Yield strength, Shear Stress and Toughness of YBCO samples
textured by Bridgman technique

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Abstract. Mechanical properties of the orthorhombic phase of YBa₂Cu₃O₇₋δ (Y-123) at room temperature have been investigated at different applied loads using nanoindentation technique. The study was carried out for several monodomains on the (001) planes for textured Bridgman samples with dispersed Y₂BaCuO₅ (Y-211) particles as pinning centers. The yield strength (σₚ), shear stress (τₚ) and toughness (K蒋) of Y123/Y211 composite was determined at different applied loads. First and second mechanical properties have been calculated though the Hertz equations and the last one with Lawn et al. equations. Finally, the ultra-low imprints obtained by nanoindentation have been correlated with parameters obtained by Field Emission Scanning Electron Microscope (FE-SEM).

1. Introduction

It is well known that bulk superconductor materials exhibit high critical current density and high magnetic field at cryogenic temperatures (liquid nitrogen). In order to prepare bulk pieces, a fine and well-dispersed Y-211 precipitate distribution in the Y-123 matrix has to be achieved.

Most superconducting applications of interest for electric utilities require superconductors in the form of bulk, wire or tape. Useful superconductors need to be flexible, ductile and carry large current densities. Hence, the extreme brittleness of ceramics is the leading obstacle to the practical implementation of high temperature superconductors (HTSCs). It has been suggested that these poor mechanical properties limit the performance of melt-textured YBCO in applications where magnetic field and/or thermal cycling is unavoidable.[1]

Nanoindentation is a versatile technique for measuring mechanical properties at very small scale, namely in the micron and sub-micron range [2]. Nanoindentation is a non-destructive and selective technique. It can work from 50 nN to 500 mN.

The purpose of this experimental study is to determine the yield strength, shear stress and fracture toughness of Y-123/Y-211 composite at room temperature. So different loads (5, 10, 30 and 100 mN) have been applied on the ab plane (001) of textured Bridgman samples.
Yield Strength, Shear Stress of Y-123/Y-211 composite have been calculated through Hertz equations and Toughness with Lawn et al. equations [3-4].

2. Experimental procedure

2.1. Preparation of bulk YBCO pieces and monodomain growth
The YBCO powders were prepared by PVA method [5]. Ratio used here (69% w/w Y123, 30% w/w Y211 and 1% w/w CeO2·nH2O) has been demonstrated to maximize critical current density [6]. The standard composition of the starting material was Y-123 with an Y-211 excess of 30% w/w. CeO2·nH2O was added in order to achieve a refinement of the Y-211 distribution. The calcined powder was deagglomerated by ball milling in an agate mortar.

Green bulk pieces were obtained by uniaxial isostatic cold pressure and further textured using the Bridgman method [6-8]. After this, bulk textured pieces were oxygenated in a horizontal furnace at 450 ºC for 240 h [9]. From the oxygenated pieces with a common c-axis tilt of 45º, small pieces of 2 mm height were cut by the (001) planes[1].

2.2. Mechanical Properties
Nanoindentation test were performed with a Nano Indenter® XP system (MTS Systems Corporation) equipped with Test Works 4 Professional level software. Nanoindentation imprints were observed with field emission Hitachi H-4100 scanning electron microscope (SCT Barcelona). The experiments were performed on the (001) plane at room temperature. Applied loads were 5, 10, 30 and 100 mN. The loading/unloading time was selected to be constant for all indentations, 15 s.

The nanoindentations were made by a three-sided pyramid Berkovich diamond indenter. The displacement (penetration depth) was continuously monitored and load-time history of indentation recorded. The tip was calibrated with a fused silica standard and the frame stiffness and the thermal drift were automatically corrected.

2.2.1. Yield strength and Shear Stress
The yield strength of YBCO bulk was calculated from the nanoindentation hardness value using Hertz equations for blunt contact [3].

Figure 1 presents a scheme of load-penetration depth (P-h) curve for a sharp indenter with its associate nomenclature. During the first steps of indentation the curve follows the relation, $P = C \cdot h^{3/2}$. This relation corresponds to the elastic deformation, and the yield strength can be obtained with the Hertzian equations, where C is the indentation curvature, which is a measure of the “resistance” of the material to indentation. This is due to the fact that the tip is rounded and, therefore, follows the equations for elastic contact with a blunt indenter. When the applied load induces a plastic deformation of material during loading process, the curve generally follows the next relation, $P = C \cdot h^2$, typical of a sharp indenter. Yield strength is defined as the stress at which a material begins to plastically deform. Prior to yield point the material will deform elastically and will return to its original shape when the applied load is removed. Once the yield point is passed, some fraction of the deformation will be permanent and non-reversible.
The stresses and deflection arising from the contact between two elastic solids are of particular interest to those understand the first steps of indentation testing. The contact between a rigid sphere and a flat surface for small penetration depths was described by Hertz. This phenomena is shown in Figure 2 [3]. The radius of the circle of contact is \( a \), the total depth of penetration is \( h_t \), the depth of the circle of contact from the specimen free surface \( h_a \), and \( h_p \) is the distance from the bottom of the contact to the contact circle.

Hertz [12] found that the radius of the circle of contact \( a \) is related to the indenter load, \( P \), the indenter radius, \( R \), and the elastic properties for small penetration depths of the material by:

\[
a^3 = \frac{3}{4} \frac{P \cdot R}{E_{\text{eff}}}
\]  

(1)

where \( E_{\text{eff}} \) is the effective modulus between the sample and the indenter. \( E_{\text{eff}} \) can be rewritten as:

\[
\frac{1}{E_{\text{eff}}} = \frac{1 - \nu^2}{E} + \frac{1 - \nu_i^2}{E_i}
\]

(2)

where \( E \) and \( \nu \) are the Young’s modulus and Poisson’s ratio for material of study and \( E_i \), \( \nu_i \) are the Young’s and Poisson’s moduli for the indenter \( (E_i=1140\text{GPa and } \nu_i=0.07 \text{[11]}) \), respectively.

The mean contact pressure, \( p_m \), between the indenter and the material is:


\[ p_m = \frac{P}{\pi \cdot a^2} = \frac{4 \cdot E_{\text{eff}}}{3 \cdot \pi} \left( \frac{a}{R} \right) \]  

(3)

The mean contact pressure is often referred to as the “indentation stress” and the quantity \( a/R \) as the “indentation strain”.

The maximum tensile stress occurs at the edge of the contact circle in the surface and can be calculated by [10]:

\[ \sigma_{\text{max}} = \frac{1}{2} \left( 1 - 2 \cdot \nu \right) \cdot p_m \]  

(4)

The maximum tensile stress is the yield strength of the material. This parameter will make the transition from elastic to elastic-plastic response [12].

The maximum shear stress (\( \tau_m \)) is produced beneath the indentation axis at a depth close to 0.5\( \cdot \)a, and equals to:

\[ \tau_m = 0.46 \cdot p_m \]  

(5)

The maximum shear stress, is also known as the Tresca criterion. This assumes that yield occurs when the shear stress \( \tau \) exceeds the shear yield strength \( \tau_{\text{ys}} \):

\[ \tau = \frac{\sigma_1 - \sigma_3}{2} \leq \tau_{\text{ys}} \]  

(6)

where \( \sigma_1 \) and \( \sigma_3 \) are principal stress (also, can be rewritten as \( \sigma_x \) and \( \sigma_z \), respectively).

2.2.2. Toughness

Conventional indentation toughness methods were initially developed for monolithic bulk materials tested by microindentation when well-developed radial cracks form [3]. The fracture toughness \( K_{\text{IC}} \) is related to the applied load, \( P \), and the crack dimension, c.

When an external stress (residual stress “\( \sigma_r \)”) is applied to the sample, the crack will assume a new equilibrium length, c. The stress intensity can be expressed as [4]:

\[ K_{IC} = K_i + K_r = \chi \left( \frac{E}{H} \right)^{1/2} \cdot \frac{P^{3/2}}{c^{3/2}} + \psi \cdot \sigma_r \cdot c^{1/2} \]  

(7)

where, \( K_i \) is the indentation stress intensity factor, \( K_r \) is the residual stress intensity factor, \( \chi \) is a constant that is a function of the indenter (for a Berkovich indenter, \( \chi = 0.016 \)), E and H are the Young’s Modulus and Hardness of the studied material, and \( \psi \) is a constant related to the crack geometry and loading conditions. If only one surface cracks are considered, then \( \psi = \pi^{1/2} \) [13].

Normally, the residual stress intensity factor is lower than the indentation stress intensity factor. For this reason, equation 7 can be re-written as follow:

\[ K_{IC} = \chi \left( \frac{E}{H} \right)^{1/2} \cdot \frac{P^{3/2}}{c^{3/2}} \]  

(8)

3. Results and Discussion

Load/Unload curves, Nanohardness and Young’s modulus values used to calculate yield strength, shear stress and toughness had been obtained in a previous work [14].

3.1. Yield strength and Shear Stress

The indenter radius, \( R \), has been determine by FE-SEM, and the value is 460 nm. Figure 3, shows the calculated yield strength and shear stress values of the orthorhombic Y-123/Y-211 composite for the different monodomain samples studied when the applied loads were 5, 10, 30 and 100 mN. Each point in Figure 3 is an average of 40 measurements performed on two different samples in order to achieve statistical significance.
In Figure 3, it can be observed that yield strength and shear stress display an exponential law. Moreover, yield strength and shear stress can be strongly affected by the presence of defects and impurities, that can cause almost no change in dislocation movement, which would affect these mechanical properties. We can observe that both mechanical properties increase when the applied load is increased. It is due to surface defects. Yield strength of Y-123/Y-211 composite is lower than shear stress. This fact could be due to different reasons: (a) shear stress only depends on the mean contact pressure, $p_m$, and yield strength depends on $p_m$ and also on the Poisson ratio (this is an intrinsic material property), and/or (b) the melt-processed ceramic composites contain a dense population of fine peritectic particles, acting as nucleation sites for dislocation onto a (001) plane, which affects drastically the microstructure [15].

A relationship between yield strength and shear stress at different applied loads has been found (see Figure 3), which can be used to calculate yield strength and shear stress as a function of $P$. Therefore, from Figure 3 we obtain:

$$\sigma_{ys} = 4.25 + 5.67 \cdot \left(1 - e^{-\frac{P}{9.09}}\right) + 19.37 \cdot \left(1 - e^{-\frac{P}{195.39}}\right)$$  \hspace{1cm} (9)$$

$$\tau_m = 8.83 + 28.35 \cdot \left(1 - e^{-\frac{P}{65.04}}\right) + 9.45 \cdot \left(1 - e^{-\frac{P}{3.73}}\right)$$  \hspace{1cm} (10)$$

The integration of the first equation gives the work to perform a plastic deformation.

### 3.2. Toughness
In Figure 4, two types of indentations can be observed, one with a crack at the corners of the nanoindentation imprints performed at 30 mN, and the other one with porosity and radial cracks performed at 100 mN.

When the applied load is higher than 30 mN, the toughness cannot be determined because the crack length cannot be measured. In this case, other fracture factors exist, such as porosity due to the applied load or radial cracks (see Figure 4b).

Toughness of this material can be only studied when applied load is 30 mN. When applied load is 10 mN or lower, the toughness value of each phase cannot be calculated, because the length of the cracks at the Y-123 and Y-123/Y-211 composite imprints cannot be observed. In spite of that, Y-211 present other fracture factors such as chipping [14].
Figure 4. Nanoindentation imprints a) at 30 mN with crack propagation at the corners of the indentation, and b) at 100 mN with porosity and radial cracks.

With the crack length and the equation 8, the toughness can be calculated for an applied load of 30 mN. The obtained value is $2.85 \pm 0.11 \text{ MPa} \cdot \text{m}^{1/2}$.

4. Conclusions

Nanoindentation is a versatile and non-destructive technique to determine the mechanical properties of superconductor materials at ultra low load.

Yield strength and shear stress for Y-123/Y-211 composite depend on an exponential law with the applied load. Therefore, these mechanical properties can be previously determined at a wide range of loads (from 5 to 100 mN), with equations 9 and 10, respectively, with a 5% error.

If we integrate equation 9 between two different loads, we can calculate the minimum work necessary to perform a plastic deformation under this load range.

Fracture toughness can only be determined at 30 mN of applied load. The imprints obtained under higher loads present different fracture events such as: cracks only at one of the corners of nanoindentation imprint, porosity, chipping, etc.

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