Environmental effects on electron spin relaxation in N@C\textsubscript{60}

John J. L. Morton,\textsuperscript{1,2} Alexei M. Tyryshkin,\textsuperscript{3} Arzhang Ardavan,\textsuperscript{1,2} Kyriakos Porfyراكis,\textsuperscript{1} S. A. Lyon,\textsuperscript{3} and G. Andrew D. Briggs\textsuperscript{1}

\textsuperscript{1}Department of Materials, Oxford University, Oxford OX1 3PH, United Kingdom
\textsuperscript{2}Clarendon Laboratory, Department of Physics, Oxford University, Oxford OX1 3PU, United Kingdom
\textsuperscript{3}Department of Electrical Engineering, Princeton University, Princeton, NJ 08544, USA

(Dated: July 16, 2018)

We examine environmental effects of surrounding nuclear spins on the electron spin relaxation of the N@C\textsubscript{60} molecule (which consists of a nitrogen atom at the centre of a fullerene cage). Using dilute solutions of N@C\textsubscript{60} in regular and deuterated toluene, we observe and model the effect of translational diffusion of nuclear spins of the solvent molecules on the N@C\textsubscript{60} electron spin relaxation times. We also study spin relaxation in frozen solutions of N@C\textsubscript{60} in CS\textsubscript{2}, to which small quantities of a glassing agent, S\textsubscript{2}Cl\textsubscript{2} are added. At low temperatures, spin relaxation is caused by spectral diffusion of surrounding nuclear spins \textsuperscript{35,37}Cl in the S\textsubscript{2}Cl\textsubscript{2}, but nevertheless, at 20 K, T\textsubscript{2} times as long as 0.23 ms are observed.

PACS numbers: 76.30.-v, 81.05.Tp

\section{I. INTRODUCTION}

The N@C\textsubscript{60} molecule is well known for its remarkably well-shielded electron spin \textsuperscript{1}, prompting several proposals for fullerene-based quantum information processing (QIP) \textsuperscript{2,3}. Indeed, extraordinarily long electron spin relaxation times, satisfying the strict requirements for QIP \textsuperscript{2}, have been reported for N@C\textsubscript{60} in liquid solutions \textsuperscript{4,5} and in solid matrices \textsuperscript{2}, thus demonstrating the remarkable capability of the fullerene cage for protecting the enclosed spin from fluctuating perturbations in various host environments. This property opens the possibility of using almost any host material when “designing” N@C\textsubscript{60}-based QIP processors. For example, in proposed architectures include N@C\textsubscript{60} arrays positioned at interfaces (e.g. arranged on solid templates) where they would be expected to be exposed to a broad spectrum of environmental perturbations.

Two important spin relaxation mechanisms have recently been identified for N@C\textsubscript{60} in liquid solutions \textsuperscript{1,2}, both involving internal motion of the fullerene cage (e.g. vibrational or rotational motion). These two mechanisms explain a large body of the experimental data. An Orbach mechanism via a vibrational mode of C\textsubscript{60} cage was shown to determine the spin relaxation of N@C\textsubscript{60} in a CS\textsubscript{2} solvent environment over a broad range of temperatures \textsuperscript{5}. Nevertheless, this Orbach mechanism remains weak resulting in very long relaxation times (T\textsubscript{1}=0.5 ms and T\textsubscript{2}=0.24 ms at 160 K, just above the melting point of CS\textsubscript{2}). Even longer relaxation times might be expected at lower temperatures; however, the CS\textsubscript{2} solvent is not suitable for frozen solution studies since it freezes as a polycrystal with consequent grain boundary segregation of the dissolved fullerene molecules.

A second relaxation mechanism was found for asymmetric N@C\textsubscript{70} fullerenes, which possess a permanent zero field splitting (ZFS) \textsuperscript{6}. Random rotational reorientation of this ZFS contributes significantly to N@C\textsubscript{70} spin relaxation at temperatures lower than 260 K, a temperature range in which rotational mobility is insufficient to achieve efficient motional averaging of the non-zero ZFS.

Relaxation of N@C\textsubscript{60} (and N@C\textsubscript{70}) in solid matrices has not been comprehensively studied yet. Very long T\textsubscript{1}\approx 1 s have been reported in low-purity N@C\textsubscript{60}/CS\textsubscript{2} powders at 4 K, while considerably shorter T\textsubscript{2}= 20\mu s were found \textsuperscript{2}. The mechanism behind such an unexpectedly short T\textsubscript{2} remains unexplained.

In this paper, we extend the studies of electron spin relaxation of N@C\textsubscript{60} and examine the role of nuclear spins in the solvent environment, both in liquids and in frozen solutions. The CS\textsubscript{2} solvent used in our previous studies had no naturally abundant nuclear spins (i.e. only 1.1\% of \textsuperscript{13}C with nuclear spin I=1/2, and 0.76\% of \textsuperscript{33}S with I=3/2). In this work we use a toluene solvent and a CS\textsubscript{2}/S\textsubscript{2}Cl\textsubscript{2} mixture; both contain substantial numbers of magnetic nuclei. We show how the presence of a high concentration of nuclear spins from solvent molecules can significantly shorten the relaxation time of N@C\textsubscript{60}. Depending on the temperature regime, i.e. liquid or frozen solutions, translational \textsuperscript{7,8} or spectral \textsuperscript{4,7,8,9,10} diffusion of nuclear spins surrounding the N@C\textsubscript{60} molecule contributes to electron spin relaxation.

\section{II. MATERIALS AND METHODS}

The aggregation (or clustering) of C\textsubscript{60} in certain solvents and concentrations has been widely reported \textsuperscript{11,12,13,14,15,16,17}. Furthermore, the solubilities of C\textsubscript{60} in toluene and in CS\textsubscript{2} show a strong temperature dependence, peaking at 280 K and falling rapidly upon further cooling \textsuperscript{18}. The result is that the convenient picture of isolated fullerenes in solution is rather naive; instead the behaviour is a complex, non-monotonic

\footnote{Electronic address: john.morton@materials.ox.ac.uk}
function of temperature, fullerene concentration, choice of solvent, and even time from initial dissolution. For example, in CS$_2$ at room temperature the onset of aggregation has been measured to be at a concentration of around 0.06 mg/ml [11]. At concentrations above 0.36 mg/ml, the clusters themselves further agglomerate to form ‘flowerlike’ structures with an open hole in the centre. In toluene, clusters ranging from 3 to 55 fullerences have been observed over a dilute range of concentrations (0.18 to 0.78 mg/ml) [17]. This clustering can have important consequences on electron spin relaxation rates resulting in a distribution of the relaxation times depending on the location of N@C$_{60}$ within the cluster. An additional complication can arise in samples of higher N@C$_{60}$/C$_{60}$ purity — if the large C$_{60}$ cluster contains two N@C$_{60}$ molecules their relaxation will be strongly affected by the dipole-dipole interaction between the two N@C$_{60}$ electron spins. For example, in a sample of 3% N@C$_{60}$/C$_{60}$ purity, we have observed a decrease in $T_2$ with increasing fullerene concentration above about 0.1 mg/ml.

To eliminate uncertainties associated with C$_{60}$ cluster formation, dilute solutions with concentrations of less than 0.06 mg/ml were used in this study. High-purity (≈ 80%) endohedral N@C$_{60}$ was used to prepare samples in toluene, enabling the use of dilute solutions (2 µg/ml) of well-isolated fullerences which nevertheless provide sufficient signal for pulsed EPR experiments. Solutions were degassed by freeze-pumping in three cycles to remove paramagnetic O$_2$. We observe that while samples of N@C$_{60}$ in CS$_2$ are stable, the EPR signal from the sample in degassed toluene decayed when exposed to light. The precise nature of this decay is unknown and possibly occurs via the photo-excited triplet state of the C$_{60}$ cage leading to escape of the nitrogen from the cage. Other experimental parameters, including a brief description of the N@C$_{60}$ spin system are provided elsewhere [5]. $T_2$ and $T_1$ times were obtained using Hahn echo and inversion recovery sequences, respectively [19].

Given the strong reactivity of S$_2$Cl$_2$, there was some concern that it might attack the fullerences in the solution — this dictated the sample preparation procedure adopted. 50 µl samples of N@C$_{60}$ (4% purity) in CS$_2$, and pure S$_2$Cl$_2$ were degassed in two separate arms of a λ-shaped quartz vessel. The solvents were then mixed and quickly frozen; the resulting mixture contained approximately 25% S$_2$Cl$_2$ by volume (corresponding to 20 mol%).

### III. SPIN RELAXATION OF N@C$_{60}$ IN TOLUENE SOLUTION

When N@C$_{60}$ is dissolved in a solution containing nuclear spins (such as the hydrogen atoms of toluene), additional relaxation pathways may be introduced. These arise from fluctuating fields caused by the motion of solvent molecules around the fullerene cage. The use of both regular (hydrogenated) and deuterated toluene as solvents can provide further insights into the effect of local nuclear spins. Figures 1 and 2 show the $T_1$ and $T_2$ times measured for high-purity N@C$_{60}$ in toluene solution, as a function of temperature.

The temperature dependence of $T_1$ in toluene is suggestive of an Orbach relaxation mechanism, similar to that reported for N@C$_{60}$ in CS$_2$ [5]. However, the slopes of the temperature dependence are markedly different in the two solvents. In CS$_2$ the energy splitting derived from the slope matched well the first excited H$_g$(1) vibrational mode of C$_{60}$ at 33 meV, and in toluene the slope corresponds to an energy splitting of 60(2) meV which coincides with the second major line seen in the Raman spectra (62 meV), corresponding to the $A_g(1)$ mode (Figure 1B). Solvent effects have been reported extensively in the Raman spectroscopy of C$_{60}$ [20], and it is concluded that the nature of the solvent-fullerene interaction can distort the icosahedral symmetry leading to splittings of the $H_g$ Raman transitions [21]. Consistently, the results here could also be attributed to interactions between the cage and the solvent (e.g. a π-stacking arrangement in the case of the aromatic toluene molecule); the transitions involving the $H_g(1)$ mode may be suppressed, and electron spin relaxation of the endohedral nitrogen takes places more effectively via the higher-energy $A_g(1)$ squeezing mode.

The $T_2$ relaxation data in Figure 2 reveal a non-

![FIG. 1: (A) Spin relaxation time $T_1$ for N@C$_{60}$ in toluene as a function of temperature, plotted as log (1/$T_1$) against (1/T), where $T_1$ is given in microseconds. $T_1$ times are indistinguishable for regular toluene (red triangles) and deuterated toluene (green circles). The linear fit (dashed line) is consistent with an Orbach relaxation mechanism, and the slope of the fit gives an energy splitting $\Delta = 60(2)$ meV of the excited state involved in the relaxation process. Similar linear dependence has been reported for N@C$_{60}$ in CS$_2$ [5], but the linear fit (shown in blue, for comparison) gave a different $\Delta = 33$ meV. (B) Two major absorption peaks in the Raman spectrum of C$_{60}$ lie at 273 and 497 cm$^{-1}$ (33 and 62 meV, respectively).](image-url)
monotonic temperature dependence in contrast to that observed for N@C_{60} in CS_{2}. In CS_{2}, a simple ratio of T\_2 = 2/3 \_T\_1 was found over this broad temperature range indicating that both T\_1 and T\_2 times are determined by the same Orbach relaxation mechanism. In toluene, T\_2 diverges noticeably from the T\_1 dependence indicating that an additional relaxation mechanism must be involved which suppresses T\_2 at low temperatures. In the following discussion we argue that this additional relaxation mechanism is due to nuclear spins (protons) of the toluene solvent.

In liquid solutions, solvent molecules can diffuse around N@C_{60} and therefore the distance between the electron spin of N@C_{60} and the nuclear spins of toluene molecules changes in time. This results in fluctuating hyperfine (contact and dipolar) fields seen by the electron spin which can drive its relaxation. In the hard-sphere approximation, the spin-spin separation varies between a value called the *distance of closest approach* (d), and infinity. The translation diffusion time, \( \tau_D \), becomes the important correlation time \( \tau_D \).

\[
\tau_D = \frac{2\pi^2}{D(T)},
\]

where \( D(T) = D_{C_{60}}(T) + D_{tol}(T) \) is the sum of the temperature-dependent diffusion coefficients of the fullerene and toluene molecules. According to common models for diffusion-induced spin relaxation \cite{22, 23, 24}, the resulting T\_1 and T\_2 times are \( T\_1^{-1} = 2\kappa \frac{c(T)}{d \cdot D(T)} 10J(\omega_e) \)

\[
(T\_1)^{-1} = 2\kappa \frac{c(T)}{d \cdot D(T)} 10J(\omega_e),
\]

\[
(T\_2)^{-1} = \kappa \frac{c(T)}{d \cdot D(T)} [4J(0) + 10J(\omega_e) + 6J(\omega_n)].
\]

\( \omega_e \) and \( \omega_n \) are the electron and nuclear Zeeman frequencies, respectively. The constant prefactor, \( \kappa \), is given by

\[
\kappa = \frac{16\pi}{405} \gamma_e^2 \gamma_n^2 h^2 I(I + 1).
\]

\( \gamma_e \) and \( \gamma_n \) are the electron and nuclear gyromagnetic ratios, \( c(T) \) is the temperature-dependent concentration of hydrogen (or deuterium) spins, and the spectral density function \( J(\omega) \) is given by

\[
J(\omega) = \frac{1 + 5\omega^2/8 + \omega^2/8}{1 + \omega^2 + \omega^2/6 + 4\omega^2/81 + \omega^2/81 + \omega^2/648},
\]

with \( \omega = \sqrt{2\omega_0 D} \).

The only unknown quantities in the above expressions are nuclear spin concentration \( c(T) \), distance of closest approach \( d \), and the diffusion coefficient \( D(T) \). The temperature dependence of \( ^1H \) concentration in toluene is given in Perry’s Chemical Engineer’s Handbook (7th Ed) as

\[
c(T) = (4.089 \cdot 10^{21}) \left( 0.26655^{-(1+(1-\frac{T}{150})^{0.2875})} \right),
\]

and varies between about 4.5 - 5 \cdot 10^{22} \text{ cm}^{-3} over the temperature range 150 - 300K. Evidently, the variation in this parameter is not great and therefore could not explain the temperature dependence of T\_2. It must be \( D(T) \) and its strong temperature dependence that dominates the effect on T\_2.

The self-diffusion coefficient \( D(T) \) of toluene has been studied as a function of temperature \cite{24}. In the temperature range 135 to 330K, the data fit well to

\[
D_{tol}(T) = 6.1 \cdot 10^{-4} \exp \left( \frac{-1000}{T} \right) \exp \left( \frac{-190}{T} \right)^6
\]

The diffusion coefficient for C\_{60} can be roughly estimated by the Stokes-Einstein equation:

\[
D_{C_{60}}(T) = \frac{k_B T}{6\pi\eta a(T)},
\]

where \( a = 0.35 \text{ nm} \) is the radius of the N@C\_{60} molecule, and \( \eta(T) \) is the solvent viscosity which can also be temperature dependent. However, reports on toluene viscosity only go down to 225K \cite{23}, below which one would expect substantial changes in behaviour. As a result, both \( D_{C_{60}}(T) \) and \( d \) were left as fitting parameters.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig2.png}
\caption{Spin decoherence time T\_2 of N@C\_{60} in toluene, measured using the central M\_1 = 0 line, with regular toluene (red squares) and deuterated toluene (green squares). The solid curves are generated using the model that involves two relaxation mechanisms, and the dashed curves show individual contributions of the two mechanisms. The blue dashed curve is the ‘intrinsic’ decoherence time due to the Orbach relaxation process; T\_2 = (2/3)T\_1 is assumed based on the study of N@C\_{60} in CS\_2 \cite{5}. The red and green dashed curves show the relaxation effect due to translational diffusion of proton and deuterium nuclei of toluene molecules.
}
\end{figure}
To fit the experimental data in Figure 2 we assume two relaxation processes: the translational diffusion mechanism described above and the Orbach relaxation mechanism which if alone would produce $T_2 = (2/3) T_1$, as was found for N@C$_{60}$ in CS$_2$ solution [5]. The individual contribution of each of the two relaxation mechanisms and their overall effect are shown in Figure 2. The best fit was achieved using a diffusion coefficient whose temperature dependence is shown in Figure 3, and $d = 0.35$ nm (though it was possible to obtain reasonable fits for $d$ up to about 0.45 nm). The radius of the C$_{60}$ molecule is 0.35 nm, so these values for distance of closest approach are reasonable. The best-fit diffusion coefficient of C$_{60}$ converges with that predicted by the Stokes-Einstein equation (Eq. 8) for temperatures below 250K, however it deviates by as much as a factor of 10 at higher temperatures (310K).

Finally, evaluating Eq. 2 with the parameters extracted from the study of $T_2$, we confirm that the $T_1$ times for h-toluene and d-toluene are expected to be equal, as the translational diffusion $T_1$ rates are much slower than the intrinsic (Orbach) decay mechanism (see Figure 4).

**IV. SPIN RELAXATION OF N@C$_{60}$ IN A FROZEN SOLUTION**

A glass-forming solvent is essential for frozen solution studies of N@C$_{60}$, in order to ensure homogeneity of the frozen solution and to avoid clustering of N@C$_{60}$. The ideal solvent would also contain a minimal concentration of nuclear spins since it is known that nuclear spins of the solvent molecules can provide a significant mechanism for electron spin decoherence, e.g. via the process known as spectral diffusion caused by flip-flops of the local nuclear spins [7, 8, 9]. While such an ideal solvent has not come to our attention, it is possible to add relatively small quantities of sulphur chloride (S$_2$Cl$_2$) to CS$_2$ to act as a glassing agent [27]. The addition of 15 mol% S$_2$Cl$_2$ in CS$_2$ is sufficient to permit vitrification of small samples. CS$_2$ has no major isotopes with non-zero nuclear spins, however, S$_2$Cl$_2$ has chlorine whose major isotopes both have nuclear spin $I = 3/2$ and gyromagnetic ratios of about 4 MHz/T. Therefore, while this mixture is not an optimal solution, it was hoped that the reduced nuclear spin concentration in the mixture solution would permit relatively long decoherence times, not limited by the nuclear spectral diffusion.

The measured $T_1$ and $T_2$ times are shown in Figures 5 and 6 in the temperature range 20 to 165K (below the melting point of the mixture). $T_1$, which was mea-
FIG. 6: Temperature dependence of $T_2$ for N@C$_{60}$ in a frozen solution of CS$_2$ : S$_2$Cl$_2$ (volume 3:1), measured on the central ($M_I = 0$) and high-field ($M_I = -1$) hyperfine lines of the N@C$_{60}$ EPR spectrum. For $M_I = -1$, two $T_2$ times, $T_{2,o}$ and $T_{2,i}$, are extracted for outer ($M_S = \pm 3/2 : \pm 1/2$) and inner ($M_S = +1/2 : -1/2$) transitions within the S=3/2 multiplet, using their different ESEEM frequencies \cite{5}. The curves are visual guides.

sured on the central $M_I = 0$ hyperfine line, has a monotonic temperature dependence and follows closely that seen in a dilute powder of N@C$_{60}$/C$_{60}$. It seems that the residual concentration of nuclear spins in S$_2$Cl$_2$/CS$_2$ mixture has no effect on $T_1$ in the temperature range studied. However, both solid samples show $T_1$ values which are less than that expected by extrapolating the Orbach mechanism suggested for N@C$_{60}$ in CS$_2$ solution. Apparently, other (yet unidentified) relaxation mechanisms contribute significantly in both solid matrices at low temperatures, resulting in $T_1$ shorter than would be expected from the Orbach mechanism alone. Relaxation experiments at different microwave frequencies will be required to shed light on these unidentified mechanisms.

On the other hand, $T_2$, when measured on the $M_I = 0$ line, shows a minimum at around 100 K, coinciding with the approximate glass transition temperature, $T_g$, of the solvent mixture \cite{27}. For measurements on the $M_I = -1$ high-field hyperfine line, two different $T_2$ times corresponding to the outer ($M_S = \pm 3/2 : \pm 1/2$) and inner ($M_S = +1/2 : -1/2$) transitions can be separated using the ESEEM method described elsewhere \cite{5}. $T_{2,o}$ (outer) falls dramatically upon cooling towards $T_g$, while $T_{2,i}$ (inner) reaches a minimum at $T_g$, but then rises as the temperature is lowered further. We can now see that the $T_2$ measured on the central line is indeed a weighted average of the two separate $T_2$ times (inner and outer), for temperatures above $T_g$. Below $T_g$, the outer coherences decay sufficiently quickly (T$_{2,o}$< 1\mu s) and thus they become unobservable in spin echo experiment. Indeed, only T$_{2,i}$ can be measured below $T_g$. Recognizing the fact that $T_{2,i}$ measured for $M_I = 0$ and $-1$ are almost identical (within the error of the experiment) in a broad temperature range below 120K, we can conclude that hyperfine interaction with $^{14}$N nucleus has no visible effect on $T_2$ in N@C$_{60}$ at low temperatures.

The fact that T$_{2,o}$ is much shorter than T$_{2,i}$ at low temperatures can be explained by the effect of a non-zero ZFS. The glassy solvent matrix around the fullerene imposes a distortion of the N@C$_{60}$ cage, inducing a ZFS strain to the nitrogen atom. At temperatures approaching $T_g$ and below, the rotational mobility of fullerenes slows down and therefore complete motional averaging of the non-zero ZFS is not achieved. In this case, the ZFS strain creates an inhomogeneous broadening of the EPR transitions, and the outer transitions within the S=3/2 multiplet are broadened more significantly, i.e. via the first-order ZFS, in contrast to the inner transition which are broadened only via the second-order ZFS. Provided the ZFS broadening is small compared to the excitation bandwidth of the microwave pulses, and thus the second pulse in spin echo experiment refocuses all transitions within the S=3/2 multiplet, such a ZFS broadening would not be refocused for the outer coherences and appears instead as an additional dephasing mechanism, leading to fast decay of the outer transitions. On the other hand, the inner transition is fully refocused, and its decoherence time, $T_{2,i}$, appears unaffected by the ZFS.

As follows from the above discussion, the two strongest interactions in N@C$_{60}$, the ZFS strain and the hyperfine coupling to the central $^{14}$N nucleus, have little effect on $T_{2,i}$. Therefore, some other interactions need to be considered to explain $T_{2,i}$, and its temperature dependence. Here we propose that these mechanisms involve nuclear $^{35}$Cl and $^{37}$Cl spins of solvent molecules in frozen S$_2$Cl$_2$/CS$_2$ mixture. The theory of decoherence for electron spins interacting with a bath of nuclear spins (so-called theory of spin diffusion) has been developed decades ago \cite{7,8,9}. More recently the theory has been extended beyond stochastic treatment of random nuclear flip-flops to a coherent treatment of all spins together as a single many-body system \cite{10,28}. The new theory is also robust to translational diffusion of solvent molecules, covering the fast and slow diffusion regimes, from motional narrowing at high temperatures to the rigid limit at low temperatures. Thus this theory is ideal for the temperature range studied here. We notice however that this theory has been developed for a bath of nuclear spins 1\rightarrow 1/2 and as such it may only be used as an approximation in analyzing our data for 1\rightarrow 3/2 of $^{35}$Cl and $^{37}$Cl.

In the rigid limit, i.e. no translational diffusion, spin diffusion theory predicts a stretched exponential dependence of the echo decays, e.g. $V(\tau) = A \cdot \exp(-2\tau/T_{2,i})^n$, with $2 \leq n \leq 3$, and $\tau$ being the delay between pulses in a two-pulse echo experiment \cite{7,8,5,28}. This dependence seems to be inconsistent with the simple exponential decay, $V(\tau) = A \cdot \exp(-2\tau/T_{2,i})$, observed in our experiments for N@C$_{60}$ in S$_2$Cl$_2$/CS$_2$ at all temperatures studied from 20 K to 170 K.
An echo decay close to a simple exponential is predicted in the slow diffusion regime and assuming low nuclear spin concentrations [10]. In this case the echo decay is dominated by a term $\tau^{9/8}$ in the exponential, which is close enough to be indistinguishable from a simple exponential decay in our experiments. For the CS$_2$/S$_2$Cl$_2$ (3/1) mixture used here, we can estimate $c/d^3 < 0.1$ (where $c$ is concentration of $^{35}$Cl or $^{37}$Cl nuclei, and $d$ is distance of closest approach between electron and nuclear spins) which satisfies the derived criteria for low nuclear spin concentration [10]. Using Eqn.(3.7) from Ref. [10], we can reproduce the mono-exponential decay with $T_{2,i} = 230 \mu s$ for N@C$_{60}$ at 20 K assuming a diffusion coefficient $D = 5 \cdot 10^{-10}$ cm$^2$/s for solvent molecules in CS$_2$/S$_2$Cl$_2$. This $D$ is small but nevertheless large enough for the exponential term $\tau^{9/8}$ to dominate over spin diffusion term $\tau^2$ expected in the rigid limit [28].

As temperature increases from 20 K (and consequently $D$ also increases), $T_2$ is predicted to initially decrease and then increase after reaching a minimum at a temperature where $D \approx 0.1 g_\gamma \gamma_\nu \hbar \cdot d$ [28]. This minimum corresponds to a transition from the intermediate to fast diffusion regimes; a mono-exponential term continues to dominate spin echo decay in both these regimes. For CS$_2$/S$_2$Cl$_2$ this $T_2$ minimum is expected to occur at temperature where $D = 10^{-10}$ cm$^2$/s. Comparing with our $T_{2,i}$ data in Figure 6, we see that $T_{2,i}$ indeed develops a minimum at around 100 K. Thus, as temperature increases from 20 to 100 K, $T_{2,i}$ decreases by one order of magnitude (from 230 $\mu$s to 20 $\mu$s) and $D$ increases by five orders of magnitude (from $10^{-15}$ cm$^2$/s to $10^{-10}$ cm$^2$/s). This corresponds to an approximate dependence $T_2 \sim D^{-0.2}$ and thus differs slightly from $D^{-0.36}$ predicted by the theory for $I=1/2$ [28]. As temperature increases beyond 100 K, $T_{2,i}$ increases to 100 $\mu$s at 165 K, and we can infer that $D$ increases only by about an order of magnitude.

To conclude, by comparing our data with the relationship between decoherence rate and diffusion coefficient described in Ref. [28], we infer that $D$ changes relatively slowly above about 100 K, in contrast to the sharp drop in $D$ observed below 100 K. This is consistent with the expected behaviour around the glass transition temperature, $T_g$.

V. CONCLUSIONS

In summary, the effect of nuclear spins in toluene surrounding N@C$_{60}$ on the decoherence time has been demonstrated using two different isotopes of hydrogen. The data fit well to a model for relaxation by translational diffusion, providing estimates of the diffusion coefficient for C$_{60}$ in toluene.

The nuclear spin concentration can be reduced by using a solvent mixture of CS$_2$ and S$_2$Cl$_2$. Using such mixture, decoherence times approaching $0.23$ ms were observed at temperatures below 20 K, demonstrating this to be a good choice of solvent for low-temperature studies on N@C$_{60}$. Below about 100 K, the outer coherences are not refocussed, turning N@C$_{60}$ into a ‘quasi’ S=1/2 spin system. Translational diffusion of local nuclear spins continues to play the dominant role in decoherence, even for an estimated $D$ as low as $10^{-15}$ cm$^2$/s.

VI. ACKNOWLEDGEMENTS

We acknowledge helpful discussions with Mark Sambrook, and thank the Oxford-Princeton Link fund for support. This research is part of the QIP IRC www.qipirc.org (GR/S82176/01) and was supported by EPSRC grant number EP/D048559/1. JJLM is supported by St. John’s College, Oxford. AA is supported by the Royal Society. GADB is supported by the EPSRC (GR/S15808/01). Work at Princeton was supported by the NSF International Office through the Princeton MR-SEC Grant No. DMR-0213706 and by the ARO and ARDA under Contract No. DAAD19-02-1-0040.

[1] C. Knapp, K.-P. Dinse, B. Pietzak, M. Waiblinger, and A. Weidinger, Chem. Phys. Lett. 272, 433 (1997).
[2] W. Harneit, Phys. Rev. A 65, 32322 (2002).
[3] S. C. Benjamin, A. Ardavan, G. A. D. Briggs, D. A. Britz, D. Gunlycke, J. Jefferson, M. A. G. Jones, D. F. Leigh, B. W. Lovett, A. N. Khlobystov, et al., quant-ph/0511198 (2004).
[4] E. Dietel, A. Hirsch, B. Pietzak, M. Waiblinger, K. Lips, A. Weidinger, A. Gruss, and K.-P. Dinse, J. Am. Chem. Soc. 121, 2432 (1999).
[5] J. J. L. Morton, A. M. Tyryshkin, A. Ardavan, K. Poryfrikis, S. A. Lyon, and G. A. D. Briggs, J. Chem. Phys. 124, 014508 (2006).
[6] L. Banci, I. Bertini, and C. Luchinat, Nuclear and Electron Relaxation (VCH, Weinheim, 1991).
[7] J. R. Klauder and P. W. Anderson, Phys. Rev. 125, 912 (1962).
[8] G. M. Zhidomirov and K. M. Salikhov, Soviet Physics JETP - USSR 29, 1037 (1969).
[9] A. D. Milov, K. M. Salikhov, and Y. D. Tsvetkov, Fiz. Tverd. Tela 15, 1187 (1973).
[10] A. A. Nevzorov and J. H. Freed, J. Chem. Phys. 117, 282 (2002).
[11] A. D. Bokare and A. Pataia, J. Chem. Phys. 119, 4529 (2003).
[12] Q. Ying, J. Marecek, and B. Chu, J. Chem. Phys. 101, 2665 (1994).
[13] V. N. Bezmel’nitsyn, A. V. Eletskii, and E. V. J. Sepanov, J. Phys. Chem. 98, 6665 (1994).
[14] S. Nath, H. Pal, D. K. Palt, A. V. Sapre, and J. P. Mittal, J. Phys. Chem. B 102, 10158 (1998).
[15] R. G. Alargova, S. Deluchi, and K. Tsuji, J. Am. Chem.
Soc. 123, 10 (2001).

[16] L. A. Bulavin, I. I. Adamenko, V. M. Yashchuk, T. Ogul'chansky, Y. I. Prylutskyy, S. S. Durov, and P. Scarff, J. Mol. Liq. 93, 187 (2001).

[17] S. Nath, H. Pal, and A. V. Sapre, Chem. Phys. Lett. 327, 143 (2000).

[18] R. S. Ruoff, R. Malhotra, and D. L. Huestis, Nature 362, 140 (1993).

[19] A. Schweiger and G. Jeschke, Principles of Pulse Electron Paramagnetic Resonance (Oxford University Press, Oxford, UK; New York, 2001).

[20] S. H. Gallagher, R. S. Armstrong, P. A. Lay, and C. A. Reed, Chem. Phys. Lett. 248, 353 (1996).

[21] S. H. Gallagher, R. S. Armstrong, W. A. Clucas, P. A. Lay, and C. A. Reed, J. Phys. Chem. A 101, 2960 (1997).

[22] L.-P. Hwang and J. H. Freed, J. Chem. Phys. 63, 4017 (1975).

[23] J. H. Freed, J. Chem. Phys. 68, 4034 (1978).

[24] C. F. Polnaszek and R. G. Bryant, J. Chem. Phys. 81, 4038 (1984).

[25] G. Hinze and H. Sillescu, J. Chem. Phys. 104, 314 (1996).

[26] M. J. Assael, H. M. T. Avelino, N. K. Dalaouti, J. M. N. A. Fareleira, and K. R. Harris, Int. J. Thermophys. 22, 789 (2001).

[27] C. A. Angell, B. E. Richards, and V. Velikov, J. Phys. Cond. Matt. 11, A75 (1999).

[28] A. A. Nevzorov and J. H. Freed, J. Chem. Phys. 115, 2416 (2001).