The electromagnetic form factors of light and heavy pseudoscalar mesons are calculated within two covariant constituent-quark models, viz., a light-front and a dispersion relation approach. We investigate the details and physical origins of the model dependence of various hadronic observables: the weak decay constant, the charge radius and the elastic electromagnetic form factor.

I. INTRODUCTION

The light-front quantum field theory is discussed by N. Bogoliubov et al. in Ref. 1 and an early application to study hadronic quark bound states may be found in Refs. 2, 3. A self-consistent relativistic treatment of the quark spins can be performed within the light-front quark model, which allows for a calculation of the reference-frame independent partonic contribution to the form factor. The non-partonic contribution cannot be generally calculated, however it can be eliminated for space-like momentum transfers by an appropriate choice of reference frame. Therefore, the partonic contribution obtained in this specific reference frame yields the full form factor.

The light-meson sector, which includes the pion and kaon, allows us to test QCD hypotheses on the subatomic structure of hadrons at low and intermediate energies. Yet, many aspects of quantum field theory on the light-front and its application to bound-state systems give rise to various open questions; for example, the problems of regularization and renormalization on the light-front.

For the pion and kaon, the light-front constituent quark model (LFCQM) has been studied 4, 5 to describe relativistic and renormalization on the light-front. The space-like electromagnetic form factor of a pseudoscalar meson with mass $M$ is generally given by the covariant expression

$$\langle P(p')|J_{\mu}^{em}|P(p)\rangle = (p + p')_\mu F^{em}(q^2),$$

where $p^2 = p'^2 = M^2$ and the four-momentum transfer $q = p' - p$, $q^2 < 0$. The electromagnetic current is $J_{\mu}^{em} = \bar{q}(0)\gamma_\mu q(0)$ where $q(0)$ denotes a current quark. Here, $F^{em}(q^2)$ describes the virtual photon emission (absorption) amplitude by the composite state of a quark of charge $e_1$ and an antiquark of charge $e_2$. This form factor depends on the three independent Lorentz invariants $p^2$, $p'^2$ and $q^2$. The constituent quark amplitude of the electromagnetic form factor is assumed to have the following structure

$$\langle Q(p')|\bar{q}(0)\gamma_\mu q(0)|Q(p)\rangle = \bar{Q}(p')\gamma_\mu Q(p)\xi_c(q^2),$$

where $Q(p)$ represents the constituent quark. The form factor is normalized such that $F^{em}(0) = e_1 + e_2$ and we neglect the anomalous magnetic moment of the constituent quark in Eq. (2). The function $\xi_c(q^2)$ describes a constituent quark transition form factor. Since the quark model is not formally derived from QCD, it is unknown.
In the following we assume that ξ_c ≃ ε_c = e_1 or e_2 owing to the fact that constituent quarks behave like bare Dirac particles \[e_{1,2}\].

### III. LIGHT-FRONT CONSTITUENT QUARK MODEL

The electromagnetic form factor for pseudoscalar particles is calculated in the impulse approximation, using the Mandelstam formula

\[
F_{\text{em}}(q^2) = \frac{e_1 N_c}{(p + p')^\mu} \int \frac{d^4k}{(2\pi)^4} \text{Tr} \left[ \gamma^\mu S_1(k - p') \times \gamma^\nu S_2(k - p) \right] \Lambda(k, p) \Lambda(k, p') + [1 \leftrightarrow 2],
\]

where \(S_i(p)\) is the Feynman propagator of quark \(i\) with constituent mass \(m_i\), \(N_c\) the number of colors, and \(\Lambda(k, p)\) is our hadron-quark vertex function model. The bracket \([1 \leftrightarrow 2]\) is a shortcut for the subprocess of constituent quark \(2\) interacting with the photon.

The momentum component Bethe-Salpeter (BS) vertex model is chosen such that it regularizes the amplitude of the photo-absorption process and constructs a light-front valence wave function \[4, 5, 19\]. In the present study, we use two different models for the vertex functions taken from previous work, one of which has a non-symmetrical form under the exchange of the momentum of the quark and antiquark \[4\],

\[
\Lambda(k, p) = \frac{N}{(p - k)^2 - m_R^2 + i\epsilon},
\]

while the other has a symmetric form \[5\],

\[
\Lambda(k, p) = \left[ \frac{N}{k^2 - m_R^2 + i\epsilon} + \frac{N}{(p - k)^2 - m_R^2 + i\epsilon} \right].
\]

The normalization constant \(N\) is obtained from \(F_{\text{em}}(0) = e_1 + e_2\).

The light-front constituent quark model for hadrons used here is based on quantum field theory and our ansatz comes with the choice of the BS vertex and point-like quarks. It is worthwhile to mention that the present LFCQM reproduces in its full complexity a covariant calculation. Technically, the use of the Drell-Yan frame (longitudinal momentum transfer \(q^+ = q^0 + q^3 = 0\)) and the projection on to the light-front (performing the integration on the minus momentum component analytically in the Mandelstam formula) simplifies drastically the computation of the form factor. This approach has been applied to the pion \[4, 5, 19\], the kaon \[21\], as well as to the \(\rho\) \[21\].

The use of light-front variables in the evaluation of the Mandelstam formula, with the corresponding projection on the light-front hypersurface through the \(k^- = k^0 - k^3\) integration, has its subtleties. Covariance of the starting expression in Eq. \(6\), which corresponds to a frame independent form factor, is an important property to be checked in the final results. In some cases, as for vector mesons in the present model, it is necessary for obtaining a careful analysis of the light-front calculation of the photo-absorption amplitude which accounts for pair terms or Z-diagrams that survive in the Drell-Yan frame (see, e.g., Ref. \[22\]). The Z-diagram vanishes in the calculation of the plus component of the electromagnetic current \((j^+)\) with \(q^+ = 0\) for pseudoscalar mesons with \(\gamma_5\) coupling and the momentum component of the BS vertices from Eqs. \(1\) and \(5\).

Therefore, we adopt the plus-component convention of the electromagnetic current in the Breit-frame with the Drell-Yan condition \(q^+ = 0\) to compute the form factor of pseudoscalar mesons. The \(k^-\) integration is performed analytically by evaluating the residues in Eq. \(6\). In the case of the non-symmetric vertex \(4\), the resulting expression for the electromagnetic form factor is:

\[
F_{\text{em}}(q^2) = \frac{e_1 N_c^2 N_c}{(p + p')^\mu} \int \frac{d^4k_1 dk_2}{4\pi^4} \frac{\text{Tr}_1^+ \left[ \right]}{k^+(p^+ + k^+)^2} \times \frac{\Lambda(k, p) \Lambda(k, p') \Lambda(k, p'_{2\text{on}}) \Lambda(k, p'_{2\text{on}})}{(p^+ - k^+_{2\text{on}}(p^+ - k^+_{2\text{on}})} \times \left[1 \leftrightarrow 2\right],
\]

where the on-minus-shell momentum is \(k^+_{1\text{on}} = (k^2_1 + m_1^2)/k^+\) \(k^+_{2\text{on}} = (k^2_2 + m_2^2)/k^+\) and the Dirac trace from Eq. \(3\) for \(\mu = +\) (good component of the current) is

\[
\text{Tr}_1^+ = -4 \left( (p^+ - k^+) \left( 2m_1 m_2 + (p + p') \cdot k - 2k^2 \right) - k^+ \left( (p - k) \cdot (p - k) - m_2^2 \right) \right).
\]

The electromagnetic form factor written for the non-symmetric vertex \(4\) in terms of the Bjorken momentum fraction \(x = k^+/p^+\) is given by

\[
F_{\text{em}}(q^2) = e_1 \frac{N_c^2 N_c}{8\pi^4} \int \frac{d^2k_1 dx}{x(1 - x)^4} \times \frac{\xi(x, \vec{k}_1, \vec{q}_1, m_1, m_2)}{(M^2 - M_0^2)(M^2 - M^2(m_1, m_2))} \times \frac{1}{(M^2 - M_0^2)(M^2 - M^2(m_2, m_R))} + [1 \leftrightarrow 2],
\]

where \(\xi(x, \vec{k}_1, \vec{q}_1, m_1, m_2) = (p^+)^{-1} \text{Tr}_1^+ \left[ \right] k^+ = k^+_{2\text{on}}, 0 < x < 1\) and the free two-quark mass is \(M_0^2 = M^2(m_2, m_1)\), with

\[
M^2(m_1, m_R) = \frac{k^2_2 + m_2^2}{x} + \frac{(p - k)^2_2 + m_R^2}{1 - x} - p^2_1.
\]

Analogous expressions follow for \(M_0^2\) and \(M^2(m_2, m_R)\) with \(p_2^2\) replaced by \(p_2^2\). The calculation of the electromagnetic form factor with the symmetrical vertex \(5\) can be done following the steps presented above. For the interested reader, the derivation of the form factor for the pion in this model is performed in detail in Ref. \[5\].

The mass parameters in these models are limited by \(m_1 + m_2 > M, m_1 + m_R > M\) and \(m_2 + m_R > M\).
due to the unphysical continuum threshold as seen in the denominator of Eq. [8]. Quark confinement does not allow for a scattering cut, but since in the present model the meson is as a real bound state, i.e. the conditions $m_1 + m_2 > M$ and $m_4 + m_5 > M$ are satisfied, the cut is harmless. However, if the meson is a weakly bound composite particle, the form factor will be very sensitive to changes in the constituent quark mass. This is certainly not the case for pions and kaons, as they are Goldstone bosons and strongly bound, yet this sensitivity appears in the case of heavy pseudoscalars with small binding energies in nonconfining models (see, e.g., Ref. [23, 24]). In particular, our numerical results for $D^+$ will exemplify the strong dependence of the heavy pseudoscalar electromagnetic form factor on the constituent masses, whereas

\[ 2 \tilde{p}_\mu(q) \Delta(s, s', q^2|m_1, m_2) = \frac{1}{8\pi} \int d^4k_1d^4k_1'd^4k_2 \delta(k_1^2 - m_1^2)\delta(k_1'^2 - m_1^2)\delta(k_2^2 - m_2^2) \]

\[ \times \delta(\tilde{p} - k_1 - k_2)\delta(\tilde{p}' - k_1' - k_2) \text{Tr} \left[ -(\gamma'_4 + m_1)\gamma^\mu(\gamma'_1 + m_1)i\gamma^5(m_2 - \gamma_2)i\gamma^5 \right], \]

with $\tilde{p}_\mu(q) = \tilde{p}_\mu - \frac{\mathcal{E}a}{q^2}q_\mu$ which ensures the Ward identity and thus charge conservation $F^{em}(0) = e_1 + e_2$ with the proper vertex normalization.

The vertex of the pseudoscalar meson in the constituent quark picture has the structure

\[ \bar{Q}^a(k_1, m_1)i\gamma^5Q^a(-k_2, m_2) \sqrt{N_c} \]

\[ G_v(s), \]  

where $Q^a(k_1, m_1)$ represents the spinor state of the constituent quark of color $a$ and $N_c$ the number of colors. The bound state vertex function may be related to the mesonic BS amplitude by

\[ \phi(s) = \frac{G_v(s)}{s - M^2}. \]  

For a confining potential, the pole at $s = M^2$ should appear in the physical region for $\phi(s)$ at $s = M^2 > (m_1 + m_2)^2$. This is, however, not the case; as well known from the behavior of the bound-state wave function in an harmonic oscillator potential, $\phi(s)$ is a smooth exponential function of $s \geq (m_1 + m_2)^2$. This means that the would-be pole in $\phi(s)$ at $s = M^2$ is completely blurred out by the interaction and it is therefore more appropriate to analyze the meson form factors in terms of $\phi(s)$ rather than $G_v(s)$.

For a pseudoscalar meson in the dispersion approach of the constituent quark model, the BS amplitude $\phi(s)$ which accounts for soft constituent quark rescattering is given by [13]

\[ \phi(s) = \frac{\pi}{\sqrt{2}} \sqrt{\frac{s^2 - (m_1^2 - m_2^2)^2}{s - (m_1 - m_2)^2}} \frac{w(k)}{s^{3/4}}. \]  

\[ \text{FIG. 1: The electromagnetic form factor in the impulse approximation is obtained from the triangle diagram. The vertices and momenta depicted in the diagram represent the momentum assignment in the DR approach.} \]  

\[ \text{This effect is minor for confining models like the DR approach.} \]  

\[ \text{IV. DISPERSION RELATION APPROACH} \]  

The amplitude is obtained from the triangle diagram shown in Fig. [4] where the kinematical variables are displayed. The on-shell meson momenta are $p_1^2 = M^2$ and $p_2^2 = M^2$. The triangle diagram may be calculated in various ways — we choose to put the constituent quarks on-mass shell while keeping the external momenta off-shell with

\[ \tilde{p}^2 = s, \quad \tilde{p}'^2 = s', \quad (\tilde{p}' - \tilde{p})^2 = q^2. \]  

Note, however, that $\tilde{p}' - \tilde{p} = \tilde{q} \neq q$.

In the DR approach, the electromagnetic form factors $F^{em}(q^2)$ are expressed by a double spectral representation (see references [10, 11, 12, 13, 14]),

\[ F^{em}(q^2) = e_1 \int \frac{ds G_v(s)}{\pi(s - M^2)} \frac{ds'}{\pi(s' - M^2)} \times \Delta(s, s', q^2|m_1, m_2) \left[ 1 \leftrightarrow 2 \right]. \]

We apply the Landau-Cutkosky rules to calculate the double spectral density $\Delta_V$: we place all internal particles on their mass shell, $k_1^2 = m_1^2$, $k_1'^2 = m_1'^2$, $k_2^2 = m_2^2$ but take the variables $p_1^2$ and $p_2^2$ off-shell. The double spectral density is then derived from calculation of the triangle diagram
The dynamical factor multiplying $w(k)$ stems from the loop diagram associated with the meson-vertex normalization. The modulus of the center of mass momentum is

$$k = \sqrt{\frac{(s + m_1^2 - m_2^2)^2 - 4sm_1^2}{4s}}. \quad (16)$$

It can be shown [13] that the vertex normalization of $G_v(s) = \phi(s)(s - M^2)$, which describes soft constituent rescattering, reduces to a simple normalization of the wave function

$$\int_0^\infty w^2(k)k^2 \, dk = 1. \quad (17)$$

A heuristic choice must be made for $w(k)$. For phenomena that are predominantly governed by infrared mass scales, it is sensible in the case of heavy mesons to choose a BS amplitude parameterized by a function whose support is in the infrared; for instance functions of Gaussian form,

$$w(k) = N \exp\left(-4\nu k^2/\mu^2\right), \quad (18)$$

where the reduced mass of the quark-antiquark pair is $\mu = m_1m_2/(m_1 + m_2)$ and $N$ a normalization constant. For light pseudoscalar mesons, dynamical chiral symmetry and the Ward-Takahashi identity are of great importance for their structure and properties. In non-perturbative approaches, using for example Schwinger-Dyson equations which incorporate these QCD features, appropriate parameterizations for the pion or kaon BS amplitudes are derived [23]. In this work, we employ power-law wave functions of the form

$$w_n(k) = \frac{N}{(1 + \nu(k/\mu)^2)^n}, \quad n \geq 2, \quad (19)$$

inspired by the form suggested in Ref. [28] from the analysis of the ultraviolet physics of QCD.

The size parameter $\nu$ is to be determined from experimental and theoretical considerations. On the experimental side, on can either choose to constrain the vertex functions, or equivalently the BS amplitude, by the weak decay constant or by the electric charge radius. It is worthwhile to observe that both wave function models, Gaussian and power-law, do not present the singularity problem brought by the scattering cut due to changes in the constituent quark masses, differently from the present LFCQM.

V. NUMERICAL RESULTS

The electromagnetic form factor of light and heavy pseudoscalar mesons are calculated with the two covariant constituent quark models. In the LFCQM, the quarks are in a bound state while in the DR model the wave functions corresponds to confined quarks with Gaussian and power-law forms. The shape of these functions is obtained from a fit to the experimental values of $f_\pi$, $f_K$ and $f_\Omega$ or the charge radius (when available) of the regulator mass $m_R$ in the LFCQM and size parameter $\nu$ in the DR approach. The light constituent quark masses $m_u = m_d$ are allowed to take the values 0.22 and 0.25 GeV (and 0.28 GeV in case of the $D^+$). The strange and charm constituent masses are fixed to $m_s = 0.508$ GeV and $m_c = 1.623$ GeV, respectively (see Ref. [27]).

The results for the pion electromagnetic form factor compared to experimental data [6,7,8] are shown in Fig. 2. The quark masses used in these calculations are $m_u = m_d = 0.22$ GeV in both the LFCQM and DR approaches. The pion charge radius is used to fit the parameters $m_R$ and $\nu$ (power-law wave function with $n = 3$). The regulator mass is $m_R = 0.946$ GeV [4] for the non-symmetric vertex and 0.546 GeV [2] the symmetric vertex. In this case, we show results only for the power-law wave function with $n = 3$ ($\nu = 0.088$) in the DR approach because the Gaussian vertex produces a form factor strongly damped with increasing $q^2$, which violates the asymptotic QCD result predicting a $q^{-2}$ falloff. The pion electromagnetic form factor for the power-law wave function and non-symmetric vertex are very similar, while the symmetrical model has a longer tail. These results indicate that the electromagnetic form factor of the pion as a strongly bound system does not particularly distinguish between models with a scattering cut. The high momentum experimental data appear to favor the more complex structure of the symmetrical vertex. It is expected that in this region the details of the regulator structure are crucial, and moreover a symmetric form of the vertex is natural.

We remind that the tail of the momentum component of the pion light-front wave function corresponding to

![Figure 2: The pion electromagnetic form factor in the LFCQM and DR approaches compared with experimental data from Ref. 6, 7, 8. The model and respective parameters are explained in the legend.](image-url)
the non-symmetric [4] and to the symmetric vertex [5] both decrease as \( \sim k^{-4}_\perp \), which can also be verified by inspecting Eq. (8). The power-law wave function model with \( n = 3 \) also displays a tail that falls off with \( \sim k^{-4}_\perp \).

Thus, in the space-like region up to 10 GeV\(^2\), we find that the pion electromagnetic form factor favors the power-law damping of the wave function with a \( \sim k^{-4}_\perp \) tail.

The electromagnetic form factor of the \( K^+ \) obtained in both models are compared with experimental data [28, 29] in Fig. 3. The quark masses used in these calculations are \( m_u = m_d = 0.22 \) GeV and \( m_s = 0.508 \) GeV in both the non-symmetric vertex and DR approaches. In order to study the mass dependence of the form factor, we also give results for a calculation with \( m_u = m_d = 0.25 \) GeV in LFCQM case. The regulator mass is fixed to the pion’s value \( m_R = 0.946 \) GeV for the non-symmetric vertex which corresponds to a reasonable kaon charge radius [20]. We observe in Fig. 3 that the change of 0.03 GeV in the constituent quark mass is not important as it is much smaller than the kaon binding energy of about 0.2 GeV. A similar finding can be reported for the DR approach, where the size parameter \( \mu \) of the power-law wave function with \( n = 2 \) is fitted (\( \nu = 0.061 \)) to reproduce the kaon charge radius and is readjusted for \( n = 3 \) (\( \nu = 0.158 \)). Again, we observe that the non-symmetric vertex as well as the power-law model essentially yield the same form factor once the radius is reproduced.

Our numerical results for \( D^+ \) are shown in Fig. 4 for the DR approach and LFCQM. The size parameter of the Gaussian and power-law (\( n = 3 \)) models are fitted to \( f_D \) for \( m_d = 0.25 \) GeV. Up to 10 GeV\(^2\) there is no sizable difference between the two calculations. This is reasonable as \( m_c \) sets one large scale whereas the momentum transfer goes only up to 3 GeV, which is not large enough to discriminate between the models. The regulator mass of 1.77 GeV in the non-symmetric vertex model is chosen so as to give a sample of the LFCQM results. Here, we want to illustrate the constituent quark mass sensitivity when the symmetric and non-symmetric vertices are used. We remind that the mass parameters in these models are limited by \( m_1 + m_2 > M, m_1 + m_R > M \) and \( m_2 + m_R > M \) due to the unphysical continuum threshold as evident from the denominator in Eq. (8). The model binding energy of \( D^+ \) is only a few tenths of MeV, as can be inferred from the \( D^* \) and quark masses. Since the \( D^+ \) meson mass is fixed to the experimental value of 1.8694 GeV and \( m_c = 1.623 \) GeV, the light quark mass \( m_d \) must be larger than the value 0.22 GeV we used for the pion and kaon. The increase of the light quark constituent mass from 0.25 to 0.28 GeV corresponds to a large increase in binding and consequently to a decrease of the radius, as seen in Fig. 4.

VI. CONCLUSION

We have concentrated on the model dependence of elastic electromagnetic form factors of light and heavy pseudoscalar mesons. Two different cases were studied by changing the form of the vertex or wave function and by varying the constituent quark masses. In the light sector, we computed the pion and kaon electric form factors for which experimental data is available; we then adjusted our models to make predictions for the charmed sector. Two ansatzes have been studied in the LFCQM which involve a symmetric and a non-symmetric vertex form. In the DR approach, Gaussian and power-law wave functions were used in the calculations.

The form factors of the pion and kaon, both being
strongly bound systems, are sensitive to the short-range part of the vertex functions. Therefore, the tail of the momentum component of the light-front wave functions for the non-symmetric \( \omega \) and symmetric vertex \( \bar{\omega} \) as well as the power-law model \( (n = 3) \), all decreasing as \( \sim k_{\perp}^{-4} \), is essential to reproduce the pion space-like data up to 10 GeV\(^2\). Moreover, as a consequence of the strong binding of the quarks, changes in the constituent mass of about ten percent are not important for the elastic form factor of light mesons, provided the charge radius (or decay constant) is accordingly refitted. We have exemplified this in the kaon calculation. The light quark constituent masses are relevant for low momentum transfers of the order \( m_{u,d,s}^2 \) around 0.05 – 0.3 GeV\(^2\), which is dominated by the charge radius and consequently compensated by fitting the size or regulator mass parameters. Therefore, in qualitative agreement with QCD scaling laws in the ultraviolet limit, a power-law form of the wave function and our choice of vertices are reasonable in reproducing the form factor data once the charge radius is fitted.

A recent calculation of the pion form factor within the dispersion relation approach including \( O(\alpha_S) \) QCD perturbative contribution \([15]\), showed in a model independent way that the nonperturbative part stays above 50% for \( Q^2 \leq 20 \) GeV\(^2\). The nonperturbative part is compatible with a pion wave function close to the asymptotic one, with a momentum scale given by the effective continuum threshold that determines to a great extent their results for the form factor. The value of the threshold is extracted from the experimental pion decay constant. Similarly in our analysis the size or regulator mass parameters are fixed by the experimental values of the weak decay constants within models that have momentum tails decreasing with \( \sim k_{\perp}^{-4} \), which does not leave not too much freedom for the pion form factor results below 20 GeV\(^2\), as we have shown. In that respect our calculation and \([15]\) show the dominance of the scale given by the pion decay constant that dials the vertex or wave function (decaying as a power law) in the pion form factor up to a fairly large value of momentum transfers.

The electromagnetic form factor of pseudoscalar mesons in the heavy-light sector is strongly sensitive to the infrared behavior of QCD, compared to the case of light mesons. The relevance of soft physics in this sector is supported by our calculations of the elastic \( D \) meson form factor both within the dispersion relation and light-front approaches. Once the size parameter of the Gaussian and power-law wave functions are adjusted to reproduce the decay constant, the elastic form factor is insensitive to the vertex model in the space-like region up to 10 GeV\(^2\). Therefore, the large-momentum tail of the wave function is not important for these results. We presume that the asymptotic behavior will be important only for \( q^2 \gg m_c^2 \) beyond the results we presented. The importance of soft physics may also be appreciated in the covariant calculations of the form factor with the symmetric and non-symmetric vertices in LFCQM. The corresponding BS amplitude models a lightly bound heavy-light system with respect to the light quark mass. The infrared dynamics appears to be important for the \( D \) meson, as the sensitivity to changes of the constituent quark mass by about 10% suggests. This small modification produces a sensible change in the nearby unphysical continuum threshold, as the mass of the \( D \) is about the sum of the constituent quark masses. Therefore, the condition \( m_1 + m_2 > M \) is barely satisfied (see, e.g., the denominator of Eq. \( 8 \)).

In summary, our study of the model dependence of elastic form factors for pseudoscalar mesons in the light and heavy-light sectors suggests a separation of the ultraviolet and infrared physics. The ultraviolet properties of QCD dominate the form factor of light pseudoscalars, whereas infrared physics and details of quark confinement appear to be important for the space-like form factor of heavy mesons below \( q^2 = 10 \) GeV\(^2\). Hence, the electromagnetic form factors of heavy-light systems, such as the \( D \) and \( B \) mesons, provide a valuable tool in the effort to investigate the nonperturbative physics of confinement, in contrast with light pseudoscalar form factors insensitive to the details of infrared physics even at low momentum transfers once the weak decay constants are fixed to the experimental values.

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[1] N. N. Bogoliubov, V. A. Matveev and A. N. Tavkhelidze, in “Gravitation and Elementary Particle Physics”, ed. by A. A. Logunov (Mir, Moscow, 1983), p. 220.
[2] M. V. Terentev, Sov. J. Nucl. Phys. 24, 106 (1976) 106; L. A. Kondratyuk and M. V. Terentev, Sov. J. Nucl. Phys. 31, 561 (1976).
[3] V. B. Berestesky and M. V. Terentev, Sov. J. Nucl. Phys. 24, 547 (1976); Sov. J. Nucl. Phys. 25, 347 (1977).
[4] J. P. B. C de Melo, H. W. Naus, and T. Frederico, Phys. Rev. C 59, 2278 (1999).
[5] J. P. B. C de Melo, T. Frederico, E. Pace and G. Salmè, Nucl. Phys. A \textbf{707}, 399 (2002).
[6] R. Baldini et al., Eur. Phys. J. C \textbf{11} 709 (1999); Nucl. Phys. A \textbf{666} & \textbf{667}, 3 (2000).
[7] The Jefferson Lab F(pi) Collaboration (J. Volmer et al.), Phys. Rev. Lett. \textbf{86}, 1713 (2001).
[8] The Jefferson Lab F(pi) Collaboration (T. Horn et al.), Phys. Rev. Lett. \textbf{97}, 192001 (2006).
[9] The Jefferson Lab F(pi) Collaboration (V. Tadevosyan et al.), Phys. Rev. C \textbf{75}, 055205 (2007).
[10] V. V. Anisovich, M. N. Kobrinsky, D. Melikhov, A. Sarantsev, Nucl. Phys. A\textbf{544}, 747 (1992).
[11] V. V. Anisovich, D. Melikhov, V. Nikonov, Phys. Rev. D\textbf{52}, 5295 (1995).
[12] V. V. Anisovich, D. Melikhov, V. Nikonov, Phys. Rev. D\textbf{55}, 2918 (1997).
[13] D. Melikhov, Phys. Rev. D \textbf{53}, 2460 (1996).
[14] D. Melikhov, Eur. Phys. J. C \textbf{4}, 2 (2002).
[15] V. Braguta, W. Lucha and D. Melikhov, Phys. Lett. B \textbf{661}, 354 (2008).
[16] V. M. Braun, A. Khodjamirian and M. Maul, Phys. Rev. D\textbf{61}, 073004 (2000).
[17] W. Lucha, D. Melikhov and S. Simula, Phys. Rev. D\textbf{74}, 054004 (2006).
[18] S. Weinberg, Phys. Rev. Lett. \textbf{65}, 1181 (1990).
[19] B. L. G. Bakker, H. M. Choi, C. R. Ji, Phys. Rev. D \textbf{63}, 074014 (2001).
[20] F. P. Pereira, J. P. B. C. de Melo, T. Frederico and Lauro Tomio, Nucl. Phys. A \textbf{790}, 610c (2007); Phys. Part. Nucl. \textbf{36}, 217 (2005).
[21] J. P. B. C. de Melo, T. Frederico Phys. Rev. C \textbf{55}, 2043 (1997).
[22] J. P. B. C. de Melo, J. H. O. Sales, T. Frederico, P. U. Sauer, Nucl. Phys. A \textbf{631}, 574c (1998).
[23] T. Frederico, H.-C. Pauli, Phys. Rev. D \textbf{64}, 054007 (2001).
[24] L. A. M. Salcedo, J. P. B. C. de Melo, D. Hadjmichef and T. Frederico, Braz. J. Phys. 34 (2004) 297; Eur. Phys. J. A \textbf{27}, 213 (2006).
[25] P. Maris, C. D. Roberts and P. C. Tandy, Phys. Lett. B \textbf{420}, 267 (1998).
[26] F. Schlumpf, Phy. Rev. D \textbf{50}, 6895 (1994).
[27] E. F. Suisso, J. P. B. C. de Melo, T. Frederico, Phys. Rev. D \textbf{65}, 094009(2002).
[28] E. B. Daily et al., Phys. Rev. Lett. \textbf{45}, 232 (1980).
[29] S. R. Amendolia et al., Phys. Lett. \textbf{178}, 435 (1986).