Design and analysis of experiments linking on-line drilling methods to improvements in knowledge

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Abstract

An on-line drilling system, the tutor-web, has been developed and used for teaching mathematics and statistics. The system was used in a basic course in calculus including 182 students. The students were requested to answer quiz questions in the tutor-web and therefore monitored continuously during the semester. Data available are grades on a status exam conducted in the beginning of the course, a final grade and data gathered in the tutor-web system. A classification of the students is proposed using the data gathered in the system; a Good student should be able to solve a problem quickly and get it right, the “diligent” hard-working Learner may take longer to get the right answer, a guessing (Poor) student will not take long to get the wrong answer and the remaining (Unclassified) apparent non-learning students take long to get the wrong answer, resulting in a simple classification GLUP. The (Poor) students were found to show the least improvement, defined as the change in grade from the status to the final exams, while the Learners were found to improve the most. The results are used to demonstrate how further experiments are needed and can be designed as well as to indicate how a system needs to be further developed to accommodate such experiments.

1 Introduction

With the increasing number of web-based educational systems several types of educational systems have emerged. These include learning management system (LMS), learning content management system (LCMS), virtual learning environ-
ment (VLE), course management system (CMS) and Adaptive and intelligent Web-based educational systems (AIWBES)\(^1\).

The LMS is designed for planning, delivering and managing learning events, usually adding little value to the learning process nor supporting internal content processes [3]. A VLE provides similar service, adding interaction with users and access to a wider range of resources [5]. The primary role of a LCMS is to provide a collaborative authoring environment for creating and maintaining learning content [3].

Many systems are merely a network of static hypertext pages [1] but adaptive and intelligent Web-based educational systems (AIWBES) use a model of the goals, preferences and knowledge of each student and use this to adapt to the needs of that student [2]. These systems tend to be subject-specific because of their structural complexity and therefore do not provide a broad range of content.

The tutor-web (at http://tutor-web.net) used here is an open and freely accessible AIWBES system, available to students and instructors at no cost. The system has been a research project since 1999 and is completely based on open source computer code with material under the Creative Commons Attribution-ShareAlike License. The material and programs have been mainly developed in Iceland but also used in low-income areas (e.g. Kenya). Software is written in the Plone\(^2\), CMS (content management system), on top of a Zope\(^3\) Application Server.

In terms of internal structure, the material is modular, consisting of departments (e.g. math/stats), each of which contains courses (e.g. introductory calculus/regression). A course can be split into tutorials (e.g. differentiation/integration), which again consist of lectures (e.g. basics of differentiation/chain rule). Slides reside within lectures and may include attached material (examples, more detail, complete handouts etc). Also within the lectures are drills, which consist of quiz items. The drills/quizzes are designed for learning, not just simple testing. The system has been used for introductory statistics, mathematical statistics, earth sciences, fishery science, linear algebra and calculus in Iceland and Kenya, with some 2000 users to date.

A fundamental aspect of the system is that students can continue requesting and answering \textit{ad infinitum}. They receive immediate feedback, usually including a detailed solution (see Fig. 1). In-class surveys indicate that students really like this. Naturally, students can monitor their own progress. Several grading schemes can be implemented, but using the last 8 answers has been the norm until 2013.

An Item Allocation Algorithm (IAA) is used to choose drill items (questions)...

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\(^1\) The terms VLE and CMS are often used interchangeably, CMS being more common in the United States and VLE in Europe.

\(^2\) http://plone.org

\(^3\) http://zodb.org
for learning, within each lecture. Aspects include the desire to start with easy items and increase difficulty with increasing grade. Given that iteration is known to enhance learning, the IAA also occasionally chooses an item from earlier material (lectures). It is likely to be useful to choose again from earlier mistakes or go to prerequisites if there is no learning, but these have not been investigated to date.

The IAA is simply implemented as a probability mass function (p.m.f., Fig. 2), which is a function of difficulty. In addition, the p.m.f. depends on the grade, thus implementing personalized education appropriate for the student in question.

Student surveys are conducted in most courses using the system. A typical example of results is given in Fig. 3. Although it is useful to know that students appreciate a drilling system, more concrete evidence is needed in order to justify its use. One such is provided using an experimental design which compared groups of students using the system or using traditional homework in a crossover design [4]. The basic conclusion from this experiment was that the difference between the groups was insignificant, both statistically and from the point of view that the confidence interval for the two groups was very tight. It follows that the system can be used to reduce regular homework considerably, but not replace it completely.
Figure 2: Tutor-web probability mass function used by the item allocation algorithm. The x-axis indicates the ranked item difficulty and the y-axis gives the probability of the next item, where the p.m.f. chooses depends on the grade of the student.

(cf. Fig. 3).

Figure 3: Student satisfaction survey results. Note how the tendency to like web-assisted methods (left panel) does NOT imply that regular homework can be dropped (right panel).
2 Monitoring students

Consider next the data available to the system and how this may relate to the actual knowledge, as determined by exams, either an initial status exam or a final exam. A calculus course with data for 182 students is used for these analyses for the remainder of this paper. A status exam was submitted in the second week of the course. The problems on the exam covered numbers and functions, basic algebra, equation of a straight line, trigonometric, differentiation and integration, vectors and complex numbers. The performance on the status exam was poor with an average score of 35%. Students were also evaluated multiple times during the semester, and monitored continuously using the tutor-web. In the following, summaries of the tutor-web grade and response times along with grades from an initial status exam and the final exam are used. In the tutor-web, the response time for each item is measured, along with a 0/1-grade. The items are grouped in lectures as described in section 1 with 34 lectures belonging to this particular course. As an example, consider the average grade and average time spent on the first item in each lecture. This provides 182 pairs. Each of these can now be labelled in 4 ways, according to whether the student passed the status exam and/or the final exam. These results are given in Fig. 4. Notice how it is not at all clear from the figure whether there is a link between t-w performance and grades on either exam.

A simple linear regression of grade improvement, defined as the change in grade from the status exam to the final exams, on the grade and the time used per item within the tutor-web reveals that those are important variables, but relationships to performance on exams may be nontrivial. For example, one would expect the time taken to solve a problem to be a complex combination of the student’s expertise and diligence. Thus a “Good” student should be able to solve a problem quickly and get it right, but the “diligent” hard-working Learner who may not know the material very well may take longer to get the right answer. A guessing (Poor) student will not take long to get the wrong answer. The remaining (Unclassified) apparent non-learning students take long to get the wrong answer. This GLUP classification is derived from Fig. 4 and used below.

3 Relating on-line monitoring results to other performance measures

3.1 Relating on-line monitoring results to learning

Although there is no trivial grouping seen in the figure, consider using the GLUP - classification to predict actual learning, or “improvement”, using a regular ANOVA.
Figure 4: Plot of average grade and timing for first item request within each lecture. Vertical and horizontal lines indicate classification of students according to time and grade (using medians). Color: green/red=Pass/Fail on final exam. Shape: Circle/Diamond=Pass/Fail on status exam.

The “improvement” is defined as the change in grade from the status to the final exams where the grade of the exams has been scaled to be on the interval from 0 to 100. The ANOVA was performed using the \texttt{lm} function in R \cite{R}. The results are shown in Table\ref{table:results}. In this linear model the Poor students form a baseline and the estimates for the other groups can be interpreted as gain in improvement. It is therefore seen that all the other groups perform better on average than the baseline.

The main results from this analysis are that the point estimate for the poor performers is the lowest among the four groups. The greatest increase from P is amongst the learners, L, but this is not significantly different from e.g. the Good students. It is interesting to note that the unclassified group (U) shows consider-
ably (and significantly) more improvement than the poor performers (P). The only difference in their classification is the average amount of time spent on the items. Thus, although both groups perform poorly at the outset, those who spent more time on each item outperformed the other group by quite a bit on average in terms of improvement.

### 3.2 Linking to absolute performance

Predicting the improvement during a semester, or the “value-added” is done directly above by fitting to the improvement in grade, from the initial status exam to the final exam. For several reasons it is also of interest to consider predictions of the final exam grade ($finalG$) directly, including the status exam as a regular explanatory variable ($statusG$). Many variables can in principle be defined and used. Here the average grades from different stages within the tutor-web are included ($g1$, $g5$ and $gn$, $gn$ being the grade on the last item requested in the lecture), as is the average time spent per item at different points ($T1$, $T5$ and $Tn$), the squared time spent per item ($T1.2$, $T5.2$ and $Tn.2$), an indicator variable of whether students spend more or less time on the last (usually most difficult) item compared with the first one ($Tn>T1$), the GLUP class variable ($class1$), number of items requested ($twnattl$) and finally the squared number of items requested ($twnattl2$). The model was fitted using the `lm` function and reduced using the `step` function in R [6]. The result is shown in Table 2.

Of the variables selected here, one has a slightly different status from the others: $statusG$ is defined on data outside the tutor-web whereas other variables are defined completely with the on-line learning system.

As can be seen in the table, the GLUP class variable is not significant when included with the grade and time at different stages, which is not surprising since the classification is defined by those variables. It should also be noted that the squared number of attempts is significant, implying that there tends to be a reduction in grade for students who give more than 27 answers on average (per lecture). Earlier attempts at quantification of the effect of the number of attempt have given mixed output. For example, one might surmise that the number of attempts is like the time

|                | Estimate | Std. Error | t value | Pr(>|t|) |
|----------------|----------|------------|---------|----------|
| (Intercept)    | 9.5582   | 2.7223     | 3.51    | 0.0006   |
| class1G        | 6.9671   | 4.3282     | 1.61    | 0.1092   |
| class1L        | 11.4772  | 3.9247     | 2.92    | 0.0039   |
| class1U        | 9.0109   | 4.1953     | 2.15    | 0.0331   |

Table 1: Predicting improvement (final-status) from GLUP classification.
Estimate | Std. Error | t value | Pr(>|t|)
--- | --- | --- | ---
(Intercept) -46.7506 | 11.0469 | -4.23 | 0.0000
rwnattl 2.4488 | 0.7809 | 3.14 | 0.0020
statusG 0.5211 | 0.0609 | 8.55 | 0.0000
g5 54.3603 | 10.1337 | 5.36 | 0.0000
T5 6.0022 | 3.6711 | 1.63 | 0.1039
Tn 2.9232 | 2.0771 | 1.41 | 0.1611
'Tn>T1'TRUE 10.3281 | 4.2538 | 2.43 | 0.0162
twnattll2 -0.0462 | 0.0182 | -2.54 | 0.0119
T5.2 -1.0496 | 0.6013 | -1.75 | 0.0826

Table 2: Final model selected using the AIC.

spent per item, i.e. be a measure of diligence, but there are also guessers and in fact the analyses in [8] showed a net negative linear relationship with the number of attempts. The greater number of students in the present study may be the reason why it appears to be possible to accommodate both effects using a quadratic response curve.

Note also how the effect of the time spent per item is positive (both T5 and Tn), i.e. the longer the student spends on an item the higher the final grade. As above, this is a measure of the effect of “diligence”. Finally note that the squared time spent on the 5th item was selected in this model. The point estimate corresponds to a reduced performance for students who use on average more than $T^*_5 = 3$ minutes on the fifth item.

4 Conclusions

It is clear from a number of student surveys, that students from Iceland to Kenya like an on-line drilling system, they feel they learn from it and, based on the results given here, one can statistically demonstrate this learning.

Research reported elsewhere [4] implies that student learning is almost the same, regardless of whether an on-line system or traditional homework is used. Since the in-class surveys consistently indicate that students prefer to also get graded homework, it is not possible to replace all homework by computerized drills, but one can easily replace half the homework by on-line multiple-choice questions.

Since the instructor can make the drills form a part of the final grade and can set minimum return requirements as criterion for passing, this gives considerable potential for changes in emphases or reductions in instructor workload.
5 Discussion: Avenues of research

Applications of the tutor-web system have varied in student requirements as formal requirements are set by the instructors, not the system. The above results imply that it may be beneficial to incorporate features which drive the students towards certain behavior or performance.

In the course studied here, as well as in other courses where this system have been tested [e.g. 7] students tend to work towards a fairly high grade (median $g_n = 0.94$ and median of last 8 is 0.92 in the present course). Hence changes to either the allocation algorithm or the grading scheme will likely lead to a change in behavior where the students still work towards a goal of a high grade, assuming it is still a feasible goal. Similarly, a timeout option is also likely to lead to changes in student behavior. A generic positive system change has benefits over an instructor-defined criterion since it will affect all students at all times, not just the course in question.

The students appear to gain (in terms of exam grade) through requesting more items (up to 27) than normally required (8 for this course) or normally taken (median=15, upper 75% quartile=20). It would therefore seem reasonable to encourage an increase in the number of items requested by students.

The current “last 8” internal tutor-web grade assumes incorrect answers until at least 8 questions have been answered in a given lecture. Most students therefore answer at least 8 questions in each lecture. This scheme, however, implies that if the 8th answer is incorrect after a run of 7 answers, the grade will not increase unless a new run of 8 correct answers is obtained. Many students stop at this stage and this behavior is contrary to the goal of positive reinforcement. A simple change would be to use the most recent 30 answers, or, more generally, to use for grading the most recent
\[ n_g = \max(8, \min(n/2, 30)) \]
answers, possibly tapered, where $n$ is the total number of answers given. This will penalise the guesser by introducing a longer tail and simultaneously give reduced weight to the accidental 8th incorrect response. A next-generation mobile-web version of the tutor-web will include multiple grading schemes, including these. This will facilitate a simple experiment to investigate the relationship between the grading scheme and the number of attempts per lecture.

Although the tutor-web is a significant predictor of the final grade, it is not a very good one. For example, of the 113 students who obtain a grade of over 90% on the tutor-web work, 34% do not attain a grade of 50% on the final exam. The main problem with this is that the tutor-web grade is not a reliable indicator for the students themselves. The students with full marks, 100% on the tutor-web, have an 83% chance of passing the exam however. From this it is seen that the
tutor-web grade is “too high” in the sense that it indicates more knowledge than is estimated using traditional exams. Future work therefore needs to investigate whether changes in the grading scheme, to the effect of lowering most grades, can provide better indicators of exam performance.

Another way of “reducing the tutor-web grade” is to include timeout features. Such a timeout could be a function of grade, i.e. a student can only get into a certain grade range by answering questions correctly within certain time limits.

![Figure 5: Possible curves to define time allocated to items, as a function of grade.](image)

This will almost certainly keep students working longer within grade intervals with a timeout and this could be used e.g. to ensure expertise within easier items before continuing. This approach will also increase the number of attempts (except for the best students), including the guessers since this will make it harder to obtain a higher grade. To quantify the effect of the timeout, one approach is to focus on a single parameter in a formula such as

\[ t = a \left[ 1 - \left( 1 - \frac{b}{a} \right) e^{-\left(\frac{g - g^*}{2s}\right)^2} \right] \]

which will give an upside-down bell-curve with an upper bound of \( t = a \) and a minimum of \( t = b \) at \( g = g^* \). Given that the median time is about 2 minutes, one could take e.g. \( a = 10, b = 2, g^* = 5 \) and \( s = 1 \) as initial values (cf Fig. 5) and set up a formal experimental design by selecting either \( b \) or \( g^* \) at random from within some intervals for each student within each lecture. Performance can be evaluated statistically either by how the number of attempts within a lecture changes as a function of \( b \) or by how the performance on an algebra item in an exam varies as a function of \( b \). This particular choice of parameter values enforces a bottleneck
where the students have to obtain a certain level of expertise before getting above a certain grade, upon which the timeout parameter is no longer limiting. A different approach (using a higher $g^*$ and $s$) would be to set a similar limit access to the higher grades. Given the complex relationship described in this paper, between time spent on each item and subsequent performance, it is not trivial to predict the full effect of any timeout parameter settings.

Finally, since the Poor students (in the GLUP classification) are the poorest performers by all measures, one needs to consider methods to move these students into the otherwise Unclassified group, who spend more time on each item. When students have answered a question the system provides a detailed explanation of how the answer is obtained (most items have such explanations). A possible method to slow these students down is therefore to use pop-ups, such as a warning when a student has answered incorrectly and clearly asks for the next item without first reading the explanation. The net effect of this can easily be tested by randomly assigning such stop-signs to half the P-students and evaluating whether there is a statistical difference in how they move out of the P group.

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The calculus material content used as a basis for this research has been developed by numerous faculty and students at the University of Iceland.
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