Stabilisation of tetragonal FeCo structure with high magnetic anisotropy by the addition of V and N elements

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The development of magnetic materials with high saturation magnetization ($M_s$) and uniaxial magnetic anisotropy ($K_u$) is required for the realisation of high-performance permanent magnets capable of reducing the power consumption of motors and data storage devices. Although FeCo-based materials with the body-centred cubic structure (bcc) exhibit the highest $M_s$ values among various transition metal alloys, their low $K_u$ magnitudes make them unsuitable for permanent magnets. Recent first-principles calculations and experimental studies revealed that the epitaxial FeCo thin films with the body-centred tetragonal (bct) structure and thicknesses of several nanometres exhibited $K_u$ values of $10^6 \text{J} \cdot \text{m}^{-3}$ due to epitaxial stress, which required further stabilisation. In this work, the FeCo lattice stabilised via VN addition were characterised by high $K_u$ magnitudes exceeding $10^6 \text{J} \cdot \text{m}^{-3}$. The obtained bct structure remained stable even for the films with thicknesses of 100 nm deposited on an amorphous substrate, suggesting its possible use in bulk systems.

The continuously increasing power consumption of motors utilised in electrical vehicles and air conditioners, and magnetic devices inside hard disk drives and random access memory chips has become a serious issue. Permanent magnets represent very important components of these applications. They are typically used in the bulk form in motors, actuators, and flux sources, and as thin films in storage and spintronic devices. Hence, enhancing the performance of permanent magnets represents the simplest and most efficient method for reducing their power consumption. The energy utilised by these magnets depends on the magnitudes of the saturation magnetization ($M_s$) and uniaxial magnetic anisotropy ($K_u$) of magnetic materials, whose high thermal stability can be achieved at high values of the Curie temperature ($T_c$).

FeCo with the body-centred cubic (bcc) structure is a well-known magnetic material characterised by the highest $M_s$ and very high $T_c$ values among various transition metal alloys. Although FeCo-based materials exhibit strong magnetic properties, their low $K_u$ magnitudes make them unsuitable for the fabrication of permanent magnets. However, if the $K_u$ of FeCo could be increased to a sufficiently high value, one of the strongest permanent magnets would be obtained.

The results of recent first-principles calculations have predicted a high $K_u$ exceeding $10^6 \text{J} \cdot \text{m}^{-3}$ for the FeCo with the body-centred tetragonal (bct) structure. Generally, the bct lattice is considered an intermediate structure between the bcc and face-centred cubic (fcc) lattices. This relationship is known as the Bain (bcc–bct–fcc) transformation, which typically occurs in martensitic materials. In this respect, the bcc–bct–fcc transformation can be related to the unified lattice constant ratio $c/a$; the $c/a$ of the bcc lattice is 1.0, and that of the fcc lattice is $\sqrt{2}$.

In the equilibrium phase diagram constructed for FeCo, the fcc phase is stable at temperatures higher than 1258 K. Its transformation to the bcc phase occurs at lower temperatures, leading to the formation of the CsCl-type (B2) ordered bcc structure at temperatures below 1003 K without producing a bct intermediate. However, after considering the Bain transformation, two methods can be used to stabilise the bct structure: (A) applying a uniaxial stress to the FeCo lattice via epitaxial effects and (B) adding a third element to the FeCo structure.

Various experimental studies based on method A have been performed to investigate the magnetic anisotropy of FeCo by epitaxially growing it on several Rh, Pd, Ir, Pt, or CuAu buffer layers, which were selected because a proper misfit between the buffer layer and a FeCo thin film produced the bct structure. The results of these
studies revealed that the magnitude of $K_u$ experimentally exceeded $10^8 \text{J} \cdot \text{m}^{-3}$ when the $c/a$ of FeCo was around 1.2, which was consistent with the theoretical predictions. However, structural relaxation rapidly occurred in the epitaxially grown thin films with an increase in the film thickness, and the bct structure with $c/a = 1.2$ was realised only in a few films with thicknesses ($t$) of 1–2 nm.

Several experimental studies based on method B have been conducted as well. The addition of certain third elements is expected to generate a macroscopic tetragonal distortion in the FeCo lattice leading to the relaxation of the local stress in their vicinity. B, C, and N represent typical interstitial elements that are widely used for the manufacture of tetragonal Fe-based alloys. For instance, Fe$_{50}$N$_{50}$ was reported as a tetragonal compound with $c/a = 1.1$ and $K_u = 0.45 \times 10^8 \text{J} \cdot \text{m}^{-3}$ \cite{1}. In FeCo-based alloys, (Fe$_{50}$Co$_{50}$)$_x$–(B, C, N) ($y \geq 0.7$) films with $t = 300$ nm deposited on MgO substrates have been studied, and a tetragonal structure resembling that of Fe$_{50}$N$_{50}$ was detected in the Fe-rich regions \cite{29,30}. The (Fe$_{43}$Co$_{43}$)$_2$C$_{60}$ films with $t = 100$ nm deposited on AuCu buffer layers were characterised by $c/a = 1.03$ and $K_u = 0.44 \times 10^8 \text{J} \cdot \text{m}^{-3}$ \cite{16,19}. The FeCoTiN film with $t = 23.5$ nm exhibited $c/a = 1.08$ and $K_u = 0.57 \times 10^8 \text{J} \cdot \text{m}^{-3}$ \cite{28}. However, for the FeCo-based alloys, no $c/a$ values of around 1.2 have been achieved yet.

In our previous study \cite{27}, we focused on the use of vanadium as the third additive element because of its ability to form a bcc solid solution around Fe$_{50}$Co$_{50}$ clusters, which was subsequently transformed into the fcc phase with an increase in the V content. A stabilisation of the bct phase was expected to occur at the boundary between the bcc and fcc phases. Furthermore, FeCo compounds containing 8–20 at.% V (called vicalloys) have semi-hard magnetic properties with coercivity values of 0.03–0.05 T \cite{31–33}. FeCo-based materials containing less than 10 at.% V are called vicalloys of type I (typically Fe$_{50}$Co$_{50}$V$_{30}$), and those with 10–20 at.% V are called vicalloys of type II (typically Fe$_{44}$Co$_{44}$V$_{12}$). The magnetic hardening mechanism of these vicalloys has not been fully elucidated yet. Five possible factors can be considered: (1) pinning the domain walls at non-magnetic precipitates or at the B2 anti-phase boundaries, (2) shape anisotropy of the bcc phase, (3) stress-induced anisotropy, (4) magnetic anisotropy of martensitic needles, and (5) magnetic anisotropy of ordered bct precipitates. Previously \cite{27}, it was reported that the semi-hard magnetic properties of vicalloys could be mainly attributed to the fifth factor (the presence of tetragonally distorted precipitates or clusters during the bcc–fcc transformation) and that they could be potentially improved by the formation of the bcc phase. Although V addition was expected to stabilise the bct phase, the examined FeCoV and FeCoVC films were unable to achieve $c/a = 1.2$ \cite{27}. In this study, the effect of the VN addition to FeCo films on their tetragonal deformation and magnetic properties was investigated.

### Structural Bcc to Fcc Transformation of FeCo Due to VN Addition

The crystal structures of the MgO (100) substrate/Rh ($t = 20$ nm)/FeCo$_{50}$V$_{50}$ films with $t = 5$ nm were examined. Rh was selected as the buffer layer material because it exhibited the lattice mismatch ($\Delta a_{\text{Rh}}/\sqrt{\lambda} = 0.05–0.07$ across the bcc–fcc FeCo structures, which was considered suitable for epitaxial growth. According to the results of our previous studies \cite{27}, the addition of 10 at.% V to FeCo films produced the maximum value of $K_u$.

Figure 1a,b show the in-plane and out-of-plane X-ray diffraction (XRD) patterns of the studied samples, respectively. The black vertical dashed lines represent the peak positions determined with respect to the background (B.G.) of the MgO substrate/Rh ($t = 20$ nm)/SiO$_2$ ($t = 5$ nm). The lattice constant $a$ calculated for the bcc FeCo structure was in the range of 0.284–0.286 nm (bcc Fe$_{50}$Co$_{50}$, B2 Fe$_{50}$Co$_{50}$, and bcc Fe$_{44}$Co$_{44}$V$_{12}$), while that determined for the fcc FeCo structure was within the range of 0.355–0.357 nm (fcc Fe$_{50}$Co$_{50}$, fcc Fe$_{40}$Co$_{40}$V$_{40}$, and fcc Co$_{75}$V$_{25}$) \cite{30,34}. The expected bcc FeCo (200), fcc FeCo (220), fcc FeCo (002), and bcc FeCo (002) diffraction angles were calculated from the reported values, and the expected peak positions are denoted by the red vertical dashed lines in Fig. 1a,b (here the red arrows represent the experimental peak positions).

Figure 1b indicates that the films grew epitaxially on the Rh (001) buffer layer, and that the FeCoVN [001] direction is perpendicular to the film plane. The deviation angles of the Rh [001] and FeCoVN [001] orientations determined with respect to the film plane by rocking curve measurements were equal to approximately 1.5$^\circ$ and 2.5$^\circ$, respectively. Figure 1a also shows that the FeCoVN [100] axis is parallel to the [110] axes of both the Rh buffer layer and MgO substrate; therefore, their structural relation can be described by the formula MgO (001) [100]//Rh (001) [100]//FeCoVN (001) [110]. No diffraction peaks corresponding to vanadium-nitrogen compounds (such as VN) were observed in both figures, suggesting the formation of a solid FeCoVN solution without any precipitates. The in-plane and out-of-plane FeCoVN diffraction peaks denoted by the red arrows range from 65$^\circ$ to 76$^\circ$ and 51$^\circ$ to 66$^\circ$, respectively, indicating the existence of an intermediate structure between the bcc and fcc phases. Hence, it can be concluded that the studied films underwent tetragonal distortion to form the bct structure stabilised by the interstitial nitrogen atoms.

The lattice constants $a$ and $c$ of the bct structure were calculated from the bcc FeCo (200) (Fig. 1a) and bcc FeCo (002) (Fig. 1b) angles, respectively. The dependences of the $a$ and $c$ values on the N content $x$ are shown in Fig. 2a, whose inset illustrates the relationship between the Rh buffer layer and FeCo layer from the top view. The obtained magnitudes of $a$ and $c$ lie in the ranges of 0.26–0.29 nm and 0.29–0.38 nm, respectively. The $a$-values are lower than the lattice constant of the bcc FeCo ($a_{\text{bcc-FeCo}}$) structure, while the $c$-values are higher than $a_{\text{bcc-FeCo}}$. With increasing $x$, the $a$-value approaches the $a_{\text{B2}}/\sqrt{\lambda}$ limit due to the epitaxial growth on the Rh layer, while the $c$-value approaches the magnitude of $a_{\text{Rh}}$), indicating the formation of the fcc structure. Figure 2b shows the dependence of the $c/a$ ratio on $x$, while its inset contains the schematic describing the Bain (bcc–fcc–fcc) transformation. The obtained $c/a$ ratio increases from 1.02 (bcc) at $x = 0$ at. % to 1.43 (fcc) at $x = 5.5$ at. %.

It should be noted that the bct structure with 1.05 < $c/a$ < 1.30 exists in the range of 1.0 < $x$ < 5.5 at. %.
In order to examine the stability of the N-modified-FeCoV films with thicknesses of 100 nm, the in-plane and out-of-plane XRD patterns of the MgO (100) substrate/Rh (t = 20 nm)/(Fe0.5Co0.5)90−x/2V10−x/2N x (x = 9.6 at.%, t = 100 nm)/SiO2 (t = 5 nm) continuous films were recorded (see Fig. 3a,b, respectively). The diffraction angles of both FeCoVN films denoted by the red arrows are very close to each other despite their deposition on different buffer layers: Rh (aRh = 0.381 nm) and MgO (aMgO = 0.421 nm). The lattice constants of the FeCoVN structures calculated from Fig. 3a,b are equal to abcc = 0.266 nm (abcc = 0.376 nm) and cbcc = cbcc = 0.384 nm, respectively, resulting in the ratio cbcc/abcc = 1.44 (cbcc/abcc = 1.02), which is close to that of the fcc structure. It should be noted that the fcc phase can exhibit relatively high stability at a sufficient amount of added N (x ≤ 5.5 at.%), although the most stable phase of FeCoV (x = 0 at.%) corresponds to the bcc structure, as will be explained in the next paragraph.

Next, the stable crystal structures of the FeCo and FeCo-X (X = V, VC, and VN) films deposited on the amorphous SiO2 substrates were compared. Their compositions determined at a film thickness of 100 nm were...
Fe₅₀Co₅₀, (Fe₀.₅Co₀.₅)₉₀V₁₀, (Fe₀.₅Co₀.₅)₉₀V₅C₅, and (Fe₀.₅Co₀.₅)₈₉V₉N₂, respectively. Figure 4 shows the out-of-plane XRD patterns recorded for the studied samples. Except for the FeCoVN film, single peaks with close positions corresponding to the bcc FeCo (110) diffraction and denoted by the red arrows were observed. The diffraction...
angle of the FeCoVC film was slightly lower than those of the other (FeCo and FeCoV) films, resulting in a slight increase in its lattice constant (it was assumed that the added C atoms were located at the interstitial sites of both the a and c-axes corresponding to the bcc structure with \( c/a = 1.00 \)). On the other hand, the existence of double peaks indicated by the red arrows was observed only for the FeCoVN film. The calculated lattice constants of FeCoVN are \( a_{\text{bcc}} = 0.272 \text{ nm} \) and \( c_{\text{bcc}} = 0.310 \text{ nm} \), resulting in the bct structure with \( c/a = 1.14 \) (it was assumed that the added N atoms were attached only to the interstitial sites of the c-axis, which was consistent with the previous results obtained for the epitaxially grown FeCoTiN film with \( c/a = 1.0824 \)). It should be noted that the FeCoV crystal structure could be easily transformed from the bcc to fcc configuration by the addition of N atoms. The bct structure of FeCoVN (1.0 < x < 5.5 at.%) is stable even in the case of its deposition on an amorphous substrate, suggesting a possibility of its realisation in bulk systems without any epitaxial effects, which can be used for the development of an optimum manufacturing procedure for bct FeCo-based permanent magnets.

**Uniaxial Magnetic Anisotropy of Bct FeCoVN**

Figure 5 shows the magnetization curves for the MgO (100) substrate/Rh (\( t = 20 \text{ nm} \))/(Fe0.5Co0.5)90V10−x/C5 (0 ≤ x ≤ 9.6 at.%) continuous films obtained at a room temperature of 298 K using a vibrating sample magnetometer (VSM). The in-plane (//) and perpendicular (⊥) magnetization data points are denoted by the black triangles and red circles, respectively. For some curves, a small background resulting from the image effects at magnetic fields of \( \mu_0 H > 1.0 \text{ T} \), where \( \mu_0 \) was the vacuum permeability, could not be subtracted completely (for example, at \( x = 2.0 \text{ at.\%} \)). The effective magnetic easy-axis changes from the in-plane direction to that perpendicular to the film plane with increasing x, and the samples with the perpendicular magnetic easy-axis component are obtained in the range of 1.7 ≤ x ≤ 2.2 at.\% (their values of the perpendicular saturation field (\( \mu_0 H_s \)) are lower than that of the in-plane \( \mu_0 H_s \)).

Figure 6a–c show the x dependences of \( \mu_0 M_s \), perpendicular \( \mu_0 H_s \), and \( K_u \), respectively. The magnitude of \( M_s \) decreases with increasing x (Fig. 6a), and the same trend is observed for the demagnetisation field (\( \mu_0 H_d \)) indicated by the red dotted line in Fig. 6b. In the range of 0 ≤ x ≤ 6.5 at.\%, the perpendicular \( \mu_0 H_s \) values are lower than the \( \mu_0 H_s \) values (Fig. 6b) due to their perpendicular magnetic anisotropy components, resulting in the positive \( K_u \) values depicted in Fig. 6c. The latter were calculated via the following equation:

\[
K_u = K_{u(\text{eff})} + \mu_0 M_s^2 / 2
\]

where \( K_{u(\text{eff})} \) is the effective magnetic anisotropy estimated by calculating the differential area between the magnetization curves obtained for the easy-axis and hard-axis. Generally, \( K_u \) takes into account all intrinsic
contributions to the magnetic anisotropy, including the volume effects caused by the tetragonal distortion and B2 chemical ordering and surface effects except for the shape magnetic anisotropy ($\mu_0 M_s^2/2$). At $x = 2.0$ at.%, the magnetic easy-axis was perpendicular to the film plane (Fig. 5), and the maximum magnitude of $K_u$ is equal to about $1.24 \times 10^6$ J·m$^{-3}$ with $\mu_0 M_s = 1.60$ Wb·m$^{-2}$.

To elucidate the mechanism of the uniaxial magnetic anisotropy, the $K_u$ values are plotted as a function of $c/a$ in Fig. 6d along with the theoretical values determined by first-principles calculations for Fe$_{50}$Co$_{50}$ in previous

Figure 5. Magnetisation curves recorded for the FeCoVN films with a thickness of 20 nm. Magnetisation curves obtained for the MgO (100) substrate/Rh ($t = 20$ nm)/[Fe$_{50}$Co$_{50}$]$_{30-x}$V$_{30-x}$/N$_x$ ($0 \leq x \leq 9.6$ at.%, $t = 20$ nm)/SiO$_2$ ($t = 5$ nm) continuous films at a room temperature of 298 K. The in-plane (∥) and perpendicular (∥) magnetisation curves are denoted by the black triangles and red circles, respectively.
A high $K_u$ of around $10^6$ J·m$^{-3}$ was obtained in the range of $1.05 < c/a < 1.30$, which was experimentally realised for $1.0 < x < 5.5$ at.% (see Fig. 2b). High $K_u$ values were also confirmed at a film thickness of 100 nm. The entire dependence of $K_u$ on $c/a$ can be reproduced by performing first-principles calculations assuming the tetragonal distortion and absence of $B2$ chemical ordering (the order parameter $S = 0$ in Fig. 6d). The results of these calculations attributed the origin of the uniaxial magnetic anisotropy of bct FeCo to its unique electronic structure and hybridization of $d_{xy}$ and $d_{x^2−y^2}$ orbitals due to spin-orbit interactions$^{9,10}$. Furthermore, both the first-principles

**Figure 6.** Magnetic properties of the FeCoVN films with a thickness of 20 nm. $x$ dependences of the (a) $\mu_0M_s$, (b) perpendicular $\mu_0H_{r}$, and (c) $K_u$ of the MgO (100) substrate/Rh ($t = 20$ nm)/$(\text{Fe}_{0.5}\text{Co}_{0.5})_{90−x/2}\text{V}_{x/2}\text{N}_x$ ($0 \leq x \leq 9.6$ at.%, $t = 20$ nm)/$\text{SiO}_2$ ($t = 5$ nm) continuous films. (d) $K_u$ as a function of $c/a$ along with the theoretical values obtained for the $\text{Fe}_{50}\text{Co}_{50}$ (the order parameter $S = 0$).
calculations and experimental results obtained in previous studies suggest that the interfacial anisotropy at the FeCo/Rh interface is negligible\(^{13,14}\); hence, the high values of \(K_u\) experimentally observed in this study can be mainly attributed to the volume effect caused by tetragonal distortion (magnetocrystalline anisotropy).

**Conclusion**

In this work, the FeCo crystal was transformed from the bcc to the fcc structure through the bct intermediate by VN addition, and a high uniaxial magnetic anisotropy of over \(10^6 \text{J} \cdot \text{m}^{-3}\) was obtained for the bct lattice. The fcc structure was stable at sufficiently large N contents (\(x \geq 5.5\) at.%), and the bcc structure was stable at \(x = 0\) at.% (corresponding to the stoichiometric formula FeCoV). The bct structure with \(1.05 < c/a < 1.30\) was realised in the range of \(1.0 < x < 5.5\) at.% and exhibited high stability at a film thickness of 100 nm even after the deposition on the amorphous SiO\(_2\) substrate, suggesting its possible use in bulk systems. The perpendicular magnetic easy-axis component was observed in the range of \(1.7 < x < 2.2\) at.%, and the maximum \(K_u\) of about \(1.24 \times 10^5 \text{J} \cdot \text{m}^{-3}\), with \(\mu_0 M_s = 1.60 \text{Wb} \cdot \text{m}^{-2}\), was obtained at \(x = 2.0\) at.%. The high values of \(K_u\) achieved in this study were attributed to the magnetocrystalline anisotropy caused by the tetragonal distortion.

**Methods**

The \((\text{Fe}_{0.5}\text{Co}_{0.5})_{90-x} \text{VN}_{x}\) \((0 \leq x \leq 9.6\) at.%, \(t = 20–100\) nm) films were prepared by dc-magnetron co-sputtering at a base pressure of \(1 \times 10^{-7}\) Pa using Ar and N\(_2\) as the sputtering gases. The total pressure of both gases was constant (0.1 Pa), and the N content \(x\) in the produced films was controlled by varying the Ar and N\(_2\) partial pressures. The resulting pressure ratio \((N_2/(Ar+N_2))\) varied in the range of 0–50%. The composition of \((\text{Fe}_{0.5}\text{Co}_{0.5})_{90} \text{VN}_{10}\) alloy was determined using an electron probe X-ray microanalyser; a measurement error of less than 1 at.% was achieved by averaging the compositions of 10 points on the surfaces of the films with dimensions of \(1 \times 1 \text{ cm}\). The magnitude of \(x\) in the produced films was determined by X-ray photoelectron spectroscopy. The sputtering conditions utilised for each film were as follows. The 20.0 nm thick Rh buffer layer was deposited on a single-crystalline MgO(100) substrate at 573 K; the FeCo VN film was deposited on the Rh buffer layer on a single-crystalline MgO (100) substrate or a thermally oxidized Si (100) (SiO\(_2\)) substrate at 473 K and the 5.0 nm thick SiO\(_2\) capping layer was deposited on the FeCoVN surface at 298 K. The crystal structures of the films were investigated using a conventional out-of-plane XRD with the Bragg-Brentano geometry and an in-plane XRD instrument with an in-plane scanning vector. In all XRD measurements, CuK\(_\alpha\) radiation was used. The magnetisation curves were obtained with the VSM under a magnetic field of up to 2.0 T.

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Acknowledgements
This work was supported by the Japan Society for the Promotion of Science KAKENHI through its Grant-in-Aid for Young Scientists (A) program (JP15H05518) and New Energy and Industrial Technology Development Organization (NEDO), Japan. We would also like to thank Editage and Dr. E. Watters for English language editing.

Author Contributions
T.H. supervised the study and wrote the manuscript. T.N. prepared the samples. T.N., Y.T. and M.O. measured crystal structures and magnetic properties. All authors discussed the results and commented on the manuscript.

Additional Information

Competing Interests: The authors declare no competing interests.

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