Breakdown at Multiple Protrusions in SF$_6$ and CO$_2$

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Abstract: The electric breakdown at single and multiple protrusions in SF$_6$ and CO$_2$ is investigated at 0.4 and 0.6 MPa, respectively. Additionally, the breakdown fields at rough surfaces of two different areas were determined. From the measurements, breakdown probability distributions for single protrusions were determined and fitted by Weibull distributions. This allowed the determination of statistical enlargement laws for the 50% breakdown probability fields $E_{50}$. Such enlargement laws describe, for example, the scaling of breakdown field with electrode area or number of protrusions. The predictions were compared to the experimental data, and both agreement and discrepancies were observed depending on polarity and number of protrusions and gas. Discharge predictions including first electron, streamer inception and crossing, as well as leader propagation, gave further insight to this. It was found that predictions from enlargement laws based on statistical processes may not describe the measured breakdown fields well and that relevant physical breakdown criteria must also be considered.

Keywords: Gaseous breakdown; SF$_6$; CO$_2$; surface roughness; statistical enlargement laws

1. Introduction

Gaseous insulation is used in many high voltage applications as, for example, gas-insulated switchgear (GIS) and circuit breakers (CB) [1–6]. For compact insulation compressed gas in the pressure range of 0.13–1 MPa is used. In most applications today, SF$_6$ is used; however, it is a strong greenhouse gas (e.g., [7,8]). Therefore, the search for alternative insulation gases has significantly increased during the last years. The most promising gas in HV switchgear applications for replacing SF$_6$ is CO$_2$, which is used in mixtures with low-additive concentrations of, e.g., O$_2$, Perfluoroketones (PFK) or Perfluoronitriles (PFN) [8–12]. The additive concentrations are typically in the range of a few percent due to boiling point requirements. This will be referred to as CO$_2$-based insulation.

Gaseous insulation strength depends on the critical field of the gas [2,5,6], the field at which ionization leads to multiplication of electrons within an avalanche. This is determined by the zero crossing of the effective ionization coefficient, which is specific for a gas. The slope of the effective ionization coefficient determines the sensitivity of the insulation system to the surface imperfections [13–24]. Thus, depending on the properties of the gases, the insulation performance is determined not only by the critical field of the gas but also by imperfections like surface roughness or particulate contamination. This is especially more pronounced at higher pressures of 0.7 to 1 MPa, which is the preferred pressure range for CO$_2$-based insulation [25–33]. Since CO$_2$ is the base gas in these mixtures, a good understanding of the insulation characteristics of CO$_2$ at conditions of practical applications is needed.

Several investigations addressed the effect of electrode surface roughness and representations of those by single or multiple protrusions in SF$_6$—see [14,16–18,21]. Single-protrusion models have
shown reasonable agreement with measurements when taking into account the availability of a start electron for an avalanche, streamer inception and leader propagation [34–38]. Surface roughness and the effect of insulating coatings in SF₆ have been investigated experimentally by [23,24].

CO₂-based insulation is still less investigated than SF₆, and investigations with fluorinated additives to CO₂ just recently appeared. The effect of surface roughness and protrusions in pure CO₂ was investigated by [29–31] and [32,33,36,37], respectively. Breakdown at surfaces in CO₂-PFK and CO₂-PFN mixtures is reviewed in [8–10]. The effect of surface roughness at pressures above 1 MPa was investigated, e.g., by [27,36]. Breakdown at single protrusions in CO₂ was investigated by [37], showing that streamer propagation, in contrast to SF₆, also plays an important role for the breakdown in practical configurations, like in the presence of particulate contamination.

Several investigations addressed the effect of enlargement laws, i.e., the reduction of the breakdown field by the size of the electrode area or volume and time laws—see [5,6,13,39]. A theoretical investigation on approximation of surface roughness by an array of multiple protrusions was done by [40]. In this investigation, the surface roughness was approximated by multiple protrusions of given length and with hemispherical tip. The influence of the distance between protrusions was also addressed. Application of discharge inception and breakdown criteria based on start electron, streamer inception and leader inception were used to estimate breakdown fields for such arrays.

The previous investigations have shown that there is still only limited understanding how to describe the surface roughness induced breakdown fields by single and multiple protrusions, especially when considering the surface area and time scaling effects. Therefore, measurements are still needed to characterize breakdown fields in practical applications as, e.g., shown in [5,27,29,34]. It would be desirable to have models for surface roughness or protrusion/particle induced breakdown which can, for arbitrary gases, electrode size and number of protrusions, describe the breakdown fields sufficiently reliable. The present investigation addresses this in a first step by measuring breakdown fields at single and multiple protrusions for short duration voltage waveform, which is similar to Lightning Impulse (LI) in standard testing according to IEC [6]. This procedure is similar to the theoretical study of [40]. Investigation of different gases in this study allows for understanding the differences between strongly attaching (SF₆) and weakly attaching (CO₂) gases. A novel test setup with a multiple protrusion array in a uniform background field is used and fill pressures of 0.4 MPa SF₆ and 0.6 MPa CO₂ are tested. The protrusion lengths are varied between 50 µm and 2 mm. The number of protrusions is varied between 1 and 100. Protrusions of small lengths of a few 10 to few 100 µm correspond to the surface roughness, whereas long protrusions of more than 500 µm correspond to particulate contamination or severe surface damages [35]. The effect of the number of protrusions, i.e., the statistical enlargement law, is addressed by scaling of the measured breakdown probability distributions using Weibull approximations—see [6,39,41,42]. This allows the validity of enlargement laws for such well-defined situations to be checked. Further insight is obtained by comparison to theoretical discharge inception and breakdown models based on start electron, streamer inception and streamer and leader propagation from [34–38]. Additionally, the surface area scaling is investigated experimentally on rough electrodes of similar surface structure. Results are interpreted with the findings from the protrusion arrays.

Section 2 shows the experimental setups and Section 3 presents the results. Discussion and conclusion are given in Section 4.

2. Test Setups

2.1. Test Circuit and Protrusion Setup

The experiments and the analysis were performed at Hitachi ABB Power Grids Research, Switzerland. The setup is shown schematically in Figure 1. It is a similar setup as used in previous investigations where the partial discharges and breakdown at a single protrusion was investigated [37,38]. In the present investigation, the plate electrode with the protrusion on the ground side was replaced by a plate with a protrusion array. The protrusion array plate had 20 × 20 holes of 1.2 mm
diameter and 2 mm center to center spacing—see Figure 2a. The protrusions were at ground potential. When we refer to polarity in the following always the polarity of the protrusions is meant.

![Schematic setup with a single protrusion](image)

**Figure 1.** Schematic setup with a single protrusion. The gap length was \( D = 10 \) or 15 mm. The load capacitance was charged via a Van de Graaf (VdG) DC source and switched via a resistor and closing switch onto the test gap. The discharges were observed by a high-resolution digital camera (Nikon D9000).

![Protrusion array](image)

(a) Protrusion array with 100 protrusions. (b) Protrusion tip details.

In the shown case in Figure 2a, 100 protrusions were inserted, but also fewer protrusions were tested. The protrusions were fixed to a matching grid by a magnet on a table below the perforated plate. The matching grid was moved by a stepper motor (Thorlabs GmbH, Bergkirchen, Germany, Model ZFS13B) with high positioning accuracy (<1 \( \mu \)m). The setup was placed, as in previous experiments, in a GIS test vessel filled with 0.4 MPa \( \text{SF}_6 \) or 0.6 MPa \( \text{CO}_2 \). With the stepper motor the protrusion lengths could be adjusted from outside, i.e., without opening the GIS. The overall reproducibility of the length adjustment was experimentally determined to be better than 20 \( \mu \)m for a single protrusion. In experiments with several protrusions, the total variation of lengths was less than 100 \( \mu \)m.

The protrusions were made out of steel with diameter 1 mm and had a conical tip of 1.6–1.7 mm length and tip radius of 66 \( \mu \)m at its end, marked by the yellow circle—see Figure 2b. The spacing between the protrusions was usually 4 mm. Only for \( \text{CO}_2 \) when using 20 protrusions also a spacing of 2 mm was tested. The protrusions were replaced regularly, typically after a few hundred tests. The effect of erosion was checked by repeating experiments in new and worn conditions. The differences in the breakdown voltages due to this were within the uncertainties of protrusion lengths adjustments, i.e., repeating experiments with the same protrusion in new condition led to a similar breakdown voltage as in worn condition.

The applied voltage was a stepped DC pulse, as used in [37,38], with a rise time of 200 ns and voltage application time of 15 s, typically. In experiments with multiple protrusions, the voltage dropped due to partial discharges after a few 10 \( \mu \)s; thus, we focused on early breakdowns in the
time range from the voltage peak to 10 μs after the peak was reached. From the time to breakdown, this can be associated with standard lightning impulse (LI) breakdown.

The applied voltage peak was varied over a wide range in order to obtain breakdown and withstand values. Typically, at least 100 tests were done per case. Between the tests, a small bias voltage of 20 kV was applied for 2 s to remove remaining ions from the gap, which could influence the start electron statistics. Thus, in the present investigation we determine breakdown fields at protrusions which can be related to LI standard wave shape. For small protrusion size in the order of 100 μm, breakdown also occurred at the plate electrode, e.g., at dust particles. With a single-shot digital camera (see Figure 1), it was checked that only breakdowns that occurred at a protrusion were taken into consideration.

2.2. Electrodes With Surface Roughness

Two different electrode types were tested: a small plug-type contact of 19 mm diameter, as seen in Figure 3, and a larger Rogowski-shaped electrode of 120 mm diameter. The electrodes were placed against a plate electrode, as in setup 1 with a 10 mm gap. Both electrodes were made from stainless steel and were sandblasted with Corundum white grains, resulting in a surface roughness of $R_z = 5–7 \, \mu m$ and $R_t = 62–65 \, \mu m$ with the average roughness $R_a = \frac{1}{L} \int |z(x)| \, dx$ over the sampling length $L$ of the contour $z(x)$ and the mean peak-to-valley height $R_z = \frac{1}{N} \sum_{i=1}^{N} R_{z,i}$ over an assessment length consisting of various sampling sections with the maximum peak to valley height $R_0$ within each section; see [43] for details. The surface roughness was determined by a non-contacting 3D profilometer Hyperion Compact from OPM. The effective area of the electrodes exposed to the electric field was about 240 and 6450 mm$^2$, respectively. This effective field exposed area was determined from the location of the breakdown marks after test, as can be, e.g., judged from the photographs in Figure 3 for the plug-type contact. For the plug-type contact, the field enhancement factor was calculated to be 1.42.

![Figure 3](image_url)

**Figure 3.** Plug-type contact with diameter 19 and 10 mm length in new (right) and worn condition after test (left). The surface has a biradial shape with a radius of 5 mm at the side and 20 mm at the tip, respectively.

3. Evaluation Procedures

3.1. Breakdown Probability Distributions

From the recorded breakdown fields, the empirical cumulative breakdown probability distributions were determined by the Turnbull algorithm [44] and fitted with three-parameter Weibull distributions [41] as proposed in [6,42]. The zero crossing $E_0$ of the Weibull distribution was set to the streamer inception field, calculated for each protrusion length as will be described below in Section 3.2.2. From the distributions, the 50% BD probability field $E_{50}$ and the standard deviation $\sigma$ was determined. Note that these values refer to the background field, i.e., $E_{50} = U_{50}/D$ with 50%
breakdown probability voltage $U_{50}$ and the gap length $D$. Generally, for the identical protrusions of $m$, the enlargement law based on the Weibull distributions generally follows from [6]

$$p(E) = 1 - e^{-m \left[ \frac{E - E_0}{E_{63} - E_0} \right]^\gamma}$$

(1)

With the shape parameter $\gamma$ and the 63% breakdown probability field $E_{63}$. In the present case for $\gamma$ and $E_{63}$ the values from the fits to the empirical cumulative breakdown probability distributions were used. An example of the enlargement scaling is shown in Figure 4. With increasing number of protrusions, the breakdown probability distribution becomes steeper and shifts towards $E_{63}$. Note, that such scaling is purely a statistical process and does not necessarily describe the scaling of any physical processes. This can be interpreted as follows: if the breakdown probability distribution follows the scaling from (1), it can be expected that the underlying processes are of statistical nature, e.g., by the availability of a first electron to start an avalanche. For electrodes with surface roughness, $m$ is the ratio of the surface areas.

![Figure 4](image)

Figure 4. Example of Weibull distributions for increasing number of protrusions $m$. In this example, $E_{63} = 250$ kV/cm, $E_0 = 100$ kV/cm, $\gamma = 7$ was chosen arbitrarily.

3.2. Discharge Inception and Breakdown Models

In the following subsections, models for the description of first electron, streamer inception and leader propagation will be described. The models are the same as presented in [38] for SF$_6$ and will only be briefly summarized here with the specific adaptations for CO$_2$. For these models, the decay of the electric field at the protrusion and at the electrode surface is needed. The field enhancement in the axis of symmetry in front of a protrusion was calculated by a multipole approximation

$$\frac{E(x)}{E_b} \approx 1 + \frac{l/r - 1}{(x/r + 1)^2} + \frac{2}{(x/r + 1)^3}$$

(2)

with the protrusion length and radius $l$ and $r$, respectively, as used in [36]. $E_b$ is the undisturbed background field. It was checked by 3D electric field calculations with COMSOL for some cases that this approximation was sufficiently precise for the present purpose. With $r = 100$ $\mu$m as assumed protrusion radius, average deviations in the field decay were within 10%. The formula is only correct until $l = r$, i.e., $l = 100$ $\mu$m. Therefore, predictions will only be shown for $100$ $\mu$m length and higher. For rough surfaces $l/r = 1$ with $l = 20$ $\mu$m as a typical peak height of roughness structures was assumed. This is similar to the approach of [14]. The chosen length is deduced from the measured $R_z$ by assuming $l = R_z/3$. Note that $R_z$ describes the average difference between highest peaks and lowest valleys of the surface.
3.2.1. First Electron

The electric field needed for a start electron at positive polarity in SF$_6$ can be estimated from the volume where the electric field is above the critical field and where an electron can be detached from a negative ion in the available time of voltage application, i.e., in the present case within 10 μs—see [38] for details of the model. All parameters for SF$_6$ were taken from [34].

At negative polarity, a start electron is assumed to be delivered from the electrode surface. For SF$_6$, this could be described reasonably well by using the Fowler–Nordheim (FN) equation in [34], which gives the electron production rate emitted from a surface area at given electric field. The statistical time lag at negative polarity is then

$$t_s = (A_{eff} \cdot 10^{4.52})/\sqrt{\Phi} \cdot 1.54 \cdot 10^{-6} \cdot \frac{(\beta \cdot E_b)}{\Phi} \cdot \exp[-(\Phi^{1.5} \cdot 2.84 \cdot 10^6)/(\beta \cdot E_b)]/e)^{-1}$$

(3)

where \(\Phi = 4.5\) eV is the work function for steel, \(e\) the elementary charge, \(\beta = (2 + l/r) \cdot \beta_2\) a field enhancement factor at \(l\) to the protrusion tip (see also (2)) and due to micro-surface roughness and \(A_{eff}\) the effective electron emitting area. For SF$_6$ values for \(\beta_2\) and \(A_{eff}\) were taken from the fits in [34] with \(\beta_2 = 20\) and \(A_{eff} = 10^{-16}\) m$^2$. From this, the necessary electric field for a start electron within the available time can be deduced.

For CO$_2$, the same approach and models as for SF$_6$ were used but with CO$_2$ specific adaptions and empirical approximations for the relevant parameters. For the statistical time lags, the field dependence of the electron detachment rate, the equilibrium negative ion concentration and the parameters in the FN equation were adapted to experimental data from [37]. At positive polarity, best agreement, within a large scatter, was achieved by empirically using an equilibrium concentration of $10^4$ ions/m$^3$ at 0.1 MPa in the pressure-dependent ion concentration, as given in [38], and a field dependence of the electron detachment rate coefficient of

$$\delta = 10 \cdot \left(\frac{E}{E_{cr}}\right)^{13} [1/s]$$

(4)

with the critical electric field of CO$_2$ at pressure \(p\): \(E_{cr} = p \cdot (E/p)_{cr,0}\), with \((E/p)_{cr,0} = 23\) V/(m·Pa) [37]. To our knowledge, no experimental data are available to verify this scaling of the electron detachment rate. At negative polarity, the field enhancement parameter \(\beta_2\) in (3) was set to \(\beta_2 = 70\) and the effective area needed to be set to \(A_{eff} = 10^{-24}\) m$^2$ to achieve best agreement with the experimental data. Such small value for \(A_{eff}\) is probably not realistic, but one has to consider the simplicity of the FN equation. The approximations have to be seen, therefore, just as physically motivated fits to the experimental data which are valid in the given parameter range of protrusions up to a 4.5 mm length. Examples for statistical time lags for negative and positive polarity with the data from [37] are shown in Figure 5. For surface roughness, values from the rod plane experiment in [37] are used. The field enhancement factor at the surface of the rod (\(E_{surface}/(1/D)\)) of the rod in these experiments was about 17. The background field in the plots is the undisturbed electric field U/D without field enhancement by a protrusion or by the rod.
3.2.2. Streamer Inception

Streamer inception fields were calculated using the semi-empirical approach in [38]

\[ K = \int_{0}^{l_{c}} \alpha d \theta \] (5)

With the ionization integral parameter \( K = 10.5 \) and 13 for SF\(_6\) [45] and CO\(_2\) [37], respectively. The effective ionization coefficient \( \alpha \) was taken from [38] for SF\(_6\) and [37] for CO\(_2\). The integration is done along the axis of symmetry starting from the protrusion tip at \( z = 0 \) where the electric field is above the critical field, up to the distance \( z = l_{c} \), where the field has dropped to the critical field.

3.2.3. Streamer Crossing and Spark Transition

Streamer crossing followed by spark transition is only relevant for CO\(_2\), since in SF\(_6\) this occurs at the critical field, which is much higher than leader propagation fields [38]. In [37], it was shown that streamer crossing for long duration voltage application times of several 100 \( \mu s \) is approximately sufficient for breakdown in the pressure range investigated here. In case of short-duration voltage application time, a higher field than that necessary for streamer crossing is needed to allow for the spark transition within the short available time of 10 \( \mu s \), since the heating processes in the streamer channel need a sufficient electric field and time. This field increase was estimated from [47] to roughly 35\% compared to the streamer crossing field, which is based on the breakdown voltage ratio for short and long duration waveforms.

3.2.4. Leader Propagation and Breakdown

As shown in [35,38], leader propagation through the gap can be associated with breakdown. Leader inception and propagation was calculated using the previous model from [35] for SF\(_6\). In this model, the streamer corona charge at the protrusion tip or a propagating leader is calculated and fed into the streamer or leader channel. This leads to stepped heating followed by stepwise leader propagation through the gap. Crossing 90\% of the gap distance was defined as sufficient for breakdown. For CO\(_2\), the same model but with adapted thermodynamic properties of mass density, enthalpy, velocity of sound and effective ionization coefficients [46] from our own, in-house-developed solver were used.
4. Results

4.1. Protrusions With SF6

The results for the single protrusions in SF6 are shown in Figure 6 for positive and negative polarity. The $E_0$ background fields are normalized to the critical field, which eases the interpretations and comparison between different gases. In agreement with [38], the breakdown values for positive polarity are slightly lower than those at negative polarity. Only for protrusion length of 200 μm or less the differences between the polarities are within the scatter. At such small lengths, many breakdowns also happened away from the protrusions, which were, however, not considered for the determination of $E_0$, as mentioned above. The decrease of the normalized $E_0$ breakdown field with increasing protrusion length is reasonably described by the prediction for leader breakdown, which occurs significantly below the critical field. Streamer inception and the first electron criterion are fulfilled at lower fields, such that leader breakdown is expected to be the decisive criterion. Only for very small lengths below 250 μm and positive polarity, the first electron criterion might require slightly higher fields than the leader breakdown. This is, however, within the uncertainties of the predictions. We can also observe a higher scatter for positive polarity compared to negative polarity.

![Figure 6](image)

*Figure 6.* Normalized breakdown fields $E_0/E_{cr}$ vs. protrusion length $L$ for SF6 and single protrusion at 0.4 MPa at (a) positive and (b) negative polarities

Using 20 protrusions—see full symbols in Figure 7—lowers the normalized $E_0$ breakdown fields significantly. For comparison, the experimental results and predictions for single protrusions are also shown. The difference between positive and negative polarity in the figure seems more pronounced than for single protrusions. The experimental breakdown fields are now lower than the predictions for leader breakdown for a single protrusion. The enlargement law predictions from (1) are shown by the black dash-dotted curves and agree for both polarities with the experimental results. Thus, the lowering of the experimental breakdown fields for 20 protrusions is well described by the enlargement law based on the breakdown probability distributions of single protrusions.
Figure 7. Normalized breakdown fields $E_50/E_{cr}$ vs. protrusion length $L$ for SF6 and 20 protrusions. Not all protrusion lengths could be measured when using multiple protrusions at (a) positive and (b) negative polarities.

For 100 protrusions this is different at positive polarity—see Figure 8a. There is no further lowering of the breakdown fields when using 100 instead of 20 protrusions and the prediction of the enlargement law (1) is significantly lower than the measurement. There seems to be a lower limit which is not further exceeded when using a larger number of protrusions. This is not the case for negative polarity—see Figure 8b—where we see a good agreement of the enlargement law predictions with the experimental results for 100 protrusions.
Figure 8. Normalized breakdown fields $E_{50}/E_{cr}$ vs. protrusion length $L$ for SF6 and 100 protrusions. Not all protrusion lengths could be measured when using multiple protrusions at (a) positive and (b) negative polarities.

Typical partial discharge images, which were taken at breakdown events, are shown in Figure 9. It can be seen that many discharges happened in parallel, i.e., simultaneously within 10 μs. These discharges could be observed in case of breakdown since the discharge channels are illuminated by the strong light emission from the breakdown spark channel occurring elsewhere in the gap. These images are, therefore, similar to a Shadowgraphs or Schlieren images [48]. The discharge channels have the typical signature of leader channels [35], which confirms the interpretation from leader breakdown predictions, i.e., the breakdown is determined by leader propagation. The negative leader channels (Figure 9c) are thicker and less structured than positive leader channels (Figure 9b); this observation is in agreement with the expectation from [49].
4.2. Protrusions With CO₂

Results for single protrusions in CO₂ are shown in Figure 10. The figure shows the experimental normalized $E_{50}$ breakdown values and predictions for first electron, streamer inception and leader breakdown and the background fields for streamer crossing and spark transition of negative streamers. The complete range where streamer crossing and spark transition is expected at negative polarity is indicated by the cyan colored area in the figure. For positive streamers we expect streamer crossing only at the critical field [37], which is, therefore, probably not relevant in the present case, since this needs fields higher than the leader breakdown criterion.

![Figure 10. Normalized breakdown fields $E_{50}/E_c$ vs. protrusion length $L$ for CO₂ and single protrusion at 0.6 MPa at (a) positive and (b) negative polarities.](image-url)

For protrusion lengths below 1.5 mm with positive polarity, the breakdown happens at or slightly above the critical background field—see Figure 10a. The leader BD predictions do not explain this. Probably this can be explained by the first electron criterion (red dashed curve). At or above the critical field, avalanches can start everywhere in the gap, which is in agreement with the experiment. Many breakdowns did not occur at the protrusion but in other locations of the gap in this case. There was also a larger scatter in the breakdown fields, which is reflected in the error bars of the experimental breakdown values, especially at negative polarity.

At negative polarity, experimental $E_{50}$ values are close to the leader breakdown predictions for protrusions larger than 1 mm—see Figure 10b. An additional possibility for breakdown at negative polarity might be streamer crossing and transition to spark. Therefore, at negative polarity both
mechanisms might be decisive for breakdown. From the partial discharge images—see Figure 11—this could not be decided unambiguously. For smaller protrusions, breakdown occurs at the critical field. As for positive polarity, breakdowns often occurred at the plate electrodes and not at the protrusion for smaller protrusion lengths.

Figure 11. Images of partial discharges and breakdown in CO₂ at 0.6 MPa for (a) positive polarity at 115 kV/cm with 100-μm protrusions and (b) negative polarity at 139 kV/cm with 200-μm protrusions.

Using 20 protrusions, see Figure 12, the measured breakdown fields decrease at both polarities compared to the results from the single protrusion experiments. For positive polarity, this is in agreement with the prediction from the enlargement law (1)—see Figure 12a. Note that predictions for the enlargement law were not possible for small protrusion lengths due to the limited amount of data and large uncertainties of the breakdown probability distributions. The measured breakdown values are for the positive polarity at the first electron prediction for single protrusions but still higher than the leader breakdown predictions. For negative polarity, a lowering of $E_{50}$ values is observed mainly below 1 mm protrusion length—see Figure 12b. The measured breakdown fields below 0.5-mm protrusion length coincide with the first electron and streamer inception prediction. Interestingly, for protrusion lengths of 1 mm and more, no significant decrease of the $E_{50}$ values for 20 protrusions compared to single protrusions is observed. The breakdown fields are at the expected spark transition level, which is assumed to be independent of protrusion length.

As mentioned in Section 2.1, also a smaller spacing of 2 mm between the protrusions was tested with 20 protrusions for CO₂. These results were not significantly different from the usual spacing of 4 mm—see Figure 12. Only a small reduction of less than 6% in field maximum was expected from the comparison of electric field calculations when using the smaller spacing (not shown in Figure 12), which is similar to the experimental uncertainties.
Figure 12. Normalized breakdown fields $E_{50}/E_c$ vs. protrusion length $L$ for CO$_2$ and 20 protrusions at (a) positive and (b) negative polarities.

For 100 protrusions and positive polarity—see Figure 13a—the measured breakdown fields drop to the leader breakdown predictions for protrusions of 0.5 mm length and more. This is not predicted by the enlargement law, which results only in a moderate reduction. For smaller protrusions, the breakdown fields are still significantly higher than the leader breakdown prediction, probably due to the lack of a first electron. For larger protrusions of 1 mm and more, the positive breakdown fields are now similar or even lower than the negative ones, as would be expected from the leader breakdown criterion.
Figure 13. Normalized breakdown fields $E_\text{50}/E_\text{cr}$ vs. protrusion length $L$ for CO$_2$ and 100 protrusions at (a) positive and (b) negative polarities. Not all protrusion lengths could be measured when using multiple protrusions.

For 100 protrusions and negative polarity—see Figure 13b—the breakdown values drop significantly only for small protrusions below 0.5 mm lengths, compared to the previous case of 20 protrusions. For 250 μm and below, they are probably determined by streamer inception. Above 250 μm protrusion length, there is only a small drop of breakdown fields with increasing protrusion length. It seems that a saturation is reached, which is probably not due to the first electron criterion, but due to streamer crossing followed by spark transition. The enlargement law predictions are now significantly lower than the measurements.

Images of partial discharges and breakdown in CO$_2$ are shown in Figure 11. Local channel illuminations indicated local channel heating could be clearly observed, which might be during leader propagation but also for a streamer to spark transition. Similarly to SF$_6$, discharges occurred simultaneously in the time window of 10 μs. Weak density variations in the non-luminous regions indicate some channel heating also in these regions. Interestingly, breakdows from the bottom plate electrode could also be observed.

4.3. Electrodes With Surface Roughness

The results from the electrodes with surface roughness are shown in Figures 14 and 15 for SF$_6$ and CO$_2$, respectively. Note that for the $E_{50}$ evaluation the electric field at the surface of the electrodes was used, since the fields are weakly non-uniform in the case of the small surface. Again, the $E_\text{50}$ breakdown field is normalized to the critical field. For comparison calculations for first electron, streamer inception and breakdown are shown for a single protrusion in the figures. Increasing the area in SF$_6$ at positive polarity led to a significant lowering of the $E_{50}$ breakdown fields at positive, but negligible decrease at negative polarity—see Figure 14a. This can be understood by the streamer inception and first electron criterion. At positive polarity, the experimental breakdown field drops roughly to the predicted streamer inception field for large areas. This can probably be explained by a sufficiently high number of sites for discharge inception for large electrodes areas, i.e., there is a high likelihood for a first electron at a small surface protrusion. Then, the streamer inception becomes a
sufficient breakdown criterion. For small areas a first electron is probably lacking, and the breakdown field becomes even higher than the critical field. In the predictions for a single protrusion a first electron is only available at the critical field, i.e., probably these predictions are still too optimistic. The prediction from the enlargement law (solid arrow) for increasing area reproduces qualitatively the decrease of breakdown field with increasing surface area. However, it predicts for large areas the breakdown at the critical field and not at the streamer inception field. Using (1) to predict the breakdown field scaling from large to small area would quite underestimate the measured breakdown field (dashed arrow). Thus, at positive polarity, the enlargement law predictions do not agree well with the experiments.

![Graph showing breakdown fields E50/Ecr vs. effective surface area in SF6 at 0.4 MPa for both positive and negative polarities.](image)

**Figure 14.** Normalized breakdown fields E50/Ecr vs. effective surface area in SF6 at 0.4 MPa at (a) positive and (b) negative polarities. Calculations for first electron, streamer inception and breakdown at a single hemispherical protrusion of 20 μm height are shown for comparison.

At negative polarity, this is different—see Figure 14b. Here, the predictions in both directions, i.e., from small to large electrode, or vice versa, give the correct breakdown fields. Note that the experimental breakdown field is in this case again approximately at the predicted streamer inception field. This is plausible, since at negative polarity there is no lack of a first electron (see dashed line in Figure 14b) and breakdown occurs for small and large electrode roughly at similar fields, which is at streamer inception. Note that streamer inception is independent of polarity, i.e., for large areas, the breakdown fields are similar for both polarities.
Figure 15. Normalized breakdown fields $E_50/E_{cr}$ vs. effective surface area in CO$_2$ at 0.6 MPa at (a) positive and (b) negative polarities. Calculations for first electron, streamer inception and breakdown at a single hemispherical protrusion of 20 μm height are shown for comparison.

In CO$_2$, the observations are similar—see Figure 15. At positive polarity (Figure 15a), experimental breakdown fields drop for large electrodes to close to the critical field, which is slightly higher than the predicted streamer inception and breakdown field. This discrepancy is probably still within the accuracy of the predictions. Only for small area and positive polarity there is probably again a lack of a first electron which leads to an increase of $E_{50}$ in the experiments. Note that this lack of first electron is not predicted by the model. Due to the strongly non-linear field dependence of (4), at the critical field, a first electron is always predicted. Probably the model is not sufficiently precise for CO$_2$ and small protrusions. At negative polarity in CO$_2$ (Figure 15b), there is a slightly more pronounced area effect than for SF$_6$. Again, the breakdown happens for large areas close to the critical field, which is only slightly above the first electron criterion prediction—see dashed horizontal line in Figure 15b. Thus, there is possibly also a lack of first electron for small areas at negative polarity, which is, however, much less pronounced than at positive polarity. The discrepancies can be probably explained by the simplicity of the model for the first electron.

Images of partial discharges and breakdown are shown in Figures 16 and 17 for both gases used. For CO$_2$, there are again discharges from the plate electrode, similarly to the protrusion results—see Figure 16. Arrested discharges could also be observed at breakdown for SF$_6$—see Figure 17. This shows that there is a competition between various discharge channels.
Figure 16. Images of partial discharges and breakdown in CO$_2$ at the small surface. (a) Positive polarity at a surface field of 322 kV/cm and (b) Negative polarity at 235 kV/cm surface field.

Figure 17. Images of partial discharges in SF$_6$ at 0.4 MPa, negative polarity at a surface field of 375 kV/cm. The picture is edited with different brightness on the two halves to better show the structures of the partial discharge.

5. Discussion

The results at multiple protrusions have shown that the experimental breakdown E$_{50}$ values can be interpreted by the predictions of the various physical processes as first electron, streamer inception and leader propagation for a single protrusion. In SF$_6$, breakdown will only occur if all criteria are fulfilled. This is also valid in CO$_2$. However, error bars were much larger for the CO$_2$ experiments, resulting in larger uncertainties of the interpretations. In CO$_2$, streamer crossing and spark transition is a possible mechanism for breakdown at negative polarity, additionally to the leader breakdown, which is dominant at positive polarity. Similarly, this was found in [37]. In CO$_2$, breakdowns at protrusions occur much closer to the critical field, which is also reflected in the predictions. This is likely due to the lower slope of the effective ionization coefficient in CO$_2$, which is only a weakly electron attaching gas and, therefore, needs relatively higher fields for streamer and leader inception compared to the critical field than in SF$_6$ [50]. This leads to lower sensitivity to surface roughness or protrusions in case of CO$_2$ compared to SF$_6$.

Increasing the number of protrusions and comparing the resulting E$_{50}$ breakdown fields with predictions from the enlargement law (1) leads to reasonable agreement for SF$_6$ at negative polarity. This indicates that the statistical processes for a single protrusion, resulting in the measured breakdown probability distribution, can be scaled according to the enlargement law without reaching other, e.g., physical limitations at the tested number of protrusions. This can be possibly understood by the very low first electron and streamer inception fields, i.e., these criteria are not limiting the
scaling of the breakdown fields and the statistical scatter is probably mainly due to leader transition and propagation. This is different at positive polarity in SFs. Whereas, the reduction of breakdown field with 20 protrusions is still well described by the enlargement law, we see a significant discrepancy using 100 protrusions. This is possibly produced by the availability of a first electron which needs a certain minimum field and can, therefore, not be described by statistical phenomena alone—see [34,38]. Thus, if the field is below a certain threshold using a large number of protrusions cannot compensate for the necessary field for creating the first electron in the critical volume. Note that the first electron depends on the size of the critical volume, which increases with the number of protrusions, but also strongly non-linearly on the applied electric field within the critical volume—see (4). Additionally, in CO2, limits for the reduction of breakdown field with increasing number of protrusions can be seen. At negative polarity, such a limitation is the streamer inception criterion for small protrusions of 250 μm and smaller. For larger protrusions there is a lower limit which could be explained by streamer crossing and spark transition, but possibly also by the leader mechanism. This could not be determined unambiguously so far and would need more detailed optical diagnostic investigations. At positive polarity in CO2, a reasonable agreement with the enlargement law is seen for 20 protrusions, which is similar to SFs. For 100 protrusions and positive polarity the experimental breakdown fields drop to the predicted leader breakdown field. This drop is underpredicted by the enlargement law, which indicates that the breakdown probability distributions for single protrusions does not include all the relevant phenomena with sufficient precision in this case.

For rough surfaces, we investigated the case of very small protrusions in the range of only a few 10 μm in height. We used here the approach of Pedersen [14] to approximate surface roughness by hemispherical protrusions. Thus, this case has similarities to the protrusion array, only that the number of protrusions is probably much higher than in the case of the protrusion array. A detailed surface structural analysis was not done in the present case but unpublished investigations on a similar surface has shown that we can expect one protrusion of 20 μm height per mm² as an order of magnitude. For the small surface of 240 mm² we can expect, therefore, about 240 protrusions very roughly. For the larger area this was increased by more than a factor 20 to investigate the enlargement law in a more realistic situation. Thus, for the larger surface we can expect as an order of magnitude about 6450 protrusions of a 20-μm size. For negative polarity and SFs, the area scaling due to this increase is satisfactorily described. This indicates that the probability distributions at negative polarity in SFs describe well the statistical phenomena. In this case, we do not expect a lack of a first electron and the statistical processes of the breakdown like streamer inception and leader transitions are probably decisive for the breakdown statistical scatter. In CO2 and negative polarity, the reduction of breakdown field with increasing area is less well described by the enlargement law. Here, the statistical scatter of the first electron is also probably important. This is similar at positive polarity, where the breakdown fields in the experiments drop roughly to the streamer inception fields for large surfaces and the enlargement laws underpredict this. Possibly, statistical phenomena of the first electron do not follow a simple enlargement law scaling. This needs further investigations.

The investigation showed that enlargement laws cannot be applied without caution. The physical processes which might limit the scaling of statistical distributions, e.g., first electron or streamer inception, must be taken into account. Additionally, the enlargement law is sensitive to the precise shape of breakdown probability distributions, which might lead to insufficient accuracy if the distributions are not determined with sufficient precision. Finally, underlying physical processes might not follow a simple enlargement law scaling, e.g., due to strongly non-linear effects like for the first electron criterion. This is especially the case if various physical processes are involved.

In the present investigation, the lower limit of the Weibull distribution $E_0$ was set to the streamer inception values, which can be regarded as a minimum requirement for breakdown. As can be seen from the figures, in none of the cases this was reached with multiple protrusions. Only for rough surfaces and large area it was approached, i.e., in this case it influenced significantly the enlargement law. The satisfactory agreement for this case might indicate that this assumption for $E_0$ was justified.

The breakdown images have revealed some further information showing especially many discharges occurring in parallel during breakdown events on the short time scale of only a few
microseconds. These discharges could bridge the gap or remain arrested in the gap. This shows that a first electron was not lacking in such cases, in agreement with the model predictions. Thus, at breakdown electrons were not only available at one protrusion but also at other sites. Interestingly, in CO₂ also discharges from the bottom plate could be sometimes observed at negative polarity, similar to a return stroke in lightning. This was not observed in SF₆. Possibly, this is linked to a different breakdown mechanism, which might be of streamer to spark transition type in this case.

6. Conclusions

Breakdown experiments on multiple protrusions and on artificially roughed surfaces were done in uniform and weakly uniform background fields with SF₆ and CO₂ at 0.4 and 0.6 MPa, respectively. The voltage waveform was a stepped DC pulse with time to breakdown within 10 μs, which is comparable to that of standard lightning impulse (LI). With the multiple protrusion array, the number of protrusions and the lengths of the protrusions was varied in the ranges of 1–100 and 0.05–2 mm, respectively. For the roughened surfaces, a mean peak-to-valley roughness (Rᵥ) of 62...65 μm was realized, and two different surface areas were tested. From the breakdown experiments, Weibull breakdown probability distributions were deduced and 50% breakdown probability fields and the standard deviation σ of the distributions were determined. Enlargement law scaling predictions according to (1) were done to predict the effect of changing the number of protrusions or surface area. These predictions were compared to the experiments. Additionally, calculations by physical models, describing first electron, streamer inception and breakdown by leader propagation or streamer-to-spark transition at single protrusions were done for interpretation of the experimental results. The interpretations were supported by optical observation of the discharges.

The following main observations were obtained: In SF₆, breakdown fields are well below the critical field, even for protrusions below 1 mm length, whereas for CO₂ breakdown occurs closer to the critical field. The breakdown fields can be interpreted and roughly described by the physical models, taking into account the uncertainties of the experiments and of the models. In SF₆ the leader propagation criterion is decisive for breakdown at both polarities for single protrusions. Increasing the number of the protrusions to 20 lowers the breakdown field for both gases in agreement with the predictions from the enlargement laws, compared to the single protrusion. No significant effect on the protrusions spacing was seen in CO₂ with 20 protrusions. Discrepancies with the enlargement law scaling were observed for both gases in some cases when increasing the number of protrusions to 100. The results show that enlargement laws cannot be generally applied without considering the various physical processes which influence breakdown, i.e., the availability of a first electron, streamer and leader inception and propagation and spark transition. The decisive breakdown criteria depend on the gas, the protrusion lengths and polarity of the applied voltage, which leads to different minimum limiting fields which cannot be exceeded by an enlargement law. Additionally, the various physical processes will not scale in the same way when using an enlargement law. All this limits the accuracy of an enlargement law scaling. This is confirmed by the results from the rough surfaces. At positive polarity the breakdown fields dropped for SF₆ and CO₂ approximately to the streamer inception field, when increasing the surface from 240 to 6450 mm², i.e., there is a physical limit for breakdown which is reached for sufficiently large surfaces. This decrease was underpredicted by the enlargement law. At negative polarity and SF₆ only a very small enlargement effect is seen in the experiments, in agreement with the predictions. In CO₂ and negative polarity, there is a more pronounced effect of the surface area, which is still much smaller than for positive polarity, however. Again, this decrease is underpredicted by the enlargement law. The effect of the protrusion spacing was investigated only in CO₂ with 20 protrusions. No significant effect within the experimental scatter was seen.

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