Imaging strain-localized excitons in nanoscale bubbles of monolayer WSe$_2$ at room temperature

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In monolayer transition-metal dichalcogenides, localized strain can be used to design nanoarrays of single photon sources. Despite strong empirical correlation, the nanoscale interplay between excitons and local crystalline structure that gives rise to these quantum emitters is poorly understood. Here, we combine room-temperature nano-optical imaging and spectroscopic analysis of excitons in nanobubbles of monolayer WSe$_2$ with atomistic models to study how strain induces nanoscale confinement potentials and localized exciton states. The imaging of nanobubbles in monolayers with low defect concentrations reveals localized excitons on length scales of around 10 nm at multiple sites around the periphery of individual nanobubbles, in stark contrast to predictions of continuum models of strain. These results agree with theoretical confinement potentials atomistically derived from the measured topographies of nanobubbles. Our results provide experimental and theoretical insights into strain-induced exciton localization on length scales commensurate with exciton size, realizing key nanoscale structure-property information on quantum emitters in monolayer WSe$_2$. 

The intense light–matter interactions of two-dimensional (2D) monolayer transition-metal dichalcogenides (1L-TMDs) are mediated by a diverse suite of excitonic phenomena that present a wealth of opportunities for novel optoelectronic functionalities in areas spanning from high-performance sensing and non-traditional photovoltaics to the quantum information sciences. Many of these opportunities emerge from—and heavily rely on—the unique ways in which the 2D transition-metal dichalcogenide (TMD) semiconductors enable the manipulation of excitonic phenomena on the nanoscale. Within this collection of capabilities, strain engineering is pre-eminent, offering unprecedented flexibility and precision, and opening new routes to highly tailored optoelectronic materials. Extrinsic strains of up to several per cent can be endured without fracture and have been shown to continuously reduce the optical bandgap as well as to modify the exciton–photon coupling, thus narrowing the photoluminescence linewidth. Further, such strain can be localized, embedding nanoscale potential energy wells for the funnelling and localization of excitons. Notably, in 1L-WSe$_2$, it has become evident that local strain is a key ingredient for the formation of low-temperature quantum emitters and that strain engineering can potentially extend their operating range to room temperature. The resulting highly integrable solid-state non-classical light sources underscore the technological potential of harnessing strain to engineer nanoscale exciton localization in 2D TMD semiconductors.

Despite the observations of exciton funnelling and single-photon emission in localized strained regions of 2D TMDs, an understanding of the induced exciton localization is notably lacking, especially on the nanoscale. This absence of a fundamental picture has led to critical ambiguities, particularly concerning the formation of quantum emitters in 1L-WSe$_2$, in which the roles and interplay between strain, excitons and crystallographic defects remain largely a mystery. For instance, it has been shown that the quantum emission can be co-localized with a nanobubble, where strain models derived from continuum elastic plate theory predict that a single region of maximum strain (and thus exciton localization) occurs at the apex of the nanobubble. However, multiple emitters per nanobubble are typically observed, which is at odds with a single localization site and suggests a possible role of crystallographic defect states or some other sub-nanobubble inhomogeneity. Recently, improved microscopic theoretical models have predicted that quantum dot-like electronic states in TMDs can form within nanobubbles in the absence of defects. In particular, a first-principles approach that carefully considers the strain-induced atomic structure and which we employ here has predicted that strain maxima and multiple low-energy states form in a doughnut-like distribution near the nanobubble periphery. This surprising strain distribution is an apparent result of atomic-scale wrinkling around the edges of highly strained nanobubbles, leading to more localized lower-energy states relative to the case of a nanobubble with a smooth topography. Such predicted states provide the critical missing piece of the puzzle for understanding and controlling the strain localization of excitons in 2D TMD semiconductors. However, due to their nanoscale size and distribution within a nanobubble, these localized energy states cannot be directly resolved with far-field optical characterization methods, necessitating interrogation by more sophisticated higher-resolution techniques.

In this work, we employed apertureless scanning near-field optical microscopy to image the localized exciton (LX) states within nanobubbles of 1L-WSe$_2$. Using hyperspectral nanophotoluminescence

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Nano-optics of nanobubbles of WSe$_2$

Numerous processes that are critical for developing advanced functionalities and devices with 1L-TMD semiconductors have been studied with nano-optical methods, revealing a rich suite of highly localized optoelectronic phenomena$^{29-31}$. Figure 1a illustrates the experimental configuration of our nanophotoluminescence investigations of individual nanobubbles of 1L-WSe$_2$ in which a sharp silver tip (Horiba) has been positioned within 2 nm of the 1L-WSe$_2$ (Fig. 1a). A complete discussion of the experimental techniques is presented in the Supplementary Information. Briefly, the tip-sample junction was illuminated from the side with p-polarized, continuous-wave laser excitation (637.27 nm, 75–100 µW) at an oblique angle of incidence such that the induced polarization of the tip can couple with the in-plane and out-of-plane transition dipoles$^{32-34}$. As the sample was raster-scanned, nanophotoluminescence from the tip-sample junction and the local topography of the 1L-WSe$_2$ were simultaneously recorded.

As indicated in the atomic force microscopy (AFM) micrograph (Fig. 1b), the entirety of the 1L-WSe$_2$ in Figs. 1–3 is supported by an underlying crystalline hexagonal boron nitride (h-BN; ~200-nm thick), forming a 2D 1L-WSe$_2$/h-BN heterostructure. We note that a portion of this 1L-WSe$_2$ flake is fully encapsulated and covered by a second, thin h-BN crystal (~3 nm). However, all of the results presented here were acquired from the exposed 1L-WSe$_2$ that is directly accessible to the nano-optical antenna (as illustrated in Fig. 1a). Details of the ‘dry-stamping’ sample fabrication process are provided in an earlier report$^{31}$ and the Supplementary Information. This process is known to produce structural ‘imperfections’ such as nanobubbles, tears, folds and wrinkles. In our case, a portion of the 1L-WSe$_2$ folded on top of itself to form a bilayer and several pronounced creases (Fig. 1b). In addition, small topographical nanobubbles, with characteristic heights of ~2–10 nm, are observed in the 1L-WSe$_2$ and are attributed to trapped substances between the layers$^{32}$. Such nanobubbles have been repeatedly observed in heterostructures of layered materials$^{33,34,35}$, and as noted above, correlate with quantum emitters in 1L-WSe$_2$ at cryogenic temperatures$^{11}$.

Figure 1c contrasts the nanophotoluminescence spectra collected from a flat region and a nanobubble of the 1L-WSe$_2$ at room temperature. The spectrum of the flat region is composed of the standard excitonic photoluminescence of 1L-WSe$_2$, at ~1.65 eV$^{29,34}$, which we will refer to as the primary exciton (PX). The emission spectrum recorded when the nano-optical antenna was positioned over a nanobubble is dramatically different, exhibiting redshifted excitonic emission and an additional intense low-energy emission band centred at ~1.56 eV, as determined by Gaussian peak fitting (Supplementary Fig. 2 and Supplementary Methods). We note in these spectra that there is increased noise in the region of the PX state due to the subtraction of the far-field signal, as discussed in the Supplementary Information. In the 1L-WSe$_2$, every region that was found to exhibit strong low-energy emission correlated with a nanobubble (see white arrows in Figs. 1b and 1d). A selection of such emission spectra from four individual nanobubbles together with their associated topographies is shown in Supplementary Fig. 3. The lateral extents of the nanobubbles are in the range of ~30–140 nm with heights of 1.5–20 nm and, depending on size, they exhibit a diverse set of broad emission spectra, some of which show signatures of multiple low-energy states. In general, low-energy emission occurs at emission energies that span a range of about 70 meV (from ~80 to ~150 meV below the PX) and exhibits linewidths of ~150 meV that are attributed to thermal broadening$^{30}$ and plasmonic coupling to the tip$^{34}$.

Close inspection of the nanophotoluminescence spectra in Fig. 1c reveals several characteristics of the low-energy photoluminescence that are different from the well-studied PX state. First, we concurrently observe both the low-energy emission and strong emission at ~1.65 eV, corresponding to the PX spectra measured in
the far field (inset in Fig. 1c), within our nano-optical mode volume. Second, the low-energy band here is well below the energies of other native excitonic complexes in this material (for example, trions, the dark exciton \[^{40}\] and biexcitons \[^{41}\]) and in an energetic region that is often associated with defect states \[^{41}\]. Third, the linewidth is substantially larger than that of the PX, which contrasts with what has been observed for strain-tuned PX states \[^{4}\]. Finally, the energy separation of this band with respect to the PX state (see also Supplementary Fig. 2) and its localization in nanobubble regions are in line with the corresponding observations for single-photon emitter states at cryogenic temperatures in bare 1L-WSe\(_2\) (refs. 11,18) and 1L-WSe\(_2\) the corresponding observations for single-photon emitter states at Fig. 2) and its localization in nanobubble regions are in line with the experimental data, the measured LX energy was plotted against the low-energy emission is isolated in the nanobubble periphery. The calculated confinement potentials correspond remarkably well with the nanoscale spatial distribution of the measured LX energies (Fig. 3d; see the Supplementary Information for fitting details). This correspondence is further in direct accordance with the experimental spectra in Fig. 2b, which shows that the low-energy emission is isolated in the nanobubble periphery. To demonstrate the correlation between the theoretical predictions and experimental data, the measured LX energy was plotted against the predicted confinement potential at the corresponding region of the nanobubble (Fig. 3e; see the Supplementary Information for analysis details). Around the periphery of the nanobubble, a strong correlation between LX energy and the depth of the confinement potential is observed: regions of stronger confinement correspond to lower LX energy. In contrast, in the central region, very little correlation of energy with confinement potential is observed, which suggests a lack of strongly confined excitons in that area (masks for each of these regions are shown in Supplementary Fig. 6). This different behaviour may indicate a more general exciton tunnelling effect in the central region \[^{4}\], whereas the periphery is dominated by highly confined states.

**Influence of defects**

The correspondence between the theoretical analysis of the strain and resulting electronic states within the nanobubble and our nano-optical dataset presented in Fig. 3 strongly suggests that the experimentally observed localized states are the predicted quantum dot-like states \[^{27}\]. In principle, point defects in the 1L-WSe\(_2\) lattice can also localize excitons in a similarly inhomogeneous way. To better elucidate the potential role of defects, we repeated our nanobubble photoluminescence mapping and theoretical calculations in high-quality flux-grown 1L-WSe\(_2\), which has been shown to have defect densities approximately two orders of magnitude lower than commercially grown crystals, providing an average spacing between defects on the order of our nano-optical resolution \[^{24}\]. As shown in detail in the Supplementary Information, every nanobubble...
identified in this higher-quality material exhibits similar LX emission to that of the commercial material (see Supplementary Fig. 1 and the corresponding discussion). More specifically, the occurrence of the LX emission band in the nanobubbles does not depend on the defect density in the ranges probed here.

In Fig. 4, we provide a collage of four nanobubbles in the monolayer area of the high-quality (that is, flux-grown) 1L-WSe$_2$. Figure 4a,b shows the measured AFM topography images of the four nanobubbles and their corresponding spatial distributions of LX emission energies, respectively. Here, the nanophotoluminescence measurements were performed with optical excitation at 785 nm, which is below the energy of the PX and enhances the contrast between the LX and PX states, allowing the LX states to be observed with a greater signal-to-noise ratio (see the Supplementary Information). Figure 4c–e show the calculated confinement potentials, overlap of the electron–hole wave functions and the predicted shifts in photoluminescence emission energies, respectively. As with the nanobubble shown in Fig. 3b, each nanobubble in the flux-grown 1L-WSe$_2$ exhibits lower-energy emission at the nanobubble periphery. This peripheral spatial distribution of low-energy states is replicated in the predicted confinement potentials and electron–hole wave-function overlap shown in Fig. 4c,d, respectively. Finally, the predicted photoluminescence energy shifts and corresponding spatial distributions shown in Fig. 4e agree well with the measured LX emission energies presented in Fig. 4b. Considering the challenges of room-temperature hyperspectral imaging on the 10–20-nm scale, the limitation of the topographical maps in Fig. 4a to a resolution of ~15 nm, as well as the complexities of directly incorporating these measurements into a feasible atomistic model (for details, see the Supplementary Information), the agreement between experiment and theory is particularly remarkable.

The similarities between Figs. 3 and 4, despite dramatically different defect densities, suggest that the LX emission distribution in nanobubbles is not substantially determined by atomic defects in the lattice. As noted above, because there is on average approximately one defect in every 15 nm $\times$ 15 nm in flux-grown material, which is close to the spatial resolution of the nano-optical probe, major defect-associated optical changes would be resolvable. Although defects may still play a role in the emission, the implication here is that the primary effect in terms of the nanoscale spatial distribution and the creation of quantum dot-like states is the local strain profile, with localized regions of maximum strain occurring at locations around the edge of nanobubbles. However, it is certainly possible that defects play a role in, for example, the further localization or the exact distribution of wrinkles on the atomic scale. Such ångström-level effects are beyond the resolution of our current nano-optical probes, which use AFM tips with radii of curvature ranging from ~15 to ~40 nm. Future correlations with, for example, atomic-resolution AFM or atomic-resolution transmission electron microscopy or combined cathodoluminescence and electron

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**Fig. 3** | Comparison of atomistic theory with experimental data. a, Calculated carrier confinement potential for the nanobubble topography shown in the inset of Fig. 2a. The solid lines represent topographic contours based on the AFM measurement. b, Corresponding values of the surface normal deviation, defined as the average angle, $\alpha$, between normal vectors at neighbouring unit cells, obtained from relaxed atomic positions, showing wrinkling of the lattice. c, Map of the shear component of the strain tensor, originating from local wrinkling of the lattice. The positive values indicate larger atomic distances leading to a local reduction of the bandgap. d, Spatial map of the LX emission energy of the nanophotoluminescence data shown in Fig. 2. e, Correlation between the local confinement potentials shown in a and the LX emission energies shown in d. The data points are separated into points at the centre of the nanobubble (red triangles) and points at the periphery of the nanobubble (blue diamonds). All scale bars, 50 nm. The theoretical calculations with atomic resolution are scaled up by a factor of five (see the Supplementary Information).
Fig. 4 | Comparison of experiment and theory for four nanobubbles in 1L-WSe₂ with a low concentration of defects. a, b. AFM topography images (a) and nanophotoluminescence emission energies (b) of the LX state, respectively. The images in a reveal the heights of the nanobubbles. The insets in b show the integrated nanophotoluminescence intensity after low-pass energy filtering to isolate the LX emission. c. Theoretical confinement potentials obtained from the displaced atomic positions derived from nanobubble strain calculations⁴⁶,⁴⁷ and Harrison’s rule⁴⁸. d, e. Electron-hole wave-function overlap (d) and predicted photoluminescence energy shifts (e) of the nanobubbles, respectively. The solid lines in c–e represent the topographic contours of the AFM measurements shown in a. All scale bars, 50 nm. The theoretical calculations with atomic resolution are scaled up by a factor of five (see the Supplementary Information). For the nano-optical data in b, the integration time per pixel is 200 ms, and the pixel size is 20 x 20 nm².
diffraction measurements, as recently demonstrated with single quantum emitters in h-BN (ref. 45), may enable these effects to be mapped on the atomic scale, providing the ultimate picture of localized states in 2D monolayer semiconductors.

Conclusion

By using nano-optical techniques, strain-localized exciton states within single nanobubbles of 1L-WSe₂ have been observed at room temperature with localization lengths of less than 50 nm that are markedly smaller than the nanobubble itself. In general, the spatial distribution of these low-energy states forms a doughnut-like pattern around the periphery of the nanobubble, surrounding a region of higher-energy states at the centre, which is consistent with previous theoretical predictions of atomic-scale strain effects. By integrating the experimentally determined topography with this atomistic model, the experimental results are qualitatively replicated by the theoretical model, establishing the first robust experiment-theory connection for the formation of strain-induced quantum-dot states in monolayer TMD semiconductors. Furthermore, these findings were reproduced in flux-grown 1L-WSe₂ with orders-of-magnitude lower defect densities, implying that the nanoscale localization is primarily influenced by strain and not crystalline defects. Our results show that LX states accessed with nano-optical techniques remain localized at room temperature, leading to compelling potential applications in practical strain-engineered optoelectronic and quantum optical architectures.

Online content

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Data availability
The data that support the plots within this paper and other findings of this study are available from the corresponding authors upon reasonable request.

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Author contributions
P.J.S., N.J.B. and T.P.D. conceived the nano-optical study. Experimental measurements were conducted by T.P.D., E.Y., N.J.B. and A.K. Samples for these measurements were prepared by O.A., J.A., E.Y., A.G., D.A.R., A.N.P. and J.C.H. K.W. and T.T. provided critical materials for the preparation of these samples. The experimental data were analysed by T.P.D., N.J.B. and P.J.S. with important contributions from J.W.K. Theoretical calculations were carried out by C.C., M.F. and F.J. All authors contributed to the preparation of the manuscript.

Competing interests
The authors declare no competing interests.

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