DECOMPOSING DUSTY GALAXIES. I. MULTICOMPONENT SPECTRAL ENERGY DISTRIBUTION FITTING

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ABSTRACT

We present a new multicomponent SED decomposition method and use it to analyze the UV to millimeter wavelength SEDs of a sample of dusty infrared-luminous galaxies. Each SED is decomposed into emission from populations of stars, an AGN accretion disk, PAHs, atomic and molecular lines, and distributions of graphite and silicate grains. Decompositions of the SEDs of template starburst galaxies and AGNs provide baseline properties to aid in quantifying the strength of star formation and accretion in the composite systems NGC 6240 and Mrk 1014. We find that obscured radiation from stars is capable of powering the total dust emission from NGC 6240. The presence of a small quantity of 1260 K dust in this source suggests a ~2% AGN contribution, although we cannot rule out a larger contribution from a deeply embedded AGN visible only in X-rays. The decomposition of Mrk 1014 is consistent with ~65% of its power emerging from an AGN and ~35% from star formation. We suggest that many of the variations in our template starburst SEDs may be explained in terms of the different mean optical depths through the clouds of dust surrounding the young stars within each galaxy. Prompted by the divergent far-IR properties of our template AGNs, we suggest that variations in the relative orientation of their AGN accretion disks with respect to the disks of the galaxies hosting them may result in different amounts of AGN-heated cold dust emission emerging from their host galaxies. We estimate that 30%–50% of the far-IR and PAH emission from Mrk 1014 may originate from such AGN-heated material in its host galaxy disk.

Subject headings: galaxies: Seyfert — galaxies: starburst — infrared: galaxies — methods: numerical

1. INTRODUCTION

Optical and near-IR imaging has revealed that most luminous and ultraluminous infrared galaxies (LIRGs and ULIRGs; see Sanders & Mirabel 1996), as well as many lower luminosity dusty galaxies (e.g., starbursts and active galactic nuclei [AGNs]), are interacting systems that have recently merged or are in the process of merging (Armus et al. 1987; Sanders et al. 1988; Murphy et al. 1996). Large quantities of gas and dust driven into the nascent nuclei of these systems catalyze massive bursts of star formation and/or fuel accretion onto supermassive black holes (Mihos & Hernquist 1996; Struck 1999). Ultraviolet and optical emission from many of these dusty galaxies is significantly obscured by the same gas and dust providing their infrared power, a fact that greatly diminishes the background and star formation energy density at higher redshifts.

Great progress toward this goal was made using data from the Infrared Space Observatory (ISO). Diagnostic diagrams based on high-ionization mid-IR lines (e.g., [O iv] and [Ne v]), the slope of the mid-IR continuum, and the strengths of the 6.2 and 7.7 μm polycyclic aromatic hydrocarbon (PAH) emission features were constructed to quantify the relative contributions from accretion and star formation activity in many sources (e.g., Genzel et al. 1998; Lutz et al. 1998; Laurent et al. 2000; Tran et al. 2001). These observations provided evidence that ULIRGs are powered primarily by star formation, with the fraction of AGN activity increasing with bolometric luminosity. However, due to the limited wavelength coverage and sensitivity of the ISO spectrometers, this analysis was limited to a relatively small number of bright nearby sources. These observational challenges have largely been abated with the improved wavelength baseline and sensitivity of the Infrared Spectrograph8 (IRS; Houck et al. 2004) on the Spitzer Space Telescope (Werner et al. 2004). Large samples of starburst galaxies (Brandl et al. 2006), AGNs (Hao et al. 2005b; Weedman et al. 2005; Schweitzer et al. 2006), local ULIRGs (Armus et al. 2007), and their high-redshift counterparts (e.g., Houck et al. 2005; Yan et al. 2005; Lutz et al. 2005) have been observed with the IRS. As with the previous generation of studies with ISO, diagnostic diagrams have been constructed using the properties of high-ionization lines (with much improved sensitivity to place strict limits on [Ne v] emission), mid-IR spectral slopes (with a much broader mid-IR wavelength baseline), and PAH feature emission (now detected to z > 2).

In addition to these observational diagnostics, many tools have been developed to model the spectral energy distributions (SEDs) of emission from dusty galaxies. Models containing a variety of grain sizes and chemical compositions have been used to calculate the dust temperatures, optical depths, and emissivities. These models have been calibrated using ultraviolet to far-infrared observations (now detected to z > 2).

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the spectrum of emission from astronomical dust embedded in single (e.g., Desert et al. 1990; Li & Draine 2001; Draine et al. 2007) and multiple (e.g., Dale et al. 2001; Li & Draine 2002) incident radiation fields. In addition, numerous radiative transfer models have been published, including several to calculate the emission from an AGN and its obscuring torus (e.g., Nenkova et al. 2002; Dullemond & van Bemmel 2005). Finally, methods intended to decompose the SEDs of galaxies into a number of components have also been developed. For example, Klaas et al. (2001) present such a method and use it to decompose the far-IR SEDs of a sample of ULIRGs into contributions from several dust-modified blackbodies at different characteristic temperatures.

We present in this work a new method used to decompose the SEDs of galaxies into emission from populations of stars, an AGN accretion disk, PAH molecules, atomic and molecular lines, and distributions of thermally heated graphite and silicate grains at different fitted characteristic temperatures. Given the many observational and theoretical techniques to study dusty galactic nuclei described above, it is fair to question our decision to introduce yet another. We are motivated to do so for two principal reasons. First, while the radiative transfer methods incorporating realistic dust models described above provide the most physically complete method of calculating the SEDs of dusty galaxies, these methods are also the most dependent on the assumed geometry of the source. Unfortunately, detailed spatial information to constrain these assumptions is available for only a handful of nearby galaxies, so the parameter space in which to search for best-fitting models in agreement with observations is both sizable and degenerate. Second, the methods for calculating the emission from dusty galaxies described above are primarily intended to model starburst galaxies or AGNs. None of them, however, are particularly well suited to calculating the emission from sources containing a starburst and an AGN, each of which may be distinguished by different levels of obscuration (see § 5.4 for an expanded discussion).

Our goal for this paper is therefore to convince the reader that our decomposition method is well suited to analyzing the SEDs of composite sources and is motivated by the desire to address the following: (1) What energy source is primarily responsible for powering the emission from dusty galaxies? (2) How homogeneous are the SEDs of dusty galaxies that have similar AGN and starburst fractions? (3) What geometries can explain any homogeneities in the SEDs of similarly powered dusty galaxies? To meet this goal, we apply our decomposition method to a small sample of well-studied galaxies, including the relatively unobscured starburst NGC 7714, the obscured starburst NGC 2623, the quasar PG 0804+761, and the Seyfert 2 Mrk 463. These fits provide templates by which to understand the properties of pure starburst galaxies and AGNs, the constituents of composite sources such as many ULIRGs. In addition, as examples of such composite sources, we present fits to the LIRG NGC 6240 (believed to be powered primarily by star formation) and the ULIRG Mrk 1014 (believed to be powered primarily by accretion).

We begin in § 2 with an overview of the spectral decomposition method. In § 3 we detail the method used to calculate the spectrum of emission from the various source components. In §§ 4 and 5 we describe the adopted dust model and the method used to calculate the thermal emission from dust. In §§ 6 and 7 we describe PAH feature and atomic and molecular line emission, respectively. In § 8 we describe the sample of galaxies analyzed in this work, in § 9 we present their decompositions, and in § 10 we present detailed analysis of the results. The breadth of our conclusions is clearly limited by the size of our sample. In a subsequent paper our method will be applied to a much larger sample of starburst galaxies, AGNs, LIRGs, and ULIRGs obtained as part of the Spitzer GTO program.

2. SPECTRAL DECOMPOSITION METHOD

2.1. Decomposition Components

The principal assumption in our decomposition method is that the ultraviolet to millimeter wavelength (10 Å–1000 μm) SED of a dusty galaxy may be completely described in terms of emission from evolved stars in the disk of the host galaxy (ISRF), populations of young stars in starbursts (SB), an AGN accretion disk (AGN), PAH molecules (PAHs), atomic and molecular lines, and several distributions of thermally heated graphite and silicate grains (hot, warm, cool, and cold). In this paper the ISRF, SB, and AGN components are collectively referred to as “source” emission components since they represent the primary illuminating sources heating dust within a galaxy. The hot, warm, cool, and cold components are collectively referred to as “dust” emission components. Assuming that these components form a complete basis describing the emission from dusty galaxies, the observed flux density may be expressed as

\[
f'_\nu = \frac{L_{\text{source}}}{4\pi D_e^2} \sum_{\text{source}} \bar{\alpha}_{\nu} f'_{\nu}^{\text{source}} + \frac{L_{\text{dust}}}{4\pi D_e^2} \sum_{\text{dust}} \bar{\alpha}_{\nu} f'_{\nu}^{\text{dust}} + f'_{\nu}^{\text{PAHs}} + f'_{\nu}^{\text{lines}},
\]

where \(L_{\text{source}}\) and \(L_{\text{dust}}\) are the total apparent luminosities of the source and dust components derived from the fit, respectively, \(D_e\) is the luminosity distance to the galaxy, \(\bar{\alpha}_\nu \equiv L_\nu/L_{\text{source}}\) and \(\bar{\alpha}_\nu \equiv L_\nu/L_{\text{dust}}\) are the fitted contributions to the total source and dust luminosities from each component, respectively, the \(f'_{\nu}^{\text{PAHs}}\) and \(f'_{\nu}^{\text{lines}}\) are the fitted PAH and emission-line flux densities, respectively. We include a maximum of four dust components that are typically heated to characteristic temperatures of \(T_{\text{hot}} \approx 1400\) K, \(T_{\text{warm}} \approx 200\) K, \(T_{\text{cool}} \approx 80\) K, and \(T_{\text{cold}} \approx 35\) K. The actual temperature of each dust component is determined from the fitted magnitude of its illuminating radiation field energy density.

Figure 1 presents an illustration of one possible geometric structure of a dusty galaxy within which to interpret the roles played by each decomposition component in equation (1). Figure 1a depicts the optically thin (at mid-IR wavelengths) disk of the host galaxy from which evolved photospheric (ISRF) and cold dust emission emerges. Figure 1b shows an enlarged view of the central region of the galaxy consisting of an AGN and a starburst surrounded by screens of cool and cold dust. Figure 1c depicts the composite nucleus of the dusty galaxy, while the details of each nuclear component are shown in Figure 1d. The starburst is composed of SB emission from young stars, warm dust in the shells surrounding the young stars, and possibly cool and/or cold dust in spherical screens around each individual star-forming cloud. The AGN consists of emission from the AGN accretion disk, hot and warm dust on the illuminated and shaded sides of the dust clouds creating the obscuring torus (or dust in illuminated and shielded regions of a “classic” torus with a smooth dust distribution; see Fig. 6 below), and warm and cool dust in narrow-line region

9 See http://www.its.caltech.edu/~jam258/cafe.html for more information about the method and the Continuum And Feature Extraction (CAFE) software.
10 All names of decomposition components are printed in italic type throughout this work.
11 Note that \(f'_{\nu}\) units may be substituted for \(f_{\nu}\) units throughout this work and that variables accented with tildes are free parameters in the fitting.
clouds (again from dust in illuminated and shaded regions). We emphasize that our method does not require the definition of any specific geometry (i.e., we derive the contributions from each emission component without the need to define its proximity to any other component), and the actual geometry of a dusty galaxy may look quite different from the one presented. The illustration in Figure 1 should therefore not be taken as a literal description of the geometry of a particular galaxy (since our method requires none), but instead it is intended to provide a structure within which to visualize the multiple roles potentially played by each decomposition component.

We note that star formation in the disk of the host galaxy and that in starburst regions are both explicitly accounted for via the ISRF and SB components. Furthermore, while Figure 1 depicts the specific case of a nuclear starburst, the actual location of the star formation (e.g., nuclear vs. off-center) has no effect on the decomposition (assuming that any off-center emission is contained within the spectroscopic slits and photometric apertures used to construct the SEDs). For example, in the decomposition of an off-center starburst, the cool and cold decomposition components (or portions thereof) could be interpreted as belonging to off-center obscuring clouds. Note, however, that if a galaxy contains both a highly enshrouded nuclear starburst and a less enshrouded off-center starburst, our decomposition method cannot explicitly fit both components simultaneously. Instead, a mean optical depth somewhere between the optical depths of the two individual components is obtained. Thus, care must be taken when interpreting the optical depths inferred from a globally integrated SED (this admonishment is not unique to our analysis but is a general statement about the nature of spatially integrated data).

2.2. Decomposition Algorithm

Once assembled, the ultraviolet to millimeter wavelength SEDs of the galaxies in our sample are fitted to the model of the total flux density from equation (1). The best-fit parameters are determined using a Levenberg-Marquardt least-squares routine to minimize

\[ \chi^2 = \sum_k w_k \left( f_{\nu}^{\text{data}}(\lambda_k) - f_{\nu}^{\text{total}}(\lambda_k) \right)^2, \]

where the \( w_k \) are the weights applied at each wavelength \( \lambda_k \) (see §2.3), \( f_{\nu}^{\text{data}} \) is the observed flux density, and \( f_{\nu}^{\text{total}} \) is the modeled flux density from equation (1). For photometric data, we integrate the modeled flux density over the filter transmission curve (if available) to properly calculate the broadband flux density. This is important for photometric bands containing emission and absorption features (e.g., J-band photometry containing the 3.3 \( \mu \)m PAH, 3.1 \( \mu \)m water ice, and 3.4 \( \mu \)m HAC features; see §§ 4.8 and 6), as well as those bands covering spectral regions that change rapidly with wavelength (e.g., J-band photometry sampling extinguished photospheric emission; see the near-IR fit to NGC 6240 in § 9.1).

Experience has taught us that the greater the number of free parameters in a fitting model, the less likely the resulting “best fit” will converge to the desired global minimum in the \( \chi^2 \) function. Correspondingly, it becomes increasingly likely that the fit will converge to a local minimum, often with very unsatisfactory results. This is a practical matter and not a mathematical one since a fit with any number of parameters will reach the global minimum given sufficiently well chosen initial conditions. In practice, however, it is desirable to have a more robust fitting method such that any reasonably chosen initial conditions will converge to the global minimum. To meet this goal, we have developed an algorithm that separates the processes of fitting the continuum, defined as the sum of the source and dust components, and the individual PAH features and atomic and molecular emission lines. Such a division into two separate least-squares processes greatly reduces the total number of free parameters in each fit. Parameter errors are calculated after the first step of the fitting procedure and propagated through to the following fit (see § 2.3), so that the net accumulated uncertainty is reliably calculated.

After an SED has been fitted, we perform a series of tests to ensure that all components are well constrained (i.e., that the parameter errors are smaller than their values). First, if the ISRF luminosity is <1% the sum of the luminosities of all source components, then the fit is repeated without the ISRF component. Similarly, if any of the observed dust component luminosities are <1% the sum of the apparent luminosities of all dust components, the fit is repeated without those components. All three source components and the hot dust component emit strongly at ultraviolet to near-IR wavelengths. For some galaxies these overlapping emission components are degenerate and result in unconstrained parameters. Our second check is therefore to test if either the SB or AGN components are unconstrained (i.e., if their luminosity uncertainties exceed their luminosities). If the SB component is unconstrained, we fix the SB-to-PAH luminosity ratio (i.e., the ratio of the unextinguished SB luminosity to the...
PAHs luminosity; see § 9.2) to the value derived from fits to the template starbursts NGC 7714 and NGC 2623 and restart the fit. Similarly, if the AGN component is unconstrained, we fix the AGN—
to—hot dust luminosity ratio (i.e., the ratio of the unextinguished AGN luminosity to the unextinguished hot dust luminosity; see § 9.2) to the value derived from fits to the template AGNs PG 0804+761 and Mrk 463 and restart the fit. As our final test, if any of the fitted optical depths are unconstrained, we fix the most unconstrained to zero and restart the fit. This sequence provides a well-defined method by which to sequentially impose constraints until a successful fit is obtained.

The steps in the fitting method are therefore as follows: (1) input the observed SED and the initial estimates of the PAHs and lines components (see §§ 6 and 7); (2) subtract the initial PAHs and lines components from the observed SED to create an observed continuum emission spectrum; (3) fit this spectrum to obtain the model continuum; (4) subtract the model continuum from the observed SED to create an observed PAH feature and line emission spectrum; (5) fit the individual features in this spectrum; (6) perform the sequence of tests to ensure that the fit is well constrained; and (7) if necessary, repeat the fitting process with the constrained components.

2.3. Data Weighting

The success or failure of a fitting algorithm and the reliability of the results are largely dependent on the chosen method of weighting the data in equation (2). We adopt the function

$$w_k = \frac{\hat{\lambda}_k}{\sigma^2(\hat{\lambda}_k)},$$

where $\sigma(\hat{\lambda}_k)$ is the total 1σ uncertainty in the flux density at wavelength $\lambda_k$ and $\hat{\lambda}_k$ is a term that compensates for nonuniform wavelength sampling (i.e., ensuring that a region of the SED does not dominate the fit simply because it is sampled more finely; see Appendix A). The total uncertainty in any observed data is given by the quadratic sum of the statistical and calibration (i.e., systematic) uncertainties. For IRS spectroscopic data, we use the difference of two spectra obtained at different nod positions (as produced during a typical IRS observation) to calculate the statistical uncertainties (see Appendix B for details). Carefully extracted low-resolution IRS spectra may still exhibit some residual calibration uncertainties (e.g., fringes in the long-low modules), which we estimate to be ~2% of the flux density at any given wavelength. For photometric data, the total uncertainty is taken to be equal to the quadratic sum of the uncertainties provided in the literature and an absolute calibration uncertainty (e.g., from scaling to the IRS apertures) taken to be 5%. The actual systematic uncertainties in the photometric data are difficult to estimate, although we note that the adopted uncertainties yield reasonable reduced $\chi^2$ values and so are likely good estimates.

As described in § 2.2, each decomposition consists of two separate least-squares fits. In the first (step 3 above), the flux density to fit is obtained by subtracting the PAHs and lines components from the observed SED, i.e., $f_\nu = f_\nu^{\text{data}} - f_\nu^{\text{PAHs}} - f_\nu^{\text{lines}}$. When a component is subtracted from observed data to create an SED to be fitted, the uncertainty of the subtracted component must be propagated through the analysis. Thus, the total uncertainty input into the least-squares routine for this first fit is $\sigma^2 = \sigma^2_{\text{data}} + \sigma^2_{\text{PAHs}} + \sigma^2_{\text{lines}}$. Here $\sigma_{\text{data}}$ is the uncertainty in the observed flux density, while $\sigma_{\text{PAHs}}$ and $\sigma_{\text{lines}}$ are the uncertainties in the estimated PAHs and lines components, respectively. Since the estimated strengths of the PAHs and lines components are derived from the observed spectrum, $\sigma_{\text{PAHs}}$ and $\sigma_{\text{lines}}$ are dominated by the IRS uncertainties. We therefore adopt $\sigma_{\text{PAHs}} = \sigma_{\text{lines}} = 0$, since the uncertainties in the IRS data on which they depend are already included through $\sigma_{\text{data}}$. In the second fit (step 5 above), the flux density to fit is obtained by subtracting the fitted continuum from the observed SED, i.e., $f_\nu = f_\nu^{\text{data}} - f_\nu^{\text{cont}}$, so that the total uncertainty input into the least-squares routine is $\sigma^2 = \sigma^2_{\text{data}} + \sigma^2_{\text{cont}}$. Here $\sigma_{\text{cont}}$ is the formal uncertainty in the continuum calculated using the full covariance matrix from the first fit.

3. SOURCE EMISSION

3.1. IRSF Component Emission

We adopt the model of the average interstellar radiation field presented in Mezger et al. (1982) and Li & Draine (2001) to represent the SED of emission from stars in the disk of a galaxy. In this model, the mean energy density in the solar neighborhood, $c u_{\nu} = \frac{f_{\nu} \text{IRSF}}{\text{ISRF}}$, is given by

$$u_{\nu}^{\text{ISRF}} \propto \begin{cases} 0, & \lambda < 912 \, \text{Å}, \\ \lambda^{5.4172}, & 912 \, \text{Å} < \lambda < 1100 \, \text{Å}, \\ \lambda^{2}, & 1100 \, \text{Å} < \lambda < 1340 \, \text{Å}, \\ \lambda^{0.3322}, & 1340 \, \text{Å} < \lambda < 2460 \, \text{Å}, \\ \sum_n W_n B_n(T_n), & \lambda > 2460 \, \text{Å}, \end{cases}$$

where $B_n$ is the Planck function per unit frequency and the $W_n = (0.025, 0.25, 1)$ are weighting factors for each blackbody component of temperature $T_n = (7500 \, \text{K}, 4000 \, \text{K}, 3000 \, \text{K})$. This model spectrum is shown in Figure 2, normalized to have unit integrated energy density. Emission from the IRSF decomposition component is assumed to emerge nearly unobscured from a galaxy disk, so that the line-of-sight extinction to the emitting stars is small in the infrared ($\lambda > 1 \, \text{µm}$). The flux density per unit frequency interval of emission from the IRSF component for use in equation (1) is therefore

$$f_{\nu}^{\text{ISRF}} \propto u_{\nu}^{\text{ISRF}}.$$

An example IRSF component SED, $f_{\nu}^{\text{ISRF}}$, is shown in Figure 3. Displayed alongside the IRSF component is the emission from a 3500 K blackbody (characteristic of evolved stars) scaled to match at 1.5 µm. The two curves are nearly identical at $\lambda > 1 \, \text{µm}$, so that
fitting near-IR data with the ISRF component is very similar to fitting with a 3500 K blackbody.

### 3.2. SB Component Emission

In contrast to the modest ~1 $M_\odot$ yr$^{-1}$ star formation rate characteristic of emission from the ISRF component, the rates in starbursts are often much higher (e.g., $\geq 10$–100 $M_\odot$ yr$^{-1}$), resulting in significantly different stellar populations. In order to properly characterize the spectral properties and bolometric luminosities of these populations, we use Starburst99 (Leitherer 1990) to generate SEDs of instantaneous bursts at different epochs. We assume a Kroupa initial mass function having an $M_1^{1.3}$ power law in the 0.1–0.5 $M_\odot$ range and an $M_2^{2.3}$ power law in the 0.5–100 $M_\odot$ range. We further assume Padova asymptotic giant branch tracks with solar metallicity. Populations of stars in starbursts evolve dramatically during the first 10 Myr after a burst. At 4 Myr the most massive stars still exist on the main sequence, but by 10 Myr all of the photoionizing stars have evolved into supergiants. As shown in Figure 2, the emission from a starburst 2 Myr after a burst emerges almost exclusively at ultraviolet wavelengths. Since we have very little data in this wavelength range for the sources in our sample, we are unable to explicitly constrain the presence or absence of such a population. In contrast to this, the 10 and 100 Myr populations emit a large fraction of their luminosity at optical and longer wavelengths, where our SEDs are better constrained. Therefore, in order to adequately sample the evolutionary stages in a starburst that we are sensitive to, and to smoothly transition into the evolved population modeled with the ISRF component, we create a composite starburst spectrum containing equal contributions from the 10 and 100 Myr populations, i.e., $u_\nu^{SB} = (u_\nu^{SB10} + u_\nu^{SB100})/2$. We note, however, that the omission of an ultraviolet-luminous young stellar population from $u_\nu^{SB}$ may result in an underprediction of the total SB luminosity for some sources, perhaps by up to ~1 if the 2 Myr population contributes at the same level as each of the older populations.

Unlike emission from the ISRF component, we assume that SB component emission emerges from regions that may be obscured by screens of dust out to infrared wavelengths. If the obscuration to the SB component is dominated by dust in the cocoons of material surrounding each star-forming knot, and not by extinction between the various knots, then the majority of the obscuration occurs via a screened geometry. Levenson et al. (2007) use radiative transfer models to show that such a screened geometry is actually required to reproduce the deep 9.7 μm silicate features observed in many ULIRGs, suggesting that the assumption of a screened geometry is reasonable for highly obscured sources. At lower optical depths (i.e., $\tau < 1$), mixed and screened geometries both give rise to extinctions scaling approximately as $f/f_0 \approx 1 - \tau$, so that the choice between the form of extinction is less critical. We therefore model the flux density per unit frequency interval of emission from the SB component as

$$f_\nu^{SB} \propto u_\nu^{SB} e^{-\tau_{SB}}$$

where the optical depth through the obscuring screen to the SB component is given by

$$\tau_{SB}(\lambda) = \pi^{SB} \frac{\Sigma_{abs}(\lambda)}{\Sigma_{abs}(5500 \text{ Å})}.$$  

Here $\pi^{SB}$ is the screen optical depth to the SB component at 5500 Å and $\Sigma_{abs} = \Sigma_{ext} - \Sigma_{scat}$ is the total dust absorption opacity.

**Fig. 3.— Example SEDs of emission from a starburst (SB) 10 and 100 Myr after an instantaneous burst, evolved disk stars (ISRF), and an AGN accretion disk (AGN).** Also shown are the SEDs of the SB components extinguished by obscuring screens with the indicated optical depths, and the SEDs of the AGN component behind an $\tau_V = 25$ screen for the indicated covering factors (dot-dashed lines). Note that emission from the 2 Myr starburst population declines steeply at $\lambda > 3000$ Å and that the ISRF component is very similar to a 3500 K blackbody for $\lambda > 1$ μm (dotted lines; see text).
obtained by subtracting the scattering opacity from the total extinction opacity (see § 4.7). We use the absorption and not the extinction opacity in equation (7) since scattering tends to cancel itself out in sufficiently spherical geometries, such as depicted in Figure 1 (i.e., light scattered out of the beam along the direct path to the observer is offset by light scattered into the beam along another path). Furthermore, the extinction and absorption opacities of dust in our model have similar slopes between 1000 Å and 3 μm, where the SB component emits strongly. Since the derived optical depth depends only on the opacity slope and not its absolute value, the omission of scattering has very little effect. We note, however, that this omission may introduce some small uncertainties at the point of view of the observer), which has an approximate visual band optical depth equal to \( \tilde{\tau}_F^{AGN} \). Note that the same qualifications regarding the relative importance of scattering and the subsequent uncertainties in the emergent flux density for \( \lambda \lesssim 3 \mu m \) that were made for the SB component apply here as well. Since the clumpy torus is by definition not spherically symmetric, we use the full extinction opacity (including scattering) in equation (10). As described for the SB component, this choice has very little effect on the results since the extinction and absorption opacities have similar slopes from the ultraviolet to the near-IR, where the AGN component emits strongly.

3.3. AGN Component Emission

The spectral properties of radiation emerging from an AGN accretion disk depend sensitively on the assumed geometry of the surrounding obscuring structure, i.e., the putative torus of AGN unification models (Antonucci 1993). Important geometrical factors include the height of the inner edge of the torus, its proximity to the nucleus, the clumpy versus smooth structure of the obscuring medium, and the orientation of the torus with respect to the observer. Radiative transfer calculations incorporating these geometric properties have been used to construct models of the emission from an AGN accretion disk and its obscuring torus (e.g., Pier & Krolik 1992; Laor & Draine 1993; Granato & Danese 1994; Nenkova et al. 2002; Dullemond & van Bemmel 2005). Since our intent in this work is to characterize the general properties of the emergent SEDs of large samples of galaxies, and not to discern the detailed properties of the obscuring torus in individual sources, such modeling is unnecessary for our purposes.

Instead, we adopt an empirical model of the emission from an AGN accretion disk and assume that this SED may be extinguished by a foreground screen of dust. We use the accretion disk model from Schartmann et al. (2005), in which the emergent energy density, shown in Figure 2, is modeled by

\[
u_\nu^{AGN} \propto \begin{cases} 0, & \lambda < 10 \text{ Å}, \\ \lambda^{1.7}, & 10 \text{ Å} < \lambda < 500 \text{ Å}, \\ \lambda^{1.8}, & 500 \text{ Å} < \lambda < 1216 \text{ Å}, \\ \lambda^{0.46}, & 1216 \text{ Å} < \lambda < 10 \mu m, \\ B_{\nu}^{(1000 K)}, & \lambda > 10 \mu m. \end{cases} \]

(8)

The flux density per unit frequency interval of emission from the AGN component, including an obscuring screen with a nonuniform covering factor, is modeled as

\[ f_{\nu}^{AGN} \propto f_{\nu}^{AGN}[(1 - \tilde{\tau}_{\nu}^{AGN}) + \tilde{\tau}_{\nu}^{AGN}e^{-\tau_{AGN}}], \]

where \( 0 \leq \tilde{\tau}_{\nu}^{AGN} \leq 1 \) is the fraction of the accretion disk obscured by a screen of optical depth \( \tau_{AGN} \), with

\[ \tau_{AGN}(\lambda) = \tilde{\tau}_{\nu}^{AGN} \frac{\sum_{\nu}(\lambda)}{\sum_{\nu}(5500 \text{ Å})}. \]

(10)

Here \( \tilde{\tau}_{\nu}^{AGN} \) is the screen optical depth to the AGN component at 5500 Å. An example unobscured AGN component SED, \( f_{\nu}^{AGN} \), is shown in Figure 3. Also shown are the SEDs of AGN component emission obscured by a \( \tilde{\tau}_{\nu}^{AGN} = 25 \) screen, for several values of the screen covering factor \( \tilde{\tau}_{\nu}^{AGN} \). Note that significant ultraviolet and optical emission may still emerge from a highly extinguished accretion disk if the covering factor is less than unity.

In the bottom panel of Figure 1, the AGN accretion disk is depicted as being surrounded by an obscuring structure composed of discrete clouds and/or a smooth dusty component. The covering factor, \( \tilde{\tau}_{\nu}^{AGN} \), may therefore be interpreted as the fraction of the accretion disk covered by this obscuring material (from the point of view of the observer), which has an approximate visual band optical depth equal to \( \tilde{\tau}_{\nu}^{AGN} \). Note that the same qualifications regarding the relative importance of scattering and the subsequent uncertainties in the emergent flux density for \( \lambda \lesssim 3 \mu m \) that were made for the SB component apply here as well. Since the clumpy torus is by definition not spherically symmetric, we use the full extinction opacity (including scattering) in equation (10). As described for the SB component, this choice has very little effect on the results since the extinction and absorption opacities have similar slopes from the ultraviolet to the near-IR, where the AGN component emits strongly.

4. ASTRONOMICAL DUST MODEL

4.1. Grain Properties

We adopt the grain size distribution function from Weingartner & Draine (2001, hereafter WD01) and the optical properties of graphitic carbon and smooth astronomical silicate from Draine & Lee (1984) and Laor & Draine (1993) with modifications from WD01 and Li & Draine (2001). The WD01 distribution function has been modified to include a small grain size exponential cutoff to model the deficit of small grains resulting from sublimation in intense heating conditions (see § 4.2). The modified distribution function for graphite and silicate grains takes the form

\[
\frac{1}{n_{ii}} \frac{dn_i}{da} = \left(\frac{1}{n_{ii}} \frac{dn_i}{da}\right)_{WD01} \left[1 - \exp\left(-\frac{a}{a^*}\right)\right],
\]

(11)

where \( (n_{ii}^{-1}dn_i/da)_{WD01} \) is the WD01 distribution function for grains with radii satisfying \( 3.5 \leq a \leq 1 \mu m \). \( a = a_0 (\tilde{U}) \) is the minimum surviving grain size in a distribution embedded in a radiation field with an energy density of magnitude \( \tilde{U} \) (see § 4.2 and eq. [12]), and \( \beta \) determines the exponential cutoff rate. In the limit of \( \beta \to \infty \), the exponential provides a sharp cutoff at \( a = a_0 \). We choose \( \beta = 3 \), the same value adopted for the large grain size exponential cutoff in WD01. Absorption and extinction efficiencies, \( Q_{abs}^D \) and \( Q_{ext}^D \), have been tabulated for graphite and silicate spheres as described in Laor & Draine (1993) for wavelengths \( 10 \mu m \leq \lambda < 1000 \mu m \). Absorption cross sections are calculated using \( C_{ext}^D(a, \lambda) = \pi a^2 Q_{ext}^D(a, \lambda) \) and \( C_{abs}^D(a, \lambda) = \pi a^2 Q_{abs}^D(a, \lambda) \), with similar expressions for the extinction cross sections \( C_{ext}^D(a, \lambda) \) and \( C_{ext}^D(a, \lambda) \).

4.2. Grain Sublimation

Graphite and silicate grains sublimate when heated to temperatures above 1750 and 1400 K, respectively (Laor & Draine 1993). The minimum surviving grain size in a distribution, \( a_s \), is determined by the size of the smallest grain that does not sublimate in the radiation field in which the distribution is embedded. As the magnitude of the radiation field energy density increases, the grain distribution becomes increasingly depleted of small grains. A stronger radiation field therefore changes the SED of emission from a distribution of grains both by increasing the temperature of the grains and by weighing the grain size distribution function.
to larger grains. In addition, due to their lower sublimation temperatures, silicate grains become depleted before graphite grains. Sublimation is one of many physical processes that can set the minimum grain size within a distribution. Shock waves (Jones et al. 1994; Draine 1995), sputtering (Draine & Salpeter 1979), and grain-grain collisions (Tielens et al. 1994) can also influence the minimum grain size. However, these other effects are more difficult to model than sublimation, since they require a dynamic model of the region where the grains are located. We do not consider them further.

4.3. Thermal Heating

The equilibrium temperature attained by a grain is a function of its composition, size, and the spectrum and strength of the radiation field in which it is embedded. Our adopted dust model contains grains spanning several orders of magnitude in size, so the temperatures of individual grains within a distribution embedded in a given radiation field vary greatly. For a graphite or silicate grain embedded in a radiation field with normalized energy density \( \tilde{u}_v \) (see Fig. 2) that has a fitted magnitude \( \tilde{U} \), energy conservation requires that

\[
\int C_{abs}^{i}(a, \nu) \tilde{U} e^\tilde{u}_v d\nu = \int C_{abs}^{i}(a, \nu) 4\pi B_\nu \left[T_{eq}^{i}(a)\right] d\nu. \tag{12}
\]

Here the left- and right-hand sides represent the rates at which energy is absorbed and emitted by a grain, respectively. Equation (12) is therefore an implicit equation for the equilibrium temperatures, \( T_{eq}^{i}(a) \), of the graphite and silicate grains in a distribution. These temperatures are used in equation (15) to properly calculate the spectrum of emission from each decomposition component. We calculate the temperatures of grains in the hot dust component using the normalized AGN energy density, \( \tilde{u}_{v,AGN} \), and the temperatures of grains in the warm, cool, and cold dust components using the normalized ISRF energy density, \( \tilde{u}_{v,ISRF} \) (see Fig. 2). Note that although the shape of the illuminating radiation field does affect the temperatures of grains (since grains absorb and emit more efficiently at certain wavelengths), similar grain temperatures may be obtained from two different radiation fields by suitably adjusting the magnitude of the energy density of each field. Thus, the specific choices about which illuminating radiation fields we use to calculate our dust equilibrium temperatures do not have a significant impact on our results. Note also that once the shape of the normalized energy density is chosen, the temperature of a grain in that field will scale with the fitted magnitude of the energy density, \( \tilde{U} \).

4.4. Stochastic Heating

The heat capacities of very small grains are sufficiently small that they undergo large temperature fluctuations on absorption of individual photons and radiate most of the deposited energy on timescales much shorter than the typical time between photon strikes. To estimate the importance of this stochastic heating for our dust components, we calculate the threshold grain size below which grains fall out of thermal equilibrium. For graphite grains, Draine & Li (2001) calculate this to occur for

\[
a_{min} \approx 100 \AA \left(\frac{u}{u_{MMP}}\right)^{-0.2}, \tag{13}
\]

where \( u \equiv \int u_v d\nu \) is the integrated spectral energy density of the illuminating radiation field and \( u_{MMP} \) is the integrated spectral energy density of the local interstellar radiation field from Mezger et al. (1982). For our cold, cool, warm, and hot dust components, typical threshold grain sizes from equation (13) are \( a_{min} \approx 53, 14, 7.5, \) and \( 3 \AA \), respectively.

In the model of Li & Draine (2001) stochastically heated grains exhibit strong spectral feature emission (i.e., PAHs) but have very weak continua (due to the low continuum opacities of small grains). Most dusty galaxies contain a significant amount of thermally heated \( T \gtrsim 100 \) K dust that emits more continuum radiation than these stochastically heated grains (see also Laor & Draine 1993). Thus, the continuum radiation from stochastically heated grains in our cold component (i.e., grains with \( a < 53 \AA \)) is weak compared to the thermal emission from warmer dust. In addition, since the threshold grain size decreases as the magnitude of the illuminating radiation field energy density increases, stochastically heated continuum emission is even less important for grains in our cool, warm, and hot components. Since the stochastic continuum emission of all components is weak compared to the emission from thermally heated grains, and given that the stochastically heated feature emission attributed to PAHs is included in our model through the PAHs component, we do not incorporate a detailed model of stochastic heating.

4.5. Dust Emissivity

The total emissivity per hydrogen nucleon of a distribution of grains (in units of ergs s\(^{-1}\) Hz\(^{-1}\) sr\(^{-1}\) H\(^{-1}\)) is obtained by summing over the emissivity of each grain species

\[
E_{\nu} = E_{\nu}^{gr} + E_{\nu}^{sil}. \tag{14}
\]

Here the emissivities of graphite and silicate grains are

\[
E_{\nu}^{i} = \int_{50 \AA}^{\infty} \frac{1}{m_i} \frac{dn_i}{da} C_{abs}^{i}(a, \nu) B_{\nu} \left[T_{eq}^{i}(a, \tilde{U})\right] da, \tag{15}
\]

which is an average over the individual emissivities of the grains in the distribution. Note that in contrast to models using a single effective grain size, the dust emissivity in our adopted model is not directly proportional to the dust opacity (see § 4.7), since the equilibrium grain temperatures in equation (15) depend on grain size and composition.

4.6. Characteristic Distribution Temperature

As discussed in § 4.3, the many grains within a distribution are brought to different equilibrium temperatures through interactions with the radiation field in which they are embedded. In our decomposition method this distribution of equilibrium temperatures is determined from the fitted magnitude of the illuminating radiation field energy density, \( \tilde{U} \). A given dust component therefore has many temperatures associated with it, none of which uniquely characterize the properties of the distribution. This is clearly not a desirable situation, as we would like to associate a single characteristic temperature with each value of \( \tilde{U} \), preferably a temperature that communicates the position of the spectral peak of the resulting emission from the distribution. To meet this goal, we define the luminosity-weighted characteristic distribution temperature

\[
\bar{T} \equiv \bar{T}(\tilde{U}) = \frac{\int_{50 \AA}^{\infty} \sum_i f_{\nu}^{i}(a, \tilde{U}) T_{eq}^{i}(a, \tilde{U}) da}{\int_{50 \AA}^{\infty} \sum_i f_{\nu}^{i}(a, \tilde{U}) da}, \tag{16}
\]

where the sum is over the two grain compositions and

\[
f_{\nu}^{i}(a, \tilde{U}) = \frac{1}{n_i} \frac{dn_i}{da} \int C_{abs}^{i}(a, \nu) B_{\nu} \left[T_{eq}^{i}(a, \tilde{U})\right] d\nu \tag{17}
\]
is the grain-luminosity distribution function (which is essentially the spectrally integrated emissivity of an individual grain; see § 4.5). Note that the integration starts at $a = 50$ Å, since smaller grains are not in thermal equilibrium.

Using this weighting function, $\tilde{T}$ is properly interpreted as the composition-averaged temperature of the luminosity-dominating grain size. With this definition, the emission peak from a distribution of grains occurs near the wavelength expected from the dust-modified Wien’s law

$$\lambda_{\text{peak}} \approx \left(\frac{300 \text{ K}}{T}\right)10 \mu \text{m},$$

where the peak is defined to occur at the wavelength coinciding with the maximum value of $E_{\nu} = \Sigma_{\text{abs}} B_{\nu}(T)$ (i.e., the emissivity of a distribution in the limit in which the temperatures of its constituent grains are independent of their size and composition).

Figure 4 shows the range of equilibrium temperatures, $T_{\text{eq}}$, of the grains within a distribution as a function of the characteristic distribution temperature $\bar{T}$. The dark shaded region shows the range of equilibrium temperatures within a given distribution (i.e., at a fixed value of $\bar{T}$), while the solid line shows their luminosity-weighted characteristic temperature. Light shaded regions indicate typical characteristic temperature ranges for the decomposition components. The sublimation temperature of silicates is also labeled (dashed line).

which is an average over the individual opacities of the grains in the distribution. The total extinction opacity per hydrogen nucleon, $\Sigma_{\text{ext}}$, is calculated in an analogous way with $C_{\text{abs}} \rightarrow C_{\text{ext}}$. According to Li & Draine (2001, Table 6), $\Sigma_{\text{abs}} \propto \lambda^{-2}$ over the range $20 \mu \text{m} < \lambda < 700 \mu \text{m}$ and $\Sigma_{\text{abs}} \propto \lambda^{-1.68}$ over the range $700 \mu \text{m} < \lambda < 10^4 \mu \text{m}$ to within $\pm 10\%$.

4.8. Water Ice and HAC Opacity

Mid-IR spectra often exhibit 5.6–7.8 $\mu \text{m}$ opacity produced from a combination of water ice absorption near 6.1 $\mu \text{m}$ (see, e.g., Chiar et al. 2000; Gibb et al. 2000) and absorption from hydrogenated amorphous carbon (HAC) near 6.85 and 7.25 $\mu \text{m}$ (Furton et al. 1999). Such water ice and HAC absorption is particularly prominent in ULIRG spectra (e.g., Spoon et al. 2002). We derive 5.6–7.8 $\mu \text{m}$ water ice and HAC opacity templates from the IRS spectrum of the heavily obscured ULIRG IRAS F00183–7111 (Spoon et al. 2004). This high signal-to-noise ratio spectrum exhibits strong water ice and HAC absorption with very little PAH emission, thereby providing a clean spectrum from which to extract profiles of the various opacity sources. We fit a smooth spline to the observed spectrum between continuum points on either side of the water ice and HAC features and use the ratio of the observed spectrum to the estimated continuum to obtain the opacity templates displayed in the right panel of Figure 5.

Additional opacity from 3.1 $\mu \text{m}$ water ice and 3.4 $\mu \text{m}$ HAC features may significantly affect the broadband photometry of some sources (see Fig. 5). We therefore use the L-band spectra of ULIRGs presented in Imanishi et al. (2006) to derive opacity templates for these features to use in our decompositions. The opacities of the 3.1 $\mu \text{m}$ water ice and 3.4 $\mu \text{m}$ HAC features are derived from spectra of the deeply obscured ULIRGs IRAS 00188–0856 and IRAS 08572+3915, respectively. Note that we do not derive the 6.1 $\mu \text{m}$ water ice template from the IRS spectrum of IRAS 00188–0856 since it is contaminated by 6.2 $\mu \text{m}$ PAH emission. As measured from their L-band and IRS spectra, the water ice features of IRAS 00188–0856 have apparent $\tau_{\text{HAC}^\text{ice}}/\tau_{\text{HAC}} \approx 3.9$, while the HAC features of IRAS 08572+3915 have apparent $\tau_{\text{HAC}^\text{HAC}}/\tau_{\text{HAC}} \approx 3.3$. Our full opacity templates, shown in Figure 5, are constructed using these optical depth ratios to set the scalings between the 3.1–3.4 $\mu \text{m}$ and 5.6–7.8 $\mu \text{m}$ features.

4.9. Total Optical Depth

The total optical depth along a line of sight is the sum of the optical depths from each opacity source. Thus, in our case

$$\tau(\lambda) = \tau_{\text{dust}}(\lambda) + \tau_{\text{ice}}(\lambda) + \tau_{\text{HAC}}(\lambda).$$

The optical depth through a column of dust having total absorption or extinction (depending on the situation) opacity $\Sigma(\lambda)$ is given by

$$\tau_{\text{dust}}(\lambda) = N_{\text{H}} \Sigma(\lambda) = \tilde{\tau}_{\text{dust}} \frac{\Sigma(\lambda)}{\Sigma(9.7 \mu \text{m})},$$

where $N_{\text{H}}$ and $\tilde{\tau}_{\text{dust}}$ are the hydrogen nucleon column density and 9.7 $\mu \text{m}$ optical depth through the dust, respectively. The optical depth due to ice absorption is given by

$$\tau_{\text{ice}}(\lambda) = \tilde{\eta}_{\text{ice}} \tilde{\tau}_{\text{ice}} \frac{\Sigma_{\text{ice}}(\lambda)}{\Sigma_{\text{ice}}(6.1 \mu \text{m})},$$

where $\Sigma_{\text{ice}}$ is the ice opacity template from Figure 5 and $\tilde{\eta}_{\text{ice}} \equiv \tilde{\tau}_{\text{ice}}/\tilde{\tau}_{\text{dust}}$ determines the amount of ice opacity for a given dust
opacity. Similarly, the optical depth due to HAC absorption is given by
\[
\tau_{\text{HAC}}(\lambda) = \tilde{\eta}_{\text{HAC}} \frac{\Sigma_{\text{HAC}}(\lambda)}{\Sigma_{\text{HAC}}(6.85 \ \mu m)},
\]
where \(\Sigma_{\text{HAC}}\) is the HAC opacity template from Figure 5 and \(\tilde{\eta}_{\text{HAC}} \equiv \frac{h_{\text{HAC}}}{h_{\text{dust}}^{9.7}}\) determines the amount of HAC opacity for a given dust opacity. The ratios of the apparent 6.1 \(\mu m\) water ice and 6.85 \(\mu m\) HAC optical depths to the apparent 9.7 \(\mu m\) silicate optical depth are both \~0.1 for the various ULIRGs used to derive the opacity templates. We therefore restrict the fitted values of these ratios to satisfy \(0 \leq \tilde{\eta}_{\text{Ice}} \leq 0.1\) and \(0 \leq \tilde{\eta}_{\text{HAC}} \leq 0.1\) in our decomposition method.

5. DUST EMISSION

5.1. Optically Thin Dust Emission

Figure 6 presents an illustration of the optically thin dust shell approximation used to calculate the SEDs of emission from the dust components in our decomposition that are heated directly by ultraviolet and optical photons from the SB and AGN source components (see also Fig. 1). The left panel depicts a starburst containing an SB source component surrounded by a shell of dust. The

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**Fig. 5.**—Water ice and HAC opacity templates derived from L-band (Imanishi et al. 2006) and IRS (Spoon et al. 2004) spectra of ULIRGs (see text). Also shown in the left panel is the arbitrarily scaled IRAC 3.6 \(\mu m\) transmission curve for sources at \(z = 0, 0.1, \) and \(0.2\) (right to left).

**Fig. 6.**—Cross-sectional views illustrating the optically thin dust shell approximation used to calculate the SEDs of emission from the dust components that are directly heated by ultraviolet and optical radiation from the SB and AGN source components (see text). The left panel depicts an SB source component surrounded by a shell of dust. The right panel shows an AGN accretion disk and torus (made of either discrete clouds as on the left or a smooth dust distribution as on the right) and more distant narrow-line region clouds.
right panel shows an AGN comprised of an AGN accretion disk, a dusty torus (either smooth or made of discrete clouds), and more distant narrow-line region clouds. In this geometry, ultraviolet and optical photons emitted by the source components either escape freely or are absorbed within shells of dust on the illuminated sides of clouds. By definition, these shells have an optical depth of order unity at the wavelength of peak energy absorption

$$
\lambda_{\text{peak}} = \frac{\int \Sigma_{\text{abs}}(\lambda) u_{\lambda} \lambda d\lambda}{\int \Sigma_{\text{abs}}(\lambda) u_{\lambda} d\lambda}.
$$

Here the absorption-weighted distribution function is obtained by integrating the energy absorbed by a single grain (i.e., the left-hand side of eq. [12]) over the distribution. As described in §4.3, we assume that grains in the hot component are heated by the AGN radiation field (Fig. 2), while grains in the other dust components are heated by the ISRF field. The peak absorption wavelengths from equation (25) for these fields are 1470 and 4550 Å, respectively. At these wavelengths, the dust absorption opacity is approximately 20 and 5 times greater than its value at 9.7 μm, so that the 9.7 μm optical depths of the thin dust shells illuminated by the AGN and ISRF radiation fields are \( \tau_{9.7} \approx 0.05 \) and 0.2, respectively.

All emission from these shells therefore emerges from regions that are optically thin at all infrared wavelengths (i.e., \( \lambda \gtrsim 1 \mu m \)). The emerging intensity from these shells, calculated from the radiative transfer equation, is therefore

$$
I_{\nu} = \int_{0}^{\tau_{\text{hot}}} S_{\nu}(\tau') e^{-(\tau_{\text{hot}} - \tau')} d\tau' = (1 - e^{-\tau_{\text{hot}}}) S_{\nu}.
$$

Here the source function \( S_{\nu} \equiv E_{\nu}/\Sigma_{\text{abs}} \) is assumed to be constant (i.e., the magnitude of the radiation field energy density, and thus the dust temperature distribution, is assumed to be uniform). As shown above, \( \tau_{\text{shell}} < 1 \) for all infrared wavelengths, so that equation (26) simplifies to

$$
I_{\nu} \approx N_{\text{H}} \Sigma_{\text{abs}} E_{\nu},
$$

where \( N_{\text{H}} \Sigma_{\text{abs}} \) is the hydrogen number density times the dust mass per unit volume.

### 5.2. Hot and Warm Component Emission

Using equation (27), the flux densities per unit frequency interval from the hot and warm components are

$$
 f_{\nu}^{\text{hot}} \propto E_{\nu}(U_{\text{hot}}) e^{-\tau_{\text{hot}}}, \quad f_{\nu}^{\text{warm}} \propto E_{\nu}(U_{\text{warm}}) e^{-\tau_{\text{warm}}},
$$

where \( \tau_{\text{hot}} = \tau(U_{\text{hot}}) \) and \( \tau_{\text{warm}} = \tau(U_{\text{warm}}) \) are the characteristic component temperatures determined from the fitted values of \( U_{\text{hot}} \) and \( U_{\text{warm}} \) (see §4.6) and

$$
\tau_{\text{hot}} = \tau_{9.7} \frac{\Sigma_{\text{abs}}(\lambda)}{\Sigma_{\text{abs}}(9.7 \mu m)}; \quad \tau_{\text{warm}} = \tau_{9.7} \frac{\Sigma_{\text{abs}}(\lambda)}{\Sigma_{\text{abs}}(9.7 \mu m)}.
$$

are the optical depths through the screens of dust obscuring the hot and warm components (e.g., provided by the cool and cold components in the geometry of Fig. 1). Here \( \tau_{9.7}^{\text{hot}} \) and \( \tau_{9.7}^{\text{warm}} \) are the screen optical depths to the hot and warm components at 9.7 μm. Note that we use the absorption and not the extinction opacity since scattering is negligible for \( \lambda \gtrsim 3 \mu m \), where essentially all dust emission is radiated. Example hot and warm component SEDs, \( f_{\nu}^{\text{hot}} \) and \( f_{\nu}^{\text{warm}} \), are shown in Figure 7 for the characteristic temperatures \( T_{\text{hot}} = 1400 \) K and \( T_{\text{warm}} = 200 \) K. The fitted hot component characteristic temperature is constrained to satisfy \( 500 \text{ K} < T_{\text{hot}} < 1500 \text{ K} \), and the fitted warm component characteristic temperature typically satisfies \( 150 \text{ K} < T_{\text{warm}} < 500 \text{ K} \). Also shown in Figure 7 are example hot and warm component SEDs obscured by screens having \( \tau_{9.7} = 1, 2, \) and 3. Note that departures from a smooth continuum near 9.7 and 18 μm are caused by emission and absorption from silicates.

### 5.3. Cool and Cold Component Emission

In the geometry of Figure 1, dust in the cool and cold components may serve as sources of opacity to obscure the emission from other components. Given this geometry and the observation that the mid-IR obscuration in dusty galaxies is often quite high (e.g., \( \tau_{9.7} \approx 3-5 \) for many of the local ULIRGs in Armus et al. 2006), the optically thin approximation used to obtain equation (27) is not necessarily valid for the cool and cold components. However, as a result of their relatively cool characteristic temperatures and 40–100 μm SED peaks, the optical depth through these components at the wavelengths over which they emit strongly is ~10–30 times smaller than at 9.7 μm. Therefore, despite potentially large 9.7 μm optical depths, both components are actually optically thin at the wavelengths over which the majority of their emission is radiated. Thus, the conditions required for the validity of equation (27) are in fact still satisfied so that the flux densities per unit frequency interval of emission from the cool and cold dust components are

$$
 f_{\nu}^{\text{cool}} \propto E_{\nu}(U_{\text{cool}}), \quad f_{\nu}^{\text{cold}} \propto E_{\nu}(U_{\text{cold}}),
$$

where \( T_{\text{cool}} = \tau(U_{\text{cool}}) \) and \( T_{\text{cold}} = \tau(U_{\text{cold}}) \) are the characteristic component temperatures determined from the fitted values of \( U_{\text{cool}} \) and \( U_{\text{cold}} \). We assume that emission from both the cool and cold components emerges unextinguished since the optical depths required to achieve significant extinctions at \( \lambda \sim 50 \mu m \) where they emit strongly would imply implausibly high optical depths at shorter wavelengths. Example cool and cold component SEDs, \( f_{\nu}^{\text{cool}} \) and \( f_{\nu}^{\text{cold}} \), are shown in Figure 7 for the characteristic temperatures \( T_{\text{cool}} = 80 \text{ K} \) and \( T_{\text{cold}} = 35 \text{ K} \). The fitted cool and cold component characteristic temperatures typically satisfy \( 50 \text{ K} < T_{\text{cool}} < 100 \text{ K} \) and \( 25 \text{ K} < T_{\text{cold}} < 40 \text{ K} \), respectively. Also shown
in Figure 7 are the cool and cold SEDs obscured by screens having \( \gamma_7 = 1, 2, \) and 3, demonstrating that the obscured cool and cold component SEDs are changed very little.

### 5.4. Comparison with Other Methods

The emergent flux density from dust embedded in a distribution of radiation fields with energy densities \( U \) is

\[
f_{\nu}^{\text{dust}} \propto \int \frac{dM_{\text{dust}}}{dU} E_{\nu}(T(U)) dU.
\]

(31)

Here \( M_{\text{dust}}(U) \) is the mass of dust heated to the characteristic temperature \( T(U) \) by the field with strength \( U \). Our four-component dust model characterizing the emission from a galaxy is derived from equation (31) by taking

\[
\frac{dM_{\text{dust}}}{dU} = \sum_{i=1}^{4} M_{\text{dust}}^i \delta(U - U_i),
\]

(32)

where the sum is over four discrete values of \( U_i \) illuminating a mass \( M_{\text{dust}}^i \) of dust each. Clearly, equation (32) is an oversimplification of the true distribution of mass in a galaxy. Dale et al. (2001) and Li & Draine (2002) both calculate the integrated emission from dust in galaxies by assuming a power-law distribution of dust mass over heating intensity

\[
\frac{dM_{\text{dust}}}{dU} \propto U^{-\alpha},
\]

(33)

where \( \alpha \) determines the relative contributions from each value of the radiation field energy density. Given a sufficient number of discrete temperature components, the model in equation (32) can be used to approximate the emission from the power-law model to arbitrary precision (with the appropriate weighting of each component through the \( M_{\text{dust}}^i \)). The fact that both our multicomponent model and these power-law models produce excellent fits to the integrated spectra of galaxies implies that the required “sufficient number” of discrete components postulated above must be approximately four.

The real power of our multicomponent approach stems from the fact that it is capable of approximating not only the emission from the mass distribution of star-forming galaxies in equation (33) but also the emission from mass distributions that are not characterized by a power law (since we do not make the geometrical assumptions concerning the distribution of dust within a galaxy implied by eq. [33]). For example, the composite emission from a galaxy containing both a starburst and an AGN may have a total mass distribution function dominated by a star-formation-driven power law at low energy densities superposed with an AGN-driven power law (having a different exponent) at high energy densities. Since the sum of two power laws with different exponents is not necessarily itself a power law, a model such as equation (33) cannot properly model this scenario. This, coupled with the fact that our method allows us to fit for different levels of obscuration toward each component (as expected for physically distinct AGN and starburst regions), drives our decision to utilize the multicomponent discrete temperature approach to describe the composite SEDs of dusty galaxies.

### 5.5. Dust Emission in Previous Publications

The decompositions of IRAS 10214+4724 in Teplitz et al. (2006), NGC 6240 in Armus et al. (2006), and the BGS sample of ULIRGs in Armus et al. (2007) were performed using an earlier version of the method described in this work, which utilized a different model to calculate the emission from each dust component. In these previous publications, dust emission is calculated from an optically thin shell of constant density material surrounding the illuminating source. As in equation (33), the dust in this shell is exposed to different radiation fields (depending on its distance from the central source) and is therefore brought to different equilibrium temperatures. In these previous works, we assume that the dust shells had a thickness \( r_{\text{out}}/r_{\text{in}} = 10 \), which fixes the range of radiation fields and therefore dust temperatures, once the temperature at the minimum radius is defined (taken to be the sublimation temperature). Since each of these dust components contains a range of temperatures (from dust at different radii), only three components were needed to fit the sources instead of the four used in the current work. We choose to adopt the four-component method for this work since it improves the fits at long wavelengths and simplifies the interpretation.

### 6. PAH EMISSION

Observations with ISO and Spitzer have shown that the presence of PAHs (Leger & Puget 1984; Allamandola et al. 1985) can be used as an indicator of star formation (e.g., Förster Schreiber et al. 2004; Peeters et al. 2004). We note, however, that Calzetti et al. (2005) find that PAH emission does not correlate well with other star formation tracers in M51. In addition, Engelbracht et al. (2005) and Wu et al. (2006) find that PAH emission varies with metallicity and so may therefore not be a useful tracer of star formation in low-metallicity systems. With these cautionary notes in mind, the presence or absence of PAH emission nevertheless provides an important clue to help distinguish between star formation and accretion-dominated ULIRGs (e.g., Genzel et al. 1998), thereby necessitating the development of a method to carefully decompose the contributions from PAHs to the total emission from dusty galaxies.

This process is complicated by the fact that it is difficult to establish the level of the continuum beneath the PAH features, especially in the presence of 9.7 \( \mu m \) silicate absorption. The method presented here provides a systematic means of estimating this continuum, and therefore the strength of the PAH features, without the need for the observer to define the continuum level by hand. We model the flux density per unit frequency interval of the PAHs component as

\[
f_{\nu}^{\text{PAHs}} = f_{\nu}^{0,\text{PAHs}} \frac{\tilde{f}^{\text{PAHs}}(6.2 \, \mu m)}{f_{\nu}^{\text{PAHs}(6.2 \, \mu m)}},
\]

(34)

where \( f_{\nu}^{0,\text{PAHs}} \equiv f_{\nu}^{\text{data}(6.2 \, \mu m)} - f_{\nu}^{\text{cont}(6.2 \, \mu m)} \) is the estimated peak flux density of the 6.2 \( \mu m \) PAH feature obtained from the local continuum-subtracted observed spectrum and

\[
\tilde{f}_{\nu}^{\text{PAHs}} = \sum_i \frac{\gamma_{i,0} f_{\nu}^{0,\text{PAHs}}}{\left( \lambda/\lambda_0^i - \lambda_0^i/\lambda \right)^\delta + \gamma_i^2},
\]

(35)

is the PAH emission template shown in Figure 8 constructed by summing over a series of Drude profiles with the parameters presented in Table 1. As suggested by the definition of \( f_{\nu}^{0,\text{PAHs}} \), the overall strength of the PAH template is held fixed during the continuum fit, but the strengths of the individual features are allowed to vary in the subsequent PAH fit (see § 2.2 and the following paragraph).

The central wavelengths and widths of our \( \lambda_0 > 3.3 \, \mu m \) features are adapted from those used in the analysis of Smith et al.
to fit the low-obscuration \((\tau_{9.7} \approx 0.24)\) mean starburst galaxy spectrum created from 13 IRS spectra in Brandl et al. (2006). The 3.3 \(\mu\)m PAH feature central wavelength and width are obtained from Li & Draine (2001), and the peak flux density of this feature is derived from the ratio of the strengths of the PAH features at 3.3 and 6.2 \(\mu\)m in the \(L\)-band and IRS spectra of the star-forming ULIRG IRAS 12112+0305 presented in Imanishi et al. (2006) and Armus et al. (2006). We include this 3.3 \(\mu\)m PAH feature so that its contribution to the integrated \(L\)-band (or IRAC 3.6 \(\mu\)m channel; see Fig. 8) flux density is explicitly included in the fitting method. As described in 2.2, after fitting the continuum, we fit the continuum-subtracted observed spectrum to refine our PAHs component (the properties of which are held fixed during the continuum fit). In this fit, the central wavelengths and FWHM of the PAH features are fixed to the values in Table 1, and the peaks are allowed to vary freely. This fit provides accurate luminosities for all PAH complexes, as well as error estimates derived from the full covariance matrix.

7. ATOMIC AND MOLECULAR LINE EMISSION

In order to accurately fit the continuum and PAH features in an IRS spectrum, the contributions from atomic and molecular lines must be properly fitted as well. Of course, the strength of these lines is scientifically interesting, but we caution against using our decomposition method to measure them since the fitted continuum around each line is not necessarily as accurate as one estimated by hand (a statement that cannot be made concerning the underlying continuum beneath PAH features). Therefore, although we obtain integrated flux values for the lines we fit, we do not recommend using these measurements for scientific purposes (at least not without carefully checking the validity of the fitted local continuum around each line). The one caveat to this recommendation where we do suggest using the fitted integrated flux is for the [ Ne ii] 12.81 \(\mu\)m line, which our decomposition method is capable of deblending from the 12.7 \(\mu\)m PAH complex in low-resolution IRS spectra.

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**TABLE 1**

| Feature | \(\lambda_0\) \((\mu\m)\) | \(\gamma_i\) | \(L_i\) \((10^{-2})\) | \(L_i\sum L_i^{ab}\) \((10^{-2})\) | Complex |
|---------|-----------------|-------------|-----------------|-----------------|---------|
| 1       | 3.30            | 1.2         | 0.07            | 0.6             | 1       |
| 2       | 5.27            | 3.4         | 0.66            | 1.0             | 2       |
| 3       | 5.70            | 3.5         | 0.77            | 1.1             | 3       |
| 4       | 6.22            | 3.0         | 0.77            | 9.7             | 4       |
| 5       | 6.69            | 7.0         | 0.10            | 2.7             | 5       |
| 6       | 7.42            | 12.6        | 0.24            | 39.3            | 6       |
| 7       | 7.60            | 4.4         | 0.89            | ...             | ...     |
| 8       | 7.85            | 5.3         | 0.86            | ...             | ...     |
| 9       | 8.33            | 5.0         | 0.25            | 3.9             | 7       |
| 10      | 8.61            | 3.9         | 0.65            | 7.6             | 8       |
| 11      | 11.23           | 1.2         | 1.29            | 11.3            | 9       |
| 12      | 11.33           | 3.2         | 1.04            | ...             | ...     |
| 13      | 11.99           | 4.5         | 0.32            | 3.2             | 10      |
| 14      | 12.62           | 4.2         | 0.85            | 7.9             | 11      |
| 15      | 12.69           | 1.3         | 0.19            | ...             | ...     |
| 16      | 13.48           | 4.0         | 0.22            | 1.7             | 12      |
| 17      | 14.19           | 2.5         | 0.18            | 0.8             | 13      |
| 18      | 16.45           | 1.4         | 0.43            | 8.4             | 14      |
| 19      | 17.04           | 6.5         | 0.64            | ...             | ...     |
| 20      | 17.38           | 1.2         | 0.29            | ...             | ...     |
| 21      | 17.87           | 1.6         | 0.26            | ...             | ...     |
| 22      | 18.92           | 1.9         | 0.31            | 0.8             | 15      |

*Fraction of total PAH luminosity emerging from each complex \(j\).

\(L_i = \sum_i L_i\) is the total luminosity of a complex of Drude profiles, where \(L_i = 4\pi D_j^2(\ln 2)/\lambda_0\gamma_i^2\) is the apparent total luminosity of a single profile, with \(D_j\) the luminosity distance to the source.

As defined in Smith et al. (2007), the 7.7, 11.3, 12.7, and 17 \(\mu\)m complexes are each composed of multiple Drude profiles.

We create our atomic and molecular emission line spectrum by estimating the peak flux density of each line in Table 2 from the local continuum-subtracted IRS spectrum. The flux density per unit frequency interval of the \(\text{lines}\) component is modeled as a sum over unresolved Gaussian profiles having central wavelengths \(\lambda_0\), widths \(\gamma_i\), and peak flux densities \(f_{\nu,0}\).

\[
f_{\nu} = \sum_i f^{i}_{\nu,0} \exp \left\{-\frac{1}{2} \left[ \frac{\lambda - \lambda_0^{i}}{\gamma_i^i} \right]^2 \right\}^{36}
\]

Since the Gaussian profiles are unresolved, the width of each line is a function of the IRS module in which it is detected (see Table 2 for values of \(\gamma\) as a function of source redshift). As described in 5.6 for the PAHs component, after fitting the continuum we perform a fit to the continuum-subtracted observed spectrum in order to refine the lines component (the parameters for which are held fixed in the continuum fit). In this fit, the central wavelengths and FWHM of the atomic and molecular emission lines are fixed to the values in Table 2, and their peak flux densities are allowed to range freely. From this fit, we obtain line luminosities and their uncertainties, although, as noted above, we recommend measuring all unblended line fluxes by hand.

8. CONSTRUCTING DUSTY GALAXY SEDs

8.1. Sample Selection

Table 3 presents a summary of the galaxies in our sample. They have been selected with the goal of demonstrating the capabilities of our decomposition method on a variety of dusty galaxy SEDs, representative of the diverse properties of the group. We include examples of unextinguished and obscured starbursts, a quasar, a...
DECOMPOSING DUSTY GALAXIES. I.

### Supplementary Photometry

| Galaxy         | Ultraviolet | Optical | Near-IR | Far-IR | Submillimeter |
|----------------|-------------|---------|---------|--------|---------------|
| NGC 7714........ | 1           | 5       | 12      | 13, 17 | 13, 17        |
| NGC 2623........ | 2           | 6       | 9       | 12     | 17, 18        |
| PG 0804+761..... | 3           | 3       | 10, 11  | 14, 15 |               |
| Mrk 463 .......... | 1           | 7       | 10      | 14, 16 |               |
| NGC 6240........ | 4           | 8       | 9       | 12, 16 |               |
| Mrk 1014......... | 3           | 7       | 9       | 14, 15 |               |

### References

1. Kinney et al. 1993; 2. GALEX 2006; 3. Baskin & Laor 2005; 4. Smith et al. 1992; 5. Lacon et al. 2001; 6. Taylor et al. 2005; 7. Surace & Sanders 2000; 8. de Vaucouleurs et al. 1991; 9. Scoville et al. 2000; 10. 2MASX PSC; (11) Neugebauer et al. 1987; (12) Sanders et al. 2003; (13) Knudt et al. 1998; (14) Moshir et al. 1990; (15) Haas et al. 2003; (16) Klaas et al. 2001; (17) Dunne et al. 2000; (18) Benford 1999.

AGNs, starbursts, normal, dwarfs, and ellipticals, so long as their SEDs are composed of emission from stars, dust, PAHs, atomic and molecular lines, and possibly an AGN accretion disk (i.e., our decomposition components).

### 8.2. IRS Spectroscopy

The IRS spectra of the sources in our sample were first presented in the papers referred to in Table 3. All spectra in this paper have been extracted using the method described in Armus et al. (2006). In brief, the IRS pipeline at the Spitzer Science Center was used to reduce the data, and one-dimensional spectra were extracted using the SMART package (Higdon et al. 2004). After scaling and stitching the individual orders together, each spectrum was scaled to match the MIPS 24 μm flux density if available (see § 8.4), or the IRAS 25 μm flux density otherwise.

### 8.3. Supplementary Photometry

The spectral coverage of the IRS low-resolution modules ends at an observed-frame wavelength of ~38 μm. Emission from typical cool component dust (T ~ 80 K) therefore only contributes to the last few microns, while emission from typical cold component dust (T ~ 35 K) contributes negligibly at IRS wavelengths. To better constrain these cooler components that dominate the dust mass and frequently provide ~50% of the total dust luminosity, we supplement our IRS spectra with far-IR to millimeter wavelength photometry from the literature. Furthermore, the spectral coverage of the IRS modules begins at an observed-frame wavelength of ~5.2 μm. As seen in Figure 2, our source components all radiate significantly at shorter wavelengths. Thus, to better constrain these components, we supplement our SEDs with ultraviolet to near-IR photometry from the literature. Table 4 provides references to the literature for all photometry used in our decompositions.

In each wavelength range, we construct our SEDs using data that most closely sample the spatial region contained within the IRS slits. We treat photometric points that sample larger spatial regions (i.e., for wavelength ranges where no data at a similar spatial resolution are available in the literature) as upper limits to the flux density of the area covered by the IRS slit. To include such a limit as input to the χ² fitting routine (which requires both the flux density of each data point and its associated error), we assign the data to have an upper limit flux density f_guess and an uncertainty σ_i = f_guess / 3. If, in addition to an upper limit to the flux density contained in the IRS slit, we also have an estimate of the lower limit (e.g., as estimated using a very small aperture

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**TABLE 2**

**ATOMIC AND MOLECULAR LINE PARAMETERS**

| i   | Line       | λ_0 (μm) | γ_0 | γ_0+0.1 | γ_0+0.25 | γ_0+0.5 |
|-----|------------|----------|-----|---------|----------|---------|
| 1   | H2 S(8)    | 5.053    | ... | 6.0     | 6.0      | 12.1    |
| 2   | [Fe ii]   | 5.340    | ... | 6.0     | 6.0      | 12.1    |
| 3   | H2 S(7)    | 5.511    | ... | 6.0     | 6.0      | 12.1    |
| 4   | [Fe ii]   | 5.674    | ... | 6.0     | 6.0      | 12.0    |
| 5   | H2 S(6)    | 6.109    | ... | 6.0     | 12.1     | 12.1    |
| 6   | [Fe ii]   | 6.721    | ... | 6.0     | 12.1     | 12.1    |
| 7   | H2 S(5)    | 6.910    | ... | 12.1    | 12.1     | 12.1    |
| 8   | [Ar ii]   | 7.985    | ... | 12.1    | 12.1     | 12.1    |
| 9   | [Ne v]    | 7.652    | ... | 12.1    | 12.1     | 12.1    |
| 10  | H2 S(4)    | 8.025    | ... | 12.1    | 12.1     | 12.1    |
| 11  | [Ar iii]  | 8.991    | ... | 12.1    | 12.1     | 12.1    |
| 12  | H2 S(3)    | 9.665    | ... | 12.1    | 12.1     | 16.9    |
| 13  | [S iv]    | 10.511   | ... | 12.1    | 12.1     | 16.9    |
| 14  | H2 S(2)    | 12.279   | 12.1 | 16.9    | 16.9     | 16.9    |
| 15  | [Ne ii]   | 12.814   | 12.1 | 16.9    | 16.9     | 16.9    |
| 16  | [Ne v]    | 14.322   | 16.9 | 16.9    | 16.9     | 33.9    |
| 17  | [Ne ii]   | 15.555   | 16.9 | 16.9    | 22.3     | 33.9    |
| 18  | H2 S(1)   | 17.035   | 16.9 | 16.9    | 33.9     | 33.9    |
| 19  | [S ii]    | 18.713   | 16.9 | 33.9    | 33.9     | 33.9    |
| 20  | [Ne v]    | 24.317   | 16.9 | 33.9    | 33.9     | 33.9    |
| 21  | [O iv]    | 25.890   | 33.9 | 33.9    | 33.9     | 33.9    |
| 22  | H2 S(0)   | 28.219   | 33.9 | 33.9    | 33.9     | 33.9    |
| 23  | [S iii]   | 33.481   | 33.9 | 33.9    | 33.9     | 33.9    |
| 24  | [Si ii]   | 34.815   | 33.9 | 33.9    | 33.9     | 33.9    |
| 25  | [Ne iii]  | 36.014   | 33.9 | 33.9    | 33.9     | 33.9    |

**Notes:** The FWHM = λ_0γ_0 of a particular atomic or molecular line is a function of the IRS module in which it is detected and therefore depends on the redshift of the source. We give example values of γ_0 for all lines at z = 0.0, 0.1, 0.25, and 0.5. Values of γ_0 are not given for lines that fall out of the IRS wavelength range at a given redshift.

**TABLE 3**

**DUSTY GALAXY PROPERTIES**

| Galaxy         | z  | D_L (Mpc) | Class     | References |
|----------------|----|-----------|-----------|------------|
| NGC 7714........ | 0.009 | 39       | Starburst | 1, 2       |
| NGC 2623........ | 0.018 | 78       | Obscured starburst | 2       |
| PG 0804+761..... | 0.130 | 610      | Quasar    | 3         |
| Mrk 463 .......... | 0.050 | 222      | Seyfert 2 | 4         |
| NGC 6240........ | 0.024 | 105      | Starburst+AGN | 5         |
| Mrk 1014......... | 0.163 | 781      | Quasar+starburst | 4       |

**Notes:** The IRS spectra of the first three sources are from Spitzer program 14, and the spectra of the last three are from Spitzer program 105. Luminosity distances are calculated assuming a flat ΛCDM cosmology with H₀ = 70 km s⁻¹ Mpc⁻¹, Ωₐ = 0.3, and Ωₐ = 0.7.

**References:** (1) Brandl et al. 2004; (2) Brandl et al. 2006; (3) Hao et al. 2005; (4) Armus et al. 2004; (5) Armus et al. 2006.
and are estimated to be 10% at 24 µm and 20% at 70 and 160 µm. No color corrections are applied to the IRAC or MIPS photometry since all corrections are much smaller than the uncertainties.

9. DECOMPOSING DUSTY GALAXIES

9.1. Spectral Decomposition Results

In Figures 9 and 10 we present our decompositions of the nuclear SEDs of the dusty galaxies in our sample. In these fits, the MIPS photometric points are used to constrain the nuclear far-IR SEDs, while the globally integrated IRAS, ISO, and submillimeter data provide upper limits to this nuclear emission. The entire ultraviolet to millimeter wavelength SEDs are presented in Figure 9, and enlarged views focusing on the IRS regions are shown in Figure 10. In Figure 9 we also show the global fitted flux densities obtained using the full values of the large-beam IRAS, ISO, and submillimeter data. The temperatures of the cold and cool dust components obtained in the global fits are held fixed to these values in the nuclear decompositions. Note that the IRSF component contributes minimally (only in Mrk 463) since the small-aperture near-IR photometry used to match the IRS slits is dominated by emission from young stellar populations and not evolved stars.

9.2. Decomposition Parameters and Constraints

The decomposition parameters obtained from the fits to the nuclear SEDs of the dusty galaxies in our sample are presented in Tables 6 and 7. There are a total of 17 free parameters. The SB component has two free parameters: \( \beta_{SB} \) and \( \tau_{SB} \), which determine the fractional SB contribution to the total luminosity (see eq. [1]) and the 5500 Å optical depth (see eq. [6]). The ISRF source component has only one free parameter: \( \alpha_{ISRF} \) (see eq. [5]). The AGN source component has a total of two free parameters: \( \beta_{AGN} \) and \( \tau_{AGN} \), where the latter determines the fraction of the AGN component covered by the obscuring screen (see eq. [9]). The optical depth through the obscuring clouds to the AGN component is fixed to \( \tau_{AGN} = 25 \). The hot and warm dust components each have three free parameters: \( \beta_i \), \( \tau_{i,SB} \), and \( \tau_{i,AGN} \). These determine the component luminosities, 9.7 µm optical depths, and dust temperatures via \( T_i \equiv T(U_i) \) (see eq. [28]). The cool and cold components each have two free parameters: \( \beta_i \) and \( T_i \) (see eq. [30]). Finally, there are two additional free parameters that control the water ice and HAC contributions to the total opacity: \( \beta_{isf} \) and \( \beta_{i,ice} \) (see eqs. [23] and [24]).

We impose the following constraints to provide sensible limits over which these parameters may range: (1) the magnitude of the radiation field energy density illuminating each dust component is constrained to give characteristic dust temperatures satisfying 20 K < \( T_{cold} \) < 50 K, 50 K < \( T_{cool} \) < 150 K, 150 K < \( T_{warm} \) < 500 K, and 500 K < \( T_{hot} \) < 1500 K; (2) the maximum water ice and HAC contributions to the total opacity are constrained by their strengths in sources with very clean absorption spectra (see § 4.8); (3) the extinction to the AGN source component is fixed to \( \tau_{AGN} = 25 \); (4) the extinction to the SB source component must satisfy \( \tau_{SB} < 5 \); (5) the optical depths through the screens obscuring the hot and warm components must not exceed the critical values beyond which their extinction-corrected luminosities would exceed the total dust luminosity; (6) the ratio of the unextinguished luminosity of the SB component to the luminosity of the PAHs component must be between the values obtained for our unobscured and obscured template starbursts NGC 7714 and NGC 2623; and (7) the hot dust covering fraction (i.e., the ratio of the unextinguished hot dust luminosity to the unextinguished AGN luminosity) must be > 0.5, consistent

### Table 5

| Galaxy       | PID | IRAC (mJy) | MIPS (Jy) |
|--------------|-----|------------|-----------|
|              |     | 3.6        | 4.5       | 24        | 70        | 160       |
| NGC 7714…….. | 59  | 17.0       | 13.5      | 1.96      | 6.67      | 4.64      |
| NGC 2623…….. | 32  | 11.8       | 13.5      | 1.33      | 16.4      | 7.56      |
| PG 0804+761…. | 49  |            |           | 0.19      | 0.11      | 0.033     |
| Mrk 463………. | 32  | 115        | 156       | 1.50      | 1.90      | 0.89      |
| NGC 6240……. | 32, 3672 | 33.7       | 46.0      | 2.71      | 14.7      | 9.98      |
| Mrk 1014……. | 32  | 19.2       | 23.2      |           |           |           |

Notes.—IRAC flux density errors are estimated to be 5% for Mrk 1014 and Mrk 463 and 10% for the other three sources. MIPS flux density errors are driven by the post-BCD calibration uncertainties and are ~10% for the 24 µm band and ~20% for the 70 and 160 µm bands. No color corrections are applied since they are much smaller than the uncertainties. The PIDs are the Spitzer program numbers for the IRAC and MIPS observations.
9.3. Derived Quantities

9.3.1. Source and Dust Component Luminosities

Apparent and extinction-corrected source and dust component luminosities from the nuclear decompositions are presented in Table 7. The apparent luminosity of each component is calculated from

\[
L_i = 4\pi D_L^2 \int f'_\nu \, d\nu \equiv \left\{ \begin{array}{ll}
\hat{\alpha}_i L_{\text{source}}, & L_i \in L_{\text{source}}, \\
\hat{\alpha}_i L_{\text{dust}}, & L_i \in L_{\text{dust}},
\end{array} \right.
\]

(37)

where \( D_L \) is the luminosity distance to the galaxy (see Table 3) and \( L_{\text{source}} \) and \( L_{\text{dust}} \) are the sums of the luminosities of all source and dust components, respectively. Extinction-corrected luminosities are calculated from

\[
L'_i = 4\pi D_L^2 \int \frac{f'_\nu}{\tau_i(\nu)} \, d\nu \equiv \left\{ \begin{array}{ll}
\hat{\alpha}_i' L_{\text{source}}, & L_i \in L_{\text{source}}, \\
\hat{\alpha}_i' L_{\text{dust}}, & L_i \in L_{\text{dust}},
\end{array} \right.
\]

(38)

where the \( \tau_i \) are the extinction terms for each component [i.e., \( \tau_{\text{AGN}} = (1 - \tilde{\epsilon}_{\text{AGN}}) + \tilde{\epsilon}_{\text{AGN}} \exp(-\tau_{\text{AGN}}) \) for the AGN component and \( \tau_i = \exp(-\tau_i) \) for the warm, hot, and SB components].

9.3.2. Dust Component Masses

The mass of dust in each of the cold, cool, warm, and hot nuclear decomposition components is provided in Table 8. We generalize the expression used to calculate dust masses for a single grain size and composition (see, e.g., eq. [4] of Klaas et al. 2001) to the case in which grains are distributed in both size and composition. The mass of dust in each component is therefore given by

\[
M_i = D_L^2 \frac{f'_\nu(\lambda_0)}{E'_\nu(\lambda_0) e^{-\tau_i(\lambda_0)}} \sum_j \frac{4}{3} \pi a_j^3 \rho_j \frac{1}{n_H} \frac{dn_j}{da},
\]

(39)

which is the product of the number of hydrogen nucleons required to power the fitted dust component and the total dust mass per hydrogen nucleon for the adopted dust model (summed over
TABLE 6

Nuclear SED Decomposition Parameters and Characteristic Dust Temperatures

| Galaxy       | χ²/dof | dof | Tcold | Tcool | Twarm | Thot | Twarmed | Thotd | VAGN | VSB | VSBd | VAGNe | VHACf |
|--------------|--------|-----|-------|-------|-------|------|----------|-------|------|-----|------|-------|-------|
| NGC 7714     | 1.33   | 382 | 31    | 71    | 165   | ...  | 0.19     | 0.97  | ...  | ... | 0    | 0     |
| NGC 2623     | 1.33   | 382 | ±1    | ±1    | ±1    | ...  | ±0.03    | ±0.02 | ...  | ... | ...  | ...   |
| PG 0804+761  | 2.46   | 383 | 29    | 53    | 206   | ...  | 3.52     | 4.81  | ...  | ... | 0.1  | 0.1   |
| Mrk 463      | 2.46   | 383 | ±1    | ±1    | ±1    | ...  | ±0.06    | ±0.11 | ...  | ... | ...  | ...   |
| NGC 6240     | 2.77   | 363 | 42    | 150   | 400   | 1410 | 0.78     | 1.22  | 0    | 0.25| 0.050| 0.044 |
| Mrk 1014     | 1.90   | 364 | 55    | 211   | 1130  | 1.30 | 2.06     | 1.12  | 1    | 0.012| 0.004| 0.009 |
| PG 0804+761  | 2.77   | 363 | ±2    | ±6    | ±3    | ±10  | ±0.01    | ±0.03 | ±0.01| ±0.012| ±0.012| ±0.035 |
| Mrk 463      | 1.90   | 364 | ±2    | ±2    | ±1    | ±6   | ±0.05    | ±0.01 | ±0.26| ... | ...  | ...   |
| NGC 6240     | 1.77   | 369 | 29    | 61    | 193   | 1260 | 3.64     | 4.68  | 1    | 0.067| 0.1   |
| Mrk 1014     | 1.77   | 369 | ±1    | ±1    | ±1    | ±30  | ±0.07    | ±0.08 | ...  | ... | ...  | ...   |
|              | 2.00   | 362 | ±1    | ±1    | ±1    | ±1   | ±0.02    | ±0.04 | ±0.01| ±0.005| ±0.005| ...   |

Notes.—Formal statistical parameter uncertainties are given beneath each parameter value. If no uncertainty is given, the corresponding parameter was pegged at a limiting value. The 5500 Å optical depth to the AGN component is fixed to ∇AGN = 25 for all fits.

a Total weighted reduced χ² value (see eqs. [2] and [3]) for the indicated number of degrees of freedom (dof).
b Characteristic dust temperature (see § 4.3) determined from the fitted value of the magnitude of the illuminating radiation field energy density, Uᵢ.
c The 9.7 μm optical depth through the screen obscuring the warm and hot dust components (see eq. [28]).
d V-band (5500 Å) optical depth through the screen obscuring the SB source component (see eqs. [6] and [7]).
e Fraction of the AGN source component covered by the obscuring screen (see eq. [9]).
f Ratio of the 6.1 μm water ice and 6.85 μm HAC optical depths to the 9.7 μm optical depth of each dust component (see eqs. [23] and [24]).
the graphite and silicate compositions). In this equation, $\lambda_0$ is an arbitrary wavelength at which the terms are evaluated, and the densities of graphite and silicate are taken to be $\rho_{\text{gra}} = 2.24$ and $\rho_{\text{sil}} = 3.50$ g cm$^{-3}$. For comparison to the dust masses and luminosities obtained from the nuclear decompositions, we present the corresponding properties for the global decompositions in Table 9.

9.3.3. Comparison with Previous Results

Klaas et al. (2001) fit the far-IR to submillimeter wavelength SEDs of a sample of ULIRGS using dust-modified blackbodies with temperatures typically ranging between 28 and 50 K. Included among their sources are two galaxies that are also in our sample, Mrk 463 and NGC 6240, for which they fit single $\beta = 2$ dust components with temperatures of 40 and 33 K, respectively. In a similar study of quasars presented in Haas et al. (2003) the far-IR SED of PG 0804+761 is fitted with a 47 K dust component. The temperatures we derive from our decompositions are all consistent with these values. Our decomposition of Mrk 463 includes contributions from 30 and 55 K dust components, while our fit to NGC 6240 includes emission from dust at 29 and 61 K. Finally, our decomposition of PG 0804+761 is dominated in the far-IR by emission from 42 K dust. For all three sources, the temperatures of the single-component fits in the literature fall between the temperatures of the dust in our multicomponent fits. Klaas et al. (2001) also fit the $\lambda > 60 \mu$m SED of NGC 6240 with multiple $\beta = 2$ dust components and obtain temperatures of 31 and 41 K (they also include a 10 K component to fit to submillimeter upper limits). Again, these temperatures are quite comparable to ours, noting that our warmer component is at a somewhat higher temperature in order to fit to the shorter wavelength data included in our fits.

As illustrated by these decompositions, multicomponent fits including dust at different temperatures are rarely unique since several components can usually be added together to approximate the SED of emission from a smaller number of components. In fact, dust in galaxies is likely to be distributed throughout many regions with various heating conditions and is therefore distributed over a continuum of temperatures. Any multicomponent decomposition therefore serves only to characterize these distributions of temperatures. In addition, if either or both of the restrictions that dust is optically thin to its own emission and that its far-IR emissivity index is characterized by $\beta = 2$ imposed above are lifted, yet different dust temperatures may be obtained for the same SEDs. For example, Klaas et al. (2001) perform fits in which the dust optical depth and emissivity are free parameters and obtain much higher temperatures: 52 and 57 K for Mrk 463 and NGC 6240, respectively. Given the multiple factors determining the temperatures derived from spectral decompositions (e.g., fixed vs. variable $\beta$), we emphasize that caution must be taken when comparing temperatures derived from different methods to ensure that they are in fact comparable.

The total far-IR luminosity from dust inferred from a multi-component decomposition is largely independent of the number of components and the choice of their characteristic temperatures (since the luminosity is just the integral under the SED). The total mass of dust, however, depends on these choices (since the mass is a strong function of temperature). Since the total mass of dust in galaxies is dominated by low-temperature material, decompositions with multiple components (including very cold dust) produce much higher dust masses. For example, Klaas et al. (2001) estimate the mass of dust in Mrk 463 to be greater than $5 \times 10^6 M_\odot$ and less than $1.2 \times 10^7 M_\odot$ as derived from their single- and multicomponent fits, respectively. Similarly, they estimate that the mass of dust in NGC 6240 is between $3.6 \times 10^7$ and

### Table 7
**Nuclear SED Decomposition Source and Dust Component Luminosities**

| Source | $L_{\text{source}}$ ($10^{10}$ $L_\odot$) | $\tilde{a}_{\text{IRF}}$ | $\tilde{a}_{\text{SB}}$ | $\tilde{a}_{\text{AGN}}$ | $\tilde{a}_{\text{AGN}}'$ | $L_{\text{dust}}$ ($10^{10}$ $L_\odot$) | $\tilde{a}_{\text{cold}}$ | $\tilde{a}_{\text{cool}}$ | $\tilde{a}_{\text{warm}}$ | $\tilde{a}_{\text{warm}}'$ | $\tilde{a}_{\text{hot}}$ | $\tilde{a}_{\text{hot}}'$ |
|--------|---------------------------------|-----------------|-----------------|-----------------|-----------------|---------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| NGC 7714 | 0.78 ± 0.03 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 3 ± 0.00 | 0.78 ± 0.03 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 3 ± 0.00 |
| NGC 2623 | 0.72 ± 0.05 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 2 ± 0.00 | 0.72 ± 0.05 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 2 ± 0.00 |
| Mrk 1014 | 0.36 ± 0.02 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 1 ± 0.00 | 0.36 ± 0.02 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 0 ± 0.00 | 1 ± 0.00 |

**Notes:** Apparent and extinction-corrected luminosities of each source and dust component in the nuclear decompositions are given as fractions of $L_{\text{source}}$ and $L_{\text{dust}}$ (see eqs. [37] and [38]). Formal statistical uncertainties for the fitted luminosities are given beneath their values. The nuclear dust luminosity of Mrk 1014 is uncertain by ~20% (i.e., the difference between its nuclear and global values), and its cold component luminosity is undetermined since no MIPS data are available to constrain its far-IR SED.

### Table 8
**Nuclear SED Decomposition Dust Masses**

| Galaxy | $M_{\text{cold}}$ ($10^7 M_\odot$) | $M_{\text{cool}}$ ($10^8 M_\odot$) | $M_{\text{warm}}$ ($10^8 M_\odot$) | $M_{\text{hot}}$ ($10^8 M_\odot$) |
|--------|--------------------------------|----------------------------|----------------------------|-----------------|
| NGC 7714 | 4.26 ± 0.13 | 4.90 ± 0.04 | 5.55 ± 0.05 | 0.00 ± 0.00 |
| NGC 2623 | 19.8 ± 1.4 | 335 ± 2 | 9.3 ± 0.2 | 0.00 ± 0.00 |
| PG 0804+761 | 1.53 ± 0.07 | 0.91 ± 0.01 | 2.95 ± 0.04 | 1.75 ± 0.09 |
| Mrk 463 | 23.7 ± 0.9 | 185 ± 3 | 101 ± 13 | 7.9 ± 0.2 |
| NGC 6240 | 67.3 ± 2.6 | 201 ± 1 | 69 ± 6 | 0.049 ± 0.003 |
| Mrk 1014 | 736 ± 5 | 333 ± 3 | 1.13 ± 0.03 | 0.00 ± 0.00 |

**Notes:** Formal statistical uncertainties for the fitted masses of the dust components in the nuclear decompositions are given along with their values. The mass of cold dust in the nucleus of Mrk 1014 is undetermined since no MIPS data are available to constrain its far-IR SED.
Our decompositions yield total globally integrated dust masses of \(2.8 \times 10^7\) and \(1.6 \times 10^8\) \(M_\odot\) for the two sources, relatively consistent with the previously derived masses (within the uncertainties of the methods). Klaas et al. (2001) estimate the \(\text{H}_2\) mass of NGC 6240 to be \(3.7 \times 10^{10}\) \(M_\odot\) [assuming \(M(\text{H}_2) = 4.6\, M_\odot\)] This value, along with our estimate of the total dust mass in NGC 6240, gives a gas-to-dust ratio of \(\sim 230\), in reasonable agreement with the canonical value of \(\sim 165\) from Li (2005).

### 9.3.4. Diagnostic Ratios

In Table 10 we present several "diagnostic" ratios for each galaxy derived from the nuclear decomposition masses and luminosities presented in Tables 7 and 8. The first entry in this table gives the ratio of the total dust luminosity to the total gas mass. The total gas mass is calculated from the fitted value of the total dust mass and the gas-to-dust ratio of our adopted dust model: \(M_{\text{dust}}/M_{\text{gas}} = 1.4 M_\odot/124 = 0.001\) (Li & Draine 2001). The definition of this quantity is motivated by the fact that two sources with equivalent values of \(L_{\text{dust}}/L_{\text{gas}}\) may have completely different physical properties (e.g., a very massive but inactive system may have the same dust luminosity as a relatively small but highly active galaxy). The total dust luminosity is therefore a degenerate quantity that does not alone provide great insight into the nature of a galaxy. Normalizing the dust luminosity by the dust mass, however, does provide a means of breaking this degeneracy. This ratio characterizes the radiative efficiency of a galaxy, with smaller \(L_{\text{dust}}/M_{\text{gas}}\) ratios indicating lower efficiencies and cooler dust temperatures and larger ratios indicating higher efficiencies and warmer dust temperatures.

Also included in Table 10 are the ratios of the extinction-corrected \(S\) and \(AGN\) source component luminosities to the total nuclear dust luminosity. A ratio of unity or greater in these quantities indicates that the total observed dust emission could be heated by the fitted source component. A ratio significantly greater than unity indicates that either the source extinction correction was overpredicted or the dust covering fraction is less than unity. In the latter case, the fraction of the source that is covered by dust is obtained from the inverse of the source-to-dust ratio. A ratio significantly less than unity indicates that either the extinction to the source component is underpredicted or additional unmodeled source emission is present that has not been accounted for in the decomposition (e.g., the apparent near-IR luminosity of a deeply embedded source may be small in comparison to a relatively unextinguished source, even though the two may be intrinsically similar in strength). In addition to the source-to-dust luminosity ratios, we also calculate source-to-dust mass ratios, where the extinction-corrected \(S\) and \(AGN\) luminosities are given as a fraction of the total gas mass. This quantity indicates the relative "dustiness" (in terms of mass) of a source compared to others of the same luminosity.

### 9.3.5. PAH Feature Luminosities

The total apparent PAH luminosity of each source (integrated over all features), normalized to both the total dust luminosity and the total gas mass, is presented in Table 10. In addition, the
various values of galaxy from Table 11 after passing through screens of dust with PAH complexes to the total PAH luminosity for the mean starburst parent ratios may vary as a result of extinction from intervening its emission features (see Draine & Li 2001). In addition, the ap-

fitted ratios of the luminosities of the four primary PAH complexes (see Table 1) to the total PAH luminosity are presented in Table 11. For reference, we also provide the corresponding ratios for the mean starburst galaxy spectrum from Brandl et al. (2006), used to create our PAH template, and the median ratios for the star-forming SINGS galaxies from Smith et al. (2007). With the ex-

cept of Mrk 1014, the fitted PAH luminosity ratios of the four sources in our sample with well-detected PAH emission are fairly consistent with the values of the mean starburst and SINGS tem-
plates (see § 10.1 for more on the PAH emission of Mrk 1014).

The apparent ratios of PAH emission from a galaxy may differ from those of the low-obscuration templates in Table 11 for sev-

eral reasons. First, the size of a PAH (i.e., the number of carbon atoms) and its ionization state can alter the relative strengths of its emission features (see Draine & Li 2001). In addition, the ap-

parent ratios may vary as a result of extinction from intervening dust. In Table 12 we present the ratios of the 6.2, 7.7, and 11.3 μm PAH complexes to the total PAH luminosity for the mean starburst galaxy from Table 11 after passing through screens of dust with various values of $\tau_{0.7}$. In addition to the feature ratios, we also provide correction factors used to convert the total apparent PAH luminosity into the actual emitted PAH luminosity for a partic-

ular value of $\tau_{0.7}$ estimated from the feature ratios.

10. DISCUSSION

10.1. Detailed Descriptions of Decompositions

NGC 7714.—Our low-obscuration template starburst is a mas-

sive barred spiral galaxy that makes up the western component of the interacting system Arp 284. The compact ultraviolet-luminous starburst nucleus of NGC 7714 has very low extinction, and there is no evidence at any wavelength for the presence of an AGN. The IRS spectrum of this galaxy (see Brandl et al. 2004) exhibits a rising continuum, strong PAH feature and line emission, and no perceivable 9.7 μm silicate absorption. As suggested by the rela-

tively flat continuum near 10 μm, all parameters from our fitting are consistent with this starburst galaxy being relatively unobscured at all wavelengths. The warm dust and SB source components have fitted values of $\tau_{0.7} \approx 0.19$ and $\tau_{8.6} \approx 0.97$, respectively. Puxley & Brand (1994) estimate a screen extinction to the ionized gas within NGC 7714 of $A_V \approx 0.86 \pm 0.13$ using optical and near-IR recombination lines, a value that is entirely consistent with our SB component optical depth. For our adopted dust model, $A_V \approx 0.86$ corresponds to $\tau_{0.7} \approx 0.07$–0.22, depending on the influence of scattering in the total effective opacity (the latter value is for zero scattering contribution, as expected for spherical symmetry). This range is again completely consistent with the extinction we find for the warm dust component.

The extinction-corrected SB-to-dust ratio given in Table 10 is $L_{\text{SB}}/L_{\text{dust}} = 0.91$, indicating that the fitted source component is capable of powering nearly all (i.e., 91%) of the total dust emit-

tion. Although we attempt to calculate the true far-IR dust luminosity of the nuclear point source, we may nonetheless overestimate this quantity since our MIPS photometry may still contain flux from outside the nucleus. Such an overestimate could give rise to the fitted slight source-luminosity deficit (i.e., there is not enough source emission to explain the observed dust emission). Given this possible explanation and the fact that the deficit is small (<10%), we conclude that the observed source-to-dust ratio of NGC 7714 is consistent with the total system being powered by star formation.

Our decomposition of this galaxy therefore indicates that the warmest dust in pure low-obscuration starbursts typically has a temperature $\sim 165$ K and that emission from $\sim 1000$ K dust is therefore negligible. Also, the observed PAH luminosity in NGC 7714 is $\sim 5.2\%$ of its total nuclear dust luminosity, providing an estimate of the typical total PAH strength in low-obscuration starbursts. Smith et al. (2007) find a median PAH-to-dust luminosity ratio of $\sim 10\%$ for the “normal” (i.e., nonstarburst) star-

forming galaxies in the SINGS sample, with the ratio ranging between 3.2% and 16% for the sample. Thus, the ratio measured for NGC 7714 is consistent with this range, with the nearly fac-

tor of 2 difference from the median value likely indicating real differences in the emission from galaxies with different levels of star formation. Note also that the PAH ratio $L_{11.3}/L_{7.7} \approx 0.28$ for NGC 7714 is very similar to the value of this ratio for the unobscured mean starburst template ($\sim 0.27$). The PAH emission in NGC 7714 therefore appears to be relatively unobscured, consistent with the results from other extinction indicators.

The total global dust emission in our sample (i.e., obtained using IRAS and ISO far-IR data) ranges from $\sim 1.0$ to 1.4 times

| Galaxy          | $L_{6.2}/L_{\text{PAH}}$ | $L_{7.7}/L_{\text{PAH}}$ | $L_{11.3}/L_{\text{PAH}}$ | $L_7/L_{\text{PAH}}$ |
|-----------------|--------------------------|--------------------------|---------------------------|---------------------|
| NGC 7714        | 0.114 ± 0.002            | 0.396 ± 0.004            | 0.114 ± 0.002             | 0.067 ± 0.004       |
| NGC 2623        | 0.088 ± 0.002            | 0.407 ± 0.005            | 0.074 ± 0.001             | 0.026 ± 0.002       |
| PG 0804+761     |                          |                          |                           |                     |
| Mk 463          |                          |                          |                           |                     |
| NGC 6240        | 0.115 ± 0.005            | 0.371 ± 0.009            | 0.105 ± 0.002             | 0.069 ± 0.004       |
| Mrk 1014        | 0.112 ± 0.013            | 0.211 ± 0.014            | 0.067 ± 0.008             | 0.051 ± 0.016       |
| Mean starburst  | 0.10                     | 0.39                     | 0.11                      | 0.08                |
| Median SINGS    | 0.11                     | 0.42                     | 0.12                      | 0.06                |

Notes.—Ratios of the luminosities of each of the four main PAH complexes to the total PAH luminosity. Formal statistical uncertainties for the fitted properties are given along with their values. Also shown are the ratios for the mean star-

burst galaxy spectrum used to derive our PAH template (see Table 1) and the median values for the SINGS sample of star-

forming galaxies presented in Smith et al. (2007).
the nuclear emission (i.e., obtained using MIPS data). Laçon et al. (2001) estimate that only 10%–50% of the stellar emission in NGC 7714 emerges from the $2'' \times 2''$ ($\approx 0.37$ pc$^2$) nucleus and therefore infer that 50%–90% of the far-IR *IRAS* emission likely emerges from the extended disk of the galaxy. They further reason that the strength of the extranuclear far-IR emission is likely to be toward the lower end of this range, since the ultraviolet observations used to quantify the stellar emission strength are prone to missing emission from extinguished populations. In comparing the results of our global and nuclear spectral decompositions of NGC 7714, we calculate that at least $\approx 50\%$ of the cold dust component luminosity (and $30\%$ of the total dust emission) emerges from extended regions, consistent with the Laçon et al. (2001) prediction.

NGC 2623.— Our extinguished template starburst galaxy is a late-stage merger with long tidal tails and an $1''$ nuclear stellar light profile (Wright et al. 1990; Scoville et al. 2000). The radio continuum (Condon et al. 1991) and mid-IR (Soifer et al. 2001) emission is similarly dominated by a compact nuclear source. The IRS spectrum of NGC 2623 is dominated by deep silicate absorption features at 9.7 and 18 $\mu$m and a very steep continuum beyond 20 $\mu$m. The fitted optical depths to the warm dust and SB source components of NGC 2623 are $\tau_9 = 3.5$ and $\tau_{18} = 4.8$, respectively. Note that Brandl et al. (2006) find an apparent 9.7 $\mu$m optical depth of $\approx 1.5$, which is more than a factor of 2 lower than our fitted value. This difference occurs as a result of the method they employ to determine the apparent optical depth, namely, interpolating a smooth continuum above the silicate absorption feature and using the ratio of this “unextinguished” continuum to the observed value to infer $\tau_9$. In contrast, the unextinguished continuum in the dust model used in our decomposition method is not smooth at 9.7 $\mu$m, but instead features a silicate emission feature (the presence of which is consistent with observations; see, e.g., the fit for PG 0804+761), therefore requiring a higher optical depth to obtain the same extinguished continuum.

We find no evidence for the presence of an AGN contribution to the SED of NGC 2623, consistent with the similar conclusion in Risaliti et al. (2000) based on hard X-ray observations. The extinction-corrected SB-to-dust ratio given in Table 10 is $L_{SB}/L_{dust} = 0.88$, indicating that the fitted source component is capable of powering most of the total dust emission. As with NGC 7714, it is likely that this ratio is indicative of an entirely star formation–powered system (taking into account the likely small overprediction of the nuclear dust luminosity due to the MIPS resolution). Like NGC 7714, the mid-IR spectrum of NGC 2623 also exhibits significant emission from PAHs, albeit a factor of $\approx 2.5$ weaker. The PAH ratio $L_{11.3}/L_{7.7} \approx 0.18$ for NGC 2623 is also lower than the value for NGC 7714, with the lower ratio being consistent with PAH emission obscured by a screen of dust with $\tau_9 = 1$ (as determined by comparison with the obscured mean starburst template properties in Table 12). For this optical depth, the apparent PAH luminosity of the mean starburst template is only $\approx 71\%$ of its emitted value. Using this correction factor, we estimate that the true PAH-to-dust luminosity ratio of NGC 2623 is $L_{PAH}/L_{dust} \approx 0.029$, a factor of $\approx 1.8$ lower than NGC 7714. See § 10.2 for a detailed comparison of the properties of the low-obscuration system NGC 7714 and the obscured starburst NGC 2623.

PG 0804+761.— Our Type 1 template AGN is a variable source displaying $\approx 40\%$ near-IR and 10.6 $\mu$m brightness fluctuations over the course of a decade (Neugebauer & Matthews 1999). The first deep infrared observations of this source were obtained with *ISO* (Haas et al. 2003), which revealed a power-law spectral shape and a very warm infrared continuum peaking at $\approx 30 \mu$m. Analysis of its IRS spectrum by Hao et al. (2005b) revealed the presence of strong 9.7 and 18 $\mu$m amorphous silicate emission features. In our decomposition, these emission features are produced by grains in the warm dust component. If we assume that the warm component is directly illuminated by the PG 0804+761 accretion disk ($L_{AGN} = 1.26 \times 10^{12} L_{\odot}$), then equation (12) with $\mu c \rho \rightarrow L_{\nu}/4\pi \nu^2$ indicates that this dust is located $\approx 19$ pc from the nucleus. Jaffe et al. (2004) analyze 10 $\mu$m VLTI interferometric observations of the nucleus of the nearby Type 2 AGN NGC 1068 and conclude that its torus emission must be confined to a region $\lesssim 2$ pc in size. Thus, some of the optically thin warm component emission from PG 0804+761 may emerge from regions beyond the torus, perhaps from clouds in the narrow-line region. Note that this distance to the warm dust is actually an upper limit to the true distance, since the emission may also originate from indirectly illuminated torus clouds (see Fig. 6) at $r < 19$ pc.

The unextinguished AGN-to-dust ratio in the PG 0804+761 decomposition is $\approx 2$ (see Table 10), indicating that the AGN source component is more than capable of heating the total observed dust emission. The inverse of this ratio provides an estimate of the total dust covering factor (i.e., the fraction of sky covered by the torus as seen from the nucleus), which is $f_{\text{torus}} \approx 0.5$ (note that this value is at the constraint imposed during the fit; see § 9.2). This covering factor is consistent with a torus opening angle of $\approx 30^\circ$ (i.e., $\sin \theta_{\text{torus}} = f_{\text{torus}}$, where $\theta_{\text{torus}}$ is the angle extending from the midplane to the top of the torus as viewed from the accretion disk). Based on the statistics of Seyfert galaxies (i.e., the relative numbers of Type 1 and 2 galaxies), Schmitt et al. (2001) find approximately twice as many Type 2 AGNs and hence estimate $\theta_{\text{torus}} = 45^\circ$. More recently, Hao et al. (2005a) study the AGNs in the Sloan Digital Sky Survey and conclude that $\theta_{\text{torus}} \approx 30^\circ$, consistent with the value obtained from our decomposition.

Jaffe et al. (2004) find that the 8–13 $\mu$m VLTI spectrum of NGC 1068 can be decomposed into a $T > 800$ K dust component (then $r_{\text{torus}} = 2.1 \pm 0.5$ screen and a $T = 320 \pm 30$ K component behind a $r_{\text{torus}} = 0.3 \pm 0.2$ screen. The temperatures and screen optical depths of these components are comparable to those obtained in our spectral decomposition (see also the properties of Mrk 463). PG 0804+761 has the worst reduced $\chi^2$ of the galaxies in our sample, due primarily to the poor fit to its IRS spectrum between 7.5 and 10 $\mu$m (although the fit to the rest of the SED is quite good).

Jaffe et al. (2004) report a similar problem in this wavelength range in their fit to the spectrum of NGC 1068 and conclude that the fit is improved using high-temperature calcium aluminum silicate dust instead of the standard olivine-type silicates (the opacity of the 9.7 $\mu$m feature of the former species begins near 9 $\mu$m as opposed to the $\approx 8 \mu$m onset for olivine). We finally note that our decomposition of the ultraviolet and optical emission is consistent with a largely uncovered AGN accretion disk (with only $\approx 25\%$ covered) consistent with a Type 1 source.

Mrk 463.— Our Type 2 template AGN is a merging system with two nuclei separated by $\approx 4''$ (Mazzarella et al. 1991). The portion of the IRS spectrum obtained with the short-low module is likely dominated by Mrk 463e (since the slit of this module is only $\approx 3.6''$ wide and the observation targeted the eastern component), while the portion obtained with the wider slit of the long-low module likely contains emission from both nuclei (although the optically bright western component may not contribute significantly at these wavelengths). Mrk 463 has a luminous steep-spectrum radio core, and bright lines are seen in scattered optical (Miller & Goodrich 1990) and direct near-IR light (Goodrich et al. 1994; Veilleux et al. 1997). Like the quasar PG 0804+761, the mid-IR spectrum of this galaxy shows no discernible PAH emission features (Armus et al. 2004). Silicate absorption at 9.7 $\mu$m is
clearly seen in the spectrum of Mrk 463, producing a mid-IR continuum dominated by a broad emission feature at ~8 μm, characteristic of self-absorbed silicate dust. In our decomposition, this feature is primarily produced by the warm component, which has a screen optical depth τ_s ~ 1.3. Unlike the quasar PG 0804+761, Mrk 463 has a moderately obscured (τ_s ~ 2.1) hot dust component. The warm component optical depth and the deviations of the fit to the IRS spectrum from 7.5 to 9 μm are both similar to the reported properties of PG 0804+761 and NGC 1068 described above. Unlike the fit to the quasar PG 0804+761, the AGN component of Mrk 463 is completely covered by obscuring clouds (i.e., f_{AGN} = 1) as is expected for a Type 2 source.

The AGN-to-dust ratio for Mrk 463 is 1.93 (similar to the value for PG 0804+761), consistent with the AGN source component powering the total observed dust emission, and implying a torus opening angle θ_{torus} ~ 31°. There is evidence for ISRF and SB contributions in the decomposition, although these are bolometrically weak compared to the power of the AGN (~5%). Although Mrk 463 and PG 0804+761 have similar AGN-to-dust ratios, they have very different quantities of cooler dust. Mrk 463 has 16 times more cold dust by mass (see Table 8), and it also has a 14 times smaller dust luminosity-to-mass ratio (also indicative of cooler mean dust temperatures; see Table 10). Similarly, the ratio of the unextinguished AGN component luminosity to the total gas mass is 14 times smaller for Mrk 463 (i.e., it has 14 times more gas mass for the same accretion disk luminosity). In the standard AGN unification scenario, the only difference between a Type 1 source (such as PG 0804+761) and a Type 2 source (such as Mrk 463) is the orientation of the obscuring torus with respect to the observer. Thus, within this picture, Type 1 and Type 2 AGNs should have similar cold dust masses relative to their total masses, and they should therefore have similar AGN luminosity-to-mass ratios (since the accretion disk luminosity and the total mass of dust do not depend on orientation). In § 10.4 we suggest that the relative orientations of the accretion and host galaxy disks may explain why this simple consequence of the unification scenario does not hold for some galaxies. We therefore emphasize that the SEDs of individual AGNs may appear falsely inconsistent with the unification scenario due to local geometrical factors, even if unification holds for AGNs as a class.

**NGC 6240.**—The first of our two composite sources is an interacting system containing two nuclei separated by ~1” (so that both nuclei are contained within all IRS slits). With an L_{IR} ~ 6.5 × 10^{11} L_☉, NGC 6240 is technically a LINIR, although it is often treated as a ULIRG since it shares most properties with other members of the class. Based on its optical nuclear spectrum, NGC 6240 is classified as a LINER (Armus et al. 1989), and X-ray observations (Komossa et al. 2003) provide clear evidence for the presence of a pair of AGNs located behind significant columns of absorbing neutral gas [N_H = (1–2) × 10^{24} cm^{-2}]. The mid-IR spectrum of NGC 6240 is extremely rich, displaying strong PAH features, both low- and high-ionization lines (e.g., [Ne v] 12.8 μm and [Ne v] 14.3 μm), and strong emission from molecular hydrogen (see Armus et al. 2006). Like NGC 2623, the mid-IR continuum of this galaxy is shaped by strong absorption from silicate grains at 9.7 and 18 μm, as indicated by the warm component screen optical depth of τ_s ~ 3.6. The near-IR continuum of NGC 6240 is well fitted by a combination of apparently unobscured weak hot dust and extinguished (τ_v ~ 4.7) SB component emission. The detection of [Ne v] 14.3 μm in the high-resolution IRS spectrum of NGC 6240 presented in Armus et al. (2006) and the evidence for X-rays are both consistent with the presence of hot dust in our decomposition, indicating that a (perhaps small) fraction of the near-IR emission is powered by an AGN.

Based on Chandra X-ray observations, Lira et al. (2002) conclude that the AGN in NGC 6240 likely contributes between 30% and 50% of the bolometric luminosity. However, as reported in Armus et al. (2006), the small [Ne v]/[Ne ii] and [Ne v]/IR flux ratios are both consistent with an AGN contribution of only 3%–5% of the bolometric luminosity. Similarly, the apparent hot dust emission in our decomposition makes up just ~2% of the total dust luminosity (compared to >30% and 30% for PG 0804+761 and Mrk 463, respectively), so that any contribution to the observed near- and mid-IR from an AGN is very small. On the other hand, the SB-to-dust ratio for NGC 6240 is 1.43, indicating that the total observed dust emission could be powered by the observed SB component. This galaxy therefore presents quite a puzzle, whereby its appearance changes radically depending on where you look: although X-rays suggest powerful AGNs, data at optical and longer wavelengths do not require such a presence. We note that even though the hot component in the decomposition is unobscured, it could still be associated with a deeply obscured AGN in a clumpy geometry where most of the hot dust is too obscured to be seen, and we view only the most unobscured portions (see § 10.3). If this scenario is true, the actual hot dust contribution to the total bolometric luminosity could easily be pushed higher.

**Mrk 1014.**—Our second composite source is a radio-quiet infrared-luminous QSO with broad optical emission lines (FWHM Hβ > 4000 km s^{-1}). Mrk 1014 displays twin tidal tails, indicative of a recent interaction and merger (MacKenty & Stockton 1984). It is a relatively warm far-IR source, with the peak of its SED located around 70 μm. Its mid-IR spectrum is characterized by a nearly power-law continuum, with no obvious silicate emission or absorption features, and weak PAH emission (see Armus et al. 2004). This power-law continuum is rather remarkable (assuming that the continuum is thermal in origin) since a nearly featureless SED must be constructed from emission components that are known to have significant features (i.e., silicates). The decomposition that provides a solution to this puzzle is consistent with Mrk 1014 being a composite source, containing a combination of dust components seen in both our template starbursts and AGNs. Like the AGNs, Mrk 1014 contains a moderately obscured (τ_s ~ 2.7) hot dust component and a much less obscured warm component (τ_s ~ 0.14). Like the starbursts (and unlike the quasar), Mrk 1014 also contains bolometrically significant emission from cooler dust, comprising ~60% of its total dust luminosity (we argue in § 10.4 that some of this far-IR emission is likely powered by the AGN).

The extinction-corrected AGN-to-dust and SB-to-dust luminosity ratios of Mrk 1014 are 0.66 and 0.17, respectively, indicating that the AGN is capable of powering ~66% of the observed dust emission from the galaxy. As fitted, the AGN and SB components are together capable of powering 83% of the observed dust emission, thereby requiring the presence of at least an additional 17% source luminosity to power the remaining dust emission (note also that the total nuclear dust luminosity from Mrk 1014 is uncertain by ~20% since no MIPS data are available to constrain its far-IR SED). If all of this undetected source luminosity emerges from the AGN accretion disk (e.g., if we underpredict the AGN component luminosity as a result of too rigid a constraint on the hot-to-AGN luminosity ratio), the AGN would account for 83% of the bolometric luminosity of Mrk 1014. If, on the other hand, the remaining undetected source luminosity is entirely produced by a starburst (e.g., if we underpredict the SB component luminosity as a result of missing emission from highly embedded regions), then the AGN would account for 66% of the bolometric luminosity.
Armus et al. (2007) create diagnostic diagrams based on mid-IR spectral lines (see their Figs. 5–8) that are all consistent with an AGN fraction between 50% and 90% for Mrk 1014. In addition, Boller et al. (2002) conclude that Mrk 1014 is dominated by an AGN and not star formation based on X-ray observations. If we take the PAHs-to-dust luminosity fractions of the galaxies NGC 2623 and NGC 6240 to be representative of the range of values in obscured starbursts, then the PAHs-to-dust ratio of Mrk 1014 suggests that between ~38% and 57% of its bolometric luminosity is powered by obscured star formation (assuming that all PAH emission comes from star formation). Given our conclusion above that the starburst contribution is between 17% and 34%, it is therefore likely either that we are underestimating the total starburst contribution based on the source components (which seems improbable given the corroborating X-ray and emission-line evidence) or that some of the observed PAH emission may actually be powered by the AGN (see § 10.4). We note as well that the PAH feature luminosity ratios for Mrk 1014 (see Table 11), in particular the 7.7 μm complex, differ significantly from the template starbursts, perhaps indicative of an AGN contribution giving rise to nonstandard PAH emission.

10.2. Comparison of Starburst SEDs

From our modest sample of two starburst galaxy decompositions, it is apparent that starburst SEDs do not form a homogeneous group. Comparing the fits of NGC 2623 and NGC 7714, noticeable differences include a 30% higher maximum dust temperature, a 20 times higher maximum optical depth, a 2.5 times weaker PAHs-to-dust luminosity ratio, and comparatively weaker [Ne ii] 15.56 μm, [S iii] 18.71 μm, [S ii] 33.48 μm, and [Si ii] 34.82 μm line emission. If the nuclear emission from each starburst emerges from distinct star-forming clouds consisting of embedded stars surrounded by cocoons of dust (see Fig. 1), then many of the observed variations in the SEDs of NGC 7714 and NGC 2623 can be understood as resulting from (1) differences in the total number of star-forming clouds (i.e., if individual cloud complexes in each galaxy have similar intrinsic luminosities, then the total luminosity of each galaxy is determined by the total number of clouds it contains) and (2) the mean optical depth through an individual cloud. There are, of course, many other factors shaping the SEDs of starbursts as well, e.g., age and metallicity. The simple model described in this section is therefore not intended to provide a comprehensive explanation of all starburst properties, but rather a structure within which to understand several general properties.

If we assume for simplicity that each cloud in a starburst has constant gas density, then the optical depth through a cloud is \( \tau(r) = \tau_{\text{cloud}}(r/r_{\text{cloud}}) \), where \( \tau_{\text{cloud}} \) and \( r_{\text{cloud}} \) are the total optical depth and radius of the cloud, respectively. As described in § 5.1, direct emission from stars heats a shell of dust out to a radius \( r_{\text{shell}} \), corresponding to the optical depth \( \tau_{\text{shell}} \), where the cloud becomes optically thick to the heating stellar photons (i.e., essentially the outer edge of the photodissociation region). Using the equation for the optical depth above, we obtain \( \tau_{\text{shell}}(r) = \tau_{\text{cloud}}(r/r_{\text{cloud}}) \). Here we assume that \( \tau_{\text{shell}} \) is the same for all clouds since it depends only on the properties of dust and the illuminating radiation field. With \( \tau_{\text{shell}} \rightarrow \tau_{\text{warm}} \) (i.e., using the warm component optical depth as a proxy for the total cloud optical depth), this gives \( r_{\text{shell}}(r) = \frac{r_{\text{cloud}}}{\tau_{\text{shell}}} \). If the clouds in each galaxy are similar in size, this suggests that \( r_{\text{shell}}(r) < 1 \) (i.e., the warm dust shell from Fig. 6 is geometrically more extended in NGC 7714 than NGC 2623), so that stellar photons penetrate to much larger radii in the star-forming clouds of NGC 7714. Furthermore, the fractional cloud volume containing dust at the temperature of the warm component should be smaller in NGC 2623 than NGC 7714, and consequently the mass of warm dust relative to the total mass should be smaller as well. Indeed, from Table 8 we find that \( (M_{\text{warm}}/M_{\text{dust}})_{2623} \approx 1.3 \times 10^{-4} \) and \( (M_{\text{warm}}/M_{\text{dust}})_{7714} \approx 4 \times 10^{-3} \), consistent with this prediction.

For \( r < r_{\text{shell}} \), energy conservation dictates that the temperatures of grains within a cloud scale roughly as \( T \propto r^{-1/2} \). This, coupled with the fact that \( r_{\text{shell}} < r_{\text{cloud}} \), implies that the mean temperature of such grains should be higher in NGC 2623 than NGC 7714, a prediction that is consistent with its 25% higher warm component temperature. The luminosities per unit mass of dust at the temperatures of the two galaxies scale approximately as \( \left( T_{2623}/T_{7714}\right)^{3} \approx (1.25)^{3} = 2.4 \) (i.e., a mass of warm dust from NGC 2623 will be \( \sim 2.4 \) times more luminous than an equivalent mass from NGC 7714). This ratio, along with the absolute warm component dust masses for the two galaxies, suggests that the ratio of the warm component luminosities should be \( L_{\text{warm}}(\text{NGC 2623})/L_{\text{warm}}(\text{NGC 7714}) \approx 4 \). The actual fitted ratio is 4.7, in reasonable agreement with this prediction. Furthermore, the \( L_{\text{dust}}/L_{\text{H}} \) ratio from Table 10 is ~30% higher in NGC 2623 than in NGC 7714. If the warm dust in NGC 7714 were at the temperature of the warm dust in NGC 2623, the total luminosity of NGC 7714 would increase by ~40%, and the resulting dust luminosity-to-mass ratios of the two sources would differ by only ~7%. Thus, the different values of \( L_{\text{dust}}/L_{\text{H}} \) for the two galaxies scale approximately as (\( \bar{M}_{\text{warm}}/\bar{M}_{\text{dust}} \))0.77, where the cloud-to-dust luminosity ratios of the two galaxies differ by only ~10%. Given that both our template starbursts are believed to be entirely powered by star formation, it is clear that there is...
significant variation in the relative strength of PAH emission in pure starbursts. We therefore caution that great care must be taken when using any of these metrics to derive absolute quantities of star formation, since both extinction and geometrical effects may result in different ratios for pure starburst galaxies.

10.3. Hot Dust Emission from Clumpy AGN Tori

If the obscuring dust surrounding an AGN accretion disk is arranged in a smooth (i.e., nonclumpy) toroidal distribution, then the \( \sim 3-8 \mu m \) SEDs of Type 1 sources should be dominated by emission from relatively unobscured hot dust (since this hot dust is viewed directly by the observer, with no intervening material from the torus along the line of sight to obscure it). If, however, the obscuring structure is instead composed of discrete clouds distributed in a roughly toroidal shape (i.e., a clumpy torus), then hot dust emission is not expected to emerge unobscured. As illustrated in Figure 11, the directly illuminated (and therefore hotter) faces of clouds in a clumpy torus always point radially toward the nucleus, and therefore away from the observer. Thus, emission from these hot cloud faces, and therefore hot component emission from such sources, is obscured by cooler dust on the shaded sides of clouds. Our decomposition of the quasar PG 0804+761 includes a moderately obscured (\( \tau_\gamma \approx 1.2 \)) hot dust component, consistent with such a clumpy obscuring torus.

The SED of the hot dust component from the PG 0804+761 decomposition is shown in the bottom right panel of Figure 11. Also shown is a curve representing emission from dust at the temperature of the PG 0804+761 hot component, with 75% obscured by a \( \tau_\gamma = 25 \) screen (i.e., equivalent to the screen obscuring the AGN component), and the remaining 25% emerging unobscured. While this model with nonuniform coverage does not exactly reproduce the SED from the fully covered model (in particular at shorter wavelengths), it nonetheless produces a very similar spectrum that would also provide an adequate fit to the PG 0804+761 SED (with...
suitable small adjustments to the AGN and warm components). Thus, the SED of hot component emission from a highly obscured geometry with a few clear lines of sight may appear similar to the emission from a fully covered but less obscured geometry. For a traditional torus made from a smooth dust distribution, hot dust emission from a face-on source would emerge unobscured with strong silicate emission features (since there are no shaded sides of clouds to obscure the hot emission). Our decomposition of PG 0804+761 does not show such strong features from the hot component, suggesting that its hot dust, and possibly that of most Type 1 sources, may therefore be significantly obscured by the shadowed sides of clumpy torus clouds.

The bottom left panel of Figure 11 depicts the fitted NGC 6240 hot dust component SED (unobscured in the decomposition), along with a model in which 50% of its hot dust is covered by a screen with $\tau_V = 25$ and the remainder emerges unobscured. As with PG 0804+761, this partially covered model does not precisely reproduce the fitted hot dust component. It is, however, similar enough to the fitted component to provide a reasonably good fit (i.e., since the hot component of NGC 6240 contributes in a region with strong contributions from several other components, the small deviations between the two models would not affect the decomposition greatly). The near equivalence of these two models demonstrates that emission from a highly obscured, but only partially covered, geometry may appear quite similar to emission from a fully covered geometry at much lower levels of obscuration. Therefore, despite the small apparent optical depth derived from the fit to NGC 6240, it is possible that the hot component in this source is actually much more significantly obscured (i.e., we may only see direct emission from a few clear lines of sight, while the majority of the hot dust is completely obscured).

10.4. Origin of the Far-IR Emission in AGNs

Since emission from dust at far-IR ($\lambda > 50 \mu m$) wavelengths is likely to emerge unobscured from galaxies, the average properties of the far-IR SEDs of AGNs (e.g., their relative cold dust luminosities and masses) should be similar for all sources (assuming that their nuclei are similarly structured), independent of their orientation-based (i.e., Type 1 vs. Type 2) classification. As described in § 10.1, the two template AGNs in our sample have very different far-IR properties (e.g., Mrk 463 has a dust luminosity-to-mass ratio $\sim\times 15$ times that of PG 0804+761), in sharp contrast to these expectations. Farrah et al. (2003) use a two-component (starburst+AGN) template decomposition to conclude that some optically classified AGNs with strong far-IR emission likely have significant contributions from starbursts. While this is likely true for many AGNs with cool far-IR SEDs, it does not appear to hold for Mrk 463 (see § 10.1). As illustrated in Figure 12, we instead suggest that the far-IR emission from some AGNs (including Mrk 463) is powered by the AGN itself and originates from cool dust in the disk of the host galaxy. We note here that this suggestion is based on the SEDs of only two AGNs, so further study using a much larger sample (to be presented in a subsequent paper) is needed before conclusions are drawn about the origin of far-IR emission from the class of AGNs.

While it is often assumed that an AGN accretion disk and the disk of the galaxy hosting the AGN are coplanar (as in the top of Fig. 12), this geometrical assumption is not necessarily always true. After the merger of two galaxies, the resulting accretion and host galaxy disks may eventually come to rest in the same plane (e.g., due to torques), but there is a period of time after the merger during which their relative orientation is essentially random. If the two disks are tilted with respect to each other, a significant quantity of dust in the disk of the host galaxy may be heated by the

AGN out to large radial distances (see the bottom of Fig. 12). Assuming that the galaxy disk is not a significant source of opacity, a galaxy therefore appears as a Type 1 or Type 2 AGN depending on the relative orientation of the obscuring torus with respect to the observer (i.e., the standard AGN unification scenario). In addition, depending on the relative orientation of the host galaxy and AGN accretion disks (but independent of the orientation of the observer), the source may exhibit weak or strong far-IR emission (i.e., “Warm” or “Cold” far-IR SEDs as labeled in Fig. 12). In this model, Mrk 463 and PG 0804+761 are therefore “Cold” and “Warm” far-IR sources, respectively, with emission arising from geometries similar to those in the bottom and top of Figure 12, respectively. We note that the geometry suggested here has a similar impact on the SEDs of galaxies as the “warped disk” geometry from Sanders et al. (1989).

As described in § 10.1, we estimate that $\sim 35\%$ of the bolometric luminosity of Mrk 1014 is powered by star formation. If all of this luminosity emerges in the form of cool dust, this still leaves $\sim 30\%$ of its 70 K emission component to be powered by its AGN. We therefore suggest that the geometry of Mrk 1014 is likely to be similar to that of Mrk 463 (i.e., the bottom of Fig. 12). In addition, the luminosity of the Mrk 1014 PAHs component compared to its inferred starburst fraction suggests that between $\sim 20\%$ and $\sim 50\%$ of its PAH emission is powered by its AGN (i.e., derived by comparison with the properties of the obscured starbursts NGC 2623 and NGC 6240; see § 10.1). Schweitzer et al. (2006) argue against AGN-powered far-IR emission in a sample of QSOs observed with Spitzer based largely on the fact that PAHs are destroyed in a hard AGN radiation field. However, in the geometry of Figure 12, the radiation field gradually softens as the photons propagate through the galaxy disk, so that at some radius PAH molecules illuminated by the AGN may survive. Clearly, more work is required (e.g., radiative transfer calculations with realistic PAH destruction models) to verify if this scenario is indeed realistic, and we do not dispute that some far-IR emission in AGNs is powered by starbursts, but the suggested mechanism to generate far-IR and PAH emission in AGNs as a result of the interaction of the accretion disk with its host galaxy should be considered as well. Furthermore, we warn against the blanket assumption that all PAH and far-IR emission is directly associated with star formation, as this could result in an overestimation of the true level of star formation activity in galaxies.
11. SUMMARY

We have presented a new multicomponent SED decomposition method. Our principal goal for this paper is to demonstrate the effectiveness of the method for studying composite dusty galaxies, although we note that the method is quite general and may be applicable to much broader selections of galaxies. To demonstrate the efficacy of the method, we have applied it to the ultraviolet through millimeter wavelength SEDs of the nuclei of the unobscured and obscured template starbursts NGC 7714 and NGC 2623, as well as the template Type 1 and Type 2 AGNs PG 0804+761 and Mrk 463. We find that the pan-spectral SEDs of these sources are all consistent with being entirely powered by star formation and accretion, respectively. We compare the SEDs of the two starbursts galaxies and demonstrate that the differences in their properties (including the luminosities and masses of their dust components and the strength of their PAH emission) can largely be explained in terms of the different mean optical depths through the dusty cocoons surrounding their newly formed stars. In comparing the template AGNs, we find that the far-IR SEDs of the two sources differ significantly, which we suggest may result from variations in the relative orientation of their host galaxy and AGN accretion disks.

We also decompose the nuclear SEDs of the composite sources NGC 6240 and Mrk 1014. Our decomposition finds very little evidence for an AGN contribution in NGC 6240 (~2%), with the total dust emission in that galaxy being powered by a starburst with mean optical depth $\tau_T \approx 5$. We note, however, that we cannot rule out a larger contribution from a deeply embedded AGN visible only in X-rays. The SED of Mrk 1014 is consistent with a galaxy that is ~65% AGN powered, with a ~35% contribution from star formation. Like Mrk 463, we find that Mrk 1014 has a far-IR excess (compared to the Type 1 AGN PG 0804+761) and attribute this to cold dust in the disk of its host galaxy, which is heated directly by its AGN. We also estimate that up to 50% of the detected PAH emission in Mrk 1014 may be powered by radiation from the AGN that has softened as it propagates through the galaxy disk (and therefore does not destroy the fragile PAH molecules). In a future paper, we will apply this decomposition method to a much larger sample of starbursts, AGNs, LIRGs, and ULIRGs observed as part of the Spitzer GTO program in order to provide a suite of templates to aid in understanding both the local dusty galaxy population and the high-redshift LIRGs and ULIRGs now being uncovered by Spitzer.

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APPENDIX A

WEIGHTING OF NONUNIFORMLY SAMPLED DATA

The sampling term, $\lambda$, in equation (3) is required to produce sensible and fair fits of nonuniformly sampled data, as is the case when coarsely sampled photometry is joined together with spectral data. If such a term is excluded (i.e., $\lambda_k = 1$ for all $\lambda_k$), then $\chi^2$ will be dominated by the more finely sampled spectral data, simply because it contains many more data points. To establish a weighting scheme for nonuniformly sampled data, we define the quantity

$$n_{\text{IRS}} \equiv N_{\text{IRS}} / \log(\lambda_{\text{max}}^{\text{IRS}} / \lambda_{\text{min}}^{\text{IRS}}),$$

(A1)

which is the number of spectral samples per logarithmic wavelength interval in an IRS spectrum. Here $N_{\text{IRS}}$ is the total number of spectral samples in the IRS spectrum, and $\lambda_{\text{max}}^{\text{IRS}} \equiv \min(\lambda_{\text{IRS}})$ and $\lambda_{\text{max}}^{\text{IRS}} \equiv \max(\lambda_{\text{IRS}})$, where $\lambda_{\text{IRS}}$ is the array of wavelength points in the IRS spectrum. We then divide the full SED into $N_{\text{bins}}$ wavelength bins (typically 10), distributed in even logarithmic wavelength intervals, with each bin $l \in [0, 1, \ldots, N_{\text{bins}} - 1]$ containing minimum and maximum wavelengths

$$\lambda_{\text{min}}^l \equiv \min(\lambda_l) = \lambda_{\text{min}}(\frac{\lambda_{\text{max}}^l}{\lambda_{\text{min}}})^{l/N_{\text{bins}}}, \quad \lambda_{\text{max}}^l \equiv \max(\lambda_l) = \lambda_{\text{min}}(\frac{\lambda_{\text{max}}}{\lambda_{\text{min}}})^{(l+1)/N_{\text{bins}}},$$

(A2)

where $\lambda_{\text{min}} \equiv \min(\lambda)$ and $\lambda_{\text{max}} \equiv \max(\lambda)$ are the minimum and maximum wavelength in the SED having wavelength array $\lambda$. Each bin is then assigned a total weight based on the sampling of the IRS spectrum

$$\lambda_{\text{bins}}^l = n_{\text{IRS}} \log \left( \frac{\lambda_{\text{max}}^l}{\lambda_{\text{min}}^l} \right) = \frac{N_{\text{IRS}}}{N_{\text{bins}}} \log \left( \frac{\lambda_{\text{max}}^{\text{IRS}}}{\lambda_{\text{min}}^{\text{IRS}}} \right),$$

(A3)

The weight of bins containing no data points is redistributed to the nearest bins containing data above and below, with the weight going to each bin being a linear function of the proximity to the bin with no data; i.e., for a bin $l'$ containing no data, the weight distributed to the bins $l''$ and $l'''$ above and below is

$$\delta \lambda_{\text{bins}}^{l'' - l'} = \lambda_{\text{bins}}^{l''} \frac{l'' - l'}{l'' - l'}, \quad \delta \lambda_{\text{bins}}^{l''' - l''} = \lambda_{\text{bins}}^{l'''} \frac{l''' - l''}{l''' - l''}.$$  

(A4)
The weighting in each bin is then distributed to the data points within that bin, so that for a data point at wavelength $k$ that is in bin $l$, 
\[ \Lambda_k \in l = \frac{\Lambda_{l \text{ bins}}}{N_l}, \]  
(A5)
where $N_l$ is the number of data points in bin $l$. Thus, the $\Lambda_k$ represent the number of effective spectral samples that each data point represents so that the sampling over the entire SED is equivalent to the IRS sampling. Finally, we normalize and scale the weighting function 
\[ \hat{\Lambda}_k = N_{\text{tot}} \frac{\Lambda_k}{\sum k \Lambda_k}, \]  
(A6)
so that $\sum_k \hat{\Lambda}_k = N_{\text{tot}} = N_{\text{phot}} + N_{\text{IRS}}$, the total number of data points in the spectral energy distribution, as would be the case if the weighting function were taken to be unity at all wavelengths (i.e., $\hat{\Lambda}_k = 1$ for all $\hat{\lambda}_k$).

**APPENDIX B**

**IRS STATISTICAL FLUX DENSITY UNCERTAINTIES**

We derive the statistical flux density uncertainty at each wavelength element of an IRS spectrum by differencing two spectra obtained at different nod positions of each slit. The initial estimate of the uncertainty at each wavelength is 
\[ \delta f_k = \frac{f_1(\hat{\lambda}_k) - f_2(\hat{\lambda}_k)}{(\sqrt{2})^2}, \]  
(B1)
where $f_1$ and $f_2$ are the observed flux densities in nod positions 1 and 2, and the two factors of $\sqrt{2}$ both correct for the introduction of noise resulting from the subtraction and account for the reduction in noise of the final flux densities resulting from averaging the two nods. At each wavelength, this array contains a single sample of the true uncertainty drawn from the probability distribution function having standard deviation $\sigma(\hat{\lambda}_k)$. We estimate the true value of the statistical uncertainty at each wavelength by calculating the standard deviation of the points in a window of width $W$ (typically around 20 wavelength bins, with the window size decreasing near the edges of the spectrum) and assigning this value as the standard deviation of the central wavelength, i.e., 
\[ \sigma^2(\hat{\lambda}_k) = \frac{1}{W + 1} \sum_{i=k-W/2}^{k+W/2} (\delta f_i - \langle \delta f \rangle)^2, \]  
(B2)
where $\langle \delta f \rangle \approx 0$ is the mean value of $\delta f$ for the points within the window. Since we are approximating a function that in principle should be sampled on an infinitely fine grid, our estimated $\sigma$ array will always show some residuals from our finite grid size. As a result, the $\sigma$ array does not always have the expected property that $\sim 68\%$ of the $\delta f_k$ are enveloped by the $1 \sigma$ contour. We therefore perform one final step, smoothing our estimated $\sigma$ array with a window of width $W$ and scaling the entire array until it has the expected behavior that the $1 \sigma$ error contour envelops $68\%$ of the $\delta f_k$.

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