Impact of dark matter decays and annihilations on reionization

M. Mapelli, 1⋆A. Ferrara 1 and E. Pierpaoli 2

1SISSA, International School for Advanced Studies, Via Beirut 4, 34100 Trieste, Italy
2Theoretical Astrophysics, California Institute of Technology, Pasadena, CA 91125, USA

Accepted 2006 March 31. Received 2006 March 30; in original form 2006 February 16

ABSTRACT

One of the possible methods to distinguish among various dark matter (DM) candidates is to study the effects of DM decays. We consider four different DM candidates [light dark matter (LDM), gravitinos, neutralinos and sterile neutrinos], for each of them deriving the decay/annihilation rate, the influence on reionization, matter temperature and cosmic microwave background (CMB) spectra. We find that LDM particles (1–10 MeV) and sterile neutrinos (2–8 keV) can be sources of partial early reionization (z ≤ 100). However, their integrated contribution to Thomson optical depth is small (≤ 0.01) with respect to the 3-yr WMAP results (τ e = 0.09 ± 0.03). Finally, they can significantly affect the behaviour of matter temperature. On the contrary, effects of heavy DM candidates (gravitinos and neutralinos) on reionization and heating are minimal. All the considered DM particles have completely negligible effects on the CMB spectra.

Key words: neutrinos – dark matter.

1 INTRODUCTION

The nature of dark matter (DM) is one of the crucial open questions in cosmology. In the so-called cold dark matter (CDM) theory, DM particles are defined as ‘cold’ particles, because of their negligible free-streaming length (i.e. the length below which dark matter fluctuations are suppressed). The most famous alternative model to CDM is called warm dark matter (WDM), where DM particles are defined as ‘warm’ because of their longer free-streaming length. In WDM scenarios, the velocity dispersion of the particles is sufficient to smear out the fluctuations up to galactic scales, depending on the mass of the particles (Padmanabhan 1995). This means that WDM models can alleviate the so-called substructure crisis, which represents one of the most serious problems of CDM theories (Bode, Ostriker & Turok 2001; Ostriker & Steinhardt 2003). At present, there is no definitive evidence which allows us to exclude one of the two scenarios and even the properties (mass, lifetime, etc.) of CDM and WDM particles are substantially unknown.

From an observational point of view, one of the most direct ways to detect DM particles and, maybe, distinguish between CDM and WDM is represented by particle decays (Chen & Kamionkowski 2004; Pierpaoli 2004). A small fraction of DM particles is expected to decay, the lifetime of this process generally depending on their density and mass. Many of the possible decay channels (Dolgov 2002) involve the emission of photons at wavelengths depending on the particle mass. So, in principle, it is possible to distinguish among various dark matter models, depending on the characteristics of emitted photons. It has also been pointed out (Sciama 1982; Chen & Kamionkowski 2004; Hansen & Haiman 2004; Kasuya, Kawasaki & Sugiyama 2004; Kasuya & Kawasaki 2004; Mapelli & Ferrara 2005; Padmanabhan & Finkbeiner 2005; Zhang et al. 2006) that photons due to particle decays or annihilations can be sources of partial early reionization. In addition, the heating induced by particle decays can leave an imprint in the 21-cm background, which could be detected by new generation of radio telescopes (LOFAR, PAST, SKA, etc.).

At the moment, constraints on the radiation emitted by particle decays are loose. The SPI spectrometer aboard ESA’s INTEGRAL satellite recently detected an excess in the 511-keV line emission, due to positron–electron annihilation, from the galactic bulge (Knödlseder et al. 2005). The only two viable explanations are that this excess is due to positrons produced by thermonuclear Type Ia supernovae (Dermer & Murphy 2001) or by decaying/annihilating dark matter (Boehm et al. 2004; Hooper & Wang 2004). This last hypothesis, although exotic, has triggered many theoretical studies (Cassé & Fayet 2005; Kawasaki & Yanagida 2005; Kasuya & Takahashi 2005; Ascasibar et al. 2006; Kasuya & Kawasaki 2006), which are aimed to put constraints on various DM properties by using SPI/INTEGRAL observations.

In this paper, we consider some of the most popular CDM and WDM particles, calculating their approximate decaying rate (Section 2), their influence on the ionization fraction, on the Thomson optical depth, on the behaviour of matter temperature (Sections 3 and 4) and on the cosmic microwave background (CMB) spectra (Section 5).

In all the cases, we make the assumption that the DM is composed of one single species of particles. We consider only ‘standard’ DM

1⋆E-mail: mapelli@sissa.it

© 2006 The Authors. Journal compilation © 2006 RAS

Downloaded from https://academic.oup.com/mnras/article-abstract/369/4/1719/1089692 by guest on 27 July 2018
candidates, neglecting more exotic scenarios (such as Q-balls, light scalar bosons, etc.). In particular, we study three different candidates for the case of CDM: (i) the axino, as representative of light dark matter (LDM; 1–100 MeV; Hooper & Wang 2004), (ii) the gravitino and the (iii) neutralino, as heavy DM candidates (≥100 MeV). For the WDM, we consider only the sterile neutrino, reducing our analysis to its radiative decay channel. In fact, we do not pretend to present a complete overview of DM candidates. Instead, we would like to give a basic description of the effects of DM decays, taking as an example some of the standard DM candidates. Our aim is to point out the differences among the considered DM particles, with particular care for cosmic reionization and heating.

2 METHOD

For each considered particle model, we derived the energy injection rate per hydrogen nucleus, $\epsilon_{\text{DM}}$, as follows.

In comoving coordinates, the photon emission rate due to particle decay can be generally written as:

$$\frac{dn}{dt} = \frac{n_0}{\tau} e^{-(n_0 - n_0(\tau/r))r},$$

(1)

where $n_0$ and $\tau$ are the current density and the lifetime of particles, respectively, and $t(\tau) = \frac{1}{2}H_0^{-1}\Omega_0^{1/2} (1 + z)^{-3/2}$ (neglecting $\Omega_\Lambda$) is the time elapsed from the big bang to redshift $z$.

Instead, in the case of annihilations, the photon emission rate in comoving coordinates is

$$\frac{dn}{dt} = n_0^2 (1 + z)^3 \sigma v C,$$

(2)

where $\sigma v$ is the annihilation cross-section (see Section 3.3 for details) and $C$ is the clumping factor. To quantify $C$ is beyond the scope of this paper. However, especially at very high redshift ($z \gg 10$), where annihilations play their most important role, we can roughly approximate $C \sim 1$.

Then, in both the cases $\epsilon_{\text{DM}}$ is simply:

$$\epsilon_{\text{DM}} = \frac{dn}{dt} \frac{E_v}{n_b},$$

(3)

where $E_v \sim m_{\text{DM}}/2$ is the energy of the emitted photon ($m_{\text{DM}}$ being the mass energy of the DM particle), and $n_b$ the current density of baryons (we take $n_b = 2.7 \times 10^{-7}$ cm$^{-3}$, Spergel et al. 2003).

The energy $\epsilon_{\text{DM}}$ partially goes into ionizations of hydrogen and helium atoms and partially into heating. We adopt the rough approximation by Chen & Kamionkowski (2004), for which a fraction $(1 - x)/3$ of $\epsilon_{\text{DM}}$ contributes to ionizations and a fraction $(1 + 2x)/3$ goes into heating ($x$ being the ionized fraction). This approximation is correct if the DM decays/ annihilations produce (directly or via secondary interactions) photons whose energy is mostly absorbed by the intergalactic medium in a Hubble time. As fig. 2 of Chen & Kamionkowski (2004) shows, photons emitted by sterile neutrinos (∼1–4 keV) fully satisfy this requirement. Particle decays/ annihilations which produce electrons of energy lower than ∼1 GeV (Chen & Kamionkowski 2004) equally satisfy this requirement, because these electrons can lead (by collisional ionization, excitation or inverse-Compton scattering) to photons which are immediately absorbed. Then, also for LDM and gravitinos we can adopt the approximation of Chen & Kamionkowski (2004).

For neutralinos (whose mass is higher than 30 GeV), this approximation is far too optimistic; however, we can consider it as an upper limit. In practice, in the optically thin case most of the decay/annihilation products can propagate to a redshift of 0 and can be constrained by observing the X-ray/gamma-ray background (Chen & Kamionkowski 2004).

We made our calculations using an upgraded version of the public code RECFAST (Seager, Sasselov & Scott 1999, 2000). In particular, we modified the evolution equations as follows (Padmanabhan & Finkbeiner 2005).

$$-\frac{dE_{\text{He}}}{dz} = \frac{\epsilon_{\text{DM}}}{E_{\text{He}}} \left[ \frac{1 - x_{\text{He}}}{3(1 + f_{\text{He}})} \right] \epsilon,$$

(4)

$$-\frac{dE_{\text{He}}}{dz} = \frac{\epsilon_{\text{DM}}}{E_{\text{He}}} \left[ \frac{1 - x_{\text{He}}}{3(1 + f_{\text{He}})} \right] \epsilon,$$

(5)

$$-\frac{dT_{\text{He}}}{dz} = \frac{2\epsilon_{\text{DM}}}{3k_B} \left[ 1 + 2x_{\text{He}} + f_{\text{He}} (1 + 2x_{\text{He}}) \right] \epsilon,$$

(6)

where $x_{\text{He}}$ is the ionized fraction of hydrogen (helium) atoms, $E_{\text{He}} = 13.6$ eV ($E_{\text{He}} = 24.6$ eV) is the ionization energy of hydrogen (helium) atoms, $f_{\text{He}}$ is the helium-to-hydrogen ratio by number, $T_M$ is the matter temperature and $k_B$ the Boltzmann constant and $\epsilon \equiv [H(z)(1 + z)]^{-1}$.

3 COLD DARK MATTER

First, we consider CDM particles. Heavy CDM particles (≥100 MeV) are not considered a viable source for the 511-keV emission in the galactic centre. In fact, in the case of neutralinos (with mass higher than 30 GeV), the request of a sizable R-parity violation, needed to allow considerable neutralino decays, would determine a too short lifetime and the neutralino would cease to be a good DM candidate (Hooper & Wang 2004). On the other hand, gravitinos decays are possible; but the gravitino lifetime is far too long to match the 511-keV emission from the galactic centre (Hooper & Wang 2004). Then, previous studies (Boehm et al. 2004; Hooper & Wang 2004; Ascasibar et al. 2006) proposed light cold DM candidates (1–100 MeV) to be sources of the 511-keV emission from the galactic centre. In the following, we will consider first LDM particles (axinos) and secondly heavy DM particles (gravitinos and neutralinos).

3.1 Light dark matter

LDM candidates (1–100 MeV) can produce positrons both via decay (axinos, Hooper & Wang 2004) and via annihilation (Boehm et al. 2004). They can easily explain the 511-keV emission from the galactic centre and satisfy the DM relic density ($\Omega_\text{DM} \sim 0.23$, Spergel et al. 2003). The upper limit of their mass, if they are the source of the 511-keV line, is probably much less than 100 MeV, due to constraints on the bremsstrahlung emission (Beacom, Bell & Bertone 2005; Cassé & Fayet 2005; Beacom & Yüksel 2006).

Hooper & Wang (2004) derived in a very simple way the lifetime of decaying LDM particles (i.e. axinos) necessary to produce the observed 511-keV emission:

$$\tau \sim 4 \times 10^{38} \left( \frac{m_{\text{LDM}}}{\text{MeV}} \right)^{-1} \text{s},$$

(7)

where $m_{\text{LDM}}$ is the mass of a LDM particle. Under our assumptions, the current density of LDM particles can easily been derived as:

$$n_0 = \Omega_\text{DM} \rho, \frac{m_{\text{LDM}}^{-1}}{m_{\text{LDM}}},$$

(8)

where $\rho_*$ is the critical density of the Universe. Substituting equations (7) and (8) into equation (1) and implementing it in RECFAST.
that gravitinos are unable to produce the 511-keV excess from the galactic centre.

### 3.3 Heavy dark matter: neutralinos

Here, we will consider as ‘heavy’ dark matter the neutralinos. It is a merely indicative classification, given the uncertainties on the various models. The discussion of the details of different supersymmetric models is beyond the purpose of this paper. Neutralinos are thought to be very massive ($m_{\chi} > 30$ GeV). So, if they could decay (violating the R-parity), their lifetime should be very short, and they could not be a viable DM candidate. Then, the neutralino, if exists, must be perfectly stable, and we will not treat neutralino decay. However, neutralinos can annihilate. The annihilation cross-section is generally fit by (Bertone, Hooper & Silk 2005):

$$\sigma v = a + b v^2 + O(v^4), \quad (10)$$

where $a$ and $b$ are constant, whose values are constrained by the DM relic density condition, and $v$ is the neutralino velocity, which depends on the DM temperature and thus on the redshift. In the present epoch neutralinos are non-relativistic, then the current annihilation cross-section can be written as $\sigma v \sim a$. However, the cross-section at the freeze-out time should depend on $v$ and be higher than the current value. As a rough approximation, Padmanabhan & Finkbeiner (2005) considered a thermally averaged, redshift-independent cross-section, $\langle \sigma v \rangle = 2 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$. For comparison, we made the same assumption. Then, the annihilation rate becomes:

$$\frac{dn}{dt} = 2.88 \times 10^{-42} (1 + z)^3 \text{cm}^3 \text{s}^{-1} \left(\frac{n_0}{1.2 \times 10^{-8} \text{cm}^{-3}}\right)^2 \times \left(\frac{\langle \sigma v \rangle}{2 \times 10^{-26} \text{cm}^3 \text{s}^{-1}}\right), \quad (11)$$

where $n_0 = \Omega_{\text{DM}} \rho_c / m_\chi$. In our calculations, we assume $m_\chi = 100$ GeV. We have implemented this equation into RECFAST. The contribution of neutralino annihilations both to ionizations and heating is negligible (Fig. 3; dashed line) for $\langle \sigma v \rangle = 2 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$ (in agreement with Padmanabhan & Finkbeiner 2005). As an upper limit, we considered also the case where $\langle \sigma v \rangle = 10^{-24} \text{cm}^3 \text{s}^{-1}$,
which is the highest value to be consistent with the first year WMAP data (see Colafrancesco, Profumo & Ullio 2005). Also in this case, the contribution to heating is negligible and the ionization fraction remains of the order of $10^{-3}$. However, annihilations are particularly important at very high redshift ($z \gtrsim 100$), where the particle density is very high. For this reason, even if the ionization fraction due to annihilations remains always very low, the Thomson optical depth is significantly high ($\tau_e \sim 0.05$), even more than for LDM.

These results must be considered very optimistic upper limits. In fact, we are assuming that nearly all the energy of the DM particle is immediately deposited into ionization or heating; whereas we expect that the electrons produced by neutralino annihilations Compton-scatter the CMB photons up to a energy $\sim 1$–$10(1+z)$ MeV, which cannot be significantly absorbed by the intergalactic medium within a Hubble time (Chen & Kamionkowski 2004).

4 WARM DARK MATTER: STERILE NEUTRINOS

Sterile neutrinos are one of the most popular WDM candidates (Colombi, Dodelson & Widrow 1996; Sommer-Larsen & Dolgov 2001), even if Seljak et al. (2006) seem to exclude that they are the only component of DM on the basis of Ly$\alpha$ forest power-spectrum measurements. They can exist only if neutrinos have non-zero mass and mixing angles, as predicted by the standard oscillation theory (Dolgov & Hansen 2002; see Dolgov 2002 for a complete review of sterile neutrino properties). There are many possible decay channels of sterile neutrinos (Dolgov 2002). In this paper, we are interested on the radiative decay, that is, the decay of a sterile neutrino into a lighter neutral fermion (such as an active neutrino) and a photon, because of its effects on the cosmic ionization and heating. From the comparison between the predicted background flux due to radiatively decaying sterile neutrinos and the hard X-ray background (Bauer et al. 2005), Mapelli & Ferrara (2005) have established an upper limit of 14 keV for the sterile neutrino mass. This limit can now be lowered to $m_{\nu_s} < 11$ keV, adopting the relation between the mixing angle and the mass recently derived by Abazajian (2006).

A stronger upper limit, $m_{\nu_s} < 8.2$ keV, has been derived from X-ray observations of the Virgo cluster (Abazajian 2006). Furthermore, Viel et al. (2005) derived a lower limit $m_{\nu_s} > 2$ keV from the study of matter power-spectrum fluctuations. Then, sterile neutrino masses are allowed from 2 to 8 keV, a very narrow range.

The lifetime for sterile neutrino radiative decay is (Mapelli & Ferrara 2005):

$$\tau = \frac{512 \pi^4}{9 \alpha_{em}^2} G_F^2 m^{-5}_{\nu_s} \sin^{-2} \theta,$$

where $\alpha_{em}$ is the fine structure constant, $G_F$ the Fermi constant, $m_{\nu_s}$ the sterile neutrino mass and $\sin^2 \theta$ the mixing angle. To derive $\sin^2 \theta$, we adopt the following relation (Abazajian 2006):

$$\sin^2 \theta = 2.5 \times 10^{-9} \left[ \frac{3.4 \text{ keV}}{m_{\nu_s}} \left( \frac{\Omega_{\text{DM}}}{0.26} \right)^{1/2} \right]^{1.626} \times \left\{ 0.527 \text{erfc} \left( -1.15 \left( \frac{T_{\text{QCD}}}{170 \text{ MeV}} \right)^{2.15} \right) \right\}^{1.626},$$

where $\Omega_{\text{DM}}$ is the dark matter density and $T_{\text{QCD}}$ the temperature of quark-hadron transition.

Assuming that all the DM is composed by sterile neutrinos and substituting equation (12) into equation (1), we derive through RECFAST the ionization and heating history also for WDM particles (Fig. 4). Also sterile neutrinos start to play a role into the reionization and heating at redshift $z \sim 100$, and their behaviour is close (even if the global contribution is slightly lower) to that of LDM.

5 EFFECTS ON THE CMB SPECTRUM

In the previous section, we have shown that decaying DM, and especially LDM and sterile neutrinos, can modify the ionization fraction, with respect to the value due to relic electrons, already at high redshift. This fact should leave some imprint on the CMB spectrum (Chen & Kamionkowski 2004; Pierpaoli 2004; Padmanabhan & Finkbeiner 2005). To check whether these effects are measurable, we simulated the expected CMB spectrum in the case we take...
a very small Thomson optical depth ($\tau_e \approx 0.09$), expected EE spectra by considering (dashed line) and neglecting (solid line) DM decays. We found that the effects of DM decays alone is negligible. There is a sensible difference only in the lowest multipoles ($l < 10$) of the EE spectrum. This effect can be seen in the central panel of Fig. 5, where the thin lines show the expected EE spectra by considering (dashed line) and neglecting (solid line) DM decays, respectively. This effect, small and concentrated at low multipoles, is justified by the fact that DM decays produce a very small Thomson optical depth ($\tau_e \lesssim 0.01$) and that they are important especially at very low redshift, due to their long lifetime. Is such a modification of the EE spectrum measurable? If there are other sources of reionization besides DM decays (as it seems to be likely, considering the Thomson optical depth, $\tau_e = 0.09^{+0.01}_{-0.03}$ measured by WMAP; Spergel et al. 2006), the influence exerted on the EE spectrum by the decaying DM would be completely hidden by the stronger effects due to these other reionizing sources. This can be seen in Fig. 5, where the thick lines show the TT, TE and EE spectra assuming $\tau_e = 0.09$ in the case with (dashed line) and without (solid line) DM decays. We found that the effects of DM decays are washed out by those of other reionizing sources also for lower values of $\tau_e$ consistent with the 3-yr WMAP results (down to $\tau_e = 0.06$, corresponding to a sudden reionization at $z \sim 6$). Because 10-MeV LDM particles produce the highest ionization fraction among the considered models, the effects on the CMB spectra due to other species of DM particles will be far more negligible. However, stronger effects on the CMB spectra can be due to annihilations of LDM particles (Zhang et al. 2006), which are not considered by this paper.

6 CONCLUSIONS

We examined the contribution to cosmic reionization and heating of different models of decaying/annihilating DM. In the case of quite light particles ($\lesssim 10$ MeV), this contribution is significant. Light particles (LDM, or sterile neutrinos) become important at $z \sim 100$, as they provide an early source of (partial) ionization for the intergalactic medium. They are expected to produce a Thomson optical depth $\tau_e \lesssim 0.01$ ($\tau_e \lesssim 0.001$) in the case of LDM particles (sterile neutrinos), which is smaller than the value derived from the 3-yr WMAP data ($\tau_e = 0.09$), but non-negligible. Changes in the matter temperature are also important, and the role of DM decays on the history of 21-cm emission should be investigated. On the contrary, heavier particles (gravitinos and neutralinos) do not have significant influence on reionization and heating.

This result could be crucial in distinguishing between light and heavy DM models, if new measures will be available of the reionization history and/or the behaviour of the matter temperature (e.g. mapping the 21-cm emission at $z \sim 10–50$). However, it is quite impossible to distinguish among different species of light DM particles, such as sterile neutrinos or LDM.

Finally, in the case of light particles, an early ($z > 20$) increase of the ionization fraction and of the baryon temperature could catalyse the production of $H_2$ and HD molecules, affecting the entire history of structure formation (Shchekinov & Vasiliev 2004; Biermann & Kusenko 2006). On the contrary, no constraints on DM particles can be derived from their effects on the CMB spectra.

ACKNOWLEDGMENTS

We thank P. Ullio, A. Provenza, E. Ripamonti and K. Abazajian for useful discussions. We also acknowledge the Referee for his critical reading of the manuscript. EP is an ADVANCE fellow (NSF grant AST-0340648), also supported by NASA grant NAG5-11489.

REFERENCES

Abazajian K. J., 2006, Phys. Rev. D, 73, 3506
Ascasibar Y., Jean P., Boehm C., Knödlseder J., 2006, MNRAS, 368, 1695
Bauer F. E., Alexander D. M., Brandt W. N., Schneider D. P., Treister E., Homscheimeier A. E., Garmire G. P., 2004, AJ, 128, 2048 [B04]
Beacom J. F., Yuksel H., 2006, astro-ph/0512411
Beacom J. F., Bell N. F., Bertone G., 2005, Phys. Rev. Lett., 94, 1301
Bertone G., Hooper D., Silk J., 2005, Phys. Rept., 405, 279
Biermann P. L., Kusenko A., 2006, Phys. Rev. Lett., 96, 1301
Bode P., Ostriker J. P., Turok N., 2001, ApJ, 556, 93
Boehm C., Hooper D., Silk J., Casse M., Paul J., 2004, Phys. Rev. Lett., 92, 1301
Cassé M., Fayet P., 2005, in Mannon G., Combes F., Defayet C., Fort B., eds, Proc. 21st IAP Colloq., Mass Profiles and Shapes of Cosmological Structures, preprint (astro-ph/0510490)
Chen X., Kamionkowski M., 2004, Phys. Rev. D, 70, 3502
Cofalanchi S., Profumo S., Ullio P., 2005, A&A, submitted (astro-ph/0507575)
Colombi S., Dodelson S., Widrow L. M., 1996, ApJ, 458, 1
Dermer C. D., Murphy R. J., 2001, in Battrick B., Gimenez A., Reglero V., Winkler C., eds, Proc. Fourth INTEGRAL Workshop, Exploring the Gamma-ray Universe. ESA SP-459, ESA Publications Division, Noordwijk, p. 115

© 2006 The Authors. Journal compilation © 2006 RAS, MNRAS 369, 1719–1724

Downloaded from https://academic.oup.com/mnras/article-abstract/369/4/1719/1089692 by guest on 27 July 2018
Dolgov A. D., 2002, Phys. Rept., 370, 333
Dolgov A. D., Hansen S. H., 2002, APh, 16, 339
Hansen S. H., Haiman Z., 2004, ApJ, 600, 26
Hinshaw G. et al., 2006, ApJ, submitted
Hooper D., Wang L.-T., 2004, Phys. Rev. D, 70, 3506
Kasuya S., Kawasaki M., 2004, Phys. Rev. D, 70, 3519
Kasuya S., Kawasaki M., 2006, Phys. Rev. D, 73, 063007
Kasuya S., Kawasaki M., Sugiyama N., 2004, Phys. Rev. D, 69, 3512
Kasuya S., Takahashi F., 2005, Phys. Rev. D, 72, 5015
Kawasaki M., Yanagida T., 2005, Phys. Lett. B, 624, 162
Knödlseder J. et al., 2005, A&A, 441, 513
Mapelli M., Ferrara A., 2005, MNRAS, 364, 2
Nowakowski M., Rindani S. D., 1995, Phys. Lett. B 348, 115
Ostriker J. P., Steinhardt P., 2003, Sci., 300, 1909
Padmanabhan N., Finkbeiner D. P., 2005, Phys. Rev. D, 72, 3508
Padmanabhan T., 1995, Structure Formation in the Universe. Cambridge
Univ. Press, Cambridge
Page L. et al., 2006, ApJ, submitted
Palla F., Salpeter E. E., Stahler S. W., 1983, ApJ, 271, 632
Pierpaoli E., 2004, Phys. Rev. Lett., 92, 031301
Sciama D. W., 1982, MNRAS, 198, 1
Seager S., Sasselov D. D., Scott D., 1999, ApJL, 523, 1
Seager S., Sasselov D. D., Scott D., 2000, ApJS, 128, 407
Seljak U., Makarov A., McDonald P., Trac H., 2006, Phys. Rev. Lett., submitted (astro-ph/0602430)
Seljak U., Sugiyama N., White M., Zaldarriaga M., 2003, Phys. Rev. D, 68, 2507
Seljak U., Zaldarriaga M., 1996, ApJ, 469, 437
Shchekinov Y. A., Vasiliev E. O., 2004, A&A, 419, 19
Sommer-Larsen J., Dolgov A., 2001, ApJ, 551, 608
Spergel D. N. et al., 2003, ApJS, 148, 175
Spergel D. N. et al., 2006, ApJ, submitted
Viel M., Lesgourgues J., Haehnelt M. G., Matarrese S., Riotto A., 2005, Phys. Rev. D, 71, 3534
Zhang L., Chen X., Lei Y.-A., Si Z., 2006, Phys. Rev. D, submitted (astro-ph/0603425)

This paper has been typeset from a T\LaTeX file prepared by the author.