Electronic structures and edge effects of Ga$_2$S$_2$ nanoribbons

Bao-Ji Wang, Xiao-Hua Li, Li-Wei Zhang, Guo-Dong Wang, and San-Huang Ke

1School of Physics and Chemistry, Henan Polytechnic University, 2001 Shiji Road, Jiaozuo 454000, P. R. China
2School of Electrical Engineering Automation, Henan Polytechnic University, 2001 Shiji Road, Jiaozuo 454000, P. R. China
3MOE Key Laboratory of Microstructured Materials, School of Physics Science and Engineering, Tongji University, 1239 Siping Road, Shanghai 200092, P. R. China
4Beijing Computational Science Research Center, 10 Dongbeiwang West Road, Beijing 100094, P. R. China

Abstract density functional theory calculations are carried out to predict the electronic properties and relative stability of gallium sulfide nanoribbons (Ga$_2$S$_2$-NRs) with either zigzag- or armchair-terminated edges. It is found that the electronic properties of the nanoribbons are very sensitive to the edge structure. The zigzag nanoribbons (Ga$_2$S$_2$-ZNRs) are metallic with spin-polarized edge states regardless of the H-passivation, whereas the bare armchair ones (Ga$_2$S$_2$-ANRs) are semiconducting with indirect band gaps. This band gap exhibits an oscillation behavior as the width increases and finally converges to a constant value. Similar behavior is also found in H-saturated Ga$_2$S$_2$-ANRs, although the band gap converges to a larger value. The relative stabilities of the bare ANRs and ZNRs are investigated by calculating their binding energies. It is found that for a similar width the ANRs are more stable than the ZNRs, and both are more stable than some Ga$_2$S$_2$ nanoclusters with stable configurations.

PACS numbers:

INTRODUCTION

Low-dimensional materials, especially one-dimensional (1-D) nanoribbons, have attracted significant attention from the scientific community during the past two decades due to their interesting electronic properties associated with their low dimensionality and the resulting quantum confinement effect. In the past few years, graphene nanoribbons (GNRs) – thin strips of graphene – have been extensively studied because of their rich and exotic physical properties which depend on their size and edge termination[1,2]. First-principles calculations have revealed that GNRs with hydrogen saturated armchair- or zigzag-shaped edges always have a nonzero direct band gap which decreases as the ribbon width increases. The band gap variation for armchair GNRs (AGNRs) exhibits distinct “family behaviors”[3]. The band gaps of AGNRs arise from both quantum confinement and the crucial effect of the edges, while for zigzag GNRs (ZGNRs), gaps appear because of a staggered sublattice potential on the hexagonal lattice due to edge magnetization[4]. Besides GNRs, some other layer-structured nanoribbons, such as boron nitride nanoribbons (BNNRs) and MoS$_2$ nanoribbons, have also been studied intensively[5]. It is found that the band gap of hydrogen-terminated zigzag BNNRs is indirect and decreases monotonically with the increasing ribbon width. Whereas, direct band gap oscillation is observed for armchair BNNRs[6,7], which tends to converge to a constant value when the ribbon is wider than 3 nm. In contrast, zigzag edged MoS$_2$ nanoribbons show a metallic behavior irrespective of the ribbon width, while armchair edged ones are semiconducting and the band gaps converge to a constant value as the ribbon width increases[8].

As a wide indirect-band-gap semiconductor with uniform layered structure, gallium sulfide (GaS) [9] has been used in photoelectric devices, electrical sensors, and nonlinear optical applications and gained renewed interest[10]. In its bulk form, GaS usually crystallizes into a layered structure, S-Ga-Ga-S (Ga$_2$S$_2$), in which each layer consists of two AA-stacked hexagonal sublayers of Ga atoms sandwiched between two hexagonal sublayers of S atoms. These layers are bound in a three-dimensional (3-D) structure by the nonbonding interaction through the S atoms along the vertical axis[11]. Recently, the micromechanical cleavage technique (as originally used in peeling off graphene from graphite) was successfully used to fabricate single-layer sheets of Ga$_2$S$_2$ [12,13]. A theoretical calculation based on the density functional theory (DFT) has showed that the Ga$_2$S$_2$ sheet is dynamically stable and is an indirect-band-gap semiconductor with an unusual inverted sombrero dispersion of holes near the top of the valence band[14]. As for the electronic properties of Ga$_2$S$_2$ nanoribbons (Ga$_2$S$_2$-NRs) which are important in realistic device applications, very few reports are available in the literature, to the best of our knowledge.

The purpose of this work is to investigate the electronic structures of Ga$_2$S$_2$-NRs by performing first-principles DFT calculations. The effects of different ribbon widths and different edge structures are studied. Also studied are the relative stabilities of these nanoribbons. In the next section, we describe our computational method. Section III presents our calculated results, and the last section is devoted to conclusions.

STRUCTURE AND COMPUTATION

The models of Ga$_2$S$_2$-NRs are constructed by cutting out a stripe of Ga$_2$S$_2$ sheet with the desired edges and widths. Adopting a similar notation used to describe GNRs[1,12,15], we use the number of zigzag lines ($N_z$) or dimer lines ($N_d$) to present the width of a zigzag-edged ribbon (Ga$_2$S$_2$-ZNR) or an armchair-edged ribbon (Ga$_2$S$_2$-ANR) and denote the ribbon by $N_z$-Ga$_2$S$_2$-ZNR (as illustrated in Fig. 1(a)) or $N_d$-Ga$_2$S$_2$-
Calculations of structure optimization and band structure are carried out by using a first-principles pseudopotential plane wave method based on DFT, as implemented in the Vienna *ab initio* simulation package (VASP)\[16\]. The projector augmented wave method (PAW)\[17\] is used to describe the ion-electron interaction. The electron exchange and correlation are treated by the generalized gradient approximation (GGA)\[18\] in the version of Perdew-Burke-Ernzerhof (PBE)\[19\]. A kinetic energy cutoff of 600 eV is adopted for the plane-wave expansion of the wave function. The 3s2p2 electrons of Ga, and 3s2p3 electrons of S are treated as valence electrons. Periodic boundary conditions (PBC) are employed for the infinitely long nanoribbon systems and a vacuum space of 10 Å in each direction perpendicular to the ribbon is used to eliminate the interaction between the periodic images. The atomic structures of the systems, including the lattice parameters and atomic positions, are fully relaxed by the conjugate gradient method until the residual forces acting on each atom are less than 0.001 eV/Å. For the structure optimization a Monkhorst-Pack k-mesh of 1 × 1 × 12 is used for the Brillouin zone (BZ) sampling. The band structures are presented by 45 k-points along the X-axis in the BZ.

**RESULTS AND DISCUSSION**

We first optimize the atomic structure of an periodic 2-D Ga2S2 sheet, in which Ga-S and Ga-Ga atoms are linked covalently in the quadruple layer. The optimized bond lengths of Ga-S and Ga-Ga are 2.37 Å and 2.47 Å, respectively. The Ga-S-Ga (or S-Ga-S) and Ga-Ga-S bond angles are 100.38° and 117.50°, respectively. The thickness of the quadruple layer is 4.76 Å. The computed binding energy is 3.64 eV per atom. The Ga2S2 sheet is found to be a semiconductor with an indirect band gap of 2.38 eV on the DFT/PBE level. These results are in good agreement with recent DFT calculations\[14, 20\].

![Optimized atomic structure of Ga2S2 sheet](image)

We note that Kohn-Sham DFT calculations usually underestimate band gaps of semiconductors because of the lacking of the derivative discontinuity in the energy functionals. A hybrid DFT calculation\[14\] gives a larger value of the indirect band gap, 3.28 eV. Although the Kohn-Sham DFT has the band gap issue, it can usually give reasonable shapes of energy bands and wave functions in the vicinity of the Fermi level, compared to results from quasiparticle GW calculations.

We consider two different directions of termination for Ga2S2-ANRs, zigzag and armchair, and for each direction of termination we consider the bare and H-saturated edge configurations. In order to investigate the width dependence of the electronic properties, we perform calculations for different ribbon widths, up to \(N_z=24\) and \(N_y=19\) (i.e., 24-Ga2S2-ZNR and 19-Ga2S2-ANR). Since qualitatively similar results are observed for the different widths, we first take the 6-Ga2S2-ZNR with width of 17.37 Å and 11-Ga2S2-ANR with width of 18.37 Å as prototypes to present our results (see Fig. 1). After the structure optimization, the bond length between Ga and S atoms varies depending on their position in the ribbon. For the 6-Ga2S2-ZNR, the Ga-S bond lengths are 2.36 Å and 2.37 Å at inner sites, and 2.41 Å and 2.24 Å at the Ga-terminated and S-terminated edges, respectively. The bond angles of Ga-Ga-S and S-Ga-S at the inner sites are 117.43° and 100.24°, respectively. Because of the edge relaxation, the two angles change to 105.60° at the Ga-terminated edge and 108.48° at the S-terminated edge. In the case of the 11-Ga2S2-ANR, the edge S atoms tend to shift outward slightly. The Ga-S bond lengths are 2.36 Å, 2.37 Å and 2.41 Å at the inner sites and 2.21 Å at the two edges. The Ga-Ga bond lengths are 2.48 Å, 2.47 Å and 2.50 Å at the inner sites and 2.48 Å at the two edges. The bond angles of Ga-Ga-S and S-Ga-S are 117.50° and 100.36°, respectively, at the inner...
FIG. 2: Calculated spin-polarized band structures (left: majority spin; right: minority spin) and corresponding local density of states (LDOS) near the Fermi level for bare $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ ((a),(b)) and H-terminated $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ ((c),(d)).

FIG. 3: Spin-dependent total and partial density of states for bare $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ (a) and H-terminated $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ (b).

sites. These results show strong edge-induced atomic relaxation which results in quite different bond lengths and angles at the edges compared to those in 2-D $\text{Ga}_2\text{S}_2$ sheet. This behavior is quite different from the cases of GNRs and BNNRs where the edge distortion is much smaller.

Our calculations for the ZNRs show that their electronic structures are spin polarized. As an example, the band structures of $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ with bare and H-saturated edges are shown in Figs. 2(a),(c) for the two spin components: up-spin (majority) and down-spin (minority), respectively. One can see that the band structures of $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ exhibit a metallic nature: There are one or two bands crossing the Fermi level regardless of the H-passivation, which is similar to the behavior of $\text{MoS}_2$ Nanoribbons\cite{21,22}. We find that this metallic nature holds for all $\text{Ga}_2\text{S}_2$-$\text{ZNRs}$ studied (up to $N_z=24$) regardless of the ribbon width. One should note that the difference between the up-spin and down-spin band structures exists only around the Fermi energy, indicating that the spin polarization originates from the states near the Fermi energy.

To understand the characteristics of these bands near the Fermi energy, we plot their local density of states (LDOS) in Fig. 3(b),(d) for the bare and H-saturated ribbons, respectively. It can be seen that in both cases the LDOS is located around the edges, indicating that the metallic nature of $\text{Ga}_2\text{S}_2$-$\text{ZNRs}$ is mainly due to the spin-polarized edge states. To further show the origin of these metallic bands, we also calculate the total density of states (TDOS) and projected density of states (PDOS) of $6$-$\text{Ga}_2\text{S}_2$-$\text{ZNR}$ (see Fig. 3). The states around the Fermi level in both spin channels are dominated by the $4s$ and $4p$ states of edge Ga atoms and $3p$ states of edge S atoms. Further Mulliken population analyses show that the spin polarization is mainly due to the ferromagnetic state of the Ga-terminated edge regardless of the H-saturation.

In contrast, our calculations for the ANRs show that their electronic structures are spin unpolarized. Both the bare and H-saturated $\text{Ga}_2\text{S}_2$-$\text{ANRs}$ exhibit a semiconducting nature.
FIG. 4: Band structures and corresponding LDOS for CBM and VBM of the 11-Ga$_2$S$_2$-ANR. (a),(b),(c) correspond to the bare Ga$_2$S$_2$-ANR, (d), (e), (f) correspond to the H-terminated Ga$_2$S$_2$-ANRs. Each LDOS figure contains a top view (left) and a side view (right) of the LDOS isosurface of the specified states at CBM or VBM. The Fermi level is set to be zero.

As an example shown in Fig. 4(a), bare 11-ZGa$_2$S$_2$-ANR is a typical semiconductor with an indirect band gap of 1.44 eV. In this case, the valence-band maximum (VBM) occurs along the $\Gamma - K$ direction, and the conduction band minimum (CBM) lies at the $K$ point. We note that the lowest conduction band and highest valence band are very flat, which is similar to the case of BNNRs[23]. When the edge Ga and S atoms are saturated by H atoms, Ga$_2$S$_2$-ANRs are still indirect band gap semiconductors but with a larger band gap (see Fig. 4(f)) and the VBM and CBM are now located at the $\Gamma$ and $K$ point, respectively.

To analyze the characteristics of the VBM and CBM and the influence of the edges, we calculate the LDOS isosurfaces for the energies around the VBM and CBM of the bare and H-saturated 11-Ga$_2$S$_2$-ANR (see Fig. 4(b),(c),(d), and (e)). In the bare system, the large edge relaxation (reconstruction) may weaken the dangling-bond states. However, the states of VBM and CBM are still mainly determined by the dangling-bond-related states which are driven from Ga-4p and S-3p orbitals. Therefore, their LDOS are mainly localized around the edges of the ribbon (see Fig. 4(b),(c)) and form flat bands[21]. Because of this edge-state effect, the converged band gap (1.45 eV) (see the discussion later) of bare Ga$_2$S$_2$-ANRs becomes smaller than that of the 2-D Ga$_2$S$_2$ sheet (2.38 eV).

When the edge Ga and S atoms are saturated by H atoms, the dangling-bond edge states disappear and thus the band gap increases. As can be seen in Fig. 4(d), now the LDOS of the CBM are mainly located near the center of the ribbon. For the VBM, its LDOS are nearly uniformly distributed throughout the ribbon though very weak edge states are remained (see Fig. 4(e)). In contrast with the bare systems, now the converged band gap (2.45 eV) (see the discussion later) of H-saturated Ga$_2$S$_2$-ANRs becomes slightly larger than that of the 2-D Ga$_2$S$_2$ (2.38 eV).

Next let us look at the variation of band gap as a function of ribbon width for both the bare and H-saturated ANRs. As shown in Fig. 5, all the Ga$_2$S$_2$-ANRs are semiconducting and their band gaps are sensitive to the structural symmetry and ribbon width. Generally, owing to the quantum confinement effect the band gap $E_C$ should decrease with increasing ribbon width $N_a$. However, here the variation of...
$E_G$ with $N_a$ shows an oscillatory (or family) behavior, especially for the narrow ribbons ($N_a < 8$). Specifically, anti-symmetric Ga$_2$S$_2$-ANRs ($N_a = 2m$, where $m$ is an integer) have larger band gaps than the neighboring symmetric ones ($N_a = 2m - 1$). This ‘family behavior’ was also observed previously in armchair-edged GNRs$^9$, BNNRs$^2$, and MoS$_2$ nanoribbons$^6$, where a width-dependent oscillation in band gap occurs. When the ribbon becomes wide enough ($> 13 \text{Å}$ or $N_a > 8$), the band gaps tend to converge to a constant value ($\sim 1.45 \text{eV}$), being smaller than the bulk band gap of the 2-D Ga$_2$S$_2$ sheet ($2.38 \text{eV}$). To carefully confirm this tendency, we further do a calculation for 19-Ga$_2$S$_2$-ANRs (width 33 Å), which also shows a band gap of 1.45 eV. In the case of H-terminated ANRs (see Fig. 5), similar behavior is found although their band gaps converge to a larger value of 2.46 eV due to the diminishing edge states. The variation of the band gap with $N_a$ may be an important advantage for their applications in nanotechnology because it may lead to formation of quantum dot or multiple quantum wells through the width modulation$^9$.25.

Finally, we would like to discuss the stability of Ga$_2$S$_2$-NRs, which is quite important because it determines whether this nanostructure can be realized experimentally. The stabilities of different nanoribbons and nanoclusters can be evaluated with their binding energies; those with larger binding energies would be more stable. To estimate the stability, we calculate the binding energy per atom as a function of the ribbon width for bare Ga$_2$S$_2$-NRs in the following way$^9$: 

$$E_b = (nE_{Ga} + mE_S - E_{Ga,S_{nm}})(n + m)$$

where $E_{Ga}$, $E_S$, and $E_{Ga,S_{nm}}$ are the total energies of Ga, S atoms, and Ga$_n$S$_m$, respectively, with $n$ and $m$ being the number of Ga and S atoms, respectively. As is shown in Fig. 6, the binding energy increases monotonically with increasing ribbon width for both zigzag and armchair Ga$_2$S$_2$-NRs. The binding energies of the armchair ribbons are slightly higher than those of the zigzag ribbons with comparable widths, indicating that armchair Ga$_2$S$_2$-NRs are more stable than zigzag ones. It is important to note that although the binding energies of the nanoribbons (except for $N_a = 3$) is smaller than the 2-D Ga$_2$S$_2$ sheet, it is larger than that of Ga$_2$S$_2$ nanoclusters with stable configurations$^{26}$. Therefore, it is reasonable to expect that stable bare Ga$_2$S$_2$-NRs are possible to make experimentally in the future. Since dangling bonds are saturated by H atoms in H-saturated Ga$_2$S$_2$-NRs, their stability should be even better.

**CONCLUSION**

In summary, by performing first-principle DFT calculations we have investigated systematically the electronic properties of Ga$_2$S$_2$ nanoribbons which have not been realized yet but the corresponding 2-D sheet has been successfully fabricated experimentally. We have considered the bare and H-saturated zigzag- and armchair-edged nanoribbons with different ribbon widths (up to 3 nm). It is found that the electronic properties of the nanoribbons strongly depends on their edge structures. The Ga$_2$S$_2$-ZNRs are metallic with spin-polarized edge states while the Ga$_2$S$_2$-ANRs are indirect-band-gap semiconductors without spin polarization. The band gap of bare Ga$_2$S$_2$-ANRs exhibits an oscillation behavior with increasing ribbon width and ultimately converges to a constant value of 1.45 eV when the ribbon becomes wide enough ($> 13 \text{Å}$). The H-saturated Ga$_2$S$_2$-ANRs have the similar behavior but with larger converged band gap of 2.46 eV due to the saturation of the dangling bonds at the edges. Finally, we have studied the relative stabilities of the bare ZNRs and ANRs by calculating their binding energy per atom, and found that the ANRs are more stable than the ZNRs with a similar width. The binding energies are found to be slightly smaller than that of the 2-D sheet, but is larger than that of Ga$_2$S$_2$ nanoclusters with stable configurations, indicating that the bare ribbons can be expected to be realized experimentally in the future.

**ACKNOWLEDGMENTS**

This work was supported by the National Natural Science Foundation of China (No. 11174220 and 11374226), and by the Key Scientific Research Project of the Henan Institutions of Higher Learning (No. 16A140009), and by the Program for Innovative Research Team of Henan Polytechnic University (No. T2015-3), as well as by the Doctoral Foundation of Henan Polytechnic University (No. B2015-46).

* Corresponding author, E-mail: shke@tongji.edu.cn

[1] K. Nakada, M. Fujita, G. Dresselhaus, and M. Dresselhaus, Phys. Rev. B 54, 17954 (1996).
[2] H. Zhao, K. Min, and N. R. Aluru, Plasmonics 9, 3012 (2009).
[3] Y. W. Son, M. L. Cohen, and S. G. Louie, Phys. Rev. Lett. 97, 216803 (2006).
[4] S. Okada and A. Oshiyama, Phys. Rev. Lett. 87, 146803 (2001).
[5] Y. W. Son, M. L. Cohen, and S. G. Loui, nature 444, 347 (2006).
[6] M. S. Xu, T. Liang, M. M. Shi, and H. Z. Chen, Chem. Rev. 113, 3766 (2013).
[7] J. Nakamura, T. Nitta, and A. Natori, Phys. Rev. B 72, 205429 (2005).
[8] A. Du, S. C. Smith, and G. Lu, Chem. Phys. Lett. 447, 181 (2007).
[9] Y. F. Li, Z. Zhou, S. B. Zhang, and Z. F. Chen, J. Am. Chem. Soc. 130, 16739 (2008).
[10] C. H. Ho and S. L. Lin, J. Appl. Phys. 100, 083508 (2006).
[11] G. Z. Shen, D. Chen, P. C. Chen, and C. W. Zhou, ACS Nano 3, 1115 (2009).
[12] D. J. Late, B. Liu, J. Luo, A. Yan, M. H. S. Ramakrishna, M. Grayson, C. N. R. Rao, and V. P. Dravid, Advanced Materials 24, 3549 (2005).
[13] Q. Tang and Z. Zhou, Progress in Materials Science 111, 1244 (2013).
[14] V. Zólyomi, N. D. Drummond, and V. I. Fal’ko, Phys. Rev. B 87, 195403 (2013).
[15] K. Wakabayashi, M. Fujita, H. Ajiki, and M. Sigrist, Phys. Rev. B 59, 8271 (1999).
[16] G. Kresse and J. Hafner, Phys. Rev. B 47, 558 (1993).
[17] P. E. Blöchl, Phys. Rev. B 50, 17953 (1994).
[18] J. P. Perdew, J. A. Chevary, S. H. Vosko, K. A. Jackson, M. R. Pederson, D. J. Singh, and C. Fiolhais, Phys. Rev. B 46, 6671 (1992).
[19] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996).
[20] T. Köhler, T. Frauenheim, Z. Hajnal, and G. Seifert, Phys. Rev. B 69, 193403 (2004).
[21] C. Ataca, H. Şahin, E. Aktürk, and S. Ciraci, J. Phys. Chem. C 115, 3934 (2011).
[22] H. Pan and Y. W. Zhang, J. Mater. Chem. 22, 7280 (2012).
[23] C. H. Park and S. G. Louie, Nano Lett. 8, 2200 (2008).
[24] Y. Q. Cai, G. Zhang, and Y. W. Zhang, J. Am. Chem. Soc. 136, 6269 (2014).
[25] H. Sevincli, M. Topsakal, and S. Ciraci, Phys. Rev. B 78, 245402 (2008).
[26] A. Dwivedi1, A. K. Pandey1, and N. Misral, J. Comput. Methods Mol. Des. 2, 68 (2012).