Resonator-free optical bistability based on epsilon-near-zero mode

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A majority of existing research on optical bistability rely on resonant schemes using nonlinear materials, which inevitably require a trade-off between the switching intensity and response time. In this work, we propose a novel non-resonant scheme, which utilizes strong light enhancement of the epsilon-near-zero (ENZ) mode to realize optical bistability. We used graphene as a non-linear ENZ material and designed an integrated optical bistability device composed of a graphene-embedded Si waveguide, which supports an ENZ mode. The proposed scheme can overcome the trade-off necessary in resonance-based optical bistability, and the designed optical bistability device simultaneously allows for a short response time (~200 fs) and low switching intensity (~700 kW/cm²).

Optical bistability is one of the key functionalities required to implement all-optical switching and optical memory that are essential functions for all-optical signal processing1–3. The optical bistability is a nonlinear phenomenon that has two stable output states for a given input state and exhibits hysteresis; the steady-state output depends on the history of the excitation. This phenomenon can be induced by a bell-shaped output response to an input variation, which is generally caused by a feedback mechanism in a resonator with nonlinear refractive index or absorption. For practical applications of the optical bistability, it is important to realize a low switching intensity and short response time simultaneously. So far, numerous studies have focused on reducing the switching intensity and Q factor (Q) and strong field enhancement, such as photonic crystals⁴,⁵, surface plasmons⁶, ring resonators⁷,⁸, and waveguide gratings with guided mode resonance⁹. However, because the response time is proportional to the Q factor, reducing switching intensity by increasing Q factor inevitably increases the response time⁹. Therefore, these resonant schemes cannot avoid a trade-off between a response time and a switching intensity.

To avoid this trade-off, non-resonant schemes for optical bistability have been proposed, which achieve fast optical bistability by effective permittivity variation¹⁰ and the hyperbolic dispersion property¹¹ of the metal-dielectric structure, resulting in response times of ~1 ps and ~350 fs, respectively. However, the switching intensity is above 100 MW/cm², which should be reduced.

In this study, a simple integrated waveguide structure supporting the epsilon-near-zero (ENZ) mode is proposed to realize optical bistability at a wavelength of 1.55 μm. The ENZ mode defined as an even-symmetry plasmonic mode (long-range surface plasmonic mode) in ultra-thin ENZ material (|ε| = ~0) confines most of the electric field in the ultra-thin film¹²–¹⁴. We realized optical bistability with strong non-resonant light confinement of the ENZ mode in a nonlinear ENZ material. We used monolayer graphene as a nonlinear ENZ material. Graphene is widely used as an active nonlinear material for optical bistability because of its tunable permittivity and high nonlinear coefficient¹⁵–¹⁸. We show that graphene supports the ENZ mode and the nonlinearity of graphene combined with the ENZ mode effect results in optical bistability, simultaneously achieving a short response time and low switching intensity. All calculations in this paper have been carried out using finite-difference time-domain (FDTD) method.

Results

Epsilon near zero mode in graphene. For the investigation of the ENZ mode in graphene, a Si/graphene/Si structure as shown in Fig. 1(a) is considered. The conductivity of graphene is obtained by Kubo formalisms¹⁹,²⁰ assuming a Fermi velocity of v_F = 10⁶ m/s and a mobility of μ = 10,000 cm²/Vs. The permittivity of graphene is obtained from ε_G = 1 + iσ/ωε₀d_G, assuming the thickness of monolayer graphene, d_G = 0.34 nm. The permittivity of Si is set as 3.45. Figure 1(b) shows the real part, imaginary part, and magnitude of permittivity of graphene for Fermi level of E_F = 0.5 eV as a function of frequency. It can be seen that the real part of the permittivity of

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graphene is zero and the magnitude of graphene permittivity is minimized at the plasma frequency \((\omega_p)\). We also plot a dispersion curve of the guided mode in Si/graphene/Si geometry shown in (a) and the complex permittivity of graphene for Fermi level of \(E_F = 0.5\) eV. (c) Amplitude of the surface-normal component of the electric field \(|E_x|\) for \(E_F = 0.5\) eV at \(P_1\) (red line) and \(P_2\) (black dash) indicated in (b). (d) Dispersion curves of Si/Graphene/Si geometry for various Fermi level: \(E_F = 0.5\) eV.

Optical bistability based on ENZ. The proposed structure to realize optical bistability is schematically illustrated in the inset of Fig. 2, which consists of a Si waveguide and a graphene sheet embedded in the Si layer, where the thicknesses of the graphene sheet and Si waveguide are assumed to be 0.34 nm and 220 nm, respectively. Figure 2 shows the imaginary part of the wave-number at \(\lambda = 1.55\) µm as a function of the Fermi level of graphene for different mobility values, which represents the loss in the guided mode. It can be seen that the imaginary part of the wave-number increases when the Fermi level approaches \(E_F = 0.5\) eV, where the permittivity of graphene is almost zero at \(\lambda = 1.55\) µm. As the Fermi level approaches the ENZ region (\(E_F = 0.5\) eV), the electric field becomes confined to the graphene layer owing to the ENZ mode, which results in an increase in the loss in the graphene. In addition, the loss in the guided mode can be tuned by adjusting the Fermi level at fixed wavelength.
We exploited the strong and tunable field confinement and nonlinearity of graphene to realize optical bistability. Because the permittivity of graphene can be modified through the nonlinear Kerr effect, the same effect as the Fermi level shift can be implemented by varying the input intensity. In other words, by modifying the input intensity, the light confinement can be tuned. Therefore, the loss in the mode can be tuned to a considerable extent by adjusting the input intensity.

The imaginary part of wave number (i.e., loss) varies with respect to the variation in mobility, and its slope and peak value deteriorate as the mobility decreases. This stems from the degradation of the ENZ effect due to poor graphene quality. It appears that a graphene mobility of $\mu = 5,000 \text{ cm}^2/\text{Vs}$ is sufficient for obtaining high performance optical bistability because the imaginary part of wave-number does not vary much for graphene mobility values larger than $\mu = 5,000 \text{ cm}^2/\text{Vs}$.

We set the operating Fermi level to $E_F = 0.515 \text{ eV}$, which deviates slightly from the ENZ region, and in this case, the permittivity of graphene is $\varepsilon_G = -1.07527 + 0.217745i$ at $\lambda = 1.55 \mu \text{m}$. The nonlinear susceptibility of graphene is assumed to be $0.515 \times 10^{-15}$

In the proposed structure, optical bistability is realized based on the guided-mode confinement variation near the ENZ mode, which is the non-resonant case. The permittivity of graphene is $\varepsilon_G = \mu + i\lambda$, where $\mu$ may be varied from 2.095 to 1.55, depending on the applied electric field confinement in graphene. However, if the input intensity increases further, the permittivity of graphene drifts away from the ENZ region and thus, the loss decreases again as a result of the weakened confinement of the non-ENZ mode. This functions as a feedback mechanism for optical bistability, which shows features similar to the bell-shaped transmission-input power relationship in resonator-based optical bistable devices. Figures 3(a,b) show optical bistability behavior for various lengths ($l$) of the proposed structure: (a) $l = 500 \text{ nm}$ and (b) $l = 1 \mu \text{m}$. The red and blue curves represent the output intensities for the increasing and decreasing input intensities, respectively. The calculated switching intensities are the same as 700 kW/cm$^2$ regardless of the device length. However, the hysteresis width decreases as the device length decreases because the propagation length in the ENZ mode is shorter, which results in the weaker ENZ mode effect. Figure 3(c,d) show the temporal responses of the optical bistability for various device lengths: (c) $l = 500 \text{ nm}$ and (d) $l = 1 \mu \text{m}$. To analyze the temporal response, we first set the input intensity below the switching intensity (denoted as $P_1$) for 500 fs and applied an additional 500-fs wide square pulse of 450 kW/cm$^2$ height to the input, triggering the output transition from $P_1$ to $P_1^*$ through $P_2$. Then, we triggered the output transition from $P_1^*$ to $P_1$ through $P_2$, by applying another 500-fs wide square pulse of $-300$ kW/cm$^2$ height to the input. As seen in Fig. 3(c,d), the output intensity shows overshooting and oscillating behavior before stabilization only when it goes through a nonlinear variation, that is, in the processes of $P_1 \rightarrow P_1^*$ and $P_1 \rightarrow P_1$, where there is no nonlinear variation of the output. In nonlinear processes, the abrupt change in intensity inside the device will cause abrupt changes in the local guided mode profile, and mode mismatch occurs in addition to the change in propagation loss. In general, at the mode mismatch, the incident wave requires a certain propagation distance to adapt to the mode. During the mode adaptation, the local propagation loss will also change, resulting in another change in the local mode. Therefore, this interaction between the change in mode profile and the propagation loss at the local mode mismatch seems to cause the oscillation behavior, which takes some time for stabilization. By contrast, in the linear processes, the gradual variation in the loss causes no abrupt local mode mismatch and thus, no oscillating behavior. The estimated rising and falling response times for the nonlinear transitions are about 200 fs and 150 fs, respectively. In the proposed structure, optical bistability is realized based on the guided-mode confinement variation near the ENZ mode, which is the non-resonant scheme. Therefore, the build-up time for the change in refractive index of graphene to support the ENZ mode is very short, and fast optical bistability behavior could be achieved. It should be noted that the device length does not

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**Figure 2.** Imaginary part of the wave-number in the proposed optical bistability device as a function of the Fermi level ($E_F$) for different mobility values ($\mu$). Inset shows the schematic of the proposed optical bistability device.
affect the response time considerably because the propagation time of the guided mode for a few hundred nanometers is just a few femtoseconds. It appears that in the short device at the wavelength scale, the response time is mainly determined by the stabilizing time of the overshoot power.

Conclusions
We numerically investigated the optical bistability behavior based on the ENZ mode in graphene. We showed that a simple, graphene-embedded Si waveguide structure supports an ENZ mode and its propagation loss varies drastically with the permittivity change in graphene, which enables optical bistability by virtue of the optical nonlinearity of graphene. The switching intensity and response time in the proposed structure are approximately 700 kW/cm² and 200 fs, respectively. The proposed scheme may lead to a new class of non-resonant optically bistable devices that can avoid the hitherto necessary tradeoff between the switching intensity and response time. In addition, we believe that the proposed scheme can be applied to other material systems that support the ENZ mode such as an ultra-thin doped semiconductor layer, achieving similar optical bistability behavior.

Methods
The dispersion relation of the guided mode was calculated by solving the one-dimensional Maxwell’s equation using the root-finding algorithm. In our numerical analysis of the optical bistability, the permittivity of graphene was calculated using the Kubo formula, assuming a graphene thickness of 0.34 nm, Fermi velocity of 10⁶ m/s, and mobility of 10,000 cm²/Vs, and the nonlinear susceptibility of graphene was assumed to be \( \chi^{(3)} = 2.095 \times 10^{-15} \). The optical bistability curve and the temporal response were calculated using the commercial FDTD software (Lumerical FDTD). In the FDTD calculation, the third-order (Kerr-type) nonlinearity is handled by the relation of \( E(t) = D(t)/(\varepsilon_0 \varepsilon_r + \varepsilon_0 \chi^{(3)}|E(t-\Delta t)|^2) \) assuming an instantaneous nonlinear response, where \( \Delta t \) is the time step of the iterative field update. The latest value of \( E \) calculated from the latest value of \( D \) and the previous value of \( E \) is used for the update of \( H \) in the next iteration, which is followed by the update of \( D \). This process repeats cyclically. The input and output intensities were calculated by integrating the Poynting vector over the waveguide cross section and calculating its time average.

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**Author Contributions**

M.K. and S.K.1 conceived the idea. M.K. performed numerical calculations under the supervision of S.K.1 and S.K.2 All authors discussed the results and contributed to the writing of the manuscript.

**Additional Information**

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