CRT-Based Color Image Zero-Watermarking on the DCT Domain

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ABSTRACT
When host images are watermarked with CRT (Chinese Remainder Theorem), the watermark images are still robust in spite of the damage of the host images by maintaining the remainders in an unchanged state within some range of the changes that are incurred by the attacks. This advantage can also be attained by “zero-watermarking,” which does not change the host images in any way. This paper proposes an improved zero-watermarking scheme for color images on the DCT (Discrete Cosine Transform) domain that is based on the CRT. In the scheme, RGB images are converted into YCbCr images, and one channel is used for the DCT transformation. A key is then computed from the DC and three low-frequency AC values of each DCT block using the CRT. The key finally becomes the watermark key after it is combined four times with a scrambled watermark image. When watermark images are extracted, each bit is determined by majority voting. This scheme shows that watermark images are robust against a number of common attacks such as sharpening, blurring, JPEG lossy compression, and cropping.

Key words: CRT, Color Images, DCT, Watermarking, Zero-watermarking.

1. INTRODUCTION
Digital watermarking is the process for hiding a digital watermark into a digital signal such as image data. As the age of Internet and multimedia advances, such a technique for protecting intellectual property of digital contents from illegal usage becomes more and more important. Most methods of digital watermarking modify the original data while embedding the watermark [1]. The secret watermark information distorts more or less the original data at the same time. This incurs a conflict between robustness and invisibility.

Zero-watermarking was proposed for solving this conflict. It is a way to build some connection between the original data and the watermark [2]. There is no distortion of the original data in building the connection. That is, the distortion problem to the original data due to watermark embedding is completely eliminated. After retrieving the so-called relationship, it could be stored in a watermark registration center, where it became the resource for copyright protection. The most important part of a zero-watermarking method is the image feature detection method [3]. Two desirable properties are stability and otherness. The one is the ability to detect the image feature after it is attacked. The other is the ability to differentiate the image features from those of different images.

Chinese remainder theorem (CRT) [4] is about how to find an integer, when some divisors and their corresponding remainders are given. The use of the CRT in watermarking gray images provides advantage in terms of improved security and low computational complexity as the study of Patra et al. [5] shows. In addition, CRT-based watermarking is robust by keeping remainders unchanged within some range of changes in spite of distortion in host images.

For employing this advantage of CRT in zero-watermarking, DCT0CRT (DCT domain Zero-watermarking based on CRT) [6] was proposed. It is a CRT-based zero-watermarking technique for gray images in the domain of DCT. Among the DC and two low-frequency AC coefficients of each DCT block chosen in a chaotic way from the original data (i.e. host image in image watermarking), one is selected by testing whether it satisfies the CRT-based condition matching with the watermark bit to be embedded. The first element of the DCT block, i.e. the DC coefficient, is the average of the pixel values, while the remaining elements, i.e. AC coefficients, are independent of the average. Low frequency AC coefficients represent gradual color change across the pixel values. That is, the most stable and important coefficients of each DCT block are used for building the relationship. Experimental results show that inserted watermarks are robust against some common attacks such as sharpening, blurring, and JPEG lossy compression. However, DCT0CRT is just for gray images and has some drawbacks in protecting host images against attacks such as cropping. This paper proposes how to apply CRT-based zero-watermarking to color images with enhanced robustness by improving the drawbacks.

The rest of the paper is organized as follows: Section 2 reviews the previous work in the area of CRT-based DCT-domain watermarking. The zero-watermarking scheme for color images is then proposed in Section 3. The experimental
results and performance comparison with the other two schemes introduced in Section 2 are provided in Section 4. Finally, the paper is summarized with some future research directions in Section 5.

2. RELATED WORK

2.1 CRT

The theorem can be compactly defined as follows [5]. Let \( \mu \) be a set of \( r \) integers given by \( \mu = \{ M_1, M_2, \ldots, M_r \} \), such that any two \( M_i \) are pair-wise relatively prime. Let’s assume that a set of \( r \) simultaneous congruences be given by

\[
Z \equiv R_1 \pmod{M_1}, \quad (1)
\]

where \( R_i, i = 1, 2, \ldots, r \), are called residues. The solution for the integer \( Z \) can be found as

\[
Z \equiv \left( \sum_{i=1}^{r} R_i \frac{M}{M_i} K_i \right) \pmod{M}, \quad (2)
\]

where \( M \) is the product of all \( M_i \) and \( K_i \) are determined from

\[
K_i \frac{M}{M_i} \equiv 1 \pmod{M_i} \quad (3)
\]

Let us take a simple example with \( r = 2, M_1 = 7, M_2 = 9 \). \( R_1 = 3 \) and \( R_2 = 4 \). That is, \( Z \) satisfies the two congruences: \( Z \equiv R_1 \pmod{M_1} \) and \( Z \equiv R_2 \pmod{M_2} \). \( M = 55 \) by the product of \( M_1 \) and \( M_2 \). \( K_1 \) and \( K_2 \) are determined by the two congruences \( K_1, M_2 \equiv 1 \pmod{M_1} \) and \( K_2, M_1 \equiv 1 \pmod{M_2} \). We can find that \( K_1 = 4 \) and \( K_2 = 4 \) satisfy the congruences. From \( Z \equiv R_1 M_2 K_1 + R_2 M_1 K_2 \pmod{M} \), we can conclude that \( Z = 31 \).

Inverse CRT is to represent a positive integer \( Z \) (which is less than \( M \)) by a set of integers \( \{ R_1, R_2, \ldots, R_r \} \) given \( \mu \) and \( M \). Each \( R_i \) is obtained from the congruence (1). Let us take a simple example with \( M_1 = 7, M_2 = 9, Z = 49 \). From \( 49 \equiv R_1 \pmod{7} \) and \( 49 \equiv R_2 \pmod{9} \), we can find that \( R_1 = 0, R_2 = 4 \). Therefore, \( Z \) can be represented as \( \{0, 4\} \).

2.2 CRT-Based Watermarking on the DCT Domain

Digital watermarking techniques can be classified into two categories: spatial-domain techniques and transform-domain techniques [7]. The former techniques modify the pixel values of the host image. On the other hand, the latter techniques first convert the host image into frequency domain by a transformation method such as discrete cosine transform (DCT), discrete Fourier transform (DFT), discrete wavelet transform (DWT), and so on. Transform-domain coefficients are then modified by the watermark. Inverse transform is finally applied to obtain the watermarked image. Transform-domain techniques are generally more robust against attacks than spatial-domain ones.

A discrete cosine transform (DCT) expresses a finite sequence of data points in terms of a sum of cosine functions oscillating at different frequencies. There are several variants of the DCT with slightly modified definitions. The most commonly used form can be expressed by the following equation. \( N \) real numbers \( x_0, \ldots, x_{N-1} \) are transformed into \( N \) real numbers \( X_0, \ldots, X_{N-1} \) according to the equation.

\[
X_k = \sum_{n=0}^{N-1} x_n \cos \left( \frac{\pi}{N} (n + \frac{1}{2}) k \right), \quad k = 0, 1, \ldots, N - 1 \quad (4)
\]

DCT is usefully employed in diverse science and engineering applications, e.g. JPEG lossy image compression, where \( N \) is typically 8. The 64 coefficients of a JPEG DCT block are arranged in a sequence of Fig. 1 in which the left-top element is the DC (zero-frequency) component and entries with increasing vertical and horizontal index values represent higher vertical and horizontal spatial frequencies. The DC coefficient is the average of the pixel values, while the remaining elements, i.e. AC coefficients, are independent of the average. Low frequency AC coefficients represent gradual color change across the pixel values.

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---|---|---|---|---|---|---|---|
| 0 | 1 | 5 | 6 | 14 | 15 | 27 | 28 |
| 1 | 2 | 4 | 7 | 13 | 16 | 26 | 29 |
| 2 | 3 | 8 | 12 | 17 | 25 | 30 | 41 |
| 3 | 9 | 11 | 18 | 24 | 31 | 40 | 44 |
| 4 | 10 | 19 | 23 | 32 | 39 | 45 | 52 |
| 5 | 20 | 22 | 33 | 38 | 46 | 51 | 55 |
| 6 | 21 | 34 | 37 | 47 | 50 | 56 | 59 |
| 7 | 35 | 36 | 48 | 49 | 57 | 58 | 62 |

Fig. 1. Sequence numbers of coefficients of a DCT block

Based on the CRT properties, a CRT-based DCT-domain watermarking scheme has been reported in [5] in order to improve a CRT-based spatial-domain watermarking scheme [8] whose main drawback is its inability to withstand JPEG compression. CRT is mainly employed in watermarking for increasing security. A large integer \( Z \) can be represented by a set of smaller integers called residues of dividing it by a set of relatively prime numbers. Such computation is efficient due to the CRT properties of simultaneous congruence and modular arithmetic. On the contrary, it is very difficult to get back the original integer \( Z \) without knowledge of the set of divisors.

The scheme embeds one watermark bit per DCT block by checking the required condition of \( d\equiv D/s \) for watermark bit 1 and of \( d\equiv D/s \) for watermark bit 0, where \( d = \text{abs}(R1-R2), R1 = Z \pmod{M1}, R2 = Z \pmod{M2}, D = \text{max}(M1,M2) \) - 1. Is = 2 if \( Z \) is DC coefficient, otherwise, \( s = 4 \). M1 and M2 are the pair-wise co-prime numbers to be used in the CRT. If the condition does not satisfy, then 8 is added to or subtracted from \( Z \) recursively until the condition satisfies. The reason for using \( \pm 8 \) to make
modifications to the selected DCT coefficient is that it provides sufficient amount of modification in the DCT domain that would be reflected in the spatial domain [5]. However, it is inevitable that this modification degrades the quality of the host image in spite of much effort for maintaining imperceptibility.

2.2 CRT-Based Zero-Watermarking on the DCT Domain

Zero-watermarking was proposed for solving the conflict between robustness and invisibility in conventional digital watermarking, where the secret watermark information embedded into the host image distorts more or less the original data. Instead of watermark embedding, zero-watermarking extracts some distinctive features from the host image. As a result, there is no distortion of the original data in zero-watermarking. The owner’s information is not reflected in the image features because they are just meaningless bit stream. An encryption method can be employed for embedding meaningful information into the features. The zero-watermark is then stored in a watermark registration center, where it becomes the resource for copyright protection.

Two desirable properties of zero-watermarking are stability and othersness [3]. The one is the ability to detect the image features after it is attacked. The other is the ability to differentiate the image features from those of different images. For supporting the properties, there are many fields of research on image zero-watermarking [9]: spatial-domain, transform-domain, image moment, principal components analysis, and so on.

DCT has been a hot topic for the digital watermarking in transform domain because it needs less computation and is compatible with the international standards of data compression [10]. Based on DCT, a zero-watermarking method DCT0CRT for gray images was introduced by Kim and Sohn [6], where CRT was applied to one of DC and 2 low-frequency AC values of each DCT block chosen by a chaotic way. The method tries to embed one watermark bit per DCT block by checking the required condition of \( d = \frac{D}{s} \) for watermark bit 1 and of \( d < \frac{D}{s} \) for watermark bit 0, where \( d = \text{abs}(R1-R2) \), \( R1 = Z \mod M1 \), \( R2 = Z \mod M2 \), \( D = \max(M1,M2) - 1 \). The same variables are used as in the CRT-based DCT-domain watermarking scheme. If the condition satisfies with DC, two bits of ‘00’ are added to the private key K. If not, the two AC coefficients are checked sequentially. Two bits of ‘01’ or ‘10’ are added to the private key, if the condition satisfies. Otherwise, two bits of ‘11’ are added to the private key.

The use of the CRT in the zero-watermarking method provides advantage in terms of improved security and low computational complexity as in conventional watermarking [5]. In addition, it is robust by keeping watermark data from damage in spite of some degree of the host image distortion. This enhances the stability of the zero-watermarking. However, the method does not consider color images and the key does not catch the image features. Furthermore, the method does not use any encryption method to embed meaningful information into image features or the key.

Simple DCT-based zero-watermarking methods are also proposed for protecting medical images [10] and text images [11]. They are using signs of low-frequency AC coefficients of DCT blocks as the zero-watermark. They are also just for gray images.

3. PROPOSED SCHEME FOR COLOR IMAGES

Current zero-watermarking algorithms mainly focus on the methods of embedding watermarks into the gray host image in spite of much research on the conventional watermarking algorithms for color images [12]. Based on the DCT0CRT, this paper proposes an improved zero-watermarking algorithm for color images.

3.1 Watermark Embedding Procedure

In the first phase, a RGB host image is converted to YCbCr color space by the following equations, where Y component is luminance, Cb component blue chrominance, and Cr component red chrominance.

\[
\begin{align*}
Y &= 0.299 * R + 0.587 * G + 0.114 * B \\
Cb &= -0.168736 * R - 0.331264 * G + 0.5 * B + 128 \\
Cr &= 0.5 * R - 0.418688 * G - 0.081312 * B + 128
\end{align*}
\]

This is done because the latter is more robust and has higher imperceptibility than the former [13]. The algorithm uses the blue chrominance component for extracting features from the cover(host) image on the basis of HVS (Human Visual System). According to the HVS, the higher the background luminance and the more complicated the image texture, the lower the human visual system’s sensitivity to its variations. In order to get better transparency, it is strongly recommended to select those blocks with high luminance and complicated texture for the conventional image watermarking [14]. There were largely two approaches for block selection in the conventional image watermarking: the selection of best blocks [14] and the selection of a best region such as a quadrant [13]. In order to simplify the zero-watermarking process, the algorithm removes the complex selection of blocks or regions. Instead, the algorithm adopts multiply embedding the watermark image into regions such as quadrants.

In the watermark embedding process, scrambling transformation is applied to the binary watermark \( W \), where the watermark image becomes a meaningless chaotic one. It plays the role of secondary encryption of the watermark image via upsetting the relationship between the space locations of pixels [15]. This will improve the robustness of the algorithm. Two-dimensional Arnold scrambling as follows is used:

\[
\begin{bmatrix}
x' \\
y'
\end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix} \mod N, \quad x, y \in \{0,1,\ldots,N-1\}
\]

The pixel coordinates of the original space are \( x \) and \( y \), while those after scrambling are \( x' \) and \( y' \). \( N \) is the size of the rectangular image, also referred to as a step number. The transformation can be applied iteratively taking \( K \) as the iteration number.

The initial state can be restored according to the corresponding iterations by the following equation.
The watermark embedding algorithm can be described as follows:

1. Divide the host image \( I \) into 8x8 pixels blocks.
2. Set the private key \( K \) to blank.
3. For each block:
   A. Apply DCT conversion to the block.
   B. Select DC and 3 low-frequency AC coefficients of a block to extract the features of the host image.
   C. Let \( M_1 \) and \( M_2 \) be the pairwise co-prime numbers to be used in CRT with values 38 and 107, respectively, in the case of DC. Otherwise, those of \( M_1 \) and \( M_2 \) are selected as 38 and 55, respectively.
   D. Find \( R_1 \) and \( R_2 \) by applying the inverse CRT to the selected DC and AC coefficients.
   E. Determine \( d = \text{abs}(R_1-R_2) \) and \( D = \max(M_1,M_2) - 1 \).
   F. Add ‘1’ bit to the private key \( K \) if \( d \geq D/s \). Otherwise, add ‘0’ bit to \( K \).

(4) Scramble the watermark image \( W \) of size \( m \times n \) with \( IN \) as the iteration number of Arnold transformation into the scrambled watermark \( SW \).

(5) Apply bitwise XOR operations to the key \( K \) and a multiple of the scrambled watermark \( MSW \) in order to build the watermarked key. The multiple is noted as \( MSW' \).

(6) Register the watermarked key into the third party to preserve the ownership of the host image.

3.2 Watermark Extraction Procedure

The process of acquiring the features of a test image is the same as in steps (1)-(3) of the watermark embedding procedure. Let the features (i.e. the private key of the test image) be noted as \( K' \). The watermark extraction algorithm can be summarized as follows:

1. Divide the test image \( I' \) into 8x8 pixels blocks.
2. Set the private key \( K' \) to blank.
3. For each block:
   A. Apply DCT conversion to the block.
   B. Select DC and 3 low-frequency AC coefficients of a block to extract the features of the test image.
   C. Let \( M_1 \) and \( M_2 \) be the pairwise co-prime numbers to be used in CRT with values 38 and 107, respectively, in the case of DC. Otherwise, those of \( M_1 \) and \( M_2 \) are selected as 38 and 55, respectively.
   D. Find \( R_1 \) and \( R_2 \) by applying the inverse CRT to the selected DC and AC coefficients.
   E. Determine \( d = \text{abs}(R_1-R_2) \) and \( D = \max(M_1,M_2) - 1 \).
   F. Add ‘1’ bit to the private key \( K' \) if \( d \geq D/s \). Otherwise, add ‘0’ bit to \( K' \).

(4) Apply bitwise XOR operations to the private key \( K' \) of the test image and the watermarked key \( K \), fetched from the third party, in order to extract multiple scrambled images, denoted as \( MSW' \).

(5) Unscramble \( MSW' \) with \( IN \) as the iteration number of Arnold transformation into multiple images \( MW' \).

(6) Determine the extracted watermark image \( W' \) from \( MW' \) using a strategy such as voting and best region selection. In the voting strategy, each region votes for the bit value of a specific position of the extracted watermark image. This strategy does not need the watermark image. On the other hand, in the best region selection strategy, one region such as a quadrant of \( MW' \) is selected as \( W' \) for best matching the watermark image. Tamper Assessment Function (TAF) [16] as follows can be used for selecting the best region.

\[
TAF(W,W') = \frac{1}{mn} \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} W(i,j) \oplus W'(i,j) \times 100
\]

(7) Calculate TAF between \( W \) and \( W' \). Given a watermark detection threshold \( T \), if \( TAF < T \), then we conclude that there is the watermark in the test image. Otherwise, we conclude that there is not.

4. EXPERIMENTAL RESULTS

In order to verify the effectiveness of the proposed algorithm, experiments are carried out using 24-bit true color host images of size 512x512 commonly called “Lena”, “Peppers”, and “Baboon” as in Fig. 2. A gray image of size 64x64 shown in Fig. 3 has been used for the digital watermark.

![Fig. 2. The three host images (512x512)](a) Lena       (b) Peppers      (c) Baboon

![Fig. 3. The watermark image (64x64)](a) Lena       (b) Peppers      (c) Baboon
keep the watermarked key into the third party to preserve the ownership of the host image.

![Fig. 4. The private key extracted from “Lena”](image)

In this study, performance comparison is carried out among the 3 CRT-based watermarking schemes: the scheme of Patra et al. [5], DCT0CRT [6], and the scheme proposed in this paper, considering the quality of the watermarked images, the quality of the watermarks extracted, and robustness of the schemes to different attacks. The quality of modified (watermarked) images against the host image is measured by Peak Signal-to-Noise Ratio (PSNR), which is given by the following equation:

$$PSNR(dB) = 10 \log_{10} \left( \frac{mn \times \max_{i,j} I(i,j)^2}{\sum_{i=0}^{m-1} \sum_{j=0}^{n-1} [I(i,j) - I'(i,j)]^2} \right)$$  \hspace{1cm} (8)$$

Because DCT0CRT and the scheme proposed in this paper are using the zero-watermarking technique which makes watermarked images distortion-free, quality of watermarked images in PSNR is infinitive by the definition of (8) and is better than that of Patra et al.’s as the following table shows.

**Table 1. Quality of watermarked images compared with respective host image**

| Scheme         | Image  | Patra et al. [5] | DCT0CRT [6] | Proposed Scheme |
|----------------|--------|------------------|--------------|-----------------|
| Lena           |        | 48.85            | ∞             |                 |
| Peppers        |        | 49.21            | ∞             |                 |
| Baboon         |        | 49.33            | ∞             |                 |

Comparative experiments of robustness resisting typical kinds of conventional attacks such as sharpening, blurring, JPEG lossy compression (quality factor 90), cutting edges, and cutting a quadrant have been performed. Samples of the zero-watermarked Lena images under the attacks are shown in Fig. 8.

![Fig. 8. Zero-watermarked Lena image under different attacks](image)

The extraction process is the reverse of the embedding process. Let’s assume the test image is the same with the host image. If we apply an XOR operation to the private key Fig 4 extracted from the test image and the watermarked key, we get the scrambled image of Fig. 6. Through unscrambling, we get the extracted watermark image of Fig 5. Using any strategy, we get the watermark image of Fig. 3.
extracted watermarks from the watermarked Lena images can be summarized by as in Table 2, those from the watermarked Peppers images in Table 3, and those from the watermarked Baboon images in Table 4.

As you can see from the tables, the scheme of Patra et al. does not show better performance than the other two schemes under all attacks. Even without any attacks, extracted watermarks have some errors due to the rounding in the conversion of RGB and YCrCb as well as the watermark embedding. Furthermore, it is hard to recognize the symbol of the watermark image from extracted watermarks in attacks other than sharpening. If we select a TAF value as the threshold for watermark detection, e.g., 5.0%, it is impossible to detect the watermark from all the attacked images in the scheme.

The scheme of DCT0CRT and the proposed scheme show much better performance than that of Patra et al. However, under attacks of cropping (edges and a quadrant), performance of the DCT0CRT scheme is not so good. On the other hand, good performance is retained in the proposed scheme even under the cropping attacks due to the redundancy in watermark embedding and voting in extraction.

Table 2. Comparison of extracted watermarks for Lena (Values in TAF)

| Scheme of Attack | Scheme of Patra et al. | Scheme of DCT0CRT | Proposed Scheme |
|------------------|-----------------------|-------------------|----------------|
| No attack        | 6.01%                 | 0.00%             | 0.00%          |
| Sharpening       | 20.09%                | 0.00%             | 0.02%          |
| Blurring         | 38.82%                | 0.10%             | 0.05%          |
| JPEG lossy compression | 48.68%                | 0.12%             | 0.10%          |
| Cutting edges    | 31.03%                | 14.79%            | 3.10%          |

Table 3. Comparison of extracted watermarks for Peppers (Values in TAF)

| Scheme of Attack | Scheme of Patra et al. | Scheme of DCT0CRT | Proposed Scheme |
|------------------|-----------------------|-------------------|----------------|
| No attack        | 10.79%                | 0.00%             | 0.00%          |
| Sharpening       | 25.59%                | 0.37%             | 0.02%          |
| Blurring         | 40.16%                | 0.12%             | 0.02%          |
| JPEG lossy compression | 48.83%                | 0.39%             | 0.20%          |
| Cutting edges    | 34.08%                | 14.01%            | 2.81%          |
| Cutting a quadrant | 35.40%                | 9.01%             | 0.00%          |

Table 4. Comparison of extracted watermarks for Baboon (Values in TAF)

| Scheme of Attack | Scheme of Patra et al. | Scheme of DCT0CRT | Proposed Scheme |
|------------------|-----------------------|-------------------|----------------|
| No attack        | 8.57%                 | 0.00%             | 0.00%          |
5. CONCLUSION

In this paper, a novel zero-watermarking scheme for color images has been presented. It applies DCT and CRT to the blue chrominance channel of color images in the YCrCb color space. As in watermarking host images conventionally with CRT, where watermark images are robust in spite of damages in host images, the proposed zero-watermarking scheme has a very strong robustness against different attacks. In addition, it has no affect on the quality of the original image as zero-watermarking schemes do. The following can be concluded by the experimental results:

i) the performance of the scheme is fundamentally better than that of the conventional CRT-based scheme,

ii) the performance of the scheme is mostly better than that of the CRT-based zero-watermarking scheme for gray images, and

iii) redundant embedding of a watermark and voting in the watermark extraction improves the quality of extracted watermarks, especially in cropping.

Further research directs toward how to apply the scheme to diverse applications such as sharing delivery receipts watermarked for identifying their receivers in mobile environments.

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