Di-Jet Production in Photon-Photon Collisions at $\sqrt{s_{ee}}$ from 189 to 209 GeV

The OPAL Collaboration

Abstract

Di-jet production is studied in collisions of quasi-real photons at $e^+e^-$ centre-of-mass energies $\sqrt{s_{ee}}$ from 189 to 209 GeV at LEP. The data were collected with the OPAL detector. Jets are reconstructed using an inclusive $k_T$-clustering algorithm for all cross-section measurements presented. A cone jet algorithm is used in addition to study the different structure of the jets resulting from either of the algorithms. The inclusive di-jet cross-section is measured as a function of the mean transverse energy $\bar{E}_T$ of the two leading jets, and as a function of the estimated fraction of the photon momentum carried by the parton entering the hard sub-process, $x_\gamma$, for different regions of $\bar{E}_T$. Angular distributions in di-jet events are measured and used to demonstrate the dominance of quark and gluon initiated processes in different regions of phase space. Furthermore the inclusive di-jet cross-section as a function of $|\eta^{\text{jet}}|$ and $|\Delta\eta^{\text{jet}}|$ is presented, where $\eta^{\text{jet}}$ is the jet pseudo-rapidity. Different regions of the $x_\gamma^+-x_\gamma^-$-space are explored to study and control the influence of an underlying event. The results are compared to next-to-leading order perturbative QCD calculations and to the predictions of the leading order Monte Carlo generator PYTHIA.

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1 Introduction

We have studied the production of di-jets in the collisions of two quasi-real photons at an \(e^+e^-\) centre-of-mass energy \(\sqrt{s_{ee}}\) from 189 to 209 GeV, with a total integrated luminosity of 593 pb\(^{-1}\) collected by the OPAL detector at LEP. Di-jet events are of particular interest, as the two jets can be used to estimate the fraction of the photon momentum participating in the hard interaction, which is a sensitive probe of the structure of the photon. The transverse energy of the jets provides a hard scale that allows such processes to be calculated in perturbative QCD. Fixed order calculations at next-to-leading order (NLO) in the strong coupling constant \(\alpha_s\) for di-jet production are available and are compared to the data, providing tests of the theory. Leading order Monte Carlo (MC) generators are used to estimate the importance of soft processes not included in the NLO calculation.

Inclusive jet cross-sections in photon-photon collisions have previously been measured at \(\sqrt{s_{ee}} = 58\) GeV at TRISTAN \[1,2\] and at \(\sqrt{s_{ee}}\) from 130 to 172 GeV at LEP \[3,4\]. This paper extends the latter analysis to higher \(e^+e^-\) centre-of-mass energies, and provides an approximately thirty-fold increase in integrated luminosity. The \(k_t\)-clustering algorithm \[5\] is used as opposed to the cone algorithm \[6\] in \[3,4\] for the measurement of the differential cross-sections, because of the advantages of this algorithm in comparing to theoretical calculations \[7\]. The cone jet algorithm is used to demonstrate the different structure of the cone jets compared to jets defined by the \(k_t\)-clustering algorithm. The large amount of data allows us to measure the cross-section for di-jet production in photon-photon interactions as a function of the mean transverse jet energy \(\bar{E}_{T\text{jet}}\), the jet pseudo-rapidity \(|\eta_{\text{jet}}|\) and the absolute difference in pseudo-rapidity \(|\Delta\eta_{\text{jet}}|\) of the jets, with \(\eta_{\text{jet}} = -\ln \tan(\theta_{\text{jet}}/2)\) \(^1\). For the first time, the differential cross-section is also measured as a function of the estimated fraction of the photon momentum carried by the parton entering the hard sub-process, \(x_\gamma\), with full unfolding for detector effects. Angular distributions in di-jet events are measured and used to demonstrate the dominance of quark and gluon initiated processes in different regions of phase space.

At \(e^+e^-\) colliders the photons are emitted by the beam electrons\(^2\). Most of these photons carry only a small negative four-momentum squared, \(Q^2\), and can be considered quasi-real (\(Q^2 \approx 0\)). The electrons are hence scattered with very small polar angles and are not detected. Events where one or both scattered electrons are detected are not considered in the present analysis. Three processes contribute to di-jet production in photon-photon collisions: the direct process where two bare photons interact, the single-resolved process where a bare photon picks out a parton (quark or gluon) of the other photon, and the double-resolved process where partons of both photons interact \[8\]. This separation is only unambiguous at leading order. At higher orders it becomes dependent on the process scales.

\(^1\)The coordinate system of OPAL has the \(z\) axis along the electron beam direction, the \(y\) axis pointing upwards and \(x\) towards the center of the LEP ring. The polar angle \(\theta\) and the azimuthal angle \(\phi\) are defined relative to the +\(z\)-axis and +\(x\)-axis, respectively.

\(^2\)Positrons are also referred to as electrons.
2 The OPAL detector

A detailed description of the OPAL detector can be found in [9]. Only the main features relevant to the present analysis will be given here.

The central tracking system is located inside a solenoidal magnet which provides a uniform axial magnetic field of 0.435 T along the beam axis. The magnet is surrounded in the barrel region (|cos θ| < 0.82) by a lead glass electromagnetic calorimeter (ECAL) and a hadronic sampling calorimeter (HCAL). Outside the HCAL, the detector is surrounded by muon chambers. There are similar layers of detectors in the endcaps (0.82 < |cos θ| < 0.98). The small angle region from 47 to 140 mrad around the beam pipe on both sides of the interaction point is covered by the forward calorimeters (FD) and the region from 33 to 59 mrad by the silicon tungsten luminometers (SW).

Starting with the innermost components, the tracking system consists of a high precision silicon micro-vertex detector, a vertex drift chamber, a large volume jet chamber with 159 layers of axial anode wires and a set of z chambers measuring the track coordinates along the beam direction.

The barrel and endcap sections of the ECAL are both constructed from lead glass blocks with a depth of 24.6 radiation lengths in the barrel region and more than 22 radiation lengths in the endcaps. The HCAL consists of streamer tubes and thin multiwire chambers instrumenting the gaps in the iron yoke of the magnet, which provides the absorber material of 4 or more interaction lengths.

The FD consists of two cylindrical lead-scintillator calorimeters with a depth of 24 radiation lengths divided azimuthally into 16 segments. The SW detectors consist of 19 layers of silicon detectors and 18 layers of tungsten, corresponding to a total of 22 radiation lengths.

3 Monte Carlo simulation

The MC generators PYTHIA 5.722 [10, 11] and PHOJET 1.10 [12] are used to study detector effects. PYTHIA is based on leading order (LO) QCD matrix elements for massless quarks with added parton showers and hadronisation. PHOJET also simulates hard interactions through perturbative QCD in LO, but includes soft interactions through Regge phenomenology before the partons are hadronised. The probability of finding a parton in the photon is taken from parametrisations of the parton distribution functions. The default choices of SaS 1D [13] for PYTHIA and LO GRV [14] for PHOJET are taken for the samples used to study detector effects.

An increased flow of transverse energy, $E_T$, apparently not directly related to the hard subprocess has been observed in photon-hadron scattering [15], and has been labeled the underlying event. Both PHOJET and PYTHIA include a model of multiple parton interactions (MIA) to simulate such effects. In PYTHIA the amount of MIA added to the event...
is controlled by a lower cutoff parameter $p_t^{mi}$, which describes the transverse momentum of the parton involved. Following the studies carried out in [3, 4], $p_t^{mi}$ is set to 1.4 GeV for the SaS1D parton densities. In PHOJET the default setting for MIA is used.

Three non-signal processes are important: hadronic decays of the $Z^0$, where initial state photon radiation has reduced the centre-of-mass energy of the hadronic final state to be close to the $Z^0$ mass, $\gamma\gamma \rightarrow \tau\tau$ reactions, and photon-photon collisions where one of the photons is virtual ($\gamma^*\gamma$) but the scattered electron is not detected. The hadronic $Z^0$ decays are simulated using PYTHIA. The pair-production of $\tau$-leptons in photon-photon collisions is simulated using BDK [16]. Deep-inelastic electron-photon scattering events are studied with the HERWIG 5.9 [17] generator.

All signal and background MC samples were generated with the full simulation of the OPAL detector [18]. They are analysed using the same reconstruction algorithms as are applied to the data.

4 Definition of di-jet observables

All cross-section measurements use jets reconstructed with the inclusive $k_T$-clustering algorithm as proposed in [5] with $R_0 = 1$. In addition, a cone jet algorithm [6] with a cone size of 1.0 in $\eta-\phi$-space is employed to study the dependence of the jet structure on the algorithm used. A di-jet event is defined as an event with at least two jets fulfilling the requirements detailed below. In events with more than two jets, only the two jets with the highest $E_T^{jet}$ values are taken.

The primary intentions of this analysis are to study the ability of QCD theory to describe jet production in photon-photon collisions, and to explore the photon structure revealed in these hadronic interactions. The most advanced theoretical predictions to date are provided by fixed order perturbative calculations up to NLO for the production of di-jets. These calculations need as input a scale that is in principle arbitrary, but commonly set to a value related to the hardness of the interaction. Possible choices for di-jet production are for example the mean transverse energy $\bar{E}_T^{jet}$ or the maximum $E_T^{jet}$ of the di-jet system.

The separation of quasi-real and virtual photons is somewhat arbitrary and therefore needs to be defined. For this analysis we choose values of $Q^2 < 4.5$ GeV$^2$ to define quasi-real photons. It is the same value as used in previous analyses [3, 4], motivated by the acceptance of the low angle calorimeters. The median $Q^2$ resulting from this definition cannot be determined with the data since the scattered electrons are not tagged. For the kinematic range of this analysis both PHOJET and PYTHIA predict the median $Q^2$ to be of the order $10^{-4}$ GeV$^2$. 
4.1 Properties of di-jet events

In LO QCD, neglecting multiple parton interactions, two hard parton jets are produced in $\gamma\gamma$ interactions. In single- or double-resolved interactions, these jets are expected to be accompanied by one or two remnant jets. A pair of variables, $x_+^\gamma$ and $x_-^\gamma$, can be defined [19] that estimate the fraction of the photon’s momentum participating in the hard scattering:

$$x_+^\gamma \equiv \frac{\sum_{\text{jets}=1,2} (E_{\text{jet}}^+ + p_{z,\text{jet}})}{\sum_{\text{hfs}} (E + p_z)} \quad \text{and} \quad x_-^\gamma \equiv \frac{\sum_{\text{jets}=1,2} (E_{\text{jet}}^- - p_{z,\text{jet}})}{\sum_{\text{hfs}} (E - p_z)},$$

(1)

where $p_z$ is the momentum component along the $z$ axis of the detector and $E$ is the energy of the jets or objects of the hadronic final state (hfs). In LO, for direct events, all energy of the event is contained in two jets, i.e., $x_+^\gamma = 1$ and $x_-^\gamma = 1$, whereas for single-resolved or double-resolved events one or both values are smaller than 1. The di-jet differential cross-section as a function of $x_\gamma$ is therefore particularly well suited to study the structure of the photon, since it separates predominantly direct events at high $x_\gamma$ ($x_\gamma > 0.75$) from predominantly resolved events at low $x_\gamma$ ($x_\gamma < 0.75$). The fraction of direct, single-resolved and double-resolved events as a function of $x_\gamma$ predicted by PYTHIA is shown in Figure 1 (a)-(c). The dominance of resolved events for $x_\gamma < 0.75$ is clearly visible. In these distributions and in the definitions below, $x_\gamma$ indicates that each event enters the distribution twice, at the value of $x_+^\gamma$ and the value of $x_-^\gamma$.

Due to the different nature of the underlying partonic process one expects different distributions of the angle $\Theta^*$ between the jet axis and the axis of the incoming partons or direct photons in the di-jet centre-of-mass frame. The leading order direct process $\gamma\gamma \to q\bar{q}$ proceeds via the $t$-channel exchange of a spin-$\frac{1}{2}$ quark, which leads to an angular dependence $\propto (1 - \cos^2 \Theta^*)^{-1}$. In double resolved processes the sum of all matrix elements, including a large contribution from spin-1 gluon exchange, leads to an approximate angular dependence $\propto (1 - |\cos \Theta^*|)^{-2}$ [20]. The contribution of the different processes to all resolved events depends on the parton distribution functions of the photon. An estimator of the angle $\Theta^*$ can be formed from the pseudo-rapidities of the two jets as

$$\cos \Theta^* = \tanh \left( \frac{\eta_{1,\text{jet}} - \eta_{2,\text{jet}}}{2} \right),$$

(2)

where it is assumed that the jets are collinear in $\phi$ and have equal transverse energy. Only $|\cos \Theta^*|$ can be measured, as the ordering of the jets in the detector is arbitrary. To obtain an unbiased distribution of $|\cos \Theta^*|$ the measurement needs to be restricted to the region where the di-jet invariant mass $M_{jj} = 2E_T^{\text{jet}} / \sqrt{1 - |\cos \Theta^*|^2}$ is not influenced by the cuts on $E_T^{\text{jet}}$ [4]. In the present analysis a cut of $M_{jj} > 15$ GeV ensures that the $|\cos \Theta^*|$ distribution is not biased by the restrictions on $E_T^{\text{jet}}$ for the range $|\cos \Theta^*| < 0.8$ and $|\eta^\text{jet}| = \left| \left( \eta_{1,\text{jet}} + \eta_{2,\text{jet}} \right) / 2 \right| < 1$ confines the measurement to the region where the detector resolution on $|\cos \Theta^*|$ is good.
4.2 Differential di-jet cross-sections

The following differential cross-sections are measured, where the labels 1 and 2 refer to the two jets with highest $E_{T}^{\text{jet}}$ in the event, defined by the $k_{T}$ algorithm:

$$\frac{d\sigma_{\text{dijet}}}{d\bar{E}_{T}} \quad \text{with} \quad \bar{E}_{T} \equiv \frac{E_{T,1}^{\text{jet}} + E_{T,2}^{\text{jet}}}{2} \quad \text{and} \quad \bar{E}_{T} > 5 \text{ GeV}$$  \hfill (3)

$$\frac{d\sigma_{\text{dijet}}}{dx_{\gamma}} \quad \text{in 3 bins of} \quad \bar{E}_{T} \quad [5 - 7 - 11 - 25] \text{ GeV}$$  \hfill (4)

$$\frac{d\sigma_{\text{dijet}}}{d\log_{10}(x_{\gamma})} \quad \text{for} \quad 5 \text{ GeV} < \bar{E}_{T} < 7 \text{ GeV}$$  \hfill (5)

$$\frac{d\sigma_{\text{dijet}}}{d|\eta_{\text{jet}}|} \quad \text{for} \quad \bar{E}_{T} > 5 \text{ GeV}$$  \hfill (6)

$$\frac{d\sigma_{\text{dijet}}}{d|\Delta\eta_{\text{jet}}|} \quad \text{for} \quad E_{T}^{\text{jet}} > 5 \text{ GeV}, \quad |\eta_{\text{jet}}| < 1, \quad M_{jj} > 15 \text{ GeV}$$  \hfill (7)

with in all cases

$$|\eta_{1,2}| < 2 \quad \text{and} \quad \frac{|E_{T,1}^{\text{jet}} - E_{T,2}^{\text{jet}}|}{E_{T,1}^{\text{jet}} + E_{T,2}^{\text{jet}}} < \frac{1}{4}$$  \hfill (8)

Here, $|\eta_{\text{ctr}}^{\text{jet}}|$ and $|\eta_{\text{fwd}}^{\text{jet}}|$ denote the jet with the smaller and larger value of $|\eta_{\text{jet}}^{\text{jet}}|$ respectively, and $|\Delta\eta_{\text{jet}}|$ is defined to be the absolute distance in pseudo-rapidity between the two leading jets.

The combination of the second condition in Equation (8) with the minimum $E_{T}^{\text{jet}}$ requirement defines asymmetric $E_{T}^{\text{jet}}$ thresholds for the two jets of the di-jet system, which is important in comparisons to NLO QCD calculations [21]. This method of defining asymmetric thresholds has previously been used in [22].

Four regions in $x_{\gamma}^{+}$-$x_{\gamma}^{-}$-space are considered (see Figure 1(d)): (A) the complete $x_{\gamma}^{+}$-$x_{\gamma}^{-}$-space (full $x_{\gamma}^{\pm}$ range), (B) both $x_{\gamma}^{+}$ and $x_{\gamma}^{-}$ larger than 0.75 ($x_{\gamma}^{\pm} > 0.75$), (C) either $x_{\gamma}^{+}$ or $x_{\gamma}^{-}$ smaller than 0.75 ($x_{\gamma}^{+} < 0.75$), (D) both $x_{\gamma}^{+}$ and $x_{\gamma}^{-}$ smaller than 0.75 ($x_{\gamma}^{\pm} < 0.75$).

The cross-sections (3), (4) and (5) are measured in regions (A), (C) and (D). For the cross-sections in (6) regions (C) and (D) are considered. The cross-section as a function of $|\cos \Theta^{*}|$ in (7) is measured in regions (B) and (D).

4.3 Jet structure in di-jet events

The internal structure of jets is studied using the jet shape, which is defined as the fractional transverse jet energy contained in a subcone of radius $r$ concentric with the jet axis,
averaged over all jets of the event sample:

$$\psi(r) \equiv \frac{1}{N_{\text{jets}}} \sum_{\text{jets}} \frac{E_{\text{jet}}^T(r)}{E_{\text{jet}}^T(r = 1.0)} \quad \text{with} \quad r = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}. \tag{9}$$

$N_{\text{jets}}$ is the total number of jets analysed. Both $k_\perp$ and cone jets are analysed in this way. As proposed in [23], only particles assigned to the jet by the jet finders are considered. Events entering the jet shape distributions are required to have at least two jets with a transverse energy $3 \text{ GeV} < E_{\text{jet}}^T < 20 \text{ GeV}$ and a pseudo-rapidity $|\eta_{\text{jet}}| < 2$. The cone jet algorithm is used in addition to the $k_\perp$-clustering algorithm to demonstrate the different structure of the cone jets with respect to those defined by the $k_\perp$-clustering algorithm.

The jet shape is measured in the two regions of $x^+_{\gamma^\ast} - x^-_{\gamma^\ast}$ space, $x^+_{\gamma^\ast} < 0.75$ and $x^+_{\gamma^\ast} > 0.75$, in four bins of $E_{\text{jet}}^T$ with bin boundaries at 3, 6, 9, 12 and 20 GeV and four bins of $|\eta_{\text{jet}}|$ between 0 and 2, each bin 0.5 units wide.

## 5 Event selection

In this analysis, a sum over all particles in the event or in a jet means a sum over two kinds of objects: tracks and calorimeter clusters, including the FD and SW calorimeters. A track is required to have a minimum transverse momentum of 120 MeV and at least 20 hits in the central jet chamber. The point of closest approach to the origin must have a distance of less than 25 cm in $z$ and a radial distance of less than 2 cm to the $z$-axis. Calorimeter clusters have to pass an energy threshold of 100 MeV in the barrel section or 250 MeV in the endcap section for the ECAL, 600 MeV for the barrel and endcap sections of the HCAL, 1 GeV for the FD, and 2 GeV for the SW. An algorithm is applied to avoid double-counting of particle momenta in the central tracking system and their energy deposits in the calorimeters [3]. The measured hadronic final state for each event consists of all objects thus defined.

Di-jet events are preselected using the $k_\perp$ algorithm by requiring at least two jets with $|\eta_{\text{jet}}| < 2$ and a transverse energy $E_{\text{jet}}^T > 3 \text{ GeV}$. Photon-photon scattering events are selected using the requirements detailed below. The corresponding distributions in Figure 2 compare the sum of the simulated signal and background processes to the data, uncorrected for detector effects. For each distribution shown, all selection criteria are applied except the one on the quantity plotted. The signal MC generators PHOJET and PYTHIA are found to underestimate the cross-section by about 20% in these comparisons, and are scaled up accordingly. Of all non-signal processes studied, only those listed in Section 3 contribute significantly. Comparisons of the rate of di-jet events in photon-photon collisions where one of the photons is virtual (see for example [24]) show that the prediction of the MC generator used is too low by about a factor of two. The prediction of the contribution from $\gamma^\ast \gamma$ events has been scaled up accordingly.

All distributions are sufficiently well described by the sum of signal and background contributions. The total contribution of non-signal processes to the selected event sample is about 5% after the following selection criteria have been applied:
- The sum of all energy deposits in the ECAL and HCAL (Figure 2(a)) has to be less than 55 GeV to remove background from hadronic $Z^0$-decays in events with a radiative return to the $Z^0$-peak.

- The visible invariant mass measured in the ECAL, $W_{\text{ECAL}}$, has to be greater than 3 GeV to suppress low energy events.

- The missing transverse momentum of the event, $P_{T,\text{MISS}}$, calculated from the measured hadronic final state, has to be less than $0.05 \cdot E_{\text{BEAM}}$.

- At least 7 tracks must have been found in the tracking chambers. This cut reduces mostly the contamination from $\gamma\gamma \rightarrow \tau\tau$ events. The distribution of the track multiplicity is shown in Figure 2(b). The discrepancy in shape between data and simulation is not present when using PYTHIA instead of PHOJET as signal MC generator, and is addressed in the study of model dependencies in Section 8.

- To remove events with scattered electrons in the FD or in the SW calorimeters, the total sum of the energy measured in the FD has to be less than $0.25 \cdot E_{\text{BEAM}}$ and the total sum of the energy measured in the SW calorimeter has to be less than $0.18 \cdot E_{\text{BEAM}}$. These cuts also reduce the contamination from hadronic $Z^0$-decays with their thrust axis close to the beam direction. The energy sum in the FD calorimeter scaled by the beam energy is shown in Figure 2(c).

- The $z$ position of the primary vertex is required to satisfy $|z| < 5$ cm and the net charge $Q$ of the event calculated from adding the charges of all tracks is required to be $|Q| \leq 5$ to reduce background due to beam-gas interactions.

- To remove events originating from interactions between beam electrons and the beam-pipe the radial distance of the primary vertex from the beam axis has to be less than 3 cm.

- To further reject background from hadronic $Z^0$-decays and from deep-inelastic electron-photon scattering an invariant mass, $M_{J1H2}$, is calculated from the jet with highest $E_T$ in the event and the four-vector sum of all hadronic final state objects in the hemisphere opposite to the direction defined by this jet. The quantity $M_{J1H2}$ is a simple reconstruction of the $Z^0$-mass in case of background from hadronic $Z^0$-decays, and will therefore be larger on average for this type of background than for signal events. Events with $M_{J1H2} > 55$ GeV are rejected. The distribution of $M_{J1H2}$ is shown in Figure 2(d).

We use data at centre-of-mass energies $\sqrt{s_{ee}}$ from 189 GeV to 209 GeV. For the purpose of this analysis, the difference between the data taken at the various values of $\sqrt{s_{ee}}$ is small and therefore the distributions for all energies have been added. The luminosity weighted average centre-of-mass energy $\sqrt{s_{ee}}$ is approximately 198.5 GeV. The efficiency to trigger di-jet events in the region of phase space considered in this analysis has been shown to be close to 100% [4].
6 Transverse energy flow in di-jet events

NLO QCD calculations do not take into account the possibility of an underlying event which leads to an increased $E_T$-flow and therefore to an increased jet cross-section above a given threshold of $E_T^{jet}$. In PYTHIA and PHOJET the underlying event is simulated by multiple parton interactions. The contribution from multiple parton interactions is not known a priori, but has to be adjusted to give a good description of the data. In this analysis the size of this contribution is taken from our previous study of di-jet events in [1].

The transverse energy flow from an underlying event is expected to be small compared to the transverse energy of the leading jets, and it is not correlated to the direction of the jet axes. The energy flow outside the jets will therefore be most sensitive to the presence of an underlying event [2]. Additional energy outside the leading jets will shift the $x_\gamma$ distributions towards lower values.

To study the performance of the MC generators in describing the energy flow several uncorrected distributions are used. The average $E_T$-flow per event is measured with respect to the jet axis as a function of $\Delta \phi$ and $\Delta \hat{\eta}$. The variable $\hat{\eta}$ is equivalent to $\eta$, except that it is signed positively if $x_\gamma^+ \geq x_\gamma^-$, and signed negatively otherwise. The definition of $\hat{\eta}$ ensures that the energy flow associated with the “more resolved” photon, i.e., the smaller value of $x_\gamma$, will always appear on the left hand side of the plots. The profiles in $\Delta \phi$ consider a range of $|\Delta \eta| = 1$ around the jet-axis, while a $|\Delta \phi|$-range of $\pi/2$ around the jet-axis is considered for the profiles in $\Delta \hat{\eta}$. The two leading jets in $E_T^{jet}$ in each event are considered. Another sensitive variable is the energy flow with the leading two jets in the event removed, $E_T^{out}$, as a function of $\hat{\eta}$. All objects are excluded inside a cone of radius 1.3 in $\eta, \phi$ around the two leading jets.

Multiple parton interactions are important in interactions where the photon is resolved. It is therefore interesting to study separately the three cases of (a) two resolved photons, (b) one resolved photon, or (c) no resolved photon in the interaction. Experimentally these situations can be approximated by choosing events with $x_\gamma^+ < 0.75$, $x_\gamma^+ > 0.75$, or $x_\gamma^- > 0.75$, i.e. regions (D), (C) and (B) defined in Section 4.

Figures 3 and 4 show the jet profiles and the energy flow outside the leading jets. The data are compared to a mixture of signal (PHOJET or PYTHIA) and background MC simulation. The contributions of signal and background are weighted according to their cross-section in each region of phase space. The background MC generators used are the same as in Figure 2.

For the $\phi$-profiles in Figure 3 it is evident that both PHOJET and PYTHIA are able to describe the data in the region of the high $E_T$ jets around zero. Moving away from the jet axis PHOJET predicts an energy flow which is too low compared to the data, especially for $x_\gamma^+ < 0.75$. This corresponds to the area where effects from an underlying event are expected to be most prominent. PHOJET improves towards higher $x_\gamma$. PYTHIA reproduces the data reasonably well. Such differences between PHOJET and PYTHIA are not evident in the $\hat{\eta}$-profiles. Here in the case of resolved photons the $E_T$-flow is dominated by the photon remnant(s), and is reasonably well described by both generators. The jets entering Figure 3 are selected from the range $10 < E_T^{jet} < 25$ GeV. No significant deviation
from the behaviour just described is observed when selecting $E_T^{\text{jet}} < 10$ GeV.

The energy-flow outside the two leading jets is shown in Figure 4. Again PYTHIA describes the data well, while PHOJET is somewhat low. With both models used to unfold the data as a systematic check, we conclude that the details of the energy flow around the two leading jets are sufficiently well under control and remaining influences are included in the systematic uncertainty of the cross-section and jet shape measurements.

7 Data corrections

An example of the uncorrected distributions as a function of $x_\gamma$ including the contribution of the remaining background events is shown in Figure 5. To obtain jet cross-sections which can be compared to theoretical calculations, we use MC simulations to correct for the selection cuts, the resolution effects of the detector and the background from non-signal processes. Backgrounds are first subtracted bin-by-bin from all distributions. For the differential cross-sections as a function of $E_T^{\text{jet}}$ and $x_\gamma$, sizable migration and resolution effects are to be expected. We therefore apply a matrix unfolding method, as implemented in the GURU program [26], for these distributions. The results are cross checked using a bin-by-bin correction. By definition $x_\gamma$ can only take values between zero and unity. At either extremity no adjacent bins are available. To avoid instabilities expected from the smoothing procedures in the unfolding for the first and last bin, the central values for these bins are taken from the bin-by-bin correction method. The $|\cos \Theta^*|$, $|\eta^{\text{jet}}|$ and $|\Delta\eta^{\text{jet}}|$ distributions are corrected bin-by-bin, as only small migrations are expected here. PHOJET is used as the default signal MC generator for the unfolding.

The correction method employed for the jet shapes is a bin-by-bin correction using the MC simulations to correct for detector effects. The contribution of the same background processes as for the cross-section measurements was studied. The influence on the signal was found to be less than 1%. Therefore the subtraction of the background was omitted in this analysis. Both PYTHIA and PHOJET were used to estimate the correction factors to study their model dependence.

8 Systematic uncertainties

The overall systematic uncertainty is determined from the sources listed below added in quadrature. The same sources are considered for the measurement of the differential cross-sections and the jet shapes, with the exception of the background, which has been neglected for the jet shapes as discussed in Section 7.

- To assess the uncertainty associated with the subtraction of background events, the predictions for hadronic decays of the $Z^0$ and for $\gamma\gamma \rightarrow \tau\tau$ reactions are conservatively varied by 10% without contributing significantly to the systematic error. The
prediction of the contribution from $\gamma^*\gamma$ events has been scaled up by a factor of two as described above. By comparing the predictions to the data for large $E_{FD}/E_{BEAM}$ and $M_{JH2}$ (see Figure 2), where this background dominates, we determine that this scaling factor can be varied by no more than about 30% in order to keep a good description of the data. The scaling factor is varied accordingly. The uncertainty from all the background subtraction is typically 2-4%.

- To estimate the systematic error arising from the specific model used for the unfolding, both PYTHIA and PHOJET are used to unfold the data. The estimated uncertainty derived from this study is typically 10%, and up to 20% in some cases for the differential cross-sections, and 1-2% for the jet shapes.

- The absolute energy scale of the ECAL calorimeter is known to about 3% for the range of jet energies in this analysis. To estimate the influence on the observables the energy scale is varied by this amount and the analysis is repeated. The cross-sections change by 5-10% due to this variation. The estimated uncertainty for the jet shapes is about 1%.

- The selection criteria described in Section 4 are varied simultaneously both to be more restrictive and to allow more events into the analysis to exclude a strong dependence on the event selection. Selection criteria based on energy measurements are varied by 10% of their central value, which is considered conservative given the uncertainty in the energy scale and the energy resolution of the calorimeter. The number of tracks required and the maximum net charge of the event are changed by $\pm 1$. The allowed radial distance and z position of the primary vertex are varied by 0.5 cm and 1 cm respectively. The uncertainty on the cross-section derived from all these variations is typically 5-10%, and up to 20% in some cases for the differential cross-section, and about 2-4% for the jet shapes.

The uncertainty on the determination of the integrated luminosity is much less than 1%, and is neglected. For the differential cross-sections the systematic uncertainties evaluated for each bin were averaged with the results from its two neighbours (single neighbour for endpoints) to reduce the effect of bin-to-bin fluctuations.

9 Hadronisation corrections

The differential di-jet cross-sections measured are compared to NLO QCD calculations which predict jet cross-sections for partons, whereas the experimental jet cross-sections are presented for hadrons. Effects due to the modelling of the hadronisation process are not taken into account in the NLO calculation. Because the partons in the MC generators and the partons in the NLO calculations are defined in different ways there is as yet no rigorous procedure to use the MC generators to correct the data so that they can be compared to the NLO parton level predictions. However, as the MC generators are the only available option so far, they are used to study the approximate size of these hadronisation corrections. For this purpose the prediction of the MC generators at the level of the partonic final state
is calculated and divided by the prediction obtained from the hadronic final state. The resulting correction factor is labeled \((1 + \delta_{\text{hadr}})\). The partonic final state consists of all partons at the end of the parton shower. The hadronic final state utilises all charged and neutral particles with lifetimes greater than \(3 \times 10^{-10}\) s, which are treated as stable.

Examples of hadronisation corrections estimated by PYTHIA 6.161 and HERWIG 6.1 for the observables defined in Section 4 are shown in Figure 6. The numerical values can be found in [28]. In PYTHIA the partonic final state is hadronised according to the string fragmentation model, while HERWIG uses cluster fragmentation. In all plots the full \(x_\gamma^+ - x_\gamma^-\)-range is considered. The theoretical calculations are corrected bin-by-bin using the mean of the hadronisation corrections estimated using PYTHIA and HERWIG.

Figure 6 (a) shows \((1 + \delta_{\text{hadr}})\) as a function of \(\bar{E}_T^\text{jet}\). The correction is less than 10% for \(\bar{E}_T^\text{jet}\) greater than about 10 GeV, but rises to about 25% for PYTHIA and 15% for HERWIG towards small \(\bar{E}_T^\text{jet}\). The corrections for observables involving the jet pseudo-rapidities are dominated by the low \(\bar{E}_T^\text{jet}\) region. They are essentially flat and around 20% for PYTHIA. HERWIG estimates these corrections to be around 10%.

Figure 6 (b) shows \((1 + \delta_{\text{hadr}})\) as a function of \(x_\gamma\) for the lowest bin in \(\bar{E}_T^\text{jet}\) defined in Section 4. From the figure it is evident that hadronisation causes large corrections for \(x_\gamma > 0.75\). The effect is reduced for higher values of \(\bar{E}_T^\text{jet}\), as can be seen in Figure 6 (c) and (d). The large corrections for \(x_\gamma > 0.75\) are mainly due to the large influence hadronisation has on the distribution of direct events, which are peaked at \(x_\gamma = 1\) for the partonic final state of the LO calculation, but are much more smeared out at the level of stable hadrons (see Figure 6 (a)-(c)). While both the measurement and the NLO calculation are perfectly valid for the presented bin sizes, the hadronisation corrections needed for the comparison introduces a large migration between the two bins above \(x_\gamma = 0.75\). For a sensible comparison in this region one should therefore consider the sum of the two bins above \(x_\gamma = 0.75\) and compare it to the corresponding sum for the data.

10 Results

10.1 Jet structure in di-jet events

In Figure 7(a) the jet shape, \(\Psi(r)\), is shown for the \(k_\perp\) algorithm for both \(x_\gamma^+ > 0.75\) and \(x_\gamma^- < 0.75\). The first sample is dominated by direct photon-photon interactions and hence by quark-initiated jets. As is demonstrated in the figure, jets in this sample are more collimated than for small values of \(x_\gamma\), where the cross-section is dominated by resolved processes and hence has a large contribution from gluon-initiated jets. In both cases the jets become more collimated with increasing transverse energy, as is shown in Figure 7(c). There is no significant dependence on the jet pseudo-rapidity (Figure 7(d)). Both PHOJET and PYTHIA give an adequate description of the jet shapes as can be seen in Figures 7(b), (c), and (d).

Figure 8 compares the shapes of jets defined by the cone algorithm and the \(k_\perp\) algorithm,
in each case compared to the shape as obtained from PYTHIA. As for the $k_\perp$-jets, the jets defined by the cone algorithm are more collimated in the quark-dominated sample and always become more collimated for increasing transverse energy, while there is no dependence on the jet pseudo-rapidity. The cone-jets are significantly broader than the jets defined by the $k_\perp$ algorithm at low $E_{T}^{\text{jet}}$. With increasing $E_{T}^{\text{jet}}$, jets become more collimated and the two jet algorithms give similar results. While the $k_\perp$-jets are well described by PYTHIA and PHOJET, the jet shapes obtained for the cone-jets are somewhat broader than in the data.

10.2 Differential di-jet cross-sections

Only the $k_\perp$ jet algorithm is used for the measurement of the differential di-jet cross-sections. The experimental results are compared to a perturbative QCD calculation at NLO [29] which uses the GRV HO parametrisation of the parton distribution functions of the photon [14], and was repeated for the kinematic conditions of the present analysis. The renormalisation and factorisation scales are set to the maximum $E_{T}^{\text{jet}}$ in the event. The calculation was performed in the MS-scheme with five light flavours and $\Lambda^{(5)}_{\text{QCD}} = 130$ MeV. The average of the hadronisation corrections estimated by PYTHIA and HERWIG have been applied to the calculation for this comparison.

Figure 9 and Table 1 show the differential di-jet cross-section as a function of $|\cos \Theta^*|$ for both $x_\pm^{\pm} > 0.75$ and $x_\gamma^{\pm} < 0.75$. The steeper rise with increasing $|\cos \Theta^*|$ from the dominating spin-1 gluon exchange in the second sample is clearly visible (see Section 4). The shape of both samples is well described by NLO QCD. For $x_\gamma^{\pm} < 0.75$ the NLO calculation is about 20% below the data. It should be noted that in this region the contribution from the underlying event, not included in the calculation, is expected to be largest, as discussed in more detail below. For $x_\gamma^{\pm} > 0.75$ the NLO QCD prediction is about 20% above the data. While here the contribution from MIA is small, this region is affected by rather large hadronisation corrections as discussed in Section 9, which translates into an uncertainty of the normalisation in comparing the theoretical prediction to the data.

The differential di-jet cross-section as a function of the mean transverse energy $E_{T}^{\text{jet}}$ of the di-jet system is shown in Figure 10 and Table 2. At high $E_{T}^{\text{jet}}$ the cross-section is expected to be dominated by direct processes, associated with the region $x_\gamma^{\pm} > 0.75$. Consequently we observe a significantly softer spectrum for the case $x_\gamma^{\pm} < 0.75$ than for the full $x_\gamma^{\pm}$-space. The calculation is in good agreement with the data for the full $x_\gamma^{\pm}$-range and for $x_\gamma^{\pm} > 0.75$. The cross-section predicted for $x_\gamma^{\pm} < 0.75$ is again below the measurement. PYTHIA 6.161 is in good agreement with the measured distributions using the SaS 1D parton densities.

Figure 11 and Tables 3 and 6 show the di-jet cross-section as a function of $x_\gamma$ and $\log_{10}(x_\gamma)$. The cross-section for the lowest values of $E_{T}^{\text{jet}}$ shows the largest fraction of events at $x_\gamma < 0.75$ of the three ranges considered, and is hence most sensitive to gluon-initiated processes. The di-jet cross-section logarithmic in $x_\gamma$ emphasises the region of lowest accessible $x_\gamma$, which extends down to approximately 0.02.
As $E_T^{\text{jet}}$ increases, the fraction of events with $x_\gamma > 0.75$ increases. In MC simulations these are predominantly direct events. The sensitivity to the gluon density in the photon is hence expected to decrease with increasing $E_T^{\text{jet}}$. On the other hand, NLO QCD predictions which use $E_T^{\text{jet}}$ as the process-relevant scale are expected to become more reliable as this scale increases. It is hence important to provide measurements at both low and high values of $E_T^{\text{jet}}$, to study all aspects of the theory.

PYTHIA using SaS 1D is in good agreement with the measured distributions, with a tendency to be too low for small values of $x_\gamma$. The shaded histogram at the bottom of each plot indicates the MIA contribution to the PYTHIA prediction. The numerical values of this contribution can be found in [28]. NLO QCD predicts the shape of the cross-sections well for $x_\gamma < 0.75$, but is too low by about 10-20% especially at low $E_T^{\text{jet}}$. As MIA are not included in this calculation it is interesting to note that the MIA contribution to the cross-section as obtained from PYTHIA is similar in size to the discrepancy.

The region of $x_\gamma > 0.75$ suffers from large hadronisation corrections as discussed in Section 9. The uncertainty for the data-theory comparison associated with these large corrections can be reduced by considering the sum of the two bins above $x_\gamma = 0.75$, for which NLO QCD indeed gives an adequate description of the data.

Figure 12 demonstrates the effect of using different parton distribution functions of the photon on the NLO QCD prediction. AFG HO [30] and GS96 HO [31] are used in addition to the default GRV HO. The sensitivity of the cross-section to the different gluon density in each case is clearly visible for the gg-contribution (Figure 12 (b)), but is less pronounced for the full cross-section as can be seen in Figure 12 (a), due to compensating effects from processes involving the quark densities (Figures 12 (c) and (d)). A global analysis, beyond the scope of this paper, using for example $F_\gamma^2$ measurements to constrain simultaneously the quark densities hence promises to yield the highest sensitivity to the gluon density in the photon.

In Figure 13 (Tables 4 and 6) the same cross-sections as in Figure 11 are shown for the case $x_\gamma^+ < 0.75$. Here the cross-section is dominated by interactions where one of the two incident photons is resolved. The multiple parton interactions used in PYTHIA to model an underlying event are much suppressed in this case, and NLO QCD describes both the shape and normalisation of the data well. The opposite effect can be observed in Figure 14 (Tables 5 and 6), where for the case $x_\gamma^- < 0.75$ one expects a large influence of multiple parton interactions, as demonstrated again by the shaded histogram at the bottom of each plot. The cross-sections change by as much as 50% in the low $E_T^{\text{jet}}$ region, when MIA are switched on. For higher $E_T^{\text{jet}}$ the influence is not as strong. Even with MIA switched on, PYTHIA using SaS 1D is too low. The deficit visible in the normalisation of the NLO calculation is again of similar size as the MIA contribution to the cross-section obtained from PYTHIA.

Complementary information can be obtained by measuring the angular distributions of the two highest $E_T^{\text{jet}}$ jets in di-jet events. The $|\eta^{\text{jet}}|$ and $|\Delta \eta^{\text{jet}}|$ dependence of the di-jet cross-section is dominated by the low $E_T^{\text{jet}}$ events. The cross-sections measured are listed in Tables 7, 8 and 9. In Figure 15 the di-jet cross-sections as a function of $|\Delta \eta^{\text{jet}}|$, $|\eta^{\text{jet}}_{\text{centr}}|$ and $|\eta^{\text{jet}}_{\text{fwd}}|$ are shown for the case $x_\gamma^+ > 0.75$. Again the multiple parton interactions
used in PYTHIA to model an underlying event are much suppressed in this case. PYTHIA using SaS 1D is about 20% too low. The prediction of NLO QCD is in good agreement with the data in both shape and normalisation.

In Figure 16 the same cross-sections are presented for the case of $x_\gamma < 0.75$. As expected, the effect of including MIA in PYTHIA is again sizable. When multiple parton interactions are switched on, the prediction obtained from PYTHIA reproduces the data reasonably well. Again the prediction of NLO QCD is too low by about the size of the MIA contribution to the cross-section obtained by PYTHIA.

11 Conclusions

We have studied di-jet production in photon-photon interactions with the OPAL detector at $e^+e^-$ centre-of-mass energies $\sqrt{s_{ee}}$ from 189 to 209 GeV with an integrated luminosity of 593 pb$^{-1}$. The data are combined into one sample with a luminosity weighted average centre-of-mass energy of approximately $\sqrt{s_{ee}} = 198.5$ GeV. Jets are reconstructed using an inclusive $k_\perp$-clustering algorithm for the measurement of differential di-jet cross-sections, and using both the inclusive $k_\perp$ and a cone algorithm for the study of jet structure.

Jet shapes, $\Psi(r)$, have been studied in two separate samples: $x_\gamma > 0.75$, which is dominated by direct processes and hence by quark-initiated jets, and $x_\gamma < 0.75$, dominated by resolved events and therefore by gluon-initiated jets. As expected from QCD the jets in the first sample are significantly more collimated than for $x_\gamma < 0.75$. Jets in both samples become more collimated with increasing transverse energy, but show no significant dependence on the jet pseudo-rapidity. Jets defined by the cone algorithm are substantially broader than those defined by the $k_\perp$ algorithm at low $E_T^{\text{jet}}$. However the difference decreases with increasing $E_T^{\text{jet}}$. The shape of $k_\perp$-jets is well described by PYTHIA and PHOJET. The jet shapes obtained for the cone-jets are somewhat broader in PYTHIA and PHOJET than in the data.

Inclusive differential di-jet cross-sections have been measured as a function of $|\cos \Theta^*|$, $E_T^{\text{jet}}$, $|\eta^{\text{jet}}|$ and $|\Delta \eta^{\text{jet}}|$ and, for the first time, as a function of $x_\gamma$ in several bins of $E_T^{\text{jet}}$. Different regions of the $x_\gamma^+-x_\gamma^-$-space are explored to separate experimentally direct from resolved interactions and to study and control the influence of an underlying event. By measuring the cross-sections for events in which either $x_\gamma^+$ or $x_\gamma^-$ is smaller than 0.75 we have isolated a region of phase space in which resolved photon processes dominate, and which at the same time is much less sensitive to multiple parton interactions. By performing the measurement also for $x_\gamma < 0.75$, observables are made available which are sensitive to the amount of multiple parton interactions added in the prediction, and which can be used to study these effects in detail.

A strong rise with increasing $|\cos \Theta^*|$ is observed for the differential di-jet cross-section for $x_\gamma^+ < 0.75$, as expected from QCD for a sample with a significant contribution from spin-1 gluon exchange. The flatter distribution for direct events is also in good agreement with the QCD calculation.
The differential di-jet cross-sections as a function of $E_T^{jet}$, $|\eta^{jet}|$, $|\Delta \eta^{jet}|$ and $x_\gamma$ are in good agreement with the next-to-leading order perturbative QCD calculation except for $x_\gamma^{\pm} < 0.75$, where the calculation is too low. As this calculation does not include a model for the underlying event that is expected to be largest in this region, it is interesting to note that the discrepancy is of similar size to the contribution of multiple parton interactions to the PYTHIA prediction. The sensitivity of the results presented to the gluon density in the photon is clearly visible in NLO QCD predictions using different parton distribution functions, but is compensated to some extent by anti-correlated differences in the respective quark-densities. A global analysis using additional data sets to simultaneously constrain the quark densities hence promises to yield the highest sensitivity to the gluon density in the photon.

The measurements carried out for events in which only either $x_\gamma^+$ or $x_\gamma^-$ is smaller than 0.75 are a unique data set. While this region is almost insensitive to multiple parton interactions, the fraction of events at small $x_\gamma$ is still sizable, which indicates a significant contribution of resolved processes and hence a good sensitivity to the hadronic structure of the photon. The good agreement of data and theory in this region in particular confirms that perturbative QCD in next-to-leading order is able to describe correctly the inclusive production of di-jets in photon-photon collisions.

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| | \(|\cos \Theta^*|\) | \(\frac{d\sigma_{\text{di-jet}}}{d|\cos \Theta^*|}\) [pb] | \(\delta_{\text{stat}}\) [pb] | \(\delta_{\text{sys}}\) [pb] |
|---|---|---|---|---|
| | | | | |
| \(x_\gamma^+ > 0.75\) | | | | |
| 0.0 – 0.1 | 5.04 | 0.49 | 0.32 |
| 0.1 – 0.2 | 4.96 | 0.49 | 0.34 |
| 0.2 – 0.3 | 5.22 | 0.49 | 0.32 |
| 0.3 – 0.4 | 5.35 | 0.48 | 0.38 |
| 0.4 – 0.5 | 4.90 | 0.45 | 0.32 |
| 0.5 – 0.6 | 6.73 | 0.56 | 0.47 |
| 0.6 – 0.7 | 7.09 | 0.54 | 0.43 |
| 0.7 – 0.8 | 8.42 | 0.61 | 0.51 |
| | | | | |
| \(x_\gamma^- < 0.75\) | | | | |
| 0.0 – 0.1 | 1.50 | 0.31 | 0.24 |
| 0.1 – 0.2 | 2.63 | 0.46 | 0.36 |
| 0.2 – 0.3 | 2.91 | 0.50 | 0.41 |
| 0.3 – 0.4 | 3.73 | 0.62 | 0.43 |
| 0.4 – 0.5 | 4.36 | 0.61 | 0.62 |
| 0.5 – 0.6 | 6.52 | 0.80 | 0.74 |
| 0.6 – 0.7 | 9.90 | 0.92 | 1.07 |
| 0.7 – 0.8 | 13.05 | 0.96 | 1.02 |

*Table 1*: The di-jet cross-section as a function of \(|\cos \Theta^*|\) for the two regions in \(x_\gamma^+ - x_\gamma^-\) space indicated in the table. The total uncertainty for each bin is the quadratic sum of the statistical and systematic uncertainty given in the table.
| $E_T^{\text{jet}}$ [GeV] | $\frac{d\sigma_{\text{dijet}}}{dE_T^{\text{jet}}}$ [pb/GeV] | $\delta_{\text{stat}}$ [pb/GeV] | $\delta_{\text{sys}}$ [pb/GeV] |
|------------------------|----------------------|------------------|------------------|
| full $x_\gamma^+ - x^-_\gamma$ - range |
| 5.00 - 6.54 | 11.54 | 0.36 | 0.59 |
| 6.54 - 8.55 | 4.16 | 0.16 | 0.25 |
| 8.55 - 11.18 | 1.45 | 0.07 | 0.09 |
| 11.18 - 14.62 | 0.543 | 0.036 | 0.044 |
| 14.62 - 19.12 | 0.176 | 0.020 | 0.020 |
| 19.12 - 25.00 | 0.0607 | 0.0117 | 0.0087 |
| $x_\gamma^+$ or $x^-_\gamma < 0.75$ |
| 5.00 - 6.54 | 3.56 | 0.21 | 0.22 |
| 6.54 - 8.55 | 1.32 | 0.09 | 0.10 |
| 8.55 - 11.18 | 0.475 | 0.045 | 0.037 |
| 11.18 - 14.62 | 0.190 | 0.025 | 0.024 |
| 14.62 - 19.12 | 0.0518 | 0.0127 | 0.0073 |
| $x^-_\gamma < 0.75$ |
| 5.00 - 6.54 | 5.94 | 0.41 | 0.66 |
| 6.54 - 8.55 | 1.84 | 0.16 | 0.23 |
| 8.55 - 11.18 | 0.461 | 0.060 | 0.071 |
| 11.18 - 14.62 | 0.0781 | 0.0192 | 0.0130 |

Table 2: The di-jet cross-section as a function of the mean transverse energy $E_T^{\text{jet}}$ of the di-jet system, for the three regions in $x_\gamma^+, x^-_\gamma$-space indicated in the table.
Table 3: The di-jet cross-section as a function of $x_\gamma$ for the regions of the mean transverse energy $\bar{E}_{T}^{\text{jet}}$ of the di-jet system and the region in $x_+^\gamma - x_-^\gamma$-space indicated in the table.
| $x_\gamma$ | $\frac{d\sigma_{\text{di}}}{dx_\gamma}$ [pb] | $\delta_{\text{stat}}$ [pb] | $\delta_{\text{sys}}$ [pb] |
|------------|---------------------------------|-----------------|-----------------|
| $x_\gamma^+$ or $x_\gamma^-$ < 0.75 |
| $5 \text{ GeV} < \bar{E}_{\text{jet}}^T < 7 \text{ GeV}$ |
| 0.000 – 0.125 | 12.47 | 0.96 | 1.18 |
| 0.125 – 0.250 | 8.87 | 0.74 | 1.16 |
| 0.250 – 0.375 | 7.00 | 0.69 | 0.83 |
| 0.375 – 0.500 | 5.12 | 0.58 | 0.65 |
| 0.500 – 0.625 | 5.99 | 0.69 | 0.56 |
| 0.625 – 0.750 | 12.36 | 1.27 | 0.98 |
| 0.750 – 0.875 | 38.50 | 1.92 | 4.19 |
| 0.875 – 1.000 | 11.80 | 1.72 | 1.30 |
| $7 \text{ GeV} < \bar{E}_{\text{jet}}^T < 11 \text{ GeV}$ |
| 0.000 – 0.125 | 5.44 | 0.73 | 0.62 |
| 0.125 – 0.250 | 4.84 | 0.52 | 0.48 |
| 0.250 – 0.375 | 3.45 | 0.44 | 0.31 |
| 0.375 – 0.500 | 2.91 | 0.41 | 0.21 |
| 0.500 – 0.625 | 3.28 | 0.48 | 0.25 |
| 0.625 – 0.750 | 5.38 | 0.76 | 0.39 |
| 0.750 – 0.875 | 15.03 | 1.17 | 1.94 |
| 0.875 – 1.000 | 8.63 | 1.19 | 1.31 |

Table 4: The di-jet cross-section as a function of $x_\gamma$ for the regions of the mean transverse energy $\bar{E}_{\text{jet}}^T$ of the di-jet system and the region in $x_\gamma^+ - x_\gamma^-$-space indicated in the table.
Table 5: The di-jet cross-section as a function of $x_\gamma$ for the regions of the mean transverse energy $\bar{E}_T^{\text{jet}}$ of the di-jet system and the region in $x_\gamma^+ - x_\gamma^-$-space indicated in the table.

| $x_\gamma$ | $\frac{d\sigma_{\text{di-jet}}}{dx_\gamma}$ [pb] | $\delta_{\text{stat}}$ [pb] | $\delta_{\text{sys}}$ [pb] |
|------------|---------------------------------|----------------------------|-----------------------------|
| $x_\gamma^+ < 0.75$ |
| $5 \text{ GeV} < \bar{E}_T^{\text{jet}} < 7 \text{ GeV}$ |
| 0.000 - 0.125 | 42.37 | 2.94 | 4.71 |
| 0.125 - 0.250 | 37.66 | 2.44 | 4.32 |
| 0.250 - 0.375 | 26.87 | 1.99 | 2.66 |
| 0.375 - 0.500 | 19.63 | 1.88 | 1.49 |
| 0.500 - 0.625 | 17.84 | 1.55 | 1.10 |
| 0.625 - 0.750 | 26.71 | 3.86 | 1.73 |
| $7 \text{ GeV} < \bar{E}_T^{\text{jet}} < 11 \text{ GeV}$ |
| 0.000 - 0.125 | 8.81 | 1.08 | 1.54 |
| 0.125 - 0.250 | 11.00 | 1.00 | 1.72 |
| 0.250 - 0.375 | 10.30 | 0.96 | 1.24 |
| 0.375 - 0.500 | 8.10 | 0.81 | 0.76 |
| 0.500 - 0.625 | 7.49 | 0.94 | 0.64 |
| 0.625 - 0.750 | 8.51 | 1.58 | 0.72 |
| log$_{10}(x_\gamma)$ | $\frac{d\sigma}{d\log_{10}(x_\gamma)}$ [pb] | $\delta_{\text{stat}}$ [pb] | $\delta_{\text{sys}}$ [pb] |
|---------------------|---------------------------------|-----------------|-----------------|
| 5 GeV $< E^{\text{jet}}_T$ < 7 GeV |
| full $x_\gamma^+ - x_\gamma^-$ range |
| -1.65 - -1.32 | 4.00 | 0.42 | 0.42 |
| -1.32 - -0.99 | 9.54 | 0.76 | 1.07 |
| -0.99 - -0.66 | 16.55 | 1.12 | 1.83 |
| -0.66 - -0.33 | 27.51 | 1.39 | 2.35 |
| -0.33 - 0.00 | 76.87 | 1.69 | 5.05 |
| $x_\gamma^+$ or $x_\gamma^- < 0.75$ |
| -1.65 - -1.32 | 1.29 | 0.18 | 0.18 |
| -1.32 - -0.99 | 2.38 | 0.24 | 0.32 |
| -0.99 - -0.66 | 3.64 | 0.30 | 0.44 |
| -0.66 - -0.33 | 4.87 | 0.38 | 0.47 |
| -0.33 - 0.00 | 25.87 | 0.99 | 2.16 |
| $x_\gamma^+ < 0.75$ |
| -1.65 - -1.32 | 3.08 | 0.44 | 0.41 |
| -1.32 - -0.99 | 7.81 | 0.63 | 1.02 |
| -0.99 - -0.66 | 13.95 | 0.92 | 1.55 |
| -0.66 - -0.33 | 19.39 | 1.13 | 1.78 |
| -0.33 - 0.00 | 25.87 | 1.53 | 1.36 |

Table 6: The di-jet cross-section as a function of log$_{10}(x_\gamma)$ for the region of the mean transverse energy $E^{\text{jet}}_T$ of the di-jet system and the regions in $x_\gamma^+ - x_\gamma^-$-space indicated in the table.
Table 7: The di-jet cross-section as a function of $|\Delta \eta^{\text{jet}}|$ for the two leading jets in $E_T^{\text{jet}}$, for the two regions in $x_{\gamma^+}^\pm$-$x_{\gamma^-}^\pm$-space indicated in the table.
| $|\eta^\text{jet}_{\text{cntr}}|$ | $\frac{d\sigma_{\text{di-jet}}}{d|\eta^\text{jet}_{\text{cntr}}|}$ [pb] | $\delta_{\text{stat}}$ [pb] | $\delta_{\text{sys}}$ [pb] |
|---|---|---|---|
| $x_\gamma^+$ or $x_\gamma^-$ < 0.75 |
| 0.00 – 0.25 | 11.48 | 0.50 | 0.65 |
| 0.25 – 0.50 | 9.25 | 0.44 | 0.55 |
| 0.50 – 0.75 | 7.19 | 0.38 | 0.46 |
| 0.75 – 1.00 | 5.30 | 0.32 | 0.31 |
| 1.00 – 1.25 | 3.49 | 0.26 | 0.23 |
| 1.25 – 1.50 | 2.60 | 0.24 | 0.25 |
| 1.50 – 1.75 | 1.49 | 0.21 | 0.17 |
| $x_\gamma^\pm$ < 0.75 |
| 0.00 – 0.25 | 14.93 | 0.67 | 1.24 |
| 0.25 – 0.50 | 13.38 | 0.65 | 1.17 |
| 0.50 – 0.75 | 10.83 | 0.60 | 0.96 |
| 0.75 – 1.00 | 7.17 | 0.47 | 0.60 |
| 1.00 – 1.25 | 5.59 | 0.46 | 0.54 |
| 1.25 – 1.50 | 3.20 | 0.41 | 0.41 |
| 1.50 – 1.75 | 2.01 | 0.41 | 0.32 |

Table 8: The di-jet cross-section as a function of $|\eta^\text{jet}_{\text{cntr}}|$ for the two regions in $x_\gamma^+ - x_\gamma^-$-space indicated in the table.
| $|\eta_{\text{fwd}}^{\text{jet}}|$ | $\frac{d^2\sigma_{\text{di-jet}}}{d|\eta_{\text{fwd}}^{\text{jet}}|}$ [pb] | $\delta_{\text{stat}}$ [pb] | $\delta_{\text{sys}}$ [pb] |
|----------------|----------------|----------------|----------------|
| $x_+^\gamma$ or $x_-^\gamma < 0.75$  
0.00 – 0.25 | 0.906 | 0.137 | 0.065 |
0.25 – 0.50 | 2.68 | 0.23 | 0.18 |
0.50 – 0.75 | 4.30 | 0.29 | 0.26 |
0.75 – 1.00 | 5.65 | 0.33 | 0.33 |
1.00 – 1.25 | 6.18 | 0.34 | 0.33 |
1.25 – 1.50 | 6.86 | 0.36 | 0.34 |
1.50 – 1.75 | 7.27 | 0.40 | 0.48 |
1.75 – 2.00 | 7.03 | 0.44 | 0.55 |
| $x_\gamma^\pm < 0.75$  
0.00 – 0.25 | 1.03 | 0.17 | 0.16 |
0.25 – 0.50 | 4.11 | 0.38 | 0.54 |
0.50 – 0.75 | 5.64 | 0.40 | 0.60 |
0.75 – 1.00 | 6.71 | 0.41 | 0.51 |
1.00 – 1.25 | 8.40 | 0.47 | 0.74 |
1.25 – 1.50 | 10.72 | 0.62 | 0.94 |
1.50 – 1.75 | 11.30 | 0.68 | 1.18 |
1.75 – 2.00 | 9.86 | 0.72 | 0.96 |

Table 9: The di-jet cross-section as a function of $|\eta_{\text{fwd}}^{\text{jet}}|$ for the two regions in $x_\gamma^+ - x_\gamma^-$-space indicated in the table.
Figure 1: (a)-(c): The relative contribution of direct, single-resolved, and double-resolved processes according to PYTHIA at the hadron level for the cross-sections as a function of $x_\gamma$ for the full $x_+^\gamma - x^-_\gamma$-range (see Section 4). In (d) the regions in $x_+^\gamma - x^-_\gamma$-space used in addition to the full $x_+^\gamma - x^-_\gamma$-range (referred to as (A)) are illustrated: (B) both $x_+^\gamma$ and $x^-_\gamma$ larger than 0.75 ($x_+^\gamma > 0.75$), (C) either $x_+^\gamma$ or $x^-_\gamma$ smaller than 0.75 ($x_+^\gamma$ or $x^-_\gamma < 0.75$), (D) both $x_+^\gamma$ and $x^-_\gamma$ smaller than 0.75 ($x_+^\gamma < 0.75$).
Figure 2: Comparison of event quantities for uncorrected data with the simulation for the di-jet sample including contributions from background processes. (a) shows the sum of energy measured in the electromagnetic and hadronic calorimeter, (b) the number of tracks in the event, (c) is the sum of energy in the FD detector scaled by the beam energy, and (d) the invariant mass of the jet with the highest $E_{T}^{jet}$ in the event and the four-vector calculated from all objects in the opposite hemisphere as seen from this jet. The statistical error is shown where larger than the marker size. The label $\gamma^*\gamma$ stands for simulated photon-photon collision events in which one of the photons has a virtuality larger than 4.5 GeV$^2$ as discussed in Section 7.
Figure 3: Jet profiles: The $E_T$-flow normalised to the number of jets $N_{jet}$ as a function of the distance from the jet axis in $\phi$ and $\hat{\eta}$. Jets are selected from the range $10 < E_{jet}^T < 25 \text{ GeV}$. The statistical error is shown where larger than the marker size. The data are compared to a mixture of signal (PHOJET or PYTHIA) and background MC simulation. The background MC simulations used are the same as in Figure 2.
Figure 4: The energy-flow as a function of $\hat{\eta}$ where the area around the two leading jets in the event has been excluded in a cone of radius 1.3 in $\eta$-$\phi$-space. The distributions are normalised to the number of di-jet events $N$. The statistical error is shown where larger than the marker size. The regions in $x_{\gamma}^+$-$x_{\gamma}^-$-space considered and the MC simulations used are the same as in Figure 3.
Figure 5: The uncorrected $x_\gamma$ distributions in the data compared to the sum of signal and background processes in the simulation. The statistical error is shown where larger than the marker size. The MC simulations used are the same as in Figure 2.
Figure 6: Hadronisation corrections estimated by PYTHIA and HERWIG for (a) $E^{\text{jet}}_T$ and (b)-(d) $x_\gamma$ for the regions of $E^{\text{jet}}_T$ given in the figure. In all cases the full $x_\gamma^+ - x_\gamma^-$-space is considered.
Figure 7: The jet shape, $\Psi(r)$, for the two regions of $x^+_\gamma-x^-_\gamma$-space indicated in the figure (a), and $\Psi(r)$ for $x^\pm_\gamma < 0.75$ compared to the predictions of the LO MC generators PHOJET and PYTHIA (b). Figures (c) and (d) show the value of $\Psi(r = 0.4)$ as a function of the transverse energy and pseudo-rapidity of the jet respectively, compared to the PYTHIA prediction. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors.
Figure 8: The value of the jet shape $\Psi(r)$ at $r = 0.4$ as a function of the jet transverse energy for $x_\gamma^\pm < 0.75$ (a) and $x_\gamma^\pm > 0.75$ (b), and as a function of the jet pseudo-rapidity for $x_\gamma^\pm < 0.75$ (c) and $x_\gamma^\pm > 0.75$ (d). In each figure the results obtained using the inclusive $k_\perp$ and the cone jet algorithm are shown and compared to the PYTHIA prediction. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors.
Figure 9: The di-jet cross-section as a function of $|\cos \Theta^*|$ for the two regions in $x_{\gamma}^\pm - x_{\gamma}^-$ space indicated in the figure. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Table 1. A perturbative NLO QCD prediction [29] using the GRVHO parton densities is compared to the data after hadronisation corrections have been applied to the calculation. The shaded band indicates the theoretical uncertainty estimated by the quadratic sum of two contributions: variation of the renormalisation scale by factors of 0.5 and 2 and the difference between using HERWIG or PYTHIA in estimating the hadronisation corrections.
Figure 10: The di-jet cross-section as a function of the mean transverse energy $E_T^{\text{jet}}$ of the di-jet system, for the three regions in $x_\gamma^+-x_\gamma^-$-space given in the figure. The factor $f$ is used to separate the three measurements in the figure more clearly. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Table 2. The prediction of the LO program PYTHIA using the parton distribution function SaS 1D is compared to the data. The NLO calculation is the same as in Figure 9.
Figure 11: The di-jet cross-section as a function of $x_\gamma$ and $\log_{10}(x_\gamma)$ for the regions of the mean transverse energy $\bar{E}_T^{\text{jet}}$ of the di-jet system indicated in the figures. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Tables 3 and 6. The prediction of the LO MC generator PYTHIA using the parton distribution function SaS1D is compared to the data. The shaded histogram at the bottom of each plot indicates the MIA contribution to the PYTHIA prediction. The NLO calculation is the same as in Figure 9.
Figure 12: The prediction of NLO QCD using different parton distributions for the photons. The di-jet cross-section as a function of $x_\gamma$ for $5 \text{ GeV} < \bar{E}_{\text{jet}}^{T} < 7 \text{ GeV}$ (upper left plot in Figure 11) is shown. In (a) the full cross-section is shown after hadronisation corrections have been applied, while (b), (c) and (d) show the $gg$, $gq$ and $qq$ contributions to this cross-section without hadronisation corrections. The NLO calculation is the same as in Figure 9.
Figure 13: The di-jet cross-section as a function of $x_\gamma$ and $\log_{10}(x_\gamma)$ for the regions of the mean transverse energy $E_T^{\text{jet}}$ of the di-jet system indicated in the figures and for $x_\gamma^+ \text{ or } x_\gamma^- < 0.75$. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Tables 4 and 6. The NLO calculation and MC simulation are the same as in Figure 11.
Figure 14: The di-jet cross-section as a function of $x_\gamma$ and $\log_{10}(x_\gamma)$ for the regions of the mean transverse energy $\overline{E}_T^{\text{jet}}$ of the di-jet system indicated in the figures. For these cross-sections $x_\gamma^\pm < 0.75$ is required. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Tables 5 and 6. The NLO calculation and MC simulation are the same as in Figure 11.
Figure 15: The di-jet cross-section as a function of $|\Delta \eta_{\text{jet}}|$ for the two leading jets in $E_T^{\text{jet}}$ and separately for the central and the forward jet, for $x_\gamma^+ \text{ or } x_\gamma^- < 0.75$. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Tables 7, 8 and 9. The NLO calculation and MC simulation are the same as in Figure 11.
Figure 16: The di-jet cross-section as a function of $|\Delta\eta_{\text{jet}}|$ for the two leading jets in $E_{\text{jet}}^T$ and separately for the central and the forward jet. For these cross-sections $x_{\gamma}^\pm < 0.75$ is required. The total of statistical and systematic uncertainties added in quadrature is shown where larger than the marker size. The inner error bars show the statistical errors. The numerical values are given in Tables 7, 8 and 9. The NLO calculation and MC simulation are the same as in Figure 11.
\[ \frac{d\sigma}{d|\Delta\eta_{\text{jet}}|} \] 

- OPAL

\[ x_\gamma^+ < 0.75 \]

\[ \text{NLO (1+\delta_{\text{hadr}})} \]

- PYTHIA SaS 1D

- PYTHIA MIA

contribution