THE DENSITY OF CORONAL PLASMA IN ACTIVE STELLAR CORONAE

PAOLA TESTA,1,2,3 JEREMY J. DRAKE,2 AND GIOVANNI PERES3

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ABSTRACT

We have analyzed high-resolution X-ray spectra of a sample of 22 active stars observed with the High Energy Transmission Grating Spectrometer on Chandra in order to investigate their coronal plasma density. Densities were investigated using the lines of the He-like ions O vii, Mg xi, and Si xii. Si xii lines in all stars of the sample are compatible with the low-density limit (i.e., \( n_e \leq 10^{13} \text{ cm}^{-3} \)), casting some doubt on results based on lower resolution Extreme Ultraviolet Explorer (EUV) spectra finding densities \( n_e > 10^{13} \text{ cm}^{-3} \). Mg xi lines betray the presence of high plasma densities up to a few times \( 10^{12} \text{ cm}^{-3} \) for most of the sources with higher X-ray luminosity \( (\geq 10^{30} \text{ ergs s}^{-1}) \); stars with higher \( L_X \) and \( L_X/L_{bol} \) tend to have higher densities at high temperatures. Ratios of O vii lines yield much lower densities of a few times \( 10^{10} \text{ cm}^{-3} \), indicating that the “hot” and “cool” plasma resides in physically different structures. In the cases of EV Lac, HD 223460, Canopus, \( \mu \) Vel, TY Pyx, and IM Peg, our results represent the first spectroscopic estimates of coronal density. No trends in density-sensitive line ratios with stellar parameters effective temperature and surface gravity were found, indicating that plasma densities are remarkably similar for stars with pressure scale heights differing by up to 3 orders of magnitude. Our findings imply remarkably compact coronal structures, especially for the hotter \((\sim 7 \text{ MK})\) plasma emitting the Mg xi lines characterized by the coronal surface filling factor, \( f_{\text{Mg xi}} \), ranging from \( 10^{-4} \) to \( 10^{-1} \), while we find \( f_{\text{O vii}} \) values from a few times \( 10^{-3} \) up to \( \sim 1 \) for the cooler \((\sim 2 \text{ MK})\) plasma emitting the O vii lines. We find that \( f_{\text{O vii}} \) approaches unity at the same stellar surface X-ray flux level as characterizes solar active regions, suggesting that these stars become completely covered by active regions. At the same surface flux level, \( f_{\text{Mg xi}} \) is seen to increase more sharply with increasing surface flux. These results appear to support earlier suggestions that hot \( 10^7 \text{ K} \) plasma in active coronae arises from flaring activity and that this flaring activity increases markedly once the stellar surface becomes covered with active regions. Comparison of our measured line fluxes with theoretical models suggests that significant residual model inaccuracies might be present and, in particular, that cascade contributions to forbidden and intercombination lines resulting from dielectronic recombination might be to blame.

Subject headings: plasmas — stars: activity — stars: coronae — stars: late-type — Sun: corona — X-rays: stars

1. INTRODUCTION

X-ray and EUV spectra present the most effective means to investigate the physics of the hot magnetically confined plasma in the outer atmospheres of late-type stars. The aim of spectroscopic diagnosis of these astrophysical plasmas is to probe the physical conditions of the gas and to derive relevant parameters such as electron density, thermal structure, and relative element abundances: such information should help us to constrain models of the coronal heating and structuring. As an intermediate step toward this goal, by studying the emission properties of stellar coronae we can test the validity of the solar analogy, i.e., whether the basic components of stellar coronae are analogous to those observed in the solar corona, whose dominant X-ray-emitting structures are defined by the looplike morphology of coronal magnetic fields.

The new generation X-ray observatories, Chandra and XMM-Newton, with their unprecedented spectral resolution and large effective areas, are providing us with high-resolution coronal X-ray spectra in which individual spectral lines can be readily resolved. The X-ray plasma diagnostics these spectra now allow for stars were previously accessible only for the Sun. It is also worth noting that Chandra and XMM-Newton stellar coronal spectra offer significantly more extensive X-ray wavelength coverage than achieved with solar instrumentation. In particular, with regard to this paper, the High Energy Transmission Grating Spectrometer (HETGS) on Chandra provides high-resolution \((\lambda/\Delta \lambda \sim 100–1000)\) spectra in the energy range 0.4–8.0 keV \((1.5–30 \text{ Å})\) where we observe simultaneously a large number of prominent emission lines that, at least in principle, provide both temperature and density diagnostics.

Of special importance for the purposes of this paper are the complexes of He-like “triplets” of O, Ne, Mg, and Si, which include the resonance line \((r: 1s^2 1S_0−1s2p \ ^3P_1)\), the intercombination lines \((i: 1s^2 1S_0−1s2p \ ^3P_2,1)\), and the forbidden line \((f: 1s^2 1S_0−1s2s \ ^3S_1)\), which correspond to transitions between the \( n = 2 \) shell and the ground level, \( n = 1 \). The utility of these lines for plasma diagnostics was pointed out by Gabriel & Jordan (1969; see also Pradhan & Shull 1981 and Porquet & Dubau 2000 for a recent treatment): the ratio \( R = f/i \) is mainly density sensitive, as a result of the metastable \( 1s2s \ ^3S_1 \) level, while the ratio \( G = (f+i)/r \) is mostly temperature sensitive. Similar diagnostic techniques have been widely exploited for electron density estimates in EUV spectra (see, e.g., Mariska 1992 for solar applications and Laming 1998 for a review of stellar work). Chandra and XMM-Newton data offer the opportunity to apply these techniques to the X-ray range and to explore different temperature
and density regimes. In this context, analyses of He-like triplets seen in the X-ray spectra of a few different stars have appeared in recent literature (e.g., Brinkman et al. 2000; Canizares et al. 2000; Aundard et al. 2001; Güdel et al. 2001a, 2001b, 2002; Huemmoerder et al. 2001; Ness et al. 2001, 2002a; Raassen et al. 2002; Stelzer et al. 2002; Sanz-Forcada et al. 2003b). The study of Ness et al. (2002b) is more extensive and involves several stars observed with the Chandra Low Energy Transmission Grating Spectrograph (LETGS).

While all the results from these studies cannot be easily summarized, it is apparent, mostly from O vii/C lines, that there is a general trend showing that plasma of temperatures with up to a few million kelvin has densities similar to those found in solar active regions, up to a few times \(10^{10} \text{ cm}^{-3}\). These results, however, are not without controversy. Brickhouse (2002), for example, notes that different density values have resulted from different analyses of the same stars observed with the different Chandra and XMM-Newton spectrometers. These instruments have different resolving powers, and density-sensitive lines can be blended to greater or lesser extents with other lines. In this regime, the analysis is also sensitive to the continuum level adopted. For the case of XMM-Newton spectra, this is further complicated by the extended wings of the instrumental profile, which can give rise to a significant pseudocontinuum.

The best instrumentation to study the He-like lines of O, Ne, Mg, and Si is that with the highest resolving power: the Chandra HETGS. We were therefore motivated to perform a systematic study of these lines in a large sample of stars observed with the HETGS in order to attempt to characterize plasma physical conditions in a sample of stars with very different stellar parameters. The results would be used to probe possible trends of the plasma parameters with more global coronal parameters, such as X-ray luminosity or flux, or probe possible trends of the plasma parameters with more global coronal parameters, such as X-ray luminosity or flux, or stellar effective temperature, gravity, rotational period, etc.

In this paper we have analyzed in detail the lines of Si

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We describe the observations and the stellar sample in § 2 and the detailed line analysis in § 3; we discuss the results obtained in the context of coronal activity in § 4, and we draw our conclusions in § 5.

2. OBSERVATIONS

The sample analyzed consists of all the late-type stars for which observations were available in the Chandra public archive\(^4\) at the time in which this study was undertaken. The sample comprises 22 cool stars at different activity levels and includes single stars (the flare stars AU Mic, Proxima Cen, and EV Lac; the zero-age main-sequence star AB Dor; the T Tauri star TW Hya; and the giants HD 223460, 31 Com, \(\beta\) Ceti, Canopus, and \(\mu\) Vel) and multiple systems (the close eclipsing binary system Algol; two eclipsing binary systems of W UMa type, namely, ER Vul and 44 Boo; and the RS CVn systems TZ CrB, UX Ari, \(\xi\) UMa, II Peg, \(\lambda\) And, TY Pyx, AR Lac, and IM Peg).

These sources were all observed using the Chandra HETGS and the Advanced CCD Imaging Spectrometer (ACIS-S) detector (Canizares et al. 2000). The HETG disperses X-rays through two different gratings, whose spectral coverage partially overlaps; they are optimized for “medium” (MEG) and “high” (HEG) energies. The spectral resolution obtained with the HETGS is in the range \(\lambda/\Delta\lambda = 100–1000\). The data used here were either recently processed by the standard pipeline and obtained directly from the archive or else, in the case of older observations, reprocessed using standard CIAO 3.0 tools and analysis threads to take advantage of recent improvements in the spectrum reduction software and ancillary calibration data. Our analysis of spectral lines was based on the summed data from positive and negative orders.

Tables 1 and 2 summarize, respectively, the stellar parameters and the characteristics of the observations. For each source the listed X-ray luminosity was derived by integrating the photon energies over all the wavelengths in the spectral ranges of the two different instruments, HEG and MEG.

As summarized in Table 1, the single stars in our sample are four late-type flare stars, namely, AU Mic, Proxima Centauri, EV Lac, and the rapid rotator AB Dor (\(P_{\text{rot}} \sim 44\) ks); the giants, HD 223460, 31 Com, \(\beta\) Ceti, Canopus, and \(\mu\) Vel; and the T Tauri star TW Hya. The other sources are binaries, and most are classified as systems of RS CVn type. In detail, among the RS CVn systems, II Peg is a system of a K2 V star and an unseen companion, analogously \(\lambda\) And is a binary system of which we see only one component (G8 IV–III), and finally TY Pyx is an eclipsing active close binary system of two G5 IV stars. As for the remaining sources, \(\xi\) UMa is a binary system of two optically identical components (G0 V), one of which is a rapid rotator, and there are two eclipsing binaries of W UMa type: ER Vul, a contact binary system of which we see only one component (G8 V + G5 V) that are rapid rotators (\(v \sim 81\) and 71 km s\(^{-1}\), respectively), and 44 Boo, a contact binary system of G1 V–G2 V stars.

\(^4\) Available at http://cxc.harvard.edu/cda.
It is worth noting that our sample contains sources whose X-ray luminosities span a very wide range, from a few times $10^{26}$ ergs s$^{-1}$ of Proxima Cen up to a few times $10^{31}$ ergs s$^{-1}$ of the giant HD 223460. As for the ratio of X-ray to total luminosities, $L_X/L_{bol}$, our sample covers the range $L_X/L_{bol} = 10^{-6}$ to $10^{-3}$. We are therefore analyzing spectra of stars whose activity levels cover almost the whole activity range observed for late-type stars; however, most of them are very active stars.

Spectra for each source were extracted from photon event files obtained from the Chandra Data Archive (see footnote 4) using CIAO 3.0. Effective areas were calculated using standard CIAO procedures, and we included the effects of the ACIS-S contamination layer (e.g., Plucinsky et al. 2002) using version 1 of the effective area contamination correction. The resulting HETG spectra are shown in Figures 1 and 2; spectra of sources of the same type are grouped together: Figure 1 shows the spectra of single stars (both dwarfs and giants), and Figure 2 shows the spectra of binary systems. For sources with several different observations we show the co-added spectra.

3. DATA ANALYSIS
3.1. Light Curves

As a first step of the analysis we have extracted the light curves to check whether the spectra integrated over the whole observation time are influenced by significant variability or large flare events. In order to obtain the light curves, we excluded the zeroth-order events that can be drastically compromised by photon pileup effects and considered just the dispersed events. The light curves were obtained by summing

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Footnote 4: See http://cxc.harvard.edu/ciao/threads/aciscontam.
all the counts of HEG and MEG spectra for spectral orders \( n \geq 1 \) in temporal bins of 100 s.

The resulting light curves are shown in Figures 3 and 4. We see from these figures that there are no remarkable variations in X-ray count rate for 31 Com, \( \beta \) Ceti, Canopus, \( \mu \) Vel, ER Vul, UX Ari, \( \xi \) UMa, \( \lambda \) And, AR Lac, and IM Peg. In the remaining cases, the light curves of AU Mic and EV Lac show flaring activity and, in particular, flares of different intensity and temporal extent; the Proxima Centauri light curve shows a flare at the beginning of the observation and then a decay over about 3 ks, and then the emission stabilizes at a low level; the AB Dor emission is almost steady with the exception of a moderate flare extending over about 10 ks (among the \( \sim 53 \) ks of the total observation); HD 223460 shows a large flare over half of the observing time; it is worth noting that flares have been thought of as fairly unusual on single giants (e.g., Ayres et al. 1999, 2001); the light curve of Algol shows evidence of a big flare with a peak at about 10 ks after the beginning of the observation and then a slow decrease over about 40 ks to approximately the initial emission level; TZ CrB shows a flare with a rapid increase of the emission by a factor of 4 over the last \( \sim 3.5 \) ks among the 83.7 ks of total exposure time; II Peg shows a big flare analyzed in detail by Huenemoerder et al. (2001); the TY Pyx total emission is quiescent with a slight modulation for almost the whole observation except a short flare (lasting \( \sim 3 \) ks) in the middle of the observation. The light
curve of 44 Boo exhibits periodic modulation that was analyzed in detail by Brickhouse et al. (2001), who exploited, for the first time, the possibility of a crude Doppler imaging at X-ray wavelengths to derive geometrical properties of coronal X-ray-emitting structures.

Regarding the influence of these variations on the integrated spectra, in most of the cases they do not affect substantially the basic properties of line emission, whereas the continuum emission changes significantly during the flares. For example, for the II Peg observation, Huenemoerder et al. (2001) show that at “low” temperatures \( T < 10 \text{ MK} \) the modulation of the line fluxes during the flare is low (\( \Delta T < 15\% \)), and in particular, since the triplet lines do not show substantial variations, they use the data integrated over the entire observation for the density diagnostics. In other cases, e.g., AU Mic, TZ CrB, TY Pyx, and AB Dor, the flares extend over a very small portion of the observing time; thus, they do not affect substantially the total spectra. Unfortunately, in these cases the flaring intervals are also too short to provide adequate signal for separate analysis. Finally, in the case of Proxima Centauri, the flaring portion of the emission is the only detectable signal, and even when considering the total spectra, it is not possible to measure the fluxes of most of the lines because of the low signal. In light of the above considerations, our analysis here is based on spectra integrated over entire observations.

3.2. Spectra

We illustrate the lines used in this analysis in the MEG spectrum of \( \beta \) Ceti, illustrated in Figure 5; the relevant lines are labeled by element and ionization stage. As already mentioned in § 1, in the HETGS spectral range the lines of He-like ions are among the most intense, although our analysis hinges on the measurement of relatively weak components of these. The theoretical wavelengths of these line complexes, as they appear in the APED database (Smith et al. 2001), are listed in Table 3. Our plasma density analysis basically consists of a comparison between measured and theoretical relative intensities of the forbidden and intercombination lines (the \( R \) ratio).

For this comparison, we adopt the line emissivities of APED, and in Figure 6 we show the dependence of the \( R \) ratio on \( n_e \) at the temperature of maximum formation of each of the He-like ions considered here. For comparison we plot also the values from Porquet et al. (2001).

As Figure 6 illustrates, the \( R \) ratios at the low-density limit differ by about 10% between the different calculations. At densities above the lower sensitivity threshold, the calculations are in much better agreement for O and Mg, although differences persist for Si at higher densities. The Porquet et al. (2001) and Smith et al. (2001) emissivities are based on different input atomic data, and so small discrepancies are to be expected. Mewe et al. (2003) noted the same differences in predicted \( R \) ratios for O vii and attributed these to the different sources used for the direct excitation terms: Smith et al. (2001) used the excitation rate coefficients from Kato & Nakazaki (1989) (for \( n < 5 \)) and from HULLAC (Liedahl et al. 1995; for \( n = 6-10 \)), while Porquet et al. (2001) adopted coefficients from Zhang & Sampson (1987) (for \( n < 3 \)) and from Sampson et al. (1983) (for \( 2 < n < 6 \)). We also note that dielectronic recombination and radiative recombination rates are from different sources in the two models. Since the 1s2s \( ^3S_1 \) and 1s2p \( ^3P_{1,2} \) levels are primarily populated by cascades from higher levels that in turn are largely populated by dielectronic recombination (e.g., Smith et al. 2001), it seems plausible that the treatment of these processes could also contribute significantly to differences in predicted \( R \) ratios.

In this paper we emphasize as much as possible trends in the observed \( R \) ratios, rather than in the exact conversion to
density values using theoretical models; had we adopted the Porquet et al. (2001) theoretical $R$ ratios instead of those of Smith et al. (2001), none of our conclusions would be significantly changed.

Observed spectra were analyzed with the IDL 5.3
PINTofALE 1.0 software (Kashyap & Drake 2000). Line fluxes were determined by fitting with a modified Lorentzian function described by the relation

$$F(\lambda) = \frac{a}{1 + [(\lambda - \lambda_0)/\Gamma]^2},$$

where $a$ is the amplitude and $\Gamma$ is a characteristic line width, and with a value of 2.5 for the exponent $\beta$. This function has been found to be a good match to observed line profiles in

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6 Interactive Data Language, Research Systems, Inc.
7 Available at http://hea-www.harvard.edu/PINTofALE.
stellar coronal spectra with counts of a few thousand or less (see, e.g., the Chandra Proposers’ Observatory Guide\(^8\)).

The measured $R$ ratio can be somewhat sensitive to the level assumed for the underlying continuum, and so we took particular care in locating this. For a few spectra of the very active stars the continuum is quite strong in the vicinity of the Mg and Si triplets (HD 223460, Algol, Tz CrB, II Peg, AR Lac, HR 1099, and IM Peg), while in the 21–22 Å range where the O vii lines are located the continuum level was always close to zero and essentially negligible. The continuum in a coronal plasma at temperatures exceeding a few million kelvin is predominantly due to bound-free and free-free emission from hydrogen. Over small wavelength intervals this continuum is quite flat and can be modeled using the instrument effective area function pinned down in adjacent “line-free” regions. For the very active stars, we also used a generic continuum model computed for the RS CVn–type binary HR 1099 by Drake et al. (2001), scaled again according to the lines are more likely to be affected by blending. Indeed, the Si\(\text{xi}\) triplet lies in a more crowded region and the latter lines are listed in Table 4.

...the $f$ and $i$ lines, the differences in measured fluxes were always smaller than the statistical uncertainties in the fluxes themselves such that uncertainty in continuum placement was not a significant source of error in the analysis.

We measured the spectral line intensities of the Si\(\text{xiii}\), Mg\(\text{xi}\), and O vii He-like triplets from both HEG and MEG spectra wherever the data offer useful signal. The results obtained from the two spectra are in good agreement, as shown below. The O vii lines were measured only in the MEG spectra since they are outside the wavelength range of the HEG. For all the He-like line complexes we fitted the three lines simultaneously; the free parameters of the fit were the position and the flux of each of the lines, while the widths of all lines were constrained to have the same value.

### 3.3. Mg\(\text{xi}\) Spectral Region

While the Si\(\text{xiii}\) and the O vii triplet lines are relatively isolated, the Mg\(\text{xi}\) triplet lies in a more crowded region and the lines are more likely to be affected by blending. Indeed, the APED database predicts a number of Fe xix–xxii lines in the 9.15–9.35 Å region, although each of these is considerably weaker than the Mg lines of interest. Moreover, lines from the Lyman series of H-like Ne with upper levels $n > 5$ also lie in this region. The latter lines are listed in Table 4.

We investigated the possible influence of line blends in our measurement of the Mg\(\text{xi}\) triplet components in some detail. First, we carefully examined HEG spectra with both the highest signal-to-noise ratio (S/N) and the highest relative intensity of Fe or Ne lines with respect to Mg lines (e.g., UX Ari for both Fe and Ne; AB Dor for Fe; HR 1099, II Peg, and AU Mic for Ne) for evidence of spectral features close to, or blending with, the triplet lines. In particular, in the spectra of stars in which Ne has been found to be strongly enhanced relative to Fe, such as HR 1099 (Drake et al. 2001)

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**TABLE 3**

| ION         | Resonance $(i)$ | Intercombination $(i)$ | Forbidden $(f)$ |
|-------------|-----------------|------------------------|-----------------|
| Si\(\text{xiii}\) | 6.6479          | 6.6850/6.6882          | 6.7403          |
| Mg\(\text{xi}\) | 9.1687          | 9.2282/9.2312          | 9.3143          |
| O vii       | 21.6015         | 21.8010/21.8036        | 22.0977         |

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**TABLE 4**

| Transition | $\lambda$ (Å) | $f^*$ |
|------------|---------------|------|
| Ly$\beta$: 2 $\rightarrow$ 1 | 12.134 | 1.0000 |
| Ly$\beta$: 3 $\rightarrow$ 1 | 10.239 | 0.1900 |
| 4 $\rightarrow$ 1 | 9.708 | 0.0697 |
| 5 $\rightarrow$ 1 | 9.481 | 0.0335 |
| 6 $\rightarrow$ 1 | 9.362 | 0.01874 |
| 7 $\rightarrow$ 1 | 9.291 | 0.01157 |
| 8 $\rightarrow$ 1 | 9.246 | 0.0076 |
| 9 $\rightarrow$ 1 | 9.215 | 0.0053 |
| 10 $\rightarrow$ 1 | 9.194 | 0.0038 |

$^*$ Oscillator strength normalized to the $f$-value of the Ly$\alpha$ transition.

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**Fig. 6**—Theoretical $R$-values from APED (Smith et al. 2001), at the temperature of maximum formation of each triplet, plotted vs. $n_e$ for the three analyzed He-like triplets. The gray curves correspond to the theoretical values from Porquet et al. (2001).
and II Peg (Huenemoerder et al. 2001), the Ne Lyman series lines at 9.215 (9 → 1), 9.246 (8 → 1), and 9.291 (7 → 1) are readily discernible. Some lines of highly ionized Fe also probably blend with the Ne features at some level, although the dominant components appear fairly well centered on the expected Ne wavelengths. A simple fit to the Mg components of the HR 1099 in the HEG spectrum, ignoring the Ne blends, is illustrated in Figure 7 (top panel). It is clear from this figure that the fit to the intercombination line also encompasses a significant fraction of the Ne lines: ignoring these blends results in a spuriously large intercombination line flux.

In order to account for the blends, we constructed an empirical model of the region that included the major Mg xi lines, together with blending components. These components comprised four additional lines corresponding to the positions of the Ne Lyman series lines with upper levels \( n = 7, 8, 9, 10 \). While it is desirable to include explicitly any significant lines of Fe, this presents difficulties because the wavelengths of the relevant Fe lines in this region are poorly known. To our knowledge, the best wavelengths currently available for this particular region are those predicted by the APED database, and these are based primarily on theoretical calculations, rather than on experiment. The model itself was constrained by comparison with, and by fitting to, co-added HEG spectra with the highest S/N (β Ceti, TZ CrB, AR Lac, and HR 1099). Since Fe features might distort and displace the centroids of the Ne features, in the fitting process we allowed the wavelengths of the four blends to vary. Line widths were all constrained to the same value, and the wavelength separations of the Mg lines were also fixed at their accurately known theoretical values.

In Figure 7 we show the best-fit model together with the individual components superimposed on the co-added HEG spectra. The wavelength intervals between the blends and the Mg xi resonance line found from this fit were then fixed into the model, which was then tested on the co-added MEG spectra of the same four sources. The latter fit, which is also illustrated in Figure 7, provided an excellent match to the MEG spectrum and yielded relative line fluxes in agreement with the HEG values to within statistical uncertainties. The individual wavelengths of the different line and blend components in the final model of the Mg xi spectral region determined in this way from the co-added HEG spectra are listed in Table 5, together with the identifications we attribute to the features.

While the blending components include the contribution of all the Ne lines of the Lyman series present in this spectral range, there are doubtless contributions at some level from Fe lines, and we list candidates in Table 5. The relative strengths of the Ne Lyman lines for the higher \( n \) transitions should scale in proportion to the oscillator strengths of the transitions. This appears to hold for those with upper levels \( n = 7, 8, \) and 9; however, the 10 → 1 transition at 9.194 Å appears too strong and is shifted slightly blueward of its predicted location. Examination of the APED database reveals an Fe xxi transition in this vicinity that we attribute to this. In comparison to this Fe xxi line, other potential Fe blends predicted in APED appear significantly weaker by factors of at least 3 and are likely less significant. The wavelengths fitted for the other blend components also remained very close to the values of the Ne lines, and the presence of further significant blends that we have omitted seems unlikely.

We compare in Figure 8 the \( R \) and \( G \) ratios obtained for the Mg xi triplet in each star for the case in which only the continuum and Mg xi lines themselves were included in the line fitting with the ratios obtained when we fitted the region using the model including blends. As expected, because the intensity of \( i \) is generally diminished compared to that of \( f \) in the latter approach, the effect is of raising the \( R \) ratio and slightly decreasing the \( G \) ratios compared to the former approach; i.e.,
including blends implies shifts toward lower derived densities and slightly higher temperatures.

As an additional test that our final Mg line fluxes, and especially those of the density-sensitive $i$ and $f$ pair, are not significantly affected by unseen blends, we have investigated the observed $i/f$ ratios as a function of both Ne and Fe relative line strength. As a measure of relative line strengths of Ne and Fe, we chose the ratios of the Mg xi resonance line with Fe xxiv $\lambda 12.29$, Fe xviii $\lambda 14.21$, and Ne x $\lambda 12.13$. The two lines of iron at different ionization stages provide tests at different temperatures, which could be important since the thermal structure of our sample stars that cover a fairly wide range in X-ray activity might be quite varied. The observed $R$ ratios are illustrated as a function of our control ratios in Figure 9.

We note from Figure 9 that the relative intensities of the chosen Fe and Ne lines with respect to the Mg resonance line span wide ranges of factors of 4–5 (Fe xviii, xxiv) and $\sim 15$ (Ne x). Both the thermal structure and the elemental abundances of the emitting coronae contribute to produce these differences; the Mg xi resonance line, for example, is formed at temperatures intermediate between those of Fe xviii and Fe xxiv. We might also expect some degree of correlation between coronal density and both temperature structure and chemical composition.

Of the three panels in Figure 9, only the Mg xi $R$ ratio variation as a function of Mg $r$/Fe xviii line strength appears completely flat, indicating an $R$ ratio that is independent of Fe xviii line strength. This is encouraging because Fe xviii can be considered a rough proxy for the coronal Fe abundance, and in the case in which remaining Fe blends were affecting our derived $R$ ratios, we would expect to see some correlation between the two. The hidden Fe lines that we might expect to blend with the Mg lines come from slightly higher ionization stages, however. In the case of Fe xxiv, the $R$ ratio appears somewhat higher for the very lowest Fe xxiv/Mg $r$ values, with a step to lower $R$ ratio for Fe xxiv/Mg $r > 1.3$. While the reason for this is not clear (as we emphasize above, both temperature structure and relative abundances play a role in the Fe/Mg and Ne/Mg ratios), we discount blends as the culprit because the trend in $R$ ratio remains flat while Fe xxiv/Mg $r$ varies by a factor of 3–4. The Fe xxiv $\lambda 12.29$ line is also sensitive to density and decreases in intensity with densities above several $10^{12}$ cm$^{-3}$. While this could contribute to the trend in Figure 9, we do not expect this to be a major effect since densities of order $10^{13}$ cm$^{-3}$ or more would be required; in the analysis described below we rule out such high densities based on our observed Si xiii $R$ ratios.

Perhaps the most interesting trend is that between $R$ and Ne x/Mg $r$; there does appear to be a weak correlation here, with Ne x/Mg $r$ increasing as the $R$ ratio decreases. At face value this might suggest residual Ne blending problems; however, the Ne Lyman series lines have very precise wavelengths and our blending model should accurately account for them. We conclude that the observed trend is real, i.e., that there is probably a weak trend of increasing Ne x line strength with increasing $R$ ratio. We return to this in § 4.

3.4. Results

Tables 6 and 7 summarize the results for the measured line fluxes and 1 $\sigma$ uncertainties for all the stars. The uncertainties were obtained from a full search of parameter space for each spectral fit. HEG and MEG line fluxes were found to differ beyond their 1 $\sigma$ uncertainties to a small degree. We first investigated to determine whether or not this could be the result of the spectral resolution difference between them, resulting in systematically different estimated continua, but were able to rule this out: the required continuum placement errors are implausibly large. Instead, we have found that similar flux differences are obtained by integrating spectral flux in arbitrary intervals across the bandpass. We attribute this to effective area calibration errors, which seem to be at the 10%–20% level at this time.9 Flux differences across the bandpass vary only very slowly with wavelength such that over narrow intervals the effect is gray and does not influence the measured line ratios.

Figure 10 shows examples of the HEG spectra in the region of the Si xiii He-like triplet for one star of each class: single

#### TABLE 5

| $\lambda_{\text{obs}}$ (Å) | Ion | Transition | Emissivity ($\text{photons cm}^{-2} \text{s}^{-1}$) |
|--------------------------|-----|------------|------------------------------------------|
| 9.1689                    | Mg xi | $r$: $1s2p\,1P_{1} \rightarrow 1s^{2}\,1S_{0}$ | $1.10 \times 10^{-18}$ |
| 9.1900                    | Fe xxiv | $1s^{2}2s2p^{3}\,3P_{1/2} \rightarrow 1s^{2}2s2p^{2}\,3P_{0}$ | $1.14 \times 10^{-17}$ |
| Fe xx | $1s^{2}2s2p_{3}\,2P_{3/2} \rightarrow 1s^{2}2s2p^{3}\,3S_{1/2}$ | $3.29 \times 10^{-18}$ |
| Ne x | $10 \rightarrow 1$ | $1 \times 10^{-18}$ |
| 9.2187                    | Fe xx | $2s2p^{3}\,(\lambda 5d \, 2)F_{3/2} \rightarrow 2s2p\,3D_{3/2}$ | $1.63 \times 10^{-18}$ |
| Ne x | $9 \rightarrow 1$ | $1.4 \times 10^{-18}$ |
| 9.2304                    | Mg xi | $i$: $1s2p\,1P_{2} \rightarrow 1s^{2}\,1S_{0}$ | $1.60 \times 10^{-17}$, $2.23 \times 10^{-18}$ |
| 9.2467                    | Ne x | $8 \rightarrow 1$ | $2.1 \times 10^{-18}$ |
| 9.2882                    | Fe xx | $2s2p^{3}(\lambda 5d \, 4)P_{3/2} \rightarrow 2s2p\,3D_{3/2}$ | $3.1 \times 10^{-18}$ |
| Fe xxiv | $1s^{2}2s2p^{2}(\lambda 4d \, 4)D_{17} \rightarrow 1s^{2}2s2p^{2}\,2D_{3/2}$ | $1.37 \times 10^{-18}$ |
| 9.3144                    | Mg xi | $f$: $1s2s\,1S_{1} \rightarrow 1s^{2}\,1S_{0}$ | $5.31 \times 10^{-17}$ |

9 From the fit to the HEG co-added spectrum of β Ceti, TZ CrB, AR Lac, and HR 1099 shown in Fig. 7.
stars, giants, and multiple systems. We plot the different components of the best-fitting model (continuum emission and single spectral line features), together with their sum, superimposed on the data.

Analogously, Figures 11 and 12 show examples of the MEG spectra for the Mg $\text{xi}$ and O $\text{vii}$ He-like triplet regions, together with spectral fits. None of the spectra obtained for giant stars yielded significant O $\text{vii}$ line measurements. The spectrum of TW Hya is extremely interesting, since the forbidden line is essentially not detected, and thus it is the only case of line fluxes at the high-density limit for oxygen (see also § 4 and Kastner et al. 2002).

Figure 13 summarizes all the results obtained for the $R$ ratios for all the sources, plotted as a function of surface X-ray flux and X-ray luminosity. Some of the ratios, mostly from HEG spectra, are missing as a result of the low S/N of the relevant features (see Table 6). We use different symbols for different classes of sources as indicated in the figures. It is clear from these figures that HEG and MEG measurements are generally compatible within experimental uncertainties. The dashed lines of Figure 13 mark the low-density limits of the sensitivity of the different diagnostics; i.e., $R$ ratios consistent with the dashed lines to within experimental uncertainty provide only an upper limit to the plasma density, while those significantly below the limit provide density estimates (see Fig. 6).

At face value, all the Si $\text{xiii}$ $R$ ratios are compatible with the low-density ratio limit, $n_e \leq 10^{13}$ cm$^{-3}$. However, we note that a good fraction of the measured ratios lie above this limit. This suggests that either the theoretical low-density limit $R$ ratio is too low or some fraction of our observed $R$ ratios are spuriously high. We return to this in § 4.

For the Mg $\text{xi}$ triplet lines, formed at lower temperatures with respect to the Si $\text{xiii}$ lines, in many cases the $R$ ratio is lower than the low-density limit value and yields useful density diagnostics. The Mg $\text{xi}$ $R$ ratio versus surface flux (Fig. 13) shows a discernible trend that stars yielding high densities tend to have higher fluxes. One exception is the low surface flux supergiant Canopus ($F_X = 0.17 \times 10^5$ ergs cm$^{-2}$ s$^{-1}$), whose Mg triplet lines point to high density. An analogous trend appears in the figures illustrating the $R$ ratios versus X-ray luminosity; in particular, for the Mg $\text{xi}$ $R$ ratio this trend with
luminosity is even more pronounced than with surface flux. One exception is the late-type single star EV Lac, which, because of its late spectral type, has a relatively low X-ray luminosity but apparently high plasma density.

Since the He-like triplet features are mildly sensitive to temperature, in order to derive actual density values from the measured $R$ ratios, we need to determine the plasma temperatures at which the density-sensitive lines are formed. The natural choice would be to use the temperature-sensitive $G$ ratio; however, based on our measurements, the $G$ ratio seemed to yield temperatures systematically lower than what we would expect. The true temperature of line formation should reflect the density-sensitive temperatures at which the density-sensitive lines are formed. Since we discount the $G$ ratio; lower values of $R$ correspond to higher density (see Fig. 6). Data points from HEG measurements are shifted by +10% along the $x$-axis, to distinguish the error bars corresponding to HEG and MEG measurements for the same source, otherwise overlapping.

Fig. 9.—Investigation of possible correlations of the $R$ ratio with Fe or Ne intensity in order to check for blending effects on Mg triplet lines. The dashed line marks the limiting value of the $R$ ratio; lower values of $R$ correspond to higher density (see Fig. 6). Data points from HEG measurements are shifted by +10% along the $x$-axis, to distinguish the error bars corresponding to HEG and MEG measurements for the same source, otherwise overlapping.

4. DISCUSSION

The survey described here provides information on plasma densities in the X-ray–emitting coronae of a wide sample of stars. We feel in particular that our measured fluxes are robust and that the debinding procedure discussed in § 3.3 provides for much more accurate measurement of the density-sensitive Mg $\xi$ lines than has been presented in other studies to date.

4.1. Atomic Data

The derived plasma densities we discuss below depend on the predictions of atomic models, and it is natural to ask what systematic errors might be associated with converting the measured $R$ ratios into electron densities. In particular, our study highlights two potential problems with recent calculations of He-like emissivities for Si, Mg, and O.

In the case of Si, the APED-predicted low-density limit value of the $R$ ratio is about 50% lower than what we observe, assuming that the source plasmas are indeed at the low-density limit. The Porquet et al. (2001) predicted ratio is slightly higher (Fig. 6) although still discrepant with regard to our measured ratio. Instead, for Mg the low-density limit $R$ ratio from both APED and Porquet et al. (2001) agrees very well with the upper envelope of the observed ratios, as we would expect if some of the coronae were at the low-density limit and some comprised higher density plasma. The case of O $\nu$ is more difficult to evaluate, since it appears that all the measurements imply densities above the theoretical low-density limits, although some of these are of course not statistically significant.

The temperatures derived from the APED $G$ ratios of both Mg and O are much lower than we would expect for these temperatures as spuriously low and the ionization temperatures as slightly high, for simplicity in the derivation of densities we adopted the temperature of peak emissivity for both O $\nu$ and Mg $\xi$. It is worth emphasizing here that the $R$ ratio is only weakly dependent on temperature, and electron densities derived using all the different temperatures obtained with different methods yield density values that differ by a factor of at most 2, considerably lower in most cases than the statistical uncertainty associated with measurement errors in the $R$ ratio. The final density values as derived from the $R$ ratios are illustrated as a function of both X-ray luminosity and surface flux in Figure 15 and listed in Table 8.
coronal plasmas. In the case of O VII, the observed G ratios should have reached a limiting value of ~0.6 for most of the stars in our study, according to the APED emissivity ratio. The situation is improved for the case of the Porquet et al. (2001) ratios, although G ratio temperatures still seem too low.

While direct excitation dominates other mechanisms in populating the 1s2p 1P upper level of the resonance line, in the case of the forbidden line cascades from higher n levels are much more important. These cascade contributions predominantly come from dielectronic recombination. The G ratio is therefore quite sensitive to the balance between dielectronic recombination and direct excitation processes. Since our G ratio temperatures are too low, this suggests that either the model populations of the f and i upper levels are underestimated or the resonance line, r, 1P upper level population is overestimated. Considering that the predicted Si R ratio low-density limit seems too low to explain the observations, our results suggest that the culprit is likely in the cascade contributions and the equipartition between cascade rates into 1P and 3S. The size of the discrepancy we see suggests errors in the relative level populations of about 20% or so. As we noted earlier in connection with the comparison of Smith et al. (2001) and Porquet et al. (2001) predicted R ratios, uncertainties of at least 10% or so are clearly present in these calculations.
In this study we emphasize trends with the observed $R$ ratio itself, in addition to the values of the derived plasma densities. While it appears that only the Si $R$ ratio is significantly affected by the model discrepancies described above, it should be kept in mind in the following discussion that there is an inherent systematic uncertainty in converting the observed ratios to densities, in addition to photon counting statistics.

4.2. Densities

We characterize the general $R$ ratio and plasma density findings here as follows:

1. $R$ ratios and, consequently, plasma densities at temperatures of $\sim 10^6$ K are all very similar, with typical densities of $n_e \sim 2 \times 10^{10}$ cm$^{-3}$ and a scatter between different stars of approximately a factor of 2.

2. We find a trend of higher plasma density in sources with higher coronal temperatures and higher coronal X-ray luminosities. This trend is less obvious when cast in terms of surface flux and more obvious when viewed as a function of the ratio of X-ray to bolometric luminosities.

3. In all the stars studied, the observed Si xii $R$ ratios are above or similar to the predicted low-density limit. At face value this indicates that no star has a coronal plasma density $\geq 10^{13}$ cm$^{-3}$ at temperatures of $\sim 10^7$ K or higher.

The general finding of higher plasma densities at higher temperatures in active stars has already been suggested by the growing bulk of work from other EUV and X-ray observations of active stars (e.g., Bowyer et al. 2000 and Drake 2001 for summaries of EUVE studies; Brickhouse 2002; Sanz-Forcada et al. 2002, 2003a, 2003b; Huenemoerder et al. 2001; Argiroffi et al. 2003). Our survey here confirms the findings of the earlier work; the EUV studies were often not unambiguous, as a result of the possible influence of lines blending with the density-sensitive diagnostics (e.g., Drake 2001). Indeed, the upper limit of $n_e \leq 10^{13}$ cm$^{-3}$ imposed by Si xii for all stars of our sample casts doubt on findings from some Fe EUV line
ratios of densities $n_e \sim 10^{13}$ cm$^{-3}$, as reported, e.g., by Sanz-Forcada et al. (2003a), although we have to keep in mind possible inaccuracies in the theoretical Si xiii $R$ ratio.

The results for different groups of stars are summarized below. Among our results, coronal density estimates are presented here for the first time for several sources of our sample: the single dwarf EV Lac, the giants HD 223460, Canopus, and $\mu$ Vel, and the RS CVn systems TY Pyx and IM Peg. For the remaining sources, the results we obtain here are compared with findings of previous works in Tables 9 and 10.

### 4.2.1. Single Dwarfs

In single dwarfs, excluding the peculiar case of TW Hya that we discuss below, high density seems to be associated with the presence of evident flaring events as observed for AU Mic (Monsignori Fossi et al. 1996; Magee et al. 2003), Proxima Cen (Güdel et al. 2002), and EV Lac$^{10}$ (this work).

The results obtained for single dwarfs are generally compatible with the results present in the literature (see Table 9), at lower temperatures (2–3 MK), while some disagreement is present for higher temperatures (6–10 MK). For example, for the rapidly rotating zero-age main-sequence K0 dwarf AB Dor, our density estimates are in good agreement with the finding of Sanz-Forcada et al. (2003b), based on both \textit{XMM-Newton} and \textit{Chandra} spectra, although their estimate from Mg xii is slightly higher than our estimate, possibly because of the blending due to Ne and Fe that we have taken into account here. However, our results for Mg are somewhat in conflict with the analysis of Fe xix–xii lines in \textit{EUVE}, \textit{Chandra}, and \textit{XMM-Newton} spectra by Sanz-Forcada et al. (2002, 2003a), who find somewhat higher densities of $n_e \sim 10^{12}$–$10^{13}$ cm$^{-3}$.

In particular, the densities estimated from X-ray Fe lines by Sanz-Forcada et al. (2003a) span an order of magnitude. While it is possible that the slightly higher temperatures probed by these Fe lines could be characterized by significantly higher densities than the plasma responsible for the Mg xxi lines, the limits placed on the density by the Mg lines tend to rule out the presence of significant amounts of plasma at densities close to $10^{13}$ cm$^{-3}$.

#### 4.2.1.1. TW Hya

The same \textit{Chandra} HETG spectra of the pre–main-sequence T Tauri star TW Hya have been analyzed by Kastner et al. (2002), who reported similar results to those obtained here: the Mg xxi lines have not been detected, and the O vii lines yield $n_e \lesssim 10^{12}$ cm$^{-3}$. The O vii spectral region of TW Hya is strikingly different from the spectra of all the other sources in our sample that yield $n_e \gtrsim 10^{10}$ cm$^{-3}$. Stelzer & Schmitt (2004) analyzed \textit{XMM-Newton} observations of TW Hya at both high (with the Reflection Grating Spectrometer) and intermediate (with the European Photon Imaging Camera) spectral resolution, finding densities based on O vii in good agreement with our results and those

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{example_spectra.png}
\caption{Examples of analyzed spectral regions, as in Fig. 10, for MEG spectra in the Mg xii triplet region, for single stars (left), giants (middle), and binary systems (right).}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{example_spectra_o_vii.png}
\caption{Examples of analyzed spectral regions, as in Fig. 10, for MEG spectra of the O vii triplet region, for single stars (left) and binary systems (right). None of the spectra of giant stars yielded significant measurements. For better readability we omitted the error bars in the TW Hya spectrum.}
\end{figure}
of Kastner et al. (2002). Since, during the XMM-Newton observations, no clear flare is detected, Stelzer & Schmitt (2004) conclude that the unusually high density found in TW Hya is not due to any flaring activity. Echoing Kastner et al. (2002) and Stelzer & Schmitt (2004), the X-ray emission from TW Hya seems radically different from that typical of stellar coronae, supporting conjectures that it originates from a fundamentally different plasma, such as one heated by a shock at the bottom of an accretion column.

4.2.2. Single Giants

None of the spectra of the single giants analyzed here yielded useful measurements of the O vii lines. In the case of Mg xi, however, we find clear indication of high densities of a

![Graphs showing measurements and comparisons](image-url)

**Fig. 13.**—Measured $R$ ratios for the He-like emission triplets, Si xii (left), Mg xi (middle), and O vii (right), from both HEG (filled symbols) and MEG (open symbols) data, vs. the stellar X-ray surface flux (top) and the X-ray luminosity (bottom) for all the analyzed stars. The dashed line marks the limiting value of the $R$ ratio; lower values of $R$ correspond to higher density (see Fig. 6). Symbols as in Fig. 9.

**Fig. 14.**—Comparison between the temperatures derived from the $G$ ratio of He-like triplet lines and the temperatures derived from the ratio of the Ly$\alpha$ line of the H-like ion and the resonance line of the He-like ion, for Mg (left) and O (right). The dashed lines mark the locus of equal values. Symbols as in Fig. 9.
Fig. 15.—Plasma densities derived from the $R$ ratio of He-like triplets of Mg (top) and O (bottom) as a function of the surface X-ray flux (left) and vs. the X-ray luminosity (right). Error bars compatible with the lower and the upper limit of the density range of sensitivity of the $R$ ratio are represented by downward- and upward-pointing arrows, respectively. The upper limit symbols mark densities compatible with the low-density limit. Symbols as in Fig. 9.

| Source* | $n_e$ (cm$^{-3}$) | HEG | MEG | MEG | MEG |
|---------|------------------|-----|-----|-----|-----|
|         |                  |     |     |     |     |
| AU Mic  |                  |     |     | $<5.62 \times 10^{12}$ | $<5.62 \times 10^{11}$ |
| Prox Cen|                  |     |     | $<5.6 \times 10^{12}$ | $<5.6 \times 10^{12}$ |
| EV Lac  | $5.6^{+26}_{-6} \times 10^{12}$ | $5.6^{+4.6}_{-0.4} \times 10^{12}$ | $5.6^{+2.5}_{-1.4} \times 10^{10}$ | $5.6^{+2.5}_{-1.4} \times 10^{10}$ |
| AB Dor  | $<3.2 \times 10^{13}$ | $<1.8 \times 10^{12}$ | $<7.8 \times 10^{11}$ | $<7.8 \times 10^{11}$ |
| TW Hya  |                  |     |     |     |     |
| HD 223460 |                  |     |     | $3.2^{+2.5}_{-1.4} \times 10^{12}$ | $3.2^{+2.5}_{-1.4} \times 10^{12}$ |
| 31 Com  | $5.6^{+26}_{-6} \times 10^{12}$ | $5.6^{+4.6}_{-0.4} \times 10^{12}$ | $5.6^{+2.5}_{-1.4} \times 10^{10}$ | $5.6^{+2.5}_{-1.4} \times 10^{10}$ |
| $\beta$ Cet | $<1.8 \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ |
| Canopus |                  |     |     | $3.2^{+2.5}_{-1.4} \times 10^{12}$ | $3.2^{+2.5}_{-1.4} \times 10^{12}$ |
| $\mu$ Vel | $<5.6 \times 10^{12}$ | $<1.0 \times 10^{12}$ | $<1.0 \times 10^{12}$ | $<1.0 \times 10^{12}$ |
| Algol   | $<5.6 \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ |
| ER Val  |                  |     |     |     |     |
| 44 Boo  | $<5.6 \times 10^{12}$ | $1.0^{+0.8}_{-0.6} \times 10^{12}$ | $1.0^{+0.8}_{-0.6} \times 10^{12}$ | $1.0^{+0.8}_{-0.6} \times 10^{12}$ |
| TZ CrB  | $3.2^{+2.5}_{-1.4} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ |
| UX Ari  | $5.6^{+12}_{-5} \times 10^{12}$ | $10^{+4}_{-0.4} \times 10^{12}$ | $10^{+4}_{-0.4} \times 10^{12}$ | $10^{+4}_{-0.4} \times 10^{12}$ |
| $\xi$ UMa | $1.8^{+0.8}_{-0.6} \times 10^{11}$ | $3.2^{+0.6}_{-0.4} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ |
| II Peg  | $5.6^{+12}_{-5} \times 10^{12}$ | $5.6^{+0.8}_{-0.6} \times 10^{12}$ | $3.2^{+1.4}_{-1.2} \times 10^{10}$ | $3.2^{+1.4}_{-1.2} \times 10^{10}$ |
| $\lambda$ And | $<3.2 \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $<1.0 \times 10^{11}$ | $<1.0 \times 10^{11}$ |
| TV Pyx  |                  |     |     | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ |
| AR Lac  | $3.2^{+2.5}_{-1.4} \times 10^{12}$ | $<1.8 \times 10^{12}$ | $<1.8 \times 10^{12}$ | $<1.8 \times 10^{12}$ |
| HR 1099 | $3.2^{+2.5}_{-1.4} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ | $1.8^{+0.8}_{-0.6} \times 10^{12}$ |
| IM Peg  |                  |     |     | $3.2^{+2.5}_{-1.4} \times 10^{12}$ | $3.2^{+2.5}_{-1.4} \times 10^{12}$ |

* AU Mic through TW Hya are single dwarfs, HD 223460 through $\mu$ Vel are single giants, and Algol through IM Peg are active binaries.
### TABLE 9
Comparison of Derived Densities with Previous Work: Single Stars

| Source     | log $T^b$ (MK) | log $n_e$ (cm$^{-3}$) | Ion$^c$ | log $T^b$ (MK) | log $n_e$ (cm$^{-3}$) | Ion$^c$ | Data$^d$ | References |
|------------|----------------|-----------------------|---------|----------------|-----------------------|---------|-----------|------------|
| AU Mic     | 6.8            | <12.75                | Mg $xi$ | 7              | ~13                   | Fe $xxi$ | D         | 1          |
|            | 6.3            | <11.75                | O $vii$ | 6.3            | 10.0–10.3 (flaring)   | O $vii$ | C         | 2          |
|            |                |                       |         | 6.3            | ~9 (quiescent)        | O $vii$ | C         | 2          |
|            |                |                       |         | 5.3            | 10.7–11               | O $v$, O $iv$, Si $iv$ | D, E, F | 3, 4       |
| Prox Cen   | 6.8            | <11.75                | Mg $xi$ | 6.3            | ~11.6 (flaring)       | O $vii$ | C         | 5          |
|            |                |                       |         | 6.3            | ~10.3 (quiescent)     | O $vii$ | C         | 5          |
| AB Dor     | 6.8            | <12.25                | Mg $xi$ | 7              | 12–13                 | Fe $xxi$–$xxii$ | A, C, D | 6, 7       |
|            | 6.3            | 10.7±0.4              | O $vii$ | 6.3            | ~10.8                 | O $vii$ | A, C      | 8          |
|            |                |                       |         | 6.3            | ≥12                    | O $vii$ | A, C      | 9, 10      |
| HD 223460  | 6.8            | 12.5 ± 0.25           | Mg $xi$ | 6.3            | ~7                    | O $vii$, Ne $ix$, Si $xii$ | C | 11        |
| 31 Com     | 6.8            | 12.5 ± 0.25           | Mg $xi$ | 6.3            | 9.8–11.3              | O $vii$ | C         | 12         |
| β Cet      | 6.8            | 12.25±0.2             | Mg $xi$ | 7              | 11.9–13.1             | Fe $xix$–$xxi$ | D | 6          |
| μ Vel      | 6.8            | <12.25                | Mg $xi$ | 6.3            | ≥12                    | O $vii$ | F         | 13         |

$^a$ AU Mic through TW Hya are single dwarfs, and HD 223460 through μ Vel are single giants.

$^b$ Temperature of maximum formation of the ion emitting the density-sensitive lines used for the density diagnostics.

$^c$ Ion emitting the density-sensitive lines used for the diagnostics.

$^d$ A: Chandra HETGS; B: Chandra LETGS; C: XMM-Newton RGS; D: EUVE; E: FUSE; F: HST.

### TABLE 10
Comparison of Derived Densities with Previous Work: Active Binaries

| Source     | log $T^b$ (MK) | log $n_e$ (cm$^{-3}$) | Ion$^c$ | log $T^b$ (MK) | log $n_e$ (cm$^{-3}$) | Ion$^c$ | Data$^d$ | References |
|------------|----------------|-----------------------|---------|----------------|-----------------------|---------|-----------|------------|
| Algor      | 6.8            | 12.3±0.15             | Mg $xi$ | 6.1–6.3       | ~10.5                | N $vi$, O $vii$ | B | 1, 2       |
| ER Vul     | 6.8            | <12.3                 | Mg $xi$ | 7              | 12.2–12.8            | Fe $xix$–$xxi$ | D | 3          |
| 44 Boo     | 6.8            | 12±0.2                | Mg $xi$ | 7              | 12–14                | Fe $xix$–$xxi$ | D | 4          |
|            | 6.3            | 10±0.2                | O $vii$ | 6.3            | 10.0–10.8            | O $vii$ | A         | 5          |
| TZ CrB     | 6.8            | 12.3±0.15             | Mg $xi$ | 6.6–7         | 12.0–12.5            | Ne $ix$, Mg $xi$, Si $xii$ | A | 5          |
| UX Ari     | 6.8            | 13±0.03               | O $vii$ | 6.3            | 10.0–10.8            | O $vii$ | A         | 5          |
|           |    .          |                       |         | 6.6            | 12.1–12.9            | Fe $xix$–$xxi$ | D | 6          |
|           |    .          |                       |         | 6.1            | 9.8–10.8             | O $vii$ | B         | 1          |
| ξ UMa      | 6.8            | 12.5±0.15             | Mg $xi$ | 7              | 11.8–12.3            | Fe $xix$–$xxi$ | D | 3          |
|            | 6.3            | 10.3±0.2              | O $vii$ | 6.3            | 10.6–11.6            | O $vii$ | A         | 7          |
|           | .             |                       |         | 6.8            | 12.8–13.8            | Mg $xi$ | A         | 7          |
|            | .             |                       |         | 6.6            | 11–12                | Ne $ix$ | A         | 7          |
| λ And      | 6.8            | 12.3±0.15             | Mg $xi$ | 7              | 11.7–12.4            | Fe $xix$–$xxi$ | D | 6          |
| AR Lac     | 6.8            | 12.5 ± 0.5            | Mg $xi$ | 6.8            | ≤12.8                | Mg $xi$ | A         | 8          |
|           | 6.3            | 10±0.2                | O $vii$ | 6.3            | 9–12                 | O $vii$ | A         | 8          |
| HR 1099    | 6.8            | 12.3±0.15             | Mg $xi$ | 6.8            | 11–12                | Mg $xi$ | B         | 1          |
|            | 6.3            | 10±0.2                | O $vii$ | 6.6            | ≤11                  | Ne $ix$ | B         | 1          |
|            |                |                       |         | 6.3            | 10.1–10.6            | O $vii$ | A, B      | 1, 9       |
|            |                |                       |         | 6.3–7         | ≤11                  | Mg $xi$, Si $xiii$ | A | 9          |
|            |                |                       |         | 7              | ≤12–13               | Fe $xii$ | D | 9          |

$^a$ Temperature of maximum formation of the ion emitting the density-sensitive lines used for the density diagnostics.

$^b$ Ion emitting the density-sensitive lines used for the diagnostics.

$^c$ A: Chandra HETGS; B: Chandra LETGS; C: XMM-Newton RGS; D: EUVE.

$^d$ A: Chandra HETGS; B: Chandra LETGS; C: XMM-Newton RGS; D: EUVE.

References.—(1) Ness et al. 2002a; (2) Ness et al. 2002b; (3) Sanz-Forcada et al. 2003a; (4) Brickhouse & Dupree 1998; (5) Osten et al. 2003; (6) Sanz-Forcada et al. 2002; (7) Huenemoerder et al. 2001; (8) Huenemoerder et al. 2003; (9) Ayres et al. 2001.
few times $10^{12}$ cm$^{-3}$ for all the giants except $\mu$ Vel, for which both HEG and MEG measurements suggest that $n_e$ is compatible with the low-density limit ($n_e \approx 10^{12}$ cm$^{-3}$).

One remarkable result among the giants is that the coronal density in the case of the supergiant Canopus appears to be high—of order $3 \times 10^{12}$ cm$^{-3}$—indicated by Mg $\lambda I$ at temperatures $\sim 10^7$ K. Consequently, the surface filling factor is tiny—a few millionths of the stellar surface. We discuss filling factors for the sample as a whole in more detail below.

4.2.3. Active Binaries

Conspicuous among the active binaries is the clear indication of high densities ($n_e \gtrsim 10^{12}$ cm$^{-3}$) from the Mg line analysis for most systems. Most of the upper limits found correspond to HEG measurements that are generally affected by larger statistical uncertainties.

Several previous analyses of spectra of the active stars of our sample exist, as summarized in Table 10. EUVE spectra of active binaries were analyzed by Sanz-Forcada et al. (2001, 2002), who estimated plasma densities using Fe xix–xxii lines ($T \sim 10$ MK) and invariably found $n_e \sim 10^{12} - 10^{13}$ cm$^{-3}$. Other earlier EUVE results are summarized by Drake (2001) and Bowyer et al. (2000); Ness et al. (2002a, 2002b) presented an analysis of X-ray spectra obtained with the Chandra LETGS that provides a slightly higher sensitivity to the O vii lines than the HETG+ACIS-S combination.

Some inconsistencies exist between our and earlier results for high-temperature plasma ($\sim 10^7$ K). For example, Brickhouse & Dupree (1998) estimated $n_e > 10^{12}$ cm$^{-3}$ up to $\sim 10^{14}$ cm$^{-3}$, diagnosed from Fe xix–xxii ($T \sim 10$ MK) lines in EUVE spectra of 44 Boo. Again, our Si xiii, and possibly Mg xii, densities seem incompatible with the EUV estimates based on Fe lines, suggesting that the latter might be spuriously high. As previously mentioned, the effect of lines blending with the density-sensitive diagnostics (e.g., Drake 2001), or an inaccurate theoretical Si xiii $R$ ratio, might be responsible for this disagreement.

4.2.4. General Trends

Taking advantage of the large star sample analyzed, we investigated the presence of any specific trend related to the physical characteristics of the observed stars. We mainly concentrated on the results obtained from the Mg $\lambda I$ measurements, since this is the most complete sample.

We first investigated trends in $R$ ratio with stellar fundamental parameters effective temperature and surface gravity. A correlation with surface gravity might be expected, for example, because surface gravity dictates the density and pressure that would characterize the plasma under hydrostatic equilibrium. The underlying stellar effective temperature might be expected to have a more subtle influence on coronal gas properties. In fact, we did not find any evident trend of the measured $R$ ratios or derived densities with surface gravity or effective temperature. The most graphic illustration of this is when contrasting the giants, including the supergiant Canopus, and the dwarfs. $R$ ratios are indistinguishable between these groups.

Perhaps more surprising, we also do not see obvious trends of the measured $R$ ratio with rotation period or Rossby number. Instead, the only obvious trend in the $R$ ratios is with stellar X-ray luminosity and in the ratio of X-ray luminosity to bolometric luminosity, $L_X/L_{bol}$. The former trend is shown in Figure 13, where we illustrate the O vii, Mg $\lambda I$, and Si xiii $R$ ratios as a function of both $L_X$ and the surface flux $F_X$. While there is arguably no discernible trend in any of the ratios with $F_X$, the Mg $\lambda I$ ratio shows a decrease in $R$ ratio for $L_X > 10^{30}$ ergs s$^{-1}$ or so. It is tempting to see the same trend in the Si xiii $R$ ratio for $L_X > 10^{31}$ ergs s$^{-1}$, but there are simply too few observations at the highest X-ray luminosities. The O vii $R$ ratio is essentially the same for the whole range of surface fluxes and X-ray luminosities.

The trend of declining Mg $\lambda I$ ratio in more active stars becomes more clear when shown as a function of $L_X/L_{bol}$, as shown in Figure 16. We consider the derived densities for O vii and Mg $\lambda I$ as a function of $L_X$ and $F_X$ in Figure 15; a significant fraction of the measurements here formally yield upper limits to the plasma density, and these tend to obscure the results that are more obvious in Figure 13; it is only when the measured $R$ ratio sample is taken together that the trends clearly emerge. Nevertheless, the trend of increasing density derived from Mg $\lambda I$ is still apparent at $L_X > 10^{30}$ ergs s$^{-1}$ or so; below this value the results are characterized more by upper limits.

We emphasize that this trend of Mg $\lambda I$ ratio and derived density with $L_X$ is not determined by a possible selection effect related to the S/N of the HETG spectra; in fact, the relative error on the Mg $\lambda I$ $R$ measurement, $\delta(R)/R$, has no specific trend with $L_X$.

4.2.5. Density Correlated with Ne/Mg?

In § 3.3 we pointed out an apparent trend of measured Mg $\lambda I$ ratio with Ne $x$/Mg $\lambda I$ line strength seen in Figure 9. We do not believe that this trend is a result of residual blending; instead, we suggest that we are seeing a trend of coronal abundance variation in which the Ne/Mg ratio is higher in stars characterized by higher Mg $\lambda I$ $R$ ratios: higher density at temperatures of $\sim 10^7$ K. Such a result might be expected based on the emerging trend of coronal abundance anomalies in active stars. The coronae of RS CVn-type binaries, in particular, exhibit high Ne/Fe abundances compared to their expected photospheric compositions (see, e.g., reviews by Drake 2003; Audard 2003). Since we see in this study good evidence for a trend of decreasing Mg $\lambda I$ $R$ ratio with increasing $L_X/L_{bol}$, the correlation of Ne $x$/Mg $\lambda I$ line strength...
with Mg \( \alpha \) \( R \) ratio would be expected if the Ne/Mg abundance ratio increased with \( L_\gamma/L_{bol} \). While the Ne/Mg abundance ratio remains to be investigated thoroughly in the stars of our sample, the evidence from analyses to date summarized by Drake (2003) and Audard (2003) does suggest that the relative Ne enhancement increases with stellar activity.

4.3. Filling Factors

One of the most important aspects of density measurements is the associated insight into the structuring of the plasma and into the emitting volume. In the stellar application, we can also use the density information to investigate coronal filling factors. For coronal line emission we can write \( I_k^\text{obs} = \int V n_e G_k(T_n) dV \), for the intensity of a line \( k \) emitted by optically thin plasma. In the isothermal approximation we have \( I_k^\text{obs} = G_k(T_n) \text{EM} \), where \( \text{EM} = n_e^2 V \) is the volume emission measure and \( G_k(T_n) \) is the contribution function of the emission line \( k \). If we further assume that the plasma is at the temperature of maximum formation of the line \( k \), we end up with a lower limit for the EM of the plasma emitting that line. In turn, from EM we obtain an estimate of the surface coronal filling factor defined as

\[
f = \frac{V}{\mathcal{L} A_s} = \frac{1}{n_e^2 \mathcal{L} A_s} = \frac{I_k^\text{obs}}{n_e^2 G_k(T_n)} \frac{1}{\mathcal{L} A_s},
\]

where \( \mathcal{L} \) is the scale height of the emitting plasma and \( A_s \) is the surface area of the star. A possible choice of \( \mathcal{L} \) is given by the hypothesis that the emitting coronal plasma is confined in hydrostatic loops smaller than, or comparable to, the pressure scale height. Under this assumption we can use the scaling laws of a hydrostatic loop model, such as that of Rosner et al. (1978) for which \( \mathcal{L} \sim \sqrt{T/(1.4 \times 10^9)} \). In this way, from the measured densities and assuming a temperature equal to the temperature of maximum formation of the line, we can derive an estimate of the filling factors.

In Figure 17 we illustrate the surface filling factors, \( f \), derived from Mg \( \alpha \) as a function of the rotation period and of the Rossby number. There is a sharp increase in filling factor at rotation periods of 3–4 days, below which the filling factor appears to saturate at values of several percent of the stellar surface, and above which there is an approximately linear trend between logarithmic rotation period and filling factor. A rotation period of 3–4 days also marks the general location of coronal “saturation,” and the saturation of filling factor here is not a surprise. We note that Canopus, whose rotation period is not accurately known (e.g., Decin et al. 2003), is missing from Figure 17. Nevertheless, if its rotation period is of order several hundred days, it would not be out of place in the relation between filling factor and period for \( P_{rot} > 4 \) days.

Figure 18 illustrates the filling factors derived from both Mg \( \alpha \) and O \( \alpha \) lines versus X-ray luminosity and surface flux. In order to have a more complete sample and investigate the relation with X-ray emission, we assumed an electron density of \( 2 \times 10^{10} \) cm\(^{-3} \) for the stars whose O \( \alpha \) lines were not measurable. This is not unreasonable given that almost all the spectra of our active stars (with rare exceptions like the case of TW Hya) yield \( n_e \) close to this value; this estimate is also supported by analyses of Chandra LETGS and XMM-Newton observations of some of the sources of our sample for which we did not obtain O \( \alpha \) measurements, like 31 Com (Scelsi et al. 2004), Algol (Ness et al. 2002a), UX Ari (Ness et al. 2002b), and Prox Cen (Güdel et al. 2002). Nevertheless, it is notable that we find filling factors greater than 1 (a nonsensical value) for three of the active binaries (ER Vul, TY Pyx, and AR Lac) for which we assume the common density value, indicating that the true density at a few times \( 10^6 \) K in these stars must be higher than \( 2 \times 10^{10} \) cm\(^{-3} \) or that the assumed scale height is too low.

With some degree of scatter, the O \( \alpha \) filling factor, \( f_{O \alpha} \), is directly proportional to the X-ray surface flux. It is interesting that this filling factor begins to saturate, i.e., reach values between 0.1 and 1, at a mean surface flux of \( \sim 10^7 \) ergs cm\(^{-2} \) \( \text{s}^{-1} \). While our data are sparse here, this saturation of \( f_{O \alpha} \) seems to occur at surface flux values approximately 1 order of magnitude lower than the surface fluxes of the most active stars in the sample. The same value of surface flux, \( 10^7 \) ergs \( \text{s}^{-1} \text{cm}^{-2} \), was found for the areas of the solar surface covered with active regions by Withbroe & Noyes (1977). This suggests, then, that at plasma temperatures of up to a few times...
These "O vii saturated" stars are essentially covered in active regions possibly similar in nature to those of the Sun.

The behavior of the Mg xi filling factor is different. First, there is a clear break in the \( f_{\text{Mg xi}} - F_X \) relation at the same surface flux level, \( F_X \sim 10^7 \) ergs s\(^{-1}\) cm\(^{-2}\), as we see \( f_{\text{O vii}} \) saturate. At lower \( F_X \) levels, the \( f_{\text{Mg xi}} - F_X \) relation appears to have a shallower slope than that for \( f_{\text{O vii}} \) versus \( F_X \) although the level of scatter precludes a definitive statement.

Finally, we examine the relative behavior of the two filling factors, \( f_{\text{O vii}} \) and \( f_{\text{Mg xi}} \), in Figure 19. For \( f_{\text{O vii}} \lesssim 0.2 \), the two factors are approximately proportional to one another. For \( f_{\text{O vii}} \gtrsim 0.2 \), \( f_{\text{Mg xi}} \) increases much more sharply than \( f_{\text{O vii}} \). At higher activity levels (i.e., higher \( f \)) the coronae are preferentially filling with hotter plasma with respect to the cooler plasma emitting the O vii lines.

### 4.4. Summary

The density and filling factor results suggest a scenario that has been outlined before based on the emission measure distributions as a function of temperature of active dwarfs as compared to those of solar active regions by Drake et al. (2000; see also Güdel 1997): going toward activity levels higher than the Sun, the trend appears to be one of increased filling factor of solar-like active regions characterized by essentially the same plasma density of \( n_e \sim 2 \times 10^{10} \) cm\(^{-3}\). For these active stars, there is an attendant hot, high-density plasma with \( n_e \sim 10^{12} \) cm\(^{-3}\) whose contribution to the total X-ray increases toward higher activity stars.

As the surface becomes "saturated" with, or full of, active regions, with filling factors between 0.1 and 1, the nature of the corona begins to change. This surface saturation occurs at X-ray luminosities well below the highest observed for the most active stars, by 1 or 2 orders of magnitude. Drake et al. (2000) and Güdel (1997) suggested that interaction between adjacent active regions could give rise to increased flaring behavior, which is manifest as the growth of the hotter 10\(^7\) K corona characterized in the Mg xi \( R \) ratio by higher plasma densities and with a concomitant increase in the filling factor of this plasma.

The quite different gas densities found for "high" and "low" coronal temperatures reinforce the fact that the dominant
emission at these temperatures cannot originate from the same structures: models seeking to explain active coronae need to account for the increase in gas pressure with increasing temperature.

5. CONCLUSIONS

We have investigated the density of coronal plasma at different temperatures through the analysis of the He-like triplet of O, Mg, and Si in high spectral resolution X-ray observations obtained with Chandra of a wide sample of active stars. As in previous works in the literature (e.g., Brickhouse 2002; Ness et al. 2003), the unprecedented Chandra spectrometer resolution proves to be vital for an accurate analysis: in this work we have especially emphasized the effect of lines blending with the Mg xi triplet lines and the need to take these into account in order to obtain reliable measurements of the \( R \) ratio. Ignoring these blends results in \( R \) ratios significantly different from values obtained when blends are accounted for.

Our measured \( R \) and \( G \) ratios provide some insights into the propriety of recent theoretical calculations of the relative line strengths from He-like ions. In the case of Si xiii, we find some evidence suggesting that the low-density limit \( f/i \) ratios predicted by both APED and Porquet et al. (2001) are too low by 20%–40% or so based on our observed values. Temperatures inferred from theoretical \( G \) ratios also tend to be lower than expected. We tentatively identify the cascade contributions from dielectronic recombination as the likely culprit for modeling inaccuracies.

For most of the observed sources in which O vii yielded a useful \( R \) ratio measurement, we find for plasma at temperatures of a few times \( 10^6 \) K densities of \( \sim2 \times 10^{10} \) cm\(^{-3}\). Mg xi lines formed closer to \( 10^7 \) K yielded densities \( n_e \sim10^{12} \) cm\(^{-3}\), confirming the scenario outlined in the recent literature in which hotter \( (6-10 \text{ MK}) \) plasma is characterized by densities 2 orders of magnitude higher than the cooler plasma, and in which the latter has both temperature and density similar to those characterizing solar coronal active regions. No star shows good evidence for Si xii \( R \) ratios significantly below the theoretical low-density limits; while this might partly be a problem associated with the theoretical ratios, which appear too low, it seems clear that there are no stars with electron densities significantly above \( 10^{13} \) cm\(^{-3}\). This result casts some doubt on earlier studies based on Fe xx–xxii lines seen in EUVE spectra that suggested the presence of densities exceeding \( 10^{13} \) cm\(^{-3}\) in active stellar coronae.

We have found a distinct correlation between the measured Mg xi \( R \) ratio and X-ray luminosity, with lower \( R \) ratios and, by inference, higher densities found in more X-ray–luminous coronae. This trend is also visible as a function of the X-ray “production efficiency,” \( L_X/L_{bol} \). Instead, no correlations were found between \( R \) ratio and stellar parameters surface gravity and effective temperature, or with Rossby number.

The surface coronal filling factors obtained from our density estimates are significantly smaller for the hotter plasma with \( T \sim10^7 \) K, with \( f_{\text{Mg xi}} \sim10^{-4} \) to \( 10^{-3} \), than for the cooler \( (2-3) \times10^6 \) K plasma characterized by \( f_{\text{O vii}} \) values in the range \( 10^{-3} \) to 1. The remarkably small filling factors for hot plasma suggest the potential for studying X-ray rotational modulation using the hotter lines available in high-resolution X-ray spectra. In this regard, we note that Marino et al. (2003) have recently found for the first time X-ray rotational modulation in a supersaturated star; Orlando et al. (2004) also show that such rotational modulation may be present in the hardness ratio.

The O vii filling factor, \( f_{\text{O vii}} \), is found to be directly proportional to the X-ray surface flux and reaches values between 0.1 and 1 at a mean surface flux of \( \sim10^7 \) ergs cm\(^{-2}\) s\(^{-1}\), the same surface flux that characterizes solar active regions. Instead, at higher temperatures the \( f_{\text{Mg xi}}-F_X \) relation shows a break at the same surface flux level, \( F_X \sim10^7 \) ergs cm\(^{-2}\) s\(^{-1}\), after which it increases more strongly with increasing surface flux.

The density and filling factor results suggest the following picture: at plasma temperatures of up to a few times \( 10^6 \) K, stars with increasingly higher activity level become more and more covered with solar-like active regions with \( n_e \sim2 \times10^{10} \) cm\(^{-3}\). At the same time, there is a similar growth in hotter plasma with temperatures close to \( 10^7 \) K and with \( n_e \sim10^{12} \) cm\(^{-3}\). This hotter plasma is likely associated with continuous superimposed flaring activity associated with the active regions, analogous to the solar case. For stars at the “O vii saturated” level, when X-ray surface fluxes are similar to those of active regions on the solar surface, the whole star is essentially covered by active regions. Further growth in X-ray emission at higher activity levels still is in the form of increased flaring, probably arising because of the crowding of active magnetic structures on the stellar surface. This activity gives rise to a growth in the surface coverage of \( 10^7 \) K plasma at higher densities of \( n_e \sim10^{12} \) cm\(^{-3}\). This picture is essentially that described earlier by Güdel (1997) and Drake et al. (2000).

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