Small Signal Stability Analysis in SMIB & 3 Machine 6 Bus System using GWO Optimization Technique

Deepshika Lodha¹, Kapil Parkh², Raunak Jangid³, Sagar Trivedi³
¹M.tech Scholar, ²Assistant Professor, Electrical Engineering, SITE Nathdwara
³, ⁴Assistant Professor, Electrical Engineering SITE, Nathdwara

Abstract: A power system is a complicated network which has the task of fulfilling various consumer power demands continuously. But in its process too many disturbances occurs. These disturbances may be a common single line to ground fault, double line, double line to ground fault, three phase fault or it could be small signal disturbances. To eliminate it is utmost importance to resume the continuity of power supply which in turn ensures its reliability. Hence, a power system is always equipped some kind of controllers to come back to its original operating status after this disturbances.

Here, a SMIB system more specifically a Modified Phillip-Heffron’s model is presented which has Static Synchronous Series Compensator (SSSC) as the controller. To further improve its dynamic performance a nature inspired optimization technique is utilized. This is Grey Wolf Optimization (GWO). The system is tested for electrical power deviation, power angle deviation and speed deviation under two different cases. The first case is when reference voltage setting is increase by 5% step and the second case is the step increase of 10% in mechanical torque. The results of GWO based SSSC are compared and tabulated with SMIB without any controller and with Gravitational Search Algorithm (GSA) based SSSC.

The further analyses consider the more real scenario of multi machine system (MMPS) which has 3 machine and 6 bus. It utilizes GWO based coordinated damping controller consisting of SSSC and PSS. This model is tested under different fault conditions as mentioned above and then its results are compared with MMPS without any controller and with conventional power system stabilizer (CPSS). For simulation both the above model of SMIB and MMPS MATLAB/SIMULINK is used.

Keywords: Power System: Power System Stabilizers (CPSSs); Single Machine Infinite Machine System; 3 machine 9 bus System; Grey Wolf Optimization (GWO)

I. INTRODUCTION

A. Introduction

Load demand has been increasing at a fast rate and it is difficult to fulfill it. Hence, the solution for it is to interconnect many power systems together. These are tied via the tie lines and usually these are weak in nature. This is the reason for the introduction of low frequency oscillations and if these persist can cause loss of synchronism. To eliminate these oscillations a damping controller is required[2]. This has led to take a closer look and analysis the power system so as to maintain its stability within the margin while maintain its security. Previously, keeping the power system away from its stability limits ensure the better dynamic control over the whole system. Other studies were also carried out in the area so as to address the problem stability.

There are namely these types of stability in power system, large and small signal. Large signal stability is also known as transient stability. In case of small signal stability when there is no proper damping it occurs. While when power system encounters the serious transient disturbance like short circuit or the tripping of line it is the case of large signal stability. Starting Operating state and severity of disturbances influences the stability. The configuration of the system is so set in order to be in the stable state following set of chosen contingencies [1]. With the development of new and better technology to tackle this issue, we now have Flexible AC transmission devices (FACTS). These are electronic based modern devices. This family of devices has the capability of controlling the factors which affects the performance of the power system. It has ability of repeatability and smoother control resulting in less response time and efficient. The following work is more focused around compensating series reactance of the line in order to improve the stability especially transient stability. The big family of FACTS includes Static Synchronous Series Compensator (SSSC), Interline Power Flow Controller (IPFC), Thyristor Controlled Series Capacitor (TCSC), Thyristor Switched Series Capacitor (TSSC), Thyristor Controlled Series Reactor (TCSR) and Thyristor Switched Series Reactor (TSSR). But here SSSC has been chosen to show its usefulness in addressing the given problem of stability [15].
There are several techniques where SSSC has been associated with various optimization techniques like particle swarm optimization (PSO), genetic algorithm (GA), fuzzy logic, etc. A new technique is discussed to achieve the given goal which is known as Grey Wolf Optimization (GWO). This algorithm is based on the social behavior of the grey wolf pack. The process is inspired from the various features of social pack of these creatures for hunting and preying. This kind of problem in single machine Infinite bus (SMIB) system can be solved with much ease as compared to the system where more than one machine is involved i.e. a multi machine system. It is more practical system where observation of such problems can lead to practical solutions. Although, SMIB study did give the idea of characteristics of machine subjected to different conditions. The following context consists of two work theory, one is related to SMIB and other is related to Multi Machine Power System (MMPS). In SMIB the low frequency oscillations are damped out with the implementation of SSSC which is optimized using the GWO algorithm. In the next set of section a MMPS model is developed in which conventional Power system Stabilizer (CPSS) is used is in integration with SSSC for inter area oscillation. This MMPS designed with 3 machine interlinked by 6 buses. The machines are named $G_1$, $G_2$, and $G_2$. Here, the power system is modeled with CPSS coordinated by SSSC which is tuned using GWO and to compare it was also simulated with CPSS only and without it. The results have been tabulated and compared with different conditions[7].

### B. Objective Function

The problem is given as an integral time absolute error of the speed deviations $\Delta \omega$. The objective function to be minimized is termed as $J$ and is given as below,

For SMIB

$$J = \int_{0}^{t_f} |\Delta \omega| . t . dt$$  \hspace{1cm} (1)

For multi machine system

$$J = \int_{0}^{t_f} \left( \sum |\Delta \omega_k| + \sum |\Delta \omega_l| \right) . t . dt$$  \hspace{1cm} (2)

$\Delta \omega_k$: inter area $\Delta \omega$

$\Delta \omega_l$: Oscillations local modes

$t_f$: Simulation time range

Therefore, the problem of design focuses on minimizing both the fitness function at the same time which are bounded by the set of parameters as shown below[25][20],

$$K_i^\text{min} \leq K_i \leq K_i^\text{max}$$  \hspace{1cm} (3)

$$T_{1i}^\text{min} \leq T_{1i} \leq T_{1i}^\text{max}$$  \hspace{1cm} (4)

$$T_{2i}^\text{min} \leq T_{2i} \leq T_{2i}^\text{max}$$  \hspace{1cm} (5)

$$T_{3i}^\text{min} \leq T_{3i} \leq T_{3i}^\text{max}$$  \hspace{1cm} (6)

$$T_{4i}^\text{min} \leq T_{4i} \leq T_{4i}^\text{max}$$  \hspace{1cm} (7)

### II. SYSTEM MODEL

#### A. Power System with SSSC linear Dynamic Model

The linearization of nonlinear model gives the linear Heffron-Phillips model of a SMIB system including SSSC around a nominal operating point.

![Heffron-Phillips model along SSSC](Fig.1: Heffron-Phillips model along SSSC[3])
B. Multi Machine Power System

In the above single line diagram there are three generating units G1, G2 and G3. Also, there are 6 buses in the system (B1, B2, B3, B4, B5, B6). G1 is considered to be the largest unit out of the three which is connected to B1 and hence it is the slack bus. G2 and G3 are connected on bus B2 and B3 respectively. Load 1, 2, 3 and 4 are the loads connected on bus bar 1, 2, 3 and 4.

![3 Machine 6 Bus System Single Line Diagram](image)

Fig.2: 3 Machine 6 Bus System Single Line Diagram[8]

C. Power System Stabilizer (PSS)

The power system considered here for study receives control command from PSS via exciter. The excitation system with PSS taken here is IEEE type STI

![Structure of Excitation system with PSS](image)

Fig.3: Structure of Excitation system with PSS

The output of PSS $V_{pss}$ is provided to excitation system where it will add to $V_{ref}$ which is the reference voltage of excitation system.

III. PSS TUNED BY GWO

A. Grey wolf optimization (GWO)

This optimization technique is given by Mirjalili. It imitates the grey wolf hierarchy leadership as they are known for group hunting\[12\]. It is among the newest set of meta-heuristic optimization algorithms. It was developed for solving the double layer grids problem which takes into account the non linearity. Its results are superior to the other algorithms in set. For the first time to learn Multi Layer Perception (MLP) it was used.

With reference to the above statement these wolfs live pack and are basically from canidae family. As these, live in pack they have a leader who is Alpha indicating their strict social dominant hierarchy. As Alpha is the leader, most of the decision for group is taken by him. And, hence his decision should be followed by other members of the pack. The common decision involves sleeping place, hunting, waking time etc. The Alpha may not be the strongest member of the pack but the best to manage the whole group. This implies that the discipline and organization in the pack is considered prior to the strength\[10\].

Group hunting is among the many features of their social environment. The main phases in hunting are,

1) Tracking the prey, then chasing them and at last approaching them.
2) The act of pursuing, encircling and harassing of prey until it stop moving.
3) Last is attack on prey.
B. Algorithm Pseudo code and GWO Flow Chart

1) Grey wolves population is created initially let it be $X_i$ (i=1,2, . . . ., n)
2) $\alpha$, A and C is initialized.
3) Search agent fitness is calculated, $X_{\alpha}$= best search agent $X_{\beta}$= 2nd best search agent $X_{\delta}$= 3rd best search agent
4) while (t< maximum iteration count) for each search agent
   Current search agent position is updated by
   \[
   \bar{X}(t + 1) = \frac{X_1 + X_2 + X_3}{3}
   \]
   end for
   $\alpha$, A and C are updated
   all search agents are fitness are calculated
   $X_{\alpha}$, $X_{\beta}$ and $X_{\delta}$ are updated
   t=t+1
   end while
   return $X_{\alpha}$

IV. RESULT AND DISCUSSIONS

In this section, the results of the developed simulation model under different contingencies are presented and discussed. There are two types of the proposed model as a single machine infinite bus system & multimachine system. In SMIB system define with Modified Heffron-Phillips model with SSSC. The result tested with two cases 5% step increase in reference voltage settings & 10% step increase in mechanical torque power input at a different speed, power angle, electrical power angle deviation at without controller, with GSA, with GWO technique. In multimachine system define with 3 machine 6 bus system & tested at various cases three-phase fault, double line to ground fault(L-L-G),line to ground fault(L-G),line to line fault(L-L),line outage, small disturbance, signal transmission delay at various mode inter-area mode of oscillations, local area mode of oscillation, variation of SSSC injected voltage.

A. Case-1 SMIB System

| S.N. | System    | SSSC Parameter Tuned by GWO |
|------|-----------|------------------------------|
| 1.   | SMIB System | $73.4989$ | $0.0036159$ | $0.0428$ |

Fig. 4 shows the convergence rate of objective functions of SMIB system.

**Table1: SSSC Parameters Tuned by GWO**

![Fig. 4: Convergence of Objective Function for Best Cost in SMIB System](image-url)
1) Case-1 10% Step Increase in Mechanical Torque Input & 5% Step Increase in Reference Voltage Setting: For completeness, the effectiveness of the SSSC controllers is additionally tested by considering a disturbance in mechanical torque input & reference voltage setting. The reference voltage setting ($V_{ref}$) & mechanical torque input is increased by a step of 10% & 5% at $t = 1$ s. Finally, SSSC tuned by GWO shows superior response & improve the stability of the power system. These positive results of the proposed GWO optimized SSSC based controller can be attributed to its faster response with less overshoot compared to that of GSA.

![Graph](image1.png)

**Fig. 5: Speed Deviation in SMIB System for Mechanical Torque Input**

![Graph](image2.png)

**Fig. 6: Power Angle Deviation in SMIB System for Reference Voltage Setting**

![Graph](image3.png)

**Fig. 7: Electrical Power Deviation in SMIB System for Reference Voltage Setting**
Table 2: 10% Step Increase in Mechanical Torque Input 5% Step Increase in Reference Voltage Setting at SMIB System

| S.N. | Types of Deviation    | Without SSSC (Settling Time) | With GSA SSSC (Settling Time) | With GWO SSSC (Settling Time) |
|------|------------------------|-----------------------------|-----------------------------|-----------------------------|
| 1.   | Speed Deviation        | Highly Oscillatory           | 2.1069                      | 1.4928                      |
|      | Power Angle Deviation  | Highly Oscillatory           | 2.0165                      | 1.4414                      |
|      | Electrical Power Deviation | Highly Oscillatory       | 1.7480                      | 1.5545                      |

B. Condition-2: Multi-Machine System(3 Machine 6 Bus System)

Fig. 8 shows the convergence rate of objective functions of MMPS system & table 3,4 shows SSSC & PSS parameters optimized by GWO

![Objective space](image)

Table 3: SSSC Parameters Tuned by GWO

| S.NO. | Parameters | K   | T₁   | T₂   | T₃   | T₄   |
|-------|------------|-----|------|------|------|------|
|       | SSSC       | 32.2106 | 3.2532 | 3.2574 | 2.6826 | 8.1381 |

Table 4: PSS Parameters Tuned by GWO In MMPS System

| S.NO. | Number of PSS | Parameters of PSS |
|-------|---------------|-------------------|
| 1     | PSS₁          | K₁₁ T₁₁ T₁₂ T₁₃ T₁₄ |
|       |               | 10.7838 7.8073 4.0340 2.0506 2.5979 |
| 2     | PSS₂          | K₂₁ T₂₁ T₂₂ T₂₃ T₂₄ |
|       |               | 73.3871 3.2836 3.9248 4.2172 3.6642 |
| 3     | PSS₃          | K₃₁ T₃₁ T₃₂ T₃₃ T₃₄ |
|       |               | 72.0643 9.4737 7.9172 8.2412 6.4456 |

Fig. 9-14 shows various graphs at different cases In this case at t = 1 s, in between bus 1 and bus 6 a 3-cycle, 3-phase self-clearing fault, L-L-G, L-G, L-L fault and small disturbances is applied with as regards to bus 6. Various figure represents the system responses with this kind of disturbance and numerous kinds of the response given as inter-area mode, local-area mode of oscillation and SSSC injected voltage. These figures clearly demonstrate that the responses are oscillatory in nature if the controllers aren’t within the system. The system response with none controller is diagrammatical during a blue line with the legend ‘No Control’, the system response with CPSS is diagrammatical during a line with legend ‘CPSS’ and so as to represent the proposed system then SSSC optimized by GWOPSS. The system response with GWOPSS is diagrammatical during a black line with legend ‘GWOPSS’. It’s evident from that proposed SSSC controller tuned by GWOPSSS offer higher dynamic response having lesser subsidence time.
Fig. 9: Inter-Area Mode of Oscillation in Three Machine System for 3-Phase Fault

Fig. 10: Local-Area Mode of Oscillation in Three Machine System for L-L-G Fault

Fig. 11: SSSC Injected Voltage in Three Machine System for L-G Fault

Fig. 12: Inter-Area Mode of Oscillation in Three Machine System for L-L Fault
Fig. 13: Local-Area Mode of Oscillation in Three Machine System for Small Disturbance

Fig. 14: SSSC Injected Voltage in Three Machine System for Line Outage Disturbance

1) Signal Transmission Delay applied at 3 Machine 6 Bus Systems: Fig. 15-17 shows various time delay as 25 ms, 75 ms & 100 ms. The system performance tested with time delay but there is the negligible effect of the system performance. The system shows a superior response in the presence of the proposed controller. That the effect is almost negligible with the variation of the time delays.

Fig. 15: Inter-Area Mode of Oscillation in Three Machine System for Signal Transmission Delay
Fig. 16: Local-Area Mode of Oscillation in Three Machine System for Signal Transmission Delay

Fig. 17: SSSC Injected Voltage in Three Machine System for Signal Transmission Delay

Table 5: MMPS System at Without Controller and with CPSS and GWO SSSC Controller at Different Types of Loading at Different Types of Fault

| S. N. | Types of Fault | Types of oscillation | Without Controller (Settling Time) Seconds | With CPSS Controller (Settling Time) Seconds | With Coordinated (SSSC+PSS) Tuned by GWO (Settling Time) Seconds |
|-------|----------------|----------------------|-------------------------------------------|---------------------------------------------|---------------------------------------------------------------|
| 1     | 3-Phase        | Inter-Area Mode of Oscillation | Highly Oscillatory                          | 2.7442                                      | 1.7454                                                        |
| 2     | L-L-G          | Inter-Area Mode of Oscillation | Highly Oscillatory                          | 2.7766                                      | 1.7570                                                        |
| 3     | L-G            | Inter-Area Mode of Oscillation | Highly Oscillatory                          | 2.7442                                      | 1.7434                                                        |
| 4     | Small Disturbance | Inter-Area Mode of Oscillation | Highly Oscillatory                          | 2.7442                                      | 1.7434                                                        |
| 5     | Line Outage Disturbance | Inter-Area Mode of Oscillation | Highly Oscillatory                          | 2.4637                                      | 2.1538                                                        |
V. CONCLUSIONS
The system is tested with two cases as SMIB system & multimachine system. In SMIB system a Modified Heffron-Phillips model with SSSC is developed here and it is optimized using GWO. System tested in two cases in first case reference voltage setting is increased by 5% step and then it is tested with step increase of 10% in mechanical torque input. All condition GWO optimized shows superior response. In multimachine system the system of 3 machine 6 bus system is tested, with GWO technique at different faults which are three-phase fault, double line to ground fault (L-L-G), line to ground fault (L-G), line to line fault (L-L), line outage, small disturbance, signal transmission delay at various mode inter-area mode of oscillations, local area mode of oscillation, variation of SSSC injected voltage. Overall a robust performance is achieved when PSS is coordinated by SSSC. On application of GWO, its performance further increases.

REFERENCES
[1] SR Paital, PK Ray and A Mohanty, "A review on stability enhancement in SMIB system using artificial intelligence based techniques." In 2018 IEEMA Engineer Infinite Conference (eTechNxt), pp. 1-6. IEEE, 2018.
[2] E Hadavandi, S Mostafayi and P Soltani, "A Grey Wolf Optimizer-based neural network coupled with response surface method for modeling the strength of siro-spun yarn in spinning mills." Applied Soft Computing 72, pp. 1-13, 2018.
[3] AM Baraeen and HN Al-Duwaish, "Coordinated Design of a Fuzzy Logic Power System Stabilizer and an SVC-based Stabilizer for Single-Machine Infinite-Bus Power System." In 2018 5th International Conference on Control, Decision and Information Technologies (CoDIT), pp. 464-469. IEEE, 2018.
[4] R Jena, S Chirantan, SC Swain and PC Panda. "Load flow analysis and optimal allocation of SVC in nine bus power system." In 2018 Technologies for Smart-City Energy Security and Power (ICSESIP), pp. 1-5. IEEE, 2018.
[5] A Saxena, BP Soni, R Kumar and V Gupta, "Intelligent Grey Wolf Optimizer–Development and application for strategic bidding in uniform price spot energy market." Applied Soft Computing 69, pp. 1-13, 2018.
[6] A. Haldera, N. Palb and D. Mondalc, “Transient Stability Analysis of a Multimachine Power System with TCSC Controller – A Zero Dynamic Design Approach”, Electrical Power and Energy Systems 97, 2018, pp. 51–71.
[7] X Mi, J Wang and R Wang, "Stochastic small disturbance stability analysis of nonlinear multi-machine system with Itô differential equation." International Journal of Electrical Power & Energy Systems 101, pp. 439-457, 2018.
[8] T Guesmi, A Farah, HH Abdallah and A Ouali, "Robust design of multimachine power system stabilizers based on improved non-dominated sorting genetic algorithms." Electrical Engineering, pp. 1-13, 2017.
[9] Sreediva KM, P A Jeyanth and D Devaraj, "Fuzzy logic based power system stabilizer for damping low frequency oscillations in power system." In 2017 International Conference on Innovations in Electrical, Electronics, Instrumentation and Media Technology (ICEEIMT), pp. 201-205. IEEE, 2017.
[10] L Rodríguez, O Castillo and J Soria, "Grey wolf optimizer with dynamic adaptation of parameters using fuzzy logic." In 2016 IEEE Congress on Evolutionary Computation (CEC), pp. 3116-3123. IEEE, 2016.
[11] G Ravibabu and T GowriManohar, "Comparative study of FACTS devices used for stability enhancement of off shore integrated multi machine system." In 2016 IEEE 7th Power India International Conference (PIICON), pp. 1-6. IEEE, 2016.
[12] S. S. Shingare, " Modelling and Analysis of Single Machine Infinite Bus System with and without UPFC for Different Locations of Unsymmetrical Fault", International Journal of Engineering Research and General Science, Volume 3, Issue 1, pp 418-426, January-February, 2015.
[13] S Sharma and S Narayan, "Damping of low frequency oscillations using robust PSS and TCSC controllers." In Computing, Communication and Networking Technologies (ICCCNT), 2017 8th International Conference on, pp. 1-7. IEEE, 2017.
[14] O Bozorg-Haddad, ed. Advanced optimization by nature-inspired algorithms. Springer Singapore, 2018.
[15] P Kundur, NJ Balu and MG Lauby, Power system stability and control. Vol. 7. New York: McGraw-hill, 1994.
[16] KR Padiyar, FACTS controllers in power transmission and distribution. New Age International, 2007.