Extra dimensions, dilaton and dark energy

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1. Introduction

Recent observations indicate that the expansion of the universe is accelerating and the data is compatible with a cosmological constant, $\Lambda$, as the responsible actor. The value of $\Lambda$ turns out to be many orders of magnitude below the canonical estimate from quantum theoretical considerations. If one restricts the study to non-quantum approaches $\Lambda$ could be seen just as another fundamental constant of physics. Surely even the non-quantum cosmology is beset with fine tuning problems such as the cosmic coincidence of the onset of acceleration. Nevertheless this is a problem somewhat unrelated to the ease by which the cosmological constant accommodates the observations. Such could be the view of a pragmatic who ignores aesthetics.

However even the pragmatic would feel a somewhat pronounced unease in trying to reconcile acceleration of observed space with the assumption of extra dimensions since the naive introduction of $\Lambda$ to the d-dimensional Einstein–Hilbert action mandates a time dependent compactification radius in clear disconcert with stringent bounds on the cosmological evolution of fundamental constants.

An important ingredient of string inspired extra dimensional theories is string/brane gas cosmology. This framework is rather successful for cosmology of the very early universe and can even be a candidate to replace the inflationary paradigm in that it also solves the problems of standard cosmology and yields the same type of spectrum for density perturbations [9,10]. To raise an intriguing point let us ignore acceleration for a moment and assume that the universe expands as if it is dominated by objects which exert no pressure along observed dimensions. In such a scenario of the late universe string/brane gas cosmology is as successful compared to its phenomenology for early times, if not aesthetically better. In fact it can not only accommodate a static radius for extra dimensions and constant dilaton but also in doing so has a working idea to explain the number of observed dimensions and has for instance arguments on the possibility for dark

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matter of string/brane origin [5–8,26]. However the acceleration of the observed dimensions poses a challenge to string/brane gas cosmology in view of the fact its constituents generally behave like pressureless dust along observed dimensions at late times. Thus it is of crucial importance to find an element compatible with string/brane gas cosmology that would stabilize extra dimensions and the dilaton while allowing our observed universe to expand in an accelerating fashion, desirably commensurable with a cosmological constant dynamics in a four-dimensional point of view. Clearly if we would like to have a constant dilaton and radion, the right-hand sides of (6b) and (6c) must vanish. Now assuming the observed dimensions expand in an accelerated fashion as $B(t) = Ht + B_0$, mimicking a four-dimensional cosmological constant and hence yielding $ω = -1$, it is a simple exercise to show that one must have

\[
\begin{align*}
v &= -\frac{m + 1}{m - 1}, \\
a &= -\frac{4}{m - 1}. 
\end{align*}
\]

In a pure Einstein gravity context, that $v = -2$ for $m = 3$ was shown in [48] for flat $M_{C}$ and $M_{E}$. There it was also shown that dynamical stabilization of the radion could be established via a curvature term for $M_{E}$ next to our $\rho$. A curvature term for extra dimensions is a plausible companion to $\rho$ since in a perfect fluid approach it represents a term with $ω = -1$. In short what was shown in [48] was that $M_{E}$ has to have negative curvature and $v \leq 2$ to have stabilization in the true sense of the word. But this is not much in accord with the expectations of string theory; for instance with the flatness of Calabi–Yau manifolds which are of crucial phenomenological importance. On the other hand if another perfect fluid term, now not a curvature term for $M_{E}$, again with $ω = -1$ and yet with another $v$ accompanies our $\rho$ the observation is invariant: one pressure coefficient along extra dimensions has to be less than $-2$. After [48] appeared Greene and Levin [49] reemphasized the need for $v = -2$ for constant radion and they argued that dynamical stabilization can be achieved via Casimir effect along extra dimensions, including massive contributions. At any rate here the impact of our phenomenological approach is clear: the constraint on $v$ remain the same and as a side nuisance we have the above condition on $a$.

That $v = -2$ in the analysis of this chapter, and $v \leq -2$ of [48] for that matter, are all in close relation and accord with the recently proved no-go theorems [51–53]. A general result of the mentioned theorems is that for a constant radion (and dilaton with a slight modification of the arguments) and observed acceleration one has to allow for violations of null energy condition and that this violation has to be generally along extra dimensions. And that it has to be strong.

So one has to come up with objects in string theory satisfying the amendments on $v$ and $a$. We would like to contrast this to the ease with which a simple cosmological constant is able to accommodate the observational requirements of four-dimensional cosmology.

We would also like to point out as a side remark that $v = -2$ along with $a = -2$ would mean that the Lagrangian in (1) along with the particular choice in (3) is invariant under both $S$ and $T$ duality transformations for $d = 10$ and $m = 3$: an observation that follows from the application of the general findings of [38] to the particulars of this work.

### 3. A note on dilaton coupling to conserved energy–momentum tensors

At this point we would like to emphasize a detail about the dilaton coupling to sources that yield a conserved energy–momentum tensor. For concreteness let us assume $L$ in (1) is not specified. Using the equations of motion arising from varying (1)
with respect to the metric and \( \phi \) and the fact that the energy–momentum tensor originating from \( \sqrt{-g}L \) is conserved one can arrive at the following invoking the contracted Bianchi identity, as was done in [32],

\[
\tau e^{\alpha \phi} \left( L \delta^\nu_\mu - 2 T^\nu_\mu \right) \nabla^\nu \phi = 0. \tag{8}
\]

One can read the implications of this equation in various ways. If one has \( \tau = 0 \), this is a quite general resolution. This implies \( a = 2 \) meaning that the fields in \( L \) couple minimally to the dilaton-gravitational part of the Lagrangian in (1); the principle of equivalence is obeyed. We would like to point out however the following fact; let us assume \( L \) represents everything else, then if the dilaton couples to all of them with the same \( a \) one can argue that there is still a vast of equivalence principle at work in view of this universality, albeit this would not be the usual one; it would be one generalized with the presence of the dilaton. Nevertheless \( a \neq 2 \) has rather non-trivial consequences even in the absence of knowledge about the exact form of the Lagrangian. So let us assume it for the sake of argument. Then, (8) represents an interesting constraint on \( \nabla^\nu \phi \) in that if it is not identically zero it has to be a vector in the null-space of the matrix

\[
M_{\mu \nu} = (L g_{\mu \nu} - 2T_{\mu \nu}) = -2 \frac{\partial L}{\partial g^{\mu \nu}}. \tag{9}
\]

One can also approach (8) in another way. One could fix the dependence of \( \phi \) on the metric co-ordinates and digress on the form of \( L \). As pointed out in [32] if the dilaton depends only on time and \( T_{\mu \nu} \) is diagonal we must have \( L = 2T^{\nu}_0 = -2 \rho \). Elaborating on this observation still assuming that the energy–momentum tensor is of perfect fluid form we can see that if the dilaton depends on any other co-ordinate along with time, the respective pressure coefficient has to be \(-1\). For instance if the dilaton is to depend on time and on the co-ordinates of extra-dimensions, it must have pressure \(-1\) along them, as long as \( a \neq 2 \). Furthermore, again in a perfect fluid approach, if the dilaton is to have non-trivial dependence on all co-ordinates we end up with \( \omega = -1 \) and \( \nu = -1 \), compatible with a d-dimensional cosmological constant or a pure dilaton potential. It is tempting to speculate that these observations are somehow related to the previously mentioned no-go theorems presented in [51–53].

4. A generalization

The analysis of Section 2 does not yield a true stabilization of the radion and the dilaton, it simply studies the constraints on the parameters to have a constant dilaton and radion of unspecified value. In fact if one performs a linear stability analysis around solutions one will find that the perturbations of both radion and dilaton have zero mass. This is quite expected as a consequence of the fact that our toy model so far depends on only one \( \rho \); if the right-hand sides of (6b) and (6c) are to vanish any further derivative of these terms with respect to \( C \) or \( \phi \) also vanish at the solution. A massless excitation is not phenomenologically favoured thus we need to have true stabilization with positive masses for the radion and dilaton perturbations. This vanishing of masses is in principle related to the fact that the system was invariant under both T and S duality transformations. Any lifting, however partial, of these symmetries at any part of the system should provide us with non-zero masses.

As a general rule of thumb we need to have at least two sources to have dynamical stabilization. Both of these sources must have the same \( \omega \), which should be \(-1\) to yield \( B(t) = Ht + B_0 \). So for example we can pick one of them to be like (3) and another to be a pure dilaton potential. Let us therefore assume (1) still applies but now with

\[
e^{\alpha \phi} L = -2e^{\alpha \phi} \rho - 2V(\phi). \tag{10}
\]

This generalization will yield the following equations of motion

\[
\ddot{B} + \dot{k} \dot{B} = -e^{\alpha \phi} (1 + \tau) - \frac{1}{2} V', \tag{11a}
\]

\[
\ddot{C} + k \dot{C} = e^{\alpha \phi} (1 - \tau) - \frac{1}{2} V', \tag{11b}
\]

\[
\ddot{\phi} + k \ddot{\phi} = -\frac{1}{2} e^{\alpha \phi} [T - (d - 2) \tau] \dot{\rho} - V - \frac{d - 2}{4} V', \tag{11c}
\]

\[
\ddot{k} = \frac{m^2}{2} + p \dot{C}^2 + 2 e^{\alpha \phi} \rho + 2V. \tag{11d}
\]

The conditions for the existence of an extremum and that \( B = Ht + B_0 \) with \( H > 0 \) are simply given as

\[
0 < -(1 + \tau) U_0 - \frac{1}{2} V', \tag{12a}
\]

\[
0 = (v - \tau) U_0 - \frac{1}{2} V', \tag{12b}
\]

\[
0 = \frac{1}{2}(T - (d - 2) \tau) U_0 - V_0 - \frac{d - 2}{4} V'. \tag{12c}
\]

where the subscripts \( o \) refer to the values at the extrema. We have also defined \( U_0 = \rho e^{\alpha \phi_0} (1 + v) p c \), to have compact expressions. A linear stability analysis around this solution will yield the following

\[
\delta \dot{X} = -F \delta X - \Sigma \delta X \tag{13}
\]

with \( \delta X^T = (\delta B, \delta C, \delta \phi) \). Also \( F \) is the friction matrix and has the following form

\[
F = \begin{pmatrix}
2mH & pH & -2H \\
0 & mH & 0 \\
0 & 0 & mH
\end{pmatrix} \,
\]

which clearly enforces damping on all equations. On the other hand the matrix \( \Sigma \) responsible for the frequencies of oscillations around the extrema has the form

\[
\Sigma = \begin{pmatrix}
\Sigma_{BC} & \Sigma_{B\phi} \\
\Sigma_{CC} & \Sigma_{C\phi} \\
\Sigma_{CS} & \Sigma_{\phi}\phi
\end{pmatrix} \,
\]

where we have

\[
\Sigma_{BC} = -\frac{1}{2} \left[ (1 + \nu + \tau) U_0 \right. \tag{16a}
\]

\[
\Sigma_{B\phi} = \frac{1}{2} V_0'' + a \left( 1 + \tau \right) U_0 \tag{16b}
\]

\[
\Sigma_{CC} = \left( 1 + \nu \right) \left( v - \tau \right) U_0 \tag{16c}
\]

\[
\Sigma_{C\phi} = \frac{1}{2} \left[ (1 + \nu) \left( T - (d - 2) \tau \right) U_0 \right. \tag{16d}
\]

\[
\Sigma_{CS} = a \left( 1 + \nu \right) \left[ T - (d - 2) \tau \right] U_0 + V_0' + \frac{d - 2}{4} V_0'' \tag{16e}
\]

\[
\Sigma_{\phi}\phi = -\frac{1}{2} a \left[ (T - (d - 2) \tau) U_0 + V_0' + \frac{d - 2}{4} V_0'' \right. \tag{16f}
\]

\[8\] One must however keep in mind that this results from the Bianchi identities and hence must be automatically satisfied via the equations of motion of the fields in \( L \) if we knew its form. Nevertheless the implications of (8) are rather illuminating.

\[9\] If one insists on the usual equivalence principle one must take \( a = 2 \). But for instance, D-branes are known to have \( a = 1 \).

\[10\] This is still commensurable with a cosmology which is isotropic and homogeneous along the observed dimensions.

\[11\] Otherwise one will redshift faster than the other and we will eventually end up with a single source.
The existence of a vanishing column in (15) is simply a consequence of the fact that \( \omega = -1 \); the derivatives of the right-hand sides of all (11a)-(11c) with respect to \( B \) identically vanishes. In order to have stabilization we would require positive eigenvalues for \( \Sigma \). But this is not the whole issue; as it stands \( \Sigma \) also describes a general mixing between the perturbations which can be detrimental since it implies mixing of \( \delta C \) and of \( \delta B \). A simple and somewhat elegant way of getting around this obstacle is to assume \( \Sigma_{\delta C} = 0 \). Requiring positive eigenvalues along with this simplifying restriction will yield

\[
0 < (1 + \nu)(v - \tau),
\]

\[
0 < -\frac{1}{2} a(T - (d - 2)\tau)U_0 + V_0' + \frac{d - 2}{4} V_0''.
\]

\[
0 = (1 + \nu)(T - (d - 2)\tau).
\]

Analysing (17c) we immediately see that for these equations to be consistent one has as before \( T - (d - 2)\tau = 0 \) for the other solution is \( v = -1 \) ans this is in conflict with (12a) used along with (12b). In fact from these considerations we have \( v < -1 \). Therefore we again see that for \( d = 10 \) the \( \rho \) contribution to the Lagrangian is \( S \) dual.\(^{12} \) Having picked \( \Sigma_{\delta C} = 0 \) we have achieved the following: the equations for \( \delta \phi \) completely decoupled and its solutions are simply damped oscillations since \( F_{\phi \delta} > 0 \) and \( \Sigma_{\phi \delta} > 0 \). As a result of this one can take this solution and paste in into \( \delta C \) equations where it will act as a source term: a source which asymptotically vanishes as a result of the damping. The solution of \( \delta C \) thus obtained can be used in the \( \delta B \) equation again as a source. Consequentially the evils of mixing are somewhat circumvented. One could along with \( \Sigma_{\delta C} = 0 \) which completely decouples the radion and the dilaton but this is not necessary for this simple example. However we would like to stress again the fact that taking \( \Sigma_{\delta C} = 0 \) is synonymous with the \( S \) duality of the \( \rho \) term, at least for ten dimensions. Using the above intermediate result along with (17a) we arrive at the following

\[
v < -\frac{m + 1}{m - 1},
\]

\[
a = \frac{p - 2 + pv}{4}.
\]

For say \( m = 3 \) and \( d = 10 \) it is clear that \( v < -2 \) and \( a < -2 \). We have thus established that true stabilization can be achieved and that the stringent constraints on \( v \) and \( a \) remain as upper bounds. There are further consistency conditions on \( V \) given as

\[
V_0' < 0,
\]

\[
V_0 = -\frac{d - 2}{4} V_0',
\]

\[
V_0'' > -\frac{4}{d - 2} V_0'.
\]

These constraints on \( V \) are not too illuminating and can possibly be satisfied somewhat easily for a wide range of models. However, in general the dilaton potential in string inspired models are functions of \( e^\phi \) which is simply the string coupling. The above constraints on the stable minimum of the potential may yield some clues as to which stringy object, among the many possible ones, might be responsible for dilaton stabilization.

In this chapter we have presented this simple generalization as an example evidencing that the constraints of Section 2 are somewhat robust. There can be aesthetical objections to our approach since the extremum condition on (11b) in essence assumes a fine tuning between the \( \rho \) and \( V \) terms; two contributions that possibly have nothing to do with each other.

But again, our emphasis was not on the precise way dilaton and radion stabilization along with accelerating observed dimensions is achieved, it was on making the case for the necessity for rather exotic sources to achieve it in general.

Nevertheless this aesthetical objection will generally be present whenever we want to achieve both radion and dilaton stabilization with few sources having \( \omega = -1 \). Such terms aren’t exactly in abundance; a pure dilaton potential, a \( \rho \) of the type we have studied and a curvature term for the extra dimensional manifold are the simplest ones that come to mind. A deeper reason for the mentioned fine tuning between sources that are at face value unrelated could be the fact that these sources become overworked in that we require both radion and dilaton stabilization from them. In reality what we truly need is the consistent presence of only one such term for the equation of the scale factor of observed space to ensure \( B = Ht + B_0 \). Thus it is an intriguing possibility to check for sources with different pressure coefficient along observed dimensions such that the responsibilities to have accelerated observed space and stabilized radion and dilaton are separated.

As a simple counter example to this somewhat attractive possibility we would like to digress on the impact of \( (m, n) \) strings as studied in [33]. In that work there are two contributions to the energy–momentum tensor; the winding and momentum modes of strings. Both of these sources have zero pressure along observed dimensions. On the other hand they also bring about a potential term for the dilaton equations. It can be shown that in this picture both the dilaton and the radion can be stabilized. The crucial point is that these sources will force the observed dimensions to grow as pressureless ordinary matter would; in a decelerating way. So what we need is a source with \( \omega = -1 \) that does not contribute to the \( C \) and \( \phi \) equations. The resolution is very simple; on top of the winding and momentum mode contributions of \( (m, n) \) strings add a source which satisfies (7). This should work since we have already seen that these conditions mean that the mentioned source is invariant under \( T \) and \( S \) dualities and thus will not contribute to the right-hand sides of the dilaton and radion equations but will have an effect on the \( B \) equations. The situation will be described by the following equations

\[
\ddot{B} + k\dot{B} = e^{-m\delta B} S_B(\phi, C) - (1 + \tau)e^{\phi}\rho,
\]

\[
\ddot{C} + k\dot{C} = e^{-m\delta C} S_C(\phi, C),
\]

\[
\ddot{\phi} + k\dot{\phi} = e^{-m\delta \phi} S_\phi(\phi, C).
\]

The first term in the \( B \) equations is becoming less and less relevant since the \( \rho \) term does not depend on \( B \). So in time we will have \( B = Ht + B_0 \). The terms \( S_C \) and \( S_\phi \) represent contributions from the winding and momentum modes of \( (m, n) \) strings and for their explicit expressions we refer the reader to [33]. Consequently we will have dynamically stabilized radion and dilaton along with accelerated observed dimensions. However the price we pay is that the masses of the excitations around the minima are becoming exponentially small in time even though they are always positive since the right-hand sides of both \( C \) and \( \phi \) equations above are multiplied by \( e^{-m\delta} = e^{-m\delta \phi} \). Furthermore this multiplicative factor cannot change the location of the minima in \( (C, \phi) \) space. Now since \( H \) is rather small one can possibly argue in favour of such a scenario at least for now but as time evolves we would have less and less massive excitations and this is undoubtedly a source for stringent constraints on such an approach.

We can thus conclude that we typically need sources with the same \( \omega \) achieving both dilaton and radion stabilization and that

\(^{12} \) In this case, as opposed to the example of Section 2, the \( \rho \) term is not \( T \) duality invariant. It better not be because \( V \) term also contributes to the right-hand side of the \( C \) equations.
the aesthetical objection raised at the beginning of this subsection is, even though still standing, a bit too restrictive.

Another way to achieve stabilization without a fine-tuning between radion dependent objects and a pure dilaton potential is to include a curvature term for extra dimensions along with our $\rho$. This is possible but it will, along with [18], require a $\mathcal{M}_G$ which is negatively curved. A situation that, as we have stressed before, is not compatible with the need of string theory for Calabi–Yau manifolds.

5. Conclusion

We have presented stringent constraints on parameters of theories yielding accelerated observed space as well as providing stable radion and dilaton. The constraints on the dilaton couplings are just as strong as those on the pressure coefficients along extra dimensions. This can possibly be understood via the fact that the dilaton can be seen as the scale factor of a compactified eleventh dimension. The observations we have presented are related and in accord with the rather strong no-go theorems on a marriage between dark energy and extra dimensional models [51–53] in that the sources are shown to very strongly violate the null energy condition along extra dimensions. In fact the theorems mentioned not only require strong NEC violation along extra dimensions but also that this violation has to be time dependent to allow for the observed cosmological history of the universe. Such time dependence is still a possibility within string/brane gas cosmology nevertheless we have only worked in the regime where a pure de Sitter phase has already settled in the past.

Perhaps a stronger result of these theorems is that they require non-trivial distribution of density and pressure along extra dimensions. Since we have worked with homogeneous quantities it seems the simple approach we have presented here violates this fact. Nevertheless in view of this the constraints we have presented could be seen as averages over extra dimensions and still operational. This means for instance that the average of the pressure along extra dimensions should be $-2$ and thus there must be regions where it is considerably less if the pressure – and hence the energy density – is inhomogeneously distributed.

On the other hand, dark energy is not the only source to put stringent constraints on multidimensional theories. Recently Eingorn and Zhuk have shown that if one assumes point like sources, toroidal extra dimensions are incompatible with classical tests such as the perihelion advance of Mercury and gravitational frequency shift [54–56]. Even though there the sources cannot provide NEC violation they are inhomogeneously distributed along extra dimensions. So it is tempting to speculate on an interplay between the theorems in [51–53] as providing an avenue for even stronger constraints on extra dimensional theories.

To conclude we reemphasize the need for a source satisfying (7) to provide for stable radion and dilaton and allowing de Sitter type expansion for observed dimensions. As we have stated, in the absence of the dilaton one can argue that these constraints can be accommodated by Casimir effect along extra dimensions [49] but it is not clear how this can be extended to dilaton gravity. Nevertheless recent research [50] shows that supersymmetry breaking via gaugino condensation in string gas cosmology can be the responsible actor for dilaton stabilization. It is tempting to expect that this approach, since it introduces a dilaton potential, could provide a resolution.

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