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Ventilation procedures to minimize the airborne transmission of viruses in classrooms

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1. Introduction

The COVID-19 pandemic caused by the novel SARS-CoV-2 virus has put indoor environments in the spotlight since they are where virus transmission predominately occurs \cite{1-4}. Indeed, insufficient ventilation in highly crowded environments such as restaurants, schools, and gyms does not allow proper dilution of virus-laden respiratory particles emitted by infected subjects, leading to a high percentage of secondary infections amongst exposed susceptibles \cite{2,5-8}. To this end, governments worldwide have imposed temporary shutdowns of most indoor environments, including schools \cite{9-14}, being in the difficult role of deciding whether to prioritize the right to education or to health. After the first pandemic wave (early 2020), guidelines for reopening schools were prepared and adopted in view of opening the schools in the late (northern hemisphere) summer, but they mainly relied upon promoting personal behaviors and basic non-pharmaceutical mitigation measures (i.e. social distancing, hand washing hand, wearing masks) that address close contact transmission \cite{15}, which is a minor route of transmission in indoor environments if a social distance is guaranteed \cite{16,17}. The limited effect of such measures was confirmed by a resurgence of the virus in late 2020 that caused schools to close once more in many countries worldwide \cite{18,19} (en.unesco.org/covid19/educationresponse). Thus, in order to open schools safely at the time of pandemics, airborne transmission related to the small airborne respiratory particles (droplet nuclei) \cite{15} needs to be taken into account since it is potentially the dominant mode of transmission of numerous respiratory infections, including SARS-CoV-2 \cite{3,20-23}; therefore, while waiting for the vaccination campaign to be completed, a suitable solution to minimize the virus transmission potential in schools is providing \textit{ad-hoc} ventilation able to lower the virus concentration indoors \cite{6,8,24,25}.

The provision of a proper ventilation rate certainly cannot be taken for granted since most of the schools worldwide rely upon natural ventilation and manual airing (e.g. 86% of the European school buildings investigated within the SINPHONIE project \cite{26,27}). In these schools, in order to minimize the risk of infection, common sense rules based on a frequent airing of the classrooms were suggested (e.g. opening windows for 5 min every 20 min as stated by the German Environmental Agency) but this cannot be definitively considered as a science-based control strategy. For such schools, a potential approach to monitor and minimize the virus spread in indoor environments could be...
the use of a proxy providing real-time information on the virus concentration indoors then suggesting to apply manual ventilation procedures accordingly. Exhaled CO₂ has been proposed as a possible proxy for virus transmission indoors as it is a commonly used indicator of the ventilation rate and, more generally, indoor air quality [28–31]. While in principle exhaled CO₂ could be a good proxy for indoor-generated gaseous pollutants (e.g. VOCs, radon) [32], it cannot predict behaviors and dynamics of virus-laden particles which are affected by phenomena typical of all airborne particles such as deposition, and filtration (if any) in addition to virus inactivation. As such, the best application of exhaled CO₂ is estimating the air exchange rate of confined spaces [33,34]. Nonetheless, at this stage of the scientific debate, the question is not just demonstrating the qualitative association between ventilation (or CO₂ levels) in buildings and the transmission of infectious diseases [3,5,6,24,28,35,36], but quantifying and guaranteeing the required ventilation in highly crowded environments (e.g. schools) to reduce the spread of infectious diseases via airborne route whether mechanical ventilation systems are installed or not.

In the present paper we evaluated the required air exchange rates for mechanically-ventilated schools and adequate airing procedures for naturally-ventilated schools to reduce the transmission potential of a respiratory virus (expressed as reproduction number) through the airborne route of transmission. Moreover, a suitable feedback control strategy, based on the continuous measurement of the indoor exhaled CO₂ concentration, was proposed to monitor that an acceptable individual risk of infection is continuously maintained even in schools not equipped with mechanical ventilation systems. To this end, simulations based on virus and exhaled CO₂ mass balance equations considering typical school scenarios were performed.

2. Materials and methods

The required air exchange rates and the adequate airing procedures to maintain an acceptable level of the virus transmission risk were calculated adopting the virus and CO₂ mass balance equations (described in section 2.1 and 2.2) under the simplified hypothesis that they are both instantaneously and evenly distributed in the confined space under investigation (box-model). Here particle deposition and virus inactivation phenomena were taken into account and dynamic scenarios (described in section 2.3) have been simulated within the 5-h school-day. Two different viruses, characterized by extremely different emission rates (i.e. different viral loads and infectious doses) [37], were considered: SARS-CoV-2 and seasonal influenza. The study involves infected people breathing and/or speaking whereas severely symptomatic persons frequently coughing or sneezing were not included in the scenarios. The simulations were performed under the hypothesis that the students are adequately spaced so that ballistic deposition of large respiratory particles (>100 μm) onto mucous membranes is considered negligible [15]; thus, virus transmission results solely from the inhalation of airborne particles (i.e. airborne transmission).

2.1. Evaluation of the virus transmission potential

The virus transmission potential due to the airborne route was assessed in terms of event reproduction number ($R_{event}$) which is the expected number of new infections arising from a single infectious individual at a specific event [38] (e.g. a single school day). In particular, the $R_{event}$ was evaluated adopting the approach proposed and applied in previous papers [5,6,39]; involving successive steps: (i) the quanta emission rate, (ii) the exposure to quanta concentration in the microenvironment, (iii) the dose of quanta received by exposed susceptible subjects, (iv) the probability of infection on the basis of a dose-response model, (v) the individual risk of the exposed person, and, finally, (vi) the event reproduction number. The above-mentioned “quanta” is a measure to quantify the virus emission or concentration, it is defined as the infectious dose for 63% of susceptibles by inhalation of virus-laden particles. In particular, the evaluation of the quanta emission rate ($ER_q$, quanta h⁻¹) was described in our previous papers taking into account the viral load, infectious dose, respiratory activity, activity level, and particle volume concentration expelled by the infectious person [5,6,37]. In particular, particle volume concentrations for breathing, speaking and loudly speaking expiratory activities hereinafter adopted were obtained from Stadnytskyi et al. [40] and Morawska et al. [41] as already applied in our previous papers where the quanta emission rate model was developed and implemented [5]. The emission model provides a distribution of quanta emission rates, i.e. the probability density function of $ER_q$. It represents a major step forward to properly simulate and predict infection risk in different indoor environments via airborne transmission since previous studies were performed adopting quanta emission rates obtained from rough estimates based on retrospective assessments of infectious outbreaks only at the end of an epidemic [24,42]. The authors point out that the quanta emission model is not reported for the sake of brevity, nonetheless, readers interested in deepening their knowledge on the model itself and/or on the adopted parameters should refer to our previous papers [5,6]. The predictive approach also enables stochastic analysis of individual risk of infection that is not possible when using a point estimate obtained from a superspreading event.

The indoor quanta concentration over time, $n(t,ER_q)$, is evaluated, for each possible $ER_q$ value, adopting the above-mentioned simplified mass balance equation as:

$$n(t,ER_q) = n_0 e^{-\lambda t} \cdot \frac{ER_q I}{(AER+k+\lambda) V} (1-e^{-(AER+k+\lambda) t}) \, \text{(quanta m}^{-3}\text{)}$$

(1)

Where $n_0$ represents the initial quanta concentration (i.e. at time $t = 0$), $AER$ (h⁻¹) is the air exchange rate, $k$ (h⁻¹) is the deposition rate on surfaces, $I$ (h⁻¹) is the viral inactivation rate, $I$ is the number of infectious subjects, and $V$ is the volume of the indoor environment. The authors point out that further droplet removal processes could occur in case of using portable air cleaners and/or recirculation and air filtration by HVAC systems. In those cases, equivalent air change rates of these removal processes should be added to the ($AER+k+\lambda$) term [43,44].

In the quanta concentration equation (eq. (1)) we calculated the total quanta emission rate as a simple product of the number of infected subjects ($I$) times the $ER_q$ of the infected occupant. In the exposure scenarios hereinafter reported this simple calculation still holds since we have considered just one infected subject for each scenario. Anyway, in case of multiple infected occupants in a shared indoor microenvironment, a more accurate quantification of the higher expected cumulative quanta emission for over-dispersed pathogens should be obtained creating $ER_q$ distributions through Monte Carlo simulations, i.e. randomly sampling the $ER_q$ distribution of each infected subject and summing the results, instead of roughly applying the product $ER_q I$.

The dose of quanta ($D_q$) received by a susceptible subject exposed to a certain quanta concentration for a certain time interval, $T$, can be evaluated by integrating the quanta concentration over time as:

$$D_q(ER_q) = IR \int_0^T n(t,ER_q) \, dt \, \text{(quanta)}$$

(2)

where IR (m² h⁻¹) is the inhalation rate of the exposed subject which is a function of the subject’s activity level and age [45,46]. The probability of infection ($P(ER_q)$, %) of exposed persons is the conditional probability of the infection, given a certain $ER_q$, and it is evaluated on the basis of simple Poisson dose-response model [47,48] as:

$$P(ER_q) = 1 - e^{-\lambda I(ER_q)} \, \%$$

(3)

The individual risk of infection (R) of an exposed person for a given
exposure scenario is then calculated integrating, over for all the possible ERq values, the product between the conditional probability of the infection for each ERq (Pq(ERq)) and the probability of occurrence of each ERq value (Pq(ERq)):

\[ R = \int_{\text{ERq}} (P_{q}(\text{ERq}) \cdot P_{\text{ERq}}) \, d\text{ERq} \quad (\%) \] (4)

Such an individual risk R, for a given exposure scenario, represents the ratio between the number of new infections (number of cases, C) and the number of exposed susceptible individuals (S). The Renvent (expected number of new infections, C, arising from a single infectious individual, I, at a specific event) can be obtained as the product of R and S:

\[ R_{\text{event}} = R \cdot S \quad \text{(infections)} \] (5)

Therefore, the maximum number of susceptibles that can stay simultaneously in the confined space under investigation for an acceptable Renvent < 1 (hereinafter referred as maximum room occupancy, MRO) is:

\[ MRO < 1/R \quad \text{(susceptibles)} \] (6)

2.2. Evaluation of the CO2 indoor levels

To estimate the trend of indoor (exhaled) CO2 concentration over time (CO2out) a mass balance equation was applied considering the initial indoor CO2 concentration (at t = 0) equal to outdoor air (CO2out,0), the mass balance equation can be simplified as [33]:

\[ CO2_{\text{out}}(t) = CO2_{\text{out}} + \frac{ER}{V\text{-AER}} \left(1 - e^{-\lambda t} \right) \quad \text{ppm} \] (7)

where ER represents the overall exhaled CO2 emission rate in the indoor environment under investigation; the emission rate per-capita are available in the scientific literature (typically expressed in m3 h−1 person−1) as a function of the activity level, age, and gender [49]. As mentioned above, for known and steady state emission rate and outdoor CO2 concentration, the indoor concentration is just affected by the air exchange rate of the room, and the AER can be back-calculated from the eq. (7) measuring continuously the indoor CO2 concentration (CO2out,i): this measurement method is known as “constant injection rate method” [33,50].

2.3. Simulated scenarios

The individual risk of infection and the event reproduction number of a disease due to the airborne transmission route of the virus were assessed considering a high-school classroom (e.g. students aged 17–18) with a floor area of 50 m2 and a height of 3 m (V = 150 m3). A crowding index suggested by the standard EN 16798 [51,52] on the design of the ventilation for a proper indoor air quality (2 m3 person−1) was adopted then obtaining a total number of occupants (including the teacher) of 25 persons. A total school-time of 5 hours was considered. The simulations were performed considering one infected subject (I = 1), the teacher or one of the students, and 24 exposed susceptibles (S = 24) hypothesizing that none of them is already immune (e.g. vaccinated). Therefore, in order to obtain a Renvent < 1, the individual risk of infection (R) of the exposed susceptible over the 5-h school-time should be less than 1/24, i.e. < 4.2%.

The simulations were conducted for different scenarios, i.e. combination of emitting subject and mitigation solution (if any). Two different emitting subjects were considered in the simulation: the teacher and the student. In particular, simulations were performed considering (a) the infected teacher giving lesson (i.e. speaking or loudly speaking) for 1 h, in particular, the first hour of lesson was considered as it is clearly the worst exposure scenario for susceptible students attending the lesson (in fact, the later the infected teacher enters the classroom, the shorter the exposure period of the susceptible persons), or (b) the infected student attending lessons, then just breathing, and/or speaking occasionally. The exposed susceptibles were considered performing activities in a sitting position then inhaling at IR = 0.54 m3 h−1 [45,46].

The emitting scenarios are summarized in Table 1, whereas the corresponding quanta emission rate probability distribution function for SARS-CoV-2 and seasonal influenza viruses, as a function of activity level (i.e. sitting) and respiratory activity, are summarized in Table 2 as obtained from previous papers [5,6]. The ERq clearly increases for more severe respiratory activities, e.g. the median SARS-CoV-2 ERq ranges from 0.575 quanta h−1 for oral breathing to 15.85 quanta h−1 for loudly speaking. Moreover, due to its higher infectious dose (i.e. RNA copies to reach a quanta), for similar activity levels and respiratory activities, the SARS-CoV-2 ERq values were much higher than the seasonal influenza ones [5,37,53–55] (e.g. more than 10-fold at median value).

Despite the base scenarios, as summarized in Table 1, the possible effects of infected student’s speaking duration (10%–40% of the time), class duration (school hour of 55, 50, 45, or 40 min instead of 60 min), infected teacher’s voice modulation (e.g. using microphone), and wearing mask were considered in the simulations and described in detail. The effect of the mask was simulated considering an overall 40% reduction of the dose of quanta received by the susceptibles [56], to this end, in such simulations the ERq values multiplied by 0.6.

The emission rate of exhaled CO2 was evaluated considering a per-capita emission rate equal to 0.0158 m3 h−1 person−1 as an average value between male and female teenager students (e.g. aged 17–18) with a level of physical activity of 1.3 met [49], which is the suggested level for reading, writing, typing in a sitting position at school. The same emission rate was adopted for the teacher and, for the sake of simplicity, we did not consider possible variations in the exhaled CO2 due to the different expiratory activities (e.g. breathing, speaking or loudly speaking). Thus, the overall emission rate (ER) was evaluated multiplying the per-capita emission rate by the number of student/teacher (25 persons), then it resulted equal 0.396 m3 h−1. In the simulations here proposed the outdoor CO2 concentration (CO2out,0) was set at 500 ppm.

2.4. Required air exchange rates and airing procedures

The required air exchange rate to maintain a Renvent < 1 in mechanically-ventilated schools for the abovementioned scenarios was calculated adopting the methodology described in section 2.1 and, especially, the eq. (1)–(5). We point out that for mechanically-ventilated classrooms we refer to classrooms where the ventilation is guaranteed exclusively through the ventilation system extracting indoor exhaust air and supplying outdoor fresh air; thus, all the windows are kept closed during the school time (no hybrid ventilation). Quanta emission rates were selected from Table 2 on the basis of the activity of the emitting subject (Table 1), the geometry of the classroom were reported in the section 2.3, the virus inactivation rate (λ) for SARS-CoV-2 (0.63 h−1) [57] and seasonal influenza (0.80 h−1) [58] as well as the particle deposition rate (k = 0.24 h−1) [59] were obtained from the scientific literature. Having set these data, the individual risk of infection and, consequently, the event reproduction number, were just affected by the air exchange rate and the airing procedure of the classroom.

Quantifying the air exchange rate for mechanical ventilation systems is straightforward, as the outdoor air ventilation rate can be easily measured in most cases, and should be consistent with the original design parameters of the system (assuming proper installation and routine maintenance).

For schools not equipped with mechanical ventilation systems, which are the majority [26,27], to maintain a Renvent < 1 ad-hoc manual airing procedures based on manual airing cycles [32,60], i.e. adopting periods with windows closed and open alternatively, have to be determined. Indeed, unlike mechanical ventilation systems which are able to provide constant air exchange rate, the manual airing cycles will
analyze periods at low air exchange rates (with window close) and periods at higher air exchange rates (with window open), and most importantly, such air exchange rates are not known a priori but need to be evaluated and monitored continuously, as hereinafter reported, on the basis of a regression fit of indoor CO₂ concentration trends. Thus, for naturally-ventilated schools, an air exchange rate of the manual airing procedure can be calculated a-posteriori as school-day average resulting from the airing cycles (i.e. weighted average air exchange rate): \[ AER = \left( AER_{NV} \cdot t_{NV} + AER_{MA} \cdot t_{MA} \right) / \left( t_{NV} + t_{MA} \right) \ (h^{-1}) \] (8)

where AER_NV and AER_MA are the air exchange rates with window close (natural ventilation, NV) and window open (manual airing, MA), respectively, and t_NV and t_MA represent the total time during which the windows were kept closed and open, respectively; the sum of t_NV and t_MA clearly is the overall school time (i.e. 300 min). Since the air exchange rate is not constant all over the school day, the time at which the airing is adopted can significantly affect the quanta concentration trends. In fact, if a high quanta emission occurs when the windows are closed, the susceptibles could be exposed to high quanta concentrations then leading to a dose of quanta (and then an individual risk) larger than expected for a constant air exchange rate. In other words, for a certain exposure scenario, even when a school-day average AER provided with manual airing cycles is equal to the mechanical ventilation one, higher dose of quanta and individual risk can happen. Thus, in the case of manual airing cycles, higher average air exchange rates are needed to maintain a \( R_{event} < 1 \) with respect to classrooms equipped with mechanical ventilation systems, in particular for high but brief virus emissions. In our simulations, the manual airing cycles were applied at the end of each school-hour (instead of at the beginning of each lesson or between lessons), this just represents a constraint adopted in order to limit the number of scenarios to be simulated, nonetheless, it does not undermine the findings and the procedures we described.

Modeling air exchange rates from natural ventilation is extremely complex as leakages of the building (AER_NV) and airing (AER_MA) are strongly influenced by the airtightness of the building and of the windows, the wind conditions, the temperature difference between indoor air and outdoor air, the windows positioning within the classroom (single-sided vs. cross ventilation), and the window opening angle [60-64]. As an example, previous papers [32,62] performed experimental campaigns to measure the air exchange rate with window closed and opened through a CO₂ decay method in classrooms and obtained significant variations of AER_NV (<0.3 h⁻¹) and AER_MA (up to 5 h⁻¹).

Summarizing, the ventilation rate via natural ventilation and manual airing is not controlled; therefore, in view of maintaining a \( R_{event} < 1 \) a feedback mechanism (the indoor CO₂ concentration) is needed. We develop and apply this proper feedback control strategy to help optimize ad hoc airing in classrooms.

3. Results and discussions

3.1. Required air exchange rates for mechanically-ventilated schools

Fig. 1 presents the trends of quanta concentration, individual risk, maximum room occupancy, and indoor CO₂ concentration for the scenarios T-60-LS (teacher giving lesson loudly speaking for the first 60 min of the school-day) and T-60-S (i.e. speaking using a microphone instead of loudly speaking) in the case of SARS-CoV-2 virus when required AERs (to maintain a \( R_{event} < 1 \)) are provided through mechanical ventilation systems. In particular, for the scenario T-60-LS, as summarized in Table 3, the required AER is 9.5 h⁻¹ (i.e. > 15 L s⁻¹ person⁻¹). The quanta concentration trend increases sharply in the first 60 min (i.e. when the virus source is still in the classroom), then exponentially decays as soon as the teacher leaves the room and goes to zero at about 90 min. The individual risk reaches the maximum permitted value (4.2%) at 90 min, then remaining constant up to the end of the school-day (300 min) as we hypothesized that no other infected people enter the classroom. Similarly, as designed, the maximum occupancy decreases to the needed value of 24 persons at the end of the school-day. The authors point out that in the scenario T-60-LS the whole dose of quanta (and then individual risk) is received by the susceptibles in roughly 90 min, thus, we would have designed the same air exchange rate also in the hypothesis that the infected teacher gave a lesson at the second, third or fourth hour. Due to the high (and constant) AER = 9.5 h⁻¹, the CO₂ indoor reaches the (very low) equilibrium concentration of approximately 750 ppm in about half an hour.

For the scenario T-60-S, a much lower AER (0.8 h⁻¹; i.e. 1.3 L s⁻¹ person⁻¹) is required to maintain a \( R_{event} < 1 \), indeed, the CO₂ indoor concentration does not even reach an equilibrium level and continuously increases above 3000 ppm in 5 h, which is well above the concentrations suggested and obtainable if EN 16798 indoor air quality standards are adopted [51,52].

In Table 3 the required AERs to maintain a \( R_{event} < 1 \) for all the investigated scenarios are reported for SARS-CoV-2 for mechanically-ventilated classrooms; the required AER for seasonal influenza-
infected subjects is not reported since it is < 0.1 h⁻¹ for all the scenarios under investigation. Thus, all the ventilation techniques are able to protect against the spreading of the seasonal influenza virus in classroom through airborne transmission. On the contrary, for SARS-CoV-2-infected subjects, the required AERs can be quite high: as mentioned above, for a teacher giving lesson for 1 h the required AER is 9.5 h⁻¹. Such AER can be reduced adopting shorter lessons (e.g. for 40-min lessons it can decrease down to 6.1 h⁻¹) or, even more, as discussed above, keeping the voice down while speaking (e.g. using microphones, this would require just 0.8 h⁻¹) and simultaneously wearing masks (then lowering the required AER down to 0.2 h⁻¹). If the infected subject is a student, an AER of 0.8 h⁻¹ is needed if she/he does not speak for the entire school-day, then increasing for longer speaking periods (e.g. 3.5 h⁻¹ are required if she/he speaks for 40% of the school-day).

In Fig. 2 the individual risk, R, of students for different exposure scenarios characterized by the presence of a SARS-CoV-2-infected teacher giving lesson for 60 min as a function of the air exchange rate provided by a mechanical ventilation system is presented. In particular, the base scenario (teacher loudly speaking) and the mitigation solutions (voice modulation and use of mask) are graphed. As expected the individual risk clearly decreases for higher AERs and, as summarized in Table 3, very high AERs are required for the teacher when loudly speaking. Such high AERs are likely not reproducible in schools without mechanical ventilation systems; indeed, in our previous papers [32,60,62,65] we have estimated that the AER, when no airing procedures are provided (e.g. side-ventilation) are occurring.

### Table 2

| Quanta emission rate distribution | SARS-CoV-2 | Seasonal influenza |
|----------------------------------|------------|-------------------|
| Log₁₀ERₐ average                 | 0.240      | 1.400             |
| Log₁₀ERₐ st. dev.                | 1.200      | 0.840             |
| 5th percentile (quanta h⁻¹)      | 0.006      | 0.002             |
| 25th percentile (quanta h⁻¹)     | 0.089      | 0.011             |
| 50th percentile (quanta h⁻¹)     | 0.575      | 0.040             |
| 75th percentile (quanta h⁻¹)     | 3.710      | 0.147             |
| 95th percentile (quanta h⁻¹)     | 54.17      | 0.959             |

### Table 3

| Scenarios                          | AER (h⁻¹) |
|-----------------------------------|-----------|
| Base scenarios                    | T-60-LS 9.5 |
| S-0%-S                            | 0.8       |
| Student’s speaking effect         | S-10%-S 1.5 |
| S-20%-S                           | 2.1       |
| S-30%-S                           | 2.8       |
| S-40%-S                           | 3.5       |
| Class duration effect             | T-55-LS 8.6 |
| T-50-LS                           | 7.8       |
| T-45-LS                           | 6.9       |
| T-40-LS                           | 6.1       |
| Voice modulation effect           | T-60-S 0.8 |
| Mask effect                       | T-60-S-L-M 5.8 |
| Voice modulation & mask effect    | T-60-S-M 0.2 |

Fig. 1. Trends of quanta concentration (n), individual risk (R), maximum room occupancy (MRO), and indoor CO₂ concentration (CO₂ᵛ) resulting from the simulation of the base scenarios T-60-LS (solid lines) and T-60-S (dotted lines) in the case of SARS-CoV-2 virus having adopted the required constant AERs to maintain a R̅ᵣ<sub>ᵣ</sub> < 1 (9.5 h⁻¹ and 0.8 h⁻¹ for T-60-LS and T-60-S, respectively) through a mechanical ventilation system.
The high AERs required in some of the above-mentioned scenarios can be higher than those typically suggested by the current indoor air quality standards defined by the EN 16798 [51,52]. Indeed, the EN 16798 provides the AERs as a function of the category of the indoor air quality (I, II, or III) and categories of pollution from building itself (very low polluting building, low polluting building, non low polluting building). As an example, for the classroom under investigation, considering students as “non-adapted” persons (default choice for non-residential buildings), the air exchange rates suggested by the standard would be: 6.6 h\(^{-1}\) (very low polluting building), 7.2 h\(^{-1}\) (low polluting building) and 8.4 h\(^{-1}\) (non low polluting building) for building category I, 4.6 h\(^{-1}\), 5.0 h\(^{-1}\), and 5.9 h\(^{-1}\), for building category II, and 2.6 h\(^{-1}\), 2.9 h\(^{-1}\), and 3.4 h\(^{-1}\) for building category III, respectively. Thus, for such a critical scenario, in order to maintain a R\(_{\text{event}}\) < 1 at lower air exchange rates the number of susceptibles (S) should be reduced; to this end the most effective solution is increasing the vaccination fraction of the population. As an example, in Fig. 3 the R\(_{\text{event}}\) as a function of the air exchange rate (provided through a mechanical ventilation system) and of the percentage of vaccination for the T-60-LS scenario is reported. The figure clearly highlights that for such a critical scenario a percentage of vaccinated people >60% (i.e. > 14 persons) would allow reducing the required air exchange rate to about 3 h\(^{-1}\), i.e. to the AER suggested by the EN 16798 for building category III which is, by the way, the category recommended by the standard for existing buildings. The graph also confirms that reopening naturally ventilated schools by allowing up to 50% attendance as adopted in several countries would not guarantee a low transmission potential of the SARS-CoV-2, at least for highly emitting infected subjects. In that case, 12 susceptibles would be still present in the classroom, thus, according to the graph shown in Fig. 3, an AER > 4 h\(^{-1}\), not easily achievable in naturally-ventilated classrooms, would be required to obtain R\(_{\text{event}}\) < 1.

As mentioned in the methodology (section 2.4), for mechanically-ventilated classrooms, the R\(_{\text{event}}\) < 1 condition can be maintained if the required AERs obtained for the selected scenarios are adopted. In particular, in that case, a simple constant air volume flow system is enough to provide the required AER and no complex control algorithms, typical of demand-controlled ventilation systems, are needed. In fact, once the scenario is defined, in principle no feedback information is required: a possible procedure in the case of schools equipped with mechanical ventilation is schematically presented in Fig. 4. In particular, data regarding the expected scenario (e.g. teacher giving lesson for the first 60 min of the school-day using a microphone; total exposure time; classroom volume) should be provided to the control unit (e.g. inputting through a user input screen) that will be able to evaluate the required AER on the basis of the equations reported in the section 2.1 and, consequently, will set the needed air flow rate of the mechanical ventilation system. In other words, different modes of operation can be selected based on pre-determined activities and durations for the classroom (e.g. lecture, lunch, exercise activity, etc.). Optimizing the provided ventilation based on demand is important given the high energy cost of conditioning outside air in many climates [65-69]; however, our proposed strategy for practical infection control is based on the activities of the occupants rather than CO\(_2\) \(a\) \(p\)\(riori\). Where activity schedules are consistent, modes of operation can be scheduled in advance to eliminate the need for constant adjustment.

3.2. Airing procedures for naturally-ventilated schools

In the case of school without mechanical ventilation, maintaining a R\(_{\text{event}}\) < 1 is a challenge for scenarios characterized by high emitting infected subjects for two main reasons: i) keeping the windows opened could be not enough to guarantee very high outdoor air flow rates, ii) keeping the windows opened for long periods could be detrimental for thermal comfort and energy conservation purposes [62,65,70]. Adopting manual airing cycles described in the section 2.4 represents a practical solution, but it should be kept in mind that the scheduling of window opening and closing period can affect the infection risk of the exposed susceptibles and a required AER cannot be determined \(a\) \(p\)\(riori\). As an example, if AER\(_{\text{NV}}\) and AER\(_{\text{MA}}\) were a constant 0.2 and 4.0 h\(^{-1}\), respectively, for the scenario T-60-S, a R\(_{\text{event}}\) < 1 (i.e. R = 4.2%) could be obtained opening the windows for about 10 min at the end of each hour. The resulting school-day average AER would be equal to 0.8 h\(^{-1}\), which similar to that needed in case of constant mechanical ventilation systems. But, for lower AERs, e.g. constant AER\(_{\text{NV}}\) and AER\(_{\text{MA}}\) equal to 0.15 and 2.0 h\(^{-1}\), respectively, the required opening period at the end of each hour is 36 min then resulting in a school-day average AER of 1.3 h\(^{-1}\) which is significantly higher than that required in the case of steady state mechanical ventilation system. These two easy examples, highlight that the lower the AER\(_{\text{NV}}\) and AER\(_{\text{MA}}\) values, the longer the required airing period and, consequently, the higher the resulting school-day average AER.

Thus, the airing strategies are strongly affected by the air exchange rate values, therefore adopting scheduled airing procedures could be misleading. As an example, in October 2020 the German Environment Agency (UBA) and the Standing Conference of the Ministers of Education and Cultural Affairs of the Länder presented a joint press release (available at www.umweltbundesamt.de/en/press/pressinformations/coronavirus-protection-in-schools-airing-rooms-for) where recommendations on the school ventilation were provided: in particular, they

![Fig. 3. R\(_{\text{event}}\) for the T-60-LS scenario as a function of the air exchange rate (provided through a mechanical ventilation system) and of the percentage of vaccination.](image-url)

![Fig. 2. Individual risk, R (%), of students for different exposure scenarios characterized by the presence of a SARS-CoV-2 infected teacher giving lesson for 60 min as a function of the air exchange rate for mechanically-ventilated classrooms. Expected CO\(_2\) peak concentration as a function of the air exchange rate for mechanically-ventilated classrooms. Expected CO\(_2\) for 60 min as a function of the air exchange rate for mechanically-ventilated classrooms.](image-url)
recommend airing classrooms for 5 min after every 20 min. If such recommended scheduling were applied in the case of T-60-S scenario, in the likely hypothesis of having AER_{NV} at least equal to 0.2 h⁻¹, the simulation of quanta concentration, dose and individual risk of infection (eqs. (1)–(4)) would suggest a AER_{MA} > 3.3 h⁻¹ to maintain a R_{event} < 1. Nonetheless, as mentioned above, it’s doubtful that such air exchange rate can be reached through manual airing.

The above-mentioned examples highlight how AER_{NV} and AER_{MA} need to be continuously monitored so that the airing procedure can be adjusted in real-time. This procedure is obviously more complex than providing mechanical ventilation, and the support of control unit is even more important as it should be able to communicate with a CO₂ sensor and provide visual alerts on when opening and closing the windows, which will be performed manually by personnel in the classroom (e.g. teacher).

Alternatively, since it may be challenging to have a teacher or student reliably open and close a window in response to frequent prompts from the control unit, for relatively minor incremental cost one or more windows in the room could be fitted with a motorized louver, or damper, connected to the control unit such that the percent open of the window can be automatically adjusted by the system. Anyway, whatever the windows are automatically or manually opened, the ventilation procedure is equivalent and provided by the control unit. Indeed, data regarding the expected scenario will be provided to the control unit (through the user input screen as well), then the control unit will evaluate and suggest the manual airing procedure to be adopted in order to guarantee a R_{event} < 1. In particular, the control unit will use as feedback information the indoor CO₂ concentration continuously measured by an in-room sensor and, on the basis of the number of persons and their activity levels (that will be provided through the user input screen) and of the initial indoor CO₂ concentration, it will back-calculate the actual AERs during both the period with windows close (AER_{NV}) and open (AER_{MA}) using the CO₂ mass balance equation (eq. (7)) (Fig. 4). Such calculation should be performed adopting a multi-points method, i.e. finding the best regression fit to the continuous CO₂ data, which is more accurate than the two-points method (i.e. considering just the CO₂ measurement of start point and end point of natural ventilation and manual airing periods) [71] since it will be less affected by CO₂ sensor accuracy and intermittent “noisy” measurements. On the basis of the actual AERs the corrected t_{MA} and t_{NV} periods will be calculated by the control unit and the windows opening periods will be scheduled as well for the further 4 h (i.e. four cycles) in order to obtain a R_{event} < 1 (i.e. R = 4.2%) including the entire school-day (i.e. 5 h) in the calculation. The scheduled opening and closing periods also consider that if the infected teacher gives lesson on the second, third, fourth or fifth hour the R_{event} < 1 condition must be verified. Actually, the later the infected teacher enters the classroom, the shorter the exposure...
period of the susceptible persons (students in this case), this is the reason why we have considered the first hour in the simulations as worst scenario. Nonetheless, in case of very different airing periods amongst the airing cycles, the resulting risk for exposed people could be higher for teacher entering the classroom on the last hours than on the first ones, indeed, an infected teacher giving lesson on the last school hour could emit virus-laden droplets when the AER of that hour is not enough to reduce the risk of infection. This situation confirms the need for real-time feedback on what is going on in the classroom; to this end, the control unit needs to check if the opening periods based on actual AERs can guarantee a $R_{\text{event}} < 1$ also for infected teacher entering the classroom at different hours.

At the end of the second cycle $AER_{\text{MV}}$ and $AER_{\text{MA}}$ will be back-calculated again and, in case, the opening and closing periods will be modified again. Indeed, a high variability of the air exchange rate with windows open could occur, thus, significant corrections of the length of opening and closing periods may be needed.

An example application of the correction procedure is presented in Fig. 5 for the scenario T-60-S. In the figure the indoor $CO_2$ concentration, SARS-CoV-2 quanta concentration, and individual risk trend are presented. During the first hour a tentative airing cycle made up of 50 min with windows closed and 10 min with windows open was adopted. From the $CO_2$ trend, the actual $AER_{\text{MV}}$ and $AER_{\text{MA}}$ values were back-calculated and (in this illustrative example) are equal to 0.15 and 2.0 $h^{-1}$, respectively. On the basis of the actual AERs, in order to maintain a $R_{\text{event}} < 1$ (i.e. $R = 4.2\%$), the control unit schedules equally-spaced window opening periods of 42 min for the remaining 4 h to be applied at the end of each hour. Thus, the total times during which the windows were kept closed and open for the entire school day are $t_{\text{MV}} = 122$ min and $t_{\text{MA}} = 178$ min (having included the 50 min and 10 min of window closing and opening periods of the first hour) then resulting in a school-day average AER of about 1.3 $h^{-1}$. The tentative opening and closing periods adopted for the first hour were then too short compared to the actual low AERs, for this reason the quanta concentration in the first hour increases significantly and the individual risk trend as well with respect to the same scenario occurring in a classroom equipped with a mechanical ventilation system where a constant AER $= 0.8$ $h^{-1}$ is enough to maintain $R_{\text{event}} < 1$. The scheduled opening and closing periods also maintain a $R_{\text{event}} < 1$ if the infected teacher gave lesson in the second ($R = 4.1\%$), third ($R = 4.1\%$), fourth ($R = 3.8\%$) or fifth hour ($R = 2.4\%$). In this example the actual AERs were considered constant during the entire school-day, nonetheless, if the AERs at the end of each closing and opening periods do not match with the expected ones (0.15 and 2.0 $h^{-1}$ in this example) further corrections of the length of opening and closing periods are needed at the end of each hour.

3.3. Applicability and limitation of the methodology for ventilation control

The methodology presented in the paper addresses the proposed goals of (i) quantifying the required ventilation (provided through mechanical systems or manual airing) to reduce the spread of infectious diseases via the airborne route and (ii) proposing a suitable feedback control strategy to monitor and adjust such ventilation in naturally-ventilated classrooms. The methodology was then applied to some scenarios typically occurring in classrooms; we point out that our main aim was the definition of the methodology, thus the selected scenarios do not presume to be representative of all the possible situations or mitigation solutions potentially applicable in classrooms: as an example, we have not considered the use of more efficient masks, the use of air purifiers, the adoption of intermittent occupancy of the classroom [72]. Actually, the methodology proposed still holds for other scenarios (including other infected subject’s activities and emissions) here not considered and the ventilation procedure could be easily modified accordingly. Nonetheless, in order to effectively reduce the transmission potential of a disease, the uncertainty of the event reproduction number ($R_{\text{event}}$) should be taken into account such that, the required air exchange rate maintains ($R_{\text{event}} - U_{\text{event}} < 1$, with $U_{\text{event}}$ representing the expanded uncertainty (e.g. with a coverage factor of 95%). The evaluation of $U_{\text{event}}$ cannot be easily evaluated as it depends on several parameters and models adopted in the calculations presented in the section 2.1 (eqs. (1)-(5)). Indeed, when evaluating the $R_{\text{event}}$ (eqs. (1)-(5)) the following data are needed: quanta emission rate ($R_{\text{Q}}$), deposition rate ($k$), inactivation rate ($\lambda$), inhalation rate ($I$), room volume ($V$), air exchange rate ($AER$), time of exposure ($T$). The quanta emission rate was investigated in our previous papers where we highlighted that uncertainty relates to the quality of data on viral load, infectious dose and particle volume: such data, at least for SARS-CoV-2, are not definitive [47,55,73] also due to the presence of different viral lineages [74]. Therefore, even if the $R_{\text{Q}}$ data provided by our model are much more suitable than those typically estimated based on retrospective assessments of infectious outbreaks, a not negligible uncertainty exists. The deposition rate is mainly affected by the particle size [59] and, thus, adopting an average parameter, as typical of easy-to-use box-models, results in additional uncertainty as well; similarly, data on the virus inactivation rate for SARS-CoV-2 are still limited [57,75]. The inhalation rate depends on the activity levels of the subject; different scientific papers [45,76] reported different IR values for the same activity then confirming a significant variability as well. Room volume and time of exposure can be considered as fixed values (or at least with a not significant uncertainty contribution) as well as the AER if provided through a mechanical ventilation system. The uncertainty budget should also include the physical limitations of the box model (i.e. homogeneous concentration within the room), particle dosimetry model, and dose-response model as well. In particular, the homogenous concentration of quanta within the room could represent a major issue for naturally ventilated classrooms where higher concentration gradients are expected. However, such possible gradients could be only investigated through complex thermo-fluid dynamic models [77]; anyway, such models can just provide a solution valid for a certain classroom under investigation and for specific boundary conditions, thus it is not immediately transferable to other scenarios, classrooms, and outdoor conditions.

The uncertainty budget would be even more complex for confined spaces without mechanical ventilation where manual airing procedures, corrected on the basis of the measured $CO_2$ values, are put in place. Indeed, in this case, the uncertainty of the $CO_2$ measurements and of the $CO_2$ mass balance equation (“constant injection rate method” [33,50]) to back-calculate the corrected AERs should be included too. The effect of the $CO_2$ measurement uncertainty is quite straightforward: indeed, in view of correcting the manual airing cycles on the basis of the $CO_2$
In order to reduce the virus transmission potential, ad-hoc procedures were defined in the case of both mechanically- and naturally-ventilated classrooms. In particular,

- for mechanically-ventilated classrooms a very straightforward procedure was defined since, once the scenario (in terms of emitting subject, classroom geometry, etc.), a control unit can calculate the required air exchange rate accordingly and set the corresponding constant fresh flow rate of the mechanical ventilation system. Such a scenario can be established as a selectable mode of operation for the control unit;
- for naturally-ventilated classrooms a suitable feedback control strategy was included and applied in the method. In these classrooms, manual airing cycles help increase the air exchange rate but, due to the dynamic of the emission and of the airing cycles, a required air exchange rate cannot be defined a-priori. Thus, the design parameter is not just the air exchange rate but the $\Re_{\text{event}} < 1$ condition itself which informs scheduling of the manual airing procedures. Such manual airing would be continuously checked and, in case, re-scheduled on the basis of the indoor CO$_2$ concentration monitoring. The monitoring would allow evaluation of the actual ventilation rates during the airing cycles and inform proper adjustments to the airing periods.

While further efforts are needed to quantify and reduce the uncertainties of the models, parameters and measured data in the evaluation of individual risk and virus transmission potential, the suggested method provide critical support for national public health authorities to minimize the contribution of school environments to the spread of the pandemics.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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