ABSTRACT

Click-through rate (CTR) prediction is an essential task in web applications such as online advertising and recommender systems, whose features are usually in multi-field form. The key of this task is to model feature interactions among different feature fields. Recently proposed deep learning based models follow a general paradigm: raw sparse input multi-fielded features are first mapped into dense field embedding vectors, and then simply concatenated together to feed into deep neural networks (DNN) or other specifically designed networks to learn high-order feature interactions. However, the simple unstructured combination of feature fields will inevitably limit the capability to model sophisticated interactions among different fields in a sufficiently flexible and explicit fashion.

In this work, we propose to represent the multi-field features in a graph structure intuitively, where each node corresponds to a feature field and different fields can interact through edges. The task of modeling feature interactions can be thus converted to modeling node interactions on the corresponding graph. To this end, we design a novel model Feature Interaction Graph Neural Networks (Fi-GNN). Taking advantage of the strong representative power of graphs, our proposed model can not only model sophisticated feature interactions in a flexible and explicit fashion, but also provide good model explanations for CTR prediction. Experimental results on two real-world datasets show its superiority over the state-of-the-arts.

The first two authors Zekun Li and Zeyu Cui contribute to this work equally. Shu Wu and Xiaoyu Zhang are both corresponding authors.

CCS CONCEPTS

- Information systems → Recommender systems; Business intelligence; - Applied computing → Online shopping.

KEYWORDS

Feature interactions, Graph neural networks, CTR prediction, Recommender system

1 INTRODUCTION

The goal of click-through rate prediction is to predict the probabilities of users clicking ads or items, which is critical to many web applications such as online advertising and recommender systems. Modeling sophisticated feature interactions plays a central role in the success of CTR prediction. Distinct from continuous features which can be naturally found in images and audios, the features for web applications are mostly in multi-field categorical form. For example, the four-fields categorical features for movies may be: (1) Language = [English, Chinese, Japanese, ...], (2) Genre = [action, fiction, ...], (3) Director = [Ang Lee, Christopher Nolan, ...], and (4) Starring = [Bruce Lee, Leonardo DiCaprio, ...] (noted that there are much more feature fields in real applications). These multi-field categorical features are usually converted to sparse one-hot encoding vectors, and then embedded to dense real-value vectors, which can be used to model feature interactions.

Factorization machine (FM) [23] is a well-known model proposed to learn second-order feature interactions from vector inner products. Field-aware factorization machine (FFM) [9] further considers the field information and introduces field-aware embedding. Regrettably, these FM-based models can only model second-order interaction and the linearity modeling limits its representative power. Recently, many deep learning based models have been proposed...
to learn high-order feature interactions, which follow a general paradigm: simply concatenate the field embedding vectors together and feed them into DNN or other specifically designed models to learn interactions. For example, Factorisation-machine supported Neural Networks (FNN) [34], Neural Factorization Machine (NFM) [8], Wide&Deep [2] and DeepFM [6] utilize DNN to model interactions. However, these models based on DNN learn high-order feature interactions in a bit-wise, implicit fashion, which lacks good model explanations. Some models try to learn high order interactions explicitly by introducing specifically designed networks. For example, Deep&Cross [30] introduces Cross Network (CrossNet) and xDeepFM [15] introduces Compressed Interaction Network (CIN). Nevertheless, we argue that they are still not sufficiently effective and explicit, since they still follow the general paradigm of combining feature fields together to model their interactions. The simple unstructured combination will inevitably limit the capability to model sophisticated interactions among different feature fields in a flexible and explicit fashion.

In this work, we take the structure of multi-field features into consideration. Specifically, we represent the multi-field features in a graph structure named feature graph. Intuitively, each node in the graph corresponds to a feature field and different fields can interact through edges. The task of modeling sophisticated interactions among feature fields can be thus converted to modeling node interactions on the feature graph. To this end, we design a novel model Feature Interaction Graph Neural Networks (Fi-GNN) based on Graph Neural Networks (GNN), which is able to model sophisticated node (feature) interactions in a flexible and explicit fashion. In Fi-GNN, the nodes will interact by communicating the node states with neighbors and update themselves in a recurrent fashion. At every time step, the model interact with neighbors at one hop deeper. Therefore, the number of interaction steps equals to the order of feature interactions. Moreover, the edge weights reflecting importances of different feature interactions and node weights reflecting importances of each feature field on the final CTR prediction can be learnt by Fi-GNN, which can provide good explanations. Overall, our proposed model can model sophisticated feature interactions in an explicit, flexible fashion and also provide good model explanations.

Our contributions can be summarized in threefold:

- We point out the limitation of the existing works which consider multi-field features as an unstructured combination of feature fields. To this end, we propose to represent the multi-field features in a graph structure for the first time.
- We design a novel model Feature Interaction Graph Neural Networks (Fi-GNN) to model sophisticated interactions among feature fields on the graph-structured features in a more flexible and explicit fashion.
- Extensive experiments on two real-world datasets show that our proposed method can not only outperform the state-of-the-arts but also provide good model explanations.

The rest of this paper is organized as follows. Section 2 summarizes the related work. Section 3 provides an elaborate description of our proposed method. The extensive experiments and detailed analysis are presented in Section 4, followed by the conclusion in Section 5.

2 RELATED WORK

In this section, we briefly review the existing models that model feature interactions for CTR prediction and graph neural networks.

2.1 Feature Interaction in CTR Prediction

Modeling feature interactions is the key to success of CTR prediction and therefore extensively studied in the literature. LR is a linear approach, which can only models the first-order interaction on the linear combination of raw individual features. FM [23] learns second-order feature interactions from vector inner products. Afterwards, different variants of FM have been proposed. Field-aware factorization machine (FFM) [9] considers the field information and introduces field-aware embedding. AFM [33] considers the weight of different second-order feature interactions. However, these approaches can only model second-order interaction which is not sufficient. With the success of DNN in various fields, researchers start to use it to learn high-order feature interactions due to its deeper structures and nonlinear activation functions. The general paradigm is to concatenate the field embedding vectors together and feed them into DNN to learn the high-order feature interactions. [16] utilizes convolutional networks to model feature interactions. Factorisation-machine supported Neural Networks (FNNs) [34] uses the pre-trained factorization machines for field embedding before applying DNN. Product-based Neural Network (PNN) [21] models both second-order and high-order interactions by introducing a product layer between field embedding layer and DNN layer. Similarly, Neural Factorization Machine (NFM) [8] has a Bi-Interaction Pooling layer between embedding layer and DNN layer to model second-order interactions, but the followed operation is summation instead of concatenation as in PNN. Some works on another line try to model the second-order and high-order interactions jointly via a hybrid architectures. The Wide&Deep [2] and DeepFM [6] contain a wide part to model the low-order interaction and a deep part to model the high-order interaction. However, all these approaches leveraging DNN learn the high-order feature interactions in an implicit, bit-wise way and therefore lack good model explainability. Recently, some work try to learn feature interactions in an explicit fashion via specifically designed networks. Deep&Cross [30] introduces a CrossNet which takes outer product of features at the bit level. On the contrary, xDeepFM [15] introduces a CIN to take outer product at the vector level. Nevertheless, they still don’t solve the most fundamental problem, that is to concatenate the field embedding vectors together. The simple unstructured combination of feature fields will inevitably limit the capability to model sophisticated interactions among different fields in a flexible and explicit fashion. To this end, we proposed to represent the multi-field features in a graph structure, where each node represents a field and different feature fields can interact through the edges. Accordingly, we can model the flexible interactions among different feature fields on the graphs.

2.2 Graph Neural Networks

Graph is a kind of data structure which models a set of objects (nodes) and their relationships (edges). Recently, researches of analyzing graphs with machine learning have been receiving more
and more attention because of the great representative power of graphs. Early works usually convert graph-structured data into sequence-structured data to deal with. Inspired by word2vec [18], the work [19] proposed an unsupervised DeepWalk algorithm to learn node embedding in graph based on random walks. After that, [27] proposed a network embedding algorithm LINE, which preserve the first- and second-order structural information. [5] proposed node2vec which introduces a biased random walk. However, these methods can be computationally expensive and non-optimal for large graphs.

Graph neural networks (GNN) are designed to tackle these problems, which are deep learning based methods that operate on the graph domain. The concept of GNN is first proposed by [24]. Generally, nodes in GNNs interact with neighbors by aggregating information from neighborhoods and updating their hidden states. There have been many variants of GNN with various kinds of aggregators and updaters proposed these days. Here we only present some representative and classical methods. Gated Graph Neural Networks (GGNN) [12] uses GRU [3] as updater. Graph Convolutional Networks (GCN) [10] considers the spectral structure of graphs and utilizes the convolutional aggregator. GraphSAGE [7] considers the spatial information. It introduces three kinds of aggregators: mean aggregator, LSTM aggregator and Pooling aggregator. Graph attention network (GAT) [29] incorporates the attention mechanism into the propagation step. There are some surveys [32, 35] which provide more elaborate introduction of various kinds of GNN models.

Due to convincing performance and high interpretability, GNN has been a widely applied graph analysis method. Recently, there are many application of GNN like neural machine translation [1], semantic segmentation [20], image classification [17], situation recognition [11], recommendation [31], script event prediction [14], fashion analysis [4, 13]. GNN is suitable for modeling node interactions on graph-structured features intrinsically. In this work, we proposed a model Fi-GNN based on GGNN to model feature interactions on the graph-structured features for CTR prediction.

3 OUR PROPOSED METHOD
We first formulate the problem and then introduce the overview of our proposed method, followed by the elaborate detail of each component.

3.1 Problem Formulation
Suppose the training dataset consists of $m$-fields categorical features ($m$ is the number of feature fields) and the associated labels $y \in \{0, 1\}$ which indicate user click behaviors. The task of CTR prediction is to predict $\hat{y}$ for the input $m$-fields features, which estimates the probability of a user clicking. The key of the task is to model the sophisticated interactions among different feature fields.

3.2 Overview
Figure 1 is the overview of our proposed method ($m=4$). The input sparse $m$-field feature vector is first mapped into sparse one-hot embedding vectors and then embedded to dense field embedding vectors via the embedding layer. The field embedding vectors are then represented as a feature graph, where each node corresponds to a feature field and different feature fields can interact through edges. The task of modeling interaction can be thus converted to modeling node interactions on the feature graph. Therefore, the feature graph is feed into our proposed Fi-GNN to model node interactions. An attention layer is applied on the output of Fi-GNN to estimate the click-through rate $\hat{y}$. In the following, we will introduce the details of our proposed method.

3.3 Embedding Layer
The multi-field categorical feature $x$ is usually sparse and of huge dimension. Following previous works [6, 21, 22, 30, 34], we represent each field as a one-hot encoding vector and then embed it to a dense vector, noted as field embedding vector. Let us consider the example in Section 1, a movie {Language: English, Genre: fiction, Director: Christopher Nolan, Starring: Leonardo DiCaprio} is first transformed into a high-dimensional sparse features via one-hot encoding:

$$[1, 0, ..., 0], [0, 1, ..., 0], [0, 1, ..., 0], [0, 1, ..., 0]$$

A field-aware embedding layer is then applied upon the one-hot vectors to embed them to low dimensional, dense real-value field embedding vectors as shown in Figure 2. Likewise, the field embedding vectors of $m$-field feature can be obtained:

$$E = [e_1, e_2, e_3, ..., e_m],$$

where $e_i \in \mathbb{R}^D$ denotes the embedding vector of field $i$ and $D$ denotes the dimension of field embedding vectors.

3.4 Feature Graph
Distinguished from the previous works which simply concatenate the field embedding vectors together and feed them into designed models to learn feature interactions, we represent them in a graph structure. In particular, We represent each input multi-field feature...
where a graph $G = (N, E)$, where each node $n_i \in N$ corresponds to a feature field $i$ and different fields can interact through the edges, so that $|N| = m$. Since each two fields ought to interact, it is a weighted fully connected graph while the edge weights reflect importances of different feature interactions. Accordingly, the task of modeling feature interactions can be converted to modeling node interactions on the feature graph.

### 3.5 Feature Interaction Graph Neural Network

Fi-GNN is designed to model node interactions on the feature graph, which is based on GGNN [12]. It is able to model the interactions in a flexible and explicit fashion.

#### Preliminaries

In Fi-GNN, each node $n_i$ is associated with a hidden state vector $h^i_n$ and the state of graph is composed of these node states

$$H^t = [h^1_n, h^2_n, h^3_n, ..., h^m_n],$$

where $t$ denotes the interaction step. As shown in Figure 2, the nodes interact and update their states in a recurrent fashion. At each interaction step, the nodes aggregate the transformed state information with neighbors, and then update their node states according to the aggregated information and history via GRU and residual connection. Next, we will introduce the details of Fi-GNN elaborately.

#### Initial Node States

The initial node states are that of the input feature graphs, i.e., the field embedding vectors. In particular, the embedding vector $e_i$ of field $i$ is utilized as the initial state vector of the corresponding node $n_i$, which can be formalized as,

$$H^1 = E,$$

$$h^i_n = e_i, i \in [1, 2, ..., m].$$

Accordingly, $h \in \mathbb{R}^D$, $H \in \mathbb{R}^{m \times D}$.

#### State Aggregation

At interaction step $t$, each node will aggregate the state information from neighbors. Formally, the aggregated information of node $n_j$ is sum of its neighbors’ transformed state

$$a^t_j = \sum_{n_j \rightarrow n_j \in E} A[n_j, n_i]W_p h^{t-1}_j,$$

where $W_p$ is the transformation function. $A \in \mathbb{R}^{m \times m}$ is the adjacency matrix containing the edge weights. For example, $A[n_j, n_i]$ is the weight of edge from node $n_j$ to $n_i$, which can reflect the importance of their interaction. Apparently, the transformation function and adjacency matrix decide on the node interactions. Since the interaction on each edge ought to differ, we aim to achieve edge-wise interaction, which requires a unique weight and transformation function for each edge.

1. **Attentional Edge Weights.** The adjacency matrix in the conventional GNN models is usually in the binary form, i.e., only contains 0 and 1. It can only reflect the connected relation of nodes but fails to reflect the importances of their relations. In order to infer the importances of interactions between different nodes, we propose to learn the edge weights via an attention mechanism. In particular, the weight of edge from node $n_i$ to node $n_j$ is calculated with their initial node states, i.e., the corresponding field embedding vectors. Formally,

$$w(n_i, n_j) = \frac{\exp(\text{LeakyRelu}(W_w [e_i || e_j]))}{\sum_i \exp(\text{LeakyRelu}(W_w [e_i || e_j]))},$$

where $W_w \in \mathbb{R}^{2D}$ is a weight matrix, $||$ is the concatenation operation. The softmax function is utilized to make weights easily comparable across different nodes. Therefore, the adjacency matrix is,

$$A[n_i, n_j] = \begin{cases} w(n_i, n_j), & \text{if } i \neq j, \\ 0, & \text{else} \end{cases}$$

Since the edge weights reflects the importances of different interaction, Fi-GNN can provide good explanations on the relation of different feature fields of input instance, which will be further discussed in Section 4.5.

2. **Edge-wise Transformation.** As discussed before, a fixed transformed function on all the edges is unable to model the flexible interactions and a unique transformation for each edge is essential. Nevertheless, our graph is complete graph with a huge number of edges. Simply assigning a unique transformation weight to each edge will consuming too much parameter space and running time. To reduce the time and space complexity and also achieve edge-wise transformation, we assign an output matrix $W^{i}_{out}$ and an input matrix $W^{i}_{in}$ to each node $n_i$ similar with [4]. As shown in Figure 2, when node $n_i$ sends its state information to node $n_j$, the state information will first be transformed by its output matrix $W^{i}_{out}$ and then transformed by node $n_j$’s input matrix $W^{j}_{in}$ before $n_j$ receives it. The transformation function of edge $n_i \rightarrow n_j$ from node $n_i$ to node $n_j$ thus could be written as,

$$W^{n_i \rightarrow n_j}_{p} = W^{i}_{out} W^{j}_{in},$$

Likewise, the transformation function of edge $n_j \rightarrow n_i$ from node $n_j$ to node $n_i$ is

$$W^{n_j \rightarrow n_i}_{p} = W^{j}_{out} W^{i}_{in}.$$
Accordingly, the Equation 3 could be rewritten as,

\[ a_i^t = \sum_{n_j \rightarrow n_i \in E} A[n_j, n_i] W_{out}^i \tilde{h}_j^{t-1} + b_p. \]  

In this way, the number of parameters is proportional to the number of nodes rather than numerous edges, which greatly reduces the space and time complexity and meanwhile achieves edge-wise interaction.

**State Update.** After aggregating state information, the nodes will update the state vectors via GRU and residual connections.

1. **State update via GRU.** In traditional GGNN, the state vector of node \( n_i \) is updated via GRU based on the aggregated state information \( a_i^t \) and its state at last step. Formally,

\[ h_i^t = GRU(h_i^{t-1}, a_i^t). \]  

It can be formalized in detail as:

\[ \begin{align*}
    z_i^t &= \sigma(W_{z}a_i^t + U_{z}h_i^{t-1} + b_z), \\
    r_i^t &= \sigma(W_{r}a_i^t + U_{r}h_i^{t-1} + b_r), \\
    \tilde{h}_i^t &= tanh(W_{h}a_i^t + U_{h}(r_i^t \odot h_i^{t-1}) + b_h), \\
    h_i^t &= h_i^{t-1} \odot z_i^t + \tilde{h}_i^t \odot (1 - z_i^t),
\end{align*} \]  

where, \( W_z, W_r, W_h, b_z, b_r, b_h \) are weights and biases of the updating function Gated Recurrent Unit (GRU) \([12]\). \( z_i^t \) and \( r_i^t \) are update gate vector and reset gate vector, respectively.

2. **State update via Residual Connections.** Previous works \([2, 25, 26]\) have proved that it’s effective to combine the low-order and high-order interactions together. We thus introduce extra residual connections to update note states along with GRU, which can facilitate low-order feature reuse and gradients back-propagation. Therefore, the Eq. (9) can be rewritten as,

\[ h_i^t = GRU(h_i^{t-1}, a_i^t) + h_i^t. \]  

### 3.6 Attention Layer

After \( T \) propagation steps, we can obtain the node states

\[ H^T = [h_1^T, h_2^T, ..., h_n^T]. \]

Since the nodes have interacted with their \( T \)-order neighbors, the \( T \)-order feature interactions is modeled. We need a graph-level output to predict CTR.

**Attentional Node Weights** The final state of each field node has captured the global information. In other words, these filed nodes are neighborhood-aware. Here we predict a score on the final state of each field respectively and sum them up with an attention mechanism which measures their influences on the overall prediction. Formally, the prediction score of each node \( n_i \) and its attentional node weight can be estimated via two multiple layers perceptions respectively as,

\[ \hat{y}_i = MLP_3(h_i^T), \]

\[ a_i = MLP_2(h_i^T), \]

The overall prediction is a summation of all nodes:

\[ \hat{y} = \sum_{i=1}^{m} a_i \hat{y}_i. \]

Note that it is actually same as the work \([12]\). Intuitively, \( MLP_3 \) is used to model the prediction score of each field aware of the global information and \( MLP_2 \) is used to model the weights of each field (i.e., importance of fields’ influence on the overall prediction).

### 3.7 Training

Our loss function is Log loss, which is defined as follows:

\[ L = -\frac{1}{N} \sum_{i=1}^{N}(y_i \log(\hat{y}_i) + (1 - y_i) \log(1 - \hat{y}_i)). \]

where \( N \) is the total number of training samples and \( i \) indexes the training samples. The parameters are updated via minimizing the Log Loss using RMSProp \([28]\). Most CTR datasets have unbalanced proportion of positive and negative samples, which will mislead the predictions. To balance the proportion, we randomly select equal number of positive and negative samples in each batch during training process.

1. **Parameter Space.** The parameter needed to be learnt mainly consists of the parameters correlated to nodes and the perception networks in attention mechanism. For each node \( n_i \), we have an input matrix \( W_{in} \) and an output matrix \( W_{out} \) to transform state information. Totally we have 2m matrices, which are proportional to the number of nodes \( m \). In addition, we have two matrices of perception networks in the self-attention mechanism and also parameters in GRU. Overall, there are \( O(2m) \) matrices.

2. **Time Complexity.** For each input instance, the time complexity of training process in Fi-GNN consists of three parts. The first part is embed the one-hot feature into field embedding, which is \( O(m) \). The second part is receiving neighbors’ state information and updating the state of the concerned nodes, each propagation it is \( O(m) \) and overall it is \( O(mp) \). The last part is estimating the prediction score via two perception networks. According, the total complexity is \( O(m(p + 1)) \). Noted that the number of fields \( m \) is usually less than 100.

### 3.8 Model Analysis

1. **Comparison with Previous CTR Models.** As discussed before, the previous deep learning based CTR models model high-order interactions in a general paradigm: raw sparse input multi-filed features are first mapped into dense field embedding vectors, then simply concatenated together and feed into deep neural networks (DNN) or other specifically designed networks to learn high-order feature interactions. The simple unstructured combination of feature fields inevitably limits the capability to model sophisticated interactions among different fields in a sufficiently flexible and explicit fashion. In this way, the interaction between different fields is conducted in a fixed fashion, no matter how sophisticated the used network is. In addition, they lack good model explanation.

Since we represent the multi-field features in a graph structure, our proposed model Fi-GNN is able to model interactions among different fields in the form of node interactions. Compared with the previous CTR models, Fi-GNN can model the sophisticated feature interaction via flexible edge-wise interaction function, which is more effective and explicit. Moreover, the edge weights reflecting importance of different interactions can be learnt in Fi-GNN, which provides good model explanations for CTR prediction. In fact, if the edge weight is all 1 and the transformation matrix on each edge
We first present some fundamental experimental settings before features and ad attributes. The fields are partial anonymous. Played mobile ads. There are 23 feature fields including user/device page he is visiting, the goal is to predict the probability that he will click on a given ad.

As discussed before, the node interaction on each edge in GNN depends on the edge weight and the transformation function on the edge. The conventional GGNN uses binary edge weights which fails to reflect the importance of the relations, and a fixed transformation function on all the edges. In contrast, our proposed Fi-GNN can model edge-wise interactions via attention edge weights and edge-wise transformation functions. When the interaction order is high, the node states tend to be smooth, i.e., the states of all the nodes tend to be similar. The residual connections can help identity the nodes by adding initial node states.

| Dataset   | #Instances | #Fields | #Features (sparse) |
|-----------|------------|---------|--------------------|
| Criteo    | 45,840,617 | 39      | 998,960            |
| Avazu     | 40,428,967 | 23      | 1,544,488          |

## 4 EXPERIMENTS

In this section, we conduct extensive experiments to answer the following questions:

- **RQ1** How does our proposed Fi-GNN perform in modeling high-order feature interactions compared with the state-of-the-art models?
- **RQ2** Does our proposed Fi-GNN perform better than original GGNN in modeling high-order feature interactions?
- **RQ3** What are the influences of different model configurations?
- **RQ4** What are the relations between features of different fields? Is our proposed model explainable?

We first present some fundamental experimental settings before answering these questions.

### 4.1 Experiment Setup

#### 4.1.1 Datasets.

We evaluate our proposed models on the following two datasets, whose statistics are summarized in Table 1.

1. **Criteo**

   This is a famous industry benchmark dataset for CTR prediction, which has 45 million users’ click records in 39 anonymous feature fields on displayed ads. Given a user and the page he is visiting, the goal is to predict the probability that he will click on a given ad.

2. **Avazu**

   This dataset contains users’ click behaviors on displayed mobile ads. There are 23 feature fields including user/device features and ad attributes. The fields are partial anonymous.

For the two datasets, we remove the infrequent features appearing in less than 10, 5 times respectively and treat them as a single feature “<unknown>”. Since the numerical features may have large variance, we normalize numerical values by transforming a value $z$ to $\log_2(z)$ if $z > 2$, which is proposed by the winner of Criteo Competition.

### 4.1.2 Evaluation Metrics.

We use the following two metrics for model evaluation: AUC (Area Under the ROC curve) and Logloss (cross entropy).

- **AUC** measures the probability that a positive instance will be ranked higher than a randomly chosen negative one. A higher AUC indicates a better performance.
- **Logloss** measures the distance between the predicted score and the true label for each instance. A lower Logloss indicates a better performance.

#### 4.1.3 Baselines.

As described in Section 2.1, the early approaches can be categorized into three types: (A) Logistic Regression (LR) which models first-order interaction; (B) Factorization Machine (FM) based linear models which model second-order interactions; (C) Deep learning based models which model high-order interactions on the concatenated field embedding vectors.

We select the following representative methods of three types to compare with ours.

- **LR** (A) models first-order interaction on the linear combination of raw individual features.
- **FM** (B) models second-order feature interactions from vector inner products.
- **AFM** (C) is a extent of FM, which considers the weight of different second-order feature interactions by using attention mechanism. It is one of the state-of-the-art models that model second-order feature interactions.

**DeepCrossing** utilizes DNN with residual connections to learn high-order feature interactions in an implicit fashion.

**NFM** (C) utilizes a Bi-Interaction Pooling layer to model the second-order interactions, and then feeds the concatenated second-order combinatorial features into DNNs to model high-order interactions.

**CrossNet** (Deep&Cross) is the core of Deep&Cross model, which tries to model feature interactions explicitly by taking outer product of concatenated feature vector at the bit-wise level.

**CIN** (xDeepFM) is the core of xDeepFM model, which takes outer product of stacked feature matrix at vector-wise level.

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with 100 hidden units. NFM has one hidden layer of size 200 on

Table 2: Performance Comparison of Different methods. The best performance on each dataset and metric are highlighted. Further analysis is provided in Section 4.2.

| Model Type | Model | Criteo AUC | Criteo RI-AUC | Criteo Logloss | Criteo RI-Logloss | Avazu AUC | Avazu RI-AUC | Avazu Logloss | Avazu RI-Logloss |
|------------|-------|------------|---------------|----------------|-------------------|-----------|-------------|---------------|-----------------|
| First-order | LR    | 0.7820     | 3.35%         | 0.4695         | 6.05%             | 0.7560    | 7.41%       | 0.3964        | 3.71%           |
|             | FM [23] | 0.7836     | 3.11%         | 0.4700         | 6.15%             | 0.7706    | 5.37%       | 0.3856        | 1.01%           |
|             | AFM[33] | 0.7938     | 1.81%         | 0.4584         | 3.77%             | 0.7718    | 5.21%       | 0.3854        | 0.96%           |
| Second-order | DeepCrossing [25] | 0.8012     | 0.87%         | 0.4513         | 2.26%             | 0.7643    | 6.24%       | 0.3889        | 1.85%           |
|             | NFM [8] | 0.7957     | 1.57%         | 0.4562         | 3.31%             | 0.7708    | 5.35%       | 0.3864        | 1.22%           |
|             | CrossNet [30] | 0.7907     | 2.47%         | 0.4591         | 3.92%             | 0.7667    | 4.53%       | 0.3868        | 1.32%           |
|             | CIN [15] | 0.8009     | 0.91%         | 0.4517         | 2.35%             | 0.7758    | 4.67%       | 0.3829        | 0.31%           |
|             | Fi-GNN (ours) | 0.8082     | -             | 0.4411         | -                 | 0.8120    | -           | 0.3817        | -               |
| High-order  | DeepCrossing [25] | 0.8012     | 0.87%         | 0.4513         | 2.26%             | 0.7643    | 6.24%       | 0.3889        | 1.85%           |
|             | NFM [8] | 0.7957     | 1.57%         | 0.4562         | 3.31%             | 0.7708    | 5.35%       | 0.3864        | 1.22%           |
|             | CrossNet [30] | 0.7907     | 2.47%         | 0.4591         | 3.92%             | 0.7667    | 4.53%       | 0.3868        | 1.32%           |
|             | CIN [15] | 0.8009     | 0.91%         | 0.4517         | 2.35%             | 0.7758    | 4.67%       | 0.3829        | 0.31%           |
|             | Fi-GNN (ours) | 0.8082     | -             | 0.4411         | -                 | 0.8120    | -           | 0.3817        | -               |

4.1.4 Implementation Details. We implement our method using Tensorflow\(^4\). The optimal hyper-parameters are determined by the grid search strategy. Implementation of baselines follows [26]. Dimension of field embedding vectors is 16 and batch size is 1024 for all methods. DeepCrossing has four feed-forward layers, each with 100 hidden units. NFM has one hidden layer of size 200 on top of Bi-Interaction layer as recommended in the paper [8]. There are three interaction layers for both CrossNet and CIN. All the experiments were conducted over a sever equipped with 8 NVIDIA Titan X GPUs.

4.2 Model Comparison (RQ1)

The performance of different methods is summarized in Table 2, from which we can obtain the following observations:

(1) LR achieves the worst performance among these baselines, which proves that the individual features is insufficient in CTR prediction.

(2) FM and AFM, which model second-order feature interactions, outperform LR on all datasets, indicating that it’s effective to model pair-wise interaction between feature fields. In addition, AFM achieves better performance than FM, which proves the effectiveness of attention on different interactions.

(3) The methods modeling high-order interaction mostly outperform the methods that model second-order interactions. This indicates the second-order feature interactions is not sufficient.

(4) DeepCrossing outperforms NFM, proving the effectiveness of residual connections in CTR prediction.

(5) Our proposed Fi-GNN achieves best performance among all these methods on two datasets. Considering the fact that previous improvements with respect to AUC at 0.001-level are regarded significant for CTR prediction task, our proposed method shows great superiority over these state-of-the-arts, owing to the great representative power of graph structure and the effectiveness of GNN on modeling node interactions.

(6) Compared with these baselines, the relative improvement of our model achieves on Avazu dataset is higher than that on Criteo dataset, which may because that the features in Avazu dataset are mostly categorical while there are some numerical feature in Criteo dataset. This indicates that our model perform better on categorical features than numerical features.

4.3 Ablation Study (RQ2)

Our proposed model Fi-GNN is based on GNN, upon which we mainly make two improvements: (1) we achieve edge-wise node interactions via attentional edge weights and edge-wise transformation; (2) we introduce extra residual connections to update state along with GRU. To evaluate the effectiveness of the two improvements on modeling node interactions, we conduct ablation study and compare the following three variants of Fi-GNN:

- **Fi-GNN-(E)**: Fi-GNN without the two above mentioned improvements: edge-wise node interactions (E) and residual connections (R).
- **Fi-GNN-(E/R)**: Fi-GNN without edge-wise interactions (E) and residual connections (R), which is also GNN with edge-wise interactions.

The performance comparison is shown in Figure 3(a), from which we can obtain the following observations:

(1) Fi-GNN-(E) and Fi-GNN-(R) both outperform GNN, which proves the effectiveness of residual connections and edge-wise interaction in modeling node interactions. Fi-GNN-(E/R) outperform Fi-GNN-(E/R) by a margin, which suggests that it is crucial to model the edge-wise interaction. Fi-GNN-(E) also achieves better performance than Fi-GNN-(E/R), proving the effectiveness of residual connections.

(2) Fi-GNN achieves best performance among these variants, indicating that the two improvements we make, i.e., residual connections and edge-wise interactions, can jointly boost the performance.

We take two measures to achieve edge-wise node interactions in Fi-GNN: attentional edge weight (W) and edge-wise transformation (T). To further investigate where dose the great improvement come from, we conduct another ablation study and compare the following three variants of Fi-GNN:

- **Fi-GNN-(W/T)**: Fi-GNN without self-adaptive adjacency matrix (W) and edge-wise transformation (T), i.e., uses binary adjacency matrix (all the edge weights are 1) and a shared transformation matrix on all the edges. It is also Fi-GNN-(E).
- **Fi-GNN-(W)**: Fi-GNN without attentional edge weights, i.e., uses binary adjacency matrix.

\(^4\)The code is released at https://github.com/CRIPAC-DIG/FiGNN
Fi-GNN(-T): Fi-GNN without edge-wise transformation, i.e., uses a shared transformation on all the edges.

The performance comparison is shown in Figure 3(a). We can see that Fi-GNN(-T) and Fi-GNN(-W) both outperform Fi-GNN(-W/T), which proves their effectiveness. Nevertheless, Fi-GNN(-W) achieves greater improvements than Fi-GNN(-T), suggesting that the edge-wise transformation is more effective than attentional edge weights in modeling edge-wise interaction. This is quite reasonable since the transformation matrix ought to have stronger influence on interactions than a scalar attentional edge weight. In addition, Fi-GNN achieves the best performance demonstrates that it’s crucial to take both the two measures to model edge-wise interaction.

4.4 Hyper-Parameter Study (RQ3)

4.4.1 Influence of different state dimensionality. We first investigate how the performance change w.r.t. the dimension of the node states $D$, which is also the dimension of field embedding vectors. The results on Criteo and Avazu datasets are shown in Figure 4(a). On both datasets, we can see that the performance continuously increase along with the increasing of the dimension size since larger size can provide sufficient information. When the dimension size reaches 16, the performances begin to decrease, which may due to that state of this size has been represented enough information and the model is overfitted when too many parameters are used.

4.4.2 Influence of different interaction steps. We are interested in what the optimal order of feature interactions is. Our proposed Fi-GNN can answer the question, since the interaction step $T$ equals to the order of feature interaction. Therefore, we conduct experiments on how the performance changes w.r.t. the order of feature interaction, i.e., the interaction step $T$. The results on Criteo and Avazu datasets are shown in Figure 4(b). On both datasets, we can see that the performance increases along with the increasing of $T$ until it reaches 3, after that the performance starts to decrease. This finding suggests 3-order interactions is enough for Criteo and Avazu dataset. It is reasonable since the two datasets have 39 and 23 fields respectively and 3 interaction steps are enough for the field nodes to fully interact with other nodes in the feature graphs.

4.5 Model Explanation (RQ4)

In this section, we will answer the question that can Fi-GNN provide explanations. We apply attention mechanisms on the edges and nodes in the feature graphs and obtain attentional edge weights and attentional node weights respectively, which can provide explanations from different aspects.
global average cases

Figure 6: Heat map of attentional node weights at both global- and case-level on Avazu, which reflects the importance of different feature fields on the final prediction.

4.5.1 **Attentional Edge weights.** The attentional edge weight reflects the importance of interaction between the two connected field nodes, which can also reflect the relation of the two feature fields. Higher the weight is, stronger the relation is. Figure 5 presents the heat map of the globally averaged adjacency matrix of all the samples in Avazu dataset, which can reflect the relations between different fields in a global level. Since they are some anonymous feature fields, we only show the remaining 13 feature fields with real meanings.

As can be seen, some feature fields tend to have a strong relations with others, such as site_category and site_id. This makes sense since the two feature field both corresponds to the website where the impressions are put on. They contain the main contextual information of impressions. Hour is another feature which have close relations with others. It is reasonable since Avazu focuses on mobile scene, where user surfing online at any time of a day. The surfing time has strong influence on other advertising features. On the other hand, device_ip and device_id seem to have weak relations with other feature fields. This may due to that they nearly equal to user identity, which is relatively fixed and hard to be influenced by other features.

4.5.2 **Attentional Node weights.** The attentional node weights reflect the importances of feature fields’ influence on the overall prediction score. Figure 6 presents the heat map of global-level and case-level attentional node weights. The leftmost is an globally averaged one of all the samples in Avazu dataset. The left four are randomly selected, whose predicted scores are [0.97, 0.12, 0.91, 0.99], and labels are [1, 0, 1] respectively. At the global level, we can see that the feature field app_category have the strongest influence on the clicking behaviors. It is reasonable since Avazu focuses on mobile scene, where the app is the most important factor. At the case level, we observe that the final clicking behavior mainly depends on one critical feature field in most cases.

5 CONCLUSIONS

In this paper, we point out the limitations of the previous CTR models which consider multi-field features as an unstructured combination of feature fields. To overcome these limitations, we propose to represent the multi-field features in a graph structure for the first time, where each node corresponds to a feature field and different fields can interact through edges. Therefore, modeling feature interactions can be converted to modeling node interaction on the graph. To this end, we design a novel model Fi-GNN which is able to model sophisticated interactions among feature fields in a flexible and explicit fashion. Overall, we propose a new paradigm of CTR prediction: represent multi-field features in a graph structure and convert the task of modeling feature interactions to modeling node interactions on graphs, which may motivate the future work in this line.

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