Sivers function in a spectator model with axial-vector diquarks

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We perform a calculation of the Sivers function in a spectator model of the nucleon, with scalar and axial-vector diquarks. We make use of gluon rescattering to produce the nontrivial phases necessary to generate the Sivers function. The inclusion of axial-vector diquarks enables us to obtain a nonzero Sivers function for down quarks. Using the results of our model, we discuss the phenomenology of transverse single spin asymmetries in $\pi^+$, $\pi^-$, and $\pi^0$ production, which are currently analysed by the HERMES and COMPASS collaborations. We find that the inclusion of axial-vector diquarks substantially reduces the asymmetries.

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I. INTRODUCTION

The Sivers function was introduced for the first time in Ref. [1], in an attempt to explain the observation of single-spin asymmetries in hard hadronic reactions. Since then, some phenomenological extractions of the Sivers function have been performed [2, 3, 4], from data on pion production in proton-proton collisions [5, 6]. The Sivers function gives a contribution also to the single-spin asymmetry observed by the HERMES collaboration in pion production via deep inelastic scattering off polarized targets [7, 8, 9]. In all the above cases, however, the presence of competing effects (in particular the Collins effect) did not allow clear conclusions up to now [3, 10].

Despite the phenomenological indications, for several years the Sivers function was believed to vanish due to time-reversal invariance [11]. However, this statement was contradicted by an explicit calculation by Brodsky, Hwang and Schmidt, using a spectator model [12]. As the Sivers function is an example of T-odd entity, it requires the interference between two amplitudes with different imaginary parts [11, 13]. Spectator models at tree level cannot provide these nontrivial phases, but they can arise as soon as a gluon is exchanged between the struck quark and the target spectator [12]. More generally, the presence of the gauge link, which insures the color gauge invariance of parton distributions, can provide nontrivial phases and thus generate T-odd functions [11, 13, 14, 15, 16]. The main ingredient of the model calculation of [12] is nothing else than the one-gluon approximation to the gauge link. It is also interesting to note that T-odd distribution functions vanish in a large class of chiral soliton models, where gluonic degrees of freedom are absent [15].

The work of Brodsky, Hwang and Schmidt was not aimed at producing a phenomenological estimate. A step forward in this direction has been accomplished in Refs. [19, 20]. In our article, we present an alternative calculation, using the version of the spectator model presented by Jakob, Mulders and Rodrigues in Ref. [21]. In particular, we include in the model a dynamical axial-vector diquark as a possible spectator, and we explore the Sivers function for down quarks. The necessity to include axial-vector diquarks is also discussed, e. g., in Refs. [22, 23, 24]. Finally, we point out that a calculation of the Sivers function in the MIT bag model has been recently presented in Ref. [25].

II. UNPOLARIZED DISTRIBUTION FUNCTION $f_1$

The unpolarized distribution function $f_1$ can be defined as

$$f_1(x,\vec{k}_T) = \frac{1}{4} \text{Tr} \left[ (\Phi(x,\vec{k}_T; S) + \Phi(x,\vec{k}_T; -S)) \gamma^+ \right],$$

where $\Phi(x,\vec{k}_T; S)$ is the parton distribution function.

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\[ \Phi(x, k_T; S) = \int \frac{d\xi}{(2\pi)^3} e^{+ik\xi} \langle P, S \rangle \langle \psi(0) | \mathcal{L}_{[0-, \xi]} \mathcal{L}_{[0-, \xi]} \mathcal{L}_{[\infty, \xi]} | \psi(\xi) | P, S \rangle |_{\xi^+=0}, \]  

where the notation \( \mathcal{L}_{[a,b]} \) indicates a straight gauge link running from \( a \) to \( b \). In Drell-Yan processes the link runs in the opposite direction, to \(-\infty\) \([17]\). For the calculation of the unpolarized function \( f_1 \), the transverse part of the gauge link does not play a role and the entire gauge link can be reduced to unity. Therefore, for this first part of the calculation it is sufficient to consider only the handbag diagram.

At tree level, we follow almost exactly the spectator model of Jakob, Mulders and Rodrigues \([21]\). In this model, the proton (with mass \( M_\text{p} \) can couple to a constituent quark of mass \( m \) and a diquark. The diquark can be both a scalar particle, with mass \( M_s \), or an axial-vector particle, with mass \( M_v \). The relevant diagram at tree level (identical for the scalar and axial-vector case) is depicted in Fig. 1 (a). In our model, the nucleon-quark-diquark vertices are

\[ \Upsilon_s = g_s(k^2), \quad \Upsilon_v = \frac{g_v(k^2)}{\sqrt{2}} \gamma_5 \gamma^\mu. \]

We make use of the dipole form factor

\[ g_{s/v}(k^2) = N_{s/v} \frac{(k^2 - m^2)(1-x)^2}{(k_T^2 + L_{s/v}^2)^2}, \]

where

\[ k_T^2 = -(1-x)k^2 - xM_{s/v}^2 + x(1-x)M^2, \]
\[ L_{s/v}^2 = (1-x)\Lambda^2 + xM_{s/v}^2 - x(1-x)M^2. \]

The only difference with respect to Ref. \([21]\) is the form of \( \Upsilon_v \) — the vertex involving nucleon, quark, and axial-vector diquark. This change modifies the original results only slightly. Note that our choice of the form factor, defined in Eq. \([17]\), is very different from the Gaussian form factor employed in Ref. \([19]\). Both choices have the effect of eliminating the logarithmic divergences arising from \( k_T \) integration and suppress the influence of the high \( k_T \) region, where anyway perturbative corrections should be taken into account \([21]\).

The final results for the unpolarized distribution function \( f_1 \) are

\[ f_1^s(x, k_T^2) = \frac{g_s^2}{2(2\pi)^3} \frac{1}{(1-x)} \frac{\left[(xM + m)^2 + k_T^2\right]}{(k_T^2 + L_s^2)^2} = \frac{N_s^2 (1-x)^3 [xM + m]^2 + k_T^2]}{16\pi^3 (k_T^2 + L_s^2)^4}, \]
\[ f_1^v(x, k_T^2) = \frac{g_v^2}{2(2\pi)^3} \frac{1}{(1-x)} \frac{\left[(xM + m)^2 + k_T^2 + 2xmM\right]}{(k_T^2 + L_v^2)^2} = \frac{N_v^2 (1-x)^3 [xM + m]^2 + k_T^2 + 2xmM]}{16\pi^3 (k_T^2 + L_v^2)^4}. \]
FIG. 2: Model calculation of $x f_1(x)$: with scalar diquarks only (dashed line), with scalar and axial-vector diquarks (solid line). The $d$ quark distribution is zero when only scalar diquarks are used.

Both functions can be integrated over the transverse momentum to give

$$f_s^u(x) = \frac{N_s^2}{96 \pi^2 L_s^6} \left[ 2(xM + m)^2 + L_s^2 \right],$$

(9)

$$f_v^u(x) = \frac{N_v^2}{96 \pi^2 L_v^6} \left[ 2(xM + m)^2 + L_v^2 + 4xmM \right].$$

(10)

In order to obtain the distribution functions for $u$ and $d$ quarks, we use the following relation, coming from the analysis of the proton wave function,

$$f_u^1 = 3 \left( \frac{N_s^2}{N_v^2} \right) f_s^1 + \frac{1}{2} f_v^1, \quad f_d^1 = f_v^1.$$  

(11)

Here we refrain from discussing the choice of parameters of the model and its quality, for which we refer to the original work [21]. We choose the following values for the parameters of the model:

$$m = 0.36 \text{ GeV}, \quad M_s = 0.6 \text{ GeV}, \quad M_v = 0.8 \text{ GeV},$$

(12)

$$\Lambda = 0.5 \text{ GeV}, \quad N_s^2 = 6.525, \quad N_v^2 = 28.716.$$  

(13)

The factors $N_s$ and $N_v$ are chosen in order to normalize the functions $f_s^1$ and $f_v^1$ to 1 and consequently to normalize $f_u^1$ to 2 and $f_d^1$ to 1. The results of the model are shown in Fig. 2. The dashed line represents the result of the spectator model with scalar diquarks only (with $f_u^1 = 2 f_s^1$). As can be seen, the difference for the $u$ distribution is not big, but it is particularly relevant at small $x$. The $d$ quark distribution is zero when only scalar diquarks are used, which is clearly unrealistic.

One of the problems when trying to match the model and the phenomenology is that it is not clear at which energy scale the model should be applied. A way to estimate this energy scale is to compare the total momentum carried by the valence quarks in the model and in some parametrization [24, 26]. Taking, for instance, the CTEQ5L parametrization [27] it turns out that this scale is about $0.078 \text{ GeV}^2$. Then, by applying standard DGLAP equations, we can evolve our model results to $1 \text{ GeV}^2$ and compare it with the CTEQ5L parametrization at that scale. The result is shown in Fig. 3. Admittedly, the model reproduces the parametrization of the valence quark distribution only qualitatively. In any case, in this work we mainly aim at giving rough estimates of the relative magnitude of the $u$ and $d$ Sivers function and of the related single-spin asymmetries, as well as studying the changes induced in the model results when an axial-vector diquark is introduced. Therefore, we refrain from improving and tuning the model.

\footnote{We use leading order evolution with three flavors and $\Lambda_{LO}^{(3)} = 0.222$, in order to match the CTEQ5 results.}
dependence of our results is not very strong. We cannot evolve our results to a higher energy scale, as we have done for the unpolarized distribution function, since in Refs. [12, 19, 20] are due to the different choice of form factors in the nucleon-quark-diquark vertex. Unfortunately, a sign error in those computations has been recently identified [29]. The other differences between our results and those note that our result for the scalar diquark has the opposite sign compared to similar computations [12, 20]. However, a

applying Cutkosky rules or, equivalently, by taking the imaginary part of the propagator 1 and the imaginary part of amplitude (b). The imaginary part of amplitude (b) can be computed by to introduce the one-loop amplitude described in Fig. 1 (b). This is nothing else than the one-gluon approximation of any final state interaction that can provide the imaginary parts necessary to generate T-odd functions. We need to the gauge link included in Eq. (2). The Sivers function receives a contribution from the interference between (a) and the imaginary part of amplitude (b). The imaginary part of amplitude (b) can be computed by applying Cutkosky rules or, equivalently, by taking the imaginary part of the propagator 1/\(l^+ + i\epsilon\) [15]. Note that in Drell-Yan processes the different topology of the one-gluon diagram implies that the imaginary part of the propagator 1/(\(l^+ - i\epsilon\)) has to be taken, with the effect of changing the overall sign of the Sivers function [14, 28]. This is consistent with the change in direction of the gauge link mentioned before [17].

Following Ref. [12] we perform the calculations initially with Abelian gluons and generalize the result to QCD at the end. We use Feynman gauge. In order to compute the one-loop diagram, we have to make the appropriate choice for the vertex between the gluon and the scalar or axial-vector diquark. We choose the following forms

\[ \Gamma^a_s = -ie_2(2p - 2k - l)^a, \]

\[ \Gamma^{\alpha\beta}_v = ie_2 \left[ (2p - 2k - l)^\nu g^{\alpha\beta} - (p - k - vl)^\beta g^{\nu\alpha} - (p - k - (1 - v)l)^\alpha g^{\nu\beta} \right], \]

where \( e_2 \) denotes the color charge of the diquark, which we assume to be the same for both kinds of diquark. The gluon-axial-vector diquark coupling is identical to the photon-axial-vector diquark coupling suggested in Ref. [22]. The parameter \( v \) is the anomalous magnetic moment of the axial-vector diquark; for \( v = 1 \) the vertex is analogous, for instance, to the standard photon-W vertex. In any case, our results at leading order do not depend on the anomalous magnetic moment of the diquark.

The final results for the Sivers function are

\[ f_{1T}^{s}(x, \vec{k}_T^2) = \frac{e_1 e_2 N_c^2 (1 - x)^3 M (xM + m)}{4(2\pi)^4 L_s^2 [\vec{k}_T^2 + L_s^2]^{3/2}}, \]

\[ f_{1T}^{v}(x, \vec{k}_T^2) = -\frac{e_1 e_2 N_c^2 (1 - x)^3 xM^2}{8(2\pi)^4 L_v^2 [\vec{k}_T^2 + L_v^2]^{3/2}}. \]

Note that our result for the scalar diquark has the opposite sign compared to similar computations [12, 20]. However, a sign error in those computations has been recently identified [29]. The other differences between our results and those in Refs. [12, 19, 20] are due to the different choice of form factors in the nucleon-quark-diquark vertex. Unfortunately, we cannot evolve our results to a higher energy scale, as we have done for the unpolarized distribution function, since the equation evolutions for the Sivers function have not been established yet [30, 31]. We hope, however, that the \( Q^2 \) dependence of our results is not very strong.

We introduce the \( k_T \) moments

\[ f_{1T}^{s/(1/2)}(x) \equiv \int d^2 k_T \frac{k_T^2}{2M} f_{1T}^{s}(x, \vec{k}_T^2), \]

\[ f_{1T}^{v(1)}(x) \equiv \int d^2 k_T \frac{k_T^2}{2M^2} f_{1T}^{v}(x, \vec{k}_T^2), \]

FIG. 3: Model calculation of \( x f_1(x) \) (solid line) compared to the CTEQ5L parametrization [27] (dashed line) at 1 GeV^2.

III. SIVERS FUNCTION AND ITS MOMENTS

We use the following definition of the Sivers function

\[ \frac{e_2 k_{T} S_{T} J_{T}}{M} f_{1T}^{s}(x, \vec{k}_T^2) = -\frac{1}{4} \text{Tr} \left[ (\Phi(x, \vec{k}_T; S) - \Phi(x, \vec{k}_T; -S)) \gamma^+ \right], \]

where \( 4i e_2 k_{T} S_{T} J_{T} = \text{Tr} [\gamma_5 \gamma^+ \gamma_5 \vec{J}] \). At tree level the Sivers function turns out to vanish. This is due to the lack of any final state interaction that can provide the imaginary parts necessary to generate T-odd functions. We need to introduce the one-loop amplitude described in Fig. 1 (b). This is nothing else than the one-gluon approximation to the gauge link included in Eq. (2). The Sivers function receives a contribution from the interference between amplitude (a) and the imaginary part of amplitude (b). The imaginary part of amplitude (b) can be computed by applying Cutkosky rules or, equivalently, by taking the imaginary part of the propagator 1/(\(l^+ + i\epsilon\)) [15]. Note that in Drell-Yan processes the different topology of the one-gluon diagram implies that the imaginary part of the propagator 1/(\(l^+ - i\epsilon\)) has to be taken, with the effect of changing the overall sign of the Sivers function [14, 28]. This is consistent with the change in direction of the gauge link mentioned before [17].
for which we get the following results

\[ f_{1T}^{\perp(1/2)}(x) = \frac{e_1 e_2 N_s^2 (1-x)^3 (xM + m)}{1024 \pi^2 L_s^5}, \]

\[ f_{1T}^{\perp(1/2)}(x) = \frac{e_1 e_2 N_s^2 (1-x)^3 (xM + m)}{256 \pi^3 M L_s^4}, \]

\[ f_{1T}^{\perp(1/2)}(x) = -\frac{e_1 e_2 N_s^2 (1-x)^3 x M}{2048 \pi^2 L_s^5}, \]

\[ f_{1T}^{\perp(1/2)}(x) = -\frac{e_1 e_2 N_s^2 (1-x)^3 x}{512 \pi^3 L_s^4}. \]

The only parameter to be fixed is the product of the quark and diquark charges. Following Ref. \[12\] we fix \( e_1 e_2 = 4 \pi C_F \alpha_s \) and we choose \( C_F = 4/3 \) and \( \alpha_s \approx 0.3 \).

Relations equivalent to those of Eq. \[11\] hold for the Sivers function and its moments. In Fig. 4 we show the model results for the first moment of the Sivers function. The inclusion of the axial-vector diquark results in some change to the only phenomenological extractions available at present \[2, 3, 32\]. However, there is a sharp difference in the relative contribution. We point out that this difference could be due to a significant contribution of sea quarks (in particular \( \bar{u} \)) to the asymmetry studied in Refs. \[2, 3\].

Note that our model calculation complies with the positivity bound \[33\]

\[ f_{1T}^{\perp(1/2)}(x) \leq \frac{1}{2} f_1(x). \]

We performed also the calculation of the function \( h_{1T}^{\perp} \), introduced by Boer and Mulders in Ref. \[34\] and defined as

\[ \frac{c_{1T}^{xT}}{M} h_{1T}^{\perp}(x, \vec{k}_T^2) = \frac{1}{4} \text{Tr} \left[ (\Phi(x, \vec{k}_T; S) + \Phi(x, \vec{k}_T; -S)) i \sigma^i \gamma_5 \right]. \]

For the scalar diquark, we found that \( h_{1T}^{\perp} = f_{1T}^{\perp} \), confirming the results already obtained in Refs. \[19, 20\]. For the axial-vector diquark, we obtain

\[ h_{1T}^{\perp}(x, \vec{k}_T^2) = -\frac{e_1 e_2 N_s^2 (1-x)^3 M (2xM + m)}{4 (2\pi)^4 L_s^5 \left[ \vec{k}_T^2 + L_s^2 \right]^3}, \]

\[ h_{1T}^{\perp}(x) = -\frac{e_1 e_2 N_s^2 (1-x)^3 (2xM + m)}{256 \pi^3 M L_s^4}. \]

IV. SINGLE SPIN ASYMMETRIES

We consider the weighted transverse spin asymmetries

\[ \langle \sin(\phi_h - \phi_S) \rangle_{UT}(x, z) = \frac{\int dy \, d^2 \vec{P}_h \sin(\phi_h - \phi_S) (d^6 \sigma_{UT} - d^6 \sigma_{UL})}{\int dy \, d^2 \vec{P}_h (d^6 \sigma_{UT} + d^6 \sigma_{UL})}, \]

\[ \langle \frac{1}{z M} \sin(\phi_h - \phi_S) \rangle_{UT}(x, z) = \frac{\int dy \, d^2 \vec{P}_h (d^6 \sigma_{UT} + d^6 \sigma_{UL})}{\int dy \, d^2 \vec{P}_h \sin(\phi_h - \phi_S) (d^6 \sigma_{UT} - d^6 \sigma_{UL})}, \]
where the notation $d\sigma_{UT}$ indicates the cross section with an unpolarized lepton beam off a transversely polarized target. The angles involved in the definition of the asymmetry are depicted in Fig. 5. These asymmetries are currently measured by the HERMES and COMPASS collaborations [35, 36].

Under the assumption that the pion transverse momentum with respect to the virtual photon is entirely due to the intrinsic transverse momentum of partons, i.e., $\vec{P}_{h\perp} = z\vec{k}_T$, the first asymmetry can be written as

$$\langle \sin (\phi_h - \phi_S) \rangle_{UT} (x, z) \approx \frac{1}{x} \frac{\sum_a e_a^2 f^{(1/2)a}_{UT}(x) \cdot D_1^a(z)}{\sum_a x^2 f^a_1(x) \cdot D_1^a(z)},$$

with $a$ indicating the quark flavor. Our model results are displayed in Fig. 6. We took the unpolarized fragmentation functions from Ref. [37] at a scale $Q^2 = 1 \text{ GeV}^2$. In order to make predictions useful for the HERMES experiment, to produce Fig. (a) and (b) we integrated the asymmetries over $z$ from 0.2 to 0.7. To produce Fig. (c) and (d) we integrated the asymmetries over $x$ from 0.023 to 0.4.

Evidently, there is not a big difference between $\pi^+$ and $\pi^-$ asymmetries. We do not plot the results for $\pi^0$.
FIG. 7: Model estimate of the single-spin asymmetry $\langle \frac{|\vec{P}_h \perp M}{M} \sin (\phi_h - \phi_S) \rangle_{UT}$: with scalar diquarks only (dashed line), with scalar and axial-vector diquarks (solid line). The $x$ and $z$ dependence is shown for $\pi^+$ and $\pi^-$. 

production, since they lie between the previous two. We point out that assuming 

$$f_1^d D_1^d(\pi^{\pm,0}) \ll 4 f_1^u D_1^u(\pi^{\pm,0}), \quad (28)$$

the above asymmetry can be written as 

$$(\sin (\phi_h - \phi_S))_{UT}^{\pi^{\pm,0}}(x, z, 0) \approx \frac{3}{2} \frac{f_{1T}^{(1/2)a}(x)}{f_1^a(x)} + \frac{1}{2} \frac{f_{1T}^{(1/2)v}(x)}{f_1^u(x)} \left(1 + \frac{1}{2} D_1^d(\pi^{\pm,0})(z)\right). \quad (29)$$

The first term in this equation is the dominant one. This explains why there are only small differences between the $\pi^+$ and $\pi^-$ asymmetry. However, the axial-vector contribution to $f_1^u$ cannot be neglected. From Eq. (29) it is also evident that the dependence of the asymmetries on $z$ is due to the influence of the unfavoured fragmentation functions. In the case of $\pi^-$ the last term in Eq. (29) is bigger and therefore the $z$ dependence is stronger. In the case of $\pi^0$ – not shown in our pictures – the term in parentheses would be exactly $3/2$ and the $z$-dependent asymmetry would be a flat line at about $5\%$.

The asymmetry in Eq. (29) can be written in an assumption-free way as 

$$\left\langle \frac{|\vec{P}_h \perp M}{M} \sin (\phi_h - \phi_S) \right\rangle_{UT}^{\pi^{\pm,0}}(x, z) = \frac{1}{x} \sum_a e_a^2 f_{1T}^{(1/2)a}(x) z D_1^a(z) \left(1 + \frac{1}{2} D_1^d(\pi^{\pm,0})(z)\right). \quad (30)$$

The calculated asymmetries are shown in Fig. 7 where we performed the integrations over $x$ or $z$ as in the previous case. As before, assuming Eq. (28) the asymmetry can be simplified to 

$$\left\langle \frac{|\vec{P}_h \perp M}{M} \sin (\phi_h - \phi_S) \right\rangle_{UT}^{\pi^{\pm,0}}(x, z) \approx \frac{3}{2} \frac{f_{1T}^{(1/2)a}(x)}{f_1^a(x)} + \frac{1}{2} \frac{f_{1T}^{(1/2)v}(x)}{f_1^u(x)} \left(1 + \frac{1}{2} D_1^d(\pi^{\pm,0})(z)\right). \quad (31)$$

V. CONCLUSIONS

We calculated the Sivers function in a spectator model of the nucleon with scalar and axial-vector diquarks. The final state interaction necessary to generate T-odd distribution functions was provided by gluon rescattering between the struck quark and the diquark.
The inclusion of axial-vector diquarks allowed us to calculate the Sivers function for the $d$ quarks. The function turns out to have the opposite sign compared to the $u$ quarks and to be much smaller in size. The $u$ quark Sivers function is substantially reduced by the axial-vector contribution. Although the reliability of the model is very limited, we think that our results on the relative behavior of $u$ and $d$ quarks could be qualitatively relevant.

Using the results of our model, we estimated some single spin asymmetries containing the Sivers function. These asymmetries are at present being measured by the HERMES and COMPASS collaborations. We noticed that the inclusion of axial-vector diquarks can make drastic changes in the asymmetries as compared to the spectator model with scalar diquarks only, particularly at low $x$. We were able for the first time to estimate the Sivers single spin asymmetry in $\pi^+$ and $\pi^-$ production. We observed that the $\pi^+$ and $\pi^-$ asymmetries are not very different, due to the dominance of the $u$ quark contribution in both cases. The $\pi^0$ asymmetries (which we did not show) lie between the $\pi^+$ and $\pi^-$ estimates.

The present approach does not take into account sea quarks. Unfortunately, at the moment we have no indication about the size and sign of the sea-quark Sivers function.

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