Behavior analysis of bar gaps in welded YT-joints for rolled-steel circular hollow sections

Abstract

We present a parametric analysis of gap variation between the lap brace and through brace of YT welded joints for rolled-steel circular hollow sections on plane steel structures. Our aim is to investigate the collapse behavior of YT-joints under lap brace axial compression. In particular, we focus on e/d0 ratios above 0.25 so bending moments can be taken into account during the design. We find that joint failure is primarily due to chord wall plastification (Mode A) and cross-sectional chord buckling (Mode F) in the region underneath the lap brace. Our joint design followed the Limit States Method, and our results were based on a comparative analysis of three different methods: an analytical solution derived from a set of international technical norms, an experimental analysis, and numerical modeling using Ansys as calibrated by our experimental results.

Keywords

Circular hollow sections, joint, bar gap, finite-element analysis, parametric study.

1 INTRODUCTION

The extensive use of steel frame structures is primarily due to the economic advantages of manufacturing steel frames. In this work, we study the strength of connection joints for tubular steel frames as a function of gap length between the lap and through braces of YT-joints. This work extends earlier studies of tubular joints that focused on experimental tests [5], theoretical analyses using the Finite Element Method [2–4], and analytical work aimed at developing mathematical expressions of the joint strength [6].

2 CALCULATION OF CONNECTION RESISTANCE

The YT joint prototype design uses the methodology presented by Wardenier et al. [10] and Packer and Henderson [7].

The Fig. 1 shows forces general scheme using as a limit the maximum capacity of the vertical brace member of the YT joint and the bending moment due the eccentricity was not considered [9].
NOMENCLATURE

\( A_i \) cross sectional area of member \( i \) \( (i = 0, 1, 2, 3) \);
\( E \) modulus of elasticity;
\( E_t \) modulus of elasticity tangent;
\( M_0 \) bending moment in the chord member;
\( N_i \) axial force applied to member \( i \) \( (i = 0, 1, 2, 3) \);
\( N^* \) joint design resistance expressed in terms of axial load in member \( i \);
\( N_{0P} \) pre-stressing axial force on the chord;
\( W_0 \) elastic section modulus of member \( i \) \( (i = 0, 1, 2, 3) \);
\( d_i \) external diameter of circular hollow section for member \( i \) \( (i = 0, 1, 2, 3) \);
\( e \) nodding eccentricity for a connection;
\( f_y \) yield stress;
\( f_{yi} \) yield stress of member \( i \) \( (i = 0, 1, 2, 3) \);
\( f_0 \) pre-stress in chord;
\( f(n') \) function which incorporates the chord pre-stress in the joint resistance equation;
\( g \) gap between the bracings members of a K, N or KT joint, at the face of the chord;
\( g' \) gap divided by chord wall thickness;
\( n' \) \( \frac{N_{0P}}{f_{0y} A_0} + \frac{M_0}{W_0 f_{0y}} \);
\( t_i \) thickness of hollow section member \( i \) \( (i = 0, 1, 2, 3) \);
\( \beta \) diameter ratio between bracing on chord;
\( \gamma \) ratio of the chord’s half diameter to its thickness;
\( \nu \) Poisson’s ratio;
\( \theta \) included angle between bracing member \( i \) \( (i = 0, 1, 2, 3) \) and the chord;
\( \epsilon \) maximum specific proportionality strain;
\( f \) stress;
\( f_{lP} \) maximum proportionality stress;
\( f_r \) maximum resistance stress;
\( f_1 \) principal stress 1;
\( f_2 \) principal stress 2;

Table 1 shows the geometric characteristics of the VMB 250 circular hollow sections used in the YT joint. The nominal physical proprieties yield stress \( (f_y) \) are equal 250 MPa.

2.1 Validity limits

The YT joint meets all geometrical requirements described in the aforementioned references.
Figure 1 Forces general scheme of YT joint.

Table 1 Physical and geometrical characteristics.

| Member       | Hollow Section | Thickness | Area   | Elastic resistant modulus | Load          |
|--------------|----------------|-----------|--------|---------------------------|---------------|
|              | mm             | mm        | mm²    | mm³                       | kN            |
| Chord        | 114.3          | 6.02      | 2047.83| 52677.51                  | N₀ = -70.39   |
|              |                |           |        |                           | N₀P = 65.75   |
| Lap brace    | 73.0           | 5.16      | 1099.73| 17433.30                  | N₁ = -137.00  |
| Through brace| 73.0           | 5.16      | 1099.73| 17433.30                  | N₂ = 176.67   |
2.2 Calculations

A) YT joint parameters

The YT joint parameters are given by Eq. (1) through Eq. (5):

$$\beta = \frac{d_1 + d_2}{2 \cdot d_0};$$  \hspace{1cm} (1)

$$g' = \frac{g}{t_0};$$  \hspace{1cm} (2)

The stress on the chord, $f_{0P}$, depends most critically on the compressing stress.

$$n' = \frac{f_{0P}}{f_y} = \frac{N_{0P}}{A_0 \cdot f_y} + \frac{M_0}{W_0 \cdot f_y};$$  \hspace{1cm} (3)

$$f (n') = 1.0 + 0.3 \cdot n' - 0.3 \cdot n'^2 \leq 1;$$  \hspace{1cm} (4)

$$f (\gamma, g') = \gamma^{0.2} \cdot \left(1 + \frac{0.024 \cdot \gamma^{1.2}}{1 + \exp(0.5 \cdot g' - 1.33)}\right);$$  \hspace{1cm} (5)

B) Plastic failure of the chord face (Mode A)

Vertical lap brace:

$$N^*_1 = \frac{f_y \cdot t_0^2}{\text{sen} \theta_1} \left(1.8 + 10.2 \cdot \frac{d_1}{d_0}\right) \cdot f (\gamma, g') \cdot f (n');$$  \hspace{1cm} (6)

Diagonal through brace:

$$N^*_2 = N^*_1 \cdot \left(\frac{\text{sen} \theta_1}{\text{sen} \theta_2}\right);$$  \hspace{1cm} (7)

C) Punching shear failure of the chord face (Mode B)

Vertical lap brace and diagonal through brace are both given by Eq. (8):

$$N^*_i = \frac{f_y \cdot t_0 \cdot \pi \cdot d_i}{\sqrt{3}} \cdot \frac{1 + \text{sen} \theta_i}{2 \cdot \text{sen}^2 \theta_i};$$  \hspace{1cm} (8)

D) YT Joint Resistance

The joint resistance is the lowest value obtained in items (B) and (C) above.

Vertical lap brace:

$$\frac{N_i}{N^*_i} < 1;$$  \hspace{1cm} (9)

Diagonal through brace:
\[
\frac{N_2}{N_2^*} < 1;
\]  

Table 2 presents the results of the calculation.

| Joint parameters                                      | Acronym | Calculation |
|-------------------------------------------------------|---------|-------------|
| Relation between diameters                            | \(\beta\) | 0.64        |
| Relation between diameter and thickness               | \(\gamma\) | 9.49        |
| \(n' = \frac{\text{stress}}{f_y} \) (compression)    | \(n'\)  | -0.14       |
| Function of prestress on chord                         | \(f(n')\) | 0.95        |
| Resistance plastic failure of the chord face (Mode A)  | \(N_1^*(Pl)\) | 137.40 kN   |
| Resistance punching shear failure of the chord face (Mode B) | \(N_1^*(Pu)\) | 199.27 kN   |
| Lap brace use                                         | \(N_1/N_1^*\) | 1.0         |
| Resistance plastic failure of the chord face (Mode A)  | \(N_2^*(Pl)\) | 216.42 kN   |
| Resistance punching shear failure of the chord face (Mode B) | \(N_2^*(Pu)\) | 404.16 kN   |
| Through brace use                                     | \(N_2/N_2^*\) | 0.82        |

3 EXPERIMENTAL PROGRAM

To study the joint, four prototypes constructed from seamless rolled tubes were manufactured by V&M do Brasil. They were called pre-experiment, experiments I, II and III [9].

3.1 YT joint prototypes

The dimensions of the prototypes are shown in Fig. 2. The prototypes are fixed by four screws at each end. They were loaded axially at the top of the lap brace.

3.2 Instrumentation for tests

In EXPERIMENTS I, II and III, sixteen 5mm electrical resistance KFG-5-120-C1-11 extensometers were used. Their positions are marked EER1 to EER16 in Fig. 3.

The EERs were placed on the prototype to measure longitudinal strain, drawing on the work of Fung et al [5]. In EXPERIMENT III, 2 rosette gauges and 2 individual extensometers were added (for a total of 24 EERs). Rosette 1 was composed of EER20, EER21 and EER22; rosette 2 was composed of EER17, EER18 and EER19. EER23 and EER24 were placed at the bases of the lap brace and through brace respectively.

In EXPERIMENTS I, II and III, 19 manual reading displacement transducers (TD1 to TD19) and two digital reading displacement transducers (TD20 and TD21) were placed on the prototype as shown in Fig. 4.
3.3 Experimental results

The testing methodology used was defined in three stages, as shown below:

**Stage I.** Before starting the test, the prototype was subjected to a cycle of 10 loading of approximately 20% of the estimated collapse loading for the connection, to minimize friction and check the torque of the screws. Based on pre-test the loading was estimated at 50kN. This level of loading is within the elastic limit of the material. The force was applied in small increments and then it was done downloading.

**Stage II.** During the test the speed of the actuator load was kept as slow and steady as possible.
for both the case of loading and for unloading. The step load was previously set depending on the stage supposed to loading. At each step of loading, when the pre established loading was reached, expected time to stabilize the transducers and then did the reading.

**Stage III.** The prototype was loaded to the ultimate state, where the prototype did not offer more resistance, even after he reached the break. Then the prototype was unloaded.

Fig. 5 shows the overall strain of the prototype in EXPERIMENT III, characterized by the development of failure Mode A.

The results presented by extensometers in each EXPERIMENTS I, II and III are similar, are representing the state of tension expected for each region and thus show that the tests were equivalent.

The results of the last loading for each of the tests are shown in Table 3.

| EXPERIMENTS    | Last loading (kN) |
|----------------|-------------------|
| EXPERIMENT I   | 240.0             |
| EXPERIMENT II  | 358.6             |
| EXPERIMENT III | 316.4             |

Figure 4  Positioning of the DTs on the YT joint prototype.
Two failure modes were observed: plastic failure of the chord face (Mode A) and local buckling of the chord walls (Mode F).

4 ANALYSIS OF FINITE ELEMENTS

Two numerical models were created in Ansys [1], one using a bilinear stress-strain diagram (BISO – Bilinear Isotropic Hardening) and the other a multilinear (piecewise linear) diagram (MISO – Multilinear Isotropic Hardening). Their results were compared to the experimental tests [9].

Both physical and geometrical non-linearity were considered in the analysis. To implement physical non-linearity, we used the stress-strain diagrams obtained through test-body traction. Test bodies cp1a, cp1b for hollow section of diameter 73mm and cp2a e cp2b for hollow section of diameter 114.3mm [9].

The contour conditions were simulated in Ansys through displacement restrictions. Force was applied in an increasing way, that is, at unit load pitches.

Fig. 6 and Fig. 7 show the stress-strain diagrams of test bodies selected for the numerical analysis. The multilinear model is represented by 26 points (crossed circles), and the bilinear model by two straight lines (triangles).

Table 4 shows data used to represent the material properties of test bodies cp1b and cp2b in the numerical model. Note that the bilinear stress-strain diagram always runs from the origin to the first stress peak ($f$), then from this point to the maximum stress ($f_r$) of the material.

The 26 points to represent the multilinear stress-strain diagram is shown by Table 5.
Figure 6  Experimental, bilinear and multilinear stress-strain diagrams used for test body cp1b, from the through brace and lap brace ($\phi 73$mm).

Figure 7  Experimental, bilinear and multilinear stress-strain diagrams used for test body cp2b, from the chord ($\phi 114.3$mm).

Table 4  Data used to represent the bilinear stress-strain diagram with the Ansys software (BISO).

| Test Body   | $f_y$ (MPa) | $f$ (MPa) | $f_r$ (MPa) | $E$ (MPa) | $E_t$ (MPa) |
|-------------|-------------|-----------|-------------|-----------|-------------|
| cp1b($\phi 73$mm) | 326.0       | 331.1     | 486.9       | 189114.6  | 856.5       |
| cp2b($\phi 114.3$mm) | 322.6       | 322.6     | 473.6       | 227390.8  | 840.6       |
Table 5  Data used to represent the multilinear stress-strain diagram with the Ansys software (MISO).

| Points | $\varepsilon$ (Dimensionless) | $f$ (GPa) | $E$ (GPa) | $\varepsilon$ (Dimensionless) | $f$ (GPa) | $E$ (GPa) |
|--------|------------------|------------|-----------|------------------|------------|-----------|
| 0      | 0                | 0          | 0         | 0                | 0          | 0         |
| 1      | 0.001165         | 0.22031    | 189.1146  | 0.001165         | 0.2649     | 227.3908  |
| 2      | 0.0013373        | 0.24958    | 186.6298  | 0.0014234        | 0.31285    | 219.7906  |
| 3      | 0.0015613        | 0.27689    | 177.3458  | 0.0017508        | 0.32257    | 184.2415  |
| 4      | 0.0017853        | 0.29975    | 167.899   | 0.023651         | 0.33273    | 14.06833  |
| 5      | 0.001992         | 0.32604    | 163.6747  | 0.026081         | 0.34245    | 13.13025  |
| 6      | 0.0022849        | 0.3311     | 144.9079  | 0.028562         | 0.3501     | 12.25754  |
| 7      | 0.0176722        | 0.3324     | 18.80942  | 0.031181         | 0.3607     | 11.56794  |
| 8      | 0.021394         | 0.34219    | 15.99467  | 0.034834         | 0.37027    | 10.62956  |
| 9      | 0.023668         | 0.35058    | 14.8124   | 0.037418         | 0.38073    | 10.17505  |
| 10     | 0.026442         | 0.36218    | 13.69715  | 0.043173         | 0.39133    | 9.06423   |
| 11     | 0.029286         | 0.3713     | 12.67841  | 0.047222         | 0.40085    | 8.39969   |
| 12     | 0.032646         | 0.38115    | 11.67524  | 0.052478         | 0.41042    | 7.820801  |
| 13     | 0.036229         | 0.39585    | 10.92633  | 0.059905         | 0.42068    | 7.022452  |
| 14     | 0.038728         | 0.40007    | 10.33025  | 0.068554         | 0.43103    | 6.287452  |
| 15     | 0.043656         | 0.41183    | 9.43526   | 0.0786           | 0.44115    | 5.612595  |
| 16     | 0.048567         | 0.42287    | 8.706941  | 0.0874737        | 0.45456    | 5.092552  |
| 17     | 0.055838         | 0.43131    | 7.72431   | 0.093987         | 0.45077    | 4.796089  |
| 18     | 0.061989         | 0.44038    | 7.104164  | 0.1006035        | 0.45302    | 4.50305   |
| 19     | 0.068227         | 0.4504     | 6.601492  | 0.11285          | 0.46019    | 4.077891  |
| 20     | 0.080736         | 0.46188    | 5.720868  | 0.12118          | 0.46171    | 3.810117  |
| 21     | 0.096589         | 0.47179    | 4.884511  | 0.13124          | 0.465      | 3.543127  |
| 22     | 0.1074614        | 0.47472    | 4.417572  | 0.14001          | 0.46647    | 3.331691  |
| 23     | 0.1159           | 0.48035    | 4.144521  | 0.15042          | 0.46932    | 3.120064  |
| 24     | 0.1316533        | 0.48221    | 3.662694  | 0.1611           | 0.4701     | 2.918063  |
| 25     | 0.14347          | 0.48564    | 3.384959  | 0.17035          | 0.47025    | 2.760493  |
| 26     | 0.18417          | 0.48688    | 2.643644  | 0.18148          | 0.47364    | 2.609874  |
The Poisson’s ratio was obtained by compression test tube used. The value obtained was \( \nu = 0.3 \).

The SHELL element was considered most appropriate to represent hollow structures. Specifically, the SHELL181 element was used to generate a mesh for the hollow sections. The SHELL63 element was used for fixation plates. Table 6 shows their characteristics.

| Elements   | Nr of nodes per element | Degrees of freedom | Special features       |
|------------|-------------------------|--------------------|------------------------|
| SHELL 63   | 4                       | 6                  | Elastic Large deflection Little strain |
| SHELL 181  | 4                       | 6                  | Plastic Large deflection Large strain |

5 COMPARISON BETWEEN EXPERIMENTAL TEST RESULTS AND NUMERICAL MODEL RESULTS

The experimental tests and numerical models can be compared on the basis of strains obtained by the extensometers [9].

For the rosettes, comparisons between theory and experiment can be made between the principal stresses.

Fig. 8 show the principal stresses \( f_1 \) measured at rosette 1 in EXPERIMENT III and the numerical models.

![Figure 8](image)

Figure 8  Principal stress \( f_1 \) measured at rosette 1 in EXPERIMENT III and the numerical models.
The principal stresses $f_1$ of the two numerical models were in good agreement with those obtained by rosette 1 in EXPERIMENT III.

6 METHODS USED FOR PARAMETRIC ANALYSIS

Summarizing, the overall geometry and minimum allowable gap size of the YT-joint described in this work is shown in Fig. 2. Using this schematic, we fabricated and tested four test specimens in the laboratory and generated numerical models using program Ansys. Our numerical models were calibrated using our experimental results, so as to precisely represent the predefined gap in the YT-joint [9]. These models used a SHELL181 four-node element for the tubular sections, and we took into account both material and geometric nonlinearity effects [8], the latter using a Multilinear Isotropic Hardening (MISO) material.

We performed a parametric analysis to study the effect of gap size between the lap brace and through brace on the overall strength of the YT-joint. The motivation for this study stems from the observation that the gap length can influence the resistance to chord wall plastification failure (Mode A) for YT-joints using circular hollow sections.

According to Packer and Henderson [7], the $e/d_0$ ratio for the joint must satisfy the limits given by Eq. (11); this represents the range over which the effects of the joint’s bending moments can be disregarded, namely.

$$-0.55 \leq \left( \frac{e}{d_0} \right) \leq 0.25.$$

If these eccentricity boundaries are exceeded, then the generated moment has a detrimental effect on the joint strength since the moment must be distributed between the braces. If this occurs, the joint capacity must be checked for interaction between the axial force and the bending moment.

Note that for gap lengths greater than the lowest acceptable value of $g=10.33$ mm, we have $g \geq t_1 + t_2$ and the $e/d_0$ ratio exceeds the boundary condition of 0.25. Consequently, this work will focus on $e/d_0$ ratios between 0.25 and 0.97 when analyzing new models. Our overall focus is to study the strength YT-joints for gap lengths greater than $g=10.33$ mm, with emphasis on the influence of bending moments on the overall joint design.

7 GAP LENGTH MODELS

Table 7 shows the gap lengths studied here, along with their corresponding eccentricity “e” values and $e/d_0$ ratios.

A numeric model was generated using Ansys for each gap size; hereafter, we refer to each model using the gap size as “GAP10.33”, “GAP30”, “GAP50”, “GAP70”, “GAP90” and “GAP110”.

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Table 7  Gap lengths, eccentricities and $e/d_0$ ratios of models studied in this work.

| Gap Lengths (mm) | e (mm) | $e/d_0$ |
|------------------|--------|---------|
| gap=10.33 (GAP10.33) | 28.57 | 0.25 |
| gap=30 (GAP30) | 44.73 | 0.39 |
| gap=50 (GAP50) | 61.17 | 0.54 |
| gap=70 (GAP70) | 77.60 | 0.68 |
| gap=90 (GAP90) | 94.03 | 0.82 |
| gap=110 (GAP110) | 110.47 | 0.97 |

8 RESULTS FOR THE EFFECT OF GAP LENGTH ON YT-JOINT STRENGTH

The principal stresses $f_1$ for each gap size are shown in Figs. 9 through 14. For all models, the largest stresses were observed on the chord at the joint intersection.

![Figure 9 Principal stress $f_1$ for model “GAP10.33”](image)

Figure 9  Principal stress $f_1$ for model “GAP10.33”.

Our models show that the stress distributions between the lap brace and through brace are indeed influenced by the gap size. As seen in Fig. 15, varying gap sizes from the “GAP10.33” to “GAP110” models produces approximately twice the principal stress $f_1$ for the same load of 100kN.

For each model, the respective yield load was then determined based on a yield strength of $\sigma_e = 0.33$ GPa, as defined by a tensile test [8]. Table 8 shows the yield load for each of the new models. As the gap size increases, the yield load of the joint decreases, which translates into a smaller load supported on the top of the lap brace. Hence the larger the gap size, the smaller the load transfer efficiency between the braces.
Figure 10  Principal stress \( f_1 \) for model "GAP30".

Figure 11  Principal stress \( f_1 \) for model "GAP50".
Figure 12  Principal stress $f_1$ for model "GAP70".

Figure 13  Principal stress $f_1$ for model "GAP90".
Figure 14 Principal stress $f_1$ for model "GAP110".

Figure 15 Principal stress $f_1$ for our numeric models.
### Table 8 Yield load for our numeric models.

| Gap Length (mm) | Yield Load (kN) |
|-----------------|-----------------|
| gap=10.33 (GAP10.33) | 161 |
| gap=30 (GAP30) | 131 |
| gap=50 (GAP50) | 121 |
| gap=70 (GAP70) | 115 |
| gap=90 (GAP90) | 109 |
| gap=110 (GAP110) | 104 |

### 8.1 Failure modes

The predominant failure modes for “GAP30” through “GAP110” are shown in Figs. 16 through 19, respectively. This shows that the main failure mechanisms are due to chord wall plastification (Mode A) and chord buckling (Mode F).

![Figure 16](plastic_failure_gap30.png)  
*Figure 16 Plastic failure due to chord wall plastification in model "GAP30".*

### 9 NUMERICAL ANSYS ANALYSIS OF DIMENSION LOAD VERSUS YIELD LOAD

We designed the tubular YT-joint specimen using values presented by CIDECT [10] and Packer and Henderson [7]. This gave a dimension load of 137 kN with 100% efficiency on the top of the lap brace and 82% efficiency for the through brace (Item 2). Note that we did not take bending moments into consideration during the design calculations since $e/d_0=0.25$.

Recall that the Mode A failure depends on the gap length. The dimension loads for each
Figure 17  Chord buckling in model “GAP30”.

Figure 18  Plastic failure due to chord wall plastification in model “GAP110”.

of the new models were calculated in the same way as before, except that we took bending moments into consideration since $e/d_0 > 0.25$. We compared the results with the yield loads supplied by Ansys, and our results are presented in Fig. 20.

Table 9 shows the values of dimension load, yield load and the percent difference between them.

| Gap Model | Dimension Load (kN) | Yield Load (kN) | Percent Difference |
|-----------|---------------------|----------------|-------------------|
| GAP10.33  | 137                 | 161            | 17.52%            |
| GAP30     | 114                 | 131            | 14.91%            |
| GAP50     | 112                 | 121            | 8.04%             |
| GAP70     | 113                 | 115            | 1.77%             |
| GAP90     | 111                 | 109            | -1.80%            |
| GAP110    | 108                 | 104            | -3.70%            |
10 CONCLUSIONS

We found that variation in gap lengths do not alter the principal failure mode for YT-joints. The principal failure modes are due to wall chord plastification (Mode A) and chord buckling (Mode F) regardless of the gap length. For gap lengths between $g=10.33$ mm and $g=110$ mm, the percent difference between the dimension load and the yield load decreases as the gap length increases. For gap values up to $g=70$ mm, the yield load of the numerical model is above the dimension load, implying that such designs are safe. For gap lengths greater than $g=70$ mm, the yield load falls short of the dimension load, implying that such designs are unsafe and the existing formulations of such joint designs should be reexamined.

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