A Novel Approach for Evaluating Eddy Current Loss in Wind Turbine Generator Step-Up Transformers

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ABSTRACT

South Africa is aiming to achieve a generation capacity of about 11.4GW through wind energy systems, which will contribute nearly 15.1% of the country’s energy mix by 2030. Wind energy is one of the principal renewable energy determinations by the South African government, owing to affluent heavy winds in vast and remote coastal areas. In the design of newfangled Wind Turbine Generator Step-Up (WTGSU) transformers, all feasible measures are now being made to drive the optimal use of active components with the purpose to raise frugality and to lighten the weight of these transformers. This undertaking is allied with numerous challenges and one of them, which is particularly theoretical, is delineated by the Eddy currents. Many times the transformer manufacturer and also the buyer will be inclined to come to terms with some shortcomings triggered by Eddy currents. Still and all, it is critical to understand where Eddy currents emanate and the amount of losses and wherefore the temperature rise that may be produced in various active part components of WTGSU transformers. This is the most ideal choice to inhibit potential failure of WTGSU transformers arising from excessive heating especially under distorted harmonic load conditions. In the current work, an extension of the author’s previous work, new analytical formulae for the Eddy loss computation in WTGSU transformer winding conductors have been explicitly derived, with appropriate contemplation of the fundamental and harmonic load current. These formulae allow the distribution of the skin effect and computation of the winding Eddy losses as a result of individual harmonics in the winding conductors. These results can be utilized to enhance the design of WTGSU transformers and consequently minimize the generation of hotspots in metallic structures.

1. Introduction

South Africa remains engaged in diversifying the power mix that will make it possible to reduce the subjection to coal power generation. The ongoing decommissioning of various coal power plants resulting from end of service life, can potentially make way for a radically distinct power mix as opposed to the current monopolization by coal power plants which have an installed capacity of 40GW [1]. At the present day, South Africa’s Department of Energy through the Renewable Energy Independent Power Producer’s Procurement Programme (REI4P) has deployed a total of 64 renewable energy facilities, of which 25 are wind energy constituting of 961 wind turbines with a total generation capacity of 2.1 GW [2]. Wind energy currently contributes 52% of the country’s renewable energy capacity [3]. The wind energy tariff is currently at about R0.62/kWh, in which is about 45% less than the tariff for a coal plant. Each turbine generator in a wind energy facility is furnished with a step-up transformer at the bottom of the tower as shown in Figure 1 (a), which transforms its output voltage to a desired medium voltage (MV) collector level. In South Africa, these Wind Turbine Generator Step-Up (WTGSU) transformers are failing at an unnerving rate and utility owners are confounded to ascertain the potential causes for these prevailing deficiencies. A typical WTGSU transformer failure arising from an insulation failure which is attributable to a disc-to-disc short circuit failure to generate a spark that ignites the transformer oil as shown in Figure 1 (b).

Field experience is indicating that these failures are triggered by the use of regular distribution (RD) transformers that cannot meet the required operational requirements of the wind energy environment. With the objective to pledge future dependability of wind energy in South Africa, WTGSU transformers must integrate these requirements particularly with regard to a deformed loading.
cycle, harmonics and distortion, de-rating, switching over-voltages and stray gassing.

Owing to the increasing renewable energy market and applications of nonlinear loads, the evaluation of the winding stray losses in WTGSU transformer necessitates the consideration of the harmonic load current spectrum (HLCS), with appropriate computation of the electromagnetic fields (EMFs). Consequently, it is essential to study the impact of the HLCS on the winding stray losses and associated temperature rise of active part components.

In the current work, an extension of the author’s previous work [29], comprehensive analytical formulae to calculate the winding Eddy losses in the presence of harmonics by taking into account of the winding conductor dimensions, EMF and skin effect are derived. The acquired formulae ensure that the examination of the contribution of individual harmonics to the power losses is done. Therefore, these are effective formulae that can produce rapid results for electrical designers without the requirement of costly and high-class computational resources.

The remainder of this work is structured as follows. Section 2 outlines the challenges and electrical design considerations of WTGSU transformers. In Section 3, a winding Eddy loss formula is derived under normal operating conditions by taking into account the fundamental frequency, EMF, local flux density and winding conductor material properties. In section 4, a winding Eddy loss formula is derived under harmonic load conditions and takes into account the winding conductors, EMFs, skin effect, additionally, a new and simplified harmonic loss factor (HLF) is derived to account for the additional losses that will be seen by the WTGSU transformer during service. In Section 5, a case scenario of a WTGSU transformer supplying a distorted harmonic load is presented and corresponding losses are computed using proposed formulæ. These results are then compared with the method for calculating transformer losses recommended by the IEC standard and simulation results obtained by Finite Element Method. Finally, the conclusion is presented in Section 6.

2. Electrical design concerns

A large portion of wind turbine transformers currently in service are afflicted with numerous electrical concerns. These are prevalently on account of the unpredictable wind speed round the clock during their service. These inefficiencies are the main drivers of the premature failures of these transformers.

2.1. Distorted load cycle

Wind turbines depend to a large extent upon regional wind and other weather patterns, and their annual average capacity factor is close to 40% [30]. A majority of the power producers in the past projected the operational loading would be more than 50%. The comparatively light loading of WTGSU transformer present two
distinct and operationally momentous challenges that must be embedded into the design philosophy of WTGSU transformer.

The foremost challenge is that the WTGSU transformer’s relatively low average capacity factor falsify purchasing adjudication and invalidate classical economic models for regular distribution transformers. On account of the ideational nature of wind energy facility developments in South Africa, the Engineering, Procurement and Construction (EPC) developer is most frequently concerned with a cheaper initial transformer price. The utility owner who takes over responsibility of the facility from the EPC take a greater interest in the Total ownership cost (TOC) of the WTGSU transformer over its designed service lifetime. These costs include the initial purchase cost of the transformer, the cost of service no-load and load losses and routine maintenance costs [31-32]. The TOC models developed by authors in [31-34] do not take into consideration the relatively low average capacity factor of WTGSU transformers. Bearing in mind that the loading cycle of WTGSU transformers is so distinct from regular distribution transformers, EPCs must be mindful of the obsolete loss capitalization formulae when evaluating the TOC for WTGSU transformers.

Another challenge is that the WTGSU transformers are susceptible to regular thermal load cycling on account of the sporadic characteristic of the wind turbines. The latter give rise to the generation of hotspots in the transformer active part components including core, windings, clamping structure, flitch plates, tank walls et cetera. Recurrent thermal stresses drives the immersion of nitrogen gas into the hot insulating oil and it is emancipated as the insulating oil cools down. This phenomena results in the production of combustible gaseous bubbles that can potentially generate partial discharges and consequently damage the cellulose insulation. Additionally, sporadic thermal cycling can expedite the aging of electrical connections within the transformer tank.

2.2. Harmonics and distortion

The transformer design principle is formed on the rationale of generating an alternating EMF from a steady sinusoidal power supply voltage to instigate the flow of current and voltage potential in the winding conductors across that EMF.

During service, a steady sinusoidal wave shape is not practical. In the power system, the voltage and current wave shapes are distorted from the theoretical sinusoidal wave shapes. In practical terms, the total harmonic distortion (THD) ranging between 1 and 2 is prevalent at the point of common coupling (PCC). The application of non-linear loads in the facility can further contribute to distortion of the voltage and current wave shapes. These accumulative distortions reiterate very cycle, embellishing peaks that mount the voltage and current wave shapes and arise at distinct frequencies from the fundamental frequency of 50 Hertz (Hz) as shown in Figure 2.

The adverse effects of harmonics is that they trigger an upsurge in the copper loss, winding Eddy loss and stray loss in other metallic components. Eddy current and circulating current generate overheating in the transformer active part components, which must be treated by a sufficient cooling system design to thermal aging and untimely failures of WTGSU transformers during service. The wind turbine generator output, much like other renewable energy sources is intermittent and will produce distorted harmonic wave shapes. In this regard, the WTGSU transformer is operated with solid state controls which furnish additional harmonics and distortion.

Electrical generator systems that employ electronic switching devices and circuits also present specific problems for WTGSU transformers. From a manufacturer perspective, design philosophies to minimize the Eddy current loss to redress for harmonic load currents are imperative. While harmonic filtering is particularly not a function of a WTGSU transformer, magnetic shields strategically positioned between the windings may act as filters to mitigate the distorted harmonic currents into the collector bus. As a result, magnetic shielding should be deemed compulsory in the design of WTGSU transformers.

2.3. Switching Over-Voltages

A major concern with vast, wind turbine arrays is the necessity for connecting individual WTGSU transformers to the utility collector bus, leading to lengthy runs of cables. In large-scale wind facilities with a cluster of wind turbine towers, the WTGSU transformers may be positioned near the tower base as shown in Figure 1 in order to minimize the costs of large and lengthy runs of copper cables. Problems including excessive voltage drop, cable losses and risk of ground faults may arise from lengthy cable runs.

In view of the fact that wind energy facilities are in remote areas, they are more susceptible to lightning surges. As a result, surge arrestors must be mandatory for all WTGSU transformers.

Other things being equal, the biggest concern about switching over-voltages may be that generated by the wind turbines. On a 24-hours period, depending on the intermittent nature of wind; the wind turbines may be connected and disconnected online and offline when the wind speed increase and decline respectively. The latter may also occur when circuit breakers opens and closes the WTGSU transformer from the collector bus circuit. The switching phenomena by circuit breaker operation trigger transient over-voltages into the WTGSU transformers. This occurrence is aggravated by the application of vacuum circuit breakers, which have high-speed switching times. The fusion of the transient over-voltages and capacitance of the copper cables either HV or LV WTGSU transformer side may result in stationary waves and ringing that exceed the sinusoidal voltage amplitude as shown in Figure 3.
Excessive transient over-voltages can trigger WTGSU transformer insulation failures. The transient over-voltages as shown in Figure 3 contain fast rise-time and high voltage amplitudes which clash with the resonant frequencies on the windings and can introduce electrical stresses exceeding the dielectric capability of the windings.

### 3. Winding Eddy loss under normal conditions

During service the winding conductor is immersed in an alternating magnetic field and subsequently the Eddy current starts to flow. The energy loss dissipated as thermal energy on account of the Eddy current bring forth the Winding Eddy losses. The phenomena in rectangular winding conductors is demonstrated in Figure 4.

\[
B = B_{\text{max}} \sin \omega t \quad (1)
\]

The amount of magnetic flux passing through the unit area in eq. (2) is expressed as follows in Eq. (3).

\[
\Phi = B \times A \quad (3)
\]

It follows then, that the amount of magnetic flux characteristic that is perpendicular to the height and thickness in the closed-path can be described by the eq. (4).

\[
\Phi = B_{\text{max}} \times \sin \omega t \times 2hx \quad (4)
\]

The induced voltage in the closed-path can be expressed in accordance with the Faraday’s law of induction as expressed in Eq. (5).

\[
E = 4.44 \times f \times \Phi_{\text{max}} \quad (5)
\]

Equating the constant 4.44=√2 π yields the formula in Eq. (6)

\[
E = \sqrt{2} \pi \times f \times \Phi_{\text{max}} \quad (6)
\]

Taking into account the amount of magnetic flux passing through the closed-path unit area the eq. (6) yields the formula expressed in Eq.(7).

\[
E = \sqrt{2} \pi \times f \times B_{\text{max}} \times A \quad (7)
\]

Substituting the area of the closed-path in the induced voltage formula in Eq. (7) yields eq. (8).

\[
E = \sqrt{2} \pi \times f \times B_{\text{max}} \times 2hx \quad (8)
\]

The resistance of the closed-path can then be expressed as follows in Eq. (9).

\[
R = \rho \times \frac{(2h + 4x)}{L} \quad dx \quad (9)
\]

The winding Eddy loss in the closed-path dx is then expressed as shown in Eq. (10). Considering that the thickness of the closed-path is extremely small in relation to the height, then the distance x I negligible.

\[
dp = \frac{E^2L}{\rho \times 2h} \quad dx \quad (10)
\]

Substituting eq. (7) into eq. (10) yields the expression in Eq. (11).

\[
dp = \left[\frac{\sqrt{2} \pi \times f \times B_{\text{max}} \times 2hx}{\rho \times 2h}\right]^2L \quad dx \quad (11)
\]

Equating the constant √2 π=4.44 in Eq. (11) yields the formula in Eq. (12).

\[
dp = \left[\frac{4\pi \times f \times B_{\text{max}} \times 2hx}{\rho \times 2h}\right]^2L \quad dx \quad (12)
\]

Removing the square and expressing each terms to the exponent 2 yields eq. (13).
The standardized winding Eddy loss is then expressed by dividing eq. (18) with the rated copper loss to yield eq. (21).

\[ \Phi = B \times A \]  

Taking into consideration that the copper loss has a directly proportional relationship with the root mean square (RMS) load current under harmonic conditions [38-40] then first part of eq. (21) yields Eq. (22).

\[
\frac{P_{DC}}{P_{DC.R}} = \left( \frac{I_h}{I_R} \right)^2 \sum_{h=1}^{h_{max}} h^2 I_h^2
\]  

The contribution of the second part of Eq. (20) is as expressed in Eq. (17). The magnetic flux leakage under harmonic conditions has a directly proportional relationship to the RMS load current as expressed in Eq. (23).

\[ B = K_B I \]  

Under harmonic current conditions, the current I is expressed in Eq. (24).

\[
I = \sqrt{\sum_{h=1}^{h_{max}} I_h^2}
\]  

The harmonic current in Eq. (24) is expressed as \( I_h \). As such, the Eq. (24) yields Eq. (25).

\[
P_{WEC} = K \sum_{h=1}^{h_{max}} h^2 I_h^2
\]  

Here, the constant K is expressed as Eq. (23).

During service, when the transformer is operating at fundamental frequency, the equivalent rated winding Eddy loss is expressed as shown in Eq. (26).

\[
P_{WEC,R} = K I_R^2
\]  

Combining Eq. (25) and Eq. (26), the winding Eddy loss for a transformer operating under harmonic current can be expressed as shown in Eq. (27).

\[
P_{WEC} = P_{WEC,R} \sum_{h=1}^{h_{max}} h^2 \left( \frac{I_h}{I_R} \right)^2
\]  

Subsequently, combining Eq. (22) and Eq. (27) yields Eq. (28). This equation is formulated on the premise that induced current is at fundamental load current \( I_R \) of the transformer during service.

\[
P_{Winding} = \frac{P_{DC}}{P_{DC,R}} \sum_{h=1}^{h_{max}} \frac{h^2 I_h^2}{I_R^2} + P_{WEC} \sum_{h=1}^{h_{max}} h^2 \left( \frac{I_h}{I_R} \right)^2
\]  

Further simplification of Eq. (28) yields Eq. (29).
The allowance made in order to take into account of the harmonic load current in relation to their effects on transformer thermal performance is then expressed as follows in Eq. (30).

\[
F_{hl} = \frac{\sum_{h=1}^{h_{\text{max}}} h^2 I_h^2}{\sum_{h=1}^{h_{\text{max}}} I_h^2} = \frac{\sum_{h=1}^{h_{\text{max}}} h^2 \left(\frac{I_h}{I_1}\right)^2}{\sum_{h=1}^{h_{\text{max}}} \left(\frac{I_h}{I_1}\right)^2}
\]

(30)

In principle, the following conclusions can be drawn with regards to the Eddy current loss under harmonic current loading:

- The winding Eddy loss is directly proportional to the RMS load current and the harmonic order. This relationship is similar in the computation of the stray loss in tank walls, core clamps et cetera except that the harmonic order is expressed to an exponent of 0.8 [35].
- The skin effect is not taken into consideration at high harmonic order. The magnetic flux under these conditions does not completely penetrate the surface of the winding conductors.

In the next section, a weighted loss factor that considers the skin effect is derived.

4.2. Winding Eddy loss under harmonic current loading

The Eddy current problem form part to the area of quasi-stationary electromagnetic effects of conductors. Insomuch that, the displacement current enclosed by winding conductors may incessantly be ignored in relation to the conductive current. This is indeed the case even at high frequencies given that in practice only winding conductors comprising high electric conductivity are used. Eddy currents give rise to uneven dissemination of current density in a studied cross sectional area of a conducting conductor. This inherently leads to rise in joule heating as opposed to the state produced by direct current (DC). The Eddy currents and related uneven dissemination of the magnetic flux are known as the skin effect. The rise in current density give rise to resistive heating as opposed to the DC resistance as well as a reduction in the inductance. In addressing the skin effect problem, this study adopts the Maxwell equations in [38] and remodel these equations to treat the quasi-stationary electromagnetic effects of conductors. These equations are expressed as follows in Eq. (31) and Eq. (32).

\[
curl E = -\mu \frac{\partial H}{\partial t} \quad (31)
\]

\[
curl H = \sigma \quad (32)
\]

On the above equations an add-on of the Ohm’s law as expressed in Eq. (33).

\[
\sigma = \gamma E \quad (33)
\]

The electric field intensity must fulfil Eq. (34).

\[
div E = 0 \quad (34)
\]

Similarly, the magnetic field must fulfil Eq. (35).

\[
div H = 0 \quad (35)
\]

In investigating the dissemination of current, small but sufficiently long conductors are considered. The location of the conductors in a coordinate system as demonstrated in Figure 5. The height and ratio of these conductors fulfill the condition \( h > 2b \) and the spatial dependence on the \( y \)-coordinate may be ignored with insignificant error. When the current flows in the \( z \)-coordinate, the magnetic field has one component as described in Eq. (36).

\[
H = jH \quad (36)
\]

In the same order, the electric field intensity has a single component as expressed in Eq. (37).

\[
E = kE \quad (37)
\]

In the event that a winding conductor has the conductivity \( \gamma \) \([1/\Omega m]\), the permeability \( \mu \) \([H/m]\) and time-variant harmoniously at angular frequency \( \omega \) \([rad/s]\), by elimination the ordinary second-order differential Maxwell equations for magnetic field intensity vector is expressed as follows in Eq. (38).

\[
\frac{d^2 H}{dx^2} = k^2 H \quad (38)
\]

Here, the constant \( k \) is expressed as shown in Eq. (39).

\[
k^2 = j \omega \gamma \mu \quad (39)
\]

In investigating the skin effect in winding conductors with a spasmodic magnetic flux, the rectangular copper conductors in Figure 5 are considered.

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Figure 5: Two winding conductors immersed in alternating EMFs

The spasmodic magnetic flux streams along in the \( z \)-coordinate and the interaction of winding conductor 1 and 3 with respect to
winding conductor 2 is investigated in terms of the winding Eddy loss under harmonic conditions. The effect of the remainder of winding conductors will be disregarded in order to presume that the impact of winding conductor 1 and 3 will be completely offset in the center winding conductor. Presupposing a harmonic time response of the 2nd order differential equation in Eq. (38), with the initial conditions necessitated for symmetry along the edges of the winding conductors shall be valid the equation $H_{(x=±b)} = H_{(x=-b)}$ and will yield the solutions in Eq. (40) and Eq. (41) as expressed below. It is evident that the solution in this case scenario is of $h ≫ 2b$ nature.

$$H_0 = H_1 e^{kb} + H_2 e^{-kb}$$

$$H_0 = H_1 e^{-kb} + H_2 e^{kb}$$

Here, $H_0$ is the root mean square (RMS) magnetic field strength. Additionally, the condition of $x = ±b$ is valid since the impact along the edges of the winding conductors $±h/2$ is negligible if $x = ±b$ is satisfied. The constants of integration from Eq. (40) and Eq. (41) can then be expressed as follows in Eq. (42).

$$H_1 = H_2 = \frac{H_0}{\cosh kb}$$

The solution of the magnetic field strength presume the format expressed in Eq. (43).

$$H = H_0 = \frac{\cosh kx}{\cosh kb}$$

By association, the magnetic flux density by Eq. (42) is expressed as shown in Eq. (44).

$$B = \mu H_0 = \frac{\cosh kx}{\cosh kb}$$

Maxwell’s 1st equation in Eq. (33), can then be expressed as follows in Eq. (45).

$$\sigma = (\text{curl} H)_y = -kH_0 \frac{\sinh kx}{\cosh kb}$$

The constant $k$ is introduced into the rationalization of the equilateral hyperbola as shown in Eq. (46).

$$k = \frac{1 + j}{a}$$

The skin depth of penetration $a$ under harmonic conditions may be calculated as follows in Eq. (47).

$$a = \frac{2}{\sqrt{\omega \gamma \mu}}$$

The skin depth at various harmonic orders is demonstrated in Figure 6.

The formulation of the current density is acquired and expressed as shown in Eq. (48).

$$\sigma = \frac{1 + j}{a} H_0 \frac{\sinh(1 + j) x/a}{\cosh(1 + j) b/a}$$

With the expansion of the equilateral hyperbola the modulus of the current density is expressed shown in Eq. (49).

$$|\sigma| = \frac{\sqrt{\gamma}}{a} \frac{H_0}{H_0} \sqrt{\frac{\cosh(2x/a) - \cos(2x/a)}{\cosh(2b/a) + \cos(2b/a)}}$$

The dissemination of the magnetic flux density and current density along the surface of the winding conductors is described by Figure 7.

The magnetic flux leakage impinging upon one conductor is expressed by Eq. (50).

$$\Phi = \int_{-b}^{b} hB dx = \frac{2\alpha h \mu}{1 + j} H_0 \tanh(1 + j) \frac{b}{a}$$
The peak value of the magnetic flux leakage is given by Eq. (51).

\[ \sqrt{2} \Phi = 2ah\mu H_0 \frac{\cosh(2x/a) - \cos(2x/a)}{\cosh(2b/a) + \cos(2b/a)} \]  

Similarly, the magnetic flux density is expressed by Eq. (52).

\[ B_{\text{max}} = 2\mu H_0 \frac{a}{2b} \frac{\cosh(2x/a) - \cos(2x/a)}{\cosh(2b/a) + \cos(2b/a)} \]  

By employing Eq. (49) and introducing Eq. (52), the formulation of the current density is expressed as shown in Eq. (53).

\[ \frac{1}{2y} \int_{-b}^{b} |\sigma|^2 dx = \frac{1}{\omega b} \left( \frac{3}{6} \sinh(2b/a) - \sin(2b/a) \right) \]  

The variable \( \Xi \) is introduced here to account for expression of \( 2b/a \) above as shown in Eq. (54).

\[ \Xi = \frac{2b}{a} \]  

Forthwith, the Eddy loss per unit of volume of a winding conductor can be calculated using Eq. (17), where the weighted factor will be employed as expressed in Eq. (55).

\[ P = B_{\text{max}}^2 \gamma \omega b^2 \frac{3}{6} \frac{\sinh(2b/a) - \sin(2b/a)}{\cosh(2b/a) - \cos(2b/a)} \times F(\Xi) \]  

Here, the weighting function that takes into consideration the skin effect in winding conductors under harmonic conditions is expressed as follows in Eq. (56).

\[ F_H = \frac{3}{2} \frac{\sinh \Xi - \sin \Xi}{\cosh \Xi - \cos \Xi} \]  

This function is presented graphically at different conductor dimensions as shown in Figure 8.

It is evident from Figure 8, that at higher harmonic order, the magnetic flux leakage does not completely penetrate upon the surface of the conductors. The latter addresses the short coming of Eq. (30).

## 5. Materials and Methods

In this section, a WTGSU transformer rated at 5000 KVA, 11000/33000 volts, 3-phase, 50 cycles, oil-immersed, naturally cooled (ONAN), core type, double wound with copper conductor and fitted with on load tap changer is studied. The temperature rise in oil and winding conductors is 50 °C and 55 °C respectively. The rated losses under consideration are at 75°C on normal Tap position (in Watts) as shown in Table 1.

| Type of loss | Rated Losses (Watts) |
|--------------|----------------------|
| No load      | 4 500                |
| Copper       | 25 000               |
| Winding Eddy | 938                  |
| Other Stray  | 1 253                |
| Total        | 31 691               |

The studied transformer has a full load low voltage (LV) winding current of 262,43A with a mean winding Eddy loss at the highest loss ratio under rated conditions at 15% of the Copper losses.

The load that will been seen by the studied WTGSU transformer is described as shown in Figure 9. It is preferential that this harmonic load spectrum (HLS) to which the WTGSU will be susceptible be indicated to the transformer manufacturer during bid stage. A precise evaluation for the appropriate sizing of WTGSU transformers can only be designed by estimating the particular HLS.

![Figure 9: Harmonic Load Spectrum](image)

The resultant HLFs and service losses are computed and discussed in the next section.

## 6. Results

### 6.1. Computation of Harmonic Loss Factor

It is handy to specify a single digit that may have recourse to evaluate the capability of the studied WTGSU transformer in facilitating power to the supplied harmonic spectrum above. This
value viz. the harmonic loss factor (HLF) illustrates the effective RMS heating on account of the harmonic spectrum. The calculation of the HLF is tabulated in Table 2. The HLF by FEM is computed using the procedure described in [38].

Table 2: Computation of HLFs.

| h  | $I_h/I_1$ | $(I_h/I_1)^2$ | IEC    | Proposed | FEM   |
|----|-----------|---------------|--------|----------|-------|
| 1  | 0.97      | 0.941         | 0.941  | 0.941    | 0.941 |
| 3  | 0.37      | 0.137         | 1.232  | 1.090    | 1.213 |
| 5  | 0.35      | 0.123         | 3.063  | 2.569    | 2.924 |
| 7  | 0.1       | 0.010         | 0.490  | 0.100    | 0.448 |
| 9  | 0.028     | 0.001         | 0.064  | 0.063    | 0.055 |
| 11 | 0.11      | 0.012         | 1.464  | 1.455    | 1.184 |
| 13 | 0.071     | 0.005         | 0.852  | 0.807    | 0.640 |
| 15 | 0.026     | 0.001         | 0.152  | 0.135    | 0.106 |
| 17 | 0.057     | 0.003         | 0.939  | 0.925    | 0.600 |
| 19 | 0.047     | 0.002         | 0.797  | 0.774    | 0.468 |
|    |           |               | Total  | 1.234    | 9.994 |
|    |           |               | $I_{rms}(p.u)$ | 1.111   |       |

| HLF | 8.10 | 7.177 | 6.948 |

The ratio of the harmonic load current for each respective method and the RMS current (p.u) yields the HLFs as indicated previously.

6.2. Computation of Winding Eddy loss under harmonic current loading

The evaluation of the total service losses as a result of the HLC using the IEEE Std. C57.110-2018 is tabulated as shown in Table 3.

Table 3: Computation of total service losses: IEEE Std. C57.110-2018.

| Type of loss | Rated Losses (W) | Load Losses (W) | HLF | Service Losses (W) |
|--------------|------------------|-----------------|-----|--------------------|
| No load      | 4 500            | 4 500           | -   | 4 500              |
| Copper       | 25 000           | 30 859          | -   | 30 859             |
| Winding Eddy | 938              | 1158            | 8.10| 9 372              |
| Other Stray  | 1 253            | 1547            | 1.58| 2 442              |
| Total        | 31 691           | 38 064          | 47 173|                |

Under the supplied HLS, the service losses are witnessed to have a surge of about 33% and 19% from the rated and load losses respectively. The peak local load loss ratio for the HLC is computed as follows:

$$P_{LL}(p.u) = 1.234 \times [1 + 0.15 \times 8.177] = 1.249 \text{ p.u}$$

By applying proposed method, the maximum permissible harmonic load current with the supplied harmonic spectrum is as follows:

$$I_{max}(p.u) = \sqrt{\frac{P_{LL,R(pu)}}{1 + F_{HL}\times P_{EC,R}(p.u)}}$$

$$I_{max}(p.u) = \sqrt{\frac{1.15}{1 + 0.15 \times 8.1}} \times 262.43 = 261.048A$$

Consequently, with the supplied harmonic spectrum the studied WTGSU transformer capability is about 261.048A.

Table 4: Computation of total service losses: Proposed method

| Type of loss | Rated Losses (W) | Load Losses (W) | HLF | Service Losses (W) |
|--------------|------------------|-----------------|-----|--------------------|
| No load      | 4 500            | 4 500           | -   | 4 500              |
| Copper       | 25 000           | 30 859          | -   | 30 859             |
| Winding Eddy | 938              | 1158            | 7.177| 8 308              |
| Other Stray  | 1 253            | 1547            | 1.58| 2 442              |
| Total        | 31 691           | 38 064          | 46 110|                |

Under the supplied HLS, the service losses are witnessed to have a surge of about 31% and 17% from the rated and load losses respectively. The peak local load loss ratio for the HLC is computed as follows:

$$P_{LL}(p.u) = I_{rms(p.u)}^2 \left(1 + F_{HL} \times P_{EC,R}\right)$$

$$P_{LL}(p.u) = 1.234 \times [1 + 0.15 \times 7.177] = 1.248 \text{ p.u}$$

By applying proposed method, the maximum permissible harmonic load current with the supplied harmonic spectrum is as follows:

$$I_{max}(p.u) = \sqrt{\frac{1.15}{1 + 0.15 \times 7.177}} \times 262.43 = 259.85 A$$

Consequently, with the supplied harmonic spectrum the studied WTGSU transformer capability is about 259.85A. The evaluation of the total service losses as a result of the HLC using FEM [38] is tabulated as shown in Table 5.

Table 5: Computation of total service losses: FEM

| Type of loss | Rated Losses (W) | Load Losses (W) | HLF | Service Losses (W) |
|--------------|------------------|-----------------|-----|--------------------|
| No load      | 4 500            | 4 500           | -   | 4 500              |
| Copper       | 25 000           | 30 859          | -   | 30 859             |
| Winding Eddy | 938              | 1158            | 6.948| 8 043              |

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Other Stray & 1 253 & 1547 & 1.58 & 2 442 \\ Total & 31 691 & 38 064 & 1.58 & 45 844 

Under the supplied HLS, the service losses are witnessed to have a surge of about 31% and 17% from the rated and load losses respectively. The peak local load loss ratio for the HLC is computed as follows:

$$P_{LI}(p, u) = I_{rms(p,u)}^2 (1 + F_{PL} \times P_{EC,R})$$

$$= 1.234 \times [1 + 0.15 \times 6,948] = 1.247p, u$$

Based upon the FEM procedure [38], the maximum permissible harmonic load current with the supplied harmonic spectrum is as follows:

$$I_{max}(p, u) = \sqrt{\frac{1.15}{1 + 0.15 \times 6,948}} \times 262,43$$

$$= 258,70 A$$

Consequently, with the supplied harmonic spectrum the studied WTGSSU transformer capability is about 258,70A.

7. Conclusions

In the current work, an extension of the author’s previous work [29], new analytical formulae for the Eddy loss computation in transformer winding conductors have been explicitly derived, with appropriate contemplation of the fundamental and harmonic load current. These formulae allow the distribution of the skin effect and computation of the winding Eddy losses as a result of individual harmonics in the winding conductors. The rectangular winding conductors considered are based on real transformer geometries and represents the configuration of the conductors carrying harmonic load current.

The new formulae were triumphantly corroborated by comparing their performance with computationally intensive FEM simulations, authenticating their adequacy and efficacy. On that account, our findings are handy for the transformer manufacturing industry, where the transformer anatomy and design necessitate specific performance and inexpensive computational resources.

Additionally, it has been demonstrated that the harmonic load currents minimizes the depth of skin effect, lead to an increase in the copper losses and winding stray losses and, thereby, consideration must be given for proper evaluation and design of air for purpose transformers capable of facilitating wind power. These formulae can be applied in the transformer design systems for calculating the effects of harmonics on the transformer active part components. These results can be utilized to enhance the design of transformer s and consequently minimize the generation of hotspots in metallic structures. In this way, the developed formulae are a critical furtherance to the existing methodologies employed by manufacturers.

The method herein provides a fundamental basis for subsequent development such as analysis of thermal performance of transformers in wind power technologies.

Future work involves the development of TOC model for WTGSSU transformers to evaluate their economic life by considering the intermittent nature of wind turbine generators.

Conflict of Interest

The authors declare no conflict of interest.

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