Study of the Suppressed Decays $B^\pm \to [K^\mp \pi^\pm]_D K^\pm$ and $B^\pm \to [K^\mp \pi^\pm]_D \pi^\pm$ at Belle

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Abstract

We report an updated study of the suppressed decays $B^− \rightarrow [K^+\pi^-]DK^−$ and $B^− \rightarrow [K^+\pi^-]D\pi^−$ where $[K^+\pi^-]_D$ indicates that the $K^+\pi^−$ pair originates from a neutral $D$ meson. A data sample containing 386 million $B\bar{B}$ pairs recorded at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric $e^+e^−$ storage ring is used. This decay mode is sensitive to the CKM angle $\phi_3$. We do not see a significant signal for $B^− \rightarrow [K^+\pi^-]DK^−$, and we set a limit on the ratio of $B$ decay amplitudes $r_B < 0.18$ at the 90% confidence level. We measure the $CP$ asymmetry of the $B^− \rightarrow [K^+\pi^-]D\pi^−$ mode, $A_{D\pi} = 0.10 \pm 0.22$ (stat) $\pm 0.02$ (syst).
INTRODUCTION

Precise measurements of the elements of the Cabibbo-Kobayashi-Maskawa matrix [1] constrain the Standard Model and may reveal new physics. However, the extraction of the Unitarity Triangle angle $\phi_3$ [2] is a challenging measurement even with modern high luminosity $B$ factories. Several methods for measuring $\phi_3$ use the interference between $B^- \to D^0K^-$ and $B^- \to \bar{D}^0K^-$, which occurs when $D^0$ and $\bar{D}^0$ decay to common final states [3, 4]. $CP$ violation occurs when both weak and strong phase differences between the amplitudes are non-trivial. As noted by Atwood, Dunietz and Soni (ADS) [5], $CP$ violation effects are enhanced if the final state is chosen so that the interfering amplitudes have comparable magnitudes; the archetype uses $B^- \to [K^+\pi^-]_D K^-$, where $[K^+\pi^-]_D$ indicates that the $K^+\pi^-$ pair originates from a neutral $D$ meson. In this case, the colour-allowed $B$ decay followed by the doubly Cabibbo-suppressed $D$ decay interferes with the colour-suppressed $B$ decay followed by the Cabibbo-allowed $D$ decay (Fig. 1). Previous studies of this decay mode by BaBar [6] and Belle [7] have not found any significant signals for $B^- \to [K^+\pi^-]_D K^-$. For the suppressed decay $B^- \to [K^+\pi^-]_D \pi^-$, both topology and phenomenology are similar to $B^- \to [K^+\pi^-]_D K^-$; our previous publication reported the first observation of this mode [7].

ANALYSIS

In this paper, we report an updated analysis of the suppressed decays $B^\pm \to [K^\pm\pi^\pm]_D K^\pm$ and $B^\pm \to [K^\mp\pi^\mp]_D \pi^\pm$. In addition, the allowed decays $B^\pm \to [K^\pm\pi^\mp]_D K^\mp$ and $B^\pm \to [K^\pm\pi^\pm]_D \pi^\mp$ are used as control samples to reduce systematic uncertainties. The same selection criteria for the suppressed decay modes are applied to the control samples whenever possible. The main changes with respect to our previous publication [7] are the inclusion of additional data corresponding to 111 million $B\bar{B}$ pairs, and improved suppression of the dominant continuum background. Throughout this report, charge conjugate states are implied except where explicitly mentioned and we denote the analysed decay modes as follows:

- Suppressed decay $B^- \to [K^+\pi^-]_D h^- : B^- \to D_{\text{sup}} h^-$
- Allowed decay $B^- \to [K^-\pi^+]_D h^- : B^- \to D_{\text{fav}} h^- (h = K, \pi)$.

The results are based on a data sample containing 386 million $B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric energy $e^+e^-$ collider [8].
The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Čerenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect $K^{0}_{S}$ mesons and to identify muons (KLM). The detector is described in detail elsewhere [9]. Two different inner detector configurations were used. For the first sample of 152 million $B\bar{B}$ pairs, a 2.0 cm radius beampipe and a 3-layer silicon vertex detector were used; for the latter 234 million $B\bar{B}$ pairs, a 1.5 cm radius beampipe, a 4-layer silicon detector and a small-cell inner drift chamber were used [10].

**Event selection**

$D$ mesons are reconstructed by combining two oppositely charged tracks. These charged tracks are required to have a point of closest approach to the beam line within ±5 mm of the interaction point in the direction perpendicular to the beam axis ($dr$) and ±5 cm in the direction antiparallel to the positron beam axis ($dz$). A $K/\pi$ likelihood ratio $P(K/\pi) = \mathcal{L}_{K}/(\mathcal{L}_{K} + \mathcal{L}_{\pi})$ is formed for each track, where $\mathcal{L}_{K}$ and $\mathcal{L}_{\pi}$ are kaon and pion likelihoods, calculated using $dE/dx$ measurements from the CDC, Čerenkov light yields in the ACC and timing information from the TOF. We used the particle identification requirement $P(K/\pi) > 0.4$ and $P(K/\pi) < 0.7$ for kaons and pions from $D \rightarrow K\pi$ decays, respectively. $D$ candidates are required to have an invariant mass within ±2.5σ of the nominal $D^0$ mass: 1.850 GeV/$c^2 < M(K\pi) < 1.879$ GeV/$c^2$. To improve the momentum determination, tracks from the $D$ candidate are refitted according to the nominal $D^0$ mass hypothesis and the reconstructed vertex position (a mass-and-vertex-constrained fit).

$B$ mesons are reconstructed by combining $D$ candidates with primary charged hadron candidates. For the primary charged tracks, we require $P(K/\pi) > 0.6$ for the kaon in $B^- \rightarrow DK^-$ and $P(K/\pi) < 0.2$ for the pion in $B^- \rightarrow D\pi^-$. The signal is identified by two kinematic variables, the energy difference $\Delta E = E_D + E_{K^-(-\pi^-)} - E_{beam}$ and the beam-energy-constrained mass $M_{bc} = \sqrt{E_{beam}^2 - (\vec{p}_D + \vec{p}_{K^-(-\pi^-)})^2}$, where $E_D$ is the energy of the $D$ candidate, $E_{K^-(-\pi^-)}$ is the energy of the $K^-(\pi^-)$ and $E_{beam}$ is the beam energy, in the centre of mass (cm) frame. $\vec{p}_D$ and $\vec{p}_{K^-(-\pi^-)}$ are the momenta of the $D$ and $K^-(-\pi^-)$ in the cm frame. We define the signal region as $5.27$ GeV/$c^2 < M_{bc} < 5.29$ GeV/$c^2$ and $-0.05$ GeV $< \Delta E < 0.05$ GeV. In the case of multiple candidates, which occurs in 1–2% of events with at least one candidate, we choose the best candidate on the basis of a $\chi^2$ determined from the difference between the measured and nominal values of $M_{bc}$.

$q\bar{q}$ continuum suppression

To suppress the large background from the two-jet like $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) continuum processes, variables that characterise the event topology are used. We construct a Fisher discriminant [11] of modified Fox-Wolfram moments [12], which we denote $SF_{FW}$. The Fisher coefficients are optimized by maximising the separation between signal events and continuum events. Furthermore, $\cos \theta_B$, the angle in the cm system of the $B$ flight direction with respect to the beam axis is also used to distinguish $B\bar{B}$ events from continuum events.
These two independent variables, $SFW$ and $\cos \theta_B$, are combined to form a likelihood ratio ($R$),

$$R = \frac{L_{\text{sig}}}{(L_{\text{sig}} + L_{\text{cont}})}$$

$$L_{\text{sig(cont)}} = L_{\text{SFW}}^{\text{sig(cont)}} \times L_{\cos \theta_B}^{\text{sig(cont)}}$$

where $L_{\text{sig}}$ and $L_{\text{cont}}$ are likelihoods defined from $SFW$ and $\cos \theta_B$ distributions for signal and continuum backgrounds, respectively. We optimize the $R$ requirement by maximising $S/\sqrt{S+N}$, where $S$ and $N$ denote the expected number of signal and background events in the signal region. The signal expectations are calculated from our previous results [7], the efficiency obtained from Monte Carlo simulation (given later), and the number of $B\bar{B}$ pairs; the background expectations are obtained using events in the $M_{bc}$ sideband ($5.240 \text{ GeV}/c^2 < M_{bc} < 5.265 \text{ GeV}/c^2$), with the extrapolation into the signal region based on Monte Carlo. For $B^- \to D_{\text{sup}}K^-(\pi^-)$ we require $R > 0.90$ (0.74), which retains 40.0% (65.7%) of the signal and removes 99.0% (94.3%) of the continuum background.

**Peaking backgrounds**

For $B^- \to D_{\text{sup}}K^-$, one can have a contribution from $B^- \to D^0\pi^-$, $D^0 \to K^+K^-$, which has the same final state and can peak under the signal. In order to reject these events, we veto events that satisfy $1.843 \text{ GeV}/c^2 < M(KK) < 1.894 \text{ GeV}/c^2$. The allowed decay $B^- \to D_{\text{fav}}h^-$ can also cause a peaking background for the suppressed decay modes due to $K\pi$ misidentification. Therefore, we veto events for which the invariant mass of the $K\pi$ pair is inside the $D$ mass cut window when the mass assignments are exchanged. Furthermore, three-body charmless decays $B^- \to K^+K^-\pi^-$ and $B^- \to K^+\pi^-\pi^-$ can peak inside the signal region for $B^- \to D_{\text{sup}}K^-$ and $B^- \to D_{\text{sup}}\pi^-$, respectively. These peaking backgrounds are estimated from the $\Delta E$ distributions of events in a $D$ mass sideband, corresponding to $\pm(2.5-10)\sigma$ away from the nominal $D$ mass ($1.807 \text{ GeV}/c^2 < M(K\pi) < 1.850 \text{ GeV}/c^2$ and $1.879 \text{ GeV}/c^2 < M(K\pi) < 1.937 \text{ GeV}/c^2$). We fit these distributions, which are shown in Fig. 2, using a procedure similar to that used for candidate signal events (described later). For $B^- \to D_{\text{sup}}\pi^-$, the peaking background estimated by fitting the plot is consistent with zero. Since the Standard Model prediction for the $B^- \to K^+\pi^-\pi^-$ branching fraction is smaller than $10^{-11}$ [13], this background contribution is ignored. On the other hand, for $B^- \to D_{\text{sup}}K^-$, the peaking background yield in the $D$ mass sideband is $7.3^{+6.6}_{-6.0}$ events, from which we expect $2.4^{+2.3}_{-2.0}$ peaking background events inside the $\Delta E$ signal region.

After applying all the cuts, the signal efficiencies are 14.6% and 24.5% for $B^- \to D_{\text{sup}}K^-$ and $B^- \to D_{\text{sup}}\pi^-$, respectively. The signal yields are extracted by fitting the $\Delta E$ distributions.

**Fitting the $\Delta E$ distributions**

Backgrounds from decays such as $B^- \to D\rho^-$ and $B^- \to D^*\pi^-$ are distributed in the negative $\Delta E$ region and make a small contribution to the signal region. The shape of this $B\bar{B}$ background is modelled as a smoothed histogram from generic Monte Carlo (MC) samples. The continuum background populates the entire $\Delta E$ region. We model its shape with as a first order polynomial. The signal $\Delta E$ distribution is modelled as the sum of two Gaussian distributions with a common mean.
FIG. 2: $\Delta E$ distributions for events in the $D^0$ mass sideband for (left) $B^- \rightarrow D_{\text{sup}}K^-$ and (right) $B^- \rightarrow D_{\text{sup}}\pi^-$. The signal shapes are modelled using the results of the $B^- \rightarrow D_{\text{fav}}h^-$ ($h = K, \pi$) fit.

| Mode               | Efficiency (%) | Signal Yield       |
|--------------------|----------------|-------------------|
| $B^- \rightarrow D_{\text{sup}}K^-$ | 14.6 ± 0.2     | 2.4$^{+4.9}_{-4.4}$ / 0.0$^{+3.3}_{-5.0}$ |
| $B^- \rightarrow D_{\text{sup}}\pi^-$ | 24.5 ± 0.3     | 50$^{+10}_{-11}$   |
| $B^- \rightarrow D_{\text{fav}}K^-$  | 14.5 ± 0.2     | 634$^{+59}_{-90}$  |
| $B^- \rightarrow D_{\text{fav}}\pi^-$ | 24.9 ± 0.3     | 14518 ± 125       |

In the fit to the $\Delta E$ distribution of $B^- \rightarrow D_{\text{fav}}\pi^-$, the free parameters are the position, widths, area and fraction in the tail of the signal peak, the slope and normalisation of the continuum component and the normalisation of the $B\bar{B}$ background. For the $B^- \rightarrow D_{\text{fav}}K^-$ fit, there is an additional component due to feed-across from $D_{\text{fav}}\pi^-$, which we model with a Gaussian shape that has different widths on the left and right sides of the peak, since the shift caused by wrong mass assignment makes the shape asymmetric. The normalisation and shape parameters of this function are free parameters of the fit (all parameters which are floated in the $B^- \rightarrow D_{\text{fav}}\pi^-$ fit are again free parameters).

For $B^- \rightarrow D_{\text{sup}}K^-$ and $B^- \rightarrow D_{\text{sup}}\pi^-$, the signal and $B\bar{B}$ background shapes are modelled using the results of the fits to the corresponding favoured modes. The free parameters are the normalisations of the three components, and the slope of the continuum. The amount of feed-across from $D_{\text{sup}}\pi^-$ to $D_{\text{sup}}K^-$ is a free parameter, but is found to be negligible, as expected. The fit results are shown in Fig. 3. The numbers of events for $B^- \rightarrow D_{\text{sup}}h^-$ and $D_{\text{fav}}h^-$ are given in Table I.
FIG. 3: ∆E fit results for (top left) $B^- \rightarrow D_{sup} K^-$, (top right) $B^- \rightarrow D_{sup} \pi^-$, (bottom left) $B^- \rightarrow D_{fav} K^-$, (bottom right) $B^- \rightarrow D_{fav} \pi^-$. Charge conjugate modes are included.

RESULTS

Ratio of branching fractions $R_{Dh}$

We calculate ratios of product branching fractions, defined as

$$R_{Dh} \equiv \frac{B(B^- \rightarrow D_{sup} h^-)}{B(B^- \rightarrow D_{fav} h^-)} = \frac{N_{D_{sup} h^-} / \epsilon_{D_{sup} h^-}}{N_{D_{fav} h^-} / \epsilon_{D_{fav} h^-}} (h = K, \pi),$$

where $N_{D_{sup} h^-}$ ($N_{D_{fav} h^-}$) and $\epsilon_{D_{sup} h^-}$ ($\epsilon_{D_{fav} h^-}$) are the number of signal events and the reconstruction efficiency for the decay $B^- \rightarrow D_{sup} h^-$ ($B^- \rightarrow D_{fav} h^-$), and are given in Table I. We obtain

$$R_{DK} = (0.0^{+8.4}_{-7.9} \, \text{(stat)} \pm 1.0 \, \text{(syst)}) \times 10^{-3},$$
$$R_{D\pi} = (3.5^{+0.8}_{-0.7} \, \text{(stat)} \pm 0.3 \, \text{(syst)}) \times 10^{-3}.$$ 

Since the signal for $B^- \rightarrow D_{sup} K^-$ is not significant, we set an upper limit at the 90% confidence level (C.L.) of $R_{DK} < 13.9 \times 10^{-3}$, where we take the likelihood function as a Gaussian distribution with width given by the quadratic sum of statistical and systematic errors, and the area is normalised in the physical region of positive branching fraction.
Most of the systematic uncertainties from the detection efficiencies and the particle identification cancel when taking the ratios, since the kinematics of the $B^- \to D_{sup}^{h-}$ and $B^- \to D_{fav}^{h-}$ processes are similar. The systematic errors are due to uncertainties in the yield extraction and the efficiency difference between $B^- \to D_{sup}^{h-}$ and $B^- \to D_{fav}^{h-}$. The uncertainties in the signal shapes and the $q\bar{q}$ background shapes are determined by varying the shape of the fitting function by $\pm 1\sigma$. The uncertainties in the $B\bar{B}$ background shapes are determined by fitting the $\Delta E$ distribution in the region $-0.07 \text{ GeV} < \Delta E < 0.20 \text{ GeV}$ ignoring the $B\bar{B}$ background contributions — this is the largest source of uncertainty: the signal yields are affected by $7.4\%$ and $28.4\%$ for $D_{sup}\pi$ and $D_{sup}K$ (before peaking background subtraction) respectively. The uncertainties in the efficiency differences are determined using signal MC. The total systematic error is the sum in quadrature of the above uncertainties.

The ratio $R_{DK}$ is related to $\phi_3$ by

$$R_{DK} = r_B^2 + r_D^2 + 2r_Br_D \cos \phi_3 \cos \delta,$$

where

$$r_B \equiv \left| \frac{A(B^- \to \bar{D}^0 K^-)}{A(B^- \to D^0 K^-)} \right|, \quad \delta \equiv \delta_B + \delta_D,$$

$$r_D = \left| \frac{A(D^0 \to K^+ \pi^-)}{A(D^0 \to K^- \pi^+)} \right| = 0.060 \pm 0.003.$$

and $\delta_B (\delta_D)$ is the strong phase difference between the two $B (D)$ decay amplitudes. Using the above result, we obtain a limit on $r_B$. The least restrictive limit is obtained allowing $\pm 2\sigma$ variation on $r_D$ and assuming maximal interference ($\phi_3 = 0^\circ, \delta = 180^\circ$ or $\phi_3 = 180^\circ, \delta = 0^\circ$) and is found to be $r_B < 0.18$ at the 90\% confidence level, as shown in Fig. 4.

![FIG. 4: Constraint on $r_B$ from $R_{DK}$.](image-url)
FIG. 5: $\Delta E$ fit results for (left) $B^- \rightarrow D_{sup}^{*} \pi^-$ and (right) $B^+ \rightarrow D_{sup}^{*} \pi^+$. 

**CP asymmetry**

We search for $CP$ violating asymmetry in the $B^\pm \rightarrow D_{sup}^{*} \pi^\pm$ mode. We fit the $B^+$ and $B^-$ yields separately, and determine $A_{D\pi}$ as

$$A_{D\pi} \equiv \frac{B(B^- \rightarrow D_{sup}^{*} \pi^-) - B(B^+ \rightarrow D_{sup}^{*} \pi^+)}{B(B^- \rightarrow D_{sup}^{*} \pi^-) + B(B^+ \rightarrow D_{sup}^{*} \pi^+)}.$$ 

The fit results are shown in Fig. 5. We find $25.6^{+7.4}_{-6.7} B^- \rightarrow D_{sup}^{*} \pi^-$ events and $21.0^{+7.7}_{-7.0} B^+ \rightarrow D_{sup}^{*} \pi^+$ events, giving an asymmetry of

$$A_{D\pi} = 0.10 \pm 0.22 \text{(stat)} \pm 0.02 \text{(syst)},$$

where systematic uncertainties arise from possible detector charge asymmetry (0.017; determined from the $B^\pm \rightarrow D_{fav}^{*} \pi^\pm$ sample [15]), and the $B^+$ and $B^-$ yield extraction (0.016; determined as for $R_{D\pi}$). The total systematic error is obtained by taking the quadratic sum. The measured partial rate asymmetry $A_{D\pi}$ is consistent with zero.

**SUMMARY**

Using 386 million $B\bar{B}$ pairs collected with the Belle detector, we report studies of the suppressed decays $B^- \rightarrow D_{sup}^{*} h^-$ ($h = K, \pi$). We do not observe a signal for $B^- \rightarrow D_{sup}^{*} K^-$, and place a limit on the ratio of $B$ decay amplitudes $r_B < 0.18$ at the 90% confidence level. We have measured the $CP$ asymmetry in the related mode, $A_{D\pi} = 0.10 \pm 0.22 \text{(stat)} \pm 0.02 \text{(syst)}$.

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