Construction of virtual mulch film model based on discrete element method and simulation of its physical mechanical properties

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Abstract: In China, especially in Xinjiang Region, mulch film remaining in the soil has severely jeopardized the safety of soil resources. To numerically simulate the residual film-soil-recovery implementation system, a virtual mulch film model with consistent physical and mechanical properties with real mulch film needs to be established. In this study, a flexible deformable virtual mulch film model was constructed using YADE software based on the Minkowski Sum principle and the ball-ball force-displacement constitutive rule, as well as the contact failure rule were established. The deformation behaviors of cylinders and PFacet elements, such as stretching, bending, and torsion, were described. By splicing the basic PFacet elements, a virtual mulch model was established. The mechanical model of a virtual mulch film under tension was established and the axial tensile stiffness coefficient $k_t$ was determined to be 43.30 N-m. To verify the physical and mechanical properties of this virtual mulch film, both real and virtual stretching and tearing tests were conducted. The experimental results showed that: in the process of stretching and tearing of real and virtual films, the properties of morphological features of both are basically identical; however, they clearly differ in force-displacement. The viscoelastic constitutive model between balls and yield judgment conditions requires further study.

Keywords: discrete element method, mulching film, physical and mechanical properties, virtual test

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1 Introduction

China has introduced under-film drip irrigation technology since the 1970s, which has greatly increased the utilization efficiency of water resources and crop output. Because of the high labor intensity, high recycling costs, immaturity of the required recycling equipment, and farmers’ lack of attention for the recycling of plastic mulch film, a large amount of mulch film is not recycled and has been buried in the tillage soil layer. According to a survey conducted by the Agriculture Department of Xinjiang Uygur Autonomous Region, China, the average residual mulch film in the soil in Xinjiang has reached 268.65 kg/ha. This severely jeopardizes the safety of agricultural soil resources in Xinjiang Region[1–5].

The Chinese Government has paid much attention to residual-film pollution in tillage soil. At present, the recycling methods for this type of pollution are mainly via rotary tiller, chain sieve, excavation screening, shovel, chain rake, and other instruments[6–11]. The process of recycling residual film from tillage soil involves interaction with residual film-soil-recycling machinery. To conduct numerical simulation research on this type of interaction, the first important task is to construct a virtual plastic mulch film and ensure that the virtual model has the same physical and mechanical properties with real mulch film[12,13].

In China, most scholars used the finite element method to construct membranes. Wen et al.[14] used the software ANSYS to analyze the natural vibration characteristics of cable-membranes. Han et al.[15] performed a finite element simulation of an inflatable membrane, based on LS-DYNA. Jin[16] used ADINA software to perform a finite element simulation of tensile membranes.

Lobo-Guerrero et al.[17] constructed a flexible film using the discrete element method (DEM). Tran et al.[18] studied geogrid-soil interaction using the finite-discrete coupling method. Effendzourou et al.[19] proposed a general method for the building of deformable and arbitrarily shaped object models under the DEM framework. Thoen[20] used the Minkowski sums method to establish a discrete element model of geotextile.

Both geotextiles and mulch films are flexible, but their features are significantly different in thickness, strength, and structural composition. Therefore, the construction of virtual mulch differs from geotextile construction. In this paper a physical model of mulch film was established based on the Minkowski sums method under the framework of DEM. For this, virtual stretching and tearing simulation were used to verify the physical and mechanical properties of the virtual mulch film.

2 Methods for virtual mulch film construction

The existing methods of constructing virtual mulch film mainly include the particle cluster method and the Minkowski sums method.
2.1 Particle cluster method

Figure 1 shows the particle clustering method in which a multitude of spherical particles are added and joined to form a flexible film. Spherical particles are allowed to move relative to each other, thus enabling flexible deformation. However, adjacent spherical particles are in point contact, and there is a gap between them. The existence of the resulting pores results in the surface of a flexible membrane to not be smooth, i.e., producing artificial surface roughness. Therefore, virtual mulch constructed by particle clustering is significantly different from a real smooth mulch film.

![Figure 1: Virtual film structure using the particle cluster method](image1)

2.2 Minkowski sums method

The Minkowski sums theory superimposes two arbitrary spatial bodies in Euler coordinates and forms a new space body. In the extended particle model, a space body can adopt a straight line, a disk, a rectangle, or a polyhedron. The base unit can be simplified as a sphere. The expansion unit can be regarded as covering a surface of the base unit with a layer of an expanding sphere, the center of gravity of which is located on the surface of the basic unit body. Since the basic unit can be set to any shape, the extended sphere can be of any size and can be expanded into units of any shape based on this method.

A membrane constructed by the Minkowski sums method has a smooth surface, no artificial surface roughness, and has a more similar appearance to the real film. Therefore, this method was chosen in this study. YADE is the only discrete element software that enables the creation of a film structure using the Minkowski sums method. Therefore, YADE was used.

3 Discrete element method based on ball-ball contact rule

The ball-ball contact constitutive rule is the basic constitutive rule for the construction of the virtual mulch film model by the DEM. The types of spherical particles that currently constitute the DEM are classified into rigid-ball and soft-ball model. This paper adopts the rigid-ball model, which does not allow deformation. The ball-ball contact constitutive rule is mainly composed of the force-displacement rule and the contact failure rule.

3.1 Force-displacement rule

The force-displacement rule of ball-ball contact is shown in Figure 2. Only an axial remote virtual contact force is considered, while mutual torsion, friction, and scroll are ignored.

The contact force $\mathbf{F}$ was only considered between adjacent balls, and the direction $\mathbf{n}$ is the direction of the line that connects the center of ball $A$ and $B$, as shown in Equation (1):

$$\mathbf{F} = k_n (d^{AB} - D_{eq}) \mathbf{n}$$  (1)

where, $k_n$ represents the equivalent normal contact stiffness coefficient; $d^{AB}$ represents the actual distance between the centers of ball $A$ and $B$; $D_{eq}$ represents the equilibrium distance between the centers of ball $A$ and $B$; $\mathbf{n}$ represents a unit vector with the direction from the center of ball $A$ to that of ball $B$.

When $d^{AB} = D_{eq}$, the axial contact force is zero; when $d^{AB} > D_{eq}$, the contact force is tensile; when $d^{AB} < D_{eq}$, the contact force is compressive. Because of the flexible physical properties of mulch film, the compression phenomenon was not considered, i.e., only the cases of $d^{AB} > D_{eq}$ and $d^{AB} = D_{eq}$ were considered.

Because the thickness of mulch film is typically 0.01 mm, the flexibility of mulch film is particularly high; therefore, the contact torque of mulch film was ignored.

![Figure 2: Force-displacement constitutive model of ball-ball contact](image2)

3.2 Contact failure rule

The damage modes of mulch film were mainly tensile failure and tear failure, regardless of bending and torsion damage. The same failure rule was adopted for tensile failure and tear failure, i.e., when the tensile force between particles exceeds the ultimate connection force, the connection between particles fails and the membrane unit breaks. The rule of failure is shown in Figure 3.

$$\sigma \leq \frac{\mathbf{F}}{A} = F_{max}$$  (2)

where, $\sigma$ represents the tensile strength, and $A$ represents the equivalent contact area.

When the tensile force exceeds the tensile limit, this results in tensile failure, the virtual mulch film breaks, the tensile force becomes zero, and the bending and torsional moment also become zero.

![Figure 3: Rule of failure](image3)

4 Virtual mulch film construction

The constructed virtual mulch film model consists of three basic primitives: sphere, cylinder, and PFacet element. Both the cylinder and PFacet are deformable bodies, which are constructed based on the Minkowski sums principle. A discrete element model of mulch film was formed by adding geometric relationships to spherical, cylindrical, and PFacet.
4.1 Cylinder element

A cylinder corresponds to Minkowski sums of a ball and a line segment; therefore, it does not introduce any numerical roughness compared with a bounded particle model. It can withstand tensile, shear, bending, and torsional loads. The deformability of a cylinder is defined by the position and orientation of its two nodes.

As shown in Figure 4a, when the distance $d_{AB}$ between both ends of the cylinder exceeds the equilibrium distance $d_{eq}$, tensile force, equivalent to the tensile deformation of a cylinder, is generated in the axial direction. As shown in Figure 4b, when node B rotates around node A, bending deformation occurs, $\Omega_{AB}$ represents the bending angle; as shown in Figure 4c, when node B rotates around the normal of nodes A and B, a torsional deformation occurs, $\Omega_{AB}$ represents the torsion angle.

4.2 PFacet element

PFacet element is represented by a triangle line segment and a sphere through Minkowski sums. As shown in Figure 5, PFacet element consists of three nodes and three interconnected cylinders. The mechanical behavior can be represented by three cylinders. PFacet is similar to three connected cylinders. The difference is that a PFacet element has two contact surfaces (top surface and bottom surface), and the contact between these surfaces and other particles is defined by two contact surfaces; the thickness of PFacet depends on the diameter of spherical particles at the node.

The deformation behavior of a PFacet element is defined by changes in the coordinates and orientation of the three nodes. The mechanical behavior of a PFacet element is calculated by the constitutive law between the balls at the joint.

4.3 Establishment of a virtual mulch film model

The virtual mulch film is formed via splicing PFacet elements. A variety of methods is available to splice PFacet elements into a virtual mulch film. Figure 7 shows two geometric topological
structures. The topology shown in Figure 7a is asymmetric, Figure 7b shows a symmetric topology. Therefore, the mechanical properties of the topology shown in Figure 7b in all directions are consistent and continuous. In the end, the topology shown in Figure 7b was used to construct the virtual mulch film model.

At present, because of the requirements of the manufacturing process, polyethylene mulch has different mechanical properties in lateral and longitudinal directions. Because of topology, the virtual mulch with Topology 2 structure has the same mechanical properties in lateral and longitudinal directions. Many research tasks are still required to build a more realistic virtual mulch film.

![Figure 7: Topological mechanism of virtual mulch film](image)

It is required following a number of assumptions to splice discrete PFacet elements into a virtual mulch film model:

1) The quality of virtual mulch film is concentrated on the nodes;

2) Force and moment only exist in adjacent nodes;

3) The node-node distance is very large with respect to the diameter of the balls, independent of the friction between adjacent particles;

4) The diameter of the balls (0.01 mm) is equivalent to the thickness of the virtual mulch film.

The virtual mulch film is finally constructed as shown in Figure 8.

![Figure 8: Discrete element model of mulch film](image)

**5 Verification test of the physical and mechanical properties of the virtual film**

**5.1 Determination of the axial stiffness coefficient**

Figure 9 shows a schematic diagram of stretching real mulch film and virtual mulch film model.

![Figure 9: Schematic diagram of real and virtual stretching](image)

Figure 9 shows that the virtual mulch film model is equivalent to a simple truss mechanism, where only adjacent nodes can withstand the tensile force; however, the real mulch film is a continuous body, and can thus withstand continuous tension. Therefore, the axial stiffness coefficient of the virtual mulch film model cannot be simply transformed by the elastic modulus of real mulch film. To ensure consistent tensile performance between virtual and real plastic mulches, the following assumptions are made.

1) At the initial stretching stage, the virtual film is only displaced in the XOY plane, and does not undergo any prestress;

2) The gravity of the virtual film model is ignored;

3) Moments between particles in the XOY plane are ignored;

4) For small tensile displacement, transverse shrinkage deformation is ignored.

As shown in Figure 9, the initial distance between adjacent lateral and longitudinal nodes is defined as \(u\) (unit: mm), \(d\) represents the radius of the ball, \(D=2d\) is the equivalent thickness of virtual mulch film. When real and virtual mulch film both stretch for a length of \(\Delta l\), the tensile forces are \(F_1\) and \(F_2\), respectively. \(F_1=F_2\) should be satisfied when stretching for the same length.

The relationship between tensile force and displacement of real mulch film is as follows:

\[
F = A.E.\frac{\Delta L}{L} = W.D.E.\frac{\Delta L}{L}
\]

where, \(A\) represents the cross-sectional area of real film, \(A=W.D\), \(W\) represents the width of real mulch film, \(D\) represents the thickness of real and virtual mulch film, \(E\) represents the elastic modulus of real mulch film; \(\Delta L\) represents the stretch length of real and virtual mulch film, and \(L\) represents the length of real and virtual mulch film.

As shown in Figure 10, to simplify the virtual modeling, four adjacent PFacet elements are considered as basic primitives for the analysis. When the basic primitive is stretched and deformed in the vertical direction, node 3 is subjected to the actions of node 2, node 0, and node 4. The resultant force on node 3 is \(F_3\);
where $F_{SS}$ represents the force of node 0 to node 3; $F_{SS}'$ represents the force of node 2 to node 3; $F_{SS}^X$ represents the force of node 4 to node 3; $F_{SS}^Y$ represents the resultant force in the horizontal direction, and $F_{SS}'$ represents the resultant force in a vertical direction.

![Figure 10 Basic primitives of the discrete model of mulch film](image)

Because of the symmetry of the basic primitive, the resultant force $F_{SS}'$ of particle 2 is equal to $F_{SS}'$.

$$F_{SS}' = F_{SS}'$$  \hspace{1cm} (6)

Then, when the base primitive is stretched $\Delta l'$ in the vertical direction.

$$F_S = F_{SS}' + F_{SS}^Y = 2F_{SS}^Y$$  \hspace{1cm} (7)

where, $F_S$ represents the resultant pulling force of the base primitive.

According to the constitutive law of the discrete element method, Equation (8) can be obtained.

$$F_{SS,\Delta} = K_x(D_1 - D_{1e})$$  \hspace{1cm} (8)

where, $D_1$ represents the distance between nodes 0 and 3; $D_{1e}$ represents the equilibrium distance between nodes 0 and 3; $D_2$ represents the distance between nodes 4 and 3; $D_{2e}$ represents the equilibrium distance between nodes 4 and 3, and $\theta$ represents the angle between the line direction of nodes 4 and 3 and horizontal direction.

According to initial conditions, $D_{1e} = u$, $D_{2e} = \frac{\sqrt{E}}{2}u$, and $\theta = \frac{\pi}{4}$. The following Equations can be obtained when the stretching length is $\Delta l'$:

$$D_1 = D_{1e} + \Delta l'$$  \hspace{1cm} (9)

$$D_2 = \sqrt{(u/2)^2 + (D_1/2)^2}$$  \hspace{1cm} (10)

$$\theta = \arctan\left(\frac{u/2}{D_1/2}\right) = \arctan\left(\frac{u}{D_1}\right)$$  \hspace{1cm} (11)

Then, the resultant force $F_{SS}'$ can be calculated:

$$F_{SS}' = F_{SS,\Delta} = k_x\Delta l' + k_x\left(\sqrt{(u/2)^2 + (D_1/2)^2} - \frac{\sqrt{E}}{2}u\right)\cos(\arctan\left(\frac{u}{D_1}\right))$$  \hspace{1cm} (12)

According to the relationship between the base primitive and virtual mulch film stretching model, the following Equations can be obtained:

$$\Delta l = \frac{L}{u}\Delta l'$$  \hspace{1cm} (13)

$$F_1 = \left(\frac{W}{u} + 1\right)F_{SS}'$$  \hspace{1cm} (14)

where, $F_2$ represents the virtual stretching force.

Combining and simplifying the above Equations yields the following:

$$F_2 = \left(\frac{W}{u} + 1\right)\left(k_x\Delta l' + k_k\left(\sqrt{(u/2)^2 + (D_1/2)^2} - \frac{\sqrt{E}}{2}u\right)\cos(\arctan\left(\frac{u}{D_1}\right))\right)$$  \hspace{1cm} (15)

When $\Delta l'$ is very small, $\theta = \frac{\pi}{4}$, $\sqrt{(u/2)^2 + (D_1/2)^2} = \frac{\sqrt{E}}{2}D_1$. The following conclusion can be obtained from Equation (15):

$$F_2 = \left(\frac{W}{u} + 1\right)\left(k_x\Delta l' + k_k\left(\frac{\sqrt{E}}{2}D_1 - \frac{\sqrt{E}}{2}u\right)\frac{\sqrt{E}}{2}\right) = \left(\frac{W}{u} + 1\right)$$  \hspace{1cm} (16)

Therefore, $F_1 = F_2$ can be converted into the following:

$$WDE\Delta l = \frac{3}{2}k_k\left(\frac{W}{u} + 1\right)\left(\Delta l - \frac{u}{L}\right)$$  \hspace{1cm} (17)

Equation (18) can be obtained by simplifying Equation (16).

$$k_k = \frac{2}{3}\left(\frac{D_1E}{(1+u/W)}\right)$$  \hspace{1cm} (18)

The following conclusion can be obtained from Equation (18): The tensile stiffness coefficient of the virtual model is related to the elastic modulus $E$, initial adjacent node distance $u$, length $W$, and thickness $D$ of the real mulch. Therefore, when setting the axial stiffness of the virtual mulch film, all the above-mentioned parameters should be considered comprehensively.

From the tensile test of mulch film, the elastic modulus of real mulch film $E=6.82$ MPa. The thickness of the mulch film is $D=1e-5$ m. The width of the test mulch is $W=2e-2$ m. The equilibrium distance between adjacent particles is $D_{1e}=1$ mm. By calculating Equation (18), the value of the axial stiffness coefficient $K_x$ is 43.3 N.m.

6 Results of the virtual simulation test

To verify whether virtual mulch film has similar physical and mechanical properties to real mulch film, stretching and tear contrast tests of virtual and real mulch film were conducted.

6.1 Stretching test

(1) Test method

The method of real stretching is shown in Figure 9a. This method was conducted in accordance with the Chinese national standard GB/T13022-1991 "Test method for tensile properties of plastic films", which applies to plastic films with a thickness below 1 mm. The sample is a long strip specimen with a width of 20 mm, an effective length of 60 mm, and a total length of 150 mm. The real tensile test equipment was an Instron universal material test bench (model 2519-104). The test accuracy was 0.0001 N, the measurement range was 500 N, and the test speed
was 50±5 mm/min.

The method of virtual stretching is shown in Figure 9b. At the fixed end, the six degrees of freedom of the spherical particles are completely restricted and therefore cannot be moved. At the stretched end, only one translational freedom of the stretching directions is retained. Other particles do not impose any constraints. Finally, the spherical particles at the stretched end are subjected to the same constant speed as caused by real stretching in the stretching direction.

(2) Tensile results

Figure 11 shows the results of real film stretching, Figure 12 shows the simulation results of virtual film stretching, and Figure 13 shows the relationship between tensile displacement and tensile force.

A comparison between Figure 11 and Figure 12 shows 1) Elongation change: the tensile elongation of real mulch film was 183%, and the tensile elongation of the virtual mulch film was 200%. The elongation changes of both are basically identical. 2) Morphological changes: Before tensile fracture, the longitudinal shrinkage morphology of both are basically identical; after tensile fracture, the real residual film has yielded to deformation and the deformed residual film cannot be recovered. Virtual mulch film did not yield to deformation after fracture, and the fractured residual membrane recovered rapidly. 3) Fracture position: The fracture position of the real mulch film sample was the middle part; the fracture position of the virtual mulch film sample was at approximately the tensile clamping end.

Figure 15 shows that the tensile force-displacement curve of real mulch film indicates the process of elastic deformation-yield-fracture; the virtual mulch film model indicates the process of elastic deformation-fracture. The difference between the force-displacement laws of both during the stretching process is obvious.

Analysis of the reasons: The current particle contact law is an ideal spring model; therefore, the deformation of the virtual mulch is equivalent to a linear deformation. The deformation of the real mulch film is plastic deformation. To describe the plastic deformation behavior, the viscoelastic model should be further studied. The existing particle contact constitutive rules have not set the yield judgment conditions, i.e., when the deformation of the PFacet element reaches the set value, the deformation cannot be recovered. Further work is needed to establish and verify the yield rule.

![Figure 11 Results of physical stretching (length units: m)](image1)

![Figure 12 Results of virtual stretching (length units: m)](image2)
6.2 Tearing test

(1) Tearing method

The real tearing test is shown in Figure 14a. This method adopts the Chinese national standard GB/T16578-2008 “Test method for tear resistance of plastic film and sheet-pants tearing method”. The tearing sample was prepared by cutting a slit of a certain length into the middle of a rectangular mulch film, resulting in the final sample akin to a pair of pants; therefore, this method is called the pants-shaped tearing method. The film tearing force was defined as the force required to tear the crack along the slit at a constant tear speed. The test speed was 200±20 mm/min, and the length of clamping was 30 mm.

The virtual tearing method is shown in Figure 14b. The five degrees of freedom of spherical particles of the upper and lower end are limited, and all particles have only one translational degree of freedom in the tear direction. Other particles do not limit any degree of freedom. Under the virtual stretching, the spherical particles at both the upper and lower end are moved in the upper and lower tearing directions, respectively, and the velocity value is the same as in the real tearing test.

(2) Tearing results

Figure 15 shows the tearing results of real mulch film, Figure 16 shows the tearing results of virtual mulch film, and Figure 17 shows the relationship between tearing force and displacement of both virtual and real mulch films.
Figure 17 shows that during real tearing, the tearing force first gradually increases, then gradually decreases when the tearing force increases to the maximum until tearing is completed. During virtual tearing, the tearing force gradually increases, then suddenly becomes smaller, and then gradually increases again; this process reciprocates until the tear is complete.

Analysis of the reason: the virtual mulch model is a discrete structure, similar to a truss, rather than a continuous surface structure, when a node breaks, the tearing force changes suddenly.

7 Conclusions

(1) A flexible and deformable virtual mulch film model was constructed based on the Minkowski sums principle. The ball-ba particle force-displacement contact constitutive rule and the contact failure rule are established. Deformation behaviors such as stretching, bending, and torsion of the flexible cylinder and PFacet element were defined. The virtual mulch film model was finally established by programming and splicing of PFacet elements.

(2) To ensure that the established virtual mulch model has the same physical and mechanical properties as real mulch film, and to determine the physical parameters of virtual mulch film, a mechanical model of virtual mulch film was established by mathematical analysis during stretching. When the elastic modulus value of the real mulch film is 6.82 MPa, the thickness D is 1e-5 m, the width W is 2e-2 m, and the equilibrium distance between adjacent particles D_{eq} is 1 mm. By solving the mathematical model, the axial tensile stiffness coefficient k was identified as 43.3 N·m.

(3) The real and virtual stretching results are as follows:

① The tensile elongations of real and virtual mulch films were 183% and 200%, respectively. ② Real mulch film has yield deformation and the deformed residual film cannot be recovered. For virtual mulch film, there was no yield deformation after a fracture. ③ The fracture position of real and virtual mulch film samples is at the middle and around the tensile clamping end, respectively. ④ The tensile force-displacement curve of real and virtual mulch films show the process of elastic deformation-yield-fracture and elastic deformation-fracture, respectively.

(4) The real and virtual tear test results were as follows: the tear elongations of virtual and real mulch film were 230.8% and 217.7%, respectively; The morphological characteristics of virtual and real mulch film during the tearing process are basically identical; The tear force-displacement curves of both differ completely.

(5) In the process of stretching and tearing of real and virtual films, the properties of morphological features of both are basically identical; however, the difference in force-displacement is apparent. The viscoelastic constitutive model between balls and yield judgment conditions requires further study.

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