A reusable iterative optimization software library to solve combinatorial problems with approximate reasoning

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Abstract

Real world combinatorial optimization problems such as scheduling are typically
too complex to solve with exact methods. Additionally, the problems often have to
observe vaguely specified constraints of different importance, the available data may
be uncertain, and compromises between antagonistic criteria may be necessary. We
present a combination of approximate reasoning based constraints and iterative opti-
mization based heuristics that help to model and solve such problems in a framework
of C++ software libraries called StarFLIP++. While initially developed to schedule
continuous caster units in steel plants, we present in this paper results from reusing
the library components in a shift scheduling system for the workforce of an industrial
production plant.

Keywords: combinatorial optimization, iterative improvement, multiple criteria
decision making, scheduling under uncertainty, knowledge acquisition, knowl-
edge base consistency, shift scheduling, steel making
1 Introduction

Government as well as industry require practical approaches to a diverse set of complex combinatorial optimization problems. In industry, the distinction between commercial viability and failure often lies in the ability to control the production process through efficient optimization. Scheduling is one example of such combinatorial optimization problems. Like most combinatorial optimization problems of practical relevance, it is usually very hard to solve, both in practice as well as for theoretical reasons. Results from complexity theory [12] indicate that in the worst case, the fastest algorithm that is able to find the optimal solution of a typical problem can only be as fast as an algorithm that compares all possible schedules. Since the search space is by far too big, systematic search must be ruled out, and it therefore seems clear that some random sampling technique has no worse chance to hit relatively ‘good’ solutions than any other algorithm. While scheduling has been studied in isolation for many years, recent advances in artificial intelligence and operations research indicate a renewed interest in the area [20]. In addition, the scheduling problem is being defined more generally, and work is beginning to consider the closed loop use of scheduling systems in operational contexts. However, a primary source of difficulty in constructing good schedules stems from the conflicting nature of the objectives.

As with many real life decision making situations, it is usually not possible to fulfill perfectly all objectives when building new schedules. This applies to

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classroom schedules, staff rosters, as well as production schedules in manufacturing. Existing approaches to scheduling have tended to reduce the complexity of the problem by considering only a small subset of objectives. In real world situations, it would often be more realistic to find viable compromises between the objectives. For many problems, it makes sense to partially satisfy objectives. The satisfaction degree can then be used to evaluate the achieved compromise.

In addition, real objectives are often prioritized, therefore it is necessary to weight their satisfaction with importance factors. One especially straightforward way to achieve these two aspects of scheduling problems — to satisfy constraints to a certain degree, and to take into account relative importances — is the modeling of these constraints through fuzzy constraints. Fuzzy constraints are particularly well suited for modeling, since constraints can be written in a format easily understood by human experts, and because they feature a robust behavior which needs almost no tuning to yield reasonable control. In addition, the evaluation of their gradual satisfaction can be very efficiently used to guide repair based heuristic search methods as described for instance by Slany in [17], in order to find approximate ‘good’ solutions while at the same time greatly reducing the time needed to find them.

Repair based heuristic search methods are local methods that collect information on the problem by more or less random sampling it at various points, and mainly differ in the way the next random sample is chosen. A step from one sample to the next is defined by a neighborhood concept. Functionally, this neighborhood concept is implicitly defined through so-called repair operators that represent a transition from one variable instantiation to another one, both corresponding to more or less possible schedules. Repairing a random initial and typically bad schedule therefore corresponds to applying a series of repair operators until one reaches a neighborhood in which the included schedules violate few constraints, and thus get better evaluation scores than the random initial one.

These repair based heuristic search methods stand in contrast to the more systematic, traditional constructive methods. There, a feasible schedule is built from scratch, i.e., the variables initially are all uninitialized and step by step are assigned values by the algorithm. If a deadlock is reached, some variables that had already a value assigned must be reinitialized and a new search path has to be chosen. In practice, there is a plethora of different methods that basically follow this line of thought: Common to them all is that they in principle do not work on complete instances that still violate some constraints, but instead build-up the schedule constructively.

Additionally, since fuzzy constraints allow a wide range of values for variables, the constructive approaches are faced with an even huger search space compared to the usual constraint problems. By intuition, this huge search space lends itself in a much more natural way to random sampling techniques such as repair based methods. On the other hand, mathematical analysis is made much more difficult in the random sampling case combined with multi-criteria
non-linear fuzzy constraints. However, empirical benchmark results indicate that the aforementioned intuition is right, in that the performance of repair based heuristic search methods on real world problems is much better than the performance of constructive methods, see \cite{17, 5}.

Real world descriptions naturally contain vaguely formulated relations, because further details are simply not known or would anyway not lead to better results as they would be canceled out through noise in the data. The down-to-earth reason behind our choice of fuzzy logic as a basis for knowledge representation is that it allows straightforward modeling of typical combinatorial optimization problems and is perfectly combinable with heuristics that find ‘good’ solutions in acceptable time.

Repair based heuristics have a much better efficiency to solve typical large optimization problems compared to constructive or enumerative algorithms. In particular, they need no explicit constraint relaxation to still be able to implicitly assess trade-offs between conflicting constraints when the latter are modeled using the mentioned fuzzy constraints. Further, these repair based heuristics do not need to prune search space to still yield very good results for well-known benchmark problems. Indeed, almost all other fuzzy constraint satisfaction algorithms found in the literature (see \cite{17} for a survey) rely on search space pruning to achieve better performance, but often explicitly do not look at possibly better compromise solutions (in particular methods that prune all paths where $\alpha$-cuts fall below a certain level), implying that a solution featuring a relatively unimportant sub-constraint with very low satisfaction but constituting nevertheless the real optimum because of the other, more important constraints being satisfied to a higher degree than in all other instantiations, could be neglected forever. In this sense, the method proposed in the StarFLIP++ project could be seen as an — albeit not 100% perfect — solution to the question whether fuzzy set theory can solve large and complex problems computationally efficiently.

Additionally, in industrial applications, reacting to a changing situation, i.e., rescheduling has to be done quite frequently when some production parameters change due to machine breakdowns. Usually, most human errors are made in these rescheduling situations since time to think is scarce and the situation often worsens rapidly (e.g., forgetting for some time a waiting machine, resulting in longer waiting times or worse qualities for certain jobs) if no action is taken. Iterative optimization based methods are inherently well suited to deal with such situations.

The paper is organized as follows. The next section introduces the shift scheduling application. Section 3 then goes on to present the major components of the StarFLIP++ project. Section 4 presents the constraints and repair steps of the shift scheduling application that we chose to model with StarFLIP++. Section 5 presents specific details of the challenges encountered in integrating the concepts to the shift scheduling problem in the StarFLIP++ framework and presents benchmark results indicating the effectiveness of StarFLIP++ for this kind of combinatorial optimization problem. Finally, we conclude and take a
look at possible future steps that will make StarFLIP++ even more useful in a distributed context on the Internet.

2 The Shift Scheduling Application

Right from its beginning the StarFLIP++ project has always been strongly coupled with problems encountered in the process of steel production. This was partly due to the fact that the entire project has been initiated by a research cooperation with the Austrian steel production industry. A wide range of publications have been published on the steel production domain over the last couple of years out of this fruitful research cooperation. Slany gives in a more in-depth discussion of this domain in connection with fuzzy scheduling. Dorn and Shams discuss an expert system approach designed initially for a similar domain.

With versatility and reuse being key objectives of the StarFLIP++ project, we chose to move on from the original steel production domain. We expected to gain further experience about the process of knowledge acquisition and transformation into a StarFLIP++ compatible format, which led us eventually to a system that is more or less a generic tool as far as the representation of domain knowledge is concerned. Secondly, another problem domain also gave us numerous hints on weaknesses of the system. These weaknesses were located in the optimization methods, in the performance of the system, and in the representational power provided by the fuzzy tools of the FLIP++ library.

The shift scheduling domain is a promising field of application for several reasons. To begin with, scheduling research in this area is almost nonexistent despite the fact that it is an important but difficult application area. One major conclusion drawn out of the existing research efforts is the fact that one soon runs into major difficulties in this area when conventional optimization methods are applied, e.g. with simplex, enumeration or backtracking methods. According to Gärtner and Wahl a high degree of fuzziness can be attributed to many requirements encountered with shift scheduling problems. They also argue that due to the complexity of the problem and the lack of powerful optimization methods it is more important to move the focus from automation of design towards aiding design. We also believe that any system used to solve such shift scheduling problems must be a cooperative tool that allows to find an optimal schedule via the interaction with the knowledge engineer. Nevertheless, StarFLIP++ contains elements that allow to use it eventually as a closed loop system. Moreover, the flexibility offered by StarFLIP++ when it comes to the definition of fuzzy variables, fuzzy constraints and aggregation operators should make it superior compared to classical optimization methods which often show a lack of representational power. Moreover, the repair based optimization process that tries to tackle constraint violations with specifically defined repair steps shows very good results as discussed in Section.
Furthermore, the problem of developing ‘good’ shift schedules is a highly practical application. It has many consequences on people that are working in shifts. The industrial optimization potential and social implications of shift schedules (e.g. consequences on family life) are considerable.

In the present paper, we describe a subset of the actual constraints in order to focus on the major aspects of StarFLIP++, the shift scheduling application serving only as an illustration to the program description. In particular, the number of represented constraints was reduced by focusing on a problem instance with simple shift types. For example, the concept of night shifts has been completely left out. Consequently, all constraints referring to night shifts could be left out. However, the example was chosen with sufficient complexity to illustrate the main points of StarFLIP++. Once a proper representation of a problem is found, enhancing the constraints of the problem does not cause much difficulty.

The objective of our problem is to find a shift schedule for twelve employees. These employees are aggregated in three groups with an even distribution, i.e., each group consists of four employees. The groups are further divided into subgroups of two employees each. Each of the subgroups is fully covering the requirements of operation, hence no interdependencies between the various subgroups have to be taken into consideration. Ruling out interdependencies is a further simplification that is rare in real world problems but makes it easier to follow the problem description. Again, as mentioned above, such a simplification does not impede the judgment of the basic functionality of StarFLIP++ in connection with a shift scheduling problem, as there will be enough constraints to allow a rich and highly nonlinear interaction. The groups are named A, B, and C with subgroups A1, A2, B1, B2, C1, and C2, respectively. The working hours are 38.5 hours per week. Weekly working hours can vary over the length of the shift schedule, but the average per week must be 38.5 hours. There exist several shift types that can be allocated only at specific times (see Figure 1).

| name                                | length (in hours) | shortcut |
|-------------------------------------|-------------------|----------|
| day shift:                          | 8–9               | (TD)     |
| day shift at weekends:              | 4                 | (TDWE)   |
| shift substitution at weekends:     | 12                | (SWWE)   |

Figure 1: Shift type definitions.

The roster is defined in Figure 2 and displays the requirements of the shift plan. It can be easily seen that the shifts required for operation remain the same week by week, with one notable exception: On every third Saturday of the shift schedule, a different setting is required due to maintenance work. Because of this, the cycle of the operation plan is set to three weeks.
|       | Mon       | Tue       | Wed       | Thu       | Fri       | Sat       | Sun       |
|-------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Week 1| 5 SG TD   | 5 SG TD   | 5 SG TD   | 2 G TD    | 2 G TD    | 1 SG TDWE + 1 G SWWE | 1 SG TDWE |
| Week 2| 5 SG TD   | 5 SG TD   | 5 SG TD   | 2 G TD    | 2 G TD    | 1 SG TDWE + 1 G SWWE | 1 SG TDWE |
| Week 3| 5 SG TD   | 5 SG TD   | 5 SG TD   | 2 G TD    | 2 G TD    | 2 G SWWE   | 1 SG TDWE |

SG...Subgroup, G...Group
TD...day shift, TDWE...day shift weekend, SWWE...shift substitution weekend

Figure 2: Operation plan.

The optimization methods applied in the StarFLIP++ environment are all dependent on an initial solution. It does not really matter whether the quality of the solution is good or bad, as several studies have already shown (e.g., in [3]), and our experiments empirically confirmed these results. An initial suboptimal template problem instantiation (= initial solution) is given. The initial solution has to satisfy the ‘hard’ requirements of operating hours and average working hours per week. The repair steps that will be explained in Section 4 change the solutions only in such a way as not to violate these hard constraints. The generation of an initial problem instantiation is actually a nice example of a combinatorial problem in itself. The problem is to find an initial solution that satisfies the hard constraints of operating hours and average working hours per week. This problem however is not considered in the present paper. We now turn to the major parts of the StarFLIP++ project used to model and solve the presented shift scheduling problem.

3 Solving combinatorial optimization problems with StarFLIP++

The following section gives an overview of the StarFLIP++ project. It puts the system and application presented in this paper into a wider context. After shortly touching upon the entire StarFLIP++ project, we concentrate on the part most relevant for the shift scheduling application.

StarFLIP++ is a library [15, 16] for real world decision making. It is a tool for optimization under vague constraints of different importance using uncertain data. Through the use of fuzzy computations, compromises between antagonistic criteria can be modeled. Typical application areas include scheduling, design, configuration, planning, and classification.

A production scheduling problem in a steel production plant has been the key application area for the major part of the development time of StarFLIP++. Nevertheless, the design of the library has never been explicitly biased towards a certain application problem. Due to this fact, an open system evolved that can treat a large variety of problems with shift scheduling being just one of them.
StarFLIP++ (pronounce: StarFlipPlusPlus; this refers to the fact that StarFLIP++ stands as a regular expression for all names of the individual sub-libraries, and all of the latter are based on FLIP++) was created to investigate real world combinatorial optimization problems such as the shift scheduling problem described in the previous section. It was designed and implemented as a family of C++ libraries. StarFLIP++ is composed of the following layered sub-libraries:

- FLIP++: the basic fuzzy logic inference processor library.
- ConFLIP++: the static fuzzy constraint library which recently has been merged with DynaFLIP++.
- DynaFLIP++: the dynamic fuzzy constraint generation and interpreter library for the constraint script interpretation (CSI) language.
- DomFLIP++: the domain knowledge representation library.
- OptiFLIP++: the heuristic optimizing library; several repair based heuristics have so far been implemented and tested.
- CheckFLIP++: the knowledge-change consistency checker library that also allows fine-tuning of the configuration parameters of a problem.
- InterFLIP++: the graphical user interface for all other libraries, with platform support for X-Windows (XView/OpenLook, Motif) and MS Windows 3.1/95/NT.
- ControlFLIP++: the control center where the interplay between the other parts is coordinated (mainly data I/O and calling functionality).
- DocuFLIP++: the online documentation available separately for end-users, knowledge engineers, and programmers, and accessible via the World-Wide-Web\textsuperscript{1} as HTML documents.

Furthermore, the following parts are under development:

- ReaFLIP++: the reactive optimizer as an extension of DomFLIP++.
- NeuroFLIP++: the neural network extension that allows automatic tuning of fuzzy membership functions.
- TestFLIP++: the version control and test environment for the complete library set.
- SimFLIP++: the simulation toolkit library.
- JavaFLIP++: a major reuse/redesign of the existing StarFLIP++ libraries currently under way in the JAVA programming language.

Figure\textsuperscript{2} shows a view of the layered structure of StarFLIP++.

These libraries come without domain knowledge base. Therefore, during a first knowledge acquisition phase, the knowledge engineer describes the items

\textsuperscript{1}http://www.dbai.tuwien.ac.at/proj/StarFLIP/

\textsuperscript{2}
(e.g., products, workforce groups, . . .) and the logical objects (e.g., machinery, shift plan tasks, . . .) with their respective attributes for the environment. This information is stored using DomFLIP++. In a second step, the functional relations among process variables have to be defined. A variety of mathematical description methods have been implemented for this goal. In a further step, constraints for these process variables can be entered to define restrictions in the value domains of these variables. This is done in two stages: First, static template constraints are defined using the ConFLIP++ part of DynaFLIP++, for instance to specify a due date constraint, i.e., the constraint that a generic job will have to be finished by some time yet to be specified, with a certain gradual satisfaction defined through fuzzy variables, terms and associated membership functions. Second, rules governing the application and specialization of such template constraints to particular instances of the combinatorial optimization problem at hand are defined by the knowledge engineer in DynaFLIP++. This specialization occurs normally during optimization time as constraints need to be interpreted to allow their flexible adaptation to, for instance, a particular
number of jobs that cannot be foreseen at specification time. This is similar to the use of aggregation functions in spreadsheets or databases.

When this knowledge modeling step is finished, a given instantiation of a schedule can be constructed from actual process data and, after a schedule has been proposed, evaluated. After the evaluation of all constraints, changes on the schedule are usually done in order to find a more satisfying instantiation. What these changes are and how they look like is specified by the knowledge engineer in relation to the optimization methods supported by the OptiFLIP++ library. For instance, the genetic optimization algorithm uses special genetic operators such as the crossover operator to perform changes on the schedule, which are useless in the tabu search type optimization. So for each optimization algorithm the knowledge engineer wants to apply to the problem at hand, it is possible to specify a range of corresponding repair operators that change some parts of the schedule.

Several repair based algorithms were integrated in OptiFLIP++, namely

- a tabu list min-conflicts repair based hill climbing heuristic,
- a min-conflicts repair based iterative deepening heuristic,
- a min-conflicts repair based random search hill climbing heuristic, and
- a min-conflicts repair based genetic algorithm heuristic.

All repair based algorithms have several variants and many parameters. A conflict identification function is used together with a domain dependent repair operator library to quickly choose the repair operator that will most probably minimize conflicts for a given situation. However, the algorithms are independent of this library since the guidance provided through the conflict identification function is in all cases combined with a fall-back random strategy if nothing else helps to find better instantiations.

The following sections illustrate the main modules necessary to define a new problem instance such as the shift scheduling application.

### 3.1 Modeling fuzzy constraints with ConFLIP++

The reusable C++ object library ConFLIP++ is a constraint handling extension to FLIP++, which itself is a general purpose fuzzy logic inference library. ConFLIP++ was merged into DynaFLIP++ for efficiency reasons but provides an independent interface with its own functionality. Because it constitutes the basis of the rest of the project, we will explain it in this section. First, however, let us describe it in the context of FLIP++ which handles everything concerning fuzzification, membership functions, and linguistic variables. The user can choose between several different fuzzy inference methods, various priority schemes, different aggregation operators, and several defuzzification methods. FLIP++ also permits the graphical editing of membership functions and the easy manipulation of rule sets. Bonner et al. describe for instance how to solve a fuzzy
control problem using FLIP++ alone. The InterFLIP++ userinterface tool supports all functionality provided by ConFLIP++ and FLIP++. This includes creating, interactively editing, saving and reloading named sets of constraints including all parameters, and evaluating constraints. Figure 4 shows a typical screen-shot during an XView interaction with InterFLIP++.

Figure 4: Typical screen-shot during an XView interaction with InterFLIP++.

In ConFLIP++, the first step is creating simple constraints such as the following taken from the steel making application:

\[ \text{alu-cntnt} \leq 0.08 \]

and naming them in the case of the example for instance ‘alu-cons’ using the objects and methods defined in ConFLIP++. The aim is to catch vagueness in constraint-equations where the \( \leq \) sign is not meant to be interpreted in its strict
mathematical sense, but such that ‘smaller’ violations are acceptable. What these ‘smaller’ violations could be has to be defined explicitly (and precisely) through the membership functions associated to the ‘terms’ of the variable as defined below. Additionally, ConFLIP++ is able to handle uncertainty about the exact value of ‘alu-cntnt’, which is possible by propagating possibility distributions instead of defuzzified values. The operators to infer values and to aggregate several constraints are then applied to fuzzy values, which can always be represented as membership functions. This capability to model with accuracy vague relations and uncertain data is the major contribution of fuzzy and possibilistic logics.

In our example of a simple constraint, the aluminum content ‘alu-cntnt’ is a so called linguistic variable, a generalization of the conventional concept of a variable. A linguistic variable has a finite set of terms, which are mapped to an interval of real numbers by a membership function. By a linguistic variable we mean a variable whose values are words or sentences in a natural or artificial language rather than numbers. In ConFLIP++ fuzzy sets like linguistic terms are represented by the ParameterSet-object. For example the fuzzy set temperature has the linguistic terms cold, medium, warm, which are mapped to intervals of real temperature values by the appropriate membership function. The object to model a simple constraint has the following structure:

\[
\text{ConstraintCompare(name, importance, dilatation, comment, variable, compare\_operator, compare\_value)}
\]

In the next step, several such constraints are logically combined, i.e., they are aggregated by one of the aggregation operators, such as AND and OR, which for example could be implemented as minimum and maximum operators, to build more and more complex constraints with a hierarchical structure. The object to model such complex constraints has the following structure:

\[
\text{ConstraintConcat(name, importance, dilatation, comment, constraint, constraint, concat\_operator)}
\]

where dilatation is the type of the constraint (either crisp, fuzzy, or mixed), and constraint is either a ConstraintCompare or a ConstraintConcat. ConFLIP++ then automatically creates a rule-set out of default or user-defined terms of sets for standard linguistic variables, standard rule set tables, standard membership functions for the term sets, default priority values, and various default operators using FLIP++. FLIP++ is repeatedly called later to evaluate the constraints for some instantiations of the free linguistic variables appearing in the constraint. Additionally, the system checks the scores of all constraints having a priority different from zero as well as of their constituent sub-constraints before these constraints are aggregated to find out whether a hard constraint violation occurred (evaluation score equals zero) in order to invalidate instantiations that crossed the hard barrier of the corresponding constraint, which is not allowed.

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The rule-set is built for instance such that, if the first linguistic variable is compared to its term ‘positive big’, and the involved inequality is ‘variable ≥ constant’, and another linguistic variable is compared to ‘zero’, and the constraints corresponding to the two linguistic variables are concatenated by ‘or’, then the resulting term for the aggregated rule is ‘very good’. The latter term comes from the predefined template term set {‘very good’, ‘good’, ‘zero’, ‘bad’, ‘very bad’}.

The human expert will usually have to fine-tune the automatically created rule-set and the membership functions associated to the terms. However, it is possible to store user defined standard sets of term sets and the associated set of semantic rules. Additionally, fuzzy methods are quite robust, such that the exact determination of the membership functions is not essential. The predefined triangular membership functions often perform well in a first approximation. Nevertheless, one reason that makes fine-tuning necessary is that ConFLIP++ has no a priori domain knowledge. If the constraint is ‘alu-cntnt ≤ 0.08’, some generated default rules are for instance:

IF alu-cntnt is positive_small THEN alu-cons is zero
IF alu-cntnt is positive_medium THEN alu-cons is bad
IF alu-cntnt is positive_big THEN alu-cons is very_bad

The really important object of ConFLIP++ is SetOfConstraints. Each SetOfConstraints has a name and a list of constraints. Furthermore, it needs a rule-set-object, tables for concatenating and comparing constraints with the appropriate operators defined in the OperatorSet, and a parameter set describing fuzzy linguistic variables.

The next step is the evaluation of a constraint. The evaluation happens according to the rule-set of the constraint. First, the free linguistic variables have to be given values, the latter being either defuzzified real numbers or possibility distributions. The evaluation function returns by default a defuzzified value that describes the degree of satisfaction of the constraint with the given values. The ConFLIP++ object that holds evaluated constraints for further operations is the SetOfEvalConstraints.

The human expert can influence the decision making behavior of ConFLIP++ in various ways. After a constraint knowledge base has been compiled, it can be copied and the copy can be edited. First, the human expert can select one of several aggregation, implication, and defuzzification operators. The weighing scheme can be chosen as well. Of course, the individual membership functions and priorities of the constraints can be graphically edited. For instance, it is easy to selectively edit the constraint responsible for the observation of due dates. These changes will immediately take effect on the decision function. To ease configuration of a complete constraint knowledge base built up from scratch, the default values for all these parameters are pre-specified in a way that seems to apply reasonably well to most cases. However, the human
expert can later soften or harden all those constraints that have not yet been fine-tuned on an individual base. In such a case, ConFLIP++ searches the complete knowledge base for membership functions that make the decision making behavior of the constraint knowledge base fuzzier or crisper.

3.2 Evaluating dynamic constraints with DynaFLIP++

Dechter and Dechter [4] introduced the term dynamic constraint network to deal with changes from one constraint network to another one, such that new facts about the environment can be modeled. While this issue is taken care of in the CheckFLIP++ part of StarFLIP++ (see Section 3.3), in DynaFLIP++ we want to focus on a different problem, namely on the dynamic generation of constraints at runtime, based on environment data and so called template or static constraints. Thus, our use of the term dynamic constraint is unrelated to the dynamic constraint networks defined in [4].

The DynaFLIP++ library subsumes ConFLIP++, the latter being needed to formulate static fuzzy constraints and then operate on them. DynaFLIP++ wraps additional functionality around these fuzzy constraints and reaches this functionality up to DomFLIP++ where the actual domain knowledge is processed and optimization is performed. This additional functionality has become necessary because of factors encountered in many real world combinatorial optimization problems, of which we only became aware of after trying to handle several different problems. Since special consideration is given to the reusability aspect of all libraries, we found that static fuzzy constraints are good to model the aspects associated with partial satisfaction, compromising, and relative importance of constraints. However, other aspects require dynamic generation of constraints from template constraints. For instance, the actual number and kind of constraints often depend upon the current instantiation of the problem that is to be optimized. With each repair step in the optimization process, the structure of this instantiation may change. Therefore, the structure of the constraint evaluation tree has also to change. For example, it is possible that a job with an associated delivery date is exchanged with another job that has no delivery date, therefore this constraint must not be evaluated for the second schedule.

Another aspect is that it is normally not useful to tune each constraint separately. Instead, a static constraint is tuned for a selected reference value, and DynaFLIP++ then uses this static constraint to generate a dynamic constraint adapted to the actual situation. Again, looking at the delivery date example, this implies that the template is a static constraint that is tuned around the value zero, with an appropriate fuzzy distribution around it. DynaFLIP++ then specializes this to an actual time in the scheduling horizon. This dynamic adaptation is mostly harmless for simple constraints such as delivery dates, but becomes more tricky when complex constraints are involved. A more complex example, also taken from the steel making domain, would be the duration of
tundish life expectancy. The tundish, a part of the caster, has to be maintained after approximately 240 minutes, but this length can vary between 100 and 300 minutes. The problem is that the attributes of a finite number of jobs must be aggregated, in this case by adding their durations, without knowing at the time when the static constraint is defined how many jobs will have to be eventually aggregated. Their number can only be determined dynamically at optimization time by looking up compound data values in the actual schedule instantiation. These aggregation operators are similar to those found in spreadsheet software that process a range of values. At this point we would like to clarify the meaning of the term *aggregate* that in the context of steel making it is a synonym for large metallurgical equipment such as continuous casters or blast furnaces. On the other hand, *aggregation* stands for the conjunction of constraints by soft AND and OR operators as we have seen before. Additionally, *aggregation* as in *aggregation operators* in the context of this section can also be found in the field of constraint databases as described by Kuper [11]. This is because the number of arguments in constraints evaluated by DynaFLIP++ depends on conditions that can be checked only at execution time.

A difficulty arises because DynaFLIP++ contains absolutely no knowledge about the domain. Using DomFLIP++, optimization structures are defined together with their associated constraints, using the knowledge engineering features of DynaFLIP++. Additionally, relations between attributes of items in these optimization structures and the static constraints must be defined using a special rule based language that is interpreted at evaluation time by DynaFLIP++. A rule, slightly simplified but taken from the actual steel making domain, illustrates this mechanism as given in Figure 5.

![Figure 5](image_url)

**CONDITION:**
\[
\langle \text{Job}_i, \text{Job}_{i+1} \rangle \in \text{CC}_3 \land \\
\text{quality separation} \notin \langle \text{Job}_i, \text{Job}_{i+1} \rangle \land \\
\text{tundish change} \notin \langle \text{Job}_i, \text{Job}_{i+1} \rangle \land \\
\text{CC setup} \notin \langle \text{Job}_i, \text{Job}_{i+1} \rangle
\]

**CONSTRAINT:**
\[
\text{Chemical Compatibility}_{\text{CC}_3}(\text{Job}_i, \text{Job}_{i+1})
\]

Figure 5: A rule specifying when and how a template constraint is used.

The actual compatibility encompasses 12 more chemical alloying elements, the
Job$^i$.C.high \text{soft} < \text{alloy\_limit}.C \text{soft} \wedge \text{Job}^i+1.C.high \text{soft} < \text{alloy\_limit}.C \text{soft} \vee \\
\text{Job}^i+1.C.high \text{soft} \leq \text{Job}^i.C.high \text{soft} \wedge \text{Job}^i.C.low \text{soft} \leq \text{Job}^i+1.C.low \text{soft} \vee \\
\text{Job}^i.C.high \text{soft} \leq \text{Job}^i+1.C.high \text{soft} \wedge \text{Job}^i+1.C.low \text{soft} \leq \text{Job}^i.C.low \text{soft} \vee \\
\text{overlapping}.C(\text{Job}^i,\text{Job}^i+1) \geq \text{pair\_limit}.C \\
\text{(where } \text{overlapping}.C(\text{Job}^i,\text{Job}^i+1) := \max(0, \min(\text{Job}^i.C.high,\text{Job}^i+1.C.high) - \max(\text{Job}^i.C.low,\text{Job}^i+1.C.low))) \text{)} \\
\vdots \text{ similar for other chemical elements.}

Figure 6: Sketch of macro definition for a restriction to carbon of Chemical Compatibility CC$_3$($\text{Job}^i,\text{Job}^i+1$).

degasging procedure in the secondary metallurgy aggregates, as well as the casting format between the jobs.

To evaluate a given instantiation of a partial constraint satisfaction problem, a decision function aggregating all the constraints with their respective priorities, using an appropriate aggregation operator and a corresponding weighing scheme, must be established. Whereas the representation of template constraints is handled with the ConFLIP++ library, we present in this section the DynaFLIP++ library responsible for efficiently establishing a new global constraint representation for a specific instantiation of the problem. This global constraint will result in a highly structured constraint tree for the whole schedule. The constraint evaluation function will return the weighted global satisfaction score based on the current schedule and the constraint evaluation tree. The nodes of this dynamically constructed tree nodes are weighted aggregation operators (in the simplest case conjunctions) and the leafs are ConFLIP++ objects representing individually fine-tuned static constraints, again taken from the steel making domain. DynaFLIP++ is able to use most of the framework provided by ConFLIP++ to efficiently compute the evaluation scores for a new schedule.

When optimizing, it is often advisable to introduce an additional measure into the decision function dependent upon whether the current instance of the combinatorial optimization problem contains certain difficult items. In the scheduling context, this would mean that if the scheduling of these jobs is not introduced as a bonus into the decision function, these jobs might never be considered for actual scheduling. There usually exists a non empty pool of waiting jobs, and only a subset of jobs from the pool can be scheduled immediately. Therefore, the danger is that some difficult jobs will remain in the pool forever.
unless additional measures are taken. It is clear that this ‘difficulty’ or ‘importance’ of a job must increase over the time for which it is still reasonable to ‘produce’ it, to allow its eventual scheduling. The easiest way to introduce this ‘difficulty’ is to formulate a corresponding constraint with an associated priority that will represent these difficult jobs and which will therefore be represented by another branch of a certain constraint type. Thus, the ‘difficulty’ of jobs will be one criteria considered when the partial constraint satisfaction problem is optimized. The same applies equally to other partial constraint satisfaction problems such as those encountered in design or planning.

To build up the evaluation tree, DynaFLIP++ has to consider the domain structure with its aggregates and scheduling objects, so that the evaluating tree is built up analogous to the hierarchical structure of the modeled application. The structure of the scheduling objects depends on the application they are designed for. Considering production scheduling in industrial environments as a special combinatorial optimization problem, we encounter different types of imprecision, stemming from constraints that are blurred in definition and include vagueness and uncertainty. We can imagine that an operation on the schedule may start a ‘little’ earlier and that ‘small’ deviations of optimal values may be acceptable. The scheduling object ‘Order’ then has attributes such as plant, plant-mark, throughput, weight, format, thickness, speed, slab-group, chemical_elements, delivery_date, ... and associated constraints like

\[
\text{domain constraint: } \text{out\_date} \leq \text{delivery\_date}
\]

In this case, an aggregate could be the continuous caster CC-4, with constraints concerning tundish durations, average throughput, or setup-restrictions. Of course there would exist a variety of other constraints, such as compatibility constraints, capacity constraints, or temporal constraints. To evaluate a schedule for one aggregate, DynaFLIP++ has to first create and instantiate all SetOfConstraints for the domain objects which were specified by the knowledge engineer. In a second step, all the variables that have restrictions in form of constraints have to be computed. This is done by evaluating the computation clauses designed parallel to the related constraints. Of course all variables have to be computed before they are compared to constraints. The next step is the adaptation of template constraints to the actual situation on the schedule. We can imagine that a template compare value has a fuzzy distribution around zero, but the real compare value may be an aggregation of other processes variables and would have another value.

\[
\text{template constraint: fuzzy\_var\_foo1} \leq 0
\]

\[
\text{specialized constraint: } \text{out\_date} - \text{delivery\_date} \leq 0
\]

On the evaluation of each constraint, DynaFLIP++ invokes the evaluation mechanisms of ConFLIP++. The evaluated constraints are put into the SetOfEvalConstraints, where they can be aggregated as described in Figure 3.
all relevant constraints determined by the rule based language are evaluated, the overall evaluation score is returned to DomFLIP++. Further, we are interested in the biggest violations on the schedule, so we select bad evaluations at runtime and put them into an appropriate data structure, which is later used by DomFLIP++ to make changes on the schedule in order to avoid these violations. The repair steps depend on the optimization algorithm used by DomFLIP++. If a local change on the schedule has occurred, DynaFLIP++ has to check where the changes took place, in order not to build up a complete new evaluation tree, but only to recompose those parts of the schedule that have been changed. This reuse of already computed data structures will, similar to a caching mechanism, influence the runtime behavior of the evaluation process.

The most important object of DynaFLIP++ is the evaluation tree which contains the specialized constraints, the evaluated constraints, and the aggregation of the latter. The variables with their actual values and the violations are stored in a separate structure.

3.3 OptiFLIP++ and ControlFLIP++

To guide the search of the OptiFLIP++ algorithms as discussed in [17], it is necessary to identify the constraint with the worst weighted evaluation, i.e., the severest conflict which can be attacked to minimize conflicts. This can be considered as a side product of evaluating the current instantiation. It corresponds to computing the evaluation using the minimum operator, and more importantly, to remember the constraint involved in the minimal weighted evaluation. This constraint represents the largest conflict for the current instantiation. Often the constraint corresponds to a general feature of the instantiation and cannot be attributed to a specific part of the instantiation. Depending on the repair operators available to the repair based constraint satisfaction algorithms, it can be helpful to find additionally the second largest and third largest conflict. Generally, the search should return the largest conflict being of a type that can be handled by an available repair operator. When DynaFLIP++ has to generate a new dynamic constraint representation for a given instantiation, it computes the individual ‘leaf’ constraints by calling ConFLIP++ repeatedly with new variable instantiations on one of the stored reference constraints, and stores the results in an intermediate form that can be used by ConFLIP++ for further aggregation. This ensures a relatively efficient processing of the constraints since the sometimes very large data structure of a static constraint can be reused for all dynamic constraints of its type. At the same time, DynaFLIP++ sorts all the computed intermediate evaluation scores, together with type information, for later selection of ‘good’ repair operators.

We designed our constraint satisfaction engine StarFLIP++ with a real world problem in mind, namely the scheduling of fine grained production in a steel making plant. Typically, this involves more than a thousand binary soft and hard constraints and a matching number of variables with continuous do-
mains. The number of constraint checks until a satisfactory solution is found ranges in the several hundred thousands. In view of these numbers, it is clear that complexity issues play at least as important a role as the one played by good knowledge acquisition tools. As mentioned above, we therefore adopted repair based algorithms that have been shown to be very efficient strategies for large constraint satisfaction problems. Minton et al. [14] could find solutions in less than four minutes on a Sparc workstation 1 for the million queens problem, while the best general backtracking approach (found in an empirical study by Stone and Stone [19] to be a most-constrained backtracking algorithm) became intractable for $n > 1000$. Minton et al. [14] even found that their repair based method exhibits linear time and space complexity for large $n$. The min-conflicts heuristic combined with a repair based hill climbing heuristic specifies that, starting from an initial suboptimal solution, the system attempts to minimize the number of constraint violations after each repair step. Minton et al. [14] showed convincingly that for certain problems, the use of the additional knowledge gained from operating on complete but suboptimal solutions instead of building solutions from scratch as in constructive approaches pays off well. Such repair based heuristics perform orders of magnitude better than traditional backtracking techniques. Though repair based methods can be combined with many general search strategies, they found that hill climbing methods were especially well suited for the problems they investigated. While this result is very nice for a general constraint satisfaction technique, the apparently not well known fact that Abramson and Young [1] found a constructive method to solve the general $n$ queens problem with linear time complexity should not be left untold. Though this implies that $n$ queens is not an intractable problem, it shows that general repair based algorithms often attain almost the optimal theoretical complexity, which seems to be untrue for general constructive backtracking algorithms. Statistics and a detailed analysis of the different algorithms can be found in [17]. All repair based heuristics were much faster and yielded better results than the constructive approach that was evaluated using the same configuration parameters on real world instances of combinatorial optimization problems.

Another point speaking in favor of repair based approaches for combinatorial optimization problems is that these algorithms do not need to prune away search branches and can still be very efficient. While pruning as described in [7] is well suited to solve classic constraint satisfaction problems, its application to combinatorial optimization problems poses several problems. For one, compromises can only be evaluated by looking at all constraints. Additionally, real world problems actually often cannot be completely described by constraints, because for instance future events cannot be predicted in scheduling. Therefore, it is sometimes desirable to reject optimal solutions in favor of slightly worse but robust solutions, in the sense that small alterations in the actual execution of, e.g., a schedule, still belong to good instantiations, while the superficially best solution is surrounded by very bad ones. By early pruning, it is of course
impossible to investigate such a situation.

3.4 Defining an optimization problem with DomFLIP++

The DynaFLIP++ library was located between ConFLIP++ and the domain knowledge representation library DomFLIP++, which is a description tool for the environment that has to be optimized. The structure of a domain holds a list of aggregates, which themselves hold a schedule of objects with their respective attributes and variables. Additionally, on each level one or more SetOfConstraints can be specified in order to describe relations and restrictions on the process variables. DomFLIP++ is also responsible for repair steps on a badly evaluated schedule, using a list of violations and badly evaluated variables, which are computed at runtime by DynaFLIP++, and the optimization algorithms supported by OptiFLIP++.

DomFLIP++ is the knowledge representation module of the StarFLIP++ project. StarFLIP++ focuses on optimizing combinatorial problems that can be expressed as multiple criteria problems. It uses fuzzy constraints to model optimizing criteria and applies various iterative improvement techniques such as Tabu search, genetic algorithms, and iterative deepening to the problems. It allows the definition of new optimization problems by aiding the domain engineer in the design of the structure of a new problem at hand. Generally, a division between domain dependent and domain independent methods and data structures characterizes the structure of DomFLIP++. While the domain dependent data structures are specific to the problem, the domain independent part is provided as a framework by the library. Moreover, there is a domain independent interface to other StarFLIP++ modules such as OptiFLIP++, DynaFLIP++, and CheckFLIP++. After each iteration in the optimization process, the considered instantiations of the problem are evaluated. Each evaluation produces a list of evaluated constraints and hence provides hints on violations of requirements. For each constraint, modification operators, also called repair steps, are defined that can be used to increase the score of the constraint in further iterations of the optimization. A domain can be fine-tuned through modifying of constraints and their fuzzy representation, changing the choice of repair steps, and varying optimizing parameters. A well-tuned domain can then be successfully optimized.

The shift scheduling domain presented in this paper is a fruitful area of investigating the power of DomFLIP++. This is due to its variety of constraints, inherent fuzziness of requirements, and large search space that recommends the application of heuristics.

3.5 Changing domain descriptions using CheckFLIP++

Slany [17] has shown that the ordering behavior of the priority values can be chaotic, in the sense that small changes in the knowledge base can have large effects on the ranking of solutions. While this seems rather counterintuitive at
first, it makes sense after looking closer at the situation. One example in [17] has
the ranking of several partial solutions inverted because of unforeseeable inter-
actions between operator fix-points and weights of constraints, i.e., the rankings
of instantiations (large results) are sensitive to certain threshold values in the
knowledge base (small changes), so changes can produce unpredictable, chaotic
results. In light of the link between non-monotonic logics and combinatorial
optimization problems as developed by Brewka et al. [3], such non-monotonic
reactions to changes in knowledge bases seem to be an obvious result.

Since there is no unique way to compute weights of constraints for a given
problem, there is also no clear way to relate weights to the wishes of the field
expert regarding priorities, other than experimenting and fine-tuning by testing
different variants. It is possible to completely change the ranking behavior of
weights by switching to another aggregation operator or to a different weigh-
ing scheme. The examples given in [17] demonstrate that fine-tuning of the
parameters for a combinatorial optimization problem is absolutely necessary in
order to obtain meaningful results. Section 3.5 indicates how this tuning can be
done rationally while avoiding inconsistencies with former decisions. Since the
method is based on trial-and-error, and since test cases are used to implicitly
limit changes in a knowledge base, the method effectively helps to harness the
chaotic behavior described above.

A major concern in decision making problems is how to correctly elicit knowl-
edge from human experts. The project comprises a method of eliciting the crit-
eteria’s importances from human experts. Especially when many human experts
have to agree on a problem description such as the rules involved, the impor-
tances of certain criteria, etc., it is important to have a method that allows
make reasonable and consistent changes to the parameters of the problem
description. The test implemented in the CheckFLIP++ part of the project
highlights all inconsistencies in configuration changes. The test also helps to
evaluate the sensitivity to configuration changes and provides a possible way to
allow automatic learning of problem descriptions.

Freuder and Wallace [7] observe that weakening constraints in effect means
creating a different problem. In the present section, we have shown that it is
often unclear which problem we should solve, and that small changes in param-
eters describing a combinatorial optimization problem might cause large and
unforeseeable changes in the corresponding solutions. Therefore, it seems justi-
fied to ask what kind of changes should be allowed and what implications these
changes might entail.

An answer to the problem of making sure that fine-tuning is done consist-
tently with earlier decisions is to adopt a consistency test for configuration
changes. Such configuration changes could be changes in the priorities be-
tween constraints, adopting a new aggregation operator, changing hard barriers,
changing membership functions, or changing the logical structure of constraints.
Basically, this change together with the test produces a new ranking for a given
set of new instantiations, while observing predefined rankings for a set of old

21
reference ranking of pairs of instantiations. The mechanism works such that, if the human expert is dissatisfied with a ranking produced by the system, he or she can slightly change the weights of some constraints, or the exact form of some membership function (e.g., to specify that a hard barrier is actually located slightly higher), or any other parameter of the problem, such as the aggregation operator used. A consistency test will then check whether the new configuration is consistent with the rankings for a set of reference pairs of instantiations. This is done by applying the new configuration, e.g., the set of new weights, to all the old ordered pairs of instantiations, and by calculating their evaluation scores with this new configuration. If for each reference pair the order between the two reference instantiations remains unchanged, this indicates that the new configuration does not invalidate any previous reference ordering. It is compatible with all decisions made in the past that became reference ranking pairs.

If one reference ranking pair is ranked in the opposite order, this means that either the new configuration is wrong and has to be changed again, or that some reference ranking pairs are obsolete and should therefore be removed from the reference ranking pair database. In both cases, an inconsistency among the reference rankings and the new ranking is pointed out. This inconsistency has to be resolved such that the resulting system makes rational, predictable, understandable and self consistent decisions. The probability that the inconsistency is due to noise in the problem description and should therefore be neglected is zero, since all reference rankings have been generated with the explicit aim to change the configuration in order to give them a certain, new order. An inconsistency can point to earlier errors in configuration changes. Since each change is done under supervision, usually by a human expert, and changes are normally only adopted with the explicit goal to produce a different ordering, the inconsistency cannot be attributed to noise. Whether such a decision making behavior can be termed objective or subjective depends on other factors. However, it is usually possible to lead several human experts to agree on a common, undisputed subset of some reference ranking pairs of instantiations, or at least to establish several different sets that correspond to configurations which can be further characterized by and saved for later use under such names as, e.g., for scheduling combinatorial optimization problems, ‘risky/cost-cutting’, ‘highest-quality’, ‘observe-temporal-constraints’, ‘standard-mix’, etc., indicating their general tendency for decision making. This makes clear that there is no notion of a best combinatorial optimization problem in our approach, but that several combinatorial optimization problems optimizing a solution of a real world problem from slightly different points of view can coexist. The corresponding last configuration is saved together with these reference ranking pairs of instantiations as one knowledge base. Of course, not all intermediate stages have to be stored permanently. This permits modeling the intentions of the human expert with maximal flexibility while ensuring rational and predictable behavior after changes in the configuration.
If the new configuration is adopted, the best solution before making the configuration change and the best solution after making the configuration change become a new reference ranking pair added to the new database associated with the new configuration. In this pair, the best solution after making the configuration change is ranked first, and the best solution before making the configuration change is ranked second. All data influencing the overall decision function must be stored together with the pair to be able to apply the resulting new decision function in the old context, given the new configuration. \[17\] contains a listing of the consistency test in procedural form.

Human experts can specify implicitly the overall configuration of the constraints by asserting a set of ‘normal’ reference rankings. The easiest way to apply the heuristic that establishes consistent configuration parameters for the constraints is to let the human expert do parameter changes, and to later check them out with the introduced consistency test.

### 3.6 Automatic knowledge acquisition

Huard and Freuder \[10\] view constraint knowledge base debugging as a partial constraint satisfaction problem in itself. If the constraint knowledge base is erroneously over-constrained, a change that entails a small number of new solutions is more in keeping with Occam’s Razor than one that entails many. However, Huard and Freuder \[10\] consider only over-constrained networks, while we are interested in finding a combinatorial optimization problem model that approximates as closely as possible the implicit problem at hand, thus leading us to move from one combinatorial optimization problem to another instead of moving from an over-constrained constraint satisfaction problem to an approximating combinatorial optimization problem. Similar to our approach, Huard and Freuder \[10\] work in cooperation with a human expert. This permits the human user to interactively play what-if games, i.e., allowing the expert to see how decision making behavior evolves as changes are made to the combinatorial optimization problem model. On the one hand, Huard and Freuder \[10\] allow only one constraint to be weakened, while our approach is able to cope with any kind of change. On the other hand, our method so far does not make any suggestions for knowledge change, while the knowledge assistant proposed by Huard and Freuder \[10\] does. In general, the ‘inverse’ problem of finding an appropriate combinatorial optimization problem model given a certain a priori optimal solution, is extremely difficult because of the multitude of changes that could actually occur. Not without good reason do Huard and Freuder \[10\] limit changes to only one weakening of one constraint and apply it to rather small problems. The difficulty is that humans easily overlook some constraints, especially when the number of constraints is large and the constraints are only vaguely defined. Therefore, the subjective ‘better’ ranking obtained a priori from a human expert will often objectively not be better than the instantiation found by the system because the human expert forgot some constraints, thus
forcing the system to learn suboptimal decision making. Therefore, the fine-tuning scenario, where human experts repeatedly change constraint parameters such as weights by hand and then compare the respective best solutions, is much better suited to establishing the best configuration for the problem. This certainly comes from the fact that human experts do often have an intuitive notion of ‘good’ and ‘bad’ solutions of combinatorial optimization problems without being totally aware why they think so. However, it is an open research problem whether this fine-tuning can be fully automated when an objective, not prone to human error, a posteriori meta-evaluation is used, such as one guided by results of quality evaluations.

According to Freuder and Wallace [7], such meta constraints, as for instance induced by the consistency test proposed in Section 3.3, “are reminiscent of the concept hierarchies that provide initial bias in machine learning settings, and indeed it is intriguing to think of the constraint satisfaction process as a form of concept learning, synthesizing a relationship from positive and negative information.”

Future work lies in comparing our work to approaches from knowledge acquisition (e.g., human expert models, cooperative knowledge base tuning), machine learning (e.g., case base reasoning), as well as model based diagnosis (e.g., McIlraith and Reiter [13] study the design of tests whose outcomes confirm or refute a hypothesis).

Huard and Freuder [10] test their knowledge elicitation method on random problems. However, they start from an idealized constraint satisfaction problem \( P \) that must be approximated; our method is useful to find an unknown \( P \), therefore random combinatorial optimization problems do not help. We currently believe that our method can only be tested through satisfactory application to real world problems such as the steel making application or the shift scheduling problem presented in Section 2.

4 Shift planning constraints and repair steps

We now come back to the application of StarFLIP++ concepts as described in Section 3 to the shift scheduling problem we introduced in Section 2.

The constraints of the shift scheduling problem define certain requirements. Normally, constraints are of dynamic nature, i.e., their concrete instantiations depend on the instantiation of the problem. In our application this means that different shift schedules lead to different constraint instantiations of the same type of constraint. Hence it is necessary to define constraints in a language-like style that is based on the use of variables. Each evaluation run of DynaFLIP++ is based on variables whose values are fed by the problem instantiation of DomFLIP++.

In the following we will shortly explain typical constraints that have been implemented and that will serve to illustrate the introduced concepts.
• **Constraint of even distribution of working hours**
  This constraint tries to guide the evaluation towards smooth shift schedules, meaning that deviations between weekly working hours should be relatively small. It computes the difference in working hours between consecutive weeks and detects those pairs of weeks where the difference is comparatively high, so that they will be used as possible starts for a repair step. This should lead to a more evenly distributed sequence of shifts and hence working hours.

• **Constraint for weekends**
  Weekends are a crucial area with most shift scheduling problems. Often, a human expert has to pay especially attention to this area of the shift schedule. One constraint simply checks the number of free weekends for one subgroup and leads to better evaluations the more free weekends there are.

  Repair steps represent the modification operators of a problem. They allow to move from one valid instantiation of the problem to another one. Such modifications are the basis for every optimizing algorithm that uses iterative improvement techniques to arrive at — in terms of evaluation — better problem instantiations.

  Generally, it is easy to specify certain types of repair steps for a problem. In our example, the definition of repair steps is almost entirely dictated by the plan of operation, i.e., the roster. With the use of the roster as depicted in Figure 2, it is possible to define for each day what kinds of shift and how many of them must be allocated. Due to performance reasons, repair steps should be preferably kept simple since they are heavily used during the optimization process. Mostly, the modifications for a problem can be broken down to simple swap or move operations. This has also been shown for the application in the steel production domain in [9].

  Repair steps represent modifications of the shift schedule. Without any guidance these modifications would take place randomly. To avoid that, the positions where constraint violations are identified are used as input for repair steps. This can be any position in the shift schedule. As we will see in the next paragraph, in our problem the position in the shift schedule will also determine which repair step is applied. In our application, repair steps take the position as an input and then try to find a possible modification while iterating through the shift schedule beginning from a start position. The indication of a start position allows some leeway in the application of the repair step. One is not restricted concerning the start of the search for a successful modification. The start position could be a random one, or the same as the position of the violation, or whatever seems to be appropriate for the problem at hand.

  Taking a closer look at the roster of our shift scheduling problem shown in Figure 2, one can identify four main clusters where operations might be the same within that cluster. From Monday to Friday the operation is identical and
there is only one shift type involved. Since Thursday and Friday do have a more complex operation plan, as they use different operation units, namely groups, we have to split this cluster into two: One modification operator will be defined for modifications from Mondays to Wednesdays, another one will be defined for those from Thursdays to Fridays. The third modification operator is focused on changes that involve the day shift at weekends on Saturdays and Sundays. Finally, a repair step for the shift substitutions at weekends on Saturdays is defined. In the following one type of repair step will be explained.

Repair step ‘Monday–Wednesday’

The operation plan shows that on the days from Monday to Wednesday there is only one shift type required, the day shift. If a violation of a constraint and its derived repair start position is within this range, there are two ways of applying a modification operator.

First, the position of the violation, which is characterized by the day and the subgroup (= smallest unit of operation in our problem) affected, can be swapped with another position in the Monday to Wednesday range. Actually, two swaps have to be made in order to preserve the requirements of the operation plan. The reason is straightforward: From Monday to Wednesday, five subgroups are allocated with day shifts, resulting in one subgroup without a shift. If the violation is on a position where a day shift is allocated, a swap is sought with a position in the same subgroup where no shift is allocated. Because the number of shifts allocated to subgroup is not affected by such a swap this hard constraint is preserved. Furthermore, by making a second opposite swap the hard constraint for the required shifts at one day is preserved, too. Both swaps involve an exchange of a free subgroup, i.e., one that has no shift allocated, with a day shift subgroup. The operation is illustrated in Figure 7.

Second, since the day shift can also be found on Thursday and Friday, it is also possible to seek destinations for swaps within this range. There is only one thing that has to be considered in addition to the above swap operation: On Thursday and Friday, groups are required. Consequently, a swap operation must take care of this and preserve the group structure of the operation requirements on Thursday and Friday. This results in a more complex two-step modification described in Figure 8.

5 Results from the shift planning domain

The algorithm that has been chosen out of the OptiFLIP++ library for this problem is based on iterative improvement techniques. Such an algorithm tries to improve an initial preliminary schedule iteratively. The modifications, or repair steps, are the operations to move from one schedule to another. The problem of getting trapped in a local optimum can be overcome in several ways.
Violation at (Subgroup A2, Day 1)
Swap 1: (Subgroup A2, Day 1) - (Subgroup A2, Day 8)
Swap 2: (Subgroup B2, Day 1) - (Subgroup B2, Day 8)

Figure 7: Repair step 1 for Monday to Wednesday type of shifts.

Our approach, which is a variant of the iterative deepening heuristic described in Section 3, works as follows: In a first try, a search to depth 1 is made. This means that starting from the initial schedule one modification is made. The execution of one modification does imply that a certain number of possible modifications of that type are tried on a random position out of a set of the worst violated positions. After a number of such tries, the best schedule survives as the new problem instantiation for the next step and it is also remembered as the best overall schedule. Hence, it is possible that one step produces a worse intermediate schedule eliminating the possibility of getting trapped in a local optimum. We discarded an earlier approach of avoiding local optima traps that recursively increased the depth of a step if no improvement could be achieved with current depth level due to performance reasons.

Starting from the evaluated sets of constraints there are various degrees of randomization that guide the optimizing algorithm. First, the choice of which violated constraint to work on is randomized within the set of worst violated constraints. Second, each type of constraints has its own function of how to derive a position where the repair modification is applied. If this function delivers several such positions, one is randomly selected. Third, the set of possible modifications applied by the repair operators provides another pool for random choices.

In the following, we briefly summarize the results depicted in Figure 9 which empirically show the effectiveness of the StarFLIP++ libraries in solving the shift scheduling problem as defined in Section 3. As one sees, results steadily improve until further improvements can only be gained by unproportionally long search sequences. The four depicted batches correspond to four different iteration sequences starting with the same initial suboptimal solution. Since the optimal curves do not differ very much, we conclude that the presented
optimization method is quite robust and will usually be able to find adequate solutions. In terms of effective running time, ‘good’ solutions with an objective function above 7200 were found in the average after 1h44’ on a Sparc-station 5 (170 MHz Turbo-SPARC processor) with 64 MB memory running under Solaris 2.5.1. A run with 6500 complete shift schedule evaluations took 8h15’. While these timings may seem large, it is no problem in the shift scheduling context as there is more than enough time available to optimize a schedule which will then be used for an extended period of time. In reactive scheduling situations, simpler constraints and faster hardware should make it possible to optimize the problem efficiently.

6 Conclusions and outlook

In a first expert system approach, Stohl et al. [18] applied a constructive domain heuristic to a steel making scheduling problem. Although the system found good feasible solutions, Stohl et al. believed that their solutions could be further improved, especially since constraints could only be broken through explicit user intervention, and because the relaxing of constraints was not evaluated. The iterative optimization library StarFLIP++ allowed to handle these aspects and therefore proved to be more suitable for the steel making scheduling problem.

In this paper, we reused enhanced StarFLIP++ components to present a new shift scheduling problem as well as its solution.

This allows to highlight characteristics of major application areas for StarFLIP++: Whenever rules can be elicited from human domain experts, and
when these rules are not absolute in the sense that they can be more or less applicable for a certain data set, and additionally one wants to allow trade offs to be made in order to find adequate solutions, then this iterative optimization library to solve combinatorial problems with approximate reasoning methods is well suited for the problem at hand. It should be clear that these characteristics apply to many industrial combinatorial optimization problems, whereas artificially clean problems found in classical operations research often do not fall in this category. However, because of these characteristics, it is difficult to compare directly the different methods as they do not solve the same kind of problems.

In this paper, we presented problems as well as solutions associated with approximate reasoning methods in real world combinatorial optimization problems. We presented the knowledge engineering tools ConFLIP++ and DomFLIP++ for modeling fuzzy constraints that can be aggregated to complex, hierarchical constraint structures. We showed its practical application in a shift scheduling application using fine-tuning and specializing concepts. We presented the DynaFLIP++ library which, based on ConFLIP++, is responsible for the evaluation of an instantiated combinatorial optimization problem. We also gave an overview of the heuristics and repair based OptiFLIP++ algorithms. We developed a combination of repair based methods and fuzzy constraints for real
world multi criteria decision making, with a bias towards scheduling problems. We presented improved methods for compromising between antagonistic criteria, for assessing priorities among fuzzy constraints, as well as a new method for ensuring consistent and reasonable changes in configurations. We also introduced a method that allows interactive what-if games for arbitrary decision problems. The method is an argument based consistency test with a meta constraint knowledge base that allows several experts to agree on parameters of a knowledge base for real world decision making problems. Through the consistency tested by the method, non-monotonic changes in knowledge bases of combinatorial optimization problems can be made more predictable. Theoretical analysis and experiments indicate that our method makes real world problems from this area manageable.

The results obtained from a shift scheduling application indicate the suitability of our approach for similar combinatorial optimization problems in terms of modeling expressiveness and performance.

Up to now all libraries have been implemented in the object oriented language C++, which was the obvious choice at the start of the project. Today, with more appealing programming languages and object oriented concepts having reached a more mature and stable level, there are other options available as far as the implementation is concerned. In particular, the JAVA programming language with such convenient standard features like networking classes implying full Internet connectivity and a high degree of platform independence is the first choice for future StarFLIP++ implementations. Nevertheless, C++ is still a well justified environment especially with such powerful extensions as the Standard Template Library.

Current extensions aim at providing a distributed simulation package over the Internet including an environment to test reactive scheduling behavior. The programming of these extensions in Java instead of C++ should allow easier porting of the software to new computer architectures, as well as help avoiding pitfalls encountered when programming in C++.

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