THE STRUCTURE OF PRE-TRANSITIONAL PROTOPLANETARY DISKS. I.
RADIA TIVE TRANSFER MODELING OF THE DISK+CAVITY IN THE PDS 70 SYSTEM*

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Received 2012 June 25; accepted 2012 September 17; published 2012 November 14

ABSTRACT

Through detailed radiative transfer modeling, we present a disk+cavity model to simultaneously explain both the spectral energy distribution (SED) and Subaru H-band polarized light imaging for the pre-transitional protoplanetary disk PDS 70. In particular, we are able to match not only the radial dependence but also the absolute scale of the surface brightness of the scattered light. Our disk model has a cavity 65 AU in radius, which is heavily depleted of sub-micron-sized dust grains, and a small residual inner disk that produces a weak but still optically thick near-IR excess in the SED. To explain the contrast of the cavity’s edge in the Subaru image, a factor of ~1000 depletion for the sub-micron-sized dust inside the cavity is required. The total dust mass of the disk may be on the order of $10^{-4} M_{\odot}$, only weakly constrained due to the lack of long-wavelength observations and the uncertainties in the dust model. The scale height of the sub-micron-sized dust is ~6 AU at the cavity edge, and the cavity wall is optically thick in the vertical direction at H-band. PDS 70 is not a member of the class of (pre-)transitional disks identified by Dong et al., whose members only show evidence of the cavity in the millimeter-size dust but not the sub-micron-sized dust in resolved images. The two classes of (pre-)transitional disks may form through different mechanisms, or they may simply be at different evolution stages in the disk-clearing process.

Key words: circumstellar matter – protoplanetary disks – radiative transfer – stars: individual (PDS 70) – stars: pre-main sequence

Online-only material: color figures

1. INTRODUCTION

Recent years have witnessed a rising interest in a special kind of protoplanetary disk in which a giant central cavity is present and reveals itself in the spectral energy distribution (SED; e.g., Strom et al. 1989; Skrutskie et al. 1990; Calvet et al. 2005; Furlan et al. 2006; Espaillat et al. 2007a, 2007b, 2008), or in submillimeter (sub-mm) interferometry observations (e.g., Pietu et al. 2006; Hughes et al. 2007, 2009; Brown et al. 2009; Isella et al. 2010, 2012; Andrews et al. 2011, 2012; Mathews et al. 2012; Cieza et al. 2012a). Depending on whether a small residual optically thick inner disk is left at the center, these objects could be classified into two categories—pre-transitional disks (with an optically thick residual inner disk; Espaillat et al. 2010) and transitional disks (without an optically thick residual inner disk; Espaillat et al. 2007b). Studying these objects at
multiple wavelengths is of great interest because the inner disk clearing process may be a signpost of planet formation and disk evolution in general (Zhu et al. 2011; Williams & Cieza 2011; Dodson-Robinson & Salyk 2011; Birnstiel et al. 2012; Cieza et al. 2012b).

Thus far, the study of (pre-)transitional disks was done primarily via measurements of the SED and resolved images at sub-mm wavelengths. More recently, direct imaging in the optical to near-infrared (NIR) started playing a crucial role. Protoplanetary disks usually have dust grains with sizes ranging from submicron (called small dust in this study), similar to the pristine interstellar medium (ISM) dust, to mm or larger (big dust), forming as a result of grain growth and coagulation (Dullemond & Dominik 2005; Birnstiel et al. 2012). The SED of a disk is degenerate with many disk parameters since it is spatially integrated over the entire disk. Resolved images at the sub-mm level, on the other hand, provide more detailed information, but they are only sensitive to the distribution of big dust due to its dominance in opacity at these wavelengths. Using eight-meter-class ground-based telescopes equipped with adaptive optics and/or coronagraph systems, direct imaging at optical to NIR wavelengths provides resolved disk maps with high spatial resolution (∼0′′.06) and a small inner working angle (∼0′′.2). These maps are directly related to the distribution of small dust.

An ongoing survey scale project, the Strategic Explorations of Exoplanets and Disks with Subaru (SEEDS; Tamura 2009), is directly imaging a large sample of protoplanetary disks at NIR (J, H, and K) bands in a systematic way, using the High-Contrast Coronographic Imager for Adaptive Optics (HiCIAO; Suzuki et al. 2010). SEEDS disk observations specialize in taking polarized intensity (PI = \( \sqrt{Q^2 + U^2} \)) where Q and U are components in the Stokes vector) disk images, which greatly enhances our ability to probe disk structure (especially in the inner part), by utilizing the fact that the central source is usually not polarized, so that the stellar residual in PI images is much smaller than in full intensity (FI) images (Perrin et al. 2004; Hinkley et al. 2009; Quanz et al. 2011). The signal in NIR imaging usually comes from the scattering of starlight off the surface of the disk since dust at separations of ∼10 AU in the disk is not hot enough to contribute significantly at NIR wavelengths. A number of protoplanetary disks have been studied in SEEDS (LkCa 15, Thalmann et al. 2010; AB Aur, Hashimoto et al. 2011; SAO 206462, Muto et al. 2012; MWC 480, Kusakabe et al. 2012; and UX Tau A, Tani et al. 2012), and more are on their way. Recently, Dong et al. (2012) pointed out that in a large sample of (pre-)transitional disks whose central cavity has been confirmed in resolved images at sub-mm, SEEDS did not find the cavities in their NIR images. This discrepancy has been interpreted as evidence for the cavity’s existence only in big dust, with the small dust having a continuous distribution in surface density from the outer disk all the way to the inner working angle of SEEDS (∼0′′.1–0′′.15, or about ∼15–20 AU in Taurus). This may be explained by the dust filtration model proposed by Paardekooper & Mellema (2006), Rice et al. (2006), and Zhu et al. (2012). In their model, the pressure bump in the disk acts like a filter, which filters the small dust through but traps the big dust, resulting in the depletion of big dust inside the cavity.

In this article, we study the structure of the pre-transitional disk PDS 70 using detailed radiative transfer modeling, following the observational paper by Hashimoto et al. (2012). PDS 70 is a K5-type weak-lined T Tauri star located at the Centaurus star-forming region (coordinate 14h08m10.15s, −41d23m52.5s), with an age < 10 Myr and a distance estimated to be ∼140 pc (Gregorio-Hetem & Hetem 2002; Riaud et al. 2006; Metchev et al. 2004; Hashimoto et al. 2012). The photometry of this star has been measured at multiple wavelengths (e.g., Metchev et al. 2004; Kessler-Silacci et al. 2005), and its disk has been detected in scattered light by Very Large Telescope (VLT) K-band imaging (Riaud et al. 2006). SEEDS directly imaged PDS 70 in the H-band using the polarization differential imaging (PDI) mode on 2012 February 27. The Subaru observation and the data reduction were described in detail in Hashimoto et al. (2012, which also presented the Gemini L′-band imaging).

Unlike most previous objects of this type, the cavity in PDS 70 is first detected by SEEDS NIR imaging. And unlike the objects in Dong et al. (2012), it indeed has a cavity in the small dust, which also contradicts the predictions in various dust filtration models mentioned above.

Radiative transfer modeling of (pre-)transitional disks has been mostly used to fit the SED and sub-mm observations in the past (e.g., Hughes et al. 2009; Andrews et al. 2011, 2012; Mathews et al. 2012). Here, we demonstrate the power of modeling in the NIR by producing synthetic disk images in scattered light and comparing them with observations. Sensitive to dust at different sizes and locations, SED, sub-mm observations, and NIR imaging can be used to probe the disk structure in different and complementary ways. Particularly, NIR imaging can provide effective constraints on the scale height of the disk, and the depletion factor for the small dust inside the cavity, neither of which is well constrained using the other two types of observations (Andrews et al. 2011; Dong et al. 2012).

This paper is the first in a series in which we study the structures of (pre-)transitional disks by modeling SEEDS NIR imaging data and observations at other wavelengths. The paper is arranged in the following way. In Section 2 we introduce the method for our radiative transfer modeling. The fiducial model of PDS 70 is presented in Section 3, where we simultaneously fit both its SED and its scattered light image. The constraints on various disk+cavity parameters from current observations are discussed in Section 4, where we focus on the ones that are directly probed by NIR imaging and are important in revealing the disk evolution. We discuss the possible formation mechanisms of (pre-)transitional disks in Section 5, followed by a short summary in Section 6.

2. RADIATIVE TRANSFER MODELING

We use the Monte Carlo radiative transfer (MCRT) code developed by B. A. Whitney et al. (2012, in preparation; see also Whitney et al. 2003a, 2003b; Robitaille et al. 2006) to model the SED and SEEDS H-band PI imaging of PDS 70. The SED data collected from literature, the SEEDS observations, and its data reduction are described in detail in Hashimoto et al. (2012). MCRT simulations are run with \( 4 \times 10^7 \) photons for high-signal-to-noise images. Disk setup is largely adopted from the model in Dong et al. (2012), which is briefly summarized here. We construct an axisymmetric disk 200 AU in radius on a 600 × 200 grid in spherical coordinates (\( R, \theta \)), where \( R \) is the radial component and \( \theta \) is the poloidal component (\( \theta = 0^\circ \) is the disk midplane). We uniformly deplete the central region of the disk to form a cavity with radius \( R_{cav} \), i.e., we reduce the dust surface density by a constant factor within this radius. The disk is assumed to be at ∼140 pc. The inner radius of the disk (within the cavity) is self-consistently determined by dust sublimation (\( T_{sub} \sim 1600 \) K). The accretion rate of PDS 70 is
considered to be very low, since the object has been identified as a weak-line T Tauri object with an Hα equivalent width of 2 Å (Gregorio-Hetem & Hetem 2002). For the central source, we assume a pre-main-sequence star of K5 spectral type, radius of 1.35 \( R_\odot \), mass of 1.0 \( M_\odot \), and temperature of 4500 K, as suggested by Gregorio-Hetem & Hetem (2002). The surface density \( \Sigma(R) \) in the outer disk is taken as

\[
\Sigma(R) = \frac{R e^{-R/R_c}}{R_c} \text{e}^{-R/R_c}, \quad \text{at } R \geq R_{\text{cav}},
\]

where \( R_c \) is a characteristic scaling length assumed to be 50 AU, and the normalization \( \Sigma_0 \) is determined by the total dust mass of the disk \( M_{\text{dust}} \). The choices of the surface density radial profile and \( R_c \) are common in protoplanetary disk modeling (Williams & Cieza 2011; Andrews et al. 2011), and represent a snapshot of a solution for a fully viscous disk with a constant \( \alpha \) parameter (as in the Shakura & Sunyaev 1973 \( \alpha \) disk model) and \( T \propto R^{-1/2} \) (Hartmann et al. 1998). Inside the cavity, the disk is uniformly assumed to be very low, since the object has been identified as a weak-line T Tauri object with an Hα equivalent width of 2 Å (Gregorio-Hetem & Hetem 2002). For the central source, we assume a pre-main-sequence star of K5 spectral type, radius of 1.35 \( R_\odot \), mass of 1.0 \( M_\odot \), and temperature of 4500 K, as suggested by Gregorio-Hetem & Hetem (2002). The surface density \( \Sigma(R) \) in the outer disk is taken as

\[
\Sigma(R) = \delta_{\text{cav}} \Sigma_0 \frac{R e^{-R/R_c}}{R_c} \text{e}^{-R/R_c}, \quad \text{at } R < R_{\text{cav}},
\]

where \( \delta_{\text{cav}} \) is the constant depletion factor (which may be different for different dust populations).

Various grain evolution models predict that the pristine dust grains in the disk coagulate, grow to bigger size, and subsequently settle to the disk midplane (Dullemond & Dominik 2004a, 2004b, 2005). To take this effect into account, we assume a two-component model of dust distribution: a thick disk with small grains (sub-micron size), and a thin disk with large grains (up to \( \sim \)mm size). Below we will use subscripts “b” and “s” for various quantities relating to big and small dust, respectively, and superscripts “o” and “c” to indicate the outer disk and the cavity, respectively (for example, \( \Sigma_{b} \) represents the surface density of the small dust inside the cavity). Both big and small grains are assumed to have a Gaussian density profile in the vertical direction,

\[
\rho(R, z) = \frac{\Sigma(R)}{\sqrt{2\pi h}} \text{e}^{-z^2/2h^2},
\]

where \( h \) is the scale height, with \( h_b \) (scale height of the big dust) assumed to be much smaller than \( h_s \) (scale height of the small dust). We note that the scale heights are provided to the code as input parameters, instead of being self-consistently determined from the disk temperature calculated in the simulations. In our fiducial model shown below, we check this assumption and find that the input is consistent with the output (Section 3). Radially, both scale heights vary with radius as

\[
h \propto R^\beta,
\]

where \( \beta \) is the constant power-law index. Our experiments show that as long as the big dust is settled to the disk midplane (i.e., \( h_b \ll h_s \)), the details of its vertical distribution hardly affect the details of NIR images and SED, while both crucially depend on the spatial distribution of the small dust, as we will show below in Section 4.3.

The total mass of the big dust in the disk is \( f \times M_{\text{dust}} \), where \( f \) is a variable parameter. For the small dust, we assume a size distribution as in the standard ISM dust model from Kim et al. (1994) up to a maximum size of 0.2 \( \mu \text{m} \) (roughly a power-law size distribution \( n(s) \propto s^p \) with power index \( p \sim 3.5 \)). The dust composition is assumed to be 70% mass in silicate and 30% mass in graphite, with the properties for both adopted from Laor & Draine (1993). Preferentially forward scattering (i.e., Mie scattering) is assumed. For the big dust we primarily use Model 2 from Wood et al. (2002; from now on called steep-big-dust), which assumes a power-law size distribution \( n(s) \propto s^p \) with \( p = 3.5 \) up to a maximum size of 1 mm, and a composition of amorphous carbon and astronomical silicates. In Section 4.2 Model 3 from Wood et al. (2002) is also tried (from now on called the flat-big-dust model), whose only difference from the steep-big-dust model is that it assumes \( p = 3.0 \) (a “flatter” size distribution, so more mass is at the large size end). As a consequence, the flat-big-dust model has a lower opacity than the steep-big-dust model at wavelengths \( \lambda \gtrsim 1 \text{ mm} \). The opacity of these dust models is shown in Figure 1.

PDS 70 shows a cavity with radius \( \sim60–70 \text{ AU} \), and the disk is inclined by about 45°–50° (Hashimoto et al. 2012). In our fiducial model shown below we choose 65 AU (\( \sim0.46 \)) and 45° for the two, as they produce a model SED and an image that match observations reasonably well (Section 3). We note that a mild deviation from these “fiducial” values can be tolerated without much difficulty (i.e., \( \pm5 \text{ AU} \) in cavity size and \( \pm5° \) in geometry). These parameters are fixed below to keep the models simple.

We produce \( H \)-band polarized images from MCRT simulations. To obtain realistic images that can be directly compared with SEEDS observations, the raw simulated images are post-processed, as described in detail in Dong et al. (2012). The SEEDS observations of PDS 70 were conducted in PDI mode without a coronagraph (Hashimoto et al. 2012), so that we produce mock images in the same mode in this work. The raw model images of the entire disk+star are convolved by a real \( H \)-band SEEDS point-spread function (PSF). The inner working angle of the images, \( \psi_{\text{in}} \), is assumed to be 0.15 in radius (\( \sim21 \text{ AU} \) at the estimated distance of PDS 70). We measure the surface brightness radial profile (SBRP) of the disk along major and minor axes, by calculating the average surface brightness (SB) of the pixels within \( \pm22.5 \) on each side of the axes at various radial bins 0.05 in width, the same as we measured for the SBRP of the SEEDS PDS 70 image (Hashimoto et al. 2012).

3. THE FIDUCIAL DISK MODEL FOR PDS 70

Here we present a fiducial disk model for PDS 70 to fit all the observations. The disk parameters in this model are listed

![Figure 1. Opacity \( \kappa \) for the dust models used in this study (showing the dust opacity only).](image-url)
in Figure 2. In summary, the disk has a heavily depleted cavity in Table 1, and the surface density of the small dust is plotted in Figures 5(a) and (b). The horizontal dashed line indicates where the vertical optical depth is 1 at 1 μm, representing the peak of the stellar spectra. The vertical optical depth due to the small dust is ~14 at the inner edge of the disk (~0.06 AU) and ~4 at the cavity wall. On the other hand, the gap between the inner rim and the outer disk (i.e., from ~1 AU to R_{cav}) is optically thin to stellar radiation, which justifies the classification of PDS 70 as a pre-transitional disk (Espaillat et al. 2010). The total dust mass M_dust is 3 x 10^{-5} M_⊙, and most of it is in the big dust, with a big-to-small-dust ratio at about 30:1 (i.e., f = 0.97). However, as we will discuss in Section 4.2, the constraints on the big dust are rather weak (including the total amount, its structure, and the big-to-small-dust ratio), given the current data. We assume a scale height power-law index of 1.2 for both dust populations (β_b and β_s), both inside and outside the cavity (indicated by subscripts “c” and “o”), reasonably close to the canonical value ~1.25–1.3 for irradiated disks (Chiang & Goldreich 1997; Hartmann et al. 1998). The gas in the disk is in hydrostatic equilibrium in the vertical direction, so that h_{gas} is set by the vertical temperature profile, through h_{gas} \approx \sqrt{k_b T / \mu} and c_s \approx \sqrt{k_b T / \mu}, where c_s is the sound speed, Ω is the rotational angular velocity, T is the midplane temperature, and μ is the average molecular weight. Various grain settling models predict that the small grains tend to be well coupled with the gas (Dullemond & Dominik 2004b) and as a result the two would share a similar vertical distribution, h_i \sim h_{gas}. The small-dust scale height is 6.0 AU at R_{cav}, both inside the cavity (h_c^{(S)})

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**Figure 2.** Surface-density radial profile of the small dust ρ_s, for models shown in Figures 5(a) and (b). The horizontal dashed line indicates where the vertical optical depth is 1 μm (characteristic wavelength of the stellar radiation). The fiducial model and model SCM1 have vertically optically thick innermost disks, and models SCM3 and SCM4 have optically thin innermost disks, while model SCM2 is on the margin.

(A color version of this figure is available in the online journal.)
and outside the cavity \(h^c\), which corresponds to a midplane temperature of 28.2 K. This value is close to the output from the radiative transfer calculation, 31.8 K. The big-dust scale height inside and outside the cavity \(h^c\) is one-fifth of the value for the small dust.

The model H-band PI images are shown in Figure 3, along with the observed SEEDS image. The SED and SBRP (defined in Section 2) of the image are shown in Figure 4. Our model SED matches the observations very well. For the scattered-light (i.e., cavity edge) are present at closer separation from the center (also \(\psi_{in}\)), where the photon noise is generally larger.

We note that the parameters and geometry of our fiducial model come from an overall consideration of simultaneously fitting the SED, NIR image, and radial profile of the scattered light instead of simply measuring from the image as in Hashimoto et al. (2012). Also, the fiducial model presented here is by no means unique, i.e., the only one that can provide a good fit to all of the observations, because the constraints on some of the disk+gap parameters are rather weak (Section 4).

Finally, we comment on the previous VLT K-band imaging of PDS 70 reported by Riaud et al. (2006) as well as their derived disk model. Observationally, the inclination and position angle found by Riaud et al. (2006) is similar to our results (Hashimoto et al. 2012). However, our Subaru H-band PI images provide far more details and are at a higher quality than the VLT K-band FI images presented by Riaud et al. (2006), which detected the disk in scattered light but did not reveal a clear giant cavity structure, and showed a jet structure that is not present in our observations. Riaud et al. (2006) employed a smooth disk model with a radius larger than 500 AU, and a total dust mass between 0.001 and 0.002 \(M_\odot\) to reproduce the observations, which is one order of magnitude larger than in our fiducial model. The difference is mostly caused by the fact that the inner region is heavily depleted in our models but not in Riaud et al. (2006).
4. CONSTRAINTS ON VARIOUS DISK AND CAVITY PARAMETERS

The fiducial model presented above provides a reasonably good fit to observations, and gives us a basic idea about the disk+cavity structure. In this section, we intend to determine the constraints on some of the parameters from modeling and fitting so that we can understand what these observations are really telling us. In general, disk properties at short wavelengths (i.e., scattered light images and NIR excess in the SED) are sensitive to the spatial distribution of the small dust, while this dependence shifts to the big dust at long wavelengths (i.e., far-IR excess and sub-mm observations), due to the difference in opacity of the two populations (Figure 1). Since there are too many free parameters in our model, it is not realistic to vary every one of them and study their effects. Rather, we narrow our scope to a few key parameters.

1. The ones that are crucial for revealing the evolution of protoplanetary disk, and the formation mechanisms of (pre-)transitional disks. These are the depletion factor of both dust populations, and the total mass of the disk.

2. The ones that can only be effectively constrained by scattered-light images, such as the scale height and depletion factor of the small dust, which has a large degeneracy in SED and sub-mm observations. Since SEEDS virtually opens a new window for systematically studying a large uniform sample of disks using scattered-light images, we intend to provide an example to demonstrate the power of NIR imaging for probing disk structure.

Below, we study the role played by these factors, both in disk SED and scattered-light imaging, by exploring the corresponding parameter space around the fiducial model. We examine the cavity depletion factors for both dust populations (dcb and dcs) in Section 4.1, the total dust mass (Mdust) in Section 4.2, and the scale height of the small dust in the cavity and the outer disk (hc, βc, ho, and βo) in Section 4.3. Models and their parameters in each section are listed and described in the corresponding section of Table 1. For the SED we focus on comparing it with the photometry data, and for the scattered light we only look at the SBRP along the major axis.
the SED only weakly depends on $\delta$, the SBRP plots ((b) and (d)) have the same line types as they have in the SED plots ((a) and (c)). The results show that as long as the innermost disk is vertically optically thick, the SED only weakly depends on $\delta_c$; once $\delta_c$ drops enough for the innermost disk to be optically thin, the NIR excess becomes sensitive to the amount of small dust there. The inner disk is brighter and the outer disk is dimmer in scattered light for a bigger $\delta_c$. On the other hand, both the SED and scattered light image are almost independent of $\delta_b$.

(A color version of this figure is available in the online journal.)

4.1. The Depletion Factor Inside the Cavity

The cavity depletion factor of the small dust $\delta_c$ could be constrained by both the SED and the scattered-light image. Qualitatively, depleting the cavity more in the small dust reduces the short-wavelength excess on the SED, and enhances the contrast of the cavity in the image. Technically, the SED is more sensitive to the depletion in the inner part of the cavity (at AU scales) since most of the short-wavelength excess is produced there, while the scattered light images are more sensitive to the depletion in the outer part of the cavity where the contrast of the cavity edge is produced (the inner part of the disk within $\psi_m$ cannot be directly accessed in imaging observations). As a result, the two could in principle be constrained “independently.” However, to simplify our discussion, we use a uniform, instead of a radius-dependent, $\delta_c$ (and $\delta_b$), and note that this treatment does not affect our conclusion (see Dong et al. 2012 for a discussion on radius-dependent $\delta_c$).

Figure 5(a) shows the effect of $\delta_c$ on the SED ($\delta_b$ is locked to $\delta_c$, but this hardly affects our result, as shown below). The surface density profile of the small dust ($\Sigma_c$) for these models is plotted in Figure 2. Whether 2–20 $\mu$m excess strongly correlates with $\delta_c$, sensitively depends on whether the innermost disk (at AU scales) is optically thick or not (characterized at the peak of the stellar spectra, $\sim 1$ $\mu$m). When the innermost disk is optically thick (pre-transitional disks), the IR excess is almost independent of the amount of small dust inside the cavity (the fiducial model and model SCM1). However, once $\Sigma_c$ at the inner disk decreases below the optically thick limit and enters the transitional disk phase, the 2–20 $\mu$m excess drops significantly as a result of the decreasing $\delta_c$ (models SCM2 to SCM4). If the inner disk is completely depleted (SCM4), excess below $\sim 10$ $\mu$m disappears, and a nearly blackbody thermal component peaking at $\sim 40$ $\mu$m clearly reveals itself, which arises from the cavity wall. Though not as isolated as in SCM4, this wall emission signal is prominent in all models. Comparing with observations, we conclude that the NIR excess in PDS 70 is consistent with an optically thick innermost disk, which requires $\delta_c > 10^{-4}$.

Figure 5(b) shows the SBRP of the convolved image for the above models. As expected, decreasing $\delta_c$ makes the inner disk fainter. Moreover, the blocking effect due to the inner disk is reduced, so that a larger area of the cavity wall is illuminated, and more starlight (rays closer to the disk midplane) reaches the wall and outer disk, increasing their brightness in scattered light. Similarly, increasing $\delta_c$ tends to wipe out the signal of the
cavity in scattered light (i.e., the bump at \( \sim 0.05 \)), and makes the SBP smoother. The observed SEEDS SBP is broadly consistent with \( \delta_{\text{cav},s} \sim 10^{-3} \), while a modest deviation (i.e., a factor of \( \sim 3 \)) around this value could be tolerated without too much difficulty.

On the other hand, the cavity depletion factor of the big dust could only be directly constrained by sub-mm properties of the disk (Andrews et al. 2011; Cieza et al. 2012a; Isella et al. 2012; Mathews et al. 2012). Figures 5(c) and (d) show that changing \( \delta_{\text{cav},b} \) hardly affects either the disk SED or NIR image (we fix the small dust to isolate the effect, i.e., the depletion factor for the small-dust component inside the cavity is fixed to \( \delta_{\text{cav},s} \sim 10^{-3} \) in all the models plotted here). We leave the constraint on \( \delta_{\text{cav},b} \) for future sub-mm observations.

In conclusion, \( \delta_{\text{cav},s} \sim 10^{-3} \) is needed for the models to be consistent with both the SED and the SEEDS images. The constraint is modest, roughly half a decade around the fiducial value.

4.2. The Total Dust Mass of the Disk

The total dust mass of the disk \( M_{\text{dust}} \) is a quantity that is crucial for a thorough understanding of disk evolution. In general, \( M_{\text{dust}} \) is determined by the big dust since it dominates in mass over the small dust, and for (pre-)transitional disks like PDS 70, most of the mass resides in the outer disk since the inner disk is heavily depleted. \( M_{\text{dust}} \) is best constrained by sub-mm or mm observations because the disk is usually optically thin at these wavelengths, so \( M_{\text{dust}} \) can be calculated from the measured sub-mm or mm flux, assuming a dust temperature and opacity model (i.e., Equations (2) and (3) in Williams & Cieza 2011). However, the total disk mass derived in this way normally contains large uncertainties, introduced by poorly unconstrained dust opacity and gas-to-dust ratio, if converting dust mass to total gas mass (Panić et al. 2008).

For PDS 70, we constrain the disk mass using the longest-wavelength photometric data point available, which is at \( 160 \mu m \). Our models are all vertically optically thin (sometimes only marginally) at \( 160 \mu m \) given our dust models. Models BOM1 and BOM2 (both have the steep-big-dust model) in Figure 6(a) show the SED dependence on \( M_{\text{dust}} \). While the fiducial choice of \( M_{\text{dust}} = 3 \times 10^{-5} \, M_\odot \) agrees well with the observed photometry at \( 160 \mu m \), a factor of \( \sim 3 \) deviation in \( M_{\text{dust}} \) from this value leads to a factor of \( \sim 2 \) difference in \( 160 \mu m \) flux, while the SED at wavelengths shorter than \( 100 \mu m \) is largely unchanged.

One issue that deserves special attention in this exercise of \( M_{\text{dust}} \) determination is the effect of the big dust model. Since the long-wavelength flux in the optically thin regime is proportional to the opacity of the dust at that wavelength, changing the type of the big dust model has a direct impact on \( M_{\text{dust}} \). Figure 6 shows two examples in which the flat-big-dust model is assumed instead of the steep-big-dust model. As mentioned in Section 2 and shown in Figure 1, the flat-big dust has a flatter size distribution, resulting in smaller opacity at wavelengths shorter than \( \sim 1 \, mm \). Model BOM3-flat has an identical set of disk parameters to the fiducial model. While the difference in SED between the two models is negligible at \( \lambda \lesssim 100 \mu m \), the IR excess in BOM3-flat sharply drops below the fiducial model at longer wavelengths. To pull the \( 160 \mu m \) flux back to the observed value, the disk mass needs to rise to \( 1.5 \times 10^{-4} \, M_\odot \), as in model BOM4-flat. On the other hand, since all the BOM models have an identical spatial distribution for the small dust, their scattered-light images are almost the same, as shown in Figure 6(b).

We conclude that the total dust mass of PDS 70 \( M_{\text{dust}} \) is probably on the order of \( 10^{-4} \, M_\odot \), depending on the dust model for the big dust: a flatter grain size distribution for the big dust corresponds to a larger \( M_{\text{dust}} \). Observations at longer wavelengths are needed to distinguish different big dust models and to pin down the disk mass.

4.3. The Scale Height of the Small Dust

The scale height of the small dust \( h_s \), which dominates the absorption of starlight, is a central quantity involved in determining almost all of the observable properties of the disk.\(^{24}\)

\(^{24}\) The big dust is generally considered to have settled to the disk midplane, and its opacity at the peak of the stellar spectrum is much lower than that of the small dust. As a result, the detailed vertical distribution of the big dust does not have a prominent effect on the SED and the scattered-light image.
Scale height and total mass of the small dust determine the shape of the disk surface, on which the stellar radiation is absorbed and re-emitted at longer wavelengths. Part of that emission escapes and gets observed, and part of it goes deeper into the disk interior to heat the disk, subsequently being reprocessed into disk emission at even longer wavelengths. Despite its importance, unfortunately very few types of observations can determine $h_s$ in a straightforward manner (see the example in Muto et al. 2012, where the shape of the spiral waves in SAO 206462 is used to estimate $h_s$). However, scattered light is an excellent tool for probing $h_s$, since its signal comes right from the disk scattering surface, which is directly determined by $h_s$.

In this section, we use several models to investigate the effects of $h_s$ on the disk SED and the NIR image. Figures 7(a) and (b) show the result of models SOS1–4, in which the scale height at $h_s$ is varied. We find that the radial dependence of $h_s$ has a minimal effect on both the SED and the scattered-light image (models SOS1 and SOS2), while the overall scale of $h_s$ plays a prominent role in both the SED and the NIR image. A much larger area of the cavity wall in model SOS4, whose $h_s$ is 1.5 times the fiducial value, is directly exposed to stellar radiation, due to its larger height. As a result, its SED is a factor of $\sim 2$ higher at the peak of the wall emission ($\sim 40 \mu$m) compared with the fiducial model and the observed SED, and the cavity edge is $\sim 50\%$ brighter.

Figures 7(c) and (d) show the effect of $h_s$ inside the cavity ($h_s$, model SCS1–4). Similar to $h_s$, the absolute scale of the scale height plays a bigger role than its radial dependence. Models SCS1 and SCS3, both having a thinner innermost disk, produce less NIR excess and slightly less scattered light from the inner disk. Also, since less starlight is blocked by the innermost disk and more of it reaches the cavity edge, the two have more mid-ZIR excess around $40 \mu$m and a slightly brighter cavity edge in the $H$ band. On the contrary, model SCS4 has a thicker disk inside the cavity, resulting in more short-wavelength excess and less long-wavelength excess, due to less starlight reaching the outer disk. Its inner disk is also brighter and its outer disk is fainter in the scattered-light image. In general, the effect of $h_s$ on the SED is modest, echoing the finding in Section 4.1 that once the inner disk becomes optically thick the NIR excess is insensitive to the distribution of small dust.

In sum, the scale height of the small dust at $R_{cav}$, $h/R \sim 0.09$, is relatively well determined by both the SED and the scattered-light image (note that this value is consistent with the output temperature from radiative transfer calculation; Section 3). On the other hand, the constraint on the radial dependence of $h_s$ is weaker, as a broad range of $\beta$ from 1.15 to 1.25 (both inside and outside the cavity) in the parameter space we explored here does not contradict the observations.
5. INDICATION ON THE FORMATION OF (PRE-)TRANSITIONAL DISKS

PDS 70 is a special pre-transitional disk in the sense that unlike most of its previous cousins, whose cavities were usually first inferred from the shape of the SED and then confirmed by resolved sub-mm images, the cavity in PDS 70 was first found in the SEEDS scattered-light image (see also Honda et al. 2010 for AB Aur). Follow-up interferometer observations at long wavelengths, for example using the Submillimeter Array (SMA) or the Atacama Large Millimeter Array (ALMA), are needed to check the existence of the cavity in the big dust. If it is indeed confirmed, then this object will represent a class of (pre-)transitional disks that are in clear contrast to the ones discussed in Dong et al. (2012). Dong et al. (2012) reported the discovery of a class of (pre-)transitional disks, whose cavities are confirmed using the SMA interferometer but are not seen in SEEDS scattered-light images, despite the fact that the inner working angle of the SEEDS images is small enough to reveal these cavities (if they exist). In addition, observations at long wavelengths will help to determine the total dust mass of the disk, which is currently poorly contained to be \( \sim 10^{-4} M_\odot \). Due to the lack of long-wavelength observations and the uncertainties in the dust model.

There are only a handful of objects whose cavities have been revealed in resolved images at multiple wavelengths covering a broad range. A special group of them are circumbinary disks (with the secondary being a stellar or sub-stellar object), such as GG Tau. The cavity in GG Tau has been found in the optical (Krist et al. 2005), NIR (Itoh et al. 2002), mm (Piétu et al. 2011), and CO line emission (Guilloteau et al. 1999), all at roughly the same position. The formation mechanism of cavities in circumbinary systems has been studied by Artymowicz & Lubow (1994). It is thought that the gravitational interaction between the massive (sub-)stellar secondary and the disk naturally truncates the disk and the cavity formed in this way exists in all disk components, including gas and dust at different sizes. The imaging in the \( L' \) band shown in Hashimoto et al. (2012) has put an upper limit of \( \sim 30-50 M_J \) for any possible companion at the radii of interest (assuming their age of the system and the (sub-)stellar object evolution model), which rules out the possibility of a stellar-mass companion. Future observations with better sensitivity and contrast performance are needed to answer whether a sub-stellar companion exists (i.e., a brown dwarf). On the other hand, the possibility of a gap opening due to multiple Jovian planets has been explored by Zhu et al. (2011) and Dodson-Robinson & Salyk (2011). The general picture in that scenario, that a wide, deep gap is opened while a small optically thick innermost disk is left at the center, qualitatively agrees with the observations of PDS 70, though it is generally harder to directly image Jovian planet(s) in a bright protoplanetary disk.

The dust filtration model has been proposed by Paardekooper & Mellema (2006) and Rice et al. (2006), in which the pressure maximum at the planet-induced gap outer edge acts like a filter, so that big grains are trapped but small grains penetrate into the inner disk. As a result, it is predicted that the cavity must be depleted of big dust grains, but with a significant amount of small dust particles left inside. PDS 70, with its heavily depleted cavity in small dust grains, is inconsistent with the dust filtration model alone. On the other hand, Zhu et al. (2012) proposed a dust filtration+dust growth model as a possible explanation for the transitional disk GM Aur. The grain growth and coagulation at the innermost disk may turn the small grains into big grains, resulting in a (pre-)transitional-disk-like NIR excess (see also Birnstiel et al. 2012). The dust and gas components of the disk are decoupled in their model and provide an explanation for both the moderate accretion rate of GM Aur and its strong NIR deficit. Furthermore, this dust-size-dependent filtration model may explain the different gap properties between NIR and sub-mm reported in Dong et al. (2012). However, unlike GM Aur, PDS 70 is a WTTS, suggesting a very low gas-accretion rate. Together with the clear cavity revealed in the NIR imaging, a consistent picture emerges for PDS 70 that both the small dust and the gas are heavily depleted at the inner disk, and there is no clear evidence for decoupling between the two. On the other hand, without sub-mm/mm observations, we do not know whether or not small and big dust are decoupled.

Nevertheless, following the dust filtration+dust growth model, we can still provide an explanation for the PDS 70 class of objects. They may start as systems modeled in Dong et al. (2012), which do have a significant amount of small dust inside the cavity and without the NIR cavity being present. Later on, grain growth and coagulation, which happen at a faster rate in the inner disk due to high density and short dynamical timescale, gradually spread over the entire inner disk, eventually leading to the formation of a small-dust cavity. If this scenario is true, then these two kinds of (pre-)transitional disks are simply at different evolutionary stages in their cavity-clearing process—the ones in Dong et al. (2012) are at an early stage, whereas PDS 70 is at a later stage. Consequently, we should expect to see a statistical “time delay” between the two types of objects. This time delay is partly supported by the facts that PDS 70 is a WTTS and that it is a relatively old system. This argument can be tested further if a large sample of objects in both categories with accurate age determination could be provided by future observations. Also, another piece of possible strong evidence in favor of this scenario would be the detection of objects in the intermediate phase of this process, such as (1) objects with a “partially cleared” small-dust cavity whose edge is between the center and the edge of the big-dust cavity, or (2) objects with a radius-dependent cavity depletion factor for the small dust (probably smaller in the inner disk), showing that the clearing process is moving outward. Furthermore, the by-product of grain growth and coagulation—a slight enhancement of the big-dust signal inside the cavity at a later stage—may be observable using a sub-mm interferometer with very high sensitivity, such as ALMA (Dong et al. 2012).

6. SUMMARY

We carry out a study of the disk+cavity structure for PDS 70, using radiative transfer modeling to fit both the observed SED and the SEEDS polarized scattered-light image in the \( H \) band of this object. Good agreement with observations is achieved by our models. The disk has a giant cavity at its center with a radius of 65 AU. The small dust (sub-micron-sized) inside the cavity is depleted by a factor of \( \sim 1000 \), resulting in a low-density but still vertically optically thick innermost disk, producing a pre-transitional-disk-like NIR excess. This heavy depletion is also needed to explain the surface-density depression inferred from the scattered-light image. The scale height of the small dust at the cavity edge is \( \sim 6 \) AU, constrained by both the SED and the image, which is consistent with the output midplane temperature of the disk. On the other hand, the total mass of the disk can be estimated only crudely to be on the order of \( 10^{-4} M_\odot \).
the cavity depletion factor for the big (mm-sized) dust, would be determined by future observations at longer wavelengths.

Unlike most previously classified (pre-)transitional disks, the cavity in PDS 70 is identified in NIR scattered light, which only informs us of the depletion in the small dust but tells us little about the spatial distribution of the big dust. Pending the confirmation of the cavity in the big dust by radio interferometer observations, PDS 70 may be a prototype of its group, in which the cavity is seen in both dust populations. It is in clear contrast with the (pre-)transitional disks discussed in Dong et al. (2012), where the small-dust cavities were not seen outside the inner working angle of the scattered-light images. The (pre-)transitional disks with or without an NIR cavity may be formed through different mechanisms (i.e., binary versus planets or grain growth), or they may just be caught at a different evolutionary stage in their disk clearing process. Observational predictions for both mechanisms are made in Section 5, and more objects with multi-wavelength observations in both categories are needed to reveal the nature of (pre-)transitional disks.

R.D. thanks Edwin Bergin, Tilman Birnstiel, Brendan Bowler, Nuria Calvet, L. Ilseeedore Cleeves, Bruce Draine, Catherine Espaillat, Lee Hartmann, Shu-ichiro Inutsuka, Andrea Isella, James Owen, Thomas P. Robitaille, Fredrik Windmark, and Yanqin Wu for useful discussions. The authors are also grateful to the anonymous referee who helped improve the manuscript.

REFERENCES

Andrews, S. M., Wilner, D. J., Hughes, A. M., et al. 2009, ApJ, 698, 131
Andrews, S. M., Wilner, D. J., Calvet, N., et al. 2007, ApJ, 664, 536
Espaillat, C., Natta, A., Wilner, D., Carpenter, J. M., & Testi, L. 2010, ApJ, 725, 1735
Isella, A., Pérez, L. M., & Carpenter, J. M. 2012, ApJ, 747, 136
Itoh, Y., Tamura, M., Hayashi, S. S., et al. 2002, PASJ, 54, 963
Kessler-Silacci, J. E., Hillenbrand, L. A., Blake, G. A., & Meyer, M. R. 2005, ApJ, 622, 404
Kim, S.-H., Martin, P. G., & Hendry, P. D. 1994, ApJ, 422, 164
Krist, J. E., Stapelfeldt, K. R., Golimowski, D. A., et al. 2005, AJ, 130, 2778
Kusakabe, N., Grady, C. A., Sitko, M. L., et al. 2012, ApJ, 753, 153
Laor, A., & Draine, B. T. 1993, ApJ, 402, 441
Matthews, G. S., Williams, J. P., & Ménard, F. 2012, ApJ, 753, 59
Metchev, S. A., Hillenbrand, L. A., & Meyer, M. R. 2004, ApJ, 600, 435
Muto, T., Grady, C. A., Hashimoto, J., et al. 2012, ApJ, 748, 122
Paardekooper, S.-J., & Mellema, G. 2006, A&A, 453, 1129
Panić, O., Hogerheijde, M. R., Wilner, D. J., & Qi, C. 2008, A&A, 491, 219
Perrin, M. D., Graham, J. R., Kalas, P., et al. 2004, Science, 303, 1345
Pietu, V., Dutrey, A., Guillostre, S., Chapillon, E., & Pety, J. 2006, A&A, 460, L43
Pietu, V., Gaeth, F., Hily-Blant, P., Schuster, K.-F., & Pety, J. 2011, A&A, 528, A81
Quanz, S. P., Schmid, H. M., Geisler, K., et al. 2011, ApJ, 738, 23
Riaud, P., Mawet, D., Absil, O., et al. 2006, A&A, 458, 317
Rice, W. K. M., Armitage, P. J., Wood, K., & Lodato, G. 2006, MNRAS, 373, 1619
Robitaille, T. P., Whitney, B. A., Indebetouw, R., Wood, K., & Denzmore, P. 2006, ApJS, 167, 256
Shakura, N. I., & Sunyaev, R. A. 1973, A&A, 24, 337
Skrutskie, M. F., Dutcherich, D., Strom, S. E., et al. 1990, AJ, 99, 1187
Strom, K. M., Strom, S. E., Edwards, S., Cabrit, S., & Skrutskie, M. F. 1989, AJ, 97, 1451
Suzuki, R., Kudo, T., Hashimoto, J., et al. 2010, Proc. SPIE, 7735, 773530
Tamura, M. 2009, in AIP Conf. Proc. 1158, Exoplanets and Disks: Their Formation and Diversity, ed. T. Usuda, M. Ishii, & M. Tamura (Melville, NY: AIP), 11
Tananbaum, H. S., Kudo, T., et al. 2012, PASJ, in press (arXiv:1206.1215)
Thalmann, C., Grady, C. A., Sitko, M. L., et al. 2012, ApJ, 753, 153
Thi, W.-S., Menard, F., & Dufour, M. 2012, A&A, 537, A5
Wong, T. J., Sargent, A. I., Reipurth, B., et al. 2012, ApJ, 748, 122
Zhu, Z., Nelson, R. P., Hartmann, L., Espaillat, C., & Calvet, N. 2011, ApJ, 729, 47