Morphology control of epitaxial monolayer transition metal dichalcogenides

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To advance fundamental understanding and ultimate application of transition-metal dichalcogenide (TMD) monolayers, it is essential to develop capabilities for the synthesis of high-quality single-layer samples. Molecular beam epitaxy (MBE), a leading technique for the fabrication of the highest-quality epitaxial films of conventional semiconductors has, however, typically yielded only small grain sizes and suboptimal morphologies when applied to the van der Waals growth of monolayer TMDs. Here, we present a systematic study on the influence of adatom mobility, growth rate, and metal:chalcogen flux on the growth of NbSe2, VSe2, and TiSe2 using MBE. Through this, we identify the key drivers and influence of the adatom kinetics that control the epitaxial growth of TMDs, realizing four distinct morphologies of the as-grown compounds. We use this to determine optimized growth conditions for the fabrication of high-quality monolayers, ultimately realizing the largest grain sizes of monolayer TMDs that have been achieved to date via MBE growth.

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I. INTRODUCTION

Transition metal dichalcogenides (TMDs), composed of a transition-metal (M) layer sandwiched between two chalcogen (X) layers, represent a particularly diverse materials family. In bulk, such covalently bonded MX2 monolayers are stacked with weak van der Waals bonding between neighboring layers. Depending on the filling of the transition-metal d-orbitals, a large variety of electronic properties are found, including semiconductors, metals, charge-density wave (CDW) systems, superconductors, and topologically nontrivial materials [1–4]. Excitingly, their properties can be significantly modified by changing the material’s thickness down to the monolayer limit. Famous examples include a thickness-tuned crossover from an indirect to a direct band gap in MoS2 [5,6], the realization of extremely high exciton binding energies as a result of reduced dielectric screening in the monolayer limit of various MX2 semiconductors [7], and the emergence of an Ising superconductivity in single-layer NbSe2, arising due to the combination of broken inversion symmetry and strong spin-orbit coupling [8–10].

The group-IV and -V TMDs, which are the focus of the current paper, are perhaps most famous for the CDW phases which they host. The group-V systems are perhaps most famous for the CDW phases which they host. The group-V systems are perhaps most famous for the CDW phases which they host. The group-V systems are perhaps most famous for the CDW phases which they host. The group-V systems are perhaps most famous for the CDW phases which they host. The group-V systems are perhaps most famous for the CDW phases which they host. The group-V systems are perhaps most famous for the...
here, however, on HOPG substrates enabling the study of the fundamental growth processes of TMDs via van der Waals epitaxy. Fresh HOPG surfaces were exfoliated in atmosphere before rapidly transferring into a vacuum load lock. Substrates are first degassed at $\sim 200^\circ C$ in the load lock overnight before transferring to the growth chamber. The quality of the substrate surface was monitored using in situ reflection high-energy electron diffraction (RHEED). Prior to growth, the substrate is further annealed at 600–950 $^\circ C$ for $\sim 20$ min before cooling to growth temperature, which varied from 300 to 900 $^\circ C$.

For transition metal sources, high-temperature effusion cells containing 4N pure V, 3N5 pure Ti, and an electron-beam evaporator containing 3N5 pure Nb were used. A valved cracker cell was used to generate 5N pure Se flux. The cracker zone of the Se source was maintained at an elevated temperature of 500 $^\circ C$ during growth to generate cracked Se monomers or dimers and to prevent condensation near the valve. During a typical growth, V and Ti fluxes were maintained at $\sim 6 \times 10^{-10}$ mbar beam-equivalent pressure (BEP), which was measured by positioning a retractable beam flux monitoring ion gauge in front of the substrate, just before growth. The Nb flux was measured using a flux monitor built into the e-beam assembly. A Nb flux of 1.5 nA is used for typical growths, unless otherwise specified. For this study, we used a varying Se BEP from $\sim 1 \times 10^{-8}$ to $\sim 3 \times 10^{-7}$ mbar. During growth, the sample surfaces were monitored using the RHEED operated at 15 keV.

Surface morphology analysis was performed after removing the as-grown sample from vacuum, in atmospheric conditions. Since metallic TMDs are very sensitive to atmospheric exposure, every effort was taken to reduce the time taken to transfer the samples from the growth chamber to the atomic force microscope (AFM) facility. For a typical sample, this time varied from 1 to 3 h and no noticeable differences were observed between samples scanned within this timescale, while samples scanned at much later times are visibly degraded. A Bruker Multimode AFM was used to examine the morphology of the epilayers. Samples were scanned in tapping mode using a Si tip. The step height obtained using AFM for the monolayers studied here was in the range of $\sim 8 \AA$, which is in very good agreement with the height value of typical TMDs, where a monolayer is composed of three layers of atoms (Supplemental Material, Fig. S1) [32]. Although we have shown only one AFM image in the text corresponding to each growth condition studied, similar results were obtained from different patches of the same sample as well as from at least one more different growth performed under nominally identical growth conditions (see, e.g., Supplemental Material, Fig. S2) [32].

III. RESULTS AND DISCUSSION

Our approach is summarized in Fig. 1. We employ HOPG as a substrate throughout, which was cleaved immediately prior to loading into the growth system for each growth (see experimental section). This gives rise to a somewhat spotty (1 \times 1) RHEED pattern [Fig. 1(c)], which is typical of a freshly cleaved HOPG surface. AFM measurements [Fig. 1(e)] indicate a smooth surface, with only occasional cleavage steps, over typical AFM scan dimensions of $<10 \mu m \times 10 \mu m$. Over larger areas, cleaved HOPG surfaces exhibit an additional structure resulting from repeated exfoliation processes. Epitaxial TMD monolayers were grown on the cleaved substrate surface by coevaporation of the transition-metal and chalcogen. The sticking coefficient of Se at the growth temperatures used (300–900 $^\circ C$) is very low compared to the metal species due to the huge differences in vapor pressures and the chemical environment. This necessitates a very high Se to metal flux ratio, which is also crucial in preventing the formation of 3D metal clusters via metal-metal bonding. A recent kinetic Monte Carlo simulation of the growth of WSe$_2$ has estimated the mean dwelling time of a Se adatom on the surface before desorption to be over four orders of magnitude.
FIG. 2. Influence of adatom mobility on surface morphology. $1 \times 1 \mu m^2$ AFM images showing surface morphology of three different materials, (a) TiSe$_2$, (b) VSe$_2$, and (c) NbSe$_2$ as a function of growth temperature. Both the metal and chalcogen adatom mobility increases from left to right, with an increasing growth temperature. Similarly, at a given growth temperature, the metal adatom mobility increases from bottom to top with increasing vapor pressure of the transition metal.

less than that of the metal adatoms [33]. Similarly, the mean diffusion distance of Se as compared to the metal adatoms was two orders of magnitude shorter. During the growths performed for this work, we have therefore maintained a metal:Se flux ratio of at least 1:60, although for most parts of the study, a ratio as high as 1:500 was used.

As the growth progresses, the RHEED pattern of the HOPG substrate begins to slowly fade, while a new pattern starts to appear which we attribute to the TMD epilayer. Toward the end of the growth, the new features become strong and streaky [Fig. 1(d)], confirming a flat morphology of the monolayer surface. From the spacing of the TMD RHEED streaks, we can extract a lattice constant for the TiSe$_2$ monolayer shown in Fig. 1(d) of $3.52 \pm 0.05$ Å. This is in excellent agreement with the in-plane bulk lattice constant of TiSe$_2$, despite the nearly 30% lattice mismatch with the HOPG substrate. Equivalent results were obtained for VSe$_2$ and NbSe$_2$, confirming that the TMD monolayers are grown without strain and misfit dislocations, facilitated by a relaxed substrate-epilayer interaction at the interface via van der Waals epitaxy. Large-area AFM imaging [Fig. 1(f)] indicates that growth yields a number of islands distributed across the sample surface. Around defects on the substrate (such as grain boundaries between neighboring lateral domains with random in-plane rotational alignment, which are known to form in HOPG), there are a large number of nucleation sites and inhomogeneous growth is observed. Away from such substrate grain boundaries, there are a lower density of larger islands. In the following, we focus on the growth dynamics which dictate the morphology, size, and structure of these isolated islands, and elucidate the key parameters that can be tuned to optimize these.

Figure 2 shows AFM images of monolayer NbSe$_2$, VSe$_2$, and TiSe$_2$ grown on HOPG at growth temperatures of between $300 \degree C$ and $600 \degree C$ (throughout, we report the growth temperature as the temperature measured by a thermocouple positioned behind the sample plate). With an increasing growth temperature, the sticking coefficient decreases which results in a lower growth rate as evident from the smaller coverage of the epilayer (particularly clear for VSe$_2$). More importantly, changing both growth temperature and the transition metal atom leads to pronounced changes in the morphology of the as-grown monolayer islands.

For NbSe$_2$, growth at the lowest temperature studied here leads to randomly branched growth with very small feature sizes. We refer to this morphology as dendritic. With increasing growth temperature, a somewhat more symmetrical, but still branched, morphology of the growing islands is observed, while at the highest growth temperature ($T_g$) of $600 \degree C$, small triangular islands are formed, with a side length of ca. 50 nm. We note that at around $600 \degree C$ growth temperature, NbSe$_2$ was previously reported to undergo a phase transition from the 1H
(at low growth temperature) to the 1T (at higher growth temperature) polymorph, as judged from changes in the electronic structure measured using angle-resolved photoemission [34]. Our own photoemission measurements (Supplemental Material, Fig. S3) [32] indicate that for growths at 500 °C and below, our samples are purely in the 1H phase, while at a growth temperature of 600 °C, we still have a predominantly 1H phase, but with a partial admixture of regions of 1T phase. No clear morphological differences are evident in different regions of the AFM scans shown in the bottom right panel of Fig. 2, suggesting that the polytype does not have a major impact on the island morphology here, although this remains an interesting topic for future detailed exploration.

VSe$_2$ and TiSe$_2$ are both expected to be stable in the 1T polymorph for all growth temperatures studied here. For both of these compounds, randomly branched growth is not observed at the lowest temperatures studied, in contrast to NbSe$_2$. Rather, at a growth temperature of 300 °C, a symmetrically branched growth mode is obtained. As is particularly clear for VSe$_2$, the growing islands have treelike morphologies, with additional branching evident on the side of a growing spur, reminiscent of self-similarity. We thus attribute the symmetrically branched structures as arising from a fractal growth mode. With increasing temperature, a trend toward a triangular growth mode is again observed. For a given growth temperature, the largest island sizes are observed for TiSe$_2$, with the smallest for NbSe$_2$ [35]. The transition from branched to a triangular growth mode also occurs at lower growth temperatures for TiSe$_2$ vs NbSe$_2$.

The formation and evolution of these structures can be understood on the basis of varying adatom surface diffusion lengths. At a given growth temperature, the transition-metal mobility is the lowest for Nb atoms, while the Ti atoms are the most mobile. Moreover, higher growth temperatures lead to an increase in thermally promoted adatom surface diffusion, yielding longer surface diffusion lengths of both the metal and chalcogen species. The dendritic and fractal growth modes observed here can thus be understood due to the kinetic limitations of the adatoms at very low temperatures within a simple model of diffusion-limited aggregation [36]. An adatom randomly diffuses on the substrate surface until it comes in contact with an already formed cluster or a nucleation site and sticks at the first point of contact. Once condensed at the edge of an island, edge diffusion is restricted or negligible at lower temperatures and this results in the formation of dendrites [37]. The dendritic growth observed for NbSe$_2$ at $T_g = 300$ °C can thus be attributed to the extremely low mobility of Nb adatoms at lower temperatures.

With increasing growth temperature, thermal excitation of the adatoms enables a moderate edge mobility. Randomly attached adatoms become more mobile and diffuse preferentially toward higher-symmetry bonding sites, enabling the steady coalescence of nucleating islands into morphologically more compact fratacals. The mobility and directionality at this stage is still limited, however, and so the transition between the two growth morphologies is subtle. A key diagnostic is the increased symmetry of the fractal mode as compared to the dendritic one, similar to the morphological changes observed in the initial stages of growth of elemental metals on surfaces [38]. The transition is evident here with increasing growth temperature above 300 °C for NbSe$_2$. Dendrites are not, however, formed during VSe$_2$ or TiSe$_2$ growths even at $T_g = 300$ °C, due to the relatively higher surface diffusion lengths of V and Ti adatoms as compared to Nb ones at that temperature.

The growth of compact triangular domains at higher temperatures differs from diffusion-limited aggregation. For the more compact growth, adatoms diffuse to an existing cluster, and then relax to a lower energy site through edge diffusion. As the rate of relaxation increases with respect to the rate of adatom diffusion to the cluster, a stochiometric transition occurs from fractal growth to the more thermodynamically favorable triangular island growth mode. As the growth progresses, various islands begin to develop from different nucleation sites and they compete for the available adatoms. This naturally explains the steady transition from fractal to triangular domain growth mode evident for all three materials at intermediate/high growth temperatures discussed above.

It is also evident, however, that there is a large difference in island size and density between the different compounds. This can again be understood from the varying adatom mobility of the different transition metals at a given growth temperature: In the absence of nucleation sites, an impinging atom diffuse until (within the surface dwell time) it comes in contact with another diffusing adatom which results in the formation of a seed. The mobility and stability of these seeds depend on the growth temperature. As the growth progresses, the number of seeds increases linearly until the the density is comparable to normal adatoms. At this point, island growth competes with any seed formation. At higher growth temperatures, the surface diffusion lengths of adatoms become larger than the mean island separation distances, which results in the adatoms diffusing into existing islands [39]. The significantly higher nucleation density present in NbSe$_2$ as compared to both VSe$_2$ and TiSe$_2$ can thus also be attributed to a lower thermally activated diffusion hopping rate of Nb vs V or Ti adatoms at comparable temperatures.

We note that postgrowth annealing at an elevated temperature is sometimes used for improving the quality of MBE grown epilayers. This would indeed be expected to promote additional edge diffusion, leading to higher quality monolayers. However, upon comparing the morphology of a limited number of TiSe$_2$ samples, we also observed the onset of monolayer to bilayer conversion upon annealing (Supplemental Material Fig. S4) [32]. While postgrowth annealing can provide a valuable additional route to optimize TMD monolayer growth, care must therefore be taken to avoid monolayer to bilayer conversion, as well as the introduction of Se vacancies when using higher growth (and therefore annealing) temperatures such as those studied here.

The above results demonstrate the major impact that variations in the adatom surface diffusion length, governed by changing growth temperature and transition-metal atom, have on the morphology of TMD monolayers grown by MBE. Nonetheless, other parameters can also influence the fractal to triangular domain transitions observed above. In the following, we focus on TiSe$_2$ and NbSe$_2$ as these show the extremes of behavior of transition-metal surface diffusion. Figure 3 shows the morphology of TiSe$_2$ and NbSe$_2$ monolayers grown at temperatures between 300 °C and 500 °C under two
FIG. 3. Effect of Se flux. 1 × 1 μm² AFM images showing the influence of increasing Se flux and growth temperature on the island morphology of (a) TiSe₂ and (b) NbSe₂ monolayers.

different Se fluxes, corresponding to a Se BEP of \(~2 \times 10^{-8}\) mbar and \(~2 \times 10^{-7}\) mbar, respectively. The AFM scans from the growth in the more Se-rich conditions is reproduced from Fig. 2 to aid comparison.

While qualitatively the same transitions from dendritic to fractal to triangular growth modes are still evident, this evolution is slowed down when growing using the lower Se flux. A noticeable change for the high Se, high temperature growth is the increased domain sizes as compared to growth in a lower Se flux. Considering the constant metal fluxes used here, it is evident that the excess Se impinging on the surface takes part in bonding with the metal adatoms and by means of edge diffusion forms the energetically favorable triangular domains. The increased surface diffusion lengths at higher temperature enables the formations of larger islands. It is also evident that in the absence of any excess Se, the extra metal adatoms otherwise available for bonding do not form any metallic clusters, possibly due to a combination of lower sticking coefficients and higher adatom mobilities. We also note that even at the lowest temperature we have used, the Se sticking coefficient has a huge dependence on the metal fluxes and hence Se atoms do not take part in the growth in the absence of the metal adatoms.

We stress that even at the lower Se BEP of \(~2 \times 10^{-8}\) mbar used here, this still corresponds to a very Se-rich growth condition with a high metal:Se ratio of \(~1:60\). This is higher than typically utilized for epitaxial growth of TMDs by MBE. One reason that this is required is the broad growth temperature range we have investigated here (300–900°C).

At higher growth temperatures, the Se sticking coefficient becomes extremely low, which results in a very low growth rate and high desorption of Se, creating unwanted vacancies. Given the extremely volatile nature of Se, however, we find that increasing the Se flux still has a notable effect on the growth morphologies even for the more typical lower growth temperatures. Our results therefore suggest that higher transition metal:Se fluxes than typically employed should be considered even for lower temperature growths.

Given the pronounced influence of adatom mobility on the morphology of the synthesized epilayers outlined above, it is of interest to also investigate the influence of growth rate. In the following, we thus fix the growth temperature to 500°C and the Se BEP to \(~2 \times 10^{-7}\) mbar, and vary the impinging transition-metal flux. Figure 4(a) shows 1 × 1 μm² AFM images of TiSe₂ samples for which the Ti effusion cell temperature was varied from 1330°C to 1350°C. We note that since the transition metal flux is very low (BEP \(~6 \times 10^{-10}\) mbar), the change in Ti flux is modest for this change in cell temperature, and the error in measuring the BEP is high at these low values, we report simply the cell temperature used here. To compensate the changes in surface coverage due to a varying metal flux, growth times were adjusted accordingly (from 55 min for the sample grown with 1350°C cell temperature to 90 min for the sample growth with 1330°C cell temperature) to maintain approximately equivalent coverage for the different growth rates used.

Two key features are evident in the case of TiSe₂ [Fig. 4(a)]. First, the triangular domains seen on all three AFM images consist of a larger monolayer island with side length varying from \(~0.9 \sim 1.2\) μm and a smaller bilayer island on
by the formation of three fractal islands separated by 120° 

growth-rate dependent studies here suggest that, at around this temperature, the growth of a monolayer is initiated by the formation of three fractal islands separated by 120° rotation. These fractal islands originate from the same nucleation site and, as the growth progresses, slowly evolve and merge to form a large triangular island. As seen from Fig. 4(a), this transformation is highly growth-rate dependent: At faster growth rates, there is not enough time for the adatoms to participate in edge diffusion and the domains remain more fractal, while at slower growth rates the adatoms have a longer time for edge diffusion, thus facilitating the formation of larger triangular grains. Slow growth rates are thus clearly preferable to generating large triangular islands.

These are not isolated monolayers, however, but have a small bilayer region forming at the middle of the island. The bilayer exhibits good epitaxial registry with the underlying monolayer. Interestingly, unlike the monolayer, we find that the bilayer region forms as a near-perfect triangle immediately from the initial stages of growth. This is likely due to the differences in growth kinetics when a layer is grown on a graphite substrate vs a monolayer substrate of the same kind as the growing epilayer, which thus acts a favorable substrate. A reduction in size of the bilayer is evident with increasing growth rate. We speculate that this reflects the fact that, for the faster growth rates, the three 120° rotated fractal legs of the underlying monolayer have lateral dimensions less than the surface diffusion lengths of adatoms. Thus, adatoms which absorb on the monolayer surface can diffuse to the edge of the monolayer, where they can then participate in edge diffusion of the monolayer itself. Less adatoms thus contribute to forming a bilayer region. In contrast, for the slower growth rates, the monolayer becomes more triangular and its center becomes further away from any nucleation edges, which in turn ultimately favors nucleation of a second layer atop the monolayer. This suggests that the formation of bilayer patches can be reduced by again increasing the surface diffusion length of the adsorbed adatoms, such that they reach the edge of the growing monolayer island within their surface diffusion time, and thus participate in edge diffusion, resulting in the formation of larger monolayers without bilayer growth. Consistent with this, we note that for TiSe$_2$ growth at a temperature of 600°C (Fig. 2), for which the adatom mobility is consequently increased as compared to the growths shown in Fig. 4, no bilayer formation is observed. In fact, these monolayer islands, with edge length of ca. 600 nm, are—to our knowledge—the largest pure monolayers (i.e., without partial bi- or multilayer coverage) of any TMDs achieved to date via MBE growth.

Figure 4(b) shows equivalent growth-rate dependent measurements for NbSe$_2$. Here, a larger change in flux from 0.5 to 2.5 nA (as measured by a flux monitor integrated into the electron-beam evaporator used for the evaporation of Nb) was used, with the corresponding growth times changed from 540 to 35 min, respectively, to maintain approximately equivalent surface coverage. As evident in Fig. 4(b), such changes in the NbSe$_2$ growth rate have a significant influence on both the onset of nucleation and the sizes of islands. At faster growth rates, there is an increased number of nucleation sites and resulting islands. However, when the growth is slowed down, the nucleation site density decreases as the adatoms have more time to migrate over longer distances, increasing their probability of a subsequent encounter with an existing island. This enhancement in the surface migration length also gives rise to larger monolayer islands. As for TiSe$_2$, there is evidence of some fractal to triangular domain transformation occurring at the lowest growth rates. Nonetheless, there are no clear triangular domains formed for NbSe$_2$ here, as the 500°C growth temperature used is still below the temperature where this transition occurs (Fig. 2), due to the significantly lower adatom surface diffusion lengths of Nb atoms as compared to Ti. It is clear, however, from the measurements shown in Fig. 4 that the transition from a fractal to triangular growth mode is not simply a function of the surface adatom mobilities, but can also be strongly modified by the growth rate used, as well as the ratio of metal:chalcogen flux, as shown in Fig. 3.

From the above, it is thus clear that enhancing adatom mobility and utilizing slow growth rates are key to obtaining more compact and thermodynamically favorable morphological configurations of the epitaxial TMD islands, and for realizing true monolayer growth without additional bilayer patches. To explore this further, and to investigate whether other close-packed configurations may be obtained, we have synthesized TiSe$_2$ monolayers using even higher growth temperatures. Figure 5 shows AFM images of the resulting TiSe$_2$ monolayers grown at 600, 750, 800, 850, and 900°C. We find
that the triangular domains discussed above slowly transform into hexagons, via a gradual truncation of the tips of the original triangular domain with increasing growth temperature. The process starts when increasingly energetic atoms attached to the three corners of a triangle undergo edge diffusion at elevated temperatures. In CVD synthesis of WSe$_2$, a transition from islands of triangular morphology to hexagonal islands was previously observed to be associated with a cross-over from monolayer to multi-layer structures [40]. A transition to hexagonal monolayer patches was also reported during the CVD growth of MoS$_2$, where the change in morphology was attributed to the changes in the Mo:S ratio of the precursors [41]. In contrast, the triangular to hexagonal transition observed in our work can be attributed simply to the increasing adatom mobilities with temperature, and thus reflects the intrinsic stability of the hexagonal morphology of the as-grown layer given high adatom diffusion lengths.

IV. CONCLUSIONS

We summarize our key findings in the schematic phase diagram shown in Fig. 6. For low adatom mobilities, an undesirable dendritic growth mode is found. Within the parameter range investigated here, this was only observed for NbSe$_2$, pointing to the additional challenges for TMD growth associated with the low diffusion lengths of the heavier transition metals, which have lower vapor pressures as compared to the lighter transition metals. Nonetheless, morphological control for such systems is still possible. With reducing growth rate or increasing surface diffusion lengths promoted via increased growth temperature, or higher intrinsic adatom mobility of different transition metals, the dendritic growth mode transforms into a fractal mode, with treelike branching morphologies. Within the fractal growth region, there is a clear dependence of the size of the monolayer islands on both growth rate and adatom mobility; smaller fractals are obtained when materials with smaller adatom mobilities are grown at lower temperatures under faster growth rates. The fractals get larger with an increasing adatom mobility and with reducing growth rate.

Upon further increasing the adatom diffusion lengths and lowering the growth rate, a more thermodynamically favorable compact triangular domain growth regime can be achieved. The growth conditions in this region further promotes the transformation of neighboring fractal domains into single triangular islands. Finally, a regime where the growth of the most stable and thermodynamically favourable hexagonal domains is be obtained can be found for the highest adatom mobilities. A clear and steady transition region is observed between the triangular and hexagonal growth regimes.

Ultimately, our study therefore indicates that, to achieve large monolayer triangular or hexagonal domains, growth should proceed at high substrate temperature to promote surface adatom mobility, and at low growth rate to increase time available for surface diffusion. The high growth temperatures in turn necessitate the use of very high Se overpressures to compensate surface desorption due to the extremely high vapor pressure of this element. The required growth conditions will vary for a given transition-metal atom used: for NbSe$_2$, growth at an extremely slow rate of ca. 0.05 ML/h was required to obtain domain sizes of ca. 150 nm for a ~0.5 ML coverage, while for TiSe$_2$, island sizes of over 1 $\mu$m$^2$ could be achieved for a similar surface coverage at a much faster growth rate of ca. 0.5 ML/h. For TiSe$_2$, via use of the optimized growth conditions as determined here, we were able to achieve the largest monolayer islands of a TMD grown by MBE to date.

While we studied three specific TMDs here, our conclusions should be generally applicable to the growth of other TMDs using this method. Our study thus paves the way to the synthesis of improved-quality epilayers in challenging systems such as 4$d$ and 5$d$ systems, which are of interest, for example, for their optoelectronic properties, strong spin-orbit interactions, and possibilities to stabilize exotic quantum states [1,3,42]. Moreover, by further extending the parameter range studied here, our results suggest the route to even larger island sizes of the lighter 3$d$ systems, which may consequently be able to approach the grain sizes achieved in other monolayer preparation methods such as mechanical exfoliation.

The research data underpinning this publication can be accessed through the University of St. Andrews Research Portal [43].

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