Optimal spike-based communication in excitable networks with strong-sparse and weak-dense links

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The connectivity of complex networks and functional implications has been attracting much interest in many physical, biological and social systems. However, the significance of the weight distributions of network links remains largely unknown except for uniformly- or Gaussian-weighted links. Here, we show analytically and numerically, that recurrent neural networks can robustly generate internal noise optimal for spike transmission between neurons with the help of a long-tailed distribution in the weights of recurrent connections. The structure of spontaneous activity in such networks involves weak-dense connections that redistribute excitatory activity over the network as noise sources to optimally enhance the responses of individual neurons to input at sparse-strong connections, thus opening multiple signal transmission pathways. Electrophysiological experiments confirm the importance of a highly broad connectivity spectrum supported by the model. Our results identify a simple network mechanism for internal noise generation by highly inhomogeneous connection strengths supporting both stability and optimal communication.

The dynamics of a complex network depend crucially on the particular connection architecture of the network1–5. In the absence of sensory stimulation, cortical networks are far from silent, but generate rich and ubiquitous forms of electrical activity that represent noisy internal brain states. Such states typically display low-frequency (<10 Hz, typically 1–2 Hz) irregular neuronal firing6–9, interact bidirectionally with sensory experience10–15, and, moreover, involve a rich repertoire of complex sequential activity patterns16,17. There has been much recent interest in the genesis18–24 and function10–13 of spontaneous activity or noise in the brain, since noise may be the basic mechanism underlying our percept and decision process, which are essentially probabilistic14,15. While the role of network connectivity in complex neural dynamics has been studied extensively18–24, weighted networks have been investigated only recently29–32 and the dynamical and functional implications of the distribution of link weights remain largely unknown in excitable systems.

Recent experiments revealed that the amplitude of excitatory synaptic potentials (EPSPs) between cortical pyramidal neurons obeys a long-tailed, typically lognormal, distribution33,34. Such a distribution creates a synaptic spectrum spanning from vast numbers of weak synapses (typically, the amplitude of EPSP < 1 mV) to a small fraction of extremely strong synapses, for which EPSP amplitude can be several millivolts. Here, we numerically and analytically study the significance of these strong-sparse and weak-dense (SSWD) connections for the dynamics of recurrent networks, in which the weights of recurrent excitatory synaptic inputs to each neuron obey a long-tailed distribution. We asked whether reverberating synaptic input generated by such a distribution is sufficient for the genesis of stable spontaneous activity, and whether this internal noise provides an optimal solution for efficient information processing.

**Results**

The dynamics of each neuron are described by a leaky integrate-and-fire model:

$$\frac{dv}{dt} = -\frac{1}{\tau_m} (v - V_L) - g_E (v - V_E) - g_I (v - V_I),$$

where $v$ is the membrane potential. The membrane time constant $\tau_m$ is 20 [ms] for excitatory neurons and 10 [ms] for inhibitory neurons, and the reversal potentials of leak, excitatory and inhibitory postsynaptic currents are...
Figure 1 | Maximizing the fidelity of spike transmission with long-tailed sparse connectivity. (a) Each excitatory neuron has a lognormal amplitude distribution of EPSPs. The resultant mean and variance of the model are 0.89 [mV] and 1.17 [mV^2], respectively, whereas those shown in a previous experiment [1] were 0.77 [mV] and 0.97 [mV^2]. Inset is a normal plot of the same distribution. (b) Schematic illustration of the neuron model with strong-sparse and weak-dense synaptic inputs. Colors (red, green and blue) indicate inputs to the top three strongest weights. (c) C.C.s between the output spike train and input spike trains at the 1st (red), 2nd (green) and 3rd (blue) strongest synapses on a neuron are plotted against the mean membrane potential and the corresponding input firing rate at each synapse. The dashed line and shaded area show the mean and SD of the membrane potential and the corresponding input firing rate at each synapse. (d) Similar C.C.s obtained by dynamic clamp recordings from a cortical neuron. The color code and vertical bars are the same as in C. (e) The trial-averaged C.C.s for the strongest synapses on n = 14 neurons.

\[
V_L = -70 \text{ [mV]}, \quad V_E = 0 \text{ [mV]}, \quad V_I = -80 \text{ [mV]}, \quad \text{respectively.}
\]

The excitatory and inhibitory synaptic conductances \(g_E\) and \(g_I\) [ms^{-1}] normalized by the membrane capacitance obey

\[
\frac{dg_X}{dt} = -\frac{g_X}{\tau_X} + \sum_j G_{X,j} \sum_s \delta(t - s_j - t_s), \quad X = E, I
\]  

where \(\delta(t)\) is the delta function, \(G_{j}\), \(s_{j}\) are the weight, delay and spike timing of synaptic input from the \(j\)-th neuron, respectively. The decay constant \(\tau_X\) is 2 [ms] and synaptic delays are chosen randomly between \(d_0 - 1\) to \(d_0 + 1\) [ms], where \(d_0 = 2\) for excitatory-to-excitatory connections and \(d_0 = 1\) for other connection types. The values are determined from the stability of spontaneous activity (Methods). Spike threshold is \(V_{\text{thr}} = -50 \text{ [mV]}\) and \(v\) is reset to \(V_e = -60 \text{ mV}\) after spiking. The refractory period is 1 [ms].

The values of \(G_{i}\) for excitatory-to-excitatory connections are distributed such that the amplitude of EPSPs \(x\) measured from the resting potential obey a lognormal distribution

\[
p(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x - \mu)^2}{2\sigma^2}}
\]

on each neuron (Fig. 1a), where the values \(\sigma = 1.0\) and \(\mu - \sigma^2 = \log(0.2)\) well replicate the experimentally observed long-tailed distributions of EPSP amplitudes. We declined any unrealistic value of \(G_i\) that gives an amplitude larger than 20 [mV] by drawing a new value from the distribution. The resultant amplitude of strongest EPSP was about 10 [mV] on each neuron. For simplicity, excitatory-to-inhibitory, inhibitory-to-excitatory and inhibitory-to-inhibitory synapses have uniform values of \(G_i = 0.018, 0.002\) and 0.0025, respectively. Excitatory-to-excitatory synaptic transmissions fail at an EPSP amplitude-dependent rate of \(p_E = a/\exp(a + \text{EPSP})\), where \(a = 0.1 \text{ [mV]}^{1/4}\).

We first demonstrate numerically that the long-tailed distribution of EPSP amplitudes achieves aperiodic stochastic resonance for spike sequence on a single neuron receiving random synaptic inputs (Fig. 1b). Stochastic resonance refers to a phenomenon wherein a specific level of noise enhances the response of a nonlinear system to a weak periodic or aperiodic stimulus, and has been observed in many physical and biological systems. We vary the average membrane potential of the neuron by changing the rate of presynaptic spikes at a portion of the weakest excitatory synapses (EPSP amplitudes < 3 mV). Interestingly, the cross-correlation coefficients (C.C.) between output spikes and inputs to the strongest synapses are maximized at a subthreshold membrane potential value about 10 [mV] above the resting potential and 10 [mV] below firing threshold (Fig. 1c). At more hyperpolarized levels of the average membrane potential, even an extremely strong EPSP (~10 mV) cannot evoke a postsynaptic spike, and the fidelity of spike transmission is reduced. On the contrary at more depolarized average membrane potentials, the neuron can fire without strong inputs, also degrading the fidelity.

We can express the C.C.s in terms of the conditional probability of spiking by strong-sparse input, which we can analytically obtain from the stochastic differential equations for weak-dense synapses (Methods). The analytic results well explain the optimal neuronal response obtained numerically (Fig. 1c). The phenomena can be regarded as stochastic resonance for aperiodic spike inputs. We find that the stochastic enhancement of spike transmission is much weaker in a neuron (Fig. 1c, dashed curve) having Gaussian-distributed EPSP amplitude, which give the same mean and variance of synaptic conductances as the lognormal distribution but no tails of strong synapses (Supplementary Methods). The results prove the advantage of long-tailed distributions of EPSP amplitude.

We confirmed the above model’s prediction by performing dynamic clamp recordings from cortical neurons (n = 14). To mimic synaptic bombardment with long-tailed distributed EPSP amplitudes, we injected the synaptic current given in equation (2) by using the same values of excitatory and inhibitory conductances as used in Fig. 1c (Supplementary Methods). The rate of random synaptic inputs was varied in a low-frequency regime. The physiological result also demonstrated the maximization of the fidelity of synaptic transmission (Fig. 1d, e).

Now, we ask whether the above stochastic resonance is achievable by the noise generated internally by SSWD recurrent neural networks. To see this, we conduct numerical simulations of equations (1) and (2) for a network model of 10000 excitatory and 2000 inhibitory neurons that are randomly connected with coupling probabilities of excitatory and inhibitory connections being 0.1 and 0.5, respectively. Since the network has a trivial stable state in which all neurons are in the resting potentials, we briefly apply external
inhibitory neurons in the noisy spontaneous firing state. Activity is spontaneous. (a) Upper, Spike raster of excitatory (red) and inhibitory (blue) neurons in the noisy spontaneous firing state. Lower, The population firing rates of excitatory (red) and inhibitory (blue) neurons can be fitted by lognormal distributions (black lines). Mean firing rates are 1.6 and 14 [Hz] for excitatory and inhibitory neurons respectively. (b) Firing rate distributions of excitatory (red) and inhibitory (blue) neurons can be fitted by lognormal distributions (black lines). Mean firing rates are 1.6 and 14 [Hz] for excitatory and inhibitory neurons respectively. (c) CVs of inter-spike intervals are distributed around unity in excitatory (red) and inhibitory (blue) neurons. (d) Time courses of the membrane potentials of excitatory (red) and inhibitory (blue) neurons exhibit large amplitude fluctuations. (e) Scatter plot of the instantaneous population activities of excitatory and inhibitory neurons. The solid line represents linear regression. (f) Distribution functions of the fluctuating membrane potentials of excitatory (red) and inhibitory (blue) neurons. (g) The mean (solid) and standard deviation (dashed) of membrane potentials (mV) minimum EPSP (mV). The presence of precise spike sequences has been reported in the brain of behaving animals. We note that the same spikes are sensed as noise if they are input to weak synapses.

Figure 2 | Spontaneous noise in the SSWD recurrent network. The network receives neither external input nor background noise, and hence activity is spontaneous. (a) Upper, Spike raster of excitatory (red) and inhibitory (blue) neurons. (b) Firing rate distributions of excitatory (red) and inhibitory (blue) neurons. (c) CVs of inter-spike intervals are distributed around unity in excitatory (red) and inhibitory (blue) neurons. (d) Time courses of the membrane potentials of excitatory (red) and inhibitory (blue) neurons exhibit large amplitude fluctuations. (e) Scatter plot of the instantaneous population activities of excitatory and inhibitory neurons. The solid line represents linear regression. (f) Distribution functions of the fluctuating membrane potentials of excitatory (red) and inhibitory (blue) neurons. (g) The mean (solid) and standard deviation (dashed) of the membrane potential fluctuations of an excitatory neuron when all EPSPs smaller than the minimum value given in the abscissa are eliminated. Here, we remove a portion of excitatory synapses on a neuron from the weakest ones.

Poisson spike trains to all neurons during initial 100 [ms] to trigger a spontaneous firing. In the absence of external input, the model sustains a stable asynchronous firing initiated by a brief external stimulus (Fig. 2a). The spontaneous network activity emerges purely from reverberating synaptic input, is stable in a very low-frequency regime (Fig. 2b) and is highly irregular (Fig. 2c) as experimentally observed. Firing rate distributions are well fitted by lognormal distributions. Each neuron exhibits large membrane potential fluctuations, on top of which spikes are generated occasionally (Fig. 2d), owing to the dynamic balance between excitatory and inhibitory activities (Fig. 2a and 2c). All these properties are consistent with the spontaneous activity observed in cortical neurons. Importantly, the average values of the membrane potentials are around ~60 mV in excitatory neurons (Fig. 2f), at which spike transmission at strong-sparse synapses becomes most reliable (Fig. 1a, shaded area). Inputs to weak-dense synapses maintain the average membrane potential of each neuron (Fig. 2g), whereas inputs to strong-sparse synapses govern sparse spiking. Therefore, weak-dense and strong-sparse synapses have different roles in stochastic neural dynamics, although they distribute continuously.

Long-tailed distributions of coupling strengths offer a much wider region of the parameter space to stable spontaneous activity than Gaussian-distributed coupling strengths (Supplementary Fig. 1). Furthermore, a linear stability analysis reveals the homeostasis of the ongoing state of the SSWD network (Methods).

What is the underlying mechanism and functional implications of the spontaneous noise generation? Strong-sparse synapses form multiple synaptic pathways in the recurrent neural network (Fig. 3a). Owing to the stochastic resonance effect at these synapses, spike sequences are routed reliably along these pathways (Fig. 3b: Supplementary Methods) that may branch and converge (Fig. 3c). Since strong synapses are rare, spike propagation along a pathway is essentially unidirectional, as indicated by the cross-correlograms for presynaptic and postsynaptic neuron pairs (Fig. 3d). If, therefore, external stimuli elicit spikes from the initial neurons of some strong pathways, the spikes can stably travel along these pathways without much interference (Fig. 3e). The number of spikes received at the end of a pathway is proportional to that of spikes evoked at the start, although fluctuations in the spike number increase with the distance of travel (Fig. 3f). These results imply that spikes can carry rate information along the multiple synaptic pathways embedded by strong-sparse synapses. The presence of precise spike sequences has been reported in the brain of behaving animals. We note that the same spikes are sensed as noise if they are input to weak synapses.

Discussion
In this study, we have explored a coordinating principle in neural circuit function based on a long-tailed distribution of connection weights in a model neural network. The network properties conferred by the long-tailed EPSP distribution account for a role of noise in information routing and present a novel hypothesis for neural network information processing. Namely, we have demonstrated that a single neuron shows spike-based aperiodic stochastic resonance; the cross-correlation coefficient between output spikes of a single neuron and inputs to the strongest synapses are maximized when the neuron receives a certain amount of background noise. Stochastic resonance has been studied in neuronal systems in various contexts. The presence of sensory noise improved behavioral performance in humans and other animals. Synaptic bombardment enhanced the responsiveness of neurons to periodic sub-threshold stimuli. Asynchronous neurotransmitter release can give a noise source for stochastic resonance in local circuits of model neurons with short-term synaptic plasticity. A surprising result here is that the networks may internally generate optimal noise without external noise sources for the spike-based stochastic resonance on sparse-strong connections. Weak-dense connections redistribute excitation activity routed reliably on strong connections over the network as optimal noise sources to sustain spontaneous firing of recurrent networks.

Internal noise or asynchronous irregular firing may provide the neural substrate for probabilistic computations by the brain, and how such activity emerges in cortical circuits has been a fundamental problem in cortical neurobiology. Such neuronal firing has been replicated by sparsely connected networks of binary or spiking neurons, and the importance of excitation-inhibition balance has been repeatedly emphasized. However, the mechanism to generate extremely low-rate spontaneous asynchronous firing (<10 Hz) remained unclear, and our model gives a possible solution...
to this. A large-scale model of mammalian thalamocortical systems consisting of a million neurons with realistic electrophysiological and morphological properties generated asynchronous irregular states, implying that interactions between dynamical and anatomical processes significantly contribute to internal noise generation. By contrast, such states appears in our model from a special synaptic connectivity within local cortical circuits. It is worth while noting that the asynchronous irregular firing of our model does not rely on slow synapses like NMDA receptor-mediated ones. Though slow synapses may improve the stability of such states, our model suggests that such a role of slow synapses is subsidiary.

Long-tailed amplitude distributions of EPSPs can arise from activity-dependent synaptic plasticity. In networks of rate neurons with linear response functions, a Hebbian learning rule induces a lognormal weight distribution when the rule of weight increment depends nonlinearly on the weights. In networks of spiking neurons, spike-timing dependent plasticity results in a long-tailed conductance distribution if the weight dependence for long-term depression depends sublinearly on synaptic weights. Activity-dependent plasticity may switch and reroute different pathways of strong synapses due to sensory or motor experiences of animals while total distribution of EPSP amplitude of the network are kept intact. It is intriguing whether the activity-dependent pathway rerouting may provide a mechanism to represent Bayesian priors of sensory experiences in spontaneous cortical activity and habitual motor coordination.

In summary, we conjoin two fundamental principles in signal processing and complex phenomena observed in cortical neural networks: stochastic resonance and noisy internal brain states. The key of this link is the coexistence of a spectrum of strong-sparse and weak-dense connections that gives a mechanism to represent Bayesian priors of sensory experiences in spontaneous cortical activity and habitual motor coordination.

Methods
Cross-correlation coefficient. We can analytically calculate cross-correlation coefficients by assuming that spike trains are well approximated by a low-rate Poisson process. Then, the cross-correlation coefficient between input and output spike sequences is estimated as

![Figure 3](https://example.com/figure3.png)

**Figure 3** | Spike information routing in the SSWD recurrent network model. (a) A schematic illustration of the SSWD recurrent network. Thick lines stand for strong-sparse connections and thinner lines for weak-dense connections. In reality, the strength of connections is continuous obeying a long-tailed distribution. (b) Examples of spike sequences routed in the network are shown by different colors. Insets magnify the raster plot. (c) Examples of branching (left) and converging (right) pathways formed by the strong synapses. Numbers refer to neurons, and colors to the corresponding pathways in (b). (d) Cross-correlograms are averaged over strongly connected neuron pairs (EPSP > 8mV). (e) Repeated external stimuli (arrows) evoke simultaneous spike propagations in two pathways. (f) Linear relationship between the number of input spikes and that of output ones in a pathway. The dashed line and vertical bars represent linear regression and SD over trials, respectively.
The firing rates of excitatory and inhibitory neuron pools, \( r_E \) and \( r_I \), can vary in time due to interactions between them. Since the mean output rate is equal to the mean rate of input given synaptic delays in a recurrent network, we may represent the time evolution of the mean firing rates of these neuron pools as the following relaxation process with their effective membrane time constants:

\[
\frac{dr_E}{dt} = -\frac{1}{\tau_r} \{ r_E(t) - r_{\text{out},E}(t) \} + \frac{1}{\tau_s} \{ r(E) - r_{\text{in},E}(t) \},
\]

\[
\frac{dr_I}{dt} = -\frac{1}{\tau_r} \{ r_I(t) - r_{\text{out},I}(t) \} + \frac{1}{\tau_s} \{ r_I(t) - r_{\text{in},I}(t) \},
\]

where \( r_{\text{in},E}(t) \) and \( r_{\text{in},I}(t) \) are firing rate of input and output sequences respectively, \( T \) is a short period of time satisfying \( r_{\text{in}},T < 1 \) and \( r_{\text{in}},T < 1 \), and \( \text{Pr}(x_{\text{in}}|x_{\text{out}}) \) is the conditional probability of output spike for given input spike at inhibitory synapses. In numerical simulation, we evaluated \( \text{Pr}(x_{\text{in}}|x_{\text{out}}) \) by detecting a post-synaptic spike within the epoch of EPSP rise from the arrival of an input spike.

**Analytical solution of the cross-correlation coefficient.** We can analytically calculate the firing rate and cross-correlation coefficient of each neuron by dividing excitatory synaptic inputs to the neuron into two parts, one consisting of weak and modestly strong synapses and one consisting of extremely strong synapses. In this approximation, we may treat inputs to the former excitatory synapses and inhibitory synapses by the diffusion approximation\(^{5,7}\), in which Poisson spike inputs on (2) are approximated as the sum of the conditional firing probabilities over inputs to these synapses. Then, by summing these contributions, we obtain the firing rate of the neuron as

\[
\tau_E \frac{dr_E}{dt} + \tau_I \frac{dr_I}{dt} = \sum_{i=1}^{n} (P_i(r_{\text{in}}) - r_{\text{in},i}) + \sum_{i=2}^{n} P_i(r_{\text{in}}) \frac{dr_i}{dt} + \sum_{i=2}^{n} P_i(r_{\text{in}}) \frac{dr_i}{dt}.
\]

Finally, by substituting \( P_i \) of the strongest synapse into \( P(x_{\text{in}}|x_{\text{out}}) \) and using equation (10), we obtain an analytical expression of the correlation coefficient given in equation (4). To derive the analytical curve shown in Fig. 1c, we classified the five strongest synapses into the second group and the remaining ones into the first group.
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