Fourier-component engineering to control light diffraction beyond subwavelength limit

Abstract: Resonant physical phenomena in planar photonic lattices, such as bound states in the continuum (BICs) and Fano resonances with 100% diffraction efficiency, have garnered significant scientific interest in recent years owing to their great ability to manipulate electromagnetic waves. In conventional diffraction theory, a subwavelength period is considered a prerequisite to achieving the highly efficient resonant physical phenomena. Indeed, most of the previous studies, that treat anomalous resonance effects, utilize quasiguided Bloch modes at the second stop bands open in the subwavelength region. Higher (beyond the second) stop bands open beyond the subwavelength limit have attracted little attention thus far. In principle, resonant diffraction phenomena are governed by the superposition of scattering processes, owing to higher Fourier harmonic components of periodic modulations in lattice parameters. But only some of Fourier components are dominant at band edges with Bragg conditions. Here, we present new principles of light diffraction, that enable identification of the dominant Fourier components causing multiple diffraction orders at the higher stopbands, and show that unwanted diffraction orders can be suppressed by engineering the dominant Fourier components. Based on the new diffraction principles, novel Fourier-component-engineered (FCE) metasurfaces are introduced and analyzed. It is demonstrated that these FCE metasurfaces with appropriately engineered spatial dielectric functions can exhibit BICs and highly efficient Fano resonances even beyond the subwavelength limit.

Keywords: bound state in the continuum; diffraction; Fano resonance; Fourier component; metasurface

1 Introduction

The analysis of light diffracted by periodic structures has a history of more than 200 years. Since the pioneering studies by Young and Fraunhofer [1, 2], frequency-selective functionalities have been realized by utilizing higher diffraction orders when the period of the grating ($\Lambda$) is larger than the wavelength of incident light ($\lambda$). The directions of the diffracted light can be predicted exactly from the grating equation [3]. However, the discovery of Wood’s anomalies in 1902 [4] prompted the study and development of subwavelength ($\Lambda < \lambda$) resonant photonic lattices, which are typically composed of a waveguide and periodic diffracting elements and are commonly known as resonant gratings, photonic crystal slabs, metamaterials, and metasurfaces. Recently, anomalous leaky-wave effects in resonant photonic lattices, such as bound states in the continuum (BICs) and Fano resonances, have been utilized extensively to manipulate electromagnetic waves [5–21]. Fano resonances arise in one-dimensional (1D) and two-dimensional periodic structures because quasiguided Bloch modes with finite $Q$ factor exchange electromagnetic energy with radiating waves in the radiation continuum [22]. The resonance properties are governed by the eigenfrequencies of the Bloch modes in the lattices [23]. However, under special circumstances where the interactions between the Bloch modes and radiating waves are completely prohibited, BICs with exceptionally high radiative $Q$ values may appear [24]. Different types of photonic lattices supporting BICs and Fano resonances have been presented for fundamental research as well as practical applications [25–32].

Fourier-component-engineered (FCE) metasurfaces are a new type of photonic lattices that were recently introduced to achieving BICs and sharp Fano resonances [33]. In the absence of the first Fourier harmonic components in the lattice parameters, the Bloch modes in the FCE metasurfaces exhibit noticeably increased radiative $Q$ factors as out-of-plane radiations occur because of the first Fourier harmonic components of periodic modulations in the vicinity of the second stopband. However, till date, anomalous resonant leaky-wave effects via
Fourier-component engineering have been realized only in the vicinity of the second stopband. In photonic lattices surrounded by air \((n = 1)\) or conventional low-refractive-index materials \((n \approx 1.45)\), the second stop bands open in the subwavelength region \(\lambda > n\Lambda\), where the Bloch modes are diffracted only in the zero-order direction; this is important for practical applications because the second stop bands admit BICs and diverse zero-order spectral responses with 100% diffraction efficiency. However, higher (beyond the second) stop bands open in the non-subwavelength regions \(\lambda < n\Lambda\), where the Bloch modes are diffracted in multiple directions, have so far attracted little attention for fundamental studies as well as practical applications because the unwanted higher diffraction orders render it difficult to achieve BICs and highly efficient Fano resonances.

Realizing BICs and highly efficient Fano resonances at higher stopbands is important as it can provide new opportunities for manipulating electromagnetic waves in artificial periodic structures. In principle, resonant diffraction phenomena are governed by the superposition of scattering processes, owing to higher Fourier harmonic components of periodic modulations in lattice parameters. However, FCE metasurfaces are enabled because only some of Fourier harmonic components are dominant at band edges with Bragg conditions. In this study, we present new principles of diffraction that enable the identification of the dominant Fourier components causing out-of-plane diffraction orders at the higher stopbands in the nonsubwavelength regions. By utilizing the new principles of diffraction, we introduce and analyze novel FCE metasurfaces that operate in the vicinities of the higher, i.e., third, fourth, and sixth, stopbands. We show that by suppressing the unwanted diffraction orders via engineering the Fourier harmonic components of periodic dielectric functions, the FCE metasurfaces exhibit BICs and highly efficient Fano resonances beyond the subwavelength limit.

2 Resonant gratings and conventional diffraction theory

Figure 1(a) illustrates the simplest representative 1D resonant photonic lattice, i.e., a binary dielectric grating (BDG). It comprises high- \(\epsilon_a\) and low- \(\epsilon_b\) dielectric constant materials and is enclosed by a surrounding medium \((\epsilon_s = 1)\). The thickness of the grating is \(t\), and the width of the high-dielectric-constant section is \(\rho\Lambda\). The grating layer supports transverse electric (TE) guided modes because its average dielectric constant \(\epsilon_{av} = \epsilon_b + \rho(\epsilon_a - \epsilon_b)\) is greater than \(\epsilon_s\). Figure 1(b) schematically illustrates the dispersion curves for the fundamental TE\(_0\) mode. The \(n\)th photonic bandgap opens between the guided bands TE\(_0\), \(n\) and TE\(_0\), \(n+1\). While the guided modes in the green region are nonleaky, those in the white, gray, and yellow regions are described by the complex frequency \(\Omega = \Omega_{Re} + i\Omega_{Im}\) and are prone to out-of-plane radiations by resonant diffractions. The numbers of diffraction orders are one, two, and three in the white, gray, and yellow regions, respectively. In

![Figure 1](image_url)

**Figure 1:** (a) Schematic of a conventional BDG that supports multiple diffraction orders. (b) Dispersion curves for the fundamental TE\(_0\) mode; \(K = 2\pi n / \Lambda\) is the magnitude of the grating vector. (c) Diffraction orders according to the conventional diffraction equation near the fourth stopband (black dotted circle).
this study, we first analyze the resonant out-of-plane radiations in the yellow and gray nonsubwavelength regions and then present the FCE metasurfaces having unusual electromagnetic responses associated with the fundamental TE modes.

When a light beam of frequency $\Omega_{req} = k_0 / K$ is incident on a BDG at an angle $\theta_i$, the waveguide modes in the vicinity of the fourth stopband in the yellow region generate diffracted beams with orders $m = -1, 0, +1$. Typically, the directions of the $m$th-order diffracted light beams can be precisely determined using the conventional diffraction equation:

$$k_0 \sin \theta_{r,m} = k_0 \sin \theta_{t,m} = \Delta k_z + mK,$$  \hspace{1cm} (1)

where $\theta_{r,m}$ and $\theta_{t,m}$ represent the angles of the reflected and transmitted beams, respectively, and $\Delta k_z = k_0 \sin \theta_i$. As illustrated in Figure 1(c), the diffraction orders can be visualized with the equifrequency surfaces of the surrounding media [34]. Because $\theta_{r,m} = \theta_{t,m}$ for a BDG surrounded by a single transparent medium, only the transmitted orders are illustrated. In this conventional scheme, the waveguide mode with $k_z = k_0 \sin \theta_i$ experiences out-of-plane radiation with an additional momentum of $mK$ and a period of $\Lambda$. In principle, the periodic dielectric function can be expanded as a Fourier cosine function series $c(z) = \sum_{n=0}^{\infty} c_n \cos(nKz)$, where the Fourier coefficients are given by $c_0 = c_a + \rho(c_a - c_b)$ and $c_{n=1} = (2\Delta\epsilon / n\pi) \sin(n\pi\rho)$. But only some of these Fourier harmonic components cause out-of-plane radiations at the band edges [35–38]. FCE metasurfaces are enabled by engineering the dominant Fourier harmonic components. To design FCE metasurfaces, therefore, it is essential to identify the important Fourier harmonic components at the band edges. However, conventional Eq. (1) does not describe the roles of the individual higher Fourier harmonic components with period $\Lambda_{n=1} = \Lambda / n$.

### 3 Principles of resonant diffraction and FCE metasurfaces

We first identify the dominant Fourier components that cause out-of-plane radiations at the fourth stopband by introducing the new diffraction equation. For periodic photonic structures, the electric field can be generally expressed in the Bloch form [39, 40]. For the guided modes near the fourth stopband that open at the third-order $\Gamma$ point ($k_z = 2K$ in the extended Brillouin zone), the field distribution can be expressed as

$$E_y(x, z) = A \exp[i(\Delta k_z + 2K)z] \varphi(x) + B \exp[i(\Delta k_z - 2K)z] \varphi(x) + E_{rad},$$  \hspace{1cm} (2)

where $A$ and $B$ are slowly varying envelopes of the two counterpropagating waves, $\varphi(x)$ characterizes the mode profile of the unmodulated waveguide, and $\Delta k_z = k_0 \sin \theta_i$ [41–45]. With the consideration that the two counterpropagating waves, $P(x, z) = A \exp[i(\Delta k_z + 2K)z] \varphi(x)$ and $N(x, z) = B \exp[i(\Delta k_z - 2K)z] \varphi(x)$, produce the diffracting wave $E_{rad}$ by superposition of the scattering processes owing to the higher Fourier harmonics $c_{n=1} \cos(nKz)$, we introduce the new resonant diffraction equation as follows:

$$k_0 \sin \theta_{r,m} = k_0 \sin \theta_{t,m} = \Delta k_z \pm (2K - vnK),$$  \hspace{1cm} (3)

where the $+$ and $-$ signs represent the propagating waves $P(x, z)$ and $N(x, z)$, respectively, $nK$ is the magnitude of the grating vector by the $n$th Fourier harmonic, and $v$ represents the order of the scattering processes. Figure 2 illustrates the resonant diffraction according to Eq. (3).

**Figure 2:** Resonant diffraction by Eq. (3) near the fourth stopband beyond the subwavelength limit.
near the fourth stopband. Comparing Eqs. (3) and (1), it is observed that Eq. (1) with \( m = 0 \) is equivalent to Eq. (3) with \((v, n) = (1, 2) \) and \((2, 1) \) for both the \( P \) and \( N \) waves. For a higher diffraction order with \( m = +1 \), Eq. (1) is equivalent to Eq. (3) with \((v, n) = (1, 1) \) for the \( P \) wave and \((v, n) = (1, 3) \) and \((3, 1) \) for the \( N \) wave. Similarly, Eq. (1) with \( m = -1 \) is equivalent to Eq. (3) with \((v, n) = (1, 1) \) for the \( P \) wave and \((v, n) = (1, 3) \) and \((3, 1) \) for the \( N \) wave. As a result, we can conclude that in the region near the fourth stopband beyond the subwavelength limit, the zero-order resonant diffraction is determined by the first and second Fourier harmonic components, whereas higher diffraction orders with \( m = \pm 1 \) are determined by the first and third Fourier harmonic components. Inspired by this analysis using Eq. (3), we introduce and analyze new FCE meta-surfaces, namely FCE MS1 and FCE MS2 through rigorous finite element method (FEM) simulations. The FCE MS1 does not possess the first and third Fourier harmonic components in the spatial dielectric function and is expected to realize highly efficient zero-order spectral responses beyond the subwavelength limit. By employing FCE MS2, which does not possess the first, second, and third Fourier harmonic components, we expect to obtain high-\( Q \) bound states near the fourth stopband [33].

In Figure 3, we compare the key properties of the conventional BDG with those of the corresponding FCE MS1 and FCE MS2. As shown in Figure 3(a), (e), and (i), while the conventional BDG has simple step-like dielectric functions \( \epsilon_{BDG} = \epsilon_a \) and \( \epsilon_b \) when \(|z| < \rho \Lambda/2 \) and \(|z| \geq \rho \Lambda/2 \), respectively, FCE MS1 and FCE MS2 have complex dielectric functions \( \epsilon_{MS1} = \epsilon_{BDG} - \epsilon_1 \cos(Kz) - \epsilon_3 \cos(3Kz) \) and \( \epsilon_{MS2} = \epsilon_{BDG} - \epsilon_1 \cos(Kz) - \epsilon_2 \cos(2Kz) - \epsilon_3 \cos(3Kz) \), respectively. The simulated dispersion relations depicted in Figure 3(b), (f), and (j) shows that the fourth band gaps open at \( k_z = 0 \) beyond the subwavelength limit \( (\Omega_{Re} > 1) \) for the conventional BDG and FCE meta-surfaces. The dispersion curves for the BDG and FCE meta-surfaces seem to be similar; however, noticeable differences are observed among the BDG, MS1, and MS2 from the spatial electric field \( (E_y) \) distributions in the insets. In the conventional BDG, both the lower and upper band edge modes with asymmetric (A) and symmetric (S) spatial electric field distributions are radiative out of the grating owing to the higher diffraction orders with \( m = \pm 1 \), as shown in Figure 3(b). We note that protection by the symmetry mismatch is valid only for the zero-order diffraction radiating in the vertical direction. In the FCE MS1 (shown in Figure 3(f)), while the symmetric upper band edge mode is radiative out of the meta-surface, the asymmetric lower edge mode becomes the symmetry-protected BIC. This is because there are no higher diffraction orders without the first and third Fourier harmonics. In the FCE MS2 (shown
in Figure 3(j)), the symmetric upper and asymmetric lower band edge modes are strongly localized in the metasurface layer because there is no radiative scattering by the higher Fourier harmonics. The effects of the higher Fourier harmonic components are similarly observed by investigating the radiative Q factors, which are plotted in Figure 3(c), (g), and (k). In the BDG, the Bloch modes in both the lower and upper band branches have low Q values (∼10^3), and no BIC is observed. In the FCE MS1, the BIC in the lower band exhibits a Q factor greater than 10^8 at the Γ point; however, the Q values decrease rapidly as k_z moves away from the Γ point. In the FCE MS2 (shown in Figure 3(k)), the Bloch modes in both the lower and upper band branches become strongly confined BICs with high Q values (∼10^8) in the computational range of |k_z| ≤ 0.07K.

Figure 3(d), (h), and (l) illustrates the transmission spectra through the conventional BDG, FCE MS1, and FCE MS2, respectively, for two different incident angles \( \theta = 0^\circ \) and \( 1^\circ \). The periodic photonic structures exhibit three transmitted diffraction orders: \( m = -1, 0, \) and +1. The transmittance curves for \( m = -1 \) and +1, shown by blue and green lines, respectively, are the same when \( \theta = 0^\circ \); however, they can be distinguished when \( \theta = 1^\circ \). As illustrated in Figure 3(d), no diffraction is observed with 100% efficiency for the BDG. However, as illustrated in Figure 3(h), the zero-order transmittance curves (red lines) through FCE MS1 exhibit the ordinary profiles of Fano resonances [46], in which the transmitted diffraction efficiency rapidly varies from 0 to 100% in the vicinities of the resonant frequencies, irrespective of the incident angle \( \theta \). At normal incidence with \( \theta = 0^\circ \), the zero-order transmittance curve exhibits only the low-Q resonance by the upper band edge mode because the embedded BIC in the lower band edge mode (shown by a blue solid circle in the transmittance curve) does not generate any resonance effect. When \( \theta = 1^\circ \), the simulated transmittance curve for \( m = 0 \) exhibits low- and high-Q resonances by the upper and lower band modes, respectively. Diffraction orders with \( m = -1 \) and +1 exhibit only zero transmittance through the FCE MS1. As illustrated in Figure 3(l), when \( \theta = 0^\circ \), the zero-order transmittance curve through the FCE MS2 exhibits a high-Q resonance, in which the diffraction efficiency varies from 0 to 97%, and the BIC is not associated with resonance. When \( \theta = 1^\circ \), two quasi-BICs are observed in the transmittance curve for \( m = 0 \). In the vicinities of the quasi-BICs by the lower and upper band modes, the zero-order transmission efficiencies vary from 18 to 79% and from 0 to 96%, respectively. In this study, the dielectric components are assumed to be dispersionless and lossless. Even though the real dielectrics are dispersive, we believe that the proposed FCE metasurfaces can be designed to operate within narrow frequency ranges where the dielectric constants are nearly constant. BICs and Fano resonances are caused by the resonant coupling between lateral Bloch modes in the FCE metasurface and outside plane waves. During the resonant coupling process, incident waves inevitably lose their electromagnetic energy due to the intrinsic material loss. Hence, it is reasonable to infer that the FCE metasurfaces with intrinsic material loss can support only quasi-BICs with finite Q factors. The diffraction efficiency of the Fano resonance also decreases. Investigation of the effects of material loss is beyond the scope of the present study and may be the issue of our future work.

We now identify the dominant Fourier components at the sixth stop band open at the fourth-order Γ point (\( k_z = 3K \) in the extended Brillouin zone). With the electric field distribution \( E_y(x, z) = P(x, y) + N(x, y) + E_{rad} \), where \( P(x, y) = A \exp[i(\Delta k_z + 3K)x]p(x) \) and \( N(x, y) = B \exp[i(\Delta k_z - 3K)x]n(x) \), the resonant diffraction equation can be written as follows:

\[
k_0 \sin \theta_{r,m} = k_0 \sin \theta_{t,m} = \Delta k_z \pm (3K - unK).
\]  

Figure 4(a) illustrates the resonant diffraction using Eq. (4). We note that Eq. (1) with \( m = 0 \) is equivalent to Eq. (4) with \( (\nu, n) = (1, 3) \) and (3, 1) for both the P and N waves. For a diffraction order of \( m = +1 \), Eq. (1) is equivalent to Eq. (4) with \( (\nu, n) = (1, 2) \) and (2, 1) for the P wave and \( (\nu, n) = (1, 4), (4, 1), \) and (2, 2) for the N wave. Likewise, Eq. (1) with \( m = -1 \) is equivalent to Eq. (4) with \( (\nu, n) = (1, 4), (4, 1), \) and (2, 2) for the P wave and \( (\nu, n) = (1, 2) \) and (2, 1) for the N wave. To summarize, the zero-order resonant diffraction, shown in Figure 4(a), is determined by the first and third Fourier harmonics, whereas the higher diffraction orders with \( m = \pm 1 \) are determined by the first, second, and fourth Fourier harmonics.

Based on the analysis using Eq. (4), we introduce an additional metasurface, FCE MS3, which has the engineered dielectric function \( \varepsilon_{MS3} = \varepsilon_{BDG} - \varepsilon_2 \cos(Kz) \), as shown in Figure 4(b). Analysis using Eq. (4) indicates that the higher diffraction orders of \( m = \pm 1 \) can be suppressed by eliminating the first, second, and fourth Fourier components from \( \varepsilon_{BDG} \). To avoid complex spatial profiles of the dielectric constant, we set the second and fourth Fourier coefficients, \( \varepsilon_2 \) and \( \varepsilon_4 \), to zeros using the lattice parameter \( p = 0.5 \) instead of eliminating the spatial modulations \( \varepsilon_2 \cos(2Kz) \) and \( \varepsilon_4 \cos(4Kz) \). The simulated dispersion curves and radiative Q factors, shown in Figure 4(c) and (d), respectively, indicate that the fourth bandgap opens at the fourth-order Γ point. The lower band edge mode with an
asymmetric field distribution becomes a BIC, whereas the upper edge mode with a symmetric field distribution radiates out of the metasurface layer. The spatial electric field distribution of the symmetric edge mode, illustrated in the inset of Figure 4(c), indicates that the out-of-plane radiation occurs only in the zero-order vertical direction because the higher diffraction orders are suppressed by the engineered Fourier harmonic components. The simulated transmittance curves for the FCE MS3 shown in Figure 4(e) demonstrate that irrespective of the incident angle \( \theta \), the diffraction orders of \( m = \pm 1 \) exhibit only zero transmittance, whereas the zero-order spectral responses vary from 0 to 1 in the vicinities of the resonance frequencies beyond the subwavelength limit.

Next, we consider the out-of-plane diffraction in the vicinity of the third stopband in the gray region, where two diffraction orders of \( m = 0 \) and \( m = -1 \) coexist. Using the resonant diffraction equation, given by

\[
k_0 \sin \theta_{r,m} = k_0 \sin \theta_{i,m} = \Delta k_z \pm (K - vnK),
\]

and the corresponding phase-matching processes illustrated in Figure 5(a), we conclude the following: in the vicinity of the third stopband, both diffraction orders, \( m = 0 \) and \( m = -1 \), are determined by the first and second Fourier harmonic components. Thus, the diffraction order of \( m = -1 \) cannot be selectively suppressed through the engineering of the Fourier harmonic components. However, high-Q BICs can be achieved by utilizing the engineered dielectric function \( \epsilon_{MG4} = \epsilon_{BDG} - \epsilon_1 \cos(Kz) \) or \( \epsilon_{BDG} - \epsilon_1 \cos(Kz) \) with \( \rho = 0.5 \). As an additional example of the engineering of Fourier harmonic components, we introduce a metasurface, FCE MS4, that exhibits a high-Q BIC at one edge of the third stopband. The dielectric function of FCE MS4 was set to

Figure 4: Resonant diffraction near the sixth stop band beyond the subwavelength limit. (a) Diffraction orders by Eq. (4). (b) Spatial dielectric function with respect to \( z \). Simulated (c) dispersion relations, (d) radiative Q factors, and (e) transmission spectra near the sixth stop band of FCE MS3. In the simulations, the following structural parameters were used: \( \epsilon_\mu = 4.00, \Delta \epsilon = 1.00, \epsilon_s = 1.00, t = 0.15\Lambda, \) and \( \rho = 0.50 \).
$\epsilon_{MG4} = \epsilon_{BDG} - \mu \times \epsilon_1 \cos(Kz)$, where the coefficient $\mu$ is introduced to control the strength of the first Fourier harmonic component. By varying the value of $\mu$, as shown in Figure 5(b), there exist two critical values $\mu_1 = 0.708$ and $\mu_2 = 1.303$, where out-of-plane radiations, owing to the first and second Fourier harmonic components, eliminate each other via destructive interference. When $\mu = \mu_1$ ($\mu = \mu_2$), the BIC with an asymmetric (symmetric) field distribution is observed in the lower (upper) band edge. There are two critical values, $\mu_1 < 1$ and $\mu_2 > 1$, because the contribution of the first Fourier component increases as the value of $\mu$ increases or decreases from 1. We consider that the BIC is observed at one of the band edges because the condition for complete destructive interference strongly depends on the eigenfrequency of the band edge mode. Figure 5(c) shows that the band edge frequencies vary as $\mu$ increases.

In this study, we performed analytical and numerical investigations to control light diffraction in the vicinities of higher stopbands. The proposed FCE metasurfaces may be practically implemented by utilizing the metamaterial concept [47, 48], which can mimic the required dielectric constant profile using a series of discrete step functions [33, 49]. Owing to the complex spatial variations, it is challenging to implement FCE metasurfaces at optical wavelengths. However, current microfabrication technology is sufficient to demonstrate the effects of engineered dielectric functions in the microwave range. To visualize this, as shown in Figure 6(a), we consider an alumina-air metasurface consisting of air slits, $S_j$, in an alumina slab.
The effective dielectric function of the alumina-air metasurface varies in discrete steps, not only the dispersion curves of the alumina-air metasurface in Figure 6(c) are nearly the same as those of the FCE MG2 in Figure 3(j) but also the radiative $Q$ factors in the alumina-air metasurface in Figure 6(d) are comparable to the high $Q$ values in the FCE MG2 in Figure 3(k). The radiative $Q$ factors in the alumina-air metasurface are approximately $10^4$ times larger than those in the conventional BDG in Figure 3(c).

4 Conclusions

In conclusion, we introduced and analyzed novel FCE metasurfaces that operate in the vicinities of higher stopbands open in the nonsubwavelength regime. In principle, resonant diffraction phenomena are governed by the superposition of scattering processes, owing to higher Fourier harmonic components of periodic modulations in the lattice parameters. However, FCE metasurfaces are enabled because only some of Fourier harmonic components are dominant at band edges with Bragg conditions. We revealed that both BICs and highly efficient Fano resonances could be achieved beyond the subwavelength limit by suppressing the unwanted diffraction orders via engineered Fourier harmonic components. To engineer the spatial dielectric functions, we presented new principles of light diffraction that enable the identification of the dominant Fourier harmonic components causing out-of-plane radiations at the higher stopbands. The proposed metasurface concepts can help control the unwanted diffraction orders and extend the BICs and Fano resonances to higher stopbands; thus, they provide new opportunities to manipulate the electromagnetic waves in artificial periodic structures.

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