Climate Sensitivity From Both Physical and Carbon Cycle Feedbacks

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Abstract The surface warming response to anthropogenic forcing is highly sensitive to the strength of feedbacks in both the physical climate and carbon cycle systems. However, the definitions of climate feedback, \( \lambda_{\text{Climate}} \) in W·m\(^{-2}\)·K\(^{-1}\), and climate sensitivity, \( S_{\text{Climate}} \) in K/(W/m\(^2\)), explicitly exclude the impact of carbon cycle feedbacks. Here we provide a new framework to incorporate carbon feedback into the definitions of climate feedback and sensitivity. Applying our framework to the Global Carbon Budget reconstructions reveals a present-day terrestrial carbon feedback of \( \lambda_{\text{Carbon}} \) = 0.31 ± 0.09 W·m\(^{-2}\)·K\(^{-1}\) and an ocean carbon feedback of \(-0.06\) to \(0.015\) W·m\(^{-2}\)·K\(^{-1}\) in Earth system models. Observational constraints reveal a combined climate and carbon feedback of \( \lambda_{\text{Climate+Carbon}} \) = 1.48 W·m\(^{-2}\)·K\(^{-1}\) with a 95% range of 0.76 to 2.32 W·m\(^{-2}\)·K\(^{-1}\) on centennial time scales, corresponding to a combined climate and carbon sensitivity of \( S_{\text{Climate+Carbon}} \) = 0.67 K/(W/m\(^2\)) with a 95% range of 0.43 to 1.32 K/(W/m\(^2\)).

Plain Language Summary Feedback processes in the physical climate system and the carbon cycle affect the Earth’s climate response to emissions of greenhouse gases, such as carbon dioxide. Physical climate feedbacks include the responses of clouds and atmospheric water vapor to rising surface temperatures, while carbon cycle feedbacks affect how much of the emitted carbon dioxide is removed from the atmosphere and stored in the ocean and on land. Conventionally, definitions of climate feedback and climate sensitivity include all the feedbacks in the physical climate system but do not include carbon cycle feedbacks. This study provides a new framework to incorporate carbon feedback into the definitions of climate feedback and sensitivity. Evaluating the historical strengths of physical climate system and carbon cycle feedbacks suggests emissions of carbon dioxide will cause equilibrium (century time scale) surface warming to increase between 0.6 and 2.0 °C for every 1,000 PgC emitted when an equilibrium is approached between the atmosphere and the ocean over many centuries.

1. Introduction Climate change is driven by a combination of radiative forcing and climate feedbacks operating in the climate system (see review in Knutti et al., 2017). The climate feedback is usually expressed in terms of the change in surface temperature multiplied by a feedback parameter, \( \lambda \) in W·m\(^{-2}\)·K\(^{-1}\), defined in terms of a wide range of physical processes, including the Planck response of enhanced longwave emission from a warmer surface and physical feedbacks from changes in water vapor, lapse rate, cloud cover, and ice albedo (Andrews et al., 2012; Andrews et al., 2015; Armour et al., 2013; Ceppi & Gregory, 2017; Gregory et al., 2004). In contrast, the carbon cycle responses and feedbacks are usually defined in terms of how atmospheric carbon dioxide and temperature linearly combine to alter the carbon inventories of the climate system (Arora et al., 2013; Friedlingstein et al., 2003, 2006), which may be expressed in terms of a radiative feedback parameter in W·m\(^{-2}\)·K\(^{-1}\) (Gregory et al., 2009). However, there are difficulties in applying this carbon feedback method due to nonlinearities in how the separate atmospheric carbon dioxide and temperature effects combine together (Schwinger et al., 2014) giving rise to errors in the overall carbon feedback (Arora et al., 2013). This linearization method also cannot be used to calculate the carbon feedback directly from observational reconstructions of the carbon cycle (e.g., le Quéré et al., 2018), since there is no observational method to generate the hypothetical state with a range of feedback processes turned off for the real world.

The separation of forcing and feedback is dependent upon the nature of the climate perturbation. In climate model experiments driven by an imposed atmospheric CO\(_2\) trajectory, a radiative forcing is provided from the increase in atmospheric CO\(_2\) that automatically includes the effects of carbon cycle feedbacks. In
contrast, for climate model experiments driven by carbon emissions, a radiative forcing is provided from the increase in atmospheric CO2 directly caused by the carbon emission together with a radiative feedback from the change in atmospheric CO2 caused by changes in the terrestrial and ocean carbon reservoirs.

To understand this distinction between forcing and feedback, consider the response of a conceptual Earth system model to a pulse of carbon released to the atmosphere, which is partitioned between the atmosphere, ocean, and terrestrial systems (Figure 1a). The original carbon release drives a radiative forcing from the CO2 forcing from emissions without carbon feedbacks (red), plus the non-CO2 feedbacks (blue), and from the carbon feedbacks (light blue). (c) Total climate feedback, $\lambda_\text{Climate}$ (light blue line and shading), and (d) total carbon feedback, $\lambda_\text{Carbon}$ (light blue line and shading), both showing contributions from individual feedback processes (dashed lines and arrows). On all panels, lines show the ensemble median, dark shading is 66% range, and light shading is the 95% range.

Our aim is to define and evaluate a new feedback parameter for the carbon system that
1. takes into account the combined effects of the non-CO2 and CO2 feedbacks operating in the climate system, thus avoiding the need to make a linearizing assumption that introduces error;
2. allows direct comparison between magnitudes of, and uncertainties in, feedbacks in the climate and carbon systems; and
3. allows the practical application of real-world observational data to analyze carbon feedback.

2. Definition of a Climate and Carbon Feedback Parameter

Consider the global energy balance for a climate system perturbed from an initial steady state (e.g., Figures 1a and 1b). The radiative forcing perturbation, $\Delta R'$, from the original forcing perturbation combined with subsequent feedback terms is balanced by additional outgoing longwave radiation emitted due to surface warming, $\lambda_\text{Planck}\Delta T$, and the net Earth system heat uptake, $N$, all terms defined in W/m²,
\[ \Delta R' = \lambda_{\text{Planck}} \Delta T + N, \]  
\[ \text{(1)} \]

where \( \lambda_{\text{Planck}} \) is the Planck feedback parameter in W·m\(^{-2}\)·K\(^{-1}\) and \( \Delta T \) is the change in global-mean surface temperature in K. The radiative forcing, \( \Delta R' \), consists of an original forcing perturbation, \( \Delta R_{\text{forcing}} \) plus a subsequent feedback term, \( \Delta R_{\text{feedback}} \), \( \Delta R' = \Delta R_{\text{forcing}} + \Delta R_{\text{feedback}} \), and the feedback may be written in terms of the separate non-CO\(_2\) and CO\(_2\) components, \( \Delta R_{\text{non-CO}_2} \) and \( \Delta R_{\text{CO}_2} \), respectively (Figure 1b), such that

\[ \Delta R' = \Delta R_{\text{forcing}} + \Delta R_{\text{feedback}_{\text{non-CO}_2}} + \Delta R_{\text{feedback}_{\text{CO}_2}}. \]  
\[ \text{(2)} \]

The radiative feedback term from non-CO\(_2\) feedbacks, \( \Delta R_{\text{feedback}_{\text{non-CO}_2}} \), includes the effects of changes in water vapor, lapse rate, clouds, and surface albedo, while the radiative feedback term from CO\(_2\), \( \Delta R_{\text{feedback}_{\text{CO}_2}} \), includes how radiative forcing from atmospheric CO\(_2\) is altered by changes in the ocean and terrestrial carbon inventories.

The radiative response is often defined in terms of a climate feedback, \( \lambda_{\text{Climate}} \Delta T \) in W/m\(^2\), by combining the Planck response, \( \lambda_{\text{Planck}} \Delta T \), with the radiative forcing from non-CO\(_2\) feedbacks, \( \Delta R_{\text{feedback}_{\text{non-CO}_2}} \) (e.g., see Intergovernmental Panel on Climate Change, 2013; Knutti et al., 2017),

\[ \lambda_{\text{Climate}} \Delta T = \lambda_{\text{Planck}} \Delta T - \Delta R_{\text{feedback}_{\text{non-CO}_2}}, \]  
\[ \text{(3)} \]

such that the energy balance in (1) may be reexpressed from (2) and (3) by

\[ \Delta R_{\text{forcing}} + \Delta R_{\text{feedback}_{\text{CO}_2}} = \lambda_{\text{Planck}} \Delta T - \Delta R_{\text{feedback}_{\text{non-CO}_2}} + N = \lambda_{\text{Climate}} \Delta T + N. \]  
\[ \text{(4)} \]

The standard form of the climate feedback definition in (3) does not encapsulate the full sensitivity of the Earth system to perturbation, as the definition only accounts for the strength of the non-CO\(_2\) feedbacks in the system and ignores the impact of carbon cycle feedbacks, which are instead treated as part of the forcing perturbation in (4). Here, we reexpress the energy balance relations (1) and (4) using a new combined carbon plus climate feedback, \( \lambda_{\text{Climate}+\text{Carbon}} \) in W·m\(^{-2}\)·K\(^{-1}\), defined as the sum of the climate and carbon feedbacks,

\[ \lambda_{\text{Climate}+\text{Carbon}} \Delta T = \lambda_{\text{Planck}} \Delta T - \Delta R_{\text{feedback}_{\text{non-CO}_2}} - \Delta R_{\text{feedback}_{\text{CO}_2}} = (\lambda_{\text{Climate}} + \lambda_{\text{Carbon}}) \Delta T, \]  
\[ \text{(5)} \]

where \( \lambda_{\text{Carbon}} = -\Delta R_{\text{feedback}_{\text{CO}_2}} / \Delta T \). The energy balance in (1) may now be more explicitly written in terms of the original radiative forcing, \( \Delta R_{\text{forcing}} \), balancing the radiative response from the combined climate and carbon responses, \( \lambda_{\text{Climate}+\text{Carbon}} \Delta T \), plus the planetary heat uptake, \( N \), such that

\[ \Delta R_{\text{forcing}} = \lambda_{\text{Climate}} \Delta T - \Delta R_{\text{feedback}_{\text{CO}_2}} + N = \lambda_{\text{Climate}+\text{Carbon}} \Delta T + N. \]  
\[ \text{(6)} \]

To progress, we now wish to evaluate the carbon feedback \( \lambda_{\text{Carbon}} \) in terms of changes in ocean and terrestrial carbon inventories.

### 3. Extracting the Feedback Component to CO\(_2\) Change

A small carbon emission into a preindustrial state, \( \delta I_{\text{em}} \) in PgC, is distributed between the atmospheric, ocean, and terrestrial carbon reservoirs (Figure 1a),

\[ \delta I_{\text{em}} = \delta I_{\text{atmos}} + \delta I_{\text{ocean}} + \delta I_{\text{ter}} = M \delta C_{\text{CO}_2} + V \delta C_{\text{DIC}} + \delta I_{\text{ter}}, \]  
\[ \text{(7)} \]

where \( \delta I_{\text{atmos}} = M \delta C_{\text{CO}_2} \) is the change in atmospheric CO\(_2\) inventory since the preindustrial, with \( M \) the molar volume of the atmosphere and CO\(_2\) the atmospheric CO\(_2\) mixing ratio; \( \delta I_{\text{ocean}} = V \delta C_{\text{DIC}} \) is the change in ocean dissolved inorganic carbon (DIC) inventory, with \( V \) the ocean volume and \( C_{\text{DIC}} \) the mean ocean concentration of DIC; \( \delta I_{\text{ter}} \) is the change in terrestrial (soil + vegetation) carbon inventory; and the symbol \( \delta \) is used to indicate a small infinitesimal change since the preindustrial.
Radiative forcing is related to the log change in atmospheric CO$_2$, $R_{\text{CO}_2} = a \Delta \ln \text{CO}_2$ (Myhre et al., 2013), so our goal is to find an expression for the change in log CO$_2$ due to some initial carbon emission, $\delta I_{\text{em}}$, and subsequent responses to forcing and feedbacks within the atmosphere-ocean-terrestrial carbon system (7). The ocean inventory of carbon involves the DIC concentration $C_{\text{DIC}}$, which may be expressed as a sum of process-driven components (Goodwin et al., 2008; Ito & Follows, 2005; Williams & Follows, 2011) involving the DIC concentration at chemical saturation with atmospheric CO$_2$, $C_{\text{sat}}$; the disequilibrium concentration at subduction, $C_{\text{dis}}$; and the DIC contribution from regenerated biological material, $C_{\text{bio}}$ ($C_{\text{DIC}} = C_{\text{sat}} + C_{\text{dis}} + C_{\text{bio}}$; Appendix A). Applying this ocean partitioning allows the perturbation to the global carbon inventory (7) to be reexpressed as

$$\delta I_{\text{em}} = \left( I_{\text{atmos}} + \frac{VC_{\text{sat}}}{B} \right) \delta \ln \text{CO}_2 + V \left( \delta C_{\text{dis}} + \delta C_{\text{bio}} + \frac{\delta C_{\text{sat}}}{\delta A_{\text{pre}}} \delta A_{\text{pre}} + \frac{\partial C_{\text{sat}}}{\partial T_{\text{oc}}} \delta T_{\text{oc}} \right) + \delta I_{\text{ter}},$$

where $A_{\text{pre}}$ is the global mean ocean preformed titration alkalinity; $T_{\text{oc}}$ is the global mean ocean temperature; $B = \partial \ln \text{CO}_2/\partial \ln C_{\text{sat}}$ is the Revelle buffer factor of seawater; and $I_{\text{atmos}} + (VC_{\text{sat}}/B) = I_{\text{B}}$ is the buffered carbon inventory of the air-sea system (Goodwin et al., 2007, 2008, 2015).

Rearranging (8) for $\delta I_{\text{OC}}$, and integrating for large changes using a constant buffered carbon inventory approximation (Goodwin et al., 2007, 2008, 2009, 2011, 2015: Appendix), decomposes $\Delta R_{\text{CO}_2}$ into the initial response to forcing from anthropogenic carbon emissions in the absence of feedbacks, $\Delta R_{\text{forcing}}^{\text{feedback}}$, plus components from terrestrial and ocean carbon cycle feedbacks, $\Delta R_{\text{CO}_2} = \Delta R_{\text{feedback}}^{\text{terrestrial}} + \Delta R_{\text{feedback}}^{\text{ocean}}$ (Figures 1a and 1b), such that

$$\Delta R_{\text{CO}_2} = \Delta R_{\text{forcing}}^{\text{CO}_2} + \Delta R_{\text{feedback}}^{\text{CO}_2} = \Delta R_{\text{forcing}}^{\text{terrestrial}} + \Delta R_{\text{feedback}}^{\text{terrestrial}} + \Delta R_{\text{feedback}}^{\text{ocean}},$$

where $\Delta R_{\text{forcing}}^{\text{CO}_2}$ is related to terms involving the carbon emission $\Delta I_{\text{em}}$ and the change in ocean disequilibrium carbon $\Delta C_{\text{dis}}$ from (8); $\Delta R_{\text{feedback}}^{\text{terrestrial}}$ is related to the feedback from the change in the terrestrial carbon inventory; $\Delta I_{\text{ter}}$; and $\Delta R_{\text{feedback}}^{\text{ocean}}$ is related to the feedback from the changes in the ocean carbon inventory involving the saturated and regenerated carbon pools (8) from $\Delta C_{\text{bio}}$, $\Delta A_{\text{pre}}$, and $\Delta T_{\text{oc}}$ (Appendix A).

### 4. Evaluating Carbon Feedback From Observational Constraints and Numerical Simulations

#### 4.1. Terrestrial Carbon Feedback

The change in the radiative forcing, $\Delta R_{\text{feedback}}^{\text{terrestrial}}$, in (9), is related to the change in the cumulative terrestrial carbon inventory relative to the preindustrial, $\Delta I_{\text{ter}}$ in PgC (Figures 1a and 1b; Goodwin et al., 2007: 2008, 2009, 2011, 2015: Appendix A), which is given by

$$\Delta R_{\text{feedback}}^{\text{terrestrial}} = - \left( \frac{a}{I_{\text{B}}} \right) \Delta I_{\text{ter}}.$$

The terrestrial carbon feedback $\lambda_{\text{Carbon}}$ is diagnosed from reconstructions of the change in the terrestrial carbon inventory and surface temperature record by substituting (10) into (5),

$$\lambda_{\text{Carbon}} = - \frac{\Delta R_{\text{feedback}}^{\text{terrestrial}}}{\Delta T} = - \left( \frac{a}{I_{\text{B}}} \right) \frac{\Delta I_{\text{ter}}}{\Delta T}.$$

This new relation (11) is now used to quantify terrestrial carbon feedback from observational reconstructions and Earth system model simulations. $\lambda_{\text{Carbon}}$ is estimated using the following parameters: the radiative forcing coefficient from CO$_2$, $a = 5.35 \pm 0.27$ W/m$^2$ (Myhre et al., 2013); the buffered carbon inventory, $I_{\text{B}} = 3451 \pm 96$ PgC (Williams et al., 2017); the global-mean surface temperature change $\Delta T$ from the Goddard Institute for Space Studies (GISS) Surface Temperature Analysis (GISTEMP) temperature record (Hansen et al., 2010), including an 11-year average smoothing (Figure 2a, black dotted and full lines); and change in the terrestrial carbon inventory $\Delta I_{\text{ter}}$ from the Global Carbon Budget (le Quéré et al., 2018; Figure 2b, black). Uncertainties in the terrestrial carbon budget are taken from the additional data for the 16
individual dynamic global vegetation models (DGVMs) in the Global Carbon Budget (le Quéré et al., 2018; supporting information; Acknowledgments).

These historical reconstructions for the terrestrial carbon inventory and surface temperature reveal an observation-constrained estimate of the terrestrial carbon feedback parameter, \( \lambda_{\text{Carbon}} = 0.33 \pm 0.09 \text{ W} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \) for the present day (Figure 2c, black line and shading), which represents a negative feedback that reduces global warming through terrestrial carbon uptake. The strength of this negative feedback reached a peak magnitude of \( \lambda_{\text{Carbon}} = 0.86 \pm 0.34 \text{ W} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \) in the late 1960s but then has decreased in time as the rate of increase in surface warming since the early 1970s (Figure 2a, black) (Hansen et al., 2010) has not matched the rate of increase in the cumulative terrestrial carbon sink (Figure 2b, black; le Quéré et al., 2018).

The terrestrial carbon feedback is now evaluated from four Coupled Model Intercomparison Project Phase 5 (CMIP5) Earth system models (CanESM2, HadGEM2-ES, HadGEM2-CC, and NorESM-ME), chosen as these have a reliable net export production (nep) variable allowing calculation of \( \Delta I_{\text{ter}} \) in (11). From the simulated \( \Delta I_{\text{ter}} \) and 11-year average \( \Delta T \) (Figures 2a and 2b), and estimates of \( a \) and \( I_B \) for each model (Williams et al., 2017), \( \lambda_{\text{Carbon}} \) is evaluated from years 1959 to 2100 for the Representative Concentration Pathway 4.5 (RCP4.5) scenario (Figure 2c; Meinshausen et al., 2011). These four CMIP5 Earth system models have a smaller present-day terrestrial carbon feedback parameter ranging from 0.02 to 0.65 W·m\(^{-2}\)·K\(^{-1}\), broader than the 1σ range from observational reconstructions (Figure 2c, compare dashed lines to black line and shading). These differences between the Earth system models and the observational estimate arise from...
their discrepancy between the modeled and observational reconstructions of surface warming and terrestrial carbon uptake (Figures 2a and 2b). The future simulated $\lambda_{\text{Carbon}}$ remains stable under the RCP4.5 scenario, remaining close to the present-day values to year 2100 (Figure 2c).

Additional projections of carbon feedback are made using a very large ensemble of observation-constrained simulations from the Warming Acidification and Sea level Projector (WASP; Goodwin, 2016), for the RCP4.5 scenario (Figure 2, blue line and shading). We adopt the WASP model configuration of Goodwin (2018), with climate feedback including components from different processes operating on different response time scales (Figure 1). An ensemble is generated of many thousands of observation-consistent simulations using the Monte Carlo plus history matching (Williamson et al., 2015) methodology of Goodwin et al. (2018). First, the initial ensemble of 10 million Monte Carlo simulations is generated as in Goodwin (2018), with varied model input parameters, and we integrate each simulation from years 1765 to 2017 with historical forcing. Next the observation-consistency test of Goodwin (2018; see Table 2 therein) is applied with an updated terrestrial carbon range (supporting information Table S1) based on the 16 observation-consistent DGVMs of the Global Carbon Budget 2018 (le Quéré et al., 2018). Only 6,273 simulations pass the observation-consistency test, and a further 3 simulations are rejected as nonphysical since $\lambda_{\text{Climate}}$ becomes negative on long time scales.

The remaining ensemble of 6,270 WASP simulations are then consistent with historic observations of surface warming (Figure 2a, compare blue to black), terrestrial carbon uptake (Figure 2b, compare blue to black), and ocean heat content changes (supporting information Table S1; Goodwin, 2018). Due to the observation-simulation agreement in $\Delta T$ and $\Delta I_{\text{ter}}$, the final WASP ensemble is also in good agreement with the observational reconstructions of terrestrial $\lambda_{\text{Carbon}}$ using (11) from years 1959 to 2017 (Figure 2c, compare blue to black). Under the RCP4.5 scenario, the observation-constrained WASP ensemble shows a similar future behavior as in the response of the CMIP5 models (Figure 2c, compare blue solid line and shading to dashed lines), with $\lambda_{\text{Carbon}}$ displaying only a small change in magnitude from the present day to year 2100.

### 4.2. Ocean Carbon Feedback

In a similar manner to how the terrestrial carbon feedback is defined relative to $\Delta I_{\text{ter}}$ (11), the ocean carbon feedback is defined in relation to changes in the ocean DIC from regenerated carbon, $\Delta C_{\text{bio}}$, and changes in the ocean saturated carbon inventory from preformed alkalinity $\Delta A_{\text{pre}}$ and ocean temperature $\Delta T_{\text{oc}}$ (equations 8 and A8), via

$$\lambda_{\text{Carbon}} = \frac{\Delta A_{\text{feedback}}}{\Delta T} = -\left(\frac{a}{I_{\beta}}\right) \frac{\Delta C_{\text{bio}} + (\partial C_{\text{sat}}/\partial A_{\text{pre}})\Delta A_{\text{pre}} + (\partial C_{\text{sat}}/\partial T_{\text{oc}})\Delta T_{\text{oc}}}{\Delta T}. \quad (12)$$

This ocean feedback term represents how changes in ocean temperature and ocean biological cycling of carbon and alkalinity from an initial carbon perturbation then feed back to alter the radiative forcing from atmospheric CO$_2$. Based on Earth system models (evaluating $\Delta C_{\text{bio}}$, $\Delta A_{\text{pre}}$, and $\Delta T_{\text{oc}}$), observational reconstructions for ocean heat uptake (Cheng et al., 2017), and the WASP ensemble (both evaluating $\Delta T_{\text{oc}}$ only), the ocean carbon feedback is diagnosed as being much smaller than the terrestrial carbon feedback in the present day, ranging from −0.015 to 0.06 W·m$^{-2}$·K$^{-1}$ (Figures 2c and 2d), and remains small for the 21st century. The magnitude of the ocean carbon feedback might though increase beyond year 2100 due to continued climate-driven changes in ocean temperature, $\Delta T_{\text{oc}}$, and ocean biological carbon drawdown, $\Delta C_{\text{bio}}$.

Our estimate of ocean carbon feedback (Figure 2d) is much smaller than that implied by Gregory et al. (2009) because the previous approach (Friedlingstein et al., 2006) considers the transient disequilibrium of ocean DIC, $C_{\text{dis}}$ (eq. 8), to be part of the ocean carbon feedback, while our method considers $C_{\text{dis}}$ as part of the transient ocean response. An idealized feedback grows in magnitude over time, from zero the instant a forcing is applied to some final equilibrium value on long timescales. We do not consider $C_{\text{dis}}$ part of the ocean carbon feedback because the time evolution of $C_{\text{dis}}$ is the opposite sense: Ocean CO$_2$ disequilibrium is large the instant CO$_2$ is emitted into the atmosphere and then decays to zero over long time scales due to ocean carbon uptake (supporting information Figure S1).
5. Estimating the Combined Carbon-Climate Feedback and Sensitivity

We now place observational constraints on the combined climate plus carbon feedback, $\lambda_{\text{Climate+Carbon}}$, and sensitivity, $S_{\text{Climate+Carbon}}$ in K/(W/m²), by evaluating both $\lambda_{\text{Climate}}$ and $\lambda_{\text{Carbon}}$ for an idealized perturbation experiment in the observation-constrained WASP ensemble. Each of the 6,270 observation-consistent WASP ensemble members (Figure 2, blue line and shading) is reinitialized at a preindustrial spin-up and integrated for 500 years, forced with an idealized scenario consisting of a 1,000 PgC emission over the first 100 years (Figure 1a).

The total radiative forcing $\Delta R'$ is decomposed into the initial emission forcing, $\Delta R_{\text{CO}_2}^{\text{forcing}}$, non-CO₂ feedback, $\Delta R_{\text{non-CO}_2}^{\text{feedback}}$, and CO₂ feedback, $\Delta R_{\text{CO}_2}^{\text{feedback}}$, terms (Figure 1b) using equations (1)–(6). From this decomposition, $\lambda_{\text{Climate}}$ and $\lambda_{\text{Carbon}}$ (Figures 1c ans 1d) are evaluated over multiple response time scales in the observation-consistent ensemble, where the $\lambda_{\text{Climate}}$ results are comparable to the similarly constrained ensemble in Goodwin (2018; see Figure 2 therein). Here $\lambda_{\text{Carbon}}$ in WASP includes both the larger...
terrestrial and smaller ocean temperature-CO$_2$ solubility effects (Figure 1d), but WASP does not simulate changes in $C_{bio}$ which remain small in Earth system models (Figure 2d). For illustration purposes, $\lambda_{\text{Climate}}$ and $\lambda_{\text{Carbon}}$ contributions from individual processes are shown by integrating the WASP ensemble with combinations of feedback processes switched off (Figures 1c and 1d, dashed lines are ensemble median values).

Estimates of the carbon and climate feedback parameters, $\lambda_{\text{Carbon}}$ and $\lambda_{\text{Climate}}$, applicable on century time scales, are made from the observation-consistent ensemble distributions at the end of the 1,000-PgC emission simulations (Figure 1). The 500-year carbon feedback after a 1,000-PgC emission has a median (and 95% range) of $\lambda_{\text{Carbon}} = 0.21$ (−0.02 to 0.5) W·m$^{-2}$·K$^{-1}$ (Figure 1c), while the physical climate feedback after a 1,000-PgC emission is $\lambda_{\text{Climate}} = 1.27$ (0.73 to 1.88) W·m$^{-2}$·K$^{-1}$ (Figures 1b and 3a, blue).

The impact of carbon feedbacks is therefore to increase the overall carbon plus climate feedback above $\lambda_{\text{Climate}}$, with an observation-constrained distribution of $\lambda_{\text{Climate+Carbon}} = \lambda_{\text{Carbon}} + \lambda_{\text{Climate}} = 1.48$ (0.76 to 2.32) W·m$^{-2}$·K$^{-1}$ (Figure 3a). Consequently, the climate sensitivity, $S = 1/\lambda_{\text{Climate}}$, from non-CO$_2$ feedbacks alone, $S_{\text{Climate}} = 0.79$ (0.53 to 1.37) K/(W/m$^2$), is reduced to $S_{\text{Climate+Carbon}} = 0.67$ (0.43 to 1.32) K/(W/m$^2$), when encapsulating both non-CO$_2$ and CO$_2$ feedbacks acting together (Figure 3b). This estimate of $S_{\text{Climate+Carbon}}$ (Figure 3b, black) represents the total sensitivity of the climate system to perturbation by carbon emission over century time scales, including both physical climate and carbon-cycle feedbacks.

### 6. Conclusions

A new method is presented to constrain the carbon feedback parameter, finding for the present-day terrestrial carbon system $\lambda_{\text{Carbon}} = 0.33 \pm 0.09$ W·m$^{-2}$·K$^{-1}$ (Figure 2c) based on observational reconstructions of carbon uptake and warming (Hansen et al., 2010; le Quéré et al., 2018) and $\lambda_{\text{Carbon}} = 0.02$ to 0.65 W·m$^{-2}$·K$^{-1}$ in four CMIP5 models. This compares to a previous method implying terrestrial carbon feedback of $\lambda_{\text{Carbon}} = 0.72^{±0.5}$ W·m$^{-2}$·K$^{-1}$, based on analysis of the earlier Coupled Climate-Carbon Cycle Model Intercomparison Project (C4MIP) climate model ensemble (Arnell et al., 2010; Friedlingstein et al., 2006; Gregory et al., 2009) and comprising a linearization of separate CO$_2$-carbon (1.1 ± 0.5 W·m$^{-2}$·K$^{-1}$) and climate-carbon (−0.4 ± 0.2 W·m$^{-2}$·K$^{-1}$) components. The linearization assumed by the previous method introduces errors (Arora et al., 2013; Schwinger et al., 2014), and this means the method cannot be applied to observational reconstructions. To avoid making the linearization assumption, and so be applicable to observational reconstructions, our method assumes a constant buffered carbon inventory (Appendix A), a good approximation for carbon perturbations up to ~5,000 PgC or for atmospheric CO$_2$ reaching ~1,100 ppm (Goodwin et al., 2007, 2008, 2009).

The Equilibrium Climate Response to Emission (ECRE), in K/1,000 PgC, expresses the warming per unit carbon emitted once ocean heat uptake approaches zero over centennial to multicentennial time scales, ECRE = $\Delta T / \Delta I_{\text{em}}$ (Frölicher & Paynter, 2015). This atmosphere-ocean equilibrium is approached over many centuries, but not necessarily reached due to the effect of other longer time scale carbon and climate feedbacks, such as ice sheet-albedo feedbacks (Rohling et al., 2018) and multimillennial CaCO$_3$ sediment and weathering responses (Archer, 2005). In the absence of carbon feedbacks, Williams et al. (2012) related the ECRE to climate feedback, $\lambda_{\text{Climate}}$, via ECRE = $a/(\lambda_{\text{Climate}}I_{\text{em}})$. Here we extend the relationship to include the effects of both climate and carbon feedbacks, ECRE = $a/(\lambda_{\text{Climate+Carbon}}I_{\text{em}})$, applicable after ocean CO$_2$ invasion and heat uptake but prior to significant CaCO$_3$ sediment and weathering responses (Archer, 2005; Goodwin et al., 2007, 2008, 2015). Our historically constrained feedback estimates (Figures 3a and 3b) imply ECRE = 1.0 (0.6 to 2.0) K/1,000 PgC emitted (Figure 3c), with the upper half of our range (from 1 to 2 K/1,000 PgC) consistent with a CMIP5-based estimate (Frölicher & Paynter, 2015). Carbon and climate feedbacks not constrained historically (e.g., MacDougall & Knutti, 2016; Pugh et al., 2018; Rohling et al., 2018; Zickfeld et al., 2013) may alter future $\lambda_{\text{Climate+Carbon}}$ and so alter ECRE. We anticipate this relationship, ECRE = $a/(\lambda_{\text{Climate+Carbon}}I_{\text{em}})$, will be useful in elucidating how different carbon and climate feedbacks contribute to the multicentury warming response to carbon emission.
Appendix A: Connecting Radiative Feedbacks to Changes in Carbon Inventories

Our aim is to separate the total CO$_2$ radiative forcing into a sum of linearly separable terms representing different processes and feedbacks. We start by considering how carbon emissions perturb carbon storage across the atmosphere-ocean-terrestrial system. We now write identities for the changes in atmospheric and ocean carbon inventories containing terms with $\delta$ln CO$_2$. Using the identity for small perturbations in $x$, $\delta x = x \delta \ln x$, we write an identity for a small perturbation in atmospheric CO$_2$ inventory, $\delta$I$_{\text{atmos}}$, in terms of a small perturbation to the logarithm of atmospheric CO$_2$, $\delta$ln CO$_2$, where $I_{\text{atmos}}$ is the initial atmospheric CO$_2$ inventory at the unperturbed preindustrial state.

\[ \delta I_{\text{atmos}} = I_{\text{atmos}} \delta \ln \text{CO}_2, \]  

(A1)

The change in ocean DIC is considered, via a process-driven viewpoint (Goodwin et al., 2008; Ito & Follows, 2005; Williams & Follows, 2011), in terms of the sum of components from the change in chemically saturated DIC arising from changes in atmospheric CO$_2$ and seawater properties, $\delta$C$_{\text{sat}}$; the change in chemical disequilibrium of ocean DIC relative to atmospheric CO$_2$, $\delta$C$_{\text{dis}}$; and the combined change in ocean DIC from regenerated soft tissue and CaCO$_3$ drawdown, $\delta$C$_{\text{bio}}$:

\[ \delta C_{\text{DIC}} = \delta C_{\text{sat}} + \delta C_{\text{dis}} + \delta C_{\text{bio}}. \]  

(A2)

Due to the carbonate chemistry system, the perturbation to $C_{\text{sat}}$ is a function of the change to the logarithm of atmospheric CO$_2$, $\delta$ln CO$_2$; the change in mean ocean preformed titration alkalinity, $\delta$A$_{\text{pre}}$; the change in mean seawater temperature, $\delta$T$_{\text{oc}}$; and the change in mean seawater salinity, $\delta$S:

\[ \delta C_{\text{sat}} = \delta C_{\text{sat}}(\delta \ln \text{CO}_2, \delta A_{\text{pre}}, \delta T_{\text{oc}}, \delta S). \]  

This small perturbation to $C_{\text{sat}}$ is now expanded after Goodwin and Lenton (2009) into components from $\delta$ln CO$_2$, $\delta$A$_{\text{pre}}$, $\delta$T$_{\text{oc}}$, and $\delta$S:

\[ \delta C_{\text{dis}} = \frac{\partial C_{\text{sat}}}{\partial \ln \text{CO}_2} \delta \ln \text{CO}_2 + \frac{\partial C_{\text{sat}}}{\partial A_{\text{pre}}} \delta A_{\text{pre}} + \frac{\partial C_{\text{sat}}}{\partial T_{\text{oc}}} \delta T_{\text{oc}} + \frac{\partial C_{\text{sat}}}{\partial S} \delta S, \]  

(A3)

where the salinity term, $(\partial C_{\text{sat}}/\partial S)\delta S$, is small and henceforth will be omitted. Again, using the identity for small perturbations in a variable $x$, $\delta x = x \delta \ln x$, but applying to $C_{\text{sat}}$, the term for the sensitivity of $C_{\text{sat}}$ to ln CO$_2$ in (A3) becomes

\[ \frac{\partial C_{\text{sat}}}{\partial \ln \text{CO}_2} \delta \ln \text{CO}_2 = C_{\text{sat}} \frac{\partial \ln C_{\text{sat}}}{\partial \ln \text{CO}_2} \delta \ln \text{CO}_2 = \frac{C_{\text{sat}}}{B} \delta \ln \text{CO}_2, \]  

(A4)

where $B = (\delta \ln \text{CO}_2/\delta \ln C_{\text{sat}})$ is the Revelle buffer factor expressing how fractional chemical in atmospheric CO$_2$ is much larger than fractional changes in DIC with B, the order 10 for the present ocean (e.g., Williams & Follows, 2011). Substituting (A4) into (A3), and noting that $I_{\text{ocean}} = V C_{\text{DIC}}$, produces an identity for $\delta I_{\text{ocean}}$ containing a term in $\delta$ln CO$_2$:

\[ \delta I_{\text{ocean}} = \frac{r_{\text{ocean}}}{B} \delta \ln \text{CO}_2 + V \left( \delta C_{\text{dis}} + \delta C_{\text{bio}} + \frac{\partial C_{\text{sat}}}{\partial A_{\text{pre}}} \delta A_{\text{pre}} + \frac{\partial C_{\text{sat}}}{\partial T_{\text{oc}}} \delta T_{\text{oc}} \right), \]  

(A5)

where $r_{\text{ocean}} = V C_{\text{sat}}$ is the ocean inventory of saturated DIC at current atmospheric CO$_2$. Substituting $\delta I_{\text{ocean}}$ (A5) and $\delta I_{\text{atmos}}$ (A1) into (7), and rearranging to solve for the log change in atmospheric CO$_2$ mixing ratio to small perturbations to $I_{\text{em}}$, $I_{\text{ter}}$, $C_{\text{dis}}$, $C_{\text{bio}}$, $A_{\text{pre}}$, and $T_{\text{oc}}$ reveals

\[ \left( I_{\text{atmos}} + \frac{r_{\text{ocean}}}{B} \right) \delta \ln \text{CO}_2 = \delta I_{\text{em}} - \delta I_{\text{ter}} - V \left( \delta C_{\text{dis}} + \delta C_{\text{bio}} + \frac{\partial C_{\text{sat}}}{\partial A_{\text{pre}}} \delta A_{\text{pre}} + \frac{\partial C_{\text{sat}}}{\partial T_{\text{oc}}} \delta T_{\text{oc}} \right). \]  

(A6)

The issue now is that this identity for $\delta$ln CO$_2$ (A7) applies only to small infinitesimal perturbations, and we wish to solve for the change in log CO$_2$ for large finite perturbations. The next step is therefore to integrate (A6) over large finite perturbations in $I_{\text{em}}$, $I_{\text{ter}}$, $C_{\text{dis}}$, $C_{\text{bio}}$, $A_{\text{pre}}$, and $T_{\text{oc}}$.

To integrate (A6), we note that the left-hand side contains the buffered carbon inventory, $I_B$ (Goodwin et al., 2007, 2008), defined as the atmospheric carbon inventory added to the ocean saturated-DIC inventory.
divided by the Revelle buffer factor, $I_B = I_{\text{atmos}} + \left( \frac{\text{nat}}{\text{ocean}} / B \right)$. $I_B$ represents the total buffered CO$_2$ and DIC in the atmosphere-ocean system that is available for redistribution between the CO$_2$ and carbonate ion pools (Goodwin et al., 2009), given that the majority of ocean DIC is in the form of bicarbonate ions. At the pre-industrial state, $I_B = 3,451 \pm 96$ PgC in the CMIP5 models analyzed by Williams et al. (2017).

Using this constant buffered carbon inventory approach (supporting information), we integrate (A6) to find the change in atmospheric CO$_2$ for large finite perturbations to total carbon emitted, $\Delta I_{\text{atmos}}$, the change in terrestrial carbon storage, $\Delta I_{\text{ter}}$, and the large changes in mean ocean values of $\Delta C_{\text{dis}}, \Delta C_{\text{bio}}, \Delta A_{\text{pre}}, \Delta T_{\text{oc}}$, so that

$$I_B \delta \ln \text{CO}_2 = \Delta I_{\text{em}} - \Delta I_{\text{ter}} - V \left( \Delta C_{\text{dis}} + \Delta C_{\text{bio}} + \frac{\delta C_{\text{sat}}}{\delta A_{\text{pre}}} \Delta A_{\text{pre}} + \frac{\delta C_{\text{sat}}}{\delta T_{\text{oc}}} \Delta T_{\text{oc}} \right).$$  \hspace{1cm} (A7)

Multiplying (A7) by the CO$_2$-radiative forcing coefficient, $a$, produces an expression for the radiative forcing from CO$_2$ in (9),

$$\Delta R_{\text{CO}_2} = \Delta R_{\text{CO}_2}^\text{forcing} = (a/I_B) \left( \frac{\delta I_{\text{em}}}{V} \Delta C_{\text{dis}} \right),$$  \hspace{1cm} (A8a)

as a sum of separable terms representing different processes, each linked to a different change in a carbon inventory. The CO$_2$ radiative forcing,

$$\Delta R_{\text{feedback}}^\text{terrestrial} = -(a/I_B) \Delta I_{\text{ter}},$$  \hspace{1cm} (A8b)

depends on the change in terrestrial carbon storage since the preindustrial, and that for the ocean,

$$\Delta R_{\text{feedback}}^\text{ocean} = -(a/I_B) V \left( \frac{\delta C_{\text{bio}}}{\delta A_{\text{pre}}} \Delta A_{\text{pre}} + \frac{\delta C_{\text{sat}}}{\delta T_{\text{oc}}} \Delta T_{\text{oc}} \right),$$  \hspace{1cm} (A8c)

depends on the changes to the ocean biological drawdown of soft tissue and CaCO$_3$, including the titration alkalinity effects, and on the changes in the seawater temperature since the preindustrial, altering the solubility of CO$_2$ in seawater.

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