Are Changes in the Mean or Variability of Climate Signals More Important for Long-Term Stochastic Growth Rate?

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Abstract

Population dynamics are affected by changes in both the mean and standard deviation of climate, e.g., changes in average temperature are likely to affect populations, but so are changes in the strength of year-to-year temperature variability. The impacts of increases in average temperature are extensively researched, while the impacts of changes in climate variability are less studied. Is the greater attention given to changes in mean environment justified? To help answer this question we developed a simple population model, explicitly linked to an environmental process. We used the model to compare the sensitivities of a population’s long-term stochastic growth rate, a measure of fitness, to changes in the mean and standard deviation of the environment. Results are interpreted in light of a comparative analysis of the relative magnitudes of change in means and standard deviations of biologically relevant climate variables in the United States. Results show that changes in the variability of the environment can be more important for many populations. Changes in mean conditions are likely to have a greater impact than changes in variability on populations far from their ideal environment, for example, populations near species range boundaries and potentially of conservation concern. Populations near range centres and close to their ideal environment are more likely to be affected by changes in variability. Among pest and insect disease vectors, as well as species of commercial value, populations likely to be of greatest economic and public health significance are those near species range centers, living in a near-ideal environment for the species. Observed changes in the variability of climate variables may benefit these populations.

Introduction

Ongoing climate change is most readily characterized by changes in the mean state of climate variables (e.g., increases in mean temperature [1]), and the impacts on ecosystems of changes in mean environmental state are studied closely [2,3]. However, rising levels of greenhouse gases may also affect climate variability [4]. An increase in variability could also affect populations’ fitness [5–9]. How do changes in the variability of climate compare to changes in the mean values of climate variables in terms of the importance of their impacts on populations? To help answer this question, here consider the simplest possible population model that can be linked to an environmental process.

Changes in mean climate have been well documented (e.g., [1]), and while changes in variability have received less attention, they have been studied at different temporal resolutions (e.g., daily [10]; monthly [11,12]; seasonal [13]; annual [4,14]), using both empirical data michaelsetal [15–17], and forecasts from a range of models [18–20]. These studies show that for some temporal resolutions, the variability of climate is changing.

Environmental variables affect annual population growth rates and vital rates such as survival probabilities and fecundity rates; it is through these rates that changes in the mean or variability of climate can affect long-term population growth rates. Determining the consequences of climatic changes on population growth therefore requires understanding the relationship between environment and annual growth and vital rates, i.e., how an environmental signal is translated into biological processes [3,21]. For ectotherms, which comprise over 99% of all species [22], temperature alters the speed at which individuals pass through life stages, thereby influencing population growth rate [23–25]. In ectotherms, the relationship between temperature and annual net population growth rate (henceforth called the response function) typically has a single peak; there is an ideal temperature that maximizes the population’s performance [21,23,26–32]. An argument for a single-peaked response function can also be made for endotherms [33] and other environmental variables such as precipitation [26]. Alternative shapes of functional responses may occasionally be reported in studies, but these can often be considered special cases of the single-peaked response function; we come back to this point in the Discussion. The specific shape of the response function for a species may determine how variability in temperature or another environmental variable affects the long-term population growth rate [34–37]. If a response function is log-convex (the log of the function opens up) for the range of an environmental variable that pertains in a locale, then an increase in variability may in fact benefit the population; if the function is...
log-concave (its log opens down) for the pertinent range of the variable, then variability is detrimental for the population [34,35].

The response function therefore plays an important role in determining the impacts of climate change on populations. There are several important studies that compare the effects of changes in mean and variability of vital rates on long-term population growth rate (e.g., [3,38–40]). However, changes in the mean environment can modify both the mean and standard deviation of vital rates and annual growth rates, as can changes in the standard deviation of the environment; understanding the relative importance of changes in means and variabilities of vital rates and annual growth rates does not necessarily translate directly to the relative importance of changes in the means and variabilities of environmental variables for long-term growth. A priori, the translation from environments to annual growth and vital rates may affect the relative importance of means and standard deviations. This possibility can be investigated by explicitly using response functions to characterize the relative sensitivities of a population to changes in the means and standard deviations of environmental variables.

In addition to examining relative sensitivities, to understand the relative importance for populations of changes in the means and standard deviations of environmental variables, it is also necessary to understand the relative magnitudes of these changes. Even if, hypothetically, a population were more sensitive to changes in the standard deviation of an environmental variable than to changes in the mean of the same variable, if the mean of the variable is changing much more rapidly than the standard deviation, changes in mean may impact the population more. Sensitivities of a population to changes in means and standard deviations of environmental variables must be multiplied by the changes taking place to assess relative importance of the two types of change.

We know of only two studies that incorporate response functions and compare the effects of changes in mean and variability of the environment, as opposed to vital rates, on a population. Van de Pol et al. [37] and Jonzén et al. [41] parameterized stage-structured stochastic population models using populations of oystercatchers in the Netherlands and red kangaroos in South Australia, respectively. Van de Pol et al. concluded that time to extinction is more sensitive to changes in the environment’s mean than its standard deviation, a result further magnified by the fact that climate models predict greater changes in mean temperature than in its standard deviation in the Netherlands. Jonzén et al. also found sensitivity of population growth to be greater changes in mean rainfall than to changes in the standard deviation of rainfall, although the two sensitivities were similar enough that changes in standard deviation would still be important unless changes in mean rainfall were much greater than changes in the standard deviation of rainfall.

In this study we aim to compare the effects of changes in mean and variability of inter-annual physical environmental conditions on long-term population growth rate, which we use as a measure of fitness, adopting a simple, strategic approach rather than parameterising a complex model of a single population as in [37,41]. Both approaches are valuable. We provide a theoretical approach based on an unstructured, annually censused population, which we assume is explicitly linked to an annual environmental variable via a response function. The model is the simplest possible stochastic matrix model, a class of model very widely used for analysis of the growth rates and extinction risks of real populations (e.g., references [42,43]). We first derive the population long-term stochastic growth rate as a function of the environment and the response function. We then derive the sensitivity of long-term growth rate to changes in environmental mean and variability. Finally, we compare sensitivities to observed changes in the means and standard deviations of several environmental variables likely to influence populations. We provide answers based on our model to the following three questions: (1) Given an increase in the mean or standard deviation of the environment, does the long-term growth rate increase or decrease? (2) If mean and standard deviation are perturbed by the same small amount, which causes the greater impact on the long-term growth rate? (3) What are the relative magnitudes of observed changes in mean and standard deviation of climate variables, and how do these relate to the sensitivities computed in (2) to yield an overall idea of whether changes in climate means or standard deviations are more important for population dynamics?

We discuss results in view of currently ongoing climate change, and identify potential consequences for populations of conservation concern as well as pests, disease vectors, and exploited populations. We indicate conceptually why results are likely to generalize from the simple model we employ to more complex models and real populations.

**Methods**

**Theory**

For $n_t$, representing the population in year $t$, the base model [44] is

$$n_{t+1} = \lambda_t n_t,$$

where $\lambda_t$ is the net growth rate of the population in year $t$. We assume $\lambda_t = f(w_t)$, where $w_t$ is the physical environmental variable and $f$ is the response function. Let $p(w_t) = \ln f(w_t)$ be the log of the response function. For the stochastic model, population size asymptotically approaches a lognormal distribution, with mean $t$ times a quantity denoted $\ln \lambda_t$ ($\mu$ in [45]); “infinitesimal mean” $\mu$ in [46]; $\ln \lambda_s$ is the long-term stochastic growth rate [42,45,48],

$$\ln \lambda_s = E(\ln \lambda_t) = \int_{-\infty}^{\infty} p(w_t) \phi(w_t|\mu,\sigma) dw_t,$$

where $\phi(w_t|\mu,\sigma)$ is the probability density function (pdf) of $w_t$, with mean parameter $\mu$ and standard deviation parameter $\sigma$ [47,48]. The integral in equation (2) is the probability of $\lambda_t$'s expected value. Second-order approximations to $\ln \lambda_s$ [45,48] are used, but equation (2) is an exact formula that applies in the case of an unstructured population. The long-term stochastic growth rate $\ln \lambda_s$ represents the rate at which almost every realization of the population grows [7,42,49] and is widely studied as a fitness parameter byoyceet.al06 and in practical application [42,43]. The sensitivities of $\ln \lambda_s$ to changes in mean and standard deviation of the environment are obtained simply by taking the partial derivatives of equation (2) with respect to $\mu$ and $\sigma$, moving the partial derivatives under the integral symbol and applying them to $\phi(w_t|\mu,\sigma).$ This approach applies generally, for any $p(w_t)$.

For concreteness, we adopt a flexible parameterization for $p$. We transform $w_t$ such that its distribution in the focal location is $\mathcal{N}(0,1)$ (see Section S1 in File S1). This step should result in no loss of generality for many environmental variables, such as mean annual temperature and rainfall. For some $z > 0, p(w_t)$ is taken to be $a_1 (w_t - b)^2 + c$ for $w_t \leq b$ and $a_2 (w_t - b)^2 + c$ for $w_t \geq b$ (Figure 1). This function is single peaked. The maximum height of the response function is controlled by $c$. The ideal environment, at which the response function is maximized, is controlled by $b$; the term “ideal environment” is henceforth used to refer simply to the
value of \( w_t \) at which \( f \) is maximized. The rate of falloff of \( p \) as \( w_t \) decreases (respectively, increases) from the ideal environment is controlled by \( a_1 \) (respectively, \( a_2 \)); both are taken to be negative. The ratio \( f_s = a_1/a_2 \) is a measure of asymmetry of the response function around \( b \); so \( a_1 \) and \( a_2 \) control the rate of falloff of the response function from the ideal environment and their relative magnitude controls symmetry. The functional form or general shape of the falloff is determined by \( z \) (Figure 1E, F); \( z \) is included as a variable (as opposed to a fixed value such as 2) for flexibility, so that response functions of a variety of shapes can be considered. The log concavity of each half of the response is controlled by \( z \), with \( z > 1 \) corresponding to log-concave response functions and \( z < 1 \) to log-convex ones; log-concavity has been important in prior work [34–37]. The response function shapes that can be generated with our parameterization (examples in Figure 1) are similar to many reported response functions [23,26,28,29]. The parameterization of \( p \) was chosen because it is very flexible, encompassing a wide range of possible relationships between the environment and vital rates, including asymmetries and different rates, functional forms, and log-curvatures for falloff of the vital rate from the optimum. The parameter \( b \) is measured in units equal to the standard deviation of the local environment because we re-scaled \( w_t \) to make it standard normally distributed. Here the term “local environment” refers to the distribution of \( w_t \). Larger values of \(| b | \) describe populations living in a suboptimal environment (for example, those living in environmental range margins or struggling to adapt to climate change), whereas \(| b | = 0 \) represents populations living in a close-to-ideal environment.

Substituting the above parameterization of \( p(w_t) \) into equation (2), we get \( \ln \lambda_s \) as a function of the parameters that define the log response function,

\[
\ln \lambda_s = a_1 \int_{-\infty}^{\infty} (-w_t + b)^s \varphi(w_t|\mu, \sigma) dw_t + a_2 \int_{b}^{\infty} (w_t - b)^s \varphi(w_t|\mu, \sigma) dw_t + c
\]

(Section S2 in File S1), where \( \varphi(w_t|\mu, \sigma) \) now represents the pdf of the normal distribution with mean \( \mu \) and standard deviation \( \sigma \). It is straightforward to compute the partial derivatives of \( \ln \lambda_s \) with respect to \( \mu \) and \( \sigma \) at \( \mu = 0 \) and \( \sigma = 1 \) (Sections S3 and S4 in File S1). These are the instantaneous rates of change of \( \ln \lambda_s \) per unit change in \( \mu \) and \( \sigma \) respectively, where the unit of change in \( \mu \) and \( \sigma \) is one standard deviation of \( w_t \). The signs of these sensitivities indicate whether a small increase in mean or standard deviation of the environment increases or decreases \( \ln \lambda_s \). Following the rationale of [37], the relative magnitudes of these sensitivities provide an estimate of whether small changes in environmental mean or standard deviation have a bigger influence on \( \ln \lambda_s \).

### Analysis of climate data.

To analyze changes in environmental variables, we downloaded Version 2 of the United States Historical Climatology Network database (USHCN [50,51]) and extracted annual time series of mean summer and winter temperatures, minimum winter temperatures, maximum summer temperatures, and total spring precipitation for locations in the conterminous United States (Section S5 in File S1). Annual time series were used because our model is more consistent with annually measured populations and environmental variables. We chose weather variables that are likely to be biologically meaningful to populations living in temperate latitudes. The USHCN data were filtered to include only time series that covered the entire 1911–2010 period. Each time series was then split into two periods (1911–1945 and 1976–2010), each of 35 years length. We calculated the mean and standard deviation of the climate variables listed above, for the two periods separately. Prior to calculating the standard deviation, each time period was detrended to remove quadratic and linear trends that could otherwise inflate the amount of variability measured. Because detrending can also remove low-frequency variability, we repeated analyses with linear detrending, and again with no detrending. To approximate normality, square-root precipitation data were used.

Although prior climatological analyses have examined changes in the means and standard deviations of climate variables (e.g., [1,4,10–17]) these studies have not sought explicitly to compare the relative magnitudes of changes in means and standard deviations for multiple biologically important variables, using the same data for both statistics to ensure comparability. A direct comparison is key for our research purposes. Hansen et al. [17] computed means and standard deviations using the same data set, but examined only season-average temperature variables, and used data which represent spatial averages computed over 250 by...
250 km or 1200 by 1200 km grid squares. Such low spatial resolution is probably less relevant to many populations than the higher resolution used here.

Results

Theoretically Predicted Sensitivities

We now provide answers to questions (1) and (2) posed in the Introduction by considering a simple special case and then by showing the general case produces substantially the same results. The special case is \( z = 2 \) and \( a_1 = a_2 = a \) (so \( f_z = 1 \)). For this special case, the log response function is symmetric (Figure 1A and B) and \( \ln \lambda_z \) and sensitivities can be calculated entirely analytically:

\[
\ln \lambda_z = a(b^2 + 1) + c;
\]

\[
\frac{\partial \ln \lambda_z}{\partial \mu} \bigg|_{\mu=0} = -2ab;
\]

\[
\frac{\partial \ln \lambda_z}{\partial \sigma} \bigg|_{\sigma=0} = 2a;
\]

(Section S6 in File S1). The signs of the sensitivities of \( \ln \lambda_z \) to changes in \( \mu \) and \( \sigma \) provide an answer to the first question posed in the Introduction: given a change in the mean or standard deviation of the environment, does the growth rate increase or decrease? The sign of the sensitivity of \( \ln \lambda_z \) to changes in \( \mu \) is the same as the sign of \( b \), since \( a < 0 \); hence any change in the mean environment toward a population’s optimum will increase \( \ln \lambda_z \), as expected. The sensitivity to changes in \( \sigma \) is always negative; hence any increase in \( \sigma \) is detrimental to the population in this special case; this is consistent with prior work relating the effects of increased environmental variation to log-concavity of the response function [34–37] because for \( z = 2 \), the response function is log-concave. Analysis of the absolute ratio of the two sensitivities, which is \( |b| \), answers our second question: if mean and standard deviation are perturbed by the same amount, which causes the greater impact on the growth rate? For \( |b| < 1 \), changes in \( \sigma \) have a greater effect, whereas for \( |b| > 1 \), changes in mean environment are more important. For fixed values of \( a \) and \( c \), larger \( \ln \lambda_z \) happens only through smaller \( |b| \) (recall \( a < 0 \)), which means the absolute ratio of the two sensitivities is smaller; so larger long-term growth rates mean greater relative sensitivity of the growth rate to changes in environmental variability.

Log response functions may often be asymmetric and \( z \) may differ from 2, so how contingent are the above results on the assumptions made by the special case? We numerically analyzed the sensitivities of \( \ln \lambda_z \) for a range of values of \( f_z \) and for \( z = 1, 2, 1/2, 2, 1 \) and 2 and results remain largely the same in substance. Figure 2A–C shows that \( \partial \ln \lambda_z / \partial \mu \) plotted against \( b \) changes sign from negative to positive at a value of \( b \) close to 0, with some small variation in the value of \( b \) at which the sign changes, depending on the values of \( f_z \) and \( z \). Figure 2D–F illustrates that for \( z \geq 1 \), \( \partial \ln \lambda_z / \partial \sigma \) is always negative. For \( z < 1 \), this sensitivity can be positive for larger values of \( |b| \). Since \( z < 1 \) means parts of the log-response function, \( p \), are convex, and earlier work shows that convexity of the log-response function is associated with the possibility that increased environmental variance can benefit populations [34–37], the result from our model that \( \partial \ln \lambda_z / \partial \sigma \) can be positive for \( z < 1 \) is consistent with earlier work. Figure 3 compares the absolute magnitudes of the sensitivities. For \( b \) close to 0, the sensitivity of \( \ln \lambda_z \) to changes in \( \sigma \) is generally comparable or larger in magnitude than the sensitivity to changes in \( \mu \). The specific interval of \( b \) in which the sensitivity of \( \ln \lambda_z \) to changes in \( \sigma \) is larger varies depending on \( f_z \) and \( z \). But regardless of this variation the conclusion holds that for small \( |b| (|b| < 2 \) for the model parameters we examined), changes in environmental standard deviation are expected to be comparably or more important for long-term stochastic growth rate than changes of the same magnitude in the mean environment. This conclusion holds regardless of the concavity of \( p \), controlled by \( z \). This suggests that the overwhelming emphasis of past research on the impacts on populations of changes in means of environmental states is misplaced and more attention should be paid to impacts of changes in environmental variability. Generality of the results to different distributions of \( w_i \) and different parameterizations of \( p \) is explored in Section S7 in File S1. Figure 3D–F shows that for given \( c \) and \( a \), larger values of \( \ln \lambda_z \) are within the range for which \( \partial \ln \lambda_z / \partial \sigma \geq \partial \ln \lambda_z / \partial \mu \), i.e., across a species environmental range, populations with comparatively higher growth rates are likely to be more affected by changes in variability of the environment than changes in mean.
Results of Climate Data Analysis

The third question posed in the Introduction was: what are the relative magnitudes of observed changes in mean and standard deviation of climate variables? Results are shown for mean winter temperature and total spring precipitation in Figure 4, and for mean summer temperature, minimum winter temperature, and maximum summer temperature in Figure S1 in Section S8 in File S1. The magnitudes of changes in the means of all variables, except total spring precipitation, were generally slightly but not markedly larger than those of standard deviations. For total spring precipitation, changes in mean and standard deviation were of almost the same magnitude. Results are also spatially heterogeneous. The only variable for which changes in standard deviation are of the same sign throughout most of the United States is minimum winter temperature (Figure S1E in Section S8 in File S1), where variability decreased from 1911–1945 to 1976–2010. For all other variables, the sign and magnitude of changes depend on location. Changes in mean were generally slightly but not markedly bigger in magnitude than changes in standard deviation at local scales too (Figure 4E–F), although there are many locations and weather variables where the reverse is true (e.g., for summer mean temperature and precipitation). Although changes in means were more often larger than changes in standard deviation, both types of changes were similar in size, so results comparing relative sensitivities of long-term stochastic growth rate can also be interpreted as approximately reflecting the relative importance of the two types of environmental change for population dynamics. Results were very similar when linear detrending or no detrending were used in place of quadratic detrending.

Discussion

We showed for a simple model how the effects on population dynamics of changes in the mean and variability of an environmental variable compare. Our results indicate that for small $|b|$, changes in the standard deviation of the environment are at least comparably important to changes in the mean environment. In other words, whenever the distribution of values of the local environment deviates from the value of the environmental variable at which the response function peaks. We discuss the contrasting implications of these results for two different kinds of populations: those living close to or far from their ideal environment.
exploited species (e.g., copepods), are also of greatest interest, for economic reasons, in locations close to the species’ ideal environments. For these populations, our results show that any increase in variability of the environment is detrimental, and that furthermore, changes in variability are more important than changes in mean. Given that the variability of temperature has decreased in many locations of the United States over the past 100 years, our model suggests that pests and disease vectors, but also potentially some exploited species, may stand to benefit from ongoing climate change in areas where the environment is already ideal for the species and they are already most prevalent.

Climate change has led to shifts and contractions in species’ range sizes [2,54] compounded by habitat loss and fragmentation [55]. Populations struggling to adapt to rapid climate changes will often be those living on the trailing edge of changing species ranges, where environmental conditions are suboptimal. Such populations may be of conservation interest; they are interpreted in our model as having large $|b|$. For these populations, environmental variability can be beneficial if the log response function is described by $\gamma < 1$, i.e., if it is convex. Our results also show that for these populations, changes in mean environmental conditions have a greater effect than changes in variability.

Comparisons with other Studies

Prior studies, mentioned in the Introduction, have compared the impacts of changes in mean and variability of vital rates on $\ln \lambda_s$, generally finding that populations are more sensitive to changes in vital rate means than they are to changes in vital rate standard deviations. Our study complements these earlier studies by using a response function to compare the impact of changes in mean and variability of the environment on $\ln \lambda_s$. Our finding that changes in environmental variability can be more important than changes in environmental mean stands in counterpoint to the earlier results, and emphasizes the non-equivalence of studying the effects of changes in environmental and vital rate distributions. Morris et al. morrietal08 concluded that although all species they examined were more sensitive to changes in vital rate means than variances, the greater importance of changes in means was reduced for shorter-lived, faster growing species. Our result that faster-growing populations, i.e., those close to their ideal environment, are more susceptible to changes in environmental variance appears to parallel the result of Morris et al., but for environments instead of vital rates.

Only two empirical studies currently exist that can be directly compared to our theoretical predictions, and they provide support for our conclusions, though with caveats. Van de Pol et al. [37] and Jonzén et al. [41] used structured population models, parameterized for a population of oystercatchers [37] and a population of red kangaroos [41]. The oystercatcher population has been declining at a rate of $\sim 5\%$ per year vandepeoetal10; it therefore may be living in less than ideal conditions. Van de Pol et al. conclude, as our model would suggest, that changes in mean environmental conditions will have a greater effect on this population than do changes in variability. The red kangaroo population of [41] probably lives in a closer-to-ideal environment for the species, as it has a substantially positive $\ln \lambda_s$: Jonzén et al. estimate that growth rate will be greater than 1 even with annual harvesting of up to 20%. Consistent with our model, the sensitivity of $\ln \lambda_s$ to changes in mean rainfall (after converting the elasticities provided in [41] to sensitivities) is only $\sim 2.4$ times greater in magnitude than that to changes in the standard deviation of rainfall: sensitivity to changes in standard deviation is important for the kangaroo population. These comparisons are subject to the caveats that: 1) other hypotheses besides a sub-optimal environment have been proposed as possible causes of the decline of the oystercatcher population [56]; 2) only these two studies are currently available for comparison. More insight can be gained in future work by replicating the efforts of [37] and [41] for other

![Figure 4. Relative changes in mean and standard deviation of climate variables in the United States.](image-url)
populations. This is a non-trivial effort. Many years worth of data are necessary for each population (e.g., 25 years of data were used in [37]). Each monitored population would correspond to a single point in parameter space of a general theoretical analysis. A principle value of our modeling is in guiding future empirical work. Our findings help inform what populations may be of interest to compare. We suggest the comparison of populations thought to be living in close-to-ideal conditions with those far from ideal conditions. For example, one could replicate the study of van de Pol et al. with other oystercatcher populations across a gradient of environmental conditions, including expanding populations.

The distinction between log-concave and log-convex response functions has been emphasized in prior work as important for whether increased environmental variance will increase or decrease population long-term stochastic growth rate [34–37]; for log-concave (respectively, log-convex) response functions, it is easy to see that geometric-mean vital rate values are lower (respectively, higher) under increased environmental variance. However, if the mean local environment maximizes or nearly maximizes a response function, then the response function is effectively log-concave for relevant environments: increased environmental variance can only decrease geometric-mean vital rate values, because increased variance includes more environments that are farther from the environment that optimizes the vital rate. Thus, distance of the mean local environment from the population ideal environment (with distance measured in units of the standard deviation of the local environment) supersedes the question of log-convexity. The log-concavity distinction still makes a difference far from the ideal environment (compare figures 2D–F).

Biological Realism and Possible Future Work

Our model is simple, but main conclusions are intuitively sensible and seem likely to generalize to other models. Because the relationship between log annual population growth rate and environment peaks in our model at the optimum environment, geometric-mean growth rate will not be strongly sensitive to changes in environmental mean when environmental mean is close to optimal. For instance, when \( z > 1 \), the slope of the log-response function close to the ideal environment is close to zero, so small changes in mean environment from the optimum have little effect on geometric-mean annual growth rate. On the other hand, because rates decline with departures from the optimal environment in either direction of the optimum, changes in environmental variance may strongly affect geometric-mean annual growth when the mean environment is optimal, because larger environmental variances include more values of the environment that are far from the optimum. This simple conceptual reasoning is made precise by our modeling results. Similar reasoning holds for any model for which all vital rates can be written approximately as functions of a single environmental variable. For any fixed value of environmental variance, \( \ln \lambda_s \) must have a maximum at some value of the environmental mean. Sensitivity of \( \ln \lambda_s \) to changes in the mean environment must approach zero here, as long as \( \ln \lambda_s \) is a smooth function of environmental mean. For fixed environmental variance, the ideal mean environment is the one that maximizes \( \ln \lambda_s \). As long as the local environment is close to this ideal environment, one therefore expects sensitivity of \( \ln \lambda_s \) to changes in the mean environment to be very small, and hence it is likely that sensitivity will be greater to changes in the standard deviation of the environment. This reasoning applies to stage structured models, and to density-dependent models if \( \ln \lambda_s \) is replaced with some other measure of population success (e.g., average population size). The potential importance of these observations for real populations seems largely overlooked by prior work, which generally compares the importance of changes in the means and variances of vital rates. For populations strongly affected by two or more environmental variables, potentially acting on different vital rates, there may be no single ideal environment. Instead, tradeoffs may occur, whereby various mean values for one environmental variable can be paired with different mean values of the other variable to maximize \( \ln \lambda_s \). This may be an important topic for future study.

Many species show a "storage effect," a well-studied phenomenon by which some life stages are less susceptible to adverse environments than other life stages; storage effects are a classic mechanism of species coexistence [37–39]. Our model cannot incorporate storage effects because it is unstructured, so investigating how storage effects impact the main conclusions of this study may be another important topic for future research. Species exhibiting storage effects include long-lived species with resistant adult stages (e.g., trees), as well as species with spores or seed banks (e.g., fungi and annual grasses; [60]). Our model corresponds instead to another large category of species with no storage stage, e.g., insects and other organisms that overwinter as eggs which are not viable beyond the following spring. Although eggs may be insensitive to the winter environment, this is not a storage stage as long as eggs cannot remain viable beyond spring. The insensitivity of storage phases to bad environments may make it appear as though species with storage phases must be more sensitive to changes in environmental means than to changes in environmental variation. However, storage phases are only insensitive to environmental variation in the sense that they can tolerate bad conditions. From another perspective, storage phases are very sensitive to environmental variation because they respond strongly to good environments. For instance, spores or seeds in a seed bank emerge when conditions are suitable. Also, adult stages may reproduce prolifically under good conditions. This alternative form of sensitivity to the environment may translate into sensitivity of population long-term stochastic growth rates to changes in environmental variability. Both modified standard deviation of environment and changes in the mean of the environment can decrease the fraction of years for which environmental conditions are acceptable for seeds or other storage phases to become active. If all vital rates are affected primarily by the same environmental variable, then the logic of the prior paragraph still applies, even if there are storage effects, suggesting the main conclusions of this study may still hold in many cases even with storage effects.

Stage structure must be introduced into the model to analyze storage effects or to illuminate possible consequences of multiple environmental variables acting on different vital rates. For a general stage-structured model, \( n \) vital rates or stochastic matrix elements would be linked to \( n \) potentially different environmental variables \( w_{ij} (i = 1, \ldots, n) \) by different response functions, each with its own \( a_i, a_{ij}, a_{i2}, b_i, \) and \( c_i \), resulting in \( n \) sensitivities of \( \ln \lambda_s \) to changes in \( \mu_i \) and \( \sigma_i \). The \( w_i \) may also be correlated and this correlation structure may be affected in unknown ways by climate change. The mathematical complexity here may be difficult to manage in the general case. Not all parameter combinations are equally likely, though. For instance, slow-growing populations such as oystercatchers have high adult survival rates probably described by a concave function, and have low fecundity rates likely described by a convex function [37]. A similar pattern is observed in many organisms (e.g., fish [61]; perennial and annual plants [62,63]). Whether these biological regularities can be formalized and used to simplify the mathematics remains to be seen. If a general model proves too complicated to immediately provide insight, a sensible next step may be a \( 2 \times 2 \) matrix model of a population with juveniles and adults (non-
semelparous, as semelparous populations are covered by our model; Section S9 in File S1). Such a model would make it possible to study the differing impacts of climate change on fecundity and survival rates, as well as effects that may only emerge when some stage structure is present. For an age or stage structured model, the exact formulation of \( \ln L_x \) used in this study would no longer be valid, but Tuljapurkar’s \([45,48]\) approximation could be used. For the unstructured case, the approximation yields qualitatively similar results to the ones presented here (results not shown). An alternative approach would be possible if sufficiently many case studies were available for which population models were empirically established, with vital rates explicitly linked to environmental variables. Given such a model, it is straightforward to evaluate the relative sensitivities of \( \ln L_x \) to changes in the mean and standard deviation of the environmental variable, as done in references \([37]\) and \([41]\), but a substantial number of case studies would be needed to draw general conclusions.

The long-term stochastic growth rate for a stage-structured model is also affected by autocorrelation in the environment \([42,45,48]\). The autocorrelation of environmental variables is also changing due to climate change \([64]\). It would be possible, using a stage-structured model, to compare the relative effects of changes in mean, variance, and autocorrelation of the environment on population dynamics (as done for a single oystercatcher population in \([65]\)). Finally, the sensitivities of \( \ln L_x \) are linear approximations of the functions that relate \( \ln L_x \) to \( \mu \) and \( \sigma \), and therefore assume small changes in the environment. More substantial environmental changes may entail nonlinearities for which a linear approximation is no longer sufficient. An examination of such nonlinear effects may be analytically intractable, though simulations and numeric work may provide insights.

We considered annual environmental variables because most demographic data and models of the type we consider have an annual time step. But annual environmental variables, such as spring mean temperature, are averages of shorter-time-scale events (e.g., spring mean temperature may be calculated as the mean of daily temperatures during spring). We do not here consider standard deviation of, for instance, daily temperatures measured in the spring, nor do we consider the effects of changes in such a standard deviation. Other studies do consider these shorter time-scales \([66]\) instead of considering inter-annual standard deviations, as we do. A comparison of the importance of changes in inter- and intra-annual standard deviation may be an interesting topic of future research.

Common sense and appropriate empirical evidence support the assumption of a peaked, skewed response function, but we admit the possibility that other response functions could occur in some circumstances; our analytic approach could easily be adapted to essentially any response function. Focal-population studies, such as \([67]\), in which vital rates of a single population are related to values of an environmental variable experienced by that population, need not necessarily show a peak in the response function, even when one exists. A population would need to live close to its ideal environment for the peak in the response function to be apparent in locally gathered data, and even in that case, unless the local environmental variability was large, the response function may appear to be flat to within the accuracy of measurement of vital rates or annual growth rates. Local environmental variables do not usually span much of the range of environmental values the species could potentially experience across its geographic range, hence peaks will often not be visible in such studies. This does not, however, preclude the presence of a peak in the whole response function, but instead indicates that many studies look at narrow environmental ranges \([29]\). Different kinds of studies in which response functions are measured across a wider range of values of the environmental variable are more appropriate for assessing the shape of a response function. Empirical evidence of peaked response functions in both ectotherms and endotherms can be found in \([27–29,31,32]\), and theoretical support is provided by \([30]\) (some results of these studies are summarized in Section S7).

Apparently saturating response functions are usually more likely to be unimodal response functions, with a peak that is remote from the range measured in a locally focussed study. Threshold response functions may also be possible, for instance if populations respond differently below and above the freezing point of water. However, these seem more likely to be important at shorter time-scales (e.g., daily or hourly) than the annual time-scales considered here. The annualized environmental variables we use are more likely to be statistically related to annually measured vital rates, and will not usually have discontinuous thresholds. Nevertheless, our analytic approach can easily be applied to any alternative response function if a particular shape not encompassed by the parameterization we have used is found to be common enough to warrant study (Section S7).

Supporting Information

File S1 Supporting information. (PDF)

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Author Contributions

Analyzed the data: BGC DCR. Contributed reagents/materials/analysis tools: BGC DCR. Wrote the paper: BGC DCR.

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