Multiband model for tunneling in MgB$_2$ junctions

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A theoretical model for quasiparticle and Josephson tunneling in multiband superconductors is developed and applied to MgB$_2$-based junctions. The gap functions in different bands in MgB$_2$ are obtained from an extended Eliashberg formalism, using the results of band structure calculations. The temperature and angle dependencies of MgB$_2$ tunneling spectra and the Josephson critical current are calculated. The conditions for observing one or two gaps are given. We argue that the model may help to settle the current debate concerning two-band superconductivity in MgB$_2$.

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Soon after the discovery of superconductivity in MgB$_2$[1], first principle calculations were performed to determine the electronic structure of this material. It was found that the Fermi surface consists of two three-dimensional sheets, from the $\pi$ bonding and antibonding bands, and two nearly cylindrical sheets from the two-dimensional $\sigma$ bands. The multi-band picture has given rise to the concept that two superconducting energy gaps can coexist in MgB$_2$.

Two-band superconductivity is a phenomenon that has been observed in Nb doped SrTiO$_3$.[2] Recent experimental STM and point-contact spectroscopy, high-resolution photo-emission spectroscopy, Raman spectroscopy, specific heat measurements and muon-spin-relaxation studies of the magnetic penetration depth support the concept of a double gap in MgB$_2$ (see Ref. 3 for a review of experiments). However, there is an ambiguity in the interpretation of point-contact data concerning the existence of two gaps. Moreover, some tunneling measurements show only one gap with a magnitude smaller than the BCS value of $\Delta = 1.76 \hbar k_B T_c$.

In order to resolve this discrepancy, we address the question, how multiband superconductivity will manifest itself in tunneling. We present the theoretical model for quasiparticle and Josephson tunneling in MgB$_2$-based junctions. Using the results of band-structure calculations, we apply an extended Eliashberg formalism to obtain the gap functions in different bands, taking strong coupling effects into account. Tunneling from a normal metal (N) into MgB$_2$ is considered in an extended Blonder-Tinkham-Klapwijk (BTK) model.[4] The temperature dependencies and absolute values of the energy gap functions from a normal metal (N) into MgB$_2$ are calculated in MgB$_2$-based SIS tunnel junctions, where $S$ denotes a superconductor and $I$ an insulator. Tunneling in the direction of the $a$-$b$ plane, the $c$-axis direction and under arbitrary angle is considered. Furthermore, the Josephson supercurrent between a single-gap superconductor and MgB$_2$ is calculated.

According to the labeling of Liu et al.,[5] the four Fermi surface sheets in MgB$_2$ are grouped into quasi-two-dimensional $\sigma$ bands and three-dimensional $\pi$ bands. Hence, normal and superconducting properties of MgB$_2$ can be described by an effective two-band model. Within this model, Liu et al.[6] estimated the coupling constants and energy gap ratio in the weak coupling regime. More recently, the band decomposition of the superconducting and transport Eliashberg functions $\alpha_i^2 F_i(\omega)$ (where $i$ and $j$ denote $\sigma$ or $\pi$ bands), which describe the electron-phonon coupling in MgB$_2$ as function of the frequency $\omega$, was provided in Ref. 19. This allows to perform a strong coupling calculation of the superconducting energy gap functions $\Delta_i(\omega_n)$ in different bands. The functions $\Delta_i(\omega_n)$ in turn determine the Josephson critical current in a tunnel junction between multiband superconductors, which is given by a straightforward generalization of the well-known result to the case of several conducting bands as well as strong coupling. The critical current component for tunneling from band $i$ into $j$ is given by

$$I_{ij} = \pi T \frac{\Delta L_{i}(\omega_n) \Delta R_{j}(\omega_n)}{\sqrt{\omega_n^2 + \Delta_{i}^2(\omega_n) \sqrt{\omega_n^2 + \Delta_{j}^2(\omega_n)}}},$$

where $L$ and $R$ denote left and right superconductors respectively, $R_{ij}^{-1} = \min\{R_{L_{ij}}, R_{R_{ij}}^{-1}\}$ is the normal-state conductance of a junction for the bands $(i, j)$ which is given by the integral over the Fermi surface $S_{L_{i}(R_{j})}$

$$(R_{L_{i}(R_{j})};A)^{-1} = \frac{2e^2}{h} \int_{v_n > 0} \frac{D_{ij} v_{n,L_{i}(R_{j})}}{(2\pi)^{1/2}} v_{F,L_{i}(R_{j})} S_{L_{i}(R_{j})},$$

where $A$ is the junction area, $v_n$ is the projection of the Fermi velocity $v_F$ on the direction normal to the junction plane, and $D_{ij}$ is the probability for a quasiparticle to tunnel from band $i$ in $L$ into band $j$ in $R$. The total critical current is the sum of the components $I_c = \sum_{ij} I_{ij}$.

The gap functions $\Delta_i(\omega_n)$ can be calculated with an extension of the Eliashberg formalism to two bands

$$\Delta_i(\omega_n) Z_i(\omega_n) = \pi T \sum_{j} \frac{\lambda_{ij} - \bar{\mu}_{ij}}{\sqrt{\omega_{j}^2 + \Delta_{j}^2(\omega_n)}} \Delta_j(\omega_n),$$

where $\lambda_{ij}$ is the critical current and $R_{ij}$ is the normal state resistance are calculated in MgB$_2$-based SIS tunnel junctions, where S denotes a superconductor and I an insulator. Tunneling in the direction of the $a$-$b$ plane, the $c$-axis direction and under arbitrary angle is considered. Furthermore, the Josephson supercurrent between a single-gap superconductor and MgB$_2$ is calculated.
\[
Z_i(\omega_n) = 1 + \frac{\pi T}{\omega_n} \sum_j \sum_m \lambda_{ij} \frac{\omega_m}{\sqrt{\omega_m^2 + \Delta_j^2(\omega_m^2)}}.
\]

where \(\lambda_{ij} = 2 \int_0^\infty \alpha \omega^2 F_{ij}(\omega) \, d\omega / [\omega^2 + (\omega_m - \omega_n)^2]\), \(Z_i(\omega_n)\) are the Migdal renormalization functions and \(\omega_n = \pi T(2n + 1)\). These equations are solved numerically with the electron-phonon \(\alpha_{ij}^2 F_{ij}(\omega)\) functions from Ref.13. The cutoff frequency \(\omega_c\) is taken equal to 10 times the maximum phonon frequency. The functions \(\mu_{ij}^*\) represent a matrix of the Coulomb pseudopotentials defined at \(\omega_i\), calculated up to a common prefactor that is used as an adjustable parameter to get \(T_c = 39.4\,\text{K}\). The matrix \(\mu^*\) at the frequency \(\omega_i\) (relevant for the McMillan expression for \(T_c\) in the isotropic case) is given by \(\mu^* = [1 + \mu^* \ln(\omega_i/\omega_n)]^{-1} \mu^*\), where \(\omega_i\) follows from \(0 = \int_0^\infty \ln(\omega/\omega_i) \omega^{-1} \alpha_{ij}^2 F_{ij}(\omega) \, d\omega\). The corresponding matrix elements are \(\mu_{\sigma\sigma} = 0.13, \mu_{\sigma\pi} = 0.042, \mu_{\pi\sigma} = 0.03, \mu_{\pi\pi} = 0.11\) and \(\lambda_{ij}(\omega_m = \omega_n)\) from Ref.19 are \(\lambda_{\sigma\sigma} = 1.017, \lambda_{\sigma\pi} = 0.213, \lambda_{\pi\sigma} = 0.155, \lambda_{\pi\pi} = 0.448\). Due to the interband coupling terms in Eqs. (3) and (4) both gaps close at the same \(T_c\). The resulting temperature dependences of the energy gaps, \(\Delta_\sigma(T)\), are plotted in the inset of Fig. 1 and it is found that \(\Delta_\sigma(T = 0) = 7.09\,\text{meV}\) and \(\Delta_\pi(T = 0) = 2.70\,\text{meV}\), with the \(2\Delta/T_c\) ratios being equal to 4.18 and 1.59, respectively. For comparison, also the BCS curve is shown for \(T_c = 39.4\,\text{K}\). The BCS value for the gap that corresponds to \(T_c = 39.4\,\text{K}\) is 6.0\,\text{meV} at 0\,\text{K}\). It can be seen that the temperature dependences are qualitatively different from the BCS temperature dependence. The ratio of the gaps \(\Delta_\sigma/\Delta_\pi\) increases for increasing temperatures, as was experimentally observed for example in Ref.13.

The influence of impurities can be incorporated into the model. Intraband scattering does not change the two gaps (Anderson’s theorem), while the interband scattering can be included by terms \(\gamma_{ij} \Delta_j / \sqrt{\omega_n^2 + \Delta_j^2}, \gamma_{ij} \omega_i / \sqrt{\omega_n^2 + \Delta_j^2}\) in the Eliashberg equations (3) and (4) respectively. The smallness of \(\gamma_{ij}\) compared to \(\pi T_c\) indicates that the double-gap feature should experimentally be observable, also in thin films, even for a certain amount of impurity scattering. A large amount of impurity scattering (\(\gamma_{ij}\) exceeding the maximum phonon frequency) will cause the gaps to converge to the same value. From Eqs. (3) and (4) and including the scattering terms an asymptotic value of \(\Delta_\sigma = \Delta_\pi = 4.1\,\text{meV}\) and \(T_c = 25.4\,\text{K}\) is found, giving a \(2\Delta/k_B T_c\) ratio of 3.7.

In order to obtain the normal state resistance, we have to evaluate the effective junction transparency components \(D_{ij}\). In the case of a specular barrier, \(U(x) = U_0b(x - x_0)\), \(D_{ij}\) is given by

\[
D_{ij} = \frac{\langle n_i\rangle \langle n_j\rangle}{\frac{1}{2} \langle n_i\rangle + \langle n_j\rangle} - U_0^2/\hbar^2.
\]

It follows from Eqs. (2) and (3) and as first pointed out in Ref.13 that the normal state conductance \(R_{ij}\) in the large \(U_0\) limit is proportional to the Fermi-surface average \(\langle N_i^2 \rangle_j\). The latter is proportional to the contribution of the electrons in band \(i\) to the squared plasma frequency \(\omega_p^2\). This essentially simplifies the task of summing up the interband currents since the partial plasma frequencies are available from the band structure calculations. The normal state junction conductance is thus proportional to \(\omega_p^2\), neglecting the difference in \(\langle n_i\rangle\). This is a reasonable assumption since the difference between \(v_F\) in the \(\pi\) bands in the \(a\)-\(b\) plane is rather small, while for \(c\)-axis tunneling the only \(\pi\) band contributes, as will be shown later, so that the problem of summation does not appear in this case.

**SIN tunneling**. The conductance in a MgB\(_2\)–I–N tunnel junction is the sum of the contributions of two bands. Each of the conductances is given by the BTK model [2] where the corresponding normal state conductances \(R_{ij}^{-1}\) are proportional to the minimum of the square of the plasma frequencies at the N and MgB\(_2\) sides. Since the plasma frequency in a typical normal metal (e.g. Au, Ag) is larger than the plasma frequencies in MgB\(_2\), the conductances are limited by the electrons on the MgB\(_2\) side

\[
R_{N\sigma}^{-1}/R_{N\pi}^{-1} = (\omega_p^\sigma)^2/(\omega_p^\pi)^2.
\]

Finally, the normalized conductance of an N–I–MgB\(_2\) contact is given by

\[
\sigma(V) \equiv \left[ \frac{dI}{dV} \right]_{NIS} = \omega_p^\sigma \sigma_\pi(V) + \omega_p^\pi \sigma_\sigma(V) \left[ \omega_p^\sigma - \omega_p^\pi \right].
\]

Here, the dimensionless conductances \(\sigma_\sigma,\pi(V)\) are provided by the BTK model, with the calculated values for the gaps and plasma frequencies, as shown in Table 1.

In the conductance versus voltage plot (Fig. 1) for tunneling in the \(a\)-\(b\) direction, two peaks are clearly visible, in qualitative agreement with the experimental data. The ratio of peak magnitudes is not only determined by the ratio of the plasma frequencies, but also by thermal rounding and by the barrier strength \(Z_{BTK} = U_0/hv_F\) (where \(hv_F\) is taken constant for the different bands for the same reason as was given in the determination of \(R_{ij}\)). In particular, the peak at the smaller gap dominates in the small \(Z_{BTK}\) regime (point-contact), while the second peak dominates at large values of \(Z_{BTK}\) (tunneling), as may be seen in Fig. 1 at 4.2 K.

Due to the smallness of \(\omega_p^\pi\) in the \(c\)-direction, it can be seen from Eq. (7) that the conductance in the \(c\)-direction is only determined by the \(\pi\) band. In this case, no double-peak structure is expected in the conductance spectrum. This explains, together with the dependence on \(Z_{BTK}\), why in some experiments only one peak was observed or why the second peak was weak.
Note, that the assumption of the ratio of the normal state conductivities being equal to the ratio of the square of the plasma frequencies holds when the interface is a $\delta$-function shaped tunnel barrier, with large $Z_{BTK}$. This means that for small $Z_{BTK}$, the results should be considered as a qualitative indication only. In the latter case, as well as for other types of barriers, a numerical integration of Eqs. (2, 5) must be performed.

**SIS Josephson tunneling.** We consider Josephson tunneling between two MgB$_2$ superconductors. With the values for the plasma frequencies, $\omega_p^c < \omega_p^z$, this gives $R_{\pi\pi} = R_{\pi\sigma} = \max (R_{\pi\pi}, R_{\pi\pi}) = R_{\pi\sigma}$ and $R_{\pi\pi}/R_{\pi\pi} = R_{\pi\sigma}/R_{\pi\pi} = (\omega_p^c/\omega_p^z)^2 > 1$. The total conductance is given by $\frac{I_c}{R_N} = \frac{1}{\sum_{i,j} R_{ij}^{-1}}$.

For tunneling in the $a$-$b$ plane (as can be realized for example in an edge configuration), with $R_{\pi\pi} = R_{\pi\sigma}$ and $I_{\pi\pi} = I_{\pi\pi}$, the total $I_c/R_N$ product becomes

$$I_c/R_N = \frac{I_{\pi\pi} R_{\pi\pi} + 2I_{\pi\pi} R_{\pi\pi} + I_{\pi\pi} R_{\pi\pi} \left(\frac{\omega_p^c}{\omega_p^z}\right)^2}{3 + \left(\frac{\omega_p^c}{\omega_p^z}\right)^2}. \tag{8}$$

The results of numerical calculations are presented in Fig. 3. Due to strong-coupling and interband coupling effects, the temperature dependencies of $I_{ij} R_{ij}$ differ from the well-known Ambegaokar-Baratof result for an SIS junction between isotropic superconductors, most clearly demonstrated by the positive curvature of the $I_{\pi\pi} R_{\pi\pi}$ contribution. The $I_c/R_N$ value at $T = 4.2$ K is 5.9 mV.

For tunneling along the c-axis, the only contribution to the $I_c/R_N$ product comes from $I_{\pi\pi} R_{\pi\pi}$, because of the negligible value for $\omega_p^c$ in the c-axis direction. This gives $I_c/R_N = 4.0$ mV at $T = 4.2$ K.

The plasma frequency in a certain direction, under an angle $\varphi$ with the $a$-$b$ plane, can be determined from the ellipsoid equation $(\omega_p^a)^2 = (\omega_p^i)^2 + (\omega_p^j)^2$, and $(\omega_p^i)^2 = \frac{(\omega_p^i)^2}{(\omega_p^a)^2}$, where $\omega_p^i$ and $\omega_p^j$ form the decomposition of $\omega_p^c$. Because of the negligible value of $\omega_p^c$, it is evident that $\omega_p^c$ is negligible for nonzero values of $\varphi = \arctan(\omega_p^i/\omega_p^j)$. This implies that tunneling under a nonzero angle with the $a$-$b$ plane gives the same result as tunneling in the c-axis direction, namely $I_c/R_N = 4.0$ mV at $T = 4.2$ K. For angles approaching zero (of the order of 0.6°), $I_c/R_N$ rapidly increases towards the maximal value for tunneling from $a$-$b$ plane to $a$-$b$ plane, namely $I_c/R_N = 5.9$ mV at $T = 4.2$ K. For a large amount of impurity scattering the $I_{ij} R_{ij}$ values converge to the same value. It follows in that case from Eq. (8), with the plasma frequencies from Table 1, that $I_c/R_N$ becomes almost isotropic.

Finally, tunneling from MgB$_2$ into a superconductor $S'$ with a single gap will be considered (we take Nb as an example). The resulting $I_{\pi S}/R_{\pi S}$ temperature dependencies are calculated numerically, using 1.4 mV for the energy gap in Nb. The ratio of resistances is determined from Eq. (2). Since typical values of plasma frequencies in other superconductors are bigger than in MgB$_2$ (e.g. 9.47 eV for Nb, 12.29 eV for Al and 14.93 eV for Pb, see Ref [23], the following expression is obtained

$$I_c/R_N = \frac{I_{\pi S} R_{\pi S} + I_{\pi S} R_{\pi S} \left(\frac{\omega_p^a}{\omega_p^z}\right)^2}{1 + \left(\frac{\omega_p^a}{\omega_p^z}\right)^2}, \tag{9}$$

when tunneling occurs into the $a$-$b$ plane of the MgB$_2$. In the case of c-axis tunneling, only the $I_{\pi S} R_{\pi S}$ contribution remains. The results for tunneling from Nb to MgB$_2$ are also indicated in Fig. 3. Other superconductors give qualitatively similar results. The only scaling parameter is the critical temperature of the superconducting counter-electrode.

Our results for Josephson tunneling provide an upper bound for $I_c/R_N$ products, being 5.9 mV and 4.0 mV for tunneling
into the $a$-$b$ plane and $c$ direction respectively. There have already been several observations of Josephson currents in MgB$_2$ junctions with $I_c R_N$ values that are much lower than our predictions. This can be due to extrinsic reasons such as a degradation of the $T_c$ of surface layers in the vicinity of the barrier, the barrier nature and barrier quality. From our model, however, it follows that polycrystallinity does not reduce the Josephson coupling very much, as indicated by the calculated value of $I_c R_N$ of 4.0 mV for $c$-axis transport, neither does strong impurity scattering because of the relatively large average gap of 4.1 meV in this case.

In conclusion, Josephson tunneling in MgB$_2$-based junctions is discussed theoretically in the framework of a two-band model. The gap functions in different electronic bands are calculated using the Eliashberg formalism together with band structure information. This provides a basis to interpret electronic transport in MgB$_2$. We have shown the possibility to observe either one or two gaps in point-contact spectra of MgB$_2$, depending on the tunneling direction, barrier type and amount of impurities. The results are also relevant for the electronic application of MgB$_2$ since they provide the limit for the Josephson coupling strength in MgB$_2$ based junctions. For MgB$_2$ in the clean limit we have shown that $I_c R_N$ values as high as 5.9 mV can be expected for MgB$_2$ tunnel junctions if tunneling occurs in the direction of the $a$-$b$ plane. In other cases the limiting $I_c R_N$ values will not exceed 4.0 mV. Our predictions for the gap and $I_c R_N$ anisotropy and for the $I_c$ vs $T$ dependence in MgB$_2$-based junctions can be verified experimentally and thus may help to settle the current debate on two-band superconductivity in MgB$_2$.

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