Review
Challenges in Raw Material Treatment at the Mechanical Processing Stage

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Abstract: This paper concerns problems related to the mechanical processing of mineral raw materials. The aspects explored were limited to the analysis of comminution technologies in terms of their effectiveness and energy consumption, modeling and simulation approaches, the assessment of crushing results, and environmental aspects. This article includes investigation of new technologies of comminution, comparing HPGR, high-voltage pulses, and electromagnetic mills. In the area of modeling and optimization, special attention was paid to the approximation of the particle size distribution of crushing products by means of Weibull, log-normal, and logistic functions. Crushing products with an increased content of fines were well characterized by Weibull’s distribution, while log-normal function adequately described HPGR products with a relatively low content of fines.

Keywords: raw materials; mineral processing; enrichment; comminution; HPGR; approximation of particle size

1. Introduction

The processing technology used for mineral raw materials is crucial in terms of the production of numerous metals and non-metallic products sourced and extracted by means of mining techniques. Though the entire value chain of metal production includes a number of steps (from geology, through to mining, metallurgy, and manufacturing), the mineral processing stage, to some extent, influences the quality of the final product and the effectiveness of the entire process of commercial product manufacturing. Despite its complexity and the application of many physical, mechanical, chemical, and other types of separation processes and operations, ore mineral processing can generally be divided into two overarching stages:

(a) reduction in the size of the feed material;
(b) separation of useful mineral from the gangue.

The primary purpose of the size reduction stage is the liberation of useful mineral in a way that allows for proper separation in the downstream separation stage. This process for the case of ores is presented in Figure 1. The ROM (run-of-mine) material is a mix of compounds of ferrous or non-ferrous metals and gangue. Useful elements and compounds (black color on Figure 1) are “locked” among the gangue material in the ROM. In such a form, it is rather difficult to separate them from the gangue with high efficiency. Through the application of comminution operations, the size of individual particles can be made finer and thus the liberation of useful compound is more intense compared to the ROM material (center of Figure 1). Compared to non-crushed ores, the separation of such materials can be carried out in a less complicated manner and higher recoveries can be achieved. The separation product contains a significant amount of useful compounds (lower part of Figure 1). This situation applies to ore enrichment, which are generally divided into ferrous and non-ferrous minerals (i.e., cupriferous, gold or silver-bearing, and other metals except for iron).
In both aggregates production and the processing of rock materials, (such as crushing stones, sands, and gravels), the stage of size reduction (comminution) constitutes the primary step. This directly influences the qualitative parameters of final products in terms of size and shape (aggregate production sector) or specific surface (cement clinker industry) [1].

Considering previous text, the mechanical processing of raw materials is a crucial stage in the technology of both ore processing and the aggregate production sector. Proper passage through this stage initially influences the potential effectiveness of the core beneficiating operations of minerals from the scope of useful mineral recovery, and much research has been carried out in this area. Current trends in these investigations mainly include:

- development of new comminution technologies;
- optimizing the performance of recent applications;
- modeling, simulation, and performance optimization of mechanical processing circuits.

Recently, environmental aspects have been gaining greater attention, especially in terms of decreasing the negative impact of mechanical processing operations on the environment and society; in particular, attention has been paid to harmful and annoying emissions of dusts, gases, heat, and noise. Operations of industrial comminution account for as much as 3% to 5% of the total usage of electric energy in the world [2]. Despite this, their performance effectiveness is relatively low and has an inverse relationship to the size of the crushed material. For example, the energetic efficiency of tumble mill operation is estimated to be around 15%. Meanwhile, the production efficiency of some types of very fine grinding products can be as low as 1% [3]. Comminution energy utilization is higher in crushers, particularly in impact crushers. However, it is dependent on the type of raw material used and the crushing stage within the technological circuit [4]. Research generally confirms that crushing uses between 0.5 and 1 kWh/Mg, and that crushing devices using attrition and shear forces consume between 40% and 80% more comminution energy than machines based on impact forces [5]. Compression and impact forces techniques in material disintegration save the most energy. However, the low energy utilization for a breakage mechanism in conventional crushing and grinding equipment leads to the development of innovative comminution technologies [6].
2. Development in Crushing and Grinding Technology

2.1. HPGR Technology

HPGR devices are considered one of the most energy-efficient comminution machines. However, despite their lengthy existence in industrial mineral processing circuits, there have been many research projects aimed at improving their operational performance. While HPGRs indisputable energetic benefits have been largely proven in the literature [7,8], results from more recent investigations show room for improvement in both separation in flotation and leaching processes [9–11], mostly due to the intense liberation of useful mineral [12].

The average unit energy consumption for HPGR devices varies between 2 and 3–4 kWh/Mg; however, this depends on the mechanical properties of the material, the equipment size, and the recirculation scheme of the HPGR feed and product. Industrial practice shows that in calculations the value of 2.5 kWh/Mg is quite often accepted. Compared to tertiary crushing devices, applying HPGR to the comminution circuits of ore lowers grinding energy by 20%–30% in downstream operations.

In the SAG-based grinding circuit, the ball mill grinding energy consumption is comparable to the grinding energy used in mills following the HPGR. However, the overall energy reduction in a HPGR-mill configuration can be greater than 30%. The benefits of HPGR in mineral beneficiation are visible at the level of useful mineral liberation. Microscopic analysis has found [12] values of 75% to 95% for copper minerals liberated from sulfide ores, depending on the operating pressure value. Copper recovery in downstream flotation varies from 80% to 85%, while the same value for ore that has been conventionally crushed (i.e. without using of high-pressure technology) is 80%. HPGR is beneficial in the recovery of minerals, as well as in leaching and cyaniding operations. Copper extraction from sulfide ores was 2% to 8% higher when leaching from HPGR-based circuit products, and kinetic readings of the process were more favorable [13]. Comparable effects are evident when heap leaching other minerals from upstream ores treated by HPGR. The metal extraction rate for HPGR is 10%–15% higher than that of conventional crushing devices [14].

2.2. High Voltage Breakage

Investigations into improving the efficiency of breakage energy led to the development of other innovative techniques of comminution. High-voltage electrical pulse technology helps to achieve more intense liberation in ore comminution. The efficiency of this technique greatly depends on the regime of pulsation, as well as the texture and mechanical and electrical properties of the ore material. The optimization of pulse parameters is considered a very significant issue; however, it also creates problems, and a pulse generator dedicated especially to mineral liberation should be used [15]. Laboratory practice shows that if electric pulses are not adjusted to the material properties, there is no improvement in the effectiveness of liberation compared to using mechanical comminution techniques. In one example, gold ore which had been treated upstream by electric pulses did not record significantly improved extraction compared to mechanical breakage. However, after the optimization of the pulsating regime, the gold recovery was 35% higher due to the more intense liberation [16].

Gold recovery in cyanidation can be 15%–50% higher than in that in ores that have been mechanically ground; however, this depends on the material’s properties. In some cases, a 60%–70% recovery can be observed.

Lower rates of metal recovery in flotation can be found; however, some results show that up to a 20% higher concentration of metal can be obtained in tail flotation following high-voltage pulses. Estimates of the unit energy consumption for the high-voltage pulse technique show that it varies from 3 to 5 kWh/Mg. There are relatively few publications in world scientific databases concerning investigations on the using of high-voltage pulses in comminution. The bibliometric analysis of the Core collection of Web Science database
searching for the terms “high voltage pulses” and “comminution” or “liberation” shows that 100 publications have been published on this topic since 2012.

2.3. Electromagnetic Mills

The grinding technology used in electromagnetic mills is a novel method of material disintegration that utilizes rotating electromagnetic fields [17]. Fast-moving grinding media in the shape of short rods, made of ferromagnetic material, cause material breakage in the working chamber. Laboratory tests confirm the very short duration of the process; it requires from several to few tenths of seconds to prepare a 500 g sample for flotation operation. In terms of comminution ratio, the achieved results are very good compared to those achieved using conventional tumbling mills, thus the level of liberation is also higher. The technology is relatively new; only 50 publications can be found in international scientific databases, with nearly 75% issued within the last 5 years. Similarly to high-voltage pulses, the main issue is the lack of full-scale plant installation. However, in this case a quarter-scale machine is available. No test results for ore beneficiation in hydrometallurgy operations for electromagnetic mill products have been obtained so far; however, the results of flotational separation for sulfide copper ore show copper recovery increased by about 10%–15% compared to conventional crushing and grinding devices. It is, however, difficult to find indisputable evidence for overall separation improvement, especially at the semi-plant and plant scale; however, it seems that for some specific purposes, the technology may bring be beneficial.

Table 1 summarizes the three characterized technologies for raw material comminution in terms of their capacity, energy consumption, and technological effectiveness.

| Type of Benefit                                           | Unit            | Type of Comminution Technology |
|-----------------------------------------------------------|-----------------|--------------------------------|
| Unit energy consumption                                  | kWh/Mg          | HPGR  | Electromagnetic Mill | Electric Pulses |
| Benefits in mineral liberation compared to conventional crushing | %               | 2–4   | 50–150             | 3–5             |
| Benefits in useful mineral recovery compared to conventional crushing, hydrometallurgy | %               | 10–20 | 10–15              | 10–15           |
| Benefits in useful mineral recovery compared to conventional crushing; flotation | %               | 1–4   | 5–20               | up to 20        |
| Plant-scale operation of the technology                  |                 |       | Yes               | No              |
| Energy savings compared to conventional crushing circuit   | %               | Up to 30 | No data             | No data         |
| Capacity increases compared to conventional crushing circuit | %               | 0–15           | No data             | No data         |

3. Circuits Layout and Optimization

3.1. Design Assumptions

A suitable circuit layout, with properly designed material flows among specific operations, including recycle streams, is of great significance in optimizing feed disintegration processes. Following the one overarching principle of mechanical processing: “do not crush unnecessarily”, special attention is (or, at least, should be) paid to the by-passing of fully or sufficiently liberated particles [18]. This is especially true for comminution techniques that cause greater generation of micro-cracks during grain disintegration processes which may contribute to higher liberation. Such materials are proceeded to pre-concentration, where some share of useful minerals can be quickly recovered. Such an approach can be characterized by the following effects:
• A reduction in the capacity requirements of downstream grinding stage(s), which allows the installation of smaller grinding devices. More intense disintegration occurs in upstream crushing processes, which requires much less energy than grinding operations (Figure 2). The Figure gives a general idea of relationship between the size of treated material and the required energy for comminution. An exponential increase in the grinding energy can be observed, together with further decreasing the size of already fine material;

• The optional application of separation within comminution circuits, especially devices based on physical separation, such as jigs [19]. Jig separation has a long history of existence in technological circuits of mechanical processing or raw materials; however, many investigations aiming to improve the process for specific conditions and individual materials have been carried out [20,21]. This cost-efficient technology may give favorable results in the extraction of useful mineral amongst certain particle size fractions. Available results also confirm the potential for the separation of materials with relatively low differences in densities, provided specially designed devices are used [22].

• Decrease in the grinding energy consumption, which decreases the overall energy consumption of the circuit operational costs.

![Figure 2. Relationship between energy usage for breaking and the size of treated particles.](image)

Economic benefits include a reduction in CAPEX due to the possibility of the installation of smaller size devices, as well as contributing to the reduction in a major component of OPEX.

Such non-conventional layouts—i.e., where the breakage is more intensive on earlier comminution stages—are popular, especially in HPGR-based circuits. The relative energy savings in such configurations may reach 25% [23].

3.2. Simulation in Mineral Processing

Nowadays, many techniques and methods supporting the design, efficient operation, and performance assessment of mechanical processing are used in investigations. Among the most significant characteristics determining the effectiveness of comminution operations are particle breakage intensity and size reduction ratio, the size distribution of products, productivity, energy consumption, wear of liners, and movable parts of machines and others [24,25]. These can be distinguished following major directions in the modeling of mineral processing:

• Simulation tools and techniques showing models of behavior of grained material during the specific process, operation of a device, interactions amongst particles of the material, and interactions between the material and device. Various numerical
techniques can be used in these simulations. The Discrete Element Method (DEM) is an especially popular technique used for this process, as well as in other disciplines outside mineral processing.

- Models capable of predicting the specific results of process performance. These include the approximation of particle size of comminution product, screening efficiency, comminution ratio, volume of material recycle, and others. These models are either based on theoretical distributions of random variables with confirmed applications in mineral processing or utilize principles of mathematical modeling.

- Optimization tools and applications based on the principles of mathematical and statistical modeling [26–28].

Modeling and simulation techniques for mapping the behavior of discrete mediums, such as grained materials, have become useful and powerful tools as the computational power and potentials of dedicated hardware accelerated in the last few decades. As a result, it is now possible to carry out very large numbers of calculations in very short time sequences for each modeled element. It is also now possible to characterize short-distance interactions (i.e., particle–particle, particle–device) as well as long-range impacts, (i.e., gravity, electrostatic, magnetic, or other forces). The mentioned DEM method gained significant popularity in the modeling of various enrichment processes, and many examples concerning this issue are present in the literature.

The mineral processing constitutes only a fraction of the wide practical usage of this simulation technique, but some significant aspects of mineral processing were covered to some extent:

- Description of granular material flow in comminution processes;
- Potential prediction of particle size distribution for selected crushing products;
- Equipment design on the basis of analyzed process behavior;
- Simulation of conveyor transportation operations;
- Description of motion of particles in selected processes of gravitational separation.

There are, however, gaps and challenges for this method, especially in the simulation of fine and very fine particle motion, (i.e., in fine grinding processes). The problem is that a number of particles in simulation is limited, what requires the use of a method of extrapolation, especially for finer sizes.

4. Modeling Approach

The use of the correct modeling approach assists in the description of an operation, as well as the results achieved for specific operations in mineral processing. These have significant cognitive meaning, especially for conditions beyond the operational regime, such as an increased throughput, exceeded values of operational parameters of devices (i.e., increased $F_{sp}$ in HPGR, higher rotational speed of shaft in impactors, higher/lower amplitude/frequency of vibration screen), and others. These situations, however, are undesirable and efforts have been made to eliminate them or at least to limit their impact on the process course. The issue of greater significance is the possibility of the assessment results of mechanical processing proceeded through specific operation. Comminution results seem to be the most important among them, and the most popular approach consists in approximation of PSD of crushing products [29]. The second significant issue seems to be assessment of the useful mineral liberation degree, but nowadays it appears that only analytical methods utilizing scanning electron microscopy (SEM), such as MLA, can be effective. The PSD approximation method is not new and has been present in mineral processing investigations for decades. It consists of the assumption that the act of particle breakage is a kind of probability, especially concerning the size of newly created particles in the crushing product [30,31]. The approximation of crushing results technically utilize the Least Squares method (LS) and can be performed by means of various mathematical functions (distributions). Most of these have a confirmed application into a specific type and size of feed material and crushing device [32]. For example, the Weibull (or RRB) distribution was introduced into mineral processing in the 1930s [33].
for the assessment of the particle size of crushing products. Log-norm distribution, in turn, has found application for the approximation of fine crushing (grinding) products [34]. In recent decades, functions previously used in other disciplines have also been used in mineral processing. The logistic distribution could be such an example. Approximation functions used in the estimation of particle size distribution of crushing products usually have two parameters, denoted as shape and scale parameters. It is worth mentioning that the application of theoretical distributions with a greater number of parameters may improve the modeling results; however, problems can appear in the interpretation of results, especially when the model is used in more general cases. So-called “censored distributions”, (i.e., theoretical distributions with additional parameters that limits the particle size of the product by introducing minimum or maximum particle ($d_{\text{min}}$ or $d_{\text{max}}$)) can be more efficient in some cases [35].

The fitting accuracy can be assessed through the estimation error $s_r$, which is defined through Formula (1).

$$
s_r = \sqrt{\frac{\sum_{i=1}^{n} (y_{\text{emp}} - y_{\text{mod}})^2}{n-2}},
$$

where $y_{\text{emp}}$, empirical data; $y_{\text{mod}}$, modeling data; $n$, number of data points.

An exemplary approximation of the particle size distribution of a HPGR product was performed using three approximation functions, as presented in Table 2.

Table 2. Approximation functions used in fitting and the obtained results.

| Approximation Function | Approximation Formula |
|-----------------------|----------------------|
| Weibull’s distribution | $F(d) = 1 - \exp\left(-\frac{d}{d_0}\right)^n$ |
| Log-norm distribution | $F(d) = \frac{1}{\pi} \int_{-\infty}^{\infty} \exp\left(-\frac{t^2}{2}\right) dt, \quad t = \ln\left(\frac{d}{d_0}\right)$ |
| Logistic distribution | $F(d) = \frac{1}{1 + \exp(-c \times d)}$ |

The testing program included the crushing of feed material in the laboratory HPGR device under two values of operational pressing forces $F$: 15 and 10 kN. The width of rolls $L = 100$ mm, diameter $D = 300$ mm. Three samples of the same feed material with a similar particle size distribution were crushed in the HPGR press device under various conditions in order to obtain products with diverse particle size distributions:

- product 1: the material with increased content of fines, the feed was crushed twice under base pressing force (15 kN);
- product 2: the material with relatively lower content of fines—crushed under lower pressing force (10 kN);
- product 3: the material with balanced content of individual particle size fractions—crushed once under base pressing force (15 kN).

The PSD of all products, along with fittings with three functions, are presented in Figures 3–5.

The test results clearly show that the results of comminution depend on the manner of crushing device operation. However, it is also evident that the results of the comminution in each case can be approximated with different effects depending on the function used in calculations. It appears evident that crushing products with an increased content of fines can be described well through the use of Weibull’s formula. The HPGR crushing product obtained for average crushing force turned out to be very well characterized by logistic distribution.

When the feed material was crushed under a lower pressing force, the particle size composition of the obtained product could be adequately described with the use of a log-normal distribution. Detailed characteristics of the approximation in terms of fitting error values are given in Table 3.
The test results clearly show that the results of comminution depend on the material and its properties. The composition of fines can be described using statistical distributions such as the normal, logistic, or Weibull distribution. When the feed material was crushed under base pressing force (15 kN), crushing devices with higher pressing force resulted in more fines than those with lower pressing force. However, the negative relationship between the size of the particle and emission volume (Formula (2)): $E_{TSP} = A \cdot d^B$ is evident in various aspects. One of the most commonly described seems to be the size of particles, type of device, and its productivity in each case, which can be approximated with different effects on the results of comminution.

Values of fitting errors for individual crushing products are given in Table 3.

Figure 3. Fitting results for product 1.

Figure 4. Fitting results for product 2.

Figure 5. Fitting results for product 3.
Table 3. Values of fitting errors for individual crushing products.

| Approximation Function      | Approximation Error |
|-----------------------------|--------------------|
|                            | Product 1 | Product 2 | Product 3 |
| Weibull’s distribution      | 1.67      | 7.78      | 15.25     |
| Log-norm distribution       | 4.59      | 3.79      | 12.92     |
| Logistic distribution       | 10.26     | 17.06     | 2.05      |

5. Environmental Issues

As previously mentioned, negative impacts of mineral processing (and mining in general) are evident in various aspects. One of the most commonly described seems to be the dust pollution. A wide range of investigations in this area can be found in the literature, particularly those concerning the operation of the mining industry. These include investigations into dust emissions directly from the open pit mines or quarries resulting from their routine operation [36–39], emissions from tailing deposits [40] or transport of run-of-mine and aggregate products, including loading and unloading of material [41]. Operations of mechanical processing are characterized by various rates of dust emission, depending on the size of particle, type of device and its productivity, and crushing stage [42]. Typical relationships between the size of handling material and the total amount of dust generated are described by means of exponential function with negative relationships between the size of the particle and emission volume (Formula (2)):

\[ E_{TSP} = \frac{A}{d^B} \]  

where \( E_{TSP} \), total emission of dust particles (mg/m\(^3\)); \( d \), particle size (mm); \( A, B \), coefficients. Selected values of total dust emissions according to different sources are presented in Table 4.

Table 4. The TSP emission of selected devices according to various investigations.

| Processing Stage         | Relative Emission (Primary Crushing = 1) [43] | Total Emission [mg/m\(^3\)] [44] |
|--------------------------|-----------------------------------------------|----------------------------------|
| Primary crushing         | 1                                             | 2.8                              |
| Secondary crushing       | 3 [45]                                        | 3.2                              |
| Tertiary crushing (dry)  | 51 (dry), 2 (wet)                             | 30                               |
| Screening (dry)          | 214                                           | No data                          |
| Screening (wet)          | 12                                            | No data                          |

The dust emission is often described as TSP or total suspended particulates. It denotes particles with a diameter smaller than 20 µm, as larger grains usually fall to the ground quickly and do not constitute the air contaminants.

To overcome this negative impact, many models which determine and predict the volume of dust emissions have been developed. These models consider the general principles [46,47] and are built on empirical data relating to the specific site [48,49]. The formulas were devised on the bases of empirical data, the specific location of a mine, and atmospheric conditions. Parameters characterizing properties of the material (such as moisture and silt contents) were taken into account.

Noise emission is another important factor that affects the life of local society around the mineral processing plant, as well the working conditions at the site [50]. The limitation of this source of pollution seems to be relatively less complex technically than in the case of dust, and typically involves building suitable soundproof and sound-absorbing screens and walls.
6. Summary

Mining and mineral processing are relevant for numerous disciplines and have significant impacts on the operation of various sectors of the economy, especially in raw material management within the metal value chain production. An increasing number of mining companies are facing problems concerning decreases in orebody grades and finer mineralization due to the depletion of deposits. At such a time, the idea of a zero-waste economy gains importance and popularity. These aspects give rise to the development of mineral processing technology and the more efficient utilization of raw material. Efforts are focusing more on the effective utilization of recent techniques in mechanical processing than on the introduction of new feed material treatment technology. This article presented select problems that are especially popular in contemporary mineral processing at the stage of mechanical processing. The increased effectiveness of specific operations can be observed from different scopes, but energy efficiency and useful mineral loss seem to be of major importance. The development of computational techniques and new methods of material analysis will undoubtedly create new opportunities and potential improvements of operation effectiveness.

Not all directions of development have been covered, and the visual analysis and characterization of grained materials are only mentioned. Nevertheless, the results of many investigations and the operational practice of mineral processing plants, show that the stage of the mechanical processing of raw materials preliminarily impacts the potential of effective separation and useful metal recovery.

It is also necessary to highlight major critical aspects and gaps that should be the objects of investigations both in the near future and from a longer-term perspective. There is some consensus that the high energy consumption of comminution processes stands among the most significant issues within the field. However, the problem lies in the more efficient utilization of energy for the breakage and limitation of losses, particularly in fine grinding operations. This is connected to the need for handling the fine mineralized feed material. The scale problem also needs to be solved in electromagnetic grinding, as well as in high-voltage pulse breakage. To some extent, this is also valid for other operations of mechanical processing, such as vibrating mills, SAG and AG grinding, and HPGR. It is also necessary to remember that, when facing the depletion of deposits, (Table 5) it is harder to maintain the overarching aim of mineral processing: achieving a high level of useful mineral recovery.

| Type of Ore       | Unit | Average Grade in 80's | Current Average Grade |
|-------------------|------|-----------------------|-----------------------|
| Copper            | %    | 1.5                   | 0.62                  |
| Lead + Zinc       | %    | 8                     | 6.05                  |
| Nickel            | %    | 4                     | 1                     |
| Gold (surface mining) | g/Mg | 3.5                   | 2                     |

Table 5. World average grades of selected ore minerals [51,52].

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Abbreviations

HPGR  high-pressure grinding rolls
ROM  run-of-mine
CAPEX  capital expenditure
OPEX  operational expenditure
DEM  discrete element method
WOS  Web of Science (database)
PSD  particle size distribution
SEM  scanning electron microscopy
MLA  mineral liberation analyzer
LS  least squares (method)
RRB  Rosin–Rammer–Bennett (distribution)
SAG  semi-autogenous grinding
AG  autogenous grinding

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