How are mathematicians as part of mathematics history represented in contemporary Chinese school mathematics textbooks?

Summary: As part of our efforts to understand how history and culture are manifested in mathematics textbooks, we investigate particularly in this study how mathematicians are represented across three different series of contemporary school mathematics textbooks used in primary and junior secondary schools in China. The study intends to document the ways of representation of mathematicians in the three series of textbooks, compare the similarities and differences, and explore the reasons and implications of the findings concerning mathematics textbook research and development. Our findings show that each series of mathematics textbooks introduced both Chinese and non-Chinese mathematicians in a commendable way, though most of the mathematicians introduced were ancient mathematicians, and all the three series introduced mathematicians each year from Grade 2 to Grade 9. There is also a high level of consistency in the distribution of the introduction of mathematicians in the three series in terms of mathematics contents and the structures of the chapters. In comparison, we found the mathematics textbook series by the PEP presented a more balanced distribution of the introductions of mathematicians in terms of grade levels, ethnic origins and the history timeline. The explanations and implications of the findings are discussed at the end of the paper.

Keywords: Mathematics textbooks, Chinese mathematics education, mathematicians in textbooks, history of mathematics, textbook analysis.

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Introduction and Background

As is well known, mathematics textbooks play an important role in the teaching and learning of mathematics in many countries. Related to this fact, mathematics textbook research has received a rapidly increasing attention from researchers over the last two decades or so in different parts of the world (e.g., see Fan et al., 2013; Schubring & Fan, 2018). This development can be seen from the fact that, for example, ZDM published two special issues in 2013 and 2018, with the theme being “textbook research on mathematics education” and “recent advances in mathematics textbook research and development” respectively, and a highly visible conference series, the International Conferences on Mathematics Textbook Research and Development, were held in the UK in 2014 (Jones et al., 2014), Brazil in 2017 (Schubring & Fan, 2018), and Germany in 2019 (Rezat et al., 2019).

Under the general background of mathematics textbook research, there have been a number of studies focusing on the history of mathematics in mathematics textbooks (e.g., Eren et al., 2015; Ju et al., 2016; Schorcht, 2018), and some researchers further argued that the topic of mathematicians is an aspect of the history of mathematics (e.g., Shen et al., 2013; Wang et al., 2015). However, there have been very few studies so far directly looking into the issue about how mathematicians are represented in school mathematics textbooks (e.g., see Castaneda et al., 2019), even though some researchers have argued that introducing mathematicians was a way to use history in mathematics education (cf. Fauvel, 1991).

There is no doubt that researchers have paid attention to the role of the history of mathematics in the teaching and learning of school mathematics.

For example, Jones (1957) analysed the history of mathematics as a teaching tool for students’ learning of mathematics. Gulikers and Blom (2001) conducted a survey of literature on the use and value of history in geometry education and they maintained that the history of mathematics could help teachers to teach mathematics and pupils to learn mathematics in many aspects, especially for pupils’ learning. Furthermore, Jankvist (2009) categorized the “whys” and “hows” of using history in mathematics education, dividing the former into history as a tool and as a goal and dividing the latter into the illumination, the modules and the history-based approaches in terms of the ways of using.

The role of the history of mathematics in the teaching and learning of mathematics has also received reasonable attention in contemporary mathematics education in China. In fact, both Chinese national curriculum standards and the Shanghai mathematics curriculum standards for primary and secondary stage emphasize that the history of mathematics should be integrated into mathematics textbooks (Shanghai Municipal Education Commission, 2004; Ministry of Education of the People’s Republic of China, 2011). Such ideas are also reflected in the national mathematics curriculum standards in other countries such as England (Department for Education, 2013 & 2014), which also treat the history of mathematics, more or less, as an integral aspect of teaching of mathematics.

It is worth noting that the national curriculum standards in China particularly stressed that students can understand better, by learning from the work and spirit of mathematicians, what the rigor of mathematics means and hence benefit from their learning of mathematics. In a sense, this reflects the importance of the introduction of mathematicians in Chinese mathematics textbooks as mathematics textbooks play the most dominant role in Chinese mathematics classrooms (Fan et al., 2004).

In this study, as part of our efforts to understand how history and culture are manifested in
mathematics textbooks (e.g., see Fan et al., 2018), we aim to particularly investigate how mathematicians are represented across three different series of contemporary school mathematics textbooks used in primary and junior secondary schools in China. By doing so, our purpose is to document the ways of representation of mathematicians in the three series of textbooks, compare the similarities and differences between them, and explore the reasons and implications of the findings concerning mathematics textbook research and development.

Research Questions

In the research, focusing on the three series of Chinese primary and junior secondary school mathematics textbooks, one published and used in Shanghai and the others published by People's Education Press and Beijing Normal University Press respectively and used in many different parts of China, we intend to address the following questions:

- How are mathematicians as part of mathematics history represented in the Chinese mathematics textbooks?
- What are the similarities and differences in the representation of mathematicians among the three series of the mathematics textbooks?

As aforementioned, by addressing these research questions, we also hope to explore the reasons and implications of the findings in relation to mathematics textbook research and development.

Methods and Procedures

Textbook selection

At present, there are two mathematics curriculum standards implemented in the stage of compulsory education in China, i.e., the Shanghai Mathematics Curriculum Standards for Primary and Secondary Schools (Trial Version) and the Mathematics Curriculum Standards for Compulsory Education (2011 Edition). It should be noted that the Shanghai’s curriculum standards is approved by the Chinese central government and implemented in virtually all primary and secondary schools in the city of Shanghai. On the other hand, the Mathematics Curriculum Standards for Compulsory Education (2011 Edition), or simply the national mathematics curriculum standards, is implemented in all the regions except Shanghai in the Chinese mainland.

The stage of compulsory education in China lasts 9 years, from primary school to junior secondary school, but the school system in Shanghai is different from other parts of China, which follow the national curriculum standards. In general, there are 6 years of primary education, followed by 3 years of junior secondary education in all the regions except Shanghai in China. In Shanghai, primary education lasts 5 years and junior secondary education lasts 4 years, so it is more comparable if we select the whole stage of compulsory education.

In this study, to investigate how primary and junior secondary school mathematics textbooks in China represent mathematicians, as mentioned earlier, we selected the three series of mathematics textbooks from Grade 1 to Grade 9. They are as follows:

Series 1: The mathematics textbooks published by Juvenile & Children's Publishing House (Grade 1-2) and Shanghai Educational Publishing House (Grade 3-9) and used in Shanghai;

Series 2: The mathematics textbooks published by the People's Educational Press;

Series 3: The mathematics textbooks published by Beijing Normal University Press.

For Shanghai, the mathematics textbooks used were developed in accordance with the Shanghai’s curriculum standards. They were published by two publishers, the first and second grades’ mathematics textbooks were published by Juvenile & Children's Publishing House, while all the remaining
seven grades’ textbooks were published by Shanghai Educational Publishing House.

The mathematics textbooks published by the People's Education Press (PEP) and Beijing Normal University Press (BNUP) are two most widely used series in China in terms of the number of regions where they are used. Besides, the two series of mathematics textbooks we selected in this study were developed according to the national mathematics curriculum standards.

There are two textbooks for every grade level in all the above three series of mathematics textbooks except for Grade 9 in the Shanghai textbooks, because there is an additional textbook in Grade 9 for the enrichment of learning, which is the compulsory curriculum for every student who uses the series.

**Process**

After selecting the textbooks, we used the content analysis method and examined all the textbooks to address the research questions mentioned above with focus on the following aspects.

- Regarding how mathematicians are represented in the mathematics textbooks, we focused on how the topics of mathematicians are distributed in the textbooks in terms of the grade level, mathematical content, the structure of chapters in the textbooks, the nationality and the periods of time.
- Regarding the similarities and differences on the representation of mathematicians among the three series of textbooks, we further examined the textbooks from the perspective of comparison in terms of the distribution as mentioned above.

More specifically, focusing on the representation of mathematicians in the selected textbooks, we identified the mathematicians by their names appearing in the textbooks by reading the three series of mathematics textbooks. It should be noted that the portraits and pictures of mathematicians are also included in this study, but some mathematical terms with mathematicians’ names, for example, Pythagoras’ Theorem, Heron-Qin Jiushao Formula and so on, were not taken into consideration in the study.

We looked at the distribution in the following aspects by counting the numbers of pages, the paragraphs where mathematicians appear and the number of times mathematicians were mentioned in the selected textbooks. In this regard, we firstly analysed the distribution of mathematicians from Grade 1 to Grade 9. Secondly, consistent with the Chinese national curriculum standards, we divided mathematical contents into the three broad areas: number and algebra, shape and geometry, and probability and statistics. Thirdly, we analysed each chapter in the textbooks in terms of the introduction, main texts, examples, exercises and reading materials. Finally, we categorised the nationalities or ethnic origins of the mathematicians introduced in the textbooks into Chinese and non-Chinese in terms of the periods of time, i.e., ancient time (before 1840), modern time (1840-September 1949) and contemporary time (October 1949-present), which is based on the commonly used division of the timelines of the Chinese history in China.

To ensure reliability of the coding, we invited an external coder to code the number of times mathematicians were mentioned in the mathematics textbooks of both the Shanghai series and the PEP series, and we got a high consistency with agreement of 0.988 and 0.993 respectively, which indicates that the data collected from the coding is highly reliable.

**Findings and Discussions**

The findings of the study are reported below in four aspects of the distributions of the introduction of mathematicians in the three series of the mathematics textbooks, i.e., the distribution across the grade level, the distribution across mathematics

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4 Qin Jiushao (1208-1268) is an ancient Chinese mathematician living in the Song Dynasty.
content areas, the distribution in terms of the structure of chapters, and the distribution in terms of ethnic origins and timelines of history.

1. How the introductions of mathematicians are distributed across the grade levels

The distribution of the introductions of mathematicians in the three series of mathematics textbooks across the different grade levels is shown in Table 1.

It can be seen from Table 1 that among the textbooks of each selected series, pages where mathematicians are mentioned account for no more than 2% of the total number of pages. In other words, it is common for the three series that the contents related to the topic of mathematicians take up a very small percentage of the entire series. To us, this result is largely expected and understandable as the main intention of introducing the topic of mathematicians into school mathematics textbooks is to help pupils learn mathematics instead of mathematicians; after all, these are textbooks of school mathematics, not mathematics history.

Among the three series of mathematics textbooks, the PEP mathematics textbooks used the largest number of pages to introduce mathematicians and its proportion in the total number of pages is also the largest. In comparison, the number of pages where mathematicians were introduced in the Shanghai mathematics textbooks is the smallest. In fact, it is almost half the number in the textbooks published by PEP. In a sense, this also explains why the total number of pages in the Shanghai mathematics textbooks is the smallest. Nevertheless, although the pages where mathematicians were mentioned in the textbooks published by BNUP are more than the Shanghai textbooks, these pages take up 1.37% and 1.34% of the total number of pages in the two series respectively. In other words, the proportions

| Grade level | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Total |
|-------------|---|---|---|---|---|---|---|---|---|-------|
| Shanghai    |   |   |   |   |   |   |   |   |   |       |
| Pages       | 0 | 1 | 1 | 1 | 1 | 1 | 6 | 3 | 9 | 25    |
| Times       | 0 | 1 | 1 | 2 | 3 | 13| 8 | 33| 4 | 65    |
| PEP         |   |   |   |   |   |   |   |   |   |       |
| Pages       | 0 | 2 | 1 | 3 | 4 | 7 | 14| 8 | 10| 49    |
| Times       | 0 | 1 | 1 | 2 | 3 | 13| 8 | 33| 4 | 65    |
| BNUP        |   |   |   |   |   |   |   |   |   |       |
| Pages       | 0 | 1 | 3 | 2 | 4 | 2 | 6 | 8 | 6 | 32    |
| Times       | 0 | 1 | 1 | 2 | 3 | 7 | 10| 20| 16| 81    |

Note: 1 Each figure in the brackets in the rows of “Pages” in the table above refers to the percentage that the number of pages where mathematicians were mentioned takes up in all the pages of each series of mathematics textbooks in each grade level, e.g., “(0.62)” means 0.62%.

2 Each figure in the brackets in the rows of “Times” in the table above refers to the number of different mathematicians who appear in each series of mathematics textbooks in each grade level.

3 Each figure in the first rows of “Times” in the table above refers to the number of the names of mathematicians appearing in each series of mathematics textbooks in each grade level.
of the topic of mathematicians in both the Shanghai textbooks and the BNUP textbooks are very close. A similar finding about the number of different mathematicians introduced was also observed in the three series of textbooks, i.e., the mathematics textbooks published by PEP introduced the largest number of mathematicians, more than 1.5 times the number in any of the other two series.

The study also looked at the number of paragraphs mentioning mathematicians on each page where mathematicians were introduced, as an indicator of how long mathematicians were actually introduced each time. The results show that the average length of the introduction of mathematicians in the three series of textbooks are all more than 1.5 paragraphs, and from the longest to the shortest, it is the PEP textbooks, the Shanghai textbooks and the BNUP textbooks. Furthermore, the average length in the first two series of textbooks are slightly over 2 paragraphs, and this descending order is consistent with the order of the number of times introducing mathematicians on each page where the topics of mathematicians were introduced, with the average number of the times in each of the three series is slightly over 2.5 times.

Further examining the distribution of the introduction of mathematicians across all the nine grades, we can see that all three series of textbooks start to introduce the topic from Grade 2, though the mathematicians introduced in Grade 2 of the three series are all different. Figure 1 shows an example introducing a Chinese mathematician ZU Chongzhi.

Figure 1. A reading material introducing a well-known ancient Chinese mathematician at Grade 2 from the BNUP series (Wang & Qian, 2014: 30).
found in the third chapter, “Large Number in Life”, in the BNUP mathematics textbooks for the second semester of Grade 2.

It was also found that, although the introductions of mathematicians in all the three series is widely spread over both primary and junior secondary stages, they are much more heavily concentrated in the junior high school stage. This distribution is understandable as, in comparison with the primary stage, the junior secondary stage covers more mathematics contents, especially those with well known historical roots which are largely linked to mathematicians. In addition, the presentations of mathematicians in all the three series at the primary stage were consistently found with shorter paragraphs and fewer words, compared with the junior secondary stage. It appears clear to us this is related to the cognitive levels of pupils at different stages of learning.

How the introductions of mathematicians are distributed across different mathematics content areas

Table 2 presents a summary of the results about the distribution of the introductions of mathematicians across different mathematics content areas.

As shown in Table 2, although the PEP mathematics textbooks introduced more mathematicians than the other two textbooks, the introductions of mathematicians in all three series of mathematics textbooks are concentrated highly consistently in two areas: the first is “number and algebra” and the second is “shape and geometry”.

In contrast, the introduction of mathematicians in the area of “probability and statistics” is very little, and in particular there are no mathematicians mentioned in the textbooks published by BNUP, which in our view is not ideal. On the other hand, it should be pointed out that the result is to some extent not surprising, as the content of probability and statistics only takes up a small percentage in the curriculum for the compulsory education stage in China.

It was also noticeable that some mathematicians were introduced a few times in each series of the textbooks and in different topics, indicating those mathematicians made contributions to the advancement of mathematics in different areas and/or have special historical and cultural values in the learning of mathematics. A particular case of this treatment is LIU Hui, a great ancient Chinese mathematician, who was introduced in two areas, namely, “number and algebra” and “shape and geometry”.

| Mathematics content | Number and algebra | Shape and geometry | Probability and statistics |
|---------------------|--------------------|--------------------|----------------------------|
| Pages (Shanghai)    | 14                 | 10                 | 1                          |
| Paras (Shanghai)    | 23                 | 29                 | 1                          |
| Times (Shanghai)    | 28                 | 36                 | 1                          |
| Pages (PEP)         | 24                 | 23                 | 2                          |
| Paras (PEP)         | 52                 | 57                 | 4                          |
| Times (PEP)         | 57                 | 73                 | 4                          |
| Pages (BNUP)        | 16                 | 15                 | 0                          |
| Paras (BNUP)        | 28                 | 29                 | 0                          |
| Times (BNUP)        | 41                 | 39                 | 0                          |

Note: A Chinese mathematician, HUA Luogeng, is introduced one time in the preface of the mathematics textbook published by BNUP for the second semester of Grade 5 and it doesn’t relate to any specific mathematics content, so it was not included in the table.
Figure 2 and Figure 3 show how LIU Hui was introduced in the textbooks, with one from the chapter of "Meaning and Nature of Decimals" in the PEP mathematics textbooks for the second semester of Grade 4, and the other from the chapter of "Circle and Sector" in the Shanghai mathematics textbooks for the first semester of Grade 6.

Do you know?
Decimals were first proposed and used in our country. It was in the third century AD that LIU Hui, a mathematician in China, proposed that the part smaller than the one digit in a whole number that could not be denoted be called Wei (tiny) number.

Figure 2. A reading material introducing Hui LIU in the PEP series (Lu & Yang, 2014: 33).

Reading materials
LIU Hui is an outstanding mathematician in the Wei Jin period of China and one of the founders of the ancient Chinese mathematical theory. While carefully studying the ancient Chinese mathematical masterpiece "Nine Chapters of Arithmetic", he adopted the method of gradually increasing the number of the sides of regular polygons to approach the circumference (also known as the method of circle cutting) to get the approximate value of $\pi$ as $\frac{3927}{1250} = 3.1416$, which was the most accurate approximate value in the world at that time.

Figure 3. A reading material introducing LIU Hui in the Shanghai series (Huang, 2015: 120).
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It is also interesting to know that the numbers of pages and paragraphs where LIU Hui was mentioned and the number of times LIU Hui was mentioned in each of the three series were almost evenly distributed across the two parts, i.e., “number and algebra” and “shape and geometry”. In a sense, it suggests that LIU Hui’s contribution and its related educational value in terms of the history of mathematics are commonly recognized by the textbook developers of all the three series of textbooks.

How the introductions of mathematicians are distributed in terms of structure of the chapters

The study further looked at where mathematicians were introduced in each chapter of the textbooks across the three series. The results are shown in Table 3.

In Table 3 we can see that the introduction of mathematicians in all the three series of mathematics textbooks is predominantly found in reading materials, and we think it is understandable as students can learn more about mathematicians by reading materials than in other ways. In fact, many reading materials provided in the textbooks were intended to introduce mathematics culture and history related to the mathematics contents covered in the chapter.

Apart from the reading materials, the three series introduced mathematicians in different places in the chapters and a considerable difference exists across these three series, as shown in Table 3.

Figure 4 and Figure 5 provide two related examples, showing how the same ancient great Greek mathematician, Diophantus, was introduced in the PEP and BNUP textbooks, both in the same chapter, “linear equation with one unknown”, in the first semester of Grade 7.

Table 3. Distribution of the introductions of mathematicians in terms of structure.

| Textbook series | Chapter introduction | Main texts | Examples | Exercises | Reading materials |
|-----------------|----------------------|------------|----------|-----------|-------------------|
| Shanghai        | Pages 1              | 6          | 0        | 1         | 17                |
|                 | Paras 5              | 7          | 0        | 1         | 40                |
|                 | Times 6              | 8          | 0        | 1         | 50                |
| PEP             | Pages 0              | 9          | 1        | 6         | 33                |
|                 | Paras 0              | 19         | 1        | 14        | 79                |
|                 | Times 0              | 20         | 1        | 14        | 99                |
| BNUP            | Pages 2              | 1          | 1        | 2         | 26                |
|                 | Paras 5              | 1          | 3        | 2         | 47                |
|                 | Times 5              | 1          | 4        | 2         | 69                |
13. (Ancient problem) Diophantus is a mathematician in Greece (between the third century AD and the fourth century AD), and his tombstone tells:

“His boyhood lasted one sixth of his life; his beard grew after one twelfth more of his life; he married after one seventh of his life more; and his son was born 5 years later; the son lived to half of his father’s age, and the father died 4 years after the son.”

Based on the information above, please work out:
(1) the life span of Diophantus;
(2) the age of Diophantus when he became a father;
(3) the age of Diophantus when his son died.

Figure 4. An exercise about Diophantus from the PEP series (Li, 2012: 108).

In the above examples, both series used the same Diophantus’s life story (though with slightly different Chinese translations) and provided the same question about the life of Diophantus, but the PEP mathematics textbook treated it as an exercise with two additional questions as part of students’ review of the chapter they have learned, while the BNUP textbook used it as an introduction to open the chapter for students to learn. It is clear from the examples that there are different ways to present mathematicians in the textbooks.

How the introductions of mathematicians are distributed in terms of ethnic origins and timelines of history

Finally, the study examined the distribution of the introduction of mathematicians in terms of ethnic origins and the timelines of history across the three series of the textbooks. The results are shown in Table 4.

As we can see in Table 4, most mathematicians introduced in the three series belong to ancient times and most of them are non-Chinese; and only a very small number of mathematicians introduced in the textbooks belong to the modern and contemporary times, which is particularly the case in the Shanghai textbooks and the BNUP textbooks.
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Diophantus is an ancient Greek mathematician. People know very little about his life, but an epitaph passed down described his life:

Here lies Diophantus, the wonder behold. Through art algebraic, the stone tells how old: God gave him his boyhood one sixth of his life, one twelfth more as youth while whiskers grew rife; and then yet one-seventh ere marriage begun; in five years there came a bouncing new son. Alas, the dear child of master and sage after attaining half the measure of his father’s life chill fate took him. After consoling his fate by the science of numbers for four years, he ended his life.

-from the 126th problem in the Greek anthology

Can you find how old Diophantus was when he was dead?

What do you know about equations?

What is the key for solving real life problems using equations?

In this chapter, we will learn the concept of equation, its solution and its application. There will be adequate opportunities for us to appreciate the ideas of modelling using equations.

Figure 5. An introduction of the chapter about Diophantus from the BNUP series (Gu, 2013: 129).

Table 4. Distribution of the introductions of mathematicians in terms of ethnic origins in timeline of history.

| Timeline of history | Nationality |  |  |  |  |  |
|---------------------|-------------|---|---|---|---|---|
|                     | Ancient     |  |  |  |  |  |
|                     | Chinese     | Non-Chinese | Chinese | Non-Chinese | Chinese | Non-Chinese |
| Shanghai            | Pages       | 9 | 17 | 0 | 1 | 2 | 0 |
|                     | Paras       | 22 | 26 | 0 | 2 | 3 | 0 |
|                     | Times       | 29 | 31 | 0 | 2 | 3 | 0 |
| PEP                 | Pages       | 17 | 30 | 1 | 4 | 4 | 2 |
|                     | Paras       | 28 | 66 | 3 | 3 | 8 | 5 |
|                     | Times       | 32 | 76 | 3 | 4 | 10 | 8 |
| BNUP                | Pages       | 12 | 22 | 2 | 2 | 3 | 0 |
|                     | Paras       | 10 | 32 | 2 | 1 | 3 | 0 |
|                     | Times       | 27 | 46 | 3 | 2 | 3 | 0 |

Note: 1 In this study, we adopted the commonly used definition of timelines of history in China, i.e., Ancient: before 1840, Modern: 1840-1949, and Contemporary: after 1949.
2 There are some overlaps on the numbers of pages as the result of the different classifications.
At the same time, it can also be observed in Table 4 that more mathematicians introduced who belong to ancient times are non-Chinese in all the three series of mathematics textbooks in terms of the three indicators in the above table.

It is also clear that there exist considerable differences in the introduction of mathematicians, particularly those in modern and contemporary times, across the three series. In comparison, the PEP textbooks present a more widely spread distribution of the introduction of mathematicians both in terms of ethnic origins and in terms of the timelines of history, which to us is commendable and probably related to the textbook developers' experiences and guiding principles.

**Summary and concluding remarks**

This study examined how mathematicians are represented in three series of Chinese mathematics textbooks at the primary and secondary levels. The results revealed that starting from Grade 2, the three series of the Shanghai mathematics textbooks, the PEP mathematics textbooks and the BNUP mathematics textbooks all paid some attention to the introductions of mathematicians across the different grade levels. On the other hand, all the series paid more attention in the junior secondary school stage as compared with the primary school stage, which we think is clearly related to the content of mathematics for students to learn in the two different stages.

In terms of mathematics contents, the introductions of mathematicians in all the three series are concentrated in the topics of "number and algebra" and "shape and geometry". In terms of the structure of chapters, most mathematicians were introduced in the reading materials instead of the other parts. The former is consistent with the distribution of mathematics contents in mathematics curriculum standards at the compulsory education stage, while a possible reason for the latter is that students can learn more about mathematicians by reading materials than other ways.

We think it is commendable that each of the Shanghai, PEP and BNUP series introduced both Chinese and non-Chinese mathematicians, though most of the mathematicians introduced are ancient mathematicians, which in our view is understandable as the knowledge covered in the school textbooks is mainly basic knowledge in mathematics that mankind has known or discovered since ancient times.

From a comparative perspective, the mathematics textbooks published by PEP introduced the most mathematicians, which largely suggests that the PEP series paid more attention to the introduction of mathematicians, as compared with the other two series.

Furthermore, it appears clear to us that the mathematics textbook series by the PEP presented a more balanced distribution of the introductions of mathematicians in terms of grade levels, ethnic origins and the timeline of history. It would be interesting to find out what are the reasons behind the different treatments as mentioned earlier, which is beyond the scope of this study and deserves further investigation, e.g., through interviewing the authors of these series of school mathematics textbooks to know their views about the values and methods of integrating the topic of mathematicians into school mathematics textbooks and why they treated it in this way or that way. In addition, it is also worth exploring how different treatments of the topic of mathematicians would impact teachers' teaching and students' learning of mathematics in classroom.
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How are mathematicians as part of mathematics history represented in contemporary Chinese school mathematics textbooks?

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КАКО СУ МАТЕМАТИЧАРИ КАО ДЕО ИСТОРИЈЕ МАТЕМАТИКЕ ПРЕДСТАВЉЕНИ У САВРЕМЕНИМ КИНЕСКИМ УЏБЕНИЦИМА МАТЕМАТИКЕ?

У оквиру исјајавања о уџбеницима мајемајмайксе, која су у Јошдеве две деценије ириукла Јошдеве научника широм Јошдеве због важне улоге коју уџбеници имају у настави мајемајмайксе (нпр. Fan et al., 2013; Schubring & Fan, 2018), има много исјајавања која се базе исјајавијом мајемајмайксе у уџбеницима за овај јеремеи (нпр. Eren et al., 2015; Ju et al., 2016; Schorcht, 2018). Неки исјајававачи су иши корак даље ийердеви да су мајемајмайчари као јема займава асекти исјајари мајемајмайксе (нпр. Shen et al., 2013; Wang et al., 2015). Међутим, мали је број исјајавања која се базе начином на који су мајемајмайчари јередсіаљвени у школским уџбеницима мајемајмайксе (вица у Castaneda et al., 2019), иако неки исјајававачи смажају да је увођење мајемајмайчара у уџбенике начин да се исјајори мајемајмайксе корисни у мајемајмичком образовању (уй. Fauvel, 1991).

Као део наших наставоља да разумемо како се исјајори и култура манифестују у уџбеницима мајемајмайксе, у овом исјајавању Јосиве смо исјајавали како су мајемајмайчари јередсіаљвени у љире различите серије савремених уџбеника мајемајмайксе које се кориспе у основним школама и низним разредима средње школе у Кини. Послали смо два исјајавачки вишеља:

1. Како су мајемајмайчари, као део исјајори мајемајмайксе, јередсіаљвени у љире серије савремених кинеских уџбеника мајемајмайксе?
2. Које сличносји и разлике Јосиве у јередсіаљвљању ових мајемајмайчара у уџбеницима?

Међу и Јосивуци. За Јођеве исјајавања изабране су следеће љире серије уџбеника мајемајмайксе:

Серија 1: Уџбеници мајемајмайксе у издању Shanghai Juvenile and Children Publishing House (Разрег 1.-2.) и Shanghai Education Publishing House (разрег 3.-9.);
Серија 2: Уџбеници мајемајмайксе у издању People's Educational Press (PEP);
Серија 3: Уџбеници мајемајмайксе у издању Beijing Normal University Press.
После селекције уџбеника користили смо мейндру анализе садржаја и анализирали све уџбенике, а јосеће нас је занимало да утврдимо како су јеме о математичарима распоређене у уџбеницима у односу на разред, математичке садржаје, структуру и огледало у уџбеницима, националност представљених математичара и временске периоде у историји математике.

Према налазима истраживања, све три серије уџбеника уврштавају на јохвалан начин како кинеске математичаре, шако и оне који нису Кинези, мада се углавном ради о математичарима из античких времена. Такође је уочено да се у све три серије уџбеника математичар доследно представља сваке године и у сваком разреду, од другог до деве- што разреда, с тим да им се мало већа пажња поклања у нижим разредима средње школе. Поређење нивоа доследности у посредству редоследа представљања математичара у ове три серије у односу на математички садржај, са фокусом на теме као што су „број и алгебра” и „облик и геометрија”, и структуру погледа, шако и огледало математичара у уврштавања у односу на читале. Поређења нивоа, ойкирили смо да је у серији уџбеника математичар у уврштавања People’s Educational Press редослед представљања математичара уравновешенији у посредству нивоа разреда, етничког порекла и временске линије. Било би занимљиво да се у наредним истраживањима ойкирије разлоги за разлику у редоследу представљања математичара и како ћа разлика утиче на наставу математике.

Кључне речи: уџбеници математике, математичко образовање у Кини, математичари у уџбеницима, историја математике, анализе уџбеника.