Searching for tetraquark through weak decays of b-baryons

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Abstract

After the experimental observation of charged and neutral $Z_c(3900)$, it is of prime importance to pursue searches for additional production modes of these exotic states. In this work, we investigate the possibility to study the $Z_c(3900)$ through weak decays of b-baryons at the LHCb. Decay amplitudes for various processes have been parametrized in terms of the SU(3) irreducible nonperturbative amplitudes. A number of relations for the partial decay widths of b-baryons could be estimated. The results presented in this paper can be tested experimentally at hadron colliders in the future.

1 Introduction

In 2013, the BESIII Collaboration analyzed the invariant mass spectrum of $\pi^{\pm}J/\psi$ in the process $e^+e^- \rightarrow \pi^{+}\pi^{-}J/\psi$ at $\sqrt{s}=4.26$ GeV [1]. The result suggests there exists an interesting substructure in the $Y(4260) \rightarrow \pi^{+}\pi^{-}J/\psi$ process in the charmonium region, which became renowned as $Z_{c}^{\pm}(3900)$. This is an important finding since a charged hadron decaying into a charmonium state plus a charged meson must contain at least four quarks. Subsequently, this finding was confirmed by Belle and CLEO-c experiments [2,3]. Soon after the neutral partner $Z_{c}^{0}(3900)$ has been also observed [4]. Such new particles changed dramatically our understanding of exotic states which can not be included in the conventional quark-antiquark and three-quark schemes of standard spectroscopy.

The observed exotic state $Z_{c}(3900)$ carries an electric charge and couples to charmonium, this makes it a unique platform for sharp tests of QCD. Further studies on the properties of the exotic hadrons would help to understand the formation of exotic hadron states and the character of the strong force. With no doubt, these discoveries have aroused great enthusiasm in theoretical research. Proposed interpretations for $Z_{c}(3900)$ include were also attempts to describe these newly discovered charмонium-like states as excitations of ordinary $c\bar{c}$ charmonium [5–22]. All these attempts aim at revealing the internal quark-gluon structure and explaining the masses and decay widths of $Z_{c}(3900)$, one can find much pretty encouraging results in these papers and state that the whole picture of exotic multiquark states is clearer than when BESIII Collaboration firstly discovered $Z_{c}(3900)$. However, we should stress that the precise structures of the $Z_{c}(3900)$ and other “XYZ” states remain unknown, there is no consensus as to the underlying dynamics which form these states.

Therefore, to further understand the nature of $Z_{c}(3900)$, it is of prime importance to pursue searches for additional production modes of $Z_{c}(3900)$ instead of electron-positron collision. There are some proposals such as pion-induced production and $pp$ production of $Z_{c}(3900)$ [23–25]. Here, we study the possibility of searching for $Z_{c}(3900)$ from weak decays of b-baryons at the LHCb. In 2015, the LHCb collaboration has reported two exotic structures $P_{c}(4380)$ and $P_{c}(4450)$, firstly observed in the $\Lambda_{b}^{0} \rightarrow P_{c}(\rightarrow J/\psi p)K^{-}$ process [26]. From an experimental viewpoint, the decay $\Lambda_{b}^{0} \rightarrow \Lambda^{0}Z_{c}$ might be a suitable search channel. As shown in Fig. 1, the tree-level amplitudes of the exclusive decays of $\Lambda_{b}^{0} \rightarrow K^{-}P_{c}$ and $\Lambda_{b}^{0} \rightarrow \Lambda^{0}Z_{c}$ are comparable. Nevertheless, we should
stress that constrained by the lack of data and nonperturbative nature, there is no universal factorization approach established to handle production processes of \( Z_c \). This gives a barrier for us to predict their production widths through weak decays of \( b \)-baryons systematically. On the other hand, the approach of flavor SU(3) symmetry allows us to relate decay modes in the bottom-quark decays in spite of the nonperturbative dynamics of QCD [27–54]. The diquark model predicts that the charged and neutral \( Zc \) states or new production modes \( Zc \) and a light baryon. In Sect. 3, an analysis of the angular distributions for the decays \( b \to Zc \) will be presented as well as the results of some other decay modes. A discussion based on the results will be also given in this section. Finally, we summarize in this multiplet will provide crucial evidence for this model.

In this work, we consider nonleptonic decay channels of \( b \)-baryons by utilizing flavor SU(3) analysis. Some testable relations for \( b \)-baryon decays into a \( Zc \) and a light baryon are presented. These relations can be used as tests for pinning down the suitable model for \( Zc \) states. Very recently, the angular distributions for the decays \( \Lambda_b^0 \to \Lambda^0 J/\psi \), where the \( \Lambda^0 \) is \( \Lambda^0 \)-type excited states, have been derived in terms of the helicity amplitude technique [55,56]. We will also use this technique to calculate the partial decay widths of \( \Lambda_b^0 \to \Lambda^0 Z_c^0 \) and \( \Xi_b^- \to \Sigma^- Z_c^0 \) and \( \Xi_b^0 \to \Lambda^0 Z_c^0 \). Having these results at hand, one can get pieces of information on the various related decay channels through flavor SU(3) symmetry. The main motivation of this work is to provide some suggestions which may help experimentalists find new \( Zc \) states or new production modes of already observed \( Zc \) states.

The present paper is arranged as follows. In Sect. 2, we discuss the weak decays of \( b \)-baryons whose final states include \( Zc \) and a light baryon. In Sect. 3, an analysis of \( \Lambda_b^0 \to \Lambda^0 Z_c^0 \) will be presented as well as the results of some other decay modes. A discussion based on the results will be also given in this section. Finally, we summarize in the last section.

2 Production of tetraquark through weak decays of \( b \)-baryon

In this section, we start with collecting the relevant representations for hadron multiplets under the flavor SU(3) group.
where \( q \) can be \( d \) or \( s \). The \( G_F \) and \( V_{ij} \) are Fermi-coupling constant and CKM matrix element, respectively. \( O_i \) is the low-energy effective operator and \( C_i \) is the corresponding Wilson coefficient obtained by integrating out the high energy contributions. We have neglected contributions from penguin diagrams which are significantly suppressed compared to the tree contributions. The operators \( O_1 \) transfer under the flavor \( SU(3) \) as \( 3 \), the corresponding quark level transition \( b \rightarrow c \bar{c}d/s \) can form a \( SU(3) \) triplet with \( (H_3)_{13} = -(H_3)_{12} = V_{cd}^* \) and \( (H_3)_{21} = V_{cs}^* \).

For a b-baryon which belongs to the anti-triplet multiplet decays into an octet tetraquark and a light baryon, the corresponding effective Hamiltonian can be constructed as

\[
H_{\text{eff}} = a_1 (B) i (H_3)_{ij} (Z_c)_{ij}^* (T_b)_{ij} + a_2 (B) i (H_3)_{ik} (Z_c)_{ik}^* (T_b)_{ik} + a_3 (B) i (H_3)_{lj} (Z_c)_{lj}^* (T_b)_{lj}.
\]

(6)

For a b-baryon belongs to the sextet multiplet, the effective Hamiltonian reads

\[
H_{\text{eff}} = b_1 (C) i (H_3)_{ik} (Z_c)_{ik}^* (T_b)_{ik} + b_2 (C) i (H_3)_{lj} (Z_c)_{lj}^* (T_b)_{lj} + b_3 (C) i (H_3)_{ik} (Z_c)_{ik}^* (T_b)_{ik}.
\]

(7)

Where the \( a_i \) and \( b_i \) are \( SU(3) \) irreducible nonperturbative amplitudes. Feynman diagrams for these modes are given in Fig. 2. After expanding the above effective Hamiltonian, we can obtain the individual decay amplitudes which are collected in Tables 1 and 2. Many properties concerning weak decays of b-baryons to a tetraquark and a light baryon can be read off from these results. We present some of the interesting properties in the following.

1. Tables 1 and 2 are arranged according to the decay amplitude’s dependence on CKM matrix elements, \( c \rightarrow s \) transition is proportional to \( |V_{cs}^*| \sim 1 \), while \( c \rightarrow d \) transition has a Cabibbo suppressed CKM matrix element \( |V_{cd}^*| \sim 0.2 \).

2. A number of relations for different decay widths can be readily deduced from Table 1:

\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{-}) = \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Sigma^{0}),
\]
\[
\Gamma(A_{b}^{0} \rightarrow Z_{cK^{0}} n) = \Gamma(A_{b}^{0} \rightarrow Z_{cK^{-}} p),
\]
\[
\Gamma(A_{b}^{0} \rightarrow Z_{cK^{0}} n) = \frac{1}{2} \Gamma(A_{b}^{0} \rightarrow Z_{cK^{-}} p),
\]
\[
\Gamma(Z_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{-}) = \Gamma(Z_{b}^{0} \rightarrow Z_{cK^{-}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{0} \rightarrow Z_{cK^{0}} \Lambda^{0}) = \Gamma(Z_{b}^{0} \rightarrow Z_{cK^{-}} \Lambda^{0}),
\]
\[
\Gamma(A_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{-}) = \Gamma(A_{b}^{0} \rightarrow Z_{cK^{-}} \Sigma^{0}) = \Gamma(A_{b}^{0} \rightarrow Z_{cK^{-}} \Sigma^{+}),
\]
\[
\Gamma(A_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{-}) = 2 \Gamma(A_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Sigma^{-}) = \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{0} \rightarrow Z_{cK} \Lambda^{0}) = \frac{1}{2} \Gamma(Z_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Lambda^{0}) = \frac{1}{2} \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Lambda^{0}) = \frac{1}{2} \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Lambda^{0}) = \frac{1}{2} \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}).
\]

And the relations deduced from Table 2:

\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Lambda^{0}) = \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Lambda^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK} \Lambda^{0}) = 2 \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Lambda^{0}),
\]
\[
\Gamma(Z_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{0}) = 2 \Gamma(Z_{b}^{0} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Sigma^{0}) = 2 \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Sigma^{0}) = 2 \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}),
\]
\[
\Gamma(Z_{b}^{-} \rightarrow Z_{cK^{-}} \Sigma^{0}) = 2 \Gamma(Z_{b}^{-} \rightarrow Z_{cK^{0}} \Sigma^{0}).
\]
3. Some theoretical researches predict that the charged and neutral $Z_c(3900)$ belong to the same octet multiplet of SU(3) group. Based on the different valence quark components, we take $Z_c^\pm(3900)$ as $Z_{c\pi^\pm}$ and $Z_c^\mp(3900)$ as $Z_{c\pi^0}$ in this work. Therefore, once a few branching fractions have been measured or calculated in the future, some of these relations shown above may provide hints for the exploration of new decay modes. The process $\Lambda_b^0 \to \Lambda^0 Z_c^0(3900)$ would be analyzed for instance in the next section.

It is necessary to point out that the above relations between different decay widths are obtained in the flavor SU(3) symmetry limit, where the mass differences between final state hadrons have been ignored. Besides, the hadronization processes whose information contained in different decay constants and form factors would also affect the relations derived in this paper. It is widely believed that the symmetry breaking in bottom-quark decays is pretty small in comparison with charm-quark decays, hence we expect that the relations...
derived in our analysis basically hold and many of them can be precisely examined in the future.

3 Analysis of \( \Lambda_b^0 \to \Lambda^0 Z^0_c(3900) \) by helicity amplitude technique

We carry out an analysis of \( \Lambda_b^0 \to \Lambda^0 Z^0_c(3900) \) in terms of the helicity amplitude technique. As we will see later the helicity amplitudes are particularly convenient for expressing various observable quantities in the \( \Lambda_b^0 \) decays [55–58]. The amplitude \( \mathcal{M}(\Lambda_b^0 \to \Lambda^0 Z^0_c(3900)) \) is induced by the \( b \to s c \bar{c} \) transition whose effective Hamiltonian has been presented in Eq. (4). The factorizable diagram of this process is enhanced by color factor compared with the nonfactorizable one. One may adopt the factorization ansatz to predict its decay width, the amplitude is
The helicity amplitudes for $\Lambda_b^0 \to \Lambda^0 Z_c^0(3900)$ are given as

$$H_{1\Lambda} \left( s_{\Lambda_b^0} = -\frac{1}{2}, s_\Lambda = \frac{1}{2}, s_w = 0 \right) = H_{1\Lambda} \left( s_{\Lambda_b^0} = \frac{1}{2}, s_\Lambda = \frac{1}{2}, s_w = 1 \right).$$

The helicity amplitudes for $\Lambda_b^0 \to \Lambda^0 Z_c^0(3900)$ are then formulated as

$$H_{1\Lambda} \left( s_{\Lambda_b^0} = -\frac{1}{2}, s_\Lambda = \frac{1}{2}, s_w = 0 \right) = H_{1\Lambda} \left( s_{\Lambda_b^0} = \frac{1}{2}, s_\Lambda = \frac{1}{2}, s_w = 1 \right).$$
appears in the final states decay in which the tetraquark branching fractions of b-baryon estimation of Table 4 daughter baryon momentum in the $\Lambda_b$ rest frame.

$$
\Gamma(\Lambda_b^0 \rightarrow \Lambda^0 Z_c^0(3900)) = \sum_{s_{\Lambda_b}, s_{\Lambda}} \frac{|p_{\Lambda_b}|}{8\pi m_{\Lambda_b}} \times \frac{1}{2} |M(\Lambda_b^0 \rightarrow \Lambda^0 Z_c^0(3900))|^2
$$

$$
= \sum_{s_{\Lambda_b}, s_{\Lambda}} \frac{|p_{\Lambda_b}|}{8\pi m^2_{\Lambda_b}} \left| \frac{G_F}{\sqrt{2}} V_{cb} V_{\ell c}^* a_2 f_{Z_c} \right|^2 \times M_{Z_c} \sum_{s_{\Lambda}} \sum_{s_{\Lambda}} H_1(s_{\Lambda_b}, s_{\Lambda}, s_{\Lambda}) \right|^2 .
$$

(17)

Using the form factors in Table 3, we obtain an order-of-magnitude estimation of partial decay width and branching fraction

$$
\Gamma(\Lambda_b^0 \rightarrow \Lambda^0 Z_c^0(3900)) = 8.61 \times 10^{-20} \text{ GeV} ,
$$

$$
\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda^0 Z_c^0(3900)) = 1.93 \times 10^{-7} .
$$

(18)

The estimated branching fraction of $\Lambda_b^0 \rightarrow \Lambda^0 Z_c^0(3900)$ is at the order $10^{-7}$. According to the experimental result from BESIII, $Z_c^0(3900)$ would subsequently decay into $\pi^0 J/\psi$ and most of $\Lambda^0$ decay into $p \pi^-$. Therefore the cascade decay would be $\Lambda_b^0 \rightarrow \Lambda^0 Z_c^0(3900) \rightarrow p J/\psi \pi^- \pi^0$. It is worth noting that our result is consistent with the transition matrix element $\Lambda_b^0 \rightarrow \Lambda^0$ given in [66]. The matrix elements of $\Xi_b^- \rightarrow \Sigma^-$ and $\Xi_b^0 \rightarrow \Lambda^0$ have also been calculated in [66] which could be incorporated into the theoretical formalism shown in this section. Similarly, one obtains the estimation of partial decay widths and branching fractions

The results displayed above is an order of magnitude lower than Eq. (18) mainly due to the ratio of CKM matrix elements $|V_{cs}/V_{ud}|^2$. Notably, at this stage the SU(3) symmetry is helpful for figuring out the promising decay channels toward the discovery of $Z_c$ states through b-baryon decay. According to the SU(3) symmetry induced results in Table 1 and the branching fractions in Eqs. (18) and (19), we collect several channels of b-baryon decay with estimated branching fractions in Table 4. The presented branching fractions are on the order of $10^{-7}$ or less. At present, LHCb could detect the branching fraction down to $10^{-6}$ among $\Lambda_b^0$ decay modes whose final states contain $J/\psi$ or its excited states plus a proton and light mesons [67]. Thus, the decay channels shown in Table 4 can be only observed with a large amount of data in the future, such as the high luminosity LHC.

It should be stressed here that the results listed in Table 4 are preferred to be regarded as rough estimations rather than accurate ones since they are based on the naive factorization ansatz. To rigorously study the dynamics of nonleptonic two-body b-baryon decays whose final states contain a tetraquark, some popular theoretical approaches such as perturbative QCD (pQCD) [68,69], QCD factorization (QCDF) [70] and SCET [71,72] would be necessary. This issue goes surely beyond the scope of this paper.

### 4 Conclusions

In summary, we have studied the weak decays of b-baryon to a tetraquark and a light baryon, decay amplitudes for various transitions have been parametrized in terms of the SU(3)-independent amplitudes. Using these results, we provide a number of relations which can be served as tests for finding out the suitable theoretical explanation for $Z_c$ states. The partial decay widths as well as branching fractions of several decay channels have also been presented in terms of the helicity amplitude technique.

At present, with limited data it is not possible to distinguish the mechanism by which the component quarks

### Table 4 Estimation of branching fractions of b-baryon decay in which the tetraquark appears in the final states

| Channel | Branching fraction |
|---------|-------------------|
| $\Xi_b^- \rightarrow \Sigma^- Z_c^0(3900)$ | $2.01 \times 10^{-8}$ |
| $\Xi_b^0 \rightarrow \Lambda^0 Z_c^0(3900)$ | $2.16 \times 10^{-8}$ |
| $\Xi_b^0 \rightarrow \Lambda^0 Z_{c8}$ | $5.94 \times 10^{-9}$ |
| $A_b^0 \rightarrow \Lambda^0 Z_{c8}(3900)$ | $1.93 \times 10^{-7}$ |
are held together to form $Z_c$ states. Since the discovery of $X(3872)$ [73], over nearly 20 years, we still have no satisfactory landscape about the precise structures of "$XYZ$" states. Progress in clarifying this picture requires measurements of improved precision and searches for additional states. To obtain further insights of the nature of exotic charged and neutral $Z_c$ states, we suggest measurements of their production rates in the weak decays of $b$-baryons by the LHCb experiments in the future. In recent years, LHC has helped us find out doubly heavy baryon and pentaquark states [26, 74, 75], undoubtedly, it will provide a sustained progress in heavy baryon field. Naturally, we wish it would also provide a new milestone in the research of $Z_c$ states which will help resolve the current and longstanding puzzles in the exotic charmomium sector.

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Data Availability Statement

This manuscript has no associated data or the data will not be deposited. [Authors’ comment: This is a theoretical study, all the related data can be found on the website of particle data group: https://pdg.lbl.gov/]

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References

1. M. Ablikim et al., BESIII. Phys. Rev. Lett. 110, 252001 (2013). https://doi.org/10.1103/PhysRevLett.110.252001.
2. Z.Q. Liu et al. [Belle], Phys. Rev. Lett. 110, 252002 (2013). (Erratum: Phys. Rev. Lett. 111, 019901 (2013)). https://doi.org/10.1103/PhysRevLett.110.252002.
3. T. Xiao, S. Dobbs, A. Tomaradze, K.K. Seth, Phys. Lett. B 727, 366–370 (2013). https://doi.org/10.1016/j.physletb.2013.10.041.
4. M. Ablikim et al., BESIII. Phys. Rev. Lett. 115(11), 112003 (2015). https://doi.org/10.1103/PhysRevLett.115.112003.
5. Q. Wang, C. Hanhart, Q. Zhao, Phys. Rev. Lett. 111(13), 132003 (2013). https://doi.org/10.1103/PhysRevLett.111.132003.
6. F.K. Guo, C. Hidalgo-Duque, J. Nieves, M.P. Valderrama, Phys. Rev. D 88, 054007 (2013). https://doi.org/10.1103/PhysRevD.88.054007.
7. G. Li, Eur. Phys. J. C 73(11), 2621 (2013). https://doi.org/10.1140/epjc/s10052-013-2621-5.
8. J.R. Zhang, Phys. Rev. D 87(11), 116004 (2013). https://doi.org/10.1103/PhysRevD.87.116004.
9. J.M. Dias, F.S. Navarra, M. Nielsen, C.M. Zanetti, Phys. Rev. D 88(1), 016004 (2013). https://doi.org/10.1103/PhysRevD.88.016004.
10. E. Braaten, Phys. Rev. Lett. 111, 162003 (2013). https://doi.org/10.1103/PhysRevLett.111.162003.
11. E. Wilbring, H.W. Hammer, U.G. Meiβner, Phys. Lett. B 726, 326–329 (2013). https://doi.org/10.1016/j.physletb.2013.08.059.
12. D.Y. Chen, X. Liu, T. Matsuki, Phys. Rev. D 88(3), 036008 (2013). https://doi.org/10.1103/PhysRevD.88.036008.
13. Y.R. Liu, Phys. Rev. D 88, 074008 (2013). https://doi.org/10.1103/PhysRevD.88.074008.
14. Q. Wang, C. Hanhart, Q. Zhao, Phys. Lett. B 725(1–3), 106–110 (2013). https://doi.org/10.1016/j.physletb.2013.06.049.
15. A. Ali, C. Hambrock, W. Wang, Phys. Rev. D 85, 054011 (2012). https://doi.org/10.1103/PhysRevD.85.054011.
16. X.H. Liu, G. Li, Phys. Rev. D 88, 014013 (2013). https://doi.org/10.1103/PhysRevD.88.014013.
17. D.Y. Chen, X. Liu, T. Matsuki, Phys. Rev. Lett. 110(23), 232001 (2013). https://doi.org/10.1103/PhysRevLett.110.232001.
18. F. Aceti, M. Bayar, A. Martinez Torres, K.P. Khemchandani, J.M. Dias, F.S. Navarra, M. Nielsen, Phys. Rev. D 90(1), 016003 (2014). https://doi.org/10.1103/PhysRevD.90.016003.
19. Z.G. Wang, T. Huang, Phys. Rev. D 89(5), 054019 (2014). https://doi.org/10.1103/PhysRevD.89.054019.
20. D.Y. Chen, Y.B. Dong, Phys. Rev. D 93(1), 014003 (2016). https://doi.org/10.1103/PhysRevD.93.014003.
21. C.F. Qiao, L. Tang, Eur. Phys. J. C 74(10), 3122 (2014). https://doi.org/10.1140/epjc/s10052-014-3122-x.
22. N. Brambilla, S. Eidelman, B.K. Hilselt, R. Vogt, G.T. Bodwin, E. Eichten, A.D. Frawley, A.B. Meyer, R.E. Mitchell, V. Papadimitriou et al., Eur. Phys. J. C 71, 1534 (2011). https://doi.org/10.1140/epjc/s10052-010-1534-9.
23. Y. Huang, J. He, X. Liu, H.F. Zhang, J.J. Xie, X.R. Chen, Phys. Rev. D 93(3), 034022 (2016). https://doi.org/10.1103/PhysRevD.93.034022.
24. Z. Zhang, L. Zheng, G. Chen, H.G. Xu, D.M. Zhou, Y.L. Yan, B.H. Sa, Eur. Phys. J. C 81(3), 198 (2021). https://doi.org/10.1140/epjc/s10052-021-09893-3.
25. V.M. Abazov et al., [D0], Phys. Rev. D 98(5), 052010 (2018). https://doi.org/10.1103/PhysRevD.98.052010.
26. R. Aaij et al., LHCb. Phys. Rev. Lett. 115, 072001 (2015). https://doi.org/10.1103/PhysRevLett.115.072001.
