Abstract
The Kepler-9 system harbors three known transiting planets. The system holds significant interest for several reasons. First, the outer two planets exhibit a period ratio that is close to a 2:1 orbital commensurability, with attendant dynamical consequences. Second, both planets lie in the planetary
mass "desert" that is generally associated with the rapid gas agglomeration phase of the core accretion process. Third, there exist attractive prospects for accurately measuring both the sky-projected stellar spin–orbit angles as well as the mutual orbital inclination between the planets in the system. Following the original Kepler detection announcement in 2010, the initially reported orbital ephemerides for Kepler-9 b and c have degraded significantly, due to the limited time base-line of observations on which the discovery of the system rested. Here, we report new ground-based photometric observations and extensive dynamical modeling of the system. These efforts allow us to photometrically recover the transit of Kepler-9 b and thereby greatly improve the predictions for upcoming transit mid-times. Accurate ephemerides of this system are important in order to confidently schedule follow-up observations of this system, for both in-transit Doppler measurements as well as for atmospheric transmission spectra taken during transit.

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1. Introduction

In our own solar system, the major planets all lie within a few degrees of the ecliptic, and the plane containing the planets aligns quite well with the Sun's equator. By contrast, hot Jupiters are frequently observed to have orbital planes that are strikingly misaligned with the equators of their host stars (as reviewed by Winn & Fabrycky 2015). Spin–orbit angle determinations are made through measurement of the Rossiter–McLaughlin (R–M) effect (Rossiter 1924; McLaughlin 1924), a time-variable anomaly in the stellar spectral-line profiles, which generates an apparent stellar radial velocity variation during the transit (Queloz et al. 2000). The large observed range in spin–orbit angles is now interpreted as evidence that at least a subset of hot Jupiters were subject to violent dynamical migration at some point in their histories (Winn & Fabrycky 2015). This interpretation can be directly tested if the spin–orbit angles can be measured in multi-transiting planetary systems, especially ones hosting planets in mean motion resonance (MMR) configurations. The existence of MMR configurations implies that dissipation in the protoplanetary precursor disk played a key role in sculpting the final planetary orbital configuration, while simultaneously disfavoring a dynamically violent history. Kepler-9 was the first multiple-planet system discovered using the transit method (Holman et al. 2010). It is also the first definitive transit timing variation (TTV) system published with an orbital period ratio of outer two planets close to 2:1 commensurability. In addition to suggesting past dissipation generally, such configurations are believed to be the natural consequence of convergent disk migration (Kley & Nelson 2012). As a consequence, spin–orbit alignment of the planets and the stellar equator is expected. The Kepler-9 system, however, is identified as a candidate
misaligned multi-transiting planetary system (Walkowicz & Basri 2013) based on an assessment with the approximate $v \sin i$ method. Further R-M effect measurement is urgently needed to obtain a definitive answer. The R-M effect is much more easily measured when transits are deep, and as a practical consequence, R-M observations of multi-transiting planetary systems are hard to make. They usually involve fainter stars and smaller transit depths, and as yet, very few high quality measurements exist (Kepler-89 d, Hirano et al. 2012; Albrecht et al. 2013; Kepler-25 c, Albrecht et al. 2013; Benomar et al. 2014; WASP-47 b, Sanchis-Ojeda et al. 2015). Both Kepler-9 b and c, however, have very large planet-star size ratios of $R_p/R_* = 0.074$ and $R_p/R_* = 0.076$, respectively (Twicken et al. 2016)—among the largest ratios yet detected in multi-transiting planetary systems. Kepler-9 thus offers a rare opportunity to carry out a high signal-to-noise spin–orbit angle measurement in a multi-transiting planetary system. Successful acquisition will provide a key zeroth-order test of the origin scenarios of spin–orbit misalignments and will potentially help to delineate competing formation paradigms for hot Jupiters. Moreover, extended transit mid-time measurements will significantly improve the precision of planetary mass determinations, which will aid resolution of the ongoing discrepancy between masses measured through modeling of TTVs and masses modeled through accumulation of Doppler radial velocities (Holman et al. 2010; Borsato et al. 2014; Dreizler & Ofir 2014; Hadden & Lithwick 2017).

In addition, canonical planet formation theory is challenged by the Kepler-9 planetary masses (Kepler-9 b: 44.17 $M_\oplus$, Kepler-9 c: 30.37 $M_\oplus$; S. Wang & G. P. Laughlin 2017, in preparation). In the standard planet formation model (Pollack et al. 1996), the planetary mass should grow rapidly from 30 $M_\oplus$ to 100 $M_\oplus$ and beyond. It is difficult to arrest run-away gas accretion in the midst of this intermediate range; few planets are known in the "intermediate mass desert." It would therefore be of great interest to obtain a high signal-to-noise transmission spectrum to better delineate the atmospheric composition and the planetary structure of this special class of planet. Any prospective transit-related follow-up studies will require precisely scheduled observations of the transit of Kepler-9 b and c. Such scheduling, however, is not easy. Transit mid-times for Kepler-9 b and c vary by up to 0.78 day and 1.78 day (Figure 1), respectively, due to the significant planet–planet gravitational interactions in the system. In this work, we report the successful relocation of Kepler-9 b's transit on UT 2016 September 1, which serves to confirm dynamical modeling of the TTVs derived from the full Kepler data set. To provide optimal ephemerides for future observations, we provide the predicted future transit windows of the Kepler-9 system by jointly analyzing the TTVs from both the legacy Kepler data as well as our new observations. We also discuss the feasibility of carrying out R-M observations of Kepler-9 b and c, as well as the prospects for directly measuring the mutual inclination between their orbital planes.
Figure 1. TTVs (blue circles) of Kepler-9 b and c compared to our best fit and prediction (open yellow-green circles) obtained using the full Kepler data set. Mutual gravitational interactions between the planets induce TTVs with very high signal-to-noise; the transit mid-times of Kepler-9 b and c vary by up to 0.78 day and 1.78 day, respectively. To facilitate future scheduling of transit-related observations (e.g., the measurement of the R-M effect, or the acquisition of an atmospheric transmission spectrum), we observed Kepler-9 on UT 2016 September 1, when a transit of Kepler-9 b was predicted to occur according to our dynamical model. As indicated with an arrow on the upper panel, the transit was successfully recovered (see Figure 2 for more details).

This paper adheres to the following organization. In Section 2, we describe the dynamical model that we have employed to predict future transit mid-times for Kepler-9 b and c, based on transits observed during the full 17-quarter Kepler data set. In Section 3, we describe our coordinated observations of a Kepler-9 b transit on UT 2016 September 1, along with the data reduction strategies that we employed. In Section 4, we describe the photometric model that we employed to analyze the transit light curve. In Section 5, the transit mid-time obtained with our light curve is used together with the complete Kepler data set to predict an extensive set of the aperiodic future transits for both Kepler-9 b and c. In Section 6, we discuss the prospects for obtaining spin-orbit angle measurements and mutual orbital inclination measurements for the system. Finally, we summarize the results and discuss the potential for further investigations in Section 7.
2. Predicting the Transit Window

To predict the transit mid-times for Kepler-9 b and c, we carried out a differential evolution Markov chain Monte Carlo-based (DEMCMC; Ter Braak 2006) dynamical fitting analysis to infer the orbital parameters of Kepler-9 b and c based on their transit mid-times and uncertainties from the full 17-quarters of Kepler data (Holczer et al. 2016). Given the mass and the six orbital elements of the planets and the mass of the host star, we calculated the individual transit mid-times of Kepler-9 b and c using a Runge-Kutta-Fehlberg 7(8) N-body code which integrates the full Newtonian equations of motion. The inner planet, Kepler-9 d, is ignored in the model due to its negligible influence on the transit mid-times of Kepler-9 b and c (Dreizler & Ofir 2014).

The free parameters considered by the DEMCMC fit are \( P, e, i, \omega + M_0, \omega - M_0, \Delta \Omega, \) and \( m, \) where \( P \) is the orbital period, \( e \) is the eccentricity, \( i \) is the orbital inclination, \( \omega \) is the argument of periastron, \( M_0 \) is the initial mean anomaly, \( \Delta \Omega \) is the difference of the ascending nodes between two planets, and \( m \) is the planetary mass. We assume normally distributed priors with median values and uncertainties given in Dreizler & Ofir (2014). The central stellar mass is fixed to 1.034 \( M_\odot \) (Johnson et al. 2017). We run 40 parallel DEMCMC chains, each with \( 2 \times 10^7 \) iterations, and we save every thousandth set of parameters. The first \( 1 \times 10^7 \) iterations of each chain are discarded to eliminate burn-in bias. The statistics of the parameters are derived from the final \( 1 \times 10^4 \) elements of each MCMC assessment. The \( \hat{R} \) statistics (Brooks & Gelman 1998) for all parameters were below 1.1 at the conclusion of the calculation. The reported parameters, as detailed in Table 1, are derived in terms of the medians and standard deviations of the posterior parameter distributions. Our overall best fit agrees well with the models obtained by Dreizler & Ofir (2014), Borsato et al. (2014), and Hadden & Lithwick (2017). All four studies, however, report slightly different orbital periods. For further details of Kepler-9 system parameters, we refer the reader to S. Wang & G. P. Laughlin (2017, in preparation).

**Table 1.** Dynamical Parameters for Kepler-9 System from the Best \( N \)-body Fit to TTVs

| Parameter | \( \text{Kepler Data} \) | \( \text{Kepler Data + Our New Data} \) |
|-----------|----------------|-----------------|
| \( m_b \) (\( m_\oplus \)) | 43.98 \( \pm \) 0.47 | 43.97 \( \pm \) 0.49 |
| \( m_c \) (\( m_\oplus \)) | 30.25 \( \pm \) 0.33 | 30.24 \( \pm \) 0.33 |
| \( P_b \) (days) | 19.225 \( \pm \) 0.0000 | 19.225 |
| \( \sigma \) | \( \sigma \) | \( \sigma \) |
With the orbital parameters in hand, we can proceed to predict the future transit mid-times for both Kepler-9 b and Kepler-9 c by integrating Newton's equations of motion for the model three-body system. We randomly draw 1000 samples from the converged chains and integrate them independently to determine the future transit mid-times. The best-predicted transit mid-times and the estimated uncertainties (as provided in Table 2 and shown by the open yellow-green circles in Figure 1), are derived as the median values and standard deviations of the integrated transit mid-time distributions (see Figure 3 for example). The predicted transit mid-times agree with the results from Dreizler & Ofir (2014) to within 2 and 3 minutes for Kepler-9 b and c, respectively.

**Table 2.** Prediction of Aperiodic Future Transit Mid-times (day) for Kepler-9 b and c from our Best N-body Fit to TTVs

| Parameter | Value | $\sigma$ | Value | $\sigma$ |
|-----------|-------|---------|-------|---------|
| $P_c$ (days) | 39.015 | 0.0001 | 39.015 | 0.00013 |
| $e_b$ | 0.0637 | 0.0009 | 0.0637 | 0.0009 |
| $e_c$ | 0.0680 | 0.0004 | 0.0680 | 0.0003 |
| $i_b$ (°) | 89.98 | 1.01 | 89.88 | 1.02 |
| $i_c$ (°) | 89.98 | 0.63 | 90.01 | 0.63 |
| $\omega_b$ (°) | 357.04 | 0.44 | 357.05 | 0.45 |
| $\omega_c$ (°) | 168.65 | 0.30 | 168.65 | 0.31 |
| $M_{0b}$ (°) | 224.90 | 0.53 | 224.88 | 0.56 |
| $M_{0c}$ (°) | 253.39 | 0.29 | 253.39 | 0.30 |
| $\Delta\Omega$ (°) | 0.17 | 1.54 | 0.43 | 1.55 |

**Note.** The orbital elements are given for the reference epoch $T_0 = 2454900.0$ BJD$_{TDB}$. Download table as: [ASCII](#) [Typeset image](#)

With the orbital parameters in hand, we can proceed to predict the future transit mid-times for both Kepler-9 b and Kepler-9 c by integrating Newton's equations of motion for the model three-body system. We randomly draw 1000 samples from the converged chains and integrate them independently to determine the future transit mid-times. The best-predicted transit mid-times and the estimated uncertainties (as provided in Table 2 and shown by the open yellow-green circles in Figure 1), are derived as the median values and standard deviations of the integrated transit mid-time distributions (see Figure 3 for example). The predicted transit mid-times agree with the results from Dreizler & Ofir (2014) to within 2 and 3 minutes for Kepler-9 b and c, respectively.

**Table 2.** Prediction of Aperiodic Future Transit Mid-times (day) for Kepler-9 b and c from our Best N-body Fit to TTVs

| Parameter | Value | $\sigma$ | Value | $\sigma$ |
|-----------|-------|---------|-------|---------|
| Kepler-9 b | 2733.1877 | ±0.0 | 2718.1377 | ±0.0 |
| Kepler-9 c | 2733.1877 | ±0.0 | 2718.1377 | ±0.0017 |
| Kepler-9 b   | Kepler-9 c   | Kepler-9 b   | Kepler-9 c   |
|--------------|--------------|--------------|--------------|
| 2752.4069±0.006 |
| 2757.2123±0.0017 |
| 2752.4069±0.006 |
| 2757.2123±0.0017 |
| 2771.6269±0.006 |
| 2796.2862±0.0017 |
| 2771.6269±0.006 |
| 2796.2862±0.0017 |
| 2790.8465±0.006 |
| 2835.3593±0.0018 |
| 2790.8464±0.006 |
| 2835.3593±0.0018 |
| 2810.0672±0.006 |
| 2874.4314±0.0018 |
| 2810.0672±0.006 |
| 2874.4314±0.0018 |
| 2829.2872±0.006 |
| 2913.5022±0.0019 |
| 2829.2872±0.006 |
| 2913.5022±0.0019 |
| 2848.5087±0.006 |
| 2952.571±0.0019 |
| 2848.5087±0.006 |
| 2952.571±0.0019 |
| 2867.7291±0.007 |
| 2991.6364±0.0019 |
| 2867.7291±0.007 |
| 2991.6364±0.0019 |
| 2886.9513±0.007 |
| 3030.6962±0.0019 |
| 2886.9513±0.007 |
| 3030.6962±0.0019 |
| 2906.1724±0.007 |
| 3069.7478±0.0019 |
| 2906.1724±0.007 |
| 3069.7478±0.0019 |
| 2925.3952±0.007 |
| 3108.7876±0.0018 |
| 2925.3952±0.007 |
| 3108.7876±0.0018 |
| 2944.6172±0.007 |
| 3147.8113±0.0017 |
| 2944.6172±0.007 |
| 3147.8113±0.0017 |
| 2963.8408±0.008 |
| 3186.8147±0.0017 |
| 2963.8408±0.008 |
| 3186.8147±0.0017 |
| 2983.064±0.0019 |
| 3225.7934±0.0019 |
| 2983.064±0.0019 |
| 3225.7934±0.0019 |
| 3002.2885±0.008 |
| 3264.7438±0.0023 |
| 3002.2885±0.008 |
| 3264.7438±0.0023 |
| 3021.5133±0.0028 |
| 3303.6637±0.0028 |
| 3021.5133±0.0028 |
| 3303.6637±0.0028 |
|               | Kepler-9 b | Kepler-9 c | Kepler-9 b | Kepler-9 c |
|---------------|------------|------------|------------|------------|
| Kepler Data   | 3040.7391±0.0008 | 3342.5525±0.0033 | 3040.7391±0.0009 | 3342.5527±0.0033 |
|               | 3059.9661±0.0009 | 3381.4122±0.0038 | 3059.9661±0.0009 | 3381.4125±0.0038 |
|               | 3079.1937±0.0009 | 3420.2461±0.0042 | 3079.1936±0.0009 | 3420.2465±0.0042 |
|               | 3098.4237±0.0009 | 3459.0591±0.0044 | 3098.4236±0.001 | 3459.0595±0.0044 |
|               | 3117.6535±0.001 | 3497.8569±0.0046 | 3117.6535±0.001 | 3497.8573±0.0046 |
|               | 3136.8874±0.0011 | 3536.6458±0.0045 | 3136.8873±0.0011 | 3536.6462±0.0046 |
|               | 3156.1203±0.0011 | 3575.4325±0.0044 | 3156.1202±0.0012 | 3575.433±0.0044 |
|               | 3175.3589±0.0013 | 3614.2238±0.0042 | 3175.3589±0.0013 | 3614.2242±0.0043 |
|               | 3194.5957±0.0013 | 3653.0262±0.0039 | 3194.5956±0.0013 | 3653.0266±0.0034 |
|               | 3213.84±0.0015 | 3691.8462±0.0036 | 3213.8399±0.0015 | 3691.8466±0.0037 |
|               | 3233.0814±0.0016 | 3730.6898±0.0032 | 3233.0813±0.0016 | 3730.6902±0.0034 |
|               | 3252.3321±0.0018 | 3769.5617±0.0029 | 3252.332±0.001 | 3769.5621±0.0031 |
|               | 3271.5788±0.0019 | 3808.4654±0.0026 | 3271.5787±0.0019 | 3808.4658±0.0029 |
|               | 3290.8364±0.0021 | 3847.402±0.0005 | 3290.8363±0.0021 | 3847.4024±0.0008 |
|               | 3310.0887±0.0022 | 3886.3706±0.0026 | 3310.0886±0.0022 | 3886.3709±0.0029 |
|               | 3329.3532±0.0024 | 3925.3682±0.0027 | 3329.3531±0.0024 | 3925.3684±0.0031 |
|                | **Kepler Data** |                | **Kepler Data + Our New data** |
|----------------|-----------------|-----------------|-------------------------------|
|                | Kepler-9 b      | Kepler-9 c      | Kepler-9 b                     | Kepler-9 c                     |
| 3348.6114 ±0.025 | 3964.3903 ±0.003 | 3348.6113 ±0.025 | 3964.3905 ±0.0033             |
| 3367.8824 ±0.027 | 3367.8822 ±0.002 | ...             | 3387.146 ±0.002               |
| 3387.1461 ±0.028 | ...             | 3387.146 ±0.002 | ...                           |
| 3406.4227 ±0.029 | ...             | 3406.4226 ±0.002 | ...                           |
| 3425.6915 ±0.003 | ...             | 3425.6913 ±0.002 | ...                           |
| 3444.9726 ±0.031 | ...             | 3444.9724 ±0.003 | ...                           |
| 3464.2454 ±0.031 | ...             | 3464.2452 ±0.003 | ...                           |
| 3483.5297 ±0.032 | ...             | 3483.5295 ±0.003 | ...                           |
| 3502.8055 ±0.032 | ...             | 3502.8053 ±0.003 | ...                           |
| 3522.0915 ±0.032 | ...             | 3522.0913 ±0.003 | ...                           |
| 3541.3691 ±0.032 | ...             | 3541.3689 ±0.003 | ...                           |
| 3560.6554 ±0.032 | ...             | 3560.6552 ±0.003 | ...                           |
| 3579.9334 ±0.032 | ...             | 3579.9332 ±0.003 | ...                           |
| 3599.2184 ±0.031 | ...             | 3599.2182 ±0.003 | ...                           |
| 3618.4956 ±0.031 | ...             | 3618.4954 ±0.003 | ...                           |
| 3637.7779 ±0.003 | ...             | 3637.7776 ±0.003 | ...                           |
| Kepler Data |  | Kepler Data + Our New data |
|-------------|--------------------------|----------------------------|
|             | Kepler-9 b | Kepler-9 c | Kepler-9 b | Kepler-9 c |
| 3657.0529±0.003 | ... | 3657.0527±0.029 | ... |
| 3676.3309±0.029 | ... | 3676.3306±0.029 | ... |
| 3695.6024±0.028 | ... | 3695.6022±0.028 | ... |
| 3714.8748±0.027 | ... | 3714.8746±0.027 | ... |
| 3734.1418±0.026 | ... | 3734.1416±0.026 | ... |
| 3753.4075±0.026 | ... | 3753.4072±0.026 | ... |
| 3772.6688±0.025 | ... | 3772.6686±0.025 | ... |
| 3791.927±0.002  | 4  | 3791.9268±0.024  | ... |
| 3811.1821±0.023 | ... | 3811.1819±0.023 | ... |
| 3830.4326±0.022 | ... | 3830.4324±0.022 | ... |
| 3849.6811±0.021 | ... | 3849.6809±0.022 | ... |
| 3868.924±0.002  | ... | 3868.9238±0.021  | ... |
| 3888.1661±0.002  | ... | 3888.1659±0.002  | ... |
| 3907.4021±0.0019 | ... | 3907.402±0.0002 | ... |
| 3926.6383±0.0018 | ... | 3926.6382±0.0019 | ... |
| 3945.8686±0.0018 | ... | 3945.8684±0.0019 | ... |
### Table 1

|               |                       |               |               |               |               |
|---------------|-----------------------|---------------|---------------|---------------|---------------|
|               | Kepler-9 b            |               | Kepler-9 c    |               |               |
|               | 3965.0996±0.0017      | ...           | 3965.0995±0.0018 | ...           |               |
|               | 3984.3252±0.0017      | ...           | 3984.3251±0.0018 | ...           |               |

**Note.** The time is given as $B_{JDB} - 2454900.0$.

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## 3. Observations and Data Reduction

Using the predicted transit mid-times from our dynamical model, we coordinated observations of a transit of Kepler-9 b on UT 2016 September 1. We secured involvement of eight telescopes at four different observatories in China, all of which are members of the TEMP Network (Wang et al. 2017a). Planned observations from the Xinglong Station (2.16 m, 60/90 cm Schmidt, 85 cm, 80 cm, 60 cm telescopes), as well as from the Weihai Observatory (1 m telescope) were not executed due to the influence of Typhoon Lionrock. The weather at two other observatories, however, was generally cooperative on the transit night. One complete (Section 3.1) and one partial (Section 3.2) transit was obtained.

### 3.1. Nanshan Station, Xinjiang Observatory

We observed the full transit of Kepler-9 b in a Cousins- $R$ filter using the Nanshan One-meter Wide-field Telescope (hereafter, NOWT) at Nanshan Station (87°10'30"E, 43°28'24.66"N) of the Xinjiang Astronomical Observatory. The NOWT is equipped with a $4 \times 4$ K CCD that gives a 1°3 field of view (FOV) and a pixel scale of 1/″13 pixel$^{-1}$. For further details of this telescope, see Liu et al. (2014). A 1200 × 1200 pixel (approximately 22/″5 × 22/″5) subframe was used in our observations to shorten the readout time and increase the duty-cycle of the observations. In total, 554 scientific images were obtained with exposure times varying from 20 to 60 s depending on atmospheric conditions. To avoid adversely affecting the measurement of the transit mid-time, the exposure time was not varied during the transit ingress or egress phases. The recorded mid-exposure time in the image header is synchronized with the USNO time server and was converted to the $B_{JDB}$ timescale using the techniques of Eastman et al. (2010). The intrinsic error arising from these conversions is estimated to be less than 1 s.

All images were debiased and flat-fielded using standard procedures. Aperture photometry was then performed using the DAOPHOT aperture photometry routine (Stetson 1987). The final differential light curve was
obtained from weighted ensemble photometry. The choice of photometric comparison stars was made with the goal of minimizing the light-curve scatter. The resulting light curve (yellow-green points) is compared in Figure 2 to the best-fit model.

Figure 2. Transit light curves for Kepler-9 b, acquired on UT 2016 September 1 with the NOWT (yellow-green points) and NEOST (blue points) telescopes. The solid red line shows the best-fit model. The residuals of light curve from the best-fit model are plotted in the lower panel of the figure.

3.2. Xuyi Station, Purple Mountain Observatory

A portion of the transit of Kepler-9 b was also observed through an SDSS-i filter using the 1 m Near Earth Object Survey Telescope (hereafter, NEOST) located at the Xuyi astronomical station (118°28'E, 32°44'N) of the Purple Mountain Observatory of China. The telescope has a 10 K × 10 K CCD with 16 readout channels. No binning or windowing was used, resulting in a 3° × 3° FOV, and a pixel scale of 1″/029 pixel⁻¹.

We obtained 251 images at an observing cadence of ~77 s comprising a 60 s exposure time and a 17 s readout/reset time between exposures. Due to clouds, the observations were interrupted for about 30 minutes during the ingress phase, and the observations had to be stopped during the transit because of the elevation limits of the telescope.

The time recording approach and data reduction strategy were identical to the method used above (Section 3.1). The resulting light curve (blue points) is compared in Figure 2 to the best-fit model.
4. Light Curve Analysis

In order to accurately measure the transit mid-time of our new transit observation of Kepler-9 b, we performed a joint fit to the NOWT and NEOST light curves. The photometric modeling was carried out using JKTEBOP code (Southworth 2008), which employs Levenberg–Marquardt minimization to find the best fit, and a residual-permutation algorithm to determine the error estimates for the derived parameters. Due to the limited quality of our new ground-based light curve of the Kepler-9 b transit, a refinement of the system parameters was not a goal in this work. Moreover, while there are substantial variations in the transit mid-times, none of the other transit parameters for Kepler-9 b showed significant deviation over the 4-year duration of *Kepler* observations (Holman et al. 2010; Dreizler & Ofir 2014). Therefore, we estimated the mid-time of our new Kepler-9 b transit by allowing only the transit mid-time, $T_c$, as well as the light-curve specific base-line flux, $F_0$, to float, while holding the remaining parameters fixed. We fixed the basic transit parameters—the planet-to-star radius ratio, $R_p/R_*$, the scaled semimajor axis, $a/(R_* + R_p)$, and the orbital inclination, $i$,—at the best-fit values derived from the high-precision *Kepler* transit light curves (Twicken et al. 2016). We held the orbital period, $P$, and the two quantities $e \cdot \cos \omega$ and $e \cdot \sin \omega$ relating the eccentricity, $e$, and the argument of periastron, $\omega$, (which are typically poorly constrained by a single transit observation) fixed to the values determined from the TTV analysis described in Section 2. A limb-darkening law containing both a linear and a quadratic term was adopted, with coefficients fixed to the tabulated values $\mu_{1,R} = 0.37$ and $\mu_{2,R} = 0.28$, using the spectroscopic stellar parameters—effective temperature, $T_{\text{eff}} = 5779$ K, metallicity, $[\text{Fe/H}] = 0.12$, and surface gravity, $\log g = 4.491$,—from Huber et al. (2014).

The best fit to the new transit light curves for Kepler-9 b is plotted in Figure 2. The measured transit mid-time is $T = 2457633.219 \pm 0.026$, which is in good agreement with the transit mid-time derived using only the complete transit obtained with NOWT. (NEOST’s light curve alone, without sampling of the ingress and egress cannot be used for transit mid-time estimation.) Our new observations robustly reveal a transit event for Kepler-9 b, but as shown in Figure 3, the transit event occurs 45 minutes (1.2σ) later than predicted. We cannot claim a large significance for this discrepancy between the predicted and the observed transit mid-times for Kepler-9 b’s UT 2016 September 1 transit, as substantial systematic errors may have affected the determination of transit mid-time. There may be, however, some possible physical reasons for the 45 minute discrepancy. As our new observation occurred three years after the last *Kepler* observation, secular TTV drifts arising from an unknown stellar or planetary companion(s), may have contributed to the deviation. A similar conclusion was also reached by Dreizler & Ofir (2014) based on the substantial rms scatter in the Doppler...
velocity residuals of the Kepler-9 system, which are consistent with the possibility that it is harboring additional companions. Unfortunately, by adding only one new transit, we are unable to shed definitive light. The collection of further photometry and velocimetry would appear quite well advised.

Figure 3. Predicted mid-time vs. observed mid-time for Kepler-9 b's transit on UT 2016 September 1. It is unclear how such a ~45 minutes (1.2σ) discrepancy between prediction and observation could arise, although one possible source would be the secular TTV effect from an additional unknown companion or companions in the system. Further photometric and velocimetric observations of Kepler-9 system are recommended to help understand this discrepancy.

5. Improved Transit Predictions

As we have successfully observed the transit of Kepler-9 b on UT 2016 September 1 and obtained the transit mid-time by modeling the light curve, we refit the orbital parameters of Kepler-9 b and c based on transit mid-times from both Kepler data and our new data using the approach described in Section 2. With only one more transit observed, the re-derived parameters remained almost the same, aside from a small increase in uncertainties as shown in Table 1. The corresponding future transit mid-times also show little variation with those calculated with Kepler data only (Table 2).
6. Stellar Obliquity and Mutual Orbital Inclination

Although R–M observations of multi-transiting planetary systems may play a significant role in shaping the observed properties of exoplanets and distinguishing the competing formation scenarios for hot Jupiters, they are hard to make. The R–M effect is most easily observed when transits are deep and when the target star is bright. Multi-transiting planetary systems, however, usually involve smaller transit depths and fainter parent stars.

The Kepler-9 system, however, is an exception. It has a very large planet-star size ratio—among the largest ratios yet detected in multi-transiting planetary systems, and it is a proven target for obtaining high-precision radial velocities with 2.5 m s$^{-1}$ error using 45 minutes exposures with HIRESr on the Keck I telescope (Holman et al. 2010). Indeed, Kepler-9 may offer a rare to measure the spin–orbit angle of a multi-transiting planetary system. We have therefore made a detailed examination of the feasibility of carrying out R–M observations of Kepler-9 b and c using Keck/HIRESr.

This was done by first generating synthetic radial velocities of the R–M effect with added Gaussian noise, assuming both Kepler-9 b and c are in spin–orbit alignments. To span the transit with at least 10 observations, we set the length of each exposure to 20 minutes. This provides us with 11 and 12 radial velocities during the Kepler-9 b and c transits, respectively, with uncertainties of 5 m s$^{-1}$ (Burt et al. 2015), which is consistent with the radial velocity precision achieved by Holman et al. (2010) with Keck/HIRESr. The R–M effect-induced velocity anomaly is modeled using the analytical approach of Hirano et al. (2010) and is discussed in detail in Addison et al. (2013). The parameters used in the R–M effect modeling include: the spin–orbit angle, $\lambda$, the stellar rotation velocity, $v \sin i$, the planet-to-star radius ratio, $R_p/R_*$, the orbital inclination, $i$, the orbital period, $P$, the planet-to-star mass ratio, $m_p/M_*$, the orbital eccentricity, $e$, the argument of periastron, $\omega$, and two adopted quadratic limb-darkening coefficients, $\mu_1$, and $\mu_2$. $\lambda$ is set to 0, the spin of the star is modeled with $v \sin i = 2200$ m s$^{-1}$ (Buchhave et al. 2012), and the other parameters are set to the values given in Twicken et al. (2016) and Table 1 (parameters derived from Kepler data+ our new data). The predicted R–M anomalies for Kepler-9 b and c are shown in Figures 4 and 5 with half-amplitudes of 14.3 m s$^{-1}$ and 12.5 m s$^{-1}$, respectively.
**Figure 4.** Synthetic Keck/HIRESr radial velocities of the Kepler-9 b transit with an assumed $v \sin i = 2200$ m s$^{-1}$, $\lambda = 0$, and 20 minutes exposure ($\sigma_{rv} = 5$ m s$^{-1}$). The best-fit R–M effect is over-plotted as the dashed orange line. The bottom panel shows the residuals of the best fit. The spin-orbit angle of Kepler-9 b can be measured to $\pm 5.3^\circ$. 
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Figure 5. Same as Figure 4 but for Kepler-9 c. The spin–orbit angle of Kepler-9 c can be measured to ±6°3. The measurement of spin–orbit angles for two different planets in the same system, like Kepler-9, will provide us with a unique chance to directly measure their mutual orbital inclination (see Equation (1) for more details).

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After generating the synthetic radial velocities, we used the Exoplanetary Orbital and Simulation and Analysis Model (ExOSAM; see Addison et al. 2016) to fit the generated R–M observations to recover the spin–orbit angle and probe the level of uncertainty that can be measured. Gaussian distributions are assumed on the priors for Kepler-9 b and c, based on their best-fit parameter values and 1σ uncertainties given in Twicken et al. (2016) and Table 1 (parameters derived from Kepler data augmented by our new data). To determine the best-fit λ, we imposed a Gaussian prior on $v \sin i$ of 2200 ± 1000 m s$^{-1}$ (Buchhave et al. 2012).

We generated 20000 accepted MCMC iterations with an acceptance rate of 25%. This ensured good convergence and thorough mixing of the Markov chains. The mean and standard deviation of the MCMC chains were then
used to compute $\lambda$ and $\sigma_\lambda$, resulting in $-2^{0}5 \pm 5^{0}3$ and $-7^{0}5 \pm 6^{0}3$ for Kepler-9 b and c, respectively. The best-fit models to the simulated radial velocities are over-plotted in Figures 4 and 5. Our simulations strongly suggest that the spin-orbital angles of Kepler-9 b and c can be successfully measured with uncertainties less than 10 deg using Keck/HIRESr. The assessment of the degree of projected spin–orbit angles for two different planets in the same system, such as Kepler-9, will provide us with a unique chance to directly measure mutual orbital inclination $\delta$ through

$$\cos \delta = \cos i_b \cos i_c + \sin i_b \sin i_c \cos (\lambda_b - \lambda_c),$$

where $i_{b,c}$ and $\lambda_{b,c}$ are the orbital inclinations and the sky-projected spin–orbit angles for two planets, respectively.

In our own solar system, the major planets all lie within a few degrees of the ecliptic. This is compelling evidence that the solar system planets originated within a flat rotating disk. It is still unclear, however, whether other multiple-planet systems, especially those with significantly massive planets, also generally adhere to this organizational principle, because directly measuring mutual orbital inclination between the planets is challenging (Winn & Fabrycky 2015). Kepler-9 is a unique target to carry out the mutual orbital inclination measurement through measuring the spin–orbit angles for both Kepler-9 b and c, which will provides us the fundamental architectural data that will answer this critical question.

7. Summary and Conclusion

The Kepler-9 system imparts significant historical interest as a consequence of exhibiting the first observed exoplanetary TTVs. These inconstant eclipses confirmed the promise of the forward-looking analyses of Agol et al. (2005) and Holman & Murray (2005) and set the stage for many insights to emerge from the study of TTVs, culminating with mass estimates for the Earth-sized planets in the TRAPPIST-1 system by Gillon et al. (2017) and Wang et al. (2017b). In this paper, using both the full complement of Kepler photometry and a ground-based photometric recovery of the transit of Kepler-9 b, we have substantially improved the transit ephemerides for both planets b and c. These predictions will permit the accurate scheduling of follow-up measurements with large space-based or ground-based telescopes. We are thankful to the anonymous referee for providing helpful comments that greatly improved the manuscript.

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