Growth of carbon chains in IRC +10216 mapped with ALMA* **

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ABSTRACT

Linear carbon chains are common in various types of astronomical molecular sources. Possible formation mechanisms involve both bottom-up and top-down routes. We have carried out a combined observational and modeling study of the formation of carbon chains in the C-star envelope IRC +10216, where the polymerization of acetylene and hydrogen cyanide induced by ultraviolet photons can drive the formation of linear carbon chains of increasing length. We have used ALMA to map the emission of Δ 3 mm rotational lines of the hydrocarbon radicals C2H, C2H, and C4H, and the CN-containing species CN, C2N, HCN, and H2CN with an angular resolution of ~1″. The spatial distribution of all these species is a hollow 5–10″ wide spherical shell located at a radius of 10–20″ from the star, with no appreciable emission close to the star. Our observations resolve the broad shell of carbon chains into thinner subshells that are 1–2″ wide and not fully concentric, indicating that the mass-loss process has been discontinuous and not fully isotropic. The radial distributions of the species mapped reveal subtle differences: while the hydrocarbon radicals have very similar radial distributions, the CN-containing species show more diverse distributions, with HCN appearing earlier in the expansion and the radical CN extending later than the rest of the species. The observed morphology can be rationalized by a chemical model in which the growth of polynynes is mainly produced by rapid gas-phase chemical reactions of C2H and C2H radicals with unsaturated hydrocarbons, while cyanopolyynes are mainly formed from polynynes in gas-phase reactions with CN and C2N radicals.

Key words. astrochemistry – molecular processes – techniques: interferometric – stars: AGB and post-AGB – circumstellar matter – radio lines: stars

1. Introduction

Linear acetylenic carbon chains, with a polyyne (≡C≡C)n–H or cyanopolyyne (≡C≡C)n–≡C≡N backbone, have long been observed in a wide range of astronomical environments, such as cold molecular clouds, star-forming regions, photon-dominated regions, and the ejecta of evolved stars (Morris et al. 1976; Winnemesser & Walmsley 1978; Guélin et al. 1978; Broten et al. 1978; Bujarrabal et al. 1981; Cernicharo & Guélin 1996; Pardo et al. 2005; Gupta et al. 2009; see Loomis et al. 2016 for a recent disproof of HCN detected). The chemical synthesis of carbon chains in these environments has been a matter of debate over the years, with hypotheses based on top-down mechanisms involving very small carbonaceous grains or aromatic polycyclic hydrocarbons as precursors (Kroto et al. 1987; Pety et al. 2005), and bottom-up chemical schemes driven by cosmic rays or ultraviolet photons (Herbst & Leung 1989; Fukuzawa et al. 1998; Cernicharo 2004).

Carbon chains are particularly conspicuous in circumstellar envelopes around carbon-rich asymptotic giant branch (AGB) stars, which are also the main factories of carbonaceous dust grains in the Galaxy. Circumstellar envelopes provide an ideal laboratory in which to study the formation of carbon chains because their geometry and velocity field are relatively simple, and the composition of the precursor material is well constrained. Because chemical processes take place as matter is ejected from the star through a nearly isotropic outflow, the sequential formation of molecules can be tracked as a function of the radial position in the envelope. The central AGB star is not expected to emit at ultraviolet wavelengths, and thus the main source of ultraviolet photons is the ambient radiation field from nearby stars. Chemical models point to a bottom-up scenario in which the formation of carbon chains of increasing length occurs because their geometry and velocity field are relatively simple, and the composition of the precursor material is well constrained. Because chemical processes take place as matter is ejected from the star through a nearly isotropic outflow, the sequential formation of molecules can be tracked as a function of the radial position in the envelope. The central AGB star is not expected to emit at ultraviolet wavelengths, and thus the main source of ultraviolet photons is the ambient radiation field from nearby stars. Chemical models point to a bottom-up scenario in which the formation of carbon chains of increasing length occurs because of ultraviolet-driven polymerization of C2H and HCN. These small precursors are injected into the expanding wind from the inner circumstellar regions and are photodissociated in the outer circumstellar layers, where the external ambient ultraviolet field is no longer blocked by the circumstellar dust and gas. In these outer regions, the production of the radicals
chains such as C\textsubscript{4}H and CN drives the growth of acetylenic carbon chains (Glassgold et al. 1986; Nejad & Millar 1987; Cherchneff et al. 1993a; Cherchneff & Glassgold 1993b; Millar & Herbst 1994; Millar et al. 2000; Agúndez 2009; Cordiner & Millar 2009; Li et al. 2014).

Owing to its close proximity and brightness, most observational studies of circumstellar envelopes have focused on the prototypical carbon star envelope IRC+10216. In this source, brightness distributions of rotational lines of the radicals C\textsubscript{2}H, CN, and polynye and cyanopolyne chains such as C\textsubscript{2}H, C\textsubscript{3}N, HC\textsubscript{2}N\textsubscript{2}, and HC\textsubscript{5}N\textsubscript{2} have been mapped using single-dish radio telescopes such as IRAM 30 m (Audinos et al. 1994) and radio interferometers such as BIMA (Bieging & Tafalla 1993; Dayal & Bieging 1995), IRAM Plateau de Bure (Guélin et al. 1993, 1997, 1999; Lucas et al. 1995), VLA (Dinh-V-Trung & Lim 2008), and SMA (Patel et al. 2011; Cooke et al. 2015). Despite their moderate sensitivity and angular resolution (ranging from 2′′ to 11′′), these observations were consistent with the presence of C\textsubscript{2}H, CN, and the aforementioned carbon chains to an outer hollow shell of a few arcseconds of width located at a distance between 10″ and 20′′ from the star. This finding implies that regardless of the formation mechanism of carbon chains in IRC+10216, it is only activated in a very specific region of the outer envelope. However, there are still many open questions, such as whether all carbon chains occur precisely in the same circumstellar region or if there is some degree of radial stratification depending on the carbon chain length. A deeper look into the exact chemical mechanisms behind the formation of carbon chains requires observations with a significantly higher sensitivity and angular resolution.

In this article, we present sensitive ALMA observations of IRC+10216 in several rotational lines of carbon chains across the λ 3 mm band. The observations have an angular resolution of ∼1′′, which allows us to resolve the detailed structure and to precisely locate the circumstellar regions where the emission of each carbon chain arises. A chemical model has been developed to interpret the observations and to explain the carbon chain chemistry that is taking place in the outer envelope of this archetypical carbon star.

2. Observations

A λ 3 mm spectral survey of IRC+10216 covering the frequency range 84.0–115.5 GHz was carried out with ALMA band 3 during Cycle 2. Observations were obtained with compact and extended array configurations. The field of view (primary beam) of the 12 m ALMA antennas ranges from ~69′′ at 84 GHz to ~50′′ at 115.5 GHz. Additional observations were performed with the IRAM 30 m telescope to recover the flux filtered out by the interferometer. Observations were centered on the position of the star, with co-ordinates 12000.10 RA = 0°17′57″446 and Dec = 13°16′43″86, according to the position of the λ 1 mm continuum emission peak (Cernicharo et al. 2013). A thorough description of the spectral survey will be presented elsewhere (Cernicharo et al., in prep.). Here, we focus on the large-scale emission of carbon chains. For the emission lines studied here, data from the ALMA compact and extended configurations were merged, after continuum subtraction, with the short spacings data obtained with IRAM 30 m, providing an angular resolution of ∼1′′.

There are several emission lines from carbon chains in the λ 3 mm ALMA spectrum of IRC+10216. In this article we focus on linear carbon chains of the families of polyynes and cyanopolyynes. With respect to polyynes, we concentrate on the radicals of increasing length C\textsubscript{2}H, C\textsubscript{3}H, and C\textsubscript{4}H, which belong to a chemical series resulting from the addition of C\textsubscript{2} subunits. These radicals are chemical descendants of acetylene and the symmetric polyynes C\textsubscript{3}H\textsubscript{2} and C\textsubscript{4}H\textsubscript{2}, molecules that lack a permanent electric dipole moment and thus cannot be observed at these wavelengths. For cyanopolyynes, we study the emission of the radical CN, the cyanopolyynes HC\textsubscript{2}N and HC\textsubscript{5}N, and the related radical C\textsubscript{2}N. We concentrated on these seven species because they display intense emission lines in the λ 3 mm spectrum of IRC+10216 and share a close chemical relationship as precursors or members of the family of acetylenic carbon chains.

An overview of the spatial distribution of C\textsubscript{2}H, C\textsubscript{3}H, and C\textsubscript{4}H (left side) and CN, HC\textsubscript{2}N, HC\textsubscript{3}N, and C\textsubscript{5}N (right side) is shown in Fig. 1, where we plot the brightness distribution of a representative line of each species, averaged over a velocity range of 3 km s\textsuperscript{−1} centered at V\textsubscript{LSR} = V\textsubscript{sys} (where V\textsubscript{sys} = −26.5 km s\textsuperscript{−1} for IRC+10216; Cernicharo et al. 2000). The choice of this velocity range is very convenient for spherically expanding envelopes such as IRC+10216 because the maps show the brightness distribution in a plane perpendicular to the line of sight intersecting the star, allowing us to identify the radial dependence of the emission.

C\textsubscript{2}H and CN. For the small radicals C\textsubscript{2}H and CN, only the N = 1−0 rotational transition of each falls within the frequency range of the survey. This transition consists of two spin-rotation fine-structure components, which are further split into several hyperfine components as a result of the nuclear spin of the hydrogen (C\textsubscript{2}H) or nitrogen (CN) nucleus. Some of the hyperfine components, which are blended in the spectrum of IRC+10216, are closer in frequency than half the line width, which is given by the terminal expansion velocity of the envelope (14.5 km s\textsuperscript{−1}; Cernicharo et al. 2000), implying that the emission at V\textsubscript{LSR} = V\textsubscript{sys} for one component is contaminated by blue- or redshifted emission from the overlapping component. These components are therefore not adequate to trace the spatial distribution of C\textsubscript{2}H or CN in the plane of the sky. In the top left panel of Fig. 1 we show the spatial distribution of C\textsubscript{2}H through a map of the J = 3/2−1/2 F = 1−0 component, lying at 87 328.625 MHz, which is the most intense free-of-blending component. In this map the synthesized beam is 1″07 × 0″92, and the rms per 3 km s\textsuperscript{−1} channel is 0.4 mJy beam\textsuperscript{−1}. In the case of CN, there are various intense non-overlapping components that show similar brightness distributions. The spatial distribution of CN is illustrated in the top right panel of Fig. 1 through the brightness distribution of the J = 3/2−1/2 F = 1/2−1/2 component, whose rest frequency is 113 499.644 MHz. For this map, the synthesized beam is 0″85 × 0″74 and the rms per 3 km s\textsuperscript{−1} channel is 1.0 mJy beam\textsuperscript{−1}. C\textsubscript{3}H and C\textsubscript{4}H. The radicals C\textsubscript{3}H and C\textsubscript{4}H have four and three rotational transitions, respectively (each consisting of a spin-rotation doublet), within the frequency range 84.0–115.5 GHz. The brightness distributions of the individual lines of the two species are discussed in Appendix A. In Fig. 1 we show the emission map of a selected line of each of these radicals to illustrate their spatial distributions in IRC+10216. The maps of C\textsubscript{3}H and C\textsubscript{4}H in Fig. 1 have a similar angular resolution, 1″14 × 0″98 and 1″10 × 0″92, respectively, and sensitivity, with rms levels per 3 km s\textsuperscript{−1} channel of 1.3 and 0.7 mJy beam\textsuperscript{−1}, respectively.

HC\textsubscript{2}N and HC\textsubscript{5}N. The cyanopolyynes HC\textsubscript{2}N and HC\textsubscript{5}N have several rotational transitions within the frequency range covered, 3 in the case of HC\textsubscript{2}N, and up to 12 for HC\textsubscript{5}N. A detailed discussion on the brightness distributions of the individual lines of the two molecules is also presented in Appendix A. In Fig. 1, the spatial distributions of HC\textsubscript{2}N is traced by the emission
Fig. 1. Brightness distributions of $\lambda$ 3 mm rotational transitions of the polyyne-like radicals C$_2$H, C$_4$H, and C$_6$H, and the cyanopolyne-like species CN, HC$_3$N, HC$_5$N, and C$_3$N, averaged over a velocity range of width 3 km s$^{-1}$ centered at $V_{\text{LSR}} = V_{\text{sys}}$. Details on the maps can be found in Sect. 2. The maps are centered on the star, indicated by a cross, and the synthesized beam ($\sim 1''$ in all maps but that of C$_6$H, where it is $\sim 3''$) is shown in the bottom left corner of each panel. A white circle of radius 15'' centered on the star is drawn to facilitate comparison among maps.
of the $J = 10–9$ line in a map with an angular resolution of $1.08 \times 0\farcs81$ and a rms per 3 km s$^{-1}$ channel of 0.9 mJy beam$^{-1}$, while the distribution of HC$_3$N is illustrated by the emission of the $J = 32–31$ line, with an angular resolution of $1.11 \times 0\farcs99$ and an rms per 3 km s$^{-1}$ channel of 0.6 mJy beam$^{-1}$.

C$_6$H. The radical hexatriynyl, C$_6$H, has a plethora of rotational transitions in the $1.3$ mm spectrum of IRC +10216, consisting of two series of doublets arising from the $^3\Pi_{1/2}$ and $^3\Pi_{3/2}$ spin-orbit fine structure states, the former lying 21.6 K above the latter. Because of the lower sensitivity of the interferometric data of each individual line, we only considered ALMA data obtained with the compact configuration and stacked the maps of a selected list of 19 lines, all free of blending and observed with a sufficient quality, to obtain a more sensitive map of the spatial distribution of C$_6$H (see Fig. 1). Because we have omitted the ALMA data obtained with the extended configuration, the angular resolution of the C$_6$H map is on the order of $\sim 3\arcsec$, that is, significantly poorer than in the rest of maps shown in Fig. 1. The set of C$_6$H lines stacked cover a wide range of upper level energies, 64–86 K for lines from the $^3\Pi_{1/2}$ state and 86–113 K for $^3\Pi_{3/2}$ lines, and thus it is possible that their different excitation requirements result in different brightness distributions. However, we note that on the basis of the behavior of other molecules such as HC$_3$N (see Appendix A), these differences are unlikely to be larger than the current angular resolution of $\sim 3\arcsec$.

3. Observed spatial distributions of carbon chains

A cursory view of the maps shown in Fig. 1 reveals a clear and well-defined ring structure in the seven species: the three hydrocarbon radicals C$_2$H, C$_3$H, and C$_6$H, and the four cyanides CN, HC$_3$N, HC$_5$N, and C$_7$N. The maps correspond to the emission at the line center, that is, at $V_{LSR} = V_{sys}$, and thus indicate how the emission is distributed along a plane perpendicular to the line of sight intersecting the star. The two-dimensional ring structure, together with the emission maps at red- and blueshifted velocities (not shown in Fig. 1), indicate that the three-dimensional structure of the seven species consists of a hollow spherical shell with a width of $5–10''$ located at a distance between 10'' and 20'' from the star. This distribution has been known for most species studied here from previous interferometric maps, albeit at lower angular resolution (see Guélin et al. 1997 and references therein).

The higher angular resolution of the ALMA observations presented here reveals that in fact the broad $5–10''$ wide hollow shell consists of several clumpy thinner shells of width $1–2''$, which are not fully concentric, as indicated by the arcs that cross each other and by a spiral-like structure seen in the $\sim 1''$ resolution maps of Fig. 1. This type of substructure was seen earlier in IRC +10216 at larger scales in light scattered by dust grains (Mauron & Huggins 1999; Leão et al. 2006) and in emission from CO (Cernicharo et al. 2015), and it has been interpreted in terms of episodic or discontinuous mass loss owing to the presence of a binary companion (Cernicharo et al. 2015). Observations carried out with the VLA at an angular resolution of $\sim 2–3''$ also showed that the centimeter-wavelength emission of HC$_5$N and HC$_3$N consists of clumpy shells consistent with a non-isotropic and episodic mass-loss process (Dinh-V-Trung & Lim 2008). More recently, high angular resolution ALMA observations of the emission in different molecular lines have also provided hints of departures from the spherical symmetry and spiral-like structures in the inner regions of the envelope (Decin et al. 2015; Velilla Prieto et al. 2015; Agúndez et al. 2015; Quintana-Lacaci et al. 2016). The $\sim 1''$ angular resolution maps (see Fig. 1 using white circles as a reference) show that the molecular shell is not exactly centered on the position of the star, but shifted by a few arcseconds in the NE direction. It seems as though the shell of carbon chains is compressed from the SW direction, a result that is also observed at larger scales in CO (Cernicharo et al. 2015). It is currently unclear whether this feature is the result of an enhanced ultraviolet illumination from the direction of the Galactic plane (SW) or is linked to the non-isotropic character of the mass-loss process. It is noteworthy that unlike some of the previous observations at lower angular resolution (see, for example, the case of C$_2$H in Guélin et al. 1997), the maps in Fig. 1 show no evidence of axial symmetry.

The structure of thin shells and intercrossing arcs is common to the emission distribution of the different species studied (at least for those mapped with $\sim 1''$ angular resolution; see Fig 1). These similarities indicate that the brightness maxima correspond to locations with an enhancement in the total volume density of matter, and not in the fractional abundance of a particular species. Such a finding is consistent with some mechanism that has shaped the envelope by driving the mass-loss process out of the strictly uniform isotropic character.

Fig. 2. Emission distribution of C$_2$N $N = 10–9$ (black contours) superimposed on the brightness distribution of CN $N = 1–0$ (color map in the left panel) and of HC$_3$N $J = 10–9$ (color map in the right panel).
The brightness distributions of different species reveal subtle differences. Even if there is a good match between the arcs and shells seen for different species, radially away from the star, some arcs or thin shells that are observed in some species are not seen in others, which provides information about the chemical particularities of each species. This point is illustrated in Fig. 2, where we superimpose the emission distribution of the radical C$_3$N, shown as contours, on the brightness distribution of the small radical CN and of the cyanopolyyne HC$_3$N. Referring first to the left panel of Fig. 2, the shells and arcs in C$_3$N are well matched by CN, although it is also true that CN shows shells beyond ~20$''$ that are not seen in C$_3$N. That is, the CN radical extends farther from the star than the radical C$_3$N. Referring now to the right panel in Fig. 2, we note again that the shells and arcs in C$_3$N are well matched by similar structures in HC$_3$N. We also note that the well-defined outer arcs indicated by the lowest contour in the NW and SW directions in C$_3$N are well matched by tenuous, although appreciable, features in HC$_3$N. In this case, HC$_3$N shows shells inward of ~14$''$ that are not seen in its radical C$_3$N, which leads us to conclude that in the framework of an expanding envelope, the cyanopolyyne HC$_3$N appears in regions where the radical C$_3$N has not yet been formed.

Figure 3 shows in a different way how emission distributions of different species match each other. In this plot we have extracted the surface brightness along a strip intersecting the star at PA = 45$'$ from the maps of the cyanides CN, C$_2$N, HC$_3$N, and HC$_5$N shown in Fig. 1. There are several aspects that are worthy of comment. First, the brightness distributions along the selected strip are not symmetrical with respect to the position of the star, indicating that the circumstellar shells are not strictly concentric, but instead consist of intersecting arcs and a spiral-like structure. Second, in the SW direction (positive values along x-axis) are several shells of width ~2$''$ at approximately +11$'$, +15$'$, +21$'$, and +27$''$ from the star. These shells are not traced by the four species, however. The shells at +15$'$ and +21$'$ are seen in the four species. The shell at +11$'$ is traced by the cyanopolyynes HC$_3$N and HC$_5$N, but not by the radicals C$_3$N and CN, and the farthest shell at +27$''$ is mostly seen in CN and to a lesser extent in the cyanopolyynes. Of the four cyanides, the cyanopolyynes therefore appear at shorter radii than their radicals, while the radical CN extends farther in the envelope.

Information on the radial distribution of the species can be obtained by azimuthal average of the brightness distribution (see Fig. 4). The lack of strictly concentric shells, with arcs that cross each other within a spiral-like arrangement, produces a smoothing effect when azimuthally averaging. That is, the spatial resolution is degraded by averaging shells that are not strictly at the same radial position. Still, the information provided by this plot is highly useful in analyzing whether species share the same radial regions or if there is some degree of stratification as a function of radius. The hydrocarbon radicals C$_2$H, C$_3$H, and C$_5$H reach their maximum brightness at the same radial position, between 15$'$ and 16$'$, although the smallest radical, C$_2$H, extends somewhat farther than the heavier radicals. The cyanides, however, show much more disparate radial distributions. The distribution of HC$_3$N is shifted the most to inner regions, as it emerges at radii as short as 7$''$, while the rest emerge at radial distances greater than 10$''$. The radial distribution of CN is also markedly different from the rest of the species as it extends out to radial distances beyond 30$''$. As for HC$_5$N, it appears at the same radial distance as CN and disappears with HC$_3$N, while the radical C$_3$N appears somewhat farther than the cyanopolyynes HC$_3$N and HC$_5$N. All this information is of great value in understanding the formation mechanism of each of these species in IRC +10216 and is the subject of further discussion in Sect. 4.

4. Model

The ALMA emission maps of carbon chains obtained toward IRC +10216 provide an excellent opportunity to determine the main chemical processes responsible for their formation along the circumstellar outflow. To this end, we have constructed a simple model of IRC +10216 that consists of a spherical envelope of gas and dust that expands around an AGB star with a constant velocity. The parameters of the star and envelope are taken from Agúndez et al. (2012), that is, the adopted mass-loss rate is $2 \times 10^{-5} M_\odot$ yr$^{-1}$. For the distance, we use the recent value of 123 pc determined by Groenewegen et al. (2012). First we constructed a chemical model to describe the chemical composition


of the gas as it expands, and then we carried out radiative transfer calculations to convert the abundance radial distributions into brightness radial distributions that can be compared with the ALMA observations.

### 4.1. Chemical model: formation of carbon chains

In the chemical model, the gas is assumed to expand isotropically from an initial radius of $2 \times 10^{16}$ cm. We consider as parent molecules at the initial radius $\text{H}_2$, $\text{CO}$, $\text{C}_2\text{H}_2$, $\text{CH}_4$, $\text{C}_2\text{H}_2$, $\text{H}_2\text{O}$, $\text{N}_2$, $\text{HCN}$, $\text{NH}_3$, $\text{CS}$, $\text{H}_2\text{S}$, $\text{SiS}$, $\text{SiO}$, $\text{SiH}_4$, $\text{PH}_3$, and $\text{HCP}$, with abundances from Agúndez et al. (2012) and a value of $4 \times 10^{-5}$ relative to $\text{H}_2$ for $\text{N}_2$, based on chemical equilibrium calculations and a solar elemental abundance for nitrogen. Of special interest for the formation of carbon chains in the outer envelope are the parent molecules $\text{C}_2\text{H}_2$ and $\text{HCN}$, for which the adopted abundances relative to $\text{H}_2$ are $8 \times 10^{-5}$ and $4 \times 10^{-5}$, respectively (Fonfría et al. 2008). We assume that the envelope is externally illuminated by the local ultraviolet radiation field of Draine (1978). Under the assumption of a smooth envelope and adopting the $N_{\text{H}}/A_V$ ratio of $1.87 \times 10^{21}$ cm$^{-2}$ mag$^{-1}$ determined for the local interstellar medium by Bohlin et al. (1978), chemical models of IRC+10216 predict that photochemistry occurs at shorter radii than indicated by interferometric observations (see, e.g., discussion in Appendix B of Agúndez & Cernicharo 2006 and Figs. 1 and 4 in Cordiner & Millar 2009). For the purpose of reproducing the observed radial location of carbon chains, we have adopted a $N_{\text{H}}/A_V$ ratio 1.5 times lower than the canonical interstellar value of Bohlin et al. (1978), regardless of the implicit assumption on the dust opacity. The adopted cosmic-ray ionization rate of $\text{H}_2$ is $1.2 \times 10^{-17}$ s$^{-1}$, a value typical of the local interstellar medium that is well suited for IRC+10216, according to observations of HCO$^+$ (Agúndez & Cernicharo 2006; Pulliam et al. 2011). We use a large network of gas-phase chemical reactions, whose rate constants have been taken from the literature on gas-phase chemical kinetics and from the UMIST and KIDA databases (McElroy et al. 2013; Wakelam et al. 2015). More details on the reactions important for the chemistry of carbon chains in IRC+10216 and on the rate constants are given below.

Figure 5 summarizes some salient features of the chemical model in relation to the growth of carbon chains in IRC+10216. According to the model, the formation of carbon chains begins when the parent molecules $\text{C}_2\text{H}_2$ and HCN are photodissociated, in the region of the outer envelope where $A_V \sim 1$ mag, producing the radicals $\text{C}_2\text{H}$ and CN. A series of rapid neutral-neutral reactions involving these radicals then drives the growth of carbon chains. The schemes shown at the top of Fig. 5, inspired by Millar & Herbst (1994), illustrate the main processes involved in the synthesis of polynes and cyanopolyynes. The schemes include only those processes that according to the chemical model are the main contributors to the formation of each species. Nevertheless, below we discuss the reliability of these schemes and whether other types of reactions may play a role.

The formation of carbon chains begins with the photodissociation of $\text{C}_2\text{H}_2$ and HCN, whose cross sections are well known from laboratory experiments. We computed photodissociation rates for the local ultraviolet radiation field of Draine (1978)
and dust-shielding factors (see Table 1) using the Meudon PDR code (Le Petit et al. 2006). For C3H2 we adopted the photoabsorption cross section measured by Cooper et al. (1995) and subtracted the photoionization cross section from the compilation by Hudson (1971) to obtain the cross section of photodissociation, which is assumed to yield the C2H radical with a 100% efficiency. For HCN, photodissociation is assumed to yield only CN radicals with the cross section measured by Nuth & Glicker (1982). Acetylene photodissociates faster than hydrogen cyanide, which translates into a shorter photodissociation radius for C3H2 (see bottom panels in Fig. 5). The photodissociation rates computed here for C3H2 and HCN are similar to those given in the compilation of Heays et al. (2017). These authors, however, computed a photodissociation rate of acetylene that is about twice lower than our value, which would shift the photodissociation radius of C2H2 to somewhat larger outer radii with respect to our predictions.

4.1.1. Polyynes

The main pathway for forming polyynes of increasing chain length with an even number of carbon atoms involves successive reactions with the radical C2H,

\[
\text{C}_2\text{H} + \text{C}_2\text{H}_2 \rightarrow \text{C}_2\text{H}_2 + \text{H}, \tag{1}
\]

where diacetylene (C2H2) is synthesized when \( n = 1 \), triacetylene (C3H2) is formed when \( n = 2 \), and so on. The reaction between C2H and C2H2 is fast at low temperatures. The measured rate constant in the temperature range 15–295 K shows a slight negative temperature dependence, with values in the range \((1.1–2.3) \times 10^{-10} \text{ cm}^3 \text{s}^{-1} \) (Chastaing et al. 1998). There are no measurements of the rate constant at low temperatures for \( n > 1 \). The reaction between C2H and C2H2 has been studied theoretically and experimentally using the crossed beams technique (Landera et al. 2008; Gu et al. 2009). These studies indicate that the kinetics of the reaction at low temperatures should be similar to that of the reaction C2H + C2H2, with a rate constant of the same order of magnitude and the H loss channel strongly favored. Reactions of C2H with polyynes larger than C2H2 can be reasonably expected to proceed in a similar way, although there are no experimental or theoretical studies on the kinetics of reaction (1) with \( n > 2 \).

Triacetylene (C3H2) and larger polyynes are also formed by another route involving the C4H radical,

\[
\text{C}_4\text{H} + \text{C}_2\text{H}_2 \rightarrow \text{C}_2\text{H}_2 + \text{H}, \tag{2}
\]

where the reaction of C4H and C3H2 has been experimentally found to be rapid at low temperatures, with a rate constant of \((1.5–2.6) \times 10^{-10} \text{ cm}^3 \text{s}^{-1} \) in the temperature range 39–300 K (Bertolote et al. 2010). For polyynes larger than C4H2, routes similar to reactions (1) and (2) but involving radicals larger than C4H, such as C6H and C8H, are likely to show a similar kinetic behavior (see, e.g., Sun et al. 2015) and thus to contribute significantly to the formation of large polyynes in environments such as IRC +10216.

When the polyynes have been formed, the corresponding radicals, such as C6H and C8H, form directly by photodissociation, although reactions involving C2 are also important, but to a lesser extent. Diacetylene and triacetylene are easily photodissociated owing to their large absorption cross sections in the ultraviolet. The photodissociation rate of C2H2 has been computed from the photoabsorption cross section measured by Ferradaz et al. (2009), after subtraction of the photoionization cross section measured by Schwell et al. (2012). The main channel in the photodissociation of C2H2 is the production of C4H radicals (Silva et al. 2008). For C2H2, the photoionization cross section has not been measured, and therefore the photodissociation rate has been directly computed from the photoabsorption cross section measured by Kloster-Jensen et al. (1974) and Shindo et al. (2003), assuming that the main channel is C2H + H. The reactions involving C2 of interest here are

\[
\text{C}_2 + \text{C}_2\text{H}_2 \rightarrow \text{C}_2\text{H}_2 + \text{H}, \tag{3}
\]
where the radicals $C_2H$ and $C_3H$ form by addition of $C_2$ sub-units to $C_2H_2$ and $C_3H_2$, respectively. The reaction between $C_2$ and $C_2H_2$ is rapid at low temperatures, with a rate constant of $(2.4\text{−}4.8) \times 10^{-10}$ cm$^3$ s$^{-1}$ in the temperature range 24\text{−}300 K (Canosa et al. 2007; Daugey et al. 2008; Páramo et al. 2008).

The low-temperature kinetics of reactions of $C_2$ with $C_2H$ and larger polyynes has not been studied experimentally, and thus in the model we assume that they proceed with the same rate constant as the $C_2 + C_2H_2$ reaction.

According to the model, reactions (1) and (2) account for the bulk of formation of polyynes in IRC +10216, while the radicals are mainly formed by photodissociation of the corresponding polyynes and by reaction (3). Other types of reactions, which are rapid and might be important synthetic routes in other environments, contribute little in IRC +10216 because they involve reactants that are not abundant enough in this source. For example, neutral carbon atoms and CH radicals have been experimentally found to react rapidly at low temperatures with $C_2H_2$ (Chastaing et al. 2001; Clary et al. 2002; Canosa et al. 1997; Loison & Bergeat 20019), and they probably react rapidly with $C_2H_2$ and larger polyynes as well. These reactions tend to produce unsaturated carbon chains with an odd number of carbon atoms and in fact, in the chemical model, are major formation routes to species such as $C_3H$, $C_4H_2$, and $C_5H_3$, which are abundant in IRC +10216. However, here we focus on the chemistry of carbon chains $C_2H$ and $C_3H_2$ with $n$ even, species for which reactions involving C atoms and CH radicals are not important.

Molecular anions have been found to play a non-negligible role in the formation of neutral carbon chains in dark clouds (Walsh et al. 2009), and thus it is worth discussing whether they play a similar role in IRC +10216. According to the chemical model, reactions of the type

$$C_2nH^- + H \rightarrow C_{2n}H + e^-,$$

which are rapid (Eichelberger et al. 2007), appear high in the list of reactions that contribute most to the formation of polyynes, especially at radii beyond \textasciitilde 15” from the star. However, since the precursor anion $C_2nH^-$ is mostly formed from its neutral counterpart $C_2nH$, which is in turn formed by photodissociation of the respective polyyne $C_2nH_2$, the net contribution of reaction (4) to the formation of polyynes and growth of carbon chains is essentially zero.

### 4.1.2. Cyanopolyynes

Cyanopolyynes in IRC+10216 are formed in a bottom-up scenario analogous with polyynes (see scheme at the top right of Fig. 5). We first concentrate on the potentially important synthetic route given by the reaction

$$C_2nH + HC_{2n-1}N \rightarrow HC_{2n-2}N + H + N,$$

where the simplest case is with $n = 1$ and $m = 1$, which corresponds to the reaction between $C_2H$ and $HCN$ to form $HC_3N$. The rate constant of this reaction has not been measured at low temperatures, but measurements in the temperature range 297\text{−}360 K (Hoobler & Leone 1997) and theoretical studies (Fukuzawa & Osamura 1997) point to the presence of an activation barrier of \textasciitilde 800 K that would make the reaction too slow at low temperatures. For this reason, we assume that reaction (5) shows the same kinetic behavior for values of $n$ and/or $m$ higher than one, that is, for reactions of $C_3H$, $C_4H$, or larger radicals with $HCN$, $HC_3N$, or larger cyanopolyynes. As a consequence, reaction (5) is not efficient in IRC +10216, and this is the reason that it does not appear in the scheme at the top right of Fig. 5. The UMIST and KIDA databases make different assumptions on the kinetic behavior of reaction (5) for $n$ and/or $m > 1$. For example, the UMIST database does not consider these reactions, while in the KIDA database some of them, the reaction $C_2H + HC_2N$, for instance, are assumed to be rapid at low temperatures. It would be of great interest to study the low-temperature chemical kinetics of reactions such as $C_2H + HC_3N$ and $C_2H + HCN$ to clarify whether there are some values of $n$ and $m$ for which reaction (5) is rapid at low temperatures, and thus contributes to the growth of cyanopolyynes in IRC +10216 and in cool interstellar clouds.

If reaction (5) is indeed completely closed at low temperatures, then the growth of cyanopolyynes does not occur at the expense of cyanopolyynes of smaller size, but at the expense of polyynes in reactions involving the CN radical

$$CN + C_{2n}H_2 \rightarrow HC_{2n+1}N + H,$$

where $C_2H_2$ serves as the precursor of $HC_3N$, the polyyne $C_2nH_2$ for $HCn$, and so on. Reaction (6) with $n = 1$, that is, $CN + C_2H_2$, has been experimentally found to be fast at low temperatures, with a rate constant of $(2.6\text{−}4.7) \times 10^{-10}$ cm$^3$ s$^{-1}$ in the temperature range 25\text{−}298 K (Sims et al. 1993). Other studies confirm that the reaction proceeds without an activation barrier, yielding $HC_3N$ as the main product (Fukuzawa & Osamura 1997; Huang et al. 2000; Choi et al. 2004). Reaction (6) with $n = 2$, that is, $CN + C_3H_2$, is also rapid at room temperature, with a measured rate constant of $4.2 \times 10^{-10}$ cm$^3$ s$^{-1}$ (Seki et al. 1996), although it has not been experimentally studied at low temperatures. Theoretical calculations and crossed-beam experiments, however, indicate that the reaction of $CN$ with $C_3H_2$ as well as those of $CN$ with larger polyynes are rapid at low temperatures and provide an efficient route to large cyanopolyynes (Fukuzawa et al. 1998; Zhang et al. 2009). According to our chemical model, reaction (6) serves as the main formation route to cyanopolyynes in IRC +10216.

For cyanopolyynes larger than $HC_3N$, there is another important formation route involving the radical $C_3N$,

$$C_3N + C_{2n}H_2 \rightarrow HC_{2n+1}N + H.$$

It has recently been found that the radical $C_3N$ reacts as fast as the radical CN with $C_2H_2$, with a rate constant of $(2.5\text{−}4.7) \times 10^{-10}$ cm$^3$ s$^{-1}$ in the temperature range 24\text{−}294 K (Fournier 2014). Assuming that the same kinetic behavior holds for $C_3N$ reacting with $C_2H_2$ and longer polyynes, reaction (7) becomes an important formation route of cyanopolyynes. In fact, in our chemical model, reactions (6) and (7) contribute similarly to the formation of $HC_3N$. Moreover, routes similar to reactions (6) and (7), but involving radicals larger than $C_3N$, such as $C_4N$, are likely significant contributors to the formation of cyanopolyynes larger than $HC_3N$ in IRC +10216.

The radicals $C_2N$ and $C_3N$ are mainly formed by direct photodissociation of the corresponding cyanopolyynes, $HC_3N$ and $HC_4N$, respectively. As with polyynes, cyanopolyynes have large absorption cross sections at ultraviolet wavelengths and are thus easily photodissociated. The photodissociation rate of $HC_3N$ has been computed from the photoabsorption cross section measured by Ferradaz et al. (2009), after subtracting the photoionization cross section measured by Leach et al. (2014). We have adopted the wavelength-dependent branching ratios computed by Silva et al. (2009) for the two open channels, $C_3N + H$ and $C_3N + CN$, which are in agreement with experiments (Halpern et al. 1988; Clarke & Ferris 1995; Seki et al. 1996b). In the case of $HC_3N$, the ionization potential
and photoionization cross section are not known, and therefore the photodissociation rate has been computed from the photoabsorption cross section measured by Fray et al. (2010), where we have assumed that the H and CN channels occur with similar branching ratios as for HC$_3$N.

4.2. Radiative transfer models: emission of carbon chains

In the top panels of Fig. 6, the abundance radial profiles calculated for C$_2$H, C$_4$H, and C$_6$H (left) and for CN, HC$_3$N, HC$_5$N, and C$_3$N (right) are shown, in which abundances are expressed in absolute rather than relative terms, that is, as the number of particles per unit volume. These abundance distributions provide a good indication of how the rotational emission of each species is distributed as a function of radius in the plane of the sky. Nevertheless, significant differences can arise depending on the transition owing to excitation effects, because of the way the rotational levels are populated through collisions and radiative processes such as infrared pumping at different radii. To take these effects into account, we have carried out excitation and radiative transfer calculations to convert the abundance radial distributions into radial brightness distributions of 3 mm transitions, which can in turn be compared with the ALMA observations.

The radiative transfer calculations have been performed with the multi-shell LVG code and physical model of IRC $+$10216 used by Agúndez et al. (2012), with the radial abundance distributions calculated with the chemical model. The calculations require spectroscopic and collision excitation data, which have different degrees of accuracy depending on the species and type of data. Rotational constants of the ground-vibrational state, and for some species, vibrationally excited states as well, are well known from microwave laboratory experiments: C$_2$H (Müller et al. 2000; Killian et al. 2007), CN (Klisch et al. 1995), C$_2$H and C$_3$N (Gottlieb et al. 1983), C$_4$H (Linnartz et al. 1999), HC$_3$N (Thorwirth et al. 2000), and HC$_5$N (Bizzocchi et al. 2004). Dipole moments have been measured for the radical CN (Thompson & Dalby 1968) and the closed electronic-shell species HC$_3$N (DeLeon & Muenter 1985) and HC$_5$N (Alexander et al. 1976), and ab initio theoretical values, with significantly higher uncertainties, have been calculated for the radicals C$_2$H, C$_4$H, C$_6$H (Woon 1995), and C$_3$N (McCarthy et al. 1995).

In addition to thermal excitation through collisions with H$_2$ and He, absorption of infrared photons and pumping to excited vibrational states, followed by radiative decay to rotational levels in the ground-vibrational state, is an important excitation mechanism of molecules in IRC $+$10216 (Deguchi & Uyemura 1984; Agúndez & Cernicharo 2006; González-Alfonso et al. 2007; Agúndez et al. 2008, 2015; Corder & Millar 2009; Daniel et al. 2012; De Beck et al. 2012). Here, we have included excitation through infrared pumping for all studied species, mostly through bands lying in the mid-infrared, where the flux in IRC $+$10216 is large (Cernicharo et al. 1999). To facilitate the excitation and radiative transfer calculations, we have collapsed the fine rotational structure of the radicals and simply treated these species as linear molecules with a $\Sigma$ electronic state. For C$_3$H, we have included the first four vibrationally excited states of the bending mode ($v_3 = 1, 2, 3, 4$), and the first vibrationally excited states of the stretching modes ($v_1 = 1$ and $v_1 = 1$). The vibrationally excited state that plays the most important role, through infrared pumping, in the excitation of C$_3$H in IRC $+$10216 is $v_2 = 1$, which lies 371 cm$^{-1}$ above the ground-vibrational state. The wavelengths and strengths of the vibrational bands have been taken from Tarroni & Carter (2004). For the radical CN, we have included the $v = 0 \rightarrow 1$ band, lying at 2042 cm$^{-1}$ (Hübner et al. 2005; Brooke et al. 2014), which plays a minor role on the excitation of the $\lambda$ 3 mm lines in IRC $+$10216, however. For HC$_3$N, we have included the first excited states of the vibrational bending modes $v_3$ and $v_4$, which have strong fundamental bands at 663 and 498 cm$^{-1}$. The wavelengths and strengths of the vibrational bands are from the compilation by J. Crovisier$^1$, which are based on extensive laboratory work (e.g., Uyemura et al. 1982; Jolly et al. 2007). For cyanodicyclopentadiene, we have included the first excited states of the vibrational bending modes $v_3$ and $v_4$, whose calculated fundamental bands, lying at 566 and 685 cm$^{-1}$, have been found to be important for the rotational excitation of HC$_3$N in IRC $+$10216 (Deguchi & Uyemura 1984). For the radicals C$_4$H, C$_5$H, and C$_6$H there is little information on the wavelengths and strengths of vibrational bands. For these species we have instead included a generic vibrationally excited state lying at 15 µm above the ground-vibrational state, with an Einstein coefficient of spontaneous emission of 5 s$^{-1}$ for the $P(1)$ transition of the vibrational band. A similar treatment, with slightly different parameters, was adopted for C$_4$H and C$_5$H by Cordiner & Millar (2009).

Rate coefficients for rotational excitation induced by collisions with H$_2$ and He are scarce in the literature for the species studied here. We have adopted the rate coefficients calculated by Dumouchel et al. (2010) for HCN in collisions with He, properly corrected by the square root of the ratio of reduced masses with He and H$_2$, for the excitation of the radicals C$_2$H and CN. Green & Chapman (1978) calculated rate coefficients for the excitation of HC$_3$N in collisions with He, and these values, corrected for H$_2$ and extrapolated to higher J levels through the IOS approximation when needed, have been used for HC$_5$N as well as for the radicals C$_3$N and C$_4$H. For the longer carbon chains HC$_4$N and C$_6$H, we have adopted collision rate coefficients from the approximate generic expression given by Deguchi & Uyemura (1984).

The calculated radial distributions of brightness in the plane of the sky are shown in the bottom panels of Fig. 6, in comparison with the observed distributions. We leave the discussion of the comparison between calculated and observed emission distributions for Sect. 5 and focus here on the comparison between radial distributions of abundance and emission (top panels and upper and middle curves in the bottom panels of Fig. 6). When infrared pumping is neglected and rotational excitation occurs exclusively through collisions with H$_2$ and He (upper curves in the bottom panels of Fig. 6), calculations show that the radius where the $\lambda$ 3 mm emission maximum does not exactly coincide with the radius where the number of particles per unit volume is maximum. In general, the emission tends to peak a few arcseconds inward from where the abundance is maximum. This is evident in C$_2$H, CN, C$_4$N, and the cyanopolyynes HC$_3$N and HC$_5$N. The origin of this effect is that the circumstellar envelope has strong radial gradients of density and temperature. More internal regions are characterized by denser and warmer gas, and the excitation of rotational levels by collisions is more favorable. Thus, the radius of maximum brightness represents a compromise between a high absolute abundance and a high excitation rate through collisions. The shift to shorter radii of the maximum of brightness becomes more pronounced for high-J transitions, whose upper levels are high in energy and are more difficult to excite through collisions in the lower density environments.

The situation may change significantly when infrared pumping to excited vibrational states is included in the calculations

$^1$ www.lesia.obspm.fr/perso/jacques-crovisier/basemole
Fig. 6. Top panels: calculated radial distributions of abundances expressed as number of particles per unit volume. Curves have been arbitrarily scaled in the $y$-axis for display. Bottom panels: comparison between calculated (neglecting and including infrared pumping) and observed radial distributions of the emission at velocities around $V_{LSR} = V_0$, for the lines of $\text{C}_2\text{H}$, $\text{C}_3\text{H}$, and $\text{C}_6\text{H}$ (left), and $\text{CN}$, $\text{C}_2\text{N}$, $\text{HC}_3\text{N}$, and $\text{HC}_5\text{N}$ (right) plotted in Fig. 1. The observed brightness distributions are those previously shown in Fig. 4. Curves have been arbitrarily scaled and shifted along the $y$-axis for display.

(middle curves in bottom panels of Fig. 6). If a species has strong vibrational bands at wavelengths at which the flux of infrared photons in the envelope is high, then infrared pumping may dominate collisions in exciting the rotational levels of the ground-vibrational state. Our calculations indicate that for most of the species studied here, infrared pumping plays an important role in the excitation of the $\lambda\ 3\ mm$ lines, and in some cases, it has important consequences for the emerging line intensities and radial distributions of the brightness. Infrared pumping tends to increase the excitation temperatures of the rotational transitions of the ground-vibrational state and the intensities of the rotational lines, and it extends the emission region to outer locations in the envelope. The importance of this effect, however, varies depending on the species and transition. For the species studied here, infrared pumping has a marked effect on the brightness radial distribution of the $\lambda\ 3\ mm$ lines of $\text{C}_2\text{H}$ (through absorption of $27\ \mu m$ photons and pumping to the $v_2 = 1$ state), $\text{HC}_3\text{N}$ (by excitation of the $v_5 = 1$ and $v_6 = 1$ states with $15\ \mu m$ and $20\ \mu m$ photons), and $\text{HC}_5\text{N}$ (exciting the $v_7 = 1$ and $v_8 = 1$ states with $14.6$ and $17.7\ \mu m$ photons). In contrast, there is little effect of infrared pumping on the emission distribution of the $N = 1–0$ line of $\text{CN}$, which can only be pumped by $4.9\ \mu m$ photons through the fundamental band of the stretching mode of the $\text{C}–\text{N}$ bond. In the case of the radicals $\text{C}_3\text{H}$, $\text{C}_6\text{H}$, and $\text{C}_7\text{H}$, the hypothesized vibrational band at $15\ \mu m$ has different effects on the $\lambda\ 3\ mm$ emission distribution of each species, the effects being more marked for $\text{C}_7\text{H}$, somewhat less important for $\text{C}_6\text{H}$, and of little importance for $\text{C}_3\text{H}$. We would like to stress, however, that the lack of knowledge of the wavelengths and strengths of vibrational bands for these three radicals create significant uncertainties in the predicted brightness radial distributions. Moreover, the presence of density enhancements in the form of arcs, which are not
includes the current model, will increase the importance of collisions with respect to infrared pumping, modifying the relative roles of both processes in the excitation of the $\lambda$ 3 mm lines.

In summary, although the abundance radial distribution provides a good first-order estimate of how the $\lambda$ 3 mm emission is distributed radially, there can be shifts of up to several arcseconds depending on the peculiarities of the excitation of each species.

5. Discussion

A comparison between the observed and calculated $\lambda$ 3 mm emission distributions of carbon chains allows us to draw conclusions about the formation mechanism of carbon chains in IRC +10216. For this discussion we focus on Fig. 6, specifically on the bottom panels, where calculated and observed brightness radial distributions are compared. We concentrate on the emission distributions calculated when infrared pumping is taken into account (middle curves in the bottom panels of Fig. 6), which are more realistic than those obtained when excitation by collisions is considered alone (upper curves in the bottom panels of Fig. 6), even if just an approximate treatment of the pumping scheme is adopted, as occurs for the radicals $\text{C}_2\text{H}$, $\text{C}_6\text{H}$, and $\text{C}_5\text{N}$. Before drawing firm conclusions, we must keep in mind that the observed brightness radial distributions are the result of an azimuthal average of the brightness distributions shown in Fig. 1. These maps show the existence of an azimuthal structure, with shells that are not strictly concentric, as indicated by the presence of intercrossing arcs, probably the consequence of a mass-loss process that is not strictly continuous and isotropic. Because the envelope in our model is the result of an isotropic uniform mass-loss process and the angular resolution has been degraded in the observational data owing to the azimuthal average, the comparison between the calculated and observed emission distributions can only be done to first order and not at the subarcsecond level.

Observations locate the emission of the three hydrocarbon radicals $\text{C}_2\text{H}$, $\text{C}_6\text{H}$, and $\text{C}_4\text{H}$ at the same radial position in the envelope, with maxima between 15\arcsec 5 and 16\arcsec 0 from the star. It is remarkable that the chemical model also predicts a similar behavior of the abundance radial profiles, with a slight radial stratification in which the radial position decreases as the size of the radical increases (see the top left panel in Fig. 6). This radial stratification is slightly more marked when abundances are converted into brightness distributions (middle curves in the bottom right panel of Fig. 6), although the predictions for $\text{C}_2\text{H}$ and $\text{C}_6\text{H}$ have to be viewed with caution due to the approximate treatment of infrared pumping. Taking into account that the formation of these radicals in the chemical model occurs sequentially with respect to increasing size (see scheme at the top right of Fig. 5), we might intuitively expect that the time delay needed to produce an increase in the size of the carbon chain (e.g., to go from $\text{C}_2\text{H}$ to $\text{C}_6\text{H}$ via the reaction $\text{C}_2\text{H} + \text{C}_4\text{H}_2$ followed by the photodissociation of $\text{C}_4\text{H}_2$) should result in a radial shift, in which the larger carbon chains should appear later in the expansion, and thus farther from the star. Such behavior is neither predicted by the chemical model nor observed in the maps, which is a consequence of the rapidity at which photochemistry takes place compared with the expansion of the envelope in IRC +10216. This finding is important, since it limits the use of the brightness radial distributions of $\text{C}_2\text{H}$, $\text{C}_4\text{H}$, and $\text{C}_6\text{H}$ as a chemical clock. The chemical model predicts that a significant radial stratification with hydrocarbon radicals $\text{C}_2\text{H}$ of increasing size would only take place if the chemical reactions were significantly slower or the expanding wind were significantly faster. We stress that this conclusion is reached using numerical simulations to model the circumstellar chemistry, and that simple timescale arguments may lead to erroneous conclusions.

The CN-bearing species show more diverse brightness radial distributions than the hydrocarbon radicals as a result of a slightly different chemistry. We first note that the emission of the radical CN shows a rather broad radial distribution, extending to radii greater than 30\arcsec. This observational fact is correctly predicted by the chemical and excitation model. The slower photodissociation rate of HCN, compared to that of $\text{C}_2\text{H}_2$, is at the origin of the much more extended radial distribution of CN emission with respect to that of $\text{C}_2\text{H}$. A second interesting aspect is that the observed emission of $\text{HC}_3\text{N}$ appears at rather short radial distances (i.e., inside of 10\arcsec), a fact that is fairly well reproduced by the model. This early appearance is related to the fact that $\text{HC}_3\text{N}$ is mainly formed in the reaction between $\text{C}_2\text{H}_2$, a parent molecule that is injected from the innermost circumstellar regions and is destroyed by photodissociation in the outer envelope, and CN, a daughter species that is formed by photodissociation of HCN. Therefore, $\text{HC}_3\text{N}$ must be formed when the abundances of both reactants, having nearly complementary distributions, are high enough. This situation occurs in a transition region of the envelope where the abundance of acetylene decreases as the gas expands, while that of CN increases. Thus, species whose direct precursor is a parent species may be considered as first-generation daughter species as opposed to second-generation daughter species, which are instead formed from precursors that are themselves daughter species. First-generation daughter species, such as $\text{HC}_3\text{N}$, thus tend to appear earlier in the expansion than second-generation daughter species, such as the radicals $\text{C}_2\text{H}$, $\text{C}_6\text{H}$, and $\text{C}_5\text{N}$. The observed emission of the longer cyanopolyne $\text{HC}_5\text{N}_2$ rises at larger radii than that of $\text{HC}_3\text{N}$, an observational fact that is not reproduced by the model, which instead predicts similar radial distributions for the two cyanopolyynes in terms of both the abundance and the $\lambda$ 3 mm emission. The early appearance of $\text{HC}_3\text{N}$ in the model can be traced to the important contribution of the formation route involving the $\text{C}_5\text{N}+$ $\text{C}_2\text{H}_2$ reaction, which involves as reactant the parent species $\text{C}_2\text{H}_2$ and thus occurs in more inner regions than the other important $\text{HC}_5\text{N}$-forming reaction $\text{CN} + \text{C}_2\text{H}_2$. Stated differently, the model predicts for $\text{HC}_3\text{N}$ a more marked character of first-generation daughter species than suggested by observations. The discrepancy for $\text{HC}_3\text{N}$ is more likely due to the chemical model rather than to the excitation and radiative transfer calculations.

An interesting piece of information is provided by the availability of observational data for the electronic closed-shell molecule $\text{HC}_5\text{N}_2$ and its photodissociation descendant $\text{C}_5\text{N}$. The observations show that the brightness distribution of $\text{C}_5\text{N}$ is shifted to outer radii with respect to that of $\text{HC}_3\text{N}$ (see the bottom right panel in Fig. 6), a result that is well reproduced by the current model. This result suggests that analogous pairs of species, whose spatial distribution may be more difficult to map, may behave similarly as, for example, occurs for the pair $\text{HC}_5\text{N}/\text{C}_5\text{H}$, in which the rotational lines of the radical are too weak to map, or the pairs $\text{C}_5\text{H}_2/\text{C}_6\text{H}$ and $\text{C}_6\text{H}_2/\text{C}_7\text{H}$, where the polyynes lack a permanent dipole moment.

A last aspect that is worth discussing concerns the fact that the model assumes a density radial distribution that decreases smoothly with increasing radius, while observations show that a good fraction of the circumstellar matter is locked into clumpy arcs. The non-uniform density structure can affect the abundance and emission radial distributions of the molecules in different ways. First, external ultraviolet photons can more easily...
penetrate the regions between clumps where the density of gas and dust is depressed, allowing photochemical processes to take place inside the envelope (Decin et al. 2010; Agúndez et al. 2010). This effect can explain the formation in inner circumstellar regions of some key molecules such as the hydrides H$_2$O and NH$_3$, for which conventional chemical models are not able to account for their formation. In contrast, our ALMA observations show that carbon chains, which are efficiently produced by photochemistry, are confined to the outer envelope, with no or little presence in inner regions. The action of photochemistry in the inner envelope must therefore affect only a few selected regions or be selective with respect to the formation of different types of molecules owing to, for example, temperature effects (warm photochemistry in inner regions vs. cold photochemistry in the outer envelope). Second, the existence of shells and arcs where the density is enhanced compared to the surrounding medium may provide shelters to carbon chains, because the enhanced densities boost the rates of carbon chain reactions and provide a more efficient production of CN-containing species CN, C$_2$H, and HC$_3$N. All of these species show a radial stratification, with HC$_3$N appearing at shorter radii and the CN radical extending out to larger radii. This behavior is reasonably well reproduced by our chemical model, which validates a scenario of carbon chain growth initiated by photodissociation of acetylene and hydrogen cyanide, rapid gas-phase chemical reactions of C$_2$H, and C$_2$H radicals with unsaturated hydrocarbons as the main mechanism responsible for the growth of polyynes, and reactions of CN and C$_2$N radicals with unsaturated hydrocarbons as the dominant formation route for cyanopolyynes.

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Appendix A: Emission maps in different rotational transitions of C\textsubscript{4}H, C\textsubscript{3}N, HC\textsubscript{3}N, and HC\textsubscript{5}N

The radicals C\textsubscript{4}H and C\textsubscript{3}N have several rotational transitions \(N-(N-1)\) in the \(\lambda\) 3 mm band, each split into two closely spaced spin-rotation doublets of nearly equal intensity labeled as “a” and “b” (see Figs. A.1 and A.2), while the cyanopolyynes HC\textsubscript{3}N and HC\textsubscript{5}N also have several rotational transitions within the frequency range covered (see Fig. A.5). Here we present the emission maps of each individual line and discuss whether the different lines of a given species have brightness distributions significantly different among them and whether the individual maps show any anomalies.

In Figs. A.1 and A.2 we show the brightness distributions of each component of the doublet rotational transitions for the radicals C\textsubscript{4}H \((N = 9–8 \text{ through } N = 12–11)\) and C\textsubscript{3}N \((N = 9–8 \text{ to } N = 11–10)\). The upper level energies of these transitions, in the range 20.5–35.6 K for C\textsubscript{4}H and 21.4–31.3 K for C\textsubscript{3}N, do not differ enough so to expect important differences in the excitation, which could in turn lead to significantly distinct emission distributions. Apart from some slight differences in the absolute intensities, the brightness distributions of the lines of C\textsubscript{3}N are very similar both in the locations of the maxima and the arrangement of the arcs that shape the overall ring. The same is also true for C\textsubscript{4}H, with the exception of the anomaly in the map of the \(N = 12–11\) \(b\) transition. This line shows the same ring structure seen in the rest of the C\textsubscript{4}H lines, but there is also a compact component centered on the star that is not resolved by the \(1'14 \times 0'98\) synthesized beam. If the compact emission...
were to arise from C$_2$H, it would be very difficult to explain why it is only seen in this line while there is no hint of it in the maps of the other seven lines of C$_2$H. Instead this compact emission arises from CO $J = 1-0$ in its first vibrationally excited state, whose rest frequency, 115 221.754 MHz, is only 0.7 MHz away from that of the $N = 12-11$ b transition of C$_2$H. Emission from CO in the vibrational state $v = 1$ had been detected in IRC+10216 in the pure rotational transitions $J = 2-1$ and $J = 3-2$ with the Submillimeter Array (SMA) by Patel et al. (2009). The emission in these lines remains unresolved with an angular resolution of ~2\arcsec, while that from the $J = 1-0$ line we have detected remains unresolved with an angular resolution of ~1\arcsec, indicating that the emission from CO $v = 1$ arises from a region closer than $\sim 10^{13}$ cm ($\sim 25$ $R_\odot$) to the star. It is also worth noting that recently, emission from the pure rotational transition $J = 3-2$ of CO in the vibrational state $v = 1$ has been observed using ALMA with sub-arcsecond resolution in five additional AGB stars (Khouri et al. 2016), pointing to a line-formation region closer than $\sim 10$ $R_\odot$ in radius.

In Fig. A.3 we show the brightness distribution of C$_2$H in the rotational transition $N = 24-23$, lying at 228.3 GHz. The map corresponds to an average of the two spin-rotation components in the central velocity channel and was obtained with ALMA band 6 during Cycle 2. More details on these observations will be given elsewhere (Guélin et al., in prep.). The map of this line shows the same structure of thin shells and inter-crossing arcs displayed by the $J = 3$ mm lines of C$_2$H, but seen at a higher angular resolution, ~0.3\arcsec, and with a higher contrast because part of the extended emission filtered out by the interferometer has not been recovered owing to the lack of short-spacings data.

According to the ALMA maps of the four doublet lines of C$_2$H shown in Fig. A.1 and the transition shown in Fig. A.3, the emission of C$_2$H is clearly restricted to the outer hollow shell, with no emission arising from the surroundings of the star. Cooksy et al. (2015), however, find in their SMA maps of the doublet line $N = 27-26$ of C$_2$H that there is compact emission centered on the star. This doublet, lying at 256.9 GHz, has been covered in our ALMA Cycle 0 observations of IRC+10216, a large portion of which has been already published (Cernicharo et al. 2013; Velilla Prieto et al. 2015; Agúndez et al. 2015; Quintana-Lacaci et al. 2016). As shown in Fig. A.4, at velocities around $V_{\text{LSR}} = V_{\text{sys}}$, the outer ring is barely seen in our ALMA Cycle 0 data because the size of the ring is larger than the field of view (~23\arcsec) and thus this emission is not properly sampled. In contrast, compact emission around the star is clearly seen, but only in the b component of the $N = 27-26$ doublet and not in the a component. This was not recognized in the data shown by Cooksy et al. (2015) because these authors stacked the maps of the two components of the doublet to improve the sensitivity. As shown for the C$_2$H $N = 12-11$ doublet in Fig. A.1, it is more likely that the compact emission seen in the map of the $N = 27-26$ b component does not arise from C$_2$H but rather from a different carrier that has a transition which accidentally coincides with the $N = 27-26$ b component of C$_2$H. At this stage we do not have a fully convincing assignment for this line, but the emission maps of the entire set of $J = 3$ and $1$ mm lines of C$_2$H strongly support that this species is only present in the outer shell and not in regions close to the star.

There are several rotational transitions of cyanoacetylene and cyanodiacylente in the $J = 3$ mm band observed here. For HC$_3$N just three lines are covered, from $J = 10-9$ to $J = 12-11$. These transitions have similar upper level energies, in the range 24.0–34.1 K, and thus, like the carbon chain radicals, we do not expect great differences in their excitation, and thus in their emission distribution. The maps of brightness of these three lines, centered on the systemic velocity, are shown in the top panels of Fig. A.5, where it can be seen that there are indeed no substantive differences.

For HC$_3$N, 12 rotational lines, ranging from $J = 32-31$ through $J = 43-42$, have been covered. These transitions involve upper levels with energies from 67.5 to 120.9 K, i.e., substantially higher than those involved in the HC$_2$N transitions. The emission maps of each individual line of HC$_3$N (see a sample in the lower panels of Fig. A.5) show that there is a noticeable decline in intensity with increasing $J$. This decrease in line intensity can be understood as a consequence of a less efficient excitation of levels of increasing energy in the outer shell at ~15\arcsec from the star, where the gas kinetic temperature and the volume density of particles are expected to be just 10–30 K and
Fig. A.5. Brightness distributions of the $J = 10–9$, $J = 11–10$, and $J = 12–11$ lines of HC$_3$N (top panels), and $J = 32–31$, $J = 35–34$, and $J = 38–37$ lines of HC$_5$N (bottom panels), averaged over the central 3 km s$^{-1}$ of each line. The size ($\sim 1''$ for all lines) and shape of the synthesized beam is shown in the bottom left corner of each panel. The maps are centered on the position of the star, indicated by a cross.

(1–5) $\times$ $10^4$ cm$^{-3}$. As such, one might reasonably expect some radial shift in the emission peak between low-$J$ and high-$J$ lines, the latter being more easily excited at shorter radii because of the higher temperatures and densities. At current angular resolution and sensitivity of the measurements, there is no evidence of such shift among the $\lambda$ 3 mm lines of HC$_5$N, whose emission distributions appear quite similar. It therefore seems that the structure of density enhancements in the form of arcs and shells is much more important than differential excitation effects in shaping the brightness distributions. The same is found for C$_4$H, C$_3$N, and HC$_3$N, where the transitions that we mapped involve levels with more similar energies. Therefore we conclude that regardless of the particular $\lambda$ 3 mm transition adopted for any of the carbon chains studied here, the brightness distribution is a good proxy of the spatial distribution of the species. Keller et al. (2015) have recently presented preliminary results on $\sim 1''$ angular resolution VLA maps of cm-wavelength rotational lines of carbon chains in IRC +10216. These transitions involve rotational levels with energies significantly below those associated to the $\lambda$ 3 mm lines presented here, and thus it will be interesting to see if there are significant differences in the distribution of the emission of cm- and 3 mm-wavelength lines that could arise from excitation effects.