Parallel battery pack charging strategy under various ambient temperatures based on minimum lithium plating overpotential control

Hanqing Yu, Long Yang, Lisheng Zhang, Junfu Li, Xinhua Liu
lijunfu@hit.edu.cn (J.L.)
liuxinhua19@buaa.edu.cn (X.L.)

Highlights
A cell model is established accurately under various C-rates and temperatures

The contact and wire resistances are considered into the battery pack circuit model

Side reactions like Li plating are accurately described in the model during cycling

Charging strategy for parallel battery pack is adopted to prevent side reactions

Yu et al., iScience 25, 104243 May 20, 2022 © 2022 The Author(s). https://doi.org/10.1016/j.isci.2022.104243
Parallel battery pack charging strategy under various ambient temperatures based on minimum lithium plating overpotential control

Hanqing Yu,1,2 Long Yang,1 Lisheng Zhang,2 Junfu Li,1,* and Xinhua Liu2,3,*

SUMMARY

With the aggravation of environmental pollution and energy crisis, lithium-ion batteries are widely regarded as promising. However, the current distribution in the parallel battery pack branches is highly heterogeneous. Charging strategies based on the models can be adopted to prevent side reactions that may lead to severe degradation or even thermal runaway under various ambient temperatures. In this study, a battery model for a single cell is established by coupling a single particle model with electrolyte, degradation model, and thermal model. Besides, considering the contact resistance and wire resistance, the circuit model of a battery pack is established. A charging strategy based on minimum Li plating overpotential control is then adopted, and the effectiveness under high C-rate and low temperature to reduce capacity loss is verified by simulation. This study provides a low-loss charging strategy that can reduce the safety risk of battery packs with better performance under various ambient temperatures.

INTRODUCTION

As the aggravation of environmental pollution and energy crisis, the use of new energy has become a hot-spot, such as new energy vehicles and energy storage systems. Lithium-ion batteries (LIBs) have been widely used because of stable discharge, low self-discharge rate, long cycle life, and other advantages (Chen et al., 2019; Zhao et al., 2021). However, a single cell is far from meeting the requirements of a system, so a large number of cells need to be connected in series or parallel with each other to form a battery pack. Compared to series battery packs, the current distribution of each branch for parallel battery pack is very inconsistent and complicated because of the resistances caused by the wire and welding (Hosseinzadeh et al., 2021; Wu et al., 2021). In addition, the current is closely related to the side reactions; performance of the battery packs will degenerate after some cycles (Tang et al., 2021). Meanwhile, with the continuous improvement of energy consumption level, there is an increasing demand for large-capacity new energy storage and power facilities, which requires corresponding digital life-cycle management solution (Yang et al., 2020; Wu et al., 2020; Gao et al., 2021), and charging technology is an important part.

LIB is a complicated system for its internal interaction. Thus, the mathematical relationship between environmental factors and battery characteristics should be determined by establishing the model, which is very important to optimize battery design and manage batteries (Zhou et al., 2022; Hosen et al., 2021). There are many battery models based on experience and data, such as the equivalent circuit model (ECM) and the data-driven model (Nikdel, 2014; Dang et al., 2016). However, they often do not fully reflect the overall state of the battery, so have certain limitations. There are many studies to establish models for predicting voltage based on the electrochemical properties of LIB. The most recognized model is the pseudo-two-dimensional (P2D) model proposed by Doyle et al. (1993). However, because the calculation process of the P2D model is too complicated and will consume too many computing resources, many studies have simplified it, among which the single particle model (SPM) is the most common one (Zhang et al., 2000). SPM ignores the concentration and potential changes in the electrolyte, which results in poor accuracy of the model, especially at large C-rates and low ambient temperatures. To solve this problem, a single particle model with electrolyte (SPMe) has been used (Li et al., 2021a). It improves the prediction accuracy by considering the influence of electrolyte. Besides, the electrochemical process of LIB also affects aging and heat generation. As for the aging process, side reactions on the anode have been the focus of research (Lu et al., 2021), and the processes of solid electrolyte interface (SEI) film growth and Li
plating are usually modeled (Reniers et al., 2019). For the heat generation process, Bernardi et al. (1985) proposed a universal thermal model based on thermodynamic energy balance, which had been used in almost all studies of battery heat generation. However, the original model is complicated. Considering the characteristics of commercial batteries, some factors with relatively small effects can be ignored to simplify the model (Gottapu et al., 2021).

For parallel battery packs, the inconsistency of current distribution has been studied in many previous studies (Wu et al., 2013; Brand et al., 2016). In addition, ambient temperature is an important factor (Xie et al., 2021). Compared with single cells, different degradation behaviors at the battery pack level have also been reported (Shi et al., 2016; Wang et al., 2019). Dubarry et al. (2016) developed a useful equivalent circuit model to simulate the spontaneous transient balancing currents among parallel strings. The study could help understand transient behavior to help with battery management, maintenance, and repair. Schindler et al. (2020) further studied the influence of connection characteristics inside the battery pack on current distribution. It was found that cross-connectors could effectively balance the battery system. In addition, the study showed that string-connect resistances contributed more toward current distribution than welding seam and cross-connector resistances. In the previous study of Liu et al. (2019a), the circuit model of six parallel cells was established, and each single cell was realized by a thermally coupled single particle model. The effects of intercell variation and thermal gradient on the performance and degradation were studied in detail.

With the rapid increase of the demand for fast charging, battery charging technology has gradually attracted widespread interest. Tomaszewska et al. (2019) reviewed the literature on the physical phenomena that limit battery charging speeds, the degradation mechanisms that commonly result from charging at high currents, and the approaches that have been proposed to address these issues, which suggested that the problem of fast charging could be solved by developing battery multi-scale design and charging strategies. In terms of battery design, emerging materials that can improve battery performance are always the focus, such as electrodes with low tortuosity and electrolytes with high Li transference number, which can fundamentally improve the charging C-rate without serious degradation (Liu et al., 2019b; Peng et al., 2021; Yan et al., 2021). Based on already established commercial LIBs, there are also many fast charging strategies for health and efficiency, such as constant current-constant voltage (CC-CV), multistage constant-current (MCC), and pulse charging (Tomaszewska et al., 2019). These charging strategies are convenient but lack feedback from the battery itself. They may cause side reactions to affect battery performance and safety, and bring some additional risks, such as thermal runaway. Ouyang’s group (Li et al., 2019) explained that the reaction between the plated lithium and electrolyte was revealed to be the mechanism of thermal runaway triggering and warned us of the danger of the plated lithium in the utilization of lithium-ion batteries. Thus, it is necessary to limit Li plating during fast charging. As a result, there are more and more studies on exploring charging strategies based on the characteristics of models (Zhang et al., 2017; Yang et al., 2021). In addition, it should be noted that because of the complex operating environment, the charging strategies must meet the requirements of fast charging under various ambient temperatures. There have also been some studies reported on fast charging at low ambient temperatures (Xie et al., 2020; Nambisan et al., 2021). However, most of these studies are based on ECM, which cannot reflect the physical information inside the battery. At the same time, most of them are based on existing charging protocols and lack precise feedback control.

However, it is difficult and important to study the fast charging strategy of battery packs because of the inconsistencies of cells. Ouyang et al. (2019) proposed a distributed charging strategy considering both charging time and capacity loss, which had low computational cost and high robustness. Li et al. (2021b) established a complete battery pack model by combining the cell model, battery pack cooling model, and battery pack balance management model. In addition, a fast charging strategy based on the shortest charging time was proposed. The results showed that the fast charging strategy could significantly shorten the charging time but would lead to increased aging and energy loss. In addition, there is no feedback in the established fast charge protocols, which cannot control the side reactions of batteries. However, the current of fast charging is relatively large. Besides, owing to the current inconsistency of parallel battery packs, the currents on some branches tend to reach a higher C-rate, which will lead to excessive degradation of the cell on the branch, resulting in accelerating degradation of the battery pack performance. These causes can easily cause serious harm to the electrochemical and safety performance of batteries leading to accelerated degradation (Tomaszewska et al., 2019; Wang et al., 2021a) or even catastrophic events like...
thermal runaway under extreme conditions (Feng et al., 2020). At the same time, the fast charging and discharging is an important approach to improve the efficiency of vehicle-to-grid (V2G) storage configuration (Dioha et al., 2022). In this case, both vehicles and power grid energy storage facilities are faced with the problem of degradation in the process of fast charging. Therefore, it is necessary to design a model-based fast charging strategy, which can well control the occurrence of side reactions, and can significantly reduce the degradation of electrochemical and safety performance. Yang et al. (2019) reported a controllable cell structure, which could quickly heat the battery to high temperatures to eliminate lithium plating during charging. Chu et al. (2017) constructed a close-loop observer of lithium deposition status based on the simplified P2D model. The charging current was modified online using the feedback of the lithium deposition status. In addition, the postmortem observation and degradation tests were performed. The results showed that no lithium deposition occurred during fast charging.

In this paper, in terms of the fast charging strategy of parallel battery packs, an appropriate model should be established to control side reactions under various ambient temperatures, so as to prevent side reactions. Firstly, the cell model was established by coupling the SPMe, degradation model and thermal model. Then, considering the contact resistance and the wire resistance, the circuit model of the parallel battery pack was established. After that, based on the model, a parallel battery pack charging strategy based on minimum Li plating overpotential control (MLPOC) was adopted to realize the control of minimum Li plating. The closed-loop optimization framework of input current under various ambient temperatures was established. Finally, the simulation based on the model and charging control strategy was carried out, and the results were compared to verify the effectiveness of the proposed model and strategy.

RESULTS
Parallel battery pack model
In this chapter, a SPMe is developed for the single cell considering thermal effects and typical side reactions. In addition, six cells are parallel-connected to create a battery pack with current input and output on the one side. There is a branch resistance in each branch in series with the cell and an interconnect resistance at each end of each branch. There is also an electrochemical performance simulation of one particular cell in this chapter.

Single cell model
To better describe the behaviors of LIBs in fast charging and under various ambient temperatures, the single cell model can be divided into three main parts: SPMe, degradation model because of side reactions, and thermal model.

SPM is the most widely used simplified version of the P2D model, and is based on the following assumptions:

[A1] The concentration distribution within the electrolyte is ignored, and the potential of the liquid phase is assumed to be 0 V when calculating the terminal voltage.

[A2] The active material in each electrode region is abstracted as a single particle and the solid phase is homogeneous. This means that the potential of the anode and cathode in their respective regions is a fixed value and does not change with the change of position in the direction of the electrode plate thickness.

The thermally coupled SPM has been discussed in depth in our previous studies (Liu et al., 2019a; Yang et al., 2021). In this study, in order to improve the accuracy of the model and the applicability under various ambient temperatures, the Assumption [A1] is canceled and the SPMe is established by considering the concentration distribution and liquid phase potential within the electrolyte.

LIBs are mainly composed of anode, separator, and cathode and are filled with electrolyte inside. The basic structure of LIBs is shown in Figure 1. In the x direction, the compositions are superposed. Since the Assumption [A2], the active material in each electrode region can be approximately described as a spherical active material particle, respectively. The radial direction inside the particle is defined as r direction. For the convenience of describing the behavior of lithium-ions in electrolyte, the distribution of ion current
density $i_e$ and molar ion flux $j_n$ in the direction of the electrode plate thickness are shown in Figure 2. In addition, the block diagram of SPMe is shown in Figure 3.

Detailed descriptions for the three submodels of the single cell model are provided in Method details. They are related to each other. The coupling relationship among them is shown in Figure 4. At the top of the figure, there is the SPMe which works with lithium-ion transferred between the cathode and anode. It should be noted that lithium-ion must be intercalated or delaminated through the film on the anode surface. On the left of the figure, there is the degradation model which is used to calculate SEI film growth and Li plating. On the right of the figure, there is the thermal model, which considers both the heat generation and external natural convection heat dissipation. In the process of model calculation, the SPMe provided the current and reaction polarization overpotential for the thermal model to calculate the heat generation rate, and provided the side reaction overpotentials for the degradation model. The thermal model is used to determine the battery temperature and the influence of the electrochemical parameters in the SPMe and degradation models. The degradation model causes the increase of internal resistance and the capacity loss in SPMe, and the increase of internal resistance can lead to the increase of heat generation, thus affecting the thermal model.

In this work, the simulated cell was the pouch cell with capacity of 5 Ah, which contains NCM-LCO composite cathodes and graphite anodes. Specific parameters for the cell are shown in Table S1. The cell model is
further used in exploration of the charge strategy proposed later. Since the cell does not change much with
the high ambient temperatures (Wang et al., 2021b), this study mainly investigates the performance of the
cell with the low ambient temperatures because of the great influence on the side reactions. Figure 5 shows
the simulation results of the single cell in the battery pack at different C-rates (0.5C, 1C, and 2C) and tem-
peratures (−10°C, 0°C, 10°C, and 20°C). Figure 5A shows the change of cell voltage, and Figure 5B shows
the change of cell temperature. For side reactions, the electrochemical overpotential of Li plating and the
capacity loss caused by SEI growth and Li plating are shown in Figures 5C and 5D, respectively.

It should be noted from Figure 5A that with the increase of C-rate or the decrease of ambient temperature,
the battery voltage curve with high C-rate, or low ambient temperature will be higher because of more
serious polarization, thus reaching cut-off voltage in advance. In the absence of a CV process, cells with
higher C-rate or lower ambient temperature have lower charging capacity. In addition, as can be seen
from the local magnified image of Figure 5A, the increase of C-rate tends to lead to upward movement
of the curve, making the reaction more intense; the decrease of ambient temperature tends to cause
the curve to shift to the left, bringing forward the reaction. They all result in the cell reaching the cut-off
voltage earlier. According to Equation 37, when the convective transfer coefficient $h$ is 5 (W/m²K) as natural
convection, the temperature rise also increases with the increase of C-rate or the decrease of ambient tem-
perature. For side reactions, as $\eta_{pl}$ decreases during charging, a danger zone, which indicated in blue in
Figure 5C, is formed when $\eta_{pl}$ is below 0 V, with a risk of Li plating. Obviously, the C-rate is higher or

**Figure 3. Block diagram of SPMe**

**Figure 4. Coupling relationship of the three submodels of the single cell model**
the ambient temperature is lower, and the risk of Li plating is greater. As shown in Figure 5C, under the charging condition of C-rate of 2C and ambient temperature of 20°C, the cell is at risk during most of the charging time, resulting in more severe capacity loss, as shown in Figure 5D. In contrast, under the ambient temperature of 20°C, Li plating stays above 0 V all the time at the C-rate of 0.5C and 1C, whose capacity loss is mainly because of the growth of SEI film. At the same time, with the decrease of ambient temperature, Li plating overpotential will also be lower, increasing the risk of Li plating and the capacity loss. The aforementioned conclusions are in accordance with the law, the increase of C-rate or the decrease of ambient temperature will make the working conditions of the cell become bad, thus reducing the electrochemical performance (Wang et al., 2021b; Yu et al., 2022).

Parallel circuit model
The current distribution of parallel battery packs is complex and heterogeneous, mainly because of the differences between the cells in the battery pack and the specific circuit configurations. In this study, to discuss the battery pack control strategy, a circuit model of parallel battery pack is established, as shown in Figure 6. The battery pack model is composed of six cell models in parallel and each cell model is in a separate branch. Each branch uses a branch resistance $R_b$ of 10 mΩ to describe the contact resistance between the connecting plate and the battery pole. The equations of the SPMe are integrated into the MATLAB environment, and the battery pack model is established in the Simulink SimPowerSystems toolbox. There is an

Figure 5. Simulation results of a single cell at different C-rates and different ambient temperatures
(A–D) (A) Voltage curve with charging capacity (V-Ah), (B) Temperature change, (C) Li plating overpotential, and (D) Capacity loss due to side reactions.
interconnection resistance $R_i$ of 0.5 mΩ indicating the influence of wire resistance at both ends of each branch. The current input and output are applied on the left side of the battery pack, with additional interconnection resistances at both ends. Voltage and current measuring tools are placed on each branch and the bus. It should be noted that the values of resistances were determined after referring to some literatures (Xie et al., 2021; Masomtob et al., 2017).

Here, the simulations of battery pack current distribution are carried out under different C-rates. The results under two C-rates (1C and 0.5C) are shown in Figure 7. The results for the other two C-rates (0.75C and 0.25C) are shown in Figure S1. The results show the serious heterogeneity of current distribution because of the particularity of parallel configuration. Similar trend of current distribution can be observed from curves of different C-rates. Cell B₁ usually has the largest fluctuation of current among the six cells. The current amplitudes of the six cells continued to show severe instability throughout the whole process. It should be noted that the branch currents fluctuated in Figure 7. This was because different branch currents at the beginning led to different charging or discharging capacities of each cell; that is, each cell had a different SOC. Considering the nonlinear OCV-SOC curve, the OCV variation of each cell was nonlinear and very complex. At the same time, there were also a series of inflection points and steps in the OCV curve (Li et al., 2021c). A series of factors caused the currents to fluctuate.

Charging strategy based on minimum Li plating overpotential control

Although charging technology has been greatly developed, most of the current research is applied to single cells, and there is little focus on the control strategy preventing side reactions during charging. When the overpotential of Li plating is close to 0 V or even lower, Li plating is easy to occur on the anode surface, resulting in irreversible capacity loss, and even short circuit inside the cell, threatening cell safety. The capacity loss caused by the growth of SEI film is more moderate than that caused by Li plating and occurs almost continuously throughout the cycle life. The growth of SEI film does not seriously affect battery safety. Therefore, based on the proposed electrochemical-side reactions-thermal coupling cell model, a parallel battery pack charging strategy based on minimum Li plating overpotential control (MLPOC) is adopted in this study to achieve the minimum Li plating control during rapid charging under various ambient temperatures, as shown in Figure 8, where $I_{ini}$ is the initial input total current.

Figure 7. Simulation results of current distribution of a battery pack with six identical cells in parallel at different C-rates
(A and B) (A) 1 C and (B) 0.5 C.
At the start of charging, a total current is input to the parallel battery pack model. Because the diffusion process has not been established at the start of charging, temperature only affects the electrochemical reaction. The temperature is lower, and the risk of Li plating is more. As the temperature rises, the overpotentials of reaction polarization and Li plating increase, resulting in the ability to withstand larger applied current without Li plating. However, the effect of electrochemical reaction on battery performance is limited, and when the ambient temperature varies within the conventional range, the proportional change in temperature in Kelvin is relatively small. Particle swarm optimization (PSO) algorithm was used to find the maximum initial charging current of a single cell under various ambient temperatures. According to the previous analysis, the maximum initial charging current changed monotonously with the increase of ambient temperature, so it was only necessary to find the current at the maximum and minimum temperatures. The temperature and initial conditions were set first, and then Li plating overpotential $\eta_{\text{pl}}$ was calculated according to the model. Finally, the maximum initial charging current was obtained when $\eta_{\text{pl}}$ equaled 0 V through iteration. When the ambient temperature range was $-20^\circ\text{C}$ to $40^\circ\text{C}$, the maximum initial current of a single cell varied between 5.96 A to 6.01 A, which is about 1.2C. Therefore, under different ambient temperatures, the initial charging current can be selected as the same value. For convenience, 2C was selected as the initial charging current in consideration of all charging situations such as directly charging after discharging without shelving. In other words, for a parallel battery pack, the initial input total current is the current of a cell multiplied by the number of branches. At the same time, as the charging process goes on, the overpotential will decrease, requiring subsequent control.

After the initial total current is input to the parallel battery pack, the Li plating overpotentials of all single cells are continuously monitored. The minimum value of all overpotentials is obtained through the minimum calculation module, which subtracts the reference value of Li plating 0 V. The result of subtraction is then entered into a proportional integration (PI) controller with a proportional parameter of 0.01 and an integral parameter of 0.00005. It should be noted that the parameters of the PI controller were obtained by the tuning method (Kull et al., 2020). Therefore, a closed loop optimization of charging current is realized by adjusting the charging current according to the output of the PI controller. It should be noted that in the charging process, the temperature will rise, which will affect the internal process of the cells. The PI controller can comprehensively control these effects. In addition, the external performance parameters of all cells are constantly logged into the workspace for further analysis.

**DISCUSSION**

**Battery pack performance without MLPOC**

To verify the control effect of MLPOC under various ambient temperatures, the simulations of battery pack with and without MLPOC under 2C and 1.5C was carried out under the ambient temperature of $0^\circ\text{C}$. Figure 9 shows the simulation results in one cycle under 2C and $0^\circ\text{C}$ without MLPOC. When the average current is 1.5C, the simulation results without MLPOC in one cycle are shown in Figure S2. As shown in Figure 9A, the battery pack voltage is always below or above those of all the cells during the whole process, mainly because of the interconnection resistance between parallel branches. Figure 9B describes the change process of Li plating overpotentials. Combined with the changes of all the cells, in the late discharging process, the overpotentials presents a rising trend overall. This is because the cell temperatures increase with the working process, which improves the working environment of the cells to some extent. In addition, it
can be seen that the Li plating overpotential of cell B_1 is below 0 V during the whole charging process, that is, it has the risk of Li plating during the whole charging process. As shown in Figure 9C, the current fluctuation of cell B_1 is the largest in the charging and discharging process. This is because the cell is located closest to the external structure in the parallel circuit and is most affected by the inconsistency of the battery pack. It should be noted that cell B_1 has the largest charging current of all cells at the start of charging, reaching 20 A (i.e., 4C). Figure 9D describes the temperature changes of the cells. Because the heat generation rate is closely related to the current, the temperature change is related to the current. For example, during the charging process, the current of cells B_1 and B_6 decreases and increases respectively, resulting in their heat generation rate decreases and increases respectively; and during discharging, the temperatures of the cells increase gradually. As shown in Figure S2D, the temperature of cell B_6 even decreases slightly at the end of discharging.

Obviously, with the higher current, the risk of Li plating is higher. In this case, Li plating overpotential of cell B_1 was negative during the charging process, and all cells would undergo Li plating to varying degrees, resulting in huge capacity loss. Without any control, side reactions can result in huge capacity loss and high safety risks under constant charging of high C-rate and low temperature. Specific quantitative analysis will be discussed in the next section. Therefore, for parallel battery packs, a reasonable active charging control strategy under various ambient temperatures is very necessary.
Battery pack performance with MLPOC

Figure 10 shows the simulation results of the battery pack model with MLPOC and some without MLPOC under 2C and 0°C in one cycle. At the beginning, the discharging process with MLPOC is identical with that of 2C without MLPOC. Once the charging process starts, the control strategy takes effect. As shown in Figure 10A, because of the use of MLPOC, the voltage does not rise rapidly at the start of charging as that without MLPOC. Figure 10B shows the change of Li plating overpotential during one cycle, especially comparing the Li plating overpotential of cell B1 at the start of charging with and without MLPOC. In the local magnified image of Figure 10B, the solid line represents the Li plating overpotential with MLPOC, and the dotted line represents that without MLPOC. The sudden reversal of current may lead to a huge drop of Li plating overpotentials, in which the lowest overpotential immediately causes the response of the PI controller. This results in a corresponding interference signal, so that the input total current is reduced, which makes the minimum Li plating overpotential maintain at the reference value of 0 V. In
addition, the input total currents of the battery pack with and without MLPOC during the whole process are compared in Figure 10D. It should be noted that at the beginning of charging, the electrochemical reaction inside the cells was violent because there was no rest after discharging. It caused the Li plating overpotential curve in Figure 10B to drop sharply and then rise. Therefore, there would be a little Li plating at that time. However, it would not have a serious effect on the cells, because Li plating cannot be completely avoided (Chen et al., 2021) and can be restored (Hein et al., 2020). The variation of current distribution is shown in Figure 10C. Obviously, during charging, the current of cell B1 is always the largest among all the branch currents, so cell B1 becomes the cell with the lowest Li plating overpotential. Figure 10E shows the temperature change. As the charging current decreases, the heat generation rate decreases, and the cells are gradually difficult to maintain a high temperature. Thus, the temperatures of all the cells show a trend of decline in the late charging phase. If thermal management is added to the model to make the ambient temperature of the cells rise, the model can be further improved to increase the superiority of the control strategy. This is also the direction of further research. The capacity losses caused by side reactions with and without MLPOC are shown in Figure 10F. Without MLPOC, the branch currents of cells B1 and B2 are higher, resulting in a more severe capacity loss. At the same time, the inconsistency of current distribution leads to highly inconsistent degradation among the six cells. With MLPOC, the capacity loss and the inconsistency are significantly smaller. In addition, due to the maximum current, cell B1 always has the greatest capacity loss.

As a comparison, the simulation results under 1.5C and 0°C are shown in Figure S3. It should be noted that 1.5C is close to the maximum initial charging current of a cell without Li plating, which is obtained in Chapter 3. Therefore, the capacity loss in the charging process under 1.5C is relatively mild compared with that under 2C. Nevertheless, MLPOC can eliminate the risk of Li plating successfully, which keeps the minimum Li plating overpotential at 0 V.

After the simulation, some indicators during the charging process are counted. The statistical results of 2C and 1.5C are shown in Tables 1 and S2, respectively. Table 1 shows the quantitative results of charging process indicators with and without MLPOC under 2C and 0°C. It should be noted that the CC-CV protocol was not used in this study, mainly because the CC-CV protocol would cause the current to drop when the voltage of cell B1 reached the cut-off voltage of 4.2 V, which would lead to confusion and make it difficult to distinguish the contributions of MLPOC and the CV phase. Therefore, the results of MLPOC are only compared with those of the CC phase. Under 0°C and without MLPOC, the simulation results of charging capacity at CC stage show a downward trend with the increase of C-rate. However, lowering the charging current inevitably increases the cost of charging time, and there is no guarantee that Li plating will not occur. In contrast, MLPOC can increase charging capacity while ensuring minimal Li plating. For charging time, the charging capacity of the parallel battery pack is 20.50 Ah in 1964 s, which is equivalent to charging the battery pack at a constant current of 37.58 A (i.e., 1.25C). In addition, the effect is significantly better than the fast charging of CC-CV of 1C. In fact, compared with Tables 1 and S2, the final charging indicators of 2C and 1.5C are similar under 0°C with MLPOC, except that the capacity loss under 1.5C is a little better than under 2C. This is because MLPOC controls the total current of charging. Comparing Figures 10D and S3D, the shape of the total current is very similar at the late charging phase. Therefore, the selected initial total current has little influence on MLPOC, whose influence is mainly reflected in the control results at the start of charging. If the initial total current of charging is selected too large, the minimum Li plating overpotential will be too small, resulting in very drastic current changes, which may cause damage to the hardware circuit. Therefore, it is important to choose the initial total current of charging reasonably.

**Conclusions**

This study established a battery model for a single cell by coupling a single particle model with electrolyte, degradation model, and thermal model, which could accurately describe battery performance under various ambient temperatures. On this basis, six cell models were connected in parallel, considering the

| Charge scheme for parallel battery pack | Charge time (s) | Charge capacity (Ah) | Charge capacity rate (–) | Capacity loss (mAh) |
|----------------------------------------|----------------|---------------------|--------------------------|---------------------|
| 2C and 0°C w/o MLPOC                   | 525            | 9.41                | 31.37%                   | 13.44               |
| 2C and 0°C w MLPOC                    | 1964           | 20.50               | 68.33%                   | 8.43                |
contact resistance and wire resistance, and the parallel battery model was established. A parallel battery pack charging strategy based on minimum potential was then adopted based on the provided model. It could achieve minimum Li plating overpotential control under various ambient temperatures to keep the minimum Li plating overpotential at 0 V. The ambient temperature and total current were input, and MLPOC took the minimum Li plating overpotential of all the cells as feedback for the controller, thus adjusting the input total current of the battery pack to avoid Li plating. Here, the PSO algorithm was used to find the maximum initial charging current of a cell under various ambient temperatures. Combined with the actual situation, an appropriate total current value for input was selected. Finally, the charging performances of battery packs with and without MLPOC were simulated at 1.5C and 2C under 0°C ambient temperature, and their results were compared. Comparative results showed that MLPOC could effectively keep the minimum Li plating overpotential at 0 V under various conditions, and reduced the capacity loss caused by Li plating. Although the charging time of MLPOC was relatively long, the total charging capacity of the parallel battery pack was improved. In addition, the charging time of MLPOC was still less than that of the CC-CV fast charging of 1C.

The charging strategy based on MLPOC fits with the battery digital twin framework. Sensors can be added to the batteries, which will realize the impact of physical entity to digital model to achieve digital twin. Meanwhile, it can also provide a new perspective for the application and promotion of V2G, which leaves room for further study.

**Limitations of the study**

This charging strategy was simulated only by a parallel circuit structure. Different circuit models may present different current distributions, which are worth studying in the future. At the same time, considering the interaction of the cells in the battery pack, the model of thermal management can be further added to the battery pack model to study the relationship between thermal management system and charging strategy in the future.

**NOMENCLATURE**

| List of symbols | Description |
|-----------------|-------------|
| \(a_s\) | specific interfacial area (m\(^{-2}\)) |
| \(A_n\) | convective surface area of the cell (m\(^2\)) |
| \(c\) | Li-ion concentration (mol m\(^{-3}\)) |
| \(C_p\) | specific heat capacity (J kg\(^{-1}\) K\(^{-1}\)) |
| \(D\) | diffusion coefficient (m\(^2\) s\(^{-1}\)) |
| \(E_{\text{act}}\) | thermal activation energy corresponding to \(\Psi\) (J) |
| \(F\) | Faraday constant (C mol\(^{-1}\)) |
| \(h\) | convective heat transfer coefficient (J m\(^{-2}\) s\(^{-1}\) K\(^{-1}\)) |
| \(i_{\text{app}}\) | whole cell current externally provided (A) |
| \(i_{\text{lpl}}\) | reaction current density of Li plating (A m\(^{-2}\)) |
| \(i_{\text{s}}\) | reaction current density of SEI growth (A m\(^{-2}\)) |
| \(i_{\text{lpl}}\) | exchange current density of Li plating (A m\(^{-2}\)) |
| \(i_{\text{s}}\) | exchange current density of SEI growth (A m\(^{-2}\)) |
| \(j_n\) | molar ion flux (m\(^{-2}\) mol s\(^{-1}\)) |
| \(k\) | reaction rate constant (m\(^{2.5}\) mol\(^{-0.5}\) s\(^{-1}\)) |
| \(L\) | thickness of electrode (m) |
| \(M_s\) | molecular weight of SEI (kg mol\(^{-1}\)) |
| \(M_{\text{lpl}}\) | molecular weight of Li metal (kg mol\(^{-1}\)) |
| \(r\) | radius (m) |
| \(R\) | ideal gas constant (J mol\(^{-1}\) K\(^{-1}\)) |
| \(R_{\text{film}}\) | SEI film resistance (\(\Omega\)) |
| \(R_{\text{film,0}}\) | initial SEI film resistance (\(\Omega\)) |
| \(R_s\) | radius of electrode particle (m) |
| \(t\) | time (s) |
| \(\tau\) | Li transference number (-) |
| \(T\) | cell temperature (K) |
| \(T_{\text{amb}}\) | ambient temperature (K) |
STAR METHODS

Detailed methods are provided in the online version of this paper and include the following:

- KEY RESOURCES TABLE
- RESOURCE AVAILABILITY
  - Lead contact
  - Materials availability
  - Data and code availability
- METHOD DETAILS
  - Single particle model with electrolyte
  - Degradation model
  - Thermal model

SUPPLEMENTAL INFORMATION

Supplemental information can be found online at https://doi.org/10.1016/j.isci.2022.104243.

ACKNOWLEDGMENTS

This work was financially supported by the Project funded by China Postdoctoral Science Foundation (2021M690740), the Weihai Scientific Research and Innovation Funds (2019KYCXJYB09), and the National Natural Science Foundation of China (No. 52102470).

AUTHOR CONTRIBUTIONS

Conceptualization, H.Y. and X.L.; Writing – Original Draft, H.Y.; Revision, H.Y., L.Y., and J.L.; Validation, H.Y., L.Y., and L.Z.; Supervision, J.L. and X.L.; Funding Acquisition, J.L. and X.L.
Renew. Sustain. Energy Rev. https://doi.org/10.1016/j.rser.2014.01.048. https://www.sciencedirect.com/science/article/pii/S2352152X21006320.

Nikdel, M. (2014). Various battery models for various simulation studies and applications. Renew. Sustain. Energy Rev. 32, 437–485. https://doi.org/10.1016/j.rser.2014.01.048. https://www.sciencedirect.com/science/article/pii/S2352152X21006320.

Ouyang, Q., Wang, Z., Liu, K., Xu, G., and Li, Y. (2019). Optimal charging control for lithium-ion battery packs: a distributed average tracking approach. IEEE Trans. Ind. Inform. 15, 3400–3418. https://doi.org/10.1109/TII.2019.2931640. https://ieeexplore.ieee.org/abstract/document/8889673/.

Peng, J.M., Chen, Z.Q., Li, Y., Hu, S.J., Pan, Q.C., Zheng, F.H., Wang, H.Q., and Li, Q.Y. (2021). Conducting network interface modulated rate performance in LiFePO4/C cathode materials. Rare Met. 1–9. https://doi.org/10.1016/j.isci.2021.103103. https://www.sciencedirect.com/science/article/pii/S2589004221001836.

Reniers, J.M., Mulder, G., and Howey, D.A. (2019). Review and performance comparison of mechanical-chemical degradation models for lithium-ion batteries. J. Electrochem. Soc. 166, A3189. https://doi.org/10.1149/2.0281914jes. https://iopscience.iop.org/article/10.1149/2.0281914jes/meta.

Schindler, M., Durdel, A., Sturm, J., Johcher, P., and Jossen, A. (2020). On the impact of internal cross-linking and connection properties on the current distribution in lithium-ion battery modules. J. Electrochem. Soc. 167, A20542. https://doi.org/10.1149/1.1945-7111/abadbb. https://iopscience.iop.org/article/10.1149/1.1945-7111/abadbb/meta.

Shi, W., Hu, X., Jin, C., Jiang, J., Zhang, Y., and Yip, T. (2016). Effects of imbalanced currents on lithium-ion battery packs. J. Power Sources 243, 544–554. https://doi.org/10.1016/j.jpowsour.2013.05.164. https://www.sciencedirect.com/science/article/pii/S0378775313039622.

Wu, B., Widanage, W.D., Yang, S., and Liu, X. (2020). Battery digital twins: perspectives on the fusion of models, data and artificial intelligence for smart battery management systems. Energy 200, 109816. https://doi.org/10.1016/j.energy.2019.109816. https://www.sciencedirect.com/science/article/pii/S0360544220300161.

Xie, W., Li, X., He, R., Li, Y., Gao, X., Li, X., Peng, Z., Feng, S., Feng, X., and Yang, S. (2020). Challenges and opportunities toward fast-charging of lithium-ion batteries. J. Energy Storage 32, 101837. https://doi.org/10.1016/j.est.2020.101837. https://www.sciencedirect.com/science/article/pii/S2352152X20316741.

Xie, Y., Wang, X., Hu, X., Li, W., Zhang, Y., and Lin, X. (2021). An enhanced electro-thermal model for EV battery packs considering inhomogeneous distribution in parallel branches. IEEE Trans. Power Electron. 37, 1027–1043. https://doi.org/10.1109/TPEL.2021.310229. https://ieeexplore.ieee.org/abstract/document/9588844.

Yang, X., Lin, L., Chen, Q., Xie, Q., Gu, B., Wang, L., and Peng, D.L. (2021). Multifunctional roles of carbon-based hosts for Li-metal anodes: a review. Carbon Energy 3, 303–329. https://doi.org/10.1002/cey2.95. https://onlinelibrary.wiley.com/doi/full/10.1002/cey2.95.

Yang, X.G., Liu, T., Gao, Y., Ge, S., Leng, Y., Wang, D., and Wang, C.Y. (2019). Asymmetric temperature modulation for extreme fast charging of lithium-ion batteries. Joule 3, 3002–3019. https://doi.org/10.1016/j.joule.2019.09.021. https://www.sciencedirect.com/science/article/pii/S2542435119304817.

Yu, H., Li, J., Ji, Y., and Pecht, M. (2022). Life-cycle parameter identification method of an electrochemical model for lithium-ion battery pack. J. Energy Storage 47, 103591. https://doi.org/10.1016/j.est.2021.103591. https://www.sciencedirect.com/science/article/pii/S2352152X2101269X.

Zhang, D., Popov, B.N., and White, R.E. (2000). Modeling lithium intercalation of a single spinel particle under potentiodynamic control. J. Electrochem. Soc. 147, 831. https://doi.org/10.1149/1.1393297. https://iopscience.iop.org/article/10.1149/1.1393297/meta.

Zhang, C., Jiang, J., Gao, Y., Zhang, W., Liu, Q., and Hu, X. (2017). Charging optimization in lithium-ion batteries based on temperature rise and charge time. Appl. Energy 194, 569–577. https://doi.org/10.1016/j.apenergy.2016.10.059. https://www.sciencedirect.com/science/article/pii/S0378779616315033.

Zhao, Y., Zhang, Y., Wang, Y., Cao, D., Sun, X., and Zhu, H. (2021). Versatile zero-to-three-dimensional carbon for electrochemical energy storage. Carbon Energy 3, 895–915. https://doi.org/10.1002/cey2.137. https://onlinelibrary.wiley.com/doi/full/10.1002/cey2.137.

Zhou, C.C., Su, Z., Gao, X.L., Cao, R., Yang, S.C., and Liu, X.H. (2022). Ultra-high-energy lithium-ion batteries enabled by aligned structured thick electrode design. Rare Met. 41, 14–20. https://doi.org/10.1007/s12598-021-01785-2. https://link.springer.com/article/10.1007/s12598-021-01785-2.
**STAR METHODS**

## KEY RESOURCES TABLE

| REAGENT or RESOURCE | SOURCE | IDENTIFIER |
|---------------------|--------|------------|
| Software and algorithms | MATLAB 2019b MathWorks | https://www.mathworks.com/products/matlab.html |
| PID Controller | MathWorks | https://www.mathworks.com/help/simulink/slref/pidcontroller.html |

## RESOURCE AVAILABILITY

### Lead contact

Further information and requests for resources and reagents should be directed to and will be fulfilled by the lead contact, Xinhua Liu (liuxinhua19@buaa.edu.cn).

### Materials availability

This study did not generate new materials.

### Data and code availability

No additional data was used. This paper does not report original code. Any additional information for reanalyzing this work is available from the lead contact upon request.

## METHOD DETAILS

The single cell model consists of SPMe, degradation model and thermal model, explained in detail in this section. It should be noted that the processes in the following equations are related to time, and the time variable $t$ is not written in the processes for convenience.

### Single particle model with electrolyte

The terminal voltage of the battery is calculated by the solid phase potentials $\varphi_s$, as shown in (Equation 1). According to the electrochemical overpotentials $\eta$ and equilibrium potentials $U$, the solid phase potentials of cathode and anode are defined as Equations (2) and (3), which are related to the state of lithiation. Note that due to considering side reactions, the total current density $i$ is the sum of the applied current density $i_{\text{app}}$, SEI growth current density $i_s$, and Li plating current density $i_{\text{lpl}}$, as shown in (Equation 4). At the same time, it should be noted that the resistance of the film on the cathode is ignored due to the little effect.

$$
V = \varphi_s^+ - \varphi_s^- \quad \text{(Equation 1)}
$$

$$
\varphi_s^+ = \eta^+ + \varphi_a^+ + U^+ \quad \text{(Equation 2)}
$$

$$
\varphi_s^- = \eta^- + \varphi_a^- + U^- + \frac{R_{\text{film}}i}{a_i L} \quad \text{(Equation 3)}
$$

$$
i = i_{\text{app}} + i_s + i_{\text{lpl}} \quad \text{(Equation 4)}
$$

The electrochemical overpotentials for anode and cathode follow the Butler-Volmer (BV) equation, which can be approximated as Equations (5) and (6). The equilibrium potentials are related to the state of lithiation of the electrodes. The equilibrium potential of the anode adopts a fitting function, as shown in (Equation 7). The stoichiometry of the anode $x_a$ is defined by the surface and maximum lithium concentration of the solid phase, as shown in (Equation 8). The equilibrium potential and $x_a$ of the cathode were tested by the half-cell experiment, which can be found in our previous study (Liu et al., 2019a).

$$
\eta^- = \frac{2RT}{F} \sinh^{-1}\left( \frac{j_a^-}{2k_a j_a^0} \sqrt{c_e c_{\text{sur}} (c_{\text{limax}} - c_{\text{sur}})} \right) \quad \text{(Equation 5)}
$$
the current, as shown in (Equation 20). Therefore, the distribution of ion current density
is related to the applied current; while at the particle center, the flux of lithium-ion concentration is not
allowed.

\[
\eta^+ = \frac{2RT}{F} \sinh^{-1}\left( \frac{j_i}{2k_i/m_i} \left( c_i^{\text{surf}} - c_i^{\text{surf}} \right) \right)
\]

(Equation 6)

\[
U^- = 0.7222 + 0.1387x_i + 0.029x_i^{0.5} = \frac{0.0172}{x_i^{0.5}} + 0.0019 + 0.2808e^{(0.9 - 15x_i)} - 0.7984e^{(0.4466x_i - 0.4108)}
\]

(Equation 7)

\[x_i = \frac{c_i^{\text{surf}}}{c_i^{\text{surf}}} \]  

(Equation 8)

As mentioned above, the active material for each electrode is assumed to be a particle. The diffusion in the solid phase follows the Fick’s law as (Equation 9), and the boundary conditions for both anode and cathode can be expressed as (Equations 10) and (11). At the particle surface, the flux of lithium-ion concentration is related to the applied current; while at the particle center, the flux of lithium-ion concentration is not allowed.

\[ \frac{\partial c_i^+}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left[ D_{i,\text{eff}} r^2 \frac{\partial c_i^+}{\partial r} \right] \]  

(Equation 9)

\[ \frac{\partial c_i^+}{\partial r} = 0, (r = 0) \]  

(Equation 10)

\[ \frac{\partial c_i^+}{\partial r} = \pm \frac{j_{\text{app}}}{D_{i,\text{eff}}} L_i^+ \quad (r = R_i^+) \]  

(Equation 11)

The diffusion of lithium-ion in the liquid phase follows (Equation 12). The boundary conditions of the entire battery domain can be expressed as (Equations 13, 14, 15, 16, and 17). It should be noted that \( c_{\text{Li}} \) represents the lithium-ion concentration in the liquid phase, and the superscript of \( c_{\text{Li}} \) represents different regions of the battery. The boundary conditions are as follows: (1) at the boundary positions where the two electrode regions contact with the current collectors, there are no liquid lithium-ion concentration gradients in the \( x \) direction; (2) at the junctions of the anode and the separator as well as the cathode and the separator, the liquid lithium-ion concentrations on both sides of the interfaces are equal, and the concentration gradients are also equal considering the property of the pore.

\[ \frac{\epsilon_s}{D_{s,\text{eff}}} \frac{\partial c_{\text{Li}}}{\partial t} = \frac{\partial}{\partial x} \left( D_{s,\text{eff}} \frac{\partial c_{\text{Li}}}{\partial x} + 1 - \frac{t_0^+}{F} \delta \right) ; \quad j \in \{-, \text{sep}, +\} \]  

(Equation 12)

\[ \frac{\partial c_{\text{Li}}}{\partial x} = \frac{\partial c_{\text{Li}}}{\partial x} \]  

(Equation 13)

\[ \frac{c_{\text{Li}} (L -)}{\partial x} = \frac{c_{\text{Li}} (L -)}{\partial x} \]  

(Equation 14)

\[ c_{\text{Li}} (L -) = c_{\text{Li}} (L -) \]  

(Equation 15)

\[ D_{s,\text{eff}} \frac{\partial c_{\text{Li}}}{\partial x} = D_{s,\text{eff}} \frac{\partial c_{\text{Li}}}{\partial x} \]  

(Equation 16)

\[ D_{s,\text{eff}} \frac{\partial c_{\text{Li}}}{\partial x} = D_{s,\text{eff}} \frac{\partial c_{\text{Li}}}{\partial x} \]  

(Equation 17)

Where, \( t_0^+ \) is the Li transference number, \( D_{s,\text{eff}} = D_{s,\text{eff}} (t_0^+)^{1/5} \) is the effective liquid phase diffusion coefficient of lithium-ion, which is given by Bruggeman relation. The ionic current densities \( i_n \) in the regions for anode and cathode are shown in (Equation 18), and its boundary conditions are shown in (Equation 19), where \( j_n \) is molar ion flux. There is no molar ion flux in the diaphragm region, i.e., \( i_{\text{app}} = 0 \).

\[ \frac{\partial j_n}{\partial x} = a_n^+ F j_n^* \]  

(Equation 18)

\[ i_{\text{app}} (0) = i_{\text{app}} (L - + L^+ + L^-) = 0 \]  

(Equation 19)

Based on the above Assumption [A2], it can be further concluded that \( j_n^+ \) is a fixed value in the corresponding electrode region and does not change with the position in the direction of the electrode plate thickness. By combining (Equations 18) and (19), it can be expressed that the molar ion flux is proportional to the current, as shown in (Equation 20). Therefore, the distribution of ion current density \( i_n \) and molar ion flux \( j_n \) in the direction of the electrode plate thickness are shown in Figure 2.

\[ j_n^+ = - \frac{i_{\text{app}}}{F a_n^+} \]  

(Equation 20)
By combining Equations (12), (18) and (20), the liquid phase diffusion equation of lithium-ion can be deduced as shown in Equations 21, 22 and 23, and the boundary conditions are the same as Equations 13, 14, 15, 16, and 17. Here, the SPMe model contains partial differential equations (PDEs) to represent the concentration, which can be solved by finite difference method or finite volume method.

\[
\frac{\partial c_i}{\partial t} = \frac{1}{\varepsilon_i} \left[ \frac{D_{i,eff}}{\varepsilon_i} \frac{\partial c_i}{\partial x} \right] + \frac{1 - \beta_i \eta_c}{\varepsilon_i} F L \Delta \eta
\]  
(Equation 21)

\[
\frac{\partial c_i^{app}}{\partial t} = \frac{1}{\varepsilon_i^{app}} \left[ \frac{D_{i,eff}^{app}}{\varepsilon_i^{app}} \frac{\partial c_i^{app}}{\partial x} \right]
\]  
(Equation 22)

\[
\frac{\partial c_i^{*}}{\partial t} = \frac{1}{\varepsilon_i^{*}} \left[ \frac{D_{i,eff}^{*}}{\varepsilon_i^{*}} \frac{\partial c_i^{*}}{\partial x} \right] - \frac{1 - \beta_i \eta_c}{\varepsilon_i} F L \Delta \eta_{app}
\]  
(Equation 23)

The PDE of the electrolyte potential is shown in (Equation 24), whose boundary conditions are shown in Equations 25, 26, and 27. The PDE describes the process of the liquid phase lithium-ion conduction in the regions of the anode, separator, and cathode.

\[
k_i^{app} \frac{\partial \phi_{app}}{\partial x} = - \delta_i + \frac{2RT}{F} \left( 1 - \frac{\delta_i}{\varepsilon_i} \right) \frac{\partial \ln \rho_{app}}{\partial x}
\]  
(Equation 24)

\[
\phi_{app}^{*}(0) = 0
\]  
(Equation 25)

\[
\phi_{app}^{*}(L^{-}) = \phi_{app}^{*}(L^{+})
\]  
(Equation 26)

\[
\phi_{app}^{*}(L^{-} + L^{+}) = \phi_{app}^{*}(L^{-} + L^{+})
\]  
(Equation 27)

Where, \( \kappa_{app}^{*} = \kappa \cdot (\varepsilon_i^{*})^{1.5} \) is the effective liquid phase conductivity of lithium-ion, which is given by Bruggeman relation. The electrolyte potential difference is obtained by integrating (Equation 24) with respect to \( x \) across the entire cell width:

\[
\phi^{*} - \phi^{*} = \left( \frac{L^{+}}{2k_{eff}} + \frac{L^{+}}{2k_{eff}^{app}} + \frac{L^{+}}{2k_{eff}^{app}} \right) \Delta \eta_{app} - \frac{2RT}{F} \left( 1 - \frac{\delta_i}{\varepsilon_i} \right) \ln \frac{c_i(L^{-} + L^{+} + L^{+})}{c_i(0)}
\]  
(Equation 28)

The liquid phase potential difference can be calculated by substituting the calculated liquid phase lithium-ion concentration. At this point, the required calculated physical quantities are substituted into (Equation 1) to find the corresponding terminal voltage value. It should be noted that the output of terminal voltage is only a nonlinear function of current, and other variables are parameters or current dependent.

A block diagram of SPMe is shown in Figure 3. The model includes: (1) two spherical diffusion PDEs which simulate the electrode dynamics of solid phase concentration distribution; (2) PDEs across three regions which simulate the electrolyte dynamics of liquid phase concentration distribution; (3) a nonlinear output function which maps conditions, such as solid phase concentration, liquid phase concentration, and current boundary value, to voltage. It should be noted that the \( c_i^{*}, c_i^{-}, c_i \) subsystems in Figure 3 are independent of each other.

**Degradation model**

In this model, we assume that the main degradation modes can be attributed to the growth of SEI film and Li plating on the anode surface, which consume recyclable lithium by thickening the passivation layer and forming Li dendrites, respectively. These two side reactions can cause permanent capacity loss externally, or even lead to catastrophic accidents like thermal runaway under some extreme conditions such as fast charging and low temperature charging (Li et al., 2019).

In general, the growth of SEI film and the reaction of Li plating can be described by BV equation with Tafel approximation, as shown in Equations (29) and (31) respectively, where their overpotential can be defined as Equations (30) and (32) respectively. To be clear, \( i_{0,i} \) and \( i_{0,ipl} \) represent the current density of the reactions. Note that the equilibrium potentials of SEI film and Li metal are assumed to be 0.4 V and 0 V, respectively (Yang et al., 2021). When the driving overpotential of Li plating becomes negative, the Li plating reaction will be triggered (Ge et al., 2017).

\[
J_i = - i_{0,i} a_i \exp \left( - \frac{F}{2RT} \eta_i \right)
\]  
(Equation 29)

\[
\eta_i = \phi_i^{-} - \phi_i^{*} - U_i - \frac{J_i}{a_i} R_{lim}
\]  
(Equation 30)
\[ J_{\text{pl}} = -j_{\text{pl}}a_s \exp\left(-\frac{F}{2RT}\eta_{\text{pl}}\right) \]  
(Equation 31)

\[ \eta_{\text{pl}} = \varphi_s - \varphi_e - U_{\text{pl}} - \frac{J}{a_s}R_{\text{lim}} \]  
(Equation 32)

The film thickness growth rate and the resistance can be described as a combination of the two side reactions, as shown in Equations (33) and (34). To be clear, \( M_s \) and \( M_{\text{pl}} \) are the molecular weights of SEI film and Li metal respectively; \( \rho_s \) and \( \rho_{\text{pl}} \) are the densities of the two substances respectively; \( \kappa_s \) is the conductivity of the film.

\[ \frac{\partial \delta_{\text{lim}}}{\partial t} = -\frac{J_sM_s}{a_s\rho_sF} - \frac{J_{\text{pl}}M_{\text{pl}}}{a_s\rho_{\text{pl}}F} \]  
(Equation 33)

\[ R_{\text{lim}} = R_{\text{lim},0} + \frac{\delta_{\text{lim}}}{\kappa_s} \]  
(Equation 34)

**Thermal model**

The heat generated by LiBs in the working process can be divided into two categories: reversible heat and irreversible heat (Reniers et al., 2019). Reversible heat is due to the entropy change of open circuit voltage with temperature change. Irreversible heat is generated by the overpotentials, which includes ohmic heat, enthalpy heat, reaction heat and mixing heat. For convenience, the thermal model is simplified in this paper. Considering the stable electrochemical performance, good transmission characteristics and limited concentration gradient of commercial batteries, the heat generated by entropy change, enthalpy heat and mixing heat can be ignored. The ohmic heat and reaction heat considered are defined as Equations (35) and (36), and the energy balance law is described as (Equation 37), where \( C_p \) is specific heat capacity, \( h \) is convective heat transfer coefficient, \( A_s \) is convective surface area, \( T \) is battery Temperature, and \( T_{\text{amb}} \) is ambient temperature. It should be noticed that the interaction of temperature among cells is not considered in this battery pack model. That is because the temperature change of the simulated cell is small, and the battery pack has fewer cells and simple structure which is the cells in a row.

\[ q_e = j F R_{\text{lim}} \]  
(Equation 35)

\[ q_i = i(\eta^+ - \eta^-) \]  
(Equation 36)

\[ \frac{\partial (\rho C_p T)}{\partial t} = q_e + q_i + hA_s(T - T_{\text{amb}}) \]  
(Equation 37)

The effect of temperature on the electrochemical process can be described by Arrhenius equation, as shown in (Equation 38), where the \( \Psi_{\text{ref}} \) represents the property of a parameter at the reference temperature.

\[ \Psi = \Psi_{\text{ref}} \exp\left[\frac{E_{\text{act}}}{R}\left(\frac{1}{T_{\text{ref}}} - \frac{1}{T}\right)\right] \]  
(Equation 38)