Efficiency of the leaf disc method for estimating the leaf area index of soybean plants

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ABSTRACT. The objective of this study was to evaluate the efficiency of the leaf disc method for estimating the leaf area index (LAI) of soybean plants in comparison with the digital photo method. A split-plot experimental design was used with three replications. The LAIs calculated by the leaf disc and digital photo methods were compared at four growth stages in four soybean cultivars (subplot). These soybean cultivars were sowed in Guarapuava, Paraná State, Brazil, at three different sowing dates (main plot) in the 2010/2011 growing season. Regression analysis was used for each group of samples, and the efficiency of the leaf disc method was evaluated on the basis of the coefficient of determination (R²), the calculated F and the intersection and abscissa errors. The regression analysis that compared the two methods resulted in highly significant F values and low errors for all sample groups, which showed the effectiveness of the leaf disc method. Although the R² value was high for all of the analyses, the values were minor for the separate growth stage analysis, especially for the samples collected at the V9 and R2 stages. The results indicated that the specific leaf area calculated by the leaf disc method was lesser to the specific leaf area calculated by the digital photo method. The leaf disc method is an efficient and robust method for estimating the LAI of soybean plants.

Keywords: Glycine max, cultivars, digital photos, growth stages, sowing dates.

Introduction

The leaf area (LA) of a plant culture is related to its growth (PEKSEN, 2007) and can indicate crop yield (FAVARIN et al., 2002). It is important to determine the capacity of plants to synthesize and translocate photoassimilates to several organs (FONTES et al., 2005).

In studies that involve seeding density, fertilization, irrigation, pruning or pesticides application (among other treatments), the leaf area index (LAI) is required to manage crop growth and to serve as a basis for plant growth analysis (FAVARIN et al., 2002; DAMMER et al., 2008; TAVARES JÚNIOR et al., 2002).

There are several measurement methods that are used for estimating crop LA (KUMAR, 2009). However, faster, cheaper and more accurate LAI measurement methods that can be used in the field and laboratory are needed. One conventional method that is used is the digital photo method, which has accuracy comparable with that of the optical leaf
counting method (for example, leaf area integrator, ADAMI et al., 2008), the primary method for LA measurements. However, the digital photo method requires the software uses photo edition, which is time consuming and can cause errors (JONCKHEERE et al., 2004). According to Tavares Júnior et al. (2002), who studied coffee plants, the leaf disc area method has a higher standard error than the digital photo method, but the leaf disc area method is simpler and faster.

In soybean (Glycine max (L.) Merrill) plants, parameters such as the crop growth rate and net assimilation rate depend on the LAI of the plants and can be used to explain an increase in the number of pods (ISODA et al., 2010). The growth and yield of soybean plants can be explained by the LAI before the pod filling period and by the net assimilation rate after the vegetative period (ISODA et al., 2010). The LAI is highly correlated with yield, it is important for calculating growth parameter for different cultivars, environments and growth stages. This way, the use of a simple and practical LAI prediction method, such as the leaf disc method, is of interest for researchers, growers and agronomists. However, it is necessary to verify the efficiency of the LAI prediction method for different field conditions.

This study tests the hypothesis that there is no difference between the digital photo and leaf disc estimation methods of the LA. The objective of this study was to evaluate the efficiency of the leaf disc method in comparison with the standard digital photo method for estimating LAI in soybean plants. This efficiency was evaluated in different environments, for different cultivars and at different phenological growth stages.

Material and methods

The experiment was conducted in Guarapuava city, in the state of Paraná, Brazil, which is at a latitude of 25°23'36" S, a longitude of 51°27'19" W and an altitude of 1,120 m. The 2010/2011 crop season was tested. According to the Köppen classification system, the regional climate is altitude seasoned - Cfb (KOTTEK et al., 2006). A split plot experimental design was used with three replications (blocks). The main plots consisted of three sowing dates in 2010 (21/10, 18/11 and 20/12), and the subplots consisted of four cultivars (BMX Apolo® RR, BRS 284®, BMY Energia® RR and FPS Urano® RR). The subplots had four rows that were 11 m long and 0.4 m apart. The sowing rate was 20 seeds meter⁻¹, which resulted in a total population of 500,000 seeds ha⁻¹. For all cultivars, the plants were thinned during the VE (FEHR; CAVINESS, 1977) stage to achieve a final population of 260,000 plants ha⁻¹.

The LAI was estimated by the following methods

The digital photo method. Random samples of approximately 1,000 cm² of leaves were extended with the assistance of a glass and were photographed with a scale of known dimensions to measure the LA with the Image-J® software (ABRAMOFF et al., 2004). To determine the specific leaf area (SLA, cm² g⁻¹), the photographed samples were dried in a forced aeration oven at 70°C until a constant mass was achieved. This method was used as a standard experimental method. According to Adami et al. (2008), this method provides excellent LA measurements with a level of precision similar to that of LA integrator equipment.

The LAI was calculated by using the following formula:

\[ \text{LAI}_{\text{photos}} = \frac{\text{DMt} \times (\text{SLA})}{\text{SA}} \times 10,000 \]

where:

- LAI photos = Leaf area index, calculated by digital photo method;
- DMt = Total dry matter of the leaves (g);
- SLA = Specific leaf area (cm² g⁻¹); and
- SA = Soil surface area (m²).

The leaf disc method. The leaf discs were obtained with a puncher of known area (2.66 cm²) using the method described by Brandelero et al. (2002), Benincasa (2003) and Lima et al. (2007). This method was compared with the standard method. Each leaf was perforated once in the center, including the central nervure. Ten leaves were chosen randomly from each plot. The leaf discs were dried in a forced aeration oven at 70°C until a constant mass was achieved. This mass was used for determining the SLA and the posterior LAI with the following formula:
The FPS Urano® RR cultivar was used as a reference to determine the phenological growth stage. When the FPS Urano® RR cultivar achieved one of the different phenological growth stages (V4, V9, R2 and R5.3), the FPS Urano® RR cultivar was used as a reference to determine the phenological growth stage. When the FPS Urano® RR cultivar achieved one of the four cited stages, all four cultivars were sampled. A 0.4 m boarder was left between each sampling stage.

Between the two methods, the plant stages, cultivars, the sowing date and all parameters were compared. The F regression (p-value < 0.01) was used to compare the results. The determination coefficient ($R^2$), the angular coefficient of regression and the intersection and abscissa errors were compared. The average SLA’s from the two methods were compared with a t-test.

### Results and discussion

Table 1 presents the calculated F, the significance, and the regression error values for the digital photo and leaf disc methods for all analysis groups.

#### Table 1. The calculated F values, the significance of F and the intersection and abscissa errors of the regression analyses between the digital photo and leaf disc methods for leaf area estimates in soybean plants. Samples were collected during four growing stages, at three sowing dates and for four cultivars in the 2010/2011 growing season in Guarapuava, Paraná State.

| Samplings | Calculated F | Significance F | Intersection error | Abscissa error |
|-----------|--------------|----------------|--------------------|---------------|
| V4        | 276.0        | 6.9E-18        | 0.032              | 0.044         |
| V9        | 105.8        | 5.7E-12        | 0.234              | 0.093         |
| R2        | 135.0        | 2.19E-13       | 0.402              | 0.092         |
| R5.2      | 236.4        | 7.1E-17        | 0.228              | 0.046         |
| EP1       | 561.0        | 2.06E-27       | 0.159              | 0.037         |
| EP2       | 1193.9       | 1.89E-34       | 0.090              | 0.026         |
| EP3       | 834.9        | 3.89E-31       | 0.092              | 0.033         |
| Apolo     | 824.3        | 2.10E-25       | 0.102              | 0.032         |
| BRS 284   | 101.1        | 6.30E-22       | 0.145              | 0.038         |
| Urano     | 242.8        | 1.80E-22       | 0.151              | 0.040         |
| General   | 2322.7       | 6.85E-09       | 0.068              | 0.019         |

The calculated F value was highly significant, and the regression errors were small for all analyses. Thus, the leaf disc method reliably and efficiently estimates the digital photo method results. In a study of Crambe abyssinica, Toebe et al. (2010) verified the correlation between the leaf disc and the digital photo methods, corresponding to the results of the present soybean plant study.

The SLA estimated by the leaf disc method was smaller than that estimated by the digital photo method (except for estimates during the V9 and R2 stages) (Table 2). This difference was probably results from the consistent collection of the central nervures in the leaf disc method, which decreases the SLA in comparison to the digital SLA photos. The coefficient of variation (CV) of the leaf disc method was similar to that of the digital photo method, which suggests that the precision of both methods is similar.

#### Table 2. Specific leaf area (SLA, cm² g⁻¹) and coefficient of variation (CV) of soybean plant estimates by the digital photo method (photos) and the leaf disc method (discs). Samples were collected at four growth stages, for four soybean cultivars and at three different sowing dates in the 2010/2011 growing season in Guarapuava, Paraná State.

| Samplings | t values | SLA (cm² g⁻¹) | Photos CV | Discs CV |
|-----------|----------|---------------|-----------|----------|
| V4        | 3.76E-11*| 279.9         | 14.8      | 260.9    |
| V9        | 7.26E-04*| 275.3         | 10.5      | 257.3    |
| R2        | 2.57E-05*| 265.4         | 10.5      | 241.9    |
| R5.2      | 1.07E-14*| 244.5         | 14.4      | 213.5    |
| EP1       | 1.90E-03*| 277.3         | 20.1      | 258.3    |
| EP2       | 3.02E-05*| 287.2         | 13.6      | 268.9    |
| EP3       | 2.34E-05*| 275.3         | 7.8       | 253.0    |
| Apolo     | 1.67E-05*| 282.2         | 14.3      | 256.2    |
| BRS 284   | 7.26E-04*| 275.3         | 10.5      | 257.3    |
| Energia   | 9.96E-03*| 292.4         | 19.0      | 271.6    |
| Urano     | 3.76E-11*| 277.3         | 20.1      | 258.3    |
| General   | 3.76E-11*| 265.4         | 10.5      | 241.9    |

* and **: The SLA results from the digital photo and leaf disc methods were or were not different, respectively, as determined by a t-test with a 5% probability level.

A high correlation was found between the digital photo and leaf disc methods at different culture growth stages, particularly during the first (V4) and last (R5.3) growth stages (Figure 1).

#### Figure 1. Relationship between leaf area index (LAI) estimated by the digital photo method (photos) and the leaf disc method (discs), at four growth stages, (a) V4, (b) V9, (c) R2 and (d) R5.3, in the 2010/2011 growing season in Guarapuava, Paraná State. ***: Statistically significant at 0.1%.
The second and third samplings (Figure 1b and 1c, respectively) that were conducted during the V9 and R2 stages had the smallest R² values. However, the significant F value from the regression analysis (Table 1) shows that the leaf disc method is highly efficient for estimating the LAI.

By comparing the LAI estimations between the two methods, a subestimation of the LAI is obtained from the leaf disc method. In contrast to the results obtained by Tavares Júnior et al. (2002) and Dombroski et al. (2010), who compared the digital scanner method with the leaf disc method, we concluded that the LA was overestimated in the leaf disc method. Dombroski et al. (2010), working with a pine cone culture, used a correction factor (0.894) to balance the overestimation of LA by the leaf disc method. In a study that used *Chrysobalanus icaco*, Cunha et al. (2010) found a high coefficient of determination (R² = 0.978) and a high angular coefficient (0.994) between the digital scanner and the leaf disc methods. However, to reduce errors due to sampling and variation that occurred between the leaves, the authors emphasize that a LA correction factor is necessary for measurements made with the leaf disc method.

The discrepancy between the leaf disc method LAI results in the present study and those from other studies likely results from the fact that other researches avoided the perforated central leaf area. Thus, the central nervure was excluded from sampling. The smaller SLA value for the leaf disc method in comparison to the digital photo method explains why the angular coefficient is below 1. In addition, this finding partially clarifies the differences between the present and past research results. The underestimation of LA in the present study is proportional to or smaller than the overestimation that was observed in other studies, such as those by Dombroski et al. (2010), Marrocos et al. (2010) and Lucena et al. (2011).

In a comparison between the leaf disc method and the digital scanner analysis method in beet plants, Marrocos et al. (2010) obtained a result of R² = 0.87. The authors suggest that this result occurred because the leaves were not always perforated in the same place, which increased the SLA variability and error and decreased the R² value. Lucena et al. (2011) compared different LA measurement methods in acerola plants and obtained the smallest R² value (0.859) with the leaf disc method. This finding was hypothesized to result from the high SLA variability of the acerola plants. Specifically, the plasticity within the plant differed depending on the plant age, the canopy position and the leaf adaptation to light microenvironments. Nevertheless, the authors concluded that the leaf disc method was efficient for measuring the LA of acerola plants.

It could be suggested that the branching and uneven leaf development during the V9 and R2 stages was responsible for reduced sampling efficacy and the relatively low observed R² during the V4 and R5.3 stages. However, this hypothesis is not supported by the similar CVs for the observed SLAs at each sampling date (Table 2).

Lopes et al. (2007) determined that the highest accuracy of digital photo LA estimations occurred during the phenological growth stages. In this study, the authors only used one cultivar and only sampled at one date of plant development. However, as observed in this study, mixing cultivars and sowing dates for estimating LA at different growth stages probability decreased the resulting R². Therefore, we suggest that the LA analysis of soybean plants should be conducted separately for different cultivars or sowing dates within each growth stage to estimate the LA of different cultivars at different sowing dates and growth stages.

Monteiro et al. (2005) worked with cotton plants and reported that morphological uniformity of the leaves within and between plants is important. They mention that the estimation of LA by the length of leaves also depends on leaf uniformity. Therefore, the sampling performed without standards can increase the sample error. In this study, the inclusion of the central nervure proved to be an effective method for reducing variability and increasing the estimation efficiency.

In the curve fits of each of the cultivars (Figure 2), the leaf disc method had a robust estimation and a R² of between 93 and 96% among the cultivars.

![Figure 2. Relationship between leaf area index (LAI) estimated by the digital photo method (photos) and by the leaf disc method (discs) in four soybean cultivars, including (a) BMX Apolo® RR, (b) BRS 284®, (c) BMX Energia® RR and (d) FPS Urano® RR in the 2010/2011 growing season in Guarapuava, Paraná State. ***: Statistically significant at 0.1%.](image)
Thus, the significant F and the intersection and the abscissa errors were similar for all cultivars (Table 1). The estimated LA regressions for the cultivars in this work had higher $R^2$ values than those obtained by Lucena et al. (2011) and by Marrocos et al. (2010). In a study that calibrated the LA method for leaf sizes in chestnut plants, Serdar and Demirsoy (2006) observed that no differences occurred among genotypes, which agrees with the results of this study. Therefore, it is suggested that the leaf disc method is also highly accurate for estimating the LA of soybean cultivars that were not used in the present study (such as BMX Apolo® RR, BRS 284, BMX Energia® RR and FPS Urano® RR) when it is used during the entire culture life cycle. Soybean cultivars are generally compared with many genotypes, which results in multiple plots. The leaf disc method is fast, easy and accurate, which are important advantages for LAI estimations in such studies.

Similar results are presented in Figure 3, which compares the two methods across sowing dates. In this case, the leaf disc method was also efficient. However, the intersection error of the first sowing date is higher than the others sowing dates (Table 1). This difference was probably caused by the higher LAI in the plants from the first sowing date relative to the later sowing dates. Thus, it is suggested that it is necessary to sample a larger number of leaf discs when the LAI of soybean plants is high (for example, more than 10) to obtain high accurate results.

Estimating the LA with the leaf disc method for different sowing dates was efficient and accurate, as indicated by the high $R^2$ (Figure 3). However, Isoda et al. (2010) observed high variation in the LAI across sowing dates and different environmental conditions. Once that the sowing dates of the present study include the typical regional soybean sowing dates and the variations in the environmental conditions that are faced by the soybean plants, the equations in the Figure 3 can be used to estimate the LAI of the soybean plants in south-central Brazil with high precision.

The leaf disc method for estimating the LAI can be done according to the growth stages of the soybean crop. However, when conducted in this manner, the $R^2$ values were smaller than when they were conducted according to cultivars or by sowing dates. Thus, it is preferable that the LA estimations by the leaf disc method are conducted separately according to cultivar or sowing date. This finding is important for researchers and for growers who cultivate several cultivars and/or plant them at different times. In addition, using the leaf disc method resulted in high LA estimations across the various sampling stages (Figure 1), cultivars (Figure 2) and sowing dates (Figure 3). This result demonstrates the robustness and validity of the leaf disc method.

Figure 4 shows the relationship between the LAI values that were determined by either the digital photo method or the leaf disc method for all of the studied samples. The coefficient of determination for this correlation was high ($R^2 = 0.940$), which demonstrated the general efficiency of the leaf disc method. In addition, a highly significant F value and a small error (Table 1) occurred as a result of the large sample number.

Therefore, the leaf disc method can be used to estimate soybean plant LA by using a correction factor of 1.082, ($x = 1.082 \times y$) when the LAI estimation is not performed separately for growth stage, cultivar or sowing date.
Conclusion

Estimating the leaf area index in soybean plants with the leaf disc method by perforating the central nerved of the leaves resulted in a high coefficient of determination (R²) in comparison with the traditional method. The leaf disc method is a fast, easily applied and reliable method with small errors and coefficients of variation. Thus, the leaf disc method is an efficient method for estimating soybean leaf area in different evaluation situations.

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Received on March 7, 2012.  
Accepted on July 17, 2012.

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