Superconducting Coherence Length and Magnetic Penetration Depth of a p-wave Holographic Superconductor

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A classical $SU(2)$ Einstein-Yang-Mills theory in 3+1 dimensional anti-de Sitter spacetime is believed to be dual to a p-wave superconductor in 2+1 dimensional flat spacetime. In order to calculate the superconducting coherence length $\xi$ of the holographic superconductor near the superconducting phase transition point, we study the perturbation of the gravity theory analytically. The superconducting coherence length $\xi$ is found to be proportional to $(1 - T/T_c)^{-1/2}$ near the critical temperature $T_c$. We also obtain the magnetic penetration depth $\lambda \propto (T_c - T)^{1/2}$ by adding a small external homogeneous magnetic field. The results agree with the Ginzburg-Landau theory.

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I. INTRODUCTION

The AdS/CFT correspondence\textsuperscript{[3-4]} has played an important role in understanding strongly coupled gauge theories. Recently, it also has been applied to superconductivity. The key point of the holographic theories for superconductors is that in the gravity theory, a black hole coupled with matter fields will have symmetry breaking solutions. There are mainly two holographic models of superconductors with different matter sectors. The first one is an Abelian-Higgs model which is the gravity dual of an s-wave superconductor with a scalar order parameter. The properties of this holographic superconductor model have been studied by many authors\textsuperscript{[5-31]}. The other one is an Einstein-Yang-Mills (EYM) theory in which the condensate carries angular momenta\textsuperscript{[32-43]}.

Gubser\textsuperscript{[44]} firstly presented an argument that by coupling the Abelian Higgs model to gravity with a negative cosmological constant, one can get solutions which spontaneously break the Abelian gauge symmetry via a charged complex scalar condensate near the horizon of the black hole. Hartnoll et al\textsuperscript{[5]} explored this Abelian-Higgs model of superconductivity further. They built an s-wave holographic (in the sense of AdS/CFT duality) superconductor with scalar order parameter which exhibits the basic features of a superconductor such as the existing of a critical temperature below which a charged condensate forms. The behaviors of the s-wave holographic superconductor under magnetic field have been studied in many papers\textsuperscript{[6-9, 16-19]}. Especially, Maeda and Okamura\textsuperscript{[8]} studied the superconducting coherence length $\xi$ of the s-wave holographic superconductor near the critical temperature $T_c$. They obtained that $\xi$ is proportional to $(1 - T/T_c)^{-1/2}$, which is in agreement with the Ginzburg-Landau theory.

The other holographic superconductor model which is an EYM model with fewer parameters whose Lagrangian is determined by symmetry principles is constructed later by Gubser\textsuperscript{[45]} and is shown to have spontaneous symmetry breaking solutions due to a condensate of non-Abelian gauge fields in the theory. Gubser and Pufu studied this model with both p-wave backgrounds and $(p + ip)$-wave backgrounds\textsuperscript{[32]}. Roberts and Hartnoll studied the $(p + ip)$-wave backgrounds and found two major nonconventional features for this holographic superconductor that are different from the s-wave counterpart. One is the existence of a pseudogap at zero temperature, and the other is the spontaneous breaking of time reversal symmetry\textsuperscript{[33]}. In our recent paper\textsuperscript{[39]}, we studied the phase transition properties of this model in constant external magnetic field. We found that the added magnetic field indeed suppresses the superconductivity. In the present paper, we further study the p-wave holographic superconductor composed of a non-Abelian gauge fields (the matter sector) and a black hole background (the gravity sector) by using perturbation theory near the critical temperature, following closely Maeda and Okamura\textsuperscript{[8]}. According to the Ginzburg-Landau
theory, the superconducting length, or the correlation length of the order parameter is an important characteristic parameter for a superconductor. Since the order parameter of the \( p \)-wave holographic superconductor is the vector operator dual to the charged non-Abelian gauge field, we investigate the static fluctuation of the condensed non-Abelian gauge field with nonvanishing spatial momentum along one spatial direction of the AdS boundary to get the correlation length \( \xi \). A homogeneous magnetic field in the field theory is added by placing a small vector potential in the matter sector. The magnetic penetration length \( \lambda \) is obtained by calculating the London current of the holographic superconductor.

The organization of this paper is as follows. In Section II, we reconstruct the superconducting solution of the EYM theory which is dual to a \( p \)-wave superconductor by perturbation techniques. Section III is devoted to the derivation of \( \xi \) by solving the eigenvalue equations from the perturbation. In Section IV we find that the London current can be induced by a homogeneous magnetic field, and the magnetic penetration length is also studied. The conclusion and some discussions are given in Section V.

**II. MODEL OF A \( p \)-WAVE HOLOGRAPHIC SUPERCONDUCTOR**

In this section, we review the gravity dual theory of the \( p \)-wave superconductor. The starting point of studying holographic superconductor at finite temperature \( T \) is choosing a black hole solution with a negative cosmological constant such that the Hawking temperature of the black hole is \( T \). The full EYM theory in 3+1 dimensional spacetime considered in Refs. \([32, 33, 45]\) has the following action

\[
S_{\text{EYM}} = \int \sqrt{-g} d^4x \left[ \frac{1}{2\kappa^4} \left( R + \frac{6}{L^2} \right) - \frac{L^2}{2g_{\text{YM}}^2} \text{Tr}(F_{\mu\nu}F^{\mu\nu}) \right], \tag{II.1}
\]

where \( g_{\text{YM}} \) is the gauge coupling constant and \( F_{\mu\nu} = T^aF^a_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu} - i[A_{\mu}, A_{\nu}] \) is the field strength of the gauge field \( A = A_{\mu}dx^\mu = T^aA^a_{\mu}dx^\mu \). For the SU(2) gauge symmetry, \([T^a, T^b] = i\epsilon^{abc}T^c\) and \( \text{Tr}(T^aT^b) = \delta^{ab}/2 \), where \( \epsilon^{abc} \) is the totally antisymmetric tensor with \( \epsilon^{123} = 1 \). The Yang-Mills Lagrangian becomes \( \text{Tr}(F_{\mu\nu}F^{\mu\nu}) = F^a_{\mu\nu}F^{a\mu\nu}/2 \) with the field strength components \( F^a_{\mu\nu} = \partial_{\mu}A^a_{\nu} - \partial_{\nu}A^a_{\mu} + \epsilon^{abc}A^b_{\mu}A^c_{\nu} \).

Working in the probe limit in which the matter fields do not backreact on the metric as in Refs. \([32, 33, 45]\) and taking the planar Schwarzchild-AdS ansatz, the black hole metric reads (we use mostly plus signature for the metric)

\[
ds^2 = -f(r)dt^2 + \frac{dr^2}{f(r)} + \frac{r^2}{L^2}(dx^2 + dy^2), \tag{II.2}
\]

where the metric function \( f(r) \) is

\[
f(r) = \frac{r^2}{L^2}(1 - \frac{r_0^3}{r^3}), \tag{II.3}
\]

\( L \) and \( r_0 \) are the radius of the AdS spacetime and the horizon radius of the black hole, respectively. They determine the Hawking temperature of the black hole,

\[
T = \frac{3r_0}{4\pi L^2}, \tag{II.4}
\]

which is also the temperature of the dual gauge theory living on the boundary of the AdS spacetime. Now we introduce a new coordinate \( z = r_0/r \). The metric \( \text{II.2} \) then becomes

\[
ds^2 = \frac{L^2 \beta^2(T)}{z^2}(-h(z)dt^2 + dx^2 + dy^2) + \frac{L^2 dz^2}{z^2h(z)}, \tag{II.5}
\]
where \( h(z) = 1 - z^3 \) and \( \beta(T) = r_0/L^2 = 4\pi T/3 \).

Using the Euler-Lagrange equations, one can obtain the equations of motion for the gauge fields,

\[
\frac{1}{\sqrt{-g}} \partial_\mu \left( \sqrt{-g} F^{a\mu
u} \right) + \epsilon^{abc} A_b^\mu F^c{}^{\mu\nu} = 0. \tag{II.6}
\]

For the \( p \)-wave backgrounds, the ansatz \([32]\) takes the following form,

\[
A = \phi(z) T^3 dt + w(z) T^1 dx. \tag{II.7}
\]

With this ansatz, we can derive the equations of motion for the two dimensionless quantities \( \tilde{w}(z) = w(z)/\beta(T) \) and \( \tilde{\phi}(z) = \phi(z)/\beta(T) \),

\[
\frac{d}{dz} \left( h(z) \frac{d\tilde{w}}{dz} \right) + \frac{\tilde{\phi}^2 \tilde{w}}{h(z)} = 0, \tag{II.8}
\]

and

\[
\frac{d^2 \tilde{\phi}}{dz^2} - \frac{\tilde{\phi} \tilde{w}^2}{h(z)} = 0. \tag{II.9}
\]

Here the \( U(1) \) subgroup of \( SU(2) \) generated by \( T^3 \) is identified to the electromagnetic gauge group \([45]\) and \( \phi \) is the electrostatic potential, which must vanish at the horizon for the gauge field \( A \) to be well-defined, but need not vanish at infinity. Thus the black hole can carry charge through the condensate \( w \), which spontaneously breaks the \( U(1) \) gauge symmetry. This is a Higgs mechanism, but there are Goldstone bosons corresponding to changing the directions of the condensate in real space or gauge space. They must be visible in the bulk as normal modes or (more likely) quasi-normal modes.

The exact solution of the equations of motion is

\[
\tilde{w} = 0, \quad \tilde{\phi} = \mu/\beta(T) - qz = q(1 - z), \tag{II.10}
\]

where \( \mu \) is interpreted as the chemical potential of the field theory. This trivial solution is parameterized by the dimensionless constant \( q \), which is related to the charge density of the dual field theory which couples to \( \mu \) as

\[
\langle J^0 \rangle = \frac{\delta S_{\text{on-shell boundary}}}{\delta A_0} = \frac{1}{2g_{\text{YM}}^2} \beta^2(T) q. \tag{II.11}
\]

The superconducting solution with non-vanishing \( \tilde{w} \) takes the following asymptotic form at the \( \text{AdS} \) boundary,

\[
\tilde{w} = \frac{\langle O \rangle}{\sqrt{2}} z + \cdots, \tag{II.12}
\]

\[
\tilde{\phi} = \mu/\beta(T) - qz + \cdots, \tag{II.13}
\]

where \( \langle O \rangle \) is the condensate of the charged operator dual to the field \( w \) and is the order parameter for the superconductivity phase. We demand that the constant term vanish since we require that there is no source term in field theory action for the operator \( \langle O \rangle \) \([32, 33]\).

According to numerical calculations \([32]\), the order parameter behaves as

\[
\langle O \rangle \sim (1 - T/T_c)^{1/2} \tag{II.14}
\]
near the critical phase transition point. For the reason of continuity, the solution at the critical temperature should be

$$\tilde{w}_c = 0, \tilde{\phi}_c = q_c (1 - z).$$

(II.15)

The non-trivial solution near the critical temperature can be obtained by a perturbation expansion in terms of $\epsilon = (1 - T/T_c)$ since $\epsilon$ is a small parameter. We expand $\tilde{w}(z)$ and $\tilde{\phi}(z)$ as

$$\tilde{w}(z) = \epsilon^{1/2} \tilde{w}_1(z) + \epsilon^{3/2} \tilde{w}_2(z) + \cdots ,$$

(II.16)

$$\tilde{\phi}(z) = \tilde{\phi}_c(z) + \epsilon \tilde{\phi}_1(z) + \cdots .$$

(II.17)

Substituting Eq. (II.16) and Eq. (II.17) into Eq. (II.9) and Eq. (II.8), we obtain equations for $\tilde{w}_1$ and $\tilde{\phi}_1$.

$$\mathcal{L}_w \tilde{w}_1(z) = 0,$$

(II.18)

$$\frac{d^2 \tilde{\phi}_1(z)}{dz^2} - \frac{\tilde{\phi}_c(z) \tilde{w}_1^2(z)}{h(z)} = 0,$$

(II.19)

where we have defined the following operator,

$$\mathcal{L}_w = - \left( \frac{d}{dz} h(z) \frac{d}{dz} + \frac{\tilde{\phi}_c^2(z)}{h(z)} \right).$$

(II.20)

III. THE SUPERCONDUCTING COHERENCE LENGTH

As an important parameter for superconductor, the superconducting coherence length is obtained from the complex pole of the static correlation function of the order parameter in Fourier space:

$$\langle \hat{O}(\vec{k}) \hat{O}(-\vec{k}) \rangle \sim \frac{1}{|\vec{k}|^2 + 1/\xi^2} .$$

(III.1)

The pole $|\vec{k}|^2$ can be calculated in the probe limit by perturbing the fields ($\tilde{w}$, $\tilde{\phi}$) in the equations of motion Eq. (II.9) and Eq. (II.8). It is enough to consider a linear perturbation with fluctuation of the field in the $y$-direction which takes the following form,

$$\delta \tilde{\phi}(z, y) dt = [\Phi(z, k) dt] e^{iky},$$

(III.2)

$$\delta \tilde{w}(z, y) = [W(z, k)] e^{iky}.$$

(III.3)

Using this perturbation, we get the following linearized equations for $W$ and $\Phi$:

$$\hat{k}^2 W = (\frac{d}{dz} h(z) \frac{d}{dz} + \frac{\tilde{\phi}_c^2}{h(z)}) W + \frac{2 \tilde{w} \tilde{\phi}}{h(z)} \Phi,$$

(III.4)

$$\hat{k}^2 \Phi = (h(z) \frac{d^2}{dz^2} - \tilde{w}^2) \Phi - 2 \tilde{\phi} \tilde{w} W.$$

(III.5)
where $\tilde{k} = k/\beta(T)$ is dimensionless.

Now, our task is to solve the eigenvalue equations near $T_c$ analytically. Using the perturbation expansions in Eq. (II.16) and Eq. (II.17), we get

\begin{equation}
- \tilde{k}^2 W = (\mathcal{L}_w - \frac{2\tilde{\phi}_c \tilde{w}_1}{\tilde{h}(z)}) W - \frac{2\tilde{\epsilon}^{1/2} \tilde{\phi}_c \tilde{w}_1}{\tilde{h}(z)} \Phi,
\end{equation}

\begin{equation}
- \tilde{k}^2 \Phi = (-h(z) \frac{d^2}{dz^2} + \epsilon \tilde{w}_1^2) \Phi + 2\epsilon^{1/2} \tilde{\phi}_c \tilde{w}_1 W.
\end{equation}

The boundary conditions for the two equations are

\begin{equation}
W(1) = \text{regular}, \quad \Phi(1) = 0
\end{equation}

at the horizon and

\begin{equation}
W(z) = (\text{const}) \times z + O(z^2),
\end{equation}

\begin{equation}
\Phi(z) = (\text{const}) \times z + O(z^2)
\end{equation}

near the AdS boundary $z = 0$.

The trivial solution is the zeroth order solution $\Phi_0$ and $W_0$ with $\tilde{k} = 0$,

\begin{equation}
\Phi = 0, \quad W_0 = \tilde{w}_1,
\end{equation}

where equation (II.18) is used. The non-trivial solutions can be obtained by a series expansion around the zeroth order solution in $\epsilon$,

\begin{equation}
W = \tilde{w}_1 + \epsilon W_1 + \epsilon^2 W_2 + \cdots,
\end{equation}

\begin{equation}
\Phi = \epsilon^{1/2} \tilde{\phi}_1 + \epsilon^{3/2} \Phi_2 + \cdots,
\end{equation}

\begin{equation}
\tilde{k}^2 = \epsilon \tilde{k}_1^2 + \epsilon^2 \tilde{k}_2^2 + \cdots.
\end{equation}

Using this expansion in Eq. (III.6) and Eq. (III.7), one has

\begin{equation}
- \tilde{k}_1^2 \tilde{w}_1 = \mathcal{L}_w \tilde{w}_1 - \frac{2\tilde{\phi}_c \tilde{w}_1}{\tilde{h}(z)} (\tilde{\phi}_1 + \Phi_1),
\end{equation}

\begin{equation}
\frac{d^2 \Phi_1}{dz^2} = \frac{2\tilde{\phi}_c \tilde{w}_1^2}{\tilde{h}(z)} = \frac{2d^2 \tilde{\phi}_1}{dz^2}.
\end{equation}

Eq. (III.15) can be solved for $\tilde{k}$ by defining an inner product for the states $w_I$ and $w_{II}$,

\begin{equation}
\langle w_I | w_{II} \rangle = \int_0^1 dz w_I^*(z) w_{II}(z).
\end{equation}

Using this inner product for Eq. (III.15) and $\tilde{w}_1$, with the fact that $\mathcal{L}_w \tilde{w}_1 = 0$, we have

\begin{equation}
\tilde{k}_1^2 \langle \tilde{w}_1 | \tilde{w}_1 \rangle = \frac{\langle \tilde{w}_1 \frac{2\tilde{\phi}_c \tilde{w}_1}{\tilde{h}(z)} \tilde{\phi}_1 \rangle}{h(z)} + 2\int_0^1 dz \frac{\tilde{\phi}_c \tilde{w}_1^2}{h(z)} \Phi_1.
\end{equation}
The first term of the above equation vanishes, which can be seen from the Hermiticity of $L_w$ and

$$L_w \hat{w}_2 = \frac{2\lambda}{\hbar(z)} \hat{\bar{\epsilon}}_1. \tag{III.19}$$

Eq.\,[III.19] is the equation of motion for $\hat{w}_2$ defined in (II.16). Using the fact that $\hat{k}^2 = \lambda \hat{k}_1^2$, the eigenvalue $\hat{k}$ in a first order approximation can be written as

$$\hat{k}^2 = \frac{N}{D} + O(\epsilon^2), \tag{III.20}$$

where

$$N = 2 \int_0^1 dz \frac{\tilde{\phi}_c \tilde{w}_2}{\tilde{h}(z)} \Phi_1 \quad \text{and} \quad D = \int_0^1 dz \psi_1^2. \tag{III.21}$$

Finally, the superconducting coherence length is given by

$$\xi = \frac{\epsilon^{-1/2}}{\beta(T_c)} \sqrt{\frac{D}{N}} + O(\epsilon^2) \propto \left(1 - \frac{T}{T_c}\right)^{-1/2}. \tag{III.22}$$

We have thus obtained the same critical exponent ($-1/2$) for $\xi$ as given by the Ginzburg-Landau theory.

**IV. THE LONDON EQUATION AND MAGNETIC PENETRATION LENGTH**

In order to calculate the magnetic penetration length for the holographic superconductor, we add a homogenous external magnetic field by assuming a perturbative non-zero $\delta A_y^0(z, x) = b(z)x$, where $\lim_{z \to 0} \delta A_y^0(z, x) = Bx$. Then the magnetic field in the field theory is $F_{xy} = \partial_x \delta A_y = B$. We still work in the probe limit where the magnetic field does not affect the metric. If we only focus on the neighborhood of $x = 0$, the equation of motion for $b(z)$ can be treated as decoupled from $\hat{w}$,

$$\left(\frac{d}{dz} h(z) \frac{d}{dz} - \hat{w}^2\right)b(z) = 0, \tag{IV.1}$$

where $b(z)$ must satisfy the regularity boundary condition at the horizon $z = 1$. This equation can also be solved by perturbation. We can expand $b(z)$ as

$$b(z) = b_0(z) + \epsilon b_1(z) + \cdots. \tag{IV.2}$$

Substituting this expansion and Eq.\,[III.16] into Eq.\,[IV.1], we obtain the equations,

$$\frac{d}{dz} h(z) \frac{d}{dz} b_0(z) = 0, \tag{IV.3}$$

$$\frac{d}{dz} h(z) \frac{d}{dz} b_1(z) - \hat{w}_1^2(z)b_0(z) = 0. \tag{IV.4}$$

The solution of Eq.\,[IV.3], which satisfies the required boundary conditions is

$$b_0(z) = C, \tag{IV.5}$$
where $C = B$ is a constant since the condition $\lim_{z \to 0} b(z) = B$ must be satisfied. So the solution of Eq. (IV.4) should be,

$$\frac{db}{dz} = -\frac{B}{h(z)} \int_z^1 dz_0 \tilde{w}_1^2(z_0).$$ \hspace{1cm} (IV.6)

Integrating the above equation, we have,

$$b(z) = B - \epsilon B \int_0^z \frac{dz_1}{h(z_1)} \int_{z_1}^1 dz_0 \tilde{w}_1^2(z_0) + O(\epsilon^2).$$ \hspace{1cm} (IV.7)

Using the fact that $B = \lim_{z \to 0} b(z)$ and $\delta A_y^{3(0)}(x) = \lim_{z \to 0} \delta A_y^3(z, x)$, we can rewrite Eq. (IV.7) as

$$\delta A_y^3(z, x) = \delta A_y^{3(0)}(x) \left(1 - \epsilon \int_0^z \frac{dz_1}{h(z_1)} \int_{z_1}^1 dz_0 \tilde{w}_1^2(z_0)\right) + O(\epsilon^2).$$ \hspace{1cm} (IV.8)

According to the AdS/CFT dictionary, we can read out the current $\langle J_y(x) \rangle$ near $T_c$ to be,

$$\langle J_y(x) \rangle = -\frac{L^2}{g_{YM}^2} \frac{4\pi T_c}{3} (1 - \frac{T}{T_c}) \int_0^1 dz \tilde{w}_1^2(z) \delta A_y^{3(0)}(x) + O(\epsilon^2),$$ \hspace{1cm} (IV.9)

or

$$\langle J_y(x) \rangle \sim -T_c \epsilon \delta A_y^{3(0)}(x).$$ \hspace{1cm} (IV.10)

This is similar to the London equation for real world superconductors,

$$J = -\frac{e^2}{m_s} \psi^2 A = -e_s n_s A,$$ \hspace{1cm} (IV.11)

where $e_s$ and $m_s$ are effective charge and mass of the order parameter respectively, and $n_s$ is the superfluid number density.

Comparing Eq. (IV.10) and Eq. (IV.11), we find that the superfluid density $n_s$ near the critical point in the field theory is

$$n_s \sim \epsilon T_c \sim T_c - T.$$ \hspace{1cm} (IV.12)

According to the Ginzburg-Landau theory, the magnetic penetration depth $\lambda$ is given by

$$\lambda \sim \frac{1}{\sqrt{n_s}}.$$ \hspace{1cm} (IV.13)

Then, we get the behavior of $\lambda$ in the vicinity of the critical temperature,

$$\lambda \propto (T_c - T)^{-1/2},$$ \hspace{1cm} (IV.14)

which is the expected result as in the Ginzburg-Landau theory.

V. CONCLUSION AND DISCUSSIONS

For the EYM theory with a $p$-wave backgrounds, we investigated the linear fluctuation of the condensation solution under the probe limit. By solving the linearized eigenvalue equations with only spatial momentum along one spatial direction by the perturbation method, we obtain that the
correlation length \( \xi \) diverges as \( \xi \sim (1 - T_c/T)^{-1/2} \) at the critical temperature. We also find that the magnetic penetration length behaves as \( \lambda \sim (T_c - T)^{-1/2} \) near the critical temperature. The London type equation Eq. [LV.10] implies a Meissner effect in the superconductor. These results are consistent with the Ginzburg-Landau theory, which supports the idea that the non-Abelian holographic model can be used to describe superconductors. Our results are similar to those of the \( s \)-wave holographic superconductor studied by Maeda and Okamura [8]. Though the holographic models have made many achievements, it is still a unsolved question why the Ginzburg-Landau behavior is expected and when one would expect deviations from it in these models. Recently, vortex solutions of the \( s \)-wave holographic superconductor in homogeneous external magnetic field have been studied in Ref. [16-19]. It will be interesting to study possible localized vortex solutions in the \( p \)-wave holographic superconductor.

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