EXTRAGALACTIC BACKGROUND LIGHT FROM HIERARCHICAL GALAXY FORMATION: GAMMA-RAY ATTENUATION UP TO THE EPOCH OF COSMIC REIONIZATION AND THE FIRST STARS

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ABSTRACT

We present a new model of the extragalactic background light (EBL) and corresponding $\gamma\gamma$ opacity for intergalactic gamma-ray absorption from $z = 0$ up to $z = 10$, based on a semi-analytical model of hierarchical galaxy formation that reproduces key observed properties of galaxies at various redshifts. Including the potential contribution from Population III stars and following the cosmic reionization history in a simplified way, the model is also broadly consistent with available data concerning reionization, particularly the Thomson scattering optical depth constraints from Wilkinson Microwave Anisotropy Probe (WMAP). In comparison with previous EBL studies up to $z \sim 3-5$, our predicted $\gamma\gamma$ opacity is in general agreement for observed gamma-ray energy below 400/(1 + $z$) GeV, whereas it is a factor of $\sim 2$ lower above this energy because of a correspondingly lower cosmic star formation rate, even though the observed ultraviolet (UV) luminosity is well reproduced by virtue of our improved treatment of dust obscuration and direct estimation of star formation rate. The horizon energy at which the gamma-ray opacity is unity does not evolve strongly beyond $z \sim 4$ and approaches $\sim 20$ GeV. The contribution of Population III stars is a minor fraction of the EBL at $z = 0$, and is also difficult to distinguish through gamma-ray absorption in high-$z$ objects, even at the highest levels allowed by the WMAP constraints. Nevertheless, the attenuation due to Population II stars should be observable in high-$z$ gamma-ray sources by telescopes such as Fermi or the Cherenkov Telescope Array and provide a valuable probe of the evolving EBL in the rest-frame UV. The detailed results of our model are publicly available in numerical form at http://www.slac.stanford.edu/~yinoue/Download.html.

Key words: cosmic background radiation – dark ages, reionization, first stars – diffuse radiation – galaxies: evolution – gamma rays: general

Online-only material: color figures

1. INTRODUCTION

The extragalactic background light (EBL), the diffuse, isotropic background radiation from far-infrared (FIR) to ultraviolet (UV) wavelengths, is believed to be predominantly composed of the light from stars and dust integrated over the entire history of the universe (see Dwek & Krennrich 2013 for reviews). The observed spectrum of the local EBL at $z = 0$ has two peaks of comparable energy density. The first peak in the optical to the near-infrared (NIR) is attributed to direct starlight, while the second peak in the FIR is attributed to emission from dust that absorbs and reprocesses the starlight.

The precise determination of the EBL has been a difficult task. Direct measurements of the EBL in the optical and NIR bands have been hampered by bright foreground emission caused by interplanetary dust, the so-called zodiacal light (see Hauser & Dwek 2001 for reviews). Recently, Matsuoka et al. (2011) reported measurements of the EBL at 0.44 $\mu$m and 0.65 $\mu$m from outside the zodiacal region using observational data from Pioneer 10/11. On the other hand, integration over galaxy number counts provides a firm lower bound on the EBL, and the observed trend of the counts with magnitude indicates that the EBL at $z = 0$ has been largely resolved into discrete sources in the optical/NIR bands (e.g., Madau & Pozzetti 2000; Totani et al. 2001; Keenan et al. 2010), even when the effect of incomplete detection due to cosmological dimming of surface brightness is taken into account (Totani et al. 2001).

The EBL can also be probed indirectly through observations of high-energy gamma rays from extragalactic objects (e.g., Gould & Schréder 1966; Jelley 1966; Stecker et al. 1992; Mazin & Raue 2007). Gamma-rays propagating through intergalactic space can be attenuated by photon–photon pair production interactions ($\gamma\gamma \rightarrow e^+e^-$) with low-energy photons of the EBL. For gamma-rays of a given energy $E_\gamma$, the pair production cross section peaks for low-energy photons with energy $E_\gamma$:

$$\epsilon_{\text{peak}} \approx \frac{2m_ec^4}{E_\gamma} \approx 0.5 \left( \frac{1 \text{ TeV}}{E_\gamma} \right) \text{eV},$$

where $m_e$ is the electron mass and $c$ is the speed of light. In terms of wavelength, $\lambda_{\text{peak}} \approx 2.5 (E_\gamma [\text{TeV}]) \mu$m. Measuring the resultant attenuation features in the spectra of extragalactic GeV–TeV sources would offer a valuable probe of the EBL that is indirect, yet unique in being redshift-dependent. Although this method can be limited by incomplete knowledge of the intrinsic spectra of the source before attenuation, by assuming a plausible range for such spectra, observations of blazars by current ground-based telescopes have been able to place relatively robust upper limits to the EBL at $z = 0$ and up to $z \sim 5$ (e.g., Aharonian et al. 2006a; Albert et al. 2008). This has been complemented by Fermi observations of blazars and gamma-ray bursts (GRBs) that placed upper limits on the $\gamma\gamma$ opacity up to $z = 4.35$ (Abdo et al. 2009, 2010a). The energy density of the local EBL has been constrained to be $<24$ nW m$^{-2}$ sr$^{-1}$ at optical wavelengths, and
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in the range $52–99 \text{nW m}^{-2} \text{sr}^{-1}$ between $8 \mu\text{m}$ and $31 \mu\text{m}$ (Meyer et al. 2012). Combined with the lower limits from galaxy counts, the total EBL intensity at $z = 0$ from $0.1 \mu\text{m}$ to $1000 \mu\text{m}$ is inferred to lie in the range $52–99 \text{nW m}^{-2} \text{sr}^{-1}$ (Horiiuchi et al. 2009). Very recently, HESS has succeeded in positively measuring the imprint of the local EBL in the spectra of bright blazars, assuming only that their intrinsic spectra have smooth shapes (Abramowski et al. 2013). Fermi has also positively detected the redshift-dependent signature of EBL attenuation up to $z = 1.5$, utilizing the collective spectra of a large number of blazars (Ackermann et al. 2012). However, the EBL at higher redshifts is still highly uncertain.

Currently available theoretical models for the EBL can be broadly categorized into three types. First, in backward evolution models, one starts from the observed properties of galaxies in the local universe and describes their evolution by extrapolating backward in time in a parameterized fashion (e.g., Malkan & Stecker 1998; Totani & Takeuchi 2002; Stecker et al. 2006; Franceschini et al. 2008). This extrapolation entails uncertainties in the properties of the EBL that will certainly increase at high redshifts. Nevertheless, based on the observed rest-frame $K$-band luminosity function (LF) of galaxies from $z = 0$ up to $z = 4$, Domínguez et al. (2011) were able to model the EBL without any assumptions for the LF. Helgason & Kashlinsky (2012) and Stecker et al. (2012) constructed evolving EBL models in a relatively robust way by utilizing multiwavelength photometric survey data.

Second, in forward evolution models, the basis is a description for the cosmic star formation history (CSFH), over which models for the spectral energy distribution (SED) of the stellar population are convolved to obtain the evolving EBL (e.g., Kneiske et al. 2004; Finke et al. 2010). However, such models cannot follow the detailed evolution of physical quantities such as the metallicity and dust content, which can significantly affect the spectral shape of the EBL. Furthermore, although most forward evolution models employ the CSFH of Hopkins & Beacom (2006), it is known that this CSFH model overproduces the stellar mass density (Fardal et al. 2007; Choi & Nagamine 2012) and is also inconsistent with the observed rate of core-collapse supernovae (Horiiuchi et al. 2011). Recent studies by Kobayashi et al. (2013) show that Hopkins (2004) and Hopkins & Beacom (2006) may have overestimated the CSFH at $z > 1$, arising from overcorrection for dust obscuration effects and in conversion from luminosity to star formation rate.

Finally, rooted in the modern cosmological framework of large-scale structure formation driven by cold dark matter, semi-analytical models of hierarchical galaxy formation account for the merging history of dark matter halos as well as the physical evolution of the baryonic component, including the effects of gas cooling, star formation, metal enrichment, feedback heating, etc. (Primack et al. 2005; Gilmore et al. 2009, 2012b; Younger & Hopkins 2011). Such models successfully reproduce various observed properties of galaxies from the local universe up to $z \sim 6$ (see, e.g., Kauffmann et al. 1993; Cole et al. 1994; Nagashima et al. 1999, 2005; Somerville & Primack 1999; Nagashima & Yoshii 2004; Baugh et al. 2005; Kobayashi et al. 2007, 2010; Somerville et al. 2012). At present, semi-analytical models can be considered the most detailed and well-developed models for the EBL over a wide range of redshifts.

A subject that has yet to be fully explored in the context of the EBL and gamma-ray absorption is the epoch of cosmic reionization above $z \sim 6$. Measurements of NIR absorption troughs in the spectra of high-$z$ quasars, together with those of anisotropies in the polarization of the cosmic microwave background (CMB), prove that the majority of intergalactic hydrogen in the universe has been reionized somewhere between $z \sim 30$ and $z \sim 6$ (see, e.g., Robertson et al. 2010). Although the most widely suspected source of reionization is UV photons emitted by early generations of massive stars, the observational constraints are still very limited, so that the actual sources, history, and topology of cosmic reionization remain largely unknown. A closely related topic is the possible existence and formation history of Population III (Pop-III) stars, very massive stars that are expected to originate in nearly metal-free conditions, particularly for the very first generation of stars appearing in the universe, and their potential role in cosmic reionization (see, e.g., Bromm & Yoshida 2011; Glover 2012 and references therein).

Since the current observational constraints on reionization mostly concern the neutral or ionized intergalactic gas, it would be very valuable and complementary to obtain independent information on the evolving, UV intergalactic radiation field itself. A unique and promising approach may be offered by the effects of gamma-ray absorption in situ in high-energy sources at $z > 6$. UV radiation fields with sufficient intensities to cause cosmic reionization may induce significant gamma-ray absorption at observer energies above a few tens of GeV (Oh 2001; Inoue et al. 2010a). Based on a semi-analytical model of galaxy formation that includes Pop-III stars and reproduces a variety of reionization-related observations (Choudhury & Ferrara 2006; Choudhury 2009), the recent study by Inoue et al. (2010a) suggested that appreciable attenuation may be expected above $\sim 12 \text{ GeV}$ at $z \sim 5$ and down to $\sim 6–8 \text{ GeV}$ at $z \gtrsim 8–10$, mainly caused by Population II (Pop-II) stars at these epochs. However, the relative contribution of Pop-III stars was found to be difficult to discern observationally. On the other hand, without addressing the implications for reionization, some studies have concentrated on the prospects for constraining Pop-III star formation through gamma-ray absorption in objects at lower redshifts (e.g., Gilmore 2012).

The Fermi Gamma-ray Space Telescope (Fermi; Atwood et al. 2009) may eventually detect blazars at $z > 6$ (Inoue et al. 2011), and the Cherenkov Telescope Array (CTA; Actis et al. 2011) may possibly do the same for GRBs (Inoue et al. 2013). Therefore a deeper investigation into the above issues is worthwhile and timely. The above studies (Oh 2001; Inoue et al. 2010a; Gilmore 2012) have not accounted consisently for the EBL resulting from galaxy formation at lower redshifts. For example, the model of Inoue et al. (2010a) was optimized to describe the reionization epoch and did not include the contribution from Population I (Pop-I) stars or dust, and thus could only evaluate the gamma-ray opacity above $z = 4$.

In this paper, we present a new study of the EBL and consequent gamma-ray opacity, covering the entire redshift range from $z = 0$ up to $z = 10$ within a consistent framework, accounting for the process of cosmic reionization, and including Pop-III stars in a simplified way. As a baseline model, we adopt the Mitaka model $^7$ of semi-analytical galaxy formation (Nagashima & Yoshii 2004). The model can reproduce various observed properties of galaxies such as their LF, luminosity density (LD), and stellar mass density (Nagashima & Yoshii 2004), as well as the LFs of high-redshift Lyman-break galaxies (LBGs) and Ly$\alpha$ emitters (LAEs) up to $z \sim 6$ (Kobayashi...

$^7$ Named after the city of Mitaka where the model was mainly developed at the National Astronomical Observatory of Japan.
et al. 2007, 2010). As regards Pop-III stars, in view of the presently large theoretical uncertainties on their formation efficiency, metal production, conditions for transition to Pop-II star formation, etc., we choose not to fully incorporate them into our semi-analytical scheme. Instead, their formation history is characterized in a simple, parameterized way, which we constrain by modeling the cosmic reionization process and comparing with available observations, particularly the Thomson scattering optical depth measured by the Wilkinson Microwave Anisotropy Probe (WMAP).

We introduce our semi-analytical model in Section 2. Cosmic reionization is modeled and compared with observations in Section 3. Section 4 presents the results of our EBL models. The consequent gamma-ray opacity and comparison with current gamma-ray observations are described in Section 5. We conclude in Section 6. Throughout this paper, we adopt the standard cosmological parameters of \((h, \Omega_M, \Omega_{\Lambda}) = (0.7, 0.3, 0.7)\), and a Salpeter initial mass function (IMF; Salpeter 1955) within a mass range of 0.1–60 \(M_\odot\).

\section{Semi-Analytical Galaxy Formation Model}

In the framework of the Mitaka semi-analytical model of galaxy formation, we follow the merger history of dark matter halos and the evolution of baryonic components. The evolution of the baryons within halos is modeled with physically motivated, phenomenological prescriptions for radiative cooling, star formation, supernova feedback, chemical enrichment, and galaxy merging. We can compute a variety of physical and observational quantities for individual galaxies as well as the global average over the universe at any redshift, such as the CSFH, and LFs and dust content of galaxies. A mock catalog of galaxies can be generated that can be compared with different observations. More details of the Mitaka model are described in Nagashima & Yoshii (2004), Kobayashi et al. (2007), and Kobayashi et al. (2010). Several free parameters in the prescriptions for baryons are fixed so that they fit a number of observed properties of local galaxies, such as their \(B\)-band and \(K\)-band LFs, neutral gas fraction, and gas mass-to-luminosity ratio as a function of \(B\)-band luminosity (Nagashima & Yoshii 2004). For simplicity and consistency, we keep these parameters unchanged throughout this paper.

\subsection{Cosmic Star Formation History}

Figure 1 shows the CSFH expected in the Mitaka model over \(z = 0–18\) in different ranges of metallicity. Pop-III stars are expected to form from gas with metallicity below a critical value, such that the gas can only cool rather inefficiently through rotational transitions of molecular hydrogen, which leads to fragmentation into relatively massive protostellar clouds, and ultimately the formation of very massive stars. Once the metallicity exceeds this value, the gas can cool more efficiently via metal emission lines, and a transition to the formation of less massive, Pop-II stars is thought to take place (e.g., Mackey et al. 2003; Bromm & Loeb 2003; Yoshida et al. 2004). However, the exact value of this critical metallicity has been debated, ranging from \(Z = 10^{-6} Z_\odot = 10^{-7.7}\) (Schneider et al. 2006) to \(Z = 10^{-2} Z_\odot = 10^{-3.7}\) (Aykutalp & Spaans 2011). In this paper, we consider stars with metallicity \(Z < 10^{-4} = 5 \times 10^{-3} Z_\odot\) to correspond to Pop-III stars. We adopt a Salpeter IMF in the mass range of 0.1–60 \(M_\odot\) for all types of stars. Recent radiation-hydrodynamics simulations of Pop-III star formation suggest that their typical masses may be limited to \(\leq 40 M_\odot\) due to radiative feedback effects (Hosokawa et al. 2011), which would be in accord with our choice of the maximum mass for Pop-III stars.

We also plot the data compiled by Hopkins (2004), Pascale et al. (2009), Rodighiero et al. (2010), Karim et al. (2011),

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure1}
\caption{Cosmic star formation history. The solid curve shows the total in the baseline Mitaka model, while the dashed, dotted, dot-dashed, and double-dot-dashed curves show the fractional contributions from stars with metallicity \(Z/Z_\odot < 5 \times 10^{-3}\), \(5 \times 10^{-3} \leq Z/Z_\odot < 2 \times 10^{-2}\), \(2 \times 10^{-2} \leq Z/Z_\odot < 1\), and \(Z/Z_\odot \geq 1\), respectively. We also plot the observational data compiled by Hopkins (2004), that deduced from LBGs (Ouchi et al. 2004; Bouwens et al. 2007, 2008; Mannucci et al. 2009), and that inferred from GRBs (Yüksel et al. 2008; Kistler et al. 2009). For the LBG sample, limiting luminosities adopted by each author are indicated in the corresponding legend in terms of the characteristic luminosity \(L^*_\odot\) of the LF.}
\end{figure}

\footnote{We adopt \(Z_\odot \simeq 0.02\) (Anders & Grevesse 1989; Grevesse & Sauval 1998), although an updated value of \(Z_\odot \simeq 0.0134\) has been given by Asplund et al. (2009).}
and Cucciati et al. (2012), that deduced from LBGs (Ouchi et al. 2004; Bouwens et al. 2007, 2008, 2011b; Mannucci et al. 2007; Verma et al. 2007), and that inferred from GRBs (Yüksek et al. 2008; Kistler et al. 2009). Above \( z > 4 \), each LBG data point is obtained by integrating its LF down to a certain limiting luminosity which is parameterized by the characteristic luminosity \( L_* \), of the LF, a choice which often differs among authors. Our model shows the star formation in all galaxies, down to the faintest luminosities.

There is an apparent discrepancy between our model and the observed CSFH data at \( 1 < z < 5 \). In our semi-analytical model, we directly estimate the star formation rate for each galaxy and evaluate the CSFH by integrating over all galaxies. The CSFH data points are converted from the observed galaxy LFs and involve uncertainties in the faint-end slope of the LF, dust obscuration correction from UV data, contamination LFs and involve uncertainties in the faint-end slope of the LF, a choice which often differs among authors. Our model shows the star formation in all galaxies, down to the faintest luminosities.

We calculate \( j_{\text{star}}(v, z) \) from the CSFH using stellar population synthesis models that provide the SEDs as a function of metallicity and dust attenuation, namely the models of Bruzual & Charlot (2003) for \( Z \gg 10^{-4} \) and Schaerer (2003) for \( Z < 10^{-4} \) (Pop-III); note that the latter metallicity range is not covered by Bruzual & Charlot (2003). We adopt the Salpeter IMF for the models with a correction for the IMF mass range used in our model. Thus,

\[
j_{\text{star}}(v, z) = \int_0^\infty \frac{dt}{dz'} \left| \frac{dz}{d\nu} \right| \int_0^{\infty} d\nu' \int_0^{\infty} dA V f_{\text{esc}}(\nu', z, A_V) \times \varepsilon(\nu', z', z, Z) \exp[-\tau_{\text{ISM}}(\nu', A_V) \times \tau_{\text{IGM}}(\nu', z', z)],
\]

(3)

where \( A_V \) is the interstellar dust attenuation strength in the \( V \) band, \( \rho_{\text{star}}(z, Z, A_V) \) is the CSFH for stars with metallicity \( Z \) and dust attenuation \( A_V \) at redshift \( z \) in units of \( M_\odot \) yr\(^{-1}\) Mpc\(^{-3}\), \( \varepsilon(\nu, z', z, Z) \) is the intrinsic emissivity at frequency \( \nu \) at \( z \) from stars with metallicity \( Z \) born at \( z' \) in units of erg s\(^{-1}\) Hz\(^{-1}\) M\(_\odot\)^{-1} given by stellar population synthesis models, and \( \nu' = (1 + z')\nu/(1 + z) \). \( \tau_{\text{ISM}} \) and \( \tau_{\text{IGM}} \) are the attenuation opacities in the interstellar medium (ISM) and the intergalactic medium (IGM), respectively. We adopt the ISM dust attenuation law of Calzetti et al. (2000) and the IGM opacity of Yoshii & Peterson (1994). \( f_{\text{esc}} \) is the escape fraction of photons from galaxies with energy above the threshold for ionization of hydrogen, \( E = 13.6 \) eV; non-ionizing photons with lower energies are assumed to escape freely.

Various observations have constrained the UV LD up to \( z \sim 6 \) (Wyder et al. 2005; Schiminovich et al. 2005; Dahlen et al. 2007; Bouwens et al. 2007; Reddy et al. 2008). Figure 2 compares the UV LD from our model with the observed LD data at a rest-frame wavelength of 1500 Å. All the data agree well with our semi-analytical model. Comparisons with other kinds of data are shown in Nagashima & Yoshii (2004), Nagashima et al. (2005), Kobayashi et al. (2007), and Kobayashi et al. (2010).

Dust emits mid-IR (MIR; \( 5 \sim 30 \) \( \mu \)m) and FIR (\( \sim 30 \sim 1000 \) \( \mu \)m) photons by reemitting the absorbed starlight. For dust

![Figure 2](image-url)

**Figure 2.** Luminosity density at rest-frame wavelength 1500 Å. The solid curve is the result from the baseline Mitaka model. The observed data at various redshifts are also shown as indicated in the figure (Wyder et al. 2005; Schiminovich et al. 2005; Dahlen et al. 2007; Bouwens et al. 2007; Reddy et al. 2008).

(A color version of this figure is available in the online journal.)
emission, we also utilize a new implementation in the Mitaka model (see R. Makiya et al., in preparation, for details). We set the total dust emissivity $J_{dust}(z) = \int_{0}^{\infty} d\nu J_{dust}(\nu, z)$ to be equivalent to the total starlight energy absorbed by dust in the ISM.

$$J_{dust}(z) = \int d\nu \int_{z}^{\infty} \left| \frac{d\nu}{d\nu'} \right| dz' \int_{0}^{\infty} d\nu' \int_{0}^{\infty} dA_{V} \rho_{dust}(z', Z, A_{V}) \times \mathcal{E}(\nu', z', Z) \left[ 1 - \exp[-\tau_{ISM}(\nu', A_{V})] \right].$$

(4)

To determine $J_{dust}(\nu, z)$, we utilize the model of dust emission SED by Dale & Helou (2002), where the IR SED shape is defined by the exponent $\alpha$ of their Equation (1). We adopt $\alpha = 1.2$ for all galaxies in our model in order to reproduce the peak wavelength of the FIR EBL. Different $\alpha$ parameters result in different positions of the FIR peak wavelength.

Although our dust emissivity model can reproduce the local Herschel galaxy LF (Vaccari et al. 2010), the redshift evolution of the IR LF (e.g., Rodighiero et al. 2010) has yet to be reproduced (R. Makiya et al., in preparation). Thus, we predict an IR EBL at $z = 0$ that is lower than the current lower limits to the EBL by a factor of two. To remedy this, here we set the dust emissivity in our model to be three times more luminous than in the version of the Mitaka model by R. Makiya et al. (in preparation). Our model predictions in the MIR–FIR are therefore uncertain, while they should be more reliable in the UV–NIR band. We also note that the gamma-ray opacity due to the dust emission should be important only above several TeV in the local universe (see Equation (1)).

3. COSMIC REIONIZATION HISTORY

After the epoch of cosmic recombination, the universe entered the so-called dark ages, a period with no significant sources of radiation. As the initially small fluctuations in the matter density field grew by gravitational instability and collapsed to form dark matter halos, the baryons that fell into sufficiently massive halos are expected to have cooled efficiently to form the first stars and galaxies (Bromm & Yoshida 2011; Glover 2012). Such stars and galaxies should generate UV radiation that ionize their environments to create the first H II regions, which eventually grow and overlap to reionize the entire IGM. Observationally, cosmic reionization is known to have proceeded at least partially by $z \sim 10$ and been essentially completed by $z \sim 6$. However, the actual history, nature, and sources of reionization are still largely unconstrained (see Barkana & Loeb 2001; Fan et al. 2006, for reviews). In this section, we discuss how we model the reionization history of the universe with our Mitaka model.

3.1. Ionizing Photon Emission Rate

First, we evaluate the emissivity of photons with energies greater than 13.6 eV that can ionize hydrogen atoms. A key uncertainty is the escape fraction $f_{esc}$ of ionizing photons from galaxies, which we assume here to be a constant value of 0.2 at all redshifts. This is motivated by the numerical simulations of Yajima et al. (2009, 2011), although they also showed that $f_{esc}$ can depend on halo mass. Observationally, $f_{esc} \approx 0.05$ is found in LBGs at $z \sim 3$ (Shapley et al. 2006; Iwata et al. 2009), but values at $z \geq 4$ have not been determined yet. Ono et al. (2010) have set upper limits of $f_{esc} \lesssim 0.6$ at $z = 5.7$ and $f_{esc} \lesssim 0.9$ at $z = 6.6$ for LAEs.

Figure 3 shows the ionizing photon emissivity $dn_{ion}/dt$ in units of $s^{-1} Mpc^{-3}$, compared with various observations. We set $f_{esc} = 0.2$ for the interpretation of all the observed data as well. The observed ionizing emissivities were derived by Ouchi et al. (2009) from galaxy UV LFs at $z = 4-7$ (Yoshida et al. 2006; Bouwens et al. 2008; Ouchi et al. 2009, filled symbols in Figure 3). The conversion from LF to ionizing photon emissivity is based on Equation (5) in Ouchi et al. (2009), where continuous...
star formation history is assumed for all galaxies. The data are integrated down to $L = 0$. We also show the ionizing photon rate inferred from the Lyα forest by combining hydrodynamical simulations with measurements of the Lyα opacity of the IGM (Bolton & Haehnelt 2007, open symbols in Figure 3).

As shown later, the baseline Mitaka model does not produce enough ionizing photons to account for the Thomson scattering optical depth measured by WMAP, although it can reionize the universe sufficiently at $z \lesssim 8$. In order to achieve consistency with observations, we extend the baseline model by considering an additional potential contribution of ionizing photons from Pop-III stars in a simplified way. Although ideally one would like to incorporate Pop-III stars self-consistently into our semianalytic scheme, this is currently precluded by very large uncertainties in their formation efficiency, metal yield, etc. Instead, we introduce two new parameters and simply enhance uncertainties in their formation efficiency, metal yield, etc. like to incorporate Pop-III stars self-consistently into our semi-analytic approach. Above a critical redshift $z_c$, and attribute such an additional component to Pop-III stars. An alternative procedure might be to enhance the emissivity of only the stellar population with $Z < 10^{-4}$ in the baseline model (Figures 1 and 3), but this will not be more satisfactory in any way as the actual evolution of the metallicity would be altered. Thus we choose to simply enhance the total ionizing emissivity. In Figure 3, we show the cases with $(\xi, z_c) = (50, 0.1, 10)$ and $(50, 10, 0.1)$, referred to as the lower-Pop-III model and the upper-Pop-III model, respectively. Also shown is the contribution of stars with $Z < 10^{-4}$ in the baseline model with $(\xi, z_c) = (1, 0.0)$. The corresponding star formation rates of Pop-III stars at $z = 10$ will be $4.5 \times 10^{-4}, 4.4 \times 10^{-2}$, and $8.8 \times 10^{-2}$ M$_\odot$ Mpc$^{-3}$ yr$^{-1}$ for the baseline, the lower-Pop-III, and the upper-Pop-III model, respectively.

Although the overall behavior of our ionizing photon emissivity at $2 < z < 7$ is similar to that derived from the observed data, we overpredict the ionizing photon emissivity by a factor of two. We note that the data points are very sensitive to the assumed spectral index of the ionizing emission $\alpha_{\text{ion}}$ (see Equation (5) in Ouchi et al. 2009), which is set to be 3.0 for the data in Figure 3 but is actually not well determined. If $\alpha_{\text{ion}} = 1.5$, then it will double the data derived from the galaxy UV LF and the Lyα forest opacity, bringing it into closer agreement with the model.

Figure 3 also shows $dn_{\text{ion}}/dt$ that is required to balance the recombination of intergalactic hydrogen based on the formulation of Madau et al. (1999),

$$
\frac{dn_{\text{ion}}}{dt} = \frac{n_H^0}{t_{\text{rec}}(z)} \simeq 10^{47.4} C (1 + z)^3 \text{[s}^{-1}\text{Mpc}^{-3}] \tag{5}
$$

where $n_H^0$ is the total number density of intergalactic hydrogen atoms (in both H I and H II phases), $t_{\text{rec}}(z)$ is the recombination time scale at $z$, and $C = \langle n_H^0/n_H^2 \rangle$ is a time-dependent, volume-averaged clumping factor, for which the cases of $C = 1$, 3, and 10 are shown. Note that $C = 1$ corresponds to a uniform IGM. All our models have a sufficient budget of photons to ionize the universe at $z \lesssim 7$–8. However, the baseline model cannot do so above $z = 8$, in contradiction with WMAP observations that constrain the reionization redshift to be $z = 10.6 \pm 1.2$ if it was instantaneous (Komatsu et al. 2011). Even if reionization occurred gradually, more ionizing photons may actually be necessary above $z \sim 8$ than is implied by the estimates of Madau et al. (1999).

3.2. Probing the Cosmic Reionization History

Important observational indicators of the reionization history are the optical depth to electron scattering and the neutral fraction of intergalactic hydrogen. Following Barkana & Loeb (2001), we compute the reionization history of the universe. The equation of ionization equilibrium in terms of the volume filling factor $Q_{\text{HI}}$ of H II regions is given by

$$
\frac{dQ_{\text{HI}}}{dt} = \frac{1}{n_H^0} \frac{dn_{\text{ion}}}{dt} - \frac{C}{a(t)} n_H^0 Q_{\text{HI}}, \tag{6}
$$

where $t$ is the cosmic time, $n_H^0 = X_H n_B^0$ is the present-day number density of hydrogen with $n_B^0$ as the present-day baryon number density and $X_H = 0.76$ as the mass fraction of hydrogen, $dn_{\text{ion}}/dt$ is the production rate of ionizing photons (see Figure 3), and $\alpha_B = 2.6 \times 10^{-13}$ cm$^3$ s$^{-1}$ is the recombination rate of hydrogen at temperature $T = 10^4$ K. The recombination time scale $t_{\text{rec}}(z)$ in Equation (5) is given by $a(t)^3/\alpha_B C n_H^0$, where $a(t)$ is the cosmic scale factor.

Assuming a constant clumping factor $C$, Equation (6) can be solved to give (see Barkana & Loeb 2001, for details)

$$
Q_{\text{HI}}(z_0) = \int_{z}^{\infty} dz \left[ \frac{dt}{dz} \right] \frac{1}{n_H^0} \frac{dn_{\text{ion}}}{dt} e^{F(z, z_0)}, \tag{7}
$$

where $dt/dz$ is calculated from the Friedmann equation in the standard, flat universe cosmology as

$$
\frac{dt}{dz} = \frac{1}{(1 + z)H_0 \sqrt{\Omega_M (1 + z)^3 + \Omega_\Lambda}}. \tag{8}
$$

Once $Q_{\text{HI}}$ reaches 1, the IGM is fully ionized, and ionizing photons propagate freely in intergalactic space. The function $F(z, z_0)$ accounts for recombination and is given by

$$
F(z, z_0) = \frac{2}{3} \frac{\alpha_B n_H^0}{\sqrt{\Omega_M} H_0} C[f(z) - f(z_0)], \tag{9}
$$

where $f(z)$ is defined as

$$
f(z) = \sqrt{(1 + z)^3 + \frac{1 - \Omega_M}{\Omega_\Lambda}}. \tag{10}
$$

For the purpose of calculating $Q_{\text{HI}}$, we set $C = 3.0$, motivated by the numerical simulations of Pawlik et al. (2009). We do not change $C$ as a function of redshift. We also assume $Q_{\text{He}} = Q_{\text{HI}}$ for the volume filling factor of He II regions and neglect the free electrons in He III regions for computing the optical depth to electron scattering. The number density of free electrons at $z$ is then

$$
n_e(z) = \left( Q_{\text{HI}}(z) X_H + \frac{Q_{\text{He}}(1 - X_H)}{4} \right) n_B^0 (1 + z)^3
\begin{align*}
&= \frac{1 + 3X_H}{4} Q_{\text{He}}(z) n_B^0 (1 + z)^3. \tag{11}
\end{align*}
$$

The optical depth to electron scattering is

$$
\tau_e(z_0) = \int_{0}^{z_0} dz \frac{dt}{dz} \sigma_T n_e(z), \tag{12}
$$
where $\sigma_T$ is the Thomson cross section and $dl/dz$ is the cosmological line element for a standard, flat universe cosmology given by

$$\frac{dl}{dz} = c \frac{dt}{dz} = c \frac{(1+z)H_0}{\sqrt{\Omega_m (1+z)^3 + \Omega_\Lambda}}. \quad (13)$$

Figure 4 shows the Thomson scattering optical depth of the universe, together with the range of $\tau_e = 0.088 \pm 0.015$ derived from the 7-year WMAP data (Komatsu et al. 2011). As mentioned above, the baseline model cannot reproduce the WMAP data, despite managing to reionize the universe at $z \lesssim 8$. The results of the lower-Pop-III and upper-Pop-III models are close to the lower and upper limits from WMAP, respectively, implying that 50–100 times more ionizing photons are necessary at $z \gtrsim 10$ than is conservatively expected from our semi-analytical galaxy formation model that successfully accounts for various observations at $z \lesssim 8$. The fact that the ionizing photon budget estimated from galaxy populations directly observed so far are insufficient to account for the WMAP $\tau_e$ is well documented (e.g., Stark et al. 2007; Chary 2008; Oesch et al. 2009; Ouchi et al. 2009; Pawlik et al. 2009; Bunker et al. 2010; Labbé et al. 2010; Robertson 2010; Bouwens et al. 2011a, 2012).

Figure 5 shows $x_{H\alpha} = 1 - Q_{H\alpha}$, the neutral fraction of intergalactic hydrogen, compared with constraints from analysis of Gunn–Peterson (GP) troughs (Gunn & Peterson 1965) in the spectra of quasars (Mesinger & Haiman 2007; Mortlock et al. 2011) and a GRB (Totani et al. 2006). Also shown are constraints from LFs and clustering amplitudes of LAEs by Ouchi et al. (2010). They derived $x_H < 0.40$ at 1σ confidence level by comparing the observed LAE LFs at $z = 6.6$ with a theoretical model including Ly$\alpha$ transmission through the IGM, but the limit varies from 0.1 to 0.53 depending on the model (see Section 6.1.1 in Ouchi et al. 2010, for details). They also derived $x_H \lesssim 0.50$ by comparing the angular correlation functions and bias of their LAE samples at $z = 6.6$ with the theoretical predictions of McQuinn et al. (2007) and Furlanetto et al. (2006).

We have not attempted a detailed comparison with GP measurements of quasars at $z \lesssim 6$ (e.g., Fan et al. 2006). Such effects depend rather sensitively on the detailed distribution of regions with low neutral gas density, which is not essential for our purposes of modeling the EBL.

Our baseline model that was inconsistent with WMAP is also seen to contradict the LAE constraints on the neutral fraction (Ouchi et al. 2010; which are rather model-dependent as discussed above). In contrast, both the lower-Pop-III and the upper-Pop-III models are generally consistent with the current observational limits, although the latter may be in marginal conflict with the GP constraints of Mesinger & Haiman (2007). Our simplifying assumption of a large enhancement of the ionizing photon emissivity only above $z = z_c$ in these two models leads to their nontrivial evolution of $x_{H\alpha}$, with a dip at $z \sim 10$ due to reionization by Pop-III stars alone, followed by a peak at $z \sim 7–8$ due to partial recombination after Pop-III termination, and then finally complete reionization by Pop-II stars (cf. Cen 2003). More realistic modeling with a smoother transition from Pop-III to Pop-II populations may make such features less pronounced.

Besides a large contribution from Pop-III stars, we note that various other aspects may be important in achieving sufficient ionizing photons at $z \gtrsim 8$ to account for the WMAP data (e.g., Haardt & Madau 2012; Kuhlen & Faucher-Giguère 2012). These include steeping of the faint-end slope of the LF (Bouwens et al. 2012), smaller clumping factor (Bolton & Haehnelt 2007; Pawlik et al. 2009), larger escape fraction (Yajima et al. 2011), more top-heavy IMF (McKee & Tan 2008), and X-rays from accreting black holes (Ricotti & Ostriker 2004; Mirabel et al. 2011).

4. EXTRAGALACTIC BACKGROUND LIGHT

The background intensity $I(v_0, z_0)$ at redshift $z_0$ and frequency $v_0$ is computed by integrating the radiation from all sources between $z = z_0$ and the maximum redshift of the source
distribution \( z_{\text{max}} \) (see, e.g., Peacock 1999),

\[
I(v_0, z_0) = \frac{1}{4\pi} \int_{z_0}^{z_{\text{max}}} dz \frac{dl}{dz} j(v, z) ,
\]

where \( j(v, z) \) is the comoving volume emissivity at redshift \( z \) and frequency \( v = v_0(1 + z) \), calculated by combining our CSFH and stellar population synthesis models. We set \( z_{\text{max}} = 20 \).

From Equation (14), the specific radiation energy density (in units of erg s\(^{-1}\) cm\(^{-3}\) Hz\(^{-1}\)) in the proper volume is

\[
\rho(v_0, z_0) = \frac{4\pi}{c} (1 + z_0)^3 I(v_0, z_0) .
\]

The photon proper number density is

\[
\frac{dn(\epsilon_0, z_0)}{d\epsilon_0} = \frac{\rho(v_0, z_0)}{\epsilon_0} ,
\]

where \( \epsilon_0 = h_p v_0 \) is the photon energy and \( h_p \) is the Planck constant.

Figure 6 plots the proper photon density for our models. The proper photon number density increases from \( z = 10 \) up to \( z \sim 1–3 \) where the CSFH reaches a peak and then decreases toward the local universe. Once we increase the Pop-III component, the UV photon density at high redshifts becomes higher and comparable to that at \( z = 1 \). Although the IR photon density also increases, it is not as significant as the UV since there is little dust at high redshifts.

The EBL intensity at \( z = 0 \) for the baseline model is displayed in Figure 7 as a function of wavelength \( \lambda \). We also show other theoretical models for comparison (Kneiske et al. 2004; Stecker et al. 2006; Franceschini et al. 2008; Gilmore et al. 2009, 2012b; Finke et al. 2010; Kneiske & Dole 2010), together with current measurements of the EBL and the integrated brightness of galaxies. Detailed predictions for the proper photon number density and the local EBL intensity is publicly available at our website.\(^9\)

\(^9\) http://www.slac.stanford.edu/~yinoue/Download.html

The overall shape of our EBL model is consistent with the observational data. Our model is in good agreement with the observations by Pioneer 10/11 (Matsuoka et al. 2011, open pentagon symbols in Figure 7) which directly measured the EBL from outside the zodiacal region. It also does not violate the limits from gamma-ray observations (Aharonian et al. 2006a; Albert et al. 2008).

Compared to other models, we tend to predict more photons at \( \lambda \leq 0.4 \mu m \) and less photons at \( \lambda > 0.4 \mu m \). In the UV range, all other models except for Stecker et al. (2006) are consistent with the GALEX data (Xu et al. 2005), while ours are consistent with the Hubble Space Telescope (HST) data (Gardner et al. 2000). Both observational data points show the galaxy counts integrated down to zero luminosity. One reason for this difference may be in the treatment of dust obscuration. The Calzetti law (Calzetti et al. 2000) that we use was shown by Somerville et al. (2012) to result in more UV photons compared to the multi-dust component model adopted by Gilmore et al. (2012b) and Somerville et al. (2012). We also note that the data points by Madau & Pozzetti (2000) are galaxy counts integrated down to the detection limit of the HST, implying a weaker lower-limit to the EBL.

At \( 0.4 \mu m < \lambda < 10 \mu m \), our model is in reasonably good agreement with Kneiske & Dole (2010) who provide lower-limits to the EBL. The CSFHs in our model and in Kneiske & Dole (2010) are a factor of two to three lower than those of Hopkins & Beacom (2006) that were used in most previous studies. We note that Kneiske & Dole (2010) only discussed the global average over the universe and did not account for the distributions of metallicity and dust attenuation in different galaxies.

Figure 8 shows the Pop-III contribution to the EBL in our models, which are all \( \lesssim 0.03 \) nW m\(^{-2}\) sr\(^{-1}\) and less than 0.5% of the total NIR background radiation. It is far too low to explain the IRTS data (Matsumoto et al. 2005), even at the highest levels allowed by the reionization constraints (cf. Fernandez et al. 2012). Moreover, even if the ionizing photons from Pop-III stars...
that are absorbed inside galaxies are converted to Ly\alpha photons, the NIR flux will increase by only 15% in case B recombination. Therefore, the NIR background is unlikely to provide strong constraints on Pop-III stars, at least in the framework of our model. Note that our Pop-III EBL spectrum shows two peaks, one in the optical caused by the minor population at low z, and one in the NIR due to the redshifted, enhanced population at $z > z_c = 10$. For the upper-Pop-III model, the contribution from dust in the FIR can be a few percent of the total FIR EBL at $\lambda \gtrsim 1000\mu m$. 

(A color version of this figure is available in the online journal.)
5. GAMMA-RAY ATTENUATION

5.1. Gamma-Ray Opacity

From the redshift-dependent intensity of the EBL as given in Section 4, we can compute the opacity for high-energy gamma rays to $\gamma\gamma$ pair production interactions. The cross section for this process is Heitler (1954)

$$\sigma_{\gamma\gamma}(E_\gamma, \epsilon, \theta) = \frac{3\sigma_T}{16}(1 - \beta^2) \times \left[ 2\beta(\beta^2 - 2) + (3 - \beta^4) \ln \left( \frac{1 + \beta}{1 - \beta} \right) \right],$$

(17)

where $\epsilon$ is the energy of the background photon, $E_\gamma$ is the energy of the propagating high energy photon, and $\beta$ is

$$\beta \equiv \sqrt{1 - \frac{2m_e^2c^4}{\epsilon E_\gamma(1 - \cos \theta)}}, \quad \mu \equiv \cos \theta,$$

(18)

where $\theta$ is the angle between the two colliding photons. The photon energy for which the cross section peaks is given by Equation (1).

For a photon emitted by a source at redshift $z_s$ and observed at $z = 0$ with energy $E_\gamma$, the contribution to the $\gamma\gamma$ optical depth between $z_s$ and $z_0$ ($0 < z_0 < z_s$) is

$$\tau_{\gamma\gamma}(E_\gamma, z_0, z_s) = \int_{z_0}^{z_s} dz \int_{-1}^{1} d\mu \int_{\epsilon_{th}}^{\infty} d\epsilon \frac{d\tau_{\gamma\gamma}}{dz} \sigma_{\gamma\gamma}(E_\gamma(1 + z), \epsilon, \theta),$$

(19)

where $\epsilon_{th}$ is the pair production threshold energy,

$$\epsilon_{th} = \frac{2m_e^2c^4}{E_\gamma(1 + z)(1 - \mu)}.$$  

(20)

Figure 9 shows the $\gamma\gamma$ optical depth as a function of the observed gamma-ray energy $E_\gamma$ for sources at selected redshifts $z = 0–10$, compared with various previous models (Kneiske et al. 2004; Franceschini et al. 2008; Finke et al. 2010; Gilmore et al. 2012b; Inoue et al. 2010a). For all models, $z_0 = 0$ in Equation (19), except for Inoue et al. (2010a) where $z_0 = 4$, the minimum redshift in this model. For our model, only the baseline case is shown, since the Pop-III contribution turns out to be nearly indistinguishable (see below and Section 4). The detailed output for the $\gamma\gamma$ optical depth are publicly available at our website.\(^{10}\) Absorption by the CMB photons is not included here. As described in Section 2.2, there are uncertainties in the redshift evolution of our dust emissivity model in the MIR–FIR, and consequently also in $\tau_{\gamma\gamma}$ above several TeV at $z = 0$. However, at these energies, the opacity due to stellar emission is already of the order of $\sim 10$ (see Figure 10) and will likely mask such uncertainties.

Our model is consistent with the measurements of gamma-ray opacity by Fermi at $z \approx 1$ at the 95% confidence level (Ackermann et al. 2012). Although it is also generally consistent with previous models (Kneiske et al. 2004; Franceschini et al. 2008; Finke et al. 2010; Gilmore et al. 2012b; Inoue et al. 2010a) at $E_\gamma \lesssim 400/(1 + z)$ GeV for $z \lesssim 5$, the opacity above $E_\gamma \sim 400/(1 + z)$ GeV is a factor of $\sim 2$ lower. We recall that our local EBL is lower at $\lambda > 0.4 \mu$m (Figure 7), corresponding to $\gamma\gamma$ interactions preferentially with $\gtrsim 300$ GeV photons (Equation (1)).

For very high-redshift sources at $z \gtrsim 6$, we expect spectral attenuation above $\sim 20$ GeV. This is appreciably higher than in the model of Inoue et al. (2010a), who suggested $\sim 12$ GeV at $z \sim 5$ and $\sim 6–8$ GeV at $z \gtrsim 8–10$. Their basis was the models of cosmic reionization by Choudhury & Ferrara (2006) and Choudhury (2009), which included Pop-III stars as well as QSOs and were developed to explain essentially all observational constraints related to reionization, including $\tau_{e}$ from WMAP and $\chi_{H_1}$ from GP measurements. However,
Figure 9. Optical depth to $\gamma\gamma$ interactions for observed gamma-ray energy $E_\gamma$ and sources at $z = 0.1, 0.3, 1.0, 3.0, 5.0, 7.0$, and $10.0$. The solid curves show our baseline model, which is nearly indistinguishable from our models including Pop-III stars. The dashed, dotted, dot-dashed, double dot-dashed, and triple dot-dashed curves show the models by Kneiske et al. (2004), Franceschini et al. (2008), Finke et al. (2010), Gilmore et al. (2012b), and Inoue et al. (2010a), respectively. The shaded region represents the 95% confidence level measurement of the gamma-ray opacity by Fermi at $z \approx 1$ (Ackermann et al. 2012). The horizontal thin dotted line marks $\tau_{\gamma\gamma} = 1$.

(A color version of this figure is available in the online journal.)

Figure 10. Same as Figure 9, but separately for each stellar population. The solid, dashed, dotted, dot-dashed, and double dot-dashed curves show the contributions to the baseline model from all stars plus dust, all stars, Pop-I stars, Pop-II stars, and Pop-III stars, respectively. The contribution of Pop-III stars is small and does not appear in the panel for $z = 0.1$.

(A color version of this figure is available in the online journal.)

optimized for the reionization epoch, they focused on $z \geq 4$ and did not account for Pop-I stars with $Z > 0.02 Z_\odot$ or dust. While a thorough comparison between the two models is not feasible, the principal difference appears to be in the CSFH for Pop-II stars, which is a factor of $\sim 3–10$ higher at $z \gtrsim 6$ in Inoue et al. (2010a) compared to our baseline model here. This demonstrates that such differences in the CSFHs can be clearly distinguishable through future gamma-ray observations.
The highest redshifts of high-energy gamma-ray sources known so far are \( z \sim 3 \) for blazars and \( z = 4.35 \) for GRBs. Based on a model for the gamma-ray LF of blazars, Inoue et al. (2011) proposed that Fermi may eventually detect blazars up to \( z \sim 6 \). GRBs are known to occur at \( z > 6 \) (Kawai et al. 2006; Greiner et al. 2009), at least up to \( z \sim 8.2 \) (Tanvir et al. 2009; Salvaterra et al. 2009), and probably out to the epoch of first star formation in the universe (Bromm & Loeb 2006). If a bright burst similar to GRB 080916C (Abdo et al. 2009) occurs at such redshifts, then CTA may be able to measure its spectrum up to \( z \sim 7−10 \) (Inoue et al. 2013; and possibly even higher, see, e.g., Toma et al. 2011), offering a unique probe of the EBL during cosmic reionization.

Figure 10 shows the \( \gamma \gamma \) opacity due to each stellar population separately for the baseline model: Pop-I stars \( (10^{−4} < Z < 10^{−2.5}) \), Pop-II stars \( (10^{−1} < Z < 10^{−2.5}) \), and Pop-III stars \( (Z < 10^{−4}) \). Here we have chosen the dividing metallicity between Pop-II halo stars and Pop-I disk stars to be \( Z = 10^{−2.5} \), as the distinction between the two populations is known to occur at \( [\text{Fe/H}] \simeq −1 \), corresponding to \( Z \simeq 10^{−2.7}−10^{−2.3} \) (Wheeler et al. 1989; McWilliam 1997; Prochaska et al. 2000). Although the gamma-ray attenuation signature of Pop-III stars seems difficult to discern, that due to Pop-II stars should be observable in future observations of high-\( z \) gamma-ray sources and will provide a valuable probe of the evolving UV EBL in the cosmic reionization epoch. The detection of even one photon from such redshifts will impose useful limits on cosmic reionization models as well as Pop-III stars.

Figure 11 shows the differential contributions to the \( \gamma \gamma \) optical depth \( d\tau_{\gamma\gamma}/dz \) with respect to redshift \( z \) for observed gamma-ray energy \( E_{\gamma} \) and sources at \( z = 1.0, 4.0, 6.0, 8.0, \) and \( 10.0 \). The solid, dashed, and dotted curves show the baseline, lower-Pop-III, and upper-Pop-III models, respectively.

(A color version of this figure is available in the online journal.)

Figure 11. Differential \( \gamma \gamma \) optical depth \( d\tau_{\gamma\gamma}/dz \) with respect to redshift \( z \) for observed gamma-ray energy \( E_{\gamma} \) and sources at \( z = 1.0, 4.0, 6.0, 8.0, \) and \( 10.0 \). The solid, dashed, and dotted curves show the baseline, lower-Pop-III, and upper-Pop-III models, respectively. (A color version of this figure is available in the online journal.)

5.2. Comparison with Current GeV and TeV data

Gamma-ray astronomy has seen enormous progress during the last decade, led by new generation facilities such as Fermi, H.E.S.S., MAGIC, and VERITAS, among others. Further progress is anticipated in the near future with CTA. CTA is expected to detect >100 blazars up to \( z \sim 2.5 \) (Inoue et al. 2010b; Inoue 2011c; Sol et al. 2013). It is also expected to detect GRBs at a rate of the order of a few per year, possibly out to much higher redshifts (Kakuwa et al. 2012; Gilmore et al. 2012a; Inoue et al. 2013). Such observations will allow us to greatly clarify the evolution of the EBL in the UV–NIR bands. Detailed observations of TeV blazars at low \( z \) will also be crucial for probing the FIR EBL, which would not be possible with high-\( z \) sources. Starburst galaxies have also been suggested as alternative targets for studying the FIR EBL (Dwek & Krennrich 2013), even though internal gamma-ray absorption may limit their usefulness (e.g., Inoue 2011b).

The gamma-ray horizon energy at which \( \tau_{\gamma\gamma} = 1 \) as a function of \( z \), known as the Fazio–Stecker relation (Fazio & Stecker 1970), is shown in Figure 12 in comparison with other models (Kneiske et al. 2004; Franceschini et al. 2008; Finke et al. 2010; Gilmore et al. 2012b; Inoue et al. 2010a). We also plot the maximum energies of photons detected from a sample of blazars (see Finke & Razzacaue 2009, for a list and references) as well as GRB 080916C (Abdo et al. 2009). The inset in Figure 12 is a blow up for \( z = 5−10 \) to emphasize the differences among our models with and without Pop-III stars.

The highest photon energies for many blazars lie in regions considerably above the \( \tau_{\gamma\gamma} = 1 \) curves for all EBL models, indicating that their spectra are likely to be highly attenuated. It is also clear that GRB 080916C provides an important constraint on the EBL at \( z \sim 4 \). Our model predicts that the universe is transparent below 20 GeV even at \( z > 4 \).

Figures 13 and 14 show the observed spectra of TeV blazars at \( z \leq 0.15 \) and \( z > 0.15 \), respectively, together with their intrinsic
Figure 12. Gamma-ray horizon energy where $\tau_{\gamma\gamma} = 1$. The baseline, lower-Pop-III, and upper-Pop-III models are shown by the thick solid, thick dashed, and thick dotted curves, respectively. The dashed, dotted, dot-dashed, double dot-dashed, triple dot-dashed curves represent the models by Kneiske et al. (2004), Franceschini et al. (2008), Gilmore et al. (2012), and Inoue et al. (2010a), respectively. The thin solid curve shows the case of $\tau_{\gamma\gamma} = 5$ for the baseline model. The filled data points are the observed maximum energies of photons from a sample of blazars (Finke & Razzaque 2009) and GRB 080916 C (Abdo et al. 2009). Since other papers do not cover the opacity at $z = 0–10$, we do not show the opacity of each model at the outside of the redshift range of each paper. The small panel in the figure shows the gamma-ray opacity horizon at $z = 5–10$.

(A color version of this figure is available in the online journal.)

Figure 13. Spectra of TeV blazars at $z \leq 0.15$ as observed (circle) and inferred before EBL attenuation (triangle) with our baseline model. References for the data are Mrk 421 (Albert et al. 2007c), Mrk 501 (Albert et al. 2007d), BL Lac (Albert et al. 2007a), PKS 2005-489 (Aharonian et al. 2005a), W Comae (Acciari et al. 2008), PKS 2155-304 (Aharonian et al. 2005b), B3 2247+381 (Aleksić et al. 2012), RGB J0710+591 (Acciari et al. 2010), H 1426+428 (Aharonian et al. 2002), 1ES 0806-524 (Acciari et al. 2009a), 1ES 0229+20 (Aharonian et al. 2007b), and 1RXS J1010--3119 (Abramowski et al. 2012b).

(A color version of this figure is available in the online journal.)

spectra before attenuation by the EBL, assuming our baseline model. If the TeV emission from these sources originates from electrons accelerated according to the simplest test-particle theory of diffusive shock acceleration (Blandford & Eichler 1987), then the hardest spectrum is expected to be that of photon index $\Gamma_{\text{int}} = 1.5$. Although the intrinsic spectra inferred here are generally consistent with $\Gamma_{\text{int}} \geq 1.5$, some sources such as 1ES 0229+20 and 1ES 1101–232 show evidence of
harder spectra above several hundred GeV (see also Finke et al. 2010).

To explain such intrinsically hard spectra, some authors have recently suggested secondary cascade components generated by very high energy cosmic-rays or gamma-rays, which may also offer a probe of intergalactic magnetic fields (e.g., Essey & Kusenko 2010; Essey et al. 2011; Essey & Kusenko 2012; Murase et al. 2012; Aharonian et al. 2013). Others have proposed effects of time-dependence, stochastic acceleration, or multiple emission components (Lefa et al. 2011a, 2011b). However, in order to account for the Thomson scattering optical depth measured by WMAP, the ionizing photon emissivity is required to be 50–100 times higher at $z > 10$. This is in line with recent observations of galaxy candidates at $z \sim 8$, as long as the contribution from faint galaxies below the sensitivity of current telescopes is not large (e.g., Bouwens et al. 2012). The “missing” ionizing photons may possibly be supplied by Pop-III stars forming predominantly at these epochs in sufficiently small galaxies.

The EBL intensity at $z = 0$ in our model is generally not far above the lower limits derived from galaxy counts. Our model is also in good agreement with the data from Pioneer (Matsuoka et al. 2011) directly measured from outside the zodiacal region. The Pop-III contribution to the NIR EBL is $\lesssim 0.03$ nW m$^{-2}$ sr$^{-1}$, less than 0.5% of the total in this band, even at the maximum level compatible with WMAP measurements. The putative NIR EBL excess (Matsumoto et al. 2005), which also conflicts with the upper limits from gamma-ray observations (Aharonian et al. 2006a), may have a zodiacal origin rather than Pop-III stars.

Up to $z \sim 3–5$, the $\gamma\gamma$ opacity in our model is comparable to that in the majority of previously published models (Kneiske et al. 2004; Franceschini et al. 2008; Finke et al. 2010; Gilmore et al. 2012b) below $E_\gamma \sim 400/(1 + z)$ GeV, while it is a factor of $\sim 2$ lower above this energy. The universe is predicted to be largely transparent below 20 GeV even at $z > 4$. 

6. CONCLUSIONS

We have developed models for the EBL over the redshift range $z = 10$ to $z = 0$ on the basis of a semi-analytical model of hierarchical galaxy formation, into which Pop-III stars were incorporated in a simplified fashion. Our baseline model is consistent with a wide variety of observational data for galaxies below $z \sim 6$ (Nagashima & Yoshii 2004; Kobayashi et al. 2007, 2010), and is also capable of reionizing the universe by $z < 8$. However, a zodiacal origin rather than Pop-III stars. Future CTA observations of these objects with high energy and time resolution will elucidate such issues.

The signature of EBL absorption has not been seen in the spectrum of the extragalactic gamma-ray background (EGB) above 100 GeV (Ackermann 2011), even though it is naturally expected if its origin is cosmological (Inoue 2011a; Inoue & Ioka 2012). By considering the effects of cascade emission, Inoue & Ioka (2012) have recently shown that if the EGB at $< 100$ GeV (Abdo et al. 2010b) is entirely composed of known types of sources whose spectra are well constrained by existing observations, then the measured EGB at $> 100$ GeV would be inconsistent with this hypothesis, even for a low EBL such as proposed here. Further detailed spectral studies of extragalactic gamma-ray sources are required to resolve this issue.

Figure 14. Same as Figure 13, but for sources at $z > 0.15$. References for the data are H 2356-309 (Aharonian et al. 2006b), RX J0648.7+1516 (Aliu et al. 2011), 1ES 1101+496 (Aharonian et al. 2007a), RBS 0413 (Aliu et al. 2012), 1ES 1011+496 (Albert et al. 2007b), 1ES 0347+009 (Aharonian et al. 2007c), 1ES 1218+304 (Aharonian et al. 2007a), RX J0648.7+1516 (Aliu et al. 2011), 1ES 0347+009 (Aharonian et al. 2007b), 1ES 0114+184 (Abramowski et al. 2012a), S5 0716+714 (Anderhub et al. 2009), 4C+21.35 (Aleksić et al. 2011a), 3C 66A (Aleksić et al. 2011b), and 3C 279 (Albert et al. 2008). (A color version of this figure is available in the online journal.)
Estimates based on the observed gamma-ray LF of blazars show that Fermi may detect blazars up to $z \sim 6$ (Inoue et al. 2011). CTA may possibly detect GRBs up to similar redshifts (Inoue et al. 2013). However, the contribution of Pop-III stars may be difficult to discern in the attenuated spectra of high-redshift gamma-ray sources, even at the highest levels allowed by the WMAP constraints. Nevertheless, the signature of Pop-II stars is expected to be observable in high-$z$ gamma-ray sources, providing a unique and valuable probe of the evolving EBL in the rest-frame UV.

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APPENDIX
COSMIC STAR FORMATION HISTORY

In this appendix, we briefly review the method of conversion to the CSFH from the measurement of the 1500 Å UV LD $\rho_{\text{obs}}(z)$, for which there are two steps (see Kobayashi et al. 2013, for details). One is the correction for dust obscuration to derive the intrinsic LD $\rho_{\text{int}}(z)$ and the other is the conversion of the intrinsic LD to the star formation rate density $\rho_{\text{star}}(z)$. Dust obscuration correction and star formation rate conversion are given by

$$\rho_{\text{int}}(z) = C_{\text{dust}}(z) \rho_{\text{obs}}(z), \quad (A1)$$

$$\rho_{\text{star}}(z) = C_{\text{SFR}}(z) \rho_{\text{int}}(z). \quad (A2)$$

Hopkins (2004) assumed redshift-independent $C_{\text{dust}}$ and $C_{\text{SFR}}$, while Bouwens et al. (2007) and Cucciati et al. (2012) assumed redshift-dependent $C_{\text{dust}}$ but with redshift-independent $C_{\text{SFR}}$ (see Bouwens et al. 2007; Cucciati et al. 2012, for details). However, these simple assumptions for all redshifts can cause an overestimation of the CSFH. Kobayashi et al. (2013) have recently proposed a new redshift dependent conversion method based on their semi-analytical galaxy formation model as

$$C_{\text{dust}}(z) = 2.983 \exp[-0.3056(1+z)] + 1, \quad (A3)$$

$$C_{\text{SFR}}(z) = 10^{-28.01}[1 - 5.915 \times 10^{-5}(1+z) + 7.294 	imes 10^{-4}(1+z)^2] M_\odot \text{yr}^{-1} \text{erg s}^{-1} \text{Hz}^{-1} \cdot (A4)$$

Figure 15 shows the CSFH converted from the observed 1500 Å LD using the methods developed by Hopkins (2004), Bouwens et al. (2007), Cucciati et al. (2012), and Kobayashi et al. (2013). The 1500 Å UV LD data used in Hopkins (2004) are from Giavalisco et al. (2004) and Massarotti et al. (2001). The expected CSFH from our baseline Mitaka model fits well to the CSFH following Kobayashi et al. (2013).

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