decay temperature \( T_D \) is given by

\[ T_D = 1.4 \text{ GeV} \left( \frac{70}{g_\ast} \right)^{1/4} \left( \frac{3 \times 10^{-7} \text{ s}}{\tau_\tilde{a}} \right)^{1/2}. \]  

If \( T_D \) is larger than the freeze-out temperature \( T_f \) of the neutralino LSP, the overproduced LSPs will thermalize to be settled down to the usual freeze-out relic density. For \( T_D < T_f \), the overabundant neutralino density can be depleted by reannihilation and the final relic density is determined by

\[ Y_{\tilde{\chi}}^{-1}(T) \approx Y_{\tilde{\chi}}^{-1}(T_D) + \frac{\langle \sigma_A v \rangle s(T_D)}{H(T_D)}, \]  

where \( Y_{\tilde{\chi}}(T_D) = Y_{\tilde{\chi}}(T_H) + Y_\tilde{a} \approx Y_\tilde{a} \) for the reheat temperature above the electroweak scale. Since \( T_D < T_f \), we need the annihilation rate \( \langle \sigma_A v \rangle \) of the neutralino LSP larger than the canonical value in order to get a right relic density for dark matter.

For low reheat temperature, \( Y_\tilde{a} \) can become comparable to or smaller than \( Y_{\tilde{\chi}}(T_H) \). For example, we can find this occurs around the temperature \( T \sim 40 \text{ GeV}, 50 \text{ GeV}, \) and \( 60 \text{ GeV} \) for \( v_{PQ} = 10^{10} \text{ GeV}, 10^{11} \text{ GeV}, \) and \( 10^{12} \text{ GeV} \), respectively, from the result of Fig. 7 with the assumed mass spectrum. Below this temperature, the neutralino relic abundance is given by the standard results with a negligible axino contribution.

In the case of the KSVZ axino, the axino lifetime determined by the coupling (6) can be long enough so that there could occur a period of axino matter domination [15]. On the other hand, the DFSZ axino lifetime determined by the coupling (3) is typically shorter than that of the KSVZ axino, and thus there occurs no DFSZ axino domination as shown explicitly in
Figs. [10][12] To get an rough estimate, let us consider the largest axino lifetime $\sim 10^{-5} \text{ sec}$ found in Fig. [12] for $v_{PQ} = 10^{12} \text{ GeV}$. This give $T_D \sim 0.1 \text{ GeV}$ from Eq. [14]. This can be compared with the axino-radiation equality temperature $T_{eq}$ determined by $T_{eq} = 4m_{\tilde{a}}Y_{\tilde{a}}/3$ [15] which give $T_{eq} \sim 10^{-4} \text{ GeV}$ for $m_{\tilde{a}} \sim 1 \text{ TeV}$ and $Y_{\tilde{a}} \sim 10^{-7}$. Thus, it becomes clear to have $T_{eq} < T_D$, that is, the axino decays before it overdominates the Universe, for almost all the parameter space. Note that the axino lifetime can become much larger near the boundary line between the neutralino LSP and axino LSP, so the axino dominated universe can be realized. In this case, however, the neutralino abundance becomes too large to get right dark matter density.

Let us now analyze the relic abundance of the neutralino dark matter in the simplified MSSM parameter space varying the PQ scale $v_{PQ}$. Only relevant MSSM parameters are $M_1$, $M_2$ and $\mu$ in our calculation.

In Fig. [9] we show the contours of the usual freeze-out relic abundance of the neutralino LSP and the direct detection rate in $M_1-\mu$ plane, setting $M_2 = 2 \text{ TeV}$ for simplicity. Contours are numerically obtained by using SUSY-HIT [24] and micrOMEGAs 2.4 [23]. Note that the WMAP consistent relic density $\Omega_{DM}h^2 \approx 0.1$ [25] is obtained in the Higgsino-like LSP region ($M_1 \approx \mu$) and the resonant annihilation region with $M_1 \approx m_A/2$ as expected. One can also see that the direct detection experiment [26] excludes the Higgsino-like region and
Let us proceed to consider the effect of the axino late decay in Figs. [10][12] for the reheat temperature above the electroweak scale. We take $m_{\tilde{a}} = 500$ GeV and $\tan \beta = 10$ for all the plots, and $v_{PQ} = 10^{10}$ GeV in Fig. [10] $v_{PQ} = 10^{11}$ GeV in Fig. [11] and $v_{PQ} = 10^{12}$ GeV in Fig. [12].

As can be seen in the left panel of Fig. [10] the Higgsino-like LSP with $\mu \approx 400$ GeV in the upper-left part gives the correct dark matter relic density. In this part, the Bino-
Higgsino mixing becomes negligible, and the axino decay is determined by the tree-level axino-Higgino-Higgs coupling (3). This is why the contour is almost parallel to the vertical axis in the large $M_1$ region. Note that the phase space of the axino 2-body decay to the Higgsino-like LSP and the Higgs becomes very small for $\mu \approx 400$ GeV. For $\mu \gtrsim 400$ GeV, the phase space of the axino 2-body decay is closed, but the axino can decay to the Higgsino-like LSP through the processes like 3-body decays with almost massless quarks and leptons via the off-shell Higgses or Z-boson, 2-body decay by the axino-photon-neutralino interaction in Eqs. (9), etc. However all these processes are much suppressed by phase space factors or the 1-loop factor. So in this region, the axino lives long enough to decay after the Higgsino-like LSP freeze-out. Thus, one can understand that the vertical line with $\mu \approx 400$ GeV with $M_1 \gtrsim 400$ GeV is the parameter region which provides a correct dark matter density with an appropriately enhanced annihilation rate for the given axino lifetime $\tau_\tilde{a} \approx 10^{-8}$ s (as shown in the right panel) according to the reannihilation equation (15). On the other hand one can see that the thick contour line for the correct dark matter density in the lower-right part of the left panel is almost same as in Fig. 9 as the corresponding axino lifetime is short enough for the axino to decay before the Bino-like LSP freeze-out.

For $v_{PQ} = 10^{11}$ GeV, the axino decays later as seen in the right panel of Fig. 11. As a consequence, the contour line for the right dark matter density changes slightly compared to the previous case. More dramatic change can be found for $v_{PQ} = 10^{12}$ GeV as in Fig. 12. The Higgsino-like dark matter becomes significantly lighter ($\mu \sim 250$ GeV) and the Bino-
like dark matter needs more fine-tuned resonance both of which guarantee more enhanced reannihilation by a factor of $T_f/T_D$. Note also that the light Higgsino-like dark matter is allowed by the direct detection experiment only for the region of $M_1 \gtrsim 700$ GeV and the Bino-like dark matter region requiring stronger resonance is more restricted (compare with the blue lines in Fig. 9).

V. CONCLUSION

We examined thermal production of the DFSZ axino and its impact on the dark matter property. The DFSZ axino interactions are governed by two important couplings: the axino-Higgs-Higgsino and axino-top-stop coupling proportional to $\mu/v_{PQ}$ and $m_t/v_{PQ}$, respectively. The latter coupling, which arises from the axino-Higgsino mixing, is effective only after the electroweak symmetry breaking. All the scattering, decay and inverse decay processes if allowed are shown to produce the typical DFSZ axino density of $Y_\tilde{a} \sim 10^{-5}(10^{11}$GeV/$v_{PQ})^2$ when the reheat temperature is larger than the electroweak scale. In a certain mass parameter region, a resonant scattering can occur to allow enhanced axino production. Thus, if the axino is the LSP, its mass has to be very light to get the right dark matter density. If the axino LSP mass is at the TeV scale, the reheat temperature needs to be below around 50 GeV in order not to overclose the Universe.

A heavy DFSZ axino can decay to a neutralino LSP through the axino-Higgs-Higgsino coupling, which leads to a huge neutralino population. Its impact is studied to identify the Bino-Higgsino LSP region consistent with the observed dark matter density and the direct detection limit of dark matter. For lower PQ scale, a new Higgsino-like LSP region appears to meet an appropriate reannihilation condition, whereas the usual Bino-like LSP region with a resonant annihilation through a CP-odd Higgs boson remains unchanged as the axino decays before the neutralino freeze-out. For higher PQ scale, the axino decay occurs much later than the neutralino freeze-out which requires stronger reannihilation. As a result, the neutralino dark matter region is more depleted to a lighter Higgsino-like LSP and a more restricted Bino-like LSP.

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Appendix

A. Axino-neutralino mixing

In the supersymmetric DFSZ axion model, we have axino-neutralino mixing because of vacuum expectation values of Higgs doublets. Let us write down the axino-neutralino mass matrix in the basis of \( (\tilde{a}, \tilde{B}, \tilde{W}^3, \tilde{H}_d^0, \tilde{H}_u^0) \):

\[
M = \begin{pmatrix}
m_\tilde{a} & 0 & 0 & c_{H\mu}v_s/\mu & c_{H\mu}c_\beta/\mu \\
0 & M_1 & 0 & -c_\beta s_W m_Z & s_\beta s_W m_Z \\
0 & 0 & M_2 & c_\beta c_W m_Z & -s_\beta c_W m_Z \\
-c_{H\mu}v_s/\mu & c_\beta s_W m_Z & c_\beta c_W m_Z & 0 & -\mu \\
c_{H\mu}c_\beta/\mu & s_\beta s_W m_Z & -s_\beta c_W m_Z & 0 & -\mu \\
\end{pmatrix}, \tag{16}
\]

where \( s_\beta = \sin \beta, c_\beta = \cos \beta, s_W = \sin \theta_W, c_W = \cos \theta_W \) and \( v = 174 \text{ GeV} \). The above matrix can be diagonalized by the method of perturbative diagonalization as in Ref. [19]:

\[
M_{\text{diag}} = N M N^T = V M' V^T = V U M U^T V^T \tag{17}
\]

where

\[
U = \begin{pmatrix}
1 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 \\
0 & 0 & \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\
0 & 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & 0 \\
\end{pmatrix}, \tag{18}
\]

and

\[
M' = \begin{pmatrix}
A & B \\
B^T & C \\
\end{pmatrix}, \tag{19}
\]
with

\[
A = \begin{pmatrix} m_\tilde{a} & 0 & 0 \\ 0 & M_1 & 0 \\ 0 & 0 & M_2 \end{pmatrix}, \quad B = \begin{pmatrix} (c_H \mu v(s_\beta - c_\beta))/\sqrt{2}v_{PQ} & c_H \mu v(s_\beta + c_\beta))/\sqrt{2}v_{PQ} \\ -m_Z s_W(s_\beta + c_\beta)/\sqrt{2} & m_Z s_W(s_\beta - c_\beta)/\sqrt{2} \\ m_Z c_W(s_\beta + c_\beta)/\sqrt{2} & m_Z c_W(s_\beta - c_\beta)/\sqrt{2} \end{pmatrix}, \quad C = \begin{pmatrix} \mu & 0 \\ 0 & -\mu \end{pmatrix}.
\]

(20)

In the leading order we have

\[
V_{nm} = M'_{mn}/(M_{nn} - M_{mm}).
\]

(21)

As far as \(|M_1 - \mu|, |m_\tilde{a} - \mu| \gg v/v_{PQ}, \mu/v_{PQ}\), we find

\[
V_{03} = \frac{M'_{30}}{m_\tilde{a} - \mu} = -\frac{c_H \mu v(s_\beta - c_\beta)}{\sqrt{2}v_{PQ}(\mu - m_\tilde{a})},
\]

(22)

\[
V_{04} = \frac{M'_{40}}{m_\tilde{a} + \mu} = \frac{c_H \mu v(s_\beta + c_\beta)}{\sqrt{2}v_{PQ}(\mu + m_\tilde{a})},
\]

(23)

\[
V_{13} = \frac{M'_{31}}{M_1 - \mu} = \frac{m_Z s_W(s_\beta + c_\beta)}{\sqrt{2}(\mu - M_1)},
\]

(24)

\[
V_{14} = \frac{M'_{41}}{M_1 + \mu} = \frac{m_Z s_W(s_\beta + c_\beta)}{\sqrt{2}(\mu + M_1)}.
\]

(25)

where the zeroth component denotes the axino component. Hence we have

\[
N_{03} = \frac{1}{\sqrt{2}}(V_{03} + V_{04}) = -\frac{c_H \mu v(m_\tilde{a} s_\beta - \mu c_\beta)}{v_{PQ}(\mu^2 - m_\tilde{a}^2)},
\]

(26)

\[
N_{04} = \frac{1}{\sqrt{2}}(-V_{03} + V_{04}) = \frac{c_H \mu v(\mu s_\beta - m_\tilde{a} c_\beta)}{v_{PQ}(\mu^2 - m_\tilde{a}^2)},
\]

(27)

\[
N_{13} = \frac{1}{\sqrt{2}}(V_{13} + V_{14}) = \frac{m_Z s_W(\mu s_\beta + M_1 c_\beta)}{\mu^2 - M_1^2},
\]

(28)

\[
N_{14} = \frac{1}{\sqrt{2}}(-V_{13} + V_{14}) = -\frac{m_Z s_W(M_1 s_\beta + \mu c_\beta)}{\mu^2 - M_1^2}.
\]

(29)

Having obtained the mixing matrices \(N, U\) and \(V\), one can now get the following axino couplings following Ref. [20].

**Axino-neutralino-\(Z\) boson coupling:**

\[
\mathcal{L}_{Z\tilde{a}\chi^0} = -\frac{g_2}{c_W} O''_{0n} Z_{\mu} \bar{\tilde{a}} \gamma^\mu \gamma^5 \chi^0_n + \text{h.c.}
\]

(30)
where

\[ O''_{0n} = \frac{1}{2} (-N_{03} V_{n3} + N_{04} V_{n4}). \]  

(31)

Axino-chargino-\(W\) boson coupling:

\[ \mathcal{L}_{W^\pm\tilde{a}\tilde{\chi}^\mp} = g_2 W^- \tilde{a} \gamma^\mu \left[ O'^L_{0n} P_L + O'^R_{0n} P_R \right] \tilde{\chi}_n^+ \]  

+ h.c.,  

(32)

where

\[ O'^L_{0n} = - \frac{1}{\sqrt{2}} N_{04} V_{n2} + N_{02} V_{n1}, \]  

(33)

\[ O'^R_{0n} = \frac{1}{\sqrt{2}} N_{03} U_{n2} + N_{02} U_{n1}. \]  

(34)

Axino-neutralino-neutral Higgs coupling:

\[ \mathcal{L}_{h\tilde{a}\tilde{\chi}^0} = g_2 T_{h0n} h \tilde{a} \tilde{\chi}^0_n, \]  

(35)

\[ \mathcal{L}_{H\tilde{a}\tilde{\chi}^0} = g_2 T_{H0n} H \tilde{a} \tilde{\chi}^0_n, \]  

(36)

\[ \mathcal{L}_{A\tilde{a}\tilde{\chi}^0} = i g_2 T_{A0n} A \tilde{a} \gamma^5 \tilde{\chi}^0_n, \]  

(37)

where

\[ T_{h0n} = \sin \alpha Q''_{0n} + \cos \alpha S''_{0n}, \]  

(38)

\[ T_{H0n} = - \cos \alpha Q''_{0n} + \sin \alpha S''_{0n}, \]  

(39)

\[ T_{A0n} = - \sin \beta Q''_{0n} + \cos \beta S''_{0n}, \]  

(40)

\[ Q''_{0n} = \frac{1}{2} N_{03}(N_{n2} - \tan \theta_W N_{n1}) + \frac{c_{H\mu}}{\sqrt{2} g_2 v_P Q} N_{00} N_{n4} + (0 \leftrightarrow n), \]  

(41)

\[ S''_{0n} = \frac{1}{2} N_{04}(N_{n2} - \tan \theta_W N_{n1}) - \frac{c_{H\mu}}{\sqrt{2} g_2 v_P Q} N_{00} N_{n3} + (0 \leftrightarrow n). \]  

(42)

Axino-chargino-charged Higgs coupling:

\[ \mathcal{L}_{H^\pm\tilde{a}\tilde{\chi}^\mp} = - g_2 H^- \tilde{a} \left[ Q'^L_{0n} P_L + Q'^R_{0n} P_R \right] \tilde{\chi}_n^+ \]  

+ h.c.,  

(43)
where

\[ Q_{0n}^{L} = \cos \beta \left[ N_{01} V_{n1} + \frac{1}{\sqrt{2}} (N_{02} + \tan \theta_W N_{01}) V_{n2} \right] + \sin \beta \frac{c_{H \mu}}{g_2 v_{PQ}} N_{00} V_{n2} \]  

(44)

\[ Q_{0n}^{R} = \sin \beta \left[ N_{03} U_{n1} + \frac{1}{\sqrt{2}} (N_{02} + \tan \theta_W N_{01}) U_{n2} \right] + \cos \beta \frac{c_{H \mu}}{g_2 v_{PQ}} N_{00} U_{n2} \]  

(45)

**B. Axino decay rate**

We first consider the case of \( m_\tilde{a} < \mu \). Among the 4 possible decay modes, (2) is one-loop suppressed and (10) is suppressed by 3 body phase space. On the other hand, (11) and (12) are tree-level processes which arise from the axino-Higgsino and Higgsino-Bino mixing. Being 2-body decays they are the dominant processes. The decay rates are given by

\[ \Gamma(\tilde{a} \rightarrow Z + \chi) = \frac{m_\tilde{a} \lambda^{1/2}(1, \kappa_Z, \kappa_\chi^2)}{16\pi} \frac{g_2^2}{c_W^2} |O_{10}''|^2 \frac{(1 + \kappa_\chi^2 - \kappa_Z^2)(1 - \kappa_\chi^2 + 2\kappa_Z^2)}{\kappa_Z^2} \]

\[ \approx \frac{g_2^2 t_W^2 v^2 m_\tilde{a}^5}{64 \pi^2 v_{PQ}^2 v_\mu^4} \]  

(46)

\[ \Gamma(\tilde{a} \rightarrow h + \chi) = \frac{m_\tilde{a} \lambda^{1/2}(1, \kappa_h, \kappa_\chi^2)}{16\pi} \frac{g_2^2}{c_W^2} |T_{h01}|^2 \frac{(1 + \kappa_\chi^2 - \kappa_h^2)}{2} \]

\[ \approx \frac{g_2^2 t_W^2 v^2 m_\tilde{a}}{16 \pi^2 v_{PQ}^2} \]  

(47)

\[ \Gamma(\tilde{a} \rightarrow H + \chi) = \frac{m_\tilde{a} \lambda^{1/2}(1, \kappa_h, \kappa_\chi^2)}{16\pi} \frac{g_2^2}{c_W^2} |T_{H01}|^2 \frac{(1 + \kappa_\chi^2 - \kappa_H^2)}{2} \]

\[ \approx \frac{g_2^2 t_W^2 v^2 m_\tilde{a}^3}{64 \pi^2 v_{PQ}^2 v_\mu^2} \]  

(48)

\[ \Gamma(\tilde{a} \rightarrow A + \chi) = \frac{m_\tilde{a} \lambda^{1/2}(1, \kappa_h, \kappa_\chi^2)}{16\pi} \frac{g_2^2}{c_W^2} |T_{A01}|^2 \frac{(1 - \kappa_\chi^2 - \kappa_A^2)}{2} \]

\[ \approx \frac{g_2^2 t_W^2 v^2 m_\tilde{a}^3}{64 \pi^2 v_{PQ}^2 v_\mu^2} \]  

(49)

where \( g_2 \) is \( SU(2) \) coupling constant, \( c_W = \cos \theta_W, t_W = \tan \theta_W, \theta_W \) is the weak mixing angle, \( \lambda^{1/2}(1, a, b) = [(1 - a - b)^2 - 4ab]^{1/2} \), \( \kappa_Z = m_Z/m_\tilde{a}, \kappa_\chi = M_\chi/m_\tilde{a}, \kappa_h = m_h/m_\tilde{a}, \kappa_H = m_H/m_\tilde{a}, \) and \( \kappa_A = m_A/m_\tilde{a} \). \( O_{10}'' \), \( T_{h01}, T_{H01} \) and \( T_{A01} \) are given in (38), (39) and (40), respectively. The approximation in the second line of each decay rate is valid for \( \kappa_i \ll 1 \).

For the case of \( m_\tilde{a} > \mu \), the axino can directly decay to a Higgsino-like neutralino and a chargino so that the decay rates can be even higher than those in the case of \( m_\tilde{a} < \mu \). The
axino decay rates are

\[
\Gamma(\tilde{a} \rightarrow h + \tilde{H}^0) = \frac{m_{\tilde{a}} \lambda^{1/2}(1, \kappa_h, \kappa_\tilde{a})}{16\pi} g_2^2 |T_{h03}|^2 + |T_{h04}|^2 \left\{ (1 + \kappa_\mu)^2 - \kappa_h^2 \right\}
\]

\[
\approx \frac{1}{32\pi} \frac{\mu^2 m_{\tilde{a}}}{v_{PQ}}
\]

\(\text{(50)}\)

\[
\Gamma(\tilde{a} \rightarrow H + \tilde{H}^0) = \frac{m_{\tilde{a}} \lambda^{1/2}(1, \kappa_H, \kappa_\tilde{a})}{16\pi} g_2^2 |T_{H03}|^2 + |T_{H04}|^2 \left\{ (1 + \kappa_\mu)^2 - \kappa_H^2 \right\}
\]

\[
\approx \frac{1}{32\pi} \frac{\mu^2 m_{\tilde{a}}}{v_{PQ}}
\]

\(\text{(51)}\)

\[
\Gamma(\tilde{a} \rightarrow A + \tilde{H}^0) = \frac{m_{\tilde{a}} \lambda^{1/2}(1, \kappa_A, \kappa_\tilde{a})}{16\pi} g_2^2 |T_{A03}|^2 + |T_{A04}|^2 \left\{ (1 - \kappa_\mu)^2 - \kappa_A^2 \right\}
\]

\[
\approx \frac{1}{32\pi} \frac{\mu^2 m_{\tilde{a}}}{v_{PQ}}
\]

\(\text{(52)}\)

\[
\Gamma(\tilde{a} \rightarrow Z + \tilde{H}^0) = \frac{m_{\tilde{a}} \lambda^{1/2}(1, \kappa_Z, \kappa_\tilde{a})}{16\pi} g_2^2 \left[ |O''_{03}|^2 + |O''_{04}|^2 \right] \left\{ (1 + \kappa_\mu)^2 - \kappa_Z^2 \right\} \left( 1 + \kappa_\mu - \kappa_Z^2 \right) \kappa_\mu^2
\]

\[
\approx \frac{g_2^2}{64\pi c_W^2 v_{PQ}^2 m_{\tilde{a}}^2} v^2 \mu^2
\]

\(\text{(53)}\)

\[
\Gamma(\tilde{a} \rightarrow W^\pm + \tilde{H}^0) = \frac{m_{\tilde{a}} \lambda^{1/2}(1, \kappa_W, \kappa_\tilde{a})}{16\pi} g_2^2 \left\{ |O_{01}^L|^2 + |O_{01}^L|^2 \right\} \left\{ (1 - \kappa_Z^2)^2 + (1 + \kappa_\mu^2 - 2\kappa_W^2) \kappa_\mu^2 \right\}
\]

\[
\times \left\{ (1 - \kappa_\mu)^2 + (1 + \kappa_\mu^2 - 2\kappa_W^2) \kappa_\mu^2 \right\} \kappa_\mu^2
\]

\[
\approx \frac{g_2^2}{32\pi v_{PQ}^2 m_{\tilde{a}}^2} v^2 \mu^2 \kappa_\mu^2
\]

\(\text{(54)}\)

\[
\Gamma(\tilde{a} \rightarrow H^\pm + \tilde{H}^0) = \frac{m_{\tilde{a}} \lambda^{1/2}(1, \kappa_{H^\pm}, \kappa_\tilde{a})}{16\pi} g_2^2 \left\{ |Q_{01}^L|^2 + |Q_{01}^R|^2 \right\} \left\{ (1 + \kappa_\mu^2 - \kappa_{H^\pm}^2) + (Q_{01}^L Q_{01}^R) \kappa_\mu^2 \right\}
\]

\[
\approx \frac{1}{16\pi} \frac{\mu^2 m_{\tilde{a}}}{v_{PQ}}
\]

\(\text{(55)}\)

where \(\kappa_W = m_W/m_{\tilde{a}}, \kappa_{H^\pm} = m_{H^\pm}/m_{\tilde{a}}\) and \(\kappa_\mu = \mu/m_{\tilde{a}}\).

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