Multichannel Audio Source Separation with Independent Deeply Learned Matrix Analysis Using Product of Source Models

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Abstract—Independent deeply learned matrix analysis (IDLMA) is one of the state-of-the-art multichannel audio source separation methods using the source power estimation based on deep neural networks (DNNs). The DNN-based power estimation works well for sounds having timbres similar to the DNN training data. However, the sounds to which IDLMA is applied do not always have such timbres, and the timbral mismatch causes the performance degradation of IDLMA. To tackle this problem, we focus on a blind source separation counterpart of IDLMA, independent low-rank matrix analysis. It uses nonnegative matrix factorization (NMF) as the source model, which can capture source spectral components that only appear in the target mixture, using the low-rank structure of the source spectrogram as a clue. We thus extend the DNN-based source model to encompass the NMF-based source model on the basis of the product-of-expert concept, which we call the product of source models (PoSM). For the proposed PoSM-based IDLMA, we derive a computationally efficient parameter estimation algorithm based on an optimization principle called the majorization-minimization algorithm. Experimental evaluations show the effectiveness of the proposed method.

I. INTRODUCTION

Multichannel audio source separation is a technique to separate concurrent sources out of mixture signals observed by a microphone array [1]. In the overdetermined case, many blind source separation (BSS) methods using the statistical independence between sources have thus far been proposed for decades, for example, frequency-domain independent component analysis [2], [3] and independent vector analysis [4], [5]. One of the state-of-the-art BSS methods is independent low-rank matrix analysis (ILRMA) [6], which estimates demixing filters, using the nonnegative matrix factorization (NMF) [7] as a source model. When a sufficient amount of training data of the sources is available, we previously showed that the separation performance can be further improved by replacing the NMF-based source model of ILRMA with the source model based on a deep neural network (DNN) [8]. We call this DNN-based method independent deeply learned matrix analysis (IDLMA), which is one of the state-of-the-art supervised but spatially blind multichannel audio source separation methods.

IDLMA uses the sourcewise DNN-based source models that are trained in advance to extract power spectrograms of target sources from noisy mixtures. Thus, its separation performance strongly depends on the DNN-based power estimation performance. The DNNs work well for sounds that include sources having timbres similar to those of the training data. However, owing to the difference in musical genre and mixing, the sounds to which ILRMA is applied sometimes differ in timbre from those of the training data, which leads to performance degradation of IDLMA. For example, in the DSD100 dataset [9], which we will use in the experiments described in Section IV, most of the sounds labeled as bass are played on an electric bass guitar. The DNN trained with these sounds should work well for the electric bass guitar sounds. However, some of the test data labeled as bass are played by bass instruments other than the electric bass guitar, e.g., synth bass. This difference leads to the failure of the DNN-based source power estimation, as we will later show in Section IV-C.

On the other hand, since ILRMA is a fully blind method, it is free from such performance degradation caused by the timbral discrepancy. However, the separation performance of ILRMA is often lower than that of IDLMA because its NMF-based source model assumes the low-rank structure of the source spectrograms, which does not always hold. For the sources that do not have the low-rank structure, the DNN-based source model is effective as long as the timbral discrepancy is less significant. From this viewpoint, the DNN- and NMF-based source models are complementary.

Motivated by this observation, we extend the DNN-based source model to encompass the NMF-based source model on the basis of the product-of-expert concept [10]. Since this extension combines the source models of IDLMA and ILRMA, we call it the product of source models (PoSM). For the data to which the proposed method is applied, the DNN part represents the source components similar to the training data, whereas the NMF part represents those that appear only in the target mixture. We build an IDLMA extension that instead uses the proposed PoSM as the source model, and we derive a computationally efficient parameter estimation algo-
where \( A \) is the STFT is sufficiently longer than the reverberation time, the mixing system is time-invariant and the window length of observed signal \( x \) whose complex Gaussian distribution with zero mean and variance \( H \) channel indices, respectively, and \( T \) operator. We define the matrices \( M \) represented as \[\pi \in \mathbb{C}^{I \times J} \] \[\theta \in \mathbb{C}^{K \times J} \] where \( i, j \in \mathbb{N} \), \( m = 1, \ldots, M \) are the frequency, time frame, source, and channel indices, respectively, and \( T \) denotes the transpose operator. We define the matrices \( X_n \in \mathbb{C}^{I \times J} \) and \( Y_n \in \mathbb{C}^{I \times J} \) whose \((i, j)\)th entries are \( x_{ijm} \) and \( y_{ijm} \), respectively. When the mixing system is time-invariant and the window length of the STFT is sufficiently longer than the reverberation time, the observed signal \( x_{ij} \) is represented as \[ x_{ij} = A_i s_{ij}, \] where \( A_i \in \mathbb{C}^{M \times N} \) is a mixing matrix. If the number of channels is equal to that of sources (i.e., \( M = N \)) and the mixing matrix \( A_i \) is nonsingular, the separated signal \( y_{ij} \) is represented as \[ y_{ij} = W_{ij} x_{ij}, \] where \( W_{ij} = (w_{ij1}, \ldots, w_{ijN})^H \in \mathbb{C}^{N \times M} \) is a demixing matrix and \( H \) denotes the Hermite transpose operator.

As in [6] and [8], we assume that \( y_{ijm} \) follows an isotropic complex Gaussian distribution with zero mean and variance \( r_{ijm} \): \[ p(y_{ijm}; r_{ijm}) = N_C(y_{ijm}; 0, r_{ijm}) = \frac{1}{\pi r_{ijm}} \exp \left( -\frac{|y_{ijm}|^2}{r_{ijm}} \right). \] Owing to the generative model given by (6), the problem of separating the source signals \( y_{ijm} \) out of the given observed signals \( x_{ijm} \) can be formulated as a maximum likelihood estimation problem with respect to \( r_{ijm} \) and \( W_{ij} \). The cost function is given as the negative log-likelihood of the observed signals [1]: \[ \mathcal{L} = -\log p(X) = -\log p(Y) - 2J \sum_i \log |\det W_i| \] \[ = \sum_{i,j,n} \left( \log r_{ijm} + \frac{|w_{ijm}^H x_{ijm}|^2}{r_{ijm}} \right) - 2J \sum_i \log |\det W_i| \] where \( X = \{X_1, \ldots, X_M\} \) and \( Y = \{Y_1, \ldots, Y_N\} \) denote the sets of observed and separated signals, respectively. Here, \( \sum \) denotes equality up to constants. Let us denote a matrix whose \((i, j)\)th entry is \( r_{ijm} \) by \( R_n \in \mathbb{R}^{I \times J} \). ILRMA and IDLMA are derived on the basis of the above formulation, and their difference lies in the representation of \( R_n \). To distinguish the NMF- and DNN-based source models, we hereafter add superscripts \((\text{NMF})\) and \((\text{DNN})\) to \( R_n \), respectively.

B. ILRMA [6]

1) Representation of \( R_n^{(\text{NMF})} \): ILRMA uses NMF as the source model. The NMF represents \( R_n^{(\text{NMF})} \) as a product of two nonnegative matrices, one of which is a basis matrix \( T_n \in \mathbb{R}^{I \times K} \) consisting of \( K \) spectral templates and the other of which is an activation matrix \( V_n \in \mathbb{R}^{K \times J} \) representing the temporal energies of the corresponding spectral templates.

\[ t_{ijm}^{(\text{NMF})} = \sum_k t_{ikm} v_{kjm}. \] Here, \( t_{ikm} \) and \( v_{kjm} \) are the \((i, j)\)th entries of \( T_n \) and \( V_n \), respectively. By substituting (8) into (7), we can write the cost function of ILRMA \( \mathcal{L}_{\text{ILRMA}} \) as

\[ \mathcal{L}_{\text{ILRMA}} = \sum_{i,j,n} \left( \log \left( \sum_k t_{ikm} v_{kjm} + \frac{|w_{ijm}^H x_{ijm}|^2}{r_{ijm}} \right) \right) - 2J \sum_i \log |\det W_i|. \]  

2) Parameter Estimation Algorithm: The parameter estimation algorithm of ILRMA iteratively updates \( t_{ikm}, v_{kjm}, \) and \( W_{ij} \) [6]. The first two terms of the cost function (9) are the same form as in the cost function of NMF with the Itakura–Saito divergence criterion [12] up to constants. For updating \( t_{ikm} \) and \( v_{kjm} \), we can use the convergence-guaranteed iterative algorithm derived in [12], which is based on the MM algorithm [11].

The MM algorithm consists of two steps. For a to-be-minimized cost function of \( \theta \) and \( f(\theta) \), by introducing an auxiliary variable \( \bar{\theta} \), we construct its upper bound \( f^+(\theta, \bar{\theta}) \) to satisfy the condition that there exists \( \theta \) such that \( f^+(\bar{\theta}, \theta) \) is tangent to \( f(\theta) \) for any \( \theta \) as follows:

\[ \min \ f^+(\theta, \bar{\theta}) = f(\theta). \]  

If \( f^+ \) can be minimized with \( \theta \) and \( \bar{\theta} \) in closed form, we iteratively update \( \theta \) and \( \bar{\theta} \):

\[ \theta \leftarrow \arg \min_{\theta} f^+(\theta, \bar{\theta}), \] \[ \bar{\theta} \leftarrow \arg \min_{\theta} f^+(\theta, \theta). \]  

Since \( f^+ \) always satisfies (10), \( f \) is guaranteed to be non-increasing at each iteration.

The application of the MM algorithm to the minimization of (9) with respect to \( t_{ikm} \) and \( v_{kjm} \) yields the following update
The outline of the ILRMA separation process is shown in Fig. 1(a). The separation process of ILRMA is as follows:

\[ t_{ik,n} ← t_{ik,n} \]
\[ v_{kj,n} ← v_{kj,n} \]

By using \( t_{ik,n} \) and \( v_{kj,n} \) obtained from (13) and (14), we update \( r_{ijm}^{(\text{NMF})} \) in accordance with (8).

Since \( t_{ik,n} \) and \( v_{kj,n} \) determine the scale so that the sum of terms in \( w_{in} \) is applied, which guarantees the nonincrease in the cost function. This method updates \( w_{in} \) sequentially with respect to \( n \):

\[ w_{in} ← (W_i U_{in})^{-1} e_n, \]
\[ w_{in} ← \frac{w_{in}}{\sqrt{w_{in}^H U_{in} w_{in}}}, \]
\[ U_{in} := \frac{1}{J} \sum_{j} \frac{1}{r_{ijm}^{(\text{NMF})}} x_{ij} x_{ij}^H, \]

where \( e_n \in \mathbb{R}^N \) is a unit vector whose \( n \)-th element is one.

To compensate for the scale uncertainty between \( w_{in} \) and \( r_{ijm}^{(\text{NMF})} \), the projection back (PB) technique [14] is applied to \( y_{ij} \). This technique determines the scale so that the sum of the separated signals matches the observation of the reference microphone whose index is denoted by \( m_{\text{ref}} \):

\[ x_{ijm_{\text{ref}}} = \sum_n y_{ijn} = \sum_n w_{in}^H x_{ij}, \]

The PB technique scales \( y_{ij} \) as

\[ y_{ij} ← \text{diag}(d_i) y_{ij}, \]

where \( \text{diag}(d_i) \in \mathbb{C}^{N \times N} \) has the elements of \( d_i \in \mathbb{C}^N \) on the main diagonal and 0 elsewhere, and \( d_i \) is computed by

\[ d_i = (W_i^T)^{-1} e_{m_{\text{ref}}}. \]

The outline of the ILRMA separation process is shown in Fig. 1(a), where \(| \cdot |^q \) returns the absolute value of each entry of a matrix to the \( q \)-th power.

### C. IDLMA [8]

The cost function of IDLMA is given as (7) by replacing \( r_{ijm} \) with \( r_{ijm}^{(\text{DNN})} \). In contrast to ILRMA, \( R_n^{(\text{DNN})} \) is updated using the pretrained DNNs. The DNN for \( n \)-th source, \( DNN_n \), takes the magnitude spectrogram of the current separated signal \( Y_n \) and outputs the estimate of the source standard deviation \( \Sigma_n \in \mathbb{R}_{\geq 0}^J \):

\[ \Sigma_n = DNN_n(|Y_n|^1). \]

\( R_n^{(\text{DNN})} \) is updated as

\[ r_{ijm}^{(\text{DNN})} ← \max(\sigma_{ijm}^2, \epsilon), \]

where \( \sigma_{ijm} \) denotes the \((i,j)\)-th entry of \( \Sigma_n \), and \( \epsilon \) is a small value to avoid numerical instability. The demixing matrix \( W_i \) can be updated with the IP algorithm, as in ILRMA. To reduce the linear distortion, the PB technique is also applied to \( y_{ij} \). The outline of the IDLMA separation process is shown in Fig. 1(b).

The DNNs are trained in advance to extract the target source spectrogram \( \tilde{S}_n \in \mathbb{C}^{I \times J} \) from the single-channel instantaneous noisy mixture \( Y_n \in \mathbb{C}^{I \times J} \). The loss function of training \( DNN_n \) is defined as

\[ L^{(\text{IDLMA})} = \sum_{ij} \left( |\hat{s}_{ijm}|^2 + \delta - \log \frac{|\hat{s}_{ijm}|^2 + \delta}{|s_{ijm}|^2 + \delta} \right), \]

where \( \hat{s}_{ijm} \in \mathbb{R}_{\geq 0} \) and \( s_{ijm} \in \mathbb{C} \) denote the \((i,j)\)-th entry of \( DNN_n(|Y_n|^1) \) and \( \hat{S}_n \), respectively, and \( \delta \) is a small value to prevent division by zero. Since (23) is given by replacing \( w_{in}^H x_{ij} \) with \( |s_{ijm}| \) in (7) up to constants, the minimization of (23) with respect to \( \hat{s}_{ijm} \) can be seen as a simulation of the maximum likelihood estimation with respect to \( r_{ijm}^{(\text{DNN})} \) based on the IDLMA cost function.

### III. PROPOSED METHOD

#### A. Motivation

Since IDLMA uses trained DNNs, its separation performance is affected by the gap in timbre between the DNN training data and the sounds to which IDLMA is applied. Such a timbral gap frequently appears in music audio signals owing to differences in mixing, musical styles, and genres. For example, as a bass instrument, the electric bass guitar is
typically used in rock and pop music, whereas the synth bass is frequently used in electronic music. Although the sounds played by the electric and synth basses are both labeled as bass in the DSD100 dataset [9], their spectral characteristics differ significantly, which can lead to the performance degradation of IDLMA, as we will show later in Section IV. Although one method to address this problem would be to combine them, following the product-of-expert concept [10].

Interestingly, when we set $\beta > 0$, the cost function of the proposed method (27) reduces to that of ILRMA given by (9). If $\alpha = 0$ and $\beta = 1$, the cost function of the proposed method (27) reduces to that of IDLMA.

C. DNN Training and Update Rules

1) Outline of Separation Process: Fig. 2 shows the outline of the separation process of the proposed PoSM-based IDLMA. As in ILRMA and IDLMA, the separation is achieved by iteratively updating the parameters of the PoSM and the demixing matrix. For the PoSM parameters, $\alpha_{ijn}^{(DNN)}$ is updated in the same manner as IDLMA, and $t_{ik,n}$ and $v_{k,n}$ are updated by a convergence-guaranteed algorithm, as we will show in Section III-C3. The variance of the PoSM $\tilde{r}_{ijn}$ is then updated using the current estimates of $t_{ik,n}$, $v_{k,n}$, and $r_{ijn}^{(DNN)}$. The demixing matrix is updated by the IP algorithm followed by the PB technique.

2) DNN Training and Update Rule of $R_n^{(DNN)}$: Since $r_{ijn}^{(NMF)}$ represents the source components independent of the training data, we can set $\alpha = 0$ and $\beta = 1$ during the DNN training, which reduces the cost function (27) to that of IDLMA, as described in Section III-B. This justifies training the DNNs in the same manner as in IDLMA, using the cost function (23). In the separation process, we update $\Sigma_n$ and $R_n^{(DNN)}$ in accordance with (21) and (22), respectively.

3) Update Rules of $R_n^{(NMF)}$: The first and second terms of (27) respectively include the sums over $k$ in the logarithmic function and the denominator of the fractional function. These terms make it difficult to analytically solve the minimization of (27) with respect to $t_{ik,n}$ and $v_{k,n}$. However, we can instead derive a computationally efficient algorithm that iteratively updates $t_{ik,n}$ and $v_{k,n}$ using the MM algorithm [11].

Focusing on the first term of (27), when $\alpha, \beta, r, z > 0$, its second-order derivation with respect to $z$ is always negative:

$$\frac{\partial^2}{\partial z^2} \left[ - \log \left( \frac{\alpha}{z} + \frac{\beta}{r} \right) \right] = -\frac{\alpha(r + 2\beta z)}{z^2(\alpha r + \beta z)^2} < 0. \quad (28)$$

Since $-\log (\alpha/z + \beta/r)$ is concave, by applying the tangent
inequality to the first term of (27), we obtain its upper bound:

\[
- \log \left( \frac{\alpha}{t_{ik,n}} + \frac{\beta}{v_{kj,n}} \right) \leq \frac{1}{\alpha r_{ij,n}^{(\text{DNN})}} \left( \sum_k t_{ik,n} v_{kj,n} - c_{ijn} \right) - \log \left( \frac{\alpha}{c_{ijn}} + \frac{\beta}{r_{ij,n}^{(\text{DNN})}} \right),
\]

(29)

where \( c_{ijn} > 0 \) is an auxiliary variable. The equality of (29) holds if and only if

\[
c_{ijn} = \sum_k t_{ik,n} v_{kj,n}.
\]

(30)

Since \( 1/z \) is convex for \( z > 0 \), we can apply Jensen’s inequality to the second term of (27):

\[
\frac{1}{\sum_k t_{ik,n} v_{kj,n}} \leq \sum_k \frac{\lambda_{ijk,n}^2}{t_{ik,n} v_{kj,n}},
\]

(31)

where \( \lambda_{ijk,n} \) is an auxiliary variable that satisfies \( \lambda_{ijk,n} \geq 0 \) and \( \sum_k \lambda_{ijk,n} = 1 \) for all \( i, j, \) and \( n \). The equality of (31) holds if and only if

\[
\lambda_{ijk,n} = \frac{t_{ik,n} v_{kj,n}}{\sum_k t_{ik',n} v_{kj',n}}.
\]

(32)

By substituting the equality conditions (30) and (32) into (34)
Algorithm 1 Iterative algorithm of proposed method

Input: \(X_1, \ldots, X_M, DNN_1, \ldots, DNN_N\)
Output: \(Y_1, \ldots, Y_N\)

1: for \(l = 1, \ldots, L\) do
2:     for all source index \(n\) do
3:         Update DNN source model \(\mathbf{R}_n^{(DNN)}\) by (21) and (22)
4:     Update source model \(\mathbf{R}_n\) by (26)
5: end for
6: for \(l' = 1, \ldots, L'\) do
7:     for all source index \(n\) do
8:         Update NMF source model \(\mathbf{R}_n^{(NMF)}\) by (36) and (37)
9:     Update source model \(\mathbf{R}_n\) by (26)
10: end for
11: for all frequency bin \(i\) and source index \(n\) do
12:     Update \(w_{ijn}\) by (15) and (16) with (17)
13: end for
14: for all frequency bin \(i\) and time frame \(j\) do
15:     Update \(y_{ij}\) by (5)
16: end for
17: for all frequency bin \(i\) and time frame \(j\) do
18:     Apply PB technique to \(y_{ij}\) by (19) with (20)
19: end for
20: end for
21: end for

4) Update Rule of \(W_i\): Since the cost function (27) is an IP-applicable form, we can reuse the update rule (17) merely by replacing \(r_{ijn}^{(NMF)}\) with \(r_{ijn}\). The PB technique is used as in ILRMA and IDLMA.

5) Summary of Update Rules: The entire separation process of the proposed method is shown in Algorithm 1, where \(L\) denotes the number of DNN-based source model updates and \(L'\) denotes that of NMF-based source model and demixing matrix updates per DNN-based source model update.

IV. EXPERIMENTAL EVALUATION

A. Experimental Setting

To evaluate the effectiveness of the proposed method, we conducted a multichannel music source separation experiment using the DSD100 dataset [9]. We downsampled the audio signals to 8 kHz and used the Hamming window of 512 ms with a shift length of 256 ms for STFT.

As the test data, we created multichannel mixtures by convolving dry sources and the E2A impulse response (reverberation time is 300 ms) in the RWCP database [15]. The dry sources were the 30- to 60-s segments of the top 25 songs in the test set in alphabetical order. We prepared three pairs of instruments: vocal and bass (Vo./Ba.), bass and drums (Ba./Dr.), and vocal and drums (Vo./Dr.). Fig. 3 shows the two recording conditions, and the number of the multichannel mixes for each instrument pair was 50.

We compared the proposed method with ILRMA [6] and IDLMA [8]. In accordance with the experimental conditions used in [6] and [8], we set \(L = 10\) and \(L' = 10\) for both IDLMA and the proposed method. Since ILRMA does not use the DNNs, its NMF parameters and demixing matrix were updated for 100 iterations, i.e., we set the number of NMF parameter updates to be the same as in the proposed method. In accordance with [8], the number of bases for NMF was \(K = 20\) for both ILRMA and the proposed method. The sourcespecific DNN consists of five fully connected (FC) blocks, each of which consists of an FC layer with 2048 hidden units and a rectified linear unit (ReLU) nonlinearity. A dropout layer with a drop rate of 0.3 was placed after each ReLU in the FC blocks except for the last one. As described in Section III-C2, the proposed method can use the DNNs trained in the same manner as in IDLMA, and we used the same trained DNNs for IDLMA and the proposed method. In the proposed method, we varied \(\alpha\) from \(5 \times 10^{-1}\) to \(1 \times 10^{-5}\) with the constraint of \(\alpha + \beta = 1\).

B. DNN Training

We used all 50 songs in the dev set of the DSD100 dataset for DNN training, and the bottom 25 songs in alphabetical order in the test set for the validation. During the DNN training, as described in Section II-C, single-channel noisy mixtures were created. The mixtures were created as described in [16]. The DNNs were trained for 2000 epochs on an Adadelta [17] optimizer with a batch size of 128. The learning rate was set to 1.0 with a weight of \(l^2\) regularization of \(10^{-5}\). We clipped the norm of the gradients of the DNN parameters before the parameter updates so that their \(l^2\) norms were less than or equal to 10. The other hyperparameters were set as \(\delta = 10^{-5}\) and \(\varepsilon = 10^{-1}\), following [8].
Fig. 4 SDR improvements of proposed method with varying $\alpha$ and of conventional methods.

Fig. 5 Examples of SDR improvements of IDLMA and of proposed method for Ba./Dr.

C. Results

Fig. 4 shows the average source-to-distortion ratio (SDR) improvements over 50 mixtures of test data for each instrument pair, which were computed with the BSSEval toolbox [18]. Compared with ILRMA, IDLMA provided SDR improvements of more than 3 dB higher in Vo./Ba. and Vo./Dr. separations. However, for Ba./Dr., IDLMA provides an SDR improvement of only 0.4 dB higher than ILRMA, which is lower than for the other instrument pairs. This may be because the spectrograms of bass and drums are likely to be of low-rank, which fits the assumption of NMF. On the other hand, the proposed method outperformed IDLMA with the appropriate choice of $\alpha$ for any instrument pair, showing the effectiveness of the proposed method.

Fig. 5 shows the average SDR improvement at each iteration for IDLMA and the proposed method with $\alpha = 5 \times 10^{-1}$. The results were for the Ba./Dr. mixture and averaged over the two instruments. In IDLMA, the SDR improvements at the DNN updates increased until the 40th iteration, but they decreased at subsequent iterations, as shown in Fig. 5(a). Although most of the DNN training data labeled as bass were performed by the electric bass guitar, the bass sound of this musical piece was performed by the synth bass. This result shows the performance degradation caused by the timbral discrepancy between the DNN training data and the data to which IDLMA was applied. On the other hand, the SDR improvements of the proposed method did not decrease even after approximately the 40th iteration. This phenomenon can also be observed in Fig. 5(b). The drums sound of this musical piece was performed by the conga, which was not included in the training data. Although the average SDR improvements of IDLMA seemed to reach the upper performance limit, the proposed method gave higher average SDR improvements in the later iterations. These results show that the introduction of the source model independent of the DNN training data reduces the performance degradation caused by the timbral gap.

V. Conclusion

We proposed the PoSM by combining the DNN- and NMF-based source models, which are respectively used in IDLMA and ILRMA. The DNN-based part represents the components similar to the training data, and the NMF-based part represents the components independent of the training data. We introduced the PoSM into IDLMA to develop the PoSM-based IDLMA and derived the computationally efficient separation algorithm of its parameters. For the NMF parameters, we derived the convergence-guaranteed iterative algorithm based on the MM algorithm. Through the multichannel music source separation experiments, we showed the effectiveness of the proposed PoSM-based IDLMA. Furthermore, we showed that the use of the PoSM reduces the performance degradation caused by the timbral discrepancy.
caused by the timbral gap between the DNN training data and the sounds to which the proposed method is applied.

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