A COMPLETE SCHEME FOR A MUON COLLIDER *

Robert B. Palmer, J. Scott Berg, Richard C. Fernow, Juan Carlos Gallardo, Harold G. Kirk (BNL, Upton, NY); Yuri Alexahin, David Neuffer (Fermilab, Batavia, IL); Stephen Alan Kahn (Muons Inc, Batavia, IL); Don J. Summers (University of Mississippi, Oxford, MS)

Abstract

A complete scheme for production, cooling, acceleration, and ring for a 1.5 TeV center of mass muon collider is presented, together with parameters for two higher energy machines. The schemes starts with the front end of a proposed neutrino factory that yields bunch trains of both muon signs. Six dimensional cooling in long-period helical lattices reduces the longitudinal emittance until it becomes possible to merge the trains into single bunches, one of each sign. Further cooling in all dimensions is applied to the single bunches in further helical lattices. Final transverse cooling to the required parameters is achieved in 50 T solenoids.

Table 1: Parameters of three muon colliders. Note 1: Depth is relative to any nearby low land, e.g. Fox river at FNAL. Note 2: Survival is from the end of phase rotation to the collider ring.

| Energy (TeV) | L (10^{34} cm^2 sec^{-1}) | μ/bunch (10^{12}) | <B_{ring}> (T) | β\* = σ_z (mm) | rms dp/p (%) | Depth for ν rad (m) | Muon Survival 2 |
|-------------|----------------------------|-------------------|----------------|----------------|---------------|-------------------|-----------------|
| 1.5         | 1                          | 2                 | 5.2            | 10             | 0.09          | 13                | ≈0.07           |
| 4           | 4                          | 2                 | 5.2            | 3              | 0.12          | 135               | ≈0.07           |
| 8           | 8                          | 2                 | 10.4           | 3              | 0.06          | 540               | ≈0.07           |

INTRODUCTION

Muon colliders were first proposed by Budker in 1969 [1], and later discussed by others [3]. A more detailed study was done for Snowmass 96 [4], but in none of these was a complete scheme defined for the manipulation and cooling of the required muons.

Muon colliders would allow the high energy study of point-like collisions of leptons without some of the difficulties associated with high energy electrons; e.g. the synchrotron radiation requiring their acceleration to be essentially linear, and as a result, long. Muons can be accelerated in smaller rings and offer other advantages, but they are produced only diffusely and they decay rapidly, making the detailed design of such machines difficult. In this paper, we outline a complete scheme for capture, phase manipulation and cooling of the muons, every component of which has been simulated at some level.

The work in this paper was performed as part of the NFMCC collaboration [5], the recently formed MCTF [6], and Muons Inc. [7].

COLLIDER PARAMETERS

Table 1 gives parameters for muon colliders at three energies. Those at 1.5 TeV correspond to a recent collider ring design [9]. The 4 TeV example is taken from the 96–study [4]. The 8 TeV is an extrapolation assuming higher bending fields and more challenging interaction point parameters. All three use the same muon intensities and emittances, although the repetition rates for the higher energy
machines are reduced to control neutrino radiation.

PROPOSED SYSTEM

Figure 1 shows a schematic of the components of the system. Figure 2 shows a plot of the longitudinal and transverse emittances of the muons as they progress from production to the specified requirements for the colliders. The subsystems used to manipulate and cool the beams to meet these requirements are indicated by the numerals 1–9 on the figures.

Proton Driver

The proton driver requirements depend on the muon survival estimates that will be discussed in a later section. We further assume, from the neutrino factory studies, that pion production in the 21 best bunches, at the end of phase rotation, is 1.7% per proton per GeV. The resulting required proton bunches, for different energies, are given in Table 2.

For efficiency in the following phase rotation, an rms bunch length of 3 ns is required. The space charge tune shift and required longitudinal phase space densities are challenging at the lower proton energies, but easier at the higher energies.

Table 2: Proton bunch intensity for three different proton energies

| E (GeV) | Np (10^{13}) |
|--------|--------------|
| 8      | 21           |
| 24     | 7            |
| 60     | 2.8          |

Production, Phase Rotation, and Initial Cooling

The muons are generated by the decay of pions produced by proton bunches interacting in a mercury jet target [8]. These pions are captured by a 20 T solenoid surrounding the target, followed by an adiabatic lowering of the field to 3 T in a decay channel.

The first manipulation (#1), referred to as phase rotation [10], converts the initial single short muon bunch with very large energy spread into a train of bunches with much reduced energy spread of which we use only 21. The initial bunch is allowed to lengthen and develop a time-energy correlation in a 110 m drift. It is then bunched into a train, without changing the time-energy correlation, using rf cavities whose frequency varies with location, falling from 333 MHz to 234 MHz. Then, by phase and frequency control, the rf accelerates the low energy bunches and decelerates the high energy ones. Figure 3 shows ICool [11] simulations of the phase spaces before bunching, after bunching, and after rotation.

Muons of both signs are captured and then (#2) cooled transversely in a linear channel using LiH absorbers, periodic alternating 2.8 T solenoids, and pillbox 201 MHz rf cavities. All the components up to this point are identical to those described in a recent study [12] for a Neutrino Factory.
6D Cooling Before Merge

The next stage (#3) cools simultaneously in all 6 dimensions. The lattice [13], shown in figure 4, uses 3 T solenoids for focus, weak dipoles (generated by tilting the solenoids) to generate bending and dispersion, wedge shaped liquid hydrogen filled absorbers where the cooling takes place, and 201 MHz rf, to replenish the energy lost in the absorbers. The dipole fields cause the lattices to curve, forming a slow upward or downward helix (see inset in Fig. 5). The following stage (#4) uses a lattice essentially the same as (#3), but with twice the field strength, half the geometric dimensions, and 402 instead of 201 MHz rf. Figure 5 shows the results of a simulation of both systems using ICOOL. Although this simulation was done for circular, rather than the helical geometry, it used realistic coil and rf geometries. Preliminary studies [14] suggest that the differences introduced by the helical, instead of circular, geometries will be negligible. The simulation did not include the required matching between the two stages. The simulations also used fields that, while they satisfied Maxwell’s equations and had realistic strengths, were not actually calculated from specified coils. Simulations reported in reference [13], using fields from actual coils, gave slightly better results.

6D Cooling After Merge

After the bunch merging, the longitudinal emittance of the single bunch is now similar to that at the start of cooling. It can thus be taken through the same, or similar, cooling systems as (#3) and (#4); now numbered (#6) and (#7). One more (#8) stage of 6D cooling has been designed (Fig. 7), using 10 T magnets, hydrogen wedge absorbers, and 805 MHz rf. Its ICOOL simulated performance is shown in Fig. 8. Again, the simulation shown used fields that, while they satisfied Maxwell’s equations and had realistic strengths, were not actually calculated from specified coil configuration.
Final Transverse Cooling in High Field Solenoids

To attain the required final transverse emittance, the cooling needs stronger focusing than is achievable in the 6D cooling lattices used in the earlier stages. It can be obtained in liquid hydrogen in strong solenoids, if the momentum is allowed to fall sufficiently low. But at the lower momenta the momentum spread, and thus longitudinal emittance, rises relatively rapidly. However, as we see from Fig. 2 the longitudinal emittance after (#8) is far less than that required, so such a rise is acceptable. Figure 9 shows the results of ICOOL simulation of cooling in seven 50 T solenoids. The simulation did not include the required matching and re-accelerations between the solenoids.

A 45 T hybrid Cu and superconductor solenoid[15] is currently operating at NHFML and an upgrade to 50 T is planned, but this magnet uses a lot of power. A 27 T solenoid using an 8 T YBCO insert at 4K has recently been successfully tested [16]. There is a conceptual design of an all superconducting 50 T solenoid [17].

Acceleration

Sufficiently rapid acceleration is straightforward in linacs and recirculating linear accelerators (RLAs). Lower cost solutions might use fixed field alternating gradient (FFAG) accelerators, rapidly pulsed magnet synchrotrons, and/or hybrid SC and pulsed magnet synchrotrons [18].

Muon Losses

The estimate of muon losses is very preliminary. The simulations assumed Gaussian initial distributions and were not very well matched into each lattice, leading to larger initial losses. And no tapering of the focus parameters as function of length was included, leading to larger losses as the emittances approached their equilibrium. As a result, the losses observed were larger than those deduced using the performances in the mid range of each simulation. Table 3 shows the result of an attempt to estimate realistic losses, but this remains very preliminary. Since it is this estimate that was used to determine the required proton driver specifications used above, these too must be considered very preliminary.

Table 3: Calculated transmission tune shifts at different stages in the system.

| Transmission                  | Cumulative |
|-------------------------------|------------|
| Linear transverse pre-cooling  | 0.7        | 0.7      |
| Pre-merge RFOFO cooling        | 0.5        | 0.35     |
| Merging                       | 0.8        | 0.28     |
| Post-merge RFOFO cooling       | 0.5        | 0.14     |
| Final 50 T solenoid cooling    | 0.7        | 0.1      |
| Acceleration to 0.75 TeV       | 0.7        | 0.07     |

Collider Ring

For the 1.5 TeV c.m.s, a lattice has been developed [9]. The parameters as given in Tb. 1 were achieved with adequate momentum acceptance but with dynamic transverse acceptance of only at little over 2σ for the specified final emittance. We note however that since luminosity is dependent on the square of the bunch densities, there would be little luminosity loss if the larger amplitudes were collimated prior to injection into the ring.
Space Charge Tune Shifts

For bunches with Gaussian distributions in all dimensions:

$$\frac{\Delta \mu}{\nu_{\text{cell}}} = \left( \frac{N_\mu}{\epsilon_\perp} \right) \frac{\beta_{\perp,\text{ave}} r_\mu}{2 \sqrt{2\pi} \sigma_z \beta_\gamma \gamma^2}$$

where $$\beta_{\perp,\text{ave}} = \frac{L_{\text{cell}}}{\sqrt{2} \pi H_{\text{cell}}}$$ and $$r_\mu = 1.35 \times 10^{-17} \text{ m}$$

Then at the end of a number of stages in this system, one obtains the tune shifts given in Table 4.

Table 4: Calculated maximum space charge tune shifts at different stages in the system.

| (#) | $$N_\mu$$ | $$\beta_{\perp,\text{ave}}$$ | $$\sigma_z$$ | $$\epsilon_\perp$$ | p | $$\Delta \nu/\nu$$ |
|-----|-----------|-----------------|-------------|-------------|---|---------------|
| (7) | 2         | 292             | 27          | 1500        | 200 | 1.6           |
| (9) | 6         | 191             | 13          | 400         | 200 | 14.5          |
| (9+) | 3        | 222             | 27          | 400         | 100 | 26.1          |
| (9+) | 3        | 93              | 354         | 25          | 42  | 20.0          |

Note that $$N_\mu$$ is larger at earlier cooling stages to allow for losses. The first order shifts can be corrected by increasing the focus strength, but tune spreads of half the shifts cannot be corrected.

Before the merge, the shifts are small because the numbers of muons per bunch are small. The only 6D cooling in the specified magnetic fields. This is under study.

CONCLUSION

Although much work remains to be done, the scenario outlined here appears to be a plausible solution to the problems of capturing, manipulating, and cooling muons to the specifications for muon colliders with useful luminosities and energies, even up to 8 TeV in the center of mass.

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