Opacity Effects on Pulsations of Main-Sequence A-Type Stars

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Abstract: Opacity enhancements for stellar interior conditions have been explored to explain observed pulsation frequencies and to extend the pulsation instability region for B-type main-sequence variable stars [see, e.g., 1–6]. For these stars, the pulsations are driven in the region of the opacity bump of Fe-group elements at \( \sim 200,000 \) K in the stellar envelope. Here we explore effects of opacity enhancements for the somewhat cooler main-sequence A-type stars, in which \( p \)-mode pulsations are driven instead in the second helium ionization region at \( \sim 50,000 \) K. We compare models using the new LANL OPLIB [7] vs. LLNL OPAL [8] opacities for the AGSS09 [9] solar mixture. For models of 2 solar masses and effective temperature 7600 K, opacity enhancements have only a mild effect on pulsations, shifting mode frequencies and/or slightly changing kinetic-energy growth rates. Increased opacity near the bump at 200,000 K can induce convection that may alter composition gradients created by diffusive settling and radiative levitation. Opacity increases around the hydrogen and 1st He ionization region (13,000 K) can cause additional higher-frequency \( p \) modes to be excited, raising the possibility that improved treatment of these layers may result in prediction of new modes that could be tested by observations. New or wider convective zones and higher convective velocities produced by opacity increases could also affect angular momentum transport during evolution. More work needs to be done to quantify the effects of opacity on the boundaries of the pulsation instability regions for A-type stars.

Keywords: stars: pulsation; stars: evolution; opacities

1. Introduction

Opacities, element abundances, and convection affect pulsation instabilities in nearly all types of stars. Studies of pulsating B-type stars, namely the \( \beta \) Cep pressure-mode pulsators, SPB (Slowly Pulsating B) gravity-mode pulsators, and their hybrids that pulsate in both types of modes, have motivated opacity investigations. For these stars, pulsations are driven by the \( \kappa \) (opacity valving) mechanism [10] in the stellar envelope around 200,000 K, where the opacity is increased by bound-bound transitions in Fe-group elements (the so-called Z-bump). SPB/\( \beta \) Cep stars show fewer modes than expected, and hybrids that are not predicted [see, e.g., 11, re. \( \nu \) Eri and 12 Lac]. Increasing the Fe/Ni opacities by a factor of 1.75, as inferred from Sandia pulsed-power experimental data [12], widens the hybrid instability region enough to include 12 Lac [4]. Opacity modifications improve the match to pulsation observations for \( \nu \) Eri [3]. The SPB and \( \beta \) Cep pulsation-instability regions are somewhat wider [1] using the new Los Alamos OPLIB [7] opacities.

The “solar abundance problem” also motivates opacity increases. Standard solar models using the latest abundance determinations and taking into account uncertainties in input physics show disagreement between the sound speed inferred from solar \( p \) modes and that of the standard model [13]. The sound-speed discrepancy becomes slightly smaller using the new LANL OPLIB opacities instead of the LLNL OPAL opacities [7,14]. Inversions for solar entropy [15] and the Ledoux discriminant [16] give additional constraints on the solar interior, highlighting further the effects of opacity differences between OPAL and OPLIB.
For A-type stars, namely the δ Sct variables, $p$-mode pulsations are driven by the $\kappa$ effect produced by the 2nd ionization of helium around 50,000 K. Balona et al. [17] carried out an extensive parameter study to search for pulsation instability of low-frequency modes that are found in many δ Sct variables observed by the Kepler spacecraft. They varied mass, helium abundance, metallicity, rotation rate, and considered OPAL vs. OP [18] opacities. They also consider opacity enhancements around the Z-bump (log $T = 5.35$, or $T = 224,000$ K), and at the so-called “Kurucz bump” at log $T = 5.06$ (T = 114,800 K), first noted in opacities developed for model atmospheres [19] and discussed by Cugier [5] for B-type star pulsations. Balona et al. [17] find that an opacity enhancement of at least a factor of two at the Kurucz bump is needed to excite low-frequency modes; however, they do not advocate such an opacity enhancement as the explanation for the low frequencies observed in δ Sct stars.

Daszyńska-Daszkiewicz et al. [20] explored the effects of opacity enhancements to explain the 16 to 115 $\mu$Hz variability of the rapidly rotating Maia variables, with spectral types B8 to A2, between the δ Sct and SPB variables. They explored opacity enhancements for 2.5-3.2 M$_{\odot}$ rotating models, finding that a factor of 1.5 enhancement around log $T = 5.1$ (T = 126,000 K), near the Kurucz bump, produces pulsation instability in the observed frequency range.

Here we further explore the consequences of opacities and opacity enhancements for A-type stars. We compare 2 M$_{\odot}$ evolution and pulsation models using the new LANL OPLIB vs. the LLNL OPAL opacities. We examine the effects of opacity multipliers in the region of bumps at 15,000, 50,000, and 2.6 million K, in addition to the Z-bump region around 200,000 K. We use different stellar evolution and pulsation codes than those used in previous studies. We show the effects of opacity enhancements on inducing and widening convection zones and increasing convective velocities, in the context of the mixing-length theory of convection [21]. We estimates the effects of turbulent broadening on line opacities that could contribute to opacity enhancements.

2. Stellar Evolution and Pulsation Models

We use as our testbed for opacity studies the evolution of 2 M$_{\odot}$ models with OPAL [8] and OPLIB opacities [7], and the AGSS09 [9] solar abundance mixture. See [14] and references therein for details of the stellar evolution and nonadiabatic pulsation codes used for these studies. We used mixing-length to pressure scale-height ratio 2.0 and did not include convective overshoot or rotation in our models.

2.1. LLNL OPAL vs. LANL OPLIB opacities

We first examine the difference in evolution track in the Hertzsprung-Russell (H-R) diagram (log luminosity vs. log effective temperature) and the calculated frequencies and growth rates of degree $l=0-2$ $p$ modes for $T_{\text{eff}} = 7600$ K models using OPAL vs. OPLIB opacities (Fig. 1). The 2 M$_{\odot}$ model using OPAL opacities evolves at slightly higher luminosity for the same effective temperature. We found slightly higher growth rates at for the $l=0-2$ $p$ modes using the OPLIB opacities.

2.2. ×2 Z-bump at 200,000 K

We next explored how the evolution and $p$-mode pulsation predictions change when Z-bump opacities are increased. Note that the $\kappa$ mechanism in the 2nd He ionization region ∼50,000 K drives $p$-mode pulsations in δ Sct stars, so the Z-bump at ∼200,000 K should not have a large effect on the δ Sct $p$ modes. We modified the opacity by multiplying by a Gaussian function peaking at ×2 at 200,000 K (Fig. 2, left). This Z-bump opacity increase has almost no effect on the 2 M$_{\odot}$ evolution track. The Z-bump ×2 opacity increase also has almost no effect on $l=1$ $p$-mode pulsations; the growth rates are slightly lower for some modes. However, the Z-bump opacity increase induces a small convection zone in these models near 200,000 K (Fig. 3). In the Z-bump region, the convective velocities are $10^5$ cm/s, and convection carries only 10% of the luminosity.
Figure 1. Evolution tracks in H-R diagram for 2 M$_\odot$ models with OPAL and OPLIB opacities (left); fractional kinetic-energy growth rate per period (dimensionless) vs. frequency for $l=0$, 1, and 2 $p$ modes for T$_{\text{eff}} = 7600$ K models (right). The Xs mark the model locations on the H-R diagram.

Figure 2. Opacity vs. stellar interior temperature for 2 M$_\odot$ models with T$_{\text{eff}} = 7600$ K, showing modification of the Z-bump opacity at 200,000 K (left) and of the 2nd He ionization region opacity at 50,000 K (right).

Figure 3. Convective velocity (left) and fraction of luminosity carried by radiation (right) vs. temperature for 2 M$_\odot$ models with T$_{\text{eff}} = 7600$ K, with and without $\times 2$ and $\times 5$ opacity increases in the Z-bump region.
Figure 4. Evolution tracks for 2 $M_\odot$ models with and without $\times 2$ opacity increase in He+ ionization region at 50,000 K (left); fractional kinetic-energy growth rate per period (dimensionless) vs. frequency for $l=0$, 1, and 2 $p$ modes of 2 $M_\odot$ $T_{\text{eff}} = 7600$ K models with and without opacity enhancements in the He+ ionization region (left).

2.3. $\times 2$ He+ Ionization bump at 50,000 K

Could neglected line broadening be responsible for too-low stellar opacities? Turbulence and convection not taken into account in opacity simulations could broaden lines and features. We present estimates of the magnitude of this effect in Section 4 below. It is also possible that photo-excitation processes (Stark line widths) may not be calculated properly in opacity simulations [22]. However, Krief et al. [22] note that a factor of 100 increase in all line widths would be needed to account for missing solar opacity.

What are the consequences for pulsations of A-type stars of an opacity increase in the 2nd He ionization region where $\delta$ Sct $p$ modes are driven? This opacity bump is produced by ionization, rather than by line excitation; therefore the opacity modification may be more correctly referred to as ‘edge broadening’ or ‘edge blending’. Unlike the Z-bump region around 200,000 K, the 2nd He ionization region in A-type stars responsible for $\delta$ Sct pulsations is convective/turbulent, even without opacity enhancements (Fig. 5).

We multiplied the opacity by a Gaussian function peaking at $\times 2$ in the 2nd He ionization region centered at 50,000 K (Fig. 2, right). We find that this He+ ionization region opacity increase has very little effect on the 2 $M_\odot$ evolution track in the H-R diagram (Fig. 4, left). Increased He+ opacity shifts the unstable $l=0$-$2$ $p$-mode frequency range to lower frequencies and also reduces the growth rates (Fig. 4, right). Increased He+ opacity causes more luminosity to be carried by convection, weakening the $\kappa$-effect pulsation driving. With the opacity increase, convective velocities become larger by a factor of two, as high as $4 \times 10^5$ cm/s. Convection then carries 25% of the luminosity, instead of 10% (Fig. 5).

2.4. $\times 5$ Z-bump at 200,000 K

If enhanced opacities cause a small convection zone to develop in the Z-bump region for A-type stars, convection could also cause line broadening that would further increase opacities. The combination of diffusive settling and radiative levitation can concentrate Fe in the envelope at $\sim 200,000$ K, and may also cause a Z-bump convection zone to develop for A-type stars [see, e.g., 23,24].

We multiplied the opacities by a Gaussian function peaking at $\times 5$ for the Z-bump region centered at 200,000 K. The $\times 5$ Z-bump opacity increase has almost no effect on the 2 $M_\odot$ evolution track in the H-R diagram (Fig. 6, left). However, the $\times 5$ Z-bump opacity increase induces a wide convection zone at $\sim 200,000$ K, and convective velocities $\sim 2 \times 10^5$ cm/s, with convection carrying almost 60% of the
Figure 5. Convective velocity (left) and fraction of luminosity carried by radiation (right) vs. temperature for 2 M\(_\odot\) models with T\(_{\text{eff}}\) = 7600 K, with and without \times 2 opacity increase in the He\(^{+}\) ionization region.

luminosity (Fig. 3). The Z-bump \times 5 opacity increase has almost no effect on \(l=0\)-2 \(p\)-mode pulsations; growth rates become slightly lower for some modes (Fig. 6, right).

Long time-series high-precision photometry has revealed low-frequency \(g\)-mode pulsations among many A-type and \(\delta\) Scuti variables that were not predicted by theoretical models [25–27]. \(g\)-mode pulsations are observed for cooler late-A to F-type \(\gamma\) Doradus variable stars, and explained by the convective-blocking mechanism [28] operating at the base of the deeper convective envelope that is not present in early A-type stars. We were hoping that the new convection zone induced by opacity enhancements in the Z-bump region might cause \(g\)-mode pulsation driving via the convective-blocking mechanism. However, we find that for 2 M\(_\odot\) T\(_{\text{eff}}\) = 7600 K models, the \times 5 Z-bump enhancement does not affect low-order \(l=1\) or 2 \(g\)-mode stability; the low-order \(g\) modes have slightly less negative growth rates, but are still stable (Fig. 7, left). One or two of the highest frequency \(l=2\) \(g\) modes become unstable for cooler (T\(_{\text{eff}}\) = 7245 K) models, even without an opacity enhancement (Fig. 7, right). The growth rates become lower with the \times 5 Z-bump increase, likely because these modes are actually driven by the \(\kappa\) effect (and not the convective-blocking mechanism) that is weakened by convection.

We also calculated frequencies for a 2 M\(_\odot\) model closer to the blue edge of the instability region at T\(_{\text{eff}}\) = 8318 K. For this T\(_{\text{eff}}\), there are only three unstable \(p\) modes at frequencies 420-580 \(\mu\)Hz for each degree \(l=0, 1,\) and 2 with the \times 5 Z-bump enhancement. There are the same number of unstable modes for the comparable model with no Z-bump enhancement, with the exception of a fourth unstable mode for \(l=0\). Again, we do not find any unstable \(g\) modes. Note that [17] conclude that it is possible to create \(g\)-mode instability with a Z-bump enhancement of at least \times 3, based on results from their more extensive parameter study.

Daszyńska-Daszkiewicz et al. [3] investigate enhanced opacities for B-type stars at somewhat higher interior temperature, log T = 5.46, or T = 288,400 K, corresponding to the region of maximum contribution of nickel to the opacity. Because lower-frequency \(g\)-mode pulsations that have also been seen in many A-type stars are driven most effectively at temperature of about 350,000 K in the cooler, less massive \(\gamma\) Dor variables [28], we also explored a \times 2 opacity bump at 350,000 K. However, introducing additional opacity at this temperature, unlike for the 200,000 K Z-bump region, did not induce a new convective region, or significantly change the evolution or \(p\)-mode frequencies, or result in driving of \(g\)-mode pulsations.

Would higher opacities that extend a convective region or induce a new convective region have observable signatures? Deal et al. [29,30] discuss the effects of molecular-weight gradient instabilities and “fingering convection” induced by localized element accumulation via diffusive
Figure 6. Evolution tracks for 2 $M_\odot$ models with and without $\times 5$ opacity increase in Z-bump region (left); fractional kinetic-energy growth rate per period (dimensionless) vs. frequency for $l=0$, 1, and 2 $p$ modes of 2 $M_\odot$ $T_{\text{eff}} = 7600$ K models with and without $\times 5$ opacity enhancement in the Z-bump region (right).

Figure 7. Fractional kinetic-energy growth rate per period (dimensionless) vs. frequency for $l=2$ $g$ modes for models with and without $\times 5$ Z-bump for $T_{\text{eff}} = 7600$ K (left) and 7245 K (right).
settling and radiative levitation on the evolution and surface abundances of $\delta$ Sct stars. They find that surface abundances of C, N, O, Ne, Mg, Ca and Fe can be altered if fingering convection connects the surface convective layers to deeper layers. A transition from a radiative to convective region at the Z-bump location could also have a signature in asteroseismic inversions for example, on the inferred sound-speed gradient. Fig. 8 compares the radial derivative of the squared sound speed vs. temperature for models with and without the $\times 5$ Z-bump enhancement. High precision observations of $\delta$ Sct variables showing many $p$ modes of several angular degrees may be amenable to inversion techniques that could detect changes in the sound-speed gradient.

2.5. $\times 1.5$ opacity bump at 2.6 million K

In addition to an opacity enhancement at the Z-bump, Zdravkov and Pamyatnykh [6] advocate a 16% opacity increase near a deeper bump around 2 million K to improve agreement with pulsation observations for hybrid $\beta$ Cep/SPB star $\gamma$ Peg. In our cooler A-type stars, this deeper bump occurs around 2.6 million K. We introduced a 50% opacity enhancement peaking at 2.6 million K (Fig. 9, left) for the 2 $M_\odot$ evolution models. This relatively deep opacity enhancement has a more substantial effect on the 2 $M_\odot$ evolution track in the H-R diagram, causing the model to evolve at cooler temperatures and slightly lower luminosity (Fig. 9, right). However, the effects on $l=1$ $p$-mode pulsations (Fig. 10, left) and $l=2$ $g$-mode pulsations (Fig. 10, right) for $T_{\text{eff}} = 7600$ K models are again very small.

2.6. $\times 2$ bump at 13,000 K in H and 1st He ionization region

It is also possible that turbulence could increase opacity in the H and 1st He ionization region around 13,000 K. In this region there is a high convective velocity, $\sim 2 \times 10^6$ cm/s, and convection carries over 90% of the luminosity (Fig. 5). Turbulent pressure (and its perturbation) in the H-ionization zone has been proposed as a mechanism to drive coherent modes in A-type stars [31], as seen in, e.g., HD 187547 observed by the Kepler spacecraft. Stochastically excited solar-like $p$ modes were also anticipated for $\delta$ Sct stars [32].

We multiplied the opacity bump in this region by a Gaussian function peaking at $\times 2$ centered at 13,000 K (Fig. 11, left). This opacity enhancement has almost no effect on the evolution track in the H-R diagram. The opacity enhancement only slightly increases the convective velocity (Fig. 12, left) and widens the convective region (Fig. 12, right). However, the enhanced opacity results in predicted driving of additional $p$ modes at higher frequencies (Fig. 11, right). This pulsation driving prediction is not reliable because of the frozen-in convection treatment of our pulsation modeling.
Figure 9. Opacity vs. stellar interior temperature for 2 M$_\odot$ models with T$_{\text{eff}}$ = 7600 K, showing opacity multiplied by Gaussian function centered at 2.6 million K with $\times1.5$ peak (left); evolution track in H-R diagram for 2 M$_\odot$ models with and without opacity modification (right). The Xs mark the T$_{\text{eff}}$ = 7600 K model positions on the evolution tracks.

Figure 10. Fractional kinetic-energy growth rate per period (dimensionless) vs. frequency for $l=1$ $p$ modes (left) and $l=2$ $g$ modes (right) for T$_{\text{eff}}$ = 7600 K models with and without $\times1.5$ opacity enhancement at 2.6 million K.
Figure 11. Opacity vs. interior temperature for 2 $\text{M}_\odot$ models with $T_{\text{eff}} = 7600$ K, showing modification of the hydrogen and 1st He ionization opacity bump at 13,000 K (left); fractional kinetic-energy growth rate per period (dimensionless) vs. frequency for $l=1$ $p$ modes for $T_{\text{eff}} = 7600$ K models (right).

Figure 12. Convective velocity (left) and fraction of luminosity carried by radiation (right) vs. temperature for 2 $\text{M}_\odot$ models with $T_{\text{eff}} = 7600$ K, with and without $\times2$ opacity increase in the hydrogen and first He ionization region.

code. However, the appearance of additional $p$ modes suggests that improved treatments of the surface layers, including treatments of turbulent pressure and time-dependent convection, along with opacities, may help to explain unexpected pulsation modes found in A-type stars. Observations and characterization of higher-frequency modes in $\delta$ Scut stars would be useful to help constrain the many physical processes in the near-surface layers of these stars, including diffusive settling and levitation, development of peculiar chemical abundances, flares and magnetic activity, extent of convection zones and convective overshoot, turbulent pressure, opacities, mechanisms for mode selection and regulating mode amplitudes, and would provide additional asteroseismic constraints for inversions.

3. Summary of opacity and model parameters

Table 1 summarizes the opacity multipliers used for the evolution models discussed in this paper, as well as the core hydrogen mass fraction and age for the $T_{\text{eff}} = 7600$ K models. The opacity multipliers have the form:

$$\kappa = \kappa_0 (1.0 + M e^{-[(T-T_c)/W]^2})$$  \hspace{1cm} (1)
where $T_c$ is the center of the opacity bump, and $W$ is the width parameter. We chose the width so that the bump enhancement would smoothly disappear at the edge of the original bump. We did not explore the effects of variations of the bump width. Larger widths could enhance the effects, but are perhaps unrealistic as there are no obvious atomic processes outside the bump regions to motivate opacity enhancements.

In general, for fixed 7600 K effective temperature, the core hydrogen mass fraction becomes larger and ages decrease when opacities are increased in the deepest layers.

Table 1. Opacity bump multiplier parameters, core hydrogen mass fraction and age for 2 M$_\odot$ main-sequence models with $T_{\text{eff}} = 7600$ K.

| Model          | Bump Coefficient $M$ | Bump Center $T_c$ (K) | Bump Width Parameter $W$ (K) | Core H Fraction | Age (Myr) |
|----------------|----------------------|-----------------------|-----------------------------|-----------------|-----------|
| OPAL           | —                    | —                     | —                           | 0.2075          | 788.4     |
| OPLIB          | —                    | —                     | —                           | 0.2085          | 767.7     |
| $\times 2$ Hy bump | 1                   | 13,000                | 8,000                       | 0.2082          | 767.4     |
| $\times 2$ He+ bump | 1                   | 50,000                | 12,000                      | 0.1997          | 777.1     |
| $\times 2$ Z-bump | 1                   | 200,000               | 30,000                      | 0.2097          | 766.2     |
| $\times 5$ Z-bump | 4                   | 200,000               | 30,000                      | 0.2027          | 773.6     |
| $\times 2$ deeper bump | 1                   | 350,000               | 30,000                      | 0.2103          | 765.8     |
| $\times 1.5$ deep bump | 0.5                 | $2.6 \times 10^6$    | 875,000                     | 0.2536          | 720.8     |

4. Turbulent broadening estimates

As alluded to throughout this paper, the problem with invoking turbulent broadening to enhance opacities for stellar pulsation studies is that many types of pulsations are driven by the $\kappa$ (opacity valving) mechanism, which requires radiation instead of convection to transport the luminosity in the layer of interest. However, turbulence/convection must transport at least some of the luminosity in the pulsation driving layer in order for turbulent broadening to affect the opacity.

We carried out some preliminary calculations of the effects of turbulent broadening on Rosseland mean opacity in the region of the Z-bump produced by bound-bound transitions of Fe-group elements in A and B-type main-sequence stars. For the solar abundance mixture, turbulent velocity $4 \times 10^5$ cm/s, temperatures 15 to 20 eV (175,000 - 232,000 K), and densities $4.6 \times 10^{-6}$ to $8.0 \times 10^{-6}$ g/cm$^3$, the Rosseland mean opacity increases by only 0.6%, far from the factors of nearly two proposed to solve some problems with B-type star pulsations. However, if the Fe abundance is enhanced at these temperatures because of diffusive element settling and radiative levitation, the opacity increases could be larger.

We estimate the increase in Doppler broadened line widths taking into account turbulent line broadening for a Fe line in the Z-bump region of the stellar interior. The thermal width is given by the standard formula:

$$W_{\text{thermal}} = \sqrt{2kT/Mc^2} f_0$$  \hspace{1cm} (2)

where $T$ is temperature, $k$ is Boltzmann’s constant, $M$ is the atomic mass of the element, $c$ is the speed of light, and $f_0$ is the frequency of the line center of interest. The turbulent width is given by the formula:

$$W_{\text{turb}} = \left( \frac{v_{\text{turb}}}{c} \right) f_0$$  \hspace{1cm} (3)

where $v_{\text{turb}}$ is the turbulent velocity and $c$ is the speed of light. To obtain the Doppler width, these two terms are added in quadrature:

$$W_{\text{Doppler}} = \sqrt{W_{\text{thermal}}^2 + W_{\text{turb}}^2}$$  \hspace{1cm} (4)
Using $k = 8.617 \times 10^{-5} \text{eV/K}$, $T = 200,000 \text{K}$, $v_{\text{turb}} = 4 \times 10^5 \text{cm/s}$, Fe atomic mass 56, mass per nucleon $931.5 \times 10^6 \text{eV/c}^2$, and speed of light $3 \times 10^{10} \text{cm/s}$,

$$W_{\text{thermal}} = 2.571 \times 10^{-5} f_0 \quad (5)$$

$$W_{\text{turb}} = 1.333 \times 10^{-5} f_0 \quad (6)$$

$$W_{\text{Doppler}} = 2.896 \times 10^{-5} f_0 \quad (7)$$

Therefore turbulent broadening would produce a 13% increase in the Doppler width of a given Fe line. For the A-type stellar models studied here, a turbulent velocity of $4 \times 10^5 \text{cm/s}$ is already twice as high as the turbulent velocity produced in the Z-bump region with a $\times 5$ opacity enhancement. For a smaller turbulent velocity of $2 \times 10^5 \text{cm/s}$, the Doppler width is increased by only 3%. These turbulent velocities are calculated by mixing-length theory, with a mixing-length to pressure scale height ratio of 2.0. A more sophisticated treatment of turbulence and multidimensional models would show a distribution of turbulent velocities, with significantly higher local velocities.

Other elements in the abundance mixture that contribute to opacity in stellar radiative interiors, e.g., C, N, O, and Ne, are more abundant, but are significantly lighter than Fe. Therefore, the enhancement due to turbulence is expected to be less because of the $1/\sqrt{M}$ dependence in the thermal broadening versus the constant value of $v_{\text{turb}}$ for all elements.

This estimate does not directly indicate the corresponding expected increase in Rosseland mean opacity for the stellar abundance mixture, of which Fe is only one element. Detailed opacity calculations are required, taking into account all of the lines and full abundance mixture under various conditions found in stellar interiors in order to determine whether turbulent broadening can be neglected to a good approximation. We have yet to estimate the potential effects of edge blending on opacity increases for the regions of ionization of H and He, where the turbulent velocities are higher.

5. Conclusions

A-type stars may turn out to be useful testbeds for opacity studies. Opacity increases could cause convection zones to appear or widen, abundance gradients to be altered, instability strip boundaries to change, unstable mode frequency ranges to change, and could affect operation of pulsation driving mechanisms such as the $\kappa$ effect and mechanisms involving pulsation-convection interactions. Although angular momentum transport is not investigated in the 1-D non-rotating evolution models presented here, new or wider convection zones and higher convective velocities produced by opacity enhancements could also affect angular momentum transport during stellar evolution and change interior rotation profiles that may have detectable signatures in pulsation frequency spacings.

The tests presented here show that opacity increases proposed to explain discrepancies with pulsations in B-type stars have a more modest effect on pulsations of A-type stars. With the possible exception of enhancements around the Kurucz bump not explored here, opacity increases do not help to explain the unexpected g-mode pulsations discovered in many A-type stars. However, opacity enhancements in the hydrogen and 1st helium ionization region near the stellar surface may result in driving of additional p modes, confirming that improved treatments of the surface layers may explain the frequency content of A-type stars such as HD 187547 and HR 7284. More work is warranted to explore the effects of opacities and opacity enhancements on the pulsation instability region boundaries for $\delta$ Sct p-mode pulsators.

Convective velocities in pulsation driving layers reach $10^5-10^6 \text{cm/s}$ may produce turbulent line and edge broadening, and therefore may need to be taken into account in opacity calculations. However, our estimates show that Rosseland mean opacity increases, taking into account turbulent broadening, are likely to be modest, only around 1%.
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