Full optical characterization of single nanoparticles using quantitative phase imaging

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This paper introduces a procedure aimed to quantitatively measure the optical properties of nanoparticles, namely the complex polarizability and the extinction, scattering, and absorption cross sections, simultaneously. The method is based on the processing of intensity and wavefront images of a light beam illuminating the nanoparticle of interest. Intensity and wavefront measurements are carried out using quadriwave lateral shearing interferometry, a quantitative phase imaging technique with high spatial resolution and sensitivity. The method does not require any preknowledge on the sample and involves a single interferogram image acquisition. The full determination of the actual optical properties of nanoparticles is of particular interest in plasmonics and nanophotonics for the active search and characterization of new materials, e.g., aimed to replace noble metals in future applications of nanoplasmonics with less-lossy or refractory materials. © 2020 Optical Society of America under the terms of the OSA Open Access Publishing Agreement

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1. INTRODUCTION

Nanoparticles (NPs) featuring localized plasmon or Mie resonances have been extensively studied for plasmonics and nanophotonics applications to achieve light confinement at nanoscale [1], enhancement [2,3], scattering [4], heat generation [5], SERS [6], and phase control [7,8]. For these applications, a large variety of materials including highly doped semiconductors [9], oxides, nitrides [10–12], alkali metals [13,14], alloys/intermetallics [15–18], and dielectrics [19], have been proposed recently. Quantifying the optical responses of all these NPs and comparing them with each other is intricate and remains the main issue for the search of better optical materials. To quantitatively estimate the efficiency of a material, or of a NP, simple figures of merit [20] or analytical models can be used for simple geometries, or numerical simulations for complex geometries and environments. However, the material is modeled via its bulk complex permittivity, usually measured on material layers. This approach proved efficient with gold, but may be inappropriate when considering NPs made of other materials, where surface effects dominate or where surface oxidation occurs [21], or for alloys where the theoretical determination of the effective permittivity is not straightforward [22,23].

The optical characterization of individual NPs usually consists in measuring cross sections, which is all the more difficult when the NP is downsized. To effectively extract signal out of noise, most of the experimental techniques are based on the spatial modulation (SM) of a focused laser beam associated with a lock-in detection. Arbouet et al. introduced the SM technique in 2004 to quantitatively retrieve the extinction cross section (σ_{ext}) of single NPs as small as 5 nm in diameter [24]. This approach is quantitative only when absorption is dominant over scattering, since it neglects the portion of scattered light that is not collected. In practice, quantifying only extinction is not enough to fully characterize the optical properties of NPs. Other experimental procedures have been designed to retrieve scattering (σ_{sca}) or absorption (σ_{abs}) cross sections as well [25,26], although these quantities are more difficult to access and to be quantitatively measured. The Link’s group reported in 2010 quantitative measurements of both absorption and scattering cross sections of single NPs using two separate techniques, namely dark-field spectroscopy and another SM technique called photothermal imaging [27]. SM techniques have been used to measure absorption and scattering cross sections originating this time from the same signal [28,29]. Recently, the use of an integrating sphere implemented upon an optical microscope has been demonstrated to enable absorption and scattering measurements on single NPs [30,31]. The main drawbacks of all these techniques are that they require expensive equipment such as lasers, modulating elements, and lock-in amplifiers, and they are sensitive to optical alignments. The analysis procedures are also complex and often based on a precise knowledge of the point spread function of the microscope [32]. These drawbacks make SM techniques impractical for routine characterization of NPs [31]. Very recently, Zilli et al. introduced a technique aimed to measure all the optical cross sections of individual NPs at once, which is not based on the...
use of a focused laser and SM measurements [32]. The technique aims to be simple and requires only a wide-field illumination, a camera, and a standard optical microscope. It consists in successively acquiring and postprocessing bright-field and dark-field images of single NPs. This technique requires a precise characterization of the collection properties of the microscope objective lens.

Even more fundamental than the three cross sections is the complex optical polarizability. For instance, for a dipolar NP, the sole knowledge of its complex optical polarizability \( \alpha \) enables the derivation of all the cross sections of the NP at once [33]:

\[
\sigma_{\text{ext}} = \frac{k_0}{n} \text{Im} (\alpha), \tag{1}
\]

\[
\sigma_{\text{sca}} = \frac{k_0^3}{6\pi} |\alpha|^2, \tag{2}
\]

\[
\sigma_{\text{abs}} = \sigma_{\text{ext}} - \sigma_{\text{sca}}, \tag{3}
\]

where \( k_0 \) is the free-space wavevector and \( n \) is the refractive index of the surrounding medium of the NP. Moreover, \( \alpha \) does not only quantify the magnitude of the optical response, but also its phase, a physical quantity of utmost importance in plasmonics [34], or for the design of metasurfaces and meta-atoms [7,8].

Previous studies aiming at retrieving the polarizability of NPs have been reported. Davis and Carney determined the anisotropic polarizability using coherent confocal microscopy [35]. This method allows the estimation of the complex polarizability tensor and the position of the NP. However, the implementation of this method is complex in both the used experimental setup as well as the polarizability retrieval procedure. Celebrano et al. determined the amplitude and the phase of the response of single plasmonic particles by combining far-field and near-field imaging [36], but did not measure polarizabilities. Stoller et al. reported in 2006 on the measurements of the complex dielectric constant of gold NPs using a differential interference contrast technique [37]. But it only applies for small nanospheres and relies on the preknowledge of the NP diameter.

In this paper, we introduce a procedure based on quantitative phase microscopy aimed at quantifying the full optical properties of a NP, namely its complex dipolar polarizability and all the optical cross sections at once. First, we introduce the experimental approach and some experimental imaging concepts, such as the normalized complex transmission image. Then, we introduce the theoretical model to explain how to process intensity and phase images to retrieve the NP optical properties. Finally, we illustrate the procedure with measurements on gold and dielectric NPs, and compare with numerical simulations. We finally highlight the robustness of the technique by showing that the measurements are dependent neither on the microscope focus nor on the objective’s numerical aperture (NA).

2. EXPERIMENTAL METHOD

Optical images of particles were acquired using a bright-field transmission microscope and a quadrifocal lateral shearing interferometry (QLSI) camera [38] to map the complex transmittance \( t \) of the sample containing the NPs. QLSI image measurements result from the prior acquisition of a reference image \( (h_0) \), at a free location, before acquiring a transmission image \( (t) \) at the location of the object of interest [39]. The normalized transmission image \( t/h_0 \) is then computed as a means to get rid of any imperfection of the optics of the microscope and of the illumination. We define the normalized complex transmission image \( t/h_0 \) as

\[
\frac{t}{h_0}(x, y) = \frac{\tilde{t}(x, y)}{T(x, y)} e^{-\frac{2\pi}{k_0} \delta T(x, y)}, \tag{4}
\]

where \( T(x, y) \) is the transmittance image of the sample and \( \delta T(x, y) \) is the wavefront distortion caused by the presence of the particle or, equivalently, the optical path difference (OPD). \( k_0 = 2\pi/k_0 \) is the wavelength of the incoming light in vacuum. QLSI enables the mapping of both \( T \) and \( \delta T \) from a single interferogram image (see Fig. S1 in Supplement 1). As an example, we show in Fig. 1 the measured intensity \( T \) and wavefront distortion \( \delta T \) images and their profiles for a 100 nm gold NP embedded in a homogeneous medium. These two images contain the information required to retrieve all the optical properties of the particle, as introduced in the next section.

3. THEORETICAL MODEL

Let us consider a particle, located at \( r_0 \), excited by an incoming electric field \( E_{\text{inc}} \) oscillating at the frequency \( \omega \). The resulting oscillating electric dipole \( p \) reads

\[
p = \varepsilon_0 \alpha E_{\text{inc}}(r_0), \tag{5}
\]

where \( \tilde{\alpha} = (\alpha_{ij})_{i, j \in \{x, y, z\}} \) is the complex electric dipolar polarizability tensor. If one considers \( E_{\text{inc}} \) as a plane wave propagating along \( z \) and polarized along \( x \), then left-multiplying Eq. (5) by \( E_{\text{inc}}^\star \) yields

\[
\alpha_{\text{xx}} = \frac{1}{\varepsilon_0 |E_{\text{inc}}(r_0)|^2} E_{\text{inc}}^\star(r_0) \cdot p. \tag{6}
\]

For larger particles, Eq. (6) cannot be used as \( E_{\text{inc}}(r) \) is not necessarily uniform within the particle. Yet, one can still formally define what we shall coin here the generalized polarizability along the direction of \( E_{\text{inc}} \) following Eq. (6), as

\[
\tilde{\alpha} = \frac{1}{\varepsilon_0 |E_{\text{inc}}|^2} \iiint V E_{\text{inc}}^\star(r) \cdot P(r) \, dr, \tag{7}
\]
where \( P \) is the polarization density field within the particle, defining the domain of integration \( \mathcal{V} \). This expression only assumes that \( \mathbf{E}_{\text{inc}} \) corresponds to a linearly polarized plane wave, so that \( |\mathbf{E}_{\text{inc}}| \) is uniform. The benefit of extending the definition of \( \alpha \) this way is twofold. (i) The expression Eq. (1) of the extinction cross section using the generalized polarizability Eq. (7) is valid, and is no longer restricted to dipolar NPs, since one retrieves the general expression well known from the discrete dipole approximation (DDA) [40],

\[
\sigma_{\text{ext}} = \frac{k}{n_\mathcal{V}} |\mathbf{E}_{\text{inc}}|^2 \iint \mathcal{V} (\mathbf{E}_{\text{inc}}^*(\mathbf{r}) \cdot \mathbf{P}(\mathbf{r})) \, d\mathbf{r}. \tag{8}
\]

(ii) The quantity defined by Eq. (7) is what we can measure experimentally from intensity and phase images processing. In Supplement 1, we demonstrate that the polarizability of a particle, as defined by Eq. (6) or Eq. (7), can be calculated from its image intensity and phase images of the polarizability of any single NP by a processing of the intensity and phase images (PIWI) using

\[\alpha = \frac{i\lambda_0 n}{\pi} \sum \left[ 1 - \int_{-\infty}^{\infty} \exp \left( \frac{2\pi i}{\lambda_0} \right) \right] \text{pxSize}^2. \tag{10}\]

For the sake of simplicity, this expression assumes a NP embedded in a homogenous medium with a refractive index \( n \), albeit not a requirement. Thus, one can retrieve the real and imaginary parts of the polarizability of any single NP by a processing of the intensity \( I(x, y) \) and wavefront \( \delta \ell(x, y) \) images (PIWI) using

\[
\alpha_r = \frac{\lambda_0 n}{\pi} \iint \sqrt{I(x, y)} \sin \left( k_0 \delta \ell(x, y) \right) \, dx \, dy, \tag{11}\]

\[
\alpha_i = \frac{\lambda_0 n}{\pi} \iint \left[ 1 - \sqrt{I(x, y)} \cos \left( k_0 \delta \ell(x, y) \right) \right] \, dx \, dy. \tag{12}\]

No assumption is necessary regarding the composition (dielectric, metallic, etc.) of the NP or its shape. Only the preknowledge of the refractive index of the medium, \( n \), and the illumination wavelength \( \lambda_0 \) are required, two easily accessible parameters. Using Eq. (1) of the extinction cross section as a function of \( \alpha \), one gets

\[
\sigma_{\text{ext}} = 2 \iint \left[ 1 - \sqrt{I(x, y)} \cos \left( k_0 \delta \ell(x, y) \right) \right] \, dx \, dy. \tag{13}\]

Importantly, this expression is valid for any particle, not necessarily dipolar. This can be derived from the optical theorem, as shown in Supplement 1. PIWI is thus capable of determining \( \alpha \) and \( \sigma_{\text{ext}} \) for any NP of any composition and geometry, without any preknowledge. However, the estimation of the scattering and absorption cross sections using Eqs. (2) and (3) remains an approximation, even using the generalized complex polarizability. In practice, the approximation yields correct estimations for NP sizes until typically 100 nm.

### 4. RESULTS

#### A. Metal and Dielectric Nanospheres

In order to illustrate the applicability of the PIWI method, we first present measurements on metal and dielectric spherical NPs, at \( \lambda_0 = 530 \) nm. This simple, isotropic geometry allows us to easily compare our measurements with numerical simulations. Colloidal gold nanospheres of 100 nm in diameter and polystyrene nanospheres of 200 nm in diameter were dispersed on a glass substrate and then covered by glycerol as a means to obtain a homogeneous medium of refractive index 1.5.

An example of measured intensity and OPD images of gold and polystyrene NPs is shown in Fig. 2(a). The measured polarizabilities using PIWI are displayed in the complex plane in Fig. 2(b). Each point corresponds to the polarizability of one NP. The measured polarizabilities for different NPs occupy two separate domains of the complex plane [Fig. 2(a)], associated to gold and polystyrene nanospheres (orange and blue points, respectively). For comparison, we also plot on the same space the calculated complex polarizabilities using DDA for a 100 nm gold nanosphere and a 200 nm polystyrene nanosphere (with gold permittivities taken from Johnson and Christy’s dataset [41] and PS permittivities from Ref. [42]). Furthermore, by using the same images, we also extracted the extinction, scattering, and absorption cross sections of the same NPs using PIWI, and compared them with numerical values [Fig. 2(c)], showing a good agreement. Note that the scattering cross section is weak compared with absorption, despite the dielectric nature of the particles, because the particles are immersed in glycerol, leading to a good refractive index matching and making them quasi-transparent. The dispersion in the measured values of the polarizability and the cross sections mainly arises from the dispersion in NP diameters and sometimes shapes (see Fig. S4 in Supplement 1). The measurement errors reported in Figs. 2(d) and 2(e) mainly stem from the shot noise on the camera sensor. Error bars are not displayed in Figs. 2(b) and 2(f) for the sake of readability, but they are displayed in Fig. S6 of Supplement 1.

Spectral measurements of the complex polarizability of 100 nm gold NPs over the entire visible range are shown in Figs. 2(d) and 2(e), with a good agreement with numerical simulations. The imaginary part (proportional to extinction cross section) presents a peak around \( \lambda_{\text{res}} = 510 \) nm, associated with an abrupt transition of the values of \( \text{Re}(\alpha) \), which corresponds to the localized surface plasmon resonance (LSPR) wavelength. From these measurements, optical cross sections were computed using Eqs. (1)–(3) and displayed in Fig. 2(f). The agreement with DDA simulations is good for the extinction cross section. This is consistent with the underlying theory of the experimental approach, which predicts quantitative \( \sigma_{\text{ext}} \) measurements, without approximation, for any NP size. The rule does not apply for \( \sigma_{\text{abs}} \) and \( \sigma_{\text{sca}} \), for which measurements may deviate from actual values when retardation effects occur. This presumably explains the small deviation between experiments and simulation in the blue–green region of the spectra for \( \sigma_{\text{ext}} \) and \( \sigma_{\text{abs}} \) observed in Fig. 2(f).

#### B. Asymmetric Particles

We focus now on the case of anisotropic particles for which the polarizability depends on the illumination polarization angle, to illustrate the versatility of the method. We studied gold nanorods fabricated by nanosphere lithography (see Supplement 1 for more details on the fabrication process) on a glass substrate covered with...
Fig. 2. (a) Intensity and OPD images of 100 nm gold and 200 nm polystyrene beads acquired by QLSI at $\lambda_0 = 530$ nm. Gold and polystyrene are indicated with orange and blue arrows, respectively (100 x magnification; 1.3 NA; scale bar, 2 µm). (b) Extracted polarizabilities using PIWI for gold and polystyrene NPs. Squares represent DDA numerical simulations for gold nanoparticles 100 ± 8 nm in diameter, and PS nanoparticles 200 ± 16 nm in diameter. (c) Extracted extinction, scattering, and absorption cross sections compared to theoretical values given DDA. Experimental (d) real and (e) imaginary parts of the polarizability of a 100 nm Au nanosphere determined by PIWI (circles), and compared with DDA simulations (solid lines). (f) Cross sections determined from the measured polarizabilities reported in (d) and (e) (circles), and compared with DDA (solid lines).

Fig. 3. (a) Measured longitudinal (orange dots) and transverse (blue dots) polarizabilities of a set of gold nanorods compared with theoretical longitudinal (circle symbol) and transverse (square symbol) polarizabilities of nanorods with dimensions of $120 \times 50 \times 50$ nm$^3$ in a medium of $n = 1.5$. (b) and (c) Examples of the intensity and OPD images of the nanorods at two different polarization states (100 x magnification, 1.3 NA).

C. No-Effect of the Numerical Aperture and Focus

The effect of the defocus when recording the intensity and OPD images is shown in Fig. 4(a). As expected, the Airy patterns vary substantially as a function of the focus, with even a contrast inversion for the OPD image above and below the focus plane [43]. Yet,
the real and imaginary parts of the polarizability extracted from the intensity and OPD images do not depend on the focus, as shown in Fig. 4(b), and as shown theoretically in Supplement 1 (Section 2). This property makes the measurements particularly robust, since they are independent of any thermal drift of the microscope over time or of any precise focusing of the image.

The effect of the objective’s NA is presented in Fig. 4(c). Again, although the diffraction patterns are highly dependent on this parameter [Fig. 4(c)], it surprisingly does not affect the real and imaginary parts of the polarizability extracted using Eq. (10), as plotted in Fig. 4(d). This property is derived in Supplement 1. Again, this independence of the particular objective NA makes the measurements of particle polarizabilities using PIWI particularly robust. No care has to be used regarding the quality of the image and the focus.

5. CONCLUSION

We reported in this article an experimental method allowing the retrieval of the complex polarizability and optical cross sections of NPs, in a single image acquisition without any assumption on their nature and geometry. The measurements depend neither on the focus of the microscope nor on the NA of the objective lens, making the measurements particularly robust. The complex optical polarizability is measured quantitatively with no assumption, no matter the composition or shape of the particle, and without preknowledge on the system. Absorption and scattering cross sections are only measured approximatively, with a satisfactory estimation for particle sizes typically below 100 nm. This technique is envisioned to become a standard in metrology for nanophotonics, for instance for the active search and characterization of new materials with relevant properties for heterogeneous chemistry, photovoltaics, biosensing, or thermoplasmonics.

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See Supplement 1 for supporting content.

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