Deep Attributed Network Representation Learning via Attribute Enhanced Neighborhood

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Abstract—Attributed network representation learning aims at learning node embeddings by integrating network structure and attribute information. It is a challenge to fully capture the microscopic structure and the attribute semantics simultaneously, where the microscopic structure includes the one-step, two-step and multi-step relations, indicating the first-order, second-order and high-order proximity of nodes, respectively. In this paper, we propose a deep attributed network representation learning via attribute enhanced neighborhood (DANRL-ANE) model to improve the robustness and effectiveness of node representations. The DANRL-ANE model adopts the idea of the autoencoder, and expands the decoder component to three branches to capture different order proximity. We linearly combine the adjacency matrix with the attribute similarity matrix as the input of our model, where the attribute similarity matrix is calculated by the cosine similarity between the attributes based on the social homophily. In this way, we preserve the second-order proximity to enhance the robustness of DANRL-ANE model on sparse networks, and deal with the topological and attribute proximity to enhance the robustness of DANRL-ANE model on social homophily. In this way, we preserve the second-order proximity to enhance the robustness of DANRL-ANE model on sparse networks, and deal with the topological and attribute proximity to enhance the robustness of DANRL-ANE model on social homophily. In this way, we preserve the second-order proximity to enhance the robustness of DANRL-ANE model on sparse networks, and deal with the topological and attribute proximity to enhance the robustness of DANRL-ANE model on social homophily.

Index Terms—attributed network representation learning, network structure, link prediction, node classification, social homophily.

I. INTRODUCTION

NETWORKS are generally utilized to explore and model complex systems, such as online social networks and citation networks, where an entity is represented as a node and the interaction between two entities is represented as an edge. Network analysis is an effective way to gain insight into different aspects of complex systems, which derives many machine learning applications, such as the online advertisement targeting [1] and anomaly detection [2]. Hence, identifying effective features of nodes (or edges) in a network is essential. However, traditional methods tend to manually mine the specific domain features depending on the expert experience, which not only require the high cost of labor and time, but also limit the scalability of models on different prediction tasks [3]. Network representation learning (NRL) [4] as an alternative of automatic feature mining has been proved to be beneficial to various network analysis tasks, such as the node classification [5] [6], link prediction [7], clustering [8] and visualization [9].

Early NRL methods are mostly based on the matrix factorization [10]. To reduce the computational complexity on large-scale networks, inspired by word modeling, Perozzi et al. propose DeepWalk [4]. Notably, the above-mentioned shallow model design cannot well capture the highly non-linearity that is universal in the networks, which would lead to the sub-optimal network representation [11]. Then, many deep models, such as structural deep network embedding (SDNE) [11], have emerged.

Considering only the network structure is not enough to learn the informative and accurate node representations, especially when the network structure is sparse. Social science theories like the homophily [12] [13] and social influence theory [14] suggest that there is a strong correlation between the structure and the attributes. Therefore, many studies focus on attributed NRL [15] [16] [17], which mainly learn the consistent node representations from the network structure and node attributes. Nevertheless, the above models are likely susceptible to the sparsity of one of the heterogeneous information sources. Afterwards, the deep coupling paradigm is introduced to enhance the robustness of the representations. Attributed network representation learning (ANRL) [18] is one of the representative examples. However, the ANRL model could be affected by the characteristics of the local network structure. In addition, the previous attributed NRL methods rarely preserve all the microscopic structural information, i.e., the first-order, second-order, and high-order proximity [19], together, where these proximities indicate the one-step, two-step, and multi-step relationship between two nodes. Nevertheless, explicitly taking full advantage of the microscopic structure tends to be essential for learning the network representation [20].

To utilize the microscopic structural information as well as the node attributes, we propose a novel deep coupling attributed NRL model, namely, the deep attributed network representation learning via attribute enhanced neighborhood (DANRL-ANE) model. The proposed model consists of three coupled modules, i.e., the self-built first-order proximity preserved, attribute enhanced neighborhood autoencoder and community-aware skip-gram module, which preserve the first-order, second-order, and high-order proximity, respectively. The three modules share connections to the encoder.
cially, we model the attributes based on the social homophily, and incorporate the attribute semantics into the adjacency matrix to enhance the direct neighborhood of each node.

To summarize, our main contributions are as follows:

(i) We propose a deep three-part coupling model, DANRL-ANE, which learns the robust and effective node representations by jointly mining the microscopic structure and node attributes. The attributes are preprocessed to be used as the input of our model together with the adjacency matrix, which is advantageous to obtain the accurate second-order proximity.

(ii) We construct the self-built first-order proximity preserved module, which innovatively extends the sigmoid cross-entropy loss function for capturing the local pairwise relationship between node pairs on undirected and unweighted networks.

(iii) Our proposed model is not only good for the machine learning tasks that benefit from the pairwise properties between nodes, i.e., the link prediction and node classification, but also not susceptible to the sparsity and neighborhood distribution of either the structure or the attributes. Moreover, our model even can deal with the networks with isolated nodes when we obtain the sufficient node attributes.

The rest of the paper is organized as follows. We discuss the related work in Section II, and introduce the preliminaries involved in the paper in Section III. We give the detailed description of our model in Section IV, and then show the experimental settings and results in Section V. Finally, we conclude the paper in Section VI.

II. RELATED WORK

The network representation is first proposed as the part of dimensionality reduction technologies [21][22][23] in the early 20th century. However, the early methods suffers from both computational and statistical performance drawbacks [3]. Afterwards, Perozzi et al. [4] generalize the advancements in language modeling to large-scale networks. A large number of related excellent algorithms have been proposed. For example, DeepWalk [4] uses the uniform sampling to collect the node sequences [20]. Node2vec [3] extends the DeepWalk model, which captures the diversity of connectivity patterns in a network. Intuitively, the skip-gram-based methods capture the high-order proximity [24]. LINE [25] utilizes different carefully designed objective functions to preserve the first-order and second-order proximity. However, all of the above methods cannot preserve the different $k(k \geq 3)$-step relationships in distinct subspaces [20]. Therefore, Cao et al. propose GraRep [20], which concatenates all the local $k(k \geq 3)$-step representations as the representations of nodes. The mentioned methods all utilize the network structure only to learn network representation. Besides the structure, nodes in the real world are usually affiliated with various attributes.

Then, researchers begin to focus on mining the network features from attributed networks, such as GAT2VEC [26] and SANE [27]. To further capture the highly non-linearity, some algorithms, such as DANE [15], ASNE [16] and MDNE [17], have been recently designed based on the deep learning technologies, which all model the network structure, encode the attribute information, and then depend on the strong correlation between the structure and the attributes to obtain the consistent network embedding. Giving an example, DANE [15] utilizes the autoencoder to preserve the high-order structural proximity and attribute semantics, the joint probability to capture the first-order proximity from the structure and attributes, and the likelihood estimation to learn the node embeddings by jointly the structure and attributes. The above methods might be susceptible to the sparsity of either the structure or the attributes. For learning the robust representations, Zhang et al. [18] propose a deep coupling model ANRL, which preserves the second-order and high-order proximity from the topological structure. On the basis of the encoder part, ANRL constructs a neighbor enhancement autoencoder module, and designs an attribute-aware skip-gram module. Nevertheless, the design of the autoencoder makes ANRL limited by the choice of datasets.

In summary, attributed NRL is still an open problem in at least two aspects as follows: (1) the network structure and node attributes are two heterogeneous information sources, we need to consider how to preserve their characteristics in a vector space; (2) the first-order, second-order and high-order proximity define different neighborhood relations among directly or indirectly connected nodes. To capture local closeness proximities could help preserve the entire microscopic structure features of original networks, yet how to design a proper model is a challenge. Here, we propose the DANRL-ANE model under the paradigm of deep coupling, in which three coupled modules are designed to capture the different order proximity. Especially, the attribute information is mined as the supplement of the adjacency matrix.

III. PRELIMINARIES

In this section, we first briefly introduce two types of node attributes, notations and definitions which are used in this work. Then, the schematic of attributed network representation learning is given.

A. Node Attributes

The node attributes refer to the auxiliary information used to describe a node besides the network structure. For instance, in social networks, personal information such as age, gender and hobbies can be used as attributes. As declared in [16], regardless of the semantics, the attributes could be categorized into two types: the discrete attributes and continuous attributes.

- **Discrete attributes.** The typical example of the discrete attributes is the categorical attributes, which can be transformed into the binary vectors via one-hot encoding.

- **Continuous attributes.** The continuous attributes naturally exist in social networks. They could be artificially generated from the transformation of the categorical variables. The continuous attributes can be represented as the real-valued vectors after being preprocessed. For example, in the document modeling, after obtaining the bag-of-words representation of a document, it is common to transform it to a real-valued vector via TF-IDF to reduce the noises [16].

Our proposed model DANRL-ANE is suitable for the networks with either discrete attributes or continuous attributes.
B. Notations

Let $G = (V, E, A, X)$ be an attributed information network, where $V = \{v_1, \ldots, v_n\}$ denotes a set of nodes, $E \subseteq (V \times V)$ denotes a set of edges among nodes, $A$ is the adjacency matrix and $X$ is the node attribute matrix. In the adjacency matrix $A$, if there is an edge between nodes $v_i$ and $v_j$, $a_{ij} > 0$, particularly, if the network is unweighted, $a_{ij} = 1$; otherwise, $a_{ij} = 0$. If the network is undirected, $a_{ij} = a_{ji}$. In the node attribute matrix $X$, the element $x_{ik}$ indicates the value of node $v_i$ on the attribute $k$. In this work, we focus on the undirected and unweighted networks.

C. The Closeness Proximity

We here introduce the definition of the first-order, second-order and high-order proximity involved in our model.

**Definition 1: First-order proximity**

The first-order proximity describes the pairwise proximity between nodes [11]. For each node pair $(v_i, v_j)$, if there is an edge between them, the first-order proximity between nodes $v_i$ and $v_j$ is $a_{ij}$; otherwise, the first-order proximity between nodes $v_i$ and $v_j$ is 0.

**Definition 2: Second-order proximity**

The second-order proximity between a pair of nodes describes the proximity of the neighborhood structure of the node pair [11]. Let $A_2 = [a_{i1}, a_{i2}, \ldots, a_{in}]$ denote the first-order proximity between node $v_i$ and all other nodes, then the second-order proximity between nodes $v_i$ and $v_j$ is decided by the similarity measure, such as cosine similarity, between $A_i$ and $A_j$. Notice that the second-order proximity captures the 2-step relation between node pairs, which could be measured by the 2-step transition probability from node $v_i$ to node $v_j$, equivalently [19].

**Definition 3: High-order proximity**

Compared with the second-order proximity, the high-order proximity captures the more global structure, which explores the $k$-step ($k \geq 3$) relation between node pairs [19]. The high-order proximity could be measured by the $k$-step($k \geq 3$) transition probability from node $v_i$ to node $v_j$.

D. Attributed network representation learning

The goal of the attributed network representation learning is that with a given attributed information network $G = (V, E, A, X)$, learning a mapping function makes the whole network embedded into a new low-dimensional vector space, namely, $f : G \rightarrow Y \in \mathbb{R}^{n \times d}$, where $d$ denotes the dimension of embedding. Then, each node can be represented by a low-dimensional and dense vector. The vectors store the relationship information between each node and the other nodes, and record the attribute semantics of the nodes. Taking the node representations as the input is beneficial for the subsequent machine-learning-based network analysis tasks. A schematic of attributed network representation learning is shown in Fig. 1. It can be seen that the nodes close to each other in the original network and/or nodes with the similar attributes are also close to each other in the new vector space.

IV. THE DANRL-ANE MODEL

A. Overview

The proposed DANRL-ANE model is a deep three-part coupling model, which consists of the self-built first-order proximity preserved module, the attribute enhanced neighborhood autoencoder module and the community-aware skip-gram module. Fig. 2 shows the framework of DANRL-ANE model. The input of the encoder is the reconstructed adjacency matrix, which is obtained by integrating the node attributes and adjacency matrix. The self-built first-order proximity preserved module captures the direct relations between nodes, the attribute enhanced neighborhood autoencoder module reconstructs the target neighbors of nodes to learn the relations between the neighborhoods of two nodes, and the community-aware skip-gram module is trained on the linear node sequences to preserve the high-order relations. By training the three modules iteratively until the model converges, the final node representations are obtained, namely, the representation output of the autoencoder.

B. Preprocessing

Considering that the attributes can provide direct evidence for the similarity measurement between nodes from the attribute level, we propose to construct an attribute similarity matrix. The formal description is given as follows.

1) **Attribute Similarity Matrix** $X^{(S)} \in \mathbb{R}^{n \times n}$

Every row $X_i$ of an attribute matrix $X$ represents the attribute information of the corresponding node $v_i$. The attribute similarity $x_{ij}^{(S)}$ between nodes $v_i$ and $v_j$ could be calculated based on the similarity measurement methods. Inspired by the previous work [28], we utilize the cosine similarity to calculate the attribute similarity

$$x_{ij}^{(S)} = \text{CosineSimilarity}(X_i, X_j) = \frac{X_i X_j^\top}{|X_i||X_j|}. \quad (1)$$

Furthermore, we intend to combine the adjacency matrix $A$ and the attribute similarity matrix $X^{(S)}$ into a new reconstructed adjacency matrix to strengthen the relationship between nodes.
2) Reconstructed Adjacency Matrix $R \in \mathbb{R}^{n \times n}$

Different from the attribute similarity matrix $X(S)$, the adjacency matrix $A$ describes the similarity between nodes from the structure level. By setting the hyperparameters $\eta$ and $\psi$, we linearly combine the adjacency matrix $A$ and attribute similarity matrix $X(S)$ to build the reconstructed adjacency matrix $R$

$$R = \eta A + \psi X(S).$$  (2)

3) Self-built First-order Proximity Preserved Module

Next, we give the detailed description of each module.

2) Self-built First-order Proximity Preserved Module

The first-order proximity can reveal the similarity between nodes intuitively and simply. We here propose a self-built first-order proximity preserved module. To model the first-order proximity, inspired by the LINE [25] and DANE [15] model, we define the joint probability $w_{ij}(v_i, v_j)$ between nodes $v_i$ and $v_j$ with the sigmoid function $\sigma(x) = \frac{1}{1+\exp(-x)}$. Let $x = y_i^{(K)}y_j^{(K)}$, then we obtain

$$w_{ij}(v_i, v_j) = \frac{1}{1 + \exp(-w_{ij}(v_i, v_j))},$$  (6)

where $y_i^{(K)}$ and $y_j^{(K)}$ denote the representation of nodes $v_i$ and $v_j$, respectively.

Especially, the first-order proximity on undirected and unweighted networks describes the existence or non-existence of edge between node pairs, which is equivalent to a binomial classification problem. The sigmoid cross-entropy loss function is a typical objective function for a binomial classification, which is defined as

$$L_{ScE} = -[t \log p_s(s) + (1-t) \log(1-p_s(s))],$$  (7)

where $t$ represents the label of a sample, and can be either 1 or 0. If the sample belongs to the positive class, $t = 1$, else $t = 0$. The probability $p_s(s)$ indicates the possibility that the sample is predicted to belong to the positive class, and is calculated by the sigmoid function. Here, $t = a_{ij}$ and $p_s(s) = w_{ij}(v_i, v_j)$, equivalently.

Because only the information about the existing edges is useful for the network representation, we set $t = 1$, and take the first term of Equation (7) into consideration. We average all the losses when the edges exist, and thus obtain the objective of the self-built first-order proximity preserved module

$$L_{FoP} = \sum_{a_{ij}=1} \left(- \log w_{ij}(v_i, v_j)\right),$$  (8)

where $a_{ij}$ represents the element of the $i$-th row and the $j$-th column of the adjacency matrix $A$.

3) Attribute Enhanced Neighborhood Autoencoder Module

The deep autoencoder model is widely used to mine the proximity between the neighborhood structure of node pairs [11], since it could smoothly capture the data manifolds, and preserve the similarity between samples [29].
The autoencoder consists of two parts, i.e., the encoder and decoder. The decoder is the inverse calculation process of the encoder. The representation in the representation space is mapped into the reconstruction space in the decoder process.

The purpose of the autoencoder is to minimize the reconstruction error between the input data and the reconstructed data, so that the abstract representation of the mid-layer output can capture the manifold structure in the input data. To be specific, the objective of the autoencoder is

$$L_{ae} = \sum_{i=1}^{n} ||\hat{R}_i - R_i||^2_2,$$  \hspace{1cm} (9)

where $n$ is the number of the nodes in the networks, and $\hat{R}_i$ represents the reconstructed output of the input data $R_i$.

Although the direct neighborhood of each node gets enhanced after integrating the attribute semantics and adjacency matrix, the reconstructed adjacency matrix $R$ could still be a sparse matrix, that is, the number of non-zero elements is far less than that of zero elements. A sparse input matrix could further make the autoencoder tend to preserve more zero elements. Since the non-zero elements record the connections between nodes, it is more essential to preserve non-zero elements as much as possible instead of zero elements.

Inspired by SDNE [11], we employ the Hadamard product as the penalty factor, and extend the loss function of the autoencoder. The modified objective is

$$L_{ae}^M = \sum_{i=1}^{n} ||(\hat{R}_i - R_i) \odot b_i||^2_2,$$  \hspace{1cm} (10)

where $\odot$ indicates the Hadamard product, $b_i = \{b_{i,j}\}_{j=1}^{n}$. If $R_{i,j} = 0$, $b_{i,j} = 1$, else $b_{i,j} = \chi > 1$.

The attribute enhanced neighborhood autoencoder module takes each row vector of the reconstructed adjacency matrix $R$ as the sample input, where the row vector denotes the neighbor structural information with the attribute semantics of the corresponding node. In other words, the autoencoder could preserve the second-order proximity.

4) Community-aware skip-gram module

Inspired by DeepWalk [4], we design the community-aware skip-gram module for capturing the high-order proximity in this work.

To reduce the time complexity, we adopt the node sequences sampling procedure performed by node2vec [3], where the return parameter $p_n = 1.0$ and in-out parameter $q_n = 1.0$, and use the negative sampling to approximate the following loss function

$$L_{sg} = -\sum_{i=1}^{n} \sum_{c \in C} \sum_{b \leq j \leq b, j \neq 0} \log p(v_{i+j}|R_i),$$

$$= -\sum_{i=1}^{n} \sum_{c \in C} \sum_{b \leq j \leq b, j \neq 0} \log \frac{\exp(h'_{i+j}y_i^{(K)T})}{\sum_{f=1}^{n} \exp(h_f y_i^{(K)T})},$$  \hspace{1cm} (11)

where $n$ is the number of nodes in the network, $c \in C$ denotes the node sequences sampled by the random walk, $b$ is the size of the window. The input data $R_i$ occupies the $i$-th row of the input matrix $R$. The node $v_{i+j}$ is the context node of the current node $v_i$ located in the generated random sequences in the window $b$. The node representation $y_i^{(K)}$ is the output of the sample input $R_i$ through the $K$ layer encoder. The matrix $H'$ is the transition matrix between the representation output layer of the autoencoder and the output layer of the skip-gram, and $h'_i$ is in Row $i$ of the transition matrix $H'$.

Then, we obtain the following Equation (12)

$$L_{reg}^{NS} = -\sum_{i=1}^{n} \sum_{c \in C} \sum_{b \leq j \leq b, j \neq 0} \{\log \sigma(h'_{i+j}y_i^{(K)T})\} +$$

$$\sum_{s=1}^{\text{neg}} \mathbb{E}_{v_n \sim P_n(v)}[\log \sigma(-h'_n y_i^{(K)T})],$$  \hspace{1cm} (12)

where $\sigma(x) = \frac{1}{1 + \exp(-x)}$ is the sigmoid function, $\text{neg}$ denotes the number of the sampled negative samples. The sampling distribution $P_n(v) \propto d_i^{-3/4}$ is set as suggested in [30] and $d_i$ represents the degree of node $v_i$.

Minimizing Equation (12), we can get the result that if the two nodes co-occur, they have similar embedding vectors. Algorithm 1 describes the learning process of the entire model and all model parameters are denoted as $\Theta$.

Algorithm 1 Framework of DANRL-ANE Model

**Input:** An attributed information network $G = (V, E, A, X)$, preprocessing hyperparameters $q$ and $\psi$, hadamard product operation parameter $\chi$, walks per node $r$, walk length $l$, window size $b$, return $p$, in-out $q$, negative samples $\text{neg}$, trade-off parameters $\alpha$ and $\beta$, regularizer coefficient $\gamma$, embedding dimension $d$

**Output:** node vector representations $Y \in \mathbb{R}^{n \times d}$

1: Use cosine similarity measurement method on attribute matrix to achieve attribute similarity matrix $X^S$

2: Obtain the reconstructed adjacent matrix $R$ by linearly combining the adjacency matrix $A$ with attribute similarity matrix $X^S$ by $q$ and $\psi$

3: Adopt random walk procedure of node2vec model with $p$ and $q$ both set as 1, and start $r$ times of random walks with length $l$ at each node

4: Random initialize all parameters $\Theta$

5: while not converged do

6: Sample a mini-batch of nodes with its context

7: Compute the gradient of $\nabla L_{reg}$ based on Equation (8)

8: Update first-order proximity preserved module parameters

9: Compute the gradient of $\nabla L_{ae}^M$ based on Equation (10) and the gradient of $\nabla L_{reg}$ based on Equation (5)

10: Update autoencoder module parameters

11: Compute the gradient of $\nabla L_{sg}^{NS}$ based on Equation (12)

12: Update skip-gram module parameters

13: end while

14: Obtain representations $Y = Y^{(K)}$ based on Equation (3)

V. Experiments

In the section, compared with the state-of-the-art models, we verify the superiority of our proposed DANRL-ANE model via
two downstream tasks, namely, the link prediction and node classification on five datasets, including Citeseer, PubMed, Cora, Facebook and Flickr.

A. Experimental Settings

1) Datasets: In the experiments, we select five public and widely used datasets, which belong to two network types, i.e., the citation networks and social networks. The dataset statistics are summarized in Table I. To further illustrate the broad applicability of our model to various networks, we analyze the basic topological properties of employed datasets, including the density, average degree, average clustering coefficient and average distance of the networks, as shown in Table II.

- **Citation networks:** Citeseer [18], PubMed [18] and Cora [27].
  - The node indicates the publication, and the edge indicates the citing or cited relation between publications. By using the bag-of-words model to deal with a publication, and stemming and removing the stop-words, a vocabulary of the remaining unique words is used as the node attributes.
  - In Citeseer, publications are classified into six classes, namely, Agents, AI, DB, IR, ML and HCI; in PubMed, publications are classified into three classes, namely, Diabetes Mellitus Experimental, Diabetes Mellitus Type 1 and Diabetes Mellitus Type 2; and in Cora, publications are classified into seven classes, namely, Case Based, Genetic Algorithms, Neural Networks, Probabilistic Methods, Reinforcement Learning, Rule Learning and Theory. The group categories are regarded as the labels of nodes.

- **Social networks:** Facebook [18] and Flickr [31].
  - **Facebook:** It is one of the most famous online social networks. In the dataset, the node denotes the user, and the edge represents the friendship relation between two users. Furthermore, the personal profile is treated as the attribute information used to describe the user. Note that there are no labels in the dataset, so we cannot employ Facebook for the node classification.
  - **Flickr:** It is an image hosting and sharing website. Similarly, the node and the edge represent the user and the following or followed relation between users, respectively. The users can specify a list of tags that reflect their interests, which are processed into the attributes. The photos are organized under the pre-specified categories, so the labels refer to the photo interest groups that the users join in.

2) Baselines: We compare our model, DANRL-ANE, with seven state-of-the-art models, which can be divided as the following groups:

- **Structure-only:** The set of baseline models aim to capture the structural information, including: (i) the skip-gram based models which focus on preserving different order proximity of the structure, such as DeepWalk, node2vec, LINE and GraRep, (ii) the autoencoder based model, such as SDNE. Particularly,
  1. *DeepWalk:* The truncated random walk is employed to capture the high-order proximity.
  2. *node2vec:* The biased random walk is designed to explore the high-order structural information.
  3. *LINE:* The objective is to preserve the first-order and second-order proximity. Specifically, LINE models the direct and indirect neighbor relationship between node pairs through joint probability and conditional probability, respectively.
  4. *GraRep:* All the local k(k ≥ 3)-step relational information between node pairs are considered and concatenated as the final representations of nodes.
  5. *SDNE:* Laplacian Eigenmaps and the deep model autoencoder are employed to preserve the first-order and second-order proximity, respectively.

- **Structure & Attribute:** The models preserve the structural and attribute information based on the deep learning model autoencoder, which can be further classified: (i) the consistent learning based model, such as DANE, (ii) the deep coupling framework based model, such as ANRL.
  1. *DANE:* The joint probability and autoencoder are used to mine the corresponding first-order and high-order proximity from the network structure, and to capture the corresponding first-order proximity and attribute semantics from the node attributes. Then, the likelihood estimation is used to learn the consistent network embedding from the structure and the attributes.
  2. *ANRL:* It is a deep coupling model. The neighbor enhancement autoencoder module encodes the attribute semantics, and captures the second-order proximity. The attribute-aware skip-gram module is designed to preserve the high-order proximity. Furthermore, a large number of experiments in [18] have proved that in the ANRL variants, the performance of ANRL-WAN is superior. Hence, in the paper, we choose the ANRL-WAN as the benchmark.

3) Parameter settings: For all baselines, we use the public source code provided by the original author, and tune the parameters to make each model achieve the optimal performance on the different datasets and experimental tasks. We set the final embedding dimension d as 128. For LINE, we concatenate the representations of the first-order and second-order proximity as the final embeddings. We set the walks per node r as 10, walk length l as 80, window size b as 10, negative samples $|\text{neg}|$ as 10. The hyperparameters $\eta$, $\psi$, $\chi$, $\alpha$, $\beta$ and $\gamma$ are tuned by using the grid search. In addition, after the performance comparison of trying the application of Relu, LeakyRelu, softsign, tanh and sigmoid in our model, we use the tanh function, $\text{tanh}x = \frac{\sinhx}{\coshx} = \frac{e^x - e^{-x}}{e^x + e^{-x}}$, as the non-linear activation function of the autoencoder. Table III shows the number of layers and dimension of each layer in the autoencoder, and there is no other layer between the representation layer of the autoencoder and the output layer of the skip-gram.
Inspired by [18], in the link prediction experiment, we rank the similarity function, and employ the AUC [33] index to judge both the positive and negative instances according to the cosine similarity function, and employ the AUC [33] index to judge the ranking quality. A higher score indicates that the network representation is more informative. The link prediction task is utilized as the feature inputs to predict the unobserved edges. Together, constitute the test set. Furthermore, we use the residual network to train the embedding models, which is to obtain the network representation. Then, these representations are combined to perform better than those considering only the structure. This phenomenon shows that incorporating the attributes into NRL in a reasonable way is beneficial to obtain the excellent link prediction results.

- **Structure vs. Structure & Attribute:** We find that the models considering both the structure and attributes tend to perform better than those considering only the structure. Furthermore, our proposed DANRL-ANE model has always achieved better performance than GraRep, especially on social networks, which is worth noting that the node attributes in the PubMed dataset are relatively sparse. The above phenomenon shows that incorporating the attributes into NRL in a reasonable way is beneficial to obtain the excellent link prediction results.

**Structure & Attribute vs. Structure & Attribute:** The comparison among DANRL-ANE, DANE and ANRL-W AN shows that DANRL-ANE has better experimental results on almost all datasets, which further proves the importance of capturing the first-order, second-order, high-order proximity and the attribute semantics together. Meanwhile, it demonstrates that DANRL-ANE can learn the robust and efficient network representation.

### C. Node Classification

Node classification aims to predict the categories of nodes by any known information of the network, which is another common downstream task to evaluate the performance of network embedding [19] [21] [32]. In the experiment, we first learn the vector representation of each node through different models. Then, following the popular practices [18], we randomly sample 30% nodes from the remaining network as the test set. Furthermore, we use the residual network to train the embedding models, which is another common downstream task to evaluate the performance of network embedding [19] [21] [32].
the labeled nodes as the training set, and treat the rest as the test set. Here, SVM is employed as the classifier. To measure the multilabel classification performance, we use Micro-F1 and Macro-F1 as the evaluation metrics. Notably, the above classification process is repeated 10 times and we report the average results. Because we don’t have the ground truth of node labels in Facebook, the node classification task is only performed on four datasets, i.e., Citeseer, PubMed, Cora and Flickr. Furthermore, Table V shows the performance of each network embedding method on different datasets, in which the optimal result is strengthened in bold. We analyze the results as follows.

- **Structure vs. Structure**: Node2vec also shows similar or superior results to DeepWalk on different datasets, which is the same as the previous experiments. Compared with LINE, SDNE shows poor performance on citation networks, especially in the PubMed dataset. Analyzing the characteristics of these networks, we find that the average degree of a network is a key factor affecting the performance of SDNE, and the larger the network average degree is, the worse the performance of SDNE is. The observation indicates that modeling the directly connected relationship between two nodes with joint probability is beneficial to capture the accurate first-order proximity, which explains why the joint probability is used in our model. Unlike that in link prediction, GraRep, which considers all the microscopic structural information, has worse performance than DeepWalk, node2vec and LINE, on citation networks. The result reveals that simply concatenating different order information is not always suitable for any tasks, which emphasizes that a careful design is critical.

- **Structure vs. Structure & Attribute**: Table V shows that the methods incorporating the node attributes into NRL have better experimental results than those only focusing on the structure, which demonstrates the integration of the structural information and attribute semantics is advantageous to learn informative node vectors. For PubMed, compared with DeepWalk, the performance of DANE is poor, which is probably caused by the sparse attributes.

- **Structure & Attribute vs. Structure & Attribute**: Based on the above discussion, the optimal result of DANRL-ANE for PubMed shows that our method is not susceptible to the sparsity of either network structure or node attributes. Meanwhile, the superiority of the proposed DANRL-ANE model over ANRL-WAN and DANE on almost all datasets proves that our method could learn the robust and efficient network representation, and explains the necessity of preserving the first-order, second-order and high-order proximity, which is noteworthy that the Citeseer and Cora dataset are both disconnected networks. In a word, in the node classification task, the proposed DANRL-ANE model is applicable to all kinds of networks, even on sparse networks or networks with isolated nodes, if we can obtain the sufficient attribute information.

VI. CONCLUSION

To integrate the microscopic structural and attribute information for learning the robust and effective node embeddings from various networks, we propose a deep coupling model DANRL-ANE, where three newly designed modules are used to preserve the first-order, second-order and high-order proximity from the structure, respectively. In particular, the node attributes are incorporated into the adjacency matrix based on the social homophily, as the input of our model, so that the structure and attribute information are explored simultaneously. The extensive experiments on the tasks of link prediction and node classification show that our DANRL-ANE model achieves the superior performance comparing with other representation learning models. The work demonstrates that integrating more sources of information in a principled manner is conducive to learning higher quality network representation.

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TABLE V

| Datasets | Citeseer  | PubMed  | Cora  | Flickr  |
|----------|----------|---------|-------|---------|
|          | Micro-F1 | Macro-F1 | Micro-F1 | Macro-F1 | Micro-F1 | Macro-F1 |
| DeepWalk | 0.5665   | 0.5212  | 0.8109 | 0.7978  | 0.7900   | 0.7782  |
| node2vec | 0.6002   | 0.5465  | 0.8104 | 0.7968  | 0.8038   | 0.7942  |
| LINE     | 0.5605   | 0.5256  | 0.8049 | 0.7926  | 0.7884   | 0.7786  |
| GraRep   | 0.4775   | 0.4352  | 0.7416 | 0.7248  | 0.7636   | 0.7496  |
| SDNE     | 0.4161   | 0.3632  | 0.4258 | 0.2900  | 0.5813   | 0.5201  |
| DANE     | 0.6870   | 0.6433  | 0.8063 | 0.7940  | 0.8110   | 0.7944  |
| ANRL-WAN | 0.7246   | 0.6764  | 0.8595 | 0.8584  | 0.8161   | 0.8030  |
| DANRL-ANE| 0.7248   | 0.6744  | 0.8745 | 0.8728  | 0.8291   | 0.8166  |

* We use bold to highlight the best performance.