We consider improving the sensitivity of future interferometric gravitational-wave detectors by simultaneously injecting two squeezed vacuums (light), filtered through a resonant Fabry-Perot cavity, into the dark port of the interferometer. The same scheme with single squeezed vacuum was first proposed and analyzed by Corbitt et al. [Phys. Rev. D 70, 022002 (2004)]. Here we show that the extra squeezed vacuum, together with an additional homodyne detection suggested previously by one of the authors [F. Ya. Khalili, Phys. Rev. D 77, 062003 (2008)], allows reduction of quantum noise over the entire detection band. To motivate future implementations, we take into account a realistic technical noise budget for Advanced LIGO and numerically optimize the parameters of both the filter and the interferometer for detecting gravitational-wave signals from two important astrophysics sources, namely, neutron-star–neutron-star binaries and bursts. Assuming the optical loss of the ~30 m filter cavity to be 10 ppm per bounce and 10 dB squeezing injection, the corresponding quantum noise with optimal parameters lowers by a factor of 10 at high frequencies and goes below the technical noise at low and intermediate frequencies.

I. INTRODUCTION

During the last decade, several laser interferometric gravitational-wave detectors including LIGO [1], VIRGO [2], GEO600 [3], and TAMA [4] have been built and operated almost at their design sensitivity, aiming at extracting gravitational-wave signals from various astrophysical sources. At present, developments of next-generation detectors such as Advanced LIGO (AdvLIGO) [5] are also under way, and sensitivities of these advanced detectors are anticipated to be limited by quantum noise nearly over the whole observational band from 10 to \(10^4\) Hz. At high frequencies, the dominant quantum noise is photon shot noise, caused by phase fluctuation of the optical field; while at low frequencies, the radiation-pressure noise, due to the amplitude fluctuation, dominates and it exerts a noisy random force on the probe masses. These two noises, if uncorrelated, will impose a lower bound on the noise spectrum, which is called the standard quantum limit (SQL). In terms of gravitational-wave strain \(h = \Delta L/L\), it is given by

\[
S_h^{\text{SQL}} = \frac{6h}{m\Omega^2L^2}.
\]

(1)

It can also be derived from the fact that position measurements of the free test mass do not commute with themselves at different times [6].

The existence of SQL was first realized by Braginsky in the 1960s [7,8]. Since then, various approaches are proposed to beat the SQL. One recognized by Braginsky is to measure conserved quantities of the probe masses (also called quantum nondemolition quantities). This can be achieved, e.g. by adopting speed-meter configurations [9–14], which measure the conserved quantity momentum rather than the position. An alternative is to change the dynamics of the probe mass, e.g. using optical rigidity [15,16], in which case the free mass SQL mentioned is no longer relevant. As shown by Buonanno and Chen [17–19], optical rigidity exists in signal-recycled (SR) interferometric gravitational-wave detectors; therefore we can beat the SQL without radical redesigns of existing topology of the interferometers. Another approach is to modify input and/or output optics of the interferometers such that photon shot noise and radiation-pressure noise are correlated. After the initial paper by Unruh [20], this was further developed by other authors [21–29]. A natural way to achieve this is by injecting squeezed vacuum, in which phase and amplitude fluctuations are correlated, into the dark port of the interferometers. With great advancements in preparation of the squeezed state [30,31], squeezed-input interferometers will be promising candidates for third-generation gravitational-wave detectors. As elaborated on in the work of Kimble et al. [26], frequency-dependent squeezing is essential to reduce the quantum noise at various frequencies of the observation band. In addition, they demonstrated that this can be realized by filtering the frequency-independent squeezed vacuum through two detuned Fabry-Perot cavities before sending into the interferometer. Their results were extended by Buonanno and Chen [27], where the filters for general cases were discussed.

Another method, which also uses an additional filter cavity and squeezed light, but in a completely different...
way, was proposed by Corbitt, Mavalvala, and Whitcomb (hereafter referred to as CMW) \cite{21}. They proposed to use a tuned optical cavity as a high-pass filter for the squeezed vacuum. This scheme does not create the noises correlation, but instead, renders the noise spectral densities frequency dependent. At high frequencies, the phase squeezed vacuum gets reflected by the filter and enters the interferometer such that high-frequency shot noise is reduced; while at low frequencies, ordinary vacuum transmits through the filter and enters the interferometer, thus low-frequency radiation-pressure noise remains unchanged. One significant advantage is that the squeezed vacuum does not really enter the filter cavity and thus it is less susceptible to the optical losses. However, it does not perform as well as hoped for, and there is a noticeable degradation of sensitivity in the intermediate-frequency range. One of us \cite{32} pointed out that this has to do with the quantum entanglement between the optical fields at two ports of the filter cavity. Equivalently, it can be interpreted physically as the following: some information about phase and amplitude fluctuation flows out from the idle port of the filter cavity and the remaining quantum state which enters the interferometer is not pure. In order to recover the sensitivity, the filter cavity needs to have a low optical loss such that this information can be collected with an additional homodyne detector (AHD) at the idle port. Given an achievable optical loss of the filter cavity of $10^{-10}$ per bounce, Khalili showed that we can obtain the desired sensitivity at intermediate frequencies. A natural extension of this scheme is sending additional squeezed vacuum into the idle port of the filter cavity such that the low-frequency radiation-pressure noise is also suppressed. The corresponding configuration is shown schematically in Fig. 1, where two squeezed vacuums $\hat{s}$ and $\hat{p}$ are injected from two ports of the filter cavity, and some ordinary vacuum $\hat{n}$ leaks into the filter due to optical losses. By optimizing the

![Diagram](image-url)

FIG. 1 (color online). Schematic plot of the proposed configuration. Two squeezed vacuums $\hat{s}$ and $\hat{p}$ are injected from both sides of the filter cavity rather than the one which was considered in Refs. [21, 32]. The signal is detected by the main homodyne detector (MHD) and an additional homodyne detector (AHD) is made in the idle port of the filter cavity. ETM: end test mass; ITM: input test mass; PRM: power recycling mirror; PBS: polarized beam splitter; IM: input mirror; EM: end mirror; SQZ: squeezed light.
squeezing angles of squeezed states, we will show that the resulting quantum noise is reduced over the entire observational band.

The outline of this paper is as follows. In Sec. II, we will calculate the quantum noises in this double squeezed-input CMW scheme with AHD (later referred to as CMWA). We will use the same notation as in Ref. [19], which enables us to extend the results in Ref. [32] to the case of signal-recycled interferometers easily. In Sec. III, we numerically optimize the parameters of this new scheme for searching the gravitational-wave signals from neutron-star–neutron-star (NSNS) binaries and bursts. Finally, we will summarize our results in Sec. IV. For simplicity, we will neglect the optical losses inside the main interferometer, but we consider the losses from the filter cavity and also nonunitary quantum efficiency of the photodiodes. As shown in Refs. [17,26,33], these losses will be significant.

The main notations used in this paper are listed in Table I.

II. QUANTUM-NOISE CALCULATION

A. Filter cavity

In this section, we will derive single-sided spectral densities of the two outgoing fields \( \hat{a} \) and \( \hat{q} \) as shown in Fig. 1. From the continuity of optical fields, we can relate them to ingoing fields, which include two squeezed vacuums with single-sided spectral densities:

\[
\rho = \left( \begin{array}{c} S_A \rho_A \sqrt{S_A} \\
S_A \rho_A \sqrt{S_A}, \rho_A \sqrt{S_A} \end{array} \right) = \rho_A \sqrt{S_A}. \tag{3}
\]

The noise spectral densities of the two filter-cavity outputs can then be written as

\[
\tilde{S}_{\hat{a} \hat{p}}(\Omega) = |R_i(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_i(\Omega)|^2 \tilde{I}, \tag{4}
\]

\[
R_i(\Omega) = \frac{\gamma_{11} - \gamma_{12} + \gamma_{22} + i \Omega}{\gamma_{11} - \gamma_{12} - \gamma_{22} + i \Omega}, \tag{5a}
\]

\[
R_E(\Omega) = \frac{\gamma_{11} - \gamma_{12} + \gamma_{22} - i \Omega}{\gamma_{11} - \gamma_{12} - \gamma_{22} - i \Omega}, \tag{5b}
\]

\[
A_i(\Omega) = \frac{2\gamma_{11} - \gamma_{12} + \gamma_{22} - i \Omega}{\gamma_{11} - \gamma_{12} - \gamma_{22} - i \Omega}. \tag{5c}
\]

The noise spectral densities of the two filter-cavity outputs can then be written as

\[
\tilde{S}_{\hat{a} \hat{p}}(\Omega) = |R_i(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_i(\Omega)|^2 \tilde{I}, \tag{6}
\]

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = |R_E(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_E(\Omega)|^2 \tilde{I}, \tag{7}
\]

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = |R_i(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_i(\Omega)|^2 \tilde{I}, \tag{8}
\]

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = |R_E(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_E(\Omega)|^2 \tilde{I}, \tag{9}
\]

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = |R_i(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_i(\Omega)|^2 \tilde{I}, \tag{10}
\]

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = |R_E(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |T(\Omega)|^2 \tilde{R}(2r_{p}, 2\theta_p) + |A_E(\Omega)|^2 \tilde{I}, \tag{11}
\]

where \( \tilde{S}_{\hat{a} \hat{q}}(\Omega) \) is the cross correlation between two outputs; \( \tilde{I} \) is the identity matrix, and

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = \left( \begin{array}{c} \tilde{S}_{A_{i} A_{i}}(\Omega) \\
\tilde{S}_{A_{i} A_{e}}(\Omega) \\
\tilde{S}_{A_{e} A_{i}}(\Omega) \\
\tilde{S}_{A_{e} A_{e}}(\Omega) \\
\end{array} \right) \tag{12}
\]

with \( i = \hat{a} \hat{a}, \hat{a} \hat{q}, \) and \( \hat{a} \hat{q} \), whose elements are single-sided spectral densities.

\[
\tilde{S}_{\hat{a} \hat{q}}(\Omega) = \left( \begin{array}{c} \tilde{S}_{A_{i} A_{i}}(\Omega) \\
\tilde{S}_{A_{i} A_{e}}(\Omega) \\
\tilde{S}_{A_{e} A_{i}}(\Omega) \\
\tilde{S}_{A_{e} A_{e}}(\Omega) \\
\end{array} \right). \tag{13}
\]
B. Quantum noise of the interferometer

According to Ref. [19], the input-output relation, which connects ingoing fields \( \hat{a} \) and gravitational-wave signal \( h \) with the outgoing fields \( \hat{b} \), for a signal-recycled interferometer can be written as

\[
\hat{b} = \frac{1}{M} \left( \tilde{C} \hat{a} + D \frac{h}{\hbar_{\text{SQL}}} \right).
\]

In the above equation,

\[
M = [\delta^2 - (\Omega + i\gamma)^2] \Omega^2 - \delta \iota_c,
\]

and \( \tilde{C} \) is the transfer function matrix with elements

\[
\begin{align}
\tilde{C}_{11} &= \tilde{C}_{22} = \Omega^2 (\Omega^2 - \delta^2 + \gamma^2) + \delta \iota_c, \\
\tilde{C}_{12} &= -2\gamma \delta \Omega^2, \\
\tilde{C}_{21} &= 2\gamma \delta \Omega^2 - 2\delta \iota_c,
\end{align}
\]

where \( \iota_c = 8\omega_0 L_c/(mcL) \). The elements of the transfer function vector \( D \) are

\[
D_1 = -2\delta \sqrt{\gamma \iota_c} \Omega, \\
D_2 = -2(\gamma - i\Omega) \sqrt{\gamma \iota_c} \Omega.
\]

The effective detuning \( \delta \) and bandwidth \( \gamma \) are given by

\[
\begin{align}
\delta &= \frac{2r_{\text{SR}} \gamma_{\text{arm}} \sin(2\phi_{\text{SR}})}{1 + r_{\text{SR}}^2 + 2r_{\text{SR}} \cos(2\phi_{\text{SR}})}, \\
\gamma &= \frac{(1 - r_{\text{SR}}^2) \gamma_{\text{arm}}}{1 + r_{\text{SR}}^2 + 2r_{\text{SR}} \cos(2\phi_{\text{SR}})}.
\end{align}
\]

where \( r_{\text{SR}} \) is the amplitude reflectivity of the signal recycling mirror (SRM) and \( \phi_{\text{SR}} \) is phase detuning of the SR cavity. If the main homodyne detector (MHD) measures

\[
\tilde{b}_\phi(\Omega) = \sqrt{\eta} [\sin \phi \tilde{b}_\Lambda(\Omega) + \cos \phi \tilde{b}_\varphi(\Omega)] + \sqrt{1 - \eta} \hat{\nu}(\Omega),
\]

where \( \phi \) is the homodyne angle and \( \hat{\nu} \) is the additional vacuum due to nonunity quantum efficiency of the photodiode, and then the corresponding \( h \)-referred quantum-noise spectral density can be written as

\[
S_h(\Omega) = h^2_{\text{SQL}} \frac{(\sin \phi \cos \phi) \tilde{C} \tilde{S}_{\text{E}}(\sin \phi \cos \phi)^T + \frac{1 - \eta}{\eta} |M|^2}{(\sin \phi \cos \phi) \tilde{D} \tilde{D}^\dagger (\sin \phi \cos \phi)^T}.
\]

It can be minimized by adjusting the squeezing angle \( \theta \) of \( \hat{s} \) and \( \hat{p} \). We can estimate the optimal \( \theta \) qualitatively from the asymptotic behavior of the resulting noise spectrum. At very high frequencies (\( \Omega \gg \gamma \)), from Eq. (2), \( \hat{a} \sim \hat{s} \) and thus

\[
S_h(\Omega) \approx \cosh(2r_s) + \cos[2(\phi + \theta_s)] \sinh(2r_s).
\]

If the squeezing angle of \( \hat{s} \)

\[
\theta_s = \frac{\pi}{2} + n\pi - \phi,
\]

where \( n \) is an integer, we achieve the optimal case, namely, \( S_h \approx e^{-2r_s} \). Similarly, at very low frequencies (\( \Omega \ll \gamma \)), we have \( \hat{a} \sim \hat{p} \) and the spectral density \( S_h \approx e^{-2r_f} \) if

\[
\theta_p = \arctan \left( \frac{2 \cos \phi \sin \beta}{\cos(\beta - \phi) + 3 \cos(\beta + \phi)} \right).
\]

More accurate values for optimal \( \theta_{s,p} \) can be obtained numerically as we will apply in the next section. Given optimal \( \theta_{s,p} \), the sensitivity of this double squeezed-input scheme improves at both high and low frequencies. However, due to the same reason as in the case of single squeezed-input that two outputs of the filter cavity are entangled [32], this double squeezed-input scheme does not perform well in the intermediate-frequency range. To recover the sensitivity, we need to use an AHD at the idle port \( E \) of the filter cavity. The corresponding measured quantity is

\[
\hat{q}_\xi(\Omega) = \sqrt{\eta} [\sin \xi \tilde{b}_\Lambda(\Omega) + \cos \xi \tilde{b}_\varphi(\Omega)] + \sqrt{1 - \eta} \hat{v}'(\Omega),
\]

where \( \xi \) is the homodyne angle and \( \hat{v}'(\Omega) \) is the addition vacuum, which enters due to nonunity quantum efficiency of the photodiode. We combine \( \hat{q}_\xi(\Omega) \) with the output \( \tilde{b}_\phi(\Omega) \) using a linear filter \( \mathcal{K}(\Omega) \), obtaining

\[
\tilde{b}(\Omega) = \mathcal{K}(\Omega) \hat{q}_\xi(\Omega).
\]

Corresponding, the noise spectral density of this new output \( \tilde{b}(\Omega) \) can be written as

\[
S_b(\Omega) = S_{\tilde{b}_\phi}(\Omega) - 2\eta |\mathcal{K}(\Omega)S_{\tilde{b}_\phi}\hat{q}_\xi(\Omega)| + |\mathcal{K}(\Omega)|^2 S_{\hat{q}_\xi}(\Omega).
\]

The minimum quantum noise is achieved when \( \mathcal{K}(\Omega) = S_{\tilde{b}_\phi}\hat{q}_\xi(\Omega)/S_{\tilde{b}_\phi}(\Omega) \) and the resulting \( h \)-referred noise spectrum with AHD is then

\[
S_h^{\text{AHD}}(\Omega) = S_h(\Omega) - h^2_{\text{SQL}} \eta |(\sin \phi \cos \phi) \tilde{C} \tilde{S}_{\text{E}}(\sin \xi \cos \xi)^T|^2 / (\sin \phi \cos \phi) \tilde{D} \tilde{D}^\dagger (\sin \phi \cos \phi)^T S_{\hat{q}_\xi}(\Omega),
\]

where \( S_{\hat{q}_\xi}(\Omega) \equiv \eta |(\sin \xi \cos \xi) \tilde{S}_{\text{E}}(\sin \xi \cos \xi)^T + 1 - \eta \). The second term has a minus sign, which shows explicitly that the sensitivity increases as a result of additional detection.

III. NUMERICAL OPTIMIZATIONS

In this section, we will take into account realistic technical noise and numerically optimize interferometer parameters for detecting gravitational-wave signals from specific astrophysics sources which include NSNS binaries and bursts.

For a binaries system, according to Ref. [34], the spectral density of a gravitational-wave signal is given by
The upper limit of the integral

\[ S_h(2\pi f) = \frac{\pi}{12} \left( \frac{GM^{5/3}}{c^3} \right) \frac{f_{\text{max}} - f}{(\pi f)^{7/3}}. \]  

(26)

Here the “chirp” mass \( \mathcal{M} \) is defined as \( \mathcal{M} \equiv \mu^{3/5}M^{2/5} \) with \( \mu \) and \( M \) being the reduced mass and total mass of the binaries system. With other parameters being fixed, the corresponding spectrum shows a frequency dependence of \( f^{-7/3} \). Therefore, as a measure of the detector sensitivity, we can define an integrated signal-to-noise ratio (SNR) for NSNS binaries as

\[ \rho_{\text{NSNS}} \propto \int_{f_{\text{min}}}^{f_{\text{max}}} \frac{f^{-7/3} \, df}{S_\text{h}^{\text{quant}}(2\pi f) + S_\text{h}^{\text{tech}}(2\pi f)}. \]  

(27)

The upper limit of the integral \( f_{\text{max}} \approx f_{\text{ISCO}} = \frac{4400}{(M/M_\odot)} \) Hz is determined by the innermost stable circular orbit frequency, and the lower limit \( f_{\text{min}} \) is set to be 10 Hz, at which the noise can no longer be considered as stationary. Here we choose \( M = 2.8M_\odot \), the same as in Ref. [35]. Here \( S_\text{h}^{\text{quant}} \) is the quantum-noise spectrum derived in the previous sections and \( S_\text{h}^{\text{tech}} \) corresponds to the technical noise obtained from BENCH [36].

Bursts are another interesting astrophysical source [37]. The exact spectrum is not well modeled and a usual applied simple model is to assume a logarithmic-flat signal spectrum, i.e. \( S_h(2\pi f) \propto f^{-1} \). The corresponding integrated SNR is then given by

\[ \rho_{\text{burst}} \propto \int_{f_{\text{min}}}^{f_{\text{max}}} \frac{d \log f}{S_\text{h}^{\text{quant}}(2\pi f) + S_\text{h}^{\text{tech}}(2\pi f)}. \]  

(28)

The integration limit is taken to be the same as the NSNS binaries case.

To estimate the SNR and also motivate future implementation of this scheme, we assume the filter cavity has a length of \( \sim 30 \) m and an achievable optical loss 10 ppm per bounce and also consider the nonunity quantum efficiency of the photodiodes \( \eta = 0.9 \) for both MHD and AHD. Other relevant parameters will be further optimized numerically. For comparison, we will also optimize other related configurations, which include AdvLIGO, AdvLIGO with frequency-independent squeezed-input (FISAdvLIGO for short), and the CMW scheme. Specifically, free parameters for these different schemes that need to be optimized are the following:

\[ \text{AdvLIGO: } r_{\text{SR}}, \phi_{\text{SR}}, \phi, \]  

(29a)

\[ \text{FISAdvLIGO: } r_{\text{SR}}, \phi_{\text{SR}}, \phi, \theta, \]  

(29b)

\[ \text{CMW: } r_{\text{SR}}, \phi_{\text{SR}}, \phi, \gamma_1, \gamma_E, \theta, \theta_p, \zeta. \]  

(29c)

\[ \text{CMWA: } r_{\text{SR}}, \phi_{\text{SR}}, \phi, \gamma_1, \gamma_E, \theta, \theta_p, \zeta. \]  

(29d)

The resulting optimal parameters for different schemes are listed in Table II. They are rounded to have two significant digits at most to balance various uncertainties in the technical noise. The integrated SNR \( \rho \) is normalized with respect to that of the AdvLIGO configuration. The optimal \( \theta_s \) from the numerical result is in accord with the asymptotic estimation, namely, \( \theta_s = (\pi/2) - \phi \) [cf. Eq. (20)].

The corresponding quantum-noise spectra of different schemes optimized for detecting gravitational waves from NSNS binaries are shown in Fig. 2. The FISAdvLIGO, FISAdvLIGO, and CMW schemes almost have the identical integrated sensitivity and the CMWA scheme shows moderate 20% improvement in SNR. This is attributable to the fact that the signal spectrum of NSNS binaries has a \( f^{-7/3} \) dependence and low-frequency sensitivity is very crucial. However, due to low-frequency tech-

\begin{table}[h!]
\centering
\caption{Optimization results for different schemes.}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline
\textbf{Configurations} & \textbf{NSNS} & \textbf{Bursts} \\
\hline
\text{AdvLIGO} & \( r_{\text{SR}} \) & \( \phi_{\text{SR}} \) & \( \phi \) & \( \gamma_1 \) & \( \gamma_E \) & \( \phi \) & \( \theta_p \) & \( \zeta \) & \( r_{\text{SR}} \) & \( \phi_{\text{SR}} \) & \( \phi \) & \( \theta_p \) & \( \zeta \) \\
\hline
\text{FISAdvLIGO} & 1.0 & 0.8 & 1.5 & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots \\
\text{CMW} & 1.0 & 0.7 & 1.6 & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots \\
\text{CMWA} & 1.0 & 0.8 & 1.6 & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots \\
\hline
\end{tabular}
\end{table}

\begin{figure}[h!]
\centering
\includegraphics[width=\textwidth]{fig2.png}
\caption{(color online). Quantum-noise spectra of different schemes with optimized parameters for detecting gravitational waves from NSNS binaries. The optimal values for the parameters are listed in Table II.}
\end{figure}

\footnote{This is the squeezing angle \( \theta \) in the case of single squeezed-input.}
technical noise, advantages of the CMWA scheme are at most limited in the case for detecting low-frequency sources. The case for detecting gravitational waves from bursts is shown in Fig. 3. The other three schemes have a significant 50% improvement in terms of SNR over AdvLIGO. The sensitivities of the optimal FISAdvLIGO, CMW, and CMWA schemes at high frequencies almost overlap each other. In addition, the detuned phases $\phi_{\text{SR}}$ of the signal recycling cavity of those three are nearly equal to $\pi/2$, which significantly increases the effective detection bandwidth of the gravitational-wave detectors and is the same as the resonant-sideband extraction (RSE) scheme. This is because a broadband sensitivity is preferable in the case of bursts which have a logarithmic-flat spectrum.

To show explicitly how different parameters affect sensitivity of the CMWA scheme, we present quantum-noise spectrums of different schemes using the same parameters as the optimal CMWA in Fig. 4. In the case of AdvLIGO, we obtain a RSE configuration with $\phi_{\text{SR}} = \pi/2$. The quantum noise of FISAdvLIGO with squeezing angle $\theta = \theta_s$ is lower at high frequencies but higher at low frequencies than the RSE AdvLIGO. FISAdvLIGO with $\theta = \theta_p$ behaves in the opposite way with a significant increase of sensitivity at low frequencies but worse at high frequencies. The CMW scheme with double squeezed-input, just as expected, can improve the sensitivity at both high and low frequencies but does not perform so well at the intermediate frequencies. The CMWA scheme performs very nicely over the whole observational band compared with others and it would be more attractive if the technical noise of the AdvLIGO design can be further decreased.

**IV. CONCLUSION**

We have proposed and analyzed the double squeezed-input CMWA scheme as an option for increasing sensitivity of future advanced gravitational-wave detectors. Given an achievable optical loss of the filter cavity and 10 dB squeezing, this CMWA configuration shows a noticeable reduction in quantum noise at both high and low frequencies compared with other schemes. Since the length of the filter cavity considered here is around 30 m, with the developments of low-loss coating and better squeezing-state sources, it could be a promising and relatively simple add-on to AdvLIGO without a need for dramatically modifying the existing topology.

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