A Review of Modeling Rotating Packed Beds and Improving Their Parameters: Gas–Liquid Contact

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Abstract: The aim of this review is to investigate a kind of process intensification equipment called a rotating packed bed (RPB), which improves transport via centrifugal force in the gas–liquid field, especially by absorption. Different types of RPB, and their advantages and effects on hydrodynamics, mass transfer, and power consumption under available models, are analyzed. Moreover, different approaches to the modeling of RPB are discussed, their mass transfer characteristics and hydrodynamic features are compared, and all models are reviewed. A dimensional analysis showed that suitable dimensionless numbers could make for a more realistic definition of the system, and could be used for prototype scale-up and benchmarking purposes. Additionally, comparisons of the results demonstrated that Re, Gr, Sc, Fr, We, and shape factors are effective. In addition, a study of mass transfer models revealed that the contact zone was the main area of interest in previous studies, and this zone was not evaluated in the same way as packed beds. Moreover, CFD studies revealed that the realizable k-ε turbulence model and the VOF two-phase model, combined with experimental reaction or mass transfer equations for analyzing hydrodynamic and mass transfer coefficients, could help define an RPB system in a more realistic way.

Keywords: absorption; HiGee; CFD; intensification; hydrodynamics

1. Introduction

Process intensification (PI) is defined as an engineering application utilized to improve sustainability, cleaning, safety and energy efficiency. PI in mass transfer (MT) involves three main methods: rotating, mixing, and vibrating [1]. There are good reviews available on PI that provide more details on this topic [2,3]. Researchers have been using the advantages of centrifugal fields for more than 65 years [4]. A rotating packed bed (RPB) contactor is a piece of PI equipment, also called a “HiGee” (high g) because of the high gravity applied in this contactor by the centrifugal force used for increasing the contact of phases [5]. This device was first patented in 1963, and includes concentric rings for packing purposes [6]. Industrial applications of this equipment started in the 1970s when Imperial Chemical Industries worked on technology derived from NASA research projects [7]. Almost a decade later, Ramshaw and Mallinson presented a report on NH₃ absorption and MT coefficient intensification using an RPB for the first time [8]; later, this technology was licensed by Glitsch in the USA [9]. Investigations into and the development of RPBs were have been out by numerous researchers in many MT and reaction fields, such as distillation. Several kinds of RPB have been reviewed and their advantages discussed in [10], while the results and some of their industrial applications are presented in [11].

As CO₂ emissions are now a global concern, investigations in this field employ three main approaches: post-combustion, oxy-fuel combustion, and pre-combustion for CO₂ capture [12,13]. Chemical absorption has been applied and developed more extensively in
post-combustion than in other industrial processes [14]. Therefore, a large amount of waste is produced by the use of certain conventional gas treatment packed bed columns (PBCs), and this approach requires high quantities of absorbent solvents in order to prevent hydrate formation with the small quantities of other components, such as CO₂ and H₂S. The most common acidic gas removal problems include absorption heat, high energy consumption for regeneration, and amine solutions’ corrosive nature and temporal degradation [15,16]. The previous field studies on chemical absorption will be explained, along with some brief examples, below.

1. Absorbent formulation, in which a highly soluble, reactive, absorbent, and aqueous solution of alkanolamines is made and blended by adding activators or promoters, such as sterically hindered amine AMP, and effective promoters, such as PZ.

2. Process intensification involves the application of PI techniques or devices and optimization parameters. This category contains many techniques that can be considered to enhance transport in numerous processes, such as bioremediation [17], water deaeration [18], and absorption. As regards devices, many popular contactors are available, such as rotating discs, membranes, and RPBs.

For instance, Hosseinzadeh et al. [19] examined CO₂ capture with a hallow fiber membrane contactor (HFMC), using MEA to increase the chemical reaction rate and the contact of phases. M. Theils et al. [20] performed a comparison between several arrangements of PBs and RPBs, and demonstrated that reducing the packing volume in the RPBs resulted in equal removal efficiencies. Additionally, this kind of method is applied in many fields, and the simultaneous application of the above two intensifying absorption methods (a and b) can offer advantages such as energy reduction in thermal regeneration using an RPB on MEA–CO₂ system, as reported by Cheng et al. [21]. Their results show that the same regeneration efficiency in PBCs could be achieved with RPBs that were at least 10 times smaller than the PBCs, and they demonstrated that RPBs had higher MT and heat transfer coefficients and involved less HTU and regeneration energy consumption. Other benefits of this approach have also been reported. An investigation into CO₂ capture with water-based NFs (absorbing solutions) in HFMC revealed possible enhancements to MT and removal efficiency [22]. In addition, Luo et al. [23] reported that the relative effective gas–liquid interfacial surface area and volumetric liquid-side MT coefficient were both increased when using ultrasonic induction, in comparison with an RPB without ultrasonic induction under the same conditions. These approaches, referred to as hybrid processes, have been further discussed in [24].

RPB is a piece of equipment that operates via centrifugal acceleration, which affects the hydrodynamics to induce PI. Therefore, improving an RPB’s characteristics via hydrodynamic analysis is the main goal of this investigation. In this paper, the status of the gas–liquid contact in the RPB, and especially the absorption processes taking place in various models and methods, have been evaluated and reviewed. The comparison of publications shows that various configurations of RPBs have been developed to expand contact zones and effective surface areas, and to achieve a higher MT and capacity, as well as a reduced pressure drop.

In the first section, the main concepts, such as the advantages of centrifugal gravity, the geometry and classification of RPB, the directions of investigations (i.e., hydrodynamic and mass transfer enhancement) and modeling outlooks, are described. In the second section, the modeling of hydrodynamic parameters and their development to attain accurate systems are analyzed. In the third section, the developments in the modeling of MT’s parameters as regards its rate are studied. Finally, in the last sections, two powerful methods suitable for hydrodynamic analysis and scaling-up, as well as the effects of centrifugal gravity on the dimensionless numbers that form the main focus of this analysis, are reviewed and evaluated. Here, all the above-mentioned items are reviewed simultaneously, because no previous review has evaluated all the parameters that together characterize the RPB.

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2. RPB Advantages and Configurations

An RPB contactor consists of packing mounted on a horizontal/vertical shaft (rotor), casing, and a liquid distributor. A simple conventional RPB is made up of a rotor enclosed in casing, with a liquid distributor that injects liquid into the packing center. The packing is divided into three zones: the bulk packing, the end-effect (the part near the inner edge of the rotor), and cavity zones, which are between the outer edge of the packing and the inner edge of the casing [25]. The acceleration in RPBs (typically 1000 g) is greater than that in PBCs, which allows for improved micro-mixing, as demonstrated, for instance, by the experimental results of Yue’s investigation of an RPB [26]. The high gravity leads to higher gas–liquid interfacial surface area accessibility in RPBs, compared with conventional PBCs.

Ramashaw and Mallinson applied average centrifugal accelerations of up to 1000 $\times g$, and showed that the MT coefficient would increase by $\omega$, with a power of 0.28–1.08 [8]. This was confirmed in other studies, such as those by Guo et al. [27] and Liu et al. [28], and in reports on MT coefficients, which examined parameters of 1500 rpm and higher. Tsai et al. conducted a similar experiment and added 38% to the MT coefficient’s value, with an annular speed increase from 600 to 1800. They reported that this was due to the boundary layer thickness reduction [29]. On the other hand, the liquid film becomes thinner with higher annular speeds and greater radii from the axis, due to the lower difference between the phase interface and average bulk concentrations [30]. Additionally, the effective surface has been shown to increase with an increase in the $\omega$ [31]. Lin et al. examined the effective surface area, which they increased from 5.9 to 31.7 m$^2$/m$^3$ by increasing the rotational speed from 600 to 1800 rpm [32].

Chen et al. examined the liquid hold-up in two RPBs with different sizes of packing and with rotations of 300–1500 rpm (providing 4–152 g), and showed that the liquid hold-up was reduced with an increase in $\omega$ [33]. The MT rate directly depends on hold-up, which is a function of the rotational speed, and $\omega$ directly depends on the radius of the packing [34]. Furthermore, the rate of pressure drop within the RPB increases with an increased rpm, as illustrated by the results of Zheng et al. and Sandalia et al. [35,36]. Additionally, as examined and discussed in [37,38], the height of transfer unit (HTU) achieved in an RPB is lower than that in a PBC under the same conditions.

Some researchers focused on acidic gas removal efficiency, showing that it increased with an increase in the rpm [39,40]. Moreover, Thiels et al. [20] demonstrated that a lower packing volume was required at higher rpms than at lower ones to achieve the same value of removal efficiency.

Based on the above information and in order to optimize the RPBs, many researchers have refined the operation parameters of RPB contactors by focusing on increasing the contact between the phases and staging, which allows better feed injection between the stages and increases the capacity of the contactor. A summary of US patents registered in 1935–2018 is given in Table 1, which shows that US patent development has been focusing on modifying RPBs to increase their contact zone. More detailed information about several patents can be found in [6].
Table 1. US RPB patents published in 1939–2018.

| Type of Rotor | CCF                  | Improvements                              | Patent No.     | Inventor(s)                        | Published Year |
|---------------|----------------------|--------------------------------------------|----------------|------------------------------------|----------------|
| Single CC     | Contact zone and    | US 2,172,222 W. J. Podbielniak [41]       | 1939           |                                    |                |
|               | seals                | US 2,281,796 W. J. Podbielniak [42]       | 1935           |                                    |                |
|               | Contact zone         | US 2,758,783 W. J. Podbielniak [43]       | 1951           |                                    |                |
|               | Contact zone, reduced entrainment | US 2,878,993 W. J. Podbielniak [44] | 1959           |                                    |                |
|               | Contact zone, increased capacity | US 2,941,872 C. W. Pilo et al. [45] | 1960           |                                    |                |
|               | Contact zone         | US 3,034,730 C. W. Pilo et al. [46]       | 1962           |                                    |                |
|               | CC                   | US 3,233,880 W. J. Podbielniak [47]       | 1962           |                                    |                |
| Multi-rotor   | Contact zone, increased capacity | US 3,344,981 W. J. Podbielniak [48] | 1965           |                                    |                |
| Single CC     | Contact zone         | US 3,415,501 C. W. Pilo et al. [49]       | 1965           |                                    |                |
| Multi-rotor   | Contact zone, increased capacity | US 3,486,743 D. B. Todd [50] | 1967           |                                    |                |
| Single CC & COC | Contact zone     | US 4,283,255 C. Ramshaw and R. H. Mallinson [8] | 1981           |                                    |                |
| Single CC     | Liquid distribution and contact zone | US 4,397,794 C. W. Pilo [51] | 1981           |                                    |                |
| Single CC     | Liquid distribution and contact zone | US 6,884,401 B2 S. Yang et al. [52] | 2002           |                                    |                |
| Multi-rotor   | CC & COC             | US 7,344,126 B2 J Ji et al. [53]          | 2004           |                                    |                |
| Single CC & COC | Contact zone     | US 8,448,926 B2 M. D. Mello et al. [54] | 2011           |                                    |                |
| Multi-rotor   | CC & COC             | US 20130319235A1 H. Wolf et al. [55]      | 2012           |                                    |                |
| Single CC & COC | Contact zone     | US 20160317967 A1 M. Kotagiri et al. [56] | 2016           |                                    |                |
| Single CC     | Contact zone         | US 20170028311A1 B. K. Namdeo et al. [57] | 2017           |                                    |                |
| Two stages    | CC & COC             | US 20170157554A1 C. H. Yu and C. S Tan [58] | 2017           |                                    |                |
| Multi-rotor   | CC & COC             | US20180016159A1 M. V. D. e Mello et al. [59] | 2018           |                                    |                |

CCF: contacting conditions of fluids; CC: counter-current; COC: co-current; MTP: mass transfer process.

The different RPB names depend on the structure of the rotor, e.g., baffle [29] and blade [60], the bulk zones of which consist of baffles or blades, respectively; split (RSB) [61], the rotor of which includes dual packings rotating in the same or opposite directions; zigzag (RZB), which comprises a special rotor with a zigzag flow direction [62].

Generally, RPBs can be classified according to six criteria, as shown in Figure 1.
Contact zone, reduced entrainment

Comparing the cross-current and countercurrent flows of simple RPBs, Chia-Chang Lin et al. investigated CO\textsubscript{2} removal using caustic solution, and reported that the $K_{GA}$ values of the cross-current flows were higher than those of the countercurrent flows [63]. In the same year, G. Q. Wang et al. [62] developed RZBs with similar MT efficiency and better operability and turn-down ratios. This contactor was first patented in 1952 by Kapitza [64]. After consulting the review papers of Visscher et al. [65] and Wang et al. [66], which were published in 2013 and 2019, respectively, the advantages of RZBs over simple RPBs may be listed as follows:

1. less maintenance due to their static seal;
2. possibility of multiple feeds and more flexibility;
3. no need for liquid distributors;
4. more liquid hold-up and residence time;
5. multi-rotor operability on one shaft.

Additionally, Wang et al. [67] contributed to RZB optimization by making modifications to its structure.

The disadvantages of this kind of RPB in comparison with simple RPBs include a lower MT rate, which is attributed to the replacement of packings with baffles and rings, and higher power consumption.

RPBs equipped with blades and RPBs with a number of liquid inlets have greater MT efficiency than simple RPBs due to the intensified MT rate in their end-effect zone, as Guang-Wen Chu et al. reported [68].

Moreover, counter-rotation RSBs achieve greater MT efficiency than the co-rotation type [69]. Furthermore, the benefits of an RZB over an RPB include the possibility of additional feed streams, the replacement of a dynamic seal with a static one, the need for fewer liquid streams for distributors, greater liquid hold-up, and the operability of stages by one rotor [65].
Different layouts with RPBs or PBCs in series or in parallel may help to achieve specific process parameters [70]. For instance, C. H. Yu et al. [71] studied the effect and removal efficiency of these configurations by examining eight single-, parallel- and series-mode configurations of RPBs and PBCs with MEA, and showed that the greatest level of gas treatment was achieved with two RPBs in a parallel mode, the regeneration energy consumption of which was approximately equal to that of a PB.

3. Modeling Rotating Packed Beds

RPB contactors can be modeled via various approaches based on the MT’s characteristics and hydrodynamic analysis, as shown in Figure 2. Theoretical and mechanical models help us to comprehend the nature of gas–liquid flows and reactions. These methods result in significant discrepancies with experimental data due to the simplification of assumptions. Statistical and empirical methods developed to increase accuracy rely on semi-empirical and statistical regressions. Generally, these models give acceptable results, but due to their dependency on experimental data, it is not possible to infer general correlations from these models. Numerical simulation is another useful approach, and it is categorized into chemical-based and computational fluid dynamics-based (CFD) types, which are more detailed and accurate in comparison with previous methods [72]. Additionally, in the context of CFD complexity and the numbers of empirical model errors, machine learning, or artificial intelligence, is another method that has been developed by researchers such as Saha, who used artificial neural networks (ANN) to estimate the overall gaseous MT coefficient by applying the radial basis transfer function [73]. Lashkarbolooki et al. [74] employed ANN for pressure drop modeling and estimation in RPBs under various operations. Zhao et al. [75] proposed an intelligent approach to MT coefficient estimation in CO$_2$–NaOH systems by employing the radial basis transfer function. Saha reported that the developed model was more accurate than multiple nonlinear regression and ANN. Li et al. [76] applied three ANN models to simulate adsorption in RPBs. Liu et al. [77] developed an ANN-based approach for biosorption modeling, which was used the Re$_G$, Re$_L$, maximum contact time, ratio of particle diameter to bed height (D$_{particle}$/Z), and ratio of initial concentration to packing density, as input variables. Recently, Liu et al. employed ANN to a model and estimated the overall MT coefficient ($K_{L,a}$) in the ozone absorption process in RPBs, using input variables such as Re$_G$, Re$_L$, Fr$_L$, and We$_L$. [78].
3.1. Hydrodynamic Modeling

Hydrodynamics is the study of fluid motions [79] and includes pressure drop, flooding and liquid hold-up [79]. Basic and detailed experimental research is required for explaining hydrodynamics and MT in RPBs, as well as their correlations [80]. On the other hand, MT performance strongly depends on fluid flow patterns [66]. The hydrodynamic parameters employed for RPB scale-up and design [81], which are going to be reviewed in this section, are shown in Figure 3. Regarding these important issues, investigators have determined many correlations for three models—flooding, pressure drop and hold-up models—as described below.

![Hydrodynamics of RPBs](image)

**Figure 3.** Approaches to the modeling of hydrodynamic parameters.

3.1.1. Liquid Behavior and Hold-Up

The liquid patterns in RPBs can be classified into the three categories of droplet flows, film flows and pore (thread or ligaments) flows, which were proposed by Burns and Ramshaw [82] following visual observation and photography, which confirmed the presence of pore and droplet pattern flows, as shown in Figure 4.

![Liquid behavior](image)

**Figure 4.** Liquid flow patterns in an RPB.

When the rotational speed is between 300 and 600 rpm, the pore flow regime is the dominant pattern in the RPB, wherein the liquid primarily flows in the form of radial rivulets, while the zones between them are empty, and this leads to a reduction in the MT effective surface area. When the rotational speed exceeds 600 rpm, the liquid’s behavior changes to a droplet flow and then to a film flow pattern [27,82,83]. Generally speaking, centrifugal increments make film flows thinner and cause the mass fluxes to increase [84].

Generally, the most prominent visualization techniques for determining flow fields and behavior in packed beds include gamma scanning [85], tomography [86], X-ray [83], PIV measurement [87], RTNR [88], and CCD camera [89].

S. Munjal et al. illustrated that δ was affected by the liquid kinematic viscosity, flow rate, packing radius and annular speed of RPBs [30]. Later, researchers developed empirical correlations for predicting the thickness of liquid elements. A brief summary of these correlations, developed between 2000 and 2020, is given in Table 2, which confirms
the results of Manjal et al.’s study and illustrates that the liquid’s properties, along with packing configuration and rotation rate, determine the amount of $\delta$.

Some investigators applied the above findings in the hydrodynamic analysis of RPBs in their studies. X. Li et al. [90], for example, reported that when the acceleration was lower than 60 g in a rotating fin baffle packed bed contactor, the dominant regime was film flow, and that Guo et al.’s correlation could be used to calculate the thickness of the liquid film. This correlation, as shown in Table 2, demonstrates that liquid thickness reduces when the rotational speed increases.

Sang et al. [91] analyzed fluid patterns in RPBs with high-speed photography. They found that the liquid flow would take the form of ligaments, which exited the packing at lower rotational speeds (pore flow) and grew in numbers at higher speeds, then finally disappeared. Drawing on the results of their study, they categorized liquid patterns into ligament or pore flows and droplet flows, suggested six parameters that affect the flow regime, and proposed a criterion to determine the regime based on the relation between the Re and We numbers via the new dimensionless number of $q$, which is defined by the liquid’s initial velocity, the annular speed, and the outer rotor diameter.

Additionally, Sang et al. reported that most of the MT in the cavity zone of their RPB was carried out by droplet collisions with the casing wall. They considered the deposition splashing of a liquid (droplets) using Ohnesorge and Reynolds numbers. They proposed a set of criteria relation criteria named “splash criteria”, and reported that the MT in the cavity zone was due to droplet interaction with the inner wall of the casing [25].

Li et al. studied the liquid flow situation in an RPB with a charge-coupled device (CCD) camera [89]. They reported the non-continuity of film–ligament droplets at low velocities and weaker surface tension at higher velocities, showing that the liquid flow turned into droplets at higher velocities. Moreover, they argued that the break-up and coalescence of liquids may occur when droplets fly in RPBs, which is determined by

$$We = \frac{\rho \left| v_L - v_G \right|^2 D}{\sigma_L} > 12$$  \hspace{1cm} (1)

where Weber numbers lower than 12 indicate that liquid breaking occurred in the cavity zone. They proposed a correlation with a $\pm 15\%$ error using

$$d = 5.03 \times N^{-0.347} \nu_0^{0.183}$$  \hspace{1cm} (2)
Table 2. Estimation of liquid element thickness via empirical correlations.

| Author           | Year | RPB Type       | Kind of Packing        | Liquid Form                                                                 | Correlation                                                                 |
|------------------|------|----------------|------------------------|-----------------------------------------------------------------------------|-----------------------------------------------------------------------------|
| Burns et al. [92]| 2000 | Glass sphere   |                        | $\delta = 2.25 \left( \frac{u_L \omega}{\rho_{L} \sigma} \right)^{1/3}$  | $\delta = 2.59 \left( \frac{u_L \omega}{\rho_{L} \sigma} \right)^{1/3} \frac{1 - (1 - K)^2}{K^{2/3}}$: Inertia flow  |
| C. C. Lin et al. [93] | 2000 | Glass sphere   |                        | $\delta = 4Q \frac{d}{L_{in}} \delta = \frac{1}{K_{c}} \int_{R_i}^{R_c} \delta \, dR$ | For complete wetted packing: $\delta = 4106\nu_{L}^{0.454} \mu_{G,j}^{-0.002} \omega^{-0.104}$  |
| Chen et al. [33] | 2003 | Metal wire mesh|                        | $\delta = 4Q \frac{d}{L_{in}} \delta = \frac{1}{K_{c}} \int_{R_i}^{R_c} \delta \, dR$ | For partial wetted packing: $\delta = 2055\nu_{L}^{0.183} \mu_{G,j}^{0.003} \omega^{-0.109}$  |
| Yi et al. [94]   | 2009 | Wire mesh      |                        | $d = [0.826 + 17.4(r - r_i)]d_1$, $r - r_i < 0.01$ m Cavity zone          | $d = 12.84 \left( \frac{\sigma}{\rho_{L} \omega^2} \right)^{0.63} \mu_{L}^{0.201}$ Bulk zone |
| Li et al. [95]   | 2009 | Wire mesh      |                        | $d = [0.826 + 17.4(r - r_i)]d_1$, $r - r_i < 0.01$ m Cavity zone          | $d = 12.84 \left( \frac{\sigma}{\rho_{L} \omega^2} \right)^{0.63} \mu_{L}^{0.201}$ Bulk zone |
| Yang et al. [96] | 2010 | Wire mesh      |                        |                                                                               |                                                                               |
| Sang et al. [91] | 2017 | Wire mesh      |                        |                                                                               |                                                                               |
| Sang et al. [97] | 2019 | Simple         | Wire mesh              |                                                                               |                                                                               |
| Wang et al. [98] | 2020 | Wire mesh      |                        |                                                                               |                                                                               |
| Su et al. [99]   | 2020 | Metal wire mesh|                        |                                                                               |                                                                               |
Recently, Hacking et al. [100] examined several kinds of concentric redistribution rings in an RPB operated in the speed range of 500–1200 rpm, and reported that this type of liquid distribution could improve the uniformity of liquid distribution, thus increasing the wetting and effective surface areas and reducing the channeling area in the packing zone.

In PBCs, it is important to know the hold-up in order to determine the dynamics of the tower, because this affects the mass transfer and pressure drop. In addition, the hold-up directly affects the operating weight of PBCs and, therefore, the design of the supports [101]. The term “hold-up” describes the volume of liquid present on the surface of the packing in the form of a film or ligaments, or droplets in the voidage of the packing in the form of rivulets. There are two types of hold-up: static and dynamic (operating). The first term refers to the liquid inventory in the packing where gas and liquid do not flow, and the second one refers to the liquid inventory when both liquid and gas flow. The hold-up in random packing is defined by the summation of both (static and dynamic) the terms [102]. Most researchers report total hold-up, and do not establish this parameter separately in their correlations [102]. Hold-up estimation allows for the determination of residence time in the packing, and is especially important when the system contains a special mixture that is sensitive to temperature or reactive absorption processes [103]. There are many correlations available to help predict the liquid hold-up in PBCs [104,105], but because of the existence of radial flows in an RPB’s geometry, the liquid hold-up equations for RPBs are not the same as those for PBCs. The rotational speed reduces the hold-up and simplifies the gas passage, as Lashkarbolooki [106] showed. Theoretically, the mean hold-up in RPBs may be defined by the following equations [93]:

\[ h_L = \frac{V_L}{V_B} \]  
\[ V_B = \pi \left( R_o^2 - R_i^2 \right) Z \]  

Other methods for hold-up measurement, such as gamma absorption [103], conductance measurement [107] and the neural network method [108], are empirical.

Basic and Dudukovic [107] defined a correlation, according to their empirical data, using Re and Ga numbers and packing characteristics. F. Guo et al. focused on cross-flow simple RPBs equipped with wire gauze packings, and determined the amount of hold-up by considering the ratio of the liquid area flow rate to the liquid mean radial velocity [27]. C. C. Lin et al. [93] developed a correlation via the theoretical analysis of liquid hold-up for a simple counter-current RPB based on one rotating disk. They modeled their work on the layers of hypothetical rotating disks, and verified their analysis with experimental pressure drop data. Considering the mean liquid film, they described the hold-up thickness as follows:

\[ h_L = \bar{\delta} \times a_w \]  
\[ \bar{\delta} = \frac{1}{R_o - R_i} \int_{R_i}^{R_o} \delta \, dr \]  

Finally, according to their experimental data, they proposed a prediction correlation to estimate the hold-up for co-current systems that used the modified Galileo number, Ga*.

In the same year, Burns et al. [92] reported that hold-up prediction for RPBs can be performed using the following equations for pore and droplet flows, respectively.

\[ h_L = 1.41 \frac{\mu_L}{a_L^2 \delta_{pore}^2} \left[ 1 - \frac{(1 - K)^{1/2}}{K^{1/2}} \right], \quad 0 < K < 1 \]  
\[ h_L = 1.41 \frac{\mu_L}{a_L^2 \delta_{pore}^2} \]
They performed electrical resistance measurements to empirically determine the hold-up and residence time in RPBs with a kind of reticulated foam packing, and proposed the following general equations, which exclude the effects of gas flows on hold-up for propylene glycol and water, respectively.

\[
h_L = 0.039 \left( \frac{a_c}{a_0} \right)^{-0.5} \left( \frac{u_L}{u_0} \right)^{0.6} \left( \frac{\nu}{\nu_0} \right)^{0.22} \tag{9}
\]

\[
h_L = 0.034 \left( \frac{a_c}{a_0} \right)^{-0.38} \left( \frac{u_L}{u_0} \right)^{0.62} \tag{10}
\]

where

- \(a_0\): 100 m/s²
- \(u_0\): 0.01 m/s
- \(\nu_0\): 1CS or \(10^{-6}\) m²/s

They also highlighted that when \(Re\delta \gg d_{pore}\), an inertia flow is dominant, while when \(Re\delta \ll d_{pore}\), a viscous flow is dominant.

Later, Chen et al. [33] studied this subject, assuming that the gas and liquid took the form of plug and film flows in steel wire mesh RPBs, and derived a hold-up correlation with regression from their experimental data. They illustrated that hold-up could be determined via the initial superficial liquid and gas velocities, as well as the annular velocity.

For the accurate estimation of hold-up in RPBs, Yang et al. [83] used an X-ray CT scanner. Their analysis of the time-averaged tomographic photographs of the surface area showed that a high rotating speed improved liquid distribution in the packing. Their experimental results showed that the hold-up decreased with an increase in rotation. Finally, Yang et al. proposed the following correlation with a ±22% error by adding the Kapitza number, which included surface tension, to Basic and Dudukovic’s correlations.

\[
h_L = 12.159 Re^{0.923} Ga^{-0.61} Ka^{-0.019} \text{ For wire mesh packing} \tag{11}
\]

\[
h_L = 12.159 Re^{0.479} Ga^{-0.392} Ka^{-0.033} \text{ For nickel foam packing} \tag{12}
\]

After that, Liu et al. [109] carried out the same study, and proposed correlations with a lower error (±15%) that were similar to those of Yang et al., and which were devised for an RPB that was equipped with a mesh-pin rotor.

\[
h_{L,IMZ} = 5.835 Re^{0.854} Ga^{-0.454} Ka^{0.037} h_{L,OPZ} = 0.247 Re^{0.427} Ga^{-0.239} Ka^{0.031}
\]

Another operating parameter in RPBs is the liquid residence time, which can be determined via liquid hold-up prediction [107]. K. Guo et al. [110] studied the residence time distribution (RTD) in an RPB with simple wire mesh screen packing. They reported that the average residence time was a function of the liquid flow rate and rotational speed, with a reverse relationship. Similarly, D. Xinlin et al. explained liquid mean residence time in a simple RPB based on a modified surface renewal model [111].

### 3.1.2. Flooding and Pressure Drop

Generally speaking, the flooding point is defined as the upper limit of a contactor’s operation, its permissible flow rates, as well as the liquid and gas velocities at which high rates of pressure drop and low MT efficiency occur. The flooding point in PBCs is not exactly the same as that in RPBs because of the presence of centrifugal acceleration, the orientation of the rotors, and the flow areas in RPBs. However, the flooding point in RPBs depends on the total pressure drop, as well as gas and liquid flow rates [84,112], and it does not allow operation at high throughputs. Sivakumar [113] also argued that high gravity limits flooding in RPBs, compared to PBCs, and establishes more effective gas–liquid surface areas in the packing. RPBs have a higher flooding capacity due to their...
high gravity, as reported by Hendry et al. [81], who also showed how a flooding point could be determined and measured. Gas velocity and effective surface area increase as a result of an increase in acceleration, which can reduce the volume of the contactor. Greater centrifugal acceleration allows for greater flooding capacity [84,114]. Neumann et al. [114] examined knit meshes, metal foam, and two types of fixed nozzles (flat fan (FF) and full jet (FJ)), and reported that FF nozzles reduced the flooding point and that the effect of the packing type was tiny. Their experimental results indicate that the flooding point depends on gas capacity, liquid loads, rotational speeds, liquid distributor types, and packing characteristics.

A greater flooding capacity allows the use of high-volume of more porous packings. Furthermore, the flooding is locally affected, with the liquid hold-up from the inner to the outer edge decreasing and becoming thinner due to centrifugal acceleration and flow area increment. Therefore, selecting the most suitable liquid distributor can improve these aspects. Near the flooding point, a greater pressure drop and MT rate are achieved, after which the MT rate drops to a minimum and the NTU decreases when the operation reaches its flooding point [81,84,112,113,115].

There are two approaches to flooding prediction in PBCs. One method is based on generalized correlation charts for irrigated beds, known as GPDC (Generalized pressure drop correlation) charts, and the second method focuses on theoretical models for describing one or two phases in the column. With these approaches, famous correlations, such as those of Wallis and Sherwood, were established [116]. In the Sherwood approach, $u^2_g \frac{g a_t}{\mu} \varepsilon^{0.2} \left(\frac{\rho_L}{\rho_G}\right)^{0.5}$ (Y axis) vs $L \left(\frac{\rho_G}{\mu_L}\right)^{0.5}$ (X axis) gives the flooding limitation [117], and in that of Wallis, two other parameters are used, the summation of which is one constant, as follows [118]:

$$C_G^{0.5} + mC_L^{0.5} = C$$  \hspace{1cm} (13)

$$C_G = \frac{M_G}{\rho_G A} \left(\frac{\rho_G}{\rho_L - \rho_G}\right)^{0.5}$$  \hspace{1cm} (14)

$$C_L = \frac{M_L}{\rho_L A} \left(\frac{\rho_L}{\rho_L - \rho_G}\right)^{0.5}$$  \hspace{1cm} (15)

Furthermore, in 1992, Singh et al. proposed a modified Sherwood correlation in the following form, according to their RPB experimental data for a VOC removal system [119]:

$$\log \left[ \frac{u^2_g a_t}{R_0 a^2 \varepsilon^3} \left(\frac{\rho_G}{\rho_L}\right)^{0.2} \left(\frac{\mu_L}{\mu_w}\right)^{0.2} \right] = -2.27 - 1.14 \log \left( \frac{L}{G} \sqrt{\frac{\rho_G}{\rho_L}} \right) - 0.17 \left[ \log \left( \frac{L}{G} \sqrt{\frac{\rho_G}{\rho_L}} \right) \right]^2$$  \hspace{1cm} (16)

They examined the hydraulic capacity of a simple counter-current RPB, and compared their experimental results with those of the Sherwood correlation. The experimental data showed good compatibility with wire gauze packing, and they underestimated the $\omega$ for the Sumitomo packing. Kelleher and Fair [84] reported that the hydraulic capacity and area of the flows on the packing’s inner surface could be predicted via the Sherwood method by replacing $g$ with $a_c$ for RPBs. Rao et al. [112] suggested that the term “ejection point” was a better expression than “flooding point”, which denotes the point where at the pressure drop across the rotor increases with a reduction in the angular speed, and they made use of the Sherwood approach in their investigation of an RPB by replacing $g$ with $a_c$. The experimental results of Wang et al.’s investigation [62] demonstrate that the hydraulic capacity is a function of vapor velocity at the eye of the rotor. Y. Li et al. [115] investigated an air–water system, and showed that the flooding point in RZBs and RPBs was that at which the pressure drop increased quickly when the superficial liquid velocity increased. They proposed a modified Sherwood correlation (17) for RZBs, without considering $a_t$ and $\varepsilon$, as follows:
\[
\log \left[ \frac{u_G \Delta r}{R_i \omega^2 \Delta r} \left( \frac{\rho_G}{\rho_L} \right) \right] = -2.281 - 0.9788 \log \left( \frac{L}{G} \sqrt{\frac{\rho_G}{\rho_L}} \right) - 0.1605 \left[ \log \left( \frac{L}{G} \sqrt{\frac{\rho_G}{\rho_L}} \right) \right]^2
\]

(17)

where \( \Delta r \) is the distance between the inner rotational and stationary baffles.

Lockett [120] reported that the Wallis type plot was better than the Sherwood type for correlating flooding data in RPBs, and proposed a correlation based on the Wallis correlation that Rajan et al. [121] provided. This correlation, based on their experimental data for an \( RSB \), is as follows:

\[
C_{0.5}^G + m C_{0.5}^L = 1.57 \beta^{0.25} a_i^{-0.25} \left( \frac{\mu_L}{\mu_w} \right)^{-0.03}
\]

Lockett’s extended form (18)

\[
C_{0.5}^G + 1.51 C_{0.5}^L = 130 \beta^{0.434} a_i^{-0.9343} \left( \frac{\mu_L}{\mu_w} \right)^{-0.03}
\]

Rajan et al.’s extended form (19)

\[
C_G = \frac{u_G}{\sqrt{\rho_G / \rho_L}}
\]

(20)

\[
C_L = \frac{u_L}{\sqrt{\rho_L / \rho_G}}
\]

(21)

Another important parameter is the minimum height for an RPB without flooding, which was defined by K. Gudena et al. [122] as Equation (22):

\[
h_f = \frac{Q_G}{2 \pi R_i u_g}
\]

(22)

In addition, they applied Equation (23) to determine the minimum length of an RPB’s inner radii.

\[
r_{i,\text{min}} = \left( \frac{Q_G}{\pi d_{\text{jet}} (1 - f_d)} \right)^{1/2} \left( \frac{\rho_G \xi}{\rho_L} \right)^{1/4}
\]

(23)

where the unit of \( Q_G \) is \( m^3/s \).

The loss of momentum in RPBs due to fluid flow resistance across porous media causes a pressure drop in the whole packing [123], which can be computed using the various models and approaches developed by investigators. The measurement and calculation of the pressure drop in RPBs is more complicated than in PBCs. Additionally, a pressure drop in RPBs may be described as dry or wet by investigators. A dry pressure drop is determined when only gas flows across the RPB, while it is called a wet pressure drop when liquid and gas are introduced simultaneously.

In 1990, Kumar and Rao [124] proposed a correlation to evaluate the pressure drop for counter-current simple RPBs with wire mesh packing, and defined the total pressure via friction forces, centrifugal pressure drop, and increases in (rotating and translational) kinetic energy, as follows:

\[
\Delta P_t = \Delta P_c + \Delta P_f + \Delta P_k
\]

(24)

Singh et al. [119] evaluated RPBs with three kinds of rotor in the context of removing VOC from water, and proposed the following correlation, which only includes a pressure drop due to the rotation and friction of fluid in the packing.

Foumeny et al. [125] investigated equilateral and non-equilateral solid cylinders as packing in a tube, and proposed an empirical correlation useful for pressure drop estimation that uses the size of particles and their relation to the bed diameter, thus resolving the deficiencies of Ergun’s correlations. In the same year, Hwai-Shen Liu et al. evaluated the dry and wet pressure drop in a simple counter-current RPB using the gas capacity factor, as well as the wetted and dry resistance coefficients, which depend on \( Q_L, Q_G \), and the annular velocity of the packing [28]. Additionally, their experimental results showed that,
due to the reduced liquid hold-up, the effects of \( Q_l \) were more significant in rectangular packing than in elliptical packing with different rotor speeds.

Rao et al. [112] contended that a dry pressure drop across the stationary rotors in simple RPBs can be predicted by the Ergun correlation, as follows:

\[
\frac{dP}{dr} \left( \frac{\varepsilon}{1-\varepsilon} \right) = \frac{150(1-\varepsilon)}{R_e_p} + 1.75
\]  

(25)

and according to the flow area variations, they changed it to the following form:

\[
\Delta P = \frac{(1-\varepsilon)}{\varepsilon^3} \frac{Q_g}{2\pi Z_d_p} \left[ \frac{150(1-\varepsilon)\mu_g}{d_p} \ln \frac{R_o}{R_i} + 1.75 \frac{Q_g \rho_g}{2\pi Z} \left( \frac{1}{R_i} - \frac{1}{R_o} \right) \right]
\]  

(26)

They reported that a dry pressure drop was induced linearly with a change in the rotor’s speed, and that it initially decreased when liquid flowed in, while it remained constant when the speed was increased, which might have caused a reduction in the liquid hold-up [112]. In this experiment, the total pressure drop was defined in three segments across the RPB by Equation (24); Equation (26) was employed to determine the amount of \( \Delta P_f \), and Equations (27) and (28) were used to estimate the kinetic and centrifugal pressure drop.

\[
\Delta P_k = \frac{\rho_g}{8} \left( \frac{Q_g}{\pi Z} \right)^2 \left( \frac{1}{R_0^2} - \frac{1}{R_i^2} \right)
\]  

(27)

\[
\Delta P_c = \frac{A}{2} \rho_g \omega^2 \left( R_o^2 - R_i^2 \right)
\]  

(28)

where A is a constant in the range of 0.5–2.

Chandra et al. [126] reported that gas velocity and rotor speed could increase the total pressure drop through rotors in an RSB. Wei-Der Sung and Yu-Shao Chen presented an RPB that was equipped with a blade and baffle. Their enforced modification baffle reduced the pressure drop by 53% [127]. Wang et al. [128] studied a cross-flow RPB with concentric ring packing (CRB), and suggested a correlation that could calculate the degree of pressure drop according to the gas and liquid’s superficial velocities and rotational speeds. The experimental results of this investigation show that the degree of dry pressure drop did not vary with an increase in the gas velocity. Furthermore, the rotational speed had no effect on the dry pressure drop, but the degree of wet pressure drop increased with an increase in the rotational speed.

Although Lashkarbolooki [106] reported that the major parameters impacting simple RPBs’ pressure drop rates were gas and liquid flow rates and rotor speeds, Neumann et al. [80] employed a channel model, and pointed out that the geometry of the packing was not considered in Ergun’s correlation. They showed that the centrifugal pressure drop mainly depends on the outer radii of the rotors, and the friction pressure drop depends on the geometry of the rotors and the packing characteristics when under the operation conditions of RPBs.

Several of the pressure drop correlations proposed by investigators between 2009 and 2017 are summarized in Table 3. These correlations illustrate that the total pressure drop depends on the gas capacity factor, gas and liquid flow rates, the rotational speed of the packing, and gas density.
### Table 3. Summary of several pressure drop correlations published by investigators between 2009 and 2017.

| RPB Type | Year | Kind of Packing | Flows Contacting | Correlation | Div. (%) | Refs. |
|----------|------|-----------------|-----------------|-------------|----------|-------|
| CRB      | 2009 | Concentric ring | Cross-current    | $\Delta P = 0.019n^{0.35}Q_s^{0.018}u_s^{0.95}$, $u_s = \frac{4n_s}{p_s^{2/3}Q_s}$, $Q_s, L = \frac{3600n_s}{\pi R_s L}$ | ±20 | [128] |
| Simple   | 2009 | Wire mesh       | Counter-current  | $-\Delta P_I = \Delta P_{II} + \Delta P_{III}$ $-\Delta P_I = \frac{\rho C_d^2}{8\pi^2} \left( \frac{Q_s}{\rho u_s^2} \right)^2 \left( \frac{1}{R_s^2} - \frac{1}{R_o^2} \right) + \int f_{R_o} \rho G u_s^2 dR$ $-\Delta P_{II} = \frac{\rho C_d^2}{8\pi^2} \left( \frac{Q_s}{\rho u_s^2} \right)^2 \left( \frac{1}{R_s^2} - \frac{1}{R_o^2} \right) + \int f_{R_o} \rho G u_s^2 dR$ $-\Delta P_{III} = \frac{\rho C_d^2}{8\pi^2} \left( \frac{Q_s}{\rho u_s^2} \right)^2 \left( \frac{1}{R_s^2} - \frac{1}{R_o^2} \right) + \int f_{R_o} \rho G u_s^2 dR$ | ±5 | [129] |
| Simple   | 2010 | Plastic porous plate packing Rippled porous plate packing | Cross-current | $\Delta P_{II} = 0.06920 \frac{1}{0.674} Q_s^{0.803}$ | ±10 | [130] |
| RZB      | 2013 | Stationary and rotating baffle | Counter-current | $\Delta P_I = A \left( \frac{Q_s}{\pi D_s^2} \ln \frac{R_o}{R_s} \right) + B \left( \frac{Q_s}{\pi D_s^2} \right)^2 \left( \frac{1}{R_s^2} - \frac{1}{R_o^2} \right) + \frac{Q_s}{2} (K\omega)^2 (R_o^2 - R_s^2) + (S_1 + S_2)(u_G - u_L)$ | 4.02–12.38 | [131] |
| Simple   | 2017 | Wire mesh, Sumitomo, foam metal | Counter-current | $\Delta P_t = A \left( \frac{Q_s}{\pi D_s^2} \ln \frac{R_o}{R_s} \right) + B \left( \frac{Q_s}{\pi D_s^2} \right)^2 \left( \frac{1}{R_s^2} - \frac{1}{R_o^2} \right) + \frac{Q_s}{2} (K\omega)^2 (R_o^2 - R_s^2) + (S_1 + S_2)(u_G - u_L)$ | 7.24 | [106] |
| Simple   | 2017 | Knit meshes and metal foams | Counter-current | $\Delta P_{tot} = \Delta P_{II} + \Delta P_{III} + \Delta P_f,sta + \Delta P_f,empty + \Delta P_f,rotor + \Delta P_{rot}$ $\Delta P_{f,sta} = \Psi_0 (1 - \varphi) \frac{1}{\varphi} \frac{1}{\sigma} \frac{1}{d_p} \frac{R_G - R_s}{R_s}$ $\Delta P_{f,rotor} = \Psi_0 \frac{1}{\varphi} \frac{1}{\sigma} \frac{1}{d_p} \frac{R_G - R_s}{R_s}$ $\Delta P_{f,empty} = \Psi_0 \frac{1}{\varphi} \frac{1}{\sigma} \frac{1}{d_p} \frac{R_G - R_s}{R_s}$ $\Delta P_{rot} = \Psi_0 \frac{1}{\varphi} \frac{1}{\sigma} \frac{1}{d_p} \frac{R_G - R_s}{R_s}$ $\Delta P_{rot} = \Psi_0 \frac{1}{\varphi} \frac{1}{\sigma} \frac{1}{d_p} \frac{R_G - R_s}{R_s}$ | ±15 | [80] |
3.2. Mass Transfer and Performance Modeling

3.2.1. Mass Transfer Coefficients and Removal Efficiency

The mass transfer of soluble components depends on fluid motion in the field. The MT coefficient is a function of the fluid properties and flow rate, and will vary if these parameters cause any variations in the flow direction [132]. The MT rate can be affected by several parameters, such as the packing type, the absorbent physicochemical’s properties and concentration, the absorbing component’s partial pressure, gas flow rate, liquid flow rate, liquid temperature, and the loading of the components in the absorbents in PBCs [133]. The gas velocity and flow area change radially in RPBs; therefore, MT coefficients change from point to point in the contactor [134], but there is no general theory in this case, and the prediction of MT coefficients in RPBs is theoretically complicated [30]. The MT correlations developed by researchers for RPBs are theoretical or empirical correlations, and some of them replace the term “g” with “rω” so as to use the conventional PBC correlations. For instance, H. H. Tung and R. S.H. Mah developed a theoretical equation for penetration theory, and showed that it could be made applicable for HiGee processes by replacing “g” with “rω” [135].

$$k_{Ld} = \frac{2}{\pi} \frac{Q}{\Delta x} \frac{1.33}{Re^{0.33}} \frac{a_i}{a_e} \left( \frac{a_d^2 \rho L^{0.5}}{\mu_L^{0.167}} \right)$$

(29)

Kang et al. [136] examined a CO₂–MEA system in an RPB by employing the two-film theory for mass transfer determination. Similarly, Joel et al. [137] worked on a CO₂–MEA system in 2015, and employed previous researchers’ correlations for PBCs. Both of these replaced “g” with “rω” to use the correlations for RPBs. However, E. Oko et al. [138] demonstrated that estimating the gas–liquid effective interfacial area with the above method led to a noticeable error of around 50%.

The mathematical modeling of packed beds requires a system derived from heat, mass, and momentum conservation [139]. Reddy et al. [134] employed Equations (30) and (31) in the context of mass and energy balance to predict the overall gas volumetric MT coefficient, $k_{Ga}$, in SO₂–NaOH systems, and the overall liquid volumetric MT coefficient, $k_{La}$, when stripping oxygen from water for an RSB, as:

$$k_{Ga} = \frac{Q_G}{\pi (R_o^2 - R_i^2)} Z \frac{C_{G,i}}{C_{G,o}}$$

(30)

$$k_{La} = \frac{Q_L}{\pi (R_o^2 - R_i^2)} Z \frac{C_{L,i}}{C_{L,o}}$$

(31)

Yu et al. [140] applied Equation (30) in a simple RPB to predict $k_{Ga}$ and Equation (32) to calculate HTU in CO₂ removal with a mixture of PZ-DEG.

$$HTU = \frac{R_o - R_i}{ln \left( \frac{Y_i}{Y_o} \right)}$$

(32)

According to this approach, Yu et al. [141] assumed an RPB in the form of several stirred tanks in series-mode and used a mole balance. Chu et al. [142] worked on SO₂–Na₂SO₃ systems, and similarly, Liangliang et al. [143] worked on SO₂ capturing with a calcium-based solution. Zhan et al. [144] studied the simultaneous absorption of H₂S and CO₂ into an MDEA-PZ solution in a simple RPB, and employed theoretical Equation (30).

Additionally, empirical and statistical correlations have been developed by investigators to enhance the accuracy and to identify more effective parameters. Munjal et al. [30] devised the following equations based on laminar liquid film flow to predict the liquid MT coefficient:

$$k_L = 2.6 \left( \frac{Q_L}{\Delta x} \right) \frac{S_{CL}}{L} \frac{1}{Re^{0.5}} Gr^{0.5}_{L}$$

(33)
where $\Delta X = \frac{d_p}{2}$ is employed with higher liquid Reynolds numbers and $\Delta X = d_p$ with lower ones.

Liu et al. [28] and Chen and Liu [145] evaluated MT coefficients experimentally with gas and liquid Reynolds and Grashof numbers, gas diffusivity, total packing surface area, and effective packing surface area.

Lin et al. [146] examined CO$_2$ absorption with NaOH, MEA, AMP, and MEA-AMP solutions in a simple RPB, reported the separation efficiency, and argued that $K_Ga$ was a function of the rotational speed, absorbent concentration, CO$_2$ concentration, and gas and liquid flow rates. Chen et al. studied the effects of RPB geometry using different radius values of packing, and estimated the $k_{La}$ according to their experimental results for the Sc, Re, Gr, and We numbers of liquid flow and packing characteristics [147]. Additionally, they reported that MT decreased with an increase in the outer radius of the packing at low rotational speeds, and that this decrease was small at high rotational speeds. Similarly, Chen et al. [148] evaluated MT for various types of structured and random packing (beads, Rashing rings, Intalox Saddles and wire meshes) at greater detail, considering packing characteristics such as the size, material shape, surface property, and fluid surface tension.

Yi et al. [94] worked on carbon dioxide capturing with a DEA-promoted hot potassium carbonate solution in a simple RPB, and demonstrated that the $K_Ga$ in the end-effect zone was higher than in the bulk zone of the packing. They employed Onda et al.’s correlation (34) for PBCs.

$$k_{GRT} = 2 \times \frac{Re_G^{0.7} Sc_G^{0.33} (a_d d_p)^{-2.0}}{a_t D_G}$$

Equation (34) shows the co-rotation and counter-rotation modes and describes the volumetric liquid MT coefficient using liquid Reynolds, Froude, and Schmidt numbers, liquid diffusivity, total packing surface area, and equivalent diameter. A higher $k_{La}$ was achieved using counter-rotation. Moreover, the liquid and gas’ superficial velocities and centrifugal acceleration were changed radially in RPBs, and the Re, Fr, and We numbers were functions of the liquid’s superficial velocity. In addition, the Fr and We changed with the centrifugal acceleration and packing surface area, respectively.

Lin and Chu [60] worked on a CO$_2$–NaOH system in a blade-type RPB, and their experimental data indicate that the carbon dioxide removal efficiency increased with the rotational speed, solvent flow rate, and concentration. Chen et al. [149] studied CO$_2$–NaOH and O$_2$ desorption from water in an RPB with two kinds of packing (plain-woven packing and knit-woven packing), and reported that RPBs with dense wire meshes would show reduced $k_{La}$ and surface renewal due to their high resistance against flows. Their experimental results indicate that the $a_e$ would be higher with stainless steel than with PTFE. They established a correlation by considering the shape parameter $\phi$ in addition to the Reynolds, Froude and Weber numbers, the surface property, the fluid surface tension, the gas diffusivity, and the equivalent diameter of the packing.

Recently, Chen et al. [150] worked on simultaneous NO$_x$–SO$_2$–CO$_2$ removal in a simple RPB, and proposed correlations based on the two-film theory, using the total surface area, gas diffusivity, equivalent diameter of packing, and the Reynolds, Froude, and Grashof numbers to estimate the gaseous volumetric MT coefficients, which increase with Fr reduction and increase with Re and Gr.

Another approach to MT prediction was proposed by Luo et al. [151], who contended that MT could be evaluated by dividing an RPB into three sections, namely, the bulk (packing), the cavity, and the end zone. This approach was proposed in Guo’s dissertation, in which he argued that the liquid volumetric MT coefficients were highest in the end-effect zone, second highest in the bulk zone, and lowest in the cavity zone, but in industrial applications, the evaluation of MT in the bulk zone is more important than that in the other zones. It is assumed that the MT in the end-effect zone was related to the intense contact between the liquid elements and the packing, the strong interaction between gas and liquid, and the fast outlet of fresh liquid from the liquid distributor.
Yang et al. [152] reported that the MT in the cavity zone was 13–25% of the overall MT in the whole RPB. The experimental results of Guo et al.’s investigation [153] illustrate that the effective interfacial gas–liquid surface area in the cavity zone was approximately 30% of that of the whole RPB, and the residual value in the bulk zone was 70%. Sang et al. [25] investigated this issue in detail with a high-speed camera in a NaOH–CO$_2$ system, and analyzed the MT interfacial area in the cavity zone by considering the liquid elements as mother and daughter droplets and a liquid film. In the same year, the experimental result of Luo et al.’s investigation [154] demonstrated that the MT effective interfacial area in the cavity zone was about 9% of the whole interfacial area in their RPB.

In conclusion, correlations may be found via statistical regression analysis and dimensional analysis. A summary of the correlations developed by investigators in 2002–2019 to predict MT coefficients is given in Table 4. This table indicates that $K_G$, $K_L$, $k_G$, and $k_L$ are functions of dimensionless numbers, which are expressed in terms of factors and variables depending on the system’s behavior, as follows:

$$K_G = g(Re_G, Fr_G, Re_L, We_L, Fr_L, Ga, N, pH, C_{solvent})$$ (35)

$$k_Ga = h(Re_G, Re_L, Gr_G, Sc_G, \left(\frac{a_1D_G}{d_p}\right), Ga, We)$$ (36)

$$k_La = l(Re_L, Gr_L, Sc_L, \left(\frac{a_1D_G}{d_p}\right), Fr_L, We_L, Re_G, Gr_G, Sc_G)$$ (37)

Additionally, as the table clearly shows, researchers have described the geometry of the system, the fluid’s viscosity, and the effects of external forces such as the turbulence of the fluid flow (resulting from the packing and RPB geometry), the liquid surface tension, and the effect of rotational speed (using the Re, We and Gr numbers, respectively), to evaluate the performance of the contactor and determine the volumetric MT coefficient. Furthermore, it is possible to scale up this correlation and achieve dynamic similarity by adding the Fr number. Further details are provided in Section 4.
Table 4. MT correlations proposed by various investigators for RPBs in 2002–2019.

| Type of RPB | Absorbent | Absorbing Component | MT Correlations | Div.% | Year | Refs. |
|-------------|-----------|---------------------|-----------------|-------|------|-------|
| CCSR        | —         | O₂ desorption       | $k_m = 0.478 R_l^{0.906} G_l^{0.275}$ | ±10   | 2002 | [155] |
| CCSR        | Water     | VOC                 | $k_m = 0.077 R_l^{0.323} R_c^{0.328} G_l^{0.18}$ | ±30   | 2002 | [145] |
| CCSR        | Water     | VOC                 | $k_m = 0.061 R_l^{0.712} R_c^{0.507} G_l^{0.326}$ | ±30   | 2004 | [156] |
| CCSR        | —         | O₂ desorption       | $k_m = 0.9 R_l^{0.5} G_l^{0.275}$ | ±10   | 2005 | [157] |
| CCSR        | —         | O₂ desorption       | $k_m = 0.65 R_l^{0.17} G_l^{0.3} W_l^{0.29}$ | ±30   | 2005 | [147] |
| RSB         | NaOH      | SO₂                 | For co-rotation: $k_Ga = \left(7.62 \times 10^{-3}\right) R_l^{0.832} G_l^{0.194} S_l^{1/2} \left(\frac{a D_l}{d_f}\right)$ | ±20   | 2006 | [134] |
| RSB         | NaOH      | SO₂                 | $k_La = 0.152 R_l^{0.569} G_l^{0.140} S_l^{1/2} \left(\frac{a D_l}{d_f}\right)$ | ±20   | 2006 | [134] |
| Blade       | Water     | IPA                 | $k_m = 0.027 R_l^{0.679} R_c^{0.245} G_l^{0.14}$ | ±10   | 2007 | [155] |
| CRCSR       | NaOH      | CO₂                 | $K_l = 0.003689 R_l^{0.5449} W_l^{0.5476} G_a^{0.3428}$ Plastic porous plate | ±10   | 2010 | [130] |
| CCSR        | Water     | Ammonia and VOC     | $k_Ga = 0.025 R_l^{1.13} R_c^{0.14} G_l^{0.31} W_l^{0.07} \left(\frac{a D_l}{d_f}\right)^{1.4}$ | ±30   | 2011 | [158] |
| COCSR       | NH₃ based sol. | SO₂            | $K_Ga = 0.08 Q_l^{0.01} Q_l^{0.58} N_l^{0.36} H_l^{0.57} C_l^{0.76} C_{SO}_2^{0.09}$ | ±8    | 2014 | [39]  |
| CCSR        | A.S       | SO₂                 | $K_Ga = 2.6 \times 10^{-4} R_l^{0.60} F_r^{0.34} G_a^{0.47}$ SiC structured packing | ±5    | 2015 | [159] |
| CCSR        | A.S       | SO₂                 | $K_Ga = 2.7 \times 10^{-5} R_l^{0.77} F_r^{0.21} G_a^{0.26}$ Plastic structured packing | ±10   | 2015 | [159] |
| Type of RPB | Absorbent | Absorbing Component | MT Correlations                                                                                     | Div.% | Year  | Refs. |
|------------|-----------|---------------------|-----------------------------------------------------------------------------------------------------|-------|-------|-------|
| CRCSR      | NaOH      | CO₂                 | \( k_{L,a} = 1.8221 \left( \frac{a_d}{D_a} \right) Re^{0.6371} Gr^{0.0548} Sc^{0.0623} \)               | ±10   | 2015  | [160] |
| CCSR       | TEG       | H₂O                 | \( \frac{K_{G,a}}{D_{PG}} = 0.1697 \left( \frac{Y_{w1}}{Y_{w2}} \right)^{0.231} \left( \frac{Q_{G}}{Q_{L}} \right)^{-0.236} Sc^0.333 Re_G^{1.614} \) | ±20   | 2018  | [161] |
| CCSR       | NaOH      | SO₂                 | \( K_{G,a} = 0.456 Re_{G}^{0.59} We_{L}^{0.07} Fr_{L}^{-0.06} \left( \frac{e}{\eta} \right)^{0.1} \)       | ±20   | 2018  | [162] |
| CCSR       | Na₂SO₃    | SO₂                 | \( K_{G,a} = 2.76 \times 10^{-5} Q_{L}^{0.22} Q_{G}^{0.43} N^{0.55} p_{H}^{2.27} C_{\text{Solvent}}^{0.1} \) | ±15   | 2018  | [142] |
| COCSR      | NaClO     | VOC                 | \( K_{G,a} = 8.5173 Q_{L}^{1.2357} \omega^{-0.2783} \left( \frac{H}{H^*} \right)^{-0.2351} C_{\text{NaClO}}^{0.0346} \) | ±30   | 2018  | [163] |
| CCSR       | MEA       | CO₂                 | \( k_G = 2a_t^{0.7} Sc^{\frac{1}{2}} (a_d d_p)^{-2} \) Bulk and end-effect zone                      | ±20   | 2019  | [97]  |
|            |           |                     | \( k_G = \frac{D_p}{a_t} (2 + 0.552 Re_G^0.5 Sc_G^0.5) \) Cavity zone                               |       |       |       |

A.S: ammonia-based solution; PWP: Plain-woven packing; KWP: knit-woven packing; CCSR: counter-current simple RPB; COCSR: co-current simple RPB; CRCSR: cross-current simple RPB.
3.2.2. Effective Interfacial Surface Area and Performance

The effective gas–liquid interfacial surface area of a contactor is central to absorption systems and depends on system characteristics [152]. The effective surface area in bubble absorbers is equivalent to the wet and total contacting surface areas, while, in PBCs, the effective surface area of the packing may be smaller than the wetted surface area in small packings with very high loadings [164]. The effective interfacial surface area in contactors is highly dependent on hydrodynamics [165]—with highly turbulent flows and super-high gravity, a thinner liquid film and finer droplets are produced, which enhances the gas–liquid surface area and MT. This was demonstrated through Liu et al.’s experimental results regarding the absorption of ozone into water in counter-current RPBs [166], and through the results of Liangliang et al.’s investigation [143] of the absorption of SO$_2$ in RPBs with plastic and metal packings. Therefore, effective liquid distribution can be considered as essential to achieving a higher value of MT.

The method for the determination of effective gas–liquid interfacial surface area is shown in Figure 5. Due to the lack of physical methods and their complexity when employed in RPBs to predict the value of $a_e$, chemical methods have often been applied by investigators, using the known kinetics of the reaction along with absorption theory. Examples of this include Munjal et al.’s investigation [31] with simple RPBs, Yang et al.’s study [152] of a simple RPB with various radii of packing, and Rajan et al.’s experiments [121] on RSBs. All of these researchers used NaOH–CO$_2$–N$_2$ systems in RPBs with a pseudo first-order reaction, and applied the Danckwerts model and Henry’s law to define the absorption flux and total gas–liquid interfacial area; they then determined the effective interfacial surface area by dividing the result by the overall volume of the packing. Similarly, Luo et al. [151,167] used this method in an RPB with simple wire mesh and blade packing, and defined the pseudo first-order reaction as follows:

$$R_{CO_2} = k_L a_e C_{CO_2,L} \sqrt{1 + \frac{D_{CO_2} k_2 C_{NaOH,L}}{k_L^2}} = k_L a_e C_{CO_2,L} \sqrt{1 + M} \quad (38)$$

When $M \gg 1$, then

$$a_e = \frac{R_{CO_2}}{C_{CO_2,L} \sqrt{D_{CO_2} k_2 C_{NaOH,L}}} \quad (39)$$

**Figure 5.** Effective interfacial surface area determination methods.

In the same situation, Dong et al. [160] applied the following equation for a simple cross-flow RPB.

$$a_e = \frac{R_{CO_2}}{H_{CO_2} P_{CO_2,L} \sqrt{D_{CO_2} k_1}} \quad (40)$$

Similarly, Tsai and Chen used a chemical method with a NaOH–CO$_2$ system in their RPB, which was equipped with blades and baffles, and proposed the following relationship for the CO$_2$ absorption flux (mol/m$^2$·s) [29]:

$$N_{CO_2} = \sqrt{D_{CO_2} k_1 a C_{CO_2} \pi \left(R_o^2 - R_i^2\right) Z} \quad (41)$$

wherein the rate constant of the pseudo first-order reaction is $k_1$. 

$$\begin{align*}
R_{CO_2} &= k_L a_e C_{CO_2,L} \sqrt{1 + \frac{D_{CO_2} k_2 C_{NaOH,L}}{k_L^2}} = k_L a_e C_{CO_2,L} \sqrt{1 + M} \\
\text{when } M &\gg 1, \\
a_e &= \frac{R_{CO_2}}{C_{CO_2,L} \sqrt{D_{CO_2} k_2 C_{NaOH,L}}} \\
\text{Similarly, Dong et al. [160] applied the following equation for a simple cross-flow RPB.} \\
a_e &= \frac{R_{CO_2}}{H_{CO_2} P_{CO_2,L} \sqrt{D_{CO_2} k_1}} \\
\text{Similarly, Tsai and Chen used a chemical method with a NaOH–CO}_2\text{ system in their RPB, which was equipped with blades and baffles, and proposed the following relationship for the CO}_2\text{ absorption flux (mol/m}^2\text{·s) [29]:} \\
N_{CO_2} &= \sqrt{D_{CO_2} k_1 a C_{CO_2} \pi \left(R_o^2 - R_i^2\right) Z} \\
\end{align*}$$
Generally, in PBCs, it is assumed that the gas–liquid interfacial area is the same as the wetted surface area of the packing. In 1968, Ondea et al. [168] proposed an empirical correlation with a discrepancy of ±20% to express the ratio of the effective interfacial area in the following form (basing this assumption on their experimental data for PBCs with four packing types):

\[
\frac{a_e}{a_t} = 1 - \exp\left[ -1.45\left( \frac{\sigma_c}{\sigma} \right)^{0.75} Re^{0.1} Fr^{-0.05} We^{0.2} \right]
\] (42)

Similarly, Puranik and Vogelpohl [169] published the following empirical correlation with a ±20% error:

\[
\frac{a_e}{a_t} = 1.045 Re^{0.041} We^{0.133} \left( \frac{\sigma}{\sigma_c} \right)^{-0.182}
\] (43)

In high-gravity and -turbulence situations, the liquid layers are thinner and the droplets are finer, which gives rise to a wider contacting surface area and an intensified MT rate [143,166]. Lin et al. [93] developed the following correlation for an RPB with a maximum error of ±20%:

\[
\frac{a_w}{a_t} = 584 Re_L^{-1.03} We_L^{0.576} Fr_L^{0.23}
\] (44)

Luo et al. [167] examined the effective interfacial surface area in an RPB with stainless steel wire mesh packing, and obtained an empirical correlation in a CO₂–NaOH system similar to that in Equation (44), with the addition of the shape factor to increase the accuracy of the system.

Xie et al. [170] proposed a correlation via the regression of 31 sets of CFD simulation data for RPBs with real 3D packings, with an error value of ±20%, as follows:

\[
a_e = 202.3485 \left( \frac{a_c}{205.6} \right)^{0.0435} \left( \frac{H}{0.0106} \right)^{0.4275} \left( \frac{\nu_L}{3.35} \right)^{0.1200} \left( \frac{\gamma}{75} \right)^{-0.5856}
\] (45)

Yan-Zhen Lu et al. [171] used surface-modified stainless steel wire mesh (SSM) and non-surface modified stainless steel wire mesh (NSM) in a simple counter-current RPB with an NaOH–CO₂ system, and their experimental results demonstrate that suitable liquid dispersion increased the \(a_e\).

Other empirical correlations for gas–liquid interfacial surface areas developed by other researchers are shown in Table 5.
### Table 5. Empirical correlations proposed by investigators for the prediction of effective surface areas.

| Author     | Year | RPB type | Packing   | System        | Correlation                                                                                     | Div. % |
|------------|------|----------|-----------|---------------|-------------------------------------------------------------------------------------------------|--------|
| Rajan et al. [121] | 2011 | RSB      | MF        | NaOH-CO₂       | \[
\begin{align*}
\left( \frac{a}{\eta} \right) &= 54999 \Re^{-2.2186} \Fr^{-0.1748} \We^{1.316} : \text{for co-rotation} \\
\left( \frac{a}{\eta} \right) &= 11906 \Re^{-1.8070} \Fr^{-0.0601} \We^{0.9896} : \text{for counter-rotation}
\end{align*}
\] | ±15    |
| Dong et al. [160]   | 2015 | Simple   | SSWM      | NaOH-CO₂       | \[
\frac{a}{\eta} = 2980.9 \Re^{0.2349} \Fr^{-0.045} \We^{0.5023} \phi^{-0.5}
\] | ±10    |
| Chen et al. [149]   | 2016 | Simple   | PTFE WM   |               | \[
\begin{align*}
\frac{a}{\eta} &= 11.057 \Re^{0.359} \We^{0.448} \Fr^{-0.224} \phi^{-0.202} \left( \frac{\sigma}{\sigma_c} \right)^{1.099} : \text{for PWP} \\
\frac{a}{\eta} &= 21.558 \Re^{0.283} \We^{0.317} \Fr^{-0.218} \phi^{-0.748} \left( \frac{\sigma}{\sigma_c} \right)^{1.099} : \text{for KWP}
\end{align*}
\] | ±20    |
| Luo et al. [154]    | 2017 | CCSR     | SSWM      |               | \[
\frac{a}{\eta} = 15.17 \Re^{0.16} \Fr^{-0.38} \We^{0.13} \phi^{-0.29}
\] | ±15    |
| Xie et al. [170]    | 2019 | Simple   | Expanded SS mesh | MEA            | \[
\frac{a}{\eta} = 202.3485 \left( \frac{d}{\eta} \right)^{0.0435} \left( \frac{\sigma}{\sigma_c} \right)^{0.4275} \left( \frac{\gamma}{\gamma_c} \right)^{0.12} \left( \frac{\phi}{\phi_c} \right)^{-0.29}
\] | ±20    |

KWP: knit-woven packing; MF: metal foam; PWP: plain-woven packing; PTFE: polytetrafluoroethylene; SS: stainless steel; WM: wire mesh.
Additionally, three methods are available to evaluate the MT performance of a PBC, namely, evaluating the height of a transfer unit (HTU), evaluating the height equivalent to a theoretical plate (HETP), and evaluating the overall gas phase transfer unit. The main difference between a PBC and a Higee is the height of the transfer unit (HTU) \[84,165\].

S. P. Singh et al. proposed Equation (46) to predict the area of the transfer unit (ATU) in counter-current simple RPBs [118].

\[
ATU = \left( \frac{3.4 \times 10^4}{a_t^2} \right) \left( \frac{Q_L}{\mu L} \right)^{0.6} \left( \frac{p_L^2}{\pi L} \right)^{0.15}
\]

(46)

T. Kellehr and J. R. Fair [84] reported that the value of NTU could be increased by raising the rotational speed, and that a higher-pressure operation requires a higher NTU. It has also been argued that the MT performance may be measured via the size of the packing (R_o-R_i) and the NTU, which reveal the separation efficiency of a simple counter-current RPB. Gue et al. reported that the HTU could be defined as follows for a simple RPB [27]:

\[
HTU = \frac{Q_L}{\pi K_L a (R_o^2 - R_i^2)}
\]

(47)

where \(K_L a\) is the liquid phase volumetric MT coefficient (mol/m^3·s), and \(Q_L\) is the liquid flow rate (m^3/m^2s).

C. C. Lin et al. [146] studied CO\(_2\) absorption with NaOH, MEA, and AMP, and showed that another important parameter was the NTU, which could be evaluated by considering the mole fraction of CO\(_2\) in the gas streams of the inlet and the outlet of an RPB. They suggested the following equation:

\[
NTU = \int_{Y_i}^{Y_o} \frac{1}{Y - Y^*} dY
\]

(48)

where they assumed that \(Y^*\) equals zero due to the fast reaction of CO\(_2\) with the absorbing aqueous solution, and they proposed the following MT coefficient:

\[
K_G a = \frac{Q_G (NTU_G)}{h \pi (R_o^2 - R_i^2)} = \frac{Q_G}{h \pi (R_o^2 - R_i^2)} \ln \left( \frac{Y_i}{Y_o} \right)
\]

(49)

D. P. Rao et al.‘s investigation showed that the reduction in HTU in their simple RPBs was 5–10 times greater than that in conventional columns, and reported that the HTU did not change with angular velocity when MT-resistant control was enforced on the gas [113].

Additionally, G. Q. Wang et al. employed Equation (50) for the determination of HETP values in an RZB contactor [62]:

\[
HETP = \frac{d_o - d_i}{N_T}
\]

(50)

In 2009, Hsu-Hsiang Cheng and Chung-Sung Tan [37] applied Equation (51) to determine the HTU for CO\(_2\) removal with blended alkanolamines as part of their evaluation of centrifugal acceleration and a fast reaction in a simple counter-current RPB equipped with stainless wire mesh packing.

\[
HTU = \frac{R_o - R_i}{\ln \left( \frac{Y_{\text{out}, CO_2}}{Y_{\text{in}, CO_2}} \right)}
\]

(51)

C. H. Yu et al. examined CO\(_2\) removal systems with aqueous and non-aqueous absorbents in a simple counter-current RPB, and showed that HTU would be reduced when
the rotating speed increased, and would increase with the gas flow rate [140]. Sheng et al. defined the HTU via the NTU in a simple counter-current RPB using Equation (52) [172]:

\[ HTU = \frac{R_o - R_i}{NTU} \]  

(52)

3.3. Numerical Methods

The numerical methods for analyzing RPBs are generally divided into two groups: chemistry-based (chemisorption) and CFD-based [72]. The chemistry-based methods are related to reaction kinetics and the above-mentioned correlations for mass transfer, while the other type is based on CFD models, which are described below.

CFD is an interdisciplinary topic that can be used to simulate flow characteristics and transport phenomena under certain conditions, and which includes mathematics, hydrodynamics, the computation of the conservation of mass, heat and momentum equations, and a discretizing method [173]. The velocity field in RPBs must be studied in order to determine heat and MT mechanisms, but the conditions in RPBs are complicated, turbulent, swirling and anisotropic [89], and CFD is a good tool in such situations. To improve the RPB’s efficiency and flow, numerous researchers have focused on the CFD as related to hydrodynamic parameters, which include pressure drop and flow analysis. CFD modeling includes geometry definition, a meshing method, and models (multiphase, turbulence, and moving reference frame), as shown in Figure 2. Sometimes CFD modeling requires user-defined functions (UDF) for explaining reactions or MT. As for geometry generation, one of the following methods may be employed [173]:

1. Obstacle simplification (use of a simple geometry model or a representative elementary unit (REU), as used in [170];
2. Porous areas (use of mathematical methods that include viscosity and inertia resistance, which appear as a source term in momentum equations), which are suitable for RPB simulation on pilot and industrial scales;
3. Innovative models, such as Lu et al.’s [174], in which porous media are described based on the Kolodziej model, and that contained in another of Liu et al.’s investigations, wherein a physical model was defined via computed tomography (CT) reconstruction [175].

Yu-Cheng Yang et al. [173] reviewed the trends in CFD methods used to characterize an RPB, and concluded that obstacle simplification was a good approach for determining the liquid behavior, but it was not suitable for the 3D, pilot, or industrial scales, whereat porous media could be used.

One of the most important stages in RPB simulation is multiphase model selection. There are two major methods available for this goal: Euler–Lagrange and Euler–Euler, the second of which is widely used, and includes the volume of fluid (VOF), mixed, and Eulerian models [173]. The VOF model is not suitable for two- or three-dimensional (2D or 3D) pilot studies, while the Eulerian model, when used along with porous media models, is a good alternative, although it has been less commonly applied by investigators than the VOF model [66]. As regards the rotation of RPBs, it is necessary to define this situation with the multiple reference frame (MRF) or sliding mesh (SM) model [173]. H. Llerena-Chavez and F. Larachi applied the 3D physical unsteady-state model to simulate the air flow in a simple RPB, and applied porous media to define the packing. They validated the developed model with the experimental results of three RPBs [129]. Similarly, Wenjing Yang et al. [176] simulated the fluid flow in RPBs by applying 2D and 3D models to analyze the velocity profile in the bed. It was demonstrated that the effect of the packing rotation on the flow pattern was lower at a low inlet velocity. Martinez et al. [177] simulated multiphase flow behavior in a 3D model, which consisted of a water–sulfur dioxide system, and investigated the effect of the rotor speed on the flow pattern in an RPB. They considered the porous media in packed beds, which must be added as a momentum source term into standard fluid flow equations, and derived the same results for the gas inlet situation.
There is no general turbulent model for the simulation of RPBs. There are various models, which are categorized into the following two major approaches [173]:

1. Eddy viscosity models;
2. Reynolds stress transport models (RSM).

The RSM has a greater ability to give accurate predictions of complex flows, while five and seven additional equations, respectively, are required for 2D and 3D flows, which implies an increase in the calculation time and computational memory [173]. As such, the second group of models requires more time and computational memory, and is less attractive for researchers. Xin Shi et al. further developed this subject by studying the liquid droplet size and effect, size distribution, hold-up, and the effect of modifying the intensification of MT. They applied a 2D VOF model, a sliding mesh model, and an RSM in Fluent solvers to simulate the velocity and liquid volume distribution, and concluded that the VOF model was suitable for defining the gas–liquid interface in RPBs [178]. A two-phase flow in an RPB was simulated with a 2D model, and the RNG k-ε and large discrete phase model (DPM) were selected by Cheng et al. as turbulence models for the continuous gas phase and liquid size distribution analyses, respectively [179]. They implemented a moving reference frame (MRF) of the packing area for the rotational section, and considered the following methods to compute the droplets’ breakup:

1. Taylor analogy breakup (TAB) for \( \text{We} < 100 \);
2. Wave model for \( \text{We} > 100 \).

They reported that the value of the Weber number of the droplets increased in a radial direction, and that increasing the gas flow rate and rotor speed would increase the merging or breaking up of droplets in the packing. Yongli Sun et al. [180] simulated an RZB using a 3D model to analyze the pressure distribution and the optimal sizing of the packing. Yucheng Yang et al. studied the MT phenomena in a simple RPB. They developed a UDF solver in the Fluent software and adopted VOF and RSM models to simulate the multiphase flows in three different rotors [181]. Similarly, in the same year, Xue-Ying Gao et al. [182] worked on MT characterization for a simple RPB with a CO₂–NaOH system, using numerical simulation. They proposed a mathematical model that incorporated diffusion and reaction. Yi Liu et al. [183] developed a 3D physical model that used realizable k-ε, applied MRF models to simulate a simple RPB in a steady-state mode, and evaluated the air flow inside the packing and the pressure profile at various rotational speeds and gas flow rates. Additionally, Li et al. [89] employed an air–water system and studied the flow field in a perforated-ring RPB with a 2D obstacle physical model, using the RSM turbulence model. They defined air as the first phase and water as the second phase in a VOF model. They also used a PIV visualization method and compared the results, which indicated a suitable accuracy.

Finally, several approaches to CFD investigation for the characterization of RPBs, published in 2010–2020, are summarized in Table 6. According to this table, it is clear that the obstacle, VOF and realizable models were more attractive to, and more widely applied by, researchers.
Table 6. Models recently applied by various investigators for CFD analysis.

| Physical Model | Dimensions | Multiphase Model | Turbulence Model | Solving Approach | Scope                                      | Published Year | Refs.      |
|----------------|------------|------------------|------------------|------------------|--------------------------------------------|----------------|------------|
| Obstacle       | 2D and 3D  | Single phase     | Realizable k-ε   | —                | Pressure field and gas flow characteristics analysis | 2010           | [176]      |
| Porous         | 3D         | —                | Standard k-ε     | —                | Pressure field and hydrodynamic analysis   | 2012           | [177]      |
| Obstacle       | 2D         | Single phase     | Standard k-ε     | SIMPLE           | Hydrodynamic analysis                      | 2013           | [184]      |
| Obstacle       | 2D         | VOF              | RSM              | SIMPLE           | Hydrodynamic analysis                      | 2013           | [178]      |
| Porous         | 3D         | Euler            | Standard k-ε     | —                | Hydrodynamic analysis                      | 2013           | [185]      |
| Obstacle       | 2D         | DPM              | RNG k-ε          | SIMPLE           | Mixing and droplet size analysis           | 2014           | [179]      |
| Obstacle       | 3D         | VOF              | RNG k-ε          | PISO / PRESTO    | Hydrodynamic and MT analysis               | 2014           | [180]      |
| Obstacle       | 2D         | VOF              | RSM              | SIMPLE           | Micro-mixing efficiency analysis           | 2016           | [186]      |
| Obstacle       | 2D         | VOF              | —                | PISO / PRESTO    | Hydrodynamic and MT analysis               | 2017           | [187]      |
| Real           | 3D         | Single phase     | Realizable k-ε   | —                | Pressure drop and gas flow characteristics analysis | 2017           | [183]      |
| Obstacle       | 2D         | VOF              | SST k-ω          | PISO / PRESTO    | Hydrodynamic analysis                      | 2017           | [188]      |
| Obstacle       | 2D & 3D    | VOF              | Realizable k-ε, RSM, k-ω | SIMPLE           | Hydrodynamic and droplet size analysis     | 2017           | [189]      |
| Obstacle       | 2D         | VOF              | Realizable k-ε   | SIMPLE           | Micro-mixing efficiency analysis           | 2018           | [190]      |
| Porous         | 2D and 3D  | Single phase     | Realizable k-ε   | SIMPLE           | Gas flow characteristics analysis          | 2018           | [191]      |
| Obstacle       | 2D         | VOF              | Standard k-ε     | SIMPLE           | Hydrodynamic analysis                      | 2018           | [192]      |
| Obstacle       | 3D         | Single phase     | Standard k-ε     | SIMPLE / PRESTO  | Droplet behaviors                          | 2019           | [193]      |
| Obstacle       | 2D         | VOF              | Realizable k-ε   | PISO             | Hydrodynamic analysis                      | 2019           | [194]      |
| Obstacle       | 2D         | VOF              | Realizable k-ε   | SIMPLE / PRESTO  | Micro-mixing efficiency analysis           | 2019           | [195]      |
| Obstacle       | 2D         | VOF              | Realizable k-ε   | SIMPLE / PRESTO  | Hydrodynamic analysis                      | 2019           | [196]      |
| Obstacle       | 2D         | VOF              | RSM              | PISO / PRESTO    | MT analysis                                | 2016           | [181]      |
| Real           | 2D         | VOF, Euler       | RSM, LES         | —                | Hydrodynamic and liquid behavior analysis  | 2019           | [196]      |
| REU            | 3D         | VOF              | SST k-ω          | PISO             | Hydrodynamic analysis                      | 2019           | [170]      |
| Obstacle       | 3D         | VOF              | SST k-ω          | SIMPLE           | Hydrodynamic and liquid behavior analysis  | 2019           | [197]      |
| Real           | 3D         | Single phase     | Realizable k-ε   | SIMPLE / PRESTO  | Gas flow characteristics analysis          | 2020           | [198]      |

DPM: Lagrange discrete phase mode.
4. Dimensional Analysis

There are several approaches to scaling up in addition to dimensional analysis (DA). For instance, G. Jan Harmsen [199] divided the scale-up process in a pilot plant into the following categories, and recommended the following classifications for PI:

1. Brute force;
2. Rate model.

The DA method was used in this section due to the lack of data on scale-up methods for RPBs analysis. Several important parameters are required for the scaling up of RPBs, such as MT parameters, hydrodynamic information, etc., which can be found via several means, such as fundamental investigations or CFD analysis, as discussed in previous sections. DA can help to create more accurate and unique design parameters. In agitation contactors, the power requirement per unit volume and the mixing quality or fluid behavior are the scale-up criteria [200,201]. The same is true of an RPB, but the geometry and configuration of the rotor are different here; therefore, it is clear that the high-gravity factor should be a dimensionless number that may be used in gravity field analysis (as defined by Equation (53)), as employed by Jiao et al. [130] to study the gas pressure drop and MT in CO2–NaOH system. This study demonstrated that this parameter linearly increased with the radii of the rotor at a constant rate.

\[
\lambda = \frac{\omega^2 r}{g}
\]  

(53)

Youzhi Liu et al. [69] examined the effects of this dimensionless parameter in a special RPB and an RSB, and showed that \( K_G a \), \( a \) and \( k_y \) were augmented when \( \lambda \) increased. This dimensionless number enhanced the contacting situation, with finer droplets and increased MT when its value was increased, as Gui and Li [202] pointed out. S. B. Cao et al. [161] reported that a high \( \lambda \) value caused a change in the liquid flow pattern in the packing, from liquid film to droplets and small filaments, as follows:

1. liquid films \( \lambda < 60 \) g;
2. liquid droplets and small filaments \( \lambda > 100 \) g.

Additionally, their experimental results indicate that an increase in \( \lambda \) could reduce the \( HTU \) and increase \( K_G a \) significantly.

It is worth noting that a correlation that considers \( Re, Sc \) and \( Sh \) only could not be suitable for MT coefficient prediction, because packing geometry is not included [203]. In light of this, Rajan et al. [121] reported that the Reynolds, Froude, and Weber numbers are the other important dimensionless numbers for determining the functions of \( u_{l,s} \), and they could change with the radios of the RPB and \( u_g \). Furthermore, \( a_c \) and \( a_t \) can affect the Froude and Weber numbers, respectively. Xu et al. [179] reported hydrodynamic similarity as another criterion required for effective scaling up. The Weber number reflects the droplets’ break-up status inside the packing, and is defined as the ratio of the inertial force to the surface tension; its value increases as the rotor speed increases. Moreover, B. Zhao et al. [75] developed a model that uses dimension analysis, and defined three issues that could influence the RPB’s performance, namely, gas–liquid properties, operation conditions, and geometrical dimensions.

In light of all of the above, we have clarified the parameters that could affect performance—applying the Buckingham \( \pi \) theory to do so—and outlined the five independent dimensionless numbers of \( Re_G, Re_L, Sc_G, Sc_L, Mr \), and \( Sh \) as dependent dimensionless numbers. Hence, the following correlation was proposed:

\[
Sh = 3.788 \times 10^{-6} Re_G^{0.1404} Re_L^{0.3684} Sc_G^{1.2280} Sc_L^{0.0337} Mr^{0.4286}
\]  

(54)

where \( Sh \) indicates the effective convective MT, and the exponent values of the \( Gr \) and \( Re \) numbers indicate the degree of turbulence [204].
Regarding the geometrical dimensions, it must be noted that the geometry of an RPB can influence the $Re$, $Gr$ and $Sc$ via changes in the average radial gas velocity and MT coefficients [205].

The Hatta number ($Ha$) is another important dimensionless number in RPBs incorporating a reaction system. This number is useful in comparing the reaction rate in the liquid film with the diffusion rate. For instance, S. Munjal et al. described this number for CO$_2$ absorption with NaOH solution, using a pseudo first-order reaction. The value of this dimensionless number exceeds 1 for fast reaction rates, while a value of lower than 1 indicates that physical absorption overcomes the kinetic reaction.

Gas treatment capacity, $\tau$, is another variable to consider when characterizing the parameters of RPBs, as highlighted by Sheng et al. [172]. This factor can be used to scale up and determine the processing capacity, which is described by Equation (55).

$$\tau = \frac{Q_G}{V_b \times 10^6} \quad (55)$$

Additionally, as Neumann et al. [4,114] showed in 2017 and 2018, two considerable factors, maximum and integrated gas capacity and maximum and integrated liquid load, could be applied for benchmarking RPBs.

5. Power Consumption

Keyvani and Gardner [206] reported that the total power consumption of RPBs, as shown in Figure 6, includes rotor power consumption, mechanical friction, and friction loss due to liquid passing through the bed. Singh et al. [119] defined this parameter as follows:

$$N_L = 1.2 + 1.1 \times 10^{-3} \left( \rho_L R_o^2 \omega^2 Q_L \right) \quad (56)$$

and for CRBs, Wang et al. [128] proposed the following correlation:

$$N_{tot} = 5.5n^{0.67} + 0.338n^{0.16} Q_{s,L}^{0.5} \quad (57)$$

Agarwal et al. developed a model to calculate the total power consumption of RSBs via Equation (58) [207]:

$$N_{tot} = 1.2 + 1.1 \times 10^{-3} \rho_L Q_L R_o^2 \omega^2 + \frac{\rho_L \omega Q_L^2}{4\pi hl} \left( \frac{2r_i(s + 1/2) + s(s + 1)(w + t)}{4\pi hl} \right) \times 10^{-3} \quad (58)$$

As Jiang et al. reported, high rotational speeds in RPBs cause increases in the device cost [208].
Jonathan Lee et al. [209] calculated the total power consumption of a simple counter-current RPB equipped with a stainless steel mesh, using Equation (59):

$$N_{tot} = \omega_m L_{tor} F_{tor}$$  \hspace{1cm} (59)

where $\omega_m$ is the rotational speed of the motor (1/s), $L_{tor}$ is the torque arm length (m), and $F_{tor}$ is the force required to hold the torque arm horizontal (N).

Finally, it is worth noting that detailed cost estimation formula have been developed for RPBs by Gudena et al. [122].

6. Future Perspective

Analyses and evaluations of the above research results show that further research is required for achieving MT and reaction models with greater result transparency; wet and effective interfacial gas–liquid surface area measurements, computed with theoretical and empirical models for physical absorption and volumes in the cavity, bulk, and end-effect zones in various kinds of RPB with different kinds of packing; the analysis of MT rate computations and liquid distribution patterns in RSBs and RZBs. It is also clear that conceptual systematic dimensional analysis, rigorous scale-up methods, cost estimation, residence time, and power consumption formulations with greater accuracy require further study as well. Other subjects that can be considered in future investigations include the effects of magnetic fields (DC and AC) and ultrasonic induction on the MT and hydrodynamics in RPBs when ionic fluids or nanofluids are employed as the solvent; the development of more suitable and accurate models for the simplification of various kinds of packing, hydrodynamics and mass transfer analyses for wire mesh packing, especially when the layers of mesh are placed together horizontally, as in a sandwich, rather than vertically, as in [149]; performance comparisons between RPBs and PBCs in terms of the MT rate and the reduction in energy consumption in the stripping process when using nanofluids or other advanced solvents; the analysis of industrial applications, which can reduce the environmental effects, especially with the use of CFD tools; finally, more 3D CFD simulations of multiphase RPBs to investigate the real definition of hydrodynamics and MT, and the further development of simple and acceptable accuracy models to define porous media that can reduce the time and cost of computation, especially in 3D simulations.

7. Conclusions

In this study, a comprehensive review was conducted of the process intensification equipment used for gas absorption processes, which are known as rotating packed beds (RPB) or HiGee contactors. Using centrifugal acceleration in RPBs intensifies the MT coefficient, and this leads to a reduction in the packing volume and energy consumption in comparison with packed beds. The gas velocity and flow area change radially in RPBs; therefore, MT coefficients change from point to point in contactors, but there is no general theory for this, and the prediction of MT coefficients in RPBs is theoretically complicated. Past investigations have shown that the internal $K_Ga$ in the end-effect zone is higher than the value of this coefficient in the bulk zone of the packing, and the MT coefficient strongly depends on the hydrodynamics of two phases. Therefore, further evaluation of this subject is necessary to improve and optimize RPBs. Previous studies have shown that MT coefficients are increase by reductions in boundary layer thickness, as a result of which the HTU will be decreased. Then, the liquid hold-up and pressure drop in RPBs were investigated. Past researchers have demonstrated that suitable dimensionless numbers, such as $Re$, $Ga$, and $Ka$, make hold-up predictions more accurate. Research results have shown that pressure drops are mainly related to the outer radius of the RPB and its packing type. Moreover, a suitable estimation of pressure drop can be achieved using the channel model. Moreover, by adding blades and baffles, one can reduce the total pressure. Unlike in PBCs, the effective MT surface area is not equal to the wet surface area or total surface area in RPBs. A contact area covered by flying droplets, which can be defined by the $We$ number, affects the size of the effective surface area in RPBs. Previous studies have demonstrated
that, in addition to the packing type, a good distribution of the fluid increases the effective surface area in the cavity and packing zones, and is considered as a parameter that effects flooding. The dimensionless numbers that affect MT description correlations are $Re$, $Gr$, $Sc$, $Fr$ and $We$, which were recently improved by adding the geometry factor. The MT rate can be changed locally via the alteration of the flow area, gas, and liquid velocity. CFD and dimensional analysis are efficient tools for studying the RPB. CFD is a suitable tool for surveying hydrodynamic details and the MT rate. The results reveal that, for the achievement of maximum accuracy in the modeling of RPB in the gas–liquid transition process, one can use innovative models that use CT reconstruction for the generation of packing geometry, the VOF model for two-phase modeling, and the realizable $k$-$\varepsilon$ turbulence model for hydrodynamic analysis. Dimensional analysis is an efficient method for the scaling up and benchmarking of RPB systems.

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**Nomenclature**

- $a$: Effective gas–liquid surface (interfacial) area per unit volume of the packed bed, $m^2/m^3$
- $a_c$: Centrifugal acceleration, $= \omega^2 r_{avg} m/s^2$
- $a_s$: Specific surface area, $m^2/m^3$
- $a_t$: Surface area of the packing per unit volume of the bed, $m^2/m^3$
- $a_w$: Wetted surface area, $m^2/m^3$
- $A$, $B$, $C$: Experimental constant,
- $C_{i, CO_2}$: Absorbing component (CO$_2$) inlet concentration, ppm
- $C_{o, CO_2}$: Absorbing component (CO$_2$) outlet concentration, ppm
- $C_s$: Concentration of absorbent media, mol/L or g/L
- $C_{CO_2}^*$: Concentration of absorbent salt, g/L
- $d$: Diameter of packing or equivalent spherical diameter $= \frac{6(1-\varepsilon)}{a_t}$, m
- $d_b$: Average droplet diameter in bulk zone, m
- $d_e$: Average droplet diameter in end zone, m
- $d_h$: Hydraulic diameter, m
- $d_i$: Inner diameter of RZB rotor, m
- $d_o$: Inner diameter of RZB rotor, m
- $d_p$: Pore diameter, mm
- $d_N$: Diameter of nozzles, mm
- $d_w$: Diameter of wire/fiber, mm
- $D$: Diffusivity of the phase, $m^2/s$
$D_i$ Inner diameter of the casing of rotating bed, m
$E$ Reaction enhancement factor
$E_i$ Instantaneous reaction enhancement factor
$f$ Friction factor in RPB or friction coefficient of mechanical seal in RZBs
$f_d$ Reaction enhancement factor
$f_G$ The fraction of volume the liquid distributor occupies in the inner radius of RPBs
$f_e$ Dry resistance coefficient, which depends on the $Q_G$ and $\omega$
$f_{fw}$ Wetted resistance coefficient, which depends on $Q_L$, $\omega$ and $\beta$
$
F_G, int : F_L, int : F_f$ $F$-factor, kg$^{1/2}$/m$^{1/2}$s
$g$ Gravitational acceleration of earth, m/s$^2$
$G$ Gas mass flow rate, kg/s or kg/h
$h$ The (axial) height of packing in RPBs or the height of the annual space at the inner edge of the RZB’s rotor, m
$h_c$ The height of the concentric rings, rotors and packing beds in CRBs, m
$h_f$ The minimum height of the RPB required to prevent its operation in a flooding regime
$H$ Henry’s constant, atm.m$^3$/mol
$H_s$ Solubility coefficient of CO$_2$ in solution, kmol/m$^3$·Pa
$HTU$ Height of a transfer unit, m
$k_G$ Gas phase mass transfer coefficient, g mol/(atm$^2$·m$^2$·s)
$k_L$ Liquid phase mass transfer coefficient, m/s
$k_1$ Reaction rate constant, m$^3$/s
$k_2$ Second-order rate of reaction, m$^3$/kmol·s
$k_{\text{g}}$ Collision kinetic energy loss
$k_{G,a}$ Overall volumetric gas phase mass transfer coefficient, g mol/(atm$^2$·m$^3$·s)
$k_{L,a}$ Overall volumetric liquid phase mass transfer coefficient, 1/s
$k_1$ Departure coefficient of gas (the departure of power for a real liquid flow with a gas flow equal to zero) in RZBs
$k_2$ Departure coefficient of real liquid (the departure of power for a real liquid flow from that of the ideal liquid flow when no gas flows through the rotor) in RZBs
$k_R$ Pseudo first-order rate constant, 1/s
$L, L_p$ Liquid mass flow rate, kg/s or kg/h
$L_p$ Perimeter of rotational baffle channel in contact with fluid, m
$m$ Mass flow rate, kg/s or ton/h
$n$ or $N$ Rotational speed, rpm and number
$N_G$ Power requirement for a gas flow through the rotor, W
$N_i$ Absorption rate of a component, kmol/m$^3$·s
$N_L$ Power requirement for the liquid flow through the rotor, including liquid acceleration and friction losses, W
$N_{LD}$ Power transmitted to liquid flow by a rotation disk and rotational baffles for the ideal liquid flow at a zero gas flow, W
$N_{L,R}$ Power requirement for a liquid flow at a zero gas flow, W
$N_M$ Power requirement due to mechanical friction, proportional to $\omega$, W
$N_o$ Power requirement due to frictional windage drag of a rotor, proportional to $\omega^{1.5}$, W
$N_{tot}$ Total power (Load) consumption, W
$N_T$ Number of theoretical trays
$P_c$ Pressing pressure between the stationary and rotational rings in RZBs
$\Delta P$ Total pressure drop, kPa
$\Delta P_c$ Pressure drop due to centrifugal force, kPa
$\Delta P_{co}$ Wet pressure drop due to centrifugal force without a gas flow, kPa
$\Delta P_d$ Dry pressure drop, kPa
$\Delta P_f$ Pressure drop due to frictional force, kPa
$\Delta P_k$ Pressure drop due to kinetic energy, kPa
$\Delta P_{mo}$ Pressure drop due to momentum gain by gas radial motion in rotors, kPa
$\Delta P_{wo}$ Wet pressure drop, kPa
$\Delta P_{Ts}$ Total pressure drop through stationary rotors (of RSBs), kPa
$q$ Dimensionless initial velocity of liquid
$Q$ Flow rate, m$^3$/h
$Q_{C,CO_2}$ Captured CO$_2$, L/min
| Abbreviation | Description |
|--------------|-------------|
| Q_{CO_2}    | CO_2 flow rate, L/min |
| Q_m         | Minimum wetting rate of packing, m³/m·h |
| Q_s         | Specific flow rate, m³/h |
| r           | Radius of packing or coordinate direction parallel to disk surface, m |
| r_{avg}     | Average radius of a packed bed, m |
| r_RB        | Radius of rotational baffle in RZBs, m |
| r_i         | Inside radial length of packing, mm |
| r_o         | Outside radial length of packing, mm |
| r_h         | Hydraulic radius, m |
| r_z         | Radius of the stationary housing, m |
| r_{M1}      | Outer radius of the annular face with a stationary ring against the rotating ring in RZBs, m |
| r_{M2}      | Inner radius of the annular face with a stationary ring against the rotating ring in RZBs, m |
| Δr          | Distance between the rotational and stationary baffles, m |
| R_{CO_2}    | Rate of CO_2 absorption per unit volume, mol/m³·s |
| R_i         | Inner rotor radius, m |
| R_o         | Outer rotor diameter, m |
| R_p         | Quadratic mean of radius of packing, m |
| s           | Number of packing splits in RSB |
| S           | Area of rotational baffle channel through which fluid passes in a radial direction, m² |
| t           | Treatment time, min |
| T           | Temperature, K |
| π_L         | Liquid mean radial velocity, m/s |
| u_L,r       | Liquid velocity in the radial direction, m/s |
| u_g         | Gas superficial velocity, m/s |
| u_L,s       | Liquid superficial velocity, m/s |
| u_{jet}     | Liquid jet velocity, m/s |
| u_0         | Liquid initial velocity, m/s |
| u_θ         | Gas tangential velocity, m/s |
| V_b         | Packing volume = π (r_o² − r_i²)h, m³ |
| V_i         | Volume inside the inner radius of the bed, m³ |
| V_o         | Volume between the outer radius of the bed and the stationary housing, m³ |
| V_L         | The volume held by liquid in the packing, m³ |
| W_{TEG}     | TEG concentration, % |
| Y           | Mole fraction, % |
| Y_i         | Mole fraction of a component in the inlet gas stream, % |
| Y_o         | Mole fraction of a component in the outlet gas stream, % |
| Y_w         | Mole fractions of water in a gas phase, % |
| Y^*         | Gas phase mole fraction of CO_2 in equilibrium with the concentration of CO_2 in liquid |

**Abbreviations**

- AMP: 2-amino-2-methyl-1-propanol
- ATU: area per transfer unit, m²
- CCD: Charge-coupled device camera
- CRB: Concentric ring rotating bed
- DEA: Diethanolamine
- DEAB: 4-diethylamino-2-butanol
- DEEA: N,N-diethyl ethanolamine
- DIPA: Diisopropandamine
- DMEA: N,N-dimethyl ethanolamine
- 1DMA2P: 1-dimethylamino-2-propanol
- DO: Dissolved oxygen in water
- GS: Gamma scanning
- LDV: Laser doppler velocimetry
- LIF: Laser-induced fluorescence
LES Large eddy simulation
IPA Isopropyl alcohol
HETP Height equivalent to a theoretical plate
MEA Monoethanolamine
MDEA Methyl diethanolamine
NMP N-methyl-2-pyrrolidone
NTU number of transfer units
PIV Particle image velocimetry
PZ Piperazine
RSB Rotating split bed
RTNR Real-time neutron radiography
RZB Rotating zigzag bed
SST Shear–stress transport
TEG Triethylene glycol
VOF Volume of fluid
XCT X-ray computational tomography scanner

Greek Letters

$\beta$ Liquid hold-up, volume of liquid sustained per unit volume of packing, dimensionless
$\beta_v$ mean saturation of packing, the ratio of the overall liquid volume and of the PB total void volume
$<\beta>$ radial saturation mean of the RPB
$\gamma$ Contacting angle, degree
$\delta$ Liquid film thickness, m
$\delta'$ Mean thickness of liquid, m
$\varepsilon$ Porosity of packing
$\zeta$ Liquid maldistribution of injector, %
$\nu$ Kinematic viscosity of liquid, m$^2$/s
$\rho$ density, kg/m$^3$
$\omega$ Angular speed, rad/s or s$^{-1}$
$\sigma$ Surface tension of liquid, N/m or kg/s$^2$
$\sigma_w$ Surface tension of water in 25 $^\circ$C, 0.072 kg/s$^2$
$\sigma_c$ Critical surface tension of packing, N/m or kg/s$^2$
$\xi$ the ratio of liquid jet to the exit-gas kinetic energy
$\phi$ Fractional opening area of rotational baffle in RZBs, dimensionless shape factor number
$\lambda$ Gravity factor
$\tau$ Gas treatment capacity of packing, 1/hr

Subscripts

B, b Packing
L Liquid phase
G Gas phase
W Water
IMZ Inner wire mesh packing zone
OPZ Outer resin pin zone

Dimensionless groups

$A$ Absorption factor, $A = \frac{Q_L}{n_{O}}$
$Ca$ Capillary number
$Fr$ Froude number, $Fr = \frac{Q_L}{\sqrt{R_{k}}}$
$Ga$ Galileo number, $Ga = \frac{n_1^{3/2}r_c^{3/2}}{\rho g a}$
$Ha$ Hatta numbers, $Ha = \frac{\sqrt{k_{CO_2} k}}{r_c^{3/2}n_{O}}$ (where $k$ is reaction rate constant of CO$_2$ m$^3$/kmol·s in case of NaOH solution)
$H_y$ Dimensionless Henry’s constant
Kapitza number $Ka = \frac{\mu^2 \rho a}{\rho_0 d^2}$
Modified Galileo number $Ga^* = \frac{D_p L \left( \rho_p u - \rho a \right)}{\mu_L}$
Molar Ratio $Mr = \frac{Q_L C_a}{Q \Delta C}$
Ohnesorge number $Oh_{in} = \frac{\mu L}{ad_p \sqrt{\rho_0 d m \Delta p}}$
Reynolds number $Re = \frac{\rho L u d_p}{\mu}$
$Re_{in} = \frac{\rho L u d_p}{\mu_L}$
Particle Reynolds number $Re_p = \frac{m u d_p}{\mu a}$
Rotational Reynolds number $Re_\omega = \frac{\omega \rho a d_p^3}{\mu L}$
Schmidt number $Sc = \frac{\mu}{\rho D}$
Weber number $We = \frac{Q^2 \rho u d_p}{(2\pi R^2) \sigma}$

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