Rupture risk assessment for multiple intracranial aneurysms: why there is no need for dozens of clinical, morphological and hemodynamic parameters

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Abstract

Introduction: A multitude of approaches have been postulated for assessing the risk of intracranial aneurysm rupture. However, the amount of potential predictive factors is not applicable in clinical practice and they are rejected in favor of the more practical PHASES score. For the subgroup of multiple intracranial aneurysms (MIAs), the PHASES score might severely underestimate the rupture risk, as only the aneurysm with the largest diameter is considered for risk evaluation.

Methods: In this study, we investigated 38 patients harboring a total number of 87 MIAs with respect to their morphological and hemodynamical characteristics. For the determination of the best suited parameters regarding their predictive power for aneurysm rupture, we conducted three phases of statistical evaluation. The statistical analysis aimed to identify parameters that differ significantly between ruptured and unruptured aneurysms, show smallest possible correlations among each other and have a high impact on rupture risk prediction.

Results: Significant differences between ruptured and unruptured aneurysms were found in 16 out of 49 parameters. The lowest correlation were found for gamma, aspect ratio (AR1), aneurysm maximal relative residence time (Aneurysm_RRT_max) and aneurysm mean relative residence time. The data-driven parameter selection yielded a significant correlation of only two parameters (AR1 and the Aneurysm_RRT_max) with rupture state (area under curve = 0.75).

Conclusion: A high number of established morphological and hemodynamical parameters seem to have no or only low effect on prediction of aneurysm rupture in patients with MIAs. For best possible rupture risk assessment of patients with MIAs, only the morphological parameter AR1 and the hemodynamical parameter Aneurysm_RRT_max need to be included in the prediction model.

Keywords: hemodynamics, morphology, multiple intracranial aneurysms, rupture risk assessment, unruptured intracranial aneurysms
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with MIAs are more likely to have a familial predisposition for IA formation and longitudinal studies showed a higher rate of aneurysm growth.5,9,10 Furthermore, the discussion about the higher risk rupture of MIAs compared with singular IAs forms a controversy in the treatment decision of these patients.11–15

Over the last decade a huge number of morphological and hemodynamic parameters as predictive factors for aneurysm rupture has been introduced.16–23 As a limitation, these studies do not specifically address the subgroup of MIAs. Furthermore, the amount of potential predictive factors is not practical and thus does not impact rupture risk assessment in clinical practice. As a consequence, treatment decisions in most neurovascular centers for MIAs are mainly based on the PHASES score. This is indeed practical but might severely underestimate the rupture risk for the MIA subgroup, as only the aneurysm with the largest diameter is considered for risk evaluation.24 Another approach to estimate the rupture risk of IAs is the establishment of reliable regression models, which combine morphological and hemodynamic predictive factors. Namely, two regression models showed a high area under the curve (AUC) of 0.84 and 0.86, respectively.20,25 Nonetheless, neither of these models addresses the different subgroups of IAs specifically.

We investigated how many parameters are necessary for aneurysm status prediction and how much prediction power the potential parameters have. We focused exclusively on morphological and hemodynamic parameters. Therefore, we raised the number of these parameters from 13 used by Xiang et al.20 to 49 (21 morphological and 28 hemodynamic) parameters. Moreover, we aimed to keep the influence of patient characteristics on rupture of IAs as constant as possible by using data from 38 patients with MIAs, with one ruptured and at least one unruptured IA. Based on this unique approach, the patient characteristics do not influence the results, yet they allow a clear relation of both morphological and hemodynamic characteristics to rupture status.

Our study, first, we investigated the statistical significance of the difference between ruptured intracranial aneurysms (RIAs) and unruptured intracranial aneurysms (UIAs) with respect to their parameters. We selected the most important (with respect to the predictive power) parameters for further analyses. In the second phase, we examined whether the parameters contain redundant information by calculating correlations between them. We chose the parameter combinations with low information overlap for a regression analysis, which should be able to predict the aneurysm rupture status.

Materials and methods

After obtaining permission from the local ethics committee of the Hanover Medical School and the Otto-von-Guericke University, we retrospectively analyzed the data of all patients who presented with a SAH and were treated at our Neurovascular Center in Hanover and Magdeburg between 2012 and 2019. Inclusion criteria for this study were: all patients had at least two IAs, of which one had ruptured; all patients had undergone complete neuroradiological diagnostics including three-dimensional (3D) rotational angiography (RA) and the ruptured aneurysm was identified by intraoperative findings or computed tomography scan imaging. Patients who suffered from a SAH and did not present with another IA were excluded. In addition, all patients who had not undergone complete neuroradiological diagnostic were excluded. Furthermore, all patients who suffered from fusiform aneurysms, additional vascular anomalies (e.g. arteriovenous malformation, Moyamoya disease, dural arteriovenous fistula) or polycystic kidney disease were excluded.

A total of 38 patients harboring 87 IAs were included in this study; the mean age at SAH was 57.5 years. Patients characteristics are shown in Table 1.

Table 1.

Extraction of morphological and hemodynamic parameters

From the reconstructed and digital subtracted 3D RA dataset, 3D surface models were extracted according to Saalfeld et al.26 Next, we applied a semiautomatic neck curve segmentation, which also allows for the automatic extraction of 21 morphological parameters27 (Figure 1, Table 2). In contrast to manual measurement, an improved objective observation of the 3D vessel, as well as the possibility of the analysis of large volumes of data in a short time can be exploited. Based on the 3D surface model, highly resolved, time-dependent blood flow simulations using computational fluid dynamics were carried out in accordance with Berg et al.28 We included the following boundary conditions: scaled flow rates at the inlet opening from a healthy volunteer,29 pressure distribution at
the outlet openings, and rigid vessel walls. Blood was treated as a Newtonian fluid (1055 kg/m³) with constant viscosity (4 mPa·s) and the flow was assumed to be laminar. For each case, the simulation of three cardiac cycles was performed, of which only the last cycle was included in the analysis of the 28 extracted hemodynamic parameters (Figure 2, Table 2).

**Statistical analysis**
For the determination of the best suited parameters based on their predictive power we conducted three phases of statistical evaluation using R version 3.5.3.

In the first phase of the statistical analysis, we analyzed the parameters in more detail with respect to differences between RIAs and UIAs. As each patient of our study harbored a RIA and at least one UIA, we tested the possible superiority of a multilevel model compared with hierarchical logistic regression analysis. If this was the case, a multilevel model was employed. Otherwise, deviation from normal distribution was tested based on histogram analysis in combination with skew and kurtosis values divided by two standard errors. Because significant values in large samples arise from even small deviations from normality, we decided on a threshold of 3.5. If the variables exceeded this threshold, they were transformed by means of logarithmization. Parameters with several equal (zero) values were analyzed with the nonparametric Wilcoxon rank-sum test, while the remaining parameters were evaluated with parametric Welch two sample t-test. The underlying dataset was screened with respect to outliers and plausibility of values. IAs were excluded from further analysis due to outliers (mean ± 4 × standard deviation) in the data, which affected nine parameters of six aneurysms. Another IA was excluded due to a failure of the neck reconstruction.

For the second phase, correlation analysis between significant parameters from phase one was evaluated to identify independent parameters which do not correlate with each other. We used parametrical Pearson product-moment correlation for normally distributed parameters and nonparametrical Spearman’s rank-sum correlation for non-normally distributed parameters.

In phase three, a hierarchical logistic regression analysis was performed based on the groups of parameters with low correlations. Parameters were added to the model in order of their importance, for example, effect size, calculated in phase one and included in the model if they improved its prediction quality. For the logistic regression analyses, we had to exclude four IAs, as not all parameter values (problems of parameter extraction occurred due to certain complex, highly irregular aneurysm morphologies) were present in all variables.

In order to provide a qualitative comparison with the current most well-established prediction model, we applied the PHASES score to our MIA patient collective. We calculated the PHASES...
Results

Significant differences between RIAs and UIAs were found in 13 out of 21 morphological parameters. However, the results show medium effects ($0.30 \leq r \leq 0.50$). Analysis of hemodynamic parameters yields differences between RIA and UIA for 3 out of 28 parameters. However, only one variable showed a medium effect (Aneurysm_RRT_max); other variables showed small effects.

In the second phase, we investigated the correlation of the 16 parameters identified in phase one using Spearman’s rank-sum test. Morphological parameters showed a correlation with each other, with the exception of gamma ($0.05 < r < 0.30$) and AR1. Correlations between hemodynamic parameters showed medium and large effects. In terms of the correlation between morphological and hemodynamic parameters, Aneurysm_RRT_max and Aneurysm_RRT_mean showed the lowest correlations.

The presentation of the test statistics from the first and the second phase of the statistical analysis are published as online supplemental material.

Based on the results of phase two, we developed three models each containing two morphological and two hemodynamic parameters (which also exhibit a relatively low correlation to each other):

Figure 1. Illustration of the morphological parameters Hmax, Wmax, Hortho, Wortho and Dmax [a]. The semi-automatically determined neck curve separates the aneurysm from the parent vessel surface mesh and area $A_a$ and volume $V_a$ of the aneurysm sac are extracted [b]. The surface area of the ostium is extracted for the reconstructed neck curve [OA1] as well as for the projected neck curve [OA2] [c]. The angle-related parameters account for the tilting of the aneurysm [d–f]. Even if the aspect ratio is identical, $\gamma$ and $\Delta\alpha\beta$ differ [e, f].

$A_a$, Surface area of the aneurysm.

$D_{max}$, Maximum diameter of the aneurysm.

$H_{max}$, Maximum height of the aneurysm.

$H_{ortho}$, Height of the aneurysm, measured vertically to the aneurysm neck.

$V_a$, Volume of the aneurysm.

$W_{max}$, Maximum width perpendicular to $H_{max}$.

$W_{ortho}$, Maximum width perpendicular to $H_{ortho}$.
| Parameter                  | Definition                                                                 |
|----------------------------|----------------------------------------------------------------------------|
| Morphological parameters   |                                                                            |
| $H_{\text{max}}$          | Maximum height of the aneurysm                                            |
| $W_{\text{max}}$          | Maximum width perpendicular to $H_{\text{max}}$                          |
| $D_{\text{max}}$          | Maximum diameter of the aneurysm                                          |
| $H_{\text{ortho}}$        | Height of the aneurysm, measured vertically to the aneurysm neck          |
| $W_{\text{ortho}}$        | Maximum width perpendicular to $H_{\text{ortho}}$                        |
| $N_{\text{max}}$          | Maximum diameter of the aneurysm neck                                     |
| $N_{\text{avg}}$          | Average diameter of the aneurysm neck                                     |
| AR1                        | Aspect ratio 1 ($H_{\text{ortho}}/N_{\text{max}}$)                      |
| AR2                        | Aspect ratio 2 ($H_{\text{ortho}}/N_{\text{avg}}$)                      |
| EI                         | Ellipticity index (1–18^(1/3) $V_{\text{CH}}^{*2/3}/A_{\text{CH}}$)     |
| NSI                        | Nonsphericity index (1–18^(1/3) $V^{2/3}/A_{\text{avg}}$)               |
| UI                         | Undulation index (1–$V/V_{\text{CH}}$)                                    |
| $A_{\text{a}}$            | Aneurysm area (Surface area of the aneurysm)                             |
| OA1                        | Ostium area 1 (Area of the aneurysm ostium)                              |
| OA2                        | Ostium area 2 (Area of the aneurysm ostium with the neck curve projected onto a plane) |
| $V_{\text{a}}$            | Volume of the aneurysm                                                   |
| $V_{\text{CH}}$           | Volume of the convex hull of the aneurysm                                 |
| $A_{\text{CH}}$           | Surface area of the convex hull of the aneurysm                           |
| Alpha                      | Angle at B1 describing angle from base line to the dome point            |
| Beta                       | Angle at B2 describing angle from base line to the dome point            |
| Gamma                      | Angle on the aneurysm dome depending on base points                      |
| Hemodynamic parameters     |                                                                            |
| $A_{\text{inflow}}$       | Area of the inflow at aneurysm ostium                                    |
| $A_{\text{inflow\_mean}}$ | Mean area of the inflow at aneurysm ostium                               |
| NeckFlowRate               | Flow rate that enters the aneurysm at a certain time point               |
| MeanNeckInflowRate         | NeckFlowRate averaged over one cardiac cycle                             |
| $Q_{\text{vessel}}$       | Flow rate within the parent vessel                                       |
| $Q_{\text{vessel\_mean}}$ | Mean flow rate within the parent vessel                                  |
| $F_{\text{aneurysm}}$     | Shear stress of the aneurysm area                                        |
| $F_{\text{high}}$         | Shear stress of the aneurysm area under high wall shear stress            |
| $F_{\text{low}}$          | Shear stress of the aneurysm area under low wall shear stress             |
| Aneurysm_AWSS\_mean       | Mean average wall shear stress of the aneurysm                           |
| Aneurysm_AWSS\_max        | Maximal average wall shear stress of the aneurysm                        |
| $A_{\text{high}}$         | Area of the aneurysm under high wall shear stress                         |
| $A_{\text{low}}$          | Area of the aneurysm under low wall shear stress                          |

(Continued)
Table 2. (Continued)

| Parameter                  | Definition                                                                 |
|----------------------------|-----------------------------------------------------------------------------|
| MeanAWSS_vessel            | Mean average wall shear stress of the parent vessel                          |
| VarianceAWSS_vessel        | Variance of the wall shear stress of the parent vessel                       |
| sdAWSS_vessel              | Standard deviation of average wall shear stress occurring on the parent vessel |
| AWSS_vessel_high           | Abnormally high average wall shear stress on the parent vessel               |
| AWSS_vessel_low            | Abnormally low average wall shear stress on the parent vessel                |
| Aneurysm_OSI_mean          | Mean oscillatory shear index of the aneurysm                                |
| Aneurysm_OSI_max           | Maximal oscillatory shear index of the aneurysm                             |
| Aneurysm_RRT_mean          | Mean relative residence time of the aneurysm                               |
| Aneurysm_RRT_max           | Maximal relative residence time of the aneurysm                             |
| ICI                        | Inflow concentration index                                                  |
| ICI_mean                   | Mean inflow concentration index                                              |
| SCI                        | Shear concentration index                                                   |
| HSI                        | High shear index                                                            |
| LSI                        | Low shear index                                                             |
| LSA                        | Low shear stress area percentage                                            |

Figure 2. Exemplary illustration of relevant hemodynamic parameters. Upper row (flow visualization) from left to right: cycle-averaged streamlines color-coding the velocity magnitude; mean isosurface velocity highlighting occurring flow structures; vortex core lines revealing complex flow and the presence of interacting vortices. Lower row (hemodynamic surface forces) from left to right: cycle-averaged wall shear stress (AWSS); oscillatory shear index (OSI); relative residence time (RRT).
Model A: AR1, Aneurysm_RRT_max, W_{ortho}, A_{low}
Model B: AR1, W_{ortho}, Aneurysm_RRT_mean, A_{low}
Model C: W_{ortho}, gamma, Aneurysm_RRT_mean, A_{low}

In the third phase, we constructed the regression models using forward selection. We tested each model (Model A–C) for improvement of prediction quality by adding parameters. The analysis revealed a combination of two parameters (AR1, $p = 0.01$ and Aneurysm_RRT_max, $p = 0.04$) with significant improvement of the model. The AR1 was here defined as the height of the aneurysm neck measured vertically to the aneurysm neck ($H_{ortho}$) divided by the maximum diameter of the aneurysm neck ($N_{max}$), while the AR2 was defined as $H_{ortho}$ divided by the average diameter of the aneurysm neck ($N_{avg}$). Aneurysm_RRT_max describes the maximal relative residence time of the aneurysm. Both parameters account together for 13% of the variance in the rupture status ($R^2 = 0.13$). The AUC of the final model was 0.75. (Figure 3).

Analysis of PHASES score distribution showed that 84% of the patients had a PHASES score of 0–6 points with an estimated 5-year rupture risk of <2%. We observed the following distribution of corresponding 5-year rupture risk in our patient cohort of patients with MIA: 47% of all patients had a 5-year rupture risk of <1%, 37% of all patients had a 5-year rupture risk of 1–1.9%, 11% of all patients had a 5-year rupture risk of 2–4.9% and 5% of all patients had a 5-year rupture risk of >5%. (Figure 4).

**Discussion**

The concept of IAs as a homogenous disease is challenged by recent studies. Among IA subgroups, MIAs constitute one of the most
important subgroups of patients harboring IAs, accounting for 20% of all IA patients. In clinical practice, the presence of MIAs has an impact on treatment decisions. Although, several studies elucidated the morphological and hemodynamic characteristics of MIA, thus far a prediction model for MIAs has not been presented.

The PHASES score is established in the daily clinical practice in neurovascular centers; however, several limitations considering the rupture risk in the subgroup of MIAs are apparent. Although other studies already questioned the aneurysm size as the key parameter in rupture risk prediction, the PHASES score still attributes this parameter as having the highest impact on aneurysm rupture. Furthermore, the PHASES score only integrates the cumulative rupture risk of patients with MIAs by taking earlier SAH into account. It is questionable whether this approach is able to reproduce the real cumulative rupture risk of patients with MIAs. Therefore, the introduction of a new prediction model based on morphological and hemodynamic parameters might lead to a better prediction.

As MIAs have the peculiarity of a location within the same patient, we aimed to use a nested comparison of IAs within the same patient. This approach would have been able to abbreviate the influence of patient characteristics on rupture risk of MIAs and lead to a stronger emphasis on morphological and hemodynamic characteristics. However, the application of a multilevel model only led in 6 of 49 parameters to a better model fit. Therefore, this finding implicates no significant impact of patients’ characteristics on the prediction of aneurysm rupture in our cohort.

The first phase of our statistical analysis targeted the identification of morphological and hemodynamic parameters with high effect sizes in prediction of aneurysm rupture of MIA. With respect to that, we analyzed 49 (21 morphological and 28 hemodynamic) out of 81 established parameters according to their significance level and, more importantly, to their effect sizes, revealing the precise parameter impact on the rupture risk. Although 13 morphological parameters and 3 hemodynamic parameters yielded significant results, they only achieved medium effect size. These findings suggest that a large number of introduced morphological and hemodynamic parameters show no significant results in the rupture risk assessment of MIAs. In addition, significant parameters seem to have only a medium effect on the rupture prediction in our patient collective. Despite the high number of parameters examined in this study, it is important to point out that we did not include all established parameters in our analysis. Especially those parameters considering the parent vessel were not automatically extracted by our semiautomatic neck curve reconstruction. Therefore, we are not able to draw any conclusions regarding the influence of these parameters on the rupture risk of MIAs in the context of this study. However, it should be mentioned that among the group of parameters including information about the parent vessel, the size ratio (aneurysm size divided by the average parent vessel diameter) shows significant associations with the rupture of IAs in numerous studies.

As previously reported studies affirmed correlations between a small number of morphological and hemodynamic parameters, we considered it a possible cause for the medium effect sizes achieved in phase one. A potential explanation for strong correlations between morphological and hemodynamic parameters might be that they are all size-related to some extent. In phase two of our statistical analysis in order to investigate this hypothesis, we performed an extended investigation of correlations between the calculated parameters. The analysis revealed strong correlations between morphological and hemodynamic parameters in general. In order to minimize the number of parameters included in the final prediction model, we aimed to select parameters with the comparatively lowest correlations coefficients. The six selected parameters still showed medium to high correlation coefficients in the majority of cases. Based on these results, we assume that the introduction of new parameters will only advance the rupture risk prediction if they exhibit low correlations with existing aneurysm size-related parameters.

The final hierarchical logistic regression revealed a prediction model for patients with MIAs based on two parameters (AR1 and Aneurysm_RRT_max). Although the results published here are based on an extensive and meticulously performed analysis, our final prediction model only achieved an AUC of 0.75. In connection with the results revealed by phase one and two of our statistical analysis, the only moderately high AUC,
along with the low number of parameters with independent impact on rupture risk prediction, raises the question of whether morphological analysis and blood flow simulations are capable of improving the rupture risk assessment of patients with MIAs. However, further studies including a higher number of patients need to be carried out to evaluate the real impact of morphology and hemodynamics on the rupture of MIAs.

Limitations
There are several limitations related to the study design and the used methodology. The number of patients with MIAs investigated in this study is low, compared with other studies addressing rupture risk assessment of IAs in general. To obtain results with significance for the clinical routine, a higher number of cases needs to be included in further investigations. In addition, the underlying classification of an IA as unruptured or ruptured is not based on a prospective study. Therefore, there might be a bias due to the unknown natural progression of an unruptured IA, which means that it is unclear whether these aneurysms would have ruptured during follow up. Apart from this, uncertainty remains as to whether aneurysm rupture leads to changes in aneurysm morphology and, therefore, influences the morphological analysis. Our semiautomatic neck curve segmentation shows limitations in the analysis of aneurysms with particularly complex morphology. The exclusion of these aneurysms due to reconstruction failures had implications for the further statistical analysis presented in this study. Finally, the implemented boundary conditions were not patient specific due to a lack of availability of patient-specific information on exact flow conditions and in vivo local wall thickness differences.

Conclusion
A high number of established morphological and hemodynamic parameters seem to have no or low effect on the prediction of aneurysm rupture in patients with MIAs. Moreover, meaningful parameters show a high amount of correlations between each other and seem to contain redundant information due to their relation to the aneurysm size. New parameters could improve the prediction accuracy if they are not aneurysm size-related. Consequently, for best possible rupture risk assessment of patients with MIAs, only the morphological parameter AR1 and the hemodynamic parameter Aneurysm_RRT_max need to be included in the prediction model.

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Author’s contributions
- Data acquisition: BN, VMS, SS
- Data analysis: BN, VMS, SS, PB, MS, JH, OB, KPS
- Conception and design of study: BN, SS, PB, MS, IES, BP
- Writing of manuscript: BN, VMS, SS

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Conflict of interest statement
The authors declare that there is no conflict of interest.

Ethics statement
The ethics committee waivered the need for ethics approval due to the retrospective implementation of the study.

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Supplemental material
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