Process of Efficiently Parallelizing a Protein Structure Determination Algorithm

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Abstract—Computational protein structure determination involves optimization in a problem space much too large to exhaustively search. Existing approaches include optimization algorithms such as gradient descent and simulated annealing, but these typically only find local minima. One novel approach implemented in REDcRAFT is to instead of folding a protein all at the same time, fold it residue by residue. This simulates a protein folding as each residue exits from the generating ribosome.

While REDcRAFT exponentially reduces the problem space so it can be explored in polynomial time, it is still extremely computationally demanding. This algorithm does have the advantage that most of the execution time is spent in inherently parallelizable code. However, preliminary results from parallel execution indicate that approximately two thirds of execution time is dedicated to system overhead. Additionally, by carefully analyzing and timing the structure of the program the major bottlenecks can be identified. After addressing these issues, REDcRAFT becomes a scalable parallel application with nearly two orders of magnitude improvement.

Index Terms—Protein Folding, Residual Dipolar Coupling (RDC), Residual Dipolar coupling based Residue Assembly and Filter Tool (REDSRAFT), Message Passing Interface (MPI), Parallel Optimization.

I. INTRODUCTION

STRUCTURAL elucidation, including complete structures of individual domains of proteins as well as the assembly of biomolecular complexes, is often a requisite step in understanding fundamental physiological processes or in the design of drugs to combat disease. Therefore, the development of computational methods leading to rapid, cost-effective structure elucidation is an important task. In addition, it is important to develop methods that can simultaneously deal with internal motion in these assemblies. Motion on a physiologically relevant time scale has always been suspected to play an important role in the biological function. The breathing motion of myoglobin [1], [2], [3], [4] can be cited as a historic example. Traditionally, full characterization of intermolecular dynamics has been treated separately from structure elucidation, increasing the cost and time of these studies. Furthermore, conceptually, it is difficult to separate structure from dynamics since observables used for structure determination are perturbed by motion, and therefore any attempt at structure elucidation that disregards the dynamics (or vice versa) can produce faulty results [5]. Here we present a method of simultaneous characterization of structure and dynamics of polypeptide chains from mainly the analysis of residual dipolar coupling data. Residual dipolar couplings are observables obtained from Nuclear Magnetic Resonance (NMR) spectra that have come into use recently as a source of structural information [6], [7], [8], [9]. The tool we present is unique in its simultaneous consideration of motion and structure based on inherent sensitivity of the used data to motions over the broad range of timescales spanning physiological processes.

Structure determination protocols based primarily on RDCs are becoming more common and require new programs that operate in fundamentally different ways from those that use NOE data. Some of these have been put forward [10], [11], [12], [13]. However, information richness and complexity of RDC data continues to challenge the abilities of any single analysis tool in existence today. Additionally, rapid development of new experimental methods of acquiring RDC data with continuously improving accuracy and precision, necessitate the existence of a parallel pursuit of information extraction methods. In this report, we present REDCRAFT (REsidual Dipolar Coupling Residue Assembly and Filtering Tool), a new open source analysis tool that accommodates the analysis of RDC data for simultaneous structure and dynamics characterization of proteins and polypeptides. Although utility of the current version of REDCRAFT is limited in application to proteins, the same principles can easily be applied to carbohydrates and nucleic acids.

II. BACKGROUND AND ALGORITHM

A. Traditional Techniques

Many approaches attempt to optimize [14] the energy landscape [15] in order to determine the most favorable structure. Methods include gradient descent as implemented by Xplor-NIH [16] as well as simulated annealing [14]. However, these algorithms usually suffer from a limited search space and local extrema. The massive order of the problem therefore requires more innovative approaches outside of general optimization in order to more accurately determine a native structure.

B. REDcRAFT

One promising algorithm is implemented as REDcRAFT [17], [18]. This program attempts to fold the strand sequentially instead of attacking the problem all at once. It first considers all possible angles between each neighboring pair of residues. Many of these are initially eliminated through the use of a Ramachandran [19], [20] filter and a scalar coupling filter [21]. Residues are then added one at a time to the strand, each time considering only the most suitable combinations
Fig. 1. Stage 1 of REDcRAFT first reads in information about the protein fragment. It begins with the first pair of residues and generates a list of all possible φ and ψ angles with resolution R. This list is then reduced using Ramachandran and scalar coupling filters. The fitness of each remaining angle pair is calculated by using experimental RDC data stored in a file. The list is then sorted based on fitness and written to a file, and the process is repeated for every pair of neighboring residues.

of previous angles. By eliminating unfavorable combinations early in the algorithm, the search space of the problem is exponentially reduced.

The program can more specifically be broken up into two stages. The first stage is illustrated in Figure 1. The purpose of this stage is to take a protein sequence and generate a list of acceptable torsion angles by considering data from a pair of neighboring residues, based on the Ramachandran and scalar coupling filter. These lists are then sorted based on how closely they mimic experimental Residual Dipolar Coupling (RDC) data. These lists are stored as files, allowing trivial separation between the first and second stage of REDcRAFT.

Once the lists have been generated, the second stage of REDcRAFT attempts to fold the fragment by adding one residue each iteration, as illustrated in Figure 2. This is done by taking the M most favorable sets of angles for the section of the fragment that has already been evaluated, and crossing it with the M most favorable pairs of angles between the new residue and its attaching neighbor to create every possible combination. Each of these $M^2$ angle combinations are then evaluated for fitness to experimental data and sorted. This sorted list is then written back out as a file, to be used in the next iteration.

C. Search Space

Considering every angle from -180 to 180 degrees with a resolution of 10 degrees gives 36 possible angles. Each pair of residues has a φ and ψ angle between them, giving $36 \times 36$ possible combinations. Therefore a protein with 50 residues would have $36^{98}$ possible combinations.

$$C = \frac{(360/R)^2}{N-1}$$ (1)

Equation (1) gives the number of possible combinations $C$ with angle resolution $R$ in degrees and number of residues $N$. REDcRAFT however only considers the $M^2$ most favorable combinations at each iteration, so the total possible combinations with a search depth of $M$ is reduced to Equation (2)

$$C \leq (N - 1)M^2$$ (2)
This algorithm therefore runs in polynomial time, yet can still be very computationally intensive. An interesting note is that this runtime is not relative to angle resolution. However a fine resolution with a small depth \( M \) can lead to the rejection of possibly valid combinations, and a large resolution may not even consider valid combinations. Therefore it is desirable to have as large of a search depth as computationally possible.

### III. PARALLELIZATION STRATEGY

#### A. Environment

The initial implementation of REDcRAFT was written with a mixture of C, C++, and Perl. The core that calculates RDC fitness of each set of angles is illustrated in Figure 3 where three separate programs (NewGenpp, svd, and mysolve) written in C/C++ are tied together using intermediate files. This core is then wrapped with Perl scripts, one for each of Stage 1 and Stage 2. There are also auxiliary Perl scripts used for data extraction and filter application.

Message Passing Interface (MPI) [22] was chosen for the parallel implementation due to its standardization, speed over queue based systems, and flexibility for future enhancements that could make use of communication between nodes. Therefore the entire Stage 2 was implemented in C, with MPI used to scatter the angle combinations and gather the fitness calculations. The computer system used for data collection is a 32 node Linux Beowulf cluster [23], where each node has a single 932 MHz Pentium III processor and 1 GB of memory. During each run, processor usage is recorded at significant intervals of execution.

#### B. Algorithmic Analysis

Before optimization begins, one needs to determine where the most time is spent in a program. If the speed of a section of code that constitutes 5% of a program’s runtime is doubled, then a speedup of only 2.5% has been achieved, and the maximum theoretical speedup from this section could only be 5%. However if the speed of a section constituting 50% of the program’s runtime is doubled, a speedup of 25% has been achieved. Therefore it is crucial to determine where the most time is being spent, and why.

Since REDcRAFT consists of two easily separable stages, it is worthwhile to look at the individual runtimes. Stage 1 has runtime \( O(\frac{M}{N^2}) \) relative to angle resolution \( R \) for each residue, so given \( N \) residues the total runtime is given by Equation 3. Stage 2 however has runtime relative to search depth \( M \). Each iteration of Stage 2 has runtime \( O(M^2) \), so given \( N \) residues the total runtime is given by Equation 4. Therefore given \( M \gg \frac{360}{R} \), Stage 2 constitutes the majority of runtime.

\[
O\left(\frac{N}{R}\right) \quad \text{(3)}
\]

\[
O(N \ast M^2) \quad \text{(4)}
\]

#### C. Parallel Algorithm

Since Stage 1 of REDcRAFT only contributes to a small percentage of total runtime, optimization is focused on the second stage. Of particular interest is the core calculation of RDC fitness which is naturally parallel, providing the potential for good scalability. By distributing the list of \( O(M^2) \) angle combinations across \( NP \) nodes, the core calculation runtime can be reduced to \( (\frac{SR}{NP} + OP) \) where \( SR \) is the sequential runtime on a single node. \( OP \) is the parallelization overhead, such as time required for scattering and gathering [24] of data. This parallel algorithm is illustrated in Figure 4. Two questions arise from this however: How much of the total runtime is spent in this core, and how large is \( OP \)?

### IV. IMPLEMENTATION AND OPTIMIZATION

#### A. Initial Analysis

Our first examination focused on the ratio of user to system time for the running program. User time is time spent calculating, while system time is consumed by operating system overhead, such as memory allocation, file input and output, etc. [25], [26]. This time breakdown can be obtained by using standard system libraries. Figure 5 displays the composition of user and system time for search depths of 25, 50, and 100. Immediately it can be seen that approximately \( \frac{2}{3} \) of the execution time is spent on system overhead. A look at the core calculation implementation illustrated in Figure 5 explains where this extensive overhead originates. Information is passed to each of the three subprograms (NewGenpp, svd, and mysolve) using a total of five files. Each iteration performs five file reads and three file writes per data set. Therefore a search depth of 100 (with two data sets) requires the system to handle 100,000 file reads and 60,000 file writes for each residue.
Fig. 4. The calculation section of Stage 2 can be parallelized by distributing the angle combinations to multiple processors. After the angle lists are crossed, the resulting combinations are divided up and transferred to each of the $NP$ nodes to be used. After all nodes are finished calculating their local combinations, the results are transferred back to the head node which proceeds with the sorting step of Stage 2. Note that scattering requires the transfer of a list of angle sets, while gathering only requires a list of single values to be transferred. Therefore scattering is more costly than gathering, which can be seen in Figure 7.

Fig. 5. Individual user and system times with search depth $M$. Note that the sum of system and user time does not equal actual execution time. For example, a heavily loaded multiuser system may display the same system and user times as a fully dedicated system, but will have a longer real execution time due to the other running processes sharing the system.

### TABLE I

| Execution Time (s) | Depth $M$ | Intermediate Files | Internal Matrices |
|--------------------|-----------|---------------------|-------------------|
| 25                 | 59.4      | 13.2                |
| 50                 | 224.6     | 35.0                |
| 100                | 648.6     | 53.9                |

B. Removal of Intermediate Files

The first step of optimization is to reduce system overhead by removing the intermediate files depicted in Figure 5. The files b.k.in and PolyGly.out.txt are still read in, but only once for each residue instead of for every iteration. This is necessary because these files change depending on the current residue. However, there are generally less than 100 residues being analyzed, making the overhead negligible. Originally the three subprograms NewGenpp, svd, and mysolve were separate programs run using system calls, necessitating the use of intermediate files. This also adds the overhead required for the system to create a new process for each call [27]. This was addressed by compiling all three programs into the main program, modified to take matrices as arguments instead of reading and writing files. These three subprocesses are now accessed as function calls instead of system calls.

The implementation using internal data structures instead of intermediate files is much faster than the original, with sample runtimes documented in Table I. While actual runtimes can vary based on system load, these data were collected under similar conditions on an unloaded system and present a significant improvement. With the system overhead in the core of the algorithm reduced, the algorithm as a whole can be evaluated to identify which sections can be improved.
six major sections identified are described as follows:

- **Folded Angles**
  - The lists of angle combinations (stored in files) have been processed and trimmed to contain at most \( M^2 \) combinations.
- **Formatted**
  - The lists of all angle combinations and their calculated fitness have been written to a file. The standard Linux `sort` program is then called which sorts the file. Note that this is done using only a single node, as illustrated in Figure 6.
- **Crossed / Read**
  - The lists of angles have been read into the program and all combinations have been formed in memory.
- **Scattered**
  - The combinations of angles that each node needs to calculate have been distributed to the respective nodes. This section contributes to \( OP \), or parallelization overhead.
- **Calculated**
  - All angle combinations for each node have been calculated. This is done by the core of the program illustrated in Figure 3.
- **Gathered**
  - The calculated fitness for each geometry has been collected from every node. This section also contributes to the parallelization overhead \( OP \).
- **Written / Sorted**
  - The list of all angle combinations and their calculated fitness has been written to a file. The standard Linux `sort` program is then called which sorts the file. Note that this is done using only a single node, as illustrated in Figure 6.

Examples of this itemized analysis are shown in Figures 7 and 8. For each of these figures, the maximum user time out of all nodes was recorded for each section. These maximum values were then averaged for every residue iteration. So for a run with 14 residues, 14 individual maximum values are recorded and averaged for each section. Figure 7 illustrates the parallelization of the `calculated` section, and also the sequential runtime of the external sort. As more nodes are added, this sorting begins to dominate total runtime and causes sublinear speedup relative to the number of nodes.

Figure 8 shows the scalability relative to search depth \( M \). An interesting observation is that runtime does not reflect the quadratic relationship to \( M \) that is shown in Equation (4). Instead, runtime appears to increase linearly with respect to \( M \). This is due to each iteration combining a list of length \( M \) with the new list of angles that often has length less than \( M \). The length \( M_1 \) of the combination list for previous residues achieves the maximum length \( M \) after the first couple of iterations. Search depth \( M \) is only a maximum length, however, and the length \( M_2 \) of the angle list for the newly added residue is generally much smaller. Equation (4) can be broken down using \( M_1 \) and \( M_2 \) to become Equation (5). As search depth \( M \) increases, \( M_1 \) becomes much larger than \( M_2 \), making runtime effectively linear with respect to \( M \) given a fixed number of residues \( N \) as shown in Equation (5).

\[
O(N \times M_1 \times M_2)
\] (5)
### Table II

| Depth M | Execution Time (m) |
|---------|-------------------|
| 1000    | 3.6               |
| 2000    | 6.3               |
| 5000    | 17.2              |

\[ O(N \ast M_1), M_1 \gg M_2 \] \hfill (6)

**D. Parallelization of Sort**

By calling an external sorting routine, the entire list of all combinations is sorted on the head node only. This use of a nonparallel sorting algorithm reduces the scalability of the program, as shown in Figure 7. Recall that the runtime of Stage 2 with \( N \) residues and a search depth of \( M \) is quadratic with respect to \( M \), as shown by Equation 4. However, sorting requires \( O(nlgn) \) comparisons where \( n \) is the length of the list to be sorted [28]. Therefore the runtime of Stage 2 when considering the sorting section is given in Equation 7 where the second term is the sequential sort as illustrated in Figure 8. This means that as \( M \) increases, the sort will begin to dominate runtime.

\[ O(N(M^2 + M^2 lg(M^2))) \] \hfill (7)

Although a sort requires \( O(nlgn) \) runtime, a merge can be performed linearly in \( O(n) \). Therefore if each node sorted their sublist before sending it to the head node, the head node could then just merge the \( NP \) sorted lists together. A total of \( NP - 1 \) merges are required, producing \( O(M^2 \ast NP) \) runtime since the maximum size of the list is \( M^2 \). These merges can also be done in parallel, requiring only \( lg(NP) \) steps. The runtime for merging is negligible however, even on a single node. Given a sorting runtime of \( O(M^2 \ast N P \ast lg(M^2 \ast N P)) \) for each node (since their sublist is \( M^2 \) items long and mergesort is \( O(nlgn) \) [29]), the total runtime for the parallelized sort is shown in Equation 8. This sorting algorithm is illustrated in Figure 9. In addition to improved asymptotic runtime of the parallel sort, the entire list of angle combinations with calculated fitness can be sorted in memory and does not have to be written to the disk every iteration. While this only happens \( N \) times, these files get quite large and outputting them takes a noticeable amount of time.

\[ O(N(M^2 \ast N P \ast lg(M^2 \ast N P) + M^2 \ast NP)) \] \hfill (8)

**VI. Results**

Sample runtimes of REDcRAFT after optimized parallelization are given in Figure 10. Note that runtime dedicated to sorting has become negligible with the new parallelism. Although the parallelization overhead can be seen in the scattered section, it is also negligible compared to the performance increase given by the parallel calculated section. Also, the increase in overhead for each additional node decays as the number of nodes increases, due to Equation 5 which gives the amount of data transfer needed between nodes given a fixed search depth \( M \).

\[ \Theta\left(\frac{NP - 1}{NP}\right) \] \hfill (9)

Given the almost complete use of total runtime in the calculated section and the scalability of this section, the REDcRAFT algorithm as a whole becomes practically linearly scalable relative to the number of nodes. As illustrated in Figure 8 the algorithm also approaches linearity relative to the search depth. The runtimes of this optimized parallel algorithm are not even comparable to the original times, with some samples given in Table II. With a search depth of 1000 and fragment length of 14 the new algorithm finishes in under four minutes, and with a search depth of 5000 it finishes in under 20 minutes, while the initial implementation took hours to days.

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