Radiative Processes, Spectral States and Variability of Black-Hole Binaries

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We review radiative processes responsible for X-ray emission in hard (low) and soft (high) spectral states of black-hole binaries. The main process in the hard state appears to be scattering of blackbody photons from a cold disk by thermal electrons in a hot inner flow, and any contribution from nonthermal synchrotron emission is at most small. In the soft states, blackbody disk emission dominates energetically, and its high-energy tail is due to scattering by hybrid, thermal/nonthermal electrons, probably in active regions above the disk surface. State transitions appear to correspond to a variable inner radius of the cold disk driven by changes of the accretion rate. The existence of two accretion solutions, hot and cold, in a range of the accretion rate leads to hysteresis in low-mass X-ray binaries.

§1. Introduction

We present here a brief review of energy and power spectra, radiative processes giving rise to them, spectral states, and some aspects of variability of black-hole binaries. Our emphasis is on interpretation of the X-ray and soft $\gamma$-ray (hereafter X$\gamma$) observations in terms of simple physical models and unifying various aspects of the wealth of the present observational data. We also discuss millisecond flares recently discovered from Cyg X-1,\textsuperscript{24) where we present some important new results.

We refer the reader to Ref. 45) for an exhaustive review of observational aspects of black-hole binaries, and, e.g., to Refs. 3), 14), 78) and 79) for some other relevant reviews.

In our presentation, we use the so-called $\nu F_\nu$ representation for both energy and power spectra. The motivation for this choice is provided by a trivial mathematical consideration. Namely, any differential dependence, e.g., flux per unit energy, $dF/dE$, equivalently expressed as $F(E)$ or $F_E$, can be plotted as $F(E)$ vs $E$. However, when we plot $F$ vs. log $E$, it should be $F(\log E) = dF/d\log E$, i.e., $F(E)(d \log E/dE)^{-1} \propto EF(E)$. This gives us $F$ per a logarithmic interval of $E$. Graphically, $EF(E)d \log E$ represents the area under the curve, $F$, in a plot vs log $E$. Then, a peak in this representation shows us at which photon energy range most of the power is radiated, or which frequency range corresponds to most of variability of a source. An added benefit of this representation is that plots vs. photon energy or wavelength become identical, as $\lambda F(\lambda) = EF(E)$. We also plot the energy spectra

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with the same length per decade on each axis, in order to enable direct comparison of the shape spectra on different figures.

On the other hand, it is common in X-ray astronomy to plot photon flux vs. energy. However, this makes it incompatible with most of other branches of astronomy (e.g., those from the radio to the UV), where energy flux is used. Also, energy is a much more fundamental quantity in physics than photon number, with many physical laws concerning the former, not the latter (as photon number is not conserved in most of physical processes). Indeed, all quantities of radiative transfer, e.g., flux, specific and average intensity, radiation pressure, are defined in terms of energy.

A practical consequence of plotting photon number per unit energy on a logarithmic plot is that such spectra look usually extremely steep, covering many orders of magnitude on the vertical axis, appear very similar to each other, and make it very difficult to actually see any spectral features. This is due to the artificial steepening of such a spectrum by $E^{-2}$, described above.

It is also very common in X-ray astronomy to plot instrumental counts instead of photons or energy. The motivation for it is that high-energy instruments have rather limited energy resolution, which makes the process of deconvolution not unique. However, this purist point of view would actually require plotting only instrumental counts, as plotting together predictions of a model and/or residuals is already model-dependent. In fact, residuals given as, e.g., ratios or contributions to $\chi^2$, are identical for either counts vs. model or a deconvolved spectrum vs. model. However, the latter has the enormous advantages of presenting a physical spectrum, allowing comparison with other spectra, and showing features originating in the source. The count-rate plot, though model-independent, is by its nature instrument-dependent, showing mostly features of the instrumental response, not related to the physics of the source.

§2. Spectra and spectral states of black-hole binaries

2.1. Classification of the states

The simplest classification of spectral states of black-hole binaries consists of two states, the hard and the soft. Very roughly, the photon spectral indices around $\sim 10$ keV during those states are $\Gamma < \sim 2$ and $\sim 2$, respectively. The hard state (also called low, LS) is characterized by a weak soft blackbody component and a high-energy spectral cutoff at $\gtrsim 100$–200 keV, whereas the soft state is characterized by a strong blackbody component and no observable (as yet) high-energy cutoff in the spectral tail beyond the blackbody. The hard state can take place at a very large range of the Eddington ratio, up to $L/L_E \sim 0.2$–0.3,$^{15}$ where $L_E \approx 1.5 \times 10^{38}(M/M_\odot)$ erg s$^{-1}$. Weak (‘off’) states have usually relatively hard spectra as long as they can be measured, so they probably are a subset of the hard state. However, the detailed form of spectra of weak states remains uncertain, with some observations showing $\Gamma \gtrsim 2$, e.g., in XTE J1118+480$^{46}$ or GX 339–4.$^{85}$

Then, the soft state is often subdivided into the high (HS), very high (VHS) and intermediate (IS) states. The ‘pure’ high, or ultrasoft, state is supposed to have only the blackbody disk component, without a high-energy tail, but this definition is
clearly dependent on the sensitivity of the instrument used. In fact, most of spectra claimed to represent this state have high-energy tails at some level, e.g., all of those presented in Ref. 45). The IS takes place during transitions between the hard and soft states, and spectrally it is characterized by the high-energy tail starting close to the peak of the disk blackbody. Then, the VHS is often defined as having the same spectral type as the IS, but at high luminosities. In fact, the VHS usually takes place during transitions from the hard state to the soft state, so the difference with respect to the IS is small, if any.

The VHS/IS can take place at a large range of the luminosity, between $\sim 0.02L_E$ or even less, e.g., during state transitions of Cyg X-1, and $\gtrsim 0.3L_E$ (e.g., in XTE J1550–564, GX 339–4, GRS 1915+105). Then, the HS (with a weak tail) can also take place at any luminosity $\gtrsim 0.02L_E^{35}$ up to $\sim L_E$, e.g., in the $\gamma$ state (in the classification of Ref. 4) of GRS 1915+105.

Overall, various states can take place at various luminosities, being a function of both the accretion rate, $\dot{M}$, in Eddington units, $\dot{m}$, and the preceding behavior of the source (which gives rise to hysteresis, see below). The presence of a high-energy tail in a soft state appears universal, but it can be at virtually any level with respect to the disk blackbody. Below, we give some examples.

2.2. Cyg X-1

Figure 1 shows the two main states of Cyg X-1. The spectrum of the hard state peaks at $\sim 100–200$ keV, which property is very characteristic of this state in black-hole binaries. There is by now a very strong body of evidence that the dominant radiative process in this state is Comptonization of disk black-body photons (at the characteristic temperature of a fraction of a keV) by thermal electrons in a plasma at a temperature of $kT_e \sim 50–100$ keV and a Thomson optical depth of $\tau \sim 1$. The power in hard photons from the Comptonizing plasma, $L_H$, is $\gg L_S$, the power in the soft blackbody photons. A brief history of the thermal Compton model applied to accreting black holes is given, e.g., in Ref. 79). In addition, there is a secondary, reprocessing, component due to Compton reflection from a cold medium accompanied by Fe K fluorescent emission. The reflector is likely to be the same accretion disk that gives rise to the disk blackbody emission. The reprocessing component is sometimes relativistically broadened, especially, in softer of the hard states of Cyg X-1.

The components of a hard-state spectrum of Cyg X-1 are shown in Figure 2a. Although the scattering plasma is predominantly thermal in the hard state, there are indications that the electron distribution has some high-energy tail, i.e., it is hybrid, thermal/nonthermal. The main evidence for it has been provided by $CGRO$/COMPTEL observations of Cyg X-1 in the hard state. The photon tail beyond the thermal-Compton spectrum is relatively weak, as shown in Figure 2b. The spectra in the soft state appear to contain the same ingredients as those in the hard state, but there are different proportions between the disk blackbody and Comptonization and between the thermal and nonthermal parts of the electron distribution in the Comptonizing plasma. Opposite to the hard state, the disk blackbody emission is energetically dominant, $L_S \gg L_H$, and the nonthermal electron tail is much stronger. These properties are illustrated by the soft-
Fig. 1. Spectra of the soft state of 1996 June and of the average hard state of Cyg X-1. The models (solid curves) in both states consist of hybrid Comptonization of disk blackbody photons, Compton reflection and fluorescent Fe K emission. The dashed curves give the model spectra before absorption. We also show the upper limit from the EGRET observations in the hard state and an expected sensitivity of GLAST, see §2.2 for details. See astro-ph for color versions of this and subsequent figures.

state spectrum of Cyg X-1 shown in Figure 1 with the components of the fit shown in Figure 2(b). We see that Comptonization by nonthermal electrons dominates at $E \gtrsim 10$ keV. The Compton reflection and Fe K fluorescence are present as well, and their strength, the ionization of the reflector, and the degree of relativistic broadening are all larger than those in the hard state.\textsuperscript{26), 27)}

No high-energy cutoff in the power-law tail of the soft state has been detected as yet.\textsuperscript{26), 48), 82)} The highest observed energy of the nonthermal photon power law is $\sim 10$ MeV, measured in Cyg X-1 by the \textit{CGRO}/COMPTEL,\textsuperscript{48)} see Figure 1.

It is of major importance where the high-energy cutoff in the soft state is and how it can be measured. Figure 1 shows a sensitivity of \textit{GLAST}\textsuperscript{50)} for a $4 \times 10^5$ s net exposure\textsuperscript{4).} We see that \textit{GLAST} will be able to strongly constrain the high-energy spectra of Cyg X-1 in both states. The model spectra\textsuperscript{48)} shown here assume the maximum Lorentz factor of the power-law electrons (beyond the respective Maxwellian distributions) in each state of $10^3$. If this Lorentz factor were higher or lower, the cutoffs would be at somewhat higher or lower energies, respectively, than the ones shown. On the other hand, the models use the compactness parameter, $\ell$ ($\propto L/R$,

\textsuperscript{4)} For the effective area of www-glast.slac.stanford.edu/software/IS/glast_lat_performance.htm and requiring 20 photons per unit $\ln E$. This relatively large number is intended to approximately take into account the presence of the strong diffuse emission in the Galactic plane region.
Fig. 2. Components of fits to typical (a) hard and (b) soft state spectra of Cyg X-1, and (c) a VHS/IS spectrum of XTE J1550–564. The hard-state spectrum is from an observation by BeppoSAX, and the soft-state is from a multi-instrument observation in 1996 June. All the spectra are intrinsic, i.e., corrected for absorption, and solid curves give the total spectra. The (green) long dashes, and (red) dots correspond to the unscattered blackbody and Compton reflection/Fe Kα fluorescence, respectively. The (blue) short dashes give the main Comptonization component, which is due to scattering by (a) hot thermal electrons with $kT \approx 75$ keV and $\tau \approx 1$, (b) nonthermal electrons of a hybrid distribution, and (c) the total hybrid distribution. The (cyan) dot-dashes show (a) the soft excess, seen in the hard state of Cyg X-1 and some other sources, most likely due to Compton scattering in a region spatially different from that of the main hot plasma, and (b) scattering by thermal electrons of the hybrid distribution.
where $R$ is the characteristic size of the Comptonizing plasma, see, e.g., Ref. 26) for details of the definition), fitted in Ref. 48) to have relatively low values of $\sim 4$, $\sim 30$ for the soft and hard state, respectively. If these parameters were higher, the high-energy cutoffs would appear at lower energies due to absorption in photon-photon

Fig. 3. Histograms (normalized to unity) of the distributions of the RXTE/ASM hardness ratios in the bands of 1.5–3–5–12 keV observed from Cyg X-1. The upper axes show the corresponding values of the spectral index of a power law going through the two adjacent energy bands and yielding the observed hardness ratio$^{83)}$ (without correcting for absorption). We clearly see bimodal distributions corresponding to the hard and soft states.

Fig. 4. The range of energy (a) and power (b) spectra of Cyg X-1 measured by pointed RXTE observations. The models of the PCA/HEXTE data shown in (a) involve hybrid Comptonization of disk blackbody emission and reflection, see §2.2 for details. The power spectra correspond to the $\sim 2–60$ keV range and have been corrected for dead time of the PCA.
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production of $e^\pm$ pairs.

The current upper limit to the $\sim 100$ MeV flux from Cyg X-1 is from the CGRO/EGRET,$^{31,47}$ and it is also shown in Figure 1. We have taken into account the dependence of the effective area on energy$^*$ and normalized it to the position-dependent upper limit for the number of photons $\geq 100$ MeV.$^{31}$ Unfortunately, the EGRET performed rather few observations of Cyg X-1, and, in particular, it did not observe Cyg X-1 during its 1996 bright soft state (shown in Fig. 1).

Given the sensitivity of GLAST, we expect to be able to put strong constraints on the presence of hadronic processes in Cyg X-1. If protons are accelerated to high energies together with electrons, proton collisions will produce pions. Then, decay of neutral pions gives rise to a spectral hump around $\sim 100$ MeV (see, e.g., the models of figures 2–4 of Ref. 76). Also, decay of charged pions produces additional relativistic pairs, which further modify the $\gamma$-ray spectrum. This issue was studied by Ref. 7), who found that the measurements$^{82}$ of GRS 1915+105 at high energies constrain the fractional power in nonthermal protons to $\lesssim 5\%$. Still, though hadronic processes may not play the dominant role, measuring their contribution is of major importance for our understanding of the physics of black-hole binaries.

The distribution of the states of Cyg X-1 is bimodal, see Figure 3. Figure 4(a) shows the range of spectra (observed over the timescale of hours) observed so far from Cyg X-1 by the PCA and HEXTE on board of RXTE. The spectra 1–2 belong to the hard state, and we see the characteristic pivot at $\sim 30$ keV within this state.$^{83}$ The spectrum 4 is from the 1996 soft state, and it is very similar to that shown in Figure 1. On the other hand, spectra observed during the long 2002 soft state were often much softer,$^{24}$ occasionally as soft as the spectrum 5. Then, the spectrum 3 is an intermediate one, measured during the 1996 hard-to-soft state transition.$^{26}$

Figure 4(b) shows the power spectra corresponding to those energy spectra. We see the hard-state spectra (1–2) have the characteristic broad maximum in the $\sim 0.1–3$ Hz in the power per logarithm of frequency, sometimes with two peaks, see e.g., Ref. 27). The upper peak is usually referred to as the low-frequency QPO, while the lower one, as the break frequency. The soft states (4–5) is characterized by a flat (in power per log $f$) power law with a high-frequency cutoff above $\sim 1–10$ Hz, see, e.g., Ref. 8). On the other hand, the intermediate state (3) shows a relatively

$^*$ From cossc.gsfc.nasa.gov/egret/egret_tech.html.
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narrow single peak (a QPO) at \( \sim 3 \text{ Hz} \), often seen in IS/VHS power spectra.\(^{33}\)

The transitions to and out of the soft state in Cyg X-1 take place at about the same flux level, as illustrated in Figure 5. The hard state is observed at \( L \sim (0.01–0.02)L_E\) (\( d/2 \text{kpc} \))^2 (10\( M_\odot /M \)), and higher luminosities always correspond to intermediate and soft states.\(^{83}\) The luminosity of the soft-state spectrum shown in Figures 1, 2b is \( L \sim 0.05L_E\) (\( d/2 \text{kpc} \))^2 (10\( M_\odot /M \)),\(^{83}\)

2.3. Hysteresis in Low-Mass X-ray Binaries

Unlike the case of Cyg X-1, where the transitions between the soft and hard states take place approximately at the same \( L \) (which corresponds to a one-to-one correspondence between the luminosity and the spectral state), state transitions in LMXBs can take place in a wide range of \( L/L_E \), and, consequently, various spectral states can correspond to the same \( L/L_E \).\(^{36},\,53,\,62,\,85\) This is obviously related to the existence of ranges of \( L/L_E \) and radii at which two stable accretion solutions, optically thick (soft)\(^{67}\) and optically thin (hard),\(^{54},\,68\) exist. The maximum possible luminosity of the hard state (probably limited by cooling of the hot plasma) is larger than the minimum possible luminosity of the soft state (probably limited by evaporation of the disk\(^{49},\,64\)). The state of a variable source in a given moment is then determined not solely by \( L/L_E \) but also by its history. This leads to a hysteresis (lagging of the effect in a physical system when the acting force is changed) in the lightcurve of the source; the hard-to-soft state transitions during the rise phase occur at higher luminosities than the soft-to-hard one during the decline phase.

The presence of pronounced hysteresis in LMXBs is illustrated in Figure 6 showing the history of the two recent outbursts of GX 339–4.\(^{85}\) The upper panels show the ASM lightcurve and the 3–12 keV spectral index (which clearly identifies the spectral state in a given moment). The lower panels show the corresponding inner radius of the optically-thick disk and the bolometric \( L \), the latter estimated from an accretion model and available PCA/HEXTE data.\(^{85}\) We see that the transitions from the hard to the soft state took place at much higher fluxes and luminosities than the transitions from the soft to the hard state, in agreement with our discussion above. Both soft-to-hard transitions took place at about the same \( L \sim 0.02L_E \), also typical for other black-hole binaries.\(^{35}\) Thus, the history determining the moment of the transition appears to be simply the pre-existence of an optically-thick inner disk, presumably extending close to the minimum stable orbit.

However, the transition out of the hard state during the second outburst took place at \( L \sim 0.2L_E \), a few times higher than \( L \sim 0.07L_E \) for the first outburst. This is also in agreement with data for other LMXBs\(^{36},\,62\) showing this type of transition taking place at a wide range of \( L/L_E \). The reason for the variety of the transition \( L/L_E \) has to be related to the structure of the hot accretion flow being more complex than that of the cold disk extending to the minimum stable orbit. This additional complexity is likely to be the value of the inner radius of an outer cold disk, most likely existing in this type of flow. In the example of Figure 6 the first transition followed a \( \sim 10^3 \) d of sustained hard-state activity of GX 339–4.\(^{85}\) The cold disk extending relatively close to the black hole, \( r_{\text{in}} \equiv R_{\text{in}}c^2/GM \sim 10^2 \), was then probably built by viscous processes long time before the transition towards the
soft state started. Then, it took a relatively short time for this cold disk to build all the way down to the minimum stable orbit after $\dot{M}$ started to increase. On the other hand, the second outburst took place after a $\sim 10^3$ d of quiescence. That outburst presumably started in outer regions ($r_{\text{in}} \gg 10^2$) with the standard H ionization instability. The buildup of the inner cold disk took longer than in the previous case, which allowed the hot flow to exist up to a later stage of the increasing-$\dot{M}$ phase, i.e., up to a higher $L$.

As shown in Figure 5, there is no noticeable hysteresis in Cyg X-1. This is clearly related to this object being persistent and with a high-mass companion. This may be directly due to its relatively narrow range of observed $L$, in which case the outer cold accretion disk in the hard state presumably stays relatively close to the black hole. It may be also related to the outer disk radius being relatively small due to the accretion process being quasi-spherical [6], [34].

Apart from the uncertain details of the accretion processes, we have a firm observational fact that transitions between the hard and the soft state can happen in a wide range of $L/L_\text{E} \sim 0.01-0.2$. Correspondingly, the IS/VHS can also take

![Fig. 6. The 1.5–12 keV RXTE/ASM flux and the 3–12-keV photon spectral index with the values of $L/L_\text{E}$ and the inner radius of the accretion disk, $r_{\text{in}}$, fitted by a simple accretion model (for $M = 10M_\odot$ and $d = 8$ kpc) as a function of time during the two main outbursts of GX 339-4. [85] State transitions are marked by the vertical lines. The circles in the bottom panels show $L/L_\text{E}$ based on the available PCA/HEXTE data [85] which are in a relatively good agreement with the ASM model. We see that whereas the transitions out of the soft state take place at $\sim 0.02L_\text{E}$, the transitions from the hard to the soft state take place at substantially higher $L$, which are also different for each of the two outbursts.]
place at various values of $L/L_E$.

2.4. The nature of the high and very high states

Here, we begin with a historical note on the use of the VHS term. It was introduced by Ref. 52) to describe a bright state of GX 339–4 observed by Ginga. Those authors defined it by three criteria: (i) the X-ray flux higher than that of the HS; (ii) the energy spectrum consisting of a blackbody with a power law with $\Gamma \sim 2.5$, which they considered softer than the high-energy tail of the soft state; (iii) rapid X-ray variability, much higher than that in the soft state. The spectrum 1 in Figure 7a shows a characteristic spectrum of Ref. 52) (we note that those authors showed their spectra only in count space of the Ginga LAD, which made comparison with spectra from other instruments difficult).

Since that time, GX 339–4 has shown HS (ultrasoft) spectra at similar or higher flux level than that of the original VHS (see, e.g., the spectrum 1 in Figure S and thus the criterion (i) cannot be used any more. We also see in Figure 7 that this spectrum is very similar to the HS spectrum of Cyg X-1 shown in Figure H, which high-energy tail also has $\Gamma \sim 2.5$, but which occurs at a much lower luminosity, $\sim 0.05L_E$, several times below that of the VHS of GX 339–4. The only visible difference is that the peak of the blackbody component (and presumably its maximum temperature) is at an energy about twice higher in GX 339–4 than in Cyg X-1. Thus, the criterion (ii)
also cannot be used given our present knowledge of X-ray spectral states of black-hole binaries. Finally, although rapid X-ray variability is indeed often seen during the VHS, the spectrum 4\textsuperscript{(82)} in Figure 7 (classified as belonging to the VHS by Ref. 15), was observed during one of the least variable states (χ in the classification of Ref. 4) of GRS 1915+105, see also Ref. 16). Thus, the criterion (iii) of rapid X-ray variability appears not universal as well.

Following the criterion (i) of Ref. 52, it was proposed\textsuperscript{(17)} that the VHS takes place at the highest accretion rate, when the optically-thick accretion disk extends all the way to the minimum stable orbit but it is also surrounded by a powerful corona, dissipating most of the available energy. However, it appears that the actual brightest states of black-hole binaries are sometimes ultrasoft, not of the VHS type. This is the case, e.g., in GRS 1915+105, where such an ultrasoft spectrum (number 2 in Fig. 8) was observed\textsuperscript{(82)} at \( L \approx L_E \), i.e., it was \( \sim 3 \) times brighter than the VHS one shown in Fig. 7. As mentioned above, the brightest state observed by RXTE from GX 339–4 was ultrasoft\textsuperscript{(85)} (spectrum 1 in Figure 8). Figure 8 also shows the ultrasoft spectrum of Cyg X-3, which also corresponds to the brightest state of that system.\textsuperscript{(71)}

Then, we note that the VHS appears to be almost always associated with a transition between hard and soft states (in particular, this is the case for spectra 2 and 3 in Fig. 8 and spectrum 3 in Fig. 4a). Rare exceptions to this rule\textsuperscript{(33)} appear to be related to failed state transitions. Thus, the VHS and IS are indeed basically identical, as suggested by Refs. 33),65). The state transition can occur at any \( L \sim (0.02–1) L_E \), and the associated IS spectra may or may not correspond to the highest bolometric luminosity in a given object. Hereafter, we will define the IS by the presence of a soft (\( \Gamma > 2 \)) power law originating close to the peak of the blackbody component, which definition also includes the VHS (but not the original VHS of Ref. 52). Physically, such a spectrum corresponds to comparable powers in the soft seed photons and the hard Comptonized photons, \( L_S \sim L_H \). Spectral components of a typical VHS/IS spectrum are shown in Figure 2(c).

Furthermore, the IS can be a brief episode during a hard-to-soft transition (e.g., in
GX 339–4), or it can be an extended state showing substantial luminosity evolution, as in the case of XTE J1550–564. In that case, the transition from the hard state to the VHS/IS occurred at \( \sim 0.25L_E \) (for \( M = 10M_\odot \) and \( d = 5.3 \) kpc), after which the source continued to brighten in the same state, reaching \( \sim 1L_E \). The source then faded, and showed a transition to the HS only at \( \sim 0.1L_E \). This may be then classified as the ‘true’ VHS, corresponding to the brightest state of the source. However, this is not the case for most of the states classified as ‘very high’ in literature. E.g., the transitions to the soft state in GX 339–4 during each of the last two outbursts occurred at levels somewhat below the respective global maxima.

Thus, we are led to a modification of the picture of Ref. 17), with the VHS/IS occurring not as a unique function of \( \dot{m} \) at its highest values, but between the hard and soft states. Whether the VHS is or not the brightest state of a given object depends on the time profile of \( \dot{m} \), with the state at a given \( \dot{m} \) being a function of both the \( \dot{m} \) and the preceding behaviour of the source.

Figures 9(a) and (b) compare the characteristic spectra of XTE J1550–564 and of Cyg X-3.\(^{71}\) The structure of the latter remains uncertain. It probably contains a high-mass Wolf-Rayet star with huge mass loss,\(^{72}\) but the nature of the compact object is unknown. We see the general similarity between the spectra of the two objects, apart from the very strong absorption in Cyg X-3 (with the depth of the \( \sim 9 \) keV Fe K edge indicating the presence of a very strongly ionized Thompson-thick
absorber component). We see here an ultrasoft spectrum very similar to that of XTE J1550–564 (as well to other ultrasoft spectra shown in Fig. 5). Interestingly, this spectrum corresponds to the highest X-ray luminosity of the system (as, e.g., in GX 339–4). Then, there are spectra similar to the VHS one of XTE J1550–564. Finally, we see the hardest spectra, which may be identified with the low/hard state. However, their peak energies are at ∼20 keV, much lower than the peaks at ∼100–200 keV characteristic to the hard state in black-hole binaries. Thus, we cannot unambiguously classify all of the spectra of Cyg X-3 as characteristic to black-hole binaries.

An intriguing observational feature is the form of the high-energy tail in the ultrasoft spectra (Fig. 8). It appears always to have $\Gamma \simeq 2$, substantially harder than the tails in the VHS/IS, or HS with stronger tails (e.g., in the soft state of Cyg X-1). Currently, there seems to be no theoretical explanation of that $\Gamma$.

2.5. Radiative processes in the hard state

As discussed above, there exists very strong evidence that the dominant radiative process in the hard state of black-hole binaries is thermal Comptonization. Many broad-band X-ray spectra of black-hole binaries are very well fitted by this model (although a weak non-thermal tail may be seen at ∼1 MeV). The uniform high-energy cutoff above ∼100 keV characteristic to this process is seen in all spectra measured so far. Figure 11 shows a number of hard-state spectra from Cyg X-1 and GX 339–4, all showing the cutoff, see also Ref. 30) for a number of such spectra from other objects.

The electron temperature corresponding to this cutoff is ∼50–100 keV. Such temperatures are predicted for inner regions of hot accretion flows at high accretion rates. Physically, the prevalence of this temperature range is accounted for by thermostatic properties of thermal Comptonization and $e^\pm$ pair production. At higher temperatures, cooling becomes very efficient and copious pair production starts. This reduces the available energy per electron, causing the temperature to return to the above stable range.

Furthermore, the spectral variability patterns observed in black-hole binaries are well interpreted by adjustment of the hot thermal plasma to variable irradiation by soft seed photons. For example, the hard X-ray slope responds to variability of the soft excess in GX 339–4 in a manner well fitted by thermal Comptonization.

An alternative process proposed to account for the hard-state spectra is synchrotron radiation from power-law electrons. However, in order to account for the observed X-ray spectra, this model requires extreme fine-tuning of both the energy and shape of the high-energy cutoff of the electron power law. Furthermore, the observed X-ray pattern of pivoting variability would predict extremely strong radio/IR variability (due to extrapolating to that regime of the X-ray spectrum with a variable spectral index), contrary to observations, showing the rms variability of both X-rays and radio to be similar.

The main motivation for the above model is the presence of a very good correlation between the radio and X-ray fluxes in a few bands ∼3 keV in GX 339–4, as well as somewhat weaker correlations in a number of other black-hole binaries.
However, the presence of these correlations does not necessarily require that both radio and X-rays are due to the same radiative process. A likely origin of the correlation is the formation of the radio jet out of energetic particles in the hot inner flow (i.e., the base of the jet being that flow), which also radiates X-rays. In particular, power-law dependencies between the jet radio flux and $\dot{M}^{32}$ and the accretion luminosity and $\dot{M}^{54}$, $68$, $77$ are predicted theoretically. Thus, we expect a corresponding power-law dependence between the jet radio flux and the bolometric accretion $L$.

Indeed, the original correlation of the 8.6 GHz flux with band-limited X-ray emission in GX 339−4\(^{11}\) was later shown to hold for the bolometric Xγ flux from this source\(^{85}\) as well (see Fig. [10]). This correlation does not require at all that the radio and Xγ emission are from the same process; it can be due to the global energetics correlations discussed above.

It seems worth to mention an analogous controversy regarding a correlation between the IR and X-ray emission in AGNs. An extremely good correlation was found between the fluxes at 3.5 μm and 2 keV in several classes of AGNs.\(^{39}, 40\) This was well explained by a model in which both the IR and X-ray emission was due to synchrotron/self-Compton emission of the same nonthermal electron distribution,\(^{76}\) very similar to the model for the radio/X-ray correlation in black-hole binaries of Refs. 43 and 44). However, this model was later ruled out, e.g., after the OSSE

![Graphical Illustration](image-url)

Fig. 10. (a) Hard-state OSSE spectra from Cyg X-1 (3 upper spectra; red, green and blue) and GX 339−4 (2 lower spectra, black and cyan). The Cyg X-1 spectra are averages from 1991–1996 observations grouped according to the 100 keV flux (W. N. Johnson, private communication). The GX 339−4 spectra are from 1991\(^{80}\) and 1997\(^{73}\) observations. (b) Correlation between the 8.6 GHz radio flux\(^{11}\) and the bolometric (estimated from best-fit model to PCA/HEXTE data) Xγ flux in the hard state of GX 339−4.\(^{85}\)
showed the presence of a high-energy cutoff in Seyferts very similar to that in black-hole binaries.\(^{29,81}\) The exact origin of this correlation remains unknown, but it appears it is related to some global scaling relations of AGNs\(^{66}\) and/or radiation of dust.\(^{9}\)

§3. Millisecond flares from black-hole binaries

Cyg X-1 is a persistent source with rather modest variability on various timescales. A transition between spectral states has a typical timescale of weeks\(^{74,83}\) (Figure 5), with the corresponding change in the bolometric \(L\) by a few. Shorter flaring episodes on timescales of days\(^{12}\) and hours\(^{28,70}\) have also been observed. On subsecond timescales, relatively weak flares or shots are seen in the lightcurves.\(^{19,63}\) Typical timescales of these short events are \(\sim 10\) ms, and the observed count rate increases by a factor \(\lesssim 2\). High-frequency power spectra of Cyg X-1 show very little variability at \(\gtrsim 100\) Hz.\(^{61}\)

This rather modest variability of Cyg X-1 is contrasted by the recent discovery of powerful fast flares\(^{24}\) in the RXTE/PCA lightcurves. The shortest time-scales recorded are \(\sim 1\) ms and the peak count rates are up to more than an order of magnitude above the persistent emission. Figure 11a shows the strongest and the fastest flare found so far, during the extended soft state of 2002. The photon energy and power spectrum no. 5 in Figure 4 correspond to the RXTE observation containing that flare. The independent observation by two HEXTE units (Fig. 12a) confirms the origin of the flare from within \(1^\circ\) of the direction of Cyg X-1 and rules out a background event, e.g. a high-energy particle from a solar flare or cosmic rays. The

![Figure 11](image1.png)

Fig. 11. (a) The PCA and HEXTE (multiplied by 20 for clarity) time profiles of the strongest millisecond flare detected from Cyg X-1 as yet.\(^{24}\) (b) A comparison of the time profile of its precursor with (c) the 4.5–8 keV time profile of the flare in Sgr A*.\(^{2}\) The vertical axes in (b) and (c) have the same logarithmic length, and the time axis for Sgr A* is rescaled with respect to that for Cyg X-1 by their probable mass ratio, \(3 \times 10^5\).
Fig. 12. (a) The count rates from two HEXTE units during the strongest flare, Fig. 11a. The two units look alternatively at the source (black) and the background (red; 1° away). We see that the flare came from the direction of Cyg X-1 within the < 1° accuracy. (b) The positions of the PCA observations containing the 13 brightest flares detected from Cyg X-1$^{24}$ (black triangles) on the color-color diagram$^{15}$ showing all observations available so far (cyan circles). The upper and right axis gives the average spectral index$^{83}$ in the 3–6.4 keV and 6.4–16 keV energy band, corresponding to the soft and hard color, respectively. The line corresponds to both $\Gamma$ equal.

PCA count rate profile is well fitted by a stretched exponential with the FWHM of \( \sim 25 \) ms (red curve in Fig. 11b). The 3–30 keV flux in the peak of the flare had reached \( (3.0 \pm 0.6) \times 10^{-7} \) erg cm\(^{-2}\) s\(^{-1}\), which is \( \sim 30 \) times the flux before the flare. The profiles and time-scales of the shots reported in Refs. 19 and 56 are similar to this powerful flare, but their amplitudes are much weaker.

Even shorter time-scales were observed in the precursor \( \sim 0.5 \) s before the main flare, as shown in detail in Figure 11b. During the dramatic rise the count rate increased tenfold in just 2 ms. This is of the order of the light-travel time across an inner accretion disk around a 10$M_\odot$ black hole (1 ms \( \sim 20GM/c^3 \)), and it is about a half of the Keplerian period on the minimum stable orbit in the Schwarzschild metric. It also closely corresponds to the e-folding time of the 1999 flare$^2$ of \( \sim 400 \) s, which is \( \sim 30GM/c^3 \) for a 3 \( \times 10^6 M_\odot \) black hole. In Figure 11b, we show the lightcurve of the Sgr A* flare rescaled to the same dynamical timescale as Cyg X-1 flare in Fig. 11b.

Apart from this fastest and most powerful flare, 12 more flares from Cyg X-1 with the peak count rate in excess of 10$\sigma$ above the preceding average were discovered,$^{24}$ all of them in the hard state. Fig. 12(b) shows the positions in the color-color diagram of observations containing these flares. We see that the soft-state flare and hard-state ones are both associated with the extremes of the color distribution. More flares with smaller amplitudes can be found, and the distribution of the 12 hard-state flares is consistent with the high-amplitude tail of the log-normal shot distribution proposed in Ref. 55).
The limited photon statistics and bandwidth do not allow detailed spectral studies of the flares, though they are sufficient to determine the overall spectral index. The hard-state flares soften around the peak, while the powerful soft-state flare hardens, both reaching similar $\Gamma \sim 2$ at the peak. Still, the underlying physical mechanisms of the flares may be the same as in the persistent emission, i.e., thermal (hard state) or nonthermal (soft state) Comptonization (Fig. 2). The persistent emission models after increasing $L$ and adjusting the $L_H/L_S$ ratio to account for spectral softening/hardening are consistent with the flare spectra. The models yield the peak bolometric $L \sim 0.3L_{\text{Edd}} (d/2 \text{ kpc})^2 (10 M_\odot/M)$ for both soft and hard-state flares. This is about an order of magnitude brighter than the persistent $L$.

Powerful millisecond flares are not inherent to Cyg X-1 only. Similar events have been observed in two other black holes: XTE J1118+480 and GX 339–4 (Fig. 13). It is possible that more of the black holes exhibit powerful flares, but limitations in the photon statistics prevent us from detecting them.

The physical origin of the millisecond flares is yet to be established. Because of their very short time-scales they must be due to sudden release of the accretion energy in the inner region of the disk. This can be due to amplification of the magnetic field in the innermost plunging region of the disk, due to flipping among multiple state of the accretion flow with large amplitude on short dynamical time-scales or due to accumulation of a very large amount of energy in a flare above the disk surface and its subsequent fast release.

§4. Discussion and conclusions

We have reviewed spectral states of black hole binaries and their respective dominant radiative processes. In the hard state, the dominant process is thermal Comptonization of soft photons, most likely blackbody ones from an outer accretion disk. The thermal character of the distribution of the scattering electrons is probably related to the most likely source geometry, consisting of an inner hot accretion flow, see Fig. 14a. The electrons in the flow are powered by energy transfer from the hot ions, which receive most of the available gravitational energy. The stochastic nature of the energy transfer, probably via Coulomb interactions, results in the electron distribution being nearly thermal.

In addition, the cold medium gives rise to reprocessing, including Compton reflection and fluorescence. Relativistic broadening observed in some cases indicates
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Fig. 14. (a) A schematic representation of the likely geometry in the hard state, consisting of a hot inner accretion flow surrounded by optically-thick accretion disk. The hot flow constitutes the base of the jet (with the counter-jet omitted from the figure for clarity). The disk is truncated far away from the minimum stable orbit, but it overlaps with the hot flow. The soft photons emitted by the disk are Compton upscattered in the hot flow, and emission from the hot flow is partly Compton-reflected from the disk. (b) The likely geometry in the soft state consisting of flares/active regions above an optically-thick accretion disk extending close to the minimum stable orbit. The soft photons emitted by the disk are Compton upscattered in the flares, and emission from the flares is partly Compton-reflected from the disk.\(^{83}\)

that, in addition to an outer disk, there is some cold medium close to the black hole, e.g., from collapse of the innermost hot flow.\(^{75}\) The variability pattern observed on long timescales indicates that the dominant driver of the variability is changing irradiation of the hot flow by soft seed photons from the outer cold disk.\(^{83,84}\)

In the soft states, Compton scattering is by a hybrid, thermal/nonthermal electron distribution. The scattering plasma forms, most likely, active regions above the surface of an accretion disk, which emit the energetically dominant blackbody emission, see Fig. 14(b). The active regions are powered by energy transfer from inside the disk, most likely via magnetic buoyancy and subsequent magnetic field annihilation, leading then to acceleration of particles. This is inherently a nonthermal process, which explains the observed nonthermal photon spectra, showing no high-energy cutoff up to high energies. The ratio of the power in the active regions to the disk power increases in the sequence of the soft states: ultrasoft, high, intermediate/very high. Thus, the last state is characterized by a powerful corona surrounding most of the disk, in a modification of the picture of Fig. 14(b).

In a range of \(L/L_E\), either the hard/hot and soft/cold accretion flows are possible. This leads to hysteresis in the long-term lightcurve of black-hole binaries, and the corresponding long-term limit cycle.

A very interesting new phenomenon in black-hole binaries is that of millisecond
flares, extreme events occurring on timescales comparable to $GM/c^3$. In particular, the strongest flare discovered from Cyg X-1 appears to be the most extreme event detected from black-hole accretion yet.

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