Local Feature Hashing With Binary Auto-Encoder for Face Recognition

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ABSTRACT The learning-based hashing has recently made encouraging progress in face recognition. However, most existing hashing methods disregard the discrete constraint during optimization, inducing the accumulated quantization errors. In this work, we develop an effective learning-based hashing model, namely local feature hashing with binary auto-encoder (LFH-BAE), to directly learn local binary descriptors in the Hamming space. It attempts to exploit structure factors to well reconstruct the face image from binary codes. Specifically, we first introduce a binary auto-encoder to learn a hashing function to project each face region into high-quality binary codes. Since the original problem is a tricky combinational function, we then present a softened version to decompose it into separate tractable sub-problems. Next, we propose an effective alternating algorithm based on the augmented Lagrange method (ALM) to solve these sub-problems, which helps to generate strong discriminative and excellent robust binary codes. Moreover, we utilize the discrete cyclic coordinate descent (DCC) method to optimize binary codes to reduce the loss of useful information. Lastly, we cluster and pool the obtained binary codes, and construct a histogram feature as the final face representation for each image. Extensive experimental results on four public datasets including FERET, CAS-PEAL-R1, LFW and PaSC show that our LFH-BAE is superior to most state-of-the-art face recognition algorithms.

INDEX TERMS Binary auto-encoder, binary feature, discrete optimization, face recognition, feature hashing.

I. INTRODUCTION
Face recognition has been a popular research topic in computer vision due to its potential applications in various real-world scenarios. Over the past thirty decades, a variety of face recognition algorithms have been proposed in the literatures [1]–[11]. These algorithms have achieved encouraging recognition performance but often only in the controlled scenarios. With the development of the social network technology and image capturing devices, there has been grown interest in face recognition under the uncontrolled scenarios. However, face recognition under those conditions is even more difficult due to the unpredictability of numerous variations such as pose, occlusion, aging, illumination, expression and resolution. According to the existing works, face representation is the most important component of a face recognition system. Therefore, the key challenge for practical face recognition system is to obtain robust face representations that are invariant to the real-world variations.

In recent years, local features have been studied extensively due to their stabilities and robustness to local changes. Numerous local feature algorithms have sprung up in the field of face recognition. Based on the designing methodology, existing local features can be classified into two categories: hand-crafted features [1], [2], [4] and learning-based features [3], [5], [7]. Typical hand-crafted features are local binary pattern (LBP) [1], scale-invariant feature transform (SIFT) [2] and Gabor wavelets [4]. The hand-crafted features are data-independent and usually require strong prior knowledge to elaborately engineer them, which only work well against the variations of the controlled scenarios. Unlike the hand-crafted features, the learning-based features are extracted from the raw face data in a data-driven way and they can obtain satisfying performance in the unconstrained scenarios. Various learning-based features have been proposed such as local quantized pattern (LQP) [12], discriminant face descriptor (DFD) [3], compact binary feature descriptor (CBFD) [5] and context-aware local binary feature learning (CA-LBFL) [7]. Among them, the binary codes obtained by the learning-based hashing methods
Fig. 1 illustrates the framework of our proposed LFH-BAE model for face recognition. In the training procedure, we first extract patch-wise pixel difference vectors (PDVs) from each face image and learn an encoding matrix $R$ and an encoding bias $\delta_1$ to project the PDVs into high-quality binary codes, which are produced in the Hamming space in a closed form. Then, an unsupervised clustering is performed on the binary codes to obtain a codebook $D$ for feature pooling. In the testing procedure, we first extract the PDVs for the testing image and then utilize the learned encoding matrix and bias to project the PDVs into discriminative binary codes. Finally, we use the learned codebook to pool the binary codes into histogram feature representations.

(i.e., CBFD and CA-LBFL) show stronger discriminative power due to their compact nature, energy saving and even distribution.

Due to the binary constraint imposed on the binary codes, the discrete hashing optimization is a NP-hard problem. To simplify the solving process, the above learning-based hashing methods follow the two-step “relaxing + thresholding” optimization procedure to learn binary codes. Specifically, they first relax the binary constraint to obtain continuous solutions, and then binarize the resulting values to binary codes by thresholding. However, such traditional two-step optimization disregards the binary nature of the hashing codes, inducing the accumulated quantization errors and leading to the loss of useful information. Therefore, how to learn high-quality binary codes to eliminate the accumulated quantization errors remains a central problem in face recognition.

In this paper, we introduce a simple unsupervised binary hashing model, dubbed local feature hashing with binary auto-encoder (LFH-BAE), to directly learn binary codes in the Hamming space for face representation. The proposed LFH-BAE differs from previous binary hashing methods for face recognition in two aspects. For one thing, the proposed LFH-BAE combines the binary encoder with decoder, so the encoder can receive the feedback of the decoder in the feature learning stage. Thus, the binary auto-encoder can exploit more salient information for subsequent feature pooling. For another, it respects the binary nature of the problem when implementing the discrete hashing optimization, so that the accumulated quantization errors can be somehow eliminated.

Fig. 1 illustrates the framework of our proposed LFH-BAE model. Firstly, we extract the patch-wise pixel difference vectors (PDVs) from each face image and cascade them into a large pixel difference matrix (PDM). Inspired by the fact that local binary codes are robust to intra-class variations and auto-encoder can capture the manifold structure, we then introduce the binary auto-encoder to learn a hashing function to project PDM into high-quality binary codes. It is tricky to solve the original objective function of the auto-encoder due to the three hard constraints imposed on the output of the encoder. To address this, we propose a softened version of the binary auto-encoder by introducing an auxiliary variable to minimize the binary quantization loss. By doing so, we can break the combinational complexity of the original problem and convert it into separate feasible sub-problems. We put forward an effective alternating optimization algorithm based on the augmented Lagrange method (ALM) [13] to solve these sub-problems, which not only can explicitly cope with the discrete constraint, but also consider the bit-independent constraint and bit-balanced constraint together. To deal with the most pivotal sub-problem, i.e., discrete optimization for binary codes, we utilize the discrete cyclic coordinate descent (DCC) method to directly learn binary codes in the Hamming space. The ALM-based alternating optimization algorithm enables LFH-BAE to generate strong discriminative and excellent robust binary codes, which are very favorable for face recognition. Finally, we construct a codebook by clustering on the obtained binary codes and pool them into a high-dimensional histogram feature as the final representation for each face image. We perform extensive experiments on FERET, CAS-PEAL-R1, LFW and PaSC datasets and experimental results show that our proposed model outperforms most existing state-of-the-art methods.

The main contributions of this work are summarized as follows:

1) We propose an unsupervised binary auto-encoder to capture the salient structure inherent in the raw data and learn high-quality binary features for face representation. With the well-trained binary auto-encoder, the learned binary codes can best approximate the global data space and deliver more identity information.

2) To reduce the combinational complexity of the original problem, we transform the binary auto-encoder with three constraints to a softened version by minimizing the binary quantization loss, and then decompose the original problem into separate tractable sub-problems.

3) Moreover, we propose an efficient alternating optimization algorithm based on the ALM to directly compute the discrete solution in the Hamming space. Our method can not only address the binary constraint, but also take the bit-balanced and bit-independent constraints into consideration. Thus, the accumulated quantization errors caused by the “relaxing + thresholding” optimization method can be effectively eliminated and high-quality binary codes can be obtained.
4) We conduct extensive face recognition experiments on four public datasets consisting of FERET, CAS-PEAL-R1, LFW and PaSC to evaluate the effectiveness and generalization ability of our LFH-BAE. The results on these datasets demonstrate that our model is superior to most of state-of-the-art face recognition algorithms.

II. BACKGROUND AND RELATED WORKS

Since our proposed hashing model is a learning-based binary auto-encoder for face recognition, in this section, we concentrate on the following three related topics: 1) face feature learning, 2) feature representation based on auto-encoders, and 3) binary hashing.

A. FACE FEATURE LEARNING

Recently, feature learning has made abundant achievements in the field of face recognition [3], [14]–[19]. Lei et al. [3] combine the image filter with the optimal soft sampling to obtain LBP-like features. Chang et al. [14] incorporate the sparse constraints into the low-rank regression optimization to analyze the importance of each feature under the PCA criteria. Aslan et al. [15] propose a multi-channel multi-model method that uses various techniques to extract features from multiple regions. Yi et al. [16] utilize the Restricted Boltzmann Machines (RBMs) to learn the shared representations from the extracted Gabor features to eliminate the heterogeneity locally. He et al. [17] propose a dynamic feature matching (DFM) method, which deals with partial face images by combining the fully convolutional network (FCN) with sparse representation classification (SRC). Liu et al. [18] propose a deep hypersphere embedding method to learn face features with angular margin. Liu et al. [19] present a graph-based manifold learning method to extract sparse feature representations for face recognition.

Since the learning-based algorithms can exploit discriminative information from the face data in a data-driven way, these methods, especially the convolutional neural networks (CNNs), perform better than the hand-crafted methods in various face recognition tasks. However, there are two drawbacks of CNNs in practical applications. Firstly, the CNNs are required to estimate extensive parameters from a large amount of labeled samples, which leads to time consuming in the training process. Secondly, due to privacy protection, it is very difficult to collect the labeled data in real applications. Therefore, we propose an unsupervised low-level feature learning algorithm for face recognition.

B. FEATURE REPRESENTATION BASED ON AUTO-ENCODES

As a typical learning method, auto-encoder can extract structure factors inherent in the input data automatically. It has shown its effectiveness and efficiency in various computer vision tasks [20]–[24]. Kan et al. [20] use the stacked progressive auto-encoder to extract the pose-robust features for face recognition. Cheng et al. [21] propose a double channel stacked sparse denoising auto-encoder (DC-SSDA) to eliminate or reduce the influence of the occlusions. Gao et al. [22] first associate the label information with the auto-encoder to form a deep supervised auto-encoder. Then, they introduce the similarity preservation term into the supervised auto-encoder to extract robust representations for single sample per person face recognition. The work [23] employs the stacked auto-encoder to pre-train the weights of the deep CNN and improves the performance of the facial emotion recognition. Xu et al. [24] use two shallow neural networks to connect two auto-encoders to deal with the age-invariant face recognition and retrieval problems.

The objective functions of these auto-encoder methods are similar to that of ours. Different from these methods, on the one hand, we only employ one layer auto-encoder to learn projections effectively and efficiently. The reason for choosing this strategy is that binary codes show strong robustness to local intra-class variants. On the other hand, there are three challenging constraints imposed on the output of the binary encoder, so it is more difficult to optimize the objective function than those of existing auto-encoders.

C. BINARY HASHING

Binary codes has gained increasing attention due to their high storage efficiency, fast matching speed and strong robustness in computer vision. In recent years, a lot of works on binary hashing have emerged in the area of computer vision [25]–[34]. Locality Sensitive Hashing (LSH) [25] is a classic hashing method in existing hashing strategies, which obtains hashing functions according to random projections. As an extension of the LSH, density sensitive hashing (DSH) [26] exploits the geometric information of the data to generate hashing codes consistent with the distribution of data points. The work [27] introduces an effective sparse regularizer in the objective function to improve the computational efficiency and solve the overfitting problem. Zhu et al. [28] propose a discrete semantic transfer hashing (DSTH) method to exploit the auxiliary contextual patterns to enhance the semantics of hashing codes for image retrieval. He et al. [29] present a bidirectional discrete matrix factorization hashing (BDMFH) model to force the hashing codes to inherit the latent structure of the raw data. Supervised discrete multi-view hashing (SDHM) [30] applies the integrated multi-view feature mapping and latent binary coding to the image data to learn discriminative hashing codes. Robust discrete code modeling (RDCM) [31] uses the $\ell_{2,p}$ norm to restrain the impact of the unreliable discrete codes and noise labels. The collective reconstructive embeddings (CRE) [32] method employs specific hashing modalities for varying modes to reduce the loss of detailed information. Xu et al. [33] develop a discrete cross-modal hashing (DCH) method to exploit the discriminative information of the class labels to learn unified hashing codes for cross-modal retrieval. Han et al. [34] employ the residual net architecture into the hashing model to address the uneven
distribution problem. However, these available hashing methods are proposed for visual search.

Some learning-based hashing methods are also put forward for face recognition. For example, Lu et al. [5] propose a compact binary feature descriptor (CBFD) method to learn compact binary features for face representation in an unsupervised way. They then develop a simultaneous local binary feature learning and encoding (SLBFL) [6] approach to jointly learn the projection matrix and the codebook (also known as dictionary) for each face patch to obtain discriminative face representations. The work [7] presents a context-aware local binary feature learning (CA-LBFL) method, an improvement of CBFD, which exploits the exploitation within each binary feature to extract more robust information. However, these algorithms ignore the discrete constraint in the binary hashing optimization, causing the loss of useful information and obtaining inferior hashing functions. In contrast, our proposed LFH-BAE respects the discrete nature of the binary codes and constrains the hashing optimization in the Hamming space to obtain high-quality hashing functions.

III. LOCAL FEATURE HASHING WITH BINARY AUTO-ENCODER

In this section, we first describe how to extract the PDM from a face image patch. Then, we present the formulation and optimization process of LFH-BAE in details. Finally, we show the face representation process based on the LFH-BAE. The notations of this work are summarized in table 1.

### A. THE EXTRACTION PROCESS OF PDM

Since PDV measures the difference between the central pixel and the neighboring ones of the same patch, it can encode important visual patterns [5], and we utilize the PDVs to learn the face feature representation. Let \( \Omega = \{ \Omega_1, \Omega_2, \ldots, \Omega_n \} \) be the training set including \( n \) original face samples, where \( \Omega_i \) is the \( i \)th face image and \( 1 \leq i \leq n \). We extract the patch-wise PDVs from each face image and cascade them into a PDM. All \( N \) PDV samples of the training set are grouped into a large PDM \( X = \{ x_1, x_2, \ldots, x_N \} \), where \( x_j \in \mathbb{R}^d \) is the \( j \)-th PDV and \( 1 \leq j \leq N \). Fig. 2 illustrates the extraction approach of the PDM from an original face image. The neighbors of each pixel of the original image are considered within a range of \((2R + 1)(2R + 1)\), so the dimensionality of each PDV can be computed as \( d = (2R + 1)(2R + 1) - 1 \).

### B. FORMULATION

The binary hashing codes can well reflect the visual information of local image region, and encode important visual patterns (such as edges and lines) of the face image, thereby effectively alleviating the influence of noise factors. In order to obtain binary codes with three properties of effective reconstruction ability, excellent robustness and strong discriminative power, our proposed model should follow the following three restrictions. 1) The objective function should comply with a whole reconstruction criterion to exploit structure information to best approximate the entire face data space. 2) The binary bits should be independent and balanced to reduce redundancy factors while delivering more discriminative information. 3) The binary constraint of the problem should be taken into consideration in the hashing optimization to avoid the accumulated quantization errors to obtain high-quality binary codes.

By integrating the above first two restrictions, we formulate the following objective function

\[
\begin{align*}
\min_{\{R_i, \delta_i\}_{i=1}^N} & \left( \frac{1}{2} \right) \left\| X - (R_1(R_1X + \delta_11^T) + \delta_21^T) \right\|_F^2 \\
& + \left( \frac{\beta}{2} \right) \left( \|R_1\|_F^2 + \|R_2\|_F^2 \right) \\
\text{s.t.} & \ (R_1X + \delta_11^T) \in \{-1, 1\}^{K \times N}, \\
& \ (R_1X + \delta_11^T)1 = 0, \\
& \ (R_1X + \delta_11^T)^T(R_1X + \delta_11^T) = NI_K.
\end{align*}
\]

where \( \beta \) is a turning parameter to adjust the balance of different terms. The encoding matrix \( R_1 \in \mathbb{R}^{K \times d} \) and bias

| TABLE 1. Notations and their descriptions in this paper. |
|-----------------|-----------------|
| Notation | Description |
|----------------|----------------|
| \( X \) | \( X = \{ x_i \}_{i=1}^n \in \mathbb{R}^{d \times N} \): training set of \( N \) PDV samples |
| \( R \) | the radius of sampling patch |
| \( K \) | binary code length |
| \( D \) | codebook size |
| \( R_i, \delta_i \) | \( R_i \in \mathbb{R}^{d \times K}, \delta_i \in \mathbb{R}^d \): encoding matrix and bias of encoder |
| \( R_j, \delta_j \) | \( R_j \in \mathbb{R}^{d \times K}, \delta_j \in \mathbb{R}^d \): decoding matrix and bias of decoder |
| \( I \) | column vector with all ones |
| \( I \) | identity matrix |
\( \delta_1 \in \mathbb{R}^{K \times 1} \) map each PDV \( x_i \in \mathbb{R}^d \) into a low-dimensional binary vector \((R_1x_i + \delta_1) \in \{-1, 1\}^{K \times 1}\), while \( R_2 \in \mathbb{R}^{d \times K} \) and \( \delta_2 \in \mathbb{R}^{d \times 1} \) in turn map the binary code back to \( \mathbb{R}^d \) in an attempt to reconstruct the PDV. Note that the weight-tying constraint \((R_1 = (R_2)^T)\) is not involved in our binary auto-encoder.

The first term of problem (1) ensures that the reconstruction loss between the input and the output of the binary auto-encoder is minimized, which enables (dis)similar input information loss between the input and the output of the binary encoder.

We introduce a new auxiliary variable \( B \) and reformulate (1) as

\[
\min_{B, \|R_1, \delta_1\|_1} \left( \frac{1}{2} \|X - (R_2B + \delta_2^1I)\|_F^2 \right.
\]

\[
+ \left( \frac{\alpha}{2} \right) \|B - (R_1X + \delta_1^1I)\|_F^2
\]

\[
+ \left( \frac{\beta}{2} \right) \left( \|R_1\|_F^2 + \|R_2\|_F^2 \right)
\]

s.t. \( B \in \{-1, 1\}^{K \times N}, \quad B1 = 0, \quad BB^T = N I_K \). \hspace{1cm} (2)

where \( \alpha (\alpha > 0) \) adjusts the balance between terms. Such a softened version is encouraging due to the absence of the sgn(·) function in the encoder. The second term of (2) minimizes the quantization loss by compelling the output of encoder close to binary hashing values, and meanwhile the first term still guarantees a good reconstruction of the global input space. The solution of (2) will be closer to that of the original problem (1) by setting the parameter \( \alpha \) reasonably large enough.

By introducing the auxiliary variable \( B \), the awkward original problem can be decomposed into separate tractable subproblems. We solve them via alternating optimization, which will be discussed in details in the next section.

C. OPTIMIZATION

The objective function (2) is a NP-hard problem due to the three constraints imposed on the binary codes. To address this, we utilize the alternating approach based on the ALM [13] to optimize (2), i.e., optimizing the objective function for one variable each time while the others are fixed. We optimize the variables by iteratively solving the following subproblems.

1) \( \text{FIX } \delta_1, \delta_2 \text{ AND } B, \text{ OPTIMIZE } R_1, R_2 \)

When \( \delta_1, \delta_2 \) and \( B \) are fixed, the objective functions for \( R_1 \) and \( R_2 \) can be rewritten as

\[
\min_{R_1} \left( \frac{\alpha}{2} \|B - (R_1X + \delta_1^1I)\|_F^2 + \left( \frac{\beta}{2} \right) \|R_1\|_F^2 \right. \hspace{1cm} (3)
\]

\[
\min_{R_2} \left( \frac{\alpha}{2} \|B - (R_1X + \delta_1^1I)\|_F^2 + \left( \frac{\beta}{2} \right) \|R_2\|_F^2 \right) \hspace{1cm} (4)
\]

The objective functions (3) and (4) are both regularized least squares problems. By computing the derivatives of the functions for \( R_1 \) and \( R_2 \), and then set them to 0, respectively, we get the closed form solutions for \( R_1 \) and \( R_2 \) as follows

\[
R_1 = \alpha (B - \delta_1^1I)^T X (\alpha X X^T + \beta I)^{-1} \hspace{1cm} (5)
\]

\[
R_2 = (X - \delta_2^1I) B^T (B B^T + \beta I)^{-1} \hspace{1cm} (6)
\]

2) \( \text{FIX } R_1, R_2 \text{ AND } B, \text{ OPTIMIZE } \delta_1, \delta_2 \)

When \( R_1, R_2 \) and \( B \) are fixed, the objective functions for \( \delta_1 \) and \( \delta_2 \) are reformulated as follows

\[
\min_{\delta_1} \left( \frac{1}{2} \|B - (R_1X + \delta_1^1I)\|_F^2 \right) \hspace{1cm} (7)
\]

\[
\min_{\delta_2} \left( \frac{1}{2} \|X - (R_2B + \delta_2^1I)\|_F^2 \right) \hspace{1cm} (8)
\]

The closed solutions for (7) and (8) with respect to \( \delta_1 \) and \( \delta_2 \) can be denoted as

\[
\delta_1 = (1/N)(B - R_1 X) 1 \hspace{1cm} (9)
\]

\[
\delta_2 = (1/N)(X - R_2 B) 1 \hspace{1cm} (10)
\]

3) \( \text{FIX } R_1, R_2, \delta_1 \text{ AND } \delta_2, \text{ OPTIMIZE } B \)

We first fix \( R_1, \delta_1, R_2 \) and \( \delta_2 \), and then discard the constant terms, problem (2) for \( B \) can be rewritten as

\[
\min_{B} \left( \frac{1}{2} \|R_2B\|_F^2 - \text{Tr}(B^T R_1 X (X - \delta_2^1I)) \right)
\]

\[
- \alpha \text{Tr}(B^T (R_1 X + \delta_1^1I)) \hspace{1cm} (11)
\]

s.t. \( B \in \{-1, 1\}^{K \times N}, \quad B1 = 0, \quad BB^T = N I_K \)

where \( \text{Tr}(\cdot) \) denotes the trace norm.

According to the above third restriction (see section III B) of our LFH-BAE, the discrete optimization should be constrained in the Hamming space to reduce the information loss caused by the traditional two-step optimization procedure. In this work, we employ ALM [13] to optimize (11) and adopt the DCC method to explicitly address the discrete constraint with one step. Our main idea is to separate the three challenging constraints by introducing another auxiliary variable \( Z \) and impose the balanced and independent constraints on it, and meanwhile apply quadratic penalty between \( B \) and \( Z \). Thereby, the objective function (11) is transformed into an augmented Lagrangian (AL) function

\[
\min_{B, Z} \left( \frac{1}{2} \|R_2B\|_F^2 - \text{Tr}(B^T R_1 X (X - \delta_2^1I)) \right)
\]

\[
- \alpha \text{Tr}(B^T (R_1 X + \delta_1^1I)) \hspace{1cm} (11)
\]

\[
+ \left( \frac{\gamma}{2} \right) \|B - Z + \delta_1^1I\|_F^2 \hspace{1cm} (11)
\]
s.t. $B \in \{-1, 1\}^{K \times N}$, $Z1 = 0$, $ZZ^T = NI_K$.  

where $\Delta, \gamma$ is defined as the difference between the target variable $B$ and auxiliary one $Z$, and $\gamma$ is defined as the AL penalty parameter.

When $R_1$, $\delta_1$, $R_2$, $\delta_2$, $Z$ and $\Delta, \gamma$ are fixed, problem (12) for $B$ can be rewritten as

$$
\min_{B} \frac{1}{2} \|B2_B\|_F^2 - \text{Tr}(B^T R_2 (X - \delta_1 1^T)) - \alpha \text{Tr}(B^T(R_1 X + \delta_1 1^T)) - \gamma \text{Tr}(B^T(Z + \Delta, \gamma / \gamma))
$$

s.t. $B \in \{-1, 1\}^{K \times N}$

(13)

We directly optimize $B$ in the Hamming space with respect-ting the binary constraint $B \in \{-1, 1\}^{K \times N}$. Let $\bar{X} = X - \delta_1 1^T$, $O = R_1 X + \delta_1 1^T$, $P = Z - \Delta, \gamma / \gamma$, with a series of mathematical operations, (13) can be equivalently transformed into the following problem

$$
\min_{B} \|B2_B\|_F^2 - 2\text{Tr}(B^T R_2 \bar{X} + \alpha B^T O + \gamma B^T P)
$$

s.t. $B \in \{-1, 1\}^{K \times N}$

(14)

For convenience, problem (14) can be simply rewritten as

$$
\min_{B} \|B2_B\|_F^2 - 2\text{Tr}(B^T Q)
$$

s.t. $B \in \{-1, 1\}^{K \times N}$

(15)

where $Q = R_2^T \bar{X} + \alpha O + \gamma P$. Similar to the optimization idea of [35] and [36], we adopt the DCC method to learn the binary codes $B$ bit-by-bit. Let $b_i^T$, $q^T$ and $r^T$ be the ith row of $B$, $Q$ and $R^2_i$, respectively, where $i = 1, 2, \ldots, K$, we utilize $B$, $Q$ and $R$ to denote the remaining matrix of $B$, $Q$ and $R^2_i$, respectively. From the derivation in [37], problem (15) can be converted into the following form

$$
\min_{b} \|r^T B - q^T b\|_2
$$

s.t. $b \in \{-1, 1\}^N$

(16)

The optimal solution for $b$ can be denoted as

$$
b = \text{sgn}(q - \bar{B}^T \bar{R} r)
$$

(17)

4) FIX $R_1$, $R_2$, $\delta_1$, $\delta_2$, $B$ AND $\Delta, \gamma$, OPTIMIZE $Z$

When $R_1$, $\delta_1$, $R_2$, $\delta_2$, $B$ and $\Delta, \gamma$ are fixed, problem (12) for $Z$ can be reformulated as

$$
\min_{Z} \|B - Z + \Delta, \gamma / \gamma\|_F^2
$$

s.t. $Z1 = 0$, $ZZ^T = NI_K$

(18)

The above objective function is simplified to the following maximization problem

$$
\max_{Z} \text{Tr}(Z^T S)
$$

s.t. $Z1 = 0$, $ZZ^T = NI_K$

(19)

where $S = B + \Delta, \gamma / \gamma$. By performing singular value decomposition (SVD), $S$ can be formulated as $S = U \Lambda V^T = \sum_{k=1}^r \sigma_k u_k v_k^T$, where $r \leq K$ is the rank of $S$, $\Lambda$ is a rectangular diagonal matrix and its diagonal elements $\sigma_1, \sigma_2, \ldots, \sigma_r$ are non-negative singular values of $S$. $U = [u_1, u_2, \ldots, u_r]$ and $V = [v_1, v_2, \ldots, v_r]$ are left- and right-singular vectors of $S$, respectively. Based on the above analyses, it is easy to derive that $V^T Z^T U U^T Z V = NI$.

**Algorithm 1** Local Feature Hashing with Binary Auto-encoder

**Input:** training data: $X$, binary code length: $K$, iteration number: $T$, parameters: $\alpha, \beta, \gamma, \eta$.

**Output:** encoding matrix: $R_1$, encoding bias $\delta_1$, decoding matrix: $R_2$, decoding bias: $\delta_2$.

1: **Initialization:** Initialize $B$ using ITQ, initialize $Z$ randomly, initialize $\delta_1 = 0$, $\delta_2 = 0$ and $\Delta, \gamma = 0$.

2: **repeat**

3:   $(R_1, R_2) \rightarrow$ step: Optimize $R_1$ and $R_2$ according to (5) and (6), respectively.

4:   $(\delta_1, \delta_2) \rightarrow$ step: Optimize $\delta_1$ and $\delta_2$ according to (9) and (10), respectively.

5: **repeat**

6:   $B \rightarrow$ step: Optimize $B$ utilizing DCC method with (17) by iteratively learning $(b_i)_{i=1}^K$ bit-by-bit.

7:   $Z \rightarrow$ step: Optimize $Z$ according to (21).

8:   $(\Delta, \gamma) \rightarrow$ step: Update $\Delta, \gamma$ according to (22).

9: **until** convergences

10: **until** convergences

11: **Return**: $R_1$, $\delta_1$, $R_2$ and $\delta_2$.

On the basis of the Theorem 3 in [38] and [39], the optimal value of $Z$ can be obtained if and only if $V^T Z^T U = \text{diag} (\sqrt{N})$. The solution of $Z$ can be written as

$$
Z = \sqrt{N} U V^T
$$

(20)

In addition, in order to meet the balanced constraint $Z1 = 0$, the Gram-Schmidt process is used to construct the matrices $U \in \mathbb{R}^{K \times (K-r)}$ and $V \in \mathbb{R}^{N \times (K-r)}$, which satisfy the following four conditions: $U^T U = I_{K-r}$, $[U, 1]^T U = 0$, $V^T V = I_{K-r}$, $VV^T = 0$. So the ultimate optimal solution for $Z$ is

$$
Z = \sqrt{N} [U, \bar{U}] [V, \bar{V}]^T
$$

(21)

5) FIX $R_1$, $R_2$, $\delta_1$, $\delta_2$, $B$ AND $Z$, OPTIMIZE $\Delta, \gamma$

When $B$ and $Z$ are fixed, $\Delta, \gamma$ and $\gamma$ are updated according to the following rules

$$
\Delta, \gamma = \Delta, \gamma + \gamma (B - Z), \quad \gamma = \eta \gamma
$$

(22)

The learning rate $\eta (\eta > 0)$ controls the convergence of the objective function.

We repeat the above steps until the objective function converges. The detailed procedure of our proposed method is summarized in **Algorithm 1**. After obtaining $(R_1, \delta_1)$, the hash function can be denoted as $H(X) = \text{sgn}(R_1 X + \delta_1 1^T)$.

**D. FACE REPRESENTATION BASED ON LFH-BAE**

Having obtained the hashing function equipped with the encoding matrix $R_1$ and the encoding bias $\delta_1$, each PDV is first projected into a low-dimensional hashing vector. Since the traditional K-means is an effective and simple
FIGURE 3. The process of face representation based on the LFH-BAE. Firstly, each training face image is divided into several non-overlapping regions, which are used to learn the encoding matrix $R_1$, the encoding bias $\delta_1$ and the codebook $D$. Then, they are applied on corresponding regions to extract histogram features, which are cascaded into a longer feature vector for face representation. Finally, the classifier with cosine similarity is used for face matching.

FIGURE 4. The aligned and cropped face samples with $128 \times 128$ pixels from the FERET.

unsupervised clustering method, we apply it to the training set to construct the codebook $D$. Then, we pool each hashing code as a bin with the codebook, and use histogram feature to represent the hashing codes of the same face region. At last, the histogram features of all the regions are cascaded into a high-dimensional feature, which is considered as the final representation for the whole face image. Fig. 3 illustrates the approach of face representation based on LFH-BAE.

IV. EXPERIMENTS

We conduct extensive experiments on four public face datasets to evaluate the performance of our LFH-BAE model. To be more specific, we first use two constrained datasets (FERET and CAS-PEAL-R1) to show the effectiveness of our LFH-BAE model. Then, we employ two other unconstrained datasets (LFW and PaSC) to demonstrate the robustness and discriminative power of the LFH-BAE model. At last, we perform cross-dataset evaluation to estimate the generalization ability of our proposed model.

A. PERFORMANCE ON FERET

The FERET is a widely used large-scale public database, which contains 13539 human faces of 1565 subjects, varying in age, gender and race. Following the standard FERET evolution protocol [40], we conduct experiments on six disjoint sets: one training set, one gallery set ($fa$), and four probe sets ($fb$, $fc$, $dup1$ and $dup2$). All images are aligned according to the provided eye coordinates and cropped into $128 \times 128$ pixels. Some cropped images from the FERET are shown in Fig. 4.

In our experiments, we divide each face image into $8 \times 8$ non-overlapping regions, and evaluate our model with two different neighborhood radius sizes ($R = 3$ and $R = 5$), yielding 48- and 120-dimensional PDV for each pixel, respectively. The training set is utilized for feature learning, and the learned hashing function and codebook are performed on the other five sets for feature extraction. Whitened PCA (WPCA) is applied on the high-dimensional histogram representation to generate a compressed 1195-dimensional feature vector to reduce redundancy. The compressed feature vector is fed to the nearest neighbor classifier for face recognition.

1) PARAMETER ANALYSIS

In this section, we test the impact of different parameters in our LFH-BAE model on the FERET. We first study the effects of one parameter while the others are fixed. Then, we apply the determined parameters to the subsequent experiments.

We fix $R = 5$ to explore the influence of the coefficients $\alpha$, $\beta$, $\gamma$ on recognition rates. The learning rate $\eta$, code length $K$ and codebook size are set to 1.5, 25 and 600, respectively, and the impact of them will be studied in the following experiments. Table 2 shows the recognitions rates on the FERET for different empirical values. It can be observed that the best performance is obtained when $\alpha$, $\beta$, $\gamma$ are chosen to be 0.01, 0.1 and 100, respectively.

| Parameters | fb | fc | dup1 | dup2 | Ave. |
|------------|----|----|------|------|------|
| $0.1$      | $0.1$ | $0.1$ | $99.8$ | $100.0$ | $94.5$ | $93.6$ | $97.0$ |
| $0.01$     | $0.1$ | $0.1$ | $99.5$ | $100.0$ | $95.3$ | $94.0$ | $97.2$ |
| $0.01$     | $0.01$ | $0.1$ | $99.5$ | $100.0$ | $94.7$ | $93.2$ | $96.9$ |
| $0.001$    | $0.01$ | $0.1$ | $99.6$ | $100.0$ | $94.9$ | $93.6$ | $97.0$ |
| $0.001$    | $0.01$ | $0.1$ | $99.6$ | $100.0$ | $94.5$ | $92.3$ | $96.6$ |
| $0.01$     | $0.1$ | $1.0$ | $99.5$ | $100.0$ | $95.0$ | $94.9$ | $97.3$ |
| $0.01$     | $0.1$ | $1.0$ | $99.6$ | $100.0$ | $94.3$ | $92.7$ | $96.7$ |
| $0.01$     | $0.1$ | $10.0$ | $99.8$ | $100.0$ | $95.8$ | $96.2$ | $97.9$ |
| $0.01$     | $0.1$ | $10.0$ | $99.7$ | $100.0$ | $95.4$ | $94.4$ | $97.4$ |
| $0.001$    | $0.01$ | $10.0$ | $99.5$ | $100.0$ | $94.7$ | $93.6$ | $97.0$ |

In our experiments, we divide each face image into $8 \times 8$ non-overlapping regions, and evaluate our model with two dictionary sizes and the codebook size is fixed at 600. The code length should be set at $25$ for the highest recognition rate, as depicted in Fig. 5(a). With the fixed parameters in the above experiments, varying dictionary sizes are also studied and Fig. 5(b) shows that the best results are obtained when the codebook size is 600.

Next, we study the effects of the learning rate $\eta$ in our LFH-BAE model. The other parameters are the same as those determined in the above experiments. The values of learning rate are empirically varied from 1 to 9. Fig. 6 shows the encoding-decoding time and the average recognition rates of our LFH-BAE versus different values of $\eta$. We can observe that the encoding-decoding time decreases non-linearly as the learning rate increases, and the average recognition rate reaches a maximum at $\eta = 1.5$. This demonstrates that a small learning rate may result in a poor convergence of the multiplier iteration, while a large learning rate may force...
much ill-conditioning upon the objective function too early. The key is to find a right balance point where the LFH-BAE not only ensures fast encoding and decoding but also achieves high recognition rate. Thus, $\eta$ is set to 1.5 as a moderate rate in the following experiments.

Lastly, we investigate the impact of iterations $T$ on LFH-BAE. The property of the proposed alternating optimization process and ALM optimization theory make Algorithm 1 converge, and enable that the objective function value non-incremental and bounded. Fig. 7 shows the convergence of the objective function of our LFH-BAE. We observe that the objective function converges in 3 iterations.

2) COMPARISON WITH EXISTING HASHING ALGORITHMS

Although most existing hashing algorithms are presented for visual retrieval [25], [26], [41]–[44], they can still be implemented and remain effective in face recognition tasks. In this section, we compare our LFH-BAE with the following seven representative hashing methods: One Layer Anchor Graphs Hashing (AGH1) [41], Two Layer Anchor Graphs Hashing (AGH2) [41], Locality-Sensitive Hashing (LSH) [25], Spherical Hashing (SPH) [42], PCA-iterative Quantization (PCA-ITQ) [43], Density Sensitive Hashing (DSH) [26], and Hashing with Angular Reconstructive Embeddings (ARE) [44]. The first six algorithms are all conducted using the source codes and determined parameters of the original authors, except that ARE is implemented by ourselves. To ensure a fair comparison, we only replace the objective function of LFH-BAE (i.e., problem (1)) with those of other hashing methods, while the other steps remain the same. In this experiment, the neighborhood radius size is 5 and other parameters of those hashing algorithms are consistent with LFH-BAE. WPCA is employed to project the high-dimensional feature into a 1195-dimensional representation vector. Table 3 shows the rank-one recognition rates of different algorithms on the FERET.

Graphs Hashing (AGH2) [41], Locality-Sensitive Hashing (LSH) [25], Spherical Hashing (SPH) [42], PCA-iterative Quantization (PCA-ITQ) [43], Density Sensitive Hashing (DSH) [26], and Hashing with Angular Reconstructive Embeddings (ARE) [44]. The first six algorithms are all conducted using the source codes and determined parameters of the original authors, except that ARE is implemented by ourselves. To ensure a fair comparison, we only replace the objective function of LFH-BAE (i.e., problem (1)) with those of other hashing methods, while the other steps remain the same. In this experiment, the neighborhood radius size is 5 and other parameters of those hashing algorithms are consistent with LFH-BAE. WPCA is employed to project the high-dimensional feature into a 1195-dimensional representation vector. Table 3 shows the rank-one recognition rates of different algorithms on the FERET.

It can be obviously seen that our LFH-BAE model outperforms those existing hashing algorithms. On one hand, the above first six hashing methods ignore the discrete
TABLE 3. The rank-one and average recognition rates (%) of our LFH-BAE and other existing binary hashing methods on the FERET.

| Algorithm    | fb  | fc  | dup1 | dup2 | Ave  |
|--------------|-----|-----|------|------|------|
| AGH1 [41]   | 98.7| 99.0| 84.2 | 83.3 | 91.3 |
| AGH2 [41]   | 99.1| 98.5| 84.2 | 83.8 | 91.4 |
| LSH [25]    | 99.5| 100.0| 93.6 | 91.0 | 96.0 |
| SPH [42]    | 99.7| 100.0| 95.2 | 93.6 | 97.1 |
| PCA-ITQ [43]| 99.3| 100.0| 94.5 | 94.0 | 97.0 |
| DSH [26]    | 99.4| 100.0| 92.7 | 92.9 | 96.3 |
| ARE [45]    | 99.7| 100.0| 95.6 | 94.9 | 97.6 |
| LFH-BAE (R=5) | 99.8| 100.0| 95.8 | 96.2 | 97.9 |

Table 3 shows the rank-one and average recognition rates (%) of our LFH-BAE and other existing binary hashing methods on the FERET. The reconstruction term in LFH-BAE helps to exploit the inter-class structure factors that can approximate the entire image data space, and the direct discrete optimization can reduce the loss of useful information. Therefore, our proposed hashing model achieves the best performance on the face recognition task.

3) COMPARISON WITH STATE-OF-THE-ART FACE ALGORITHMS

In this section, we evaluate the performance of our LFH-BAE model on the FERET with the standard evaluation protocol. We compare our proposed LFH-BAE model with the hand-crafted local descriptors (such as LGBP, DT-LBP, LGFV/LN/SNP, FCPRF, LDENP) and learning-based descriptors (such as shallow descriptors: DFD, CBFD, SLBFLE, SPMBD, and deep descriptors: 2-FFC\textsubscript{Gabor−PCA}, CA-LBFL, and PCANet\textsubscript{S+}). Table 4 lists the rank-one recognition rates of our LFH-BAE and other approaches on the FERET.

We can observe that our LFH-BAE model obtains much competitive performance on the four probe sets of the FERET. As a tangible description, our LFH-BAE model obtains much higher accuracies on all probe sets than the hand-crafted descriptors, because it doesn’t require prior knowledge and can adaptively extract more discriminative information from the original data. Compared with the learning-based hashing descriptors, LFH-BAE achieves the highest average rate, which further proves the direct discrete optimization can facilitate binary features retaining more useful information. Moreover, the recognition performance of LFH-BAE is also better than the real-valued descriptors (such as shallow descriptors LGFV/LN/SNP, FCPRF and deep descriptors 2-FFC\textsubscript{Gabor−PCA}, PCANet\textsubscript{S+}). Table 4 indicates that our LFH-BAE model obtains much higher accuracies on all probe sets than the hand-crafted descriptors, because it doesn’t require prior knowledge and can adaptively extract more discriminative information from the original data. Compared with the learning-based hashing descriptors, LFH-BAE achieves the highest average rate, which further proves the direct discrete optimization can facilitate binary features retaining more useful information.

4) RECONSTRUCTION ERROR

In this section, we compare the reconstruction ability of the learning-based hashing methods, including PCA-ITQ, CBFD, CA-LBFL and our LFH-BAE. Each face image of the FERET is divided into $8 \times 8 = 64$ non-overlapping regions, and the neighborhood radius is set to 5. The parameters of the other three hashing methods are consistent with those of our LFH-BAE, so that all methods can be compared fairly. We compute the mean reconstruction errors on the FERET. For PCA-ITQ, CBFD and CA-LBFL, the decoder is unavailable in their implementation, but it is taken into account in the design of LFH-BAE and can be obtained in the learning process. Therefore, following [35], we compute the optimal linear decoders for the other three methods. Specifically, we use the learned binary codes of the training data to compute the optimal linear decoder ($R_2, \delta_2$). Let $Y$ be the binary codes of the testing data, the reconstructed testing data can be calculated as $\hat{X} = R_2^T Y + \delta_2^T$.

Table 5 tabulates the mean reconstruction errors and average recognition rates of our LFH-BAE and other learning algorithms on four probe sets of FERET.

| Algorithm        | Reconstruction Error | Ave. |
|------------------|----------------------|------|
| CBFD [5]         | 1.58 x 10^{-2}       | 96.7 |
| PCA-ITQ [43]     | 1.44 x 10^{-2}       | 97.1 |
| CA-LBFL [7]      | 1.43 x 10^{-2}       | 97.3 |
| LFH-BAE (R=5)    | 1.15 x 10^{-2}       | 97.9 |

Table 5 indicates that the reconstruction abilities of PCA-ITQ and CA-LBFL are comparable, and our LFH-BAE is optimal in terms of reconstruction ability and recognition performance.

This experimental configuration confirms that our LFH-BAE can extract the structure information inherent in the input face data, which can improve the discriminative power of the feature representations.
5) VARIOUS LEARNING STRATEGIES

In order to explore the contributions of discrete optimization and binary auto-encoder of the proposed LFH-BAE model, we develop three learning strategies to study the importance of these components:

1) TLFH-BAE: Traditional local feature hashing with binary auto-encoder.
2) LFH-BE: Local feature hashing with only binary encoder.
3) LFL-RAE: Local feature learning with real-valued auto-encoder.

The parameter settings in this part are consistent with those in Part 4). TLFH-BAE uses the traditional two-step “relaxing+thresholding” procedure to learn binary codes. LFH-BE conduct the iterative optimization without considering the reconstruction term in problem (2) (i.e., disregarding the first term). LFL-RAE learns real-valued features by discarding the discrete constraint. The remaining stages of these three learning strategies are the same as those of LFH-BAE, and each face sample is projected into a 1195-dimensional representation vector with WPCA. The rank-one recognition rates of the three strategies and our LFH-BAE on the FERET are shown in Table 6. We can summarize the following four conclusions:

1) Discrete optimization can eliminate the accumulated quantization errors, thereby reducing the loss of useful information.
2) Binary auto-encoder can exploit structure factors from the face image and extract excellent discriminative features.
3) Compared with the real-valued codes, binary codes show stronger robustness to intra-class changes of the face image.
4) When these three components are combined together, significantly high recognition performance can be obtained.

6) COMPUTATIONAL TIME

At last, we conduct experiment on the FERET to estimate the computational cost of the real-valued descriptors and LBP-like features. The parameter settings in this experiment are also the same as those in above Part 4), and they are applied to other methods to ensure a fair comparison. For the CBFD, CA-LBFL and our LFH-BAE, a 600-dimensional feature vector is extracted from each region, so the dimension of the cascaded feature vector for each image is 38400 (600 × 64 = 38400). Note that all methods are implemented with the matlab software and carried out on a PC with a 2.70 GHz and a 24G RAM configurations. Table 7 shows the feature dimensions and computational time of different methods.

We can observe that feature descriptors with high dimensions can improve the recognition performance to a certain extent, but the computational cost increases accordingly. Compared with the real-valued 2-FFC_{Gabor–PCA}, our LFH-BAE is slightly inferior in the computational cost, but it is excellent in terms of storage efficiency and recognition performance. Moreover, although there are encoding biases in our LFH-BAE, its computational cost is almost the same as CBFD and CA-LBFL, but lower than that of DFD. This is because only one scale PDV for each pixel is extracted in LFH-BAE, while multiple scale PDVs for each pixel are extracted in DFD. Therefore, the computational cost of our LFH-BAE is less than that of DFD.

B. PERFORMANCE ON CAS-PEAL-R1

The CAS-PEAL-R1 dataset contains more than 9000 face images from 1040 individuals with various variabilities, such as accessory, pose, lighting and expression. Following the standard evaluation protocol [57], we conduct the experiment on five subsets for face recognition, i.e., training, gallery, accessory, lighting and expression. The training set contains 1200 face images of 300 individuals (4 images per subject). The gallery set consists of 1040 subjects with 1040 face images, which are captured under normal conditions. The probe sets are collections of accessory, expression and lighting, consisting of 2285, 2243, 1570 images, respectively. All face images of the above five sets are aligned and cropped into 150 × 130 pixels according to the provided eye coordinates. Fig. 8 shows the aligned and cropped examples of the CAS-PEAL-R1.
Firstly, we learn the LFH-BAE on the training set and then use the learned projections to extract features from the gallery and the other three probe sets. Parameters of the LFH-BAE model are kept the same as those used on the FERET dataset. Finally, WPCA is used to reduce the high dimension to 1039 and the cosine metric is applied for face matching. Table 8 tabulates the rank-one recognition rates of our LFH-BAE and other different face descriptors on the CAS-PEAL-R1. Compared with state-of-the-art methods, our proposed LFH-BAE model obtains the best recognition rates on all probe sets. In particular, the proposed LFH-BAE obtains higher accuracy than the previous best SPMBD with the gain of 5.3% on the lighting set. It is demonstrated that our LFH-BAE shows strong robustness to expression, occlusion, especially in the face of lighting.

### C. PERFORMANCE ON LFW

The LFW dataset [60] contains more than 13,000 face images of 5,749 subjects and it is designed to study face recognition of unconstrained scenarios. As all face images are collected in the wild conditions, they suffer from large intra-class variations, such as varying poses, expressions, illuminations and backgrounds. In this experiment, we use the unsupervised setting [61] to evaluate the verification performance of LFH-BAE on LFW. According to the standard evolution protocol [61], there are 3000 matched pairs and 3000 mismatched pairs in the “View 2” dataset. It is divided into 10 folds, and each fold consists of 300 matched image pairs and 300 mismatched pairs, which are randomly selected from the original dataset. We use a conventional 2D affine transformation to align each face image and crop it into a region with the size of $128 \times 128$ pixels. The aligned and cropped face samples are shown in Fig. 9.

In this experiment, parameters of the proposed LFH-BAE are consistent with those used on the above FERET dataset. We perform feature learning on the training set, and apply WPCA to the high-dimensional feature to obtain a 700-dimensional representation vector. The nearest neighbor classifier with cosine similarity is used for face verification. Table 9 and Fig. 10 show the excellent average AUC and ROC curves of the proposed LFH-BAE and state-of-the-art strategies for the unsupervised setting, respectively. Note that we only plot the ROC curves for the algorithms that are released on the LFW website.

It can be observed that our LFH-BAE model achieves competitive performance with the existing learning-based hashing methods such as CA-LBFL, SLBFLE and SPMBD, and outperforms hand-crafted feature descriptors such as LHS, LARK and MRF-MLB. This again demonstrated that LFH-BAE can not only exploit structure factors from face images data-adaptively, but also eliminate the accumulated quantization errors, therefore more discriminative features are extracted for face verification.

Although the deep LBPNet [52] show better performance than our LFH-BAE, it requires prior knowledge to design a deep funneled network containing multiple types LBP filters and PCA filters. The deep network PCANet+[SF] [56] utilizes various filters to extract various PCA-based features, increasing the computational cost. The methods in [63], [66] and the deep real-values descriptor 2-FFC−PCA achieve excellent results on the LFW dataset with the unsupervised setting, they all use the high-fidelity pose and expression.

1 As described in section III D, the statistical histogram feature is used to represent the learned hashing codes, the cosine similarity of two faces can be denoted as $\text{sim}(i,j) = \frac{y_i^T \cdot y_j}{\|y_i\|_2 \cdot \|y_j\|_2}$, where $y_i$ and $y_j$ are the feature representations of the $i-\text{th}$ and $j-\text{th}$ face images, respectively.

2 The results of the other algorithms are available at http://vis-www.cs.umass.edu/lfw/results.html#Unsupervised
normalization (HPEN) [68] to process the face images and extract features at multiple scales, which is time or storage consuming in the recognition stage. On the contrary, we only use a simple 2D affine transformation to process the face images, and use a simple learning-based hashing strategy to extract only two-scale features to achieve encouraging performance.

D. PERFORMANCE ON PASC

The combination of point-and-shoot camera technology and social network technology increases the difficulty of face recognition tasks in real scenarios. In this section, we employ a recently released challenging face dataset, namely PaSC, to estimate the robustness of our LFH-BAE model. The still image portion of the PaSC includes 9376 images from 293 subjects. The balance of alternative sensors, distance to cameras, varying views and different positions are taken into account in image collection. This results in rare complications in controlled and less controlled scenarios, including poor focusing, over and under exposure, blur, and poor lighting. As the constraints on imaging conditions are relaxed, the challenges of face recognition increase dramatically. The standard evaluation protocol [69] for the still portion of PaSC is to compare all images of the query set to those of target set. We align each image with the provided eye coordinates and crop it into the size of 128×128 pixels. Fig. 11 shows some aligned and cropped sample images of the PaSC.

We utilize the target set to train the proposed LFH-BAE model, and extract feature representations from the target set and query set. The parameters are kept as the same as those used on the FERET dataset and each face image sample is projected into a 500-dimensional representation space with WPCA. By matching images in the target set to those in the query set, we compute the cosine distance for all pairs and obtain a 4688 × 4688 similarity matrix. The resulting similarity matrix is the basis for plotting the ROC curves for the frontal and all (frontal and non-frontal) images. In addition to comparing with the algorithms published on the PaSC website (one commercial PittPatt algorithm and two baseline real-valued descriptors: LRPCA, CohortLDA), we also compare the LFH-BAE model with other existing popular methods, such as LBP, LPQ, BSIF, CBFD and CA-LBFL.

Table 10 and Fig. 12 show the verification rates at 1.0% FAR and ROC curves for the frontal images and all images, respectively. In order to provide a concise figure, we only plot the ROC curves of some representative algorithms.

We can see that the proposed LFH-BAE model is significantly superior to the existing popular methods and baseline algorithms, except for the commercial PittPatt. The minimal gains of verification rates for all images and frontal images are 2.1% and 3.2%, respectively. Moreover, feature representations that learned from two-scale cascaded PDVs can further improve the verification performance of LFH-BAE.

The results demonstrate that, even for the point-and-shoot data, our LFH-BAE model is capable of extracting robust and discriminative feature representations. Binary auto-encoder not only promotes the learned binary features to inherit salient factors inherent in the raw data, but also make them show strong robustness to intra-class variations. Moreover, the ALM-based optimization strategy avoids the accumulated quantization errors and reduces the loss of discriminative information. Therefore, our LFH-BAE model can be employed in the real-world scenarios to handle the challenging face recognition tasks.

E. PERFORMANCE ON CROSS-DATASET

In practical applications, the appearances of the training set and testing set are apparently different due to the varying scenarios. In this section, we conduct a cross-dataset experiments to further investigate the generalization capability of our proposed strategy. Firstly, we utilize the constraint
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**FIGURE 11.** The aligned and cropped face samples with 128 × 128 pixels of the (a) frontal and (b) non-frontal settings from the PaSC.

**FIGURE 12.** The ROC curves of different algorithms on the (a) all setting and (b) frontal setting of the PaSC.

**TABLE 11.** Cross-dataset evaluation of our proposed LFE-SBAE on different training sets.

| Training Set | LFW AUC | PaSC | All AUC | Frontal AUC |
|--------------|---------|------|---------|-------------|
| FERET        | 89.72   | 62.2 | 46.3    |             |
| LFW          | 91.95   | 27.8 | 49.3    |             |
| PaSC         | 90.13   | 29.0 | 50.7    |             |

FERET dataset, the unconstraint LFW⁴ and PaSC datasets to train our LFH-BAE model to obtain the encoding matrix $R_1$, the encoding bias $\delta_1$ and the codebook $D$. Then, we evaluate the performance of the learned LFH-BAE models on LFW⁵ and PaSC. In these experiments, we only use the two-scale PDVs and the other parameters are consistent with the above sections.

Table 11 shows the AUC of LFW and verification rates (All and Frontal) at 1.0% FAR of PaSC for the cross- and same-dataset evaluations. We can observe that our LFH-BAE achieves excellent performance on the same-dataset evaluation, but in the case of cross-dataset evaluation, its performance decreases slightly. This is because the images of the training set and testing set are captured under different environments. Nevertheless, the performance of the cross-dataset evaluation is still comparable with that of state-of-the-art strategies based on the same-dataset evaluation (see the above sections C and D), which demonstrates the effectiveness of the LFH-BAE under different conditions. Moreover, the performance of the unconstrained cross-dataset (unconstrained training set and unconstrained testing set) evaluation is slightly better than that of the semi-unconstrained cross-dataset (constrained training set and unconstrained testing set) evaluation, which can be attributed to more diverse intra-class variations of the unconstrained training dataset. In a word, the LFH-BAE has a good generalization ability and can be competent for face recognition tasks under different conditions.

**V. CONCLUSION**

In this work, we propose a simple and effective unsupervised learning-based hashing model for face recognition.
Unlike previous hashing methods, we respect the binary nature of the problem and enforce the binary constraint in the discrete optimization to learn high-quality binary codes. To exploit the salient semantics inherent in the raw data, we utilize the binary auto-encoder that seeks to well reconstruct a face image from the learned robust binary codes. When optimizing the awkward original objective function, we simplify it into separate manageable sub-problems by introducing an auxiliary variable, and then solve them via the ALM-based alternating optimization. Such an alternating optimization not only respects the discrete constraint, but also takes the bit-independent and bit-balanced constraints into consideration. When solving the critical sub-problem, i.e., discrete optimization, we adopt the DCC method to learn binary codes in a closed form in the Hamming space. Experiments are conducted on four public face datasets and the results demonstrate that our proposed method achieves superior or very competitive performance compared with state-of-the-art algorithms. Our LFH-BAE concentrates on modeling the entire data space to extract the salient inter-class factors. However, the local geometric structure of the face image is still important and should be taken into consideration in the future to improve the performance our model. Moreover, we also intend to apply our model to other computer vision tasks such as video surveillance and multi-media search.

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