Recent results from HERA and their impact for LHC

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Abstract. Recent measurements of inclusive and semi-inclusive deep inelastic scattering in electron-proton collisions at HERA are reviewed. These measurements are used to determine the parton distribution functions (PDFs) of the proton, a necessary input to theory predictions for hadron colliders. An introduction to the PDF determination with an emphasis on HERA PDFs is presented. Theory predictions based on HERAPDF are compared to a selection of recent LHC and Tevatron measurements. The impact of jet and charm production measurements on the PDFs is discussed.

1 Introduction

A deep understanding of the proton structure is one of the most important topics in modern particle physics. A precise knowledge of the Parton Distribution Functions (PDFs) of the proton is essential in order to make predictions for the Standard Model and beyond the Standard Model processes at hadron colliders.

The cross sections of processes in proton-(anti)proton collisions are factorized by a convolution of the matrix element of parton-parton interaction and the proton structure. The latter is described by parton density functions (PDFs). A PDF, \( f_i(x, Q^2) \), represents the probability of finding in the proton a parton \( i \) (quark or gluon) carrying a fraction \( x \) of the proton momentum with \( Q^2 \) being the energy scale of the hard interaction. In case of proton-(anti)proton interactions PDFs of both protons enter multiplicatively into the calculation of the process cross section. Therefore the precision of the PDFs is of particular importance for accurate cross-section predictions. In the last decades, the measurements of lepton-nucleon and proton-antiproton scattering have been used to determine the proton PDFs. At low to medium \( x \) the PDFs are constrained by HERA data. The measurements at fixed target experiments and Tevatron contribute mainly at high \( x \). The recent precise data from Tevatron and the LHC experiments have the potential to improve the precision on the PDFs further.

2 Proton Structure and DIS at HERA

The knowledge of the proton PDFs is obtained to a large extent from the measurements of the structure functions in deep inelastic scattering (DIS) experiments. In Fig. 1 the diagram of DIS is represented. The lepton is scattered off the nucleon via the exchange of a \( \gamma \) or \( Z^0 \)-boson (neutral current, NC, process) or via the exchange of a \( W^\pm \)-boson (charged current, CC). Here the scattering of an electron (or positron) off the proton is discussed.

The NC (and similarly CC) cross section can be expressed in terms of the generalized structure functions:

\[
\frac{d^2 \sigma_{NC}^\pm}{dx dQ^2} = \frac{2 \pi \alpha_s}{x Q^4} \left[ Y_x \tilde{F}_{2}^\pm + Y_{-x} \tilde{F}_{3}^\pm - y^2 \tilde{F}_{L}^\pm \right],
\]

where \( Y_x = 1 \pm (1-y)^2 \) with \( y \) being the transferred fraction of the lepton energy. The (generalized) structure function \( F_2 (\tilde{F}_2) \) is the dominant contribution to the cross section, \( x \tilde{F}_3 \) is important at high \( Q^2 \) and \( \tilde{F}_L \) is sizable only at high \( y \).

In the framework of perturbative QCD the structure functions are directly related to the parton distribution functions, i.e. in leading order (LO) \( F_2 \) is the momentum sum of quark and anti-quark distributions, \( F_2 \approx \sum q \bar{q} (q + \bar{q}) \), and \( x \tilde{F}_3 \) is related to their difference, \( x \tilde{F}_3 \approx \sum 2 \epsilon_q \delta_q (q - \bar{q}) \). At higher orders, terms related to the gluon density distribution \( \langle \alpha_s g \rangle \) appear. In analogy to neutral currents, the inclusive CC \( ep \) cross section can be expressed in terms of function structure and in LO the \( e^+ p \) and \( e^- p \) cross sections are sensitive to different quark densities:

\[
e^+ : \quad \sigma_{CC}^e = x[ \bar{u} + \bar{c} ] + (1 - y)^2 x[ d + s ]
\]

\[
e^- : \quad \sigma_{CC}^e = x[ u + c ] + (1 - y)^2 x[ d + s ].
\]

At HERA at DESY in Hamburg, electrons (or positrons) were collided with protons at centre-of-mass energies \( \sqrt{s} = 225-318 \) GeV. The measurements of the NC and CC cross sections from HERA extend the kinematic regime in \( Q^2 \)

\[\hspace{1cm} \text{Fig. 1. Diagrams of neutral NC and charged CC current deep inelastic scattering processes. The symbols denote the particles, the label ”X” denotes the hadronic final state.}\]
by more than two orders of magnitude with respect to the
fixed target experiments and cover the wide $x$ range from
$10^{-7}$ to 0.7. At the HERA collider experiments, H1 and
ZEUS, the cross sections of NC and CC DIS are measured
with high precision. The measurements of the two experi-
ments are combined and are further used to determine par-
ton distribution functions HERAPDF [2].

3 HERAPDF

The PDFs are determined from the structure function mea-
surements using the corresponding coefficient functions cal-
culated to a certain order in perturbative QCD (pQCD).
The structure functions, and in turn the PDFs, depend on $x$ and $Q$. The $x$-dependence of the parton distributions is not
yet calculable in pQCD and has to be parametrized at a cer-
tain starting scale $Q_0$. The dependence on $Q$ is described
by the DGLAP evolution equations [1]. Starting from a
parameterisation of the PDFs at a starting scale, either by
making ad-hoc assumptions on their analytical form or by
using the neural-net technology, fits to various sets of ex-
perimental data, with HERA DIS data being the backbone,
are performed within the DGLAP evolution scheme.
The resulting PDFs depend on the order in which the pertur-
bative QCD calculation is performed, the assumptions about
the PDF parametrisation, the treatment of heavy quarks,
the choice for the value of $\alpha_s(M_Z)$ and the treatment of
the uncertainties. The data sets included in the PDF fit and the
consistency of these data sets determines the experimental uncertainty of the PDFs.

In Fig. 2 the parton distributions HERAPDF1.5
are shown. In addition to the exper-
imental, model and parametrisation un-
certainties, the variation of model inputs and
parametrisation assumptions. HERAPDF1.5NLO and NNLO sets
are obtained by solving the DGLAP evolution equations
at NLO (or NNLO) in the $M_S$ scheme with the renormal-
isation and factorisation scales chosen to be $Q^2$. The QCD
predictions for the structure functions are obtained by the
convolution of the PDFs with the NLO coefficient func-
tions calculated using the general mass variable flavour
number RT scheme [4]. For the parametrisation of PDFs at
the input scale the generic form $x f(x) = A x^n (1-x)^p (1 +
E x^2)$ is used. The parametrised PDFs are the gluon dis-
bution, the valence quark distributions and the $u$-type and
d-type anti-quark distributions. The normalisation paramet-
ers $A$ are constrained by the quark number and momentum
sum-rules.

The parton distributions HERAPDF [2] are determined
using only combined HERA DIS data, where the correla-
tions of the systematic uncertainties are properly taken
into account. This allows the usage of the conventional $\chi^2$
tolerance of $\Delta \chi^2 = 1$. Since this QCD analysis is solely
based on $e p$ data, the PDFs do not depend on the approach
for nuclear corrections needed for fixed target data. Several
phenomenological schemes of heavy quark treatment can
be used in the HERAPDF approach. Therefore direct tests of
the models are possible. The full statistics of the HERA
inclusive CC and NC data are used for NLO and NNLO
QCD fits resulting in HERAPDF1.5 [3]. As an example,
the combined NC cross sections are shown in Fig. 2 to-
gether with QCD prediction based on HERAPDF1.5NLO.

The QCD analysis HERAPDF1.5 follows the formal-
ism, model and parametrisation assumptions as reported in
the PDF parametrisation in the determination of HERAPDF are per-
formed within the DGLAP evolution equations. Starting from a
parameterisation of the PDFs at a starting scale, either by
making ad-hoc assumptions on their analytical form or by
using the neural-net technology, fits to various sets of ex-
perimental data, with HERA DIS data being the backbone,
are performed within the DGLAP evolution scheme.
The resulting PDFs depend on the order in which the pertur-
bative QCD calculation is performed, the assumptions about
the PDF parametrisation, the treatment of heavy quarks,
the choice for the value of $\alpha_s(M_Z)$ and the treatment of
the uncertainties. The data sets included in the PDF fit and the
consistency of these data sets determines the experimental uncertainty of the PDFs.

In Fig. 3 the parton distributions HERAPDF1.5NNLO
at $Q^2 = 10000$ GeV$^2$ are shown. In addition to the exper-
imental uncertainties, the variation of model inputs and
parametrisation in the determination of HERAPDF are per-
formed and provided as additional eigenvectors. The model
uncertainties are evaluated by varying the input assump-
tions on minimum $Q^2$ of the data used in the fit, the stran-
genesis fraction and the masses of heavy quarks. The paramet-
risation uncertainty is formed by an envelope of the maximal deviations from the central fit varying parametris-
ation assumptions. HERAPDF1.5NNLO and NNLO sets
are the recommended HERA PDFs to be used for the pre-
dictions of processes at the LHC. The corresponding eigenvectors are available [5].

4 Benchmarking HERAPDF

The PDFs are intrinsic properties of the proton and are therefore process-independent. Cross section predictions
for processes in proton-(anti)proton collisions can be obtained using HERAPDF, evolved in $Q^2$ using DGLAP equations.

The measurements of jet production at hadron colliders is an important instrument to probe PDFs at high $x$ and also provide additional constraints on the value of $\alpha_S(M_Z)$. In Fig. 4 the jet production cross sections as measured by D0 experiment [6] is presented. The measurement is confronted with the QCD prediction at NLO [7] based on HERAPDF1.5NLO. The data is very well described by this prediction. In Fig. 5 the jet measurement from ATLAS experiment [9] in a central rapidity bin is shown in comparison with NLO predictions using HERAPDF1.5NLO together with several other PDFs. The QCD prediction using HERAPDF1.5NLO describes the data very well.

Production of electroweak bosons provides important constraints on the light quark distributions. For example, the W lepton charge asymmetry $A_L(W) = \frac{d(\mu^-)}{d(\mu^+)+d(\mu^-)} \approx \frac{[n_u - n_d]}{n_u + n_d}$ is sensitive to the valence $u$ and $d$ quark ratio.

The W-boson muon asymmetry as measured by the CMS experiment [10] is shown in Fig. 6. The measurement is compared to NLO predictions [12] obtained using HERAPDF1.5NLO, MSTW08 [13] and CT10W [14] PDFs. The prediction based on HERAPDF1.5NLO describes the data well.

Top quark pair production at the LHC probes the gluon density at high $x$. In Fig. 7 the cross-section measurement of top pair production is shown as a function of the top-quark pole mass in comparison to approximate NNLO calculations [16,17] based on HERAPDF1.5NNLO. The theory uncertainty accounts for the variation of the QCD scales, PDFs error and the variation of $\alpha_S(M_Z)$ in the PDF. For the PDF uncertainty of HERAPDF1.5NNLO, only the eigenvectors for experimental errors are used. The predictions describe the data very well.

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5 Global benchmarking exercise

Presently, the determination of PDFs is carried out by several groups, namely MSTW [18], CTEQ [19], NNPDF [20], HERAPDF [2], AB(K)M [21] and GJR [22]. The large number of PDF parameters and their treatment in the fitting procedure within the different groups results in differences of the PDFs provided. In order to study these differences, a benchmarking exercise is being carried out by the PDF4LHC working group [23] formed by the members of the PDF fitting groups mentioned above. As an example, the NLO prediction for the Higgs cross section ($M_H = 120$ GeV) at the LHC is shown in Fig. 8 for different PDF sets as a function of $\alpha_S(M_Z)$. For different PDF groups not only the value of $\alpha_S(M_Z)$, but also the running of the strong coupling is different, resulting in different cross section predictions. The HERAPDF is an active participant in the benchmarking exercise. In contrast to other PDF groups, HERAPDF is not restricted to one particular heavy flavour treatment scheme, several schemes are implemented and can be tested. Also, by providing the PDF eigenvectors for model parameter and parametrization variations, HERAPDF allows for tests of specific parameterisation and model assumptions during the QCD analysis of different data sets. In the following, the inclusion of semi-inclusive DIS data in the QCD analysis HERAPDF and the impact of these data on assumptions on $\alpha_S(M_Z)$ and the charm quark mass value in the PDF fit is discussed.

6 Semi-inclusive data in HERAPDFs

Semi-inclusive measurements in DIS like jet and heavy flavour production, provide additional constraints on the PDFs when included into the QCD analysis together with inclusive DIS data. The jet production is directly sensitive to both the gluon distribution in the proton and the strong coupling $\alpha_S$. Therefore, including the jet data in the QCD analysis can help disentangling the effects from the gluon and $\alpha_S$ in the PDF fit. Similarly, charm and beauty production in $ep$ collisions provide direct access to the gluon distribution in the proton, which also depends on the assumption of the charm and beauty mass values used in the PDF fit.

6.1 Including jet data in the PDF fit: HERAPDF1.6

In addition to the combined HERA inclusive DIS data as used in the QCD analysis HERAPDF1.5, H1 and ZEUS measurements of jet production cross sections [24] are included in the PDF fit. The resulting parton distributions HERAPDF1.6 [25] are determined using a fixed value of $\alpha_S(M_Z)$ and also using $\alpha_S(M_Z)$ as a free parameter in the fit. The impact of the inclusion of jet data in the PDF fit on the gluon distribution and the value of $\alpha_S$ is demonstrated in Fig. 9. Here, the PDFs obtained using the inclusive data only (HERAPDF1.5) and the PDFs resulting from including the jet data (HERAPDF1.6) are determined using $\alpha_S(M_Z)$ as a free parameter in the QCD analysis. In case of the simultaneous fit of PDFs and $\alpha_s$ in HERAPDF1.5, the uncertainties on the gluon PDF becomes large at low $x$ but as soon as the jet data are included, the correlation between the gluon PDF and $\alpha_s(M_Z)$ is reduced, resulting in significantly reduced uncertainties on the gluon PDF. In Fig. 10 the quality of the PDF fit in terms of $\chi^2$ is represented as a function of the assumption on the value of $\alpha_S(M_Z)$. In case of HERAPDF1.5, where only inclusive data are used, a very shallow minimum in the $\chi^2$ distribution is observed. The inclusion of the jet measurements in the fit results in the clear minimum, which allows the simultaneous determination of the PDFs and $\alpha_S(M_Z)$.

![Fig. 8. NLO Higgs cross section predictions ($M_H = 120$ GeV) using different PDFs at the LHC with $\sqrt{s} = 7$ TeV.](image)

![Fig. 9. Left panel: The parton distribution functions from HERAPDF1.5. Right panel: the parton distribution functions from HERAPDF1.6 (with HERA jet data included in the fit). In both cases, the QCD analysis is performed treating $\alpha_s(M_Z)$ as a free parameter in the fit. The PDFs are presented for $Q^2$=10 GeV$^2$.](image)

![Fig. 10. Distribution of $\chi^2$ for PDF fit as a function of the assumption on the $\alpha_S(M_Z)$ value. The dashed line corresponds to HERAPDF1.5, where only inclusive DIS data are used. The solid line represents HERAPDF1.6, where the jet data are included.](image)
6.2 Charm quark measurements in the PDF fit.

The factorization scheme, used for the PDF determination depends on the assumption on the number of flavours in the proton, which varies depending on the value of the scale, which has to be compared to the threshold, at which charm and beauty quarks can be treated as partons. This threshold is determined by the mass of charm and beauty quarks. Therefore, the treatment of heavy quarks and the assumptions on their masses have particular importance in the QCD analysis of the proton structure. Different approaches to treat heavy quark (heavy quark schemes) are used by different PDF fitting groups, corresponding to different treatment of mass terms in perturbative calculations, but also implying different assumptions on their masses. The experimental uncertainties are represented by solid lines, the theory uncertainties are shown by dashed lines.

Taking into account the whole spread of cross section predictions using the studied schemes, an uncertainty of 7% on the $W^+$ production cross section arises due to assumption on $m_c^{\text{mod}}$ in the PDF. However, when using the optimal values, $m_c^{\text{mod (opt)}}$, corresponding to minima from Fig. 12 as constrained by HERA charm data, this uncertainty is reduced to 1%.

A value of $\alpha_s(M_Z) = 0.1202 \pm 0.0013^{\text{exp}} \pm 0.0007^{\text{mod/param}} \pm 0.0012^{\text{(hadronisation)}} \pm 0.0015^{\text{scale}}$ is determined [25]. This result is in very good agreement with different results of $\alpha_s$ determination at HERA and with the world average as shown in Fig. 11. It is important to note, that the dominant uncertainty arises from the variation of the renormalization and factorisation scales in the NLO calculation for the jet cross sections. This variation is used to mimic the effect of the missing contribution from higher orders.

Different assumptions on $m_c^{\text{mod}}$ in VFN schemes impact the charm contribution to the sea quark distribution and thus affect the composition of $\bar{u}(x)$ from the $\bar{s}F(x)$ and the $cF(x)$ contributions. These in turn influence the value of the $W^\pm$ and $Z$ cross section predictions at LHC. In Fig. 13 the NLO prediction [12] for the $W^+$ production cross section is shown, using parton distributions evaluated with different assumptions on $m_c^{\text{mod}}$ in various heavy quark schemes.

Fig. 11. The summary of $\alpha_s(M_Z)$ determination results using the jet production at HERA as compared to the world average. The upper point corresponds to the simultaneous determination of $\alpha_s(M_Z)$ and the PDF, as described in the text. The experimental uncertainties are represented by solid lines, the theory uncertainties are shown by dashed lines.

Fig. 12. Comparison of the $\chi^2$ distributions of fits to the inclusive HERA $1 + F_2c$ data using different heavy flavour schemes represented as lines of different styles.

Fig. 13. NLO prediction of $\sigma_{W^+}$ at the LHC for $\sqrt{s} = 7$ TeV as a function of $m_c^{\text{mod}}$ in the input PDF. The lines show predictions for different VFN schemes. The stars show the predictions obtained with the optimal value of $m_c^{\text{mod}}$ used in a given scheme. The dashed horizontal lines indicate the range of $\sigma_{W^+}$, determined for $m_c^{\text{mod}} = m_c^{\text{mod (opt)}}$. 
7 Summary

Precision of the parton distribution functions is essential for accurate predictions of cross sections of the processes at hadron colliders. The proton PDFs are determined using the experimental data of DIS and proton-proton collisions. Combined data of HERA collider experiments provide the most precise constraint on the PDFs at small and medium $x$. HERAPDF is one of the modern QCD analyses in which PDFs are determined. The advantages of these PDFs is no need for nuclear corrections (in contrast to PDFs using the fixed target data), consistent treatment of the systematic uncertainties of the experimental data and implementation of several phenomenological approaches of heavy flavour treatment. Currently, HERAPDF1.5 at NLO and NNLO are among the recommended parton densities for predictions of LHC cross sections. Recent developments in the HERAPDF fits include the QCD analyses of HERA inclusive DIS data together with jet and charm measurements. The inclusion of the jet measurements in the HERAPDF analysis reduces the correlation between the gluon distribution and the strong coupling constant. In such a fit, the PDF is determined together with the $\alpha_s(M_Z)$ value. The resulting $\alpha_s(M_Z)$ value is in a very good agreement with the world average and its precision is limited by the missing NNLO calculation for jet production. The inclusion of the charm data reduces the correlation between the gluon density and the value of the charm mass used in different schemes of heavy flavour treatment in the PDF fit. In particular, a proper choice of the charm quark mass value is important for accurate QCD predictions of W and Z boson rates at the LHC. The QCD predictions based on the HERAPDF1.5 describe the measurements at Tevatron and the LHC very well. With increasing precision of the LHC data, particular processes like $W$-boson, jet or top-pair production will provide additional constraints on the PDFs.

The open source code for QCD analysis of different data sets HERAFitter [33] is released by the H1 and ZEUS collaborations. The program aims for implementation of various schemes of heavy flavour treatment in the PDF fit. In particular, a proper choice of the charm quark mass value is important for accurate QCD predictions of W and Z boson rates at the LHC. The QCD predictions based on the HERAPDF1.5 describe the measurements at Tevatron and the LHC very well. With increasing precision of the LHC data, particular processes like $W$-boson, jet or top-pair production will provide additional constraints on the PDFs.

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