Mass accretion to young stars triggered by flaring activity in circumstellar discs

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ABSTRACT

Young low-mass stars are characterized by ejection of collimated outflows and by circumstellar discs which they interact with through accretion of mass. The accretion builds up the star to its final mass and is also believed to power the mass outflows, which may in turn remove the excess angular momentum from the star-disc system. However, although the process of mass accretion is a critical aspect of star formation, some of its mechanisms are still to be fully understood. A point not considered to date and relevant for the accretion process is the evidence of very energetic and frequent flaring events in these stars. Flares may easily perturb the stability of the discs, thus influencing the transport of mass and angular momentum. Here we report on 3D magnetohydrodynamic modelling of the evolution of a flare with an idealized non-equilibrium initial condition occurring near the disc around a rotating magnetized star. The model takes into account the stellar magnetic field, the gravitational force, the viscosity of the disc, the magnetic-field-oriented thermal conduction (including the effects of heat flux saturation), the radiative losses from optically thin plasma and the coronal heating. We show that, during its first stage of evolution, the flare gives rise to a hot magnetic loop linking the disc to the star. The disc is strongly perturbed by the flare: disc material evaporates under the effect of the thermal conduction and an overpressure wave propagates through the disc. When the overpressure reaches the opposite side of the disc, a funnel flow starts to develop there, accreting substantial disc material on to the young star from the side of the disc opposite to the flare.

Key words: accretion, accretion discs – MHD – circumstellar matter – stars: flare – stars: pre-main-sequence – X-rays: stars.

1 INTRODUCTION

Classical T Tauri stars (CTTSs) are young low-mass stars actively accreting mass from a surrounding disc (Hartmann 1998; Bouvier & Appenzeller 2007). On the basis of the largely accepted magnetospheric accretion scenario (Koenigl 1991), the accretion process from the disc is regulated by the stellar magnetic field which is strong enough to disrupt the inner part of the disc at a distance of a few stellar radii (the truncation radius) where the magnetic pressure is approximately equal to the total gas pressure. The field guides the circumstellar material along its flux tubes towards the central protostar, around free-fall velocity, terminating in a shock at the photosphere. This scenario is supported by much observational evidence, among others, the photospheric magnetic field of a few kG that has been detected in a number of CTTSs by exploiting the Zeeman effect (Johns-Krull et al. 1999).

One of the fundamental issues in the magnetospheric accretion scenario is the mechanism of inward transport of matter and outward transport of angular momentum needed to explain the final mass and angular momentum of mature stars. The turbulence in the disc has been proposed to be the main mechanism responsible for the required outward angular momentum transport, thus controlling the mass accretion on the central star (Shakura & Sunyaev 1973). Nowadays, there is a large consensus in the literature that the turbulence is mainly driven by the magnetorotational instability (MRI; Balbus & Hawley 1991, 1998). MRI operates in regions where the ionization is sufficient to couple the gas to the magnetic field and leads to the transfer of angular momentum along the magnetic field lines connecting gas located in different orbits (Brandenburg et al. 1995; Hawley, Gammie & Balbus 1995; Armitage 1998; Hawley 2000; Hirose, Krolik & Stone 2006). Despite the significant

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theoretical progress achieved in this field, the details of this transport mechanism have yet to be fully understood, and it is not clear if MRI alone is able to account for the mass accretion and for the removal of excess angular momentum (Fromang & Papaloizou 2007; King, Pringle & Livio 2007; Bodo et al. 2008). Given the complexity of this mechanism and our poor knowledge of its details, the efficiency of angular momentum transport within the disc is often modelled in the literature by including a viscosity in the disc modulated via an analogue of the Shakura–Sunyaev α-parameter (Shakura & Sunyaev 1973) which can be expressed in terms of the fluctuating velocity and magnetic field (Romanova et al. 2002, 2003; Kulkarni & Romanova 2008).

On the other hand, observations in the X-ray band have shown that pre-main-sequence stars are strong sources with X-ray luminosity 3–4 orders of magnitude greater than that of the present-day Sun (Getman et al. 2005; Audard et al. 2007). The source of this X-ray radiation is a plasma at 1–100 MK in the stellar outer atmospheres (corona), heated by magnetic activity analogous to the solar one but much stronger (Feigelson & Montmerle 1999). X-ray flares are violent manifestations of this magnetic activity and are triggered by an impulsive energy input from coronal magnetic field. X-ray observations in the last decades have shown that flares in CTTSs have amplitudes larger than solar analogues and occur much more frequently (Favata et al. 2005; Getman et al. 2005; Audard et al. 2007; Aarnio, Stassun & Matt 2010). Examples of these flares are those collected by the Chandra satellite in the Orion star-formation region (COUP enterprise; Favata et al. 2005). The analysis of these flares revealed that they have peak temperatures often in excess of 100 MK, are long-lasting, and are confined in very long magnetic structures – extending for several stellar radii – which may connect the star’s photosphere with the accretion disc (structures that could be of the same kind as those which channel the plasma in the magnetospheric accretion).

At the present time, it is unclear where these flares occur. The differential rotation of the disc together with the interaction of the disc with the magnetosphere may cause magnetic reconnection close to the disc’s surface, triggering large-scale flares there. In this case, the flares may perturb the stability of the circumstellar disc causing, in particular, a strong local overpressure. The pressure gradient force might be able to push disc’s matter out of the equatorial plane into funnel streams, thus providing a mechanism to drive mass accretion that differs from that, commonly invoked in the literature, based on the disc viscosity which determines the accumulation of disc matter and the increase of gas pressure close to the truncation radius (Romanova et al. 2002). Bright flares close to circumstellar discs may therefore have important implications for a number of issues such as the transfer of angular momentum and mass between the star and the disc, the powering of outflows and the ionization of circumstellar discs, thus influencing also the efficiency of MRI (see also Aarnio et al. 2010).

In this paper, we investigate the effects of a flare on the stability of the circumstellar disc with a 3D magnetohydrodynamic (MHD) simulation. We model the evolution of the star–disc plasma heated by a strong energy release (with intensity comparable to that of flares typically observed in young stars), close to a thick disc surrounding a rotating magnetized CTTS. The model takes into account all key physical processes, including the gravitational force, the viscosity of the disc, the magnetic-field-oriented thermal conduction, the radiative losses from optically thin plasma and the coronal heating. The wealth of non-linear physical processes governing the star–disc system and the evolution of the flare made this a challenging task. In Section 2 we describe the MHD model and the numerical setup; in Section 3 we describe the results; in Section 4 we discuss the implications of our results and draw our conclusions.

2 PROBLEM DESCRIPTION AND NUMERICAL SETUP

Our model describes a large flare in a rotating magnetized star surrounded by a thick quasi-Keplerian disc. The flare occurs close to the inner portion of the disc, within the corotation radius (i.e. where a Keplerian orbit around the star has the same angular velocity as the star’s surface), where accretion streams are expected to originate (Romanova et al. 2002; Bessolaz et al. 2008). The magnetic field of the star is aligned dipole-like, with intensity $B \approx 1 \text{kG}$ at the stellar surface according to observations (Johns-Krull et al. 1999). The fluid is assumed to be fully ionized with a ratio of specific heats $\gamma = 5/3$.

2.1 MHD equations

The system is described by the time-dependent MHD equations in a 3D spherical coordinate system $(R, \theta, \phi)$, extended with gravitational force, viscosity of the disc, thermal conduction (including the effects of heat flux saturation), coronal heating (via a phenomenological term) and radiative losses from optically thin plasma. To our knowledge, this is the first numerical time-dependent global simulation of the star–disc system that takes into account simultaneously all key physical ingredients necessary to describe accurately the effects of a flare on the structure of the circumstellar disc. The time-dependent MHD equations written in non-dimensional conservative form are

\begin{equation}
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho u) = 0, \tag{1}
\end{equation}

\begin{equation}
\frac{\partial \rho u}{\partial t} + \nabla \cdot (\rho uu - BB + I P_t - \tau) = \rho g, \tag{2}
\end{equation}

\begin{equation}
\frac{\partial \rho E}{\partial t} + \nabla \cdot [u(\rho E + P_t) - B(u \cdot B) - u \cdot \tau] \\
= \rho u \cdot g - \nabla \cdot F_e - n_H \Lambda(T) + Q(R, \theta, \phi, t), \tag{3}
\end{equation}

\begin{equation}
\frac{\partial B}{\partial t} + \nabla \cdot (u B - Bu) = 0, \tag{4}
\end{equation}

where

\begin{equation}
P_t = P + \frac{B \cdot B}{2}, \quad E = \epsilon + \frac{u \cdot u}{2} + \frac{B \cdot B}{2 \rho},
\end{equation}

are the total pressure and the total gas energy per unit mass (internal energy, $\epsilon$, kinetic energy and magnetic energy) respectively, $t$ is the time, $\rho = \mu m_{H} n_{H}$ is the mass density, $\mu = 1.28$ is the mean atomic mass (assuming metal abundances of 0.5 of the solar values; Anders & Grevesse 1989), $n_{H}$ is the mass of the hydrogen atom, $n_{H}$ is the hydrogen number density, $u$ is the gas velocity, $\tau$ is the viscous stress tensor, $g = \nabla \Phi_s$ is the gravity acceleration vector, $\Phi_s = -GM/R$ is the gravitational potential of a central star of mass $M_s$, $G$ is the gravitational constant, $R$ is the distance from the gravitating centre, $T$ is the temperature, $B$ is the magnetic field, $F_e$ is the thermal conductive flux, $\Lambda(T)$ represents the optically thin radiative losses per unit emission measure derived with the PINTOFABLE spectral code (Kashyap & Drake 2000) and with the APED v1.3 atomic line data base (Smith et al. 2001), assuming the same metal abundances as before (as deduced from X-ray observations of CTTSs; Telleschi et al. 2007) and $Q(R, \theta, \phi, t)$ is a function of space and time.
describing the phenomenological heating rate (see Section 2.3). We use the ideal gas law, $P = (\gamma - 1)\rho e$.

The viscosity is assumed to be negligible in the extended stellar corona and effective only in the circumstellar disc. In order to make the transition between the disc and the corona, we track the original disc material by using a tracer that is passively advected in the same manner as the density. We define $C_{\text{disc}}$ as the mass fraction of the disc inside the computational cell. The disc material is initialized with $C_{\text{disc}} = 1$, while $C_{\text{disc}} = 0$ in the extended corona. Then the viscosity works only in zones consisting of the original disc material by more than 99 per cent or, in other words, where $C_{\text{disc}} > 0.99$. The viscous stress tensor is defined as

$$\tau = \eta_\nu \left[ (\nabla \mathbf{u}) + (\nabla \mathbf{u})^T - \frac{2}{3}(\nabla \cdot \mathbf{u})I \right], \quad (5)$$

where $\eta_\nu = \nu_\nu \rho$ is the dynamic viscosity, and $\nu_\nu$ is the kinematic viscosity. Several studies suggest that turbulent diffusion of magnetic field in the disc is determined by the same processes that determine turbulent viscosity, leading to angular momentum transport in the disc (Bisnovatyi-Kogan & Lovelace 2001). Thus, we assume that turbulent magnetic diffusivity is of the same order of magnitude as turbulent viscosity like in the Shakura–Sunyaev model (Shakura & Sunyaev 1973). The kinematic viscosity is expressed as $\nu_\nu = \alpha c_s^2/\Omega_K$, where $c_s$ is the isothermal sound speed, $\Omega_K$ is the Keplerian angular velocity at a given location, and $\alpha < 1$ is a dimensionless parameter regulating the efficiency of angular momentum transport within the disc, which can be expressed in terms of the fluctuating velocity and magnetic field. The parameter $\alpha$ varies in the range 0.01–0.6 in the Shakura–Sunyaev accretion model (Balbus 2003). In our simulation, we assume $\alpha = 0.02$.

The thermal conduction is highly anisotropic due to the presence of the stellar magnetic field, the conductivity being highly reduced in the direction transverse to the field (Spitzer 1962). The thermal flux therefore is locally split into two components, along and across the magnetic field lines, $F_\parallel = F_{\parallel,1} + F_{\parallel,2}$. The thermal conduction formulation also accounts for heat flux saturation. In fact, during early phases of flares, rapid transients, fast dynamics and steep thermal gradients are known to develop (Reale & Orlando 2008). Under these circumstances, the conditions required for classical ‘Spitzer’ heat conduction may break down to the extent that the plasma thermal conduction becomes flux-limited (Brown, Spicer & Melrose 1979). The two components of thermal flux are therefore written as (Orlando et al. 2008, 2010)

$$F_{\parallel,1} = \left( \frac{1}{[q_{\parallel,1}]} + \frac{1}{[q_{\parallel,2}]} \right)^{-1},$$

$$F_{\parallel,2} = \left( \frac{1}{[q_{\parallel,3}]} + \frac{1}{[q_{\parallel,4}]} \right)^{-1}, \quad (6)$$

to allow for a smooth transition between the classical and saturated conduction regime, where $[q_{\parallel,1}]$ and $[q_{\parallel,2}]$ represent the classical conductive flux along and across the magnetic field lines (Spitzer 1962):

$$[q_{\parallel,1}] = -\kappa_1 [\nabla T]_\parallel \approx -9.2 \times 10^{-7} T^{5/2} [\nabla T]_\parallel,$$

$$[q_{\parallel,2}] = -\kappa_2 [\nabla T]_\perp \approx -3.3 \times 10^{-16} \frac{\eta_\nu^2}{T^{1/2} B^2} [\nabla T]_\perp, \quad (7)$$

where $[\nabla T]_\parallel$ and $[\nabla T]_\perp$ are the thermal gradients along and across the magnetic field, and $\kappa_1$ and $\kappa_2$ (in units of erg s$^{-1}$ K$^{-1}$ cm$^{-2}$) are the thermal conduction coefficients along and across the magnetic field, respectively. The saturated flux along and across the magnetic field lines, $[q_{\parallel,3}]$ and $[q_{\parallel,4}]$, are (Cowie & McKee 1977)

$$[q_{\parallel,3}] = -\text{sign} ([\nabla T]_\parallel) 5\eta_\nu c_s^3,$$

$$[q_{\parallel,4}] = -\text{sign} ([\nabla T]_\perp) 5\eta_\nu c_s^3, \quad (8)$$

where $\psi$ is a number of the order of unity; we set $\psi = 1$ according to the values suggested for stellar coronae (Giuliani 1984; Borkowski, Shull & McKee 1989; Fadeyev, Le Coroller & Gillet 2002).

The calculations were performed using \texttt{PLUTO} (Mignone et al. 2007), a modular, Godunov-type code for astrophysical plasmas. The code provides a multiphysics, multialgorithm modular environment particularly oriented towards the treatment of astrophysical flows in the presence of discontinuities as in the case treated here. The code was designed to make efficient use of massive parallel computers using the message-passing interface (MPI) library for interprocessor communications. The MHD equations are solved using the MHD module available in \texttt{PLUTO}, configured to compute intercell fluxes with the Harten–Lax–Van Leer approximate Riemann solver, while second order in time is achieved using a Runge–Kutta scheme. A Van Leer limiter for the primitive variables is used during the heating release (at the very beginning of the simulation for $t < 300$ s) and a monotonized central difference limiter at other times. The evolution of the magnetic field is carried out adopting the constrained transport approach (Balsara & Spicer 1999) that maintains the solenoidal condition $(\nabla \cdot \mathbf{B} = 0)$ at machine accuracy. We adopted the ‘magnetic field-splitting’ technique (Tanaka 1994; Powell et al. 1999; Zanni & Ferreira 2009), by splitting the total magnetic field into a contribution coming from the background stellar magnetic field and a deviation from this initial field. Then, only the latter component is computed numerically. This approach is particularly useful when dealing with low-$\beta$ plasma as it is the case in proximity of the stellar surface (Zanni & Ferreira 2009). \texttt{PLUTO} includes optically thin radiative losses in a fractional step formalism (Mignone et al. 2007), which preserves the second time accuracy, as the advection and source steps are at least of the second-order accurate; the radiative losses $L$ values are computed at the temperature of interest using a table lookup/interpolation method. The thermal conduction is treated separately from advection terms through operator splitting. In particular, we adopted the super-time-stepping technique (Alexiades, Amiez & Gremaud 1996) which has been proved to be very effective to speed up explicit time-stepping schemes for parabolic problems. This approach is crucial when high values of plasma temperature are reached (as during flares), explicit scheme being subject to a rather restrictive stability condition [i.e. $\Delta t < (\Delta x)^2/(2\eta)$, where $\eta$ is the maximum diffusion coefficient], as the thermal conduction time-scale $\tau_{\text{cond}}$ is shorter than the dynamical one, $\tau_{\text{dyn}}$ (e.g. Hujerat & Camenzind 2000; Hujerat 2005; Orlando et al. 2005, 2008); in particular, during the early phases of the flare evolution, we find $\tau_{\text{cond}}/\tau_{\text{dyn}} \approx 10^{-2}$. The viscosity is solved with an explicit scheme, using a second-order finite difference approximation for the dissipative fluxes.

### 2.2 Initial and boundary conditions

A star of mass $M_\star = 0.8\, M_\odot$ and radius $R_\star = 2\, R_\odot$ is located at the origin of the 3D spherical coordinate system $(R, \theta, \phi)$, with the rotation axis coincident with the normal to the disc mid-plane. The rotation period of the star is assumed to be 9.2 d. The initial unperturbed stellar atmosphere is approximately in equilibrium and consists of three components: the stellar magnetosphere, the extended stellar corona and the quasi-Keplerian disc.

The pre-flare magnetosphere is assumed to be force-free, with dipole topology and magnetic moment $\mu_B$ aligned with the
isothermal with \( T_c = 4 \, \text{MK} \) and at low density\(^1\) with \( n_e \) ranging between \( \approx 10^6 \) and \( 10^9 \, \text{cm}^{-3} \). As shown in equation (14), we allow the corona to be initially rotating with angular velocity equal to the Keplerian rotation rate of the disc in order to have approximately equilibrium conditions and reduce the effects of transients caused by the initial differential rotation between the disc and the corona (Romanova et al. 2002; Zanni & Ferreira 2009).

Fig. 1 shows the initial condition together with the numerical grid adopted in our simulation. The computational domain extends between \( R_{\text{min}} = R_s \) (i.e. the inner boundary coincides with the stellar surface) and \( R_{\text{max}} = 14 \, R_s \) in the radial direction, and encompasses an angular sector going from \( \theta_{\text{min}} = 5^\circ \) to \( \theta_{\text{max}} = 175^\circ \) in the angular coordinate \( \theta \), and from \( \phi_{\text{min}} = 0^\circ \) to \( \phi_{\text{max}} = 360^\circ \) in the angular coordinate \( \phi \). The inner and outer boundaries in \( \theta \) do not coincide with the rotation axis of the star–disc system to avoid extremely small \( d\theta \) values, vastly increasing the computational cost. On the other hand, all the evolution relevant for this study never involve portions of the domain close to the star–disc rotation axis.

The radial coordinate \( R \) has been discretized on a logarithmic grid with the mesh size increasing with \( R \) (see Fig. 1), giving a higher spatial resolution closer to the star as it is appropriate for simulations of accretion flows to a star with a dipole field (Romanova et al. 2002). The radial grid is made of \( N_R = 80 \) points with a maximum resolution of \( \Delta R = 4.8 \times 10^3 \, \text{cm} \) close to the star and a minimum resolution of \( \Delta R = 6.4 \times 10^8 \, \text{cm} \) close to the outer boundary. The angular coordinate \( \theta \) has been discretized uniformly with \( N_\theta = 90 \) points, giving a resolution of \( \Delta \theta = 2^\circ \). The angular coordinate \( \phi \) is non-uniform with the highest resolution in an angular sector of \( 180^\circ \) placed where the flaring loop and the stream evolve (see bottom panel in Fig. 1). The \( \phi \)-grid is made of \( N_\phi = 110 \) points with a maximum resolution of \( \Delta \phi = 2^\circ \) and a minimum resolution of \( 9^\circ \). The numerical grid is not static but tracks the hot loop and the stream as the calculation progresses, in such a way that the loop and the stream evolve in the portion of the domain with the highest spatial resolution (namely that with \( \Delta \phi = 2^\circ \)).

The boundary conditions at the stellar surface \( R_{\text{min}} \) amount to assuming that the infalling material passes through the surface of the star as done by Romanova et al. (2002) (outflows boundary condition; see also Romanova et al. 2003; Kulkarni & Romanova 2008), thus ignoring the dynamics of the plasma after it impacts on the star. Zero-gradient boundary conditions are assumed at the outer boundary of the coordinate \( R \) (\( R_{\text{max}} \)) and at the boundaries of the angular coordinate \( \theta \) (\( \theta_{\text{min}} \) and \( \theta_{\text{max}} \)). Finally, periodic boundary conditions are assumed for angular coordinate \( \phi \) (\( \phi_{\text{min}} \) and \( \phi_{\text{max}} \)).

### 2.3 Coronal heating and flare

The phenomenological heating is prescribed as a component, describing the stationary coronal heating, plus a transient component, triggering a flare. The former component works at temperature \( T \leq 4 \, \text{MK} \) and is chosen to balance exactly the local radiative losses, leading to a quasi-stationary extended corona during the whole simulation. The transient component describes the injection of a heating pulse at the surface of the accretion disc. The flare could be driven by a stressed field configuration resulting from the twisting of magnetic field lines induced by the differential rotation of the inner rim of the disc and the stellar photosphere.

\(^1\) Note however that the density of the outer corona is not important for the flare evolution.
Figure 1. Initial conditions and computational domain. Upper panel: volume rendering of the mass density, in log scale, at the beginning of the simulation ($t = 0$). The selected magnetic field lines marked in red describe the initial dipolar magnetic field. The yellow sphere at the centre of the spatial domain represents the central protostar. Middle panel: slice in the ($x$, $z$) plane of the mass density distribution with overplotted the computational grid. Bottom panel: as in the middle panel for the slice in the equatorial plane ($x$, $y$).

(Shu et al. 1997). The heat pulse has a 3D Gaussian spatial distribution located at the disc border at a distance of 5 $R_\ast$ (namely well below the corotation radius $R_{co} = 9.2 R_\ast$) with width $\sigma = 2 \times 10^{10}$ cm. Its intensity per unit volume is $H_0 = 32$ erg cm$^{-3}$ s$^{-1}$. The pulse starts at the beginning of the simulation ($t = 0$) and is switched off completely after 300 s. The flare parameters are analogous to those adopted in a 1D hydrodynamic model that reproduces the evolution of a large flare observed in an Orion young star from COUP (Favata et al. 2005). The total energy released during our simulated flare is $E_{fl} = 10^{36}$ erg, namely the same order of magnitude of the energy involved in the brightest X-ray flares observed in COUP (Favata et al. 2005; Wolk et al. 2005).

3 RESULTS

3.1 Evolution of the flare and X-ray emission

We followed the evolution of the star–disc system for $\approx 2$ d, focusing on its effects on the disc structure. Fig. 2 shows the distributions of density and temperature in ($R$, $z$) slices passing through the middle of the heating pulse during its evolution. During this impulsive phase, the local magnetic field is perturbed by the flare, and an MHD shock wave develops in the magnetosphere above the disc and propagates radially away from the central protostar in regions where $\beta > 1$. At the same time, the sudden heat deposition determines a local increase of temperature (up to a maximum of 800 MK) and pressure (above 6000 dyn cm$^{-2}$). The dense disc material is heated and expands in the magnetosphere with a strong evaporation front at speeds above 4000 km s$^{-1}$. The fast thermal front propagates towards the star along the magnetic field lines and reaches the stellar surface on a time-scale of $\approx 1$ h (left-hand panels in Fig. 2). At this point, a hot magnetic tube (loop) of length $L \approx 10^{12}$ cm (i.e. comparable to loop lengths inferred from COUP observations; Favata et al. 2005) is formed, linking the inner part of the disc to the star’s photosphere. The loop is illustrated in the left-hand panels of Fig. 3, showing a cutaway view of the star–disc system at $t = 1.2$ h (upper panel; the flaring loop is marked in red), and a schematic view of the system during the evolution of the flaring loop (lower panel). Due to the efficient thermal conduction and radiation, the plasma begins to cool immediately after the heat pulse is over, and the maximum temperature rapidly decreases to $\sim 50$ MK in $\approx 1$ h. The disc evaporation is fed by thermal conduction from the outer hot plasma, even after the end of the heat pulse.

Fig. 2 also shows that the overheating of the disc surface at the loop footpoint makes a significant amount of material expand and be ejected in the magnetosphere. A small fraction of this evaporated disc material streams along the loop accelerated towards the star by its gravity, fills the whole tube in $\approx 10$ h, and the density keeps increasing throughout the loop up to values ranging between $10^9$ and $10^{10}$ cm$^{-3}$ at its apex. On the other hand, most of the evaporated disc material is not efficiently confined by the magnetic field and channeled into the hot loop but is rather ejected away from the central star in the outer stellar corona, carrying away mass and angular momentum (see Fig. 2). Due to the high values of $\beta$ there, the magnetic field lines are dragged away. The outflowing plasma is supersonic and its speed is of the order of the local Alfvén speed $u_A \approx 300$ km s$^{-1}$. We note that our results on the dynamics of the outflowing plasma are similar to those found with an MHD model proposed by Hayashi, Shibata & Matsumoto (1996) to describe hard X-ray flares in protostars observed by the ASCA satellite.
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Figure 2. Close view of the flaring loop during its early evolution. The figure shows slices in the ($R, z$) plane passing through the middle of the flaring loop, reporting the distributions of density (upper panels) and temperature (lower panels). The slices encompass an angular sector going from the rotation axis to the disc mid-plane. The white lines represent sampled poloidal magnetic field lines. The arrows represent the poloidal flow velocities. The magenta line delimits the region with plasma $\beta < 1$ (on the left of each panel).

From the model results, we synthesized the X-ray emission originating from the flare, applying a methodology analogous to that described in the literature in the context of the study of novae and supernova remnants (Orlando et al. 2006; Orlando, Drake & Laming 2009). In particular, we first calculate the emission measure in the jth domain cell as $\text{em}_j = n_{Hj} V_j$ (where $n_{Hj}$ is the hydrogen number density in the cell, $V_j$ is the cell volume, and we assume fully ionized plasma). From the values of emission measure and temperature in the cell, we synthesize the corresponding X-ray spectrum, using the PINToALE spectral code (Kashyap & Drake 2000) with the APED V1.3 atomic line database, and assuming the same metal abundances of the simulation, namely 0.5 of the solar values, as deduced from X-ray observations of CTTSs (Tellieschi et al. 2007). We integrate the X-ray spectra from the cells in the whole spatial domain and, then, derive the X-ray luminosity by integrating the spectrum in the [0.6–12] keV band.

Fig. 4 shows the evolution of the maximum temperature and emission measure of the flaring loop, and its X-ray light curve. The peak temperature of the flare is reached very soon at $t \approx 100$ s and the emission measure peaks later at $t \approx 1000$ s. The X-ray luminosity evolves as the emission measure, reaching a peak value of $L_X \approx 6.5 \times 10^{32}$ erg s$^{-1}$ at $t \approx 500$ s, namely after the end of the heat pulse. Then the luminosity (and the emission measure) decreases by more than 2 orders of magnitude until $t \approx 3 \times 10^3$ s, is steady till $t \approx 2 \times 10^4$ s, and decreases again afterward. The peak X-ray luminosity of the simulated flare is consistent with the values derived for the brightest X-ray flares observed in COUP (see table 1 in Favata et al. 2005) which range between $10^{32}$ erg s$^{-1}$ (source COUP 752) and $8 \times 10^{32}$ erg s$^{-1}$ (source COUP 1568). On the other hand, it turns out that $3/4$ of the COUP flares have a peak X-ray luminosity approximately 1 order of magnitude lower than that simulated here although the total energy released during the simulated flare (namely $E_{\text{fl}} = 10^{36}$ erg, see Section 2.3) is comparable with the median total energy of the flare inferred from the COUP observations (Wolk et al. 2005). This may be due to the fact that the simulated flare lasts for a time interval significantly shorter than those typical of stellar flares and is only partially confined by the magnetic field (see discussion below).

The evolution of our simulated flare has significant differences with respect to the evolution of flares simulated with 1D models (Reale et al. 1988). In fact, at variance with 1D models where the flare is assumed to be fully confined by the magnetic field, in our simulation the flare is only partially confined by the magnetic field at the loop footpoint anchored at the disc surface. There, a substantial amount of the evaporated disc material escapes in the outer stellar magnetosphere and does not fill the post-flare loop. We conclude therefore that our results could be intermediate between those found with models of fully confined flares (Reale et al. 1988) and those of models of unconfined flares (Reale, Bocchino & Peres 2002) which show that the flare evolution is much faster than that observed in the confined case. On the other hand, for the purposes of this work (namely the study of the perturbation of the disc by a bright flare), we have used a simplified and idealized configuration of the initial stellar magnetic field (namely a magnetic dipole), whilst many
Figure 3. Evolution of the bright flare and accretion stream. The upper panels show cutaway views of the star–disc system showing the mass density of the disc (green) at $t = 1.2$ h (on the left) and, from the opposite side, at $t = 36$ h (on the right) since the injection of the heat pulse. The upper-left panel also overplots the 3D volume rendering of the plasma temperature (in MK; see colour table in the upper left corner of the panel), showing the flaring loop (in red) linking the inner part of the disc with the star. The upper-right panel shows the accretion stream triggered by the flare in the side of the disc opposite to the flaring loop. Selected magnetic field lines are overplotted in red. Lower panels show schematic views of the system during the evolution of the flaring loop (on the left) and in the subsequent period, during the evolution of the stream (on the right).

Observations indicate that the stellar atmospheres are permeated by magnetic fields with a high degree of complexity (e.g. Gregory et al. 2010, and references therein). In particular, the magnetic field in proximity of a heat release (due to magnetic reconnection) near the disc is expected to be more complex than that modelled here. In the presence of complex magnetic field configurations, the magnetic structure hosting the flaring plasma is expected to confine more efficiently the hot plasma, producing a flare evolution more similar to that described by 1D models.

It is worth emphasizing that our 3D simulation is focused on the effects of the flare on the stability of the disc and does not pretend to describe accurately the evolution of the flaring loop. Nevertheless, we show here that, even if the flare evolution is not described accurately, the length, maximum temperature and peak X-ray luminosity of the flaring loop reproduced by our simulation resemble those derived from the analysis of the brightest X-ray flares observed in young low-mass stars (Favata et al. 2005). We are confident, therefore, that the flare simulated here is appropriate to investigate the effects of bright flares observed in young stars on the stability of the disc.

3.2 Dynamics of the accretion stream

During the flare evolution, the injected heat pulse produces an over-pressure in the disc at the footpoint of the loop. This over-pressure travels through the disc and reaches the opposite boundary after $\approx 5$ h, where it pushes the plasma out to form an intense funnel stream. Fig. 5 shows the distributions of density and pressure in $(R, z)$ slices passing through the middle of the stream. The over-pressure wave triggering the stream is evident in the bottom panels. This new intense stream flows along the dipolar magnetic field lines and impacts on to the stellar surface $\approx 25$ h after the injection of the heat pulse. The right-hand panels in Fig. 3 show a cutaway view of the star–disc system (upper panel) after the impact of the stream on to the stellar surface and a schematic view of the system during the stream evolution (lower panel). As a result, the stream accretes substantial mass on to the young star from the side of the disc opposite to the post-flare loop. Our 3D simulation follows the evolution of the accretion stream for additional 23 h, for a total of 48 h. In this time lapse the stream gradually approaches a quasi-stationary condition.
We analysed the dynamics of the stream by deriving the forces at work along a fiducial magnetic field line nested within the stream. Initially the stream is triggered by a strong pressure gradient due to the overpressure wave originating from the flare. The pressure gradient force drives the material out of the disc and channels it into a funnel flow. Then the gravitational force accelerates the escaped material towards the central star. These forces evolve with time, and Fig. 6 shows them along the fiducial field line after the stream impacts the stellar surface. At this stage, the pressure gradient is still effective in pushing the disc material out of the disc, but it acts in the opposite direction (against the free-fall of matter) in most of the accretion stream. The pressure gradient becomes the dominant force close to the stellar surface, substantially braking (but not stopping) the accretion flow. As discussed below, at this stage of evolution, the stream has not yet reached a quasi-stationary condition. Later, when the stream stabilizes, the gravitational force dominates the stream evolution and the plasma continuously accelerates towards the star, approaching the free-fall speed $u_{\text{ff}}$ at the star’s photosphere. Other forces acting against the free-fall of matter are the centrifugal force and a backward force due to the magnetic mirror effect when the material approaches the star (see also Romanova et al. 2002; Zanni & Ferreira 2009). However, these forces are much smaller than the others and do not play any relevant role in the stream dynamics (Fig. 6; see also Romanova et al. 2002; Zanni & Ferreira 2009).

Fig. 7 shows the profiles of particle number density and different velocities along the fiducial magnetic field line shown in Fig. 6 at time $t = 36$ h. The matter flows with poloidal velocity $u_{\text{str}}$. The flow
is accelerated by gravity and becomes supersonic at a distance of \( \approx 2 \times 10^{11} \) cm from the disc, while the stream density decreases. The flow gradually approaches the free-fall velocity \( u_{\text{ff}} \), reaching a maximum velocity of \( u_{\text{ff}} \approx 200 \text{ km s}^{-1} \) at \( s \approx 10^{11} \) cm (\( u_{\text{ff}} \approx 0.8 u_{\text{th}} \)). Then the flow slightly brakes while the stream density increases again approaching the stellar surface. As discussed above, the slowdown of the flow is due to the pressure gradient force acting against the free-fall of matter for \( s \) ranging between \( 0.5 \times 10^{11} \) and \( 1 \times 10^{11} \) cm (see Fig. 6). This feature is present until the end of our 3D simulation at \( t \approx 48 \) h.

To further investigate the evolution of the accretion stream, we performed an additional simulation with the same parameters of the 3D simulation discussed above, but carried out in 2.5 dimensions (2.5D), that is, in spherical coordinates \((R, \theta)\) assuming axisymmetry around the rotation axis of the star–disc system. Note that, in this configuration, the heat pulse is not localized in a relatively small portion of the disc (as in our 3D simulation), but is distributed in a ring. Nevertheless, we found that the evolution of the flare and the stream described by the 2.5D simulation is quite similar to that of our 3D simulation. The 2.5D simulation allowed us to extend our analysis of the stream dynamics, following its evolution until \( t = 100 \) h (i.e. approximately 4 d). Fig. 8 shows the profiles of the relevant velocities derived from the 2.5D simulation at \( t = 36 \) h (upper panel) and \( t = 68 \) h (lower panel). The velocity profiles at \( t = 36 \) h resemble those derived from the 3D simulation (lower panel in Fig. 7). In particular, the flow slightly brakes approaching the stellar surface due to a pressure gradient force slowing down the free-fall of matter, as found in the 3D simulation. In addition, the 2.5D simulation shows that, at this stage, the stream has not reached yet a quasi-stationary condition. Later, the stream stabilizes (after \( t \approx 60 \) h); the gravitational force becomes dominant along the stream and the matter is accelerated until it impacts the stellar surface, reaching there a maximum velocity of \( u_{\text{ff}} \approx 300 \text{ km s}^{-1} \) corresponding to \( \approx 0.9 u_{\text{th}} \).

The above results, therefore, show that the physical characteristics of the accretion stream triggered by the flare closely recall those, largely discussed in the literature, of streams driven by the accumulation of mass at the disc truncation radius under the effect of the viscosity and pushed out of the equatorial plane because of the growing pressure gradient there (Romanova et al. 2002, 2003; Bessolaz et al. 2008; Zanni & Ferreira 2009). Our simulation shows that the stream is relatively cold (its temperature remains below 1 MK). After the disc material enters the stream, its density slightly decreases and, close to the stellar surface, increases again as a result of the gas compression by the dipolar magnetic field. The stream velocity \( u_{\text{ff}} \) gradually increases towards the star: it becomes supersonic already at a distance of \( \approx 2 \times 10^{11} \) cm from the disc, and \( u_{\text{ff}} \) approaches the free-fall speed \( u_{\text{ff}} \) close to the stellar surface. Fig. 9 shows the density distribution on the stellar surface at \( t = 36 \) h; the dense spot on the surface is the region of impact of the stream. The spot covers a small percentage of the stellar surface and the stream is inhomogeneous with its mass density varying across the stream and being the largest in the inner region, according to Romanova et al. (2004).

Finally, we derived the mass accretion rate \( \dot{M} \) due to the stream from the side of the disc opposite to the post-flare loop and found \( \dot{M} \gtrsim 2.5 \times 10^{-10} \text{ M}_\odot \text{ yr}^{-1} \). Accretion rates derived from optical–near-UV continuum emission typically range between \( 10^{-12} \) and \( 10^{-8} \text{ M}_\odot \text{ yr}^{-1} \) with \( \dot{M} \) varying in the same star even by a factor of 10 and depending on the age and mass of the star (Muzerolle et al. 2005; Mohanty, Jayawardhana & Basri 2005; Natta, Testi & Randich 2006). In general, more evolved low-mass young stars are characterized by lower accretion rates (e.g. Herczeg & Hillenbrand 2008, and references therein). We compared the rate \( \dot{M} \) derived from our 3D simulation with the rates derived from optical–UV observations and available in the literature. In particular, we considered a sample of low-mass stars and brown dwarfs observed with the Low Resolution Imaging Spectrometer (LRIS) on Keck I and a sample of solar mass young accretors observed with Hubble Space Telescope Imaging Spectrograph (STIS) (both samples analysed by Herczeg & Hillenbrand 2008), and an X-ray selected sample of CTTSs observed with various optical telescopes (analysed by Curran et al. 2011). Herczeg & Hillenbrand (2008) found
that the excess UV and optical emission arising in the Balmer and Paschen continua yields mass accretion rates ranging between \(2 \times 10^{-12}\) and \(10^{-8} \, \text{M}_\odot \, \text{yr}^{-1}\) in the case of low-mass stars and brown dwarfs, and ranging between \(2 \times 10^{-10}\) and \(5 \times 10^{-8} \, \text{M}_\odot \, \text{yr}^{-1}\) in the case of solar mass stars. Curran et al. (2011) calculated \(\dot{M}\) for the stars of their sample by measuring H\(\alpha\), H\(\beta\), H\(\gamma\), He\(\text{II}\) (4686 Å), He\(\text{I}\) (5016 Å), He\(\text{I}\) (5876 Å), O\(\text{I}\) (6300 Å) and He\(\text{I}\) (6678 Å) equivalent widths and found that the mass accretion rates range between \(2 \times 10^{-10}\) and \(5 \times 10^{-8} \, \text{M}_\odot \, \text{yr}^{-1}\). Fig. 10 shows the rate \(\dot{M}\) derived from our 3D simulation compared with the three samples of young accreting stars. The accretion rate of our simulation is in the range of the rates measured in low-mass stars and lower than those of fast-accreting objects such as BP Tau, RU Lup or T Tau.

4 SUMMARY AND CONCLUSIONS

We investigated the evolution of a bright flare occurring close to the disc surrounding a magnetized CTTS and its effects on the stability of the disc, through numerical MHD simulations. To our knowledge, the simulation presented here represent the first attempt to model the 3D global evolution of the star–disc system that simultaneously include stellar gravity, viscosity of the disc, magnetic field, radiative cooling and magnetic-field-oriented thermal conduction (including
the effects of heat flux saturation). Our findings lead to several conclusions.

(i) During its first stage of evolution, the flare gives rise to a hot magnetic loop linking the inner part of the disc to the star; we found that the length, maximum temperature and peak X-ray luminosity of the simulated flaring loop are similar to those derived from the analysis of luminous X-ray flares observed in young low-mass stars (Favata et al. 2005).

(ii) During the flare evolution, disc material evaporates in the outer stellar atmosphere under the effect of the thermal conduction. A small fraction of the evaporated disc material gradually fills the loop in $\approx 10$ h. Indeed most part of the evaporated disc material is not efficiently confined by the magnetic field and channelled into the loop, but is rather ejected away from the central star in the outer stellar corona, carrying away mass and angular momentum.

(iii) In the aftermath of the flare, the disc is strongly perturbed: the injected heat pulse produces an overpressure in the disc at the loop’s footprint that travels through the disc. When the overpressure reaches the opposite side of the disc, a funnel flow starts to develop there, flowing along the dipolar magnetic field lines and impacting on to the stellar surface $\approx 1$ d after the injection of the heat pulse.

(iv) We found that the mass accretion rate $M$ of the stream triggered by the flare is in good agreement with those measured in low-mass stars and brown dwarfs, and in some solar mass accretors (e.g. Herczeg & Hillenbrand 2008; Curran et al. 2011). The stream therefore accretes substantial mass (comparable with the observed) on to the young star from the side of the disc opposite to the post-flare loop.

We conclude therefore that the brightest flares detected in CTTSs (e.g. Favata et al. 2005) can be a mechanism to trigger mass accretion episodes on to protostars with accretion rates in the range of those measured in low-mass stars and lower than those of fast-accreting objects. On the other hand, it is worth mentioning that large flares do not occur continuously in CTTSs and therefore cannot explain alone the time-averaged accretion rates derived in young accretors; an average of 1 flare per star per 650 ks ($\approx 7$ d) has been inferred by analysing the COUP observations (Wolk et al. 2005) and clusters much older than Orion (Wolk et al. 2004). To ascertain the contribution that flares may have to the observed time-averaged accretion rates, it is necessary to determine the frequency of those flares able to trigger accretion streams. In future, an exploration of the parameter space of our model is therefore needed to determine to which extent the total energy released during the flare can be reduced to still produce an accretion stream. This point is rather important to ascertain if a storm of small-to-medium flares (very frequent in CTTSs and often not even resolved in the light curves) occurring on the accretion disc of young stars is able to trigger accretion streams with high cadence, thus leading to a significant and persistent mass accretion. This issue deserves further investigation in future studies.

The initial conditions adopted in our simulations are largely used in the literature (e.g. Romanova et al. 2002, and subsequent works) and are appropriate to describe the star–disc system in CTTSs. However, as discussed in Section 3.1, these conditions may result to be idealized and simplified in some aspects. Many observations indicate that the stellar atmospheres are permeated by magnetic fields with a degree of complexity much higher than the magnetic dipole adopted here (e.g. Gregory et al. 2010, and references therein); the flare may occur in the presence of existing accretion streams induced by the coupling of the magnetic field to the disc below the corotation radius (e.g. Romanova et al. 2002, 2003; Bessolaz et al. 2008; Zanni & Ferreira 2009) or triggered by other flares. In particular, the magnetic field in proximity of the heat release (due to magnetic reconnection) is expected to be more complex than that modelled here, thus confining more efficiently the hot plasma and enhancing the effects of the flare energy deposition on the system. On the other hand, the flaring loop and the flare-induced accretion stream could be strongly modified or even disappear if the flare occurs in a flux tube initially filled with cold infalling gas. However, Reale (2009) showed that a flare involving dense infalling plasma would decay much faster than generally observed, so that the flares we address here do not occur in such a configuration. Nevertheless, the flaring loop and the flare-induced accretion stream may be strongly perturbed and have a more complex structure than that described here if the flare energy release occurs in proximity of an existing accretion stream.

Following other works in the literature (e.g. Romanova et al. 2002, 2003, 2004; Kulkarni & Romanova 2008), we assumed the turbulent diffusivity to be uniform within the disc, setting $\alpha$ as a constant. However, numerical simulations indicate that the MRI stress would be substantial in the disc mid-plane where the plasma $\beta$ is high, but would drop in outer disc layers where $\beta$ is relatively low. As a result, the turbulent diffusivity, scaled appropriately to the MRI, is expected to be smaller in the outer disc layers than in the disc mid-plane. Since the $\alpha$ value adopted in our simulation (namely $\alpha = 0.02$) lies in the lower limit of the range of the parameter $\alpha$ (namely 0.01 $\leq \alpha \leq 0.6$; Balbus 2003; Kulkarni & Romanova 2008), we expect that the turbulent diffusivity would be larger in the disc mid-plane than assumed in our simulation, thus influencing the mass accretion from the disc on to the star. However, the time lapse covered by our simulation ($\approx 48$ h) is $\approx 1/5$ of the star rotation period which is much shorter than the time required by the turbulent diffusivity.

Figure 10. The solid line shows the mass accretion rate during the evolution of the funnel flow developed on the side of the disc opposite to the flaring loop. The crosses report the values of mass accretion rate derived from optical-near UV observations for a sample of low-mass stars and brown dwarfs (green; Herczeg & Hillenbrand 2008), for a sample of solar-mass young accretors (blue; Herczeg & Hillenbrand 2008) and for an X-ray-selected sample of CTTSs (red; Curran et al. 2011).
Accretion to young stars triggered by flares

Note that, as discussed above, Reale (2009) has shown that the opposite is unlikely, that is flares cannot be triggered in an accreting flux tube.

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