Simulation Analyses of Two On-Ramp Lane Arrangements

Xu Wang · Xiao-Bo Qu · Pan Li

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Abstract
Ramps are vital pieces of infrastructure connecting city traffic networks to freeways. The performance of a ramp is to some extent determined by the on-ramp lane arrangement. In this paper, our primary aim is to evaluate the performance in terms of travel time and vehicle emissions for two on-ramp lane arrangements: added lane and zip merging. We estimate the travel time and CO₂ emissions on the basis of the speed, and acceleration of vehicles in accordance with the improved comprehensive modal emission model (CMEM), and then analyse the impacts of traffic volume and heavy goods vehicles (HGVs) on travel time and emissions. The impacts of main road traffic flow on travel time and emissions for the two on-ramp lane arrangements are analysed under scenarios with traffic volumes of 800, 1 000, 1 200, 1 400, 1 600 and 1 800 vehs/h/lane. Meanwhile, the relationships between travel time, emissions and various proportions of HGVs (2%, 4%, 6%, 8% and 10%) for both on-ramp lane arrangements are evaluated as well. We eventually present emission contour charts for the two on-ramp lane arrangements based on the possible combinations of traffic volumes and HGV percentages.

Keywords On-ramp lane arrangement · comprehensive modal emission model (CMEM) · Micro-traffic simulation model · Travel time · CO₂ emissions · Traffic volume · heavy goods vehicles (HGVs)

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Pan Li
yongpanli@163.com

Xu Wang
michael.wang@griffithuni.edu.au

Xiao-Bo Qu
drxiaoboqu@gmail.com

1 Griffith School of Engineering, Griffith University, Gold Coast, QLD 4222, Australia
2 Department of Architecture and Civil Engineering, Chalmers University of Technology, SE-412 96 Gothenburg, Sweden
3 School of Urban Rail Transportation, Soochow University, Suzhou 215131, Jiangsu, China
1 Introduction

Nowadays, freeways are serving in an increasingly significant role, carrying vehicles safely and efficiently and sustaining traffic at consistently high speeds, in the urban transport system [1]. However, with the increased utilization of freeways, frequent traffic delays have resulted in a loss to travel time and high emissions of carbon dioxide [2]. Therefore, addressing the loss of travel time and environmental pollution due to traffic delays is of utmost concern by traffic agencies [3]. In this regard, optimizing on-ramp lane arrangements is a solution worth being considered by traffic engineers.

There is a relatively extensive literature focusing on the improvements in freeway operation. Among them, many researchers recommended to reduce travel time in the on-ramp adjacent zones through traffic control and freeway geometry upgrade (e.g. [2, 4–9]). Few researches have discussed the impact of on-ramp lane arrangements on freeway operation. In this paper, we will explore the effect. Additionally, due to the correlation between travel time and emissions, the impact of both on-ramp lane configurations on emissions will be also explored. Emissions estimation has been a concern of researchers for decades (e.g. [10, 11]). The existing emissions prediction models can be divided into macroscopic and microscopic models [12]. In the macroscopic world, the emissions for a certain pollutant and a given type of vehicles are typically considered as a function of average speed [13]. Afterwards, the emissions models have been progressively perfected by adding new emission factors and new vehicle classifications. However, the input of single data (the average speed) restricts the accuracy of emissions estimation. Accordingly, scholars devoted themselves to the exploration of microscopic models. In 1996, Barth et al. assessed an engine emissions based on the engine output power and developed the comprehensive modal emissions model (CMEM). Afterwards, Rakha et al. [14] proposed the Virginia Tech microscopic (VT-Micro) energy and emission model in the form of a regression model linking vehicle energy consumption rate and emission rate to the instantaneous speed and acceleration. However, the VT-Micro was only calibrated by light duty vehicles and trucks, which cannot be widely applied. Therefore, we applied the CMEM to predict emissions for the research freeway section.

This paper investigated the impacts of variability of mainline traffic volumes and mainline heavy goods vehicles (HGVs) on travel time and emissions in the investigated road segments fitted with two types of on-ramp lane arrangements. The research could provide traffic engineers with a guideline, regarding how to select a proper on-ramp lane configuration for those road segments with closely spaced on- and off-ramps, in terms of travel time and emissions. The rest of the paper is organized as follows. Section 2 describes the investigated road segment and data collection process. The CMEM is formulated in Sect. 3. Section 4 demonstrates the validity of simulation models. A comparative analysis is carried out in Sect. 5. Section 6 concludes.

2 Site Description and Data Collection

As can be seen in Fig. 1, one 800 m bottleneck on Australia Pacific Motorway, in the vicinity of Nerang (a suburb of Gold Coast), was selected as the investigated road
segment, as the local council has been seeking a proper solution to address the recurring congestion in peak hours. The traffic data used for emissions calculation are hard to be collected in the real world [15–17]. As a consequence, we applied VISSIM models to generate traffic data assessing travel time and calculating emissions. Before they were formally used, the parameters in VISSIM need to be calibrated and the simulated data need to be validated with the observed data. Towards this end, the videos were recorded from four different time periods. We extracted traffic volumes and HGVs counts from them for the sake of the development of simulation models. Besides, traffic trajectory data were also retrieved to validate the reliability of simulated traffic data. Table 1 simply aggregates the observed traffic data.

### Table 1 The summary of traffic flow at research segment

| Time periods       | Mainline traffic flow (vehs/h) | Mainline HGVs (vehs/h) | On-ramp traffic flow (vehs/h) |
|--------------------|--------------------------------|------------------------|-------------------------------|
| Morning peak       | 5 478                          | 411^a (7.5%)           | 269^b (4.9%)                 |
| (7:00 am–8:00 am)  |                                |                        |                               |
| Transitional off-peak | 3 405                       | 266^a (7.8%)           | 161^b (4.7%)                |
| (12:00 pm–1:00 pm) |                                |                        |                               |
| Afternoon peak     | 4 644                          | 341^a (7.3%)           | 242^b (5.2%)                |
| (4:00 pm–5:00 pm)  |                                |                        |                               |
| Night off-peak     | 2 427                          | 157^a (6.5%)           | 124^b (5.1%)                |
| (7:00 pm–8:00 pm)  |                                |                        |                               |

^aThe proportion of HGVs on freeway main carriageways  
^bThe percentage that on-ramp traffic flow occupies mainline traffic flow
3 Methodology

The CMEM has been widely used for the emissions estimates of numerous classes of vehicles, which make up for the usage limitations in the VT-Micro energy and emission model. It can estimate distance-based fuel consumption rates caused by vehicles’ driven force, engine friction and air-conditioning. Vehicles’ fuel consumption rates are to a great extent dependent upon the instantaneous speeds \((v)\) and accelerations \((a)\). In this research, we simply hypothesize that the instantaneous speed and acceleration for each vehicle is invariable in the 10 m road segment. We collected all vehicles’ instantaneous speeds and accelerations in any 10 m road segment by means of 80 virtual data collection points set up in VISSIM models. By using Eq. 3.1, the fuel consumption \(F(v, a)\) for each vehicle can be calculated in the unit of grams per metre per vehicle. Once the fuel consumption for each vehicle is known, based on the concept of carbon balance [18], the CO\(_2\) emissions for each vehicle are calculated as per Eq. 3.2. The summation of CO\(_2\) emissions for a certain vehicle in the investigated road segment can be estimated according to Eq. 3.3.

\[
F(v, a) = \frac{\varphi}{\lambda} \left( \sum_{i=0}^{3} \alpha_i \cdot v^{i-1} + \beta \cdot a \right), \quad (3.1)
\]

where the coefficients are given by

\[
\alpha_0 = \frac{p_a}{\eta}, \quad \alpha_1 = Zg \frac{G + c_1}{\eta \varepsilon} + c_4 K_0 V \theta \left( r + c_3 v_h \right), \quad \alpha_2 = Zg \frac{c_1}{c_2 \eta \varepsilon} - 2c_3 c_4 K_0 V v_h \theta,
\]

\[
\alpha_3 = \frac{\rho C_d A}{2 \eta \varepsilon} + c_3 c_4 K_0 V \theta \quad \beta = \frac{Z(1 + e_0)}{\eta \varepsilon},
\]

\[
E_{CO_2}(v, a) = \gamma_1 F(v, a) + \frac{\gamma_0}{v}, \quad (3.2)
\]

where

\[
\gamma_0 = -\frac{A_r(CO_2) \cdot c_8}{A_r(C) + \mu}, \quad \gamma_1 = \frac{A_r(CO_2)}{A_r(C) + \mu} \left( \frac{1 - c_7}{A_r(C) + \mu} - \frac{c_5(1 - \varphi^{-1}) + c_6}{A_r(CO)} \right),
\]

\[
\sum E = \int_0^X E_{CO_2}(v, a) dx. \quad (3.3)
\]

In the above three equations, the specific parameter descriptions and values for passenger cars and HGVs can be found in “Appendix”. They are complicated to be gathered in the real world. Therefore, in this research, we referred to and cited the parameter values of previous researches.
4 Simulation Model Calibration and Validation

Prior to utilizing VISSIM, the parameters in the simulation model need to be calibrated. Firstly, the geometric characteristics of the investigated site, including the number of through lanes, lane widths, link lengths, and grade were coded in the simulation model by using Google Earth Pro. Secondly, four parameters affecting simulation precision [CC0, CC1, CC2 and the desired lane change distance (DLCD)] were sorted out. Thirdly, we applied genetic algorithm (GA) to find out the best set of values for these four parameters under four different time periods. Table 2 shows the best fitted parameter sets for each time period.

The collative data shown in Table 1 were imported into VISSIM in order to develop four simulation models. To validate the reliability of the calibrated simulation models, the traffic trajectory curves for 20 consecutive vehicles in each time period were, respectively, extracted from the observed videos and the simulated animation and then are illustrated in Fig. 2(a–d). Four types of error tests were conducted to evaluate the differences between the simulated speeds and the observed speeds (e.g. [19–25]). These four error tests are the root mean square error (RMSE), the root mean square percentage error (RMSPE), the mean percentage error (MPE) and Theil’s inequality coefficient ($U$), mathematically represented by,

\[
\text{RMSE} = \sqrt{\frac{1}{N} \sum_{n=1}^{N} (v_{ns}^n - v_{nf}^n)^2},
\]

\[
\text{RMSPE} = \sqrt{\frac{1}{N} \sum_{n=1}^{N} \left( \frac{v_{ns}^n - v_{nf}^n}{v_{nf}^n} \right)^2},
\]

\[
\text{MPE} = \frac{1}{N} \sum_{n=1}^{N} \left( \frac{v_{ns}^n - v_{nf}^n}{v_{nf}^n} \right),
\]

| Time periods | CC0/m | CC1/s | CC2/m | DLCD/m |
|--------------|-------|-------|-------|--------|
| Morning peak (7:00 am–8:00 am) | 1.3 | 0.7 | 3.5 | 800.0 |
| Transitional off-peak (12:00 pm–1:00 pm) | 2.0 | 1.9 | 5.0 | 200.0 |
| Afternoon peak (4:00 pm–5:00 pm) | 1.8 | 1.0 | 4.1 | 250.0 |
| Night off-peak (7:00 pm–8:00 pm) | 2.0 | 2.1 | 5.0 | 200.0 |
| Default values | 1.5 | 0.9 | 4.0 | 200.0 |
Fig. 2 The differences between the simulated and observed data in different time (a) morning peak time; (b) transitional off-peak time; (c) afternoon peak time; (d) night off-peak time

\[
U = \frac{\sqrt{\frac{1}{N} \sum_{n=1}^{N} (v_n^n - v_f^n)^2}}{\sqrt{\frac{1}{N} \sum_{n=1}^{N} (v_n^n)^2} + \sqrt{\frac{1}{N} \sum_{n=1}^{N} (v_f^n)^2}},
\]  

(4.4)
where $v^n_s$ represents the simulation value (speed) of the $n$th vehicle, $v^n_f$ denotes the field value (speed) of the $n$th vehicle, and $N$ is the number of vehicles observed or simulated. The comparative results based on the four time groups are aggregated in Table 3.
As can be seen in Table 3, the average difference between the simulated speeds and the observed speeds in all time groups is 2.99 m/s based on the RMSE test. For a speed limit of 110 km/h (30.56 m/s), the error of 2.99 m/s is in the acceptable range. All groups have RMSPEs of less than 15%, and the mean across all vehicles is 12.82%. The average MPE is positive (6.41%), which indicates that the simulated speeds are slightly over-estimated by VISSIM compared with real speeds. Furthermore, Theil’s inequality coefficient is close enough to zero. The closer the coefficient is to zero, the smaller is the difference in speeds. Accordingly, we can draw the conclusion that VISSIM is a useful traffic simulation model, which can simulate the real traffic situation reasonably well on the microscopic level and can be used in this study.

### 5 Results

#### 5.1 Travel Time Analysis

##### 5.1.1 Impact of Traffic Flow

The average travel time that all vehicles spent on passing through this research segment fitted with two on-ramp lane arrangements are shown in Fig. 3(a). Apparently, as the freeway traffic flow increases, the travel time for these two on-ramp configurations reveals a growing tendency in the context of a fixed percentage of HGVs. Under any traffic flow scenario, vehicles spend less average travel time on the freeway section with added lane than that with zip merging. With the growth of traffic volume, the travel time increase rate for these two on-ramp configurations both become greater. Meanwhile, the two travel time consumption gaps also become greater.

##### 5.1.2 Impact of HGVs

In addition, the impacts of the proportion of HGVs on freeway mainline on travel time are compared below. The analysis will be carried out for two different cases: 1 600 and 1 800 vehs/h/lane. This is because, when the traffic volume ranges from 1 600 to

---

Table 3 Error tests of speeds

| Time periods              | RMSE (m/s) | RMSPE/% | MPE/% | U/% |
|---------------------------|------------|---------|-------|-----|
| Morning peak (7:00 am–8:00 am) | 2.64       | 11.86   | 5.75  | 0.23|
| Transitional off-peak (12:00 pm–1:00 pm) | 3.28       | 13.73   | 6.67  | 0.26|
| Afternoon peak (4:00 pm–5:00 pm) | 2.68       | 11.51   | 5.51  | 0.24|
| Night off-peak (7:00 pm–8:00 pm) | 3.37       | 14.19   | 7.69  | 0.28|
| Mean                      | 2.99       | 12.82   | 6.41  | 0.25|
2 200 vehs/h/lane, the level of service (LOS) curve that depicts average speed versus traffic flow will exhibit a clear transformation. When the traffic volume is less than 1 600 vehs/h/lane, the average vehicle speed is almost invariable. Moreover, 1 600 and 1 800 vehs/h/lane, respectively, satisfies LOS D and E. Therefore, we can more clearly distinguish the impacts of the proportion of HGVs on travel time for both on-ramps under two LOS conditions.

Through the above analysis, the relationships between travel time and the percentage of HGVs on mainline for both on-ramp lane arrangements under LOS D and E are illustrated in Fig. 3(b, c). Overall, the travel time consumed in the research segment with the two on-ramp configurations both goes up with the increase in proportion of HGVs, and under the same percentage of HGVs, the greater the traffic flow is the longer the average travel time is spent. According to Fig. 3(b) and Fig. 3(c), when the percentage of HGVs on freeway is small enough (2%) or great enough (10%), the difference in average travel time can be ignored. Comparatively, when the proportion of HGVs ranges from 4% to 8%, the performance of added lane is superior to that of zip merging. This reflects the following three mechanisms. Firstly, when the number of HGVs on the freeway is small, those small cars can freely change lane and are not subject to the impact of vehicle interaction, particularly HGVs. Secondly, when the number of HGVs is in the normal range, the auxiliary lane attached to added lane can contribute to longer acceleration lane and more accommodation for those
merging cars than zip merging. As a consequence, the whole traffic situation is more organized. Thirdly, when the proportion reaches its critical value, a large number of HGVs running along with outward lane may form a series of hindrance to vehicles so that they cannot merge or diverge as usual. Therefore, either on-ramp lane arrangement can be adopted in this case.

5.2 Emissions Analysis

5.2.1 Impact of Traffic Flow

The fuel and CO₂ emissions calculated by CMEM model completely depend upon a vehicle’s acceleration and speeds. However, the acceleration and speed of every vehicle are not constant in the research segment, which increases the difficulty of calculating emissions. To overcome it, we adopt the sectioning method to collect each vehicle’s instantaneous speed and acceleration and calculate every vehicle’s CO₂ emissions in the corresponding sections using the CMEM model. Finally, all the emissions can be accumulated together. Figure 4(a) depicts the relationship between CO₂ emissions for both on-ramp lane arrangements and the mainline traffic flow when the percentage of HGVs on freeway is 7.3%.

As can be seen in Fig. 4(a), we can conclude that, with an increase in traffic flow, CO₂ emissions for the two on-ramp lane arrangements present a logarithmic increasing tendency. In any case, vehicles travelling through the freeway section with zip merging
emit more greenhouse gases than those do under the other on-ramp lane arrangement. However, with the growth in traffic volume, the difference in CO\textsubscript{2} emissions between the two arrangements becomes greater and the increase rates of emissions for both lane arrangements gradually diminish, which implies that vehicles in the zip merging situation undertake a higher frequency of changes in speed and acceleration.

5.2.2 Impact of HGVs

Overall, greenhouse gas emissions in the research segment under both on-ramp lane arrangements go up with an increase in the percentage of HGVs under any traffic flow, and under the same percentage of HGVs, the greater the traffic flow is the more greenhouse gases vehicles emit. According to Fig. 4(b), the performance in terms of CO\textsubscript{2} emissions of the added lane is superior to that of zip merging under any proportion of HGVs. In addition, the gap between CO\textsubscript{2} emissions for both lane arrangements is gradually magnified. Figure 4(c) shows the same variation tendency as Fig. 4(b).

To sum up, when the proportion of HGVs on freeways and the mainline traffic flow are small enough, the two on-ramp lane arrangements fail to show a significant difference in emissions. By taking the initial construction costs into account, zip merging should be chosen here. However, with the increase in the proportion of HGVs on freeways and the mainline traffic flow, the added lane has a greater ability to resist the rise of emissions.

5.3 CO\textsubscript{2} Emissions Contour Chart

The impact analyses of two relevant factors, traffic volume and percentage of HGVs, on CO\textsubscript{2} emissions are carried out. Towards this end, the following impact analysis procedure is followed. First, the ranges of traffic volume ($T_i$) and the percentage of HGVs ($H_j$) are determined and discretized. The traffic volume ranges from 800 to 1800 vehs/h/lane in accordance with real-life observations, and the step is taken to be 200 vehs/h/lane based on previous research [26, 27]. The proportion of HGVs is assumed to range from 2% to 10% and a 2% step is adopted. Therefore, the typical traffic volumes and percentages of HGVs are, respectively, taken to be 800, 1 000, 1 200, 1 400, 1 600 and 1 800 vehs/h/lane, and 2%, 4%, 6%, 8% and 10%. Then, all possible combinations of the two contributing factors (percentage of HGVs and traffic volume) are applied to calculate CO\textsubscript{2} emissions for the two on-ramp lane arrangements. Figure 5 shows the two-factor-based impact analysis procedure.

Further, the CO\textsubscript{2} emissions contour charts for the two on-ramp lane arrangements can be drawn to show the changing pattern of CO\textsubscript{2} emissions. To do so, all 30 possible combinations of the two factors are taken into account. All points that emit the same quantity of greenhouse gases are plotted and connected using a smooth line. These charts are drawn in Fig. 6(a) and Fig. 6(b) for an added lane and zip merging respectively.

As shown in Fig. 6(a) and Fig. 6(b), the CO\textsubscript{2} emissions will grow as the traffic volume and percentage of HGVs increase. These two CO\textsubscript{2} emissions contour charts could help traffic engineers to select the most suitable combination of the percentage of HGVs and the traffic volume for any given CO\textsubscript{2} emissions target.
Determine ranges of Parameter 1 \((T_1, T_M)\) and Parameter 2 \((H_1, H_N)\)

Discretise the ranges
Parameter 1: \((T_1, T_2, T_3, \ldots T_i, \ldots T_M)\) and
Parameter 2: \((H_1, H_2, H_3, \ldots H_j, \ldots H_N)\)

\[i=1, j=1\]

Retrieve every vehicle’s instantaneous speed and acceleration using VISSIM for combination \((T_i, H_j)\)

Calculate CO\(\text{2}\) emissions using CMEM model for combination \((T_i, H_j)\)

\[j<N\]

\[j=j+1\]

\[i=i+1\]

\[i<M\]

\[N\]

Generate CO\(\text{2}\) emissions contour chart

End

Fig. 5 Two-factor-based impact analysis procedure
6 Conclusion

In this paper, we compared the performances of two on-ramp lane arrangements (zip merging and added lane) at the research segment in terms of travel time and CO$_2$ emissions, in order to assist traffic engineers in choosing the appropriate on-ramp arrangement based on a given CO$_2$ emissions target. To this end, we first recorded the real traffic trajectory at the selected site and utilized them to validate reliability of VISSIM-based simulated data. Second, the CMEM, depending upon two variables, instantaneous speed and acceleration, was applied to calculate CO$_2$ emissions. Third, we evaluated travel time and CO$_2$ emissions for two on-ramp lane arrangements under scenarios with traffic volumes varying from 800 to 1 800 vehs/h/lane in steps of 200, for an observed percentage of HGVs of 7.3%. In all cases, the performance of the added lane was superior to that of the zip merging lane. Meanwhile, the average travel time and CO$_2$ emissions for scenarios with HGV percentages of 2%, 4%, 6%, 8% and 10%, respectively, and for traffic volumes of 1 600 (LOS D) and 1 800 (LOS E) vehs/h/lane were also compared. In regard to the travel time, for the scenarios with high traffic volumes and within a normal range of HGVs, the added lane can be a better selection; but for the cases with high traffic volumes and low or critical proportion of HGVs, either can be selected. In terms of environmental sustainability, the added lane indeed performed better than the zip merging in this study. Fourth, we provided the concept of emissions contour charts to facilitate transport agencies’ simultaneous analysis of the impact of HGVs and traffic volume.

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## Appendix

### Description of nomenclature used in calculating fuel and CO\textsubscript{2} emission rates

| Name | Description | Unit | Default value for passenger cars | Default value for HGVs | References |
|------|-------------|------|----------------------------------|------------------------|------------|
| $\phi$ | Air–fuel equivalence ratio | _ | 1.00 | 1.13 | Nam [28] |
| $\lambda$ | Lower heating value | J/g | 44 000 | | Nam [28] |
| $P_a$ | Axillary power | W | 1 000 | 1500 | Nam [28] |
| $\eta$ | Engine efficiency | _ | 0.40 | 0.35 | Barth et al. [30] |
| $Z$ | Mass | kg | Depends on the simulated data | | |
| $g$ | Acceleration of gravity | Nm/s\textsuperscript{2} | 9.81 | | Nam [28] |
| $G$ | Grade | _ | Flat = 0 | | |
| $\varepsilon$ | Drivetrain efficiency | _ | 0.85 | | Barth et al. [30] |
| $K_0$ | Constant | J/rev/l | 200 | | Barth et al. [30] |
| $V$ | Engine displacement | L | Depends on the simulated data | | |
| $\theta$ | Constant | _ | 0.8159 | | Nam [28] |
| $\tau$ | Constant | _ | 10 | | Nam [28] |
| $r_\text{c}$ | Constant | _ | 2 | | Nam [28] |
| $v_h$ | Constant | m/s | 35 | | Barth et al. [30] |
| $\rho$ | Air density | kg/m\textsuperscript{3} | 1.247 | | Mannering et al. [29] |
| $C_d$ | Drag coefficient | _ | 0.3 | 0.5 | Mannering et al. [29] |
| $A$ | Frontal area | m\textsuperscript{2} | 2 | 3 | Austroads [2] |
| $e_0$ | Mass factor | _ | 0.1 | | Nam [28] |
| $\mu$ | Constant | _ | 1.85 | | Nam [28] |
| $A_r$(CO\textsubscript{2}) | Constant | _ | 44 | | Nam [28] |
| $A_r$(CO) | Constant | _ | 28 | | Nam [28] |
| $A_r$(C) | Constant | _ | 12 | | |
| $c_1$ | Constant | _ | 0.01 | | Mannering et al. [29] |
| Name | Description | Unit        | Default value for passenger cars | Default value for HGVs | References                  |
|------|-------------|-------------|----------------------------------|------------------------|----------------------------|
| $c_2$ | Constant    | m/s         | 44.73                            |                        | Mannering et al. [29]      |
| $c_3$ | Constant    |             | 0.0065                           |                        | Mannering et al. [29]      |
| $c_4$ | Constant    |             | 1.25                             |                        | Mannering et al. [29]      |
| $c_5$ | Constant    |             | 0.4074                           |                        | Mannering et al. [29]      |
| $c_6$ | Constant    |             | 0.1174                           |                        | Mannering et al. [29]      |
| $c_7$ | Constant    |             | 0.01                             |                        | Mannering et al. [29]      |
| $c_8$ | Constant    | g/s         | 0.0049                           |                        | Mannering et al. [29]      |

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