Simultaneous measurement of torsional oscillations and NMR of very dilute $^3$He in solid $^4$He

Toda, Ryo; Gumann, Patryk; Kosaka, Kei; Kanemoto, Masatomo; Onoe, Wakana; Sasaki, Yutaka

CITATION:
Toda, Ryo ...[et al]. Simultaneous measurement of torsional oscillations and NMR of very dilute $^3$He in solid $^4$He. Physical Review B 2010, 81(21): 214515.

ISSUE DATE:
2010-06

URL:
http://hdl.handle.net/2433/128875

RIGHT:
© 2010 The American Physical Society
Simultaneous measurement of torsional oscillations and NMR of very dilute $^3\text{He}$ in solid $^4\text{He}$

Ryo Toda,$^{1,2,6}$ Patryk Gumann,$^{1,3}$ Kei Kosaka,$^2$ Masatomo Kanemoto,$^2$ Wakana Onoe,$^2$ and Yutaka Sasaki$^{1,2}$

$^1$Research Center for Low Temperature and Materials Sciences, Kyoto University, Sakyoku, Kyoto 606-8501, Japan
$^2$Graduate School of Science, Kyoto University, Sakyoku, Kyoto 606-8502, Japan

(Received 9 July 2009; revised manuscript received 28 March 2010; published 16 June 2010)

We have investigated the NMR properties of dilute $^3\text{He}$ impurities in solid $^4\text{He}$ contained in a torsional oscillator (TO) by the simultaneous measurement of the NMR and the torsional oscillator response of the so-called supersolid $^4\text{He}$.

I. INTRODUCTION

Superfluidlike behavior in a solid, referred to as a supersolid, was originally attributed to Bose-Einstein condensation of delocalized zero-point vacancies in a crystal.1–3 However, although many studies attempted to demonstrate a supersolid phase in solid $^4\text{He}$, none were successful in providing evidence of the same.4 In 2004, Kim and Chan5 observed the nonclassical rotational inertia (NCRIf) of solid $^4\text{He}$ by a torsional oscillator (TO) experiment. The resonant period of a TO filled with solid helium exhibits a drop below some characteristic temperature near 200 mK. This drop in the resonant period can be attributed to the decoupling of a part of the mass of solid $^4\text{He}$ from the TO, as in the case of a TO with superfluid $^4\text{He}$ in it. The observed NCRIf fraction (NCRIf), defined as the ratio of the decoupled inertia to the total inertia of solid helium in the TO, varies from 0.1% to 20% depending on the sample geometry.6 Although it is much smaller than the value in the case of a bulk liquid, it agrees with the theoretical expectation.7 This experimental result attracted considerable interest and served as a starting point for many theoretical and experimental works.7 Thus far, considerable information about the phenomenon of supersolidity has been obtained. The observed NCRIf decreases with an increase in the driving velocity.5 The reduction in the NCRIf is well characterized by a critical velocity.5 The annealing effect has been investigated by several groups,6,9,10 and these studies have proved that the NCRIf depends on the history of the solid sample. Another important observation is the strong dependence of the NCRIf on relatively small amounts of $^3\text{He}$ impurities.11 Although several TO experiments have shown the existence of NCRIf, a dc flow study failed to detect the mass flow that would be expected in a supersolid.12 Several theoretical models have been proposed thus far but none have been satisfactory. Recently, the consensus that has been arrived at is that supersolidity is probably related to some nonuniformity in the solid samples. However, this phenomenon has not yet been clearly understood. Therefore, it is necessary to obtain more information in order to understand supersolid $^4\text{He}$.

The fact that the NCRIf response of solid $^4\text{He}$ is affected by very small amounts [from parts per billion (ppb) to parts per million (ppm)] of $^3\text{He}$ suggests that this phenomenon is not a bulk one because it is difficult to visualize any long-range interaction between $^4\text{He}$ and tiny amounts of $^3\text{He}$, which are located separately in solid $^4\text{He}$. Even if all $^3\text{He}$ impurities are localized in a region exhibiting supersolid behavior with 0.1% NCRIf, a hundred ppm is too tiny an amount of impurity to destroy the supersolid response of $^4\text{He}$ if the supersolidity is a phenomenon similar to the superfluidity in bulk liquid $^4\text{He}$. Therefore, it is desirable to study how a tiny amount of $^3\text{He}$ impurity can influence the supersolid properties of $^4\text{He}$; this should lead to insights into this fascinating field of research. It is well known that a solid mixture of $^3\text{He}^-^4\text{He}$ has a finite phase-separation temperature that depends on the concentration of $^3\text{He}$, even for 1 ppb of $^3\text{He}$ impurities.13 Above the phase-separation temperature $T_{PS}$, $^3\text{He}$ atoms distribute homogeneously in the matrix of hcp solid $^4\text{He}$, whereas below $T_{PS}$, they tend to form tiny clusters of pure $^3\text{He}$ in solid $^4\text{He}$. Because the movement of $^3\text{He}$ atoms in solid $^4\text{He}$ due to diffusion is relatively slow, a large droplet of solid $^3\text{He}$, as in the case of a liquid mixture, cannot be formed. As reported earlier,14,15 NMR measurements revealed the formation of $^3\text{He}$ clusters in solid $^4\text{He}$. In a percent solution, the clusters typically have diameters of the order of several micrometers. Similarly, the NMR properties of $^3\text{He}$ in supersolid $^4\text{He}$ will provide information about the state of $^3\text{He}$ surrounded by $^4\text{He}$.

II. EXPERIMENT

We have developed an apparatus to carry out simultaneous TO/NMR measurements of the same sample. Our TO contains a Be-Cu torsion rod and a cylindrical polycarbonate cell. The TO assembly is supported by a massive copper isolator block that is thermally anchored to the mixing cham-

DOI: 10.1103/PhysRevB.81.214515 PACS number(s): 67.80.bd, 67.60.–g, 67.80.dk
ber of a dilution refrigerator. The inner diameter of the TO cell body is 14 mm and the height of the sample space is 16 mm. The TO is driven by a constant excitation voltage feedback system. The measured $Q$ value of TO is approximately $2 \times 10^3$ at 800 mK and the resonant frequency of the empty TO is 1175 Hz. The NMR coil is wound around the bottom of the cell without touching the cell body so as not to degrade the $Q$ value of the TO, and it is thermally anchored to the mixing chamber directly in order to prevent sample from being heated by the rf pulses used for NMR measurement. The static magnetic field of 0.15 T for NMR is applied perpendicular to the axis of the TO.

A solid sample of $^3$He-$^4$He mixture is produced using the blocked capillary method by the following process. First, the necessary amount of $^3$He gas is condensed in the cell at 10 mK. After most of the $^3$He gas condenses, $^4$He gas at 0.5 MPa, which is filled in a closed volume of the filling line at room temperature, is introduced into the cell. In a few minutes, the pressure reduces to approximately 0.05 MPa. Then, additional $^4$He gas at 0.5 MPa is condensed again. This filling process is repeated in order to condense all of the $^3$He gas in the filling line into the cell. After the cell is filled by the liquid mixture, the cell is pressurized up to 2.5 MPa. Then, the refrigerator is warmed up to 3 K and the cell is pressurized up to 6.5 MPa. The cell is gradually cooled down over 6 h to a temperature at which the pressure leaves melting curve to let a seed of the solid grow larger and fill the cell completely. The resonant frequency drops by 15 Hz due to the inertia of the solid. The final pressure of the solid $^4$He is estimated to be approximately $3.6 \pm 0.1$ MPa from the melting temperature while warming up. Our samples of $^4$He with commercial purity (0.3 ppm), 100 ppm, 300 ppm, and 1000 ppm of $^3$He are produced in this manner. Another sample of $^4$He with a few hundred ppm of $^3$He is produced by diluting a sample of $^4$He with 1000 ppm of $^3$He. First, we depressurize the cell that contains the 1000 ppm sample to approximately 0.1 MPa and repressurize the cell to approximately 2.5 MPa by filling $^4$He. We repeat this process in order to dilute the concentration of $^3$He in the cell. Finally, the refrigerator is warmed up to 3 K and the cell is pressurized up to 6.5 MPa. We estimate the concentration of $^3$He in this sample to be $350 \pm 150$ ppm.

We have measured the resonant frequency and amplitude of the TO with an empty cell; a $^4$He sample of commercial purity at 3.6 MPa; and $^4$He samples with 100, 300, and a few hundred ppm of $^3$He impurity at 3.6 MPa. The results for the empty cell, commercial purity sample, and sample with a few hundred ppm of $^3$He are shown in Fig. 1. In case of the commercial purity sample, sudden increases in the resonant frequency and extra energy dissipation are observed below 200 mK. This agrees with the experimental results of other groups.5,8–10 In the case of the sample with a few hundred ppm of $^3$He, an NCRI response similar to that mentioned above is not observed. This result indicates that the NCRI response is destroyed because of the strong effect of $^3$He impurities. The temperature dependence of the frequency and amplitude of solid samples with 100 and 300 ppm of $^3$He are similar in this temperature range. For samples with over a hundred ppm of $^3$He impurity, the phase-separation temperature $T_{\text{PS}}$ is estimated to be approximately 100 mK; this temper-
attributed to cascaded relaxation processes. We also measured $T_2$ of the S and L components using a $\pi/2-\tau-\pi$ pulse sequence with various $\tau$ and various waiting times $\Delta t$ after the last saturation pulse. We show the results for the sample with a few hundred ppm of $^3$He in Fig. 3. For $\Delta t=100$ s, the observed signal originates from only the S component because $T_{1S}\gg \Delta t$. The $T_2$ value of the S component is determined to be approximately 20 ms from this measurement. For $\Delta t=2000$ s, we observe both the S and the L components. The $T_2$ value of the L component can be obtained by subtracting the signal of the S component estimated from the result of $\Delta t=100$ s. The obtained $T_2$ of the L component is approximately ten times longer than that of the S component. This evidences the fact that the two components are completely different from each other.

The solid line shown in Fig. 2 fits the data for the sample with a few hundred ppm of $^3$He with $T_{1S}=10$ s and $T_{1L}=3200$ s. The slight deviation near $T_{1S}$ indicates that $T_{1S}$ has some distribution. For the sample with 300 ppm of $^3$He, the signal intensity mostly increases near $\Delta t=1000$ s. The broad distribution of the signal below $\Delta t=100$ s suggests that $T_{1S}$ for this sample distributes in the range between $10^0$ and $10^2$ s.

We should note that the ratio of the intensities of the S and the L components differs considerably between the samples with 300 and a few hundred ppm of $^3$He. This might depend on the sample quality because the former sample was maintained at a temperature slightly below the melting point for more than a day whereas the latter sample was cooled much faster. For the sample with 100 ppm of $^3$He, the L component almost disappears. This suggests that for $^3$He the location of the S component is more favorable than that of the L component.

The S and L components correspond to $^3$He clusters, which are formed by the phase separation, because the signal intensity of both components increases with time after cooling through $T_{PS}$ (see Fig. 5). This result implies that a third invisible component (I component) with extremely long $T_1$ exists in this system even below $T_{PS}$, and this is the source of the $^3$He atoms that form clusters. The I component probably corresponds to isolated atoms that are separated from each other in the lattice of hcp solid $^4$He. Thus, three different components, namely, S, L, and I, of $^3$He exist in the system at low temperature. Because it is difficult to investigate the I component, whose $T_1$ is a large fraction of a day, we investigate the other two components in this experiment.

Figure 4 shows the temperature dependences of the echo height after a $\pi/2-\tau-\pi$ pulse sequence with various waiting times $\Delta t$ after the last saturation pulse for the sample with a few hundred ppm of $^3$He. During warming, the echo height for $\Delta t=2800$ s (solid circle) is larger than that for $\Delta t=1000$ s (solid triangle). During cooling, the echo height (open circle and open triangle) is smaller than that obtained during warming. The echo height for two different $\Delta t$ is similar. The solid line is a fit to Curie’s law. An echo height for $\Delta t=41000$ s at 160 mK is shown (solid square) to indicate the existence of a component with much longer $T_1$.
At the lowest temperature, the echo height for $\Delta t = 2800 \text{ s}$ is approximately 10% larger than the one for $\Delta t = 1000 \text{ s}$. This difference indicates the existence of the L component. Then, the system is warmed slowly over $20 \text{ h}$. During warming, the echo height decreases as the temperature increases and it disappears in the noise above $140 \text{ mK}$, which is above the phase-separation temperature $T_{\text{PS}} \approx 100 \text{ mK}$. Because the time scale of warming is not sufficiently long, we observe the signal even above $T_{\text{PS}}$, however, the signal disappears after a while. After a wait time of $\Delta t = 41,000 \text{ s}$ at $160 \text{ mK}$, a very strong signal is observed, as indicated by the solid square in Fig. 4 because of the recovery of the I component. The sample was left at $160 \text{ mK}$ for approximately $80 \text{ h}$. Soon after cooling to $8 \text{ mK}$, the signals from both components are not observable. This indicates that $^3\text{He}$ atoms contained in both the S and the L components escape completely and merge into the I component. The difference between these two experiments suggests that the $^3\text{He}$ atoms contained in the S component remain in a nearby location, whereas the $^3\text{He}$ atoms contained in the L component separate in space in the temperature range slightly above $T_{\text{PS}}$. This feature of the S components is called the stability.

### III. DISCUSSION

Such stability of the S component is also observed in other samples. Although both clusters disappear above $T_{\text{PS}}$, the $^3\text{He}$ atoms in the S component remain in a nearby location, where atoms can easily form clusters again below $T_{\text{PS}}$. On the other hand, $^3\text{He}$ atoms contained in the L component get separated completely. We attribute this difference to the state of the surrounding $^4\text{He}$ crystal. Because of the fact that the S component is more stable than the L component, we propose that the S component is formed in the nonuniform part of the crystal, whereas the L component is formed in the homogeneous part of the crystal. If there exists a macroscopic disorder such as this nonuniformity, an extra trapping potential for $^3\text{He}$ appears as a natural consequence. The shorter relaxation time for the S component also suggests considerably active motion of atoms due to the imperfect lattice structure in the disorder. The volume fraction of the disordered part could be as large as $100 \text{ ppm}$ because the L component almost disappears in the solid with $100 \text{ ppm}$ of $^3\text{He}$. However, further investigations are required to understand the nature of this nonuniformity.

Next, we discuss the strong effect of $^3\text{He}$ impurities on the supersolid. As discussed earlier, $100 \text{ ppm}$ of $^3\text{He}$ can destroy the NCRI response. Although one normalizes $100 \text{ ppm}$ by the NCRIi of $\approx 0.1\%$, it is still $10\%$, which is too small a fraction to destroy the NCRI response completely. If the effect of $^3\text{He}$ impurities in the supersolid is similar to that of the $^3\text{He}$ impurities in superfluid $^4\text{He}$, then, the strong impurity effect is likely to be caused by $^3\text{He}$, whose local concentration is much higher than the averaged concentration. The $^3\text{He}$ atoms in the S component of our sample are a good candidate for this type of concentrated $^3\text{He}$ because they remain in a nearby location even above the phase-separation temperature $T_{\text{PS}}$. If this is the case, the NCRI
response must originate from the region where the S component forms. This is further evidence of the hypothesis that some nonuniformity of hcp $^4$He is strongly related to the cause of the NCRI response. Because our measurement is performed with an impurity concentration that is sufficient to completely destroy the NCRI response, further investigations with lesser impurities are required to confirm our proposal.

ACKNOWLEDGMENTS

This research was supported by the Grant-in-Aids for Scientific Research on Priority Area “Physics of new quantum phases in superclean materials” (Grant No. 17071004) and for the Global COE Program “The Next Generation of Physics, Spun from Universality and Emergence” from the Ministry of Education, Culture, Sports, Science and Technology (MEXT) of Japan.

---

*rtoda@scphys.kyoto-u.ac.jp

1Present address: Department of Physics and Astronomy, Rutgers University, Piscataway, NJ 08854-8019, USA.

1A. Andreev and I. Lifshitz, Sov. Phys. JETP 29, 1107 (1969).

2G. Chester, Phys. Rev. A 2, 256 (1970).

3A. Leggett, Phys. Rev. Lett. 25, 1543 (1970).

4M. W. Meisel, Physica B 178, 121 (1992).

5E. Kim and M. H. W. Chan, Science 305, 1941 (2004).

6Ann Sophie C. Rittner and J. D. Reppy, Phys. Rev. Lett. 97, 165301 (2006).

7D. Galli and L. Reatto, J. Phys. Soc. Jpn. 77, 111010 (2008) see this review article.

8Y. Aoki, J. C. Graves, and H. Kojima, Phys. Rev. Lett. 99, 015301 (2007).

9A. Penzev, Y. Yasuta, and M. Kubota, J. Low Temp. Phys. 148, 677 (2007).

10M. Kondo, S. Takada, Y. Shibayama, and K. Shirahama, J. Low Temp. Phys. 148, 695 (2007).

11E. Kim, J. S. Xia, J. T. West, X. Lin, A. C. Clark, and M. H. W. Chan, Phys. Rev. Lett. 100, 065301 (2008).

12J. Day and J. Beamish, Phys. Rev. Lett. 96, 105304 (2006).

13D. O. Edwards and S. Balibar, Phys. Rev. B 39, 4083 (1989).

14S. C. J. Kingsley, V. Maidanov, J. Saunders, and B. Cowan, J. Low Temp. Phys. 113, 1017 (1998).

15M. Poole and B. Cowan, J. Low Temp. Phys. 134, 211 (2004).