Towards Safe Landing of Falling Quadruped Robots Using a 3-DoF Morphable Inertial Tail

Yunxi Tang\textsuperscript{1,}, Jiajun An\textsuperscript{1,}, Xiangyu Chu\textsuperscript{1,2*}, Shengzhi Wang\textsuperscript{1}, Ching Yan Wong\textsuperscript{2}, and K. W. Samuel Au\textsuperscript{1,2}


ded in an initial falling quadruped robot experiment, where the robot Unitree A1 with the 3-DoF tail can land safely subject to non-negligible initial body angles.

I. INTRODUCTION

A sequence of motions such as aerial reorientation and stable landing have been investigated in both animals \cite{1,2,5} and robots \cite{7,8}. Such motions are critical for safety and survival when animals or robots are subject to unexpected falls. For example, a falling cat can rotate its front and back bodies, swing its tail and legs to self-right before safe landing with four feet pointing downwards \cite{1}. Squirrels that were catapulted off a track could stabilize themselves using tail motion, allowing them to land successfully \cite{2}. In robots, especially for medium-size quadruped robots like Mini Cheetah and Unitree A1, they may suffer from the same safety issues in falling. Referring to the famous falling cat problem, we can call it falling quadruped robot problem. Thus, landing the quadruped robots safely needs to be solved.

There are two paradigms to approach such a problem:
1) designing landing strategies to search optimal contact sequence and optimize contact forces for landing impact;
2) using limbs or extra appendages to right the body to a horizontal pose and then applying simple landing controllers.

In the state-of-the-art work \cite{6}, the first paradigm has been implemented, but their results show that Mini Cheetah can only handle horizontal drops in hardware. Besides, the robot may be damaged because of uneven leg force distribution at touch-down when the body has significant orientation offset from the horizontal. The second paradigm aims to reorient the body to the horizontal even the desired pose (accommodating the terrain and environment) before touching down. This alleviates the burden of landing control and mitigates robots’ mechanical damage. In this paper, we will focus on the second paradigm and integrate a 3-DoF tail into a quadruped robot to enhance the capability of safe landing.

Although, recently, a few efforts have been made to acquire the reorientation-for-landing capability in quadruped robots, their performance is still far from that of their biological counterparts. The work \cite{7} has enabled, a big robotic cat, Mini-Cheetah to land on its feet from falls with initial pitch within ±90°, but the motion was constrained in sagittal plane. Similarly, \cite{8} presented a combination of 2D reorientation and landing locomotion behaviors based on a physical quadruped robot SpaceBok, although the same 3D behaviors were achieved in simulation. Within the mentioned work, the leg swinging is not effective in inducing angular momentum change, because 1) the Moment of Inertia (MoI) of the legs is relatively small, compared with that of bodies;
2) the workspace of the legs is limited and it may consume more time, compared with that of tails which are common in many quadruped animals. These limitations also explain why [7] added additional mass to the feet for increasing the legs’ MoI and [8] assumed the drop happened in a low gravity environment for increasing aerial duration.

Except for using legs [7]–[9], reaction wheels and tails have been included in quadruped robots for enhancing locomotion capability in both flight and stance phases. [10]–[12] used reaction wheels to assist locomotion, however, [10] can only stabilize the pitch motion in airborne, and [11], [12] showed the aerial reorientation capability in simulations although they built prototypes. In terms of the tails, a simple application is using a tail to reject disturbance along pitch [14], yaw [15], roll [16] directions. [17] used a 2-DoF tail to allow a quadruped robot Minitaur to reorient from a 90° pitch angle before landing. [19] proposed to use a serpentine robotic tail to stabilize body’s pitch and roll while landing. Among the work related to the tailed quadruped robots, only a few of them have provided hardware verification, especially focusing on planar (aerial) motion [16], [18]. Although [20] only built a reduced complexity quadruped robot for studying the serpentine robotic tail, no experimental results on the tailed robot have been provided. Considering multiple functions of the tail in quadruped robots, here we will constrain our attention on the reorientation-for-landing capability and the study of improving forward velocity (e.g., in [21]) or facilitating sharp turning (e.g., in [22]) will be our future interest.

In this paper, we propose to integrate a 3-DoF morphable inertial tail (pitch, yaw, and telescoping) into a quadruped robot for enabling 3D aerial reorientation and then inducing safe landing. To our best knowledge, only a few 3-DoF tails have been designed [26] [27], one of which [27] investigated the use of the 3-DoF tail for somersault motion with a twist, but only a small-size tethered monopod robotic platform was used. Although a 2-DoF tail is commonly used for 3D aerial reorientation, e.g., [23], there is a conflict between aerial reorientation and landing balance using a 2-DoF tail, because the 2-DoF tail configuration (or location) at the end of reorientation is uncontrolled and varies as different initial body angles. However, the tail configuration during stance phase has preference such that the tail’s collision with the ground should be avoided and minimal disturbance would be imposed on body balance. To this end, for the first time, we introduce the 3-DoF tail to a quadruped robot where the tail with the maximal length (degenerating to a 2-DoF tail) can be used for self-righting in 3D effectively. Also, the tail can be retracted before touch-down for impressing the tail’s side-effect and increasing the landing success. What we want to emphasize is the 3-DoF tail can be designed to be modular and potentially available for other robots.

The contributions of this paper are: 1) We integrate a 3-DoF morphable inertia tail into a quadruped robot and the tail can increase the quadruped robot’s 3D aerial righting capability for safe landing. In experiments, the tail can help the robot recover from a large 3D inclined posture to a desired posture during falling, which provides good preparation for the following safe landing task. 2) To reduce the potential damage to the quadruped robot, we design a flight-phase test platform that has a similar size and weight to the quadruped robot (Unitree A1) for initial experiments. Experimental results on the platform show the tail’s effectiveness on 3D body reorientation and its fast retraction speed (~2 m/s) before touch-down. 3) We complete a consecutive large 3D reorientation (zeroing 30° pitch and 30° roll offsets, and keeping yaw zero) and safe landing motion on the tailed A1 robot hardware.

II. SYSTEM MODELLING

The motion patterns of a tailed quadruped robot in the flight phase and stance phase are different. As mentioned before, the tail will keep its maximum length for effective body reorientation in most of the flight phase. The 3-DoF morphable tail actually degenerates to a 2-DoF tail in airborne and thus we can simplify the system as a low-dimensional model, 

![Fig. 2. Simplified system models of the tailed quadrupedal robot.](image)

simplified rigid body dynamic model (tSRBD) as shown in Fig. 2. \( L \) is the maximum tail length. \( \theta_{\text{pitch}} \) and \( \theta_{\text{yaw}} \) are the tail swing angles along the pitch and yaw directions, respectively. We only focus on the tail’s usage and assume the leg joints are kept at a proper configuration for preparing the robot to avoid the small weight and MoI are ineffective in aerial righting. Referring to the conventions in [29], the system state of tSRBD is defined as,

\[
q_f := [\mathbf{p} \ \Theta \ \mathbf{q}_i] \in SE(3) \times \mathbb{R}^2, \\
u_f := [\dot{\mathbf{p}} \ \omega \ \dot{\mathbf{q}}_i] \in \mathbb{R}^8,
\]

where \( \mathbf{p} = [p_x, p_y, p_z] \) is the position of the body’s center of mass (CoM) and \( \mathbf{q}_i = [\theta_{\text{pitch}}, \theta_{\text{yaw}}] \) is the tail’s joint positions. \( \Theta = [q_x, q_y, q_z, q_w] \) is the unit quaternion representation of the body orientation. Note that the body’s position, orientation, and linear velocity are represented in the inertial frame \( \{I\} \). The body’s angular velocity \( \omega \) is represented in the base frame \( \{B\} \). The equations of motion can be written as,

\[
M_f(q_f)u_f + b_f(q_f, u_f) + g_f(q_f) = S^T \tau,
\]

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where $M_f$ is the inertia matrix, $b_f$ is the Coriolis and centrifugal terms, and $g_f$ is the gravitational term. $\tau$ is the joint torques of the tail. $S$ is the selection matrix representing the under-actuation of the base,

$$S = [0_{2 \times 6} \ I_{2 \times 2}] \in \mathbb{R}^{2 \times 8}.$$ 

After an effective aerial reorientation, the tail will quickly retract to 1/4 of its maximum length (Fig. 2) before landing and the robot has similar mass distribution to its original state. In this paper, we focus on showing the paradigm of reducing landing control burden via effective flight phase control and thus a controller specific to landing (e.g., [6]) will not resort. Therefore, a stance-phase dynamic model is not specified as a simple PD leg joint controller works well enough for the stance-phase safe landing task.

### III. CONTROL FRAMEWORK

As a single controller is challenging in controlling a hybrid system, we develop a control framework to achieve the **falling quadruped robot** task in this section. The planning and control framework is shown in Fig. 3. The whole motion is divided into two phases: flight phase and stance phase. In the flight phase, the robot adjusts its body orientation via swinging the tail with its maximum length. Then, the tail will be retracted close to the body for landing preparation after body self-righting. In the stance phase, the robot mainly uses its legs instead of the tail to keep balance on the ground. Each phase can use different controllers in corresponding blocks (green blocks in Fig. 3). In this paper, we select a trajectory optimization based controller for the flight phase and a compliant joint PD controller for the stance phase.

#### A. Trajectory Optimization for Aerial Reorientation

To realize the reorientation task of the tailed quadruped robot, the internal dynamics (conversation of angular momentum) can be utilized to adjust the body orientation in airborne. Trajectory optimization (TO) is an effective way to plan trajectories or design controllers by exploiting system dynamics and incorporating state/control constraints. Here, we adopt the TO method to obtain an optimized trajectory offline given the height and initial configuration of the robot, and the optimal trajectories provides a safe reorientation reference due to the satisfaction of physical constraints. Specifically, a custom-made differential dynamic programming (DDP) solver is employed in the offline stage. More details of the solver can be found in [30]. The trajectory optimization problem is formed as below:

1) **Objective Function:**

$$J(x_0, \tau_{0:N-1}) = \sum_{k=0}^{N-1} \ell(x_k, \tau_k) + \ell_f(x_N),$$  \hspace{1cm} (3)

where $N$ is the horizon length and $x_0$ is the given initial state. State $x_k$ at the $k$-th time step is,

$$x_k = [p \ \Theta \ q_t \ \dot{p} \ \omega \ \dot{q_t}]_k.$$ 

The running and terminal objective functions, $\ell(x, \tau)$ and $\ell_f(x)$, are smooth functions which encode the reorientation tasks. To reorient the body, the running/terminal costs are chosen as,

$$\ell(x, \tau) = e(\Theta_d, \Theta) + \frac{1}{2} u_f^T Q_u u_f + \frac{1}{2} \tau^T R_\tau \tau$$  \hspace{1cm} (4)

where the attitude error $e(\cdot, \cdot)$ function (as in [25]) between the current body orientation and the desired $\Theta_d$ is defined as

$$e(\Theta_d, \Theta) = \frac{1}{2} \text{tr}(I - R^T(\Theta_d)R(\Theta)),$$  \hspace{1cm} (5)

where $R(\Theta)$ is the rotation matrix corresponding to the quaternion and $w$ is the weight for the final cost of the orientation ($w = 500$ in this paper). $Q_u$ and $R_\tau$ are positive semi-definite matrices for the regularization on the velocities and tail torques, respectively. As the translation of body CoM is not of interest during reorientation, the diagonal elements of $Q_u$ corresponding to $\dot{p}$ are set as zeros.

2) **System Dynamics Constraint:** The dynamical feasibility is enforced by the forward Runge-Kutta (RK4) integration of the system dynamics in the rollout of DDP method.

3) **Tail Joint Limitations:** In the tailed quadrupedal system, the workspace of the tail is limited within a cone in Cartesian space to avoid the self-collision with the body and legs. Hence the joint limitations of tail must be considered to avoid self-collisions,

$$f(q_t) \in X_t,$$  \hspace{1cm} (6)

where $f$ is the relative forward kinematics of the tail and $X_t$ is the feasible set of tail position.

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[Fig. 3. Planning and control framework for the tailed quadruped robot. An offline trajectory optimization is employed for the aerial reorientation and an additional flight tracking controller is designed as shown in the Flight Phase block. $h_s$ is the remained height after reorientation. A PD stance controller is used to keep the robot balance as shown in the Stance Phase block.]

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This page contains text related to the planning and control framework for a tailed quadruped robot. The framework includes an offline trajectory optimization for aerial reorientation and additional flight tracking control for stabilization during the stance phase. The dynamics of the robot, including the tail module, are modeled to ensure safe and efficient landing. The text explains the formulation of the optimization problem, which aims to minimize reorientation costs while respecting system dynamics and control constraints. The paper discusses the use of a custom-made differential dynamic programming (DDP) solver for the offline stage, emphasizing the importance of satisfying physical constraints and avoiding self-collisions with the tail. The trajectory optimization involves both running and terminal costs, with a focus on adjusting body orientation and maintaining balance during reorientation and landing. The control framework is depicted in Fig. 3, showing how different controller blocks are utilized in the flight and stance phases of the robot's motion.
4) Tail Actuation Limitations: The motor torques of the tail are also limited, which are piece-wise box constraints on the inputs
\[ \tau_{\text{min}} \leq \tau \leq \tau_{\text{max}}. \]  (7)

DDP can efficiently solve trajectory optimization problem through the parameterized control trajectory. The constraints in the problem are handled with Augmented Lagrangian approach and relaxed barrier function method sequentially in a hybrid framework [30]. The linear feedback policy along the optimal solution returned by DDP solver can also be used to stabilize the trajectory tracking in the flight phase.

B. Flight Controller

In the flight phase, the optimized trajectory is tracked with a time-varying linear feedback controller. The feedback tracking controller is in form of
\[ \tau = \tau_{\text{ref}} + K_p(q - q_{\text{ref}}) + K_d(q' - q'_{\text{ref}}), \]  (8)
where \( \tau_{\text{ref}}, q_{\text{ref}} \) and \( q'_{\text{ref}} \) are the optimized reference torques and reference joint trajectories obtained in the offline TO stage. \( K_p \) and \( K_d \) are proportional and derivative gains obtained from the feedback terms returned by DDP approach as mentioned in previous subsection. In addition, joint PD controllers are used to maintain leg configurations in airborne.

After the body orientation is adjusted to the desired orientation or the body descends to a certain height, the tail will be retracted to its minimum length quickly. Within the time duration of tail retraction, the robot legs are controlled by joint position controllers for landing preparation. Compared with the extended tail, the tail retractability makes the system CoM stay close to the geometric center of the support polygon, which alleviates the uneven force distribution of the feet in contact. Hence, the telescoping DoF turns to be important for the practical usage of appendages in falling quadruped robots.

C. Stance Controller

Once contact is detected, the system will switch to the stance controller. When the body orientation is well adjusted near the horizontal, less effort is needed to design a stance control strategy. To verify the feasibility of the proposed control framework, we employ a simple compliant joint PD controller to maintain each leg’s configuration and keep the system balance in the stance phase. More advanced stance control (e.g., [6]) will be our interest in the future work.

IV. SIMULATION VALIDATION

We firstly evaluated the proposed system integration and control framework in MuJoCo [32], which is a high-fidelity physics engine. The simulator runs at 1 kHz, where the system dynamics is simulated and the contacts between the feet and ground are detected. The friction coefficient is set as \( \mu = 0.8 \). In simulation, the tailed A1 robot was simulated to reorient its body and land safely from various initial orientations with a falling height of 1.85 m (\( p_z = 1.85 \)). We assumed that the tailed A1 robot started from static states in all simulations.

A. Aerial Reorientation

In the offline trajectory optimization stage, the desired orientation \( \Theta_d \) was set as [0, 0, 0, 1] and the time budget for the reorientation task was 0.4 s with \( N = 200 \). The forward dynamics of tSRBD in TO was implemented using the spatial-v2 package [28] in MATLAB. The nonlinear optimization problem was then solved with a custom-made DDP solver [30], where \textit{casadi} [31] was used as a tool of auto-differentiation for the derivative computations of the system dynamics, objective functions, and constraints. Solving such an optimization problem with zero controls as initial guess usually took from 100 to 200 iterations. The optimized results \( \tau_{\text{ref}}, q_{\text{ref}} \) and \( q'_{\text{ref}} \) were then interpolated with polynomials as the reference inputs for the tracking controller.

To verify the aerial reorientation capability, the tailed A1 robot fell with various initial body orientations in simulator. To give an intuitive visualization, the orientation was plotted in Euler angles (in yaw-pitch-roll). The simulation results with an initial orientation of [15°, 25°, 35°] were shown in Fig. 4 (a-b). The optimized trajectory (dashed line) was well tracked and the body attitude was adjusted to the desired, even though model errors (e.g., 1.4 x tail mass) were introduced manually. Simulation results with other initial body orientations were presented in Fig. 4 (c-d). These results demonstrated the robot’s 3D reorientation capability.

B. Consecutive Motion

To validate the consecutive motions of aerial orientation and safe landing, one trial was shown in Fig. 5. The robot was dropped with an initial Euler angle of [40°, 40°, 30°]. The tailed robot adjusted its body orientation by swinging the tail within the first 0.4 s then retracted the tail for landing. The contact was detected at 0.56 s and the system switched to the stance controller for keeping balance. From Fig. 5 (b),
there were body orientation errors at touch-down because of the disturbance caused by tail retraction. Small errors in pitch and roll (several degrees) can be eliminated by the landing control after the robot was settled down. To eliminate the error in yaw, three DoFs of the tail can be activated together under proper control, which will be our future study.

V. EXPERIMENTAL RESULTS

A. Experimental Setup

A 2.3 kg 3-DoF robotic tail prototype (850 g tail base package, 820 g tail scissor linkages, and 630 g tail mass end) was integrated into the Uniree A1 robot. The tail base was placed above the middle of the robot’s hinder hip motors. The tail can provide a large range of motion (pitch: $-90^\circ \sim 180^\circ$, yaw: $\pm 180^\circ$, tail length: 0.12 $\sim 0.49$ m). The tail end mass includes a T-motor Antigravity 5008 KV170 (Incl. Cable, open-source hardware VESC as the motor driver) and a worm gearbox (gear ratio 10:1), which controls the tail length. The tail’s pitch/yaw motions are controlled by the tail base that consists of two AK60-6 T-motors and a differential bevel gear gearbox. The differential actuation mechanism can provide a large range of motion and output torques. Other electrical components (battery, Raspberry Pi 3B+ control board, and IMU) were placed at the bottom of the body.

To verify the tailed quadruped robot’s aerial reorientation and landing capability safely and repeatably, we built up an auxiliary truss-structured platform for hanging and releasing the robot as shown in Fig. 6 (d). The tailed robotic system was suspended by four cables via electromagnetic holders. By adjusting the length of each cable, the initial body orientation and height can be set as desired. Once the start button in Fig. 6 (d) was pressed, the electromagnets de-energized and the controller was activated at the same time.

Since repeated dropping experiments may damage the motors of the quadruped robot, we designed a flight-phase test platform (Fig. 6 (a)) to test the aerial reorientation function initially. The flight-phase test platform consisted of a cuboid body and the same 3-DoF tail. The physical parameters of the test platform were given in Table I. We mainly repeated the aerial reorientation experiments on the test platform and then transferred to the tailed A1 robot with fine tuning. The body orientation and angular velocity were estimated from the internal IMU. A contact was detected by a sudden acceleration change in the vertical direction. A soft cushion was also laid on the ground to protect the robot.

B. Flight-Phase Test Platform Experiments

To validate the tail can increase the quadruped robot’s 3D aerial righting capability for safe landing, we dropped the test platform from various initial orientations onto the cushion from 1.85 m height. The initial body orientation was manually adjusted and the tail was kept in its zero joint configuration with maximal length. With the initial orientation, an optimized trajectory and tracking controller were offline planned as in discussed in Section III. To handle the model uncertainties, an additional feedback PD controller was hand-tuned to improve the tracking performance. We show the experimental results of three trials in Fig. 7 (a). The platform fell from three totally different initial orientations and the final orientations were successfully adjusted to the neighbourhood of the desired orientation at the end of the
flight phase. The observed errors are tolerable (within $\pm 10^\circ$) 
for quadrupedal robots’ landing. Especially, in the third trial, 
the initial roll offset was up to $-50^\circ$, which was a challenging 
orientation for common quadrupedal robots to recover from 
in falling. The motion snapshots of Trial #3 was shown in 
Fig. 7 (b). In the experimental results, we can see the 
tail started to retract its length at 0.35 s in airborne and 
kept retracting till touch down. The tail retraction speeds in 
experiments were repeatable (~2 m/s). In the experiments, 
the tail retraction sometimes got stuck because the tail’s 
fast swing speed created large centrifugal force and the tail 
telescoping motor attained its torque limits.

C. Tailed A1 Robot Experiments

To validate a consecutive large 3D reorientation and safe 
landing on a tailed quadruped robot, the tailed A1 robot was 
dropped from a non-negligible initial body angle (Fig. 1). 
The initial body angle was $[0^\circ, 30^\circ, 30^\circ]$ and the desired 
orientation was $[0^\circ, 0^\circ, 0^\circ]$. A relatively low height, 1 m, was 
selected for dropping, because the robot would not suffer 
from too large motor current. This safety-oriented height 
selection did not affect our goal of demonstrating feasibility. 
Limited by the flight duration, the tail control strategy was 
slightly different and the tail would retract earlier for a trade-off 
between the functions of tail swing and retraction. At 
0.38 s, the robot touched the ground and the tail retracted 
to its minimum length (Fig. 8). The body orientation almost 
converged to the horizontal plane, although the yaw angle 
was around $10^\circ$. One of reasons is that the tail retraction was 
not considered during reorienting the body. As shown in Fig. 
1, the robot can land stably even with the small orientation 
error. The same trial without tail retraction was conducted 
and a robot falling was observed (see supplementary videos). 
This further emphasizes the importance of the telescoping DoF.

VI. DISCUSSION

We have successfully used the 3-DoF tail for quadruped 
robot’s 3D aerial reorientation and further safe landing. 
However, the tail usage is still straightforward. To show the 
proof of concept, the 3-DoF tail degenerated to a 2-DoF one 
before body self-righting and the telescoping function was 
only used for landing preparation. Actually, the telescoping 
DoF can be involved in the whole flight phase, which may 
generate more effective reorientation behaviors towards more 
robust and safe landing. Although this practice requires a new 
model, it can eliminate the disturbance of tail retraction that 
occurrs currently. In the landing control, we used a simple PD 
controller since small orientation offset was achieved. More 
advanced landing strategies like contact-aware trajectory 
optimization can be introduced and it can fully make use of 
legs’ control authority to improve landing success. Lastly, we 
admit that the introduction of the tail would increase the total 
mass and may affect robot walking, but we did not directly 
change the foot design as [7]. The tail package weight can 
be further reduced by optimizing the tail design.

VII. CONCLUSION AND FUTURE WORK

In this paper, we proposed to integrate a 3-DoF tail 
module into a falling quadruped robot, enabling 3D aerial 
reorientation capability for safe landing. The simplified robot 
dynamic model was presented. We proposed a simple but 
effective control framework to demonstrate the feasibility 
of the system integration. A flight-phase test platform with 
comparable inertial properties to Unitree A1 was built for 
initial experimental verification, demonstrating the tail’s 
effectiveness on 3D body reorientation and fast retractability 
during falling. A consecutive large 3D reorientation and safe 
landing motion was successfully validated on the tailed A1 
robot. In the future, besides addressing the concerns 
mentioned in Discussion, we will investigate the advantages of 
the 3-DoF tail on assisting the quadrupedal locomotion, such 
as accelerating/decelerating and turning sharply. Besides, the 
tail’s telescoping function can be used for simple interactions 
with the environment, facilitating the deployment in real 
world. Further, developing an extensible soft tail (e.g., [33]) 
could be one alternative option for our 3-DoF rigid tail in 
the future.
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