A New Graphical Method to Diagnose the Impacts of Model Changes on Climate Sensitivity

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Abstract

Equilibrium climate sensitivity (ECS) is defined as the change in the global mean surface air temperature due to the doubling or quadrupling of CO$_2$ in a climate model simulation. This metric is used to determine the uncertainty in future climate projections, and therefore, the impact of model changes on ECS is of large interest to the climate modeling community. In this paper, we propose a new graphical method, which is an extension of Gregory’s linear regression method, to represent the impact of model changes on ECS, climate forcing, and climate feedbacks in a single diagram. Using this visualization method, one can (a) quantify whether the model or process change amplifies, reduces, or has no impact on global warming, (b) evaluate the percentage changes in ECS, climate forcing, and climate feedbacks, and (c) quantify the ranges of the uncertainties in the estimated changes. We demonstrate this method using an example of climate sensitivity simulations with and without interactive chemistry. This method can be useful for multimodel assessments where the response of multiple models for the same model experiment (e.g., usage of interactive chemistry compared with the prescribed chemistry as shown here) can be assessed simultaneously, which is otherwise difficult to compare and comprehend. We also...
demonstrate how this method can be used to examine the spread in ECS, climate forcing, and climate feedbacks with respect to the multimodel mean (or one benchmark model) for multimodel frameworks such as Coupled Model Intercomparison Project Phase 5 or for different ensemble members in a large ensemble of simulations conducted using a single model.

**Keywords** new graphical method; climate sensitivity; interactive chemistry; climate forcing and climate feedbacks; multimodel assessments

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1. Introduction

The Earth’s climate is sensitive to the concentrations of greenhouse gases (GHGs) in the atmosphere. The concentrations of GHGs have a large impact on radiative forcing and surface climate change. One widely used metric to estimate this impact is equilibrium climate sensitivity (ECS). ECS, which is defined as the response of global and annual mean surface air temperatures to a change in GHG concentrations, can be calculated using an idealized long-period climate simulation in which atmospheric CO₂ concentration is instantaneously doubled (2 × CO₂) or quadrupled (4 × CO₂) from the pre-industrial (PI) level. Climate sensitivity is also used as a measure of uncertainty for the assessment of future projections in similarly forced general circulation models (GCMs) or Earth system models (ESMs). A wide range of climate sensitivity across models would imply a lower confidence in future projections, and thus, continuous efforts are being made to determine and understand the factors on which the climate sensitivity depends in models.

Recent research shows that using interactive chemistry instead of prescribed values, as done in Coupled Model Intercomparison Project Phase 5 (CMIP5), can impact surface climate and estimates of ECS in climate models (e.g., Chiodo et al. 2016; Dietmüller et al. 2014; Marsh et al. 2016; Muthers et al. 2014; Nowack et al. 2015, 2017, 2018). Nowack et al. (2015), using the UK Met Office chemistry-climate model, showed that the global mean surface warming is reduced by ~1 K (~20 %) when the model computes the chemistry processes interactively instead of using prescribed values at PI levels. In contrast to this, Marsh et al. (2016) showed no large impacts of interactive chemistry on the climate sensitivity in the Community Earth System Model–Whole Atmosphere Community Climate Model.

To evaluate the response of surface climate to the imposed forcing (doubling or quadrupling of CO₂), these studies used the following linear energy balance equation introduced by Gregory et al. (2004) and used by others (Aldrin et al. 2012; Andrew et al. 2012; Annan and Hargreaves 2006; Dessler and Forster 2018; Lewis and Curry 2015; Otto et al. 2013; Skeie et al. 2014):

\[ N(t) = F + \alpha \Delta T(t), \]

where \( t \) is time (annual mean), \( N(t) \) is the net radiative flux (W m⁻²) at the top of the atmosphere (TOA), \( F \) is the imposed forcing (W m⁻²), \( \alpha \) is the climate feedback parameter (W m⁻² K⁻¹), and \( \Delta T(t) \) is the global mean surface air temperature change (K). Equation (1) is linear, and therefore, \( F \) can be estimated by the y-axis intercept and \( \alpha \) by the slope of the line of best fit from the scatter plot of \( \Delta T(t) \) versus \( N(t) \). ECS is defined as the global mean surface air temperature change \( \Delta T \) in response to abrupt 2 × CO₂ or 4 × CO₂ experiments (Andrews et al. 2012) under the limit of time \( t \) tending to very large values (generally hundreds of years for atmosphere-ocean coupled GCMs). It is a convenient metric for quantifying the joint effect of climate forcing and climate feedbacks under the implicit assumption of \( N \) approaching zero. ECS is given as \(-F/\alpha\) in a 2 × CO₂ experiment, whereas it is \(-F/(2\alpha)\) in a 4 × CO₂ experiment.

Although the information that is provided in the climate sensitivity studies is of extreme importance for future climate change assessments, the results presented in these papers can be challenging to comprehend unless accompanied by a detailed textual description. These studies also emphasize the need for multimodel assessments in which each model’s response to the interactive chemistry should be compared with its prescribed chemistry simulation and also with the results of other models for the same experiment. However, in that case, the intercomparison of the myriad of results will be complex. To overcome this, we propose...
a new graphical method in which information that is typically presented in the form of text and tables can be summarized and collated in one single diagram.

One of the applications of this method is for multi-model assessments in which the impact of model or process change on ECS, climate forcing, and climate feedbacks can be simultaneously diagnosed for multiple models. Using the proposed method, each model can be represented by its own marker with standard error intervals in a single diagram, which simplifies the intercomparison of multiple models for the same experimental framework (e.g., using interactive chemistry instead of prescribed values in each model). In this paper, we demonstrate this method using the example of climate sensitivity simulations with interactive and prescribed chemistry, conducted using Japan Meteorological Agency–Meteorological Research Institute (JMA-MRI) Earth System and coupled atmosphere-ocean models. We also show how this method can be used to estimate the spread in ECS, climate forcing, and climate feedbacks for multiple models with respect to the multimodel mean (MMM) or a benchmark model, using CMIP5/6 or other data. This method can also be used to estimate the spread or change in the same experimental framework (e.g., using interactive chemistry instead of prescribed values in each model).

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the initial transient response to the abrupt quadrupling of CO₂. Note that the % change in ECS in the expt simulation with respect to ctrl simulation is given as 

\[ \frac{R_f}{R_c} - 1 \times 100. \]

Equation (7) leads to five possible scenarios (Cases 0 to IV) as follows:

Case 0: \( R_f = R_c \) and \( \Delta T_{sw} = 0 \), represents the case that the impact of the experiment on the global mean surface air temperature, i.e., ECS, is zero.

Case I: \( R_f > R_c \) and \( \Delta T_{sw} > 0 \), represents the case of global warming as \( \Delta T_{sw} > 0 \), and the warming is amplified.

Case II: \( R_f > R_c \) and \( \Delta T_{sw} < 0 \), represents the case of global cooling as \( \Delta T_{sw} < 0 \), and the cooling is amplified.

Case III: \( R_f < R_c \) and \( \Delta T_{sw} > 0 \), represents the case of global warming as \( \Delta T_{sw} > 0 \), and the warming is reduced.

Case IV: \( R_f < R_c \) and \( \Delta T_{sw} < 0 \), represents the case of global cooling as \( \Delta T_{sw} < 0 \), and the cooling is reduced.

### 2.3 Uncertainty in feedback parameter, forcing, and their ratios

Given that the relationship between \( \Delta N_i(t) \) and \( \Delta T_i(t) \) is not entirely linear in a model simulation, there will be associated uncertainties in \( \alpha_i \) and \( F_i \) that are estimated using linear regression. The possible values for \( \alpha_i \) are given by \( \alpha_i \pm E_{\alpha,i} \), and \( F_i \) by \( F_i \pm E_{F,i} \), where \( E_{\alpha,i} \) and \( E_{F,i} \) are the uncertainties in \( \alpha_i \) and \( F_i \), respectively. The uncertainties (or the standard errors), \( E_{\alpha} \) and \( E_{F} \), are given as follows (e.g., Montgomery et al. 2012):

\[
E_{\alpha,i}^2 = \sigma_i^2 \frac{I}{\sum_{i=1}^{I} (\Delta T_{i})^2 - (\sum_{i=1}^{I} \Delta T_{i})^2},
\]

\[
E_{F,i}^2 = \sigma_i^2 \frac{1}{\sum_{i=1}^{I} (\Delta T_{i})^2 - (\sum_{i=1}^{I} \Delta T_{i})^2},
\]

where \( i \) is a sequential integer for each year and \( I \) is the total number of years used for the linear regression, and \( \sigma_i \) is given as

\[
\sigma_i^2 = \frac{\sum_{i=1}^{I} (\Delta N_{i} - \alpha_i \Delta T_{i})^2}{I - 2}.
\]

The uncertainties \( E_{\alpha,i} \) and \( E_{F,i} \) are obtained for both ctrl and expt simulations. The magnitudes of uncertainty for the ratios \( R_a \) and \( R_f \) are also obtained using the law of propagation of errors (e.g., Bohm and Zech 2014):

\[
E_{R_a} = R_a \left( \frac{E_{\alpha}^2}{\alpha} + \frac{E_{\alpha}^2}{\alpha} \right)^{1/2},
\]

\[
E_{R_f} = R_f \left( \frac{E_{H}^2}{H} + \frac{E_{H}^2}{H} \right)^{1/2},
\]

\[
H = \frac{\Delta N_i - F_i}{\alpha_i},
\]

\[
E_{H,i} = \sqrt{E_{\Delta N,i}^2 + E_{F,i}^2},
\]

where \( E_{\Delta N,i} \) is the standard error in \( \Delta N_i \) and given as:

\[
E_{\Delta N,i} = \frac{\sigma_{\Delta N,i}}{\sqrt{J}},
\]

where \( J \) is the number of model years used to calculate \( \Delta N_i \) and \( \sigma_{\Delta N,i} \) is the standard deviation in \( \Delta N_i(t) \) for the \( J \) years.

It is also noted that each year in \( \Delta T(t) \) and \( \Delta N(t) \) time series is not independent (Gregory et al. 2004), which would lead to the underestimation of the errors calculated above. The appropriate statistical confidence intervals can be obtained by replacing the total number of model years used for the error estimation (i.e., \( I \) or \( J \)) with the effective number of years estimated after the consideration of time lag correlation (e.g., Naito and Yoden 2005) or by using the bootstrapping method as used by Andrews et al. (2012).

### 2.4 Model simulations and data

We demonstrate the application of this method using two sets of simulations, namely, (i) PI and 4C simulations with prescribed chemistry (FIXED, instead of ctrl above) and (ii) PI and 4C simulations with interactive chemistry (ACTIVE, instead of expt above). For the experiments with the prescribed chemistry (PI FIXED and 4C FIXED), the MRI atmosphere-ocean-aerosol GCM, CGCM3 (Yukimoto et al. 2012) was used. The simulations with interactive chemistry (PI ACTIVE and 4C ACTIVE) were conducted using MRI ESM1 (Earth System Model version 1, Adachi et al. 2013; Yukimoto et al. 2011).

The MRI ESM1 and CGCM3 models applied in this study are the same as those used by Noda et al. (2017, 2018) for similar PI FIXED and PI ACTIVE experiments for paleoclimates (Mid-Holocene and the Last Glacial Maximum, respectively). Although the MRI-ESM1 simulations in CMIP5 applied the carbon cycle processes, the carbon cycle processes were deactivated in the ESM1 simulations conducted here.
(for both PI and 4C). Both MRI ESM1 and CGCM3 have the same components except for the chemical component, which includes 90 chemical species with 172 gas-phase reactions, 59 photolysis reactions, and 16 heterogeneous reactions and also includes improved grid-scale transport with a semi-Lagrangian scheme (Yukimoto et al. 2011). For the FIXED PI and 4C simulations, the concentrations of the chemical species are prescribed at 1850 level. The stratosphere includes seasonal and latitude–height variations of the chemical species, whereas the troposphere includes seasonal and 3-D variations of the species. The ozone values are taken from the Atmospheric Chemistry and Climate/Stratosphere-troposphere Processes and their Role in Climate (ACC/SPARC) database (https://climatedataguide.ucar.edu/climate-data/stratospheric-tropospheric-ozone-accsparc-atmospheric-chemistry-and-climate). The concentrations of other GHGs and anthropogenic aerosols or their precursors at 1850 level are taken from the Representative Concentration Pathways (RCP) database (http://www.iiasa.ac.at/web-apps/tnt/RcpDb). More details on the prescribed chemical species are provided in Yukimoto et al. (2012). For ACTIVE PI and 4C simulations, the model had the initial chemical concentrations at 1850 level, which were taken from the “esmControl” run in CMIP5, which is the same as the ACTIVE PI simulation here.

For PI simulations, we use the same datasets of 100 years as obtained by Noda et al. (2017) for both FIXED and ACTIVE simulations. There is no significant climate drift noted in the 100 year PI simulation. For 4C simulations (both FIXED and ACTIVE), the model was started using the restart files of the corresponding PI runs and run for 110 years in total, with the CO₂ quadrupled abruptly after 10 years. The horizontal resolution of the model was a triangular truncation at the maximum wavenumber 42 (T42), corresponding to a grid resolution of ~2.8° across longitude and latitude. The model had 68 vertical layers (L68) extending from the surface to the mesopause, 0.01 hPa (Deushi and Shibata 2011). The treatment of water vapor feedback was similar to that described in Noda et al. (2018). More details on the model setup can be found in Noda et al. (2017, 2018).

The output data from 16 CMIP5 models were also used to demonstrate the application of this method for multimodel frameworks (Subsection 3.3). The CMIP5 data were obtained from the Earth System Grid Federation (ESGF) website (https://esgf-node.llnl.gov/search/esgf-llnl/).

3. Results

3.1 Demonstration of the method—Impact of interactive chemistry

To demonstrate this graphical method, we use the two sets of climate sensitivity simulation data generated from the MRI models, i.e., ACTIVE and FIXED for PI and 4C simulations as described in the previous section. Figure 1a shows the time series of \( \Delta T_x(t) \) as given by Eq. (2) for ACTIVE (blue) and FIXED (red) simulations. The vertical dotted line marks the time \( t = 0 \) when CO₂ concentration is quadrupled and the time before \( t = 0 \) corresponds to the PI condition. The response of the global mean surface air temperature anomalies to the abrupt \( 4 \times \text{CO}_2 \) is evident in the initial few decades, and the temperature changes asymptote to a similar value for both ACTIVE and FIXED simulations for around the last 50 years.

Figure 1b shows \( \Delta N_x(t) \) versus \( \Delta T_x(t) \) for the last 100 years of ACTIVE and FIXED simulations. The initial 10 years of the 110 year simulation are discarded as they correspond to the period before the quadrupling of \( \text{CO}_2 \) concentration. Figure 1b confirms the almost linear relationship between \( \Delta N_x(t) \) and \( \Delta T_x(t) \), and \( \alpha_x \) and \( F_x \) are estimated by the slope and intercept of the lines of best fit (solid blue and red lines, respectively). Note that we use the data for the full \( 4 \times \text{CO}_2 \) period (i.e., 100 years) to determine the coefficients \( \alpha_x \) and \( F_x \) using linear regression. The ratio \( R_x \) is obtained using \( \alpha_x \), and the ratio \( R_F \) is obtained from \( \Delta N_x \) and \( F_x \) as defined in Eq. (7). To calculate the climatological mean of \( \Delta N_x \), i.e., \( \Delta N_{x,F} \), we use data for the last 50 years of the simulation period, when the model is in a quasi-equilibrium state. The values of \( \Delta N_{x,F} \) are shown by horizontal dotted lines with the corresponding color in Fig. 1b. The standard errors in \( \alpha_x \) are estimated using Eqs. (8) and (10), and those in \( F_x \) are estimated using Eqs. (9) and (10), with \( i = 1 \) to 100 ( = 1). The errors in \( \Delta N_x \) are calculated using Eq. (15), with \( J = 50 \). The errors in \( R_x \) and \( R_F \) are estimated using Eqs. (11)–(15). Table 1 provides the values of all quantities and their corresponding errors.

Figure 2 shows the obtained value of \( R_x \) and \( \bar{R}_F \) (black dot) with its standard errors (horizontal and vertical bars, as described in Subsection 2.3) on \( R_x - \bar{R}_F \) plane. Figure 2 is our proposed new graphic method to visualize the impact of model changes on ECS, climate forcing, and climate feedbacks. The abscissa, \( R_x \), represents the ratio of the climate feedback parameter. The unity value of \( R_x \) represents no change in the climate feedback parameter \( \alpha_x \), and every 0.1 increase (or decrease) in the magnitude of
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R_α corresponds to the 10% increase (or decrease) in feedback strength in ACTIVE simulation compared with FIXED simulation. Similarly, the unity value on the ordinate, \( R_F = 1 \), represents no change in the difference between radiative flux imbalance and forcing (\( \Delta N - F \)).

The % change in ECS in ACTIVE simulation with respect to that in FIXED simulation is given by \( [(R_F/R_\alpha) - 1] \times 100 \). The thick black dashed line represents Case 0 as described in Subsection 2.2 with \( R_F = R_\alpha \) and therefore corresponds to the case of no impact of the experiment on the global mean surface air temperature or ECS. This line is referred to as the no-impact line. Any point lying above this no-impact line corresponds to Case I (as \( \Delta T_{\text{ctl}} > 0 \)) with \( R_F > R_\alpha \), and thus represents the amplification of global warming in the ACTIVE compared with the FIXED simulation. On the other hand, any point lying below the no-impact line corresponds to Case III with \( R_F < R_\alpha \), representing the reduction of global warming in ACTIVE simulation compared with that in FIXED simulation. Four red (blue) dashed lines in the plot show consecutive 10% increases (decreases) in the values of ECS of up to ±40%: \( R_F = \left(1 \pm \frac{a\%}{100}\right)R_\alpha \), \( (a = 10, 20, 30, \text{ and } 40) \).

In the present example, \( R_\alpha \) is \( \sim 1.08 \pm 0.04 \), which implies that the climate feedback parameter \( \alpha_x \) is

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Fig. 1. (a) Time series of global and annual mean surface air temperature anomaly, \( \Delta T(t) \), for ACTIVE (blue) and FIXED (red) simulations. (b) Net radiative flux (all components) at the TOA, \( \Delta N(t) \), versus \( \Delta T(t) \) for each year for ACTIVE (blue dots) and FIXED (red dots) simulations. Corresponding lines represent ordinary least squares regression fits to the last 100 year data. Dotted lines parallel to abscissa correspond to the time mean of \( \Delta N(t) \) for the last 50 years.

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Table 1. Summary of the parameters obtained from the linear regression fits and uncertainty in their estimation.

|                | All radiation | CS LW       | CS SW       | CRE LW       | CRE SW       |
|----------------|---------------|-------------|-------------|--------------|--------------|
| \( \alpha_{\text{ACTIVE}} \pm \varepsilon \alpha_{\text{ACTIVE}} \) | -1.312 ± 0.037 | -2.048 ± 0.016 | 0.819 ± 0.014 | -0.175 ± 0.019 | 0.093 ± 0.029 |
| \( \alpha_{\text{FIXED}} \pm \varepsilon \alpha_{\text{FIXED}} \) | -1.215 ± 0.035 | -2.000 ± 0.014 | 0.850 ± 0.014 | -0.218 ± 0.021 | 0.154 ± 0.029 |
| \( F_{\text{ACTIVE}} \pm E F_{\text{ACTIVE}} \) | 6.708 ± 0.137 | 7.561 ± 0.060 | 0.309 ± 0.054 | -1.256 ± 0.073 | 0.094 ± 0.108 |
| \( F_{\text{FIXED}} \pm E F_{\text{FIXED}} \) | 6.290 ± 0.129 | 7.714 ± 0.052 | 0.094 ± 0.052 | -1.345 ± 0.076 | -0.173 ± 0.105 |
| \( \Delta N_{\text{ACTIVE}} \pm E \Delta N_{\text{ACTIVE}} \) | 1.363 ± 0.031 | -0.813 ± 0.034 | 3.645 ± 0.016 | -1.975 ± 0.017 | 0.506 ± 0.024 |
| \( \Delta N_{\text{FIXED}} \pm E \Delta N_{\text{FIXED}} \) | 1.413 ± 0.032 | -0.352 ± 0.038 | 3.519 ± 0.018 | -2.208 ± 0.018 | 0.454 ± 0.027 |
| \( R_\alpha \pm E R_\alpha \) | 1.080 ± 0.043 | 1.024 ± 0.011 | 0.964 ± 0.023 | 0.803 ± 0.117 | 0.600 ± 0.219 |
| \( R_F \pm E R_F \) | 1.096 ± 0.041 | 1.038 ± 0.012 | 0.974 ± 0.023 | 0.833 ± 0.115 | 0.657 ± 0.210 |
| % change in ECS ± \( \delta \text{ECS} \) (%) | 1.502 ± 5.597 | 1.391 ± 1.574 | 1.015 ± 3.381 | 3.737 ± 20.806 | 9.404 ± 53.048 |
increased by ~8 % in ACTIVE simulation compared with FIXED simulation with the standard error of ±4 %. Similarly, $\Delta N_f$ is $\sim 1.10 \pm 0.04$, which means the difference between radiative flux imbalance and forcing ($\Delta N_f - F_f$) is also increased by ~10 % with a standard error of 4 %. Consequently, the ratio $R_f / R_a$ remains close to 1 with only a 1.5 % increase in ECS. It can be concluded from Fig. 2 that the impact of interactive chemistry on ECS is small in the MRI climate models. The scatter in the linear fit for $\Delta N_x(t)$ versus $\Delta T_x(t)$ is quite small for the MRI models (Fig. 1b), and thus, the uncertainties are also small. We have data only from MRI models for this demonstration, and hence, there is only one symbol in Fig. 2. However, if the multimodel outputs are available for the same experimental framework (e.g., for interactive and prescribed chemistry), then each model can be plotted by its own symbol in this diagram, and the intercomparison of ECS, climate forcing, and climate feedbacks for the multiple models is straightforward.

### 3.2 Application to individual radiative components

According to the linear climate feedback theory, the net global climate feedback is the linear sum of longwave (LW) and shortwave (SW) contributions for each clear sky (CS) and cloud radiative effect (CRE) component, as described in the Methods section of Nowack et al. (2015). The net radiative imbalance at the TOA due to all-radiative components is the linear sum of the imbalance caused by the four individual components (CS-LW, CS-SW, CRE-LW, and CRE-SW).

The corresponding values of $\Delta N(t)$ and $\Delta T(t)$ are almost linearly related to the individual radiative components in each FIXED and ACTIVE simulation as shown in Figs. 3a and 3b. The values of all metrics for the individual radiative components are obtained by estimating Gregory’s linear relations for CS and CRE components separately and given in Table 1. The CS radiative feedback, which is given by the slope of the line of best fit, is much larger in magnitude than the CRE feedback for both LW and SW components. Furthermore, the feedback for LW and SW components is opposite in sign with larger magnitudes for LW for both the CS and CRE components (see Table 1 for the estimated values). This indicates that the LW feedbacks in the atmosphere are partially offset by the corresponding SW feedbacks.

The values of $R_a$ and $R_f$ (and their uncertainties) for individual and all-radiative components are plotted in Fig. 3c. The CRE-SW (CRE-LW) component shows a large reduction of ~40.0% (~19.7%) in the climate feedback with a relatively smaller reduction of ~34.3% (~16.7%) in the climate forcing, thus indicating a net amplification of the global warming by ~9.4% (~3.7%) in ACTIVE simulation com-
pared with that in FIXED simulation. Both CS-LW and CS-SW components show small changes with the same tendency in the feedback and forcing (~2–4 % increase and ~3–4 % decrease, respectively); thus, the ratios $R_\alpha$ and $R_F$ for these components remain close to one. The uncertainties in ratios $R_\alpha$ and $R_F$ are also larger for CRE components than for CS components, which is also confirmed by Figs. 3a and 3b, showing larger scatter in CRE components than in CS components.

ACTIVE simulation leads to slight amplification of global warming by ~1.5 % compared with FIXED simulation for all-radiative components (black circle), as described in Subsection 3.1. The individual radiative components, CS-LW and CS-SW components lie near the no-impact line and show slight amplification of global warming by approximately 1 %. The CRE-LW and CRE-SW components show amplification of global warming by approximately 4 % and 9 %, respectively (the bottom row in Table 1). Also, notably, each radiation component is regressed against the same $\Delta T$, and ideally, the impact of individual components on temperatures should be the same and close to the impact noted for the all-radiative component. Here, however, $R_\alpha$ and $R_F$ for CRE have a large impact and uncertainty compared with the all-radiative component. The large uncertainties in the CRE component arise because of the large scatter in the linear fit and smaller values of climate feedback and climate forcing than those in the CS component as shown in Figs. 3a and 3b (see also Eqs. 11 and 12).

3.3 Application to multiple CMIP5 models

In the previous subsections, we showed the impact of interactive chemistry on ECS, climate forcing, and climate feedbacks for the JMA-MRI climate models as shown in Figs. 2 and 3c. To compare the outputs of multiple models, the results for other models with the same experimental framework can also be included in this diagram. Note that in this case, the impact of chemistry is examined by comparing ACTIVE (expt) simulation for each model with respect to its own FIXED (ctrl) simulation.

Here, we demonstrate to use of this method to visualize the spread in ECS, climate forcing, and climate feedbacks across multiple CMIP5 models. In this case, ctrl simulation can be replaced with the MMM, and each model can be used as an expt simulation, to examine the relative difference of ECS, climate forcing, and climate feedbacks for each model from those for the MMM. Figure 4 shows the relative difference of 18 models (16 CMIP5 models and two MRI models used above) from the MMM ($R_F = R_\alpha = 1$), plotted with their own symbols as listed.

The CMIP5 models show a large spread in ECS varying from approximately −38 % to 35 % with respect to the MMM (see Table 2 for the parameter values and standard errors of each model). In total, 10 models show more global warming when compared with the MMM (above the black dashed line), whereas the rest of the models show less global warming (below the black dashed line) when compared with the MMM. The climate forcing shows a large spread from approximately −43 % to 39 % when compared with the MMM (see $R_F$ of the sixth column in Table 2).
Fig. 4. Intercomparison of CMIP5 models for abrupt $4 \times \text{CO}_2$ experiment relative to the multimodel mean (MMM; $R_F = R_\alpha = 1$). Each model is plotted with its own symbol with standard errors in $R_F-R_\alpha$ plane. See the main text for details.

Table 2. Summary of parameters obtained for CMIP5 models for abrupt $4 \times \text{CO}_2$ experiment.

| Model            | $\alpha \pm E_\alpha$ | $F \pm E_F$ | $\Delta N \pm E_N$ | $R_\alpha \pm E_{R\alpha}$ | $R_F \pm E_{RF}$ | % change in ECS $\pm \delta$ECS (%) |
|------------------|------------------------|-------------|---------------------|-----------------------------|------------------|-----------------------------------|
| MMM             | $-1.002 \pm 0.020$     | $6.542 \pm 0.090$ | $1.878 \pm 0.017$   | $1.000 \pm 0.029$          | $1.000 \pm 0.028$ | $-8.811 \pm 14.602$               |
| ACCESS1.0       | $-0.641 \pm 0.062$     | $5.273 \pm 0.287$ | $2.024 \pm 0.043$   | $0.640 \pm 0.063$          | $0.697 \pm 0.064$ | $8.345 \pm 9.436$                 |
| ACCESS1.3       | $-0.712 \pm 0.053$     | $5.259 \pm 0.223$ | $2.066 \pm 0.032$   | $0.711 \pm 0.055$          | $0.685 \pm 0.050$ | $-3.621 \pm 10.291$               |
| CNRM-CM5-2      | $-1.050 \pm 0.064$     | $7.260 \pm 0.301$ | $2.062 \pm 0.029$   | $1.048 \pm 0.067$          | $1.115 \pm 0.068$ | $6.345 \pm 6.893$                 |
| CNRM-CM5        | $-1.202 \pm 0.050$     | $7.738 \pm 0.238$ | $1.713 \pm 0.030$   | $1.199 \pm 0.055$          | $1.292 \pm 0.057$ | $-6.231 \pm 15.860$               |
| CSIRO-Mk3.6.0   | $0.536 \pm 0.057$      | $4.638 \pm 0.259$ | $1.990 \pm 0.054$   | $0.535 \pm 0.058$          | $0.568 \pm 0.058$ | $18.580 \pm 5.017$                |
| GISS-E2-H       | $-1.466 \pm 0.058$     | $7.115 \pm 0.208$ | $1.559 \pm 0.028$   | $1.463 \pm 0.065$          | $1.191 \pm 0.051$ | $-15.780 \pm 5.179$               |
| GISS-E2-R       | $-1.468 \pm 0.074$     | $6.518 \pm 0.224$ | $1.792 \pm 0.027$   | $1.465 \pm 0.080$          | $1.013 \pm 0.052$ | $-30.841 \pm 5.179$               |
| INM-CM4         | $-1.570 \pm 0.204$     | $6.292 \pm 0.581$ | $1.738 \pm 0.027$   | $1.567 \pm 0.206$          | $0.977 \pm 0.126$ | $-37.687 \pm 11.487$              |
| IPSL-CM5A-LR    | $-0.749 \pm 0.045$     | $6.137 \pm 0.229$ | $2.034 \pm 0.034$   | $0.747 \pm 0.048$          | $0.880 \pm 0.053$ | $-17.770 \pm 10.304$              |
| IPSL-CM5A-MR    | $-0.771 \pm 0.045$     | $6.408 \pm 0.232$ | $2.134 \pm 0.028$   | $0.769 \pm 0.047$          | $0.916 \pm 0.053$ | $19.125 \pm 10.084$               |
| IPSL-CM5B-LR    | $-0.971 \pm 0.086$     | $5.087 \pm 0.319$ | $1.227 \pm 0.055$   | $0.969 \pm 0.088$          | $0.828 \pm 0.071$ | $-14.597 \pm 10.716$              |
| MIROC-ESM       | $-0.753 \pm 0.046$     | $7.575 \pm 0.274$ | $2.852 \pm 0.034$   | $0.751 \pm 0.049$          | $1.013 \pm 0.062$ | $34.833 \pm 12.051$               |
| MIROC5          | $-1.551 \pm 0.104$     | $8.511 \pm 0.416$ | $2.041 \pm 0.060$   | $1.548 \pm 0.108$          | $1.387 \pm 0.094$ | $-10.373 \pm 8.732$               |
| MPI-ESM-LR      | $-1.081 \pm 0.073$     | $7.874 \pm 0.375$ | $1.997 \pm 0.051$   | $1.079 \pm 0.076$          | $1.260 \pm 0.085$ | $16.807 \pm 11.376$               |
| MPI-ESM-MR      | $-1.101 \pm 0.078$     | $7.665 \pm 0.392$ | $1.864 \pm 0.058$   | $1.099 \pm 0.081$          | $1.244 \pm 0.088$ | $13.195 \pm 11.615$               |
| MPI-ESM-P       | $-1.115 \pm 0.074$     | $7.843 \pm 0.370$ | $1.942 \pm 0.059$   | $1.113 \pm 0.077$          | $1.265 \pm 0.084$ | $13.674 \pm 10.892$               |
| MRI-ESM1        | $-1.312 \pm 0.037$     | $6.708 \pm 0.137$ | $1.363 \pm 0.031$   | $1.309 \pm 0.045$          | $1.146 \pm 0.038$ | $-12.441 \pm 4.169$               |
| MRI-CGCM3       | $-1.215 \pm 0.035$     | $6.290 \pm 0.129$ | $1.413 \pm 0.032$   | $1.212 \pm 0.043$          | $1.046 \pm 0.035$ | $-13.736 \pm 4.204$               |
Similarly, the climate feedback \((\alpha)\) also shows a larger spread from \(-46\%\) to \(57\%\) with respect to the MMM (the fifth column in Table 2).

The MIROC-ESM model shows a \(~35\%\) larger warming than that shown by the MMM (Case I), which is mainly due to the difference in climate feedback \(~25\%\) less than that in the MMM), whereas the forcing is almost the same as that in the MMM. Similarly, the INM-CM4 model shows a small difference in the forcing \(~2\%\) less than that in the MMM), whereas the feedback is \(~57\%\) more than that in the MMM, leading to \(~38\%\) lower ECS than that in the MMM (Case III). The CSIRO-Mk3.6.0 model shows the largest reduction in forcing and feedbacks (approximately \(~43\%\) and \(~47\%\), respectively), but since the changes in both forcing and feedback are comparable, the net impact on ECS remains small \(~6\%).

It is interesting to note that different models from the same modeling center also show different variations in ECS, climate forcing, and climate feedbacks. For instance, the MIROC5 and MIROC-ESM models are quite different when compared with the pair of MRI models (CGCM3 and ESM1). The MIROC5 model shows \(~10\%\) less warming than that in the MMM, whereas the MIROC-ESM model shows \(~35\%\) more warming than that in the MMM. The forcing for MIROC-ESM is close to the MMM, but the feedback is relatively smaller \(~25\%\), whereas, for MIROC5, the feedback and forcing are approximately \(55\%\) and \(39\%\) larger, respectively.

Similar to the intermodel comparison with respect to the MMM presented above, one can also compare the outputs of other models with respect to one benchmark model. In such a case, ctrl can be replaced with the benchmark model, and each model that is being compared can be represented by expt. It is also possible to examine the spread in ECS, climate forcing, and climate feedbacks for different ensemble members in a large ensemble of simulations conducted using a single model (e.g., Dessler et al. 2018), with the ensemble mean as ctrl and individual members as expt.

4. Concluding remarks

We proposed a new graphical method that provides a concise summary of the impact of model or process change on ECS, climate forcing, and climate feedbacks. The method is based on the linear regression method that was introduced by Gregory et al. (2004). Using this method, one can (a) quantify whether the model or process change amplifies, reduces, or has no impact on global warming, (b) evaluate the percentage changes in ECS, climate forcing, and climate feedbacks, and (c) quantify the ranges of the uncertainties in the estimated changes. Using this graph, the outputs of multiple models for the same experimental framework (e.g., usage of interactive chemistry compared with the prescribed one) can be collated and visualized in one single diagram, which is otherwise challenging to compare and comprehend.

We demonstrated this method using an example of climate sensitivity simulations with and without interactive chemistry with JMA-MRI climate models. An application of this method for four individual radiative components (CS and CRE for LW and SW components) was also described, after confirming the appropriateness of the linear fittings of Gregory’s regression. We also presented the application of this method to visualize and quantify the spread in ECS, climate forcing, and climate feedbacks for individual models with respect to the MMM in multiple model frameworks such as CMIP5 (Taylor et al. 2012), Coupled Model Intercomparison Project Phase 6 (CMIP6; Eyring et al. 2016), Geoengineering Model Intercomparison Project (GeoMIP; Kravitz et al. 2011), and nonlinear climate responses to CO\(_2\) (nonlinMIP; Good et al. 2016). Furthermore, it could be used to determine the differences in these three parameters for multiple models against any benchmark model instead of the MMM or to estimate the spread or change in the three parameters for a large ensemble of simulations done by using a single model (e.g., Dessler et al. 2018).

It is also important to remark here that this method is based on Gregory’s linear regression and the uncertainties (or standard errors) in climate forcing and climate feedbacks are calculated under the approximation that the relationship between the net radiative imbalance, \(\Delta N(t)\), and the global mean surface air temperature change, \(\Delta T(t)\), is linear. The nonlinear response of \(\Delta T\) to \(\Delta N\), if any, will be included in the uncertainty estimates given in Subsection 2.3. In this paper, we described the graphical method and demonstrated its application using an example of climate sensitivity simulations for instantaneously quadrupled CO\(_2\) with and without interactive chemistry. More detailed findings on the impact of using interactive chemistry on the surface and other atmospheric variables in the MRI climate models will be provided in a separate paper.

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