Abstract—Symmetry is ubiquitous in everyday objects. Humans tend to grasp objects by recognizing the symmetric regions. In this letter, we investigate how symmetry could boost robotic grasp detection. To this end, we present a learning-based method for detecting grasp from single-view RGB-D images. The key insight is to explicitly incorporate symmetry estimation into grasp detection, improving the quality of the detected grasps. Specifically, we first introduce a new grasp parameterization in grasp detection for parallel grippers based on symmetry. Based on this representation, a symmetry-aware grasp detection network method is presented to simultaneously estimate object symmetry and detect grasp. We find that the learning of grasp detection greatly benefits from symmetry estimation, improving the training efficiency and the grasp quality. Besides, to facilitate the cross-instance generality of grasping unseen objects, we propose Principal-directional scale-Invariant Feature Transformer (PIFT), a plug-and-play module, that allows spatial deformation of points during the feature aggregation. The module essentially learns feature invariance to anisotropic scaling along the shape principal directions. Extensive experiments demonstrate the effectiveness of the proposed method. In particular, it outperforms previous methods, achieving state-of-the-art performance in terms of grasp quality on GraspNet-1-Billion and success rate on a real robot grasping experiment.

Index Terms—RGB-D perception, deep learning in grasping and manipulation, deep learning for visual perception.

I. INTRODUCTION

A S ONE of the most fundamental skills for intelligent robots, grasping has a wide range of applications from bin-picking for industrial robots to general object grasping for home service robots. With the recent progress of RGB-D sensing and 3D learning techniques, detecting feasible grasp from cluttered scenes has attracted a surge of research attention from robotics and computer vision communities.

Recent advances in grasp detection are dominated by learning-based approaches. According to whether the object geometry is known beforehand or not, these approaches can be divided into two categories: the model-based methods [36] and the model-free methods [9]. While the former is not always applicable to novel object grasping, the latter requires a large number of data with careful annotations to be trained with. In particular, those methods are prone to fall short in grasping novel objects located in cluttered scenes, due to the inferior generality caused by insufficient network training. To solve this problem, recent research has been focused on improving the quality of the train data [9], [38] or involving the advanced learning models [18], [24]. In this paper, we study the problem of grasp detection from a new perspective. The key insight is simple: symmetry is prevalent in everyday objects, and humans tend to grasp objects with fingers placed at symmetric regions. Theoretically, symmetry detection and grasp detection are highly relevant tasks in both psychology [8], [16] and robotics [1], [2]. Besides, from the prospect of geometry learning, symmetry is a lightweight yet informative representation of 3D geometry, which can potentially narrow the searching space of grasp detection. As such, understanding object symmetry seems to be an intermediate and complementary stage of grasp detection. It is therefore interesting to study whether symmetry detection could be incorporated into the grasp detection pipelines and boost the performance.

We present SymmetryGrasp, a learning-based method for detecting antipodal grasp from single-view RGB-D images with the guidance of symmetry estimation (Fig. 1). Our contributions are two-fold. First, we introduce a new parameterization of grasp detection for parallel grippers based on symmetry. The parameterization is designed to explicitly exploit symmetry clues and is expected to improve the robustness and generality of general grasp detection. Based on this parameterization, a symmetry-aware grasp detection network method is presented to simultaneously estimate symmetry and detect grasp. The detected grasps are located in local symmetric regions and regularized by the estimated symmetry. With a dedicated network design,
the network is able to detect plausible grasps on objects with multiple symmetry types, i.e., reflection, rotation, and sphere. Since the network is even applicable to objects whose symmetric region only occupies a small portion, it is not only designed for grasping symmetric objects but provides a universal solution for general grasp detection.

Second, to improve the cross-instance generalization ability in grasping the unseen objects, we propose Principal-directional scale-Invariant Feature Transformer (PIFT), a plug-and-play module for point convolutional networks. PIFT allows spatial deformation of points in the point convolution processing, facilitating feature invariance to scaling along principal directions of the symmetry plane/axis. Equipped with PIFT, SymmetryGrasp is able to detect high-quality grasps on novel objects.

Extensive experiments demonstrate that SymmetryGrasp is able to estimate symmetry and detect grasp in various scenes with good performance. In particular, the learning of grasp detection greatly benefits from symmetry estimation. SymmetryGrasp is robust in detecting grasps on objects with heavy occlusion and novel geometry, outperforming the prior methods. It achieves state-of-the-art performance in terms of grasp quality on GraspNet-1-Billion and success rate on a real robot grasping experiment.

II. RELATED WORK

A. Learning-Based Grasp Detection

Learning-based grasp detection methods can be roughly classified into two categories: model-based and model-free. Model-based methods [3], [31], [36], [41] rely on the pre-scanning of the target objects. The plausible grasps are generated by the mechanics-based approaches and are transferred into the captured data, usually by feature matching techniques, during inference. The drawback of model-based grasp detection methods is that they can hardly generalize to unseen objects whose 3D model is inaccessible. Conversely, model-free methods do not require the 3D model of the target objects to be fully known and are thus more general. The early research in this direction focuses on detecting planar grasp from single-view or multi-view images [14], [17], [20], [21], [29]. Recently, several algorithms and datasets have been proposed to learn high-DoF grasps [11], [25], [28], [35], [43]. Our method falls into this category. However, it is different to the previous works since it explicitly incorporates symmetry estimation into the grasp detection workflow, resulting in grasp detection with higher quality.

B. Symmetry Detection

Symmetry is a universal concept and is deemed to be one of the most basic geometric clues for object understanding [23], [30]. As such, symmetry detection could potentially benefit many downstream applications [26], such as shape completion [34] and pose estimation [5]. Prior works of symmetry detection are only applicable to synthetic objects in the virtual world, limiting the effectiveness of robotic applications. Several recent works studies detecting symmetry from partially observed data with various formats, such as RGB image [42], RGB-D image [32], [33], and 3D volume [10]. Our method is inspired by the above methods. However, it requires a significantly smaller number of training data, thanks to the designs on feature aggregation.

III. METHOD

A. Problem Setting

Our goal is to grasp objects with a robot arm. The robot arm is equipped with a parallel gripper. A depth camera is deployed around the robot arm to acquire RGB-D images. We assume the geometry of the gripper, the intrinsics of the camera, as well as the transformation between the camera and the robot arm, are already known. The objects are cluttered with each other, incurring mutual object occlusions and various object poses. Our method detects grasps from a single-view RGB-D image. To be specific, it generates a 7D grasp $R(t, d)$ from each of the objects from the acquired RGB-D image $I$, where $R$, $t$ and $d$ are the 3D rotation, the 3D translation, and the opening width of the two-finger gripper, respectively. $R$ and $t$ together determine a rigid transformation from the model coordinate of the gripper to the camera coordinate.

B. Symmetry-Guided Grasp Detection Parameterization

Directly estimating all 7 DoFs of the grasp is hard. We propose a decomposed grasp parameterization in grasp detection guided by symmetry. The idea is inspired by human behaviors on grasp. In order to perform robust grasping, humans are likely to first infer the contact points on the objects with the fingers (i.e. where to grasp), and then determine the direction of our hand to approach these contact points (i.e. how to grasp). We mimic the procedure and decompose the estimation of the 7D grasp into two stages.

On the first stage, the locations of the two contact points are estimated, determining 6 DoFs (i.e. 3 DoFs in translation, 2 DoFs in rotation, and 1 DoF in opening width):

$$\alpha, \beta, t, d = F(I),$$

where $\alpha$ and $\beta$ are the two Euler angles of the rotation $R$. In particular, we select one of the contact points from the input points and estimate its symmetric counterpart to be another one. The translation $t$ and opening width $d$ could then be determined accordingly.

On the second stage, the rotation of gripper around the line that connects the two contact points is estimated (i.e. 1 DoF in rotation):

$$\gamma = G(I, \alpha, \beta, t, d),$$

where $\gamma$ is the third Euler angle of rotation, determining the in-plane rotation.

The symmetry-guided grasp parameterization has the following advantages. First, it has a clear and natural task division that makes the first stage focus on intra-object geometry and the second stage analyze the inter-object layout, facilitating a more effective network training. Second, since it explicitly takes the symmetry as a prior, the grasp detection is well-constraint and therefore expected to be more accurate and stable. Third, it
allows the gripper to contact with the symmetric counterparts which might be located in the unseen region, the grasping location is not restricted to the observed points, expanding the manipulation range of the robot.

C. Method Overview

We present SymmetryGrasp to implement the above idea. The method starts by performing an instance segmentation to detect symmetric regions in the scene. Then, a symmetry-aware grasp detection network (i.e. $F(\cdot)$) is proposed to detect the contact points of the gripper. That is achieved by detecting symmetry and estimating the point-wise grasp affordance with a unified network. Last, a physics-based grasp selection algorithm (i.e. $G(\cdot)$) is present to generate plausible grasps. The overview of the method is illustrated in Fig. 2. In the following, we describe each step in detail.

D. Symmetric Region Detection

The first step is to detect graspable objects or regions in cluttered scenes. Existing works on robotic grasping have demonstrated that it is possible to detect grasps without performing an object detection [39], [40]. Nevertheless, these methods need to be trained on large-scale data with various scene layouts and are less robust in novel scenes.

To avoid this issue, our method follows the detect-first-then-grasp route. Unlike previous works in this route, our method detects symmetric regions which include both symmetric objects (for objects with global symmetry) and symmetric object regions (for objects with local symmetry). Noteworthy, detecting symmetric regions is more general for grasping, compared to detecting symmetric objects. This is because the former does not require the target object to be perfectly symmetric, and it includes simple primitives that repeat across multiple object types, greatly increasing the cross-instance generalities.

We implement the symmetric region detection by a Mask R-CNN [12] with an FPN backbone. The network is pre-trained on the COCO dataset [19] and fine-tuned on the GraspNet-1-Billion dataset [9]. To collect training data of symmetric regions, we manually annotate the symmetric regions on 12 objects in the GraspNet-1-Billion dataset. The annotations are then propagated to the objects in the RGB-D frames with using the 6D object poses. Our MaskRCNN model achieves an mAP at 0.72 and 0.55 with 0.5 IoU threshold on the seen and unseen subsets, respectively.

E. Symmetry-Aware Grasp Detection Network

Next, we describe the architecture and several key considerations of the symmetry-aware grasping detection network.

Principal-directional scale-invariant feature learning: Real-world symmetry annotation is prohibitive to be acquired due to the high labor cost [23]. Existing symmetry detection datasets are annotated by dedicated algorithms and manual adjustment procedures [32]. We propose a learning-based solution to alleviate the problem of insufficient symmetry annotation and increase the cross-instance generality.

The key insight of the solution is: object scaling along some specific directions will not influence the object symmetry. Those include all the directions that are perpendicular or parallel to the normal direction of the reflectional plane and the direction of the rotational axis. Those directions are referred to as principal directions. We determine the principal directions of each object based on its symmetry annotation in the canonical coordinate and then transfer them into the camera coordinate using the 6D object pose.

During training, for each detected object, we augment the input points by performing shape scaling on the principal directions and then propose Principal-directional scale-Invariant Feature Transformer (PIFT) to learn the feature invariance to scaling along the principal directions. We see this as analogous to the strategies of first adding noise and then denoising in conventional network training. As shown in Fig. 3, taking the cropped point cloud (converted from the RGB-D image) of the detected regions as input, we first augment the initial points by randomly scaling along one of its principal directions. The initial and the augmented point clouds are then fed into our Siamese network respectively for feature extraction. The extracted features are expected to be consistent. To achieve this, we use $L_{f}^{L}$ loss function to minimize the distance of the two features: $L_{f}^{L} = \sum_{j=1}^{N} L_{2}(f_{j}^{I}, f_{j}^{A})$, where $f_{j}^{I}$ and $f_{j}^{A}$ are the extracted features of the $j$-th point in the initial and augmented point cloud, respectively, $N$ is the number of points.

The backbone of the Siamese network is a PointNet++ [27] with PIFT modules. The PointNet++ takes $N$ points as input and outputs the point-wise features with the feature-length...
being 128. The PIFT modules are inserted in front of each set abstraction layer [27]. Formally, given the point cloud $P_i$ at the $i$-th layer and the corresponding point-wise feature $E_i$, PIFT learns a transformation $T_i = S_i R_i$ that deforms $P_i$ in the camera coordinate to $\tilde{P}_i$ in a transformed coordinate:

$$T_i = F_{\text{PIFT}}(P_i, E_i),$$

$$\tilde{P}_i = T_i P_i,$$

where $F_{\text{PIFT}}$ is a point convolutional network with a regression layer, $R_i \in \mathbb{R}^{3 \times 3}$ is the rotation matrix, $S_i \in \mathbb{R}^{3 \times 3}$ is the scaling matrix. The transformed point cloud $\tilde{P}_i$ is then fed into a set abstraction layer for feature aggregation:

$$\tilde{P}_{i+1}, E_{i+1} = F_{\text{SetAbstraction}}(\tilde{P}_i, E_i),$$

where $F_{\text{SetAbstraction}}$ is the set abstraction layer, $E_{i+1}$ is the extracted feature. The sampled points of the set abstraction layer $\tilde{P}_{i+1}$ (represented in the transformed coordinate) are then transformed back to the camera coordinate:

$$P_{i+1} = T_i^{-1} \tilde{P}_{i+1},$$

Fig. 3. The feature extraction network is trained in a Siamese fashion. The initial points and the augmented points are passed through a PointNet++ with PIFT modules. A feature consistency loss is adopted to facilitate the learning of principal-directional scale-invariant features.

Fig. 4. Principal-directional scale-Invariant Feature Transformer (PIFT) estimates a transformation that allows spatial deformation of points in the point convolution processing, facilitating feature invariance to scaling along principal directions of the symmetry plane/axis.

Symmetry and grasp predictions: To estimate the symmetries and detect the grasps, the point-wise features of the initial non-augmented point cloud are fed into several MLPs to make per-point predictions. Each point makes two predictions. First, it predicts the grasp affordance, indicating the confidence the object could be grasped when one finger of the gripper lies on the point. This is achieved by using a regression module. Second, it detects the potential reflectional, rotational, and spherical symmetries. Since the regions in our experiments could have at most 3 reflectional symmetries, 1 rotational symmetry, and 1 spherical symmetry, the network first predicts whether these potential symmetries exist by a classification module and then estimates the parameters of the valid symmetries by a regression module. The network architecture is shown in Figs. 2 and Fig. 5.

As such, the per-point loss consists of the grasp affordance loss $\mathcal{L}^g_j$ and the symmetry loss $\mathcal{L}^s_j$. To be specific, the affordance loss is:

$$\mathcal{L}^g_j = \mathcal{L}_i(a_j, \hat{a}_j),$$

where $a_j$ and $\hat{a}_j$ are the predicted and ground-truth affordance, respectively. The symmetry loss at the $k$-th point is:

$$\mathcal{L}^s_j = \sum_{k=1}^M w^s \mathcal{L}_c(c_{jk}, \hat{c}_{jk}) + w^s \mathcal{L}_r(s_{jk}, \hat{s}_{jk}) a_{kj},$$

where $c_{jk}$ is the estimated probability of the $k$-th symmetry prediction to be valid. $\hat{c}_{jk}$ is the ground-truth. $\mathcal{L}_c$ is the cross-entropy loss. $s_{jk}$ is the estimated symmetry parameters. $\hat{s}_{ij}$ is the ground-truth. For reflectional symmetry, the estimated parameters include the center of the object and the normal direction of the mirror plane. For rotational symmetry, the estimated parameters include the center of the object and the axis direction. For spherical symmetry, the estimated parameters only include the center of the object. $w^s$ and $w^r$ are the weights. We set $M = 5$ by assigning 3 output ends for reflectional symmetry estimation, 1 output end for rotational symmetry estimation, and 1 output end for spherical symmetry estimation, as shown in Fig. 5.

The parameterizations of $s_{jk}$ are set according to the symmetry type. For reflectional symmetry, $s_{jk}$ contains the center location of the object/region and the normal direction of the mirror plane. For rotational symmetry, it includes the center of the object and the axis direction.
location and a direction along the rotational axis. $\mathcal{L}_r$ is the dense symmetry loss that penalizes the difference between two symmetries [32], if the symmetry type is rotation or reflection. For spherical symmetry, our network only predicts the center location, so $\mathcal{L}_r$ is the MSE loss.

The symmetry loss is weighed by a regularization term $a_j$. Intuitively, this means that symmetry estimation will mostly rely on the points with high grasp affordance prediction. This is due to the fact that those points usually lie on the planar regions and will be less influenced by the scanning noise, providing more stable features. To sum up, the overall loss is the sum of feature consistency loss, grasp affordance loss and symmetry loss: $\mathcal{L} = w_f \mathcal{L}_f + w_a \sum_{j=1}^{N} \mathcal{L}_j^a + w_s \sum_{j=1}^{N} \mathcal{L}_j^s$, where $w_f, w_a$ and $w_s$ are the weights.

**Detecting multiple reflectional symmetries:** We use Hungarian algorithm [15] to solve the problem of optimal assignment that matches the symmetry predictions and ground-truth of multiple reflectional symmetries during training. Our method might output multiple reflectional symmetries with high affordance, which needs proper protocol to select the most plausible one to conduct grasp. To achieve this, we compute the normal direction of the target point and that of their predicted counterparts. The symmetry whose corresponding counterpart has the minimum angle difference in the normal direction to the target point is selected as the most plausible one.

**Determining grasp points from predicted symmetry:** The object symmetry is generated by the per-point symmetry predictions by an averaging operation. For points that have a high estimated grasp affordance (>0.5), we compute their symmetric counterparts. Each point together with its symmetric counterpart represent the contacting points between the object and the gripper. For rotational and spherical symmetries, we only consider the symmetric counterpart with the farthest Euclidean distance as the contacting point.

**F. Physics-Feasible Grasp Selection**

The above network generates graspable points simply based on the local geometry of the symmetric region, which might be physically infeasible or unstable. Therefore, we adopt a grasp selection algorithm to select the plausible ones.

First, we filter the incorrect grasp by checking if the estimated symmetry counterpart (i.e. the grasp point of the gripper) is located in the observed area of the RGB-D frustum. This could happen when the symmetry estimation is incorrect.

Second, we check if the gripper collides with the point cloud of the scene. For each grasp point pair, we sample $M$ grasp candidates via rotating the gripper around the line that connects the two points. The pre-defined gripper model is then transformed into the scene coordinate and conducts a collision detection with the input points. For objects that contain no valid grasp after the above selection protocols, we adopt a lightweight grasp detection approach based on object boundary to generate planar grasps.

Last, we present a heuristic method to rank the grasp candidates. The score of each grasp is computed as:

$$s = \tanh(w^b \cdot b) \cdot \tanh(w^h \cdot h),$$  \hfill (8)

where $b = 5$ cm is the shortest distance between the gripper to the scene points apart from the target region, $h = 3$ cm is the maximum height of scene points inside the gripper in the gripper coordinate, $w^b$ and $w^h$ are hyperparameters. For each object, the detected grasp with the highest score is selected as the optimal grasp.

**G. Implementations**

**Network architecture, parameters:** The number of input points is 1,500. The PointNet++ backbone contains 4 set abstraction layers, each with a PIFT module inserted in front of it, and 4 feature propagation layers. The weights of network training are $w_f = 1$, $w^a = 1$, $w^s = 5$, $w^c = 1$ and $w^r = 5$. The MLPs for symmetry and grasp predictions contain four fully-connected layers. We use Adam optimizer with an initial learning rate of 0.001 which is decreased by 0.9 for every 2 epoch. The batch size is set to be 36 on an NVIDIA Tesla V100 GPU. The training takes about 36 hours to be converged. The inference time is about 0.3 seconds. The hyperparameters in grasp selection are $w^b = 1$ and $w^h = 5$.

**Symmetry annotation generation:** We first detect the ground-truth symmetry in the canonical coordinate system by the method in [32] and then transfer it into the camera coordinate by using the 6D object pose.

**Grasp affordance annotation refinement:** Existing high-DoF grasp detection annotations are mostly generated by the sample-and-validate methods [22]. It requires expensive computational costs and is prohibitive to be scaled up. To improve the quality and increase the quantity of the training data, we propose a symmetry-guided grasp affordance annotation enhancement. As shown in Fig. 6, we augment the existing grasp detection dataset [9] by two strategies. First, for objects with reflectional symmetries, we refine the grasps by symmetrizing them. Second, for objects with rotational symmetries, we rotate the object and thus duplicate the grasps. These procedures are simple and effective, facilitating more stable network training via resolving the symmetry ambiguity caused by insufficient grasp sampling during the sample-and-validate process.

**IV. RESULTS AND EVALUATION**

In this section, we provide details about our experiment setup, results, and evaluations.
A. Datasets & Evaluation Metrics

To evaluate the performance of the proposed method, we conduct experiments on both the existing dataset and a real robot grasping platform. First, we evaluate our method on the large-scale GraspNet-1-Billion dataset [9]. The dataset contains 97,280 RGB-D images from 190 scenes with 88 objects including symmetric objects, such as plier and bottle, as well as non-symmetric objects, such as the printed 3D model of animals. Second, we conduct experiments on a real robot grasping platform (Fig. 8). The platform contains a UR-5 robot arm with an RG-2 gripper. A realsense camera is on the table to capture the RGB-D images.

We adopt the following evaluation metrics: 1) Grasp Quality: An analytic computation method [18] is adopted to compute whether a grasp is plausible, given a friction coefficient. By altering the friction coefficient from (0,1], we obtain the smallest friction coefficient $\mu$ on which the object could be grasped. The grasp quality is then computed as $1 - \mu$. 2) Antipodal Score: A simple force closure property of grasps that measures the angle between the normal of the contact points and the line connecting two contact points [28]. The metric is computationally lightweight, which could be applied to real-time grasp evaluation. 3) Success Rate: The percentage of objects being successfully grasped by the robot arm. The metric is straightforward and intuitive. It is also sensitive to the gripper type in the robot arm. Since the output of our method is the most confident grasp on each object which is different to the problem of detecting all the possible grasps, we did not use the AP metrics [9].

B. Performance on GraspNet-1-Billion

We first compare our method against several baselines on GraspNet-1-Billion. The baselines are selected: 1) Multi-Grasp [4]: A baseline that generates multiple planar grasps in a single shot with a deep neural network. 2) GG-CNN [24]: A baseline that first estimates pixel-level dense grasp affordances and then generates planar grasps with real-time performance. 3) PointNetGPD [18]: The state-of-the-art two-stages 6D grasp detection approach. It first generates grasp candidates with heuristic rules and then adopts a PointNet to evaluate the quality of the candidates. 4) GraspNet [9]: The state-of-the-art 6D grasp detection approach. It generates multiple grasps by a one-stage neural network. All the baselines were trained on GraspNet-1-Billion. While the first two were trained on the planar grasp annotations, the rest were trained on the 6D grasp annotations.

Quantitative Results: We make quantitative comparisons in two evaluation metrics. The results are shown in Table I and Table II, respectively. There are several interesting phenomena we can observe. First, 6D grasp detection approaches are generally better than the planar ones, demonstrating the problem of grasp detection in this dataset is non-trivial. Second, SymmetryGrasp produces the state-of-the-art performance in terms of Grasp Quality on all test sets. This demonstrates its effectiveness and generality. Third, the high Antipodal Score of our method indicates that it is able to produce more stable grasps, implying symmetry is indeed helpful.

Qualitative Results: The qualitative results are visualized in Fig. 7. It is shown that SymmetryGrasp successfully detects grasps in various scenes. In particular, it produces high-quality grasps on symmetric regions of objects with complex geometry and heavy occlusion.

C. Performance on Real Robot Platform

We also evaluate our method on the real robot platform. For each scene, we use the proposed method to predict the grasps. Then, the robot arm is deployed to perform the grasp with the highest confidence. The task is challenging, as the experimental scenes might contain severe occlusion, various camera viewpoints, and unseen objects. To better reveal the advantages of our method, we divide the objects into several subsets according to their symmetry types: reflection, rotation, sphere, and no-symmetry. Each subset contains 5 objects in various poses with 100 RGB-D images in total being collected. We perform one grasp attempt on each image being collected. In total, there are 400 grasps on all four test subsets. The quantitative comparison is reported in Table III. Note that all methods are trained on GraspNet-1-Billion without any fine-tuning. Our method achieves the best overall performance, providing a more robust solution. The inferior performance of our method on non-symmetric objects reveals the limitation of our method, i.e., it can hardly estimate the contact points on non-symmetric objects with neither global nor local symmetry.
Fig. 7. Visualization of the detected grasps in cluttered scenes. Our method is able to produce high-quality grasps on objects with complex geometry and heavy occlusion, thanks to the guidance of symmetry estimation.

Fig. 8. Left: the experimental robotic grasping platform. Right: the representative objects used in the experiment.

### TABLE IV

**Ablation Studies**. The experiments are conducted on GraspNet-1-Billion. The metric is Grasp Quality.

| Method                             | Seen  | Unseen |
|-----------------------------------|-------|--------|
| No PIFT                           | 0.337 | 0.092  |
| No Siamese Training               | 0.364 | 0.148  |
| No symmetric region segmentation  | 0.350 | 0.257  |
| No dataset enhancement            | 0.355 | 0.240  |
| Full method                       | **0.382** | **0.297** |

**D. Ablation Studies**

We conduct several ablation studies to quantify the efficacy of the crucial components. The experimental dataset is GraspNet-1-Billion. Results are reported in Table IV.

**No PIFT**: We remove the principal-directional scale-invariant feature transformer and retrain the network. This baseline achieves competitive performance compared to the full method on the seen objects, but shows inferiority on the unseen objects. This verifies the need for this component.

**No Siamese Training**: We turn off the feature consistency loss so there is no Siamese network training component. This baseline learns to estimate symmetry from the initial points and the augmented points separately. Results show the Siamese training scheme is crucial.

**No Symmetric Region Segmentation**: We conduct an experiment that was only trained to detect and grasp the globally non-symmetric objects. This leads to a slight drop in performance, due to the incapacity of grasping objects, such as the printed 3D models of the animals.

**No Dataset Refinement**: The affordance annotations are optimized by our refinement procedure. We found that without it, the network training tends to be less efficient and the overall performance declines. This is due to the ambiguous affordances caused by insufficient grasp generation sampling.

**E. Evaluation on Symmetry Estimation**

Symmetry estimation is at the core of our method design. To better illustrate how the estimated symmetry facilities grasp detection, we directly evaluate our symmetry estimation module. We unitize the pre-trained model on GraspNet-1-Billion to estimate symmetries and evaluate the performance on its test sets. The evaluation method is the average precision [32]. For reflectional symmetry and rotational symmetry, we use the dense symmetry error [32] to determine whether the prediction is true positive. For spherical symmetry, we regard the predictions whose Euclidean distance error is smaller than 5 cm as true positives. The experiments report the average precision of symmetry estimation at 0.56, 0.61, and 0.73 for the reflection, rotation, and sphere, respectively, on the test set. As comparisons, the state-of-the-art learning-based symmetry detection method [32] achieves 0.39, 0.32, and 0.58, respectively. The recent geometry-based symmetry detection method [7] achieves 0.17, 0.08, and 0.34 respectively. It shows that our method outperform the baselines and is able to accurately detect most of the symmetries despite the shape variations, thanks to the proposed PIFT module.

**V. Conclusion**

We presented SymmetryGrasp, a learning-based method that detects antipodal grasps from single-view RGB-D images with the guidance of symmetries estimation. We found that grasp detection could greatly benefit from symmetry estimation. In particular, a principal-directional scale-invariant feature transformer is proposed to increase the performance of grasping unseen objects. An interesting future direction is to explore the equivariant networks [6], [37] to enhance the proposed method. We would also like to exploit symmetry in other robotic manipulation tasks, such as object assembling.
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