Ultra-low noise optical injection locking amplifier with AOM-based coherent detection scheme

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A novel optical injection locking amplifier with acousto-optic modulator based phase modulation and a coherent detection scheme for optical frequency transfer applications is experimentally demonstrated in this study. A commercial distributed feedback diode laser is injection-locked to the resonant frequency of the optical signal with an optical fiber path length of hundreds of kilometers. This provides approximately 59 dB gain and ensures that the input carrier frequency fractional stability can be as good as $10^{-20}$ at 1000 s. The amplifier was tested for the transfer of a commercial narrow-linewidth laser in a 180 km fiber link to a remote site with only a single amplification step. The transferred frequency at the remote end reached $10^{-20}$ at 20000 s, which is suitable for optical frequency distribution and remote comparison between optical atomic clocks.

Immense progress in the development of frequency standards has facilitated high performance in various research fields. State-of-the-art optical frequency standards are superior to the current cesium-based atomic clocks, in which a fractional systematic uncertainty1-2 can reach as low as $10^{-18}$, and the fractional instabilities3-4 in the same regime are below $10^{-17}$. They serve as frequency references for testing basic theories such as quantum electrodynamics, general relativity, and their foundations, for example, to verify the constancy of the fundamental constants and other experiments that can be performed locally5-6. However, studies in fundamental physics, navigation, time keeping, or geodetic applications7-9 require that the clock signal be transferred to remote sites. Traditional satellite-based frequency transfer is far from meeting the requirements as its stability is only $10^{-16}$ over an entire day. Therefore, optical fiber links have been widely investigated as possible media for transferring today’s most stable existing frequencies to remote locations10-19. In order to transmit an optical signal across a distance up to thousands of kilometers, the noise introduced by the optical fiber link should be eliminated and the power loss caused by long-distance transmission should be compensated in order to significantly improve the signal-to-noise ratio of the optical signal detected at both the local and remote end.

An erbium-doped fiber amplifier (EDFA) is the most commonly used amplifier for amplification in an optical fiber link. However, the bidirectional nature of the frequency transfer system (Doppler phase noise cancellation technology) limits the gain of the system and deteriorates the stability of transmission; this is because the point reflections and Rayleigh scattering in the fiber link may send feedback into the EDFAs, which may trigger the stimulated effect20,21. Fiber Brillouin amplification (FBA) is an alternative technique that can provide an amplification gain of 50 dB with approximately 30 mW pump power only. Further, since the pump laser frequency will be locked at the signal laser frequency to achieve a narrow gain bandwidth (i.e., quasi-unidirectional amplification), Rayleigh scattering and point reflections have negligible effects during transmission of the optical frequency22,23. Kim et al.24 proposed an optical injection phase-locked loop (OIPLL) scheme that can provide a high net gain of approximately 44 dB with narrow gain bandwidth when an optical signal is transmitted through a 146 km fiber link. They obtained the phase noise of the optical injection locking system based on intensity modulation and direct detection, and they realized the locking effect by driving the pump current in the slave laser using an electronic feedback loop with a 750 Hz feedback bandwidth.

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An amplifier with better performance is urgently needed with stability much better than $10^{-18}$ at 1000 s to meet the transmission of optical frequency standards. In this article, we propose a novel OIPLL structure with four improvements. (1) A different type of distributed feedback (DFB) diode laser is used as the slave laser so that the amplifier can have a higher output power of 10 dBm to 15 dBm. (2) The actuator device used to execute OIPLL feedback is an acousto-optic modulator (AOM), which can provide a feedback loop with higher bandwidth and hence improve noise suppression. (3) The error signal used in the OIPLL is obtained by phase modulating the AOM signal combined with coherent detection, which can provide higher detection sensitivity. (4) By combining the polarization-maintaining (PM) structure within the OIPLL, the system can be more robust without an additional polarization controller. As a result, we built an optical injection locking amplifier (OILA) with approximately 59 dB gain and frequency stability as good as $10^{-25}$ at 1000 s.

Results

Optical injection locking amplifier (OILA). The OILA configuration is shown in Fig. 1. A weak optical carrier $\omega_0$, as shown in the black box (a), is divided into two parts (A and B) by an optical coupler. Part A is used as a reference while part B passes through an AOM with a PM fiber. The frequency thus shifts to $\omega_0 + \omega_{\text{AOM}} + \Delta \phi_c$, as shown in (b), where $\omega_{\text{AOM}}$ is the fixed 80 MHz frequency shift and $\Delta \phi_c$ is the frequency shift of the AOM generated by the control signal of the proportional-integral (PI) circuit. Light then passes through a PM three-port cyclic optical circulator and is injected into a commercial DFB diode laser ("slave" laser with optical frequency $\omega_s$), which is shown in the black box (c). Since the optical fibers between the AOM and DFB are PM fibers, we did not include an additional polarization controller between the AOM and the optical circulator. Inside the DFB laser, if the detuning frequency $\Delta \omega_{\text{det}} = \omega_0 + \omega_{\text{AOM}} + \Delta \phi_c - \omega_s$ is within the optical injection locking bandwidth, the optical frequency of the "slave" laser becomes locked at the optical frequency of the injected signal, and a frequency fluctuation of $\Delta \phi_s$ due to the injection locking process gets added at point C. The signal $\omega_s + \omega_{\text{AOM}} + \Delta \phi_c + \Delta \phi_s$ at point D again gets divided into two parts. One part is an amplified output signal, and the other part is compared with the reference signal in a 50/50 optical coupler, as shown in the black frame (d). Two optical signal beats at the photodiode (PD) generate an error signal $\omega_{\text{AOM}} + \Delta \phi_c + \Delta \phi_s$, the signal is detected using single sideband coherent detection with high sensitivity. The RF signal after amplification and filtering is mixed with the 80 MHz reference signal through an analog RF phase discriminator. The output of the phase fluctuations $\Delta \phi_c + \Delta \phi_s$ (error signal) will be dealt with a PI algorithm to make $\Delta \phi_c + \Delta \phi_s = 0$ and to produce the control signal $\Delta \phi_c = - \Delta \phi_s$ that acts on the AOM. The frequency shift introduced by the AOM eliminates phase fluctuations introduced by the injection locking process. The amplified output signal is the stable optical frequency signal $\omega_s + \omega_{\text{AOM}}$, as shown in the black frame (e).

We constructed an optical Mach–Zehnder interferometer to test the OILA, as shown in Fig. 2. The input signal is a commercial narrow-linewidth fiber laser (NKT-X15 with 100 Hz Lorentz linewidth). The light is divided into two arms: one for the amplifier, which under different injection ratios can be controlled by tuning the variable attenuator in the measurement arm, and the light in the other functions as the reference. All PM structures in the OILA and the polarization-insensitive property of the AOM help achieve long-term robustness without any polarization controller in the interferometer. The OILA frequency shift is approximately 80 MHz. Thus, the frequency of the reference arm would not be shifted. The beat signal of the reference and OILA is detected with a PD. It is then sent to a phase noise test set or a digital frequency counter to measure the phase noise or long-term stability.

The phase noise power spectral density (PSD) of the OILA for different amplification gains are shown in Fig. 3(a). The interferometer noise floor is measured by removing all components from the OILA except the AOM. The noise bump in the PSDs, above 200 kHz, is the bandwidth of the optical phase-lock loop used to eliminate phase fluctuations $\Delta \phi_s$ introduced by the optical injection locking process. The integrated phase noise of the
OILA at $-43\text{ dB}$ and $-49\text{ dB}$ injection ratios in the frequency range from $1\text{ Hz}$ to $500\text{ kHz}$ is equal to $0.0247\text{ rad}$ and $0.0269\text{ rad}$, respectively. Since the difference is only $0.0022\text{ rad}$, we can conclude that phase fluctuations due to the optical injection locking process can still be completely suppressed when the injection ratio is reduced to nearly $-50\text{ dB}$. The OILA phase noise increases as the injection ratio decreases. When the OILA injection ratio reaches $-55\text{ dB}$, $-61\text{ dB}$, and $-66\text{ dB}$, the integrated phase noise deteriorates to $0.0461\text{ rad}$, $0.0656\text{ rad}$, and $0.1095\text{ rad}$, respectively. The optical injection locking bandwidth is also proportional to the injection ratio. In our experiment, we measured the bandwidth to be $60\text{ MHz}$ when the injection ratio was $-66\text{ dB}$.

The integrated OILA phase noise for an injection ratio ranging from $-43\text{ dB}$ to $-66\text{ dB}$ corresponds to an Allan deviation (ADEV) and modified Allan deviation (MDEV) at $1\text{ s}$; this is basically in accordance with the $\pi^{-3/2}$ type dead time free frequency counter measurements, as shown in Fig. 3(b,c). The MDEV follows the rule of $\tau^{-3/2}$ for an averaging time less than $20\text{ s}$, indicating white phase noise at this time scale. The OILA stability degrades as the injection ratio decreases. However, the MDEV of the OILA still reaches $8.7 \times 10^{-17}$ at $1\text{ s}$ and
improves to more than $8.6 \times 10^{-20}$ at 1000 s for an injection ratio of $-66$ dB. The results ensure that this technique can be used for achieving accurate optical frequency transfer.

**OILA in optical frequency transfer.** To further test the performance of the OILA, we transferred a precise optical frequency over a spool fiber link based on Doppler phase noise cancellation technology, as shown in Fig. 4. The OILA under test is placed at the remote end, and the optical frequency transfer is conducted for 100 km, 120 km, 140 km, 160 km, and 180 km fiber lengths. The power attenuation caused by these lengths causes the OILA injection ratio to correspond exactly to $-43$ dB, $-49$ dB, $-55$ dB, $-61$ dB, and $-66$ dB, respectively. The transmitted signal is derived from a commercial NKT-X15 narrow-linewidth fiber laser, as mentioned earlier, with an optical frequency close to 194 THz and an output power of 6 dBm. After passing through a 30/70 optical coupler, a circulator, and an AOM, the power injected into the fiber is 0 dBm. At the remote end, the optical power attenuated due to the fiber link (we take 180 km transmission as an example) is approximately 49 dB. Inside the OILA, the attenuation of a 50/50 optical coupler, an AOM, and a circulator was 7 dB in total, implying an injection power of $-56$ dBm (equivalent to 2.5 nW). Since the output power from the OILA is 10 dBm, the net amplification gain in the amplifier is 59 dB (the output power of 10 dBm minus the input power of $-49$ dBm)$^{24}$. Moreover, since the OILA includes an AOM for phase-locking, it can also function as a frequency shifter. Therefore, the remote end does not need to have an additional AOM for frequency-shifting. The uncompensated fiber is minimized, and all fiber-optic components are packaged in a 10 cm $\times$ 8 cm box. The box is then temperature-protected to reduce air currents that cause temperature drifts.

We use a phase noise test set to measure the noise added to the light, as shown in Fig. 5(a). The phase noise added to the light after a 180 km link when the transmission system is in the free-running state follows the power law $S_{\phi}^\text{fiber}(f) = h/f^2$ for frequencies ranging from 1 Hz to 1 kHz. This indicates that the type of noise introduced by the fiber link is white phase noise. The green dashed line shows the coefficient $h = 120$ in this experiment. When the fiber link is stabilized, the phase noise added to the light for a 180 km link can be remarkably suppressed to $2 \times 10^{-3}$ rad$^2$/Hz for frequencies ranging from 1 Hz to 1 kHz. The bump at approximately 278 Hz is the bandwidth of the compensation system for the 180 km fiber link, which fits the estimated value calculated using $1/4\tau_d$. A comparison of the phase noise in the 180 km link between the stabilized and free-running conditions shows that the noise suppression at 1 Hz is approximately $-48.67$ dB, while the theoretical limit is given by $-49.72$ dB, suggesting that our transmission system is approaching the theoretical limit.

Figure 5(b,c) shows the ADEV and MDEV of the optical transmissions for different distances. Compared with the brown curve for the free-running state, the results show that noise added by the optical fiber is suppressed. After 180 km of transfer with only one amplifier, the MDEV at the remote end reaches $1.3 \times 10^{-15}$ at 1 s and $1.5 \times 10^{-18}$ at 1000 s.

Meantime, the MDEV for the corresponding injection ratio of $-66$ dB in Fig. 2(d) is $8.6 \times 10^{-20}$ at 1000 s. A comparison of these two MDEVs shows that the noise added by the OILA is approximately one order of magnitude smaller than that added by the stabilized fiber link. We can thus conclude that the OILA does not significantly deteriorate the transfer performance.
Discussion
We propose an OILA for optical frequency transmission applications. The phase noise and frequency stability of the OILA with different injection ratios was tested, and the results suggested that it can provide higher gain, narrower gain bandwidth, and lower noise than the bidirectional EDFA in12. We only used one amplifier at the remote end in our experiment on transferring a commercial NKT-X15 narrow-linewidth fiber laser carrier in a round-trip fiber link ranging from 200 km to 360 km (corresponding optical attenuation range is 72 dB to 98 dB). The amplifier was used for the mid-stage amplifier and the frequency regenerator. In this way, the output of the OILA at the remote end could be divided into two parts. One part can transfer to the next stage with 180 km fiber length, and the other returns back to the local end to determine the fiber noise14. Further, we did not use an additional polarization controller inside the OILA. At the remote end, the MDEV reaches values of $1.4 \times 10^{-20}$ and $7.8 \times 10^{-20}$ at an averaging time of 20000 s for 100 km and 180 km distances, respectively. Hence, a smaller number of amplifiers, as well as control and maintenance efforts, are required for transmission over thousands of kilometers compared to EDFAs with normal single relay distances of approximately 80 km to 100 km12. In the next step, the OILA will be used on an urban fiber link to distribute a cavity-stable laser carrier because the OILA is polarization-insensitive and robustness.

Methods
The optical injection locking system used as an amplifier in an optical frequency transfer system primarily needs to consider two basic parameters. The first, commonly referred to as the detuning frequency25–27, is the difference between the solitary lasing frequencies of the “master” and “slave” lasers. When light from the “master” laser is injected into the “slave” laser, and the detuning frequency is less than the bandwidth of the injection locking system, the “slave” laser can establish a stable oscillation at the same optical frequency as the “master” laser, and its free-running mode is suppressed25. The second parameter, called the injection ratio, is the ratio of the injected optical power from the “master” laser to the output power of the free-running “slave” laser. The injection ratio can affect phase fluctuations in the injection locking system, as shown below27:
\[ \Delta \phi_L = \sin^{-1}\left( -\frac{\Delta \omega_{\text{inj}}}{\kappa \sqrt{1 + \alpha^2}} \sqrt{\frac{P_{\text{inj}}}{P_{\text{in}}}} \right) - \tan^{-1}\alpha \]

where \( \Delta \phi_L \) is the additional phase noise of the optical injection locking system, \( \Delta \omega_{\text{inj}} = \omega_{\text{inj}} - \omega_{\text{p}} \) is the detuning frequency, \( \kappa \) is the coupling rate, \( \alpha \) is the linewidth enhancement factor of the slave laser, and \( P_{\text{inj}} \) and \( P_{\text{in}} \) are the powers of the free-running slave and the injected signal, respectively. Inside the amplifier, the input signal power will be much less than the output power from the "slave" laser. This will create additional phase fluctuations \( \Delta \phi_L \) in the amplifier, as observed from Eq. 2. We present a design for an AOM-based phase modulation and coherent detection scheme to suppress phase fluctuations. This design helps to realize high gain and low noise in the amplifier.

Data Availability
The datasets generated during and analyzed during the current study are available from the corresponding author upon reasonable request.

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Author Contributions
Zitong Feng and Fei Yang conceived the experiments and wrote this report. Both have contributed equally to this work. Haiwen Cai conceived the experiments and managed the projects. All authors carried out the experiments and contributed to the final manuscript.

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