Dielectric Mie Resonance-Enhanced Photocatalysis on Cuprous Oxide Nanostructures

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ABSTRACT

Nanostructured metal oxides, such as Cu$_2$O, CeO$_2$, α-Fe$_2$O$_3$, and TiO$_2$ can efficiently mediate photocatalysis for solar-to-chemical energy conversion and pollution remediation. In this contribution, we report a novel approach, dielectric resonance-enhanced photocatalysis, to enhance the catalytic activity of metal oxide photocatalysts. Specifically, we report that Cu$_2$O cubic particles of 297 nm edge length and spherical particles of 115 nm diameter exhibit a higher photocatalytic rate as compared to Cu$_2$O spherical nanoparticles of 37 nm diameter. Using transient absorption measurements, we demonstrate that the higher photocatalytic rates observed on submicron Cu$_2$O particles are due to a coherent electronic process that supports dielectric-resonance mediated charge carrier generation. For small Cu$_2$O spherical nanoparticles of 37 nm diameter, the dielectric resonances are absent. Although we demonstrated the concept using Cu$_2$O particles, our FDTD simulations predict that this concept can be broadly applied to other metal oxide photocatalysts, including CeO$_2$, α-Fe$_2$O$_3$ and TiO$_2$.

TOC GRAPHICS
Ever since the discovery of titanium dioxide (TiO$_2$) semiconductor-based photo-electrochemistry for water splitting by Fujishima and Honda in 1972, they have opened the gateway for semiconductor-assisted photocatalysis.$^1$ The idea of bandgap-facilitated photochemistry on semiconductors has been the basis for research over the next five decades. In bandgap-facilitated photocatalysis on semiconductors, the photo-excited electrons and holes can drive reduction and oxidation reactions, respectively (Figure 1a). The excited electron-driven reduction of protons (H$^+$) into hydrogen (H$_2$) and hole-driven oxidation of water into oxygen (O$_2$) are the examples of photon-excited charge carriers-driven chemistry.

Researchers have explored the properties of semiconductors such as cerium oxide (CeO$_2$), cuprous oxide (Cu$_2$O), hematite iron (III) oxide ($\alpha$-Fe$_2$O$_3$) and TiO$_2$ in the last four decades for the solar-to-chemical energy and pollution mitigation applications.$^{2-7}$ But some challenges still exist in using semiconductor (only)-based photocatalysts for the efficient conversion of solar energy into chemical energy. For instance, the semiconductor nanostructures lack efficient utilization of incoming photons because of their inherently poor absorption cross section.$^8$ Plasmonic metal nanostructures (PMNs) have emerged as promising materials to overcome some of these limitations. Specifically, studies in the last decade have shown that hybrid and composite photocatalysts built on PMNs (e.g., Al, Ag, Au, and Cu) and metal oxide semiconductors (e.g., Cu$_2$O, $\alpha$-Fe$_2$O$_3$, and TiO$_2$) can exhibit enhanced photocatalytic activity as compared to semiconductor (only) photocatalysts.$^{8-15}$

The absorption cross sections of PMNs are four to five orders of magnitude higher than dye molecules.$^{16}$ This strong interaction of PMNs with the incident ultraviolet/visible (UV/Vis) light is due to the localized surface plasmon resonance (LSPR).$^{16-18}$ The PMN can therefore efficiently
harvest the incident light and transfer the energy into the nearby metal oxide semiconductor via a number of electron- and energy-transfer pathways, including plasmon-induced hot electron transfer, nanoantenna effect, and plasmon-induced resonance energy transfer (Figure 1b).\textsuperscript{8–11} The plasmonic resonance-mediated energy transfer from PMN into the nearby metal oxide semiconductor can result in an enhanced rate of formation of excited electrons and holes in the conduction and valence bands of the semiconductor, respectively (Figure 1b).\textsuperscript{9} These enhanced rates of formation of charge carriers are shown to result in enhanced photocatalytic activity in PMN-metal oxide composite photocatalysts.\textsuperscript{8–12,19} In our previous contribution,\textsuperscript{20} we have reported that similar to the plasmonic resonances in PMNs, tunable dielectric resonances can be created in metal oxide particles by controlling their size and shape. Herein, we demonstrate that these dielectric resonances can be utilized to enhance the inherent photocatalytic activity of metal oxide photocatalysts (Figure 1c). In the plasmonic resonance-mediated photocatalytic approach shown in Figure 1b, two building blocks are required: PMN to facilitate the plasmonic resonance and semiconductor for the bandgap-facilitated reduction and oxidation (redox) reactions. In contrast, in the proposed dielectric resonance-mediated photocatalytic approach shown in Figure 1c, a single metal oxide building block can serve the dual function and exhibit both the dielectric resonance behavior and the bandgap-facilitated redox reactions.
Figure 1. Schematic diagram illustrating (a) formation of photoexcited electrons (e\(^{-}\)) and holes (h\(^{+}\)) in semiconductor (SC), (b) plasmonic resonance-mediated formation of excited electrons and holes in SC, and (c) the proposed dielectric resonance-mediated formation of excited electrons and holes in SC. In (a), (b), and (c), excited electrons in the conduction band (CB) and excited holes in the valence band (VB) of SC can drive reduction and oxidation reactions.

The plasmonic and dielectric resonances are two distinct sub-categories of Mie resonances.\(^{21,22}\) The plasmonic resonances occur for materials with negative values of the real part of the permittivity (\(\varepsilon < 0\)). The Mie resonances can also occur for materials with positive values of permittivity (\(\varepsilon > 0\)). When Mie resonances occur in the positive permittivity region, the resonances
are known as dielectric resonances. Specifically, dielectric resonances can occur in materials with moderate (2.5-3.5) and high refractive index (>3.5).\textsuperscript{23} Compared to plasmonic, Mie resonances which exhibit only the electric multipole resonances (e.g., electric dipole, quadrupole, etc.), the dielectric Mie resonances can exhibit electric and magnetic multipole resonances upon light excitation.\textsuperscript{20} Similar to the plasmonic resonances, the dielectric resonance wavelengths are also tunable with the size and shape of the particle.\textsuperscript{20} At the resonance wavelengths, the dielectric nanostructures can act as optical nanoantenna and exhibit orders of magnitude enhancements for the electric and magnetic fields of the incident light. The nanoantenna and light trapping effects of dielectric nanostructures are utilized for dielectric resonance-enhanced light absorption, fluorescence, and Raman scattering.\textsuperscript{21} For example, dielectric Mie resonances have been demonstrated for their use in controlling and enhancing light absorption for solar fuel generation and thin-film solar cell applications.\textsuperscript{24,25}

The dielectric resonances can also result in the appearance of Mie absorption peaks in the UV-Vis-near infrared (UV-Vis-near IR) absorption spectra of medium- and high-refractive index dielectric particles.\textsuperscript{20} These Mie absorption peaks, which are not present in their bulk counterparts, provide an opportunity for enhanced light harvesting capability in dielectric particles. For example, FeS\textsubscript{2} nanocubes with dielectric Mie absorption have been demonstrated to exhibit a higher photothermal conversion efficiency as compared to the small FeS\textsubscript{2} nanoparticles not exhibiting dielectric Mie absorption.\textsuperscript{26} Herein, we demonstrate that submicron Cu\textsubscript{2}O cubic particles with dielectric Mie absorption peaks exhibit a higher photocatalytic rate as compared to small Cu\textsubscript{2}O spherical nanoparticles not exhibiting dielectric Mie resonances.

Cu\textsubscript{2}O is a semiconductor with a bandgap of \textasciitilde2.1 eV.\textsuperscript{5-7,27} It is also a moderate refractive index material with the values of the real part of the refractive index in the range of \textasciitilde2.6 - 3.1 (SI).\textsuperscript{20}
Cu$_2$O is also known for exhibiting a relatively long lifetime of excited charge carriers (electrons and holes) that is on the order of milliseconds.$^{28,29}$ In our previous contribution$^{20}$, we have demonstrated that: (i) submicron Cu$_2$O cubic particles of edge lengths greater than ~ 100 nm exhibit strong dielectric resonances in the Vis-near IR regions, (ii) the dielectric resonance strengths of these Cu$_2$O cubic particles are similar to or greater than plasmonic resonances of Ag particles of similar sizes, and (iii) small Cu$_2$O spherical and cubic particles of sizes less than 100 nm exhibit light absorption features similar to their bulk counterparts and does not exhibit any Mie resonances in the Vis-near IR regions. In this contribution, we demonstrate that large Cu$_2$O cubic particles of 297 nm average edge length exhibit higher visible-light photocatalytic activity for methylene blue (MB) dye degradation as compared to small Cu$_2$O spherical nanoparticles of 37 nm average diameter. We attribute the higher photocatalytic rate of large Cu$_2$O cubes to their dielectric Mie resonances, which are not present in the small Cu$_2$O spheres. The results from the photoreactor studies are supported by the transient-absorption measurements that are used to identify the incoherent or coherent charge carrier dynamics that are markedly different for the small Cu$_2$O spheres and large Cu$_2$O cubes.

Syntheses and characterizations of small Cu$_2$O spheres, large Cu$_2$O spheres, and large Cu$_2$O cubes: Microemulsion technique$^{30,31}$ is used for the synthesis of small Cu$_2$O spheres. For the syntheses of large Cu$_2$O spheres and cubes, chemical reduction method$^{20}$ is used. The detailed procedures followed for the syntheses and characterizations of Cu$_2$O particles, and finite-difference time-domain (FDTD) simulations, photocatalytic experiments, and transient absorption measurements are provided in the supporting information (SI).

Figure 2a and Figure 2b show the representative TEM images of large Cu$_2$O nanocubes of 297 nm average edge length and small Cu$_2$O spheres of 37 nm average diameter, respectively. The Cu$_2$O
phase of these cubical and spherical particles are confirmed using the XRD analysis of the respective particles (e.g., Figure S1b and Figure S1c in SI). The photocatalytic performances of large Cu$_2$O nanocubes and small Cu$_2$O nanospheres towards MB degradation are evaluated under visible light irradiation. In these studies, the photocatalytic MB dye degradations are carried out for the same weight load of small Cu$_2$O spheres and large Cu$_2$O cubes. The blue and green LED lamps that emit light with peak wavelengths at 456 and 519 nm, respectively, are used as the visible light source. In Figure 2c, we provide the spectrum of blue and green LEDs and the absorption spectrum of MB. As seen from Figure 2c, there is minimal overlap between the spectrum of the light source (i.e., blue and green LEDs) and the absorption spectrum of methylene blue. This minimal overlap will ensure that the MB dye degradation due to direct dye excitation is minimal. In Figure 2d, we show the extent of MB dye degradation (i.e., ratio of concentration of MB to its initial concentration, $C/C_0$) by large Cu$_2$O cubes and small Cu$_2$O spheres as a function of visible light irradiation time. As seen from Figure 2d, large Cu$_2$O nanocubes exhibit a significantly higher MB degradation rate than small Cu$_2$O nanospheres. We also performed photocatalytic experiments under visible light irradiation in the absence of Cu$_2$O particles and found no significant MB degradation under these blank conditions (Figure 2d).
Figure 2. Representative TEM images of (a) large Cu$_2$O nanocubes of 297 ± 38 nm edge length, and (b) small Cu$_2$O nanospheres of 37 ± 6 nm diameter. (c) Absorption spectrum of MB (left ordinate) and spectrum of blue and green LED light source used for photocatalytic degradation of MB (right ordinate). (d) Plot of C/C$_0$ versus irradiation time for photocatalytic degradation of MB in ethanol using large Cu$_2$O nanocubes (blue squares), small Cu$_2$O nanospheres (orange circles), and under blank conditions in the absence of photocatalyst (green diamonds).

To confirm that the MB degradations shown in Figure 2d are not due to the light-induced heating effect, we measured the change in temperature of the reaction mixture as a function of irradiation time. We found that visible light irradiation increases the temperature of the reaction mixture from ~20 °C to a maximum of ~31 °C (Figure S2a-c in SI). Specifically, we observed a similar extent of increase in temperature for the photocatalytic experiments performed using small Cu$_2$O spheres,
large Cu$_2$O cubes, and under blank conditions in the absence of Cu$_2$O particles (Figure S2a-c in SI). The heat localization in our system is also expected to be minimal since the photocatalytic experiments are performed in the liquid medium under stirring.$^{32}$ We also carried out heating experiments in the presence of large Cu$_2$O cubes under dark conditions. In these heating experiments, the temperature of the reaction mixture is maintained at 60 °C. For all tested experimental conditions, the heating trials revealed no significant MB degradation in the absence of light exposure across an extended period (Figure S2d in SI).

To show that the higher photocatalytic rates of large Cu$_2$O cubes in Figure 2d are due to their dielectric Mie resonances, in Figure 3a, we show the UV-Vis extinction spectra of large Cu$_2$O cubes and small Cu$_2$O spheres. As seen from Figure 3a, small Cu$_2$O spheres, in consistent with what is expected for their bulk counterparts, exhibit no resonance peaks in the UV-Vis-near IR extinction spectra. In contrast, large Cu$_2$O cubes exhibit multiple resonance peaks in the visible to near IR regions. To understand the nature of these resonance peaks, we performed FDTD simulations of Cu$_2$O spherical particle of 37 nm diameter and Cu$_2$O cubical particle of 297 nm. The simulated extinction spectra of these particles are shown in Figure S3a in SI. The features observed in the simulated extinction spectra of small Cu$_2$O spheres and large Cu$_2$O cubes are consistent with the experimentally measured extinction spectra of the respective Cu$_2$O particles shown in Figure 3a. The magnetic and electric field distributions at different wavelengths across the resonance peaks of the Cu$_2$O cubes of 297 nm edge length are also provided in Figure S3b-c in SI. The field distributions confirm that the resonance peaks observed in the extinction spectra of the Cu$_2$O cube are due to the dielectric Mie resonances.$^{20}$ From the field distribution maps, we assign the lowest energy resonance peak observed in the extinction spectrum of the Cu$_2$O cube to the combination of electric and magnetic dipoles (Figure S3b-c in SI).$^{20}$ Similarly, we assign the
second lowest energy resonance peak and higher-order resonance peaks to the combination of electric and magnetic quadrupoles and the combination of higher-order electric and magnetic resonance modes, respectively.\textsuperscript{20}

In Figure 3b, we show the simulated absorption spectra of small Cu\textsubscript{2}O spheres and large Cu\textsubscript{2}O cubes. The y-axis values in the figure correspond to the volume-normalized absorption cross section. This normalized absorption cross section is a good descriptor to predict the relative photocatalytic rates of large Cu\textsubscript{2}O cubes and small Cu\textsubscript{2}O spheres (see SI for more details). Also, the wavelengths of interest for comparison are in the range of 400-600 nm since the blue and green LEDs used in our system cover this wavelength region. As seen from Figure 3b, in the 400-600 nm wavelengths region, large Cu\textsubscript{2}O cubes exhibit relatively higher overall light absorption capacity than small Cu\textsubscript{2}O spheres. Specifically, the higher-order dielectric Mie resonances in the Cu\textsubscript{2}O cube provide enhanced overall light absorption capacity in the 400-600 nm region. Therefore, we attribute the enhanced photocatalytic rate of large Cu\textsubscript{2}O cubes shown in Figure 2d to their dielectric Mie resonances-mediated Mie absorption, which is absent in small Cu\textsubscript{2}O spheres.

To compare and confirm this Mie resonance effect in Cu\textsubscript{2}O particles of the same shape, we carried out photocatalytic experiments using large spherical particles of 115 ± 25 nm diameter. We find that these large spherical particles of 115 nm average diameter exhibit dielectric Mie resonance peaks and a higher photocatalytic rate as compared to small Cu\textsubscript{2}O spherical nanoparticles not exhibiting dielectric Mie resonances (Figure S3d-f in SI).
Figure 3. (a) Experimentally measured UV-Vis-near IR extinction spectra of large Cu₂O nanocubes of 297 ± 38 nm edge length and small Cu₂O nanospheres of 37 ± 6 nm diameter dispersed in ethanol. (b) FDTD-simulated normalized absorption cross section (normalized σ_{acs}) as a function of incident light wavelength for a large Cu₂O nanocube of 297 nm edge length and a small Cu₂O nanosphere of 37 nm diameter. (c) Temporal response of the differential transmission of small Cu₂O spheres of 37 ± 6 nm and 43 ± 5 nm diameters and large Cu₂O cubes of 297 ± 38 nm and 292 ± 39 nm edge lengths. (d) Temporal response of the normalized differential transmission with exponential fits overlaid for small Cu₂O spheres of 43 ± 5 nm diameter and large
Cu$_2$O cubes of 292 ± 39 nm edge length. A pump pulse of 400 nm wavelength and a probe pulse of 800 nm wavelength are used in (c) and (d).

To further illustrate the Mie resonance-mediated photocatalysis, we show the transient absorption spectra of large Cu$_2$O cubes and small Cu$_2$O spheres in Figure 3c-d. Specifically, Figure 3c shows the transients for short time periods for two sets of small Cu$_2$O spheres of 37 ± 6 nm and 43 ± 5 nm diameters and two sets of large Cu$_2$O cubes of 297 ± 38 nm and 292 ± 39 nm edge lengths. Using the pump and probe conditions described in the methods section, the excitation in either sample is sufficiently above any absorption edge of the Cu$_2$O, creating excited-state charge carriers. The probe pulse then senses the excited-state carriers through free-carrier absorption of the pumped carriers, pushing them further into their respective bands. For the positive delay time both small Cu$_2$O spheres and large Cu$_2$O cubes exhibit a three-component exponential decay with typical delay times corresponding to a few picoseconds, a few tens of picoseconds, and a few hundred picoseconds. Fits are overlaid on the transient-absorption data shown for the full-data range for one of each sample type in Figure 3d and extracted parameters are given in Table 1.

Markedly, the negative delay time response from the large Cu$_2$O cubes does not have the fast rise that is seen exhibited by the small Cu$_2$O spheres. In the latter, the rise is limited to the autocorrelation of the pump and probe pulses in the sample, typically the same order of magnitude as the laser pulse width (~100 fs). The response of large Cu$_2$O cubes is indicative of a coherent response, like that seen as perturbed free induction in bleachable dyes,$^{33}$ GaAs quantum well,$^{34}$ single interfacial quantum dots,$^{35}$ and Au@SiO$_2$@Cu$_2$O core-shell nanoparticles that demonstrate plasmon-induced resonance energy transfer (PIRET, Figure 1b).$^9$ Experimentally, these processes are observed because the weaker probe pulse imparts its coherent wavefront into the samples,
which evolves over time, but has sufficient “memory” to then scatter some of the stronger pump light into the probe-detection direction, hence making this coherent process visible during negative delay times. The negative delay time response is fit with a double exponential decay, which reveals a faster component of a similar rise time as that of the nanospheres, which do not exhibit the protracted rise and a slower (~5 ps) response that is associated with the coherent energy transfer mechanism. Extracted fit parameters are also shown in Table 1.

Table 1. Extracted fitting parameters for the differential transmission data.

| Cu₂O Sample        | t₁ (ps) | t₂ (ps) | t₁₂ (ps) | t₂₀ (ps) | t₂₃ (ps) |
|--------------------|---------|---------|----------|----------|----------|
| Spheres (37 ± 6 nm)| 0.41    | -       | 0.36     | 34.0     | 2282.9   |
| Spheres (43 ± 5 nm)| 0.64    | -       | 0.95     | 40.0     | 2073.6   |
| Cubes (292 ± 39 nm)| 0.72    | 5.4     | 2.37     | 37.1     | 669.6    |
| Cubes (297 ± 38 nm)| 0.53    | 4.5     | 2.43     | 37.5     | 672.0    |

The coherent signature observed in the transient absorption of large Cu₂O cubes is expected because the dielectric Mie resonance-mediated charge carriers generation in dielectric Cu₂O particles (Figure 1b) is most likely a coherent process, in a similar way to the PIRET-mediated charge carriers generation in the Cu₂O shell of Au@SiO₂@Cu₂O core-shell nanoparticles (Figure 1b).⁹ Hence, the results of transient absorption measurements shown in Figure 3c-d and Table 1 provide direct evidence of a coherent process in the large Cu₂O cubes.

To illustrate the photocatalytic mechanism that is responsible for the MB degradation on large Cu₂O cubes, we investigated the possible role of the solvent and superoxide (O₂⁻) on the MB degradation. To investigate the solvent dependency on the MB degradation, we performed photocatalytic experiments using two different solvents, dimethylformamide (DMF) and ethanol,
and the representative results are shown in Figure 4a. In the solvent-dependent studies, Cu$_2$O cubes exhibited a similar or slightly faster MB degradation in DMF compared to ethanol. We attribute the observed slightly faster MB degradation to the expected higher solubility of dissolved oxygen in DMF compared to ethanol. Previous studies have demonstrated that MB degradation on semiconductor photocatalysts can occur via a superoxide-mediated mineralization mechanism.$^{36,37}$

To investigate whether the photocatalytic MB degradation occurs via a superoxide-mediated mechanism, we performed the photocatalytic experiments with and without benzoquinone, a well-known scavenger of the superoxide.$^{38}$ The results from these experiments are shown in Figure 4b. The direct evidence of the superoxide-mediated mechanism can be gathered from Figure 4b, with the benzoquinone successfully inhibiting the MB degradation via scavenging of the superoxide.

Based on these findings, we propose the following photocatalytic mechanism for the MB degradation on large Cu$_2$O cubes. This mechanism, schematically illustrated in Figure 4c, involves the excitation of dielectric Mie resonances by the incident photons. The energy stored in Mie extinction dissipates into Mie scattering and Mie absorption. A major fraction of the energy that corresponds to Mie absorption transfers into and results in the coherent generation of excited electrons (e$^-$) and holes (h$^+$) in the conduction and valence bands of Cu$_2$O, respectively. The excited electrons from the conduction band reduce the dissolved oxygen (O$_2$) into superoxide (O$_2^-$). The superoxide then reacts with the MB molecule and forms several intermediate products, one of them being a carboxylic acid (RCOO$^-$) intermediate.$^{36,37}$ This intermediate can be oxidized by the excited hole (h$^+$) in the valence band into degradation products.$^{36,37}$
Figure 4. (a) Plot of $C/C_0$ versus irradiation time for photocatalytic degradation of MB in ethanol (red and blue squares) and DMF (red and blue diamonds) using large Cu$_2$O nanocubes. (b) Plot of $C/C_0$ versus irradiation time for photocatalytic degradation of MB in the presence (blue circles) and absence (red diamonds) of benzoquinone using large Cu$_2$O nanocubes in DMF. (c) Schematic diagram illustrating the proposed dielectric resonance-enhanced photocatalytic degradation of MB that occurs via a superoxide (O$_2^-$)-mediated mechanism. (d) FDTD-simulated normalized absorption cross section (normalized $\sigma_{\text{acs}}$) as a function of incident light wavelength for a large $\alpha$-Fe$_2$O$_3$ nanosphere of 300 nm diameter and a small $\alpha$-Fe$_2$O$_3$ nanosphere of 10 nm diameter.
The dielectric resonance-enhanced photocatalytic approach demonstrated herein can be potentially applied to other metal oxide photocatalysts. For example, CeO$_2$, $\alpha$-Fe$_2$O$_3$, and TiO$_2$ semiconductors are also moderate and high refractive index materials with the values of the real part of the refractive index in the range of 2.1-2.5, 2.7-3.3, and 1.4-5.4, respectively (SI). To investigate whether these metal oxide particles exhibit dielectric resonance characteristics similar to that of Cu$_2$O, we performed FDTD simulations to simulate the absorption spectra of different sizes of CeO$_2$, $\alpha$-Fe$_2$O$_3$, and TiO$_2$ particles. The representative spectra are shown in Figure 4d and also in Figure S4a-c in SI. Our FDTD simulations show that CeO$_2$, $\alpha$-Fe$_2$O$_3$, and TiO$_2$ particles exhibit dielectric resonance characteristics that are similar to Cu$_2$O particles. Specifically, our findings show that small nanoparticles such as spherical nanoparticles of 25 nm diameter exhibit light absorption features similar to their bulk counterparts and do not exhibit any Mie resonances in the near UV-Vis-near IR regions. In contrast, large nanoparticles such as spherical nanoparticles of 200 nm diameters exhibit strong dielectric resonances. For example, Figure 4d shows the normalized absorption cross section values as a function of incident light wavelengths for 25 and 200 nm spherical $\alpha$-Fe$_2$O$_3$ particles. As seen from Figure 4d, in the visible region, 200 nm spherical particle exhibits relatively higher light absorption capacity than small spheres of 25 nm diameter. Similar to the dielectric resonance-enhanced photocatalysis demonstrated in larger Cu$_2$O cubic particles in this contribution, the dielectric resonance features of larger CeO$_2$, $\alpha$-Fe$_2$O$_3$, and TiO$_2$ particles can be possibly explored to enhance their inherent photocatalytic activity. We also used this rational approach to develop structure-performance relationship between the size of Cu$_2$O spheres and cubes and their photocatalytic performance. The results are shown in Figure 5. The weight load of NPs was kept constant in these experiments. As seen from Figure 5, our simulation
as well as experimental results predict a volcano-type relationship between the photocatalytic rate and the size of Cu$_2$O nanostructures.

![Volcano plot showing the predicted and experimentally measured relative photocatalytic rate as a function of size of Cu$_2$O spheres and cubes. Cu$_2$O cubes of 292 nm average edge length is used as a reference.](image)

**Figure 5.** Volcano plot showing the predicted and experimentally measured relative photocatalytic rate as a function of size of Cu$_2$O spheres and cubes. Cu$_2$O cubes of 292 nm average edge length is used as a reference.

In conclusion, the present work demonstrates dielectric resonance-enhanced photocatalysis in submicron Cu$_2$O cubical and spherical particles. Specifically, submicron Cu$_2$O particles with dielectric resonances exhibit a higher photocatalytic rate for MB degradation in comparison to small Cu$_2$O spherical nanoparticles not exhibiting dielectric resonances. These results are supported by the transient absorption measurements that differentiate the charge carrier dynamics
of large Cu$_2$O cubes and small Cu$_2$O nanospheres, indicating an optical resonance process that involves the coherent generation of charge carriers in the submicron cubes. The dielectric resonance-enhanced photocatalytic approach demonstrated in this study using Cu$_2$O particles is expected to translate to other metal oxide photocatalysts such as CeO$_2$, α-Fe$_2$O$_3$, and TiO$_2$ that exhibit size- and shape-dependent dielectric resonances. The dielectric Mie resonance-mediated charge carrier generation in the metal oxide semiconductors has a number of advantages over plasmonic resonance-mediated charge carrier generation. Specifically, in the latter case, the plasmonic Mie mode decays to a hot electron (and hole). In comparison to the lifetime of hot electron (and hole), the electron-hole pair lifetime in the metal oxide semiconductor is longer, which will translate to a much more efficient photocatalysis. Therefore, the dielectric resonance-enhanced photocatalysis demonstrated in our study opens a new avenue for solar light harvesting and photocatalysis.

ASSOCIATED CONTENT

Supporting Information

Detailed descriptions of photocatalysts syntheses and characterization procedures, photocatalytic experimental procedures, transient absorption measurements, FDTD simulations and supporting figures are listed and supplied in Supporting Information.

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Supporting Information

Dielectric Mie Resonance-Enhanced Photocatalysis on Cuprous Oxide Nanostructures

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I. Syntheses and characterizations of small and large Cu$_2$O spherical particles and large Cu$_2$O cubic particles

Small Cu$_2$O nanoparticles of quasi-spherical shape and 37 ± 6 nm diameter were synthesized at room temperature (~20 °C) using the microemulsion technique. In this synthesis method, 54.5 mL of n-heptane (oil phase) and polyethylene glycol-dodecyl ether (Brij, average Mn ~362) as surfactant are added to a 250 mL round bottom flask and allowed to stir at 550 rpm. 5.4 mL of 0.1 M copper nitrate aqueous solution is added to this mixture and 1 M hydrazine solution (5.4 mL) is added as a reducing agent. This oil in water micro-emulsion utilizes the fact that small sizes of reverse micelles are formed in which the Cu$_2$O nanoparticles are formed. The mixture is allowed to stir for 12 hours after which acetone is added to break the emulsion and centrifuged. These nanoparticles are washed three times (sonicated and centrifuged) to remove the surfactant and to obtain Cu$_2$O spherical nanoparticles that are ready to be used as photocatalyst for methylene blue dye degradation.

Large Cu$_2$O cubes of 297 ± 38 nm edge length were synthesized using a chemical reduction method performed at room temperature (~20 °C). In this method, we first prepared a copper source of 30 mL of 0.0032 M aqueous CuCl$_2$ solution. This solution is put into a three-neck round bottom flask, which is put in an inert environment filled with nitrogen. We added 1 mL of 0.35 M aqueous NaOH solution to this solution at room temperature, which should result in the creation of blue-colored Cu(OH)$_2$ colloids almost immediately. The sodium ascorbate (reducing agent) was then added in 1 mL increments. The solution subsequently became orangish-yellow, suggesting that Cu$_2$O cubic particles are formed. The synthesis duration was a period of one hour after which, the Cu$_2$O cubes were washed using ethanol three times (sonicated and centrifuged). The catalyst is suspended in 4 mL of the reaction solvent as per the reaction procedure mentioned in section II and is ready for use in photocatalytic experiments.

The chemical reduction method at a synthesis temperature of 55 °C was used for the synthesis of large Cu$_2$O quasi-spherical particles of 115 ± 25 nm diameter. 50 mL of 10 mM CuCl$_2$ aqueous solution was prepared in a 100 mL round bottom flask. The mixture was allowed to stir at 900 rpm at 55°C. 5 mL of 2 M NaOH solution was added to the mixture and allowed to stir under constant heating (55 °C) for 30 minutes, followed by the addition of 5 mL of 0.6 M ascorbic acid aqueous solution as reducing agent. The synthesis mixture was allowed to stir for 5 hours. The resulting nanoparticles were separated by washing them in DI water and ethanol three times each to remove all residue from the synthesis mixture. The washed and clean large Cu$_2$O spherical nanoparticles were then used in the photocatalytic experiments.

The synthesized Cu$_2$O spherical and cubical particles were characterized using UV-Vis-near IR extinction spectroscopy, X-ray diffraction (XRD) analysis, transmission electron microscopy (TEM), and scanning electron microscopy (SEM). All UV-Vis-near IR extinction spectra were taken using an Agilent Cary 60 Spectrophotometer. XRD patterns were acquired using a Philips X-Ray diffractometer (Phillips PW 3710 MPD, PW2233/20 X-Ray tube, Copper tube detector – wavelength ~ 1.5418 Angstroms), operating at 45 KW, 40 mA. The TEM images were taken using JEOL JEM-2100 TEM and Thermo Fisher Scientific Titan Themis 200 G2 aberration-corrected TEM. The JEOL JEM-2100 system is equipped with a LaB6 gun and an accelerating voltage of
200 kV. The Titan Themis 200 system is equipped with a Schottky field-emission electron gun and operated at 200 kV.

II. Experimental procedure for performing photocatalytic experiments

Photocatalytic dye degradation reaction conditions: A 6 mL quartz tube and the Luzchem Exposure Panels provided with LED lamps (Figure S1f in SI) were used as a reaction chamber and the visible-light source, respectively. To measure the photocatalytic activity of small Cu$_2$O spheres and large Cu$_2$O cubes, the reaction mixture containing 1 mM concentration of MB and 5.8 mg of Cu$_2$O photocatalyst in 4 ml of solvent (dimethylformamide or ethanol) was first allowed to equilibrate at room temperature (~20 °C) for 3 hours in the dark. The reaction mixture was then sparged with air for 30 minutes to keep the soluble oxygen (O$_2$) content in the solvent same for all experiments. The equilibrated mixture under the stirring conditions at room temperature was then exposed to the visible light (i.e., blue and green LEDs). The intensity of this light source, when measured at the surface of the photoreactor, was 88,680 mW/m$^2$. To measure the extent of photodegradation of MB by small Cu$_2$O spheres and large Cu$_2$O cubes, the MB concentration (C) in the reaction mixture was quantified as a function of reaction time. The MB absorption value at its peak absorption wavelength (i.e., 665 nm) was used to quantify the MB concentration in the reaction mixture. More specific details are also provided below.

5.8 mg of Cu$_2$O nanocatalyst (spheres or cubes) is uniformly dispersed (sonicated for 2 minutes) in 4 mL of reaction solvent (dimethylformamide, DMF, or ethanol, EtOH). The mixture is added to a 6 mL quartz test tube (i.e., photoreactor). For experiments with benzoquinone, 43.2 mg (100 mM) of benzoquinone is added to the reaction mixture. 10 mM methylene blue (MB) solution is made in the same reaction solvent (DMF or EtOH) used for photocatalytic reaction. 150 µL of 10 mM MB solution is added to the reaction mixture in the quartz test tube and allowed to stir at 1150 rpm and equilibrate at room temperature for three hours in the dark environment. The reactor is transferred to the Luzchem LED Panels (arranged with 4 Luzchem Exposure panels), where LED lamps can be attached as shown in Figure S1f. Sampling was done as a function of reaction time by taking 100 µL of the reaction mixture and diluted in 4 mL dilution solvent (DMF or EtOH). Care was taken to make sure the reaction solvent and diluent are the same. These samples were characterized by UV-Vis to obtain absorption of methylene blue and corresponding C/C$_0$ values as a function of time were obtained. Incident light intensities were measured using Intell Pro Instruments Pro, Smart Sensor purchased from Luzchem Research Inc. The detector is placed exactly where the reactor is placed inside the Luzchem reactor (arranged with 4 Luzchem Exposure panels). Using the Smart sensor and AR823 Digital Lux meter (i.e., purchased from Luzchem Research Inc), the corresponding settings based on the wavelength range of the LED light intensity are measured in Lux. The values are converted to Light intensity in mW/m$^2$ by multiplying measured lux with the calibration factors.

III. Transient absorption measurements

Transient absorption measurements: Optical pump-probe experiments were performed using ~100 fs pulses from a 1-kHz laser amplifier, with a pump center wavelength of 400 nm and a probe center wavelength of 800 nm. Photoexcitation by the pump pulse is above the Cu$_2$O bandgap and created photoexcited charge carriers. The probe pulse determines the subsequent photocarrier
dynamics predominantly through free-carrier absorption. All samples are mixed with a ~1% concentration by mass into a KBr matrix and compressed into a semitransparent disc and measured at room temperature. More specific details are also provided below.

Transient absorption measurements were performed using ~100-fs pulses from a laser amplifier with a 1-kHz repetition rate. The amplifier emits pulses with a center wavelength of 800 nm, which are separated into two replica pulses, time-delayed with a mechanical translation stage with a total relative delay time of ~2 ns. The pump pulses are frequency-doubled in a β-barium borate crystal to 400-nm, so they have photon energy well above the bandgap of Cu2O. The probe pulse remains at 800 nm, close to the band edge of the samples. The probe light transmits (and scatters) through the sample. Each transmission sample is a compressed disk, consisting of approximately 1% of the powdered sample in a KBr matrix, produced in a light vacuum for samples with lower scattering.

At the samples, the pump beam has a 1/e² diameter of ~0.35 mm and an average beam power of 1.12 mW, whereas the probe beam has a 1/e² diameter of ~0.1 mm and an average beam power of 0.5 mW. Differential transmission data is recorded in a silicon photodetector, feeding a lock-in-amplifier that is referenced to a mechanical chopper placed in the pump beam and synchronized to a sub-harmonic of the laser amplifier.

IV. Details of finite-difference time-domain (FDTD) simulations

To implement FDTD simulations, we employed the Lumerical FDTD package. The real (n) and imaginary (k) parts of the refractive indexes used in the simulations for Cu2O, CeO2, α-Fe2O3, and TiO2 are shown in Table S1-S4, respectively. The perfectly matched layer (PML) boundary conditions were used for the simulations in all x, y, and z directions. The simulations were performed in a surrounding medium with a refractive index of 1. For the simulations of extinction, scattering, and absorption spectra, the respective cross sections as a function of wavelengths were calculated using the total-field/scattered-field (TFSF) formalism. The incident light source used for these simulations was the Gaussian source in the simulated wavelength region. On implementing the simulations of the magnetic and electric field distributions, a plane wave was used as electromagnetic field incidence with propagation in the x-axis direction, and polarization along the y-axis and the z-axis for the electric field and the magnetic field, respectively.

For the calculation of the normalized absorption cross section, we propose here a simple approximation to relate the photocatalytic rates to the optical and geometrical properties of metal oxide particles. This approximation is similar to the approximation proposed by Ingram et al\textsuperscript{2} for understanding plasmonic resonance-enhanced photocatalysis. In our proposed approximation, the photocatalytic rate (r) at given incident light wavelength is proportional to the incident light intensity (I₀), the ratio of absorption cross section (σ_{acs}) to geometric cross section (G) of the particle, and surface to volume (S/V) ratio of the particle as shown in the equation below.

\[ r \propto I_0 \times \frac{\sigma_{acs}}{G} \times \frac{S}{V} \]  

(1)

When a constant incident light intensity is used as in our case of photocatalytic experiments with large Cu2O cubes and small Cu2O spheres, the above approximation can be written as: \( r \propto \frac{\sigma_{acs}}{G} \times \frac{S}{V} \). Therefore, we define the normalized absorption cross section as normalized \( \sigma_{acs} = \frac{\sigma_{acs}}{G} \times \frac{S}{V} \).
Supplementary Information Figures

Figure S1a. Time-evolution of extinction spectra of Cu$_2$O cubes synthesized using chemical reduction method. The arrow shows the direction of synthesis time. The legends show the synthesis time.
Figure S1b. Representative X-ray diffraction pattern of large Cu$_2$O cubes of 297 ± 38 nm edge length synthesized using chemical reduction method.
**Figure S1c.** Representative X-ray diffraction pattern of small Cu₂O spheres of 37 ± 6 nm diameter synthesized using microemulsion method.
**Figure S1d.** Representative transmission electron microscopy image of large Cu$_2$O cubes of 297 ± 38 nm edge length synthesized using chemical reduction method.
Figure S1e. Representative transmission electron microscopy image of small Cu₂O quasi-spherical particles of 37 ± 6 nm diameter synthesized using microemulsion method.
Figure S1f. Photoreactor reactor set up of Luzchem Exposure Panels connected with 10 blue and 10 green LED lamps.
**Figure S2a-c.** Temperature profile measured as a function of irradiation time during photocatalytic degradation of MB in ethanol for different conditions: (a) blank conditions in the absence of photocatalyst, (b) using small Cu$_2$O nanospheres of $37 \pm 6$ nm diameter, (c) using large Cu$_2$O nanocubes of $297 \pm 38$ nm edge length. The data represented by green squares, red diamonds, and blue circles show the temperature of the sample in the photoreactor, temperature of the reactor surrounding, and ambient room temperature of the laboratory, respectively.
Figure S2d. Pot of $C/C_0$ of methylene blue versus reaction time measured during heating experiments at 60 °C in the presence of large Cu$_2$O cubes in ethanol under dark conditions (i.e., in the absence of LED light exposure).
Figure S3a. FDTD-simulated volume-normalized extinction cross section of large Cu$_2$O nanocube of 297 nm edge length and small Cu$_2$O nanospheres of 37 nm diameter.
Figure S3b (I). FDTD-simulated spatial distribution of enhancement in magnetic field intensity $[\frac{H^2}{H_0^2}]$ in YZ plane at different wavelengths across the lowest energy Mie resonance peak wavelength (i.e., 986 nm) for Cu$_2$O cube of 297 nm edge length.
Figure S3b (II). FDTD-simulated spatial distribution of enhancement in magnetic field intensity $[H^2/H_0^2]$ in YZ plane at different wavelengths across the second lowest energy Mie resonance peak wavelength (i.e., 701 nm) for Cu$_2$O cube of 297 nm edge length.
Figure S3c (i). FDTD-simulated spatial distribution of enhancement in electric field intensity $[E^2/E_0^2]$ in XY plane at different wavelengths across the lowest energy Mie resonance peak wavelength (i.e., 986 nm) for Cu2O cube of 297 nm edge length.
Figure S3c (II). FDTD-simulated spatial distribution of enhancement in electric field intensity \([E^2/E_0^2]\) in XY plane at different wavelengths across the second lowest energy Mie resonance peak wavelength (i.e., 701 nm) for Cu2O cube of 297 nm edge length.
**Figure S3d.** Representative scanning electron microscopy image of large Cu$_2$O quasi-spherical particles of 115 ± 25 nm diameter synthesized using chemical reduction method.
**Figure S3e.** Experimentally measured UV-Vis-near IR extinction spectra of large Cu$_2$O nanospheres of 115 ± 25 nm diameter and small Cu$_2$O nanospheres of 37 ± 6 nm diameter.
Figure S3f. Plot of C/C₀ versus irradiation time for photocatalytic degradation of MB in DMF using small Cu₂O nanospheres of 37 ± 6 nm diameter (grey circles) and large Cu₂O nanospheres of 115 ± 25 nm diameter (green circles) under green and blue LED illumination.
**Figure S4a.** FDTD-simulated normalized absorption cross section (normalized $\sigma_{acs}$) as a function of incident light wavelength for $\alpha$-Fe$_2$O$_3$ spherical particles of different sizes. Normalized $\sigma_{acs} = \sigma_{acs}/G \times S/V$; where $\sigma_{acs}$, $G$, $S$, and $V$ are absorption cross section, geometric cross section, surface area, and volume of the particle.
Figure S4b. FDTD-simulated normalized absorption cross section (normalized \( \sigma_{\text{acs}} \)) as a function of incident light wavelength for CeO\(_2\) spherical particles of different sizes. Normalized \( \sigma_{\text{acs}} = \frac{\sigma_{\text{acs}}}{G \times S/V} \); where \( \sigma_{\text{acs}} \), \( G \), \( S \), and \( V \) are absorption cross section, geometric cross section, surface area, and volume of the particle.
**Figure S4c.** FDTD-simulated normalized absorption cross section (normalized $\sigma_{acs}$) as a function of incident light wavelength for TiO$_2$ spherical particles of different sizes. Normalized $\sigma_{acs} = \sigma_{acs}/G \times S/V$; where $\sigma_{acs}$, $G$, $S$, and $V$ are absorption cross section, geometric cross section, surface area, and volume of the particle.
Table S1. The real (n) and imaginary (k) parts of refractive index values of Cu$_2$O used in the simulations.\textsuperscript{3}

| $\lambda$ (nm) | n  | k   |
|----------------|----|-----|
| 300            | 2  | 1.85|
| 350            | 2.4| 1.44|
| 400            | 2.8| 0.99|
| 450            | 3.06| 0.6 |
| 500            | 3.12| 0.35|
| 550            | 3.1 | 0.19|
| 600            | 3.02| 0.13|
| 650            | 2.9 | 0.1 |
| 700            | 2.83| 0.083|
| 750            | 2.77| 0.07|
| 800            | 2.7 | 0.06|
| 850            | 2.66| 0.053|
| 900            | 2.63| 0.048|
| 950            | 2.61| 0.043|
| 1000           | 2.6 | 0.04|
| 1100           | 2.59| 0.033|
| 1200           | 2.58| 0.027|
| 1300           | 2.57| 0.021|
| 1400           | 2.57| 0.017|
| 1500           | 2.57| 0.013|
| 2000           | 2.56| 0.002|
Table S2. The real (n) and imaginary (k) parts of refractive index values of CeO$_2$ used in the simulations.$^4$

| $\lambda$ (nm) | n  | k  | $\lambda$ (nm) | n  | k  | $\lambda$ (nm) | n  | k  |
|----------------|----|----|----------------|----|----|----------------|----|----|
| 401            | 2.47| 0.11| 624           | 2.16| 0.00| 854           | 2.13| 0.00|
| 410            | 2.41| 0.08| 635           | 2.15| 0.00| 864           | 2.13| 0.00|
| 421            | 2.38| 0.03| 646           | 2.15| 0.00| 876           | 2.13| 0.00|
| 429            | 2.36| 0.02| 657           | 2.15| 0.00| 886           | 2.13| 0.00|
| 439            | 2.31| 0.01| 668           | 2.15| 0.00| 897           | 2.12| 0.00|
| 450            | 2.29| 0.01| 679           | 2.15| 0.00| 908           | 2.12| 0.00|
| 461            | 2.28| 0.00| 690           | 2.15| 0.00| 919           | 2.12| 0.00|
| 471            | 2.25| 0.00| 701           | 2.15| 0.00| 929           | 2.12| 0.00|
| 483            | 2.24| 0.00| 712           | 2.14| 0.00| 940           | 2.12| 0.00|
| 494            | 2.22| 0.00| 722           | 2.15| 0.00| 951           | 2.12| 0.00|
| 504            | 2.21| 0.00| 733           | 2.15| 0.00| 962           | 2.11| 0.00|
| 516            | 2.20| 0.00| 744           | 2.14| 0.00| 973           | 2.11| 0.00|
| 526            | 2.19| 0.00| 755           | 2.14| 0.00| 984           | 2.11| 0.00|
| 537            | 2.18| 0.00| 766           | 2.14| 0.00| 996           | 2.11| 0.00|
| 548            | 2.18| 0.00| 777           | 2.14| 0.00| 854           | 2.13| 0.00|
| 559            | 2.18| 0.00| 788           | 2.14| 0.00| 864           | 2.13| 0.00|
| 570            | 2.18| 0.00| 799           | 2.13| 0.00| 876           | 2.13| 0.00|
| 581            | 2.17| 0.00| 810           | 2.14| 0.00| 886           | 2.13| 0.00|
| 592            | 2.16| 0.00| 821           | 2.13| 0.00| 897           | 2.12| 0.00|
| 602            | 2.16| 0.00| 831           | 2.13| 0.00| 908           | 2.12| 0.00|
| 613            | 2.16| 0.00| 842           | 2.13| 0.00| 919           | 2.12| 0.00|
Table S3. The real (n) and imaginary (k) parts of refractive index values of $\alpha$-Fe$_2$O$_3$ used in the simulations.\textsuperscript{5}

| $\lambda$ (nm) | n   | k   |
|----------------|-----|-----|
| 400            | 2.756 | 1.294 |
| 450            | 3.181 | 1.02  |
| 500            | 3.282 | 0.675 |
| 550            | 3.318 | 0.498 |
| 600            | 3.265 | 0.149 |
| 650            | 3.074 | 0.057 |
| 700            | 2.972 | 0.031 |
| 750            | 2.903 | 0.021 |
| 800            | 2.853 | 0.02  |
| 850            | 2.824 | 0.027 |
| 900            | 2.805 | 0.024 |
| 950            | 2.789 | 0.022 |
| 1000           | 2.775 | 0.015 |
| 1050           | 2.759 | 0.011 |
| 1100           | 2.745 | 0.011 |
| 1150           | 2.734 | 0.01  |
| 1200           | 2.723 | 0.011 |
Table S4. The real (n) and imaginary (k) parts of refractive index values of TiO$_2$ used in the simulations.$^{6,7}$

| $\lambda$ (nm) | n    | k    | $\lambda$ (nm) | n    | k    | $\lambda$ (nm) | n    | k    |
|---------------|------|------|---------------|------|------|---------------|------|------|
| 180           | 1.37 | 1.998| 330           | 5.291| 1.5698| 480           | 3.08 | 0.0001 |
| 190           | 1.535| 1.831| 340           | 4.969| 1.0926| 490           | 3.054| 0.0001 |
| 200           | 1.536| 1.696| 350           | 4.477| 0.6508| 500           | 3.03 | 0.0001 |
| 210           | 1.46 | 1.65 | 360           | 3.87 | 0.251 | 510           | 3.014| 0.0001 |
| 220           | 1.433| 1.806| 370           | 3.661| 0.033 | 520           | 3    | 0.0001 |
| 230           | 1.443| 2.084| 380           | 3.498| 0.0001| 530           | 2.985| 0.0001 |
| 240           | 1.363| 2.454| 390           | 3.375| 0.0001| 540           | 2.97 | 0.0001 |
| 250           | 1.365| 2.847| 400           | 3.286| 0.0001| 550           | 2.954| 0.0001 |
| 260           | 1.627| 3.197| 410           | 3.225| 0.0001| 560           | 2.94 | 0.0001 |
| 270           | 1.952| 3.432| 420           | 3.186| 0.0001| 570           | 2.929| 0.0001 |
| 280           | 3.355| 3.561| 430           | 3.162| 0.0001| 580           | 2.92 | 0.0001 |
| 290           | 3.835| 3.535| 440           | 3.149| 0.0001| 590           | 2.91 | 0.0001 |
| 300           | 4.732| 3.28 | 450           | 3.141| 0.0001| 600           | 2.9  | 0.0001 |
| 310           | 5.235| 2.734| 460           | 3.13 | 0.0001| 610           | 2.889| 0.0001 |
| 320           | 5.391| 2.076| 470           | 3.104| 0.0001| 620           | 2.88 | 0.0001 |
| $\lambda$ (nm) | n   | k         | $\lambda$ (nm) | n   | k         | $\lambda$ (nm) | n   | k         |
|---------------|-----|-----------|---------------|-----|-----------|---------------|-----|-----------|
| 630           | 2.875 | 0.0001   | 780           | 2.8 | 0.0001   | 930           | 2.759 | 0.0001   |
| 640           | 2.87 | 0.0001   | 790           | 2.794 | 0.0001 | 940           | 2.76 | 0.0001   |
| 650           | 2.86 | 0.0001   | 800           | 2.79 | 0.0001   | 950           | 2.761 | 0.0001   |
| 660           | 2.85 | 0.0001   | 810           | 2.79 | 0.0001   | 960           | 2.76 | 0.0001   |
| 670           | 2.844 | 0.0001 | 820           | 2.79 | 0.0001   | 970           | 2.755 | 0.0001   |
| 680           | 2.84 | 0.0001   | 830           | 2.785 | 0.0001 | 980           | 2.75 | 0.0001   |
| 690           | 2.835 | 0.0001 | 840           | 2.78 | 0.0001   | 990           | 2.749 | 0.0001   |
| 700           | 2.83 | 0.0001   | 850           | 2.78 | 0.0001   | 1000          | 2.75 | 0.0001   |
| 710           | 2.825 | 0.0001 | 860           | 2.78 | 0.0001   | 1010          | 2.75 | 0.0001   |
| 720           | 2.82 | 0.0001   | 870           | 2.775 | 0.0001 | 1020          | 2.749 | 0.0001   |
| 730           | 2.814 | 0.0001 | 880           | 2.77 | 0.0001   | 1030          | 2.749 | 0.0001   |
| 740           | 2.81 | 0.0001   | 890           | 2.77 | 0.0001   | 1040          | 2.748 | 0.0001   |
| 750           | 2.81 | 0.0001   | 900           | 2.77 | 0.0001   | 1050          | 2.747 | 0.0001   |
| 760           | 2.81 | 0.0001   | 910           | 2.765 | 0.0001 | 1060          | 2.747 | 0.0001   |
| 770           | 2.806 | 0.0001 | 920           | 2.76 | 0.0001   | 1070          | 2.746 | 0.0001   |
| $\lambda$ (nm) | n   | k   | $\lambda$ (nm) | n   | k   | $\lambda$ (nm) | n   | k   |
|---------------|-----|-----|---------------|-----|-----|---------------|-----|-----|
| 1080          | 2.745 | 0.0001 | 1230          | 2.729 | 0.0001 | 1380          | 2.721 | 0.0001 |
| 1090          | 2.744 | 0.0001 | 1240          | 2.729 | 0.0001 | 1390          | 2.721 | 0.0001 |
| 1100          | 2.742 | 0.0001 | 1250          | 2.728 | 0.0001 | 1400          | 2.72  | 0.0001 |
| 1110          | 2.741 | 0.0001 | 1260          | 2.728 | 0.0001 | 1410          | 2.719 | 0.0001 |
| 1120          | 2.74  | 0.0001 | 1270          | 2.727 | 0.0001 | 1420          | 2.719 | 0.0001 |
| 1130          | 2.739 | 0.0001 | 1280          | 2.727 | 0.0001 | 1430          | 2.718 | 0.0001 |
| 1140          | 2.738 | 0.0001 | 1290          | 2.726 | 0.0001 | 1440          | 2.717 | 0.0001 |
| 1150          | 2.737 | 0.0001 | 1300          | 2.726 | 0.0001 | 1450          | 2.716 | 0.0001 |
| 1160          | 2.736 | 0.0001 | 1310          | 2.725 | 0.0001 | 1460          | 2.715 | 0.0001 |
| 1170          | 2.735 | 0.0001 | 1320          | 2.725 | 0.0001 | 1470          | 2.714 | 0.0001 |
| 1180          | 2.734 | 0.0001 | 1330          | 2.724 | 0.0001 | 1480          | 2.713 | 0.0001 |
| 1190          | 2.733 | 0.0001 | 1340          | 2.724 | 0.0001 | 1490          | 2.711 | 0.0001 |
| 1200          | 2.732 | 0.0001 | 1350          | 2.723 | 0.0001 | 1500          | 2.71  | 0     |
| 1210          | 2.731 | 0.0001 | 1360          | 2.723 | 0.0001 |               |      |      |
| 1220          | 2.73  | 0.0001 | 1370          | 2.722 | 0.0001 |               |      |      |
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