Interfacial instability of charged–end-group polymer brushes

Y. Tsori¹(a), D. Andelman² and J.-F. Joanny³

¹ Department of Chemical Engineering, Ben-Gurion University of the Negev - P.O. Box 653, 84105 Beer-Sheva, Israel
² Raymond and Beverly Sackler School of Physics and Astronomy, Tel Aviv University - Ramat Aviv, Tel Aviv 69978, Israel
³ Physico Chimie Curie, Institut Curie–Centre de Recherche (CNRS UMR 168, Université Paris IV)
26 rue d’Ulm, F-75248, Paris Cedex 05, France, EU

received 21 January 2008; accepted in final form 25 March 2008
published online 25 April 2008

PACS 61.25.H– Macromolecular and polymers solutions; polymer melts
PACS 41.20.Cv – Electrostatics; Poisson and Laplace equations, boundary-value problems

Abstract – We consider a polymer brush grafted to a surface (acting as an electrode) and bearing
a charged group at its free end. Using a second distant electrode, the brush is subject to a
constant electric field. Based on a coarse-grained continuum model, we calculate the average brush
height and find that the brush can stretch or compress depending on the applied field and charge
end-group. We further look at an undulation mode of the flat polymer brush and find that the
electrostatic energy scales linearly with the undulation wavenumber, q. Competition with surface
tension, scaling as q², tends to stabilize a lateral q-mode of the polymer brush with a well-defined
wavelength. This wavelength depends on the brush height, surface separation, and several system
parameters.

Copyright © EPLA, 2008

Introduction. – There are different ways to bind
copolymers to surfaces. Either by adsorption from solution
or grafting them onto the surface with a terminal group
or having an adhering block in case of block copolymers.
Such coated surfaces have many important applications
in colloidal and interfacial science. The polymer layer
can change the hydrophobicity of the surface, prevent
absorption of other molecules from solution and, in
general, plays an important role in colloidal suspensions
by preventing flocculation and aggregation of coated
colloidal particles [1,2].

A densely grafted polymer layer is called a polymer
brush. The layer is grafted irreversibly on a solid surface
by an end-group. Both neutral and charged polymer
brushes have been studied extensively in the last few
decades [3–11]. If there is no strong interaction between
the monomers and the surface, the brush properties are
mainly determined by the chain entropy. Neutral brushes,
to a large extent, are characterized by their height that
scales linearly with N, the polymerization index [4–7].
Charged polymer brushes depend in addition on the
charge density of the chain as well as the solution ionic
strength [8–13].

In this letter we aim at understanding another variant
of polymer brushes having a terminal charge group, Ze,
at their free end, where e is the electronic charge and Z
the valency (see fig. 1). The main advantage of having a
charged end-group is that we can control the layer height
and other properties by applying an external electric
field and varying it continuously. This field stretches
(or compresses) the chains and is in direct competition
with their elastic energy and entropy. Even without
any external field, we expect the brush to be affected
by the charged end-groups, because of their repulsive
interactions. Indeed, the height profile depends on the
charged group and an instability of the flat brush toward
an undulating one may occur.

Flat end-charged polymer brush. – Let us briefly
recall the equilibrium properties of a neutral grafted layer.
The condition of highly dense layers (the brush regime) is
ℓ ≪ Rg, where Rg is the chain radius of gyration, and ℓ is
the average distance between chains (fig. 1(a)). The brush
height, defined as the average distance of chain ends from
the substrate, is denoted by h. In the 1970s, a simple free
energy was proposed by Alexander and de Gennes [4,5] to
determine the layer equilibrium height. In the Alexander-
de Gennes model, the brush height is taken to be the same
for all chains; namely, the height distribution is stepwise.
Later, in more refined theories, the free-end distribution
was found to be parabolic [6,7]. In the present work we
remain within the stepwise distribution approximation,
Fig. 1: (a) Schematic illustration of a polymer brush with a terminal charged group. The polymer is grafted onto a flat and conducting surface at \( y = 0 \), while the other electrode at \( y = L \) provides an electrostatic potential difference \( V \), with an average electric field, \( E = -V/L \). Each chain end-group carries a charge \( Z_e \), the grafting chain density is \( \ell^{-2} \) and the average brush height is \( h \). (b) A continuum model of the brush used to calculate the electrostatic properties. The dielectric constant \( \varepsilon \) has the same value throughout the gap between the two electrodes. The chain end charges are bound to a two-dimensional layer, with a charge density per unit area, \( \sigma = Z_e/\ell^2 \).

which is adequate as long as the wavelength of the predicted instability (see discussion below) is larger than the width of the chain-end distribution [6,7].

The Alexander-de Gennes expression for the brush free-energy is

\[
F_{\text{brush}} = \frac{1}{6} K h^2 + \frac{k_B T}{2} v_0 \ell^{-2} N^2 h^{-1},
\]

where the entropic “spring” constant is \( K = 9 k_B T/(Na^2) \), \( a \) is the Kuhn statistical length, \( N \) the polymerization index, \( k_B T \) the thermal energy, and \( v_0 = a^3 (1 - 2 \xi) \) is the excluded-volume parameter depending on the Flory-Huggins parameter \( \chi \). For a neutral brush, minimization of \( F_{\text{brush}} \) with respect to the profile height \( h \) gives the well-known Alexander-de Gennes height of the brush at equilibrium \( h_0 \). It scales linearly with \( N \):

\[
h_0 = N \left( \frac{1}{6} v_0 a^2 \ell^{-2} \right)^{1/3}.
\]

Next, the end-charged brush is considered. As before, the chains are grafted onto the surface located at \( y = 0 \), but the surface is conducting and held at potential \( \psi = 0 \) (see fig. 1). At the other (free) end, the chains carry a charge \( Z_e \). Without loss of generality we will take this charge to be positive, \( Z_e > 0 \). A second conducting and flat surface at \( y = L \) is held at a potential \( \psi = V \) with respect to the surface at \( y = 0 \). Hence, the polymer brush is subject to a vertical average electric field \( E = -V/L \). For \( V > 0 \), the field is compressing the chains, while for \( V < 0 \), it is stretching them.

\footnote{The presence of a thin insulating layer to which the chains are grafted is not expected to change our results.}

Although the chain elastic deformation is considered explicitly, the electrostatic properties are calculated within a continuum model where the chains are coarse grained in the following way. The entire gap \( 0 < y < L \) between the two electrodes is assumed to contain the same dielectric medium with dielectric constant \( \varepsilon \). The discrete end-group charges are replaced by a two-dimensional layer having a continuous surface charge density. We assume that the continuum limit is adequate and provides a good description of the system electrostatics. Finally, we treat the charged brush without taking into account the presence of counterions. This assumption and the possible influence of counterions are discussed further below for a few relevant limits.

The electric field has a jump at \( y = h \), \( \Delta E(h) \sim \sigma/\varepsilon \), where \( \sigma = Z_e/\ell^2 \) is the layer charge density per unit area. For a typical grafting density \( \ell \approx 10 \, \text{nm} \), dielectric constant \( \varepsilon \approx 10 \, \varepsilon_0 \) with \( \varepsilon_0 \) being the vacuum permittivity and \( Z \approx 1 \), the electric-field jump is of order \( \Delta E \approx 10^7 \, \text{V/m} \approx 10^6 \, \text{V/m} \). Because the charged layer at \( y = h \) creates a discontinuity in the electric field \( E(y) \), the electrostatic problem is solved separately in two regions: the potential is marked as \( \psi \) in the region below the charged layer, \( 0 \leq y < h \), and as \( \psi_b \) for the region above it, \( h < y < L \). Solving the Laplace equation in the gap \( 0 < y < L \), we get

\[
\psi_a = b y, \quad 0 < y < h, \quad \psi_b = c + d y, \quad h < y < L,
\]

where the coefficients \( b, c, \) and \( d \) are determined from the boundary conditions: \( \psi_a \big|_{y=0} = 0 \), and \( \psi_b \big|_{y=L} = V \). At the charged layer itself \( y = h \), the potential is continuous, \( \psi_a \big|_{y=h} = \psi_b \big|_{y=h} \), and the jump in its electric field is proportional to the charge density \( \sigma \):

\[
b = \frac{V}{L} \frac{\sigma}{\varepsilon} (1 - h/L), \quad c = \frac{\sigma h}{\varepsilon}, \quad d = \frac{V - \sigma h}{\varepsilon L}.
\]

The total free energy can be written as the sum [14]

\[
F = F_{\text{brush}} - \frac{1}{2} \int \varepsilon (\nabla \psi)^2 \, d^3 r + \int \rho \psi \, d^3 r,
\]

where \( F_{\text{brush}} \) is the brush free energy, and the last two terms represent the electrostatic energy (in SI units). The volume charge density \( \rho \) is related to the surface one via the Dirac delta-function, \( \rho = \sigma \delta(y-h) \).

We first consider the case where the electrostatic interactions have a small effect on the thickness and we expand \( F_{\text{brush}} \) around its value at \( h_0 \) to second order in \( h-h_0 \). The resulting total free-energy per grafting site is

\[
F = \frac{1}{2} K (h-h_0)^2 - \frac{1}{2} \ell^2 \varepsilon \frac{V^2}{L} + \ell^2 \left( \frac{\sigma V}{L} + \frac{1}{2} \frac{\sigma^2}{\varepsilon} \right) h - \frac{1}{2} \ell^2 \sigma^2 h^2 + \text{const}.
\]
Minimization of $F$ with respect to the brush height $h$ yields the equilibrium brush height $h_{\text{el}}$ for the charged case:

$$h_{\text{el}} \approx h_0 \left(1 - \frac{\sigma^2 \ell^2}{K \epsilon} \left[ \frac{1}{2h_0} - \frac{1}{L} \right] - \frac{\sigma \ell^2 V}{K L h_0} \right).$$  \hspace{1cm} (7)

This expression is valid for low enough $\sigma$, i.e. when $\sigma^2 \ll K \epsilon h_0 / \ell^2$ and $\sigma V \ll K L h_0 / \ell^2$.

Note that the brush height is compressed, $h_{\text{el}} < h_0$, even when the external potential gap between the two electrodes vanishes, $V = 0$. In this case, the charges at the brush end-groups are attracted to the induced image charges on the two grounded electrodes, and the interaction with the closer electrode (at the origin) is stronger.

In the opposite case of strong charge-charge interactions, the brush height can be much smaller than $h_0$, which makes eq. (6) invalid. In this case, the brush free energy is dominated by excluded-volume interactions (last term in eq. (1)). In the limit $h \ll L$ the brush height is

$$h_{\text{el}}^2 = \frac{1}{2} k_B T v_0 \ell^{-4} N^2 \frac{1}{\left(\frac{\sigma L}{\ell^2} + \frac{\sigma^2 \ell^2}{K \epsilon} \right)}. \hspace{1cm} (8)$$

**Undulating charged brush.** – We now look for an interfacial instability of the brush layer. A classical interfacial instability occurs when two immiscible liquids are subjected to a perpendicular electric field. The instability is a result of dielectric constant or conductivity difference (or both) between the two liquids [15]. Here we focus on a different physical mechanism, resulting from repulsion between neighboring chains carrying identical charges. The electrostatic energy can be reduced if the chains compress or stretch alternatively, thereby increasing the distance between chain ends. This mechanism is at play even if the dielectric constants of the two media are the same. To make this point more evident, we take $\epsilon$ to be constant throughout the gap.

To investigate whether such an interfacial instability exists, consider the illustration in fig. 2. We assume that the brush height has a single undulation mode along one of the lateral surface dimensions, $x$:

$$h(x) = h_{\text{el}} + h_q \cos(qx), \hspace{1cm} (9)$$

where $h_{\text{el}}$ is the equilibrium location of a flat brush (eq. (7)), $q = 2\pi / \lambda$ is the modulation $q$-mode, and $h_q$ the amplitude. As was done above for the flat layer, the gap is divided into two regions and the potential is $\psi = \psi_a$ for $y < h(x)$ and $\psi = \psi_b$ for $h(x) < y < L$. The potential $\psi(x, y)$ satisfies Laplace’s equation $\nabla^2 \psi = 0$, with the following four boundary conditions:

$$\begin{align*}
\psi_a |_{y=0} &= 0, & \psi_b |_{y=L} &= V, \\
\psi_a &= \psi_b |_{y=h(x)}, \\
\sigma \hat{n} \cdot \nabla (\psi_a - \psi_b) |_{y=h(x)} &= \sigma_{\text{eff}}(x).
\end{align*} \hspace{1cm} (10)$$

Here $\hat{n} = \left(q h_q \sin qx, 1 / \sqrt{1 + (q h_q \sin qx)^2}\right)$ is a unit vector normal to the undulating interface given by $h(x)$. The density $\sigma_{\text{eff}}(x)$ appearing in the above boundary condition is: $\sigma_{\text{eff}} = \sigma / \sqrt{1 + (q h_q \sin qx)^2}$ and is related to the constant density $\sigma$ on the projected area, as defined in the previous section for the flat layer. Even within the uniform dielectric media assumption, we are able to show that the flat interface can be unstable. This demonstrates that the instability, due to charge-charge interactions, is different from other instabilities considered in refs. [16–18], and related to heterogeneous dielectric materials placed in external electric fields.

The potential within the polymer layer, $\psi_a$, and above it, $\psi_b$, are written as a power series in $h_q$:

$$\begin{align*}
\psi_a &= \sum_{n=0}^{\infty} \psi_a^{(n)}(h_q)^n, \\
\psi_b &= \sum_{n=0}^{\infty} \psi_b^{(n)}(h_q)^n.
\end{align*} \hspace{1cm} (11)$$

Clearly the Laplace equation is satisfied separately for each order $n$ in the expansion: $\nabla^2 \psi_a^{(n)} = 0$ and $\nabla^2 \psi_b^{(n)} = 0$. Note also that the zeroth-order terms, $\psi_a^{(0)}$ and $\psi_b^{(0)}$, are the solution of the flat charged layer (eqs. (3) and (4)). It then follows that for $n > 0$

$$\begin{align*}
\psi_a^{(n)} &= \sum_{k \neq 0} \left(a_k^{(n)} \exp(ky) + b_k^{(n)} \exp(-ky)\right) \cos kx, \\
\psi_b^{(n)} &= \sum_{k \neq 0} \left(d_k^{(n)} \exp(ky) + e_k^{(n)} \exp(-ky)\right) \cos kx.
\end{align*} \hspace{1cm} (12)$$

The leading contributions in $h_q$, the layer undulation amplitude, can be examined by assuming that $h_q \ll h_{\text{el}}$ and expanding the electrostatic free energy up to order $\sim (h_q)^2$. We therefore limit ourselves to the first order in $h_q$: $\psi = \psi^{(0)} + \psi^{(1)} h_q$. Furthermore, we focus on the long-wavelength limit, $q h_q \ll 1$, relevant to small amplitude modulations.

For linear order in $h_q$, only the first Fourier component $k = q$ does not vanish, and we find

$$\begin{align*}
a_q^{(1)} &= -b_q^{(1)} = -\frac{\sigma}{2\epsilon} \cosh q(L - h_{\text{el}}) \cosh qL, \\
d_q^{(1)} &= -e_q^{(1)} = \frac{\sigma}{2\epsilon} \cosh q h_{\text{el}} \sinh qL \sinh qL \sinh qL.
\end{align*} \hspace{1cm} (13)$$
Expanding to second order in \( h_q \), both the \( k = 0 \) mode and the second harmonics \( k = 2q \) do not vanish.

The electrostatic energy difference \( \Delta f_{\text{el}} \) (per unit area) between the undulating \( (h_q \neq 0) \) and the flat layer \( (h_q = 0) \) is given to second order in \( h_q \) by

\[
L_x L_z \Delta f_{\text{el}} = -\frac{\varepsilon}{2} \int \int dx \, dz \int_{y=0}^{y=h} dy \left[ 2 h_q \nabla \psi_{a}^{(0)} \cdot \nabla \psi_{a}^{(1)} + h_q^2 \left( \nabla \psi_{a}^{(1)} \right)^2 \right] \\
-\frac{\varepsilon}{2} \int \int dx \, dz \int_{y=h}^{y=L} dy \left[ 2 h_q \nabla \psi_{b}^{(0)} \cdot \nabla \psi_{b}^{(1)} + h_q^2 \left( \nabla \psi_{b}^{(1)} \right)^2 \right] \\
+ \sigma h_q \int \int dx \, dz \left[ a_q^{(1)} \exp(qh) + b_q^{(1)} \exp(-qh) \right] \cos qx,
\]

where \( L_x \) and \( L_z \) are the two lateral dimensions and \( h \) is \( h(x) \) from eq. (9). Straightforward algebraic manipulations give the final answer for the electrostatic energy difference per unit area of the brush in the long-wavelength limit \( (qh_q \ll 1) \):

\[
\Delta f_{\text{el}} = -\frac{\sigma^2}{\varepsilon} \frac{\cosh(qh_{\text{el}}) \cosh[q(L - h_{\text{el}})]}{\sinh(qL)} q h_q^2.
\]

The scaling of the last expression could have been guessed from the outset. The electrostatic energy is symmetric in \( h_q \rightarrow -h_q \) and, to lowest orders, is quadratic in \( h_q \). In addition, the prefactor \( \sigma^2/\varepsilon \) has dimensions of dielectric constant times electric field squared, and thus \( \Delta f_{el} \) must be linear in \( q \). The derivation above gives us in addition the numerical factors and an extra dependence containing trigonometric functions. These functions are symmetric with respect to the transformation \( h_{\text{el}} \rightarrow L - h_{\text{el}} \).

Note that the externally imposed potential \( V \) does not appear explicitly in \( \Delta f_{el} \). The external field simply stretches the brush uniformly, thereby increasing \( h_{\text{el}} \).

The interfacial instability is solely due to charge-charge interactions, as exemplified by the \( \sigma^2 \) prefactor. The simple case of a thin isolated charged layer embedded in an infinite medium of uniform dielectric constant is obtained in the symmetric limit \( h_{\text{el}} = \frac{1}{2} L \), and \( L \rightarrow \infty \). In this case one finds \( \Delta f_{el} = -\left(\sigma^2/2\varepsilon\right) \cdot q h_q^2 \).

**Brush surface instability.** – The brush instability mentioned above causes a deformation of the flat layer and costs interfacial and elastic energy. We consider first the effect of surface tension and then comment on the elasticity. For a single \( q \) mode, the interfacial energy per unit area is \( \Delta f_{\text{s}} = \frac{1}{2} \gamma q^2 h_q^2 \). The total free-energy difference \( \Delta f = \Delta f_0 + \Delta f_{el} + \Delta f_{\text{s}} = \frac{\sigma^2}{\varepsilon} \cosh(qh_{\text{el}}) \cosh[q(L - h_{\text{el}})] q h_q^2 + \frac{1}{2} \gamma q^2 \).

\[
\Delta f_{\text{s}} = \frac{\sigma^2}{\varepsilon} \frac{\cosh(qh_{\text{el}}) \cosh[q(L - h_{\text{el}})]}{\sinh(qL)} q^2 + \frac{1}{4} \gamma q^2.
\]

\( \Delta f \) has a minimum at a finite wave number \( q^* \) as seen in fig. 3(a), where \( \Delta f \) is plotted with a choice of typical parameter values. The value of \( q^* \) can be obtained by solving the transcendental equation

\[
q^* = \frac{2}{\gamma h_q^2} \frac{\partial \Delta f_{\text{el}}}{\partial q} \Bigg|_{q^*}.
\]

In fig. 3(b) we show the dependence of \( q^* \) on \( h_{\text{el}}/L \). The most stable wave number \( q^* \) decreases monotonically as \( h_{\text{el}} \) increases.

In order to check whether the predicted instability can be seen in experiments, we estimate its order of magnitude by taking the brush charge to be \( Z = 1 \), chain separation \( \ell = 10 \text{ nm} \), dielectric constant \( \varepsilon = 10\varepsilon_0 \) and surface tension of the brush layer \( \gamma = 1 \text{ mN/m} \). From fig. 3(b), we find \( q^* \approx 10^7 \text{ m}^{-1} \), resulting in an undulation wavelength \( \lambda^* = 2\pi/q^* \approx 0.63 \text{ nm} \). This long-wavelength limit indeed agrees with the various approximations we made. By further changing the system parameters: \( \ell, Ze \) and \( \gamma \) it is possible to tune \( q^* \) and adapt its value (in the micrometer range) in specific experimental setups.

**Discussion and conclusions.** – In this letter we revisit the problem of polymer brushes. The new feature considered was to attach a charge \( Ze \) to the chain terminal free-end. The brush can be grafted onto an electrode
the in-plane density can be modulated in the in-plane density can be

The charged brush creates an effective surface charge density that is localized at the $y = h$ interface. These charges repel each other and also interact with the external electric field. The equilibrium height $h_{el}$ depends on the competition between all electrostatic interactions and the elasticity and entropy of the neutral chain, as seen from eqs. (7) or (8). It can lead to a compression or expansion of the layer height with respect to the neutral brush case. However, the more interesting effect may be the onset of an instability in the layer height. Employing a linear stability analysis, the conditions leading to an instability of the uniform layer are analyzed, and a preferred wave number $q^*$ stabilized by surface tension is found. When elasticity of the polymer brush is included, it contributes a $q^4$ term in eq. (15) in addition to the $q^2$-term originating from surface tension. The qualitative system behavior is similar, with a modified expression for the preferred wave number $q^*$.

The full system behavior in the presence of counterions is quite complicated and should be explored in a separate work, especially the limit of highly charged brushes.

Here, we comment briefly on two extreme limits. In the first limit, the brush charge and the external potential are taken to be small enough so that the counterions are uniformly distributed throughout the available volume, and behave like an ideal gas. It then follows that the electrostatic potential depends quadratically on the direction $y$. In this approximation, the counterions do not contribute to the pressure difference $\Delta P$ across the brush end. The only source of pressure difference is electrostatic and is due to the difference in $\frac{1}{2} \varepsilon E^2$ between the two sides of the brush. We find $\Delta P = \sigma V/L + \sigma^2/\varepsilon - 3\sigma^2 h/\varepsilon L$.

In a second scenario, the brush charge is small, but the electrostatic energy of counterions in contact with the electrode, $eV$, is much larger than the thermal energy $k_B T$. Here we find that all counterions migrate to one of the electrodes. However, because the above calculation assumes a fixed voltage gap, $V$, the electrodes will accumulate extra charge to balance exactly the counterions. Therefore, the results in eqs. (6), (7) and (8) stay valid. Lastly, we point out that in a more physically feasible setup, the system may contain added salt [12,13]. In this case, the electric field is screened and the brush ends do not “feel” the electrodes as long as the brush length is larger than the Debye-Hückel screening length.

It is worthwhile to mention some similarities between our charged brush and other two-dimensional systems of charges or dipoles. A two-dimensional layer of electric dipoles pointing in the perpendicular direction was investigated [20] in relation with dipolar Langmuir monolayers at the water/air interface [20]. When the dipoles have a fixed out-of-plane moment but their in-plane density can vary, a modulated phase in the in-plane density can be stabilized with a preferred wave number $q^*$. In addition, the dipolar free energy also scales linearly in $q$ [20]. The similarity between the two systems can be understood in the following way. The charge displacement from their average position at $y = h_{el}$ in our case is similar to an effective dipole whose moment points “up” or “down” with respect to this reference plane. Increase in the external $E$ field in our system translates into an increase proportional to the average dipole strength in the dipolar system.

More recently [21], a $q$-mode instability was found for an electric double layer where a charge density bound to a surface was allowed to fluctuate laterally. The model is motivated by an experimental setup where charged amphiphiles coat heterogeneously a mica surface. In the experiment the surface contains patches of positive and negative charges but the overall surface charge (summed over all patches) remains zero. As the surface was placed in contact with a salt solution, a local electric double layer is formed. Positively and negatively charged counterions are attracted, respectively, to negative- and positive-charge domains, resembling our system as well as the undulating dipolar one [20,21].

We hope that the simple considerations mentioned here will motivate experimental studies of end-charged brushes where some of our predictions can be tested.

***

We would like to thank T. COSGROVE for suggesting us this problem and D. BEN-YAAKOV for helpful discussions. YT acknowledges support from the Israel Science Foundation (ISF) under grant no. 284/05, and German-Israeli Foundation (GIF) grant no. 2144-1636.10/2006. DA acknowledges support from the Israel Science Foundation (ISF) under grant no. 160/05 and the US-Israel Binational Foundation (BSF) under grant No. 2006055.

REFERENCES

[1] Evans D. F. and Wennerström H., *The Colloidal Domain: Where Physics, Chemistry, Biology and Technology meet* (Wiley-VCH, New York) 1999.

[2] Fleer G. J., Cohen Stuart M. A., Scheutjens J. M. H. M., Cosgrove T. and Vincent B., *Polymers at Interfaces* (Chapman & Hall, London) 1993.

[3] For a recent review, see Netz R. R. and Andelman D., *Phys. Rep.*, **380** (2003) 1, and references therein.

[4] Alexander S., *J. Phys. (Paris)*, **38** (1977) 983.

[5] de Gennes P.-G., *Macromolecules*, **13** (1980) 1069.

[6] Milner S. T., Witten T. A. and Cates M. E., *Macromolecules*, **21** (1988) 2610.

[7] Semenov A. N., *Sov. Phys. JETP*, **61** (1985) 733.

[8] Pincus P. A., *Macromolecules*, **24** (1991) 2912.

[9] Borisov O. V., Birshtein T. M. and Zhulina E. B., *J. Phys. II*, **1** (1991) 521.

[10] Israels R., Leermakers F. A. M., Fleer G. J. and Zhulina E. B., *Macromolecules*, **27** (1994) 3249.

[11] Miklavic S. J. and Marcelja S., *J. Phys. Chem.*, **92** (1988) 6718.
[12] Carignano M. A. and Szleifer I., Mol. Phys., 100 (2002) 2993.
[13] Gong P. and Szleifer I., Ind. Eng. Chem. Res., 45 (2006) 5466.
[14] Lifshitz E. M., Landau L. D. and Pitaevskii L. P., Electrodynamics of Continuous Media, 2nd edition (Butterworth-Heinemann, Boston) 1984.
[15] Melcher J. R. and Smith C. V., Phys. Fluids, 12 (1969) 778.
[16] Schäffer E., Thurn-Albrecht T., Russell T. P. and Steiner U., Nature, 403 (2000) 874.
[17] Schäffer E., Thurn-Albrecht T., Russell T. P. and Steiner U., Europhys. Lett., 53 (2001) 518.
[18] Lin Z., Kerle T., Russell T. P., Schäffer E. and Steiner U., Macromolecules, 35 (2002) 3971.
[19] Kosevich A. M., Lifshitz E. M. and Landau L. D., Theory of Elasticity, 3rd edition (Butterworth-Heinemann, Boston) 1986.
[20] Andelman D., Brochard F. and Joanny J. F., J. Chem. Phys., 86 (1987) 3673.
[21] Naydenov A., Pincus P. A. and Safran S. A., Langmuir, 23 (2007) 12016.