Geometric projection-based switching policy for multiple energy harvesting transmitters

Hongbin Chen, Fangfang Zhou, Jun Cai, Feng Zhao, and Qian He

Abstract

Transmitter switching can provide resiliency and robustness to a communication system with multiple energy harvesting transmitters. However, excessive transmitter switching will bring heavy control overhead. In this paper, a geometric projection-based transmitter switching policy is proposed for a communication system with multiple energy harvesting transmitters and one receiver, which can reduce the number of switches. The results show that the proposed transmitter switching policy outperforms several heuristic ones.

Index Terms

Rechargeable wireless communications, energy harvesting, transmitter switching.

I. INTRODUCTION

Along with the advancement of wireless communication technologies and energy harvesting devices, energy harvesting communication systems attract great research attention in recent
years [1]–[3]. However, in an energy harvesting communication system, the energy that can be harvested from the environment is unstable and varies over time. Thus, in order to guarantee the quality-of-service requirements, such harvested energy has to be used carefully.

Transmission completion time minimization is an important goal for energy harvesting communication systems. In literature, many transmission scheduling schemes to achieve this goal or the dual goal of throughput maximization under a given deadline have been developed by considering different scenarios, such as point-to-point communication [4], [5], broadcasting [6]–[8], finite battery [9], fading channels [10], multiple access channel [11], parallel broadcast channels [12], two-user Gaussian interference channel [13], time varying channels [14], wireless energy transfer [15], Markovian energy harvesting [16], energy storage losses [17], and packet arrivals during transmission [18]. However, none of these works considered transmitter switching when there are multiple transmitters available.

Transmitter switching has been discussed in an opportunistic relaying scheme [19]. With transmitter switching, resiliency and robustness of a communication system can be improved, especially when a transmitter fails or is not in the best condition. However, excessive transmitter switching will bring heavy switching control overhead and transmission interruption. Therefore, a transmitter switching policy should be designed to reduce the number of switches and switching control overhead.

In our earlier work [20], a transmitter switching policy for a broadcast communication system with energy harvesting transmitters was proposed. It focused on the case of two transmitters and ignored the number of switches. In this letter, a geometric projection-based transmitter switching policy for a communication system with multiple energy harvesting transmitters and one receiver is proposed, towards the goal of reducing the number of switches. First, regarding the transmitters as a whole [20], given the amount of bits to be sent, the transmission completion time is obtained in a deterministic manner [4]. Then, the time-data plane is constructed with the transmission completion time and the amount of bits to be sent. To complete data transmission with less number of switches, transmitter switching should follow the straight line connecting the transmission start point and the transmission completion point. With this criterion at hand, geometric projection is applied to find the suitable transmitter to work. To our knowledge, no transmitter switching policy has been proposed for energy harvesting communication systems. Therefore, the proposed transmitter switching policy is compared with several heuristic ones to
Fig. 1. Communication system with multiple energy harvesting transmitters and one receiver.

show its merit.

II. ENERGY HARVESTING COMMUNICATION SYSTEM MODEL

We consider a communication system consisting of \( M \) energy harvesting transmitters \( TX_1, TX_2, \ldots, TX_M \) and one receiver RX, as shown in Figure 1. Each transmitter has an energy queue while all the transmitters share the same data queue (This kind of communication systems have wide potential applications. Take cellular networks for example: several base stations are deployed in a wild environment where electric power supply is unavailable. They harvest solar energy from the environment. If the data transmission for a user is not completed by a base station, the transmission can be handed over to another base station in order to provide uninterrupted data transmission service). A transmitter switching policy will be designed to choose one of the transmitters to send data at every switching moment. This can be done in a centralized or distributed fashion, which may bring some control overhead. The energies arriving to the transmitters are stochastic and independent of each other. It is assumed that the arriving time of every energy harvesting process obeys Poisson distribution \([21]\) and the amount of harvested energy in the arriving time of every energy harvesting process obeys uniform distribution (Since there is no model available in literature on the distribution of the amount of harvested energy, for explanation purpose, uniform distribution is considered in this paper. However, the proposed switching policy and the analysis procedure hold for other possible distributions). Moreover, the distribution of the amount of harvested energy does not depend on
the distribution of the arriving time of every energy harvesting process. For the \( m \)-th transmitter \( TX_m \), the length of the energy harvesting time slot \( T_{m,n} \) obeys exponential distribution with parameter \( \lambda_m \) and the amount of harvested energy \( E_{m,n} \) obeys uniform distribution in the interval \( (dn_m, up_m) \). Note that these parameters can be the same or different for different transmitters. It is assumed that all data bits have arrived and are ready at the transmitters before the transmission starts [4]. Energies harvested by the transmitters are used for sending the data. It is assumed that the batteries have sufficient capacity and the harvested energy will not overflow. At every moment only one transmitter is sending data. When this transmitter uses up its energy, another transmitter will turn to send data. The switched transmitter may be chosen to work again later. In the following, data transmission will be analyzed from the information-theoretic point of view. It is assumed that transmission is always successful no matter which transmitter works. Moreover, the transmitters will not send duplicated data.

Each transmitter sends data to RX through an additive white Gaussian noise (AWGN) channel with path loss. When \( TX_m \) works, the received signal can be represented by

\[
y_m = h_m x + v_m, \quad m = 1, \ldots, M
\]

where \( x \) is the transmitted signal, \( h_m \) is the path loss between \( TX_m \) and RX, \( v_m \) is an AWGN with zero mean and variance \( \sigma^2_m \). Without loss of generality, we assume that \( \sigma^2_1 = \sigma^2_2 = \cdots = \sigma^2_M = N_0 B_w \), where \( N_0 \) is the noise power spectral density and \( B_w \) is the bandwidth.

Suppose that \( TX_m \) sends data with power \( \bar{P}_m \). Because there is only one transmitter sending data at every time, the channel shown in Figure 1 is actually a point-to-point AWGN channel. Then, the capacity region is

\[
r_m \leq B_w \log_2 \left( 1 + \frac{\bar{P}_m h_m}{N_0 B_w} \right), \quad m = 1, \ldots, M
\]

Following our previous work in [20], we treat the transmitters as a whole. The term “whole transmitter” means that we only care about the amount of bits that has been sent, rather than which transmitter does the transmission. Assuming the arriving time and the amount of harvested energy of every energy harvesting process are known and following the method in [4], within the transmission completion time for a given amount of bits to be sent, we partition the time into slots and calculate the optimal transmission power in each time slot, as shown in Figure 2. Note that each time slot may cover multiple energy harvesting moments and multiple transmitter
switchings. In Figure 2, $T$ is the present time, $t_j$, for $j = 1, 2, 3 \cdots$, is an energy harvesting moment for a transmitter (called an epoch), and $P_j$ is the optimal transmission power of the “whole transmitter” during the time slot $[t_j-1, t_j]$ (Note that $P_j$ is adopted by any transmitter working in this time slot). Following the method in [4], at any given time $T_e$, we can obtain the maximum amount of bits that can be sent, denoted by $B_e$. In turn, if we set the amount of bits to be sent as $B_e$, the time $T_e$ would be the transmission completion time. When the “whole transmitter” works with the optimal transmission power, the transmission completion time reaches its minimum. After the minimum transmission completion time is obtained, we design the transmitter switching policy which intends to reduce the number of switches.

The problem of minimizing the number of switches can be formulated as follows:

$$
\min_{l_{m,u}} \quad f = \frac{\sum_{m=1}^{M} f_m}{l_{m,u}} \\
\text{s.t.} \quad \sum_{m=1}^{M} \sum_{u=1}^{f_m} l_{m,u} = T_e \\
\quad l_{m,u} = \frac{E_{m,u}}{P_{l_{m,u}}}, \quad m = 1, \cdots, M; u = 1, \cdots, f_m \\
\quad B_w \sum_{m=1}^{M} \sum_{u=1}^{f_m} l_{m,u} \log_2 \left(1 + \frac{P_{l_{m,u}} h_m}{N_0 B_w} \right) = B_e. \quad (3)
$$

where $l_{m,u}$ is the length of the time slot for TX$_m$ at the $u$th working with the available energy $E_{m,u}$ and working power $P_{l_{m,u}}$, $f$ is the total number of switches, and $f_m$ is the number of switches for TX$_m$ before the transmission completion time $T_e$. Because the relationship between $f_m$ and $l_{m,u}$ cannot be obtained and $E_{m,u}$ depends on the length of the past working time slots, this optimization problem is very difficult to solve. Therefore, we resort to the geometric projection-based approach to reduce the number of switches.

Fig. 2. Slot-by-slot optimal transmission power of the whole transmitter.
III. GEOMETRIC PROJECTION-BASED TRANSMITTER SWITCHING POLICY

Our goal is to design a switching policy that can reduce the number of switches within the transmission completion time. The geometric projection approach is illustrated in Figure 3. For a given amount of bits to be sent $B_e$ and the corresponding transmission completion time $T_e$, we plot them in a point with label W. The point of the present time $T$ and the amount of sent bits $B$ is plotted with label L. The point of the next switching moment $T + \bar{T}_m$ and the amount of sent bits $B + B_m$ is plotted with label F, where $B_m$ is the amount of sent bits during the interval $[T, T + \bar{T}_m]$.

As we know, a straight line is shortest between two points. Hence, the fastest way to finish sending out $B_e$ bits is making the transmission follow the line LW. To reduce the number of switches, at the next switching moment we will choose the transmitter corresponding to LH, which is the longest projection of LF on LW (the projection is made for every transmitter except for the current working one). When the energy harvesting processes are unknown, to find out the transmitter that corresponds to the longest projection, we have to predict the mean of the working time of the transmitters (to predict LF) and the transmission completion point W in advance. In this case, it is impossible to use the real values of the working time of the transmitters to perform projection. Therefore, it is natural to use the average value instead. When the energy harvesting processes are known, the working time of the transmitters can be directly used and the transmission completion point can be obtained.

The proposed switching policy is summarized as follows. First, the working time of each transmitter is calculated with the available energy and transmission power. Then, the amount of
bits that can be sent within the working time for each transmitter is calculated and the points are plotted in the time-data plane. Finally, geometric projection on LW is done and the transmitter corresponding to the longest projection is chosen as the next working transmitter.

The process of predicting the mean of the working time of the transmitters is described as follows (illustrated in Figure 4). Assuming that in the interval \([0, T]\) TX\(_1\) is working, we need to predict the mean of the working time of TX\(_2\) to TX\(_M\), respectively. Take the prediction process of TX\(_m\) as an example. At the energy harvesting moment \(T_{m,n}\), TX\(_m\) harvests energy \(E_{m,n}\). The length of the time slot between two consecutive energy harvesting moments is \(T_{m,n} = T_{m,n} - T_{m,n-1}\). At the present time \(T\), TX\(_m\) has the amount of left energy \(E_{m}\). The last energy harvesting moment before \(T\) is denoted by \(T_{m,0}\).

Denote the duration from \(T\) until the moment the left energy is used up as the first working time period. Then, we can obtain the length of the first working time period \(T_{m,1}\) as \(T_{m,1} = \frac{E_{m}}{P_{1}}\). During the first working time period, if there is no energy arriving, the working time of TX\(_m\) is \(T_{m,1}\); otherwise, the newly harvested energy \(E_{m,1}\) can be used immediately and the length of the first working time period changes to \(T_{m,2}\).

Let \(ma = T + T_{m,1} - T_{m,0}\). Then, we can get the probability of no energy arriving in the first working time period as

\[
PP_1 = PP(T_{m,1} \geq ma) = e^{-\lambda_{m} ma}
\]  

(4)

When \(T_{m,1} < ma\), \(E_{m,1}\) can be used during the first working time period and TX\(_m\) can work for a longer time \(T_{m,2}\), as \(T_{m,2} = \frac{E_{m} + E_{m,1}}{P_{1}}\). Before the epoch \(T + T_{m,2}\), the probability of no
energy arriving is

\[
PP_2 = PP\left( T_{m,1} < ma, T_{m,1} + T_{m,2} \geq \frac{E_{m,1}}{P_1} + ma \right)
\]

\[
= PP(T_{m,1} < ma)
\times PP(T_{m,1} + T_{m,2} - \frac{E_{m,1}}{P_1} \geq ma)
\]

\[
= (1 - PP_1) \times \tilde{PP}_2
\]

where \( \tilde{PP}_2 = PP(T_{m,1} + T_{m,2} - \frac{E_{m,1}}{P_1} \geq ma) \). And likewise, we can calculate the following probabilities:

\[
T_{m,3} = \frac{E_m + E_{m,1} + E_{m,2}}{P_1}
\]

(6)

\[
PP_3 = PP\left( T_{m,1} < ma, T_{m,1} + T_{m,2} < \frac{E_{m,1}}{P_1} + ma, \right.

\[
T_{m,1} + T_{m,2} + T_{m,3} \geq \frac{E_{m,1} + E_{m,2}}{P_1} + ma \left. \right)
\]

\[
= (1 - PP_1 - PP_2) \times \tilde{PP}_3
\]

\[
\vdots
\]

\[
T_{m,n} = \frac{E_m + E_{m,1} + E_{m,2} + \cdots + E_{m,n-1}}{P_1}
\]

(8)

\[
PP_n = PP(T_{m,1} < ma, T_{m,1} + T_{m,2} < \frac{E_{m,1}}{P_1} + ma, \cdots ,

\[
T_{m,1} + T_{m,2} + \cdots + T_{m,n}
\]

\[
\geq \frac{E_{m,1} + E_{m,2} + \cdots + E_{m,n-1}}{P_1} + ma \left. \right)
\]

\[
= (1 - PP_1 - \cdots - PP_{n-1})
\]

\[
\times PP(T_{m,1} + T_{m,2} + \cdots + T_{m,n}
\]

\[
- \frac{E_{m,1} + E_{m,2} + \cdots + E_{m,n-1}}{P_1} > ma \left. \right)
\]

\[
= (1 - PP_1 - \cdots - PP_{n-1}) \times \tilde{PP}_n
\]

where

\[
\tilde{PP}_n = PP(T_{m,1} + T_{m,2} + \cdots + T_{m,n}
\]

\[
- \frac{E_{m,1} + E_{m,2} + \cdots + E_{m,n-1}}{P_1} > ma \left. \right)
\]

(10)
Next, we will discuss the way to get $\tilde{P}P_n$, in order to obtain the probability of no energy arriving. Let $X = \mathcal{T}_{m,1} + \mathcal{T}_{m,2} + \cdots + \mathcal{T}_{m,n}$, $Y = E_{m,1} + E_{m,2} + \cdots + E_{m,n-1}$. Then, (10) turns into

$$
\tilde{P}P_n = PP\left( X - \frac{Y}{P_1} > ma \right)
$$

(11)

From [22], we can get the probability density function of $X$ and $Y$ as

$$
f_X(x) = \frac{\lambda^m}{(n-1)!} x^{n-1} e^{-x}, \quad x \geq 0
$$

(12)

$$
f_Y(y) = \sum_{k=0}^{n-1} (-1)^k \binom{n-1}{k} \left( C\left( \frac{y - (n-1)dn_m}{up_m - dn_m} - k \right) \right)^{n-2}
$$

$$
\frac{1}{(up_m - dn_m)(n-2)!},
$$

(13)

where

$$
C(y) = \begin{cases} 
0, & \text{if } y < 0 \\
y, & \text{if } y \geq 0 
\end{cases}
$$

Since $X$ and $Y$ are independent, their joint probability density function is

$$
f_{X,Y}(x, y) = f_X(x) f_Y(y)
$$

(14)

We can get $\tilde{P}P_n$ as

$$
\tilde{P}P_n = \int_{ma + \frac{(n-1)dn_m}{P_1}}^{ma + \frac{(n-1)up_m}{P_1}} dx \int_{(n-1)dn_m}^{(x-ma)P_1} f_{X,Y}(x, y) dy
$$

$$
+ \int_{ma + \frac{(n-1)up_m}{P_1}}^{+\infty} dx \int_{(n-1)dn_m}^{(n-1)up_m} f_{X,Y}(x, y) dy
$$

(15)

By substituting (15) into (5), (7), and (9), $PP_2, PP_3, \ldots, PP_n$ are obtained.

With $PP_1, PP_2, \ldots, PP_n$ at hand, we can find out the mean of the working time variables

$$
\mathbb{E}(\mathbb{T}_m) = \mathbb{T}_{m,1} \times PP_1 + \mathbb{T}_{m,2} \times PP_2 + \cdots + \mathbb{T}_{m,n} \times PP_n
$$

(16)
Algorithm 1 The prediction of working time for a transmitter

Initialize: Set \( n = 0 \).

while \(( PP_n \times T_{m,n} = 0 \) or \( PP_n \times T_{m,n} \geq 0.01 \)) do

\( n = n + 1; \)

Calculate \( T_{m,n}, PP_n \).

if \( PP_n \times T_{m,n} < 0.01 \) then

Calculate \( \bar{E}_m \) for TX\(_m\).

end if

end while

\( T_{m,n} \) is a function of \( E_{m,n} \) and \( E_{m,n} \) is random, which makes \( \mathbb{E}(T_m) \) a random variable. We need to seek the mean again. We write the mean of \( \mathbb{E}(T_m) \) as

\[
\mathbb{E}(T_m) = PP_1 \times T_{m,1} + PP_2 \times \left( T_{m,1} + \frac{E_{m,1}}{P_1} \right) + \cdots + PP_n \times \left( T_{m,1} + \frac{E_{m,1} + E_{m,2} + \cdots + E_{m,n}}{P_1} \right)
\]

\[
= T_{m,1} + \frac{PP_2 + 2PP_3 + \cdots + (n-1)PP_n}{P_1} \times \frac{up_m - dn_m}{2}
\]

By substituting \( P_1 \) into (2), the rate \( r_m \) is obtained. After multiplying \( r_m \) with \( \mathbb{T}_m \), the amount of data that can be sent by TX\(_m\) is obtained (denoted by \( B_m \)). Note that the principle of predicting the working time does not alter with the optimal transmission power. The same prediction process can be executed in the other time slots for the “whole transmitter”. For clarity, the above prediction process is shown in Algorithm 1.

To do projection under unknown energy harvesting processes, the prediction of the transmission completion point is also needed. However, it is very complex and is left for future work.

IV. Simulation Results

As the performance of the proposed transmitter switching policy in terms of number of switches cannot be analyzed theoretically, a simulation example is used to illustrate it. There are four transmitters which are denoted by TX\(_1\), TX\(_2\), TX\(_3\), and TX\(_4\). The energy parameters are set as \( \lambda_1 = 1, \lambda_2 = \frac{1}{10}, \lambda_3 = \frac{1}{20}, \lambda_4 = \frac{1}{50}, \) dn\(_1\) = 1 mJ, up\(_1\) = 5 mJ, dn\(_2\) = 20 mJ, up\(_2\) = 24 mJ, dn\(_3\) = 100 mJ, up\(_3\) = 104 mJ, dn\(_4\) = 4 mJ, up\(_4\) = 44 mJ. The amount of data to be sent to the receiver are 6000 bits. The channel parameters are set as follows: bandwidth \( B_w = 1 \) MHz,
the path loss between the four transmitters and the receiver are \( h_1 = -100 \) dB, \( h_2 = -101 \) dB, \( h_3 = -102 \) dB, \( h_4 = -103 \) dB, the noise power spectral density is \( N_0 = 10^{-19} \) W/Hz. The transmission rates can be written as follows:

\[
 r_m = B_w \log_2(1 + \frac{P_j h_m}{N_0 B_w}), \quad m = 1, 2, 3, 4
\]

\[
 r_1 = \log_2(1 + \frac{P_j}{10^{-3}}) \text{ Mbps},
\]

\[
 r_2 = \log_2(1 + \frac{P_j}{10^{-2.9}}) \text{ Mbps},
\]

\[
 r_3 = \log_2(1 + \frac{P_j}{10^{-2.8}}) \text{ Mbps},
\]

\[
 r_4 = \log_2(1 + \frac{P_j}{10^{-2.7}}) \text{ Mbps}
\]

According to the above simulation parameters, we can get the optimal transmission powers of the “whole transmitter” [20] as \( P_1 = 11.2082 \) mW, \( P_2 = 11.4031 \) mW, \( P_3 = 13.7658 \) mW, \( P_4 = 16.3307 \) mW, \( P_5 = 22.8431 \) mW, \( P_6 = 36.9349 \) mW, \( P_7 = 43.9203 \) mW, \( P_8 = 50.8242 \) mW. The epoches are \( t_1 = 1588.7393 \) s, \( t_2 = 1655.3670 \) s, \( t_3 = 1846.6092 \) s, \( t_4 = 1858.2105 \) s, \( t_5 = 1859.2382 \) s, \( t_6 = 1860.5000 \) s, \( t_7 = 1861.9891 \) s, \( t_8 = 1862.0000 \) s. With the optimal transmission power, until the epoch \( t_8 \), 2207 times of energy are harvested and utilized by the system, all the bits are sent to the receiver, and the number of switches is 82.

To show the advantage, the proposed switching policy is compared with several heuristic switching policies:

1) **Left Energy Maximum** (EM) policy: This policy only depends on the amount of left energy \( E_m \) at a switching moment. One can choose the largest \( E_m \) and switch to \( \text{TX}_m \).

2) **Rate Maximum** (RM) policy: As we know, for a given transmission completion time, higher rate means sending a larger amount of bits out. In the same time slot, we have \( r_1 > r_2 > r_3 > r_4 \). So the switching order is \( \text{TX}_1 \) first, \( \text{TX}_2 \) second, \( \text{TX}_3 \) third, and \( \text{TX}_4 \) last.

3) **Bits Maximum** (BM) policy: No matter what the switching policy is, as long as all energies are consumed, the same amount of bits is transmitted. Recall that the amount of bits sent by the \( m \)-th transmitter in the working time is \( B_m \). We pick out the largest \( B_m \) and let \( \text{TX}_m \) work.

4) **Working Time Maximum** (TM) policy: For a given transmission completion time, longer working time leads to a lower number of switches. In this policy, we calculate the working
time of each transmitter, pick out the longest one, and let the corresponding transmitter work.

With the optimal transmission power, the number of switches under the switching policies are shown in Figure 5. From this figure, we can see that the proposed switching policy leads to a lower number of switches than all aforementioned heuristic switching policies. It should be emphasized that the heuristic switching policies follow the line of maximizing one of the system parameters, which are sub-optimal.

Furthermore, we take 500 and 1000 independent runs of the same simulation and get the average number of switches under the switching policies respectively, as shown in Figure 6. This result also indicates that the average number of switches under the proposed switching policy is the least.
V. CONCLUSION

A geometric projection-based transmitter switching policy for a communication system with multiple energy harvesting transmitters and one receiver has been presented, which reduces the number of switches. Transmitter switching is determined by the projection on a line connecting the transmission start point and the transmission completion point in the time-data plane. The proposed switching policy leads to a lower number of switches than several heuristic ones. In this work, we have assumed that the channel states do not vary within the transmission completion time and the channel path losses are known [4]. In the future, the impact of channel path losses will be incorporated in the design of transmitter switching policies.

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