The Enemy of My Enemy is My Friend:
Exploring Inverse Adversaries for Improving Adversarial Training

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Abstract

Although current deep learning techniques have yielded superior performance on various computer vision tasks, yet they are still vulnerable to adversarial examples. Adversarial training and its variants have been shown to be the most effective approaches to defend against adversarial examples. A particular class of these methods regularize the difference between output probabilities for an adversarial and its corresponding natural example. However, it may have a negative impact if a natural example is misclassified. To circumvent this issue, we propose a novel adversarial training scheme that encourages the model to produce similar output probabilities for an adversarial example and its “inverse adversarial” counterpart. Particularly, the counterpart is generated by maximizing the likelihood in the neighborhood of the natural example. Extensive experiments on various vision datasets and architectures demonstrate that our training method achieves state-of-the-art robustness as well as natural accuracy among robust models. Furthermore, using a universal version of inverse adversarial examples, we improve the performance of single-step adversarial training techniques at a low computational cost.

1. Introduction

Deep learning has achieved revolutionary progress in numerous computer vision tasks\textsuperscript{[24, 40, 55]} and has emerged as a promising technique for fundamental research in multiple disciplines\textsuperscript{[31, 35, 52]}. However, a well-established study has demonstrated that Deep Neural Networks (DNNs) are extremely vulnerable to adversarial examples\textsuperscript{[42]}, which are indistinguishable from natural examples in human vision. In other words, a visually undetectable perturbation to the original example can lead to a significant disruption of the inference result of DNNs. The imperceptibility of these tailored examples also makes them easy to bypass manual verification\textsuperscript{[3, 15]}, posing a potential security threat to the safety of deep learning-based applications.

Various defense methods have been proposed to improve adversarial robustness of DNNs\textsuperscript{[21, 46, 48]}. As the primary defense method, adversarial training\textsuperscript{[10, 25, 42]} improves intrinsic network robustness via adaptively augmenting adversarial examples into training examples. State-of-the-art adversarial training methods mainly focus on the distribution alignment between natural and adversarial examples to preserve the consistency of the DNN prediction\textsuperscript{[7, 44, 53]}. However, there still exists an undesirable decrease in the standard accuracy for adversarially trained models due to limited data and restricted model capacity. The misclassification of natural examples can further undermine the distribution alignment during adversarial training.

The natural intuition is that: adversarial examples corre-
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et al. studied them in inverse adversarial examples (IAE) that are created via minimizing the objective function as an inverse procedure of adversary generation. Specifically, inverse adversarial examples are beneficial to DNNs, which can be more possibly to be correctly classified. To support this claim, we study the accuracy of trained classification models on two groups of samples (see Figure 1). We present the accuracy of adversarial examples and their inverse counterparts under different attack strengths. Even a small adversarial perturbation can induce a drastic accuracy decrease for the naturally trained model. For the adversarially trained model, the robust accuracy of examples with higher loss values (Bottom 50%) suffers from a heavier drop than that of examples with lower loss values (Top 50%) under larger attack strengths. This indicates that the adversarial counterparts of low-confidence or even misclassified examples are also misclassified. Therefore, the distribution alignment between two misclassified examples might have an unnecessary or even harmful effect on the adversarial robustness establishment.

In this paper, to mitigate the unnecessary or even harmful matching manner between misclassified examples, we propose a novel adversarial training framework based on an inverse version of adversarial examples, dubbed Inverse Adversarial Training (IAT), which implicitly bridges the distribution gap between adversarial examples and the high-likelihood region of their belonging classes. Adversarial examples of a certain category can thus be pulled closer to the high-likelihood region instead of their original examples. Specifically, we propose an inverse procedure of the standard adversary generation to reach the high-likelihood region. The generated inverse adversaries can also be viewed as the rectification of original examples for reducing prediction errors. Considering the multi-class decision surface and computational cost, we further design a class-specific inverse adversary generation paradigm as opposed to the instance-wise version. Furthermore, we establish a momentum mechanism for the prediction of inverse adversaries to stabilize the training process. A one-off version of our inverse adversarial training is also proposed for improving time efficiency.

Comprehensive experiments demonstrate the superiority of our method in comparison with state-of-the-art adversarial training approaches. We also show that our method can be adapted to larger models with extra generated data for robustness enhancement. Besides, the robustness of single-step adversarial training methods can be further improved at a low cost by incorporating our method.

The main contribution of this paper can be summarized as follows:

- By analyzing the unnecessary, or even harmful, alignment between misclassified examples, we propose a novel adversarial training framework based on the inverse version of adversarial examples, which promotes the aggregation of adversarial examples to the high-likelihood region of their belonging classes.
- Based on our Inverse Adversarial Training (IAT) paradigm, we design a class-specific universal inverse adversary generation method to mitigate the individual bias of different examples with high efficiency. We also propose a one-off strategy to reduce computational costs with a negligible performance loss.
- Extensive experiments demonstrate the effectiveness and generalizability of our method compared to state-of-the-art adversarial training methods. Our method can also be combined with single-step adversarial training methods as a plug-and-play component for boosting robustness at a low cost.

Related works. The lethal vulnerabilities of deep neural networks against adversarial examples have been witnessed in [4, 10, 28, 42]. A myriad of attempts have been made to defend against these tailored examples, including adversarial training [17, 25, 44, 53], adversarial detection [14, 43], and input transformation-based methods [37, 48, 49]. Among them, adversarial training consistently remains to be the most effective method [2] to improve intrinsic network robustness via augmenting the training data with adversarial examples. In addition, most existing works generally incorporate a regularization term to narrow the distribution difference between natural examples and their adversarial counterparts [7, 44, 53], which has been demonstrated to be beneficial for robustness enhancement. This matching manner seems natural but might be misguided by misclassified natural examples, as we showed in Figure 1. Several efforts have been devoted to resolving such an issue by assigning weights on losses in terms of the intensity of adversarial examples [23, 54]. However, they mainly concentrate on mitigating the imbalance of disturbance effect among adversarial examples, while our primary focus is to alleviate the harmful alignment between misclassified examples by incorporating inverse adversarial examples.

Inverse adversarial examples were first formally described in [36], where Salman et al. studied them in vision systems to enhance in-distribution performance against new corruptions. In comparison, we investigate the rectification effect of inverse adversarial examples on the distribution alignment during adversarial training for robustness enhancement. A concurrent work [22] also exploits the inverse version of adversarial examples for adversarial robustness by incorporating different distance metrics. However,

1The formal definition will be given in the following sections.
we built on class-specific universal inverse adversaries for adversarial training with more efficiency and robustness. Furthermore, we show how our method can be combined with single-step adversarial training techniques to improve both the natural performance and robustness.

2. Background

We consider a DNN classifier \( f_{\theta} : \mathcal{X} \rightarrow \mathbb{R}^C \) with parameters \( \theta \), which predicts probabilities of \( C \) classes. Also, we denote the input feature representation of the last fully-connected layer as \( F_{\theta}(x) \) for a given example \( x \in \mathcal{X} \). Adversarial training can be an effective way to enhance the robustness of DNNs against adversarial perturbations, which adaptively involves adversarial examples in training as strong data augmentation. For a specific dataset \((x, y) \sim D\), the standard adversarial training [25] against attacks under \( \ell_{\infty}\)-norm threat model can be formulated as the following min-max optimization problem:

\[
\min_{\theta} \mathbb{E}_{(x,y) \sim D} \left[ \max_{\|\delta\|_{\infty} < \epsilon} \mathcal{L}_{\text{CE}} \left( f_{\theta}(x + \delta), y \right) \right],
\]

where \( \mathcal{L}_{\text{CE}} \) is the cross-entropy loss and \( \delta \) is the adversarial perturbation under the \( \ell_{\infty}\)-norm bound \( \epsilon \). The outer minimization is to optimize empirical adversarial risk over the network parameters \( \theta \). The inner maximization can be viewed as searching for the worst-case adversarial examples \( \hat{x} = x + \delta \), which can be simplified as an iterative Projected Gradient Descent (PGD) algorithm [25] on the negative loss function.

Besides standard adversarial training, TRADES [53] and MART [44] proposed to utilize Kullback–Leibler (KL) divergence for distribution matching between natural examples and their adversarial counterparts. The objective function of TRADES [53] can be defined as follows:

\[
\min_{\theta} \mathbb{E}_{(x,y) \sim D} \left[ \mathcal{L}_{\text{CE}} \left( f_{\theta}(x), y \right) + \omega \cdot \max_{\|\delta\|_{\infty} < \epsilon} \mathcal{L}_{\text{KL}} \left( f_{\theta}(x) \| f_{\theta}(x + \delta) \right) \right],
\]

where \( \mathcal{L}_{\text{KL}} \) denotes KL divergence and \( \omega \) is the balancing parameter for the trade-off of natural accuracy and adversarial robustness. Generally, KL divergence encourages the predictions of benign examples and adversarial examples to share the same distribution. Nevertheless, this distribution alignment can further undermine the adversarial robustness when benign examples are misclassified, resulting in the wrong guidance during adversarial training. A major drawback in adversarial training is that it costs more considerable computing resources than natural training [1, 38, 47], which hinders robust establishment on larger models. In addition, adversarial training can suffer from more severe overfitting than the natural training paradigm [34]. Later in this paper, we will provide some insights related to the above-mentioned challenges regarding adversarial training.

3. Method

In this section, we first formally define the inverse adversarial example and introduce its class-specific (universal) variant. We then propose a new adversarial training scheme, coined as Universal Inverse Adversarial Training (UIAT), via a regularizer that encourages the prediction alignment between adversarial examples and the high-likelihood region of their corresponding classes. Furthermore, the inverse adversary momentum is also proposed for the stabilization of the training process. To boost time efficiency, we design a one-off version of our UIAT by computing inverse adversaries only in one of the training epochs without losing much performance.

3.1. Inverse Adversarial Examples

For the image classification task, the adversary generation can be viewed as a process of crossing the decision boundary for misclassification. On the contrary, generating inverse adversarial examples can be regarded as moving away from the decision boundary to the high-likelihood region of a certain class. Specifically, this process can be obtained by iteratively minimizing the classification loss values of inverse adversarial examples. Formally, inverse adversarial examples are inputs to machine learning models, which are tailored to cause the model to obtain more accurate predictions than corresponding natural examples. Similar to adversarial examples, inverse adversaries are obtained by adding visually tiny perturbations to natural ones. We here focus on \( \ell_{\infty}\)-norm bound \( B(x, \epsilon') \) with radius \( \epsilon' \) around natural examples on inverse adversaries. One can use PGD to generate inverse adversarial perturbations:

\[
x^{t+1} = \Pi_{B(x, \epsilon')}(x^t - \alpha' \cdot \text{sign} (\nabla_{x^t} \mathcal{L}_{\text{Inv}} (x^t, y))),
\]

where \( \alpha' \) is the gradient descent step size, \( x^t \) represents the \( t \)th iteration update, and \( \mathcal{L}_{\text{Inv}} \) denotes the loss function for the inverse adversary generation. Generally, the cross-entropy loss can be a good choice for guiding the inverse adversary generation. Nevertheless, the high-likelihood region of a certain class is far away from any adjacent decision boundaries [18, 45], which means that inverse adversaries are far away from adversarial examples at the feature level. Meanwhile, natural feature embeddings are also desired to lie on the high-likelihood region from the geometric perspective. We thus append a feature-level regularization during the inverse adversary generation for supplementary supervision. Therefore, given a sample \( x \) and its adversarial counterpart \( \hat{x} \), our inverse adversarial loss can be written as follows:

\[
\mathcal{L}_{\text{Inv}} (x, \hat{x}) = \mathcal{L}_{\text{CE}} (f_{\theta} (x), y) + \beta \cdot [\mathcal{L}_1 (f_{\theta} (x), f_{\theta} (\hat{x})) - \mathcal{L}_1 (f_{\theta} (x), f_{\theta} (\hat{x}))],
\]

where \( \beta \) denotes the weighting factor. Similar to insights from adversarial feature space analysis [26], our triplet term is designed to prevent them from being too close to each other.
on latent representations can further prevent the overfitting of inverse adversaries from extremely high predictions for better guidance. The obtained inverse adversarial examples can then be incorporated into the adversarial training for robustness enhancement.

3.2. Class-specific Inverse Adversaries

We have introduced the instance-wise inverse adversarial example in the previous section, which is effective in approximating the high-confidence region in the decision surface. However, the inverse adversary generation suffers from a high computational cost due to iterative gradient computation. In general, the instance-wise inverse adversary generation can take almost the same time as the original adversary generation. To reduce the computational cost of inverse adversary generation, we further design a Class-Specific Universal inverse adversary generation strategy inspired by [27, 39]. The universal strategy allows examples of the same class to share a universal adversarial perturbation. In other words, each class owns a universal inverse adversarial perturbation that can be effective in approaching its high-confidence region (lower the objective loss). In this way, we can find a shared direction to reach high-confidence regions, which can also mitigate the individual noise between different examples. The class-specific universal adversarial perturbation $z_c$ for class $c$ can be defined as:

$$L_{\text{inv}} (\Pi_{\theta}(x^c, c)) (x^c + zc, y_c) < L_{\text{inv}} (x^c, y_c) \text{ for "most" } x^c \sim D^c.$$  (5)

We sample natural examples $x^c$ and corresponding labels $y_c$ from dataset $D^c$ of category $c$. The class-specific universal inverse perturbation $z_c$ is effective in most of the examples from the same class $c$ for reducing the loss. Note that we keep updating class-specific inverse perturbations throughout the whole training stage. For a certain batch of data, we can obtain the updated universal inverse perturbation by solving the following optimization problem:

$$\min_{\|z_c\|_\infty < \epsilon} \frac{1}{N_c} \sum_{i=1}^{N_c} L_{\text{inv}} (x^c_i + z_c, y^c_i),$$  (6)

where $N_c$ is the number of training samples belonging to class $c$ of a batch. Specifically, we can further use PGD to solve the above optimization problem to obtain class-specific inverse adversarial perturbation $z_c$. For time efficiency, we only conduct a single-step PGD to update the universal inverse perturbation for a certain category.

3.3. Universal Inverse Adversarial Training

We here show how the universal inverse adversaries can be used to devise an effective adversarial training algorithm. The universal inverse adversarial example $\hat{x}$ can be obtained by adding the class-specific inverse perturbation to the original example $x$. Recall that we obtain adversarial examples $\hat{x}$ by maximizing the cross-entropy loss during adversarial training. The loss function of Universal Inverse Adversarial Training (UIAT) can be formulated as:

$$L_{\text{UIAT}} = L_{\text{CE}} (f_\theta (\hat{x}), y) + \lambda \cdot L_{\text{KL}} (p^{(t)} \| f_\theta (\hat{x})),$$  (7)

where $t$ denotes the current training epoch number. To mitigate the oscillations of noisy predictions throughout the training process, we design a momentum mechanism on the predicted probability of inverse adversaries via incorporating predictions from previous epochs. The momentum mechanism to obtain aggregate predicted probability $p^{(t)}$ can thus be described as:

$$p^{(t)} = \begin{cases} f_\theta (\hat{x}), & \text{if } t < T \\ \gamma \cdot p^{(t-1)} + (1 - \gamma) \cdot f_\theta (\hat{x}), & \text{if } t \geq T \end{cases}$$  (8)

where $\gamma$ is the momentum factor. Note that we start to enable the inverse adversary momentum at epoch $T$ to stabilize the training process. The main reason is that the learned representation is unstable during the early training period. Our UIAT method can thus bridge the gap between adversarial examples and the high-confidence region of their belonging classes for robustness enhancement. The pseudocode of our UIAT is provided in Algorithm 1. We can easily obtain standard IAT by replacing universal inverse adversaries with instance-wise ones. (Details can be found in the supplementary material)

To further reduce the computational overhead, we provide a one-off strategy, which only conducts the inverse adversary generation in a certain epoch $T'$ instead of generating inverse adversaries throughout the whole training process. Before epoch $T'$, we replace $p^{(t)}$ in Equation (7) with $f_\theta (\hat{x})$ for adversarial training, which is similar to [44]. Afterward, we keep replacing $p^{(t)}$ with the temporary probability $p^{(T')}$ in following epochs $t > T'$. More details of our one-off strategy are given in the supplementary material.

4. Experiments

In this section, we conduct extensive experiments to demonstrate the effectiveness and generalizability of our method. We first introduce our experimental settings, including datasets and implementation details. Next, we compare our method with state-of-the-art adversarial training methods in various settings, demonstrating the superiority of our inverse adversarial training. Moreover, we show that our method can be combined with single-step adversarial training methods, which meaningfully increases their performance at only a small additional cost.

4.1. Experimental Setups

Datasets. We conduct experiments on three standard datasets: CIFAR-10, CIFAR-100 [20], and SVHN [30]. Details of datasets are provided in the supplementary material.
We compare our proposed UIAT \( \mathcal{C}/2 \) whilst im-
portantly, the return of our CIFAR-10 classifier \( \theta \) for \( A \) followed by \( L \) for each \( l \) on SVHN...

\[
\begin{align*}
\text{Algorithm 1 Universal Inverse Adversarial Training (UIAT)} \\
\text{Input:} & \text{ DNN classifier } f_\theta; \text{ dataset } \mathcal{D} = \{(x_j, y_j)\} \text{ with } C \text{ classes; batch size } m; \text{ learning rate } \tau; \text{ radius for adversaries } \epsilon \text{ and inverse adversaries } \epsilon'; \text{ step size } \alpha' \text{ for inverse adversary generation; weighting factors } \lambda; \text{ momentum factor } \gamma.
\end{align*}
\]

1. Randomly initialize the network parameter \( \theta \). Initialize \( z_c \sim 0.001 \cdot \mathcal{N}(0, 1) \), for \( 1 \leq c \leq C \)

```plaintext
2. while not at end of training do
3.     for each mini-batch \( \{(x_j, y_j)\}_{j=1}^m \) do
4.         Initialize \( \ell_{inv} \leftarrow 0 \), for \( 1 \leq c \leq C \)
5.         for \( j = 1, 2, \ldots, m \) do
6.             \( \hat{x}_j \leftarrow \text{PGDAttack}(x_j, y_j, f_\theta, \mathcal{L}_{CE}) \) \hspace{1cm} \( \triangleright \) Find PGD adversarial example
7.             \( x_j \leftarrow \hat{x}_j + \zeta_{y_j} \)
8.             \( \ell_{inv}^{ij} \leftarrow \ell_{inv}^{ij} + \mathcal{L}_{inv}(x_j, y_j) \)
9.         end for
10.     for \( c = 1, \ldots, C \) do
11.         \( z_c \leftarrow \Pi_{\|\zeta_c\|_{\infty} \leq \epsilon'} (z_c - \alpha' \cdot \text{sign} (\nabla_{\zeta_c} \ell_{inv})) \) \hspace{1cm} \( \triangleright \) Update class-specific inverse adversaries
12.     end for
13.     Obtain \( p_j^{(t)} \), for \( 1 \leq j \leq m \), by Eq. (8) according to current epoch number \( t \) \hspace{1cm} \( \triangleright \) Inverse adversary momentum
14.     \( \theta \leftarrow \theta - \tau \cdot \nabla_\theta \left\{ \sum_j \mathcal{L}_{CE} (f_\theta (\hat{x}_j), y_j) + \lambda \cdot \mathcal{KL} \left( p_j^{(t)} \| f_\theta (\hat{x}_j) \right) \right\} \)
15. end for
16. end while
17. return Inverse adversarially trained model \( f_\theta \).
```

Table 1. Comparison of our methods (UIAT) using ResNet-18 trained on CIFAR-10, CIFAR-100, and SVHN with other adversarial training methods. The \( \ell_{\infty} \)-norm adversarial perturbations are restricted in \( \epsilon = 8/255 \). We report both natural accuracy (%) and robust accuracy (%). The best result in each column is in **bold**.

| Method         | CIFAR-10 Natural | PGD | CW | AA | CIFAR-10 Natural | PGD | CW | AA | SVHN Natural | PGD | CW | AA |
|----------------|------------------|-----|----|----|------------------|-----|----|----|---------------|-----|----|----|
| SAT [25]       | 83.80            | 51.40 | 50.17 | 47.68 | 57.39           | 28.36 | 26.29 | 23.18 | 92.46        | 50.55 | 50.40 | 46.07 |
| TRADES [53]    | 82.45            | 52.21 | 50.29 | 48.88 | 54.36           | 27.49 | 24.19 | 23.14 | 90.63        | 58.10 | 55.13 | **52.62** |
| MART [44]      | 82.20            | 53.94 | 50.43 | 48.04 | 54.78           | 27.89 | 26.15 | 24.58 | 89.88        | **58.48** | 52.48 | 48.44 |
| HAT [32]       | 84.86            | 52.04 | 50.33 | 48.85 | 58.73           | 27.92 | 24.60 | 23.34 | 92.06        | 57.35 | 54.77 | 52.06 |
| **UIAT**       | **85.01**        | **54.63** | **51.10** | **49.11** | 59.55           | **30.81** | **28.05** | **25.73** | **93.28** | **58.18** | **55.49** | 52.45 |
| **UIAT** (One-off) | **84.98**        | **54.79** | **51.29** | **49.05** | **60.01** | **30.49** | **27.56** | **25.45** | **93.14** | **58.30** | **55.45** | **52.49** |

Implementation details. Following the setting on RobustBench [5], we adopt ResNet-18 [12], Pre-activation ResNet-18 (PRN-18) [13], and Wide-ResNet-28-10 (WRN-28-10) [51] as the target networks. For training without extra data, we set the batch size to 128 and the total number of epochs to 100 for CIFAR10/100 [20], and 30 for SVHN [30]. We adopt Stochastic Gradient Descent (SGD) optimizer with Nesterov momentum factor of 0.9 [29], cyclic learning rate schedule [41] with a maximum learning rate of 0.1, and a weight decay factor of \( 5 \times 10^{-4} \). We adopt the PGD method [25] on the cross-entropy loss with 10 iteration steps for adversary generation during the training stage. The maximum \( \ell_{\infty} \)-norm of adversarial perturbation is \( \epsilon = 8/255 \), while the step size \( \alpha \) is set as \( 2/255 \) for CIFAR-10/100 and \( 1/255 \) for SVHN following common practices. We set the inverse adversary radius as \( \epsilon' = 4/255 \). We adopt \( \lambda = 3.5 \) for CIFAR10/100 and \( \lambda = 3.0 \) for SVHN. The regularization hyper-parameters \( \beta \) and \( \gamma \) are set to 1.0 and 0.9 in Equation (4) and Equation (8). More experimental details are included in the supplementary material.

4.2. Results

Performance of UIAT. We compare our proposed UIAT method with state-of-the-art adversarial training schemes, as shown in Table 1. We report the accuracies on natural examples as well as adversarial examples obtained using three strong adversarial attacks: PGD [25] with 20 steps (step size \( \alpha = 2/255 \)), CW [4], and Auto Attack (AA) [6] for a rigorous robustness evaluation. Note that AA is a reliable and powerful ensemble attack that contains three types of white-box attack as well as a strong black-box one. Not only does our method enhance robust accuracy on these three datasets, but it also achieves a better clean accuracy, hence a smaller robustness gap. For CIFAR-100, our method significantly boosts the AA robust accuracy by nearly 2% whilst improving the natural accuracy. Our superior performance on CIFAR-100 also represents the generalizability of UIAT on a more complicated dataset with more classes. In addition, we demonstrate that our UIAT with one-off inverse adversary generation can also obtain a similar performance as the standard version of UIAT. In other words, the freezing of...

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well-learned class-specific perturbations can still facilitate the distribution alignment for robustness improvement.

**Computational cost comparison.** In addition to outperforming state-of-the-art adversarial training methods on natural accuracy and robustness, our UIA T method also has a faster training speed. We compare the average training time (min/epoch) of our methods against other adversarial training methods, as presented in Table 2. For a fair comparison, we conduct all the training experiments on a single NVIDIA Tesla A100 GPU with the same batch size $m = 128$ on the CIFAR-10 dataset using three different network architectures. It can be seen that our one-off UIA T method obtains better robust accuracy while maintaining a comparable natural accuracy as HA T, which means that we only use one gradient ascent step during training. Nevertheless, there still exists a considerable robustness gap between single-step adversarial training methods and multi-step ones.

**Adversarial training with additional data.** Following the experimental settings of [11, 32, 33], we also conduct several experiments to measure the generalizability of our method with extra data. Particularly, we present the robustness results using different model architectures trained on CIFAR-10 and CIFAR-100 with 1M synthetic images produced by the Denoising Diffusion Probabilistic Model (DDPM) [16] as the additional data. We compare our UIA T method and its one-off variant version with state-of-the-art approaches in Table 4. Note that we do not apply the CutMix operation [50] following [32]. As observed, our method obtains better robust accuracy while maintaining the same or even better natural accuracy.

### 4.3. Single-Step Adversarial Training

The computational cost for multi-step adversarial training is expensive, which has become prohibitive to adversarially train on larger models/datasets. In comparison, single-step methods try to approximate the most harmful adversarial examples with a single gradient ascent step [1, 8, 19, 47] during training. Nevertheless, there still exists a considerable robustness gap between single-step adversarial training methods and multi-step ones.

In this section, we combine the one-off version of our UIA T method with state-of-the-art single-step adversarial training approaches to demonstrate the generalizability and the low time cost of our methods. For time efficiency, we set $\beta = 0$ for Equation (4), which means that we only use cross-entropy loss for inverse adversary generation. More details about how to combine our UIA T method with single-step adversarial training can be found in the supplementary.

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**Table 2.** Time cost comparison of adversarial training methods on CIFAR-10 dataset with different network architectures. We report the average training time (min/epoch) of these methods.

| Method          | ResNet-18 | WRN-28 | WRN-34 |
|-----------------|-----------|--------|--------|
| Natural Training| 0.35      | 0.93   | 1.22   |
| TRADES [53]     | 2.57      | 14.13  | 16.60  |
| HAT [32]        | 4.02      | 16.88  | 18.95  |
| IAT             | 2.83      | 15.37  | 17.82  |
| UIAT            | 2.20      | 11.90  | 14.77  |
| UIAT (One-off)  | 1.96      | 10.74  | 13.36  |

**Table 3.** Adversarial robustness results under different attack configurations using ResNet-18 on CIFAR-10. We present natural accuracy and (Auto-Attack) robust accuracy of different attack radii.

| $\epsilon$ | Method      | Natural | Robust  |
|------------|-------------|---------|---------|
| 10/255     | TRADES [53] | 82.28   | 38.55   |
|            | HAT [32]    | 81.94   | 40.12   |
|            | UIAT        | 82.79   | 40.61   |
|            | UIAT (One-off)| 82.76  | 41.16   |
| 12/255     | TRADES [53] | 79.37   | 31.84   |
|            | HAT [32]    | 79.43   | 33.28   |
|            | UIAT        | 79.50   | 34.32   |
|            | UIAT (One-off)| 79.30  | 34.61   |
| 16/255     | TRADES [53] | 74.89   | 18.70   |
|            | HAT [32]    | 74.45   | 19.42   |
|            | UIAT        | 74.29   | 21.82   |
|            | UIAT (One-off)| 74.86  | 21.96   |

**Table 4.** Comparison of adversarial training methods using different networks on CIFAR-10/CIFAR-100 with extra training data. We report natural accuracy and (Auto-Attack) robust accuracy.

| Dataset    | Architecture | Method          | Natural | Robust  |
|------------|--------------|-----------------|---------|---------|
| CIFAR-10   | PRN-18       | HAT [32]        | 86.86   | 57.09   |
|            | UIAT         | 87.34           | 58.46   |
|            | UIAT (One-off)| 87.10           | 58.15   |
| CIFAR-100  | PRN-18       | HAT [32]        | 86.86   | 57.09   |
|            | UIAT         | 87.34           | 58.46   |
|            | UIAT (One-off)| 87.10           | 58.15   |

12/255; 16/255. As shown in Table 3, we observe that our UIAT method can achieve better robustness results while preserving a comparable natural accuracy as HAT [32] when facing stronger adversarial attacks.

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Table 5. Robustness results of single-step adversarial training methods combined with our one-off UIAT approach on CIFAR-10. We conduct single-step adversarial training with various adversarial radii for comprehensive evaluation. We present the natural accuracy, (Auto-Attack) robust accuracy, and the average time for training an epoch.

| Method          | $\epsilon = 6/255$ | $\epsilon = 8/255$ | $\epsilon = 10/255$ | Time(s) |
|-----------------|-------------------|-------------------|-------------------|---------|
|                 | Natural | Robust | Natural | Robust | Natural | Robust | Natural | Robust | Time(s) |
| N-FGSM [8]      | 84.66   | 56.36  | 80.29  | 48.24  | 75.59  | 41.54  | 48.4    |        |
| N-FGSM + UIAT   | 85.53   | 58.21  | 81.85  | 49.84  | 77.85  | 42.77  | 57.3    |        |
| RS-FGSM [47]    | 86.72   | 55.28  | 84.07  | 46.15  | 86.32  | 0.00   | 32.4    |        |
| RS-FGSM + UIAT  | 87.60   | 55.85  | 85.18  | 46.31  | 88.29  | 0.00   | 40.7    |        |
| GradAlign [1]   | 83.85   | 55.25  | 80.17  | 46.57  | 76.46  | 39.85  | 96.0    |        |
| GradAlign + UIAT| 85.52   | 55.46  | 82.31  | 46.74  | 79.11  | 39.56  | 107.8   |        |

Table 6. Ablation study using ResNet-18 of three component modules of UIAT for adversarially robust accuracy (%) on CIFAR-10.

| Method | UAG | FR | IAM | Natural | PGD-20 | AA |
|--------|-----|----|-----|---------|-------|----|
| 1      |     |    |     | 83.97   | 53.98 | 48.33 |
| 2      | ✓   |    |     | 85.19   | 53.56 | 47.63 |
| 3      | ✓   | ✓  |     | 85.11   | 54.13 | 48.47 |
| 4      | ✓   | ✓  | ✓   | 84.85   | 54.29 | 48.83 |
| 5      | ✓   | ✓  | ✓   | 85.01   | 54.63 | 49.11 |

UAG: Universal Adversary Generation. FR: Feature-level Regularization. IAM: Inverse Adversary Momentum.

As shown in Table 5, we can observe that UIAT can serve as a plug-and-play component for boosting both natural and robust accuracy. Moreover, we show that our method can effectively adapt to various adversarial training radii for better performance. The additional computational cost for the UIAT method is also acceptable. For instance, in the case of N-FGSM [8], our method can further improve nearly 1.5% for both natural accuracy and adversarially robust accuracy ($\epsilon = 8/255$) with only about an additional 9 seconds time cost for each training epoch.

5. Analysis

5.1. Ablation Study

In this section, we thoroughly investigate the contributions of three components in our UIAT method: 1) Universal Adversary Generation (UAG) in Equation (6), 2) Feature-level Regularization (FR) in Equation (4), and 3) Inverse Adversary Momentum (IAM) in Equation (8). We report both natural accuracy and robust accuracy on CIFAR-10 using ResNet-18 during the ablation study in Table 6.

Our baseline method (The first row in Table 6) is the instance-wise Inverse Adversarial Training (IAT), which has already achieved a competitive robustness performance compared to other methods. It can be seen that the universal inverse adversary generation can effectively improve the performance on natural accuracy, while the robust accuracy slightly drops. Both the feature-level regularization and the inverse adversarial momentum contribute to enhancing the adversarially robust accuracy. We can obtain our UIAT method by integrating these three components, which can effectively improve natural accuracy and robustness.

5.2. Robust Overfitting

Recent research has demonstrated that adversarial training methods primarily suffer from the robust overfitting issue [34], resulting in the robustness plunge. The robust overfitting induces an irreversible robustness drop (on the test set) after adversarial training for several epochs, especially after the learning rate decay operation. We illustrate the learning curves of standard adversarial training and our one-off version of UIAT in Figure 2.

For better visualization, we increase the number of training epochs to 200. We can easily observe that the PGD-based Adversarial Training (PGD-AT) [25] severely suffers from the robust overfitting issue. In comparison, our one-off UIAT method can largely mitigate the robust overfitting issue, which means our method does not suffer from a sharp robustness reduction during adversarial training. It can potentially be explained by the observation made in [9], which demonstrates that the robust overfitting comes from the large-loss data during adversarial training. However, our UIAT method implicitly regularizes the large-loss data, a.k.a., misclassified examples to obtain the high-likelihood region of their true classes, which can thus mitigate the robust overfitting problem. Furthermore, our inverse adver-
In this section, we mainly discuss the underlying reason why our method is effective. In other words, we would like to explore what we have gained from inverse adversarial training. Similar to the setting in Figure 1, we also provide the average accuracy under different attack strengths of our UIAT method compared to TRADES [53], as shown in Figure 4. It can be seen that our method can bridge the robust accuracy gap more effectively compared to TRADES. Precisely, our UIAT can effectively enhance the robust accuracy of the bottom 50% group. In addition, we observe that the inverse adversarial examples of UIAT are prone to be classified correctly, which means that our robust model is easily affected by inverse adversaries. On the contrary, our robust model is less susceptible to adversarial examples compared to TRADES.

Furthermore, we present the comparison of Auto-Attack (AA) robust accuracy under different attack strengths between our UIAT (One-off) method and TRADES [53], as shown in Figure 5. It can be easily observed that our method outperforms TRADES at weak attack strengths ($\epsilon \leq 8/255$). However, TRADES obtains better robustness than our method when confronted with strong adversarial perturbations ($\epsilon > 8/255$). In other words, our method sacrifices the adversarial robustness against larger visual perturbations to enhance the robustness against smaller ones. This is also in line with the definition and intuition that adversarial perturbations are visually undetectable. Recall that we can also obtain better robustness against larger perturbations when training with larger $\epsilon$ as discussed in Section 4.2.

6. Conclusion

In this paper, we explore the unnecessary or even harmful alignment between misclassified examples and propose a new adversarial training paradigm by incorporating the inverse adversarial examples. Furthermore, we design a class-specific universal inverse adversary generation strategy to mitigate the individual bias of different examples and accelerate our method. Extensive experiments demonstrate that our method can efficiently obtain better robustness results without compromising much natural accuracy in diverse settings on larger datasets. Moreover, we can obtain a trade-off between natural accuracy and adversarial robustness to adapt to various scenarios. Our method can also be combined with state-of-the-art single-step adversarial training methods for robustness enhancement at a low cost. Finally, we analyze the reason why our method is effective and verify that our method can potentially bridge the accuracy gap between high-accuracy examples and low-accuracy examples, thus benefiting the robustness.

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