Research Article

Effect of Hydrate on Gas/Water Relative Permeability of Hydrate-Bearing Sediments: Pore-Scale Microsimulation by the Lattice Boltzmann Method

Xin Xin, Bo Yang, Tianfu Xu, Yingli Xia, and Si Li

Key Laboratory of Groundwater Resources and Environment, Ministry of Education, Jilin University, Changchun 130021, China

Correspondence should be addressed to Xin Xin; xxxx@jlu.edu.cn

Received 9 July 2021; Revised 28 September 2021; Accepted 1 October 2021; Published 25 October 2021

Copyright © 2021 Xin Xin et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

As a clean energy source with ample reserves, natural gas hydrate is studied extensively. However, the existing hydrate production from hydrate deposits faces many challenges, especially the uncertain mechanism of complex multiphase seepage in the sediments. The relative permeability of hydrate-bearing sediments is key to evaluating gas and water production. To study such permeability, a set of pore-scale microsimulations were carried out using the Lattice Boltzmann Method. To account for the differences between hydrate saturation and hydrate pore habit, we performed a gas-water multiphase flow simulation that combines the fluids’ fundamental properties (density ratio, viscosity ratio, and wettability). Results show that the Lattice Boltzmann Method simulation is valid compared to the pore network simulation and analysis models. In gas and water multiphase flow systems, the viscous coupling effect permits water molecules to block gas flow severely due to viscosity differences. In hydrate-bearing sediments, as hydrate saturation increases, the water saturation $S_w$ between the continuous and discontinuous gas phase decreases from 0.45 to 0.30 while hydrate saturation increases from 0.2 to 0.6. Besides, the residual water and gas increased, and the capillary pressure increased. Moreover, the seepage of gas and water became more tedious, resulting in decreased relative permeability. Compared with different hydrate pore habits, pore-filling thins the pores, restricting the gas flow than the grain-coating. However, hydrate pore habit barely affects water relative permeability.

1. Introduction

Natural gas hydrate (NGH) is an ice-like, crystalline solid in which gas molecules are trapped within water molecules at low temperatures and high pressures [1, 2]. Naturally existing hydrate-bearing sediments (HBS) are widely distributed in continental margins and permafrost [3]. It has been estimated that the total carbon amount stored in the hydrates is at the same order of magnitude as all fossil fuels combined [4]. Therefore, NGH is viewed as a potential energy resource in the future. However, hydrate production is a complex process involving phase transition, multiphase flow, mass transfer, heat transfer, and reservoir deformation [5]. Thus, investigations into safe and efficient hydrate production from HBS have been widely carried out.

In-situ dissociation is proposed as a feasible and effective method for hydrate production. First, NGH is dissociated by depressurization, thermal stimulation, and inhibitor injection, after which hydrate-dissociated fluids are transported to the surface. During these two processes, HBS permeability is a crucial factor that controls fluid (water or gas) mobility and the ability to transmit pressure and temperature in the reservoir, which affects hydrate productivity [6, 7]. However, HBS permeability varies in hydrate production. Hydrate dissociation releases pore space and changes pore shape, thereby affecting reservoir permeability [8]. Therefore, it is vital to study the permeability change of the reservoir during hydrate exploitation [9]. In addition, in a multiphase flow system, rock fluids interfere with each other due to their different physical and chemical properties at the interface.
This interference can be described by relative permeability, related to the saturation of each phase. In other words, relative permeability can better reflect the flowability of fluids in HBS.

The research on gas hydrate permeability focuses mainly on the absolute permeability of sediments and the relative permeability of gas and water. The former employs single-phase fluid for assessing absolute permeability while the latter considers the complex flow behavior of two-phase fluids. However, the study of gas/water relative permeability, a multiphase flow system, is more complicated. The existing empirical relative permeability calculation models, such as the Modified Stone model and van Genuchten model, provide only the relationship between the relative permeability of each phase and phase saturation, without considering the secondary influence of NGH dissociation [10, 11]. In addition, the previous experimental studies related to permeability mainly focused on absolute permeability. In contrast, no experiments on the relative permeability of gas and water have been done to our best knowledge [12–15].

As an alternative to laboratory experiments, pore network simulation is currently and widely used to study gas/water relative permeability by fitting it with empirical data [16–20]. However, pore network simulation is still insufficient to describe the flow mechanism of multiphase fluids, such as viscous coupling. This model’s simplified porous media structure may also lead to microscopic porosity information loss [21]. Recently, Singh et al. proposed two models that consider and neglect capillary pressure, respectively [22, 23]. These models aid in studying the gas-water multiphase seepage mechanism, but the simplified pore-scale morphology in their derivation may deviate from the actual situation.

To better simulate the fluid flow properties and complex pore geometry in HBS, a more accurate pore-scale microsimulation is required. As a mesoscopic simulation method, the Lattice Boltzmann Method (LBM) has been widely used in the past two decades for porous media, multiphase, and multiphase flow, chemical reaction, and microscale gas flow [24]. The LBM has a strict microtheoretical basis and some advantages, such as model simplification, ease of handling complex geometry boundary, and good parallelism [25, 26]. However, like laboratory experiments, previous LBM studies of hydrate production have focused on the flow simulation of single-phase fluid, studying the evolution of absolute permeability varies with hydrate saturation [21, 27–30]. Some studies on multiphase flow have considered the effect of capillary number, viscosity ratio, wettability, and fluid distribution on relative permeability [31–33]. So far, the LBM has not been used to study the multiphase flow of gas and water in HBS.

The current study used the LBM of multiphase (MCMC) pseudopotential model to simulate fluid dual-phase flow in HBS [34]. To effectively simulate fluids’ properties, the Laplace test and contact angle test were used to determine the fluids’ actual density ratio, viscosity ratio, and wettability. Then, a two-dimensional, two-phase Poiseuille flow simulation was applied to verify the model. Finally, the MCMC model was used to study the gas/water dual-phase flow in the reservoir with a particle-filled hydrate for 0.2 saturation. In addition, the evolution characteristics of gas and water relative permeability under different hydrate saturation and hydrate pore habit were discussed to derive the influence of NGH on the multiphase flow.

2. Model and Method

2.1. Multiphase Flow Simulation. The adopted MCMC Shan-Chen model studies the water and methane immiscible two-phase flow in 2D porous media [35]. The LBM model simulates fluid flow, using the collision and migration of the particle distribution function, \( f^\sigma_i(x, t) \) for a set of discrete velocities, \( e_i \), at the lattice site, \( x \), and time, \( t \). The indices, \( \sigma \), and subscript, \( i \), label the fluid component and discrete velocity direction, respectively. In this study, the Bhatnagar-Gross-Krook model was used, and the evolution equation for \( \sigma \) component is described by:

\[
f^\sigma_i (x + e_i \Delta t, t+\Delta t) - f^\sigma_i (x, t) = -\frac{1}{\tau^\sigma} (f^\sigma_i (x, t) - f^\sigma_i (x, t)) + F^\sigma,
\]

where \( \tau^\sigma \) is the nondimensional relaxation time, related to the kinematic viscosity \( (\nu^\sigma = c^\sigma (\sigma^\nu - 0.5) \Delta t) \), \( \Delta t \) is the time step (i.e., 1), and \( F^\sigma \) is the forcing term for the \( \sigma \) component. The discrete velocity, \( e_i \), along the \( i \) direction for \( D_2Q_6 \) lattice model here is written as [36]

\[
\begin{bmatrix}
0 & 1 & 0 & 1 & 0 & 1 & -1 & -1 \\
1 & 0 & 0 & 1 & 1 & 1 & -1 & -1 \\
0 & 0 & 0 & 1 & 1 & 1 & -1 & -1
\end{bmatrix}.
\]

(2)

The equilibrium distribution function \( f^\sigma_{eq}(x, t) \) discretized from Maxwell-Boltzmann equilibrium distribution is given by:

\[
f^\sigma_{eq} = \omega_i \rho \sigma \left[ 1 + \frac{e_i \cdot u^\sigma}{c_i^2} + \frac{(e_i \cdot u^\sigma)^2}{2c_i^4} - \frac{(u^\sigma)^2}{2c_i^2} \right],
\]

(3)

where for the \( D_2Q_6 \) lattice model, weight, \( \omega_i \), is determined as \( \omega_0 = 4/9, \omega_{1,4} = 1/9, \) and \( \omega_{5,8} = 1/36. \) The variable \( c_i \), is the speed of sound \( (c_i = (\Delta x/\Delta t) / \sqrt{3}), \) while \( \rho \sigma \) is the fluid density, obtained as \( \rho \sigma = \sum f^\sigma_i \).

In the pseudopotential model, the phase separation of the fluid system is due to molecular forces. For the MCMC model, intramolecule force and intermolecule force exist, with the former expressed as:

\[
F_{\sigma \sigma} = -G_{\sigma \sigma} \varphi \sigma (x) c^2 \sum_{i=1}^{N} w(|e_i|^2) \varphi \sigma (x + e_i) e_i,
\]

(4)
where \( G_{e,\sigma} \) is the intramolecule interaction strength and \( \varphi_{\sigma}(x) \) is the effective mass on \( x \) site. In our MCMP model, two layers of neighboring nodes are used to calculate the two forces. In one layer of adjacent nodes (Figure 1(a)), only the nearest nodes (nodes 1, 2, 3, and 4) and next-nearest nodes (nodes 5, 6, 7, and 8) are used to calculate the molecular force. This model can lead to the fourth isotropy order (E4). However, two layers of neighboring nodes (Figure 1(b)), with 24 nodes, can reach the eighth isotropy order (E8). Compared with the former, the two layers of neighboring nodes can reduce the spurious currents at the interface and improve model stability [37]. The weight coefficients of the two layers of neighboring nodes are listed in Table 1.

The intermolecular force between different fluids can enhance the mutual diffusivity [39]. This force is expressed as:

\[
F_{e,\sigma} = -G_{e,\sigma}^2 \varphi_{\sigma}(x) \sum_{i=1}^{N} w(|\epsilon_i|^2) \varphi_{\sigma}(x + \epsilon_i) \epsilon_i, \tag{5}
\]

where \( G_{e,\sigma}^2 \) is the intermolecule force strength, while \( G_{e,\sigma} \) = \( G_{e,\sigma} = 0.5 \) [40]. Here, we studied two components: \( \sigma = 1 \) and \( \sigma = 2 \) represent the water and methane phases, respectively. Methane is regarded as an ideal fluid; thus, \( G_{2,2} = 0 \). On the other hand, water is a nonideal fluid, and the Carnahan-Starling (C-S) equation of state is adopted [41]:

\[
P = \rho RT \frac{1 + b \rho/4 + (b \rho/4)^2 - (b \rho/4)^3}{(1 - b \rho/4)^3} - a \rho^2, \tag{6}
\]

where the critical parameters of the C-S equation of state are as follows: \( a = 0.4963 R T_c^2 / P_c \) and \( b = 0.18727 R T_c / P_c \). We set \( a = 1 \), \( b = 4 \), and \( R = 1 \). To solve the equation of state, we obtained the critical density \( \rho_c \) and critical temperature \( T_c \) as 0.13045 and 0.0943, respectively [40]. The effective mass of water component \( \varphi_1(x) \) is given as:

\[
\varphi_1(x) = \sqrt{\frac{2(P(x) - c_i^2 \rho(x))}{G_{1,1}}}. \tag{7}
\]

When Equation (6) is substituted into Equation (7), the \( G_{1,1} \) cancels out. Hence, the \( G_{1,1} \) value only ensures that square-rooted components of Equation (7) are positive. In addition, the effective mass of methane \( \varphi_2(x) \) is given by:

\[
\varphi_2(x) = \rho_0 \left(1 - \exp \left(\frac{\rho_2(x)}{\rho_0}\right)\right), \tag{8}
\]

where \( \rho_0 \) is a constant coefficient, set as 1, and \( \rho_2(x) \) is methane density.

To simulate the wettability of each component toward the solid phase, the force of fluids-to-solid \( F_{ads} \) is calculated. In this study, water and methane were set as wetting and nonwetting fluids, respectively. However, their wettability to the hydrate lack reference data. Thus, we assumed that the fluids have the same wettability to hydrate and solid particles, as follows:

\[
F_{ads} = -G_{e,\sigma}^2 \varphi_{\sigma}(x) \sum_{i=1}^{N} w(|\epsilon_i|^2) \varphi_{\sigma}(x + \epsilon_i) \epsilon_i, \tag{9}
\]

where \( G_{e,5} \) is the controlling parameters for the interface strength between each fluid and the solid. Also, we set \( G_{1,5} = -1 \) and \( G_{2,5} = 1 \). \( \varphi_1(x + \epsilon_i) \) is the effective mass of solid used to adjust contact angle.

The body force \( \mathbf{G} \), a steady external force corresponding to the pressure gradient, is used to drive the fluid flow. The effect of gravity on fluid flow was not considered here. Thus, all forces acting on each component can be given as:
where \( u_{\text{eq}} \) and \( \Delta u \) are the velocity at each grid point at the saturation is used as the reference permeability. Equation (15) calculates the relative permeability:

\[
F_{\sigma} = F_{\sigma,\sigma} + F_{\sigma,k} + F_{\text{adv}} + G.
\]  

Here, the exact difference method (EDM) leads to relaxation time independence and has a relatively wide temperature range [42]. The EDM scheme can implement all forces into the LBM framework for a force term in Equation (1). The force term in the evolution equation is expressed as [43]:

\[
F_i = f_i^{\sigma eq}(\rho_\sigma, u^{eq} + \Delta u_\sigma) - f_i^{\text{eq}}(\rho_\sigma, u^{eq}),
\]

where \( u^{eq} \) and \( \Delta u_\sigma \) can be written as:

\[
u^{eq} = \sum_\alpha \rho_\alpha u_\alpha,
\]

\[
\Delta u_\sigma = \frac{F_\sigma \Delta t}{P_\sigma}.
\]

In the simulation, the velocity of each component and pressure can be calculated by Equations (13) and (14), respectively:

\[
u_\alpha = \sum_{i=1}^{N} f_i^{\sigma eq} \rho_\sigma + \frac{F_\sigma \Delta t}{2 P_\sigma},
\]

\[
P = \frac{\sum_\alpha \rho_\alpha}{2} + \sum_\alpha \frac{1}{2} [G_\alpha \sigma (\phi_\sigma^2) + G_\alpha \sigma \phi_\sigma \phi_\sigma^2 + G_\alpha \sigma \phi_\sigma \phi_\sigma^2 + G_\alpha \sigma (\phi_\sigma^2)^2].
\]

2.2. Model Parameters. To fit the actual properties of the fluids, their physical parameters (such as density and viscosity) were predetermined. However, these parameters, especially for the gas, are affected by pressure and temperature. In HBS, the pressure is much higher than the standard atmospheric pressure, resulting in higher density and viscosity. For example, the temperature and pressure in the South China Sea are approximately 14°C and 14 MPa, respectively. Assuming the pressure reduction method is used for hydrate exploitation, and the pressure reduces to 5 MPa, the resulting gas and water physical parameters are given in Table 2 (the data refer to AP1700 Material Property Calculation Query Platform).

2.3. Calculation of Relative Permeability. The relative permeability of water \( k_{w,\sigma} \) (or gas, \( k_{g,\sigma} \)) is the water (or gas) effective permeability at a given water saturation \( S_w \), normalized by

\[
\begin{tabular}{|c|c|c|c|}
\hline
Physical parameters & Water & Methane & Ratio \\
\hline
Density \( \rho \) (kg/m\(^3\)) & 1001.5 & 37.2 & 26.9 \\
Dynamic viscosity \( \mu \) (Pa \( \cdot \) s) & \( 1.16 \times 10^{-3} \) & \( 1.20 \times 10^{-3} \) & 96.7 \\
Kinetic viscosity \( \nu \) (m/s\(^2\)) & \( 1.16 \times 10^{-6} \) & \( 3.23 \times 10^{-7} \) & 3.6 \\
Surface tension \( \sigma \) (N/m) & 0.0736 & & \\
\hline
\end{tabular}
\]

2.3. Calculation of Relative Permeability.
Figure 2 shows 2D porous media, including hydrate. The hydrate pore habit of pore-filling and hydrate saturation of $S_h = 0.2$ is an example. In this model, the computational domain was a $360 \times 360$ lattice system, and the porosity (except hydrate) was 0.65. Solids are composed of similar round particles with a radius of 28 lattices.

The periodic boundary conditions were applied in all directions. The gas and water phases were initially distributed randomly in the pores, and the phase separation occurs automatically. After the phase separation reaches a steady state, the driving force is used to drive two-phase fluid flow from left to right, and then, the outflow flux of each fluid is calculated. Finally, the relative permeability of each phase can be determined from the above equations.

In the simulation, it is tedious to find a fixed value for the driving force $G$ because the viscosity of gas and water is widely different. For example, $G$ is larger for gas flow, disobeying Darcy’s law, while the same $G$ value is smaller for water flow and cannot overcome capillary pressure. Thus, we assume that the effect of capillary number on relative permeability can be negligible, and the $G$ value is changeable. In our simulation, the flow flux may change with time because in gas/water flow system, each phase is usually discontinuous and unsteady. Therefore, every simulation required more than 100000 steps to lower the error in flow flux count.

2.4. Model Validation. After the model is determined, the fluid-fluid interaction and the fluid wettability onto the solid should be validated by the Laplace test and contact angle test, respectively. Then, the 2D two-phase Poiseuille flow is simulated to validate that the relative permeability meets the analytical solution.

2.4.1. Laplace Test. The Laplace test was conducted by placing a droplet with different initial radii $R$ at the center of the lattice domain composed of a $150 \times 150$ lattice system. Besides, the periodic boundary condition was applied to the surrounding boundary. Initially, the temperature was set as $0.75 T_m$, and the density of water (gas) was set as 0.34 (0.0001) and 0.0001 (0.012) for the inside and outside the droplet, respectively, equaling the physical density ratio. To correspond with the kinematic viscosity ratio, the liquid phase and gas phase relaxation times were set as $\tau_v = 1.2$ and $\tau_g = 0.7$, respectively. Provided the density and kinetic viscosity ratios are achieved, the dynamic viscosity is also achievable. Figure 3 shows the density distribution of methane and water along the centerline of the droplet when a steady droplet of water resides within the gas. With the pressure difference between the inside and outside of the droplet and the radii $R$, the surface tension can be determined by Laplace’s law:

$$\Delta P = \frac{\sigma}{R}.$$  \hfill (18)

This relationship implies that $\Delta P$ varies linearly to $1/R$. The proportionality coefficient $\sigma$ is the interfacial tension.

Figure 4 depicts $\Delta P$ as a function of $1/R$ where the linear fit shows that the surface tension and $\sigma$ in the model was 0.0174.

2.4.2. Contact Angle Test. The fluids’ spread on the solid surface can inform on their wettability onto the solid. It depends on the static contact angle $\theta$. For $\theta < 90^\circ$, the fluid tends to wet the solid surface, i.e., a wetting fluid. On the other hand, when $\theta > 90^\circ$, the fluid alienates the solid surfaces, i.e., a nonwetting fluid. The contact angle between the fluids and the surface can be calculated through Young’s equation, which gives the relationship between the interfacial tension $\gamma_{12}$ for fluid-fluid and the interfacial tension $\gamma_{11}$ and $\gamma_{22}$ for fluids-solid. The Young’s equation is given by:

$$\cos \theta = \frac{\gamma_{12} - \gamma_{11}}{\gamma_{12}}.$$  \hfill (19)
Recollect that the gas and the water were set as nonwetting fluid and wetting fluid, respectively. In the MCMP Shan-Chen model, the contact angle is controlled by both fluids near the solid-fluid interface. However, the coefficients are weak for the high-density ratio MCMP model, and the high-density fluid mainly controls the contact angle [34].

Like single component multiphase Shan-Chen model, different static contact angles \( \theta \) can be achieved by changing the effective solid mass \( \phi_s \). To simulate different contact angles, a 140 × 100 lattice system with a solid wall at the bottom of the domain was considered. Figure 5 shows the contact angle tests for water. Finally, \( \theta = 15^\circ \) was chosen for the final simulation.

**2.4.3. Two-Dimensional, Two-Phase Poiseuille Flow.** For immiscible, two-phase flows in a 2D channel, the analytical solutions of speed and relative permeability for each component can be solved by Navier–Stokes equations. Typically, the wetting fluid covers and moves along the solid surface, while the nonwetting fluid flows in the channel center (Figure 6). The saturation of each fluid can be defined as the occupied width normalized by the entire width of the channel. The relative permeability of the nonwetting fluid in the center of the channel is affected by the viscosity ratio, \( M = \frac{\mu_{nw}}{\mu_w} \), where \( \mu_{nw} \) and \( \mu_w \) are the
viscosity of the nonwetting fluid and wetting fluid, respectively).

Huang et al. proposed analytical solutions for each fluid relative permeability as follows [44]:

\[
k_{rw} = \frac{1}{2} S_w^2 (3 - S_w),
\]

\[
k_{rnw} = (1 - S_w) \left[ \frac{3}{2} M + (1 - S_w)^2 \left( 1 - \frac{3}{2} M \right) \right].
\]

To simulate the Poiseuille flow and validate the simulation results, a 240 × 180 lattice network was established. The no-slip boundary condition was used at the top and bottom of the domain, while the periodic boundary condition was used for the left and right sides. A two-phase cocurrent flow was driven by the body force \((G = 5 \times 10^{-9})\). Figure 7

**Figure 8: Gas-water dual-phase distribution patterns in HBS.** The gas is shown as blue, water as light green, solid particles as orange, and hydrate as red. \(S_w = 0.2\), pore-filling.

![Gas-water dual-phase distribution patterns in HBS](image)

**Figure 9: Relative permeability for gas \((k_{rg})\) and water \((k_{rw})\) as a function of water saturation \((S_w)\).**

![Relative permeability graph](image)
illustrates the results of numerical simulations and analytical solutions, with a good agreement.

3. Simulation Results

3.1. Gas and Water Phase Distribution Patterns in HBS.

Figure 8 depicts gas-water phase distribution patterns in HBS as the water saturation $S_w$ changes. Under low water saturation conditions, the water phase is discontinuous, covering the surface of the solid particles and hydrate due to the wettability (Figures 8(a) and 8(b)). However, the gas phase is continuous and flows through the sediments. As the water phase saturation increases (Figure 8(c)), a minute volume of water gradually flows through the sediments. Moreover, the continuous gas phase tends to break up. In our simulation, the water saturation of 0.45 is approximately the dividing point between the continuous and discontinuous gas phases.

At $S_w = 0.56$, 0.68, and 0.84 (Figures 4(d)–4(f)), the water gradually flows continuously while the gas is disconnected, forming bubbles. Compared with the single gas-phase flow with the same driving force, the gas bubbles flow slowly because of the blockage caused by the relatively higher viscosity water.

3.2. Gas and Water Relative Permeability. Figure 9 shows the relative permeability of gas ($k_{rg}$) and water ($k_{rw}$) as a function of water saturation ($S_w$). The red and green lines represent $k_{rg}$ and $k_{rw}$, respectively. When the water phase saturation is <0.2, the water relative permeability ($k_{rw}$) is ≈0. At this time, water is bound to the solid surface and cannot flow. Therefore, it can be considered that $S_w = 0.2$ is the residual water saturation under the conditions of our model. When $0.2 < S_w < 0.45$, water starts to flow, although slowly due to lack of a continuous flow path. However, when $S_w > 0.45$, the flow velocity increases significantly as a continuous flow path gradually forms. Finally, the $k_{rw}$ approaches 1 until water fills the entire pore space.

Unlike water relative permeability, the $k_{rg}$ decreases with an increase in water saturation. Moreover, when the water saturation is <0.45, the decay rate of the gas relative permeability becomes higher than when the water saturation is >0.45. The following points explain this phenomenon: (a) When the water phase saturation is below the dividing point, the residual water is absorbed on the solid surface and remains immobile. The remaining part of the water flows gently due to the lack of a continuous flow path. In addition, water viscosity is much higher than that of a gas. Due to these reasons, the flow velocity of water is much slower than that of gas. Thus, for the gas phase, increasing water saturation means occupying more pore space. Therefore, the water phase is nearly stagnant and impedes (similar to solid particles) the gas flow. (b) As the water phase saturation exceeds the dividing point, the gas gradually becomes bubbles mixed in the water flow. Here, the gas flow rate gradually matches with the water flow rate. Meanwhile, the water flow has a relatively higher velocity at $S_w > 0.45$, which offsets some
negative effects of increasing water saturation on the gas flow rate. Therefore, when the water saturation is >0.45, the gas relative permeability gradually decreases, changing almost linearly with water saturation.

3.3. The Main Influence Factors of Gas/Water Relative Permeability. From the gas/water phase distributions and their relative permeability, we observed that high viscosity water consistently and strongly obstructed the gas flow during the entire gas/water multiphase flow. In addition, capillary force is also not conducive to the gas flow. On the contrary, low viscosity gas cannot have a significant inhibitory effect on water flow. The water flow is mainly controlled by the coadsorption of solid particles and hydrates. The $S_w$ at the dividing point is crucial for gas/water relative permeability. For example, the gas phase is continuous at the left side of the dividing point, and the flow velocity is high. However, the water is coadsorbed by the solid particles and hydrate, thereby hindering its movement. Despite that, part of the water beyond the residual water saturation could move; the movement is slow because there is no continuous flow path. On the contrary, gas forms bubbles blocked by water molecules at the right side of the dividing point. However, water’s continuous flow path gradually appears and causes the water flow speed to improve rapidly. This dividing point is for gas; it does not mean water forms a continuous flow path immediately when its saturation is beyond the gas dividing point. The dividing point for water to have a continuous flow path is hard to determine. Therefore, if $S_w$ for the dividing point changes, the relative permeability of gas and water would change.

Near the dividing point, the gas relative permeability is always <0.01 because of the 96 times difference in the viscosity of gas and water in our model. As mentioned earlier, the gas changes into bubbles mixed in the water, and its flow rate gradually matches that of the water. However, the water flow rate is 96 times different from that of the gas (single-phase) flow rate under the same driving force. Therefore, the gas relative permeability is always <0.01 if water saturation exceeds the dividing point.

4. Discussion

The simulation results show the evolution of gas/water relative permeability, and their phase distributions vary with water saturation under a certain hydrate saturation and hydrate pore habit. However, the hydrate dissociation may bring changes to the microscopic pore structure of sediments, which affects the fluid microseepage behavior and their relative permeability evolution. To analyze the influence of hydrate growth behavior (i.e., saturation and pore habit) on gas and water relative permeability, we simulated the multiphase flow behaviors at $S_h=0.2$, 0.4, and 0.6 and the hydrate pore habit of grain-coating and pore-filling.

4.1. Effect of Hydrate Saturation on Gas/Water Relative Permeability. Figure 10 shows gas-water dual-phase distribution patterns in HBS with 0.4 and 0.6 hydrate saturation.
for the hydrate pore habit of pore-filling, respectively. As the hydrate saturation increases, the fluid distribution patterns change in the following aspects: (a) Gas phase is more likely to exist as bubbles and challenging to overcome capillary resistance. Moreover, the gas phase is more likely to change from continuous to discontinuous as hydrate saturation increases under the same water saturation conditions. (b) The dividing point between the continuous and discontinuous gas phases changes from 0.45 to 0.30 as the hydrate saturation increases from 0.2 to 0.6 (Figure 10(a)). (c) More water molecules are bound to the solid surface, thereby increasing residual water saturation. However, once a continuous flow path has been established for the water phase, the flow velocity increases rapidly and is less affected by external factors. (d) The gas bubbles which could flow gradually become residual gas as hydrate saturation increases (Figure 10(c)). In general, the increased hydrate saturation hinders the fluid flow. However, water flow is less affected by hydrate saturation than gas flow.

The evolution of gas/water relative permeability caused by different hydrate saturation is shown in Figure 11. The black spot is the pore network simulation reported by Mahabadi et al. [17], the green spot is the analysis model studied by Singh et al. [23], and the solid red line is from the current research using the LBM. We observed that the simulation result of the present study matches with the analysis model but with a slight deviation from the pore network model. In pore network simulation, the relative permeability, especially gas relative permeability, is higher than that of the other two methods. It may be because the pore network simulation is difficult to capture the viscous interaction between different fluids, ignoring the obstructive effect of water on gas.

Furthermore, we observed (Figure 12) that the gas relative permeability ($k_{rg}$) reduces as hydrate saturation increases. As the hydrate saturation increases from 0.2 to 0.6, the gas relative permeability trend shrinks toward the left. In these
4.2. Effect of Hydrate Pore Habit on Gas/Water Relative Permeability. This section analyzes the effect of hydrate pore habit on gas/water relative permeability evolution behaviors. The two-phase distribution patterns for hydrate pore habit of grain-coating are shown in Figure 12. Compared with Figure 10, the hydrate pore habit of grain-coating also encounters obstacles on the fluid flow, like pore-filling. However, the extent of influence on gas/water seepage characteristics between these two habits is unclear from these phase distribution patterns.

Figure 13 shows the comparison of gas and water relative permeability in their hydrate pore habits. The red and blue lines show the pore habits of pore-filling and grain-coating, respectively. Except for $S_h = 0.4$ and $S_w > 0.5$, the gas relative permeability for grain-coating is almost higher than that of pore-filling. Because the hydrate occupied the center of pores in the pore-filling, the pores shrink than that of grain-coating, and a more prominent obstacle to the gas flow occurred. The case of $S_h = 0.4$ and $S_w > 0.5$ appearing is an abnormal situation. This scenario is due to the pore habit of grain-coating, forming larger pores than that of pore-filling, which causes gas bubbles to become residual gas more easily. However, the gas relative permeability for the hydrate pore habit of grain-coating is generally higher than that of pore-filling. However, for water relative permeability, the trends of the hydrate types are similar to hydrate saturation, increasing from 0.2 to 0.6. Therefore, the hydrate pore habit has the same effect on water relative permeability.

The hydrate pore habit has the same effect on water relative permeability because the water seepage can only be affected by hydrates when water saturation is low. Regardless, the pore-filling and grain-coating have a strong adsorption effect on water flow in low water saturation conditions. Moreover, the two types of hydrate pore habits have little difference in the residual water saturation and the water saturation required to form a continuous flow path.
In high water saturation conditions, as long as the continuous flow path for water has been formed, hydrate pore habit and hydrate saturation cannot significantly influence the water relative permeability. On the contrary, gas relative permeability is mainly influenced by viscous coupling between gas and water, capillary resistance, and residual gas saturation. Although pore-filling cannot induce more residual gas, it, however, causes pore thinning. Therefore, this form of pore-filling causes more immense capillary pressure and makes more gas form discrete bubbles. For these reasons, gas relative permeability for the pore habit of pore-filling is always lower than the pore habit of grain-coating.

5. Conclusion

We used LBM to study the effect of hydrate on gas/water relative permeability. Gas and water multiphase flows for the hydrate saturation of \( S_w = 0.2, 0.4, \) and 0.6, with the hydrate pore habit of grain-coating and pore-filling, are simulated, and their relative permeability is analyzed. The main conclusions are as follows:

(1) Our research has the same trend as these two methods compared to the pore network simulation and analysis model. This observation shows that the LBM is valid in simulating gas and water multiphase flow in HBS.

(2) During the multiphase flow process of gas and water, high viscosity water has a strong, obstructive effect on gas flow due to the viscous coupling, but the gas phase has little effect on water flow. The water flow is mainly controlled by the coadsorption of solid particles and hydrates. Whether the water forms a continuous flow path is another critical factor. In our model, the corresponding water saturation \( S_w \) of the dividing point is approximately 0.45 when hydrate saturation is 0.20. On the left side of the dividing point, the gas relative permeability quickly decreases from 1 to 0.01. In contrast, the water relative permeability starts as water saturation exceeds 0.2, but it is usually <0.1. On the right side of the dividing point, the gas relative permeability decreases gradually from 0.01 to 0, while the water relative permeability quickly increases from 0.1 to 1.

(3) Gas and water multiphase seepage becomes more difficult as hydrate saturation increases, and their relative permeability decreases. There are three main reasons for the decrease in gas relative permeability: (i) The dividing water saturation \( S_w \) between continuous and discontinuous for the gas phase decreases. In our simulation, as hydrate saturation increases from 0.2 to 0.6, the dividing water saturation \( S_w \) decreases from 0.45 to 0.30. (ii) Increased hydrate saturation causes pores to narrow, thus resulting in an enormous capillary resistance. (iii) Mobile gas bubbles gradually become residual gas as hydrate saturation increases. As hydrate saturation increases from 0.2 to 0.6, the residual gas saturation increases from 0 to 0.2. Moreover, the reduction of water relative permeability is mainly due to the coadsorption of solid particles and hydrates. The coadsorption increases the water saturation required for initial water flow and the water saturation required to form a continuous flow path. As hydrate saturation increases from 0.2 to 0.6, the residual water saturation increases from 0.2 to 0.3.

(4) For different hydrate pore habits, the gas relative permeability for pore-filling is lower than that of grain-coating because hydrate occupied in the center of pores thins the pore further. However, the water relative permeability is less affected by the hydrate pore habit.

Data Availability

The data is available at https://edx.netl.doe.gov/dataset/mrpc.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

Acknowledgments

This work was supported by the Jilin Scientific and Technological Development Program (No. 20190303083SF), the National Natural Science Foundation of China (No. 41877185), the International Cooperation Key Laboratory of Underground Energy Development and Geological Restoration (No. YDZ[202102CXMID014), and the National Key Research and Development Program of China (No. 2017YFC0307304).

References

[1] P. Wu, Y. H. Li, X. Sun, W. G. Liu, and Y. C. Song, "Mechanical characteristics of hydrate-bearing sediment: a review," *Energy & Fuels*, vol. 35, no. 2, pp. 1041–1057, 2021.
[2] E. D. Sloan, "Fundamental principles and applications of natural gas hydrates," *Nature*, vol. 426, no. 6964, pp. 353–359, 2003.
[3] B. A. Buffett, "Clathrate hydrates," *Annual Review of Earth Planetary Science*, vol. 28, no. 1, pp. 477–507, 2000.
[4] J. Joseph, D. N. Singh, P. Kumar, S. K. Dewri, C. Tandi, and J. Singh, "State-of-the-art of gas hydrates and relative permeability of hydrate bearing sediments," *Marine Georesources & Geotechnology*, vol. 34, no. 5, pp. 450–464, 2016.
[5] X. H. Zhang, X. B. Lu, and Q. P. Li, "Formation of layered fracture and outburst during gas hydrate dissociation," *Journal of Petroleum Science and Engineering*, vol. 76, no. 3–4, pp. 212–216, 2011.
[6] L. Wang, X. Sun, S. Shen et al., "Undrained triaxial tests on water-saturated methane hydrate-bearing clayey-silty sediments of the South China Sea," *Canadian Geotechnical Journal*, vol. 58, no. 3, pp. 351–366, 2021.
[7] Y. H. Li, P. Wu, X. Sun, W. G. Liu, and Y. C. Song, "Mechanical behaviors of hydrate-bearing sediment with different
cementation spatial distributions at microscales,” *iScience*, vol. 24, no. 5, p. 102448, 2021.

[8] W. F. Waite, J. C. Santamarina, D. D. Cortes et al., “Physical properties of hydrate-bearing sediments,” *Reviews of Geophysics*, vol. 47, no. 4, 2009.

[9] J. C. Cai and X. Y. Hu, “Petrophysical characterization and fluids transport in unconventional reservoirs,” *Fuel*, vol. 248, pp. 278-279, 2019.

[10] R. H. Brooks and A. T. Corey, *Hydraulic Properties of Porous Media*, Colorado State University, 1964.

[11] M. T. van Genuchten, “A closed-form equation for predicting the hydraulic conductivity of unsaturated soils,” *Soil Science Society of America Journal*, vol. 44, no. 5, pp. 892–898, 1980.

[12] H. Liang, Y. Song, Y. Chen, and Y. Liu, “The measurement of permeability of porous media with methane hydrate,” *Petroleum Science and Technology*, vol. 29, no. 1, pp. 79–87, 2011.

[13] T. J. Kneasfey, Y. Seol, A. Gupta, and L. Tomutsa, “Permeability of laboratory-formed methane-hydrate-bearing Sand: measurements and observations using X-ray computed tomography,” *SPE Journal*, vol. 16, no. 1, pp. 78–94, 2011.

[14] M. L. Delli and J. L. H. Grozic, “Experimental determination of permeability of porous media in the presence of gas hydrates,” *Journal of Petroleum Science and Engineering*, vol. 120, pp. 1–9, 2014.

[15] A. Johnson, S. Patil, and A. Dandekar, “Experimental investigation of gas-water relative permeability for gas-hydrate-bearing sediments from the Mount Elbert Gas Hydrate Stratigraphic Test Well, Alaska North Slope,” *Marine and Petroleum Geology*, vol. 28, no. 2, pp. 419–426, 2011.

[16] N. Mahabadi and J. Jang, “Relative water and gas permeability for gas production from hydrate-bearing sediments,” *Geochemistry, Geophysics, Geosystems*, vol. 15, no. 6, pp. 2346–2353, 2014.

[17] N. Mahabadi, S. Dai, Y. Seol, T. Sup Yun, and J. Jang, “The water retention curve and relative permeability for gas production from hydrate-bearing sediments: pore-network model simulation,” *Geochemistry, Geophysics, Geosystems*, vol. 17, no. 8, pp. 3099–3110, 2016.

[18] J. Wang, J. Zhao, M. Yang, Y. H. Li, W. G. Liu, and Y. C. Song, “Permeability of laboratory-formed porous media containing methane hydrate: observations using X-ray computed tomography and simulations with pore network models,” *Fuel*, vol. 145, pp. 170–179, 2015.

[19] L. Ai, J. Zhao, J. Wang, and Y. Song, “Analyzing permeability of the irregular porous media containing methane hydrate using pore network model combined with CT,” *Energy Procedia*, vol. 105, pp. 4802–4807, 2017.

[20] N. Mahabadi, X. Zheng, and J. Jang, “The effect of hydrate saturation on water retention curves in hydrate-bearing sediments,” *Geophysical Research Letters*, vol. 43, no. 9, pp. 4279–4287, 2016.

[21] J. Hou, Y. Ji, K. Zhou, Y. Liu, and B. Wei, “Effect of hydrate on permeability in porous media: pore-scale micro-simulation,” *International Journal of Heat and Mass Transfer*, vol. 126, pp. 416–424, 2018.

[22] H. Sing, E. M. Myshakin, and Y. Seol, “A nonempirical relative permeability model for hydrate-bearing sediments,” *SPE Journal*, vol. 24, no. 2, pp. 547–562, 2019.

[23] H. Singh, N. Mahabadi, E. M. Myshakin, and Y. Seol, “A mechanistic model for relative permeability of gas and water flow in hydrate-bearing porous media with capillarity,” *Water Resources Research*, vol. 55, no. 4, pp. 3414–3432, 2019.

[24] L. Chen, Q. Kang, Y. Mu, Y.-L. He, and W.-Q. Tao, “A critical review of the pseudopotential multiphase lattice Boltzmann model: methods and applications,” *International Journal of Heat and Mass Transfer*, vol. 76, pp. 210–236, 2014.

[25] H. Liu, Q. Kang, C. R. Leonardi et al., “Multiphase lattice Boltzmann simulations for porous media applications,” *Computational Geosciences*, vol. 20, no. 4, pp. 777–805, 2016.

[26] D. Zhi and F. Z. Zhi, “Numerical study of non-uniqueness of the factors influencing relative permeability in heterogeneous porous media by lattice Boltzmann method,” *International Journal of Heat and Fluid Flow*, vol. 42, no. 13, pp. 23–32, 2013.

[27] D. H. Kang, T. S. Yun, K. Y. Kim, and J. Jang, “Effect of hydrate nucleation mechanisms and capillarity on permeability reduction in granular media,” *Geophysical Research Letters*, vol. 43, no. 17, pp. 9018–9025, 2016.

[28] X. Y. Chen, R. Verma, D. N. Espinosa, and M. Prodanović, “Pore-scale determination of gas relative permeability in hydrate-bearing sediments using X-ray computed microtomography and lattice Boltzmann method,” *Water Resources Research*, vol. 54, no. 1, pp. 600–608, 2018.

[29] H. G. Feng, L. X. Qi, and S. Chandan, “2D investigation of water permeability in hydrate-bearing sediment with coexisting hydrate growth habits,” *Journal of Geophysics and Engineering*, vol. 17, no. 4, pp. 567–576, 2020.

[30] J. Sun, H. Dong, M. Arif et al., “Influence of pore structural properties on gas hydrate saturation and permeability: a coupled pore-scale modelling and X-ray computed tomography method,” *Journal of Natural Gas Science and Engineering*, vol. 88, p. 103805, 2021.

[31] A. Ghassemi and A. Pak, “Numerical study of factors influencing relative permeabilities of two immiscible fluids flowing through porous media using lattice Boltzmann method,” *Journal of Petroleum Science and Engineering*, vol. 77, no. 1, pp. 135–145, 2011.

[32] L. H. Na, P. C. Xun, and C. T. Miller, “Pore-scale investigation of viscous coupling effects for two-phase flow in porous media,” *Physical Review E*, vol. 72, no. 2, 2005.

[33] H. H. Bo and L. X. Yun, “Relative permeabilities and coupling effects in steady-state gas-liquid flow in porous media: a lattice Boltzmann study,” *Physics of Fluids*, vol. 21, no. 9, p. 092104, 2009.

[34] J. Bao and L. Schaefer, “Lattice Boltzmann equation model for multi-component multi-phase flow with high density ratios,” *Applied Mathematical Modelling*, vol. 37, no. 4, pp. 1860–1871, 2013.

[35] X. Shan and H. Chen, “Lattice Boltzmann model for simulating flows with multiple phases and components,” *Physical Review E*, vol. 473, pp. 1815–1819, 1993.

[36] Y. H. Qian, D. D’Humieres, and P. Lallemant, “Lattice BGK models for Navier-Stokes equation,” *Europhysics Letters*, vol. 17, no. 6, pp. 479–484, 1992.

[37] X. W. Shan, “Analysis and reduction of the spurious current in a class of multiphase lattice Boltzmann models,” *Physical Review E*, vol. 73, no. 4, 2006.

[38] Q. Y. Zhang, D. K. Sun, and M. F. Zhu, “A multiphase lattice Boltzmann model with large liquid–gas density ratios for simulations of wetting phenomena,” *Chinese Physics B*, vol. 26, no. 8, 2017.
[39] Y. Zhao, *A Novel Lattice Boltzmann Method for Direct Numerical Simulation of Multiphase Flows*, The Ohio State University, 2009.

[40] W. B. Zhu, M. Wang, and H. Chen, “Study on multicomponent pseudopotential model with large density ratio and heat transfer,” vol. 87, pp. 183–191, 2017.

[41] P. Yuan and L. Schaefer, “Equations of state in a lattice Boltzmann model,” *Physics of Fluids*, vol. 18, no. 4, p. 042101, 2006.

[42] Q. Li, H. K. Luo, and X. J. Li, “Forcing scheme in pseudopotential lattice Boltzmann model for multiphase flows,” *Physical Review E*, vol. 86, no. 1, 2012.

[43] A. L. Kupersh tokh, D. A. Medvedev, and D. I. Karpov, “On equations of state in a lattice Boltzmann method,” *Computers and Mathematics with Applications*, vol. 58, no. 5, pp. 965–974, 2009.

[44] H. H. Bo, T. L. Zhi, S. Liu, and X. Y. Lu, “Shan-and-Chen-type multiphase lattice Boltzmann study of viscous coupling effects for two-phase flow in porous media,” *International Journal for Numerical Methods in Fluids*, vol. 61, no. 3, pp. 341–354, 2009.