Evaluation of Translation Velocity Control by Auxiliary Coils for the Collisional Merging Formation of FRCs by 2-D Resistive MHD Simulation

Daichi KOBAYASHI, Tomohiko ASAI, Tsutomu TAKAHASHI, Junichi SEKIGUCHI, Hiroshi GOTA1), Sean DETTRICK1), Yung MOK1), Michl BINDERBAUER1) and Toshiki TAJIMA1,2)

College of Science and Technology, Nihon University, Tokyo 101-8308, Japan
1)TAE Technologies, Inc., Foothill Ranch, CA 92610, USA
2)Department of Physics and Astronomy, University of California at Irvine, Irvine, CA 92697, USA
(Received 29 November 2019 / Accepted 20 February 2020)

Previously, the collisional merging formation of FRCs has been developed to generate high performance FRCs. A drastic increase in the excluded flux and total temperature were observed in the FRCs generated with this technique; furthermore, these phenomena strongly depend on the translation velocity of individual plasmoids. However, the dependence of the merged-FRC performance on the translation velocity has not been studied in detail. To study the dependence, the effect of installed auxiliary coils on the formation region on the translation velocity of FRCs in the FAT-CM device has been evaluated by the simulation with a two-dimensional resistive magnetohydrodynamics code, which is called Lamy Ridge. The control of translation velocity by using the auxiliary coils has been demonstrated on the order of several tens of km/s in the simulation. The trapped poloidal flux and the total temperature of simulated FRCs have increased depending on the translation velocity.

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Keywords: magnetically confined plasma, field-reversed configuration, high beta plasma, FRC merging, resistive MHD simulation
DOI: 10.1585/pfr.15.2402020

1. Introduction

A field-reversed configuration (FRC) is a compact torus that has poloidal field and zero or small amount of self-generated toroidal field [1, 2]. FRC has an extremely high beta value (\(\langle \beta \rangle \sim 1\)) that makes the potential for using aneutronic fusion fuels such as D–3He and p–11B [3].

Recently, the technique of collisional merging formation of FRCs has been developed to generate high performance FRCs [4]. Two initial-FRCs formed by the field-reversed theta pinch (FRTP) method, which is a conventional technique to form an FRC are translated at super Alfvénic velocity toward each other so that they collide and merge into a single FRC state. In the collisional merging process, a drastic increase in the excluded flux and the total temperature of merged-FRCs was observed on the FAT-CM device and the C-2/C-2U device [4, 5]. These phenomena strongly depend on the translation velocity of individual plasmoids [6]. However, the dependence of the merged-FRC performance, such as the excluded flux and the total temperature, on the translation velocity has not been studied in detail. To study the dependence, a method for controlling the translation velocity of initial-FRCs that utilizes the auxiliary coils has been proposed and evaluated by the two-dimensional resistive magnetohydrodynamics (MHD) simulation.

2. FAT-CM Device

Figure 1 shows the schematic diagram of the FAT-CM device and the axial profile of the external guide magnetic field. This device consists of a central confinement chamber, quasi-steady state confinement coils, and two FRTP formation sections, called “R-formation” and “V-formation,” respectively. Each formation section consists of a transparent quartz tube (0.25 m in ID) and theta-pinch coils. The central confinement chamber is made of stainless steel (0.78 m in ID) and serves as a flux conservor during translation, collision, and merging processes because the skin time (\(\sim 0.5\ ms\)) is much longer than their timescale. In the typical FAT-CM device operation, theta pinch coils generate the main compression magnetic field of \(\sim 0.4\ T\) and quasi-steady state confinement coils generate the external magnetic field of \(\sim 0.06\ T\). Initial-FRCs, which are generated in each formation, \(\sim 0.06\ m\) radius and \(\sim 1\ m\) length, have \(\sim 2.5 \times 10^{21}\ m^{-3}\) of electron density and \(\sim 200\ eV\) of total temperature. Initial-FRCs are translated due to the gradient of the external guide magnetic field into the central confinement chamber. The translation veloc-
ity is 150 - 200 km/s, which is faster than the Alfvénic velocity (∼70 km/s) calculated with the typical electron density of merged-FRCs and the external magnetic field at the midplane of the FAT-CM device (∼0.06 T). Merged-FRCs, ~0.2 m radius and ~1.6 m length with 0.5 - 1.0 mWb of estimated trapped poloidal flux, have ~1.5 × 10^{20} m^{-3} of electron density and 100 eV of total temperature.

3. Model Equations

Lamy Ridge is a two-dimensional MHD code, which has been developed to simulate the entire process of formation, translation, and collisional merging of FRCs in the C-2 device [7, 8]. The simulation of merged-FRCs in the FAT-CM device with the Lamy Ridge code also appeared in a previous study [9]. The code consists of the resistive MHD equations supplemented with an energy equation, and neutral fluid equations. The equations for plasma and neutrals interactively exchange their momentum, density, and energy through ionization. The energy equation incorporates non-adiabatic effects, including thermal conduction, ionization loss, and radiation loss. In the code, plasma is described by

\[
\frac{\partial n}{\partial t} + \nabla \cdot nu = m_n(\sigma_{\text{ion}}v), \tag{1}
\]

\[
MnD_\theta = J \times B - \nabla P + \nabla \cdot \gamma \nabla u
- M_n\varepsilon(n(u - u_n)) - m_n(\sigma_{\text{ion}}v)u, \tag{2}
\]

\[
\frac{\partial w}{\partial t} + \nabla \cdot \left( \frac{\gamma P}{\gamma - 1} + \frac{Mn^2u^2}{2} \right) u
= u \cdot J \times B + nk_B\left(\frac{\partial T_i}{\partial t} + \frac{\partial T_e}{\partial t}\right), \tag{3}
\]

\[
nk_B\frac{\partial T_i}{\partial t} = v_{ei}nk_B(T_e - T_i) + \nabla \cdot \chi_i\nabla T_i,
+ \eta_{i}\mathbf{j}^2 - R - I. \tag{4}
\]

In addition, neutrals are described by

\[
\frac{\partial n_n}{\partial t} + \nabla \cdot n_n u_n = -m_n(\sigma_{\text{ion}}v), \tag{6}
\]

\[
Mn_n\frac{Du_n}{Dt} = -nk_B\nabla(T_nv_n) + \nabla \cdot \gamma \nabla u_n
- M_n\varepsilon(n(u - u_n)) + m_n(\sigma_{\text{ion}}v)u_n, \tag{7}
\]

\[
\frac{\partial w_n}{\partial t} + \nabla \cdot \left( \frac{\gamma P_n}{\gamma - 1} + \frac{Mn_nu_n^2}{2} \right) u_n = \nabla \cdot \chi_n\nabla T_n. \tag{8}
\]

Here, \(n\) is the density, \(u\) is the flow velocity, \((\sigma_{\text{ion}}v)\) is the ionization reaction rate, \(\nu\) is the viscosity, \(M\) is the ion mass, \(J\) is the current density in the toroidal direction, \(B\) is the magnetic flux density, \(P\) is the plasma pressure, \(\gamma\) is the specific heat ratio, \(T\) is temperature, \(\nu_{eq}\) is the reciprocal of the energy equilibration time, \(\chi\) is the thermal conductivity, and \(R\) and \(I\) are the radiative energy loss and ionization loss, respectively. Subscripts “i,” “e,” and “n” indicate ion, electron, and neutrals, respectively. The total of internal and kinetic energy density is defined as

\[
w \equiv \frac{P}{(\gamma - 1)} + \frac{Mn^2}{2}. \tag{9}
\]

Resistivity includes Spitzer resistivity \(\eta_S\), Chodura resistivity, and numerical resistivity by diffusivity \(D_\theta\),

\[
\eta = \eta_SD_S + \mu_0D_\eta + C_C \left(1 - \exp \left[-\frac{V_D}{fC V_f}\right]\right) m_e \sqrt{\frac{Mn}{e Ms}}. \tag{10}
\]

Here, \(\epsilon_0\) and \(\mu_0\) are the permittivity and magnetic permeability of free space, and \(V_D\) and \(V_f\) are the drift velocity and ion acoustic velocity, respectively. The viscosity, \(D_S\), \(C_C\), \(fC\), and \(D_\eta\) are adjustable values. In addition, magnetic field is described by

\[
B = \nabla \Psi \times \nabla 0, \tag{11}
\]

\[
\frac{\partial \hat{B}}{\partial t} = r(\mathbf{u} + \mathbf{B})_0 + \frac{\eta}{\mu_0} \Delta \Psi, \tag{12}
\]

\[
\mathbf{J} = -\frac{\Delta \Psi}{\mu_0 r} \hat{\mathbf{\theta}}, \tag{13}
\]

where \(\Psi\) is the poloidal flux per radian, and \(\hat{\mathbf{\theta}}\) is the unit vector in the toroidal direction. The code advances equations in time by using a semi-implicit algorithm to take large time steps.

The simulation result under the typical condition of FAT-CM experiments is shown in Fig. 2. The entire process of collisional merging formation of FRCs has been simulated, also the performance of simulated merged-FRCs was approximately consistent with that of experimental FRCs (Fig. 3).
Fig. 2 Contour maps of plasma temperature computed by Lamy Ridge under the typical conditions of FAT-CM experiments.

Fig. 3 Time evolution of excluded flux radius, averaged electron density, total temperature, and the trapped poloidal flux assuming the rigid-rotor equilibrium model [2].

Fig. 4 Contour plot of the magnetic flux in “V-formation” during the acceleration of FRCs with auxiliary coils. Solid and dashed lines indicate positive and negative sections, respectively. The dashed bold line indicates the separatrix. (a) Shows the formed initial-FRC; (b) and (c) show FRC accelerated by an auxiliary coil.

Fig. 5 Waveform of the current on auxiliary coils in the case of the maximum translation velocity presented in this paper (case 4).

4. Auxiliary Coil

The auxiliary coil was developed to control the translation of FRCs formed by the FRTP method [10]. In the previous study, a set of the auxiliary coils was used to separate an FRC into two parts; in addition, the ejection timing of each FRC was controlled by the gradient of the magnetic field changed by auxiliary coils.

The auxiliary coil is a set of one turn coils (20 mm width, 3 mm thickness, 320 mm OD) that are installed on each formation. The contour plot of the magnetic flux function in “V-formation” during the acceleration of FRCs with auxiliary coils is shown in Fig. 4. Also, Fig. 5 shows the typical waveform of current on auxiliary coils in the simulation. These coils are used to change the profile of the external guide magnetic field. In the operation for acceleration, the current is triggered when FRCs are under the auxiliary coils, which increases the gradient of the external guide magnetic field (Figs. 4(b), (c)). Then, FRCs are accelerated more than in the operation without auxiliary coils.
Fig. 6 Dependence of the total temperature and trapped poloidal flux on the maximum velocity during the translation.

Fig. 7 Time evolution of internal, kinetic, and total energy of FRCs.

5. Simulation Results

Here, four cases are presented. In case 1, auxiliary coils are not used. In case 2, the coils on the downstream side, also in case 3, and the coils on the upstream side are used. In case 4, the coils on both sides are used.

The dependence of the total temperature, which is volume-averaged in separatrix, and the trapped poloidal flux at the time when the kinetic energy of FRCs became zero (i.e., after merging) on the translation velocity is shown in Fig. 6. Here, the average of the axial velocity of each fluid element in the separatrix is defined as the translation velocity of FRCs. FRCs have been accelerated using auxiliary coils in the simulation. In case 4, the translation velocity is increased by up to 20 km/s. The translation velocity control by adjusting the number of installed coils and their locations has been demonstrated. Furthermore, the averaged total temperature and the trapped poloidal flux increase depending on the translation velocity. Figure 7 shows the internal, kinetic, and total energy inside the separatrix in case 1 and case 4. Translated FRCs collided at the time indicated by dashed lines in each case. The plots before the collision show the average energy of FRCs in each formation section. It is observed that kinetic energy is converted to internal energy in the collisional merging process. These results indicate that the total temperature and the trapped poloidal flux of merged-FRCs increase due to the higher kinetic energy of initial-FRCs.

6. Summary

Collisional merging formed FRC in the FAT-CM device has been reproduced in the simulation using the Lamy Ridge code. The performance of simulated FRCs was approximately consistent with that of experimental FRCs. These results indicate the usefulness of this code for evaluating the global behavior of FRCs during the collisional merging formation. The acceleration of FRCs with auxiliary coils has been evaluated by the simulations. The translation velocity control by adjusting the number of installed coils and their locations has been demonstrated on the order of several tens of km/s; in addition, the dependence of merged-FRC performance on translation velocity was observed in the simulation.

Acknowledgement

The authors would like to acknowledge all of members of Fusion-Plasma group, Nihon University and TAE who contributed to discussions. This work was partially supported by JSPS KAKENHI Grant Number JP19K21868, JP16K06939 and Grants-in-Aid of College of Science and Technology, Nihon University.

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