Timing stability of three black widow pulsars

Ann-Sofie Bak Nielsen, Gemma H. Janssen, Golam Shaifullah, Joris P. W. Verbiest, David J. Champion, Grégory Desvignes, Lucas Guillemot, Ramesh Karuppusamy, Michael Kramer, Andrew G. Lyne, Andrea Possenti, Ben W. Stappers, Cees Bassa, Ismaël Cognard, Kuo Liu and Gilles Theureau

1 Max-Planck-Institut für Radioastronomie, Auf dem Hügel 69, D-53121 Bonn, Germany
2 Fakultät für Physik, Universität Bielefeld, Postfach 100131, D-33501 Bielefeld, Germany
3 Leiden Observatory, Leiden University, Niels Bohrweg 2, NL-2333 CA Leiden, the Netherlands
4 ASTRON, the Netherlands Institute for Radio Astronomy, Oude Hoogeveensedijk 4, NL-7991 PD Dwingeloo, the Netherlands
5 Department of Astrophysics/IMAPP, Radboud University, P.O. Box 9010, NL-6500 GL Nijmegen, the Netherlands
6 LESIA, Observatoire de Paris, Université PSL, CNRS, Sorbonne Université, Université de Paris, 5 place Jules Janssen, F-92195 Meudon, France
7 Laboratoire de Physique et Chimie de l’Environnement et de l’Espace LPC2E CNRS-Université d’Orléans, F-45071 Orléans, France
8 Station de radioastronomie de Nançay, Observatoire de Paris, PSL Research University, CNRS/INSU, F-18330 Nançay, France
9 Jodrell Bank Centre for Astrophysics, School of Physics and Astronomy, The University of Manchester, Manchester M13 9PL, UK
10 INAF – Osservatorio Astronomico di Cagliari, via della Scienza 5, I-09047 Selargius (CA), Italy
11 Dept Physics, Università di Cagliari, S.P. Monserrato-Sestu Km 0,700, I-09042 Monserrato (CA), Italy
12 LUTH, Observatoire de Paris, PSL Research University, CNRS, Université Paris Diderot, Sorbonne Paris Cité, F-92195 Meudon, France

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ABSTRACT

We study the timing stability of three black widow pulsars (BWP), both in terms of their long-term spin evolution and their shorter term orbital stability. The erratic timing behaviour and radio eclipses of the first two BWP systems discovered (PSRs B1957+20 and J2051−0827) were assumed to be representative for this class of pulsars. With several new black widow systems added to this population in the last decade, there are now several systems known that do not show these typical orbital variations or radio eclipses. We present timing solutions using 7–8 yr of observations from four of the European Pulsar Timing Array telescopes for PSRs J0023+0923, J2214+3000, and J2234+0944, and confirm that two of these systems do not show any significant orbital variability over our observing time span, both in terms of secular or orbital parameters. The third pulsar PSR J0023+0923 shows orbital variability and we discuss the implications for the timing solution. Our results from the long-term timing of these pulsars provide several new or improved parameters compared to earlier works. We discuss our results regarding the stability of these pulsars, and the stability of the class of BWP in general, in the context of the binary parameters, and discuss the potential of the Roche lobe filling factor of the companion star being an indicator for stability of these systems.

Key words: binaries: close – pulsars: general – pulsars: individual: PSR J0023+0923, J2214+3000, J2234+0944.

1 INTRODUCTION

The first radio pulsar was discovered in 1967 by Jocelyn Bell Burnell (Hewish et al. 1968) and since then more than 2700 radio pulsars have been found (Manchester et al. 2005). This sample includes both isolated pulsars and pulsars in binary systems, and slow and millisecond pulsars (MSPs). MSPs are old pulsars that have gone through the recycling process (Alpar et al. 1982; Battacharya & van den Heuvel 1991). MSPs are spun up in X-ray binary systems through accretion, which transfers angular momentum on to the pulsar. During the X-ray pulsar phase, the magnetic field strength of the pulsar decreases (Chen et al. 2013). A special group of MSPs, the so-called spiders, with very low companion masses and tight orbits ($P_b < 24$ h), are the ‘redback’ pulsars (RBPs), which have companion star masses of $M_2 \approx 0.1−0.4$ $M_\odot$, and the ‘black widow’ pulsars (BWP) with $M_2 \ll 0.1$ $M_\odot$ (Chen et al. 2013; Roberts 2013). The low-mass companions of BWP are often

* E-mail: abaknielsen@mpifr-bonn.mpg.de

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thought to be semidegenerate stars, similar to brown dwarfs (see section 4.4 in Lazaridis et al. 2011). The companions of RBPs are probably non-degenerate stars, as suggested by a few cases where the optical counterpart was discovered (Ferraro et al. 2001; Roberts 2013; Al Noori et al. 2018). The fate of the companion star in the BWP systems is unclear. However, one postulated scenario is that the companion could be fully ablated, creating an isolated MSP. Alternatively, tidal effects could play a significant role in eventually destroying the companion (Stappers et al. 1998; Chen et al. 2013).

Since the discoveries of PSRs B1957+20 and J2051−0827 (Fruchter, Stonebrin & Taylor 1988; Stappers, Bessell & Bailes 1996b), the populations of BWPs and RBPs have increased greatly due to recent surveys, using either radio observations that were optimized to find MSPs, or targeted radio surveys that are guided by high-energy point sources such as those seen with the γ-ray observatory Fermi. More than 40 MSPs were found using such surveys (Roberts 2013). The two original BWP systems show eclipses of the radio emission from the pulsar. The eclipses are due to material being ablated off of the companion star by a strong pulsar wind (Fruchter et al. 1988; Stappers et al. 1996b; Chen et al. 2013). The presence of this matter in the binary, often makes the BWPs complicated systems to use for high precision pulsar timing experiments. The companion stars are often bloated, and their unstable and inhomogeneous mass distributions exert small torques on the pulsar, which in turn causes small changes in the orbit. Such orbital variations increase the number of parameters that are required in timing models, and mean that it is not possible to predict the timing behaviour and thus not possible to model the orbital variations for longer time-scales. The orbital variability could also reduce the sensitivity of the timing solution to other signals of interest, such as for example gravitational-wave (GW) signals.

By observing multiple stable pulsars in different parts of the sky, an array of pulsars, and cross-correlating their timing residuals, it should be possible to obtain the sensitivity required to measure the expected quadrupolar signature of a nHz GW. This is the general idea behind the pulsar timing arrays (PTAs; Foster & Backer 1990; Tiburzi 2018). With new BWPs being discovered, Bochenek, Ransom & Demorest (2015) considered the feasibility of using BWPs in PTAs, by testing if fitting for multiple orbital frequency derivatives significantly reduced the sensitivity to the GW signal. They used simulated data sets of five different pulsars to constrain how sensitive a timing solution would be to a GW signal, if several orbital-period derivatives were fitted. They found that the sensitivity to the GW signals was not reduced significantly, partly due to the comparatively long periods of the GW signals and the typical BWP orbital period of about 2–20 h. Recently a few BWPs have been included in PTAs, e.g. PSR J0610−20 and J2051−0827. As the SRT has only just started observing the data collected by five different telescopes around Europe: the Westerbork Synthesis Radio Telescope (WSRT) in the Netherlands, the Effelsberg 100-m Radio Telescope (EFF) in Germany, the Lovell Radio Telescope (JBO) in the UK, the Nançay Radio Telescope (NRT) in France, and the Sardinia Radio Telescope (SRT) in Italy (Desvignes et al. 2016). As the SRT has only just started observing on a regular basis, data from this telescope are not used in this paper. The three data sets for PSR J0023+0923, J2214+3000, and J2234+0944 span about 7.5, 8, and 7 yr of data, respectively, see Fig. 1. As described in Table 1 the data used are from several pulsar recording instruments (Karuppusamy, Stappers & van Straten 2008; Desvignes et al. 2011; Bassa et al. 2016; Guillemot et al. 2016; Lazarus et al. 2016).

The data were collected using dual-polarization receivers, and backends providing the capability of coherent dedispersion (except for data from the Lovell digital filterbank (DFB) backend, which employs incoherent dedispersion), thus recording four coherently dispersed timeseries (one for each Stokes parameter), integrated modulo the spin period (i.e. ‘online folding’) into subintegrations of between 10 and 60 s, depending on the telescope and date of observation (see Table 1).

Specific parts of the data that were affected by radio frequency interference (RFI) and not detected or cleaned in the pre-processing stages were cleared using standard PSRCHIVE tools (van Straten, Demorest & Osłowski 2012), where it should be noted, that the Lovell ROACH backend uses a real-time spectral kurtosis (Nita & Gary 2010) RFI removal method as implemented in DSPSR in the pre-processing of the data. The cleaned data were then averaged in frequency and time to maximize the signal-to-noise ratio (S/N). For PSR J0023+0923, some observations were taken with a total

1https://confluence.slac.stanford.edu/display/GLAMCOG/Public+List+of+FIPS+LAT-Detected+Gamma-Ray+Pulsars

2http://www.epta.eu.org/
The TOAs were measured at each observatory with reference to a local clock, which was synchronized using GPS to the Terrestrial Time standard, that is derived from the ‘Temps Atomique International’ time standard, TT(TAI). The TOAs were corrected to the Solar system barycentre using the NASA-JPL DE421 planetary ephemerides (Folkner, Williams & Bogs 2009). The TEMPO2 software package was used (Hobbs, Edwards & Manchester 2006) to fit the timing solutions presented in Table 2. Data sets generated by different telescopes were phase aligned by using constant offsets (JUMPS; following the procedure described in Verbiest et al. 2016) and a few clock offsets were applied where necessary (see also Desvignes et al. 2016 and Lazarus et al. 2016).3

Error-scaling factors (called T2EFACs) were calculated for each receiver-frequency-band combination using the timing model derived and taking the square root of the reduced χ² from fits to the TOAs for each such combination alone. The T2EFAC value corrects the statistical weights of the data by rescaling the error bars to account for probable underestimation at the template matching stage.

3 RESULTS

We obtained stable timing solutions for the three pulsars J0023+0923, J2214+3000, and J2234+0944 over time spans of 7–8 yr, using data from four of the EPTA telescopes. The best-fitting timing solutions for these three pulsars are shown in Table 2, and in Fig. 3 the timing residuals for the entire time span are shown.

3.1 New parameter measurements

For low eccentricities the location of periastron is not well measured in the TOAs and a strong covariance between the longitude of periastron (ω) and the epoch of periastron passage (T0) occurs. This leads to very large uncertainties in the estimate of χ² of these parameters (see Lange et al. 2001). This is avoided by using the ELL1 model in TEMPO2.

When using the ELL1 model, the Laplace parameters, EPS1 = e sin(ω) and EPS2 = e cos(ω), instead of the eccentricity, e, and ω, are included (Hobbs et al. 2006). Furthermore, TASC is included in the ELL1 model rather than T0. We measure EPS1 and EPS2, which are orthogonal components of the eccentricity. The eccentricity is given by e = √(EPS1² + EPS2²) and the eccentricities of the pulsars are thus nominally e = 2.1(12) × 10⁻⁵, e = 1.5(9) × 10⁻⁵, e = 9.6(33) × 10⁻⁶, respectively, for PSRs J0023+0923, J2214+3000, and J2234+0944. Given the low significance, the eccentricities are interpreted as upper limits.

In this paper we also introduce and measure a first-order derivative of the dispersion measure (DM = dDM/dt) for PSR J2214+3000, of 3.6(4) × 10⁻⁴ cm⁻³ pc yr⁻¹. This accounts for the DM variations we show in Fig. 4 (for more details see Section 3.2). We further find a very marginal detection of the first-order derivative of the semimajor axis, of −8.4(58) × 10⁻¹⁵ for PSR J2214+3000. The semimajor axis marginal upper limit measurement of PSR J2214+3000 is not used in the final timing solution presented in Table 2. In addition we derived a significant value of P FontWeight for PSR J0023+0923, of 3.9(24) × 10⁻¹², from the measured orbital frequency (FB0) and first-order orbital frequency derivative (FB1). Pfb is slightly larger than previous measurement (Arzoumanian et al.

3Throughout this work TEMPO2 version 2014.2.1 was used.

Figure 1. Timing baselines per backend for the three BWPs discussed in this paper. The colours correspond to backend and observing frequency combinations. The dark green lines represent the time span covered by the ROACH-based recorder, observing at a centre frequency of 1532 MHz, and the brown line represents the DBF at 1400 MHz, both at the Lovell radio telescope. The light blue line represents the BON backend at 1408 MHz, and the pink and red lines represent timing spans of the PSRIX backend at 1347 and 2627 MHz, respectively, at the Effelsberg 100-m radio telescope. The light blue line represents the BON backend at 1408 MHz, both at the Nancay Radio telescope. The brown line represents the DFB at 1400 MHz, both at the Lovell radio telescope. ROACH-based recorder, observing at a centre frequency of 1532 MHz, and the pink and red lines represent timing spans of the PSRIX backend at 1347 and 2627 MHz, respectively, at the Effelsberg 100-m radio telescope. Finally, the grey and black lines represent timing baselines for the PuMa-II backend at the Westerbork Synthesis Radio Telescope. More details about the backends and telescopes can be found in Section 2 and Table 1.
Table 1. Telescope (backends), centre frequency, bandwidth, number of TOAs for the different pulsars, range of the error-scaling factor (T2EFAC), and the subintegration length. The four telescopes used are part of the EPTA and they are the Westerbork telescope (WSRT), Effelsberg, Nançay, and Lovell at Jodrell Bank.

| Telescope (Backend) | $f_c$ (MHz) | BW (MHz) | No. of TOAs | T2EFAC range | Sub. int. time (s) |
|---------------------|-------------|----------|-------------|---------------|-------------------|
| WSRT (PuMaII)       | 345         | 70       | 58          | 51            | 1.1–2.4           |
| Effelsberg (PSRIX)  | 1380        | 160      | 30          | 60            | 1.0–1.6           |
| Nançay (NUPPI)      | 1484        | 512/256/128$^a$ | 791 | 184 | 1.4–2.1 | 15–60 |
| Nançay (BON)        | 1408        | 128      | –           | 108           | 1.2–1.4           |
| Lovell (DFB)        | 1400        | 384-512  | 23          | 96            | 1.2–1.6           |
| Lovell (ROACH)      | 1532        | 400      | 114         | 126           | 1.1–1.8           |

$^a$The data from Nançay, NUPPI, are affected by scintillation, and the frequency bands have thus been split into smaller bands, of 256 MHz for PSR J0023+0923 and J2214+3000. For PSR J2234+0944 we have split the band in four, so we have a bandwidth of 128 MHz. The given T2EFAC range is for the range used for all three pulsars. Furthermore, the subintegration length is given in the last column.

Figure 2. Dynamic spectra obtained with Nançay and the NUPPI backend; the scintillation in time and frequency for PSR J2234+0944 is clearly seen, and it affects the timing because the profile shape changes with frequency. The MJDs represented in this plot are 55879, 55888, 55902, 55914, 56046, and 56060. The dark area corresponds to RFI masked data and the bright areas correspond to high intensity scintels.

2018), however, this measurement is still within the error on the parameter found in this paper. In general, our results are consistent to the results found in Arzoumanian et al. (2018).

3.2 Dispersion measure variations

The turbulent nature of the ionized ISM, which causes the scintillation described in Section 2, along with significant transverse velocities characteristic to many pulsars implies that the DM along the line of sight can vary significantly over a range of time-scales. The effects of changes in the DM on the arrival times of the pulses are inversely proportional to the observing frequency squared, and are therefore more easily detectable at lower frequencies. DM variations are only detectable when the low-frequency data are included, as the DM uncertainty in the high-frequency data alone is too large to provide any sensitivity to DM variations. If we look at the combined low- and high-frequency WSRT data of PSR J2214+3000 (see Fig. 4), we detect DM variations. The DM measurements

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in Fig. 4 were obtained by fitting the DM to non-overlapping segments of data that were around 100–200 d long, to gain sufficient frequency coverage. In a separate analysis of the low-frequency WSRT data, we detected a first-order DM derivative of $3.6(4) \times 10^{-4}$ cm$^{-3}$ pc yr$^{-1}$. For PSRs J0023+0923 and J2234+0944 we did not detect any DM variations. We furthermore tested whether DM was dependent on the orbital phase, see Section 4.2.

## 4 DISCUSSION

In the following section, we will discuss some of the features that the three sources show and relate these to the long-term stability of the three BWP systems. Furthermore, we will compare the properties of stable and unstable BWPs.

### 4.1 Orbital stability

In this paper, we classify a BW pulsar as stable if it has a single timing solution spanning more than a few months to about a year, or if the timing solution is similar in quality to WSRT data, which are best suited for the determination of DM variations. The $P_b$ and $P_0$ values for PSR J0023+0923 are derived from FB0 and FB1, respectively.

### Table 2. Timing solutions for PSRs J0023+0923, J2214+3000, and J2234+0944.

| Pulsar name | J0023+0923 | J2214+3000 | J2234+0944 |
|-------------|-----------|-----------|-----------|
| MJD range   | 55309.6–58167.8 | 55112.9–58168.8 | 55523.7–58160.5 |
| Data span (yr) | 7.83 | 8.37 | 7.22 |
| Number of TOAs | 1073 | 648 | 986 |
| Weighted rms timing residual (μs) | 3.5 | 4.3 | 2.1 |
| Reduced $\chi^2$ value (before application of EFACs) | 2.49 | 2.12 | 4.45 |

### Measured quantities

- **Right ascension, $\alpha$ (hh:mm:ss)**: $00:23:16.77787(18)$, $22:14:38.852794(14)$, $23:34:46.853741(6)$
- **Declination, $\delta$ (dd:mm:ss)**: $+09:23:38.1964(3)$, $+30:00:38.1964(3)$, $+09:44:30.2564(2)$
- **Pulse frequency, $\nu$ (s$^{-1}$)**: $327.8470154891364(8)$, $320.5922873902387(20)$, $275.7078283945944(6)$
- **Dispersion measure, DM (cm$^{-3}$ pc)**: $14.32726(10)$, $22.5519(6)$, $17.8253(7)$
- **First derivative of dispersion measure, $\frac{d}{d\nu}$ DM (cm$^{-3}$ pc yr$^{-1}$)**: $-1.22773(3) \times 10^{-15}$, $-1.51368(5) \times 10^{-15}$, $-1.527888(17) \times 10^{-15}$
- **Proper motion in right ascension, $\mu_\alpha$ (mas yr$^{-1}$)**: $-12.79(15)$, $-12.77(15)$, $-12.22(10)$
- **Proper motion in declination, $\mu_\delta$ (mas yr$^{-1}$)**: $20.77(8)$, $-1.46(12)$, $-6.96(6)$
- **Orbital period, $P_b$ (d)**: $0.03844127(18)$, $0.0390811(3)$, $0.06842948(12)$
- **Projected semimajor axis of orbit, $x$ (lt-s)**: $8.33872167(8) \times 10^{-5}$, $3.6(4) \times 10^{-4}$, $3.6(4) \times 10^{-4}$
- **First derivative of orbital frequency, $\frac{d}{d\nu}$ $P_b$ (s$^{-1}$)**: $-3(2) \times 10^{-20}$, $-4(3) \times 10^{-29}$, $-5(4) \times 10^{-36}$
- **Time of Ascending node, TASC (MJD)**: $55186.1136224(4)$, $55094.1380407(6)$, $55517.4822998(3)$
- **EPS1** (1.19) $\times 10^{-5}$, $5.8(33) \times 10^{-6}$, $7.7(33) \times 10^{-6}$
- **EPS2** (1.19) $\times 10^{-5}$, $5.8(33) \times 10^{-6}$, $7.7(33) \times 10^{-6}$

### Upper limits

- **First derivative of $x$, $\dot{x}$ (10$^{-12}$)**: $-8.4(58) \times 10^{-15}$

### Derived quantities

- **Orbital period, $P_b$ (d)**: $0.138799141(1)$
- **First derivative of orbital period, $\frac{d}{d\nu}$ $P_b$ (d)**: $3.9(24) \times 10^{-12}$
- **Eccentricity ($e$)**: $2.1(25) \times 10^{-5}$, $1.5(9) \times 10^{-5}$, $9.6(33) \times 10^{-6}$
- **Mass function, $f$ (10$^{-6}$ $M_\odot$)**: $2.35717(4)$, $1.27561(2)$, $1.95351(1)$
- **DM-derived distance (YMW16 model), $d$ (kpc)**: $1.11$, $0.60$, $0.77$
- **DM-derived distance (NE2001 model), $d$ (kpc)**: $0.69$, $1.54$, $1.00$

### Set quantities

- **Epoch of frequency and position determination (MJD)**: 56738, 56640, 56842
- **Epoch of dispersion measurement determination (MJD)**: 56542, 56203, 56763

### Discussion

In this paper, we classify a BW pulsar as stable if it has a single phase-connected timing solution, with only one orbital period derivative of fixed sign (see also Freire et al. 2017). However, ‘instability’ counter to this definition would not disqualify a BW pulsar as a PTA source. A more applicable definition for that case is given before the solution is given before the $T2EFAC$ was implemented. After the error scaling was applied, they reduced $\chi^2 \approx 1$. It should be noted that the DM and $\dot{\text{DM}}$ were only fitted to the low-frequency WSRT data, which are best suited for the determination of DM variations. The $P_b$ and $P_0$ values for PSR J0023+0923 are derived from FB0 and FB1, respectively.

By this definition, the first BWP found, PSR B1957+20, is unstable over long time spans, since it was not possible to create a timing solution spanning more than a few months to about a year (Arzoumanian, Fruchter & Taylor 1994). The pulsar also shows radio eclipses due to the bloated companion and material surrounding the companion. The second BWP found, PSR J2051–0827, shows similar behaviour, including timing solutions that were stable for short periods of time, of about 3 yr (Lazaridis et al. 2011; Shaifullah et al. 2016). Contrary to the first two BWPs discovered, there is one BW system PSR J0610+2100, which shows a stable timing solution and is included in the EPTA and IPTA (Desvignes et al. 2016; Verbiest et al. 2016).
Figure 3. Left-hand panels: The timing residuals of PSRs J0023+0923, J2234+0944, and J2214+3000 after fitting the timing models presented in Table 2. The residuals show stability over the entire time span. Right-hand panels: The same residuals as a function of orbital phase measured from the ascending node. There is no evident systematic variation of the residuals as a function of orbital phase due to delays in the companion atmospheres. This indicates that there are no eclipses, whose presence would be indicated by a clear excess delay around an orbital phase of 0.25.

The three BWPs analysed in this paper are very different from those early discoveries. None of these three BWPs show radio eclipses and it is possible to find a coherent timing solution for each of the three systems that is valid at least over a 7–8 yr period. However, PSR J0023+0923 does show significant orbital period derivatives (see Table 2), and all orbital frequency (FB) parameters are non-zero, which seems to indicate that there are orbital variations present similar to what is found for e.g. PSR J2051−0827 (Shaifullah et al. 2016). However, all three pulsars have reasonably low timing residual rms (∼2.1–4.3 μs) and all are good PTA sources.

4.2 Eclipses

We examined our data sets for the three pulsars for eclipses and did not find any evidence for radio eclipses for any of the three pulsars at any of our observed frequencies. See the right-hand panels in Fig. 3, which presents averages over many orbits. These plots indicate that there is not enough material around the companion to create the eclipses, as is also suggested for PSR J0023+0923 from X-ray observations by Gentile et al. (2014). The lack of radio eclipses can be an indication that the companion stars are not filling their Roche lobes (see Section 4.3). To further test if we see any indications of eclipses, we studied the DM as a function of orbital period. If there was any indication of additional ionized material along the line of sight at around orbital phase 0.25 (i.e. when the companion is at the minimum distance from us and the MSPs is on the opposite part of the orbit), then it would be evident when looking at the DM as a function of the orbital phase (Stappers et al. 1996a). In Fig. 5, we do not see any significant DM variation around orbital phase 0.25; however, we note that the orbital period is poorly sampled for all three pulsars in this paper. The poorly sampled orbital periods are the cause of the outliers in Fig. 5. Other evidence for eclipses not being present is seen in the mass function of the three black widows in this paper (see Table 2). As mentioned by both Freire (2005) and Guillemot et al. (2019) there seems to be a correlation between eclipses, or the lack thereof, and the mass function of the pulsars. The higher values of mass functions in general seem to belong to pulsars showing eclipses and the low-mass functions, as we also see for the three pulsars in this paper, are often coinciding with BWs without eclipses (see table 2 in Guillemot et al. 2019).

4.3 Roche lobe filling factors

The companion stars for the first-known two BWPs, PSRs B1957+20 and J2051−0827, are suggested to be Roche lobe filling,
with a Roche lobe filling factor (RLFF) of about 0.9 (the filling factors are determined from fitting the optical light curve of the companion stars) (Stappers et al. 2001; Reynolds et al. 2007; van Kerkwijk, Breton & Kulkarni 2011). This means that the outer layers of the companion star are less gravitationally bound to the star and it is thus easier to expel material from, or ablate, the companion star. This is one of the essential details of the geometry of the BWPs, as it is the ablated material that causes the radio eclipses (van Kerkwijk et al. 2011). Furthermore, the BWP J1810+1744 similarly has an RLFF of about 0.8. This system also shows radio eclipses and instabilities (Breton et al. 2013; Polzin et al. 2018).

The BWP J2256−1024 was found by Breton et al. (2013) to have a relatively low RLFF of ∼0.4, but was reported by Gentile et al. (2014) to show orbital variability. Recent studies of another BWP, PSR J0636+5128 (Kaplan et al. 2018), show that this pulsar has a large RLFF, of about 0.75, but it does not show eclipses. The missing eclipses are probably due to the relatively low inclination angle of ∼24°. This system seems to be a good candidate for orbital variations (Bak Nielsen, in preparation).

Of the three pulsars discussed in this paper, the RLFF has only been measured for the companion star of PSR J0023+0923, and it is ∼0.3 (Breton et al. 2013). If the Roche lobe of a BWP system is not filled, eclipses would not be expected, which coincides with what is observed for PSRs J0023+0924, J2214+3000, and J2234+0944. However, we do find that orbital variations are present for PSR J0023+0923. Thus, it is evident that while RLFFs seem to be closely related to the inherent stability of a binary system, RLFF alone is not a good discriminator of timing solution stability.

4.4 Additional intrinsic or observational parameters at play

BWPs are still a rather heterogeneous group of objects and various factors impact on their observational properties as well as on the intrinsic process at play in these systems. Alongside the RLFF, the irradiation of the companion star by the pulsar and the distance between the pulsar and companion star are factors that have the potential to affect the orbital stability. For example, the irradiation affects how heated and ablated the companion star is and thus how much it will potentially fill its Roche lobe (Stappers et al. 2001; van Kerkwijk et al. 2011; Breton et al. 2013). The distance to the BWPs affects the measured value of the RLFF, because it is determined by light-curve modelling and is thus dependent on the apparent luminosity, and could thus affect our discussion in Section 4.3 (Breton et al. 2013). The orbital inclination of the system has no effect on the orbital stability, however, it does influence whether or not we see eclipses in these systems. The inclinations of PSRs J0023+0923, J2051−0827, and B1957+20 are similar, respectively i ∼ 58°, i ∼ 40°, and i ∼ 65°, inferred from light-curve modelling. The first one of these systems does not show eclipses and the other two do (Stappers et al. 2001; van Kerkwijk et al. 2011; Breton et al. 2013). However, one system where it is likely that the inclination angle does matter is J0636+5128, which has an inclination of ∼24°, and shows no eclipses, even though it has a similar RLFF as PSRs J2051−0827 and B1957+20 (Kaplan et al. 2018).

5 PSR J2234+0944 AS A POSSIBLE TRANSITIONAL SYSTEM

Transitional MSPs are a relatively new class of binary pulsars, that show changes between emitting in radio and X-rays, and are believed to switch states between having an active accretion disc and
no accretion disc (Archibald et al. 2009). Since the first transitional MSP, PSR J1023+0038, was discovered to switch states, two more have been found, and all three systems are RBPs (Papitto et al. 2013; Bassa et al. 2014; Roy et al. 2015). The companion stars of BWPs and RBPs are very different, as RBPs are thought to have non-degenerate companions with a higher mass than the semidegenerate companions of BWPs (Chen et al. 2013). However, variations in their orbit and the presence of radio eclipses in some of these systems are characteristics shared between the BWPs and the transitional systems (Fruchter et al. 1998; Stappers et al. 1996b; Archibald et al. 2009; Chen et al. 2013; Papitto et al. 2013; Roy et al. 2015). Torres et al. (2017) suggested that PSR J2234+0944 could be a potential transitional system, based on variations in the γ-ray spectrum, which is similar to what is seen in the transitional MSP J1227−4853. However, PSR J2234+0944 has a timing solution that is stable over 8 yr, with no obvious irregularities or eclipses. Given the data, this system appears to be different from the variable transitional systems identified so far.

6 CONCLUSIONS
We studied three BWPs: PSRs J0023+0923, J2234+0944, and J2214+3000, all of which show different behaviour than the first two BWPs discovered, PSRs B1957+20 and J2051−0827, that are counted as unstable systems. We present timing solutions for PSRs J0023+0923, J2214+3000, and J2234+0944 over a data span of 7–8 yr. PSR J0023+0923 shows orbital variations, which can be modelled with up to a third-order orbital frequency derivative (see Table 2). That seems to counter the argument that a low value of the RLFF is an indicator for stable BWPs. From the orbital frequency derivatives we derived an orbital period derivative for PSR J0023+0923, of 3.9(24) × 10−12. The other two BWPs in this study, PSRs J2214+3000 and J2234+0944, show no orbital variations. It is possible that this is due to their companion star not filling its Roche lobe. This implies that the companion stars are more gravitationally tightly bound, resulting in a cleaner system with less material to interfere with, or to affect the radio signal and the orbital parameters. Since the three pulsars show stability, or only minimal instability, over long time-scales it is possible to use the systems discussed here as part of a pulsar timing array, and all three pulsars have been added to the EPTA source list. It remains to be seen if the lack of orbital stability in some of these gravitationally tightly bound systems is tied to specific high-energy signatures. Comparing with more BWPs and other pulsar systems will provide a clearer picture of what the most important factors are for determining why a BWP system has a stable or unstable orbital solution.

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