**Design of a Wide Input Range DC-DC Converter Suitable for Lead-Acid Battery Charging**

M.W.D.R. Nayasiri and J.A.K.S. Jayasinghe, B.S. Samarasiri

**Abstract:** In this paper design and implementation of a wide input range Cascaded Buck and Boost (CBB) converter is presented with a robust power controller. Four new control strategies are proposed and tested for this converter based on input voltage and duty cycle of the control signals. Robust feature of the proposed control system ensures constant output DC current required to charge the Lead-Acid batteries in bulk charge mode. The robust feedback controller of the power converter is developed using a microcontroller which is acting as smart controller of the CBB converter. DC-DC converters which are used for battery charging applications with variable power sources should be able to both step-up and step-down the input voltage and provide high efficiency in the whole range of operation. The CBB converter with power switches and diodes is used to achieve above objective. CBB converter is constructed by cascading a Buck and a Boost Converter and eliminating the output capacitor of the Buck converter.

**Keywords:** Cascaded Buck and Boost Converter, Microcontroller, Lead Acid Batteries

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1. **Introduction**

DC-DC converters with step-up and step-down capability are required in several applications where the input and output voltage ranges overlap. As an example, in the battery charging application which uses variable input power sources such as wind mills and motor-generator units of the hybrid vehicles. Topologies such as Inverted Buck-Boost converter and Single Ended Primary Inductance Converters (SEPIC) can be used to obtain constant output voltage from variable power sources [1]. But they have low efficiency, high output ripple, high noise and spikes in the output voltage. Hence they are not suitable to implement power supplies for battery charging applications.

![Cascaded Buck and Boost Converter](image)

**Figure 1 – Cascaded Buck and Boost Converter**

A DC-DC power converter is constructed by cascading Buck and Boost Converter and eliminating the output capacitor of the Buck Converter as shown in Figure 1. This DC-DC converter has minimum components, low component stresses and low energy storage capability in order to have small size and high efficiency.

There are four possible switching states in a CBB converter topology. They are shown in Table 1.

| Switching State | S1 | S2 | Mode          |
|-----------------|----|----|---------------|
| 1               | ON | PWM| Boost         |
| 2               | PWM| PWM| Buck-Boost    |
| 3               | OFF| PWM| N/A          |
| 4               | PWM| OFF| Buck         |

In the buck mode \( V_{out} \approx V_{in} \), when duty cycle of the gate control signal is close to unity. But it is difficult to have duty cycle of the gate control signal of the power MOSFETs close to unity due to the switching limitations of the available power switches and their gate drive technologies. In boost mode of operation \( V_{out} \approx V_{in} \) occurs when duty cycle is close to zero. With existing gate drive technologies of the power MOSFETs, it is also difficult to have duty cycle close to zero.

Hence CBB converter cannot be operated satisfactorily when \( D < 0.1 \) and \( D > 0.95 \) for boost and buck mode respectively. Therefore we get a dead band as shown in Figure 2.

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In buck-boost mode, $V_{out} \approx V_{in}$ occurs when duty cycle of the power switches is close to 0.5. This range of the duty cycle can achieve easily with existing MOSFET gate drive technology. Therefore buck-boost mode is used to transfer power within the above dead band. Efficiency wise, it is not advantageous to operate this converter in buck-boost mode [2]. But in order to smooth the transients, the buck-boost mode is used to transit from buck mode to boost mode or vice versa [3], [1]. Hence four control algorithms are developed for this CBB converter to obtain smooth transition between each operation modes.

The proposed four control algorithms for this converter are based on the duty cycle of the gate control signal, input voltage and output current.

Control algorithm of the converter is based on the duty cycle of the control signal, input voltage and output current. Input voltage based control strategy is proposed in [1] for this type of converters. But, such control algorithms are not possible to use in this converter as the output load of this converter is changing while the battery pack is being charged. Hence, four new control algorithms are proposed for this converter by taking input voltage and duty cycle of the power switch control signals as control parameters.

2. Control Strategy

Control strategy of the controller is for maintaining a constant output current from the CBB converter as the converter load and input voltage changes. Main control is implemented by using a microcontroller. Closed loop control is used to develop firmware. Switching the CBB converter between buck, buck-boost and boost modes is a complex task as transients play a major role as this mode of operation changes.

2.1 Control strategy 1 - Input voltage based control strategy with zero initial duty cycle

In this algorithm, mode of operation of the CBB converter is decided using only the input voltage. The gate control signal of the power switches are initialized with zero duty cycle.

2.2 Control strategy 2 - Input voltage based control strategy with non-zero initial duty cycle

In this algorithm, mode of operation of the CBB converter is decided using input voltage. The gate control signal of the power switches are initialized with non-zero duty cycle. The duty cycle of the power switch is calculated to give minimum dips in the output current as the converter changes its mode of operation.

2.3 Control strategy 3 - Input voltage and duty cycle based control strategy

Initial mode of operation of the converter is decided using input voltage. Use input voltage as the control parameter to transit from buck-boost mode to buck mode or from buck-boost mode to boost mode. Duty cycle of the control signal is used as the control parameter when it is required to transit from boost mode to buck-boost mode or from buck mode to buck-boost mode.

2.4 Control strategy 4 - Duty cycle based control strategy

In this control algorithm, initial mode of operation is decided based on the input voltage. Subsequently controller changes its mode of operation according to the maximum and minimum allowable duty cycle in each mode of the CBB converter.
3. Specifications

CBB converter is developed to charge the 48V Lead-Acid battery pack. There are four modes in the standard Lead-Acid battery charging cycle namely: trickle charge, bulk charge, over charge and float charge. In this application, bulk charge mode is used to charge the battery pack with constant current. According to the battery standard, to charge the Lead-Acid battery in bulk charging mode, battery pack should be charged with a current rated to 10%-30% of the battery capacity. As 65Ah Lead-Acid batteries are used in this design, charging current was set to 6A.

Bulk charge mode of the Lead-Acid battery charging cycle ends up when the cell terminal voltage reaches 2.26V or 2.36V [4]. Therefore terminal voltage of the battery pack will be 56.64V at the end of bulk charge mode. Hence the output voltage of the CBB converter should vary from 48V to 56.64V.

![Table 2 – Summary of Specifications of CBB](image)

| Description         | Value               |
|---------------------|---------------------|
| I/P voltage range   | 24V-72V             |
| O/P voltage range   | 48V-56.64V          |
| O/P current         | 6A                  |
| O/P current ripple  | Max. 1A             |

4. Modes of Operation

CBB converter topology is supported for three modes of operation. In this application all three modes were implemented, inclusive of the positive buck-boost mode. Positive buck-boost mode acts as a bridge to transit from the buck mode of operation to boost mode or vice versa by providing ability to transfer the power when \( V_{in} \approx V_{out} \).

The equivalent circuit of the CBB converter is shown in Figure 3. The converter consists of input capacitor \( C_{in} \), output filter capacitor \( C_{out} \), two power switches \( Q_1 \) and \( Q_2 \), inductor \( L \) and two freewheeling diodes \( D_1 \) and \( D_2 \). The forward voltage drop of the diode is \( V_{fw} \).

![Figure 3 – Equivalent circuit of CBB converter](image)

All modes are operated at the same frequency represented by \( f \). Figure 4 depicts typical control signal provided by the microcontroller.

![Figure 4 – Control signal of power switches](image)

4.1 Buck Mode

If input voltage is greater than the output voltage or terminal voltage of the battery pack, buck mode is used. In this mode of operation, \( Q_1 \) is controlled by the Pulse Width Modulated (PWM) signal as shown in Figure 4 and \( Q_2 \) is always in OFF condition. With switching frequency \( f \) and duty cycle \( D = \frac{I_L}{T} \), input and output voltage relationship is given by equation (1).

\[
V_{out} = \frac{I_L}{T} \cdot V_{in} = D \cdot V_{in} \quad \ldots (1)
\]

This was derived by neglecting \( V_{fw} \), ON switch resistance of \( Q_1 \) and inductor resistance. The inductor current \( I_L \) has a triangle shape and its average value is determined by the load. The peak-to-peak current ripple \( \Delta I_L \) is dependent on \( L \) and can be calculated with the help of equation (2) [5].

\[
\Delta I_L = \frac{1}{T} \cdot (V_{in} - V_{out}) \cdot \frac{V_{fw}}{V_{in}} \cdot \frac{1}{f} \quad \ldots (2)
\]

4.2 Boost Mode

If input voltage is less than the terminal voltage of the battery pack, then boost mode of operation is used to step-up the voltage input in order to charge the battery. In this mode of operation, \( Q_1 \) is always ON and \( Q_2 \) is controlled by the PWM signal provided by the main controller as shown in Figure 4. The relationship between input and output voltage can be derived by neglecting diode forward voltage drop \( V_{fw} \), switch ON resistance and inductor resistance. For a switching frequency \( f \) and duty cycle \( D = \frac{I_L}{T} \), then \( V_{out} \) is given by equation (3),

\[
V_{out} = \frac{I_L}{T - \tau_m} \cdot V_{in} \quad \ldots (3)
\]
The inductor ripple current is given by equation (4) [5],
\[
\Delta i_L = \frac{1}{2} \cdot \left( V_{\text{out}} - V_{\text{in}} \right) \cdot \frac{V_{\text{in}}}{t} \cdot \frac{1}{f} \quad ... (4)
\]

4.3 Buck-Boost Mode
This mode is used when \( V_{\text{out}} \approx V_{\text{in}} \). In this mode input and output voltage relationship is given by equation (5).
\[
V_{\text{out}} = \frac{t_2}{T} \cdot V_{\text{in}} = \frac{D}{1-D} \cdot V_{\text{in}} \quad ... (5)
\]
Both power switches are controlled by PWM signals having same duty cycle \( D \). During the time \( t_2 \) both switches conduct simultaneously and during the time \( T - t_2 \) both switches are OFF and the energy stored in the inductor is released to the load.

5. System Architecture
CBB converter is constructed as a combination of different subsystems namely: input voltage monitor, output voltage monitor, output current monitor, power supply, main controller and main power path or CBB converter. This is shown in Figure 5.

![System Architecture Diagram](image)

**Figure 5 – System Architecture**

Input and output voltage monitor subsystems are implemented using voltage followers and output current monitor subsystem is implemented using a differential amplifier. Power supply of the converter is based on linear power regulators and transistor voltage regulator.

Switching frequency of the CBB is selected by considering inductor size and the power MOSFETs switching losses [6]. With higher switching frequency \( f \), size of the inductor will be small. But the switching losses of the power MOSFETs become larger as \( f \) increases. Hence operation frequency of the CBB is selected as 15.625 kHz because this value can be easily obtained from maximum PWM register value with 4 MHz crystal.

6. Design and Implementation
Same inductor (\( L \)) and same output filter capacitor (\( C_{\text{out}} \)) are used in all modes of operation of the CBB. Hence in the design process, the required inductor and output capacitor values for all modes of operation are calculated using equations (9) (11), (16) and (18). Then select the maximum value of inductor and capacitor which is calculated using above equations, as minimum inductor and capacitor value of the CBB converter.

6.1 Buck Mode
In this mode, maximum input voltage is 72V and minimum output voltage is 48V. Hence maximum duty cycle is
\[
D_{\text{max}} = \frac{V_{\text{out}}}{V_{\text{in}}} = \frac{48}{72} \quad ... (6)
\]
\[
D_{\text{max}} = 0.667 \quad ... (7)
\]
If the maximum allowable output ripple current is \( \Delta I_L = 0.2 I_C \).
\[
\Delta I_L = 0.2 I_C = 0.2 \times 6 = 1.2 A \quad ... (8)
\]
Therefore the minimum required inductor, in order to obtain continues conduction mode at the rated output current is given by equation (9).
\[
L = \frac{1}{\Delta I_L} \cdot \left( V_{\text{in}} - V_{\text{out}} \right) \cdot \frac{V_{\text{out}}}{f} = 0.853 \text{ mH} \quad ... (9)
\]
The current ripple \( \Delta I_L \) causes a voltage ripple \( \Delta V_{\text{out}} \) at the output capacitor \( C_o \). For normal switching frequencies, this voltage ripple is determined by the equivalent impedance \( Z_{\text{max}} \). The capacitors used for our design were obtained from the local market and their technical details were not available. Therefore the capacitor values were selected to give minimum output ripple current using trial and error method.

The approximate value for the output capacitor can be found using equation (10) [2],
\[
C_{\text{min}} = \frac{P_{\text{rated}} f}{\Delta V_o} \quad ... (10)
\]
This is assuming that \( \Delta V_o = 0.01 V_o \) and rated power output of the converter approximately equals to 260W.
\[ C_{o,\text{min}} = \frac{260}{15.625 \times 1.0 \times 4 \times 10} = 722 \mu F \quad \ldots (11) \]

### 6.2 Boost Mode

In this mode, minimum input voltage is 24V and maximum output voltage is 56V. Hence maximum duty cycle is,

\[ D = 1 - \frac{V_{\text{in}}}{V_{\text{out}}} = 0.5 \quad \ldots (12) \]

If maximum allowable output ripple current is \( \Delta I_L = 0.2 I_{\text{in}} \), the input current \( I_{\text{in}} \) can be calculated by assuming zero losses (\( P_{\text{in}} = P_{\text{out}} \)). Therefore:

\[ V_{\text{in}} \cdot I_{\text{in}} = V_{\text{out}} \cdot I_{\text{out}} \quad \Rightarrow \quad I_{\text{in}} = \frac{V_{\text{out}}}{V_{\text{in}}} \cdot I_{\text{out}} \quad \ldots (13) \]

\[ I_{\text{in}} = \frac{85}{24} \times 5 = 11.66A \quad \ldots (14) \]

The inductors ripple current \( \Delta I_L \) is given by equation (15).

\[ \Delta I_L = 0.2 \times 11.66A = 2.334 A \quad \ldots (15) \]

Therefore the minimum required inductor to obtain continues conduction mode at the rated output current is given by equation (16)

\[ L = \frac{1}{\Delta I_L} \cdot (V_{\text{out}} - V_{\text{in}}) \cdot \frac{V_{\text{in}}}{V_{\text{out}}} \cdot \frac{1}{f} = 0.376 \text{ mH} \quad \ldots (16) \]

By using equation (17) [2], the required output filter capacitor can be found using equation (17)

\[ C_{\text{min}} = \frac{P_{\text{rated}}}{fV_{\text{out}} \Delta V_o} \quad \ldots (17) \]

This is assuming that \( \Delta V_o = 0.01V_o \) and rated power output of the converter is approximately 260W.

\[ C_{o,\text{min}} = \frac{260}{15.625 \times 10 \times 4 \times 5} = 530 \mu F \quad \ldots (18) \]

### 6.3 Buck-Boost Mode

This mode is used in the limited input voltage range (48V-56V). In this mode, \( V_{\text{out}} \approx V_{\text{in}} \) condition is given by the duty cycle of the PWM signals in the range of \( 0.4 < D < 0.6 \).

Buck-boost mode is developed on the same physical setup is used to develop buck and boost modes and therefore same inductor and capacitor is used.

According to above calculations, the minimum inductor value was selected as 0.853 mH and minimum output capacitor as 740µF. All above calculations were performed with approximations and therefore those minimum valued components do not give the required performance. Inductor was chosen as 3.48 mH and output capacitor as 4700 µF.

Two switching transistors Q₁ and Q₂ are realized with N-channel MOSFETs (IRFP250) having 0.085Ω on resistance, 200V break down voltage, 33A maximum average current and nanosecond switching speed. In order to drive high side and low side N-channel MOSFETs, MOSFET gate drive IC (IR2101) based on bootstrap gate drive technology was used.

BYW29E low forward voltage drop (0.895V) fast switching rectifier diode was selected as D₁ and D₂. It has 200 V peak reverse voltage and 8 A continues forward current.

At the end of the design stage, the CBB converter was implemented and the test setup is shown in Figure 6.

### 7. Experimental setup

The proposed converter and control algorithm are implemented in a laboratory prototype. The performance of the buck mode and boost mode were tested separately. Then both modes were tested together against whole range of input voltage with the main controller of the CBB.

![Figure 6 – DC-DC converter test setup](image-url)

During the test, the dead band was clearly visible in the output voltage. In order to overcome this problem, buck-boost mode was developed using same test setup by modifying the firmware.

In the buck-boost mode, switching transistor Q₁ is switched with duty cycle slightly higher than that of switching transistor Q₂ due to switching limitation of the power switches. Finally all three modes were tested in the same test setup with modified main controller firmware.
8. Results

The results given below correspond to a 260W prototype with a switching frequency of 15.625 KHz.

First, the CBB converter was tested with control strategy 1 which is based on the input voltage. In this method, converter changes its mode of operation from boost to buck-boost and then to buck mode as the input voltage increases or otherwise as input voltage decreases. When converter changes its mode of operation, there were significant voltage dips in the output voltage and hence a discontinuity appeared in the output current as shown in Figure 7.

![Figure 7](image7.png)

**Figure 7 – Output current vs. Input voltage with control strategy 1.**

Then the CBB converter was tested with modified control algorithm (Control strategy 2), with an initial non-zero duty cycle for the control signals. An improvement was observed in the output current as shown in Figure 8.

![Figure 8](image8.png)

**Figure 8 – Output current vs. Input voltage with control strategy 2.**

Next the CBB converter was tested with control strategy 3 based on duty cycle and input voltage based. Dips in the output voltage and discontinuity in the output current were improved with this control strategy and the results are shown in Figure 9.

![Figure 9](image9.png)

**Figure 9 – Output current vs. Input voltage with control strategy 3.**

To overcome the deficiencies in control strategy 3, the CBB converter was tested with a control strategy which is completely based on the duty cycle of the MOSFETs control signals (Control strategy 4). With this control strategy, it was possible to solve the issues related to output voltage dips, output current discontinuity and operation voltage range. The results are shown in Figure 10.

![Figure 10](image10.png)

**Figure 10 – Output current vs. Input voltage with control strategy 4.**

The CBB converter based on control strategy 4 was used to charge the 65Ah Lead-Acid battery pack with 5.5A constant current by varying input voltage from 24V to 72V. It was observed that, this converter can be operated in pure buck and boost modes with high efficiency and in the non-inverted buck-boost mode with a lower efficiency.
Battery terminal voltage was measured with time while charging the battery pack using boost mode and varying input voltage from 24V to 40V. Results are plotted in Figure 11.

9. Conclusion

In this paper steady-state behaviour of the CBB converter is analysed and presented. The equations are derived for the buck mode and boost mode, when the converter is implemented with diodes and power switches. Selection of components and implementation details are also presented. This converter is suitable for applications which require non inverted step-up and step-down operation in a single circuit with low component count, low component stress, simplicity and high efficiency.

![Figure 11 - Battery Terminal Voltage vs. Time](image)

Although this converter is not efficient [2] in the buck-boost mode, show the importance of buck-boost mode to transfer power when $V_{out} \approx V_{in}$ in the application having overlapped input and output voltage range. Duty cycle based control strategy is more suitable to change the mode of operation of the CBB converter other than the input voltage based control strategies.

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References

1. Chakraborty, A., Khaligh, A. and Emadi, A, “Combination of Buck and Boost Modes to Minimize Transients in the Output of a Positive Buck Boost Converter” 32nd Annual IEEE Conference on Industrial Electronics Nov. 2006.

2. Schaltz Erik, Khaligh Alireza “Non-inverting Buck-Boost Converter for Fuel Cell Applications” June 2008.

3. Gaboriault, M and Notman, A “A High Efficiency, Non Inverting, Buck Boost DC-DC Converter” Applied Power Electronics Conference and Exposition, pp. 1411-1415, 2004.

4. Oconnor, John A, “Simple Switch mode Lead-Acid Battery Charger”

5. Heinz Schmidt Walter "Switched Mode Power Supplies"

6. http://schmidt-walter.eit.h-da.de/
Stormwater Management Modelling for Ungauged Watershed in Matara Municipality

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Most urban areas are having flood problems due to human activities. It is not easy to model urban watersheds since very often they are ungauged. This paper describes the modelling of an ungauged watershed in the Matara Municipal Council Area of Southern Sri Lanka using the free SWMM5 model of the EPA. Several field visits were conducted to capture the model parameters and flood scenario for model development and calibration. The watershed delineation was done using 1:10,000 topographic maps and canal slopes etc were determined using the elevation data of these maps. This watershed with an area of 1.12 km² was modelled and calibration was done for the order of magnitude of the outputs. The model shows reasonable results with the actual conditions in the absence of gauge data. This work demonstrates that urban stormwater model SWMM5 can be used in Matara Municipal Council area to a satisfactory level with adequate field data collection. However, for accurate results, it is necessary to suitably gauge the stream flows and carry out field and engineering surveys for the measurement of physical parameters. The model demonstrated the capability to identify engineering and stormwater management options. Model outputs revealed that cleaning of canals was one option for reducing the flooding at nodes. For the considered storm, a reduction of canal roughness from 0.2 to 0.015 reduced the flood peak by 56% and no flood is happening after introducing a rectangular detention unit which is having 200m² floor area.

Keywords: Urban, Stormwater, ungauged, Mathematical modelling, flooding, SWMM5

1. Introduction

Today, an urban flood due to poor stormwater management is a major issue in most parts of the country. There are many flood prone urban areas in the island of Sri Lanka. The area of concern in this paper is the Matara Municipal Council area, which is an important urban area in southern Sri Lanka located along the coastline. The study area is bounded by the River Walgama in the north and the Madihe Mudun Ela in the south. The Colombo-Matara Road forms the eastern boundary of the study area, while the western boundary is defined by the boundary line to the watershed. The study area is shown in Figure 1.

Figure 1 - Study Area

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