Extensive ro-vibrational analysis of deuterated-cyanoacetylene (DC$_3$N) from millimeter-wavelengths to the infrared domain

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Abstract

Cyanoacetylene, the simplest cyanopolyne, is an abundant interstellar molecule commonly observed in a vast variety of astronomical sources. Despite its importance as a potential tracer of the evolution of star-forming processes, the deuterated form of cyanoacetylene is less observed and less studied in the laboratory than the main isotopologue. Here, we report the most extensive spectroscopic characterization of DC$_3$N to date, from the millimeter domain to the infrared region. Rotational and ro-vibrational spectra have been recorded using millimeter-wave frequency-modulation and Fourier-transform infrared spectrometers, respectively. All the vibrational states with energy up to 1015 cm$^{-1}$ have been analyzed in a combined fit, where the effects due to anharmonic resonances have been adequately accounted for. The analysis contains over 6500 distinct transition frequencies, from which all the vibrational energies have been determined with good precision for many fundamental, overtone, and combination states. This work provides a comprehensive line catalog for astronomical observations of DC$_3$N.

Keywords: Cyanoacetylene, Interstellar species, Ro-vibrational spectroscopy, Spectral analysis, Anharmonic resonances, Line catalog

1. Introduction

Highly unsaturated molecules account for a large portion of the known interstellar species [1]. For instance, the presence of several carbon-chain molecules is one of the most characteristic features of the chemical composition of starless cores, such as the Taurus Molecular Cloud (TMC-1), one of the brightest source of carbon-chain species [2]. Among the unsaturated molecular species, cyanopolyynes, i.e., linear molecules of general chemical formula HC$_{2n+1}$N, are widespread in the interstellar medium (ISM) and all members up to HC$_{11}$N have been detected to date [3]. Cyanoacetylene (HC$_3$N, IUPAC name prop-2-yenonitrile), the simplest member of the cyanopolyynes family, was found to be an abundant species in a large variety of astronomical objects: starless cores [4], post-AGB objects [5], carbon-rich circumstellar envelopes [6].

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massive star-forming regions, protoplanetary disks, solar-type protostars, external galaxies, and Galactic Center molecular clouds.

The deuterated form of cyanoacetylene (DC$_3$N) has been detected in the ISM as well. The first astronomical observation of DC$_3$N has been reported towards TMC-1 by the detection of the $J = 5 \rightarrow 4$ emission rotational transition around 42 GHz. Consecutively, DC$_3$N has tentatively been detected in the high-mass star-forming regions Orion KL and Sagittarius B2. In these regions, deuterium fractionation is not as effective as in dark clouds, thus preventing a strong enhancement above the deuterium cosmic abundance. Recently, DC$_3$N has been detected in some low-mass cores (see e.g., Refs. [9], [15]) and in a sample of 15 high-mass star-forming cores [16]. The latter work, based on the spectroscopic results presented in this paper, suggests that DC$_3$N is enhanced in the cold and outer regions of star-forming regions, likely indicating the initial deuteration level of the large-scale molecular cloud within which star formation takes place. Rivilla et al. [16] also summarize all the astronomical observations of DC$_3$N so far.

Microwave (MW) transitions of DC$_3$N were first reported for the ground and the lowest singly-excited states during the course of an extensive study of cyanoacetylene isotopologues [17]. A larger number of vibrationally excited states was re-examined in depth some years later and a rigorous determination of the effective molecular parameters was attained [18]. Recently, the laboratory investigation of the rotational spectrum of DC$_3$N has been extended to the THz regime for the ground and the $v_7 = 1$ states [19]. In the same paper, the authors revised the $^{14}$N and $^2$H hyperfine-structure constants derived in Refs. [20, 21] from supersonic-jet Fourier-Transform Microwave (FT-MW) spectroscopy.

As far as its infrared (IR) spectrum is concerned, the experimental position and intensity of all fundamentals but the weak $v_4$ mode have been determined from low resolution (0.5 cm$^{-1}$) studies [22, 23]. Some combination and overtone bands were also observed in the same works. In addition, two medium resolution (0.025–0.050 cm$^{-1}$) IR studies were performed by Mallinson & Fayt [24] and Coveliers et al. [25]. In the former, the band center of the three stretching modes of DC$_3$N ($v_1$, $v_2$, and $v_3$) has been determined; in the latter, the far-infrared (FIR) spectrum was recorded between 200 and 365 cm$^{-1}$ and the $v_7$ fundamental was analyzed together with the bands $v_6 - v_7$, $v_5 - v_7$, and $v_4 - v_6$, and their hot-bands.

In this work, a detailed investigation of both millimeter/submillimeter-wave and infrared spectra of DC$_3$N is reported. Pure rotational transitions within all the vibrational states with energy lower than 1015 cm$^{-1}$ have been detected and 27 fundamental, overtone, combination, and hot ro-vibrational bands have been analyzed at high resolution (0.001–0.01 cm$^{-1}$). The new measurements have been combined in a fit containing almost 6700 distinct transition frequencies, thus allowing the determination of a consistent set of spectroscopic parameters. This work represents the most exhaustive spectroscopic characterization of DC$_3$N so far and provides a robust line catalog useful for astronomical applications. Moreover, the large number of vibrationally excited states are of interest for harmonic/anharmonic force field computations.

The paper is structured as follows. First, the synthesis of the sample and the spectrometers used for spectral recording are described (§2.1). Then, the effective Hamiltonian employed for the energy levels description is given (§2). Successively, the general features of the spectra and their analysis are discussed (§3). Finally, the results are summarized and the conclusions are presented (§4).

2. Experimental details

2.1. Synthesis of deuterocyanocacycyle

Methyl propiolate (HC≡CCOOCH$_3$) was purchased from TCI-Europe and used without further purification. The DC$_3$N sample was synthesized in Rennes following the procedure described in Ref. [26]. Briefly, HC≡CCOOCH$_3$ was added dropwise to liquid ammonia resulting in a 100% conversion into HC≡CCONH$_2$. The propiolamide was then mixed with phosphorous anhydride ($P_4O_{10}$) and calcined white sand; the whole system was heated up to 470 K over 2 h while connected to a liquid nitrogen-cooled trap where pure cyanoacetylene was collected. Cyanoacetylene (3 g), heavy water (D$_2$O, 4 mL) and potassium carbonate (K$_2$CO$_3$, 50 mg) were mixed together in an inert atmosphere. The biphasic mixture was then stirred for about 20 min at room temperature. Subsequently, on a vacuum line, partially deuterated cyanoacetylene was condensed in a 77 K cooled trap, while water was blocked in a first 220 K trap. The operation was
repeated 3 times by addition of D₂O and K₂CO₃ to the partially deuterated cyanoacetylene. The residual D₂O was removed by vaporisation on P₄O₁₀ and DC₃N was finally condensed in a trap cooled to 150 K. Deuterocyanoacetylene with an isotopic purity greater than 98% was obtained in a 67% yield. The sample can be stored indefinitely at 250 K without decomposition.

2.2. Infrared spectrometers

The FIR spectrum of DC₃N was recorded at the AILES beamline of the SOLEIL synchrotron facility using a Bruker IFS 125 FT interferometer [26] and a white-type multipass absorption cell whose optics were adjusted to obtain a 150 m optical path length [27][28]. For the present experiment, we used the far-IR synchrotron radiation continuum extracted by the AILES beamline. The interferometer was equipped with a 6 µm Mylar-composite beamsplitter and a 4 K cooled Si-bolometer. Two 50 µm-thick polypropylene windows isolated the cell from the interferometer, which was continuously evacuated to 0.01 Pa limiting the absorption of atmospheric water. Vapor of DC₃N was injected into the absorption cell at a 25 Pa pressure. The spectrum covers the range 70–500 cm⁻¹ and consists of the co-addition of 380 scans recorded at 0.00102 cm⁻¹ resolution.

IR spectra in the 450–1600 cm⁻¹ range were recorded in Bologna using a Bomem DA3.002 Fourier-Transform spectrometer [29]. It was equipped with a Globar source, a KBr beamsplitter, and a liquid nitrogen-cooled HgCdTe detector. A multi-pass cell with absorption-lengths from 4 to 8 m was employed for the measurements. Sample pressures ranging between 25 and 650 Pa were used to record the spectra. The resolution was generally 0.004 cm⁻¹, except for the very weak ν₄ band, which was recorded at a lower resolution of 0.012 cm⁻¹. Several hundreds of scans, typically 800, were co-added in order to improve the signal-to-noise ratio (S/N) of the spectra.

All the spectra have been calibrated using residual water or CO₂ absorption lines whose reference wavenumbers were taken from Refs. [30][31] and from HITRAN [32], respectively. No apodization functions were applied to the interferograms.

2.3. Millimeter and submillimeter spectrometers

Rotational spectra have been recorded using two frequency-modulation (FM) millimeter/submillimeter spectrometers located in Bologna and in Garching.

The Bologna spectrometer has been described in details elsewhere [33][34]. Briefly, a Gunn diode oscillator operating in the W band (80–115 GHz) was used as primary source of radiation, whose frequency and phase stability are ensured by a Phase-Lock Loop (PLL). Spectral coverage at higher frequencies was obtained by coupling the Gunn diode to passive frequency multipliers in cascade (doublers and triplers, Virginia Diodes, Inc.). The output radiation, sine-wave modulated in frequency (f = 48 kHz), was fed to the glass absorption cell containing DC₃N vapors at a pressure between 1 and 15 Pa, depending on the intensity of the lines under consideration. The outcoming signal was detected by a Schottky barrier diode and sent to a Lock-in amplifier set at twice the modulation-frequency (2f scheme); the demodulated signal is then filtered into a resistor-capacitor (RC) system before data acquisition.

In Garching the CASAC spectrometer developed at the Max-Planck-Institut für extraterrestrische Physik was used. Full details on the experimental set-up are given in Ref. [35]; here, we report only a few key details which apply to the present investigation. The instrument is equipped with an active multiplier chain (Virginia Diodes) as a source of radiation in the 82–125 GHz band. Further multiplier stages in cascade allow to extend the frequency coverage up to ~ 1.1 THz with an available power of 2–20 µW. The primary millimeter radiation stage is driven by a cm-wave synthesizer (Keysight E8257D) operating in the 18-28 GHz band, which is locked to a Rb atomic clock to achieve accurate frequency and phase stabilisation. A closed-cycle He-cooled InSb hot-electron bolometer operating at 4 K (QMC) is used as a detector. As in Bologna, frequency (f = 50 kHz) modulation technique is employed and the second derivative of the actual absorption profile is thus recorded by the computer-controlled acquisition system after lock-in demodulation at 2f. The absorption cell is a plain Pyrex tube (3 m long and 5 cm in diameter) fitted with high-density polyethylene windows. The measurement were performed using gaseous samples at pressure of a few Pa. In this condition, DC₃N is stable for ca. 2 h without significant decomposition due to hydrogen exchange.
The spectra were recorded in the frequency ranges 80–115 GHz and 920–1070 GHz in Garching, and in the window 240–440 GHz in Bologna.

Table 1: Energy and intensity of all fundamental modes of DC₃N.

| Modes       | Description     | Energy (cm⁻¹)       | Reference | Abs. intensity (atm⁻¹cm⁻²) |
|-------------|-----------------|---------------------|-----------|----------------------------|
| ν₁          | C–D stretching  | 2608.520(3)         | [24]      | 81.3 ± 5.7²         |
| ν₂          | C≡C stretching  | 2252.155(3)         | [24]      | 50.5 ± 2.4²         |
| ν₃          | C≡N stretching  | 1968.329(3)         | [24]      | 38.7 ± 4.0²         |
| ν₄          | C–C stretching  | 867.60(6)           | This Work | < 0.1³               |
| ν₀          | CCD bending     | 522.263933(7)       | This Work | 83.8 ± 4.7³         |
| ν₆          | CCC bending     | 492.759896(7)       | This Work | 106. ± 8³           |
| ν₇          | CCN bending     | 211.550293(5)       | This Work | 0.89 ± 0.11³        |

[a] From low-resolution integrated band-intensity measurements at 296 K (Ref. [23]). [b] From low-resolution integrated band-intensity measurements at 293 K (Ref. [22]).

3. Theoretical background

From a spectroscopic point of view, DC₃N is a closed-shell linear rotor. It has 7 vibrational modes: 4 stretchings (ν₁–ν₄; Σ symmetry) and 3 doubly-degenerated bendings (ν₅–ν₇; Π symmetry). They are summarized in Table 1. In the present work, only the low-lying vibrational states (ν₁, ν₅, ν₀, and ν₇, with one of multiple quanta of excitation) have been investigated for two main reasons: (i) transitions associated to the lower energy states are of astrophysical interest, and (ii) some of the vibrational states are connected by a network of anharmonic resonances fully described within our chosen energy threshold of 1015 cm⁻¹; above this limit the states are either unperturbed or involved in higher-order resonances. Therefore, the stretching modes ν₁, ν₂, and ν₃, lying above this threshold, have not been investigated. Conventionally, we labelled a given vibrational state with the notation \( |v₄, v₅^e, v₆^f, v₇^e; J, k\rangle_{e/f} \), where \( l_t \) is the vibrational angular momentum quantum number associated to the bending mode \( t \) and the \( e/f \) subscripts indicate the parity of the symmetrized wave functions [36]. When the \( l_t \) and \( e/f \) labels are not indicated, we refer to all the possible sub-levels of a state.

The full ro-vibrational wave-function is then given by the ket \( |v₄, v₅^e, v₆^f, v₇^e; J, k\rangle_{e/f} \). The vibrational part of the wave-function is expressed as combination of one- or two-dimensional harmonic oscillators, whereas the rotational part is the symmetric-top wave-function whose quantum number \( k \) is given by \( k = l_5 + l_6 + l_7 \). A substate is denoted as Σ when \( k = 0 \), Π for \( |k| = 1 \), \( \Delta \) for \( |k| = 2 \), and so on.

The following Wang-type linear combinations [37] lead to symmetry-adapted basis functions:

\[
\begin{align}
|v₄, v₅^e, v₆^f, v₇^e; J, k\rangle_{e/f} &= \frac{1}{\sqrt{2}} \left\{ |v₄, v₅^e, v₆^f, v₇^e; J, k\rangle \pm (-1)^k |v₄, v₅^e, v₆^f, v₇^e; J, -k\rangle \right\}, \\
|v₄, 0^e, 0^f, 0^e; J, 0\rangle_e &= |v₄, 0^e, 0^f, 0^e; J, 0\rangle_f.
\end{align}
\]

The upper and lower signs \( (\pm) \) correspond to \( e \) and \( f \) wave-functions, respectively. For Σ states \( (k = 0) \), the first non-zero \( l_t \) is chosen positive. Here, the omission of the \( e/f \) label indicates unsymmetrised wave-
functions. The Hamiltonian used to reproduce the ro-vibrational energy levels is equivalent to the one used for HC$_3$N [38]:

$$\mathcal{H} = \mathcal{H}_{\text{rv}} + \mathcal{H}_{\text{l-type}} + \mathcal{H}_{\text{res}},$$

(2)

where $\mathcal{H}_{\text{rv}}$ is the ro-vibrational energy including centrifugal distortion corrections, $\mathcal{H}_{\text{l-type}}$ represents the $l$-type interaction between the $l$ sub-levels of the excited bending states, and $\mathcal{H}_{\text{res}}$ accounts for resonances among accidentally quasi-degenerate ro-vibrational states. The resonance network active in DC$_3$N resembles the one found for HC$_3$N and will be described later.

The Hamiltonian matrix is built by using unsymmetrised ro-vibrational functions. It is subsequently factorized and symmetrized using Eqs. (1). The matrix elements of the effective Hamiltonian are expressed using the formalism already employed for the analysis of HC$_3$N [38].

4. General features and analysis

4.1. Vibrational spectra

Although infrared spectra were recorded up to 1600 cm$^{-1}$ in this study, our analysis is limited to the portion of the electromagnetic spectrum below $\sim$ 1040 cm$^{-1}$. This is because the highest energy state within our threshold of 1015 cm$^{-1}$ is the (0110) state, whose combination band falls in the region 999–1035 cm$^{-1}$. In total, 27 ro-vibrational bands have been observed at high resolution for the first time and successfully analyzed. They include fundamental, overtone, combination, and hot-bands, and are listed in Table 2 along with the observed sub-bands, frequency and $J$ ranges, number of data used in the analysis, and the root-mean-square ($rms$) error of the final fit. All the observed bands are also graphically displayed in Figure 1.

Figure 2 shows a general overview of portions of the FIR (180–460 cm$^{-1}$ range, upper panel) and mid-infrared (MIR, 450–800 cm$^{-1}$ range, bottom panel) spectra recorded in this work. The most prominent bands in the FIR region are the $\nu_7$ fundamental, $\nu_6 - \nu_7$, $\nu_5 - \nu_7$, and $2\nu_7$ overtone bands. The MIR region is dominated by the very strong fundamentals $\nu_6$ and $\nu_5$. The low-frequency side of the spectrum is particularly crowded due to the proximity of the two fundamentals, the presence of their associated hot-bands, and of the $\nu_6$ of HC$_3$N centered at 500 cm$^{-1}$. HC$_3$N is present in the sample as result of the H/D exchange in the cell. Having a medium IR intensity, the combination bands $\nu_6 + \nu_7$ and $\nu_5 + \nu_7$ are well visible in the high-frequency part of the MIR spectrum as seen in the bottom panel of Figure 2. Although not displayed in Figure 2, the overtone $2\nu_6$ and the combination $\nu_5 + \nu_6$ bands centered around 975–1018 cm$^{-1}$ and 999–1035 cm$^{-1}$, respectively, are clearly detectable as well, despite the presence of strong absorption lines due to HDO. The very weak ($< 0.1$ atm$^{-1}$ cm$^{-2}$) $\nu_4$ fundamental at 830–865 cm$^{-1}$ had to be recorded at higher pressure (400 Pa) and lower resolution (0.012 cm$^{-1}$). In this case, up to 2600 scans were co-added to improve the S/N of the spectrum.

4.2. Rotational spectra

Rotational spectra were recorded for all the 14 states whose vibrational energy do not exceed our threshold of 1015 cm$^{-1}$. Literature data were available for some of these states, as pointed out in Section 1. However, line positions of some millimeter-wave transitions from Ref. [17] are affected by large uncertainties (up to 300 kHz) and many data are limited to low frequencies. For these reasons, we decided to re-investigate and extend the spectrum for all these vibrational states. The largest improvements have been realized for the states (1000), (0110), (0020), and (0004) involved in a network of anharmonic resonances, for which extended data-sets were obtained. In particular, the (0110) state, not included in the analysis of Ref. [13], has been assigned for the first time in this study and its interaction with the (1000) state has been identified and properly accounted for.

Table 3 summarizes the set of rotational data used in the analysis, specifying the observed sub-levels, $J$ and frequency ranges, number of distinct fitted frequencies, the $rms$ error of the final fit, and the corresponding references used.
Table 2: Ro-vibrational bands recorded and analyzed in this work.

| Band   | Sub-bands | Freq. range (cm$^{-1}$) | $J$ range | No. of lines | $rms \times 10^4$ (cm$^{-1}$) |
|--------|-----------|-------------------------|-----------|--------------|-------------------------------|
| $\nu_7$ | $\Pi - \Sigma^+$ | 190-240 | 1-93 | 258 | 0.5 |
| $\nu_6$ | $\Pi - \Sigma^+$ | 466-522 | 2-109 | 267 | 3.6 |
| $\nu_5$ | $\Pi - \Sigma^+$ | 500-557 | 0-117 | 255 | 3.7 |
| $\nu_4$ | $\Sigma^+ - \Sigma^+$ | 830-865 | 0-61 | 109 | 9.6 |
| $2\nu_7$ | $\Sigma^+ - \Sigma^+$ | 405-445 | 2-78 | 136 | 1.0 |
| $\nu_6 + \nu_7$ | $\Sigma^+ - \Sigma^+$ | 975-1018 | 2-101 | 141 | 5.2 |
| $\nu_5 + \nu_7$ | $\Sigma^+ - \Sigma^+$ | 686-736 | 1-89 | 166 | 2.5 |
| $\nu_4 + \nu_7$ | $\Sigma^+ - \Sigma^+$ | 715-769 | 1-105 | 170 | 3.0 |
| $\nu_5 + \nu_6$ | $\Sigma^+ - \Sigma^+$ | 999-1035 | 3-63 | 102 | 3.8 |
| $\nu_6 - \nu_7$ | $\Pi - \Pi$ | 257-306 | 1-89 | 309 | 0.6 |
| $\nu_5 - \nu_7$ | $\Pi - \Pi$ | 288-333 | 1-86 | 291 | 0.7 |
| $\nu_4 - \nu_6$ | $\Sigma^+ - \Pi$ | 329-375 | 1-79 | 222 | 0.6 |
| $4\nu_7 - \nu_6$ | $\Sigma^+ - \Pi$ | 351-352 | 59-60 | 2 | 0.4 |
| $2\nu_7 - \nu_6$ | $\Sigma - \Pi$ | 193-236 | 1-78 | 391 | 0.8 |
| $3\nu_7 - 2\nu_7$ | $\Pi - \Sigma^+$ | 191-235 | 4-77 | 178 | 0.7 |
| $4\nu_7 - 3\nu_7$ | $\Sigma^+ - \Pi$ | 193-219 | 10-58 | 89 | 0.9 |
| $3\nu_7 - \nu_7$ | $\Pi - \Pi$ | 405-441 | 4-68 | 208 | 1.0 |
| $\nu_6 + \nu_7 - \nu_7$ | $(\Sigma, \Delta) - \Pi$ | 478-508 | 5-56 | 329 | 6.9 |
| $\nu_4 + 2\nu_7 - 2\nu_7$ | $\Pi - (\Sigma^+, \Delta)$ | 476-512 | 12-65 | 93 | 5.2 |
| $2\nu_6 - \nu_6$ | $\Sigma - \Pi$ | 500-519 | 10-68 | 43 | 7.0 |
| $\nu_5 + \nu_7 - \nu_7$ | $(\Sigma^+, \Delta) - \Pi$ | 505-545 | 2-75 | 464 | 4.5 |
| $\nu_5 + 2\nu_7 - 2\nu_7$ | $\Pi - (\Sigma, \Delta)$ | 505-542 | 2-82 | 106 | 3.5 |
| $\nu_4 + 2\nu_7 - \nu_7$ | $\Pi - \Pi$ | 690-718 | 4-53 | 153 | 4.7 |
| $\nu_5 + 2\nu_7 - \nu_7$ | $\Pi - \Pi$ | 721-748 | 2-45 | 296 | 4.1 |
| $\nu_6 + \nu_7 - 2\nu_7$ | $(\Sigma^+, \Delta) - (\Sigma^+, \Delta)$ | 290-330 | 2-81 | 261 | 0.9 |
| $\nu_5 + \nu_7 - 2\nu_7$ | $(\Sigma^+, \Delta) - (\Sigma^+, \Delta)$ | 256-306 | 2-84 | 402 | 0.9 |
| $4\nu_7 - 2\nu_7$ | $(\Sigma^+, \Delta) - (\Sigma^+, \Delta)$ | 406-437 | 5-67 | 302 | 1.0 |

With the exception of $\nu_4 = 1$, all the states possess a rotational constant $B$ greater than that of the ground state and therefore their rotational lines lie at frequencies higher than those of the corresponding ground state transition. This can be seen in Figure 3 where the broad scan covers the $J = 13 \leftrightarrow 12$ transitions for many vibrational satellites. In this excerpt, the $l$-type resonance patterns of all the excited bending states analyzed are visible. From a visual inspection, it is easy to associate some of these patterns to the pertaining state: the ground and $\nu_4 = 1$ exhibit a single line, while each bending state has $\Sigma = \prod_l (l_t + 1)$ lines (even though not always resolvable).

4.3. Analysis of the spectra

The sample of pure rotational and ro-vibrational data contains 6691 distinct frequencies involving 14 vibrational states of DC$_3$N. This work represents the first-ever investigation of its ro-vibrational spectrum in the region between 365 and 1040 cm$^{-1}$. Moreover, the FIR spectrum has been thoroughly re-investigated.
Figure 1: Vibrational energy-level diagram of DC$_3$N up to 1015 cm$^{-1}$, where the arrows represent the 27 IR bands analyzed in this work. Red and blue arrows indicate the bands observed at SOLEIL and in Bologna, respectively.

at higher resolution with an accuracy two or three orders of magnitude better than Ref. [25]. As far as the rotational spectrum is concerned, this work extends the observation of excited states transitions to the submillimeter-wave region. In addition, rotational transitions with $J$ up to 126 were recorded at THz frequencies (1.069 THz) although only for the ground state.

In the combined fit, a different weight was given to each datum in order to take into account the different measurements precision. Uncertainties spanning from 0.0004 to 0.00075 cm$^{-1}$ were used for the infrared measurements performed in Bologna; the weak $\nu_4$ band being the only exception, for which an uncertainty of 0.001 cm$^{-1}$ was assumed. FIR data recorded at higher resolution with the FT-IR spectrometer of the AILES beamline have been given uncertainties between 0.00005 and 0.0001 cm$^{-1}$, based on calibration residuals and the S/N of spectral lines. As far as pure rotational transitions are concerned, we assumed a typical experimental error of 10–20 kHz for our new millimeter/submillimeter measurements. Data from literature were used with the uncertainty stated in the original papers [17, 18, 19]. Only few lines from Ref. [17], whose residuals were far off their declared errors, were not used in the fit.

The spectral analysis was performed using a custom PYTHON code that employs the SPFIT program [39] as computational core (see Ref. [38] for further details about the code). The data were fitted to the Hamiltonian of Eq. (2) and its coefficients optimized in an iterative least-squares procedure. Some
Figure 2: Portions of the FIR (upper panel) and MIR (lower panel) spectra of $d$-cyanoacetylene (black traces). A simulation spectrum of the most intense bands is also reported for both DC$_3$N (red) and HC$_3$N (grey). Lines belonging to CO and various H$_2$O isotopologues were removed from the spectra.
Table 3: Summary of the rotational data used in the analysis.

| State     | \(|k|\) | \(J\) range (GHz) | Freq. range (kHz) | No. of lines | rms (kHz) | Reference          |
|-----------|--------|--------------------|-------------------|--------------|-----------|--------------------|
| Ground state | 0      | 3-126              | 33-1069           | 52           | 13.2      | TW, Ma78, Pl88, Sp08 |
| \(v_7 = 1\) | 1\(_{e,f}\) | 5-105              | 50-896            | 67           | 10.9      | TW, Ma78, Pl88, Sp08 |
| \(v_6 = 1\) | 1\(_{e,f}\) | 7-44               | 67-381            | 42           | 17.0      | TW, Pl88           |
| \(v_5 = 1\) | 1\(_{e,f}\) | 7-44               | 67-381            | 42           | 13.7      | TW, Pl88           |
| \(v_4 = 1\) | 0      | 7-51               | 67-439            | 32           | 23.6      | TW, Pl88           |
| \(v_7 = 2\) | 0, 2\(_{e,f}\) | 7-44               | 67-383            | 61           | 24.0      | TW, Ma78, Pl88     |
| \(v_7 = 3\) | (1, 3)\(_{e,f}\) | 7-44               | 68-384            | 77           | 20.0      | TW, Ma78, Pl88     |
| \(v_7 = 4\) | 0, (2, 4)\(_{e,f}\) | 7-48               | 68-419            | 85           | 19.8      | TW, Pl88           |
| \(v_6 = 2\) | 0, 2\(_{e,f}\) | 7-44               | 67-382            | 54           | 44.7      | TW, Pl88           |
| \(v_6 = v_7 = 1\) | (0, 2)\(_{e,f}\) | 7-44               | 67-382            | 93           | 30.8      | TW, Ma78, Pl88     |
| \(v_5 = v_7 = 1\) | (0, 2)\(_{e,f}\) | 7-44               | 67-382            | 78           | 20.8      | TW, Pl88           |
| \(v_5 = v_6 = 1\) | 9-44               | 84-381            | 63           | 14.6      | TW          |
| \(v_6 = 1, v_7 = 2\) | (±1,3)\(_{e,f}\) | 7-46               | 68-400            | 95           | 21.9      | TW, Pl88           |
| \(v_5 = 1, v_7 = 2\) | (±1,3)\(_{e,f}\) | 9-44               | 85-383            | 97           | 17.4      | TW          |
| interstate\(^a\) | 44-49               | 364-429            | 10           | 19.7      | TW          |

Abbreviations are used as follow: TW This work, Ma78 Mallinson & De Zafra (1978) [17]. Pl88 Plummer et al. (1988) [18], Sp08 Spahn et al. (2008) [19]. [a] Transitions between the interacting states (1000) and (0004).

Table 4: Spectroscopic constants derived for DC\(_3\)N in the ground and \(v_4 = 1\) states.

| Constant | Unit     | Ground state | \(v_4 = 1\) |
|----------|----------|--------------|--------------|
| \(G_v\)  | cm\(^{-1}\) | 0.0          | 867.594(75)  |
| \(B_v\)  | MHz      | 4221.580853(37) | 4212.271(16) |
| \(D_v\)  | kHz      | 0.4517857(89)  | 0.45312(11)  |
| \(H_v\)  | mHz      | 0.03949(78)    | 0.03949\(^a\) |
| \(L_v\)  | nHz      | −0.154(23)     | −0.154\(^a\) |

Number in parenthesis are one standard deviation in units of the last quoted digit. [a] Kept fixed to ground state value.

spectroscopic parameters could not be determined from the available experimental data. In these cases, the constant of a given vibrational level were derived from the corresponding optimized values obtained for other levels belonging to the same vibrational manifold considering, whenever feasible, a vibrational dependence. In other cases, they were simply fixed to zero. The spectroscopic parameters obtained from the combined fit procedure are collected in Tables 4-7.

As anticipated, the analysis of DC\(_3\)N follows the approach successfully adopted for HC\(_3\)N [38]. The main difference is the set-up of the anharmonic resonances network, which arises from the different energy of some vibrational levels due to the isotopic substitution. In particular, the \(v_5\) vibrational energy, 663.36848(3) cm\(^{-1}\) in HC\(_3\)N, drops to 522.26378(2) cm\(^{-1}\) in DC\(_3\)N. For HC\(_3\)N, two resonant systems were described: (i) \(v_5 = 1 \sim v_7 = 3\) and ii) \(v_4 = 1 \sim v_5 = v_7 = 1 \sim v_6 = 2 \sim v_7 = 4\). Of the two systems, the former is not present in
Figure 3: A 2 GHz broad scan of the $J = 13 \leftarrow 12$ rotational transition of DC$_3$N around 110 GHz. The spectrum was recorded at room temperature, with DC$_3$N at a pressure of 0.05 Pa, RC= 3 ms, frequency step 50 kHz, FM = 120 kHz, scan speed = 0.4 MHz/s, 2 scans. The arbitrary units of the y-axis are set so that the intensity of the ground state (GS) transition, out of scale in the figure, is 1.

Table 5: Spectroscopic constants derived for DC$_3$N in singly-excited bending states.

| Constant | Unit       | $v_7 = 1$                  | $v_6 = 1$                  | $v_5 = 1$                  |
|----------|------------|---------------------------|---------------------------|---------------------------|
| $G_v$    | cm$^{-1}$  | 211.5502859(33)           | 492.7605681(48)           | 522.2639331(49)           |
| $X_{L_{(tt)}}$ | GHz       | 19.5125$^a$               | 56.39$^a$                 | ...                       |
| $B_v$    | MHz        | 4234.519466(31)           | 4229.25208(11)            | 4225.635835(71)           |
| $D_v$    | kHz        | 0.4718865(60)             | 0.462123(45)              | 0.452490(14)              |
| $H_v$    | mHz        | 0.08240(30)               | 0.0637(45)                | 0.03949$^b$               |
| $L_v$    | nHz        | $-0.154^b$                | $-0.154^b$                | $-0.154^b$                |
| $d_{JL_{(tt)}}$ | kHz   | $-9.971^a$                | 141.5$^a$                 | ...                       |
| $q_{tt}$ | MHz        | 5.907823(56)              | 3.15995(11)               | 2.68903(13)               |
| $q_{JJ}$ | Hz         | $-13.646(11)$             | $-1.572(22)$              | $-1.627(27)$              |
| $q_{JJ}$ | µHz        | 43.37(57)                 | ...                       | ...                       |

Number in parenthesis are one standard deviation in units of the last quoted digit. $^a$ Constrained value, see text. $^b$ Kept fixed to ground state value.

DC$_3$N while the latter is almost the same, except for $v_5 = v_7 = 1$, replaced by $v_5 = v_6 = 1$. The treatment of such perturbations led to the determination of the corresponding interaction parameters, $C_{30}$ for the cubic terms, $(v_4 = 1)-(v_6 = 2)$ and $(v_4 = 1)-(v_5 = v_6 = 1)$, and $C_{50}$ for the quintic term $(v_4 = 1)-(v_7 = 4)$. Moreover, a centrifugal distortion parameter $C_{J50}$ was included in the analysis.

For the states involved in this resonance system, many experimental data are available. In the MIR
Table 6: Spectroscopic constants derived for DC$_3$N in overtone states.

| Constant | Unit  | $v_7 = 2$ | $v_7 = 3$ | $v_7 = 4$ | $v_6 = 2$ |
|----------|-------|--------|--------|--------|--------|
| $G_v$    | cm$^{-1}$ | 422.375358(61) | 632.510162(64) | 841.9860892(95) | 983.021(78) |
| $X_{L_{(v_7)}}$ | GHz | 19.354043(62) | 19.1988(19) | 19.03874(52) | 56.39(58) |
| $y_{L_{(v_7)}}$ | MHz | ... | ... | 1.82(12) | ... |
| $B_v$ | MHz | 4247.45224(11) | 4260.38118(15) | 4273.30576(21) | 4236.558(16) |
| $D_v$ | kHz | 0.491827(21) | 0.512469(34) | 0.53448(11) | 0.471993(61) |
| $H_v$ | mHz | 0.03949$^b$ | 0.03949$^b$ | 0.176(21) | 0.03949$^b$ |
| $L_v$ | nHz | $-0.154^b$ | $-0.154^b$ | $-0.154^b$ | $-0.154^b$ |
| $d_{L_{(v_7)}}$ | kHz | $-10.426(30)$ | $-10.947(24)$ | $-11.368(21)$ | 141.6(39) |
| $h_{L_{(v_7)}}$ | Hz | ... | ... | $-0.0552(64)$ | ... |
| $q_v$ | MHz | 5.93258(10) | 5.95888(12) | 5.98281(15) | 3.15095$^a$ |
| $q_{L}$ | Hz | $-13.897^a$ | $-14.149(36)$ | $-14.288(46)$ | $-1.571^a$ |
| $q_{L,1}$ | μHz | 43.37$^a$ | 43.37$^a$ | 43.37$^a$ | ... |

Number in parenthesis are one standard deviation in units of the last quoted digit. [$a$] Constrained value, see text. [$b$] Kept fixed to ground state value.

region, we recorded the $\nu_4$, $\nu_5 + \nu_6$, and $2\nu_6$ bands that provide the energy position for most of the interacting levels. The energy of the $v_7 = 4$ was determined through the FIR spectrum, where the $4\nu_7 \leftrightarrow 3\nu_7$ hot-band and the $4\nu_7 \leftrightarrow \nu_6$ band were detected. A large pure rotational data-set is also available for the polyad of interacting states. Besides several rotational transitions observed within the vibrational states, a small set of interstate transitions between the (1000) and (0004) states were identified. The coefficients $C_{mn}$ of the resonance Hamiltonian are given in Table C.

5. Conclusions

In this work, a large set of high-resolution rotational and ro-vibrational data of DC$_3$N has been recorded and analyzed in order to achieve a detailed knowledge of all the vibrational states approximately below 1000 cm$^{-1}$ of energy. To reach this goal, infrared spectra of DC$_3$N have been recorded in the range 150–1600 cm$^{-1}$ at high resolution (0.001–0.004 cm$^{-1}$). In this region, 27 fundamental, overtone, combination, and hot-bands have been observed and analyzed. Notably, the very weak $\nu_4$ fundamental has also been detected, even though at lower resolution (0.012 cm$^{-1}$). Also, pure rotational transitions for 14 states have been recorded to extend the investigation of the spectrum to the submillimeter-wave region up to ca. 500 GHz.

Almost 6700 experimental transitions were included in a least-squares fit procedure thanks to which a large number of rotational and ro-vibrational spectroscopic parameters have been determined for 14 different vibrational states. The whole set of data has been fitted with an overall weighted standard deviation $\sigma$ of 0.95, meaning that on average all data are well-reproduced within their given uncertainties. The vibrational energies were determined experimentally for all the investigated states, without any assumption. The combination of both high-resolution ro-vibrational data and pure rotational measurements allowed an accurate modeling of the spectrum of DC$_3$N, including perturbations produced by the observed anharmonic resonances. The interaction between the (1000) and (0110) states has been introduced for the first time, with the effect to eliminate the residual discrepancies described in Refs. [18, 25].

The present work shows once again the success of a combined analysis of data from different spectral regions, like infrared and millimeter-wave fields. The results are generally more coherent and fewer assumptions are needed, if not any. Also, a more extended set of spectroscopic parameters can be obtained with reliability.
| Table 7: Spectroscopic constants derived for DCN in combination states. |
|---------------------------------------------------------------|
| Constant Unit | H | b | c | a |
|----------------|---|---|---|---|
| **(ab)J** | 3.37(98) | 3.14(93) | 1.54(93) | 3.37(98) |
| **(bb)J** | 2.94(92) | 2.90(92) | 1.15(92) | 2.94(92) |
| **(cc)J** | 0.65(78) | 0.61(78) | 0.22(78) | 0.65(78) |
| **(dd)J** | 0.05(46) | 0.03(46) | 0.00(46) | 0.05(46) |

Number in parenthesis are one standard deviation in units of the last quoted digit. See text.
Table 8: Resonance parameters.

| Interacting states | Parameter | Unit | Value |
|--------------------|-----------|------|-------|
| \((v_4 = 1) - (v_6 = 2)\) | \(C_{30}\) | cm\(^{-1}\) | 17.422(33) |
| \((v_4 = 1) - (v_5 = v_6 = 1)\) | \(C_{30}\) | cm\(^{-1}\) | -6.527(13) |
| \((v_4 = 1) - (v_7 = 4)\) | \(C_{50}\) | GHz | 2.70065(76) |
| | \(C_{J}\) | kHz | 9.807(35) |

Number in parenthesis are one standard deviation in units of the last quoted digit.

This study provides an extensive line catalog (deposited as Supplementary Material) which can be used to assist future astronomical observations of DC\(_3\)N and is suitable for modeling both cold and hot regions of the interstellar medium.

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