Coherent Microwave-to-Optical Conversion via Six-Wave Mixing in Rydberg Atoms

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We present an experimental demonstration of converting a microwave field to an optical field via frequency mixing in a cloud of cold $^{87}$Rb atoms, where the microwave field strongly couples to an electric dipole transition between Rydberg states. We show that the conversion allows the phase information of the microwave field to be coherently transferred to the optical field. With the current energy level scheme and experimental geometry, we achieve a photon conversion efficiency of $\sim 0.3\%$ at low microwave intensities and a broad conversion bandwidth of more than 4 MHz. Theoretical simulations agree well with the experimental data, and indicate that near-unit efficiency is possible in future experiments.

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Coherent and efficient conversion from microwave and terahertz radiation into optical fields and vice versa has tremendous potential for developing next-generation classical and quantum technologies. For example, these methods would facilitate the detection and imaging of millimeter waves with various applications in medicine, security screening and avionics. In the quantum domain, coherent microwave-optical conversion is essential for realizing quantum hybrid systems, where spin systems or superconducting qubits are coupled to optical photons that can be transported with low noise in optical fibers. The challenge in microwave-optical conversion is to devise a suitable platform that couples strongly to both frequency bands, which are separated by several orders of magnitude in frequency, and provides an efficient link between them. Experimental work on microwave-optical conversion has been based on ferromagnetic magnons, frequency mixing in $\Lambda$-type atomic ensembles, whispering gallery resonators, or nanomechanical oscillators. All of these schemes include cavities to enhance the coupling to microwaves. The realization of near-unit conversion efficiencies as required for transmitting quantum information remains an outstanding and important goal. Recently, highly excited Rydberg atoms have been identified as a promising alternative as they feature strong electric dipole transitions in a wide frequency range from microwaves to terahertz.

In this letter, we demonstrate coherent microwave-to-optical conversion of classical fields via six-wave mixing in Rydberg atoms. Due to the strong coupling of millimeter waves to Rydberg transitions, the conversion is realized in free space. In contrast to millimeter-wave induced optical fluorescence, frequency mixing is employed here to convert a microwave field into a unidirectional single frequency optical field. The long lifetime of Rydberg states allows us to make use of electromagnetically induced transparency (EIT), which significantly enhances the conversion efficiency. A free-space photon-conversion efficiency of 0.3% with a bandwidth of more than 4 MHz is achieved with our current experimental geometry. Optimized geometry and energy level configurations should enable the broadband interconversion of microwave and optical fields with near-unit efficiency. Our results thus constitute a major step towards using Rydberg atoms for transferring quantum states between optical and microwave photons.

The energy levels for the six-wave mixing are shown in Fig. 1(a), and the experimental setup is illustrated in Fig. 1(b). The conversion of the input microwave field $M$ into the optical field $L$ is achieved via frequency mixing with four input auxiliary fields $P$, $C$, $A$, and $R$ in a cold atomic cloud. Starting from the spin polarized ground state, the auxiliary fields and the microwave field, all of which are nearly resonant with the corresponding atomic transitions, create a coherence between the states $|1\rangle$ and $|6\rangle$. This induces the emission of the light field $L$ with frequency $\omega_L = \omega_P + \omega_C - \omega_A + \omega_M - \omega_R$ such that the resonant six-wave mixing loop is completed, where $\omega_X$ is the frequency of field $X$ ($X \in \{P,R,M,C,L,A\}$). The emission direction of field $L$ is determined by the phase matching condition $k_L = k_P + k_C - k_A + k_M - k_R$, where $k_X$ is the wave vector of the corresponding field. The wave vectors of the microwave fields $k_A$ and $k_M$ are negligible since they are much smaller than those of the optical fields and to an excellent approximation, they cancel each other. Moreover, we have $k_C \approx k_R$, thus the converted light field $L$ propagates in the same direction as the input field $P$. The transverse profile of the converted light field $L$ resembles that of the auxiliary field $P$ due to pulse matching as illustrated in Fig. 1(b).

An experimental measurement begins with the preparation of a cold cloud of $^{87}$Rb atoms in the $|5S_{1/2},F = 2,m_F = 2\rangle$ state in a magnetic field of 6.1 G, as described previously in [25]. At this stage, the atomic
cloud has a temperature of about 70 \( \mu \text{K} \), a \( 1/e^2 \) radius of \( w_z = 1.85(10) \) mm along the \( z \) direction, and a peak atomic density \( n_0 = 2.1(2) \times 10^{10} \text{ cm}^{-3} \). We then switch on all the input laser and microwave fields simultaneously for frequency mixing. The beams for both \( C \) and \( R \) fields are derived from a single 482 nm laser, while the fields \( M \) and \( A \) are emitted from two separate horn antennas, and propagate collinearly along the \( z \) axis. They are focused onto the center of a Gaussian-distributed atomic cloud. The fields \( M \) and \( A \) are emitted from horn antennas enclosing an angle of 20\( ^\circ \), and propagate horizontally. The bias magnetic field \( B \) along \( z \) defines the quantization axis. The co-propagating fields \( L \) and \( P \) are separated by a polarization splitter (\( \lambda/4 \) + PBS) and detected simultaneously with avalanche photodiodes. The inset shows the simulated intensity and beam profile of the \( L \) field.

\[ \Omega_M = 45(12) \text{ MHz} \]
\[ \Omega_A = 25(12) \text{ MHz} \]

\[ \Omega_M / \Omega_A \approx 1.8 \]

\[ \Delta \approx 1.25(12) \text{ MHz} \]

\[ \text{error bars indicate the standard deviation of 5 measurements.} \]

\[ \text{The solid lines show the fit of a [sin] function to the data.} \]

\[ \text{Relative phase of the heterodyne signals for a phase modulated M field.} \]

\[ \text{Triangular modulations of 7kHz and 3\pi amplitude (green circles) and of 14kHz and 3\pi amplitude (blue squares) are shown.} \]

\[ \text{The phase is extracted by numerically demodulating the heterodyne signals.} \]

\[ \text{FIG. 2. (a) Spectra of fields P (red squares) and L (purple circles).} \]

\[ \text{The microwave field M has detuning \( \Delta_M = 0 \) and Rabi frequency \( \Omega_M = 2\pi \times 1.25(12) \text{ MHz} \).} \]

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\[ \text{FIG. 1. (a) Relevant energy levels of a} \text{ } ^{87}\text{Rb} \text{ atom coupled by six nearly-resonant electromagnetic fields:} \]

\[ |1\rangle = |5S_{1/2}, F = 2, m_F = 2\rangle, |2\rangle = |5P_{3/2}, F = 3, m_F = 3\rangle, |3\rangle = |3D_{3/2}, m_J = 1/2\rangle, |4\rangle = |3P_{3/2}, m_J = 1/2\rangle, |5\rangle = |3D_{3/2}, m_J = 1/2\rangle, |6\rangle = |5P_{3/2}, F = 2, m_F = 1\rangle. \]

\[ \text{Polarizations of the fields are indicated in brackets.} \]

\[ \text{The microwave field M (\approx 84 GHz) is converted to the light field L (\approx 780 nm) by six-wave mixing.} \]

\[ \text{(b) Experimental setup. Auxiliary light fields P, C, and R propagate collinearly along the z axis.} \]

\[ \text{They are focused onto the center of a Gaussian-distributed atomic cloud.} \]

\[ \text{The fields M and A are emitted from horn antennas enclosing an angle of 20\(^\circ\), and propagate horizontally.} \]

\[ \text{The bias magnetic field B along z defines the quantization axis.} \]

\[ \text{The co-propagating fields L and P are separated by a polarization splitter (\( \lambda/4 \) + PBS) and detected simultaneously with avalanche photodiodes.} \]

\[ \text{The inset shows the simulated intensity and beam profile of the L field.} \]

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Second, to verify the coherence of the conversion, we perform optical heterodyne measurements between the L field and a reference field that is derived from the same laser as the P field. Fig. 2(b) shows that the Fourier spectrum of a 500 μs long beat note signal has a transform limited sinc function dependence. The central frequency of the spectrum confirms that the frequency of the converted field L is determined by the resonance condition for the six-wave mixing process. Furthermore, we phase modulate the M field with a triangular modulation function and observe the recovery of the phase modulation in the optical heterodyne measurements, as shown in Fig. 2(c). This demonstrates that the phase information is coherently transferred in the conversion, as expected for a nonlinear frequency mixing process.

We simulate the experimental spectra by modelling the interaction of the laser and microwave fields with the atomic ensemble within the framework of coupled Maxwell-Bloch equations. The time evolution of the atomic density operator is given by a Markovian master equation (ℏ is the reduced Planck constant),

$$\dot{\rho} = -\frac{i}{\hbar}[H, \rho] + L_\gamma \rho + L_{\text{deph}} \rho, \quad (1)$$

where $H$ is the Hamiltonian describing the interaction of an independent atom with the six fields, and the term $L_\gamma \rho$ describes spontaneous decay of the excited states. The last term $L_{\text{deph}} \rho$ in Eq. (1) accounts for dephasing of atomic coherences involving the Rydberg states $|3\rangle$, $|4\rangle$, and $|5\rangle$ with the dephasing rates $\gamma_d$, $\gamma_{DD}$, and $\gamma_d'$, respectively. The sources of decoherence are the finite laser linewidths, atomic collisions, and dipole-dipole interactions between Rydberg atoms. The dephasing rates affect the P and L spectra and are found by fitting the steady state solution of coupled Maxwell-Bloch equations to the experimental spectra in Fig. 2(a). All other parameters are taken from independent experimental measurements and calibrations. We obtain $\gamma_d = 2\pi \times 150$ kHz, $\gamma_{DD} = 2\pi \times 150$ kHz and $\gamma_d' = 2\pi \times 560$ kHz and keep these values fixed in all simulations.

The system in Eq. (1) exhibits an approximate dark state

$$|D\rangle \propto (\Omega_0^* \Omega_1^* |1\rangle - \Omega_3^* \Omega_P^* |3\rangle + \Omega_4^* \Omega_P^* |5\rangle) \quad (2)$$

for $\Omega_1^* / \Omega_P = -\Omega_3^* / \Omega_4^* / (\Omega_2^* / \Omega_5^*)$, where $\Omega_i$ is the Rabi frequency of field $i$. This state has non-zero population only in metastable states $|1\rangle$, $|3\rangle$, and $|5\rangle$, and is decoupled from all the other fields. The population in $|D\rangle$ increases with the build-up of the converted light field along the $z$ direction, and thus $P_L$ saturates when all atoms are trapped in this state. Fig. 4 shows the dependence of the output power $P_L$ on the optical depth $D_P \propto \eta_0 z_0$ of the atomic cloud, and the theory curve agrees well with the experimental data. The predicted saturation at $D_P \approx 20$ is consistent with the population in $|D\rangle$ exceeding 99.8% at this optical depth.

Next, we analyze the dependence of the conversion process on detuning and intensity of the microwave field M. All auxiliary fields are kept on resonance and at constant intensity. Fig. 2(a) shows $P_L$ as a function of the microwave detuning $\Delta_M$. We find that the spectrum of the L field can be approximated by a squared Lorentzian function centered at $\Delta_M = 0$, and its full width at half maximum (FWHM) is $\approx 6$ MHz. The FWHM extracted from microwave spectra at different intensities $I_M$ is plotted in Fig. 2(b). The FWHM has a finite value $> 4$ MHz in the low intensity limit, and increases slowly with $I_M$ due to power broadening. This large bandwidth is one of the distinguishing features of our scheme and is essential for extending the conversion scheme to the single photon level [13]. In Fig. 4(c), we show measurements of $P_L$. 

FIG. 3. $P_L$ vs. optical depth $D_P$, with all fields on resonance. $D_P$ is varied by changing $n_0$, and the other conditions are the same as for Fig. 2(a). The circles are experimental data, and the solid line is the theoretically simulated curve. The error bars correspond to the standard deviation of 4 measurements.

FIG. 4. (a) Spectrum of $P_L$ against microwave detuning $\Delta_M$ for $I_M = 42(8)$ pW/mm$^2$. (b) FWHM vs. $I_M$. The FWHM is extracted by fitting a squared Lorentzian function to the spectra. (c) $P_L$ as a function of M field intensity $I_M$. The inset shows $P_L$ over a much larger range of $I_M$. (d) Efficiency $\eta$ calculated for the data shown in (c). Circles represent experimental data and solid curves simulation results. Vertical error bars in (a) and (c) correspond to the standard deviation of 4-6 measurements, and in (b) to the errors from fitting. Horizontal error bars in (c) are estimated uncertainties. The error bars in (d) are calculated from those in (c).
vs. the intensity of the microwave field $I_M$ at $\Delta_M = 0$. We find that the converted power $P_L$ increases approximately linearly at low microwave intensities, and thus our conversion scheme is expected to work in the limit of very weak input fields. The decrease of $P_L$ at large intensities arises because the six-wave mixing process becomes inefficient if the Rabi frequency $\Omega_M$ is much larger than the Rabi frequency $\Omega_A$ of the auxiliary microwave. All the theoretical curves in Fig. 4 agree well with the experimental data.

We evaluate the photon conversion efficiency of our setup by considering the cylindrical volume $V$ where the atomic cloud and all six fields overlap. This volume has a diameter $\sim 2w_L$ and a length $\sim 2w_z$ [see Fig. 1(b)]. We define the conversion efficiency as

$$\eta = \frac{P_L/h\omega_L}{I_M S_M / h\omega_M}, \quad (3)$$

where $S_M = 4w_P w_z$ is the cross-section of the volume $V$ perpendicular to $k_M$. The efficiency $\eta$ gives the ratio of the photon flux in $L$ leaving volume $V$ over the photon flux in $M$ entering $V$. As shown in Fig. 1(d), the conversion efficiency is approximately $\eta \approx 0.3%$ over a range of low intensities and then decreases with increasing $I_M$.

Note that $\eta$ in Eq. (3) is a measure of the efficiency of the physical conversion process in the Rydberg medium based on the microwave power $P_M S_M$ impinging on $S_M$. This power is smaller than the total power emitted by the horn antenna since the $M$ field has not been focused on $V$ in our setup.

The good agreement between our model and the experimental data allows us to theoretically explore other geometries. To this end we consider that the microwave fields $M$ and $A$ are co-propagating with the $P$ field, and assume that all other parameters are the same [28]. We numerically evaluate the generated light power $P_L^\parallel$ for this setup and calculate the efficiency $\eta^\parallel$ by replacing $P_L$ with $P_L^\parallel$ and $S_M$ with $S_M = \pi w_L^2$ in Eq. (3). We find $\eta^\parallel \approx 26\%$, which is approximately two orders of magnitude larger than $\eta$. This increase is mostly due to the geometrical factor $S_M / S_M^\parallel \approx 91$, since $P_L^\parallel \sim P_L$. Note that such a value for $\eta^\parallel$ is consistent with the efficiency achieved by a similar near-resonance frequency mixing scheme in the optical domain [23].

In conclusion, we have demonstrated coherent microwave-to-optical conversion via a six-wave mixing process utilizing the strong coupling of electromagnetic fields to Rydberg atoms. We have established the coherence of the conversion by a heterodyne measurement and demonstrated a large bandwidth by measuring the generated light as a function of the input microwave frequency. Coherence and large bandwidth are essential for taking our scheme to the single photon level and using it in quantum technology applications. Our results are in good agreement with theoretical simulations based on an independent atom model thus showing a limited impact of atom-atom interaction on our conversion scheme.

This work has focussed on the physical conversion mechanism in Rydberg systems and provides several possibilities for future studies and applications. All alkali atom transitions offer a wide range of frequencies in the optical and microwave domain with properties similar to those exploited in this work. For example, the conversion of a microwave field to telecommunication wavelengths is possible by switching to different optical transitions and/or using different atomic species [18, 30, 31], which makes our approach promising for classical and quantum communication applications. Moreover, it has been theoretically shown that bidirectional conversion with near-unit efficiency is possible by using a different Rydberg excitation scheme and well-chosen detunings of the auxiliary fields [17]. Such non-linear conversion with near-unit efficiency has only been experimentally realized in the optical domain [21]. Reaching this level of efficiency requires good mode-matching between the millimeter waves and the auxiliary optical fields [17], which can be achieved either by tightly focusing the millimeter wave, or by confining it to a waveguide directly coupled to the conversion medium [11, 32]. Eventually, extending our conversion scheme to millimeter waves in a cryogenic environment [33, 34] would pave the way towards quantum applications.
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