Simulated Annealing Decoder for Linear Block Codes

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Abstract: In this study, we introduce a novel soft decoder, the first of its kind, for linear block codes, based on Simulated Annealing algorithm (SA). The main enhancement in our contribution which let our decoder over performs with large gain (about 3 dB at 7×10^-4) the classical SA approach, is to take the most reliable information set of the received codeword as a start solution and also according to this reliability generate neighbor’s solutions. Besides, our algorithm performance is enhanced by reducing search space when we involve the code error correcting capability parameter. The performance of the designed algorithm is investigated through a parameter tuning process and then compared with other various decoding algorithms in terms of decoding performance and algorithmic complexity. Simulation results, show that our algorithm over performs its competitor decoders while keeping minimum computation cost. In fact, our algorithm has large gain over Chase-2 and GAMD, furthermore, it over performs the most efficient and up to date DDGA decoder by 2 dB at 10^-5 for RS codes.

Keywords: Error Correcting Codes, Simulated Annealing, Soft Decoding, Linear Codes, Metaheuristic

Introduction

After the emergence of error correcting codes theory, several researches were proposed to design "good" and practical decoders. The goal of these decoders is to minimize the probability of decoding error. Ideally, the Maximum Likelihood Decoding (MLD) is the best approach, but the decoding process is impracticable for large codes because all code words need to be analyzed. Scientists have designed techniques that convert this problem into graph optimization. These algorithms become impracticable or inefficient for large codes, although the use of long code is important in communication design to approach channel limit as proven by Shannon’s landmark paper (Shannon, 1948). When metaheuristic and probabilistic algorithms became widely used and recognized as efficient approaches for hard optimization problems, in the first instance, hard decoding was coupled with these techniques to design good decoders by making hard decision on the received signal then trying to find the most probable transmitted code using metaheuristic and probabilistic search. Prange (1962) proposed a decoding algorithm using information set, this method was enhanced and used later by several researchers (Lee and Brickell, 1988), (Leon, 1988) and (Stern, 1989). Recently, Genetic Algorithms are widely introduced in this field, actually Cardoso and Arantes (1999) have proposed a hard decoder based on GA, also several papers have been published in the same context (De Bona and Junior, 2015) and (Hoffman et al., 2011). It is also convenient to cite the work of Aylaj and Belkasmi (2015) by proposing a hard decoding based on SA method. However, such model discards all information about the reliability of the received signal and therefore losing accuracy in decoding capability.

In this paradigm, soft decoding decision was the alternative to take benefit from the information reliability directly from demodulation (Fig. 1), it uses the real values and decision uses euclidean distance, hence corrects more errors and reaches high performance, actually it can provide 2dB gain compared with the hard decoding (Proakis, 1995).
Soft-decoding is considered as a NP-hard problem (Berlekamp et al., 1978), in this case classical exhaustive search would not be practicable anymore in large space. In this context, several algorithms were proposed to overcome this handicap. Forney (1966) proposed a pseudo soft decoding system, called “Generalized Minimum Distance Decoding” GMDD. Chase (1972) proposed a soft decoder based on channel measurement information. After the emergence of Artificial Intelligence and metaheuristic methods, several works were published of decoders based on neural networks and Genetic Algorithms (GA). In fact GA seems to give good results which is proved by Maini et al. (1994), then several GA came after such as the SDGA (Azouaoui and Belkasmi, 2012), the AutDAG decoder by (Nouh et al., 2013) and Shakeel (2010) GA-Based Decision Soft decoder. In contrast of the most decoders, other algorithms were proposed using dual code, such as CGAD (Azouaoui et al., 2012a), then recently two algorithms, CGAD-M and CGAD-HSP were proposed based on CGAD (Berkani et al., 2017), also Maini was enhanced to DDGA decoder (Azouaoui et al., 2012b), the SDGA was also extended to DSGA (Azouaoui et al., 2012c). In other hand for LDPC codes GAMD decoder (Scandurra et al., 2006) was proposed. In this spirit, we propose in this paper, a novel soft decoder based on Simulated Annealing Algorithm (SASD).

Simulated Annealing is a physical heating process used in metallurgy. Actually physical systems reach rapidly the equilibrium state (minimum energy) by decreasing slowly the temperature, this behavior is exploited to design an optimization algorithm. In this paper we will apply this technique on linear codes. The remainder of this article will be organized as follows: In section 2, we will introduce the Simulated Annealing Algorithm (SA), then in section 3 we will define the soft decision decoding problem context, then we will explain in details our proposed SA algorithm. In the next section we will investigate the simulation results firstly, by running parameter tuning process to find the best configuration for our decoder, afterward we compare our decoder with the classical SA algorithm and later we will focus on the SASD performances compared to its concurrent decoders. Finally we investigate the influence of the error correcting capability on our algorithm performance. In the last section we present the algorithmic complexity of our algorithm and its competitor. After all, we conclude our paper by summary of this work and the future perspectives.

Materials and Methods

Simulated Annealing

Simulated Annealing algorithm is a metaheuristic method used in optimization problems. It is derived from the process of annealing in metallurgy. In this process a metal is heated and slowly cooled under specific conditions to increase the size of the crystals in the metal and reduce their defects. The heat increases the energy of the atoms while the slow cooling allows to reach equilibrium state with a low energy. Each state of metal represents a different energy level of the system mostly
modeled by Boltzmann distribution (Aarts and Korst, 1989). Heating the system results in exploring different states of the metal. When the system is cooled, the acceptance criteria will lead the changes to convergence. Once the system has cooled, the configuration will represent a state at or close to a global optimum.

This natural process was exploited to design an optimization algorithm used in several research fields. (Kirkpatrick et al., 1983) introduced SA in combinatorial problems, then several researches were published based on this approach (Hajek, 1988). In coding theory, (El Gamal et al., 1987) were among the first who used SA to design good codes. SA was also used to tackle the famous problem of finding the minimum distance of good codes. SA was also used to tackle the most k independent reliable bits, this will initialize the search closer to the global optimum.

The SA algorithm is allowed during execution, with a probabilistic model, to accept solutions that are worse than the current one, this gives the ability to escape from local optimum and explore more the search space. The following pseudo code represents a simple implementation of Simulated Annealing:

```
Parameter Initialization
N_c: number of iterations
T_c: starting temperature
T_f: final temperature
S_0: start solution
T←T_c;
S←S_0;
While (T > T_f)
{
  While (iteration < N_c)
  {
    Pick a random neighbor solution (s_n);
    Evaluate dE = E(s_n) − E(s);
    If dE≤0 then s←s_n;
    else if random(0,1) ≤ Exp(-dE/T) then
      s←s_n;
    end if
    iteration←iteration+1;
  }
  T←cool(T);
}
```

The convergence proof suggests that with long enough cooling period this algorithm converges to the global optimum. In other hand the performance could be improved by using a good neighbor selection strategy, which we will show later in this paper.

**Soft Decision Decoding as an Optimisation Problem**

Let F2 the binary field and note C(n,k,d) a linear code of length n, dimension k and minimum distance d, we note also t the error correcting capability of C. This code can be represented by a k × n matrix G over F2 called generator matrix, a message m can be then encoded as follows:

\[ c = mG \]  

In other side, we define a parity check (n-k) × n matrix noted H which satisfies HG^T = 0, then we define for every vector \( x \in F_2^n \) a syndrome \( S(x) \):

\[ S(x) = xH^T \]  

If the codeword \( x \) contains no error then the syndrome \( S(x) \) is zero.

In our study, the source generates a message \( m \) which is encoded to a codeword \( c = (c_1,c_2,…,c_n) \) using (1), then BPSK-modulated to a signal \( u = (u_1,u_2,…,u_n) \) where:

\[ u_i = 2c_i − 1 \]  

This signal is sent over a Gaussian channel, perturbed by an AWG noise which is modeled by a random n-vector \( n = (n_1,n_2,…,n_n) \), with iid components given by \( n_i \sim N(0, N_0 / 2) \). In the receiver side the received signal is \( r = (r_1,r_2,…,r_n) \) such that \( r = u + n \). The likelihood probability is given by:

\[ f_{r,u} = \frac{1}{(\pi N_0)^{n/2}} \exp\left(\sum_{i=1}^{n} \frac{-(r_i - u_i)^2}{N_0}\right) \]  

Clearly MLD can be formally expressed as an optimization problem as follows:

Given a received word \( r \), what is the codeword \( c \in C \) which maximizes the likelihood probability \( f_{r,u} \)?

\[ \min\left\{ \sum_{i=1}^{n} (r_i - u_i)^2 / c \in C \right\} \]  

Consequently, this problem is reduced to finding the minimum euclidean distance to the received word \( r \) overall codewords \( c \in C \), this optimization has \( n \) variables out of which only \( k \) form a generator base, hence we could restrict search space to \( k \) variables, in preference we select the most \( k \) independent reliable bits, this will initialize the search closer to the global optimum.

**Proposed Algorithm**

We conceptualize the Euclidean distance between the received word and a codeword as the energy level and the state as the \( k \) bits vector, then the lowest energy state corresponds to the closest code word to the received word. The mapping between physical Simulated Annealing and our algorithm is summarized in the Table 1.
When receiving a word \( r = (r_1, r_2, ..., r_n) \) our algorithm starts processing as follows:

1. Make a hard decision \( \tilde{r} = (\tilde{r}_1, \tilde{r}_2, ..., \tilde{r}_n) \) of received signal \( r = (r_1, r_2, ..., r_n) \):
   \[
   \tilde{r}_i = \begin{cases} 0, & r_i < 0 \\ 1, & r_i \geq 0 \end{cases}
   \tag{6}
   \]

2. Calculate the syndrome \( S(\tilde{r}) = \tilde{r}H^T \), if \( S(\tilde{r}) = 0 \), then \( \tilde{r} \) is estimated as the sent codeword and stop, otherwise continue

3. Sort the sequences \( r = (r_1, r_2, ..., r_n) \) in decreasing order based on reliability \( \langle r | \geq | r_{r,1} \rangle \) to obtain new sequences \( r' = (r'_1, r'_2, ..., r'_n) \), let’s note \( \pi \) the permutation \( r' = \pi(r) \), we apply \( \pi \) to \( G \) to obtain \( G' \). The most \( k \) reliable \( (r'_1, r'_2, ..., r'_n) \), will be the start solution of our algorithm, in fact this solution is estimated to be very close to the optimum solution, because if the received signal contains errors it’s probable to happen in the \((n-k)\) least reliable bits

4. Apply Gaussian elimination to \( G' \) to obtain a systematic matrix

5. We apply the SASD algorithm to obtain the best close word to the received signal and in consequence the estimated sent codeword \( c' \). This algorithm is detailed afterwards

6. The code \( c' \) is related to the \( G' \) matrix, thus our estimated transmitted codeword is then:
   \[
   \hat{c} = \pi^{-1}(c')
   \tag{7}
   \]

The SASD algorithm which is used to estimate the codeword will start from an initial state represented by a vector \( s \in F_2^n \) and uses the euclidean distance as objective function to evaluate the quality of the solution which corresponds to the energy of the system and as we know the SA algorithm tries to converge toward a state with minimum energy, which is equivalent in our space to the closest codeword to the received word. In other side, in contrast with classical SA which generates neighbor’s solution by random bit flipping, our algorithm takes again advantage of information reliability of the start solution vector \( \tilde{r} = (\tilde{r}_1, \tilde{r}_2, ..., \tilde{r}_n) \) the hard decision of sequences \( r' = (r'_1, r'_2, ..., r'_n) \), to generate next solution as follows:

| Table 1: Mapping between physical Simulated Annealing and our algorithm |
|---------------------------------------------------------------|
| Physical SA | SASD |
| State | k-bit vector |
| Energy | Euclidean distance between the received word and a codeword |
| Final State | Decoded word |

In the end The SASD algorithm could be expressed in the following pseudo code:

```plaintext
Parameter Initialization
Ni: number of iterations
Ts: starting temperature
Tf: final temperature
a: cooling ratio
S0: start solution
T = Ts
S ← S0

While (T > Tf)
{
    While (iteration < Ni)
    {
        s ← pick_neighbor();
        Evaluate dE = E(s) - E(s);
        Err = EvaluateCorrectedError();
        if err < t then break;
        if dE ≤ 0 then s ← s;
        else if random(0,1) ≤ Exp(-dE/T)
            then s ← s;
        end if
        iteration ← iteration + 1
    }
    T ← a * T;
}
```

For every \( s = (s_1, s_2, ..., s_k) \) let’s note \( c = (c_1, c_2, ..., c_n) \) the code word of \( s \) using (1). The energy \( E(s) \) of \( s = (s_1, s_2, ..., s_k) \) is expressed as follows:

\[
E(s) = \sum_{i=1}^{n} (c_i - (2c_i - 1))^2
\tag{8}
\]
Results and Discussion

SASD Parameter Tuning

In order to select the most suitable set of parameters \( \{\alpha, N_i, T_s, T_f\} \) we may choose some probabilistic models for estimation (MacKay, 2003). However in our case we assume that our parameters are independent and for this reason, we run several simulations of performance which is the Bit Error (BER) expressed as function of Signal to Noise Ratio (SNR), with different SASD parameters values. For every parameter optimization we set the remaining to default values according to the Table 2.

Parameter \( N_i \)

The number of iterations setting is often problem specific and estimated based on experiments. The simulations from the above Fig. 2, shows that the best performance is almost achieved when \( N_i = 250 \).

Parameter \( \alpha \)

From the Fig. 3 \( \alpha = 0.95 \), is almost the best choice for cooling ratio. In practice, slow cooling mechanism allows low euclidean codewords to be discovered and exploited.

Parameter \( T_s \)

Based on simulation results of Fig. 4, the best value for initial temperature \( T_s \) is 0.2. This parameter could impact accuracy, many methods have been proposed to estimate \( T_s \) (Ben-Ameur, 2004).

Parameter \( T_f \)

Intuitively, freezing temperature is used in physics to achieve equilibrium, this finding is confirmed by our simulations in Fig. 5, where we observe that the best performance is reached for almost all SNR values at the slowest temperature \( T_f = 0.001 \).

Comparison of the Proposed Algorithm Versus Classical Version

The proposed algorithm, SASD, was compared against the classical SA. The simulations where made with default parameters outlined in Table 2. The performances are given in terms of BER (bit error rate) as a function of Signal to Noise Ratio Eb/N0 (SNR).

| Parameter          | Value         |
|--------------------|---------------|
| Default code       | BCH(63,45,7)  |
| Channel            | AWGN          |
| Modulation         | BPSK          |
| Minimum number of bit error | 200          |
| Minimum number of blocs | 1000          |
| \( N_i \)          | 250           |
| \( T_s \)          | 0.2           |
| \( T_f \)          | 0.001         |
| \( \alpha \)       | 0.95          |

Table 2: Parameters setting

![Fig. 2: Number of Iteration variation](image-url)
Fig. 3: Variation of parameter $\alpha$

Fig. 4: Variation of parameter $T_s$
Fig. 5: Variation of parameter $T_f$

Fig. 6: Code BCH(31,21,5)
Fig. 7: Code BCH(63, 45, 7)

Fig. 8: Code RS(60, 28, 9)
The Fig. 6 and 7 compare the performances of SASD and classical SA for 2 BCH codes. We notice the superiority of our algorithm over the classical algorithm. In fact at 10^{-4} we have a gain of 2 dB using SASD for BCH (63,45,7) and 1dB for BCH(31,21,5).

The Fig. 8 presents the performances of SASD and classical SA for RS(60,28,9) code. According to this figure, we remark that our algorithm outperforms the classical decoder by 3 dB at 10^{-3}.

In the Fig. 9, our decoder presents a gain of about 2 dB at 10^{-3} compared to classical SA.

For the LDPC (60,30), the Fig. 10, shows that our algorithm outperforms classical SA. According to this figure, we remark that we have about 2.5 dB gain at 10^{-3}.

Comparison of the Proposed Algorithm Versus other Decoders

In this subsection, we compare our SASD decoder with some known and efficient decoders: Chase-2, OSD-1 (Fossorier and Lin, 1995), Maini, SDGA, SIHO, (Chana et al., 2011), DDGA, AutDAG, cGA-HP, cGA-M, CGAD and GAMD. For this purpose we run our simulations on several codes as a base of comparison, these simulations were made with default parameters outlined in Table 2. The performances are given in terms of BER (bit error rate) as a function of SNR (Signal to Noise Ratio Eb/N0).

The Fig. 11, shows that our algorithm performs better than AutDAG, SDGA, cGA-HSP, cGA-M and slightly the most efficient decoder DDGA for medium and low noise level.

In Fig. 12, the SASD has better performance than Chase-2, OSD-1, SDGA and SIHO for medium and low noise level. The Maini decoder is more efficient than our decoder for high noise level, however starting from 3.5dB SASD has a little edge over Maini.

The performance of SASD, Chase-2, CGAD, Maini and DDGA algorithms, for the code BCH (31,21,5) code, is shown in Fig. 13.

We notice that our algorithm has almost same performance as Maini and DDGA.

The Fig. 14 compares the performance of our decoder with other decoders for BCH(63,51,5) code. From this figure, we see that our algorithm is the most efficient. Besides at 10^{-5} it has a gain of 1dB over Chase-2.

Simulations of the non-binary RS(15,7,9), in Fig. 15, reveal the decoding power of SASD over the most efficient decoder DDGA, in fact at 10^{-5} we have a gain of 1dB, in other hand at 10^{-3} we gain about 2.5dB over SDGA and CGA-M. In Fig. 15, our algorithm is definitely more efficient than Chase-2, CGAD and cGA-HSP. In fact at 10^{-3} our decoder has a gain of 3dB over Chase-2 and at 5. 10^{-3} using SAD we gain about 2dB compared to cGA-HSP.
Fig. 10: Code LDPC(60, 30)

Fig. 11: Code BCH (63, 45, 7)
Fig. 12: Code BCH(63,45)

Fig. 13: Code BCH(31,21,5)
Fig. 14: Code BCH(63,51,5)

Fig. 15: Code RS(15,7,9)
Fig. 16: Code RS(15,7,9)

Fig. 17: Code LDPC(60,30)
The above Fig. 17, shows that for the above LDPC, SASD is applicable for non-cyclic codes and is indeed better than GAMD, actually we can gain about 1 dB by using SASD.

The Fig. 18 compares the performances of SASD, SDGA and the classical BPSK decoding for the non-cyclic RM(32,16) code. We notice the superiority of SASD over the other algorithms. Using our algorithm at 10^-4, we have a gain of 0.5 dB over SDGA and about 3.5 dB over BPSK decoding.

Influence of Error Correcting Capability

In order to enhance our algorithm we used the code error correcting capability t as a stop criterion, we will compare in this section the influence of the parameter t, below the algorithm without involving this enhancement:

Parameter Initialization

NI: number of iterations
Ts: starting temperature
Tf: final temperature
a: cooling ratio
S_0: start solution

```
T ← Ts
S ← S_0
While (T > Tf)
    { 
        While (iteration < Ni)
            { 
                s_n ← pick_neighbor();
                Evaluate dE = E(s_n) − E(s);
                If dE ≤ 0 then 
                    s ← s_n;
                else if random(0,1) ≤ Exp(-dE/T) then 
                    s ← s_n;
                end if
                iteration ← iteration + 1
            }
        T ← a*T;
    }
```

To measure the gain we get from introducing the parameter t we made simulations of the number of explored codewords for both algorithm (with t and without t) in different SNR values, the Fig. 19 summarizes the results.

We can notice that for small and medium noise level, the search space is greatly reduced for example for SNR = 4, we reduce our space by 88%.
Complexity Analysis

The Table 3 recapitulates our algorithm complexity with the concurrent decoders.

Let a linear code $C(n,k)$ and $t$ be the error correction capability of the code $C$, $N_i$ be the population size which is the total number of individuals in the population, $N_g$ be the number of generations and let $N_{g_i}$ be the number of generations of local search for Genetic Algorithm, while $N_{g_{ch}}$ represents the number of iterations for SASD, $N_i$ is a constant which represents the number of generations needed for SASD to reach final temperature $T_f$ starting from $T_i$. $T_f$ a parameter used in CGAD called the average number of generations. The parameter $p$ in Chana decoder is the number of test sequences.

The Chase-2 and SDGA algorithms increase exponentially with $t$ and OSD increases with $p$, hence for code with large error capability they have the worst complexity. However in terms of code sizes, SASD, DDGA, CGAD, Maini and AutDAG algorithms, the complexity is linear either in $k$ or $n$. OSD-1, SDGA, Chana and Chase-2 have poor performance in terms of $n$.

Conclusion

In this study, we have proposed a novel Simulated Annealing based algorithm for soft decision decoding, as far as we know our decoder is the first soft algorithm based on SA. Then we focus on parameter tuning throw several experiments and later show the superiority of our proposed algorithm over the classical SA and over the most famous and up to date decoders, in fact it beats the DDGA by 2dB at 10-5. Furthermore we investigate the enhancement introduced by the error correcting capability parameter in our decoder and we show that we can reduce the search space by 88% for high noise level. Besides, the main advantage of the SASD is that it take advantage of the information reliability of the received word to start search and to generate neighbor solutions, in other side our decoder can be used for non-cyclic and non-binary codes without any complex change. We also compare the algorithmic complexity of our decoder with its concurrent.

The obtained results let us hope to implement this decoder for dual code and try to find other neighbor’s search strategies to enhance performance.

Author’s Contributions

Lahcen Niharmine, Hicham Bouzkraoui and Ahmed Azouaoui: Contribute on the implementation of the decoder SASD.

Youssef Hadi: Review and correct the article research.

Ethics

I testify that my research paper submitted to the Journal of Computer Science, title: Simulated Annealing Decoder for Linear Block Codes not been published in whole or in part elsewhere. This research project was conducted with full compliance of research ethics norms of Ibn Tofail University, Kenitra, Morocco.

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1189