Double pion photoproduction off nuclei - are there effects beyond final-state interaction?

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Abstract

Photoproduction of \( \pi^0 \pi^0 \) and \( \pi^0 \pi^\pm \) pairs from nuclei has been measured over a wide mass range (\( ^2\text{H}, ^7\text{Li}, ^{12}\text{C}, ^{40}\text{Ca}, \text{and } ^{208}\text{Pb} \)) for photon energies from threshold to 600 MeV. The experiments were performed at the MAMI accelerator in Mainz, using the Glasgow photon tagging spectrometer and a 4\( \pi \) electromagnetic calorimeter consisting of the Crystal Ball and TAPS detectors. A shift of the pion-pion invariant mass spectra for heavy nuclei to small invariant masses has been observed for \( \pi^0 \) pairs but also for the mixed-charge pairs. The precise results allow for the first time a model-independent analysis of the influence of pion final-state interactions. The corresponding effects are found to be large and must be carefully considered in the search for possible in-medium modifications of the \( \sigma \)-meson. Results from a transport model calculation reproduce the shape of the invariant-mass distributions for the mixed-charge pairs better than for the neutral pairs, but also for the latter differences between model results and experiment are not large, leaving not much room for \( \sigma \)-in-medium modification.

1. Introduction

The generation of the mass of hadrons composed of light quarks is a central problem in quantum chromodynam-
ics (QCD), the theory of the strong interaction. Unlike any other composite system, hadrons are built out of constituents with masses which are negligible compared to their total mass which is generated by dynamical effects. A central role is played by the spontaneous breaking of chiral symmetry, a fundamental symmetry of QCD. Without this symmetry breaking, hadrons would appear as mass degenerate parity doublets. However, in the spectrum of free particles large mass splitting is observed between chiral partners, for baryons and for mesons. The order parameter of the symmetry breaking, the quark condensate, is expected to be density and temperature dependent so that the symmetry could be at least partially restored for hadrons embedded in nuclear matter. Already in 1991 Brown and Rho [1] suggested scaling laws for hadron in-medium masses: and shortly after, Lutz, Klint, and Weise [2] discussed in-medium properties of mesons in the framework of the Nambu-Jona-Lasinio (NJL) model. A recent overview of theory and experiment is given in [3]; results from photon-induced reactions are summarized in [4]. Although originally in-medium effects were mainly discussed in connection with heavy ion collisions, they should be also observable at normal nuclear density [2] in systems that can be more easily interpreted than the strongly time-dependent density and temperature variations in heavy ion collisions.

Among such effects is the mass-shift of the $\sigma$-meson in normal dense nuclear matter. This scalar $J^P = 0^+$, isoscalar $I = 0$ state is mostly regarded as the chiral partner of the $J^P = 0^-, I = 1$ pion [5–7]. However, due to its un-conventionally large width (mass between 400 - 550 MeV, width 400 - 700 MeV [8]), in some models it is treated as a correlated state of two pions (respectively four quarks) rather than a quark-antiquark state [9–12]. The mass split between the $\sigma$ and the pion in vacuum is large. However, predictions from different models [5,10] indicated that already at normal nuclear matter density $\rho_0$ the mass of the $\sigma$ should drop by $\approx 200$ MeV [5,10], while the pion, which is protected by its Goldstone boson nature, should almost be unaffected. The strong coupling of the $\sigma$ to scalar, isoscalar pion pairs should lead to a modification of the invariant-mass distribution of such pairs in nuclear matter. This effect is predicted by different model studies independent of the assumed nature of the $\sigma$ [6,7,9–11,13]. In models, in which the $\sigma$ is not treated as a quark-antiquark state, the corresponding effect comes from an in-medium modification of pion-pion final state interaction for scalar, isoscalar pion pairs. This effect must not be confused with the final state interaction of individual pions with nuclear matter by re-absorption and re-emission processes.

This prediction has been experimentally tested with pion- and photon-induced reactions. Pion induced reactions were studied by the CHAOS collaboration [14–18], which observed a mass shift for isoscalar $\pi^+\pi^-$ pairs in heavy nuclei but no effect for the like-sign $\pi^+\pi^+$ pairs where the $\sigma$ cannot contribute. The experiment had only a limited detector acceptance, which complicated the interpretation of the results. A similar effect was observed for the $\pi^-\Lambda \to A\pi^0\pi^0$ reaction by the Crystal Ball Collaboration at BNL [19] which, however, could not measure an isovector channel for comparison. Pion-induced reactions have the disadvantage that due to the large absorption cross section only the nuclear surface is probed.

Photons can probe the entire volume of nuclei. Although also in this case final-state interaction (FSI) effects cannot be avoided, they can be studied in a systematic way because they depend strongly on the kinetic energy of the produced pions [20]. Nuclei are almost transparent for low-energy pions, which means that invariant-mass distributions of pion pairs produced close to the production threshold are much less affected by FSI than at higher energies. Photon induced production of pion pairs off nuclei has been previously measured with the TAPS detector at MAMI [21,22]. These experiments found for heavy nuclei a systematic shift of the invariant mass of $\pi^0\pi^0$ pairs towards small values while the distributions for mixed-charge pairs $\pi^0\pi^\pm$ were much less effected. However, as discussed in [22] the spectra were reproduced by the results from calculations with the Boltzmann-Uehling-Uhlenbeck (BUU) transport model [23]. This model treated the pion-nucleus FSI effects in great detail, but did not include any explicit in-medium modification of $\pi^0\pi^0$ pairs. However, the model results had also non-negligible systematic uncertainties, mainly from the input for the elementary reaction cross sections.

A more systematic study was limited by the statistical quality of the data and the range of nuclear masses investigated. As discussed above, FSI effects are minimized close to the production threshold; but the production cross sections are small. The lightest nucleus included in the previous study was $^{12}$C. Invariant-mass distributions for the elementary processes off the (quasi)-free nucleon (see [24] for an overview) have been studied previously for the $p\pi^0\pi^0$ [25–27], the $n\pi^0\pi^+$ [28], and $p\pi^0\pi^-$ [29] final states. Data for $\gamma d \to X\pi^0\pi^0$ had low statistical quality in the threshold region [30] and no data were available for $\gamma d \to X\pi^0\pi^\pm$.

The present experiment therefore aimed at a precise measurement of pion-pion invariant-mass distributions for the $\pi^0\pi^0$ and $\pi^0\pi^\pm$ final states at low incident photon energies over a large range of nuclear masses, including $^2$H, $^7$Li, $^{12}$C, $^{40}$Ca, and $^{208}$Pb targets. Such data are needed to separate the FSI effects from non-trivial in-medium modifications of the double pion channels.

2. Experimental setup

The experimental setup is described in [31] where the data from the $^7$Li target have been analyzed for other meson production reactions. The measurement was performed at the tagged photon beam of the Mainz MAMI accelerator [32,33]. The primary electron beam of 883 MeV produced bremsstrahlung in a copper radiator of 10 $\mu$m thickness. The photons were tagged with the Glasgow magnetic spectrometer [34]. Four solid-state targets (thicknesses 5.4 cm (Li), 1.5 cm (C), 1 cm (Ca), 0.05 cm (Pb))
and a liquid-deuterium target (thickness 4.8 cm, 0.6% of radiation length) were used. The thickness of the solid-state targets was chosen such that they were comparable in units of the radiation lengths of the materials (from 3.5% for lithium to 9% for lead). For the measurement with the lead target a lower beam energy was used (645 MeV) in order to enhance the statistical quality of the data in the threshold region. In this Letter, we therefore summarize only the results for incident photon energies below 600 MeV. The reaction products were detected with an almost 4π-covering electromagnetic calorimeter assembled from the Crystal Ball (CB) [35] and TAPS [36] detectors. The targets were mounted in the center of the Crystal Ball. A Particle Identification Detector (PID) [37] was mounted around the targets in cylindrical geometry for identification of charged particles. For the same purpose the TAPS detector was equipped with individual plastic detectors in front of each BaF₂ module.

The trigger conditions were chosen relatively open in order to minimize systematic uncertainties. The Crystal Ball and TAPS were subdivided into logical sectors, TAPS into 8×64 modules arranged in a pizza-like geometry and the Crystal Ball into 45 rectangles. Events were accepted when at least two sectors of the calorimeter were hit and the total analog sum energy in the Crystal Ball was above 50 MeV. The charged pion was not used in the trigger. Events where the decay photons of the neutral pions had not satisfied the trigger condition were removed in the off-line analysis because of the systematic uncertainties in the simulation of the trigger efficiency for charged pions.

3. Data analysis

The analysis of data measured with the above setup is discussed for different final states in [31,38,39]. The specific analysis steps for \( \pi^0\pi^0 \) and \( \pi^0\pi^\pm \) production off nuclear targets are described in detail for the previous measurements with the TAPS detector [22]. The main improvements of the present experiment compared to the previous measurements [21,22] are the almost 4π coverage of the solid angle and the use of the PID for the identification of charged pions via the \( \Delta E - E \) method.

The first step of the analysis was the assignment of hits to photons, charged pions, protons, and neutrons. The identification of hits in TAPS (see [22] for details) used the information from the plastic scintillators in front of the TAPS crystals and a pulse-shape analysis (PSA), using the narrow- and wide-gate energy integration of the BaF₂ signals for the separation of photons from nucleons. A time-of-flight (ToF) versus energy analysis showed the characteristic bands for photons, charged pions, and nucleons. As discussed in [22], at forward angles the charged-pion band in TAPS is contaminated with protons. Therefore, charged pions were not accepted in TAPS (this excluded charged pions with polar angles \( \Theta_{\pi} < 20^\circ \) from the analysis).

In the Crystal Ball [38,39], charged hadrons were identified via their \( \Delta E - E \) spectra constructed from the energy loss \( \Delta E \) in the PID and the energy deposition in the Crystal Ball. This analysis also used the correlation between the azimuthal angles of the hits in the PID and the CB. A typical \( \Delta E - E \) spectrum shown in Fig. 1, left hand side, demonstrates the separation of charged pions from protons. In the CB, neutrons cannot be distinguished from photons, as opposed to in TAPS. Therefore, neutral hits in the CB were accepted as candidates for photons and for neutrons, while neutral hits in TAPS were separated at this stage into disjoint samples of photons and neutrons through PSA and ToF-versus-energy.

Events were then assigned to the \( \pi^0\pi^0 \) and \( \pi^0\pi^\pm \) final states. Accepted were events with four photons (for the \( 2\pi^0 \) final state) and events with two photons and one charged pion (for the \( \pi^0\pi^\pm \) final state). Detection of recoil nucleons was allowed but not required and after identification, recoil nucleons were ignored in the further analysis. Consequently, three different sub-classes of events were accepted for both reactions. For the double neutral channel, these were: events with exactly four photon candidates (50%); events with four photons and one proton (32%); and events with four photons and one neutron candidate (18%). Similarly, for \( \pi^0\pi^\pm \) pairs, events with: exactly two photon candidates and exactly one candidate for a charged pion in the Crystal Ball (59%); events with an additional proton (28%); and events with an additional candidate for a neutron (22%) were accepted.

In the next step the invariant mass of the pairs of photon candidates was constructed. For events with a neutron candidate in the Crystal Ball (which is indistinguishable from a photon), all possible pion combinations of neutral hits were tested and the ‘best’ combination was selected using a \( \chi^2 \)-test minimizing

\[
\chi^2 = \sum_{i=1}^{n_{\gamma\gamma}} \left( \frac{m_{\gamma\gamma} - m_{\gamma\gamma,i}}{\Delta m_{\gamma\gamma,i}} \right)^2,
\]

where \( m_{\pi\pi} \) is the nominal pion mass, and \( m_{\gamma\gamma,i}, \Delta m_{\gamma\gamma,i} \) are invariant mass and uncertainty of all possible combinations of ‘photon’ pairs. The unpaired neutral hit, not assigned to be a pion decay photon, was then taken as neutron and thereafter disregarded. The resulting two-dimensional

![Fig. 1. Left hand side: Energy deposition in CB versus PID. Charged pions are separated from protons and low energy electrons (data from Li target). Right hand side: Two-dimensional distribution (data from Li-target) of the invariant masses from the \( \pi^0\pi^0 \) channel for incident photon energies between 400 - 460 MeV (only ‘best’ combinations, see text).](image-url)
spectrum of pion-invariant masses for double $\pi^0$ production is shown in Fig. 1, right hand side. Events with both invariant masses in the range 110 - 160 MeV were selected for further analysis. The small combinatorial background underneath the peak, was extrapolated in a side-bin analysis and subtracted. Subsequently, the nominal mass of the pion $m_{\pi}$, was used to improve the resolution as in [22,39] by replacing the measured photon energies $E$ by

$$E'_{1,2} = E_{1,2} \frac{m_{\pi^0}}{m_{\gamma}} ,$$

where $m_{\gamma}$ is the invariant mass corresponding to the measured photon four vectors. This data sample was tested for residual background with missing mass spectra (the recoil nucleon was treated as a missing particle even if it was detected):

$$\Delta m_s = |P_\gamma + P_N - P_{\pi^+} - P_{\pi^-} - m_N| ,$$

where $P_\gamma$ and $P_N$ are the four momenta of the incident photon and nucleon (the latter assumed at rest) and $P_{\pi_i}$, $i = 1, 2$ the four momenta of the two pions. The corresponding spectra are shown in Fig. 2, bottom row. They demonstrate the cleanliness of the signal and the excellent agreement between measured data and Monte Carlo simulations.

![Fig. 2. Missing mass spectra for $E_\gamma$ between 400 MeV and 500 MeV for $^2H$, $^7Li$, and $^{40}Ca$. Top row: missing mass for $\pi^0\pi^\pm$ candidates for the background assumption of the $\pi^0p$ final state. Background from single $\pi^0$ production with protons misidentified as charged pions peaks around zero. Dashed lines indicate cut for further analysis. Middle row: missing mass for $\pi^0\pi^\pm$ candidates for the assumption of the $\pi^0\pi^\pm$ final state. Signal around zero. (Blue) triangles: raw spectra, black dots: after cut on $\Delta m_b$. Bottom row: missing mass for the $\pi^0\bar{\pi}^0$ hypothesis for double neutral meson pairs. (Red) solid lines: simulated line shape of signal.](image)

For the mixed-charge channel, the invariant-mass spectra were fitted with the simulated line-shape of the pion peak and a polynomial background (second degree polynomial). Some background arises from the quasi-free $\gamma p \rightarrow p\pi^0$ reaction from protons which contaminate the pion band in the $E - E$ spectra. The fraction of protons that intrude is small, but the cross section for single $\pi^0$ production can be larger than for $\pi^0\pi^\pm$ production by more than two orders of magnitude. The most efficient way to remove this background uses the missing mass calculated for the hypothesis of the $\gamma p \rightarrow p\pi^0$ reaction (see [22,39] for details), i.e. it is assumed that the 'charged pion' is a misidentified proton:

$$\Delta m_b = |P_\gamma + P_N - P_{\pi^0} - m_N| ,$$

with the same notation as in Eq. (3). Typical spectra are shown in Fig. 2. For the deuteron target background peak and double pion production are separated, for the heavier nuclei, due to the larger momenta of the bound nucleons and FSI, the background is only visible as a shoulder on the tail of the signal peak. Only events with $\Delta m_b > 140$ MeV have been accepted. The center row of Fig. 2 shows the missing mass $\Delta m_s$ (see Eq. (3)) calculated under the assumption of quasi-free $\pi^0\pi^\pm$ production. The (blue) triangles represent the raw spectra and the (black) dots the events that passed the above $\Delta m_b$ cut. The latter agree well with the simulated line-shape ((red) lines). Residual background was removed with the condition $\Delta m_s > -100$ MeV.

Charged pions may deposit more than their kinetic energy in the detector. When they are stopped, they may interact with nuclei or decay and deposit some fraction of their rest mass as energy (see [22] for details). The additional energy deposition was taken into account by a correction derived from the comparison of kinetic and deposited energies of charged pions in the Monte Carlo simulations. The charged pion reconstruction was tested as in [22] with an analysis of the position and shape of the invariant mass peak from the $\eta \rightarrow \pi^0\pi^+\pi^-$ decay. The results for data and Monte Carlo simulation were in good agreement, and the peak position agreed with the nominal mass of the $\eta$-meson. Since charged pion detection enters twice in this analysis, this test is very sensitive.

Total cross sections were extracted from the measured yields, the target surface densities, the photon flux, and the simulated detection efficiencies. Systematic uncertainties from the targets were in the range from 1% to 3%. The photon flux was determined from the counting of the deflected electrons in the tagger focal plane and the tagging efficiency, i.e. the fraction of correlated photons passing the collimator (typically $\approx 50\%$). The systematic uncertainty was estimated at the 5% level. Systematic uncertainties from the cuts applied for reaction identification and possible residual backgrounds were estimated at $\approx 3\%$ for $\pi^0\pi^0$ and $\approx 5\%$ (for $E_\gamma = 500$ MeV) to 10% (for $E_\gamma = 400$ MeV) for $\pi^0\pi^\pm$. The detection efficiency was simulated with the Geant4 program package [40]. The simulations were based on the event generator used for the previous experiments [21,22], which incorporates Fermi-smearing and FSI processes in a Glauber-type approximation.
The efficiency corrections were applied to the data as a function of incident photon energy and invariant mass of the pion pairs. In this way, the influence of the properties of the event generator on the results is minimized. Depending on incident photon energy, pion-pion invariant mass, and target, typical values of the detection efficiency were in the range 30% - 70% for $\pi^0\pi^0$ pairs and between 5% - 40% for the $\pi^0\pi^\pm$ channel. Total cross sections were extracted by integration of the invariant mass distributions. We estimate a systematic uncertainty of the detection efficiency of $\approx 10\%$ for neutral pairs and $\approx 20\%$ for the mixed charge pairs. It is larger for the latter because their detection efficiency depends strongly on the kinetic energy of the charged pions (see [39] for details). The total systematic uncertainties are indicated in Fig. 3 as shaded bands (error bars in all figures represent statistical uncertainties). One should, however, keep in mind that for the comparisons of reaction channels and the results for different nuclei, systematic uncertainties cancel to a large extent.

4. Results

Invariant-mass distributions of the pion pairs for incident photon energies between 400 MeV - 460 MeV are summarized in Fig. 3. The distributions measured for pion pairs produced off quasi-free nucleons from the deuteron differ in shape and magnitude from those measured off free protons (Fig. 3, top row). This may be partly attributed to Fermi-smearing, but includes also differences in the elementary cross sections for protons and neutrons. This is important for comparisons of the nuclear data to model results, which have to rely on experimental input for the elementary cross sections.

The data for carbon and lead from Messchendorp et al. [21] are in reasonable agreement with the present results for the neutral pairs; but not for the mixed-charge channel. Agreement between the $\pi^0\pi^\pm$ data for calcium from Bloch et al. [22] and the present results is much better (see Fig. 7). It had already been noticed that the $\pi^0\pi^\pm$ data from references [21,22] are probably in conflict because the mass dependence for the chain carbon - calcium - lead would have been very unnatural (the magnitude of the calcium cross section normalized by mass number had been larger than both the carbon and lead data, but one would have expected it in between of them). The present measurement favors the previous results from Bloch et al. [22] with which they agree within systematic uncertainties.

Comparison of the invariant-mass distributions in Fig. 3 shows, that for the $\pi^0\pi^0$ and the $\pi^0\pi^\pm$ pairs, strength shifts to small invariant masses for increasing mass of the nucleus. This general trend is certainly not related to properties of the $\sigma$ meson, which does not couple to the mixed-charge channel. The effect can be studied in more detail with the help of the composite ratios defined by

$$C_{\pi\pi}(A_1,A_2) = \frac{(d\sigma(A_1)/dM)/\sigma(A_1)}{(d\sigma(A_2)/dM)/\sigma(A_2)}$$

where $d\sigma(A_i)/dM$ are the invariant mass distributions and $\sigma(A_i)$ the total production cross sections for two nuclei with mass numbers $A_1$ and $A_2$. Results for incident-photon energies from 400 MeV - 460 MeV are summarized in Fig. 4. They demonstrate that, at least in this energy range, the behavior of the invariant-mass distributions is almost identical for both isospin states, so that the dominant effect is most likely due to FSI of the pions with the nucleus. Previous results [21] for the composite ratio of carbon and lead indicated a stronger enhancement at low invariant masses for neutral pion pairs than for the mixed-charge pairs. However, comparison to the present invariant-mass distributions (see Fig. 3) suggests that this was due to statistical fluctuations, in particular in the lead data. Using the lighter nuclei (deuteron and $^7$Li) as reference, the low-mass enhancement becomes larger, but in the same way for neutral and mixed-charge pairs.

An estimate of how important FSI effects are for the pions can be deduced from the scaling of the cross sections with nuclear mass number $A$. Total cross sections as a function of incident photon energy, scaled by the mass number $A$, are shown for both isospin states in the inserts of Fig. 5. The scaling changes from threshold to higher incident photon energies. This behavior can be parameterized with the scaling coefficient $\alpha$ from

![Fig. 3. Invariant mass distributions of pion pairs normalized to the nuclear mass numbers for incident photon energies 400 - 460 MeV. From top to bottom for deuteron (and proton [39], open triangles), lithium, carbon, calcium, and lead targets. Open (blue) squares: previous data from [21]. Shaded (green) bands: systematic uncertainties. (Red) solid curves: GiBUU results [41], dashed: arbitrary rescaled for easier comparison of the shapes.](image-url)
energies below 100 MeV, which may excite the ∆-resonance. In any effects due to in-medium modification of the σ-meson can only be studied on top of the FSI effects, which requires detailed model descriptions of FSI. An efficient way to treat these ‘trivial’ nuclear effects are transport-theoretical approaches [41]. We compare typical invariant-mass distributions to the results of the Giessen Boltzmann-Uehling-Uhlenbeck (GiBUU) model [41] in Figs. 3 and 7. On an absolute scale, the production cross section for the neutral pairs, (blue) squares: mixed-charge pairs (symbol s slightly displaced for better readability) Inserts: total cross sections scaled by A as a function of incident photon energy.

Two effects are important. Inelastic scattering tends to decrease the kinetic energy of the pions and their mean-free path increases with decreasing energy.

Any effects due to in-medium modification of the σ-meson can only be studied on top of the FSI effects, which requires detailed model descriptions of FSI. An efficient way to treat these ‘trivial’ nuclear effects are transport-theoretical approaches [41]. We compare typical invariant-mass distributions to the results of the Giessen Boltzmann-Uehling-Uhlenbeck (GiBUU) model [41] in Figs. 3 and 7. On an absolute scale, the production cross section for the neutral pairs, (blue) squares: mixed-charge pairs (symbol s slightly displaced for better readability) Inserts: total cross sections scaled by A as a function of incident photon energy.

Fig. 5. Scaling behavior of total cross sections. Main figure: Scaling coefficient α as a function of incident photon energy. (Red) dots: neutral pairs, (blue) squares: mixed-charge pairs (symbols slightly displaced for better readability) Inserts: total cross sections scaled by A as a function of incident photon energy.
5. Summary and Conclusions

Precise results have been obtained for the invariant-mass distributions of $\pi^0\pi^0$ and $\pi^0\pi^\pm$ pairs produced from deuterium, Li, C, Ca, and Pb targets from production threshold up to incident photon energies of 600 MeV. A pronounced shift of strength towards small invariant masses as a function of the nuclear mass number is observed for both final states. This effect increases with increasing beam energy and can be related to re-absorption and re-emission processes of the pions in the nuclei. An analysis of the scaling behavior of the total cross sections demonstrates that FSI are negligible close to production threshold and saturate at energies above 500 MeV. The general trend of the shape change of the invariant-mass distributions correlates with the energy dependence of the FSI effects. Consequently, the dominant effect on the invariant-mass distributions comes from FSI. As a consequence of these results, possible in-medium modifications of the $\sigma$ meson (respectively pion-pion interaction in the scalar, isoscalar state) cannot be easily tested with an analysis of the shape change of the pion-pion invariant-mass distributions as a function of mass number and/or beam energy as attempted in many recent works. Predictions of the invariant-mass distributions in the framework of the GiBUU transport model reproduce their shapes for the mixed-charge pairs excellently, demonstrating that the nuclear effects for this channel are understood. Small shape discrepancies for the neutral pairs require further investigation, in particular more precise input for the elementary reactions into models. In view of these uncertainties, no clear evidence for a contribution of $\sigma$ in-medium modification can be deduced, although the observed shapes of the low-energy invariant-mass distributions of $\pi^0\pi^0$ pairs suggest that a small effect might exists.
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