First-Principles Electronic Structure of Solid Picene

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To explore the electronic structure of the first aromatic superconductor, potassium-doped solid picene which has been recently discovered by Mitsuhashi et al. with the transition temperatures \( T_c = 7 - 20 \) K, we have obtained a first-principles electronic structure of solid picene as a first step toward the elucidation of the mechanism of the superconductivity. The undoped crystal is found to have four conduction bands, which are characterized in terms of the maximally localized Wannier orbitals. We have revealed how the band structure reflects the stacked arrangement of molecular orbitals for both undoped and doped (K\(_3\)picene) cases, where the bands are not rigid. The Fermi surface for K\(_3\)picene is a curious composite of a warped two-dimensional surface and a three-dimensional one.

KEYWORDS: picene, superconductivity, aromatic compound, first-principles calculation, electronic structure

Introduction — While there are mounting interests toward superconductivity in more versatile classes in recent years, fascination continues with superconductivity in \( \pi \)-electron (organic) systems. This has a long history, dating back to superconductivity in graphite intercalation compounds (GIC’s), first discovered\(^1\) in 1965 in alkali-metal doped AC\(_8\) (\( A = K, Rb, Cs \)) with transition temperatures \( T_c < 1 \) K, which was recently raised to 11.5 K in CaC\(_6\).\(^2\) The superconductivity in organic metals was first found in TMTSF compounds\(^3\) in 1980 with \( T_c = 0.9 \) K under 12 kbar. Then comes the BEDT-TTF family,\(^4\) for which \( T_c = 14.2 \) K under 82 kbar was found in 2003, the highest \( T_c \) to date among the organic superconductors. Another family is the doped fullerenes, discovered\(^5\) in 1991 for K\(_3\)C\(_{60}\) with \( T_c = 18 \) K at ambient pressure, followed by Cs\(_2\)RbC\(_{60}\) with \( T_c = 33 \) K at ambient pressure\(^6\) and Cs\(_3\)C\(_{60}\) with \( T_c = 40 \) K under 15 kbar,\(^7\) which is the highest \( T_c \) among carbon-based materials. However, a new class of superconducting \( \pi \)-electron materials has not been found over a decade.

So a recent discovery of superconductivity by Mitsuhashi et al.\(^8\) in a solid of aromatic molecule picene, with \( T_c = 7 \) and 20 K when doped with potassium, is a long-awaited breakthrough. The discovery is seminal in that this is the first aromatic superconductor, so a comparison with other classes of \( \pi \)-electron superconductors should be interesting. A picene molecule consists of five benzene rings joined in an armchair manner with a higher chemical stability than pentacene with a straight arrangement. The solid picene has in fact a much larger band gap (\( \approx 3.3 \) eV)\(^9\) than that of solid pentacene (\( \approx 1.8 \) eV), which is why the material originally attracted attention as an organic semiconductor in e.g. organic FET’s.\(^9,10\) Picene has been known to crystallize in orthorhombic and monoclinic forms,\(^11\) and Kubozono’s group discovered superconductivity in potassium-doped monoclinic crystalline picene.\(^8\) The crystal comprises layers stacked in \( c \) direction, where each layer (in \( ab \) plane) has picene molecules arranged in a herring-bone structure. The measured lattice parameters of the crystalline picene are \( a = 8.480, b = 6.154, c = 13.515 \) in Å with \( \beta = 90.46^\circ \),\(^11\) where a primitive cell contains two inequivalent molecules A and B whose positions are related with a space group \( P2_1 \). In\(^8\) K\(_3\)picene with the concentration \( x \) of K atoms per picene is found to become a superconductor for \( x \approx 3 \), and the Meissner effect has been detected with \( H_{\text{c2}} > 10^4 \) Oe suggested.

Theoretically, the first thing we have to do is first-principles electronic structure calculations, which we have done in this Letter, with the density functional theory (DFT) for both pristine and doped solids of picene as a first step to elucidate the mechanism of superconductivity. We have identified the main characters of the conduction bands in terms of the relevant molecular orbitals, and we have also constructed a downfolded four-band tight-binding model with maximally localized Wannier orbitals. From these we shall show how the band structure reflects the stacked arrangement of molecular orbitals for both undoped picene and K\(_3\)picene. The Fermi surface for K\(_3\)picene has turned out to be a curious composite of a warped two-dimensional surface and a three-dimensional one, where both the molecular arrangements modified by doping and hybridization with alkali-metal atoms are relevant.

First-principles bands — We have first optimized the atomic positions including hydrogen atoms with the lattice parameters fixed at the measured values.\(^11\) For the electronic structure calculation for the optimized structure we adopt DFT with the projector augmented-wave (PAW) method\(^12\) with the Quantum MAterials Simulator (QMAS) package\(^13\) in the local-density approximation (LDA). The pseudo Bloch wave functions are expanded by plane waves with an energy cutoff of 40 Ry and \( 4^3 \) \( k \)-points. The angle between the planes of
the inequivalent molecules in the optimized geometry is 61°, close to the measured 58°. Each molecule is not exactly planar due to the intramolecular overcrowding, as seen in the experiment, with the calculated center-of-mass vectors between two inequivalent, nearest-neighbor molecules $r_B - r_A = 0.485a \pm 0.5b$. In the calculated electronic band structure in Fig.1 (a), we first notice that the dispersion along the $c^*$/2 axis is small compared to those along the $a^*b^*$ plane, reflecting the layered structure. The lowest 102 bands are fully occupied, with the valence band top occurring at $c^*/2$. The conduction band bottom is also located there, giving a band gap of 2.36 eV, while the experimental value is 3.3 eV. Such an underestimation is generally seen in LDA calculations. As seen in Fig.1 (a), the band dispersions along $k_b = \pm 1/2$ are doubly degenerate, unlike the triclinic crystalline tetracene and pentacene but like the monoclinic crystalline naphthalene and anthracene. The electron density, displayed in Fig.1 (c), spreads over each molecules basically uniformly, with no significant dimerization seen.

For comparison we have also calculated the electronic structures of an isolated picene molecule with the molecular geometries fixed at those optimized in the crystal to obtain the HOMO and LUMO wave functions, where the LUMO-HOMO energy gap is 2.96 eV (against 1.12 eV calculated for pentacene molecule). If we regard picene and tetracene as fragments of graphene with armchair and zigzag edges, respectively, the higher stability (i.e., larger gap) in picene is consistent with the wisdom obtained in graphene, where armchair is much stabler.

If we go back to the crystal, valence bands are the 99th (VB4) - 102nd (VB1) bands in an energy region of width 0.77 eV separated from the lower ones by 0.26 eV. Looking at the Bloch wave functions for VB1 and VB2 at $\Gamma$, we can identify that they have mainly the character of the HOMO’s of picene molecule. In each layer in the crystal, the HOMO (φ) of each molecule splits into bonding and antibonding ones due to the overlap with its four adjacent inequivalent molecules to form VB1 and VB2 Bloch states, respectively. We can then symbolically express them, at $\Gamma$, as $\psi_{VB1} = \phi_A^{HOMO} - \phi_B^{HOMO}$ and $\psi_{VB2} = \phi_B^{HOMO} + \phi_A^{HOMO}$, as confirmed in Fig. 1 (a).

We also note that $\psi_{VB3}$ and $\psi_{VB4}$ are mainly $\phi_{HOMO-1}^{A,B}$ in character, so that all the four valence bands mainly derive from HOMO and HOMO-1. If we now turn to the conduction bands, they are the 103rd (CB1) - 106th (CB4) bands with a width of 0.39 eV, separated from the upper ones by 0.15 eV (Fig.1 (a)). A similar analysis shows that the Bloch states $\psi_{CB1} - \psi_{CB4}$ mainly derive from $\phi_{LUMO+1}^{A,B}$ as summarized in Fig.2 (a).

Downfolding — To build a tight-binding model for the electronic structure of the pristine picene, we have constructed maximally localized Wannier orbitals (WO’s) for the four conduction bands. The DFT calculations were performed with the Tokyo Ab initio Program Package (TAPP) and the Troullier-Martins norm-conserving pseudopotentials within LDA. The Bloch wave functions were expanded in terms of plane waves with an energy cutoff of 49 Ry. The features of the calculated band structure of the conduction bands (Fig.3 (b)), with the atomic positions optimized above, are identical to those obtained by QMAS within the numerical accuracy. Setting the energy window to cover the four conduction bands, we have obtained four maximally localized WO’s, two of which ($w_{A1}$, $w_{A2}$) are centered at molecule A while the other two ($w_{B1}$, $w_{B2}$) at molecule B. The wave functions $w_{A1}$, $w_{B1}$ (Fig.3 (a)) have the same shape around each molecule for each of $i = l, h$ with (l/h) denoting the lower (higher) energy states. The band structure in Fig.3 (b) in the tight-binding model constructed from the WO’s reproduces accurately the DFT-LDA band dispersion. The transfer integrals, $t_{ij}(d) \equiv \langle w_i(r)|H_{KS}|w_j(r - d) \rangle$, are defined as the matrix elements of the Kohn-Sham Hamiltonian $H_{KS}$ between the WO’s separated by $d = d_1a + d_2b + d_3c$. The transfer integrals with significant magnitudes are depicted in Fig.3 (c). If we examine the shapes of $w_l$ and $w_h$, they can be represented approximately as $\phi_{LUMO} \pm \phi_{LUMO+1}$, with $w_h$ having a slightly larger Wannier spread than that of
As seen in Fig. 2 (a), the LUMO (LUMO+1) are antisymmetric (symmetric) with respect to the plane that bisects the long molecular axis, and $w_1$ and $w_2$ are nearly mirror images of each other, with a slight polarization from the center of the molecule. The matrix element of $H_{KS}$ between the LUMO and LUMO+1 in the crystal is approximately given by $|\langle \phi_{\text{LUMO}} | H_{KS} | \phi_{\text{LUMO+1}} \rangle| \approx (\varepsilon_h - \varepsilon_l)/2 = 11.3\text{ meV}$, where $\varepsilon_i \equiv t_{ii}(0)$. This is not negligible against the gap of 67.8 meV between the LUMO and LUMO+1 calculated for the molecule, which leads to the hybridization of the LUMO- and (LUMO+1)-derived bands. This contrasts with pentacene, for which the calculated gap in the molecule between the LUMO and LUMO+1 is as high as 1.28 eV, and the bands derived from them do not hybridize.

**Doped solid picene —** Let us move on to the doped solid picene. In contrast to the case of BEDT-TTF or TMTSF, carriers are electrons in K$_2$picene. If we assume rigid bands and shift the Fermi energy to a position corresponding to $x = 3$, CB3 and CB4 intersect the Fermi level, and the Fermi surface, displayed in Fig. 1 (b), shows a double surface structure. However, the rigid band assumption has to be tested. The measured lattice parameters$^8$ of the K$_{2.9}$picene are $a = 8.707$, $b = 5.912$, $c = 12.97$ in Å with $\beta = 92.77^\circ$. One conspicuous feature is that the $c$ axis shrinks while the $a$ axis expands upon doping. This contrasts with the crystalline pentacene, where significant expansions of the $c$ axis are known to occur when doped with alkali elements$^{19}$ as a result of the intercalants accommodated in the interlayer region. So this suggests that, in the case of picene, the dopants are not inserted into the interlayer region.

Another issue of interest is “interlayer states” in GIC. There is a body of studies, both experimental$^{20}$ and theoretical,$^{21}$ that indicate the interlayer states of graphite that reside in the space between the carbon layers are relevant in the electronic structure in general and superconductivity in particular in GIC, where the interlayer states of the pristine graphite, located above the Fermi level, strongly hybridize with the valence states of the intercalant atoms and the electronic bands responsible for the hybridized states descend to intersect the Fermi level. In solid picene, we have found that, while there exist interlayer states (where we define a layer as the array of molecules in the $ab$ plane) with amplitudes well away from the layers, they sit in energy 1.5 eV above the conduction band bottom (Fig. 2 (b)). If the dopants are accommodated within the layer of the solid picene as suggested above, the dopant atoms are then expected to have little hybridization with the interlayer states of the solid picene.

To determine whether intralayer insertion of K atoms is energetically more favorable than interlayer insertion, we have prepared initial geometries by locating a K atom on each of $3 \times 3$ grid points on the $ab$ plane of the pristine picene, from which we started optimization. The energies of the intralayer insertions are found to be about 0.2 eV lower in energy per molecule than those of the interlayer insertions. We have therefore performed an optimization for K$_3$picene starting from an initial geometry where six K atoms are put in between the molecules (four above the end benzene rings and two above the center rings) within the layer with the lattice parameters set to those observed for K$_{2.9}$picene. The angle between the molecular planes obtained is now obtuse, $114^\circ$, which is due to the expanded $a$ and shrunk $b$ axes. Analysis of the resultant structure shows that the smaller volume of the unit cell and the presence of the dopants cause a larger distortion of the planar shape of the molecules than in the pristine case. The electronic band structure is shown in Figure 4 (b) (solid lines). They significantly differ from those in the pristine picene, so that the rigid band assumption is invalid. In Fig. 4 (b) we have also displayed (dashed lines) the result for a geometry with the K atoms removed but the other atoms and the doping level fixed. While the two results differ to some extent, which implies that potassium-states are hybridized in the conduction bands, a stronger origin of the non-rigidity against doping comes from the difference in the molecular orientations, which dominates the overlaps of the $\pi$ MO’s.

**References:**

1. T. Ando, J. Phys. Soc. Jpn. Letter 37, 312 (1979).
2. A. Fujishiro and T. Ando, J. Phys. Soc. Jpn. Letter 59, 4531 (1990).
3. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4535 (1990).
4. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4539 (1990).
5. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4543 (1990).
6. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4547 (1990).
7. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4551 (1990).
8. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4555 (1990).
9. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4559 (1990).
10. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4563 (1990).
11. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4567 (1990).
12. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4571 (1990).
13. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4575 (1990).
14. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4579 (1990).
15. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4583 (1990).
16. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4587 (1990).
17. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4591 (1990).
18. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4595 (1990).
19. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4599 (1990).
20. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4603 (1990).
21. T. Ando, J. Phys. Soc. Jpn. Letter 59, 4607 (1990).
to have still the character of the LUMO and LUMO+1, while interlayer states were not found near the Fermi level.

The Fermi surface for the doped system in Fig.4 (c) consists of multiple surfaces, which contain warped, interwoven one-dimensional (planar) surfaces and a three-dimensional (pocket) surface, some of which involve transfers between MO’s via K atoms.

To summarize we have obtained the band structure of solid picene with curious features. The geometry optimized here is not a decisive one, since there can be many metastable geometries, which was also the case with solid pentacene, and further investigations should be needed. Future problems include how the features of the Fermi surface will have implications on mechanisms of superconductivity.

Fig. 4. (a) Optimized K₃ picene geometry with large balls representing K atoms. (b) Band structure (solid curves with E = 0 corresponding to E_F), along with that for the K-removed geometry for comparison (dashed curves with E = 0 put equal to the position of E_F when we shift it to the situation for x = 3). (c) The Fermi surface for the K₃ picene.

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1) N. B. Hannay, T. H. Geballe, B. T. Matthias, K. Andres, P. Schmidt and D. MacNair, Phys. Rev. Lett. 14 (1965) 225.
2) T. E. Weller, M. Ellerby, S. S. Saxena, R. P. Smith and N. T. Skipper, Nature Phys. 1 (2005) 39; N. Emery, C. Hérold, M. d’Astuto, V. Garcia, Ch. Bellin, J. F. Maréché, P. Lagrange and G. Loupia, Phys. Rev. Lett. 95 (2005) 087003.
3) D. Jerome, A. Mazaud, M. Ribault and K. Bechgaard, J. Phys. Lett. (Paris) 41 (1980) L95.
4) H. Taniguchi, M. Miyashita, K. Uchiyama, K. Sato, N. Mori, H. Okamoto, K. Miyagawa, K. Kanoda, M. Hedo and Y. Uwatoko, J. Phys. Soc. Jpn. 72 (2003), 468.
5) A. F. Hebard, M. J. Rosseinsky, R. C. Haddon, D. W. Murphy, S. H. Glarum, T. T. M. Palstra, A. P. Ramirez and A. R. Koratkar, Nature 350 (1991) 600.
6) K. Tanigaki, T. W. Ebbesen, S. Saito, J. Mizuki, J. S. Tsai, Y. Kubo and S. Kuroshima, Nature 352 (1991) 222.
7) T. T. M. Palstra, O. Zhou, Y. Iwasa, P. E. Sulewski, R. M. Fleming and B. R. Zegarski, Solid State Commun. 93 (1995) 327.
8) R. Mitsuhashi, Y. Suzuki, Y. Yamanari, T. Kambe, N. Ikeda, H. Okamoto, A. Fujiwara, M. Yamaji, N. Kawasaki, Y. Maniwa, and Y. Kubozono, private communications.
9) H. Okamoto, N. Kawasaki, Y. Kaji, Y. Kubozono, A. Fujiwara and M. Yamaji, J. Am. Chem. Soc. 130 (2008) 10470.
10) N. Kawasaki, Y. Kubozono, H. Okamoto, A. Fujiwara and M. Yamaji, Appl. Phys. Lett. 94 (2009) 043310.
11) A. De, R. Ghosh, S. Roychowdhury and P. Roychowdhury, Acta Cryst. C 41 (1985) 907.
12) P. E. Blöchl, Phys. Rev. B 50 (1994) 17953; G. Kresse and D. Joubert, ibid. 59 (1999) 1758.
13) http://www.qmas.jp/