Generating Reference Texts for Short Answer Scoring Using Graph-based Summarization

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Abstract

Automated scoring of short answers often involves matching a student's response against one or more sample reference texts. Each reference text provided contains very specific instances of correct responses and may not cover the variety of possibly correct responses. Finding or hand-creating additional references can be very time consuming and expensive. In order to overcome this problem we propose a technique to generate alternative reference texts by summarizing the content of top-scoring student responses. We use a graph-based cohesion technique that extracts the most representative answers from among the top-scorers. We also use a state-of-the-art extractive summarization tool called MEAD. The extracted set of responses may be used as alternative reference texts to score student responses. We evaluate this approach on short answer data from Semeval 2013’s Joint Student Response Analysis task.

1 Introduction

Short answer scoring is a critical task in the field of automated student assessment. Short answers contain brief responses restricted to specific terms or concepts. There is a great demand for new techniques to handle large-scale development of short-answer scoring engines. For example an individual state assessment may involve building scoring algorithms for over two hundred prompts (or questions). The past few years have seen a growth in the amount of research involved in developing better features and scoring models that would help improve short answer scoring (Higgins et al., 2014; Leacock and Chodorow, 2003). The Automated Student Assessment Prize (ASAP-SAS (2012)) competition had a short answer scoring component.

Short answer datasets are typically provided with one or more sample human references, which are representative of ideal responses. Student responses that have a high text overlap with these human references are likely to get a higher score than those that have a poor overlap. However often these sample human references are not representative of all possible correct responses. For instance consider the question, sample reference and a set of top-scoring student responses for a prompt from the ASAP-SAS (2012) competition in Table 1. The human reference provided does not encompass all possible alternative ways of expressing the correct response.

A number of approaches have been used to extract regular expressions and score student responses. Pulman and Sukkarieh (2005) use hand-crafted patterns to capture different ways of expressing the correct answer. Bachman et al. (2002) extract tags from a model answer, which are matched with stu-
dent responses to determine their scores. Mitchell et al. (2003) use a mark scheme consisting of a set of acceptable or unacceptable answers. This marking scheme is similar to a sample reference. Each student response is matched with these marking schemes and scored accordingly. The winner of the ASAP competition spent a lot of time and effort hand-coding regular expressions from the human samples provided, in order to obtain better matches between student responses and references (Tandalla, 2012). Although hand-crafting features might seem feasible for a few prompts, it is not an efficient technique when scoring large datasets consisting of thousands of prompts. Hence there is a need to develop automated ways of generating alternate references that are more representative of top-scoring student responses.

We use two summarization techniques to identify alternative references from top-scoring student responses for a prompt. Klebanov et al. (2014) use summarization to generate content importance models from student essays. We propose a graph-based cohesion technique, which uses text structure and semantics to extract representative responses. We also use a state-of-the-art summarization technique called MEAD (Radev et al., 2004), which extracts a summary from a collection of top-scoring responses. The novelty of our work lies in the utilization of summarization to the task of identifying suitable references to improve short-answer scoring.

2 Approach

Top-scoring responses from each prompt or question are summarized to identify alternate reference texts with which student responses could be compared to improve scoring models.

2.1 Graph-based Cohesion Technique

We use an agglomerative clustering technique to group lexico-semantically close responses into clusters or topics. The most representative responses are extracted from each of the clusters to form the set of alternate references. Just as in a cohesion-based method only the most well-connected vertices are taken to form the summary (Barzilay and Elhadad, 1997), likewise in our approach responses with the highest similarities within each cluster are selected as representatives.

Steps involved in generating summaries are:

**Generating Word-Order Graphs:** Each top-scoring response is first represented as a word-order graph. We use a word-order graph representation because it captures structural information in texts. Graph matching makes use of the ordering of words and context information to help identify lexical changes. According to Makatchev and VanLehn (2007) responses classified by human experts into a particular semantic class may be syntactically different. Thus word-order graphs are useful to identify representatives from a set of responses that are similar in meaning but may be structurally different.

During graph generation, each response is tagged with parts-of-speech (POS) using the Stanford POS tagger (Toutanova et al., 2003). Contiguous subject components such as nouns, prepositions are grouped to form a subject vertex, while contiguous verbs or modals are grouped into a verb vertex and so on for the other POS types. Ordering is maintained with the edges capturing subject—verb, verb—object, subject—adjective or verb—adverb type of information. Graph generation has been explained in detail in Ramachandran and Gehringer (2012).

**Calculating Similarity:** In this step similarities between all pairs of top-scoring responses are calculated. Similarities between pairs of responses are used to cluster them and then identify representative responses from each cluster. Similarity is the average of the best vertex and edge matches.

\[
\text{Similarity}(A, B) = \frac{1}{|V_A|+|V_B|} \left( \sum_{V_A} \max \{ \text{sem}(V_A, V_B) \} \right) + \sum_{V_B} \max \{ \text{sem}(V_B, V_A) \} + \sum_{E_A} \max \{ \text{sem}(E_A, E_B) \} + \sum_{E_B} \max \{ \text{sem}(E_B, E_A) \}
\]

In equation 1 \( V_A \) and \( V_B \) are the vertices and \( E_A \) and \( E_B \) are the edges of responses \( A \) and \( B \) respectively. We identify the best semantic match for every vertex or edge in response \( A \) with a vertex or edge in response \( B \) respectively (and vice-versa). \text{sem} is identified using WordNet (Fellbaum, 1998).

**Clustering Responses:** We use an agglomerative clustering technique to group responses into clusters. The clustering algorithm starts with assigning every response in the text to its own cluster. Ini-
tially every cluster’s similarity is set to 0. A cluster’s similarity is the average of the similarity between all pairs of responses it contains.

We rank response pairs based on their similarity (highest to lowest) using merge sort, and assign one response in a pair to the other’s cluster provided it satisfies the condition in Equation 2. The condition ensures that a response (S) that is added to a cluster (C) has high similarity, i.e., is close in meaning and context to that cluster’s responses (SC).

\[
\left( C_{\text{clusterSimilarity}} - \frac{\sum \text{Similarity}(S, SC)}{|C|} \right) \leq \alpha \tag{2}
\]

The choice of cluster to which a response is added depends on the cluster’s similarity, i.e., a response is added to the cluster with higher similarity. If both responses (in the pair) have same cluster similarities, then the larger cluster is chosen as the target. If cluster similarity and the number of responses are the same, then the target is selected randomly.

**Identifying Representatives:** In this step the most representative responses from each cluster are identified. The aim is to identify the smallest set of representatives that cover every other response in the cluster. We use a list heuristic to handle this problem (Avis and Imamura, 2007). We order responses in every cluster based on (a) decreasing order of their average similarity values, and (b) decreasing order of the number of responses they are adjacent to.

Our approach ensures that responses with the highest semantic similarity that cover previously uncovered responses are selected. Representatives from all clusters are grouped together to generate the representative responses for a prompt.

### 2.2 MEAD

We use MEAD as an alternative summarization approach. Radev et al. (2004) proposed the use of an automated multi-document summarization technique called MEAD. MEAD was developed at the University of Michigan as a centroid-based summarization approach. MEAD is an extractive summarization approach that relies on three features: position, centroid and the length of sentences to identify the summary. MEAD’s classifier computes a score for each sentence in the document using a linear combination of these three features. Sentences are then ranked based on their scores and the top ranking sentences are extracted to generate summaries. The extraction can be restricted to the top N words to generate a summary of specified length.

In our study each document contains a list of top-scoring responses from the dataset, i.e., each top-scoring response would constitute a sentence. For our study we use MEAD1 to extract summaries of length that match the lengths of the summaries generated by the graph-based cohesion technique.

### 3 Experiment

#### 3.1 Data

Semeval’s Student Response Analysis (SRA) corpus contains short answers from two different sources: Beetle and SciEntsBank (Dzikovska et al., 2013)2. Beetle contains responses extracted from transcripts of interactions between students and the Beetle II tutoring system (Dzikovska et al., 2010). The SciEntsBank dataset contains short responses to questions collected by Nielsen et al. (2008).

Beetle contains 47 questions and 4380 student responses, and SciEntsBank contains 135 questions and 5509 student responses (Dzikovska et al., 2013). Each dataset is classified as: (1) 5-way, (2) 3-way and (3) 2-way. The data in the SRA corpus was annotated as follows for the 5-way classification: **correct:** student response that is correct, **partially correct, incomplete:** response that is correct but does not contain all the information in the reference text, **contradictory:** response that contradicts the reference answer, **irrelevant:** response that is relevant to the domain but does not contain information in the reference, **non domain:** response is not relevant to the domain. The 3-way classification contains the contradictory, correct and incorrect classes, while the 2-way classification contains correct and incorrect classes.

Dzikovska et al. (2013) provide a summary of the results achieved by teams that participated in this task. Apart from the dataset, the organizing committee also released code for a baseline, which included lexical overlap measures. These measures

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1We use the code for MEAD (version 3.10) available at http://www.summarization.com/mead/.

2The data is available at http://www.cs.york.ac.uk/semeval-2013/task7/index.php?id=data
Table 2: Comparing performance of system-generated summaries of top-scoring short answers with the performance of sample reference texts provided for the Semeval dataset.

| Data Type   | System               | 5-way F1-overall | Weighted-F1 | 3-way F1-overall | Weighted-F1 | 2-way F1-overall | Weighted-F1 |
|-------------|----------------------|------------------|-------------|------------------|-------------|------------------|-------------|
| Beetle      | Baseline features    | 0.424            | 0.483       | 0.552            | 0.578       | 0.788            |
|             | (Dzikovska et al., 2013) |                 |             |                  |             |                  |
|             | Graph (~62 words)    | 0.436            | 0.533       | 0.564            | 0.587       | 0.794            | 0.803       |
|             | MEAD (~63 words)     | 0.446            | 0.535       | 0.537            | 0.558       | 0.744            | 0.757       |
| SciEntsBank | Baseline features    | 0.375            | 0.435       | 0.405            | 0.523       | 0.617            |
|             | (Dzikovska et al., 2013) |                 |             |                  |             |                  |
|             | Graph (~39 words)    | 0.372            | 0.458       | 0.438            | 0.567       | 0.644            | 0.658       |
|             | MEAD (~40 words)     | 0.379            | 0.461       | 0.429            | 0.554       | 0.631            | 0.645       |

Table 3: Comparing f-measures (f) and mean cosines (cos) of every class for features generated by graph and MEAD summaries.

| Classes | Feature | correct | partially_correct | contradictory | non_domain | irrelevant | correct | contradictory | incorrect | correct | incorrect |
|---------|---------|---------|-------------------|---------------|------------|-----------|---------|---------------|-----------|--------|-----------|
| Beetle  | f       | 0.702   | 0.443             | 0.416         | 0.667      | 0.000     | 0.687   | 0.400         | 0.523     | 0.679  | 0.809     |
|         | cos     | 0.756   | 0.400             | 0.404         | 0.640      | 0.000     | 0.732   | 0.422         | 0.539     | 0.747  | 0.840     |
| SciEntsBank | f       | 0.661   | 0.332             | 0.082         | 0.550      | 0.563     | 0.062   | 0.661         | 0.528     | 0.733  |           |
|          | cos     | 0.617   | 0.302             | 0.087         | NA         | 0.482     | 0.405   | 0.059         | 0.649     | 0.548  | 0.741     |
| MEAD     | f       | 0.441   | 0.337             | 0.337         | 0.138      | 0.268     | 0.441   | 0.337         | 0.298     | 0.441  | 0.305     |
|          | cos     | 0.498   | 0.372             | 0.350         | 0.229      | 0.271     | 0.498   | 0.350         | 0.316     | 0.498  | 0.323     |

compute the degree of overlap between student responses and sample reference texts and the prompt or question texts. Both human references as well as question texts were provided with the dataset. The lexical overlap measures include: (1) Raw count of the overlaps between student responses and the sample reference and question texts, (2) Cosine similarity between the compared texts, (3) Lesk similarity, which is the sum of square of the length of phrasal overlaps between pairs of texts, normalized by their lengths (Pedersen et al., 2002) and (4) f-measure of the overlaps between the compared texts. These four features are computed for the sample reference text and the question text, resulting in a total of eight features. We compute these eight features for every system and compare their raw and weighted (by their class distributions) f-measure values.

3.2 Results and Discussion

The graph-based cohesion technique produced summaries containing an average of 62 words for Beetle and an average of 39 words for SciEntsBank. Therefore, we chose to extract summaries containing nearly the same number of words using the MEAD summarization tool.

From the results in Table 2, we see that, compared to the baseline approach, the summarization approaches are better at scoring short answers. We also tested the use of all top-scoring student responses as alternate references (i.e. with no summarization). These models perform worse than the baseline, producing an average decrease in overall f-measure of 14.7% for Beetle and 14.3% for SciEntsBank. This suggests the need for a summarization technique. Our results indicate that the summarizers produce representative sentences that are more useful for scoring than just the sample reference text. MEAD performs better on the 5-way task while the graph-based cohesion approach performs well on 3-way and 2-way classification tasks.

In the case of both the datasets, the performance of the graph-based approach on the “correct” class is higher. We looked at the average cosine similarity for data from each class with their corre-

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3 f-measure is the harmonic mean of the precision and recall of the degree of overlaps between two texts. Precision is computed as the number of overlaps divided by the length of student response, while recall of overlap is computed as the degree of overlap divided by the number of tokens in the human reference text.

4 We report results only on the unseen answers test set from Semeval because the train and test sets contain data from different prompts for the unseen domains and unseen questions sets. Summaries generated from the top-scoring responses from one set of prompts or questions in the train set may not be relevant to different prompts in the other test sets.
Table 4: Comparing references generated by the summarizers with a sample reference for a prompt from the Beetle dataset.

| Sample Reference | Graph-based Cohesion | MEAD |
|------------------|----------------------|------|
| “Terminal 1 and the positive terminal are separated by the gap OR Terminal 1 and the positive terminal are not connected. OR Terminal 1 is connected to the negative battery terminal. OR Terminal 1 is not separated from the negative battery terminal. OR Terminal 1 and the positive battery terminal are in different electrical states.” | “The terminal is not connected to the positive battery terminal. OR The terminals are not connected. OR The positive battery terminal and terminal 1 are not connected. OR Because there was not direct connection between the positive terminal and bulb terminal 1. OR Terminal one is connected to the negative terminal and terminal 1 is separated from the positive terminal by a gap. OR The positive battery terminal is separated by a gap from terminal 1.” | “Positive battery terminal is separated by a gap from terminal 1. OR Terminal 1 is not connected to the positive terminal. OR Because there was not direct connection between the positive terminal and bulb terminal 1. OR The terminals are not connected. OR Because they are not connected. OR Terminal 1 is connected to the negative battery terminal. OR The two ears not connected.” |

The results indicate that the approach can be successfully applied for improving scoring of short answers responses. These results have direct applications to automated tutoring systems, where students are in a dialogue with a computer-based agent and the system must match the student dialogue against a set of reference responses. In each of these cases, the technique provides a richer set of legal reference texts and it can be easily incorporated as a pre-processing step before comparisons are made to the student responses.
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