Analysis of Hydraulic Characteristics According to the Cross-Section Changes in Submerged Rigid Vegetation

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ABSTRACT: Recently, not only Korea but also the world has been suffering from problems related to coastal erosion. The hard defense method has been primarily used as a countermeasure against erosion. However, this method is expensive and has environmental implications. Hence, interest in other alternative methods, such as the eco-friendly vegetation method, is increasing. In this study, we aim to analyze the hydraulic characteristic of submerged rigid vegetation according to the cross-sectional change through a hydraulic experiment and numerical simulation. From the hydraulic experiment, the reflection coefficient, transmission coefficient, and energy dissipation coefficient were analyzed according to the density and width of the vegetation zone. From numerical simulations, the flow field, vorticity distribution, turbulence distribution, and wave distribution around the vegetation zone were analyzed according to the crest depth, width, density, and multi-row arrangement distance of the vegetation zone. The hydraulic experiment results suggest that the transmission coefficient decreased as the density and width of the vegetation zone increased, and the multi-row arrangement condition did not affect the hydraulic characteristics significantly. Moreover, the numerical simulations showed that as the crest depth decreased, the width and density of vegetation increased along with vorticity and turbulence intensity, resulting in increased wave height attenuation performance. Additionally, there was no significant difference in vorticity, turbulence intensity, and wave height attenuation performance based on the multi-row arrangement distance. Overall, in the case of submerged rigid vegetation, the wave energy attenuation performance increased as the density and width of the vegetation zone increased and crest depth decreased. However, the multi-row arrangement condition did not affect the wave energy attenuation performance significantly.

1. Introduction

Recently, coastal erosion has become a major issue globally. Coastal erosion occurs owing to the rise in sea levels caused by global warming, invasion of high waves caused by abnormal temperatures, reduced soil supply caused by river development (e.g., dams), and change in the coastal environment caused by coastal development (e.g., port construction). When sand is lost owing to coastal erosion, the national land area decreases, thereby damaging those regions socially and economically. Countermeasures against coastal erosion include construction of gravity-based structures, such as groins and detached breakwaters, and beach nourishment. However, gravity-based structures are expensive and not eco-friendly, and beach nourishment is not a fundamental solution. Therefore, many studies have been conducted on countermeasures, and interest in the eco-friendly vegetation method has been increasing. While studies on vegetation have been conducted in the United States and Europe, such studies are not active in Korea.

Vegetation has different characteristics depending on various conditions, such as the shape of the material used, height of vegetation, and density and width of the vegetation zone, and many related studies were conducted on this topic (Anderso et al., 2011; Manca et al., 2010; Asano et al., 1988; Abdolahpour et al., 2017; Beudin et al., 2017; Hadadpour et al., 2019). Peruzzo et al. (2018) collected actual vegetation from nature and produced flexible vegetation with a similar shape. They performed a hydraulic model experiment and calculated the vegetation drag coefficient according to the density and depth of the vegetation zone. Wang et al. (2022) studied the wave transmission coefficient and drag coefficient of cylindrical flexible vegetation according to the depth and density through a hydraulic model experiment. Furthermore, various hydraulic model experiments on flexible vegetation have been performed (Blackmar et al., 2014; Maza...
et al., 2015). Additionally, Hu et al. (2014) studied wave height attenuation and the drag coefficient of vegetation according to the density and depth of the vegetation zone under the application of waves and flow for rigid cylindrical vegetation through a hydraulic model experiment. Van Veelen et al. (2020) performed a hydraulic model experiment on the effect of changes in the vegetation material on wave height attenuation and flow velocity using flexible and rigid vegetation with the same shape and size and different materials. Jeong and Hur (2016) developed a bidirectional coupled analysis technique by combining the discrete element method with the wave field model and numerically examined the wave attenuation effect according to the behavioral characteristics of vegetation.

As for submerged breakwaters, many studies have been conducted on the wave energy reduction effect by Bragg reflection that occurs when submerged breakwaters are arranged in multiple rows (Kirby and Anton, 1990; Cho et al., 2002; Cho, 2006). However, in the case of vegetation, studies on multi-row arrangement are insufficient.

In this study, a hydraulic model experiment and numerical model experiment were performed to analyze hydraulic characteristics according to the cross-section changes in submerged rigid vegetation. From the hydraulic model experiment, the hydraulic characteristics were analyzed according to the density and width of the vegetation zone and the cross-section change in multi-row arrangement. From the numerical model experiment, the flow field, vorticity distribution, turbulence distribution, and wave height distribution were analyzed according to the crest depth, density, width, and multi-row arrangement distance of the vegetation zone.

2. Hydraulic Model Experiment

2.1 Overview of the Hydraulic Model Experiment

The hydraulic model experiment was performed to analyze hydraulic characteristics according to the cross-section variation in submerged rigid vegetation. A wave flume with a length of 37 m, height of 1 m, and width of 0.6 m was used in the experiment. A piston-type wave generator was used in the experiment. A 30 cm-high impermeable floor with a front inclination of 1:30 was constructed to generate waves, and a capacitance wave gauge was used to measure the wave height.

Fig. 1 and Table 1 show the configuration of the wave flume and the cross-section conditions of the vegetation. The density, width, and multi-row arrangement of the vegetation zone were considered for the cross-section conditions. The rigid vegetation used in the experiment was made of an acrylic material, as shown in Fig. 2(a). Fig. 3 shows

![Fig. 1 Sketch of wave flume and experimental setup](image)

![Fig. 2 Vegetation used in the experiment: (a) specification of vegetation; (b) vegetation zone installed in the wave flume](image)

![Fig. 3 Sketch of frame fixed vegetation: (a) $\rho_V = 0.123$; (b) $\rho_V = 0.032$](image)

| Case | $V_h$ (cm) | $R$ (cm) | $B$ (cm) | $V_d$ (cm) | $\rho_V$ | Number of vegetation |
|------|------------|----------|----------|------------|---------|----------------------|
| R1   | 14.8       | 2.2      | 133      | -          | 0.123   | 972                  |
| R2   | 14.8       | 2.2      | 133      | -          | 0.032   | 255                  |
| R3   | 14.8       | 2.2      | 266      | -          | 0.123   | 1944                 |
| R4   | 14.8       | 2.2      | 133      | 133        | 0.123   | 1944                 |

Note: $V_h$ = vegetation height, $R$ = vegetation zone crest depth, $B$ = vegetation zone width, $V_d$ = distance of each vegetation zone, $\rho_V$ = vegetation zone density
the frame fixed vegetation. Figs. 3(a) and 3(b) represent cases in which the vegetation densities ($\rho_v$) are 0.123 and 0.032, respectively.

$$S(f) = 0.257H_s^2T_s^{-1}f^{-3}\exp[-1.03(T_sf)^{-1}]$$  \hspace{1cm} (1)

where $S(f)$ is the wave spectral density, $H_s$ is the significant wave height, $T_s$ is the significant wave period, and $f$ is the frequency.

Table 2 shows the incident wave conditions. The incident waves were irregular waves with a wave height of 2.67–11.0 cm and a period of 0.64–1.88 s. The Bretschneider–Mitsuyasu spectrum of Eq. (1) proposed by Mitsuyasu (1969) was used to generate the irregular waves. In Fig. 4, the theoretical values of the Bretschneider–Mitsuyasu spectrum are compared with those obtained from the experiment. Figs. 4(a) and 4(b) represent wave case 4 ($H_s = 5.33$ cm, $T_s = 0.95$ s) and wave case 16 ($H_s = 11.0$ cm, $T_s = 1.88$ s), respectively.

The reflection coefficient ($K_R$), transmission coefficient ($K_T$), and energy dissipation coefficient ($K_D$) were calculated to analyze hydraulic characteristics according to the cross-section changes in submerged rigid vegetation. The reflection coefficient ($K_R$) was calculated using the incident/reflected wave separation method proposed by Goda and Suzuki (1976). The transmission coefficient ($K_T$) and energy dissipation coefficient ($K_D$) were calculated using Eqs. (2) and (3), respectively.

$$K_T = \frac{H_T}{H_i}$$  \hspace{1cm} (2)

$$K_D = \sqrt{1-K_R^2-K_T^2}$$  \hspace{1cm} (3)

2.2 Results of the Hydraulic Model Experiment

A fixed-bed hydraulic model experiment was performed as a preliminary experiment to examine the hydraulic characteristics of wave propagation according to the cross-section changes in submerged rigid vegetation. In other words, $K_R$, $K_T$, and $K_D$ were calculated according to the density, width, and multi-row arrangement conditions of submerged rigid vegetation. Fig. 5 shows the distribution of the coefficients according to the wave steepness. Figs. 5(a), 5(b), and 5(c) represent the cases of $K_R$, $K_T$, and $K_D$, respectively.

2.2.1 Reflection coefficient

The reflection coefficient was not significantly different depending on the width and multi-row arrangement for Case R1 ($B = 133$ cm, $\rho_v = 0.123$), Case R3 ($B = 266$ cm, $\rho_v = 0.123$), and Case R4 ($B = 133$, $\rho_v = 0.032$).

Table 2 Incident wave condition (wave type = irregular, $h = 17$ cm)

| Wave case | $H_s$ (cm) | $T_s$ (s) | $L_s$ (cm) |
|-----------|------------|-----------|------------|
| 1         | 2.67       | 0.64      | 60.3       |
| 2         | 5.33       | 0.64      | 60.3       |
| 3         | 2.67       | 0.95      | 107.1      |
| 4         | 5.33       | 0.95      | 107.1      |
| 5         | 2.67       | 1.26      | 150.9      |
| 6         | 5.33       | 1.26      | 150.9      |
| 7         | 9.00       | 1.26      | 150.9      |
| 8         | 11.00      | 1.26      | 150.9      |
| 9         | 2.67       | 1.57      | 193.3      |
| 10        | 5.33       | 1.57      | 193.3      |
| 11        | 9.00       | 1.57      | 193.3      |
| 12        | 11.00      | 1.57      | 193.3      |
| 13        | 2.67       | 1.88      | 234.9      |
| 14        | 5.33       | 1.88      | 234.9      |
| 15        | 9.00       | 1.88      | 234.9      |
| 16        | 11.00      | 1.88      | 234.9      |

Note: $H_s =$ significant wave height, $T_s =$ significant wave period, $L_s =$ significant wave length
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133 cm, \( \rho_v = 0.123 \), which had the same density. It decreased slightly for Case R2 (\( B = 133 \) cm, \( \rho_v = 0.032 \)), which had lower density. This is because the reflected wave was generated similarly when the density of the vegetation zone was the same and the transmission area of waves increased as the vegetation density decreased.

2.2.2 Transmission coefficient

The transmission coefficient was found to decrease in Case R3 (\( B = 266 \) cm, \( \rho_v = 0.123 \)) and Case R4 (\( B = 133, 133 \) cm, \( \rho_v = 0.123 \)), where the density was the same and the width of the vegetation zone increased compared to that in Case R1 (\( B = 133 \) cm, \( \rho_v = 0.123 \)), and in Case R2 (\( B = 133 \) cm, \( \rho_v = 0.032 \)), where the width was identical and the density decreased. This is because an increase in the density and width of the vegetation zone induces more breaking waves at the crest of the vegetation zone.

2.2.3 Energy dissipation coefficient

The energy dissipation coefficient was the lowest in Case R2 (\( B = 133 \) cm, \( \rho_v = 0.032 \)), where the width and density of the vegetation zone were low, and showed a tendency to increase as the width and density of the vegetation zone increased. Additionally, there was no significant difference in hydraulic characteristics between Case R3 (\( B = 266 \) cm, \( \rho_v = 0.032 \)) and Case R4 (\( B = 133, 133 \) cm, \( \rho_v = 0.032 \)), which had the same density and width of the vegetation zone. In the case of submerged rigid vegetation, it was assumed that the multi-row arrangement condition does not affect the wave energy attenuation of the incident wave significantly.

3. Overview of the Numerical Model Experiment

The numerical model experiment was performed to analyze hydraulic characteristics according to the cross-section changes in the submerged rigid vegetation. As for the numerical model, LES-WASS-2D (Hur and Choi, 2008), a complete nonlinear two-dimensional (2D) model that can consider the energy dissipation by fluid resistance according to the characteristics of the permeable medium based on the porous body model and volume of fluid capable of considering the effect of permeability, was used.

3.1 Governing Equations

The basic equations of the numerical model consist of the continuity equation, modified Navier-Stokes equations, and advection equation, which are shown in Eq. (4), Eqs. (5)-(6), and Eq. (7), respectively.

\[
\frac{\partial (\gamma \rho u)}{\partial t} + \frac{\partial (\gamma \rho u^2)}{\partial x} = -\gamma \frac{\partial}{\partial x} \left( \gamma \rho (2 \frac{\partial u}{\partial x}) + \frac{1}{\gamma} \left( \gamma \rho (2 \frac{\partial u}{\partial x} + \frac{\partial w}{\partial z}) \right) \right)
- \frac{M_I - E_x - D_x}{\gamma} \rho \frac{\partial w}{\partial x} = \frac{2\rho v^2}{3} \frac{\partial^2 w}{\partial z^2} - \gamma g \rho w - M_I - E_x - D_x
\]

\[
\frac{\partial (\gamma F)}{\partial t} + \frac{\partial (\gamma Fu)}{\partial x} + \frac{\partial (\gamma Fw)}{\partial z} = F' \rho
\]

where \( u \) and \( w \) are the flow velocities in the \( x \) and \( z \) directions, respectively. \( q' \) is the flow density of the wave source. \( M_I \) and \( M_f \) are inertial resistance. \( E_x \) and \( E_z \) are laminar flow resistance. \( D_x \) and \( D_z \) are turbulence resistance. \( \gamma \) is the volumetric porosity. \( \gamma_u \) and \( \gamma_w \) are the area permeabilities along the \( x \) and \( z \) directions, respectively. \( t \) is the time, \( g \) is the gravitational acceleration, \( \rho \) is the fluid density, \( p \) is the pressure, \( \beta \) is the wave attenuation coefficient, \( F \) is the volume ratio occupied by the fluid in each grid, and \( v_t \) is the sum of the kinematic viscosity coefficient and kinematic eddy viscosity.
3.2 Vegetation Drag

The fluid resistance by vegetation \((RV)\) is given by Eq. (8).

\[
RV = \frac{1}{2} C_D \rho v \sqrt{v^2 + \frac{1}{2} C_M (1 - \gamma) \frac{\partial v}{\partial t}}
\]

where \(\Phi\) is the vegetation density, \(C_D\) is the drag coefficient, and \(C_M\) is the inertial resistance.

For \(C_D\), Eq. (9), which was presented by Lee et al. (2017a) by analyzing the experimental results of Wu and Cox (2015), was applied. \(C_D = 1.5\), as proposed by Sakakiyama and Kajima (1992), was applied.

\[
C_D = 1.4 \left(1 + \frac{15}{KC} \right)
\]

where \(KC\) is the Keulegan-Carpenter number.

3.3 Verification of the Numerical Wave Tank

To examine the validity of the numerical model, a 2D numerical wave tank was constructed, as shown in Fig. 6. The lengths of the \(x\) and \(z\) axes were set to be 1000 and 30 cm, respectively. The grid sizes of \(\Delta x\) and \(\Delta z\) were set to be 1 cm. Additional dissipation zones were prepared at both ends of the tank to prevent the reflection and re-reflection of waves.

### Table 3: Conditions of incident waves and vegetation cross-section used in this study

| Case  | Wave conditions | Vegetation zone |
|-------|----------------|-----------------|
|       |                |                 |
| R1-01 | 2.67, 0.64     | 2.2, 133        |
| R1-02 | 5.33, 0.64     | 2.2, 133        |
| R1-03 | 2.67, 0.95     | 2.2, 133        |
| R1-04 | 5.33, 0.95     | 2.2, 133        |
| R1-05 | 2.67, 1.26     | 2.2, 133        |
| R1-06 | 5.33, 1.26     | 2.2, 133        |
| R1-07 | 9.00, 1.26     | 2.2, 133        |
| R1-08 | 9.00, 1.26     | 2.2, 133        |
| R1-09 | 2.67, 1.57     | 2.2, 133        |
| R1-10 | 5.33, 1.57     | 2.2, 133        |
| R1-11 | 5.33, 1.57     | 2.2, 133        |
| R1-12 | 11.00, 1.57    | 2.2, 133        |
| R1-13 | 2.67, 1.88     | 2.2, 133        |
| R1-14 | 5.33, 1.88     | 2.2, 133        |
| R1-15 | 9.00, 1.88     | 2.2, 133        |
| R1-16 | 11.00, 1.88    | 2.2, 133        |
| R2-06 | 5.33, 1.26     | 2.2, 133        |
| R3-06 | 5.33, 1.26     | 2.2, 266        |
| R4-06 | 5.33, 1.26     | 2.2, 133, 133   |
| Note: | \(H_s\) = significant wave height, \(T_s\) = significant wave period, \(R\) = vegetation zone crest depth, \(B\) = vegetation zone width, \(\rho_V\) = vegetation zone density |
The numerical wave tank was compared and verified for the experimental conditions shown in Table 3 for the wave and vegetation cross-section conditions applied in the hydraulic model experiment. As the planar arrangement of rigid vegetation could not be reproduced owing to the characteristics of the 2D numerical model, the vegetation density was replaced with porosity in the numerical model.

In Fig. 7, the results of the hydraulic and numerical model experiments are compared. Figs. 7(a), 7(b), and 7(c) represent the reflection coefficient, transmission coefficient, and energy dissipation coefficient, respectively. For the reflection and transmission coefficients, the calculation results tended to be slightly higher than the experimental values when the wave steepness was low (near \( H_s/I_s = 0.02 \)). Overall, it was assumed that the calculated values reproduced the experimental values properly. In Fig. 8, the dotted lines show the ±10% range of the values of the hydraulic and numerical model experiments. Overall, it can be seen that the results of the numerical model experiment reproduced the reflection coefficient, transmission coefficient, and energy dissipation coefficient of the hydraulic model experiment appropriately.

### 4. Results of the Numerical Model Experiment

For a closer analysis of the hydraulic characteristics according to the cross-section changes in submerged rigid vegetation, which were examined in the numerical model experiment, the flow field, vorticity distribution, turbulence distribution, and wave height distribution around the submerged rigid vegetation were examined using the validated numerical wave tank. As shown in Fig. 6 and Table 4, additional experimental conditions compared to the hydraulic model experiment were applied to the numerical wave tank. A regular wave was used as the incident wave to facilitate the analysis. Additionally, the crest depth (\( B_r \)), width (\( B_l \)), density (\( \rho_v \)), and arrangement distance (\( V_d \)) were considered for the cross-section conditions of the vegetation zone.

### Table 4 Experimental conditions used in this study (wave conditions: \( H_s = 5.33 \) cm, \( T_s = 1.26 \) s)

| Case | \( R \) (cm) | \( B_r \) (cm) | \( B_l \) (cm) | \( \rho_v \) | \( V_d \) (cm) | \( V_d/\rho_v \) |
|------|-------------|---------------|---------------|------------|-------------|----------------|
| CR-00 | 2.2 | 0.413 | 133 | 0.887 | 0.123 | - | - |
| CR-01 | 0.0 | 0.000 | 133 | 0.887 | 0.123 | - | - |
| CR-02 | 1.0 | 0.188 | 133 | 0.887 | 0.123 | - | - |
| CR-03 | 3.0 | 0.563 | 133 | 0.887 | 0.123 | - | - |
| CR-04 | 4.0 | 0.750 | 133 | 0.887 | 0.123 | - | - |
| CR-05 | 5.0 | 0.938 | 133 | 0.887 | 0.123 | - | - |

Note: \( R \) = vegetation zone crest depth, \( H_s \) = incident wave height, \( B = \) vegetation zone width, \( L_s \) = incident wave length, \( \rho_v \) = vegetation zone density, \( V_d \) = distance of each vegetation zone.

The vorticity was calculated using Eqs. (10)–(14), which were proposed by Raffel et al. (1998) and Raffel et al. (2007) as in Lee et al. (2017b). Positive (+) values in red represent the counterclockwise direction and negative (−) values in blue represent the clockwise direction.

\[
\omega_{ix} = \frac{(\Omega_A + \Omega_B - \Omega_C - \Omega_D)}{4 \Delta x \Delta z}
\]

\[
\Omega_A = \frac{1}{2} \Delta x (u_{i-1,k-1} + 2u_{i,k-1} + u_{i+1,k-1})
\]

\[
\Omega_B = \frac{1}{2} \Delta z (w_{i+1,k-1} + 2w_{i+1,k} + w_{i+1,k+1})
\]

\[
\Omega_C = \frac{1}{2} \Delta x (u_{i+1,k+1} + 2u_{i,k+1} + u_{i-1,k+1})
\]

\[
\Omega_D = \frac{1}{2} \Delta z (w_{i-1,k+1} + 2w_{i-1,k} + w_{i-1,k-1})
\]
was calculated directly. For turbulence smaller than the grid size, the large eddy simulation technique that utilizes the sub-grid scale (SGS) model was used, and the Smagorinsky SGS model (Smagorinsky, 1963) expressed using the following equations was used.

\[ \nu_t = \nu + \nu_i \]

\[ \nu_i = (C_s \Delta)^2 |S| \]

\[ |S| = (2S_{ij}S_{ij})^{1/2} \]

\[ S_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \]

\[ \Delta = (\Delta x \Delta z)^{1/2} \]

where \( \nu \) is the kinematic viscosity coefficient, \( \nu_i \) is the kinematic eddy viscosity of SGS, \( \Delta \) is the filter length scale, and \( S_{ij} \) is the deformation tensor at the grid size. As for the \( C_s \) value, Schumann (1987) proposed a value ranging from 0.07 to 0.21, but 0.1 was used in this study because it was applied in a similar study (Christensen and Deigaard, 2001; Okayasu et al., 2005).

4.1 Flow Field, Vorticity Distribution, Turbulence Distribution, and Wave Height Distribution According to the Crest Depth

Figs. 9 and 10 show the flow field, vorticity distribution, and turbulence distribution according to the crest depth of the vegetation zone. Fig. 11 shows the wave height distribution around the submerged rigid vegetation according to the crest depth. From Figs. 9 and 10(a), clockwise (−) and counterclockwise (+) vortices can be

![Fig. 9](image)

**Fig. 9** Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-03, \( R/H_i = 0.563 \)): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution

![Fig. 10](image)

**Fig. 10** Flow field, vorticity distribution, and turbulence distribution around the vegetation owing to the ridge (Case CR-05, \( R/H_i = 0.938 \)): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution
confirmed in the vorticity distribution around the rigid vegetation. Additionally, a strong vorticity distribution is formed in the clockwise direction behind the vegetation, and the case of Fig. 9(a) with a low crest depth shows a stronger and wider vorticity distribution than the case of Fig. 10(a).

Figs. 9 and 10(b) show that a large turbulence distribution is formed at the crest and back of the submerged vegetation. This is because strong flow velocity corresponding to breaking waves occurs on the crest of the rigid vegetation. Additionally, the turbulence intensity on the crest of the rigid vegetation is higher and the turbulence distribution behind the rigid vegetation is wider in the case of Fig. 9(b). However, the crest depth was lower than that shown in the case of Fig. 10(b).

In Fig. 11, it can be seen that a slight partial standing wave field is formed in front of the submerged rigid vegetation under the influence of the reflected waves by the vegetation, and the height of waves that pass through the vegetation is reduced at the back by the energy dissipation caused by the resistance of the vegetation. This wave height attenuation effect tended to increase as the crest depth decreased as with the characteristics of typical submerged breakwaters.

4.2 Flow Field, Vorticity Distribution, Turbulence Distribution, and Wave Height Distribution According to the Width

Figs. 12–14 show the flow field, vorticity distribution, and turbulence distribution according to the width of the vegetation zone. Fig. 15 shows the wave height distribution around the submerged vegetation according to the width. From Figs. 12(a), 13(a), and 14(a), it can be seen that the flow velocity decreases as the width of the vegetation zone increases owing to a reduction in waves that propagate onto the vegetation crest, thereby forming a strong clockwise vorticity distribution behind the submerged vegetation. From Figs. 12(b), 13(b), and 14(b), it can be seen that a large turbulence distribution is formed at the crest and back of the submerged vegetation, and that the turbulence intensity behind the vegetation zone increases as the width of the zone increases. Therefore, the increasing wave height attenuation effect alongside the increase in the width of the submerged vegetation can be confirmed by the wave height distribution shown in Fig. 15.
Fig. 13 Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-08, $B/L_i = 1.107$): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution

Fig. 14 Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-11, $B/L_i = 1.773$): (a) Flow field and vorticity distribution; (b) Flow field and turbulence distribution

Fig. 15 Wave height distribution according to the change in the width of the vegetation zone ($B/L_i$)
The abovementioned results indicate that wave attenuation increases as the width of the submerged vegetation increases, and it is judged from the flow field, vorticity distribution, and turbulence distribution that submerged vegetation is more effective for wave attenuation as energy attenuation on the crest of the vegetation increases owing to the drag of the vegetation.

4.3 Flow Field, Vorticity Distribution, Turbulence Distribution, and Wave Height Distribution According to the Density

Figs. 16 and 17 show the flow field, vorticity distribution, and turbulence distribution according to the density of the vegetation zone. Fig. 18 shows the wave height distribution around the submerged vegetation according to the density. From Figs. 16(a) and 17(a), it can be seen that the flow velocity on the vegetation crest increases as the density of the vegetation zone increases, thereby forming a strong clockwise vorticity distribution behind the submerged vegetation. From Figs. 16(b) and 17(b), it can be seen that a large turbulence distribution is formed at the crest and back of the submerged vegetation, confirming that the turbulence intensity at the back increases as the density of the vegetation increases. Therefore, the increasing wave height attenuation effect alongside the increase in the density of the submerged vegetation can be confirmed by the wave height distribution shown in Fig. 18. Additionally, from Fig. 18, wave attenuation owing to the change in the wave on the vegetation crest can be confirmed together with the increase in reflectivity as the density of the submerged vegetation increases.

**Fig. 16** Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-00, $\rho_V = 0.123$): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution

**Fig. 17** Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-17, $\rho_V = 0.213$): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution
The above results indicate that wave attenuation increases as the density of the submerged vegetation increases, and it is judged from the flow field, vorticity distribution, and turbulence distribution that submerged vegetation is more effective for wave attenuation as its density increases owing to the difference in energy attenuation at the crest and back of the vegetation.

4.4 Flow Field, Vorticity Distribution, Turbulence Distribution, and Wave Height Distribution According to the Arrangement Distance

Figs. 19–21 show the flow field, vorticity distribution, and turbulence distribution according to the multi-row arrangement distance of the vegetation zone. Fig. 22 shows the wave height distribution around the submerged vegetation according to the arrangement distance. From Figs. 19(a), 20(a), and 21(a), it can be seen that the flow velocity decreases as the arrangement distance increases owing to a reduction in waves that propagate onto the vegetation crest, thereby forming a strong clockwise vorticity distribution behind the submerged vegetation. From Figs. 19(b), 20(b), and 21(b), it can be seen that a large turbulence distribution is formed at the crest and back of the submerged vegetation, confirming that similar turbulence intensity occurs despite the increase in arrangement distance. Therefore, the similar wave height attenuation effect despite the increase in arrangement distance can be confirmed by the wave height distribution shown in Fig. 22.

The abovementioned results indicate that similar wave attenuation occurs regardless of the arrangement distance. From the flow field, vorticity distribution, and turbulence distribution, we assumed that similar energy attenuation occurs owing to the drag of the submerged vegetation. This result is contrary to the wave attenuation effect by Bragg reflection that occurs when submerged breakwaters are arranged in multiple rows. This is because the submerged vegetation has relatively low reflectivity than submerged breakwaters owing to its low porosity. However, additional examinations are required for the wave energy reduction effect according to the multi-row arrangement and arrangement distance of the submerged rigid vegetation.

![Fig. 18 Wave height distribution according to the changes in vegetation zone density ($\rho_v$)](image)

Fig. 18 Wave height distribution according to the changes in vegetation zone density ($\rho_v$)

The above results indicate that wave attenuation increases as the density of the submerged vegetation increases, and it is judged from the flow field, vorticity distribution, and turbulence distribution that submerged vegetation is more effective for wave attenuation as its density increases owing to the difference in energy attenuation at the crest and back of the vegetation.

4.4 Flow Field, Vorticity Distribution, Turbulence Distribution, and Wave Height Distribution According to the Arrangement Distance

Figs. 19–21 show the flow field, vorticity distribution, and turbulence distribution according to the multi-row arrangement distance of the vegetation zone. Fig. 22 shows the wave height distribution around the submerged vegetation according to the arrangement distance. From Figs. 19(a), 20(a), and 21(a), it can be seen that the flow velocity decreases as the arrangement distance increases owing to a reduction in waves that propagate onto the vegetation crest, thereby forming a strong clockwise vorticity distribution behind the submerged vegetation. From Figs. 19(b), 20(b), and 21(b), it can be seen that a large turbulence distribution is formed at the crest and back of the submerged vegetation, confirming that similar turbulence intensity occurs despite the increase in arrangement distance. Therefore, the similar wave height attenuation effect despite the increase in arrangement distance can be confirmed by the wave height distribution shown in Fig. 22.

The abovementioned results indicate that similar wave attenuation occurs regardless of the arrangement distance. From the flow field, vorticity distribution, and turbulence distribution, we assumed that similar energy attenuation occurs owing to the drag of the submerged vegetation. This result is contrary to the wave attenuation effect by Bragg reflection that occurs when submerged breakwaters are arranged in multiple rows. This is because the submerged vegetation has relatively low reflectivity than submerged breakwaters owing to its low porosity. However, additional examinations are required for the wave energy reduction effect according to the multi-row arrangement and arrangement distance of the submerged rigid vegetation.

![Fig. 19 Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-18, $V_d/L_i = 0.293$): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution](image)
Fig. 20 Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-19, $V_d/L_i = 0.593$): (a) flow field and vorticity distribution; (b) flow field and turbulence distribution

Fig. 21 Flow field, vorticity distribution, and turbulence distribution around the vegetation (Case CR-20, $V_d/L_i = 0.887$); flow field and vorticity distribution; (b) flow field and turbulence distribution

Fig. 22 Wave height distribution according to the arrangement distance of the vegetation zone ($V_d/L_i$)
5. Conclusions

A hydraulic model experiment and a numerical model experiment were performed to analyze the hydraulic characteristics according to the cross-section changes in the submerged rigid vegetation. Using the hydraulic model experiment, the reflection coefficient, transmission coefficient, and energy dissipation coefficient were analyzed according to the density, width, and multi-row arrangement distance of the vegetation zone. Using the numerical model experiment, the flow field, vorticity distribution, turbulence distribution, and wave height distribution were analyzed according to the crest depth, density, width, and multi-row arrangement distance of the vegetation zone. The following conclusions were drawn based on the results obtained.

1. From the hydraulic model experiment, the reflection coefficient, transmission coefficient, and energy dissipation coefficient according to the cross-section changes in vegetation were calculated. Additionally, the flow field, vorticity distribution, turbulence distribution, and wave height distribution according to the cross-section changes in vegetation were analyzed using the numerical wave tank, which was validated by comparing the results obtained from the hydraulic model experiment.

2. The results of the hydraulic model experiment showed that the reflection coefficient decreased as the density of the vegetation zone decreased. This is because the transmission area of waves increased in front of the vegetation zone. Additionally, we found that the transmission coefficient increased as the density and width of the vegetation zone increased. This is because more breaking waves were induced at the crest of the vegetation zone as the density and width of the vegetation zone increased.

3. The results of the numerical model experiment showed that the distribution and intensity of vorticity and turbulence increased at the crest and back of the vegetation zone as the crest depth of the vegetation zone decreased and width and density increased, thereby increasing the wave height attenuation performance.

4. When the total width of the vegetation zone was identical, the vorticity distribution, turbulence distribution, and wave height distribution according to the multi-row arrangement and arrangement distance were found to be similar. However, we believe that more examinations are required for wave energy attenuation characteristics according to the multi-row arrangement and arrangement distance of the submerged rigid vegetation.

Conflict of Interest

No potential conflict of interest relevant to this article was reported.

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