Voltage-driven quantum oscillations of conductance in graphene

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Abstract – Locally-gated single-layer graphene sheets have unusual discrete energy states inside the potential barrier induced by a finite-width gate. These states are localized outside the Dirac cone of continuum states and are responsible for novel quantum transport phenomena. Specifically, the longitudinal (along the barrier) conductance exhibits oscillations as a function of barrier height and/or width, which are both controlled by a nearby gate. The origin of these oscillations can be traced back to singularities in the density of localized states. These graphene conductance-oscillations resemble the Shubnikov-de Haas (SdH) magneto-oscillations, however, here these are driven by an electric field instead of a magnetic field.

Introduction. – The unusual and rather remarkable transport properties of graphene continue to attract considerable attention. Soon after its experimental discovery [1], studies found: unconventional quantum Hall effect [2]; the possibility of testing the Klein paradox [3]; specular Andreev reflection and Josephson effect [4]; new electric field effects [5,6]; intriguing electron lensing [7]; and other fascinating phenomena (see, e.g., recent papers [8–16] and references therein). Studies of graphene are also inspired by their potential application in nano-electronic devices, since an applied electric field can vary considerably the electron concentration and have both electrons and holes as charge carriers with high mobility.

The subject of the present study, which is a logical continuation of recent work [6], is an unusual novel transport effect, namely, voltage-driven quantum oscillations in the conductance of a single-layer gated graphene. These oscillations originate from a new type of electron states in graphene. When a graphene sheet is subject to nearby gates, these create an energy barrier for propagating electrons. Here we explicitly demonstrate that, in contrast to non-relativistic quantum mechanics, where localized states can exist only inside quantum wells, Dirac-like relativistic electrons in graphene allow energy states localized within the barrier. We show that the energy $\varepsilon(q_y)$ of the localized states (vs. the wave vector component $q_y$ along the barrier) becomes non-monotonic if $V_0D > \pi \hbar v_F$, where $V_0$ and $D$ are the barrier height and width correspondingly, and $v_F$ is the Fermi velocity. This produces singularities in the density of localized states for energies where $d\varepsilon/dq_y = 0$. When the magnitude and/or width of the barrier changes, the locations of the singularities move and periodically cross the Fermi level, generating quantum oscillations in the longitudinal (along the barrier) conductance as well as in the thermodynamic properties of graphene. This situation resembles the well known physical mechanism for Shubnikov-de Haas (SdH) magneto-oscillations (see, e.g., refs. [17–19]). Indeed, electrons in the conduction band of a metal subject to a strong magnetic field have equidistant discrete energy levels (Landau levels) separated by the cyclotron energy. The corresponding density of states has singularities at the Landau levels. When the magnetic field is changed, the positions of the Landau levels move and pass periodically through the Fermi energy. As a result of this, the population of electrons at the Fermi level also changes periodically, giving rise to the quantum oscillations of both the transport and thermodynamic properties.
of a metal. One should notice, however, a few important differences. First, in the context of gated graphene, oscillations are induced by the electric field, while the corresponding SdH oscillations are driven by a magnetic field. Second, localized energy states in graphene are non-equidistant and the resulting density of states has a rather complicated energy dependence. Thus, the corresponding oscillations in the conductance inherit all these unusual peculiarities.

**Localised energy states in a barrier.** – The tunneling of relativistic particles in graphene across a finite-width potential barrier, and its corresponding conductance, has been recently studied (see, e.g., refs. [3,7,20–22]). Here we consider another conductor of a metal. Oneshould notice, however, a few important differences. First, in the context of gated graphene, oscillations are induced by the electric field, while the corresponding SdH oscillations are driven by a magnetic field. Second, localized energy states in graphene are non-equidistant and the resulting density of states has a rather complicated energy dependence. Thus, the corresponding oscillations in the conductance inherit all these unusual peculiarities.

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![Graphene sheet schematic](image)

Fig. 1: (Color online) Schematic top view of a graphene sheet (yellow rectangle) placed under voltage gates indicated by the grey block rectangles. Bottom: gate-induced potential energy barrier $V(x)$ in graphene.

Electrons in monolayer graphene obey the Dirac-like equation (hereafter $\hbar = 1$),

$$i \frac{\partial \psi}{\partial t} = \hat{H} \psi, \quad \hat{H} = -iv_F \vec{\sigma} \cdot \vec{\nabla} + V(x),$$

(2)

where $\vec{\sigma} = (\sigma_x, \sigma_y)$ are the Pauli matrices. We then seek stationary spinor solutions of the form

$$\psi(x, y) = \psi(x) \exp(-i\varepsilon t + i q_y y),$$

(3)

with energy $\varepsilon$ and momentum $q_y$ along the barrier. We focus on states with $|q_y| > |\kappa| \equiv |\varepsilon|/v_F$. In this case, the electron waves satisfying eq. (2) damp away from the barrier, and the components $\psi_1$ and $\psi_2$ of the Dirac spinor can be written in the form

$$\psi_1(x) = \begin{cases} 
  a \exp[k_x(x + D/2)], & x < -D/2, \\
  b \exp(i q_y x) + c \exp(-i q_y x), & |x| \leq D/2, \\
  d \exp[-k_x(x - D/2)], & x > D/2,
\end{cases}$$

(4)

$$\psi_2(x) = \begin{cases} 
  \frac{ia}{\kappa + q_y} \exp[k_x(x + D/2)], & x < -D/2, \\
  -b \exp(i q_y x + i\theta) + c \exp(-i q_y x - i\theta), & |x| \leq D/2, \\
  \frac{-i d e}{k_x - q_y} \exp[-k_x(x - D/2)], & x > D/2,
\end{cases}$$

(5)

with real $k_x = (q_y^2 - \kappa^2)^{1/2}$ and $q_y = ((\kappa - V/D)^2 - q_y^2)^{1/2}$. Here $V = V_0 D/v_F$ is the effective barrier strength and $\tan \theta = q_y/q_x$.

Matching the functions $\psi_1(x)$ and $\psi_2(x)$ at the points $x = \pm D/2$, we obtain a set of four linear homogeneous algebraic equations for the constants $a, b, c,$ and $d$. Equating the determinant of this set to zero, we obtain a dispersion relation for the localized electron energy states,

$$F(\varepsilon, q_y) \equiv \tan(q_y D) + \frac{k_x q_x}{\kappa V/D - \kappa} = 0.$$  

(6)

The spectrum of localized states in graphene (eq. (6)) is shown by the solid black curves in fig. 2, for dimensionless variables

$$Q = q_y D, \quad \mathcal{E} = \varepsilon D/v_F.$$  

(7)

This spectrum consists of an infinite number of branches $\mathcal{E}_n(Q)$. Each of these branches starts from the lines $\mathcal{E} = \pm |Q|$ (red solid straight lines in fig. 2) at

$$\mathcal{E} = V/2 - \pi^2 n^2 / 2V$$

(8)

and tends asymptotically to the line $\mathcal{E} = V - Q$ with increasing $Q$ (dashed red line in fig. 2). Furthermore, a particular branch of the spectrum starts at the point $(Q = 0, \mathcal{E} = 0)$ and also tends to the line $\mathcal{E} = V - Q$.

The behavior of different branches of the spectrum depends on the barrier strength $V$. If $V < \pi/2$, then all branches satisfy $\mathcal{E} < 0$. Localized states with positive energies appear only for $V > \pi/2$. When $V$ increases, new branches in the spectrum with positive energies appear. When $V$ is within the interval $(n + 1/2)\pi < V < (n + 3/2)\pi$, the number of branches with $\mathcal{E} > 0$ is $n + 1$, for $n = 1, 2, 3, \ldots$. It is worth emphasizing that each of the branches with positive energy has a maximum $\mathcal{E}_n^{\text{max}}$ at a certain wave number $Q = Q_n^{\text{max}}$. Near these points the group velocity of localized electron waves tends to zero, which resembles the stop-light phenomena found in various media [23]. The localized states can also be observed in graphene when a voltage is applied to produce a potential well [24].

Note that defect-induced localized electron states in graphene and the enhancement of conductivity due to
an increase of the electron density of states localized near the graphene edges were recently reported [25]. In contrast to these examples, the electron states studied here are localized within the barrier and also these are tunable, i.e., the energy levels can be shifted by charging the barrier strength (e.g., via tuning a gate voltage). Interestingly, similar localized states can be engineered in the strained graphene [26]. In general, depending on the particular realization, there exist five types of possible states [27]: i) scattering states; ii) band states (states localized in the junction along the x-direction) propagating along the y-direction, which we discussed above; iii) localized states at the boundary of the junction; iv) filtered states, that is, scattering states decaying exponentially inside the junction for certain values of the incoming angle and v) completely filtered states such that the transmission occurs via evanescent waves for any orientation of the incoming momentum. Clearly, such rich picture provides many interesting possibilities for the gate or strain-controlled transport in graphene.

**Density of localized states.** – To calculate the density of electron states \( \rho(\varepsilon) \), we use the general formula 
\[
\rho(\varepsilon) = \sum_{\alpha} \delta(\varepsilon - \varepsilon_{\alpha}),
\]
where the index \( \alpha \) labels the quantum state and \( \delta(x) \) is Dirac’s delta-function. Using
\[
\sum_{\alpha}(\ldots) = 4L_xL_y(2\pi)^{-2} \int dk_x dk_y(\ldots)
\]
for a continuum spectrum one finds the already familiar expression

\[
\rho_{\text{cont}}(\varepsilon) = \rho_0 |\varepsilon|, \quad \rho_0 = \frac{2L_xL_y}{\pi v_F D}, \quad (10)
\]
where \( L_x \) and \( L_y \) are the lengths of the graphene sheet in the \( x \)- and \( y \)-directions, respectively. For localized energy states, we obtain

\[
\rho_{\text{loc}}(\varepsilon) = 2\rho_0 \frac{D}{L_x} \sum_n \frac{|d\varepsilon_n(Q)|^{-1}}{dQ} |\varepsilon_n(Q) = \varepsilon|, \quad (11)
\]
where \( n \) runs over the positive roots of the equation \( \varepsilon(Q) = \varepsilon \). The function \( \rho_{\text{loc}}(\varepsilon) \) exhibits two types of peculiarities. First, increasing \( \varepsilon \), the jumps or steps (each of magnitude \( 2D/L_x \)) in \( \rho_{\text{loc}}(\varepsilon)/\rho_0 \) occur at the points, given by eq. (8), where new branches of the spectrum arise or disappear. More importantly, singularities are observed when \( \varepsilon = \varepsilon_{\text{max}} \), where \( |d\varepsilon/dQ|^{-1} \) in eq. (11) diverges.

The locations of the singularities shift when changing the barrier strength \( V \). Therefore, they periodically cross the Fermi level \( \varepsilon_F \). This produces quantum oscillations in the density of states at the Fermi energy, which are seen in the upper panel of fig. 3, showing \( \rho_{\text{loc}}(\varepsilon)/\rho_0 \) vs. \( \varepsilon \), the effective barrier strength \( V \).

**Kubo formula and conductance.** – When studying transport, within linear response theory, one usually starts from the current-response function,

\[
K_{\mu\nu}(x, x') = -i\theta(t - t') Tr \left\{ \hat{\rho}(\hat{j}_{\mu}^{H}(x), \hat{j}_{\nu}^{H}(x')) \right\}, \quad (12)
\]
where \( \mathbf{x} = (r, t) \), \( \vartheta(t) \) is the Heaviside step-function, \( \hat{\rho} \) is the equilibrium density matrix, and \( \hat{J}_\mu^H(r, t) = \exp(i\hat{H}t)j_\mu^H(r) \exp(-i\hat{H}t) \) is the current operator in the Heisenberg representation with the Hamiltonian taken from eq. (2), and where \( \ldots \ldots \) stands for the commutator. For electrons with a linear Dirac spectrum, one finds \( j_\mu^H(r) = ev_F\hat{\psi}^\dagger(r)\hat{\sigma}_\mu\hat{\psi}(r) \). Equation (12) is used to define the frequency-dependent linear conductance as

\[
g_{\mu\nu}(\omega) = \frac{\pi}{\omega L_L L_V} \int dr' \delta(r, r'; \omega). \tag{13}
\]

Here \( \mathcal{R} \) stands for the real part of a complex number. We expand the fermionic field operator \( \hat{\psi}^\dagger(r, t) \) in terms of exact eigenfunctions (eq. (3)), namely, \( \hat{\psi}^\dagger(r, t) = \sum_\alpha \psi_\alpha(r) \exp(-i\epsilon_\alpha t)\hat{a}_{\alpha} \), and then perform quantum averaging in eq. (12) with the help of Wick’s theorem and the relation \( \text{Tr}[\hat{a}^\dagger\hat{a} \hat{b}^\dagger \hat{b}] = \delta_{\alpha\beta}\delta f(\epsilon_\alpha) \), where \( f(\epsilon) = 1/[\exp(\epsilon - \epsilon_F)/T] + 1 \) is the Fermi occupation function. Performing a Fourier transform and using \( \mathcal{R}(i/\epsilon - \epsilon' + \omega + i0) = \pi\delta(\epsilon - \epsilon' + \omega) \), (eq. 13), reduces to

\[
g_{\mu\nu}(\omega) = \frac{\pi(\epsilon_F)^2}{4\pi L_L L_V} \int_{-\infty}^{\infty} d\epsilon f(\epsilon_+ - f(\epsilon_-) \left. \right|_\omega \times \text{Tr} \left\{ \hat{\sigma}_\nu \hat{\sigma}(\epsilon_+ - \hat{H})_{rr'}^\dagger \hat{\sigma}_\mu \hat{\sigma}(\epsilon_- - \hat{H})_{rr'} \right\} , \tag{14}
\]

where \( \epsilon_\pm = \epsilon \pm \omega/2 \) and the trace incorporates spatial integrations. The operator delta-functions can be directly related to the single-particle Green’s functions \( \hat{G}_\epsilon^\nu(r, r') = \langle \epsilon | r' \rangle (\epsilon - \hat{H} - \omega)^{-1} | \epsilon r \rangle \) according to \( \delta(\epsilon - \hat{H})_{rr'} = \frac{1}{\pi^2} [\hat{G}_\epsilon^\nu(r, r') - \hat{G}_\epsilon^\nu(r, r')^\dagger] \), where the superscript \( \alpha/r \) stands for the advanced/retarded component, respectively. As a result, one finds for the conductance

\[
g_{\mu\nu}(\omega) = \frac{\pi(\epsilon_F)^2}{4\pi L_L L_V} \int_{-\infty}^{\infty} d\epsilon f(\epsilon_+ - f(\epsilon_-) \left. \right|_\omega \times \text{Tr} \left\{ \hat{\sigma}_\nu \hat{G}_\epsilon^\nu(r, r') - \hat{G}_\epsilon^\nu(r, r')^\dagger \hat{\sigma}_\mu \hat{G}_\epsilon^\nu(r', r) - \hat{G}_\epsilon^\nu(r', r)^\dagger \hat{\sigma}_\nu \hat{G}_\epsilon^\nu(r', r') \right\} , \tag{15}
\]

Next we incorporate disorder by introducing the one-particle scattering time \( \tau \), for Dirac fermions, into the Green’s function,

\[
\langle \hat{G}_\epsilon^{\nu/a}(r, r') \rangle_{\text{dis}} \approx (\epsilon - \hat{H} \pm i/\tau)^{-1}, \tag{16}
\]

which enters through the imaginary-part of the corresponding self-energy. The subindex “dis” refers to disorder. Furthermore, we factorize the average of the product of two Green’s functions by the product of their averages, \( \langle \hat{G}_\epsilon^\nu \hat{G}_\epsilon^\alpha \rangle_{\text{dis}} \approx \langle \hat{G}_\epsilon^\nu \rangle_{\text{dis}} \langle \hat{G}_\epsilon^\alpha \rangle_{\text{dis}} \). This assumption should be valid for weak disorder and together with eq. (16) is equivalent to the self-consistent Born approximation.

We now focus on the along-the-barrier \( (\mu = \nu = y) \) conductance for the geometry shown in fig. 1. At zero temperature, \( T \to 0 \), when \( f(\epsilon) = \vartheta(\epsilon_F - \epsilon) \) and the \( \epsilon \) integration is bounded by the frequency \( \omega \), for the average dc-conductance \( g \equiv \langle g_{yy}(\omega \to 0) \rangle_{\text{dis}} \) we find (per spin and per valley):

\[
g = g_{\text{cont}} + g_{\text{loc}}. \tag{17}
\]

The first contribution \( g_{\text{cont}} \) here comes from the extended electron energy states with corresponding density of states taken from eq. (10), and reads explicitly (now keeping \( h \))

\[
g_{\text{cont}} = \frac{\pi e^2}{16\hbar} L_L L_V \left[ \epsilon_F \tau + \frac{1}{\pi} \left( 1 - \frac{\epsilon_F \tau}{\epsilon_F} \arctan \frac{1}{\epsilon_F \tau} \right) \right]. \tag{18}
\]

At the neutrality point, \( \epsilon_F = 0 \), from eq. (18) one recovers a universal (i.e., scattering time \( \tau \)-independent) result \( g_{\text{cont}} = \sigma_{\text{min}}(L_L/L_y) \), where \( \sigma_{\text{min}} = (\pi/8)(\epsilon_F^2/h) \) is the minimal conductivity, which received considerable attention in a number of recent studies (e.g., refs. [21,28]). Away from the neutrality point, the conductance grows linearly with the Fermi energy,

\[
g_{\text{cont}} = \frac{\pi e^2}{16h}(L_L/L_y)\epsilon_F \tau. \tag{19}
\]

The novel result of the present study is the oscillatory part \( g_{\text{loc}} \), which originates from the electron states localized within the barrier. It can be expressed, with the help of eq. (11), as follows:

\[
g_{\text{loc}} = \frac{2e^2}{\hbar L_y} \sum_n \int_0^\infty d\epsilon \frac{dQ}{d\epsilon_n}[\epsilon_n = \epsilon \left( \frac{M(\epsilon)}{E - \epsilon_F} \right)^2 + \eta^2] \tag{20}
\]

where \( M(\epsilon) = \int dx\psi^*_\alpha(x)\hat{\sigma}_y\psi_\alpha(x) \), is the matrix element constructed from the wave functions of localized states, eqs. (4), (5), and \( \eta = D/\epsilon_F \). The remaining integration in eq. (20) is simplified realizing that everywhere away from the integrable square-root singularities of \( dQ/d\epsilon_n \), the \( \eta \)-dependent function is peaked at the Fermi energy, whereas \( M(\epsilon) \) is smooth. Thus, one finally finds,

\[
g_{\text{loc}}(\nu, \epsilon_F) = \frac{16D}{\epsilon_F L_L M(\epsilon_F)} \sum_n \left| \frac{dQ}{d\epsilon_n}[\epsilon_n = \epsilon_F] \right| , \tag{21}
\]

where the conductance \( g_{\text{loc}} \) is normalized to its continuous part taken away from the neutrality point, namely, where \( g_{\text{cont}} \propto \tau \epsilon_F \), see eq. (19). Note that \( \epsilon_F = \epsilon_F \frac{D}{\tau} \). The derivative entering equation (21) can be calculated with the help of the dispersion equation (6) as \( dQ/d\epsilon = -(dF/d\epsilon)/(dF/dQ) \), and reads

\[
\frac{dQ}{d\epsilon} = Q \frac{\l(\frac{V - \epsilon_F}{V - \epsilon_F}\sqrt{Q^2 - \epsilon_F^2}\sqrt{Q^2 - \epsilon_F^2}}. \tag{22}
\]

The oscillatory nature of \( g_{\text{loc}}(\nu, \epsilon_F) \) is illustrated in the lower panel of fig. 3. The essential observation, which follows from eq. (21), is that the longitudinal conductance traces the peculiarities in the density of localized states and opens a direct way for their experimental observation. It is also worth mentioning that close to the singularity of \( dQ/d\epsilon \), meaning \( |\epsilon_n - \epsilon_F| \lesssim \eta \), the conductance correction is regularized by the finite width of the \( \eta \)-Lorentzian under the integral of eq. (20).

Varying the concentration of free particles with constant barrier strength, one can again observe oscillations in the
Fig. 4: Dimensionless oscillating parts of the density of states $\rho_{\text{osc}}/\rho_0$ at the Fermi level (inset) and conductance $g_{\text{osc}}/g_{\text{cont}}$ (main panel) vs. the Fermi energy $E_F$, for $D/L_z = 0.1$, and $V = 16$.

density of states (see the inset of fig. 4). Thus, the part of the conductance originated from the localized states, also oscillates with the change of the Fermi energy (see main panel of fig. 4).

Conclusions. – In summary, we predict a novel type of conductance oscillations in locally gated single-layer graphene, which are related to the unusual electron states localized within a potential barrier. When the barrier height and/or width is varied, localized levels periodically cross the Fermi energy, inducing modulations in the density of states. The latter translates into unusual quantum oscillations of the conductance. These electric-field–driven quantum oscillations are similar to the Shubnikov-de Haas oscillations which are produced in metals and semiconductors when changing the external magnetic field.

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