Metal-insulator transition in a 2-dimensional system with an easy spin axis

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Abstract. The low-temperature resistivity of a SiGe 2-dimensional hole gas has been studied using the gate controlled carrier density as a parameter. A metal-insulator transition is seen in both the temperature and the electric field behaviour. Values of 1 for the dynamical exponent and 2.85 for the correlation length exponent are obtained from scaling plots. No quenching of the metallic phase in a parallel magnetic field is observed. Since in our system there is an easy axis for magnetization, this result supports the hypothesis that the transition is related to spin interactions.

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The recent discovery of a metallic phase at zero magnetic field in two-dimensional systems [1] challenges the theoretical considerations predicting a localized phase for these systems. There have been reports on MIT in Si-MOSFETs [2], p-SiGe [3], p-Ga[Al]As [4], high density n-Ga[Al]As with self-assembled InAs quantum dots [5], and recently also indications of a transition in n-Ga[Al]As with extremely low carrier concentration [6]. Here, we present evidence for temperature scaling and electric field scaling at densities around the MIT in a SiGe 2-dimensional hole gas (2 DHG), and obtain values for the two scaling coefficients.

The samples employed in this study were grown by molecular beam epitaxy, and consist of a 200 Å Si0.85Ge0.15 layer surrounded by undoped Si layers, a 150 Å B-doped Si layer with a setback of 180 Å from the well, and a 200 Å undoped Si cap. The SiGe layer forms a triangular potential well for the 2 DHG (Fig. 1a). Due to the lattice mismatch between the Si and the SiGe and due to size quantization, the heavy hole ($m_J = \pm 3/2$) potential is split from the light hole ($m_J = \pm 1/2$) potential, and ensures that the lowest bound state has heavy hole character. The transport effective mass of this state is $m^* \approx 0.25m_0$, as extracted from the temperature dependence of Shubnikov – de Haas oscillations. Conventional Hall bar structures were fabricated with the typical length between voltage probes of the order of 10 μm, and the length between current contacts and width of the Hall bars 60 – 140 μm and 10 – 30 μm, respectively. The carrier density $n_s$ could be tuned, $1.8 \cdot 10^{11} \text{ cm}^{-2} \leq n_s \leq 2.6 \cdot 10^{11} \text{ cm}^{-2}$, using a Ti/Al Schottky gate. The mobility in these structures was found to increase strongly with carrier concentration, from $1000 \text{ cm}^2/\text{Vs}$ (for $n_s = 1.8 \cdot 10^{11} \text{ cm}^{-2}$) to 7000 cm$^2$/Vs.
Fig. 1  a): Schematic diagram of the valence band structure of the sample. The heavy hole potential \( m_J = \pm \frac{3}{2} \) (full line) and light hole potential \( m_J = \pm \frac{1}{2} \) (dashed line) are separated in the SiGe well due to the built-in strain. The \( m_J = \frac{3}{2} \) lies partly above the Fermi energy (dashed-dotted line), and the 2 DHG is formed at the interface between the SiGe QW and the top Si layer.  

b): Resistivity as a function of electric field \( E \) for carrier densities in the range \((1.90 - 2.55) \cdot 10^{11} \text{ cm}^{-2}\). The critical resistivity is marked with a dotted line.  
c): Resistivity as a function of temperature \( T \) for carrier densities in the range \((1.93 - 2.25) \cdot 10^{11} \text{ cm}^{-2}\).

Current-voltage characteristics were measured with a DC-technique at 30 mK.

In Fig. 1b the differential resistivity \( \rho_{xx} \) is plotted as a function of electric field for different carrier concentrations. Plotting the differential resistivity makes undesired DC-offsets caused by our amplifier disappear and allows us to compare directly the different curves. At high carrier densities (low \( \rho_{xx} \)), the behaviour is that of a metal: for large electric fields the resistivity increases. For the lowest carrier concentrations, the behaviour is instead insulating, with a lower resistance at higher E-fields. At a critical density \( n_c = 2.0 \cdot 10^{11} \text{ cm}^{-2} \) a resistivity of \( \rho_c = 27 \text{ k}\Omega (= 1.05 \hbar/e^2) \) is observed, independent of the electric field. By plotting \( \rho_{xx} \) vs. \( \delta_n/E^q \) for different values of the exponent and \( \delta_n = |n - n_c|/n \), it is possible to find a \( q \) for which all the resistivity curves fall on one of two branches, one for the insulating (\( \rho_{xx} > \rho_c \)) and one for the metallic region (\( \rho_{xx} < \rho_c \)). An example of such a plot is shown in Fig. 2, for \( q = 0.175 \). In this figure the overlap has been optimized for the metallic phase. Close to the critical point there is a symmetry between the two resistivity branches, but this is lost at higher fields, where the insulator traces no longer fall onto one scaling curve.

The transition can also be seen in the temperature dependence of \( \rho_{xx} \). In Fig. 1c we show this for \( T = 1.5 K - 5 K \). The critical density, \( n_c = 2.1 \cdot 10^{11} \text{ cm}^{-2} \), is very close to that found in the electric field experiments. For densities close to the critical point, \( d\rho_{xx}/dT \) changes sign as the temperature is lowered. This makes the determination of the critical density less accurate than in the E-field scaling. For the temperature dependence it is possible to obtain scaling, by plotting \( \rho_{xx} \) vs. \( \delta_n/T^p \) where the exponent \( p \) is chosen such that the measured traces fall onto two separate scaling curves, with a reasonable symmetry between the two phases.
For a quantum phase transition the resistivity is expected to be a function of \( \delta_n / T^{1/z \nu} \) or \( \delta_n / (E_1/2)^{1/(z+1)\nu} \), depending on whether the correlation lengths are controlled by the temperature or the electric field. From the above stated \( \rho_{xx} \) dependence on \( E \) and \( T \) we see that the two exponents determined from \( E \)-field and temperature scaling, depend on the dynamical exponent \( z \) and the correlation length exponent \( \nu \): \( q = 1/(z + 1)\nu \) and \( p = 1/z\nu \). Assuming the same functional form of the resistivity for the \( E \)-field and temperature, the two types of scaling behaviour can be mapped onto each other via \( T \to \kappa E_1/(z+1) \) with \( \kappa \) being a system dependent constant. For a strongly interacting 2D system \( z = 1 \) is expected. In order to test this we scale \( E_1/2 \) and \( T \) on top of each other. In Fig. 2 \( \rho_{xx} \) is plotted against \( \delta_n / T^{0.35} \) and \( \delta_n / (E_1/2)^{0.35} \), with a reasonable scaling behaviour for both curves. In the inset \( E_1/2 \) has been multiplied by a constant \( \kappa = 0.4 \) \( K/(m/V) \), which demonstrates the highly identical resistivity dependence on \( T \) and \( E_1/2 \) in the metallic regime, and strongly supports \( z = 1 \). This gives a value for \( \nu \approx 2.85 \). While \( z \) is predicted to be equal to 1 \( \Box \), we are not aware of any predictions for the value of \( \nu \) for the \( B = 0 \) 2D MIT. The \( T \propto E_1/2 \) dependence suggests that the electric field can be interpreted in terms of quantum fluctuations \( \Box \), but we can not exclude the possibility of a heating mechanism due to the electric field which could lead to the same dependence.

In our system the transition is found for \( k_F l \approx 1 \), where \( l \) is the mean free path as deduced from the mobility, and \( k_F = \sqrt{2\pi n} \) is the Fermi wave vector. This point also corresponds to a ratio between the Coulomb interaction and the Fermi energy, \( r_s = 4.9 \). The value of \( r_s > 1 \) in the metallic region has been considered as evidence for the electron-electron interaction playing a major role \( \Box \).

In contrast to the Si MOSFET material system \( \Box \) in the present hole gases no resistivity increase with magnetic field applied parallel to the 2DHG is observed, and
the E-field behaviour remains the same. This is quantified by fitting the resistivity to
\[ \rho_{xx} = \rho_0 + \rho_1 \exp\left(-T^*/T\right) \]
with \( T = \kappa E^{1/2} \), where \( \kappa = 0.4 \) \( \text{Km/V} \) (see above), and
\( \rho_0 \) and \( \rho_1 \) as \( T \)-independent parameters. \( \rho_1 \) and \( T^* \) are used as fitting parameters, whereas \( \rho_0 \) has been kept constant for all fits (= 10\( k\Omega \)). In Fig. 3, the energy gap \( k_B T^* \) vs. carrier density is shown for the case of zero field and a field \( B_{||} = 4T \) applied parallel to the SiGe quantum well.

There is no indication of any magnetic quenching of the energy gap. In the inset of Fig. 3, \( \rho_{xx} \) vs. \( T \) is shown for \( B = 0 \) and for \( B_{||} = 6T \), for two different carrier densities. Except for an overall increase in the resistivity, the behaviour remains essentially the same.

The difference between the magnetic quenching of the transition in a Si MOSFET \(^8\) and the present observation can be understood by considering the Zeeman effect in a SiGe 2 DHG. The carriers populate a heavy hole subband, with the characteristics \((J, m_J) = (3/2, \pm 3/2)\), where \( J \) is the total angular momentum. Due to the symmetry of this state, \( J \) will be aligned perpendicular to the quantum well, and this arrangement is reinforced by the strain splitting, which further removes the lowest heavy hole state from the light hole states.

Thus the total angular momentum feels an easy axis, and the magnetic energy will be dominated by the magnetic field component perpendicular to the quantum well (in order to break the LS coupling, a field of the order of 100T would be needed). The lack of any influence on the metallic conduction by a parallel magnetic field, together with the breakdown of this phase in systems without an easy axis, supports the hypothesis that a spin related mechanism plays a key role for the MIT in 2 D.

In conclusion, E-field and temperature scaling behaviour have been demonstrated for the MIT observed in a SiGe 2 DHG. Scaling plots lead to a dynamical exponent \( z \approx 1 \) and a correlation length exponent \( \nu \approx 2.85 \). A magnetic field up to 6T applied parallel to the interfaces does not quench the transition.

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