Flow-to-fracture transition and pattern formation in a discontinuous shear thickening fluid

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Recent theoretical and experimental work suggests a frictionless-frictional transition with increasing inter-particle pressure explains the extreme solid-like response of discontinuous shear thickening suspensions. However, analysis of macroscopic discontinuous shear thickening flow in geometries other than the standard rheometry tools remain scarce. Here we use a Hele-Shaw cell geometry to visualise gas-driven invasion patterns in discontinuous shear thickening cornstarch suspensions. We plot quantitative results from pattern analysis in a volume fraction-pressure phase diagram and explain them in context of rheological measurements. We observe three distinct pattern morphologies: viscous fingering, dendritic fracturing, and system-wide fracturing, which correspond to the same packing fraction ranges as weak shear thickening, discontinuous shear thickening, and shear-jammed regimes.

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Granular suspensions exhibit a wide variety of complex non-Newtonian flow behaviours. Micro-scale grain-grain and grain-fluid interactions can, under different circumstances, manifest as yield stresses, shear thinning, shear thickening, thixotropy, or jamming. Shear thickening fluids display increasing viscosity with applied shear rate or stress. The most dramatic form is discontinuous shear thickening (DST), where the viscosity increases orders of magnitude and the material behaviour goes from liquid-like to solid-like.

In industry, DST behaviour is often undesirable as it can damage equipment during processing of granular suspensions, such as concrete, silica suspensions, cornstarch mixtures, and latex suspensions. Recently, DST has been explored as a useful property to be engineered into composite materials for applications in shock absorption, such as soft body armour, or into smart fluids with tunable rheologies. However, the application of DST in industrial processes is held back by an incomplete understanding of the fundamental mechanisms that govern the shear thickening behaviour.

Cornstarch mixed with water provides a readily available classic example of a granular suspension that exhibits DST behaviour. In fact, it can become so resistant to motion that a person can run across the surface of the “fluid”! Note that this behaviour is reversible: the suspension begins to relax and flow again after the stress is removed. Cornstarch in other interstitial fluids can have no DST response but cornstarch suspensions in water have been routinely used for experiments designed to study the DST phenomenon. Experiments have advanced our understanding through detailed rheological studies and benchmarking of DST models.

One proposed microscopic origin of the DST transition in dense suspensions is that the particles have a repulsive force that can be overcome by an imposed stress to cause frictional contact between particles and thus drastically increase the viscosity of the suspension. Modern theories have followed this line and have reproduced DST behaviour in rheological flow curves and modelled behaviour. As a result, recent experiments have examined the frictional properties of dense particle suspensions. It has been shown that cornstarch suspensions in water are frictionless with a low confining pressure. It has also been shown that cornstarch particles have a frictional profile that transitions from low to high friction with a normal stress that matches the critical stress at which shear thickening occurs. However, theoretical and experimental analysis of macroscopic DST behaviour and flows in confined geometries other than the classic rheometry tools remain scarce.

An alternative flow geometry is represented by the Hele-Shaw cell. Originally designed to study fluid streamlines in laminar flow, the Hele-Shaw cell has since the 1950s been used to study hydrodynamic instabilities, most notably viscous fingering (VF), where the interface between a less viscous fluid invading a more viscous defending fluid develops undulations that grow into finger-like invasion patterns. VF has been studied in different types of complex rheologies, including shear thickening, yield stress, gels, viscoelastic fluids, and saturated granular media.

Similarly to DST suspensions, it has been known since the 1960s that viscoelastic fluids can transition from a liquid-like state to a solid-like state. Here the transition is a result of the timescale of the interaction (shear rate) instead of the abrupt response of stress-induced friction found in DST systems. Two regimes of Hele-Shaw invasion patterns in viscoelastic fluids, typically suspended polymer networks, have been observed: VF at low injection rates and fracture-like patterns above a threshold injection rate where the material starts to behave like an elastic solid.

A rich literature has developed around invasion patterns in Hele-Shaw cell experiments with settled granular media, describing the variety of pattern morphologies observed and the parameters that control the transitions between them. These multiphase Hele-Shaw cell invasion experiments are dominated by the ever-present frictional contacts between grains. The only exception is for high enough injection rate to fluidise and lubricate the granular material, producing liquid-like behaviour and VF-like invasion patterns. Otherwise, as long as the granular medium is packed below the random close packing limit (above which the grains cannot mobilise and capillary invasion is observed), the invaded saturated granular media exhibits frictional behaviour as the invading secondary fluid forms either frictional fingers at low filling fraction or "fracture" patterns through intermittent growth in a dense, deformable granular packing.

Note that the invasion phenomenon referred to as “fracturing” throughout this and similar works (narrow channels formed within a granular material by an invading fluid) is distinct from conventional fracturing of elastic and cohesive materials (separation of a previously continuous solid phase due to tensile stress). Instead, the fracture-like shape of the invasion pattern is a result of pressure and surface tension forces acting on the fracture interface, frictional forces acting between grains, and frictional forces acting between grains and the confining boundaries.

Here we study the displacement by pressurised air of a shear-thickening cornstarch suspension confined in a Hele-Shaw cell. We find three distinct flow patterns: VF, dendritic fracturing (DF), and large-scale fracturing (Fr). The packing fraction ranges at which these three patterns are manifested correspond to the packing fractions at which, respectively, continuous shear thickening (CST), DST, and SJ typically are observed.

**Results**

**Rheology.** Figure 1 presents rheological measurements made with the sample concentrations used in this work. Figure 1a shows the measured flow curves: shear stress $\sigma$ as a function of shear rate $\dot{\gamma}$ for different volume fractions $\phi$. Figure 1b shows the suspension viscosity $\eta = \sigma / \dot{\gamma}$ plotted against $\dot{\gamma}$, illustrating an increasing degree of shear thickening with increasing $\phi$ as well as the shear thinning that is initially observed for all of the suspensions. The flow curves do not reveal a sharp transition from CST to DST to SJ between the different concentrations, and the choice of criteria to identify the regimes based on the flow curves alone is not inherently obvious.

One method to differentiate the varieties of shear thickening is to fit a power law to the thickening regime of the flow curve, $\sigma \propto \dot{\gamma}^{\alpha}$, and use the exponent $\alpha$ as a measure of shear thickening. Following ref. 15, here we define shear thickening regimes based on steady state flow curves obtained from rheology with Newtonian flow $\alpha = 1$, CST $\alpha > 1$, DST $\alpha > 2$, and SJ $\alpha$ tends to infinity. Thus we observe DST for the curves of $\phi \geq 0.45$, where a sharp order-of-magnitude increase in suspension viscosity is observed. DST flow curves up to and including $\phi = 0.50$ are observed to level off at a plateau representing a higher effective viscosity dominated by frictional contacts. The volume fraction of $\phi = 0.53$ had an $\alpha$ that tended to infinity and the flow curve did not recover an upper viscosity branch, instead the rheometer began to regress its shear rate indicating an SJ state.

The highest volume fraction measured, $\phi = 0.56$, always remained as a thick paste and we were unable to fill this material into
the Hele-Shaw cell for experimentation. For reference, the unstressed, frictionless, critical jamming volume fraction of cornstarch is estimated as \( \phi_c \approx 0.56 \). Overall, the measured rheometry is consistent with results in previous work by other authors.17,21,25,33.

**Hele-Shaw flow and pattern formation.** Cornstarch particles, with an average diameter of 16.1 \( \mu \)m, see Fig. 2a, were suspended in water at varying concentrations from \( \phi = 0.23 \pm 0.01 \) to \( 0.53 \pm 0.01 \). The suspension was confined in a transparent radial Hele-Shaw cell with a 0.2-mm gap height and a 10-cm radius, see Fig. 2b. Pressurised air was then released into the suspension from a central inlet in the cell while a high-speed camera filmed from below. The air pressure ranged from \( P = 0.10 \pm 0.02 \) to \( 10.00 \pm 0.02 \) bar. During the experiment, the pressurised air pushes the cornstarch suspension aside as it invades into the cell gap. This suspension displacement forms an observed radial pattern, see Fig. 2c, and the experiment ends once the pressurised air reaches the edge of the cell and is released to atmosphere. We have identified three different pattern morphologies in our experiments: VF, DFr, and Fr as displayed in the screenshots in Fig. 3a-c, respectively. It is useful to represent the volume fraction in terms of how far the system is from the unstressed critical jamming volume fraction \( \Delta \phi = \phi - \phi_c \). Figure 4 shows measured pattern characteristics plotted against \( \Delta \phi \): (a) average branch/finger width \( w \), (b) average spatial frequency of branches/ fingers \( D \), and (c) branch/finger tip velocity \( v_{tip} \).

VF, with smooth curvature at the finger tips, is seen for all concentrations at low pressure (0.1 bar, see Supplementary Movie 1) and at all pressures for dilute suspensions (\( \Delta \phi > 0.11 \), see Fig. 3a). DFr at intermediate \( \Delta \phi \) (\( \Delta \phi = 0.06–0.11 \), see e.g. Fig. 3b and Supplementary Movie 2) is different from VF by having pointed branch tips, offshoots that can be perpendicular to the parent branch, and significantly narrower branch widths averaging \( w = 0.1 \) cm (Fig. 4a). The narrow DFr branches grow by frequent tip-splitting, giving rise to spatially dense fracture networks (high \( D \), see Fig. 4b). The DFr network spreads radially outwards from the injection point.

The DFr mode displays an interesting dynamic whereby the suspension is momentarily forced into a DST solid-like state and moments later relaxes back to a fluid state after the passage of the invasion front (see Supplementary Movie 3). Figure 5a-c shows a time series of close-up images where the suspension of \( \Delta \phi = 0.06 \) (\( \phi = 0.50 \)) is invaded by air of \( P = 0.3 \) bar from the lower left hand corner. The suspension is sheared by the oncoming invasion front into a DST state that subsequently fractures into thin, jagged branches. After the pressurised front has passed, the shear stress on the suspension decreases and the suspension relaxes back to a liquid state. Surface tension then acts to smooth the interface and widen the branches, though it still retains a structure that is unlike VF with offshoots that are perpendicular to the main branch. Figure 5d illustrates the evolution of the fracture width for one branch in a series of 0.5-cm-wide radial bands that shows the fractures continue to widen, at a slower rate after their initial formation, as surface tension acts on the interface after the front has passed. Relaxation behaviour on the scale of seconds in dense cornstarch suspensions has been reported on previously and linked with the time taken for local particles in contact to flow away from each other.22,24

The densest suspension (\( \Delta \phi = 0.03 \), see e.g. Fig. 3c and Supplementary Movie 4) displays a very different fracturing pattern. Here the suspension in the entire cell appears to jam up under the stress as the air invades in long, uninterrupted branches that span the radius of the cell. While also having a narrow branch width (\( w < 0.2 \) cm), the large fracture mode (Fr) is distinguished from the DFr by having a much lower spatial fracture frequency \( D \) (Fig. 4b).

There is no abrupt change in the tip velocity as the pattern transitions from fingerling to fracturing. The general trend (Fig. 4c) is simply increased velocity for higher imposed pressures and for more dilute suspensions (with lower effective viscosity).

Summarising, the branch width \( w \) distinguishes whether the morphology is fingerling (large width) or fracturing (narrow width). The branch spatial frequency \( D \) distinguishes whether the fracturing is dendritic (high branch frequency) or system wide (low branch frequency).

**Discussion**

The behaviour of the quantities we used to characterise the different observed patterns can be displayed as a phase diagram as a function of air pressure \( P \) versus filling fraction difference \( \Delta \phi \). In particular, we show these diagrams in a log–log scale for the
branch width $w$ (Fig. 6a), branch frequency $D$ (Fig. 6b), and tip velocity $v_{\text{tip}}$ (Fig. 6c). Data have been normalised by the maximum value they assume within the analysed interval (as presented in Fig. 4). The system’s behaviour can thus be summarised in a unique phase diagram by combining the measurements for these three quantities into a three-dimensional red–green–blue colour space interpolated between a total of the 40 experiments spanning the $P$–$\Delta \phi$ space (Fig. 6d). Superposing patterns from selected experiments, it is revealed that they are thus grouped by the measured characteristics: large fractures (Fr) for the densest
suspensions in a green hue, DFr for intermediate $\Delta \phi$ and $P > 0.5$ bar in yellow–orange, and VF in blue–pink–purple hues corresponding to dilute suspensions and low imposed air pressure.

Many proposals have been made to explain the intriguing DST phenomenon. However, recent theoretical works$^{33,35,36,40,43}$ simulations$^{41,42,78}$, and experiments$^{20,23,26,45,46,79,80}$ have converged on the explanation that DST in dense suspensions is caused by inter-particle repulsion that subdues frictional contacts$^{35}$. The repulsive force between particles prevents particle contact at low stresses, but at a critical higher stress, $\sigma_c$, inter-particle pressure overcomes the repulsion allowing frictional contacts to be made and thus greatly increasing the viscosity of the system. The increase in viscosity is sudden because the repulsive force prevents a more gradual breakdown of lubrication films$^{59,81}$. Thus the rheology is split between frictionless and frictional regimes. The two regimes have a different volume fraction at which the rheology diverges due to jamming, the frictional regime $\phi$, being less than the frictionless $\phi_c$. This also explains why neither emulsions nor attractive colloids shear thicken. Emulsions are always lubricated and do not experience a frictional state, whereas attractive colloids are always frictional and do not experience a lubricated state.

Given this explanation, models suggest that three responses can be observed, depending on $\phi$, when a suspension transitions from the frictionless regime to the frictional above $\sigma_c$: CST, DST, and SJ. DST occurs in the frictional regime when the suspension can locally elastically sustain an applied stress$^{41}$. This is only possible for a minimum volume fraction $\phi > \phi_{DST}$, where the volume fraction of particles in frictional contact is high enough for solid-like behaviour to dominate the response of the suspension (in rheology, see Fig. 1 for $\phi_{DST} = 0.45$). Below $\phi_{DST}$, CST is observed with liquid-like behaviour. Above $\phi_c$ (in rheology, see Fig. 1 for $\phi_c = 0.53$) but below $\phi_c$, the system shear-jams. It no longer permits homogeneous flow at $\sigma_c$ because it is above the jamming volume fraction for the frictional regime, instead flows will be inhomogeneous. For example, particle migration and fracturing have been observed as inhomogeneous flows during rheology$^{33,34}$. Above $\phi_c$, there is no frictionless state to transition from, the system is jammed no matter the stress, i.e. it is now a system with a yield stress, see $\phi = 0.56$ in Fig. 1$^{81}$.

Mari et al.$^{42}$ suggested that a difference between the DST ($\phi_{DST} < \phi < \phi_c$) and SJ ($\phi_c < \phi < \phi_f$) phases has been observed in stress drop experiments$^{42,84,85}$. For the DST phase, the solid-like frictional state would relax quickly after the stress is relieved as the whole network is not engaged, whereas for the SJ phase the stress does not completely relax from the suspension as some of it is stored elastically in the jammed contact network. We observe this dynamic between our DFr, which readily relaxes (see Fig. 5), and Fr, which holds its form for longer than the experiment.

Rheological steady-state experiments estimate solid-like behaviour to occur at a critical stress of $\sigma_c$, which is of the order of 1 Pa as can be seen for our rheology in Fig. 1. However, the Hele-Shaw cell experiments performed here show a transition at $P_s = 0.5$ bar ($5 \times 10^4$ Pa). How the critical limit found in these Hele-Shaw cell experiments relates to the shear stress response in other systems is yet to be determined.

Fracture-like patterns are also observed in invasion experiments using settled granular materials, typically glass beads, within Hele-Shaw cells. The narrow branch patterns are described as a solid-like fracturing process because the invading fluid has to overcome the frictional mechanical forces that resist granular rearrangement to form them$^{56,68,72,77}$. The fracture growth pushes grains ahead of it and to either side, creating a local compacted front beyond which the packing is unperturbed. In other words, the fracture growth mobilises grains locally, not globally. This locality can be seen in our experiments for the DFr phase where the branches relax once the stress front has passed rather than being maintained at a distance. A transition from wide to narrow VF and then to fracturing has also been observed with increasing $\phi$ in settled granular systems$^{68,74}$. Similarly to fracturing observed in these dense settled granular systems, both the DFr and Fr phases observed here in the dense suspended cornstarch systems have offshoot branches that can be perpendicular to the parent branch, which is not observed in VF in either of the settled or suspended systems.

Comparing fracturing in settled dense granular systems with the suspended dense cornstarch systems here, it appears that a common theme is how particle friction is critical for mixtures to fracture. It is particle friction that provides the necessary resistance in the defending mixture to support the narrow patterns where a mixture that is not dominated by friction would display widening viscous fingers. What is most interesting when comparing the two systems is the response to pressure. The dense settled granular systems have two critical injection pressures: one below which the defending fluid and grains do not move but above which they fracture and another higher critical pressure above which the system flows as viscous fingers to the open boundary$^{66}$. The dense suspended cornstarch system has a somewhat inverted response with one critical injection pressure below which it always flows to the open boundary and above

![Fig. 4 Measured characteristics of Hele-Shaw cell invasion patterns.](Image)

**Measures are shown as a function of the filling fraction difference $\Delta \phi$ (corresponding volume fraction $\phi$ values in brackets) and at different pressures $P$.**

- **a** The average width of branches $w$.
- **b** The average spatial frequency of branches $D$ (the inverse of the average separation distance between branches).
- **c** Branch speed is determined by the fastest branch tip speed in an experiment $v_{tip}$. $w$ distinguishes whether the morphology is fingering (larger width) or fracturing. $D$ is inversely proportional to the separation distance between neighbouring branches and distinguishes whether the fracturing is dendritic (high branch frequency) or system wide (low branch frequency). $v_{tip}$ increases for higher imposed pressures and for more dilute suspensions (lower effective viscosity). Note that there is no step change in the tip velocity at the transition between fingering and fracturing. Error bars are calculated from the standard deviation of measurements from multiple branches.
Theoretical models feature a distinct transition from DST to SJ corresponding to the point at which the initial $\phi$ for the quiescent frictionless suspension is above that of the maximum $\phi_i$ for frictional particles. This theoretical result can be associated with our measured rheology: it occurs for $\phi \gtrsim 0.53$ when the flow curve no longer levels off at a well-defined upper viscosity branch. We suggest that this dynamic is evident in the Hele-Shaw experiments for similar values of $\phi$ where the stress imposed by the invading air causes a large fraction of the suspension contained in the cell to seize up in a solid-like state, resulting in large, system-spanning fractures.

In summary, here we have reported on the first use of a Hele-Shaw cell geometry to visualise invasion patterns in shear thickening and DST cornstarch suspensions in water. Air was released at a controlled pressure into suspensions with varying concentration of cornstarch and the resultant invasion patterns were captured with a high-speed camera. Results from image analysis led to a delineation between three distinct pattern morphologies: VF, DFr marked by dense frequently branching fractures, and Fr marked by sparse minimally branching fractures. These results were plotted in a $P$–$\Delta\phi$ phase diagram and discussed in context of rheological measurements, current DST theory, and similar patterns observed in other dense granular media.

We found that the striking invasion patterns revealed by the flow geometry of the Hele-Shaw cell correspond to the packing fraction ranges of the three different rheological responses of cornstarch suspensions. VF was observed during conditions that did not correspond to DST or SJ (i.e. CST in dilute suspension and $P < P_c$ for all suspensions). DFr was observed during conditions that correspond to DST behaviour but not SJ ($P > P_c$ for dense suspensions of $\phi < \phi_i$). Fr was observed during conditions that correspond to SJ ($P > P_c$ for $\phi > \phi_i$).

In addition, a DST relaxation phenomenon is reported in the DFr regime. The advancing local stress front caused by the invading air moves through the suspension initially as fractures. However, once the front has passed, the local stress is lowered and the fractures “relax” into fingers while the front continues to fracture ahead. This indicates that the DFr regime is categorised by a local DST response, rather than a global one as the SJ regime does.

Future experimental work involving Hele-Shaw cell set-ups can explore how varying the cell gap height can change the shear stress experienced by the suspension relative to the imposed invasion pressure. There is also the ongoing discussion regarding the pressure differences recorded for solid-like behaviour in DST suspensions between the rheology and impact-experiment literature. In addition, recent advancements in modelling dense DST suspensions based on frictionless–frictional theory have allowed complex mechanical responses of cornstarch suspensions to be simulated. The simple geometry and distinct visual results presented here could be useful as a case study to validate simulations.

**Methods**

**Experiment and analysis.** The two controlled variables for experiments were the volume fraction of the cornstarch in suspension, ranging from $\phi = 0.23 \pm 0.01$ to $0.53 \pm 0.01$, and the imposed air pressure, ranging from $P = 0.10 \pm 0.02$ to $10.00 \pm 0.02$ bar. The cornstarch was weighed out and mixed with deionised water to form the desired volume fraction $\phi$ according to the following ratio:

$$\phi = \frac{(1 - \beta) m_{cs}/\rho_w}{(1 - \beta) m_{cs}/\rho_w + m_w/\rho_w} (1 + \lambda),$$

where $m_w$ is the mass of deionised water, $\rho_w$ is the density of deionised water (1.0 $\pm$ 0.03 $\text{kg m}^{-3}$), $m_{cs}$ is the mass and density of deionised water in the cornstarch that has absorbed water in natural room humidity ($\phi = 0.13 \pm 0.28$–$48$). The variance that results from differing humidities between days that experiments were conducted on...
Fig. 6 Phase diagram for measured characteristics of the invasion patterns. Each plot has the same axes and are in a logarithmic scale, with the invasion pressure $P$ against the filling fraction difference $\Delta \phi$. a The experimental data for branch width $w$ normalised within a blue colour space. b The experimental data for the branch frequency $f$ normalised within a red colour space. c The experimental data for the branch speed $v_{\text{br}}$ normalised within a green colour space. d Samples of patterns formed at varying $P$ and $\Delta \phi$. Volume fractions are reported in brackets below the corresponding values of $\Delta \phi$. The sample patterns presented are to scale, the diameter of their image equivalent to Hele-Shaw cell diameter of 20 cm. Background plot of d represents the combined normalised experimental data from a to c in a three-dimensional RGB colour space. Similar pattern morphologies correspond to similar colours. Three phases are noted, fracturing (Fr), dendritic fracturing (DFr), and viscous fingering (VF).

is minimal, a change of approximately ±1% of the sample mass. However, to reduce the impact of this daily variation, before weighing and mixing the cornstarch it was first prepared in a vacuum chamber for 45 min to remove ambient moisture from the sample. This process was found to remove ≈ 20 ± 5% giving $\beta = 0.10 ± 0.01$, which was used for all calculations.

The prepared sample was stored in a sealed container to avoid evaporation before it was used. The experiment was run within minutes of the mixture being poured into the cell to avoid settling, which takes place over several hours even without a density-matched liquid. The particles of cornstarch were measured poured into the cell to avoid settling, which takes place over several hours even before it was used. The experiment was run within minutes of the mixture being

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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Rheology

Rheological tests were performed with a Bohlin Gemini HR Nano Rheometer on cornstarch suspensions prepared in the same fashion as for the Hele-Shaw experiments. A parallel plate geometry with 40 and 20 mm diameter plates with a gap size of 0.4 and 0.8 mm were used for $0.23 \leq \phi \leq 0.41$ and $0.45 \leq \phi \leq 0.56$, respectively. A lower height was used for the dilute suspensions to reduce flow curves will be plotted in the conventional way with shear rate on the x-axis, even though a stress-controlled experiment is used and the shear rate is the independent variable.
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Author contributions
D.O. contributed to the experiment design, performed all experiments, analysed all results, and was the main author of the paper. M.L.M. performed the rheological experiments and assisted in writing the paper. B.S. contributed to the experiment design and assisted in writing the paper.

Competing interests
The authors declare no competing interests.

Additional information
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