THE GraS HYPOTHESIS: A MODEL FOR DARK MATTER-BARYONS GRAVITATIONAL INTERACTION

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Abstract. According to the gravitational suppression (GraS) hypothesis the gravitational interaction between exotic (dark) and standard (visible) matter is suppressed below the kpc scales. We review the phenomenological motivations at the basis of this idea and its formal implementation by means of a Yukawa contribution to the usual Newtonian potential. We also discuss a class of astrophysical phenomena that may help in testing this scenario.

1 Introduction

The success of the cold dark matter (CDM) paradigm in explaining a wide range of properties of the visible structures on scales $\geq 1$ Mpc \cite{1, 2} does not extend down to sub-galactic scales. Some inconsistencies between observations and theory (via simulations) still lack a satisfactory interpretation, indeed a possible scenario of “CDM crisis” on small galactic scales has been evocated \cite{3}.

One issue is that, high-resolution observations of the inner rotation curves of low-surface brightness (LSB) galaxies suggest that the dark matter is distributed in spherical halos with nearly constant density cores \cite{4, 5, 6}, whereas DM simulations systematically predict much steeper density profiles $\rho \sim r^{-\beta}$ with $\beta \sim 1-1.5$ (see, e.g. \cite{7, 8, 9}). It now seems that the cuspy density profile of halos that form in simulations of the dark matter component is a robust and reproducible feature of the collisionless dynamics of halo formation (e.g., \cite{10}), and, as a matter of fact, steep profiles consistent with the simulations have recently been “seen” through gravitational lensing at the center of galaxy clusters \cite{11}. A parallel problem is that a scale-invariant primordial spectrum of perturbations generates significantly more virialized objects of dwarf-galaxy mass than are observed around the Milky Way \cite{12, 13, 14}. Again, preliminary observations of multiple image gravitational lenses \cite{15} seem to confirm the presence of these mass substructures, thus indicating that a possible solution to this problem may be found in some mechanism that prevents star formation in most of the low mass galactic satellites. Intriguingly enough, these problems appear to be characterized by the same physical scale length of the order of the kiloparsec.

It is known that, in order to have efficient structure formation, dark matter (DM) must be sufficiently decoupled from the Standard Model particles. As a consequence, the direct detection of DM is (and is proving to be \cite{16}) a difficult task. Moreover, DM properties must be inferred from the dynamic and distribution of the visible component, which in turn are affected and shaped by DM only through gravitation. In what follows we review the recently proposed \cite{17} gravitational suppression (GraS) hypothesis which addresses the above mentioned kpc-scale problems via a modification of the gravitational law between DM and baryons. Of course, the theoretical framework of four dimensional General Relativity hardly accomplishes departures from the Newton law, unless other light field-mediated forces are introduced. Nevertheless, from an empirical stand point, a modification of gravity may be considered as a “minimal” attempt to solve the above mentioned inconsistencies between observations and theory, since it’s just and only gravity that rules the reciprocal behavior of baryons and DM. In other terms we do not add or modify hypothetical properties of DM particles (e.g., \cite{18, 19}) but, applying "Occam razor", we suggest a modification of a measurable phenomenon whose general consequences are directly testable and falsifiable.

As recalled by Tremaine \cite{20}, there have been two major observational issues in the solar system since 1800: the unexplained residuals in the orbit of Uranus that led to the discovery of Neptune, and the anomalous precession of Mercury perihelion that was explained by General Relativity. The
Figure 1: A schematic representation of the GraS hypothesis: the suppression of gravity on kpc scales is active only between “dark” and “visible” particles. The Newtonian dynamics inside each of the two sector is untouched.

large scale issue was explained by the discovery of new matter and the small scale anomaly by a radical new physical law. In analogy, the dynamics of spiral galaxies at large radii has lead to the discover of dark matter, while the inner rotational behavior of low surface brightness (LSB) galaxies may contain a hint of fundamental new physics. We leave speculations about the theoretical origin of such a proposed modification to future work. At present we adopt an instrumentalist view and try to asses the performances of GraS as a working hypothesis.

2 The Gravitational Suppression Hypothesis

The GraS hypothesis has been formulated in [17] as follows: In the Newtonian limit of approximation (small curvatures and small velocities in Planck units), the gravitational interaction between baryonic and non baryonic particles is suppressed on small (∼ kpc) scales. The picture is very simple and schematically represented in Fig. 1: nothing changes in each of the two sectors (visible-dark) with respect to Newtonian gravity but, as two particles (one “dark” and one “visible”) get closer than a kpc to each other, they experience a suppression of the usual gravitational Newton law.

In order to model a general small scale modification of gravity we have used a Yukawa-type correction to the usual 1/r law. The resulting gravitational potential between two point-like particles of different nature goes like

\[ \phi(r) \propto -\frac{1}{r}(1 + \alpha e^{-r/\lambda}), \]

where r is the distance between the two particles. The parameter \( \alpha \) gives the strength and the type (repulsive or attractive) of the Yukawa contribution. As \( \alpha \) gets close to −1 the total gravitational interaction tends to be totally suppressed in the small scale limit. The length \( \lambda \), on the other hand, gives the typical scales over which such a suppression is effective. Accidentally, we note that the same kind of interaction is generated by a light scalar mediated force. However, a universal scalar interaction cannot be active only in the mixed sector without affecting also the dynamics internal to each sector.

3 Fitting the parameters

Low surface brightness (LSB) galaxies are very good laboratories to test our model. Since they are dominated by dark matter [21] we can neglect the dynamical contribution of the disc to the velocity
rotation curves. Moreover, since GraS doesn’t change the usual Newton law between DM particles, the general predictions of numerical simulations concerning the density profiles of DM halos hold. In particular, we expect inner power-law cusps of the type $\rho \sim r^{-\beta}$ with $\beta \sim 1.1-1.5$ [7, 8, 9]. In [17] the velocity rotation curve generated by a power-law density profile of generic slope $\beta$ has been calculated within the framework of the Yukawa model of equation (1). Such a theoretical curve has been compared to a sample of high resolution LSB rotation curves measured and reduced by different authors [5, 6, 22, 23] in order to fix the universal parameters of our model, $\alpha$ and $\lambda$, and to find the best value $\beta$ of the internal slope consistent with the GraS hypothesis (see Fig. 1 in [17]).

The value of $\alpha$ ($\alpha = -1.0 \pm 0.1$) is remarkably stable in all the galaxies considered and seems to point towards a total suppression scenario where the gravitational attraction between two particles of different nature is really “cut-off” at small distances. The characteristic scale below which the suppression mechanism is active is constrained to be $\lambda = 1.1 \pm 0.08$ kpc. Finally, the inner density slope, $\beta = 1.35 \pm 0.05$, is in good agreement with the simulations [7, 8, 9] and in particular with some recent high-precision ones which seem to indicate the value $\beta = 1.2$ [10]. The rotational velocity predicted by such a set of universal parameters has been superimposed in Fig. 2. to the observed velocity curve of a new LSB galaxy [5] for which sufficiently high resolution inner rotation data (but unfortunately large observational errors for a meaningful fit) are available.

4 GraS: Predictions

GraS provides a cosmological mechanism that segregates the fraction of baryons in halos of different mass sizes. The reason is rather intuitive: small mass halos of sizes up to a kpc are much less effective
in attracting the cosmologically diffused baryons. It may be worth noting that dwarf galaxies of $10^9$ $M_\odot$ typically grew out of fluctuations which, at decoupling, were not larger than $10^{-1}$ kpc. In [17] this effect has been calculated at linear order in perturbation theory considering the baryon fraction

$$f = \frac{\rho_B}{\rho_D} = \left(\frac{\Omega_B}{\Omega_D}\right) \frac{1 + \delta_B}{1 + \delta_D}$$

at the epoch of turnaround. As a result, the baryon fraction in halos of $10^6$ solar masses is about half the average cosmological value $\Omega_B/\Omega_D$ (see Fig. 3). This linear approach, however, is likely to underestimate the GraS effects. At turnaround, in fact, where the linear theory approximation still holds, $\delta_D \simeq 1.1$ and, even for completely frozen baryonic fluctuations $\delta_B \simeq 0$, the fraction on the RHS of (2) cannot be lower than about 1/2. As a consequence galaxy formation is not 100% efficient in trapping baryons inside small halos, and a relevant fraction of the total baryonic budget should consist of cool baryonic clouds outside virialized structures. It is tempting to speculate on how this mechanisms may help in interpreting the fact that part of the baryons expected in standard nucleosynthesis models are yet undetected in the present day universe.

Moreover, loosening the tight coupling between baryons and exotic particles, other complementary astrophysical mechanisms such as Supernovae feedback and photoionization may become more effective in preventing star formation. For instance, the GraS predicted binding energy of baryons in halos of $10^8$ solar masses is about a factor of one tenth less than predicted by Newtonian gravity. A more realistic picture of gas/star density distribution and evolution in small galaxies could be obtained by implementing GraS non-linear, non-gravitational dynamical effects into high resolution hydrodynamical simulations.

Simulations may also help in assessing the effect of GraS on the dynamical coupling between the stellar bars in galaxy discs and the surrounding dark matter halo and the subsequent evolution of both components. One may speculate that the apparent absence of slow bars in galaxies is due to a suppression of the dynamical friction between the baryons and CDM particles and thus to a less effective transfer of angular momentum between the bar and halo components.

In summary we have argued that the severe challenges facing DM models may indicate that a serious examination of the way baryons respond to a dark matter potential on small scales should be considered.
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