METHOD

A NMF-based approach to discover overlooked differentially expressed gene regions from single-cell RNA-seq data

Hirotaka Matsumoto1*, Tetsutaro Hayashi1, Haruka Ozaki2,3, Koki Tsuyuzaki1, Mana Umeda1, Tsuyoshi Iida4, Masaya Nakamura4, Hideyuki Okano5 and Itoshi Nikaido1,6

Abstract
Single-cell RNA sequencing has enabled researchers to quantify the transcriptomes of individual cells, infer cell types, and investigate differential expression among cell types, which will lead to a better understanding of the regulatory mechanisms of cell states. Transcript diversity caused by phenomena such as aberrant splicing events have been revealed, and differential expression of previously unannotated transcripts might be overlooked by annotation-based analyses. Accordingly, we have developed an approach to discover overlooked differentially expressed (DE) gene regions that complements annotation-based methods. We applied our algorithm to two datasets and discovered several intriguing DE transcripts, including a transcript related to the modulation of neural stem/progenitor cell differentiation.

Keywords: Single-cell RNA sequencing; Differential expression analysis; Non-negative matrix factorization

Background
The advancement of single-cell technology has enabled to investigate various tissues [1, 2] and species [3, 4] with single-cell RNA sequencing (scRNA-seq), which enables comprehensive cell typing and the elucidation of cell compositions and dynamics. In particular, scRNA-seq can reveal the subtle differences among cell states, such as intermediate stages of differentiation. By investigating differentially expressed (DE) genes among such cell states, we can elucidate regulatory processes including cell fate determination [5]. In addition to traditional gene-level differential expression analyses, various novel analyses have been proposed for scRNA-seq studies, including the detection of differential distributions of expression levels [6] and differential splicing [7, 8], isoform-level differential pattern analysis [9], discriminative learning approach for differential expression analysis [10], and dynamic prediction through the comparison of spliced and unspliced mRNAs [11]. Thus, the development of various computational analysis methods that utilize information at the single-cell level is essential to advance the current understanding of RNA biology.

Recent comprehensive analyses of RNA-seq data have revealed the existence of various overlooked transcripts. For example, a comprehensive tumor analysis revealed that many tumors contain aberrant splicing patterns (neojunctions) that are not detected in normal samples [12]. Additionally, numerous genetic variants are related to aberrant splicing associated with certain diseases [13]. Therefore, it is important to detect novel splicing patterns, as well as detect differential expression of annotated transcripts. The transcriptomes of unstudied cell types, including rare cell types, can be revealed by scRNA-seq analyses, and we can now discover such cell type-specific splicing events.

In addition to major types of alternative splicing (AS), underappreciated classes of AS events, such as retained introns and microexons, are known to have essential roles, for example, in neuronal development [14]. Intron retention, which is common in tumors, can generate peptides and be a source of neoepitopes for cancer vaccines, and therefore the detection of novel intron retention events is medically important [15]. Furthermore, alternative polyadenylation, which produces isoforms that have 3′-untranslated regions (UTRs) of different lengths, is also known to be associated with several biological processes [16].

To reveal such complex AS patterns, several computational approaches have been developed that can detect previously unannotated splicing patterns. For
example, spliced aligned reads (exon–exon junction reads) are beneficial in identifying the spliced mRNA structures [17, 18]. As another example, non-negative matrix factorization (NMF) has been used to decompose data into essential patterns and predict AS patterns from microarray data [19] and RNA-seq data [20].

In addition to these complex AS patterns, other types of transcripts, such as antisense transcripts transcribed from gene regions, are known to be essential regulators of gene expression [21]. In light of such complex transcript structures, typical differential expression analysis based on previously annotated transcript structures might overlook some important DE genes. To find DE genes without relying on existing annotation, distinct approaches have been proposed that identify DE regions from read coverage data [22, 23].

In single-cell technologies, full-length scRNA-seq data such as Smart-Seq [24, 25] provide powerful data that can reveal these complex transcript structures. Other scRNA-seq protocols, such as SUPeR-Seq [26], which can capture non-poly(A) transcripts, will also be useful to detect various overlooked DE transcripts. In particular, we have developed a single-cell full-length total RNA-seq (RamDA-seq) method and have validated that it precisely captures full-length transcripts and also captures various types of RNAs such as enhancer RNAs [27]. By utilizing such scRNA-seq data, we can perform differential expression analyses between cell states more precisely.

Accordingly, we have developed an approach to discover Overlooked Differentially Expressed Gene Regions (ODEGRs), which is derived from several kinds of transcripts such as novel AS patterns, intron retention, and antisense transcripts, to complement the annotation-based differential expression analysis of single-cell data (Fig.1). Our approach utilizes the composition of scRNA-seq data, which contain information from many samples (i.e., cells), and decomposes the mapped count data for gene regions using NMF. With NMF, we can computationally extract reproducible signals corresponding to transcript structures and their associated expression profiles without relying on transcript annotations (Fig.2(a)). In addition, the non-negative constraint of NMF, which is its principal difference from other matrix decomposition methods, is effective in preserving the relation of the magnitude of expression. Next, we developed the following scores for a gene region: $T_{\text{NMF}}^{+}$, $T_{\text{TPM}}^{+}$, and $\Delta T_{\text{NMF} \rightarrow \text{TPM}}$. $T_{\text{NMF}}^{+}$ represents the scores that quantify the differential expression levels between two groups based on the NMF result (Fig.2(b)), while $T_{\text{TPM}}^{+}$ represents the scores that quantify the differential expression levels for annotation-based expression data (Fig.2(c)). Thus, $\Delta T_{\text{NMF} \rightarrow \text{TPM}}$ represents the score that quantifies the differential expression that is not detected in the annotation-based approach (Fig.2(d)). We investigated gene regions with high $\Delta T_{\text{NMF} \rightarrow \text{TPM}}$ values in order to discover ODEGRs.

We applied our algorithm to two real datasets: (1) mouse embryonic stem (ES) cells and primitive endoderm (PrE) cells and (2) neural stem cells (NSCs) derived from human induced pluripotent stem (iPS) cells. First, we evaluated whether the NMF-based approach could quantify and find local DE regions from simulated data. We also evaluated whether it could detect AS switches within a gene, as determined by annotation-based analysis. Our algorithm was indeed able to detect such DE regions without relying on transcript annotations. Then, we applied our method to real datasets to detect ODEGRs and found several intriguing examples. From the perspective of previous research, our results correspond, for example, to unannotated splicing patterns, antisense transcript, and unannotated 3’-UTRs of adjacent genes. In particular, some ODEGRs are related to critical regulatory mechanisms such as the modulation of differentiation and tissue-specific imprinting. Thus, our novel differential expression analysis method identified some important ODEGRs and can complement annotation-based methods, making it a useful method for analysis in the increasing number of scRNA-seq experiments.
Results

NMF-based approach for discovering ODEGR

In this research, we focused on detecting DE gene regions that were overlooked in the differential expression analysis of previously annotated transcripts from mapped read count data. We divided a gene region into 100-bp bins and described a read count matrix for a gene region with a $C \times L$ matrix $X$, where $C$ is the number of cells and $L$ is the number of bins. First, we decomposed $X$ into two non-negative matrices (using non-negative matrix factorization):

$$X^T \approx WH$$ \hspace{1cm} (1)

where $W$ and $H$ are $L \times K$ and $K \times C$ non-negative matrices ($K$ is the factorization rank) referred to as “metagenes” and “metagene expression profiles” in previous studies, respectively [28, 29]. In this research, we hypothesized that $W$ corresponds to the transcript structure including splicing patterns and that $H$ corresponds to the expression for each structure in each cell.

Second, we quantified the differential expression level of a structure $k \in (1...K)$ between two groups $A$ and $B$ based on Welch’s $t$-test:

$$T_{NMF,k}^{(K)} = \frac{\bar{H}_{k,C_A} - \bar{H}_{k,C_B}}{\sqrt{\frac{s^2_{k,A}}{|C_A|} + \frac{s^2_{k,B}}{|C_B|}}},$$ \hspace{1cm} (2)

where $C_A$ is the list of cells whose labels are $A$ and $\bar{H}_{k,C_A}$, $s^2_{k,A}$, and $|C_A|$ are the sample mean of $H_{k,C_A}$, variance, and size of group $A$, respectively. Owing to the non-negative constraint, the relation between the two groups (i.e., $\bar{H}_{k,C_A} - \bar{H}_{k,C_B}$ can be greater or smaller than 0) will be consistent with the relation in the original expression space. Our goal was to identify overlooked differential expression, and therefore, such relations, as well as their absolute values, were effective indicators for discovering ODEGRs. Therefore, we defined the following two scores, which correspond to the relation $\bar{H}_{k,C_A} > \bar{H}_{k,C_B}$ and $\bar{H}_{k,C_A} < \bar{H}_{k,C_B}$, respectively:

$$T_{NMF}^{(K)+} = \max_k (0, \max_{k \in (1...K)} T_{NMF,k}^{(K)+}),$$

$$T_{NMF}^{(K)-} = \min_k (0, \min_{k \in (1...K)} T_{NMF,k}^{(K)-}).$$ \hspace{1cm} (3)

In NMF, the factorization rank ($K$) must be decided in advance, and the value is critical for analytical results. The various transcript structures cannot be separated with small $K$ values and are excessively separated with large $K$ values. In either case, the expression profiles become ambiguous, and we might overlook the DE regions if an inappropriate $K$ value is selected. Therefore, we decomposed the data with several $K$ values ($K \in (2, 5, 10)$ in this research) and calculated the positive maximum and negative minimum values:

$$T_{NMF}^{+} = \max_{K \in (2,5,10)} T_{NMF}^{(K)+},$$

$$T_{NMF}^{-} = \min_{K \in (2,5,10)} T_{NMF}^{(K)-}.$$ \hspace{1cm} (4)
Next, we defined similar scores for the TPM (transcripts per million) matrix, which represents the expression profile based on annotated transcripts (we used $\log_{10}(TPM + 1)$ in actuality). We described the list of transcripts for the gene region using $T$ and calculated Welch’s $t$-statistic as before for a transcript $t \in T$, which is referred to as $T_{TPM,t}$. Then, the scores for the gene region were defined by the positive maximum and negative minimum among transcripts of the gene as follows:

$$T_{TPM}^+ = \max(0, \max_{t \in T} T_{TPM,t}),$$
$$T_{TPM}^- = \min(0, \min_{t \in T} T_{TPM,t}).$$

(5)

Lastly, we developed a score to detect ODEGRs as follows:

$$\Delta T_{NMF-TPM} = \max(T_{NMF}^+ - T_{TPM}^+, -(T_{NMF}^- - T_{TPM}^-)).$$

(6)

Because there is no global NMF optimization algorithm, we calculated $\Delta T_{NMF-TPM}$ using three different random seeds and also used minimum $\Delta T_{NMF-TPM}$ to obtain reliable ODEGRs (see the Methods section).

We also developed a score $\Delta T_{NMF-Mean}$ that measured the overlooked differential expression merely using the mean of the coverage. We used this score to evaluate whether the NMF-based approach separates the signal and detects complex DE patterns. We calculated the mean of the logarithm of data for a cell $c$ ($\sum_{t=1}^{L} \log_{10}(X_{c,t} + 1)/L$, where $L$ is the number of bins) as well as the corresponding Welch’s $t$-statistic as before and $\Delta T_{NMF-Mean}$ likewise.

Dataset

In this research, we used scRNA-seq data from the following two experiments.

**mES-PrE dataset**

The first dataset is derived from mouse ES cells and primitive endoderm (PrE) cells subjected to RamDA-seq and was examined in our previous study [27]. We used the data from 5G6GR mouse ES cells samples at 0 and 72 h after dexamethasone induction and defined the cell type at each time point as ES cells (92 cells) and PrE cells (93 cells), respectively.

**hNSC-NC dataset**

The second dataset corresponds to human neural stem cells (NSCs) derived from iPSCs measured by RamDA-seq. There is heterogeneity within the population, and some subpopulations other than the NSC subpopulation were identified (Additional file 1: Fig. S1). After clustering these cells and defining the cell types based on marker gene expression, we identified 515 NSCs and 80 partially differentiated neural cells (NCs).

Validation on simulation dataset

At first, we investigated the performance of NMF-based differential expression quantification and whether our approach can quantify the local differences in a region using simulation data. The simulation data were generated from the mES-PrE dataset such that the data matrix includes local DE patterns of length $L'$. We evaluated the ability to detect local DE regions based on $\Delta T_{NMF-Mean}$. We also compared the performance when we used $K = (2, 5, 10)$, as mentioned in Eq. (4), or one fixed value (i.e., $K = 2, 5$, or $10$) for calculating $T_{NMF}^+$ and $T_{NMF}^-$. The area under the ROC curve (AUROC) values for all, $K = 2, K = 5$, and $K = 10$ were $0.98, 0.93, 0.93$, and $0.90$, respectively for simulation data with $L' = 100$ (Fig. 3(a)). The AUROC values for the $L' = 50$ dataset were $0.98, 0.91, 0.96$, and $0.93$, respectively, and those for the $L' = 10$ dataset were $0.94, 0.64, 0.86$, and $0.94$, respectively (Fig. 3(b),(c)). In all cases, our algorithm using multiple $K$ values showed high performance, and therefore, our NMF-based approach is useful for discovering various local differences.

Validation with alternative isoform expression

We also investigated whether the NMF-based approach can quantify the complex DE patterns associated with genes that have alternative isoform expression. Based on the TPM matrix calculated from the annotation, we defined the positive-control and negative-control datasets. The former consists of the gene set with different isoforms expressed in different groups, while the latter consists of the remaining genes (see the Methods section for detailed definitions). Then, we evaluated the ability to detect such complex DE patterns based on $\Delta T_{NMF-Mean}$.

The positive-control examples of alternative isoform expression in the mES-PrE dataset were *Frmd4a* and *Pde4d*, which are known for frequent transcription start site (TSS) switching events [30] (Fig. 4(a),(b)). Based on our criteria, both *Frmd4a* and *Pde4d* were highly ranked (53rd and 23rd out of 4,965 genes, respectively).

The examples in the hNSC-NC dataset were *RTN4*, also known as *NOGO*, which encodes the Nogo-A isoform that contains exon 3 and is expressed in neural precursor cells [31] (Fig. 4(c)), and *MAP4*, which
is known for its alternative isoform expression across neural cell types [32] (Fig. 4(d)). These genes were highly ranked in our criteria (40th and 1st out of 6,491 genes, respectively.) Thus, the typical genes with alternative isoform expression are highly ranked in our criteria $\Delta T_{\text{NMF}} - \text{Mean}$.

Overall, the AUROC values (for threshold 15) were about 0.79 and 0.83 for the mES-PrE and hNSC-NC datasets, respectively (Fig. 5). Although our algorithm overlooked some alternative expression patterns, the high AUCROC values demonstrated the effectiveness of our algorithm for discovering previously unannotated DE transcripts.

**Discovery of ODEGRs**

Next, we investigated the existence of ODEGRs by using $\Delta T_{\text{NMF}} - \text{TPM}$. In brief, the values of Welch’s t-statistics based on NMF ($T_{\text{NMF}}^+$ and $T_{\text{NMF}}^-$) and TPM ($T_{\text{TPM}}^+$ and $T_{\text{TPM}}^-$) were highly correlated (Pearson’s correlation coefficients for the mES-PrE dataset and hNSC-NC dataset were about 0.83 and 0.84, respectively), and large $\Delta T_{\text{NMF}} - \text{TPM}$ values were observed for only a small fraction of genes (Additional file 1: Fig. S2). Therefore, we ranked genes by $\Delta T_{\text{NMF}} - \text{TPM}$ in descending order to identify ODEGRs. (The actual procedure of $\Delta T_{\text{NMF}} - \text{TPM}$ calculation is described in the Methods section.) Only a small fraction of genes had large positive values of $\Delta T_{\text{NMF}} - \text{TPM}$ (Additional file 1). Five genes in the mES-PrE dataset had $\Delta T_{\text{NMF}} - \text{TPM}$ Z-scores over 3 while 39 genes in the hNSC-NC dataset did. Although the number of ODEGRs discovered by our algorithm were few, several intriguing ODEGRs were identified.

**mES-PrE Dataset**

The read coverage and transcript annotation for the six highest-ranking genes in the mES-PrE dataset are shown in Fig. 6.

The 1st and 4th ranked genes were Zmynd8 and Brd1, and numerous reads were mapped to the specific intron regions of these genes (Fig. 6(a)(d)). The novel enhancer-associated antisense transcripts for these genes have previously been reported in mESCs [33], and this suggests that our approach can detect several kinds of DE transcripts, including antisense transcripts.

The 2nd ranked gene was Utrn, and two distinct coverage patterns of peaks that correspond to exons were observed in ES and PrE cells, respectively (Fig. 6(b)). Since the annotation contains only one isoform, this DE pattern was overlooked in the annotation-based approach. We used GENCODE vM9 such that the DE pattern was overlooked in the annotation-based approach. We used GENCODE vM9 such that the analytical results were consistent with previous work [27], and we also considered the possibility that the latest annotation includes the isoforms corresponding to such patterns. We recalculated the TPM values using GENCODE vM18, and $T_{\text{TPM}}^+$ was 46.2 and $T_{\text{TPM}}^-$ was −15.5 for vM18, in comparison to $T_{\text{TPM}}^+$ = 0.0 and $T_{\text{TPM}}^-$ = −4.4 for vM9 (Additional file 1: Section 3.2 and Fig. S4). This result suggests the existence of DE transcripts that were not annotated in vM9. A similar result was observed for the 7th ranked gene Arid5b (Fig. S4). These results demonstrate the potential of our approach for discovering previously unannotated isoforms.

The 3rd ranked gene was Echdc2, which had numerous reads mapped to its 3′ intron region (Fig. 6(c)). Although such a pattern is consistent with intron retention, this mapping pattern is continued from adjacent gene Zyg11a, and the coverage at the 3′ intron of Echdc2 is correlated with coverage at the Zyg11a region (Additional file 1: Section 3.3 and Fig. S5). These results suggest that an unannotated long isoform of Zyg11a exists and overlaps with the Echdc2 region.

---

**Figure 3** The ROC curves for the simulated dataset. Simulation results for (a) $L’ = 100$, (b) 50, and (c) 10, where $L’$ is the length of local differential expression patterns.
Figure 4 Examples of alternative isoform expression. The visualizations of read coverage and transcript annotations for (a) Frmd4a, (b) Pde4d, (c) RTN4, and (d) MAP4, respectively. (a) and (b) are the examples from the mES-PrE dataset, while (c) and (d) are the examples from the hNSC-NC dataset. These figures are visualized with Millefy, which provides genome-browser-like visualizations of scRNA-seq datasets https://github.com/yuifu/millefy.

The 5th ranked gene was Macf1, and numerous reads were mapped to the specific intron region of the gene in PrE cells (Fig. 6(e)). An exon was annotated for the region in vM18, and the DE transcript including the exon was overlooked in differential expression analysis using vM9, which was also the case for Utrn and Arid5b (Fig. S4).

The 6th ranked gene was Gata6 (Fig. 6(f)). The exogenous Gata6, which lacks a 3’UTR end, is arbitrarily expressed in these ES cells. After dexamethasone induction, Gata6 is transported into the nucleus, ES cells differentiate into PrE cells, and the level of expressed endogenous Gata6 increases. Because the annotation file does not include exogenous structure, annotation-based TPM cannot reflect the exogenous expression patterns, which resulted in high ΔT\textsuperscript{NMF-TPM} values.

hNSC-NC Dataset

In comparison to the results of the mES-PrE dataset, the results of the hNSC-NC dataset contained uninteresting patterns among the most highly ranked genes (Additional file 1: Section 3.1 and Fig. S3). Therefore, we show six high-ranking genes of great interest in the hNSC-NC dataset (Fig. 7).

The 2nd ranked gene was PSMB7, and many reads from NSCs were mapped to its 3’ intron region, which is similar to the result for Echdc2 in the mES-PrE dataset (Fig. 7(a)). The coverage pattern was contin-
used from the adjacent gene NEK6, and the coverage of the intron region is correlated with the that of NEK6 (Fig. S5). This result suggests the existence of an unannotated long transcript of NEK6 that overlaps with the PSMB7 region.

The 6th ranked gene was COPG2, and numerous reads were mapped to its 3′ intron regions, resembling the results for Echdc2 and PSMB7 (Fig. 7(b)). These reads are also likely to be derived from transcripts of the adjacent gene MEST, which may have an unannotated long transcript. Intriguingly, in mouse, Mest is an imprinted gene, and a long isoform of Mest (referred to as MestXL) is expressed in the developing central nervous system, which results in the repression of Copg2 on the same paternal allele [34]. Therefore, the long transcript of MEST and the tissue-specific imprinting of COPG2 depending on the long transcript are thought to occur in human. Thus, the detection of overlapping unannotated transcripts can be associated with regulatory mechanisms.

The 10th and 15th ranked genes were GREB1L and GRB10, and distinct AS patterns are suggested by the difference in mapped read counts between NSCs and NCs, especially for the intron region (Fig. 7(c),(d)). In GREB1L, several reads mapped to the 5′ intron region (left side of the heatmap in Fig. 7(c)), and the long isoform appears to be expressed in NSCs. Our NMF-based algorithm detected such overlooked differences ($T_{NMF}^+ = 13.8$) in contrast to the annotation-based approach ($T_{TPM}^+ = 0.8$). Since RamDA-seq detects not only mature mRNAs but also pre-mRNAs, many reads mapped to intron regions are considered to be derived from pre-mRNA expression [27]. Because the annotation-based algorithm does not usually use intron-mapped reads, our proposed algorithm that utilizes such information is effective for AS pattern identification, especially for genes with alternative TSSs.

For GRB10, numerous reads were mapped to its 5′ intron, and cell-type-specific TSS switching likely occurs for this gene (Fig. 7(d)). GRB10 is an imprinted gene and is known for its unique TSS switch mechanism in mouse [35]. In the differentiation of mESCs into motor neurons, the expression of Grb10 changes from the maternal to paternal allele. The upstream promoter is used for maternal expression, and the downstream alternative promoter is used for paternal expression. Therefore, the 5′ intron-mapped reads, which are detected in only NSCs, support the alternative TSS based on the above mechanism and reflect DE patterns, observable by utilizing intron reads.

The 17th ranked gene was PTPRN2, and there appears to be a short unannotated transcript in NSCs (Fig. 7(e)). Notably, in mouse, an alternative promoter exists downstream of Ptprn2, and the transcription from the promoter drives the miR-153 precursor transcript embedded in the Ptprn2 gene region [36]. Moreover, miR-153 is highly expressed in mouse neural stem/progenitor cells (NSPCs), and the repression of miR-153 leads to differentiation, and hence, miR-153 modulates NSPCs [37]. Human miR-153 is located in PTPRN2 [38], and therefore, the short transcript in the 3′ region is likely a key factor that distinguishes human NSCs and NCs but is overlooked by annotation-based analysis.

The 18th ranked gene was GPI, and numerous reads from NCs were mapped to its central intron region (Fig. 7(f)). In GPI, the existence and conservation of a minisatellite in its intron have been reported [39]. Although the increase in such reads might be an artifact caused by repetitive sequences, a NC-specific transcript might exist in the region.

**Discussion**

In this research, we developed a novel computational approach for differential expression analysis of scRNA-seq data based on matrix factorization of mapped
Figure 6 Examples of high-ranking genes in the mES-PrE dataset. The results for the six top-ranked genes (in descending order) (a) Zmynd8, (b) Utrn, (c) Echdc2, (d) Brd1, (e) Macf1, and (f) Gata6 are visualized.
Figure 7 Examples of high-ranking genes in the hNSC-NC dataset. The results for (a) PSMB7, (b) COPG2, (c) GREB1L, (d) GRB10, (e) PTPRN2, and (f) GPI, the 2nd, 6th, 10th, 15th, 17th, and 18th ranked genes, respectively, are visualized.
count data to discover overlooked DE gene regions. Matrix factorization methods, such as principal component analysis, are a practical approach to extract essential structures and uncover biological knowledge from large-scale biological data [40]. To take advantage of the large number of cells assayed in scRNA-seq data, we proposed an NMF-based approach to extract reproducible patterns and quantify differences in these patterns among groups. In particular, we used non-negative constraint to quantify DE patterns while preserving information about the group in which the patterns were expressed, and we developed a score that identifies ODEGRs by using positive maximum and negative minimum values. Such computational approaches which utilize numerical constraints based on the biological subjects can facilitate further omics studies.

We applied our algorithm to two scRNA-seq datasets and discovered several unannotated DE patterns, including DE antisense transcripts. In addition, our algorithm utilized mapping patterns in intron regions to discover overlooked alternative TSS patterns. Specifically, we detected an unannotated transcript which is a key factor for regulating differentiation. Thus, our approach has the potential to identify essential overlooked DE genes.

Although our algorithm was able to identify several intriguing ODEGRs, it remains difficult to distinguish the cause of DE transcripts such as those associated with antisense transcripts or the long unannotated transcripts of adjacent genes. In addition, the detected ODEGRs are few, and thus the impact on whole expression analyses is quantitatively small. However, our approach can discover novel transcripts and will enable further experimental and computational analyses of these transcripts, which will deepen the current understanding of the complex gene expression landscape.

As shown in the validation of alternative isoform expression, our algorithm overlooked several genes with alternative isoform expression. One limitation of our algorithm is that its detection of changes involves small exons, because small changes have little effect on the objective function and are overlooked in matrix factorization. In addition, we used the count data with a 100-bp bin size (see the Methods section), which also overlooked the differences in small exons. Although this problem might be solved by using smaller bin sizes, NMF computational time and data size increase substantially with increases in matrix size, so additional improvements are therefore necessary. Moreover, our algorithm overlooks DE patterns in the filtered regions such as those with gene overlap or those with low mappability. Therefore, other approaches, such as methods based on exon-exon junction reads [17, 18], will be useful to make up for each other’s weak points and to complement annotation-based analyses.

Several effective computational expression analysis methods for scRNA-seq data, such as for cell typing and for reconstructing differentiation trajectories, have been developed so far. In this research, we have proposed a novel application of scRNA-seq data for discovering overlooked DE transcripts. Here, we have developed an algorithm for differential expression analysis between two groups, and this approach might be useful for analyzing cellular heterogeneity and discovering transcripts with an overlooked multimodal distribution.

Conclusions

In summary, we have developed an algorithm to discover overlooked DE gene regions from scRNA-seq data. First, we confirmed that our algorithm could detect complex DE patterns such as simulated local differential expression and alternative isoform expression. Then, we applied our algorithm to two single-cell full-length total RNA-seq datasets and discovered intriguing examples of differential expression, including a transcript related to the modulation of NSPC differentiation. Our approach complements annotation-based analysis and is an effective approach for better understanding cellular regulatory mechanisms using single-cell studies.

Methods

Data processing

The mouse ES-PrE dataset was derived from our previous work [27], and we regarded cells 0 h and 72 h after induction as ES and PrE cells, respectively. The scRNA-seq reads were aligned to the mouse mm10 genome using HISAT2 [41] with the parameters “-dta-cufflinks -p 4 -k 5 -X 800 –sp 1000,1000,” and uniquely mapped reads were selected using the BAMtools “filter” command with the parameters “-isMapped true -tag NH:1” and the SAMTools “view” command with the parameter “-q 40.” The genome-wide coverage data were generated from these mapped data using the “bamCoverage” command in deepTools(2.7.10) [42] with the parameters “–binSize 1 –smoothLength 1 –normalizeUsingRPKM.” We also quantified transcript-level expression data (i.e., TPM matrix) from scRNA-seq data using the Sailfish(v0.9.2) [43] “quant” command with the parameter “-U” and GENCODE vM9 annotation.

The human NSC-NC dataset was measured using RamDA-seq for cell populations derived from NSCs differentiated from iPSCs. The scRNA-seq reads were aligned to the human hg38 genome with
STAR(v2.5.2a) [44], and the coverage data was constructed with “bamCoverage” command as mentioned above. We also quantified the transcript-level expression data (TPM matrix) with Sailfish(v0.10.0) based on GENCODE v24 gene annotation. Based on the known marker gene expression, we identified subpopulations in the data (Additional file 1: Fig. S1). In particular, we found that a subpopulation expressed some stemness marker genes, such as SOX2, LIN28, and POU5F1, and another subpopulation expressed neural marker genes, such as ASCL1. We regarded the cell types corresponding to those two subpopulations as NSCs and NCs, respectively.

For both datasets, we generated a mapping count data matrix for each gene region as follows. First, we extracted the transcript list so that the mean expression of a transcript was over a set threshold (i.e., \( \sum_c \log_{10}(TPM_{t,c} + 1)/C > 0.5 \), where \( C \) is the number of cells). Next, we constructed the unique protein-coding gene list, which corresponds to the above transcript list. Then, we selected 6,921 and 9,359 genes from each dataset and constructed a count data matrix (100-bp bins) for each gene region from the genome-wide coverage data of each cell. The gene regions were defined by the genomic start location and end location of the row of the gene in the GENCODE GTF files (vM9 for the mES-PrE dataset and v24 for the hNSC-NC dataset). We filtered the bins that contained various genes because the target gene might falsely be regarded as occurring in an ODEGR owing to the differential expression of other overlapping genes. We also filtered the bins that were derived from regions with low mappability. This is because such bins might falsely be regarded as a differentially expressed region owing to the misalignment of reads. In this research, we defined bins with low mappability as those for which the minimum of 24-bp mappability (downloaded from https://bismap.hofmanlab.org [45]) was 0.5 or less. Then, the genes that remained with bin sizes under 100 were filtered. In this way, 4,965 and 6,491 genes were selected for differential expression analysis.

**Implementation and computational cost**

We computed NMF with the NMF package in the R statistical computing environment [29] and used the objective function based on the Euclidean distance between the data matrix \( X \) and the reconstructed matrix \( WH \) as calculated by factorization [46]. The raw count matrix data has excessively large values in some bins, and such large values cause the underestimation of the influence of the remaining bins in the objective function. Therefore, we applied \( \log_{10}(count + 1) \) transformation to the count values before NMF calculation. The scripts are available at GitHub (https://github.com/hmatsu226/ODEGRfinder).

Since the NMF calculations of all gene regions are independent from each other, we performed NMF for each gene region in parallel using Sun Grid Engine. In the NMF analysis with \( K = 10 \) for the first 1,000 gene regions, the computational times were about 1.7 hours and 10.9 hours with maximum memory usage of about 240 Mb and 544 Mb for the mES-PrE and hNSC-NC datasets, respectively.

**Validation method**

**Simulation dataset**

We constructed simulation data from the mES-PrE dataset. First, we calculated the mean of the logarithm of the coverage of a gene region \( \left( \sum_{i=1}^{L} \log_{10}(X_{c,i} + 1)/L \right) \) where \( L \) is the number of bins and \( c \) is the index of a cell). We then calculated the \( p \)-value of the \( t \)-test comparing this value between the ES cells and PrE cells and extracted the top 100 most significant DE genes. Second, we randomly selected a sample of gene regions \( X \) from these 100 DE genes, and reshaped the \( C \times L \) matrix \( X \) into a \( C \times L' \) matrix \( X' \) by averaging \( X_{c,i} \) from \( i = \lfloor (b - 1)(L - 1)/L' \rfloor + 1 \) to \( \lfloor bL - 1)/L' \rfloor + 1 \) for each bin \( b \) corresponding to \( X'_{c,b} \).

Then, we randomly selected a gene from among 4,965 genes and combined the count data for the gene using the above matrix \( X' \) so that the combined matrix had the local DE pattern. However, if the two selected genes had the same DE trend, that is, both satisfied \( \log_{10}(p\text{-value}) > 10 \) for the same side in the corresponding \( t \)-test, the combined matrix did not have the local DE pattern, and so we selected one of the 4,965 genes at random again. We generated a positive-control datasets with 1,000 datapoints as above for \( L' = 10, 50, \) and 100, and we regarded the raw data as the negative-control set.

**Alternative isofom expression definition**

We defined genes with alternative isofom expression based on the TPM matrix. We defined a gene that satisfied \( \log_{10}(p\text{-value}) \) for a corresponding \( t \)-test for \( T_{TPM}^{+} \) and \( T_{TPM}^{-} \) over \( \alpha \) as belonging to the positive-control set, and the remaining genes as belonging to the negative-control set. We used \( \alpha = 5, 10, \) and 15 and the number of genes in the positive-control set were 76, 25, and 8 for the mES-PrE dataset and 333, 95, and 51 for the hNSC-NC dataset, respectively.

**Discovery of ODEGR**

We investigated the ODEGRs based on their ranked \( \Delta T_{NMF-TPM} \) values in descending order. Even if \( \Delta T_{NMF-TPM} \) is large, the annotation-based approach
Also we considered the reproducibility of NMF results. As there is no global optimization algorithm for NMF, the result depends on the initialization. Accordingly, we calculated $\Delta T_{\text{NMF-TPM}}$ for a gene with three initial values generated by different random seeds, and we used only the minimum value of $\Delta T_{\text{NMF-TPM}}$ among the three trials to filter unreliable differences. The reproducibility of NMF and filtered genes is described in Additional file 1.

**Algorithm 1 Calculate $\Delta T_{\text{NMF-TPM}}$**

\[
\begin{align*}
\Delta T &\leftarrow -\infty \\
\text{if} \ T_{\text{TPM}}^+ > 10 \ &\text{then} \\
\Delta T &\leftarrow \max(\Delta T, 0, (T_{\text{NMF}}^+ - T_{\text{TPM}}^+)) \\
\text{else} \\
\text{if} \ T_{\text{TPM}}^- < -10 \ &\text{then} \\
\Delta T &\leftarrow \max(\Delta T, 0, -(T_{\text{NMF}}^- - T_{\text{TPM}}^-)) \\
\text{else} \\
\Delta T &\leftarrow \max(\Delta T, -(T_{\text{NMF}}^- - T_{\text{TPM}}^-)) \\
\end{align*}
\]

**Authors’ contributions**

HM, TH, and IN designed the study. HM designed and implemented the algorithm. HM and HOZ analyzed the mES-Pre dataset, and HM and KT analyzed the hNSC-NC data. TM, TI, MN, and HOK performed experiments for the hNSC-NC data. HM, TH, HOZ, KT, and IN wrote the manuscript. All authors read and approved the final manuscript.

**Acknowledgements**

We are grateful to all members of the Laboratory for Bioinformatics Research, RIKEN Center for Biosystems Dynamics Research, for providing helpful advice. We would especially like to thank Mr. Akihiro Matsumoto and Mr. Manabu Ishii for their assistance with the IT infrastructure for the data analysis. We are also grateful to Jun Kohyama (Department of Physiology, Keio University School of Medicine). We would also like to thank the Center for iPSC Cell Research and Application, Kyoto University, for the human iPSC clones.

**Author details**

1. Laboratory for Bioinformatics Research RIKEN Center for Biosystems Dynamics Research, Wako, 351-0198, Saitama, Japan.
2. Center for Artificial Intelligence Research, University of Tsukuba, 1-1-1 Tennodai, Tsukuba, 305-8577, Ibaraki, Japan.
3. Bioinformatics Laboratory, Faculty of Medicine, University of Tsukuba, 1-1-1 Tennodai, Tsukuba, 305-8577, Ibaraki, Japan.
4. Department of Orthopaedic Surgery, Keio University School of Medicine, 3554, Shintomicho, Shinjuku-ku, 160-8582, Tokyo, Japan.
5. Department of Physiology, Keio University School of Medicine, 3554, Shintomicho, Shinjuku-ku, 160-8582, Tokyo, Japan.
6. Bioinformatics Course, Master’s/Doctoral Program in Life Science Innovation (T-LSI), School of Integrative and Global Majors (SIGMA), University of Tsukuba, Wako, 351-0198, Saitama, Japan.

**References**

1. Grun, D., Lyubimova, A., Kester, L., Wiebrands, K., Basak, O., Sasaki, N., Clevers, H., van Oudenaarden, A.: Single-cell messenger RNA sequencing reveals rare intestinal cell types. Nature 525(7568), 251–255 (2015)
2. La Manno, G., Gyllberg, D., Codeluppi, S., Nishimura, K., Salto, C., Zeisel, A., Borm, L.E., Stott, S.R.W., Toledo, E.M., Villaescusa, J.C., Lonnerberg, P., Ryge, J., Barker, R.A., Arenas, E., Linnares, S., Molecular Diversity of Midbrain Development in Mouse, Human, and Stem Cells. Cell 167(2), 566–580 (2016)
3. Plass, M., Solana, J., Wolf, F.A., Ayoub, S., Miotto, A., Gla?ar, P., Obermayer, B., Theis, F.J., Kocks, C., Rajewsky, N.: Cell type atlas and lineage tree of a whole complex animal by single-cell transcriptomics. Science 360(6391) (2018)
4. Wagner, D.E., Weinreb, C., Collins, Z.M., Briggs, J.A., Mergason, S.G., Klein, A.M.: Single-cell-mapping of gene expression landscapes and lineage in the zebrafish embryo. Science 360(6392), 981–987 (2018)
5. Herman, J.S., Grün, D., et al.: FateMap infers cell fate bias in multipotent progenitors from single-cell rna-seq data. Nature methods 15(5), 379 (2018)
6. Korthauer, K.D., Chu, L.F., Newton, M.A., Li, Y., Thomson, J., Stewart, R., Kendziorski, C.: A statistical approach for identifying differential distributions in single-cell RNA-seq experiments. Genome Biol. 17(1), 222 (2016)
7. Huang, Y., Sanguinetti, G.: BRIE: transcriptome-wide splicing quantification in single cells. Genome Biol. 18(1), 123 (2017)
8. Song, Y., Botvinnik, O.B., Lovci, M.T., Kakaradov, B., Liu, P., Xu, J.L., Yeo, G.W.: Single-Cell Alternative Splicing Analysis with Expedition Reveals Splicing Dynamics during Neuron Differentiation. Mol. Cell 67(1), 149–161 (2017)
9. Yu, T.N., Wills, Q.F., Kalari, K.R., Niu, N., Wang, L., Pavitan, Y., Rantalanen, M.: Isoform-level gene expression patterns in single-cell RNA-sequencing data. Bioinformatics 34(14), 2392–2400 (2018)
10. Ntranos, V., Yi, L., Melsted, P., Pachter, L.: A discriminative learning approach to differential expression analysis for single-cell RNA-seq data. Nat. Methods (2019)

**Funding**

This work was supported by a Grant-in-Aid for Japan Society for the Promotion of Science (JSPS) Fellows, JSPS KAKENHI (Grant Numbers 16J05079 and 70769520). This work was also partially supported by Japan Science and Technology Agency (JST) CREST program (Grant Number JPMJCR16G3), the Projects for Technological Development of the Research Center Network for Realization of Regenerative Medicine, the Japan Agency for Medical Research and Development (AMED; Grant Number 18bk0104059h003), and the Research Center Network for Realization of Regenerative Medicine (Centers for Clinical Application Research on Specific Disease/Organ, Grant Number 18bm0204001h0006) and as a Research Project for Practical Applications of Regenerative Medicine.
12. Kahles, A., et al.: Comprehensive Analysis of Alternative Splicing Across Tumors from 8,705 Patients. Cancer Cell 34(2), 211–224 (2018).
13. Xiong, H.Y., Alipanahi, B., Lee, J.J., Bretschneider, H., Merico, D., Yuen, R.K., Hua, Y., Gueroussov, S., Najafabadi, H.S., Hughes, T.R., Morris, Q., Sebic, Y., Knire, A.R., Jovic, S.W., Sciblencov, B.J., Frey, B.J.: RNA splicing. The human splicing code reveals new insights into the genetic determinants of disease. Science 347(6218), 1254806 (2015).
14. Raj, B., Blencowe, B.J.: Alternative Splicing in the Mammalian Nervous System: Recent Insights into Mechanisms and Functional Roles. Neuron 87(1), 14–27 (2015).
15. Smart, A.C., Margolis, C.A., Pimentel, H., He, M.X., Miao, D., Adeegbe, D., Fugmann, T., Wong, K.K., Van Allen, E.M.: Intron retention is a source of neopeptides in cancer. Nat. Biotechnol. (2018).
16. Tian, B., Manley, J.L.: Alternative polyadenylation of mRNA precursors. Nat. Rev. Mol. Cell Biol. 18(1), 18–30 (2017).
17. Li, Y.I., Knowles, D.A., Humphrey, J., Barbeira, A.N., Dickinson, S.P., Im, H.K., Pritchard, J.K.: Annotating transcript quantification of RNA splicing using LeafCutter. Nat. Genet. 50(1), 151–158 (2018).
18. Wang, Q., Rio, D.C.: JUM is a computational method for comprehensive annotation-free alternative pre-mRNA splicing patterns. Proc. Natl. Acad. Sci. U.S.A. 115(35), 8181–8190 (2018).
19. Anton, M.A., Gorostiga, D., Guruceaga, E., Segura, V., Carmona-Saez, P., Pascual-Montano, A., Pio, R., Montuenga, L.M., Rubio, A.: SPACE: an algorithm to predict and quantify alternatively spliced isoforms using microarrays. Genome Biol. 9(2), 46 (2008).
20. Ye, Y., Li, J.J.: NMFP: a non-negative matrix factorization based preselection method to increase accuracy of identifying mRNA isoforms from RNA-seq data. BMC Genomics 17 Suppl 1, 11 (2016).
21. Pelechano, V., Steinmetz, L.M.: Gene regulation by antisense transcription. Nat. Rev. Genet. 14(12), 880–893 (2013).
22. Fraze, A.C., Sabuncian, S., Hansen, K.D., Irizarry, R.A., Leek, J.T.: Differential expression analysis of RNA-seq data at single-base resolution. Bioinformatics 15(3), 413–426 (2014).
23. Collado-Torres, L., Nellore, A., Fraze, A.C., Wilks, C., Love, M.I., Langmead, B., Irizarry, R.A., Leek, J.T., Jaffe, A.E.: Flexible expressed region analysis for RNA-seq with derfinder. Nucleic Acids Res. 45(2), 9 (2017).
24. Ramskold, D., Luo, S., Wang, Y.C., Li, R., Deng, Q., Faridani, O.R., Daniels, G.A., Krehbetkova, I., Loring, J.F., Laurent, L.C., Schroth, G.P., Sandberg, R.: Full-length mRNA-Seq from single-cell levels of RNA and individual circulating tumor cells. Nat. Biotechnol. 30(8), 777–782 (2012).
25. Picelli, S., Bjorklund, A.K., Faridani, O.R., Sagasser, S., Winberg, G., Sandberg, R.: Smart-seq2 for sensitive full-length transcriptome profiling in single cells. Nat. Methods 10(11), 1096–1098 (2013).
26. Fan, X., Zhang, X., Wu, X., Guo, H., Hu, Y., Tang, F., Huang, Y.: Single-cell RNA-seq transcriptome analysis of linear and circular RNAs in mouse preimplantation embryos. Genome Biol. 16, 148 (2015).
27. Hayashi, T., Ozaki, H., Sasagawa, Y., Umeda, M., Danno, H., Nikaido, I.: Single-cell full-length total RNA sequencing uncovers dynamics of recursive splicing and enhancer RNAs. Nat Commun 9(1), 619 (2018).
28. Brunet, J.P., Tamayo, P., Golub, T.R., Mesirov, J.P.: Metagenes and molecular pattern discovery using matrix factorization. Proc. Natl. Acad. Sci. U.S.A. 101(12), 4164–4169 (2004).
29. Gaujoux, R., Seoighe, C.: A flexible R package for nonnegative matrix factorization. BMC Bioinformatics 11, 367 (2010).
30. Zhang, P., Dimont, E., Ha, T., Swanson, D.J., Hide, W., Goldowitz, D.: Relatively frequent switching of transcription start sites during cerebellar development. BMC Genomics 18(1), 461 (2017).
31. Schwab, M.E.: Functions of Nogo proteins and their receptors in the nervous system. Nat. Rev. Neurosci. 11(12), 799–811 (2010).
32. Hwang, H.W., Saito, Y., Park, C.Y., Blachere, N.E., Tajima, Y., Fak, J.J., Zucker-Scharff, I., Darnell, R.B.: t-Tag-PAPERCLIP Reveals Alternative Polyadenylation Promotes Cell-Type Specific Protein Diversity and Shifts Araf Isomers with Microglia Activation. Neuron 95(6), 1334–1349 (2017).
33. Onodera, C.S., Underwood, J.G., Katzman, S., Jacobs, F., Greenberg, D., Salama, S.R., Haussler, D.: Gene isoform specificity through enhancer-associated antisense transcription. PLoS ONE 7(8), 43511 (2012).
34. Macsac, J.L., Bogut, A.B., Moriss, A.S., Lefebvre, L.: Tissue-specific alternative polyadenylation at the imprinted gene Mest regulates allelic usage at Copg2. Nucleic Acids Res. 40(4), 1523–1535 (2012).
35. Plasschaert, R.N., Bartolomei, M.S.: Tissue-specific regulation and function of Grb10 during growth and neuronal commitment. Proc. Natl. Acad. Sci. U.S.A. 112(22), 6841–6847 (2015).
36. Mathews, R.W., Tatarakis, A., Rudenko, A., Johnson-Venkatesh, E.M., Yang, Y.J., Murphy, E.A., Todd, T.P., Schepers, S.T., Siu, N., Martorell, A.J., Falls, W.A., Hammack, S.E., Walsh, C.A., Tsai, L.H., Umemori, H., Bouton, M.E., Moazed, D.: A microRNA negative feedback loop downregulates vesicle transport and inhibits memory. Elife 5 (2016).
37. Tsuwayama, J., Bunt, J., Richards, L.J., Iwamari, H., Mochizuki, Y., Hamakubo, T., Shimazaki, T., Okano, H.: MicroRNA-153 Regulates the Acquisition of Gliogenic Competence by Neural Stem Cells. Stem Cell Reports 9(3), 365–377 (2015).
38. Mandemakers, W., Abuhatabiza, L., Xu, H., Caromile, L.A., Hebert, S.S., Snellins, A., Morais, V.A., Matta, S., Cai, T., Notkins, A.L., De Strooper, B.: Co-regulation of intragenic microRNA miR-153 and its host gene Ia-2 I: identification of miR-153 target genes with functions related to Ia-2 in pancreas and brain. Diabetologia 56(7), 1547–1556 (2013).
39. Williams, R.R., Hassan-Walker, A.F., Lavender, F.L., Morgan, M., Fak, P., Ragoussis, J.: The minisatellite of the GPI/AMF/NLK/ MF gene: interspecies conservation and transcriptional activity. Gene 269(1-2), 81–92 (2001).
40. Stein-O’Brien, G.L., Arora, R., Kulhane, A.C., Favorov, A.V., Garmire, J.X., Greene, C.S., Goff, L.A., Li, Y., Ngom, A., Ochs, M.F., Xu, Y., Fertig, E.J.: Enter the Matrix: Factorization Uncovers Knowledge from Omics. Trends Genet. 34(10), 790–805 (2018).
41. Kim, D., Langmead, B., Salzberg, S.L.: HISAT: a fast spliced aligner with low memory requirements. Nat. Methods 12(4), 357–360 (2015).
42. Ramirez, F., Ryan, D.P., Gruning, B., Bhartwaj, V., Kilpert, F., Richter, A.S., Heyne, S., Dundar, F., Hanke, T.: deepTools2: a next generation web server for deep-sequencing data analysis. Nucleic Acids Res. 44(W1), 160–165 (2016).
43. Patro, R., Mount, S.M., Kingsford, C.: Sailfish enables alignment-free isoform quantification from RNA-seq reads using lightweight algorithms. Nat. Biotechnol. 32(5), 462–464 (2014).
44. Dobin, A., Davis, C.A., Schlesinger, F., Drenkow, J., Zaleski, C., Jha, S., Batut, P., Chaisson, M., Gingeras, T.R.: STAR: ultrafast universal RNA-seq aligner. Bioinformatics 30(1), 15–21 (2013).
45. Karimzadeh, M., Ernst, C., Kundaje, A., Hoffman, M.M.: Umap and Bismap: quantifying genome and methylome mappability. Nucleic Acids Res. (2018).
46. Lee, L., Seung, D.: Algorithms for non-negative matrix factorization. Advances in neural information processing systems 13, 556–562 (2001).