Plasma evolution in laser-irradiated hollow microcylinders

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Hollow microcylinder targets, 200–300 μm in diameter, have been internally irradiated at up to 5 \cdot 10^{14} \text{ W/cm}^2 with Nd:glass laser pulses directed through an axial entrance slit. The plasma evolution in the interior of the cavities was diagnosed with a pinhole imaging X-ray streak camera and a Nomarski-type interferometer. Plasma collision near the center of the cylinder is observed about 300 ps after the irradiating laser pulse. The experimental results are confirmed by a one-dimensional Eulerian fluid code.

1. Introduction

In recent years, high-temperature, short-pulse laser-produced plasmas have attracted considerable interest as possible gain media in soft X-ray laser experiments. Experimental evidence for XUV amplification was reported in plasmas generated from coated fibers (Jacoby et al. 1982), exploding foils (Matthews et al. 1985; Seely et al. 1985), and solid targets (Jaegle et al. 1986; Suckewer et al. 1985). Essentially, these schemes rely on free plasma expansion into vacuum, so that the resulting electron density profiles are convex, i.e., with the density maximum along the axis. Since in a plasma the refractive index (due to free electrons) is given by $n = (1 - n_e/n_{ec})^{1/2}$, where $n_{ec}$ is the critical electron density, refraction in a convex density profile may result in steering the X-ray laser beam out of the region of high gain (London 1988). As a consequence, the attainment of gain-length products required for saturation is prevented. Methods to avoid this difficulty have been proposed by various authors and include alternating the plasma expansion in opposite directions by oppositely focused laser beams (Hagelstein 1983), bending the target to form a curved surface along the soft X-ray laser propagation direction (Lunney 1986), and confining the expanding plasma between two planar foils (Rosen & Hagelstein 1986) or by means of an external magnetic field (Suckewer et al. 1985).

A novel scheme for the attainment of high electron densities and a concave wave-guiding density profile has been pursued at this laboratory (Balmer & Weber 1988; Cunningham et al. 1988, Weber et al. 1988). As illustrated in figure 1a, plasma inside a hollow microcylinder is produced by introducing a line focussed laser beam through an elongated aperture (slit) in the cavity wall. A primary plasma is then produced on the wall opposite the entrance slit. The remainder of the cavity's interior is subsequently exposed to laser light reflected at the primary spot, and to x-radiation and hot electrons emitted by the primary plasma. “Indirect” plasma generation thus occurs on the whole interior of the cavity, as shown schematically in figure 1b. The time scale of this process is determined by the diameter of the cavity, the speed of light and/or the velocity of the hot electrons. For the
parameters of interest in these experiments (200–300 μm inner diameter, 0.5–1 keV electron temperature), indirect plasma generation turns out to be instantaneous with respect to typical plasma expansion times. As a result, a radially symmetric flow of plasma converges towards the center. Since the material ablated from the wall is confined within the cavity, substantially higher densities and thus higher gains can be expected from such a target compared with the “open” geometries used to date. Also, in contrast to the planar foil configuration (Rosen & Hagelstein 1986), plasma confinement is cylindrically symmetric and true waveguiding is possible.

2. Experimental arrangement

The efficiency of indirect plasma generation and the subsequent plasma flow was experimentally tested by irradiating 200 and 300 μm diameter tubes fabricated from a range of metals like Al, Cu, Mo, and Au. The tubes are 1–2 mm in length and equipped with a ~100 μm wide entrance slit on one side, through which the Nd:glass laser beam can be focussed. The nominally 2–4 J, 80 ps pulses at 1054 nm produced an irradiance of ~5 \times 10^{14} \text{ W/cm}^2 on the opposite wall. The entrance slit width of ~100 μm was chosen to fit the 80 μm focal spot diameter (1/e^2-value) of the aspheric f/2 lens. In the case of irradiation with 500 μm long line focus, a cylindrical lens of focal length ~300 mm was inserted between the spherical lens and the target.

The plasma evolution within the cylinders was studied by means of a Nomarski-type interferometer (Benattar et al. 1979). A 527 nm probe beam was generated by frequency doubling a fraction of the 1054 nm main laser pulse in a type II KDP crystal. This allowed the 2ω critical density contour (4 \times 10^{21} \text{ cm}^{-3}) and the steepness of the density gradient to be diagnosed on a shot-by-shot basis. The time of arrival of the 2ω probe pulse with respect to the main laser pulse could be adjusted by means of a variable length optical delay line. More details on the experimental arrangement can be found in Cunningham et al. (1988).

The X-ray emission from the microcylinders was recorded by means of a time-integrating X-ray pinhole camera equipped with four pinholes having diameters of 20, 27, 45, and 55 μm, respectively. A 12.5 μm thick Be foil limited the observed spectrum to the region above ~1 keV. The temporal behavior of the 1 keV X-ray emission was diagnosed by means of a pinhole imaging X-ray streak camera with a temporal resolution of ~25 ps.
The details of the experimental conditions are given in Weber et al. (1988). High resolution X-ray spectra were recorded with a space-resolving miniature spectrometer equipped with a PET crystal. This covered the aluminum K-shell wavelength range between about 5 and 8 Å. The spectra were recorded on Kodak DEF film. For observations along the cylinder axis the streak camera and spectrometer had to be used alternately.

3. Experimental results and discussion

Figure 2 shows typical interferograms from a shot-by-shot temporal sequence of irradiated Cu cylinders. Two images are seen on each photograph, one for each polarization of the probe beam. Figure 2a is an interferogram of a cylinder before irradiation. Each cylinder was first photographed in this way as a reference for the measurement of the various plasma movements. Figures 2b–2d show the plasma evolution at times 50 ps, 100 ps, and 200 ps, respectively, after the peak of the laser pulse.

Figure 2. Interferograms of (a) un-irradiated Cu cylinder, (b), (c), and (d) irradiated Cu cylinders, probed at \( \tau = 50 \) ps, 100 ps, and 200 ps, respectively, after the peak of the laser pulse.
100 ps, and 200 ps after the peak of the laser pulse, respectively. Plasma is seen to grow primarily from three areas on the inside of the cylinders: the directly irradiated region and two regions opposite, on either side of the slit. It is interesting to note from figures 2a and 2b that in the early phase of plasma expansion the fringes within the cylinder remain virtually unperturbed. We regard this as evidence of the very steep electron density profile produced by the short duration laser pulse. The details at later times ($\tau \geq 100$ ps) are not resolved well, but some perturbation of fringes at the center of the cylinders is observed.
The cylinder's outer surface close to the slit is also seen to grow in a direction towards the main laser. This is consistent with on-axis time-integrating X-ray pinhole pictures shown in figure 3 which reveals that not all the laser light is focussed through the slit. It can be seen from the interferograms that the entrance slit is closed by plasma shortly after the end of the laser pulse, thus confining the plasma inside.

The position of the inwardly moving dark zones of both the primary plasma (at the back wall) and the secondary plasma (inside the slit) was measured at sequentially increasing times. Constant velocities of $2.7 \cdot 10^7$ and $1.5 \cdot 10^7$ cm/s, respectively, were calculated, giving a ratio of $Q \approx 1.7$. If one assumes that the plasma sound speed, $c_s$, scales with $T_e$ as $c_s \propto (Z/T_e/A)^{1/2}$, where $Z$ is the ionic charge and $A$ the atomic mass, then the ratio measured above leads to an estimate of the ratio of primary to secondary plasma electron temperatures of $T_{ep}/T_{es} = 2.9$.

A simple ray tracing routine was used to estimate the distribution of the irradiating laser light within the cylinders. The geometric rays passing through the main beam waist (located at the entrance slit) are specularly reflected off the back wall and irradiate a corresponding (larger) area on the inside front wall. Results of a ray tracing calculation and the subsequent plasma generation are shown in figure 4 for the case of f/2 focussing optics. It is clearly seen that the distribution of the laser light after a single reflection at the primary spot exactly reproduces the areas of plasma ablation observed in the interferograms. This implies that reflected laser light is the dominating mechanism for indirect plasma generation under the conditions of our experiment (short pulses, long wavelength laser). A substantial fraction of 1054 nm incident laser light has been shown to be reflected under similar irradiation conditions (Garban-Labaune et al. 1982). Taking a plasma reflectivity value of 0.65, the ray tracing calculation gives an irradiance ratio $I_p/I_s \approx 4.5$, where $I_p$ and $I_s$ are the laser irradiances at the primary and secondary plasmas, respectively. If one assumes that the plasma electron temperature, $T_e$, scales with irradiance, $I$, as $T_e \propto (Z \cdot I)^{2/5}$ (Mora 1982), then the expected ratio of plasma velocities becomes $Q \approx 1.4$. 

**Figure 3.** (c) Al (300/100).
This is in reasonable agreement with the measured value of 1.7, if the relatively large error bar (~30%) in the evaluation of the interferograms is taken into account.

Figure 3 shows the pinhole photographs of the X-ray emission zones from targets made of Al, Mo, and Au irradiated with 200 ps/527 nm pulses at ~5·10¹³ W/cm². A f/4 focussing lens was used in these experiments. In each case, in addition to the main plasma emission region, a second, more weakly emitting zone is observed within the original aperture of the cavity (indicated by the dashed line). Due to the time-integrating effect of the simple pinhole camera used, the possibility cannot be entirely ruled out, here, that this secondary emission is produced late in time, i.e., by impact of the expanding main plasma on the cavity wall. However, the fact that in all the photographs the secondary emission zone is detached from the cavity wall seems to favor the interpretation that this emission belongs to the region of plasma collision. This will be confirmed below by the time-resolved pinhole photography. Additional X-ray emitting regions are also observed on the outside of the entrance slit on some of the photographs, indicating that focussing and alignment as well as the size of the slit widths were not optimized in these shots.

The radial position, r, of the centroids of the second emission zones was used to infer values for the temperature ratios, Tₑₚ/Tₑₛ, of the primary and secondary (indirectly generated) plasmas, respectively, using \( \left( \frac{cₛₚ}{cₛₛ} \right) = \left( \frac{(R + r)}{(R - r)} \right) \), where R denotes the initial radius of the cylinder. The temperature of the main plasma was found to exceed the temperature of the secondary plasma by a factor of ~2.5 in the case of Al (figure 3c) up to ~9 for Au (figure 3a). This confirms that reflected laser light is the dominant mechanism for the indirect plasma ablation, because if X rays were responsible for this process, the scaling with target Z should be exactly opposite.

Figure 5 shows the streak camera recording of the X-ray emission of a 300 μm aluminum cylinder irradiated at ~5·10¹⁴ W/cm² in 80 ps/1054 nm pulses. The picture was taken from the Polaroid negative, because more details can be seen in it than on the print. Due to solarization, strongly exposed regions appear dark again, so that quantitative analysis is not possible. In the figure, vertical direction indicates position, horizontal direction the time; zero time corresponds to the peak of the irradiating laser pulse. It is seen that, at time zero, two bright spots appear, representing the primary plasma (on top) and the plasma on the outside of the entrance slit (below). We note that no emission from the region just inside the slit is observed; this is a consequence of the low irradiance at which the secondary plasma is produced. The primary plasma is then seen to flow radially inwards until after about 300 ps, the collision with the secondary plasma (invisible up to...
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Figure 5. Streaked X-ray pinhole image of a 300 μm Al cylinder irradiated at $5 \cdot 10^{14}$ W/cm$^2$ (80 ps/1054 nm). Contours at the left show the orientation of the cylinder.

This point results in a pileup of plasma near the cylinder axis, where expansion energy is dissipated into thermal energy. This manifests itself by enhanced X-ray emission. The duration of this emission (almost one nanosecond) is very long compared to the laser pulse duration, implying that the plasma conditions are varying very slowly during this phase. Enhanced X-ray emission is also observed in the entrance slit region after ~600 ps. We interpret this as some fraction of the primary plasma having penetrated the first region of collision (with plasma ablated from the inner edges of the slit) and colliding with plasma within the entrance slit.

An extended view of a typical space-resolved aluminum K-shell spectrum obtained with the time-integrating crystal spectrometer is shown in figure 6a. The He-like resonance line, He$_{\alpha}$, with its satellites, S$_1$ and S$_2$, as well as the intercombination line, IC, can be clearly distinguished. The three emitting zones represent the primary plasma (1), the plasma on the outer surface of the cylinder (2), and the region of plasma collision (3), respectively. Figure 6b shows microdensitometer traces of the complete K-shell spectra of the zones (1) and (3). As described in more detail in (Weber et al. 1988), several ratios of line intensities were used to obtain time-averaged values of the densities and temperatures inside the cylinders. Density values were deduced from the S$_1$/He$_{\alpha}$, H$_{\alpha}$/He$_{\alpha}$, and IC/He$_{\alpha}$ line ratios, while the H$_{\alpha}$/He$_{\alpha}$ ratio was used for temperature determination. As shown in figure 6c, the different line ratios yield an average primary plasma electron density between $10^{19}$ and $10^{20}$ cm$^{-3}$. The density in the region of plasma collision is systematically lower by about a factor of two for all shots. A value of 450 eV ± 30 eV is found for the average temperature of the primary plasma, while an average temperature of 350 eV is obtained, with the same error bar, in the region of plasma collision.

4. Hydrodynamic code calculations

An Eulerian code was used to solve the conservation equations for mass and momentum for an isothermal plasma. In cylindrical geometry...
FIGURE 6. (a) Space resolved spectra of Al XII resonance line with emission from the primary plasma (1), the outer surface (2), and the region of plasma stagnation (3); (b) microdensitometer traces of the complete K-shell spectra of regions (1) and (3). (Continued on facing page.)
FIGURE 6. (c) Space-resolved, time-averaged values for temperature and density inside the 300 μm Al cavity, as obtained from line intensity ratios of (b).

\[
\frac{\partial}{\partial t} n_e + \frac{1}{r} \frac{\partial}{\partial r} (r n_e v_p) = 0 \tag{1}
\]

\[
\frac{\partial}{\partial t} v_p + v_p \frac{\partial}{\partial r} v_p + \frac{Z T_e}{n_e m_i} \frac{\partial}{\partial r} n_e = 0 \tag{2}
\]

where \( n_e(r,t), T_e(t), Z(t), m_i, \) and \( v_p(r,t) \) are the electron density, electron temperature, mean ionization state, ion mass, and plasma expansion velocity, respectively. The temperature was increased according to
where $I_L(t)$ is the temporal profile of the (Gaussian) laser pulse and $A$ is the fraction of laser energy absorbed by the plasma. In this form, $A$ serves as a fit parameter which determines the peak plasma temperature, $T_p$, reached upon irradiation. The time-dependent ionisation equations were solved to yield $Z(t)$. Collisional ionisation and radiative recombination rates were taken from McWhirter (1965). The initial electron density scale-length was set at $L = 1 \mu m$.

Figure 7 shows the calculated plasma electron density contours at 50 ps intervals for a 220 $\mu m$ diameter Cu microtube and $T_p = 400$ eV. Clearly, the early phase, up to $\sim 200$ ps after the peak of the laser pulse, is characterized by a concave density profile. After this, the inward motion of the plasma ablated at the wall is seen to result in a pile-up of plasma at the center of the tube. If we take the time at which the electron density is greater than the $2\omega$ critical value everywhere in the tube as a measure for the time of plasma collision, we obtain a value of $\sim 270$ ps. This compares reasonably well with the value of $\sim 300$ ps deduced from the experimental data in figures 3 and 5.

A final point to note from the code results displayed in figure 7 is that the electron density profile remains virtually unchanged for most of its motion toward the center of the cylinder. This is consistent with the fact that no perturbation of fringes is observed in the interferograms (see figure 2) until late in time ($\tau \geq 100$ ps).

5. Conclusions

Laser irradiation of cylindrical cavities through an axial slit has been investigated with respect to its potential for providing favourable conditions in X-ray laser experiments. It was shown that indirect plasma ablation from the cavity wall is predominantly due to laser light reflected from the primary spot in the case of short pulse, long wavelength,

![Figure 7. Calculated plasma electron density contours at 50 ps intervals for a 220 $\mu m$ Cu microtube and $T_p = 400$ eV.](https://www.cambridge.org/core/core/terms.https://doi.org/10.1017/S0263034600008077)
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high irradiance conditions. Short wavelength irradiation is expected to alter this situation in favor of energy redistribution by soft x-radiation.

The symmetry of the radial plasma evolution may be improved in a number of ways. Multiple longitudinal slits will increase the area of primary irradiation. High energy, long wavelength pulses of a few picoseconds duration may improve the redistribution of laser light in the cavity due to increased plasma reflectivity. Off-center incidence of the irradiating laser beam will reduce the substantial fraction of reflected light lost through the slit. The present experiments have shown that the creation of a confined, radially symmetric, waveguiding plasma may be feasible.

One may speculate about a possible X-ray laser in such a cavity. The rapid cooling required in a recombination scheme, for example, may prove difficult to achieve in this closed geometry, unless additional cooling mechanisms such as radiation and/or conduction cooling are exploited (Milchberg et al. 1985). In this scheme, population inversion should be attained while the density profile is still concave, i.e., before the collision of the primary and secondary plasmas. A collisional excitation laser scheme could perhaps work during the long duration stagnation phase which would also be appropriate for multi-pass amplification. Due to the density hump at the center the refractive index profile will be less favourable to wave-guiding during this phase. However, this region of increased density is likely also to be a region of increased gain, so that additional benefits from gain-guiding (Kogelnik 1965) could be exploited there.

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REFERENCES

Balmer, J. E. & Weber, R. 1988 Helv. Phys. Acta 61, 132.
Benattar, R., Popovics, C. & Sigel, R. 1979 Rev. Sci. Instrum. 50, 1583.
Cunningham, P. F. et al. 1988 Opt. Commun. 68, 412.
Garban-Labaune, C., et al. 1982 Phys. Rev. Lett. 48, 1018.
Hagelstein P. L. 1983 Plasma Physics 25, 1345.
Jacoby, D. et al. 1982 J. Phys. B 15, 3557.
Jaegle, P. et al. 1986 Europhys. Lett. 1, 555.
Kogelnik, H. 1965 Appl. Opt. 4, 1562.
London, R. A. 1988 Phys. Fluids 31, 184.
Lunney, J. G. 1986 Appl. Phys. Lett. 48, 891.
Matthews, D. L. et al. 1985 Phys. Rev. Lett. 54, 110.
McWhirter, R. W. P. 1965 Plasma Diagnostic Techniques, R. H. Huddleston and S. L. Leonard eds. (Academic Press, New York), p. 201.
Milchberg, H. et al. 1985 Appl. Phys. Lett. 47, 1151.
Mora, P. 1982 Phys. Fluids 25, 1051.
Rosen, M. D. & Hagelstein, P. L. 1986 Lawrence Livermore National Laboratory Report UCRL-94412.
Seely, J. F. et al. 1985 Opt. Commun. 54, 289.
Suckewer, S. et al. 1985 Phys. Rev. Lett. 55, 1753.
Weber, R., Cunningham, P. F. & Balmer, J. E. 1988 Appl. Phys. Lett. 53, 2596.