Features of calculation and design of complex concrete monolithic slabs

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Abstract. In the article features of designing of reinforced concrete floors on the profiled flooring, leaning against steel I-beams are considered. Specific features of calculating the strength of composite slabs in accordance with JV 35.13330.2011 "Bridges and pipes" and SP 266.1325800.2016 "Structural concrete structures. Design rules". A method for determining the forces based on the real ratio of the rigidity of the overlap elements is also considered. The analysis of the results of the numerical experiment made it possible to establish the optimum coefficients of the use of materials that can be used in the design of combined overlaps.

1 Introduction

In the article features of calculation of durability of the combined beams of overlap executed in accordance with SP 35.13330.2011 «Bridges and pipes» and SP 266.1325800.2016 «Steel reinforced concrete structures. Design rules", and also by means of a calculation based on the distribution of forces in accordance with the rigidity of the overlap elements. In order to obtain efficient and least material-intensive structures, overlaps were investigated in the range of design loads from 15 to 60 kg / m for I-beam type 35B1. The analysis and comparison of the results are performed, recommendations on the design of such structures are formulated.

Many Russian and foreign scientists were studying the work of complex monolithic ceilings, supported on metal beams. For example, in [1-3] the questions of the relevance of the use of such structures in buildings of various purposes have been studied. Features of calculations of such overlaps are presented in the studies [4-14].

Traditionally, the calculation of strength was carried out in accordance with the distribution of forces, in proportion to the rigidity of the components of the overlap [15]. Since 1984, the calculation of composite structures has been carried out in accordance with [16] and its subsequent versions [17], and in 2017 a normative document [18] has been introduced, which to some extent duplicates the provisions of previous standards. At present, in Russia it is recommended to calculate the steel-reinforced concrete structures in accordance with [18].

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2 Methods

The object of the study is a monolithic complex overlap, hinged on the rolling beams 35B1, steel grade C345. Estimated span of beams 6m, step 3m. Concrete - heavy, class B15, profiled flooring - brand H75-700 with a thickness of 0.7 mm, the maximum thickness of reinforced concrete slab is 125 mm. The total design load $q$ on the overlap varied from 5.0 to 20.0 kN/m$^2$. The calculated load on the beam $q_b$ from 15 to 60 kN/m$^2$ (Figure 1).

According to [15], in such a construction, the total bending moment $M_{ex}$ is perceived by a reinforced concrete slab over the profiled floor ($M_{1ex}$) and metal beams ($M_{2ex}$)

$$M_{ex} = M_{1ex} + M_{2ex}.$$  (1)

The distribution of the moments is directly proportional to the ratio of the rigidity $B$ of these components

$$M_{1ex} / M_{2ex} = B_1 / B_2.$$  (2)

Rigidity of a monolithic reinforced concrete floor over profiled flooring $B_{gb}$

$$B_1 = B_{gb} = 0,85 \cdot E_b \cdot I_n,$$  (3)

$E_b$ - modulus of elasticity of concrete; $I_n=(b'_y \cdot h'_y)/12$ - moment of inertia of reinforced concrete section; $b'_y$ and $h'_y$ - width and height of the flange of the T-section.

The stiffness of an I-beam

$$B_2 = B_1 = 0,85 \cdot E_s \cdot I_l,$$  (4)

$E_s$ - modulus of elasticity of steel; $I_l$ - moment of inertia of the beam.

The maximum bending moment of a metal beam

$$M = R_y \cdot W_{n,min} \cdot \gamma_c,$$  (5)

$W_{n,min}$ - required moment of beam strength; $R_y$ - calculated strength of the beam material; $\gamma_c$ - coefficient of working conditions adopted by [15];

To satisfy the requirements of the strength of the overlap, the following conditions must be fulfilled:

$$M_{1ex} < M_{1in} \text{ and } M_{2ex} < M_{2in}.$$  (6)

In accordance with the norms of [17] the following conditions must be fulfilled:

1. Stiffness ratio

$$E_b \cdot I_b \leq 0.2 \cdot E_s \cdot I_s.$$  (7)

2. Check of stresses in concrete

$$\sigma_b = M_2/(a_b \cdot W_{b,red}) \cdot \sigma_{bi} < m_b \cdot R_b$$  (8)

3. Checking of stresses in the longitudinal reinforcement

$$\sigma_s = M_2/(a_b \cdot W_{b,red})+\sigma_{si} < m_s \cdot R_sc$$  (9)

4. Checking of stresses in the upper belt of the steel beam

$$(M-z_{b,st} \cdot N_{b,s})/(\alpha \cdot W_{f1,at}) - N_{b,s} / A_{st} \leq m_1 \cdot m_c \cdot R_y$$  (10)

5. Checking of stresses on the belt of steel beams

$$(M-z_{b,st} \cdot N_{b,s})/(\alpha \cdot W_{f1,at}) + N_{b,s} / A_{st} \leq m \cdot R_y$$  (11)

The notation in formulas (7-11) was adopted according to SP 35.13330.2011 "Bridges and pipes" [17].
In accordance with the norms [18] the following conditions must be fulfilled:

1. Stiffness ratio
   \[ E_b \cdot I_b \leq 0.2 \cdot E_{st} \cdot I_{st} \]  

2. Check of stresses in concrete
   \[ \sigma_b = \frac{M_2}{(\alpha_b \cdot W_{b,red})} \cdot \sigma_{bi} \leq \gamma_{bi} \cdot R_b \]  

3. Checking of stresses in the longitudinal reinforcement
   \[ \sigma_s = \frac{M_2}{(\alpha_b \cdot W_{b,red})} + \sigma_{ri} \leq \gamma_{si} \cdot R_s \]  

4. Checking of stresses in the upper belt of the steel beam
   \[ \left( M - z_{b,st} \cdot N_{b,s} \right) / W_{f,2,st} + N_{b,s} / A_{st} \leq \gamma_{1} \cdot \gamma_{c} \cdot R_y \]  

5. Checking of stresses on the belt of steel beams
   \[ \left( M - z_{b,st} \cdot N_{b,s} \right) / W_{f,1,st} + N_{b,s} / A_{st} \leq \gamma_{c} \cdot R_y \]  

The designations in formulas (12-16) are adopted according to SP 266.1325800.2016 "Steel reinforced concrete structures. Design rules" [18].

3 Results and discussion

In accordance with the above normative documents, calculations of the strength of combined beams of complex monolithic overclad were performed and the coefficients of the use of materials for different load ranges and different beam sections were found (Figures 2-4 and Table 1).

**Fig. 2.** Coefficients of use \( K \) obtained in accordance with [15].

It can be seen from figure 2 that with increasing load, the utilization factors the materials of the beam \( K_I \) and the plate \( K_p \) increase in proportion to the applied load, and the utilization factor of the beam \( K_I \) grows slower than the coefficient \( K_p \) (30-6%). At loads above 50 kN/m, the strength of the beam is fully used, and in the slab there is still a reserve of about 10%.

**Fig. 3.** Coefficients of use \( K \). a) - prepared according to [17], b) - prepared according to [18].

It can be seen from figure 3a that the utilization factor of the material in the lower belt of the beam \( K_s \) increases from 0.277 to 1.061 and exceeds the remaining strength coefficients of concrete \( K_b \), the longitudinal reinforcement \( K_s \), of the material in the upper
belt of the steel beam $K_v$ by 2-3 times, lower beam girdle for simultaneous achievement of utilization factors in all elements of overlap.

It can be seen from figure 3b that the coefficient of utilization of the material in the lower belt of the beam $K_v$ increases from 0.288 to 1.16 and exceeds the rest factors of the strengths of concrete $K_b$, the longitudinal reinforcement $K_s$, of the material in the upper belt $K_v$ by a factor of 2-5, lower beam girdle for simultaneous achievement of utilization factors in all elements of overlap.

**Table 1. Coefficient of use of strength of combined beams at different loads**

| Normative document | Coefficient of use | Load, kN/m |
|--------------------|--------------------|------------|
|                    | 15                 | 22.5       | 30       | 37.5     | 45       | 52.5     | 60       | 62.5     |
| [15]               | $K_f$              | 0.35       | 0.52     | 0.69     | 0.87     | 1.04     | 1.21     | 1.38     | 1.44     |
|                    | $K_p$              | 0.27       | 0.41     | 0.56     | 0.72     | 0.89     | 1.08     | 1.29     | 1.36     |
| [17]               | $K_b$              | 0.07       | 0.14     | 0.21     | 0.28     | 0.35     | 0.41     | 0.48     | 0.55     |
|                    | $K_L$              | 0.07       | 0.13     | 0.19     | 0.25     | 0.32     | 0.38     | 0.44     | 0.5      |
|                    | $K_s$              | 0.15       | 0.18     | 0.21     | 0.24     | 0.26     | 0.29     | 0.32     | 0.35     |
|                    | $K_n$              | 0.277      | 0.394    | 0.508    | 0.62     | 0.73     | 0.84     | 0.95     | 1.05     |
| [18]               | $K_b$              | 0.08       | 0.16     | 0.23     | 0.31     | 0.38     | 0.46     | 0.53     | 0.61     |
|                    | $K_L$              | 0.07       | 0.13     | 0.19     | 0.25     | 0.32     | 0.38     | 0.44     | 0.5      |
|                    | $K_s$              | 0.07       | 0.08     | 0.1      | 0.12     | 0.14     | 0.17     | 0.2      | 0.23     |
|                    | $K_n$              | 0.288      | 0.412    | 0.537    | 0.66     | 0.785    | 0.91     | 1.034    | 1.16     |

Figure 4 shows a comparison of the strength coefficients of the section of the I-beam 35B1, obtained by different methods.

**Fig. 4. Coefficients of use of strength of beams.**

It can be seen from figure 4 that the coefficient of use of the material of the beam $K$, calculated in accordance with [15], exceeds the analogous coefficients found by [17] and [18] by 1.2-1.4 times, with the greatest discrepancy at higher loads. The coefficients of the use of the material of the beam $K$, found from [18], are insignificant (by 4-9%) higher than the analogous coefficients calculated by [17].

4 Conclusions

1. The performed work shows that it is possible to use all the considered methods to calculate the strength of complex overlaps.
2. The largest reserves of strength of materials and overlapping in general give results obtained in accordance with [15].
3. Calculations performed in accordance with recommendations [17] and [18] give close results and can be used to calculate similar structures.
4. The limits of the applicability of calculating the strength of complex overlaps are in accordance with [15] in the range of loads 15 ~ 45 kN / m, and for calculation of strength in accordance with [17] and [18] - 15 ~ 60 kN / m.
5. Traditional calculation of the strength of a complex overlap, based on the distribution of forces in proportion to the rigidity, can be used for preliminary evaluation calculations of the strength of combined beams, in view of its simplicity and accessibility.
6. The results of this study extend to other types of complex floors, including a reinforced concrete slab, profiled flooring and steel beams.

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