STATISTICAL ANALYSIS OF ACOUSTIC WAVE PARAMETERS NEAR SOLAR ACTIVE REGIONS

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ABSTRACT

In order to quantify the influence of magnetic fields on acoustic mode parameters and flows in and around active regions, we analyze the differences in the parameters in magnetically quiet regions nearby an active region (which we call “nearby regions”), compared with those of quiet regions at the same disk locations for which there are no neighboring active regions. We also compare the mode parameters in active regions with those in comparably located quiet regions. Our analysis is based on ring-diagram analysis of all active regions observed by the Helioseismic and Magnetic Imager (HMI) during almost five years. We find that the frequency at which the mode amplitude changes from attenuation to amplification in the quiet nearby regions is around 4.2 mHz, in contrast to the active regions, for which it is about 5.1 mHz. This amplitude enhancement (the “acoustic halo effect”) is as large as that observed in the active regions, and has a very weak dependence on the wave propagation direction. The mode energy difference in nearby regions also changes from a deficit to an excess at around 4.2 mHz, but averages to zero over all modes. The frequency difference in nearby regions increases with increasing frequency until a point at which the frequency shifts turn over sharply, as in active regions. However, this turnover occurs around 4.9 mHz, which is significantly below the acoustic cutoff frequency. Inverting the horizontal flow parameters in the direction of the neighboring active regions, we find flows that are consistent with a model of the thermal energy flow being blocked directly below the active region.

Key words: Sun: activity – Sun: helioseismology – Sun: magnetic fields – Sun: oscillations – sunspots

1. INTRODUCTION

Solar acoustic waves are generated by turbulent convection near the solar surface and propagate in the solar interior. Waves below a certain frequency are trapped in the solar interior and those with a certain frequency and wavelength interfere constructively to form standing waves. Several million normal modes are excited with very small individual amplitudes and periods around five minutes. Changes in the wave properties as they propagate through the Sun can reveal spatial and temporal variations in the interior thermal structure and dynamics. In particular, the frequencies, amplitudes, and widths of the modes are modified as they propagate through a sunspot. Braun et al. (1987) were the first to observe reductions in acoustic wave power in active regions by up to half of that in magnetically quiet regions. Changes of the mode characteristics and flows in active regions have since been extensively studied using different techniques of local helioseismology, with the goals of studying the effects of magnetic fields on wave propagation, generation, and absorption, and also of inferring the subsurface structure of sunspots (see, for example, Rajaguru et al. 2001; Howe 2008; Rabello-Soares et al. 2008; Gizon et al. 2010; Baldner et al. 2013; Burtsvea et al. 2013; Tripathy et al. 2015, and references therein). However, both the physical mechanisms in play and the interpretation of the measurements are still subject to controversy.

In addition to the power reduction at frequencies below the acoustic cutoff frequency at about 5.5 mHz, there is a power enhancement of about 40%–60% at frequencies between 5.5 and 7.5 mHz in the areas surrounding active regions (Khomenko & Collados 2015, and references therein). This phenomenon, known as the “acoustic halo,” is observed both in the photosphere at the edges of active regions (Brown et al. 1992) and in the chromosphere (Braun et al. 1992) where it spreads out into the nearby quiet areas. The increase in size of the acoustic halo with height in the solar atmosphere enables tomography of the magnetic canopy.

Extraction of energy from acoustic waves incident on an inclined magnetic field by mode conversion seems to be able to explain the power reduction observed in sunspots (Khomenko & Collados 2015, and references therein). The magnetic fields lower the acoustic cutoff frequency, so that lower-frequency waves can escape into the outer atmosphere. The mode transformation happens at the critical atmospheric layer where the magnetic pressure equals the gas pressure. Mode conversion may also be responsible, at least in part, for the acoustic halo (Khomenko & Collados 2015; Pintér 2015; Rijs et al. 2016, and references therein). However, one cannot exclude other effects in the complex coupling between oscillations and the propagation medium.

The frequency of global acoustic modes as well as their amplitude and lifetime have also been observed to vary with the solar activity cycle (Elsworth et al. 2015, and references therein). The frequency variations are correlated with the local surface magnetic field strength at different latitudes at different phases of the cycle, following the magnetic butterfly diagram (Howe 2008).

Unfortunately, the determinations of wave parameters and flows in active regions may be affected by systematic errors due to the influence of the strong magnetic fields on the observational line itself (e.g., Komm et al. 2015). Local helioseismic analysis has always depended upon Doppler-shift observations of absorption lines that are also sensitive to the Zeeman effect, in order to obtain simultaneous magnetograms. As the shape of the lines is affected by strong magnetic fields (Couvidat et al. 2012), the line shifts obtained in active regions are unreliable as absolute measurements of the line-of-sight velocity (e.g., Rajaguru et al. 2006). To a certain extent, this may be true for the helioseismic inferences derived from them.
as well, although they depend only on the oscillatory component, not the absolute value. Although Rajaguru et al. (2007) found that these effects seem to be small, it is better to use observations from outside areas of strong magnetic field (Cally & Moradi 2013; Couvidat 2013). Also, because the amplitude of the oscillations is known to be strongly suppressed for undoubtedly physical reasons in regions of strong magnetic fields, it is not clear when averaging over finite areas how much of the signal is due to areas of strong versus weak fields.

In this work, we perform a statistical analysis of the perturbations in the acoustic wave characteristics in magnetically quiet regions close to active regions compared with those of quiet regions at the disk locations but far from any active region. We have analyzed the neighborhoods of each of the active regions observed by the Helioseismic and Magnetic Imager (HMI) on board the Solar Dynamics Observatory (Schou et al. 2012) during a period of almost five years. We also analyze the perturbations in the parameters obtained at the aforementioned active regions themselves for comparison. In quantifying the effect of the nearby active region on the mode parameters and flows, we aim to improve our understanding of the mechanisms involved in the interaction between acoustic waves and the strong magnetic fields in sunspots. We describe the data and our analysis method in Section 2, present our results in Section 3, and summarize and discuss them in Section 4.

2. DATA AND METHOD

The data used consist of full-disk Dopplergrams obtained at a 45 s cadence by HMI from 2010 May to 2015 January, corresponding to Carrington rotations 2097 through 2158. Small regions of the solar disk with a 5° diameter were tracked at the Carrington rotation rate for 9.6 hr each and remapped in solar latitude and longitude using Postel’s projection. Since the horizontal wavelengths of the acoustic modes seen on such a small scale are much smaller than the solar radius, they can be treated as plane waves. Hence, the power spectra calculated by three-dimensional Fourier transforms of the mapped and tracked data can be fitted to estimate the parameters of short-wavelength modes. This analysis was done by the HMI Ring-Diagram processing pipeline for regions with centers separated by 2° 5 in latitude and about 2° 5 of arc in longitude, for all regions extending from disk center to about 8°, as described in detail in Bogart et al. (2011a, 2011b).

The mode parameters were estimated using two different methods for parametric fitting of the ridges in the 3D power spectrum, \( P(k_x, k_y, \nu) \). Module “rdifit” fits a 13-parameter model to regions of the power spectrum at a set of selected frequencies within frequency bands of width \( \pm 100 \mu \text{Hz} \) for individual values of the horizontal wavenumbers \( k_x \) and \( k_y \) (Basu & Antia 1999). Module “rdifit” fits only 6 parameters to an annular region of the power spectrum at fixed frequencies at selected horizontal wavenumbers \( k \) (Haber et al. 2000). Both methods use a Lorentzian profile.

\[
P(k_x, k_y, \nu) = \frac{A}{\left(\frac{\nu - \nu_0}{\gamma}\right)^2 + 1} S_0 + B(k),
\]

where \( \nu_0 = \nu_0 + k_x U_x + k_y U_y \). In the case of rdifit, there is the addition of an asymmetry term \( S_0 \), defined as in Nigam & Kosovichev (1998), where \( S_0 = S^2 + [1 + S (\nu - \nu_0) / \gamma]^2 \); and, for rdifit, \( S = 0 \), thus \( S_0 = 1 \). The amplitude is \( A \), \( \gamma \) is the half width at half maximum, \( U_x \) and \( U_y \) are terms representing the advection due to zonal and meridional motions with respect to the tracking rate, respectively, and \( B(k) \) is the background term.

The six fitted parameters, \( p_j \), in rdifit are \( a_c, \gamma_c, \nu_0, U_x, U_y \), and one value for the background term, where \( \gamma_c = \exp(\gamma_c) / 2 \) and \( A = A_c = 2 \exp(a_c - \gamma_c) \). In this method, the spectrum is filtered prior to the fitting to minimize any anisotropy in ring power and simultaneously has its resolution decreased to increase processing speed (Haber et al. 2000). The 13 fitted parameters \( p_j, j = 1, 13 \) in rdifit are \( A_0, A_1, A_2, A_3, c, p, U_x, U_y, \gamma_e, \gamma_k, S \), and 2 background terms, where \( A = \exp[A_0 + A_1 (k - k_0) + A_2 (k_e/k)^2 + A_3 (k_e/k)^2] \), \( \gamma = \gamma_e + \gamma_k (k - k_0) \), and the mean frequency \( \nu_0 = c k \). For convenience, we will divide \( A \) into three components: \( A = A_4 A_5 A_6 \), where \( A_4 = \exp(A_1) \), \( A_5 = \exp(A_0 + \frac{A_2}{2}) \), and \( A_6 = \exp\left[\frac{A_3}{2} \cos(2\theta) + \frac{A_4}{2} \sin(2\theta)\right] \).

For each tracked region of the solar disk, the model parameters \( p_j \) are obtained for a set of oscillation modes: \( p_j(n, l, \ell) \) (Nicholas et al. 2004). Each mode is identified by its order \( n \), the number of nodes in the radial (or more correctly vertical) direction and an effective degree \( l \) given by: \( l(l + 1) = k^2 R^2 \), which need not be an integer, since the modes are analyzed as plane waves. Modes are determined with \( n \) in the range 0–3 for rdifit and 0–4 for rdifitc, and with \( l \) in the range 400–1700 (2600 for \( f \) modes). To study how the acoustic waves are modified as they propagate through a sunspot, we analyze the mode parameters in a magnetically quiet region close to an active region. The level of magnetic activity in each tracked region is given by the Magnetic Activity Index (MAI) which is also calculated by the HMI processing pipeline. Briefly, using the same mappings and temporal and spatial apodizations as the tracked Doppler data, the absolute values of all pixels in corresponding HMI line-of-sight magnetograms with an absolute value greater than 50 G \( |B| > 50 \) G are averaged, with the magnetograms sampled once every 48 minutes (i.e., about 12 magnetograms during the 9.6 hr tracking time; Bogart et al. 2011a, 2011b). We select all quiet patches with MAI < 5 G in our data set that have at least one large magnetic active region with MAI > 100 G in their vicinity. These active region patches will be referred to as target tiles (\( T \)). As the influence of the active region drops rapidly with distance (for example, Nicholas et al. 2004), we consider only tiles not more than 8° away from the center of the target tile, making a total of 36 neighboring tiles (the nearest non-overlapping tiles and the overlapping ones). In general, there are several tiles with MAI > 5 G in the vicinity of a target tile. We define the angle between the line from the center of the target tile to the nearby active region and the x-axis (longitude axis), \( \theta_{gr} \), as the average of the angles of all tiles with MAI > 5 G in the vicinity of the target tile weighted by their MAI and their distance from the target. We define also the distance from the target tile to the nearby active region (center to center) as the average of the distances to all tiles with MAI > 5 G in the neighborhood of the target tile weighted by their MAI. For all target tiles analyzed here, this distance is on average 6.71 ± 0.01 degrees.

Observed regions of the solar disk located away from disk center have a larger geometric foreshortening and a lower
effective spatial resolution, along with different resolution in the zonal and meridional directions. In order to avoid the systematic variations that these purely geometric effects have on the mode parameter determinations, for each target tile we select a set of 2 to 6 quiet tiles with no nearby active region (i.e., all patches in their vicinity have MAI <5 G as itself) at the same latitude and Stonyhurst longitude as the target. We refer to these as the comparison set, C. For a given target patch, the fitted parameters obtained for its comparison set are averaged for each mode and subtracted from the fitted parameters obtained for the target patch: \[ \Delta p_j (n, l, i) = p_j^f (n, l, i) - \langle p_j^c (n, l, i) \rangle \]. The relative difference of each fitted parameter \( p_j \) for each target tile \( i \) is given by \[ \frac{\Delta p_j (n, l, i)}{p_j^n (n, l, i)} = \frac{1}{p_j^n (n, l, i)} \left[ p_j^f (n, l, i) - \langle p_j^c (n, l, i) \rangle \right] \]. There are approximately twice as many targets with \( \theta_{ar} \) in the north-south direction (±20°) as in the east-west direction due to the tracking. Hence, the parameter differences are averaged over 10° intervals in \( \theta_{ar} \) for each mode \( (n, l) \), removing outliers greater than 3σ; these averages, \( \langle \Delta p_j (n, l, \theta_{ar}) \rangle \), are then averaged over all \( \theta_{ar} \) for each mode to form the parameter differences \( \langle \Delta p_j (n, l) \rangle \) or \( \langle \frac{\Delta p_j \left( \frac{n}{\theta} \right)}{\theta^n (n, l)} \rangle \). These parameter differences will be referred to as the nearby variations (nb).

For control purposes, we arbitrarily choose one of the tiles in the comparison set for each target and assume it is the target tile instead. We then repeat the calculation above, subtracting the mean of the comparison set (excluding the randomly chosen one) from the fake target, and averaged over \( \theta_{ar} \) intervals (using the value of the real target). We call this the control set.

We also calculate the difference in the fitted parameters obtained for an active tile with MAI between 110 and 120 G and its comparison set, C (as described above). The range in MAI was (arbitrarily) chosen to be associated with a sunspot. The parameter differences are then averaged over all tiles, \( \langle \Delta p_j (n, l) \rangle \). They will be referred to as active region variations (ar) and analyzed in comparison with the nearby variations in the next section.

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**Figure 1.** Top panels: the nearby (top left panel) and active (top right panel) region relative variation of the mean power in the ring, \( A_n \), obtained using rdft (full circles) and rdftf (open diamonds and dotted line) for \( f = 0° \) (red, \( p_1 \) (green), \( p_2 \) (blue), \( p_3 \) (cyan), and \( p_4 \) (salmon) modes). The very small symbols (full circles and diamonds) on both top panels, close to zero, are the results for the control set. The error bars represent the standard error of the mean which are very small. Bottom panels: the nearby relative variation of the maximum power in the ring, \( A_n A_{\theta} \) (bottom left panel) and of the anisotropic component of the amplitude, \( A_{\theta} \) (bottom right panel) for four different directions: \( \theta = 0° \) (in the direction of the nearby active region in black), \( \theta = 30° \) (red), \( \theta = 60° \) (salmon), and \( \theta = 90° \) (perpendicular to it in blue) obtained using rdft for \( f = 0° \) (stars), \( p_1 \) (triangles), \( p_2 \) (crosses), \( p_3 \) (diamonds), and \( p_4 \) (full circles) modes. The small black squares close to zero on the bottom left panel are the results for the control set for \( \theta = 0° \). The y range is different in the panels.
3. RESULTS

3.1. Amplitude

Figure 1 (top right panel) shows the active region relative variation of the mean power in the ring given by \( \Delta A_i \), \( \left\{ \frac{\Delta A_i}{A_i} (n, l) \right\}_{ar} \), obtained by rdfic (full circles) and rdfif (open diamonds and dotted line). As is well known, the attenuation is largest around 3 mHz (e.g., Khomenko & Collados 2015). The measured oscillation power is reduced by 40%–70% for modes with frequency smaller than \( \sim 4.8 \) mHz, with some dependence on mode order. In fact, for frequencies higher than \( \sim 3.5 \) mHz, the power reduction increases as frequency increases. It is zero around 5–5.3 mHz (depending on mode order) as determined using rdfic. At higher frequencies, we start to see an enhancement in the oscillation power due to the acoustic halo effect. The results of the two fitting methods agree well, except for \( f \) and \( p_1 \) modes with frequency larger than \( \sim 4.3 \) mHz. As mentioned in Section 2, rdfif fits less modes and only until \( n = 3 \).

Figure 1 (top left panel) shows the nearby relative variation of the mean power in the ring, \( \left\{ \frac{\Delta A_i}{A_i} (n, l) \right\}_{nb} \). It is also mainly a function of frequency. Mode amplitudes are still attenuated by as much as 10% around 3 mHz. It has been observed by several authors that the mode amplitude decreases linearly with magnetic field strength (e.g., Rabello-Soares et al. 2008; Baldner et al. 2013), and so the observed maximum nearby attenuation corresponds to the active region variation for a region with MAI \( \approx 10 \) G. The observed maximum nearby attenuation for \( f \) and \( p_1 \) modes happens at lower frequencies than the active region variation. Also, the power enhancement happens at a much lower frequency, around 4.2 mHz, and it is almost as large as in the magnetically active patch (around 20% at \( \sim 5.3 \) mHz). The \( f \) modes are not amplified for frequencies higher than \( \sim 4.2 \) mHz, its variation is close to zero for both fitting methods. Although, there are some differences between rdfic (full circles) and rdfif (open diamonds) results, there is an overall agreement between them. The variations given by the control set (small symbols in both upper panels) are much smaller than the target variation.

Simulations by Rijss et al. (2015, 2016) support the theory that the acoustic halo enhancement is caused by MHD mode conversion through regions of moderate and inclined magnetic fields as proposed by Khomenko & Collados (2009). Based on their sunspot model (Rijss et al. 2015), the distance from the nearby active region is such that the quiet regions analyzed here have magnetic field inclinations varying from 65° to 90° (i.e., horizontal), which would imply a small MAI and might account for the power enhancement at lower frequencies.

The rdfic method estimates also the anisotropy in the power, \( A_\theta \) (Section 2). It is more convenient to express \( A_\theta \) in relation to \( \theta_\text{ref} \) instead of solar latitude and longitude: \( A_\theta = \exp \left\{ \frac{\Lambda}{2} \cos^2[2(\theta' + \theta_\text{ref})] + \frac{\Lambda_2}{2} \sin^2[2(\theta' - \theta_\text{ref})] \right\} \), where \( \theta' = \theta - \theta_\text{ref} \). Figure 2 shows examples of \( \left\{ \frac{\Delta A_i}{A_i} (n, l) \right\}_{nb} \) for \( p_2 \) modes with four different frequencies. For modes with frequency smaller than 4.6 mHz, waves propagating in the direction of the nearby active region (\( \theta' = 0^\circ \)) are attenuated in relation to perpendicular to it (\( \theta' = 90^\circ \)), as one would expect. However, modes with frequency larger than 4.6 mHz have the opposite behavior and modes with frequency close to 4.6 mHz are isotropic. This is true for all \( n_s \), as can be seen in Figure 1 (bottom right panel), which shows \( \left\{ \frac{\Delta A_i}{A_i} (n, l) \right\}_{nb} \) for four propagation directions. For a given frequency, the anisotropy is larger for modes with a larger mode order \( n \) (or a smaller degree \( l \)). The anisotropy at higher frequencies is a small effect and it tends to be a constant value for frequencies higher than 5 mHz where it varies between \( \pm 1.2 \). Modes with \( n = 1 \) and \( \nu \approx 2.8 \) mHz or \( n = 2 \) and \( \nu \approx 3.2 \) mHz present the largest anisotropy, varying from \(-6.8\% \) for \( \theta' = 0^\circ \) to \( 7\% \) for \( \theta' = 90^\circ \).

These anisotropic variations are of the same order of magnitude as the attenuation in the constant term (top left panel). The total amplitude variation is shown in Figure 1 (bottom left panel) by adding the constant term in the amplitude with the azimuthal variation (top left and bottom right panels, respectively). For \( p \) modes with frequency larger than 4.2 mHz, there is an overall increase in mode amplitude due to the presence of the nearby active and this has very little dependence with the propagation direction in relation to the nearby active region. Modes with smaller frequencies are attenuated and present a strong anisotropy. Those propagating perpendicular to the nearby active region have the smaller attenuation, the largest is 4.5% for \( f \) modes with frequency close to 2.9 mHz. While modes propagating in the direction of the nearby active can be attenuated by as much as 16% (for \( p_1 \) modes with \( \nu \approx 3 \) mHz).

Cameron et al. (2011) compared their numerical simulation of the propagation of wave packets through a sunspot model with observations of active region NOAA 9787 using data from the Michelson Doppler Imager (MDI) on board the Solar and Heliospheric Observatory. We compared our results in Figure 1 (bottom right panel, black points) with their power spectra determination (Figure 9 in Cameron et al. 2011) for a point on the solar surface 60 Mm behind the sunspot and another at a 45° angle and at 85 Mm distance. The latter is used as a quiet-Sun reference, as suggested by those authors. Our results seem to agree. However, they see an attenuation \( \sim 15 \) times larger than ours (e.g., they observe a \( \sim 88\% \) power reduction for \( f \) modes with frequency close to 2.5 mHz, while here it is only 6%). At least part of this difference is due to the fact that our determination is for regions with a 60 Mm diameter, which is, on average, 80 Mm away from the sunspot in comparison to theirs, which is a very small region 60 Mm away.
3.2. Linewidth

The linewidth of a peak in the power spectrum is inversely proportional to the lifetime of the mode and contains information on the mode damping. Figure 3 (right panel) shows the active region variation of the half width at half maximum of the power in ring, \( \left\langle \frac{\Delta \gamma}{\gamma} (n, l) \right\rangle \). Although they give similar results, rdftit variation is systematically lower (by 15% on average) than rdfitc. The active region linewidth variation increases as frequency decreases below \( \sim 4.8 \) mHz until a certain frequency which varies with the mode order. These agree with previous results (e.g., Rajaguru et al. 2001; Rabello-Soares et al. 2008) and also with solar cycle variations (e.g., Pallé et al. 1990; Komm et al. 2000a, and references therein).

Figure 3 (left panel) shows the linewidth nearby variation, \( \left\langle \frac{\Delta \gamma}{\gamma} (n, l) \right\rangle \). The variation is also positive (but only by 2% or less) for frequencies smaller than \( \sim 4.2 \) mHz. On the other hand, the linewidth nearby variation for modes with frequency larger than 4.2 mHz decreases by as much as 10%. This decrease is more pronounced for frequencies larger than 4.2 mHz by as much as 8%. This decrease is a decrease in the mode excitation at frequencies smaller than 4.2 mHz, where it is \( \sim 8\% \).

The peculiar behavior of the variation for \( f \) and \( p_1 \) modes using rdftit is seen here. As in the linewidth variation for \( f \) and \( p_1 \) modes using rdfitc and rdftit (open diamonds and dotted line) for \( f \) (red), \( p_1 \) (green), \( p_2 \) (blue), \( p_3 \) (cyan), and \( p_4 \) (salmon) modes. The small symbols (full circles and diamonds) on both top panels, close to zero, are the results for the control set. The error bars indicate the standard error of the mean.

3.3. Energy

The surface velocity power of the mode is given by the area under the peak in the power spectrum, which can be approximated by the product of peak height and width. It is proportional to the mode mean square surface (radial) velocity averaged over time and over the solar surface. Thus it is also proportional to the mode energy (given by the mode kinetic energy). Figure 5 (top right panel) shows the mode energy active region variation, \( \left\langle \frac{\Delta E}{E} (n, l) \right\rangle \), where \( E \propto A_c \gamma_c \). There is a decrease in the mode energy in the active region for all modes analyzed here, even close to the cutoff frequency. Apparently, the increase in the mean power (given by \( A_c \)) at frequencies higher than 5 mHz obtained by rdftit (Figure 1 top right panel) is compensated for by the decrease in the linewidth (Figure 3 right panel). The decrease in mode energy is larger at frequencies smaller than \( \sim 4.2 \) mHz, where it is \( \sim 50\% \) on average, similar to the variation observed by others (e.g., Rajaguru et al. 2001, and references therein).

The nearby energy variation (top left panel) still shows a decrease in mode excitation at frequencies smaller than 4.2 mHz by as much as 8%. The relative energy decrease is very similar to the amplitude (Figure 1 top left panel), since the linewidth increases very little (Figure 3 left panel). At higher frequencies, there is a clear increase in the mode energy. The nearby energy variation is mainly a function of frequency varying from large negative values around 2.4 mHz toward zero at around 4.2 mHz and becoming increasingly large until 5 mHz. There is, however, for \( f \) and \( p_1 \) modes with frequency larger than 4.2 mHz, a large disagreement between the two fitting methods. This can also been seen in the active region variation as in the linewidth variation, \( p_4 \) modes have a distinct behavior in the nearby variation. Although the variation observed for \( p_4 \) modes using the control set is larger than for other modes and increases with frequency (small symbols in the same panel), it accounts only for half of the increase observed: \( \Delta \langle \Delta E/E \rangle_{nb} = 0.02 \) against 0.04. The linewidth...
Figure 4. Relative nearby (left panel) and active (right panel) region amplitude variation as a function of the width variation obtained using \(\text{rdftc}\) (full circles) and \(\text{rdff}\) (open diamonds and dotted line) for \(f\) (red), \(p_1\) (green), \(p_2\) (blue), \(p_3\) (cyan), and \(p_4\) (salmon) modes. For comparison purpose, the data in the left panel are plotted on the right panel as black crosses. The dashed line in both panels is the linear fit to the data. The vertical and horizontal error bars show the standard error of the mean.

Figure 5. Top panels: the nearby (top left panel) and active (top right panel) region relative variation of the mode energy \((\tilde{E} \propto A_{\gamma})\). Bottom panels: the nearby (bottom left panel) and active (bottom right panel) region relative variation of the mode energy rate \((\dot{\tilde{E}} \propto A_{\gamma^2})\). All panels show the variations obtained using \(\text{rdftc}\) (full circles) and \(\text{rdff}\) (open diamonds and dotted line) for \(f\) (red), \(p_1\) (green), \(p_2\) (blue), \(p_3\) (cyan), and \(p_4\) (salmon) modes. The small symbols (full circles and diamonds) on all panels, close to zero, are the results for the control set. The error bars correspond to the standard error of the mean.
variation observed for $p_4$ modes using the control set is much smaller, making it difficult to attribute $p_4$ mode distinctive behavior to bad fitting. The control set variation for other modes is very small but it is systematically displaced by 0.07 for nearby and active region energy variation. A very small systematic increase in the amplitude variation is also present in Figure 1.

Assuming, as in Libbrecht (1988), that each mode behaves like a damped oscillator, the temporal rate at which the energy is pumped in or out the mode, $\dot{E}$, is proportional to $A_n \gamma_n^2$. The temporal rate at which energy is removed from the mode at the active region (Figure 5 bottom right panel) does not vary strongly with frequency as observed for the other parameters. It is $-40 \pm 10\%$ on average for the modes analyzed here. (Komm et al. 2000b) observed a decrease in the energy rate with the increase of solar activity with no frequency dependence. Whereas, in the nearby region, energy is being removed from modes with frequency smaller than 4.2 mHz (Figure 5 bottom left panel); it is at maximum around 3 mHz. It is close to zero for modes with larger frequency, except for $p_4$ modes which seem to have a supply of energy (which would contribute to the halo effect). Again the variation observed in the control set is not enough to explain their behavior. The results obtained by rdifit for $f$ and $p_1$ modes show a more chaotic behavior, with strong decreases in the energy rate (around 3.8 and 4.8 mHz). The variation using the control set is systematically displaced 1% and is larger at higher frequencies.

3.4. Asymmetry

The asymmetry in the power spectra profile depends on the depth and properties of the acoustic sources responsible for exciting the acoustic modes and the part of the solar background noise that is correlated with the acoustic modes (e.g., Duvall et al. 1993; Kumar & Basu 1999; Toutain et al. 2006, and references therein). The larger the absolute value of the asymmetry parameter $S$, the more asymmetric is the peak. Previous studies found that the asymmetry is negative (i.e., the power in the low-frequency half of the peak is higher than that in the high-frequency part), as in Figure 6 (left panel).

Figure 6 (right panel) shows the active region and nearby variations of the line asymmetry, $\left\langle \frac{\Delta S}{S} \right\rangle$ (open diamonds and full circles, respectively), obtained using rdifit. The active region variation is divided, arbitrarily by 10 to make it comparable with the nearby variation at lower frequencies. The asymmetry variation at low frequency obtained for the control set (small symbols) is large and it was excluded from the analysis. The asymmetry seems to increase with the MAI (e.g., Rajaguru et al. 2001; Rabello-Soares et al. 2008; Salabert et al. 2011), which suggests that the modes are excited closer to the surface in active regions than in a quiet region (Kumar & Basu 1999). The asymmetry active region variation is positive for all modes, except for those $p_3$ modes with frequency smaller than 4.6 mHz and all of the $p_4$ modes observed here (Figure 6 right panel). This also agrees with results for variation with solar cycle, where Jiménez-Reyes et al. (2007) reported a 15% increase in the asymmetry negative values from minimum to maximum solar activity for low-degree modes ($l < 3$). The active region variation has a maximum for $f$ modes around 3 mHz where it is 2.5 times larger than at a quiet region and a local maximum around 5.2 mHz for $p_2$ and $p_3$ modes which the asymmetry is 100% larger. The nearby variation also has a maximum for $f$ modes around 3 mHz where it is 20% larger due to the presence of a nearby active region. For the $p$ modes, the nearby variation is quite different from the active region one. Around 5.2 mHz, where there is a local maximum for the active region variation, there is a minimum (or a maximum decrease in the asymmetry) at the nearby region by almost 3%.

3.5. Frequency

In the presence of strong magnetic fields, it is well observed that there is an increase of the mode frequency which is larger at larger frequencies until near the cutoff frequency where it sharply decreases. Figure 7 (right panel) shows the active
region variation of the mode’s central frequency, given by $V_0$ in Equation (1). This can be compared with results using 15° patches by (e.g., Rajaguru et al. 2001; Basu et al. 2004; Rabello-Soares et al. 2008 and others). The two fitting method show a similar increase with frequency, but the variation is systematically lower for rdftf. The nearby frequency variation also increases with frequency by as much as 0.1% (Figure 7 left panel). Although, this is an order of magnitude smaller than the active region variation, it is significant in comparison with the very small control set variation, which is given by the small symbols. The two fitting methods give different results for the nearby variation. However, they both show an increase with frequency until around 4.9 mHz, notably below the acoustic cutoff frequency where the variation sharply decreases, becoming negative in the case of rdftc.

In fact, here we do not observe a high enough frequency to see the sharp decrease in the active region frequency variation close to the cutoff frequency where it becomes negative, which was first observed by Ronan et al. (1994) and more recently by Rhodes et al. (2002), Howe (2008), and Rhodes et al. (2011), among others. This decrease in the mode frequency at active regions has been observed also as an increase in the degree (or wavenumber) at a given frequency (Schunker & Braun 2011). Jain & Roberts (1996) using a simple model of a chromospheric atmosphere with a horizontal magnetic field on top of a simple polytrope observed this change in the frequency shift sign and that the frequency where it happens depends on the amount of increase in magnetic field and temperature of the chromosphere. The fact that the sharp decrease observed at the nearby frequency variation happens at a lower frequency than at the active region could be due to a stronger horizontal magnetic field and/or temperature at the chromosphere near an active region.

As in the case of active region variation, the nearby frequency shift is mainly a function of frequency following roughly the inverse of inertia of the mode (before the sharp decrease). This indicates that the main mechanism responsible for the shifts is located very close to the solar surface, less than 0.5 Mm below the photosphere (Elsworth et al. 2015). However, after removing this “surface term” given by the frequency variation multiplied by the scaled mode inertia $Q(n, l)$ (i.e., normalized by the inertia of a radial mode of the same frequency), it has been estimated variations in the sound speed below an active varying between 3 and 10 Mm deep (Bogart et al. 2008; Baldo et al. 2013), which coincide in depth and magnitude with variation between solar minimum and maximum (Rabello-Soares 2012). Lin et al. (2009) showed that the above sound-speed determination have also a magnetic component since the solar models used in its determination did not include magnetic fields. The interpretation of these frequency variations has proven to be quite complicated and different local helioseismology methods give different results (Gizon et al. 2009).

The scaled nearby frequency variation, on the other hand, deviate very little from a smooth function of frequency indicating that the observed frequency variation is due to near-surface effects. The linear regression slope of the so called “surface term,” $\gamma(n, l) \equiv Q(n, l, 0) - Q(n, l, 0.03 mHz)$, is systematically lower for rdftc and three times larger for rdftf (1.4 ± 0.1 mHz$^{-1}$), in the frequency interval from 2.4 to 4.9 mHz. Note that the nearby frequency variation obtained by rdftf is negative for frequencies smaller than 3 mHz (Figure 7 left panel). The corresponding standard deviation to the straight line is 0.1 and 0.2 for rdftc and rdftf, respectively. On the other hand, for the active region variation, the standard deviation from a linear regression in frequency is much larger: 4 and 2 for rdftc and rdftf, respectively.

3.6. Flow

We will change the reference system for the flow from solar longitude–latitude given by zonal and meridional flows, $U_z(n, l)$ and $U_l(n, l)$ (Equation (1)), to parallel-perpendicular to the nearby active region by rotating the coordinate system for each target tile by its $\theta_{air}$ (defined in Section 2). The flow differences, $\langle \Delta U_z(n, l, \theta_{air}) \rangle_{ab}$, are averaged over all $\theta_{air}$, giving $\langle \Delta U_z(n, l) \rangle_{ab}$ and $\langle \Delta U_l(n, l) \rangle_{ab}$, which are plotted in Figure 8. There is no significant variation in $\langle \Delta U_l(n, l) \rangle_{ab}$ (right panel). On the other hand, the variation in $U_l$ (left panel) is much larger than the control set (small symbols). The variation in the direction of the nearby active region obtained by the two fitting methods are different.

$\langle \Delta U(n, l) \rangle_{ab}$ are inverted to infer the variation with depth using the optimally localized average (Backus & Gilbert 1968) technique as described in Basu et al. (1999). This inversion procedure was implemented in module rdnv of the HMI Ring-
Diagram processing pipeline (Bogart et al. 2011a, 2011b), which was used in this work. For the purpose of inversion, the fitted values of $\langle \Delta U(n, l) \rangle_{mb}$ are interpolated to the nearest integral value of $l$. There is a trade-off parameter in the inversion procedure, $\mu$, determining the balance between a well localized solution and a small solution error. Figure 9 shows a trade-off diagram at a depth of 3.5 Mm for the inversion results using the flow variations given by rdfite (left panel) and rdfitf (right panel) where the measurement of how well the solution is localized is given by $\Delta_{\mu}$ which is the difference between the first and third quartile points of the averaging kernel. The averaging kernel is defined as $\sum_{n,l} e_n e_l K_{n,l}(r)$, where $K_{n,l}$ are the mode kernels and $e_n e_l$ are the inversion coefficients. The best trade-off parameters for the data set obtained by rdfite and by rdfitf are $\mu = 0.0005$ and $\mu = 0.0002$, respectively (squares in Figure 9).

Figure 10 shows the solution for the parallel flow variation obtained for the rdfite (black) and rdfitf (red) data sets. The inferred flows are negative if moving away from the nearby active region (outflows) and positive if moving toward the nearby active region (inflows). The estimated flows are an average over a quiet region of 60 Mm in diameter with an active region 80 Mm away on average from its center. Since we are observing a small patch in the solar surface and, hence, fitting only modes with high degree that are trapped close to the solar surface, inversions are obtained only until a few Mm. The uncertainty in $\langle \Delta U(n, l) \rangle_{mb}$ is given by the error average of a large sample and is very small (Figure 8); consequently, the inversion solution errors are also very small.

There is a clear disagreement between the solutions for rdfite and rdfitf. The rdfite method fits a much larger number of modes than rdfitf (324 and 64, respectively) in the same power spectra range. The fewer modes obtained by rdfitf are not enough to obtain solutions as deep and as well localized as rdfite. On the other hand, the solution for rdfite presents an oscillatory behavior which is likely due to correlation between the errors in the solution at different depths. The errors in the solution at positions close to each other are generally correlated because they have been derived from the same mode set and this can introduce features in the solution as described by Howe & Thompson (1996).

Despite the disagreement between the fitting methods, they both observe a flow toward the active region at depths of, approximately, 0.5–1.5 Mm. Using rdfite, this flow is around $5 \text{ m s}^{-1}$, while for rdfitf, it is only $0.5 \text{ m s}^{-1}$. Both methods observed a region of zero horizontal flows around 2 Mm followed by a region of outward flows below. At a depth of 5 Mm, rdfite estimates a flow of $3 \text{ m s}^{-1}$ and rdfitf, $10 \text{ m s}^{-1}$. According to rdfite, the outflow persist to at least 7 Mm below the surface.

This agrees with the proposed picture described by Zhao et al. (2010) and others (Hindman et al. 2009; Gizon et al. 2003) with a circular flow below the sunspot penumbra with inflows at smaller depth and outflows deeper, forming a donut shape around the sunspot umbra. The circular flow is
believed to be powered by a downward flow caused by surface cooling within the plage which drags fluid in at shallow layers (Hindman et al. 2009) and by the obstruction of the umbra pushing away the flow at deeper layers (Gough 2013; Komm et al. 2015, and references therein). Our results agree in general with estimations of individual sunspot by different authors and are for a quiet region far away from the sunspot center. Featherstone et al. (2011) observed outflows from just below the surface until 7 Mm deep for a sunspot observed by MDI in 2002 January using ring-diagram analysis. They estimated maximum flows around a depth of 5 Mm, which are 100 m s$^{-1}$ at 28 Mm away from the sunspot’s center. Gizon et al. (2009) observed a maximum outflow 30 Mm away from the center of sunspot NOAA 9787 at all depths from 1 to 4.5 Mm. Around a depth of 4 Mm, the outflow has a maximum of 350 m s$^{-1}$ and, decreasing as the distance from the sunspot center increases, it is 20 m s$^{-1}$ when 80 Mm away. However, the estimated shallow inflow are of the same order (or much smaller, in the case of rdtf) than the outflow at deeper denser layers making the outward mass flux almost two orders of magnitude larger than inward. Since we are observing here only a small slice of the proposed circulation flow, a more complete picture might be able to account for the mass conservation.

4. SUMMARY

We analyzed differences in the acoustic mode parameters at solar magnetically quiet regions (five-degree in diameter) when there is an active region in their vicinity not farther than eight degrees away from the center of the quiet region, with those of quiet regions at the same disk location for which there are no neighboring active region. For each mode, these changes, dubbed nearby variations, are averaged over all of the data obtained by the HMI Ring-Diagram processing pipeline from 2010 May to 2015 January. We compared them with the variations observed in active regions with a mean line-of-sight magnetic field (MAI) between 110 and 120 G (in relation to quiet regions at the same location), which we refer to as active region variations. A summary of our results for each mode parameter is given below, followed by the results for the horizontal flows.

Amplitude. The amplitude nearby variation changes from attenuation to enhancement at 4.2 mHz, which is at a much lower frequency than the active region variation, around 5.1 mHz. The power reduction has a strong dependence on the wave direction. The amplitude decreases by as much as 16% if it is propagating in the direction of the nearby active region and only by less than 5% if it is perpendicular to it. The enhancement in power (known as acoustic halo effect) is as large as that observed in an active region (almost 20% at 5.3 mHz). There is some indication that the peak frequency is near 5.4 mHz. We do not observe any significant variation in the f-mode amplitudes above 4.2 mHz. There is a change in sign in the anisotropic component of the amplitude variation at 4.6 mHz. Below 4.6 mHz, it is negative (waves are attenuated) in the direction of the nearby active region and positive (they are amplified) perpendicular to it, and vice versa above 4.6 mHz. The amplitude anisotropy is important below 4.6 mHz; it can vary by as much as 13% with the wave propagation direction. It is small at higher frequencies, varying only 3% or less. At a given frequency, the anisotropy decreases (in absolute value) as the mode degree increases. The high inclined magnetic field in the vicinity of an active region might be responsible for the smaller cutoff frequency and enhanced power (Khomenko & Collados 2015; Rij s et al. 2015, 2016).

Linewidth. The change in sign in the linewidth nearby variation also happens at 4.2 mHz and at a lower frequency than the active region variation (which is around 4.8 mHz). The linewidth variation has an almost linear dependence on the amplitude variation. For the active region variation, the slope is equal to $-1$, while for the nearby variation it is $-2.6$. The increase in the linewidth is much smaller (2% or less), but the decrease is almost as large as in the active region (by as much as 9%).

Energy. As for the mode amplitude and linewidth, the mode energy nearby variation changes sign at 4.2 mHz. Below
4.2 mHz, the mode energy becomes smaller as the frequency decreases (until a given frequency) by as much as 8%. Otherwise, it increases with frequency. As a result, the nearby mode energy variation averages to zero over all modes. In active regions, there is a mode energy deficit at all frequencies, being 50% smaller on average for frequencies below 4.5 mHz.

Energy Rate. The temporal rate at which energy is pumped into or out of the mode is reduced by \((-40 \pm 10)/\%\) in active regions for all modes (assuming \(E\) is proportional to \(A_c \gamma^2\), with no frequency variation. The energy rate variation in quiet nearby regions decreases with increasing frequency, but does not usually change sign, merely reaching a maximum of zero at around 4.5 mHz.

There is a distinct behavior of \(p_s\) modes with respect to the other modes in linewidth nearby variation and, as consequence, in the energy and energy rate variations, and it cannot be easily explained by a bias in the fitting methods or in the power spectra calculation since their variation in the control set is small.

Asymmetry. Averaging over all modes with \(n < 4\) in a quiet region, we get \(S = -0.07\), which means that there is 7% more power on the low-frequency side of the power spectrum peak than on the high-frequency side. The asymmetry is larger (for most modes) in active regions. The nearby asymmetry variation for the \(f\) modes has behavior similar to the active region variation scaled down by about 15 times. It is at maximum around 2.8 mHz and decreases as the frequency increases. The \(p\) modes show a different behavior, especially at high frequencies where, instead of a maximum increase in the asymmetry as in the active region (around 5.2 mHz), the nearby variation shows a maximum decrease in the asymmetry.

Frequency. Comparing mode frequency variations, we find similar behavior in the nearby regions as in active regions, with positive shifts increasing slightly with increasing frequency until a point at which the frequency shifts turn over sharply and become negative. The maximum increase is 10 times smaller for the nearby variations. The point at which this turnover occurs in the quiet nearby regions, however, is around 4.9 mHz, significantly below the acoustic cutoff frequency, which is where it occurs in active regions. This could, in principle, be explained by a stronger horizontal magnetic field and an increase in temperature at the chromosphere according to a simple model by Jain & Roberts (1996). Below the turnover, the frequency variations vary inversely with the mode inertia, implying that their source is very close to the solar surface. This is more so for the nearby variation, since the linear regression of the relative frequency variation multiplied by the scaled mode inertia (known as the surface term) gives a standard deviation 40 times smaller for the nearby regions than for the active regions. The linear regression slope of the nearby surface term is \(0.43 \pm 0.03\) mHz\(^{-1}\) for rdtffit and 1.4 \pm 0.1 mHz\(^{-1}\) for rdfttf in the frequency interval 2.4–4.9 mHz.

Flow. The horizontal flow parameters in the direction of the nearby active regions were inverted, giving inflows toward the active regions at depths of around 1 Mm and outflows below 4 Mm, with no net horizontal flow between. These results agree with the proposed picture of a circular flow below the sunspot penumbra, forming a donut shape below and around the sunspot umbra.

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