Carbide-Derived Carbons: WAXS and Raman Spectra for Detailed Structural Analysis

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Abstract: Quick characterization methods to determine the structure of carbon materials are sought after for a wide array of technical applications. In this study we present the combined analysis of the structure of carbide-derived carbons (CDCs) with Raman spectroscopy and wide-angle X-ray scattering (WAXS) methods. We present the optimal deconvolution method to be used for the detailed analysis of Raman spectroscopy data of CDCs and comparison to corresponding WAXS results is made. For a broad set of CDCs both WAXS and Raman spectroscopy data showed that the average graphene layer extent increases with synthesis temperature of CDC, while the coherent domain lengths obtained from Raman spectroscopy higher by an average of 4.4 nm. In addition, the presence of correlations between the parameters (D-band width and the parameter $A_D/A_G$) from Raman spectroscopy and the synthesis temperature are established. Based on the WAXS and Raman spectra data analysis the strong influence of the precursor carbide structure on the graphitization pathway is shown.

Keywords: carbide-derived carbon; raman spectroscopy; porous carbon; amorphous carbon; WAXS

1. Introduction

Carbon materials are vital components to a multitude of applications, from energy storage and conversion to gas separation and filtration systems. In case of chemically pure carbons the suitability of a certain carbon material for a specific application is determined by its structural properties, e.g., porosity parameters, particle size and its distribution, level of graphitization, etc. [1–4]. For the use of a large variety of carbons in applications with different requirements for the structure of carbon it is vital to be able to characterize novel synthesized carbons with quick, relatively cheap, and available quantitative analytical methods.

Carbide-derived carbons (CDCs) are unique model carbon materials, since they contain little to no impurities and their structure can be easily influenced within range from very disordered to well-organized nano-graphitic particles. The CDCs have been successfully used in electrochemical applications such as electrode materials for supercapacitors [5–10], as catalyst carriers for polymer-electrolyte membrane fuel cells (PEMFC) [11] and in other applications such as gas adsorption [12–14]. In addition, the structure of some CDCs has been investigated in-depth with small-angle X-ray and neutron scattering methods. [15,16] While the CDC materials in this study have been introduced and reported previously, the present study aims at elucidating their $sp^2$ microstructure in more detail, with the emphasis on the interpretation of the Raman spectra.
The shape and intensity of Raman spectrum of carbon is strongly dependent on the synthesis method and heat-treatment temperature applied for the preparation of the carbon powder [17–19]. This would make the Raman spectroscopy one of the best and most sensitive methods for the characterization of the crystallographic and electronic structure of carbon materials. The first order Raman spectra of carbon materials exhibits two very pronounced and well-known bands, the D- (disordered) and G- (graphitic) band. The G-band corresponds to one-phonon Raman scattering process at the 1st Brillouin zone center Γ and consists of the collective in-plane bond stretching of the polyaromatic carbon atoms (E_{2g} symmetry) [17,20]. The D-band (~1250–1400 cm\(^{-1}\)) corresponds to the excitation of the totally symmetric transversal phonon A'\(_1\) located near the high symmetry phonon points (K or K'). This activation process (intravalley Raman mode) involves electron-phonon interaction mediated by defects [20,21]. Thus, the G-band originates from the ordered graphite-like areas, and the D-band originates from the edge of the ordered areas and from the vicinity of different defects. Therefore, as the quantity of defects increases, the intensity of the D-band (I\(_D\)) and, thus, also the ratio of intensity I\(_D\)/I\(_G\) increases (I\(_G\) is the intensity of the G-band). This was discovered by Tuinstra and Koenig in 1970 [17] and the ratio I\(_D\)/I\(_G\) has been extensively used as an indicator of the ordering or the characteristic connected with defect density in carbon materials [5,6,9,22,23]. However, the situation is more complicated in the case of disordered and/or partially graphitized carbons, where the first order Raman spectrum is rather complex. Namely, it seems to contain more vibrational bands than just the G- and the D-band [24–27] and, thus, the deconvolution of the spectrum is not straightforward. Most commonly, two extra functions are added to obtain a reasonable fit to the experimental first order region of the Raman spectrum, at ~1150 cm\(^{-1}\), at ~1450 cm\(^{-1}\) and at ~1620 cm\(^{-1}\) [24,25,27,28]. One of the explanations of these extra bands is that they are analogous to the D- and the G-band, but originate from the highly disordered areas and, thus, because of the softening of the phonon modes are present at lower frequencies [27]. Some authors argue, that there is also a D'-band at ~1620 cm\(^{-1}\), even if its tip is not separated from the G-band [18,26]. This means a total of five functions are needed to fit the first-order Raman spectrum of disordered carbons. Thus, there exists several approaches about how many and which sort of fitting functions should be used for the deconvolution of the first order Raman spectra of disordered carbons [23–27,29]. Possibly, using different approaches for various types of disordered carbons is the best solution and there have been some efforts to classify disordered carbons in terms of their graphene layer extent, L\(_a\) [19,30] or their origin [18,28].

The spectrum deconvolution procedure can have a great impact on the quantitative results obtained about the structure of the studied carbon. Therefore, one of the objectives of this work is to compare different applied deconvolution approaches [26,27,29] for getting quantitative information (widths, areas of bands, etc.) about the Raman spectrum of carbide-derived carbons (CDC) synthesized at different temperatures. The quantitative parameters of the CDCs from Raman spectra (widths of the D- and the G-band, I\(_D\)/I\(_G\), etc.) are then compared to the results obtained from the WAXS pattern analysis with the algorithm derived by Ruland and Smarsly [31]. This algorithm models the whole WAXS pattern, fitting a total of 14 interlayer and intralayer parameters, including the lateral extent of the graphene sheets (L\(_a\)).

In this study CDCs synthesized from six different precursor carbides (Mo\(_2\)C, TiC, WC, VC, Ta\(_4\)HfC\(_5\), WTiC\(_2\)) at different temperatures, T\(_{syn}\) ranging from 500 °C to 1100 °C, have been characterized in detail. This enables to study the evolution of spectra in a series of materials for which only one parameter (precursor carbide or synthesis temperature) has been varied systematically. The CDC powders are disordered porous materials with specific surface areas ranging from ~500 m\(^2\) g\(^{-1}\) to 2000 m\(^2\) g\(^{-1}\) [5–9].
2. Materials and Methods

2.1. Carbine-Derived Carbons

Porous carbide-derived carbon powders (so-called CDCs) have been prepared using the method of high-temperature chlorination of binary carbides (TiC, α-WC, VC, Mo2C from Sigma-Aldrich, Steinheim, Germany) and ternary carbides (Ta4HfC5, WTiC2 from Goodfellow, Huntingdon, UK). The full details of this process may be found elsewhere [5–10], but are briefly outlined here for convenience.

The chlorination reaction of carbide was performed in a flow of Cl2 (99.99%, Linde Gas, Solna, Sweden) at a fixed temperature, ranging from 500 to 1100 °C (Table 1). The obtained CDC powder was then treated with H2 at 800 °C (or 900 °C) to thoroughly remove residues of chlorine, chloride, and all possible functional groups from the CDC surface. Resulting carbons are noted as C-X Y in the text, where X denotes the precursor carbide and Y denotes the synthesis temperature in degrees of Celsius scale. The resulting CDC powders are disordered porous materials with specific surface areas ranging from ~500 m² g⁻¹ to 2000 m² g⁻¹.

Table 1. The precursor carbides and corresponding chlorination temperatures of carbide-derived carbon powders analyzed.

| Precursor Carbide | Chlorination Temperature (°C) | Ref. |
|-------------------|-------------------------------|------|
| Mo2C             | 600 700 800 900 1000 1100     | [5]  |
| Ta4HfC5          | 800 900 1000 1100             | [6]  |
| WTiC2            | 800 900 1000 1100             | [6]  |
| WC                | 800 900 1000 1100             | [7]  |
| TiC              | 800 900 1000 1100             | [8]  |
| VC                | 500 600 700 800 900 1000 1100 | [9]  |

2.2. Wide-Angle X-Ray Scattering Measurements

The WAXS patterns of carbon powders were measured using a Bruker D8 Advance diffractometer (Bruker) with a Cu Ka radiation, a Goebel mirror, 2.5° Soller slits and LynxEye 1D detector and Bragg-Brentano geometry. WAXS data was fitted with the algorithm derived by Ruland and Smarsly [31] using the CarbX software (https://www.uni-giessen.de/CarbX accessed on 21 March 2021) [32].

2.3. Raman Spectroscopy

The Raman spectroscopy measurements were conducted on an inVia micro-Raman spectrometer (Renishaw, Kingswood, UK) for all CDCs with excitation wavelength, $\lambda_L$, 514 nm. In addition, the Raman spectrum of C-SiC 1000, C-Mo2C 1000, and C-Mo2C 700 powders were measured with different fixed wavelengths $\lambda_L = 457, 488, 633,$ and 785 nm. While measuring the spectrum, the incident power was kept low (~1 mW at the sample) not to damage the carbon sample. Each spectrum analyzed represents the average of at least three measurements from different regions selected on the same sample.

Detailed deconvolution of the first order Raman spectra has been conducted using four different approaches using OriginPro 2016 software (OriginLab, San Francisco, CA, USA). Prior to deconvolution, the baseline (4th order polynomial function) has been subtracted from the spectrum under analysis. For the fitting of the experimental data, the Lorentzian function (henceforth noted as L) corresponds to Equation (1),

$$L = y(x) = \frac{2 S_p}{\pi} \frac{FWHM}{4(x-x_0)^2 + FWHM^2},$$

where $y(x)$ is the intensity, $S_p$ is the peak area, $x$ is the wavenumber, $x_0$ is the wavenumber of the peak maximum. FWHM is the full width at half maximum of the peak.
The Gaussian function (henceforth noted as \( G \)) follows the equation

\[
G = y(x) = S_p e^{-\frac{4 \ln 2(x-x_0)^2}{\text{FWHM}^2}} / \left( \text{FWHM} \sqrt{\frac{\pi}{4 \ln 2}} \right).
\]  

(2)

The Breit-Weigner-Fano (henceforth noted as \( \text{BWF} \)) shape is expressed by

\[
\text{BWF} = y(x) = y_{\text{max}} \left( 1 + \frac{x - x_0}{q \text{FWHM}} \right)^2 / \left( 1 + \left( \frac{x - x_0}{\text{FWHM}} \right)^2 \right),
\]  

(3)

where \( q \) is a coupling factor (at large \( q \), the function resembles the Lorentzian function).

3. Results

3.1. Wide-Angle X-Ray Scattering

In the Wide-Angle X-ray Scattering (WAXS) patterns of the studied CDCs, there is a diffuse (002) reflection located at scattering vector modulus (The scattering vector modulus, \( q \), is defined as \( q = 4\pi \sin(\theta)/\lambda \), where \( 2\theta \) is the scattering angle.), \( q \sim 18 \text{ nm}^{-1} \) and a diffuse asymmetric (10) reflection at \( q \sim 30 \text{ nm}^{-1} \) (Figure 1, Figure S1 in Supplementary information, SI). The patterns are typical of non-graphitic carbon, since no well-expressed (hkl) reflections can be seen and, thus, were analyzed using the algorithm derived by Ruland and Smarsly [31], which is implemented in the CarbX software [32] (Figure 1). Distinct tendencies of the microstructural parameters to the \( T_{\text{syn}} \) of the CDCs are obtained from fitting of the CDCs WAXS data (Table 2, Table S1 in SI). The size of the graphene layer is described by the graphene layer extent, \( L_a \), and average chord length, \( \langle l \rangle \). Both \( L_a \) and \( \langle l \rangle \) increase with \( T_{\text{syn}} \) for all CDCs, where the minimal \( L_a \) is 2.5 nm and maximal 8.3 nm in case of C-VC 600 and C-Mo_2C 1000, respectively. The standard deviation of the first-neighbor distribution, \( \sigma_1 \), which is correlated to the defect density in a graphene layer decreases slightly with \( T_{\text{syn}} \) for most CDCs, from the maximal value of \( \sim 0.022 \text{ nm} \) to a minimal value of 0.008 nm characteristic of the highest \( T_{\text{syn}} \). The average C–C bond length, \( l_{cc} \), is mostly constant at 0.141 nm (±0.0006 nm), i.e., typical of aromatic carbons. This means that CDCs derived at higher \( T_{\text{syn}} \) contain larger and more defect-free graphene sheets.

Figure 1. Wide-angle X-ray scattering data (spheres) of different carbide-derived carbons (CDCs, noted in Figure) and fit curve (solid line), where the scattering vector modulus, \( q \), is defined as \( q = 4\pi \sin(\theta)/\lambda \), where \( 2\theta \) is the scattering angle.
Table 2. Parameters derived from WAXS patterns for some CDCs. $L_a$—average graphene layer extent, $l_{cc}$—average C-C bond length, $\sigma_1$—standard deviation of the first-neighbor distribution, $\langle N \rangle$—average number of graphene layers per stack, $L_c$—average stacking size, $a_3$—average interlayer spacing, $\sigma_3$—standard deviation of interlayer spacing.

| $T_{syn}$ | C-Mo$_2$C | C-Ta$_4$HfC$_5$ | C-WTiC | C-WC | C-TiC | C-VC |
|-----------|-----------|-----------------|--------|------|------|------|
| 800       | 1000      | 800             | 1000   | 800  | 1000 | 800  |
| $L_a$, nm | 3.8 ± 0.6 | 8.3 ± 2.9       | 2.5 ± 0.3 | 5.6 ± 1.3 | 2.6 ± 0.3 | 7.1 ± 2.1 | 2.8 ± 0.3 | 4.5 ± 0.8 | 2.6 ± 0.3 | 5.6 ± 1.3 | 2.5 ± 0.3 | 6.3 ± 1.6 |
| $l_{cc}$, nm | 0.1412 | 0.1410 | 0.1381 | 0.1409 | 0.1405 | 0.1400 | 0.1411 | 0.1411 | 0.1410 | 0.1414 | 0.1416 | 0.1406 |
| $\sigma_1$, nm | 0.016 | 0.012 | 0.013 | 0.016 | 0.022 | 0.016 | 0.016 | 0.015 | 0.021 | 0.018 | 0.020 | 0.011 |
| $\langle N \rangle$ | 1.05 | 6.74 | 0.19 | 1.21 | 0.66 | 1.02 | 1.40 | 1.90 | 1.08 | 0.97 | 1.51 | 0.09 |
| $L_c$, nm | 1.3 ± 0.2 | 2.7 ± 0.2 | 0.7 ± 0.1 | 0.52 ± 0.05 | 0.57 ± 0.56 | 0.55 ± 0.03 | 0.8 ± 0.1 | 0.5 ± 0.1 | 0.6 ± 0.1 | 0.05 | 3.1 ± 0.7 |
| $a_3$, nm | 0.364 | 0.351 | 0.333 | 0.380 | 0.354 | 0.369 | 0.314 | 0.347 | 0.365 | 0.365 | 0.395 | 0.343 |
| $\sigma_3$, nm | 0.001 | 0.084 | 0.110 | 0.001 | 0.024 | 0.000 | 0.057 | 0.021 | 0.038 | 0.039 | 0.051 | 0.011 |

For most CDCs, the interlayer parameters like average stacking size, $L_c$, and average interlayer spacing, $a_3$, only slight change is seen with $T_{syn}$ (Table 2, Table S1). The effect of the stacking not changing significantly with the increase in $T_{syn}$ was also shown by Faber et al. and deemed a peculiarity of CDCs [33]. Surprisingly, the exceptions are carbons C-Mo$_2$C and C-VC, where $L_c$ increases and $a_3$ decreases with $T_{syn}$. The average number of graphene layers per stack increases significantly with the increase in $T_{syn}$ for C-Mo$_2$C, which refers to the formation of multilayer graphene at higher $T_{syn}$.

3.2. The Raman Spectra of CDCs: The Stages of Graphitization

With the increase of $T_{syn}$, the D- and G-band become narrower and the intensity between these two bands (at $\nu \sim 1450$ cm$^{-1}$) decreases. This is related to the increasing ordering of the carbon structure (Figure 2a,b). The D- and G-band raw height ratio, $I_D/I_G$, determined directly from the measured spectra, along with the width of the bands, can be used to discern the typical stages along the pathway of transformation from disordered to graphitic structure as defined by Schuepfer et al. [30]. However, while in the latter study the carbons were synthesized via heat-treatment of carbonaceous material at different temperatures, the $T_{syn}$ of CDCs has an inherently different effect on the formation of the material than the heat-treatment temperature. Namely, for CDCs the crystalline domains are formed at $T_{syn}$ as opposed to reorganizing from previously existing carbonaceous structure. Still, it has been shown for both heat-treated carbonaceous materials and CDCs that the impact of the heating temperature on the structure of the resulting carbon is strongly dependent on the starting material [30,34], i.e., for CDCs the chemical composition and crystallographic structure of the precursor carbide.

Figure 2. The Raman spectra normalized to the G-band intensity measured with excitation laser wavelength 514 nm (laser energy $E_L = 2.41$ eV) for CDCs synthesized from (a) Mo$_2$C and (b) WC at different $T_{syn}$ (noted in Figure).
Based on the characteristics of the Raman spectra, the CDCs can be divided into Stage I, Stage II and Stage III in the graphitization pathway. The disordered (in the original publication the term “amorphous carbon” was used, but this refers to carbons with considerable sp3-content (IUPAC [35]), which is not the case for CDCs.) carbon of Stage I is characterized by broad and overlapping D- and G-bands and $I_D/I_G < 1$. In the case of the nanoparticular carbon of Stage II, the D- and G-bands are still broad, but the $I_D/I_G$ ratio increases further with the increase in the heat-treatment temperature and reaches its maximum value of $I_D/I_G = 1.2−1$. Stage III (non-graphitic carbon) is characterized by narrow Raman bands and the decrease of the $I_D/I_G$ ratio towards zero with the increase in the heat-treatment temperature.

The Raman spectrum of C-WC shows very broad and overlapping bands even at the high $T_{\text{syn}} = 1100 °C$ (Figure 2b), which corresponds to Stage II (i.e., nanoparticular). C-Mo2C at $T_{\text{syn}} = 1100 °C$ can be classified as Stage III (i.e, non-graphitic, Figure 2a) based on the Raman spectrum. Thus, CDCs derived at the same $T_{\text{syn}}$ from different carbides can have vastly different structures and the graphitization pathway is strongly dependent on the precursor carbide.

Most of the studied CDCs can be classified as carbons belonging to the Stage II of graphitization based on their Raman spectra (Table 3, Figure S2 in supplementary information, SI). For carbons, which belong to Stage II of graphitization, the increase of the $I_D/I_G$ ratio is related to the increase in structural order [22,30]. The intensity of the Raman spectra D-band increases in the Stage II of graphitization because the intensity of D-band from the ordered area near the edge/defect is ~7 times greater than the intensity of the D-band originating from the border/defect area itself [27]. Thus, at Stage I of graphitization (i.e., disordered) there are not enough sufficiently ordered hexagonal carbon domains from which the D-band vibrations can effectively originate, i.e., the density of defects is much larger than the coherent carbon domain area. The density of defects decreases in Stage II, allowing for more defect-free areas from which the D-band vibrations are of higher intensity, and thus, the overall D-band intensity increases.

Table 3. Carbide derived carbons divided by the graphitization stages based on the Raman spectra.

| Carbide | Stage I | Stage II | Stage III |
|---------|---------|----------|-----------|
| C-Mo2C  |         |          |           |
| C-Ta2HfC5 |       |          |           |
| C-WTiC2 |         |          |           |
| C-WC    |         | Stage II |           |
| C-TiC   |         | Stage II |           |
| C-VC    | Stage I | Stage II | Stage III |

In the second order Raman spectrum of CDCs synthesized at $T_{\text{syn}} \geq 1000 °C$, three distinct bands are seen at ~2440 cm$^{-1}$, ~2730 cm$^{-1}$ and ~2920 cm$^{-1}$. These bands are attributed to the convolution of the band at 1150 cm$^{-1}$ and D-band (noted as 1150+D) [36,37], the 2D-band [20,21,38], and convolution of the G-band and the D-band (noted as G+D) [36,39] excitations, respectively. The most prominent feature in the second order Raman spectrum is the 2D-band, which is present in most of the CDCs spectra synthesized at $T_{\text{syn}} \geq 900 °C$. A distinct D + G band is seen only in certain CDCs, which are mostly the ones synthesized at $T_{\text{syn}} \geq 1000 °C$ (Figure 2a,b, Figure S2). The 1150+D band is a shoulder at lower wavenumbers from the 2D-band in the spectra of some CDC (Figure 2a,b).

The dispersive behavior of some Raman bands is seen from the spectra measured with different laser excitation wavelengths (Figure S3 in SI). In agreement with the results of previous studies, the D-band frequency upshifts linearly with the increasing excitation laser energy ($E_{\text{laser}}$) with the slope being about 50 cm$^{-1}$ eV$^{-1}$, but the 2D-band frequency upshifts with a slope ~100 cm$^{-1}$ eV$^{-1}$ [21,40,41]. The G-band exhibits a non-dispersive behavior and the D + D’ band upshifts by ~15 cm$^{-1}$ eV$^{-1}$ [21,41].
3.3. Impact of Band Deconvolution Method on Calculated Peak Properties

Detailed deconvolution of the first order Raman spectra has been conducted using four different approaches:

1. Deconvolution by two Lorentzian functions (Equation (1)) centered at ~1350 cm$^{-1}$ (denoted as $D_1$ and $D_2$) and a Breit-Weigner-Fano (BWF) function (Equation (3)) centered at ~1500 cm$^{-1}$ (denoted as $G$) as proposed by Mallet-Ladeira [29], henceforth denoted as $L + L + BWF$ (Figure 3a).

2. Deconvolution by two Lorentzian functions centered at ~1350 cm$^{-1}$ (denoted as $D$) and 1500 cm$^{-1}$ (denoted as $G$), respectively, and two Gaussian functions (Equation (2)) centered at both sides of the D-band (denoted as $D_S$ and $G_S$, respectively) as proposed by Ribeiro-Soares [27], henceforth denoted as $G + L + G + L$ (Figure 3b).

3. Deconvolution by two Lorentzian functions centered at ~1200 cm$^{-1}$ and 1350 cm$^{-1}$ ($D_S$ and $D$, respectively) and two Gaussian functions centered at wavenumbers ~1450 cm$^{-1}$ and 1500 cm$^{-1}$ ($G_S$ and $G$, respectively), henceforth denoted as $L + L + G + G$ (Figure 3c).

4. Deconvolution by four Lorentzian functions centered at ~1200 cm$^{-1}$, 1350 cm$^{-1}$, 1500 cm$^{-1}$ and 1620 cm$^{-1}$ ($D_S$, $D$, $G$ and $D'$, respectively) and one Gaussian function centered at ~1450 cm$^{-1}$ ($G_S$) as proposed by Sadezky et al. [26], henceforth denoted as $L + L + G + L + L$ (Figure 3d).

The asymmetric BWF line supposedly arises from the coupling of a discrete mode to a continuum [24] and its asymmetrical shape helps to better account for the regions at ~1150 cm$^{-1}$ and ~1500 cm$^{-1}$, which fits poorly with a single symmetrical function. However, the $L+L+BWF$ deconvolution method (Figure 3a) still represents these regions on both sides of the D-band.
side of the D-band worse than the 4- or 5-function deconvolution approaches (Figure 3b–d). Thus, in the case of disordered CDCs, the 4- and 5-function approaches are more successful in reproducing the Raman scattering data within the region ~1000–1500 cm\(^{-1}\).

When the D’-band has not been accounted for and a Lorentzian-like function is used to describe the G-band, like in the L+L+BWF and G + L + G + L deconvolution approaches, the intensity at higher wavenumbers in comparison to the G-band is overestimated (Figure 3a,b). This region is better represented with the other two deconvolution methods (L + L + G + G and L + L + G + L + L; Figure 3c,d). However, with the L + L + G + G approach, the height of the G-band has not been fully reproduced, which can also be seen from the residual values (Figure 3c). In conclusion, the 5-band deconvolution yields the best fit to the measured spectrum as is evident from the smallest residuals.

The main differences of the band positions and widths obtained with various deconvolution approaches become clearer by plotting the FWHM vs. the band center (\(x_0\)) (as in [28]) (Figure 3e–h). Both the G-band and the D-band (denoted as D1 in Figure 3a) have a well-defined band center position and width according to all the different deconvolution methods applied. In the case of the 4-band deconvolution methods (Figure 3f,g) both the position and the FWHM of the D\(_S\), at ~1200 cm\(^{-1}\), and G\(_S\), at 1550 cm\(^{-1}\), bands are widely scattered. However, the scattering of both D\(_S\) and G\(_S\) band positions and the FWHM of the D\(_S\) and G\(_S\) bands is greater in case of the G + L + G + L approach in comparison to the L + L + G + G approach. In case of the 5-band deconvolution approach (inset in Figure 3h) the position of the D’-band is separated from the position of the G\(_S\)-band. In addition, the position and width of the G\(_S\)-band is better defined with the L + L + G + L + L approach (Figure 3h).

3.4. First Order Raman Spectra Deconvolution Results

The relation of the D- and G-band intensities, I\(_D\)/I\(_G\), has been widely used to describe the relative structural order of a carbon material [17,22,23,42], but a clear limit of I\(_D\)/I\(_G\) for practical applications has been demonstrated previously [18,24]. In addition, as discussed in Section 3.3, the interpretation of the I\(_D\)/I\(_G\) is not always straightforward, since I\(_D\)/I\(_G\) initially increases and then decreases along the graphitization pathway of a disordered carbon from Stage I to Stage III. It has been suggested to use the width of the D-band [18,43] or the G-band [27,29,44], instead of the I\(_D\)/I\(_G\) ratio, to evaluate the structural order of carbon materials. Ribeiro-Soares et al. [27] proposed that for the analysis of Raman spectrum of polycrystalline carbons heat-treated at T\(_{\text{syn}}\) ≥ 2000 °C, contributions from four Raman bands have to be used to characterize the spectrum, resulting in parameter A\(_{\Sigma D}\)/A\(_{\Sigma G}\),

\[
\frac{A_{\Sigma D}}{A_{\Sigma G}} = \frac{A_{D}' + A_D}{A_G + A_G'} \tag{4}
\]

where A\(_{D}'\), S\(_D\), A\(_G\), G\(_S\) are the areas of the bands located at ~1200 cm\(^{-1}\), ~1340 cm\(^{-1}\), ~1500 cm\(^{-1}\), and ~1600 cm\(^{-1}\), respectively.

Since the 5-band deconvolution model is best for the CDCs in our dataset, the parameter A\(_{\Sigma D}\)/A\(_{\Sigma G}\) was modified to include the D’ band,

\[
\frac{A_{\Sigma D}'}{A_{\Sigma G}} \approx \frac{A_{\Sigma D}'}{A_{\Sigma G} + D}, = \frac{A_{D}' + A_D}{A_G + A_G + A_{D'}} \tag{5}
\]

where A\(_{D'}\) is the area of the band situated at ~1620 cm\(^{-1}\).

With the increase in the T\(_{\text{syn}}\) of CDCs the FWHM\(_D\) decreases (Figure 4a). The decrease of the FWHM\(_D\) is linear for most CDCs with the slope of 0.2–0.3 cm\(^{-1}\)/°C. However, the width of the G-band does not change remarkably with the increase in T\(_{\text{syn}}\), as it stays around 55 cm\(^{-1}\) for most CDCs (Figure 4b). Ribeiro-Soares et al. [27] defined the upper limit of L\(_a\) for carbons in which case the FWHM\(_G\) is a useful parameter, L\(_a\) < 30 nm, but apparently there is a lower limit as well. Namely, if the L\(_a\) is too small the FWHM\(_G\) does
not change remarkably and stays in the order of ~55 cm\(^{-1}\). Mallet-Ladeira et al. [45] also found that for carbons with \(L_a\) \(2-5\) nm, the width of the G-band stays constant. Only the FWHM\(_G\) of C-Mo\(_2\)C 1100 and C-VC 1100 are considerably smaller (~30 cm\(^{-1}\)) than the FWHM\(_G\)s of the rest of the CDCs. These carbons have been classified to be in the Stage III of graphitization in Section 3. In addition, the stacking size, \(L_c\), of carbons derived from Mo\(_2\)C and VC increased considerably with \(T_{\text{syn}}\). Therefore, the FWHM\(_G\) is better suited to characterize carbons in the Stage III of graphitization or carbons with \(L_c > 2\) nm.

Interestingly, when the G-band region was modeled with the BWF function (the L + L + BWF approach), there is a slight systematic decrease in the FWHM\(_G\) with the increase in \(T_{\text{syn}}\) (Figure S4). In case of the L + L + BWF approach, the G-band is not separated from the D’-band. Instead, the spectral region of the G- and D’-band is fitted with one function, the BWF function. When the G- and D’-band have been separated (L + L + G + L + L), it can be seen, that it is actually the FWHM of the D’-band that decreases with the increase in \(T_{\text{syn}}\) (Figure S5).

The \(A_{\Sigma D}/A_{\Sigma G}\) ratio expressed in Equation (5), exhibits a clear dependence on the \(T_{\text{syn}}\) of the CDC under study (Figure 4c). These results follow the theory of Ribeiro-Soares et al. [27], based on which the extra bands, D\(_S\) and G\(_S\), are related to the D- and the G-band characteristics. The \(A_{\Sigma D}/A_{\Sigma G}\) parameter changes with a slope of 0.002 \(\text{°C}^{-1}\), except for C-Mo\(_2\)C, which yields a slope of 0.004 \(\text{°C}^{-1}\).

Unlike the FWHM\(_D\) and the FWHM\(_G\) parameters, the \(A_{\Sigma D}/A_{\Sigma G}\) ratio depends on the laser energy, \(E_{\text{laser}}\), used (Figure S6a–d). However, the power dependence of \(A_{\Sigma D}/A_{\Sigma G}\) on \(E_{\text{laser}}\) is not given as \(A_{\Sigma D}/A_{\Sigma G} = E^4\) (Figure S6d) as previously established in [27,46], but instead the exponent 4 is reduced to a somewhat lower (but positive) value, which is characteristic of small crystallite sizes in carbon particles [29].

In an earlier study on the Raman spectra of CDCs [23], the equation by Ferrari and Robertson [22] was used for the calculation of the coherent domain length based on Raman spectra. However, the Ferrari-Robertson equation is meant to characterize carbons with \(L_a < 2\) nm, which is not the case for the CDCs in this study. Ribeiro-Soares et al. [27] proposed an equation for calculating the coherent domain length from Raman spectra based on the \(A_{\Sigma D}/A_{\Sigma G}\) ratio. Using this equation, the coherent domain lengths for the studied CDCs are from 6 to 16 nm (Figure 4c, Figure S7 in SI) and increase systematically with increased \(T_{\text{syn}}\) for CDCs from the same precursor carbide, proving its applicability to characterize the structure of the studied CDCs. The coherent domain lengths calculated...
from the $A_{\Sigma D}/A_{\Sigma G}$ ratio are larger by 3–6 nm (average 4.4 nm) compared to the $L_a$ from WAXS analysis. The reason for this discrepancy might be that when a layer contains defects and/or is curved, the coherent domains seen by WAXS are diminished, whereas phonon propagation is not stopped [47]. Especially given that the D-band is not only activated near the edge of the graphene domain, but also near different defects in the graphene domain [48] and even curvature without defects activates the D-band [49]. The change of curvature in the graphene planes of C-Mo$_2$C was previously shown with contrast matched small-angle neutron scattering in [50]. Consequently, the coherent domains detected via Raman spectroscopy are somewhat larger in comparison to the $L_a$ values established by the WAXS analysis method. The curved graphene layers can indeed be longer than 10 nm, as has been shown by transmission electron microscopy of CDCs [7,10,23]. Therefore, the higher the number of defects and/or increased amount of curvature in the graphene layers the larger is the discrepancy between the Raman spectroscopy and WAXS data analyzed with the used methods. In conclusion, the coherent domain length calculated from the Raman spectra of disordered carbon reflects the length to which phonon propagation can occur in the graphene domain containing defects and the $L_a$ from WAXS is characteristic of the flat, mostly defect-free graphene domains in the carbon particle. Therefore, the WAXS and Raman analysis are complementary to each other and the simultaneous use of both methods is of high value for the characterization disordered non-graphitic carbon materials.

4. Conclusions

A combination of Raman spectroscopy and WAXS methods were applied on CDC materials obtained from six precursor carbides synthesized at various temperatures, from 500 to 1100 °C. The 5-peak fit of the Raman spectrum first order scattering region, suggested by Sadezky et al., obtained the most coherent results, i.e., the influence of the $T_{syn}$ on the peak parameters was the clearest. Results from both WAXS and Raman spectroscopy methods clearly showed the influence of the precursor carbide structure and chemical composition on stage of graphitization at equivalent synthesis temperature conditions. The graphitization of C-Mo$_2$C and C-VC at $T = 1100$ °C was evident from the considerable narrowing of the G-band and from the increase in average stacking size, $L_c$, values obtained from the WAXS data.

The use of the parameter $A_{\Sigma D}/A_{\Sigma G}$ for the determination of the coherent domain length from Raman spectra based on the Ribeiro-Soares method yielded the most reliable results when compared to the $L_a$ value obtained from WAXS data. The coherent domain length obtained from the Raman spectra was larger by ~4.4 nm in comparison to the average graphene layer extent, $L_a$, value obtained from WAXS. This discrepancy is attributed to the number of defects and curvature in the graphene domains in the CDC particles. Thus, based the results under analysis in this work, our combination methodology is suggested for the characterization of CDCs and possibly other disordered non-graphitic carbons.

Supplementary Materials: The following are available online at https://www.mdpi.com/2311-5629/7/1/29/s1, Figure S1: WAXS data of different CDCs and fit curve of (a) C-VC, (b) C-WC, (c) C-Mo$_2$C, (d) C-TiC and (e) C-WTiC$_2$ synthesized at different $T_{syn}$. Table S1: Parameters derived from WAXS patterns. Figure S2: The Raman spectra of (a) C-WTiC$_2$, (b) C-TiC, (c) C-Mo$_2$C, (d) C-Ta$_4$HfC$_5$, (e) C-VC and (f) C-WC synthesized at different $T_{syn}$ (noted in Figure) and measured with excitation laser wavelength 514 nm (laser energy 2.41 eV). The Raman spectra of all the investigated CDCs (laser wavelength 514 nm). Figure S3: The Raman spectra of (a) C-SiC 1000, (b) C-Mo$_2$C 700 and (c) Mo$_2$C 1000 measured with different laser excitation energies. Figure S4: Parameters (a) FWHM$_D$ (b) FWHM$_G$ and (c) $A_{\Sigma D}/A_{\Sigma G}$ (as expressed in Equation (5)). obtained from spectra ($E_{\text{laser}} = 2.41$ eV) of CDCs using different deconvolution methods (noted in Figure) plotted against the synthesis temperature ($T_{syn}$) of the CDC. Figure S5: The width of the D’-band (FWHM$_D$) vs. the synthesis temperature of the CDC (noted in Figure) obtained with the $L + L + G + L + L$ deconvolution approach. Figure S6: Different parameters obtained from the spectra of C-Mo$_2$C 700, C-Mo$_2$C 1000 and C-SiC 1000 using different deconvolution methods (noted in Figure) plotted against the excitation
laser energy ($E_{\text{laser}}$). Full width half maximum of the (a) G-band (FWHM$_{\text{G}}$); (b) D-band (FWHM$_{\text{D}}$) and (c) ratio $A_{\text{D}}/A_{\text{G}}$ (as expressed in Equation (5)). The lines given are guides to the eye. (d) The ratio $A_{\text{D}}/A_{\text{G}}$ vs. $E_{\text{laser}}$, where the line corresponds to the equation ratio $A_{\text{D}}/A_{\text{G}} = B E_{\text{laser}}^{-x}$, where parameters B and x are fitted and seen in the graph. Figure S7: The comparison of the coherent domain length calculated from Raman spectra using ratio $A_{\text{D}}/A_{\text{G}}$ and equation $L_\text{a} = 490/E_{\text{laser}}^{1/4}$ ($y$-axis) and the graphene domain lengths, $L_\text{v}$, from wide-angle X-ray scattering pattern analysis by CarbX ($x$-axis).

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