Effects of Goldstone bosons on gamma-ray bursts

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Abstract. Gamma-ray bursts (GRBs) are the most energetic explosion events in the universe. An amount of gravitational energy of the order of the rest-mass energy of the Sun is released from a small region within a short time. This should lead to the formation of a fireball of temperature in the MeV range, consisting of electrons/positrons, photons, and a small fraction of baryons. We exploit the potential of GRB fireballs for being a laboratory for testing particle physics beyond the Standard Model, where we find that Weinberg’s Higgs portal model serves as a good candidate for this purpose. Due to the resonance effects, the Goldstone bosons can be rapidly produced by electron-positron annihilation process in the initial fireballs of the gamma-ray bursts. On the other hand, the mean free path of the Goldstone bosons is larger than the size of the GRB initial fireballs, so they are not coupled to the GRB’s relativistic flow and can lead to significant energy loss. Using generic values for the GRB initial fireball energy, temperature, radius, expansion rate, and baryon number density, we find that the GRB bounds on the parameters of Weinberg’s Higgs portal model are indeed competitive to current laboratory constraints.

Keywords: absorption and radiation processes, astrophysical fluid dynamics, particle physics - cosmology connection

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1 Introduction

Gamma-ray bursts (GRBs) are the most energetic explosion events in the universe (for recent reviews, see refs. [1–7].) They emit a huge amount of energy of the order of $10^{52}$ erg or higher [8–12], within a short timescale. The initial burst of gamma-ray radiation is usually followed by an “afterglow” at longer wavelengths, ranging from X-ray, optical to radio. First detected by the military Vela satellites in late 1960’s [13], their subsequent observations by the BATSE [14], BeppoSAX [15], Konus/Wind [16], HETE-2 [17], Swift [18], INTEGRAL [19], AGILE [20], and Fermi [21] satellites help to shed light on their nature and physical properties. It is established that they are of cosmological origin, with the highest redshift recorded so far being $z = 9.4$ [22]. Following the investigations of ref. [23], GRBs are commonly classified in two classes according to their $T_{90}$, the time during which 90% of the burst’s fluence is accumulated. Long bursts ($T_{90} > 2$ s) may be due to the collapse of massive stars [24], while short bursts ($T_{90} < 2$ s) are speculated to originate from the binary neutron star or
neutron star-black hole mergers [1, 25]. There are also ultra-long bursts [26], or bursts whose
detection requires a new classification scheme [27].

The fireball model [28–31] is the simplest and most conventional model to explain the
observed non-thermal high-energy prompt emission, the variability over short timescales,
and the generation of the afterglow of GRBs (see refs. [4, 5, 32–35] for detailed reviews.)
In this model, the central engine is a black hole or a neutron star, surrounded by a matter
accretion disc, which causes a jet of material blasted outward at relativistic speed. During
the course of the fireball expansion, the thermal energy contained in the electrons, positrons
and photons are gradually converted into kinetic energy of the baryons, which are accelerated to
a high Lorentz factor. The kinetic energy is converted to gamma-ray photons in the collisions
between internal shock waves travelling at different speeds. At some large distances away
from the central engine where the fireball becomes optically thin, the gamma-ray photons can
escape and be observed as the prompt emission. As the shock waves continue to propagate
outward, they eventually interact with the interstellar medium, causing the latter to emit
radiations. The long duration and the wide electromagnetic spectrum covered by those
radiation processes then account for the observed afterglows.

The tremendous amount of energy release and the high initial temperature of the GRB
fireball makes it an excellent laboratory for particle physics. In the Standard Model (SM),
refs. [8, 36] have studied the effects of neutrinos on the GRB initial fireballs. It is found that
although neutrino production therein is rapid enough to cool the fireball, the high opacity of
the latter to the neutrinos efficiently prevents dramatic energy losses of itself [36]. In ref. [37],
effects of the neutron component were studied in dependence of the final Lorentz factor of the
GRB plasma wind. It showed that neutrons can strongly influence a GRB by changing the
dynamics of its shocks in the surrounding medium. Beyond the SM, the possibility of using
axions and other exotic particles for transferring the gravitational energy of the central col-
lapsing object into the GRB fireball was investigated in refs. [38–41], and ref. [42], respectively.

In this work we shall show that another good example is provided by Weinberg’s Higgs
portal model [43], which was proposed to account for the fractional cosmic neutrinos in
the early universe. In this model, Weinberg considered a global U(1) continuous symmetry
associated with the conservation of some quantum number, and introduced a complex scalar
field to break it spontaneously. The Goldstone bosons arising from the symmetry breaking
would be massless or nearly massless, and their characteristic derivative coupling would make
them very weakly-interacting at sufficiently low temperatures. The latter property is crucial,
since the Goldstone bosons must decouple from the early universe thermal bath at the right
moment so that their temperature is a fraction of that of the neutrinos (see e.g. ref. [44].) We
have examined energy losses due to the emission of Weinberg’s Goldstone bosons in a post-
collapse supernovae core [45], while collider phenomenology has been investigated in ref. [46].
In this work we scrutinise the production and propagation of Weinberg’s Goldstone bosons in
the initial fireballs of gamma-ray bursts. In section 2 we briefly summarise generic properties
of the GRB fireball model. We then review Weinberg’s Higgs portal model and existing
laboratory constraints on it in section 3. In section 4 we calculate energy loss rates due to
Goldstone boson production by electron-positron annihilation, photon scattering, and nuclear
bremsstrahlung processes taking place in GRB initial fireballs. Subsequently in section 5 we
estimate the mean free path of the Goldstone bosons, which is set by their scattering on the
electrons/positrons and nucleons. In section 6 we use relativistic hydrodynamics to study the
effects of the Goldstone bosons, and confront the results with existing laboratory constraints.
In section 7 we summarise.
2 The GRB fireball model

2.1 The fireball mechanism

From the correlation of the GRB duration with the progenitor environment, it is believed that the long duration GRBs result from a collapsar, and the short GRBs from merger. In either case, relativistic outflows are powered by the central black hole or neutron star, which is surrounded by an accretion disc formed by the inwardly spiraling instellar material. Two most discussed jet production mechanisms are electromagnetic extraction of the black hole rotation energy [47], and pair annihilation of neutrinos that emanate from the accretion disc [48–50] (see also ref. [51] for a combination of both.) The outcome is a large amount (of order of the solar rest mass) of gravitational energy released within a short time, from a small region, which leads to the formation of an $e^\pm$-$\gamma$ fireball. A fraction of the gravitational energy is converted into neutrinos and gravitational waves. The thermal neutrinos are sensitive to the thermodynamics profiles of the accretion disc, while gravitational waves are sensitive to the dynamics of the progenitors. The Super-Kamiokande [52] and Sudbury Neutrino Observatory (SNO) [53] experiments have searched for MeV-neutrinos from the long and short GRBs. From the non-detection they have put upper limits on the GRB neutrino fluence.

A much smaller fraction goes into the fireball of temperature in the MeV range, which consists of $e^\pm$, photons and baryons, and may contain a comparable amount of magnetic field energy. The initial photon luminosity inferred is many orders of magnitude larger than the Eddington limit, i.e. the radiation pressure far exceeds the gravitational force, so the fireball will expand. For a steady spherically symmetrical flow with four velocity $w^\mu = (u^0, u^R, 0, 0)$ in the spherical coordinates $(t, R, \theta, \phi)$, the equations of relativistic fluid dynamics are [37]

\[
\frac{p + \rho}{n_B} u^0 = \text{const.}, \quad \frac{1}{R^2} \frac{\partial}{\partial R} (R^2 n_B u^R) = 0. \tag{2.1}
\]

Here $n_B$ is the baryon number density, and $p$ and $\rho$ are the pressure and the total energy density, respectively. All the three quantities are measured in the fluid comoving frame. The components of the flow four-velocity are $u^0 = \sqrt{-g_{00}} \Gamma$ and $u^R = \beta \Gamma / \sqrt{g_{RR}}$, with $\beta$ and $\Gamma$ its three-velocity an Lorentz factor, $\Gamma = 1 / \sqrt{1 - \beta^2}$. If the gravitational effects of the wind itself are negligible, the metric is $-g_{00} = g_{RR}^{-1} = 1 - R_S / R$, where $R_S$ is the Schwarzschild radius of the central object. The hydrodynamic equations need to be supplemented with an equation of state, e.g. $p = \rho/3$. As long as the constituents of the fireball plasma are strongly coupled, they are in thermal equilibrium, and the fireball expansion is adiabatic. Combining with the equation of adiabatic process $pn_B^{\gamma - 1} = \text{const.}$, with $\gamma = 4/3$, one arrives at the equation for the evolution of the Lorentz factor of the wind:

\[
\Gamma \propto R \quad \text{for } R \ll R_{\text{sat}}, \quad \Gamma \simeq \Gamma_l \quad \text{for } R \gg R_{\text{sat}}. \tag{2.2}
\]

Here $R_{\text{sat}}$ and $\Gamma_l$ are the saturation values for the fireball radius and the fireball Lorentz factor, respectively. If magnetic fields are included as an additional component of the GRB fireball, the Lorentz factor evolution is modified to $\Gamma(R) \propto R^\mu$ for $R < R_{\text{sat}}$, and $\Gamma \simeq \text{const.}$ for $R_{\text{sat}} < R < R_{\text{dec}}$. Here $1/3 \leq \mu \leq 1$, with $\mu = 1$ corresponding to the baryon dominated jet, and $\mu = 1/3$ to a magnetic field dominated jet [35, 54].

In any case, the Lorentz factor first increases with the radius $R$. When $R$ reaches $R_{\text{sat}} \sim 10^9$ cm, the fireball enters the coasting phase, with all the fireball thermal energy converted into the kinetic energy of the baryons. The fireball continues expanding at a constant rate
until it runs into the external medium and slows down. At the deceleration radius $R_{\text{dec}} \sim 10^{16}$ cm, the deceleration of the fireball expansion becomes significant. Correspondingly, the fireball comoving temperature evolves as $T' \propto R^{-1.5}$ for $R < R_{\text{sat}}$, and $\propto R^{-2/3}$ when $R_{\text{sat}} < R < R_{\text{dec}}$.

The bulk Lorentz factor $\Gamma$ can be measured [55–57], and lower limits on the Lorentz factor have been inferred by requiring that the GRBs be optically thin to high energy photons [58]. Ref. [10] deduced $\Gamma_{\text{min}} = 608 \pm 15$ and $887 \pm 21$ for GRB 080916C, while $\Gamma_{\text{min}} \approx 1200$ for the short gamma-ray burst GRB 090510. The saturation value for the Lorentz factor is determined by the initial ratio of radiation energy to rest mass

$$\eta_B \equiv \frac{\mathcal{E}}{M_0}. \tag{2.3}$$

This ratio must be of the order $\sim \mathcal{O}(10^2)$, so that the baryons may be accelerated to a Lorentz factor $\Gamma \approx E/M_0$ high enough to produce the observed gamma-rays. On the other hand, if the ratio is too large, the fireball is radiation-dominated. Depending on its value, there are four types of fireballs. We consider the most interesting case, the relativistic baryonic fireball, which corresponds to the case $1 < \eta_B < (3\sigma_T E/8\pi m_p R_0^3)^{1/3} \approx 10^5 (E/10^{52}$ ergs$)^{1/3} (R_0/10^7$ cm$)^{-2/3}$ [31, 32], where $\sigma_T$ is the Thompson cross section, and $m_p$ the proton mass.

Within the fireball model, there are many mechanisms proposed to explain the GRB observations. In the internal-external scenario, the prompt emission is produced by the internal shocks [59], and the afterglow by the external shocks. Under the assumption that the central engine produces ejecta shells with a highly variational distribution of Lorentz factor, the internal shocks are formed when the faster shells catch up with the slower ones. The external shocks arises when the fireball expands into external medium. For a summary or review of the GRB fireball model, we refer to refs. [4, 5, 32–35].

### 2.2 Generic GRB fireball parameters

In this work we consider the following generic parameters for the GRB fireballs as ref. [36]: the initial fireball energy is $\mathcal{E} = 10^{52}–10^{54}$ ergs. The initial radius is that of the Schwarzschild radius $R_S = 3 (M/M_\odot)$ km, or of the neutron star radius $\sim 10$ km. The initial wind velocity is about the sound speed, $\beta_0 \approx c_s = 1/\sqrt{3}$. In thermal equilibrium, the radiation energy density and the temperature is related by

$$\frac{\mathcal{E}}{V} = \frac{\pi^2}{30} g_* T^4. \tag{2.4}$$

The total number of effective massless degrees of freedom is

$$g_* \equiv \sum_{i=\text{bosons}} g_i \left(\frac{T_i}{T}\right)^4 + \frac{7}{8} \sum_{i=\text{fermions}} g_i \left(\frac{T_i}{T}\right)^4, \tag{2.5}$$

with $g_i$ the internal degrees of freedom of particle species $i$, and $T_i$ its temperature. In the initial fireball, photons, electrons, positrons, as well as three flavours of neutrinos are in thermal equilibrium, so $g_* = 43/4$. Assuming that the initial fireball is spherical, its temperature can be expressed by

$$\left(T_{11}\right)^4 = \frac{200}{g_*} \frac{\mathcal{E}_{52}}{(R_{6.5})^3}, \tag{2.6}$$

$$-4-$$
where \( T = T_{11} \cdot 10^{11} \) K, \( E = E_{52} \cdot 10^{52} \) erg, and \( R = R_{6.5} \cdot 10^{6.5} \) cm. We therefore follow ref. [36] to choose

\[
E = 10^{52} \text{ erg}, \quad R_0 = 10^{6.5} \text{ cm}, \quad T_0 = 2.1 \cdot 10^{11} \text{ K} = 18 \text{ MeV},
\]

as our fiducial value for the initial fireball total energy, radius and temperature, respectively. In view of the recent results in ref. [57], we also consider larger initial radius, e.g. \( R_0 = 10^{7} - 10^8 \) cm, and lower initial fireball temperature, values, such as \( T_0 = 8 \) and 2 MeV.

It was shown (see e.g. ref. [60]) that the sonic point of a Schwarzschild black hole should be located at the radius \( R_c = \frac{3}{2} R_S \), if the particles in the in- and outflow are relativistic so that the equation of state is \( p = \rho/3 \). In the case that the GRB jets are formed by energy injection from neutrino pair annihilation, the sonic point of the inflow, \( R_{c,1} < \frac{3}{4} R_S \) (where \( \beta_{c,1} = -\frac{1}{\sqrt{3}} \)), and that of the outflow, \( R_{c,2} > \frac{3}{2} R_S \) (where \( \beta_{c,2} = -\frac{1}{\sqrt{3}} \)), are separate. In ref. [60] the location of the outer sonic point is shown for several different energy injection profiles, which is pushed out well above that of the adiabatic flow (\( R_c = \frac{3}{2} R_S \)) in all cases (see also ref. [37].) In this work we choose

\[
\beta_0 (R = R_0) = \epsilon_s = \frac{1}{\sqrt{3}},
\]

as the fiducial value for the fireball initial wind velocity.

Since the initial temperature is higher than the nuclear binding energies, the nuclei are dissociated in nucleons. Requiring \( \eta_B \sim 1000 \) for the initial energy to rest mass ratio defined in eq. (2.3), the initial comoving baryon number density in the fireballs should be

\[
n_{B,0} = 5 \cdot 10^{31} \text{ cm}^{-3},
\]

so that the fireball rest mass \( M_0 = m_N n_{B,0} V_0 \approx 10^{49} \) ergs. The electron and the positron number density are

\[
n_{e\pm} = 2 \int f_{e\pm}(\vec{p}_e) \frac{d^3\vec{p}_e}{(2\pi)^3},
\]

with their phase space distribution functions given by \( f_{e^-}(\vec{p}_e) = \left( e^{(E_e^- - \mu_e)/T} + 1 \right)^{-1} \) and \( f_{e^+}(\vec{p}_e^+) = \left( e^{(E_e^+ + \mu_e)/T} + 1 \right)^{-1} \), respectively. The \( e^\pm \) chemical potential \( \mu_e \) is determined by the requirement of charge neutrality and beta-equilibrium in the fireball for a fixed lepton fraction \( Y_e \). For the reference temperature, it is \( \mu_e/T_0 \sim 2 \times 10^{-4} \) [36], i.e. the electrons and positrons are non-degenerate, so

\[
n_{e\pm,0} = \frac{3}{4} \frac{\zeta(3)}{\pi^2} 2T^3 = 1.4 \cdot 10^{35} \left( \frac{T}{18 \text{ MeV}} \right)^3 \text{ cm}^{-3},
\]

with \( \zeta(3) \approx 1.20206 \). Neutrinos are created rapidly in the initial fireball, majorly through the electron-positron pair annihilation process \( e^- + e^+ \rightarrow \nu + \bar{\nu} \). The emissivity for this process is [36, 61]

\[
Q_{e^- e^+ \rightarrow \nu \bar{\nu}} = 3.6 \cdot 10^{33} (T_{11})^9 \text{ erg s}^{-1} \text{ cm}^{-3},
\]

much larger than that for the photo-neutrino \( e^\pm + \gamma \rightarrow e^\pm + \nu_i + \bar{\nu}_i \), the plasma \( \gamma \rightarrow \nu_i \bar{\nu}_i \), and the URCA processes \( e^- + p \rightarrow n + \nu_e \) and \( e^+ + n \rightarrow p + \bar{\nu}_e \). Neutrino mean free path (mfp) is set by the elastic scattering on electrons and positrons \( \nu + e^\pm \rightarrow \nu + e^\pm \). It is [36]

\[
\lambda(e) = 3.7 \cdot 10^6 (T_{11})^{-5} \text{ cm}, \quad \lambda(\mu, \tau) = 1.6 \cdot 10^7 (T_{11})^{-5} \text{ cm},
\]
for the three flavours, respectively. Neutrinos decouple in two stages, when the optical depth \( \tau \equiv R/\lambda \) for each neutrino flavour, \( \tau^{(\mu, \tau)} \) and \( \tau^{(e)} \), drops to 1.

In this work we consider a baryon dominated fireball jet, and neglect the effects of the magnetic fields.

3 Goldstone bosons from Weinberg’s Higgs portal model

3.1 The model

In this subsection we briefly summarise Weinberg’s model [43] following the convention of refs. [45, 46]. Consider the simplest possible broken continuous symmetry, a global \( U(1) \) symmetry associated with the conservation of some quantum number \( W \). A single complex scalar field \( S(x) \) is introduced for breaking this symmetry spontaneously. With this field added to the Standard Model (SM), the Lagrangian is

\[
L = \left( \partial_\mu S^\dagger \right) \left( \partial^\mu S \right) + \mu^2 S^\dagger S - \lambda (S^\dagger S)^2 - g (S^\dagger S) (\Phi^\dagger \Phi) + L_{\text{SM}},
\]

where \( \Phi \) is the SM Higgs doublet, \( \mu, g, \) and \( \lambda \) are real constants, and \( L_{\text{SM}} \) is the usual SM Lagrangian. One separates a massless Goldstone boson field \( \alpha(x) \) and a massive radial field \( r(x) \) in \( S(x) \) by defining

\[
S(x) = \frac{1}{\sqrt{2}} \left( \langle r \rangle + r(x) \right) e^{2i\alpha(x)},
\]

where the fields \( \alpha(x) \) and \( r(x) \) are real. In the unitary gauge, one sets \( \Phi^\dagger = \left( 0, \langle \varphi \rangle + \varphi(x) \right) / \sqrt{2} \) where \( \varphi(x) \) is the physical Higgs field. The Lagrangian in eq. (3.1) thus becomes

\[
L = \frac{1}{2} (\partial_\mu r) (\partial^\mu r) + \frac{1}{2} \left( \frac{\langle r \rangle + r}{\langle r \rangle} \right)^2 (\partial_\mu \alpha) (\partial^\mu \alpha) + \frac{\mu^2}{2} (\langle r \rangle + r)^2 - \frac{\lambda}{4} (\langle r \rangle + r)^4 - \frac{g}{4} (\langle r \rangle + r)^2 (\langle \varphi \rangle + \varphi)^2 + L_{\text{SM}},
\]

where the replacement \( \alpha(x) \to \alpha(x) / (2 \langle r \rangle) \) was made in order to achieve a canonical kinetic term for the \( \alpha(x) \) field. In this model, the interaction of the Goldstone bosons with the SM particles arises entirely from a mixing of the radial boson with the Higgs boson. The mixing angle is

\[
\tan 2\theta = \frac{2g \langle \varphi \rangle \langle r \rangle}{m_\varphi^2 - m_r^2}.
\]

Collider searches for the SM Higgs invisible decay as well as meson invisible decays have already been used to set strong constraints on the coupling \( g \) and/or the mixing angle \( \theta \), as will be reviewed in the next subsection.

As will be presented in section 4, Goldstone boson emissivities in the GRB initial fireballs depends strongly on the total decay width of the radial field \( r \). The \( r \) field decays dominantly to a pair of Goldstone bosons, with the decay width given by

\[
\Gamma_{r \to \alpha \alpha} = \frac{1}{32\pi} \frac{m_r^3}{\langle r \rangle^2}.
\]

However, if its vacuum expectation value \( \langle r \rangle \) is very large and the coupling \( g \) is not too small, the decay widths into SM fermion pairs

\[
\Gamma_{r \to f \bar{f}} = \left( \frac{g \langle \varphi \rangle \langle r \rangle}{m_r^2 - m_\varphi^2} \right)^2 \frac{N_c m_f^2 m_r}{8\pi \langle \varphi \rangle^2} \left( 1 - \frac{4m_f^2}{m_r^2} \right)^{3/2},
\]

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Figure 1. Decay widths for the $r$ field to Goldstone boson pairs (solid), fermion pairs (dashed), and pion pairs (dotted), assuming $g = 0.011$ and $\langle r \rangle = 1$ GeV.

can be comparable or even dominant. Here $m_f$ and $N_c$ are the mass and the colour factor of the fermion, respectively. For $m_r > 2m_\pi$, the $r$ field can also decay to pion pairs through the effective coupling of the SM Higgs to pions $\langle \pi^+\pi^-|\mathcal{L}_{\text{int}}|\varphi \rangle$. The effective Lagrangian is [62–64]

$$\mathcal{L}_{\text{int}} = -\frac{\varphi}{\langle \varphi \rangle} \left\{ \frac{2}{9} \theta_\mu^\mu + \frac{7}{9} \sum_{i=u,d,s} m_i \bar{\phi}_i \phi_i \right\} ,$$

(3.7)

where $\theta_\mu^\mu$ is the trace of the energy-momentum tensor, valid only at low momentum transfers $\lesssim 0.3$ GeV (see e.g. the discussion in ref. [44].) The decay width is then

$$\Gamma_{r \rightarrow \pi^+\pi^-} = \left( \frac{g \langle \varphi \rangle \langle r \rangle}{m_r^2 - m_\pi^2} \right)^2 \left( \frac{2}{9} \right)^2 \left( \frac{m_r^2 + \frac{11}{2} m_\pi^2}{16\pi m_r} \right)^2 \left( 1 - \frac{4m_\pi^2}{m_r^2} \right)^{1/2} .$$

(3.8)

In figure 1 the three decay widths are shown for the case of $\langle r \rangle = 1$ GeV, $g = 0.011$. The decay widths for other parameter values can be easily obtained by scaling with $g^2$ or $\langle r \rangle^2$.

In the GRB fireballs, the Goldstone bosons can also be produced by nuclear processes and undergo elastic scattering with the nucleons through the $\varphi-r$ mixing. The Higgs effective coupling to nucleons, $f_N m_N / \langle \varphi \rangle$, has been calculated for the purpose of investigating the sensitivities of the dark matter direct detection experiments [65–68]. Following the Shifman-Vainshtein-Zakharov approach [69] to evaluate the contributions from the heavy quarks, it can be written in the form

$$f_N = \sum_{q=u,d,s,c,b,t} m_q \frac{m_N}{m_q} \langle N|\bar{q}q|N \rangle = \sum_{q=u,d,s} f_{Tq} + \frac{2}{9} \left[ 1 - \sum_{q=u,d,s} f_{Tq} \right] .$$

(3.9)

The authors of ref. [68] have done a statistical analysis to infer the value of $f_N$ in the light of recent lattice evaluations of the nucleon matrix elements. By exploiting two possible
statistical distributions for the strangeness matrix element, they found $f_N = 0.3 \pm 0.03$ and $f_N = 0.3 \pm 0.01$ at the 68% confidence level. Other estimates, e.g. that from ref. [67], are in agreement with those results.

3.2 Laboratory constraints

3.2.1 Collider searches for SM Higgs invisible decay

The non-standard decay branching ratio of the SM Higgs is constrained to $\Gamma_{h \rightarrow \text{inv}} < 0.97$ MeV at the 95% confidence level (corresponding to a branching ratio < 19%) by the results of a global fitting to the most updated data from the CMS and ATLAS experiments at the Large Hadron Collider (LHC), as well as those from the Tevatron [70]. In Weinberg’s Higgs portal model, the SM Higgs can decay into a pair of Goldstone bosons or a pair of the radial field $r$, with the decay widths given by

$$
\Gamma_{\phi \rightarrow \alpha \alpha} = \frac{1}{32\pi} \frac{g^2 \langle \phi \rangle^2 m^3_{\phi}}{(m^2_{\phi} - m^2_{\alpha})^2}, \quad \text{and} \quad \Gamma_{\phi \rightarrow rr} = \frac{g^2 \langle \phi \rangle^2}{32\pi} \sqrt{m^2_{\phi} - 4m^2_r m^2_{\phi}} m^2_{\phi},
$$

respectively. The constraint is translated into a bound on the Goldstone boson coupling of

$$
|g| < 0.011.
$$

In the future, the International Linear Collider (ILC) may reach a sensitivity of constraining the branching ratio of SM Higgs invisible decays to $< 0.4$–0.9% [71] in the best scenarios. If this can be realised, the collider bound on the Goldstone boson coupling will be improved by a factor of $5 \sim 7$. In this work we will estimate the effects of the Goldstone bosons on the initial GRB fireballs for the coupling in the range $0.011 < g > 0.0015$.

3.2.2 Muon anomalous magnetic moment

There is still a discrepancy between the SM prediction for the muon anomalous magnetic moment [72], $a^\text{SM}_\mu$, and the experimental results from the E821 experiment at Brookhaven National Lab (BNL) [73], $a^\text{exp}_\mu = 11 659 209(5.4)(3.3) \cdot 10^{-10}$, where the first errors are statistical and the second systematic. The observed difference of [74]

$$
\Delta a_\mu = a^\text{exp}_\mu - a^\text{SM}_\mu = 288(63)(49) \cdot 10^{-11},
$$

may point to new physics beyond the Standard Model. The contribution from the SM Higgs was first calculated in ref. [75]. The radial $r$ field can contribute to $\Delta a_\mu$ through its mixing with the SM Higgs [76]

$$
\Delta a^r_\mu = \theta^2 \frac{G_F m^2_{\mu}}{4\pi^2 \sqrt{2}} \int_0^1 dy \frac{y^2 (2-y)}{y^2 + (1-y) \left( \frac{m_r}{m_{\mu}} \right)^2},
$$

where $G_F$ is the Fermi constant. By demanding $\Delta a^r_\mu < \Delta a_\mu$ one obtains a very weak constraint on the mixing angle: $\theta \lesssim O(1)$. 
3.2.3 Radiative Upsilon decays

As first pointed out by Wilczek [77], light Higgs boson can be searched for in the radiative decays of heavy vector mesons. In Weinberg’s Higgs portal model, the branching ratio is

\[
\frac{\mathcal{B}(\Upsilon(nS) \to \gamma + r)}{\mathcal{B}(\Upsilon(nS) \to \mu^+\mu^-)} = \frac{\theta^2 G_F m_b^2}{\sqrt{2 \pi} \alpha} \left(1 - \frac{m_r^2}{m_{\Upsilon(nS)}^2}\right) \times F, \tag{3.14}
\]

for \( n = 1, 2, 3 \), where \( \alpha \) is the fine structure constant, and \( m_b \) the \( b \) quark mass. The correction factor \( F \) includes QCD and relativistic corrections (see e.g. refs. [64, 76, 78].)

For \( m_r \ll m_{\Upsilon} \), \( F \sim 0.5 \) is generally assumed. The BaBar Collaboration has set 90\% C.L. upper limits on \( \mathcal{B}(\Upsilon(1S) \to \gamma A^0) \times \mathcal{B}(A^0 \to \text{invisible}) \) in the range \((1.9 - 37) \cdot 10^{-6}\) for \( m_{A^0} < 9.2 \text{ GeV} \) [79], as well as on \( \mathcal{B}(\Upsilon(3S) \to \gamma A^0) \times \mathcal{B}(A^0 \to \text{invisible}) \) in the range \((0.7 - 31) \cdot 10^{-6}\) for \( m_{A^0} < 9.2 \text{ GeV} \) [80], where \( A^0 \) is a scalar boson. In this work we consider mass of the radial field \( r \) below 1 GeV, for which

\[
\mathcal{B}(\Upsilon(nS) \to \gamma + r) < 3 \cdot 10^{-6}, \tag{3.15}
\]

for \( n = 1 \) and \( 3 \). This is translated into a constraint on Weinberg’s Higgs portal model as \( \theta < 0.2 \).

3.2.4 \( B \) meson and kaon decays

As first pointed out in ref. [81], decays of \( B \) mesons to a \( K \) meson plus missing energy can be an efficient probe of GeV or sub-GeV scalar dark matter. In refs. [76, 82] this constraint has been applied to Weinberg’s Higgs portal model. The BaBar Collaboration has reported an upper limit at the 90\% confidence level on \( \mathcal{B}(B^+ \to K^+ + \nu \bar{\nu}) < 1.3 \cdot 10^{-5} \), as well as \( \mathcal{B}(B^0 \to K^0 + \nu \bar{\nu}) < 5.6 \cdot 10^{-5} \) [83]. The CLEO Collaboration also reported a 90\% C.L. upper limit of \( 4.9 \cdot 10^{-5} \) and \( 5.3 \cdot 10^{-5} \) on the branching ratio for the decays \( B^\pm \to K^\pm X^0 \) and \( B^0 \to K^0 X^0 \), respectively, where \( X^0 \) is any neutral massless weakly-interacting particle [84]. In the SM, the branching ratio for the total \( \mathcal{B}(B \to K \nu \bar{\nu}) \) branching ratio is estimated to be \( (4.5 \pm 0.7) \cdot 10^{-6} \). In Weinberg’s Higgs portal model, this branching ratio is [76, 82]

\[
\mathcal{B}(B^+ \to K^+ + r) = \frac{9\sqrt{2} \tau_B G_F^3 m_t^4 m_b^2 m_s^2 m_{K^0}^2}{1024 \pi^3 m_B^2} \left| V_{tb} V^*_{ts} \right|^2 \left[ f_{0BK}^B \left( m_r^2 \right) \right]^2 \times \sqrt{(m_{K^0}^2 - m_r^2)} \left( m_s^2 - m_r^2 \right) \theta^2, \tag{3.16}
\]

with the form factor given by

\[
f_{0BK}^B(x) \equiv 0.33 \exp \left( \frac{0.63 x}{m_B^2} - \frac{0.095 x^2}{m_B^4} + \frac{0.591 x^3}{m_B^6} \right), \tag{3.17}
\]

and \( \tau_B \) is the \( B \)-meson lifetime, \( V_{tb} \) and \( V_{ts} \) the CKM matrix elements, and \( m_t, m_b, m_s, m_B \) and \( m_K \) the corresponding quark and meson masses, with \( m_\pm \equiv m_B \pm m_K \). We follow ref. [82] and use the most stringent constraint

\[
\mathcal{B}(B^+ \to K^+ + r) < 10^{-5}, \tag{3.18}
\]

which imposes a constraint on the \( \varphi - \tau \) mixing angle that \( \theta < 0.0016 \), for \( m_r < m_B - m_K \).

If the radial field \( r \) is lighter than 354 MeV, the decay of \( K \) meson to a \( \pi \) meson plus missing energy is a more powerful probe. The E787 and E949 experiments at the BNL has
used stopped kaons to study the rare decay $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ [85]. The branching ratio $\mathcal{B}(K^+ \rightarrow \pi + \nu \bar{\nu}) = (1.73^{+1.15}_{-1.05}) \cdot 10^{-10}$ determined with the observed seven events and background estimation is consistent with the SM prediction of $7.8(75)(29) \cdot 10^{-11}$ [86, 87], where the first error summarises the parametric, and the second the remaining theoretical uncertainties. For $K^+$ meson decay into the radial $r$ field, the branching ratio can be calculated similarly as in eq. (3.16), using the form factor (see e.g. ref. [82]),

$$ f_0^{K\pi}(x) \approx 0.96 \left( 1 + 0.02 \frac{x}{m_\pi^2} \right), \quad (3.19) $$

In this work we follow refs. [76, 82] and use the constraint

$$ \mathcal{B}(K^+ \rightarrow \pi^+ + r) < 10^{-10}, \quad (3.20) $$

which imposes a very stringent constraint on the mixing angle as $\theta < 8.7 \cdot 10^{-5}$, for $m_r < m_K - m_\pi = 354$ MeV.

Laboratory constraints from muon anomalous magnetic moment, radiative upsilon decays, as well as $B^+$ and $K^+$ invisible decays are plotted in figure 2, in terms of upper limits on $g(r)$, the product of the Goldstone boson coupling times the vev of the $r$ field, versus its mass $m_r$ (cf. eq. (3.4)).

### 4 GRB energy losses due to Goldstone boson production

The Goldstone bosons can be produced in electron-positron pair annihilation $e^+ + e^- \rightarrow \alpha + \alpha$, photon scattering $\gamma + \gamma \rightarrow \alpha + \alpha$, as well as in nuclear bremsstrahlung processes $N + N \rightarrow N + N + \alpha + \alpha$.

#### 4.1 Electron-positron pair annihilation

The amplitude squared for $e^+(p_1) e^-(p_2) \rightarrow \alpha(q_1) \alpha(q_2)$ is

$$ \sum_{\text{spins}} |\mathcal{M}_{e^+e^-\rightarrow\alpha\alpha}|^2 = \frac{2g^2m_\pi^2}{m_\alpha^4}s^2(s - 4m_\Pi^2)(s - m_\Pi^2)^2 + m_\Pi^2\Gamma_\alpha^2, \quad (4.1) $$

where $s = (p_1 + p_2)^2 = (q_1 + q_2)^2$ is the centre-of-mass (cm) energy. Here we have used the Breit-Wigner form to take into account the resonance effect, with the $r$ field total decay width $\Gamma_r = \Gamma_{r\rightarrow\alpha\alpha} + \sum_{j=2m_f<m_\pi} \Gamma_{r\rightarrow jj} + \Gamma_{r\rightarrow \pi^+\pi^-}$ (cf. figure 1).

The energy loss rate due to Goldstone boson production in the GRB fireball comoving frame is

$$ Q_{e^+e^-\rightarrow\alpha\alpha} = \frac{1}{2!} \int \prod_{j=1}^2 \frac{d^3\vec{q}_j}{(2\pi)^3} \frac{d^3\vec{p}_j}{2\omega_j} \int \prod_{i=1}^2 \frac{2d^3\vec{p}_i}{(2\pi)^3} \frac{1}{2E_i / 4} \sum_{\text{spins}} |\mathcal{M}_{e^+e^-\rightarrow\alpha\alpha}|^2 $$

$$ \times (2\pi)^4 \delta^4(p_1 + p_2 - q_1 - q_2) f_{e^+} f_{e^-} (\omega_1 + \omega_2), \quad (4.2) $$

where $f_{e^+}(\vec{p}_1)$ and $f_{e^-}(\vec{p}_2)$ are the electron and positron distribution function, respectively, as given below eq. (2.10). The energy of the two Goldstone bosons in the final state are denoted by $\omega_1$ and $\omega_2$, while the energy of the positron and electron in the initial state by $E_1$ and $E_2$. A symmetry factor of $1/2!$ is included for the two identical particles in the final state.
Figure 2. Upper limits on $g\langle r\rangle$, the product of the coupling with the vev of the radial field $r$, versus its mass $m_r$, from the energy loss rate in the GRB initial fireball, eq. (6.9). The initial fireball temperature is chosen at the fiducial value $T_0 = 18$ MeV (lower solid line), as well as lower value $T_0 = 8$ MeV (upper solid line), the initial radius at $R_0 = 10^{6.5}$ cm, and the fireball energy at $E = 10^{52}$ erg. Here we assume that the Goldstone boson coupling saturates the collider bound of $g = 0.011$. For a smaller coupling $g = 0.0015$ which might be probed by future collider experiments, the upper limits are less stringent for $m_r > 240$ MeV if $T_0 = 18$ MeV (lower dashed line), or for $m_r > 70$ MeV if $T_0 = 8$ MeV (upper dashed line). The uncertainties in these GRB upper limits resulting from the error in the energy loss criterion $Q_X$ are indicated by the filled regions. Taking into account the uncertainty in $T_0$, we find that the region bounded by the two curves, including the filled regions, represents the parameter space in Weinberg’s Higgs portal model that can be probed by GRB physics. Also shown are the upper limits from laboratory constraints, such as the muon anomalous magnetic moment $\Delta a_{\mu}$, radiative Upsilon decays $\Upsilon(nS) \rightarrow \gamma + r$, $B^+ \rightarrow K^+ + r$, as well as $K^+ \rightarrow \pi^+ + r$ (dash-dotted lines, from top to bottom.) The supernova bound we obtained in ref. [45] in the large $m_r$ limit, here for the case $\langle r\rangle = 1$ GeV (dotted line), is indicative of the competitiveness and complementarity of the astrophysical constraints.

One can perform the $d^3q_1 d^3q_2$ integral analytically analogous to the Lenard’s Identity [88] for the $e^+e^- \rightarrow \nu\bar{\nu}$ process,

$$\int \frac{d^3q_1}{\omega_1} \frac{d^3q_2}{\omega_2} \delta^4 (p_1 + p_2 - q_1 - q_2) = 2\pi. \quad (4.3)$$

We use the Maxwell-Boltzmann statistics for the electron and positron distribution function, and make a change of integration variables from $E_1$, $E_2$, and $\cos \theta$, to $E_+ \equiv E_1 + E_2$, $E_- \equiv E_1 - E_2$, and $s = 2m_e^2 + 2E_1E_2 - 2|\vec{p}_1||\vec{p}_2|\cos \theta$. The $dE_-$ integral can be performed easily,

$$\int_{E_-}^{E_{-\text{max}}} dE_- = 2\sqrt{1 - \frac{4m_e^2}{s}} \sqrt{E_+^2 - s}. \quad (4.4)$$

Defining $x \equiv E_+ / \sqrt{s}$, $z \equiv s/T^2$, $z_r \equiv m_r^2/T^2$, $z_\Gamma \equiv \Gamma_r^2/T^2$, and $z_0 \equiv 4m_e^2/T^2$, the energy loss
rate is reduced to the simple form

\[
Q_{e^+e^-\rightarrow\alpha\alpha} = \frac{T^7}{16(2\pi)^5} \frac{g^2 m_e^2}{m_\gamma^4} \int_{z_0}^{\infty} dz \frac{z^{9/2} (1 - \frac{z_0}{z})^{3/2}}{(z - z_r)^2 + z_r \sqrt{z}} \int_1^{\infty} dx \ e^{-\sqrt{x}z} x \sqrt{x^2 - 1},
\]

which we evaluate numerically using the VEGAS Monte Carlo integration subroutine [89]. In the resonance region \( z \sim z_r \), we simplify the \( dz \) integral by taking limit of the Poisson kernel

\[
\lim_{\epsilon \to 0} \frac{1}{\pi a^2} = \delta(a).
\]

Therefore the \( dz dx \) integral part can be approximated by

\[
I(T, m_r, \langle r \rangle) \approx \frac{z_r^{9/2}}{\sqrt{z_r \sqrt{z}}} \frac{\pi^{3/2}}{\Gamma_r m_r} m_r^5 \int_1^{\infty} dx \ e^{-\sqrt{x}z} x \sqrt{x^2 - 1},
\]

for \( z \sim z_r \) and \( m_r \Gamma_r \ll T^2 \). The results for \( T_0 = 18 \) MeV and various \( m_r, \langle r \rangle \) values are shown in figure 3. In the resonance region,

\[
Q_{e^+e^-\rightarrow\alpha\alpha} \propto \frac{\Gamma_r \rightarrow e^+e^- \Gamma_r \rightarrow \alpha\alpha m_r^5}{m_\gamma^4} \int_1^{\infty} dx \ e^{-\frac{m_r x}{\sqrt{x}} x \sqrt{x^2 - 1}}.
\]

One sees that for a given \( m_r \), the Goldstone boson emissivity is enhanced significantly due to the resonance effect as \( Q_{e^+e^-\rightarrow\alpha\alpha} \propto \langle r \rangle^2 \), as long as \( \Gamma_r \rightarrow ff \ll \Gamma_r \rightarrow \alpha\alpha \). In figure 4 we show the Goldstone boson emissivity \( Q_{e^+e^-\rightarrow\alpha\alpha} \) for other GRB initial fireball temperatures than the fiducial value \( T_0 = 18 \) MeV, such as \( T_0 = 8 \) and \( 2 \) MeV. In the resonance region, the \( T \)-dependence arises solely from the \( dx \) integral. For very large \( m_r \) values away from the resonance region, the Goldstone boson emissivity depends very sensitively on the GRB fireball temperature as

\[
Q_{e^+e^-\rightarrow\alpha\alpha} \propto \left( \frac{g^2 m_e^2}{m_\gamma^4 m_r^4} \right) T^{11}.
\]

As will be presented in section 5, the opacity of the GRB fireballs to the Goldstone bosons depends strongly on the Goldstone boson energy. The Goldstone boson pairs are emitted with an average energy of

\[
\bar{\omega} = \frac{1}{T} \frac{Q_{e^+e^-\rightarrow\alpha\alpha}}{n_{e^-} n_{e^+} \langle \sigma_{e^+e^-\rightarrow\alpha\alpha} v_m \rangle},
\]

where \( \omega = \omega_1 + \omega_2 \), and \( v_m \) is the Møller velocity. The results for \( T_0 = 18 \) MeV and \( \langle r \rangle = 1, 10, \) and \( 100 \) GeV are shown in figure 5, while those for \( T_0 = 18, 8, \) and \( 2 \) MeV and \( \langle r \rangle = 1 \) GeV in figure 6. In the resonance region where the approximation with the Poisson kernel limit in eq. (4.7) is valid, the average energy of the Goldstone boson pairs is \( \bar{\omega} \propto m_r \). For large \( m_r \) values away from the resonance region, \( \bar{\omega}/T \) approaches a constant.

### 4.2 Photon scattering

The amplitude for the photon scattering process \( \gamma(p_1) \gamma(p_2) \rightarrow \alpha(q_1) \alpha(q_2) \) is

\[
\sum_{\text{pol.}} |\mathcal{M}_{\gamma\gamma\rightarrow\alpha\alpha}|^2 = \left( \frac{\alpha}{4\pi} \right)^2 \frac{G_F^2 F_\gamma^2 g^2 (\varphi)^2}{m_\gamma^4 (s - m_\gamma^2)^2 + m_\gamma^4 \Gamma_\gamma^2},
\]

where

\[
\varphi = \frac{s - 4m_\gamma^2}{2s},
\]

and

\[
\Delta = \frac{\sqrt{1 + 4s}}{2},
\]

and

\[
\Delta = \frac{\sqrt{1 - 4s}}{2},
\]

is the breit frame energy. The results for these are shown in figure 7. In the resonance region, the average energy of the Goldstone boson pairs is \( \bar{\omega} \propto m_r \). For large \( m_r \) values away from the resonance region, \( \bar{\omega}/T \) approaches a constant.
Figure 3. Energy loss rate due to Goldstone boson production from $e^- e^+ \rightarrow \alpha \alpha$ divided by the Goldstone boson coupling $g^2$ vs. the radial boson mass $m_r$. The GRB initial fireball temperature is set at the fiducial value $T_0 = 18$ MeV, and the vacuum expectation value of the radial boson is assumed to be $\langle r \rangle = 1, 10, \text{and } 100$ GeV (from bottom to top). Also shown is the energy loss rate for neutrino production, $Q_{\nu e^- e^+ \rightarrow \nu \bar{\nu}}$, at the same temperature $T_0$.

Figure 4. Energy loss rate due to Goldstone boson production from $e^- e^+ \rightarrow \alpha \alpha$ divided by the Goldstone boson coupling $g^2$ vs. the radial boson mass $m_r$. The GRB initial fireball temperature is chosen at the fiducial value $T_0 = 18$ MeV, as well as lower values $T_0 = 8$ and 2 MeV, where the vacuum expectation value of the radial boson is assumed to be $\langle r \rangle = 1$ GeV.
Figure 5. Average energy of the emitted Goldstone boson pairs from the process $e^-e^+ \rightarrow \alpha \alpha$ vs. the radial boson mass $m_r$. The GRB initial fireball temperature is chosen at the fiducial value $T_0 = 18$ MeV, where the vacuum expectation value of the radial boson is assumed to be $\langle r \rangle = 1, 10$ and 100 GeV.

Figure 6. Average energy of the emitted Goldstone boson pairs from the process $e^-e^+ \rightarrow \alpha \alpha$ vs. the radial boson mass $m_r$. The GRB initial fireball temperature is chosen at the fiducial value $T_0 = 18$ MeV, as well as at $T_0 = 8$ and 2 MeV, where the vacuum expectation value of the radial boson $\langle r \rangle$ is assumed to be 1 GeV.
where $\alpha$ and $G_F$ are the fine-structure constant and the Fermi constant, respectively. The form factor $F_\gamma$ enters through the amplitude for the SM Higgs decay to two photons, in this case a function of the centre-of-mass (cm) energy $\sqrt{s}$ in the photon collision. The cm energies attainable at the typical temperature of the initial GRB fireballs correspond to the mass of the light (sub-GeV) Higgs boson studied in refs. [90, 91]. For simplicity, we use a constant value of $|F_\gamma|^2 = 4$ to approximate the result of ref. [91]. The energy loss rate is then
denotes the pion-nucleon “fine-structure” constant. Goldstone boson pairs can also be emitted from the exchanged pion, and this contribution is of the same order as eq. (4.13) of the nucleons. Summing all diagrams and expanding in powers of $(T/m_N)$, the amplitude for the nuclear bremsstrahlung processes $N(p_1) N(p_2) \rightarrow N(p_3) N(p_4)\alpha(q_1)\alpha(q_2)$ is [45]

$$
Q_{\gamma\gamma\rightarrow N\alpha} = \frac{1}{32\sqrt{2}} \frac{T^9}{(2\pi)^5} \left( \frac{\alpha}{4\pi} \right)^2 G_F |F_\gamma|^2 \frac{g^2 \langle \phi \rangle^2}{m_{\phi}^4} \int_0^\infty dz \frac{z_{\gamma\gamma}^{(2)}}{(z - z_r)^2 + z_r z_T},
$$

where $x$, $z$, $z_r$, and $z_T$ are defined as in last subsection. In the resonance region, it can also be expressed in the form of eq. (4.8), with $\Gamma_{r\rightarrow\gamma\gamma}$ replaced by $\Gamma_{r\rightarrow\gamma\gamma}$. Since the branching ratio for $r \rightarrow \gamma\gamma$ is smaller than 10% of that for $r \rightarrow e^+e^-$ for $m_r \leq 200$ MeV, and becomes comparable only for $m_r \approx 500$ MeV, this process is always subdominant in the parameter space we consider in this work.

### 4.3 Nuclear bremsstrahlung processes

In the one-pion exchange (OPE) approximation (see e.g. ref. [92]), there are four direct and four exchange diagrams, corresponding to the Goldstone boson pairs being emitted by any one of the nucleons. Summing all diagrams and expanding in powers of $(T/m_N)$, the amplitude for the nuclear bremsstrahlung processes $N(p_1) N(p_2) \rightarrow N(p_3) N(p_4)\alpha(q_1)\alpha(q_2)$ is [45]

$$
\sum_{\text{spins}} |M_{NN\rightarrow N\alpha\alpha}|^2 \approx 64 \left( \frac{f_N g_{mN}}{m_{\pi}^2} \right)^2 \left( \frac{2m_N f_\pi}{m_\pi} \right)^4 \frac{(q_1 \cdot q_2)^2}{(q^2 - m_N^2)^2 + m_N^2 \Gamma_N^2} 
\left( \frac{|\vec{k}|^4}{(|\vec{k}|^2 + m_N^2)^2} + \frac{|\vec{l}|^4}{(|\vec{l}|^2 + m_N^2)^2} + \frac{|\vec{k}|^2 |\vec{l}|^2 - 2 |\vec{k} \cdot \vec{l}|^2}{(|\vec{k}|^2 + m_N^2) (|\vec{l}|^2 + m_N^2)} + \ldots \right),
$$

with $q \equiv q_1 + q_2$, and $k \equiv p_2 - p_4$ and $l \equiv p_2 - p_3$ are the 4-momenta of the exchanged pion in the direct and the exchange diagrams, respectively. Here, $\alpha_\pi \equiv (2m_N f_\pi/m_\pi)^2/(4\pi) \approx 15$, with $f_\pi \approx 1$ being the pion-nucleon “fine-structure” constant. Goldstone boson pairs can also be emitted from the exchanged pion, and this contribution is of the same order as eq. (4.13) in the $(T/m_N)$ expansion. We calculate the energy loss rate in the fireball comoving frame

$$
Q_{NN\rightarrow N\alpha\alpha} = \frac{S}{2!} \int \frac{d^3q_1}{2\omega_1 (2\pi)^3} \frac{d^3q_2}{2\omega_2 (2\pi)^3} \int \prod_{i=1}^4 \frac{d^3p_i}{2E_j (2\pi)^3} f_1 f_2 (1 - f_3)(1 - f_4)
\times \sum_{\text{spins}} |M_{NN\rightarrow N\alpha\alpha}|^2 (2\pi)^4 \delta^4(p_1 + p_2 - p_3 - p_4 - q_1 - q_2) (\omega_1 + \omega_2),
$$

where $\omega_1, \omega_2$ are the energy of the Goldstone bosons in the final state, and the distribution functions of the nucleons in the initial and the final state are given by $f_j(\vec{p}_j) = (n_B/2)(2\pi/m_N T)^{5/2} e^{-|\vec{p}_j|^2/2m_N T}$. The symmetry factor $S$ is $1/2$ for $nn$ and $pp$ interactions, whereas for $np$ interactions it is 1. We perform the integral over the Goldstone boson momenta first

$$
\int \frac{d^3q_1}{\omega_1} \frac{d^3q_2}{\omega_2} \frac{(q_1 \cdot q_2)^2}{(q^2 - m_N^2)^2 + m_N^2 \Gamma_N^2} \frac{(2q_2^2)^2}{(2p \cdot q)^7} \omega = \frac{2(2\pi)^2}{m_{\phi}^4} \int_0^\infty \frac{d\omega}{\omega^7} \omega^7 I_1(\omega, m_r, \langle r \rangle),
$$
where \( \omega = \omega_1 + \omega_2 \), and the dimensionless integral is

\[
I_1(\omega, m_r, \langle r \rangle) \equiv \int_0^1 d\tilde{\omega} \int_{-1}^{+1} \frac{d \cos \theta \tilde{\omega}^5 (1 - \tilde{\omega})^5 (1 - \cos \theta)^4}{2 \tilde{\omega} (1 - \tilde{\omega}) (1 - \cos \theta) - \frac{m_r^2}{m^2} \tilde{\omega}^4 + \frac{m_r^2 T^2}{\omega^4}}.
\]

(4.16)

Here \( \tilde{\omega} \equiv \omega_1/\omega \), and \( \theta \) is the angle between the two emitted Goldstone bosons. We evaluate eq. (4.16) numerically using the VEGAS subroutine, and then evaluate the integral in eq. (4.14) over the nucleon momenta following ref. [93]. In the non-relativistic limit the nucleon energies are just \( E_j = m_N + |\vec{p}_j|^2/2m_N \). To simplify the nucleon phase space integration, one introduces the centre-of-mass momenta \( \vec{P} \), so that \( \vec{p}_{1,2} = \vec{P} \pm \vec{p}_i \) and \( \vec{p}_{3,4} = \vec{P} \pm \vec{p}_f \), as well as \( z \equiv \vec{p}_i \cdot \vec{p}_f / |\vec{p}_i| |\vec{p}_f| \), the cosine of the nucleon scattering angle. The integral over \( d^3 \vec{P} \) can be done separately. After that one makes a change to dimensionless variables \( u \equiv \vec{p}_i^2/m_N T \), \( v \equiv \vec{p}_f^2/m_N T \), \( x \equiv \omega/T \), and \( y \equiv m_\pi^2/m_N T \). For simplicity we neglect the pion mass \( m_\pi \) inside the curly bracket in \( \sum_{\text{spins}} |\mathcal{M}_{NN \rightarrow N N\alpha\alpha}|^2 \), eq. (4.13), in comparison with the momentum transfer \( \vec{k} \) and \( \vec{l} \). The energy loss rate is then

\[
Q_{NN \rightarrow NN\alpha\alpha} = \frac{S\sqrt{\pi}}{(2\pi)^n} \left( 3 - \frac{2\beta}{3} \right) I_0 n_B^2 \left( \frac{f_N g m_N}{m_\phi^2} \right)^2 \left( \frac{2m_N f_\pi}{m_\pi} \right)^4 \frac{T^{5.5}}{m_N^{4.5}},
\]

(4.17)

where we have defined the integral \( I_0 \) by

\[
I_0(T, m_r, \langle r \rangle) \equiv \int du \, dv \, dx \, x^4 \, I_1(x, m_r, \langle r \rangle) \sqrt{uv} e^{-u} \delta(u - v - x),
\]

(4.18)

and the \( \beta \) term by

\[
\beta \equiv \frac{3}{I_0} \int du \, dv \, dx \, x^4 \, I_1(x, m_r, \langle r \rangle) \sqrt{uv} e^{-v} \delta(u - v - x) \int_{-1}^{+1} dz \frac{|\vec{k} \cdot \vec{l}|^2}{|\vec{k}|^2 |\vec{l}|^2}.
\]

(4.19)

With the initial comoving baryon number density in the fireball set at the fiducial value \( n_B = 5 \cdot 10^{31} \, \text{cm}^{-3} \), we find that the energy loss rate due to nuclear bremsstrahlung processes is always \( \sim 10^{-8} \) times that due to electron-positron annihilation process.

5 Goldstone boson mean free path in the GRB fireball

In this section we estimate the fireball’s opacity to the Goldstone bosons. The Goldstone boson mean free path in the initial GRB fireball is set by the elastic scattering on electrons and positrons \( \alpha + e^\pm \rightarrow \alpha + e^\pm \), as well as on nucleons \( \alpha + N \rightarrow \alpha + N \).

5.1 Scattering on electrons and positrons

The amplitude for Goldstone boson scattering on electrons and positrons \( \alpha(q_1) e^\pm(p_1) \rightarrow \alpha(q_2) e^\pm(p_2) \) is

\[
\sum_{\text{spins}} |\mathcal{M}_{\alpha e \rightarrow e\alpha}|^2 = \frac{4g^2 m_\phi^4 (q_1 \cdot q_2)^2 (p_1 \cdot p_2 + m_\phi^2)}{(t - m_\phi^2)^2},
\]

(5.1)

where \( t = (q_2 - q_1)^2 = (p_1 - p_2)^2 \). We follow ref. [94] to calculate the reaction rate

\[
R_{\alpha e \rightarrow e\alpha} = n_e \sigma_{\alpha e \rightarrow e\alpha} v_M = \int \frac{d^3 \vec{p}_1}{(2\pi)^3} f_e(\vec{p}_1) \frac{1}{2\omega_1 2E_1} \int \frac{d^3 \vec{p}_2}{(2\pi)^3} \frac{1}{2\omega_2} \times \int \frac{d^3 \vec{q}_2}{(2\pi)^3} 2E_2 \left[ 1 - f_e(\vec{p}_2) \right] \sum_{\text{spins}} |\mathcal{M}_{\alpha e \rightarrow e\alpha}|^2 (2\pi)^4 \delta^4(p_1 + q_1 - p_2 - q_2).
\]

(5.2)
Using the polar angle $\cos \theta \equiv \vec{p}_1 \cdot \vec{q}_1/|\vec{p}_1||\vec{q}_1|$ and the azimuthal angel $\phi'$ which is measured from the ($\vec{p}_1, \vec{q}_1$)-plane, the 9-dimensional integral can be simplified to

$$R_{\alpha e \rightarrow \alpha e} = \frac{1}{(2\pi)^3} \frac{m_e^4 g^2 m_e^2}{4 \omega_1^2 m_e^2} \int_1^\infty \int_1^{\epsilon_1} d\epsilon_1 f_c(\epsilon_1) \sqrt{\epsilon_1^2 - 1} \int_1^{e_1+1} \frac{d\cos \theta}{\lambda(\epsilon_1, u_1, \cos \theta)}$$

$$\times \int_{\epsilon_1^{\min}}^{\epsilon_1^{\max}} d\epsilon_2 [1 - f_c(\epsilon_2)] \int_0^{2\pi} \frac{d\phi'}{2\pi} F_3,$$  

with the dimensionless variables $\epsilon_1 \equiv E_1/m_e$, $\epsilon_2 \equiv E_2/m_e$, and $u_1 \equiv \omega_1/m_e$. The functions in the above equation are defined as

$$\lambda(\epsilon_1, u_1, \cos \theta) \equiv \frac{|\vec{p}_1 + \vec{q}_1|}{m_e} = \sqrt{\epsilon_1^2 - 1 + u_1^2 + 2u_1 (\epsilon_1^2 - 1)^{1/2} \cos \theta},$$

and

$$F_3 \equiv \frac{[q_1 \cdot (p_1 + q_1 - p_2)]^3 + 2m_e^2 [q_1 \cdot (p_1 + q_1 - p_2)]^2}{[2q_1 \cdot (p_1 + q_1 - p_2) + m_e^2]^2 m_e^2},$$

respectively, and the limits for the $d\epsilon_2$ integration are determined to be

$$\epsilon_2^{\max, \min} = \frac{1}{2} \left[ \epsilon_1 + u_1 \pm \lambda(\epsilon_1, u_1, \cos \theta) + \frac{1}{\epsilon_1 + u_1 \pm \lambda(\epsilon_1, u_1, \cos \theta)} \right].$$

To evaluate $q_1 \cdot p_2$, we need to know the angle

$$\cos \theta_{q_1p_2} \equiv \cos \theta' \cos \Delta_2 - \sin \theta' \sin \Delta_2 \cos \phi',$$

where

$$\cos \Delta_1 = \frac{\sqrt{\epsilon_1^2 - 1 + u_1 \cos \theta}}{\lambda}, \quad \cos \Delta_2 = \frac{u_1 + \sqrt{\epsilon_1^2 - 1 \cos \theta}}{\lambda},$$

with $\Delta_1 + \Delta_2 = \theta$. We evaluate eq. (5.3) numerically using the VEGAS subroutine. In figure 7 we plot the $\alpha e \rightarrow \alpha e$ scattering rate divided by the Goldstone boson coupling $g^2$, for an incident Goldstone boson energy of $\omega_1 = 540, 180$, and $90$ MeV, assuming the fiducial initial GRB fireball temperature $T_0 = 18$ MeV. The rates for $T_0 = 8$ MeV are also displayed, for Goldstone boson incident energy $\omega_1 = 320, 160$, and $40$ MeV. We find that for all Goldstone boson energies attainable in the GRB initial fireballs and all $m_\tau$ values, $R_{\alpha e \rightarrow \alpha e} < 4 g^2 s^{-1}$.

### 5.2 Scattering on nucleons

The interaction rate for $\alpha(q_1)N(p_1) \rightarrow \alpha(q_2)N(p_1)$ can be calculated similarly as $R_{\alpha e \rightarrow \alpha e}$ in eq. (5.3) by replacing $m_e$ with $m_\pi$ and using the non-relativistic Maxwell-Boltzmann distribution $f_N(\vec{p}) = (n_B/2) (2\pi/m_N T)^{3/2} e^{-m_\pi^2/2m_N T}$ for the nucleons. The amplitude squared is

$$\sum_{\text{spins}} |\mathcal{M}_{\alpha N \rightarrow \alpha N}|^2 = \frac{4f_N^2 g^2 m_N^2 (q_1 \cdot q_2)^2}{m_e^4} \frac{(p_1 \cdot p_2) + m_N^2}{(t - m_N^2)^2},$$

where $g_N$ is the effective coupling of the Goldstone bosons to nucleons. For low incident Goldstone boson energies $\omega_1 \ll m_N$, the nuclear recoil effects can be neglected, and so the interaction rate can also be easily estimated by

$$R_{\alpha N \rightarrow \alpha N} = n_B \sigma_{\alpha N \rightarrow \alpha N} v_M$$

$$= n_B \frac{\omega_1^4}{16\pi} \frac{f_N^2 g_N^2}{m_e^4} \int_{-1}^{1} d\cos \theta \omega_1^2 (1 - \cos \theta)^3 + 2m_N^2 (1 - \cos \theta)^2 \left[\frac{2\omega_1^2 (1 - \cos \theta) + m_N^2}{m_e^2}\right]^2.$$
We found that the results from this method agree with those from the full calculation within 10% for $\omega_1 \lesssim 40$ MeV. The results are shown in figure 8, where we assume the baryon number density in the GRB fireball is $n_B = 5 \cdot 10^{31}$ cm$^{-3}$. Although the baryon number density is four orders of magnitude smaller than that of the electrons and positrons, due to the large nucleon mass $m_N$, this channel dominates over the scattering on electrons and positrons. The figure indicates that there is an upper bound on the scattering rate, $R_{\alpha N \rightarrow \alpha N} \lesssim 4 \cdot 10^4 (f_N g)^2$ s$^{-1}$.

The Goldstone boson mean free path in the initial GRB fireball is then

$$\lambda_\alpha = \frac{n_e \sigma_{\alpha e \rightarrow e \alpha} + n_B \sigma_{\alpha N \rightarrow \alpha N}}{R_{\alpha N \rightarrow \alpha N}} \simeq \frac{7.5 \cdot 10^5}{f_N^2 g^2} \text{ cm} ,$$

(5.11)

for all $m_r$ and $\omega_1$ values. Using $f_N = 0.3 \pm 0.03$ as determined in ref. [68], and taking into account the current collider constraint of $|g| < 0.011$, we find that

$$\lambda_\alpha \gtrsim 7 \cdot 10^{10} \text{ cm} \gg R_0 \sim 10^{6.5} \text{ cm} ,$$

(5.12)

for all $m_r$ values. We conclude that the Goldstone bosons produced in the initial fireball of GRBs cannot be trapped therein, i.e. the GRB initial fireballs are transparent to the Goldstone bosons. The consequence will be discussed in the next section.

6 Hydrodynamics of GRB fireballs in the presence of Goldstone boson production

We apply the relativistic hydrodynamics for describing quark-gluon plasma anticipated at the LHC or the Relativistic Heavy Ion Collider (RHIC) [95] (see e.g. ref. [96] for review articles on this topic) to study the GRB fireballs.
6.1 Hydrodynamics of GRB fireballs with dissipation

The evolution of GRB fireballs is governed by the equations for the conservation of (baryon) particle number and for the conservation of energy and momentum,

\[ \partial_\mu N^\mu = 0, \quad \partial_\mu T^{\mu\nu} = j^\nu, \]  

respectively. Here \( j^\nu \) represents an effective source term, with a negative (positive) \( j^0 \) term denoting an energy sink (source). The baryon number flux is \( N^\mu = n_B u^\mu \). For each particle species \( i \) in the fluid, one expands its phase space distribution function around the equilibrium value, as \( f = f_0 + \delta f \). The deviation from the equilibrium value is related to a characteristic relaxation time. With such a correction, the stress-energy tensor is then modified to (see e.g. ref. [97])

\[ T^{\mu\nu} = (\epsilon_0 + \delta \epsilon) u^\mu u^\nu + (p_0 + \pi_b) \Delta^{\mu\nu} + \pi^{\mu\nu}, \]  

with \( u^\mu \) the four-velocity, and \( \Delta^{\mu\nu} = g^{\mu\nu} + u^\mu u^\nu \) the project tensor to the subspace orthogonal to the fluid velocity. Here we choose the signature of the metric to be \((-\hbar, +, +, +)\), and the fluid four-velocity \( u^\mu \) is specified using the definition by Landau and Lifshitz. Following this definition, the tensor equation \( \pi^{\mu\nu} u^\nu = 0 \) must be satisfied.

The shear tensor and the bulk viscosity pressure in the lowest order of the velocity gradients are of the form

\[ \pi^{\mu\nu} = -2\eta \left( \frac{1}{2} (\Delta^{\rho\sigma} \partial_\rho u^\nu + \Delta^{\rho\sigma} \partial_\sigma u^\rho) - \frac{1}{3} \Delta^{\mu\nu} \partial_\alpha u^\alpha \right), \quad \pi_b = -\zeta \partial_\mu u^\mu, \]  

respectively, with \( \eta \) and \( \zeta \) denoting the shear and the bulk viscosity coefficient. However, as mentioned in ref. [98], to avoid the acausality problems, the dissipative fields should be regarded as independent dynamical variables. The shear viscosity can be estimated using the

**Figure 8.** Results for the \( \alpha N \rightarrow \alpha N \) scattering rate divided by the coupling \( g^2 \) versus the radial field mass \( m_r \), for incident Goldstone boson energy \( \omega_1 \) = 540, 320, 180, 40, and 10 MeV (from top to bottom). The baryon density is assumed to be \( n_B = 5 \cdot 10^{31} \text{ cm}^{-3} \).
Green-Kubo relation [99] (see also, e.g. ref. [100] for a recent numerical study.) From kinetic theory, the shear viscosity coefficient is (see e.g. ref. [101])

$$\eta \approx \frac{1}{3} \sum_j n_j \langle p \rangle_j \lambda_j,$$

(6.4)
i.e. it is determined by particle species $j$ in the fluid with number density $n_j$ transporting an average momentum $\langle p \rangle_j$ over a momentum transport mean free path $\lambda_j$.

To solve the equation for the conservation of energy and momentum, one projects it in the direction of the fluid velocity and that orthogonal to the fluid velocity, obtaining (see e.g. ref. [102])

$$u^\mu \partial_\mu \epsilon + (\epsilon + p_0) \partial_\mu u^\mu - u_\nu \partial_\mu \pi^{\alpha \nu} + \pi_\alpha \partial_\mu u^\mu = -u_\nu j^\nu,$$

(6.5)
and

$$(\epsilon + p_0 + \pi_b) u^\mu \partial_\mu u^a + \Delta^a_\beta \partial_\beta (p_0 + \pi_b) + \Delta^a_\nu \partial_\nu \pi^{\mu \nu} = \Delta^a_{\nu j^\nu},$$

(6.6)
with $\epsilon = \epsilon_0 + \delta \epsilon$. These conservation equations need to be supplemented with an equation of state for the fireball plasma. When the GRB fireball expansion reaches the coasting phase, i.e. the Lorentz factor $\Gamma$ is constant, one can transform to the Milne coordinates

$$\tau \equiv \sqrt{t^2 - R^2}, \quad \chi \equiv \tanh^{-1} (R/t),$$

(6.7)
as in e.g. refs. [103, 104].

The effects of the dissipation fields are to transfer the kinetic energy into heat, while the energy source (sink) increase (decrease) the total energy. In the initial fireball of GRBs, we can assume that all particle species — the electrons and positrons, photons, as well as the protons and neutrons — are strongly coupled and thus are all in thermal equilibrium. Now consider the case that from their interactions some exotic particle species are copiously created. If they are not fully thermalised, they lead to a slower expansion of the fireball.

However, in the last section we found that the Goldstone boson mean free path $\lambda_\alpha$ exceeds the size of the initial fireball $R_0$ (cf. eq. (5.11)). The Goldstone bosons produced therein are not trapped and therefore are not thermalised at all. In this case eq. (6.4) is not applicable, since its validity requires $\lambda_\alpha \ll R_0$. The effects of the Goldstone bosons can still be estimated by transforming to the fireball comoving frame. Following the definition by Landau and Lifshitz, in this frame the terms involving $\pi^{\mu \nu}$ or $\pi_b$ completely vanish.

### 6.2 The GRB fireball energy loss criterion

In the fireball comoving frame, we demand that the Goldstone bosons transport away an amount of energy comparable to the initial fireball radiation energy before their emissivity decreases significantly with the temperature. In the GRB fireball comoving frame where the four-velocity is $u^\nu = (1, 0, 0, 0)$ in spherical coordinates ($t', R', \theta', \phi'$), the hydrodynamic equations eqs. (6.5) and (6.6) are simply

$$\frac{\partial n_B}{\partial t'} = 0, \quad \frac{\partial \epsilon}{\partial t'} = j^0 = Q, \quad \frac{\partial p}{\partial R'} = 0,$$

(6.8)
where the coordinates in the comoving frame and in the observer frame are related by the Lorentz factor, i.e. $t' = t/\Gamma$ and $R' = \Gamma R$. Here the baryon number density $n_B$, the energy density $\epsilon$ and the the pressure $p$, as well as the energy loss or creation per unit volume per
unit time $Q$, are all comoving quantities. The Goldstone bosons are emitted isotropically in the fireball comoving frame, so the net momentum flux herein is $j^1 = j^2 = j^3 = 0$. One can regard the Goldstone bosons as an energy sink. Using the equation for energy conservation in eq. (6.8), we can derive a constraint on the Goldstone boson emissivity in the GRB initial fireball as

$$|\Delta \epsilon| = | - Q_{e^+ e^- \rightarrow \alpha \alpha} \Delta t| \approx Q_{e^+ e^- \rightarrow \alpha \alpha} \frac{1}{\Gamma_0 \beta_0} \frac{\Delta R_0}{\Gamma_0 V_0} \approx \frac{\mathcal{E}}{\Gamma_0 V_0}. \quad (6.9)$$

Choosing $\Delta R_0 \sim R_0$, this criterion is equivalent to the comparison of the cooling timescale $t_c$ with the fireball expansion timescale $t_e$ in ref. [36]

$$\chi \equiv \frac{t_c}{t_e} \approx \frac{\mathcal{E}}{(Q_{e^+ e^- \rightarrow \alpha \alpha} V_0)} \frac{R_0}{\beta_0} \lesssim 1. \quad (6.10)$$

In figure 2 we plot the upper limits on $g(<r>$, the Goldstone boson coupling times the vev of the $r$ field, versus its mass, $m_r$, obtained by using the criterion in eq. (6.9). The GRB initial fireball temperature, radius, and energy, are chosen at the fiducial value $T_0 = 18$ MeV, $R_0 = 10^{6.5}$ cm, and $\mathcal{E} = 10^{52}$ erg, as well as a lower initial temperature $T_0 = 8$ MeV. If the temperature of the GRB initial fireball is as low as $T_0 = 2$ MeV, no constraint on the parameters of Weinberg’s Higgs portal model can be obtained.

An inspection of figure 2 indicates that in the mass range $m_r / T_0 \lesssim 10^{-15}$, the GRB bounds are indeed competitive to current laboratory constraints reviewed in section 3.2. They are more stringent than the constraints from muon anomalous magnetic moment and radiative upsilon decays, while weaker than those from the $B^+$ and $K^+$ meson invisible decays by 1–3 orders of magnitude.

As is clear from eq. (6.9), the GRB bounds are subject to the uncertainties in the GRB fireball total energy $\mathcal{E}$, the fireball initial radius $R_0$ and wind velocity $\beta_0$, as well as the fireball initial temperature $T_0$, which determines sensitively the energy loss rate $Q_{e^+ e^- \rightarrow \alpha \alpha}$ (cf. figure 4). The uncertainty in the fireball total energy is deduced in ref. [12] to be approximately a factor of 2, due mainly to the scatter in the X-ray measurements. The analysis done within the fireball model in ref. [57] suggests that the uncertainty in the acceleration radius (defined by $\Gamma(r_0) \simeq 1$) ranges from 20–100%, mostly around 50%. We then use eq. (2.4) or eq. (2.6) to estimate the uncertainty in $T_0$ to be about 30–80%. The error in the energy loss criterion $Q_X \equiv E \beta_0 / \Delta R_0 V_0$ in eq. (6.9) is approximately a factor of 3. In figure 2 we indicate the uncertainty in our GRB bounds on $g(<r>$ resulting from the error in $Q_X$ by the filled regions, while that resulting from the uncertainty in $T_0$ spans almost the space between the two curves for $T_0 = 18$ and 8 MeV, respectively. We therefore conclude that the region bounded by the two curves, including the filled regions, represents the parameter space in Weinberg’s Higgs portal model that can be probed by GRB physics.

7 Summary

We aimed to study the effects of the Goldstone bosons in Weinberg’s Higgs portal model on the initial fireballs of gamma-ray bursts. We first calculated the energy loss rates therein due
to Goldstone boson production in different channels, including electron-positron annihilation, photon scattering, and nuclear bremsstrahlung processes. We found that resonance effects significantly enhance the energy loss rate for the electron-positron annihilation process, even for the mass of the radial field $r$ approaching 30–40 times the initial GRB fireball temperature. On the other hand, in the calculation of the Goldstone boson mean free path, there is no such effect present in the processes of Goldstone boson scattering on nucleons and electrons or positrons. Interestingly, we found that although nuclear bremsstrahlung processes are of no importance in Goldstone boson production, the scattering on nucleons dominates over scattering on electrons and positrons by four orders of magnitude in setting the Goldstone boson mean free path in the GRB fireballs. However, for all Goldstone boson energies attainable in the GRB initial fireballs and all $m_r$ values, the Goldstone boson mean free path always exceeds the initial fireball radius. Thus the Goldstone bosons do not couple to the GRB fireball plasma. The initial GRB fireballs are transparent to the Goldstone bosons, so that they freely transport the fireball energy away and act as an energy sink.

We obtained constraints on $g \langle r \rangle$, the Goldstone boson coupling times the vacuum expectation value of the $r$ field, by using the energy loss rate criterion derived from the hydrodynamic equations in the GRB fireball comoving frame. Assuming generic values for the GRB initial fireball temperature, radius and energy, we found that in the mass range of $m_r/T_0 \lesssim 10–15$, the GRB bounds are indeed competitive to current laboratory constraints. They are more stringent than the constraints from muon anomalous magnetic moment and radiative upsilon decays, while weaker than those from the $B^+$ and $K^+$ meson invisible decays by 1–3 orders of magnitude.

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