Introducing a holistic approach to model and link fouling resistances

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Abstract
Fouling is the unwanted deposition of soils on heat transfer surfaces and is a major challenge for industry and has been subject to scientific investigations for decades, still being an unsolved problem for many applications. A fouling situation is commonly quantified with the thermal fouling resistance describing the integral fouling behavior of an apparatus. Modeling of this quantity is a permanent subject to research. This contribution presents the basics of an expanded consideration by introducing a holistic approach to model and link fouling resistances based on the extension of previous work in this field. A thermal and a mass based approach to calculate fouling resistances are considered integrally and locally. This will provide a detailed knowledge of the fouling behavior. Various variables are needed for modeling the different fouling resistances. Therefore, both experimental and analytical methods have to be applied to obtain the required data regarding local differences of crystallization deposits within double-pipe heat exchangers. Here the planned experimental and analytical approaches to receive all the required input data are described, also presenting the required test equipment briefly. Core equipment is a test rig equipped with double pipe heat exchangers, which allows the measurement of thermal and fluid flow related values and provides samples for the analysis of the fouling deposits. Furthermore, the aim of the new modeling concept is to link integral and local fouling resistances by taking into account locally varying parameters regarding the fouling layer. In order to allow for that, a recalculation of the thermal fouling resistance into a corrected version by considering heat transfer enhancing effects attempts to correlate with the mass based approach in a first step. In the end, the holistic modelling approach is presented.

List of symbols

| Symbol | Description |
|--------|-------------|
| A | Heat transfer surface, m² |
| d | Tube diameter, m |
| k | Overall heat transfer coefficient, W m⁻² K⁻¹ |
| k⁺ | Roughness height, m |
| k⁺⁺ | Roughness parameter, – |
| l | Local position, m |
| L | Tube length, m |
| mʳ | Fouling mass per unit area, kg m⁻² |
| Nu | Nusselt number, – |
| p | Pressure, Pa |
| Pr | Prandtl number, – |
| r | Tube radius, m |
| Re | Reynolds number, – |
| Rf | Fouling resistance, m² K W⁻¹ |
| t | Time, s |
| w | Flow velocity, m s⁻¹ |
| x | Thickness, m |

Greek symbols

| Symbol | Description |
|--------|-------------|
| α | Heat transfer coefficient, W m⁻² K⁻¹ |
| Δ | Difference, – |
| ϵ | Void fraction, porosity, – |
| ε₅₀ | Ratio of Nusselt numbers, – |
| λ | Thermal conductivity, W m⁻¹ K⁻¹ |
| ν | Kinematic viscosity, m² s⁻¹ |
| ξ | Friction coefficient, – |
| ρ | Density, kg m⁻³ |

Subscripts

| Subscript | Description |
|-----------|-------------|
| air | Air |
| 0 | Clean surface |
| f | Fouling |
| gyp | Gypsum |
| H₂O | Water |
| i | Inner |
| ind | Induction |
| ini | Initiation |
| m | Mean |
| mass | Mass based |
| o | Outer |
| th | Thermal |
w Tube wall
ξ Friction
ω Acceleration

1 Introduction

Fouling on heat exchanger surfaces is a severe issue in the chemical and process industry. Negative effects comprise of higher energy costs, additional investment for the oversizing of apparatus, down times for cleaning and accelerated corrosion [1, 2]. Therefore, fouling has been a subject for scientific investigations for decades [3] and was already described as the major unresolved problem in heat transfer [4]. A fundamental approach to model the fouling process was introduced in the 1950s by Kern and Seaton [5] which was the basis for most of the fouling models developed afterwards [3].

One of the most rife deposition mechanism is crystallization fouling. In general, this fouling process can be divided into nucleation, growth, adhesion, removal and aging [6]. Figure 1 shows the three consecutive phases which typically occur when evaluating the time-dependent fouling behavior: i) the initiation phase, ii) the roughness controlled phase and iii) the crystal growth phase [7]. The first two make up for the induction phase. In this phase first crystals are formed on the surface, but initially with no influence on heat transfer. With increasing crystal size and coverage of the heat transfer surface the surface roughness due to the deposit leads to an enhanced heat transfer resulting in an apparent negative thermal fouling resistance. The roughness effect remains constant from this point on while the single crystal clusters cross-link and a dense bottom layer with increasing thickness is formed and deteriorates heat transfer noticeably [8]. This negative effect is superimposed by the co-occurring enhancement of the fouling-sided heat transfer. Particularly with regard to the fouling deposition in tubes this is attributed to two effects: (i) the roughness and (ii) the constriction of the flow cross-section with the resulting acceleration of flow [8]. On the other hand roughness and constriction result in an increased pressure drop, already appearing in the induction phase, see Fig. 1. These imposing trends require a distinction of the term fouling resistance into a thermal and a mass based fouling resistance. The inlet and outlet temperatures of a heat exchanger determine the integral thermal fouling resistance $R_{f, \text{th, int}}$ while the pressure drop determines the hydraulic behavior and the integral mass based fouling resistance $R_{f, \text{mass, int}}$ [7].

Both, in the design phase of a new heat exchanger as well as for the assessment of an equipment in a fouling service, fouling behavior is typically regarded as an integral phenomena, e.g. considering the heat balance or pressure drop of an apparatus. Local phenomena as the uneven distribution of fouling deposits inside a heat exchanger are rarely described in literature and are usually not taken into account for modeling [8–12]. However, local differences found by optical inspection at different axial positions of a fouled heat exchanger tube indicate a considerable influence on the heat exchanger performance, see Fig. 2 [12]. The commonly used integral thermal fouling resistance is based on the heat exchanger’s heat balance and therefore not able to reveal such local differences [9].

Experimental investigations of local thermal fouling resistances of CaSO₄ deposits inside a double-pipe heat exchanger were presented by Goedecke et al. [9] and Albert [13]. Both found, that the integral assessment of the fouling process is not suitable to detect local processes or to identify the proceeding sub-processes and their interactions and to explain the determining mechanisms. Therefore, both a local and a time-resolved acquisition, analysis and modeling is essential for a deeper insight into the fouling process. Figure 3 shows the core structure of the new holistic modeling concept. A distinction is made between three types of fouling resistances: (i) the thermal, (ii) the corrected and (iii) the mass based fouling resistance. All fouling resistances are considered by an integral and a local approach. A direct correlation between local thermal fouling resistances, based on local temperature measurements, and the integral thermal fouling resistance, based on the integral heat balance, is not possible [9]. Therefore, they are linked by a crossed arrow. Furthermore, thermal fouling resistances cannot be correlated directly with mass based fouling resistances. Yap et al. [14] investigated the link between the thermal and hydraulic behavior of a heat exchanger subjected to crude oil fouling and outlined that the relationship is not straightforward if roughness and tube constriction need to be considered. Albert et al. [8] developed a model to correct the integral thermal fouling resistance by taking roughness and constriction effects on heat transfer into account. The resulting corrected fouling resistance provides the connecting link between thermal and mass based fouling resistances. To calculate corrected local fouling...
resistances this model will be extended and integrated into a local consideration, see Fig. 3. A similar detailed modeling approach considering the impact of roughness and aging on the thermal fouling related to crude oil fouling was presented by Coletti et al. [15].

In order to provide better understanding of the methodology and the interrelations within the new modeling concept section 2 describes the fundamental model equations. In addition, the derivation of these equations is described briefly including the assumptions made for their application. This represents the basis of the approach which is presented entirely in section 3.1. Completing the overall picture of the new approach, the procedural methods to generate and provide the input data required for modeling are presented in section 3.2.

2 Mathematical basics of the model

A general mathematical description of the thermal and the mass based fouling resistance is given in this section. The key parts of the fouling model to consider topographic and constriction effects on heat transfer which was developed by Albert et al. [8] to provide corrected fouling resistances are presented afterwards. In addition, the procedure to calculate material/physical properties of the deposit which affect the mass based fouling resistance is described.

2.1 Fouling resistances

Basically, fouling can be quantified by two different approaches to describe the fouling resistance: the thermal and the mass based fouling resistance [16]. The thermal fouling resistance quantifies the change in heat transfer due to a growing fouling layer and is formed by the difference of the overall heat transfer coefficients with a fouled ($k_f$) and a clean ($k_0$) heat transfer surface. Often fouling occurs only on one side of the heat transferring wall of a heat exchanger, which allows to describe $R_{f,th}$ for flat surfaces and thin-walled tubes ($r_0/k_i \approx 1$) by

$$R_{f,th} = \frac{1}{k_f} - \frac{1}{k_0}. \quad (1)$$

Please note, Eq. (1) does not consider occurring changes of the fouling-sided film heat transfer coefficient due to the surface roughness of the fouling layer and the constriction of the flow cross-section.

Assuming a fouling layer with the thickness $x_f$ is uniformly distributed over the heat transfer surface and has a constant density $\rho_f$ and thermal conductivity $\lambda_f$, the mass based heat transfer resistance of the fouling layer is given by

$$R_{f,mass} = \frac{x_f}{\lambda_f} = \frac{m_f}{\rho_f \lambda_f} \quad (2)$$

with the deposited solid mass per unit area

$$m_f = \rho_f x_f. \quad (3)$$

In contrast to Eq. (1) roughness and constriction have no influence and mass based fouling resistances are always positive. Instead, a homogeneously formed fouling layer all over the heat transfer surface is implied, which rarely occurs in practice [14].
2.2 Topographic effects on heat transfer

The influence of rough surfaces on heat and mass transfer has been a subject of intense research activities in particular regarding the efficiency improvement of heat exchangers [17–21]. The roughness effect on heat transfer is determined by shape, size and orientation of the roughness elements and on their distribution over a heat transfer surface [21]. Furthermore, the roughness effects of different fouling types are partially described in literature [8, 15, 22, 23]. However, a general characterization of the surface structure in case of a crystalline fouling layer, i.e. in terms of roughness parameters, is not existing [23]. For determining the influences of crystallization fouling on heat transfer Albert et al. [8] carried out experimental and theoretical investigations. Fouling experiments were conducted with a test rig equipped with two double-pipe heat exchangers operated in countercurrent flow with calcium sulphate fouling inside the inner tubes. Results showed that the change of the topography at the interphase crystal layer/salt solution, respectively heat exchanger surface/salt solution, affects the fluid dynamic as well as the heat transfer behavior. The turbulence enhancement at the boundary layer increases the heat transfer coefficient \( \alpha \). This is usually neglected in calculations of the fouling resistance \( R_f \). Therefore, a model was developed for taking these effects into account when quantifying the thermal fouling behavior [8]. The model equations are presented here in short.

The overall heat transfer coefficient through a tube wall with fouling on the inside in case of thin layers \((A_{i.f} = A_i)\) is given by

\[
\frac{1}{k_f} = \left( \frac{A}{\alpha_i A_i} + \frac{x_{w} A}{\lambda_{w} A_{m}} + \frac{A}{\alpha_o A_o} \right) R_f + R_{f,th}(t) \quad \text{with} \quad R_f(t) = \frac{x_{i.f} A}{\lambda_{i.f} A_i} \tag{4}
\]

Equation (4) shows that any increase of the heat transfer coefficient \( \alpha_i \) leads to a compensation of the thermal fouling resistance \( R_{f,th} \). To consider this change in heat transfer separately, Eq. (4) can be transformed to

\[
\frac{1}{k_f} = \frac{A}{\alpha_i A_i} + R_{f,th}(t) + \frac{1}{k_0}; \quad \text{with} \quad \frac{1}{k_0} = \frac{x_{w} A}{\lambda_{w} A_{m}} + \frac{A}{\alpha_o A_o}. \tag{5}
\]

Assuming that only the surface roughness due to deposition causes a change of the heat transfer coefficient \( \alpha_i(t) \), the friction coefficient \( \xi_f(t) \) is used to characterize the roughness and to describe the heat transfer enhancement and is determined by the change of flow resistance [8]:

\[
\alpha_i(t) = \xi_f(t) \alpha_i ; \quad \text{or} \quad Nu_w = \frac{\xi_f(t)}{\xi_0} Nu_0 \tag{6}
\]

The index “0” relates to the clean condition of the heat transfer surface at \( t = 0 \) s. Combining Eqs. (5) and (6) results in a new fouling model. The dependency of heat transfer from flow resistance \( \xi_f \) is considered by the term \( \varepsilon_{Nu, \xi} = Nu/NU_0 \) in order to take heat transfer enhancement due to fouling into account:

\[
R_{f,th}(t, \xi) = \frac{1}{k_f} - \frac{A}{(\alpha_i(t) \xi) A_i} - \left( \frac{x_{w} A}{\lambda_{w} A_{m}} + \frac{A}{\alpha_o A_o} \right) \tag{7}
\]

Albert et al. [8] applied four different heat transfer correlations from Nunner [24], Burck [25], Hughmark [26] and Ceylan and Kelbaliyev [27] in his fouling model to account for the increase in heat transfer on rough surfaces at turbulent flow.

2.3 Constriction effects on heat transfer

With increasing deposition a compact crystal layer builds up on the heat transfer surface. The roughness effects persist and the fouling layer reduces the free flow cross-section. Accordingly, the fluid flow is accelerated which increases the turbulence and the heat transfer likewise. This effect was also investigated by Albert et al. [8].

Figure 4 shows the assumption of a linear fouling layer built up from inlet to outlet of a heat exchanger tube. If the volumetric flow rate remains constant the flow accelerates in accordance with the increasing constriction of the cross-section along the tube. Hence, the flow turbulence and the effect on heat transfer varies depending on the local position.

In order to consider the dependency of heat transfer from the constriction at different local positions the well-known approach of Gnielinski for turbulent pipe flow is used [28, 29]:

\[
Nu_w = \frac{(\xi/8) Re Pr}{1 + 12.7 \sqrt{\xi/8} (Pr^{2/3} - 1)} \left[ 1 + \frac{1}{3} \left( \frac{d_{i.f}}{l} \right)^{2/3} \right] \tag{8}
\]

with

\[
\xi = (1.8 \log_{10} Re - 1.5)^2 \quad \text{and} \quad Re = \frac{w_I d_{i.f}}{\nu} \tag{9}
\]

Here \( d_{i.f} \) is the diameter of the constricted cross-section, \( l \) is the corresponding local position and \( w_I \) is the flow velocity which results from the constriction at that local position. Albert et al. [8] used the idealized deposit distribution according to Fig. 4 with knowing the constriction at the tube outlet to calculate an integral averaged value of the increased Nusselt number. More precise local results can be obtained if the exact axial distribution of the fouling layer is known. Subsequently, the improvement of heat transfer is defined by the ratio of the Nusselt numbers with flow acceleration \( Nu_w \) and without constriction \( Nu_0 \):

\[
\varepsilon_{Nu, w} = \frac{Nu_w}{Nu_0} \tag{10}
\]
$Nu_0$ is calculated in accordance with Eqs. (8) and (9) by applying the original tube diameter $d_{i,0}$ and the corresponding flow velocity $w_{i,0}$.

### 2.3.1 Combination of roughness and constriction effects

Substitution of Eqs. (8) to (10) into Eq. (7) yields a fouling model which considers both roughness and constriction effects on heat transfer [8].

$$R_f(t, \xi) = \frac{1}{k_f} \frac{A}{(\alpha_{i,0} \in Nu, \xi \in Nu_0) A_i} \left( \frac{x_w A}{\lambda_w A_m} + \frac{A}{\alpha_o A_o} \right)$$  \hspace{1cm} (11)

By applying the different heat transfer correlations of Nunner [24], Burck [25], Hughmark [26] and Ceylan and Kelbaliyev [27] corrected integral fouling resistances were calculated and compared to fouling resistances based on the assumption of a constant heat transfer [8]. It was shown that the approaches of Nunner [24] and Hughmark [26] are the most promising ones for considering roughness and constriction effects on integral heat transfer, presented in Fig. 5. Hence, these correlations will be used when adapting Eq. (11) to calculate corrected local fouling resistances.

### 2.4 Structural properties of the deposit

The internal structure of the fouling deposit affects the heat flux within the layer and determines the mass based fouling resistance, see Eq. (2). The structure depends on the fluid dynamic conditions, e.g. with increasing Reynolds number the calcium sulfate layer becomes denser and the crystal size decreases [30]. Furthermore, the interdependent material properties porosity $\epsilon$, density $\rho_f$ and thermal conductivity $\lambda_f$ are essential to determine the mass based fouling resistance, see Eq. (2). In accordance with Brahim [31] the thermal conductivity of CaSO$_4$ deposits is calculated by averaging two alternative approaches. The solid matrix and the void (porosity) of the fouling layer can be considered as resistances in series, see Eq. (13), or as resistances in parallel, see Eq. (14) [32]. Therefore, the thermal conductivity of water $\lambda_{H_2O}$ and gypsum (CaSO$_4$·2H$_2$O) $\lambda_{gyp}$ is used.

$$\lambda_f = \frac{\lambda_{f,1} + \lambda_{f,II}}{2}$$  \hspace{1cm} (12)

$$\lambda_{f,1} = \epsilon \cdot \lambda_{H_2O} + (1-\epsilon) \cdot \lambda_{gyp}$$  \hspace{1cm} (13)

$$\frac{1}{\lambda_{f,II}} = \frac{\epsilon}{\lambda_{H_2O}} + \frac{1-\epsilon}{\lambda_{gyp}}$$  \hspace{1cm} (14)
A mean value for the thermal conductivity of 1.2 W m$^{-1}$ K$^{-1}$ was determined for a CaSO$_4$ fouling layer produced in an electrically heated flow channel, see Fig. 6 [33]. This value results from a mean layer porosity of 10% and the thermal conductivity of pure gypsum ($\lambda_{\text{gyp}} = 1.3$ W m$^{-1}$ K$^{-1}$) [34].

Furthermore, Fig. 6 shows that four different sublayers were identified, which differ in structure, color and hardness. Therefore, material properties of the layer depend on the local radial position within the fouling layer as well as on the total layer thickness. An increasing total layer thickness leads to an increase of the density in the sublayers near the heat transfer wall. [31, 35]

In accordance with Eqs. (15) and (16) the density of a fouling layer is also directly related to the porosity and is calculated with the assumption of air or water within the void fraction:

\[
\rho_f = \epsilon \cdot \rho_{\text{air}} + (1-\epsilon) \cdot \rho_{\text{gyp}}
\]  
\[ (15) \]

\[
\rho_f = \epsilon \cdot \rho_{\text{H}_2\text{O}} + (1-\epsilon) \cdot \rho_{\text{gyp}}
\]  
\[ (16) \]

With the density of pure gypsum ($\rho_{\text{gyp}} = 2320$ kg m$^{-3}$) and a mean porosity of around 50% Hirsch [35] calculated mean densities of $\rho_f = 1100$ kg m$^{-3}$ for dry CaSO$_4$ layers and around $\rho_f = 1600$ kg m$^{-3}$ for moisture deposits.

### 3 Composition of the new holistic approach

The combination of different fouling models shall serve a holistic description of the fouling behavior by taking into account local variations and hence give the opportunity to predict fouling deposition precisely. This approach is developed on the basis of investigations with CaSO$_4$ crystallization fouling.

The basic structure of the new approach was introduced in Fig. 3. Figure 7 shows the entire composition of the modeling concept and gives an overview of all required parameters to model the participating fouling resistances. Measured variables are displayed in rectangles and provided by applying different experimental methods. Calculated variables are displayed in rectangles with rounded corners and are determined by using existing calculation procedures. Filled arrows indicate a direct dependency between fouling resistances. Dotted arrows indicate the missing correlation between fouling resistances. The analytical approach of the model is presented in the following. All experimental methods to provide the required variables are described afterwards.

#### 3.1 Analytical approach

The holistic model aims to link corrected with mass based fouling resistances as well as integral and local fouling resistances, see Fig. 7. The fouling resistances are based on different approaches by using various variables as input data and are described shortly in the following:

1. The **integral thermal fouling resistance** results from the temporal change of the integral heat transfer using Eq. (1). Therefore, inlet and outlet temperatures of a heat exchanger need to be measured.
2. According to Eq. (3) the **integral mass based fouling resistance** is determined by mean values of the deposit’s thickness, mass, density and thermal conductivity.
3. The **corrected integral fouling resistance** is calculated with the model of Albert et al. [8] based on the integral thermal fouling resistance, see Eq. (11). The mean layer thickness, the mean flow velocity and the integral friction coefficient are used.
4. In order to determine **local thermal fouling resistances** local temperatures measured at the wall and in the heating medium are used to quantify local overall heat transfer coefficients. The calculation process was presented by Schlüter et al. [12].
5. The calculation of **local mass based fouling resistances** is carried out by applying a local consideration of Eq. (3). Accordingly, the local material properties density and thermal conductivity are required, which are calculated...
with Eqs. (12) to (15). Furthermore the local layer thickness and/or the local fouling mass is required. This variables result from experiments, see section 3.2.

6. The corrected local fouling resistance is based on the local thermal fouling resistance and determined in accordance with Eq. (11), but here with a local consideration. Therefore, the local constriction due to the layer thickness, the local flow velocity and the local friction coefficient are used.

After the calculation procedure the corrected and mass based fouling resistances can be correlated. The experimental data from investigations with calcium sulfate and subsequently calcium carbonate will be integrated in a simulation for validating the holistic model in case of the most typical fouling crystallization products in cooling water applications. In longer term the universal applicability of the model regarding other fouling types needs to be examined. In general, the fundamental influencing factors deposition mass, layer thickness and layer structure like compactness and roughness as well as the resulting heat transfer will vary for each fouling type but have the same significance for modeling.

3.2 Experimental methods

This section presents a short description of the fouling test rig to produce crystalline deposits as well as all additional experimental methods to provide input data for modeling the different fouling resistances. The following description is segmented with regard to the square boxes in Fig. 7. First experimental results by applying these methods with CaSO₄ fouling was presented by Schlüter et al. [12].

3.2.1 Integral heat balance and pressure drop

Figure 8 shows the test rig which is used for fouling experiments [12]. The core components of the experimental setup are two identical double-pipe heat exchangers made of stainless steel (HX1 and HX2) with inner tube dimensions of 20 × 2 × 2000 mm. An aqueous salt solution flows on the tube side of both test sections and hot water passes through the shell side in counterflow. Hence, crystallization fouling is produced on the tube side. A plate and frame heat exchanger (HX3) in conjunction with an automatic valve control the heat exchanger inlet temperatures of the salt solution using cooling water from an on-site water circuit. Shell side and tube side inlet and outlet temperatures of both test sections are measured with type K thermocouples determining the integral heat balance and are used to calculate integral thermal fouling resistances, see Eq. (1). In addition, differential pressure transducers measure the integral pressure drop of both heat exchangers to monitor the integral fouling behavior.
3.2.2 Local shell side and local wall temperatures

Heat exchanger HX1 is equipped with six thermocouples (TIR) at different axial positions on the shell side and along the wall of the inner tube for local temperature measurements and the determination of the local heat transfer. In addition to the shell side thermocouples heat exchanger HX2 is equipped with a fiber optic sensor to determine local temperatures along the wall of the inner heat exchanger tube, see Fig. 9. The thermocouples are installed in the depicted manner to allow for a high axial resolution of temperature measurements towards the hot end of the heat exchanger where most deposition takes place. The fiber-based measurement system features an active monitoring unit which is connected to the passive sensor fiber (Luna, ODiSI A50). The monitoring unit transmits light into the fiber from a broadband source. Characteristics of the light traveling within the fiber are modified as a function of temperature. These changes are detected in the backscattered light which is later collected by the monitoring unit, analyzed and then converted into temperature data. This technique provides a higher resolution of the axial temperature profile and a more precise description of the local...
fouling behavior compared to the usage of thermocouples only. The sensor is inserted in a notch of 1 mm depth in the tube wall. Along the fiber sensor temperature variations can be detected with an axial resolution up to 10 mm. Since the application of this measuring technique is a novel approach for local fouling investigations, heat exchanger HX1 serves as validation for the measurements. The calculation of local thermal fouling resistances on the basis of local temperatures is described by Schlüter et al. [12].

Besides the thermal investigations various other methods provide essential data for modeling the corrected and mass based fouling resistances according to Fig. 7. The methods to determine the measured variables are described briefly in the following.

### 3.2.3 Fouling layer volume, thickness, roughness and mass

To investigate the axial distribution of the tube side deposit regarding its volume, mass, thickness and roughness the fouled heat exchanger tube is dismounted after a fouling experiment. Figure 10 shows an experimental setup designed to examine the volume of the deposit by applying the principle of communicating tubes. Water is filled incrementally over a funnel into a translucent tube and the fouled test tube. Liquid levels are noted and compared with the liquid levels obtained by using a clean test tube after adding the same volume of water. Hence, the water displaced by the deposit inside the tube is determined locally and integrally along the heat exchanger tube. The measured volume of water corresponds to volume of the fouling layer.

Subsequent to the volumetric investigation, the fouled test tube is cut into ten segments of 200 mm length by using a tube cutter. Photographs of each cross-section of all segments are taken with a digital camera. The images are analyzed with a suitable image analysis software (ImageJ, Wayne Rasband, NIH) to determine the thickness and roughness of a local fouling layer at each accessible axial position. The program can calculate the area of different circular shapes or freehand selections corresponding to layer thickness or roughness of the respective fouling deposit. With knowing the free tube area, thickness and roughness can be calculated. Subsequently, the porosity of a local deposit is determined by combining the results regarding the local volume and the local layer thickness. The thermal conductivity and density of the deposit are calculated in a next step according to Eqs. (12) and (16) with the assumption of water within the void. Finally, weighing the tube segments provides the axial distribution of the deposited mass per unit area.

### 3.2.4 Local pressure drop measurement

Local pressure drops have to be determined in order to calculate local friction coefficients, see Fig. 6. Inline measurements with pressure transducers inserted in the tube wall are not practical due to the crystalline deposit building up there.
Hence, a new experimental setup equipped with a moveable Prandtl probe was developed and will be used to measure the pressure drop within the ten tube segments individually. Figure 11 shows that the measured pressure drops of the tube segments have to add up to the total pressure difference which is measured integrally with the inline differential pressure transducer of the fouling test rig, see Fig. 8. In addition, the Prandtl probe measures the dynamic pressure in each tube segment and thereby the increase of the local velocity due to the constriction can be calculated.

4 Conclusion

This work presents a new holistic approach to model and link fouling resistances as well as showing the planned experimental and analytical way to receive all the required input data. A distinction is made between six target values: thermal and mass based as well as corrected fouling resistances, all considered locally and integrally.

The integral values are determined by the conventional way of measuring the integral pressure drop and integral heat balance of the fouled heat exchanger tubes. More experimental and analytical effort is required for investigating local fouling resistances. For the thermal approach local thermocouples and a fiber sensor are applied to measure local temperatures and determine local overall heat transfer coefficients. More parameters like the local constriction, local mass as well as local material parameters, e.g. density and thermal conductivity, are used for modeling local mass based fouling resistances. A novel experimental layout will be used for measuring local pressure drops inside fouled tube segments with a Prandtl probe and determining local friction coefficients and local flow velocities which are needed for calculating the corrected local fouling resistances. After modeling the target values the link between the different fouling resistances will be investigated by taking all presented local parameters into account. A correlation between the different fouling resistances is essential for being able to simulate the fouling process entirely.

After validating the model with CaSO4 and CaCO3 deposits, which are the most typical crystallization products in cooling water applications, the universal applicability of the model regarding other types of fouling needs to be examined. Finally, the goal of modeling and simulation is to allow for extracting local fouling parameters only by having knowledge about the integral heat transfer and pressure drop behavior in combination.

With introducing the new modeling concept this contribution is the first part of an extensive work. Experimental results and first modeling results for comparison and validation will be shown in a following second paper which deals with the local part of the introduced holistic modeling concept.

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Compliance with ethical standards

Conflict of interest The authors declare that there is no conflict of interest.

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