Multi-atom quasiparticle scattering interference for superconductor energy-gap symmetry determination

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Abstract
Complete theoretical understanding of the most complex superconductors requires a detailed knowledge of the symmetry of the superconducting energy-gap $\Delta_\alpha k$, for all momenta $k$ on the Fermi surface of every band $\alpha$. While there are a variety of techniques for determining $|\Delta_\alpha k|$, no general method existed to measure the signed values of $\Delta_\alpha k$. Recently, however, a technique based on phase-resolved visualization of superconducting quasiparticle interference (QPI) patterns, centered on a single non-magnetic impurity atom, was introduced. In principle, energy-resolved and phase-resolved Fourier analysis of these images identifies wavevectors connecting all k-space regions where $\Delta_\alpha k$ has the same or opposite sign. But use of a single isolated impurity atom, from whose precise location the spatial phase of the scattering interference pattern must be measured, is technically difficult. Here we introduce a generalization of this approach for use with multiple impurity atoms, and demonstrate its validity by comparing the $\Delta_\alpha k$ it generates to the $\Delta_\alpha k$ determined from single-atom scattering in FeSe where $s^\pm$ energy-gap symmetry is established. Finally, to exemplify utility, we use the multi-atom technique on LiFeAs and find scattering interference between the hole-like and electron-like pockets as predicted for $\Delta_\alpha k$ of opposite sign.

Disciplines
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Multi-atom quasiparticle scattering interference for superconductor energy-gap symmetry determination

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Complete theoretical understanding of the most complex superconductors requires a detailed knowledge of the symmetry of the superconducting energy-gap $\Delta_k$, for all momenta $k$ on the Fermi surface of every band $\alpha$. While there are a variety of techniques for determining $\Delta_k^\alpha$, no general method existed to measure the signed values of $\Delta_k^\alpha$. Recently, however, a technique based on phase-resolved visualization of superconducting quasiparticle interference (QPI) patterns, centered on a single non-magnetic impurity atom, was introduced. In principle, energy-resolved and phase-resolved Fourier analysis of these images identifies wavevectors connecting all $k$-space regions where $\Delta_k^\alpha$ has the same or opposite sign. But use of a single isolated impurity atom, from whose precise location the spatial phase of the scattering interference pattern must be measured, is technically difficult. Here we introduce a generalization of this approach for use with multiple impurity atoms, and demonstrate its validity by comparing the $\Delta_k^\alpha$ it generates to the $\Delta_k^\alpha$ determined from single-atom scattering in FeSe where $s_\pm$ energy-gap symmetry is established. Finally, to exemplify utility, we use the multi-atom technique on LiFeAs and find scattering interference between the hole-like and electron-like pockets as predicted for $\Delta_k^\alpha$ of opposite sign.

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INTRODUCTION

The macroscopic quantum condensate of electron pairs in a superconductor is represented by its order-parameter $\Delta_k^\alpha \propto \langle c_k^\dagger c_k^- \rangle$, where $c_k^\dagger$ is the creation operator for an electron with momentum $k$ on band $\alpha$. But electron pair formation can occur through a wide variety of different mechanisms and in states with many possible symmetries. Thus, it is the symmetry properties of $\Delta_k^\alpha$ that are critical for identification of the Cooper pairing mechanism and, moreover, for understanding the macroscopic phenomenology. While macroscopic techniques can reveal energy-gap symmetry for single-band systems, no general technique existed to determine the relative signs of $\Delta_k^\alpha$ between $k_a$ and $k_b$ for all Fermi surface (FS) momenta in an arbitrary superconductor. In 2015, a conceptually simple and powerful technique for determining $\Delta_k^\alpha$ symmetry was introduced by Hirschfeld, Eremin, Altenfeld, and Mazin (HAEM). It is based on interference of weakly scattered quasiparticles at a single, non-magnetic, impurity atom. Given a superconductor Hamiltonian

$$\mathcal{H}_k = \begin{pmatrix} H_k & \Delta_k \\ \Delta_k^\dagger & -H_k^\dagger \end{pmatrix},$$

where $H_k$ is the normal-state Hamiltonian and $\Delta_k$ the superconducting energy gap, a non-magnetic impurity atom is modeled as a weak point-like potential scatterer, with Hamiltonian $H_{imp} = V_0 G_k^\alpha$, centered at the origin of coordinates $r = 0$. Effects of scattering are then represented by a T-matrix derived from the local Green’s function $G_0(E) = \sum_k G_k^{\alpha}(E)$, where $G_k^{\alpha}(E) = (E + i0^+ - \mathcal{H}_k)^{-1}$. When the impurity potential is constant in $k$-space, the Green’s function becomes $G_{k,k'}(E) = G_{k,k'}^\alpha(E) + G_{k,k'}^\beta(E)T(E)G_{k',k}(E)$, with the T-matrix given by

$$T(E) = \left[ 1 - V_{imp}G_0(E) \right]^{-1}V_{imp},$$

where $V_{imp}$ is the impurity matrix. From $G_{k,k'}(E)$, the perturbations to the local density-of-states $\delta N(r, E)$ are predicted surrounding the impurity atom, and its Fourier transform can be determined directly from $\Delta_k$ as

$$\delta N(q, E) = -\frac{1}{\pi} \text{Im} \left[ \sum_k G_k^{\alpha}(E) T(\omega) G_k^{\beta}(E) \right]_{11},$$

which is a purely real quantity because, in the theoretical calculation, the single impurity is exactly at the origin of coordinates. The authors of ref. 4 realized that the particle-hole symmetry of Eq. (2) for scattering interference wavevector $q = k_1^\dagger - k_2^\dagger$ depends on the relative sign of the energy-gaps $\Delta_k^\alpha$ and $\Delta_k^\beta$ at these two momenta. Consequently, the experimentally accessible energy-antisymmetrized function $\rho(q, E)$ of phase-resolved Bogoliubov scattering interference amplitudes

$$\rho(q, E) \equiv \text{Re} \{ \delta N(q, +E) - \delta N(q, -E) \}$$

can be used to determine the relative sign of the superconducting energy-gaps connected by $q = k_1^\dagger - k_2^\dagger$. In the

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part of Fourier transform \(\text{Re} \delta N(r)\) from \(\delta N(r)\) in a. We use an integer grid, hence the units of Fourier transform are also \(i/q\). c Imaginary part of Fourier transform \(\text{Im} \delta N(r)\) from \(\delta N(r)\) in a. d Real part of Fourier transform \(\text{Re} \delta N_{\text{MA}}(q)\) calculated using multi-atom technique of Eq. (7). e Imaginary part of Fourier transform \(\text{Im} \delta N_{\text{MA}}(q)\) calculated using multi-atom technique of Eq. (7). f \(\text{Re} \delta N(q)\) from \(\delta N(r)\) in a for \(\theta = 0\) and \(\theta = \pi\), integrated azimuthally from b. Its strong random fluctuations versus \(q\) are due to summing the Friedel oscillations in \(\delta N(r)\) of a with random phases due to the random locations \(R\). g \(\text{Re} \delta N_{\text{MA}}(q)\) from \(\delta N(r)\) in a integrated azimuthally from d. \(\text{Re} \delta N_{\text{MA}}(q)\) is now orders of magnitude more intense than in f, and the phase of the Friedel oscillations in \(\delta N(r)\) of a is now very well defined because the effects of random locations \(R\), are removed by using Eq. (7). Note that, now, changing the oscillation phase \(\theta = 0\) to \(\theta = \pi\) surrounding all \(R\) in \(\delta N(r)\) produces the correct evolution of \(\text{Re} \delta N_{\text{MA}}(q)\).

Fig. 1 Schematic for multi-atom phase analysis. a Simulation of density of states perturbation \(\delta N(r)\) in amplitude units \(I_0\) due to two-dimensional Friedel oscillations surrounding 100 impurity atoms at random locations \(R\). b Real part of Fourier transform \(\text{Re} \delta N(q)\) from \(\delta N(r)\) in a. c Imaginary part of Fourier transform \(\text{Im} \delta N(q)\) from \(\delta N(r)\) in a. d Real part of Fourier transform \(\text{Re} \delta N_{\text{MA}}(q)\) calculated using multi-atom technique of Eq. (7). e Imaginary part of Fourier transform \(\text{Im} \delta N_{\text{MA}}(q)\) calculated using multi-atom technique of Eq. (7). f \(\text{Re} \delta N(q)\) from \(\delta N(r)\) in a for \(\theta = 0\) and \(\theta = \pi\), integrated azimuthally from b. Its strong random fluctuations versus \(q\) are due to summing the Friedel oscillations in \(\delta N(r)\) of a with random phases due to the random locations \(R\). g \(\text{Re} \delta N_{\text{MA}}(q)\) from \(\delta N(r)\) in a integrated azimuthally from d. \(\text{Re} \delta N_{\text{MA}}(q)\) is now orders of magnitude more intense than in f, and the phase of the Friedel oscillations in \(\delta N(r)\) of a is now very well defined because the effects of random locations \(R\), are removed by using Eq. (7). Note that, now, changing the oscillation phase \(\theta = 0\) to \(\theta = \pi\) surrounding all \(R\) in \(\delta N(r)\) produces the correct evolution of \(\text{Re} \delta N_{\text{MA}}(q)\).

simplest case with two isotropic gaps \(\Delta^a\) and \(\Delta^b\) on distinct bands, it was demonstrated that

\[
\rho^-(q, E) \propto \text{Im} \left[ (E_1^2 - \Delta^a \Delta^b) \sqrt{E_1^2 - (\Delta^a)^2} \right]
\]

where \(E_1 = E + i0^+\), so that the functional form of \(\rho^-(q, E)\) is very different when the product \(\Delta^a \Delta^b\) is positive or negative. An elementary implication of Eq. (4) is that, when the order parameter has opposite signs on the two bands so that \(\Delta^a \Delta^b < 0\), \(\rho^-(q, E)\) does not change sign and exhibits pronounced maxima or minima near \(E = \Delta^a \Delta^b\) whereas if the order parameter has the same sign so that \(\Delta^a \Delta^b > 0\), \(\rho^+(q, E)\) exhibits weak maxima or minima near \(E = \Delta^a \Delta^b\) with a sign of change in between. More generally, especially with multiple bands and anisotropic gaps, HAEM requires that \(\rho^-(q, E)\) be predicted in detail for a specific \(H_k\) and \(\Delta_k\) in Eq. (1) and then compared with quasiparticle interference imaging in which the scanning tunneling microscope (STM) differential electron tunneling conductance, \(g(r, E) \propto \delta N(r, E)\) is visualized.

This single-atom phase-resolved HAEM method has been established experimentally\(^a\). For example, in the case of the multiband \(s^\pm\) superconductor FeSe, the complete energy and wavevector dependence of \(\rho^-(q, E)\) was used to determine that the \(k\)-space structure including relative sign of \(\Delta^a_k\) and \(\Delta^b_k\) for all \(k\) and all \(k_g\) on two different bands. But this result required that the impurity atom be highly isolated from other impurities and centered precisely at the origin of coordinates, with respect to which the \(\text{Re} \delta N(q, E)\) of Eq. (3) is then properly defined. This was critical because, an error of on the order of \(-1\%\) of a crystal unit cell in the coordinate of the origin (at the impurity atom) produces significant errors in \(\text{Re} \delta N(q, E)\) and \(\text{Im} \delta N(q, E)\) (Supplementary Note 1 and Fig. S1). Moreover, single impurity atom-based measurements limit the \(k\)-space resolution because the field of view (FOV) is typically restricted in size, making them unsuitable for superconductors with large impurity atom densities. This provides the motivation for a variety of approaches to \(\Delta_k\) determination beyond single-atom HAEM. One is to study Bogoliubov bound-states at individual impurity atoms\(^b\), although this has proven problematic because the elementary HAEM concept (Eq. (3)) is only valid in the weak scattering range, i.e. well below the scattering strength sufficient to generate Bogoliubov bound states\(^1\). Another approach is to use sparse blind deconvolution\(^12\) to analyze images of scattering interference at multiple atoms, yielding the phase-resolved real space structure of \(\delta N(r, E)\) although not the \(\rho^-(q, E)\) of Eq. (3). Overall, therefore, widespread application of the HAEM technique (Eq. (3)) as a general tool for \(\Delta_k\) determination remains a challenge.

Here, we introduce a practical technique for determining \(\rho^-(q, E)\) of Eq. (3) from multiple impurity atoms in a large FOV. To understand this approach, consider the key issue of phase analysis as depicted in Fig. 1, a schematic simulation of Friedel oscillations \(\delta N(r)\) from multiple impurity atoms in a large FOV. To understand this approach, consider the key issue of phase analysis as depicted in Fig. 1, a schematic simulation of Friedel oscillations
Fourier transform of a single impurity atom at the Fourier transform of a scattering interference pattern surrounding a single atom at the zero of coordinates. In this regard, consider the effects occurring because the spatial phases of all the individual Friedel oscillations do not have a clear sign, and are indistinguishable from the imaginary part. Thus, we may define a multi-atom phase-preserving algorithm for QPI

\[
\delta N_{\text{MA}}(\mathbf{q}) = \sum_{\mathbf{R}} \delta N_{\text{S}}(\mathbf{q}) = \sum_{\mathbf{R}} e^{i \mathbf{q} \cdot \mathbf{R}}.
\]

The consequences of Eq. (7) are illustrated in Fig. 1d, e, (Supplementary Note 3 and Supplementary Fig. S4). The real part \(\Re \delta N_{\text{MA}}(\mathbf{q})\) now becomes well-defined and the overall magnitude is strongly enhanced compared to \(\Re \delta N(\mathbf{q})\). Moreover, the azimuthally integrated \(\Re \delta N_{\text{MA}}(\mathbf{q})\) plotted in Fig. 1g shows that the sign of \(\Re \delta N_{\text{MA}}(\mathbf{q})\) changes for \(\theta = 0\) and \(\theta = \pi\) as expected. Here it is essential that the impurity atom coordinates \(\mathbf{R}\) be determined accurately so that the phase is well-defined. We therefore employ a picometer-scale transformation which renders topographic images \(\tilde{\tau}(\mathbf{r})\) perfectly periodic with the lattice, and then use the same transformation on the simultaneously located at \(\mathbf{R} = (x, y)\), can be determined using

\[
\delta N_{\text{S}}(\mathbf{q}) = e^{i \mathbf{q} \cdot \mathbf{R}} \delta N(\mathbf{q}).
\]

This problem could be mitigated if the Fourier transform of the scattering interference pattern surrounding each \(\mathbf{R}\) were evaluated as if it were at the zero of coordinates. In this regard, consider the Fourier transform of a scattering interference pattern surrounding a single impurity atom at \(\mathbf{R} = (x, y)\).

\[
\int \delta N(\mathbf{r} - \mathbf{R}) e^{i \mathbf{q} \cdot \mathbf{r}} d\mathbf{r} = e^{i \mathbf{q} \cdot \mathbf{R}} \int \delta N(\mathbf{r} - \mathbf{R}) e^{i \mathbf{q} \cdot (\mathbf{r} - \mathbf{R})} d\mathbf{r} = e^{i \mathbf{q} \cdot \mathbf{R}} \delta N(\mathbf{q}).
\]
recorded $g(r,E)$ to register all the scattering interference oscillations precisely to the crystal lattice (Supplementary Note 2). Equation 7 then allows to correctly define the quantities in Eq. (3) for arbitrarily large numbers of scattering atoms. By using the analog of Eq. (6) for $g(r,E) \propto \delta N(r,E)$, $\rho^{-}(q,E)$ for each impurity atom is determined from

$$\rho^{-}(q,E) \propto \text{Re}\{g(q,+E)e^{iq\cdot R}\} - \text{Re}\{g(q,-E)e^{iq\cdot R}\},$$

while from Eq. (7) the sum over these $\rho^{-}(q,E)$ yields

$$\rho_{\text{MA}}(q,E) = \sum_{i} \rho^{-}_{i}(q,E).$$

This procedure adds all the individual $\rho^{-}_{i}(q,E)$ signals from every impurity atom at $R$, in-phase, while effectively averaging out the random phase variations due to both locating the origin and the contributions of all other scatterers (Supplementary Fig. S5). We designate this procedure multi-atom HAEM (MAHAEM).

RESULTS AND DISCUSSIONS
Multi-atom quasiparticle interference for $\Delta_{k}^{\alpha}$ determination

Determination of the magnitude of superconducting energy gaps $\Delta_{k}^{\alpha}$ has long been achieved using quasiparticle interference technique, and to test it we consider FeSe where the single impurity atom HAEM technique for determining $\Delta_{k}^{\alpha}$ was established experimentally. We measure the differential tunneling conductance $g(r,E) \equiv dI/dV(r,E)$ in a 30 nm FOV at $T = 280$ mK, followed by determination of $R_{i} = (x_{i},y_{i})$ for 17 scattering sites (Supplementary Note 3), some of which are shown in the FOV in Fig. 2a (Supplementary Fig. S2 shows all the sites). These sites are well-known Fe-atom vacancies identified by their crystal locations, and are non-magnetic; their empirical identity is confirmed by high-resolution electronic structure imaging. We then use Eq. (9) to calculate $\rho_{\text{MA}}(q,E)$. Figure 2b shows the FeSe FS with the hole-pocket $\alpha$ around $\Gamma$-point and electron pockets $\varepsilon$ around $(X,Y)$ points. Scattering between $\alpha$ and $\varepsilon$ at wavevector $\mathbf{p}$ was studied. A representative layer $\rho_{\text{MA}}(q,E = 1.05$ meV) is shown in Fig. 2c, where the scattering feature at wavevector $\mathbf{p}$ is marked with a circle. We then sum over the encircled $q$-region to get $\rho_{\text{MA}}(E)$ for this scattering feature which is shown as black dots in Fig. 2d. Results from our MAHAEM measurements agree very well with the experimental results using a single impurity atom $\rho_{\text{Exp}}$ (black crosses) and the theoretically predicted curve for $\rho^{-}_{\text{Th}}$ (solid, black) in FeSe. This demonstrates the validity and utility of the multi-atom HAEM technique.

Next we consider LiFeAs, a complex iron-based superconductor that is a focus of contemporary physics interest, particularly the relative sign of $\Delta_{k}^{\alpha}$ between all five bands. Figure 3b shows the FS of LiFeAs calculated using a tight-binding fit to the experimental data. It consists of three hole pockets $h_{1}, h_{2},$ and $h_{3}$.
between the electron-like and hole-like pockets. But the presence of three hole pockets, combined with relatively weak spin fluctuations, allow for several possible competing ground states in the presence of repulsive interactions. In ref. 34, it was pointed out that, under these conditions, several s-wave channels are nearly degenerate. These channels include the $s_\alpha$ state where the signs on all hole pockets are the same and opposite to the signs on the electron bands, so-called “orbital antiphase state” that occurs when the interaction is diagonal in orbital space, and a distinct sign structure obtained when vertex corrections were included. Reference 37 considered the question of whether these various proposed phases could be distinguished using HAEM based on Eq. (3) and concluded that it would be challenging.

Here we examine the relative signs of $\Delta$ in LiFeAs by using MAHAEM. Figure 3a shows the typical cleaved surface of LiFeAs. The scattering sites used in our analysis are Fe-atom vacancies which are non-magnetic (Supplementary Fig. S3). The theoretical simulations for LiFeAs were performed from the experimentally fitted tight binding model and anisotropic gap magnitude structure. At wavevectors corresponding to electron-hole fluctuations which are enhanced by nesting around $\Gamma$-point and two electron pockets $e_1$ and $e_2$ around $X$-point. The hole pockets around $\Gamma$-point on the FS revealed by spectroscopic imaging STM (SI-STM) and confirmed by angle resolved photoemission spectroscopy (ARPES) are much smaller as compared to most other Fe-based superconductors. Local density approximation (LDA) and dynamical mean field theory (DMFT) calculations have attributed the small size of hole pocket to stronger electron–electron correlation in this material. The superconducting energy-gaps $\Delta_{\alpha}$ are substantially anisotropic. Theoretically, in the case of $\Delta_{\alpha}$ with $s_\alpha$ symmetry, if both electron-like and hole-like pockets are present, the pairing arises from spin-fluctuations which are enhanced by nesting around $\Gamma$-point and two electron pockets $e_1$ and $e_2$ around $X$-point.
We report development and demonstration of an improved technique for measuring ραβ(q, E) with multiple impurity atoms or scattering centers. This MAHAEM technique efficiently demonstrates that Δαβ changes sign between electron-like and hole-like bands of LiFeAs.

Nevertheless, when the high |q| scattering between hole-like and electron-like pockets (Fig. 3b, c) is integrated within the q-space region shown by a brown circle on the ραβ(q, E) of Fig. 4a, it yields ρMA(q, E) as plotted in Fig. 4c. The theoretically predicted ρ(0) (E) curves are overlaid for comparison. It is clear that the experimental ρMA(q, E) is consistent with the ρTH(0) theory because it does not change sign and exhibits a peak at E ≈ 3.7 meV ≈ √Δ1Δ2. In this way, the MAHAEM technique efficiently demonstrates that Δαβ changes sign between electron-like and hole-like bands of LiFeAs.

Conclusions

We report development and demonstration of an improved approach for signed Δαβ determination (Eq. (9)), but now for use with multiple impurity atoms or scattering centers. This MAHAEM technique for measuring ρ(0)(q, E) is based on a combination of the Fourier shift theorem and high-precision registry of scatterer locations. It extends the original HAEM approach4 to more disordered superconductors (Figs. 2a, 3a), enables its application to far larger fields of view thereby enhancing q-space resolution (Fig. 4b), and greatly increases signal-to-noise ratios (Figs. 1d, 4b) by suppressing phase randomization in multi-atom scattering interference. Overall, MAHAEM now represents a powerful and general technique for Δαβ determination in complex superconductors.

METHODS

Sample growth and preparation

FeSe samples with Tc ≈ 8.7 K were prepared using KCl/AlCl3 chemical-vapor transport and LiFeAs samples with Tc ≈ 15 K were grown using LiAs flux method. The highly reactive LiFeAs samples are prepared in a dry nitrogen atmosphere in a glove box.

SI-STM measurements and analysis

All samples are cleaved in situ in our ultra-high cryogenic vacuum STM at low temperature. The g (E) data were acquired with a 3He-refrigerator-equipped STM. The pincer level atomic registration was performed before applying the HAEM technique as described in full detail in the Supplementary Note 2. Full details of the multi-atom HAEM analysis are presented in detail in Supplementary Note 3. Theoretical predictions for ρ(0) curves were performed using the T-matrix formalism with energy gap on each band and normal state tight binding parameters fitted to experiments.

DATA AVAILABILITY

The datasets generated and/or analyzed during this study are available to qualified requestors from the corresponding author.

CODE AVAILABILITY

The simulation code for Fig 1 is provided as Supplemental material. All the other codes used during the current study are available to qualified requestors from the corresponding author.

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AUTHOR CONTRIBUTIONS

R.S., A.Kr., and M.A.S. contributed to this project equally. P.O.S., R.S., P.J.H., and J.C.S.D. designed the project. P.O.S. and M.A.S. developed the phase-resolved multi-atom averaging method; M.P.A., A.Ko., and P.O.S. carried out the experiments; R.S. and P.O.S. carried out the data analysis; A.Kr., M.A.S., J.B., P.J.H., and I.E. carried out the theoretical analysis. P.C.C. and A.E.B. synthesized single-crystalline FeSe samples; H.E. synthesized single-crystalline LiFeAs samples. J.C.S.D. and P.J.H. supervised the investigation and wrote the paper with key contributions from P.O.S., R.S., M.A.S., and A.Kr. The manuscript reflects the contributions of all authors.

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

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