Bilayer WSe$_2$ as a natural platform for interlayer exciton condensates in the strong coupling limit

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Exciton condensates (ECs) are macroscopic coherent states arising from condensation of electron–hole pairs. Bilayer heterostructures, consisting of two-dimensional electron and hole layers separated by a tunnel barrier, provide a versatile platform to realize and study ECs$^{1-10}$. The tunnel barrier suppresses recombination, yielding long-lived excitons$^{11-13}$. However, this separation also reduces interlayer Coulomb interactions, limiting the exciton binding strength. Here, we report the observation of ECs in naturally occurring 2H-stacked bilayer WSe$_2$. In this system, the intrinsic spin–valley structure suppresses interlayer tunnelling even when the separation is reduced to the atomic limit, providing access to a previously unattainable regime of strong interlayer coupling. Using capacitance spectroscopy, we investigate magneto-ECs, formed when partially filled Landau levels couple between the layers. We find that the strong-coupling ECs show dramatically different behaviour compared with previous reports, including an unanticipated variation of EC robustness with the orbital number, and find evidence for a transition between two types of low-energy charged excitations. Our results provide a demonstration of tuning EC properties by varying the constituent single-particle wavefunctions.

Narrow-gap semiconductors or semi-metals were originally proposed as natural hosts for ECs due to a spontaneous paring instability between the electrons and holes, provided that the Coulomb interaction between them exceeds the bandgap$^1$. Signatures of ECs have been identified in several such candidate systems$^{12-18}$, though debates are still ongoing due to challenges to disentangle lattice-related effects$^{18}$. In another direction, ECs have been explored in layered structures where electrons and holes are spatially confined to separate layers$^{19-22}$. These so-called spatially indirect excitons can be generated by either optical excitation or electrical gating$^{23,24}$. The spatial separation of the electrons and holes inhibits recombination and therefore extends the exciton lifetime, making it possible to observe the EC under equilibrium conditions$^{25}$. Quantum Hall bilayers provide a robust model platform to study the spatially indirect EC$^{26-28}$. In these systems, a heterostructure consisting of electrically isolated parallel layers is exposed to a perpendicular magnetic field. Interlayer excitons can then form between partially filled Landau levels (LLs) with filled (electron) states in one layer coupling to vacancy (hole) states in the other layer. A key advantage of this approach is that, within the flat LLs, kinetic energy is quenched and Coulomb interactions necessarily play a dominant role. Quantum Hall bilayers fabricated from GaAs double wells provided the first direct evidence of exciton superfluidity$^{28,29}$, appearing when each layer was tuned to half filling of the lowest Landau level. More recently, superfluid ECs have been studied in graphene heterostructures, consisting of two graphene layers separated by a boron nitride tunnel barrier, where increased flexibility in device architecture has expanded the accessible phase space$^{30}$. The EC phase diagram is determined by the interplay between the interlayer Coulomb attraction, $E_{\text{int}} \propto 1/d$, where $d$ is the layer separation, and intralayer Coulomb repulsion, $E_{\text{int}} \propto 1/l_B$, where $l_B = \sqrt{\hbar/eB}$ is the magnetic length; $e$ is the electron charge; $B$ is the magnetic field; and $\hbar$ is the reduced Planck constant. Whereas $l_B$ can be widely varied with $B$, $d$ is more restricted since it must be small enough to promote strong coupling between the layers, at the same time remaining large enough to suppress interlayer tunnelling. In GaAs bilayers, $d > 10$ nm, and the ECs are measurable only in the so-called weak coupling limit ($d/l_B \approx 1$). Recent efforts in graphene double layers demonstrated the ability to access the strong coupling regime ($d/l_B < 0.5$), by reducing the layer separation to just a few nanometres$^{32}$. Owing to the inability to further reduce $d$ without introducing appreciable tunnelling, the regime of extreme strong coupling remains almost completely unexplored$^{33}$.

Here we identify the natural bilayer WSe$_2$ as a system that provides a unique opportunity to realize ECs in the previously inaccessible regime of extreme strong interlayer coupling. In this case, interlayer tunnelling is naturally suppressed via a spin-blocking mechanism, due to combination of the spin–valley locking and stacking order. This eliminates the need to insert a physical tunnel barrier, thereby allowing the layer separation to be reduced to the atomic limit. Previously, in the weak coupling regime, the EC has been observed only in the lowest LL ($n = 0$). Remarkably, here we observe ECs in higher LLs up to $n = 6$. Our data indicate that in the strong coupling regime, the low-energy charged excitations have a different nature in different LLs, rendering the EC more robust in high LLs than in the lowest LL.

Figure 1a shows a schematic of the crystal structure for 2H-stacked bilayer WSe$_2$, consisting of two monolayers rotated 180 degrees to each other. In Fig. 1b we sketch the low-energy
valence bands, with the valley and spin indices indicated. Strong spin–orbit coupling gives rise to spin–valley locking within each layer, with the K and K′ valleys oppositely spin-polarized. Due to the stacking order, carriers residing in the same valley have opposite spin in the two layers, leading to strongly suppressed interlayer tunnelling\(^{26-30}\) (also Supplementary Information section 1).

In our experiment, we measure the penetration capacitance \(C_p\), illustrated in Fig. 1c, which has proven to be an effective probe that circumvents non-ideal electrical contact and disorder effects in two-dimensional semiconducting transition metal dichalcogenides\(^{11}\). While \(C_p\) reflects the inverse compressibility of a monolayer system, for a multilayer system, it has an additional contribution from the polarizability. The penetration capacitance normalized to the geometric capacitance between the top and bottom gates (\(C_G\)) can be written as\(^{22,31}\)

\[
\frac{C_p}{C_G} = \frac{2\epsilon_0 \partial \mu / \partial n}{\epsilon^2 + 2\epsilon_0 \partial \mu / \partial n} + \frac{e c}{4\epsilon_0 \epsilon_0} \frac{\partial \Delta n}{\partial D}
\]

Here, \(c\) is the capacitance (per unit area) between the bilayer WSe\(_2\) and the gates, \(c_0\) is the interlayer capacitance (per unit area) of the bilayer WSe\(_2\), \(\partial \mu / \partial n\) is the inverse electronic compressibility where \(\mu\) is the chemical potential and \(n\) is the total carrier density, \(\Delta n = n_T - n_B\) is the carrier density imbalance of the two layers (T, top; B, bottom) and \(D = (V_B - V_T) / 2\epsilon_0\) is the displacement electric field on the bilayer; \(V_B\) and \(V_T\) are the top and bottom gate voltages and \(\epsilon_0\) is the vacuum permittivity. The two terms in the right hand side of equation (1) correspond to ‘incompressibility’ and ‘polarizability’ contributions, respectively; a large signal in \(C_p\) indicates that the system is either incompressible or highly polarizable.

We first demonstrate that we can achieve a layer-selective population in bilayer WSe\(_2\), through gate control. In Fig. 1d we plot the penetration capacitance versus the displacement field and total density. For a fixed carrier density, the electron polarization can be tuned through three regions, corresponding to the bottom, top or both layers populated, as schematically shown in Fig. 1f. The transition from full layer polarization to partial polarization is visible as a step in the \(C_p / C_G\) data, owing to a finite polarizability contribution in the latter. This step follows a curved shape that defines the polarization boundaries in the space of \(D\) versus \(n\) (Supplementary Information section 3).

The layer-selective population becomes more apparent as a perpendicular magnetic field is applied, and the energy spectrum splits into discrete LLs. In Fig. 1e we plot \(C_p / C_G\) as a function of \(D\) and total filling factor \(\nu_{\text{tot}} = \nu_T + \nu_B\), where \(\nu_T\) and \(\nu_B\) are the top and bottom layer LL filling fractions, respectively. Horizontal features are observed at integer values of \(\nu_{\text{tot}}\). These peaks in \(C_p\) indicate incompressibility when the Fermi level is within an integer quantum Hall (IQH) gap. In the bilayer-populated region, each feature is interrupted by exactly \(\nu_{\text{tot}}\) vertical features, as schematically illustrated in Fig. 1g. This is consistent with discrete filling of the LLs in each layer: with increasing \(D\), \(\nu_T\) increases step-wise from 0 to \(\nu_{\text{tot}}\) and \(\nu_B\) decreases from \(\nu_{\text{tot}}\) to 0. Interlayer charge transfer is allowed only when the displacement field induces crossings of LLs in the two layers. At the crossing points, the bilayer system manifests increased polarizability at both integer and non-integer fillings, giving rise

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**Fig. 1 | Independent layer population in bilayer WSe\(_2\).** a. Schematic of WSe\(_2\) bilayer crystal structure. b. Schematic illustration of the Brillouin zone (shaded hexagon) of bilayer WSe\(_2\), with the four relevant flavours in the valence band marked in the layer where they reside. c. Schematic illustration of the penetration capacitance measurements. d. Penetration capacitance of bilayer WSe\(_2\), measured at \(B = 0\) T and \(T = 0.3\) K, versus \(n\) and \(D\). e. Schematic phase diagram of layer population according to features in c, f. Penetration capacitance measured at \(B = 14.9\) T and \(T = 0.3\) K, versus \(n\) and \(D\). g. Schematic illustration of features shown in a. The filling factors in each layers are marked as (\(\nu_T\), \(\nu_B\)) of bilayer WSe\(_2\), with the four relevant flavours in the valence band marked in the layer where they reside.
to the vertical features in Fig. 1e (Supplementary Information section 4 for more details).

Next, we examine the penetration capacitance at the LL crossings. Figure 2 shows representative examples of the three types of behaviour we observe. At the centre of each $v_{tot}$–$D$ map, a light blue diamond area demarcates the region where both layers host fractional filling factors and the system has finite polarizability. Figure 2a,b shows two examples where the gap closes, leading to a disappearance of the sharp horizontal feature at integer $v_{tot}$. This behaviour is seen for most LL crossings and is consistent with the single-particle picture of LL crossings—the bilayer system is compressible since both layers are partially filled. The gap closing in Fig. 2a,b also confirms the suppression of interlayer tunnelling, which would otherwise induce LL anti-crossings and preserve the gap. Figure 2c, on the contrary, demonstrates an example where the gap persists throughout the fractional filling region. The two scenarios regarding the presence or absence of a gap at the level crossings are clearly distinguishable in linecuts taken through the centre of the fractional-filling region (bottom panels): a sharp spike in $C_p$ is seen at integer $v_{tot}$ for Fig. 2c, but is absent in Fig. 2a,b. Having established that the two layers are tunnel-decoupled, we interpret the incompressible states while both layers are partially filled in Fig. 2c as interlayer correlated states, that is, ECs.

In Fig. 3a we plot $C_p$ as a function of $v_{tot}$ and $D$ over a broad range, and mark the location of ECs by solid circles using the criteria established in Fig. 2. Remarkably, ECs appear for a large range of LLs—far beyond what has been previously observed, to the best of our knowledge—both where the layers are balanced (around $D=0$) and where they are very imbalanced (at large $D$). Figure 3b shows the corresponding schematic LL diagram, which identifies the LL orbital and spin/valley indices (Supplementary Information section 2). We note first that all of the ECs correspond to states with matched orbital number $n$. The series of ECs at $D=0$ (with Fig. 2c as an example) corresponds to the crossings of two LLs with the same orbital number and spin indices but different valley indices; while those at finite $D$ correspond to matched orbital numbers and valley indices but different spins (Supplementary Information section 5).

Our observations indicate that EC formation requires the orbital wavefunctions to match, but is independent of the spin/valley degree of freedom. Likewise, our Hartree–Fock and numerical calculations suggest that formation of ECs, characterized by a good overlap with the Halperin (111) wavefunction and a gapless neutral mode, only appears when the LLs in the two layers have matched orbital numbers (Supplementary Information sections 10 and 11). The consistency with theory further confirms the interpretation of the observed incompressible states as ECs. In addition, our observation is consistent with previous experiments in graphene double layers$^{24}$ that demonstrated that spin and valley degrees of freedom are largely irrelevant in the formation of ECs in the lowest LL. Intriguingly, the specific orbital number also plays a critical role in EC formation: EC formation is observed for $n=1–6$, but is suppressed for $n=0$, as shown by the dashed circles in Fig. 3a,b (Supplementary Information sections 5 and 6). This is precisely opposite to previous studies in double-layer systems with larger interlayer spacing$^{24,34}$, where the ECs have only been observed for $n=0$.

The critical role of the orbital number is further corroborated by the evolution of specific ECs with magnetic field. This is displayed in Fig. 3c, which plots $C_p$ versus the magnetic field and filling factor at the balanced condition $D=0$. For $B<10.5\,T$, ECs are clearly

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**Fig. 2 | EC formation and gap opening at LL crossings.** a–c. Penetration capacitance versus total filling factor $v_{tot}$ and displacement field $D$ at $B=14.9\,T$ around several LL crossings. Each bottom panel is a linecut along the red dashed line in the top panel, which tracks the equal topmost LL population in the two layers. The insets of the bottom panels illustrate the orbital, spin and valley indices.
observed for \( \nu_L=\nu_H=4.5, 5.5 \) and 6.5, but the state at \( \nu_{K1}=5.5 \) disappears abruptly above 10.5 T. This disappearance of ECs coincides with a change in the orbital number from \( n=5 \) to \( n=0 \), as illustrated in Fig. 3d. The orbital number change is due to the re-arrangement of the LLs with different spin indices, as illustrated in Fig. 3e. For a fixed filling factor, the carrier density scales linearly with the magnetic field, and at low densities, the g factor, which decides the Zeeman splitting between two spin branches, is strongly enhanced\(^{11} \). Therefore, as B increases and the carrier density is raised above a threshold value, the active LLs at a fixed filling factor can switch from one spin to another and abruptly change orbital number to \( n=0 \), leading to the disappearance of ECs (Supplementary Information section 7).

To better understand the dependence of EC robustness on orbital number, we measure the excitation gap \( \Delta \) by integrating \( \delta \mu \) over the gap at integer filling factors (Supplementary Information section 8 for details). Figure 4a plots \( \Delta \) versus the orbital number \( n \) at \( D=0 \), for \( B=14.9 \) T: it exhibits a non-monotonic behaviour with the maximum at \( n=2 \). Tuning the orbital number modifies the single-particle electron wavefunction: as \( n \) increases, the wavefunctions spread out and have more nodes. In single-layer systems, at fractional fillings, this evolution often leads to different correlated ground states for different values of \( n \). Here, although the ground state remains an EC, the non-monotonic dependence of \( \Delta \) on \( n \) stems from the change of the nature of low-energy charged excitations. The character of these excitations is more conveniently understood in the pseudospin picture. In this picture, electron states in the top (bottom) layer are viewed as pseudospin up (down), while the phase-coherent ECs manifest a macroscopically aligned pseudospin pointing in-plane\(^{15} \). On top of such a pseudospin ferromagnet ground state, one type of charged excitation is associated with a spatially extended pseudospin texture, known as a meron–antimeron pair in the case of bilayer quantum Hall systems\(^{15} \) (similar to skyrmions\(^{36} \) in quantum Hall ferromagnets in a single layer). As \( n \) increases, the energy of such excitations increases\(^{37} \). On the other hand, a conventional type of excitation, which represents a localized particle or hole, has an energy that decreases with \( n \). As a result, a change in the nature of the lowest-energy excitations is expected as \( n \) is varied. Figure 4b shows the theoretical estimate of the gap for the two types of excitations in a simple bilayer model without screening effects. The transition between two types of excitations occurs between \( n=0 \) and \( n=1 \), giving a non-monotonic dependence.
This is qualitatively consistent with our data, except that in the model, the gap maximum appears at \( n = 1 \), whereas the maximum appears at \( n = 2 \) in our measurement, suggesting that the pseudospin textured excitations also dominate at \( n = 1 \). The slight discrepancy with experimental data may be due to screening or disorder effects, which may lower the energy of pseudospin-texture excitations and shift the transition to higher \( n \).

The different characteristics of the two kinds of excitations are also suggested by the density imbalance dependence, as shown in Fig. 4c. Here, we plot the penetration capacitance as a function of \( D \), at a constant total filling factor \( \nu_{\text{tot}} = 1, 3, 5, 7 \), which are the four bottom circles in Fig. 3a,b and correspond to LL orbital number \( n = 0, 1, 2, 3 \), respectively. The colour shades in the right three panels illustrate the \( D \) range where the individual layers host fractional filling factors, as suggested by the polarizability contribution at adjacent non-integer fillings. A larger \( C_p \) suggests a smaller electronic compressibility and a larger gap for charged excitations. Our data suggest that, for \( n = 1 \), the EC gap increases with \( D \) and transitions smoothly into the IQH gap. By contrast, for \( n = 2 \) and \( 3 \), the EC gap decreases with \( D \) and has a minimum before transitioning into the IQH state.

The distinct behaviour of the two types of excitations is supported by our numerical calculations (Supplementary Information section 12), which find that the meron–antimeron pairs have a sharp increase in gap with layer imbalance, while the particle–hole excitations show a flat response. While the pseudospin points in-plane for a density-balanced bilayer system, imbalancing the bilayer is equivalent to tilting the pseudospin out-of-plane; therefore the in-plane component of the spin stiffness decreases. For meron–antimeron pairs, the excitation energy has the main contribution from the meron and antimeron self-energy, the sum of which increases with density imbalance. On the other hand, the particle–hole excitation energy is just the exchange energy, which is independent of the charge density imbalance. The decrease of the excitation gap with imbalance for \( n = 2 \) and \( 3 \) is not captured by our calculations and remains to be understood.

Finally, we remark that, in contrast to our bilayer WSe\(_2\), in other quantum Hall double-layer systems, the EC has only been observed within the LL of orbital number \( n = 0 \). We find that, although numerical calculations suggest that ECs could form in LLs of high orbital numbers, a smaller interlayer spacing is required for higher orbital numbers. As shown in Fig. 4d, the calculated critical interlayer spacing in units of the magnetic length, \( d/l_p \), decreases sharply as a function of the orbital number \( n \). The critical spacing \( d_c \) is estimated as the distance where the Goldstone mode goes soft at finite momentum, signalling the EC becoming unstable (Supplementary Information section 12).
Information section 11). On the right axis of Fig. 4d, we mark the experimentally accessible ranges of $d_{\text{B}}$ for three different systems—GaAs double quantum wells, graphene double layers with boron nitride barrier and bilayer WSe$_2$. Our calculation suggests that the absence of ECs in higher LLs in the first two systems is likely due to the large thickness of the intentional interlayer physical barrier (graphene also has the complication, as the LL wavefunctions are a mixture of simple harmonic oscillator wavefunctions). By contrast, the interlayer spacing in bilayer WSe$_2$ is set by the lattice constant in the vertical direction, which is only about 0.7 nm, and thus ECs are expected to occur in higher LLs.

To conclude, our study demonstrates bilayer WSe$_2$ as a unique platform to access ECs in the strong coupling limit, by exploiting the intrinsic spin–orbital coupling and stacking order in the host material. This designing principle could be further used in creating other quantum phases from layered van der Waals materials. For example, the interlayer hybridization could still be suppressed in, for example, a twisted bilayer WSe$_2$ at a small angle deviation from the natural 2H-stacking. Combined with the flatband originated from the moiré potential, such structures hosting strong electron–electron interactions and a well-defined layer degree of freedom may set the basis for ECs at zero field and other exotic phases. Finally, our study demonstrates ECs composed from tunable single-particle orbital wavefunctions, and how such tunability could vary the properties of ECs and the excitations on top of the ground state.

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Methods
The heterostructure was assembled using the van der Waals dry transfer technique, and prepatterned Pt electrodes were used for electrical contacts to bilayer WSe₂. Hexagonal boron nitride was used as the dielectric, and graphite or metal as the top and bottom gates for bilayer WSe₂. The top gate was lithographically shaped so that its overlap with the bottom gate covers only bilayer WSe₂, and the overlap defines the device area. In order to achieve good electrical contact, we used an additional contact gate on top to heavily dope the contact area, which was isolated from the top gate by the Al₂O₃ dielectric. Data from a different device are shown in Supplementary Information section 9. Penetration capacitance was measured with an FHX35X high electron mobility transistor serving as a low-temperature amplifier, in a similar set-up as in the literature1. Measurements were performed at T = 0.3 K unless otherwise specified.

Data availability
Experimental data relevant to figures in the main text and data of numerical calculations are available at https://doi.org/10.5281/zenodo.6377084. All other raw data are available from the corresponding author upon reasonable request.

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Author contributions
Q.S. fabricated the devices, performed the capacitance measurements and analysed the data. E.-M.S. fabricated devices and performed transport measurements that complement the capacitance data. Z.P. and D.A.A. provided theoretical input and performed the numerical calculations. D.R. and B.K. grew the WSe₂ crystals under the supervision of J.H. and K.B.; K.W. and T.T. grew the hexagonal boron nitride crystals. Q.S., C.R.D., J.H., Z.P. and D.A.A. wrote the manuscript with input from all authors.

Competing interests
The authors declare no competing interests.

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