NULL RESULT IN GAMMA-RAY BURST LENSED ECHO SEARCH

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ABSTRACT

We have searched for gravitational-lens induced echoes between gamma-ray bursts (GRBs) in BATSE data. The search was conducted in two phases. In the first phase we compared all GRBs in a brightness complete sample of the first 260 GRBs with recorded angular positions having at least 5% chance of being coincident from their combined positional error. In the second phase, we compared all GRB light curves of the first 611 GRBs with recorded angular positions having at least 55% chance of being coincident from their combined positional error. No unambiguous gravitational lens candidate pairs were found in either phase, although a “library of close calls” was accumulated for future reference. This result neither excludes nor significantly constrains a cosmological origin for GRBs.

Subject headings: cosmology, gamma-rays: bursts, gravitational lensing
1. INTRODUCTION

There is no present consensus as to the cause of or distances to gamma-ray bursts (GRBs). Recent results by the Burst and Transient Source Experiment (BATSE) on board the Compton Gamma Ray Observatory have confirmed their isotropic angular distribution and “confined” peak brightness distribution (Meegan et al. 1992). These results generate an interesting puzzle. Currently, there are more than 100 models for the origins of GRBs (Nemiroff 1993). To help eliminate inapplicable models, discriminating statistical tests are needed.

The idea of searching for a gravitational lens echo in gamma-ray burst data is not a new one. Paczynski (1986b, 1987) originally suggested that such a lens echo effect might be detectable were GRBs to lie at cosmological distances. Mao (1992) estimated that the number of BATSE GRBs that need to be inspected to find a gravitational lens echo would be between 250 and 2000. Grossman and Nowak (1994) estimate that BATSE should detect a lensing event every 1.5 - 25 years, depending on the cosmological scenario. Blaes and Webster (1992) pointed out that GRB echoes would be expected if the universe were populated with a significant fraction of compact objects near $10^6$ solar masses. Narayan and Wallington (1992) discussed what information about the lens might be derived from the discovery of a gravitational lens echo.

A preliminary echo search of the first 386 GRBs detected by BATSE was conducted by Nemiroff et al. (1993a) without success. A study searching for lens effects within the time stream of the first 44 BATSE GRBs for massive compact dark matter (Nemiroff et al. 1993b) also did not find an echo but was able to show that either GRBs do not occur at the most likely cosmological distance implied by their brightness distribution or that a universe composed to closure density of compact objects with masses between $10^{6.5}$ and $10^{8.1}$ solar masses is marginally excluded.

A gravitational lens echo is to be expected if a galaxy is near enough to the line of sight to a GRB to create more than one detectable image of the GRB. For galaxies such images would be separated by at most several arcseconds, just as lensed QSO images are. However, the time delay between images can be from hours to years, depending on the
lens geometry and the relative placement of the source behind the lens. For a canonical isothermal galaxy lens involved in QSO lensing, the time delay between the two brightest images is on the order of a few months, with one or two years possible when a cluster of galaxies is superposed in the field (Blandford and Narayan 1992). Galaxies of smaller mass, which are more numerous, are capable of creating sub-arcsecond images, and time delays on the order of a week might be expected (Grossman and Nowak 1994). For lens geometries where more than one image is expected, the shortest time between images would be on the order of several hours, while again one or two years is roughly the maximum amount of time expected between images (Narasimha 1993). In general the brighter an image pair, the shorter the time delay between images, and the less probable an observer-galaxy-source alignment would be that would create this bright pair. Images themselves created by a cluster lens would typically be expected to be separated by 10 years or more - a time period too long to search for in current BATSE data.

In general, one cannot hope to resolve GRB images angularly - one can only hope to resolve them temporally. Both the random and systematic errors in the positions to BATSE GRBs, which are on the order of degrees (Brock et al. 1992), are much greater than the expected angular separation of images created by a galactic lens effect. Therefore only GRB events with positions that could be coincident will be searched as candidates for being gravitational lens images of the same burst.

Gravitational lens image pairs would be expected to have time profiles that are identical to within a scale factor. This assumes that any beaming inherent in the GRB progenitor scenario cannot be collimated to much better than a few arcseconds, as this is a likely angular size for the galaxy lens (at least the part that would be involved in a lens effect) on the GRB’s sky.

By the equivalence principle, gravitational fields bend the light of different energies equally. Therefore, gravitational lens images would also be expected to have identical spectra. More stringently, since it is known that the spectra of most GRBs change over the duration of the burst (Norris et al. 1985), lensed images would be expected to have identical spectra at all times during the burst.

As gamma rays traverse most material without absorption, there is not expected to be
any significant absorption between images. One can not, then, rely on such a mechanism
to alter one images’ spectra relative to the other. It is even harder to imagine a scenario
where the amount of absorption changes over the time-scale of the GRB, which would be
needed to alter the light curve.

Our present search differs from the lens search and subsequent dark matter limits
discussed in Nemiroff et al. (1993b) in that here we are comparing different GRB light
curves to each other in a search for galactic lenses, while Nemiroff et al. (1993b) searched
the time stream immediately following GRBs for an echo indicative of lower mass dark
matter lenses. In §2 we describe the search for gravitational lens echoes and the statistical
method used to distinguish an echo. In §3 we present the results of the search and we
discuss these results and inferences in §4.

2. THE SEARCH FOR GRAVITATIONAL LENSING

Our search for lensed echoes occurred in two phases. In Phase I only the first 260
GRBs were considered, as these GRBs had calibrated peak fluxes. Of these 260 GRBs we
used the same peak-flux complete sample of 118 GRBs as Wickramasinghe et al. (1993).
This sample is composed of GRBs above a limiting peak flux level to which the sample
is 99% complete, and demands that the GRBs were measured during a time of normal
background.

The angular positions of these 118 were compared, and those pairs with recorded
angular positions having at least 5% chance of being coincident considering their combined
positional error were retained for further analysis. This left 104 pairs of GRBs for the Phase
I comparison.

For the Phase II search, the first 611 GRBs were considered. This incorporated
all GRBs detected by BATSE before and including 6 April 1993, with trigger numbers
from 105 to 2291. The positions of all 611 were compared and those pairs that had
recorded angular positions having at least 55% chance of being coincident considering
their combined positional error were kept. We excluded those GRB pairs with angular
separations greater than 30°, which in general were extremely weak. This weakness created
a large angular uncertainty in the GRB’s position which in turn created an inordinately
large number of potentially coincident GRB image pairs. In addition, many of these GRBs were so weak that they would never be very convincing in a statistical comparison. This left 1706 pairs of GRBs for the Phase II comparison.

The initial comparison procedure was visual. A hard copy of the light curve in channel 3 (100-330 keV) of each GRB was made and catalogued. Channel 3 was chosen because it usually has the highest signal and relatively low and featureless background. A single energy channel was chosen for the initial comparison so that other energy channels could potentially be used later for an independent comparison.

Light curves that bore a marked similarity were recorded for future numerical comparison. For a wide range of scale factors and time offsets, those pairs of recorded GRBs were compared via a modified $\chi^2$ test to see if they could both have been drawn from the same parent distribution. A similar statistical comparison test has been suggested by Wambsganss (1993). A statistic based on the Fourier transform is given in Nowak and Grossman (1994).

The $\chi^2$ statistic was computed as follows. A background level for each GRB was computed, and a subjective starting and stopping time was determined. The stronger GRB (designated #1 here) was shifted in time $\Delta t$ (usually in units of the 64 ms time bins) and decreased in flux by an amount $f$, in each bin. The dimmer GRB was designated # 2. For a wide range of $f$ and $\Delta t$ values, the running sum $\chi^2_{12} = \Sigma(f \ast (C_1 - B_1) - (C_2 - B_2))^2$ was computed, as well as running sums of $\chi^2_{1B} = \Sigma(C_1 - B_1)^2$ and $\chi^2_{2B} = \Sigma(C_2 - B_2)^2$, where $C$ refers to photon counts in each bin and $B$ refers to the background level at the same bin. The probability that the two GRBs were both above their respective background levels and also drawn from the same distribution was

$$P_{echo} = P(\chi^2_{12})[1 - P(\chi^2_{1B})][1 - P(\chi^2_{2B})],$$  \hspace{1cm} (1)$$

where $P(\chi^2_{12})$ is the probability that both GRBs were drawn from the same parent distribution, given a reasonable range of $f$ and $\Delta t$, $P(\chi^2_{1B})$ is the probability that burst #1 was drawn from the background distribution, and $P(\chi^2_{2B})$ is the probability that burst # 2 was drawn from the background distribution. The maximum $P_{echo}$ value was then recorded.
Further study includes comparing the GRB light curves in each of the 4 energy bands of BATSE’s large area detectors. As gravitational lensing effects are independent of wavelength, each of the energy bands must show acceptable echo fits for the same scale factor $f$ and time offset $\Delta t$, independently. In other words, the two GRBs must have indistinguishable hardness ratios as a function of time. In addition, the time streams before and after each GRB are checked for precursor or post-event emission. Such events must occur for both GRBs consistently for the pair to be a lensing candidate.

3. RESULTS OF THE LENS SEARCH

No clear gravitational lens examples were found. More specifically, no two GRB time profiles were deemed both bright enough for adequate statistical comparison and identical in a statistical comparison. A “library of close calls” (LOCC) was founded into which pairs of GRB light curves with subjectively determined coincidental similarities were placed. This library serves the function of allowing us to estimate the background against which a real gravitational lens event must be judged. Most of the LOCC members are bursts where one or both is quite dim, quite short in duration, or quite featureless in appearance.

Only one pair from the Phase I search was deemed significantly similar to suggest a detailed statistical comparison. The light curves of these two GRBs, BATSE trigger numbers 788 and 1308, are shown in Figure 1a and 1b. These GRBs are 26 degrees apart. Their combined positional errors are such that if they were 11° apart, there would be approximately 31.8 % chance that they could have come from the same position. The positional errors are not well described by a Gaussian distribution at large angles, but we estimate that there is about a 10 % chance that the two GRBs could have come from the same position. These GRBs occurred roughly 131 days apart. The $P(\chi^2_{echo})$ statistic was computed for a range of time offsets and dynamic ranges to see if these two GRBs had light curves that were consistent with being drawn from the same parent distribution. Figure 1c shows that $P(\chi^2_{echo})$ values were never significant, and so these GRBs cannot be considered a candidate pair for gravitational lensing.

The second LOCC entry we show here is from the Phase II search. The GRB pair shown in Figure 2 is particularly interesting as they each are highly fluent, well resolved in
time, and show similar although relatively smooth time structure over their whole duration. The positions are 3.7 degrees apart on the sky, corresponding to 0.6 $\sigma$ of their combined positional error, and the events are separated by 55 days. This pair, however, is an example of how relatively featureless GRBs can fool our search criteria. Here we show all four channels of each GRB as well as the $P(\chi^2_{\text{echo}})$ for each channel in Figures 2a-2l. In several channels, the two GRBs show similarities. But upon inspection of the time profiles in different energy bands, it is clear that they have different spectra. One can see from the fits that no single $f$ factor is implied, and the widely different $f$ factors clearly exclude a gravitational lens origin for the similarity of these GRBs.

Last we discuss two GRBs that appear similar to the eye but not to a statistical comparison. The two GRBs with BATSE triggers 1085 and 1141 arrived 14 days apart. They are separated by 12 degrees on the sky, which again corresponds to only about a 10 % chance that the two GRBs could have originated from the same location due to their combined positional errors. Both light curves show similar gross features, but 1141 is actually both significantly longer and more complex than 1085. A statistical comparison of the light curves finds that $P_{\text{echo}}$ never even reaches $10^{-10}$. These GRBs are illustrated in Figure 3 to demonstrate how different bright GRBs are, in general, from each other, even after they have been selected for similarity of appearance!

4. DISCUSSION AND CONCLUSIONS

Should we have expected to find a lensed echo in the present search? The smallest number of BATSE detected GRBs that Mao (1992) predicted would be needed to be inspected to show a gravitational lens effect was 250. Including all the limiting constraints listed in the last section, we concluded even though 611 GRBs were compared, only effectively 50 GRBs would be considered genuine candidates to show such an event. Therefore, it is not surprising that we have not found a lens effect yet, and the lack of an echo cannot be used as evidence against a cosmological setting for GRBs. As pointed out in Wickramasinghe et al. (1993), the probability of lensing is a very strong function of the redshift distribution of GRBs, which is probably only weakly determined by modeling the brightness distribution. Measurements consistent with cosmological time dilation in GRBs
(Norris et al. 1994) appear to give a GRB redshift distribution that is consistent with the probability bounds estimated by Mao (1992) and the null detection found so far in this search.

There is some question as to whether a GRB lens image pair would be believed if it were found. As a GRB is a “once and done” occurrence, it is not possible to re-observe the GRB pair to test for other potentially similar characteristics. Certainly the impossibility of distinguishing two very weak GRBs should not lead to the conclusion that they are artifacts of gravitational lensing. Also, even for brighter bursts, some profiles that are common to many GRBs might be mistaken for a lens artifact.

Clearly, if all GRBs had intrinsically identical time profiles and power-law spectra, it would impossible to judge lens-induced similarity by these two attributes. In fact, it is a statement of how different GRBs are from each other that this search can be made at all. Toward this goal, we feel that the present work has value in helping to understand the background of similarities between GRBs against which a lensed pair echo must be judged.

Indeed, so far, we have found that GRBs are like snowflakes: no two gamma-ray bursts are alike. We note that qualitatively, the GRB comparison search is not much different than a QSO comparison search. QSO lens images must have identical redshift and spectra. Were all QSO spectra identical, it would be more difficult to determine lens pairs. Clearly then, an understanding of the background of similarities between QSO spectra is important in determining which are good candidates to be lens pairs.

Is it possible that two GRBs were identical but the above described statistical test gave an unrealistically low $P_{echo}$? We consider it possible but unlikely. There are at least two reasons for a false negative correlation. The first is that the time offset of the GRB comparison might have skipped over the true time offset between the GRBs. This is particularly problematic for GRBs described by only a few time bins, or GRBs that vary rapidly compared to the bin size (Wambsganss 1993). Clearly, the GRBs must be compared at a time-scale large compared to the bin size but small compared to their variability to alleviate this problem.

Secondly, comparisons might be mistakenly pessimistic if the background levels were significantly different during the detection times of the two GRBs. This could be caused by
different solar activity levels during GRBs, a bright gamma ray source entering or leaving earth’s shadow, or Compton entering or leaving the tail end of the South Atlantic Anomaly during one observation. These effects are most apparent at lower energies, typically visible primarily in channel 1 (25 - 50 keV), and are usually not dominate in channel 3 (100-330 keV) where the initial comparison of GRB light curves were made.

Lastly, local effects pertinent to the spacecraft and its environment might create false differences between the GRBs. More specifically, electron precipitation events (Horack et al. 1992) could add false peaks to a light curve, or data gaps not properly accounted for could delete peaks from a GRBs light curve. Such electron peaks are relatively rare, usually last for several seconds, and can usually be seen in all detectors simultaneously, whereas GRBs would only be seen in at most 4 detectors. Unusual data gaps, which are also relatively rare, have been made quite clear in the data when they occur and their effects have been removed.

Could gravitational microlensing change one light curve so that it no longer appears similar to its gravitational lens twin? We consider this unlikely. It is the smooth mass distribution in galaxies that is assumed to give rise to the multiple images of GRBs. It is these “macroimages” that have been searched for here. However, galaxies have at least a reasonable fraction of their mass in stars, and these stars may themselves become important if at least one of them approaches the light path of a macroimage. This is called microlensing (Chang and Refsdal 1979, Paczynski 1986a). Most probably the macroimages involved will undergo a microlensing effect, but the typical time-scale of such an effect is likely only on the order of milliseconds, for typical values of galactic shear and microlensing optical depth. Since the typical light curve we inspected was binned with 64 millisecond bins, a microlensing effect would not be evident. Only in the unlikely event that the optical depth is very near unity would stellar induced microimages widely separated across the lensing galaxy have power (Paczynski 1986a), possibly causing a microlensing time-scale large enough to relatively distort the measured GRB light curves.

Even if it is impossible to discern absolutely whether two GRBs are lensed images of the same GRB, it might be possible statistically. Future automated searches should not focus on only GRBs that are nearby each other, but also correlate GRBs from all over the
sky. GRBs that are similar but clearly originating from widely separated positions on the sky – such that lensing can not be attributed to a galaxy – should be more likely than those occurring near each other, and this can be tested statistically.

It is possible, even likely, that were one GRB image seen, one or all of its gravitational lens counterparts would be completely missed by BATSE. Conservatively, 40 % would be hidden from BATSE by the Earth when the second image came in, and another 30 % would be lost due to BATSE not being ready to record this GRB information when it came in, due to various gaps in experiment or satellite coverage. The combined error boxes were searched to angular separations such that, including both random and systematic errors, only 45 % of lens pairs would have been found. BATSE is not uniformly sensitive to GRBs from all directions. Therefore there could be GRB echoes that BATSE would not detect because the satellite was oriented non-optimally. We estimate that about 30 % of GRB echoes would be lost to this effect. We estimate that an additional 10 % of GRBs are too dim and of such simple structure that a statistical comparison with other GRBs would not be definitive. Some fraction of GRB counter-images would be missed because either the first image arrived before BATSE originally turned on, or the later image has yet to arrive. This last fraction is a function of lens parameters.

Although no specific cases were discussed here, several cases have been occasionally discussed where two images appear similar in shape but have markedly different time-scales between them (Desai 1993). Generally, it is impossible to create two images with markedly different time-scales through gravitational lensing. The only such scenario we can envision would require source emission angle to be strongly correlated with relativistic beam velocity. Then one lensed image might be seen at one relativistic $\gamma$ factor while other images might be caught at much different $\gamma$ factors, creating the discussed effect. Although searching for relatively stretched images is outside the capabilities for this reported search, no concrete case of such an effect has yet been called to our attention that has passed our criteria for a gravitational lens image pair, even when allowing for an arbitrary “stretching” factor.

An automated search procedure is being designed and should begin being implemented by the time this paper goes to press. We are hopeful this procedure will find a gravitational
lens echo, although again it is still somewhat unlikely.

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FIGURE CAPTIONS

**Figure 1:** Light curves and probability of echo results for two BATSE GRBs with trigger numbers 788 and 1308. These GRBs are not statistically identical enough to warrant a gravitational lens interpretation for their similarity.

**Figure 2:** Light curves and probability of echo results for two BATSE GRBs with trigger numbers 1733 and 1956. These GRBs are compared in all four energy channels. Although these high fluence GRBs have marked similarities, their significantly different hardness ratios exclude a gravitational lens interpretation.

**Figure 3:** Light curves and probability of echo results for two BATSE GRBs with trigger numbers 1085 and 1141. These relatively bright GRBs have similar shapes but are not statistically comparable. Most bright GRBs are not even this similar, however.