Multiband Hypersound Filtering in Two-Dimensional Colloidal Crystals: Adhesion, Resonances, and Periodicity

Bartłomiej Graczykowski,* Nicolas Vogel, Karina Bley, Hans-Jürgen Butt, and George Fytas

ABSTRACT: The hypersonic phonon propagation in large-area two-dimensional colloidal crystals is probed by spontaneous micro Brillouin light scattering. The dispersion relation of thermally populated Lamb waves reveals multiband filtering due to three distinct types of acoustic band gaps. We find Bragg gaps accompanied by two types of hybridization gaps in both sub- and superwavelength regimes resulting from contact-based resonances and nanoparticle eigenmodes, respectively. The operating GHz frequencies can be tuned by particle size and depend on the adhesion at the contact interfaces. The experimental dispersion relations are well represented by a finite element method model enabling identification of observed modes. The presented approach also allows for contactless study of the contact stiffness of submicrometer particles, which reveals size effect deviating from macroscopic predictions.

KEYWORDS: Colloidal crystals, phononics, acoustic band gap, Lamb waves, Brillouin light scattering, GHz signal filtering

Phonons, quanta of acoustic field, similarly as photons and electrons, are carriers of energy, momentum, and information. High-frequency phonons in the GHz-THz regime corresponding to submicrometer wavelengths are responsible for hypersonic and heat transport, thus having importance for wireless communication, optomechanics, and thermal energy harvesting.1 Periodically structured materials that take advantage of the wave-like nature of phonons, such as phononic crystals (PnCs) and acoustic metamaterials, have been shown to enable new mechanical and acoustic features, including negative effective moduli and densities, frequency filtering, and acoustic cloaking.9 Recently, this field has experienced a tremendous growth of research in topological PnCs showing unidirectional propagation of sound immune to structural imperfections.9,10

To date, the majority of studies on PnCs and acoustic metamaterials has involved macroscopic structures aimed to affect Hz-kHz acoustic waves/phonons. Nowadays, however, there is a significant need in developing PnCs in the nanoscale and operating in GHz as well as THz frequency regimes.6,10,11 Nevertheless, nanofabrication of hypersonic PnCs faces several practical challenges preventing their implementation in everyday devices. The patterning needs to be performed over large areas/volumes of matrices being CMOS compatible for easy integration without sophisticated instrumentation. Furthermore, fabricated materials should keep structural order and coherence of GHz acoustic signals over long length scales. Self-assembly of nanoparticles has emerged as a solution for low-cost mass production.12 Propagation of GHz phonons in three-dimensional (3D) self-assembled PnCs, typically known as colloidal crystals, composed of glass or polymer nanoparticles was initially investigated by means of Brillouin light scattering (BLS).13−15 More recently, contact-based modes of colloidal crystals have been extensively studied using the pump−probe technique.16−25 This approach, unlike BLS, is limited to sub-GHz frequencies and often requires additional fabrication of a transducer for the acoustic wave generation.

Two-dimensional (2D) self-assembled PnCs, known as colloidal monolayers,12 offers a low-cost and large-area platform for harnessing high-frequency phonons. These materials, if supported by ultrathin membranes, can overcome the issue of signal/energy losses into the substrate. The use of inorganic membranes provides a mechanically robust framework serving as a waveguide for a discrete set of dispersive (Lamb) waves that can be tuned by the membrane thickness.26,27 The monolayer-membrane architecture enables use of stiff and low-losses materials which can maintain signal coherence, adding functionality to PnC. This solution goes hand in hand with new features of PnCs, that is, elastic and thermal size effects, unexplored schemes of band gap opening,
as well as with experimental challenges related to their investigation and understanding in the high-frequency regime.

In this work, we study the phonon propagation in large-area 2D PnCs composed of spherical polystyrene (PS) nanoparticles self-assembled on an ultrathin Si₃N₄ membrane (Figure 1). We use micro BLS (μBLS)²⁸,²⁹ to record the dispersion of thermally populated GHz phonons. To interpret the experimental results, we develop a finite element method (FEM) model. We find significant modification of the phonon dispersion revealing three types of band gaps that are related to nanoparticle: membrane contact resonance (hybridization), lattice period (Bragg), and local resonances of nanoparticles (hybridization). The latter type, unlike for the vast majority of PnCs and metamaterials, appears above the Bragg band gap frequency, that is, in the superwavelength regime.²,³,³⁰ All these mechanisms contribute to multiband filtering of hypersound that can be easily tailored by means of the nanoparticle size and the corresponding power were in the order of a few micrometers.

We recorded the dispersion of acoustic waves propagating in the samples at room temperature by means of angle-resolved μBLS in p–p (TM–TM) backscattering geometry, as shown schematically in Figure 1a. The incident laser light at λ₀ = 532 nm was focused on the sample by means of 10× microscope objective with 0.25 numerical aperture. The scattered light was collected by the same objective and analyzed by a tandem type Fabry–Perot interferometer. The laser spot size on the sample and the corresponding power were in the order of a few micrometers and <500 µW, respectively. BLS probes the frequency shift f of the laser light inelastically scattered by thermally populated acoustic phonons. For a pristine membrane, which is well-approximated as a homogeneous elastic continuum, the scattering wave vector q is the same as the wave vector k of the acoustic phonons. However, for periodic structures the momentum conservation defines the
scattering wave vector as $q = k \pm G$. In particular, for the hexagonal lattice $G = (2\pi/(a\sqrt{3}))[m_1\sqrt{3}, -m_1 + 2m_2]$ is a reciprocal lattice vector with lattice parameter $a$ and integers $m_1, m_2$. Following previous studies of thin membranes, we define the magnitude of the scattering wave vector $q$ as $q = 4\pi \sin \theta / \lambda_0$ and assume the superposition of photoelastic and moving-interface (surface ripple) effects contributing to BLS spectra. Figure 2a,b displays BLS spectra obtained for samples A and B at $q = 10 \mu m^{-1}$, which were normalized by the thermal population factor. The single peak present in the spectrum of the bare membrane can be assigned to a fundamental antisymmetric (flexural, $A_0$) Lamb plate wave mode. PS monolayer on top of the membrane results in increased complexity of the spectrum, as evident in Figure 2b. However, the latter spectrum is distinct from that of the corresponding 3D control sample showed in Figure 2c. Two peaks in Figure 2c are attributed to the dipolar (low frequency) and quadrupolar (higher frequency) spheroidal Lamb modes of nanoparticles. In principle, the contribution of spheroidal Lamb modes to BLS is due to the photoelastic effect and depends on deformation field and dimensionless magnification factor $qR$. For a free homogeneous sphere, eigenfrequencies of Lamb modes are given by the formula $f_{n,l} = A_n v_T / d$, where $n$ and $l$ are integers defining radial and angular dependence of the displacement, respectively, $v_T$ is the transverse speed of sound in bulk PS, and $A_n$ is a dimensionless mode- and material-dependent parameter. The low-frequency peak in Figure 2c originates in (1,1) mode, which is ill-defined due to the light multiple scattering from the 3D cluster. The second peak is associated with (1,2) mode, the expected frequency of which is indicated by an arrow in Figure 2c. The asymmetry of this peak is due to contact-induced splitting of (1,2) mode into weakly dispersive branches. In principle, the BLS spectra of 3D clusters characterize spheroidal Lamb modes (torsional remain silent) and contain information about interparticle forces. By comparing Figure 2b,c, we notice that the asymmetric peak of (1,2) mode in the 3D sample is replaced by three distinct peaks recorded in the monolayer-membrane. A similar comparison of the BLS spectra of the other samples can be found in Supporting Information (SI).
Figure 3 summarizes angle-resolved µBLS measurements for all membrane-monolayer samples as dispersion relations \(f(q)\). Here, the color scale refers to the normalized intensity of the scattered light, and the circles stand for the frequencies at the peak positions. The dispersion relation of sample A displayed in Figure 3a shows only one branch that we identified as a flexural (A0) wave of a bare membrane.\(^\text{26}\) The fundamental symmetric (dilatational, S0) and shear-horizontal (SH0) modes are not BLS active due to zero (SH0) or small (S0) out-of-plane displacement \(u_z\) for the measured range of wave numbers \(q\).\(^\text{35}\) As follows from Figure 3b–d, the adhered monolayers in the samples B–D result in severely modified and complex dispersion relations compared to the dispersion of sample A.

At first glance, we can indicate three distinct effects and corresponding partial gaps related to the measured bands, that is, (i) Bragg reflections, hybridization of A0 mode with (ii) nanoparticle–membrane contact-based resonance, or (iii) spheroidal modes of nanoparticles. In each case, we define the band gaps for the modes of predominant out-of-plane displacement and indicate them only for the measured range of wave numbers \(q\). For samples C and D, we identify clear zone folding and Bragg band gaps (BG) at frequencies \(f \approx 2.5\) GHz and \(f \approx 1.5\) GHz, respectively. This observation confirms the presence of wave-like/coherent effects and long-range order of PnCs extending over distances larger than the measured wavelengths. This phenomenon was neither observed nor modeled in previous works on similar, albeit sub-GHz, structures. Figure 3c,d suggests that the spectral position of BG can be estimated at the crossing of A0 mode and zone boundary (ZB). This provides simple geometric means for tunability of this type of a stop band, as A0 and ZB can be adjusted by the membrane thickness and nanoparticle diameter, respectively.

The horizontal branches that appear above \(f \approx 2\) GHz in dispersion relations of samples B–D can be attributed to the spheroidal \((n, l)\) modes of PS nanoparticles.\(^\text{35,36}\) This assignment is supported by BLS spectra of the reference fcc clusters showing similarities with the accumulative spectra of the corresponding monolayer-membrane samples (SI, Figure S1). We use the calculated frequencies of spheroidal modes of free PS nanoparticles (arrows in Figure 3c,d) for a preliminary identification of these branches.

In Figure 3b,d, we observe a split of the \(f_{1,2}\) mode that is represented by two distinct branches. A similar split was not captured for sample C, probably due to adverse \(qR\) magnification factor and thereby weak scattering intensity for the (1,2) mode.\(^\text{35}\) The (1,2) mode split can be explained by the presence of nanoparticle–nanoparticle and nanoparticle–membrane contacts.\(^\text{24,33}\) We will discuss this phenomenon in more detail later in this work, making use of FEM modeling. In the case of higher order \((n, l)\) modes, as those in the dispersion relation of sample D, it cannot be clearly stated that the mode split is experimentally resolved. Although anticipated, it could be masked by a close neighborhood of branches as for instance those related to (2,1) and (1,3) modes. Despite this ambiguity, we observe a clear hybridized interaction of the spheroidal modes with the flexural wave at frequencies above BG, as evident in Figure 3d. This results in a unique feature of membrane-based PnCs, namely, opening of the local resonance band gaps (LR) in the superwavelength regime. This phenomenon was studied theoretically for pillared membranes in terms of the impact on heat transport at THz frequencies\(^\text{57}\) and, more recently, demonstrated experimentally in the kHz regime for a macroscopic trampoline metamaterial.\(^\text{38}\)

Band diagrams of samples B–D reveal contact-based modes falling below BG that is in the subwavelength regime typical for acoustic metamaterials.\(^\text{3,5,39}\) These branches are a consequence of the hybridization and avoided crossing between A0 wave and the nanoparticle–membrane contact resonance. As we will further show using FEM, this resonance originates from the spheroidal (1,1) mode. From Figures 3b–d we can conclude that corresponding contact resonance (CR) stop bands appear in the hypersonic regime but at wavelengths longer than the lattice parameter. That type of a band gap was previously observed in the sub-GHz range for acoustic metamaterials\(^\text{18,19,21,22,24}\) and modeled using Hertzian contact\(^\text{40,41}\) and van der Waals-type adhesive forces.

The frequency of the nanoparticle–membrane resonance denoted as \(f_{\text{pm}}\) in Figure 3 yields information about the nanoparticle–membrane adhesion force. Assuming \(q \to 0\) and negligible effect of nanoparticle–nanoparticle contacts, the normal contact stiffness \(K_N\) can be determined from the two-mass oscillator equation \(2\pi f_{\text{pm}} = \sqrt{K_N (m_p^{-1} + m_m^{-1})}\), where \(m_p\) and \(m_m\) denote masses of the PS nanoparticle and corresponding fraction of the membrane, respectively (Figure 4a). Based in the latter expression, the contact resonance gap

Figure 4. (a) Schematics of the nanoparticle–membrane contact stiffness \(K_N\) and (b) JKR model of nanoparticle–membrane and nanoparticle–nanoparticle contacts. (c) 3D scheme of FEM unit cell (see text). (d) Measured (BLS) and predicted (JKR) contact stiffness \(K_N\). (e) Fitted (FEM) from the experiment and predicted (JKR) contact radii of the nanoparticle–nanoparticle and nanoparticle–membrane interfaces.

depends on the nanoparticles mass, lattice packing, and strength of the nanoparticle–membrane bonding. The determined \(K_N\) is plotted in Figure 4d and compared with expected values calculated by means of Johnson–Kendall–Roberts (JKR) model.\(^\text{55}\) For small displacements around the equilibrium point in JKR model, the linearized contact stiffness \(K_{\text{JKR}}\) (Figure 4b) is given by\(^\text{41,43,44}\)

\[
K_{\text{JKR}} = \frac{9}{5} \frac{3}{4} \pi W_{\text{pm}} R^2 E_{\text{pm}}^{1/3}
\]  

(1)
where $E_{\text{pm}} = 5.91$ GPa is the nanoparticle–membrane effective modulus, $W_{\text{pm}} = 0.103$ J/m$^2$ is the work of adhesion of PS-Si$_3$N$_4$, and $R$ is the nanoparticle radius. Both values are derived in SI (Section II). As we can infer from Figure 4d, for each sample, the measured contact stiffness $K_n$ is about five times higher than what is predicted by JKR model. This deviation stems from additional physical bonding due to liquid or solid bridges resulting from impurities in the fabrication that are evident in SEM image in Figure 1e.25 Notably, the deviation from the model increases as the nanoparticle diameter becomes smaller. Conclusively, this manifests the impact of the real size of the contact interfaces on the phonon propagation in hypersonic colloidal PnCs in addition to the geometry and bulk elastic properties.

Theoretical models used in previous studies$^{18,20,45}$ did not consider two phenomena evident in our measurements, namely, interaction of the propagating waves with local resonances and periodicity of the material. Therefore, to capture these features and explain (1,2) mode split we developed a FEM model. Figure 4c schematically describes the 3D unit cell that includes lateral periodicity and assumes fused contacts with fully deformable spheres and membrane. PS spheres of radius $R$ are connected to each other and to a membrane of thickness $t$ by fully deformable circular interfaces with radii $r_{\text{pp}}$ and $r_{\text{pm}}$, respectively. The periodicity of the structure in the $x_1x_2$ plane is implemented by applying Bloch–Floquet periodic boundary conditions to all vertical walls of the unit cell. In the fitting procedure, we used two adjustable parameters, radii of nanoparticle–membrane ($r_{\text{pm}}$) and nanoparticle–nanoparticle ($r_{\text{pp}}$) contact areas. In addition to the dispersion relation, we used FEM to determine the contribution of surface ripple and photoelastic mechanisms to BLS by means of two parameters $\xi_3$ and $\xi_{3\text{eff}}$, respectively (SI, Section V). The superposition of these effects as well as size effects (membrane thickness, $qR$ factor) are beyond the scope of this work. Further details and material properties used in the FEM model can be found in the SI (Section V).

Figure 5a shows good agreement of the calculated dispersion relation with the experimental data obtained for sample C ($d = 333$ nm). In addition, the experimental BLS intensity follows the calculated $\xi_{3\text{eff}}$ that is related to the magnitude of the BLS surface ripple mechanism. The discrepancies above about 2.5 GHz can result from the simplification, that is, neglected contribution of the photoelastic effect and its interference with the moving-interface effect, which can enhance as well as cancel the BLS signal.$^{25,29}$ Nevertheless, FEM allows sorting of $(n,l)$ modes in terms of the sphere radial displacement. For that purpose we define the $\xi_n$ parameter, which resembles BLS activity of Lamb modes due to photoelastic effect (SI, Section V).35 We note that this approach does not include the effect of the $qR$ magnification factor.$^{7}$ Figure 5b shows the dispersion relation calculated for sample C with a color scale overlaid reflecting the magnitude of $\xi_{3\text{eff}}$. The frequency levels illustrate the split of $2l+1$ degenerate vibrations of $(n,l)$ modes of a free sphere resulting from nanoparticle–membrane and nanoparticle–nanoparticle contacts and thereby symmetry lowering.$^{23,33,46}$ For transparency, we limit the analysis to BLS active modes at $q = 0$. To identify the modes, we utilized FEM displacement fields shown in Figure 5c which are sorted with respect to $(n,l)$ parent mode and the azimuthal number $m$. The example of (1,2) mode at $q = 0$ shows a split into two doublets ($m = 1, m = 2$) and one singlet ($m = 0$), which we resolve as two peaks by means of BLS. The situation is much more complex for $q \neq 0$. Namely, the degeneracy is not present, and all five modes are of different frequencies. Furthermore, they interact with propagating waves in the membrane and their BLS activity varies with $q$. A similar analysis can be performed for all spherical modes undergoing mode split as schemed in Figure 5b. Here, for instance, (1,1) $m = 0$ mode with nanoparticle and membrane vibrating out-of-phase in the out-of-plane direction is the nanoparticle–membrane contact resonance. The comparison of experimental and calculated dispersion relations for samples B and D can be found in SI (Section V).

The contact radii fitted by FEM and plotted in Figure 4e reveal a trend that follows the JKR model,$^{33,41,42}$ namely $r_{\text{JKR}} \sim (6\pi W_{\text{eff}}^2/E_{\text{eff}})^{1/3}$. In principle, the JKR model allows us to predict the contact radii from the formula (Figure 4b):

$$r_{\text{JKR}} = (6\pi W_{\text{eff}}^2/E_{\text{eff}})^{1/3}$$

Figure 5. (a, b) Dispersion relations (dashed lines) calculated for sample C ($d = 333$ nm) with overlaid color intensity plots indicating (a) out-of-plane displacement ($\xi_3$) and (b) radial displacements ($\xi_{3\text{eff}}$). Circles in (a) stand for BLS experimental data. Right-hand panel of (b) schematically illustrates $(n,l)$ modes at $q = 0$ due to nanoparticle–membrane and nanoparticle–nanoparticle contacts, where $m$ stands for the azimuthal number. Corresponding FEM displacement fields are displayed in (c).
where for the nanoparticle–membrane interface, the work of adhesion is \( W = W_{pp} = 0.1036 \, \text{J/m}^2 \), effective radius is \( R_{eff} = R \), and \( E_{eff} = E_{pp} = 5.91 \, \text{GPa} \) is the effective moduli. In the case of the nanoparticle–nanoparticle contact in eq 2, we substitute \( W = W_{pp} = 0.064 \, \text{J/m}^2 \), \( R_{eff} = R/2 \), and \( E_{eff} = E_{pp} = 3.01 \, \text{GPa} \) (see SI, Sections III and IV). From Figure 4e, we can conclude that for both types of interfaces, the JKR model predicts over twice lower contact radii as compared to values fitted by FEM model for all samples. This goes along with the already mentioned underestimation of the contact stiffness by JKR model with respect to those measured by BLS. In principle, our results call into question the applicability of JKR model to assemblies of submicrometer particles with unavoidable fabrication imperfections.

In summary, we investigated the propagation of hypersonic phonons in large-area self-assembled 2D colloidal PnCs utilizing nondestructive μBLS technique. We showed that these materials can simultaneously host three distinct mechanisms for the phonon dispersion modification toward opening of stop bands for GHz acoustic waves. Each mechanism can be tailored by simple geometrical means as they result from (i) the lattice period, (ii) nanoparticle–membrane adhesion, and (iii) mechanical eigenmodes of nanoparticles. We found Bragg band gaps accompanied by subwavelength (contact resonance) and, noteworthy, multiple nanoparticle contact ineq 2, we substitute

- \( W = W_{pp} = 0.064 \, \text{J/m}^2 \)
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