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Towards Applying Logico-numerical Control to Dynamically Partially Reconfigurable Architectures

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Abstract: We investigate the opportunities given by recent developments in the context of Discrete Controller Synthesis algorithms for infinite, logico-numerical systems. To this end, we focus on models employed in previous work for the management of dynamically partially reconfigurable hardware architectures. We extend these models with logico-numerical features to illustrate new modeling possibilities, and carry out some benchmarks to evaluate the feasibility of the approach on such models.

Keywords: Discrete Controller Synthesis, Infinite Systems, Control of Computing, Synchronous Languages, Hardware Architectures, Dynamically Partially Reconfigurable FPGA

1. INTRODUCTION

Recent proposals by Berthier and Marchand (2014) in the domain of symbolic Discrete Controller Synthesis (DCS) techniques have led to the development of a tool capable of handling logico-numerical systems and properties, i.e., involving state variables defined on infinite domains. The handling of such infinite systems opens the way to new opportunities for modeling and control, that still need to be investigated.

We extend real-life models proposed by An et al. (2013a,b) for the management of Dynamically Partially Reconfigurable (DPR) hardware architectures to: (i) assess the feasibility of the proposal on bigger systems, (ii) perform some performance evaluations of the new tool ReaX on realistic models, including for control objectives newly implemented in this tool; and (iii) introduce logico-numerical features in the model to assess that the approach can still be applied using models involving quantitative aspects.

DPR Hardware Architectures DPR hardware architectures, typically Field Programmable Gate Arrays (FPGAs) (Lysaght et al., 2006), have been identified as a promising solution for the design of energy-efficient embedded systems (Hinkelmann et al., 2009). However, such solutions have not been extensively exploited in practice for two main reasons: (i) the design effort is extremely high and strongly depends on the available chip and tool versions, and (ii) the simulation process, which is already complex for non-reconfigurable systems, is prohibitively large for reconfigurable architectures. Therefore, new adequate methods to deal with their correct dynamical reconfiguration are required to fully exploit their potential.

Dynamical reconfiguration management requires choosing new configurations depending on the history of events occurring in the system and predictive knowledge about possible outcomes of reconfigurations. Such decision-making component is difficult to design because of the combinatorics of possible choices, the transversal constraints between them, and even more, the history aspects. The work we present advocates the application of DCS techniques to fulfill this control problem.

Related Works The reconfiguration management in DPR technologies is usually addressed by using manual encoding and analysis techniques that are tedious and error-prone according to Göhringer et al. (2008). Other existing approaches dedicated to self-management of adaptive or reconfigurable systems use heuristics and machine learning techniques (Sironi et al., 2010; Paulsson et al., 2006; Jovanović et al., 2008) for instance. Maggio et al. (2012) discuss some approaches applying standard control techniques such as Proportional Integral and Derivative (PID) controller or Petri nets-based control. The same kind of control has also been used for processor and bandwidth allocation in servers (Lu et al., 2002). Eustache and Diguet (2008) applied close-loop control to select hardware/software configurations on an FPGA with a configuration control based on a data-flow model and diffusion mechanisms. We note that such a solution relies on heuristics and empirical laws that prevent instability and select the suitable configurations.

Compared to the above reconfiguration control techniques, major advantages of the discrete control approach considered by An et al. (2013a,b) are the enabled formal correctness and guarantees on run-time performance, as well as the possibility to synthesize the controller automatically.

Outline We first present in Section 2 the modeling formalism we use for expressing the reconfiguration problem, as well as the tools involved in our work. Sections 3 detail the problem of reconfiguration control for FPGA-based DPR systems. We expose the modeling and formulation as a DCS problem, as well as an illustrative logico-numerical extension of the model in Section 4, and we report on our performance evaluation experiments in Section 5.
2. MODELING FORMALISM AND TOOLS

2.1 Arithmetic Symbolic Transition Systems

The model of Arithmetic Symbolic Transition Systems (ASTSs) is a transition system with (internal or input) variables whose domain can be infinite, and composed of a finite set of symbolic transitions. Each transition is guarded on the system variables, and has an update function indicating the variable changes when a transition is fired. This model allows the representation of infinite systems whenever the variables take their values in an infinite domain, while it has a finite structure and offers a compact way to specify systems handling data.

Let \( V = \{v_1, \ldots, v_n\} \) be a tuple of variables and \( D_v \) the (infinite) domain of \( v \). We note \( D_V = \prod_{i \in [1 .. n]} D_{v_i} \) the (infinite) domain of \( V \). \( v_i(V) \) gives the value of variable \( v_i \) in vector \( V \).

**Definition 1.** (Arithmetic Symbolic Transition System). An ASTS is a tuple \( S = (X, I, T, A, \Theta_0) \) where:

- \( X = \{x_1, \ldots, x_n\} \) is a vector of state variables ranging over \( D_X = \prod_{i \in [1 .. n]} D_{x_i} \), and encoding the memory necessary for describing the system behavior;
- \( I = \{i_1, \ldots, i_m\} \) is a vector of variables that ranges over \( D_I = \prod_{i \in [1 .. m]} D_{i_j} \), called input variables;
- \( T \) is of the form \( x'_i = T^{x_i} x \), such that, for each \( x_i \in X \), the right-hand side \( T^{x_i} \) of the assignment \( x'_i = T^{x_i} x \) is an expression on \( X \cup I \). \( T \) is called the transition function of \( S \), and encodes the evolution of the state variable \( x_i \). It characterizes the dynamic of the system between the current state and the next state when receiving an input vector;
- \( A \) is a predicate with variables in \( X \cup I \) encoding an assertion on the possible values of the inputs depending on the current state;
- \( \Theta_0 \) is a predicate with variables in \( X \) encoding the set of initial states.

For technical reasons, we shall assume that \( A \) is expressed in a theory that is closed under quantifier elimination as for example the Presburger arithmetic.

ASTSs can conveniently be represented as parallel compositions of Mealy automata with numerical variables and explicit locations or in its symbolic form.

Let us consider the following example ASTS where \( X = \{\xi, x, o\} \), \( I = \{a, i\} \) with \( D_X = \{F, G\} \times \mathbb{Z} \times \mathbb{B} \), \( D_I = \mathbb{B} \times \mathbb{Z} \)

\[
T = \begin{cases} 
\xi' := & G \quad \text{if} \ (\xi = F \land a \land x \geq 0), \\
F \quad \text{if} \ (\xi = G \land i > 42), \text{otherwise} \\
\end{cases}
\]

\[
x' := \begin{cases} 
2x + 1 \quad \text{if} \ (\xi = F \land a \land x \geq 0), \\
i \quad \text{if} \ (\xi = G \land i \leq 42), \text{otherwise} \\
\end{cases}
\]

\[
o' := \begin{cases} 
(\xi = F \land a \land x \geq 0) \lor (\xi = G \land i > 42) \\
(\xi = F \land a \land x \geq 0) \\
(\xi = G \land 2x + 2i \leq 41 \land a) \\
\end{cases}
\]

\[
\Theta_0(\xi, x, o, i) = (\xi = F \land x = 0)
\]

The corresponding Mealy automaton with explicit locations (leaving \( A \) aside) can be represented as in Figure 1.

**Remark 1.** Observe that the variable \( o \) is actually an output of the system, although it belongs to the vector of state variables. Indeed, we do not distinguish between those two kinds of variables to keep the ASTS models simple. We can characterize output variables as the ones that never appear in the right hand side of the assignments in \( T \).

**Remark 2.** We qualify as logico-numerical an ASTS whose state (and non-output) and input variables are Boolean variables (\( \mathbb{B} \)) or numerical variables (typically, \( \mathbb{R} \) or \( \mathbb{Z} \)), i.e., such that \( X = \mathbb{B}^k \cup \mathbb{R}^k' \cup \mathbb{Z}^{k''} \) with \( k + k' + k'' = n \) (and similarly for the input variables). ASTSs with only Boolean non-output state variables are called finite.

For each ASTS, one can make correspond an Infinite Transition System (ITS) defined as follows:

Given an ASTS \( S = (X, I, T, A, \Theta_0) \), we make correspond an ITS \( \mathcal{S} = (X, I, T, D_S, A_S, \Theta_0) \) where:

- \( X = D_X \) is the state space of \( \mathcal{S} \);
- \( I = D_I \) is the input space of \( \mathcal{S} \);
- \( T_S \subseteq X \times I \times X \) such that \( T_S(x, \nu) = (x', \nu) \) if \( \forall j \in [1 .. n], x'_j := T^{x_j}(x, \nu) \);  
- \( A_S \subseteq X \times I \) is such that \( A_S = \{ (x, \nu) \in X \times I | A(x, \nu) = true \} \);
- \( X_0 \subseteq X \) is the set of initial states, and is such that \( X_0 = \{ x \in X | \Theta_0(x) = true \} \).

The behavior of such a system is as follows. \( \mathcal{S} \) starts in a state \( x_0 \in X_0 \). Assuming that \( S \) is in a state \( x \in X \), then upon the reception of an input \( \nu \) in \( I \) such that \( (x, \nu) \in A_S \), \( S \) evolves in the state \( x' = T_S(x, \nu) \). We denote \( X_{\text{Trace}}(\mathcal{S}) \) the set of states that can be reached in \( S \). Given an ASTS \( S \) and a predicate \( \Phi \) over \( X \), we say that \( S \) satisfies \( \Phi \) (noted \( S \models \Phi \)) whenever \( X_{\text{Trace}}(S) \subseteq \{ x \in X | \Phi(x) = true \} \).

**Control of an ASTS** Assume given a system \( S \) and a predicate \( \Phi \) on \( S \). Our aim is to restrict the behavior of \( S \) by means of control in order to fulfill \( \Phi \). We distinguish between the uncontrollable input variables \( U \) which are defined by the environment, and the controllable input variables \( C \) which are defined/restricted by the controller of the system. For technical reason, we assume that the controllable variables are Boolean. Note that the partitioning of the input variables in \( S \) induces a “partitioning” of the input space in \( S \), so we have \( I = D_I \times D_C \). A controller is then given by a predicate \( A_C \) over \( X \times U \cup C \) that constrains the set of admissible (Boolean) controllable inputs so that the traces of the controlled system always satisfy \( \Phi \).

**Definition 2.** (Discrete Controller Synthesis Problem). Given an ASTS \( S = (X, U \cup C, T, A, \Theta_0) \) and a predicate \( \Phi \) over \( X \), solving the discrete controller synthesis problem is to compute a predicate \( A_C \) such that

\[
S' = (X, U \cup C, T, A_C, \Theta_0) \models \Phi \quad \text{and} \forall x \in X \cup U \cup C, A_C(x) \Rightarrow A(x).
\]

The general control problem that we want to solve is undecidable. In (Berthier and Marchand, 2014), we then used abstract interpretation techniques to ensure, at the price of some over-approximations, that the computation...
of the controller terminates (see e.g., (Cousot and Cousot, 1977)). This over-approximation ensures that the forbidden states are not reachable in the controlled system. Thus, the synthesized controller remains correct, yet may not be maximally permissive w.r.t the invariant. For the details on how the controller is computed, one can refer to (Berthier and Marchand, 2014).

2.2 ReaX & BZR

ReaX Berthier and Marchand (2014) introduced the tool ReaX implementing the above symbolic algorithms for the synthesis of controllers ensuring safety properties of infinite state systems modeled by ASTs. Compared with what is reported in this previous work, in addition to the invariance of a predicate, one can also request the controlled system to be deadlock-free. Adapting techniques from Marchand and Samaan (2000), ReaX also implements classical algorithms of invariance and reachability enforcement for finite systems, as well as one-step optimization of numerical variables for general ASTs.

BZR An et al. (2013a,b) used the reactive data-flow language BZR (Delaval et al., 2010) to describe their solution. BZR programs are built as parallel compositions of data-flow nodes, each having input and output flows. The body of the node describes how input flows are transformed into output flows, in the form of a set of equations and/or automata. They are evaluated, all together at each step of a reactive system (hence the composition is called synchronous), by taking all inputs, computing the transitions and equations, and producing the outputs. An invariant and controllable variables can be specified, and the BZR compiler involves DCS to automatically produce a controller guarantying that the resulting controlled system satisfies the invariance property by constraining the values of the controllable variables. To do so, BZR involves a compilation phase using either Sigali (Marchand et al., 2000) or ReaX (Berthier and Marchand, 2014) DCS tools.

Remark 3. As Sigali supports the handling of cost functions for optimization purposes (functions from the finite state space and input space of the systems to integers) (Marchand et al., 2000), the Sigali BZR backend is able to make use of this device to translate programs involving nodes with Integer output flows (Delaval et al., 2013). It is however unable to translate programs with Integer state variables, like the one of Figure 1.

3. FPGA CONTROL PROBLEM

We consider applications made of tasks executing according to dependency constraints on an FPGA platform. The latter may provide various computation resources having different characteristics or specializations for the tasks to execute, and each task may be implemented in several ways using dissimilar sets of resources.

An et al. (2013a,b) provided a solution for the problem of choosing a scheduling satisfying both the execution dependencies between the tasks and the utilization constraints on the resources of the FPGA platform. This proposal consists in the model-based generation of a run-time manager whose role is to start tasks and detect their termination, and allocate appropriate computation resources for them to execute. The run-time manager is designed by first modeling the platform and the task dependency graph using a synchronous language, and then solving a DCS problem to enforce the correct behavior of the whole system.

We recall in this section the modeling principles employed in the previous work (An et al., 2013a,b) for the design of the run-time manager, and introduce the basis for the extension of the model with logico-numerical features.

3.1 Describing the System

Hardware We consider a multiprocessor architecture implemented on a reconfigurable device (e.g., Xilinx Zynq) comprising a general purpose processor A0 (e.g., ARM core) executing the run-time manager. The device also includes a reconfigurable area (e.g., FPGA-like with power management capabilities) divided into reconfigurable tiles. Figure 2-a) shows an illustrative example comprising four tiles A1–A4. The communications between architecture components are achieved by means of a Network-on-Chip (NoC). Each processor and tile implements a NoC Interface (NI). Tiles can be combined and configured to implement and execute tasks by loading predefined bitstreams.

The FPGA platform is equipped with a battery supplying it with energy; this battery may be setup to enable harvesting. We also assume that the hardware platform provides means for the programs executing on the processor to measure its remaining capacity, either directly in the case of a smart battery (SBS Implementers Forum, 1998) if the platform is equipped with the appropriate devices, or indirectly, e.g., by interpretation of output voltage measurements. Regarding power management of the FPGA, any unused tile Ai can be put into sleep mode with a clock gating mechanism such that it consumes a minimum static power.

Application Software We consider that the application software is described as a directed acyclic graph (DAG), where nodes represent individual tasks to be executed, and directed edges depict dependency constraints between tasks: e.g., an edge between nodes A and B indicates that the task A must have terminated its execution before B can execute. Figure 2-b) shows an illustrative example consisting of four tasks A, B, C and D. Note that we do not restrict the abstraction level of tasks: they can denote atomic operations or coarse fragments of system functionality.

The run-time manager is in charge of scheduling the tasks so that their execution dependencies are satisfied.

Given a hardware architecture, a task can be implemented in various ways, each having specific characteristics in terms of: (i) the set of tiles used for its execution; (ii) its worst case execution time; and (iii) peak power consumption.

Before executing a task on a reconfigurable architecture, the task implementation must be loaded to reconfigure the corresponding tiles if required. This reconfiguration
Fig. 3. Configurations and reconfigurations.

operation inevitably involves some overheads regarding, e.g., time and energy. For simplicity, we assume that the worst case execution time of each task implementation encompasses the time required to reconfigure the tiles it uses (as in the worst case, a task implementation must always be loaded before being executed).

Reconfiguration Figure 3 exemplifies three system configurations. In 1), task A is running on tiles A3 and A4 (see Figure 2-a)) while tiles A1 and A2 are in sleep mode. Configurations 2) and 3) show two scenarios where tasks B and C run in parallel. Assume tasks B and C have two implementations so that the system can go to either 2) or 3) once task A finishes its execution (according to the graph of Figure 2-b)). If the current state of the battery level is low, the system would choose 2) as 3) requires the complete circuit surface and therefore consumes more power. On the contrary, when the battery level is high, 3) would be chosen if the user expects a better performance.

3.2 System-level Objectives

The run-time manager can decide to delay the execution of a task and determines which implementation of it to trigger. These choices are made according to system objectives that define the system functional and non-functional requirements. The objectives considered in this work, are either logical control or optimization objectives. Generally speaking, logical objectives express properties about discrete states of the system (e.g., mutual exclusions), whereas optimal ones concern weights and costs.

The logical control objectives we consider are: (i) exclusive uses of tiles A1–A4 by the executing tasks; (ii) switch tiles into active or sleep mode depending on whether a task executes on them or not to save energy; (iii) avoid power consumption peaks of the hardware platform w.r.t the electrical charge of the battery; and (iv) once started, the application can always finish. Optimization objectives notably encompass the minimization of the power peaks of the platform to augment the lifespan of the battery.

4. MODELING RECONFIGURATION CONTROL AS A DCS PROBLEM

We focus on the management of computations on the tiles and dedicate the processor area A0 exclusively to the execution of the resulting run-time manager. So, we build a global system model as an ASTS representing the behavior of the reconfigurable computing system; system objectives are then specified using predicates expressed on variables of the model.

We recall, and reformulate in terms of ASTSs, the models proposed by An et al. (2013a,b). At the same time, we introduce a new, logico-numerical model for the battery, to demonstrate the added expressiveness allowed by the ASTSs handled by ReaX.

Fig. 4. Models RM, for a tile Ai, and BM for a battery.

4.1 System Model

Modeling the Tiles Figure 4-a) depicts the model describing the behavior of a tile Ai: it features two states (Sle and Act) as a tile may or may not be active at a given instant. The model switches from a state to another depending on the value of its Boolean controllable variable c_ai. The output act_i represents its current mode.

Discrete Battery Model Figure 4-b) represents a discrete model for a battery proposed by An et al. (2013a,b). It is characterized with three states/levels: H (high), M (medium) and L (low). This model is assumed to take its inputs from a dedicated software executing on processor A0, that interprets capacity measurements and drives the state of this model by emitting up and down events depending on the current electrical charge of the battery. The output st ∈ {H, M, L} reflects the internal state of the model.

Logico-numerical Battery Model We now present a new model for a smooth representation of the state of the battery in the system model. This model aims at illustrating the expressiveness of logico-numerical ASTSs handled by ReaX.

This new model receives as input a rough measure cm of the actual electrical charge (e.g., in Coulombs) provided by a dedicated sensor, and an estimation c_cap of the capacity spent since the last reaction of the model. The state of the battery in this model consists in a numerical variable c providing an estimation of the remaining capacity of the battery. The domain of c can be the domain of reals (arbitrary-precision rationals actually).

At each reaction of the model, the value of c is estimated by using some sort of exponentially weighted moving average: it is computed by using cm when the input measurement from the sensor is determined as valid by bounding its absolute difference with the estimated capacity c_cap the model tries to estimate this value by other means otherwise. The model is further parameterized with a constant smoothing factor α ∈ [0, 1] that specifies the impact of the variations of cm on the state variable c. The constant β serves as a bound to determine the validity of the measured input.

Although the value of c could be used directly in the definition of logical control predicates (and possibly optimization objectives), e.g., to decide whether a given power consumption peak is admissible by the battery, for illustrative purposes we use it directly to compute a value for the finite output st based on additional constant threshold electrical charges λ and µ. In this way, this new battery model is interchangeable with the discrete one, and system control and optimization objectives can be reused whatever the chosen battery model.

The assignment of state variable c and output st ∈ {H, M, L} can be expressed as
We consequently model tasks with automata, such as the one of Figure 6 for A; it features idle and waiting states $I_A$ and $W_A$, plus as many execution states as available implementations of $A$ ($X_A^1$ and $X_A^2$). Controllable variables $c_1$ and $c_2$ are integrated in the model to encode the choices given to the run-time manager; e.g., from the idle state, it can then choose to delay the execution of a task, or to select and start the execution of one of its implementation. The output $es_A$ reflects the execution state of the task.

Three observations of interest are considered for each task. For a task $t$, we capture them by associating a tuple $(rs_t, wt_t, pp_t)$ to the states of task models, where: $rs_t \in 2^{RA}$ ($RA$ being the set of architecture resources — i.e., the tiles in our case), $wt_t \in \mathbb{N}$ and $pp_t \in \mathbb{N}$ are the WCET and the peak power consumption for the task’s state. The observations associated with executing states are the values associated with their corresponding implementations. For idle and wait states, $rs_t = \emptyset$, $wt_t = 0$, $pp_t = 0$.

Remark 5. Task observation variables defined in this section are outputs of the model, and hence belong to the vector of state variables $X$ in the corresponding ASTS model (see Remark 1): the fact that the domain of some of them is infinite does not make the ASTS’s state space infinite.

**Global System Model** The whole system model represents all the possible system execution behaviors in the absence of control (i.e., if a run-time manager is not yet integrated). In our example case of four tiles and set $Tasks = \{A, B, C, D\}$ of tasks, it comprises the parallel composition of the sub-models for tiles $RM_1 - RM_A$, battery $BM$ and tasks $TM_A - TM_D$, plus a scheduler $Sdl$ encoding the task graph:

$$S = RM_1 || \ldots || RM_A || BM || TM_A || \ldots || TM_D || Sdl.$$  

In terms of ASTSs, and assuming variable names do not clash between the various sub-models of the system, this parallel composition essentially boils down to concatenate together, for each sub-model $m$: the vectors of state variables $X_m$’s, controllable (resp. non-controllable) inputs $c_m$’s and $U_m$’s, and assignments $T_m$. The global assumption $A$ made about the environment is the conjunction of all assumptions of the sub-models $A_m$. As for the initial state, the predicate $\Theta_0$ is defined so that $X_0 = \{(Sle_1, \ldots, Sle_4, H, I_A, \ldots, I_D)\}$.

**Global Observations** The observations output locally by each sub-model (e.g., task models) need to be combined into a set of global values in order to account for the resource consumption of the whole system. These values constitute the global observations of the model based on which logical control and optimization objectives can be expressed.

In our case, the global observations available for a particular operating state of the system is the tuple of variables $(rs, wt, pp)$ whose values are computed based on the individual tasks’ observations at the current reaction (denoted $rs_t$, $wt_t$ and $pp_t$). Global observation variables are added to the vector of state variables as any other outputs, and are computed by adding corresponding assignments in $T$ as follows:

\[
\begin{align*}
rs' &:= \sum_{t \in Tasks} rs_t' \\
wt' &:= \min_{t \in Tasks} \{wt_t' \mid wt_t' \neq 0\} \text{ if defined, 0 otherwise} \\
pp' &:= \sum_{t \in Tasks} pp_t'
\end{align*}
\]
Note that in the assignments above, primed versions of tasks’ observations are actually substituted in the ASTS model by the expression they are respectively assigned to. 

Remark 6. By construction, global observation values are outputs of the system and can be computed as functions defined on its state only.

4.2 System Objectives

Based on the model described above, we can formalize the objectives of Section 3.2 in terms of the states and observations defined on the states.

The logical control objectives to be enforced on the system by the run-time manager can be expressed by using two predicates Φ: DX → ℜ and χ: DX → ℜ, respectively encoding invariance and reachability requirements, and expressed on state variables. Φ can be expressed as a conjunction, each of its conjuncts encoding one aspect of the logical control needs:

- exclusive use of tiles: Φx(X) = ∀s,t ∈ Tasks2, s ≠ t, rsx(X) ∩ rts(X) = ∅;
- shut-down and start-up of tiles depending on whether they are used or not by an executing tasks’ implementation: Φx(X) = (∀a ∈ rs(X), acta = true) ∧ (∀a ∈ Dnx \ rs(X), acta = false);
- given a mapping ppthr: {L, M, H} → ℜ from discrete battery levels to threshold peak power values, constraining the total power peak depending on the level of the battery: Φpp(X) = pp(X) ≤ ppthr(st(X)).

In turn, the reachability predicate χ specifies that a state must be reachable where the value of the output end of SdI is true (meaning that the application has finished its execution): χ(X) = (end(X) = true).

One-step optimal objectives aim at minimizing or maximizing numerical state variables in a single step. Optimization objective of Section 3.2 belongs to this type, by requesting to select successor states minimizing power peaks pp.

4.3 Solving the DCS Problem and Using the Result

All the ASTS models above except the logico-numerical battery model are finite ASTSs as their non-output state space is finite (i.e., numerical state variables are outputs, and can thus be represented as cost functions associating numerical values to discrete states — see Remarks 1, 5 and 6). Thus, one can write these models in BZR, use either the Sigali or the ReaX backend of the compiler, solve the resulting DCS problem, and then automatically obtain a controller satisfying the system objectives. Associated with the model, this controller can be used by the run-time manager to dynamically reconfigure the system.

5. EVALUATION & EXPERIMENTAL RESULTS

We report in this section our experiments to evaluate the efficiency of ReaX to solve DCS problems on models as described above. All executions were performed on a 3.2GHz Intel® Xeon® multi-core1 processor with about 6GB of main memory. We first show comparisons of Sigali w.r.t ReaX in the case of finite models, and then present performance results of ReaX on logico-numerical ASTSs.

1 Note however that both Sigali and ReaX are single-threaded.

![Fig. 7. Synthesis times for generated benchmarks.](image1)

![Fig. 8. Synthesis times of ReaX for invariance and either reachability enforcement or one-step optimization.](image2)

Logical Control: Efficiency of ReaX w.r.t Sigali A performance evaluation of Sigali for solving reconfiguration control problems similar to the ones considered in this paper has already been presented by An et al. (2013a). In order to compare the benefits of using ReaX w.r.t Sigali for the same kind of problems, we conducted extensive experiments based on multiple instances of the reconfiguration control problem. Each one of these models is built based on a randomly generated hierarchical task graph constructed recursively by exploiting the idea mentioned in Remark 4. Every system model comprises a discrete battery model, plus four tile models. The task models involved represent either one or two execution modes, each associated to one or two tiles chosen randomly, as well as with random peak power consumption and WCET.

In order to get an idea of the variability of the performance results of each tool w.r.t the complexity of the models (the number of Boolean state variables, increasing linearly w.r.t the number of tasks in the model), we randomly generated 10 samples (from 2 to 11 tasks) of 5 task graphs each.

Figure 7 shows the measured synthesis times w.r.t the number of tasks in the generated task graph: one generated task graph results in two dots in the plot, representing one execution time for each tool. Although Sigali performs better for small problems (less than 5 tasks), ReaX scales much better when this number grows, and still takes 30 seconds to up to 15 minutes for complex applications of 11 tasks for which Sigali would execute for days.

We executed ReaX on the same samples to evaluate its performances for invariance and either reachability or one-step optimization objectives; we plot resulting synthesis times in Figure 8. Comparison with performance results
reported by An et al. (2013a) for Sigali on similar models shows that ReaX compares favorably for both objectives.

All these results show that recent developments in DCS tools can make the modeling approach advocated by An et al. (2013a,b) and used as models for benchmarking in this paper, applicable in practice to medium-sized problems for which a solution would be very difficult, if even possible, to program by hand.

Towards Logico-numerical Control  To evaluate the feasibility of applying the same method on models involving numerical aspects, hence comprising numerical state variables, we took the same set of system models as for the previous benchmarks, and replaced their model of discrete battery with the logico-numerical one described in Section 4.1. We chose the set of reals as domain of every numerical variable.

We report the times taken by ReaX to solve each one of these synthesis problems in Figure 9 — using the power abstract domain with convex polyhedra; see (Berthier and Marchand, 2014). Comparing with the results of Figure 7, we conclude that our addition of one numerical state variable in the model still allows an efficient controller synthesis for invariance enforcement by ReaX.

6. CONCLUSION

We have adapted and extended some previous work by An et al. (2013a,b) tackling the run-time management of DPR architectures. We exploited the models to carry out some performance comparisons between Sigali and ReaX on finite systems, and showed that ReaX allows to handle systems more efficiently than Sigali. Additionally, the introduction of ASTS models allowed us to propose an illustrative example of battery model to demonstrate the capability of ReaX to effectively compute controllers for such systems.

The performance evaluation of ReaX on the “simple” logico-numerical models showed promising results towards the handling of more complex models and properties, expressed using variables defined on infinite domains notably. We plan to pursue our investigations to get a better assessment about the potential of ReaX for models involving more of such numerical state variables. Although one can compute controllers ensuring one-step optimization of numerical outputs, new algorithms are needed for infinite systems to perform k-step or path optimization, i.e., to take into account, not only costs of successor states, but on paths as done by Dumitrescu et al. (2010) in the case of finite systems. At last, our models would also constitute an interesting basis to investigate modular control techniques.

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