Is Betelgeuse the Outcome of a Past Merger?

E. Chatzopoulos1,2, Juhan Frank1, Dominic C. Marcello1,3, and Geoffrey C. Clayton1

1 Department of Physics & Astronomy, Louisiana State University, Baton Rouge, LA, 70803, USA; chatzopoulos@phys.lsu.edu
2 Hearne Institute of Theoretical Physics, Louisiana State University, Baton Rouge, LA, 70803, USA
3 Center for Computation and Technology, Louisiana State University, Baton Rouge, LA, 70803, USA

Received 2019 March 11; revised 2020 May 5; accepted 2020 May 7; published 2020 June 12

Abstract

We explore the possibility that the star α Orionis (Betelgeuse) is the outcome of a merger that occurred in a low-mass-ratio ($q = M_2/M_1 = 0.07$–0.25) binary system some time in the past hundreds of thousands of years. To that goal, we present a simple analytical model to approximate the perturbed internal structure of a post-merger object following the coalescence of a secondary in the mass range 1–4 $M_\odot$ into the envelope of a 15–17 $M_\odot$ primary. We then compute the long-term evolution of post-merger objects for a grid of initial conditions and make predictions about their surface properties for evolutionary stages that are consistent with the observed location of Betelgeuse in the Hertzsprung–Russell diagram. We find that if a merger occurred after the end of the primary’s main-sequence phase, while it was expanding toward becoming a red supergiant star and typically with radius $\sim$200–300 $R_{\odot}$, then its envelope is spun up to values that remain in a range consistent with Betelgeuse observations for thousands of years of evolution. We argue that the best scenario that can explain both the fast rotation of Betelgeuse and its observed large space velocity is one where a binary was dynamically ejected by its parent cluster a few million years ago and then subsequently merged. An alternative scenario in which the progenitor of Betelgeuse was spun up by accretion in a binary and released by the supernova explosion of the companion requires a finely tuned set of conditions but cannot be ruled out.

Unified Astronomy Thesaurus concepts: Stellar mergers (2157); Binary stars (154); Close binary stars (254); Stellar evolutionary models (2046); Stellar rotation (1629); Supergiant stars (1661)

1. Introduction

Recent observational surveys of massive main-sequence (MS) stars have shown that a large number of them rotate rapidly, with some reaching rotational speeds as high as $\sim$450 km s$^{-1}$ and with a bimodal distribution of rotational velocities (Dufton et al. 2011, 2013; Ramírez-Agudelo et al. 2013). In addition, the Kepler space mission reports observations of 17 rapidly rotating $\lesssim 1$–3 $M_\odot$ stars in the giant phase of their evolution with rotational speeds up to $\sim$18 times that of the Sun (Costa et al. 2015; see also studies of the rotation rates of young spectroscopic binaries by Ramírez-Agudelo et al. 2015). These findings, coupled with the observation that the majority ($\sim$60%) of massive stars are members of binary stellar systems (Mason et al. 2009; Dunstall et al. 2015) and that most of the massive stars in such systems will at some time undergo binary interactions with a third of them even experiencing a merger (Sana et al. 2012), indicate the importance of studying the effects of stellar mergers on the long-term evolution of the rotational properties of massive stars.

Binary population synthesis models presented by de Mink et al. (2013, 2014) support the idea that $\sim$20% of massive MS stars are the products of binary interaction. Furthermore, the presence of a low-velocity component of the bimodal distribution of the rotational velocities of massive stars (Dufton et al. 2013) together with evidence of strong magnetism in some massive stars (Grunhut et al. 2012; Schneider et al. 2016) motivated theoretical studies of the merger of a massive star with a lower mass companion as an avenue to produce these properties (Ferrario et al. 2009; Langer 2012). Despite all of the evidence pointing toward the prevalence of stellar mergers and their subsequent effects on the evolution of massive stars, detailed long-term evolution studies of such post-merger stars are limited (Podsiadlowski et al. 1990, 1992; Menon & Heger 2017).

The massive red supergiant (RSG) star α Orionis, popularly known as Betelgeuse, is a potentially interesting candidate for a past binary merger event, partly because of its apparent high rotational velocity. Using long-slit spectroscopy across the minimally resolved disk of Betelgeuse obtained by the Hubble Space Telescope (HST), the estimated surface rotational velocity of the supergiant star ($v_{\text{rot}} \sin i$) is $\sim$5 km s$^{-1}$ (Gililand & Dupree 1996; Uitenbroek et al. 1998). Recent observations by the Atacama Large Millimeter Array appear to further support this result even within the uncertainties imposed by large-scale convective motions on the star’s surface (Wheeler et al. 2017; Kervella et al. 2018). Furthermore, the observation of enhanced nitrogen on the surface of Betelgeuse is indicative of enhanced mixing, triggered by rotation (Meynet et al. 2013). In particular, the measured N/C (nitrogen to carbon) and N/O (nitrogen to oxygen) surface abundance ratios for Betelgeuse are 2.9 and 0.6, respectively, while standard solar values are N/C = 0.3 and N/O = 0.1 (Lambert et al. 1984). High rotation during the supergiant phase is neither found in stellar evolution calculations of single massive stars—including those that are rapid rotators at the zero age main sequence (ZAMS)—nor is expected by simple arguments of angular momentum (AM) conservation (Wheeler et al. 2017). Measurements of giant and supergiant star rotation rates support this argument (Ceillier et al. 2017).

In addition to being a rapid rotator, Betelgeuse is also a known runaway star with a measured space velocity of $\sim$30 km s$^{-1}$ and a kinematic age of $\sim$7–11 Myr (Harper et al. 2008, 2017). Backwards extrapolation of Betelgeuse’s trajectory has led some to suggest that its possible birthplace is the Orion OB1a association (Briceño et al. 2005) though...
alternative scenarios involving two dynamical kicks have been suggested (Bally 2008). Betelgeuse’s flight through the interstellar medium is also illustrated by HST observations of a bow shock forming a 0.14 $M_\odot$ swept-up shell of material around the star at a radius of $\sim 6'–7'$ corresponding to a physical distance of $\sim 0.8$ pc using the measured $\sim 400$ pc distance of Betelgeuse (Noriega-Crespo et al. 1997). The morphology of this structure is attributed to wind from the star sweeping up interstellar medium in the direction of motion (Mohamed et al. 2012; Mackey et al. 2014).

To investigate the long-term effects of a merger during the post-MS (PMS) evolution of massive stars and to model the observed properties of Betelgeuse in particular, simulations spanning a variety of timescales that involve diverse numerical approaches are necessary: the merger occurs in a dynamical timescale while the post-merger thermal adjustment and subsequent evolution in thermal and nuclear timescales. Furthermore, any successful model of Betelgeuse has to account for both its rapid rotation rate and its runaway nature, so a sequence of events (dynamical ejection of a binary followed by a merger) has to be invoked.

In the present work, we compute an approximate, analytical model of the perturbed, post-merger structure of a massive star assuming that it suffered the coalescence of a smaller, 1–4 $M_\odot$ secondary into its envelope, and compute the long-term evolution of the post-merger object under the assumption of different initial conditions for the original binary system. We find that a merger of a binary with mass ratio in the range $q = 0.07–0.25$ occurring during the “Hertzsprung gap”–crossing phase, after the end of the MS, can yield high surface equatorial rotational velocities, in agreement with observations of Betelgeuse. In addition, our models predict that high rotation is preserved for hundreds of thousands of years following the merger event. We also show that such runaway, low-mass-ratio binary systems can be dynamically ejected from clusters without being disrupted, allowing for the merger to occur at a later time.

Our paper is organized as follows: in Section 2 we present a qualitative analysis of the kinds of binaries likely to reproduce the observed properties of Betelgeuse considering both the merger and the accretion scenarios, and find the merger path more compelling. However, we are not able to rule out completely the accretion option given the current uncertainties in the evolution of massive binaries. In Section 3, we present our initial setup and synchronization conditions for low-mass-ratio binaries of interest and introduce a simple analytical model to approximate the post-merger structure of the primary. In addition, we present a 3D hydrodynamical simulation of a merger to be used for benchmarking against some of our analytical assumptions. The MESA evolution calculations for the post-merger objects are presented in Section 4. Section 5 presents the results of our calculations, including comparisons with the observed properties of Betelgeuse. Finally, in Section 6, we discuss the implications of our results for Betelgeuse as well as other observations and describe our plans for future work.

### 2. Spun-up by Accretion or Merger?

Betelgeuse is not only a fast rotating supergiant but it is also a runaway star, probably born in one of the clusters or subassociations of OB1 in Orion (Harper et al. 2008, 2017). In this section, we consider a variety of initial progenitor configurations and evolutionary histories for Betelgeuse to show, using AM conservation and simple dynamical arguments, that it is very difficult to reconcile both the large space velocity and fast rotation without invoking a recent binary interaction yielding a fast rotating single progenitor that subsequently evolved within a million years or so to the RSG we see today. We consider two possible scenarios: a binary merger, preferably in a PMS stage of evolution, or a late case B accretion event followed by a supernova (SN) explosion of the donor. The high space velocity suggests ejection from a binary as a result of an SN explosion of a much more massive companion that disrupted the binary (Blauw 1961), or a dynamical ejection from a cluster or compact OB association (Poveda 1964).

If Betelgeuse had evolved as a single star, given its present RSG status, its age would be around 8–10 million years. Early ejection as a single star either by the disruption of a cluster binary or dynamical escape from a cluster is unlikely to yield a rapid rotator in the present supergiant stage. Single massive stars lose a fraction $f$ of their mass, which carries away some AM through winds during the MS phase. In particular, O stars evolve through rapid mass and AM losses to much slower rotating B stars with $v \sin i \lesssim 50$ km s$^{-1}$ (Maeder & Meynet 2000; Higgins & Vink 2019 and references therein). During their MS evolution, it is reasonable to assume that stars remain close to solid-body rotation. For example, for a 20 $M_\odot$ star on the ZAMS, with radius $R_i$ and gyration radius $\beta_i$, its initial AM can be written as $J_i = \beta_i^2 M_i R_i v_{eq,i}$. Similarly, after losing a mass fraction $f$ of the initial mass, $M_i = (1-f)M_i$, its AM on the terminal age main sequence (TAMS) can be written as $J_f = \beta_f^2 (1-f)M_i R_i v_{eq,f}$. Without a detailed model for the mass and AM losses carried by the wind, we do not know a priori the average specific AM lost to the wind. We may expect it to be on the order of the specific AM of the surface layers, and we can write in general that the total AM lost to the wind is

$$J_f - J_i = -fM_i \gamma R_i v_{eq,i},$$

where $fM_i$ is the mass loss, and $\gamma R_i v_{eq,i}$ is the average specific AM lost. Using AM conservation and solving for the equatorial velocity at the TAMS, we get

$$v_{eq,f} = v_{eq,i} \frac{\beta_f^2 (1-f)R_i}{\beta_i^2 (1-f)R_f},$$

where the initial equatorial velocity is unlikely to exceed $\sim 200$ km s$^{-1}$ at the ZAMS. One can easily see that for the example considered, $R_i \sim 6 R_\odot$, $R_f \sim 18 R_\odot$, and values for the gyration radii $\beta_i \simeq 0.29$ and $\beta_f \simeq 0.16$ (Claret & Gimenez 1989), it is relatively easy to decrease $v_{eq,f}$ to 50 km s$^{-1}$ and below. For a fixed value of $f$, $v_{eq,f}$ decreases linearly with $\gamma$. Despite its simplicity, this model suggests that you need at least a mass-loss fraction of $f \geq 0.07$ to reduce the equatorial velocity at the TAMS to $\sim 50$ km s$^{-1}$, unless one appeals to magnetic effects that could make $\gamma > 1$. During the rapid expansion while the PMS star crosses the Hertzsprung gap, we may assume that redistribution of AM is inefficient and that a better approximation is to take “local” AM conservation and write $v_{eq} = v_{T} R_f / R$, where the subscript “T” stands for values at the TAMS, while $v_{eq}$ and $R$ represent the values attained when the star has expanded to RSG size. With $v_{T} \approx 50$
km s\(^{-1}\), \(R_1 \approx 18 R_\odot\), and \(R \sim 10^3 R_\odot\) this estimate yields \(v_{\text{ej,1}} \sim 1\) km s\(^{-1}\). This is very much an upper limit. In fact, detailed simulations of the evolution of single massive stars, including mass and AM losses, from ZAMS to the supergiant stage, typically yield \(v_{\text{ej,1}} < 1\) km s\(^{-1}\) (Ekström et al. 2008, 2012; Brott et al. 2011a, 2011b; Wheeler et al. 2017).

If Betelgeuse’s progenitor was initially the less massive member of a massive binary, then we need to consider how the spin-up by accretion would impact the above argument. We discuss this possibility later in the context of the current incomplete understanding of the complex evolution of massive binaries of arbitrary initial mass ratios and separations.

A further apparent difficulty with Betelgeuse is that a simple backward extrapolation of its known space velocity does not appear to bring it close to any plausible subassociation of OB1 as its birthplace (Bally 2008). This suggests a two-step process: (1) a dynamical ejection of a binary within the first few million years of Betelgeuse’s birth cluster, and (2) a subsequent merger of the binary or an SN explosion of the more massive component, releasing the surviving Betelgeuse at some PMS stage of its evolution. Recent binary stellar evolution models suggest that the SN mechanism alone is not as efficient in producing runaway stars as it was previously thought, with only a tiny fraction of stars ejected by the SN of their companions reaching velocities \(>30\) km s\(^{-1}\) (Renzo et al. 2019). A two-step process gets around this difficulty. It is, however, noted that for the merger to change the flight direction of the post-merger, it would require significant asymmetric mass loss. This is possible, (e.g., mass loss via the \(L_2\) point), but that would also lead to the removal of some AM. An SN explosion in the binary instead would eject the companion star with a direction depending on the orbital phase of the binary, which requires fine-tuning to be aligned with the previous space velocity in the double-ejection scenario.

For a binary to remain bound after dynamical ejection due to interactions with other binaries and members of the early cluster, its binding energy must be greater than the kinetic energy of the escaping binary plus the binding energy of the original binary to the cluster:

\[
\frac{GM_1M_2}{2a_1} > \frac{1}{2}M(v_{ej}^2 + \sigma_c^2),
\]

where \(M = M_1 + M_2\) is the initial total mass of the binary, \(v_{ej}\) is the ejection velocity of the binary, and \(\sigma_c\) is the central velocity dispersion in the cluster. We take \(v_{ej}\) to be on the order of the observed runaway velocity of Betelgeuse (\(\sim 30\) km s\(^{-1}\)) and \(\sigma_c \approx 6.5\) km s\(^{-1}\), typical for a cluster with mass \(10^4 M_\odot\) (in agreement with the measured mass of the Ori OB1 association, the proposed birthplace for Betelgeuse; Blaauw 1964; Brown et al. 1994) and half-mass radius of \(\sim 1\) pc. Thus, the dominant term is the runaway kinetic energy, and we ignore \(\sigma_c\) in the following. From the above argument, we conclude that the initial separation should not exceed

\[
a_1 < \frac{GqM}{(1 + q)^2v_{ej}^2},
\]

where \(q = M_2/M_1\) is the mass ratio of the binary. This condition turns out not to be very restrictive because the components of massive binaries with \(M \sim 30 M_\odot\) and initial separations greater than \(15–20\) au would evolve as single stars without interacting. Therefore, most of the binaries considered in the analysis that follows would survive the ejection from their parent cluster. This is further supported by results of \(N\)-body simulations of the dynamical cluster evolution focusing on binary–binary interactions predicting a considerable fraction of binaries that escape the cluster without being disrupted (Mikkola 1983; Gies & Bolton 1986; Oh & Kroupa 2016; Kroupa et al. 2018; Wang et al. 2019). In particular, the simulations in Oh & Kroupa (2016; and private communication with Dr. Pavel Krupa) show that for a variety of initial assumptions, a handful of binaries with \(q < 0.3\) and orbital periods in the range \(2 < \log P_{\text{days}} < 3\) are ejected in the first few million years of cluster life. As we shall see, these are precisely the kinds of binaries whose merger has the potential to account for the properties of Betelgeuse.

Without loss of generality, we may assume that \(M_1 > M_2\) or \(q \leq 1\) for the ejected binary. We further assume that one or both components are moderately massive, such that \(M \sim 15–20 M_\odot\). The evolution of massive binaries is subject to many uncertainties, and there are significant differences in the detail of the outcomes of such simulations by various groups. Mass transfer starts as the more massive component evolves first and overflows its Roche lobe. Apart from differences in the detail and uncertainties in the exact critical values of \(q\), most investigators distinguish the following regimes: if the binary components are similar in mass, evolution to a contact configuration is avoided. If \(q_{\text{cont}} < q < 1\), which depends on the evolutionary phase of the donor, is somewhere in the range \((0.65, 0.8)\), \(M_2\) overflows its Roche lobe, mass transfer begins either in Case A or early Case B (Kippenhahn & Weigert 1967), and is high but stable, leading to inversion of the mass ratio and an “Algol” analog, with separation and period increasing as the system evolves (Pols 1994; Podsiadlowski 2010). While the ultimate fate of such binaries is of interest elsewhere, they do not produce Betelgeuse-like stars. As an example of such evolutions, a binary consisting of a \(16 M_\odot\) primary and a \(14 M_\odot\) secondary \((q = 0.875)\) evolves through Case A and Case AB mass transfer dumping most of the H-rich primary envelope onto the secondary, yielding a fast rotating blue supergiant (BSG), while the primary becomes a He star. In many cases, especially if the mass transfer is conservative, the secondary explodes as an SN first (Pols 1994; Wellstein et al. 2001; Paxton et al. 2015).

For mass ratios close to \(q_{\text{cont}}\), the outcome is dependent on the initial orbital period \(P_i\). For example, de Mink et al. (2013) investigated in detail the outcomes of the evolution of a binary of \(q = 0.75\), with initial components \(M_1 = 20 M_\odot\) and \(M_2 = 15 M_\odot\). For \(P_i < 2\) days, after Case A mass transfer, a rapidly rotating merger resulted, which spun down quickly. For \(2 < P_i < 5\) days, after Case AB or even Case ABB mass transfer, they obtained a rapidly spinning secondary, which then also spins down in a couple of million years. For even longer orbital periods with 10 days \(< P_i < 10^3\) days, mass transfer sets in as the primary is evolving to become a red giant (Case B) and that also may lead to a rapidly rotating secondary, now more massive than the original primary. However, the details of the evolution depend on metallicity, the efficiency of accretion (the fraction of mass transfer actually captured by the secondary), mass loss via winds, and the efficiency of semiconvection. Sometimes the H-rich accreted material is mixed down into the core and a BSG results, sometimes mixing
is not so efficient and an RSG with a small core results. In addition, it turns out that which of the two stars goes SN first also depends on these details (Wellstein et al. 2001). Therefore, in order to get a single RSG whose companion explodes first as an SN releasing a spun-up star with properties similar to Betelgeuse may require a narrow set of conditions, but to estimate the probability for this channel would require a series of binary stellar evolution calculations specifically designed for this purpose, perhaps starting with an ad hoc set of binary population synthesis. This is beyond the scope of the present work, in which we focus on the merger channel recognizing that there may well exist a set of binary parameters that would result in Betelgeuse-like outcomes in which accretion yields the relatively high equatorial velocity observed. At this point, we cannot rule that out completely.

For lower mass ratios, down to $q_{\text{blue}}$, where $q_{\text{blue}}$ is somewhere in the range (0.25, 0.33), $M_2$ is unable to adjust to the mass transfer, expands, and the system evolves into a massive contact binary. As time proceeds, the contact binary shrinks, converting orbital AM into circulation or rotation and ultimately merges, producing a massive analog of a “blue straggler.” This occurs because during the merger, hydrogen-rich material gets mixed into the core, rejuvenating the merged object. While this may well produce rapidly rotating BSGs, like the presumed progenitor of SN 1987A (Podsiadlowski et al. 1990; Menon et al. 2019), they are not applicable to Betelgeuse.

Finally, for even lower mass ratios, we have the cases that we consider in more detail in subsequent sections, which in our view offer a more likely pathway to a star with Betelgeuse’s properties. For mass ratios $q < q_{\text{blue}}$ and $P_t >$ a few tens of days, mass transfer begins as an early Case B, after H is exhausted in the primary, is rapid, and results in the primary envelope engulfing the much lower mass secondary, which then spirals inward, and producing a merger. In this scenario, the primary’s helium core is surrounded by a H-burning shell. When the secondary reaches the critical tidal disruption distance from the core of the primary, a tidal stream will form, transporting fresh H fuel toward the core as described in Ivanova (2002), Ivanova et al. (2002), Ivanova & Podsiadlowski (2003), and Schneider et al. (2016). The penetration depth of the stream into the core of the primary determines the extent of its rejuvenation; if fresh fuel reaches the core, then core H burning will be reignited, and the star may evolve toward the BSG phase. If, on the contrary, the stream does not penetrate deep into the core but rather mixes in with the H-burning shell, then the star will keep evolving toward the RSG stage. Using the same arguments as the ones presented in Ivanova et al. (2002) involving the Bernoulli integral to calculate the penetration depth, we have found that in none of our models is the stream expected to penetrate the core of the primary, thus suggesting a post-merger evolution toward the RSG phase. This is in agreement with the “quiet merger” scenario discussed in Ivanova & Podsiadlowski (2003) that, in addition, predicts the formation of rapidly rotating supergiants via this channel. We have also confirmed this via a 3D numerical merger simulation for a system in parameters in our range of interest (a 16 $M_\odot$ and a 1 $M_\odot$ secondary; Section 3.4). When $q < q_{\text{blue}}$, the lower mass companion is engulfed in the atmosphere of $M_1$ as it overflows its Roche lobe, and $M_2$ ends up spiraling inward and is tidally disrupted outside the core of the primary, so not much hydrogen-rich material is mixed into the core and the final result is an RSG that has a high equatorial velocity as these layers absorbed the bulk of the orbital AM of the secondary. The amount of orbital AM depends mostly on the separation of the binary when the primary overflows its Roche lobe. These are the cases most likely applicable to Betelgeuse.

Which binary parameters subject to the restrictions described above are likely to yield an equatorial velocity exceeding $\sim$5 km s$^{-1}$ when the merged object evolves into an RSG? Before attempting to answer this question in the following sections, it is worth obtaining a simple estimate based on AM conservation. Most of the AM of the pre-merger binary is in the orbital AM $J_{\text{orb}} = \mu v_\text{orb}$, where $\mu$ is the reduced mass, $a$ is the binary separation, and $v_{\text{orb}} = (GM/a)^{1/2}$ is the Keplerian velocity for a circular orbit. Numerical hydrodynamic simulations of binary mergers show that the immediate post-merger object is roughly of the same size as the original binary and is differentially rotating. Nonetheless, for our present purposes, we estimate the equatorial velocity of the merged object by assuming a uniform density sphere rotating as a solid body, and we set $J_{\text{orb}} = (2/5)Ma v_{\text{pm}}$, where $v_{\text{pm}}$ is the post-merger equatorial velocity. Because in all cases of interest contact, mass transfer, and merger occur during the crossing of the Hertzsprung gap, the subsequent evolution to RSG is very rapid; we may assume “local” AM conservation and set $v_{\text{eq}} \approx v_{\text{pm}} a/R_1$. Therefore, we have as our order-of-magnitude estimate the following result:

$$v_{\text{eq}}(q, a) = \frac{5q}{2(1 + q)} v_{\text{orb}}(M_1, \alpha) \frac{a}{R_1}$$

(5)

Figure 1 shows the binary parameter region likely to yield equatorial velocities consistent with the measured values of $v_{eq}$ sin $i$ for Betelgeuse, for an assumed initial binary mass of 20 $M_\odot$. All contours are limited at the maximum separation...
allowed for a binary to survive ejection as estimated by Equation (4). We will explore in detail the outcomes of mergers with such initial parameters in Sections 4 and 5.

3. Merger Model

3.1. Initial Conditions for the Binary System

We begin by considering a few possible initial configurations for our binary, differing only in the separation (and orbital period) at the point at which the primary fills its Roche lobe, initiating mass transfer and a rapid evolution leading to the plunge of the secondary into the envelope of the primary. These distinct binary separations result in contact at different stages of the evolution of the primary through the Hertzsprung gap. We will consider four situations corresponding to the primary radius \( R_1 \) filling its Roche lobe when \( R_1 = 12 \, R_\odot, 100 \, R_\odot, 300 \, R_\odot, \) and 500 \( R_\odot \). These situations correspond to contact soon after the end of the MS phase, two intermediate stages in the middle of the crossing, and one near the red end of the Hertzsprung gap as the ascent of the red giant branch is to begin shortly.

The total AM of such a binary consists of the orbital and the spin angular momenta. As the primary evolves, initially tides will exchange AM between the components and a relatively small fraction may be lost from the system due to winds. The amount of AM lost is proportional to the mass lost, and for stars in this mass range it is small, but it can be very large for more massive stars. As the primary reaches contact, mass transfer starts and a common envelope (CE) forms, and hydrodynamic processes complete the redistribution of AM in the merged object. We do not know for certain the natal spin AM of the primary, but there is some evidence that young massive stars are fast rotators with equatorial velocities \( v_{eq} \sim 200 \, \text{km} \, \text{s}^{-1} \) (Maeder & Meynet 2000; Dufton et al. 2011; Ramirez-Agudelo et al. 2013).

In the absence of tidal synchronization torques, the spin period at any stage could be estimated from spin AM conservation, but more realistically, the spin period should be determined, taking into account tidal interactions. In order to better understand the process, it is useful to estimate and compare the various timescales involved. The relevant timescales to be considered are the evolutionary times required for the primary to expand to contact at the above lobe radii and binary separations, the orbital period of the binary at that point, the tidal synchronization timescale for the primary to lock to the orbital period, the timescale for the formation of the CE enveloping the secondary, and finally, the timescale for inspiral and merger.

The evolutionary timescales are calculated by following in MESA (Paxton et al. 2011, 2013, 2015, 2018, 2019) the evolution of a single massive star with a mass of either 15 \( M_\odot \) or 20 \( M_\odot \) from the ZAMS to the four expansion stages selected above. As is well known, the evolution through the hydrogen burning and the initial expansion to \( R_1 = 12 \, R_\odot \) is the longest phase, taking about \( \sim 10^7 \) yr to complete for the 15 \( M_\odot \) primary. The expansion through the gap gradually speeds up, taking \( \sim 1.2 \times 10^6 \) yr to reach \( R_1 = 100 \, R_\odot \), an extra couple of thousand years to reach \( R_1 = 300 \, R_\odot \), and less than a thousand years to expand further to \( R_1 = 500 \, R_\odot \). These times are of the same order of magnitude but somewhat faster, and the expansion behavior is qualitatively similar for a more massive primary of 20 \( M_\odot \).

The orbital period corresponding to first contact is simply calculated from Kepler’s third law, taking into account that the primary comes into contact when \( R_1 = 0.609a \) for a mass ratio \( q = 0.067 \) corresponding to \( M_1 = 15 \, M_\odot \), where \( a \) is the binary separation (Eggleton 1983). The orbital period at the beginning of the plunge phase, when hydrodynamical drag on the companion becomes important, can be estimated by setting the binary separation to \( R_1 \). For the assumed value of \( q \), this period is shorter than the period at first contact by a factor 2.1. The orbital periods for the four assumed fiducial situations are thus \( P_{orb} = 2.5 \) days, 61 days, 319 days, and 685 days, respectively, and slightly shorter for the more massive primary.

We estimate the synchronization timescale using Equation (4.12) from the paper by Zahn (1977), which is appropriate for stars with a convective envelope (that continues to hold for our models out to radii of 300 \( R_\odot \)) and assumes efficient turbulent eddy viscosity,

\[
I_{\text{sync}} \sim \frac{1}{6q^2k_2} \left( \frac{M_0 R_1^2}{L} \right)^{1/3} I_1 \left( \frac{a}{R} \right)^6
\]

where \( q = M_2/M_1 \) is the binary mass ratio, \( k_2 \) is the second-order apsidal constant for the primary, \( I_1 \) is the moment of inertia of the primary, and \( L \) is its luminosity. It so happens that \( k_2 \) and \( I_1/M_0 R_1^2 \) nearly cancel each other to within a factor of 2, and given the uncertainties involved, it is sufficient for our purposes to take that ratio as unity. Thus, the main dependence on parameters comes from the factor \( R_1^{2/3} \). These estimates yield \( \sim 100 \) yr, \( \sim 420 \) yr, \( \sim 879 \) yr, and \( \sim 1200 \) yr for spin–orbit synchronization for the cases considered.

Upon contact, mass transfer from the primary to the secondary is dynamically unstable and results in the formation of a CE, leading quickly to engulfing the secondary into the envelope of the primary. Our 3D hydrodynamic simulation of a 16 \( M_\odot + 1 \, M_\odot \) merger at a time when the primary has expanded out to a radius of \( \sim 12 \, R_\odot \) (Section 3.4) shows that it only takes \( \sim 5 \) days for the secondary to inspiral and be disrupted as it approaches the core of the primary.

A simple analytic estimate for the inspiral time is obtained by taking the orbital AM of the secondary and dividing it by the torque (see Section 3.2 for details). The AM of the secondary is \( J_2 = M_2 a_2^2 \Omega \), where \( \Omega \) is the Keplerian orbital frequency, and \( a_2 = a/(1 + q) \) is the distance from the center of mass of the system and the center of mass of the secondary. For the hydrodynamic torque, we adopt Equation (9), but for the purposes of obtaining an order-of-magnitude estimate, we set \( \rho_s(r) \) to the average density of the primary and \( M_1(r) = M_1 \). Therefore, we expect our estimate to be a lower limit to the actual inspiral time. With these approximations, we get the following expression for the inspiral time:

\[
t_{\text{insp}} = \frac{8q^{3/2}}{3c_{\text{D}}(1 + q)^{3/2}} \left( \frac{R_1}{R_2} \right)^{7/2} \left( \frac{R_2^3}{G M_2} \right)^{1/2}.
\]

Inserting the values appropriate for the four scenarios we are contemplating, the above equation yields 4.6 days, 21 yr, 980 yr, and 5900 yr for a primary mass of 15 \( M_\odot \) and correspondingly shorter times, by a factor of 0.65, for a 20 \( M_\odot \) primary. As a check for this approach, we may compare the inspiral timescale obtained in the hydrodynamic simulation for the case \( R_1 = 12 \, R_\odot \) with our simple analytic estimate.
In summary, with the possible exception of contact at 500 $R_\odot$ and beyond, the initial mass transfer from primary to secondary is likely to start with the components synchronous with the orbit. However, as a result of the unstable mass transfer and relatively rapid orbital shrinking to the plunge and drag phases, synchronicity may be broken. The inspiral phase is also shorter than, or at most of the same order, as the synchronization time; therefore, to follow all these processes self-consistently, one would have to carry out numerical simulations with all the physics included, which is not feasible with the resources at our disposal. We will therefore adopt the approximation that the secondary spirals inward along a sequence of Keplerian orbits, depositing a fraction of order unity of the orbital AM in the atmosphere of the primary.

3.2. Merger Model Assumptions

The merger scenario described here is similar to one considered by Ivanova et al. (2002) and Menon & Heger (2017) involving the complete disruption of the secondary deep inside the envelope of a massive primary during a short-lived CE phase. Such an event is classified as a “moderate” merger that eventually leads to evolution toward the RSG phase. In our model, the inspiral of the secondary is caused solely by the effects of viscosity (dynamical friction, or drag) of the secondary within the envelope of the primary. During this process, a fraction of the AM lost by the secondary is deposited to the envelope of the primary causing it to spin up. The dynamical merger process begins at the time of contact between the expanding envelope of the primary and the secondary and continues until the secondary reaches a radius equal to its tidal radius where it gets completely disrupted. This effective tidal radius is very close to the radius of the He core of the primary ($\sim 1 R_\odot$). A main difference between this work and that of Menon & Heger (2017) is our predictions about the effect of such merger on the evolution of the AM profile of the primary and, more specifically, the surface equatorial rotational velocity.

To derive an approximate analytical model of the perturbed internal structure of a massive primary star in the context of the merger scenario discussed above, we resort to the following assumptions for the progenitor binary system:

1. A low-mass ratio for the binary progenitor system ($q = M_2 / M_1 = 0.07-0.25$). For our study, we adopt binary systems with ($M_1$, $M_2$) = (15, 1), (16, 4), and (17, 3) (in solar units) that satisfy this criterion. The choice of a low-mass ratio allows for the possibility that the secondary spends a considerable amount of time in the envelope of the primary while spiraling in toward the core, well before it is tidally disrupted. This guarantees that, in the process, the secondary deposits a fraction of its AM into the envelope of the primary and that the initial RLOF is dynamically unstable and will result in a CE. Additional arguments about the necessity of a low-mass ratio were discussed in Section 2.

2. The merger event occurs after the end of the primary’s MS phase and while its envelope is expanding while crossing the “Hertzsprung gap” over a thermal timescale (lasting a few tens of thousands of years). As such, our models consider early Case B merger events. This implies that the envelope of the primary comes into contact with the secondary, due to the expansion of the former on its way to becoming a supergiant star and at radii of 200 $< R_1 < 700 R_\odot$, where $R_1$ is the radius of the primary. This condition is necessary in order to facilitate a large density contrast between the secondary and the envelope of the primary, ensuring that the secondary remains intact during the coalescence.

3. The spiral-in timescale of the secondary is significantly smaller than the thermal adjustment timescale of the envelope of the primary. This approximation implies that in our model, we do not take into account the effect of the expansion of the primary’s envelope during the merger event and assume that it does not affect the dynamics of the spiral-in process. This is a good approximation given that, for the above-mentioned initial binary conditions during contact, the timescale it takes for the secondary to reach the tidal radius (which is approximately equal to the radius of the helium (He) core of the primary) is on the order of $\sim 100$ yr while the thermal adjustment timescale of the primary’s envelope is on the order of $\sim 10^4$ yr.

4. The magnitude of the secondary’s velocity during the spiral-in is assumed to be equal to the corresponding Keplerian value at all times: $v_2 = \sqrt{G M_1(r)/r}$, where $v_2$ is the velocity magnitude of the secondary, $G$ the gravitational constant, and $M_1(r)$ the mass of the primary enclosed within radial coordinate $r$.

5. Changes in the internal structure of the secondary are ignored during the merger event, and it is approximated as a point source. This removes the complication of considering effects such as tidal deformation of the secondary and tidal friction on the dynamical evolution of the merger. For more details on these effects, three-dimensional hydrodynamic simulations are necessary (Podsiadlowski et al. 1990; Ivanova 2002; Ivanova et al. 2002).

6. The effects of the merger on nucleosynthesis are ignored. The merger hypotheses discussed in this work imply the mixing of 1–4 $M_\odot$ of material from an MS secondary star in the hydrogen (H) envelope and the He core of the primary, potentially leading to distinct nucleosynthetic signatures. Following that distinct first dynamical phase of merger-induced mixing, in the longer term and depending on the convective and rotational mixing timescales in the envelope of the primary, it is possible to dredge-up enhanced nucleosynthetic products of the CNO process to the photosphere of the post-merger. In addition, the H fuel deposited from the secondary will increase the mass of the H-burning shell around the He core of the primary, resulting in higher luminosity, which may cause the primary envelope to expand to a larger radius. We aim to study the nucleosynthetic signatures of such merger events in a future study (see also Ivanova et al. 2002).

7. In general, we expect the secondary to enter the envelope of the primary at supersonic speeds, generating shocks in both the ambient medium and the secondary star’s atmosphere. A complex flow will be set up in which the shocked primary material and some of the secondary atmosphere will be mixed and entrained in the turbulent wake behind the secondary. Consequently, there will be an increase in the specific entropy of the perturbed layers, but the complexity of the flow prevents us from calculating this increase in detail. We adopt an
approximate approach that shows that the increase can be ignored. The change in specific entropy in a planar shock is given by

$$\Delta s = c_s [\ln \rho_2/\rho_1 - \gamma \ln (\rho_2/\rho_1)],$$  \hspace{1cm} (8)$$

where the suffixes 1 and 2 indicate pre- and post-shock values, respectively. The pressure and density ratios can be calculated given the pre-shock Mach number and the adiabatic index $\gamma$ (Landau & Lifshitz 1959). Consistent with our assumptions, we take the Mach number to be given by the ratio of the local Keplerian velocity to the local sound speed, and using values appropriate for the envelope of the primary, we can calculate the change in specific entropy. This turns out to be typically at the level of 1% compared to the local entropy of the primary throughout most of the star and only becomes comparable near the surface along the stellar equator. However, this entropy increase is limited to a toroidal region of cross section $\sim R_2^3$ in the wake of the secondary, whereas MESA, being a 1D stellar evolution code, expects the entropy increase to be distributed in a shell of radius $r$, and thus the entropy increase due to the inspiral is small compared to the ambient entropy of the primary everywhere. In conclusion, we take the post-merger entropy profile of the primary to be, in good approximation, the same as the entropy profile right before the merger.

Given those simplifying assumptions, our approach aims to be a simple proof-of-principle effort to illustrate the potential of merger events to affect the rotational properties of massive stars past the MS and an effort to reproduce the observed properties of Betelgeuse under the assumption that it suffered such a merger.

3.3. Derivation of Post-merger Structure

In order to derive an expression for the perturbed internal distribution of specific AM in the primary star following a merger event with a smaller companion, we first consider the action of a torque that acts on the secondary upon entering the envelope of the primary. This torque originates due to dynamical friction (drag) and has the generic form

$$\tau(r) = -\frac{1}{2} c_D \pi R_2^2 \rho_1(r) v_2^2 r,$$  \hspace{1cm} (9)$$

where $c_D$ is the drag coefficient, $R_2$ the radius of the secondary, $\rho_1(r)$ the density profile of the primary at radial coordinate $r$, and $v_2$ the magnitude of the secondary’s velocity, which we are assuming to be equal to the Keplerian value at all times (see Section 3.2). The basic equation is then

$$M_2 \frac{d}{dt} GM_1(r)r = -\frac{1}{2} c_D \pi R_2^2 \rho_1(r) GM_1(r),$$  \hspace{1cm} (10)$$

where $M_2$ is the mass of the secondary. Numerical solutions of Equation (10), which is a simple ordinary differential equation, yield the evolution of the radial coordinate of the secondary, $r(t)$.

Over an infinitesimal radial displacement equal to $dr$, the AM of the primary, $J_1$, increases by an amount equal to that lost due to the spiral-in of the secondary, $J_2$ as follows:

$$\frac{dJ_1}{dr} = f \frac{1}{r} \frac{dJ_2}{dr}.$$  \hspace{1cm} (11)$$

The factor $f \leq 1$ is the fraction of the AM lost by the secondary that results in bulk rotation of the layers of the primary, the rest appearing as local vorticity and being eventually dissipated. Accordingly, the specific AM deposited in the primary is equal to

$$\dot{J}_{\text{spin}}(r) = \frac{dJ_1}{dr}/\frac{dM_1}{dr} = f \frac{dJ_2}{dM_1}.$$  \hspace{1cm} (12)$$

Taking $J_2 = M_2 \sqrt{GM_1(r)r}$, with $M_2$ constant, we obtain the deposited specific AM profile of the primary following the merger event for $R_{1,\text{He}} < r_2 < R_1$, where $R_{1,\text{He}}$, $r_2$, and $R_1$ are the radius of the He core of the primary, the radial distance of the secondary from the center of the primary and the radius of the primary, respectively,

$$\dot{J}_{\text{spin}}(r) = \frac{f q_r}{2} \sqrt{GM_1(r)r} \left(1 + \frac{d \ln r}{d \ln M_1} \right),$$  \hspace{1cm} (13)$$

where $dM_1/dr = 4\pi r^2 \rho(r)$. This expression shows that the AM per unit mass deposited is proportional to the specific AM of the Keplerian orbit of the secondary times a function that rises steeply toward the surface of the primary. This can be seen clearly by considering an alternative expression for the logarithmic derivative above in terms of the ratio between the average density of the primary inside radius $r$ and the local density at that radius ($d \ln r/d \ln M = \rho(r)/\rho_1(r)$). We assume that the secondary completely dissolves when $r \approx R_{1,\text{He}}$ due to strong tidal forces, so that $\dot{J}_{\text{spin}}(r) = 0$ for $r < R_{1,\text{He}}$. If $J_1(r)$ is the original, unperturbed specific AM profile of the primary then, following the merger event, the final perturbed profile will be

$$\hat{J}_1(r) = J_1(r) + \dot{J}_{\text{spin}}(r).$$  \hspace{1cm} (14)$$

3.4. 3D Simulation of the $R_I = 12 R_\odot$ Merger Case

In order to numerically evaluate the properties of an early Case B merger and derive a better measure of the inspiral time (Section 3.1), we run a 3D merger simulation for a 16 $M_\odot + 1 M_\odot$ system with the parallelized adaptive mesh refinement code OctoTiger (Motl et al. 2007; Kadam et al. 2016). Due to computational limitations, we were only able to properly resolve the $R_I = 12 R_\odot$ case in 3D. At this phase, the primary is just past its TAMS with no H burning taking place in the core, and it is starting its Hertzsprung gap–crossing phase. For the larger primary radius choices (100, 300, 500 $R_\odot$), the density contrast between the secondary and the envelope of the primary would be such that it would require a large degree of mesh refinement and a prohibitive number of computing cells. We argue, however, that the final phase of this simulation corresponding to the plunge of the secondary into the central regions of the primary, eventually leading to its tidal disruption, will not be significantly different for the other cases.

To initialize the 3D Cartesian grid of OctoTiger, we first compute the structures of both the $16 M_\odot$ at $12 R_\odot$ and the $1 M_\odot$ components using variations of the publicly available 15M_dynamo and 1M_pre_ms_to_wd MESA test suite.
problems accordingly. Our MESA input inlist files for these runs and all of our merger models will be made publicly available at the MESA marketplace\footnote{www.mesastar.org} website. We then fit the structure of each of the components of the binary system with bipolytropic functions as required for the initialization method used in OctoTiger (Kadam et al. 2016). For the 16 $M_\odot$ primary during the phase when its radius is 12 $R_\odot$, the bipolytropic indices were found to be 3.2 for the core and 3.1 for the envelope. For the 1 $M_\odot$ secondary, accordingly, the best-fit bipolytropic indices were 3.0 and 1.5 for the core and the envelope, respectively. Upon mapping to OctoTiger the dynamical merger was driven by increasing the entropy of the primary’s envelope (Kadam et al. 2016). Within $\sim$175 orbits, the secondary came into contact with the primary and subsequently experienced an inspiral toward the He core of the primary until it got tidally disrupted. This latter phase lasted $\sim$5 days and is in excellent agreement with the simple analytical estimate for the inspiral timescale that we provided in Section 3.1. Figure 2 shows a face-on view of the initial binary arrangement (left panel) and the final phase of secondary tidal disruption (right panel) as simulated in OctoTiger.

### 4. Stellar Evolution Calculations

#### 4.1. Post-merger Structure Relaxation with MESA

To quantitatively evaluate the physical properties and long-term evolution of post-merger objects produced by the binary progenitor systems discussed in Section 3, we use the open-source stellar evolution code MESA version 10108. More specifically, we take advantage of the new model relaxation feature described in Appendix B of Paxton et al. (2018) that allows the user to import the entropy (or, alternatively, the density/temperature, density/internal energy, or pressure/temperature) profile, and the specific AM and composition profile of a 1D model into MESA, regardless of whether it was calculated in an external code or MESA itself. The original model profiles are then gradually numerically “relaxed” to the input entropy, AM, and composition profiles in MESA with the goal to achieve hydrostatic equilibrium computed with an equation of state (EOS) that is consistent with the one used in the code. Subsequently, the “relaxed” models can be evolved for long, stellar evolution timescales with all physics modules turned on.

In our analysis, we start by computing the single evolution of massive primaries with the following properties during ZAMS: $M_2 = 15$, 20 $M_\odot$, and initial equatorial rotational velocity $v_{1,rot,i} = 0, 200, 300, 500$ km s$^{-1}$, therefore accounting for both nonrotating and rapidly rotating pre-merger primary stars. For all models, we are using the Ledoux criterion for convection with the mixing-length theory (MLT) coefficient $\alpha_{MLT} = 1.5$. Semiconvective and thermohaline mixing with fiducial coefficients of $\alpha_{semi} = 0.04$ and $\alpha_{th} = 1.0$, respectively, are included (Kippenhahn et al. 1980). We also use the 21 isotope “approx21.net” nuclear reaction network (Timmes et al. 2000) and the “Helmholtz” EOS (Timmes & Swesty 2000). For the rotating models, AM diffusion and rotationally induced mixing are computed by using the supplied prescriptions (Heger et al. 2005) including the effects of magnetic fields due to Spruit–Taylor (ST) dynamo action (Spruit 2002). For each rotational instability (such as meridional (Eddington–Sweet) circulation, dynamical shear instability, secular shear instability, Goldreich–Hoiland instability, Goldreich–Schubert–Fricke instability and Spruit–Taylor (“ST” dynamo)), a viscosity and a diffusion coefficient are adopted based on standard assumptions for massive stars (Heger et al. 2000, 2003; Spruit 2002). MESA allows the user to set the efficiency of each mechanism (which we take to be 1.0) separately and then computes each contribution to the total viscosity and diffusion coefficient independently as described in Heger et al. (2000, 2005). These coefficients are then used to calculate the total viscosity and diffusion coefficients that determine the efficiency of AM mixing in different regions of the stars by solving the AM diffusion equation in 1D spherical coordinates. We note that these AM mixing processes were adopted for all of our rotating models (both the single rotating models and the rotating post-merger models). As a consequence,
Table 1
Properties of the MESA Models Considered in This Work

| Model          | \( M_{\odot} \) | \( M_{\odot} \) | \( v_{\text{rot},0} \) (km s\(^{-1}\)) | \( R_{\odot} \) | \( \log T_{\text{eff},0} \) (K) | \( \log L_{\odot}/L_{\odot} \) | \( v_{\text{rot},0} \) (km s\(^{-1}\)) | \( \Delta t_{\text{target}} \) (yr) |
|----------------|-----------------|-----------------|----------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Single star evolution |
| S15r0          | 15              | ...             | 0                                | ...             | 3.50            | 5.02            | 0.0             | 0.0             |
| S15r200        | 15              | ...             | 200                              | ...             | 3.49            | 5.04            | 0.15            | 35.0            |
| S15r200h\(^b\) | 15              | ...             | 200                              | ...             | 3.50            | 5.02            | 0.18            | 0.0             |
| S15r300        | 15              | ...             | 300                              | ...             | 3.49            | 5.03            | 0.18            | 66.7            |
| S15r500        | 15              | ...             | 500                              | ...             | 4.51            | 5.62            | 436.23          | 0.0             |
| S20r0          | 20              | ...             | 0                                | ...             | 3.49            | 5.30            | 0.0             | 0.0             |
| S20r0b\(^b\)   | 20              | ...             | 0                                | ...             | 3.49            | 5.19            | 0.0             | 0.0             |
| S20r200        | 20              | ...             | 200                              | ...             | 3.49            | 5.32            | 0.06            | 0.0             |
| Binary merger, \( q = 0.07 \) |
| M15r0c200      | 15              | 1               | 0                                | 200             | 3.50            | 5.04            | 5.00            | \( 8.3 \times 10^4 \) |
| M15r0c300      | 15              | 1               | 0                                | 300             | 3.50            | 5.03            | 5.98            | \( 2.6 \times 10^5 \) |
| M15r0c700      | 15              | 1               | 0                                | 700             | 3.48            | 5.03            | 20.40           | \( 1.7 \times 10^5 \) |
| M15r200c200    | 15              | 1               | 200                              | 200             | 3.50            | 5.04            | 4.66            | \( 1.5 \times 10^4 \) |
| M15r200c300    | 15              | 1               | 200                              | 300             | 3.50            | 5.04            | 5.59            | \( 1.6 \times 10^4 \) |
| M15r200c700    | 15              | 1               | 200                              | 700             | 3.48            | 5.04            | 19.95           | \( 1.2 \times 10^4 \) |
| Binary merger, \( q = 0.18 \) |
| M17r0c200      | 17              | 3               | 0                                | 200             | 3.50            | 5.24            | 6.83            | \( 5.0 \times 10^5 \) |
| M17r0c250      | 17              | 3               | 0                                | 250             | 3.50            | 5.24            | 6.81            | \( 5.1 \times 10^5 \) |
| M17r0c300      | 17              | 3               | 0                                | 300             | 3.50            | 5.24            | 7.49            | \( 5.3 \times 10^5 \) |
| M17r0c200c200  | 17              | 3               | 200                              | 200             | 3.50            | 5.24            | 6.82            | \( 5.0 \times 10^5 \) |
| M17r0c250c200  | 17              | 3               | 200                              | 250             | 3.50            | 5.24            | 6.79            | \( 5.1 \times 10^5 \) |
| M17r0c300c200  | 17              | 3               | 300                              | 300             | 3.50            | 5.23            | 7.48            | \( 5.3 \times 10^5 \) |
| M17r200c200    | 17              | 3               | 200                              | 200             | 3.50            | 5.29            | 4.35            | \( 6.9 \times 10^5 \) |
| M17r200c250    | 17              | 3               | 200                              | 250             | 3.50            | 5.30            | 6.18            | \( 6.9 \times 10^5 \) |
| M17r0c300      | 17              | 3               | 300                              | 300             | 3.50            | 5.31            | 8.94            | \( 6.8 \times 10^5 \) |
| Binary merger, \( q = 0.25 \) |
| M16r0c200      | 16              | 4               | 0                                | 200             | 3.50            | 5.22            | 9.10            | \( 8.0 \times 10^5 \) |
| M16r0c250      | 16              | 4               | 0                                | 250             | 3.50            | 5.21            | 10.90           | \( 7.8 \times 10^5 \) |
| M16r0c300      | 16              | 4               | 0                                | 300             | 3.50            | 5.20            | 12.05           | \( 7.6 \times 10^5 \) |
| M16r200c200    | 16              | 4               | 200                              | 200             | 3.50            | 5.28            | 4.50            | \( 7.1 \times 10^5 \) |
| M16r200c250    | 16              | 4               | 200                              | 250             | 3.50            | 5.27            | 6.17            | \( 7.2 \times 10^5 \) |
| M16r200c300    | 16              | 4               | 200                              | 300             | 3.50            | 5.25            | 8.94            | \( 7.0 \times 10^5 \) |

Notes.

\(^a\) This model was run without the effects of magnetic fields on AM transport and chemical mixing turned on.

\(^b\) This model was run with enhanced mass loss during the MS and PMS phases (by selecting a higher mass-loss coefficient for the Vink and Reimers prescriptions used).

our results on the evolution of rotation in these models may be dependent on how efficient AM mixing is in massive stars, which is an actively debated topic involving several poorly constrained parameters. Alternative AM mixing processes (see, for example, Fuller et al. 2014) may therefore impact our results. Steady-state radiatively driven mass loss is also computed following Vink et al. (2001). Temperature-dependent mass loss during the RSG phase is based on the “de Jager” prescriptions (de Jager et al. 1988). We also run a subset of models for the \( q = 0.18 \) case \((M_{\odot} = 17 M_{\odot})\) using the “van Loon” formula (van Loon et al. 2005), suggesting stronger winds during the RSG phase (Smith 2014) in order to investigate the effect of mass loss on the final surface rotation rate.

We computed two sets of models: the “Single (S)” and the “Merged (M)” group. The “S” models refer to the evolution of massive, rotating or nonrotating single stars that do not suffer a merger. We run a set of “S” models in order to calculate the evolution of the surface equatorial rotational velocity of massive stars and determine their rotation rates after the end of their MS lifetimes, during the supergiant phases of their evolution. This is equivalent to the work done by Wheeler et al. (2017) with the purpose of determining how long single massive supergiant stars rotate with speeds consistent with those reported for Betelgeuse. The “M” group of models is essentially a subsample of the “S” group but with the key difference that we stop the single evolution part of the computation during the “Hertzsprung gap—crossing phase” while the primary is expanding toward the supergiant branch after the end of the MS. It is during that phase that we assume the first contact with the secondary occurs, triggering the merger process. In our analysis, we consider different values for the initial contact radius for primary radii \( R_1 = 200, 250, 300, \) or 700 \( R_{\odot} \). Hereafter we adopt the notations \((X)(Y)r(Z)c(V)\), where \( X = S, M \) for the “Single” or the “Merged” case, \( Y = M_{\odot} \) in solar masses, \( Z = v_{\text{rot},0} \) (ZAMS surface equatorial rotation rate) in km s\(^{-1}\), and \( V = R_1 \) in \( R_{\odot} \).
Details for each models are given extensively in Table 1. As an example, model “M17r200c300” corresponds to an $M_1 = 17 \, M_\odot$ primary rotating at 200 km s$^{-1}$ during ZAMS that suffered a merger with a 4 $M_\odot$ secondary after the end of the MS and at a radius of $R_1 = 300 \, R_\odot$. We also run a model where we ignore the effects of AM transfer due to magnetic fields (model “S15r200b”) and a model with enhanced mass-loss rate during the MS (model “S20r0b,” where we set the mass-loss efficiency coefficients ($\eta_{\text{ML}}$) to five times higher than the default value of 1.0) to investigate the corresponding effects on the evolution of the surface rotation rate.

To compute the post-merger evolution of the “M” set of models, we adjust their specific AM profiles for different choices of contact radii $R_1$, according to Equations (13) and (14), by using the MESA model relaxation feature. In addition, following the arguments discussed in Section 3.2, we assume that the post-merger composition and entropy profiles remain unaffected. Figure 3 shows the pre- and post-merger internal distributions of the specific AM, angular velocity, density, and temperature for the “M15r200c200” models. It can be seen that the envelope of the primary experiences a significant spin-up due to the spiral-in of the 1 $M_\odot$ companion star. Depending on the specifics of redistribution of AM due to diffusive processes and convection in the envelope of the primary, this high rotation rate may persist for long timescales and up to the supergiant stage of the post-merger evolution. We investigate this in the following paragraph.

### 4.2. Post-merger Evolution with MESA

The long-term evolution of both the “S” and “M” class of models is followed up to the supergiant, core He-burning phases providing us with “Hertzsprung–Russell” (H-R) tracks and predictions about the evolution of surface equatorial rotational velocity that can be directly compared against observations of rapidly rotating supergiant stars and, more specifically, Betelgeuse.

Betelgeuse has been discussed as a candidate of a supergiant star that has recently suffered a merger event with a smaller companion (Wheeler et al. 2017; Nance et al. 2018). We adopt the observational results of Dolan et al. (2016), indicating $L/L_\odot = 1.3^{+0.7}_{-0.5} \times 10^5$, $R/R_\odot = 887 \pm 203$, and $T_{\text{eff}} = 3500 \pm 200$ K, where the uncertainties in luminosity and radius are dominated by the uncertainty to the distance of Betelgeuse, $d = 197 \pm 45$ pc (Harper et al. 2008, 2017). In addition, Gilliland & Dupree (1996), Uitenbroek et al. (1998), and Kervella et al. (2018) report surface rotational velocities in the range $\sim 5$–15 km s$^{-1}$.

### 5. Results

Table 1 details the properties of the models studied in this work. $\log(L_0/L_\odot)$, $\log T_{\text{eff},0}$, and $v_{\text{rot},0}$ correspond to the values of the luminosity (in solar units), effective temperature, and surface equatorial rotational velocity of each model during the supergiant phase, respectively. $\Delta T_{\text{target}}$ denotes the time (in years) that each model spends within the range of target observed values for Betelgeuse ($5$–15 km s$^{-1}$). Figure 4 shows the H-R tracks of the “S” models and Figures 5–7 the H-R tracks of the $M_{\odot}$ and “M” models, respectively, including a color scale that denotes the surface equatorial velocity at different stages in units of km s$^{-1}$. The small gaps in data between the pre-merger and the post-merger evolution in the H-R plots correspond to the first few steps of numerical relaxation that we omitted from the plot. The post-merger evolution is therefore plotted starting at the first dynamically stable, relaxed state of the post-merger object. Figure 8 shows the evolution of the surface equatorial rotational velocity for rotating “S” models and all “M” models after merger.

All the “S” models evolve to an RSG phase within $\sim 10$–13 million years with the exception of the most rapidly rotating...
model “S15r500” that evolves to a BSG that is inconsistent with the observations of Betelgeuse, and as such, we exclude it from further discussion. The luminosity and effective temperatures of the “S” models that evolve to the RSG phase are well within the error bars of those of Betelgeuse. However, after the end of the MS and during their thermal expansion toward the supergiant phase, AM conservation leads to a significant spin-down and surface rotation velocities \( \sim 0.2 \text{ km s}^{-1} \) for the rotating 15 \( M_\odot \) “S” models and \( \sim 0.06 \text{ km s}^{-1} \) for the rotating 20 \( M_\odot \) model, respectively. The exclusion of the effects of AM transport due to magnetic fields (model “S15r200b”) and enhanced MS steady-state mass-loss rates (model “S20r0b”) do not significantly affect the predictions for \( \log (L_0/L_\odot) \), \( \log T_{\text{eff,0}} \), and \( v_{\text{rot,0}} \). During the ascent toward higher luminosities and the supergiant phase, the surface equatorial rotational velocity gradually declines for all “S” models due to the envelope expansion but only spends a very short amount of time (~a few to tens of years in some cases) within the target 5–15 \text{ km s}^{-1} range. That is consistent with the findings of Wheeler et al. (2017; see their Figure 7 for more information).
This result indicates that models of single stellar evolution with rapid rotation at the ZAMS do not accurately predict the observed characteristics of Betelgeuse.

All of the models in the “M” subset evolve toward the observed 3σ luminosity and effective temperature for Betelgeuse during their post-merger evolution. In Figures 5–7, the color scale corresponds to the magnitude of surface equatorial rotational velocity values at different evolutionary stages. In the top two and the left middle panels, square symbols denote the models run with the “van Loon” formula for RSG mass loss. The middle-left panel also shows the (artificial) H-R evolution during the numerical MESA “merger” procedure. Similar effects during that stellar engineering phase are seen in Menon et al. (2019) (i.e., their Figure 4).

6. Discussion

In this paper, we study the evolution—including the AM evolution—of low-mass-ratio mergers (0.07 < q < 0.25), where a massive primary star engulfs its smaller (M₂ ~ 1–4 Mₑ) companion during their thermal expansion phase after the end of the MS. We devise the initial conditions for the binary progenitor system and an approximate, analytical model that characterizes the deposition of AM in the envelope of a massive primary during the spiraling in of the secondary and up to the point when the secondary becomes tidally disrupted around the He core of the primary. We then calculate the perturbed, post-merger specific AM distribution and use it to simulate the post-merger evolution with the stellar evolution code MESA. We consider two sets of models, one where we calculated the evolution of single, rapidly rotating stars (the “S”
Figure 7. Evolution of the nonrotating and rotating merger ("M") models in the H-R diagram for ZAMS primary and secondary masses of 16 \( M_\odot \) and 4 \( M_\odot \) accordingly (\( q = 0.25 \); left panel). The 3\( \sigma \) observed location of Betelgeuse is also marked for comparison. The color bar shows the corresponding surface equatorial rotational velocity values at different evolutionary stages.

Figure 8. Evolution of surface equatorial rotational velocity (\( v_{\text{rot, s}} \)) for 15, 20 \( M_\odot \) single evolution (upper-left panel) and post-merger evolution for primary stars with the following properties: \( M_1 = 15 \ M_\odot \), \( M_2 = 1 \ M_\odot \) (\( q = 0.07 \); upper-right panel), \( M_1 = 17 \ M_\odot \), \( M_2 = 3 \ M_\odot \) (\( q = 0.18 \); lower-left panel), and \( M_1 = 16 \ M_\odot \), \( M_2 = 4 \ M_\odot \) (\( q = 0.25 \); lower-right panel). Solid lines correspond to the initially nonrotating primaries and dashed lines to the initially rotating primaries with \( v_{\text{rot,i}} = 200 \) km s\(^{-1}\). The horizontal dashed lines denote the 5–15 km s\(^{-1}\) range, and the vertical dashed lines correspond to the times when the models are within the 3\( \sigma \) error bars of the observed luminosity and effective temperature for Betelgeuse. See Table 1 for details about the model properties.
group) and another where massive stars suffer a merger event in order to predict the evolution of surface equatorial rotational velocity toward the supergiant phase (the “M” group), and compare our results with the observations of the star Betelgeuse.

Our analysis indicates that low-mass-ratio \( q = M_2/M_1 = 0.07–0.25 \) mergers initiated during the PMS evolution of a primary with mass \( 15–17 M_\odot \) and when the primary reaches a radius of \( \sim 200–300 R_\odot \), evolve to RSG stars that are rapid rotators for up to \( \sim 200,000 \) yr, in good agreement with the observations of Betelgeuse. In Section 2, we considered also the possibility that Betelgeuse might have been spun-up by accretion and then released in an SN explosion of its companion. A survey of existing population synthesis and binary stellar evolution calculations shows that there is no clear and compelling path to the desired result, because the outcomes are extremely sensitive to initial conditions and model assumptions. On the other hand, we are unable at this point to rule out the accretion option for Betelgeuse. This may require further investigation in a future paper. In any case, a two-step process may be required to obtain both the observed runaway velocity and the high equatorial rotational velocity of Betelgeuse: (a) the dynamical ejection of a binary from Betelgeuse’s birth cluster as the origin of its observed space velocity (with binary parameters that allow the system to survive the ejection) and (b) the subsequent merger- or accretion-induced spin-up followed by an SN explosion.

We have also established via binary system energetics arguments and references to relevant past \( N \)-body simulation studies that young dense stellar clusters can successfully eject intact runaway binary systems (with ejection velocities \( >30 \text{ km s}^{-1} \)) with properties that allow the primary to obtain a noncanonical, rapid surface equatorial velocity following an early Case B merger that occurs after its TAMS and during its Hertzsprung gap–crossing phase. Furthermore, we have estimated that such “quiet” mergers will not lead to significant rejuvenation of the primary and the formation of a BSG star akin to the progenitor of SN 1987A, but will likely yield rapidly rotating RSGs instead as the secondary will not penetrate deep into the core of the primary but be deposited on the H-burning shell.

It should be emphasized that some of our results may depend on the details of AM transport in the post-merger object and the mechanisms of AM mixing that are available in the MESA code via 1D parameterized prescriptions, where we adopt standard values pertaining to massive stars (Heger et al. 2003, 2005; Ekström et al. 2012). Our results can be explored for other mechanisms of internal AM not included in this work (see, for example, Fuller et al. 2014), but that is beyond the scope of this paper.

These results indicate that stellar mergers, a natural by-product of stellar duplicity, is a prevalent feature in the universe (Sana et al. 2012; de Mink et al. 2014), a reasonable formation channel for rapidly rotating giant and supergiant stars (Tayar et al. 2015), and a mechanism that affects both the details of stellar evolution and also the properties of circumstellar environments. Even though our approach was approximate and utilized many simplifying assumptions, this work serves as a proof of principle that certain merger scenarios can reproduce observations of a subset of giant and supergiant stars, and potentially other categories of stars that are generally considered “outliers.”

In the near future, we aim to perform realistic, 3D simulations of dynamical mergers with the same initial properties as the ones discussed in this work with the aim to more accurately assess the efficiency of AM deposition but also better quantify the mechanically driven mass loss that may lead to the formation of circumstellar mass outflows. We also aim to more carefully investigate the effect of these merger processes on nucleosynthesis and the potential to detect relevant signatures in the spectra of candidate stars. These calculations will allow us to obtain a better model for the structure of the post-merger objects that can then be spherically averaged and evolved with MESA with the aim to further constrain the long-term effects of binary coalescence in massive stellar evolution.

We would like to thank J. Craig Wheeler, Pavel Kroupa, and Pablo Marchant for useful discussions and comments. We would also like to thank our referee for the very constructive criticism provided that helped us improve the quality of our paper. We wish to acknowledge the support from the National Science Foundation through CREATIV grant AST-1240655. E.C. would like to thank the National Science Foundation for its support through award number AST-1907617 and the Louisiana State University College of Science and the Department of Physics & Astronomy for their support.

Software: MESA (Paxton et al. 2015) Matplotlib (Hunter 2007).

References

Bally, J. 2008, in Handbook of Star Forming Regions, Volume I: The Northern Sky ASP Monograph Publications, Vol. 4, ed. B. Reipurth (San Francisco, CA: ASP), 459
Blaauw, A. 1961, BAN, 15, 265
Blaauw, A. 1964, ARA&A, 2, 213
Briceño, C., Calvet, N., Hernández, J., et al. 2005, AJ, 129, 907
Brott, I., de Mink, S. E., Cantiello, M., et al. 2011a, A&A, 530, A115
Brott, I., Evans, C. J., Hunter, I., et al. 2011b, A&A, 530, A116
Brown, A. G. A., de Geus, E. J., & de Zeeuw, P. T. 1994, A&A, 289, 101
Ceillier, T., Tayar, J., Mathur, S., et al. 2017, A&A, 605, A111
Claret, A., & Gimenez, A. 1989, A&AS, 81, 37
Costa, A. D., Canto Martins, B. L., Bravo, J. P., et al. 2015, ApJL, 807, L21
Dunstall, P. R., Dufton, P. L., Langer, N., et al. 2015, A&A, 580, A93
Eggleton, P. P. 1983, ApJ, 268, 368
Ekström, S., Georgy, C., Eggenberger, P., et al. 2012, A&A, 537, A146
Ekström, S., Meynet, G., Chiappini, C., Hirschi, R., & Maeder, A. 2008, A&A, 489, 685
Ferrario, L., Pringle, J. E., Tout, C. A., & Wickramasinghe, D. T. 2009, MNRAS, 400, L71
Fuller, J., Lecoanet, D., Cantiello, M., & Schneider, F. R. N. 2014, ApJ, 782, 7
Dufton, P. L., Dunstall, P. R., Evans, C. J., et al. 2011, ApJL, 743, L22
Dufton, P. L., Langer, N., Dunstall, P. R., et al. 2013, A&A, 550, A109
Dunstall, P. R., Dufton, P. L., Sana, H., et al. 2015, A&A, 580, A93
Eggleton, P. P. 1983, ApJ, 268, 368
Ekström, S., Georgy, C., Eggenberger, P., et al. 2012, A&A, 537, A146
Ekström, S., Meynet, G., Chiappini, C., Hirschi, R., & Maeder, A. 2008, A&A, 489, 685
Ferrario, L., Pringle, J. E., Tout, C. A., & Wickramasinghe, D. T. 2009, MNRAS, 400, L71
Fuller, J., Lecoanet, D., Cantiello, M., & Brown, B. 2014, ApJ, 796, 17
Gies, D. R., & Bolton, C. T. 1986, ApJS, 61, 419
Gilliland, R. L., & Dupree, A. K. 1996, ApJL, 463, L29
Granvoula, H. H., Wade, G. A., Sundqvist, J. O., et al. 2012, MNRAS, 426, 2208

Chatzopoulos et al. 2020 June 10

The Astrophysical Journal, 896:50 (15pp)
