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B2 ordering in body-centered-cubic AlNbTiV refractory high-entropy alloys

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The phase stability of a bcc AlNbTiV high-entropy alloy at elevated temperatures is studied using a combination of machine-learning interatomic potentials, first-principles calculations, and Monte Carlo simulations. The simulations reveal a B2 ordering below about 1700 K, mainly caused by a strong site preference of Al and Ti. A much weaker site preference for V and Nb is observed, strongly affecting the alloys total configurational entropy. The underlying mechanisms of the B2 phase stability as opposed to the random solid solution are discussed in terms of a high persisting configurational entropy of the B2 phase due to strong sublattice site disorder.

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I. INTRODUCTION

After refractory high-entropy alloys were proposed a decade ago by Senkov et al. [1–3], there has been recent interest in exploring the possibility of so-called refractory high-entropy superalloys (RSAs) [4]. These are multicomponent alloys, often referred to as compositionally complex or high-entropy alloys, containing refractory elements and featuring dual-phase microstructures with disordered bcc A2 and ordered B2 phases. This combination could result in improved mechanical properties as provided for their fcc Ni-superalloy counterpart. Given the relevance of conventional superalloys for manifold technological applications, the huge compositional phase space provided by the RSA design strategy promises tremendous opportunities for exploring and designing alternative alloys.

Often Al is added to form a B2 phase in bcc refractory multicomponent alloys. This has beneficial side effects, such as reducing the alloy density and improving oxidation resistance. Various potential RSAs have been found in the last decade featuring dual A2+B2 phases [5] (see also Ref. [4] for a recent overview). Among them are various Al-containing refractory multicomponent alloys. The B2 phase formation in Al-containing bcc multicomponent refractory alloys is, however, still intriguing, since in many Al binaries with refractory elements, B2 phases are typically not observed.

For this reason, conventional thermodynamic databases are often not suitable to predict B2 phase formation in Al-containing bcc refractory multicomponent alloys due to scarce B2 formability of the sub-binaries in these alloys. Experimental identification of B2 is also often challenging. In bcc MoCrTiAl, it has been shown that interpreting x-ray diffraction patterns is not sufficient to identify a potential B2-type crystal structure [6]. Another example is bcc AlNbTiV, which first has been characterized as a disordered A2 phase [7,8]. Due to the mentioned challenges, a thermodynamic analysis utilizing the Calphad approach [9] corroborated this initial assessment [8]. However, later experimental analyses [10,11] have shown that bcc AlNbTiV features a single B2 phase over a wide temperature range. Based on earlier studies on Ti alloys, it was suggested [11] that Al and Nb as well as Ti and V occupy the two sublattice sites, i.e., B2(Al,Nb)(Ti,V). However, the underlying mechanism stabilizing the B2 phase as well as the detailed site occupancies still remain unclear. One hypothesis is that a considerable sublattice disorder may still be present, thus stabilizing the B2 phase in these multicomponent alloys [4].

In this work we systematically investigate the B2 ordering in the prototypical bcc AlNbTiV alloy by performing an extensive first-principles-based investigation. Specifically, we employ density-functional theory (DFT) calculations in combination with a machine-learning potential [12–14] and Monte Carlo simulation to investigate the short-range order and phase stability. The presence of a B2 phase, in particular, the site occupancies and underlying reasons for the thermodynamic stability, are discussed.

II. METHOD AND COMPUTATIONAL DETAILS

Simulations are performed employing the low-rank interatomic potential (LRP) [12] method. This is an on-lattice machine-learning potential, particularly suited to fit multi-component alloys [12] and which has been also recently utilized to study chemical short-range order in bcc NbMoTaW...
The LRP s are fitted to density-functional theory calculations which have been carried out employing the VASP code [15–18]. The projector augmented wave (PAW) method [19] within the Perdew-Burke-Ernzerhof generalized gradient approximation (PBE-GGA) [20] has been used.

To include the impact of volume expansion, the temperature expansion has been computed based on a Debye-Grueneisen model [21]. For this the total energy of the random alloy, $E(V)$, its bulk modulus and the bulk modulus derivative are computed based on a $4 \times 4 \times 4$ (128-atom) special quasi-random structure (SQS) [22]. The derived zero-K and predicted room-temperature lattice constants are 3.187 and 3.200 Å, being close to the reported experimental value [7,11].

To include the impact of thermal expansion, the calculations for fitting the LRP s are conducted at a lattice parameter of 3.23 Å, corresponding to the computed value at around 1000 K. Note that the computation of more accurate vibrational free energies such as, e.g., performed in Refs. [23,24], may quantitatively alter the computed phase transition temperature, but is beyond the scope of the present work.

A plane-wave cutoff energy of 450 eV has been chosen. The $k$-point meshes generated by the Monkhorst-Pack [25] scheme were set to $2 \times 4 \times 4$, $5 \times 5 \times 5$, and $5 \times 5 \times 5$ for supercell sizes of $8 \times 4 \times 4$, $4 \times 4 \times 4$, and $5 \times 5 \times 5$ (containing 256, 128, and 250 atoms, respectively), corresponding to $kp$ densities of 8192, 8192, and 16,000 $kp$ atom. The convergences for the electronic minimization and relaxation conditions. The $a_1$ 4 supercells based on the two-atom primitive bcc cell) with periodic boundary conditions. The burn-in approach [26] was used, neglecting the first half of MC steps for each temperature value and thus improving the robustness of the algorithm. For temperatures higher than 2100 K, $2 \times 10^7$ MC steps and for all other temperatures $2 \times 10^6$ MC steps were chosen, where each MC step represents one swap attempt for every atom (see Appendix). For the MC simulations utilized to generate the set for retraining, 250 and 256 atoms ($5 \times 5 \times 5$ and $8 \times 4 \times 4$ supercells) were chosen.

**III. RESULTS AND DISCUSSION**

We first discuss the specific heat capacity, $C_V(T)$, as obtained from the MC simulations. The results are shown in Fig. 1. The accuracy of the retrained LRP s is exemplified by the shaded area, which represents twice the standard deviation of the MC results from the ten independently fitted potentials. The observed peak at around 1700 K indicates a phase transition which is identified as an A2-B2 transition further below. This B2 phase is stable down to about 550 K. The increase in $C_V(T)$ for temperatures below 800 K indicates another phase transition at around 500–550 K. A preliminary inspection of a MC snapshot at 480 K (not shown) indicates a decomposition, into (at least) two phases, one enriched in V. We do not discuss here the phase stability at lower temperatures, as this would be beyond the scope of the present work. The observed range of B2 stability is also consistent with annealing experiments at 1273 K [10] and 1473 K [11], where a B2 phase has been reported.
FIG. 2. (a), (b) Snapshot of the employed supercells from the Monte Carlo simulations for the B2-ordered alloy (at 600 K) for two side views. (c), (d) Top and side view for a fully random solid solution. The B2 ordering in (a, b) is mainly driven by Al (red) and Ti (blue), whereas Nb and V (light red and light blue) reveal a weaker sublattice site preference. Figures created by OVITO [27].

To elucidate the ordering, we present in Figs. 2(a) and 2(b) a snapshot from a MC simulation at 600 K featuring a B2 ordering and as comparison in (c, d), an example for an ideal random solid solution. In contrast to the completely random state at high temperatures, a B2 ordering is clearly visible in Fig. 2(a), driven mainly by Al (red) and Ti (blue) atoms.

To explore the ordering tendencies more quantitatively, we discuss next the first- and second-shell pair-correlation parameters, often referred to as the Warren-Cowley short-range order (SRO) parameters [28] as derived from the MC simulations,

\[
\alpha_{ij}^{m} = 1 - \frac{p_{ij}^{m}}{c_i c_j},
\]

where \(\alpha_{ij}^{m}\) is the Warren-Cowley SRO parameter for atom \(i\) and \(j\) in the \(m\)th shell, \(p_{ij}^{m}\) is a probability of finding atom \(j\) at the \(m\)th shell of atom \(i\), and \(c_i, c_j\) are the total concentrations of the \(i\) and \(j\) elements in the alloy. Vanishing \(\alpha\) values describe the random alloy, a positive value indicates clustering or segregation, and negative values indicate attraction of \(i\) and \(j\) atoms.

The SRO parameters, directly related to the pair-correlation parameters according to Eq. (1) above, are shown for the first and second shell in Figs. 3(a) and 3(b), respectively. Most striking is the strong positive (attractive) Al-Ti SRO parameter for the first shell and negative (repulsive) one in the second shell (both in blue). This clearly underlines that the main contribution to SRO above the ordering temperature is driven by favorable Al-Ti pairs in the first and repulsive ones in the second shell, consistent with a B2 ordering. Below 1700 K, an increasing probability for Al-V and Ti-Nb in the first shell and Al-Nb as well as Ti-V favorable pairs for the second shell are found. This indicates the tendency for enrichment of Al and Ti sites with Nb and V, respectively.

In order to explore the underlying site occupations in more detail, we analyzed the local chemical concentration of the elements on the two sublattice sites of the B2 phase [see sketch in Fig. 4(a)]. The sublattice occupations can be interpreted as an order parameter for the B2 phase (see, e.g., Ref. [29] for a recent application to a bcc high-entropy alloy). The results for one of the sublattice sites are shown in Fig. 4(b). The site occupancies clearly reflect a B2 ordering setting at around 1700 K. In particular, Al and Ti are driving the site occupations. At about 1000 K, Al is almost completely occupying one of the sublattices, whereas Ti is completely depleted, occupying mainly the other sublattice site (not shown here). As found for the SRO parameters, there is also the tendency for Nb to mix on the Al and for V to mix on the Ti sites. The enrichment of the AI sites with Nb and Ti with V is, however, over a wide temperature range very weak. For example, at 1000 K, where Al already occupies one sublattice site with over 49%, the Nb and V concentration on this Al-rich site is about 30% and 20%. This implies a strong sublattice disorder.

FIG. 3. Warren-Cowley parameters \(\alpha_{ij}^{m}\) (related to the pair-correlation parameters) for the (a) first \((m = 1)\) and (b) second shell \((m = 2)\) from Monte Carlo simulations for bcc AlNbTiV. A strong Al-Ti attraction in the first shell and repulsion in the second shell is present, also in the solid solution at high temperatures. Shaded areas indicate twice the standard deviation provided by the ten independent LRPs.

FIG. 4. (a) Sketch of the B2 structure with two sublattices indicating the sublattice occupations. (b) Site occupancies for one of the sublattices at 1700 K.
FIG. 4. (a) Sketch for a B2 ordering with distinct sites 1 and 2. (b) Sublattice occupation of the Al-rich site in the B2 phase derived from Monte Carlo simulations for AlNbTiV. The B2 ordering is mainly driven by Al and Ti, with a tendency for Nb to mix on the Al sublattice and for V to mix on the Ti sublattice. Shaded areas indicate twice the standard deviation provided by the ten independent LRPs.

and hence a considerable configurational entropy persisting in the B2 phase. To elucidate the impact of the persisting sublattice disorder in the B2 phase on the phase stability we computed the configurational entropy. This has been done by integrating $C_V(T)$ from high temperatures and subtracting it from the known limit of the random solid solution. The results are shown in Fig. 5. Consistent with the sublattice occupation, we find a relatively large configurational entropy of the B2 phase, mainly driven by the intermixed Nb and V atoms on the sublattices. To put the results into perspective, we also show the configurational entropy of the ideal random solid solution, of an ideal B2(AlNbV)(TiNbV) phase, and of an ideal B2(AlNb)(TiV) phase. The latter two scenarios provide two idealized B2 scenarios, with Nb and V having no site preference, and with Nb and V completely occupying Al and Ti sites. Indeed, the computed entropy at 1000 K is close to the scenario of a B2(AlNbV)(TiNbV) phase with almost no site preference of Nb and V. It is also about 50% larger as compared to the entropy of an ideal B2(AlNb)(TiV) phase, where Nb and V are occupying only Al and Ti sites, respectively. This can have important consequences in modeling the configurational entropy and interpreting experiments. For example, in [11] the local ordering in bcc AlNbTiV has been analyzed by assuming a B2(AlNb)(TiV) sublattice ordering. For bcc AlTiVCr [30], a B2(AlCr)(TiV) phase has been ad hoc assumed in atomistic simulations due to the lack of further SRO information. However, as shown in the present case, such assumptions could largely overestimate the configurational entropy contribution and thus bias the predicted phase transition temperature. In fact, various bcc multicomponent alloys including Al and Ti have been proposed in the last years, among them, e.g., bcc AlNbTiV, AlHfNbTi, AlHfTiTi, and AlMoNbTi, all of which show a single B2 phase [6,11,31]. Given the similarity in these alloys, it is possible that similar strong sublattice disorder may also persist in the observed B2 phase in these alloys.

IV. CONCLUSION

Chemically complex bcc alloys, containing A2-B2 dual-phase structure, may open the way to design refractory high-entropy superalloys. The B2 phase stability plays therefore a crucial role. The underlying reason for the B2 phase stability in these Al-containing refractory alloys has been unclear, and detailed sublattice ordering information were, however, lacking so far. We employed a combination of first-principles informed, machine-trained interatomic potentials and Monte Carlo simulations to investigate the ordering and phase stability of the prototypical bcc AlNbTiV alloy. A single B2 phase is revealed below 1700 K, mainly driven by Al and Ti, with a weak tendency for Nb and V enrichment on the Al and Ti sites. As a result, the derived configurational entropy is about 50% larger than one may intuit from an ad hoc assumed B2(AlNb)(TiV) scenario. Given the many proposed bcc multicomponent alloys containing Al and Ti, the obtained insights of the present study may be also valid...
for various other alloys too, highlighting the significant role of detailed SRO and phase stability explorations for modeling and designing Al-containing bcc concentrated complex alloys.

The datasets generated during the current study are available from the corresponding author on reasonable request.

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