NUCLEAR CHARM AND BOTTOM PRODUCTION: A COMPARISON AMONG HIGH ENERGY APPROACHES

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ABSTRACT

We calculate the nucleon and nuclear photoproduction cross sections for heavy quarks within the \( k_\perp \)-factorization formalism, considering the current high energy approaches which include nuclear and saturation effects. Our results demonstrate that a future experimental analysis of this process would allow to constraint the QCD dynamics at high energies.

1 Introduction

The electron-proton (\(ep\)) collider at HERA has opened up a new kinematic regime in the study of the deep structure of the proton and, in general, of hadronic interactions. This regime is characterized by small values of the Bjorken variable \(x = Q^2/s\), where \(Q^2\) is the momentum transfer and \(\sqrt{s}\) is the center-of-mass energy. The experimental results from HERA have shown a striking rise of the proton structure function \(F_2(x, Q^2)\) for values \(x < 10^{-2}\), which implies that the cross section increases faster than logarithmically on energy. This high energy behavior in the hard-scattering regime is expected if the underlying dynamics is driven by self-interacting massless vector bosons, the gluons. Thus, the steep rise of \(F_2\) certainly confirms one of the basic predictions of perturbative QCD. As the predictions of the collinear and the \(k_\perp\)-factorization approaches, relying on different assumptions, agree with the measurements of the inclusive quantities, one current open question is: what is the correct QCD dynamics at high energies?

In the collinear factorization approach [1] all partons involved are assumed to be on mass shell, carrying only longitudinal momenta, and their transverse momenta are neglected in the QCD matrix elements. Moreover, the cross sections for the QCD subprocess are usually calculated in the leading order (LO), as well as in the next-to-leading order (NLO). In particular, the cross sections involving incoming hadrons are given, at all orders, by the convolution of intrinsically non-perturbative (but universal) quantities - the parton densities - with perturbatively calculable hard matrix elements, which are process dependent. The conventional gluon distribution \(g(x, \mu^2)\), which drives the behavior of the observables at high energies, corresponds to the density of gluons in the proton having a longitudinal momentum fraction \(x\) at the factorization scale \(\mu\). This distribution satisfies the DGLAP evolution in \(\mu^2\) and does not contain
information about the transverse momenta $k_\perp$ of the gluon. On the other hand, in the large energy (small-$x$) limit, we have that the characteristic scale $\mu$ of the hard subprocess of parton scattering is much less than $\sqrt{s}$, but greater than the $\Lambda_{\text{QCD}}$ parameter. In this limit, the effects of the finite transverse momenta of the incoming partons become important, and the factorization must be generalized, implying that the cross sections are now $k_\perp$-factorized into an off-shell partonic cross section and a $k_\perp$-unintegrated parton density function $F(x, k_\perp)$, characterizing the $k_\perp$-factorization approach [2, 3, 4]. The function $F$ is obtained as a solution of the evolution equation associated to the dynamics that governs the QCD at high energies.

Recently, several authors have considered the $k_\perp$-factorization approach in order to analyze some non-inclusive observables and they have obtained a better description of these quantities than the collinear approach (For a recent review see Ref. [5]). However, the current situation is still not satisfactory, due to the large uncertainty associated to the lack of a complete knowledge of the unintegrated gluon distribution. A search for this distribution in the nucleon has been subject of active both theoretical and phenomenological research in recent years. One of the most promising process to constraint the quantity is the heavy quark production in $\gamma p$ interactions [6, 7, 8]. At high energies, the production of open-flavored $Q\bar{Q}$ pairs is described in terms of photon-gluon fusion mechanism, which is expressed in terms of the unintegrated gluon distribution and the parton-level matrix elements. As the behavior of the unintegrated gluon distribution is determined by the underlying dynamics, in Ref. [7] the deviations between the results obtained using a distribution derived from the saturation model and the DGLAP evolution equations were analyzed in detail, as well as compared with the predictions of the collinear approach. Those predictions reasonably describe the current HERA data, with sizable deviations appearing basically at higher energies. These results motivate us to analyze the heavy quark production in the context of photonuclear interactions, where the deviations among the approaches should be amplified due to the presence of the nuclear medium. Here, we estimate the cross section for the nuclear photoproduction of heavy quarks, considering the $k_\perp$-factorization approach and distinct nuclear unintegrated gluon distributions. In particular, we consider the unintegrated gluon distribution obtained recently in Ref. [9], where the saturation model was extended to the nuclear case using the Glauber-Gribov formalism. Moreover, we also consider the derivative of the EKS nuclear gluon distribution [10], which takes into account the nuclear medium effects (shadowing, antishadowing, EMC and Fermi motion). Furthermore, we compare our predictions with those obtained from the collinear factorization approach. In this case, we consider the EKS nuclear gluon distribution as input in our calculations. We also investigate the possibility of the nuclear gluon distribution to be modified by the high parton density effects, as estimated in Ref. [11]. This procedure allow us to estimate the theoretical uncertainty present in the predictions of the cross sections at high energies.

This paper is organized as follows. In the next section we present a brief review of the $k_\perp$-factorization approach for the heavy quark photoproduction and estimate the cross section for this process in the nucleon and nuclear cases. In particular, we present the proton unintegrated gluon distribution obtained from the saturation model and the derivative of the collinear gluon distribution. The results for the total cross sections are compared with the HERA experimental measurements. Similarly, we derive the nuclear unintegrated gluon distribution from the extension of the saturation model to the nuclear case and the corresponding quantity using
the EKS nuclear gluon distribution. Moreover, we present our predictions for the heavy quark nuclear photoproduction cross section in the $k_\perp$-factorization approach and compare them with those ones from the collinear factorization approach. Finally, in Section 3 we summarize the main conclusions.

2 Nuclear heavy quark photoproduction in the $k_\perp$-factorization approach

Let us start introducing the theoretical prediction for the heavy quark photoproduction in the $k_\perp$-factorization approach for the nucleon (proton) case. The relevant diagrams are considered with the virtualities and polarizations of the initial partons, taking into account the transverse momenta of the incident partons. The processes are described through the convolution of off-shell matrix elements with the unintegrated parton distribution, $F(x, k_\perp)$ (for a recent review, see [5]). The latter can recover the usual parton distributions in the double logarithmic limit by its integration over the transverse momentum of the $k_\perp$ exchanged gluon. The gluon longitudinal momentum fraction is related to the c.m.s. energy, $W_{\gamma p}$, in the photoproduction case as $x = \frac{4m_Q^2}{W_{\gamma p}^2}$. A sizeable piece of the NLO and some of the NNLO corrections to the LO contributions on the collinear approach, related to the contribution of non-zero transverse momenta of the incident partons, are already included in the LO contribution within the $k_\perp$-factorization approach. Moreover, the coefficient functions and the splitting functions giving the collinear parton distributions are supplemented by all-order $\alpha_s \ln(1/x)$ resummation at high energies [12]. Consequently, in principle, we expect that in the asymptotic regime of large energies the use of the $k_\perp$-factorization implies an enhancement of the cross sections in comparison with the predictions obtained in the collinear factorization [2]. This is associated to the opening of the $k_\perp$ phase space (away from the collinear region).

The cross section for the heavy-quark photoproduction process is expressed as the convolution of the unintegrated gluon function with the off-shell matrix elements, where the LO matrix elements are well known in the literature [5, 6, 7]. The expression for the photoproduction total cross section considering the direct component of the photon can be written as [7],

$$\sigma_{\text{tot}}^{\text{phot}}(W_{\gamma p}) = \frac{\alpha_{\text{em}} e_Q^2}{\pi} \int dz \, d^2p_{1\perp} \, d^2k_\perp \frac{\alpha_s(\mu^2) F(x, k_{\perp}^2; \mu^2)}{k_{\perp}^2} \times \left\{ [z^2 + (1 - z)^2] \left( \frac{p_{1\perp}}{D_1} + \frac{(k_\perp - p_{1\perp})}{D_2} \right)^2 + m_Q^2 \left( \frac{1}{D_1} + \frac{1}{D_2} \right)^2 \right\},$$

(1)

where $D_1 \equiv p_{1\perp}^2 + m_Q^2$ and $D_2 \equiv (k_\perp - p_{1\perp})^2 + m_Q^2$. The transverse momenta of the heavy quark (antiquark) are denoted by $p_{1\perp}$ and $p_{2\perp} = (k_\perp - p_{1\perp})$, respectively. The heavy quark longitudinal momentum fraction is labeled by $z$. The scale $\mu$ in the strong coupling constant in general is taken to be equal to the gluon virtuality, in close connection with the BLM scheme [13]. On the other hand, in the leading $\ln(1/x)$ approximation, $\alpha_s$ should take a constant value. In our further analysis on heavy quarks we use the prescription $\mu^2 = k_{\perp}^2 + m_Q^2$. In Eq.
Figure 1: The charm and bottom photoproduction cross sections as a function of c.m.s. energy $W_{\gamma p}$ in the proton case. In the plots are shown the results for the semihard approach (solid lines), the saturation model (dot-dashed lines) and collinear (long dashed lines).

(1), the unintegrated gluon function was allowed to depend also on the scale $\mu^2$, since some parametrizations take this scale into account in the computation of that quantity [5].

In order to perform a phenomenological analysis within the $k_\perp$-factorization approach, in the following we use two well known parameterizations for the unintegrated gluon distribution. First, one considers the derivative of the collinear gluon parton distribution function, $F_{\text{dgluon}}(x, k_\perp^2) = \partial xG(x, k_\perp^2)/\partial \ln k_\perp^2$, where the GRV94 LO parameterization [14] was considered for technical simplicity (a comparison using other pdfs can be found in [7]). Hereafter, we will denote as semihard the results obtained using this procedure. It is important to emphasize that if more recent parameterizations are considered, a less steep growth on energy is obtained, but still in agreement with the experimental data [7]. The low transverse momentum region was computed using the ansatz as in Ref. [7]. A shortcoming with this simple parameterization for $F$ is that it becomes negative at large $x$. This can be overcome through the introduction of the doubly logarithmic Sudakov form factor $T_g(k_\perp^2, \mu^2)$, which gives the survival probability that the parton with transverse momentum $p_\perp$ remains intact in the evolution up to the factorization scale $\mu^2$ [15]. So, we can write the unintegrated gluon distribution as $F_{\text{dgluon}}(x, k_\perp^2) = \partial [T_g(k_\perp^2, \mu^2) xG(x, k_\perp^2)]/\partial \ln k_\perp^2$. We will denote as semihard the results obtained using this procedure.

Second, one compute the heavy quark cross sections using the phenomenological saturation model [16], whose unintegrated gluon distribution is given by,

$$F_{\text{sat}}(x, k_\perp^2) = \frac{3 \sigma_0}{4 \pi^2 \alpha_s} \left( \frac{k_\perp^2}{Q_s^2(x)} \right) \exp \left( -\frac{k_\perp^2}{Q_s^2(x)} \right) (1-x)^7,$$

where one has used the parameters from [16], which include the charm quark with mass $m_c = 1.5$ GeV. The saturation scale $Q_s^2(x) = (x_0/x)^\lambda$ GeV$^2$, gives the onset of the saturation phenomenon to the process. The last factor in the equation above takes into account the low energy threshold effects. In Fig. 1 the charm and bottom photoproduction cross sections [17, 18, 19, 20] are shown comparing the referred parameterizations for the unintegrated gluon function. As already
found in Ref. [7], the saturation model gives a lower bound for the cross sections, having a mild increasing on $W_{sp}$, whereas the derivative of the usual pdf presents a steeper growth on energy. The latter disagree with the low energy data, but this can be overcome by introducing the Sudakov form factor discussed before. In the plots we also present the results considering the collinear approach for the LO process $\gamma g \rightarrow Q \bar{Q}$. We have performed fully LO calculations, including LO parton densities and a one-loop calculation evaluation of $\alpha_s$. Similar results are obtained using NLO calculations, since the NLO corrections for heavy quark photoproduction cross section can be expressed in terms of $K$-factors, which is about 1.6 for bottom and $\sqrt{s} = 1$ TeV, while the NLO parton densities are smaller by a similar factor than the LO one. Here we have used $m_c = 1.5$ GeV, $m_b = 4.5$ GeV, factorization scale $\mu_F^2 = \hat{s}$ and the GRV94 LO gluon distribution. If the the GRV98 LO parameterization is used we have that the cross section is reduced by $\approx 20\%$. In Ref. [21] we have analyzed the dependence of the heavy quark cross section in the choices of mass, pdfs and factorization scale. We have that the semihard result using $F_{dgluon}(x, k^2_\perp)$ is quite similar to the collinear one at high energies and the deviation with the saturation model is smaller for the bottom case (For a more detailed discussion see Ref. [7]).

Having reviewed the notions of the $k_\perp$-factorization approach applied to the heavy quark photoproduction and computed the relevant cross section at the nucleon level, now we will consider an attempt of its extension to the nuclear case. In order to do so, we need a parameterization for the nuclear unintegrated gluon function. Corroborated by the good results using $F_{dgluon}(x, k^2_\perp)$ we use the following ansatz for the nuclear case,

$$F_{nuc}(x, k^2_\perp; A) = \frac{\partial xG_A(x, k^2_\perp)}{\partial \ln k^2_\perp},$$

where $xG_A(x, Q^2)$ is the nuclear gluon distribution, which was taken from the EKS parameterization [10]. Consequently, with this procedure we include in our calculations the medium effects (shadowing, antishadowing, EMC and Fermi motion effects) estimated by this parameterization. Moreover, we emphasize that this nuclear gluon distribution is solution of the DGLAP evolution equations, i.e. it is associated to a linear dynamics which does not consider dynamical saturation effects. Similarly to the nucleon case, we denote as semihard the results obtained using this procedure.

In comparison, we calculate the nuclear cross section using the model proposed in Ref. [9], which is an extension of the $ep$ saturation model through Glauber-Gribov formalism. In this model the cross section for the heavy quark photoproduction on nuclei targets reads as [9, 22]

$$\sigma_{tot}^A(W, A) = \int_0^1 dz \int d^2r |\Psi_T(z, r, Q^2 = 0)|^2 \sigma_{dip}(\bar{x}, r^2, A),$$

where longitudinal contributions are suppressed and the transverse wave function is known (See e.g. Ref. [24]). The nuclear dipole cross section is given by,

$$\sigma_{dip}(\bar{x}, r^2, A) = \int d^2b 2 \left\{1 - \exp \left[ -\frac{1}{2} A T_A(b) \sigma_{dip}(\bar{x}, r^2) \right] \right\},$$
where \( b \) is the impact parameter of the center of the dipole relative to the center of the nucleus and the integrand gives the total dipole-nucleus cross section for fixed impact parameter. The nuclear profile function is labeled by \( T_A(b) \), which will be obtained from the 3-parameter Fermi distribution for the nuclear density [23]. The parameterization for the dipole cross section takes the eikonal-like form, \( \sigma_{P_{dip}}(\bar{x}, r^2) = \sigma_0 \left[ 1 - \exp \left( -Q_s^2(\bar{x}) r^2/4 \right) \right] \), with the saturation scale previously defined and \( \bar{x} = (Q_s^2 + 4m_Q^2)/W_{p}^2 \).

The equation above sums up all the multiple elastic rescattering diagrams of the \( q\bar{q} \) pair and is justified for large coherence length, where the transverse separation \( r \) of partons in the multiparton Fock state of the photon becomes as good a conserved quantity as the angular momentum, i.e. the size of the pair \( r \) becomes eigenvalue of the scattering matrix. It is important to emphasize that for very small values of \( x \), other diagrams beyond the multiple Pomeron exchange considered in this formalism should contribute (e.g. Pomeron loops) and a more general approach for the high density (saturation) regime must be considered. However, we believe that this approach allow us to obtain lower limits of the high density effects in the RHIC and LHC kinematic range. Therefore, at first glance, the region of applicability of this model should be at small values of \( x \), i.e. large coherence length, and for not too high values of virtualities, where the implementation of the DGLAP evolution in the \( ep \) saturation model should be required. Therefore, the approach is quite suitable for the analysis of heavy quark photoproduction in the kinematical ranges of the future \( eA \) colliders (eRHIC/TESLA). In Ref. [22] we have analyzed in detail the behavior of the dipole-nucleus cross section and estimated the nuclear heavy quark photoproduction cross section in the inclusive and diffractive cases. In particular, we have predicted large cross sections at eRHIC/TESLA energies.

The corresponding unintegrated gluon distribution can be recovered from a Bessel-Fourier transform to the momentum representation [9],

\[
F_{\text{nuc}}(x, k_{\perp}^2, b) = -\frac{N_c}{4\pi^2\alpha_s} k_{\perp}^2 \int \frac{d^2 r}{2\pi} \exp \left( i k_{\perp} \cdot r \right) \sigma_{dip}^{A}(\bar{x}, r^2, A) = \frac{N_c}{\pi^2\alpha_s} \left( \frac{k_{\perp}^2}{Q_s^2} \right) \sum_{m=1}^{\infty} \sum_{n=0}^{m} \left( -\frac{1}{2} A T_A(b) \frac{m}{m!} \right)^{m} C_n^{m} \left( -1 \right)^n \exp \left( -\frac{k_{\perp}^2}{nQ_s^2} \right) \quad (6)
\]

which depends on the transverse momentum \( k_{\perp} \) through the scaling variable \( \tau \equiv k_{\perp}^2/Q_s^2 \). The unintegrated gluon vanishes asymptotically at \( k_{\perp}^2 \to 0, \infty \) and its maximum can be identified with the saturation scale \( Q_sA(x) \) [9, 25].

It has been verified in Ref. [22], where one computes heavy quark photoproduction within the saturation approach, that the resummation of high density effects at the proton level is less sizeable in the final results at nuclear level. Hence, for heavy quark production, we can approximate the dipole nucleon cross section as \( \sigma_{P_{dip}}^{P}(\bar{x}, r^2) \simeq \sigma_0 Q_s^2(\bar{x}) r^2/4 \) and then compute analytically the unintegrated gluon distribution. Following the procedure in Ref. [26] (See also Ref. [27]), we obtain that the nuclear unintegrated gluon distribution may be expressed as

\[
F_{\text{nuc}}(x, k_{\perp}^2, b) = \frac{N_c}{2\alpha_s \pi^2} \left( \frac{k_{\perp}^2}{Q_s^2 A(x)} \right) \exp \left( -\frac{k_{\perp}^2}{Q_s^2 A(x)} \right), \quad (7)
\]

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Figure 2: The charm and bottom nuclear photoproduction cross sections as a function of c.m.s. energy W. In the plots are shown the results for the semihard approach (solid lines), the saturation model (dot-dashed lines) and collinear using the parameterizations for the nuclear gluon distribution: EKS (long-dashed lines) and AG (dashed lines).

where \( Q_s^2(x) = \frac{1}{2} A T_A(b) \sigma_0 Q_s^2(x) \) define the nuclear saturation scale. This result is consistent with that obtained in Ref. [9] in the first scattering approximation. Such an approximation is justified in the heavy quark case, which is dominated by small dipole configurations (large transverse momentum \( k_\perp^2 \simeq m_Q^2 \)) (See discussion in Ref. [22]). In the case of light quarks, the process receives sizeable contribution from large dipole configurations, i.e. \( k_\perp^2 \leq Q_s^2 \), and higher order rescatterings are needed for the proton as rendered by the phenomenological saturation model. It is important to emphasize that the expression (7) shows clearly the scaling property on the variable \( \tau = k_\perp^2 / Q_s^2 A \). This implies geometric scaling on \( \tau \) in the nuclear heavy quark production, which it already been shown in the nucleon case [28].

In order to compare our predictions for the nuclear photoproduction cross section obtained using the \( k_\perp \)-factorization approach with the collinear one, let us present a brief review of the latter. In this case the cross section is given by a convolution between the partonic cross section for the subprocess \( \gamma g \to Q\bar{Q} \) and the integrated gluon distribution for the nucleus \( xG_A(x, Q^2) \). Here we consider the EKS and AG parameterizations for this distribution. As discussed before, the EKS parameterization was obtained from a global fit of the nuclear experimental data using the DGLAP evolution equations, which is a linear evolution equation which does not consider dynamical saturation (high density) effects. In Ref. [11] a procedure to include these effects in the nuclear gluon distribution was proposed, resulting in a parameterization for this distribution (AG parameterization), which also includes those present in the EKS parameterization. The main characteristic of this parameterization is that it predicts a stronger reduction of the growth of the gluon distribution at small values of \( x \) than the EKS one. In order to estimate the sensitivity of nuclear heavy quark photoproduction in these effects, we also use this parameterization as input in our calculations using the collinear factorization approach.

In Fig. 2 are shown the results for the charm and bottom photoproduction cross section as a function of energy for lead and calcium. We compare the predictions of the \( k_\perp \)-factorization, considering the unintegrated gluon distributions discussed above (SAT-MOD and SEMIHARD...
in the figure) with results of the collinear factorization and two parameterizations for the nuclear gluon distribution (EKS and AG in the figure). We have that the results obtained using the derivative of the EKS gluon distribution and the $k_\perp$-factorization (SEMIHARD in the figure) are quite similar with those ones coming from the collinear approach where nuclear effects (EKS parameterization [10]) and high density corrections (AG parameterization [11]) are taken into account. In particular, we have that the predictions using the AG parameterization in the collinear approach are similar to the semihard one, which does not consider high density effects. This demonstrate that in this process we cannot distinguish if the modification in the behavior of the cross section is associated to high density effects in the collinear approach or a generalization of the factorization without high density effects in the unintegrated gluon distribution. On the other hand, if these effects are present and the factorization of the cross section is given by the $k_\perp$-factorization, as is the case for the predictions from the saturation model, we have that the difference between the cross sections is large, which should allow to discriminate between the theoretical approaches. Therefore, the nuclear cross section would provide a strong test concerning the robustness of the saturation approach in describing the observables. The situation is less clear comparing the semihard approach and the collinear one. One possible interpretation for this result is that the expected enhancement in the semihard approach, associated to the resummation of the $\left(\alpha_s \ln \frac{\sqrt{s}}{m_q}\right)^n$ in the coefficient function [2], is not sizeable for inclusive quantities in the kinematic region of the future colliders. Probably, a more promising quantity to clarify this issue would be the transverse momentum $p_\perp$ distribution. In this case, the semihard approach seems to be in better agreement with experimental data in the $pp$ collisions than the collinear approach [6].

3 Summary and Conclusions

We calculate the nucleon and nuclear cross sections for heavy quark photoproduction within the $k_\perp$-factorization approach. Two simple parameterizations for the unintegrated gluon distribution in the proton were considered: the derivative of the collinear gluon pdf and the phenomenological saturation model. The latter underestimate the measured cross section at HERA regime and provides a lower limit for the production. On the other hand, the former agrees with the available high energy data and produces similar results as the collinear approach. In the nuclear case, we have introduced a simple ansatz for the nuclear unintegrated gluon function, namely from the nuclear collinear gluon pdfs. The Glauber-Gribov extension of the saturation model to the nuclear collision is also analyzed, where we found an analytic expression for the unintegrated gluon function using a non-saturated ($r^2 \to 0$) proton dipole cross section. Such a function shows a clear geometric scaling property on the variable $\tau = k^2/Q_{sA}^2$. The nuclear cross section for lead and calcium in the energy range relevant for the future $eA$ colliders eRHIC/THERA were computed, comparing them with the results from the collinear approach which take into account nuclear medium effects and also high parton density phenomenon. Our results indicate that a future experimental analysis of this process can be useful to constraint the QCD dynamics at high energies.
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