Over 30% efficiency bifacial 4-terminal perovskite-heterojunction silicon tandem solar cells with spectral albedo

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We developed and designed a bifacial four-terminal perovskite (PVK)/crystalline silicon (c-Si) heterojunction (HJ) tandem solar cell configuration albedo reflection in which the c-Si HJ bottom sub-cell absorbs the solar spectrum from both the front and rear sides (reflected light from the background such as green grass, white sand, red brick, roofing shingle, snow, etc.). Using the albedo reflection and the subsequent short-circuit current density, the conversion efficiency of the PVK-filtered c-Si HJ bottom sub-cell was improved regardless of the PVK top sub-cell properties. This approach achieved a conversion efficiency exceeding 30%, which is higher than those of both the top and bottom sub-cells. Notably, this efficiency is also greater than the Schockley–Quiesser limit of the c-Si solar cell (approximately 29.43%). The proposed approach has the potential to lower industrial solar cell production costs in the near future.

The highest recorded efficiency of a practical single-junction silicon solar cell is 26.7%, obtained under an inter-digitated back contact (IBC) silicon heterojunction (HJ) configuration. The cell was developed by Kaneka in Japan1. However, this recorded efficiency remains lower than the theoretical efficiency limit of a single-junction silicon solar cell (i.e., 29.43%)2. The discrepancy between the practical and theoretical efficiencies can be attributed to thermalization and transmission loss3–5. To overcome this drawback, tandem solar cells consisting of multijunction configurations with various optical band gaps to harvest the entire solar spectrum range were developed following extensive investigations6. Both inorganic-inorganic and organic–inorganic materials have been examined to create tandem architectures3–13.

Tandem configurations can be roughly grouped into three categories, namely spectral splitting, four-terminal (mechanically stacked), and two-terminal (monolithically integrated)14,15. Among these, the optical splitting architecture showed an efficiency of approximately 28%16. However, the device configuration is complicated...

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such that the device cannot be feasibly produced in bulk. In a monolithically integrated configuration, top and bottom sub-cells are electrically coupled in series; hence, the short-circuit current density ($I_{sc}$) of the tandem device is limited by $I_{sc}$ of the lowest sub-cell. Thus, the tandem power conversion efficiency (PCE) is constrained. This implies that current matching between the top and bottom sub-cells must be strictly fulfilled and form the initial challenge concerning the fabrication of two-terminal tandem solar cells. Another challenge concerns the high-quality deposition of the top sub-cell on the textured surface of the bottom silicon sub-cell.

Alternatively, in the four-terminal tandem architecture, the top and bottom sub-cells are optically—but not electrically—coupled. The requirement for perfect current matching is thus negligible. The top and bottom sub-cells are independently fabricated; therefore, the high quality of the top sub-cell can be easily recreated on a glass substrate due to its smooth surface. Some effort has been expended to create the four-terminal configuration in tandem devices. Quiros et al. optimized single-junction perovskite (PVK) solar cells via nanostructure transparent electrodes using a silver nanowire. The obtained efficiency was 26.7% and 25.2% for perovskite-passivated emitter rear locally diffused (PERL) and perovskite-IBC tandem devices, respectively. Using the same device configuration, Wang et al. reported a conversion efficiency of 27.0% based on a perovskite-heterojunction with an intrinsic thin-layer (HIT) configuration. This was achieved by employing a MoO$_3$/Au/MoO$_3$ multilayer for a transparent electrode of the perovskite top sub-cell. A similar architecture employing Cao$_x$ for the electrode selective contact and a SnO$_2$/ZTO/ITO transparent electrode for the Perovskite top sub-cell was created using a perovskite–silicon tunnel oxide passivated contact (TOPCon) tandem configuration (with a PCE of 26.7%)..

Another attempt to achieve the same device configuration involved copper indium gallium selenide (CIGS) instead of crystalline silicon (c-Si) based material for the bottom sub-cell. The obtained conversion efficiency of ~5.9% was lower than that of the perovskite–Si-based HIT tandem solar cells. By employing a charge transfer–induced 2,9-dimethyl-4,7-diphenyl-1,10-phenanthroline (BCP):Ag complex between a $n_{top}$ electron-transport layer and sputtered indium–zinc oxide top electrode, the efficiency of the semi-transparent perovskite solar cells (PSCs) was improved from 16.14 to 18.19%. An efficiency of 27.59% was then obtained for the four-terminal PSCs/TOPCon configuration. The four-terminal with bifacial PSCs–metal wrap through silicon hetero-junction configuration was also reported; using this configuration, a device conversion efficiency of 30.5% was reached.

Prior studies indicate that the standard-alone Si-based HIT solar cell always exhibits high efficiency (>20%) in defiance of less than 10%. This occurred because a short wavelength range was yielded by the perovskite top sub-cell, following which the $J_{sc}$ of the bottom sub-cell, and, accordingly, the PCE were reduced. Studies have attempted to improve $J_{sc}$ of the bottom sub-cell via minimized absorption using the perovskite sub-cell, which can be accomplished using high-band-gap perovskite material or highly transparent electrodes. Therefore, to achieve higher efficiency in tandem solar cells, the top and bottom sub-cells must fulfill solar spectra with respect to their optical band gaps. To meet this requirement, a bifacial four-terminal perovskite–HIT tandem solar cell with spectral Albedo was investigated in this study for the first time. This design configuration is advantageous thought its ability to improve $J_{sc}$ of the bottom sub-cell via spectral albedo, in defiance of the top sub-cell properties and without raising costs compared with mono-facial tandem cells.

Results and discussion

Evaluating top sub-cell candidates for the bifacial four-terminal tandem solar cell. The preceding discussion suggests that the PCEs of individual sub-cells must be as high as possible, without presenting sub-cell current density matching, to obtain the highest PCE of the bifacial four-terminal tandem device. Recently, organic and inorganic materials, such as hydrogenated amorphous silicon (a-Si:H), hydrogenated amorphous silicon germanium (a-SiGe:H), hydrogenated microcrystalline silicon (μc-Si:H), and PVK, have been employed for the top sub-cell. To classify the appropriate top sub-cell candidates for tandem device application, different single-junction thin film solar cells were fabricated and characterized. Figure 1 presents the quantum efficiencies (QEs) for different types of top sub-cell candidates. QE curves can be roughly divided into two zones, namely, the short-wavelength region (<600 nm) and long-wavelength region (>600 nm). The QE behavior of the a-Si:H and a-SiGe:H thin-film solar cells (TFSs) shows negligible differences in the wavelength range of 300 to ~550 nm, whereas that of a-SiGe:H TFS shows an improvement in the wavelength range of ~350 to ~800 nm when compared to the a-Si:H TFS. Such an improvement can be attributed to the improved light absorption in the long-wavelength range for the case of a-SiGe:H with a low optical band gap, as reported previously. Figure 1 also exhibits the QE behavior of the μc-Si:H TFS. The result thereof confirmed the enhanced infrared absorption of the μc-Si:H TFS compared with the amorphous silicon TFS. It is interesting to note that the perovskite top sub-cells’ QE indicates a significant enhancement in the all-wavelength zone of interest compared with semi-transparent amorphous silicon TFS. The transparent perovskite sub-cell, on the other hand, shows substantial improvement in the wavelength range of 300 nm to ~800 nm. However, the cut-off of the perovskite's QE occurs at a wavelength of 800 nm, whereas that of the μc-Si:H TFS is still available up to 1100 nm.

Base on the experimental QE results, the integrated photocurrents were simulated and are presented in Table 1. The calculated results may be predicted. The highest integrated photocurrent is 26.76 mA/cm$^2$ for the μc-Si:H solar cell, followed by that for the semi-transparent perovskite (22.60 mA/cm$^2$), a-SiGe:H (18.50 mA/cm$^2$), and a-Si:H (15.65 mA/cm$^2$) TFS. Therefore, the semitransparent μc-Si TSF and perovskite TSF are potential candidates for achieving high conversion efficiency in the top sub-cell of a four-terminal tandem device. In addition, the characteristics of the different semitransparent cells were examined and are presented in Table 1. These results are similar to those of the QEs. The μc-Si TSF has the highest $J_{sc}$ of 26.81 mA/cm$^2$, followed by perovskite TFS ($J_{sc}$ of 22.66 mA/cm$^2$), a-SiGe:H TFS ($J_{sc}$ of 18.32 mA/cm$^2$), and a-Si:H TFS ($J_{sc}$ of 15.56 mA/cm$^2$). However, the behavior of $V_{oc}$ was found to be different than that of $J_{sc}$. The highest $V_{oc}$ was
obtained for the perovskite TFS (1100 mV), followed by a-Si:H TFS (900 mV), a-SiGe:H TFS (850 mV), and μc-Si TFS (510 mV). Finally, the PCE gathers all the characterizations of the device performance. This information is also presented in Table 1. Here, all amorphous silicon and microcrystalline silicon exhibited a PCE of ~10%. Notably, the semitransparent perovskite solar cell had a PCE of up to 17.1%. Thus, our analysis indicates that the fabricated semitransparent perovskite thin-film solar cell is potentially the top candidate for the top sub-cell in a four-terminal tandem solar cell, in defiance of the highest Jsc from the μc-Si:H thin-film solar cell.

Table 1. Calculated Jsc and performance metrics of various top sub-cell candidates.

| Material    | Jsc (mA cm⁻²) | Voc (V) | FF (%) | Efficiency (%) |
|-------------|---------------|---------|--------|----------------|
| PVK         | 22.60         | 22.66   | 1.10   | 68.60          | 17.10          |
| a-Si:H      | 15.65         | 15.56   | 0.90   | 70.40          | 9.86           |
| a-SiGe:H    | 18.50         | 18.32   | 0.85   | 64.20          | 10.00          |
| μc-Si:H     | 26.76         | 26.81   | 0.51   | 68.22          | 9.33           |

Figure 1. Measured QE spectra of the various top sub-cell candidates. The black, red, blue, and magenta lines depict the QE of the PVK, a-Si:H, a-SiGe:H, and μc-Si:H thin film solar cell, respectively.

Figure 2. Illuminated current–voltage characteristics of the various top sub-cell candidates and standard-alone a-Si:H/c-Si heterojunction solar cell under 1 sun. The black, red, blue, magenta, and olive lines indicate the J-V curves for the PVK, a-Si:H, a-SiGe:H, μc-Si:H thin film solar cell and c-Si HJ solar cell, respectively.
Bifacial four-terminal tandem solar cell fabrication and characterizations. The four-terminal tandem solar cell structure was constructed, as shown in Fig. 3a. The semitransparent perovskite serves as the top sub-cell, that is, a solar filter for the a-Si:H/c-Si bottom sub-cell. Figure 3b shows the performance of the bifacial four-terminal tandem device under 1 sun illumination on the front side. The characteristics of the standard-alone a-Si:H/c-Si HJ solar cell without a PVK filter were measured and are presented in Fig. 3b. The obtained results indicate that the performance of the PVK remains unchanged. By contrast, several characteristics of the PVK-filtered a-Si:H/c-Si HJ solar cell showed a significant decrease, particularly $J_{sc}$ (from $\sim 40.00\text{ mA/cm}^2$ to $\sim 15.15\text{ mA/cm}^2$). Hence, the conversion efficiency decreased significantly, from 23.35 to 8.68%.

To elucidate the main reason for $J_{sc}$ reduction of the PVK-filtered HIT sub-cell, the transmittance of the PVK cell was investigated, as depicted in Fig. 4a. The PVK cells absorbed all solar spectra in the short-wavelength range. This implies that the solar spectrum that reaches the bottom sub-cell is lower than that without PVK filtering, leading to decreased electron–hole pair generation, which can be detrimental to $V_{oc}$ and particularly $J_{sc}$. The result of a low $J_{sc}$ for a PVK-filtered HIT bottom sub-cell can be clearly understood upon analyzing the QE results. Figure 4b shows the QE of a PVK sub-cell and PVK-filtered HIT sub-cell. Based on the QE results, the calculated photocurrents are $21.50$ and $16.22\text{ mA/cm}^2$ for the PVK top sub-cell and PVK-filtered HIT bottom sub-cell, respectively. These values are consistent with the experimental results. A conversion efficiency (sum of the conversion efficiencies of the PVK cell and the PVK-filtered cell) of 25.78%, which is higher than that of each independent sub-cell, was achieved for the four-terminal perovskite-HIT configuration.

Thus, the a-Si:H/c-Si HJ bottom sub-cell performance remained significantly below that under the standard operation condition (AM 1.5 G or 1 Sun) ($J_{sc}$ of $\sim 15.15\text{ mA/cm}^2$ of the PVK-filtered HIT cell is significantly below...
the state-of-the-art value of the standard-alone HIT cell with a $J_{sc}$ of ~ 40 mA/cm$^2$, owing to the PVK-filter on the top, as seen in Fig. 4b. To push the PVK-filtered a-Si:H/c-Si HJ bottom sub-cell works close to 1 sun condition or the state-of-the-art, causing a rise in the $J_{sc}$ and conversion efficiency, the bifacial 4-terminal tandem design with spectral albedo was also promoted (Fig. 3a). Here, the albedo reflection intensity can be accurately adjusted in the range of 0–0.5 sun by altering the distance between the cell holder and illumination source, as seen in Fig. 5. A calibrator was used to accurately control the albedo reflection. The advantage of using the bifacial solar cell is its acquisition of the solar spectrum from both sides: direct solar spectrum from the front side and reflected solar spectrum from the background (green grass, white sand, red brick, roofing shingle, snow, etc.)$^6$. Figure 6a shows the efficiencies of the bifacial standard-alone a-Si:H/c-Si HJ and the bifacial four-terminal perovskite/c-Si HJ tandem solar cell as a function of the albedo spectrum. Here, the front illumination was kept fixed at 1 sun. The conversion efficiency of the top PVK cell (red circle) remains nearly unchanged, whereas that of the bifacial standard-alone HIT cell (black square) showed slight improvement with the albedo reflection. The conversion efficiency of the PVK-filtered HIT bottom sub-cell (blue triangle) showed a significant enhancement from 8.68 to 12.99% when the spectral albedo increased from 0 to 0.5 sun (refer to the supporting information for details in Fig. S1, S2). Consequently, the conversion efficiency (sum of the efficiencies of the PVK and PVK-filtered HIT cells) of the bifacial four-terminal tandem cell (pink triangle) showed a significant improvement from 25.78 to 30.09%, apparent in Fig. 7 and Table 2. To date, this remains a comparatively high conversion efficiency value achieved in PVK/HIT tandem solar cells.

The current density of the PVK-filtered HIT sub-cell as a function of the albedo spectrum was measured, as seen in Fig. 6b. The $J_{sc}$ of the standard-alone HIT cell (black square) under 1 sun is also presented for reference. As shown in Figs. 6b, 7 and Table 2, we observe a monotonous increase in the $J_{sc}$ of the PVK-filtered HIT cell (red square, Fig. 6b) from ~ 15.15 mA/cm$^2$ to ~ 33.64 mA/cm$^2$ (Fig. 7 and Table 2) and in the albedo reflection from 0 sun to 0.5 sun. It is worth noting that the highest $J_{sc}$ with an albedo reflection of 0.5 sun is still lower than that of the standard $J_{sc}$ value of the HIT cell (~ 40 mA/cm$^2$). It is suggested that a higher $J_{sc}$ regarding the upper
limits of the c-Si HJ solar cell of approximately 42 mA/cm² can be achieved using albedo reflection for the bifacial four-terminal tandem cell. To achieve higher conversion efficiency, further investigations such as lesser plasma damage of underlying organic–inorganic layers or higher albedo light intensity are required.

**Bifacial 4-terminal PVK/HIT tandem solar cell modeling.** Simulated results were employed to examine the PVK/c-Si HJ tandem solar cell to elucidate the reason for the improvement in $J_{sc}$ and, thereby, the con-
version efficiency. Figure 8 shows the simulated photo-generated rate distribution, which was determined using AFORS-HET software, within the PVK/c-Si JH tandem solar cell under three selected conditions: without spectra albedo (dashed red line), with spectra albedo of 0.3 sun (dotted blue line) and with spectra albedo of 0.5 sun (dash-dotted magenta line). For reference purposes, the simulated photo-generated rate distribution inside the a-Si:H/c-Si JH solar cell without a PVK filter (solid black line) is plotted as a function of the cell position. We observed that the bottom sub-cell of the PVK/HIT tandem solar cell without albedo reflection shows fewer
photo-generated electron–hole pairs in the entire device length than the standard-alone a-Si:H/c-Si heterojunction solar cell, a matter which deems detrimental to all parameters of the bottom sub-cell, as discussed earlier.

For PVK/c-Si HJ tandem solar cells, the photo-generated rate was kept unchanged through the PVK and emitter region (a-Si:H) of the bottom sub-cell, as opposed to the albedo reflection conditions. As a result, the albedo reflection did not contribute to the performance of the PVK cell, where we notice no change in the PCE of the PVK with variation in the albedo spectrum intensities. Using the albedo spectrum, the generated electron–hole pairs were improved remarkably along the bottom sub-cell position, particularly those close to the end of the cell. The higher the albedo reflection is, the higher the photo-generated rate will be.

In summary, a bifacial four-terminal PVK/c-Si HJ tandem solar cell with albedo reflection was proposed in this study. In a traditional four-terminal PVK/c-Si HJ configuration, the solar spectrum in the short-wavelength region is absorbed by the PVK top sub-cell, leaving the remaining spectrum to be absorbed by the c-Si HJ bottom sub-cell. However, not all photons corresponding to bottom sub-cell's optical bandgap can be yielded. The \( I_{sc} \) (~ 15.15 mA/cm²) and consequent the conversion efficiency (8.68%) values for the bottom sub-cell are, therefore, far below the state-of-the-art values of the standard cell. Our approach employed a bifacial four-terminal PVK/c-Si HJ tandem structure with an albedo reflection, which increases the number of absorbed photons into the a-Si:H/c-Si HJ bottom sub-cell. As a result, \( I_{sc} \) and the conversion efficiency of the c-Si HJ bottom sub-cell improved from ~ 15.15 to 33.5 mA/cm² and from 8.68 to 12.99%, respectively, when the albedo reflection increased from 0 to 0.5 sun. The excellent photon yielding of the a-Si:H/c-Si HJ sub-cell enabled a high \( I_{sc} \). We showed that the conversion efficiency of the PVK/HIT tandem solar cell was as high as 30.10%. These findings encourage further studies on the improvement of the conversion efficiency of four-terminal tandem solar cell using albedo reflection and/or low plasma damage of underlying organic–inorganic layers²³.

Methods

For the PVK solar cell fabrication, methylammonium-lead (II) iodide \((\text{CH}_3\text{NH}_2\text{PbI}_3)\) was employed as the absorbent layer, which was positioned between a NiO layer and phenyl C₆₁-butyric acid methyl ester (PCBM) material. The NiO and PCBM layers served as hole and electron transport materials, respectively. The final structure of the PVK solar cell is, thus, glass/fluorine-doped tin oxide \((\text{FTO})/\text{NiO/absorber/PCBM/BCP/aluminum-doped zinc oxide (AZO)/Ag} \). FTO glasses were treated in ultrasonic bath with acetone, ethanol, and DI water, for 10 min each in sequences. An atomic layer deposition \((\text{ALD})\) system was employed to deposit the NiO hole transport layer at a temperature of 200 °C. Stoichiometric MAPbI₃ solution was prepared by mixing DMF and DMSO solvents to prepare the perovskite precursor solution. The precursor solution, after being stirred overnight in an inert atmosphere glove box, was dropped on the NiO layer in accordance with the spin coating method, after which the layer was dried on a hot plate to form the perovskite absorber layer. The PCMB/BCP electron transport layer was then coated on the absorber layer according to the spin coating technique; AZO was grown at 100 °C by using the ALD system. Finally, the Ag electrode was developed using thermal evaporation with a shadow mask. The detailed fabrication process can be found in a previous publication by Seo et al.²².

For an a-Si:H/c-Si HJ solar cell fabrication, commercial Czochralski-grown n-type c-Si wafers 200 μm thick with an electrical resistivity of ~ 2.7 Ω·cm were used as the absorbent layer. Henceforth, the a-Si:H/c-Si HJ solar cell is termed the HJ solar cell. Passivated a-Si:H(i) layers were first deposited on both sides of the wafers. The nc-SiO:H(p) layer was then deposited on top of the a-Si:H(i) at one side as hole collector, whereas nc-SiO:H(n) layer was deposited on top of the a-Si:H(i) on the other side as the electron collector.

All a-Si:H layers were grown via plasma-enhanced chemical vapor deposition in a cluster system. For a bifacial configuration, 80 ± 5-nm-thick ITO was coated using a magnetron sputtered on top of the nc-SiO:H(p) and nc-SiO:H(n) layers in sequence. Finally, Ag finger grids were printed on top of the ITO layers via a low-temperature screen-printing method. The details of the growth conditions employed for all layers can be found in a previous report²⁴. The final structure of the HJ solar cell is as follows: Ag(finger-grids)/ITO/nc-SiO:H(n)/a-Si:H(i)/c-Si(n)/a-Si:H(i)/nc-SiO:H(p)/ITO/Ag(finger grids).

To measure the current density–voltage characteristic of the bifacial four-terminal tandem solar cell, the bifacial solar cell Zig was designed for bi-directional investigation, as illustrated in Fig. 5a. Real photographs of a bifacial solar cell Zig with an a-Si:H/c-Si HJ solar cell are shown in Fig. 5b. Real photographs of semitransparent PVK solar cell and measurement schematics are shown in Fig. 5c,d, respectively. The details of the growth conditions employed for all layers can be found in a previous publication by Seo et al.²². All a-Si:H layers were grown via plasma-enhanced chemical vapor deposition in a cluster system. For a bifacial configuration, 80 ± 5-nm-thick ITO was coated using a magnetron sputtered on top of the nc-SiO:H(p) and nc-SiO:H(n) layers in sequence. Finally, Ag finger grids were printed on top of the ITO layers via a low-temperature screen-printing method. The details of the growth conditions employed for all layers can be found in a previous report²⁴. The final structure of the HJ solar cell is as follows: Ag(finger-grids)/ITO/nc-SiO:H(n)/a-Si:H(i)/c-Si(n)/a-Si:H(i)/nc-SiO:H(p)/ITO/Ag(finger grids).

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\[
\eta_{\text{Bifacial}} - 4\% = \eta_{\text{PVK}} - \eta_{\text{Top}} + \eta_{\text{PVK-filtered a-Si:H/c-Si HJ bottom sub-cell}}
\]  

Here the conversion efficiency of the PVK-filtered c-Si HJ bottom sub-cell, \( \eta_{\text{PVK-filtered c-Si HJ bottom sub-cell}} \), is the normalized conversion efficiency (output power normalized to 1 sun illumination, that is, for 100 mW/cm²). The optical transmittance of the PVK cells was characterized using an ultraviolet–visible spectrophotometer in the wavelength range of 300–1100 nm (Sisco S-3100). The QE of each sub-cell was determined at 25 °C using a solar cell spectrum response/QE/incident photo-to-current efficiency measurement system G1218a (PV
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References
1. Kunta, Y. et al. Silicon heterojunction solar cell with interdigitated back contacts for a photoconversion efficiency over 26%. Nat. Energy. 2, 1–8 (2017).
2. Shockley, W. & Queisser, H. J. Detailed balance limit of efficiency of pn junction solar cells. J. Appl. Phys. 32, 510–519 (1961).
3. Park, J. et al. High efficiency inorganic/inorganic amorphous silicon/hetrojunction silicon tandem solar cells. Sci. Rep. 8, 15382 (2018).
4. Gilet, J., Wiek, M. M. & Janssen, R. A. J. Optimizing polymer tandem solar cells. Adv. Mater. 22, 67–71 (2010).
5. Kim, T. et al. Triple-junction hybrid tandem solar cells with amorphous silicon and polymer-fullerene blends. Sci. Rep. 8, 7154 (2015).
6. Thomas, C. R. R., Belle, S. & Bandyopadhyay, N. Characterization and analysis of Shockley-Queisser limit of a-Si:H-based tandem solar cells. J. Appl. Phys. 127, 055105 (2020).
7. Chaudhuri, S., Suresh, A. & Alegria, M. A theoretical study of silicon tandem solar cell. Sol. Energy Mater. Sol. Cells 193, 110858 (2019).
8. Stang, R., Haschke, J., & Leendertz, C. In solar energy, In: Tech e-book, Germany 2009; O. Gabriel, S. Kirner, C. Leendertz, M. Schade, H. & Smith, Z. E. Optical properties and quantum efficiency of A-Si1−xCx:H/a-Si:H solar cells. Jpn. J. Appl. Phys. 50, 052301 (2011).
9. Mailoa, J. P. et al. A 2-terminal perovskite/silicon multijunction solar cell enabled by a silicon tunnel junction. Appl. Phys. Lett. 106, 121105 (2015).
10. Kim, S. et al. High efficiency solar cells combining a perovskite and a silicon heterojunction solar cells via an optical splitting system. Appl. Phys. Lett. 106, 013506 (2015).
11. Schade, H. & Smith, Z. E. Optical properties and quantum efficiency of a-Si,„C„H/a-Si: H solar cells. J. Appl. Phys. 57, 568–574 (1985).
12. Albrecht, S. et al. Monolithic perovskite/silicon-heterojunction tandem solar cells processed at low temperature. Energy Environ. Sci. 9, 81–88 (2016).
13. Kim, S. et al. The recorded open-circuit voltage and fill factor achievement of A-Si:H p-i-n/HIT-type tandem solar cells by tuning up the crystalline in tunneling recombination junction layer. Semicond. Sci. Technol. 34, 065004 (2019).
14. Wang, Z. et al. 27%-Efficiency four-terminal perovskite/silicon tandem solar cells by sandwiched gold nanomesh. Adv. Funct. Mater. 30, 1908298 (2019).
15. Werner, J. et al. Efficient NIR-transparent perovskite solar cells enabling direct comparison of 4-terminal and monolithic perovskite/silicon tandem cell. ACS Energy Lett. 1, 474–480 (2016).
16. Uzu, H. et al. High efficiency solar cells combining a perovskite and a silicon heterojunction solar cells via an optical splitting system. Appl. Phys. Lett. 106, 013506 (2015).
17. Quiroz, C. O. R. et al. Balanced electrical and optical losses for efficient 4-terminal Si–perovskite solar cells with solution processed percolation electrodes. J. Mater. Chem. A. 6, 3583–3592 (2018).
18. Rohtagi, A. et al. 26.7% Efficient 4-terminal perovskite-silicon tandem solar cell composed of a high-performance semitransparent perovskite cell and a doped poly-Si/SiOx passivating contact silicon cell. IEEE J. Photovolt. 10, 417–422 (2020).
19. Ying, Z., Yang, Y., Zheng, J., Zhu, Y., Xu, J., Chen, W., Shou, C., Sheng, J., Zeng, Y., Yan, B., Pan, H., Ye, J., & He, Z. Charge-transfer induced multifunctional BCP:Ag complexes for semi-transparent perovskite solar cells with a record fill factor of 80.1%. J. Mater. Chem. A. 9, 12009–12018 (2021).
20. Coletti, G. et al. Bifacial four-terminal perovskite/silicon tandem solar cell and modules. ACS Energy Lett. 5, 1676–1680 (2020).
21. Lim, S. et al. Semi-transparent perovskite solar cells with bidirectional transparent electrodes. Nano Energy 82, 105703 (2021).
22. Seo, S., Jeong, S., Bae, C., Park, N. & Shin, H. Perovskite solar cells with inorganic electron- and hole- transport layers exhibiting long-term (=500 h) stability at 85 °C under continuous 1 sun illumination in ambient air. Adv. Mater. 32, 1801010 (2020).
23. Kim, S. et al. Improving the efficiency of rear emitter silicon solar cell using an optimized n-type silicon oxide front surface field layer. Sci. Rep. 8, 10657 (2018).
24. Stang, R., Haschke, J., & Leendertz, C. In solar energy, In: Tech e-book, Germany 2009; O. Gabriel, S. Kirner, C. Leendertz, M. Gerhardt, A. Heidelberg, H. Bloeß, R. Schlätman & B. Rech (eds.), Phys. Status Solidi C. 8, 2982–2985 (2011).

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Author contributions
V.A.D., J. K., and J. Y. designed the project and supervised the experimental and simulation processes. S. K. designed the project and performed all experiments and discussions. T. T. Tr., J.P., and D. P. P. performed all experiments and discussions. S. L. and N. N. D helped with experimentation. H. B. D helped with simulation.

Competing interests
The authors declare no competing interests.

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