INDUCED ROTATION IN THREE-DIMENSIONAL SIMULATIONS OF CORE-Collapse SUPERNOVAE: IMPLICATIONS FOR PULSAR SPINS

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ABSTRACT

It has been suggested that the observed rotation periods of radio pulsars might be induced by a non-axisymmetric spiral-mode instability in the turbulent region behind the stalled supernova bounce shock, even if the progenitor core was not initially rotating. In this paper, using the three-dimensional Adaptive Mesh Refinement code CASTRO with a realistic progenitor and equation of state and a simple neutrino heating and cooling scheme, we present a numerical study of the evolution in three dimensions of the rotational profile of a supernova core from collapse, through bounce and shock stagnation, to delayed explosion. By the end of our simulation (∼420 ms after core bounce), we do not witness significant spin-up of the proto-neutron star core left behind. However, we do see the development before the explosion of strong differential rotation in the turbulent gain region between the core and stalled shock. Shells in this region acquire high spin rates that reach ∼150 Hz, but this region contains too little mass and angular momentum to translate, even if left behind, into rapid rotation for the full neutron star. We also find that much of the induced angular momentum is likely to be ejected in the explosion, and moreover that even if the optimal amount of induced angular momentum is retained in the core, the resulting spin period is likely to be quite modest. Nevertheless, induced periods of seconds are possible.

Key words: hydrodynamics – pulsars: general – supernovae: general

Online-only material: color figures

1. INTRODUCTION

One of the key questions associated with radio pulsars is the origin of their spin periods (Lorimer 2009, 2010). In two recent papers (Blondin & Mezzacappa 2007, hereafter BM07; Blondin & Shaw 2007), it has been suggested that the growth in three dimensions of an $\ell = 1$ non-axisymmetric ($\ell = \{-1, 1\}$) spiral mode (Fernàndez 2010) of the so-called standing accretion shock instability (SASI) during the post-bounce delay phase seen in current supernova theory can spin up matter in the turbulent region behind the stalled shock. BM07 and Blondin & Shaw (2007) find that the accretion of this spinning matter (and its associated angular momentum) onto the inner core can spin up the nascent neutron star to rotation periods that compare favorably with the observed/inferred values for pulsars at birth. More precisely, they report final periods of ∼70 ms for moderately rotating progenitors and ∼50 ms for non-rotating progenitors. The measured period range of birth periods is from ∼10 ms to seconds, with an average “injection period” near ∼0.5 s (Chevalier & Emmering 1986; Narayan 1987).3

If this mechanism were to obtain, it would obviate the need to invoke a spinning progenitor core. However, rotation is a natural feature of stars, and there is no obvious reason the progenitor “Chandrasekhar” mass in the center of a massive star at death would not be rotating with the spins and angular momenta needed to leave a compact object with the measured spin frequencies (Ott et al. 2006a, 2006b). This is a function of the angular momentum distribution in the cores of massive stars when they collapse (Heger et al. 2005; Maeder & Meynet 2000, 2004; Hirschi et al. 2004). Hence, the possibility that the three-dimensional dynamics of the core itself could generate countervailing flows with opposite signs of angular momentum, “one stream” of which could leave the residue spinning at interesting rates while conserving overall angular momentum, is intriguing. If this were true, to zeroth order all cores at collapse could be non-rotating, and the spins could be a function of collapse dynamics alone. This would eliminate one of the current ambiguities in massive-star progenitor models, whose core spins at collapse are not observable. The progenitor cores could all be born with “zero” angular momentum, while giving birth to proto-neutron stars with respectable spins.

However, BM07 and Blondin & Shaw (2007) employed various simplifications in their simulations. They did not follow collapse itself, but started in a steady-state post-bounce configuration. They used a simple “gamma-law” equation of state (EOS), and not a full nuclear EOS. They set the mass accretion rate through the shock to a constant value and did not perform their simulations in the context of a realistic massive-star progenitor. Importantly, they excised the inner core whose very spin-up was being studied. Rather, they inferred from ostensible accretion of matter and angular momentum at their inner boundary an irreversible accumulation of spin in the proto-neutron star. Finally, they did not consider the potential role of the supernova explosion itself on the magnitude of the residual angular momentum and final induced core period. They did, however, investigate the potential role of initial rotation in the final outcome.

In this paper, we investigate the claims of BM07 and Blondin & Shaw (2007), improving upon their study in several ways. Our three-dimensional simulation is described in Nordhaus et al. (2010b) and was carried out using CASTRO (Almgren et al. 2010), an Eulerian Adaptive Mesh Refinement (AMR) hydrodynamics code with hierarchically nested rectangular grids that are refined both in space and time. We employed a realistic

3 The inferred initial spin period of the Crab pulsar is 15–16 ms (Atoyan 1999), but the average for radio pulsars is considerably longer.
EOS (Shen et al. 1998a, 1998b) and a simple neutrino transfer scheme (see Nordhaus et al. 2010b; Murphy & Burrows 2008). Both Nordhaus et al. (2010b) and Murphy & Burrows (2008) incorporated the Liebendörfer (2005) prescription for electron capture on infall and a simple neutrino heating and cooling algorithm after bounce. The driving electron and anti-electron neutrino luminosities were kept constant at $1.9 \times 10^{52}$ erg s$^{-1}$. This enabled us to heat the so-called gain region (Bethe & Wilson 1985) and investigate the pre-bounce infall, bounce, post-bounce delay, and explosion phases. In this simulation (model 3d:L$_{1.9}$ of Nordhaus et al. 2010b), a neutrino-driven explosion occurred approximately $\sim 200$–$250$ ms after bounce and we carried the simulation out to $\sim 420$ ms after bounce. Our initial model was the 15 $M_\odot$ solar-metallicity, non-rotating red-supergiant model of Woosley & Weaver (1995). An important aspect of our simulation is that the proto-neutron star itself is at all times present on the grid (which is Cartesian) and is followed throughout the run in a hydrodynamically consistent fashion.

The cubic grid in our simulations extended to $10^4$ km on each side, with $304^3$ cubic cells covering the grid’s volume at its coarsest level. Three levels of refinement of a factor of four in each dimension were followed. As a result, the resolution in the central regions (the inner 200 km) was $\sim 0.5$ km. The monopole approximation for self-gravity was adopted.

By the end of our simulation, we find that there is almost no spin-up of the proto-neutron star. During the post-bounce phase and before explosion, the region exterior to the core and interior to the shock ($\sim 60$ to $\sim 250$ km) does witness the growth of spiral modes, some spin-up (to $\sim 150$ Hz), and the emergence of countervailing rotational flows. However, the explosion ejects not only mass, but its associated angular momentum, and depending upon where the mass cut is finally imposed, the residual core can end up with some net rotation. In our most optimistic scenario the core achieves a period of only 1.2 s. This fastest possible spin does not alone seem adequate to explain the measured and/or inferred pulsar birth periods without significant initial rotation in the progenitor itself. In Section 2, we present our quantitative results and follow in Section 3 with an extended discussion and our summary conclusions.

2. RESULTS

2.1. Profiles and Temporal Evolution of Angular Momentum

We begin our analysis by calculating the amount of angular momentum present in our computational domain. We divide the innermost 2000 km of the grid into concentric spheres of increasing radius and monitor the magnitude of each of the three components ($x$, $y$, and $z$) of the angular momentum ($L_i$) enclosed within each sphere for the duration of the calculation after core bounce. The panels in Figure 1 depict three-dimensional surface representations of the temporal evolution of the three orthogonal components of the total angular momentum enclosed within a certain radius, as a function of that radius. Such panels summarize what we find in our simulation. As Figure 1 indicates, we do indeed see an initial increase of angular momentum, but only between $\sim 60$ km and $\sim 250$ km, and quasi-oscillatory behavior with a period near $\sim 30$ ms. The innermost zones that might be identified with the proto-neutron star are not spun up to periods faster than $\sim 5$–$10$ s. At later times (the last 0.17 s after bounce), we note that the angular momentum that originally resided in this inner region is ejected with the exploding mass and follows the outward progress of the re-energized shock. This ejected angular momentum “bump” can also be seen clearly in Figure 2, where we show the spatial profile of all three components of angular momentum for four different times near the end of our simulation. We address the subsequent fate of this ejected angular momentum in Sections 2.3 and 3. At the end of our simulation, very little angular momentum is left in the central region of our grid, indicating that the inner core is left rotating very slowly. At the final time step, the spin periods in the inner 10 km are all greater than $\sim 10$ s. Note that the flatness of the regions in Figure 1 at large distances demonstrates that total angular momentum is very well conserved during the simulation. In CASTRO, angular momentum is not conserved by construction, so that its global conservation during this
Figure 2. Total angular momentum enclosed within a spherical radius \( R \) and its evolution with time after bounce, for four different time steps. The three panels correspond to the three components of the angular momentum vector (\( x \), \( y \), and \( z \) components from top to bottom, respectively). Lines of different color indicate different post-bounce times during the simulation. We note again (as in Figure 1) an initial increase of the angular momentum components between \( \sim 60 \) and \( \sim 200 \) km. With time, much of the angular momentum is ejected with the exploding mass. This can be seen here in the propagating angular momentum “bump.” As discussed in the text and also in the captions to Table 1 and Figure 7, this ejected angular momentum, if actually all accreted onto the neutron star at later time, would induce a rotational period no faster than 1.2 s.

(A color version of this figure is available in the online journal.)

Figure 3. Temporal evolution (in seconds after bounce) of the average specific angular momentum (\( \ell_i \), vertical axes) of spherical shells at various enclosed spherical radii (\( R \), in centimeters). \( R \) is logarithmically distributed. From top to bottom, the three panels correspond to the \( x \)-, \( y \)-, and \( z \)-component of the specific angular momentum. To determine the averages, the computational grid was divided into thin spherical shells of width 1 km within the inner 250 km of the grid and of width 10 km for radii between 250 and 2000 km. The two-dimensional surfaces under each upper surface are projections of the upper surfaces, with the color variation indicating the value of the projected point, going from black (negative) to white (positive) through a scale of red shades. The propagation outward at later times of the induced angular momentum is manifest in these panels as well.

(A color version of this figure is available in the online journal.)

simulation is encouraging. Specifically, before and after bounce the total angular momentum of matter on the grid is conserved to better than \( \sim 1\% \), staying very near “zero” for the duration of the calculation.

Next, we divide our grid into thin spherical shells that cover the innermost 2000 km of the computational domain. For the inner 250 km the width of the shells was chosen to be 1 km, and for radii between 250 and 2000 km the width was increased to 10 km. For each of the shells we calculated the average specific angular momentum (\( \ell_i \), not the total enclosed angular momentum), for all three components of the angular momentum. Figure 3 depicts their associated spatial and temporal profiles. As discussed above and can be seen in Figures 1 and 2, regions interior to \( \sim 200 \) km experience some growth of specific angular momentum during the earlier stages after core bounce, whereas the specific angular momentum at larger radii remains close to zero until after the onset of explosion. As Figure 3 makes clear, the sign of the specific angular momentum for each component varies with time and radius, conserving total angular momentum after bounce to high precision. After the onset of explosion, angular momentum is seen to propagate outward with the ejected mass and the shock wave.

An interesting feature is observed for radii between 60 and 250 km. As time progresses in the simulation, the magnitudes of the specific angular momenta on shells in this region grow with time, indicating that in this region there is indeed some spin-up
by the spiral mode identified in BM07, Blondin & Shaw (2007), and Fernández (2010). We proceed in Section 2.2 with a discussion of this phenomenon and the associated spin periods.

2.2. Rotational Period and Frequency Profiles

Having calculated the angular momentum contained in spherical shells at various radii, we proceed to extract the rotational profiles of those shells. Figure 4 shows the temporal evolution of the average spin frequency (\(f_i\), in Hz) of each shell, for rotation around the \(x\), \(y\), and \(z\) axes (the three panels in Figure 4). We see that shells with radii \(R < 60\) km and \(R > 250\) km do not develop any significant rotational motion during the entire simulation. However, at the very early times after core bounce and for radii between \(\sim 60\) km and \(\sim 250\) km in the shocked, turbulent regions, some rotational motion does develop, which with time is amplified. By the end of the simulation, those shells have acquired spin frequencies that reach \(\sim 150\) Hz at a radius of \(\sim 100\) km, corresponding to a spin period of \(\sim 7\) ms. Furthermore, we note that although at early post-bounce times the sign of the spin vector of those shells kept flipping (as indicated by the positive and negative frequency values shown in Figure 4), at the end of the simulation neighboring shells tended to align their rotational motion. The left panel of Figure 5 depicts the velocity field on a ball at radius 90 km near the end of the simulation. As this figure clearly shows, coherent fields of rotation have emerged in this region (see also the panels in Figure 4). Near the same final time, the shock has been launched into explosion and has the multi-turbulent morphology portrayed in the right panel of Figure 5 as an isentropic surface.

In Figure 6 we show the temporal evolution of the magnitude of the specific angular momentum (top) for various shells at different radii and the corresponding magnitude of the rotational frequency (bottom) of those shells. As in Figure 4, the development of rotational motion from \(\sim 60\) to \(\sim 250\) km is obvious and the high spin rate of \(\sim 150\) Hz in this narrow range of radii is manifest. However, there is very little mass (\(\sim 0.01–0.03\) \(M_\odot\)) and, hence, total angular momentum in this fastest spinning region, and this has major consequences for the spin evolution of the entire residual neutron star.

2.3. Rotational Periods for the Final State

Our simulation shows not only that the inner core is not spun up significantly, but that the mass that does experience an interesting degree of induced rotation is likely to be ejected with the subsequent blast. An interesting question arises associated with this ejected angular momentum “bump,” shown in Figures 1 and 2. If that angular momentum were to be accreted later on onto the central regions (in a “fallback” scenario for angular momentum), what would that imply for the terminal rotation rate of the nascent neutron star? We address this issue by applying various mass cuts to the final state of our simulation. We calculate the total angular momentum enclosed within a given spherical mass cut (given in Column 2 of Table 1) and then divide it by a representative moment of inertia for the final-state neutron star (taken to be \(2 \times 10^{45}\) g cm\(^2\) and assuming solid-body rotation) to derive a final angular frequency. Our results are summarized in Figure 7 and Table 1. For a range of mass cuts between 1.2 and 1.6 \(M_\odot\) (baryonic) for our “1.9 \times 10^{52}\) erg s\(^{-1}\) explosion model, the final inferred rotational periods vary between 1.2 and 47 s (as can be seen in Figure 7). The fastest inferred period of 1.2 s is seen for a spherical mass cut of 1.53 \(M_\odot\) baryonic. Note that many measured neutron-star masses are near 1.35 \(M_\odot\) gravitational, which translates into \(\sim 1.5\) \(M_\odot\) baryonic.

Apart for the magnitude of such final-state rotational periods, we would also like to know the direction of rotation and how that varies with the different spherical mass cuts. We define two angles to describe the direction of the total angular momentum enclosed within a certain mass cut. Angle \(\theta\) (\(0^\circ \leq \theta \leq 180^\circ\)) is the polar angle, measured with respect to the \(x\)-axis and the \(\phi\) (\(0^\circ \leq \phi \leq 360^\circ\)) is the azimuthal angle, defined with respect to the \(z\)-axis. The last two columns of Table 1 show the values of \(\theta\) and \(\phi\) for the different mass cuts. The direction of the angular momentum varies little for spherical mass cuts from \(\sim 1.2\) to \(\sim 1.4\) \(M_\odot\). However, as Table 1 indicates, it does show significant variation for mass cuts in the range 1.45–1.6 \(M_\odot\).
Figure 5. Left: velocity vector field profile on a spherical shell of radius 90 km toward the end of the simulation (∼370 ms after core bounce). Both the size and color of the vectors represent the magnitude of the velocity field, with darker (lighter) shades corresponding to higher (lower) values. Right: three-dimensional rendering of an isentropic surface with entropy equal to $10^8$ baryon$^{-1}$. The colormap represents the magnitude of the entropy gradient on the surface, with values increasing going from orange to purple. The surface spans 1600 km and corresponds to a time 380 ms after core bounce.

(A color version of this figure is available in the online journal.)

Figure 6. Temporal evolution (in seconds) of the magnitude of the specific angular momentum (top) and of the magnitude of the rotational frequency (bottom) of spherical shells at various spherical radii $R$ (in centimeters, shown logarithmically). As discussed in the caption to Figure 4 and in the text, individual shells at radii $60 \text{ km} < R < 250 \text{ km}$ develop significant rotational frequencies over time. However, outside this range of radii the rotation induced by non-axisymmetric instabilities is quite modest at all times during the simulation.

(A color version of this figure is available in the online journal.)

3. DISCUSSION AND CONCLUSIONS

In this paper, we have studied the temporal and spatial evolution of the rotational profile of a newly formed neutron star. The goal was to test the possibility that the remnant neutron star created in the context of core-collapse supernova could be

![Figure 5](image1.png)

![Figure 6](image2.png)

![Figure 7](image3.png)

Table 1

| Spherical Mass Cut (Baryonic) ($M_\odot$) | $L$ ($10^{45}$ g cm$^2$ s$^{-1}$) | $P$ (s) | $f$ (Hz) | $\theta$ (°) | $\phi$ (°) |
|---------------------------------------|---------------------------------|--------|---------|-------------|---------|
| 1.20                                  | 0.501                           | 2.50   | 0.40    | 97.6        | 67.2    |
| 1.25                                  | 0.531                           | 2.37   | 0.42    | 92.1        | 67.5    |
| 1.30                                  | 0.479                           | 2.83   | 0.35    | 89.7        | 70.5    |
| 1.35                                  | 0.380                           | 3.30   | 0.30    | 96.7        | 84.2    |
| 1.40                                  | 0.252                           | 4.99   | 0.20    | 111.6       | 272.3   |
| 1.45                                  | 0.125                           | 10.17  | 0.1     | 152.5       | 0.25    |
| 1.50                                  | 0.619                           | 2.02   | 0.49    | 128.6       | 51.6    |
| 1.55                                  | 0.790                           | 1.59   | 0.63    | 21.6        | 5.3     |
| 1.60                                  | 0.027                           | 46.89  | 0.02    | 125.5       | 191.9   |

Note. *At $t = 0.422$ s after core bounce; in Column 1, we list various spherical mass cuts. The total angular momentum enclosed within that mass is given in Column 2. If this enclosed angular momentum were to be left with the nascent neutron star, which we assume to have a moment of inertia of $I \sim 2 \times 10^{45}$ g cm$^2$, then the resulting rotational periods and frequencies would be those presented in Columns 3 and 4, respectively. The direction of the total enclosed angular momentum $L$ for each case is represented by two angles given in the last two columns. The polar angle $\theta$ ($0^\circ \leq \theta \leq 180^\circ$) is defined with respect to the $y$-axis and the azimuthal angle $\phi$ ($0^\circ \leq \phi \leq 360^\circ$) is measured with respect to the $z$-direction.
induced to rotate rapidly due to the growth of a spiral, non-axisymmetric mode of the so-called SASL, even if the progenitor was initially non-rotating. We employed the three-dimensional hydrodynamics code CASTRO to carry out the simulation, starting from the infall phase of a 15 $M_\odot$ non-rotating progenitor and followed the core bounce, convection, and explosion stages. The core, whose induced rotation was being studied, was included fully on the computational grid, a realistic EOS was used, and a simple neutrino heating and cooling algorithm enabled us to simulate in approximate fashion the turbulent post-bounce delay and subsequent explosive phases. Our main findings are as follows.

1. We did not find that a significant spin rate was induced in the nascent neutron star. By the end of our simulation the inner core is seen to rotate very slowly, with spin periods no faster than $\sim 5\text{--}10$ s.

2. However, in the unstable gain region between the shock and the inner core ($60 \text{ km} < R < 250 \text{ km}$), counter-rotating shells can acquire enough specific angular momentum during the stall phase before explosion that they can achieve interestingly high spin rates, reaching frequencies around $\sim 150 \text{ Hz}$ (Figure 4) and spin periods between $\sim 6$ and $\sim 100 \text{ ms}$. However, the mass in this region and the corresponding angular momentum are rather low.

3. At the later stages in the evolution of our simulation, the explosion and ejecta transport angular momentum outward behind the exploding shock wave. Even if some of this angular momentum were to fall back at later times, the minimum spin period that the residual neutron star could achieve is likely to be quite modest (Figure 7 and Table 1).

Blondin & Mezzacappa (2007) employed a gamma-law EOS, did not follow the hydrodynamics of the inner core, did not include in their simulations the collapse or the explosion phases, and did not include any neutrino interactions. Yet, they concluded that even a non-rotating progenitor could in principle leave behind a rotating remnant. In this qualitative conclusion we agree with Blondin & Mezzacappa (2007).

However, we used a general nuclear EOS, included the entire core all the way to the center in the hydrodynamic simulation, included in a crude fashion the effects of neutrino heating, cooling, and electron capture, and followed both the collapse and the explosion phases. What we found was that the degree of induced central rotation of the residual proto-neutron star, after explosion and for any given degree of fallback, produces periods between $\sim 1$ and $\sim 10$ s. Nevertheless, those authors suggest that a longer delay could lead to even greater net spin rates and see in their simulation a significant ramp up from $\sim 0.4$ to $\sim 0.9$ s after bounce. However, they concede that the spiral-mode spin-up phenomenon should not continue beyond the onset of explosion. Since our explosion occurs near $\sim 250 \text{ ms}$, one could argue that a longer delay could result in a larger induced spin. While this seems plausible, Wongwathanarat et al. (2010) have performed a new set of approximate three-dimensional simulations of core-collapse supernovae with non-rotating progenitors, focusing on the remnant neutron star kick velocities (see also Nordhaus et al. 2010a). They also show that after as much as $\sim 1.4$ s after bounce the induced spin rates are still fairly low, with final periods in the range $\sim 500$ to $\sim 1000 \text{ ms}$. Such long periods are approximately in accord with those we derive here in our “optimum” case.

In summary, the increase in the spin rate from the optimum derived from our simulation, which terminated at $\sim 0.422$ s, to that seen in the simulations of Wongwathanarat et al. (2010), which terminated at $\sim 1.4$ s, was a factor of $\sim 2$. The calculations performed by Blondin & Mezzacappa (2007) implied that the enhancement in delaying from $\sim 0.422$ s to $\sim 0.9$ s might be a factor of $\sim 10$ or more. We take this as a further indication that induced rotation by spiral modes may not be adequate to explain the observed (or inferred) rotation rates of most pulsars. Nevertheless, induced spin remains an intriguing, if sub-dominant, potential contribution to the overall angular momentum budget of nascent neutron stars. Where final neutron-star spin periods of seconds are observed, the spiral-mode spin-up mechanism may remain viable.

One could argue that the delay to explosion we witness is already rather long. We suggest that in order for the neutrino mechanism to be robust and to generate explosion energies sufficient to overcome the binding energies of the progenitor mantle, while at the same time yielding explosion energies at infinity of $\sim 10^{51} \text{ erg}$, the onset of explosion should probably be rather early after bounce. However, this has yet to be demonstrated. We emphasize that our models start with zero angular momentum. A longer delay and total angular momentum conservation would naturally make it less and less likely that any significant net angular momentum would be left behind. This effect is implicit in Figure 7, for which the residual net spin period jumps up on the right-hand side at greater mass cuts. Individual zones could initially be left with interesting spins, but others would have to be in the opposite directions required by net angular momentum conservation. At very late times, the residue would have to be in solid-body rotation at low net angular momentum.

In this paper, we have not explored various progenitor masses, nor a range of initial spin structures. Our goal was to determine whether a sizable rotation rate could be induced in the residual proto-neutron star when the progenitor itself was non-rotating. The behavior of the modest spiral mode we do see and the overall role of rotation in the supernova phenomenon itself remain to be fully mapped out. As computational capabilities improve, and codes acquire more physics and sophistication, all these issues can and will be readdressed.

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