A metasurface composed of 3-bit coding linear polarization conversion elements and its application to RCS reduction of patch antenna

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In this paper, a metasurface composed of 3-bit coding linear polarization conversion elements and its application to RCS reduction of the patch antenna is intensively studied. At first, 3-bit coding metasurface are constructed by a sequence of eight coded unit cells, which have a similar cross-polarized reflected amplitude response and gradient reflected phase responses covering 0–2π, respectively. Equivalent circuit models of these unit cells are created to describe their electrical behavior for the two linear incident polarizations at the same time. Then, a patch antenna is integrated on the 3-bit metasurface, of which the elements are placed with a 2-dimensional linear coding sequence. The metal square ring is set around the patch antenna to protect it from the disturbance of metasurface. Both the simulation and experiment results demonstrate that the designed metasurface can primarily reduce the antenna RCS at a broadband, while the antenna performances are not degraded significantly.

The antenna is always one of the dominant scatters of a carrier¹. So it is essential to make antenna in low-observable or radio-transparent states in stealth and anti-stealth technology. Traditional RCS reduction approaches, including loading radar absorbing materials², shaping the antenna structure³, are not suitable for the general antenna due to the sacrifice of the radiation performances. In order to keep a better balance between the antenna performances and RCS reduction, the frequency selective surfaces (FSSs) are applied to reduce the RCS by controlling the energy that reaches the antenna⁴. Unfortunately, it cannot deal with the in-band RCS reduction.

With the development of metasurfaces, also called the two-dimensional version of metamaterials⁵, more attention is paid on the in-band RCS reduction of antennas by using metasurfaces to redirect the scattered energy. In⁶–⁸, various artificial magnetic conductors (AMCs) are placed in checkerboard arrangement to reduce the monostatic RCS based on the scattering cancellation. However, this kind of chessboard metasurfaces (CMs) suffers from the narrow band. The chessboard polarization conversion metasurfaces (PCMs) are used to expand the bandwidth of RCS reduction, in⁹–¹¹. Aside from the CMs, phase gradient metasurfaces (PGMs) are also utilized to reduce the RCS of antennas¹²,¹³, based on the generalized Snell-Descartes's law¹⁴. In¹⁵, a technique, which represents the generalized Snell-Descartes's law of reflection in the form of an array factor, is proposed and converges the two RCS-reduction methods: CMs and PGMs. Both the two methods would cause a sharp RCS increase in some directions, which is harmful for the invisibility of antennas under bistatic detection. Cui et al. proposed the concept of coding metamaterials¹⁶, which is very meaningful for realizing excellent scattering reductions because it simplifies the distributions of a set of artificially designed scatters in the form of coding sequences. This method makes a bridge between specific optimization algorithms and the required electromagnetic scattering effect¹⁷–¹⁹.

The cornerstone of coding metasurfaces is the design of multi-bits elements. Most multi-bits elements have similar amplitude responses and different phase responses. Moreover, they cannot change the polarization state

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of the electromagnetic wave. Linear polarization conversion phase gradient metasurfaces are introduced in 5, 20, which could provide polarization states as design freedom to multi-bits elements. Additionally, operation bandwidth of multi-bits elements is a pivotal characteristic. In 21, a thin metasurfaces made of single metallic layer, which can be used in anomalous reflections and refractions, possess an ultra-wide operation band from 9.3 to 32.5 GHz. To the best of our knowledge, there is a lack of the antenna combined with metasurfaces composed of multi-bits broadband linear polarization conversion elements.

In this paper, a metasurface composed of 3-bit coding linear polarization conversion elements and its application to RCS reduction of the patch antenna is intensively studied. Firstly, 3-bit coding metasurface are constructed by a linear phase sequence of eight unit cells. And, ECMs of these unit cells are built to describe their electrical behavior. Then, a patch antenna is integrated on the metasurface, of which the elements are placed with 2-dimensional linear coding sequence. At last, the antenna is fabricated and tested. Both the simulated and measured results indicate the proposed antenna has strong RCS reduction compared with the reference antenna over a wide frequency band, while its radiation performances are not obviously degraded.

3-bit coding unit cells and equivalent circuit model

The unit cell consists of a top metallic periodic structure, a dielectric layer (F4B, \( \varepsilon_r = 2.65, \tan \delta = 0.001 \)) with a height of \( h \) and a bottom metallic ground plane, as shown in Fig. 1a. The top metallic periodic structure is comprised of the long and short metallic arc wires, as well as the metallic disks. The structure has already been proved to achieve wideband polarization conversion22. Main resonances are excited by the long arc metallic wire and the metallic disk. Moreover, the change of the short arc wire parameters would produce small perturbations on the electromagnetic behavior of the structure, which is beneficial to get ideal cross-polarized reflected phase.

By changing some parameters, as shown in Table 1, four unit cells are introduced by numerical simulations to form nearly a \( \pi \) phase shift coverage for the cross-polarized reflected light. These unit cells are coded as 000, 001, 010, 011, as shown in Fig. 1b, which represent 0, \( -\pi/4 \), \( -\pi/2 \), \( -3\pi/4 \) cross-polarized reflected phase response, respectively. The same geometry parameters of these unit cells are as follows: \( px = py = 8 \) mm, \( r1 = r2 = 3.9 \) mm, \( w2 = 0.2 \) mm. Full-wave simulation is performed to investigate the reflection property of these unit cells by using CST microwave studio with periodic boundary conditions in x- and y- directions and open conditions along the z-direction. Polarization conversion ratio (PCR) is defined as:

![Figure 1. Configuration of 3-bit coding metasurface (a) The unit cell geometry; (b) 3-bit coding unit cells.](image-url)
where $r_{xx}$ or $r_{yy}$ represents the co-polarized reflection coefficient. $r_{yx}$ or $r_{xy}$ represents the cross-polarized reflection coefficient under x- or y-polarized incident wave. From Fig. 2a, it is found that the PCR of all unit cells is higher than 80% from 8 to 14 GHz under the incidence of the y-polarized wave. Moreover, their cross-polarized reflected phase responses are linear with the coding sequence and the phase difference between two adjacent coding unit cells keeps 45° during the same frequency band, as shown in Fig. 2b. The other four unit cells can be gotten by mirroring previous four unit cells along y-axis and noted as 100, 101, 110, 111, showing $-\pi$, $-5\pi/4$, $-3\pi/2$, $-7\pi/4$ cross-polarized reflected phase response and the same amplitude response as 000, 001, 010, 011, respectively.

To further understand the polarization conversion mechanism of these unit cells, we set up a four ports network according to the reference, as shown in Fig. 3a. $S_{11}$ or $S_{44}$ is defined as the co-polarized reflection coefficient, and $S_{41}$ or $S_{14}$ is defined as the cross-polarized reflection coefficient under the normal incidence of x- or y-polarized wave propagating along $-z$-axis, respectively. Due to the metallic ground sheet, port 2 and port 3 are loaded by conducting short. $Z_0$ is the impedance of free space ($Z_0 = 377 \Omega$). The F4B layer is equivalent to the transmission line with length $h$ and impedance $Z_r$. The top metallic structure can be described by connection quadripole in transmission parameters $T_c$, which is noted as:

\[
T_c = \begin{pmatrix}
A & B \\
C & D
\end{pmatrix} = \frac{2}{Y_u + Y_v}
\begin{pmatrix}
Y_u + Y_v & 0 \\
Y_u - Y_v & Y_u + Y_v
\end{pmatrix}
\begin{pmatrix}
Y_u - Y_v & 0 \\
2Y_uY_v & Y_u + Y_v
\end{pmatrix}
\begin{pmatrix}
Y_u - Y_v & 0 \\
Y_u - Y_v & Y_u + Y_v
\end{pmatrix}
\]

(2)

where $Y_u$ or $Y_v$ is the parallel admittance under the normal incidence of u- or v-polarized wave. The equivalent circuit of $T_c$ which must exhibit the architecture in Fig. 3b. According to the Foster representation and from the perspective of simplification, $Y_u$ can be seen as a capacitance $C_m$ in parallel with an inductance $L_v$, which is in series with a capacitance $C_v$. At the same time, $Y_v$ can be expanded in a similar condition in Fig. 3c. Compared with the ECM of cut wire, we add an extra capacitance because of the complexity of the designed structure. The ECMs of unit cells are set up and simulated using ADS software.

The final synthetic values of inductance and capacitance are as follows: for 000 element, $C_m = 8.01e-15$ F, $C_v = 3.37e-14$ F, $L_v = 6.06e-9$ H, $C_v = 1.28e-14$ F; for 001 element, $C_m = 3.49e-11$ F, $L_v = 5.92e-8$ H; for 001 element, $C_m = 3.00e-15$

Figure 2. Under y-polarized plane wave incidence, (a) simulated PCR of four polarized conversion unit cells; (b) simulated cross-polarized reflection phase of four polarization conversion unit cells.

Figure 3. (a) The ECM of the unit cell shown in Fig. 1. (b) Pi-representation of the connection quadripole; (c) Equivalent circuit of the unit cell for v-and u-polarized wave.
F, C_v = 4.16e−14 F, L_v = 5.78e−9 H, C_n = 3.26e−14 F, C_u = 3.49e−12 F, L_u = 2.55e−8 H; for 010 element, C_m = 2.40e−14 F, C_v = 5.79e−11 F, L_v = 5.53e−9 H, C_n = 1.88e−11 F, C_u = 4.50e−15 F, L_u = 5.97e−9 H; for 011 element, C_m = 1.20e−14 F, C_v = 6.83e−11 F, L_v = 7.15e−9 H, C_n = 3.05e−14 F, C_u = 1.60e−14 F, L_u = 7.30e−9 H. The Figs. 4 and 5 reveal that the simulation results of ECMs and CST are in a great agreement.

Application and simulation results in low-scatter patch antenna
Antenna structure. As shown in the right part of Fig. 6, a coaxial feed patch antenna is designed and its geometry parameters are as follows: L_p = 12.4 mm, W_p = 8.1 mm, d_f = 3.0 mm, h_p = 0.5 mm. According to the paper15, the coding elements are arranged in the 2-dimensional phase gradient sequence to achieve the best monostatic RCS reduction. So we combine the patch antenna and the phase gradient metasurface (128 × 128 mm) consisting of 3-bit coding linear polarization conversion elements, to form a low RCS antenna, which is noted as antenna I, as shown in the left part of Fig. 6. The patch antenna and metallic ground sheets of unit cell 000 and 001 are in the same horizontal plane. Thus, the antenna and metasurface share the F4B down layer with a thickness of 0.5 mm and the metallic groundsheet. The 4 × 4 unit cells above and around the patch antenna are removed and the metallic square ring (4 × 4 unit with 1.6 mm thickness and 4 mm height), is set around the patch antenna to protect antenna performance from the disturbance of metasurface. For reference, a patch antenna without the metasurface is denoted as antenna II.

Radiation characteristics. The simulated reflection coefficients, efficiency and radiation patterns of both antennas are shown in Fig. 7a–c, respectively. The Fig. 7a reveals that the antenna I operates around 10.0 GHz with −10 dB impedance bandwidth of 480 MHz. In comparison, antenna II works at around 10.5 GHz with poor impedance matching because the optimization of geometry parameters is done for the antenna I without considering antenna II. For reference, the antenna efficiency is simulated in Fig. 7b. It can be seen in the Fig. 7c that the beam width of antenna I is narrower than antenna II in both E- and H- planes. The gains of antenna I at 10 GHz and antenna II at 10.5 GHz are 8.20 dBi and 6.47 dBi, respectively. Compared with antenna II, the gain
enhancement of antenna I is attributed to the better impedance matching and increased antenna aperture due to the metasurface.

Scattering characteristics. Figure 8a,b shows the simulated monostatic RCS of both antennas for a normally impinging plane wave with x- and y-polarizations. Based on the simulated RCS results, we calculate the
RCS reduction of antenna I compared to the reference antenna, antenna II, as also shown in Fig. 8. It is evident that the average 10 dB RCS reduction bandwidth is from 8 to 14 GHz and the RCS reduction value at around 13 GHz is at least 20 dB for both polarizations. Actually, the energy is redirected to the other orientation and converted to the orthogonal polarization by the phase gradient metasurface composed of linear polarization conversion elements. Moreover, the antenna I can realize RCS reduction with different levels from 6 to 18 GHz. The 3-bit coded unit cells have different amplitude and phase responses out of the operating bandwidth (8–14 GHz), which make contributions to the diffuse of the electromagnetic wave and further expand the RCS reduction bandwidth.

In order to further illustrate the advantage of 3-bit coding phase gradient metasurface configuration over 1-bit chessboard metasurface embedded antenna in, polarization conversion unit cell of 000 were first arranged into 4 × 4 array, noted as array 0. Unit cell of 100 (the same reflection amplitude and phase difference of 180° with the unit cell of 000) is also arranged into 4 × 4 array, noted as array 1. The arrays 0 and 1 are arranged by chessboard, forming a chessboard arrangement metasurface based on polarization rotation unit as shown in Fig. 9a. As shown in Fig. 9b, it can be seen that chessboard PCM can greatly reduce the monostatic RCS under co-polarization waves, which is consistent with the paper. While under cross-polarized waves, there are four main lobes, which can be seen two in Fig. 9b. The four main lobe is symmetric distribution, located in the plane of $\phi = 45^\circ$, 135°. When 3-bit PCM is applied, shown in Fig. 9c, the direction of main lobe under co-polarized waves is still in the direction of $\theta = 0^\circ$, but its value has decreased by about 10 dB compared to the metal sheets, which is because most of the energy is converted to its cross-polarization direction. Compared with the 1-bit chessboard arrangement, the 3-bit phase gradient arrangement can reflect the energy of the incident wave to the abnormal direction, and the scattering pattern shows that there is only one main lobe ($\phi = 40^\circ$) under cross-polarization waves in Fig. 9d. Moreover, the energy of incident wave is converted to the other polarization direction, which have a better concealment effect for single-polarization radar. Compared with other phase gradient metasurface, the 3-bit coding metasurface designed in this paper can also achieve polarization conversion effect in the wide frequency range which can be applied into beam control.
Experimental verification

To validate the proposed design, the metasurface-patch antenna prototype is fabricated and its radiation performance is tested in a microwave anechoic chamber, as shown in Fig. 10a,b. Actually, the down layer of proposed antenna is too thin to retain its original shape in the experiment, so we adjust the parameters of the patch in simulation as follows: \( L_p = 12.2 \) mm, \( W_p = 7.8 \) mm, \( d_f = 2.8 \) mm. Besides, due to the thickness of soldering tin around the feed point on the patch in the experiment, the area between the upper and lower layers of F4B was filled with an air layer of 0.15 mm in the modeling of the CST simulation. Both measured and re-simulated reflection coefficients reveal that antenna I operates at 10.4 GHz with −10 dB impedance bandwidth extending from 10.24 to 10.68 GHz while antenna II at 10.9 GHz with a bad impedance matching in Fig. 11a. The measured gain of antenna I at 10.4 GHz is 7.07 dBi, while of antenna II at 10.9 GHz is 6.36 dBi, as shown in Fig. 11b. Figure 12 shows the normalized radiation patterns of both antennas. The measured results are consistent with those provided by the re-simulated results. We also test the scattering property of the fabricated prototype, as shown in Fig. 13a. Limited by the testing condition, the bistatic RCS cannot be measured at present and only monostatic RCS reduction can be obtained, which is shown in Fig. 13b. The slight change of the designed antenna structure has little impact on the monostatic RCS reduction. Both experiment and re-simulated results demonstrate that...
Figure 10. Experiment fabrication and test arrangement: (a) the top and bottom sides of two substrate layers of fabricated sample. (b) The experiment set up for the radiation pattern measurement of the fabricated patch antenna.

Figure 11. Results of radiation characteristics: (a) the measured and re-simulated reflection coefficients, and (b) gain versus frequency of the proposed antenna (antenna I) and reference antenna (antenna II).

Figure 12. The measured and re-simulated normalized radiation patterns (a) in the E-plane (xoz plane) and (b) H-plane (yoz plane) of antenna I at 10.4 GHz and antenna II at 10.9 GHz.
the proposed antenna could achieve a wideband RCS reduction from 6–18 GHz and an average 10 dB RCS reduction from 8–14 GHz.

**Conclusion**

In conclusion, we designed a metasurface composed of 3-bit coding linear polarization conversion elements. And in-depth research has conducted on its application in reducing the RCS of patch antennas. 8 unit cells are introduced by numerical simulations to form nearly 2π phase shift coverage for the cross-polarized reflected wave. Related ECMs of these unit cells are created simultaneously to describe their electrical behavior for the two linear incident polarizations. A patch antenna is integrated on the metasurface composed of the coded elements placed with a 2-dimensional linear coding sequence. Both simulation and experimental results show that the designed metasurface can significantly reduce the RCS of the antenna from 6 to 18 GHz. However, the performance of the antenna will not change significantly.

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Author contributions
X.K. and Q.W. conceived the original idea. Q.W. did the theoretical analysis and designed the metasurface. J.Y. and X.Y. fabricated the prototype metasurface. L.K. and S.J. performed the experiment. X.K. and X.Z. supervised the project. Q.W. and X.K. had deep discussion about this work and produced the manuscript, X.W. assisted in structure drawing.

Competing interests
The authors declare no competing interests.

Additional information
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