Evidence for large-scale excesses associated with low H\textsubscript{i} column densities in the sky

I. Dust excess

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ABSTRACT

Where dust and gas are uniformly mixed, atomic hydrogen can be traced through the detection of far-infrared (FIR) or UV emission of dust. We considered, for the origin of discrepancies observed between various direct and indirect tracers of gas outside the Galactic plane, possible corrections to the zero levels of the Planck-HFI detectors. We set the zero levels of the Planck High Frequency Instrument (HFI) skymaps as well as the 100 µm map from COBE/DIRBE and IRAS from the correlation between FIR emission and atomic hydrogen column density excluding regions of lowest gas column density. A modified blackbody model fit to those new zero-subtracted maps led to significantly different maps of the opacity spectral index $\beta$ and temperature $T$ and an overall increase in the optical depth at 353 GHz $\tau_{353}$ of 7.1 $\times$ 10\textsuperscript{-7} compared to the data release 2 Planck map. When comparing $\tau_{353}$ and the HI column density, we observed a uniform spatial distribution of the opacity outside regions with dark neutral gas and CO except in various large-scale regions of low $N_{\text{H\textsubscript{i}}}$ that represent 25% of the sky. In those regions, we observed an average dust column density 45% higher than predictions based on $N_{\text{H\textsubscript{i}}}$ with a maximum of 250% toward the Lockman Hole region. From the average opacity $\sigma_{e353}=(8.9\pm0.1)\times10^{-27}$ cm\textsuperscript{2} we deduced a dust-to-gas mass ratio of 0.53 $\times$ 10\textsuperscript{-2}. We did not see evidence of dust associated to a Reynolds layer of ionized hydrogen. We measured a far-ultraviolet isotropic intensity of 137\textsuperscript{\pm}15 photons s\textsuperscript{-1} cm\textsuperscript{-2} sr\textsuperscript{-1} \textcircled{\textmu}m\textsuperscript{-1} in agreement with extragalactic flux predictions and a near-ultraviolet isotropic intensity of 378\textsuperscript{\pm}45 photons s\textsuperscript{-1} cm\textsuperscript{-2} sr\textsuperscript{-1} \textcircled{\textmu}m\textsuperscript{-1} corresponding to twice the predicted flux.

Keywords: Interstellar medium (847) – Dust continuum emission (412) – Interstellar thermal emission (857) – Interstellar emissions (840) – Galaxy structure (622) – Ultraviolet surveys (1742)

1. INTRODUCTION

The hydrogen is the main component of the interstellar medium (ISM) gas. The neutral H\textsubscript{i}, both in the cold and warm phases, is traced by its radio 21 cm line radiation, and its column density $N_{\text{H\textsubscript{i}}}$ can be extracted from the 21 cm line radiation temperature often assuming a uniform spin temperature. While there is no direct large-scale observation of the warm ionized medium (WIM), its spatial distribution can be deduced from the density distribution of free electrons obtained from dispersion measures of pulsars with known distances. H\textsubscript{2} cannot be observed directly in its cold phase but should have the same distribution as its main collisional partner, the carbon-12 monoxide (CO), observed through its 2.6 mm J=1$\rightarrow$0 line. Interstellar gas is also detected indirectly by high-energy $\gamma$-ray emission produced by interactions of energetic cosmic rays (CR) with the gas nucleons mainly through the decay of secondary particles produced in hadron collisions. Once separated from other $\gamma$-ray contributors and deconvolved from CR intensity and production cross section, a complete census of interstellar hadrons can be achieved with, however, a worse angular resolution than radio and millimeter surveys.

The dust, mainly heated by far-ultraviolet (FUV) photons, radiates from far-infrared (FIR) to microwave frequencies. High-resolution observations at those frequencies provide its column density after disentangling from...
additional sky emissions and after correcting for dust temperature. Alternatively dust column density can be deduced from reddenings of background stars at optical wavelengths.

In the ISM collisions between dust grains and gas particles lead to a coupling between the gas and the dust. In the diffuse phases of the local ISM, we expect the dust spatial distribution to correlate with that of the gas. In principle, tracers of gas and tracers of dust should also spatially correlate.

While templates of dust column density mostly correlate with templates of $N_{\text{H}}$ (Boulanger & Perault 1988; Planck Collaboration et al. 2014a) discrepancies exist. In the outer envelopes of molecular clouds where the CO molecule is strongly affected by UV photodissociation, $\text{H}_2$ can exist without CO being present (van Dishoeck & Black 1988; Wolfire et al. 2010; Glover & Mac Low 2011). This effect, in addition to optically thick H I and nonuniformity of the spin temperature, lead to a large quantity of Dark Neutral Medium (DNM) gas not traced by H templates but observed through the combination of their dust and γ-ray emissions (Grenier et al. 2005; Planck Collaboration et al. 2011; Remy et al. 2018a). Independently from DNM, toward dense CO clouds, the mantle accretion on the dust grains and the formation of grain aggregates enhance dust FIR emissivity (Köhler et al. 2015; Remy et al. 2017).

At low column density $N_{\text{H}_1}$ of a few $10^{20}$ cm$^{-2}$, those issues are not relevant, and the spatial distribution of dust column density extracted from FIR observation should follow accurately that of $N_{\text{H}_1}$. In Planck Collaboration et al. (2014b) (hereafter Planck XI), Figure 21 shows the correlation between those two templates. The uncertainty of each point being notably smaller than the error bar displaying the standard deviation in the $N_{\text{H}_1}$ bin, we observe a systematic departure from linearity for $N_{\text{H}_1} > 2\times10^{20}$ cm$^{-2}$. In this figure, for low $N_{\text{H}_1}$ from 2 to $3\times10^{20}$ cm$^{-2}$, $N_{\text{H}_1}$ and the dust column density are still correlated but with a larger proportionality coefficient (opacity) in addition to a strong offset. The departure from a simple linear scaling between low $N_{\text{H}_1}$ and FIR dust emission has been the subject of numerous studies emphasizing the linear correlation below $N_{\text{H}_1}$ of a few $10^{20}$ cm$^{-2}$ and attributing the departure at intermediate column density to the hidden presence of H$_2$ or to dust overemission (Boulanger et al. 1996; Planck Collaboration et al. 2014a; Liszt 2014a,b; Lenz et al. 2017; Murray et al. 2020).

The larger value of the opacity (than the one quoted in Planck XI) observed for $N_{\text{H}_1}$ between 2 and $3\times10^{20}$ cm$^{-2}$ agrees with that needed to produce a DNM map in agreement with the Fermi Large Area Telescope (LAT) γ-ray diffuse observations (Figure 4, top of Acero et al. (2016)). Increasing the dust opacity implies lowering the zero levels to remain consistent with Planck data. This has led us to investigate a potential issue with the zero levels of the Planck detectors. Planck zero levels (offsets + cosmic infrared background, hereafter CIB) were calculated as the γ-intercept of the linear correlation between dust FIR and $N_{\text{H}_1}$ at lowest $N_{\text{H}_1}$ (Planck XI). It assumes that only a small amount of dust exists apart from the one associated with H I. Boulanger et al. (1996) and Arendt et al. (1998) validated this hypothesis. Arendt et al. (1998) excluded any contribution from dust associated to H$_2$ and estimated a maximum of 20% for the contribution of H II traced by pulsar dispersion measure and H$_\alpha$ observations. Still, the ionized gas column density that cannot be measured on large scales is uncertain. In addition one cannot exclude that the dust emissivity could increase in very diffuse H I.

In this work, we therefore derived the zero level of the Planck High Frequency Instrument (HFI) at 857 GHz outside the regions of lowest $N_{\text{H}_1}$ and in a wide region where the γ-ray data is consistent with the total gas column densities being the observed $N_{\text{H}_1}$ values. Using the new zero levels, we recalculated the dust optical depth at 353 GHz $\tau_{353}$ and we compared it to $N_{\text{H}_1}$. Since dust also scatters UV photons, we verified that the new optical depth agrees with FUV and near-ultraviolet (NUV) observations.

2. DATA

2.1. Planck-HFI

We downloaded the Planck-HFI skymaps from the Planck Legacy Archive\footnote{http://pla.esac.esa.int/pla/#home}. We selected the 2015 data release 2 (PR2) for a better comparison with the work of Planck Collaboration et al. (2016) (hereafter Planck XLVIII). No major difference was observed with the release 3 version. We made use of the generalized needlet internal linear combination (GNILC) products (Planck XLVIII) voided of CIB anisotropy and recommended for dust studies. As similarly done in Planck XI and in Planck XLVIII, we utilized the 3 maps associated to the highest HFI frequencies: 353, 545, and 857 GHz\footnote{COM\_CompMap\_Dust-GNILC-F353,2048,R2.00.fits, COM\_CompMap\_Dust-GNILC-F545,2048,R2.00.fits, COM\_CompMap\_Dust-GNILC-F857,2048,R2.00.fits}. We did not measure any significant improvement when adding to the fit lower-frequency maps. Following Planck XLVIII, we also used half-mission maps to derive the instrumental noise.
Figure 1. Thermal spectrum of a pixel located in the Lockman Hole (lower curve) and at $l=45^\circ$ and $b=30^\circ$ (higher curve). We show the intensity at 100 µm and 857, 545, 353 GHz and associated uncertainties together with the best modified blackbody fit (black lines).

Since HFI spectral responses are not uniform, we must account for the intensity variation within a detector bandpass due to the signal spectral profile. We obtained those color-correction coefficients from dedicated software routines provided by the Planck collaboration.

We transformed all HFI-Planck intensity maps as well as other skymaps used in this work into HEALPix standard (Górski et al. 2005) with a resolution parameter $N_{side} = 512$ corresponding to mean pixel spacing of 0.11°.

2.2. 100 µm

100 µm is a crucial wavelength for the fit of a modified blackbody (MBB) spectrum. The associated skymap intensity corresponds for $T \sim 20$ K to the only point in the spectral fit not located on the same side of the modified Planck curve as the Planck-HFI frequencies (Figure 1). Its value mostly drives the temperature parameter. Based on Planck XI and Planck XLVIII we choose to use the hybrid map combining at large scale the map of Schlegel et al. (1998) (itself a composite of COBE/DIRBE and IRAS) and at smaller scale the IRIS version of IRAS (Miville-Deschênes & Lagache 2005). We downloaded this map from the Planck Legacy Archive website. We approximated the color correction of this composite map with coefficients given by the COBE/DIRBE collaboration.

2.3. DIRBE

While we did not use the COBE/DIRBE maps for the MBB fit because of their low spatial resolution, we used them for calibration purposes. We utilized the maps at 140 and 240 µm. Those maps, as the previous ones, have the zodiacal light and point sources removed; the intensity was color-corrected with the dedicated coefficients.

2.4. $N_H$

As we mentioned, under certain conditions, the dust optical depth derived from far-infrared surveys can be a good tracer for the total hydrogen column density $N_H$. We derived the atomic hydrogen column density $N_{HI}$ from the HIIPI survey (HI4PI Collaboration et al. 2016) of brightness temperature ($T_B$) assuming an optically thin limit: $N_{HI}(l, b) = 1.83 \times 10^{18} \text{ cm}^{-2} \int T_B(l, b, v) dv$. In this study, we masked pixels with DNM and verified that this mask also covers all the molecular clouds.

The Doppler shifts of the H I lines have provided the kinematic Galactocentric distances of the atomic and molecular gas. We used this information to partition the gas column density map into several components as in Remy et al. (2017) and separated 11 Galactocentric annuli maps. We used this partition only for an accurate visualization of the low-latitude regions of our residual maps, not in the derivation of the zero levels or of the MBB parameters. We removed high velocity clouds from the maps. Finally, to calculate the residuals between dust and gas, we corrected the modeled gas distribution for the Galactic metallicity gradient which affects the dust abundance. We used the average abundance of O and Si (Cescutti et al. 2007; Kubryk et al. 2015) normalized to 1 for the solar neighborhood.

3. INITIAL ESTIMATES OF THE ZERO LEVELS OF FIR MAPS

3.1. Method

In this section, we describe our method to obtain initial estimates of the zero levels of the GNILC dust intensity skymaps used in this work. The zero levels include both the intrinsic detector offsets and the spatially uniform CIB monopole.

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3 https://wiki.cosmos.esa.int/planck-legacy-archive/index.php/Unit_conversion_and_Color_correction
4 IRIS_combined_SFD_really_nothole_nosource_A_2048.fits
5 https://lambda.gsfc.nasa.gov/data/cobe/dirbe/ancil/colcorr/DIRBE_COLOR_CORRECTION_TABLES.ASC
6 https://lambda.gsfc.nasa.gov/product/cobe/dirsems_data_get.cfm
Considering that contamination of the dust thermal emission by free-free emission decreases at high frequencies and that the 857 GHz intensity better correlates with gas column densities than the 100 µm intensity (see Figure 5 of Planck XI), we have first correlated $I_{857\text{GHz}}$ and $N_{\text{H}_1}$ in a mask that we called Pegasus-Aquarius corresponding to the region of longitude $0^\circ$ to $180^\circ$ and of latitude $-60^\circ$ to $-15^\circ$. Building upon our experience with Fermi-LAT interstellar modeling (Casandjian 2015; Acero et al. 2016) for which we observed a good agreement between diffuse γ-rays and a model based on $N_{\text{H}_1}$ or $\tau_{353}$ in this region, the FIR intensity of dust and $N_{\text{H}_1}$ column density are linearly correlated in this region. We excluded the regions with potential contamination by H$_2$ or significant H$_1$ self-absorption (DNM). For that we compared the H$_1$ column density provided by the dust: $\tau_{353}/\sigma_{e353}$ to $N_{\text{H}_1}$ from 21 cm survey and masked regions where $\tau_{353}/\sigma_{e353} - N_{\text{H}_1} > 10^{20}$ cm$^{-2}$. To remove a possible bias related to the choice of the initial value for the opacity $\sigma_{e353}$ and $\tau_{353}$, we strongly reduced to $N_{\text{side}}=8$ the resolution of both $\tau_{353}$ and $N_{\text{H}_1}$ in the calculation of the exclusion region. We proceeded iteratively starting from an opacity $\sigma_{e353}=6.3 \times 10^{-27}$ cm$^2$ given by Planck XI and optical depth $\tau_{353}$ obtained in Planck XLVIII. We note that, while we used a lower angular resolution to estimate the extent of the region with possible H$_2$ or self-absorbed H$_1$ contamination, the resolution of the mask itself was kept at $N_{\text{side}}=512$ for the correlation studies. We show the Pegasus-Aquarius mask in the inset of Figure 2 (later).

We derived the zero levels at 545, 353 GHz, and 100 µm from a correlation of these intensities with $I_{857\text{GHz}}$ in a dedicated mask called Isothermal. In this mask, we selected pixels for which the MBB parameters $T$ and $\beta$ did not depart by more than half a standard deviation from the sky average values. This ensures a selection of pixels with rather uniform spectral parameters; it also reduces potential inter-calibration problems between the various FIR telescopes used in this work. Again we proceeded iteratively starting from the maps of $\beta$ and $T$ from Planck XLVIII. To exclude pixels with very low or high $N_{\text{H}_1}$, we required that the mask pixels have $N_{\text{H}_1}$ within $2-15 \times 10^{20}$ cm$^{-2}$. We also excluded pixels with an absolute ecliptic latitude smaller than $15^\circ$ to avoid zodiacal light contamination. We show the Isothermal mask in the inset of Figure 3 (left). For the zero level of the 100 µm map, we also used an alternative method in which we correlated directly $I_{100\mu m}$ with $N_{\text{H}_1}$. Since the correlation is poorer in the Pegasus-Aquarius mask due to thermal changes in the dust across this region (see Figure 7 later), we performed the correlation in the Isothermal mask that reduces the effect of spectral variations.

As we describe in Section 4.1, we have used these initial zero levels to fit an MBB to the intensities observed at the four frequencies in each sky pixel. The final set of zero levels was derived from the monopoles of the residual maps that compared the observations and the best-fit MBB spectra. We measured the monopole of the residuals for pixels inside a mask called Monopole for which $\tau_{353}/\sigma_{e353} - N_{\text{H}_1} < 2 \times 10^{20}$ cm$^{-2}$ to exclude potential contamination by H$_2$ or significant H$_1$ self-absorption and for pixels with an absolute ecliptic latitude larger than $15^\circ$. We show the Monopole mask in the inset of Figure 6 (top, left).

### 3.2. Initial Zero Level at 857 GHz

We first ensured that the correlation between $I_{857\text{GHz}}$ and $N_{\text{H}_1}$ is not significantly biased by the potential presence of ionized hydrogen in regions encompassed by the Pegasus-Aquarius mask. To do so, we fitted the $I_{857\text{GHz}}$ map with a linear combination of $N_{\text{H}_1}$, isotropic, and $N_{\text{H}^+}$ maps. We used two possible spatial distributions for $N_{\text{H}^+}$ column densities: one from the electron column density ($I_{\nu E2001}$) predicted by NE2001 (Cordes & Lazio 2002) and one from the H$_\alpha$ skymap intensity ($I_{H\alpha}$) (Haffner et al. 2010). The fit did not detect any contribution to the $I_{857\text{GHz}}$ intensity from these $N_{\text{H}^+}$ distributions. It set their contribution to zero with an upper limit of $5 \times 10^{16}$ cm$^{-2}$ for potential $N_{\text{H}^+}$ contamination in this region according to the NE2001 map.

In the Pegasus-Aquarius mask, $N_{\text{H}_1}$ column densities range from 2 to $5 \times 10^{20}$ cm$^{-2}$. In this regime, the gas is little shielded from UV radiation, and H$_2$ is efficiently photodissociated (Belloni et al. 2020; Wolfire et al. 2010; Snow & McCall 2006). Based on the scaling law between FUV fluorescent H$_2$ emission and FIR dust emission (Figure 14c of Jo et al. (2017)) we estimated that the average N(H$_2$) column density in the mask region is only $2 \times 10^{17}$ cm$^{-2}$. This value is consistent with the $5 \times 10^{17}$ cm$^{-2}$ average N(H$_2$) column density inferred from the Far Ultraviolet Spectroscopic Explorer (FUSE) satellite observations toward Mrk 0509, Mrk 1513, NGC 1068 (Gillmon et al. 2006), and WD 0004+330 (Lehner et al. 2003), which are all seen inside the Pegasus-Aquarius mask. We also stress that regions with column densities of CO-dark H$_2$ typically larger than $\sim 1 \times 10^{20}$ cm$^{-2}$ have been masked out in the construction of the Pegasus-Aquarius mask. By combining diffuse γ-ray data with dust optical depths (inferred from dust reddening or dust thermal emission), we have the means to detect optically thick H$_1$ or diffuse H$_2$ column densities that are not accounted for by H$_1$.
and CO line data at the transition between the atomic and molecular phases (Remy et al. 2018b). The \( N(\text{H}_2) \) column densities inferred in this CO-dark neutral interface match those seen by FUSE or those deduced from HCO+ observations (Liszt et al. 2019). These dark-gas-rich regions have been masked out so that they do not bias the \( I_{857\text{GHz}} \) and \( N_{\text{H}_1} \) correlation, hence the zero-point derivation.

In Figure 2 we represent the contours of the scatter plot of \( I_{857\text{GHz}} \) and \( N_{\text{H}_1} \) in the Pegasus-Aquarius mask. We observe a very good affine correlation for \( N_{\text{H}_1} \) larger than about 2 \( \times 10^{20} \text{ cm}^{-2} \); below this limit, we observe a break in the slope. We observe a similar break at a similar column density in Figure 21 of Planck XI. We derived and plotted the centroid position in each \( N_{\text{H}_1} \) bin with a Gaussian curve fit. For \( N_{\text{H}_1} \) larger than about 3 \( \times 10^{20} \text{ cm}^{-2} \) we observe an overemission of dust compared to what one would expect from hydrogen column density, which signals the residual presence of gas not traced by optically thin \( \text{H}_1 \) in the mask. As a consequence, there is a tail at high \( I_{857\text{GHz}} \) in most of \( N_{\text{H}_1} \) bins. To avoid any bias in the centroids’ position, we restricted the upper limit of the Gaussian fit to a value corresponding to 1.05 times the centroid position. We fitted the centroid points for \( N_{\text{H}_1} \) between 2 and 5 \( \times 10^{20} \text{ cm}^{-2} \), with a line whose y-intercept was \( I_0(857\text{GHz})=0.33\pm0.03 \text{ MJy sr}^{-1} \) which represents the first-order zero for the 857 GHz Planck-HFI. Here the uncertainty includes systematic errors through a procedure detailed in Section 4.2.

In order to color-correct the HFI maps for \( T \) and \( \beta \), we repeated this operation three times, a first time with \( T \) and \( \beta \) given by Planck XLVIII, then using the resulting MBB fit parameters for a next iteration. As already mentioned we obtained the final value of this zero level in a second step described in Section 4.1.

### 3.3. Initial Zero Levels at 545 and 353 GHz

Once the initial zero level at 857 GHz was set, it was straightforward to derive the initial zero-level value for 545 and 353 GHz maps. We correlated \( I_{857\text{GHz}} \) and \( I_{545\text{GHz}} \) (Figure 3 left), removed the zero level of \( I_{545\text{GHz}} \) and then correlated \( I_{545\text{GHz}} \) and \( I_{353\text{GHz}} \) (Figure 3 right) in the Isothermal mask. We obtained a very good correlation, and extracted the values of \( I_0(545\text{GHz})=0.24\pm0.01 \text{ MJy sr}^{-1} \) and \( I_0(353\text{GHz})=0.081\pm0.003 \text{ MJy sr}^{-1} \) for the initial zero levels at 545 and 353 GHz respectively from the y-intercept of an affine line fit. Details about the calculation of the uncertainties are given in Section 4.2. We have checked that the zero levels found in the Pegasus-Aquarius and in the Isothermal masks are fully compatible (within 1\( \sigma \)). For the rest of the analysis, we have chosen the Isothermal values that led to smaller uncertainties because of the larger number of pixels in the correlations. The final zero values are calculated in a second step with the MBB fit residuals in Section 4.1. We applied the same method for color correction as for \( I_{857\text{GHz}} \).

### 3.4. Initial Zero Level at 100 \( \mu \)m

We first measured the initial zero level of the 100 \( \mu \)m intensity map from a simple correlation with \( N_{\text{H}_1} \) in the optimized Isothermal mask. We show the resulting plot in Figure 4 in which we extended \( N_{\text{H}_1} \) to lower column density for display purpose. As we can see, the correlation is not as strong as at 857 GHz and becomes nonlinear for \( N_{\text{H}_1}\gtrsim4\times10^{20} \text{ cm}^{-2} \). Indeed, at 100 \( \mu \)m for \( T \sim20 \text{ K} \) the intensity of the dust emission is not in the Rayleigh-Jeans regime but in the exponential decrease of the MBB spectrum (Figure 1). Small variations of \( T \) (and to a lesser extent of \( \beta \)) lead to large variations of \( I_{100\mu} \) even for pixels within our Isothermal mask for which this nuisance is minimized. We found from an affine fit a y-intercept of -0.01\( \pm0.04 \text{ MJy sr}^{-1} \).
We used a second method to get the initial zero level at 100 μm in which we correlated in the same Isothermal mask $I_{857\text{GHz}}$ and $I_{100\mu m}$ using as intermediate wavelength the COBE/DIRBE maps at 240 and 140 μm. We first correlated $I_{240\mu m}$ with $I_{857\text{GHz}}$ (Figure 5, left), then $I_{140\mu m}$ with $I_{240\mu m}$ (Figure 5, middle), and finally $I_{100\mu m}$ with $I_{140\mu m}$ (Figure 5, right). At each step, we subtracted the zero level of the reference map. After an affine fit, we obtained $I_{0(240\mu m)}=0.7 \pm 0.1$, $I_{0(140\mu m)}=0.9 \pm 0.1$ and $I_{0(100\mu m)}=0.22 \pm 0.06$ MJy sr$^{-1}$ respectively for the 240, 140, and 100 μm y-intercepts. As stated above, intensity maps were color-corrected iteratively. We note that since the COBE/DIRBE is absolutely calibrated, the value of the y-intercept at 240 μm and 140 μm should be close to the CIB. We will discuss this aspect in a forthcoming publication. Details about the calculation of the uncertainties are given in Section 4.2.

For the initial zero level of $I_{100\mu m}$ we therefore obtained $-0.01 \pm 0.04$ and $0.22 \pm 0.06$ MJy sr$^{-1}$. The former result is biased by strong effects of $T$ and $\beta$ variations and the latter by propagation of errors from intermediate 240 and 140 μm zero levels. Since this value is an important parameter for the MBB fit, especially for the temperature, we decided to use as initial zero level for $I_{100\mu m}$ a number randomly sampled between $-0.1$ and $0.2$ MJy sr$^{-1}$ (see Section 4.2). A value larger than 0.2 would lead to a large quantity of negative pixels in the 100 μm map and a zero-level smaller than $-0.1$ lead to a suspicious increase in $T$ at the Galactic poles. For each realization, we derived the final zero levels in a second step from the MBB fit residuals.

4. MODIFIED BLACKBODY FIT

4.1. Procedure

In this work we modeled the dust with an MBB spectrum that we fitted to observations at 100 μm, 857, 545 and 353 GHz with their zero offsets subtracted. For each pixel of the sky we fitted a parameterized MBB function $I_{\nu}(\tau_{353}, T, \beta) = \tau_{353} B_{\nu}(T)(\nu/353\text{GHz})^\beta$ where $B_{\nu}$ is the Planck function and where the parameters $\tau_{353}$, $T$ and $\beta$ were free to vary.

For a correct color correction of the intensity maps we must assume an initial value for $T$ and $\beta$. We used the values given in Planck XLVIII, and iterated with initial values taken from the previous iteration. Three iterations were required after which we did not observe any significant improvement beyond 1σ. We verified that no major difference on $T$ and $\beta$ was found when starting with a spatially uniform values $T=20$ K and $\beta=1.4$. The fit procedure includes 2 steps. In a first step we fitted the MBB model to intensity maps with initial zero

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**Figure 3.** Correlation of $I_{857\text{GHz}}$ and $I_{857\text{GHz}}$ (left) and $I_{353\text{GHz}}$ and $I_{353\text{GHz}}$ (right) displayed with 7 contours spaced in log between 1 and 5000 pixel counts. The dashed line corresponds to the best affine fit of the histogram points between the 5th and the 95th percentile of the dust intensity distribution (1.2 and 6.7 MJy sr$^{-1}$ for the left plot, and 0.4 and 2.2 MJy sr$^{-1}$ for the right plot). We masked data associated with the white pixels of the Isothermal mask shown in the inset.

**Figure 4.** Correlation of $I_{100\mu m}$ and $N_{HI}$ displayed with 7 contours linearly spaced between 1 and 250 pixel counts. The red points are the centroids of the distribution in bins of $N_{HI}$. We calculated the corresponding error bars, barely visible, by dividing the standard deviation in $I_{100\mu m}$ by the square root of the number of pixels in each $N_{HI}$ bin. The dashed line corresponds to the best affine fit of those points between 2 and $3.5 \times 10^{20}$ cm$^{-2}$. We masked data associated with the white pixels of the Isothermal mask displayed in the inset that we extended in this graph to lower $N_{HI}$ for display purpose.
Figure 5. Correlation of $I_{240\mu m}$ and $I_{857\text{GHz}}$ (left), $I_{140\mu m}$ and $I_{240\mu m}$ (middle), and $I_{100\mu m}$ and $I_{140\mu m}$ (right) displayed with 7 contours spaced in log between 1 and 5000 pixel counts. The dashed line corresponds to the best affine fit of the histogram points between the 5th and the 95th percentile of the dust intensity distribution (1.2 and 6.7 MJy sr$^{-1}$ for the left plot, 2.3 and 13.5 MJy sr$^{-1}$ for the middle plot, and 2.8 and 18.0 MJy sr$^{-1}$ for the right plot). We masked data associated with the white pixels of the Isothermal mask shown in the inset.

levels set from the correlation method described above. For each pixel we extracted the parameters $\tau_{353}$, $T$ and $\beta$. Using those parameters we calculated MBB model predictions for the 4 frequencies and then calculated the residual maps of Planck-HFI and COBE/DIRBE intensities (without subtracting the preliminary zero levels) minus MBB models. We measured the monopole of the residuals for pixels inside the Monopole mask. We used those monopoles as final zero levels.

In a second step, using those zero levels, we fitted again the MBB model to Planck-HFI and IRAS/DIRBE intensity maps and extracted the final values for $\tau_{353}$, $T$ and $\beta$. Simultaneously we updated the values of $\tau_{353}$ and $\beta$ used for color correction. For the $\chi^2$ minimization of the MBB fit we used the same estimates of uncertainties as in Planck XI and Planck XLVIII: the calibration uncertainty (see Table 1 of Planck XI), the associated uncertainty of the CMB removal, and the instrumental noise estimated from the half-difference of the half-mission maps (Planck XLVIII). We also verified the gain calibration of the detectors by comparing with a scatter plot the detector intensities and MBB model predictions (Figure 6). We included in this plot the COBE/DIRBE map at 60 $\mu$m not used in this work. At this wavelength the emission arising from stochastic heating of very small dust grains causes a departure from a simple MBB form extrapolation (Draine & Li 2001). We note a strong miscalibration of 13% at 140 $\mu$m. We do not have any explanation for that departure; we obtained a similar departure of 14% with $\tau_{353}$, $T$ and $\beta$ taken from Planck XLVIII.

4.2. Systematic Uncertainties

Along our procedure we introduced various parameters. We used 8 parameters to define masks latitude and longitude limits and 5 parameters for the mask column density cutoffs. We utilized 2 parameters to define the affine fit limits, 1 for the histogram resolution and 3 corresponding to initial values of $\sigma_{e353}$, $T$ and $\beta$. In order to estimate the systematic uncertainties arising from those parameters we repeated 500 realizations of the MBB fit using, instead of their nominal values, a value sampled assuming a normal distribution. In Table 1 we give the mean and $\sigma$ of those distributions. As guiding principle to estimate the values of $\sigma$, for each parameter we defined a set of possible values based mostly on the observation of residual maps and we attributed the value of $\sigma$ to the standard deviation of this distribution.
As mentioned earlier we also sampled the initial zero-level value for $I_{100}$ from a uniform distribution ranging from $-0.1$ to $0.2$ MJy sr$^{-1}$.

4.3. Final Zero Levels

From the 500 realizations we obtained a distribution of 500 values for the initial and final zero levels, and calibration gains. We fitted those distributions with a Gaussian curve and used the centroids and standard deviations as the final parameters values and uncertainties. The values of the centroids and standard deviations started to converge after only a few tens of realizations.

The final zero levels and uncertainties are shown in the second column of Table 2. At 857, 545, and 353 GHz, those final zero levels differ from the initial ones by a couple of percentages. While we randomly sampled between $-0.1$ and $0.2$ MJy sr$^{-1}$ the initial zero levels for the 100 $\mu$m map, we found a final zero level of $-0.005 \pm 0.002$ MJy sr$^{-1}$. This value is compatible with $-0.01 \pm 0.04$ MJy sr$^{-1}$ obtained in the first step from a direct correlation with $N_{\text{HI}}$. We also provide the calibration gains in the last column of Table 2.

4.4. MBB Parameters

Using the method described above, we obtained for each pixel 500 sets of MBB parameters. In Figure 7 (left), we show the skymap of $\tau$ each pixel 500 sets of MBB parameters. In Figure 9, we plot the spatial distribution of the opacity in Figure 10 (top) that for longitude between 60° and 300°, we find the same opacity spatial distribution as in Figure 10, top. While the opacity is mostly averaged over those realizations. For comparison, on the right side of the same figure, we represent the standard deviation of the 500 realizations. For the optical depth $\tau_{353}$, the correction of the zero levels mainly leads to an increase of $7.1 \times 10^{-7}$ compared to the map of Planck XLVIII. We obtain an average temperature (index) of 20.2 K (1.40) and an average uncertainty of 0.4 K (0.03). In Planck XLVIII the average temperature (index) was 19.4 K (1.6). The spatial distribution of $\beta$ varied notably from Planck XLVIII, we note a decrease in $\beta$ with Galactic latitude; it also seems that the local increases along the north and south of Loop I have disappeared.

5. COMPARISON BETWEEN THE SPATIAL DISTRIBUTIONS OF $\tau_{353}$ AND $N_{\text{HI}}$

5.1. Opacity

We have measured the opacity $\sigma_{e,353}$, the ratio between optical depth and hydrogen column density, in the Pegasus-Aquarius mask with a correlation between $\tau_{353}$ and $N_{\text{HI}}$ (Figure 9). We observe a linear correlation over a range of $N_{\text{HI}}$ from $2 \times 10^{20}$ cm$^{-2}$. As in Figure 2 we observe for the largest $N_{\text{HI}}$ a tail of over-emission of dust compared to hydrogen, which signals a residual presence of gas not traced by optically thin H$\text{I}$ in the mask. In order to remove this bias from the centroid fit, we restricted the upper limit of the $N_{\text{HI}}$ bin in the Gaussian fit to an optical depth corresponding to 1.05 times the centroid position. From an affine fit, we obtain the value $\sigma_{e,353} = (8.9 \pm 0.1) \times 10^{-27}$ cm$^2$ against $(6.3\pm0.1) \times 10^{-27}$ cm$^2$ for Planck XI measured between 1.2 and $2.5 \times 10^{20}$ cm$^{-2}$. The value of the y-intercept is $(-0.17 \pm 0.07) \times 10^{-6}$.

We show the spatial distribution of the opacity in Figure 10 (top). We normalized this map to the value of $8.9 \times 10^{-27}$ cm$^2$ measured in the Pegasus-Aquarius mask. We masked pixels with $\tau_{353}/\sigma_{e,353} - N_{\text{HI}} > 2 \times 10^{20}$ cm$^{-2}$, which removes all regions with potential contamination by H$_2$ or significant H$\text{I}$ self-absorption. We observe in this map large regions (in green) where the opacity is uniform and equal to the value obtained in the Pegasus-Aquarius mask. More interestingly, we also observe extended regions (in reddish color) of large excesses of dust compared to what would be expected from $N_{\text{HI}}$ assuming the Pegasus-Aquarius mask opacity. Those extended regions correspond to locations where $N_{\text{HI}}$ is the lowest. In Figure 10 (middle), we plot the same figure but using $\tau_{353}$ from Planck XLVIII normalized to the opacity of $6.3 \times 10^{-27}$ cm$^2$ measured between 1.2 and $2.5 \times 10^{20}$ cm$^{-2}$ in Planck XI. As noted by Planck XI, we observe an increase in dust opacity from the diffuse to the denser ISM. This is expected from figure 21 of Planck XI where the smaller opacity obtained with a fit at low $N_{\text{HI}}$ leads to an excess of dust emission at larger $N_{\text{HI}}$ where points systematically depart from the linear fit. It was partially interpreted in Planck XI as a possible increase in dust emissivity. Alternatively an opacity of $\sim 9 \times 10^{-27}$ cm$^2$ found in this paper nicely fits the data points above $2 \times 10^{20}$ cm$^{-2}$ in Figure 21 of Planck XI but leads to large excesses of dust at low $N_{\text{HI}}$. The increase in opacity observed in Planck XI at intermediate $N_{\text{HI}}$ may suffer from incorrect zero levels that lead to an offset in $\tau_{353}$. If we add to $\tau_{353}$ derived in Planck XLVIII the constant $7.1 \times 10^{-7}$ (Figure 10, bottom), we find the same opacity spatial distribution as in our work (Figure 10, top). While the opacity is mostly equal to or larger than the average opacity, we note in Figure 10 (top) that for longitude between 60° and 180° and latitude less than $-60°$ we observe a large region of lower opacity. This is likely due to an oversubtraction of the zodiacal emission in the dust maps.

Similarly to what we did in Figure 9 in the small Pegasus-Aquarius mask, we expect a linear correlation between $\tau_{353}$ and $N_{\text{HI}}$ in a wider section of the sky if we exclude pixels with potential contamination by H$_2$ or significant H$\text{I}$ self-absorption, and pixels with very low
| Name                        | Mean  | σ     | Units          | Comments                                                                 |
|-----------------------------|-------|-------|----------------|---------------------------------------------------------------------------|
| Pegasus-Aquarius mask       |       |       |                |                                                                           |
| $\sigma_{ini}$              | 9.0   | 0.1   | $10^{-27}$ cm$^2$| Opacity for the $\tau_{353}/\sigma_{e353} - N_{H1}$ cut                 |
| $C_{DNM1}$                  | 1.00  | 0.05  | $10^{20}$ cm$^{-2}$| Cut in $\tau_{353}/\sigma_{e353} - N_{H1}$ in the low-resolution map     |
| $b_{min}$                   |       |       | degree         | Min latitude cut                                                          |
| $b_{max}$                   |       |       | degree         | Max latitude cut                                                          |
| $l_{min}$                   |       |       | degree         | Min longitude cut                                                         |
| $l_{max}$                   |       |       | degree         | Max longitude cut                                                         |
| $NH_{cut low}$              | 2.0   | 0.1   | $10^{20}$ cm$^{-2}$| Low $N_{H1}$ cut                                                          |
| $NH_{cut high}$             | 5.0   | 0.25  | $10^{20}$ cm$^{-2}$| High $N_{H1}$ cut                                                         |
| Isothermal mask             |       |       |                |                                                                           |
| $NH_{cut low}$              | 2.0   | 0.2   | $10^{20}$ cm$^{-2}$| Low $N_{H1}$ cut                                                          |
| $NH_{cut high}$             | 15.0  | 1.5   | $10^{20}$ cm$^{-2}$| High $N_{H1}$ cut                                                         |
| $\Delta_e$                 | 15    | 2     | degree         | Min distance from ecliptic equator                                       |
| $N_e$                       | 0.5   | 0.1   |                | Half width (in $\sigma$) around $T_{max}$ and $\beta_{max}$              |
| FUV-NUV Mask                |       |       |                |                                                                           |
| $\Delta_{Gould}$           | 30    | 2     | degree         | Half width of Gould Belt region                                           |
| $b_{cut UV}$                | -40   | 1     | degree         | Latitude cut                                                             |
| Various                     |       |       |                |                                                                           |
| $\sigma_T$, $\sigma_\beta$| 5     | %     |                | Variation of $T$ and $\beta$ for each pixel                              |
| $N_{bins}$                  | 100   | 10    | -              | Number of bins in histograms                                             |
| $P_{fit min}$               | 5.0   | 0.5   | %              | Min percentile for affine fit                                             |
| $P_{fit max}$               | 95    | 2     | %              | Max percentile for affine fit                                             |
| $b_{cut zero}$              | 50    | 5     | degree         | Galactic cut for final zero-level monopoles                               |
| $I_{100u zero}$             | -0.1  | to 0.2| MJy sr$^{-1}$  | Initial zero level for $I_{100u}$                                         |
| $NH_{fit low FUV}$          | 2.5   | 0.5   | $10^{20}$ cm$^{-2}$| Low $N_{H1}$ fit limit (FUV)                                             |
| $NH_{fit high FUV}$         | 6.5   | 0.5   | $10^{20}$ cm$^{-2}$| High $N_{H1}$ fit limit (FUV)                                            |
| $NH_{fit low NUV}$          | 5.0   | 0.5   | $10^{20}$ cm$^{-2}$| Low $N_{H1}$ fit limit (NUV)                                             |
| $NH_{fit high NUV}$         | 9.0   | 0.5   | $10^{20}$ cm$^{-2}$| High $N_{H1}$ fit limit (NUV)                                            |

Table 1. List of Parameters Sampled in Each of the 500 MBB Fit Realizations.

Note. Parameters sampled from a normal distribution with means and standard deviations given in columns (2) and (3). $I_{100u zero}$ was sampled from a uniform distribution.

$N_{H1}$ where we observed the dust excesses of Figure 10 (top). Those regions of dust excess can be characterized by an excess of optical depth $\tau_{353} - N_{H1} \times \sigma_{e353}$ larger than $0.03 \times 10^{-6}$ and $N_{H1}$ less than $4 \times 10^{20}$ cm$^{-2}$. If we exclude those pixels and pixels with $\tau_{353}/\sigma_{e353} - N_{H1} > 2 \times 10^{20}$ cm$^{-2}$ (inset of Figure 11), we observe an excellent linear proportionality between $\tau_{353}$ and $N_{H1}$ over a wide range of $N_{H1}$ (Figure 11). We represented the average opacity of $\sigma_{e353} = (8.9 \pm 0.1) \times 10^{-27}$ cm$^2$ measured in the Pegasus-Aquarius mask by the dotted line in Figure 11. We note a departure from this value for $H\text{I}$ column densities above $\sim 35 \times 10^{20}$ cm$^{-2}$ probably caused by the presence of DNM in the mask at high column density or when the $H\text{I}$ that starts to be opaque (not corrected here).

We can also express $\tau_{353}$ in terms of absorption cross-section per dust mass $\kappa_{353}$ at 353 GHz: $\tau_{353} = M_{dust} \kappa_{353}$ where the dust mass column density $M_{dust}$ depends on the dust-to-gas mass ratio $D/G$ and on the gas mass per H-atom $\mu = 1.4$ ($M_{dust} = \mu m_H N_{H1} D/G$ where $m_H$ is the mass of a hydrogen atom). We can then deduce the dust-to-gas mass ratio: $D/G = \sigma_{e353} / (\mu m_H \kappa_{353})$. Using for $\kappa$ the power-law approximation of the dust model of Jones et al. (2017) obtained by Galliano et al. (2018), we have $\kappa = 0.64(\lambda/250)^{-1.79}$ cm$^2$g$^{-1}$ that gives $D/G = 0.53 \times 10^{-2}$ with $\sigma_{e353} = (8.9 \pm 0.1) \times 10^{-27}$ cm$^2$. Note that the main uncertainty in this number resides in the value of $\kappa_{353}$ (see Figure 4a of Galliano et al. (2018) and not in the value of the average opacity.
Table 2. Zero Levels of FIR Maps.

The columns are the following, from left to right: frequency or wavelength, final zero levels obtained in this work, zero levels of Planck XLVIII, zero levels of Planck XI, gain calibration resulting from a comparison between observations and MBB predictions \((I_{\text{obs}} = \text{gain} \times I_{\text{MBB}} + I_{\text{zero}})\) where \(I_{\text{zero}}\) is the zero level provided in column (2). Note that because PR2 maps include a CIB monopole one cannot directly compare the PR2 zero levels to the PR1 ones.

| Band  | Zero Level (MJy sr\(^{-1}\)) | Gain            |
|-------|-------------------------------|-----------------|
|       | This Work (PR2) | Planck XLVIII (PR2) | Planck XI (PR1) |
| 353 GHz | 0.0816 ± 0.0001 | 0.1248 | 0.085 ± 0.006 | 0.9998 ± 0.0001 |
| 545 GHz | 0.230 ± 0.001 | 0.3356 | 0.095 ± 0.014 | 0.9733 ± 0.0004 |
| 857 GHz | 0.343 ± 0.002 | 0.5561 | 0.093 ± 0.009 | 1.0130 ± 0.0003 |
| 240 µm | 0.55 ± 0.06 | - | - | 1.062 ± 0.002 |
| 140 µm | 0.8 ± 0.1 | - | - | 1.126 ± 0.003 |
| 100 µm | −0.005 ± 0.002 | 0.1128 | −0.174 ± 0.005 | 0.9972 ± 0.0001 |
| 60 µm | 0.50 ± 0.02 | - | - | 2.39 ± 0.04 |

Figure 7. All-sky Mollweide display of the MBB parameters \(\tau_{353}\) (top, in log scale), \(T\) (middle), and \(\beta\) (bottom) extracted from a fit to Planck-HFI and IRAS/DIRBE intensity maps obtained in this work (left) and in Planck XLVIII (right). We superimposed to the maps a 30° spaced grid.
Figure 8. Relative uncertainty of the parameters $\tau_{353}$ (top), $T$ (middle) and $\beta$ (bottom) derived from fits of observations at 100$\mu$m and 857, 545, 353 GHz with an MBB spectral form after correction of the zero levels of the intensity maps according to Table 2. Each all-sky map displays in Mollweide projection and linear color scale the ratio between the standard deviation of the 500 realizations and its average value. We superimposed to the maps a 30$^\circ$ spaced grid.

5.2. **Spatial Distribution of the Dust Excesses**

We derived the residual map of the optical depth by subtracting from $\tau_{353}$ the product of the opacity, derived in the Pegasus-Aquarius mask, with $N_{\text{H}1}$. We show the skymap of the optical depth residuals in Figure 12. Outside the regions with potential contamination by H$_2$ or significant H$_1$ self-absorption, in which correction for H$_1$ optical thickness and CO proxy prevent an accurate census of the gas, the residuals should be fluctuating around 0. As we noted for the opacity map, we observe a large excess of dust emission above the emission associated to hydrogen traced by H$_1$. The optical depth of this extra dust is $\sim 0.5$-$1 \times 10^{-6}$. It is mainly located in the northeast part of the skymap ($l=60^\circ$-$180^\circ$ and $b=30^\circ$-$90^\circ$) and in the southwest ($l=180^\circ$-$360^\circ$ and $b=0^\circ$-$90^\circ$).

To derive $N_{\text{H}1}$ from the brightness temperature, we used an optically thin approximation. The dust excess cannot result from this approximation since, at low $N_{\text{H}1}$, a spin temperature of for example 150K would lead to an $N_{\text{H}1}$ increase of only a few percent. In comparison we observe an excess of up to a factor 2.5 toward the Lockman Hole. Note that this excess was not observed previously (Schlegel et al. (1998); Planck Collaboration et al. (2014a); Planck XI; Planck XLVIII) because it was implicitly erased by calculating the zero (detector offset and/or extragalactic emission) of the dust map from a correlation with $N_{\text{H}1}$ at very low $N_{\text{H}1}$.

In Figure 13 (top), we show the anticorrelation between the excess of dust and $N_{\text{H}1}$. This anticorrela-
Figure 10. Spatial distribution of the opacity $\sigma_{353} = \tau_{353}/N_{\text{HI}}$ normalized to the average opacity obtained in this work (top). The middle map shows a similar normalized opacity plot but with $\tau_{353}$ and the average opacity from Planck XLVIII and XI. When adding $7.1 \times 10^{-7}$ to $\tau_{353}$ derived in Planck XLVIII and dividing by $N_{\text{HI}}$ (bottom), we find a similar opacity map to the one from our work shown at the top of this figure. Maps are displayed in Mollweide projection with a linear color scale and a 30° spaced grid. Masked pixels (gray) correspond to regions with $\tau_{353}/\sigma_{353} - N_{\text{HI}} > 2 \times 10^{20}$ cm$^{-2}$, which removes all regions with potential contamination by H$_2$ or significant H$_1$ self-absorption.

Figure 11. Correlation plot between $\tau_{353}$ and $N_{\text{HI}}$ displayed with 10 contours spaced in log between 2 and 25,000 pixel counts. The red points correspond to the centroids of the $N_{\text{HI}}$ bins. We calculated the corresponding error bars, barely visible, by dividing the standard deviation in $\tau_{353}$ by the square root of the number of pixels in each $N_{\text{HI}}$ bin. The dashed line corresponds to $\sigma_{353} = 8.9 \times 10^{-27}$ cm$^{2}$, average opacity extracted from the smaller Pegasus-Aquarius mask. We masked data associated with the white pixels of the mask shown in the inset and described in the text.

Howk et al. (2006) measured toward the globular cluster Messier 3 ($l=42.2°$, $b=78.7°$) a strong depletion of iron compared to sulfur in both the warm neutral medium (WNM) and WIM. Since iron is heavily incorporated into dust grains in contrast to sulfur, one expects the presence of dust associated to the WIM in that direction. This is what we may observe since this line of sight intercepts the dust excess region.

Dust or gas studies outside the plane are often based on simple latitude cuts. In this paper, we define instead three regions based on the comparison between H$_1$, CO, and FIR emission: a region of DNM and high column density gas (red pixels in Figure 14) where the optical depth of the dust deduced from FIR emission is large...
and larger than those expected from $N_{\text{H}_1}$ (traced by its 21 cm line) and $N_{\text{H}_2}$ (traced by the CO molecule), a region (that we called in this work the excess region corresponding to blue pixels in Figure 14) where the optical depth of the dust is small but larger than that expected from $N_{\text{H}_1}$, and finally a region (white pixels in Figure 14) where FIR dust emission and H1 21 cm emission linearly correlate.

6. DUST AND REYNOLDS LAYER OF THE WIM

Lagache et al. (1999) observed an excess of dust associated to H$^+$ from the WIM through a cosecant latitude dependence of the residual emission of dust detected by DIRBE/FIRAS and COBE/DIRBE once dust associated to H1 was subtracted. It was also observed in Lagache et al. (2000) from a decomposition of dust emission into a component associated with $N_{\text{H}_1}$ and another with H$_\alpha$ emission. This observation was not confirmed by Odegard et al. (2007).

We searched for dust associated to the Reynolds layer of the WIM. Similarly to what we did in the Pegasus-Aquarius mask we fitted $\tau_{353}$ derived in this work with a linear combination of $N_{\text{H}_1}$, isotropic, and $N_{\text{H}_+}$ templates predicted by NE2001 and from H$_\alpha$ intensity. We calibrated the H$_\alpha$ emission using $N_{\text{H}_+}$ from NE2001. We found a good correlation with $I_{\text{NE2001}}=(I_{\text{H}_\alpha}/1.3R+0.6)\times10^{20}$ cm$^{-2}$ up to an H$_\alpha$ intensity of 3 Rayleigh. Above this value, the H$_\alpha$ emission is dominated by bright H2 regions. We performed the linear combination fit in the same mask as in Figure 11 addition-ally masking pixels of absolute ecliptic latitudes smaller than 15° or with an H$_\alpha$ intensity larger than 3 R. The fit set the opacity associated with the NE2001 template to a value close to 0, corresponding to a dust abundance 130 times smaller in H$^+$ than in HI. With the H$_\alpha$ template, we found a larger detection corresponding to a dust abundance 14 times smaller in H$^+$ than in HI. However this marginal detection might be due to some residual contamination of free-free emission in the Planck dust maps. Our unsuccessful detection of dust associated to H$^+$ in the Reynolds layer of the WIM does not necessarily imply that this component is dust free, but rather that its FIR emission is below our detection threshold because the $N_{\text{H}_+}$ column densities are

![Figure 12. All-sky Mollweide display of the excess of optical depth at 353 GHz compared to $N_{\text{H}_1}$ predictions: $\tau_{353} - N_{\text{H}_1} \times \sigma_{e353}$. We used the opacity $\sigma_{e353}=8.9\times10^{-27}$ cm$^2$ measured in the Pegasus-Aquarius mask. The color is scaled linearly with the map intensity, and a 30° spaced grid is superimposed. We masked pixels with $\tau_{353}/\sigma_{e353} - N_{\text{H}_1} > 2 \times 10^{20}$ cm$^{-2}$ where $\tau_{353}$ is not a good tracer for $N_{\text{H}_1}$.](image-url)
Figure 13. Correlation of the optical depth of the dust excess and \(N_{\text{HI}}\) (top) and the optical depth of the dust excess and \(N_{\text{HI}}/(2.4\times10^{20}\text{ cm}^{-2}/\sin(\mid b \mid))\) (bottom). The dashed line corresponds to the function \((2.5X^2 - 4.3X + 2.1)\times10^{20}\times\sigma_{353}\) where \(X=N_{\text{HI}}/(2.4\times10^{20}\text{ cm}^{-2}/\sin(\mid b \mid))\), which represents a good approximation for the optical depth of the excess. The scatter plots have 13 contours linearly spaced between 1 and 700 pixel counts. We masked data associated to white pixels of mask shown in the inset. Gray pixels correspond to a dust excess larger than \(0.03\times10^{-6}\) and \(N_{\text{HI}}\) less than \(4\times10^{20}\text{ cm}^{-2}\).

Figure 14. All-sky map displaying the partition of the sky in 3 large-scale regions. The dust excess region is represented with blue pixels (25% of the sky) while red ones correspond to \(\tau_{353}/\sigma_{353} - N_{\text{HI}} > 2\times10^{20}\text{ cm}^{-2}\) where \(\tau_{353}\) is not a good tracer for \(N_{\text{HI}}\) (30% of the sky). In the region with white pixels FIR dust emission and \(\text{H}_2\) 21 cm emission linearly correlate (45% of the sky). The map is centered on the Galactic Center and is displayed in Mollweide projection with a 30° spaced grid.

small compared to the \(N_{\text{HI}}\) ones, and because they partially correlate with the large HI column densities in the widespread WNM.

7. FAR- AND NEAR-ULTRAVIOLET DIFFUSE EMISSION

At FUV and NUV wavelengths, the diffuse light is dominated by the scattering of UV-bright stars on interstellar dust grains (Jura 1979); at high latitudes, FUV and NUV intensities are then expected to scale with dust. Murthy (2016) calculated that \(\sim25\%\) of the scattered light arises from 10 bright stars, and half of the diffuse radiation originates within \(\sim200\text{ pc}\). Additionally, and particularly along the Gould Belt where most UV-bright stars reside, the FUV and NUV emissions include stellar sources (Henry et al. 2015). Figures 10 (top) and 12 suggest the existence of large dust excesses compared to the quantity expected from \(N_{\text{HI}}\). This excess of dust should also scatter UV photons and should lead to FUV and NUV excesses compared to predictions based on \(N_{\text{HI}}\).

7.1. UV Data

We analyzed FUV and NUV diffuse maps\(^7\) extracted by Murthy (2014) from the General Releases 6 and 7 of the Galaxy Evolution Explorer (GALEX) spacecraft (Martin et al. 2005) at 1350–1750 Å (FUV) and 1750–2850 Å (NUV). We transformed those point-source free maps downloaded from the Mikulski Archive for Space Telescopes\(^8\) with a resolution of 2’ into HEALPix standard with a resolution parameter \(N_{\text{side}} = 512\). At this resolution, the pixelization of GALEX is washed-out, and both FUV and NUV maps have a smooth spatial distribution. Both FUV and NUV maps were corrected for airglow from geocoronal oxygen. The zodiacal light was subtracted from the NUV map. This contribution is negligible in the FUV skymap because it arises from sunlight scattered off dust in the ecliptic plane and because the solar flux is strongly suppressed at FUV wavelength.

To analyze those UV skymaps, we masked, in addition to high intensity regions not observed by GALEX, pixels within 40° of the Gould Belt using the parameterization of Coşkunolu et al. (2019), or with latitude comprised between \(-40°\) and \(0°\), or \(10°\) from the bright stars Spica, Achernar, Algenib, Sirius, Mirzam, and Adhara known to possess dust-scattered UV halos (Murthy & Conn Henry 2011). Additionally we selected bright

\(^7\) hlsp_uv-bkgd_galex_map_allsky_fuv_v1_skymap.fits and hlsp_uv-bkgd_galex_map_allsky_nuv_v1_skymap.fits
\(^8\) https://archive.stsci.edu/prepds/uv-bkgd/
UV stars from the Thor-Delta (TD1) catalog (Thompson et al. 1995) with a flux at 1565 Å above 10^{-10} erg cm^{-2}s^{-1}Å^{-1} and we masked pixels within 2°.5 from sources position. We also masked pixels where $N_{\text{H}1}$ is not a good proxy for the dust column density: we first excluded pixels with $T_{353}/\sigma_{e353} - N_{\text{H}1} > 2 \times 10^{20}$ cm^{-2}, we then masked pixels corresponding to the excess of dust shown in Figure 12 and characterized by an excess of optical depth $T_{353} - N_{\text{H}1} \times \sigma_{e353}$ larger than 0.03 \times 10^{-6} and $N_{\text{H}1}$ less than 4 \times 10^{20} cm^{-2}. We show the resulting mask in the insets of Figure 15a and 15b.

7.2. Comparison with $N_{\text{H}1}$

Similarly to what we did at FIR wavelengths, we compared the GALEX FUV and NUV diffuse intensities with $N_{\text{H}1}$ inside the mask described above. With UV light being absorbed by the dust, GALEX did not detect radiation emitted at distances farther than \sim 600 pc (Murthy 2016) so here we considered only $\text{H}1$ with a radial Galactic distance comprised between 7 and 9 kpc. Figure 15 shows the scatter plot of $I_{\text{FUV}}$ and $I_{\text{NUV}}$, the GALEX FUV and NUV intensities, and local $N_{\text{H}1}$. We observe at both FUV and NUV wavelengths an affine correlation between the two observables with an average Galactic FUV intensity per $N_{\text{H}1}$ (that we call average FUV opacity by analogy with the FIR terminology) of $(130 \pm 4) \times 10^{-20}$ photons s^{-1}cm^{-2}sr^{-1}Å^{-1}cm^{-2} and an average Galactic NUV intensity per $N_{\text{H}1}$ (average NUV opacity) of $(111 \pm 6) \times 10^{-20}$ photons s^{-1}cm^{-2}sr^{-1}Å^{-1}cm^{-2}. The FUV opacity agrees with the value of $(121 \pm 30) \times 10^{-20}$ photons s^{-1}cm^{-2}sr^{-1}Å^{-1}cm^{-2} found by Hamden et al. (2013) for latitudes with absolute values between 30° and 45°, but it differs from the smaller FUV opacities they found at higher absolute value latitudes. The y-intercept of the FUV scatter plot is $I_{0(FUV)} = 137 \pm 15$ photons s^{-1}cm^{-2}sr^{-1}Å^{-1} and the one of the NUV plot is $I_{0(NUV)} = 378 \pm 45$ photons s^{-1}cm^{-2}sr^{-1}Å^{-1}. We observe in the NUV scatter plot of Figure 15b a strong departure from linearity for $N_{\text{H}1}$ less than 4 \times 10^{20} cm^{-2}. This departure may be due to zodiacal light not totally removed from the NUV map (see next paragraph). We calculated the uncertainties for those values using the same method as in the FIR sections: we derived 500 FUV scatter plots and 500 NUV scatter plots with randomly sampled mask and fit limits given in Table 1.

We present in Figure 16 (upper row) the spatial distribution of the FUV opacity ($I_{\text{FUV}} - I_{0(FUV)}$)/$N_{\text{H}1}$ and of the NUV opacity ($I_{\text{NUV}} - I_{0(NUV)}$)/$N_{\text{H}1}$ normalized to the average values obtained by the fit of Figure 15. We observe large-scale excesses of FUV and NUV emission compared to what we expect from $N_{\text{H}1}$. One does not expect a good correlation between the diffuse UV photons and $N_{\text{H}1}$ close to the Galactic plane and along the Gould Belt or close to bright UV stars. But we also note excesses in the northeast and southwest part of the maps with distributions similar to those obtained in Figure 10 (top) and in Figure 12. This seems to indicate that the excess observed in the FIR domain corresponds to an excess of dust column density rather than an increase of thermal dust emissivity at low $N_{\text{H}1}$. We do not observe major FUV emission from dust associated to molecular clouds or to regions of high DNM shielded from UV. In Figure 16 (lower row), we show the same FUV and NUV opacities, but we added to the local $N_{\text{H}1}$ the excess of optical depth observed at FIR frequencies divided by $\sigma_{e353}$. As we did previously, we defined this dust excess

![Figure 15. Correlation between local $N_{\text{H}1}$ and GALEX FUV intensity $I_{\text{FUV}}$ (a) and NUV intensity $I_{\text{NUV}}$ (b) displayed with 8 contours linearly spaced between 1 and 1500 pixel counts. The red points are the centroids of the distribution in bins of $N_{\text{H}1}$. We calculated the corresponding error bars, barely visible, by dividing the standard deviation in UV intensity by the square root of the number of pixels in each $N_{\text{H}1}$ bin. The dashed line corresponds to the best affine fit to the points calculated in the range from 2.5 to 6.5 \times 10^{20} cm^{-2} for plot (a) and 5 to 9 \times 10^{20} cm^{-2} for plot (b). We masked data associated with the white pixels of the mask shown in the inset and detailed in the text. The ratio between $(I_{\text{FUV}} - I_{0(FUV)})$ and $(I_{\text{NUV}} - I_{0(NUV)})$ divided by their respective opacities is displayed in (c).]
and 80\degree scale excess similar to that of our FIR excess (Figure 10 (top) and in Figure 12) in the ratio map of FUV to NUV intensity displayed in Figure 15(c) where the regions of the dust excesses (northeast and southwest quadrants) have ratio values close to 1. By construction of the plot of Figure 15c, a value of 1 indicates that the FUV and NUV maps correlate with a correlation coefficient compatible with the ones independently deduced from the correlation with \(N_{\text{H}1}\). Because we subtracted the isotropic intensities at both wavelengths in the ratio, any faint component present at one wavelength and not in the other readily shows up in the ratio. This is why the faint NUV extra component (or zodiacal residual) drives the ratio map to blue values toward 0.5, but the regions of the dust excesses do not strongly deviate from 1.

### 7.3. UV Extragalactic Background

Measuring of the UV extragalactic background started 50 yr ago. Murthy et al. (2019), Table 1, reviews 75 publications related to observations of diffuse UV among which 23 resulted in an assessment of the FUV extragalactic background with an average of 283 photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) at FUV wavelength and 588 \pm 37 photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) at NUV wavelength in a study of the region between the Galactic latitudes 70° and 80°.

Akshaya et al. (2018) calculated the expected UV extragalactic background taking into account photons from galaxies, quasars, and intergalactic medium. They obtained a value of 114 \pm 18 photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) in the GALEX FUV band and 194 \pm 37 photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) in the GALEX NUV band. Gardiner et al. (2000), an expected range of 144–195 photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) at FUV wavelength and 179 photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) at NUV wavelength were found from a count of resolved objects in the Hubble Deep Fields observations. Those predictions differ from the measures, and this discrepancy led to hypothesizing for alternative sources of diffuse UV emission (Kulkarni 2022; Henry et al. 2015; Hamden et al. 2013).

It is possible that the discrepancy between predicted and measured values of the UV extragalactic background fluxes could in part be due to the scattering on the dust excess displayed in Figure 12 that was not accounted for in the calculation of the foreground Galactic emission. In the scatter plots of Figures 15(a) and (b), the y-intercepts of the dashed lines represent the diffuse UV intensities extrapolated to \(N_{\text{H}1}=0\). As mentioned earlier, we found a value of \(I_{0(\text{FUV})}=137 \pm 15\) photons \(s^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Å}^{-1}\) for the FUV y-intercept, which is compatible with the prediction of Akshaya et al. (2018).
However the NUV y-intercept $I_{0(NUV)} = 378 \pm 45$ photons s$^{-1}$ cm$^{-2}$ sr$^{-1}$ A$^{-1}$ is still about twice as much as the NUV extragalactic background prediction. Given the discrepancy between the measured and the expected NUV extragalactic background, we separately fitted the eastern and western halves of the mask region. We obtained y-intercepts compatible within 1σ with the value derived in the whole mask. Our measure of the extragalactic background is therefore not significantly influenced by possible high-latitude or zodiacal excesses.

Our simplistic model based on a direct comparison with $N_{H_{1}}$ assumes a completely isotropic scattering of UV photons on dust grains; still we think that our work represents an improvement compared to previous studies that used simple latitude cuts. We tested the model of Jura (1979) where the dust scattered intensity is $I_{UV} = aI_{0}\tau_{V}(1 - 1.1g\sqrt{\sin(|b|)}) + I_{iso}$ where $I_{0}$ relates to the constant plane source that illuminates the high-latitude dust, $I_{iso}$ is the isotropic contribution, $\tau_{V}$ is the optical depth, $a$ is the albedo, and $g$ is the forward scattering asymmetry factor of Galactic dust grains, but we were not able to clearly disentangle the contributions from $I_{iso}$, $a$, and $g$. A better characterization of the UV extragalactic background probably requires a Monte Carlo simulation similarly to the work of Murthy (2016) together with a careful 3D distribution of all the local dust including the excesses observed in our work.

8. INTERPRETATION AND PERSPECTIVE

In this work, we observed, through their FIR emission and UV scattering, an excess of dust grains with a spatial extension covering 25% of the sky. This excess of dust is anticorrelated with $N_{H_{1}}$ and more precisely with $N_{H_{1}}\times\sin(|b|)$ (Figure 13). We can also see this anticorrelation in Figure 17a that represents $N_{H_{1}}$ divided by $2.4 \times 10^{20}$ cm$^{-2}$/sr to emphasize the local gas distribution. In this map, the gas deficits in the northeast and southwest (dark blue holes) correspond to excesses in the maps of Figures 10 (top) and 16 (a and b). The dust excesses noted in Figures 10 (top) and 16 (a and b) therefore seem to relate to local deficits in the WNM. We further note that these deficits surround the inclined poles of the local ISM disk structure (see Figure 4 of Steer et al. (1999); Lallement et al. (2019)). Figure 17b displaying $\tau_{353}/\sigma_{353}$ divided by $2.4 \times 10^{20}$ cm$^{-2}$/sr to emphasize the local gas distribution shows that the total gas potentially traced by $\tau_{353}/\sigma_{353}$ follows the cosecant trend (more uniform cyan and green colors toward these regions). Murthy et al. (2010) and Hamden et al. (2013) noted a similar agreement for the GALEX UV intensity maps.

In our FIR study, the only way we found to strongly reduce this excess of dust was to set the initial 100 μm map zero level to values below -0.6 MJy sr$^{-1}$ thereby significantly increasing the 100 μm intensity for low $N_{H_{1}}$ regions. This increase would translate for the fit in a significant increase in $T$ and a decrease in $\tau_{353}$ for regions of low $N_{H_{1}}$ in better agreement with the prediction based on $N_{H_{1}}$ and the excess would cancel. We disregarded this possibility for two reasons. First a value of -0.6 MJy sr$^{-1}$ is largely rejected by the two calibration methods illustrated by Figures 4 and 5. Secondly that would result in an average temperature of 25 K for dust with |$b$| > 60° while the average temperature for the rest of the sky would be 21 K. Since big grains are in thermal equilibrium with the ambient interstellar radiation field, their temperatures trace the local UV and optical radiation field intensity (Compiègne et al. 2010), and the distribution of hot O and B stars that follows the Gould Belt (Perryman et al. 1997) could not be at the origin of a large increase of temperature toward the Galactic poles.

Dust particles obscure the light from faint and distant sources. Observations with cosmological purposes often use long exposure in deep fields carefully chosen for, among other criteria, their low dust column density. The Euclid mission (Laureijs et al. 2011) has for example chosen 3 deep fields$^9$: the Euclid Deep Fields North (EDFN), the Euclid Deep Fields South (EDFS), and the Euclid Deep Fields Formax (EDFF). We estimated that on average the dust column density is 22% higher in the EDFF than predictions based on $\tau_{353}$ taken from Planck XLVIII, 74% higher in EDFS, and 90% higher in EDFF. This number reaches 120% within 2°.5 of the Lockman Hole.

If some gas is associated to the dust seen in excess, it should interact with CR and produce $\gamma$ rays from $\pi^{0}$ decay and Bremsstrahlung. With an average column density of $0.7 \times 10^{20}$ cm$^{-2}$ over 25% of the sky, we predict that more than $5 \times 10^{5}$ counts above 50 MeV in 10 years of Fermi-LAT data should arise from those interactions. This gas, assuming the same $\gamma$-ray emissivity as the local hydrogen, should be easily detectable by Fermi-LAT. It will be the subject of a forthcoming publication.

9. CONCLUSIONS

In this work, we compared, outside the Galactic plane, the spatial distribution of the dust traced by its FIR, NUV, and FUV emission to the spatial distribution of atomic hydrogen derived from radio surveys. The nonuniformity of the spatial distribution of the FIR

$^9$ https://www.cosmos.esa.int/web/euclid/euclid-survey
opacity found in previous studies led to the investigation of a possible issue in the zero level of FIR maps.

We measured the zero level (detector offset plus CIB monopole) of the Planck-HFI skymap at 857 GHz in a region where we knew from the Fermi-LAT diffuse analysis that $N_{\text{H}_1}$ provides a good template for the interstellar $\gamma$-ray sky. From that value, we deduced the zero levels of Planck maps at 545 and 353 GHz as well as the zero level of the 100 $\mu$m map from COBE/DIRBE and IRAS and zero levels of COBE/DIRBE maps. We refined those values using the monopoles of the residuals between the intensity maps and an iteratively fitted MBB model. We obtained significantly different zero levels from those deduced in regions of lowest $N_{\text{H}_1}$ in Planck XI and in Planck XLVIII. The best fits of the MBB model FIR emission at 100 $\mu$m and 857, 545, and 353 GHz lead to significantly different maps of the dust opacity spectral index $\beta$ and temperature $T$ and an overall increase in the optical depth $\tau_{353}$ of $7.1 \times 10^{-7}$ compared to the results of Planck XLVIII.

We compared $\tau_{353}$ and $N_{\text{H}_1}$ and obtained an average dust opacity of $\sigma_{e353}=(8.9 \pm 0.1) \times 10^{-27}$ cm$^2$. From the average opacity, we deduced a dust-to-gas mass ratio of $0.53 \times 10^{-2}$. The opacity displays a uniform spatial distribution outside regions with dense gas except in various large-scale regions of low $N_{\text{H}_1}$ ($\lesssim 2 \times 10^{20}$ cm$^{-2}$) that cover 25% of the sky. In those regions, we observe that on average the dust column density is 45% higher than predictions based on $N_{\text{H}_1}$. The excess reaches a maximum around the Lockman Hole where the region within $5^\circ$ of this position contains 2.5 times more dust than what is expected from $N_{\text{H}_1}$. The spatial distribution of this excess is not what one would expect from dust associated to a WIM-Reynolds-type layer.

We calculated the rate of NUV and FUV photons detected by GALEX per atomic hydrogen and studied its spatial distribution. We observed an excess of photons with a similar spatial distribution to what we obtained in our FIR study. The dust excess is then both observed through its FIR and UV emission. This excess of dust can also be interpreted as a gas deficit in regions of low $N_{\text{H}_1}$ and more precisely in regions that depart from a cosecant law.

We measured with a simplistic modeling a FUV isotropic intensity of $137 \pm 15$ photons s$^{-1}$cm$^{-2}$sr$^{-1}$Å$^{-1}$ in agreement with extragalactic flux predictions and a NUV isotropic intensity of $378 \pm 45$ photons s$^{-1}$cm$^{-2}$sr$^{-1}$Å$^{-1}$ corresponding to twice larger than the predictions.

The skymaps of the MBB dust parameters $\tau_{353}$, $T$, and $\beta$ displayed in Figure 7 (left) are available for download in Fits format.

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Software: NumPy (van der Walt et al. 2011), Matplotlib (Hunter 2007), FILLTEX (Gerosa & Vallisneri 10 https://irfu.cea.fr/dap/en/Phocea/Vie_des_labos/Ast/ast_technique.php?id_ast=5060
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