New gamma ray signal from gravitationally boosted neutralinos at the galactic center

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We discuss on the possibility that colliding dark matter particles in the form of neutralinos may be gravitationally boosted near the super-massive black hole at the galactic center so that they can have enough collision energy to annihilate into a stau pair. Since in some phenomenologically favored supersymmetric models the mass splitting between the neutralino and the lightest stau, one of the two scalar superpartners of the tau lepton, is a few GeVs, this channel may be allowed. In addition, staus can only decay into a tau lepton and another neutralino. We calculate the gamma-ray spectrum and flux generated by the tau pair discussing the observability of the obtained features.

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Dark matter (DM) accounts for more than 80% of the mass of the Universe but its nature is still one of the open problems in Physics. In a widely accepted theoretical scenario, DM is formed by a weakly interacting massive particle (WIMP) that has been in thermal equilibrium with Standard Model (SM) matter in the early Universe, leaving, after decoupling, the DM relic density as inferred by WMAP [1]. In this light, supersymmetric (SUSY) extensions of the SM provide a natural WIMP candidate. In the minimal supersymmetric standard model (MSSM), R-parity conservation assures that if the lightest supersymmetric particle is the lightest of the four neutralino states—indicated as $\chi$ in the following—, this particle is absolutely stable. In a phenomenologically favored scenario of the constrained MSSM (CMSSM), the stau coannihilation region ($\tilde{\tau}_{CR}$) [2], the lightest stau, $\tilde{\tau}_1$, one of the scalar super-partners of the tau lepton, is close in mass to the neutralino. In the $\tilde{\tau}_{CR}$ parameter space the cross section for non-relativistic annihilation into fermions of the SM, $\chi\chi \rightarrow f\bar{f}$, is typically small and results in a too large relic density. In the minimal supersymmetric standard model (MSSM), R-parity conservation assures that if the lightest supersymmetric particle is the lightest of the four neutralino states—indicated as $\chi$ in the following—, this particle is absolutely stable. In a phenomenologically favored scenario of the constrained MSSM (CMSSM), the stau coannihilation region ($\tilde{\tau}_{CR}$) [2], the lightest stau, $\tilde{\tau}_1$, one of the scalar super-partners of the tau lepton, is close in mass to the neutralino. In the $\tilde{\tau}_{CR}$ parameter space the cross section for non-relativistic annihilation into fermions of the SM, $\chi\chi \rightarrow f\bar{f}$, is typically small and results in a too large relic density. Therefore, the highest chances to detect an observable indirect signal of their existence are attained in a region with high DM density, in particular, in the galactic center (GC). Among the various signatures from DM annihilation, gamma-ray signals have received much attention. A continuum spectrum of secondary photons may arise from hadronization and decay of the annihilation products [2] and from radiation from final state charged particles [6]. Direct annihilation into photons is also possible but only at loop level [7].

The gravitational potential in the GC is dominated by a super-massive black hole (BH) with mass $M_{\text{BH}} = 4 \times 10^6 M_\odot$ and Schwarzschild radius $R_S = 2 G M_{\text{BH}}/c^2 = 4 \times 10^{-7} \text{pc}$ [8]. Recently, the idea that a BH can act as a particle accelerator has been proposed [9]. The highest center of mass frame (CMF) energies are obtained when the colliding particles approach the horizon on falling geodesics with opposite angular momentum per unit mass $L/m_\chi \leq L_c = 4 G M_{\text{BH}}/c$, in the case of the Schwarzschild metric. The maximum possible value is $\sqrt{s} = 2\sqrt{5} m_\chi$ for a non-rotating BH, while it can be arbitrarily large for the Kerr BH [9]. In principle, due to this general relativity effect, new annihilation channels into heavier states, kinematically forbidden for non-relativistic particles, could be accessible. Additionally, a realistic calculation of an indirect DM signal in this scenario would also be determined by the particle escape function at distances close to the BH. For the horizon proximity this has been calculated in [11] under the restrictive assumptions of annihilation into two massless particles with isotropic angular distribution.

In this work we show that if DM is formed by neutralinos with the characteristics of the $\tilde{\tau}_{CR}$, a new dominant annihilation channel may be opened already for sub-relativistic neutralinos [12] boosted in the inner regions of the GC.

Near the BH the DM density is described by a power-law $\rho(r) \propto r^{-\gamma}$, as we will discuss later. From the Newtonian approximation given by the Jeans equation, the root mean squared velocity is $v(r) \approx (G M_{\text{BH}}/r)^{1/2}$ [13–16], or in terms of the Schwarzschild radius, $v(r)/c \approx (R_S/2r)^{1/2}$. Since a Keplerian orbit with $L_c$ would cross the horizon if the pericenter distance is less than $r_{\text{min}} = 4 R_S$, hence we will consider safely $r > 4 R_S$. In this way,
for example, at \( r = 10R_S \) we have \( v/c \simeq 1/\sqrt{20} \simeq 0.22 \). Requiring that the neutralino has the relic density inferred by WMAP, the relative mass splitting with the \( \tilde{\tau}_1 \), \( \delta = (m_{\tilde{\tau}} - m_{\chi})/m_{\chi} \), is typically less than 5%. In the CMF the energy threshold for stau pair production is \( \sqrt{s} = 2E_\chi \geq 2m_{\tilde{\tau}} \), that implies \( v/c \geq [1 - 1/(1 + \delta)]^{1/2} \). With \( \delta = 2\% \), \( v/c \geq 0.197 \): there exists thus a range of radii where the kinetic energy is high enough to reach the threshold of the process \( \chi \chi \to \tilde{\tau}^- \tilde{\tau}^+ \). The maximum radius is given by \( r_{\text{max}} = 1/2[1 - (m_S/m_{\tilde{\tau}})^2]R_S \).

If the mass splitting \( \Delta m = m_{\tilde{\tau}} - m_\chi \) is larger than the tau mass, \( m_\tau = 1.777 \) GeV, the staus can only decay into the two body final state \( \chi \tau \), see diagrams in Fig. 1.

The neutralino is bino-like thus the vertices’ \( \chi - \chi Z \) and \( \chi - \chi (h, H) \) are suppressed, while the vertex \( \chi - \tilde{\tau}_1 \tau \) is not suppressed by mixing. In fact it is proportional to \( Z_{13}U_{12} \), the product of the relevant neutralino and stau mixing matrix elements that are both close to one. The dominant diagrams in Fig. 1 are thus the ones with \( t, u \) channel exchange of the tau. At energies near the threshold the produced staus are slow thus the propagator \( 1/(p_{\tilde{\tau}}^2 - m_{\tilde{\tau}}^2) \) becomes resonant. In the right panels we have \( 1/m_{\tilde{\tau}} - m_\tau \), \( p_{\tilde{\tau}} - m_\tau \). The cross section, proportional to the square of this quantity is, thus, enhanced for mass splittings approaching the tau mass.

We illustrate the above features in Fig. 2 where we show the relevant cross sections as a function of \( \sqrt{s} \), left panels, for four points of the \( \tilde{\tau}_{1\chi} \), that are allowed by present phenomenological constraints. The values of the universal scalar mass \( m_0 \), gaugino mass \( m_{1/2} \), trilinear scalar coupling \( A_0 \) and the ratio of the two Higgs expectation values \( \tan \beta \) that define the CMSSM parameter space are given in Table I. The numerical computation was done using the interfaced codes MicrOMEGAs [18], CalcHEP [17] and SOFTSUSY [13]. The point A is similar to best-fit point found in [19], that predict a light Higgs around 119 GeV. Next we take three cases with \( A_0 = 0 \), as usual for setting upper limits with LHC searches. In the point B the Higgs is slightly heavier. Points C and D have low \( \tan \beta \) and the Higgs is around 115 GeV. In all cases, the cross section for stau pair-production clearly dominates by one or two orders of magnitude the cross sections for annihilation into fermions except when \( \sqrt{s} \) corresponds to the heavy Higgs A, H masses where the s-channel propagators are resonant. In the right panels in Fig. 2 we show the annihilation cross section times the particle relative velocity, as a function the colliding neutralino velocity (right panels). The CMSSM points are specified in Table I and the annihilation channels are labeled in the upper left panel.
TABLE I. CMSSM points used in his work. The sign of $\mu$ is positive. The neutralino and stau masses are also reported.

| $m_0$ (GeV) | $m_{1/2}$ (GeV) | $A_0$ (GeV) | $\tan \beta$ | $m_{\tilde{\chi}}$ (GeV) | $m_{\tilde{\tau}}$ (GeV) |
|------------|----------------|-------------|--------------|----------------|----------------|
| A          | 452            | 780         | 1110         | 41             | 327.2          | 333.6          |
| B          | 858            | 1780        | 0            | 45             | 789.0          | 782.2          |
| C          | 122            | 600         | 0            | 10             | 247.6          | 252.7          |
| D          | 166            | 805         | 0            | 10             | 337.3          | 339.4          |

degenerate in mass with $\tilde{\tau}_1$ and the cross section for annihilation into pairs of these scalars is much larger than in the cases A and B. Although the masses of the particles in point B are much heavier than in the other cases, the mass splitting is around 3 GeV and $Dw$ is of the same magnitude. The same effect can be seen comparing case D with C.

A possible signal of the opening of the new channel is given by the gamma-rays produced by the tau pair. The extension of the source is set by $r_{\text{max}}$. This is too small to be resolved by present telescopes, thus we treat it as point source at the GC at a distance from us of $D = 8$ kpc. To evaluate the flux we first note that applying the small width approximation to the tau propagators, and given that $BR(\tilde{\tau}_1^\pm \rightarrow \tau^\pm \chi) = 1$, we have $\sigma(\chi\chi \rightarrow \tau^+ \tau^- \chi) = \sigma(\chi \rightarrow \tilde{\tau}_1 \tilde{\tau}_1) BR^2(\tilde{\tau}_1 \rightarrow \chi \chi) \approx \sigma(\chi \rightarrow \tilde{\tau}_1 \tilde{\tau}_1) \equiv \sigma_{\tau \tau}$. We can thus evaluate the differential photon flux as

$$\frac{d\Phi}{dE_\gamma} = \frac{R_3^3}{D^2} \int_{r_{\text{min}}}^{r_{\text{max}}} dr r^2 \sigma_{\tau \tau}(r) \rho^2(r) \frac{dN}{m_{\tilde{\chi}}^2} \frac{dN}{dE_\gamma}(r).$$

In the integral we treat the distances in units of the Schwarzschild radius, thus $r$ is dimensionless and a factor $R_3^3$ appears explicitly. We note some differences with the standard almost-static $\chi\chi \rightarrow \tau^+ \tau^-$ annihilation: (i) there is no factorization into a particle physics and astrophysics factor because all the factors in the integrand depend on $r$ through the velocity dependence. An integration over the CMF scattering angle is implied in $\sigma_{\tau \tau}(r)$ that is evaluated taking the exact spin averaged squared matrix elements from CalcHEP; (ii) we do not divide by 2 because the final state necessarily contains two neutralinos; (iii) the taus are not monochromatic and the spectrum changes with the collision energy $\sqrt{s}$ and ultimately with the distance, while in the static case the taus have an energy equal to the neutralino mass and the radiated photon spectrum is limited by $E_\gamma^\text{max} = E_\tau = m_{\chi}$.

Before proceeding further we will discuss this last point. The tau energy spectrum can be easily obtained by applying a Lorentz transformation with parameters $\beta = (1 - 4m_{\tau}^2/s)^{1/2}$ and $\gamma = \sqrt{s}/2m_{\tau}$, to the spectrum calculated in the rest frame of the tau. In this frame it has fixed energy and momentum, $E_\tau^* = (m_{\tau}^2 - m_{\tilde{\tau}}^2 + m_{\chi}^2)/2m_{\tau}$ and $p^*_\tau = (E_{\tau}^* - m_{\tau}^2)/2E_{\tau}^*$. The resulting energy distribution is flat and limited, $dN(\tau_1 \rightarrow \chi \chi)/dE_\tau = 1/\Delta E$, $\Delta E = E_{\tau}^\text{max} - E_{\tau}^\text{min}$, with $E_{\tau}^\text{min} = \gamma(E_{\tau}^* - \beta p^*_\tau) \leq E_{\tau} \leq E_{\tau}^\text{max} = \gamma(E_{\tau}^* + \beta p^*_\tau)$. The number of photons with energy $E_\tau$ produced by a tau with energy $E_{\tau}$ is given by $dN_\gamma/dx = 1/2f(x)$ with $x = E_{\tau}/E_{\tau}$ and $f(x) = x^{-3/2} \exp[g(x)] + q \log[p(1-x)](x^2-2x+2)/x$. This formula was obtained in Ref. [21], to which we refer the reader for details, by fitting the photon yield from taus obtained with Monte Carlo simulations of the non relativistic process $\chi\chi \rightarrow \tau^+ \tau^-$. In this case the taus have equal energy, hence we use a factor $1/2$ for the yield of one particle. The gamma spectrum at distance $r$ is then obtained by integrating over the tau energy distribution,

$$\frac{dN}{dE_\gamma}(r) = \frac{1}{\Delta E(r)} \int_{E_{\tau}^\text{min}(r)}^{E_{\tau}^\text{max}(r)} dE_\tau f\left(\frac{E_\tau}{E_{\tau}}\right) \theta(E_{\tau} - E_{\gamma}).$$

We have multiplied by 2 to obtain the yield of the pair. The Heaviside function takes into account that for fixed $E_{\tau}$ the integrand is zero if $E_\gamma > E_{\tau}$. For this reason the photon energy cut-off is $E_{\tau}^\text{min}$ for each $\sqrt{s}$. The absolute cut off when integrating over $\sqrt{s}$ will be at $\gamma(r_{\text{max}})E_{\tau}^\text{max}$. In fact as $r \rightarrow r_{\text{max}}$, $\beta \rightarrow 0$ and $E_{\tau}^\text{min} \rightarrow \gamma(r_{\text{max}})E_{\tau}^\text{max}$. Note that $\gamma(r_{\text{max}}) \sim 1$ and $E_{\tau}^\text{max} \lesssim (m_{\tilde{\tau}} - m_{\chi})$, thus the cut off is indicative of the mass splitting between the neutralino and the stau.

The last ingredient that we need to evaluate in Eq. (11) is the DM density profile. In [21] it was shown that the adiabatic growth of the BH at the center of the halo causes a steepening, called spike, of the initial DM profile toward the GC. Successive studies [13, 15, 22–28] showed that considering physical effects such as scattering of DM particles off stars, capture by the BH, self-annihilation and capture within stars during the evolution of the DM distribution, results in a shallower profile, $\rho_{\text{sp}}(r) \propto r^{-3/2}$. For the SUSY models A-D, and generally for all the $\tilde{\chi}_m$ parameter space, the spin independent and spin dependent elastic neutralino-nucleon cross sections are in the range $10^{-11}$–$10^{-9}$ pb and $10^{-8}$–$10^{-7}$ pb respectively, thus the energy lost by elastic collisions with baryonic matter is not likely to be important. At a certain distance from the GC the density reaches a value such that self-annihilation itself acts to stop further rising. It has been shown [27, 28] that this latter effect do not set the density to a constant value, usually called annihilation plateau or core, but results in a mild spike (MS) with $\rho_{\text{MS}}(r) \propto r^{-1/2}$. In addition, the adiabatic compression of the gravitational potential caused by the baryons already in the bulge of the galaxy [30] should also be taken into account.

We hence model the profile considering that at the radius $r_{sp} \approx 0.2r_h$, with $r_h = 1.67$ pc the influence radius
The values of $\sigma_v$ by matching the two power-laws, $r$ in [12], the cross section for annihilation into leptons is $-1$ and $t$ up to the radius $\rho$ of the BH, DM density is given by a compressed Einasto profile, $\rho_{sp} = 5 \times 10^6$ GeV/cm$^3$ as in [22]. From here the profile is given by $\rho(r) = \rho_{sp}(r/r_{sp})^{-\gamma_{sp}}$, $\gamma_{sp} = 3/2$, up to the radius $r_a$ where the density reaches the value $\rho_a = m_\chi/(c_0)t_f$. $\sigma v_0$ is the annihilation cross section and $t_f = 10$ Gyr [22, 23] is the elapsed time since the formation of the spike. Finally, the inner MS is $\rho_a(r/r_a)^{-\gamma_a}$, $\gamma_a = 1/2$, up to the limit $4R_\odot$. The radius $r_a$ is found by matching the two power-laws, $r_a = r_{sp}(\rho_a/\rho_{sp})^{1/\gamma_{sp}}$. The values of $\rho_a$ are between $10^{11} - 10^{12}$ GeV/cm$^3$ and $r_a$ are of the order $10^{-4}$ pc for the CMSSM points A-D. In the cases C and D, $\sigma v$ in the non relativistic limit is around $10^{-29}$ cm$^3$/s that would result in $\rho_a$ a factor $10^2$ larger than in A and B. Anyway, as was already noted in [12], the cross section for annihilation into leptons is strongly velocity dependent as can be seen in Fig. 2 it rises rapidly reaching values around $10^{-27}$ cm$^3$/s at $v/c \sim 0.1 - 0.2$, thus $\rho_a$ is of the same order as in A and B.

In the top panel of Fig. 3 we show the differential flux multiplied by $E_\gamma^2$ to exhibit the behavior at the highest energies near the cut off. In the bottom panel, the differential photon flux is given by the dots. We find that the spectral shape of the flux is well fitted with the sum of two exponentials, as shown by the dashed lines in the bottom panel. The functional form is $F(x) = F_0 + F_1 \exp(-E_\gamma/E_1) + F_2 \exp(-E_\gamma/E_2)$ with $F_0$, $F_1$, $F_2$, $E_1$, $E_2$ fit parameters.

The peculiar characteristics of the signal are: (i) its origin is in the innermost region around the BH where the DM distribution is given by the MS density; (ii) the differential flux presents a nearly exponential shape with a hard cut-off that is determined by the mass splitting between the neutralino and the stau; (iii) the signal shows up at energies below 10 GeV. Interestingly, in this few GeV energy region there are some unexplained excesses over the known backgrounds [31, 32]. However our predicted signal is too feeble to account for them. It is expected that after 5 years operation, the Fermi-LAT satellite reaches sensitivities of $10^{-10} - 0.5 \times 10^{-11}$ photons cm$^{-2}$ s$^{-1}$ for energies between 0.5 GeV and 10 GeV [23]. The proposed signal can be one of the components observed by the collaboration. Furthermore, it might be discriminated by the new proposed experiment Gamma-Light [33] that should achieve a better energy and angular resolution than Fermi-LAT in the interval (10 MeV-1 GeV).

In summary, we have shown that if DM is formed by neutralinos as described in the stau coannihilation region of the CMSSM, stau pair production may be the dominant annihilation channel in the innermost region of the GC near the BH. We have further shown that the gamma-ray spectrum produced by the $\tau\tau$ pair coming from the decay of the staus present peculiar features. This may further motivate the exploration of the GC by the Fermi-LAT satellite to achieve a better understanding of backgrounds and to look for a possible new indirect signal of the presence of a DM component.

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FIG. 3. Top panel: differential flux multiplied by $E_\gamma^2$. Bottom panel: Differential flux (dots) and fit (dashed lines) with $F(x) = F_0 + F_1 \exp(-E_\gamma/E_1) + F_2 \exp(-E_\gamma/E_2)$, $F_0$, $F_1$, $F_2$, $E_1$, $E_2$ are fit parameters.
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