New Aspects of the Temperature – Magnetic Field Phase Diagram of CeB$_6$

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Abstract

We have measured the magnetic field dependence of the paramagnetic to the field-induced high temperature antiferroquadrupolar magnetically ordered phase transition in CeB$_6$ from 0 to 60 T using a variety of techniques. It is found that the field-dependent phase separation line becomes re-entrant above 35 T and below 10 K. Measurements of resonant ultra-sound, specific heat and neutron diffraction show conclusively that the zero-field temperature-dependent phase transition is to a state with no ordered dipole moments, but with second order transition signatures in both the sound attenuation and specific heat.

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The nature of cooperative ordering in highly correlated electron systems continues to be a central topic of fundamental interest. In the past decade cerium hexaboride (CeB$_6$) and related materials have been the focus of many studies of their electronic, thermal, and magnetic properties to investigate the delicate balance between the Kondo-lattice ground state of these highly correlated electron systems, and various states with long range magnetic order.$^1$ CeB$_6$ is a prototype system because all the interesting properties arise from a single $4f$ electron on the Ce ion that hybridizes with the conduction electrons, giving rise to heavy fermion (HF) behavior. Three different phases so far have been identified in this material. Phase I occurs at high temperatures (≥ 10 K), where CeB$_6$ is paramagnetic and exhibits the Kondo effect (electrical resistivity increasing logarithmically with decreasing temperature)$^2$. In zero applied field an ordered state identified as antiferroquadrupolar (AFQ) order develops below $T_q$=3.3 K (Phase II), while conventional dipolar antiferromagnetic order develops below $T_N$=2.3 K (Phase III).$^3$ As a function of applied magnetic field, Phase III has been reported to exhibit three different orderings of the dipole moments, with phase boundaries that come together at 2.3 K in zero field, while the phase boundary for the AFQ order has recently been found to increase with increasing field with no indication of re-entrant behavior up to 30 T (see Fig. 1).$^4$ In this paper we present several types of measurements on high-quality single crystals of CeB$_6$. First, we have extended the phase boundary between Phase I and II to 60 T, and observe that above 35 T Phase I becomes re-entrant, in agreement with expectations of theory.$^5$ Second, we show that a weak second order phase transition does occur at zero field between Phases I and II as a function of temperature. Third, we show from neutron diffraction that in zero applied magnetic field no magnetic dipole ordering exists in Phase II. Fourth, we identify a new zero-field second order phase transition at 1.6 K, inside the accepted Phase III regime.

Figure 1. Phase diagram for CeB$_6$ determined previously, showing three main phases. At zero field there are two magnetic ordering temperatures; the quadrupolar ordering at $T_q$=3.3 K, and the Néel temperature $T_N$=2.3 K.

Cerium hexaboride is one of several rare earth hexaborides that crystallize in the primitive cubic structure with the rare earth ions at the cube center and boron octahedra at the cube corners. The cubic crystal field due to the six boron atoms in CeB$_6$ splits the single electron $4f$ 6-fold degenerate $^2F_{5/2}$ level into a 2-fold degenerate $^2T_2$ level and a 4-fold degenerate $^2G_4$ level.$^6$. 
It has been shown that in CeB₆ the Γ₈ is the lowest energy state, and the splitting between the Γ₇ and the Γ₈ levels is on the order of 530 K. The Γ₈ symmetry of the f electron on Ce allows not only a magnetic dipole moment, but higher order moments, including orbital electric and magnetic quadrupole moments, as well as a magnetic octapole moment.

For the high-field phase boundary determination we have made measurements using two different techniques. First, temperature dependent cantilever magnetometer measurements of the sample magnetization between 25 T and 45 T were made in steady fields using the hybrid superconducting-plus-resistive magnet at the National High Magnetic Field Laboratory (NHMFL) in Tallahassee, FL. This method of measurement previously has been described in Ref. 4. Second, we made constant temperature susceptibility measurements in pulsed fields to 60 T at the NHMFL, Los Alamos. For these latter measurements we placed the sample in a balanced pickup coil to measure the change in susceptibility of the sample as a function of field. The results of these measurements, along with our previous data, are shown in Fig 2. In the inset we show a quadratic fit to the data showing that, if the fit were to persist, the zero temperature transition would occur at 80 T.

Uimin has described the shape of T₉ vs. field from previously published results plotted with the current data that now extends to 60 T. Inset: Quadratic fit to the data suggesting the zero-temperature transition would occur near 80 T.

Figure 2. Quadrupolar ordering temperature (T₉) vs. field from previously published results plotted with the current data that now extends to 60 T. Inset: Quadratic fit to the data suggesting the zero-temperature transition would occur near 80 T.
and filter were employed at neutron wavelengths of 2.359 Å for BT-2 and 2.461 Å on BT-7, with relaxed angular collimations to optimize the observed intensities. Magnetic dipole moments (M1) and electric quadrupole moments (E2) have the same parity symmetry, but have opposite time reversal symmetry (M1 – odd and E2 – even). Thus the application of an external magnetic field is required to break the time reversal symmetry of M1 and allow the magnet dipole moments to co-exist with the electric quadrupole moments. Fig. 3 shows a comparison of the antiferromagnetic peak observed at the (1/4,1/4,1/4) position at 1.6 K. The asymmetry of the scattering originates from the mosaic of the crystal. The ordered antiferromagnetic moment we observe is <m>=0.26(4) µB, in good agreement with the literature. Also shown in the figure is the scattering at the AFQ position, (1/2,1/2,1/2). No scattering was detectable at 1.6, 2.8 K, or 3.3 K, which places an upper limit of 0.03 µB, for any induced dipole moment associated with the AFQ order. Note in particular that the data taken at 2.8 K is well within the Phase II region, and the absence of a peak shows that there is no significant zero-field magnetic ordering due to coupling with quadrupolar moments, in contrast to the ordering that is readily observed in the two changes in the elastic tensor near the AFQ (Tq), and the AFM (TAF) phase transitions. These changes are shown in Fig. 4a, where the transition Tq at 3.3 K is observed as a change in slope in the temperature dependent data, and TN at 2.3 K shows a discontinuity with no hysteresis. These data indicate that the 3.3 K transition (Tq) is weakly second order, while the AFM transition (TN) is a sharp second order transition. A second zero-field transition, T2, is observed in Phase III near 1.6 K. In addition to the RUS results, temperature dependent specific heat results at zero field are shown in Fig. 4b. Again, the Tq transition is seen to be weakly second order, and TN is sharp. To verify the thermodynamic order of Tq and TN, specific heat measurements were made using a pulse-relaxation technique for both increasing and decreasing temperature. The results shown in Fig. 4b clearly demonstrate the nature of the transitions with no hysteresis in either, indicating that the TN transition is also second order. Further measurements in applied fields up to 15 T showed that both transitions followed the published phase diagram.
function of field and temperature. All of the present data, taken together, show that Phase II in CeB$_6$ exists at zero field, but does not become magnetically ordered until the application of an external magnetic field breaks the time reversal symmetry between the dipole and quadrupole moments. We have observed that this magnetically ordered field-induced phase can be destroyed by fields only exceeding 35 T. Based on these results, any theory that predicts the destruction of Phase II below 30 T does not include either all of the effects, or it includes incorrect mechanisms. However, two of the theories presented to date, both of which are predicated on indirect exchange, predict destruction of the AFQ phase at fields > 30 T, and cannot be ruled out. Finally, when the RKKY interaction between the 4f electron spins overcomes the thermal effects, internal magnetic fields are produced that break time-reversal symmetry and allow spontaneous ordering of the magnetic moments in Phase III.

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