OGLE-2018-BLG-0677Lb: A Super-Earth Near the Galactic Bulge

Antonio Herrera-Martín, M. D. Albrow, A. Udalski, A. Gould, J. C. Yee, S.-J. Chung, C. Han, K.-H. Hwang, Y. K. Jung, W. Zang, S.-M. Cha, Y. K. Jung, S.-J. Chung, K.-H. Hwang, K. Ulaczyk, M. K. Szymański, P. Mróz, J. Skowron, R. Poleski, I. Soszyński, S. Kozłowski, P. Pietrukowicz, K. Ulaczyk, K. Rybicki, P. Iwanek, and M. Wrona (OGLE Collaboration)

1 School of Physical and Chemical Sciences, University of Canterbury, Private Bag 4800, Christchurch, New Zealand
2 Astronomical Observatory, University of Warsaw, Al. Ujazdowskie 4, 00-478 Warsaw, Poland
3 Department of Astronomy, Ohio State University, 140 W.18th Ave., Columbus, OH 43210, USA
4 Korea Astronomy and Space Science Institute, Daejon 34055, Republic of Korea
5 Max-Planck-Institute for Astronomy, Königstuhl 17, D-69117 Heidelberg, Germany
6 Harvard-Smithsonian Center for Astrophysics, 60 Garden St., Cambridge, MA 02138, USA
7 Korea University of Science and Technology, 217 Gajeong-ro, Yuseong-gu, Daejeon, 34113, Republic of Korea
8 Department of Physics, Chungbuk National University, Cheongju 28644, Republic of Korea
9 Department of Particle Physics and Astrophysics, Weizmann Institute of Science, Rehovot 76100, Israel
10 Division of Physics, Mathematics, and Astronomy, California Institute of Technology, Pasadena, CA 91125, USA

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Abstract

We report the analysis of the microlensing event OGLE-2018-BLG-0677. A small feature in the light curve of the event leads to the discovery that the lens is a star–planet system. Although there are two degenerate solutions that could not be distinguished for this event, both lead to a similar planet-host mass ratio. We perform a Bayesian analysis based on a Galactic model to obtain the properties of the system and find that the planet corresponds to a super-Earth/sub-Neptune with a mass of $M_{\text{planet}} = 3.96^{+3.66}_{-2.66} M_{\oplus}$. The host star has a mass of $M_{\text{host}} = 0.12^{+0.14}_{-0.08} M_{\odot}$. The projected separation for the inner and outer solutions are 0.63$^{+0.20}_{-0.17}$ au and 0.72$^{+0.23}_{-0.19}$ au respectively. At $\Delta \chi^2 = \chi^2(1L1S) - \chi^2(2L1S) = 46$, this is by far the lowest $\Delta \chi^2$ for any securely detected microlensing planet to date, a feature that is closely connected to the fact that it is detected primarily via a “dip” rather than a “bump.”

Unified Astronomy Thesaurus concepts: Gravitational microlensing exoplanet detection (2147); Gravitational microlensing (489); Astrostatistics strategies (1885); Super Earths (1655); Exoplanets (498)

Supporting material: data behind figure

1. Introduction

In the study of astronomical bodies, the search for extra-solar planets is of particular interest as their characterization not only allows us to infer the similarities or differences in the mechanisms of their formation, but it also helps us to better understand our own solar system (Ollivier et al. 2008). There is a wide range of methods for planet discovery such as radial velocity (RV), transit photometry, microlensing, direct imaging, etc. This has been a huge leap since the first detection of an extra-solar planet more than 20 yr ago (Cochran et al. 1991); to date there are 4000 extra-solar planets (≥4104 as of 2019 December), with the majority (≥3000) having been found by the transit method.

Gravitational microlensing is a particular type of gravitational lensing for which both source and lens are stellar mass objects and the angular size of the magnified images cannot be resolved (Vieri & Ostriker 1983; Paczyński 1986; Schneider et al. 2006; Tsapras 2018, etc.). Instead, we study the difference in brightness of the source produced by the gravitational interaction of the lens when it crosses through the line of sight (Einstein 1936; Paczyński 1986; Mollerach & Rout 2002; Mao 2012; Schneider et al. 2013, etc.). Although, it was theorized since the formulation of gravitational lensing, the very small likelihood of the necessary alignment discouraged its observation as having low probability. The proposition had a resurgence in interest following the work of Paczyński (1986), which led to the start of microlensing observations with the first detection in 1993 (Alcock et al. 1993; Udalski et al. 1993).

Mao & Paczyński (1991) pointed out how the formalism for binary lenses and the feasibility of their observation could be used for detecting either binary systems or a planetary system. This was developed by several authors in the following years (Gould & Loeb 1992; Griest & Hu 1992; Albrow et al. 2000; Gould 2000; An et al. 2002; Bennett et al. 2002; Rattenbury 2006, etc.). Nevertheless, it took almost a decade for the first confirmed exoplanet by a microlensing observation to be published by Bond et al. (2004).

Currently there are over 80 confirmed planets discoveries through microlensing observations. The rate of detections has increased in recent years with the advent of the Korean Microlensing Telescope Network (KMTNet; Kim et al. 2016).
This work addresses the microlensing event OGLE-2018-BLG-0677. This is a relatively faint, moderate-magnification event with some evidence for an anomaly soon after peak brightness. From a comparison with single lens, binary lens, and binary source models, we will show a strong preference for a binary lens interpretation. As we can only obtain directly two physical quantities for the system, we perform a Bayesian analysis to infer the probable physical properties for the host (lens) and companion. The resulting distributions suggest that the companion is a low-mass planet.

In Section 2 of this paper we briefly describe the observations of the event. Section 3 describes our model selection, as well as the details of the light curve fitting process, and presents the best-fit values. In Section 4, we investigate the angular size of the source and its implications for the Einstein radius, and in Section 5 we give a detailed description of the approach taken for the Bayesian analysis used to infer the properties of the lensing system, and present the resulting distributions. From these we derive the planet mass and the separation from its host. In Section 6 we discuss some of the implications of this work and, finally, Section 7 is a brief discussion concluding the paper.

2. Observations

2.1. OGLE

The event was first detected by the Optical Gravitational Lensing Experiment (OGLE) Early Warning System (Udalski et al. 1994; Udalski 2003), with designations OGLE-2018-BLG-0677 and OGLE-2018-BLG-0680, since it lies in the overlap region of two survey fields. It is located at (R.A., decl.) = (17°55′00″.27, −32°00′59″.51), which corresponds to (l, b) = (−1°561, −3°31) in Galactic coordinates. In combination, the observations from the two fields have a frequency of 1–3 data points per day. The OGLE observations were reduced using the difference image analysis from Wozniak (2000).

2.2. KMTNet

KMTNet is a wide-field imaging system, with three telescopes and cameras sharing the same specifications, installed at Cerro-Tololo Inter-American Observatory in Chile (KMTC), the South African Astronomical Observatory in South Africa (KMTS), and the Siding Spring Observatory in Australia (KMTA). The telescopes each have a 1.6 m primary mirror, and a wide-field camera (a mosaic of four 9k × 9k CCDs) that image approximately a 2.0 × 2.0 square degree field of view.

Weather permitting, the network of telescopes and cameras allow a 24 hr per day monitoring of the Galactic bulge. This allows one to trace the light curves of stars continuously and is ideal for the detection of extra-solar planets by microlensing and transit, variable objects, and asteroids and comets.

The event OGLE-2018-BLG-0677 was independently detected by KMTNet and given the designation KMT-2018-BLG-0816 (Kim et al. 2018). The event is located in the BLG01 and BLG41 KMTNet fields, giving an effective observation cadence of 15 minutes.

Photometry was extracted from the KMTNet observations using the software package PYDIA (Albrow 2017), which employs a difference-imaging algorithm based on the modified delta-basis-function approach of Bramich et al. (2013). The light curve of the event, with a single lens single-source (1L1S) model, is shown in Figure 1.

3. Light Curve Analysis

The following sections present the several models fitted to the data as well as the reasoning by which we selected the best among them.

3.1. Single Lens Single Source

This is the simplest of models, which considers a point mass lens with a point mass source. The magnification is modeled by a Paczyński (1986) curve,

\[ A(u) = \frac{u^2 + 2}{u^2 + 4}, \]

where \( u \) is the angular separation between source and lens, normalized by the Einstein angle \( \theta_E \). Given the relative motion between them, this separation will be a function of time and is assumed rectilinear as

\[ u(t) = (\tau^2 + u_0^2)^{1/2}, \]

with \( \tau \equiv (t - t_0)/t_E \); where \( u_0 \) is the impact parameter of the event, \( t_0 \) is the time at \( u = u_0 \), and \( t_E \) is the Einstein radius crossing time. These three parameters characterize completely the light-curve magnification model, \( A(t) \). We find these parameters by a Markov Chain Monte Carlo (MCMC) search while reducing the \( \chi^2 \) of a linear fit to the observed flux, \( F(t) = A(t)S_B + F_B \), where the source and blend flux, \( S_B \) and \( F_B \), are determined for each data set.

The best-fit values (after renormalization of data uncertainties as will be discussed in Section 3.4) are presented in Table 1. We note that in Tables 1–3, \( S_B \) and \( F_B \) are given in a system with 18 as the magnitude zero-point.
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Table 1

| Parameter | Value |
|-----------|-------|
| $\chi^2_{min}/N_{data}$ | 1602.51/1557 |
| $u_0$ | 0.0129 ± 0.0012 |
| $t_0$ | 8229.5417 ± 0.0007 |
| $t_F$ (days) | 4.95 ± 0.04 |
| $F_{O\text{GLE}0677}$ | 0.293 ± 0.009 |
| $F_{\text{B,OGLE}0677}$ | −0.065 ± 0.011 |

Table 2

| Parameter | Value |
|-----------|-------|
| $\chi^2_{min}/N_{data}$ | 1593.08/1557 |
| $u_{01}$ | 0.103 ± 0.004 |
| $t_{01}$ | 8229.542 ± 0.004 |
| $u_{02}$ | 0.055 ± 0.005 |
| $t_{02}$ | 8229.873 ± 0.046 |
| $q_F$ | 0.0031 ± 0.0017 |
| $t_F$ (days) | 4.96 ± 0.14 |
| $F_{O\text{GLE}0677}$ | 0.287 ± 0.009 |
| $F_{\text{B,OGLE}0677}$ | −0.063 ± 0.011 |

Table 3

| Parameter | Inner | Outer |
|-----------|-------|-------|
| $\chi^2_{min}/N_{data}$ | 1556.03/1557 | 1555.96/1557 |
| $s$ | 0.912 ± 0.002 | 0.985 ± 0.002 |
| $\log_{10}(q)$ | −4.105 ± 0.002 | −4.054 ± 0.009 |
| $\rho_s$ | 0.01200 ± 0.00013 | 0.01239 ± 0.00016 |
| $u_0$ | 0.0035 ± 0.0005 | 0.0035 ± 0.0005 |
| $\alpha_0$ | −1.98 ± 0.01 | −1.98 ± 0.01 |
| $t_0$ | 8229.544 ± 0.002 | 8229.544 ± 0.002 |
| $t_F$ (days) | 4.94 ± 0.11 | 4.94 ± 0.11 |
| $F_{O\text{GLE}0677}$ | 0.294 ± 0.009 | 0.294 ± 0.009 |
| $F_{\text{B,OGLE}0677}$ | −0.069 ± 0.011 | −0.070 ± 0.011 |

3.2. Anomaly

As can be seen in Figure 1, there is a small anomalous feature in the light curve relative to the 1L1S model that occurs over ~5 hr during the interval 8229.70–8229.90. The anomaly primarily takes the form of a dip of ~0.05 mag followed by a smaller and shorter bump. See the residuals in Figure 2. These features are well traced by the KMTC01 and KMTC41 data sets, and they are confirmed by two points from the OGLE-2018-BLG-0680 data, one each on the dip and the subsequent small bump. The OGLE-2018-BLG-0677 data set has a single point just before the start of the anomaly. We have examined the direct and difference images from KMTC and are satisfied that there are no systematic effects that can be attributable to seeing, background, or image cosmetics that could cause these features. Additionally, we have found no evidence that the dip is a repeating phenomenon, such as might be due to a starspot.

3.3. Single Lens Binary Source

We examine the possibility that the anomaly is due to a binary source. In the case that the source consists of two stars, the total flux is given by the linear combination of the individual source fluxes, $F_{\text{tot}} = A_1 F_1 + A_2 F_2 + F_B$, where $A_1$ and $A_2$ are the individual magnifications of each source (Gaudi 1998) as parameterized in Section 3.1, but sharing the same value of $t_F$.

The total magnification of the combined source flux is given by

$$A_{\text{tot}} = \frac{A_1 + A_2 q_F}{1 + q_F},$$

where $q_F = F_2/F_1$ is the luminosity ratio (Griest & Hu 1992). In total, there are six parameters: $u_{01}$ and $t_{01}$ for $A_1$; $u_{02}$ and $t_{02}$ for $A_2$; $t_F$ is shared by $A_1$ and $A_2$; and the luminosity ratio $q_F$.

We fit the data as described in the previous subsection but using this model instead. The best-fit values found for the data are presented in Table 2, and the light-curve model shown in Figure 2. It is apparent that the best binary source model does not reproduce the anomalous feature in the light curve, but produces a small “bump” deviating almost imperceptibly from the 1L1S model.

3.4. Binary Lens

We adopt the standard parameterization of a binary lens light curve by describing it with seven parameters (Gaudi 2012): $s$, $q$, $\rho_s$, $\alpha$, $u_0$, $t_0$, and $t_F$. These represent the normalized separation between binary lens components, the mass ratio of the binary lens components, the normalized source radius, the source trajectory angle with respect to the binary axis, the normalized closest approach between the lens center of mass and the source (which occurs at time $t_0$, the time of closest approach), and the timescale to cross the Einstein radius, respectively. The factor used for the normalized parameters is the angular Einstein radius,

$$\theta_E = \frac{4GM_L}{c^2} \left( \frac{1}{D_L} - \frac{1}{D_S} \right),$$

where $M_L$ is the total mass of the lens system, and $D_L$, $D_S$ are the distances from Earth to the lens and source. A visualization
of this combination of parameters can be found in Jung et al. (2015).

The fitting is done by a maximum likelihood estimation, which is equivalent to minimization of the $\chi^2$. The process is done in two parts. The first is through a fixed value grid search of the $(s, q)$ parameters to find regions where the minimum $\chi^2$ may be located. For each $(s, q)$, a grid of $(r, \alpha)$ (where $r$ is a reparameterization of $u_0$, centered-on and normalized to caustics, see McDougall & Albrwo 2016) is used to seed a minimization over $(\rho_a, t_0, t_\varphi)$ by a simple Nelder–Mead optimization (Nelder & Mead 1965). This approach for the fixed $(s, q, r, \alpha)$ is due to the relation of these parameters to the geometry.

Our fixed position results are then used as seeds for a more refined search using an MCMC algorithm implemented using the MORSE code (McDougall & Albrwo 2016). A similar two-step process can also be seen in Shin et al. (2019). During this second part of the process, the seed solutions from the grid search are used as starting points, and the search is now continuous in the parameter space.

Once a minimum value for $\chi^2$ was found, the original magnitude uncertainties for each data set were renormalized via

$$\sigma_i' = k \sqrt{\sigma_i^2 + \epsilon^2}. \quad (5)$$

The coefficients $k$ and $\epsilon$ for each data set are determined in such a way that the reduced $\chi^2$ for both the higher- and lower-magnification data points for each site are approximately unity (Yee et al. 2012). The renormalization factors are listed in Table 6. The MCMC search was then re-run with the renormalized data uncertainties to corroborate the solution and obtain a new minimized $\chi^2$. The final model parameter values and their uncertainties are directly obtained from the 68% confidence interval around the medians of the marginalized posterior parameter distributions.

Given the short total time of the event, it was not possible to obtain parallax information (Gould 1992, 2000; Alcock et al. 1995; Buchalter & Kamionkowski 2002). For the rest of our analysis, no higher-order light-curve effects were considered.

### 3.4.1. Model of OGLE-2018-BLG-0677

From the fitting process described in the previous section, we found two degenerate solutions with similar $q$. Often this situation corresponds to a well-known wide/close case degeneracy where $s < 1$ and $s > 1$ for the two solutions (see, e.g., Griest & Safizadeh 1998; Dominik 1999; Batista et al. 2011). However, in the present case, the degeneracy is between two solutions with $s < 1$, and is due to a source trajectory passage past two cusps of connected or disconnected caustics, as shown in Figure 3. Each correspond to a minor-image perturbation that demagnifies the source relative to the magnification due solely to the host star. This type of degeneracy has been detected previously for events OGLE-2012-BLG-0950 (Koshimoto et al. 2017) and OGLE-2016-BLG-1067 (Calchi Novati et al. 2019). A thorough explanation of the phenomenon is given in Han et al. (2018) with reference to the event MOA-2016-BLG-319. Following the nomenclature of that paper, we refer to the case where the source passes between the caustics as the “inner” solution, and that where it passes the single connected caustic as the “outer” solution.

For the current event, OGLE-2018-BLG-0677, we could not break this degeneracy given that both cases produce almost identical light curves, see Figure 3. Table 3 lists the best-fit parameters for both solutions. Apart from the clear difference in geometry, they share several parameters, $q_1$, $u_0$, $t_0$, and $t_\varphi$, well within their respective uncertainties. Also, the values of the minimum $\chi^2$ are close enough that there is no clear statistical difference. Despite this degeneracy, the similarities of $q, \rho, \beta$, and $t_\varphi$ will allow us to infer similar physical properties for the system, which will be discussed in the following section.

As a note, $\rho_a$ is detected rather weakly in the light-curve analysis. It may be of interest to ask whether the omission of $\rho_a$ affects our subsequent results in any significant way.

Therefore in Section 5.2 we give results that propagate the $\rho_a$ distribution, and also show the case where the $\rho_a$ information is omitted from the Bayesian estimates.

### 3.4.2. Other Local Minima

Five additional seed solutions were identified in our initial grid search close, located close in $(s, q)$ to the solutions reported above. All of these are very shallow in $\chi^2$ space, and with subsequent MCMC runs, all converged to one of either of the reported solutions. Light curves and caustic geometries for the two most prominent of these local minima are shown in Figure 4.

To analyze how these local minima are related to the best-fit solutions, we followed the procedure described in Hwang et al. (2017) and ran various “hot” and “cold” MCMC realizations to explore the regions around all the solutions. In Figure 5 we present a scatter plot of the combined samples from the various runs, color coded by their $\Delta \chi^2$ relative to the best solutions. We adopt the parameter

$$\Delta \xi = u_0 \csc \alpha - (s - 1)/s, \quad (6)$$

introduced by Hwang et al. (2017), which traces the offset between the centers of the source and the major-image caustic
source trajectory over an on-axis cusp that provides a single bump in magnification, and correspond to a major-image perturbation with degeneracies as discussed in Gaudi & Gould (1997).

Their light-curve fit parameters are listed in Table 4, without uncertainties as they are too shallow in $\chi^2$ space to retain an MCMC chain. They have a similar $t_f$ to the best solutions, but a larger $\rho_s$.

3.5. Model Selection

From Figure 1, it can be seen that there is a subtle anomaly following the peak of the light curve compared to the 1L1S model. Although a binary lens model could in principle represent this small feature found in the data, the justification for the increase in model complexity needs to be strengthened; therefore, to avoid overfitting by assuming a binary lens (Gaudi 1997), we compared with two simpler models. The three models compared are the previously described single lens single-source (1L1S), single lens binary source (1L2S), and binary lens single-source (2L1S) models. Often the $\chi^2$ value is used as an indicator of the goodness of fit, but this time instead of simply relying on this statistic to compare between different models, we obtain the log evidence given the data, $\ln Z$, for a more robust model comparison. This was done by applying the nested sampling method (Skilling 2006) for cases (1L1S) and (1L2S). For the case of (2L1S), nested sampling was too inefficient, so the approximation algorithm presented in van Haasteren (2009) for posterior distributions was used instead to estimate $\ln Z$. For completeness, we also applied the approximate algorithm to the other two cases, which led to the same results as nested sampling. The log odds ratio is obtained by $\ln O = \ln Z_{1L1S} - \ln Z_{1L2S}$, and a model is preferred as long as $\ln O > 0$, but a strong preference is given when $\ln O > 5$ (Jaynes et al. 2003; Sivia & Skilling 2006).

The 2L1S best fit has two degenerate solutions, inner and outer (see Griest & Safizadeh 1998), but the difference in $\chi^2$ between these ($\Delta \chi^2 = 0.07$) is small, with a slight preference to the outer model. On the other hand, the log evidence gives a strong preference for the inner model. We need to adopt a model for renormalization, so we decided to choose the inner solution for this purpose.

Table 5 shows the minimum $\chi^2$ and the log evidence based on the renormalized data error bars, and it is clear that the 2L1S solution is preferred with $\Delta \chi^2 > 46$ compared with the 1L1S, and is also preferred from the evidence. The renormalization parameters are found in Table 6.
One last consideration worth mentioning is the case for 1L2S. From the $\chi^2$ point of view it seems to improve compared to 1L1S, however the evidence gives an indication that the 1L1S is slightly better. Here the meaning of the evidence becomes clear. It says that the 1L2S model is not better than the 1L1S (the extra model complexity does not outweigh the reduction in $\chi^2$), and in fact the difference with the 1L1S model is only between 8229.85 and 8229.88. This can be clearly seen in Figure 2 with the 1L1S and 1L2S best-fit light curves.

4. Color–Magnitude Diagram

A sample instrumental color–magnitude diagram (CMD) for a $1.5 \times 1.5$ arcmin field around OGLE-2018-BLG-0677 is shown in Figure 6 based on KMTC data. The source position is indicated, with its magnitude determined from the source flux inferred by the light-curve model, and its color from a regression of $V$-band difference flux against $I$-band difference flux.

From an analysis of four such CMDs (KMTC01, KMTC41, KMTS01, and KMTS41), we found a color offset from the red clump, $(V-I)_0 - (V-I)_{RC} = -0.47 \pm 0.04$, and a magnitude offset, $I_0 - I_{RC} = 3.20 \pm 0.03$. Combining these with the red clump intrinsic color, $(V-I)_{RC,0} = 1.06$ (Bensby et al. 2013), and magnitude for this Galactic longitude, $I_{RC,0} = 14.534$ (Nataf et al. 2013), we find for the source that $(V-I)_{0,s} = 0.59 \pm 0.04$ and $I_{0,s} = 17.73 \pm 0.03$.

From Bessell & Brett (1988) we convert our color to $(V - K)_0 = 1.25 \pm 0.10$, and using the surface-brightness relations of Kervella et al. (2004) we determine the source angular radius to be $\theta_s = 0.789 \pm 0.025 \text{ mas}$.

5. Properties of the Lensing System

In the previous sections we presented the results from the light-curve fitting, from which our sources of physical information are $t_E$ and $\rho_s$. Also, we could not break the outer/inner geometry, but fortunately the fitting showed that the majority of the parameters are similar within their uncertainties (see Table 3), in particular the crossing time $t_E$. Doing a direct comparison of the posterior distributions for both solutions, it is clear that they also share a similar distribution of $\rho_s$ as seen in Figure 7, despite the $s$ distributions being different. This becomes important because we can proceed to the Galactic model expecting a priori that both solutions will share similar characteristics.

5.1. Bayesian Analysis

We performed a Bayesian analysis to characterize the physical properties of the system. As remarked above, our source of information from the light curve comes only from the distributions of $t_E$ and $\rho_s$, which restricts how much information we can gather. In other words, we need to limit the number of parameters used in the analysis to the most basic. The main parameters are the total mass of the lens, $M_L$, the distance to the lens, $D_L$, the proper motion, $\mu_\text{rel}$, and the source distance, $D_S$. Nevertheless, during the formulation of the analysis, the effective transverse velocity $v = D_L \mu_\text{rel}$ will be used as an intermediate step during the parameter sampling.

Our analysis resembles a hierarchical Bayes (see e.g., Gelman et al. 2003),

$$p(\Theta|y) \propto p(\Theta) \int p(t_E, \rho_s|\Theta)p(y|t_E, \rho_s)d\rho_sdt_E,$$

(7)

where

$$\Theta \equiv (M_L, D_L, D_S, v)$$

(8)

$$y \equiv \text{data}.$$

(9)

This describes the probability distribution function for $t_E$ and the weights based on the distribution of $\rho_s$, which is shown in Figure 7. The prior sampling distribution for the physical quantities is $p(\Theta)$, which includes the information of the Galactic model. For the analysis, $t_E$ and $\rho_s$ act as constraints, and they are hidden in $p(t_E, \rho_s|\Theta)$, which is the probability of a value of $t_E$ and $\rho_s$ given by the physical parameters.
Figure 7. MCMC chains and posterior distributions. The first left panel displays the fully marginalized distributions for $\rho_\star$, which shows how the inner and outer distributions overlap. The right panels show the fully marginalized distributions for $s$, log10$q$, and $t_\epsilon$ for the outer (blue) and inner (red) solutions, which will be used to derive the properties of the host and companion. The four left lower panels show the Markov chain points for these parameters projected against $\rho_\star$.

For this purpose we took a combined approach in which we perform an MCMC simulation to obtain the posterior distribution from the Galactic modeling. Ideally, we would describe the process in observable variables similar to Batista et al. (2011), Yee et al. (2012), or Jung et al. (2018), but in this case we are only able to relate two observables to the physical parameters, $t_\epsilon$ and $\rho_\star$. We therefore take advantage of the Monte Carlo simulation to take care of the marginalization. We used two different sampling algorithms in order to verify that our results contain no algorithmic bias. Independently, we ran the Emcee sampler (Foreman-Mackey et al. 2013), which uses the standard Metropolis–Hasting sampling method, and Dynasty (Higson et al. 2018), which uses nested sampling. After convergence, both algorithms arrived at the same posterior distributions.

Our approach is similar to that of Yoo et al. (2004), but we describe our Galactic model and the fact that we can define the probability of a physical property given an observed parameter, e.g., $p(\Theta | \theta^0)$, as presented in Dominik (1998) and Albrow et al. (2000).

For the Galactic model, the lens mass function, $\Phi_{\log m}$, is a power-law or Gaussian distribution depending on the mass ranges according to Chabrier (2003). The mass density distribution, $\Phi_s(x)$, considers the disk, bulge, or both depending on the case, where the disk is modeled by a double exponential with 0.3 and 1.0 kpc as the scale heights of a thin and thick disk perpendicular to the Galactic plane, and the corresponding column mass densities are $\Sigma_{\text{thin}} = 25 M_\odot \text{pc}^{-2}$ and $\Sigma_{\text{thick}} = 35 M_\odot \text{pc}^{-2}$. For the bulge we adopt a model of a barred bulge that is tilted by an angle of 20° (see Han & Gould 1995; Grenacher et al. 1999). The probability density of the absolute effective velocity, $\Phi_v(x)$, assumes Gaussian distributions, for which isotropic velocity dispersions are assumed for the Galactic disk and bulge, and the values of $\sigma_{\text{disk}} = 30 \text{ km s}^{-1}$ and $\sigma_{\text{bulge}} = 100 \text{ km s}^{-1}$ are adopted. While the velocity mean for bulge objects is assumed purely random, the disk lenses rotation velocity can described by a Navarro–Frenk–White model (see Navarro et al. 1997). The precise equations for each component of the Galactic model can be found in the appendices of Dominik (2006).

Therefore, the probability of our assumed Galactic model (galactic prior) for the lens is in the form

$$p_f(m, \zeta, x) \propto \Phi_{\log m}(\log m) \Phi_s(\zeta, x) \Phi_v(x),$$

selecting from bulge or disk populations accordingly. The parameters in this prescription are the mass, $m = M/L_\odot$, the fractional lens-source distance, $x = D_L/D_s$, and the effective transverse velocity, $\zeta = v/\nu_c$, where $\nu_c = 100 \text{ km s}^{-1}$ is a scaling constant to keep the velocity dimensionless. These distributions and prescriptions can also be found in Dominik (2006), and, as mentioned above, the assumed properties are described in its appendix.

The source distance probability distribution is defined as

$$p_{\text{source}}(D_s) = \frac{D_L^2 \rho(D_s)}{\int_0^{D_{L,\text{max}}} D_L^2 \rho(D_s) \, dD_s},$$

where $\rho(D_s)$ is the density of objects at the source distance as defined in Dominik (2006). We adopted this distribution as we do not have any information on the source location, and we based its definition on the Zhu et al. (2017) argument, but we use a value of $\gamma = 1$. For our calculations, we assumed that the source was part of the bulge population.

Therefore, the Galactic prior, which has the Galactic model information, is sampled from the probability distribution

$$p(\Theta) \propto \Omega(m, \zeta, x)p_f(m, \zeta, x)p_{\text{source}}(D_s).$$

The lens for bulge or disk populations are selected accordingly. Meanwhile, the information of the prior is weighted by

$$\Omega(m, \zeta, x) \propto (M/M_\odot)^{1/2} \zeta \sqrt{x(1 - x)}$$
The parameter $t_E$ then becomes intrinsic and is defined as

$$t_E(m, \zeta, x, D_S) = \frac{2r_{E,\odot}\sqrt{m}(1-x)}{\zeta_c},$$

(14)

where

$$r_{E,\odot} = \sqrt{\frac{GM_*}{c^2}D_S}$$

(15)

is a scale length defined as the Einstein radius of a solar mass lens located halfway between the observer and source.

The angular source size parameter,

$$\rho_s(m, x, D_S) = \theta_s/\theta_E(m, x, D_S),$$

(16)

where $\theta_s$ is the source angular radius given in the previous section and $\theta_E(m, x, D_S)$ is the Einstein angle for an MCMC realization.

Given that $\rho_s$ and $t_E$ are derived from the prior parameters, their joint probability is

$$p(t_E, \rho_s|\Theta) \propto \delta(t_E - t_E(\Theta))\delta(\rho_s - \rho_s(\Theta)).$$

(17)

Additionally, there is a weight given by the information contained in the probability distribution $p(y|t_E, \rho_s)$, which corresponds to the posterior distributions of our solution from our light-curve fitting.

The simplest to represent is the value of $t_E$, as it is well constrained and reduces simply to

$$p(y|t_E) \propto \exp \left( -\frac{(t_E - t_{E,\text{best}})^2}{2\sigma_{t_E}^2} \right).$$

(18)

Here $t_{E,\text{best}}$ and $\sigma_{t_E}$ correspond to the values from the best fit of the distribution from the light-curve fitting.

For the case of $\rho_s$, it is not as simple because the constraint is not well approximated as a Gaussian. We introduce the information by the use of $-\Delta \chi^2 = \chi^2 - \chi^2_{\text{min}}$ of each of the light-curve fitting samples. From the lower envelope of these samples, binned in $\rho_s$, we obtain a numerical function

$\Delta \chi^2(\rho_s)$, see Figure 8. The probability of $\rho_s$ is then given by

$$p(y|\rho_s) \propto \exp \left( -\frac{\Delta \chi^2(\rho_s)}{2} \right).$$

(19)

The previous weights are combined as

$$p(y|t_E, \rho_s) \propto p(y|\rho_s)p(y|t_E).$$

(20)

The information of the Galactic model is introduced into Equation (20) by the restriction imposed by the Dirac $\delta$ function in Equation (17).

The combination of the prior and these weights gives the desired posterior probability for the physical parameters, where $\mu_{\Theta,\odot}$ is appropriately obtained from $\zeta$. We note that both outer and inner models lead to the same final results. This is expected given the similarity of the $t_E$ and $\rho_s$ distributions.

5.2. Resulting Properties

The distributions obtained from the Galactic modeling are presented in Figure 9, also contour levels for the distributions of the lens mass $\log_{10}M_*/M_\odot$ and the ratio of the lens and source distance $D_L/D_S$. In addition to the total, the panels show also the separate bulge and disk distributions.

Figure 8. Minimum $\Delta \chi^2$ as a function of $\rho_s$ using the chains derived from the light-curve fitting MCMC. This shows that $\rho_s$ is weakly detected as there is clearly an upper limit for it, but the difference from a flat region on the smaller values is only $\Delta \chi^2 \approx 1.7$.

Figure 9. Posterior probability distributions from the Bayesian analysis for the lens mass $\log_{10}M_*/M_\odot$, the ratio of the lens and source distance $D_L/D_S$, the source distance $D_S$, and $\mu_{\Theta,\odot}$. In addition to the total, the four panels show also the separate bulge and disk distributions, normalized to the total.

Figure 10. Contour levels of 1, 2, and 3$\sigma$ for the distributions of the lens mass $\log_{10}M_*/M_\odot$ and the ratio of the lens and source distance $D_L/D_S$. In addition to the total, the panels show also the separate bulge and disk distributions.
noted above, the outer and inner solutions produce indistinguishable distributions.

From the resulting distributions of the basic four parameters, the lens mass, lens distance, source distance, and proper motion, we can propagate the information to derive the physical mass of the binary lens components and their physical separation. Additionally, the host-mass distribution is essentially identical to the total lens-mass distribution in Figure 9. In this case, the binary-lens mass ratio is small, and the host consists of a low-mass star or brown dwarf with a super-Earth companion. As mentioned previously, given the overlapping of the distributions of \(t_F\) and \(\rho_e\) for the inner and outer solutions, the Bayesian analysis returns indistinguishable distributions, and for these reasons it is justifiable to say that both give the same derived planet mass distribution. This is not the case for the projected separation between host and planet, which has a small but not negligible difference. The derived distributions are shown in Figure 11 and their estimators in Table 8.

Furthermore, as mentioned at the end of Section 3.4.1, the value for \(\rho_e\) is weakly constrained. The relatively broad and highly non-Gaussian form of this constraint is shown in Figure 8. For comparison purposes, in Figure 11, we show alongside the complete Galactic modeling, which includes the information of \(t_F\) and \(\rho_e\), the derived distributions produced by removing the information about \(\rho_e\) and using only \(t_F\). In such a case, the planet mass distribution is shifted a little higher, and the projected separation distributions are a little broader. Their estimators are also included in Table 8.

The inner and outer solutions for the planet in OGLE-2018-BLG-0667 both imply that the secondary lens is a super-Earth/Sub-Neptune planet with a mass of \(M_{\text{planet}} = 3.96^{+5.93}_{-2.60} M_{\oplus}\), while the host is a dwarf star or brown dwarf with a mass of \(M_{\text{host}} = 0.12^{+0.04}_{-0.05} M_{\odot}\). The projected separation between the star and planet is \(0.63^{+0.25}_{-0.23}\) au for the inner and \(0.72^{+0.17}_{-0.15}\) au for the outer solutions, respectively. The lens system is estimated to be at a distance of \(7.58^{+1.35}_{-1.15}\) kpc, with a 66.9% probability of lying in the bulge (Figure 9).

For completeness, we note the physical implications of the solutions corresponding to the two local minima discussed in Section 3.4.2. Since these are degenerate with each other in \(q\), \(t_F\), and \(\rho_e\), they imply the same primary and secondary lens mass and distance. The local minima would imply a total lens mass of \(0.1 M_{\odot}\) and a planet mass of \(6.43 M_{\oplus}\), values very similar to the favored solutions, but a lens located at a distance of \(0.99 D_S\). The projected separation of the planet from its host would be smaller, either \(0.20\) or \(0.22\) au, for the inner and outer local minima respectively.

### 6. Discussion

OGLE-2018-BLG-0677Lb has the lowest \(\Delta \chi^2\) relative to the best 1L1S model of any planet securely detected by microlensing. One of the first microlensing planets, OGLE-2005-BLG-0390 (Beaulieu et al. 2006), also had one of the lowest improvements relative to 1L1S, \(\Delta \chi^2 = 960\). One reason such seemingly high formal thresholds are generally required for secure microlensing planet detections is that “bumps,” particularly those without clear caustic features, can in principle be produced by 1L2S models (Gaudi 1998; Jung et al. 2017; Shin et al. 2019).

In the case of OGLE-2005-BLG-390, the 1L2S model was ruled out by just \(\Delta \chi^2 = 46\). Moreover, Udalski et al. (2018) examined whether OGLE-2005-BLG-390 would have been detectable if the planet-host mass ratio were lower. They concluded that at factors \(q/q < 0.63\) it would not have been because the resulting \(\Delta \chi^2 = \chi^2(1L2S) - \chi^2(2L1S) \leq 13\) would have been too marginal to claim reliable detection of a planet. Note that this threshold for unambiguous identification corresponds to \(\Delta \chi^2 = \chi^2(1L1S) - \chi^2(2L1S) \approx 457\), which is almost 10 times the value for OGLE-2018-BLG-0677.

However, OGLE-2018-BLG-0677 is detected primarily through a dip in the light curve, which cannot be reproduced by any 1L2S scenario, or any other higher-order microlensing effect. The only other possible cause for the observed dip is a systematic error in the photometry. This is extremely unlikely because the signal is detected in the data from two overlapping KMTC fields that were reduced independently, and is confirmed by two data points from the OGLE telescope, located at a different observatory, and with images reduced by different software.

With a relative lens-source proper motion greater than 5 mas yr\(^{-1}\), the separation between lens and source will be sufficient for them to be separately resolved within a decade with the advent of infrared adaptive optics imaging on either present-day or under-construction extremely large telescopes. We have no detection of flux from the blend in the current event, and so we expect that the lens is at least 10 times fainter than the source, \(I_{\text{lens}} > 22\). This implies that to be confident that a non-detection of the lens implies a non-luminous (i.e., brown dwarf) lens, these observations should be carried out after the lens and source have separated by at least 1.5 FWHM, i.e., \(12\ \text{yr}(\lambda/1.6\ \mu\text{m})/(D/10\ \text{m})\) after \(t_0\) (i.e., 2018). Here \(\lambda\) is
The wavelength of the observations and $D$ is the diameter of the mirror.

7. Summary

We have presented an analysis of the microlensing event OGLE-2018-BLG-0677/OGLE-2018-BLG-0680/KMT-2018-BLG-0816.

The light curve of the event exhibits a small dip, soon after peak on an otherwise-smooth Paczyński-like magnification profile. The dip lasts for $\sim 3.5\, \text{hr}$ and is followed by a smaller bump lasting $\sim 1.5\, \text{hr}$. These features are well traced by the KMTNet CTIO observations from two telescope pointings and are confirmed by the OGLE-2018-BLG-0680 light curve.

We have fitted several models to the light curve and obtained their $\chi^2$ and evidence. The light curves for 1L2S and 1L1S models are virtually identical and do not reproduce the anomalous features in the observations.

We also presented the fit for binary lens solutions. These suffer from a two-fold inner–outer(close-wide) degeneracy, but we found that the ratio of masses was similar for both, indicating that the lens is composed of a star plus planet system. Formally, the planet is detected with a $\Delta \chi^2 \approx 46$ and $\Delta \ln \mathcal{Z} = 5$ relative to the single lens models.

Using the binary solutions we performed a Bayesian analysis and found that outer and inner solutions agree with the same distribution for the lens mass, lens distance, and proper motion.

The derived planet mass is $M_{\text{planet}} = 3.96^{+5.88}_{-2.56} M_{\odot}$, one of the lowest yet detected by microlensing. In Figure 12 we use data from the NASA Exoplanet Archive\footnote{https://exoplanetarchive.ipac.caltech.edu} to show the mass and separation of confirmed exoplanets found with different methods such as microlensing, RV, or transits. (An example of how the mass is derived for the latter can be found in Espinoza et al. 2016.)

It can be seen that the planet mass and distance reported in this work are consistent with the lower limit of masses that have been found previously through microlensing, and also consistent with their separation range. This event reinforces the importance of high-cadence microlensing observations, which allow us to detect and characterize anomalies due to low-mass planets.

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**ORCID iDs**

Antonio Herrera-Martín \( \odot \) https://orcid.org/0000-0002-3654-4662

M. D. Albrow \( \odot \) https://orcid.org/0000-0003-3316-4012

Y.-H. Ryu \( \odot \) https://orcid.org/0000-0001-9823-2907

J. C. Yee \( \odot \) https://orcid.org/0000-0001-9481-7123

S.-J. Chung \( \odot \) https://orcid.org/0000-0001-6285-4528

C. Han \( \odot \) https://orcid.org/0000-0002-2641-9964

K.-H. Hwang \( \odot \) https://orcid.org/0000-0002-9241-4117

Y. K. Jung \( \odot \) https://orcid.org/0000-0002-0314-6000

I.-G. Shin \( \odot \) https://orcid.org/0000-0002-4355-9838

Y. Shvartzvald \( \odot \) https://orcid.org/0000-0003-1525-5041

W. Zang \( \odot \) https://orcid.org/0000-0001-6000-3463

D.-J. Kim \( \odot \) https://orcid.org/0000-0001-8263-1006

R. W. Pogge \( \odot \) https://orcid.org/0000-0003-1435-3053

J. Skowron \( \odot \) https://orcid.org/0000-0002-2335-1730

P. Pietrukowicz \( \odot \) https://orcid.org/0000-0002-2339-5899

K. Ulaczyk \( \odot \) https://orcid.org/0000-0001-6364-408X

P. Iwane \( \odot \) https://orcid.org/0000-0002-6212-7221

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**Figure 12.** Masses and orbital radii of confirmed exoplanets detected via different methods. A dashed line indicates where Earth-mass planets would lie. The data for the confirmed exoplanets can be found in the NASA Exoplanet Archive (https://exoplanetarchive.ipac.caltech.edu).
