Using Artificial Intelligence and Novel Polynomials to Predict Subjective Refraction

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This work aimed to use artificial intelligence to predict subjective refraction from wavefront aberrometry data processed with a novel polynomial decomposition basis. Subjective refraction was converted to power vectors (M, J0, J45). Three gradient boosted trees (XGBoost) algorithms were trained to predict each power vector using data from 3729 eyes. The model was validated by predicting subjective refraction power vectors of 350 other eyes, unknown to the model. The machine learning models were significantly better than the paraxial matching method for producing a spectacle correction, resulting in a mean absolute error of 0.301 ± 0.252 Diopters (D) for the M vector, 0.120 ± 0.094 D for the J0 vector and 0.094 ± 0.084 D for the J45 vector. Our results suggest that subjective refraction can be accurately and precisely predicted from novel polynomial wavefront data using machine learning algorithms. We anticipate that the combination of machine learning and aberrometry based on this novel wavefront decomposition basis will aid the development of refined algorithms which could become a new gold standard to predict refraction objectively.

Globally it is estimated that 153 million people aged 5 or above are visually impaired due to uncorrected refractive errors1. The ability to automatically refract a patient and provide a spectacle prescription, equivalent to the time consuming current gold standard of subjective refraction, is an elusive goal that has intrigued many ophthalmic clinicians and researchers2–4.

One such automated and objective method is optical wavefront sensing using aberrometry which allows mathematical reconstruction and analysis of lower and higher order monochromatic aberrations of the eye. This has led many to believe that this objective method had the potential to be the new standard for optimizing correction of refractive errors by converting aberrometry data to accurate sphero-cylindrical refractions5–7. Though several small sample studies showed promising results in terms of accuracy and precision of objective refraction from several methods related to wavefront analysis to date5–13 no study has found a validated method that can be used to prescribe a spectacle correction. It was found that results from the aberrometer, autorefractor and subjective refraction, though comparable with each other, were not accurate enough to prescribe spectacles directly from either instruments14. A recent publication found that a visual image quality metric could predict subjective refraction in myopic eyes but not habitually undercorrected hyperopic eyes, though the data set was again small15. Variability in the gold standard subjective refraction measurements themselves were also thought to be a source of poor precision1.

The ocular wavefront error is most commonly described by the Zernike polynomials16. To satisfy orthogonality constraints with low order modes, some higher order Zernike polynomials contain low order terms in their analytical expression leading to lack of accuracy when predicting the sphero-cylindrical refraction17. It is known that conventional therapies such as spectacles or contact lenses correct just the lower-order aberrations but the presence of higher-order aberrations influences the prescription itself12. An important finding by Cheng et al.6 showed that subjective judgment of best focus does not minimize RMS wavefront error (Zernike defocus = 0), nor create paraxial focus (Seidel defocus = 0), but makes the retina conjugate to a plane between these two. The levels of spherical aberration (Z4°) and secondary astigmatism (Z4 ± 2) influenced the levels of defocus and primary astigmatism that produced the best visual performance. These objective metrics were tested based on an assumption that the Zernike polynomial decomposition was producing a clear distinction between the low and high order components of the wavefront error. This assumption could explain the poor correlation between subjective and objective refraction, especially when it came to large amounts of higher order aberration5–7,9,11,12,18,19.

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A new series of polynomials, labeled LD/HD (Low Degree/High Degree), have been proposed to provide a more mathematically relevant separation of the higher and lower modes\(^{20}\). In this decomposition, the normalized higher order modes are devoid of low order terms and mutually orthogonal within but not with lower order aberrations. With this approach, the low order wavefront component is equal to the paraxial curvature matching of the wavefront map.

Machine learning is already in use in Ophthalmology for image analysis in medical retina\(^{21–23}\), and glaucoma (Visual Fields and Disc Photos)\(^{24,25}\) as well as recent developments for use in diagnoses including retinopathy of prematurity\(^{26}\). It is also used in regression tasks, notably in IOL calculations\(^{27}\). Deep learning has been applied to predict refractive error from fundus images and other image analysis techniques also\(^{28,29}\). Attempts to predict subjective refraction from Zernike polynomials have also been tried using a multilayer perceptron with two hidden layers\(^{30}\).

Our aim was to build and evaluate a set of predictive machine learning models to accurately and precisely objectively refract a patient using wavefront aberrometry with LD/HD polynomial decomposition, and to evaluate the relative importance of each polynomial in the prediction process for each vector.

**Results**

**Group comparability.** Patients demographics are presented in Table 1. Training set and test set were comparable in terms of patient ages, sex-ratio, side repartition, mean refractive spherical equivalent and mean refractive cylinder.

**Prediction performance of the different methods.** The performance of prediction methods are presented in Table 2. Figure 1 illustrates the prediction performances of the different approaches for the M vector and Fig. 2 illustrates those for the J0 and J45 vectors. Statistical testing for differences between the various prediction methods is presented in Table 3. The XGBoost models using all the polynomials, resulted in a Mean Absolute Error of 0.30 ± 0.25 Diopters (D) for the M vector, 0.12 ± 0.09 D for the J0 vector and 0.09 ± 0.08 D for the J45 vector, whilst the Paraxial matching method resulted in a Mean Absolute Error of 0.40 ± 0.35 D for the M vector, 0.17 ± 0.14 D for the J0 vector and 0.14 ± 0.10 D for the J45 vector. The XGBoost models using only the low-degree polynomials resulted in a Mean Absolute Error of 0.35 ± 0.29 D for the M vector, 0.16 ± 0.14 D for the J0 vector and 0.12 ± 0.10 D for the J45 vector. Bland–Altman plots showed a good agreement between subjective refraction and the predictions obtained with the machine learning models, with no systematic error depending on degree of refractive error (Fig. 4). Paired t-test were not significant.

| Training set | Test set | p value |
|--------------|----------|---------|
| n eyes       | 3729     | 350     | —       |
| n patients   | 1809     | 193     | —       |
| Female %     | 57.1%    | 58.9%   | 0.71    |
| Right Eye %  | 49.7%    | 49.4%   | 1.00    |

| Mean | SD  | Min. | Max. | Mean | SD  | Min. | Max. |
|------|-----|------|------|------|-----|------|------|
| Age  | 36.03 | 11.24 | 18.10 | 72.40 | 36.35 | 11.48 | 20.00 |
| Refractive SE | -1.89 | 2.54 | -6.75 | 6.13 | -1.96 | 2.58 | -6.63 |
| Refractive Cyl | -0.81 | 0.90 | -6.00 | 0.00 | -0.87 | 0.94 | -5.25 |

**Table 1.** Patients demographics in the training set and test set. T-test was performed to test for group comparability. Abbreviations used: Spherical Equivalent (SE), Cylinder (Cyl) and number (n). SE and Cyl are in Diopters (D).

| Prediction Method | Absolute Prediction Error | Prediction Error (Accuracy) | Precision |
|-------------------|---------------------------|-----------------------------|-----------|
|                  | Mean | SD  | Min. | Max. | Mean | SD  | Min. | Max. | Mean | SD  | Min. | Max. |
| PM - M           | 0.40 | 0.35 | 0.00 | 1.66 | 0.06 | 0.53 | -1.66 | 1.66 | 1.06 |
| XGB (LO only) - M| 0.35 | 0.29 | 0.00 | 1.50 | -0.02 | 0.46 | -1.43 | 1.50 | 0.91 |
| XGB (LO/HO) - M  | 0.30 | 0.25 | 0.00 | 1.41 | 0.01 | 0.39 | -1.14 | 1.41 | 0.78 |
| PM - J0          | 0.17 | 0.14 | 0.00 | 0.69 | -0.05 | 0.22 | -0.69 | 0.66 | 0.44 |
| XGB (LO only) - J0| 0.16 | 0.14 | 0.00 | 0.74 | 0.00 | 0.22 | -0.74 | 0.71 | 0.43 |
| XGB (LO/HO) - J0 | 0.12 | 0.09 | 0.00 | 0.44 | -0.01 | 0.15 | -0.44 | 0.43 | 0.30 |
| PM - J45         | 0.14 | 0.10 | 0.00 | 0.55 | 0.02 | 0.17 | -0.55 | 0.45 | 0.34 |
| XGB (LO only) - J45| 0.12 | 0.10 | 0.00 | 0.61 | 0.01 | 0.15 | -0.61 | 0.59 | 0.31 |
| XGB (LO/HO) - J45| 0.09 | 0.08 | 0.00 | 0.49 | 0.00 | 0.13 | -0.49 | 0.43 | 0.25 |

**Table 2.** Absolute Prediction Error, Prediction Error and Precision of the three methods were evaluated (Paraxial Matching, XGBoost using Low order polynomials only, XGBoost using all available polynomials) for each vector M, J0 and J45. P values for the comparison between methods are presented in Table 3. Abbreviations used: Low Order (LO), Low and High Order (LO/HO) and Paraxial Matching (PM).
**Pairwise prediction methods comparison.** The XGBoost models using all the polynomials performed statistically better than Paraxial matching for every vector and every metric, except for accuracy for the J45 vector prediction. They also performed better than the XGBoost models trained with low-degree polynomials only, although the difference was not significant for precision in predicting the M vector and accuracy in predicting the J0 and J45 vectors.

**Feature importance.** SHAP value analysis for the three XGBoost models trained with the full set of polynomials is presented in Fig. 4. It showed that $G_{2,0}^s$ (defocus) was by far the most influential feature to predict the M vector, with $G_{4,0}^s$ (primary spherical aberration) being the second most important feature. The bottom two graphs demonstrate that $G_{2,2}^s$ (Vertical astigmatism) and $G_{4,-2}^s$ (Oblique secondary astigmatism) were the most important features to predict the J0 vector, while $G_{2,-2}^s$ (Oblique astigmatism) and $G_{1,2}^s$ (Vertical secondary astigmatism) were the most important features to predict the J45 vector.
The machine learning approach using LD/HD polynomials was more effective than the paraxial matching method for predicting the results of conventional, sphero-cylindrical refraction from wavefront aberrations used by Thibos et al. previously. Interestingly, the XGBoost models trained using low-order aberrations only proved more accurate than paraxial matching. This could suggest that those low-order polynomials interact, in some circumstances, in a more complex way than previously thought. The best precision and accuracy were obtained when all the novel polynomials coefficients were used as predictors, demonstrating the significant influence of the higher order aberrations on the spectacle correction.

Gradient boosting creates new models that predict the residual errors of prior models during the training process. The models are used together to predict the target value. XGBoost is an implementation of gradient boosted trees focused on performance and computer efficiency. It can perform both regression and classification tasks. It was chosen because of its recognized performances and its resistance to overfitting.

Feature importance \( G_2^a \) (defocus) was unsurprisingly the most influential feature to predict the M vector, with \( G_4^a \) (primary spherical aberration) being the second most important feature. One interesting finding was that \( G_{4}^{-2} \) (Oblique secondary astigmatism) was the second most important feature to predict J0, and \( G_4^z \) (Vertical secondary astigmatism) the second most important feature to predict J45, while the inverse would be more intuitive. This demonstrates the interest in the machine learning approach, that allows us to discover new patterns and relationships between predictors by disregarding previous assumptions.

Our results confirm the prevalence of 4th order aberrations within the higher order coefficients influencing the sphero-cylindrical refraction as it has been previously shown. The LD/HD modes being devoid of defocus terms (radial degree 2), they unambiguously confirm the influence of the radial degree 4 of the wavefront error, on sphero-cylindrical refraction.

The predictive influence of the variables used in the model does not explain their exact role, and that is a weakness of such machine learning algorithms, as interpretability and model comprehension are limited by the big number of decision trees, their complexity and depth.

Of note, we did not test our method for repeatability. However, it relies solely on the OPD-Scan III output, and this device has already shown very good repeatability.

### Discussion

### Methods

**Patients and dataset constitution.** This study was approved by the Institutional Review Board at Rothschild foundation and followed the tenets of the Declaration of Helsinki. Informed consent was obtained from all participants. A total of 2890 electronic medical records of patients (6397 eyes) evaluated for refractive surgery at the Laser Vision Institute Noémie de Rothschild (Foundation Adolphe de Rothschild Hospital, Paris) were retrieved and consenting patients data was analyzed. We excluded patients with strabismus and any other ocular abnormalities except ametropia. After data cleaning, eyes with subjective refraction and a valid wavefront aberrometry examination were randomly split into a 350 eyes test set and a training set, with no cross over of
same patient data. A manual review of medical records of eyes in the test set was checked to ensure the quality of data, leaving 3729 eyes for the training set.

**Aberrometry.** Wavefront analysis was obtained using the OPD-Scan III (Nidek, Gamagori, Japan). The aberrometer was specially configured to run using beta-software incorporating the new series of LD/HD aberrations.
polynomials, noted $G_{nm}$ using the same double index scheme of the Zernike polynomials. The wavefronts were decomposed up to the 6th order. We chose to stop our polynomials analysis at the 6th order. This cut-off is beyond the number of polynomials that was determined by the members of the Vision Science and its Applications Standards task force (VSIA) to be necessary to describe the HOA of the human eye with sufficient accuracy in 200036. It applied to the paraxial matching analysis as well as the machine learning approach. The first three polynomials (Piston, Tilt, Tip) were removed from the features because of their low relevance in this work. Defocus, Vertical Astigmatism and Oblique Astigmatism constituted the Low order polynomial group, and all the others constituted the High order polynomials group. A 4 mm pupil disk diameter was chosen to obtain the coefficients and any pupil less than 4 mm during the acquisition of the wavefront with the OPD-Scan III, was an exclusion criterion. A 4 mm pupil diameter analysis cut-off was used because it is close to the mean physiological photopic pupil diameter in different studies37–39. Our results may not reflect the results that could be found using very large or very small pupils.

**Subjective refraction.** Corresponding non-cycloplegic subjective refractions conducted on the same day by an experienced optometrist were analyzed. The maximum plus rule was used to the nearest 0.25 D to minimize accommodation and maximize the depth of focus7.

**Power vector analysis.** Each refraction in Sphere $S$, Cylinder $C$, and axis $A$ format was transformed into 3D dioptric vector space ($M$, $J_0$, $J_{45}$) where the three components are orthogonal. Refraction data sets were vectorized using standard power vector analysis with the components $M$, $J_0$ and $J_{45}$ using Eqs. (1), (2) and (3).

$$M = S + \frac{C}{2}$$

(1)

$$J_0 = -\frac{C}{2} \times \cos(2\alpha)$$

(2)

$$J_{45} = -\frac{C}{2} \times \sin(2\alpha)$$

(3)

**Machine learning methodology.** Three machine learning models were separately trained to predict each vector component from the new series of polynomials. We used a Gradient Boosted Trees algorithm (XGBoost)41. Parameter tuning was performed using 5-folds randomized search cross-validation. Mean squared error

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**Figure 4.** Bland-Altman diagrams showing the agreement between the predictions made using the XGBoost model trained with all available aberrations, and subjective refraction, for $M$ (a), $J_0$ (b) and $J_{45}$ (c). No statistical difference was found using one sample t-test, for each vector prediction.
A p-value less than 0.05 was considered significant. We conducted a study to assess the agreement between subjective refraction and machine learning model predictions. A correlation analysis was performed to correlate subjective refraction with wave aberration metrics. The datasets generated during and analyzed during the current study are available from the corresponding author on reasonable request.

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Data availability

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Author contributions
R.R and G.D. are joint first authors. R.R. and G.D. completed data analysis, wrote the main manuscript text, prepared the tables and figures. D.G. and J.M. designed the study and developed the polynomial basis. All authors reviewed the manuscript.

Competing interests
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