How Modeling Can Reconcile Apparently Discrepant Experimental Results: The Case of Pacemaking in Dopaminergic Neurons

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Abstract
Midbrain dopaminergic neurons are endowed with endogenous slow pacemaking properties. In recent years, many different groups have studied the basis for this phenomenon, often with conflicting conclusions. In particular, the role of a slowly-inactivating L-type calcium channel in the depolarizing phase between spikes is controversial, and the analysis of slow oscillatory potential (SOP) recordings during the blockade of sodium channels has led to conflicting conclusions. Based on a minimal model of a dopaminergic neuron, our analysis suggests that the same experimental protocol may lead to drastically different observations in almost identical neurons. For example, complete L-type calcium channel blockade eliminates spontaneous firing or has almost no effect in two neurons differing by less than 1% in their maximal sodium conductance. The same prediction can be reproduced in a state of the art detailed model of a dopaminergic neuron. Some of these predictions are confirmed experimentally using single-cell recordings in brain slices. Our minimal model exhibits SOPs when sodium channels are blocked, these SOPs being uncorrelated with the spiking activity, as has been shown experimentally. We also show that block of a specific conductance (in this case, the SK conductance) can have a different effect on these two oscillatory behaviors (pacemaking and SOPs), despite the fact that they have the same initiating mechanism. These results highlight the fact that computational approaches, besides their well known confirmatory and predictive interests in neurophysiology, may also be useful to resolve apparent discrepancies between experimental results.

Introduction
Midbrain dopaminergic (DA) neurons sustain important physiological functions such as control of movement [1] and signalling of positive error in reward prediction [2]. A dysfunction of the DA system is implicated in the pathophysiology of Parkinson’s disease, schizophrenia, and drug abuse [3]. Under physiological conditions, DA neurons can switch between three distinct modes: tonic (pacemaker), irregular, and burst firing [4,5].

The nature of the channels involved in the low frequency pacemaking of DA neurons is still strongly discussed. Indeed, whereas many studies have shown that L-type calcium channels are critical for this spontaneous activity, others, including ours, have observed little effect of a blockade of these channels on this firing pattern [see Table 1]. Therefore, the respective contribution of calcium and sodium channels in pacemaking remains unclear. On the other hand, it is commonly accepted that low-frequency spontaneous firing requires oscillations in the cytoplasmic free calcium concentration [6,7].

In the presence of the sodium channel blocker tetrodotoxin (TTX), DA neurons also exhibit slow oscillatory potentials (SOPs) [8,9], which have been shown to be sustained by L-type calcium channels [10]. Guzman et al. recently observed that SOPs and spikes are not correlated in rate and regularity, from what they concluded that pacemaking and SOPs are driven by different mechanisms [10]. This conclusion is used to support the hypothesis that L-type calcium channels would not strongly contribute to pacemaking in DA neurons, which is in opposition with many experimental results [6,11] (Table 1). An additional controversy results from the fact that the block of SK channels prolongs depolarizing plateaus under sodium channel inhibition, whereas it only slightly affects the firing rate when the neurons fire action potentials.

In this paper, we use a mathematical analysis to extract the mechanisms underlying the spontaneous activity of DA neurons. For this purpose, we develop a minimal model of a DA neuron, in which we include the minimal set of conductances that are able to reproduce the firing patterns exhibited by these cells [see below]. This minimal model is able to exhibit pacemaker firing in the absence of synaptic afferents, and to switch from a low frequency single-spike firing to bursting when SK channels are blocked in the presence of excitatory inputs, as reported experimentally [12,13]. Moreover, SOPs are present during the inhibition of sodium channels, and the effect of a SK channel blockade observed...
Author Summary

Dopamine is a neurotransmitter which plays important roles in the control of voluntary movement, motivation and reward, attention, and learning. Dysfunction of midbrain dopaminergic systems is involved in various diseases such as Parkinson’s disease, schizophrenia and drug abuse. This underlines the importance of a tight regulation of dopamine levels in the brain. At the cellular level, the release of dopamine is directly correlated to the type of electrical activity (the firing pattern) of nerve cells that produce it, the so-called “dopaminergic neurons”. Therefore, an in-depth understanding of the mechanisms underlying the electrical behavior of dopaminergic neurons is of critical importance to find new strategies for the treatment of diseases that result from dysfunction of this system.

experimentally is reproduced in the model. In order to validate our analyses of the minimal model, we also test its predictions on a published detailed model of these neurons [14,15].

The main conclusion of our analysis is that pacemaker firing in DA neurons is sustained by the cooperation of sodium and L-type calcium channels (and more modestly N-type or P/Q-type calcium channels [6]), whereas variations of the intracellular calcium concentration play a major role in the rate of this spontaneous firing pattern. On the basis of this mechanism, we identify potential causes for the experimental discrepancies mentioned above, using our minimal model, as well as the detailed model. We observe that neurons only differing by less than 1% in their maximal sodium conductance react oppositely to a blockade of L-type calcium channels. Experiments performed in rat brain slices confirm that L-type calcium and sodium channels cooperate to generate pacemaking in these neurons.

As a secondary conclusion, our model shows that, even though the initiation of SOPs and spikes is sustained by the same mechanism, these oscillatory patterns are not correlated, which is in agreement with experimental results [10]. We show that this absence of correlation is due to different mechanisms of depolarizing phase termination in the two oscillatory behaviors, as well as different kinetics of calcium entry (resp. exit) during depolarizing phases (resp. hyperpolarizing phases). These results show that the lack of correlation between pacemaking and SOPs does not exclude a shared mechanism.

Results

A minimal model to capture the pacemaking mechanism of dopaminergic neurons

In order to extract the essential mechanisms of pacemaking of DA neurons, we developed a minimal model endowed with the minimal set of conductances which is necessary to reproduce the firing patterns of these cells. The conductances present in the model are shown in Fig. 1 and the corresponding equations are detailed in the Methods section. In parallel with the membrane capacitance and a leak current, the model is composed of sodium channels and delayed-rectifier potassium channels for the generation of action potentials (fast dynamics). Calcium enters through L-type calcium channels endowed with calcium dependent inactivation (CDI) [16,17], whereas calcium extrusion is carried out by calcium pumps. In addition, small conductance calcium-activated potassium (SK) channels are present. Finally, an excitatory synaptic current is added to test the effect of noise of variable amplitude on the firing of the modeled cell (small

Table 1. Effect of manipulations that block voltage-dependent $Ca^{2+}$ channels on the pacemaking of midbrain DA neurons ex vivo or in vitro.

| Reference | Nature of the preparation | Agent used | Observed effect |
|-----------|---------------------------|------------|-----------------|
| Nedergaard et al., 1993 | Slices from adult guinea-pigs, SNc, intracellular recordings. | nifedipine (1 – 20 $\mu$M) | Cessation of firing at undisclosed concentration. |
| Mercuri et al., 1994 | Slices from adult Wistar rats, SNc and lateral VTA, intracellular recordings. | nifedipine and nimodipine (0.3 – 30 $\mu$M) | Decrease in the firing rate of about 50% with 1 $\mu$M of both drugs. Cessation of firing with 20 – 30 $\mu$M of both drugs. |
| Puopolo et al., 2007 | Acutely dissociated neurons from the SNc of juvenile (16 day-old) mice, whole cell recordings. | 1.8 mM Ca$^{2+}$ in replacement of Ca$^{2+}$ nimodipine (1 $\mu$M) $\alpha$-agonist (200 nM) | Cessation of firing in all neurons (17/17). Firing rate decreased in 9/17 neurons. Firing rate decreased in 10/14 neurons. |
| Chan et al., 2007 | Slices from juvenile mice (younger than P21), SNc, cell-attached and whole-cell recordings. Slices from young adult mice (older than P28), SNc, cell-attached and whole cell recordings. | isradipine (20 $\mu$M) and nimodipine (20 $\mu$M) | “Firing largely unaffected” (but firing reduced by an $I_h$ blocker). Cessation of firing in all neurons (15/15): “plastic” phenomenon in “several” neurons (firing resumes during block > 1 hour in some neurons). |
| Guzman et al., 2009 | Slices from both juvenile and young adult mice, SNc, cell-attached and whole cell recordings | isradipine (5 $\mu$M) | Firing unaffected. |
| Putzier et al., 2009 | Slices from juvenile rats (younger than P21), SNc, whole cell recordings | nimodipine (10 $\mu$M) | Cessation of firing. |
| Khaliq and Bevan, 2010 | Slices from both juvenile and young adult mice, medial VTA, whole cell recordings | 0 Ca$^{2+}$, 3 mM Mg$^{2+}$ | Firing increased three-fold. |
| Seuít et al., unpublished | Slices from adult (> 6-week-old) rats, SNc, extracellular recordings | nifedipine (20 – 50 $\mu$M) nimodipine (5 – 20 $\mu$M) | Firing unaffected (N = 5). Variable effects, no clear trend (N = 5). |

SNc: substantia nigra, pars compacta; VTA: ventral tegmental area. Rodents are classified as juvenile (< P21), young adults (> P28) or adult (> 6 weeks). doi:10.1371/journal.pcbi.1002050.t001
amplitude noise to mimic in vitro-like conditions and high amplitude noise to mimic in vivo-like conditions). In the presence of SK channels, the minimal model does not produce high firing frequencies in response to a step of applied depolarizing current but it does so in response to a high amplitude synaptic input. Calcium dynamics is well-known to be essential to classical models of bursting neurons [18], hence the combination of a calcium-regulated inward current (carried by L-type calcium channels) and a calcium-regulated outward current (carried by calcium pumps). In our model, however, the neuron produces only one action potential per oscillation cycle of \( \frac{1}{2^{Ca^{2+}}_{in}} \), which results in low-frequency single-spike firing rather than bursting in in vitro-like conditions (Drion et. al, unpublished).

The proposed minimal model is able to reproduce the firing patterns exhibited by DA neurons, namely pacemaker firing in vitro, irregular single-spike and burst firing in vivo, or be in a hyperpolarized state (Fig. 2). As it has been shown experimentally, the switch between irregular single-spike firing and bursting can be induced by a blockade of small conductance calcium-activated potassium (SK) channels [12,13]. In the remainder of this paper, we will only discuss the mechanisms of spontaneous firing in vitro (i.e. when the neuron is submitted to small amplitude noise). Also, in order to verify that our simplified model correctly captures the firing mechanisms of DA neurons, we systematically test the predictions of the minimal model against simulations performed with the detailed model (see the equivalent circuit in [14]).

The frequency of the spontaneous activity is limited by calcium influx. Indeed, a rise of the cytoplasmic calcium concentration strongly reduces the excitability of the cell. Therefore, to ensure a calcium entry (resp. exit) during the spike generation (resp. between two successive spikes), one or several types of calcium channels (resp. calcium pumps) must be present. Moreover, in order to generate a spontaneous activity even in the absence of calcium-activated potassium channels (as is observed in DA neurons [19]), the calcium dynamics must be regulated by calcium, e.g. through the presence of calcium-inactivated calcium

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**Figure 1. Equivalent circuit diagram of the model.** The model is composed of one compartment containing the conductances shown, in parallel with a membrane capacitance. doi:10.1371/journal.pcbi.1002050.g001

**Figure 2. Comparison of the behavior of the detailed model (left) and of the minimal model (middle) in in vitro and in vivo-like conditions with experimental data obtained from dopaminergic neurons (right).** In each case, the neuron fires regularly in single spikes in vitro, and an inhibition of calcium-activated potassium channels induces burst firing in vivo. Experimental data are from Seutin (unpublished)(upper panel) and Drion (unpublished)(lower panel). doi:10.1371/journal.pcbi.1002050.g002
channels. Under these two conditions, the cell is able to generate a low-frequency spontaneous activity as well as fast firing when submitted to excitatory synaptic inputs, with a very different firing rate between these two firing patterns (0.5 to 5 Hz and more than 15 Hz, respectively, see Fig. 2).

Experiments on neurons with very similar channel build-ups may lead to contradictory observations

In the absence of synaptic inputs, DA neurons fire spontaneously in a very regular manner [19,20]. The mechanisms underlying this pacemaker activity are still strongly discussed, experimental results being contradictory (Table 1). However, it is commonly accepted that pacemaking of DA neurons requires calcium oscillations and that SK channels are not critical to sustain this firing pattern [19]. Fig. 3 illustrates the mechanisms involved in pacemaker firing in the minimal model. As it has been demonstrated experimentally [10], the spontaneous activity is synchronized with calcium oscillations. Namely, each action potential is generated when the intracellular calcium concentration reaches a constant minimal value (Fig. 3A). This is consistent with experimental results [9,10].

The mechanisms involved in the pacemaker activity of the minimal model can be fully understood using bifurcation analysis. The bifurcation diagram shown in Fig. 3B illustrates how the spike generation is governed by the intracellular calcium concentration, the latter being the bifurcation parameter. The diagram defines three distinct ranges of intracellular calcium concentration: a low range where the only stable steady-state is depolarization block \( [Ca^{2+}]_{in} \leq [Ca^{2+}]_{in,low} \); a high range where the only stable steady-state is hyperpolarization \( [Ca^{2+}]_{in} \geq [Ca^{2+}]_{in,high} \); and an intermediate bistable range where a limit cycle may coexist with the two stable steady-states \( [Ca^{2+}]_{in,low} \leq [Ca^{2+}]_{in} \leq [Ca^{2+}]_{in,high} \). The thresholds separating these zones are mainly dependent on the regulation of calcium channels and calcium pumps by the intracellular calcium concentration. Thus, a rise of the intracellular calcium concentration induces an inactivation of the L-type calcium channels [16,17], which reduces the amount of inward (i.e. depolarizing) current, and an activation of calcium pumps, which increases the amount of outward (i.e. repolarizing) current [21]. As a consequence, the excitability of the cell decreases with the intracellular calcium concentration. A variation of the intracellular calcium concentration that exceeds the high threshold will induce a switch from firing to a hyperpolarized state. Therefore, the high threshold, which is defined as the value of \( [Ca^{2+}]_{in} \) at which the stable limit cycle disappears, defines the maximal possible intracellular calcium concentration which is compatible with firing.

The low threshold in Fig. 3 defines the value of intracellular calcium concentration at which an action potential is spontaneously generated. As a consequence, the current which initiates the depolarization at this point is the critical one for pacemaking. For instance, for the set of parameter values used in Fig. 3, action potentials are generated by an opening of L-type calcium channels, and a complete blockade of these channels prevents firing. But if we use other sets of values for the conductance of sodium and L-type calcium channels, the mechanism of spontaneous initiation of spikes can vary. This suggests a strong cooperation between sodium and L-type calcium channels to drive the pacemaker activity of DA neurons, as suggested by Guzman et. al [10].

The important consequences of this cooperation are illustrated in Fig. 4. The threshold separating a hyperpolarized state (white) from pacemaking (blue) is defined by an almost linear combination of the L-type calcium conductance \( g_{Ca,L} \) and the sodium conductance \( g_{Na} \). Moreover, when the conductance of one channel type is above a threshold value, these channels are sufficient to drive a spontaneous activity during blockade of the others. As a consequence, very similar neurons which would have minimal differences in their sodium or L-type calcium channel density may exhibit very different responses to experimental manipulations that shut off one of the two conductances, as illustrated in the various insets of Fig. 4.

Panels A to D of Fig. 4 show the behavior of the minimal model in control conditions and during blockade of L-type calcium channels or sodium channels for a particular set of conductances. The blockade is modeled by setting the conductance to zero. Only the sodium and L-type calcium conductances slightly differ in the four represented situations. Note that the electrical behavior of each modeled neuron in control conditions is almost similar: the differences in parameter values are very small, and the mechanisms that underly their spontaneous activity are similar. However, these neurons react very differently to the blockade of one conductance. In the case of neuron D \( g_{Na,t} = 240mS/cm^2, g_{Ca,t} = 2.3mS/cm^2 \), L-type calcium current inhibition com-

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**Figure 3. Analysis of the spontaneous activity of the minimal model.** (A) Variations of the membrane potential (top) and the intracellular calcium concentration (bottom) over time. (B) Sketch of the bifurcation diagram of the minimal model, with \( [Ca^{2+}]_{in} \) as the bifurcation parameter. The gray part corresponds to negative values of \( [Ca^{2+}]_{in} \), which is non physiological. \( V_{ss} \) denotes the steady-state curve for each value of the bifurcation parameters. The dotted part of \( V_{ss} \) shows its unstable part. HB denotes a Hopf bifurcation and SN a saddle-node bifurcation. The trajectory of the membrane potential is plotted in red. doi:10.1371/journal.pcbi.1002050.g003
Figure 4. Cooperation between sodium and calcium channels in the generation of spontaneous activity in the minimal model and in the detailed model. The center panels show the type of pacemaker activity according to the value of sodium and L-type calcium conductances.
The white zone represents the couples of conductances which result in a hyperpolarized state of the cell and the dark blue zone accounts for pacemaking. Each insert shows the behavior of the model in control condition and during a blockade of L-type calcium channels or sodium channels for a particular set of conductances. The pacemaker behavior of the model strongly relies on the values of both the sodium and the L-type calcium conductances.

Pacemaking can be driven by different cooperating currents

The fact that L-type calcium channels and sodium channels can cooperatively drive the pacemaker activity of DA neurons can be explained by comparing the I-V curves of the two currents (Supplementary Fig. S3A). Indeed, Putzier et al. recently showed that the only critical parameter of the L-type calcium current for pacemaking is the value of its half-activation potential ($V_1$) which should not be too negative [11]. Moreover, they showed that artificial NMDA receptors that would have a similar half-activation potential would also induce sustained firing. The half-activation potentials of sodium and L-type calcium channels are very similar (Supplementary Fig. S3A), which explains why they can cooperate in the pacemaking generation.

This similarity is observed in the detailed model as well (Supplementary Fig. S3B). If we compare the I-V curves of the other calcium currents, it is clear that, in this model, N-type calcium channels have a $V_1$ similar to the one of sodium and L-type calcium channels, whereas $V_1$ of T-type calcium channels is much more negative. On the basis of these observations, the previous analysis suggests that N-type calcium channels should be able to induce pacemaking if their density is high enough whereas T-type channels, which have a significant more negative $V_1$ should not. We test this hypothesis in Fig. 6 (where we reduce the sodium conductance to reduce the contribution of sodium channels to the pacemaking) using the detailed model. As predicted, a N-type calcium current of sufficient amplitude is able to drive a low-frequency pacemaker activity, whereas a T-type calcium current is not, even with a very high maximal conductance value. Moreover, N-type channels are able to induce SOPs when sodium channels are blocked, as L-type channels do (Fig. 4C and D). These simulations are therefore in agreement with the prediction that whatever the nature of the depolarizing current, the only parameter which is critical is its voltage dependence, and more precisely its half-activation potential [11].

The common mechanism of pacemaking and slow oscillatory potentials does not imply that these oscillatory activities are correlated or are affected in the same way by the same experimental manipulation

Our minimal model also sheds light on the mechanisms of, and related controversies on, slow oscillatory potentials (SOPs). Indeed, it has experimentally been shown that SNc DA neurons exhibit SOPs...
during application of TTX \textit{in vitro} \cite{8,9}, and that these SOPs are driven by L-type calcium channels \cite{10}. Recently, it has been shown that pacemaking and SOPs are uncorrelated \cite{10}, which led to the conclusion that these two oscillatory behaviors are driven by different mechanisms, thus rejecting L-type calcium channels for pacemaking.

In addition, it has been reported that block of the SK current on TTX-treated DA neurons strongly affects the shape of SOPs. Namely, this manipulation significantly increases the duration of the depolarizing and hyperpolarizing phases \cite{9}. This observation led to the hypothesis that, in control condition, this inhibition might induce burst firing in DA neurons. However, experiments have invalidated this intuitive suggestion, SK channel blockade only inducing irregularities in the firing of these cells, but not bursting \cite{9}. These contradictory observations can be explained through an analysis of the behavior of the minimal model in configurations that mimic these experiments.

For a sufficiently high value of $\frac{C_{22}}{g_{Ca}}$, SOPs are also observed after blockade of the sodium current in the minimal model (Fig. 7C). As in the case of pacemaking, these SOPs are synchronized with the calcium oscillations (supplementary Fig. S4). Fig. 7 shows how sodium channel blockade affects the bifurcation diagram in the presence and in the absence of SK channels. As illustrated in the figure, sodium channel blockade has no effect on the low threshold, which implies that a same mechanism initiates both spikes and SOPs in the minimal model.

In contrast, sodium channel blockade has a critical impact on the high threshold. Indeed, the Hopf bifurcation which defines the high threshold in pacemaking vanishes when sodium channels are blocked. As a consequence, the high threshold of SOPs is defined at the right saddle-node bifurcation, which is masked by the Hopf bifurcation in control conditions. This implies that, whereas the depolarization mechanism is identical in spikes and SOPs, the repolarization mechanisms are different.

This difference has significant consequences on the model behavior, all consistent with experimental data:

\begin{itemize}
  \item[(i)] SK channel blockade has little effect on the left saddle-node bifurcation but a dramatic effect on the right one (compare
\end{itemize}
This effect is masked in normal conditions because of the Hopf bifurcation. As a consequence, inhibition of the SK current barely affects the pacemaker firing in normal conditions (Fig. 7A,B) but strongly affects SOP frequency when sodium channels are blocked (Fig. 7C,D). These predictions are in agreement with experimental data [9,19].

(ii) There is no reason to expect a strong correlation between spikes and SOPs.

Fig. 8A shows that the interevent interval histograms of pacemaking (in light blue) and SOPs (in dark blue) do not match either in the presence (Fig. 8A, left) or in the absence (Fig. 8A, right) of SK channels. Moreover, depending on the parameters of the model, spike rate can be lower or higher than SOP oscillation rate (Fig. 8B), as observed experimentally [10]. In Fig. 8, the parameters that are varied are the conductances of L-type calcium channels and SK channels. The main origin of this lack of correlation is that the quantity and kinetics of calcium entry taking place during an action potential strongly differ from the one taking place during the depolarized phase of SOPs. This affects the rate of their respective oscillations (Supplementary Fig. S5).

In addition, Guzman et. al recently showed that spikes are much more regular than SOPs in DA neurons [10]. In its low-noise configuration (representing the *in vitro* condition), our model exhibits similar results (Fig. 8C, which can be compared to Fig. 3c of [10]). Indeed, we found that SOPs are much more sensitive to noise than spikes in the presence of SK channels, mainly because SOP oscillations induce less calcium entry than spikes and because the kinetics of calcium entry is slower (supplementary Fig. S5).

These results show that a lack of correlation between spikes and SOPs does not necessarily imply that the generating mechanism of these two oscillatory behaviors is different. Therefore, this experimental observation may not be used to dismiss a role of L-type calcium channels in the generation of spikes in DA neurons.

**Discussion**

The generation of spikes during low-frequency pacemaker firing mainly relies on the cooperation between sodium and L-type calcium channels, whereas its rhythm follows the variations in $[Ca^{2+}]_{cyt}$.

In spite of many experimental studies, the precise mechanisms underlying the spontaneous initiation of spikes in DA neurons are still largely debated in the literature. Using our minimal model as well as a detailed model of a DA neuron, we extracted two critical parameters for the low frequency spontaneous firing.

Firstly, low-frequency single-spike firing and high-frequency intra-bursts firing have to be sustained by two dynamics operating on different time scales. Fast firing is limited by the refractory period of action potentials, which is fixed by the kinetics of voltage-gated channels. On the other hand, the dynamics that are the most likely to limit the rate of low-frequency firing are the variations of the intracellular calcium concentration. Indeed, an accumulation of calcium in the cytoplasm strongly reduces the excitability of the cells, through the inactivation of depolarizing currents (i.e. L-type calcium currents) and the activation of hyperpolarizing currents (i.e. calcium pumps and SK channels). This is in agreement with experimental data, which show that replacement of calcium with either cobalt [6] or magnesium [7] strongly affects pacemaking.
Secondly, the spontaneous initiation of action potentials in DA neurons is the result of the cooperation between various depolarizing currents. In agreement with the experimental results of Putzier et al. [11], we found in the detailed model that any depolarizing current having a half-activation potential less negative than \(-50mV\) (voltage-dependant sodium channels, L-

**Figure 7. Analysis of the effect of SK channel blockade on the spontaneous activity of the minimal model.** (A and B) Variations of the membrane potential over time (top) and sketch of the bifurcation diagram of the minimal model (bottom, with \([Ca^{2+}]_{in}\) as the bifurcation parameter) in the presence and in the absence of SK channels. The grey part corresponds to negative values of \([Ca^{2+}]_{in}\), which are non physiological. \(V_{ss}\) denotes the steady-state curve for each value of the bifurcation parameters. The dotted part of \(V_{ss}\) shows its unstable part. HB denotes a Hopf bifurcation and SN denotes a saddle-node bifurcation. Trajectories of the membrane potential are plotted in red. (C and D) Same as (A and B) but when sodium channels are blocked. The frequency of SOPs is almost halved, whereas the frequency of spikes is barely affected. This simulations were performed in the absence of noise, which would induce irregularities in the absence of SK channels.

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type and N-type calcium channels) may play a role in this initiation. Their relative contribution, as well as the robustness of pacemaking, depend on the respective density of each channel type. Therefore, the fact that the selective blockade of a particular channel does not completely disrupt pacemaking does not mean that these channels are not involved in physiological pacemaking. This might be an important note of caution for experimentalists. Moreover, we confirmed experimentally that L-type calcium and sodium channels do indeed cooperate to generate pacemaking with a degree of cooperation that is highly variable. This precise observation has never been made previously.

Experimental protocols are not robust to physiologically plausible variability

The most contradictory experimental results obtained on DA neurons are probably those concerning the role of L-type calcium channels in the spontaneous initiation of spikes in vitro (Table 1). Using very similar modeled neurons that differ by less than 1% in one conductance parameter (all remaining parameters being identical), we were able to reproduce these contradictory results both in our minimal model and in a detailed model of DA neurons.

Such subtle differences in conductance parameters are quite likely to occur in various experimental conditions. For example, it has recently been shown that there are quantitative differences between DA neurons from the SNc and the VTA in terms of density of these conductances [6,7]. It was proposed that sodium channels play a major role in the spike generation of VTA DA cells, whereas calcium channels are predominant in SNc DA neurons. Among other findings, replacement of calcium with cobalt in SNc neurons completely inhibits the firing, whereas replacement of calcium with magnesium in VTA neurons increases the firing rate [6,7]. Both these effects are also observed in the minimal and detailed models with slightly different maximal sodium conductances (supplementary Fig. S6).

A second source of contradictory experimental results might be the difference between the preparations that are used in different

Figure 8. Comparison of the pacemaking ("spikes") and slow oscillatory potentials ("SOPs") in the minimal model. Note that the simulations have been performed using in vitro-like conditions (low amplitude noise). (A) Interspike interval histograms (ISIH's) of a set of modeled cells in the presence (left) and in the absence (right) of SK channels. The light blue bars account for spikes in control conditions and the dark blue bars for SOP oscillations during sodium channel blockade. (B) Comparison of the rate of spikes and SOPs for different values of \( g_{Ca,L} \) and \( g_{Ca,K} \). (C) Plot of successive spike intervals (light blue) or successive SOP intervals (dark blue) of a set of modeled cells. Although they are driven by the same mechanisms, spikes and SOPs are not correlated. Moreover, SOPs are more sensitive to the noise.

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The lack of correlation between spikes and SOPs is compatible with a same generating mechanism

SOPs exhibited by DA neurons during blockade of sodium channels have been largely studied [8–10] and compared to the spontaneous spiking activity. Moreover, it has been recently shown that the two oscillatory patterns are not correlated [10], a phenomenon that is also observed in our model. It is tempting to conclude from this observation that their underlying mechanisms are different. However, our analysis shows that the generation mechanisms are actually the same. Moreover, Fig. 7 clearly illustrates that the different effect of SK channel blockade on pacemaking and SOPs simply arises from the fact that the high intracellular calcium concentration threshold only slightly changes when sodium channels are present, whereas a more than two fold change in this high threshold occurs when sodium channels are blocked.

Added value of a minimal model in the analysis of DA neuron electrophysiology

DA neuron electrophysiology has been modeled by several groups [14,24–29]. Most of these models were elaborated in order to reproduce experimental observations. Although they clearly succeed at making detailed predictions, their complexity may prevent a detailed analysis of the mechanisms underlying pacemaking in these neurons. On the basis of these models, we attempted to develop a minimal model containing only the most critical conductances needed to reproduce firing patterns of DA neurons. This model allowed us to explain some discrepancies found in the literature on the mechanisms underlying pacemaking of these cells. Importantly, we were able to confirm our conclusions on one detailed model [14].

There are some conceptual differences between our minimal model and some earlier models. For example, the calcium current included in the Wilson and Callaway model [26] does not include any calcium-induced inactivation, whereas ours does. We included inactivation because recent experiments have demonstrated that the L-type channels expressed by DA neurons belong to the Cav1.3 class [30] and this channel subtype is known to undergo calcium-induced inactivation in expression systems [17]. Clearly, this point has to be carefully investigated in future experiments on DA neurons. It should be pointed out, however, that inactivation of L-type channels is not fundamental for the results that we obtained in our model. Indeed, the major role of this phenomenon is to decrease the excitability of the cell when intracellular calcium rises after the action potential. This decrease could be induced by other mechanisms, such as activation of a potassium ERG-type current [29].

One limitation of our minimal model is that it is essentially qualitative and does not take into account the very specifics of DA neurons. However, because of its generality, our model could be a starting point to analyze similar firing patterns of a number of other cell types. Finally, our analysis demonstrates the value of a simplified model to reconcile apparently contradictory experimental observations.

Materials and Methods

Ethics statement

All procedures were carried out in accordance with guidelines of the European Communities Council Directive of 24 November 1986 (86 609 EEC) and were accepted by the Ethics Committee for Animal Use of the University of Liège (protocol 86).

Modeling

The model follows the common equation

$$\frac{dV_m}{dt} = -I_{ion}(+I_{app})$$

where $C_m$ is the membrane capacitance, $V_m$ the membrane potential of the cell, $I_{ion}$ accounts for all the ionic currents and $I_{app}$ is any externally applied current. The fast dynamics include a sodium current $I_{Na}$ and a delayed-rectifier potassium current $I_{K,DR}$. These currents are responsible for the creation of action potentials. The slow dynamics describe the fluctuations of $[Ca^{2+}]_m$; Calcium influx is mediated by a L-T-type calcium current $I_{Ca,L}$, which is both voltage-gated and calcium-regulated, and the calcium is pumped out of the cell by calcium pumps, which generate an outward calcium current $I_{Ca,pump}$. In order to reproduce in vivo conditions, the model can be subjected to excitatory synaptic inputs, which activate a synaptic current $I_{syn}$. The background of this synaptic activity ($R_{syn}$) was modeled through stochastic waveforms. A calcium-activated potassium current $I_{K, Ca}$ and a leak current $I_l$ are also implemented in the model.

Equations and parameters. The equation giving the membrane potential variations over time is as follows:

$$\frac{dV_m}{dt} = -I_{Na} - I_{K,DR} - I_l - I_{Ca,L} - I_{Ca,pump} - I_{syn}(-I_{K, Ca})$$

All the ionic currents equations follow a Hodgkin-Huxley scheme [31]. Each voltage-dependent channel expresses activation gates, whereas inactivation gates are only present in the equation for the sodium current. Control of L-type calcium channels by $[Ca^{2+}]_m$ is incorporated through factor $g_L$. The currents are thus implemented as follows:

$$I_{Na} = g_{Na}m^3h(V_m - V_Na)$$

$$I_{K,DR} = g_{K,DR}V^4(V_m - V_K)$$

$$I_l = g_l(V_m - V_l)$$

$$I_{Ca,L} = g_{Ca,L}d_{Ca,L}(V_m - V_Ca)$$

$$I_{Ca,pump} = I_{Ca,pump, max} \left(1 + \frac{K_{M,P}}{[Ca^{2+}]_m} \right)^{-1}$$

$$I_{syn} = R_{syn}g_{syn}(V_m - 0)$$
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\[ I_{K,Ca} = g_{K,Ca} \left( \frac{[Ca^{2+}]_{in}}{K_D + [Ca^{2+}]_{in}} \right)^2 (V_m - V_K) \]

with

\[ \frac{dm}{dt} = \alpha_m(1 - m) - \beta_m m \]

\[ \frac{dh}{dt} = \alpha_h(1 - h) - \beta_h h \]

\[ \frac{dn}{dt} = \alpha_n(1 - n) - \beta_n n \]

\[ \tau_{d_L} \frac{dd_L}{dt} = d_{L,in} - d_L \]

\[ \frac{d[Ca^{2+}]_{in}}{dt} = -k_1(I_{Ca,L} + I_{Ca,pump}) - k_2[Ca^{2+}]_{in} - k_2 I_{Na} \]

where

\[ \alpha_m = \frac{-0.025(V_m + 40)}{\exp(-(V_m + 40)/10) - 1} \]

\[ \beta_m = 1 \exp(-(V_m + 65)/18) \]

\[ \alpha_h = 0.0175 \exp(-(V_m + 65)/20) \]

\[ \beta_h = \frac{0.25}{1 + \exp(-(V_m + 35)/10)} \]

\[ \alpha_n = \frac{0.25}{100[1 - \exp(-(V_m + 55)/10)]} \]

\[ \beta_n = 0.03125 \exp(-(V_m + 65)/80) \]

\[ d_{L,in} = \frac{1}{1 + \exp(-(V_m + 55)/3)} \]

\[ \tau_{d_L} = 72 \exp(-(V_m + 45)^2/400) + 6 \]

\[ f_L = \frac{K_{M,L}}{K_{M,L} + [Ca^{2+}]_{in}} \]

In order to ensure the simplicity of our model, we chose to use the parameters of the original Hodgkin-Huxley model [31] for the sodium, potassium and leak currents. These parameters were then slightly modified to fit the firing frequency of DA neurons. However, the mechanisms highlighted are robust to parameter variations, and are still present using the original values. The parameters for the L-type calcium current were taken from [14]. The only parameter that had to be tuned was the relative difference in timescales between the fast \( \langle Na^+ - K^+ \rangle \) and slow \( \langle Ca^{2+} \rangle \) dynamics (namely the value of \( k_1 \)), to ensure a spontaneous single-spike activity rather than endogenous bursting. In the equation describing the fluctuations of \( [Ca^{2+}]_{in} \) the term \( k_2 I_{Na} \) accounts for any voltage-dependent calcium entry unrelated to L-type calcium channels, to ensure a minimal calcium oscillation even when these channels are fully inhibited. In the detailed model [14], this calcium entry is provided by other voltage-dependent calcium channels.

**Analyses**

Simulations were performed using the Neuron software, which is freely available for download at http://www.neuron.yale.edu. Analyses were performed with Matlab 7.4.0.

**Bifurcation diagram and variations of calcium thresholds.** Bifurcation diagrams were drawn both using the graphical Matlab package matcont (which is freely available for download at http://www.matcont.ugent.be/) and the results of simulations.

**In vitro extracellular recordings**

**Housing.** Adult (200-250 g) male Wistar rats were housed in groups of three or four, supplied with food and water ad libitum, and maintained on a 12 hour light/dark cycle.

**Tissue preparation.** Rats were anesthetized with chloral hydrate (400 mg/kg, i.p) and decapitated. The brain was extracted

| Parameter | Value |
|-----------|-------|
| \( C_0 \) | \( 10^{-3} \) \( \mu F/cm^2 \) |
| \( V_{Na} \) | 50 mV |
| \( V_{L} \) | -95 mV |
| \( V_L \) | -54.3 mV |
| \( V_{Ca} \) | 120 mV |
| \( g_{Na} \) | 0.16 S/cm^2 |
| \( g_{K,p} \) | 0.024 S/cm^2 |
| \( \gamma \) | 0.3 \( 10^{-3} \) S/cm^2 |
| \( g_{Ca,L} \) | 3.1 \( 10^{-3} \) S/cm^2 |
| \( g_{K,m} \) | 0.1 \( 10^{-3} \) S/cm^2 |
| \( g_{K,Ca} \) | 5 \( 10^{-3} \) S/cm^2 |
| \( I_{Ca,pump,ext} \) | 0.0156 mA/cm^2 |
| \( K_{M,F} \) | 0.0001 mM |
| \( K_{M,L} \) | 0.0018 mM |
| \( k_1 \) | 0.1375 \( 10^{-3} \) |
| \( k_2 \) | 0.04 \( 10^{-3} \) mM |
| \( k_3 \) | 0.018 \( 10^{-4} \) |

Table 2. Parameter values.

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out of the skull in less than 1 min and cooled in ice-cold (2–4°C) artificial cerebrospinal fluid (ACSF) of the following composition (in mM): NaCl, 130; KCl, 5; NaH₂PO₄, 1.25; MgSO₄, 1.25; CaCl₂, 2.5; D-glucose, 10; NaHCO₃, 24; saturated with 95%O₂ and 5%CO₂ (pH 7.4).

Horizontal slices (400 µm) containing the midbrain were cut in cold ACSF in a vibratome and transferred to a small beaker containing ACSF at 32°C. After 10–30 min slices were transferred to the recording chamber (volume 0.5 ml) in which they were completely submerged and superfused by ACSF at a rate of 2.5 ± 0.5 ml/min (T°: 34.5 ± 0.5°C). The tissue was held in position by small platinum weights.

**Action potential recordings and identification of neurons.** Action potentials (amplitude: 200 to 1000 µV) were recorded extracellularly using borosilicate capillaries (model 1403516, Hülgenberg, Malsfeld, Germany) which had been pulled on a Narishige (PE-2) vertical puller. The tip resistance was 5–20 MΩ. They were passed through an impedance adapter and amplified one thousand times with a homemade amplifier. They were displayed on an oscilloscope and fed to an analog digital interface (CED 1401) connected to a computer. Data were collected with the use of the Spike 2 software (version 4.23, Cambridge Electronic Design, Cambridge, UK). Use of an appropriate template ensured that the activity of only one cell was recorded.

Electrophysiological criteria were used in order to identify DA neurons. In vitro, these neurons exhibit a very regular firing pattern and long (≥2.5 ms), triphasic spikes, often displaying a prominent notch in the initial positive rising phase. They have a slow firing rate comprised between 0.5 and 5 Hz. A large number of previous experiments in our laboratory have shown that the firing of these cells is inhibited by nanomolar concentrations of D2 agonists such as quinpirole and BHT920 [32]. This was verified again in this study in the absence of synaptic blockers (Supplementary Fig. 2B). Neurons meeting these criteria were selected for recording.

Only one cell was studied per slice. All recordings were made in the substantia nigra pars compacta area. Drugs were applied by superfusion at known concentrations using three-way taps. Each concentration was applied for at least 10 min to ensure that the drug concentration reached equilibrium in the tissue. Drug effects were quantified by calculating the mean firing frequency over the 5 last minutes of the control period and over the last minute during which the drug was superfused. Synaptic blockers were superfused throughout all experiments unless stated otherwise. Neurons whose firing rate varied by more than 5% (average of 1 min) during the control period were discarded.

**Experimental protocol.** The activity of DA neurons was recorded in control conditions for 5 minutes. Synaptic blockers (10 µM CNQX, 1 µM MK801, 10 µM SR95531, 1 µM sulpiride and 1 µM CGP55845 to block AMPA, NMDA, GABA<sub>4</sub>, D2 and GABAA<sub>5</sub> receptors, respectively) were then superfused for the remainder of the experiment. After at least 10 minutes, L-type calcium channels were blocked by bath application of 20 µM nifedipine for 10 minutes as well. When this compound completely blocked the firing of the cell, the experiment was stopped at this stage. Otherwise, nifedipine was washed out for 10 minutes. The sodium channel blocker tetrodotoxin (TTX) was then applied at 30 nM for 10 minutes. Again, if TTX completely blocked the firing of the cell, the experiment was stopped. Otherwise, TTX and nifedipine were co-applied for the next 10 minutes. After this period, TTX and nifedipine were washed out.

**Drugs.** The sources of the drugs used were as follows. CGP55845, CNQX, MK801, TTX and Nifedipine were obtained from Tocris Cookson (Bristol, UK). SR95531 was obtained from Sigma (St Louis, MO, USA). Sulpiride was a gift from Sanofi-Aventis.

**Statistical analysis.** Experimental data were analyzed with a global ANOVA test for correlated values, followed by Tukey’s post-hoc tests for comparisons between groups.

**Supporting Information**

**Figure S1** Cooperation between sodium and calcium channels in the generation of spontaneous activity in the detailed model. The center panel shows the type of pacemaker activity according to the sodium and L-type calcium conductances. The white zone represents the couples of conductances which results to a spontaneous hyperpolarization of the cell and the dark blue zone account for pacemaking. Each insert shows the behavior of the model in control condition and during a blockade of L-type calcium channels or sodium channels for a particular set of conductances, respectively. The pacemaker behavior of the model strongly relies on the values of both the sodium and the L-type calcium conductances.

**Figure S2** Effect of synaptic blockers and a D2 receptor agonist on the firing rate of SNc DA neurons in brain slices. (A) Mean firing frequency (samples of 2 minutes) of the recorded cells over time (mean ± sem, n = 4). (B) Mean firing frequency (samples of 30 seconds) of the recorded cells over time (mean ± sem, n = 6). The application of synaptic blockers induces an increase in the firing rate which remains stable for at least one hour. The application of the D2 receptor agonist BHT 920 (100 nM) [32] strongly reduces the firing rate of the recorded cells.

**Figure S3** I-V curves of various depolarizing currents in the two models. I-V curves of sodium channels (in red) and of L-type calcium channels (in black) of the minimal model (A) and of the detailed model (B). For the detailed model, I-V curves of N-type (in blue) and T-type (in dotted black) calcium channels are also plotted. The only current which has a significantly different half-activation potential as compared to the L-type calcium current is the T-type calcium current.

**Figure S4** Analysis of the slow oscillatory potentials of the minimal model. (A) Variations of the membrane potential (top) and of the intracellular calcium concentration (bottom) over time. (B) Sketch of the bifurcation diagram of the minimal model, with [Ca<sup>2+</sup>]<sub>i</sub> as the bifurcation parameter. The gray part corresponds to negative values of [Ca<sup>2+</sup>]<sub>i</sub>, which are non physiological. V<sub>ss</sub> denotes the steady-state curve for each value of the bifurcation parameters. The dotted part of V<sub>ss</sub> shows its unstable part. SN denotes a saddle-node bifurcation. Trajectories of the membrane potentials are plotted in red.

**Figure S5** Comparison of the calcium dynamics during pacemaking and slow oscillatory potentials. (A and B) Evolution of membrane potential (top) and calcium oscillations (bottom) over time in control conditions and during a sodium blockade, respectively. (C) Variations of intracellular calcium concentrations during both oscillatory patterns.

**Figure S6** Effect of sodium channel density on the response of the detailed model to calcium channel blockade. Response of the detailed model to an inhibition of all calcium channels for two
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Author Contributions
Conceived and designed the experiments: GD RS VS. Performed the experiments: GD LM. Analyzed the data: GD LM RS VS. Contributed reagents/materials/analysis tools: GD. Wrote the paper: GD RS VS.

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