TOWARD UNDERSTANDING THE B[e] PHENOMENON. IV. MODELING OF IRAS 00470+6429

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ABSTRACT

FS CMa type stars are a recently described group of objects with the B[e] phenomenon which exhibits strong emission-line spectra and strong IR excesses. In this paper, we report the first attempt for a detailed modeling of IRAS 00470+6429, for which we have the best set of observations. Our modeling is based on two key assumptions: the star has a main-sequence luminosity for its spectral type (B2) and the circumstellar (CS) envelope is bimodal, composed of a slowly outflowing disklike wind and a fast polar wind. Both outflows are assumed to be purely radial. We adopt a novel approach to describe the dust formation site in the wind that employs timescale arguments for grain condensation and a self-consistent solution for the dust destruction surface. With the above assumptions we were able to satisfactorily reproduce many observational properties of IRAS 00470+6429, including the H I line profiles and the overall shape of the spectral energy distribution. Our adopted recipe for dust formation proved successful in reproducing the correct amount of dust formed in the CS envelope. Possible shortcomings of our model, as well as suggestions for future improvements, are discussed.

Keywords: circumstellar matter – stars: early-type – stars: emission-line, Be – stars: individual (IRAS 00470+6429)

Online-only material: color figures

1. INTRODUCTION

This series of papers is devoted to studying objects from the Galactic FS CMa type group. The group comprises about 40 objects with the B[e] phenomenon, which refers to the simultaneous presence of forbidden lines in the spectra and strong excesses of IR radiation (Miroshnichenko 2007; Lamers et al. 1998). Its members show properties of B-type stars with typical main-sequence luminosities \( \log(L/L_\odot) \sim 2.5-4.5 \). On the other hand, they exhibit extremely strong emission-line spectra that are on average more than an order of magnitude stronger than those of Be stars of similar spectral types. The group includes objects that were discovered long ago but their nature and evolutionary state were not satisfactorily determined, as well as newly found ones (Miroshnichenko et al. 2007).

One of the main problems in understanding those objects has to do with the presence of significant amounts of hot dust in their circumstellar (CS) region that cannot be left over from the time of the stars’ formation. It is also hard to explain the dust formation using typical mass-loss rates from single stars of an appropriate mass range (\( \sim 5-20 M_\odot \)). Our observations show that over 30% of the group objects show signs of secondary companions in the spectra (e.g., Li I 6708 Å absorption line). Therefore, one might assume that the large amounts of CS matter near FS CMa type objects may be a consequence of the binary evolution, although direct evidence of the mass transfer between the stellar companions is not observed.

The main goals of this series of papers are to obtain high quality observational data for the group objects, to describe the objects’ properties in detail, and to model the latter in order to put tight constraints on parameters of the stellar companions and those of the CS material. The observed properties of the first object for which we collected a good wealth of data, IRAS 00470+6429, were presented by Miroshnichenko et al. (2009, hereafter Paper III). In the present paper, we make use of the Monte Carlo code HDUST to determine the physical parameters of this intricate system.

2. MODEL DESCRIPTION

From the discussion of the available data in Paper III, it becomes clear that IRAS 00470+6429 is a very complex object, with a large and dense CS envelope composed of both ionized gas and dust. It is expected, therefore, that any model that successfully reproduces the observed properties must also be complex.

This first attempt at the modeling of IRAS 00470+6429 was conducted using the computer code HDUST (Carciofi & Bjorkman 2008, 2006; Carciofi et al. 2008, 2006, 2004). HDUST is a three-dimensional Monte Carlo radiative transfer code that combines the full non-local thermodynamic equilibrium (NLTE) treatment of the radiative transfer in gaseous media with a very general treatment for CS dust grains. This code has been already successfully applied to study the CS disks of Be stars (see, for instance, Carciofi et al. 2007; Carciofi et al. 2009).

In HDUST, the CS environment can be represented by two components: a gaseous region, containing hydrogen and free electrons, and a dusty region. The solution to the problem is obtained in two steps. The first step consists of an iterative scheme to solve the coupled problems of radiative transfer, radiative equilibrium, and statistical equilibrium. For the gaseous shell, HDUST calculates the NLTE hydrogen level populations and the electron temperature as a function of position, taking into full account all the relevant physics (continuum and line transfer, collisional processes, etc.). For the dusty shells, HDUST solves the radiative equilibrium problem, thereby obtaining the equilibrium temperature of the dust grains as a function of position. The interested reader is referred to Carciofi & Bjorkman (2006) for details of the Monte Carlo NLTE solution and Carciofi et al. (2004) for information about the dust implementation. Once the first step is completed and the state variables of the CS
material are known, HDUST is run in a post-processing mode to calculate the emergent flux (spectral energy distribution, SED, line profiles, synthetic images, etc.) for arbitrary lines of sight (LOSs).

A few words about an important feature of the code are warranted. For a given gas plus dust distribution, as, for instance, the one adopted in Section 2.1, HDUST solves for the gas and dust properties simultaneously and self-consistently. Thus, important effects, such as the shielding of the dust grains from the stellar ionizing UV photons by the CS gas, are included in the calculations. This feature allowed us to determine for each model the dust destruction surface, which is the latitude-dependent distance from the star beyond which the dust equilibrium temperature is below an adopted destruction temperature. This feature of the code proved to be a key factor for the model we describe below.

2.1. A Parametric Model for the Circumstellar Envelope

For the problem at hand, HDUST must be provided with a description of the properties of the central star (effective temperature, $T_{\text{eff}}$, and radius, $R$) and the physical properties of the CS envelope (density and velocity distribution of the gas and the characteristics of the CS dust, such as composition and grain size distribution). In addition, two geometrical parameters must be specified: the distance to the star, $d$, and the inclination angle, $i$, which is the angle between the observer’s LOS and the symmetry axis of the system. Finally, the interstellar reddening, $E(B-V)_{\text{IS}}$, must also be specified. Even though it is not an intrinsic parameter of the system, we include it as a model parameter because of the uncertainty in its determination, mainly owing to the difficulty to separate the interstellar from the CS reddening.

A long standing issue regarding the stars with the B[e] phenomenon is that very little is known about the processes that lead to the formation of their CS environment (see Zickgraf 2006 for a review). Also, in spite of the effort of numerous observers and theoreticians, the most fundamental properties of the CS envelope remain quite uncertain. In the case of supergiants B[e] (sgB[e]), a subclass of the stars with the B[e] phenomenon (Lamers et al. 1998), it is generally believed that their CS envelope is bimodal, composed of a slowly outflowing, possibly rotating disk and a fast polar wind (Zickgraf et al. 1985). Two scenarios invoked to explain this bimodality are the rotationally induced bi-stability (Lamers & Pauldrach 1991) and rotationally supported Keplerian outflows (Porter 2003).

CS envelopes of FS CMa objects are even less understood, since very little theoretical work has been done with these objects so far. For this initial theoretical effort, we adopt a model for IRAS 00470+6429 that has two key assumptions. First, we assume that the star has a luminosity similar to that of a main-sequence star with the same spectral type, i.e., the stellar luminosity is in the range of a few thousand solar luminosities. We believe this assumption is well supported by the available data (Paper III). Second, we assume that some sort of bimodal, two-component wind is present, similar in structure to the CS envelopes of sgB[e]. The results shown in Section 3 largely corroborate the above assumptions, but possible shortcomings are discussed in Section 4.

We adopt the following parametric form for the CS density and velocity structure. We assume that the underlying physical reason for the bimodal envelope is that the mass loss is, somehow, enhanced around the equator. We express the stellar mass-loss rate per unit solid angle as

$$\frac{d\dot{M}(\theta)}{d\Omega} = \frac{d\dot{M}(0)}{d\Omega} \left[1 + A_1 \sin^m(\theta)\right],$$

where $\theta$ is the colatitude measured from the pole. $A_1$ is a parameter that controls the ratio between the equatorial and polar mass-loss rates

$$A_1 = \frac{d\dot{M}(90^\circ)/d\Omega}{d\dot{M}(0)/d\Omega} - 1.$$  \hspace{1cm} (2)

Since the mass-loss rate is enhanced at the equator, $A_1 > 0$. The parameter $m$ controls how fast the mass-loss rate drops from the equator to the pole. Defining the disk opening angle, $\Delta \theta_{\text{op}}$, as the latitude for which $d\dot{M}(\theta)/d\Omega$ has dropped to half of its equatorial value, we have

$$\Delta \theta_{\text{op}} = \sin^{-1} \left[ \left( \frac{A_1 - 1}{2A_1} \right)^{1/m} \right].$$ \hspace{1cm} (3)

For the velocity structure, we assume that the gas motion is purely radial, with a latitude-dependent radial velocity given by

$$v_r(r, \theta) = v_0 + [v_\infty(\theta) - v_0](1 - \frac{R}{r})^{\beta(\theta)},$$ \hspace{1cm} (4)

where $r$ is the distance to the center of the star. For a given $\theta$, Equation (4) is a standard $\beta$-law for radiatively driven winds (Lamers & Cassinelli 1999). We assume that both the wind terminal velocity, $v_\infty$, and the acceleration parameter, $\beta$, are functions of $\theta$, and have the same latitudinal dependence as the mass loss. Thus,

$$v_\infty(\theta) = v_\infty(0)[1 + A_2 \sin^m(\theta)],$$ \hspace{1cm} (5)

and

$$\beta(\theta) = \beta(0)[1 + A_3 \sin^m(\theta)].$$ \hspace{1cm} (6)

As before, $A_2$ and $A_3$ control the ratio between the values of each quantity at the equator and at the pole,

$$A_2 = \frac{v_\infty(90^\circ)}{v_\infty(0)} - 1,$$ \hspace{1cm} (7)

and

$$A_3 = \frac{\beta(90^\circ)}{\beta(0)} - 1.$$ \hspace{1cm} (8)

Since the terminal velocity at the equator is smaller than at the pole, $A_2 < 0$.

Assuming radial outflow, the mass continuity equation is,

$$\frac{d\dot{M}(\theta)}{d\Omega} = r^2 \rho(r, \theta) v(r, \theta),$$ \hspace{1cm} (9)

so we can write the CS gas mass density distribution as

$$\rho(r, \theta) = \frac{d\dot{M}(\theta)/d\Omega}{r^2 v(r, \theta)}.$$ \hspace{1cm} (10)
2.2. Dust Condensation Site

Having chosen a prescription for the CS gas, we must now provide a site for dust formation and describe the properties of the dust grains that are formed. In an initial study of the continuum emission of sgB[e], Porter (2003) used two criteria to determine the dust formation site. In his models, dust was formed where the gas temperature, which he assumed to be an ad hoc function of the distance from the star, was lower than a given value (≈1500 K) and the gas density was larger than a critical value.

In our models, the coolest part of the envelope is in the denser equatorial regions, an expected result based on previous works (e.g., Zsargó et al. 2008; Carciofi & Bjorkman 2006; see Figure 5 below). However, even in the midplane the gas temperatures never fall below about 4000 K. This temperature is much larger than the temperature needed for dust grain condensation to occur, which is thought to be below about 1500 K (Porter 2003). It is likely that the gas temperatures predicted by hdust are overestimated, because no cooling by helium or other metals is included. However, Zsargó et al. (2008), in a study of the properties of the CS envelope of sgB[e], found that the temperature never falls below 2000–3000 K, even though they used more realistic cooling terms. These authors argue that a possible mechanism for further cooling the gas is adiabatic cooling, or an even more complex chemical composition.

Because of the above, it is clear that the gas temperature cannot be used in our models to trace the dust formation site and we use, for this purpose, a different approach than the one used by Porter (2003). We define the dust formation site using two complementary criteria.

If dust is to be present at a given location of the CS envelope,

1. the equilibrium temperature of the dust grains (not the gas temperature) must be smaller than a given grain destruction temperature, \( T_{\text{dust}} \);
2. furthermore, the gas density must be larger than a critical value, such that grain growth can occur.

The first criterion was implemented in hdust using a very simple procedure. For a given model, we start from a guess of the distance from the star beyond which the dust grains begin to condense. During the iterative process used for determining the temperatures, whenever the dust temperature in a given condensate is a normalization constant. In the standard MRN law, \( n = -3.5 \) and the distribution is confined between \( d_{\text{min}} = 0.05 \mu\text{m} \) and \( d_{\text{max}} = 0.25 \mu\text{m} \). In our models, we let both \( d_{\text{min}} \) and \( d_{\text{max}} \) to be free parameters in order to investigate the possible existence of large dust grains (Paper III). Given a dust mass density and \( f(a) \), we further need the average density of the grain material, \( \rho_{\text{dust}} \), in order to calculate the number density of dust grains. Since we do not know how fluffy the grains are, we let \( \rho_{\text{dust}} \) be a free parameter. We note, however, that \( \rho_{\text{dust}} \) and the gas-to-dust ratio are not independent parameters, since both are contained in the dust optical depth, the one quantity that effectively controls the radiative transfer in the CS dust shell.

2.3. Adopted Grid Structure

A few words are needed about the grid structure we adopted for the current problem. In hdust, the CS envelope is divided into \( N_r \) radial cells, \( N_\mu \) colatitude cells and \( N_\theta \) azimuth cells, and it is assumed that the state variables of the CS material (temperature and level populations) are constant in each cell.
The density law of Equation (4) can present difficulties for a radiative transfer solver, because it has a large radial gradient close to the star and it may have a sharp enhancement at the equator, depending on the adopted value of $m$. For the radial spacing we adopt cell sizes such that the radial electron scattering optical depth is the same for all cells, which results in very small cells close to the star and large cells in the outer envelope. This ensures that the inner regions of the envelope are sampled adequately. For the colatitude bins, we define the cell sizes is such a way that from the equator to the pole, along a ray with constant radius, the density at the center of consecutive cells falls in steps of $2/N_{\mu}$. Therefore, when $m$ is large, which corresponds to a disk with small opening angle, the cells are small at the equator and large at the pole.

Two competing issues must be taken into account when choosing the values of $N_{r}$ and $N_{\mu}$. Since H\textsc{dust} employs a statistical method for sampling cell-dependent quantities such as radiative heating (see Carciofi & Bjorkman 2006), the larger the number of cells the larger the computational effort necessary to reach a given sampling error in the rates. On the other hand, the grid structure must be fine enough to correctly describe the adopted density and to resolve possible regions of ionization changes, where a transition from ionized to neutral hydrogen occurs. The minimum number of cells necessary for a given problem can be estimated by running models with an increasing number of cells. If the cell spacing is properly defined, there will be a certain number of cells beyond which no modification of the solution is found by further refining the grid. We found that $N_{r} = 100$ (60 for the gas shell and 40 for the dusty shell) and $N_{\mu} = 40$ are a good compromise between speed and accuracy. For the current problem the number of azimuth cells was set to 1 because axisymmetry was assumed.

### 2.4. Modeling Procedure

The adopted model described above has many parameters but for this initial study we chose to let just part of them be free parameters, while keeping the rest fixed. We chose as fixed parameters the ones which can either be sufficiently well constrained by a model-independent analysis, or are associated with the basic model assumptions defined in Section 2.1. Examples of fixed parameters are the stellar characteristics and the dust composition.

Free parameters, on the other hand, are the ones about which no information can be readily obtained from the observations and, therefore, require a detailed modeling. The main free parameters in our study describe the density and velocity of the CS gas and the latitude-dependent stellar mass-loss rate. We believe that this approach is appropriate for this initial study, since it allows us to focus on the least known properties of the CS envelope. A list of model parameters for IRAS 00470+6429 is given in Table 1.

### 2.5. Stellar Parameters

The stellar parameters are all fixed in this study. As mentioned above, one of our key assumptions is that IRAS 00470+6429 has a typical luminosity of a normal main-sequence B star. Following the analysis in Paper III, we chose a spectral type of B2V for the central star. This sets the radius to $6\,R_\odot$, the effective temperature to $20,000$ K and the luminosity to $5100\,L_\odot$ (Harmanec 1988). We investigated the effects of changing $T_{\text{eff}}$ and $L$, and we found that varying $T_{\text{eff}}$ by $\approx 10\%$ (and thus $L$ by $\approx 40\%$) has only small effects on the results.

### Table 1

| Parameter                     | Value       | Type  |
|-------------------------------|-------------|-------|
| **Stellar Parameters**        |             |       |
| Spectral type                 | B2V         | Fixed |
| $R$                           | $6\,R_\odot$| Fixed |
| $T_{\text{eff}}$              | 20,000 K    | Fixed |
| $L$                           | $5100\,L_\odot$ | Fixed |
| **Geometrical Parameters**    |             |       |
| $i$                           | $84^\circ$  | Free  |
| $d$                           | $1100 \pm 100$ pc | Free  |
| **Wind Parameters**           |             |       |
| $dM(90^\circ)/d\Omega$       | Calculated  |       |
| $(1.4–1.6) \times 10^{-8} \, M_\odot$ yr$^{-1}$ sr$^{-1}$ |
| $dM(0)/d\Omega$              | Free        |       |
| $< 3 \times 10^{-9} \, M_\odot$ yr$^{-1}$ sr$^{-1}$ |
| $A_1$                         | Free        |       |
| $> 19$                        | Free        |       |
| $v_{\text{rot}}(90^\circ)$   | Calculated  |       |
| $24 \text{ km s}^{-1}$       |
| $v_{\text{rot}}(0)$          | Fixed       |       |
| $1200 \text{ km s}^{-1}$     |
| $A_2$                         | Free        |       |
| $-0.98$                      | Free        |       |
| $\beta(0)$                   | Free        |       |
| $4$                          | Free        |       |
| $\alpha$                     | Free        |       |
| $0$                          | Free        |       |
| $m$                          | Free        |       |
| $92$                         | Free        |       |
| $R_{\text{c}}$               | $\geq 10^4\,R_\odot$ | Fixed |
| **Common Dust Parameters**    |             |       |
| Composition                   | Amorphous silicate a | Fixed |
| $n$                           | $-3.5$      | Fixed |
| Gas-to-dust ratio             | 200         | Fixed |
| **Dust Model 1**              |             |       |
| $\varrho_{\text{min}}$       | $0.05–0.25 \mu$m | Fixed |
| $\varrho_{\text{max}}$       | $1.5 \text{ g cm}^{-3}$ | Fixed |
| $T_{\text{destruction}}$     | 1500 K      | Free  |
| $R_{\text{destruction}}$     | 540 $R_\odot$ | Calculated |
| $\eta$                       | 0.02        | Free  |
| $E(B-V)_{\text{BS}}$         | 1.1         | Free  |
| **Dust Model 2**              |             |       |
| $\varrho_{\text{min}}$       | $0.05–0.10 \mu$m | Fixed |
| $\varrho_{\text{max}}$       | $0.15 \text{ g cm}^{-3}$ | Fixed |
| $T_{\text{destruction}}$     | 1500 K      | Free  |
| $R_{\text{destruction}}$     | 540 $R_\odot$ | Calculated |
| $\eta$                       | 0.02        | Free  |
| $E(B-V)_{\text{BS}}$         | 1.1         | Free  |
| **Dust Model 3**              |             |       |
| $\varrho_{\text{min}}$       | $1–50 \mu$m | Fixed |
| $\varrho_{\text{max}}$       | $0.1 \text{ g cm}^{-3}$ | Fixed |
| $T_{\text{destruction}}$     | 1600 K      | Free  |
| $R_{\text{destruction}}$     | 79 $R_\odot$ | Calculated |
| $\eta$                       | 0.02        | Free  |
| $E(B-V)_{\text{BS}}$         | 1.2         | Free  |

**Note.** aThe optical constants of Ossenkopt et al. (1992) were used.

For this initial study we considered a static, non-rotating central star. This is not a limitation of H\textsc{dust} (see, e.g., Carciofi et al. 2008) but, instead, reflects the fact that the observed line profile is controlled mostly by the CS gas (Section 3.1).

For the stellar spectrum, we used the model atmosphere of Kurucz (1994) for $T_{\text{eff}} = 20,000$ K and log $g = 4.4$. To describe the photospheric specific intensity as a function of direction we adopted the limb darkening models of Claret (2000).

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4 The use of an LTE model atmosphere is not a limitation of the present work. More recent NLTE results could have been used, but the object is so deeply embedded in the CS outflow that differences in the emerging flux would be negligible (see Section 3.1).
2.6. Geometrical Parameters

The geometrical parameters (i, d, and interstellar reddening) are all free parameters. Nothing is known about i, but our previous analysis allows us to impose some limits on d and \(E(B-V)_{\odot}\). Following Paper III, we adopt d in the range of 1000–2000 pc and \(E(B-V)_{\odot}\) in the range 0.8–1.2 mag. Given a model for the CS gas and dust, d and \(E(B-V)_{\odot}\) are obtained by fitting the observed flux level and shape of the visible SED, respectively.

3. RESULTS

3.1. Circumstellar Gas

Some information about the gas dynamics can be readily obtained by analyzing the emission line profiles. For instance, the broad blue absorption profile of the H\(\alpha\) lines suggests that the absorbing material has large velocities in the LOS and the blue edge of the absorption profile indicates the terminal velocity of the fast wind. For \(v_{\infty}(0)\), we adopted a value of 1200 km s\(^{-1}\) and set this as a fixed parameter in our modeling. We note that this value of the terminal velocity is consistent with what is expected for main-sequence B stars (Grady et al. 1987).

In addition, the relatively narrow peaks of the Balmer lines suggest that the bulk of the emitting material has small velocity along the LOS. Supposing that most of the H\(\alpha\) line emission comes from the equatorial region (an assumption corroborated by our detailed calculations), this suggests that the equatorial outflow velocities are very small compared to the velocities in the polar region.

For the present work, hundreds of models were run covering a wide range of model parameters. Before presenting our solution, it is useful to discuss some trends that became clear once a large range in the parameter space was covered.

From our results we can safely rule out both large (\(\Delta \theta_{\text{op}} \gtrsim 15^\circ\) or \(m \lesssim 15\)) and small (\(\Delta \theta_{\text{op}} \lesssim 5^\circ\) or \(m \gtrsim 180\)) opening angles for the outflowing disk around IRAS 00470+6429. The opening angle, together with the equatorial mass-loss rate, controls the strength of the H\(\alpha\) line emission. For large opening angles, relatively low mass-loss rates are necessary to reproduce the observed emission strength, i.e., the larger the opening angle, the lower the equatorial densities for a given emission strength. Also, the lower the density, the farther away from the star is the dust destruction surface and, therefore, the lower the density in the dust condensation zone. The two effects combined have the consequence that models with \(\Delta \theta_{\text{op}} \gtrsim 15^\circ\) have densities below the critical density necessary to form dust (Equation (12)).

Models with small opening angles require high equatorial densities to reproduce the line emission and, therefore, can form dust. However, as we shall see in Section 3.2, in our models dust is typically confined within a wedge about one opening angle away from the equator. This is because the density drops quickly toward the pole and soon falls below the critical density for grain formation. If the opening angle is too small (\(\Delta \theta_{\text{op}} \lesssim 5^\circ\)), the dust will encompass too small a solid angle for the radiation that comes from the inner envelope (both stellar radiation and reprocessed radiation by the CS gas) and, as a consequence, will reprocess little radiation. This is a geometrical effect and is true even for very large dust opacities. Therefore, small opening angles can be ruled out on the grounds that they produce too small IR excess.

Another trend that became evident is that \(d \dot{M}(0)/d\Omega\) cannot be larger than about \(3 \times 10^{-9} M_{\odot}\) yr\(^{-1}\) sr\(^{-1}\). A large density in the poles implies that the polar regions would contribute significantly to the overall line emission. Since the polar material has a large terminal speed, the polar emission would appear as a broad red emission wing, which is not observed. The polar emission begins to alter the emission profile significantly if mass-loss rate exceeds the quoted value.

This upper limit for \(d \dot{M}(0)/d\Omega\) has an important implication on the possible range of inclination angles. Since the polar regions must be relatively optically thin, they cannot account for the broad and deep absorption component observed in the Balmer lines (see, for instance, Figure 3 of Paper III). Models with \(0^\circ < i \lesssim 75^\circ\) do not produce the necessary absorption and, therefore, this range of inclination angles can be excluded. Besides this interval, our models can also exclude inclination angles too close to edge-on (\(i \approx 90^\circ\)). In all our models, the radial optical depth along the equator is very large (\(\tau \approx 10^6\) in the Lyman continuum and \(\approx 10^5\) in the Balmer continuum). As discussed in Paper III, some features of the stellar photosphere are observed, which, therefore, excludes edge-on viewing.

Our best-fit SED, H\(\alpha\), H\(\beta\), H\(\gamma\), and H\(\delta\) line profiles for the parameters listed in Table 1 are compared to the observations in Figures 1–3. The CS gas density and velocity profiles along several latitudes are shown in Figure 4.

As said above, the opening angle and the equatorial mass-loss rate are the primary parameters that control the strength of the line emission for a given i. Our best-fit value for the opening angle is 7\(^\circ\), which corresponds to \(m = 92\). For the equatorial mass-loss rate our best-fit value is in the range \(d \dot{M}(90^\circ)/d\Omega = (1.4–1.6) \times 10^{-8} M_{\odot}\) yr\(^{-1}\) sr\(^{-1}\). The lower limit corresponds to the best-fit value for the line emission observed on 2006 December 13, whereas the upper limit corresponds to the 2006 December 27 observations, which have substantially stronger emission (see Figure 2). This result indicates that IRAS 00470+6429 presents significant changes in the mass-loss rate in very short timescales (two weeks).

Both \(m\) and \(d \dot{M}(90^\circ)/d\Omega\) are well-constrained parameters in our models, but we note that reasonable fits of the emission strength could also be obtained with slightly larger opening angles (say, by 1\(^\circ\) or 2\(^\circ\)) and slightly smaller (a few tens of per cent) \(d \dot{M}(90^\circ)/d\Omega\). The opposite is also true, i.e., similar fits can be obtained by slightly smaller opening angles and slightly larger mass-loss rates.

The opening angle and the mass-loss rate also control the SED shape. Their effects on the SED are complex and depends significantly on the adopted i. Dust also plays a major role in defining the shape of the SED, not only in the IR but also on the visible spectral region provided that the LOS of the observer crosses dusty material. For this reason, we postpone the discussion of the model SED and its comparison to observations to Section 3.2.

Contrary to the equatorial mass-loss rate, the polar mass-loss rate is rather poorly constrained. As explained above, an upper limit of about \(d \dot{M}(0)/d\Omega = 3 \times 10^{-9} M_{\odot}\) yr\(^{-1}\) sr\(^{-1}\) could be set on the basis of the absence of a broad emission component. Given the best-fit value of \(d \dot{M}(90^\circ)/d\Omega\), above, this corresponds to a lower limit of \(A_1 = 19\), which means that the ratio between the equatorial and polar mass-loss rates is at least as high as 20, but our models do not exclude much larger values of \(A_1\). The reason why our models do not constrain well the polar densities is that the H\(\alpha\) recombination lines are not suitable probes of low density regions. UV resonance lines of high ionization species are the ideal probes of those regions, but unfortunately no UV data are available for this object.
contrary to its shape, is remarkably constant. It depends on two competing processes: the absorption of resonant radiation by H\textsc{i} atoms in a given excitation state and the emission filling-in, i.e., the generation of new photons both by line emission and bound–free and free–free continuous emission that partially fills in the absorption component. The filling-in by continuous emission is particularly important because of the very large densities close to the star (see Figure 4). As shown in Figure 3, our models also fit reasonably well the depth of the absorption component for other lines of the Balmer series, which is not a trivial result.

Another important parameter is the value of $\beta$ that tells how fast the wind accelerates. We found that the best models for the line profiles are the ones with large values of $\beta$ for all latitudes. Low values of $\beta$ (say, $\beta \lesssim 2$) would result in a too broad emission component, due to the large velocities in the inner part of the wind, and also a sharp absorption edge at high velocities. Both these features are not observed. Even though in our models it was possible to have different values of $\beta$ for different latitudes, our best-fit value was for $\beta = 4$ and $A_1 = 0$, i.e., a constant value of $\beta$. Again, this is a somewhat uncertain result. For instance, a model with $A_1 = 1/3$, for which $\beta(0) = 3$, is also a good model and cannot be ruled out from the present analysis.

We end this section discussing the temperature and ionization structure of the CS gas. Figure 5 shows the midplane temperature and the fractional number of H atoms in the ground level as a function of the distance from the star. Clearly, the gas is highly non-isothermal, a result already obtained by Drew (1985) and, more recently, by of Carciofi & Bjorkman (2006) and Zsargó et al. (2008). The temperature reaches a minimum of about 5000 K at a distance of around 5 $R$ and then steadily rises to an equilibrium temperature of about 12,000 K for $r \gtrsim 100$ $R$. This rise in the temperature is probably a result of our unrealistic chemical composition. The inclusion of the cooling terms by other elements will result in a different temperature profile (see, for instance, Drew 1985).

The gas is essentially ionized everywhere in the envelope. The maximum value for the relative fraction of H\textsc{i} and H\textsc{ii} is never larger than 10%. This result agrees with the recent work by Zsargó et al. (2008), who studied the envelopes of sgB[e], and found that H is generally ionized, although this may depend on both the effective temperature of the central star and on the density scale of the wind.

### 3.2. Circumstellar Dust

Many processes are involved in defining the shape of the SED, and both gas and dust can play an important role depending on the wavelength range considered. In the visible region, the dominant processes are continuum absorption by both gas and dust, and emission by continuum processes in the gas (bound–free and free–free emission). The SED is controlled by both gas and dust emission at wavelengths of $\lesssim 2$ $\mu$m in the near-IR, but the dust becomes the major player at longer wavelengths.

For this initial study of the dusty content of IRAS 00470+6429, three different models for the CS dust were investigated. For all models the grain size distribution has the form of Equation (13) with $n = -3.5$, and each model explores different values for the minimum and maximum sizes of the distribution. The first model studied corresponds to the standard MRN model for interstellar dust grains (Mathis et al. 1977), for which $a_{\min} = 0.05$ and $a_{\max} = 0.25$ $\mu$m. The second model employs a much larger
upper limit for the distribution ($a_{\text{max}} = 10$ $\mu$m), whereas the third model has very large grains only ($a_{\text{min}} = 1$ and $a_{\text{max}} = 50$ $\mu$m). The three dust models are listed in Table 1.

At this point, it is useful to consider what controls the shape and level of the IR excess arising from dust thermal emission. The shape of the emitted spectrum is controlled mainly by the dust absorption coefficient in the IR domain, which is a function of chemical composition and size of the grain. Other factors controlling the shape are the temperature and density structure. The level of the IR excess depends on the fraction of the radiation coming from the central regions that is reprocessed by the dust grains. Since in our model the dust is confined to the dense equatorial outflow, the amount of reprocessing will be a function of the disk opening angle, $\Delta \theta_{\text{op}}$, and the dust optical
Bottom: ratio between the number density of H atoms in the ground level, \( n_H \), and the total number of H atoms \( n_{H_{\text{tot}}} \). Shown are the results for \( dM(90^\circ)/d\Omega = 6 \times 10^{-9} M_{\odot} \text{ yr}^{-1} \text{ sr}^{-1} \).

The role of \( \eta \) in defining the dust condensation site deserves a more careful examination. Recall that the dust condensation site is defined by two conditions: the density of the growing material (Si) must satisfy Equation (12), in which \( \eta \) is a scaling factor, and the dust equilibrium temperature must be smaller than a given value that corresponds to the temperature above which the dust grains are destroyed (Section 2.2). In Figure 6, we plot the equilibrium temperature of the smallest grains considered by us (\( \alpha = 0.05 \mu m \)). As we see below, the smallest grains are always hotter than the larger grains, and, therefore, are used as the tracers of the dust formation site. The plot represents a cut through the envelope such that the direction of the symmetry axis is vertical and the direction of the midplane is horizontal. The latitude-dependent inner dust radius represents our solution for the dust destruction surface. Near the midplane, where the densities are larger and the material is more shielded from the central radiation, the dust destruction surface is closer to the star, and this surface moves outward for higher latitudes.

The solid white lines in Figure 6 mark the points of the wind for which the right side of Equation (12) is equal to the left side, and it encloses the region around the equator which has densities larger than the critical density for grain formation (to draw this line we used \( \eta = 0.02 \), see below). According to our two assumptions, the site for dust formation is the region of the wind both beyond the destruction surface and inside the region enclosed by the solid white lines. The dust condensation site has an angular size of \( 2\Delta \theta_{\text{dust}} \), the value of which is controlled by the parameter \( \eta \); the larger \( \eta \) the smaller \( \Delta \theta_{\text{dust}} \).

It is important to note that the site for dust formation does not necessarily coincide with the site where dust actually is, because the dust formed in the innermost region of the condensation site will be carried outward along the wind streamlines. Therefore, dust that was formed at high latitudes will be dragged to regions where the density is much too low to form dust. This mechanism allows dust to exist at high latitudes in the outer envelope, where the density is lower than the critical value. Therefore, in our models dust is confined within a wedge with a (half) opening angle of \( \Delta \theta_{\text{dust}} \), \( \Delta \theta_{\text{dust}} \) is a function of both \( \Delta \theta_{\text{op}} \) and \( \eta \).

Figure 1 compares the best-fit SED obtained for each of the three dust models tested. We did not attempt to fit the IRAS fluxes, but focus instead on the Berkeley Automated Supernova Search (BASS) and MSX data, since the large aperture of IRAS has probably lead to some degree of contamination by the interstellar cirrus. Also, we recall, from the data description in Paper III, that the NIRIS data have large errors of up to 20% in the photometric calibration.

The MRN model (model 1, top panel of Figure 1) does not fit the data well. The integrated IR flux is in rough agreement with the observations, which means that the model does reprocess the correct fraction of the bolometric stellar luminosity. It reproduces the SED reasonably well in the 2–3 \( \mu m \) range, but fails to reproduce the slope of the SED for larger wavelengths. The model with a large upper limit for the grain size (model 2, middle panel of Figure 1) fits both the level and shape of the SED in the 2–7 \( \mu m \) range. The reason why model 2 fits better the shape of the near-IR SED than model 1 resides in an interesting physical effect: differently sized grains have different equilibrium temperatures (Carciofi et al. 2004). Figure 7 shows the temperature of the smallest and largest grains of dust models 1 and 2. For model 1, the span in grain sizes is not very large and the difference between the coolest and hottest grains is, at most, 300 K. For model 2, however, we find that the very large grains are much cooler than the small grains. This explains the difference in the slope of the SED: model 2, having on average a lower dust equilibrium temperature, has proportionally larger emission at longer wavelengths.

The 10 \( \mu m \) region of the spectrum presents a big challenge for models 1 and 2, since for both the 9.7 \( \mu m \) silicate emission feature is quite strong, in sharp contrast to the observations. This situation is much improved for the model with only large grains (model 3, bottom panel of Figure 1). This model reproduces reasonably well the shape of the thermal IR emission in the...
entire 2–13 \( \mu m \) range. As discussed above, the shape of the IR thermal continuum is controlled mainly by the dust absorption opacity, which is a function of grain size and composition. Under our assumption that the grains in IRAS 00470+6429 are oxygen-based, the observed IR excess seems to indicate that large grains (\( a \gtrsim 1 \mu m \)) are the dominant constituents of the CS dust.

The large difference between the equilibrium temperatures of small and large grains has another consequence for the models. Recall that one of the conditions for determining the dust condensation site is that the temperature of the hottest grains cannot exceed \( T_{\text{destruction}} \). For models 1 and 2 this condition is satisfied only for \( r \gtrsim 540 \, R \), but for model 3 the dust destruction surface is much closer to the star \( r \gtrsim 79 \, R \).

Another important difference between models with small and large grains lies in the bulk density of the grain material (\( \rho_{\text{dust}} \)). At a given location of the envelope, a constant fraction of the gas is converted into dust. Since the mass of the grain increases as \( a^2 \) and its cross section as \( \sim a^2 \), we have to decrease the bulk density of the material so that the dust optical depth remains approximately constant. Therefore, our modeling for the IR excess of IRAS 00470+6429 suggests that the dust grains are both large (\( a \gtrsim 1 \mu m \)) and fluffy (\( \rho_{\text{dust}} \sim 0.1 \, \text{g cm}^{-3} \)).

Finally, the three models also reproduce well the visible SED (Figure 1), but require different amounts of interstellar reddening: for the models with small grains, \( E(B-V)_{\text{IS}} = 1.1 \), and for the model with large grains, \( E(B-V)_{\text{IS}} = 1.2 \). Recall that \( E(B-V)_{\text{IS}} \) is a free parameter in the modeling and was set by fitting the visible SED. The different values of \( E(B-V)_{\text{IS}} \) can be easily understood by considering that the CS extinction of model 3 is essentially gray in the visible and for this reason its intrinsic CS reddening is smaller than the models with small grains.

The extent to which the CS disk modifies the stellar radiation can be assessed by comparing the model SED with the unattenuated stellar radiation (dashed line in Figure 1). Since the star is viewed close to edge-on, this causes the extinction of UV and visible radiation that is reprocessed into longer wavelengths. Most of the reprocessed radiation escapes in the polar direction, due to the fact that the vertical optical depth is much smaller than the radial optical depth, but part of it escapes radially. The \( U \)-band flux is particularly important for the SED fitting. Our models predict that when the object is viewed pole-on, the large bound–free excess produced by the inner envelope completely fills in the photospheric Balmer jump, thus producing a power-law SED up to the UV region. The fact that the Balmer jump is present is another evidence in support of larger inclination angles (Section 3.1).

4. DISCUSSION

At this point it is useful to recall the assumptions of the model presented here. For this exploratory study, it was assumed that a bimodal wind composed of a slowly outflowing disk and a fast polar wind, and an ad hoc density and velocity law were used to explore different characteristics of this bimodal wind model, such as the ratio between the mass-loss rate at the pole and the equator, and the opening angle of the dense equatorial outflow. Here, we intentionally limited the number of free parameters and focused our analysis on the CS region, aiming at studying its gaseous and dusty phases. The use of the radiative transfer code hdust allowed us to perform a fully consistent solution of the radiative transfer problem. Since the results are not marred by unknown radiative transfer effects, the comparisons between the models and observations represent genuine tests of the physical assumptions.

In our models, the line emission comes mostly from the dense outflowing disk, which has an opening angle of \( \Delta \theta_{\text{op}} = 7^\circ \), whereas the strong line absorption component originates in the upper layers of the disk. The model line profiles reproduce the emission component of the H1 lines, as well as important features of the absorption component, such as its depth, reasonably well.

The total stellar mass loss can be calculated by integrating Equation (2) over all solid angles

\[
\dot{M} = 2\pi \int_0^\pi \frac{dM}{d\Omega}(\theta) \sin(\theta) \, d\theta. \tag{14}
\]

Using the best-fit values from Table 1, we obtain \( \dot{M} = (2.5\pm2.9) \times 10^{-7} \, M_\odot \, \text{yr}^{-1} \). The lower limit corresponds to the fit for the 2006 December 13 epoch, whereas the upper limit describes the 2006 December 27 epoch. The total mass-loss rates derived here are 1–2 orders of magnitude lower than what is estimated for sgB[e] (Zickgraf 2006). On the other hand, it is at least 2 orders of magnitude larger than the mass-loss rate of main-sequence B stars, which is of the order of \( 10^{-10} \) to \( 10^{-9} \, M_\odot \, \text{yr}^{-1} \) (Gathier et al. 1981). This result, if corroborated by future studies, leads to the question of how mass loss is driven in FS CMa objects.

An inclination angle \( i \approx 84^\circ \) was obtained from the modeling. Since the system is viewed nearly edge-on and the emission component of the line profile is narrow, the presence of a large rotational component in the velocity field can be excluded, thereby justifying the pure radial expansion assumed here. It follows that a rotationally supported Keplerian disk, which is one of the scenarios proposed for the disks around sgB[e] (Porter 2003), can be excluded for IRAS 00470+6429.
According to our assumptions for grain formation, the dust around IRAS 00470+6429 is contained within a wedge of opening angle $\Delta \theta_{\text{dust}} \approx 10^\circ$. This opening angle was found by fitting the IR excess, which is a direct measure of the amount of radiation that is reprocessed by the CS dust. This value of $\Delta \theta_{\text{dust}}$ implies that the scaling factor $\eta$ in Equation (12) is about 0.02; therefore, much less than unity. The physical implication of this value of $\eta$ is that the critical density for grain formation derived by Gail & Sedlmayr (1988) might be overestimated, i.e., grains might be able to form on shorter timescales.

The models clearly indicate a prevalence of large grains in the dust around IRAS 00470+6429, for the reason that model 3 was the only model to satisfactorily fit the IR excess and to explain the absence of a conspicuous 9.7 $\mu$m silicate emission feature, which is to be expected for oxygen-based dust grains. This apparent contradiction can be explained by assuming that the medium around IRAS 00470+6429 is clumpy. In such a medium, dense clumps are the ideal sites for the grain formation and growth, because they provide the necessary shielding from the surrounding radiation. As the clumps expand, following the wind streamlines, they become optically thinner, exposing the grains to more radiation. Because small grains are hotter than large grains, they will have a larger probability to be destroyed. Grain sublimation may be able to explain the observed trend of the IR excess in the entire 2–13 $\mu$m range was the model with only small grains ($a = 1–50 \mu$m). The two extremes correspond to fits to observations made in 2006 December, but separated by an interval of two weeks. This gives a quantitative measure of how the mass loss varies in short timescales. The above value of $M$, while much smaller than that of sgB[e], which is of the order of $10^{-6}$ to $10^{-3} M_\odot$ yr$^{-1}$, is at least 100 times larger than that of main-sequence stars of spectral type B.

We adopted a prescription for dust formation based on two complementary criteria. In order to form dust at a given point in the CS envelope, the equilibrium temperature of the dust grains must be smaller than a given grain destruction temperature, $T_{\text{destruction}}$, and the gas density must be larger than a critical value. Several important radiative transfer effects are considered in our calculations, such as the shielding of the dust by the optically thick inner CS material and the fact that differently sized grains have different equilibrium temperatures.

We determined that the integrated stellar mass-loss rate is $M = (2.5–2.9) \times 10^{-7} M_\odot$ yr$^{-1}$. The two extremes correspond to fits to observations made in 2006 December, but separated by an interval of two weeks. This gives a quantitative measure of how the mass loss varies in short timescales. The above value of $M$, while much smaller than that of sgB[e], which is of the order of $10^{-6}$ to $10^{-3} M_\odot$ yr$^{-1}$, is at least 100 times larger than that of main-sequence stars of spectral type B.

To investigate the properties of the dusty content of IRAS 00470+6429 we studied dust models with three different grain size distributions, one with the standard MRN distribution ($a = 0.05–0.25 \mu$m), one with both small and large grains ($a = 0.05–10 \mu$m), and one with only large grains ($a = 1–50 \mu$m). The dust was assumed to be oxygen-based (silicates), an assumption supported by evolutionary arguments and our Spitzer observations of FS CMa stars.

The only model capable of reproducing the observed IR excess in the entire 2–13 $\mu$m range was the model with only large grains ($a_{\text{min}} = 1 \mu$m), because the presence of small grains always results in a strong 9.7 $\mu$m silicate emission, which is not observed. One consequence of the prevalence of large grains around IRAS 00470+6429 is that the bulk density of the grain material must be very small ($\rho_{\text{dust}} \sim 0.1$ g cm$^{-3}$). Therefore, the observed shape of the IR excess seems to firmly indicate that the CS dust grains of IRAS 00470+6429 are both very large and fluffy.
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