Anharmonic lattice dynamics and thermal transport in type-I inorganic clathrates

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Abstract
The anharmonic phonon properties of type-I filled inorganic clathrates Ba$_8$Ga$_{16}$Ge$_{30}$ and Sr$_8$Ga$_{16}$Ge$_{30}$ are obtained from the first-principles calculations by considering the temperature-dependent sampling of the potential energy surface and quartic phonon renormalization. Owing to the weak binding of guest atoms with the host lattice, the obtained guest modes undergo strong renormalization with temperature and become stiffer by up to 50% at room temperature in Sr$_8$Ga$_{16}$Ge$_{30}$. The calculated phonon frequencies and associated thermal mean squared displacements are comparable with experiments despite the on-centering of guest atoms at cage centers in both clathrates. Lattice thermal conductivities are obtained in the temperature range of 50–300 K accounting for three-phonon scattering processes and multi-channel thermal transport. The contribution of coherent transport channel is significant at room temperature (13% and 22% in Ba$_8$Ga$_{16}$Ge$_{30}$ and Sr$_8$Ga$_{16}$Ge$_{30}$) but is insufficient to explain the experimentally observed glass-like thermal transport in Sr$_8$Ga$_{16}$Ge$_{30}$.

Keywords: clathrates, thermal transport, phonon, Boltzmann transport equation

Supplementary material for this article is available online

(Some figures may appear in colour only in the online journal)

1. Introduction

Type-I intermetallic clathrates, such as Ba$_8$Ga$_{16}$Ge$_{30}$, Sr$_8$Ga$_{16}$Ge$_{30}$ have an open cage-like crystal structure (figure 1) and are actively investigated for potential application in thermoelectric energy generation due to their phonon-glass and electron-crystal like properties [1, 2]. The cages in these clathrates can be occupied by heavy guest atoms (referred to as rattlers) which are loosely bound to the host lattice. The rattlers have large thermal amplitudes around their equilibrium positions producing several interesting effects like the peculiar lattice dynamics which result in flat low-frequency phonon modes with avoided crossings and low lattice thermal conductivity [3–9].

The thermal properties of type-I ternary clathrates X$_8$Ga$_{16}$Ge$_{30}$ (X: Ba, Sr, henceforth referred to as BGG and SGG respectively) have attracted many experimental and computational research studies [10–12]. Interestingly, while BGG behaves like a typical crystalline material and has a decreasing thermal conductivity with rising temperature, SGG shows a glasslike behavior with reverse temperature-dependence [10]. The measured thermal displacement of rattlers in SGG are abnormally large and inspired the development of off-centered multi-positioned rattler theory [13]. The off-centering of rattlers is proposed as the reason for glass-like thermal conductivity of SGG, though similar glass-like thermal conductivity is also reported for other clathrates without off-centering of rattlers with p- vs n-type doping of the material [14, 15]. Further, depending on the growth conditions, crystal-like thermal conductivity is measured now for several clathrates with potential off-centering of rattlers [16].

The computations are not helpful and for SGG, the phonon dispersion obtained from \textit{ab initio} driven finite-difference approach either resulted in imaginary phonon modes or the
mode-frequencies obtained for low-lying optical phonons are severe under-prediction of the experimentally measured values [16, 17]. The large thermal displacements of rattlers render strongly temperature-dependent force interactions, not accounted for by lowest-order theories considered so far in literature [18, 19].

Here, using temperature-dependent force constants and phonon renormalization theory [20], the anharmonic phonon properties of BGG and SGG clathrates are obtained in the temperature range of 50–300 K. We report the phonon frequencies, thermal displacements, and three-phonon scattering rates in the considered temperature range. Further, using the multichannel thermal transport theory, we also report the temperature-dependent contribution to thermal transport from particle-like phonon and wave-like coherent transport channels [21].

2. Theory and computational details

The harmonic phonon frequencies, \( \omega_{q\nu} \), and eigenvectors, \( \epsilon_{q\nu} \), are obtained by diagonalizing the dynamical matrix, \( D_q \), obtained as [22, 23]:

\[
D_q^{\alpha\beta,\gamma\delta} = \frac{1}{\sqrt{m_\alpha m_\beta}} \sum_{\rho} \Phi_{ij\rho\delta}^{\alpha\beta} \epsilon_{q} (r_{ij\rho} - r_{ij\delta}),
\]

(1)

where the summation is over all unit-cells in the lattice (N), \( m_b \) is the mass of atom \( b \) in the unit-cell, \( r_{ij\rho} \) is the position vector of atom \( b \) in the \( l \)th unit-cell, \( \Phi_{ij\rho\delta}^{\alpha\beta} \) is the real-space \( (ij, \alpha\beta) \)-element of the harmonic force constant matrix \( \Phi \), and \( q, \nu \) are phonon wavevector and polarization. The obtained phonon frequencies (and eigenvectors) are self-consistently corrected for higher-order anharmonicity via renormalization which requires higher-order anharmonic force constants.

While the anharmonic force constants can be obtained from the finite-difference of density functional theory (DFT) forces by displacing one or more atoms in the computational super-cell corresponding to the equilibrium positions of atoms, the force constants obtained from this approach samples the potential energy surface (PES) at 0 K. For moderately anharmonic solids, this 0 K sampling is adequate and results in a minimal error. For strongly anharmonic solids, such as clathrates, the PES anharmonicity is strongly dependent on atomic displacements and is a strong function of temperature. In this work, \( T \)-dependent force constants are obtained by force–displacement data fitting on thermally populated supercells. The thermal displacements, \( \eta_{ij\nu} \), of atoms in computational cells are obtained as [24],

\[
u_{ij\nu} = \frac{1}{\sqrt{N}} \sum_{q\nu} \frac{h (n_{q\nu} + 1)}{m_\nu \omega_{q\nu}} \sin (2 \pi \eta_{q\nu})
\times \sqrt{-\ln (1 - \eta_{q\nu}^2)} \epsilon_{b, q\nu} \epsilon^*_{q} r_{q\nu},
\]

(2)

where \( \eta_{1,q\nu} \) and \( \eta_{2,q\nu} \) are random numbers sampled from a uniform distribution and constrained by \( \eta_{1,q\nu} = \eta_{1,-q\nu} \) and \( \eta_{2,q\nu} = \eta_{2,-q\nu} \). The forces corresponding to these thermally displaced snapshots are obtained from DFT calculations. The temperature is taken into account in equation (2) via \( T \)-dependent population \( (n_{q\nu}) \) and the phonon frequencies are obtained from equation (1) via diagonalization of the bare harmonic force constants (as obtained from the density functional perturbation theory (DFPT) [25]) based dynamical matrix.

While extracting anharmonic force constants via force–displacement data fitting, the contribution of the corrected harmonic force constants (see equation (3) below) is removed from DFT forces. The anharmonic force constants are obtained using Taylor-series fitting to residual-force displacement dataset. The corrected harmonic force constants, \( \Phi_{ij\rho\delta}^{\alpha\beta} \), are obtained via self-consistent renormalization as [26]:

\[
\Phi_{ij\rho\delta}^{\alpha\beta} = \Phi_{ij\rho\delta}^{\alpha\beta} + \frac{h}{4N} \sum_{\rho'\gamma\delta} \sum_{\nu} \sum_{\gamma'\delta'} \frac{\eta_{1,q\nu}}{\omega_{q\nu} \sqrt{m_\rho m_\rho'}} \left( \frac{n_{q\nu}}{n_{q\nu}} + 1 \right) \epsilon_{q} (r_{ij\rho\nu} - r_{ij\rho'\nu})
\times \epsilon_{q}^* (r_{ij\gamma\delta'} - r_{ij\gamma\delta'}),
\]

(3)

where \( \Phi_{ij\rho\delta}^{\alpha\beta} \) represent the bare harmonic force constants (as obtained from DFPT), and \( n_{q\nu} \), \( \eta_{1,q\nu} \), and \( \eta_{2,q\nu} \) are the Bose–Einstein distribution and quartic force constants (as obtained from residual-force displacement data fitting above). The corrected harmonic force constants are obtained by iterating through equation (3) based on updated phonon frequencies and eigenvectors. Finally, the entire cycle of residual-force displacement data fitting and self-consistent renormalization is repeated until convergence to obtain the self-consistent set of corrected force constants.

The phonon scattering rates are obtained by considering the three-phonon scattering processes as [20, 22, 26]:

\[
\frac{1}{\tau_{q\nu}} = \sum_{q_1, q_2, q_3} \left\{ \left( n_{q_1\nu} - n_{q_2\nu} \right) W^+ \right\} + \frac{1}{2} \left( n_{q_1\nu} + n_{q_2\nu} + 1 \right) W^- \right\},
\]

(4)
where $W$ represents scattering probability matrix given by:

$$W^\pm = \frac{2\pi}{\hbar} \left| \Psi_{\mathbf{q}+\mathbf{q}_1}^\pm |\Psi_{\mathbf{q}}^0 \right|^2 \delta(\omega_{\mathbf{q}+\mathbf{q}_1} \pm \omega_{\mathbf{q}} - \omega_{\mathbf{q}_1}).$$  \hspace{1cm} (5)

The $\Psi_{\mathbf{q}+\mathbf{q}_1}^\pm$ are the Fourier transform of real-space cubic constants, $\Psi_{\mathbf{b}\mathbf{b}'\mathbf{f}\mathbf{f}',\mathbf{p}\mathbf{p}'}$, and are obtained as:

$$\Psi_{\mathbf{q}+\mathbf{q}_1}^\pm = N \left( \frac{\hbar}{2N} \right)^{\frac{3}{2}} \sum_{\mathbf{b} \mathbf{b}' \mathbf{f} \mathbf{f}' \mathbf{p} \mathbf{p}'} \Psi_{\mathbf{b}\mathbf{b}'\mathbf{f}\mathbf{f}',\mathbf{p}\mathbf{p}'}^\pm \times \frac{\delta_{\mathbf{b},\mathbf{b}'} \delta_{\mathbf{f},\mathbf{f}'} \delta_{\mathbf{p},\mathbf{p}'} e^{i(q_1 \cdot \mathbf{r}_0 + q \cdot \mathbf{r})}}{\sqrt{m_\mathbf{b} m_\mathbf{f} m_\mathbf{p} \omega_{\mathbf{b}+\mathbf{q}} \omega_{\mathbf{f}' \mathbf{p}} \omega_{\mathbf{q}_1}}}. \hspace{1cm} (6)$$

The $\delta$ in equation (5) represents the delta-function ensuring energy conservation and the summation in equation (6) is performed over phonon wavevectors satisfying crystal momentum conservation, i.e., $\mathbf{q} + \mathbf{q}_1 + \mathbf{q}_2 = \mathbf{G}$, where $\mathbf{G}$ is the reciprocal space lattice vector.

The total thermal conductivity is obtained as:

$$k^{\text{tot}} = k^p + k^c, \hspace{1cm} \text{(7)}$$

where $k^p$ and $k^c$ are the contributions of particle and coherent channel towards the thermal transport \cite{21}. The contribution of particle channel towards the thermal conductivity in the $\alpha$-direction is obtained by solving the Boltzmann transport equation and using the Fourier’s law as \cite{22}:

$$k^p_\alpha = \sum_q \sum_\nu c_{\nu q} v_{\nu q,\alpha}^3 \tau_{\nu q,\alpha}, \hspace{1cm} \text{(8)}$$

where $c_{\nu q}$ is the phonon specific heat and $v_{\nu q,\alpha}$ is the $\alpha$ component of phonon group velocity vector $\mathbf{v}_{\nu q} (\nu q = \frac{\omega_{\nu q}}{c^\nu})$. The phonon specific heat are obtained from the phonon vibrational frequencies as:

$$c_{\nu q} = \frac{\hbar \omega_{\nu q}}{V} \left( \frac{\partial \omega_{\nu q}}{\partial T} \right) = \frac{\hbar k_\mathbf{q} x^2 \epsilon^x}{(e^{\epsilon^x} - 1)^2}, \hspace{1cm} \text{(9)}$$

where $V$ is the crystal volume, $k_\mathbf{q}$ is the Boltzmann constant, and $x = \frac{\hbar \omega_{\nu q}}{k_\mathbf{q} T}$. The coherent contribution towards the lattice thermal conductivity is obtained using the formulation of Simoncelli et al \cite{21} as:

$$k_\alpha^c = \frac{\hbar^2}{k_\mathbf{q} T^2 V N} \sum_q \sum_{\nu \neq \nu_1} \frac{\omega_{\nu q} + \omega_{\nu_1 q}}{2} V_{\nu q,\alpha} V_{\nu_1 q,\alpha}^* \times \frac{\omega_{\nu q} \tau_{\nu q} (\tau_{\nu q} + 1) + \omega_{\nu_1 q} \tau_{\nu_1 q} (\tau_{\nu_1 q} + 1)}{4(\omega_{\nu q} - \omega_{\nu_1 q})^2 + (\Gamma_{\nu q} + \Gamma_{\nu_1 q})^2} \times (\Gamma_{\nu q} + \Gamma_{\nu_1 q}). \hspace{1cm} \text{(10)}$$

$\Gamma_{\nu q}$ in equation (10) is phonon linewidth ($\Gamma_{\nu q} = 1/\tau_{\nu q}$) and $V_{\nu q,\alpha}$ is the $\alpha$-component of velocity operator obtained as:

$$V_{\nu q,\alpha} = \frac{1}{2 \sqrt{\omega_{\nu q} \omega_{\nu_1 q}}} \left( e_{\nu q,\alpha} \frac{\partial \mathbf{p}}{\partial q} | e_{\nu_1 q} \right). \hspace{1cm} \text{(11)}$$

The thermal mean squared displacements of atom $b$ in $\alpha$ direction are obtained as,

$$\langle |u_{\alpha}(bl, t)|^2 \rangle = \frac{\hbar}{2 N m_b} \sum_{\nu q} \omega_{\nu q}^2 (1 + 2 n_{\nu q}) |e_{\nu q}(b)|^2, \hspace{1cm} \text{(12)}$$

where the phonon frequencies, $\omega_{\nu q}$, and eigenvectors, $e_{\nu q}(b)$, are obtained using the renormalized force constants.

The open-source quantum mechanical simulation package Quantum Espresso is used to perform the DFT calculations with scalar-relativistic PBE exchange-correlation functional based ultra-soft pseudopotentials. The planewave kinetic energy cutoff and electronic wavevector grid are set at 60 Ry and $2 \times 2 \times 2$ respectively. The total energy change is less than $5 \times 10^{-5}$ Ry/atom on increasing the kinetic energy cutoff to 100 Ry or electronic wavevector grid to $6 \times 6 \times 6$. The structures are fully relaxed to ensure residual forces are less than $10^{-5}$ Ry/Bohr. The relaxed lattice constants as obtained using these settings are 10.95 Å and 10.86 Å for BGG and SGG respectively which are an over-prediction of experimentally measured lattice constants by 2% and 4% \cite{27} and is a known shortcoming of PBE functional \cite{28}. We note that we have tested the effect of overprediction of lattice constant on PES by extracting PES corresponding to 6d Sr atoms in the plane parallel to the hexagonal face of the tetrakaidecahedral cage at computationally relaxed and experimentally measure lattice constants. We found that there is no qualitative difference in the PES extracted at two considered lattice constants and, in particular, the PES has a single potential well in both cases.

The harmonic force constants are initially obtained on a $2 \times 2 \times 2$ phonon wavevector grid using the DFPT calculations and are later interpolated to a $8 \times 8 \times 8$ grid during the renormalization process. The cubic and quartic force constants are obtained by force–displacement data fitting on a $2 \times 2 \times 2$ computational cell consisting of a total of 432 atoms. 150 such thermally displaced cells are used in this study resulting in a total of 194400 equations. The cubic force constant interactions are included up to 5 Å and the quartic force constant interactions are limited to first neighbor shell. The three-phonon scattering rates are obtained on a phonon wavevector grid of size $8 \times 8 \times 8$. The obtained total thermal conductivities are converged to within 5% with these choices of simulation parameters.

### 3. Structure

The crystal structure of type-I inorganic clathrate is shown in figure 1. The structure belongs to cubic space group $Pm\bar{3}m$ with spacegroup number 223. The cage atoms occupy sites $6c$, $16i$, and $24k$ and encapsulate the guest atoms located at sites $2a$ and $6d$. The primitive unit cell is composed of 54 lattice sites of which 46 are occupied by Ga (16i) and Ge (6c and 24k) atoms and 8 ($2a$ and $6d$) are occupied by Ba/Sr atoms. The cages at $2a$ sites are isotropic and are composed of 12 regular pentagonal surfaces. The cages at $6d$ sites are asymmetric with 12 pentagonal and two hexagonal surfaces. For $2a$ cages, the bond...
stiffness corresponding to Ba and Sr guest atoms (calculated by displacing guest atom by 0.01 Å in required directions) are 1.62 and 1.06 eV Å$^{-2}$. For 6d cages, the stiffness is anisotropic and is 0.34 (0.12) and 0.84 (0.46) eV Å$^{-2}$ in directions parallel and perpendicular to six-membered rings for Ba (Sr) atom.

Previous literature studies have suggested the off-centering of the guest atoms in 6d cages for Sr atoms [5, 9, 18, 29]. There have been studies where theoretical models have been used to explain guest off-centering [13, 30], however, to the best of our knowledge, these studies are all fitted to explain the experimentally observed large thermal displacements of atoms and there are no studies explaining guest off-centering using \textit{ab initio} methods. The attempts on using \textit{ab initio} calculations for SGG either resulted in imaginary modes with on-centered guest atom or the obtained guest frequencies are way lower than experimental measurements [17]. We believe that these anomalous theoretical results are due to (i) the use of finite-difference approach for the extraction of phonon frequencies, and (ii) non-accounting of anharmonic effects on phonon frequencies. In particular, the PES is relatively flat for Sr atoms (as is evident from very low stiffness of 0.12 eV Å$^{-2}$) and the obtained forces in finite-difference method are comparable to numerical noise, thus resulting in numerical displacement-size dependent frequencies in the findings of Christensen \textit{et al} [16]. Further, in the same study, the authors obtained 1.6 times smaller phonon frequencies compared to that measured in experiments for low-lying optical modes using the experimentally extracted anisotropic harmonic force constants. To comply with experimental findings, authors assumed that somehow the atoms are experiencing isotropic forces around their equilibrium positions and the proposed isotropic model resulted in an excellent agreement with experimental results. As will be shown later, this under-prediction of frequencies from anisotropic harmonic model is due to ignorance of higher-order effects and with inclusion of anharmonicity, the obtained frequencies are in perfect agreement with experiments without the use of isotropic assumption (the latter was assumed by authors due to random hopping of rattler atoms between different off-centered sites).

Our structure relaxation suggests energetically-stable on-centered positions for both Ba and Sr clathrates. We explored the PES around the centered-positions by manually displacing rattler atoms in the plane parallel to hexagonal face of tetrakaidecahedral cage and plot the resulting energies in figure 2. We observe that for both clathrates, the on-centered position has lowest energy. We have also carried out similar PES mapping for suggested off-centered site of Sr at (0.6, 0.6, 0.1) Å [8, 10] and found the similar behavior. As such, we have used on-centered guest atoms for all calculations reported in this work. This choice is further justified since the experimentally extracted energy barrier for off-centered tunneling of rattlers in SGG is ∼5 meV and is smaller than the thermal energy of atoms in the temperature range of interest (50-300 K) [9]. It is worthwhile to emphasize that this 5 meV tunneling barrier is within the numerical noise of different simulation parameters used in this study and is, therefore, not resolvable here.

4. Phonon dispersions

The anharmonic phonon dispersion of BGG and SGG clathrates as obtained using the temperature-dependent force constants are plotted in figures 3(a) and (b) along with the atom-decomposed density of states and inverse participation ratio. The inverse participation ratio is a measure of mode localization and varies between $1/N_{\text{unit}}$ and 1 for completely localized and delocalized modes ($N_{\text{unit}}$ is the number of atoms in the unitcell, 54 for considered clathrates). The DFPT phonon dispersion in figure 3 corresponds to the lowest-order theory, i.e., under harmonic assumption and without considering $T$-dependent PES or phonon renormalization. The experimentally measured Raman modes at 300 K are from reference [29].

For both BGG and SGG, the acoustic phonons remain majorly unaffected with temperature and are delocalized with predominant contribution from cage atoms. In contrast, optical phonons undergo strong renormalization with temperature and become stiff at high temperatures. The effect is maximum for low frequency optical phonons and the frequencies become stiffer by 15 and 50% for these phonons at the gamma point at 300 K. These low frequency optical modes have predominant contribution from guest atoms centered inside 6d cages. Consistent with the rattling motion of these atoms, the inverse participation ratio of these modes is smaller than 1.

5. Mean square displacements

Moving further, the thermal mean square displacements are obtained using the temperature-dependent phonon dispersion for atoms sitting at different lattice sites and the results are presented in figure 4. For guest atoms at 2a sites and cage atoms, the thermal displacements are isotropic (i.e., $\langle u_x^2 \rangle = \langle u_y^2 \rangle = \langle u_z^2 \rangle = U_{\text{iso}}$) and varies between 0.01–0.02 Å$^2$.
Figure 3. The anharmonic phonon properties of (a) BGG and (b) SGG clathrates as obtained using the temperature-dependent sampling of the PES and quartic phonon renormalization. The open circles in dispersion plots represent experimentally measured Raman frequencies at a temperature of 300 K from reference [29, 31]. The density of states and inverse participation ratio are reported in side-figures for 300 K.

at 300 K which are consistent with experimental measurements [5, 10, 18, 32–35] and are similar in range to other crystalline materials [20, 36]. For guest atoms at 6d sites, the displacements are anisotropic and are larger than 0.02 Å² in the plane parallel to the hexagonal face of the tetrakaidecahedral cage \(\langle u_x^2 \rangle = \langle u_y^2 \rangle = U_\parallel \) and \(\langle u_z^2 \rangle = U_\perp \). The \(U_\parallel > U_\perp \) for both BGG and SGG, since the stiffness in \(\perp\) directions are higher. For BGG at 300 K, the obtained thermal displacements are 0.018 and 0.039 Å² for 6d cage atoms in the planes perpendicular and parallel to hexagonal face of tetrakaidecahedral cage. These numbers compare well with the experimental measured values of 0.015–0.018 and 0.046–0.052 Å² by Christensen et al. [18] For SGG, the corresponding calculated numbers are 0.026 and 0.067 Å². The comparison with experiments is not possible for SGG due to a wide spread in the measured values (0.03–0.08 Å² using the isotropic model and 0.03 and 0.14 Å² using the anisotropic model [5, 10, 32–34]).

The results reported in figure 4 clearly suggest that the accuracy of lowest-order harmonic theory decreases at high temperatures. At a temperature of 300 K, the lowest-order theory predicts erroneously large thermal displacement of 0.18 Å² for Sr atoms located at 6d sites; thus highlighting its failure in describing anharmonic phonons and associated thermal properties of SGG.

6. Lattice thermal conductivity

Next, we calculate the phonon scattering rates by considering the three-phonon processes and report the resulting
mode-dependent lifetimes and mean free paths at a temperature of 300 K for BGG and SGG in figures 5(a) and (b). It is recently reported that in rattler-like compounds, the mean free paths of phonons could be shorter than the Ioffe–Regel limit and thereby question the validity of particle-like phonon picture [20, 21, 37, 38]. For considered clathrates, the obtained mean free paths for majority of the phonons are larger than the Ioffe–Regel limit (obtained as the minimum interatomic distance). Nevertheless, we calculate the temperature-dependent thermal conductivities of both clathrates using the multi-channel transport model [21] and report the results in figures 5(c) and (d). The contribution of coherent transport channel towards thermal transport is 13% and 22% in BGG and SGG at a temperature of 300 K. With reducing temperature, while the total predicted thermal conductivity increase for both BGG and SGG, the experimentally observed trend is crystalline and glass-like for BGG and SGG respectively. We believe that these different temperature trends in the computed and experimentally measured thermal conductivity of SGG could be due to (a) off-centering of guest atoms in experimentally synthesised samples of SGG [16], (b) contribution from higher order phonon scattering and renormalization terms in the computed thermal conductivity of SGG, (c) electron-phonon interactions which alter the nature of thermal transport as reported earlier [11, 14].

At last, we also compute the phonon thermal conductivity accumulation functions for the particle and coherent transport channels at 300 K and report the results in figures 6(a) and (b). As can be seen from figure 6(a), the modes with frequencies lower than 2.0 THz are the main contributor to the particle-like transport channel in both BGG and SGG. As discussed above, these modes are majorly dominated by 6d rattler atoms. In case of coherent transport channel, the contribution of such modes is significantly lower, as all frequency modes contribute to thermal transport via coherent channel in BGG and SGG as shown in figure 6(b).

7. Conclusions

To summarize, we obtained temperature-dependent phonon properties of type-I clathrates BGG and SGG accounting for anharmonic effects. In contrast with experiments, our calculations suggest stable on-center position for both Ba and Sr in tetrakaidecahedral cages which could be a limitation of the pseudopotentials and/or simulation parameters used in this study. With on-centered guest atoms, we are able to reproduce experimentally observed thermal displacements of rattler atoms at various temperatures. For thermal conductivity of BGG, we are able to reproduce the experimentally measured value at 300 K and the associated temperature-dependence. In case of SGG, while we find that the coherent channel contribution to thermal transport is significant, the multi-channel thermal transport model with on-centering of guest atoms is insufficient in explaining the experimentally observed glass-like temperature-dependence of the thermal conductivity.

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Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

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