Electrical Conductivity and Dielectric Properties of Lead-Free Perovskite: 
$\text{Ca}_{0.08}\text{Na}_{0.92}\text{Sn}_{0.08}\text{Nb}_{0.92}\text{O}_3$ Ceramic

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Abstract
The physical properties of the Multiferroic $\text{Ca}_{0.08}\text{Na}_{0.92}\text{Sn}_{0.08}\text{Nb}_{0.92}\text{O}_3$ ceramic were investigated by the X-ray Diffraction (XRD), morphology, piezoelectric, dielectric and electrical measurements. The X-ray diffraction patterns at room temperature revealed a single-phase perovskite crystallizing with quadratic $P4mm$ group symmetry. The microstructural analysis shows the homogeneous grainy morphology of the compound with grain sizes varying from 2nm to 5.5nm. The piezoelectric responses were investigated as a function of temperature and frequency. The thermal evolution of the relative dielectric permittivity ($\varepsilon'_r$) exhibited a very important peak with no frequency dependence, which revealed a classical ferroelectric behavior. So as to investigate the electrical transport, a complex impedance spectroscopy is highlighted. With the Debye theory-based analysis and a series of Arrhenius relations, the Nyquist plots are well suitable to an equivalent circuit model. Moreover, the conductivity spectrum exhibits the two phase transitions detected in the dielectric measurements.

Keywords: Ceramic compound; Piezoelectric study; Ferroelectric phase transition; Nyquist plots; Conductivity analysis

Introduction
Multiferroics are materials in which at the same phase there are at least two ferroic features, i.e., ferroelectricity and ferromagnetism or ferroelasticity [1,2]. The most interesting due to their potential applications are perovskite materials of the general formula $\text{ABO}_3$. These materials are becoming increasingly widespread, such as in electronics, microelectronics, radiation detectors and electromechanical transducers [3-5]. In particular, there has been a growing interest in studying the Piezoelectric compounds mostly due to their properties such as the simplicity of crystallographic structure, their flexibility and their ability to change the physical characteristics by ionic substitutions on different structural sites. Especially, materials derived from sodium niobate $\text{NaNbO}_3$ which are the subject of several studies due to their effective dielectric, piezoelectric, pyroelectric, and electro-optical properties [6]. These materials are widely studied as active materials in the acoustic domain, starting from the energy recovery to the actuator through the ink jet print head [7].

It is well-known that a suitable substitution on different atomic sites induces important modifications in the physico-chemical properties of the pure compound [8]. Therefore, it is of great interest to study the effect of the substitution in the $\text{A}$ ($\text{Ca}$) and $\text{B}$ ($\text{Sn}$) sites in $\text{NaNbO}_3$ perovskite. We have synthesized and studied various properties of the ceramic compound, with the general formula $\text{Ca(1-x)Na}_x\text{Sn(1-x)Nb}_x\text{O}_3$ avec $x=0.92$. This compound is crystallized in the quadratic system with $P4mm$ space group, the unit cell parameters are $a=b=3.916\text{Å}, \ c=3.912\text{Å}$ and $V=59.7\text{Å}^3$ [9].

The aim of this research work is to synthesize the $\text{CSNN0.92}$ using a solid-state reaction by sintering at 1250K. Second, the crystal analysis of the sample by X-ray powder diffraction at room temperature is presented. The particle morphology of the powder is observed through EVO LS10 (Zeiss) scanning electron microscope. Finally, the piezoelectric measurements, dielectric and electrical properties of this ceramic compound are studied and discussed.
Experimental and computational method

Powder sample preparation: The polycrystalline sample of $\text{Ca}_{0.08}\text{Na}_{0.92}\text{Sn}_{0.08}\text{Nb}_{0.92}\text{O}_3$ was prepared by the solid-state reaction method under high temperature. The ingredients taken to prepare the solid solution were highly pure (>99.9 %) AR grade precursor materials: $\text{CaCO}_3$, $\text{Nb}_2\text{O}_5$, $\text{Na}_2\text{CO}_3$ and $\text{SnO}_2$, all with required stoichiometric. These precursors are carefully weighed into stochiometric proportions according to the following reaction.

$$0.08\text{CaCO}_3 + 0.46\text{Na}_2\text{CO}_3 + 0.08\text{SnO}_2 + 0.46\text{Nb}_2\text{O}_5 \rightarrow \text{Ca}_{0.08}\text{Na}_{0.92}\text{Sn}_{0.08}\text{Nb}_{0.92}\text{O}_3 + \text{CO}_2$$

Afterwards, these forerunners were grinded for 1 hour by an agate mortar. Then, methanol was added to have a homogeneous mixture that was then calcined in oxygen atmosphere at 1100 °C for 22h. After calciinations, powders have been mixed for 2 hours, a few drops of polyvinyl alcohol (PVA) were added to the powdered sample for perfect binding. A second series of calciinations at 1100 °C for 48 hours was followed by 2 hours of sintering at 1250 °C (with a disk: 8mm in diameter and 1 mm thick) (Figure 1).

Characterizations: In order to extract the crystalline structure, phase purity and lattice parameters in the obtained samples are characterized by an X-ray diffraction (XRD). The measurement is conducted at room temperature through CuKα radiation (=1.5406Å). XRD was analyzed by the Rietveld method using the “Fullprof” software [10] in the 2θ range of 10< 2θ<130 with a step scanning of 0.02.

The morphology of the obtained sample was analyzed by SEM, performed in a MEB PhilipsXL30 system, on the free surface of the material. The measurement was conducted in a high vacuum environment, using an electron beam accelerating with a voltage of 20kV.

Concerning the Piezo electric analysis, the measurements are extracted in a broad range of frequency and temperature using the impedance analyser (HP 4194A), to estimate both susceptance and conductance. The prepared sample was pressed through a hydraulic press into pellets of about 6.5mm diameter and 0.6mm thickness.

![Figure 1: The pellets of the of CSNN0.92 compound.](image)

Dielectric measurements were performed on sintered ceramic disks of 6.5mm diameter and 1mm thickness after the deposition of gold electrodes (600nm min⁻¹ for 10min) on the circular faces by cathodic sputtering. The real and imaginary parts of relative permittivity $\varepsilon'_r$ and $\varepsilon''_r$ were determined under a Helium atmosphere as a function of both temperature (300°-714K) and frequency (100Hz-200KHz) using a Wayne-Kerr 6425 frequency analyzer.

The electrical measurements were performed using a two-electrode configuration on a polycrystalline sample. In fact, this compound was pressed into a pellet of 8mm diameter and 1.1mm thickness under 3t/cm² uniaxial pressure. On both sides of pellets, a thin layer of silver is deposited by thermal evaporation in order to insure an ohmic contact. These measurements were registered in a frequency ranging from 200 Hz to 5MHz with the SOLARTRON SI 1260 automatic bridge monitored by a microcomputer.

Results and Discussion

Crystalline parameters

The XRD pattern was analyzed to confirm the symmetry and to calculate the lattice parameters for CSNN0.92 compound. The values of the lattice and profile parameters were determined using a global profile matching method with the software “Fullprof”. Figure 2 shows a typical X-ray pattern at 300K, including the observed, the calculated profile and as well as the difference profile of the title compound. All the reflexion peaks of the X-ray profile were easily indexed in the quadratic structure belonging to the space group P4mm, and the refined unit cell parameters are $a = b = 3.9164$ Å, $c = 3.9129$ Å and $V = 59.714$ Å³. These results are in agreement with the previously reported results for this compound [7]. The best refinements are listed in Table 1.

Table 1: The best refinements parameters of the CSNN0.92 ceramic compound.

| Formula | $\text{Ca}_{0.08}\text{Na}_{0.92}\text{Sn}_{0.08}\text{Nb}_{0.92}\text{O}_3$ |
|---------|-------------------------------------------------|
| Crystal system/space groups | Quadratic/ P4mm |
| Unit cell parameters (Å) | $a = b = 3.915$ Å, $c = 3.896$ Å |
| Unit cell volume (Å³) | 59.714 |
| $R_\text{wp}$ | 12.7 |
| $R_\text{wp}$ | 18.9 |
| $R_\text{wp}$ | 10.41 |
Figure 2: X-ray diffraction pattern of a CSNN0.92 powder.

Scanning Electron Microscope (SEM)

Figure 3a is the SEM image of the free surface of Ca_{0.08}Na_{0.92}Sn_{0.08}Nb_{0.92}O_{3} sample intered at 1250 °C for 2h. It consists of both large and small agglomerated grains characterized by a spherical shape only. The measurements and statistical evaluation of the grain size distribution were performed on many particles using the Image-J software. The results are displayed in Figure 3b as grain number (counts) versus particle size (nm). As it can be seen from this figure, the particles are reasonably monodisperse, and they are distributed according to a Lorentzian law (red solid line). The average diameter of the grain size is in the range of 2-5.5 nm.

Figure 3a: SEM images for CSNN0.92 ceramic compound.

Figure 3b: Size distribution histogram with corresponding Gaussian fit for CSNN 0.92 ceramic compound.
Piezoelectric measurements

The Piezoelectric measurements were performed on disk shaped ceramics with CSNN$_{0.92}$ at 155K, the conductance (G) and susceptance (B) were measured as a function of frequency around the main radial resonance mode (Figure 4). The material constants were computed using impedance equations and an equivalent circuit recommended by the IEEE Standard on Piezoelectricity [11]. It can be dearly seen that the magnitude of G and B increases with the increasing frequency. We can notice that the maximum of the conductance followed by a subsequent decrease of the susceptance at a particular frequency around 580KHz. This is the resonance frequency.

$$G(f) = \frac{R}{R^2 + P^2} + \frac{1}{R_c} \quad (1)$$

$$B(f) = C_0(\omega) - \frac{P}{R^2 + P^2} \quad (2)$$

where, $\omega = 2\pi f$ and $P = L*\omega - \frac{1}{c\omega}$

The thermal evolution of the maximum susceptance (B(f)) in resonance is given in Figure 5. This figure shows that B(f) decreases gradually with the increasing temperature and disappeared near 265K. This observation indicates the presence of the phase transition, which is an agreement with the transition observed by the dielectric analysis in the simular compounds [6].

**Figure 4**: Variation of the admittance (G) and the susceptance (B) as functions of frequency At $T = 150K$ for CSNN0.92.

These curves have been fitted based on the following relationships:

**Figure 5**: Temperature dependences for the conductance of the CSNN0.92 ceramic compound.
Figure 6: Variation of the susceptance (B) versus the admittance (G) of the CSNN0.92 ceramic compound.

Figure 6 shows the variation of the imaginary part of the admittance complex (B(f)) as a function of real parts (G(f)). It can also be seen in this figure that the variation is represented by a circle, which indicates the presence of a piezoelectric behavior of our developed compound [12]. In order to verify this behavior, we determine the piezoelectric parameters as a function of temperature, which are determined by the fitting of G and B.

The thermal evolution of the mechanical quality factor (Qm) is shows in Figure 7. This variation shows the presence of an extremum in the vicinity of 265K. This temperature verifies the approach of a phase transition, which is in good agreement with the transition obtained by the variation of the conductance as a function of the temperature. Moreover, it is well known that the factor has very high values which reflect the high loss dielectric in this material.

Figure 7: Thermal evolution of the mechanical quality factor of the CSNN0.92 ceramic compound.

The piezoelectric coefficients $d_{31}$ and $K_p$ as a function of temperature are plotted in Figure 8. It is seen that both coefficients drastically decrease as the paraelectric-ferroelectric transition temperature is approached. The decrease of $d_{31}$ is due to the thermal agitations that are responsible for the disorder in this material.

Figure 8: Thermal evolution of the transverse piezoelectric coefficient and the planar coupling factor of the CSNN0.92 ceramic compound.
Dielectric studies

The temperature dependence of the real part of the relative dielectric permittivity ($\varepsilon'_r$) in the frequency range from 1 to 100KHz is shown in Figure 9. Two dielectric anomalies have been observed, the first is detected at $T=485K$ which indicates a phase transition and the second appeared at $T_C=635K$ which originated from a phase transition of a paraelectric to a ferroelectric phase. Moreover, the real part of the dielectric permittivity exhibits a sharp and narrow peak at $T_c$ with no frequency dependence. This feature is typical of classical ferroelectrics [13,14]. Furthermore, the dielectric constant of a normal ferroelectric in the paraelectric region is generally known to follow the Curie-Weiss law described by the following equation [15]:

$$\varepsilon'_r = \frac{C}{T - T_0}$$  \hspace{1cm} (3)

Where $C$ is the Curie constant and $T_0$ is the Curie Weiss temperature.

Figure 10 shows the variation of the inverse dielectric constant $1/\varepsilon'_r$ as a function of temperature at 1kHz. The experimental data was fitted by Eq. (3) using a non-line are curve fitting method. The fitted values parameters are the Curie constant $C$ which was found to be $4.1365 \times 10^4 K$, $T_0=490K$ and $T_C=635245K$. The no coincidence of $T_C$ and $T_0$ implies that the phase transition is clearly of the first order [16]. The dependence of loss tangent (tanδ) of the title compound on temperature at some particular frequencies is represented in Figure 11. It is obvious that at low-temperature tanδ increases slowly, whereas in a high temperature region, it increases sharply. The scattering of a thermally activated charge carriers and/or defects generated during synthesis may be responsible for this sharp rise of tanδ for which the electrical conductivity also increases at high temperatures region.
Impedance analysis

The interface, grain and grain boundary properties are studied using the complex impedance formalisms that include the determination of capacitance, the relaxation frequency and the ionic conductivity [17]. The plot of \( Z'' \) versus \( Z' \) (Nyquist diagram) at different temperatures of CSNN\(_{0.92}\) sample is shown in Figure 12. There are mainly two overlapping semicircles, which correspond to grain interiors (the semicircle at low frequency) and grain boundaries (the semicircle at high frequency) [18]. In other words, centers of semi circles that compose the total electric response are centered below the real axis (\( Z' \)), which confirms the presence of non-Debye type of relaxation in this compound. As can be seen in Figure 12, the diameter of the large semicircle arc of the impedance complex plane plot (\( Z'' \)) decreased with the increasing temperature. This indicated that the total resistance decreased as temperature increased, which indicated, as a result, the existence of an activated conduction mechanism which confirms that the material behaves like a semiconductor.

\[
Z_{\text{CPE}} = \frac{1}{Q(j\omega)^\alpha} \tag{4}
\]

Where \( \omega \) is the angular frequency, \( Q \) indicates the value of the pseudo-capacitance of the fractal interface CPE element, and \( \alpha \) represents the magnitude of the departure of the electrical response from an ideal condition and also indicates the degree of depression of arc below the real axis. In order to check the choice of the equivalent circuit, we present in Figure 13 the variations of the experimental values of \( Z' \) and \( Z'' \) at some temperatures versus the simulated ones calculated using the parameters extracted from the equivalent circuit. It is obvious from this figure that the slope
obtained from a fit linear of the data points at each temperature is nearly equal to the unity. This behavior indicates that the adopted equivalent circuit describes the electric properties of the investigated compound.

![Plot of measured values versus simulated values of the real and imaginary parts of the impedance.](image)

**Figure 13:** Plots of measured values versus simulated values of the real and imaginary parts of the impedance.

Relying on the bulk resistance values and the sample dimensions, the grain electrical conductivity can be calculated at each temperature using the following equation:

$$\sigma_g = \frac{e}{RS}$$  \hspace{1cm} (5)

Where: $e$ and $S$ are respectively the thickness and the area of the pellet.

The temperature dependence of the conductivity ($\ln(\sigma_pT)$ versus $1000/T$) is shown in Figure 14. Besides, the experimental values of conductivity are fitted to the Arrhenius-type comportment described by the following expression:

$$\sigma_p = A_0\left(\frac{E_a}{k_BT}\right)$$  \hspace{1cm} (6)

![Plot of Ln (σT) versus (1000/T) of the conductivity data for CSNN0.92 ceramic compound.](image)

**Figure 14:** Plot of Ln (σT) versus (1000/T) of the conductivity data for CSNN0.92 ceramic compound.
Where $A$ is the pre-exponential factor, $k$ is the Boltzmann constant and $E_a$ is the activation energy.

All phase transitions appearing in dielectric study are affirmed by the change of the curve slope at $T_c$ and $T_T$. The values of the activation energy determined from a linear fit to the data points are $E_a(I) = 0.48\text{eV}$ in region I, $E_a(II) = 0.59\text{eV}$ in region II and $E_a(III) = 0.77\text{eV}$ in region III.

**Conclusion**

In summary, a lead-free piezoelectric perovskite solid solution CSNN$_{0.975}$ is synthesized using the solid-state reaction method. An X-ray structural analysis confirms that this material displays the quadratic structure in a P4mm space group at room temperature. The microstructural analysis shows the homogeneously grainy morphology of the compound with grain sizes varying from 2nm to 5.5nm. The piezoelectric measurements were carried out to complement the understanding of the materials’ behavior. The evolution of the real part of dielectric permittivity and dielectric loss ($\tan\delta$) versus temperatures revealed an anomaly at 635K that corresponds to the ferroelectric-paraelectric transition temperature. The investigations on the impedance further reveal that (i) the electrical conduction in the material contributed by both the grain and the grain boundary effect, (ii) the material behaves like a semiconductor.

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