Energy-dependence of skin-mode fraction in $E_1$ excitations of neutron-rich nuclei

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Abstract. We have extensively investigated characters of the low-energy $E_1$ strengths in $N > Z$ nuclei, by analyzing the transition densities obtained by the HF+RPA calculations with several effective interactions. Crossover behavior has been confirmed, from the skin mode at low energy to the $p$-$n$ mode at higher energy. Decomposing the $E_1$ strengths into the skin-mode, $p$-$n$-mode and interference fractions, we show that the ratio of the skin-mode strength to the full strength may be regarded as a generic function of the excitation energy, insensitive to nuclides and effective interactions, particularly beyond Ni.

1 Introduction

By recent experiments, sizable $E_1$ strengths have been observed at low excitation energy in a number of $N > Z$ nuclei, and are called pygmy dipole resonance (PDR) [1]. Low-energy $E_1$ strengths have been predicted in many $N > Z$ nuclei by a systematic calculation as well [2]. However, their character has not yet been established. Although oscillation of the neutron skin against the core (skin mode) has been argued in connection to the PDR, there remain other possibilities, e.g. fragmentation of the proton-neutron oscillation ($p$-$n$ mode) whose dominant part forms the giant dipole resonance (GDR). As low-energy $E_1$ strengths may greatly influence $(n, \gamma)$ reaction rates under astrophysical environment, it is significant to comprehend their character including their energy- and nucleus-dependence. Moreover, the skin-mode strengths could be correlated to the slope parameter of the nuclear symmetry energy $L$, which attracts interest in relevance to structure of neutron stars.

To investigate characters of the low-energy $E_1$ excitations, we have analyzed transition densities obtained from the HF+RPA calculations in the doubly-magic nuclei [3]. By decomposing the transition matrix elements into the skin-mode and $p$-$n$-mode fractions via the transition densities, energy-dependence of the skin-mode fraction has been argued. Here we extensively study energy-dependence of the skin-mode fraction.

2 Decomposition of $E_1$ strengths

We have proposed a decomposition method of the low-energy $E_1$ transition matrix elements into the $p$-$n$ mode and the skin mode via the transition densities, so that their mixing could be handled in a straightforward manner. With the proton and neutron transition densities of the excitation to the $1^-$ state $|\alpha\rangle$,

$$\delta \rho^{(\alpha)}_\tau (r; \alpha) = \langle \alpha | \sum_{\tau z} \delta (r-r_z) \tau (1)(\hat{r}_z) |0\rangle$$

(1)
the $E1$ transition density is given by

$$
\delta \rho^{(E1)}(r; \alpha) = \frac{N}{A} \delta \rho_p^{(E1)}(r; \alpha) - \frac{Z}{A} \delta \rho_n^{(E1)}(r; \alpha).
$$

(2)

Depending on the position, the $E1$ transition density is classified into $\delta \rho_p^{(E1)}$ and $\delta \rho_n^{(E1)}$; if $\delta \rho_p^{(E1)} / \delta \rho_n^{(E1)} > -\lambda_s$ with $0 < \lambda_s \ll 1$, we take

$$
\delta \rho_p^{(E1)}(r; \alpha) = 0, \quad \delta \rho_n^{(E1)}(r; \alpha) = \delta \rho^{(E1)}(r; \alpha),
$$

(3)

and otherwise,

$$
\frac{\delta \rho_p^{(E1)}(r; \alpha)}{\delta \rho^{(E1)}(r; \alpha)} = \frac{\delta \rho_n^{(E1)}(r; \alpha)}{\delta \rho^{(E1)}(r; \alpha)} = 0.
$$

(4)

We adopt $\lambda_s = 0.05$ below. The $pn$-mode and skin-mode matrix elements can be obtained by integrating the transition densities. The $E1$ strength is then decomposed into the $pn$-mode, skin-mode and interference contributions for individual $\alpha$. The corresponding strength function is denoted by $S^{(E1)}_{\text{mode}}(\alpha)$ (‘mode’ = ‘$pn$’, ‘skin’ or ‘intf’). The ratio of $S^{(E1)}_{\text{mode}}$ to the full strength $S^{(E1)} = \sum_{\text{mode}} S^{(E1)}_{\text{mode}}$ at the excitation energy $\omega$ is denoted by $R^{(E1)}_{\text{mode}}(\omega)$.

### 3 Energy-dependence of skin-mode fraction

Figure 1 displays $S^{(E1)}_{\text{mode}}(\omega)$ and $R^{(E1)}_{\text{mode}}(\omega)$ in $^{86}$Ni, obtained by the HF+RPA calculation with the D1S interaction [4]. Crossover behavior of the $E1$ excitations has been found, from the skin mode at low energy to the $pn$ mode at higher energy. By calculations in a number of spherical $N > Z$ nuclei with several effective interactions, the ratio of the skin-mode strength to the full strength $R^{(E1)}_{\text{skin}}$ turns out to have generic energy-dependence, insensitive to nuclides and effective interactions in the energy region of the crossover [3]. In order to view this feature more clearly, we assume a model for $R^{(E1)}_{\text{skin}}(\omega)$,

$$
R^{(E1)}_{\text{skin}}(\omega) = \left[ 1 + \exp \left( (\omega - \omega_c)/\Delta \omega \right) \right]^{-1},
$$

(5)

and adjust the parameters $\omega_c$ and $\Delta \omega$ in individual nuclides for individual interactions so as to minimize deviation of $R^{(E1)}_{\text{skin}}$ from $S^{(E1)}_{\text{skin}}$. Degree of fitting is illustrated in the lower panel of Fig. 1. The fitted values of $\omega_c$ and $\Delta \omega$ are depicted in Fig. 2, for $^{22,24}$O, $^{52,60,70}$Ca, $^{68,84,86}$Ni, $^{132}$Sn and $^{208}$Pb with the interactions SkI2 [5], D1S [4], D1M [6], M3Y-P6 and M3Y-P7 [7]. Then $\omega_c$ and $\Delta \omega$ represent how $R^{(E1)}_{\text{skin}}(\omega)$ varies according to nuclides and effective interactions.

It is confirmed, as pointed out in Ref. [3], that $R^{(E1)}_{\text{skin}}(\omega)$ is insensitive to nuclides and effective interactions. In particular, the extracted values of $\omega_c$ is quite stable from $^{68}$Ni to $^{208}$Pb, surprisingly insensitive to the effective interactions, although there is certain fluctuation in O and Ca. Fluctuation of the extracted values of $\Delta \omega$ is not significantly large. This generic nature of the skin-mode ratio may be helpful in extracting skin-mode strengths from measurements.

### 4 Summary

We have extensively investigated characters of the low-energy $E1$ strengths in $N > Z$ nuclei by the HF+RPA calculations. Confirming the crossover behavior from the skin mode at low energy to the $pn$ mode at higher energy, we apply a method decomposing the $E1$ strengths into the skin-mode, $pn$-mode and interference fractions, via the transition densities. In Ref. [3] the ratio of the skin-mode strength to the full strength was suggested to be a generic function of the excitation energy, insensitive to nuclides and effective interactions. By fitting parameters of a model function for the ratio, this insensitivity is further clarified, particularly beyond Ni.

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