Metabolic modelling in a dynamic evolutionary framework predicts adaptive diversification of bacteria in a long-term evolution experiment

Tobias Großkopf¹, Jessika Consuegra²,3, Joël Gaffé²,3, John C. Willison⁴,5,6, Richard E. Lenski⁷,8, Orkun S. Soyer¹* and Dominique Schneider²,3*

Abstract

**Background:** Predicting adaptive trajectories is a major goal of evolutionary biology and useful for practical applications. Systems biology has enabled the development of genome-scale metabolic models. However, analysing these models via flux balance analysis (FBA) cannot predict many evolutionary outcomes including adaptive diversification, whereby an ancestral lineage diverges to fill multiple niches. Here we combine in silico evolution with FBA and apply this modelling framework, evoFBA, to a long-term evolution experiment with *Escherichia coli*.

**Results:** Simulations predicted the adaptive diversification that occurred in one experimental population and generated hypotheses about the mechanisms that promoted coexistence of the diverged lineages. We experimentally tested and, on balance, verified these mechanisms, showing that diversification involved niche construction and character displacement through differential nutrient uptake and altered metabolic regulation.

**Conclusion:** The evoFBA framework represents a promising new way to model biochemical evolution, one that can generate testable predictions about evolutionary and ecosystem-level outcomes.

**Keywords:** Adaptive diversification, Experimental evolution, FBA, In silico evolution, Tradeoffs

**Background**

The ability to predict evolution would be valuable not only for understanding such processes as adaptation and speciation [1–3], but also for engineering robust industrial strains, anticipating ecosystem responses to climate change, and combating antibiotic resistance [4–7]. Models that capture the relationship between genotypes and environments, the structure and state of regulatory and metabolic networks, and the resulting phenotypes are likely to be important for developing these predictive abilities [1, 3, 8].

Ultimately, models of the relationship between genotype and phenotype will need to be combined with models of evolutionary and ecological dynamics in integrated frameworks that can predict the trajectory of evolution [5, 9].

The dynamics of evolutionary change reflect multiple processes and varying selective pressures that are influenced by many ecological, physical, and cellular constraints that may conflict with one another. Understanding whether and how these dynamics lead to the splitting and divergence of lineages is of central interest, as these processes represent the initial steps towards speciation. To this end, several theoretical studies have shown that cellular tradeoffs can promote lineage divergence [10–16].

The importance of such tradeoffs can be readily understood in the context of metabolism and growth. For example, if there were no tradeoffs, then one would predict that cells should maximize their expression of transporters and their surface area to achieve the highest
possible rate of substrate uptake [17]. However, such cellular investments would impinge on other cellular processes owing to competing requirements for membrane and cytosol space [18, 19], ribosomes [15, 16], and redox carriers [20, 21]. Thus, cells may appear suboptimal for individual physiological parameters, but this might be merely a consequence of being optimal for the combined set of parameters and associated cellular tradeoffs.

Historically, the interplay between cellular tradeoffs and evolutionary and ecological dynamics has been analyzed using game theory and differential equation-based models that consider small or idealized metabolic systems [10, 11, 14, 22]. These studies have highlighted that tradeoffs in cellular metabolism can lead to incomplete degradation of a resource, resulting in the evolution of cross-feeding interactions [10, 11]. This phenomenon has been seen in several evolution experiments under both batch and chemostat conditions [23–27]. To increase predictive power in microbial ecology and evolution, it is now desirable to develop models that can take into account cellular metabolism at a larger scale and across different organisms. Stoichiometric models offer a promising approach because, in principle, they can capture all enzyme-mediated metabolic reactions of an organism in an unbiased and non-supervised way using genomic information [8].

Flux Balance Analysis (FBA) has been developed to determine the optimal metabolic state of an organism, given knowledge of its biochemical network, biomass composition, and uptake flux rates [28]. This approach is based on the assumptions that evolution has optimized metabolism and that metabolic fluxes can be predicted by setting the growth rate for a given rate of substrate uptake (such that the ratio of the two rates represents a yield) as an optimization criterion that can be solved by linear programming [28–30]. Early applications of FBA ignored the essential role of tradeoffs in the computation of metabolic fluxes [28, 31, 32], but more recent applications have incorporated tradeoffs as constraints on total fluxes [18, 19, 33, 34] and thereby achieved better prediction of experimentally observed metabolic states, such as preferential substrate utilization [19] and acetate overflow [18]. Experimentally measured reaction thermodynamics and gene expression levels have also been used to constrain optimal metabolic states that reflect tradeoffs [35–37], and there have been efforts to combine FBA with ecological interactions between multiple species in microbial communities [38–45]. These approaches use species-specific models in a shared environment to maximize a predefined, community-level objective [39, 41, 43, 44] or apply FBA within a dynamic framework [46]. The latter approach enables prediction of ecological interactions such as competition and cross-feeding between different species making up the model community, given defined substrate uptake constraints for each model species [40, 42, 45]. However, none of these approaches can currently be used to predict the interplay between ecological and evolutionary dynamics.

Here, we begin to overcome these limitations by integrating a FBA model of multi-phenotype systems with both cellular constraints and evolutionary dynamics. We define an overall constraint on uptake rates to enforce tradeoffs while simulating multiple model organisms living in the same environment without the need to specify each organism’s uptake preferences a priori (for details on how evolution and mutations are simulated see Methods section). By limiting total uptake in the model, and including O₂ “uptake” in that total, we seek to represent cellular limitations that can arise from many diverse processes, including redox cycling [20, 47], respiratory chain [18], enzyme expression [16, 48], and substrate uptake [17]. Although O₂ uptake per se might not be limiting, limitations in the electron transport chain can effectively limit O₂ respiration. Accounting for all the different possible limitations arising from cellular processes in a mechanistic manner is beyond the scope of stoichiometric models; however, limiting total uptake provides a general constraint that allows us to implement the tradeoffs observed in different studies in a simple, consistent, albeit approximate manner [16–18, 20, 47].

This approach allows integration of evolutionary dynamics by mutations that change substrate uptake rates along with the optimization of each model organism in the context of other model organisms that are present and coevolving in the same environment. The combined framework, which we call evoFBA, thus aims to provide a more realistic way to model the interplay between ecological and evolutionary dynamics with global constraints arising from cellular tradeoffs. To the best of our knowledge, this is the first FBA modeling approach that captures the continuous adaptation of organisms to the interplay between ecological and evolutionary dynamics in systems with multiple strains or species.

To examine the ability of evoFBA to capture ecological and evolutionary dynamics, we used it to simulate the evolution of *Escherichia coli* populations in a defined glucose-limited environment with daily transfers. We then experimentally analyzed the predictions of evoFBA in the context of the long-term evolution experiment (LTEE) with *E. coli*, in which 12 populations started from a common ancestor have been propagated in a glucose-limited medium for more than 60,000 generations [2, 49]. We found that the evoFBA simulations predicted the emergence of cross-feeding model organisms as a stable end-point, which in fact has occurred in at least one of the LTEE populations [26, 50]. Moreover, we saw that key metabolic features of the model organisms were in qualitative agreement with the physiological properties we
measured for the two biological lineages that emerged and subsequently coexisted for more than 50,000 generations.

**Results**

Microbial communities and their underlying metabolic interactions reflect the ecological and evolutionary histories of the component species [51]. To capture these interactions, we combine stoichiometric metabolic models with ecological and evolutionary dynamics in the multi-layered evoFBA framework (see Methods). To test the utility of this framework, we apply it to the LTEE in which *E. coli* populations evolve in a defined glucose-limited environment [2, 52].

To model the LTEE, we ran evoFBA simulations starting with a metabolic model of *E. coli* that accounts for 14 carbon sources including glucose and byproducts that can be scavenged from the environment to produce biomass and fuel associated core metabolic reactions. In each evoFBA simulation, we allowed the metabolic model to change by random mutations under global constraints that must be obeyed. Thus, each simulation produced mutant model organisms exhibiting different uptake rates, metabolic flux patterns, and resulting growth rates.

evoFBA predicts evolution of cross-feeding between lineages with different metabolic flux distributions

Starting from a population of identical model organisms under conditions similar to the LTEE, a typical evoFBA simulation produced through random mutations more than 90,000 genetically distinct model organisms over 550 simulated daily transfer cycles (Fig. 1). The evolutionary dynamics across replicate simulations were highly reproducible in their key features, in particular the diversification of the population into two coexisting lineages (Fig. 2). Thus, throughout the paper, we will focus on results from a typical representative simulation that resulted in 97,912 different model genotypes, of which 3943 survived at least one transfer event (Fig. 1a) and 12 reached a population

---

**Fig. 1** Evolutionary dynamics in silico. a Numbers of surviving cells (i.e., post dilution) after each simulated cycle on a logarithmic scale. Each curve shows one of the 3943 model organism genotypes that survived at least one cycle (see text). b Relationships among ancestral and mutant model genotypes for those that reached a population of at least $10^5$ cells at any point during the simulation (see Methods). Model ID indicates the identifier assigned to each model genotype, with 1 being the ancestor. Line thickness is proportional to the log$_{10}$-transformed number per 10-ml volume at the start of each cycle. Coloured bars show relative uptake rates for glucose (blue), acetate (red), and oxygen (green).
Fig. 2 (See legend on next page.)
size of at least $10^6$ cells at some point (Fig. 1b). These simulations revealed specific changes in oxygen, glucose, and acetate uptake by the model organisms (Fig. 1b). Glucose uptake and incomplete oxidation resulted in acetate secretion by the ancestral model organism, which would then switch to acetate uptake and oxidation after the glucose was exhausted. Thus, the ancestral model displayed a diauxic shift (Fig. 3a), as observed in *E. coli* [21]. As the *in silico* evolution proceeded, new model organisms arose that had increased glucose uptake and acetate production. The resulting increase in acetate concentration generated an ecological niche that was colonized by other model organisms with increased acetate uptake but reduced glucose uptake. After ~300 simulated daily transfer cycles (~2000 generations), the simulated evolution came to a halt, with no mutant model organisms able to replace the dominant ones. Thus, the *in silico* dynamics produced two distinct lineages that specialized on glucose and acetate, respectively. The glucose-specialist model organisms lost the ability to consume acetate, whereas the acetate-specialist model organisms retained the ability to consume glucose but at a lower rate, and the timing of their diauxic shift was changed (Fig. 3a). As a consequence, the simulation led to a stable cross-feeding relationship between two lineages of model organisms.

We then examined the metabolic fluxes for the two model organisms when growing on glucose and acetate (Fig. 4). On glucose, both the glucose and acetate specialists displayed similar behaviours, using the TCA cycle only partially and the glyoxylate shunt not at all (Fig. 4a and c). After switching to acetate consumption (which the glucose specialists could not do), the acetate specialists showed very different fluxes, with reverse glycolysis and full use of the TCA cycle including the glyoxylate shunt (Fig. 4b and d). We emphasize that the emergence of cross-feeding model organisms and their

---

**Fig. 2** Replicate runs of evoFBA. **a** One of five replicate simulations using the same parameter set as described in the main text and shown in Fig. 1. All simulations led to qualitatively similar outcomes. **b** Running evoFBA simulations with a smaller maximum mutation step size ($+/−1$ mmol/gDW/h), see Methods eq. 5), led to the same diversification into glucose specialist and glucose-acetate co-utilizing model organisms, although the time required to achieve the diversification was substantially longer. Model ID, line thickness and coloured bars are the same as in Fig. 1.

**Fig. 3** Simulated and experimental dynamics of population density and substrate concentrations. **a** Simulated dynamics over a 24-h transfer cycle for the evolved acetate specialist (left, ID: 44490), ancestral (middle, ID: 1), and evolved glucose specialist (right, ID: 12364) model organisms. Model IDs are the same as in Fig. 1b. **b** Experimental data for the 6.5KS1 (left), ancestral (middle), and 6.5KL4 (right) clones from the LTEE. Biological experiments were performed at a 10-fold higher concentration of glucose than the simulations to increase cell density and thereby improve the accuracy of the measurements of cell growth and concentrations of residual glucose and secreted acetate. Biological data are means of three replicate cultures and error bars show standard deviations.
associated fluxes in the evoFBA simulation represents an idealized evolutionary stable state given the assumptions of the evoFBA framework.

**Adaptive diversification in one LTEE population, matching evoFBA predictions**

Two distinct lineages had emerged in one of the LTEE populations, called Ara-2, by 6500 generations, and they have coexisted ever since [26, 50]. The lineages are called S (small) and L (large) after their colony sizes on agar plates. The maintenance of this polymorphism depends on a cross-feeding interaction in which the L type is a better competitor for the exogenously supplied glucose and the S type is better at using one or more secreted byproducts [26], although the precise ecological and metabolic mechanisms are still unknown. Therefore, we used predictions from the evoFBA simulations to generate hypotheses about these mechanisms.

We hypothesized that, first, L specializes on glucose and secretes acetate and, second, S specializes by improved acetate consumption. We tested this hypothesis by analyzing two evolved clones sampled at generation 6500 from the S and L lineages, named 6.5KS1 and 6.5KL4, respectively. HPLC analyses confirmed the presence of acetate in a 24-h supernatant of 6.5KL4 that was grown in the same medium as the LTEE (see Methods). Acetate was not detected after growing 6.5KS1 in that supernatant (Additional file 1: Figure S1). We then

---

**Fig. 4** Metabolite turnover fluxes in glycolysis and TCA cycle. Fluxes in the glucose specialist (a, b) and the acetate specialist (c, d) genotypes (model IDs 12364 and 44490, respectively) during growth on glucose (a, c) and acetate (b, d). The following metabolites and reactions are shown: ac, acetate; acp, acetyl-phosphate; akg, alpha-keto-glutarate; cit, citrate; f6p, fructose-6-phosphate; fum, fumarate; glx, glyoxylate; g6p, glucose-6-phosphate; icit, isocitrate; mal, malate; oaa, oxaloacetate; pep, phospho-enol-pyruvate; succ, succinate; succoa, succinyl-coenzyme a. PGI, ACN, ACE, and ACK are the reactions catalyzed by glucose-phosphate isomerase, aconitate hydratase, malate synthase, and acetate kinase, respectively (shown in blue). Thickness of the arrow indicates the flux over the given reaction; the reference arrow at the bottom right shows a flux of 10 mmol/gDW/h.
measured the acetate and glucose concentrations over time in cultures of the ancestor, 6.5KS1, and 6.5KL4 clones in DM250-glucose medium (Fig. 3b). Both the L and S clones consumed glucose faster than the ancestor, consistent with previous assays [53]. Moreover, in agreement with the evoFBA results, 6.5KL4 secreted acetate, with its concentration remaining high for many hours in the monoculture, and 6.5KS1 drew down its own acetate secretion much faster than both 6.5KL4 and the ancestor. After exhausting the glucose by 6 h, 6.5KS1 showed diauxic growth and consumed acetate until it was depleted after 9 h, whereas 6.5KL4 had barely, if at all, begun to consume acetate at that time even as it had exhausted the glucose by 5 h (Fig. 3b). These results support the hypothesis that the stable coexistence of S and L depends on acetate cross-feeding, with acetate production by both the L and S lineages and more efficient acetate scavenging by the S lineage, which exhibits a faster metabolic switch from glucose to acetate (Additional file 2: Figure S2).

Physiology and fluxes in S and L clones agree qualitatively with evoFBA
The evoFBA simulation reaches an evolutionary equilibrium, whereas the interaction between the S and L lineages remained highly dynamic over thousands of generations [26]. Therefore, we examined the metabolic divergence of the S and L lineages over the course of the LTEE. We first measured the ability of clones from earlier and later generations to grow in minimal media containing glucose or acetate. S clones from later generations typically grew faster and with a shorter lag phase on acetate and more slowly on glucose than S clones from earlier generations, while the opposite trends were observed in the L lineage (Additional file 3: Figure S3) (in line with previous observations [53]). Compared to the ancestor, S clones improved their growth on acetate over evolutionary time, while L clones initially improved somewhat but were variable, with the 50,000-generation L clone showing weak growth similar to the ancestor (Fig. 5). On glucose, the opposite trend was observed with L clones consistently improving compared to the ancestor, while S clones improved initially but declined in later generations (Fig. 5). These patterns of growth relative to the ancestor are consistent with previous assays using the LTEE clones [53, 54]. These evolutionary trajectories of growth on acetate and glucose indicate character displacement and suggest tradeoffs that prevent the simultaneous optimization of growth on both carbon sources. The trajectories are qualitatively consistent with the evoFBA simulations, although the evoFBA predicts complete specialization on glucose without any acetate consumption. This evoFBA prediction represents a potential evolutionarily stable end point, which might eventually occur in the S and L lineages after more generations.

We then tested the flux patterns predicted by evoFBA (Fig. 4) by measuring, in several LTEE clones, the promoter activities of genes encoding four key metabolic enzymes, using transcriptional fusions with the gfp reporter gene (see Methods). Both S and L clones showed moderately increased promoter activity for pgp relative to the ancestor (Fig. 6). Both S and L clones exhibited larger increases in the promoter activities of acnB and aceB relative to the ancestor, with the S clones showing much greater increases than the L clones, consistent with the possibility of greater flux through the TCA cycle and glyoxylate shunt in the S acetate specialists. There were no obvious changes in the promoter activities of ackA in either the S or L lineages. Of course, there may be discrepancies between promoter activities and actual enzyme activities [55, 56]. Nonetheless, these patterns agree reasonably well with the flux predictions from the evoFBA simulations, especially as they relate to the higher activities in the S lineage of the genes that specifically promote growth on acetate. As noted above, we reiterate that the evoFBA simulations predict an eventual complete loss of the acetate-specific activities in the L lineage, whereas thus far they are merely expressed at a lower level in the L lineage than in the S lineage.

Discussion
We developed a modeling framework, called evoFBA, which combines metabolic models that are amenable to FBA with an evolutionary algorithm to simulate the interplay of evolutionary and ecological dynamics in systems with multiple strains or species. We applied evoFBA to the LTEE with E. coli and predicted the emergence of two stably coexisting lineages with distinct metabolic flux distributions that promote a cross-feeding interaction. These predictions fit with the polymorphism seen in the Ara−2 population, where two lineages emerged early in the LTEE that have now coexisted for tens of thousands of generations [26, 50]. The evoFBA simulations enabled us to hypothesize specific ecological and physiological mechanisms that generate and sustain this polymorphism, and we then tested these hypotheses using the bacteria from that LTEE population. On balance, we found that the ecological, physiological, and metabolic properties of these coexisting lineages agree reasonably well with the predictions of the evoFBA.

Only one of the 12 LTEE populations evolved a persistent polymorphism that has been studied in such detail [26, 50]. However, other LTEE populations show evidence of negative frequency-dependent fitness, deep phylogenetic divergence, or both, which are consistent with adaptive diversification [57–60]. These results
Fig. 5 Changes in growth rates of S and L on glucose and acetate over evolutionary time. Growth of S and L clones sampled at multiple generations of the LTEE was followed in DM250-acetate (a) and DM250-glucose (b) media. Clone names are shown above the horizontal red and blue bars, which denote S and L clones, respectively. The ancestor (Anc) and a 2000-generation clone (2K4) isolated prior to the divergence of the S and L lineages are also included. Growth rates (1/h) are shown according to the colour scale for 1-h sliding windows over 24-h and 7-h periods in the acetate and glucose media, respectively. Empty cells indicate missing values based on filtering negative rates or unreliable values (see Methods).

Fig. 6 Transcription levels of four genes encoding metabolic enzymes in the ancestor and evolved clones. Promoter activities measured as \((\text{dGFP/dt})/\text{OD}_{450}\) for genes involved in glucose and acetate metabolism during the first 8 h of growth in DM250-glucose. The clones are, from left to right: 50KS1, 6.5KS1, ancestor (Anc), 6.5KL4 and 50KL1. The genes are, from top to bottom: \(\text{pgi}\) encoding glucose phosphate isomerase, \(\text{acnB}\) encoding aconitate hydratase, \(\text{aceB}\) encoding malate synthase A, and \(\text{ackA}\) encoding acetate kinase. Activity values are means based on three-fold replication of each assay.
suggest that other populations may have evolved crossfeeding interactions similar to the one studied here, even if they were not always so persistent [59]. One possible explanation for why persistent polymorphisms did not evolve in the other populations is that the establishment of the S lineage appears to have involved epistatic interactions between multiple mutations [50], which may have limited its evolutionary accessibility [58]. This possibility reflects one of the limitations of evoFBA, which cannot capture all of the intricacies of biological evolution but instead predicts optimal end states that emerge given the simplifying assumptions of this approach. For example, mutations in evoFBA affect the rates of resource uptake, but not the rates of internal reactions in the model. This limitation reflects the computational burden of simulating a multitude of mutant genotypes, the number of which would increase greatly if all reaction rates were subject to mutation. This limitation could be relieved by the development of more efficient algorithms (allowing mutations to affect all reactions in the model), but the final evolved model organisms might not differ functionally from those based on the current approach because changes in uptake rates can already affect downstream flux distributions. Another limitation of the evoFBA approach at this time is the assumption that constraints on the uptake fluxes can be changed only by mutation, while the optimization of fluxes within those constraints is immediate through FBA [32]. In other words, metabolic fluxes change within physiological limits without delay, whereas changing the limits themselves requires mutations. These assumptions are reasonable starting points for incorporating evolutionary dynamics into an FBA framework, but physiological delays in metabolic adjustments are also sometimes important [61, 62]. Expanding the evoFBA framework to include the dynamics of physiological transitions could start by integrating previous work on incorporating gene regulation into FBA [63, 64].

Adaptive diversification is expected, and has occurred, in other evolution experiments besides the LTEE, such as when two exogenous carbon sources are provided [27, 65] and in high-glucose chemostats, where substantial acetate is produced [21, 23, 25]. However, the adaptive diversification observed in the LTEE was unexpected owing to the presence of a single carbon source, glucose, which was supplied at a low concentration [52]. Using the evoFBA framework, we predicted that acetate secretion was the primary metabolic driver leading to the emergence of the polymorphism, and that prediction was supported by our experiments. The long duration of the LTEE—including several thousand generations to establish the S and L polymorphism [26] and its persistence for tens of thousands of generations [60]—may have facilitated adaptive divergence under these more restrictive ecological conditions, in comparison with other studies of much shorter duration where glucose, acetate, or both were supplied exogenously at high concentrations [23, 25, 45]. In fact, low levels of acetate, as observed in our study, have previously been reported to favor generalists as opposed to divergence into coexisting specialists [10]. Nonetheless, the L lineage evolved higher glucose uptake rates, which led to acetate overflow and the construction of a new niche that benefited the S lineage, as occurred in the evoFBA simulations. Thus, niche construction by the bacteria led to the emergence of this polymorphism, in contrast to experiments where both carbon sources were added to the medium [45]. Despite the differences between the LTEE and previous evolution experiments [45, 65], similar metabolic processes emerged.

Conclusion

The combination of evoFBA and experimental evolution provides a useful approach that can give insights into general mechanisms involved in the emergence of bacterial diversity and community construction. This approach may stimulate the development of even more detailed and integrated studies aimed at predicting the outcomes of evolution experiments and dynamics in multi-species systems including synthetic microbial communities [51].

Methods

Evolutionary flux balance analysis (evoFBA)

In each evoFBA simulation, stoichiometric metabolic models were used to simulate clonal populations with distinct genotypes. Each genotype was represented by a metabolic model, which was simulated in a dynamical FBA formalism [46] to evaluate its growth and metabolic flux rates over time. At each time step of the dynamic FBA, the metabolic model was optimized using linear optimization and a pseudo-reaction representing biomass as the objective function [66]. This optimization thus maximized growth rate given the constraints on uptake rates, i.e. it optimized biomass yield per substrate [67]. Instead of defining specific uptake rates for a particular set of media components (as in standard FBA studies), we assumed a global constraint for all carbon and oxygen uptake reactions in each model organism. By limiting total uptake in the model (including O₂ “uptake”), we represent cellular limitations that can arise from many different factors, including redox cycling [20, 47], respiratory chain [18], enzyme expression [16, 48], and substrate uptake [17]. Similar implementations of global constraints in FBA models have been employed previously to study diauxic shift and substrate preference in *E. coli* [18, 19, 37]. The global uptake constraint implemented here favored a minimization of fluxes given the
maximization of the FBA objective in order to achieve the most efficient use of cellular resources for growth [34].

New model organisms were generated by random mutation from existing ones. Mutations altered specific bounds on individual uptake rates, while maintaining an overall total flux constraint of carbon and oxygen into the model organism. Thus, mutations change how the overall uptake flux is distributed across different substrates, and they allow a second level of optimization to occur over evolutionary time in addition to the optimization that occurs by FBA over the physiological time scale. Focusing evolution on a subset of reactions made computation of the ecological and evolutionary dynamics feasible; even so, the simulations presented here took over 20 days on a dedicated high-performance computer to simulate over 90,000 different model organism genotypes and their associated population and metabolite dynamics. A more complete simulation might encompass genome-scale models with evolution of all reactions in the model and with global constraints on total protein biomass [19] and membrane space [18]. The current implementation of evoFBA was unable to perform such simulations in a reasonable timeframe and with appropriate numbers of replicate simulations; efforts to run evoFBA with mutations allowed for all reactions caused a slowdown of over 10-fold relative to the current implementation.

For the evoFBA simulations, we implemented the in silico equivalent of the LTEE with E. coli. The simulations started with a population comprised of a single model genotype that represented the central metabolism of E. coli [68]. This model included 95 reactions, 75 metabolites, and 20 exchange reactions. The uptake of nutrients from the medium (i.e., the flux over the exchange reactions) was simulated by a Michaelis-Menten function for each substrate, $v_j$, as follows:

$$v_j = \frac{v_{\text{max},j} [S_j]}{K_m + [S_j]}$$

(1)

where $v_{\text{max},j}$ is the maximum uptake rate of the $j$th substrate in millimoles per g dry weight per h (mmol/gDW/h), $[S_j]$ is the concentration of the $j$th substrate in mmol/l, and $K_m$ is the half-saturation constant of the transporter in mmol/l. For simplicity, we arbitrarily set the initial $K_m$ values for all uptake reactions to 0.01 mmol/l. The $v_{\text{max},j}$ values were allowed to evolve by mutation (see next section below). The value of $v_j$ was then used as the uptake bound for the exchange reaction of each substrate when running FBA. For each simulated day, we evaluated each model using dynamic FBA [46] over the course of 24 h with 1-min steps; the simulation used a 10-ml batch reactor, as in the LTEE. At each time step, we set the $v_j$ values for each model using Eq. 1, used FBA to determine growth rate, and updated the biomass as follows:

$$BM_{t+1,i} = BM_{t,i} \left(1 + \frac{\mu_i}{\ln(2) \cdot 60}\right)$$

(2)

where $BM_{t,i}$ is the biomass in gDW of the clone represented by the $i$th model genotype at time $t$, and $\mu_i$ is the growth rate of that model computed by FBA [29]. After updating the biomass of all model genotypes, the resulting concentration of each substrate was reset as follows:

$$[S]_{j,t+1} = [S]_{j,t} - \sum_i BM_{t,i} v_{j,i} \cdot 60 \cdot V$$

(3)

where $[S]_{j,t}$ is the substrate concentration of the $j$th substrate at time $t$ (mmol/l), $BM_i$ is the biomass of the $i$th model clone at time $t$ (gDW/l), $v_{j,i}$ is the uptake rate of the $j$th substrate by the $i$th model genotype as computed by FBA (mmol/gDW/h), and $V$ is the culture volume (l). To mimic the LTEE, we started each day’s culture with glucose at 0.1389 mmol/l. The culture was started with one model genotype (i.e., the core E. coli model [68]) having a $v_{\text{max}}$ for glucose and acetate of 10 mmol/gDW/h each, and for oxygen of 20 mmol/gDW/h, i.e. the total uptake constraint was set at 40 mmol/gDW/h based on previous values for the combined uptake of carbon and oxygen [67]. The individual uptake rates for 14 carbon sources represented in the E. coli core model (acetate, acetaldheyde, α-ketoglutarate, ethanol, formate, fructose, fumarate, glucose, glutamine, glutamate, lactate, malate, pyruvate, succinate) and oxygen were subject to mutation in evoFBA. The exchange rates for phosphate, ammonia, water, protons, and carbon dioxide had no limits, reflecting the fact that carbon is the growth-limiting factor in the LTEE.

Representing mutations in evoFBA

The point mutation rate of E. coli in the LTEE (excluding populations that evolved mutator phenotypes [60]) has been estimated to $\sim 10^{-10}$ per base pair per generation, which equals $\sim 4 \times 10^{-4}$ per genome per generation [69]. Directly mapping mutations from bacteria to evoFBA model organisms is not possible. The mutable “genome” in the model organism has only 15 targets, as opposed to thousands of genes and millions of base pairs in an E. coli genome. Owing to these differences and computational limitations, we introduced mutations at the rate of $10^{-6}$ per model cell per generation in evoFBA. During the simulations, mutations were introduced into the population of each model genotype at each time step (i.e., simulated minute) according to the number of cells...
produced in that step and those expected to contain a mutation \( N_{m(i)} \) as follows:

\[
N_{m(i)} = \frac{N_i \mu_i}{\ln(2) \cdot 60 \cdot 10^6}
\]  

(4)

where \( N_i \) is the population size of model organism \( i \), \( N_i \) was calculated from the biomass of model clone \( i \) divided by the mass of one cell in gDW; we used a mass of 600 fg/cell, which was reported previously for exponentially growing \( E. coli \) cells [70]. When \( N_{m(i)} \) was between 0 and 1, \( N_{m(i)} \) was used as a probability to determine whether or not a mutant was introduced; when \( N_{m(i)} \) was \( \geq 1 \), a single mutant was always introduced.

As noted, each genotype in evoFBA corresponds to a different stoichiometric model with associated \( \nu_{\text{max}} \) values. When a mutation occurred, one of the uptake reactions was chosen at random and the maximum rate for that reaction was changed as follows:

\[
\nu_{\text{max}, m, \text{new}} = \nu_{\text{max}, m, \text{old}} + a
\]

(5)

where \( \nu_{\text{max}, m, \text{new}} \) and \( \nu_{\text{max}, m, \text{old}} \) are the new and old rates for the mutated reaction \( m \), and \( a \) is a random number from the uniform distribution over the interval \((-10,10)\). Each individual uptake rate was further constrained to lie between 0 and 40, such that the total uptake rate of 40 mmol/gDW/h was not violated. After any mutation, all other uptake reactions were updated as follows:

\[
\nu_{\text{max}, j, \text{new}} = \sum_k \nu_{\text{max}, k, \text{old}} \left( 40 - \nu_{\text{max}, m, \text{new}} \right)
\]

(6)

where \( k \) includes all uptake reactions except the mutated one. This adjustment ensures a constant total uptake flux across the membrane of 40 mmol/gDW/h. This mutation scheme generates strong tradeoffs between uptake reactions. The large effects of the mutations on reaction rates were chosen for computational speed of the evolutionary simulations; additional simulations with smaller maximum mutation steps produced qualitatively similar results (Fig. 2).

Simulating serial transfer and selection

To simulate the LTEE’s daily transfer cycles [2], we used dynamical FBA to compute growth over 24 h; selection is a direct consequence of the differential growth of the model genotypes. After 24 h, a dilution was performed by randomly drawing 1% of the model organisms, which constituted the initial population for the next simulated day. The next day’s medium included 99% of the initial medium and 1% of the spent medium from the end of the previous day. The simulated growth and dilution ran for a total of 550 cycles. Results from replicate simulations (Fig. 2) are qualitatively similar to those in Fig. 1.

The population dynamics arising from these simulations are expected to give rise eventually to one dominant clone in each stably coexisting lineage. However, similar model organisms may occur within a simulation as a result of independent mutations before any one of them has reached its population maximum (e.g., model genotypes 13437, 12364 and 12719 in Fig. 1). However, if the model organisms differ even slightly in their uptake rates, then one genotype should eventually prevail through competitive exclusion, unless the model organisms occupy distinct ecological niches (Fig. 1).

**Computation**

Simulations were performed using MATLAB (Math Works, Natick, Massachusetts) and dynamic FBA calculations using the COBRA toolbox [71]. The MATLAB scripts used to run evoFBA and analyze the data are freely available at [72].

**LTEE and bacterial strains**

The LTEE consists of 12 populations founded from the same ancestral strain of \( E. coli \), REL606 [73], that have been propagated since 1988 by daily 1:100 dilutions in Davis minimal medium [52] supplemented with glucose at 25 mg/l (DM25). Here, we focused on one population, called Ara–2, in which two lineages, S and L, diverged before 6500 generations and have co-existed ever since [26, 50, 60]. We studied the ancestor and one clone sampled from each lineage at 6500, 11,000, 18,000, 20,000, 30,000, 40,000 and 50,000 generations. Each evolved clone is named by its generation followed by S or L according to its lineage and an arbitrary numeral for a given clone. For example, 6.5KS1 is a clone from the S lineage that was sampled at 6500 generations.

**Media and culture conditions**

Bacteria were grown in the same medium as used in the LTEE [52], except that the carbon source was glucose at 250 mg/l (DM25-glucose), glucose at 1000 mg/l (DM1000-glucose), or acetate at 250 mg/l (DM250-acetate). These higher concentrations were used to increase cell density and thereby improve the accuracy of measurements of cell growth (e.g., Fig. 5) and concentrations of residual resources and secreted metabolites (e.g., Additional file 1: Figure S1). After overnight growth in DM1000-glucose, strains were inoculated by a 10,000-fold dilution into DM250-glucose, where they grew for 24 h at 37 °C with shaking at 120 rpm as an acclimation step. For each strain, three replicate acclimation cultures were then inoculated as duplicates, each at a 1:100 dilution, into DM250-glucose or DM250-acetate and incubated in 96-well microtiter plates at 37 °C for 24 h. Growth was monitored using an Infinite M200 microplate reader (Tecan, Lyon, France) by measuring the OD_{450nm} every
10 min. Growth rates were computed from filtered OD data as $\frac{d\ln(OD_{590})}{dt}$ over a sliding window of 1 h, using MATLAB. We report the mean of the three replicates. Filtering was performed by removing negative growth rates and mean growth rates that were more than 0.2 units above or below the immediately adjacent data points (outliers).

**Measuring glucose and acetate concentrations**
The ancestor, 6.5KS1, and 6.5KL4 clones were grown in DM250-glucose as described. Samples were taken at time 0 and every h for 9 h. After centrifugation to remove cells, we measured glucose and acetate concentrations in the supernatant using the Glucose Assay Kit (Merck Millipore, Lyon, France) and Acetic Acid Assay Kit (Megazyme, Pontchaarra-sur-Turdine, France), respectively, following the manufacturers’ recommendations.

**Analysis of flux patterns in individual model organisms**
We simulated the growth of the evoFBA model organisms with IDs 44490 and 12364 (Fig. 1) to obtain the flux values for their biochemical reactions. Each model organism was simulated using dynamical FBA in medium containing 0.1389 mM glucose, the same concentration as in the LTEE. Each simulation ran for ten 24-h periods with daily 1:100 dilutions; the last day was used to record the flux values, in order to remove any effect of the initial conditions. The flux patterns for growth on glucose were taken 10 min after the onset of growth (Fig. 4a and c), and for growth on acetate at 388 min because glucose was exhausted while acetate was still present at a substantial level (Fig. 4b and d). From the flux patterns, we identified several reactions of interest that showed differences between the two evolved model organisms (highlighted in blue in Fig. 4).

**Identification of metabolites in filtrates of spent cultures of 6.5KL4**
We analyzed by HPLC and GC-MS the metabolic byproducts secreted by clone 6.5KL4 using filtrates from 24-h spent cultures of that clone in DM25- and DM250-glucose, both before and after growth of clone 6.5KS1. For HPLC, 1 ml of filtrate was acidified with 5 μl 1 M H$_2$SO$_4$, incubated at room temperature for 5 min, and passed through a 0.45-μm regenerated cellulose syringe filter (PHENEX RC Membrane, Phenomenex, Le Pecq, France). Samples were then analyzed on an Agilent 1260 Infinity HPLC system equipped with a Rezex ROA-Organic Acid (8 %) 300 x 7.8-mm column ( Phenomenex) and a diode array detector. The analytical conditions were as follows: mobile phase, 5 mM H$_2$SO$_4$; flow rate, 0.6 ml/min; column temperature, 35 °C; injection volume, 50 μl; wavelength scan range, 190–400 nm; detection wavelength, 210 nm; and run time, 35 min. Concentrations of acetate and fumarate in the L-clone filtrates were determined from linear standard curves over the ranges of 0–10 mM and 0–100 μM, respectively, and with lower detection limits of 0.1 mM and 0.3 μM, respectively. Succinate, lactate, formate, propionate, and butyrate can also be separated under these analytical conditions with detection limits similar to acetate, but they were not detected in any samples.

GC-MS analysis of volatile compounds was performed using an Agilent GC HP6890 gas chromatograph equipped with a Varian CP-WAX 58 column (length, 25 m; internal diameter, 0.25 mm; film thickness, 0.20 μm), and coupled to an MSD5973 mass sensitive detector. The sample (600 μl) was cooled on ice, acidified with 50 μl 4 M HCl, and extracted with 0.375 g NaCl and 650 μl ice-cold ether. After vortexing three times for 10 s each, with 30 s cooling intervals, the sample was centrifuged for 5 min at 10,000 rpm and placed on ice for 5 min. The upper organic layer (2.5 μl) was then injected manually into the GC using an ice-cold syringe (injection in split mode, split ratio = 10). The column was held at 40 °C for 1 min, ramped to 200 °C at a rate of 5 °C/min, and held for a further 3 min, giving a total run time of 36 min. The solvent delay for the MSD was 1.4 min and the mass scan range was set to 35–300 atomic mass units. The presence of acetate (retention time 12.2 min) in the L filtrate after growth in both DM25- and DM250-glucose was confirmed by this method. The estimated concentration from the DM250-glucose filtrate was 510 μM, which is close to the 480 μM detected by HPLC (Additional file 1: Figure S1). The concentration of acetate in the L filtrate from DM25-glucose was about one-tenth that detected in DM250-glucose. Ethanol (retention time 2.1 min) was also detected in the filtrates of all three strains tested (ancestor, 6.5KL4, and 6.5KS1). Other metabolites including isopropanol, butanol, acetoin, acetone, formic acid, propionic acid, butyric acid, isobutyric acid, and valeric acid were not detected (with lower detection limits of 0.1 mM and 0.3 μM, respectively).

**Analysis of promoter activities in LTEE clones**
We measured the activities of the promoters of four genes—pgi, acnB, aceB, and ackA—that encode enzymes associated with reactions of interest (Table 1) given the results of evoFBA (Fig. 4). We used the corresponding

| Name                      | Gene ID | Gene | Protein | FBA model term |
|---------------------------|---------|------|---------|----------------|
| Glucose-phosphate isomerase | 948535  | pgi  | PGI     | PGI            |
| Aconitate hydratase       | 944864  | acnB | ACN     | ACN            |
| Malate synthase A         | 948512  | aceB | ACE     | MALS           |
| Acetate kinase            | 946775  | ackA | ACK     | ACKr           |
reporter plasmids from the *E. coli* library of *gfp* transcriptional fusions [74]. Each of the four plasmids, as well as the empty pUA66 reference plasmid, was introduced into the ancestor, 6.5KS1, 6.5KL4, 50KS1, and 50KL1 clones. Each plasmid-bearing clone was grown in DM250-glucose supplemented with 25 μg/ml kanamycin. Both OD450nm and GFP fluorescence were measured every 10 min for 24 h in the microplate reader. Promoter activities were estimated as the rate of GFP production from the promoter region [74]. They were computed using MATLAB as (dGFP/dt)/OD450nm, where GFP is the fluorescence signal after subtracting the value for the empty plasmid and division by OD450nm standardizes the data with respect to cell biomass density. We show the mean values from three replicate experiments (Fig. 6).

Additional files

**Additional file 1: Figure S1.** HPLC profiles of filtrate from spent cultures of 6.5KL4 before and after growth of 6.5KS1. Partial HPLC chromatograms, scaled in milli Absorbance Units (mAU) at 210 nm, showing elution time (min) of key metabolites for the filtrate of a 24-h spent culture of clone 6.5KL4 in DM250-glucose (A), and for the same filtrate after 24 h of growth of clone 6.5KS1 at 37 °C (B). The L filtrate contained 2-hydroxylglutarate, acetate, and fumarate. The S clone consumed the acetate and fumarate, but not the 2-hydroxylglutarate. The acetate peak indicates a concentration of 480 μM whereas the fumarate peak indicates a concentration of only 0.67 μM; the molar absorption coefficient of fumarate at 210 nm is more than 300 times greater than that of acetate. (PDF 64 kb)

**Additional file 2: Figure S2.** Diauxic growth in DM250 medium containing glucose and acetate at 10:90 ratio. Clone 6.5KS1 (red) exhibits a diauxic shift from glucose to acetate consumption much earlier than either the ancestor (green) or clone 6.5KL4 (blue). Curves show the average of three biological replicates. (PDF 113 kb)

**Additional file 3: Figure S3.** Growth curves of the ancestor and evolved clones in DM250-glucose and DM250-acetate media. A Growth curves of the Anc and pre-divergence clone 2 K4 (both shown in green) on glucose (left) and acetate (right). B Growth curves of S (red) and L (blue) clones sampled at seven generations (6.5, 11, 18, 20, 30, 40, and 50 K) arranged chronologically from top to bottom) on glucose (left) and acetate (right). In each panel, curves show the average (heavy line) of 3–6 replicate assays (lighter lines) for each clone; curves for individual replicates are not always visible when they are close to the mean or other replicates. (PDF 186 kb)

Acknowledgements

JC acknowledges the French ministry of research for a research fellowship. This work was supported by grants from the Biotechnology and Biological Sciences Research Council (BB/R022324/1 to OSS), Agence Nationale de la Recherche Programme Blanc (ANR-08-BLAN-0283-01 to DS), European Union programme FP7-ICT-2013-10 project EvoEvo (610427 to DS), Centre National de la Recherche Scientifique (CNRS, to DS), the U.S. National Science Foundation (DB91451740 to REL), and the BEACON Center for the Study of Evolution in Action (NSF Cooperative Agreement DBI-0939454 to REL).

Authors’ contributions

JC, TG, JG performed the experiments, analysed and interpreted the data, and drafted the article; JW performed the HPLC experiments and drafted the article; JC, TG, DS, OSS designed the study, analysed and interpreted the data, drafted and revised the article; REL directs the LTEE and helped draft and revise the article. All authors read and approved the final manuscript.

Competing interests

The authors declare that they have no competing interests.

Author details

1 School of Life Sciences, University of Warwick, Coventry, UK. 2 University of Grenoble Alpes, Laboratoire Techniques de l’Ingenierie Medicale et de la Complexite - Informatique, Mathematiques et Applications, Grenoble (TIMC-IMAG), F-38000 Grenoble, France. 3 Centre National de la Recherche Scientifique (CNRS), TIMC-IMAG, F-38000 Grenoble, France. 4 University of Grenoble Alpes, Institut de recherches en technologies et sciences pour le vivant – Laboratoire de chimie et biologie des metaux (iRTSV-LCBM), Grenoble F-38000, France. 5 CNRS, iRTSV-LCBM, F-38000 Grenoble, France. 6 Commissariat à l’énergie atomique (CEA), iRTSV-LCBM, F-38000 Grenoble, France. 7 Department of Microbiology and Molecular Genetics, Michigan State University, East Lansing, MI 48824, USA. 8 BEACON Center for the Study of Evolution in Action, Michigan State University, East Lansing, MI 48824, USA.

Received: 21 April 2016 Accepted: 4 August 2016

References

1. Stern DL, Orgogozo V, Pierre U, Bâtiment A, Saint Q. Is genetic evolution predictable? Nonrandom distribution of evolutionarily relevant mutations. Science. 2009;323:476–51.
2. Wiser MJ, Ribeck N, Lenski RE. Long-term dynamics of adaptation in asexual populations. Science. 2013;342:1364–7.
3. de Visser JAGM, Krug J. Empirical fitness landscapes and the predictability of evolution. Nat Rev Genet. 2014;15:480–90.
4. Nesse RM, Stearns SC. The great opportunity: Evolutionary applications to medicine and public health. Evol Appl. 2008;1:128–48.
5. Soyer OS, D’Malley MA. Evolutionary systems biology: What it is and why it matters. BioEssays. 2013;35:696–705.
6. Lobbeck KT, Riebesell U, Reusch TBB. Adaptive evolution of a key phytoplankton species to ocean acidification. Nat Geosci. 2012;5:346–51.
7. Novais Â, Comas I, Baquero F, Cantón R, Coque TM, Moya A, et al. Evolutionary trajectories of beta-lactamase CTX-M-1 cluster enzymes: Predicting antibiotic resistance. PLoS Pathog. 2010;6:e1000735.
8. Papp B, Notebaart RA, Pál C. Systems-biology approaches for predicting genomic evolution. Nat Rev Genet. 2011;12:591–602.
9. Prosser JI, Bohannan BJM, Curtis TP, Ellis RJ, Firestone MK, Fredleaton RP, et al. The role of ecological theory in microbial ecology. Nat Rev Microbiol. 2007;5:389–92.
10. Doebeli M. A model for the evolutionary dynamics of cross-feeding polymorphisms in microorganisms. Popul Ecol. 2002;44:59–70.
11. Pfeiffer T, Bonhoeffer S. Evolution of cross-feeding in microbial populations. Am Nat. 2004;163:E126–35.
12. Gudely J, Beadmore RE, Arkin SS, MacLean RC. Constraints on microbial metabolism drive evolutionary diversification in homogeneous environments. J Evol Biol. 2007;20:1892–90.
13. Schuster S, Pfeiffer T, Fell DA. Is maximization of molar yield in metabolic networks favoured by evolution? J Theor Biol. 2008;252:497–504.
14. Pfeiffer T, Schuster S, Bonhoeffer S. Cooperation and competition in the evolution of ATP-producing pathways. Science. 2001;292:504–7.
15. Molenar D, van Berlo R, de Ridder D, Teusink B. Shifts in growth strategies reflect tradeoffs in cellular economics. Mol Syst Biol. 2005;1:323.
16. Weißt AY, Oyarzún DA, Danos V, Swain PS. Mechanistic links between cellular trade-offs, gene expression, and growth. Proc Natl Acad Sci U S A. 2007;104:12663–8.
17. Button D. Nutrient uptake by microorganisms according to kinetic parameters from theory as related to cytoarchitecture. Microbiol Mol Biol Rev. 1998;62:636–56.
18. Zhuang K, Vemuri GN, Mahadevan R. Economics of membrane occupancy and respiro-fermentation. Mol Syst Biol. 2011;7:500.
19. Beg QK, Vazquez A, Ernst J, de Menezes MA, Bar-Joseph Z, Barabási A-L-L, et al. Intracellular crowding defines the mode and sequence of substrate uptake by Escherichia coli and constrains its metabolic activity. Proc Natl Acad Sci U S A. 2007;104:2663–8.
20. van Hoek MJ, Merks RMH. Redox balance is key to explaining full vs. partial switching to low-yield metabolism. BMC Syst Biol. 2012;6:22.
21. Vemuri GN, Altman E, Sangurdekar DP, Khodursky AB, Eiteman MA. Overflow metabolism in Escherichia coli during steady-state growth: Transcriptional regulation and effect of the redox ratio. Appl Environ Microbiol. 2006;72:3653–61.
22. Schuster S, de Figueiredo LF, Schroeter A, Kaleta C. Combining metabolic pathway analysis with evolutionary game theory. Explaining the occurrence of low-yield pathways by an analytic optimization approach. Biosystems. 2011;105:147–53.

23. Rosenzweig RF, Sharp RR, Treves DS, Adams J. Microbial evolution in a simple unstructured environment: Genetic differentiation in Escherichia coli. Genetics. 1994;137:903–17.

24. Turner PE, Souza V, Lenski RE. Tests of ecological mechanisms promoting the stable coexistence of two bacterial genotypes. Ecology. 1996;77:2119–29.

25. Treves DS, Manning S, Adams J. Repeated evolution of an acetate-crossfeeding polymorphism in long-term populations of Escherichia coli. Mol Biol Evol. 1998;15:889–97.

26. Rozen DE, Lenski RE. Long-term experimental evolution in Escherichia coli. VIII. Dynamics of a balanced polymorphism. Am Nat. 2000;155:24–35.

27. Friesen ML, Sauer G, Travisoni M, Doebeli M. Experimental evidence for sympatric ecological diversification due to frequency-dependent competition in Escherichia coli. Evolution. 2004;58:245–60.

28. Varma A, Palsson BO. Stoichiometric flux balance models quantitatively predict growth and metabolic by-product secretion in wild-type Escherichia coli W3110. Appl Environ Microbiol. 1994;60:3724–31.

29. Ort J, Thiele I, Palsson B. What is flux balance analysis? Nat Biotechnol. 2010;28:245–8.

30. Kauffman KJ, Prakash P, Edwards JS. Advances in flux balance analysis. Curr Opin Biotechnol. 2003;14:491–6.

31. Feist AM, Henry CS, Reed JL, Krummenacker M, Joyce AR, Karp PD, et al. A coherent steady state description of the metabolic capabilities of Escherichia coli K-12 MG1655 that accounts for 1260 ORFs and thermodynamic information. Mol Syst Biol. 2007;3:121.

32. Ibarra RU, Edwards JS, Palsson BO. Escherichia coli K-12 undergoes adaptive evolution to achieve in silico predicted optimal growth. Nature. 2002;420:20–3.

33. Heinrich R, Schuster S, Holzhüter H-G. Mathematical analysis of enzymatic reaction systems using optimization principles. Eur J Biochem. 1991;201:1–21.

34. Holzhüter HG. The principle of flux minimization and its application to estimate stationary fluxes in metabolic networks. Eur J Biochem. 2004;271:2005–22.

35. Hoppe A, Hoffmann S, Holzhüter H-G. Including metabolite concentrations into flux balance analysis: thermodynamic realizability as a constraint on flux distributions in metabolic networks. BMC Syst Biol. 2007;1:23.

36. Thiele I, Jarnsäili N, Fleming RMT, Palsson BO. Genome-scale reconstruction of Escherichia coli's transcriptional and translational machinery: A knowledge base, its mathematical formulation, and its functional characterization. PLoS Comput Biol. 2009;5:e1000312.

37. O'Brien EJ, Lerman JA, Chang RL, Hyduke DR, Palsson BO. Genome-scale models of metabolism and gene expression extend and refine growth phenotype prediction. Mol Syst Biol. 2013;9:693.

38. Kirkwood N, Segre D. Ecosystems biology of microbial metabolism. Curr Opin Biotechnol. 2011;22:541–6.

39. Zomorrodi AR, Maranas CD. OptCom: a multi-level optimization framework for the metabolic modeling and analysis of microbial communities. PLoS Comput Biol. 2012;8:e1002363.

40. Harcombe WR, Riehl WJ, Dukowski I, Granger BR, Betts A, Lang AH, et al. Metabolic resource allocation in individual microbes determines ecosystem interactions and spatial dynamics. Cell Rep. 2014;7:1104–15.

41. Kiltzold N, Segre D. Environments that induce synthetic microbial ecosystems. PLoS Comput Biol. 2010;6:e1000102.

42. Freilich S, Zarecki R, Ellam O, Segel ES, Henry CS, Kupiec M, et al. Competitive and cooperative metabolic interactions in bacterial communities. Nat Commun. 2011;2:589.

43. Stolyar S, Van Dien S, Hillestrand K, Finel N, Lie TJ, Leigh JA, et al. Metabolic modeling of a mutualistic microbial community. Mol Syst Biol. 2007;3:92.

44. Khandelwal RA, Olivier BG, Röbeck N, Blount ZD, Maddamsetti R, Burmeister AR, et al. Sustained fitness gains and variability in fitness trajectories in the long-term evolution experiment with Escherichia coli. Proc R Soc B. 2015;282:20152292.

45. Plucin J, Hindrét T, Le Gac M, Tenaillon O, Cruveiller S, Médigue C, et al. Epistasis and allele specificity in the emergence of a stable polymorphism in Escherichia coli. Science. 2014;343:1366–9.

46. Großkopf T, Soyer OS. Synthetic microbial communities. Curr Opin Microbiol. 2014;18:72–7.

47. Lenski RE, Rose MR, Simpson SC, Tadler SC. Long-term experimental evolution in Escherichia coli. I. Adaptation and divergence during 2,000 generations. Am Nat. 1991;138:1315–41.

48. Leiby N, Marx CJ. Metabolic erosion primarily through mutation accumulation, and not tradeoffs, drives limited evolution of substrate specificity in Escherichia coli. PLoS Biol. 2014;12:e1001789.

49. Harcombe WR, Delaney NF, Leiby N, Kiltzold N, Marx CJ. The ability of flux balance analysis to predict evolution of central metabolism scales with the initial distance to the optimum. PLoS Comput Biol. 2013;9:e1003091.

50. J. Stelling. Editor.

51. Lewis NE, Hixson KK, Conrad TM, Lerman JA, Chaussant P, Polpitiya AD, et al. Omic data from evolved E. coli are consistent with computed optimal growth from genome-scale models. Mol Syst Biol. 2010;6:390.

52. Rosselló-S, van der Weijden CC, Lindenbergh A, van Tuyl A, Francke C, Bakker BM, et al. Unraveling the complexity of flux regulation: a new method demonstrated for nutrient starvation in Saccharomyces cerevisiae. Proc Natl Acad Sci U S A. 2006;103:1266–71.

53. Elena SF, Lenski RE. Long-term experimental evolution in Escherichia coli: VII. Mechanisms maintaining genetic variability within populations. Evolution. 1997;51:1059–67.

54. Blount ZD, Bolortz C, Lenski RE. Historical contingency and the evolution of a key innovation in an experimental population of Escherichia coli. Proc Natl Acad Sci U S A. 2008;105:7899–906.

55. Maddamsetti R, Lenski RE, Barrick JE. Adaptation, clonal interference, and frequency dependent interactions in a long term evolution experiment with Escherichia coli. Genetics. 2015;200:1391–1398.

56. Tenaillon O, Barrick JE, Ribeck N, Deatherage DE, Blanchard JL, Darugupta A, et al. Tempo and mode of genome evolution in a 50,000 - generation experiment. Nature. 2016; in press.

57. Lenski RE, Souza V, Duong LP, Phan QC, Nguyen TNM, Bertrand KP. Epistatic effects of promoter and repressor functions of the Tn10 tetracycline-resistance operon on the fitness of Escherichia coli. Mol Ecol. 1994;3:127–35.

58. Le Gac M, Brazas MD, Bertrand M, Tyerman JS, Spencer CC, Hancock REW, et al. Metabolic changes associated with adaptive diversification in Escherichia coli. Genetics. 2008;178:1049–60.

59. Shlomi T, Eisenberg Y, Sharan R, Ruppin E. A genome-scale computational study of the interplay between transcriptional regulation and metabolism. Mol Syst Biol. 2007;3:101.

60. Covent MW, Palsson B. Transcriptional regulation in constraints-based metabolic models of Escherichia coli. J Biol Chem. 2002;277:28058–64.

61. Spencer CC, Bertrand M, Travisoni M, Doebeli M. Adaptive diversification in genes that regulate resource use in Escherichia coli. PLoS Genet. 2007;3:9083–8.

62. Feist A, Palsson B. The biomass objective function. Curr Opin Microbiol. 2010;13:344–9.

63. Edwards JS, Ibarra RU, Palsson BO. In silico predictions of Escherichia coli metabolic capabilities are consistent with experimental data. Nat Biotechnol. 2001;19:125–30.

64. Ort JD, Fleming RM, Palsson BO (2010a) 10.2.1 – Reconstruction and use of microbial metabolic networks: the core Escherichia coli metabolic model as an educational guide. In EcoSal – Escherichia coli and Salmonella Cellular and Molecular Biology, Karp PD (ed). 2010.2.1. Washington DC: ASM Press.

65. Wielgosz S, Barrick JE, Tenaillon O, Cruveiller S, Chané-Woon-Ming B, Médigue C, et al. Mutation rate inferred from synchronous substitutions in a long-term evolution experiment with escherichia coli. G3. 2011;1:183–6.

66. Loferer-KrólBächler M, Klima J, Piérrer R. Determination of bacterial cell dry mass by transmission electron microscopy and densitometric image analysis. Appl Environ Microbiol. 1998;64:888–94.
71. Becker SA, Feist AM, Mo ML, Hannum G, Palsson BØ, Herrgard MJ. Quantitative prediction of cellular metabolism with constraint-based models: the COBRA Toolbox. Nat Protoc. 2007;2:727–38.
72. MATLAB scripts used to run evoFBA and analyze data. http://osslab.lifesci.warwick.ac.uk/?pid=resources.
73. Jeong H, Barbe V, Lee CH, Vallenet D, Yu DS, Choi SH, et al. Genome sequences of Escherichia coli B strains REL606 and BL21(DE3). J Mol Biol. 2009;394:644–52.
74. Zaslaver A, Bren A, Ronen M, Itzkovitz S, Kikoin I, Shavit S, et al. A comprehensive library of fluorescent transcriptional reporters for Escherichia coli. Nat Methods. 2006;3:623–8.