The present study concerns the technical aspects of obtaining the energetics for the E4 state of nitrogenase, the enzyme that fixes N₂ in nature. EPR experiments have shown that the critical E4 structure that activates N₂ should contain two bridging hydrides in the FeMo-cofactor. It is furthermore in equilibrium with a structure where the two hydrides have been released and N₂ binds. These observations led to the suggestion that E4 should have two bridging hydrides and two protonated sulfides. It is important to note that the structure for E4 has not been determined, but only suggested. For a long time, no DFT study led to the suggested structure, independent of which functional was used. However, in two recent DFT studies a good agreement with the experimental suggestion was claimed to have been obtained. In one of them the TPSS functional does reproduce the experimental findings for E4, the key species in N₂ activation by nitrogenase. In the other one, Björnsson et al. showed that the TPSSh functional might also work. The suggested E4 structures were obtained after only four reductions. In our previous studies, we have not been able to reproduce the experimentally obtained energetics for E4, if the structure should be obtained after only four reductions, as suggested experimentally. Instead, four additional reductions were required to find an E4 structure that agreed with the experimental findings concerning both structure and energetics. The additional reductions were suggested to occur only once before catalysis starts. Our previous studies strongly
The structures of the reduced E-states, including E4, have just been indirectly assumed.

The experimentally deduced structure for the active E4 state, became controversial after a series of theoretical studies. The suggested E4 structure was found to be very high in energy using the B3LYP functional (for both 15% or 20% exact exchange). The experimental E4 structure, with a central carbide and two hydrides, was shown to be more than 30 kcal/mol higher than the lowest energy structure, which was found to have a triply protonated carbide. Still, it is in principle possible that B3LYP completely fails in this particular case in a way not seen for any other enzyme. Therefore, tests were made by changing the fraction of exact exchange, which has been shown to be the most sensitive parameter in B3LYP. The most critical aspect for testing this parameter is for the step where the two hydrides leave to form H2 in the step where N2 becomes bound. That step was well established experimentally to be reversible, suggesting a small energy difference between the reactant and final E4 states. The DFT tests for this step showed that the loss of H2 is very exergonic, by more than 40 kcal/mol, independent of the fraction of exact exchange, which was varied between 0% and 20%. This result suggests that all DFT functionals should have a similar problem for the suggested E4 structure. In the two recent theoretical studies by Ryde et al and Björnsson et al of the E4 state, the energetics of that step was not investigated.

A clarification is needed concerning a recent dismissal of the mechanism suggested by the present calculations. That dismissal is incorrect, since the number of electrons in the suggested E4 structure has been misread. The criticism was that the theoretically suggested structure would lead to a singlet state for E4, since it should have an even number of electrons, which would be in disagreement with the EPR analysis which shows that E4 is a doublet state. However, it is clearly stated in the theoretical paper that the suggested E4 structure has an odd number of electrons in agreement with EPR.

### 2 | COMPUTATIONAL DETAILS

The present study only concerns calculations using TPSS and TPSSh. For the calculations with the TPSSh functional, (model 1, Figure S1) is the same as the one used previously for nitrogenase, consisting of about 270 atoms. For the calculations with the TPSS functional, two extra water molecules are added into the previous model, as suggested by the study by Ryde et al (model2, Figure S2). Some backbone atoms were kept fixed from the X-ray structure, as shown in detail in the SI. The basis set used for the geometry optimization was the LACVP basis set. For the optimized geometries, single point calculations were performed with a large basis set with cc-pvtz(−f) for all atoms except for the metals, which were described by the LACV3P basis. Dielectric effects with a dielectric constant of 4.0 and the D2 dispersion effects were also added as usual. This is the standard procedure used for a large number of enzyme mechanisms. Translational entropy is important in the
The present study concerns the suggested structures of the E4 state as obtained after four reductions from the experimentally well characterized ground state E0. Only the TPSS\(^3\) and TPSSh\(^5\) functionals have been used here. For comparison the energetic results for E4 obtained in the previous B3LYP study\(^14\) are given in Table 1. For the nomenclature used, \((C, 2H^+)\) has a central carbon and two hydrides; \((CH_3)\) has a terminal CH$_3$ and no hydrides; \((C-H_2)\) has a central carbide and a free H$_2$. The percentages given refer to the amount of exact exchange used in the B3LYP functional. The two rows of highest interest here are the ones of \((C, 2H^+)\) and \((C-H_2)\). \((C, 2H^+)\) gives the energy for the experimentally suggested structure, here set to zero, and \((C-H_2)\) the energy of the structure, for which H$_2$ has been removed. It should first be noted that for all fractions of exact exchange, the energies are much lower for \((C-H_2)\), showing that the removal of the two hydrides is very exergonic. The exergonicity for 0% (non-hybrid) is 34.0 kcal/mol, for 10% it is 43.3 kcal/mol, for 15% it is 48.0 kcal/mol and for 20% it is 54.6 kcal/mol. Since the fraction of exact exchange is by far the most sensitive parameter in B3LYP, the results suggest that the large exergonicity would remain for all DFT functionals. The experimental analysis requires that the loss of H$_2$ together with the binding of N$_2$ should be almost thermoneutral, since it is easily reversible. A thermoneutral E4 step and a very exergonic H$_2$ release, would require a very strong binding of N$_2$, which is contrary to what is found in any calculation so far, particularly, when the loss of translational entropy of 9.9 kcal/mol is accounted for. Instead a very weak binding is found. Therefore, the calculated results show that all the B3LYP functionals predict a very exergonic E4 step for the experimentally suggested structure, in conflict with the experimental EPR analysis. The conclusion was therefore that the experimentally suggested structure is not correct. There has been one theoretical study suggesting how this problem might be solved for the experimentally suggested structure.\(^20\) To allow the disappearance of the hydrides and still prevent the energy loss going to a free H$_2$, the molecularly bound H$_2$ state formed was suggested to be prevented from being released from the cofactor by very high barriers. These barriers have to be at least 20 kcal/mol, but this was not demonstrated in the suggested mechanism. In a later study,\(^13\) only a small barrier of a few kcal/mol was found for releasing H$_2$, which would not be enough to explain the experiments.

Even considering the results described above, there have been two recent suggestions that there should be functionals that still reproduce the experimental energetics. Ryde et al showed that using TPSS,\(^2\) the lowest energy E4 structure is indeed the experimentally suggested structure, with a central carbide and two bridging hydrides, which was therefore suggested to reproduce the experimentally suggested mechanism. That would be the first DFT functional that gave that result. In light of the previous results in Table 1, this would be very surprising. In order to investigate if the suggestion by Ryde et al is possible, the TPSS functional was used for calculating the energy difference between the \((C, 2H^+)\) and the \((C-H_2)\) structures. The optimized structure for \((C, 2H^+)\) is shown in Figure 2. The spin-distribution, including the alternations of the spins, is the same as in the Ryde et al study, and the spin-populations are very similar. The positions of the hydrides are also the same. Removing H$_2$ from the cofactor to reach the \((C-H_2)\) structure, keeping the same sulfides protonated, reduces the energy by −16.6 kcal/mol. The optimized structure is shown in Figure S3. For the \((C-H_2)\) structure, when moving the proton from SSA to S3A, the energy goes down by an additional −10.2 kcal/mol, which means that the exergonicity drops to −26.8 kcal/mol. The optimized structure is shown in Figure S4. For the entries in Table 1, 0% has a difference of −34.0 kcal/mol, and should be the one most similar to the non-hybrid TPSS method. It should be noted that slightly different models have been used. It is clear that the E4 structure suggested by TPSS, is not able to give reasonable energetics for the nitrogenase mechanism, even though the structure with two hydrides agrees with the one suggested for E4 by experiments.

**TABLE 1** Relative energies (kcal/mol) for the E4 state of nitrogenase, using B3LYP density functionals with different fractions of exact exchange.\(^14\) TPSS and TPSSh functionals

| Structure | B3LYP | TPSS | TPSSh |
|-----------|-------|------|-------|
| C,2H⁺     | 0     | 0    | 0     |
| CH₃       | −6.1  | −38.9| −62.6 |
| C-H₂      | −34.0 | −43.3| −48.0 |

**FIGURE 2** The TPSS optimized structure \((C, 2H^+)\) with two bridging hydrides and a central carbide. Distances (Å) between the iron and the hydrides are shown in blue italic. Spin populations are shown in red italic. For clarity, only the core of the model is shown [Color figure can be viewed at wileyonlinelibrary.com]
The two recent suggestions, that TPSS2 or TPSSh4 could be used for calculating the energetics of the nitrogenase mechanism, have been investigated by calculating the most critical part of the N2 activation in nitrogenase. In previous studies by Ryde et al, 10 different DFT functionals were tried and none of them reproduced the experimentally suggested mechanism. The first DFT functional, gave the suggested structure, making it very reducing for the activation of N2. The TPSSh functional gives an exergonicity of −26.8 kcal/mol, and the TPSSh functional one of −39.5 kcal/mol. These results are in line with a previous study, systematically investigating this energy difference by varying the fraction of exact exchange. This means that all DFT functionals investigated so far, agree on the finding that the experimentally suggested structure leads to energetics of the E4 state, which is very far from the conclusions drawn by the analysis of the EPR experiments.

In the above context, it is important to point out that a different scenario has been suggested by theoretical modeling, which leads to both a structure and energetics in very good agreement with the analysis of the EPR experiments. The difference to the experimentally suggested mechanism is that an additional four reduction steps are introduced before catalysis starts. These reduction steps lead to an oxidation state for the cofactor without any Fe(III) present in E4. After hydride loss as H2, there will actually be two Fe(II) atoms in the structure, making it very reducing for the activation of N2. The suggested mechanism is also in full agreement with the Lowe-Thorneley analysis, since the activation step occurs only once before the reductions in the actual catalytic cycle starts. As previously shown, also the energetics of the remaining protonation steps to reach the NH3 product are in good agreement with available experimental thermodynamics and kinetics. At the end of the catalytic cycle, the cofactor is very highly excited due to the reductions and will eventually fall down into its lowest energy state (E0), as all systems in nature do. The lowest energy state is the initial state before reduction, which is therefore the state observed also after catalysis.

There are two possible conclusions that can be drawn from the present study. The first one is that DFT should not be used to study nitrogenase, since there are errors much larger than seen for any other similar enzyme. The second possibility is that the experimentally suggested structure is not correct. An alternative structure has been suggested with a protonated carbide with good agreement to the experimentally deduced structure and energetics.

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