Coexistence of full which-path information and interference in Wheeler’s delayed choice experiment with photons

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Abstract

We present a computer simulation model that is a one-to-one copy of an experimental realization of Wheeler’s delayed choice experiment that employs a single photon source and a Mach-Zehnder interferometer composed of a 50/50 input beam splitter and a variable output beam splitter with adjustable reflection coefficient \( R \) (V. Jacques et al., Phys. Rev. Lett. 100, 220402 (2008)). For \( 0 \leq R \leq 0.5 \), experimentally measured values of the interference visibility \( V \) and the path distinguishability \( D \), a parameter quantifying the which-path information WPI, are found to fulfill the complementary relation \( V^2 + D^2 \leq 1 \), thereby allowing to obtain partial WPI while keeping interference with limited visibility. The simulation model that is solely based on experimental facts, that satisfies Einstein’s criterion of local causality and that does not rely on any concept of quantum theory or of probability theory, reproduces quantitatively the averages calculated from quantum theory. Our results prove that it is possible to give a particle-only description of the experiment, that one can have full WPI even if \( D = 0 \), \( V = 1 \) and therefore that the relation \( V^2 + D^2 \leq 1 \) cannot be regarded as quantifying the notion of complementarity.

Key words: Wheeler’s delayed choice, complementarity, wave-particle duality, computational techniques, quantum theory

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1. Introduction

Particle-wave duality, a concept of quantum theory, attributes to photons the properties of both wave and particle behavior depending upon the circumstances of the experiment [1]. The particle behavior of photons has been shown in an experiment composed of a single beam splitter (BS) and a source emitting single photons and pairs of photons [2]. The wave character has been demonstrated in a single-photon Mach-Zehnder interferometer (MZI) experiment [2]. In 1978, Wheeler proposed a gedanken experiment [3], a variation on Young’s double slit experiment, in which the decision to observe wave or particle behavior is made after the photon has passed the slits. The pictorial description of this experiment defies common sense: The behavior of the photon in the past is said to be changing from a particle to a wave or vice versa.

Recently, Jacques et al. reported on an experimental realization of Wheeler’s delayed choice experiment using a single photon source and a MZI composed of a 50/50 input BS and a variable output BS with adjustable reflection coefficient \( R \) [4], a modification of the experiment presented in [5] in which two 50/50 BSs...
were used. A schematic picture of the experimental setup is shown in Fig. 1. The reflection coefficient \( R \) of the variable beam splitter (BS\(_{\text{output}}\)) can be controlled by a voltage applied to an electro-optic modulator (EOM), making it act as a variable wave plate. This can be done after each photon has entered the MZI. The phase-shift \( \Phi \) between the two arms of the MZI is varied by tilting the polarizing beam splitter (PBS) of the variable output BS. For \( 0 \leq R \leq 0.5 \) measured values of the interference visibility \( V \) \([6]\) and the path distinguishability \( D \) \([4]\), a parameter that quantifies the which-path information (WPI), were found to fulfill the complementary relation \( V^2 + D^2 \leq 1 \). The extreme situations \((V = 0, D = 1)\) and \((V = 1, D = 0)\), obtained for \( R = 0 \) and \( R = 0.5 \), give full and no WPI, associated with particlelike and wavelike behavior, respectively.

By choosing \( 0 < R < 0.5 \) Jacques et al. claim to have obtained partial WPI while keeping interference with limited visibility \([4]\), thereby having accomplished an affirmative delayed choice test of complementarity or wave-particle duality as it is often phrased.

Although the detection events (detector “clicks”) are the only experimental facts, the pictorial description of Jacques et al. \([4,5]\) is as follows: Linearly polarized single photons are sent through a 50/50 PBS (BS\(_{\text{input}}\)), spatially separating photons with S polarization (path 0) and P polarization (path 1) with equal frequencies. After the photon has passed BS\(_{\text{input}}\), but before the photon enters the variable BS\(_{\text{output}}\) the decision to apply a voltage to the EOM is made. The PBS of BS\(_{\text{output}}\) merges the paths of the orthogonally polarized photons travelling paths 0 and 1 of the MZI, but afterwards the photons can still be unambiguously identified by their polarizations. If no voltage is applied to the EOM then \( R = 0 \) and the EOM can be regarded as doing nothing to the photons. Because the polarization eigenstates of the Wollaston prism correspond to the P and S polarization of the photons travelling path 0 and 1 of the MZI, each detection event registered by one of the two detectors \( D_0 \) or \( D_1 \) is associated with a specific path (path 0 or 1, respectively). Both detectors register an equal amount of detection events, independent of the phase shift \( \Phi \) in the MZI. This experimental setting, corresponding to the open configuration of the MZI, clearly gives full WPI about the photon within the interferometer (particle behavior), characterized by \( D = 1 \). In this case no interference effects are observed, corresponding with a zero interference visibility \( (V = 0) \). When a voltage is applied to the EOM, then \( R \neq 0 \) (see Eq. (2) in \([4]\)) and the EOM acts as a wave plate.
rotating the polarization of the incoming photon by an angle depending on $R$. The Wollaston prism partially recombines the polarization of the photons that have travelled along different optical paths with phase difference $\Phi$ (closed configuration), and interference appears ($V \neq 0$), a result expected for a wave. The WPI is partially washed out, up to be totally erased when $R = 0.5$ ($D = 0, V = 1$).

The outcome of delayed-choice experiments [4,5,7,8,9,10,11] that is the average results of many detection events, is in agreement with wave theory (Maxwell or quantum theory). However, the pictorial description explaining the experimental facts [5] defies common sense: The decision to apply a voltage to the EOM after the photon left $BS_{\text{input}}$ but before it passes $BS_{\text{output}}$, influences the behavior of the photon in the past and changes the representation of the photon from a particle to a wave [5]. Although on one hand quantum theory can be used to describe the final outcome of this type of experiments (the average results of many detection events), on the other hand it does not describe single events [1]. Therefore, it should not be a surprise that the application of concepts of quantum theory to the domain of individual events may lead to conclusions that are at odds with common sense. Although not applying this reasoning to describe this type of experiments could prevent us from making nonsensical conclusions, this unfortunately would not give us a single clue as how to explain the fact that individual events are observed experimentally and, when collected over a sufficiently long time, yield averages that agree with quantum theory.

Since no theory seems to exist that can give a sensible description of the “whole” experiment, we adopted the idea to search for algorithms that could mimic (simulate) the detection events and experimental processes, including for example the random switching of the EOM for each photon sent into the interferometer. We moreover require that the algorithms used to simulate the action of an optical element, such as a BS or wave plate, on a photon should be independent of the experimental setup. In other words, the algorithms to simulate an optical component should be the same for all identical optical components within the same experiment but also within a different experiment. Hence, first solving the Schrödinger equation for a given experimental configuration and then simply generating events according to the resulting probability distribution is not what we have in mind when we perform an event-by-event simulation of the experiment. Similarly, first calculating the quantum potential (which requires the solution of the Schrödinger equation) and then solving for the Bohm trajectories is a different kind of event-by-event simulation than the one we describe in this paper. In this paper, the event-by-event simulation algorithm reproduces the results of quantum theory, without first solving a wave equation.

In this paper, we describe a model that, when implemented as a computer program, performs an event-by-event simulation of Wheeler’s delayed-choice experiment. Every essential component of the laboratory experiment (PBS, EOM, HWP, Wollaston prism, detector) has a counterpart in the algorithm. The data is analyzed by counting detection events, just like in the experiment [4,5]. The simulation model is solely based on experimental facts, satisfies Einstein’s criterion of local causality and does not rely on any concept of quantum theory or of probability theory. Nevertheless, our simulation model reproduces the averages obtained from the quantum theoretical description of Wheeler’s delayed choice experiment but as our approach does not rely on concepts of quantum theory and gives a description on the level of individual events, it provides a description of the experimental facts that does not defy common sense. In a pictorial description of our simulation model, we may speak about “photons” generating the detection events. However, these so-called photons, as we will call them in the sequel, are elements of a model or theory for the real laboratory experiment only. The experimental facts are the settings of the various apparatuses and the detection events. What happens in between activating the source and the registration of the detection events is not measured and is therefore not known. Although we always have full WPI of the photons in the closed configuration of the interferometer (we can always track the photons during the simulation), the photons build up an interference pattern at the detector. The appearance of an interference pattern is commonly considered to be characteristic for a wave. In this paper, we demonstrate that, as in experiment, it can also be build up by many photons. These photons have full WPI, never directly communicate with each other and arrive one by one at a detector.

The work described in this paper elaborates on the work described in [12] to simulate the experiment reported in [5]. The simulation model is built on ear-
lier work [13,14,15,16,17,18,19,20,21,22] that demonstrated that it may be possible to simulate quantum phenomena on the level of individual events without invoking a single concept of quantum theory. Specifically, we have demonstrated that locally-connected networks of processing units with a primitive learning capability can simulate event-by-event, the single-photon beam splitter and MZI experiments of Grangier et al. [2] and Einstein-Podolsky-Rosen experiments with photons [23,24,25]. Furthermore, we have shown that this approach can be generalized to simulate universal quantum computation by an event-by-event process [15,16]. Our event-by-event simulation approach rigorously satisfies Einstein’s criterion of local causality and builds up the final outcome that agrees with quantum theory event-by-event, as observed in real experiments.

2. Simulation model

The simulation algorithm can be viewed as a message-processing and message-passing process: It routes messengers one by one through a network of units that process messages. The messengers may be regarded as “particles”. These messengers carry a message which contains information about for example the relative time the particle traveled, its polarization, its color, its velocity, and so on. In other words, the message represents a so-called variable property of the particle that can be manipulated and measured given particular experimental settings. The components of the experimental setup such as the BS, the wave plates, the Wollaston prism and so on are so-called processing units that interpret and manipulate the messages carried by the particles. These processing units are put in a network that represents the complete experimental setup. Since at any given time there is only one messenger being routed through the whole network, there is no direct communication between the messengers. The only form of communication is through the processing units when the messengers are routed through the network. The model satisfies the intuitive notion of local causality.

In general, processing units consist of an input stage, a transformation stage, an output stage and have an internal vector representing their internal state. The input (output) stage may have several channels at (through) which messengers arrive (leave). Some processing units are simpler in the sense that the input stage is not necessary for the proper functioning of the device. As a messenger arrives at an input channel of a processing unit, the input stage updates its internal vector, and sends the message, represented by a vector, together with its internal vector to the transformation stage that implements the operation of the particular device. Then, a new message is sent to the output stage, using a pseudo-random number to select the output channel through which the messenger will leave the unit. We use pseudo-random numbers to mimic the apparent unpredictability of the experimental data only. The use of pseudo-random numbers is merely convenient, not essential.

In the experimental realization of Wheeler’s delayed choice experiment by Jacques et al. [4] linearly polarized single photons are sent through a PBS that together with a second, movable, variable output PBS with adjustable reflectivity $R$ forms an interferometer (see Fig. 1). The basic idea now is that we have to construct a model for the messengers representing the photons and for the processing units representing the optical components in the experimental setup. We require that the processing units for identical optical components should be reusable within the same and within different experiments. The network of processing units is a one-to-one image of the experimental setup [4] and is shown in Fig. 1. In what follows we describe some elements of our model in more detail. Additional information can be found in [12].

2.1. Messengers

In a pictorial description of the experiment the photons can be regarded as particles playing the role of messengers. Each messenger carries a (variable) message which contains information about its phase and polarization. The phase combines information about the frequency of the light source and the time that particles need to travel a given path. However, no explicit information about distances and frequencies is required since we can always work with relative phases.

The information carried by the messenger can be represented by a six-dimensional unit vector $y_{k,n} = (\cos \psi_{k,n}, \sin \psi_{k,n}, \cos \psi_{k,n}, \sin \psi_{k,n}, \cos \xi_{k,n}, \sin \xi_{k,n})$. 
The superscript H (V) refers to the horizontal (vertical) component of the polarization and $\psi_{k,n}^{H}$, $\psi_{k,n}^{V}$, and $\xi_{k,n}$ represent the phases and polarization of the photon, respectively. It is evident that the representation used here maps one-to-one to the plane-wave description of a classical electromagnetic field [6], except that we assign these properties to each individual photon, not to a wave. The subscript $n \geq 0$ numbers the consecutive messages and $k = 0, 1$ labels the channel of the PBS at which the message arrives (see below).

Since in this paper we will demonstrate explicitly that in our model photons always have full WPI even if interference is observed, we give the messengers one extra label, the path label having the value 0 or 1. The information contained in this label is not accessible in the experiment [4]. We only use it to track the photons in the network. The path label is set in the input BS and remains unchanged until detection. Therefore we do not consider this label in the description of the processing units but take it into account when we detect the photons.

2.2. Polarizing beam splitter

From classical electrodynamics we know that if an electric field is applied to a dielectric material the material becomes polarized [6]. The polarization $\mathbf{P}(\mathbf{k},t)$ is given by

$$
\mathbf{P}(\mathbf{k},t) = \int_{0}^{t} \chi(\mathbf{k},u)\mathbf{E}(\mathbf{k},t-u)du,
$$

(1)

where $\mathbf{E}(\mathbf{k},t)$ denotes the electric field vector, $\mathbf{k}$ is the wave vector, and $\chi$ is the linear response function [6].

From Eq. (1) it is evident that the dielectric material shows some kind of memory effect because the response (the polarization) of the material to the applied electric field is a function of both present and past values of the electric field. We use this kind of memory effect in our algorithm to model the PBS.

The processor that performs the event-by-event simulation of a PBS is depicted in Fig. 2. It consists of an input stage, a simple deterministic learning machine (DLM) [13,14,15,16], a transformation stage (T), an output stage (O) and has two input and two output channels labeled with $k = 0, 1$. We now define the operation of each stage explicitly.

- Input stage: The DLM receives a message on either input channel 0 or 1, never on both chan-
nels simultaneously. The arrival of a message on channel 0 (1) is named a 0 (1) event. The input events are represented by the vectors \( x_n = (1,0) \) or \( v_n = (0,1) \) if the \( n \)th event occurred on channel 0 or 1, respectively. The DLM has six internal registers \( Y^H_{k,n} = (C^H_{k,n}, S^H_{k,n}) \), \( Y^V_{k,n} = (C^V_{k,n}, S^V_{k,n}) \), \( Y^P_{k,n} = (C^P_{k,n}, S^P_{k,n}) \) and one internal vector \( x_n = (x_{0,n}, x_{1,n}) \), where \( x_{0,n} + x_{1,n} = 1 \) and \( x_{k,n} \geq 0 \) for \( k = 0,1 \) and all \( n \). These seven two-dimensional vectors are labeled by the message number \( n \) because their contents are updated every time the DLM receives a message. Note that the DLM stores information about the last message only. The information carried by earlier messages is overwritten by updating the internal registers.

Upon receiving the \((n+1)\)th input event, the DLM performs the following steps: It stores the first two elements of message \( y_{k,n+1} \) in its internal register \( Y^H_{k,n+1} = (C^H_{k,n+1}, S^H_{k,n+1}) \), the middle two elements of \( y_{k,n+1} \) in \( Y^V_{k,n+1} = (C^V_{k,n+1}, S^V_{k,n+1}) \), and the last two elements of \( y_{k,n+1} \) in \( Y^P_{k,n+1} = (C^P_{k,n+1}, S^P_{k,n+1}) \). Then, it updates its internal vector according to the rule [13]

\[
x_{i,n+1} = \alpha x_{i,n} + (1 - \alpha) \delta_{i,k},
\]

where \( 0 < \alpha < 1 \) is a parameter that controls the learning process [13]. Note that by construction \( x_{0,n+1} + x_{1,n+1} = 1, x_{0,n+1} \geq 0 \) and \( x_{1,n+1} \geq 0 \). From the solution of Eq. (2),

\[
x_n = \alpha^n x_0 + (1 - \alpha) \sum_{j=1}^{n-1} \alpha^{n-2-j} v_j,
\]

the correspondence to the expression for the polarization in classical electrodynamics Eq. (1) can be seen. The vector \( v \) plays the role of the electric field vector \( E \) and the internal vector \( x \) plays the role of the polarization \( P \). Hence, one could say that the internal vector \( x \) is the response of the PBS to the incoming messages (photons) represented by the vectors \( v \). Therefore the PBS “learns” so to speak from the information carried by the photons. The characteristics of the learning process depend on the parameter \( \alpha \) (corresponding to the response function). Equation (2) is the simplest learning rule we could think of. If experimental measurements for a single PBS would require another maybe more complicated rule to simulate the experimental outcome then we could modify the learning rule but given the information we have right now Eq. (2) suffices.

- Transformation stage: The second stage (T) of the DLM-based processor takes as input the data stored in the six internal registers \( Y^H_{k,n+1} = (C^H_{k,n+1}, S^H_{k,n+1}) \), \( Y^V_{k,n+1} = (C^V_{k,n+1}, S^V_{k,n+1}) \), \( Y^P_{k,n+1} = (C^P_{k,n+1}, S^P_{k,n+1}) \) and in the internal vector \( x_n = (x_{0,n+1}, x_{1,n+1}) \) and combines the data into an eight-dimensional vector (see Fig. 2).

Rewriting this vector as

\[
\begin{pmatrix}
    C^H_{0,n+1} + i S^H_{0,n+1} \\
    i (C^V_{0,n+1} + i S^V_{0,n+1}) S^P_{0,n+1} x_{0,n+1}^{1/2} \\
    i (C^V_{0,n+1} + i S^V_{0,n+1}) S^P_{0,n+1} x_{1,n+1}^{1/2} \\
    i (C^V_{1,n+1} + i S^V_{1,n+1}) S^P_{1,n+1} x_{0,n+1}^{1/2} \\
    i (C^V_{1,n+1} + i S^V_{1,n+1}) S^P_{1,n+1} x_{1,n+1}^{1/2}
\end{pmatrix}
\]

shows that the operation performed by the transformation stage T corresponds to the matrix-vector multiplication in the quantum theoretical description of a PBS, namely

\[
\begin{pmatrix}
    a^H_0 \\
    a^H_1 \\
    a^V_0 \\
    a^V_1
\end{pmatrix}
= \begin{pmatrix}
    b^H_0 \\
    b^V_0 \\
    b^H_1 \\
    b^V_1
\end{pmatrix}
\]

where \( (a^H_0, a^V_0, a^H_1, a^V_1) \) and \( (b^H_0, b^V_0, b^H_1, b^V_1) \) denote the input and output amplitudes of the photons with polarization \( H \) and \( V \) in the 0 and 1 channels of a PBS, respectively. Note that in our simulation model there is no need to introduce the concept of a vacuum field, a requirement in the quantum optical description of a PBS.

- Output stage: The final stage (O) sends the message

\[
w = (w_0, w_1, w_2, w_3, w_4, w_5)^T,
\]

where
rotates the polarization of the incoming photons by Eq. (2) in [4]) and the EOM acts as a wave plate that
2.3.
and the resulting averages do not change significantly.

through output channel 0 if \( u^2 > r \) where \( 0 < r < 1 \) is a uniform pseudo-random number. Otherwise,
if \( u \leq r \), the output stage sends through output
channel 1 the message \( z = (z_0, z_1, z_2, z_3, z_4, z_5)^T \),
where
\[
\begin{align*}
    w_0 &= C_{w,0}^H C_{w,1}^P \sqrt{w_{0,0} + 1}/u w_4, \\
    w_1 &= S_{w,1}^H C_{w,1}^P \sqrt{w_{0,0} + 1}/u w_4, \\
    w_2 &= -S_{w,1}^H S_{w,1}^P \sqrt{w_{0,0} + 1}/u w_5, \\
    w_3 &= C_{w,1}^V S_{w,1}^P \sqrt{w_{0,0} + 1}/u w_5, \\
    w_4 &= \sqrt{w_3^2 + w_2^2}/u, \\
    w_5 &= \sqrt{w_1^2 + w_1^2}/u, \\
    u &= \sqrt{w_0^2 + w_2^2 + w_3^2 + w_4^2},
\end{align*}
\]
(6)

Any other algorithm that selects the output channel in
a systematic manner might be employed as well. This
will change the order in which messages are being processed
but the content of the messages will be left intact
and the resulting averages do not change significantly.

2.3. Remaining optical components

The Wollaston prism is a PBS with one input channel
and two output channels and is simulated as the PBS
described earlier.

In contrast to the PBS, the HWP and the EOM are
passive devices. As can be seen from the wave mecha-
nical description, a HWP does not only change the po-
larization of the photon but also its phase [6].

When a voltage is applied to the EOM, \( R \neq 0 \) (see
Eq. (2) in [4]) and the EOM acts as a wave plate that
rotates the polarization of the incoming photons by
an angle depending on \( R \). In the simulation a pseudo-
random number is used to decide to apply a voltage to
the EOM or not. Also here we use a pseudo-random
number to mimic the experimental procedure to control
the EOM [4,5]. Any other (systematic) sequence to control the EOM can be used as well.

2.4. Detection and data analysis procedure

Detector \( D_0 \) (\( D_1 \)) registers the output events at
channel 0 (1). During a run of \( N \) events, the algorithm
generates the data set
\[
\Gamma(R) = \{ x_n, y_n, A_n | n = 1, ..., N; \Phi = \Phi_1 - \Phi_0 \}, \quad (8)
\]
where \( x_n = 0, 1 \) indicates which detector fired (\( D_0 \) or
\( D_1 \)), \( y_n = 0, 1 \) indicates through which arm of the MZI
the messenger (photon) came that generated the detec-
tion, not in the experiment), and \( A_n = 0, 1 \) is a pseudo-
random number that is chosen after the nth messenger
has passed the first PBS, determining whether or not a
voltage is applied to the EOM (hence whether the
MZI configuration is open or closed). Note that in one
run of \( N \) events a choice is made between no voltage
or a particular voltage corresponding to a certain reflec-
tivity \( R \) of the output BS (see Eq. (2) in [4]). The
angle \( \Phi \) denotes the phase shift between the two interfer-
ometer arms. This phase shift is varied by applying
a plane rotation on the phase of the particles entering
channel 0 of the second PBS. This corresponds to til-
ing the second PBS in the laboratory experiment [4].
For each \( \Phi \) and MZI configuration the number of 0 (1)
output events \( N_0 \) (\( N_1 \)) is calculated.

3. Simulation results

The algorithm described above directly translates
into a simple computer program that simulates the
messenger routing in a network that contains all the
optical components of the laboratory experiment [4].
Before the simulation starts we set \( x_0 = (x_0,0, x_1,0) =
(r, 1 - r) \), where \( r \) is a uniform pseudo-random
number. In a similar way we use pseudo-random
numbers to initialize \( Y_{0,0}^H, Y_{0,0}^V, Y_{0,0}^P, Y_{1,0}^H, Y_{1,0}^V, Y_{1,0}^P \) and
\( Y_{0,0}^H \). In this simulation, we send messengers to one input
channel of the input PBS only (see Fig. 1). The HWP in
Fig. 4. (Color online) Event-by-event simulation results of the interference visibility $V$ for different values of $R$ ((a)-(c)) and of $V^2$, $D^2$ and $V^2 + D^2$ as a function of the EOM voltage (d). (a)-(c) Circles give the results for the normalized intensities $N_0/N$ and $N_1/N$ as a function of the phase shift $\Phi$, $N_0$ ($N_1$) denoting the number of events registered at detector $D_0$ ($D_1$), for (a) $R = 0.43$ ($V = 0.98$), (b) $R = 0.05$ ($V = 0.45$) and (c) $R = 0$ ($V = 0$). For each value of $\Phi$, the number of input events $N = 10000$. The number of detection events per data point is approximately the same as in experiment. Dashed lines represent the results of quantum theory (Malus law). (d) Circles give the simulation results. Lines represent the theoretical expectations obtained from Eqs. (2), (3) and (7) in [4] with $\beta = 24^\circ$ and $V_0 = 217V$.

BS\textsubscript{output} changes the phases and also interchanges the roles of channels 0 and 1. Disregarding a few exceptional events, the PBS in BS\textsubscript{output} generates messages in one of the channels only. For a fixed set of input parameters, each simulation takes a few seconds on a present-day PC. In all simulations, $\alpha = 0.99$ [13].

We first demonstrate that our model yields full WPI of the photons. Figure 3 shows the number of detection events at $D_0$ as a function of $\Phi$ for $R = 0.5$. The events generated by photons following path 0 and path 1 of the MZI are counted separately. It is clear that the number of photons that followed path 0 and path 1 is equal and that the total intensity in output channel 0 obeys Malus law. Hence, although the photons have full WPI for all $\Phi$ they can build an interference pattern by arriving one by one at a detector.

Next, we calculate for $R = 0, 0.05, 0.43$ [4] and for each phase shift $\Phi$ and configuration (open or closed) of the MZI the number of events registered by the two detectors behind the output BS, just like in the experiment. Figure 4(a)-(c) depicts the interference visibility $V$. The simulation data quantitatively agree with the averages calculated from quantum theory and qualitatively agree with experiment (see Fig.3 in [4]). Calculation of $D$ as described in [4] gives the results for $D^2$ and $V^2$ shown in Fig. 4(d). Comparison with Fig.4 in [4] shows excellent qualitative agreement.

4. Conclusion

In this paper, we have presented a simulation model that is solely based on experimental facts, that satisfies Einstein’s criterion of local causality, that does not rely on any concept of quantum theory or of probability theory, and that provides a description of the experimental observations in [4] on the level of indi-
Fig. 3. (Color online) Event-by-event simulation results of the interference visibility $V$ for $R = 0.5$. Markers give the results for the normalized intensity $N_0/N$ as a function of the phase shift $\Phi$, $N_0$ denoting the number of events registered at detector $D_0$. Circles (triangles) represent the detection events generated by photons that followed path 0 (1) and squares represent the total number of detection events. For each value of $\Phi$, the number of input events $N = 10000$. The total number of detection events per data point (squares) is approximately the same as in experiment. The solid line represents the results of quantum theory.

individual events. In a pictorial description of our simulation model, we may speak about “photons” generating the detection events. In the simulation we can always track the photons, even in the closed configuration of the MZI. The photons always have full WPI, never directly communicate with each other, arrive one by one at a detector but nevertheless build up an interference pattern at the detector in the case of the closed configuration of the MZI. Hence, although for $0 < R \leq 0.5$ we find that $0 \leq D < 1$ and $D^2 + V^2 \leq 1$ with values for $D$ and $V$ in qualitative agreement with the experimental results, we always have access to full WPI, even in the case $D = 0$, $V = 1$. Our model thus provides a counter example for the fact that full WPI would correspond to $D = 1$. A further consequence is that the relation $V^2 + D^2 \leq 1$ cannot be regarded as quantifying the notion of complementarity: Our model allows a particle-only description for both the open and closed configuration of the MZI.

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