Large enhancement of radiative strength for soft transitions in the quasicontinuum

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Radiative strength functions (RSFs) for the 56,57Fe nuclei below the separation energy are obtained from the 57Fe(3He,αγ)56Fe and 57Fe(3He,3He′γ)57Fe reactions, respectively. An enhancement of more than a factor of ten over common theoretical models of the soft (Eγ ≤ 2 MeV) RSF for transitions in the quasicontinuum (several MeV above the yrast line) is observed. Two-step cascade intensities with soft primary transitions from the 56Fe(α,2γ)57Fe reaction confirm the enhancement.

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Unresolved transitions in the nuclear γ-ray cascade produced in the decay of excited nuclei are best described by statistical concepts: a radiative strength function (RSF) f_{XL}(E_γ) for a transition with multipolarity XL and energy E_γ, and a level density ρ(E_i, J^π_i) for initial states i at energy E_i with equal spin and parity J^π_i yield the mean value of the partial decay width to a given final state f

\[ \Gamma_{if}^{XL}(E_\gamma) = f_{XL}(E_\gamma) \frac{E^{2L+1}_\gamma}{\rho(E_i, J^π_i)} . \]  

(1)

Most information about the RSF has been obtained from photon-absorption experiments in the energy interval 8–20 MeV, i.e., for excitations above the neutron separation energy S_n. There, the giant electric dipole resonance (GEDR) is dominant. Data on the soft (E_γ < 3–4 MeV) RSF for transitions in the quasicontinuum (several MeV above the yrast line) remain elusive. Corresponding data from discrete transitions show large fluctuations and are biased toward high transition strengths due to experimental thresholds. First data in the statistical regime have been obtained from the 147Sm(n,γα)144Nd reaction 2. They indicate a moderate enhancement of the soft E1 RSF compared to a Lorentzian extrapolation of the GEDR. For spherical nuclei, in the framework of Fermi-liquid theory, this enhancement is explained by a temperature dependence of the GEDR width 2, the Kadmon-skii-Markushev-Furman (KMF) model. However, the experimental technique requires the presence of sufficiently large α widths and depends on estimates of both α and total radiative widths in the quasicontinuum below S_n.

The sequential extraction method developed at the Oslo Cyclotron Laboratory (OCL) 2 has enabled further investigations of the soft RSF by providing unique data for transitions in the quasicontinuum with sufficient averaging. For deformed rare-earth nuclei, it has been shown that the RSF can be described in terms of a KMF GEDR model, a spin-flip giant magnetic dipole resonance (GMDR), and a soft M1 resonance 2,6. In this work, we report on the first observation of a strong enhancement of the soft RSF in 56,57Fe over the sum of the GEDR and GMDR models. This enhancement has been found in Oslo-type experiments and is confirmed independently by two-step cascade (TSC) measurements. To our knowledge, there exists at present no theoretical model which can explain an enhancement of this magnitude.

The first experiment, the 57Fe(3He,3He′γ)57Fe and 57Fe(3He,αγ)56Fe reactions, was carried out with 45-MeV 3He ions at the OCL. Particle-γ coincidences were measured by eight Si particle telescopes at 45° and by an array of 28 NaI(Tl) 5° × 5° γ detectors with a solid-angle coverage of ~15% of 4π. The reaction spin window was I ∼ 0–4 h. The 3.4-mg/cm²-thick, self-supporting 57Fe target was enriched to ~ 95%. The experiment ran for one week with a beam current of ∼ 2 nA. Total γ-cascade spectra were constructed in 240-keV excitation-energy bins in the residual nuclei. These spectra were unfolded and a primary-γ matrix P was obtained by a subtraction method 2. This matrix was factorized into a level density and total RSF (summed over all multipolarities) according to the Brink-Axel hypothesis 2 by

\[ P(E_i, E_\gamma) \propto \rho(E_i, E_\gamma) f_{57}(E_\gamma) E^3_\gamma . \]  

(2)

More details on the data analysis, including the normalized level densities of 56,57Fe, are given in 2 and references therein.

RSFs are brought to an absolute scale by normalizing them to the average total radiative width (Γ_γ) of neutron resonances 2. There, the assumption of equal amounts of positive and negative parity states at any energy below S_n is made. The violation of this assumption for low excitation energies introduces a systematic error to the absolute normalization in the order of ~ 4%. In the case of 56Fe, also the value of (Γ_γ) has to be estimated from
The normalized RSFs in are consequently not affected by the above assumptions. The striking feature of the RSFs is a large strength for soft transitions which has not been observed in the case of rare-earth nuclei, where we used the same analysis tools.

The soft transition strength constitutes a more than a factor of ten enhancement over common RSF models recommended in compilations. To our knowledge, no other model can at present reproduce the shape of the total RSF either. A schematic temperature dependence of the RSF is taken into account in the KMF model.

The TSC experiment, i.e., the $^{56}$Fe($n, 2\gamma$)$^{57}$Fe reaction, was performed at the dual-use cold-neutron beam facility of the Budapest Research Reactor (see and references therein). About 2 g of natural iron was irradiated with a thermal-equivalent flux of $3 \times 10^7$ cm$^{-2}$s$^{-1}$ cold neutrons for ~7 days. Single and coincident $\gamma$ rays were registered by two Ge(HP) detectors of 60% and 13% efficiency at a distance of 8 cm from the target. They were placed at 62.5$^\circ$ with respect to the beam axis in order to minimize the effect of angular correlations. Chlorine and chromium targets as well as a certified $^{152}$Eu source have been measured to determine relative detector efficiencies up to 9 MeV $\gamma$ energy.

TSCs populating discrete low-lying levels in $^{57}$Fe produce peaks in the summed-energy spectrum shown on the left panel of Fig. Gating on the unresolved doublet of the $1/2^-$ ground state and the $3/2^-$ first excited state at 14 keV yields the TSC spectrum on the right panel of Fig. Spectra to other final levels were not investigated due to their lower statistics and higher background. The TSC spectrum is compressed to 250-keV-wide energy bins. It is symmetric around the midpoint (half of the sum energy) since always both $\gamma$ energies are recorded. When the sequence of the two $\gamma$ transitions is not determined experimentally, cascades with soft (discrete) secondary transitions are registered in the TSC spectrum as peaks on top of a continuum of cascades with soft primary transitions. Absolute normalization of TSC spectra is achieved by normalizing to five strong, discrete TSCs for their secondary transitions. Absolute normalization of TSC spectra is achieved by normalizing to five strong, discrete TSCs for their secondary transitions.
is $\sim 20\%$; the method does not rely on the knowledge of absolute detector efficiencies. The statistical portion of the TSC spectrum, i.e., the remaining smooth part when peaks due to strong, discrete cascades are removed, usually exhibits a bell shape. However, in the present case, the smooth part has a rather flat shape, especially in the wings of the spectrum below $\sim 1.5$ MeV and above $\sim 6.2$ MeV. This is already an indication for an unusual enhancement of cascades with soft primary $\gamma$ rays. In the following, the smooth part of the TSC spectrum will be investigated in more detail.

In order to separate cascades with soft primary and soft secondary transitions in the TSC spectra, we use the fact that the spacing of soft, discrete secondary transitions in regions of sufficiently low level density is considerably larger compared to the detector resolution. Thus, soft secondary transitions will reveal themselves as discrete peaks. On the other hand, soft primary transitions will populate levels which are spaced much closer than the detector resolution and will hence create a continuous contribution. Separation of soft primary and secondary transitions is therefore reduced to a separation of individual peaks from a smooth continuum (by, e.g., a fitting procedure) in the appropriate energy interval.

The spin of the compound state in $^{57}$Fe populated by $s$-wave neutron capture is $1/2^+$. Thus, in the excitation-energy region 0.55–1.9 MeV, there are only three levels which can be populated by primary $E1$ transitions: the $1/2^-$ level at 1266 keV, the $3/2^-$ level at 1627 keV, and the $3/2^-$ level at 1725 keV. All other levels have spins $5/2^-$ and higher and can only be populated by transitions with $M2/E3$ and higher multipolarity. Assuming that $\gamma$-transitions of such high multipolarities have a negligible contribution to the TSC spectrum, we do not take them into account in the further analysis. TSCs to the ground and first excited states involving the three above-mentioned levels as intermediate levels can easily be identified from their corresponding peaks in the TSC spectrum. Their contribution to the TSC spectra is subtracted. The remaining, continuous TSC spectrum in the specified energy range can be assigned to TSCs with soft primary $\gamma$-transitions. This smooth part of the TSC spectrum is used to test the soft RSF obtained from the Oslo-type experiment. Also, the mid point of the TSC spectrum, where energies of primary and secondary transitions are equal (and hence, known) has been used in the subsequent analysis. For other energy intervals, the determination of the sequence of the two transitions in TSCs is subject to large uncertainties, thus, they are unsuitable for the present analysis.

In the present analysis, the intensity of ordered TSCs between an initial and final state is calculated on the basis of the statistical model of $\gamma$-decay from compound states

$$I_{ij}(E_1, E_2) = \sum_{XL,XL',J_m} \frac{\Gamma_{im}^{XL}(E_1)}{\Gamma_i} \rho(E_m, J_m^\pi) \frac{\Gamma_{mf}^{XL'}(E_2)}{\Gamma_m},$$

(4)

where $E_1$ and $E_2$ are the energies of the first and second transition in the TSC which are connected by $E_1 - E_f = E_1 + E_2$. $\Gamma_{im}$ and $\Gamma_{mf}$ are partial and $\Gamma_i$ and $\Gamma_m$ are total decay widths of the initial and intermediate ($m$) levels, respectively. The average values of these widths can be calculated from the RSF by Eq. (1). Summing in Eq. (4) is performed over all valid combinations of multiplicities $XL$ and $XL'$ of transitions and of spins and parities of intermediate states. Thus, TSC spectra depend on the same level density and RSFs which are extracted from the Oslo-type experiment, see, e.g., Eqs. (24).

Statistical-model calculations with experimental values for the level density and the total RSF have been performed assuming the decomposition of $f_{E2}$ according to Eq. (6), and a standard spin-parity distribution for intermediate states. Four calculations were performed: one by neglecting the third term in Eq. (3), i.e., without the soft pole of the RSF, the other three under the assumption of $E1$, $M1$, and $E2$ multipolarity, respectively, for this term. In Fig. 3 results are compared to experimental data for energies where ordering of TSCs can be achieved. The calculation without the soft pole does not reproduce the data at all. The $\chi^2$ excluding the two data points at lowest $\gamma$ energies where we do not have experimental data on $f_{E2}$ yields $\sim 25$, thus, ruling out this calculation on a statistical significance level higher than 99.9%. For calculations under the assumption of $E1$ and $E2$ multipolarities for the soft pole, the $\chi^2$ gives $\sim 9$. Thus, although these multipolarities cannot be ruled out on a significance level better than $\sim 85\%$, they are unlikely. The $\chi^2_{\text{red}}$ for the calculation with the $M1$ hypothesis for the soft pole equals $\sim 1.3$ and makes this the preferred assignment. The selectivity between $M1$ and
$E1/E2$ assignment becomes better when including the two data points at lowest $\gamma$ energy. However, there, the statistical-model calculation is based on an extrapolation of $f_{\Sigma}$ below experimental data, hence, possible systematic errors can become large. To check the sensitivity of our result, we have performed calculations with an exponential and resonance description of the enhanced soft transition strength, both avoiding the pole for $E_{\gamma} \to 0$. The values of $\chi^2$ are rather insensitive to changes in the extrapolation of $f_{\Sigma}$. However, the experimental TSC intensities for the lowest two $\gamma$ energies are not so well reproduced as before. Finally, we have performed calculations where the ratio of the negative-parity levels to the total number of levels decreases linearly from $\sim$90% at 2.2 MeV to $\sim$50% at $\sim$7.6 MeV excitation energy. As expected, TSC intensities with soft primary $\gamma$ rays are rather insensitive to this variation as well.

In conclusion, a more than a factor of ten enhancement of soft transition strengths (a soft pole) in the total RSF has been observed in Oslo-type experiments using the $^{57}\text{Fe}^{(\alpha,\gamma)}^{56}\text{Fe}$ and $^{57}\text{Fe}^{(3\text{He},3\text{He}^*\gamma)}^{57}\text{Fe}$ reactions. This enhancement cannot be explained by any present theoretical model. The total RSF has been decomposed into a KMF model for $E1$ radiation, Lorentzian models for $M1$ and $E2$ radiation, and a power law to model the soft pole. In a second experiment, TSC intensities from the $^{56}\text{Fe}(n,2\gamma)^{57}\text{Fe}$ reaction were measured. Statistical-model calculations based on separated RSFs from the decomposition of the experimental total RSF and on experimental level densities from the Oslo-type experiment were performed. These calculations can reproduce the experimental TSC intensities with soft primary $\gamma$ rays only in the presence of the soft pole in the total RSF. $M1$ assignment for the soft pole is preferred, but $E1$ and $E2$ multipolarity cannot be ruled out on a significance level better than $\sim 85\%$. The satisfying reproduction of the experimental TSC data constitutes support for the physical reality of the soft pole, independent from the Oslo-type experiment. It should be noted that this support was gained by using a different nuclear reaction, a different type of detector, and a different analysis method. Finally, as further supporting evidence, we would like to mention that preliminary results on a chain of stable Mo isotopes also indicate the presence of a soft pole in the total RSF, while in the case of $^{27,28}\text{Si}$, the Oslo method was able to reproduce the total RSF constructed from literature data on energies, lifetimes, and branching ratios available for the complete level schemes.

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