Off-Line Handwritten Signature Identification Using Rotated Complex Wavelet Filters

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Abstract
In this paper, a new method for handwritten signature identification based on rotated complex wavelet filters is proposed. We have proposed to use the rotated complex wavelet filters (RCWF) and dual tree complex wavelet transform (DT-CWT) together to derive signature feature extraction, which captures information in twelve different directions. In identification phase, Canberra distance measure is used. The proposed method is compared with discrete wavelet transform (DWT). From experimental results it is found that signature identification rate of proposed method is superior over DWT.

Keywords: Signature identification, rotated complex wavelet filters, discrete wavelet transform person’s identification.

1. Introduction

1.1 Motivation
Authentication and affirmation of statements, documents, scripts etc, from times immemorial has been done through signatures. Even today, where every thing has gone digital, signature plays a vital role. They appear on many types of documents such as bank cheques, credit cheques, governmental documents, wills over assets of a person and many other documents of greater importance. But this type of authentication is also subject to mal practices and crimes. Forgery and imitation of signatures of other person may help anyone to gain access to his/her valuable assets or can lead to undesirable consequences. Identification of signatures by human eye and study may be error prone and manipulative, thus an automated document processing system that can analyze and identify a signature serves as an effective, useful and less error prone and non manipulative tool.

Signature’s validity confirmation for different documents is an important problem domain in automatic document processing. An area where signature identification finds application is in banking, user login in computers or PDA (Personal digital assistant), for access control, to check for authentication of official documents etc. There are two modes for signature identification and verification: Static or off-line and Dynamic or on-line. In static mode, the input of system is a 2D image of signature. Contrary to this, in dynamic mode, the input is signature trace in time domain. In the Dynamic mode, the person puts his signature on an electronic tablet through an electronic pen. His/ her obtained signature is sampled with each sample having three attributes: The 2- dimensional co-ordinates; x and y and time of sample occurrence, t. The time attribute of each sample is used to extract useful information such as start and stop points, velocity and acceleration of the signature stroke. Some electronic tablets in addition to time sampling can digitize the pressure. Such additional information in the dynamic mode increases identification rate as compared to the static mode. But Dynamic mode has a greater disadvantage: it is on-line, hence it requires presence of the person whose signature is needed and that too has been taken digitally. Thus it cannot be applied to other important cases where there is absence of person whose sign is needed and cases where analysis and identification needs to be carried out of existing documents with signature marks. Thus off-line signature verification becomes an inevitable choice and finds universal application.

1.2 Related works
Signature verification contain two areas: off-line signature verification, where signature samples are scanned into image representation and on-line signature verification, where signature samples are collected from a digitizing tablet which is capable of pen movements during the writing. In 2009, Ghandali and Moghaddam have proposed an off-line Persians signature identification and verification based on Image registration, DWT (Discrete Wavelet Transform) and fusion. They used DWT for features extraction and Euclidean distance for comparing features. It is language dependent method [1]. In 2008, Larkins and Mayo have introduced a person dependent off-line signature verification method that is based on Adaptive Feature Threshold (AFT) [2]. AFT enhances the method of converting a simple feature of signature to binary feature vector to improve its...
representative similarity with training signatures. They have used combination of spatial pyramid and equimass sampling grids to improve representation of a signature based on gradient direction. In classification phase, they used DTW and graph matching methods. In another work, Ramachandra et al [3], have proposed cross-validation for graph matching based off-line signature verification (CSMOSV) algorithm in which graph matching compares signatures and the Euclidean distance measures the dissimilarity between signatures.

In 2007, Kovari et.al [4] presented an approach for off-line signature verification, which was able to preserve and take usage of semantic information. They, used position and direction of endpoints in features extraction phase. Porwik [5] introduced a three stages method for offline signature recognition. In this approach the Hough transform ,center of gravity and horizontal-vertical signature histogram have been employed, using both static and dynamic features that were processed by DWT has been addressed in[6].The verification phase of this method is based on fuzzy net using the enhanced version of the MDF(Modified Direction feature)extractor has been presented by Armand et.al [7].The different neural classifier such as Resilient Back Propagation(RBP) neural network and Radial Basis Function(RBF)network have been used in verification phase of this method. In 2005, Chen and Srihari [8] described an approach that obtains an exterior contour of the image to define pseudo writing path. To match two signatures a dynamic time wrapping (DTW) method has been employed to segment signature into curves.

The main contribution of this paper is that, we have proposed an off-line handwritten signature identification using rotated complex wavelet filters and dual tree complex wavelet transform, which captures information in twelve different directions for identification. In identification phases Canberra distance measure is used. The experimental results of proposed method were satisfactory and found that it gives better results as compared with earlier approach. The rest of paper is organized as follows. In section 2, discusses the feature extraction phase. The signature identification approaches is presented in section 3. In section 4, the experimental results and the selection of training samples are presented, and finally section 5 concludes the work.

2. Feature Extraction Phase

The major task of feature extraction is to reduce image data to much smaller in size which represents the important characteristic of the image. In signature identification, edge information is very important in characterizing signature properties. Therefore we proposed the use of DT-CWT and DT-RCWF jointly, which captures the information in twelve different directions. The performance of the system is compared with standard discrete wavelet transform which captures information in only three directions.

2.1 Discrete Wavelet Transform Features

The multi resolution wavelet transform decomposes a signal into low pass and high pass information. The low pass information represents a smoothed version and the main body of the original data. The high pass information represents data of sharper variations and details. Discrete Wavelet Transform decomposes the image into four sub-images when one level of decomposing is used. One of these sub-images is a smoothed version of the original image corresponding to the low pass information and the other three ones are high pass information that represents the horizontal, vertical and diagonal edges of the image respectively. When two images are similar, their difference would be existed in high-frequency information. A DWT with N decomposition levels has 3N+1 frequency bands with 3N high frequency bands [9]. The impulse response associated with 2-D discrete wavelet transform are illustrated in Fig. 1 as gray-scale image.

![Fig.1. Impulse response of 0°, 90° and ±45° of DWT](image)

2.2 Dual Tree Rotated Complex Wavelet Filters

Drawbacks of the DWT are overcome by the complex wavelet transform (CWT). By introducing limited redundancy into the transform. But still it suffer from problem like no perfect reconstruction is possible using CWT decomposition beyond level 1, when input to each level becomes complex. To overcome this, Kingsbury [11] proposed a new transform, which provides perfect reconstruction along with providing the other advantages of complex wavelet, which is DT-CWT. The DT-CWT uses a dual tree of real part of wavelet transform instead using complex coefficients. This introduces a limited amount of redundancy and provides perfect reconstruction along with providing the other advantages of complex wavelets. The DT-CWT is implemented using separable transforms and by combining subband signals appropriately. Even though it is non-separable yet it inherits the computational efficiency of separable transforms. Specifically, the 1-D DT-CWT is implemented using two filter banks in parallel, operating on the same data. For d-dimensional input, a L scale DT-CWT outputs an array of real scaling coefficients corresponding to the low pass subbands in each dimension. The total
redundancy of the transform is $2^d$ and independent of $L$. The mechanism of the DT-CWT is not covered here. See [10], [12-13] for a comprehensive explanation of the transform and details of filter design for the trees. A complex valued $\psi(t)$ can be obtained as

$$\psi(t) = \psi_h(t) + j \psi_g(t)$$  \hspace{1cm} (1)

Where $\psi_h(t)$ and $\psi_g(t)$ are both real-valued wavelets. The impulse responses of six wavelets associated with 2-D dual tree complex wavelet transform are illustrated in Fig. 2.

2.3 Dual Tree Rotated Complex Wavelet Filters

Directional 2D RCWF are obtained by rotating the directional 2D DT-CWT filters by $45^\circ$ so that decomposition is performed along new direction, which are apart from decomposition $45^\circ$ directions of CWT[10]. The size of a filter is $(2N-1) \times (2N-1)$, where $N$ is the length of the 1-D filter. The decomposition of input image with 2-D RCWF followed by 2-D down sampling operation is performed up to the desired level. The computational complexity associated with RCWF decomposition is the same as that of standard 2-D CWT, if both are implemented in the 2-D frequency domain. The set of RCWFs retains the orthogonal property. The six sub bands of 2D DT-RCWF gives information strongly oriented at $(30^\circ, 0^\circ, -30^\circ, 60^\circ, 90^\circ, 120^\circ)$. The mechanism of the DT-RCWF is not covered here. See [10],[12-13] for a comprehensive explanation of the transform and details of filter design for the trees. Thus, the 2D DT-CWT and RCWF provide us with more directional selectivity in the direction

$$\left\{ +15^\circ, +45^\circ, +75^\circ, -15^\circ, -45^\circ, -75^\circ \right\} \text{ than } \left\{ 0^\circ, +30^\circ, +60^\circ, +90^\circ, 120^\circ, -30^\circ \right\}$$

the DWT whose directional sensitivity is in only three directions $\left\{ 0^\circ, \pm 45^\circ, 90^\circ \right\}$. The six wavelets associated with rotated complex wavelet transform are illustrated in Fig.3.

2.4 Feature Database Creation

To conduct the experiments, we were computed two different feature sets using algorithm 1 and algorithm 2, which uses DWT and combined DT-CWT and DT-RCWF respectively. To construct the feature vectors of each signature in the database, we decomposed each signature using DT-CWT and DT-RCWF up to $6^{th}$ level. The Energy and Standard Deviation (STD) were computed separately on each sub band and the feature vector was formed using these two parameter values. The Energy $E_k$ and Standard Deviation $\sigma_k$ of $k^{th}$ sub band is computed as follows

$$E_k = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} W_k(i,j)$$  \hspace{1cm} (2)

$$\sigma_k = \left[ \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} (W_k(i,j) - \mu_k)^2 \right]^{1/2}$$  \hspace{1cm} (3)

Where $W_k(i,j)$ is the $k^{th}$ wavelet-decomposed sub band, $M \times N$ is the size of wavelet decomposed sub band, and $\mu_k$ is the mean of the $k^{th}$ sub band. The resulting feature vector using energy and standard deviation are $\bar{f}_E = [E_1 \ E_2 \ ... \ E_n]$ and $\bar{f}_\sigma = [\sigma_1 \ \sigma_2 \ ... \ \sigma_n]$ respectively. So combined feature vector is $\bar{f}_{E\sigma} = [\sigma_1 \ \sigma_2 \ ... \ \sigma_n \ E_1 \ E_2 \ ... \ E_n]$  \hspace{1cm} (4)

The step by step procedure for feature database creation using discrete wavelet transform and combined DT-CWT and DT-RCWF are explained in algorithm 1 and algorithm 2 respectively.

**Algorithm 1:** Feature database creation using DWT

**Input:**
- Signature image Database: DB
- 1D filters : LF, HF
- Handwritten Signature : $S_i$

**Output:** Feature database $FV$

**Begin**

For each $S_i$ in DB do

Decompose the $S_i$ by applying low pass LF and high pass HF filters up to $6^{th}$ level

Calculate energy $E$ and standard deviation $SD$ for each subband using (2) and (3) respectively in each level

Feature vector $f = [E \ U \ SD]$

$FV = FV \ U \ f$

**End for**

**End**
Algorithm 2: Feature database creation using DT-CWT and DT-RCWF

Input:
Signature image Database: DB
2D DT-CWT filters : F
Handwritten Signature : Si

Output:
Feature database : FV

Begin
If DT-RCWF
Rotate 2D filters F by 45°
End if
For each Si in DB do
Decompose the Si by applying 2D filters F up to 6th Level. Calculate energy E and standard deviation SD for each subband using (2) and (3) respectively in each level
Feature vector f= [E U SD]
FV=FV U f
End for
End

3. Signature Identification Phase

There are several ways to work out the distance between two points in multidimensional space. We have used Canberra distance metric as distance measure. If x and y are the feature vectors of the database and query signature, respectively, and have dimension d, then the Canberra distance is given by

\[ \text{Canb}(x, y) = \sum_{i=1}^{d} \frac{|x_i - y_i|}{|x_i| + |y_i|} \]  

(5)

The step by step procedure of identification is as follows,

Algorithm 3: Handwritten Signature Identification

Input: Test signature: St
Feature database: FV

Output: Distance vector: Dist
Handwritten signature identification

Begin
Calculate feature vector of test signature St using algorithm 1
For each fv in FV do
Dist= Calculate distance between test signature and fv using (5)
End for
Display the minimum distance signature from distance vector.
End

4. Experimental Results

4.1. Image Database

The signatures were collected using either black or blue ink (No pen brands were taken into consideration), on a white A4 sheet of paper, with eight signature per page. Signatures were scanned subsequently to digitize individual with a resolution in 256 grey levels. Images were obtained in rectangular areas of size 256x256 pixels. Sample signature image database is shown in Fig.3. A group of 52 persons are selected for 16 specimen signatures which make the total of 52x16=832 signature database.

![Fig.3. Sample Signature Images Database](image)

4.2. Identification Performance

For each person 12 signatures for training and 4 signatures for testing are used. This makes the total of 4x52=208 signature. The identification rate is 90.6% using proposed method and 61.45 % using DWT. Fig.4 shows comparison between DWT and proposed method. From Fig. 4, we observed that signature identification rate of proposed method is superior over DWT.
5. Conclusions

In this paper, we introduced new approach for identification of off-line signatures. The proposed approach uses RCWF and DT-CWT jointly for extracting details in twelve different directions and Canberra distance for comparing features. The experimental results we found that signature identification rate for proposed method is superior over DWT.

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References

[1] Samanesh Ghandali and Mohsen Ebrahimi Moghaddam, “Off-Line Persian Signature Identification and Verification based on Image Registration and Fusion” In: Journal of Multimedia, volume 4, 2009, pp. 137-144.

[2] Larkins, R. Mayo, M., “Adaptive Feature Thresholding for Off-Line Signature Verification”, In: Image and vision computing New Zealand, 2008, pp. 1-6.

[3] Ramachandra, A.C. Pavitra, K.and Yashasvini, K. and Raja, K.B. and Venugopul, K.R. and Patnaik, L.M., “Cross-Validation for Graph Matching based Off-Line Signature Verification”, In IDICON 2008, India, 2008, pages: 17-22.

[4] Kovari, B. Kertesz, Z. and Major, a., “Off-Line Signature Verification Based on Feature Matching: In: Intelligent Engineering Systems, 2007, pp. 93-97.

[5] Porwik P., “The Compact Three Stages Method of the Signatures Recognition”, 6 th International Conference on Computer Information Systems and Industrial Management Applications, 2007, pp. 282-287.

[6] Wei Tian Yizheng Qiao Zhiquiang Ma, “A New Scheme for Off-Line Signature Verification uses DWT and Fuzzy net”, In: Software Engineering, Artificial Intelligence, Networking and Parallel/Distributed Computing, 2007, pages: 30-35.

[7] Armand S., Blumenstein, M., Muthukkumarasamy V. “Off-Line Signature and Neural Based Classification”, In: Neural Networks, 2006 IJCNN, pp.: 684-691.

[8] Chen S., Srikari S., “Use of Exterior Contours and Shape Features in Off-Line Signature Verification”, In: Eighth International Conference Document Analysis and Recognition, 2005, pp. 1280-1284.

[9] Gogoi Pajares, Jesus, Mahuel de la Cruz, “A wavelet-based image fusion Tutorial”, Pattern Recognition Volume 37, Issue 9, September 2004, Elsever Science Inc, pp. 1855-1872.

[10] Manesh Kokare, P.K. Biswas, and B.N. Chatterji, “Texture Image retrieval using New Rotated Complex Wavelet Filters,” IEEE Trans. on systems, man, and Cybernetics-Part B: Cybernetics, vol. 35, no.6, Dec. 2005

[11] N.G. Kingsbury, “Image processing with complex wavelet,” Phil. Trans. Roy. Soc.

[12] N. G. Kingsbury, “Complex wavelets for shift invariant analysis and filtering of signals,” J.App. Comput. Harmon. Anal., vol. 10, no.3, pp.234-253, May 2001.

[13] I. Selesnick, R. Baraniuk, and N. Kingsbury, “The dual-tree complex wavelet transform,” IEEE Signal Process. Mag., vol.22, no. 06, pp.123-151, Nov. 2005.

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