An Inexpensive Liquid Crystal Spectropolarimeter for the Dominion Astrophysical Observatory Plaskett Telescope

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ABSTRACT. A new, inexpensive polarimetric unit has been constructed for the Dominion Astrophysical Observatory (DAO) 1.8 m Plaskett telescope. It is implemented as a plug-in module for the telescope's existing Cassegrain spectrograph, and it enables medium-resolution ($R \approx 10,000$) circular spectropolarimetry of point sources. A dual-beam design, together with fast switching of the wave plate at rates up to 100 Hz and synchronized with charge shuffling on the CCD, is used to significantly reduce instrumental effects and achieve high-precision spectropolarimetric measurements for a very low cost. The instrument is optimized to work in the wavelength range of 4700–5300 Å to simultaneously detect polarization signals in the Hβ line, as well as nearby metallic lines. In this article we describe the technical details of the instrument, our observing strategy, and data reduction techniques, and we present tests of its scientific performance.

1. INTRODUCTION

Spectropolarimetry has been used for decades to detect magnetic fields in stars throughout the H-R diagram (Donati & Landstreet 2009). Our particular interest in this article, however, is in instrumentation that enables the measurement of strong, large-scale magnetic fields in the chemically peculiar stars (Ap/Bp) of the upper main sequence. Some existing polarimeters permit high-resolution (defined here as $R > 40,000$), high-precision spectropolarimetry in metallic lines of such stars (for example, MuSiCoS and NARVAL on the 2 m Bernard Lyot Telescope at Pic du Midi, and ESPaDOnS on the 3.6 m Canada-France-Hawaii Telescope), but hydrogen lines, due to their large width, provide much lower accuracy. Low-resolution ($R \approx 2000$) instruments such as FORS1 on the 8 m Antu telescope of the VLT (Bagnulo et al. 2002) enable more precise spectropolarimetric measurements of hydrogen lines, but at a cost of providing such low contrast for the metallic lines that they can not be fully utilized. Because of this, high-resolution spectropolarimeters are generally used to measure magnetic fields in Ap and Bp stars using only metallic (and perhaps helium) lines, while only hydrogen lines are measured with low-resolution instruments.

However, for many years it has been known that a number of stars show quite significant discrepancies between magnetic field strengths derived from hydrogen lines versus values found using metallic lines, but with different instruments (for example, Borra & Landstreet 1980; Bychkov et al. 1977). The differences can be from a few hundred gauss to a few kilogauss, or more than 10% of the field strength, since longitudinal magnetic fields in these stars can range from several hundred gauss to several kilogauss. As an example, in 52 Her the average longitudinal field derived from metallic lines is 1500 G, while the average field derived from hydrogen lines is 500 G (Bychkov et al. 1977). Unfortunately, it is unclear as to what part of the observed differences might be due to details of the instrumentation and data analysis techniques and what part may be produced by the very common and often very pronounced nonuniform horizontal and vertical abundance distributions of metals in the photospheres of the Ap and Bp stars.

In an attempt to resolve this long-standing question, we have investigated the possibility of constructing a low-cost, medium-resolution spectropolarimeter that provides circular polarization measurements of hydrogen and metallic lines of Ap and Bp stars and hence enables the measurement of longitudinal magnetic fields with comparable precision using both diagnostics simultaneously. The low cost was dictated by the limited operations and development budget for the DAO telescopes. Despite this constraint, we set out to build an instrument that would let us measure stellar magnetic fields in relatively bright stars with typical accuracies of about 100 G and better than 50 G for the brightest targets. We will demonstrate later that such precisions are sufficient to routinely detect discrepancies between hydrogen and metallic-line longitudinal field measurements, and we will also show for the first time that, for at least one object, these discrepancies do not have an instrumental origin.

A second science goal of the new polarimeter was to provide us with the ability to carry out (in a reasonable length of time) a large, sensitive search for globally ordered magnetic fields in relatively faint and possibly rapidly rotating upper main-sequence peculiar stars observable from the DAO. For hundreds of such poorly studied sixth- and seventh-magnitude Ap and Bp stars, we therefore needed to obtain field measurements with an accuracy on the order of 200 G from observations acquired in 2 hr or less. Such measurements, obtained many times over the
rotation period of the star, are sufficient to confidently detect and characterize the large-scale magnetic fields observed in many upper main-sequence peculiar magnetic stars.

In the remainder of this article we describe the optical and mechanical design of the spectropolarimeter dimaPol, which we have designed and constructed for use on the DAO’s 1.8 m Plaskett telescope for a very low cost of only several thousand dollars (including spare components and parts used only for testing). The polarimeter module can be switched at a rate of up to 100 Hz and is implemented as a plug-in module for the existing Cassegrain spectrograph on the DAO 1.8 m telescope. We describe our data reduction technique that not only enables the use of low-cost, off-the-shelf components in the polarimeter, but also provides near–real-time conversion of the spectropolarimetric data to a magnetic field measurement. A summary of tests we have carried out to investigate the optimal modulation rate of the polarimeter and the best observing strategy is provided, and we also present results of extensive new magnetic field measurements of well-known magnetic stars, as well as nonmagnetic standards, and we demonstrate how these new data compare very favorably with observations made with other, generally much more costly, spectropolarimeters.

2. THE DAO LIQUID CRYSTAL SPECTROPOLARIMETER

The level of polarization observed in starlight is usually very weak. Numerous instrumental effects can make these weak signals undetectable or lead to spurious detections. Most astronomical spectropolarimeters currently in operation use a dual-beam design to deal with this issue. The polarization of the input beam is transformed into an intensity difference between the two output beams. Since both spectra are taken under exactly the same conditions, the polarization signal is independent of sky transparency, seeing, or slit losses, but not the instrumental systematics. A polarization modulator is therefore used in many spectropolarimeters to fight these possible instrumental effects by interchanging the two output beams so that they travel exactly the same optical path through the instrument. Usually, the modulation is achieved by means of the mechanical rotation of an optical element, but this can be a relatively slow process. Since at least two observations are now needed for each distinct configuration of the device and these are separated in time, guiding errors can now come into play. These can cause the intensity distribution of the input light beam across the entrance aperture of the spectrograph to change from one observation to the next, which can in turn lead to a wavelength shift on the detector and hence may result in a spurious polarization signal. A change in brightness due to seeing and transparency variations and different gains in the two instrument channels can also generate a spurious signal (see the discussion of this effect in Povel [2001]). This can be a limiting factor for the sensitivity of a spectropolarimeter unless the instrument is fed by an optical fiber (as in ESPaDOnS, for example) or some form of fast modulation is used. The spectrograph currently permanently installed on the DAO Plaskett 1.8 m telescope is fed directly from the telescope’s Cassegrain focus. Because of this fact, in addition to budget constraints, we confined our design considerations for a new DAO spectropolarimeter to those that made use of a fast-modulation option.

The spectropolarimeter dimaPol is installed in the DAO 1.8 m telescope’s f/18 diverging beam immediately behind one of three possible circular entrance apertures to the Cassegrain spectrograph. The module consists of an achromatic quarter-wave plate, a ferroelectric liquid crystal (FLC) half-wave plate, a calcite beam displacer, and a mechanical shutter (Fig. 1).

We discuss the individual optical components in detail later. The single-order grating spectrograph has an off-axis hyperbolic collimator mirror, a plane diffraction grating, and a spherical camera mirror (Richardson 1968). An 1800 lines mm$^{-1}$ grating provides a spectral resolution of $R = 8000$ to 15,000, depending on the choice of entrance aperture. The 1752 × 532 STe CCD with 15 μm pixels captures an approximately 260 Å long spectral window centered on the Hβ line, and the polarimeter optics have been optimized to work in this wavelength range. The spectral resolution is high enough to resolve spectral lines in slowly rotating stars, but at the same time, it is low enough so that any polarization signal in the broad hydrogen line, as well as broad metallic lines of rapidly rotating stars, can be precisely measured.

2.1. Quarter-Wave Plate

The quarter-wave plate in the polarimeter module converts left and right circularly polarized light in the input beam into linearly polarized light with orthogonal polarization directions. The achromatic quarter-wave plate in dimaPol was made by Bolder Vision Optik and is a multilayer polymer laminated between two optically flat windows. The retardance error is less than 0.004 λ over the wavelength range where the polarimeter performance is optimized (Fig. 2). A polymer plate was selected
Another type of liquid crystal, liquid crystal variable retarders (LCVRs), could have been employed in a fast-switching polarimeter. Such devices are used, for example, in the HiVIS spectropolarimeter on the 3.67 m Advanced Electro-Optical System telescope (Harrington et al. 2010). It should be noted that LCVR plates are almost 2 orders of magnitude slower than FLC plates. After considering several different options, we decided that a FLC plate was the most cost-effective option to allow us to explore fast modulation.

2.3. Modulation

The role of the half-wave plate is to switch the orthogonal states of linear polarization produced by the preceding quarter-wave plate. When the optical axis of the half-wave plate is aligned with the polarization plane, the linearly polarized beam passes through the half-wave plate unchanged; when the optical axis of the half-wave plate is at an angle of 45° to the polarization plane, it rotates the linearly polarized light 90°. As a result, the half-wave plate effectively switches the two orthogonal polarizations by rotating both polarizations 90°.

Because of the beam displacer that follows the half-wave plate, switching the polarization states also results in the polarimeter’s two output beams exchanging places. In dimaPol the modulation of the beams is synchronized with the CCD detector. As discussed previously, the switching needs to be relatively fast in order to eliminate instrumental effects that can affect accurate polarization measurements. Simply reading out the detector frequently after short exposures is not desirable, since this would significantly increase overheads because of the CCD readout time and would likely also quickly wear out the instrument’s shutter. The STe detector is, however, a three-phase CCD that allows bidirectional charge transfer. This permits rapid shuffling of accumulated charge on the CCD back and forth between rows many times before the detector is read out. Such parallel transfers are almost 3 orders of magnitude faster than the readout time for the detector. Rather than reading out the CCD frequently, we instead shuffle the charge on the CCD up and down with every switch of the half-wave plate. This charge-shuffling technique for measuring polarization signals was first implemented by McLean et al. (1981) in the imaging spectropolarimeter at the Royal Observatory, Edinburgh. The shuffle distance in dimaPol is chosen to be the same as the final separation of the two output spectra, or about 40 pixels in a direction perpendicular to the spectra. During the charge shuffling, the orthogonal polarization states never cross each other’s path. The CCD shutter remains open for the duration of an exposure for multiple switch cycles and is kept closed during CCD readout.

The switching time of the FLC half-wave plate at room temperature is about 70 μs, and while it increases to about 120 μs at +10°C, switching at kilohertz rates is possible even at lower temperatures. This is significantly faster than the approximately 2 ms that is needed to move the charge 40 rows on the CCD, so

because of its large acceptance angle—a requirement for use in the diverging input beam from the telescope.

2.2. Half-Wave Plate

The quarter-wave plate is followed by a half-wave plate, a commercial FLC made by Displaytech, Inc. (model LV2500-OEM). This is an electrically switchable retardation plate with a fixed retardation of approximately 180° or λ/2 but the orientation of the optical axis can be switched between two distinct angles by changing the voltage applied across the liquid crystal. A commercial driver DR95 made by Displaytech, Inc., is used to supply and switch the voltage. Switching commands are issued by the CCD controller. For FLC wave plates, this switching can be very fast. In solar astronomy, FLC wave plates have been used in a number of polarimeters: for example, the Zurich Imaging Polarimeter (ZIMPOL, Gisler et al. 2004), the SOLIS Vector-Spectromagnetograph (Keller et al. 2003), La Palma Stokes Polarimeter and Tenerife Infrared Polarimeter at the solar telescopes on the Canary Islands (Martínez Pillet et al. 1999), and the spectrograph of the Pic du Midi Turret Dome (Malherbe et al. 2004). Modulation rates of up to 1 kHz are achieved with ZIMPOL’s specially designed CCD and are also quite high in the other instruments mentioned previously.

A FLC plate was chosen mainly for two reasons: low-cost and the ability to switch fast. We wanted to explore the possibility of improving the accuracy of spectropolarimetric measurements using fast modulation. Pockels cells and piezoelectric modulators, both capable of switching at a rate of many kilohertz, were also examined, but we found these devices to be too costly for our very limited budget. A piezoelectric modulator does not work at low frequencies and would therefore require a special masked detector that we do not have access to. Mechanical rotation would not allow us to explore the potential advantages of fast modulation and is also more expensive than a FLC plate.

![Figure 2](image-url) - Measured retardance of the quarter-wave plate used in dimaPol. The nominal λ/4 retardance is shown by a dashed line. Error bars are approximately the size of the data points.
there is some dead time while charge is being shuffled. Since the wave plate switching time is only a small fraction of the shuffle time, the switching is done in the middle of the charge shuffling to minimize the crosstalk between the two polarizations.

2.4. Retardance and the Switching Angle of the Half-Wave Plate

An obvious advantage of using an electrically switchable wave plate is that there are no moving parts in the polarimeter. This provides better stability and reliability, and it significantly reduces both construction and maintenance costs. FLC wave plates are also true zeroth-order retarders, and they have a large field of view. The acceptance angle of our FLC wave plate is 20°. This permits its use in the f/18 beam from the telescope without introducing any noticeable error in wave plate retardance. The deviation angle of the second polarizer from the open position is then 2 × the departure of the wave plate switching angle from 45°. One of our spare plates was used in this test, and the measurements were performed at 4600 Å, where the retardance of the plate is closest to ideal. Figure 4 shows the results. We find that the switching angle is exactly 45° at +23 ± 1°C—a typical summer temperature at the DAO. In winter, Victoria temperatures drop to +5°C, and the switching angle at this temperature is approximately 48.5°. Our modeling shows that this change in the switching angle can introduce crosstalk from linear to circular polarization of up to 13%. The crosstalk should be significantly less in summer. Crosstalk from linear to circular polarization is not uncommon in other polarimeters, but does not pose a problem when measuring circular polarization in upper main-sequence magnetic stars, because their intrinsic linear polarization is at least an order of magnitude lower than their circular polarization. Thermal stabilization of the FLC could solve the crosstalk issue, but has not been implemented for dimaPol because of lack of space and the limited impact that such crosstalk has on the science that we anticipate performing with the instrument.

\[ \delta = \frac{1}{2\pi} \arccos \left( \frac{I_2 - I_0}{I_2 + I_0} \right), \]

where \(I_2\) and \(I_0\) are the beam intensities with the polarizers open and closed respectively. The retardance of the FLC plate was measured in the same way. All of the measurements were carried out at room temperature.

While the FLC plate retardance is not temperature-dependent, the switching angle is. To examine this effect, we carried out an experiment in the cold chamber at the Herzberg Institute of Astrophysics (HIA), where the temperature of the wave plate could be controlled. The wave plate was placed at 45° between two open polarizers. The second polarizer was rotated from its open position until a minimum in the beam intensity was reached. The deviation angle of the second polarizer from the open position is then 2 × the departure of the wave plate switching angle from 45°. One of our spare plates was used in this test, and the measurements were performed at 4600 Å, where the retardance of the plate is closest to ideal. Figure 4 shows the results. We find that the switching angle is exactly 45° at +23 ± 1°C—a typical summer temperature at the DAO. In winter, Victoria temperatures drop to +5°C, and the switching angle at this temperature is approximately 48.5°. Our modeling shows that this change in the switching angle can introduce crosstalk from linear to circular polarization of up to 13%. The crosstalk should be significantly less in summer. Crosstalk from linear to circular polarization is not uncommon in other polarimeters, but does not pose a problem when measuring circular polarization in upper main-sequence magnetic stars, because their intrinsic linear polarization is at least an order of magnitude lower than their circular polarization. Thermal stabilization of the FLC could solve the crosstalk issue, but has not been implemented for dimaPol because of lack of space and the limited impact that such crosstalk has on the science that we anticipate performing with the instrument.

![Fig. 3.—Measured retardance of the FLC half-wave plate used in dimaPol. The dashed line is the plate’s nominal \(\lambda/2\) retardance.](image)

![Fig. 4.—FLC switching angle as a function of temperature. The data points measurements are performed in a cold chamber at the HIA for one of our spare wave plates. The nominal switching angle of the wave plate is shown by the dashed line. The solid line is a fit to the data of the form \(c_1 + c_2(T_0 - T)^{1/2}\), where \(T\) is the plate temperature and \(c_1, c_2,\) and \(T_0\) are constants. Such a temperature dependence is typical of that observed in FLC wave plates (Blinov & Chigrinov 1994).](image)
2.5. Crosstalk

Departures of wave plate parameters from the ideal creates crosstalk between the two polarimeter channels. Some of the light from the ordinary beam leaks into the extraordinary beam and vice versa. As a result, one will see a change in the measured Stokes $V$. We used the data in Figures 2—4 to estimate how much the Stokes $V$ measurement is affected by such crosstalk. We obtained estimates for two different temperatures: $+5^\circ C$ and $+15^\circ C$. We assumed that the instrument is fed with 100% circularly polarized light (i.e., the Stokes $V$ is equal to 1), and the results are shown in Figure 5. The departure of the Stokes $V$ from 1 tells how much crosstalk there is in the system. As expected, the amount of crosstalk is higher at the lower temperature, mostly due to the increase in the FLC switching angle from 47° at $+15^\circ C$ to 48.5° at $+5^\circ C$. This crosstalk can be significantly reduced by rotating the FLC plate by 2° around the beam and in the direction opposite to the wave plate axis tilt. The amount of crosstalk is reduced by a factor of 2 at the lower temperature and decreases insignificantly at the higher temperature. As a consequence, in the case of a simple Zeeman triplet and a magnetic field aligned parallel to the line of sight, dimaPol will underestimate the longitudinal field component by about 0.5 to 1%. However, longitudinal magnetic fields are very rarely measured with an accuracy sufficient to detect such a small discrepancy (for example, Bychkov et al. 1977).

The difference in transmittance of the FLC wave plate along the fast and slow axes (up to a few percent), together with different transmittance for ordinary and extraordinary beams inside of the spectrograph, results in spurious continuum polarization. The amplitude of this signal reaches 1% at some wavelengths, but since this unwanted signal is much broader than any spectral line in the region, including Hβ, and is a smooth function of wavelength, it can be easily filtered out during data reduction, as discussed subsequently.

2.6. Beam Displacer

A 20 mm long calcite beam displacer separates the orthogonal linear polarizations into two parallel beams. The ordinary beam with the plane of polarization along the dispersion travels straight through the displacer, while the extraordinary beam emerges from the beam displacer with a constant displacement of about 2 mm in the direction perpendicular to the dispersion. Because of this, after passing through the spectrograph, the two beams arrive at two different locations on the detector, where both orthogonal states of polarization can be measured simultaneously. At the detector the spectra are separated by $\approx 0.6$ mm, or $\approx 40$ pixels. Again, it is important to note that the two beams never move on the detector and that there are no moving parts in the polarimetric module. The two beams always illuminate the same rows of the detector.

With no half-wave plate switching and no CCD charge shuffling, the observation of a star with dimaPol would obviously result in two spectra being imaged on the CCD, but with very poor polarimetric precision because of the instrumental effects mentioned previously. The implementation of charge shuffling results in three spectra being produced as follows (and illustrated in Fig. 6). At the start of an exposure the left circularly polarized light traveling through the polarimetric module becomes the ordinary beam, while the right circularly polarized light becomes the extraordinary beam. As a result, two spectra (LO and RE) appear on the CCD. Then, when the FLC wave plate switches (and ignoring, for now, the fact that the charge shuffling takes considerably longer than the wave plate switch), the charge in the LO and RE spectra is shifted upward so that RE is brought up to where the ordinary beam is projected on the detector.
CCD, and LO is placed 40 rows higher, outside of the light collecting area. But at the same time, because of the wave plate switch, the right circularly polarized light becomes the ordinary beam (RO) and so it is projected right onto RE. RO and RE then mix together to form a single right circularly polarized spectrum. The left circularly polarized light becomes the extraordinary beam after the wave plate switch, and because of the charge shuffle, this creates a third spectrum (LE). Now there are three spectra on the CCD: LO, RO + RE, and LE. When the modulator switches again, all three spectra are shuffled 40 rows back down and the cycle repeats. How these three spectra are processed and manipulated to measure a stellar magnetic field is discussed in the next section.

Since only a single beam displacer is used in dimaPol, the ordinary and extraordinary beams travel slightly different optical path lengths and therefore have different foci. Zemax models show that the difference in the best focus position is very small—approximately 20 μm. When the spectrograph is focused at an intermediate position (when both images are slightly out of focus), the degradation in image quality amounts to less than 2 μm, or roughly 0.1 pixel. This is less than our typical focus uncertainty and can therefore be neglected. The difference in optical path between the two beams is also wavelength-dependent; as a result, the size of the extraordinary image along the dispersion is about 15% larger at the blue end of the detector. There is also a small difference in dispersion between the two beams. Despite these effects, when the ordinary and extraordinary beams are combined (see the next section), the spectral resolution is reduced by less than 5%, and so we felt that there was little need to use a much more costly Savart plate instead of a single calcite crystal. Savart plates are comprised of two plates of birefringent material rotated 90° with respect to each other. The extraordinary beam in the first plate then becomes an ordinary beam in the second plate and vice versa; as a result, both beams have nearly identical optical paths and focus positions.

After the beam displacer, a fast mechanical Uniblitz shutter is installed. The shutter has opening and closing times of 18 ms and 12 ms, respectively.

All optical surfaces in the polarimetric module are antireflection-coated. The transmission of the polarimeter module is therefore quite high and varies smoothly between 74 and 80% within its operational wavelength range.

3. FAST SWITCHING AND OBSERVING STRATEGY

We have already noted that switching a spectropolarimeter quickly helps to reduce the impact of spurious signals that can arise from changes in the spectrograph aperture illumination due to seeing and transparency variations, guiding errors, and other telescope instabilities. Some of these changes in illumination can be averaged out during long exposures, but trends that manifest themselves only on timescales of hours are not compensated for in this way. It therefore seems that a better observing strategy for effectively eliminating the effects of changes in aperture illumination is to take multiple short exposures, switch the polarimeter module after each, and then combine the resulting sequence of exposures. When a short switching time is used, it is much more efficient to do the averaging on-chip by moving the accumulated charge back and forth, rather than after many CCD readouts, and this is what we do with dimaPol.

But the question arises as to how many times the polarimeter module needs to be switched in order to provide the most effective averaging and hence elimination of spurious signals. We have performed a series of on-sky experiments in an attempt to answer this question. In these tests we kept the total integration time on the target constant, but we varied the shuffle time or the number of shuffles per exposure. We define the shuffle time as the amount of time used to expose briefly, switch the polarimetric FLC half-wave plate, and move the charge on the detector. The number of shuffles is simply the total exposure time divided by the shuffle time. Only an even numbers of shuffles are used, to make sure that the polarized spectra obtained for successive targets always appear in the same place on the CCD.

A cycle of two shuffles therefore consists of the following sequence: expose, switch the wave plate, move the charge, expose, switch the wave plate to its original state, and move the charge back. As noted earlier, it takes approximately 2 ms to move the charge 40 rows on the CCD, while the switching of the wave plate is considerably faster and is performed at the middle of the shuffling phase. The total dead time per shuffle is therefore approximately 2 ms, and this sets a lower limit to the
possible shuffle time, to ensure an efficient duty cycle. We refer to this as “dead time,” since some of the light on the detector gets spread in between the spectra during this period, and this signal is removed, together with the rest of the background signal, during processing (described subsequently).

For our switching tests, we observed Vega, which, along with its brightness, offers the advantage of having narrow spectral lines and hence makes it an easy target to obtain high-quality magnetic field measurements in a very short period of time. The exposure time for individual observations in a given observing sequence was kept constant at 6 s, to provide approximately the same signal per exposure, while the shuffle time from observation to observation was varied between 0.06 and 3 s (corresponding to a range of two to 100 shuffles per exposure). CCD charge-trapping sites begin to manifest themselves when a few hundred shuffles or more are executed (Bland-Hawthorn & Barton 1994). These traps create spikes in the extracted spectra, polluting the polarization signal. In order to avoid this effect, we limited ourselves to 100 shuffles. On three different nights we obtained a total of 21 magnetic field measurements derived from the H\beta line. Each measurement was based on the average of 30 individual 6 s exposures. We did two things to minimize the effect of changing weather conditions and flux variations on our results: first, the shuffle time was changed quasi-randomly from measurement to measurement, but within the 0.06 to 3 s range; second, the longitudinal field error bars were normalized by the flux as $\sigma(B_1)_{\text{norm}} = \sigma(B_1)(\text{flux}/\text{flux}_{\text{max}})^{1/2}$.

Figure 7 shows how the accuracy of magnetic field measurements obtained with dimaPol vary as a function of the number of shuffles. The magnetic error bar is largest when only two wave plate switches and charge shuffles are carried out. The gain in accuracy has therefore been measured by normalizing the estimated error in the longitudinal magnetic field for an arbitrary even number of shuffles to the mean value found for observations with just two shuffles. The magnetic field error bars get smaller as the number of shuffles increases until a plateau is more or less reached at about 30 shuffles. The accuracy is improved by a factor of 2 when 30 or more switches are executed. We also carried out observations of scattered solar light. The telescope was pointed at the sky near the zenith during the day, and series of 50 short 4 s exposures were obtained for several different shuffle speeds. Unlike the stellar measurements, these scattered solar light observations are not affected by slit losses and can therefore be used to test for systematics within the spectropolarimeter itself, while excluding other telescope instabilities. The results are presented in Figure 7, along with the results for Vega. For both Vega and scattered solar light, the 95% confidence interval of the standard deviation is also shown. For Vega, a third-degree polynomial approximation of points was used for $N \leq 30$, and the average accuracy gain of 2.08 was assumed for $N > 30$. The points are within the confidence intervals for both data sets. There is no change in the accuracy gain seen for the scattered solar light data, which means that slit losses are most likely responsible for the accuracy degradation in Vega at low switching speeds. Switching more than 30 times eliminates the effect these losses have on the longitudinal magnetic field measurements.

As a result of these tests, we have adopted a standard observing strategy for use with dimaPol. To make a single magnetic field measurement, we obtain a series of typically 10 to 16 short exposures (each, for example, 5 or 10 minutes long for a sixth- or seventh-magnitude star) of the target, with 60 wave plate switches and charge shuffles performed during each exposure. This keeps the switching time shorter than the typical time of instrumental response changes and also allows an estimate of the magnetic field uncertainty to be made from the scatter of measurements obtained from the individual exposures.

Because exposure times are short, we also bin every two pixels of the SITe CCD along the direction perpendicular to the dispersion to speed up the readout of the CCD and reduce the impact of readout noise. Since typical seeing at the DAO is around 2–3′′, we use the 2′′ entrance aperture for all observations with the polarimeter. We also acquire 60 s iron-argon comparison lamp exposures before the start and at the conclusion of the observing sequence for each star. The polarization module switches at 1 Hz for the arc exposures so that we have the usual 60 switches and shuffles for the arc observations that we use for our science exposures.

4. DATA REDUCTION

We have developed a collection of MIDAS scripts that enable near–real-time processing of the data produced with dimaPol. This software provides a measurement of the longitudinal
magnetic field and its associated uncertainty within a few minutes of the acquisition of the last spectrum in an observing sequence for a star. For every individual exposure, we perform bias subtraction and cosmic-ray and background removal, and then we extract the spectra. The bias level in each image is determined by measuring just the CCD overscan area and subtracting this from all of the other image pixels. The remaining background is removed in the next step.

As has been mentioned earlier, the CCD shutter remains open for many wave plate switch and charge shuffle cycles. Because of this, even though the parallel charge transfer takes very little time, some light from the source does get spread out between the three recorded spectra during the shuffling process, and this creates an additional background source on the detector. This extraneous light needs to be removed before the polarized spectra can be extracted. The background flux has a trapezoid-like shape when viewed along the CCD columns. We divide each CCD image into three sections, one for each of the three spectra, and treat the background in each section separately. In each of the two outer sections we fit second-order polynomials to the background flux measured on either side of each spectrum; a simple first-order polynomial is used to average the background flux on either side of the spectrum in the middle section. These three independent polynomials are fit to every CCD column, and the resulting background fit for each column is then subtracted from the corresponding column in the original image.

The next processing step is the extraction of the polarized spectra. The three spectra (denoted previously as LO, RO + RE, and LE) are extracted separately. During the spectrograph, CCD, and polarimeter configurations carried out in advance of each polarimeter run, considerable care is taken to ensure that the acquired spectra run parallel to the CCD rows. The spectrum inclination and curvature are then typically less than 5 μm over the approximately 26 mm length of CCD. This makes the spectral extraction process quite simple: CCD rows inside of a predefined aperture are simply co-added. We have determined that the best results are obtained when five CCD rows are co-added. Since the CCD is binned by a factor of 2 perpendicular to the dispersion, this corresponds to 10 unbinned rows on the detector. Such an aperture gives the best signal-to-noise ratio (S/N) when a 2″ spectrograph circular entrance is used. The size of the aperture is fixed, and the same size is used to extract all three spectra. The three apertures are placed 40 pixels from each other (corresponding exactly to the charge shuffle distance) to make sure that we always extract the same pixels for the RO + RE, LO, and LE spectra. The two polarizations are exposed on exactly the same set of physical pixels, even though the charge during shuffling may be stored in different places. After extraction, the LO and LE spectra are combined into a single spectrum, LO + LE.

As alluded to earlier, the FLC wave plate and other optical elements in the spectrograph introduce an extremely broadband spurious continuum polarization that can produce a weak circular polarization signal, even from an unpolarized light source. The effect is wavelength-dependent and, for an unpolarized light source, leads to an LO + LE spectrum that is ≈1% brighter than the RO + RE spectrum at both ends, while the two spectra have almost identical intensities in the middle. Even though this broadband signal changes very little from exposure to exposure and from object to object, it can affect precise line-shift measurements required for magnetic field observations, since the small wavelength-dependent difference in brightness between the two polarizations results in an artificial line shift. It is also dependent on the size of the spectral window used for measuring pixel shifts and discussed subsequently: the broader the spectral window, the larger the introduced pixel shift. If not taken into account during the data processing, this instrumental shift can be as large as a few hundredths of a pixel; as will be seen, this can lead to a spurious, and obviously significant, signal on the order of a few hundred gauss.

In order to remove this effect, we apply a chromatic correction to our data. A third-degree polynomial is sufficient to fit the variation in $I_{LO+LE}/I_{RO+RE}$ along the direction of the dispersion. The unnormalized RO + RE spectrum is then multiplied by this fit to eliminate the artificial brightness difference between the two polarizations, and it removes the spurious line shift as well. Note that the chromatic correction is only derived from and applied to the final combined LO + LE and RO + RE spectra for an entire observation, not to individual exposures. This minimizes the possible impact of low-S/N levels in individual observations on the polynomial fit for the correction. We feel that normalizing $I_{LO+LE}/I_{RO+RE}$ is far preferable to trying to normalize the intensities of the LO + LE and RO + RE spectra independently. The spurious continuum polarization as it manifests itself in $I_{LO+LE}/I_{RO+RE}$ can be fit very well with a low-order polynomial. On the other hand, the continuum in the intensity spectrum is considerably more complex in shape and is more difficult to reconstruct, especially when broad spectral lines are present and when the normalization has to be carried out in a completely automated fashion for stars with a wide range of spectral types during data acquisition.

Finally, the magnetic shift observed in a single spectral line due to the Zeeman effect is then measured by performing a Fourier cross-correlation of the final combined and corrected LO + LE and RO + RE spectra in a spectral window centered on the spectral line of interest. Several different methods of measuring the magnetic shift in a single line have been used by different authors. These include the center-of-gravity method (Rees & Semel 1979) and its implementations by Mathys (1988) and Donati et al. (1997), the so-called photopolarimetric method (Bray & Loughhead 1964) adapted by Borra & Landstreet (1973) for use with a two-channel Balmer-line photoelectric Pockels cell polarimeter and by Bagulo et al. (2002) for use with the FORS1 spectropolarimeter, and the Fourier cross-correlation technique (Monin et al. 2002). We have adopted the Fourier cross-correlation
method for use with dimaPol because of the technique’s relative insensitivity to continuum and line shapes, which permits its use with unnormalized spectra and without prior knowledge of the intrinsic profile of the line in the absence of a magnetic field.

The magnetic shift is translated into a longitudinal magnetic field, \( B_l \) (in gauss), according to the line’s magnetic sensitivity or the Landé factor and the relation (for example, Landstreet 1992)

\[
B_l = \Delta X \times 0.15/(2 \times 4.67 \times 10^{-13} \lambda^2 g),
\]

where \( \Delta X \) is the observed shift between the spectra in pixels, \( \lambda \) is the wavelength of the line center in angstroms, and \( g \) is the Landé factor for the line. For hydrogen lines, the Landé factor is 1 (Casini & Landi Degl’Innocenti 1994), while for metallic lines, the Landé factors are taken from the Vienna Atomic Line Database (VALD; Kupka et al. 2000). The measured shift in pixels is multiplied by the average dispersion of 0.15 Å/pixel\(^{-1}\). The change in dispersion that arises along the spectrum as a result of the calcite beam displacer is small and can be neglected. For H/β observations with dimaPol, this equation is transformed to the simple relation \( B_l = 6.8 \times \Delta X \) kG. In other words, a 1 pixel shift between the RO + RE and LO + LE spectra corresponds to a longitudinal magnetic field strength of 6.8 kG.

More than 10 individual observations, and hence magnetic measurements, are usually obtained in succession for a typical \( V = 7 \) target, and many more are often acquired for observations of very bright stars (usually, known magnetic standards or nulls observed during each observing run to monitor performance of the instrument). The multiple independent longitudinal field measurements are then averaged, and an error bar can then be derived from the scatter of these individual values after weighting by the flux, as discussed in the previous section.

Figure 8 shows a histogram of 100 measurements of the shift between the RO + RE and LO + LE spectra for the bright, sharp-lined Ap star HD 112413 (\( \alpha^2 \) CVn) obtained in succession over almost 1 hr on a single night. The mean shift between spectra is \( \approx 0.09 \) pixels, corresponding to a field strength of \( \approx 600 \) G, and the sample standard deviation is \( \approx 0.04 \) pixels, or \( \approx 270 \) G. The measurements are apparently distributed normally as a curve representing a normal distribution with a mean of 0.09 pixels, and variance of \((0.04 \text{ pixels})^2\) fits the histogram of observations very well. A Kolmogorov-Smirnov test confirms that the measurements are very likely normally distributed; the \( P \)-value of 0.98 indicates that the histogram points and the normal distribution differ insignificantly. When the points are normally distributed, the standard error of the mean is proportional to \( N^{-1/2} \), where \( N \) is the number of observations.

Therefore, it seems quite reasonable in the case of dimaPol data to estimate the magnetic field error bars by multiplying the standard deviation of the individual observations by this same factor. In the preceding example, the error bar is then \( 0.04 \times 100^{-1/2} = 0.004 \) pixels, or \( \approx 27 \) G.

Experimentation has demonstrated that the error bars are minimized by optimizing the size of the window used for the Fourier cross-correlation so that the window includes the part of the profile that gives the strongest polarization signal (Fig. 9). The window size ranges from 16 pixels, or about 2.4 Å, for narrow-line stars (such as \( \alpha^2 \) CVn) to 128 pixels, or 19 Å, for broad-line stars.

A careful reader may think that we have omitted some details of our data reduction procedure, but this is not the case. Flat-fielding of the DAO spectropolarimetry is not necessary for our primary goal of measuring longitudinal magnetic fields. As mentioned earlier, both of the left and right circularly polarized spectra are exposed on exactly the same CCD pixels. As a result, pixel-to-pixel sensitivity variations are the same for both and do not affect the final magnetic-line-shift determination. We do, however, normally obtain sequences of high-S/N flat-field spectra several times during each observing run in case they are needed in the future, for example, for a detailed analysis of Stokes \( I \) line-profile variations.

The use of a Fourier cross-correlation algorithm to derive the observed longitudinal magnetic field also simplifies processing by removing any need for continuum normalization. Thanks to the fast switching of the polarimeter module, variations in spectrum brightness due to changing sky conditions, slit losses, and other instrument changes are effectively averaged for both polarizations. This results in the shape of the continuum being almost identical in both polarizations. The Fourier cross-correlation algorithm that we use is insensitive to features that have a similar shape in both polarizations, and so the algorithm can be successfully applied to unnormalized spectra, which

![Image](image_url)
greatly facilitates the near–real-time processing of the polarimeter data while observing.

Wavelength calibration of the spectra is also not required for our magnetic field measurements, since the Fourier cross-correlation of the polarized spectra is carried out in pixel space. Wavelengths are generally only needed for line identification, and for this we use the two iron-argon comparison lamp exposures obtained before the start and at the conclusion of each sequence of observations for a given science target. The comparison spectra are processed in the same way as the science spectra, the arc lines are identified, and a second-order polynomial is used to derive the dispersion relation.

In addition to providing measurements of longitudinal magnetic fields, dimaPol also allows investigations of the circular polarization signal within the profiles of many spectral lines, including Hβ. The circular polarization signal, Stokes V, is calculated very simply as the difference in brightness between the LO+LE and RO+RE spectra, normalized by the total flux:

\[ V = \frac{(I_{LO+LE} - I_{RO+RE})}{(I_{LO+LE} + I_{RO+RE})}. \]

An example of a short section of a Stokes V spectrum can be seen in Figure 9.

The presence of the spurious continuum polarization introduced by the FLC wave plate and other optics and the crosstalk from linear to circular polarization makes it very difficult to measure circular continuum polarization with dimaPol. However, in sources with a high degree of circular polarization and an insignificant amount of continuum linear polarization, this can be done, albeit with somewhat limited precision.

5. MAGNETIC FIELD OBSERVATIONS WITH DIMAPOL

Details of observations of the first new magnetic star discovered with dimaPol have recently been presented by Bohlender & Monin (2011). Along with such ongoing science programs, however, regular testing of the polarimeter is also performed to confirm that the instrument does not produce spurious polarization signals that could lead to false magnetic field detections. To ensure that this is the case, during every scheduled polarimeter run, we observe magnetic null standards: bright stars that have been observed with high precision numerous times with a variety of other polarimeters and have shown no evidence for detectable magnetic fields at a level of a few tens of gauss. Seven such stars have been repeatedly observed by us over a 2 yr period. These include HD 886 (γ Peg), HD 36486 (δ Ori A), HD 76644 (ι UMa), HD 97633 (θ Leo), HD 156164 (δ Her), HD 172167 (Vega), and HD 210027 (ι Peg).

Both slowly and rapidly rotating stars are included in this collection of standards, with \( v \sin i \) ranging from 3 km s\(^{-1}\) to 290 km s\(^{-1}\). A total of 133 individual magnetic field measurements have been obtained from observations of the Hβ line, and they are all within ±3σ of 0 G. The average error bar, \( \sigma_{B_l} \), is 78 G and the best is 21 G. The null standards do not show any systematic errors at this level, and data for some of them, shown in Figure 10, also demonstrate that the measured longitudinal magnetic field error bars scale with the square root of the flux, as expected. Using the single Hβ line, an accuracy of 20 to 40 G...
is reached in 20 minutes in good weather conditions for our slowly rotating (<20 km s\(^{-1}\)) third- to fourth-magnitude standards. Obviously, the accuracy is lower for faster-rotating stars, simply because of the decrease in sensitivity of the cross-correlation measurements as the spectral lines become broader. For example, for HD 76644 (\(V = 3.1\); \(v \sin i = 150\) km s\(^{-1}\)) we obtain 70–80 G error bars in about 30 minutes. For the typical sixth- to seventh-magnitude stars in our science programs, an accuracy of 100 to 200 G is reached in between 1 and 2 hr.

Vega has recently been shown to possess an extremely weak magnetic field (<1 G; Lignieres et al. 2009; Petit et al. 2010), but a field of this level is well beyond the detection capability of dimaPol, and we therefore continue to use this convenient bright star as a magnetic null standard. As shown in Figure 11, no evidence for a magnetic field is seen in the Stokes \(V\) signature of Vega as observed with dimaPol.

One null standard, \(\iota\) Peg, has been observed 21 times on 15 different nights. The scatter of the resulting 21 individual \(H\beta\) longitudinal magnetic field measurements about the 0 G level is 48 G, in good agreement with the average \(\sigma_B = 58\) G for the individual observations (Fig. 12). This again reassures us that our derived error bars adequately reflect the true accuracy of the observations.

As an additional test of dimaPol performance, we have carried out observations of scattered solar light during several observing runs. For such observations, the telescope is usually pointed at the sky near the zenith during the day, and long series of short exposures (typically 4 to 6 s, although as long as 30 s on several occasions) are obtained. Very high precision measurements can be acquired because of the brightness of the light source and the high contrast provided by the solar spectrum’s narrow lines. We have carried out these observations 37 times over a period of 2 yr, and a total of 3660 individual spectra have been obtained. No systematic shifts between the individual RO + RE and LO + LE spectra have been detected at a level corresponding to a longitudinal magnetic field strength of 15 G.

Our preceding discussion shows that dimaPol does not produce spurious magnetic field detections, at least at the level of a few tens of gauss. This does not, however, guarantee that the instrument can reliably measure a real magnetic signal when a field is present. In order to regularly test the instrument’s ability to detect and accurately evaluate longitudinal magnetic fields, we also attempt to make observations of a few well-known magnetic Ap stars during each observing run. One example of an object that we have repeatedly observed is the bright prototypical magnetic Ap star HD 112413 (\(\alpha^2\) CVn). The star has a well-established rotation period of 5.46939 days (Farnsworth 1932) and a strong, reversing longitudinal magnetic field that varies between \(-1\) and \(+1\) kG (Kochukhov & Wade 2010). At the time of writing, we have observed it 34 times, with total integration times ranging from 7 minutes to 1 hr, with an average of 20 minutes. A representative observation showing the magnetic signature in the Stokes \(V\) profile is illustrated in Figure 13. Note that the scale used for the Stokes \(V\) spectrum in this figure is the same as that used in Figure 11 for Vega; the signature of the magnetic field in \(\alpha^2\) CVn is obvious.

Longitudinal magnetic field measurements of \(\alpha^2\) CVn have been obtained by using both the \(H\beta\) line and the single metallic line \(Fe\ II\ \lambda 4923\). The latter feature was selected because it is the strongest metallic line in the wavelength range covered by dimaPol, and with a Landé value of 1.69, it is also quite sensitive to the presence of a magnetic field. Table 1 provides the
for our new DAO data are, on average, almost 2 times better than those of Borra & Landstreet (1977), despite the approximately 3-times-shorter integration time for the new observations. The scatter of the DAO points around a best-fit sinusoid is 60 G—quite close to the average error bar of our measurements. This is another indication that our error bars adequately represent the accuracy of our magnetic field measurements.

Figure 15 shows our longitudinal magnetic field measurements obtained with the Fe II λ4923 line, as well as values derived from the least-squares deconvolution (LSD) of multiple metallic lines (Wade et al. 2000) using spectra obtained with dimaPol. The resulting magnetic field curves produced from the measurements of the Hβ and Fe II lines are shown in Figures 14 and 15, respectively. Figure 14 compares dimaPol Hβ longitudinal magnetic field measurements with those published by Borra & Landstreet (1977) and obtained with a two-channel Balmer-line photoelectric Pockels cell polarimeter. The Pockels cell polarimeter measurements have been multiplied by 4/5, as suggested by Mathys et al. (2000) in order to account for the Stark effect. This correction only applies to measurements in the line wings where the Stark effect is a factor. The agreement between the two sets of observations is very good. Note that the error bars for our new DAO data are, on average, almost 2 times better than those of Borra & Landstreet (1977), despite the approximately 3-times-shorter integration time for the new observations. The scatter of the DAO points around a best-fit sinusoid is 60 G—quite close to the average error bar of our measurements. This is another indication that our error bars adequately represent the accuracy of our magnetic field measurements.

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We have designed and constructed a very inexpensive dual-beam polarimeter for use on the DAO 1.8 m Plaskett telescope. The polarimeter, dimaPol, is implemented as a plug-in module for the telescope’s Cassegrain spectrograph and provides medium-resolution circular spectropolarimetry of point sources over a 260 Å wide spectral window centered on the H\textbeta line. The instrument therefore provides DAO 1.8 m telescope observers with the ability to measure longitudinal magnetic fields using the Zeeman effect in both the H\textbeta and metallic lines of the peculiar A and B stars of the upper main sequence.

We demonstrate that the use of an electrically switchable ferroelectric liquid crystal (FLC) half-wave plate to quickly switch the orthogonal polarizations between the instrument’s two channels, in combination with synchronized shuffling of the accumulated charge on the CCD, greatly reduces instrumental effects and increases the accuracy of the magnetic field measurements. With extensive on-sky tests, we show that by executing 30 to 100 such switches, the accuracy of the longitudinal magnetic field measurements can be improved by a factor of 2. The use of the FLC wave plate also eliminates the need for any moving parts in the polarimeter module and therefore provides better stability and reliability and significantly lower construction and maintenance costs.

A near–real-time data reduction pipeline has been implemented with MIDAS and provides observers with the ability to obtain a longitudinal magnetic field measurement and its uncertainty within seconds of completing an observing sequence on a star. The observed shift between the recorded left and right circularly polarized spectra is performed with a Fourier cross-correlation technique that is not sensitive to continuum variations or intrinsic spectral line shapes, and so it can be carried out without interaction from the user. For magnetic field measurements using the H\textbeta line, dimaPol provides the simple relation $B_l = 6.8 \times \Delta X \text{ kG}$, where $\Delta X$ is the observed shift between the polarized spectra in pixels.

A number of bright well-established magnetic stars and magnetic null standards have been repeatedly observed over a 2 yr period. No systematic errors have been found at the level of 15 to 20 G. Our multiple observations of the magnetic Ap standard $\alpha^2$ CVn (as well as other objects not discussed here) clearly demonstrate that the longitudinal magnetic field derived from dimaPol H\textbeta and metallic-line observations agree well with previously published results. In addition, the derived uncertainties of the field measurements compare favorably with, or exceed, the accuracies achieved with other, often much more expensive, polarimeters on similar-sized telescopes. To provide a rough estimate of the capabilities of dimaPol, observations of a typical sixth- or seventh-magnitude star in our current science programs reach an uncertainty of 100 to 200 G in a typical 1–2 hr observation (e.g., see Bohlender & Monin 2011).

We have begun several research programs with dimaPol on the DAO 1.8 m telescope, but we encourage any interested users to apply for observing time with the instrument. Our main survey program consists of an extensive search for magnetic fields in previously poorly studied (and generally relatively faint, $V > 7$) Ap and Bp stars. In a second program we are taking advantage of the capability of the instrument to provide longitudinal magnetic field measurements in both the H\textbeta line and metallic lines to investigate the reality and cause of the often-discrepant magnetic field strengths measured with the two diagnostics, but frequently with very different instrumentation. As discussed in the previous section, $\alpha^2$ CVn is an example of one such object.

Despite its cost of only several thousand dollars, dimaPol is proving to be a very capable addition to the complement of instrumentation available on the DAO 1.8 m Plaskett telescope and has opened up an entirely new avenue of research at the DAO.
DAO. At such a low cost, many institutes with spectroscopic capabilities on even very modest telescopes could readily consider building a similar device for research purposes or student training.

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2012 PASP, 124:329–342