I. INTRODUCTION

In recent years the 5d transition metal oxides have gained a lot of interest since the enhanced spin-orbit coupling (SOC) in these systems adds an interesting new energy scale to the rich physics of competition between crystal field (CF) and Coulomb interactions (U). This may lead to unexpected exotic magnetic phases and novel types of local-moment frustration. 22

In most cases, systems with an odd number of electrons in the d shell (Ir$^{5+}$, 5$d^6$) have been studied, such as A$_2$IrO$_4$ (A = Sr, Ba) 1,2,7–10 A$_2$IrO$_3$ (A = Na, Li) 15,16 and BaIrO$_3$. 17,18 In the case of a 5$d^4$ (Ir$^{5+}$) electronic configuration, the strong SOC of the t$_{2g}$ state with an integer low-spin state $S$ leads to a splitting into a nonmagnetic $J = 0$ ground state and magnetic $J = 1$ (and $J = 2$) excited states. 19 Magnetism can form only via a Van-Vleck-like singlet - triplet excitation over the SOC gap.

Since this singlet - triplet gap is of similar size as the spin exchange energy scale ($\sim 50 – 100$ meV), unusual magnetic states can be expected. 14 The double perovskites A$_2$BO$_6$ (with A an alkaline earth element and B and $B'$ two different transition metal ions) were suggested as potential candidates for such unusual magnetic states. 14

From the experimental side, very different interpretations concerning these double perovskites have been raised. Early magnetization and heat capacity measurements on single crystals of Sr$_2$YIrO$_6$ and Ba$_{2-x}$Sr$_x$YIrO$_6$ ($x = 0.74$) revealed an antiferromagnetically long-range ordered ground state below 1.3 K (1.6 K respectively). 15,16 In contrast to the expected $J = 0$ nonmagnetic ground state, this was assigned to result from the high distortion of the IrO$_6$ octahedra in the monoclinic structure of this compound. 15,16 De facto, lattice degrees of freedom can play a significant role in determining the ground state and the physical properties of a material. Slight alterations of the lattice may lead to strong effects in the magnetic properties, especially due to the extended 5d orbitals, as found e.g. in Sr- and Ru-doped BaIrO$_3$. 17,18 However, this explanation breaks down in the case of the cubic analogue Ba$_2$YIrO$_6$ with regular IrO$_6$ octahedra. Terizc et al., thus, interpret the observed long-range magnetic order in Ba$_{2-x}$Sr$_x$YIrO$_6$ as a result of band structure and/or electron-electron interaction effects competing with the SOC. 19 In contrast, studies on polycrystals of the series Ba$_{2-x}$Sr$_x$YIrO$_6$ reported the absence of any long-range order and no significant change in the magnetic properties upon increasing the structural disorder from cubic Ba$_2$YIrO$_6$ with regular IrO$_6$ octahedra to monoclinic Sr$_2$YIrO$_6$ with highly distorted IrO$_6$ octahedra, thus demonstrating that the CF splitting in Sr$_2$YIrO$_6$ is not enough to compete with the strong spin-orbit coupling. 20 A recent detailed single crystal x-ray diffraction analysis of Sr$_2$YIrO$_6$ even questioned the formerly reported monoclinic structure, 21 but reported a cubic unit cell with regular IrO$_6$ octahedra. Furthermore, no evidence for magnetic long-range order has been found down to 430 mK and the low temperature anomaly in the specific heat has been identified as a Schottky anomaly caused by tiny amounts (< 1%) of paramagnetic impurities. 22 Also for single crystals of Ba$_2$YIrO$_6$ long-range magnetic order has not been observed down to 0.4 K and the effective magnetic moment of 0.44 $\mu_B$/Ir (extracted from a Curie-Weiß (CW) fit to the magnetic susceptibility), could be accounted for by $\sim 2\%$ of $J = 1/2$ impurities. 23 These studies thus corroborate the dominance of the SOC leading to a nonmagnetic $J = 0$ ground state, whose weak magnetic response stems from paramagnetic impurities, such as tiny amounts of Ir$^{4+}$ or Ir$^{6+}$ ions, created by chemical disorder (Ir$^{4+}$ for Y$^{3+}$ substitution) and/or off-stoichiometry, respectively. 24

We investigated this weak magnetism by means of nuclear magnetic resonance and muon spin rotation measurements on single crystals and polycrystals of...
Ba$_2$YIrO$_6$. Taking advantage of the local probe character of these two methods in contrast to bulk characterization techniques, we can directly reveal the nonmagnetic $J=0$ ground state of Ba$_2$YIrO$_6$, and show, that the observed weak magnetism stems from small amounts of diluted paramagnetic spin centers on top of this nonmagnetic ground state. The origin of these paramagnetic spin centers may in principle be either disorder, off-stoichiometry, oxygen deficiency or excess, although some scenarios seem to be more likely than others.

II. SAMPLE PREPARATION, CHARACTERIZATION AND EXPERIMENTAL DETAILS

High purity starting materials BaCO$_3$ (Alpha Aesar 99.997 %), IrO$_2$ (Alpha Aesar 99.99 %) and Y$_2$O$_3$ (Alpha Aesar 99.99 %) were used to grow single crystals of Ba$_2$YIrO$_6$ in a flux of ultradry BaCO$_3$ (Alpha Aesar 99.5 %) as described in detail in Ref. $^{[2]}$. Single crystals of typical dimensions 0.3 x 0.3 x 0.3 mm$^3$ were obtained. Details on their characterization and magnetic properties are found in Ref. $^{[22]}$. A polycrystalline sample of Ba$_2$YIrO$_6$ has been prepared by solid state reaction method. Stoichiometric amounts of high-purity BaCO$_3$, Y$_2$O$_3$, and Ir metal powder were mixed thoroughly, pressed into pellets and calcined at 800°C for 12h. Subsequently, the mixture was heated at 1200°C for 80h with several intermediate grinding and pelletizing. From the point of view of standard bulk characterization techniques (XRD and magnetization) it appeared to be less disordered than the single crystals.

For $^{89}$Y nuclear magnetic resonance (NMR) measurements plenty of single crystals were crushed to a powder. The crushed single crystals were measured in static magnetic fields of 7 and 15 T, while the polycrystalline sample was measured in 7 T. $^{89}$Y possesses a nuclear spin $I=1/2$, thus no quadrupolar effects influenced the NMR spectra and relaxation rate measurements. NMR spectra were measured by using a normal Hahn spin-echo sequence and Fourier transforming the echo. The repetition rate between subsequent pulse sequences was chosen to be sufficiently long to prevent spin-lattice relaxation rate effects. The spin lattice relaxation rate $T_1^{-1}$ was measured by using the saturation recovery method and the recovery of the nuclear magnetization $M_z(t)$ was fitted to:

$$M_z(t) = M_0[1 - fe^{−(t/T_1)^\beta}]$$

with the nuclear saturation magnetization $M_0$, $f = 1$ for an ideal saturation recovery (otherwise $f < 1$) and a stretched exponent $\beta$. $0 < \beta < 1$ refers to a probability distribution $P$ of individual spin-lattice relaxation rates $T_{1,i}$, with which the stretched exponential function can be expressed as: $$e^{−(t/T_1)^\beta} = \int_0^\infty P(s, \beta)e^{−st/T_1}ds,$$ where $s = T_1/T_{1,i}$ and $\int_0^\infty P(s, \beta)ds = 1$. In this case, $T_1^{-1}$ denotes a characteristic relaxation rate of the system. Please note, that this characteristic relaxation rate differs from the average relaxation rate or its inverse. Instead, for $1/3 < \beta < 1$, $T_1^{-1}$ can be understood as the value for which it is equally likely for $T_{1,i}^{-1}$ to be smaller or greater than $T_1^{-1}$.

For $\beta = 1$, the probability distribution amounts to the Dirac function at $s = 1$ and yields $T_{1,i}^{-1} = T_1^{-1}$. With decreasing $\beta$, the probability distribution $P(s, \beta)$ gets broader and more and more asymmetric and its maximum shifts to slower rates $s < 1$. Former works used a log-normal distribution to mimic the probability distribution of the stretched exponential.$^{[22,28]}$ They showed that the extracted $T_1^{-1,\lognorm}$ are very similar to the characteristic $T_1^{-1}$ as extracted by a stretched exponential recovery law and do not depend on the exact form of the distribution function. We therefore decided to use the stretched exponential fitting function for this work. For a more detailed analysis of the probability distribution the interested reader is referred to Ref. $^{[22]}$.

$\mu$SR measurements on the same crushed single crystals of Ba$_2$YIrO$_6$ have been carried out at the $\pi$M3 beam line at the GPS and LTF spectrometers of the Swiss Muon Source at the Paul Scherrer Institute (PSI) in Villigen. Positively spin-polarized muons were implanted into the sample and the time evolution of the muon spin polarization, $P(t)$, was monitored by detecting the asymmetric spatial distribution of positrons emitted from the muon decay.$^{[29,30]}$ The measurements have been performed in the temperature range between 300 mK and 200 K in zero magnetic field (ZF) and in longitudinal applied magnetic fields with respect to the initial muon spin polarization up to 1000 G (LF). To improve the thermal contact in the LTF machine, the samples were glued on an Ag plate giving rise to a time and temperature independent background signal due to muons that stopped in the Ag plate. The $\mu$SR time spectra were analyzed using the free software package MUSRFIT.

III. EXPERIMENTAL RESULTS AND DISCUSSION

A. Nuclear Magnetic Resonance

NMR measurements have been performed in the temperature range from 4.2 K up to 100 K. Figs. (1a) and (b) show representative spectra measured in 7.0493 T. The main resonance line stemming from Y nuclei within the intrinsic Ba$_2$YIrO$_6$ phase is peaked around 14.692 MHz. It is asymmetric and can be described by a fit with two Gaussian lines, revealing the main peak (P1) and a high-frequency shoulder (P2). Additionally, a smaller peak is found at slightly higher frequencies (P3), with an average spectral weight of roughly 5 %. The nuclear spin-lattice relaxation rate of this small high-frequency peak is not accurately measurable. It is of the order of several thousands of seconds. Its observed temperature independent
Knight shift $K_3 \simeq 0.04\%$ [see Fig. 1(c)] agrees well with the reported chemical shift of $Y_2O_3$ (roughly 300 ppm). Furthermore, traces of unreacted $Y_2O_3$ of the same order of magnitude (about 2%) have also been found in the powder XRD characterization of these samples. Hence, we attribute $P_3$ to $Y$ nuclei within a tiny nonmagnetic $Y_2O_3$ impurity phase.

Fig. 1(c) shows the NMR Knight shift $K$ of all three peaks, extracted from their measured resonance frequencies $\nu$ as:

$$\omega = 2\pi \nu = \gamma H_0 (1 + K), \quad (2)$$

where $\gamma / 2\pi = 2.0858 \text{MHz/T}$ is the gyromagnetic ratio of the $^{89}Y$ nuclei and $\mu_0 H_0 = 7.0493 \text{T}$ is the magnetic field. The Knight shift results from the hyperfine interaction between the spins of the electrons and the nuclear spins. In an applied magnetic field, polarized electrons create an additional hyperfine field at the nuclear sites, leading to a shift of the resonance line with respect to the unshifted Larmor frequency $\omega_0 = \gamma H_0$. This shift $K$ comprises the temperature-independent contributions: $K_{\text{orb}}$ (orbital shift) and $K_{\text{dia}}$ (diamagnetic shift), as well as the temperature-dependent spin part $K_s$, which is a measure of the intrinsic local spin susceptibility $\chi_s(q = 0, \omega = 0)$:

$$K_s = A_{hf} \chi_s(q = 0, \omega = 0), \quad (3)$$

with the hyperfine coupling constant $A_{hf}$. $K_s$ itself can consist of dipolar contributions, Fermi-contact contributions (only in the case of unpaired s-electrons), and transferred Fermi-contact contributions via the polarization of the orbitals (also called core polarization).

The nearly temperature independent Knight shifts of the main $\text{Ba}_2\text{YIrO}_6$ phase. $K_1$ and $K_2$, and their low absolute values indicate that the local spin susceptibility is very small and only weakly temperature dependent, corroborating the theoretically proposed nonmagnetic $J = 0$ ground state. This stands in contrast to the measured bulk susceptibility, which cannot differentiate between the intrinsic spin susceptibility and contributions from even tiny amounts of paramagnetic impurities, leading to a Curie-Weiss-like upturn at low temperatures. In the high temperature range, where $\chi$ is still rather flat, the hyperfine coupling constant can be deduced according to Eq. (3) and including a constant term for the static part $K_{\text{stat}}$. Fig. 2 shows $K_1$ as a function of the macroscopic susceptibility $\chi$ with temperature as implicit parameter (for $T > 10\text{K}$). The deduced hyperfine coupling constant amounts to $A_{hf} = -0.1(2)\text{kOe}/\mu_B$. This small negative value is the sum of (direction-dependent negative and positive) dipolar and (negative) core polarization hyperfine interactions, which cannot be separated from each other. By extrapolating to $\chi = 0$ and considering the maximal possible values of $K_s$, we can also deduce the temperature independent part of the Knight shift, $K_{\text{stat}}$. This part comprises the orbital shift $K_{\text{orb}}$ from unfilled electronic shells and the diamagnetic shift $K_{\text{dia}}$ stemming from closed inner electronic shells. $K_{\text{stat}}$ amounts to $(-0.071 \pm 0.002)\%$. Hence, it is the dominant contribution to the measured shift, while the spin part $K_s$ is vanishingly small. These results together with the weak temperature dependence strongly hint towards a nonmagnetic ground state of $\text{Ba}_2\text{YIrO}_6$.

SOLELY the Knight shift of the shoulder peak $P_2$ shows a slight enhancement towards low temperature, suggesting the presence of diluted paramagnetic impurities. We
thus assume that the main peak P1 stems from nuclei in the nonmagnetic $J = 0$ Ba$_2$YIrO$_6$ matrix, while peak P2 might stem from nuclei which sense the previously suggested Y-Ir disorder, leading to a few percent of paramagnetic $J=1/2$ impurity centers.\[^{23}\] In fact, an energy dispersive x-ray (EDX) analysis with a scanning electron microscope (SEM) suggested a small excess of Y in the crystal. Thus, a certain off-stoichiometry, i.e. Ba$_2$Y$_{1+d}$Ir$_{1-d}$O$_6$, and/or site disorder between Y and Ir in the crystals cannot be ruled out, although the refinement of the powder XRD pattern could not reveal such effects.\[^{23}\] Note that in principal also a slight oxygen deficiency could lead to paramagnetic Ir$^{4+}$ ions. However, previous magnetization measurements comparing as-grown crystals and crystals annealed in oxygen pressure did not show any difference rendering this possibility rather unlikely. Since Ir$^{6+}$ is also magnetic ($J = 3/2$), one may assign the paramagnetic impurities to stem from Ir$^{6+}$ caused by oxygen excess, however experimental evidence for this scenario is lacking so far and former growth studies showed, that Ir$^{6+}$ can only be stabilized under high oxygen pressure and high temperature.\[^{23}\]

Note that in light of the XRD results and the magnetization measurements, the spectral weight distribution between P1 and P2 of 70% : 30% seems surprisingly large. However, if we assume that, due to the extended 5d orbitals, also nearest neighbors (nn) [and potentially next-nearest neighbors (nnn)] sense the disorder caused by some tiny Y-Ir mismatch, the effects seen by NMR will be larger than the actual disorder itself. In fact, by considering the coordination number six at the Y site, P1 can be attributed to an Y - (O-Ir)$_6$ nn environment, while P2 can be assigned to an Y - (O-Ir)$_3$-(O-Y) nn environment and the spectral weight distribution between P1 and P2 translates to a Y-Ir mismatch of $\sim 5\%$.\[^{23,33}\]

Fig. 1(d) shows the full width at half maximum (FWHM) of all three peaks. At high temperatures, the resonance lines are very narrow, pointing towards a nonmagnetic environment of the $^{89}\text{Y}$ nuclei, since any magnetic environment would lead to slightly different hyperfine fields and thus slightly different $K$, resulting in a broadening of the NMR lines. The linewidth of the shoulder peak P2 is always larger than the ones of P1 and P3, suggesting the more magnetic environment of the $^{89}\text{Y}$ nuclei at this site, likely stemming from Y-Ir disorder. A small line broadening is observed at lower temperatures, pointing towards a slowing down of magnetic fluctuations. The absolute values of the linewidth at low temperature (11.4 kHz at 4.2 K (P2)) can be well reproduced by considering the deduced hyperfine coupling constant and the magnetic moment as obtained from a Curie-Weiß fit to the macroscopic susceptibility, which amounts to $\mu_{eff} = 0.44 \mu_B$/Ir atom.\[^{24}\] The internal field $H_{int} = A_{eff} \mu_{eff} = 44$ Oe leads to a line broadening due to the effective magnetic moment of $\Delta \nu = \gamma H_{int} = 9.2$ kHz. Taken together with the linewidth in the high temperature limit, which is based on other effects, this can account for the entire linewidth of 11.4 kHz at 4.2 K. Hence, no other line broadening effects have to be considered. The observed line broadening is solely a result of the tiny amount of paramagnetic impurities.

Measurements of the NMR spin-lattice relaxation rate $T_1$ have been performed on the main peak in magnetic fields of 7 and 15 T (see Fig. 3). Since P1 and P2 are very close to each other in the spectrum, $T_1^{-1}$ can only be measured for both of them at the same time. This results in a stretched exponential recovery curve (see Eq. 4) with a basically temperature-independent stretching exponent $0.4 < \beta < 0.6$, which points towards a rather broad, temperature-independent probability distribution of individual relaxation rates $T_{1,i}^{-1}$. The characteristic spin-lattice relaxation rate of this distribution, $T_1^{-1}$, is temperature independent from 100 K down to roughly 40 K. The absolute values of $T_1 \simeq 15$ s (20 s) in 7 T (15 T) in this temperature range indicate the absence of any type of strong magnetic correlations, which would lead to a much faster relaxation.

However, upon further lowering the temperature, $T_1$ gets faster and a pronounced peak appears in $T_1^{-1}$ for both fields.\[^{36}\] Such a peak points towards a progressive slowing down of spin fluctuations, which can be described in the Bloembergen-Purcell-Pound (BPP) model.\[^{27,38}\] Within this model, the spin-lattice relaxation rate $T_{1,i}^{-1}$ is

\[ T_{max} = \frac{E_a}{k_B T_a} \left( 1 + \frac{T_a}{T} \right)^{\frac{1}{\beta}} \]

where $E_a$ is the activation energy, $T_a$ the characteristic temperature, and $h$ the magnetic field. The parameters for the BPP model are given in Table I.

![FIG. 3: (Color online) $^{89}\text{Y}$ NMR spin-lattice relaxation rate $T_1^{-1}$ of Ba$_2$YIrO$_6$, measured in magnetic fields of 7.0493 T (orange dots) and 15 T (dark blue diamonds). Lines are fits to the data according to Eq. 4. The inset shows the same data and fits with a logarithmic ordinate. Additionally, $T_1^{-1}$ of a polycrystalline Ba$_2$YIrO$_6$ sample in 7.0493 T is shown in the inset (green squares).](image)

| $T_{max}$ (K) | $E_a$ (K) | $T_a$ (10$^{-10}$) s | $h$ (Gauss) |
|-------------|-----------|----------------------|-------------|
| 7 T         | 10        | $(42.4 \pm 1.3)$     | $(1.6 \pm 0.2)$ |
| 15 T        | 14        | $(38.4 \pm 2.7)$     | $(2.7 \pm 0.4)$ |
expressed as a function of the local fluctuating magnetic field \( h_\perp(t) \) perpendicular to the applied magnetic field and its characteristic autocorrelation time \( \tau_c \): 

\[
T^{-1}_{1,\text{BPP}}(T) = \gamma^2 h_\perp^2 \frac{\tau_c(T)}{1 + \tau_c^2(T) \omega_L^2}.
\]

This leads to a peak in \( T_{1}^{-1} \) at the temperature where the correlation time of the spin fluctuations \( \tau_c \) equals the inverse Larmor frequency \( \omega_L \). For disordered systems, the temperature dependence \( \tau_c(T) \) can be well described by an activated behavior: 

\[
\tau_c(T) = \tau_0 \exp \left( \frac{E_a}{k_B T} \right),
\]

with the activation energy \( E_a \) of the magnetic fluctuations and the correlation time at infinite temperature \( \tau_0 \). Thus, the peak in \( T_{1}^{-1} \) should shift to higher temperature upon increasing the external magnetic field, which is indeed observed experimentally (see Fig. 6 and results in Table I).

Fits according to Eq. (4) (solid lines in Fig. 3 and Table I) can well describe the data and yield an activation energy of the slowing down of magnetic fluctuations of about \( E_a = (40 \pm 4) \) K, which is in good agreement with the onset temperatures of the increase of the NMR FWHM [see, Fig. (3)] and the \( \mu \)SR spin-lattice relaxation rate \( \lambda \) (see Fig. 7). The fluctuating field \( h_\perp \) amounts to around \((8 \pm 2) \) Gauss, which is fairly small. It compares well to the internal field as extracted from the linewidth of P2 by considering that \( h_\perp \) has been deduced from spin-lattice relaxation rate measurements on P1 and P2, while \( H_{\text{int}} \) has been extracted from the linewidth of P2 only. The extracted activation energy of the slowing down of spin fluctuations, \( E_a = (40 \pm 4) \) K is too small to account for singlet-triplet excitations over the SOC gap, which is of the order of 370 meV. Since the BPP peak is seen at the main NMR resonance lines P1 and P2 of the \( \text{Ba}_2\text{YIrO}_6 \) phase, we suppose that these fluctuations stem from homogeneously distributed paramagnetic spin centers in the main phase. As already cited, these spin centers may arise due to slight off-stoichiometry and chemical disorder, leading to \( \text{Ir}^{4+} \) and \( \text{Ir}^{5+} \) ions with \( J = 1/2 \) and \( J = 3/2 \), respectively. Recent electron spin resonance (ESR) investigations come to the same conclusion and give a detailed analysis of these spin centers. Certainly, the system is far from being magnetically long-range ordered, with the stoichiometric \( \text{Ba}_2\text{YIrO}_6 \) phase being in a \( J = 0 \) nonmagnetic ground state as expected from the strong SOC.

For comparison, we also measured a polycrystalline sample of \( \text{Ba}_2\text{YIrO}_6 \), which from the point of view of the bulk characterization appears to be less disordered than the single crystals. Its magnetic susceptibility is smaller than the one of the single crystal (see Fig. 4). A CW fit in the same temperature range (15 - 300 K) yielded an effective magnetic moment of 0.31 \( \mu_B/\text{Ir atom} \) \( (C = 0.01228 \text{ cm}^3/\text{K/mol}) \), which is smaller than the one of the single crystals \( (0.44 \mu_B/\text{Ir atom}) \). Furthermore, no evidence for \( \text{Y}_2\text{O}_3 \) or other impurities was found in its XRD characterization (not shown).

This is reflected in the NMR spectra of the polycrystal [see Figs. 5(a) and (b)], where peak P3, which we assigned to nonmagnetic \( \text{Y}_2\text{O}_3 \) in the NMR spectra of the single crystals, is absent. Furthermore, the spectral weight of P2, which presumably arises from chemical disorder and/or off-stoichiometry, is much smaller. An analysis of the spectral weight distribution between P1 and P2

FIG. 4: (Color online) Comparison of the temperature dependent magnetic susceptibility of a polycrystalline \( \text{Ba}_2\text{YIrO}_6 \) sample (black dots) with the one of the single crystal (grey triangles) in an external magnetic field of 5 kOe. The red line shows the CW-Fit to the polycrystal data in the range from 15 - 300 K.

FIG. 5: (Color online) Left column (a), (b): Selected \( ^{89}\text{Y} \) NMR spectra of the polycrystalline sample measured in a field of 7.0493 T. Lines are Gaussian fits to the data, resulting in an anisotropic main line [peaks P1 (orange) and P2 (dark red)], as well as an additional peak at lower frequencies for the polycrystal (P4, green). Note that P3 (P4) is absent in the spectra of the polycrystal (single crystal), respectively. The insets in the left column show a zoom into the data to better reflect P2 and P4. Right column: Temperature-dependent NMR Knight shifts (c) and FWHM (d) for the three NMR resonance lines (P1 - orange, P2 - dark red, and P4 - dark green) of the \( \text{Ba}_2\text{YIrO}_6 \) polycrystal, measured in a field of 7.0493 T. Note that due to the reduced signal-to-noise ratio at high temperatures, peaks P2 and P4 could not be resolved at 75 and 100 K.
yields a Y-Ir mismatch of about 1 - 1.5% (see discussion of the spectral weights of the single crystal NMR). The main resonance line of the nonmagnetic Ba$_2$YIrO$_6$ phase is found at the same frequency as for the single crystals and its Knight shift is the same as for the single crystal and is also temperature independent [see Fig. 2(c)]. A fit to $K_1(\chi)$ results in the same hyperfine coupling constant $A_{hf}$ and a very similar static shift $K_{stat}$ as for the single crystals [see Fig. 2]. Also its FWHM is very small (1.3 kHz at 100K) and increases even less (up to 2.4 kHz at 4.2K for P1 and ~9 kHz for P2) [Fig. 2(d)]. As for the single crystals, this is consistent with a calculated line broadening of $\Delta \nu = 6.5$ kHz due to the reduced magnetic moment of 0.31$\mu_B$/Ir atom (see discussion of the linewidth for the single crystals). Additionally, a small peak emerges at the lower frequency side (P4). This peak has a fast spin-lattice relaxation of roughly 100 - 300 ms and its Knight shift shows a rather strong temperature dependence in comparison to the other two resonance lines [see Fig. 2(c)], suggesting that it emerges from Y nuclei sitting very close to a paramagnetic impurity, which in this case might be a tiny extrinsic paramagnetic cluster. (Note that this extrinsic phase also contributes to the measured macroscopic susceptibility. This means (i) the extrinsic paramagnetic phase is indeed very tiny and, (ii) the actual magnetic moment stemming from diluted paramagnetic electrons within the Ba$_2$YIrO$_6$ main phase might even be smaller than what has been deduced from $\chi(T)$.) The spin-lattice relaxation time of P1 and P2 (which are indistinguishable) is very long, reaching the limits of a reasonable measurement duration. The $T_1^{-1}$ data shown in the inset of Fig. 3 are thus only rough estimates (note the big error bars on the logarithmic scale) and cannot be used for any further analysis. However, they suffice to point out the difference between the polycrystal and the single crystals: The $T_1^{-1}$ of the main peak of the polycrystal is at least one order of magnitude smaller than the one of the single crystals, stating that the less disordered polycrystal is even less magnetic than the single crystals. This confirms the nonmagnetic $J = 0$ ground state of stoichiometric Ba$_2$YIrO$_6$ and proves that the weak magnetic signals arising in the magnetic susceptibility and in the NMR $T_1^{-1}$ of the single crystals stem from a small amount of paramagnetic spin centers, presumably arising from a certain Y-Ir site disorder and/or off-stoichiometry within the Ba$_2$YIrO$_6$ phase.

B. Muon Spin Rotation

Zero-field (ZF) $\mu$SR measurements have been carried out in the temperature range between 200 K and 300 mK. $\mu$SR time spectra at representative temperatures are shown in Fig. 4. Down to the lowest measured temperature of 300 mK, the ZF $\mu$SR time spectra exhibit a weak exponential decay. No signal of static long-range magnetic order, or a fast muon relaxation associated with a strongly disordered magnetic state are observed, in accordance with different bulk characterization methods and NMR. The spectra have been fitted with a stretched exponential function:

$$A(t) = A_0 \exp(-\lambda t)^\beta$$

with the spin-lattice relaxation rate $\lambda$ and a stretched exponent $\beta$. The value of $\beta = 0.85$ close to one suggests that the system is rather homogeneous since for a strongly disordered system such as a spin glass or some other spin-frozen state the expected $\beta$ value should be much lower than 1 (i.e. close to 1/3 for a spin glass).

The spin-lattice relaxation rate $\lambda$ [see Fig. 4] remains temperature independent down to ~ 60 K, in conjunction with the magnetic susceptibility and the NMR $T_1^{-1}$. The non-zero value of $\lambda$ above 60 K is associated with
randomly distributed nuclear moments coupled with the
muon spin. Below $\sim 60\text{K}$, $\lambda$ starts to increase with
decreasing temperature. This increase indicates that slow
magnetic fluctuations develop, consistent with the in-
crease of the $^{89}\text{Y}$ NMR $T_{1}^{-1}$ described above. It should
be noted that the absolute values of $\lambda$ in the tempera-
ture range from 60 K down to 300 mK are still very small,
indicating that the overall density and size of the fluctuat-
ing localized moments are small. In contrast to the
NMR $T_{1}^{-1}$, the muon spin relaxation rate $\lambda$ continuously
increases down to 600 mK. This is due to the different
time windows of the electronic fluctuations, to which
NMR and $\mu$SR are sensitive to. Below 600 mK down
to 300 mK no further change of the muon spin relaxation
is observed.

To clarify whether the low temperature muon spin re-
laxation is static or dynamic in nature, two decoupling
experiments have been performed at 3.7 K and 300 mK
in different longitudinal fields (LF $\mu$SR). At 3.7 K one
can completely suppress the muon spin relaxation with
a 200 G longitudinal field (not shown). Whereas, at
300 mK [see inset of Fig. 4 even a longitudinal field of
100 G is sufficient to decouple the muon spin relaxation.
This proves that the weak magnetic field distribution is
quasistatic with a fluctuation rate below 1 MHz at 3.7 K
and 300 mK. The data support the presence of diluted
localized paramagnetic moments which exhibit a slowing
down of fluctuations due to the presence of an energy
barrier. This interpretation is consistent with the re-
sults of NMR (see above), specific heat and susceptibility
measurements.\textsuperscript{22,23}

IV. CONCLUSION

By using local probe techniques, evidence for weak
magnetic fluctuations in single crystals of Ba$_2$YIrO$_6$
could be revealed. Instead of pointing towards an exotic
quasi-static ground state of Ba$_2$YIrO$_6$, we could show
that these fluctuations stem from tiny amounts of diluted
paramagnetic impurity centers on the background of
the nonmagnetic $J = 0$ ground state. Due to the local
character of NMR measurements, an impurity phase of
nonmagnetic Y$_2$O$_3$ could be resolved in single crystals of
Ba$_2$YIrO$_6$, in nice agreement with former XRD analysis.
The local susceptibility of the intrinsic Ba$_2$YIrO$_6$ phase
as measured by the NMR Knight shift was found
to be temperature independent, in contrast to bulk
susceptibility measurements, which are influenced by
tiny amounts of Y-Ir disorder and/or off-stoichiometry,
leading to a certain amount of paramagnetic impurities.
The existence of these paramagnetic spin centers is
expressed in an additional peak (P2) of the NMR
spectrum, an increase in its FWHM and a pronounced
peak in $T_{1}^{-1}$ at low temperature, indicating a progressive
slowing down of weak magnetic fluctuations of these
spin centers. These results are in perfect agreement with
$\mu$SR measurements on the same samples, where a slight
increase of the ZF $\mu$SR spin-lattice relaxation rate $\lambda$
and corresponding decoupling experiments reveal weak
magnetic fluctuations. Comparing the activation energy
of the magnetic fluctuations $E_a = (40 \pm 4)\text{K}$ resulting
from a BPP analysis of the NMR spin-lattice relaxation
rate, and the onset temperature of the increase of the
$\mu$SR spin-lattice relaxation rate with the theoretically
and experimentally determined excitation gap between the
$J = 0$ and $J = 1$ states of about 370 meV in
this compound, it is evident that the theoretically
suggested excitonic type of magnetism cannot account
for the observed magnetic response. Instead, we propose
that these weak magnetic fluctuations stem from tiny
amounts of diluted paramagnetic impurities on the
background of a nonmagnetic $J = 0$ ground state. Mea-
surements on a less disordered polycrystal of Ba$_2$YIrO$_6$
further corroborated this scenario, since no evidence for
magnetic fluctuations was found in this sample.

\textit{Note added in proof} After submission of our
manuscript, another work appeared which also dis-
cusses the effect of site disorder on the magnetism of
Ba$_2$YIrO$_6$.\textsuperscript{48}

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