Quantum Confinement Induced Molecular Mott Insulating State in La$_4$Ni$_3$O$_8$

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The recently synthesized layered nickelate La$_4$Ni$_3$O$_8$, with its cuprate-like NiO$_2$ layers, seemingly requires a Ni$^3+$ ($d^9$) +2Ni$^2+$ ($d^8$) charge order, together with strong correlation effects, to account for its insulating behavior. Using density functional methods including strong intra-atomic repulsion (Hubbard U), we obtain an insulating state via a new mechanism: without charge order. Mott insulating behavior arises based on quantum coupled, spin-aligned Ni2-Ni1-Ni2 $d_z$ states across the trilayer (rather than based on atomic states), with antiferromagnetic ordering within layers. The weak and frustrated magnetic coupling between cells may account for the small spin entropy that is removed at the Néel transition at 105 K and the lack of any diffraction peak at the Néel point.

Nearly 25 years since the discovery of high temperature superconductivity (HTS), the question persists: why does HTS occur only in copper oxides and not other layered oxides. Nickelates with cuprate-like structures$^1$ have seemed to be the most likely candidates: the Cu$^{2+}$ $d^9$ configuration with active $d_{x^2-y^2}$ orbital maps onto the Ni$^{3+}$ configuration, but this is known to be a problematic charge state. Nevertheless, difficult charge states may sometimes be stabilized, such as the nominal Ni$^{3+}$ ("infinite layer") compound LaNiO$_2$ prepared by topotactic exchange of oxygen$^2$. Cuprate-like electronic structures in other oxides have been pursued since soon after HTS were discovered. The charge conjugate analog Sr$_2$VO$_4$ ($d^1$ vs. $d^8$) presented hope$^3$ for and displays magnetic and orbital ordering$^4$, but has never shown superconductivity. Layered nickelates have been seen as the best mimic of HTS if the $d^9$ Ni$^{3+}$ charge state can be stabilized, and theoretical interpretation of the few known prospects has begun$^5$. The LaNiO$_3$/LaAlO$_3$ superlattice$^6$ is an example that has been suggested to produce an HTS-like Fermi surface, but is based on the more common Ni$^{3+}$ ion and has not yet produced superconductivity.

The discovery by Greenblatt’s group of a Ruddleston-Popper sequence$^7$ of phases La$_{n+1}$Ni$_n$O$_{2n+2}$ with $n$ cuprate-like NiO$_2$ layers has reinvigorated interest in nickelates, with a focus on La$_{1}$Ni$_{3}$O$_{8}$ ("La438") where stoichiometry is attained$^8$. In an ionic picture, the mean Ni valence in La$_{n+1}$Ni$_n$O$_{2n+2}$ is +($n+1$)/$n$, i.e. metallic. However, La438 is highly insulating$^9$, with a room temperature resistivity $\sim 10^3$ Ω-cm increasing by six orders of magnitude down to 25 K. Magnetic ordering is observed$^{10}$ at $T_N$=105 K, with NMR data indicating an antiferromagnetic (AFM) transition$^{11}$. The entropy loss at $T_N$ is only $\frac{3}{2}$Rln2 per Ni, suggesting unconventional magnetic behavior in this system.

La438 crystallizes in a tetragonal unit cell, with space group I4/mmm (#139) and lattice parameters $a$=3.9633 Å, $c$=26.0373 Å. The structure, pictured in Fig. 1, consists of three NiO$_2$ "infinite layer" planes separated by layers of La$^{3+}$ cations but no oxygen. On either side of this trilayer slab lies a fluoride La$_2$/O$_2$/La layer, with the same structure as the corresponding layer in LaFeAsO. While in a sense isoelectronic with doped cuprates as it seems to involve some mix of Ni$^{3+}$ and Ni$^{2+}$ cations, the electronic and magnetic structure of the Ni ions is still unclear. As mentioned, the low oxidation state Ni$^{3+}$ is enigmatic; to obtain such a configuration for Ni is not easy, and these Ruddleston-Popper phases are unstable at moderate (~375 °C) temperature$^{10}$ to decomposition into La$_2$O$_3$ and Ni metal. In the Ni$^{3+}$ "infinite-layer" compound LaNiO$_2$ it was found to be impossible$^2$ to produce a Mott insulating state as might be anticipated; in fact the compound is metallic at least roughly as calculated. La438 consists of three layers of LaNiO$_2$ subject to quantum confinement, as we demonstrate below.

In La438 a simple ionic picture will give Ni configurations $d^8 + 2d^9$, which would give the natural identification of the one ‘inner’ Ni$\equiv$ Ni$^{2+}$($d^9$) and two outer Ni$\equiv$ Ni$^{3+}$($d^8$) cations, as labeled in Fig. 1. Ni1-Ni2 layers are separated by only 3.25 Å, much less than the in-plane separation $a$=3.93 Å, a characteristic that will become important below. The Ni trilayers are separated by the La$_2$/O$_2$/La unit, and an ($a/2$, $a/2$,0) translation between successive NiO$_2$ trilayers reinforces very small interplanar coupling between cells, which will be shown to produce a natural quantum confinement within the trilayers.

Here we study the electronic structure of the compound by ab initio techniques to understand the electronic and magnetic structure of La438 and to identify the differences and similarities with respect to the cuprates. Our electronic structure calculations were performed within density functional the-
ory using the all-electron, full potential code Wien2k based on the augmented plane wave plus local orbital (APW+lo) basis set, and the experimental atomic positions. The generalized gradient approximation was used. To deal with strong correlation effects we apply the LDA+U scheme including an on-site repulsion U and Hund’s coupling J for the Ni 3d states. Results were not very dependent on the specific values of U and J in the reasonable range, and we report results with U = 4.75 eV, J = 0.68 eV, values very similar to those determined from constrained density functional calculations.

The bands within LDA (U=0) are metallic as expected, and in fact the bands crossing the Fermi energy $E_F$ are dispersive (bandwidth of $\sim$2-3 eV). These bands do not suggest substantial effects of strong correlation, and Pottavets et al. suggested Fermi surface driven spin density wave (SDW) order, which might destroy part of the Fermi surface and account for the magnetic transition. The earlier calculations, even those using LDA+U, produced only metallic states. The key to obtaining a lower energy, and insulating, state is to allow extra freedom by doubling the lateral cell of La438, and we found that in-plane AFM order is readily obtained. Various configurations and types of spin order were tried, but no inter-plane AFM order could be obtained; moments along the z axis always want to align within the trilayer.

We discuss only this most energetically stable state, comprised of AFM-ordered Ni layers with spins aligned along the z axis. The spin density, pictured in Fig. 1 makes evident both the type of spin ordering and the character (shape) of the spin density, which reveals both $d_{x^2-y^2}$ and $d_{z^2}$ contributions. There is indeed some charge difference with muffin-tin charges of 8.52 (Ni1) and 8.64 (Ni2), and different moments of 1.4 and 1.3 $\mu_B$ respectively. It is understood that different formal charge states may involve surprisingly reduced difference in actual charge; it is magnetic states that are more instructive. While the moments we calculate might be consistent with an S=1 configuration ($d^8$) reduced by hybridization, neither moment (1.3-1.4 $\mu_B$) can be ascribed to an S=1/2 $d^9$ ion (which would have a maximum moment of 1 $\mu_B$). Without $d^9$ ions, the ionic, charge-ordered picture becomes untenable, and a new mechanism for producing the gap must operate.

Our LDA+U band structure, shown in Fig. 2 produces a Mott insulating state, but of an unusual type that requires broadening one’s view of how these correlation effects operate. In the AFM state, the spin-up and -down band structures are of course identical. Since the valences of La$^{3+}$ and O$^{2-}$ are clear, the Ni ions are on average Ni$^{1.33+}$, with charge $d^{8.67}$ making the maximum moment around 1.33 $\mu_B$, which is in fact what they are in our ground state. The Ni ions are thus fully polarized, meaning the majority orbitals are completely occupied and removed from consideration. Also, the minority $d_{x^2-y^2}$ orbitals are empty, centered at +3.5-4 eV on the energy scale of Fig. 2 Thus the $d_{x^2-y^2}$ orbital contributes one unit to the hole count, 1 $\mu_B$ to each Ni moment, and the in-plane superexchange coupling, but otherwise is of no interest. The relevant orbitals are solely the partially occupied minority $d_{z^2}$ orbitals on the six Ni ions in the AFM cell, which must accommodate one hole per triple (two in the AFM cell). The central question then is: how can a Mott insulating state, as we obtain, arise at “2/3 filling” if charge disproportionation into 2 Ni$^{1+}$ + Ni$^{2+}$ does not occur?

The in-plane AFM order, as is common, drastically reduces bandwidths (spin-conserving hopping takes place only between second Ni neighbors in the plane), so taking account of Ni $d$ interplanar
FIG. 2: The Mott insulating band structure of La$_4$Ni$_3$O$_8$ for the calculated ground state of Fig. 1. Left panel: the basic plot, allowing nearly degenerate bands to be distinguished. Other panels: La$_4$Ni$_3$O$_8$ fatband representation emphasizing (middle panel) Ni2, and (right panel) Ni1, $d$ character. Note that the band at the bottom of the gap has vanishing Ni1 character.

FIG. 3: Energy level diagram. The intraatomic levels are shown on the left, with occupied majority states on the far left, partially occupied minority levels just to the right. The right panel indicates how the $d_{z^2}$ orbitals on the Ni2-Ni1-Ni2 triple couple to give a gap at 2/3 band filling, following Eq. 1.

coupling $t_{\perp}$ (between Ni1 and Ni2) becomes important. For each Ni2-Ni1-Ni2 triple along the $z$ axis with neighbors coupled by $t_{\perp}$ (with zero site energy, neglecting the small on-site energy difference), the eigenvalues and eigenvectors are

$$E_j = 0, \pm \sqrt{2}t_{\perp},$$

$$|E_j> = \frac{1}{\sqrt{2}}(1,0,-1), \frac{1}{2}(1,\pm\sqrt{2},1).$$  \(1\)

The non-bonding (odd symmetry) state at $E_{j=0}=0$ which does not involve the Ni1 site is flanked below and above by even symmetry bonding ($E_+$) and antibonding ($E_-$) combinations. This coupling is pictured at the right of Fig. 3.

In the middle and right panels of Fig. 2 the Ni $d$ characters are emphasized for Ni2 and Ni1, respectively. The bands display both the spectrum (most clearly evident near the M point) and the (Ni1 vs. Ni2) character of this “triatomic molecule”. For example, the band at the bottom of the gap is (non-bonding) purely Ni2, which is $E_0$, while the other two bands have both Ni1 and Ni2 character ($E_+, E_-)$. Two of these levels will be filled (below the Fermi level) and one empty (above the Fermi level). The gap size, which is 0.6 eV here, will depend both on the coupling $t_{\perp}$ and the value of U.

Since previous LDA+U studies produced only a metallic result, one can understand the electronic structure only using a quantum-coupled unit, a molecular trimer basis, for the trilayer, from which on-site repulsion produces a (Mott) insulating state in agreement with observation. The intralayer AFM magnetic coupling is strong and is mediated by $d_{x^2-y^2}$ superexchange, as in cuprates. Between
NiO$_2$ layers, the coupling is FM direct exchange arising from the $d_{z^2}$ orbitals (Wannier functions). This FM coupling is robust in the sense that we could not obtain antialigned layer magnetic order. Experimental data suggest an in-plane magnetic coupling with $J_{||} \approx 120$ K$^{13}$, which is substantial but an order of magnitude smaller than in cuprates.

The trilayer-to-trilayer coupling will be superexchange through the fluorite La$_3$/O$_2$/La spacer layer that can be seen in Fig. 4. The $k_z$ bandwidth and related dispersion can be estimated from the splitting of the band below the gap near -0.5 eV at $\Gamma$ (this splitting vanishes at $\pi/c$). The hopping $t_z \sim 15$ meV from a Ni$_2$ ion to four Ni$_2$ ions across the blocking layer leads to $J_z = 4t_z^2/U \sim 0.2$ meV $\sim 2$ K. Such small interlayer coupling enters $T_N$ logarithmically and can still give rise to magnetic order. However, the interslab coupling is frustrated as well as being small. These facts suggest that some of the entropy will not be lost at $T_N=105$ K (full magnetic order along the $z$ axis is not established), consistent with the small observed entropy change and also with the absence of a new diffraction peak$^{13}$ below $T_N$.

The state we have obtained and analyzed has insulating, AFM order in-plane in common with the HTS cuprates, as well as the obvious similarities in structure. The differences are however substantial. First, excellent insulating character and relatively strong superexchange-mediated AFM order is obtained without integer formal oxidation states on the Ni ions. Such behavior has not been reported previously for transition metal oxides. Second, the $d_{x^2-y^2}$ hole on each Ni ion is robust, and doped carriers go only into $d_{z^2}$ states; hence the AFM order (driven by $d_{z^2}$ states) may survive to much larger doping level than in cuprates. Orbital order is ruled out. Third, holes will enter the non-bonding band that is confined to the outer Ni$_2$ layers, so beyond the insulator-to-metal transition these two conducting layers will be separated by a non-participating Ni$_1$ middle layer; the conductivity will be both orbital and layer specific. Doped electrons will go into all three Ni layers, but with half of the charge on the central Ni$_1$ layer.

The insulator-to-metal transition in either case will likely occur within the AFM ordered phase rather than occurring simultaneously. Superconductivity coexisting with AFM order is known to occur, but the competition tends to be very unfavorable for superconductivity. Moreover, the magnetic interactions between the doped carriers (in $d_{z^2}$ states) will be very weak, and very unlike cuprates where carriers are doped into the $d_{x^2-y^2}$ states. Though substantially different from cuprates, doped La438 should be an extremely interesting system, and doping should be pursued.

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