Research Article

Quantitative Evaluation for the Threat Degree of a Thermal Reservoir to Deep Coal Mining

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Taking the Suiqi coalfield located in North China as the object, where the coal seam burial depth is more than 1100 m, the water abundance of the roof pore thermal storage aquifer is better than average, the ground temperature is abnormally high, and hydrogeological data are relatively lacking, this paper selects and determines eight index factors that influence the mining of the coalfield. Based on the analytic hierarchy process (AHP), the index factor weight is defined, and then, the threat degree of the roof thermal storage aquifer to the coal mining is quantitatively evaluated and divided by using the fuzzy variable set theory. The evaluation results show that the threat degree of the roof in the eastern region is generally greater than that in the western region and that the closer it is to the coal seam outcrop line, the higher the threat degree is; near the boreholes, in the areas Qs1, Qs5, Qs8, Sx1, Tk5, Zc4, and Zc7, which are close to the hidden outcrop line of the coal seam, the classification characteristic value of the threat degree is greater than 3.5, which is in the high-threat zone for disasters caused by roof thermal storage aquifers during coal seam mining. The area above the medium-threat zone accounts for 71.82% of the total study area, indicating that deep coal mining is affected by multiple factors and that roof water and heat disasters are more likely to occur.

1. Introduction

In North China coalfields and southern Ordos Basin coalfields, minable coal seams are directly or indirectly covered by thermal storage aquifers of different thicknesses and coal seam mining operations face the serious threats of double roof water inrush and geothermal disasters. For example, the normal water inflow of a coal mine in the southern margin of the Ordos Basin reaches 106,520 m³/d and the water temperature at a depth of 700 m reaches 41°C, which greatly affect the normal production of the coal mine. To ensure the safety of underground mining engineering, the threat degree of the roof thermal storage aquifer has become an urgent problem that needs to be solved in coal mine production through scientific evaluation.

Many scholars have carried out a series of research works on the problem of coal seam roof disasters. The theories and methods formed mainly include the “upper three zones” theory [1–3], the “key layer” theory [4], the “three maps-double prediction method” [5], the mathematical comprehensive evaluation method [6], and the numerical simulation method [7]. Among them, the “upper three zones” theory is the most widely used, and the corresponding empirical formula calculation guides the prediction, evaluation, and prevention of a coal seam roof water inrush [8, 9]. In recent years, some scholars have used comprehensive methods to solve practical production problems. For example, Booth and Breuer and Wu et al. applied MODFLOW software to simulate the hydrological effects of shallow aquifers under the influence of long-wall mining, put forward the change rule of
hydrological parameters, such as the water head with the mining time and space, and hypothesized that the cracks produced during mining caused the water head drop of the aquifer system [10, 11]. Zhou et al. established a conceptual model of mine water inrush composed of a core network, an underground monitoring network, and an operating system, and the underground excavation and water inrush disaster process can be simulated by using the raw underground data [12]. Zhang et al. obtained the height of the “upper three zones” by numerical simulation and used it to study the roof overburden failure [13]. Yang and Sun determined the height of the water flowing through the fractured zone by using a field measurement, numerical simulation, and empirical formulas in the “upper three zones” theory to reasonably determine the size of a waterproof safety coal pillar [14]. Yao et al. used numerical simulation software to simulate the distribution characteristics of the water flowing fracture zone and the seepage characteristics of the roof water during the mining of the workplace; additionally, the water inrush risk of the roof aquifer was analyzed [15]. Based on the gray correlation analytic hierarchy process, Zhang and Yang proposed a prediction model for the roof water inrush when mining a shallow coal seam, and the model was verified with engineering examples [16]. Wu et al. and Zeng et al. studied the height of the water flowing fracture zone of the coal seam roof and the richness of the water-rich aquifer and then evaluated the water inrush risk of the aquifer according to the water-rich partition map [17, 18]. Ren and Wu revised the “three figure double prediction method” and evaluated the risk of water inrush in the area where the height of the caving zone formed by coal mining is lower than the elevation of the roof aquifer [19]. Rezaei and Guo et al. used a neural network intelligent prediction model to determine the height of the water flowing fracture zone and evaluate the performance of the model by using a variety of performance indicators (correlation coefficients, variances, etc.) [20, 21]. Ruan et al. proposed a prediction model for the water inrush based on the AHP and the Dempster-Shafer evidence theory, and the feasibility and applicability of the model were also verified [22].

Obviously, the above research results are mainly focused on the prediction and prevention of roof water disasters, while there are few studies on the evaluation of the threat degree of water hazard under the superimposed effect of high ground temperature. In addition, the existing methods needing to be improved generally predict the possibility of roof water inrush based on stratum lithology and mining influence, which fails to fully reflect the combined effects of multiple factors such as geology, hydrogeology, geothermal field, and mining failure. Therefore, it is of great significance to

**Figure 1: Schematic diagram of the location and geological structure of the Suiqi coalfield.**
carry out research on the threat degree of water-heat coupling disaster under deep coal mining conditions.

In this paper, taking the Suiqi coalfield located in the North China coalfield area as the object, based on the collected and measured geothermal well and exploration borehole data, the key evaluation indicators among factors such as the geology, hydrogeology, geothermal field, and mining failure were selected. Then, based on fractal theory, AHP, and fuzzy variable set theory, a mathematical model is constructed, by which the impact degree of the thermal storage...
2. Geological and Hydrogeological Characteristics

The Suiqi coalfield (Figure 1), which encompasses an area of approximately 4900 km², is located at the junction of Kaifeng City, Shangqiu City, and Zhoukou City in the central part of the North China coalfield area. At a burial depth of 1100–2000 m is the no. 21 coal seam, whose average thickness and coal reserves are 5.3 m and 23 billion tons, respectively. With the gradual depletion of coal resources in other areas, to meet the needs of economic and social development, the mining of coal resources in this coalfield will be imperative.

2.1. Geologic Characteristics. According to the drilling data, the strata overlying the no. 21 coal seam in the coalfield area include the Shanxi Formation (P.sh) and the Lower Shihize Formation (P.x) of the Permian System, the Neogene System (N), and the Quaternary System (Q). The combined geological column of the stratum can be seen in Figure 2.

The geological structure in this area is relatively developed (Figure 1), with Changsi anticline in the north and Taikang syncline in the south. The faults mainly include the Liaocheng-Lankao fault, Suixian fault, Minquan-Yucheng fault, Cuiqiao fault, and other high-angle normal faults. The faults have large drops and extensions, and the occurrence factors are shown in Table 1. These geological structures have destroyed the occurrence of coal seams at different degrees, leading to a lack of coal-bearing strata and changes in the coal thickness.

2.2. Hydrogeological Characteristics. The roof aquifers affect the excavation of the no. 21 coal seam of the sandstone fracture aquifer group of the Shanzhi Formation and Lower Shihize Formation and the pore aquifer group of the Neogene period. The water richness of the sandstone fissure aquifer group in the Shanzhi Formation and the Shihize Formation is relatively weak, and it has little effect on the mining of the no. 21 coal seam in the case of no supply source.

The Neogene aquifer group is mainly composed of a fine sand medium that has good water richness with an average unit water inflow of 0.73 L/(s·m). The aquifer group directly affects the mining of the no. 21 coal seam in the hidden outcrop area of the coal seam and indirectly threatens the mining of the no. 21 coal seam in other areas through the underlying aquifer group.

The geothermal gradient in this area is between 3.35 and 3.81°C/100 m, with an average value of 3.58°C/100 m. The average temperature of the surrounding rock and groundwater at a depth of 1100 m can reach 54.56°C. The coal mining operations will be affected by abnormally high geothermal disasters.

3. Index Factor Selection and Weight Determination

3.1. Index Factor Selection. The threat degree of the roof thermal storage aquifer during mining in the Suiqi coalfield is mainly controlled by the geological, hydrogeological, and geothermal fields; mining failure; and other factors (as shown in Figure 3).

The geological factors include the overburden structure of the coal seam, the rock thickness, the burial depth of the coal seam roof, and the fault characteristics. The roof of the no. 21 coal seam in the coalfield area is an interlayer of brittle sandstone and plastic mudstone. The greater the number of sandstone layers and the greater the thickness of a single layer, the more easily the roof will be damaged under the influence of mining. Therefore, the thickness ratio of the brittle and plastic rock (the ratio of brittle rock thickness to plastic rock thickness) exposed by drilling can be used to characterize the structure and thickness of the coal seam overburden. The deeper the burial depth of the coal seam roof and the thicker the overlying rock layer, the greater the pressure on the roof will be during mining. The more complex the faults of the coal seam roof are, the higher the roof failure height is and the greater the water inrush is. Therefore, the thickness ratio of the brittle and plastic rock, the burial depth of the coal seam roof, and the fault complexity are chosen to reflect the influence of the geological factors in this paper.

The hydrogeological factors include the thickness of the aquifer and the water richness within the height of the “upper three zones” of a roof failure. The greater the thickness and the stronger the water richness, the more water that is provided during the inrush it has and the more harmful it is. The thickness of the aquifer and water richness can be obtained from the drilling and field pumping (injection) water test data. Because the Suiqi coalfield is in the exploration stage, no pumping (injection) water test has been carried out.
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The ground temperature of the Suiqi coal

out at present. In addition, the number of geothermal wells
constructed in the area is limited, and it is difficult to obtain
the unit water inflow, which characterizes the water richness
of the aquifer. In the absence of the unit water inflow, the drill
flushing fluid consumption and core recovery rate can be
used as a substitute measure [23, 24]. The greater the con-
sumption of flushing fluid during drilling construction, the
more developed the pores and cracks in the rock layer are
and the stronger the water richness of the aquifer is.

The ground temperature of the Suiqi coalfield is abnor-
mally high. To directly show the threat of the ground tem-
perature field to deep coal seam mining, the surrounding rock
temperature at the depth of the coal seam roof is used to
indicate its influence. In the Suiqi coalfield, the bedrock
composed of sandstone and mudstone is separated between the
Neogene thermal reservoir aquifer group and the no. 21 coal
seam to be mined. The larger the difference between roof fail-
ure height and the whole thickness of the bedrock during coal

Table 2: Judgment matrix $A - B_i (i = 1, 2, 3)$.

| $A$ | $B_1$ | $B_2$ | $B_3$ | $w(A/B_i)$ |
|-----|-------|-------|-------|-------------|
| $B_1$ | 1     | 8/9   | 7/9   | 0.2925      |
| $B_2$ | 9/8   | 1     | 9/7   | 0.3164      |
| $B_3$ | 9/7   | 9/7   | 1     | 0.3911      |

Note: maximum characteristic value $\lambda_{max} = 3.0016$, CI = 0.0008 < 0.1, and CR = 0.0014 < 0.1.

Table 3: Judgment matrix $B_1 - C_i (i = 1, 2, 3)$.

| $B_1$ | $C_1$ | $C_2$ | $C_3$ | $w(B_1/C_i)$ |
|-------|-------|-------|-------|--------------|
| $C_1$ | 1     | 4/3   | 1/6   | 0.1443       |
| $C_2$ | 3/4   | 1     | 1/5   | 0.1265       |
| $C_3$ | 6     | 5     | 1     | 0.7285       |

Note: maximum characteristic value $\lambda_{max} = 3.0247$, CI = 0.0124 < 0.1, and CR = 0.0213 < 0.1.

Table 4: Judgment matrix $B_2 - C_i (i = 1, 2, 3)$.

| $B_2$ | $C_4$ | $C_5$ | $C_6$ | $w(B_2/C_i)$ |
|-------|-------|-------|-------|--------------|
| $C_4$ | 1     | 6/5   | 3/2   | 0.4000       |
| $C_5$ | 5/6   | 1     | 5/4   | 0.3333       |
| $C_6$ | 2/3   | 4/5   | 1     | 0.2667       |

Note: maximum characteristic value $\lambda_{max} = 3$, CI = 0 < 0.1, and CR = 0 < 0.1.

Table 5: Judgment matrix $B_3 - C_i (i = 1, 2)$.

| $B_3$ | $C_7$ | $C_8$ | $w(B_3/C_i)$ |
|-------|-------|-------|--------------|
| $C_7$ | 1     | 1/3   | 0.2500       |
| $C_8$ | 3     | 1     | 0.7500       |

Note: maximum characteristic value $\lambda_{max} = 2$, CI = 0 < 0.1, and CR = 0 < 0.1.

mining, the higher the influence of the Neogene thermal stor-
age aquifer is on the coal seam mining. Therefore, the differ-
ence between height of the “upper three zones” and the bedrock thickness is chosen to characterize the impact of a
mining failure.

In short, it is reasonable and practical to select the follow-
ing eight elements as index factors to evaluate the threat
degree of the overlying thermal aquifer during coal mining
operations: the thickness ratio of brittle and plastic rock,
the coal seam roof depth, the fault complexity, the aquifer
thickness, the borehole flushing fluid consumption, the core
recovery rate, the surrounding rock temperature, and the dif-
dference between the height of the “upper three zones” and
the bedrock thickness.

According to the water and heat disaster characteristics
of a coal seam roof [1], the difference between the height of
the “upper three zones” and the bedrock thickness and
the complexity of the fault should be the most important
levels among the eight index factors; the aquifer thickness,
borehole flushing fluid consumption, core recovery rate,
and surrounding rock temperature should be at the second most important influence level, while the coal seam roof depth and thickness ratio of brittle and plastic rock have been reflected in other indexes to some extent, and they should be at the third influence level.

3.2. Index Factor Weight. Referring to the existing results [25], the weights of the eight index factors can be determined by AHP. The judgment matrix of the evaluation system composed of the eight index factors is shown in Tables 2–5.

When the AHP model is used to determine the index factor weights, only when it is established that the consistency index CI < 0.1 and the consistency ratio CR < 0.1 can the judgment matrix and the single order of the factors be logically consistent and can the calculation results be credible. Obviously, the results of all the levels in this paper have passed the consistency test, and the determined index factor weights are credible. The results are shown in Table 6.

4. Quantitative Value of Index Factors Divided

4.1. Fault Complexity. The fractal theory can be used to distinguish the complexity of the faults in the study area [26]. According to a certain scale, the study area is into several square blocks, and the blocks containing faults are counted and numbered. For block $i$, first divide it according to the

| Table 6: Weights of the evaluation index factors. |
|--------------------------------------------------|
| **Index factor** | $C_1$ | $C_2$ (m) | $C_3$ | $C_4$ (m) | $C_5$ (m$^3$/h) | $C_6$ | $C_7$ (°C) | $C_8$ |
|--------------------|-------|----------|-------|-----------|----------------|-------|----------|-------|
| Weight             | 0.0422 | 0.0370   | 0.2131| 0.1267    | 0.1055         | 0.0844| 0.0978   | 0.2933|

Figure 4: Block number of the study area.
magnification of scale \( r = 1/2 \), and count the number of block segments containing fault trajectories \( N(1/2) \); further, divide it according to the scale \( r = 1/4, 1/8, 1/16 \cdots \), and count the number of blocks \( N(r) \) containing fault trajectories. Then, the fitting straight line equation of \( \log (r) \) and \( \log N(r) \) can be constructed, and the slope of the line is the fault fractal dimension \( D \) of block \( i \). In the same way, the fault fractal dimension of other blocks can be obtained. The larger the fractal dimension \( D \), the more fault traces are contained in the block and the higher the complexity of the fault [27].

The study area is divided into 49 blocks, 31 of which are fault blocks, as shown in Figure 4. According to the above steps, the fractal dimension values of each block can be determined, and the results are shown in Table 7. Obviously, the fault fractal dimension range is 0.7551~1.5838, with an average value of 1.2432. The correlation coefficients of \( \log (r) \) and

| Block number | Fractal dimension | Correlation coefficient | Block number | Fractal dimension | Correlation coefficient |
|--------------|------------------|-------------------------|--------------|------------------|-------------------------|
| 1            | 1.2644           | 0.9893                  | 17           | 1.5838           | 0.9981                  |
| 2            | 1.0247           | 0.9665                  | 18           | 0.9007           | 0.9836                  |
| 3            | 1.1963           | 0.9879                  | 19           | 1.3422           | 0.9730                  |
| 4            | 1.0095           | 0.9648                  | 20           | 1.4700           | 0.9820                  |
| 5            | 1.0000           | 1.0000                  | 21           | 1.3262           | 0.9705                  |
| 6            | 0.7551           | 0.9884                  | 22           | 1.3415           | 0.9903                  |
| 7            | 0.6000           | 0.9000                  | 23           | 1.5965           | 0.9823                  |
| 8            | 1.1755           | 0.9854                  | 24           | 1.4548           | 0.9841                  |
| 9            | 0.9007           | 0.9836                  | 25           | 1.4966           | 0.9853                  |
| 10           | 1.1288           | 0.9968                  | 26           | 1.3136           | 0.9862                  |
| 11           | 1.4963           | 0.9721                  | 27           | 1.5030           | 0.9809                  |
| 12           | 0.8340           | 0.9902                  | 28           | 1.2943           | 0.9927                  |
| 13           | 1.2807           | 0.9661                  | 29           | 1.0703           | 0.9749                  |
| 14           | 1.5975           | 0.9823                  | 30           | 1.3222           | 0.9950                  |
| 15           | 1.0247           | 0.9655                  | 31           | 1.4966           | 0.9749                  |
| 16           | 1.8279           | 0.9941                  |              |                  |                         |

Table 7: Fractal dimension and correlation coefficient of each block.

| Borehole number | Fractal dimension | Drilling number | Fractal dimension | Drilling number | Fractal dimension | Drilling number | Fractal dimension |
|-----------------|------------------|-----------------|------------------|-----------------|------------------|-----------------|------------------|
| Qs1             | 0.7551           | Qs8             | 1.1755           | Sx2             | 1.5838           | Zc1             | 1.4548           |
| Qs2             | 0.7551           | Qs9             | 1.4963           | Sx3             | 1.5838           | Zc2             | 1.4548           |
| Qs3             | 1.1755           | Qs10            | 1.4963           | Tk1             | 1.0247           | Zc3             | 1.4966           |
| Qs4             | 1.1755           | Qs11            | 1.4963           | Tk2             | 1.0247           | Zc4             | 1.4548           |
| Qs5             | 0.9007           | Qs12            | 1.4963           | Tk3             | 1.3262           | Zc5             | 1.4966           |
| Qs6             | 0.9007           | Qs13            | 1.4963           | Tk4             | 1.3262           | Zc6             | 1.4966           |
| Qs7             | 0.9007           | Sx1             | 1.5975           | Tk5             | 1.3262           | Zc7             | 1.4548           |

Table 8: Fractal dimension values of the faults in the block where the borehole is located.

| Code category | Overburden lithology | Formula 1 | Formula 2 |
|---------------|----------------------|-----------|-----------|
| Three lower code | Hard lithology       | \( H_l = 100 \sum M/1.2 \sum M + 2.0 \) + 18.9 | \( H_l = 30 \sqrt{\sum M + 20} \) |
| Medium hard lithology | Hard lithology       | \( H_l = 100 \sum M/1.6 \sum M + 3.6 \) + 15.6 | \( H_l = 20 \sqrt{\sum M + 20} \) |
| Mining area code | Medium hard lithology | \( H_l = 100 \sum M/3.3n + 3.8 \) + 15.1 | — |
drilling exploration results, and the di
rock thickness of the coal seam roof can be determined by the
for the evaluation in this paper [30] (see Table 10). The bed-
(Table 9). The maximum value is selected as the basic data

After the coal seam is excavated,
and the Bedrock Thickness.

is shown in Table 8.

the fractal dimension representing the fault complexity
fractal characteristics of the fault distribution in the study
area are good under the selected scale. Additionally, the sta-
tistical self-similarity of the fractal structure is good, and
the fractal dimension value can be used to represent the com-
plexity of the fault.

The 28 geological boreholes belong to different blocks,
and the fractal dimension representing the fault complexity
is shown in Table 8.

4.2. Difference between the Height of the “Upper Three Zones” and the Bedrock Thickness. After the coal seam is excavated,
the roof overburden rock failure is divided into the collapse
zone, crack zone, and bending zone (referred to as the “upper
three zones”). According to the code for coal pillar reservation
and mining under the pressure of buildings, water bod-
ies, railways, and main shafts [28] (referred to as the “three
lower code”) and the code for hydrogeological engineering
geological exploration in a mining area [29] (referred to as the
“mining area code”), the height of the “upper three zones”
can be calculated by using the empirical formula
(Table 9). The maximum value is selected as the basic data
for the evaluation in this paper [30] (see Table 10). The bed-
rock thickness of the coal seam roof can be determined by the
drilling exploration results, and the difference between the
height of the “upper three zones” and the bedrock thickness
is shown in Table 10.

4.3. Index Factor Set. The indexes, such as the thickness ratio
of brittle and plastic rock, the aquifer thickness, the borehole
flushing fluid consumption, the core recovery rate, the coal
seam roof depth, and the surrounding rock temperature
within the height of the “upper three zones” of roof failure,
can be statistically obtained according to the actual informa-
tion disclosed by the exploration drilling. For the conve-
nience of evaluation, the reciprocal value of the core
recovery rate is taken.

According to the 28 geological boreholes in the Suiqi
coalfield, the quantitative values of the 8 index factors used
to evaluate the threat degree of the thermal reservoir aquifer
are listed in Table 11.

5. Evaluation of the Impact Degree

5.1. Basic Formula. Let a, b, c, d, and k be the points on the
fuzzy domain U (see Figure 5), the interval [a, b] belongs to
the interval [c, d], and the point k is located at the midpoint
of the interval [a, b].

If the intervals [a, b] and [c, d] are denoted by A and B,
respectively, u is any sample on U. According to the theory
of fuzzy variable sets, the relative difference degree can be cal-
culated as follows.

When u is within interval B and to the left of the k point,
then we have the following:

\[
D_A(u) = \left(\frac{u - a}{k - a}\right)^\beta, \quad u \in [a, k], \\
D_A(u) = -\left(\frac{u - a}{c - a}\right)^\beta, \quad u \in [c, a].
\] (1)

When u is within interval B and to the right of the k point,
then we have the following:

\[
D_A(u) = \left(\frac{u - b}{k - b}\right)^\beta, \quad u \in [k, b], \\
D_A(u) = -\left(\frac{u - b}{d - b}\right)^\beta, \quad u \in [b, d].
\] (2)
When \( u \) does not belong to interval \( B \), then we have the following:

\[
D_A(u) = -1,
\]

where \( \beta \) is an index greater than 0, and usually \( \beta = 1 \).

After using formulas (1)–(3) to obtain the relative difference degree \( D_A(u) \), the following formula can be used to calculate the relative membership degree \( \mu_A(u) \):

\[
\mu_A(u) = \frac{1 + D_A(u)}{2},
\]

(4)

If there are \( n \) interval levels on the domain \( U \) and the sample \( u \) is composed of \( m \) index factors, the comprehensive relative membership degree of the sample \( u \) belonging to level \( h \) can be calculated as follows:

\[
\varphi_h(u) = 1 + \left( \frac{\sum_{i=1}^{m} \left[ w_i (1 - \mu_{h,i}(u)) \right]^{a_p}}{\sum_{i=1}^{m} \left[ w_i \mu_{h,i}(u) \right]^{a_p}} \right)^{-1},
\]

(5)

where \( \mu_{h,i}(u) \) is the relative membership of the index factor; \( w_i \) is the weight of the index factor; \( i = 1, 2, \ldots, m \); \( h = 1, 2, \ldots, n \); \( \alpha \) is the optimization criterion parameter (\( \alpha = 1 \) or \( \alpha = 2 \)); and \( p \) is the distance parameter (\( p = 1 \) is the Hamming distance and \( p = 2 \) is the Euclidean distance).
5.2. Level Matrix Construction. In view of the fact that the overlying thermal storage aquifer in the study area has good water richness and is affected by a high ground temperature, referring to the existing research results [31], the threat degree of the overlying thermal storage aquifer of the coal seam is divided into five levels, i.e., safe, low threat, medium threat, relatively high threat, and high threat, which are expressed as I, II, III, IV, and V, respectively. The corresponding level characteristic values are shown in Table 12.

| Threat level       | Safe (I) | Low threat (II) | Medium threat (III) | Relatively high threat (IV) | High threat (V) |
|--------------------|----------|----------------|---------------------|----------------------------|-----------------|
| Level characteristic value | $H \leq 2.0$ | $2.0 < H \leq 2.5$ | $2.5 < H \leq 3.0$ | $3.0 < H \leq 3.5$ | $H > 3.5$ |

The calculation formula of the level characteristic value of sample $u$ is as follows:

$$H(u) = \frac{1}{\sum_{h=1}^{n} \phi_h(u)} \sum_{h=1}^{n} \phi_h(u) h.$$  \hspace{1cm} (6)

According to the level characteristic value $H(u)$, the level of the sample $u$ can be judged.

### Table 13: Calculation formula for the $[a, b]$ and $[c, d]$ assignment.

| Threat level | Safe (I) | Low threat (II) | Medium threat (III) | Relatively high threat (IV) | High threat (V) |
|--------------|----------|----------------|---------------------|----------------------------|-----------------|
| $[a, b]$     | $[\rho - 1.25\sigma, \rho - 0.75\sigma]$ | $[\rho - 0.75\sigma, \rho - 0.25\sigma]$ | $[\rho - 0.25\sigma, \rho + 0.25\sigma]$ | $[\rho + 0.25\sigma, \rho + 0.75\sigma]$ | $[\rho + 0.75\sigma, \rho + 1.25\sigma]$ |
| $[c, d]$     | $[\rho - 1.5\sigma, \rho - 0.5\sigma]$ | $[\rho - 0.5\sigma, \rho + 0.5\sigma]$ | $[\rho, \rho + \sigma]$ | $[\rho + 0.5\sigma, \rho + 1.5\sigma]$ | $[\rho + 1.5\sigma, \rho + 2.5\sigma]$ |
| $k$          | $\rho - \sigma$ | $\rho - 0.5\sigma$ | $\rho$ | $\rho + 0.5\sigma$ | $\rho + \sigma$ |

Note: $\rho$ and $\sigma$ are the mean and standard deviation of the index factor, respectively; when $a$ or $c$ is less than 0, its value is 0.
Threat levels can be obtained, as shown in Tables 14–16.

Table 16: Composition of matrix K.

| Index factor | Safe (I) | Low threat (II) | Medium threat (III) | Relatively high threat (IV) | High threat (V) |
|--------------|----------|----------------|---------------------|-----------------------------|-----------------|
| $C_1$        | 0.4084   | 0.6858         | 0.9631              | 1.2405                      | 1.5178          |
| $C_2$        | 1270.66  | 1332.31        | 1393.96             | 1455.61                     | 1517.26         |
| $C_3$        | 1.0349   | 1.1661         | 1.2972              | 1.4284                      | 1.5595          |
| $C_4$        | 21.8961  | 28.7631        | 35.6300             | 42.4970                     | 49.3639         |
| $C_5$        | 0.0132   | 0.5887         | 11.1641             | 1.7396                      | 2.3150          |
| $C_6$        | 1.1120   | 1.2343         | 1.3566              | 1.4789                      | 1.6012          |
| $C_7$        | 48.7721  | 51.3561        | 53.9400             | 56.5240                     | 59.1079         |
| $C_8$        | -177.8983| -128.7312      | -79.5640            | -30.3969                    | 18.7703         |

Table 17: Relative difference matrix of borehole Qs1.

| Index factor | Safe (I) | Low threat (II) | Medium threat (III) | Relatively high threat (IV) | High threat (V) |
|--------------|----------|----------------|---------------------|-----------------------------|-----------------|
| $C_1$        | -1       | -0.0171        | 0.0171              | -1                          | -1              |
| $C_2$        | -1       | -1             | -1                  | 0.5291                      | -0.5292         |
| $C_3$        | -1       | -1             | -1                  | -1                          | -1              |
| $C_4$        | -1       | -1             | -0.8808             | 0.8821                      | -1              |
| $C_5$        | -1       | -1             | -1                  | 0.3162                      | -0.3162         |
| $C_6$        | -1       | -1             | 0.39                | -0.39                       | -1              |
| $C_7$        | -1       | -1             | -0.6218             | 0.6242                      | -1              |
| $C_8$        | -1       | -0.5081        | -0.6204             | 0.6203                      | -1              |

Table 18: Relative membership matrix of borehole Qs1.

| Index factor | Safe (I) | Low threat (II) | Medium threat (III) | Relatively high threat (IV) | High threat (V) |
|--------------|----------|----------------|---------------------|-----------------------------|-----------------|
| $C_1$        | 0        | 0.4914         | 0.5086              | 0                           | 0               |
| $C_2$        | 0        | 0              | 0                   | 0.7646                      | 0.2354          |
| $C_3$        | 0        | 0              | 0                   | 0                           | 0               |
| $C_4$        | 0        | 0              | 0.0596              | 0.9410                      | 0               |
| $C_5$        | 0        | 0              | 0                   | 0.6581                      | 0.3419          |
| $C_6$        | 0        | 0              | 0.6950              | 0.3050                      | 0               |
| $C_7$        | 0        | 0              | 0.1891              | 0.8121                      | 0               |
| $C_8$        | 0        | 0              | 0.1899              | 0.8101                      | 0               |

According to the assignment criteria in Table 13, the $AB$, $CD$, and $K$ matrices are composed of the index factors and threat levels can be obtained, as shown in Tables 14–16.

5.3 Evaluation Results. For the borehole Qs1, the relative difference degree and relative membership degree (as shown in Tables 17 and 18) can be obtained by using formulas (1)–(6); then, the comprehensive membership degree and level characteristic values (as shown in Tables 19 and 20) under different parameters $\alpha$ and $p$ can be further calculated. The calculation results show that the average level characteristic value of borehole Qs1 is 3.8603, which belongs to a high-threat area according to the classification standard in Table 12. According to the calculation steps of borehole Qs1, the level characteristic values of 28 boreholes can be given in turn, as shown in Table 21. It can be seen from Table 21 that the proportion of the 28 boreholes that are in the high threat and relatively high threat levels is 57.14%, 32.14% of the boreholes are in the medium threat and low threat levels, and 10.71% of the boreholes are in the high threat area according to the classiﬁcation standard in Table 21. Contour maps can be drawn based on the average level characteristic values of the 28 boreholes, and the threat degree division of the overlying thermal storage aquifer under the condition of coal mining can be delineated according to the criteria in Table 13, as shown in Figure 6. The overall threat degree of the roof thermal storage aquifer is as follows: the threat degree in the western portion of the study area is less than that in the eastern portion, and the threat degree increases as the hidden outcrop line of the coal seam is approached. Due to the influences of multiple factors, the average level characteristic value $H$ of the areas near the boreholes Qs1, Qs5, Qs8, Sx1, Tk5, Zc4, and Zc7,
which are close to the hidden outcrop line of the coal seam, is greater than 3.5, which are the high-threat areas caused by the roof thermal storage aquifer.

According to the statistical results in Figure 6, it can be seen that the high-threat zone of the roof thermal storage aquifer accounts for 10.21% of the study area, the relatively high-threat zone accounts for 33.85%, the medium-threat zone accounts for 27.76%, the low-threat zone accounts for 19.76%, and the safe zone accounts for 8.42%. Obviously, the proportion of the area above the medium-threat zone is 71.82%, and the possibility of a roof water and heat disaster accident occurring under coal mining conditions is greater.

5.4. Verification of Evaluation Results. According to the “upper three zones” theory of a coal seam roof, when the calculated height of the “upper three zones” is greater than the thickness of the bedrock, the roof failure zone of the coal mining operation will reach the overlying Neogene thermal storage aquifer with strong water richness and good permeability, which will greatly increase the risk of a roof disaster. Therefore, the difference between the thickness of the coal seam roof bedrock and the height of the “upper three zones” (referred to as “difference”) is a common index and a traditional method to evaluate the roof threat level at present. The smaller the “difference” is, the greater the roof threat level is. The areas where the “difference” is negative belong to the high-threat areas of the roof. The “difference” contour of the Suiqi field is shown in Figure 7. Obviously, the “difference” in the west is larger than that in the east during the mining of the no. 21 coal seam, which indicates that the roof disaster threat is greater as the hidden outcrop line of the coal seam is approached. In addition, the high-threat area of the roof in Figure 7 is located in the high-threat area and relatively high-threat area in Figure 6, which shows that the evaluation results of the “difference” method and the method adopted in this paper are basically the same. However, the fuzzy variable set method adopted in this paper considers more influencing factors and can obtain more precise evaluation results.

Table 21: Borehole level characteristic value and threat degree level.

| Borehole number | Level characteristic value | Threat degree level |
|-----------------|---------------------------|---------------------|
|                 | α = 1, p = 1             | α = 1, p = 2       | α = 2, p = 1       | α = 2, p = 2       | Mean value     |                     |
| Qs1             | 3.7987 3.7685 3.9472 3.9267 | 3.8603 V           |                     |                     |                 |                     |
| Qs2             | 3.1859 3.1691 3.4444 3.4207 | 3.3050 IV          |                     |                     |                 |                     |
| Qs3             | 2.5265 2.5628 2.4522 2.5588 | 2.5250 III         |                     |                     |                 |                     |
| Qs4             | 2.2011 2.2613 2.0194 2.0668 | 2.1372 II          |                     |                     |                 |                     |
| Qs5             | 4.2872 4.1676 4.8764 4.8075 | 4.5347 V           |                     |                     |                 |                     |
| Qs6             | 1.8210 1.8441 1.6587 1.6617 | 1.7464 I           |                     |                     |                 |                     |
| Qs7             | 2.5865 2.6138 1.8951 1.8889 | 2.2461 II          |                     |                     |                 |                     |
| Qs8             | 3.5078 3.4391 4.0806 3.9407 | 3.7421 V           |                     |                     |                 |                     |
| Qs9             | 3.4943 3.4589 3.5209 3.5204 | 3.4986 IV          |                     |                     |                 |                     |
| Qs10            | 3.1276 3.1309 3.2121 3.2368 | 3.1768 IV          |                     |                     |                 |                     |
| Qs11            | 3.2272 3.2326 3.3266 3.3260 | 3.2781 IV          |                     |                     |                 |                     |
| Qs12            | 2.9278 2.8802 2.7781 2.6720 | 2.8145 III         |                     |                     |                 |                     |
| Qs13            | 2.5854 2.9463 1.7968 2.5684 | 2.4742 II          |                     |                     |                 |                     |
| Sx1             | 3.8993 3.9521 4.5876 4.6299 | 4.2672 V           |                     |                     |                 |                     |
| Sx2             | 3.0592 3.0541 2.9384 3.0072 | 3.0147 IV          |                     |                     |                 |                     |
| Sx3             | 2.5640 2.7300 2.1946 2.5243 | 2.5032 III         |                     |                     |                 |                     |
| Tk1             | 1.2672 1.3886 1.0412 1.0935 | 1.1976 I           |                     |                     |                 |                     |
| Tk2             | 2.7366 2.9585 2.6189 2.9054 | 2.8048 III         |                     |                     |                 |                     |
| Tk3             | 1.8434 2.1897 1.2607 1.7741 | 1.7670 I           |                     |                     |                 |                     |
| Tk4             | 3.1855 3.1930 3.0486 2.9762 | 3.1008 IV          |                     |                     |                 |                     |
| Tk5             | 3.9012 3.7841 3.9331 3.7070 | 3.8313 V           |                     |                     |                 |                     |
| Zc1             | 3.3253 3.3231 3.6613 3.6741 | 3.4959 IV          |                     |                     |                 |                     |
| Zc2             | 2.9098 2.7651 2.6888 2.2687 | 2.6581 III         |                     |                     |                 |                     |
| Zc3             | 2.7722 3.1029 2.5133 3.2040 | 2.8981 III         |                     |                     |                 |                     |
| Zc4             | 3.7228 3.5441 3.9969 3.9215 | 3.7963 V           |                     |                     |                 |                     |
| Zc5             | 3.1836 3.1898 3.3773 3.4149 | 3.2914 IV          |                     |                     |                 |                     |
| Zc6             | 3.3586 3.4039 3.3745 3.8063 | 3.4858 IV          |                     |                     |                 |                     |
| Zc7             | 3.8714 3.8507 4.4635 4.4201 | 4.1514 V           |                     |                     |                 |                     |

Figure 6: Threat degree division of the coal seam roof.
6. Conclusions

(1) Based on the analysis of multiple factors affecting coal mining, eight factors are selected as the index factors for threat assessment, including the thickness ratio of brittle and plastic rock, the coal seam roof depth, the fault complexity, the aquifer thickness, the borehole flushing fluid consumption, the core recovery rate, the surrounding rock temperature, and the difference between the height of the "upper three zones" and the bedrock thickness, which provide a guarantee for the comprehensive and accurate identification of water and heat disasters of coal seam roofs.

(2) The mathematical model of the threat degree evaluation is established by coupling the AHP and the fuzzy variable set theory. Based on the weights and quantitative values of the eight index factors, the threat degree of the thermal storage aquifer to the deep coal mining operation was identified and the threat degree was divided, which lays the foundation for the prevention and control of water and heat disasters of the overlying strata and safe mining.

(3) The quantitative evaluation of the threat degree of the thermal storage aquifer shows that the risk in the western region is less than that in the eastern region, and the closer it is to the outcrop line of the coal seam, the greater the risk; in the areas near the boreholes Qs1, Qs5, Qs8, Sx1, Tk5, Zc4, and Zc7, which are close to the hidden outcrop line of the coal seam, the classification characteristic values of the threat degree are greater than 3.5, which belong to high-threat areas caused by the roof thermal storage aquifer. In these areas, roof water and heat disasters are prone to occur during coal mining.

(4) According to the threat degree of the thermal storage aquifer of the coal seam roof, comparing the
evaluation results of the traditional “upper three zones” theory (taking the difference between the thickness of the bedrock and the height of the “upper three zones” as parameters) with modern mathematical methods (coupling AHP and variable fuzzy set theory), it can be obtained that the evaluation results of the two methods are basically the same, but the evaluation results of the latter are more precise.

(5) For the entire study area, the high-threat zone accounts for 10.21%, the relatively high-threat zone accounts for 33.85%, the medium-threat zone accounts for 27.76%, the low-threat zone accounts for 19.76%, and the safe zone accounts for 8.42%. The area above the medium-threat zone accounts for 71.82%, which includes a greater possibility of the roof water and a heat disaster occurring during mining of the no. 21 coal seam.

Data Availability

All data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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