The QUEST–La Silla AGN Variability Survey: Connection between AGN Variability and Black Hole Physical Properties

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Abstract

We present our statistical analysis of the connection between active galactic nucleus (AGN) variability and physical properties of the central supermassive black hole (SMBH). We constructed optical light curves using data from the QUEST–La Silla AGN variability survey. To model the variability, we used the structure function, among the excess variance and the amplitude from the Damp Random Walk (DRW) modeling. For the measurement of SMBH physical properties, we used public spectra from the Sloan Digital Sky Survey (SDSS). Our analysis is based on an original sample of 2345 sources detected in both SDSS and QUEST–La Silla. For 1473 of these sources we could perform a proper measurement of the spectral and variability properties, and 1348 of these sources were classified as variable (91.5%). We found that the amplitude of the variability (A) depends solely on the rest-frame emission wavelength and the Eddington ratio, where A anticorrelates with both λrest and L/LEdd. This suggests that AGN variability does not evolve over cosmic time, and its amplitude is inversely related to the accretion rate. We found that the logarithmic gradient of the variability (γ) does not correlate significantly with any SMBH physical parameter, since there is no statistically significant linear regression model with an absolute value of the slope higher than 0.1. Finally, we found that the general distribution of γ measured for our sample differs from the distribution of γ obtained for light curves simulated from a DRW process. For 20.6% of the variable sources in our sample, a DRW model is not appropriate to describe the variability, since γ differs considerably from the expected value of 0.5.

Key words: galaxies: active – methods: statistical – surveys

1. Introduction

Active galactic nuclei (AGNs) show time-variable emission in every wave band in which they have been studied. The characteristic timescales of the variability range from hours to years, with the shortest timescales being associated with shorter emission wavelengths. This can be understood in the context of the current AGN structure models, where ultraviolet (UV) and optical emission originates in an accretion disk around a supermassive black hole (SMBH) and nonthermal X-ray emission is produced in an inner hot plasma component (corona), which is geometrically much smaller and more concentrated than the accretion disk, and therefore able to show more rapid variability. Intensive monitoring of nearby AGNs suggests that short-term variability from the UV to the near-IR could be driven by the rapid changes in the X-ray flux, which illuminates the accretion disk producing the short-term UV/ optical variations, since small lags between optical and X-ray bands have been found in reverberation mapping (RM) analyses. However, it has been noticed that at timescales of months or years the amplitude of the UV/optical variability is larger than the amplitude of the X-ray variability, which implies that X-ray reprocessing is not the main source of the UV/optical variations, and intrinsic variability from the accretion disk is required (Krolik et al. 1991; Arévalo et al. 2008; Edelson et al. 2015; Lira et al. 2015).

Even though variability is one of the defining characteristics of AGNs, we do not completely understand the mechanisms that drive such variations. In particular, it is not clear yet how physical properties of the central engine (e.g., luminosity, black hole mass, Eddington ratio) are related to variability properties of the system (e.g., characteristic timescale, variability amplitude). If we can establish a firm statistical correlation between certain AGN variability features and some SMBH physical properties, we will be able to use the variability as a tool in the future to derive physical properties for huge samples of objects from dedicated synoptic surveys such as the Large Synoptic Survey Telescope (LSST; Ivezić et al. 2008). Several efforts have been made in the past to assess this issue, some of them restricting the analysis to small numbers of well-sampled light curves (e.g., Kelly et al. 2009, 2013; Simm et al. 2016; Smith et al. 2018), or studying large samples of sources through ensemble light-curve analysis, assuming that sources with similar physical properties would have similar variability features (e.g., Wilhite et al. 2008; Bauer et al. 2009; MacLeod et al. 2010; Caplar et al. 2017). In order to test whether this assumption is correct, we need to perform an analysis of well-sampled individual AGN light curves, with known physical properties. Hence, long and intensive campaigns are crucial.

An anticorrelation between the amplitude of the UV–optical variability and luminosity has been consistently observed by previous studies (e.g., Angione & Smith 1972; Hook et al. 1994;
Between 2010 and 2015 we carried out an AGN variability survey using the wide-field QUEST camera on the 1 m ESO–Schmidt telescope at La Silla Observatory, observing five extragalactic fields: Stripe82, Elais-S1, COSMOS, ECDFS, and XMM-LSS. These are some the most intensively observed regions in the sky, with a huge amount of ancillary data ranging from X-rays to radio waves. The aims of our survey are (1) to test and improve variability selection methods of AGNs and find AGN populations missed by other optical selection techniques (Schmidt et al. 2010; Butler & Bloom 2011; Palanque-Delabrouille et al. 2011), which is the subject of a forthcoming paper; (2) to obtain a large number of well-sampled light curves, covering timescales ranging from days to years; and (3) to study the link between the variability properties (e.g., characteristic timescales and amplitudes of variation) and physical parameters of the system (e.g., black hole mass, luminosity, and Eddington ratio). Cartier et al. (2015) presented the technical description of the survey, the full characterization of the QUEST camera, and a study of the relation of variability to multiwavelength properties of X-ray-selected AGNs in the COSMOS field.

In this paper we present our statistical analysis of the connection between AGN variability and physical properties of SMBHs. For the variability analysis we used light curves from the QUEST–La Silla AGN variability survey and derived physical properties from spectra taken from SDSS. We perform the spectral fitting using the procedure of Mejía-Restrepo et al. (2016, hereafter MR16), from which we could derive physical parameters and also line-fitting properties such as the FWHM of the emission lines and continuum luminosities. For the variability analysis, we used the same approach as in Sánchez et al. (2017, hereafter S17). In this work, we used single-object light curves, in order to test the claim that sources with similar physical properties have similar variability behaviors (as proposed by Vanden Berk et al. 2004; Wilhite et al. 2008; MacLeod et al. 2010; Caplar et al. 2017, among others).

The paper is organized as follows. In Section 2 we describe the optical imaging and spectroscopic data used for the analysis. In Section 3 we describe the different variability features used and report the results of the variability analysis for our sample. In Section 4 we explain the procedure followed to obtain the physical properties from the SDSS spectra and show the distribution of these parameters for our sample. In Section 5 we define the different subsamples used in our analysis. In Section 6 we show the results of our statistical analysis done to connect the variability and physical properties. In Section 7 we analyze the differences in the variability parameters of sources classified as broad-line QSOs and normal sources, as well as sources classified as radio-loud and radio-quiet. Finally, in Section 8 we discuss the physical implications of our findings and summarize the main results. The photometry reported here is in the AB system. We adopt the cosmological parameters $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_m = 0.3$, and $\Omega_\Lambda = 0.7$.

2. Data

2.1. Optical Light Curves

We reduced the data from the QUEST–La Silla AGN variability survey (hereafter QUEST) using our own customized pipeline, following the same procedure described by Cartier et al. (2015). The survey uses a broadband filter, the $Q$ band, similar to the union of the $g$ and $r$ SDSS filters. Our QUEST fields are much bigger than just COSMOS, ELAIS, etc., even though we use the same names for them, with a surveyed area of $\sim 7$ deg$^2$ per field. One of the advantages of our survey over other surveys was the very intense monitoring.
observing the fields every possible night (although with large observing gaps from 2010 to 2012 owing to telescope failures). On average we obtained between two and five observations per night, per every observable field. Individual images reached a limiting magnitude between \( r \sim 20.5 \) and 21.5 mag for exposure times of 60 and 180 s, respectively.

To calibrate the photometry, we used public photometric SDSS catalogs (Gunn et al. 1998; Doi et al. 2010) for the COSMOS, Stripe82, and XMM-LSS fields and public catalogs from the Dark Energy Survey (DES; Abbott et al. 2018) for the ELAIS-S1 and ECDFS fields. We then constructed light curves for all the sources from the SDSS and DES catalogs with detections in the QUEST data, using the same methodology as in Cartier et al. (2015). We decided to bin our light curves every 3 days, in order to reduce the noise in our light curves, produced by changes in atmospheric conditions and the relatively low quality of the QUEST camera, among other factors. We generated a total of \(~450,000\) binned light curves.

### 2.2. SDSS Spectra

Three of our fields (COSMOS, Stripe82, and XMM-LSS) have spectroscopic information from SDSS. We used the SDSS Data Release 14 Quasar catalog (DR14Q; Páris et al. 2018), in order to identify sources with a detection in QUEST already classified as quasars. We found 2345 sources with both QUEST light curves and SDSS spectra, classified as quasars in DR14Q; this sample inherits the selection criteria of SDSS. We downloaded the calibrated SDSS spectra from the SDSS Catalog Archive Server and then corrected the spectra by Galactic extinction using the maps of Schlegel et al. (1998) and the model of Cardelli et al. (1989). The wavelength coverage of the SDSS spectra ranges from 3800 to 9200 Å for SDSS and from 3650 to 10400 Å for the BOSS survey (Dawson et al. 2013), with a spectral resolution of 1500 at 3800 Å and 2500 at 9000 Å.

From the SDSS quasar catalogs we obtained the spectroscopic redshift \((z)\) for every source. We then used these redshifts to transform every light curve to the AGN rest frame: 

\[
t_{\text{rest}} = \frac{t_{\text{obs}}}{1 + z},
\]

where \( t_{\text{rest}} \) is the light-curve time at the rest frame in days and \( t_{\text{obs}} \) is the observed time. The following analysis has been done considering the light curves in rest-frame time.

### 3. Variability Analysis

#### 3.1. Variability Features

To characterize the variability of our sources, we used the same approach as S17. We used two parameters related to the amplitude of the variability, \( P_{\text{var}} \) and the excess variance \( (\sigma_{\text{rms}})^2 \), and two methods related to the structure of the variability, the SF and the DRW process. Here we describe briefly every feature. For further details see S17 and references therein.

\( P_{\text{var}} \) (McLaughlin et al. 1996; Paolillo et al. 2004; Young et al. 2012; Lanzuisi et al. 2014; Cartier et al. 2015; Sánchez et al. 2017) corresponds to the probability that the source is intrinsically variable. It considers the \( \chi^2 \) of the light curve and calculates the probability 

\[
P_{\text{var}} = P(\chi^2) \]

which is a measure of the intrinsic variability amplitude. It is calculated as 

\[
\sigma_{\text{rms}}^2 = \frac{(\sigma_{\text{LC}}^2 - \bar{\sigma}_n^2)}{m},
\]

where \( \sigma_{\text{LC}} \) is the standard deviation of the light curve, \( \bar{\sigma}_n \) is the mean photometric error, and \( m \) is the mean magnitude. We can associate an error for \( \sigma_{\text{rms}} \) due to Poisson noise, 

\[
\text{err}(\sigma_{\text{rms}}) = \frac{S_D}{(\bar{x}^2 \text{rms})^{1/2}},
\]

Following S17, we classify a source as variable if its light curve satisfies \( P_{\text{var}} \geq 0.95 \) and \( (\sigma_{\text{rms}} - \text{err}(\sigma_{\text{rms}})) > 0 \).

Kelly et al. (2009) proposed that a DRW process can be a good descriptor for AGN light curves. This process models a light curve with a stochastic differential equation that includes a damping term that pushes the signal back to its mean: 

\[
dX(t) = -\frac{1}{\tau} X(t) dt + \sigma_{\text{DRW}} \sqrt{\tau} c(t) dt + b dt,
\]

where \( \tau \), \( \sigma_{\text{DRW}} \), and \( b \) are the drift coefficient, the dispersion of the exponential damping, and the actual noise, respectively. 

\( \tau \) is defined as the characteristic timescale, and it is calculated as 

\[
\tau = \frac{\sigma_{\text{rms}}^2}{\text{err}(\sigma_{\text{rms}})^2}.
\]

Since our light curves have an observed time coverage of \( t_{\text{obs}} \leq 5 \) yr, while the characteristic timescale is expected to be of the order of hundreds of days, we decided to exclude \( \tau \) from our analysis.

The SF (Cristiani et al. 1996; Giveon et al. 1999; Vanden Berk et al. 2004; de Vries et al. 2005; Rengstorf et al. 2006; Schmidt et al. 2010; Palanque-Delabrouille et al. 2011; Graham et al. 2014; Cartier et al. 2015; Kozłowski 2016; Caplar et al. 2017; Sánchez et al. 2017) is a measure of the amplitude of the variability as a function of the time lapse between compared observations. It is defined as 

\[
\text{SF} = \frac{\sigma_{\text{rms}}}{t_{\text{obs}}}.
\]

Since we want to study individual light curves, we have to consider only those sources with sampling dense enough to get statistically significant variability features. Figure 1 shows the distribution of the number of epochs \( (#\text{epochs}) \) and rest-frame time length of our 2345 light curves with SDSS spectra. Following a similar approach to S17, we selected for our analysis those light curves with \( t_{\text{rest}} \geq 200 \) days, and in order to ensure a high number of epochs, we also selected those light curves with \( #\text{epochs} \geq 40 \). In the figure we can see that most of our sources satisfy these conditions. After we filtered our sample by the number of epochs and the length of the light curve, we ended with 1751 sources. Hereafter, we refer to it as the “well-sampled” subsample.
3.3. Biases of the Variability Features

Figure 2 shows the different measured variability features versus the light-curve properties (i.e., the number of epochs or the length in days). We can see that the SF parameters $\gamma$ and $A$ are practically unaffected by the light-curve length and the number of epochs. The excess variance $\sigma_{\text{rms}}$ is also unaffected by the light-curve sampling. On the other hand, $\sigma_{\text{DRW}}$ is affected by the length of the light curve and strongly affected by the number of epochs. This is quantified by the Spearman rank coefficient, which gives values of $-0.59$ ($p_{\text{val}} < 1e^{-8}$), $-0.3$ ($p_{\text{val}} < 1e^{-8}$), and $-0.41$ ($p_{\text{val}} < 1e^{-8}$) for the correlations of $\sigma_{\text{DRW}}$ with $\#\text{epochs}$, $t_{\text{rest}}$, and $t_{\text{obs}}$, respectively. We decided to use $A$ and $\gamma$ as the main features for our analysis, and we use $\sigma_{\text{DRW}}$ and $\sigma_{\text{rms}}$ as references.

3.4. Variability of Simulated Light Curves

In this work, we used the parameters of the SF as the main variability features; therefore, it is important to understand how these parameters respond to different factors.

In order to understand how the sampling of a given light curve affects the measurement of its SF parameters, we simulated artificial light curves, following a similar approach to S17 (see their Sections 5.3 and 5.4). We simulated light curves using the same sampling of the light curves shown in Figure 3. The light curve at the top of the figure (short light curve) has a length of 492 days and 39 observing epochs. The light curve at the bottom (long light curve) has 175 observing epochs and a length of 1659 days.

We simulated light curves from a DRW process with $\tau = 300$ days and $S_{\text{inf}} = 0.2$ mag. For each of the long and short light curves, we simulated 1000 light curves. Figure 4 shows the results of the SF parameters measured for the short and long simulated light curves. First of all, we can see that the distributions of the parameters measured for the short light curves have a larger dispersion than the values measured for the long light curves. For the case of the short light curves, the median, mean, and standard deviation of $A$ are 0.19, 0.22, and 0.12, respectively, and for $\gamma$ are 0.3, 0.32, and 0.21, respectively. For the case of the long light curves, the median, mean, and standard deviation of $A$ are 0.22, 0.23, and 0.07, respectively, and for $\gamma$ are 0.37, 0.37, and 0.14, respectively. From Figure 4, we can also see that there is a correlation between the measured parameters. For the case of the short light curves the Spearman rank coefficient is $\rho_s = 0.91$ ($p_{\text{val}} < 1e^{-8}$), and for the long light curves we have $\rho_s = 0.87$ ($p_{\text{val}} < 1e^{-8}$).

We tested whether other definitions of the SF show the same behavior, using the definition of Kozłowski (2016) and the “traditional” definition of Schmidt et al. (2010). The results were consistent with what was found for the Bayesian method of Schmidt et al. (2010). In addition, we simulated artificial light curves with a power-law PSD (assuming different values for the exponent), following the same approach as S17, and we found similar results.

We also tested whether longer light curves can solve the degeneracy between the SF parameters. We simulated 1000 light curves from a DRW process with $\tau = 300$ days and $S_{\text{inf}} = 0.2$ mag, with 7000 days and 700 epochs, and with a similar cadence to the long light curve of Figure 3. The Spearman rank coefficient of $A$ versus $\gamma$ is $\rho_s = 0.88$ ($p_{\text{val}} < 1e^{-8}$); therefore, the parameters are still correlated. The median, mean, and standard deviation of $A$ are 0.24, 0.24, and 0.04, respectively, and for $\gamma$ are 0.39, 0.39, and 0.07, respectively. In order to see whether the previous results are produced by the gaps in the data, we simulated 1000 light curves from a DRW process with $\tau = 300$ days and $S_{\text{inf}} = 0.2$ mag, with 7000 days of length and with observations every 10 days, obtaining similar results for the correlation between $A$ and $\gamma$.

We simulated white-noise light curves, with a standard deviation of 0.2 mag, in order to test whether the correlation between the SF parameters is also present for light curves with a constant PSD. The Spearman rank coefficient for the short
Along the axes we show the histograms of every parameter.

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Figure 3. Light curves with different number of epochs and length, but similar cadence.

Figure 4. SF parameters measured for 1000 light curves simulated from a DRW process with \( \tau = 300 \) days and different values of \( S_{\text{Finf}} \) (with the long sampling). The blue circles correspond to light curves simulated with \( S_{\text{Finf}} = 0.05 \), the red triangles correspond to light curves simulated with \( S_{\text{Finf}} = 0.1 \), and the yellow squares correspond to light curves simulated with \( S_{\text{Finf}} = 0.2 \).

Along the axes we show the histograms of every parameter for the different \( S_{\text{Finf}} \). The green solid line shows the position where \( \gamma = 0.75 \), and the magenta dashed line shows the position where \( \gamma = 0.5 \), the expected value for a DRW process.

As can be seen in Figure 5, no single value of the intrinsic amplitude \( S_{\text{Finf}} \) reproduces the entire parameter space, from which we conclude that the measured values of the amplitude correlate on average with the intrinsic amplitude.

Figure 6 shows the distribution of measured values of \( A \) for different input \( S_{\text{Finf}} \). We can see that we can recover the input amplitude value, but with larger dispersions for larger values of \( S_{\text{Finf}} \). Therefore, we can say that the amplitude measured with the SF is a good estimator of the intrinsic variability amplitude, albeit with significant scatter due to the degeneracy.

We also tested the effects of the source redshift in the measured parameters, since sources at higher redshifts have shorter rest-frame light curves for a given observed light curve (\( t_{\text{rest}} = t_{\text{obs}}/(1 + z_{\text{spec}}) \)). We simulated DRW light curves with \( \tau = 300 \) days and \( S_{\text{Finf}} = 0.2 \).

In order to account for the redshift of the source, we use the sampling of the long light curve of Figure 3, dividing the time by (1 + \( z_{\text{spec}} \)), for different values of \( z_{\text{spec}} \). We simulated 1000 light curves per value of
Figures 7 and 8 show the results for $A$ and $\gamma$, respectively. We can see that both values do not change with $z_{\text{spec}}$, but the dispersion of the measured values increases a little bit with redshift. We can also see that the measured value of $A$ is close to the input value (red dashed line in the figure), but the measured value of $\gamma$ is below the expected value. This is consistent with the findings of S17 (see their Figure 7).

From all these results, we can conclude that the $A - \gamma$ degeneracy is much lower for the case of light curves with a constant PSD. For the case of stochastic light curves, the broad distribution of the measured parameters is produced by the fact that light curves with a few months or years of coverage are not a good representation of the general behavior of variability with decorrelation timescales of months or years, or with power-law PSD, and by the $A - \gamma$ degeneracy. The correlation between the measured SF parameters is present independently of the SF definition used. We can reduce the effects of this degeneracy by using light curves with several years of length. Besides, we can conclude that the values of the amplitude of the variability obtained from the SF are a good estimation of the real amplitude, independently of the redshift of the source. On the other hand, for the case of $\gamma$, we must consider that if we measure a value between 0.0 and 0.75 we cannot discard a DRW process as the best model to describe the variability.

### 3.5. Variability of the QUEST Light Curves

Following the criteria that sources with $P_{\text{var}} \geq 0.95$ and $(\sigma_{\text{rms}}^2 - \text{err}(\sigma_{\text{rms}}^2)) > 0$ are classified as variable, 1579 of the well-sampled light curves are variable, which corresponds to 90.2% of the sample. Figure 9 shows the distribution of the SF parameters, for the variable sources of the well-sampled subsample. The weighted averages of the parameters are $\bar{A} = 0.21 \pm 0.12$ and $\bar{\gamma} = 0.64 \pm 0.22$. The median and the 15.9 and 84.1 percentiles of the measured values of $A$ are 0.19, 0.11, and 0.34, respectively. The median and the 15.9 and 84.1 percentiles of $\gamma$ are 0.53, 0.39, and 0.80, respectively. The measured values of $A$ are consistent with previous findings for optical variability (e.g., MacLeod et al. 2010; Schmidt et al. 2010; Cartier et al. 2015; Rakshit & Stalin 2017; Suberlak et al. 2017). From Figure 5 we can see that our measurements are consistent with amplitudes ranging between 0.05 and 0.2; however, there are some sources with larger amplitudes.
We can also see from Figure 10 that the strongest correlation is shown between $A$ and $\sigma_{\text{rms}}^2$. This can be produced by the sampling of the light curve, since several light curves have lengths in rest frame close to 1 yr (see Figure 1).

From Figures 9 and 10, we can see that the SF parameters are correlated. The Spearman rank correlation coefficient for $A$ versus $\gamma$ is $\rho_s = 0.62$ ($\rho_{\text{val}} < 1e-8$). In Section 3.4 we showed that this correlation is a product of the degeneracy in the SF parameters, produced by the stochastic nature of the light curves, the sampling of the light curves, and the SF method by itself. Therefore, it does not have any physical implication.

### 4. Spectral Analysis

#### 4.1. Host Galaxy Subtraction

For low-redshift sources ($z_{\text{spec}} \leq 0.8$) we can have a significant degree of host galaxy contamination in the optical SDSS spectra, depending on the brightness of the nucleus. We follow the simple procedure to subtract the galactic continuum of Greene & Ho (2005) and Kim et al. (2006), where the stellar continuum is modeled using the scaled spectrum of a K giant star. In order to know how much starlight must be subtracted from the spectra, we use the equivalent width (EW) of the Ca II K absorption line ($\lambda = 3934$).

We isolated the AGN component only for those objects with $z_{\text{spec}} \leq 0.8$ (349 sources), since for sources with $z_{\text{spec}} > 0.8$ we can ensure the presence of the Mg II line in the SDSS spectra, and the H$_α$ line would be located in the edges of the spectra. For 304 of these 349 sources, the quality of the spectra was good enough to obtain the AGN and host galaxy components (i.e., with $S/N$(Ca II K) > 10).

#### 4.2. Spectral Fitting and Measurement of Physical Properties

We used the procedure proposed by MR16 to estimate the black hole masses ($M_{\text{BH}}$), the luminosity at 5100 Å ($L_{5100}$), the accretion rate ($M$), and the Eddington ratio ($L/L_{\text{Edd}}$) for our AGNs. MR16 proposed new calibrations for the measurement of these physical properties from single-epoch spectra, by fitting the H$_α$, H$_β$, Mg II $\lambda2798$, and C IV $\lambda1549$ lines. Their method relies on the assumption of virialized broad-line region (BLR) kinematics and considers the FWHM of the line as a proxy to the virial velocity of the gas in the BLR ($V_{\text{BLR}}$). Additionally, the continuum luminosity in the proximity of the emission line is used to estimate the BLR radius by means of the empirical luminosity–radius relationship derived from several reverberation mapping experiments (e.g., Bentz et al. 2013). Their method models the broad emission lines with two broad Gaussian components, and for the case of doublet lines (Mg II and C IV) they use two additional Gaussians, which are separated by the theoretical wavelength doublet separation and are forced to have the same profiles and intensity of the other two Gaussians, which is valid for optically thick BLR clouds. For the case of H$_α$ and H$_β$ their method also includes a third narrow-line component, modeled with a single Gaussian, which accounts for the narrow-line-emitting region. To model the continuum emission of the AGNs, they followed the local approach described in MR16, which consists of fitting a single power law limited within two narrow pseudo-continuum windows around the emission line. For the case of the H$_β$ and Mg II lines, their method also includes the modeling of an iron pseudo-continuum, using an

![Figure 9: Distribution of the SF parameters $A$ and $\gamma$ for the variable and well-sampled sources.](image-url)
iron template, which originates from a large number of blended features of Fe II and Fe III (for further details see MR16).

The black hole mass is calculated as

\[ M_{\text{BH}} = \frac{fG^{-1}R_{\text{BLR}}V_{\text{BLR}}^2}{K(\lambda L_\lambda)^\alpha} = KL_{6200}^{1/2}l_{\text{FWHM}}^2. \]

The values of \( K \) and \( \alpha \) for every line can be found in Table 7 of MR16. The accretion rate is estimated from Equation (1) of Netzer & Trakhtenbrot (2014), as follows:

\[ 4\pi D_L^2 F_\nu = f(\theta) |M_8\dot{M}|^{2/3} \left( \frac{\lambda}{5100 \text{ Å}} \right)^{-1/3} \text{ erg s}^{-1} \text{ Hz}^{-1}, \]

where \( M_8 \) corresponds to \( M_{\text{BH}} \) measured in units of \( 10^8 M_\odot \), \( \dot{M} \) is the accretion rate in units of \( M_\odot \text{ yr}^{-1} \), \( D_L \) is the luminosity distance, and \( f(\theta) \) is the inclination-dependent term, which describes the orientation of the accretion disk to the line of sight.

We used the calibrations derived by MR16 to estimate \( L_{5100} \) from \( L_{6200}, L_{3000}, \) and \( L_{1450} \) (see their Table 5). From this, we estimated the Eddington ratio as

\[ \frac{L}{L_{\text{Edd}}} = \frac{C_{\text{BOL}}L_{5100}}{1.5 \times 10^{38}(M_{\text{BH}}/M_\odot)^{1.5}}, \]

where \( C_{\text{BOL}} \) is the bolometric correction. In this analysis we adopted \( C_{\text{BOL}} = 9.26 \) (see Shen et al. 2008; MacLeod et al. 2010 and references therein).

Mejía-Restrepo et al. (2018a) proposed new corrections for the estimation of \( M_{\text{BH}} \), which intend to account for the effect of
the unknown distribution of the gas clouds in the BLR. They suggest that the virial correcting factor is inversely proportional to the width of the broad emission line used to compute $M_{\text{BH}}$. This can be explained either by the line-of-sight inclination effect on a planar BLR or by radiation pressure effects on the BLR gas distribution (Kollatschny & Zetzl 2013). The corrected black hole mass is calculated as $M_{\text{BH}}^c = M_{\text{BH}}^{f} f$, with $f = (\text{FWHM}_{\text{abs}}/\text{FWHM}_{\text{obs}})^3$, where the FWHM line is the FWHM of the emission line. $\text{FWHM}_{\text{obs}}$ and $\beta$ are parameters calculated per every line (see Table 1 in Mejía-Restrepo et al. 2018a). We computed $M_{\text{BH}}^C$ for our sample and used it to calculate the corrected Eddington ratio ($L/L_{\text{Edd}}^c$). In the next sections we will compare our results when using both the original and the corrected black hole masses.

4.3. Spectral Properties of the Selected SDSS Spectra

We have a total of 2345 sources with SDSS spectra; however, not all of them have a signal-to-noise ratio (S/N) high enough to allow the fitting of the emission lines. In our analysis we only consider those spectra with a mean S/N per pixel, in the continuum region around the emission line of interest, larger than or equal to 10. We also exclude from our analysis those sources classified as broad absorption line (BAL) QSOs in the catalogs of Shen et al. (2011), Pâris et al. (2017), and Pâris et al. (2018), with strong absorption lines in the region of the emission line under analysis. After we eliminated sources from our sample with low S/N and classified as BAL QSOs, we end with 102 sources having Hα inside the SDSS wavelength coverage, 304 sources with Hβ, 1561 sources with Mg II, and 801 sources with C IV. Most of our sources have more than one line available.

We fit the Hα and Hβ lines for sources with $z_{\text{spec}} < 0.8$. For 81 sources we could obtain a fit of Hα, and for 224 sources we obtained a fit of Hβ. In addition, we obtained a fit of Mg II for 1487 objects and a fit of C IV for 718 objects.

After the line fitting, we calculated $M_{\text{BH}}$, $L_{5100}$, $M$, and $L/L_{\text{Edd}}$ using the equations given in Section 4.2. We considered only those line fits where the height-to-noise ratio (H/N) of the line is H/N ≥ 5, with the height defined as the distance between the peak of the line fitted and the continuum. This is done to avoid the fit of fake lines when the broad lines are weak or are not present. Since for some objects we have more than one line available, we decided to estimate the final $M_{\text{BH}}$ as the weighted average of the measured $M_{\text{BH}}$ for the different lines, with the exception of the C IV line. It is well known that the C IV line width is not a good estimator of $V_{\text{BLR}}$, and therefore the measurements done using this line must be taken carefully (see MR16 and references therein). Therefore, whenever a source has C IV and other lines available, we excluded C IV from the estimation of $M_{\text{BH}}$, and we only consider the results of C IV when there is no other line available. In the next sections, the analyses are done with and without the results of the C IV fitting.

Following the previous procedure, we computed $M_{\text{BH}}$ for 1899 sources and $L_{5100}$ for 1951 sources. Figure 11 shows the correlations and individual distributions of $M_{\text{BH}}$, $L_{5100}$, $M$, and $L/L_{\text{Edd}}$, for all the sources with both $M_{\text{BH}}$ and $L_{5100}$ available (1899 sources). We measure the $M_{\text{BH}}$ in units of solar masses ($M_\odot$), $L_{5100}$ in units of erg s$^{-1}$, and $M$ in units of $M_\odot$ yr$^{-1}$, while $L/L_{\text{Edd}}$ is dimensionless. Our range covered for $M_{\text{BH}}$, $L_{5100}$, and $L/L_{\text{Edd}}$ is similar to that in previous variability analyses (e.g Wilhite et al. 2008; Kelly et al. 2009; MacLeod et al. 2010; Simm et al. 2016; Caplar et al. 2017).

The strongest correlations in Figure 11 are (a) $M$ and $L/L_{\text{Edd}}$, which is explained by the not particularly broad distribution of $M_{\text{BH}}$; (b) $L_{5100}$ and both $M_{\text{BH}}$ an $M$, which is related to the use of $L_{5100}$ in the determination of both quantities; and (c) $z_{\text{spec}}$ with $L_{1000}$, $M_{\text{BH}}$, and $M_{\gamma}$, which are mostly caused by a selection effect coming from the flux-limited nature of the observations.

Figure 12 shows the comparison of the $M_{\text{BH}}$ and $L/L_{\text{Edd}}$ measured using the standard single-epoch method, versus the measurements obtained using the new method proposed by Mejía-Restrepo et al. (2018a).

5. Final Sample Definition

Our final sample is composed of all those sources for which we could measure $M_{\text{BH}}$, $L_{5100}$, $M$, and $L/L_{\text{Edd}}$ and that have light curves with $t_{\text{rest}} \geq 200$ days and $\# \text{epochs} \geq 40$. We have 1473 sources in our original sample that satisfy all these conditions. We call this subsample the “QUEST-SDSS sample.” A total of 1348 of these sources are variable (91.5%).

We also define another subsample composed of all the sources with $M_{\text{BH}}$ determined from Hα, Hβ, or Mg II line fitting. We call this subsample the “not-C IV sample.” There are 1204 sources in this subsample, and 1112 are variable (92.4%).

The subsample composed of all the sources with $M_{\text{BH}}$ determined from Mg II line fitting is called the “Mg II sample.” There are 1108 sources in this subsample, and 1029 are variable (92.9%). For 107 of the sources of this sample, the Hβ line was available and used along with the Mg II line to estimate $M_{\text{BH}}$.

Finally, we define the subsample composed of all those sources whose only available emission line is C IV. We call this sample the “C IV sample”; 236 of the 269 sources in this subsample are variable (87.7%).

6. Variability Parameters versus Physical Properties

In this section we discuss the different correlations between the physical parameters measured from the SDSS spectra and the variability features measured from the QUEST light curves. For this analysis, we considered the different subsamples defined in Section 5, but in general, we worked with the most statistically significant results, which are found for the “not-C IV sample.”

6.1. Bivariate Correlations

We first analyzed the bivariate correlations between the variability features and the spectral properties, using the Spearman rank correlation coefficient ($\rho_s$), which does not consider error measurements in the variables. It is important to remember that variability features can depend on more than one spectral property, and they would define a hyperplane that is not seen “on-edge” but instead through a projection onto a specific axis. Therefore, some correlations can present large dispersions, even when there is a dependency of the variability feature on the spectral property.

Figure 13 shows the bivariate correlations between the variability features and the spectral properties. From the figure we can see that $\gamma$ shows no correlation with $z_{\text{spec}}$, $M$, and $L/L_{\text{Edd}}$ and a very weak correlation with $M_{\text{BH}}$ and $L_{5100}$. We
also see that $\sigma_{\text{DRW}}$ correlates weakly with $z_{\text{spec}}$ and anticorrelates weakly with $M_{\text{BH}}$, $L_{5100}$, $M$, and $L/L_{\text{Edd}}$. This is consistent with the findings of Kelly et al. (2009); however, we have to consider the strong effect of the light-curve properties in this parameter when we interpret these results. Finally, from the figure we see that $\sigma_{\text{rms}}^2$ anticorrelates weakly with $\dot{M}$ and $L/L_{\text{Edd}}$

Crucially, we see that $A$ correlates weakly with $z_{\text{spec}}$ and $M_{\text{BH}}$ and anticorrelates weakly with $\dot{M}$ and $L/L_{\text{Edd}}$. These weak correlations can be driven by the large dispersion produced by correlations with other variables. Moreover, we see a lack of correlation with $L_{5100}$, which is contrary to previous findings. It must be considered that the $A$ parameter is measured for sources located at different redshifts and therefore the wavelength of rest-frame emission ($\lambda_{\text{rest}}$) is different for every source. It is well known that the amplitude of the variability anticorrelates with rest-frame wavelength (see S17 and references therein), which implies a positive correlation with redshift. Since $L_{5100}$ correlates with $z_{\text{spec}}$ (Figure 11), the anticorrelation between $A$ and $L_{5100}$ can be hidden by the positive correlation of $A$ with redshift. Therefore, in order to detect correlations between $A$ and any physical property,
Instead of looking for bivariate correlations, we must perform a multivariate analysis.

### 6.2. Principal Component Analysis

Principal component analysis (PCA; Francis & Wills 1999) is a mathematical tool used to reduce the dimensionality of a data set, and it is useful to understand the correlations present in multivariate data. PCA decomposes the sample into a set of linearly independent eigenvectors that are linear combinations of the original variables. We performed a PCA on our data set, for the case of the “not-C IV sample,” in order to see the dependencies between the different SMBH physical properties and the AGN variability features. We homogenized the data set by subtracting the mean values and normalizing by the variance. In the analysis we did not include the accretion rate ($\dot{M}$) and the excess variance ($\sigma_{\text{rms}}$), since these variables are highly correlated with the Eddington ratio ($L/L_{\text{Edd}}$) and the amplitude of the SF ($A$), respectively, and including them in the analysis produces principal components (PCs) dominated by these correlations.

Table 1 shows the results of performing a PCA on the normalized variables. We show the first five PCs. The first row gives the variances (eigenvalues) associated with every PC. The second row gives the percentage of contribution of every PC to the total variance. The third row shows the cumulative percentage of variance carried by each eigenvector. It can be seen that the first four PCs together contribute ~95% of the variance. In Table 1 we also show for each PC the weights associated with every input variable (eigenvectors). It can be seen that the first PC is dominated by the positive correlations between redshift, luminosity, and BH mass. These correlations with redshift are produced by a selection effect, since at higher redshifts our sample will naturally contain more luminous and massive sources. The second PC is dominated by the anticorrelation between $L/L_{\text{Edd}}$ and the amplitude of the variability, measured from either the SF or the DRW process. The third PC is dominated by $\gamma$, and the fourth by $L/L_{\text{Edd}}$. The fifth component is not very informative, since it contributes a small fraction of the total variance.

In order to have a better idea of the degree of correlation between the input variables, we computed the Spearman rank coefficients between the input variables and the first four PCs. The results are shown in Table 2. We can see again that the first PC is dominated by the positive correlation between $z_{\text{spec}}$, $L_{5100}$, and $M_{\text{BH}}$. The second PC is dominated by the anticorrelation of the amplitude of the variability ($A$ and $\sigma_{\text{DRW}}$) with $L/L_{\text{Edd}}$ and $L_{5100}$. The third PC is dominated by $\gamma$ and demonstrates a positive correlation between $\gamma$ and $A$. In addition, the third PC shows a possible correlation between $\gamma$ and $L/L_{\text{Edd}}$. Finally, the fourth PC is dominated by $L/L_{\text{Edd}}$ and demonstrates an anticorrelation between $L/L_{\text{Edd}}$ and $M_{\text{BH}}$, which is expected from the definition of $L/L_{\text{Edd}}$. From these results we can conclude that the most important correlation between variability features and physical properties is for the case of the amplitude of the variability with $L/L_{\text{Edd}}$ and $L_{5100}$.

#### 6.3. Multiple Linear Regression

In the previous section we showed that the amplitude of the variability anticorrelates with $L/L_{\text{Edd}}$ and $L_{5100}$; however, from our PCA we cannot say whether the amplitude of the variability is mainly driven by $L/L_{\text{Edd}}$ or $L_{5100}$. Besides, it is still not clear whether $\gamma$ correlates with any physical property, but from the PCA there is a possible positive correlation between $\gamma$ and $L/L_{\text{Edd}}$.

In order to have a better idea of the correlations between variability parameters and physical properties, we computed Bayesian multiple linear regression. We used the Bayesian linear regression procedure of Kelly (2007), which takes into account the measurement uncertainties of every variable and includes the intrinsic scatter inherent to the relation. The following sections give the results of this analysis.

#### 6.3.1. Trends of the Amplitude of the SF with Physical Properties

In the previous section we showed that $A$ presents an anticorrelation with $L/L_{\text{Edd}}$ and $L_{5100}$; a multiple linear regression analysis can help us differentiate which physical property drives these anticorrelations.

$S17$ showed that there is a positive correlation between $A$ and $z_{\text{spec}}$, which is produced by an anticorrelation between $A$ and $\lambda_{\text{rest}}$ (see Figure 11 in S17). Therefore, given the wide range in redshift of our sample, we must always consider the correlation with redshift when we analyze correlations with any other physical parameter.

Table 3 shows the results of the Bayesian multiple linear regression for $A$ as the dependent variable and different combinations of the spectral properties as independent variables. In the table, every column gives the value of the intercept ($\alpha$), the slope ($\beta$) associated with a given physical property, and the intrinsic scatter associated with the regression.
When the value of the slope is replaced by $X$, it means that the parameter was not included in the regression model.

Regressions 1–5 in Table 3 correspond to models with one single independent variable. We see that the most significant correlations are for $z_{\text{spec}}$, $L/L_{\text{Edd}}$, and $M_{\text{BH}}$. Since $M_{\text{BH}}$ and $L/L_{\text{Edd}}$ are highly correlated (see Figure 11), and including these two variables together can produce multicollinearity in the regression model, we decided to exclude $M_{\text{BH}}$ from the regression models and keep $L/L_{\text{Edd}}$.

For regressions 6–10, we decided to include always $z_{\text{spec}}$ as one of the independent variables, because we are analyzing light curves observed in a fixed photometric band (Q), which implies that the rest-frame wavelength of every light curve will depend on the redshift of the source. Besides, we do not include in Table 3 a regression model with $z_{\text{spec}}$, $L_{5100}$, $M_{\text{BH}}$, and $L/L_{\text{Edd}}$ as independent variables, because the multicollinearity of the variables does not allow the Bayesian method to converge and return confident regression coefficients.

Regression 6 shows that when the model includes $z_{\text{spec}}$, $M_{\text{BH}}$, and $L_{5100}$, the slopes for $M_{\text{BH}}$ and $L_{5100}$ satisfy (within 1σ) the relation $\beta_{L_{5100}} \sim -\beta_{M_{\text{BH}}}$. This would be expected if $L/L_{\text{Edd}}$ were the driver of the amplitude variability.

Regression 11 corresponds to a model that includes both the Eddington ratio and redshift. We can see that the coefficients are statistically significant, and thus we propose this model as the best regression model for the amplitude of the variability.

In order to break the effects of the $A - \gamma$ degeneracy, we recomputed regression model 11 of Table 3, but considering only variable sources whose measured $\gamma$ range between

\begin{table}[h]
\centering
\begin{tabular}{lcccc}
\hline
 & PC1 & PC2 & PC3 & PC4 \\
\hline
Eigenvalue & 2.457 & 1.808 & 1.346 & 1.029 \\
Percentage & 35.1% & 25.8% & 19.2% & 14.7% \\
Cumulative & 35.1% & 60.9% & 80.1% & 94.8% & 98.5% \\
\hline
Variable & PC1 & PC2 & PC3 & PC4 & PC5 \\
\hline
$\log_{10}(1+z_{\text{spec}})$ & -0.520 & -0.118 & 0.231 & -0.318 & 0.706 \\
$\log_{10}(L_{5100}/10^{44})$ & -0.520 & -0.387 & -0.046 & -0.118 & -0.414 \\
$\log_{10}(M_{\text{BH}}/10^{8})$ & -0.572 & -0.001 & 0.171 & 0.366 & -0.262 \\
$\log_{10}(L/L_{\text{Edd}})$ & 0.131 & -0.478 & -0.289 & -0.644 & -0.158 \\
$\log_{10}(A)$ & -0.271 & 0.540 & -0.331 & -0.280 & -0.332 \\
$\log_{10}(\sigma_{\text{DRW}})$ & -0.202 & 0.213 & -0.749 & 0.097 & 0.343 \\
\hline
\end{tabular}
\caption{PCA Results: Eigenvectors and Eigenvalues}
\end{table}

Figure 13. Bivariate correlations between the variability features and the spectral properties, for the “not-C IV sample.” The Spearman rank correlation coefficient is shown as a reference for every pair of variables.
The dashed line shows the redshift from which we have available the Mg II line in the SDSS spectra.

### Table 2

| Variable                  | PC1        | PC2        | PC3        | PC4        |
|---------------------------|------------|------------|------------|------------|
| log₁₀(1+zₚₑₛₑ)           | -0.670     | -0.251     | 0.161      | 0.006      |
| log₁₀(L₅₁₀₀/10⁴⁴)         | -0.808     | -0.615     | -0.085     | 0.034      |
| log₁₀(Mₘ₈₉/10⁸)           | -0.932     | -0.066     | 0.243      | 0.643      |
| log₁₀(L/Lₐ₈₉)             | 0.192      | -0.712     | -0.465     | -0.831     |
| log₁₀(A)                  | -0.325     | 0.626      | -0.426     | -0.045     |
| log₁₀(γ)                  | -0.315     | 0.275      | -0.802     | 0.057      |
| log₁₀(Δ₁₈₉)               | 0.130      | 0.591      | 0.317      | -0.173     |

Note. The p-values of the coefficients are given in parentheses.

### Table 3

| No. | α     | log₁₀(1+zₚₑₛₑ) | log₁₀(L₅₁₀₀/10⁴⁴) | log₁₀(Mₘ₈₉/10⁸) | log₁₀(L/Lₐ₈₉) | log₁₀(M) | ε         |
|-----|-------|-----------------|-------------------|-----------------|---------------|----------|-----------|
| 1   | -0.88 | 0.44 ± 0.08     | X                 | X               | X             | X        | 0.26 ± 0.01|
| 2   | -0.74 | ± 0.01          | 0.03 ± 0.02       | X               | X             | X        | 0.26 ± 0.01|
| 3   | -0.77 | ± 0.01          | X                 | 0.12 ± 0.02     | X             | X        | 0.25 ± 0.01|
| 4   | -0.93 | ± 0.03          | X                 | X               | -0.19 ± 0.02  | X        | 0.25 ± 0.01|
| 5   | -0.79 | ± 0.01          | X                 | X               | X             | -0.09 ± 0.02| X        | 0.26 ± 0.01|
| 6   | -0.87 | ± 0.03          | 0.52 ± 0.11       | -0.21 ± 0.03    | 0.18 ± 0.03   | X        | X         | 0.25 ± 0.01|
| 7   | -1.08 | ± 0.04          | 0.50 ± 0.11       | -0.02 ± 0.03    | X             | -0.18 ± 0.03| X         | 0.25 ± 0.01|
| 8   | -1.14 | ± 0.06          | 0.57 ± 0.11       | -0.04 ± 0.03    | -0.22 ± 0.03  | X        | X         | 0.25 ± 0.01|
| 9   | -0.92 | ± 0.03          | 0.72 ± 0.10       | -0.10 ± 0.03    | X             | X        | X         | 0.25 ± 0.01|
| 10  | -0.83 | ± 0.03          | 0.18 ± 0.10       | X               | 0.09 ± 0.02   | X        | X         | 0.25 ± 0.01|
| 11  | -1.09 | ± 0.04          | 0.45 ± 0.07       | X               | X             | -0.19 ± 0.02| X         | 0.25 ± 0.01|

Note. The columns headed by physical quantities refer to their slope in the regression model (β).

Figure 14. Left: mean value of A in a grid of zₚₑₛₑ and L/Lₐ₈₉ for bins with three or more sources. Right: number of sources per bin of zₚₑₛₑ and L/Lₐ₈₉. The red dashed line shows the redshift from which we have available the Mg II line in the SDSS spectra (0.42).

γₘₑｄ ± 0.1, where γₘₑｄ corresponds to the median value of γ measured for the well-sampled subsample (0.53), i.e., we consider those sources with 0.43 ≤ γ ≤ 0.63. Selecting a narrow range in measured γ allows us to better discriminate between different intrinsic values of the amplitude A, as can be seen in Figure 5. There are 322 variables sources from the not–C IV sample in this range of γ. In this case, the results of the regression are α = -1.06 ± 0.05, βlog₁₀(1+zₚₑₛₑ) = 0.45 ± 0.1,
\( \beta_{\log_{10}(L/L_{\text{Edd}})} = -0.22 \pm 0.03 \), and \( \epsilon = 0.14 \pm 0.01 \). The results for the slopes of \( z_{\text{spec}} \) and \( L/L_{\text{Edd}} \) are consistent with what we found for the whole not–C IV sample, at the 1\( \sigma \) level. However, there is a considerable reduction in the intrinsic scatter measured for the reduced sample. This implies that a large part of the scatter measured in the different regression models of Table 3 comes from the \( A - \gamma \) degeneracy.

Table 4 gives the linear regression coefficients for \( z_{\text{spec}} \) and \( L/L_{\text{Edd}} \) considering the different samples defined in Section 5. From the table we can see that the results for the C IV sample are different from the results obtained for the other three samples. For the QUEST-SDSS sample, we can see a decrement in the slope of \( L/L_{\text{Edd}} \) produced by the presence of sources with C IV measurements. The slope of \( L/L_{\text{Edd}} \) is consistent for the not–C IV and Mg II samples, but the slope for \( z_{\text{spec}} \) changes. This can be produced by the reduced dynamic range in redshift for the Mg II sample, in comparison with the not–C IV sample. Moreover, from Figure 14 we can see that when we only consider sources from the Mg II sample (sources above the red dashed line), we lose most of the sources with low variability.

Table 4 also shows the linear regression coefficient for a model with redshift, \( L_{5100} \), and \( M_{\text{BH}} \). We can see that, as we showed in Table 3, for the not–C IV sample the slopes of \( L_{5100} \) and \( M_{\text{BH}} \) Satisfy \( \beta_{L_{5100}} \sim -\beta_{M_{\text{BH}}} \). However, for the QUEST-SDSS and Mg II samples, the relation between the slopes is not so evident. Again, for the case of the QUEST-SDSS sample we have contamination from C IV. The difference between the results for the Mg II and not–C IV samples can be driven by the change in the dynamic range of \( z_{\text{spec}} \) (see Figure 11) and the strong correlation between \( z_{\text{spec}} \) and \( L_{5100} \) (produced by a selection effect), since the slope for \( z_{\text{spec}} \) also increases when we include \( L_{5100} \) in the model.

In order to see whether smaller ranges of redshift can reduce the effects in the regression analysis of the \( z_{\text{spec}} \) versus \( L_{5100} \) correlation, we computed the regression models again, but considering sources from the not–C IV sample with \( 1.5 < z_{\text{spec}} < 1.8 \), since in this range of redshift the correlation between \( z_{\text{spec}} \) and \( L_{5100} \) is smaller (\( p_{\text{sel}} = 0.12, p_{\text{cal}} = 0.09 \)). We find similar results, but the results are less statistically significant owing to the low number of sources considered (there are 213 variable sources in this range of redshift). For the case of the regression model with \( z_{\text{spec}} \), \( L_{5100} \), and \( M_{\text{BH}} \), the results of the regression are \( \alpha = 0.03 \pm 0.55, \beta_{\log_{10}(M_{\text{BH}})} = 1.51 \pm 1.30, \beta_{\log_{10}(L_{5100})} = -0.20 \pm 0.08, \beta_{\log_{10}(L_{\text{Edd}})} = -0.12 \pm 0.07 \), and \( \epsilon = 0.21 \pm 0.01 \). And for the case of the regression with \( z_{\text{spec}} \) and \( L/L_{\text{Edd}} \), the results of the regression are \( \alpha = -0.22 \pm 0.56, \beta_{\log_{10}(1+z_{\text{spec}})} = 1.50 \pm 1.29, \beta_{\log_{10}(L/L_{\text{Edd}})} = -0.15 \pm 0.06 \), and \( \epsilon = 0.21 \pm 0.01 \). From these results, we can see that \( \beta_{\log_{10}(L_{\text{Edd}})} \sim -\beta_{\log_{10}(M_{\text{BH}})} \) at the 1\( \sigma \) level and that the anticorrelation between \( A \) and \( (L/L_{\text{Edd}}) \) is still present.

As mentioned in Section 4.2, Mejía-Restrepo et al. (2018a) proposed new corrections for the estimation of \( M_{\text{BH}} \). We show in Table 5 the linear regression coefficients for a model with \( z_{\text{spec}} \) and \( (L/L_{\text{Edd}})^{C} \) and for a model with \( z_{\text{spec}} \), \( L_{5100} \), and \( M_{\text{BH}} \), for the different samples of Section 5. We can see that the slopes for \( z_{\text{spec}} \) and \( (L/L_{\text{Edd}})^{C} \) increase for the QUEST-SDSS, not–C IV, and C IV samples, but the errors in the slopes also increase. The slopes for \( (L/L_{\text{Edd}})^{C} \) are more similar for the
different samples than the slopes for $z_{\text{spec}}$. This can be related to the difference in the dynamic ranges of $z_{\text{spec}}$ for different samples. For the regression model with $z_{\text{spec}}$, $L_{5100}$ and $M_{\text{BH}}$, the slopes of $L_{5100}$ and $M_{\text{BH}}$ satisfy the relation $\beta_{L_{5100}} \sim -\beta_{M_{\text{BH}}}$, for the QUEST-SDSS, not-C IV, and Mg II samples (at 1σ). This supports our idea that $L/L_{\text{Edd}}$ is the driver of the variability amplitude. The difference of these results with what we showed in Table 4 can be given by the reduction of the scatter in the determined black hole mass when we use the corrections proposed by Mejía-Restrepo et al. (2018a).

Table 6 shows three linear regression models that consider different spectral properties of the Mg II line as the independent variable. The first regression model corresponds to a model with $L_{\text{Mg} \, II}/L_{3000}$, which is a proxy of the EW of the line. Previous analyses have found that there is a strong anticorrelation between the EW of Mg II and $L/L_{\text{Edd}}$ (see Netzer 2013, and references therein). Our results shows a positive correlation between $L_{\text{Mg} \, II}/L_{3000}$ and $A$, which supports our interpretation that $L/L_{\text{Edd}}$ is the driver of the amplitude.

The second and third regression models of Table 6 include the spectral slopes $L_{5100}/L_{3000}$ and $L_{3000}/L_{1450}$. We can see that there is no statistically significant correlation between the amplitude of the variability and these spectral slopes.

We looked for correlations between $A$ and parameters derived from the line fitting. Table 7 shows the regression coefficients for models that consider the FWHM and continuum luminosity ($L_\lambda$) for the Hα, Hβ, Mg II, and C IV lines. For the case of Hα, the statistics is poor given the low number of variable sources with this line available in the SDSS spectra. Despite that, we can see a positive correlation between $A$ and FWHM($H\alpha$). For the case of Hβ, the results are similar, with a positive correlation between $A$ and FWHM(Hβ). Mg II has the best statistics, with 1063 variable sources available. In this case we also see a correlation between $A$ and FWHM (Mg II), but also an anticorrelation between $A$ and $L_{3000}$. The results for C IV are completely different, with no significant correlation between $A$ and FWHM(C IV) or $L_{1450}$. This can be related to the known problems of using the C IV line to measure black hole masses, since the line profile deviates considerably from Keplerian-type motion and can be influenced by winds emanating from the accretion disk (see Netzer 2013; Mejía-Restrepo et al. 2018b, and references therein).

The positive correlations between $A$ and the FWHM of Hα, Hβ, and Mg II are expected for a variability process whose amplitude is driven by $L/L_{\text{Edd}}$, since $L/L_{\text{Edd}} \propto \text{FWHM}^{-2} (\lambda L_\lambda)^{-1-\alpha}$ (following the equations of Section 4.2). Under this assumption, the anticorrelation between $A$ and $L_{3000}$ is also expected. The lack of correlation of $A$ with $L_{6200}$ and $L_{5100}$ can be given by the differences in the continuum luminosity range covered by these lines compared to Mg II.

### Footnotes

1. The columns headed by physical quantities refer to their slope in the regression model ($\beta$).

2. For the case of $\sigma_{\text{rms}}$, we see a significant anticorrelation with $L/L_{\text{Edd}}$, which is consistent with what we found for $A$. We also found a lack of significant correlation with $z_{\text{spec}}$. This can be given by the positive correlation between the amplitude of the variability and $z_{\text{spec}}$ and the negative correlation between the length of the light curve and $z_{\text{spec}}$. Since $\sigma_{\text{rms}}^2$ considers the variance of the whole light curve, sources at high redshift we observe shorter light curves than at low redshift and, therefore the correlation with $z_{\text{spec}}$ is considerably diminished.

3. For the case of $\sigma_{\text{DRW}}$, we see an anticorrelation with $L/L_{\text{Edd}}$ and a positive correlation with $z_{\text{spec}}$. This is in contrast with the results reported by Kelly et al. (2009), who found no correlation between $L/L_{\text{Edd}}$ and $\sigma_{\text{DRW}}$. This can be given by the strong dependency of $\sigma_{\text{DRW}}$ on the sampling of the light curve and the considerably small number of sources, with respect to our sample, used by Kelly et al. (2009). Our results also show that $\sigma_{\text{DRW}}$ correlates negatively with $L_{5100}$ and has no correlation with $M_{\text{BH}}$. Kelly et al. (2009) found a similar slope for $L_{5100}$ for their model with $z_{\text{spec}}$ included (see their Equation (25)). Since we found no correlation with $M_{\text{BH}}$, we propose that the anticorrelation between $\sigma_{\text{DRW}}$ and $L/L_{\text{Edd}}$ is given by the anticorrelation between $\sigma_{\text{DRW}}$ and $L_{5100}$. We must consider the implication of these results with caution, since $\sigma_{\text{DRW}}$ is strongly affected by the light-curve sampling. Particularly, Figure 2 shows that $\sigma_{\text{DRW}}$ anticorrelates with the number of epochs and the length of the light curve. More luminous sources have higher probabilities to be detected in more epochs than fainter sources. In fact, the Spearman rank correlation coefficient for $L_{5100}$ and the number of epochs is 0.45 ($p_{\text{val}} = 1e^{-4}$). Therefore, the anticorrelation between $\sigma_{\text{DRW}}$ and $L_{5100}$ can be just a reflection of the anticorrelation between $\sigma_{\text{DRW}}$ and the number of epochs.

### References

- Sánchez-Sáez et al. (2018a)
- Kelly et al. (2009)
- Netzer (2013)
- Mejía-Restrepo et al. (2018b)
- Netzer (2013)
these sources, the value of $\gamma$ differs considerably from 0.5, and therefore a DRW model is not sufficient to model the variability. When we compare the distributions of the SMBH physical properties of (a) the 325 sources with $\gamma > 0.75$ and (b) the rest of the sample, we do not observe any difference between the populations. We also do not observe differences in the light-curve sampling of these two populations; therefore, we can discard an observational bias in the distribution of $\gamma$.

6.4. Differences between Variable and Nonvariable Sources

From the QUEST-SDSS sample, 1348 sources are variable and 125 are nonvariable. Figure 15 shows the normalized distribution of the different physical properties considered in this work, for the variable and nonvariable sources. In the figure we can see that the distributions of $L_{\text{bol}}/L_{\text{Edd}}$ and $M_{\text{BH}}/M_*$ are similar, but for the case of nonvariable sources, the distribution of $z_{\text{spec}}$ is in general shifted toward higher values of redshift, with the exception of a few sources located at low $z_{\text{spec}}$. This difference in redshift can be related to the fact that high-redshift sources have shorter rest-frame light curves, because of the time dilation. In Figure 16 we show the normalized distribution of the light-curve properties of variable and nonvariable sources from the QUEST sample. In the figure we can see that nonvariable sources tend to have a lower number of epochs, shorter light curves in rest frame, and fainter mean magnitudes. Therefore, in our sample, the light-curve properties are more relevant for the classification of variable and nonvariable sources than the physical properties of the SMBH.

7. Variability Behavior of Different Classes of AGNs

7.1. BAL QSOs

We used the catalogs of Shen et al. (2011), Püriis et al. (2017), and Püriis et al. (2018) to classify 133 sources of our sample as BAL QSOs. Of these sources, 99 have light curves with good sampling, and 86 are variable (86.9%). In Figure 9 we show in red the distribution of $A$ and $\gamma$ for the well-sampled and variable BAL QSOs; we can see that there is no evident difference in the SF parameters.

In order to have a more quantitative comparison of the distribution of the SF parameters of BAL QSOs and the rest of the sample, we performed a two-sample Anderson–Darling test (Pettitt 1976) for the $A$ and $\gamma$ parameters. Since the Anderson–Darling test does not take into account the errors of the parameters, we only considered in the test those variable sources with a measured parameter having an S/N higher than 3. According to the test, the distributions of the $A$ parameter are the same at a 99.5% significance level, with a $p_{\text{val}}$ of 0.9, and the distributions of the $\gamma$ parameter are different, with a $p_{\text{val}}$ of 0.02. The differences in the distributions of $\gamma$ are related to the fact that for the rest of the sample most of the sources are concentrated around $\gamma = 0.5$, but for the case of BAL QSOs the sources are more homogeneously distributed in the SF parameter space. Nevertheless, we do not see that the values of $\gamma$ for BAL QSOs are systematically different from the rest of the sample.
7.2. Radio Classification

We divided our sources as radio-loud (RL) or radio-quiet (RQ) according to their radio and optical emissions. We used data from the Faint Images of the Radio Sky at Twenty cm survey (FIRST; Becker et al. 1994) to obtain fluxes at 20 cm of our sources. FIRST used the Very Large Array to produce a map of the 20 cm (1.4 GHz) sky with a beam size of 5 arcsec and an rms sensitivity of about 0.15 mJy beam$^{-1}$. The last version of the FIRST survey catalog (14Dec17 Version10) provides all the sources detected with a threshold of 1 mJy. We cross-matched our QUEST-SDSS sample with the FIRST catalog, using a radius of 1 arcsec.

We classified our sources as RL and RQ using the ratio

\[ R = \frac{F_\nu(5 \text{ GHz})}{F_\nu(4400 \text{ Å})}, \]

where $F_\nu(5 \text{ GHz})$ is the radio flux density of the source measured at 5 GHz and $F_\nu(4400 \text{ Å})$ is the flux density at 4400 Å (Kellermann et al. 1989). We applied $K$-corrections to the photometry provided by the SDSS and FIRST catalogs, considering that the radio and optical emissions follow a power-law-like $F \propto \nu^{-0.8}$ and $F \propto \nu^{-0.44}$, respectively. Then, we estimate $F_\nu(5 \text{ GHz})$ from the measurements at 1.4 GHz provided by FIRST and $F_\nu(4400 \text{ Å})$ from the SDSS $g$-band (4770 Å) measurements. Therefore, the final flux values used to determine $R$ were

\[ F_\nu(5 \text{ GHz})_{\text{rest}} = F_\nu(1.4 \text{ GHz})_{\text{obs}} \left( \frac{1.4}{5} \right)^{0.8} (1 + z)^{-0.2} \]

\[ F_\nu(4400 \text{ Å})_{\text{rest}} = F_\nu(4770 \text{ Å})_{\text{obs}} \left( \frac{6.29}{6.81} \right)^{0.44} (1 + z)^{-0.56}. \]

All the sources of the QUEST-SDSS sample are located in regions mapped by FIRST; however, not all of them have a radio detection associated. A total of 55 objects from the QUEST-SDSS sample have a FIRST counterpart. For those sources without a detection reported, we assumed that the measured flux corresponds to the detection threshold of 1 mJy. Then, we classify sources as RL if they have $R > 10$ and are detected by FIRST, and we classify sources as RQ if they have $R < 10$.

From the QUEST-SDSS sample, 373 sources are classified as RQ and 354 are variable (94.9%), while 48 are classified as RL and 38 are variable (79.2%). Figure 17 shows the distribution of the SF parameters for RL and RQ sources, as well as for sources without radio classification. In the figure we can see that there is no evident difference in the distributions of RL and RQ sources. For a more quantitative comparison, we
performed an Anderson–Darling test comparing the SF parameter distributions of the RL and RQ sources. As before, we only considered those variable sources with a measured parameter having an S/N higher than 3. According to the test, the distributions of A and γ are the same for RQ and RL sources, with $P_{\text{D}}$ of 0.64 for A and 0.22 for γ. This could imply that the radio loudness may not be relevant for the optical variability of type I AGNs.

8. Discussion and Conclusions

In Section 3.5 we showed that there is a correlation between A and γ; however, in Section 3.4 we demonstrated that such a correlation is produced by the stochastic nature of the light curves together with the light-curve sampling. We might need longer light curves to reduce this degeneracy; however, having access to long (decades of coverage) and well-sampled light curves for large samples of sources is not possible currently. In Section 6 we demonstrated that A anticorrelates with both $\lambda_{\text{rest}}$ and $L/L_{\text{Edd}}$ but γ does not correlate with any of the physical parameters studied. This confirms our assumption that the correlation between A and γ is produced by the light-curve properties and by the stochastic nature of the variability. Nonetheless, the SF is the best option that we have today to analyze typical ground-based light curves (i.e., with a few years of coverage, with a few epochs, and with gaps), since other techniques, like Fourier analyses, require well-sampled light curves (i.e., with several epochs, and without gaps).

In Sections 4.3 and 6.2 we reported that our data set presents correlations between the SMBH physical properties. Some of these correlations are produced by selection effects, since our sample is flux limited. For example, the correlations of redshift with luminosity, BH mass, and accretion rate are produced by the fact that at higher redshifts our sample will naturally contain sources with higher luminosities, higher SMBH masses, and higher accretion rates.

The results shown in Section 6 tell us that the observed amplitude of the variability depends on two variables, $z_{\text{spec}}$ and $L/L_{\text{Edd}}$, which means that, at a fixed $z_{\text{spec}}$, sources with similar $L/L_{\text{Edd}}$ will have similar variability amplitudes. The positive correlation with redshift can be interpreted as an anticorrelation with the wavelength of rest-frame emission. MacLeod et al. (2010) analyzed ugriz light curves of ~9000 spectroscopically confirmed SDSS S82 quasars. Since they had multiple bands for each quasar, they could separate the dependency of the amplitude of the variability with redshift and $\lambda_{\text{rest}}$, finding an anticorrelation with $\lambda_{\text{rest}}$ and no correlation with $z_{\text{spec}}$. S17 analyzed the near-infrared variability of X-ray-selected AGNs. They also found a correlation between the amplitude of the variability and redshift. By comparing the trends between A and $z_{\text{spec}}$ for two different bands (γ and J), they showed that the correlation with $z_{\text{spec}}$ is explained by an anticorrelation with the wavelength of emission. From this and other previous results (e.g., Koziolowski et al. 2010), we conclude that the positive correlation of A with $z_{\text{spec}}$ is produced by a dependency on $\lambda_{\text{rest}}$ and is not given by evolution over cosmic time. This anticorrelation between $\lambda_{\text{rest}}$ and A can be explained considering that the innermost regions of the disk can be the most variable, either intrinsically or by reprocessing. Since at shorter wavelengths a larger fraction of the disk emission is produced by the innermost region, it follows that shorter wavelengths display larger amplitudes of variability (Arévalo et al. 2008; Lira et al. 2011, 2015; Edelson et al. 2015; Fausnaugh et al. 2016).

We found an anticorrelation between A and $L/L_{\text{Edd}}$. When we used the standard method to determine black hole masses from single-epoch spectra, we found a slope of $\beta_{L/L_{\text{Edd}}} = -0.19 \pm 0.02$ for the regression model, with A as the dependent variable and $L/L_{\text{Edd}}$ and $z_{\text{spec}}$ as the independent variables, for the not–C IV sample. When we applied the corrections proposed by Mejía-Restrepo et al. (2018a), which intend to account for the effect of the unknown distribution of the gas clouds in the BLR, we found a slope of $\beta_{L/L_{\text{Edd}}} = -0.28 \pm 0.06$. An anticorrelation between $L/L_{\text{Edd}}$ and the amplitude of the variability has also been reported by previous works (e.g., Wilhite et al. 2008; MacLeod et al. 2010; Simm et al. 2016; Rakshit & Stalin 2017). MacLeod et al. (2010) reported a power-law slope of $-0.23 \pm 0.03$. This value was calculated by binning the parameter space of $M_{\text{BH}}$ and $L_{\text{BH}}$ (absolute magnitude) and using ensemble light curves, which can explain the small difference with the value found by us.

MacLeod et al. (2010) also proposed that an additional dependency with luminosity or black hole mass is needed in order to explain their findings. Here we conclude that such a dependency is not necessary when intrinsic scatter is included in the model. In fact, in Table 3 we can see that the value of the intrinsic scatter found with our method is pretty stable and that including $L_{\text{5100}}$ or $L_{\text{L_H}}$ in the regression model with $z_{\text{spec}}$ and $L/L_{\text{Edd}}$ produces statistically insignificant slopes for $L_{\text{5100}}$ or $L_{\text{L_H}}$. From the results of Sections 3.4 and 6.3.1 we can say that the main contributors to this scatter are the $A - \gamma$ degeneracy (produced by the stochastic nature of the AGN variability), the definition of the SF by itself, the light-curve sampling, and the fact that light curves with coverage of a few years are not a good representation of the whole variability behavior. We could notice in Section 6.3.1 that when we performed the linear regression model with $z_{\text{spec}}$ and $L/L_{\text{Edd}}$ as independent sources,
selecting only those sources from the not–C IV sample whose measured values of $\gamma$ were in the range between 0.43 and 0.63, the measured scatter in the regression was reduced considerably. This confirms our assumption that the $A - \gamma$ degeneracy is one of the main contributors to the measured scatter in the regression models.

Possible interpretations of the inverse dependency of the amplitude of the variability with $L/L_{\text{Edd}}$ are discussed by Wilhite et al. (2008), MacLeod et al. (2010), Simm et al. (2016), and Rakshit & Stalin (2017). One explanation is that $L/L_{\text{Edd}}$ is a proxy of the age of the AGN (e.g., Martini & Schneider 2003; Haas 2004; Hopkins et al. 2005). Sources with lower $L/L_{\text{Edd}}$ can suffer from a dwindling of the fuel supply, as they become old; thus, the accretion flow can be more variable, producing larger amplitude in the variability. However, the timescales of the amplitudes measured in this work are $\sim$1 yr, and therefore it is unlikely that the variability amplitudes observed are given by variations in the external fuel supply, which requires much longer timescales to be effective ($10^7$–$10^8$ days).

Another possible interpretation is that sources with higher $L/L_{\text{Edd}}$ have hotter accretion disks, as predicted by classical accretion physics (Shakura & Sunyaev 1973). For typical values of black hole mass and accretion rate, it is expected that the innermost part of the disk emits in the far-UV. Because of its smaller size, this region is also the one showing the largest variability amplitude. For lower accretion rates, however, the disk becomes cooler, and the innermost, most variable region will shift its emission from the UV to optical wave bands. This would be true regardless of whether the variation of the disk emission is produced by intrinsic processes or by reprocessing of highly variable X-ray emission by the disk surface. MacLeod et al. (2010) discarded this assumption because the timescales ($\tau$) that they measured were not in agreement with this scenario. However, they used DRW modeling to find $\tau$, while it is now clear that DRW models cannot be used to properly describe the timescales of typical ground-based light curves (see Section 3.1).

A third possible explanation for the anticorrelation between $A$ and $L/L_{\text{Edd}}$ can be related to the positive correlation between $L/L_{\text{Edd}}$ and the ratio of the UV/optical-to-X-ray flux ($\alpha_{\text{OX}}$) reported by several studies (e.g., Shemmer et al. 2008; Grupe et al. 2010; Lusso et al. 2010; Jin et al. 2012). If the UV/optical variability is produced by reflection of the variable X-ray emission, then disks located in systems with higher $\alpha_{\text{OX}}$ values will receive fractionally less X-ray radiation, and therefore the amplitude of the variability detected in the UV/optical range will be small. On the other hand, for sources with lower $\alpha_{\text{OX}}$, the disk will be irradiated with more X-ray light, and therefore we will detect higher UV/optical variability amplitudes. Kubota & Done (2018) developed a new spectral model for the SED of AGNs that includes a hot corona, an inner warm optically thick Comptonizing region, and an outer disk. Considering this model, they studied the UV/optical variability resulting from the reprocessing of the rapidly variable X-ray flux. Their model predicts an anticorrelation between the amplitude of the variability and $L/L_{\text{Edd}}$. However, their model also predicts a much lower amount of UV/optical variability than what is observed by our analysis and previous studies (e.g., MacLeod et al. 2010) at timescales of 1 yr or longer. This means that the model needs an extra source of UV/optical variability in order to explain the amplitudes observed at long timescales, as has been found by previous analyses (Krolik et al. 1991; Arévalo et al. 2008; Edelson et al. 2015; Lira et al. 2015). Therefore, the anticorrelation between $A$ and $L/L_{\text{Edd}}$ cannot be solely explained by the correlation between $L/L_{\text{Edd}}$ and $\alpha_{\text{OX}}$.

In this work, we also found that the logarithmic gradient of the variability ($\gamma$) does not correlate significantly with any of the physical parameters studied and that the general distribution of $\gamma$ measured for our sample differs from the distribution of $\gamma$ obtained for light curves simulated from a DRW process. We showed in Sections 3.5 and 6.3.3 that 20.6% of the light curves have values of $\gamma$ higher than 0.75, for which a DRW model is not appropriate to explain the variability. Kasliwal et al. (2015) and Smith et al. (2018) used Kepler light curves to study whether DRW modeling is sufficient to explain the variability of light curves with high cadence. They concluded that most of the Kepler AGN light curves analyzed cannot be described by a simple DRW model. Smith et al. (2018) also proposed that it is possible that DRW modeling can be correct for ground-based quasar light curves, which in general study different time regimes than Kepler. We need larger samples of high-cadence light curves, to see whether the results of Kasliwal et al. (2015) and Smith et al. (2018) are representative for the whole AGN population.

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