Permanent Electric Dipole Moments of Alkaline Earth Monofluorides: Interplay of Relativistic and Correlation Effects

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The interplay of the relativistic and correlation effects in the permanent electric dipole moments (PDMs) of the X2Σ+ (ν = 0) electronic ground states of the alkaline earth monofluorides (BeF, MgF, CaF, SrF and BaF) has been studied using a relativistic coupled cluster method (RCCM). The calculations were carried out using double, triple and quadruple zeta basis sets, and with no core orbitals frozen. The results are compared with those of other calculations available in the literature and with experiments. The correlation trends in the PDMs of these molecules are discussed in detail.

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I. INTRODUCTION

In this work, we report the results of our calculations of the permanent electric dipole moments (PDMs) of the alkaline earth monofluorides (BeF, MgF, CaF, SrF and BaF) using a RCCM, and elucidate the trends in the correlation effects in the PDMs, as the molecules become progressively heavier, and consequently the relativistic effects get more pronounced. To the best of our knowledge, such a study involving the interplay of relativistic and correlation effects in molecules has not been performed earlier. The coupled cluster method is considered to be the current gold standard of electronic structure calculations for atoms and diatomic molecules [1]. It is suitable for calculating a number of static properties, including the PDMs of diatomic molecules [2]. The reasons for the choice of PDMs of the alkaline earth monofluorides are that this property has been calculated earlier using different approaches for this class of molecules [2–11] and high precision experimental data are available for some of these molecules [12–14]. Moreover, PDMs are important for various applications, especially SrF, which was the first molecule to be laser cooled [15], and for BaF, which is a promising candidate for probing fundamental physics [16–17].

II. THEORY

We discuss briefly the underlying ideas of the PDM of a molecule and the coupled cluster method. The details of both of these topics are discussed in detail elsewhere [2]. The PDM of a molecule, d, is given by:

\[
d = \frac{\langle \psi | D | \psi \rangle}{\langle \psi | \psi \rangle} = \langle \Phi_0 | e^{T_1} D_N e^{T_1} | \Phi_0 \rangle_C + \langle \Phi_0 | D | \Phi_0 \rangle_C = \langle \Phi_0 | e^{T_1} D_N e^{T_1} | \Phi_0 \rangle_C + \langle \Phi_0 | (- \sum_i e r_i + \sum_A Z_A e r_i) | \Phi_0 \rangle_C + \sum_A Z_A e r_A \langle \Phi_0 | \Phi_0 \rangle_C
\]

where \( \psi \) is the electronic wavefunction of the molecule, which is expressed as \( e^{T_1} | \Phi_0 \rangle \), in the coupled cluster method. \( | \Phi_0 \rangle \) is the model state, the Dirac-Fock (DF) wavefunction of the ground state of the molecule, which is built from single particle four-component spinors. T is the cluster operator. In the coupled cluster singles and doubles (CCSD) approximation, which we work with, \( T = T_1 + T_2 \), where \( T_1 \) and \( T_2 \) are the single and double excitation operators respectively. D is the electric dipole moment operator, e is the charge of the electron, summation over the electronic coordinates is indicated by i, and that over the nuclear coordinates by A. \( r_i \) is the position vector from the origin to the coordinate of an electron, and \( r_A \) is the position vector from the origin to the coordinate of a nucleus. \( Z_A \) is the atomic number of the \( A^{th} \) nucleus. The subscript \( C \) means that each term in that expression is connected [18, 19], and \( N \) refers to the normal ordered form of that operator [20]. Note that we have invoked...
the Born-Oppenheimer approximation in the fifth line of the equations given above.

The important aspects of our relativistic CCSD method are that we use the Dirac-Coulomb Hamiltonian, correlation effects have been taken into account to all orders in the residual Coulomb interaction for the one and two hole-particle excitations. The coupled cluster method is size extensive, unlike the truncated configuration interaction (CI) method [21].

For all the molecules considered in the present work, the origin is chosen to be the fluorine atom, and hence the PDMs can be expressed as

\[
d = \langle \Phi_0 | e^{T_1} D_N e^T | \Phi_0 \rangle_C \\
  + \langle \Phi_0 | (- \sum_i c r_i) | \Phi_0 \rangle_C + Z_A e r_e
\]  

(2)

where \( r_e \) refers to the equilibrium bond length for the molecule AF, with \( A = \text{Be, Mg, Ca, Sr or Ba} \). The first term captures the electron correlation effects, while the second is the electronic contribution from the DF calculations. The third gives the nuclear contribution. The PDM depends on the mixing of orbitals of opposite parity. This is naturally achieved in polar molecules, as their orbitals are hybridized.

III. METHODOLOGY

The molecular PDMs in the present work were calculated by combining the well known UTChem and DIRAC08 codes [22–24]. The DF calculations to generate the orbitals at the Self Consistent Field (SCF) level and the atomic orbital to molecular orbital integral transformations [27] were carried out using the UTChem code. The \( C_8 \) double group symmetry was used to reduce the computational cost [26]. The CCSD calculations were carried out in the DIRAC08 code, using the one and two electron integrals from UTChem. The electronic part of the PDM was calculated by using only the linear terms in the coupled cluster wavefunction, since their contributions are the largest [27].

\[
\langle \Phi_0 | (1 + T_1 + T_2)^\dagger (- \sum_i c r_i) N (1 + T_1 + T_2) | \Phi_0 \rangle_C \\
  + \langle \Phi_0 | (- \sum_i c r_i) | \Phi_0 \rangle \tag{3}
\]

In the above expression, the cluster amplitudes are obtained by solving the full CCSD equations containing the linear and the nonlinear terms. We add the nuclear contribution to the electronic part of the PDM using the experimental value for the bond length, wherever available. The values of the bond lengths used for BeF, MgF, CaF, SrF and BaF are 1.361, 1.75, 1.967, 2.075 [3, 28] and 2.16 [3, 24] Angstrom respectively.

The details of the basis sets used for our computations are given below in Table I. We used uncontracted Gaussian type basis sets (GTOs) in all our calculations. We also imposed the kinetic balance [30] condition for all the basis sets. For Sr and Ba, we used the exponential parameters taken from the four-component basis sets obtained by Dyall [31], and added to it diffuse and polarization functions from the Sapporo-DKH3 [32] basis sets. We used the exponential parameters of cc-pV (correlation consistent-polarized valence) basis sets from the EMSL Basis Set Exchange Library [33, 34] for Be, Mg, Ca and F.

| Atom | Basis |
|------|-------|
| Be   | cc-pVDZ: 9s, 4p, 1d |
| Mg   | cc-pVTZ: 11s, 5p, 2d, 1f |
| Ca   | cc-pVDZ: 9s, 4p, 1d |
| Sr   | Dyall+Sapporo: 20s, 14p, 6d |
| Ba   | Dyall+Sapporo: 30s, 25p, 15d |
| F    | cc-pVDZ: 9s, 4p, 1d |

TABLE I: Details of the basis sets used

IV. RESULTS AND DISCUSSIONS

Table II gives the results of our calculations of energies of the molecules and their PDMs at DF and CCSD levels. The values for the PDMs have been rounded off to the second decimal place.

We observe that the absolute value of the correlation energy increases as the molecules get heavier, that is, as the relativistic effects get more pronounced. In each of the molecules BeF, MgF, and CaF, the PDM decreases at the DF level as we move from DZ through the QZ basis sets, while for BaF, the PDM oscillates. For a given molecule, the CCSD values of this quantity increase progressively as the size of the basis set is enlarged. Also, the CCSD results for the PDM converge, that is, the difference between the QZ and the TZ basis set PDMs are less than that between TZ and DZ, except for BaF. This may either be due to the correlation being inadequate or due to insufficient optimization of the basis sets. The PDM increases from BeF to SrF, that is, the PDM increases as a system becomes more relativistic, but drops slightly for BaF. We also see that the absolute value of the correlation effects monotonically increase as we go to
more relativistic systems, with MgF being an exception. The effect of correlation is 0.2 D for BeF, whereas it is 0.75 for BaF. The $T_2$ contributions, for all the CCSD calculations and for all the basis sets used, was about 0.02 for all the molecules, except BaF, for which it was 0.01. This is an indicator of the stability of our reference calculations. Our calculated values of the PDM at the QZ level differ from experiment by about 3, 4 and 7 percent for CaF, SrF and BaF respectively.

We tabulate the electronic (at the CCSD level, with QZ basis sets) and nuclear contribution to the PDM for the 5 molecules in Table III. We see from Table III that the absolute values of the electronic and the nuclear terms increase with the size of the molecules. The nuclear contribution, which is positive, 'overtakes' the electronic contribution, which is negative, as the molecules get heavier, up to SrF.

We now consider the ratio of the electronic terms to the nuclear terms. Their absolute values from BeF to BaF, 0.96, 0.97, 0.98, 0.99 and 0.99 respectively. The ratio for BaF is higher than that for SrF, with the difference occurring in the third decimal place. To understand correlation trends, we consider the contributions from each of the 9 terms in Eq. 3.

We observe that the largest contribution to the PDM comes from the DF term. The $T_1^D$ term, which embodies important pair correlation effects [1] contributes the most, among the correlation terms, in the heavier molecules, starting from CaF, and increases from CaF to BaF. It is, however, not significant for BeF and MgF. The $T_1^D$ term steadily increases from BeF to BaF. Also, the term changes sign as it increases with the size of the molecule. Furthermore there are cancellations between the various correlation effects. The fractional contributions of the correlation effects increase from lighter to heavier elements, except in the case of BeF. It is largest in the case of BaF for which the value is 0.22.

We have given below the comparison of our results with previous calculations and experiment. The first calculations on the PDM of some of the alkaline earth monofluorides were carried out by Torring et al [8]. They used an ionic model to calculate the PDMs of MgF, CaF, SrF and BaF. They compare their results with the Rittner model [37] and experiment (wherever available) in their work. Childs et al experimentally determined the PDM of CaF to be 3.07(7) D in their work [12] in the same year. In 1985, the PDM of SrF was measured, using a molecular beam microwave double resonance method [14]. Rice et al [4] used the Ligand field approach (LFA) to obtain a value of 3.01 D for CaF, later that year. The PDM of BaF was measured to be 3.170 (3) by Ernst et al in the subsequent year [13]. The first ab initio calculations on select alkaline earth monofluorides were performed by Langhoff

| Molecule | Method | Basis | $E(\text{au})$ | PDM (D) |
|----------|--------|-------|----------------|---------|
| BeF      | DF     | cc-pVDZ | -114.07       | 1.32    |
|          | DF     | cc-pVTZ | -114.23       | 1.31    |
|          | DF     | cc-pVQZ | -114.26       | 1.30    |
|          | CCSD   | cc-pVDZ | -114.38       | 0.93    |
|          | CCSD   | cc-pVTZ | -114.59       | 0.06    |
|          | Expt   |        | -114.67       | 1.10    |
| MgF      | DF     | cc-pVDZ | -299.51       | 3.21    |
|          | DF     | cc-pVTZ | -299.52       | 3.21    |
|          | DF     | cc-pVQZ | -299.57       | 3.16    |
|          | CCSD   | cc-pVDZ | -299.96       | 2.84    |
|          | CCSD   | cc-pVTZ | -300.02       | 3.02    |
|          | CCSD   | cc-pVQZ | -300.11       | 3.07    |
| Expt     |        | -      | -              | -       |
| CaF      | DF     | cc-pVDZ | -779.31       | 2.89    |
|          | DF     | cc-pVTZ | -779.33       | 2.82    |
|          | DF     | cc-pVQZ | -779.37       | 2.77    |
|          | CCSD   | cc-pVDZ | -780.09       | 3.01    |
|          | CCSD   | cc-pVTZ | -780.21       | 3.13    |
|          | CCSD   | cc-pVQZ | -780.31       | 3.16    |
| Expt     |        | -      | -              | 3.07(7) |
| SrF      | DF     | cc-pVDZ | -3277.87      | 2.83    |
|          | DF     | cc-pVTZ | -3277.70      | 2.95    |
|          | DF     | cc-pVQZ | -3277.74      | 3.01    |
|          | CCSD   | cc-pVDZ | -3278.85      | 2.95    |
|          | CCSD   | cc-pVTZ | -3279.01      | 3.42    |
|          | CCSD   | cc-pVQZ | -3279.13      | 3.60    |
| Expt     |        | -      | -              | 3.4676(1) |
| BaF      | DF     | cc-pVDZ | -8235.25      | 2.42    |
|          | DF     | cc-pVTZ | -8235.27      | 2.28    |
|          | DF     | cc-pVQZ | -8235.31      | 2.65    |
|          | CCSD   | cc-pVDZ | -8236.55      | 2.69    |
|          | CCSD   | cc-pVTZ | -8236.71      | 3       |
|          | CCSD   | cc-pVQZ | -8236.82      | 3.40    |
| Expt     |        | -      | -              | 3.170(3) |

TABLE II: Summary of the calculated results of the present work

| Molecule | Electronic term | Nuclear term |
|----------|----------------|--------------|
| BeF      | -25.05         | 26.15        |
| MgF      | -97.80         | 100.87       |
| CaF      | -185.81        | 188.97       |
| SrF      | -375.16        | 378.76       |
| BaF      | -577.64        | 581.04       |

TABLE III: Electronic (at the CCSD level, with QZ basis sets) and nuclear contributions to the PDM for all the alkaline earth monofluorides

We observe that the largest contribution to the PDM comes from the DF term. The $T_1^D$ term, which embodies important pair correlation effects [1] contributes the most, among the correlation terms, in the heavier molecules, starting from CaF, and increases from CaF to BaF. It is, however, not significant for BeF and MgF. The $T_1^D$ term steadily increases from BeF to BaF. Also, the term changes sign as it increases with the size of the molecule. Furthermore there are cancellations between the various correlation effects. The fractional contributions of the correlation effects increase from lighter to heavier elements, except in the case of BeF. It is largest in the case of BaF for which the value is 0.22.

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They employed extended Slater basis sets augmented with diffuse and polarization functions. They calculated the PDMs using the single reference configuration interaction singles and doubles (CISD) and the coupled pair functionals (CPF) methods. The CISD method does not take into account certain higher order correlation effects that are present in the CCSD method. The CPF approach is a size consistent version of CISD, but the treatment is non-relativistic. Also, not all the electrons are correlated in these calculations. Mestdagh et al [6] used an electrostatic polarization model (EPM) for calculating the PDMs of MgF, CaF, SrF and BaF, among other molecules. Bundgen et al [7] employed the multireference-configuration interaction (MRCI) approach, with the singles and doubles excitations taken into account, to compute the PDM of CaF. They used Gaussian basis sets, and a total of 17 electrons were correlated in their calculations. Allouche et al [8] used the LFA, in 1993, to calculate the PDMs of Ca, Sr and Ba monohalides. Buckingham et al [9] used Second order Moller-Plesset perturbation theory (MP2) to calculate PDMs of BeF, MgF and CaF. In CCSD, the single and double excitations to all orders of perturbation are taken care of. So, we believe that CCSD can capture correlations better at a finer level. Also, their calculations are non-relativistic. The work by Kobus et al [10] was to compare the electric moments obtained from finite basis set with finite difference Hartree-Fock (FD-HF) calculations. In an earlier work [2], we had tested the accuracy of our RCCM by computing the PDM of the SrF molecule. Sasmal et al [11] improved upon our result of SrF in their work, which involved implementing the Z vector approach in a RCCM.

The possible sources of errors in our calculations stem from the higher order terms neglected, and the choice of basis sets. If we add up the individual terms that make the PDM (other than the DF, DT1 and its conjugate), we see that the highest sum is from BaF, which is -0.05 D. It is reasonable to assume that the neglected higher order terms do not exceed this value, and we set a conservative estimate of ±0.1 D.

The error from the choice of basis sets can be estimated by taking the difference between the QZ and the TZ PDMs. They are 0.04, 0.05, 0.03 and 0.18 for the first four alkaline earth monofluorides. We set a conservative error of ±0.1 D for BeF, MgF and CaF, and ±0.2 D for SrF. The PDM doesn’t converge at the QZ level for BaF, so we cannot determine the error due to incompleteness of the basis here. However, we can roughly estimate the error to be about 0.2 D, based on comparison with a preliminary investigation that has been carried out using a larger basis based on the same method that we have used in our calculations [38].

For SrF and BaF, we have used a combination of Dyall’s and Sapporo’s basis for Sr and Ba. These contain in them diffuse and polarization functions, just as Be, Mg and Ca had these functions via cc-pV. In order to see the trends across the alkaline earth monofluorides, we have to assume that the results do not change significantly, whether we use cc-pV basis or a combination of Dyall and Sapporo basis. The error from this assumption is tested using CaF at the QZ level, since Ca is the only atom in the candidate molecules for which both Dyall and cc-pV basis sets were available. We obtain a PDM of 2.84 and 3.23 D at the DF and the CCSD levels, respectively, when we use Dyall plus Sapporo basis for CaF. Earlier, we obtained, using cc-pVQZ for Ca, 2.77 and 3.16 D at the DF and CCSD levels, respectively. The difference is about 2.5 percent at DF and 2.2 at CCSD. Since we can’t tell how this may vary for the heavier molecules, we can conservatively set an error percentage of about 5, due to the change in the choice of basis sets for the molecules.

### V. CONCLUSIONS

We calculated the PDMs of the alkaline earth monofluorides, up to BaF, using a RCCM, with no core orbitals...
frozen in our calculations. We used uncontracted cc-pV and Dyall+Sapoor basis sets for our calculations. We reported the DF and CCSD energies and the PDMs. Our results, using QZ basis sets, are in good agreement with the experimental results, wherever available. We have examined the electronic and nuclear contributions to the PDMs for all the molecules considered, as well as the importance of the individual correlation terms. The results we obtained suggest that as the molecules get heavier, that is, as the relativistic effects increase, the correlation effects get larger in size. We also provided a rough estimate of the errors in our calculations, caused by ignoring higher order terms and from the basis sets. We also give a rough estimate of the error in comparing the PDMs as we move from BeF through BaF, due to the choice of basis sets being different for the two heaviest monofluorides.

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