A Data-Driven Reaction Network for the Fluid Catalytic Cracking of Waste Feeds

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Abstract: Establishing a reaction network is of uttermost importance in complex catalytic processes such as fluid catalytic cracking (FCC). This step is the seed for a faithful reactor modeling and the subsequent catalyst re-design, process optimization or prediction. In this work, a dataset of 104 uncorrelated experiments, with 64 variables, was obtained in an FCC simulator using six types of feedstock (vacuum gasoil, polyethylene pyrolysis waxes, scrap tire pyrolysis oil, dissolved polyethylene and blends of the previous), 36 possible sets of conditions (varying contact time, temperature and catalyst/oil ratio) and three industrial catalysts. Principal component analysis (PCA) was applied over the dataset, showing that the main components are associated with feed composition (27.41% variance), operational conditions (19.09%) and catalyst properties (12.72%). The variables of each component were correlated with the indexes and yields of the products: conversion, octane number, aromatics, olefins (propylene) or coke, among others. Then, a data-driven reaction network was proposed for the cracking of waste feeds based on the previously obtained correlations.

Keywords: principal component analysis (PCA); fluid catalytic cracking (FCC); waste valorization; scrap tires; polyolefin pyrolysis

1. Introduction

The global requirement for transportation fuels is expected to grow steadily over the coming years due to an increasing demand of energy from developed and developing countries [1]. The foreseeable petroleum depletion will be anticipated by the use of heavier and low-quality crudes, together with a switch of market demand from heavy-fuel fractions towards gasoline and light olefins. These combined aspects justify the current necessity of refineries to evolve by introducing new units, revamping used ones and varying the feedstock to expand their versatility and capacity [2].

The fluid catalytic cracking (FCC) unit plays a key role in an integrated and intensified refinery as the primary catalytic conversion process (in terms of volume) greatly determining its competitiveness and margin [3]. In recent years, important efforts have been directed towards the improvement of these highly demanding units [4]. The underlying drive of these works highlights the essential role of the FCC unit in the path towards an integrated waste and bio-refinery concept [5–7]. FCC units have traditionally processed heavy petroleum fractions (vacuum gasoil, VGO) into interesting products such as gasoline, diesel or propylene [8,9]. However, taking the remarkable versatility of FCC, other non-conventional feeds have also been studied [10]: (i) secondary refinery streams; (ii) streams derived from the consumer society; or (iii) oxygenated bio-derived feedstock. As secondary refinery streams (i), Arandes et al. [11,12] studied the effect of co-feeding atmospheric distillation residue (20 wt %) with VGO in a riser simulator, observing a crucial role of the reactant accessibility for the...
efficient conversion of bulky aromatic molecules, and also the great influence of the temperature and catalyst/oil (C/O) ratio on gasoline composition. Garcia et al. [13] observed an improvement of conversion of the blend of atmospheric distillation residue (10 wt %) and VGO, compared with the VGO alone. Specifically, these authors observed a higher yield of light cycle oil (LCO) at the expense of slightly faster coke formation with the blend. Regarding streams derived from the consumer society (ii), waste polyolefins have an ideal composition as FCC feedstock and their valorization can be carried out by either dissolving the polymer in the feed [14,15] or performing a previous pyrolysis [16–19]. Lovás et al. [20] compared the catalytic cracking in FCC conditions of high-density polyethylene (HDPE) and polypropylene (PP) waxes together with VGO and it was concluded that PP should be used preferentially in order to boost gasoline production. On the other hand, the condensed pyrolysis oil derived from waste (scrap) tires also shows great prospects to become a FCC feed and produce high quality fuels [21–23]. Concerning oxygenated bio-derived streams (iii), a great research interest has been directed towards exploring the possibilities of bio-derived feedstock (i.e., bio-oil and vegetable oils) for FCC conversion [24–30].

Despite the effort, a proper assessment of the effect of the set of conditions (feed, catalyst, and operational conditions) on the results and the subsequent proposal of a reaction network are challenging due to the great number of correlated and uncorrelated variables affecting the system [31]. In this context, principal component analysis (PCA) is a valuable statistical tool that can aid in categorizing the variables by replacing a large set of parameters with a smaller set of new ones (principal components) that describe the observed patterns [32–34]. Categorizing and grouping variables is the main aim of PCA and, to date, this methodology has been used in the oil industry as a predictive tool for process monitoring and control [35], fault discovery [36], reactor modeling [37], determination of physical properties of petroleum samples [38], catalyst characterization [39] and gathering insight into catalyst behavior and classification of the main reaction routes in the catalytic cracking of decalin over Y-zeolites [40]. The application of this method has also been reported for the evaluation of the optimal reaction conditions for the catalytic oxidation of toluene [41] as well as for proposing kinetic schemes in the thermal pyrolysis of waste HDPE plastics [42] and waste tires [43]. Pasadakis et al. [39] used the PCA methodology to highlight the differences among different hydrotreating catalysts based on several physical and chemical properties of the products along with other kinetic constants. PCA is among the disruptive methodologies which can lead to new catalysts or models for complex problems, together with artificial neural networks [44]. This approach is fundamentally distinct to the empiric one that uses the principal component equations to describe observations or predict new conditions [45], namely the principal component regression (PCR) or the principal component analysis and multiple linear regression (PCA-MLR). The partial least squared regression (PLS) uses PCA methodology to select the most influential variables and subsequently calculate the (empirical) functions that describe the results with less error [46].

The main aim of this work was to obtain a reaction network for the cracking of waste feeds applying the PCA methodology over 104 uncorrelated experiments. In particular, the aim was to measure the quantitative impact of processing alone or together with VGO: scrap tire pyrolysis oil, high-density polyethylene pyrolysis waxes or dissolved high-density polyethylene. This study pursued analyzing the impact of using different experimental conditions (resembling those of industrial units) and using three different equilibrated FCC catalysts (discarded from actual industrial FCC units). The partial goal was to gather insights into the main key parameters or variables affecting product yields in terms of conversion, octane number, propylene yield or coke formation, among others.

2. Materials and Methods

The variables used in this work are shown in Table 1, categorized into four groups: (i) catalyst properties; (ii) feed properties; (iii) reaction conditions; and (iv) products.
Table 1. List of the variables (var.) assessed by the principal component analysis.

| Var.   | Name                      | Units                | Var.   | Name                      | Units                |
|--------|---------------------------|----------------------|--------|---------------------------|----------------------|
| **Catalysts properties** |                          |                      | **Var.** | **Name**                      | **Units**                |
| ST     | BET surface area          | m² g⁻¹               | GL     | Yield of LPGb (C₃–C₄)     | wt %                 |
| Sm     | Micropore area            | m² g⁻¹               | iGL    | Gasoline identified       | wt %                 |
| SM     | Matrix or mesopore area   | m² g⁻¹               | LCO    | Yield of light cycle oil (C₁₃–C₂₀) | wt %                |
| Z      | Zeolite percentage        | wt %                 | HCO    | Yield of heavy cycle oil (C₂₀+) | wt %                |
| Vm     | Micropore volume          | cm³ g⁻¹              | Ck     | Coke content on the catalyst | wt %                |
| mV     | Mean pore volume          | cm³ g⁻¹              | RON    | Octane number (GL)        |                      |
| Dc     | Zeolite cell unit size    | Å                     | A6     | Benzene                   | wt %                 |
| Cu     | Content of Cu             | ppm                  | A7     | Toluene                   | wt %                 |
| Ni     | Content of Ni             | ppm                  | A8     | Xylenes                   | wt %                 |
| V      | Content of V              | ppm                  | A9     | Aromatics with 9 carbons  | wt %                 |
| Fe     | Content of Fe             | wt %                 | A10+   | Aromatics with 10 carbons | wt %                 |
| Na     | Content of Na             | wt %                 | AT     | Total aromatics           | wt %                 |
| Al     | Content of Al₂O₃          | wt %                 | NT     | Total naphthenes          | wt %                 |
| Re     | Content of rare earths Re₂O₃ | wt %             | P3     | Propane                   | wt %                 |
| P      | Content of P₂O₅           | wt %                 | P4     | Butane                    | wt %                 |
| Ac     | Total acidity             | mmol g⁻¹             | PT     | Total paraffins           | wt %                 |
| BL     | Brønsted-Lewis acid site ratio | mol mol⁻¹         | O3     | Propylene                 | wt %                 |
| **Feed properties** |                          |                      | **Fe**    | **Name**                      | **Units**                |
| Pf     | Paraffins                 | wt %                 | O5     | Pentenes                  | wt %                 |
| Of     | Olefins                   | wt %                 | OT     | Total olefins             | wt %                 |
| Nf     | Naphthenes                | wt %                 | IT     | Total isoparaffins        | wt %                 |
| Af     | Aromatics                 | wt %                 | C3     | C₃ hydrocarbons           | wt %                 |
| Sf     | Sulfur                    | wt %                 | C4     | C₄ hydrocarbons           | wt %                 |
| Gf     | Gasoline (C₅–C₁₂)         | wt %                 | C5     | C₅ hydrocarbons           | wt %                 |
| Lf     | Light cycle oil (C₁₃–C₂₀) | wt %                 | C6     | C₆ hydrocarbons           | wt %                 |
| Hf     | Heavy cycle oil (C₂₀+)    | wt %                 | C7     | C₇ hydrocarbons           | wt %                 |
| **Reaction conditions** |                          |                      | **R**    | **Name**                      | **Units**                |
| CO     | Catalyst-to-oil ratio     | g g⁻¹                | C9     | C₉ hydrocarbons           | wt %                 |
| t      | Contact time              | s                    | C10    | C₁₀⁺ hydrocarbons         | wt %                 |
| T      | Temperature               | °C                   | CT     | Total hydrocarbons        | wt %                 |
| **Product properties** |                          |                      | **P**    | **Name**                      | **Units**                |
| X      | Conversion                | wt %                 | iOT    | Total isoolefins          | wt %                 |
| LG     | Yield of light gases (C₁–C₂) | wt %             | nOT    | Total linear olefins      | wt %                 |

a Brunauer, Emmett and Teller theory; b Liquefied petroleum gas.

2.1. Catalyst Properties

Three equilibrated commercial FCC catalysts based on HY zeolite were used in this study and designated as CAT-1 to -3. These three catalysts are considered spent, i.e., collected after exiting the stripper section and discarded from industrial FCC units [47].

The textural properties (ST, Sm, SM, Vm and mV) were measured by N₂ adsorption–desorption isotherms at −196 °C using a Micromeritics ASAP 2010 apparatus (Micromeritics, Norcross, GA, USA), after the samples were degassed at 150 °C for 8 h. The zeolite percentage (Z) was calculated using the Johnson correlation [48].

The unit cell size (Dc) was obtained from X-ray diffraction (XRD) analysis in a Philips PW 1710 apparatus (Philips Industrial & Electro-acoustic Systems Division, Almelo, the Netherlands) with a graphite monochromator using CuKα radiation (λ = 1.5544 Å). Data were collected using a coupled configuration in the 2–50° range with a step size of 0.02 and a scan time of 1 s. The acidity (Ac) was measured through temperature programmed desorption (TPD) of NH₃ adsorbed at 150 °C in a TG-DSC Setaram 111 calorimeter (Setaram, Caluire-et-Cuire, France), which was connected on-line with a Balzers Quadstar 422 mass spectrometer (Thermo Scientific, Germany). The Brønsted–Lewis acid site...
ratio (BL) was obtained using Fourier transform infrared (FTIR) spectrometry of adsorbed pyridine in a Nicolet 6700 FTIR apparatus (Agilent Technologies, Wilmington, DE, USA) with a catalytic SPECAC chamber. The elemental analysis (Cu, Ni, V, Fe, Na, Al, Re and P) was carried out by Inductively Coupled Plasma–Atomic Emission Spectroscopy (ICP-AES) using a X7-II Thermo quadrupolar mass spectrometer (QICP-MS) (TA Instruments, New Castle, DE, USA), previously subjecting the fresh catalysts to acid digestion with HF (Merck) at 90 °C.

2.2. Feed Properties

Six feeds were used: (1) vacuum gasoil, VGO; (2) high-density polyethylene (HDPE) pyrolysis waxes, PW; (3) scrap tire pyrolysis oil, STPO; (4) VGO + HDPE, 95 wt % + 5 wt %; (5) VGO + PW, 80 wt % + 20 wt %; and (6) VGO + STPO, 80 wt % + 20 wt %. VGO was provided by Petronor S.A. (Muskiz, Spain), with an API gravity of 21.1 and a viscosity at 100 °C of 8.6 cSt. Pre-grounded particles of <1 mm of HDPE were provided by Dow Chemical (Tarragona, Spain), with an average molecular weight of 46,200 g mol⁻¹ and a polydispersity of 2.89.

The pyrolysis of HDPE or tires—previously ground to particles of <1 mm, after removal of textile reinforcements and metallic components provided by Jenecan S.L. (Abanto-Zierbana, Spain)—was performed in a conical spouted bed reactor under the following conditions: (i) for HDPE (continuous flow regime): 500 °C, HDPE flow rate of 1 g min⁻¹, N₂ flow rate of 7.5 L min⁻¹, and 30 g of sand (0.63 < d_p < 1 mm) in the bed [49]; and (ii) for tires (semi-continuous regime): 500 °C, tire feed of 2 g per run, N₂ flow rate of 6.5 L min⁻¹, and 30 g of sand (0.63 < d_p < 1 mm) in the bed [50], respectively.

The fractions of the feed (Gf, Lf and Hf) were analyzed by simulated distillation, according to the ASTM D-2887 standard, in an Agilent 6890 Series GC gas chromatograph. To carry out the simulated distillation of PW, this feed was diluted in tetrahydrofuran (THF) at 55 °C in a PW:THF mass ratio of 1:2. The amount of sulfur (Sf) was analyzed by gas chromatography in an Agilent Technologies 7890A setup (Agilent Technologies, Wilmington, DE, USA) connected in line and provided with an FID detector and a pulsed flame photometric detector (PFPD). Additionally, the chemical composition (Pf, Of, Nf and Af) analysis was performed in a bi-dimensional Agilent 7890A gas chromatograph (GC × GC) (Agilent Technologies, Wilmington, DE, USA) provided with two columns and a flow modulator, coupled in line with an Agilent 5975C Series mass spectrometer (MS) (Agilent Technologies, Wilmington, DE, USA) and a flame ionization detectors (FID) (Agilent Technologies, Wilmington, DE, USA); additional details can be found elsewhere [22].

2.3. Reaction Conditions and Product Properties

The FCC runs were carried out in a CREC (Chemical Reactor Engineering Centre, University of Western Ontario, London, ON, Canada) riser simulator, using reaction condition resembling those of industrial FCC units [51]: T, 500–530–560 °C; CO, 3–5–7 g g⁻¹; t, 3–6–12 s. A detailed schematization of the reactor is described in a previous work [24]. Please note that t denotates the contact time during which reactants and products were in contact with the catalyst within the reaction chamber Once this contact time was completed, the products were withdrawn from the reactor by triggering a valve which connects the reactor with a vacuum chamber in order to avoid side reactions.

The reaction products that are gases in the reaction conditions were analyzed through the same GC described before for the analysis of Sf. The coke content (Ck) was determined by combustion in a TA Instruments TGA-Q 5000 thermobalance (TA Instruments, New Castle, DE, USA), applying a temperature ramp of 300–550 °C at a 3 °C min⁻¹ rate. The conversion (X) was defined as the fraction of the feed that yields the most important products (LG + LPG + GL + Ck). The individual yield of each product/lump referred to the total mass of products (LG + LPG + GL + LCO + HCO + Ck). The research octane number (RON) was calculated from a method established by Anderson et al. [52] and based on the composition of the GL fraction measured by gas chromatography.
2.4. Principal Component Analysis (PCA)

A routine was developed in MATLAB\textsuperscript{TM} (Version 2014a, Mathworks, Natick, MA, USA, 2014) for the multivariate analysis of the experimental results. The dataset $X$ was configured as a matrix consisting of $n$ columns (for $n$ variables) and $m$ rows (for $m$ number of independent experiments). Each of the variables is an independent or dependent one and is summarized within Table 1.

\[
X = \begin{bmatrix}
    x_{11} & x_{12} & \ldots & x_{1n} \\
    x_{21} & x_{22} & \ldots & x_{2n} \\
    \cdots & \cdots & \cdots & \cdots \\
    x_{m1} & x_{m2} & \ldots & x_{mn}
\end{bmatrix} \tag{1}
\]

The data were normalized with the command \textit{normc}. Then, the data matrix $X$ was decomposed into a score vector $t_i$ and a loading vector $p_i$ with a residual error $E$, as:

\[
X = t_1 p_1^T + t_2 p_2^T + \ldots + t_k p_k^T + E \tag{2}
\]

The correlations of the variables were obtained by first calculating the covariance (\texttt{cov} command) and then transforming it to a correlation matrix (\texttt{corrcov} command). The covariance matrix can also be expressed as:

\[
R = \sum_{j=1}^{n} p_j \lambda_j p_j^T = P \Lambda P^T \tag{3}
\]

where $P$ is a $m \times n$ matrix of eigenvectors and $\Lambda$ is a matrix of eigenvalues associated to those eigenvectors, as:

\[
\Lambda = \begin{bmatrix}
    \lambda_1 & 0 & \ldots & 0 \\
    0 & \lambda_2 & 0 & 0 \\
    \cdots & \cdots & \cdots & \cdots \\
    0 & 0 & 0 & \lambda_n
\end{bmatrix} \tag{4}
\]

The eigenvalues and eigenvectors (calculated with \texttt{eig}) were used for the calculation of the principal components of the correlation matrix. To compute the loadings of each PC, the eigenvectors were multiplied by the square root of the eigenvalues diagonal matrix (Equation (4)). The eigenvalues also allowed for calculating the portion of the total variance associated with the $j$th eigenvalue:

\[
\nu_j = \frac{\lambda_j}{\sum_j \lambda_j} \tag{5}
\]

In addition, the Varimax rotation was applied to facilitate the interpretation of the results and was calculated using the command \texttt{rotatefactors} over the loading matrix. The command \texttt{pca} was used to obtain the score matrix and \texttt{zscore} to obtain the z-score matrix.

3. Results

3.1. Properties of the Catalysts and Feeds

Some of the main properties of the catalysts are summarized in Figure 1: ST, Sm, SM, Ac and BL. The results in Figure 1 illustrate that all features of the studied catalysts correspond to those typical of the industrial FCC ones: ST of 124–190 m$^2$ g$^{-1}$; Sm of 63–139 m$^2$ g$^{-1}$; Ac of 0.04–0.12 mmol g$^{-1}$; and BL of 0.6–1.56.

CAT-1 is a spent catalyst that has been discarded from an industrial FCC unit and, as such, has relatively low ST, Ac and BL values. This is due to the degradation that occurs at the severe conditions of the FCC process. CAT-2 has a relatively high content of ST due to a greater proportion of zeolite (Z), as also shown by its high Sm proportion, and intermediate values of Ac and BL,
indicating that this catalyst is likely intended for the conversion of relatively “light” feeds (avoiding over cracking) and an increase in the olefin content and octane number of the products. On the other hand, CAT-3 has the lowest Sm value and the greatest Ac and BL values, which suggest that this catalyst would promote the conversion of heavier fraction by having the highest acidity and the highest mesopore area.

Figure 1. Main properties of the catalysts employed (CAT-1 to -3): (a) textural properties; and (b) acidic properties. See Table 1 for abbreviations.

The elemental analysis of the catalysts shows contents of Ni (741 ppm) and V (3335 ppm) one order of magnitude higher for the CAT-1 in comparison to CAT-2 and -3, again evidencing the spent nature of CAT-1. The rest of the compositions are relatively similar (Cu, Fe, Na and Al) except for the Re concentrations that are 2.50, 0.86 and 1.35 wt % for CAT-1 to -3, respectively.

Figure 2 displays the composition of the six feeds studied. All feeds (with the exception of STPO) consist primarily of an HCO (Hf) fraction with concentrations of 82.0–95.5 wt %. STPO, on the other hand, presents a significantly higher content of LCO (Lf, 29.3 wt %) and gasoline (Gf, 15.5 wt %), as a consequence of the thermal non-selective cracking that occurs in the pyrolysis process, directing product distribution towards lighter components and a low concentration of heavy hydrocarbons [53,54].

Regarding their chemical composition, while waxes consist only of linear paraffins (32.4 wt %) and olefins (67.6 wt %), the rest of the feeds are relatively similar in their chemical nature with an overall predominance of cyclic unsaturated (50.0–62.4 wt % aromatics) and saturated compounds (23.3–34.4 wt % naphthenes).
VGO + STPO mixture or VGO alone. In relation with Figure 2, this trend of scores is related with the representations. This graph also shows zooms of different sections of the PC1–PC2 (Figure 4c,d) and PC2–PC3 (not making a proper cluster). This observation indicates that processing STPO through the FCC approach at the different conditions will have a greater impact performance-wise than processing the VGO + STPO mixture or VGO alone. In relation with Figure 2, this trend of scores is related with the amount of HCO in the feed (Hf, which is particularly high for VGO and HDPE + VGO feeds, and lower for STPO). Indeed, the distinctive composition of the STPO (much lighter than the rest of feeds) is responsible to a certain degree for the clustering observed in the score plot of the cracking results (Figure 3). Overall, these results reveal that the composition of the feed should play an important role on the loadings of PC1.

Figure 4 displays the Varimax loading plots for PC1–PC2 (Figure 4a) and PC2–PC3 (Figure 4b). This graph also shows zooms of different sections of the PC1–PC2 (Figure 4c,d) and PC2–PC3 (Figure 4e,f) representations.

As shown in Figure 3a, the composition of the feed is strongly correlated with PC1, which describes 27.41% of the variance. The “negative” fractions of the feed (negative loadings), in PC1, are HCO (Hf) and paraffins (Pf), which are, hence, the least reactive fractions. On the contrary, gasoline (Gf) and LCO (Lf) present positive loading and are “favorable” fractions from an FCC performance perspective, being at the opposite side of the least reactive ones. Figure 4a indicates that there is a correlation (or proximity) between the HCO in the feed (Hf) and that of the products (HCO) and LCO indicating one
of the main pathways of reaction: HCO (unreacted) and HCO → LCO. Paraffins in the feed (Pf) are correlated with isoparaffins (IT) indicating the participation of isomerization reactions in the cracking mechanisms. On the other side of the PC1 (Figure 4a), naphthenes in the feed (Nf) are linked with the cycloolefins (naphthenes with double bounds, cOT), indicating the partial dehydrogenation of the cyclohexane and cyclopentane rings (most likely in Nf).

![Figure 3. Score plot for 104 uncorrelated runs in terms of: (a) PC1 vs. PC2; and (b) PC2 vs. PC3. The bars of the plots correspond to the histograms of the projections in each PC.](image)

Based on their loadings (highest and lowest along PC1), the distribution of boiling point fractions of the feed (Hf, Gf or Lf) has a stronger impact on process performance than its chemical composition (Pf, Of, Af or Nf). Besides, a cluster of points is observed on the left side of Figure 4a, which has been zoomed in Figure 4c. The “positive” fractions of the feed such as Lf and Gf are primarily converted into gasoline products (GL) with a high content of C7–9 hydrocarbons in the form of aromatics (AT). In particular, we observe relatively high loadings within PC1 for benzene (A6), toluene (A7), xylenes (A8) and C8+, alkyl aromatics, together with naphthenes (NT). These results illustrate the transformation of alkylated naphthenes (Nf) and aromatics (Af) present in the gasoline (Gf) and LCO (Lf) into partially dealkylated aromatics, contained in the produced gasoline (GL). It is worth mentioning that the variables describing process conditions and catalyst properties have very low impact, expressed as low loadings along PC1. The critical role of feed composition on the overall performance of the FCC process has been recurrently indicated before [12, 24, 28, 55].
Figure 4. Varimax loading plots for: (a) PC1 vs. PC2; and (b) PC2 vs. PC3. (c,d) zoomed areas of graph (a); and (e,f) zoomed areas of graph (b).

The process conditions are strongly correlated with PC2, which describes 19.09% of the variance. The three operational conditions (CO, t and T) are on one side of the plot because increasing each of
those (and specifically T) leads to an increase of severity of operation with higher cracking conversion. Within the conditions studied here, the trend of variables in increasing order of influence (loading) in the process are: catalyst-to-oil ratio (CO) < time (t) < temperature (T). A cluster of points is observed on the lower side of Figure 4a, which has been zoomed in Figure 4d. Time (t) strongly influences the content of coke (Ck) and octane number (RON), which present zero loading along PC1 and do not seem to be significantly affected by the properties of the feed. Some paraffins (such as P4 and PT) are also linked with t, presenting very similar loadings, as a result of the higher predominance of hydrogen transfer reactions at more severe process conditions, but their loadings along PC1 suggest that also feed properties are playing a role in their formation. Specifically, and based on Figure 4a, the PC1 loadings for PT and P4 indicate that the paraffin content in the feed (Pf) is determining in this regard. Temperature (T) influences the quality of the products, in terms of olefin content and RON, and quantity of the lighter fractions such as LPG and LG. Attention should be placed on the fact that olefins (OT) and propylene (O3), which is one of the most important products in the FCC, is more influenced by process conditions (PC2) and T in particular, than feed properties (PC1). These observations were already reported by Ibarra et al. [28] for the catalytic cracking of VGO + bio-oil blends. Specifically, temperature has a greater impact in the formation of gas products (LPG and LG) by favoring cracking reactions, in particular the extent of each type of reaction (monomolecular, bimolecular, etc.) [56]. Furthermore, T is also known to heavily determine the total yield of olefins in the products as a consequence of paraffin dehydrogenation reactions being favored [57,58].

The catalyst properties are strongly correlated with PC3, which describes 12.72% of the variance, as displayed in Figure 4b. Among the dependent products, only the coke content (Ck) seems to be affected by the catalyst properties, while the rest of the variables present loadings closer to zero along PC3. At the same time, Ck has a null loading of PC1 related with feed properties (see Figure 4a,d) and significant loading of PC2 related with process conditions, in particular related with time, as observed in Figure 4d. This behavior of coke demonstrated the significant impact of reaction time on coke formation [30].

The catalyst properties show two clusters of data points along PC3, which have been zoomed in Figure 4e,f. In this case, the main correlated properties to Ck are those concerning acidity and textural features (Figure 4e), in the following order: Ac > mV > BL > SM >> SM, Fe >> Al. Thus, among the catalyst properties, acidity descriptors are the ones that should be primarily considered for the modeling of cracking reactions [59]. Inversely, on the opposite side of PC3 (Figure 4f), the variables of the catalyst found present the following loading trend: P > Na > Ni ≈ V >> Re. These elements, and specifically the first four, are then correlated with the decrease of acidity in the original catalyst or the spent one.

As an overview of the variable categorization:

- Among the feed properties, the lump fraction with more than 20 carbons is the one affecting the most on the yields of cycle oils, whereas the fraction with less than 20 carbons is correlated with the amount and aromatic content of gasoline. The chemical composition of the feed is of lesser relevance than its boiling point distribution.
- Among the process conditions, the key variables are predominantly time and temperature, which are strongly correlated with the amount and olefin content of the lighter fractions (dry and liquified petroleum gases, with attention to propylene).
- Among the catalyst properties, two sets of variables have been obtained: those positively affecting the FCC performance, such as acidity and micropore area, and detrimental variables, such as the content of P, Na, V or Ni.

3.3. Reaction Network

The main goal of this work was to orientate the results of PCA for establishing a reaction network in the cracking of waste feeds. The most important set of parameters in the reaction were feed properties (PC1). Along with the feed composition (Table 1) and products, we have divided the reaction network
into a bi-dimensional area of insaturations and carbon number to facilitate reading the reaction network described in Figure 5. Table 1 shows that all feeds have a majority of aromatic and HCO fractions, except for PW (that does not contain aromatics) and STPO (that contains a significant fraction of LCO and gasoline). The amount of HCO in the feed (Hf) is linked with unconverted HCO and LCO of products (Figure 4a), and the amount of LCO and gasoline in the feed (Lf and Gf, respectively) is correlated with different aromatics in the gasoline products (Figure 4c). Given the aromatic nature of the products of FCC [60], one of the main pathways of the reaction is the dealkylation of aromatics from the HCO and LCO fractions into lighter ones in gasoline (k₁ and k₂ in Figure 5). At the same time, olefins with 5–7 carbons are linked with those reactants (Gf and Hf, Figure 4a), and thus formed as dealkylated products in gasoline (k₃).

![Reaction network proposed for the cracking of waste feeds based on PCA results.](image)

Paraffins of the feed (Pf) are correlated to the observed total isoparaffins (IT) in Figure 4a, thus PCA indicates that there is a kinetic rate constant of isomerization (k₄). All aliphatic molecules crack through β-scission and hydrogen transfer [17] to mainly sequentially produce olefins in the LCO (k₃), gasoline (k₅) and LPG (k₇) range. The cracking products (mainly olefins) are poorly affected by the composition of the feed (PC1), and strongly affected by process conditions (PC2) in particular by the temperature (Figure 4d). Thus, cracking reactions (particularly k₆ and k₉) of aliphatic molecules seem to have the highest activation energy among the overall reaction network. Paraffins (mainly pentane and butanes) derive from hydrogen transfer reactions and, at the same time, are linked with process conditions so an additional reaction rate quantifying this reaction is required in the reaction network (k₈).

The catalyst properties (PC3) do not play a significant role in the reaction network, as displayed in Figure 4b,e,f, but in coke (Ck) formation. In fact, we could establish two pathways of coke formation: one from polyaromatics and another one from paraffins (in the case of PW), as previously demonstrated [24,61]. Those two pathways would be represented in the reaction network as k₀ and k₁₀ and should depend on the HCO fraction of the feed (Hf, Figure 4b) and acid properties of the catalyst (Figure 4b,e).

4. Conclusions

We tested the principal component analysis (PCA) over a set of 104 uncorrelated fluid catalytic cracking (FCC) runs using different waste feeds, catalysts and operation conditions. This approach has proven to be suitable for assessing the impact of 64 variables categorized as feed, process, catalyst and product properties. Subsequently, we developed a simplified reaction network based on the data-driven information acquired through PCA.
The results show that each category of independent variables (feed, process and catalyst properties) has been correlated with a single principal component (PC) in such a way that the percentage of the total variance assigned to those categories results as: PC1, related with feed properties explains 27.41% of the variance; PC2, process conditions, 19.09%; and PC3, catalyst properties, 12.72%.

The PCA results show that the reaction network could be ascribed to a series of: (i) dealkylation of aromatics \( (k_{1-3}) \) to yield lighter aromatics and olefins; (ii) isomerization reactions of paraffins to isoparaffins \( (k_4) \); (iii) cracking reactions (\( \beta \)-scission) of aliphatics to yield light olefins in gasoline and LPG \( (k_{5-7}) \); (iv) hydrogen transfer reactions of olefins to yield light paraffins in LPG \( (k_8) \); and (v) coking reactions which depend on the amount of HCO of the feed and the acidic properties of the catalyst.

In this manner, we have proved that multivariate analysis is a powerful tool to propose a reaction network from where the succeeding reactor modeling could be embraced. At the same time, it provides analytical and compositional perspective, greatly simplifying highly complex FCC conversion processes, and thus presenting high industrial relevance.

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