D2CoPlan: A Differentiable Decentralized Planner for Multi-Robot Coverage

Vishnu Dutt Sharma¹, Lifeng Zhou², and Pratap Tokekar¹

Abstract—Centralized approaches for multi-robot coverage planning problems suffer from the lack of scalability. Learning-based distributed algorithms provide a scalable avenue in addition to bringing data-oriented feature generation capabilities to the table, allowing integration with other learning-based approaches. To this end, we present a learning-based, differentiable distributed coverage planner (D2CoPlan) which scales efficiently in runtime and number of agents compared to the expert algorithm, and performs on par with the classical distributed algorithm. In addition, we show that D2CoPlan can be seamlessly combined with other learning methods to learn end-to-end, resulting in a better solution than the individually trained modules, opening doors to further research for tasks that remain elusive with classical methods.

I. INTRODUCTION

Multi-robot coverage and tracking is a well-studied problem. Over the years, several approaches have been presented for planning and coordination algorithms [19]. In particular, consider the problem of covering a set of mobile targets using a team of aerial robots with downwards-facing cameras (Figure 1). A target is said to be covered if it falls within the field-of-view of one of the robots’ cameras. The objective is for the robots to choose their individual trajectories so as to maximize the total number of targets covered.

There are several reasons why this problem is challenging. Coordination amongst the robots is critical as you want to avoid overlap and maximize the coverage. This is easier in a centralized setting; however, our focus is on decentralized strategies where the robots can communicate directly only with their immediate neighbors. Decentralization is also harder since each robot only knows of the targets in their own field-of-view. Finally, since we need to cover mobile targets, we need to predict their motion over the planning horizon. However, the motion model of the targets itself may be unknown making the problem even more challenging.

In this paper, we investigate the question: Can the robots learn to plan and coordinate in a decentralized fashion for target coverage problems? Recently, there has been significant work on learning-based approaches to multi-robot planning. However, most of this work is restricted to coordination for path finding (where each robot needs to find the shortest path to its own goal position in an unknown environment) [4], [8], [9] and formation control (such as flocking) [6], [13].

This work is supported by the National Science Foundation under Grant No. 1943368 and ONR under grant number N00014-18-1-2829.

¹Vishnu D. Sharma and Pratap Tokekar are with the Dept. of Computer Science, University of Maryland, College Park, MD, USA {vishnuds, tokekar}@umd.edu
²Lifeng Zhou is with the Dept. of Electrical and Computer Engineering, Drexel University, Philadelphia, PA, USA lz4578 drexel.edu

We build on this to study a more complex task that requires planning, coordination, and prediction.

Our contribution is a decentralized, differentiable coverage planner (D2CoPlan) for multi-robot teams. D2CoPlan consists of three differentiable modules, namely map encoder, decentralized feature aggregator, and local action selector. The input to D2CoPlan is a coverage map that represents predictions of where the targets are going to be in the next timestep. This map comes from another differentiable module we call Differentiable Map Predictor (DMP). The map encoder takes the predicted maps and turns it into a compact representation which is shared with the other agents using a Graph Neural Network (GNN) [11]. The GNN aggregates information from neighboring agents and uses that for selecting the ego robot’s action. D2CoPlan is trained on an expert strategy (centralized optimal algorithm that has global information) but is executed in a decentralized fashion (following the Centralized Training, Decentralized Execution paradigm [7]). We show that D2CoPlan is a scalable, efficient approach for multi-robot target coverage. In particular, we show that D2CoPlan is able to achieve 93% of the centralized optimal algorithm in up to 150x less time but in a decentralized fashion.

A typical approach for this problem is to frame it as a submodular maximization problem with a uniform matroid constraint [1]. A decentralized greedy (DG) algorithm gives theoretical performance guarantees and works well empirically [10], [15]. We show that D2CoPlan performs as well as DG when the ground truth positions of the targets are known and better when the robots have to predict the motion of the targets. Further, the running time of D2CoPlan scales better compared to DG. A key advantage of D2CoPlan is that it consists of two differentiable modules, where the observation processor module can be trained to be compatible with the planner module. We investigate several ways of combining the two modules as well as ablation studies for the design of D2CoPlan’s architecture.

The rest of the paper is organized as follows: we first discuss the related work on this topic in Section II. Then we formulate the problem in Section III. Section IV describes the design of D2CoPlan. Section V first provides the implementation details and then describe various experiment and the results obtained. We conclude by summarizing our finding in Section VI and discuss the avenues of future work. We also share these finding on our project webpage.³

³Project Webpage: http://raaslab.org/projects/d2coplan.html
II. RELATED WORK

Multi-robot coordination problems have largely relied on using classical, non-leaning-based approaches. The centralized approaches assume presence of a single entity which can access observations from all the robots and plan accordingly. Since finding optimal solutions may be practically intractable, the centralized approaches often utilize greedy formulations to find approximate solutions. Many multi-robot tracking and coverage objectives are submodular i.e., they have diminishing return property, and greedy solutions provide constant factor approximation guarantee for them [17].

Finding solutions with centralized approaches is still computationally expensive and the runtime rapidly increases with the increase in the number of robots. Decentralized approaches provide an efficient solution at the cost of a lower, but acceptable drop in the task performance, by distributing the task of computation to cliques [12], [17], [18]. The communication could be expanded to multiple hops to increase the information horizon, but it comes at the cost of increased runtime [10], [15].

Neural networks provide an avenue to improve upon classical solutions through their ability to model complexities using data. Furthermore, a differentiable approach can be combined with other differentiable methods to enable efficient with end-to-end learning from data [2]. Introduction of GNNs [11] to solve problem with graph representations opened doors to application of neural networks to decentralized multi-robot tasks by facilitating feature sharing between robots [4]. Recent works have successfully employed GNNs to solve multi-robot problems such path planning [8], [9], persistent monitoring [3], and formation control [6], [13] among others. Specifically for multi-robot coverage problems, Tolstaya et al. [14] and Gosrich et al. [5] used GNNs in different training paradigms to learn control policies. Many of these works show that apart from achieving near-expert solutions, GNNs can help scale well to larger robot teams.

Unlike these works, we specifically focus on target coverage. Recently, Zhou et al. [16] proposed a planner for the coverage problem using GNN and show such a planner performs on par with the classical counterpart and scales marginally better. However, their approach handcrafted features and uses only 20 closest target as input. This design makes the network non-differentiable at the input layer and thus can not be used in conjunction with other learning methods. We address both these issues in our work by using a richer map representation, while also improving the coverage performance and scalability.

III. PROBLEM FORMULATION

In this work, we investigate the problem of decentralized, multi-robot action selection for joint coverage maximization. Consider the scenario in Figure 1. A set of $N$ robots are tasked to cover targets moving in a grid of size $G \times G$. Every robot $R_i$ has a set of actions $A_i$ that it must select from at each time step. All the targets that fall within the sensing range $r_s$ (e.g., camera footprint) are said to be covered by the robot. The objective is to maximize the total number of targets covered in the next step by selecting the actions for each robot.

We assume that the robots do not collide with each other (e.g., by flying at different altitudes). A robot $R_i$ can communicate with another robot $R_j$ if it is within the communication range $r_c$. The robots need to select their actions based on only local information.

Each robot has access to a local coverage map, which gives the predicted occupancy of targets near the robot (specifically, targets that can be covered by its motion primitives). Any overlap in covering the same set of targets results in the targets being counted as covered only once. We show an example in Figure 2 where robot 2 and robot 3 may end up tracking the same target. Thus, a robot must collaborate with others to minimize overlap in motion for efficient coverage. To do so, the robot must also share its local coverage map with others. It is also important to share a compact representation of the map to reduce the bandwidth requirement of the algorithm.

Our main contribution is D2CoPLAN, which solves both problems simultaneously. It consists of a map encoder that comes up with a compact representation of each robot’s coverage map, an information aggregator, followed by an action selector. Furthermore, since D2CoPLAN is differentiable, we can combine it with a Differentiable Map Predictor (DMP), that takes as input the history of observations from a robot and predicts the coverage map of where the targets are going to be when the robots move.

IV. METHODS

We present a differentiable, decentralized coverage planner called D2CoPLAN to efficiently solve the multi-robot coverage problem by predicting the best action for a robot given its local coverage map. It can be integrated with any differentiable map predictor (DMP), to solve tasks where direct observations are not available. We design D2CoPLAN as a combination of three sub-modules:

A. Map Encoder

This module takes the robot’s coverage map as input and transforms it into a feature vector that can be shared with the robot’s neighbors. We implement this module using a
Fig. 2: An illustrative example: at a given time step, each robot $R_i$ must choose a motion primitive $a_{i,k}$ (dashed curves). The background map shows areas with high target density with blue and low target density with red. Here, $R_1$ has one motion primitive $\{a_{1,1}\}$, $R_2$ has two primitives $\{a_{2,1}, a_{2,2}\}$, and $R_3$ also has two motion primitives $\{a_{3,1}, a_{3,2}\}$. The size of the coverage map depends on the robot’s sensing range $r_s$ and moving distance $d_c$. As $R_2$ and $R_3$ have overlapping coverage maps, they must communicate with each other using communication links (red arrows) of range $r_c$, to choose actions that can maximize the total coverage.

multi-layer Convolutional Neural Network (CNN), consisting of convolution, pooling, and ReLU activation layers. The input to the encoder is the coverage map as a single channel image of size $G \times G$. The output features from the CNN are flattened into a vector of size $H \times 1$ before sharing with the neighbors. This also allows for compressing the local maps making it efficient to communicate them to other robots. We choose CNN as the encoder here over a fully-connected neural network as it allows for a richer representation than the pre-processed inputs required for the latter as used in prior work [16]. Furthermore, we do not need to limit the maximum number of targets as input in our representation.

B. Distributed Feature Generator

This part of the network enables sharing of the map encoding features with a GNN. GNN enables feature aggregation for each graph node through neural networks, allowing distributed execution. The information can be shared with $K$-hop communication to the neighbors identified using the adjacency matrix. The output of this module summarize the information from the neighbors as a vector, enabling informed decision-making in the next step.

C. Local Action Selector

The last module of D2CoPLAN is responsible for prescribing the best action to the robot based on the information gathered from the neighbors in the previous step. We implement this module as a Multi-Layer Perception (MLP) which outputs a $|A|$-dimensional output, denoting the fitness of each action, $a_i \in A$. During the training the loss is calculated as cross-entropy over these outputs with the ground truth actions. Thus, this module enables the gradient flow for end-to-end training for D2CoPLAN.

For training D2CoPLAN, we use a centralized greedy algorithm as the expert algorithm to generate the target actions. The centralized greedy algorithm has access to global information (i.e., the global coverage map) and can therefore make much more informed decisions. In fact, it is known that the centralized greedy algorithm is within $\sim 66\%$ of the centralized optimal which eliminates the need to run optimal, brute force search algorithm that is infeasible for generating training data for large number of robots. The expert algorithm evaluates the coverage by each robot-action pair and selects the pair with the highest value. The selected robot and the covered targets are removed from consideration and the process is repeated till each robot is assigned an action. The algorithm has a time complexity of $O(n^2)$ for $n$ number of robots. We refer to this algorithm as Expert.

D. Differentiable Map Predictor

To transform the robot’s observation to coverage maps, we introduce a map predictor module. To allow integration with D2CoPLAN in order to learn the transformation we use a differentiable map predictor (DMP). The design of DMP depends on the task at hand and can be realized with neural networks. For example, if the task is defined as maximizing coverage with moving targets, DMP can be implemented as a recurrent neural network. We use CNN to solve this task by stacking the historical observations as a multidimensional image and train it with a pre-trained D2CoPLAN over the expert actions. This module is optional and we can use the ground truth coverage map for action selection, if available.

V. EXPERIMENTS AND RESULTS

A. Experiment Setup

In our experiments, We use D2CoPLAN trained over $N = 20$ robots. To generate the training data, we use a grid with $G = 100$ i.e., a grid with size $100 \times 100$. The target coverage maps are generated using a mixture of Gaussian to simulate low and high-density areas. The intuition is to mimic real-life situations such as animals density being higher closer to water holes and lower around ditches in a forest. For this, we choose a random number of Gaussian components in the range $[10, 30]$ with the standard deviation for each uniformly sampled from the set $\{20, 30, 40, 50\}$. The locations of the means are selected uniformly at random on the grid. Some of the components are randomly inverted by multiplying by $-1$ to simulate lower density regions. The probability density obtained by summing up the components is then normalized to obtain a categorical probability density function over the grid. As the last step, we sample locations using this density function to fill $15\%$ of the grid cells to represent the target locations. We simulate linear motion for the targets with randomly chosen initial velocity.

The robot locations are randomly selected on the grid. The action set for each robot consists of 5 actions, one per cardinal direction and one to stay in place. The sensing range $r_s = 6$, each action moves a distance of $d_c = 20$, and communication range is $r_c = 20$. With our choice of action primitives, the coverage map looks like a rectangular field on the grid of size $G \times G$, where only the target within the coverage map are visible. The communication is limited to
1-hop only. We generate total 40000 maps and run Expert on each to obtain the target actions. From this dataset, 60% instances are used for training, 20% are used for validation and the rest are used for testing.

Map encoder is implemented as a 3-layer CNN (Conv→ReLU→Maxpool) with intermediate output features of size 4, 8 and 16. The final output is flattened to a vector of size 1600. This vector acts as a compressed map representation. For Distributed feature aggregator, we use implementation by Li et al. [8] with 2 graph layers of 512 and 128 nodes and ReLU activation. Local action selector is implemented as a single layer fully connected network, directly predicting the actions. We also use dropout of 20% in the CNN layers and after the GNN to regularize the network. We train the network on a 32-core, 2.10Ghz Xeon Silver-4208 CPU and a Nvidia GeForce RTX 2080Ti GPU with 11GB of memory for 1500 epochs and use the network weights with the minimum validation loss for evaluation.

B. Evaluation

An efficient distributed planner must have some desirable properties: it should run faster than the centralized algorithm, while achieving coverage within a reasonable margin of the centralized algorithm; and it should scale well with varying number of agents by generalizing beyond the settings it is trained on. In this section, we present empirical evidence that D2CoPLAN has the aforementioned desirable properties. We go one step further and show that D2CoPLAN scales better than even DG. Finally, we demonstrate the advantages of a differentiable design. Specifically, we show that D2CoPLAN performs better when combined with DMP than DG.

1) Comparisons with Expert: We begin by comparing the coverage performance (number of targets covered) and runtime of D2CoPLAN with the Expert which is the centralized greedy algorithm that D2CoPLAN is trained using. In this set of experiments, we use the ground truth coverage map as inputs since our focus is on evaluating the planner. In subsequent experiments, we will evaluate the effect of the map predictor on the coverage task.

D2CoPLAN was trained on a dataset of 20 robots in a grid of size 100 × 100. We compare the two algorithms with increasing number of robots (from 4 to 50) in the same grid. We run 1000 Monte-Carlo simulations for each setting. The results for this evaluation are shown in Figure 4. D2CoPLAN has a clear advantage in terms of runtime and the advantage increases as the number of robots increases. For example, with 50 robots, D2CoPLAN is more than two orders of magnitude faster than Expert. This is not surprising since Expert is a centralized algorithm whose runtime scales quadratically with the number of robots whereas D2CoPLAN is a decentralized algorithm. In addition to being significantly faster, we also observe that D2CoPLAN covers 92% of the targets as the Expert, despite each robot having only a limited amount of information.

2) Comparisons with DG: Next, we compare D2CoPLAN with a classical decentralized algorithm, DG. In DG, each robot chooses its own action by running a greedy algorithm but only on the set that includes itself and its immediate neighbors (hence, decentralization). As shown in Figure 5, D2CoPLAN and DG perform almost the same in terms of the number of targets tracked. However, the real advantage of D2CoPLAN comes in the runtime where we observe it becomes much faster than DG as the number of robots increases (e.g., with 50 robots, D2CoPLAN is almost twice as fast). While both algorithms are decentralized, DG still requires running a greedy algorithm over the local neighborhood of each robot which increases the runtime as the density of the robots increase. Furthermore, in Section V-B.4 we show that D2CoPLAN outperforms DG even in terms of coverage performance when the true coverage map is not given.

3) Generalization: Next, we evaluate the generalization capability of D2CoPLAN beyond the scenario it has been trained on. We test two types of generalization: (1) across number of robots; and (2) across density of the targets (i.e., coverage map) in the environment. For both tests, we train on a specific number of robots (1) or target density (2) and test
with a different number of robots (1) or target density (2). We summarize these results in Table I and Table II obtained over 1000 Monte-Carlo runs.

We observe that D2CoPlan generalizes well in both cases. Table I shows the coverage performance when trained on the number of robots given in the row and tested on the number of robots given in the column. We see that in most cases, the performance remains unchanged. The network trained on 10 robots sees a slight drop in performance on other test configurations but still covers around 90% of the targets covered by Expert.

D2CoPlan also generalizes well across varying target density as shown in Table II. We observe that D2CoPlan trained with a target density of 15% performs almost the same when tested on other target densities. The performance is \( \sim 93\% \) of the Expert in all cases but 5% density (where it is \( \sim 91\% \)), which we believe is caused by fewer number of available targets, increasing the gap in the performance of the compared algorithms. These results validate the claim that D2CoPlan trained under one type of scenario generalizes to other deployment scenarios.

4) Prediction and Planning: A key advantage of D2CoPlan is its differentiability, allowing D2CoPlan to be combined with other gradient-based learning methods to solve challenging problems in an end-to-end manner. In this section, we evaluate how the differentiable map predictor can be trained along with the differentiable planner (D2CoPlan).

![Diagram of Coverage Scaling](image1)

![Diagram of Time Scaling](image2)

**Fig. 4:** Comparison of Expert and D2CoPlan in terms of running time (plotted in log scale) and the number of targets covered, averaged across 1000 Monte Carlo trials. D2CoPlan was trained on 20 robots. D2CoPlan is able to cover 92%-96% of the targets covered by Expert, while running at a much faster rate.

![Diagram of Coverage Scaling](image3)

![Diagram of Time Scaling](image4)

**Fig. 5:** Comparison of D2CoPlan and DG in terms of running time (plotted in log scale) and the number of targets covered, averaged across 1000 Monte Carlo trials. D2CoPlan was trained on 20 robots. D2CoPlan is able to cover almost same number of targets as DG. DG is faster for fewer number of robots, but as the number of robots increase, D2CoPlan scales better than it.

| Test | 10 Robots | 20 Robots | 30 Robots |
|------|-----------|-----------|-----------|
| 10 Robots | 93.95% | 91.12% | 89.71% |
| 20 Robots | 94.38% | 93.17% | 92.60% |
| 30 Robots | 93.25% | 93.47% | 93.73% |

**Table I:** Percentage of the targets covered (the average across 1000 trials) with respect to Expert by D2CoPlan trained and tested with varying numbers of robots.

| Target Density | Relative coverage |
|----------------|-------------------|
| 5%             | 91.40%            |
| 15%            | 93.20%            |
| 25%            | 93.46%            |
| 50%            | 93.46%            |

**Table II:** Percentage of the targets covered (the average across 1000 trials) with respect to Expert by D2CoPlan across varying target density maps.
and compare it with DG.

So far, we have used the ground truth coverage map as input to the planners. Now, we consider a scenario where the input consists of the observations of the targets over the past timesteps. The true motion model of the robots is not known to the robots. Therefore, they need a predictor to estimate the positions of the targets over the planning horizon which can then be used by DG or D2CoPLAN.

Here, we use a DMP to learn the motion model. All the targets move with the same linear velocity selected randomly in the range $[-3, 3]$ at the start of the episode (unknown to the planner). To show the advantage of having a decentralized planner, we compare three methods: (1) an ORACLE i.e., the ground truth map as the mapper along with EXPERT as the planner; (2) DMP as the learnable mapper with DG as the planner; and (3) DMP as the learnable mapper with D2CoPLAN as the planner. In (2), DMP is trained from scratch whereas in (3) DMP is trained by backpropagating the loss from D2CoPLAN. D2CoPLAN itself is frozen and aids DMP in learning better representations for action prediction. The three settings present different combinations of classical and learning-based approaches.

Coverage maps observed over last 3 time steps are used as input to DMP and it predicts the map at the next time step. We use a 4-layer CNN with 8, 16, 4, and 2 channels as DMP. We keep the map size same across each layer to avoid information loss and predict the occupancy probability of each cell as a two-channel map. The probability map thus obtained is used as input to the planner. We trained DMP over 2000 epochs with 5 examples of 20 robots (i.e., 100 training instances) in each. Given that most of the cells in the coverage map will be zero, we weigh the cross-entropy loss by a ratio of 1:10 for free and occupied cells. The action prediction loss for (3) is the unweighted cross-entropy loss.

Figure 6 shows a comparison of the three approaches and provides evidence for benefit of using a differentiable planner to realize end-to-end learning. The combination of D2CoPLAN and DMP is better compared to DG and DMP, despite DMP in the latter being trained on ground truth. We attribute this to the fact that D2CoPLAN and DMP form a differentiable chain which allows DMP to be trained directly on the downstream task (action selection) rather than on just map prediction. DG and DMP, on the other hand, are not a differentiable chain, and thus DMP cannot be trained on the downstream task directly.

We further explore this by comparing 3 ways of training DMP when used in conjunction with D2CoPLAN: (1) DMP and D2CoPLAN are trained together from scratch; (2) DMP and D2CoPLAN are trained individually and then used together; and (3) D2CoPLAN is first trained and then DMP is trained on loss from D2CoPLAN while D2CoPLAN is frozen.

Figure 7 shows the comparison of all three methods. The third approach outperforms the other two. This demonstrates the advantage of having a differentiable planner. Using a pre-trained and frozen D2CoPLAN and training directly on the downstream task loss, allows DMP to learn patterns beneficial for action prediction and not just for map prediction. If both modules are trained from scratch in an end-to-end manner, they may need more time to learn the same behavior. The third approach also does not require ground truth motion models for the targets to be available for training DMP. While in this paper we use the ground truth to generate the expert solutions used in training D2CoPLAN, in general, one can use any other expert algorithm such as human inputs to train D2CoPLAN which does not need ground truth target motion.

| Number of targets covered | DMP + DG | DMP + D2CoPLAN | ORACLE + EXPERT |
|---------------------------|----------|----------------|-----------------|
| 1000                      |          |                |                 |
| 500                       |          |                |                 |
| 300                       |          |                |                 |
| 200                       |          |                |                 |
| 100                       |          |                |                 |
| 400                       |          |                |                 |
| 500                       |          |                |                 |
| 600                       |          |                |                 |
| 700                       |          |                |                 |
| 800                       |          |                |                 |
| 900                       |          |                |                 |
| 1000                      |          |                |                 |

VI. CONCLUSION

We presented D2CoPLAN, a differentiable, decentralized target coverage planner for multi-robot teams. Our experimental results show that D2CoPLAN is more scalable than the classical decentralized algorithm that is used for such tasks while performing closer to the centralized algorithm. Furthermore, due to the fact that it is a differentiable planner, we can combine this with other differentiable modules (e.g., a coverage map predictor) to yield better performance than the classic counterparts. These results present an encouraging path forward for multi-robot coordination tasks. Our immediate work is evaluating D2CoPLAN for more complex tasks. In this paper, we train D2CoPLAN in a supervised setting. We are also working on training D2CoPLAN with reinforcement learning. Finally, an interesting avenue for extension is where we learn not just what to communicate with other robots (as we do in this paper) but also who to communicate with.
REFERENCES

[1] Gruia Calinescu, Chandra Chekuri, Martin Pal, and Jan Vondrák. Maximizing a monotone submodular function subject to a matroid constraint. SIAM Journal on Computing, 40(6):1740–1766, 2011.
[2] Devendra Singh Chaplot, Deepak Pathak, and Jitendra Malik. Differentiable spatial planning using transformers. In International Conference on Machine Learning, pages 1484–1495. PMLR, 2021.
[3] Jingxu Chen, Aniruddh Baskaran, Zhongshun Zhang, and Pratap Tokekar. Multi-agent reinforcement learning for persistent monitoring. In Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), 2021.
[4] Fernando Gama, Elvin Isufi, Geert Leus, and Alejandro Ribeiro. Graphs, convolutions, and neural networks: From graph filters to graph neural networks. IEEE Signal Processing Magazine, 37(6):128–138, 2020.
[5] Walker Gosrich, Siddharth Mayya, Rebecca Li, James Paulos, Mark Yim, Alejandro Ribeiro, and Vijay Kumar. Coverage control in multi-robot systems via graph neural networks. In 2022 International Conference on Robotics and Automation (ICRA), pages 8787–8793. IEEE, 2022.
[6] Arbaz Khan, Ekaterina Tolstaya, Alejandro Ribeiro, and Vijay Kumar. Graph policy gradients for large scale robot control. In Conference on Robot Learning, pages 823–834, 2020.
[7] Landon Kraemer and Bikranjit Banerjee. Multi-agent reinforcement learning as a rehearsal for decentralized planning. Neurocomputing, 190:82–94, 2016.
[8] Qingbiao Li, Fernando Gama, Alejandro Ribeiro, and Amanda Prorok. Graph neural networks for decentralized multi-robot path planning. In 2020 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pages 11785–11792. IEEE, 2020.
[9] Qingbiao Li, Weizhe Lin, Zhe Liu, and Amanda Prorok. Message-aware graph attention networks for large-scale multi-robot path planning. IEEE Robotics and Automation Letters, 6(3):5533–5540, 2021.
[10] Guannan Qu, Dave Brown, and NS Li. Distributed greedy algorithm for multi-agent task assignment problem with submodular utility functions. Automatica, 105:206–215, 2019.
[11] Franco Scarso, Maro Gori, Ah Chung Tsoi, Markus Hagenbuchner, and Gabriele Monfardini. The graph neural network model. IEEE transactions on neural networks, 20(1):61–80, 2008.
[12] Guangyao Shi, Md. Ishat-E-Rabban, Lifeng Zhou, and Pratap Tokekar. Communication-aware multi-robot coordination with submodular maximization. In Proceedings of the IEEE International Conference on Robotics and Automation (ICRA), 2021.
[13] E. Tolstaya, F. Gama, J. Paulos, G. Pappas, V. Kumar, and A. Ribeiro. Learning decentralized controllers for robot swarms with graph neural networks. In Conference Robot Learning 2019, Osaka, Japan, 30 Oct.-1 Nov. 2019. Int. Found. Robotics Res.
[14] Ekaterina Tolstaya, James Paulos, Vijay Kumar, and Alejandro Ribeiro. Multi-robot coverage and exploration using spatial graph neural networks. In 2021 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pages 8944–8950. IEEE, 2021.
[15] Ryan K Williams, Andrea Gasparrini, and Giovanni Ulivi. Decentralized matroid optimization for topology constraints in multi-robot allocation problems. In 2017 IEEE International Conference on Robotics and Automation (ICRA), pages 293–300. IEEE, 2017.
[16] Lifeng Zhou, Vishnu D Sharma, Qingbiao Li, Amanda Prorok, Alejandro Ribeiro, Pratap Tokekar, and Vijay Kumar. Graph neural networks for decentralized multi-robot submodular action selection. In 2022 IEEE International Symposium on Safety, Security, and Rescue Robotics (SSRR), 2022, accepted.
[17] Lifeng Zhou and Pratap Tokekar. Multi-robot coordination and planning: Recent trends. Current Robotics Reports, 2021. Invited.
[18] Lifeng Zhou, Vasileios Tzoumas, George Pappas, and Pratap Tokekar. Distributed attack-robust submodular maximization for multi-robot planning. IEEE Transactions on Robotics (TRO), 2022.
[19] Yang Zhoi, Jinliang Xiong, Yue Zhou, and Giuseppe Loianno. Multi-robot collaborative perception with graph neural networks. IEEE Robotics and Automation Letters, 7(2):2289–2296, 2022.