Topological graph-based analysis of solid-state ion migration

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To accelerate the development of ion conducting materials, we present a general graph-theoretic analysis framework for ion migration in any crystalline structure. The nodes of the graph represent metastable sites of the migrating ion and the edges represent discrete migration events between adjacent sites. Starting from a collection of possible metastable migration sites, the framework assigns a weight to the edges by calculating the individual migration energy barriers between those sites. Connected pathways in the periodic simulation cell corresponding to macroscopic ion migration are identified by searching for the lowest-cost cycle in the periodic migration graph. To exemplify the utility of the framework, we present the automatic analyses of Li migration in different polymorphs of VO(PO4)2, with the resulting identification of two distinct crystal structures with simple migration pathways demonstrating overall <300 meV migration barriers.

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INTRODUCTION

The migration of charged ions (e.g., Li, Mg, Na, O2− etc.) through solid-state materials is the primary physical mechanism behind the operation of Li-ion batteries, solid-oxide fuel cells, and solid-state electrolytes. Rapid identification and discovery of new materials with favorable migration characteristics is key to developing all-solid-state batteries where the current state-of-the-art organic electrolytes are replaced with a solid-state alternative, leading to improved power density and safety. Traditionally, the discovery of electrode materials has focused on compounds that contain the migrating ion in their as-synthesized state. However, this is not a strict requirement, and many materials synthesized without the migrating species are capable ion conductors. In fact, it has been shown that for multivalent applications, materials that are synthesized without the migrating species are capable ion conductors. In many cases, the working ion tend to exhibit a greater migration energy (∼300 meV) than the potential energy supplied by the battery (∼3.5 eV for Li). The migration energy barrier can be reduced significantly by engineering the structure of the host lattice to facilitate Li migration. For example, the migration energy barrier can be reduced by engineering the structure of the host lattice to facilitate Li migration. The established method for identifying the optimal path between two sites in a crystal is the nudged-elastic band (NEB) method. However, NEB calculations are computationally costly and are only able to analyze short-distance migration events provided that an initial, reasonably accurate, guess for the connecting path is available. To understand the migration characteristics of a material, the motion of the ion through the entire crystal must be considered. Recent high-throughput studies have attempted to address this either by simplifying the problem to analyzing the migration of a single working ion particle in a fictitious field or by focusing on individual migration events but not how they connect over larger distances. While it is possible to analyze intermediate concentrations, the large configurational space associated with the working ion ordering arrangements make a thorough investigation computationally demanding and not suitable for high-throughput evaluation of viable intercalation pathways. For vacancy migration, a priori knowledge of the working ion sites makes the construction of migration graphs trivial. In materials where we lack knowledge of working ion sites, we utilize a recently developed methodology that allows us to systematically identify metastable intercalation sites in any crystalline structure. Here, we build upon this framework and present a graph theory extension to automatically identify ion migration pathways in any periodic solid. The migration is treated as a periodic graph where symmetrically equivalent copies of the metastable sites constitute the nodes and the individual migration events between these sites are the edges. Additionally, we assign a cost to the graph edges based on the migration energy barriers and showcase how optimal intercalation pathways can be discovered with a Dijkstra’s-inspired algorithm defined on the periodic graph. The original code provided here is distributed as an extension to the pymatgen material analysis library. We demonstrate our framework on two well-known structures of MnO2 and CoO2 to show how the migration graphs can be constructed and utilized. Finally, the methodology is applied to the different configurations of VO(PO4)2 in the Materials Project to assess the migration characteristics of each polymorph, and we exemplify the capability to identify promising new ionic conductors within this set of materials.

RESULTS & DISCUSSIONS

Site identification

Our graph-based migration analysis is best suited for the two limits of working ion occupation, either single-ion migration in the dilute limit or vacancy migration in the fully intercalated limit. While it is possible to analyze intermediate concentrations, the large configurational space associated with the working ion ordering arrangements make a thorough investigation computationally demanding and not suitable for high-throughput evaluation of viable intercalation pathways. For vacancy migration, a priori knowledge of the working ion sites makes the construction of migration graphs trivial. In materials where we lack knowledge of working ion sites, we utilize a recently developed, generally robust computational workflow for identifying the metastable sites of the working ion in any structure. The methodology selects candidate sites at the local minima of charge density and, for each candidate site, a working ion is inserted and the structure is...
allowed to relax using density-functional theory calculations. An inserted structure is considered “topotactic” if the positions of its framework atoms closely resemble the relaxed atomic positions of the host material. The metastable sites are obtained by mapping the working ion in the topotactically inserted structures onto the empty host structure and identifying all symmetry-equivalent positions in the host structure. Based on the location and connectivity of the metastable sites, we build our graph-based migration analyses.

To exemplify our approach, we use two materials: MnO₂ in the \( \lambda \) phase\(^{11} \) with cubic spinel structure and layered CoO₂ with ABBA stacking\(^{12} \). After performing independent single Li insertions into the sites suggested by the charge density analysis and relaxing the new structures\(^9, \) two distinct singly-inserted structures for each material were topotactically matched to the host material as shown in Fig. 1. We denote the base structure \( S_{\text{base}} \) and the set of relaxed inserted topotactic structures \( \{ S_{\alpha} \} \) where \( \alpha \in \{ A, B \} \) for both examples. Since the host sublattice (which does not contain the working ion) of each \( S_{\alpha} \) can be mapped onto \( S_{\text{base}} \), the relaxed positions of the cations in each structure can also be mapped to position \( s_{\alpha} \) in \( S_{\text{base}} \). This mapping allows us to identify two symmetry-distinct metastable sites \( s_{\alpha} \) (blue) and \( s_{\beta} \) (orange) for MnO₂ and CoO₂, respectively. Utilizing the apglib package\(^{13} \) and its interface with pymatgen\(^{14} \), we analyze the crystal symmetry of the structure with the inserted ion, \( S_{\text{base}} \), and apply the valid point group operations to each \( s_{\alpha} \) to generate all of the possible cation positions, designated by an integer index value \( i \) at position \( r_{\alpha} \) in the unit cell.

In MnO₂, the \( s_{\alpha} \) metastable site is represented by the fractional coordinates \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) and all space-group operations of the host material will either map the site to itself or \( \left( \frac{i}{8}, \frac{j}{8}, \frac{k}{8} \right) \). The \( s_{\beta} \) site is represented by the fractional coordinates \( \left( 0, 0, 0 \right) \), which has three additional symmetry-equivalent sites as shown in Table 1. This results in a total of six metastable sites per unit cell, as shown in Fig. 1d. We perform the same analysis for CoO₂, which results in \( s_{\alpha} \) and \( s_{\beta} \) at the face centers of the primitive cell. The space-group operations of CoO₂ map the sites onto periodic images of the original, as such, no new symmetrically-equivalent sites are created from symmetry operations, the resulting two metastable sites are shown in Fig. 1g.

We can see how the charge-density based site identification performs across a wide range of structures and intercalating ion types by examining the distributions of the distances between the charge-density local minima and the nearest metastable sites. To accomplish this, we queried the Materials Project database for Li, Mg, and Ca cathode materials where the fully-charged entry does not contain the intercalating species. To keep the numbers of entries for each ion type comparable, we limit the Li search to entries where the host material's decomposition energy (energy above convex hull) is less than 0.01 eV/atom, compared to 0.1 eV/atom for Mg and Ca. This resulted in 196 battery materials for Li, 145 for Mg, and 111 for Ca. For these materials we examined the topotactically matched structure in the Materials Project database with the lowest fraction of the inserted ion to obtain a set of metastable insertion sites. The distribution of the distances between these metastable sites and the nearest local minimum in the charge-density is shown in Fig. 2 where the distributions for the different inserted species are stacked on top of each other. From this, we see that Mg and Ca ion insertions exhibit better performance for insertion algorithm. For the larger cations (Mg, Ca), the insertion algorithm is able to guess within 1 Å of the metastable site in the overwhelming majority of cases. For Li, since the insertion cavity can be much larger than the Li ion, the ion can relax to a position that is further from the initial guess once charge is exchanged between Li and the host structure. However, this degree of ionic relaxation should not be problematic for the ionic relaxation algorithms in modern DFT codes.

**Graph analysis**

Using a distance cutoff of \( l_{\text{max}} \), we connect two nearby metastable sites \( r_{i} \) and \( r_{j} \) to represent a discrete migration event in the material which we will call a “hop”. The network formed by these hops is infinite and the following convention ensures that we only consider hops that are inequivalent by lattice transitions. Each hop between sites \( i \) and \( j \) in the periodic unit cell is labeled \( h_{\alpha}^{\beta} \) where the additional index \( K \) is an integer-value vector representing the relative periodic image displacement between the endpoints [i.e. \( K = (0, 0, 1) \) means that the hop crosses a period cell boundary once in the positive c-direction]. In general, we consider the migration graph to be undirected. As such, the hops \( h_{\alpha}^{\beta} \) and \( h_{\beta}^{\alpha} \) will represent the same migration event, but only one representation will be present in the graph. As a convention to prevent double-counting, we require the site indices to satisfy \( i \neq j \). Additionally, since there is ambiguity when \( j = i \) and \( K = 0 \), we only retain the hop where the first non-zero component of \( K \) is positive.

Using a threshold value of \( l_{\text{max}} = 3 \) Å, the migration graph for Li\(^{15} \) in MnO₂ (denoted as \( \mathcal{G}(\text{MnO}_2) \)) is constructed and shown in Fig. 3a, b. There are 18 hops in \( \mathcal{G}(\text{MnO}_2) \) that are not equivalent under discrete lattice translations. Using the space group
The symmetry between the hops, we can reduce them to 2 symmetry-distinct groups indicated by the edge color in the graph. The Li⁺ migration graph in CoO₂, with 8 hops in 3 symmetry-distinct groups, is shown in Fig. 3c, d. For a complete enumeration of the migration hops in these two materials and their symmetry equivalence, see Supplementary Table 2 and 3 in the Supplementary Information. In principle, once we have identified the symmetrically equivalent groups, we can obtain the migration barrier using NEB calculations to chart the migration energy landscape of the material.

A potential ion-conducting material must enable a continuous migration pathway for the working ion across the unit cell, connecting to the next one. In a periodic system, continuous pathways are infinite, which we term “intercalating pathways”. Since our migration graph contains only one copy of each node, periodicity manifests via the image displacement vector \( \mathbf{K} \). The intercalating pathways are essentially cycles in the graph where the total image displacement is non-zero. The series of hops in such a cycle will connect a metastable site to a different periodic image of itself, which constitutes a repeating unit of an infinite periodic migration pathway. Basic examples of intercalating pathways are highlighted in light green in (b, d).

**Table 1.** Space group mapping of Li positions \( s_i \) in MnO₂ under the space group operations host crystal structure.

| Index | Label | Original position | Host transformations* | Transformed position |
|-------|-------|-------------------|----------------------|---------------------|
| 0     | \( s_0 \) | \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) | \((x, y, z), (z, -x - y - z + \frac{1}{8}, x)\) | \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) |
| 1     | \( s_1 \) | \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) | \((-x - y - z + \frac{1}{8}, z, y), (y, x, -x - y - z + \frac{1}{8})\) | \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) |
| 2     | \( s_2 \) | \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) | \((y, z, -x - y - z + \frac{1}{8}), (-x - y - z + \frac{1}{8}, x, y)\) | \( \left( \frac{1}{8}, \frac{1}{8}, \frac{1}{8} \right) \) |
| 3     | \( s_3 \) | \( (0, 0, 0) \) | \((x, y, z), (-z, -y, -x)\) | \( (0, 0, 0) \) |
| 4     | \( s_4 \) | \( (0, 0, 0) \) | \((-x - y - z, z, y)\) | \( (0, 0, 0) \) |
| 5     | \( s_5 \) | \( (0, 0, 0) \) | \((y, z, -x - y - z + \frac{1}{8}), (-y, x, -y - x - y - z + \frac{1}{8})\) | \( (0, 0, 0) \) |

*Determined by the SpaceGroupAnalyzer.

The positions of the \( s_i \)'s and their images are given in fractional coordinates.
pathways are highlighted in light green in Fig. 3b, which connect a node to a periodic image of itself. To identify these pathways, we used a modified Dijkstra’s type algorithm on the periodic graph. The key difference between the modified algorithm and the original Dijkstra’s algorithm is that the periodic image vector is tracked during graph traversal. This means that the optimal cost to reach any node during the graph traversal is defined for the combination of node index $i$ and periodic image vector $K$. A detailed description of the path-finding algorithm on the periodic graph is presented in the SI (Supplementary Algo. 1). The cost function employed in the path-finding algorithm can be any positive definite function assigned to the edges of the graph. A good choice in most cases is the migration energy barrier (defined as the maximum difference between the NEB energy and the linear interpolation between the site energies) for the ion-migration event represented by that particular edge. However, the difference between the binding energies of the endpoints, which can be computed without expensive NEB calculations, may also be used as a lower bound of the activation barrier for screening purposes.

Application to polymorphs of VO(PO₄)

We demonstrate the utility of the obtained migration graphs for Li migration in VO(PO₄). Of all 18 VO(PO₄) phases currently available in the Materials Project, five are distinct known, synthesized phases with the following IDs (spacegroup symbols): mp-25265 (Pmma), mp-556459 (Cc), mp-559299 (P4/n), mp-763482 (P4/n), mp-1104567 (C2/m). While all five phases listed above have been experimentally synthesized, only some of them have readily available electrochemical analysis data. In particular, mp-25265 ($β$-VOPO₄) demonstrates a capacity of 118.6 mAh/g against Li insertion at average 4 V$^{16}$, and mp-556459 (e-VOPO₄) has shown a capacity of 305 mAh/g against Li insertion over two voltage plateaus at about 4.0 and 2.5 V$^{16}$. For each of the five structures, we performed a set of ion insertions to generate metastable sites and constructed the migration graphs, yielding connectivity of hops to form intercalation pathways. With the connectivity of the graph established, the only missing piece to a complete description of the intercalation behavior is understanding of the ion migration energy evolution during the individual hops.

The energy profile for each hop can be estimated by utilizing the ApproxNEB method$^{17}$ in atomate. The ApproxNEB method performs independent constrained optimizations for each image structures which allows us to trade accuracy for speed since the independent relaxations are trivially parallelized. Each phase of VO(PO₄) has 3 to 10 such hops and thus 3 to 10 ApproxNEB calculations. Due to the high computational cost involved, one might find it helpful, in general, to rank migration pathways before ApproxNEB is employed. To demonstrate testing of one possible choice of cost function for this purpose, we performed charge-density analyses on these phases and compared them to our ApproxNEB results.

We examined the total charge-density in a radius 1 Å cylinder between sites the end points of a hop; $\rho_{cyl}(h^K_m)$. Since the background charge density can change between different structures, we will only focus on the relative charge barrier, defined as the ratio between the integrated charge, $\rho_{cyl}(h^K)$, and its minimum value in that particular structure; $\min(\rho_{cyl}(h^K))$. The relationship between the total charge ratio and the ApproxNEB barrier is shown in Fig. 4c, which indicates little correlation between the total charge in the cylinder and the energy barrier. Hence, while promising insertion sites could be identified by low charge-density, it is clear that local atomic relaxations around the working ion during the migration significantly impact the energy barrier such that those effects cannot be ignored. However, since the relative charge barrier is an indicator of the amount of negative charge that the migrating ion has to move through we are most interested in migration evens with low relative charge and low ApproxNEB barriers, i.e. the bottom left corner of Fig. 4c, for further analysis using ApproxNEB.

With details of the hops and their connectivity, we can now construct a complete picture of long-range migration in the system. In Figure 4a, b, we show the lowest energy barrier intercalation pathway for two of the structures (mp-25265 and mp-559299) that contain multiple low-barrier hops. In order to reach an accurate description, we performed NEB calculations when evaluating the energy landscape of each hop, the results of which show that both structures contain an intercalation pathway which has an overall energy barrier of less than 250 eV.

**Discussions**

We demonstrate that the intercalation properties of cations in a solid-state material can be fully captured by a migration graph where the metastable sites represent the nodes and the migration energy barriers are the edge weights. Using a previously-developed, unbiased cation insertion algorithm, we identify the symmetry-distinct metastable sites in the structure and generate all equivalent sites by repeatedly applying the symmetry operations of the host. The migration energy is calculated for the symmetrically-distinct hop between pairs of adjacent metastable sites and the data is replicated on symmetrically equivalent hops to obtain the migration barriers on the entire graph. To identify intercalating pathways, we detect cycles in the periodic graph. Finally, we applied this analysis framework on a diverse set of polymorph structures of VO(PO₄) and present several promising structures with low migration barriers. The framework and code presented here can be used to automatically obtain the migration properties of solid-state materials with essentially no priori knowledge. Our work opens up opportunities for high throughput studies in the future and can offer a deeper understanding of the migration properties of crystalline solids. Compared with the single-particle charge-density models by Kahle et al.$^{17,18}$, our method will typically be slower but will capture more of the quantum effects in the system since we are using NEB to analyze the discrete migration events. Since we have also developed a...
flexible charge-density API\textsuperscript{19}, we can combined these methods for future high-throughput studies.

Since this methodology relies on identification of the metastable sites, we will need to continue filling in under-explored regions of the chemical space in the Materials Project database to study migration at scale. Additionally, while our prior work\textsuperscript{9} addressed the process of identifying metastable sites to increase cation incorporation, the current work only considers the migration properties in the dilute and vacancy limits. In the future, we will need to extend the analysis to away from the dilute and vacancy limits to capture the migration characteristics for more realistic systems.

METHODS
The total energy of each atomic structure was calculated from first-principles using density-functional theory with the generalized-gradient approximation (GGA) functional of Perdew-Burke-Emzerhof (PBE) implemented in the Vienna Ab initio Simulation Package (VASP). The Hubbard $U$ values for Co, Mn, and V were set to 3.32, 3.90, and 3.25 eV, respectively.

DATA AVAILABILITY
The data that support the findings of this study are available on the Materials Project website (https://materialsproject.org).

CODE AVAILABILITY
The code for the metastable site analysis and graph analysis is available as part of the pymatgen-analysis-diffusion namespace package which acts as an add-on to the main pymatgen library.

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AUTHOR CONTRIBUTIONS
J.X.S. developed the site-mapping and graph algorithms and performed the calculations on the example MnO\textsubscript{2} and CoO\textsubscript{2} systems; H.H.L. performed the ApproxNEB and NEB calculations for the VO\textsubscript{2}(PO\textsubscript{4})\textsubscript{3} systems, A.R. developed the automated workflow to perform the ApproxNEB calculations; M.K.H. contributed design ideas and support at all stages of the algorithm development; K.A.P provided supervision and funding for the project at all stages. All authors contributed significantly to the preparation of this manuscript.

COMPETING INTERESTS
The authors declare no competing financial or non-financial interests.

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