THE ACS LCID PROJECT. IV. DETECTION OF THE RED GIANT BRANCH BUMP IN ISOLATED GALAXIES OF THE LOCAL GROUP\textsuperscript{a}

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ABSTRACT

We report the detection and analysis of the red giant branch (RGB) luminosity function bump in a sample of isolated dwarf galaxies in the Local Group. We have designed a new analysis approach comparing the observed color–magnitude diagrams (CMDs) with theoretical best-fit CMDs derived from precise estimates of the star formation histories of each galaxy. This analysis is based on studying the difference between the $V$ magnitude of the RGB bump and the horizontal branch at the level of the RR Lyrae instability strip ($\Delta V_{\text{HB}}$) and we discuss here a technique for reliably measuring this quantity in complex stellar systems. By using this approach, we find that the difference between the observed and predicted values of $\Delta V_{\text{HB}}$ is $+0.13 \pm 0.14$ mag. This is smaller, by about a factor of 2, than the well-known discrepancy between theory and observation at low metallicity commonly derived for Galactic globular clusters (GCs). This result is confirmed by a comparison between the adopted theoretical framework and empirical estimates of the $\Delta V_{\text{HB}}$ parameter for both a large database of Galactic GCs and for four other dwarf spheroidal galaxies for which this estimate is available in the literature. We also investigate the strength of the RGB bump feature ($R_{\text{bump}}$), and find very good agreement between the observed and theoretically predicted $R_{\text{bump}}$ values. This agreement supports the reliability of the evolutionary lifetimes predicted by theoretical models of the evolution of low-mass stars.

Key words: galaxies: individual (Cetus dSph, Tucana dSph, IC1613 dIrr, Leo A dIrr, LGS 3 dIrr/dSph) – galaxies: stellar content – Local Group – stars: evolution – stars: general

Online-only material: color figures

1. INTRODUCTION

In low-mass stars, the evolution of the H-burning shell along the red giant branch (RGB) involves an extremely small mass ($\approx 0.001 M_\odot$ or less near the RGB Tip). Therefore, its crossing of any discontinuity in the H-abundance profile causes a change in the H-burning efficiency and, in turn, a sudden change in the stellar surface luminosity. During the RGB evolution, the H-burning shell crosses the chemical discontinuity left by the convective envelope after the first dredge-up. When the shell encounters this discontinuity, the matter in the shell expands and cools slightly, causing a sharp drop in the stellar surface luminosity. When thermal equilibrium is restored, the stellar luminosity starts to monotonically increase up to the RGB luminosity. When thermal equilibrium is restored, the stellar luminosity starts to monotonically increase up to the RGB luminosity. When thermal equilibrium is restored, the stellar luminosity starts to monotonically increase up to the RGB luminosity. When thermal equilibrium is restored, the stellar luminosity starts to monotonically increase up to the RGB luminosity. When thermal equilibrium is restored, the stellar luminosity starts to monotonically increase up to the RGB luminosity. When thermal equilibrium is restored, the stellar luminosity starts to monotonically increase up to the RGB luminosity.

Since its detection in 47 Tucanae (King et al. 1985), the RGB bump has become the crossroad of several theoretical and observational investigations (Fusi Pecci et al. 1990; Ferraro et al. 1990; Cassisi & Salaris 1997; Alves & Sarajedini 1999; Zoccali et al. 1999; Bono et al. 2001; Riello et al. 2003; Di Cecco et al. 2010). In order to detect the bump, a large sample of RGB stars is required —$\approx 10^2$ stars in the upper four magnitudes of the RGB according to Fusi Pecci et al. (1990)— and until a few years ago it was detected only in metal-rich globular clusters (GCs). In fact, with increasing cluster metallicity, the luminosity extension of the bump is larger and the bump is also shifted to lower luminosity, where the RGB is more densely populated; both effects work in the direction of making the bump detection easier. However, in the last decade, the RGB bump has been detected in metal-poor GCs, due to the Hubble Space Telescope (HST) capability of imaging the dense GC cores and the availability of wide field-of-view CCD detectors on ground-based telescopes (Riello et al. 2003; see also Di Cecco et al. 2010).

The parameter widely adopted to study the RGB bump brightness is $\Delta V_{\text{HB}} (= V_{\text{bump}} - V_{\text{HB}})$, that is, the $V$ magnitude difference between the RGB bump and the horizontal branch (HB) at the RR Lyrae instability strip level (Fusi Pecci et al. 1990; Cassisi & Salaris 1997). From an observational point of view, this has the advantage of being independent of distance and reddening, but it requires that the instability strip is well populated (Ferraro et al. 1999). From a theoretical point of view, $\Delta V_{\text{HB}}$ depends not only on the bump level predicted by models but also on the HB luminosity set by the value of the He core mass at the He flash. For a detailed discussion of the model uncertainties and the impact on the RGB bump properties, see Cassisi & Salaris (1997), Salaris et al. (2002), and Bjork & Chaboyer (2006).

The first exhaustive comparison between theory and observations of $\Delta V_{\text{HB}}$ in Galactic GCs was performed by Fusi Pecci et al. (1990). Using the theoretical models available at that time,
they found that the observed dependence of $\Delta V_{\text{HB}}^{\text{bump}}$ on cluster metallicity was in good agreement with theoretical predictions, but theoretical $\Delta V_{\text{HB}}^{\text{bump}}$ values were smaller than the observed ones by $\approx 0.4$ mag. For a long time, this result has been considered a clear drawback of canonical theoretical models of low-mass RGB stars. Therefore, it was suggested by Alonzi et al. (1991) that this discrepancy could be removed by accounting for the efficiency of overshooting from the base of the formal boundary of the convective envelope, which shifts the bump level to a lower brightness because of the resulting deeper convective envelope.

Cassisi & Salaris (1997) reanalyzed the problem using their updated canonical stellar models applied to a sample of eight clusters with spectroscopic determinations of $[\text{Fe}/\text{H}]$ and $[\alpha/\text{Fe}]$, accounting for the effect of the $\alpha$-element over-abundance. They concluded that their models provided a good match to the available observational data. Zoccali et al. (1999) and Ferraro et al. (1999) have produced larger observational $\Delta V_{\text{HB}}^{\text{bump}}$ databases and compared these empirical data with suitable stellar models. From this comparison, one can draw the conclusion that lingering uncertainties on the HB theoretical brightness and the GC metallicity scale still leave open the possibility that a discrepancy at the level of $\approx 0.2$ mag between theory and observations may exist. The recent analysis made by Di Cecco et al. (2010) with up-to-date theoretical models seems to support this. For a detailed discussion about the differences between the stellar models adopted by Cassisi & Salaris (1997) and the most recent theoretical framework, see Di Cecco et al. (2010).

All the empirical evidence quoted above refers to RGB bump detections in Galactic GCs. However, there is a growing number of detections of—single and double—RGB bumps in dwarf spheroidal (dSph) satellites of the Milky Way (Scultor: Majewski et al. 1999; Sextans: Bellazzini et al. 2001; Sagittarius: Monaco et al. 2002; Ursa Minor: Bellazzini et al. 2002; Leo II: Bellazzini et al. 2005) while the first detection in an isolated Local Group (LG) galaxy was presented for DDO210 by McConnachie et al. (2006).

It is now well known that dSph galaxies are not simple stellar populations, but rather they are a mix of populations, with different ages and chemical properties. Therefore, it is clear that dSph galaxies are not the best target—when compared with “simple” Galactic GCs—in order to check the capability of the evolutionary framework to reproduce the RGB bump brightness. This notwithstanding, the RGB bump detections in dSph galaxies have been used for constraining properties (e.g., possible differences in age and/or metallicity) of the various stellar populations present in the corresponding stellar systems (see references above).

In the present work, we present a different approach for the analysis of the RGB bump, in particular for dwarf galaxies. Recently, we have carried out a project with the aim of studying a sample of isolated LG dwarf galaxies. A summary of the goals and results of the LCID project (Local Cosmology from Isolated Dwarfs\textsuperscript{6}) can be found in C. Gallart et al. (2010, in preparation). Here, it is worth recalling that the main aim of the LCID project was to derive precise star formation histories (SFHs) over the lifetime of the selected objects, in order to obtain a detailed description of their evolution and to analyze their properties in a cosmological context. This was possible due to the observational capabilities of the Advanced Camera for Survey (ACS) on board the HST for the LG galaxies Cetus, Tucana, Leo A, IC 1613, and LGS 3.\textsuperscript{7} The ACS observations allowed us to obtain color–magnitude diagrams (CMDs) of unprecedented depth and quality for these objects. The analysis of these CMDs allowed us to detect the RGB bump(s) in all five galaxies observed with the ACS.

Preliminary results on this issue have been presented for the Cetus dSph by Monelli et al. (2010a). In the present paper, we extend the analysis and present our approach to compare the observed and theoretical values of $\Delta V_{\text{HB}}^{\text{bump}}$. The essence of our method is to take advantage of the derived SFHs, which provide a reliable description of the ages, chemical properties, and counts of the stars in both the RGB and the HB stages. The SFHs are used to calculate a synthetic CMD, which is then compared with the observed CMD.

The outline of this paper is as follows: in the next section, we discuss the method and provide the relevant data about both the observational and the theoretical framework; in Section 3, we compare theoretical predictions based on the retrieved SFHs with the observational measurements. We close with some discussion and final remarks.

## 2. DATA REDUCTION AND ANALYSIS: THE $\Delta V_{\text{HB}}^{\text{bump}}$ PARAMETER ESTIMATE

We present the analysis of the RGB bump for five of the LCID galaxies: Cetus, Tucana, LGS 3, IC1613, and Leo A. An in-depth discussion of the data reduction and photometry can be found in Monelli et al. (2010a). We note that the photometry was obtained using both the DAOPHOT/ALLFRAME (Stetson 1994) and DOLPHOT (Dolphin 2000) packages. Monelli et al. (2010a) discuss the small zero points detected between the two photometry sets. However, note that the results of this paper, based on the magnitude difference of the RGB bump and the HB, are not affected by such small offsets. The CMDs and SFHs of the five galaxies are presented in a series of papers (Cetus: Monelli et al. 2010a; Tucana: Monelli et al. 2010b; IC1613: E. Skillman et al. 2010, in preparation; LGS 3: S. L. Hidalgo et al. 2010, in preparation; Leo A: Cole et al. 2007). The variable stars, and in particular the RR Lyrae used in this work, have been presented in Bernard et al. (2009, Cetus and Tucana), Bernard et al. (2010, IC 1613), and Bernard et al. (2009, LGS 3, Leo A).

Since galaxies are complex stellar systems with mixtures of stellar populations of different ages and metallicities, we devised a new approach to compare the theoretical and the observed $\Delta V_{\text{HB}}^{\text{bump}}$. In particular, we take advantage of the detailed knowledge of the SFHs of the sample galaxies to build a best-fit model, or best-fit CMD,\textsuperscript{8} which was used to estimate the theoretical $\Delta V_{\text{HB}}^{\text{bump}}$ to be compared with the observed one. We emphasize that the SFHs and the best-fit CMDs adopted in present analysis have been derived using the BaSTI stellar model library (Pietrinferni et al. 2004).

In the following, we outline the details of the method to estimate the $\Delta V_{\text{HB}}^{\text{bump}}$\textsuperscript{7} parameters in the empirical and in the best-fit CMDs, presenting both the HB luminosity level estimates (Section 2.1) and the bump detections (Section 2.2).

Since the data collected for this project have been observed in the ACS F475W and F814W passbands, we define

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\textsuperscript{6} http://www.iac.es/project/LCID

\textsuperscript{7} The Phoenix dwarf is the sixth galaxy in the LCID project, but was observed with the WFC2, and the WFC2 data did not allow a robust detection of the RGB bump. Therefore, this galaxy is not included in the present analysis.

\textsuperscript{8} The best-fit CMD was built using the IAC-star code (Aparicio & Gallart 2004), available at the Web site http://iac-star.iac.es.
$M_{V^*} = (M_{F475W} + M_{F814W})/2$ magnitude, which is adopted for both CMDs.\(^9\) The reason for this choice is twofold: (1) the $M_{V^*}$ magnitude is quite close to the Johnson $V$ band commonly used to study the RGB bump and (2) the $M_{V^*}$ luminosity of the HB is roughly constant as a function of color within the RR Lyrae instability strip (see below).

### 2.1. Estimate of the HB Luminosity

In concordance with other studies, we estimate the HB luminosity at the color corresponding to the RR Lyrae star instability strip ($0.4 < M_{F475W} - M_{F814W} < 0.9$ mag). However, we estimate that the mean magnitude of the HB changes by $\Delta M_{V^*} \approx 0.05$ mag from the bluest to the reddest limit of the instability strip. Therefore, we obtained the HB luminosity in a 0.2 mag wide color bin consistent with the center of the instability strip, centered at $M_{F475W} - M_{F814W} = 0.65$ mag. Note that the change in the HB luminosity is $\leq 0.03$ mag when using the full color range instead of the adopted range which is well within our quoted uncertainties.

In the case of the observed CMD, we cannot estimate the zero-age horizontal branch (ZAHB) by adopting the lower envelope of the observed stellar distribution (as is usually done in the case of Galactic GCs) since the presence of blends, unresolved galaxies, and/or RR Lyrae variables with poorly measured mean magnitudes can affect the estimate of the “real” ZAHB level. Therefore, we have adopted a different approach. By using the synthetic, best fit CMDs, we have verified that the luminosity level at $1.5\sigma$ fainter than the peak magnitude of the HB LF, calculated by means of a Gaussian fit, nicely reproduces the location of the theoretical HB lower envelope for all of the galaxies in our sample; the same method was then used for estimating the ZAHB level in all galaxies.

Figure 1 shows the example of Cetus. The left panel shows a zoom of the CMD, where the thick black line marks the estimated ZAHB. The right panel shows the histogram of the HB stellar magnitudes. The dashed line represents all the HB stars in the color range $0.4 < M_{F475W} - M_{F814W} < 0.9$, while the solid line represents the adopted sub-sample in a restricted color range. Overplotted on this we present the fitted Gaussian profile and the position of the estimated ZAHB, marked by the arrow. The observed HB levels for all the galaxies of our sample are shown in Figure 2, left panels, and summarized in Table 1.

\(^9\) With the usual notation, we will refer to $M_{V^*}$ and $V^*$ for the absolute and apparent magnitude, respectively.
Figure 2. Left panels: the observed CMDs for the five dSph galaxies in our sample. The horizontal line marks the HB luminosity level. Right panels: the observed differential RGB LFs for the galaxies in our sample. In all panels, the horizontal line marks the position of the detected RGB bumps. In the cases of Cetus and Tucana, the different colors refer to a star sample selection, adopted in order to trace in more detail the contribution of the various stellar populations to the global LF (see the text for more details).

(A color version of this figure is available in the online journal.)

Table 2
As Table 1 But for the Values Estimated from the Solution CMDs

| Galaxy  | Age (Gyr) | Metallicity (Z) | \(M_{V}^{\ast, \text{bump}}\) | \(M_{V}^{\ast, \text{HB}}\) | \(\Delta M_{V}^{\ast, \text{bump}}\) | \(R_{\text{bump}}\) |
|---------|-----------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Cetus   | >8        | [0.0003, 0.0006] | -0.55 ± 0.02    | 0.41            | -0.76 ± 0.02    | 0.48 ± 0.03     |
| IC1613  | >8        | [0.0006, 0.0010] | -0.15 ± 0.02    | 0.43            | -0.58 ± 0.02    | 0.55 ± 0.06     |
| IC1613  | >5        | [0.0006, 0.0012] | -0.19 ± 0.02    | 0.43            | -0.62 ± 0.02    | 0.48 ± 0.03     |
| LGS3    | >5        | [0.0012, 0.0020] | -0.12 ± 0.02    | 0.45            | -0.57 ± 0.02    | 0.54 ± 0.04     |
| Tucana  | >8        | [0.0001, 0.0005] | -0.31 ± 0.02    | 0.42            | -0.72 ± 0.02    | 0.44 ± 0.02     |
| Tucana  | >8        | [0.0005, 0.0010] | -0.12 ± 0.02    | 0.45            | -0.57 ± 0.02    | 0.42 ± 0.02     |

Notes. For each galaxy, we also list the metallicity and age range of the stellar populations mostly contributing to the RGB bump feature.

Table 2 summarizes the derived quantities for the best-fit CMDs: the estimated luminosity of the HB and RGB bump, and the calculated \(\Delta M_{V}^{\ast, \text{bump}}\), together with the adopted age and metallicity ranges. The error associated with the RGB bump brightness has been estimated as half of the width of the magnitude bin of the RGB LF.

We wish to emphasize that, since in retrieving the SFH we have not taken into account the RGB and HB stages...
The presence of a double bump has direct connections with the SFH of Tucana. Two of the main results of the LCID project concerning this galaxy are as follows.

1. Tucana experienced a strong initial burst of star formation, at the oldest possible ages (>12.5 Gyr ago, implying a substantial population of metal-poor stars), and followed by a steady decrease until reaching a complete termination roughly 8 Gyr ago (Monelli et al. 2010b).

2. Tucana hosts two distinct populations of RR Lyrae variable stars, characterized by different luminosity, pulsational properties, and radial distributions (Bernard et al. 2008).

These two findings suggest that the Tucana dSph was able to form two different generations of stars with different chemical properties in a very short time interval early on, so both populations are old enough to produce RR Lyrae. Therefore, there is a good qualitative agreement between these results and the independent detection of two RGB bumps, which can be interpreted using the LF of the best-fit CMD. In fact, the latter also possesses a similar double peak (Figure 3(d)). Interestingly, the two peaks are associated with two populations

(3) Notes on Individual Galaxies

TUCANA. A visual inspection of the observed CMD reveals the presence of two clear overdensities along the RGB: the brightest is located on the blue edge of the RGB, while the faintest is on the red edge. To further investigate the possible occurrence of two distinct bumps in Tucana, we calculated the LF of both the red and the blue portions of the RGB, as shown in panel (i) of Figure 2. The corresponding histograms (in color in panel (j)), shown together with the global LF (solid black line), support the detection of two distinct RGB bumps in Tucana, separated by 0.27 ± 0.06 mag.

Figure 3. Four panels show the histograms of the RGB stars of the best-fit CMDs for the four galaxies. The black lines represent the global histogram, while the lines in color show the histogram of the sub-populations with labeled ages and metallicity. With this approach we were able to constrain which population is the main contributor to the RGB bump. Note that the metallicity ranges change from one galaxy to another, due to the different details of the individual SFHs.

(A color version of this figure is available in the online journal.)
of different metallicity: the brighter population is made of stars with metallicity in the most metal-poor range, 0.0001 < Z < 0.0005, while the fainter population consists of stars in the range 0.0005 < Z < 0.001. The magnitude difference between these two features, 0.19 ± 0.06 mag, is in good agreement with the magnitude difference of the observed bumps, 0.27 ± 0.06 mag. Moreover, we verified that, as expected, the most metal-poor stars populate the blue side of the RGB, while the more metal rich are located on the red side. Therefore, as for the observed bump, the brightest bump is also the bluest, and the faintest is also the reddest. Another interesting aspect is that the two Tucana bumps are the narrowest among the LFs of the five galaxies, with estimated dispersions of σ = 0.04 ± 0.01 mag and 0.06 ± 0.01 mag for the faintest and the brightest, respectively. This is possibly linked to the intrinsic short duration of the bursts of star formation (Monelli et al. 2010b).

**CETUS.** The RGB bump of Cetus is also very prominent, as shown in Figure 2(a). Interestingly, the position of the bump is similar to the faintest bump detected in Tucana, and both are located on the red edge of the RGB. The bump clearly stands out in the observed LF as well (Figure 2(b)). The analysis of the red and the blue portion of the RGB (red and blue lines) shows that the global peak (solid black line) seems to be the result of the superposition of two different features. The main narrow peak is populated by stars on the red side of the RGB, while the bluer portion mostly contributes to broadening it. The width of the main peak, 0.06 ± 0.01 mag, is slightly larger than the corresponding faint bump in Tucana.

The comparison of the SFHs of Cetus and Tucana, presented in Monelli et al. (2010b), shows that Cetus did not experience an initial burst as strong or as early as in Tucana. In particular, Monelli et al. found that the main star formation peak is ~1 Gyr younger in Cetus than in Tucana. These differences, and the smoother SFH of Cetus, plausibly explain both the absence of a second brighter bump in Cetus, and the rather homogeneous properties of the RR Lyrae stars, which do not show any clear dichotomy, as in the case of Tucana (Bernard et al. 2009).

The theoretical LF (Figure 3, panel (a)), shows quite a broad peak, formed by the contribution of two populations, in the ranges 0.0004 < Z < 0.0007 and 0.0007 < Z < 0.001. The LF of the most metal-poor stars does not show any clear feature.

**IC 1613.** The bump region in the LF of IC 1613 is the widest among our sample (σ = 0.15 ± 0.02 mag). This can be explained by the extended SFH of this galaxy, which was continuous from the oldest epoch to the present time. There are hints of the presence of two peaks, separated by ≈0.12 mag. The theoretical LF (Figure 3(d)) shows that two populations are contributing to the main peak, in a wide range of metallicities. The corresponding peaks are separated by ≈0.07 mag.

**LEO A.** This galaxy has the most unusual SFH in our sample. Cole et al. (2007) found very low level of star formation starting ≈13 Gyr ago, in agreement with the small number of RR Lyrae stars detected (eight by Dolphin et al. 2002 and 10 by Bernard 2009). Cole et al. (2007) further found that 90% of all star formation occurred in the last 8 Gyr, resulting in the only galaxy in the LCID sample with a dominant intermediate-age population. As a result, the HB inside and to the blue of the instability strip is very scarcely populated by old stars. Moreover, the time sampling in our ACS observations was poor and not adequate to accurately estimate the periods, and therefore the mean magnitudes, of the RR Lyrae stars. For these reasons, Leo A is not included in our analysis.

Figure 4. Difference between the ΔV∗ HB parameter as estimated from the observed CMDs and the synthetic ones (see the text for more details). In the cases in which a double RGB bump has been observationally detected, the full square points correspond to the fainter RGB bump detection. In the case of Cetus, since the model fits two distinct RGB bumps, we show the magnitude difference with respect to the observational detection for both the theoretical RGB bumps. The dashed horizontal line represents the mean value of the difference, while the standard deviation with respect to the mean is labeled.

3. COMPARISON BETWEEN THEORY AND OBSERVATIONS

In the previous section, we have discussed our approach to attribute the contributions of the various sub-populations present in the galaxy to the RGB bump feature(s) in the global LF. When a double RGB bump is present in the empirical CMD, we checked the theoretical LF to determine which stellar components are responsible for the observed feature.

Since the HB luminosity level is strongly dependent on the metallicity, comparing theoretical predictions and observations of ΔV∗ HB in stellar systems with mixed stellar populations with different metallicities could be liable to uncertainties. However, by using our best-fit CMDs, we have tested that the more metal-rich populations are either too metal rich to populate the RR Lyrae instability strip, or that the difference in the HB luminosity level (the lower envelope of the two distributions within the instability strip) with respect to the lower metallicity stellar population contributing to the RGB bump feature(s) is of the order of 0.02–0.03 mag, therefore within the error bars of our estimate from the observed CMD. Thus, when estimating the empirical ΔV∗ HB, we have adopted for all galaxies the magnitude corresponding to the lower envelope of the HB distribution (estimated as detailed above).

In Figure 4, we show the V∗ magnitude difference between the ΔV∗ HB parameter as estimated from the observed and the synthetic CMDs. The error on this difference has been obtained by summing in quadrature the errors on the observational and theoretical estimates. Note that the average difference is ~ + 0.13 ± 0.14 mag. This result appears in qualitative agreement with the one obtained by comparing theory with observations of Galactic GCs concerning the ΔV∗ HB parameter: the observed magnitude difference between the RGB bump and the HB appears lower than expected on theoretical grounds. Nevertheless, the difference estimated for our sample of dwarf galaxies appears significantly less than that obtained for Galactic GCs.
In order to allow a more direct analysis of how present results compare with those obtained for galactic GCs, we show in Figure 5 the comparison between theory and observations in the \( \Delta V_{\text{HB}} \) —metallicity diagram, for a large sample of Galatic GCs investigated by Di Cecco et al. (2010), for a selected sample of LG dwarfs for which \( \Delta V_{\text{HB}} \) estimates are available in the literature (see data in Table 3), and for the LCID dwarf sample. In the latter case, the comparison between theory and observations has been performed by using the \( \Delta V_{\text{HB}} \) parameter, after transferring the model predictions into this observational plane.

We note that the adopted theoretical framework is the one provided by Pietrinferni et al. (2004), i.e., the same adopted by Di Cecco et al. (2010), and by our group in the framework of the LCID project for retrieving the SFHs of the selected dwarfs. For the galaxies in our sample, we adopt the metallicity distribution determined from the SFH analyses. That is, we have chosen the metallicity value corresponding to the average of the metallicity range of the stellar populations contributing to the RGB bump in the best-fit CMD (see the discussion in Section 2.2 and data in Table 2) and a spread equal to the half width of the same interval.

Since detailed SFH analysis, similar to those for our LCID sample, does not exist for the LG dwarfs selected from the literature, we are not able to properly characterize the particular stellar population(s) contributing to the RGB bump. Thus, we compare theoretical predictions with the measured \( \Delta V_{\text{HB}} \) by using the literature data at their face value. Table 3 summarizes the \( \Delta V_{\text{HB}} \) values from the original papers, the adopted metallicities, and the related references. In particular, the metallicity values have been taken, when available, from the most recent spectroscopic measurements, or from the comparison with fiducial RGB loci of selected Galactic GCs. We wish to note that the adopted empirical estimates for the \( \Delta V_{\text{HB}} \) parameter are not fully self-consistent due to the differences in the adopted procedure for estimating the HB luminosity level and/or the approach used for estimating the average metallicity of the stellar population to which the \( \Delta V_{\text{HB}} \) parameter is associated. Nevertheless, it is worth noting that this is, so far, the largest data set ever collected for the \( \Delta V_{\text{HB}} \) parameter of LG dwarf galaxies.

The comparison between the theoretical predictions and the empirical \( \Delta V_{\text{HB}} \) (or \( \Delta V_{\text{HB}}^{*} \)) estimates show that, despite the quoted limitations of the observational data for the dSph galaxies, a better agreement exists with the theoretical predictions in the metallicity range explored with respect to the similar comparisons for Galactic GCs.

To further investigate the level of agreement between theory and observations for the various samples of objects, we have computed for each object the difference between the empirical estimate of the \( \Delta V_{\text{HB}} \) parameter and the corresponding theoretical prediction for a mean age of 12.8 Gyr and the metallicity appropriate for the object under scrutiny. These differences are plotted in Figure 6. This figure shows that for the

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**Table 3**

| Galaxy          | \( \Delta V_{\text{HB}} \) Parameter | [M/H] |
|-----------------|--------------------------------------|-------|
| Sculptor        | \(-0.90 \pm 0.21^a\)                | \(-2.0 \pm 0.2^b\) |
| Sculptor        | \(-0.35 \pm 0.21^a\)                | \(-1.30 \pm 0.15^b\) |
| Ursa Minor      | \(-0.62 \pm 0.11^c\)                | \(-1.7 \pm 0.2^c\) |
| Sagittarius     | \(0.22 \pm 0.10^d\)                 | \(-0.45 \pm 0.15^e\) |
| Sextans         | \(-0.45 \pm 0.06^f\)                | \(-1.63 \pm 0.20^f\) |

Notes.

- \(^a\) Majewski et al. (1999).
- \(^b\) Kirby et al. (2009).
- \(^c\) Bellazzini et al. (2002).
- \(^d\) Monaco et al. (2002).
- \(^e\) Lee et al. (2003).
- \(^f\) Lee et al. (2009).
more metal-poor GCs there is a mean difference with respect to the theoretical predictions of about 0.24 ± 0.16 mag. For the more metal-rich GCs and for the dwarf galaxies this average difference decreases to 0.08 and 0.02 mag, respectively, with a standard deviation of 0.09 and 0.11 mag, respectively. In addition, note that for the dwarfs there is no evident trend with the metallicity. These results support the conclusions based on the data in Figure 4, and seem to point toward the presence of an age spread in the stellar population, and the impact of the existence of a metallicity spread has been discussed—at least in the case of our sample of galaxies—in Section 2.1. This analysis confirms that the complexity of the SFH—at least in the case of our dwarfs galaxies—does not hamper the possibility of a meaningful comparison between theory and observations. However, one has to bear in mind that, in the case of a more complex, or peculiar, SFH, this result might not be valid; therefore it is important to investigate in detail each individual case.

For our purpose, it is enough to remark that the existence of a better agreement between theory and observations with respect to Galactic GCs cannot be an artifact due to complex stellar populations. In order to understand the causes of the discrepancy existing for Galactic GCs, a detailed analysis of the possible observational biases (uncertainties) is mandatory, but this is beyond the scope of the present work.

3.1. The $R_{\text{bump}}$ Parameter

In the previous section, we have investigated the level of agreement between the observational measurements of the RGB bump brightness in our sample of dwarf galaxies and the theoretical predictions as obtained both by synthetic CMDs, reproducing the complex SFH of these galaxies, and by stellar models covering a range of age and metallicity. However, there is another important piece of information that can be retrieved from the RGB in the observed CMDs, i.e., the star counts. It is well known (for a review see Salaris et al. 2002, and references therein) that an appropriate comparison between the empirical and theoretical RGB LFs is one of the best tools for checking the capability of stellar models to predict the evolutionary lifetimes along this important evolutionary stage.

In particular, Bono et al. (2001) defined a new observable, the $R_{\text{bump}}$, parameter, defined as the ratio between the star counts across the RGB bump and in a region located at a fainter magnitude along the RGB. They used this new parameter for investigating the occurrence of non-canonical deep mixing during the RGB bump stage (see Weiss et al. 2000) in a large sample of Galactic GCs. As a result of their analysis, they found a very good agreement—with very few exceptions—between theory and observations.

Due to the evident complexity of the SFH in dwarf galaxies with respect of Galactic GCs, our CMDs are not the best tool for investigating the occurrence of deep mixing in RGB stars. This notwithstanding, we have decided to measure the $R_{\text{bump}}$ in our empirical CMDs and compare these measurements with the corresponding ones provided by the accurate best-fit synthetic CMDs. This comparison allows us to check if the predicted star counts along the RGB are in agreement with the empirical data. In this context, we wish to emphasize again that, when obtaining the best-fit synthetic CMD for each galaxy in our sample, we have not imposed any constraints on this evolutionary stage.

As far as it concerns the method for measuring the $R_{\text{bump}}$ parameter, we have adopted the same method outlined by Bono et al. (2001). The values measured in the empirical and synthetic CMDs are provided with the corresponding 1σ errors in Tables 1 and 2. In Figure 7, we plot the differences between the observed value(s) of $R_{\text{bump}}$ in each dwarf in our sample and the theoretical value(s) as estimated from the theoretical predictions as obtained both by synthetic CMDs, reproducing the complex SFH of these galaxies, and by stellar models covering a range of age and metallicity. However, there is another important piece of information that can be retrieved from the RGB in the observed CMDs, i.e., the star counts. It is well known (for a review see Salaris et al. 2002, and references therein) that an appropriate comparison between the empirical and theoretical RGB LFs is one of the best tools for checking the capability of stellar models to predict the evolutionary lifetimes along this important evolutionary stage.

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We show the theoretical data, we measured the \( \Delta \) of stellar systems. In order to perform a direct comparison with five isolated dwarf galaxies in the LG. This analysis allowed correct predictions of stellar lifetimes along the RGB stage. as well as of the evolutionary theoretical framework of providing capability of retrieving the SFH of these complex stellar systems.

The mean difference is equal in Figure 4, since the best-fit model for Cetus shows two distinct RGB bumps, the dashed horizontal line represents the mean difference of the observed and predicted brightness of the RGB bump seen predictions reveals that the well-known discrepancy between theory and observation: the mean difference is equal to \( \sim -0.02 \pm 0.05 \). This result provides further evidence of the capability of retrieving the SFH of these complex stellar systems as well as of the evolutionary theoretical framework of providing correct predictions of stellar lifetimes along the RGB stage.

4. SUMMARY AND CONCLUSIONS

We have presented a homogeneous analysis of the RGB for five isolated dwarf galaxies in the LG. This analysis allowed us to obtain the first detection of the RGB LF bump in these stellar systems. In order to perform a direct comparison with theoretical data, we measured the \( \Delta \) parameter in four galaxies in our sample.

We have designed and implemented a new approach to estimate this parameter, based on comparing an observed CMD with a theoretically calculated CMD. This method takes advantage of the detailed knowledge of the stellar content of the sample galaxies, in terms of age, metallicities, and star counts, to identify which sub-population is actually contributing to form the RGB bump. This is a fundamental advantage when working with complex stellar populations.

The comparison between the observations and the theoretical predictions reveals that the well-known discrepancy between the observed and predicted brightness of the RGB bump seen in Galactic GCs is smaller, by more than a factor of 2 in our dSph sample. This effect is supported by the inclusion of four additional dSph galaxies, for which the \( \Delta \) parameter values are available in the literature.

It may be somewhat surprising that the level of agreement between theory and observations is better for complex stellar populations (dSph galaxies) than for simple stellar populations (Galactic GCs). However, although the complex nature of the stellar population could represent a drawback for clearly detecting the observational features and reliably identifying the stellar component responsible for the observed feature—and in this context our approach is a big advantage—the statistical significance of the stellar samples is quite larger. In the case of our sample of dwarf galaxies, we have investigated if the complexity of the SFH can affect our estimates of the \( \Delta \) parameter in the empirical CMDs. As a result, we have found that—at least for our sample of dSph—the measurement of the \( \Delta \) parameter is not significantly affected by the mix of sub-populations in the host galaxy.

Our analysis has also shown the existence of a very good agreement between observations and theoretical predictions concerning the \( \Delta \) parameter. This agreement represents supporting evidence that the adopted theoretical framework is providing accurate estimates of stellar evolutionary lifetimes.

The present analysis also emphasizes the importance of combining the detection and characterization of the RGB bump(s), with other information concerning the properties of the stellar populations hosted by a galaxy. In this context, it is particularly important to note the case of the Tucana dSph; the detection of a double bump can be correlated both with the properties of the RR Lyrae stars and the SFH of this galaxy, supporting the coexistence of two old stellar populations, with slightly different metallicities, formed during an initial strong episode of star formation. This provides support for the use of the RGB bump as a stellar population indicator for CMDs which do not reach the oldest main sequence turn-off.

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Figure 7. Difference between the \( \Delta \) parameter as estimated from the observed CMDs and the synthetic ones (see the text for more details). As in Figure 4, since the best-fit model for Cetus shows two distinct RGB bumps, we show the \( \Delta \) difference with respect to the observational detection for both the theoretical RGB bumps. The dashed horizontal line represents the mean of the difference, while the standard deviation with respect to the mean is labeled.
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