Development of a Cross-Type Magnetic Coupler for Unmanned Aerial Vehicle IPT Charging Systems

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This work was supported in part by the Natural Science Foundation of Shandong Province of China under Grant ZR2019MEE052, and in part by the Major Scientific and Technological Innovation Project of Shandong Province of China under Grant 2017CXGC0921.

ABSTRACT Inductive power transfer (IPT) is an optimal way for the unmanned aerial vehicle (UAV) wireless charging. The magnetic coupler is the key component in the IPT system, which determines the power transmission capacity and efficiency in IPT system. Due to the particularity of UAV application, the magnetic field height should be strictly limited to avoid the damage caused by high frequency magnetic field heat the UAV’s metal equipment. A cross-type magnetic coupler with receiving coil placed on UAV’s one landing gear was proposed to solve this problem, but it has the possibility of making UAV fuselage imbalance. Therefore, a novel cross-type magnetic coupler is proposed to overcome its difficulties in this paper, and most of magnetic fields are restrained to be lower than UAV’s landing gear height $h_1 = 145\text{mm}$, which will not cause damage to the UAV’s equipment. And a simple and practical iterative method for designing the magnetic coupler geometry parameters is proposed, with simplification of the complex design process for the finite element analysis, improves the design efficiency. The experimental results show that the system can charge the 260W UAV normally with the system efficiency of 91.577% within the misalignment range of X-axis direction 25mm, Y-axis direction 40mm and rotation 25°.

INDEX TERMS Unmanned aerial vehicle (UAV), inductive power transfer (IPT), cross-type magnetic resonant coupling, magnetic circuit model, coupler geometry parameter design.

I. INTRODUCTION

Unmanned aerial vehicle (UAV) is an aircraft that is controlled by a radio real-time remote control or stored program in advance by itself, capable of carrying multiple functional devices to perform various tasks. It exhibits the advantages such as simple structure, small size, low cost, strong adaptability, flexible to use, etc. It has been applied in scientific research, civils [1] and military fields [2]. However, due to the limitation of volume and bearing capacity, the UAV’s battery capacity is limited, and the problem of charging has become a bottleneck in the UAV further development. At present, the manual plug is mainly used to charge the UAV. Obviously, this way has some shortcomings in flexibility, convenience, etc, which reduces the UAV’s operation scope, consumes manpower and reduces UAV automation. Therefore, it is important to incorporate the wireless power transfer (WPT) technology to UAV charging technology. WPT technology avoids the direct contact among wires, removes the step of manually plugging and unplugging, improves its operation range and implements the goal of UAV unattended.

Inductive power transfer (IPT) is one of the most widely used methods in the WPT technology. At present, IPT system has been widely used in electric vehicles [3], underwater autonomous vehicles [4], electronic equipment [5], medical devices [6], etc. IPT system consists of two parts, the transmitter and the receiver, which are completely isolated from each other by means of transmitting the electric energy from the transmitter to the receiver wirelessly through a magnetic coupler. The transmitter converts AC voltage with power frequency or DC voltage to high frequency AC voltage through power converter. The high frequency AC current generates
a high frequency alternating magnetic field surrounding the transmitting coil through resonant compensation network. The receiving coil picks up most of the alternating magnetic flux and generates the high frequency voltage. The high frequency AC voltage can be converted and adjusted by the power converter so that it can meet the requirements of various loads. By adjusting the circuit parameters and improving the coupling capability, the IPT system can obtain higher transmission power and transmission efficiency.

At present, some scholars have tried to wirelessly charge UAV to improve the UAV’s operations scope and achieve the functionality of unattended guard. The method of making air-cored coils around the UAV frame is proposed to implement an IPT system with 35W power and 71% efficiency [7]. As the air gap between the transmitting coil and the receiving coil is large, resulting in the weak coupling capability. But the strong coupling capability is the basis to ensure the efficient wireless power transmission. In order to improve the coupling capability, the receiving coil can be wound around the bottom of the landing gear [8], the receiving coil can be wound around the bottom end of the UAV landing gear. But it causes electromagnetic interference to the battery tank, pan-tilt-zoom camera or other operating equipment installed in the abdomen of the UAV, which will affect performance of the equipment. The high frequency magnetic field heats up the UAV’s metal equipment, causing damage to the equipment. Therefore, a scheme with small plane coil installed at the bottom of the landing gear is proposed [9]. Although this scheme solves the electromagnetic interference problem with high coupling capability, the tolerance to misalignment of this scheme is not sufficient. A method is proposed to extend the UAV charging area by using two receiving coils to solve the misalignment tolerance problem [10]. However, the system transmission efficiency is low, only 50%. Due to the limited UAV’s space and bearing capacity, it is necessary to reduce the UAV’s space occupied by receiver pad and its weight. In [11], the planar air-cored coil is used to reduce magnetic coupler weight, but receiving coil installed on the side of the frame can cause UAV to be unbalanced in operation. Due to limitation of UAV’s capacity and landing accuracy, it is important to design a magnetic coupler with strong coupling capability, strong misalignment tolerance and also ensure its receiver pad is of small size and light weight. More importantly, the magnetic field height of magnetic coupler should be strictly limited to avoid the damage caused by the high frequency magnetic field heat the UAV’s metal equipment. Therefore, in [12], a cross-type magnetic coupler is proposed, in which the transmitter pad adopts the DD-type structure, and the receiving coil is installed on UAV’s one landing gear. The transmitter pad and the receiving coil are perpendicular to each other, and the charging power is 624W, with 90% maximum efficiency. It is suitable for wireless charging for medium power UAV. However, the receiving coil is only wound on UAV’s one landing gear, when the turns of receiving coil are more, the coil becomes heavier, which will lead to UAV fuselage imbalance.

The above researches are focused on magnetic coupler type, and there are only few researches on the design for magnetic coupler geometry parameter at present. In [13], the finite element method is used to carry out repeating simulations and experiments to design the magnetic coupler geometry parameters. Although this method can achieve desired results, it is not universal, and only the coupling coefficient is considered, which can not achieve the balance on multiple design parameters. Therefore, a simple and practical method is needed to design magnetic coupler dimensions.

In contrast to current achievements, a novel cross-type magnetic coupler is proposed in this paper, the main merits of the developed scheme can be summed up as follows:

1) A cross-type magnetic coupler proposed in this paper is proposed, which avoid the influence of high frequency magnetic field on UAV’s internal equipment;

2) The magnetic circuit and electric circuit model are established, and a simple and practical iterative method for designing the magnetic coupler geometry parameters is proposed, with simplification of the complex design process, improves the design efficiency.

II. IPT SYSTEM OVERVIEW

A. SYSTEM OVERALL STRUCTURE

A typical IPT system block diagram is shown in Fig. 1. The high frequency sinusoidal current is first generated by DC power supply through the inverter, and the high frequency alternating magnetic field is excited by the transmitter pad. Then the receiver pad receives the electric energy from the primary side by magnetic field coupling to implement the wireless power transmission. The pick-up circuit first converts the high frequency AC voltage into DC voltage through a rectifier circuit, then the voltage and current are adjusted by DC-DC converter to charge the battery.

B. COMPENSATION CIRCUIT SELECTED

In an IPT system, compensation circuit is usually added to compensate for leakage inductance and improve the system transmission efficiency. When voltage source inverter is adopted, the basic compensation structure (primary series and secondary series (SS) [14], [15] or primary series and secondary parallel (SP) [14]–[16] compensation), or the hybrid compensation structure (inductance-capacitance-inductance (LCL) [17] compensation) can be used. Considering that the IPT system in this paper is a low voltage and high current system, if the Boost converter is selected as DC-DC converter, the current fed to the rectifier will be very large resulting in
considerable loss and low efficiency. The Buck converter can effectively reduce the current level and improve the working efficiency, which is a better scheme of the system in this paper. The Buck converter demand a voltage source excitation, so the SP or the LCL-S compensation can be selected. The reflection impedance of SP compensation is related to the load resistance, by contrast, the reflection impedance of LCL-S compensation is pure resistance, so LCL-S compensation has better stability. Therefore, the LCL-S compensation is selected in this paper. As shown in the dotted line section of Fig. 2.

In Fig. 2, $U_{in}$ is the system input DC voltage, $C_{DC}$, $C_{dc}$ and $C_4$ are filter capacitors, $S_1 \sim S_4$ are inverter switches. $L_1$ is compensation inductance, $C_P$ and $C_S$ are the compensation capacitances of the primary and secondary sides, respectively. $L_P$ and $L_S$ are the inductances of the magnetic coupler primary and secondary sides, respectively. $R_1$, $R_P$ and $R_S$ are equivalent internal resistance of coils, $D_5 \sim D_8$ are rectifier diodes. $S_2$, $D_{10}$ and $L_2$ constitute Buck converter, and lithium battery is connected finally. In order to improve the secondary induced voltage, a part of $L_P$ can be compensated first by adding the compensation capacitance $C_1$, and then the rest of $L_P$ resonates with $C_P$, where $L_1 = L_P - 1/\omega^2C_1$. It can be obtained that the system output power is as follows [18]:

$$P_{out} = U_{oc} I_{sc} Q_2 = \frac{\omega M^2 L_P^2 Q_2}{L_S} = \frac{k^2 U_{oc}^2}{\omega L_P}$$  (1)

where, $U_{oc}$ and $I_{sc}$ are the secondary open-circuit voltage and short-circuit current, respectively. $Q_2 = \omega L_S / R_{eq}$ is the secondary quality factor, $U_P$ and $I_P$ are the primary excitation voltage and current, respectively. $\omega$ is the system resonance angular frequency, $M$ and $k$ are the mutual inductance and the coupling coefficient between the coils, and there is $k = M / \sqrt{L_P L_S}$. The $Q_2$ is less than 10 generally to improve the system voltage transmission ratio and maintain the system stability [19], so it is constrained to 2-5 in this paper.

### C. MAGNETIC COUPLER LIMITATION

From (1), increasing $k$ or decreasing $L_P$ will increase the system output power. Therefore, the parameters $k$ and $L_P$ of the magnetic coupler are important factors that affect the system output power. $k$ is a key parameter to reflect the magnetic coupler coupling capability, and the magnetic coupler geometry parameter will affect $L_P$. How to ensure higher power transmission capability of magnetic coupler at lower cost is a problem that should be considered. Moreover, the application environment should also be considered in the design of magnetic coupler. Due to limitation of UAV’s bearing capacity and landing accuracy, a magnetic coupler should be designed with strong coupling capability, strong misalignment tolerance and its receiver pad takes up less UAV’s space and behaves light weight. Therefore, the planar hollow receiving coil is used to reduce receiver pad weight. And the distance between the transmitter pad and the receiver pad is reduced to increase the coupling capability. More importantly, the high frequency alternating magnetic field heats up the UAV’s internal metal equipment, resulting in a damage to them. The reference [20] shows that the minimum flux density which causes injury to the human body is $2.7 \times 10^{-5}$T, when the system working frequency variation range from 3kHz to 10MHz. Human safety standards are often stricter than those for equipment. And the magnetic field height of the magnetic coupler should be strictly limited in this paper. Therefore, the design goal in this paper is that magnetic flux density should be less than $1 \times 10^{-5}$T when the height is greater than that of UAV’s landing gear height $h_1 = 145$mm, which is smaller than $2.7 \times 10^{-5}$T to further ensure the safety of the UAV equipment.

### III. NOVEL MAGNETIC COUPLER

#### A. MAGNETIC COUPLER PROPOSED

As a key part of the IPT system, magnetic coupler’s geometry determines the magnetic field pattern and the system electromagnetic interference level. Enhancing the coupling capability of the magnetic coupler can improve the system power transfer capability. And the system adaptive capability can be improved by reducing the sensitivity of the magnetic coupler to misalignment. At present, the circular pad is one of the most common structure in the literature [18], but the circular pad has the disadvantages of strict air gap requirements and high misalignment sensitivity. Therefore, a DD-type magnetic coupler is proposed [21], which provides a charge zone approximately five times larger than that of the circular pad for a similar material cost, improves the misalignment range and overcomes the difficulty of circular pad. The receiver pad adopts DD-type hollow structure which is installed on the UAV’s landing gear to reduce its weight, and the simulation model of DD-type magnetic coupler used in UAV is shown in Fig. 3.

The peak magnetic flux density refers to the magnetic flux density corresponding to the maximum current in the

![FIGURE 2. Overall circuit diagram of the IPT system for UAV.](image2)

![FIGURE 3. The simulation model of DD-type magnetic.](image3)
coupling coils, which corresponds to the moment when the high frequency magnetic field has the greatest influence on the UAV internal equipment, and determines the magnetic field safety level of the magnetic coupler. The ampere turns per transmitting coil is set to 180A-N, and the peak magnetic field safety level of the magnetic coupler.

The magnetic field height of the case where $I_p = I_{P_{\text{max}}}$ and $I_S = 0$, and the moment of $I_p = I_{P_{\text{max}}}$ and $I_S = 0$ both correspond to the peak magnetic field. The magnetic field distributions in the direction of the receiver pad height are more concerned, and the magnetic field height of the case where $I_S = I_{S_{\text{max}}}$ and $I_p = 0$ is higher than that of the case where $I_p = I_{P_{\text{max}}}$ and $I_S = 0$. Therefore, the case where $I_S = I_{S_{\text{max}}}$ and $I_p = 0$ is only considered in this paper. The influence of X-axis direction misalignment on the system coupling coefficient when the distance $h$ between the transmitter pad and the receiver pad varies is obtained as shown in Fig. 5.

From Fig. 4, when the height is greater than 88mm, the flux density of the DD-type magnetic coupler is less than $1 \times 10^{-5}$T, which meet the requirement for magnetic field height. But the maximum flux density is mainly concentrated on the underside of the receiver pad and the system coupling capability is weak. In order to enhance the coupling capability, the distance $h$ between the transmitter pad and the receiver pad can be reduced. In Fig. 5, reducing $h$ will increase the sensitivity of X-axis misalignment. The magnetic field height can also be increased by increasing the magnetic coupler dimensions to improve the system coupling capability, which will not only increase the cost, but also increase the influence of high frequency magnetic field on the UAV internal equipment. Most UAVs put their landing gears away during flight to allow the camera to rotate the shooting by 360°, which will not block the lens and facilitate aerial photography. Obviously, this DD-type structure is only suitable for fixed landing gear UAVs but not universal. Therefore, in [12], a cross-type magnetic coupler is proposed, as shown in Fig. 6. The transmitter pad adopts the DD-type structure, which is used to expand the UAV wireless charging zone and improve the misalignment range of magnetic coupler, thus reducing the landing accuracy of UAV. A few rectangular ferrite magnetic cores are placed under the transmitting coils, which can not only reduce the leakage of the magnetic coupler, restrain the flux lines better, improve the coupling capability of the magnetic coupler, but also distribute the magnetic field in single-sided direction and eliminate the magnetic shielding device. Due to the particularity of wireless charging for UAV, the receiver pad is required to be light weight and occupy small volume of UAV, which will not affect the UAV’s working range. Therefore, the receiving air-core coil is used as the receiver pad to reduce the weight of the receiver pad. The receiving coil is installed on UAV’s one landing gear which is perpendicular to the transmitter pad each other and does not occupy the UAV internal space. It not only reduces the distance between the transmitter pad and the receiver pad, improves the coupling capability of the magnetic coupler, but also avoids the high frequency magnetic field heating up the UAV internal metal equipment. However, the receiving coil is only wound on UAV’s one landing gear, which will lead to the imbalance of UAV fuselage when the receiving coil gets heavier. Therefore, a novel cross-type magnetic coupler is proposed in this paper, as shown in Fig. 7. The receiving coil is divided into two parts on average which are installed on UAV’s two landing gears. These two receiving coils are
in series and the coils are wound in the opposite direction. Thus, the problem with imbalance of UAV fuselage caused by overweight of receiving coil is solved. A middle coil is added between the transmitting coil 1 and the transmitting coil 2, and the three transmitting coils are in series which are wound in the same direction. If the current direction flowing through the transmitting coil 1 and the transmitting coil 2 are counterclockwise, the current flowing through the middle coil is clockwise, which not only restrains the direction of flux lines better, but also maintains good characteristics of DD-type magnetic coupler.

High frequency alternating magnetic fields are generated in the process of UAV wireless charging. If the UAV’s internal equipment is exposed to such a magnetic field, it will cause electromagnetic interference to these equipment, affect their performance, and even damage the metal equipment. Therefore, the magnetic field height of the magnetic coupler is strictly limited. The ampere turns of the per transmitting coil is set to $180 \text{A} \times \text{N}$. And the transmitting and receiving coils of the two cross-type magnetic couplers have the same number of turns. The UAV’s landing gear height $h_l$ is 145 mm. The peak magnetic field distribution of two cross-types magnetic coupler is obtained by ANSYS Maxwell software for 3D simulation as shown in Fig. 8.

From Fig. 8, when the flux density is less than $1 \times 10^{-5} \text{T}$, the height of type I is higher 129mm, and the height of type II is higher 127mm, they are all below 145mm. So they are not cause the electromagnetic interference to the UAV’s internal equipment. It can be seen that two cross-types magnetic couplers have the almost same level of electromagnetic interference, but compared with type I, type II does not cause UAV fuselage imbalance due to excessive coils.

Due to the limitation that UAV has a low landing accuracy, it is impossible to guarantee that UAV can land on the charging platform accurately every time. Therefore, the designed magnetic coupler should have strong misalignment tolerance. When the geometry parameters of the two cross-type magnetic couplers are the same, which include the type and turns of Litz wire used in coupling coils, each ferrite geometry parameters and the frame sizes of each transmitter coil and each receiver coil, the curve of coupling coefficient with misalignment is obtained, as shown in Fig. 9.

![FIGURE 7. Type II cross-type magnetic coupler.](image_url)

![FIGURE 8. Peak magnetic field distribution of two cross-types magnetic coupler.](image_url)

![FIGURE 9. The curve of coupling coefficient with misalignment.](image_url)
The magnetic circuit model of the type II cross-type magnetic coupler is established, in order to better study the magnetic field distribution of the magnetic coupler, analyze the influence of the flux lines distribution on the power transmission for wireless charging system, and fundamentally explore the relationship between the system magnetic circuit and the electric circuit. The magnetic field distribution caused by the primary excitation current and the secondary induced current of the cross-type magnetic coupler is shown in Fig. 10.

From Fig. 7(b), \( l_{p1} \) and \( l_{p2} \) are the inner length and outer length of the transmitting coil, respectively. \( w_{p1} \) and \( w_{p3} \) are the inner width and outer width of two side transmitting coils, respectively. \( w_{p2} \) is the transmitting coil width. \( w_{p4} \) is the outer width of the middle coil, and the inner width of the middle coil is twice as wide as that of the two side coils to maintain the symmetry of the magnetic coupler. \( h_{p} \) is the transmitting coil thickness. \( l_{S1} \) and \( l_{S2} \) are the inner length and outer length of the receiving coil, respectively. \( w_{S} \) is the receiving coil width. \( h_{S1} \) and \( h_{S3} \) are the inner and outer heights of the receiving coil. \( h_{S2} \) is the receiving coil thickness. \( l_{f} \), \( w_{f} \) and \( h_{f} \) are the length, width and thickness of the rectangular ferrite core, respectively. \( l_{g} \) is the gap between the ferrite cores. \( h \) is the air gap between the transmitter pad and receiver pad. The relationship of the magnetic coupler geometry parameters is as follows: \( l_{p2} - l_{p1} = 2w_{p2}, \ w_{p3} - w_{p1} = 2w_{p2}, \ w_{p4} - 2w_{p1} = 2w_{p2}, \ l_{S2} - l_{S1} = 2h_{S2} \) and \( h_{S3} - h_{S1} = 2h_{S2} \).

In Fig. 10(a), the main flux \( \Phi_{m} \) is divided into three parts, one part of flux links partially with the transmitting coil and partially with the receiving coil. Another part of flux links partially with the transmitting coil and fully with the receiving coil. The last part of flux links with all the transmitting coil and all the receiving coil. The flux partially linking with the transmitting coil links with a large part of the transmitting coil, which can be equivalent to the flux linking with all the transmitting coil to simplify the calculation. Therefore, the main flux \( \Phi_{m} \) can be equivalent to a concentric semicircle closed along the ferrite core with \( O_{P1} \) as the circle center. As shown in the solid line section of Fig. 10(a), the main flux \( \Phi_{m} \) equivalent reluctance is \( R_{m} \). The leakage flux \( \Phi_{l} \) is shown in the dotted line section of Fig. 10(b). The primary leakage flux \( \Phi_{lP} \) is divided into three parts. One part of flux can be equivalent to a concentric semicircle closed along the ferrite core with \( O_{P1} \) as the circle center, and its equivalent reluctance is \( R_{aP1} \). Another part of flux can be equivalent to a concentric circle with \( O_{P2} \) as the circle center, and its equivalent reluctance is \( R_{aP2} \). These two parts of flux link with the transmitting coil partially but no receiving coil. The last part of flux links with all the transmitting coil but no receiving coil, which is relatively small and can be ignored. The equivalent resistance \( R_{aP} \) of primary leakage flux \( \Phi_{lP} \) can be regarded as \( R_{aP1} \) is connected in parallel with \( R_{aP2} \). The secondary leakage flux \( \Phi_{lS} \) is divided into two parts. One part of flux links with the receiving coil partially but no transmitting coil, which can be equivalent to a concentric circle with \( O_{S1} \) as the circle center, and its equivalent reluctance is \( R_{aS1} \). The other part of flux links with all the receiving coil but no transmitting coil, which can be equivalent to a concentric circle with \( O_{S2} \) as the circle center, and its equivalent reluctance is \( R_{aS2} \). The equivalent resistance \( R_{aS} \) of secondary leakage flux \( \Phi_{lS} \) which can be regarded as \( R_{aS1} \) is connected in parallel with \( R_{aS2} \).

Reluctance is a parameter describing the flux conduction capability of the magnetic circuit, and its effect is similar to that of the resistance in the circuit model. The reluctance magnitude is subject to the structure and size of magnetic coupler and the material permeability [22]. The reluctance with magnetic circuit equivalent length \( l \) can be expressed as follows:

\[
R_{l} = \frac{l}{\mu_{a}S}
\]  

where \( S \) is the flux equivalent cross-sectional area, \( \mu_{a} \) is the permeability of material \( a \). The permeability of ferrite material is much larger than that of air, so the reluctance of ferrite core is much smaller than that of air and can be ignored.
Taking the calculation of reluctance $R_{\alpha P1}$ as an example, the magnetic circuit modeling method is introduced.

In Fig. 10, according to the formula (2), the differential reluctance $dR_{\alpha P1}$ along the radius $r$ direction can be obtained as follows:

$$dR_{\alpha P1} = \frac{\pi r}{\mu_0 \cdot 2I_0 dr} = \frac{\pi r}{2\mu_0 l dr}$$

(3)

where $\mu_0$ is the permeability of air, and the value is $\mu_0 = 4\pi \times 10^{-7}\text{H/m}$. The transmitting coil turns $N_{\alpha P1}$ surrounded by the differential element can be approximately expressed as:

$$N_{\alpha P1} = \frac{2r}{2wP_2} \cdot N_P = \frac{r}{wP_2} \cdot N_P$$

(4)

where $N_P$ is the transmitting coil turns. According to the Ohm’s law of magnetic circuit, the following can be obtained:

$$N_{\alpha P1} I_P = d\Phi_{\alpha P1} dR_{\alpha P1}$$

(5)

Substituting (3), (4) into (5), the differential magnetic flux $d\Phi_{\alpha P}$ is obtained as:

$$d\Phi_{\alpha P} = \frac{N_{\alpha P1} I_P}{\mu_0 l (NPdPdr)} = \frac{N_{\alpha P1} I_P}{\pi wP_2}$$

(6)

According to the principle of flux linkage equality, the primary equivalent leakage flux linkage which can be equivalent to a concentric semicircle closed along the ferrite core with $O_{P1}$ as the circle center can be obtained as follows:

$$\psi_{\alpha P1} = N_P \Phi_{\alpha P1} = \int N_{\alpha P1} d\Phi_{\alpha P1}$$

(7)

Formula (4), (6) and (7) simultaneous, we can obtain the primary equivalent leakage flux $\Phi_{\alpha P1}$ which can be equivalent to a concentric semicircle closed along the ferrite core with $O_{P1}$ as the circle center:

$$\Phi_{\alpha P1} = \frac{2\mu_0 l NPdP}{\pi wP_2} \int_0^{h_P + 2h} rdr = \frac{2\mu_0 l (h_P + 2h)^2 NPdP}{\pi wP_2}$$

(8)

At the same time, according to the Ohm’s law of magnetic circuit, the magnetomotive force of transmitting coil can be obtained as follows:

$$F = NPdP = \Phi_{\alpha P1} R_{\alpha P1}$$

(9)

From (8) and (9), the equivalent reluctance $R_{\alpha P1}$ is obtained as:

$$R_{\alpha P1} = \frac{NPdP}{\Phi_{\alpha P1}} = \frac{\pi wP_2^2}{\mu_0 l (h_P + 2h)^2}$$

(10)

Similarly, the corresponding reluctance calculation results are shown in Table 1.

The equivalent magnetic circuit of the cross-type magnetic coupler in Fig. 8 can finally be obtained as shown in Fig. 11.

$N_S$ is the receiving coil turns. In Fig. 11, that equivalent magnetic circuit is divided into three sub-loops, which is $\alpha$, $\beta$ and $\gamma$. The sub-loop $\alpha$ represents the flux only passes through the transmitter pad, so it corresponds to the primary leakage magnetic circuit. The sub-loop $\beta$ represents the flux passes through both the transmitter pad and the receiver pad, so it corresponds to the magnetizing circuit. Similarly, the sub-loop $\gamma$ represents the flux only through the receiver pad, so it corresponds to the secondary leakage magnetic circuit.

The relationship between the corresponding reluctance and the inductance can be calculated as follows:

$$\begin{align*}
L_{\alpha P} &= \frac{N_P^2}{R_{\alpha P}} \\
L_m &= \frac{N_P N_S}{R_m} \\
L_{\alpha S} &= \frac{N_S^2}{R_{\alpha S}}
\end{align*}$$

(11)

where $L_m$ is the magnetizing inductance, $L_{\alpha P}$ and $L_{\alpha S}$ are the primary leakage inductance and the secondary leakage inductance, respectively. In order to express the circuit relationship of the corresponding inductance more clearly, the equivalent magnetic circuit in Fig. 11 can be converted into the circuit in Fig. 12.
From Fig. 12, the circuit consists of a magnetizing circuit and an ideal transformer with variable ratio \( n \), where \( n = N_p/N_s \), and it ignores the internal resistance of the magnetic coupling coils.

### C. SYSTEM CIRCUIT MODELING

When the parasitic resistance of the coils should be taken into consideration and the LCL-S compensation described above is added in Fig. 12, the T-type equivalent circuit which is converted to the primary side is obtained, as shown in Fig. 13. The variables relationship between the secondary side and the primary side is as follows:

\[
\begin{align*}
U'_2 &= nU_2 \\
I'_2 &= I_2/n \\
Z'_2 &= n^2Z_2
\end{align*}
\]

(12)

From (12), \( U_2, I_2 \) and \( Z_2 \) are the voltage, current and impedance of the secondary side, respectively. \( U'_2, I'_2 \) and \( Z'_2 \) are the voltage, current and impedance converted from the secondary side to the primary side, respectively.

In Fig. 13, the conversion relationship between the primary leakage inductance \( L_{\sigma P} \), the secondary leakage inductance \( L_{\sigma S} \) and the magnetizing inductance \( L_m \) and the primary self-inductance \( L_p \), the secondary self-inductance \( L_S \) and mutual inductance \( M \) described above are as follows:

\[
\begin{align*}
L_p &= L_{\sigma P} + L_m \\
L_S &= L_{\sigma S} + L_m/n^2 \\
M &= L_m/n
\end{align*}
\]

(13)

According to formula (13), when the parasitic resistance of the coils and compensation structure are considered, the circuit in Fig. 13 can be equivalent to the mutual coupling circuit shown in Fig. 2, and thus the circuit model is unified with the magnetic circuit model. In this paper, the compensation inductance and magnetic coupler are wound by Litz wires, and its parasitic resistance is very small. Therefore, the parasitic resistance of the compensation inductor and coupling coil can be ignored in the analysis process.

From Fig. 13, the total impedance of the secondary circuit can be expressed as

\[
Z_S = j\omega L_{\sigma S} + \frac{1}{j\omega C_S} + R_{eq}
\]

(14)

In order to achieve maximum output power and transmission efficiency, meanwhile minimizing the VA rating of the power supply, the system should operate at resonant. When the secondary circuit resonates, the \( L_m \) is converted to the secondary side. The resonant frequency \( \omega \) is

\[
\omega = \frac{1}{\sqrt{(L_{\sigma S} + L_m/n^2)C_S}}
\]

(15)

Now secondary circuit total impedance changes to

\[
Z_S = Z_{eq} - j\omega L_m/n^2
\]

(16)

\( Z_S \) is converted to the primary side to get:

\[
Z'_S = n^2Z_S = R_{eq} - j\omega L_m
\]

(17)

The reflect impedance of the secondary circuit equivalent to the primary side is

\[
Z'_r = j\omega L_m \parallel Z'_S = \frac{\omega^2L_m^2 + j\omega L_mR_{eq}}{R_{eq}}
\]

(18)

Therefore, Fig. 13 circuit can be equivalent to primary equivalent circuit as shown in Fig. 14.

From Fig. 14, the total impedance of primary circuit is

\[
Z_P = j\omega L_1 + \frac{1}{j\omega C_P} \parallel (j\omega L_{\sigma P_1} + Z'_r)
\]

\[
= \frac{Z_1'(1 - \omega^2C_P L_1) + j\omega \left[(L_1 + L_{\sigma P_1}) - \omega^2C_P L_1L_{\sigma P_1}\right]}{(1 - \omega^2C_P L_1) + j\omega C_P Z'_1}
\]

(19)

where \( L_{\sigma P 1} = L_{\sigma P 1}/1/\omega^2C_1 \), which is the residual leakage inductance of \( L_{\sigma P} \) compensated by \( C_1 \).

In Fig. 13, when the primary circuit resonates, the resonance frequency is the same as the secondary circuit, that is

\[
\omega = \frac{1}{\sqrt{(L_{\sigma P 1} + L_m)C_P}}
\]

(20)

\( L_1 = L_{\sigma P 1} + L_m \). The primary circuit total impedance is

\[
Z_P = \frac{j\omega L_1^2}{L_m + j\omega C_P Z'_1L_1}
\]

(21)

As can be seen from Fig. 14 and combine with formula (13). The excitation current flowing through the primary circuit is

\[
I_P = \frac{U_{AB}}{Z_P} \cdot \frac{1}{j\omega C_P} \parallel \left(\frac{1}{j\omega C_P} + (j\omega L_{\sigma P 1} + Z'_r)\right) = \frac{U_{AB}}{j\omega L_1}
\]

(22)
As long as the inverter output voltage and the system resonant frequency are constant, the primary excitation current can be kept constant, and thus the energy can be transferred steadily to the secondary side. The voltage of reflect impedance $Z'_e$ is

$$U'_e = I_P Z'_e = \frac{U_{AB} (\omega^2 L_m^2 + j \omega L_m R'_e)}{j \omega L_1 R'_e} \quad (23)$$

When the secondary side is operated at resonant frequency and combine with formula (13), the rectifier input voltage of the secondary side converted to the primary side is as follows

$$U'_ab = U'_e \cdot \frac{R'_e}{Z'_S} = \frac{L_m U_{AB}}{L_1} \quad (24)$$

$U'_{ab}$ is converted to the secondary side to get:

$$U_{ab} = \frac{U'_{ab}}{n} = \frac{L_m U_{AB}}{n L_1} = \frac{M U_{AB}}{L_1} \quad (25)$$

It can be seen from formula (25) that the primary compensation inductance and mutual inductance remain unchanged in the process of static wireless charging. As long as the inverter output voltage is constant, the rectifier input voltage can be guaranteed to be constant and the characteristics of the voltage source can be obtained. The rectifier input voltage can be improved by properly increasing the ratio of mutual inductance to primary compensation inductance.

In order to analyze easily the influence of the primary and the secondary self-inductances on the system output power and efficiency, the proportional coefficient $\lambda$ of the primary compensation inductance $L_1$ and the primary self-inductance $L_p$ is defined as follows:

$$\lambda = \frac{L_1}{L_p} \quad (26)$$

When the resistance of the coils is considered and combine with formula (13) and (26), the rectifier output power and efficiency are obtained as shown in formula (27) and (28), respectively.

$$P_{out} = \frac{|U_{ab}|^2}{R_{eq}} = \frac{M^2 U_{AB}^2 R_{eq}}{A^2} \quad (27)$$

$$\eta_{out} = \frac{|I_s|^2 R_{eq}}{|I_s|^2 R_{eq} + |I_s|^2 R_S + |I_p|^2 R_P + |I_1|^2 R_1} = \frac{\omega^2 M^2 R_{eq} R_p (R_{eq} + R_S)^2 + \omega^2 B^2 R_1}{\omega^2 M^2 (R_{eq} + R_S) + \omega^2 M^2 R_{eq} + \omega^2 B^2 R_1} \quad (28)$$

$$A = (\lambda L_P + C_P R_I R_P) \left( R_{eq} + R_S \right) + \omega^2 M^2 C_P R_1 \quad (29)$$

$$B = C_P \left[ R_P \left( R_{eq} + R_S \right) + \omega^2 M^2 \right] \quad (30)$$

In Fig. 2, the system resonant network only allows the fundamental harmonic to pass, which plays the role of band-pass filter, and thus it only needs to consider the fundamental harmonic in the analysis. For static wireless charging, the inverter can adopt complementary control mode with $180^\circ$. The fundamental effective value of the inverter output voltage can be obtained by fourier decomposition [23].

$$U_{AB} = \frac{2\sqrt{2}}{\pi} U_{in} \quad (31)$$

In (31), $U_{in}$ is the system input DC voltage. Since the output of LCL-S compensation structure is of a voltage source characteristic and the rectifier requires a large capacitance in parallel to smooth the output voltage, therefore, the relationship between the input and output equivalent load resistance $R_{eq}$ and $R_L$ of the rectifier is as follows [24]:

$$R_{eq} = \frac{8}{\pi^2} R_L \quad (32)$$

In order to better analyze the characteristics of lithium battery, the electrical model of lithium battery is established [25]. However, it is difficult to determine the parameters in the equivalent circuit model of lithium battery. The battery is usually equivalent to a varying resistance. $U_b$ and $I_b$ are charging voltage and current for the battery, respectively. $R_b$ is equivalent resistance of the battery. The rectifier output voltage $U_{out}$ is approximately constant in the charging process, but the equivalent charging resistance $R_b$ will change. Therefore, the charging voltage $U_b$ and charging current $I_b$ can meet the battery charging requirements by adjusting the duty cycle $D$ of the switch $S_3$. The output equivalent load resistance $R_L$ of the rectifier is obtained as follows:

$$R_L = \frac{R_b}{D^2} \quad (33)$$

### IV. MAGNETIC COUPLER DESIGN

#### A. DESIGN INDEX PROPOSED

In this paper, 84V DC voltage source is used as the system input voltage. This paper adopts a single phase voltage inverter and a constant frequency control mode to keep the inverter frequency $f$ constant at 50kHz, and the system circuit can always be operated in the resonance state. The single phase uncontrollable rectifier and Buck circuit are selected as the secondary power management circuit. The input voltage range of DC-DC converter is required from 40V to 48V. The battery of UAV adopts lithium battery whose capacity is 10000mAh, nominal voltage is 22.2V, maximum charging voltage is 25.2V, and the required charging rate is from 0.5C to 1C. The specific design requirements are shown in Table 2.

| Parameters                      | Value  |
|---------------------------------|--------|
| DC voltage source $U_b$/V       | 84     |
| Working frequency of the inverter circuit/fkHz | 50     |
| DC-DC converter input voltage $U_{in}$/V   | 40-48  |
| Lithium battery capacity $C_b$/mAh | 10000  |
| Nominal voltage for lithium battery $U_{b0}$/V | 22.2   |
| Maximum charging voltage for lithium battery $U_{max}$/V | 25.2   |
| Charging current for lithium battery $I_b$/A | 5-10   |
| Charging power for lithium battery $P_b$/W | 126-252 |

TABLE 2. Specific design requirements of IPT system.
The coupling coefficient $k$ of the magnetic coupler designed in this paper should be more than 0.3. Considering that the Buck circuit will produce about 4% loss, the output power range of the rectifier output equivalent load resistance $R_L$ is from 131.25W to 262.5W, and considering the loss of inverter and rectifier, there should be a certain margin for the rectifier output power. Therefore, the rectifier maximum output power is approximately 300W and the output efficiency is more than 90% to meet the battery charging requirements.

From formulas (27) and (28), the proportional coefficient $\lambda$ will affect the output power and efficiency of the rectifier. Selecting the appropriate proportional coefficient $\lambda$ can not only improve the secondary induced voltage to improve the system power transmission capability, but also weigh the rectifier output power and efficiency, which can be maintained in a high level. When the different mutual inductances $M$ are selected, the relationship between the rectifier output power $P_{out}$, efficiency $\eta_{out}$ and the proportional coefficient $\lambda$ is shown in Fig. 15.

In Fig. 15, with the increase of the $\lambda$, the rectifier output power decreases gradually and approaches to stability, but the IPT system efficiency increases gradually and tends to be stable. The proportional coefficient $\lambda$ should be chosen where the rectifier output power and efficiency are high and stable. Therefore, in this paper, $\lambda = 0.5$, that is, $L_1 = 0.5L_p$.

From Fig. 2 and formula (27)-(33), assuming that the coupling coefficient $k$ is 0.3, the resistance of the coils and compensation inductance are 0.1$\Omega$. The system input DC voltage $U_{in}$ is 84V, and the proportional coefficient $\lambda$ is 0.5. When the magnetic coupler is in a well-aligned condition, the DC-DC converter input voltage $U_L$ is 48V. The battery is charged with the maximum charging current $I_{bmax}$ of 10A until the maximum charging voltage $U_{bmax}$ of 25.2V is reached. So the equivalent load resistance of the charged battery $R_b = 25.2V/10A=2.52\Omega$ at the maximum charging power point $P_{bmax}$ of 252W, and the duty cycle of the switch $S_I\Delta D = 25.2V/48V\approx 0.525$. According to formula (33), when the equivalent load resistance of the rectifier $R_L$ is 9$\Omega$ ($2.52\Omega/0.525^2 = 9\Omega$), the transferred power to the battery corresponds to the maximum point. Therefore, a load resistance of 9$\Omega$ can be used to evaluate the system performance very well. The primary excitation voltage $U_p$ cannot exceed 400V due to the limitation of insulation and safety standards in this paper. And the primary excitation current $I_p$ should be below 12A to limit the $I^2R$ losses. According to the formula (22), (26), (31) and $L_p = U_p\omega /joL_p$, the variation range of the primary self-inductance $L_p$ is calculated to be 40-106$\mu$H. Considering a certain safety margin, the variation range of the $L_p$ is 50-100$\mu$H. According to formula (32), the input equivalent load resistance $R_{eq}$ at the maximum charging power point is 7.3$\Omega$. In this paper, the secondary quality factor $Q_2$ is 2-5, and combined with $L_S = Q_2R_{eq}/\omega$, the variation range of secondary self-inductance $L_S$ is 46-116$\mu$H. Considering a certain margin, the variation range of $L_S$ is 50-100$\mu$H. According to formula (27)-(30), when the $R_L$ is 9$\Omega$, the three-dimensional scanning diagram of the rectifier output power and efficiency with magnetic coupler self-inductances is obtained by MATLAB as shown in Fig. 16. The rectifier output power and efficiency increase with the decrease of $R_L$ and $L_p$ but the increase of $L_S$. When the $R_L$ is 9$\Omega$, the $L_p$ changes from 71.7$\mu$H to 100$\mu$H and the $L_S$ changes from 50$\mu$H to 84.2$\mu$H, the rectifier output power varies approximately from 138.2W to 318.6W and the output efficiency is more than 90%, which can meet the requirements of the rectifier output power and efficiency.

### B. GEOMETRY PARAMETERS DESIGN

As one of the key components of IPT system, the magnetic coupler geometry parameters includes multiple parameters, which is closely related to the system power transfer capability. And the system output power and efficiency are important parameters reflecting the system power transfer capability. The trade-off of the multiple geometry parameters and the system output power and efficiency can save the cost of manufacturing the magnetic coupler, and also ensure the system power transfer capability. In this paper, an iterative method is proposed to optimize the magnetic coupler geometry parameters. Firstly, the variation range of the primary and secondary self-inductances are obtained according to the design index of the system output power and efficiency, and then the relationship of the self-inductance, mutual inductance and the magnetic coupler geometry parameters are obtained according to the magnetic circuit model. Then the geometry parameters satisfying requirements are screened out by the iterative method, and the output power and efficiency corresponding to these geometry parameters are compared one by one to determine the final geometry parameters of the magnetic coupler. And the design considering the magnetic coupler geometry parameters and the system output power and efficiency is completed. The specific method is as follows:
From Fig. 7 (b), the Litz wire with size of 0.1mm×400 is adopted and its equivalent diameter $d$ is 2.75mm. The transmitting coil is wound up one layer, and its thickness $h_P$ is 2.75mm. The receiving coil is wound up three layers to reduce the UAV landing gear space occupied by the receiving coil, and its thickness $h_{S2}$ is 8.25mm. The air gap $h$ between the transmitter pad and receiver pad is 2mm. According to the UAV’s space limitation, constraints of the magnetic coupler geometry parameters are obtained as follows:

Because the receiving coil is installed on UAV’s two landing gears, some geometry parameters of magnetic coupler will be limited. The length of the UAV landing gear is 180mm, so the $l_{S2}$ is set as 180mm accordingly. At this time, the $l_P$ should choose the appropriate range according to $l_{S2}$. For receiving coil, $l_P$ is too long to fully receive the magnetic field generated by the transmitter pad. And if $l_P$ is too short, the Y-axis direction misalignment tolerance of magnetic coupler will be insufficient. So $l_P$ is required to vary from 50mm to 350mm. Similarly, the distance between the UAV’s two landing gears is 124 mm, so the middle coil outer width $w_{P4}$ is 124 mm. The receiving coil outer height $h_{S3}$ should also be reasonably selected according to $w_{P4}$, which should not exceed the UAV’s landing gear height $h_l$. The coupling capability of the magnetic coupler will be reduced due to the lack of the magnetic field received by the receiving coil, caused by low $h_{S3}$. If $h_{S3}$ is too high and the secondary leakage flux will cause electromagnetic interference to the UAV. Therefore, the variation range of $h_{S3}$ is from 20mm to 140mm. And the coupling coefficient $k$ is an important parameter to reflect the coupling capability of the magnetic coupler. Therefore, the influence of the $l_P$ and the $h_{S3}$ variation on the $k$ can be studied, respectively, to determine the appropriate values of $l_P$ and $h_{S3}$, as shown in Fig. 17.

In Fig. 17, with the increase of $l_P$ and $h_{S3}$, the $k$ increases at first and then decreases gradually. When $l_P = 204$mm and $h_{S3} = 87$mm, the $k$ reaches the maximum value. Therefore, the transmitting coil outer length $l_P$ is 204mm and the receiving coil outer height $h_{S3}$ is 87mm to improve the coupling capability. The ferrite core dimension is also an important aspect to be considered. The rectangular ferrite core dimension is too small to restrain the flux lines, leading to the lack of coupling capability of the magnetic coupler. While the rectangular ferrite core dimension is so large to waste the ferrite core material. Therefore, the rectangular ferrite core length $l_f$ varies from 92mm to $l_{P1}$, and the rectangular ferrite core width $w_f$ varies from 108mm to $2(w_{P1} + w_{P2})$. According to the magnetic circuit model established above, the self-inductance and mutual inductance of magnetic coupler are independent with the rectangular ferrite core thickness $h_f$. In order to save the ferrite core material, a thinner core can be chosen as far as possible, so the rectangular ferrite core with the thickness $h_f = 17$mm can be selected.

Assuming $N_{P1}$ is the per transmitting coil turns and $N_{S1}$ is the per layer turns of each receiving coil. $N_P = 3N_{P1}$, $N_S = 6N_{S1}$. The $N_{P1}$ range is 4-10 turns, and the $N_{S1}$ range is 1-7 turns. According to the relationship of the magnetic coupler geometry parameters in Fig. 7(b), we can get $h_{S1} = 70.5$mm and $l_{S1} = 163.5$mm. The following relationship can be obtained:

$$w_{P2} = 2.75 \times 10^{-3}N_{P1}$$  \hspace{1cm} (34)
$$w_{S} = 2.75 \times 10^{-3}N_{S1}$$ \hspace{1cm} (35)
$$l_{P1} = 0.204 - 5.5 \times 10^{-3}N_{P1}$$ \hspace{1cm} (36)
$$w_{P3} = 2.75 \times 10^{-3}N_{P1} + 0.062$$ \hspace{1cm} (37)
$$w_{P1} = w_{P3} - 5.5 \times 10^{-3}N_{P1}$$ \hspace{1cm} (38)

Combined with the expression of the corresponding reluctance in Table 1, as well as formulas (11) and (13), the relationship between self-inductance and mutual inductance of magnetic coupler and various dimensions can be obtained as follows:

$$M = \left[3.6 \times 10^{-6}N_{P1}N_{S1}I_l \ln (w_f/0.0135)\right]/n$$ \hspace{1cm} (39)
$$L_P = nM + m_1$$ \hspace{1cm} (40)
$$L_S = M/n + m_2$$ \hspace{1cm} (41)

In (40) and (41), respectively, $m_1$ represents $1.8 \times 10^{-6}N_{P1}^2 (4w_{P1} + 0.011N_{P1} + 0.204) + 2.169 \times 10^{-5}l_f$ and $m_2$ represents $3.6 \times 10^{-6}N_{S1}^2 [0.329 \ln (28.636/N_{S1}) + 0.251]$. According to the relationship between the electric circuit model and the magnetic circuit model, the appropriate geometry parameters of the magnetic coupler are designed. The flowchart for the geometry parameters design of the magnetic coupler is shown in Fig. 18.

The program in Fig. 18 is written by Visual C++, and the iterative operation is carried out. The geometry parameters of the magnetic coupler that satisfy the requirements can be selected efficiently, and the specific parameters are shown in Table 3.

The relationship between the data of each group in Table 3 and the rectifier output power $P_{out}$ and efficiency $\eta_{out}$ is obtained by substituting the data of each group in Table 3 into (27) and (28), as shown in Fig. 19.

From Fig. 19, the theoretical value of the IPT system efficiency with each group is more than 96%, because the loss of the inverter and rectifier are ignored. In this paper, the rectifier maximum output power is 262.5W, and considering the loss of inverter and rectifier, there should be
uniformity of magnetic field and cost, a plurality of ferrite bars are selected to replace a whole piece of ferrite when the magnetic coupler is actually manufactured, and these ferrite bars are standard. When two ferrite bars are selected to replace the whole piece of ferrite, the magnetic field will not be uniform, which will increase the misalignment sensitivity. When three ferrite bars are selected, the magnetic field will be more uniform and the system misalignment sensitivity will be lower. When four or more ferrite bars are selected that the magnetic field will be more uniform than that of magnetic field with three ferrite bars, but in the later batch production, multiple ferrite bars will increase undoubtedly the assembly difficulty. Therefore, considering synthetically the uniformity of magnetic field and the assembly difficulty, three ferrite bars are selected to replace the whole piece of ferrite in this paper. Each ferrite bar length $l_{f2} = l_{f}/3 = 34$mm, and the gap $l_{f1}$ between the ferrite bars is 28mm. The cross-type magnetic coupler specific parameters are shown in Table 4.

According to the parameters of magnetic coupler in Table 4, $L_p = 80.3 \mu H$, $L_s = 75.9 \mu H$ and $M = 25.6 \mu H$, measured by LCR impedance analyzer. The comparison shows that there is a slight difference between two results mentioned above, which proves the magnetic circuit model is accurate. The specific parameters of the entire IPT system for UAV in Fig. 2 are finally determined as shown in Table 5,
and based on the data in Table 4, the physical diagram of cross-type magnetic coupler is shown in Fig. 20.

C. MISALIGNMENT TOLERANCE ANALYSIS

The compensation capacitance is calculated according to the system inductance parameter when the magnetic coupler is aligned well. However, when the magnetic coupler is misaligned, the compensation capacitance value will not change. This requires that the $L_p$ and $L_s$ should be kept stable in misalignment so that it cannot affect the system operating state. At the same time, the $M$ reflects the system power transmission capability, which requires $M$ should not be reduced greatly in misalignment, so as to ensure the stability of the rectifier output voltage and output power. Therefore, the $L_p$, $L_s$ and $M$ are important parameters to represent the system misalignment tolerance capability [26]. The misalignment tolerance of the cross-type magnetic coupler is analyzed in Fig. 20. The curves for the self-inductance and mutual inductance of the cross-type magnetic coupler with misalignment are obtained as shown in Fig. 21.

In Fig. 21, when the magnetic coupler changes from full alignment to misalignment 40mm along the X-axis direction, Y-axis direction and rotation misalignment, the maximum variation of $L_p$ is 0.62 $\mu$H, 0.61 $\mu$H and 0.55 $\mu$H, respectively. The maximum variation of $L_s$ is 1.46 $\mu$H, 0.35 $\mu$H and 0.97 $\mu$H, respectively. Therefore, the misalignment of magnetic coupler has a minor effect on the self-inductance. It will also not affect the system working state. When the magnetic coupler misalignment 25mm along the X-axis direction, misalignment 40mm along the Y-axis direction and rotation misalignment 25°, the $M$ decreases to 17.4 $\mu$H, 22.8 $\mu$H and 20.9 $\mu$H, respectively. At this time, the $M$ change will not have a great effect on the rectifier output voltage and output power. However, when the magnetic coupler along the X-axis direction misalignment is more than 25mm, along the Y-axis direction misalignment is more than 40mm, or rotation misalignment is 25°, the $M$ will be reduced greatly, which will compromise the system power transmission capability. Therefore, the cross magnetic coupler has the misalignment range of X-axis direction $[-25mm, 25mm]$, Y-axis direction $[-40mm, 40mm]$, and rotation $[-25°, 25°]$. The influence of misalignment on the system will be further discussed later.

D. MAGNETIC FIELD ANALYSIS

In this paper, the $I_p$ and $I_s$ of the magnetic coupler should not exceed 12A, and the ampere turns of transmitter pad is set to 408A·N. From Fig. 21, the X-axis direction misalignment has the greatest influence on the system, so the peak magnetic field distributions of the cross-type magnetic coupler considering complete alignment and the X-axis direction maximum misalignment position are obtained by ANSYS Maxwell software for 3D simulation as shown in Fig. 22.

From Fig. 22, the magnetic field distribution is consistent with the modeling analysis of the magnetic coupler mentioned above. The peak magnetic field distributions of the misalignment case is not much different from that of the complete alignment case. But in the case of misalignment, the main flux will be decreased and the leakage flux will be increased, which is also the main reason for the decrease of the $M$ and $k$. When the height is greater than 121mm, the flux density of magnetic coupler is less than $1 \times 10^{-5}$T. Therefore, it will not cause the damage to UAV’s internal equipment by
high frequency magnetic field. The saturation of the magnetic core will cause the magnetic coupler temperature rising and the core loss increasing, so the saturation of the magnetic core should be considered in the design for wireless charging system. The PC40 ferrite core material of TDK company is used in this paper, whose saturation flux is 0.51T at 25°C, but the peak flux density of magnetic coupler is $3 \times 10^{-4}$T which is much lower than the saturation flux density. Therefore, the problem of saturation of the magnetic core will not occur.

V. EXPERIMENTAL VERIFICATION

The IPT system experimental platform with a cross-type magnetic coupler is shown in Fig. 23. It contains an input DC voltage source, a drive voltage source, a DSP controller core board, an inverter circuit, a magnetic coupler, a compensation inductance, three compensation capacitances, a rectifier circuit, an electronic load, an oscilloscope and a power analyzer. The input voltage is 84V, the inverter working frequency is 50kHz, the load resistance $R_L$ of rectifier is 9Ω, and the cross-type magnetic coupler works in a well-aligned condition.

The inverter output voltage and current and the rectifier input voltage and current waveform considering complete alignment and the maximum position of the X-axis direction misalignment are shown in Fig. 24. It can be seen that the output voltage and current of the maximum tolerated misalignment position of the X-axis direction are in the same phase compared with the complete alignment, indicating that the system is still in a resonant state. The system power transfer capability is tested by using power analyzer as shown in Fig. 25. The rectifier output power $P_{out}$ is 259.9W and the IPT system efficiency $\eta_4$ is 91.577%. When the charging voltage for lithium battery reaches the maximum charging voltage $U_{bmax}$, the duty cycle of the switch $S_5 D = 25.2V/48.47V = 0.52$, the charging current for lithium battery $I_b = 5.362A/0.52=10A$ which is the maximum charging current for lithium battery $I_{bmax}$, which meets the requirement of maximum charging power point for lithium battery. It can ensure that when the magnetic coupler is in a well-aligned operating condition, adjusting the duty cycle $D$ can make the system maintain a constant maximum charging current $I_{bmax}$ to charge lithium battery.
η\text{P}\text{is }39.69-48.47\text{V}, \text{alignment to rotation misalignment }25^\circ 91.577\%. \text{When the magnetic coupler is displaced from range is }208.8-259.9\text{W, and }\eta\text{ quickly until the maximum charging voltage }U_{\text{bmax}}\text{. Therefore, the experimental system can be used to charge UAV wirelessly.}

When the rectifier output equivalent load resistance \(R_L\) is 9Ω, the system misalignment test is carried out, with test results shown in Fig. 26. In Fig. 26, when the magnetic coupler is displaced from alignment to X-axis direction misalignment 25mm, the rectifier output voltage \(U_L\) variation range is 36.85-48.47V, the rectifier output power \(P_{\text{out}}\) variation range is 150.2-259.9W, and the IPT system efficiency \(\eta_{\text{out}}\) variation range is 90.314%-91.577%. When the magnetic coupler is displaced from alignment to Y-axis direction misalignment 40mm, \(U_L\) variation range is 43.41-48.47V, \(P_{\text{out}}\) variation range is 208.8-259.9W, and \(\eta_{\text{out}}\) variation range is 91.282%-91.577%. When the magnetic coupler is displaced from alignment to rotation misalignment 25°, \(U_L\) variation range is 39.69-48.47V, \(P_{\text{out}}\) variation range is 169.3-259.9W, and \(\eta_{\text{out}}\) variation range is 90.75%-91.577%. All of the above meet the requirements of UAV wireless charging. Therefore, the misalignment tolerance capability of IPT system is set as X-axis direction \([-25\text{mm}, 25\text{mm}]\), Y-axis direction \([-40\text{mm}, 40\text{mm}]\), and rotation misalignment \([-25^\circ, 25^\circ]\).

VI. CONCLUSION
At first, a cross-type magnetic coupler for UAV has been proposed in this paper, which has restrained effectively the magnetic field height. Secondly, the system magnetic circuit and electric circuit models have been established, whilst a simple and practical iterative method for optimizing the magnetic coupler geometry parameters has been proposed. Then the geometry parameters of the cross-type magnetic coupler have been calculated which have met the charging requirements of lithium battery. It has shown that the magnetic coupler could restrain the magnetic field effectively within the 145mm height above the transmitter pad and avoid the influence of high frequency magnetic field on UAV’s internal equipment. At last, the experimental system has been built, and the system misalignment tolerance capability has been obtained. It has been verified that the system can transfer 260W power with the IPT system efficiency of 91.577%. The model can be used to guide the wireless charging system design for special applications and special requirements for magnetic coupler, which refer to the limitation of the space occupied by the magnetic coupler and the strict limitation of the magnetic field height.

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FIGURE 26. Misalignment test results.
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