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Failure Modes in Concrete Repair Systems due to Ongoing Corrosion

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1. Introduction

Corrosion of reinforcement is the most common deterioration mechanism affecting reinforced concrete structures [1]. In general, steel reinforcement is protected from corrosion by a passive film which is formed on its surface in highly alkaline concrete. However, if this protection is lost (which could happen due to either chloride ingress [2] or carbonation [3]), the steel will begin to corrode. During corrosion, the corrosion products expand and exert pressure on the surrounding concrete. Already at moderate levels of corrosion, generated tensile stresses lead to cracking of the concrete cover [4, 5]. In the engineering practice, cracked and chloride contaminated concrete is removed, the steel bar is cleaned, and the damaged concrete is replaced with a repair material, resulting in patch repair. Nevertheless, corrosion of the steel bar often continues after the repair, due to differences in electrochemical behaviour of the old and new concrete, inadequately cleaned reinforcement and corrosion pits [6], high permeability of the repair material or the interface during the hardening period, or microcracks in the repair material due to the restrained shrinkage [7]. This could result either in an incipient anode phenomenon (when the rust is produced not in the repair itself, but in the nearby concrete) or in further corrosion occurring within the repaired location (Figure 1) [6–8]. Ongoing corrosion in a repair system is one of the most common causes for premature failure of patch repairs. As the development of the corrosion cell depends on many parameters and is difficult to control, in cases when corrosion is continuing inside the repair material itself, the occurrence of damage can be controlled by use of a suitable repair material.

In general, service life or reinforced concrete structures are considered to end once the corrosion starts. This is because the modelling and prediction of the corrosion induced damage contain high levels of uncertainty. As a result, the aforementioned approach for service life prediction is (very) conservative. This is especially true for
repair systems, which are rarely crack-free and where the time needed for the onset of corrosion may be very short. Therefore, for more practical service life predictions, it seems important to investigate corrosion induced damage propagation in repair systems.

Most investigations of strain hardening cementitious composite (SHCC) for repair applications have mainly focused on the material’s mechanical performance and deformational capacity in flexural and restrained shrinkage tests [9, 10]. Recently, its applicability for patch repair against steel corrosion has been studied [11]. It was shown that SHCC patch repair, due to its small crack widths, effectively suppressed chloride penetration and prevented the occurrence of reinforcement corrosion. However, the concrete substrate that was used in these experiments was free from chloride contamination. Furthermore, cracks that were introduced in the repair system prior to corrosion testing were a result of an externally applied mechanical loading and not the corrosion process itself. The performance of patch repair systems when continued corrosion is the underlying cause of pressure build-up is still not investigated. This can be relevant when high ductility of the repair material is needed to accommodate the high local imposed pressure.

In this paper, the feasibility and implications of using SHCC in concrete overlays and patch repairs with ongoing corrosion in the steel bar surrounded by the repair material are studied. Reinforcement imbedded in different types of repair materials was exposed to accelerated corrosion, and failure modes of repair systems were investigated. The damage development is then simulated with the lattice model. The influence of critical parameters (interface strength, surface roughness, and substrate strength) on fracture behaviour of the repair system is studied. The aim of this paper is not to study the corrosion induced cracking, which has been a topic of numerous studies [5, 12–14], but rather to focus on failure behaviour of different repair systems during ongoing corrosion and how this behaviour changes with aforementioned parameters. This was not done in the past but could provide important knowledge for damage development in repair practice.

2. Materials and Methods

2.1. Experimental Procedure. Fracture behaviour of SHCC mixtures and the same mixture without fibres (i.e., mortar) was previously studied [15]. In that study, prior to casting, a smooth steel rod with a diameter of 6 mm was placed in the centre of each specimen as a reinforcement bar (Figure 2). Specimens were left in laboratory conditions ($T = 20^\circ C$, $RH = 50\%$) for 10 days before demoulding and preparing for accelerated corrosion test. Subsequently, each specimen was immersed in a container with saturated calcium-hydroxide solution, wrapped in a titanium mesh to act as a counter electrode, and connected to a Direct Current (DC) regulator to enforce corrosion. Corrosion induced cracking of the SHCC and the mortar specimen after different exposure times were monitored by using three-dimensional micro-computed tomography (CT scan). More information about these experiments can be found in [15].

In this study, similar tests were performed on repair systems in order to study the performance of SHCC as a repair material in case of ongoing corrosion inside the repair material. Three different repair materials were used: SHCC, nonreinforced repair mortar (further referred to as repair mortar), and commercial repair mortar. Mix composition of SHCC is given in Table 1 while nonreinforced repair material...
Table 1: Mix proportion of SHCC mix (weight %).

| CEM I 42.5N | Limestone powder | Blast furnace slag | Water/powder ratio | Superplasticizer | PVA fiber (by volume, %) |
|-------------|------------------|--------------------|---------------------|------------------|-------------------------|
| 1           | 3.33             | 2.33               | 0.26                | 0.005            | 2                       |

Figure 3: Preparation of the repair systems for accelerated corrosion tests.

Table 2: Comparison of properties of commercial mortar and SHCC.

|                         | w/p | Density [kg/m³] | E [GPa] | f_c [GPa] |
|-------------------------|-----|-----------------|---------|-----------|
| Commercial mortar       | 0.16| 1950            | 16      | 45        |
| SHCC                    | 0.26| 2025            | 18.5    | 40        |

is the same mixture only without the fibres. The commercial repair material (Cuglacrete Hoogoven A middle R3) was chosen such that it has similar properties as the SHCC used in this study (comparison of properties is given in Table 2). It is a polymer modified blast furnace slag based mortar with polyacrylonitrile fibres. Note that these fibres do not enable strain hardening behaviour.

Repair materials were cast on top of a 2-year-old mortar substrate. The test set-up is shown in Figure 3(a). The substrate was made with a smooth and a grooved surface (Figure 3(b)). Both the height and the width of the grooves were 3 mm. Once the substrates were prepared (Figure 3(b)), the repair material was cast (Figure 3(c)). Specimens were demoulded after 24 h and sealed cured for six days. Subsequently, they were left to dry for 72 h in laboratory conditions (T = 20°C, RH = 50%). Finally, specimens were exposed to accelerated corrosion by applying an external voltage (Figure 4(a)). Since all specimens were tested at the same time, voltage (instead of current) was used as a controlling parameter. The voltage was increased twice during the test to speed up the onset of damage (Figure 4(b)). At the end of the experiment, all samples were impregnated with fluorescent epoxy to investigate the crack patterns. The results were then compared to simulated cracks. In parallel to these tests, compression tests were performed on the repair materials and the substrate. These tests were performed on 40 × 40 × 40 mm³ specimens.

2.2. Modelling Procedure. In order to investigate the mechanical performance of a repair system subjected to continued reinforcement corrosion, the lattice model is used [16, 17]. In the lattice model, the material is discretised as a network (lattice) of beam elements which can transfer forces. The material microstructure/mesostructure can be mapped onto the mesh by assigning different mechanical properties to beams in the lattice. In this way, fracture behaviour of composite quasi-brittle materials such as cement paste [18], concrete [16], or graphite [19] can be simulated. Usually all the single elements have linear elastic properties. In each loading step, an element that exceeds the limit stress or strain capacity is removed from the mesh. The analysis procedure is then repeated until a predetermined failure criterion for the simulated specimen is achieved. In this way realistic crack patterns can be obtained.

The procedure to generate the network is as follows [20]:

(i) A cubical grid is chosen (square for 2D lattice).

(ii) In each cell of the square (cube for 3D lattice), a random location for a lattice node is selected. First the nodes are randomly positioned inside a subcell of size s in a regular grid with size A (Figure 5). The ratio s/A is defined as randomness of a lattice and here it is set to be 0.5. This means that some disorder is built into the lattice mesh itself.

(iii) Always the three nodes (four nodes for 3D) which are closest to each other are connected by beam elements.
Titanium mesh (counter electrode)
Rebar (working electrode)

DC power supply

(a) Set-up for corrosion test

Water

Repair material
Mortar substrate

(b) Applied voltage in accelerated corrosion test

Figure 4: Accelerated corrosion test.

Figure 5: Schematic 2D representation of generation of fibre-lattice [14].

using Delaunay triangulation. Each node of the 3D system has 6 degrees of freedom (3 translations and 3 rotations)

(iv) The beams which belong to each phase are identified by overlapping material layers (i.e., concrete/mortar substrate and repair material) on top of the lattice. Interface elements are generated between substrate nodes and repair material nodes. In Figure 5, generation of interface elements for the smooth and rough (grooved) substrate surface is presented.

(v) Fibre elements are added in the repair material according to a chosen volume content (2% by volume in case of SHCC), fibre length, and diameter. The location of the first node of each fibre is chosen randomly in the specified volume and a random direction is defined which determines the position of the second node. If the second node is outside of the mesh boundary, then it is automatically cut off and accounted for in order to ensure preservation of prescribed volume content.

(vi) Extra nodes inside the fibres are generated at each location where the fibre crosses the square (in 3D cubical) grid.

(vii) Fibre interface elements are generated between fibre nodes and the matrix nodes in the neighbouring cell. Also, the end nodes of the fibres are connected with an interface element to the matrix node in the cell where the fibre end is located (Figure 5).

(viii) An element can fail either in tension or in compression, when the stress exceeds its strength. For the fracture criterion, only axial forces are taken into account to determine the stress in the beams.

(ix) In order to take material heterogeneity of the substrate into account, either a computer-generated material structure or a material structure obtained by micro-CT scanning [21, 22] can be used. Here, the
concrete mesostructure was simulated using the Anm material model originally developed by Garboczi [23] and implemented in a 3D parking algorithm by Qian et al. [24]. It is based on placing multiple irregular shape particles separated into several sieve ranges into a predefined empty container. Aggregates smaller than 4 mm are not explicitly modelled and, together with the cement matrix, are considered to constitute the mortar phase.

(x) Material overlay procedure (Figure 6(a)) is used and further extended for including the aggregates in the concrete substrate. Interface elements are generated between the substrate nodes and the repair material nodes (interface MS/RM) while aggregate-paste interface (ITZ) elements are generated between the mortar nodes and the aggregates (Figure 6(b)). In this manner, different mechanical properties are assigned to different phases (Table 3). Figure 7 shows the substrate with exposed aggregates before “casting” of the repair material. As already explained, interface elements in the model are larger than real interfaces. However, interface properties in simulations are fitted such that they represent the effect of the real interface size.

The performance of repair systems with repair mortar (without PVA fibres) and SHCC used as repair materials are simulated. The volume percentage of the crushed stone in the simulated concrete substrate is 30%. This should approximately correspond to the amount of coarse aggregates in the concrete. 67% of coarse aggregates are in the sieve range (8, 16) mm and 33% are in the sieve (4, 8) mm (see Table 1). In the simulations, apart from the interface strength, also the strength of the substrate was varied. This is done in order to account for differences in strength between the repair material and the concrete substrate, which usually exists in experiments and practice. In one of the simulations, therefore, the mortar and the ITZ strengths in the substrate were 5 MPa and 3.5 MPa, respectively (instead of 4 MPa and 2.5 MPa, Table 1).

Table 3: Input values for lattice fracture model (\(E\) stands for the modulus of elasticity, \(f_t\) stands for the tensile strength, and \(f_c\) for the compressive strength of elements).

| Element                  | \(E\) [GPa] | \(f_t\) [MPa] | \(f_c\) [MPa] |
|--------------------------|-------------|---------------|---------------|
| Matrix (repair mortar, RM)| 20          | 3.5           | 35            |
| Fibre                    | 40          | 7380          | 7380          |
| Interface (matrix/fibre) | 20          | 90            | 900           |
| Mortar substrate         | 25          | 4/5           | 40/50         |
| Aggregate                | 70          | 8             | 80            |
| ITZ                      | 15          | 2.5/3.5       | 25/35         |
| Interface (MS/RM)        | 15          | 1/3           | 10/30         |
2.3. Expansive Pressure due to Corrosion Expansion. In the presented model, expansion of the corroding reinforcement is simulated by an equivalent, imposed pressure around the reinforcing steel when full restraint by the surrounding concrete is assumed (Figures 8 and 9). The imposed pressure generated by the expansive corrosion reaction on the surrounding concrete is related to the rust volume and the rebar section loss. It also depends on the modulus of elasticity of the rust, porosity around the bar, and concrete (micro) cracking because a part of the corrosion product will go into pores and cracks and release the pressure. The correlation is, therefore, very complex and is not linear. The proposed procedure for determination of the corrosion induced pressure on the surrounding concrete by knowing the rebar section loss is described in [13]. In that paper, corrosion induced cracking of the concrete cover was studied using the lattice model.

Several important aspects of the modelling procedure need to be addressed here. In the model, the total expansion pressure depends on the geometry (i.e., the bar diameter), the loss of steel cross section, and the mechanical properties of the rust layer (the modulus of elasticity and the ratio between the density of rust versus the density of steel). When it comes to the mechanical properties of the rust layer, however, a huge range of values has been reported in the literature: for example, in [25], a value of around 0.13 GPa for modulus of elasticity of the rust layer was reported; on the other hand, values of around 50 GPa were found using nanoindentation technique [15, 26]. Since this is not a topic of the current study, herein all results are expressed in terms of the expansion pressure and not in terms of loss of steel cross section. Note, however, that the pressure is related to the loss of steel cross section, as described in [13].

3. Model Validation

Experiments presented in [15] are used to validate the modelling approach. In the experiment, cracks opened widely and the mortar specimen failed completely during the test.
Figure 10: CT scan of corrosion induced cracking [13] in (a) plain mortar (b) SHCC. Blue colour denotes the steel rebar, red the rust layer, black the material matrix, and white voids and cracks.

(Figure 10(a)). In contrast, the SHCC specimen showed high resistance to corrosion induced cracking. A large number of relatively narrow cracks were created (Figure 10(b)).

Numerical simulations show similar results (Figure 11). In the plain mortar once the cracks opened, the specimen could not take any more pressure and failed (Figure 11(a)). Brittle failure at small crack widths occurred. In SHCC, however, consecutive cracks were forming, allowing the specimen to withstand higher pressure resulting in ductile performance of the material (Figure 11(b)). Numerous cracks with small crack widths formed. Once the crack is formed (for any type of material), it allows some amount of corrosion product to go into existing cracks and reduces further cracking [27]. Potential benefits of using SHCC in a repair system with ongoing corrosion are further investigated and compared to experiments.

4. Parametric Study and Discussion

4.1. Influence of Surface Roughness and Interface Strength. In the following simulations, dimensions of the system are $80 \times 80 \text{ mm}^2$ with a repair material thickness of 40 mm and a rebar of 10 mm diameter in its centre. The thickness of the simulated specimen (i.e., out-of-plane dimension) is 5 mm. Sizes of the simulated specimens are not the same as those of experimentally tested specimens. However, the intention here was to qualitatively verify crack propagation...
with the experiments. Therefore, the dimension ratios and the geometry in the experiments and the simulations are the same.

First, repair systems with the plain repair mortar and with the smooth and the rough substrate surface (3 mm exposed aggregates) are simulated (Figure 12). In these simulations, the concrete substrate has the same tensile strength as the repair material. Three different specimens are examined: smooth surface, interface strength 1 MPa; rough surface, interface strength 1 MPa; and rough surface, interface strength 3 MPa.

In the simulation with the smooth surface, a failure of the repair system (defined as the limit when the system cannot take anymore increase in pressure) follows immediately after the onset of debonding (Figure 12(a)). The system fails at low imposed pressure with hardly any warning signs (only one vertical crack). In the test with the rough surface, however, more heterogeneity is present at the interface, enabling more stable crack development. Cracks are trapped in the roughness profiles, and this allows for further cracking to develop. As a result, the pressure that the sample can withstand is significantly higher compared to the simulation with the smooth surface (Figure 13). If appropriate roughness is provided, it seems that the interface strength does not have a significant influence in the early stage of damage (up to 20 MPa). However, as the pressure increases, the interface strength does play a role. With 1 MPa interface strength, results indicate that there is a balance between debonding and substrate cracking (Figure 12(b)), while with 3 MPa interface strength, damage occurs only through substrate cracking and no debonding is observed (Figure 12(c)).

Maximum crack widths in the SHCC repair system, under the same imposed pressure, are significantly lower compared to cracks when mortar is used as a repair material (compare Figure 16 with Figure 13). Roughness plays the same role with SHCC as a repair material. With smooth surface substrate, brittle failure at the interface occurs (Figure 14(a)). However, in the rough surface, roughness profiles are interlocking the crack and the failure is more ductile (Figure 14(b)).

The same is observed experimentally (Figure 15). Smooth specimen exhibits large debonding, resulting in interface failure (Figure 15(a)). With grooved surface, two specimens are tested. One specimen behaves similarly to the simulated specimen with the lower interface strength (compare Figure 15(b) and 14(b)). Sample 2 (sealed cured for 7 days) behaves similarly to the specimen simulated with the higher interface strength (compare Figure 15(c) and 14(c)). Note, however, that differences in these two crack patterns are minor and that, in both cases, grooves interlocked the crack from the repair material and directed it through the substrate. This indicates that, with the rough surface, interface strength becomes less important than with the smooth surface. Similar benefits of higher substrate roughness (without the need of...
Figure 14: Numerically obtained crack pattern and maximum crack widths due to the pressure imposed by expanding bar in repair systems. SHCC is used as a repair material, influence of the substrate surface roughness, and the interface strength (deformation scaled 20x; note that for different samples maximum crack widths are different).

Figure 15: Experimentally obtained damage patterns when SHCC is used as a repair material (top: repair material; bottom: mortar substrate; interface is indicated with the arrow); samples are epoxy impregnated and imaged under UV light.

Figure 16: Influence of interface strength and substrate surface roughness on imposed internal pressure and corresponding maximum crack widths prior to repair system failure. SHCC is used as a repair material (LBS corresponds to interface strength 1 MPa and HBS to interface strength of 3 MPa).

4.2. Influence of Repair Material. Numerically obtained crack patterns with different repair materials are given in Figure 17. Crack distribution is compared to experimentally obtained cracks. At the same pressure levels (around 26 MPa), maximum crack width inside the SHCC is a few times smaller compared to the repair mortar (Figure 17). More cracks form, with small cracks widths (up to 70 µm). However, the substrate is still brittle and SHCC does not prevent cracks from propagating into the substrate.

Similar results are obtained experimentally (see Figure 18). While SHCC exhibits multiple microcracking, in the
repair mortar a wide crack opens above the reinforcing bar. The commercial repair material shows a similar behaviour (Figure 18(c)). This material contains also fibres but it does not have strain hardening capacity nor the controlled crack widths.

With the interface strength of 1 MPa (around 30% of the matrix strength), a simulated damage corresponds well to experimentally obtained damage in repair systems. This is valid both when the repair mortar and the SHCC are used as repair materials. In experiments, however, there is less cracking in the mortar substrate (compare Figure 17(a) with Figure 18(a)). This could be a result of the substrate strength used in the simulations. In the simulations, the mortar substrate is assumed to have the same tensile strength as the repair material. However, according to the compressive strength results (Figure 19), the mortar substrate is significantly stronger than the repair materials. Therefore, the strength of the substrate was adjusted in order to see how this influences the behaviour of the repair system.

4.3. Influence of Substrate Strength and Interface Strength. Substrate stronger than the repair material is examined (Figure 20). The interface strength is again varied (from 1 MPa to 3 MPa). In the initial phase, when microcracking develops around the expanding bar, the interface strength does not influence the maximum crack width (Figure 21, imposed pressure of 20 MPa). The substrate is strong and it will not
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Figure 19: Compressive strength results of the repair materials and mortar substrate used in this study.

Figure 20: Numerically obtained crack pattern and maximum crack widths due to the pressure imposed by expanding bar in repair systems. Substrate is stronger than repair material, influence of the interface strength, and type of the repair material; top: repair material; bottom: substrate (deformation scaled 20x; note that for different samples maximum crack widths are different).

5. General Discussion

If the reinforcing bar surrounded by a newly placed repair material continues to corrode (due to either higher permeability of the repair material, restrained shrinkage cracking, or inadequate cleaning of the bar), further damage in the repair system can be controlled with a SHCC type of repair material. Crack widths and the failure mode in the repair system with the repair (plain) mortar are very sensitive to the type of the surface preparation and substrate strength. With SHCC, the failure mode and crack widths are still sensitive to the substrate surface preparation, but there is less sensitivity to the substrate strength. Furthermore, under these loading conditions, independent of the type of repair material, the local interface strength becomes less important if the substrate surface is rough. This is because a rough surface enables more cracking and higher ductility during failure. Roughness profiles are interlocking cracks in the substrate (similar to [18, 28]) thereby preventing complete delamination. On the other hand, some debonding (as long as it does not result in complete delamination) may be beneficial for stress relief and smaller cracks in the repair material and the substrate.

Interface strength in this paper is studied by combining modelling and experimental testing. Once the tests are performed, the interface strength in the simulation is...
adjusted so that the simulated fracture corresponds to the experimentally obtained crack pattern [29]. This should be then performed for various boundary conditions. Only in this way the interface strength, which is a micromechanical property, can be investigated at mesoscale. In these simulations and with these boundary conditions, the same fracture behaviour as in experiments was obtained when the interface strength is around 30% of the strength of the repair material. Similar results were obtained for flexure tests performed in [20].

6. Conclusions

In this paper, the influence of ongoing corrosion on damage development in repair systems is studied. For this purpose, the lattice fracture model is used. Simulated results were verified by accelerated corrosion experiments. Based on the presented results and discussions, the following conclusions can be drawn:

(i) Similar to the performance of the SHCC repair system in drying shrinkage, a smooth surface of the substrate is not advised, as it leads to brittle failure of the repair system. With SHCC as a repair material, the benefits of distributed cracking cannot be fully utilised.

(ii) With a rough surface, the interface strength becomes less important. Grooves enable interlocking and direct the crack to the substrate.

(iii) With a rough surface, SHCC repair enables distributed cracking with small crack widths (up to several times smaller compared to repair mortar). More warning signs are present prior to final failure of the repair system.
(iv) Due to ongoing corrosion (further corrosion of reinforcing bar inside the repair material), crack propagation and failure modes are predicted and explained with the lattice model. Interface strength in this way is implicitly studied. With the interface tensile strength equal to 30% of the matrix tensile strength, numerically predicted behaviour corresponds to experimentally observed behaviour.

(v) The balance between cracking and debonding is very sensitive to local material properties of the repair material, substrate, and interface. Local debonding adjacent to the crack, as long as it does not result in complete delamination, can be beneficial, as it enables reduction of stresses and smaller crack widths in the repair system.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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