1. Introduction

The Milky Way galaxy includes large scale structures such as clusters, star forming regions, and OB associations. Understanding the formation, structure, and evolution of these components has been one of the greatest challenges of modern astrophysics. Following the advent of sensitive wide-field instruments over the past two decades, a large number of photometric studies have been performed in stellar associations and clusters (e.g. Knödlseder 2000; Barrado y Navascués et al. 2004; Bejar et al. 2001; Lodieu et al. 2006; Torres et al. 2008; Erroz & Casali 1992). These surveys not only dramatically improved our knowledge of the luminosity function, but also extended it down to the substellar and planetary mass regimes. They nevertheless suffer from several limitations, making their comparison to theoretical predictions sometimes difficult. Any photometric selection indeed relies on theoretical tracks, and hence age estimates, that are still uncertain at young ages (Baraffe et al. 2009). Additionally, the photometric variability inherent to their youth can affect their luminosity and colors, leading to a significant fraction of missed members. Foreground stars and extragalactic sources will in most cases be a major source of contamination. Finally, photometric surveys are not able to disentangle members of neighboring or spatially coincident groups, possibly leading to confusion and erroneous conclusions regarding their origin. Selecting members based on their kinematics offers several advantages: it is completely independent of evolutionary models; it rejects the majority of unrelated foreground and background sources; it is insensitive to variability or flux excess and deficiency related to e.g. circumstellar material or accretion; it can disentangle coincident or neighboring associations provided that they have differing mean motions (e.g. σ Ori, Lupus, and Upper...
The study of kinematics involves two complementary observational techniques: radial and transverse velocity measurements. Systematic radial velocity surveys over extended (>10 deg^2) regions of the sky require large amounts of telescope time. The most successful and efficient spectroscopic surveys to date (e.g. RAVE, WOCS, APOGEE, MARVELS, ESO-GAIA, Steinmetz et al. 2006, Mathieu 2000, Majewski et al. 2003, Mahadevan et al. 2007, Gilmore et al. 2012) are producing libraries including several hundreds of thousands of high quality spectra and radial velocity measurements over areas as large as several thousands square degrees. They are nevertheless still limited to the brightest sources and do not reach the substellar luminosity range. Proper motion measurements are on the other hand much easier to achieve. One in principle only needs two observations separated by a sufficient period of time. A number of nearby associations have mean proper motions of a few tens of mas yr^-1 (e.g. Pleiades, Hyades, Taurus, Ophiuchus, Kharchenko et al. 2005, Bobylev 2006) making it easier to measure their members' motion over a few years only. In spite of the tremendous efforts conducted over the past 20 yr, the limited sensitivity of the various large scale kinematic projects has restricted the study to the Solar neighbourhood (e.g Hipparcos) or to the identification of nearby moving groups (Torres et al. 2006, 2008, Zuckerman et al. 2004, 2001, 2006). Local kinematics has been commonly used to confirm photometrically selected samples (see e.g Moraux et al. 2001, 2003, Kraus & Hillenbrand 2007, Lodieu et al. 2007a, 2012, 2007b, Gálvez-Ortiz et al. 2010, López Martí et al. 2011), but kinematically selected samples over large areas of young nearby associations are still sorely missing.

The future Gaia space mission (Perryman et al. 2001) will provide an exquisite accuracy and complete 6 dimension census of the sky up to G=15 mag, and a 5 dimension census up to G=20 mag. Although it represents a tremendous improvement with respect to its predecessor Hipparcos (Perryman et al. 1997), Gaia will unfortunately not be sensitive enough to study the least massive objects. G<20 mag indeed corresponds to 3-4 M_{jup} at 150 pc and for an age of 1 Myr (Baraffe et al. 1998), when the mass function is known to extend at least down to 3-4 M_{jup} (e.g Bayo et al. 2011) and references therein). Additionally, young stellar clusters and associations are very often deeply embedded and contain bright H II regions. Since it will operate in the visible part of the spectrum, Gaia will be mostly blind in the regions of heavy extinction and bright nebular emission, where precisely most of the star formation is taking place.

Recently, Anderson et al. (2006) demonstrated that high-precision astrometry could be extracted from wide-field, ground-based CCD images, and studied extended areas around galactic globular clusters (Bellini et al. 2009, Bellini & Bedin 2010, Yadav et al. 2008) using observations obtained with the ESO WFI wide-field camera. In this paper, we present a similar method designed to automatically process and analyse vast amounts of images (several thousands) originating from multiple instruments and sites and covering large (>10 deg^2) areas of the sky.

2. The DANCe Project:

Taking advantage of the wide field surveys performed in the early 2000, we are performing a comprehensive study of kinematics in a number of nearby (≤1 kpc) associations and clusters. A preliminary list of targets with publicly available archival observations is given in Bouy et al. (2011), and we are welcoming suggestions and proposals of collaborative studies for other associations and clusters of particular interest. The initial surveys reached sensitivities well beyond the substellar limit at the age and distance of these associations. Complementing these archival data with new sensitive wide field observations, we are compiling a multi-epoch panchromatic database encompassing large (several tens of square degrees) areas of young nearby associations. This database is used to derive accurate proper motions for all sources with multi-epoch detections. The scientific goals of the DANCe project are twofold:

- **mass function:** when the association mean proper motion allows it, the proper motion and accurate photometric measurements can be used to select members and/or reject contaminants and derive more accurate luminosity (mass) functions. The samples can be used to study the stellar content within each group separately, and to perform a meaningful intercomparison between groups of various ages, structures, metallicities, and densities.

- **internal dynamics:** the observed velocity distribution of confirmed members and its dependence on stellar mass, spatial distribution and environment can be compared with advanced N-Body numerical simulations and dynamical evolution models (Adams 2001, Proszkow & Adams 2009, Marks & Kroupa 2012). Ultimately, complementary radial velocity measurements can provide a complete picture of the space motions within young associations, below the substellar limit.

3. Test case: the Pleiades

Their youth and proximity have made the Pleiades one of the most extensively studied clusters over the past hundred years. In their recent review of the cluster, Stauffer et al. (2007) and Lodieu et al. (2012) have compiled an exhaustive list of candidate and confirmed members originating from more than a dozen independent surveys of the Pleiades. The total number of members and candidate members reported in their catalogs adds up to 1471 objects. The relatively large mean proper motion of the group and the vast amounts of images available in public archives makes it an ideal target to develop the large scale data processing and automatic astrometric algorithms presented in this manuscript.

4. Archival Data

In an effort to compile the most complete dataset - both in terms of spatial and time coverage - we searched the Subaru Telescope, the Isaac Newton Telescope (INT), the United Kingdom Infrared Telescope (UKIRT), the Cerro Tololo Inter-American Observatory (CTIO, at NOAO), the Kitt Peak National Observatory (KPNO, at NOAO), the Canada France Hawai`i Telescope (CFHT) and the European Southern Observatory (ESO) public archives for wide-field images within a box of 10°×10° centered on the Pleiades. Figure 1 and Table 1 give an overview of the properties and coverage of the various datasets and instruments. The filter sets used for these observations are described in Fig. 1. The data were obtained with 9 different instruments at 5 observatories. A summary of their characteristics is given in the following sections.

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1. The transmission curves were retrieved from the Spanish VO website http://svo2.cab.inta-csic.es/theory/ifs/
Fig. 1 IRAS 100 $\mu$m image of the Pleiades cluster with the various surveys used in this study overplotted. The Seven Sisters are represented with yellow stars. The full Moon is represented in the lower right corner to illustrate the scale.

- **CFH Telescope:**
  The CFH12K (Cuillandre et al. 2000) and UH8K (Metzger et al. 1995) observations of the Pleiades are described in details in Bouvier et al. (1998), Moraux et al. (2001) and Moraux et al. (2003). The MegaCam (Boulade et al. 2003) observations are described in Section 5. The individual images were processed and calibrated with the recommended Elixir system (Magnier & Cuillandre 2004), which includes detrending (darks, biases, flats and fringe frames), and astrometric registration. Nightly magnitude zero-points were derived by the CFHT team using standard star fields (Landolt 1992).

- **Subaru Telescope:**
  The Suprime-Cam (Miyazaki et al. 2002) images were processed (overscan subtraction, flat-fielding, and masking of vignette areas) using the recommended SDFRED1 package (Ouchi et al. 2004; Yagi et al. 2002) and the relevant calibration frames obtained the same night. The photometric conditions on Mauna Kea were poor during these observations, as described in the Skyprobe database (Cuillandre et al. 2004). We therefore did not attempt to calibrate the corresponding photometry.

- **INT Telescope:**
  We retrieved the detrended individual Wide Field Camera (WFC, Ives 1998) images from the ING public archive.
About 88% of these observations were obtained under photometric ambient conditions, as described by the INT data quality control system, and the nightly photometric zero-points provided by the ING were applied.

- **UKIRT Telescope:**
  The cluster was observed in the near-infrared (near-IR) with the Wide Field CAMera (WFCAM, Casali et al. 2007) in the course of the UKIRT InfraRed Deep Sky Surveys (UKIDSS, Lawrence et al. 2007). The UKIDSS survey provides a homogeneous coverage of the association in the Z, Y, J, H and Ks filters. The UKIDSS release (DR9) includes observations performed between September 2005 and January 2011, and are described in Lodieu et al. (2007) and Lodieu et al. (2012). We noticed that the Point Spread Function (PSF) of the pipeline processed interleaved images was not optimal for an accurate astrometric analysis. We therefore retrieved the individual frames from the WFCAM Science Archive (Hambly et al. 2008). These frames are flat-fielded, dark subtracted, and sky-subtracted, and include an approximate astrometric solution with an accuracy better than a few arcseconds. After extracting the sources from these individual images, a photometric calibration was derived using the UKIDSS catalogue.

- **KPNO Mayall Telescope:**
  We searched and retrieved NOAO Extremely Wide Field Infrared Imager (NEWFIRM) (Autry et al. 2003) and MOSAIC-I (Wolfe et al. 2000) images in the NOAO Science Archive. The MOSAIC-I images were processed following standard procedures using the mscred package within IRAF and the relevant calibration frames, as recommended in the User’s manual. The detrended and sky-subtracted NEWFIRM images and their respective confidence maps were retrieved from the NOAO archive (Swaters et al. 2009). The NEWFIRM J-band photometry was then tied to the UKIDSS one.

- **CTIO Blanco Telescope:**
  MOSAIC2 is a close instrument of the MOSAIC1 installed on the Blanco telescope at CTIO. We retrieved the raw images from the NOAO Science Archive, and processed them following standard procedures using the mscred package within IRAF and the relevant calibration frames, as recommended in the User’s manual.

Although in most cases sets of several consecutive and dithered images were obtained, we chose to perform the analysis on the individual images rather than on stacks. While individual images do not go as deep as stacks, this choice ensures that the PSF (and hence the astrometric accuracy) and noise are not affected by the stacking process. As we will see, using individual images offers other advantages, in particular a more efficient rejection of problematic frames or measurements, and an opportunity to reach out for faster moving objects.

### 5. New observations

To complement the archival data and increase both the time baseline and spatial coverage, we obtained deep wide field images of the cluster with MegaCam at the CFHT. The observations were designed to optimize the astrometric calibration. The various pointings were chosen to overlap by a few arcminutes, ensuring an accurate astrometric anchoring over the entire survey. Each pointing was obtained in dither mode, with a dither width of a few arcminutes. This dithering allows filling the CCD-to-CCD gaps and correcting for deviant pixels and cosmic ray events, and helps deriving an accurate astrometric solution over the entire field-of-view (see section 7.6). The nights were photometric, with an average seeing Full-Width at Half Maximum (FWHM) in the range 0.5–0.7 as measured in the images. The data were processed and calibrated with the recommended Elixir system, and the nightly magnitude zero-points measured by the CFHT team were applied.

### 6. Observation properties

Describing the properties of every single individual image used in this study would be impractical. Instead, we present general statistics of 3 observational properties especially important for the purpose of our study: airmass, image FWHM and sensitivity. The latter two are important parameters as the best positional accuracy achievable is mostly limited by the signal-to-noise ratio (hence sensitivity), the FWHM of the point sources and sampling (pixel scale) of the images (King 1983). The airmass is playing an important role as well, as atmospheric turbulence and differential chromatic refraction quickly increase with airmass.

Figure 3 shows the distribution of airmass for the observations used in this study. About 75% of the observations were obtained at airmass <1.2, and ~90% at airmass <1.3. It also shows the distribution of the FWHM measured for all individual unresolved detections (point sources). About two thirds have FWHM ≤0.8", and about 92% have FWHM ≤1". Finally, even though the sensitivity of the individual frames varies greatly, the various observations routinely reached luminosities fainter than 22 mag in the optical (λ <1.0 µm), and 18 mag in the near-IR (λ >1.0 µm).

Whenever we could assess that an observation had been performed under good photometric conditions and that an absolute photometric calibration (photometric standard field) was available, we applied the corresponding zero-point to the photometry extracted by SExtractor. The associated absolute photometric uncertainties are typically of the order of 5–10%. Most of the photometric measurements (all except the Subaru/SuprimeCam, CTIO/MOSAIC2, KPNO/MOSAIC1 and some INT/WFC) were obtained under clear or photometric conditions.

### 7. Astrometric analysis

The astrometric analysis involves vast amounts of multi-epoch, multi-instrument, multi-wavelength datasets, and requires highly automated tools; all our processing is done using the Astromatic software suite (Bertin 2010). The whole process is decomposed into the following steps, which we describe in detail in the next sections:

1. Recovering and equalizing image metadata
2. Modeling the PSF
3. Cataloging
4. Quality assurance
5. Estimating astrometric uncertainties
6. Computing a global astrometric solution
7. Robust fitting of individual source proper motions

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2 IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.

3 http://www.astromatic.net
7.1. Recovering and equalizing image metadata

The PSF modeling, source extraction and astrometric calibration tasks rely on a handful of parameters which must be set before processing the data. These parameters comprise detector gains, saturation levels, the approximate position and scale of the pixel grids on the sky, dates and times of observation, durations of exposure, airmass, filter wheel position and instrumental setups that define the instrumental context for the astrometric solution (see §7.6).

Recovering and uniformizing these parameters proves to be a laborious undertaking; one faces here not one but nine different mosaic instruments over many years of operation. In practice, and despite decades of effort from the community to promote the standardization of metadata description in FITS headers, each instrument uses slightly different conventions, which often evolves during the life of the instrument. Among all parameters, the detector saturation level (required for excluding saturated sources from the PSF modeling process and from the astrometric solution) was found the less reliable. It was often overestimated, and in one occasion it would ignore a scaling fac-
The first step in making precise measurements of the positions of individual sources is to compute an accurate model of the PSF for every chip of every exposure. A large fraction of individual sources is to be censored without degrading excessively the positional accuracy and the desired range of seeing and airmass are acceptable for this study. Problems such as tracking errors, bursts of electronic glitches, partially defocused optical reflections (“ghosts”) and residual fringing patterns can alter source centroids to a level that would affect significantly the computed proper motions. All pre-selected exposures were therefore screened for defects using semi-automated quality control based on PSFEx and SExtractor measurements. By “semi-automated quality control” we mean automatically generated statistics and plots prepared for human review (e.g., Ivezić et al. 2004, Malapert & Magnard 2006, Skrutskie et al. 2006, McFarland et al. 2012).

Table 1: Instruments used in this study and references to the corresponding surveys

| Observatory | Instrument | Filters | Platescale | Chip layout | Chip size | Field of view | Survey Epoch | Survey Area [deg²] | Ref. |
|-------------|------------|---------|------------|-------------|-----------|--------------|--------------|---------------------|------|
| CFHT        | UH 8k      | R, I    | 0.205      | 4×2         | 2k×4k     | 29′×29′      | 1996         | 2.5                 | 1    |
| CFHT        | CFHT 12K   | i       | 0.201      | 6×2         | 2k×4k     | 42′×28′      | 1999         | 2.0                 | 2,3  |
| CFHT        | MegaCam    | u, g, r | 0.187      | 4×9         | 2k×4k     | 1′×1′        | 2000-2011    | 30                  | 4    |
| Subaru      | Suprime-Cam | i, r   | 0.200      | 5×2         | 2k×4k     | 34′×27′      | 2002-2007    | 8                   | 4    |
| INT         | WFC        | U, g, r, z | 0.333      | 3×1+1       | 2k×4k     | 34′×34′      | 1998-2006    | 29                  | 4, 5, 6, 7 |
| UKIRT       | WFCAM      | Y, Z, J, H, K | 0.400      | 2×2         | 2k×2k     | 45′×45′      | 2005-2011    | 79                  | 8    |
| KPNO (Mayall) | NEWFIRM   | J       | 0.400      | 2×2         | 2k×2k     | 28′×28′      | 2009         | 10                  | 4    |
| KPNO (Mayall) | MOSAIC1  | VR-broad | 0.51       | 4×2         | 2k×4k     | 36′×36′      | 2001-2003    | 8.5                 | 4    |
| CTIO (Blanco) | MOSAIC2 | VR-broad | 0.53       | 4×2         | 2k×4k     | 36′×36′      | 2005-2006    | 1.0                 | 4    |

References: (1) Bouvier et al. (1998), (2) Moraux et al. (2001), (3) Moraux et al. (2003), (4) This study, (5) Dobbie et al. (2005), (6) McMahon et al. (2001), (7) Zapatero Osorio et al. (1999), (8) Lawrence et al. (2007)

Note that no extra-deblending of close pairs was attempted: a factor applied to the data, a problem that also plagued the gains. Because of this we ended up using SNR-vs-SPREAD_MODEL diagrams (see §7.4) to correct individual detector saturation levels.

7.2. Modeling the Point Spread Function with PSFEx

The first step in making precise measurements of the positions of individual sources is to compute an accurate model of the (variable) PSF for every chip of every exposure. A large fraction of the images (those with good seeing) are significantly undersampled with gaps of 12″ between each chip. This requires the PSF to be modeled at the sub-pixel level. The PSFE software (Bertin 2011) has been specifically designed to work with undersampled images and arbitrary PSF shapes. Briefly, PSFEx fits the image of every point-source $p_i$ with a projection on the local pixel grid of the linear combination of basis vectors $\phi_i$ by minimizing the $\chi^2$ function of the coefficient vector $c$:

$$\chi^2_{\text{PSF}}(c) = \sum_x \left( p_x - \bar{p}_x(c) \right)^2 W_x \left( p_x - \bar{p}_x(c) \right),$$

where $\bar{p}_x$ is the PSF model sampled at the location of star $x$:

$$\bar{p}_x(c) = f_j \mathbf{R}(x_j) \sum_b c_b \phi_b,$$

$f_j$ is the flux within some reference aperture, and $\mathbf{R}(x_j)$ is a resampling operator that depends on the image grid coordinates $x_j$ of the point-source centroid:

$$\mathbf{R}(x_j) = h (x_j - \eta(x_j - x_j)),$$

where $h$ is a 2-dimensional interpolant (interpolating polynomial), $x_j$ is the coordinate vector of image pixel $j$, $x_j$ is the coordinate vector of model sample $j$, and $\eta$ is the image-to-model sampling step ratio (oversampling factor). We adopt a Lanczos-4 function (Duchon 1979) as interpolant. PSFEx is able to model smooth PSF variations within each chip by expanding the set of unknowns in (Eq. 2) as a linear combination of polynomial functions of the source position $x_j$ in the chip:

$$c_b = \sum_{k \leq D} c_{b,k,j} x_j^k x_j^l,$$
Performing an extensive quality check in a large parameter space for 16,000 images coming from nine different mosaic instruments, each with its own particular breed of issues, would be excessively time-consuming. Instead we decided to focus on the consistency of the PSF, which all astrometric measurements depend on. One way to check this consistency is to analyze the distribution of the new SPREAD MODEL estimator implemented in recent development versions of SExtractor, and originally developed as a star/galaxy classifier for the Dark Energy Survey data management pipeline (Mohr et al. 2012; Desai et al. 2012). Briefly, SPREAD MODEL acts as a linear discriminant between the best fitting (local) PSF model \( \phi \) derived with PSFEx and a slightly “fuzzier” version made from the same PSF model convolved with a circular exponential model with scalelength = FWHM/16 (FWHM is the Full-Width at Half-Maximum of the local PSF model). SPREAD MODEL is normalized to allow comparing sources with different PSFs throughout the field:

\[
\text{SPREAD MODEL} = \frac{\phi^T W x}{\phi^T W \phi} - \frac{G^T W x}{G^T W G} \tag{5}
\]

where \( x \) is the image centered on the source, and \( W \) the inverse of its covariance matrix (which we assume to be diagonal). By construction, SPREAD MODEL is close to zero for point sources, positive for extended sources (galaxies), and negative for detections smaller than the PSF, such as cosmic ray hits. Figure 5 shows the typical distribution expected for source signal-to-noise ratio (SNR) as a function of SPREAD MODEL. We found this diagram to be extremely effective at revealing a wide range of cosmetic and morphometric issues that can arise with survey images:

- any significant departure of the point-source locus from a narrow distribution centered on \( \text{SPREAD MODEL} = 0 \) is a sign that the PSF model does not fit properly point-sources. The reason may be a problem with the PSF modeling process (e.g., the model cannot follow the variations of the PSF throughout the field), a non-linear behavior of the detector (e.g., saturated stars), excessive source confusion (very poor seeing), or a multi-modal PSF (SExtractor identifies as multiple source different parts of the PSF, in cases of strong defocusing or guiding errors for instance)
- a burst of bad pixels or electronic glitches shows up as a denser cloud on the left part of the diagram
- optical “ghosts”, diffraction spikes or faint satellite track are broken up into pieces by SExtractor and appear as spots on the right part of the diagram
- background inhomogeneities, such as contamination by strong fringe residuals or large textured halos, produce a large horizontal blur in the lower part of the diagram

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**Fig. 3** Upper panel: distribution of airmass for the observations used in this study. Lower panel: distribution of FWHM of all the individual unresolved detections. The lines represents the cumulative distribution.

**Fig. 4** Example of PSF reconstruction on one of the exposures (NEWFIRM frame K4h099B_20991221-0011K-kp). Left: snapshots of the variable PSF model over the field of view. Center: distribution of the PSF model FWHM. Right: distribution of the PSF model ellipticity.
However, the dominant source of positional uncertainties for bright stars on ground-based exposures, with a duration of a few minutes or less, is not photon noise, but apparent relative motion caused by atmospheric turbulence. This motion is highly correlated at small angles (Schlesinger 1916); its impact on the estimation of proper motions is small when working with very small fields of view, or when positions are measured relative to close neighbors. Neither is the case here, and the contribution from atmospheric turbulence component must be taken into account. In the regime probed by these observations (exposure time, field-of-view, telescope diameter), theoretical considerations as well as experimental studies (Lindgren 1980; Roddier 1981; Han 1989; Shao & Colavita 1992; Han & Gatewood 1995) have established that the amplitude of the relative random motion between two sources separated by angle $\theta$ (in arcmin) is well described by
\[
\sigma_{M}(\theta, T) = \sigma_{0M}(\theta/10)^{1/3} T^{-1/2},
\]
where $T$ is the exposure time in seconds, and $\sigma_{0M}$ is the standard deviation expected in unit time for a pair of stars separated by ten arcmin.

Correlated “position noise” as described by Eq. (6) translates into non-diagonal terms in the measurement error matrix of detections from individual exposures. But since the current version of our astrometry solver ignores non-diagonal terms in the weighting matrix, we are left with considering only the variance averaged over individual fields. Part of this variance is “absorbed” in the deformable distortion model (Connes 1978; Lindgren 1980) such as the second-degree polynomial we are using, but we assume this dampening effect to be small considering the wide fields of view of all the instruments involved here. The average contribution (per source) to pairwise positional variance due to relative motions in an exposure is half the integral of Eq. (6) over all possible pairs of positions within the field of view FOV:
\[
\sigma_{M}^{2}(\text{FOV}, T) = \frac{1}{2} \int F_{\text{FOV}} d\theta_{1} \int F_{\text{FOV}} d\theta_{2} \sigma_{m}^{2}(||\theta_{1} - \theta_{2}||, T). \tag{7}
\]
For rectangular FOVs, we find that the following expression provides a good approximation (within 5% for aspect ratios $< 20 : 1$) to $\sigma_{M}(\text{FOV})$:
\[
\sigma_{M}(\text{FOV}, T) \approx \frac{1}{\sqrt{2}} \sigma_{0m}(\theta_{\text{FOV}}/30\prime) T^{-1/2}, \tag{8}
\]
where $\theta_{\text{FOV}}$ is the diagonal of the field in arcmin.

Using star trails, Han & Gatewood (1995) measure $\sigma_{0m} = 54$ mas at Mauna Kea, whereas Han (1989) report a much higher $\sigma_{0m} = 143$ mas at Allegheny observatory in Pittsburgh. Zacharias (1996), analyzing astrometric calibration residuals from short, repeated observations made at Kitt Peak and Cerro Tololo, found results compatible in average with Han & Gatewood’s value; although he claims that their exposures with best seeing exhibit twice less dispersion, and hint at a dependency of turbulence-induced motion with seeing. Our own measurements using short wide-field exposures from archive data (Bouy et al., in preparation), exhibit little dependency on actual seeing, and suggest that Han & Gatewood’s value is appropriate for observations carried out in good sites. We therefore add $\sigma_{M}$ in quadrature to the measurement uncertainties estimated by SExtractor, adopting $\sigma_{0m} = 54$ mas as well as the FOV and exposure time of the current image. Note that the current version of our astrometry engine assumes that position uncertainties are isotropic.

We visually inspected SNR vs SPREAD_MODEL plots for all 16,515 exposures pre-selected for this survey. We identified and rejected 427 exposures (2.6%) exhibiting at least one of the signatures listed above, or lying amidst a sequence of “bad” frames, and for which we judged that quality issues were severe enough to harm the accuracy of astrometric measurements: 243 were plagued mostly by electronic artifacts (all UKIDSS), 97 by guiding errors, 40 by optical ghosts, 13 by very bad seeing, 13 by excessive fringing, 8 by defocused images, and 7 by various background issues. In addition, 6 short NEWFIRM exposures with poor cosmetics did not have enough “clean” stellar images to derive a proper PSF model.

7.5. Estimating astrometric uncertainties

Position uncertainties play a prominent role in our astrometric pipeline. They are the main ingredients of the relative weights given to individual detections in the global astrometric solution. They are also used in the computation of robust proper motions, as weights, and to identify outliers.

SExtractor’s 1-$\sigma$ fitting-error ellipse parameters ERRAMODEL_IMAGE, ERRBMODEL_IMAGE and ERRTHETAMODEL_IMAGE are directly extracted from the covariance matrix computed in the LevMar Levenberg-Marquardt minimization engine (Lourakis 2004). Based on repeatability tests performed with a wide range of simulated (photon-noise dominated) images, we checked that the estimated uncertainties matched the observed standard deviation of position residuals to better than 10% for isolated sources.

Fig. 5 Density plot of signal-to-noise ratio (SNR) vs SExtractor’s SPREAD_MODEL for all detections in this study. The dense vertical cloud located around SPREAD_MODEL is the point source (mostly stellar) locus. The fuzzy blob to the right of the stellar locus originates from galaxies and nebulosities, while the shallow cloud on the left is populated with cosmic ray hits and bad pixels. Note the asymmetry of the stellar locus caused by blended stars (most obvious at high SNRs).
Another source of errors in the measurement of positions is imperfect deblending of close detections. Of particular concern for the astrometric solution are the detrimental effects of deblending errors in some bright sources. The impact of deblending on centroid measurements varies a lot from object to object and is difficult to quantify \textit{a priori}. Nevertheless we find that adding a 0.1 pixel error in quadrature to position uncertainties of detections flagged as “deblended” by SExtractor alleviates the issue with the bright sources, without downweighting excessively sources that have been properly deblended.

7.6. Computing a global astrometric solution

The global astrometric solution is computed with version 2.0 of the SCAMP software package (\textit{Bertin} 2006). SCAMP is itself a mini-pipeline performing various operations before and after computing the global solution per \textit{se}. These operations are described in details in the SCAMP documentation; in the following we focus only on those that are especially important for this study.

The global solution computed by SCAMP is the result of minimizing the quadratic sum of differences in position between overlapping detections from pairs of catalogs, an approach pioneered by \textit{Eichhorn} (1960):

\[
\chi^2_{\text{astrom}} = \sum_{s} \sum_{a} \sum_{b} \frac{1}{\sigma^2_{a} + \sigma^2_{b}} \left| \xi_{a,b}(x_{a,s}) - \xi_{b}(x_{b,s}) \right|^2, \tag{9}
\]

where \(s\) is the source index, \(a\) and \(b\) are catalog indices, and \(\sigma_{a}\) is the positional uncertainty for source \(s\) in catalog \(a\). For the purpose of computing a global solution, positions in Eq. (9) are in a common system of reprojected coordinates derived from raw detector coordinates \(x\). For mosaic cameras, a catalog comprises several sub-catalogs for each exposure; one per detector chip. We express the reprojection operator \(\xi_{a}\) for chip \(a\) and exposure \(e\) as a combination of an undistorted reprojection operator \(\xi_{a,e}\) derived from the (tangential) projection approximation at the initial cross-matching stage, and two polynomials describing instrumental distortions:

\[
\xi_{c,e}(x) = \xi_{c,e}^{d}(x) + \left( \frac{d \xi_{c,e}^{d}}{dx} \right) \sum_{p} f_{c,i,p}(x) + \sum_{m} g_{c,m}(\rho). \tag{10}
\]

The first polynomial with free coefficients \(f_{c,i,p}\) describes static, chip-dependent \((c)\) and instrument-dependent \((i)\) distortions that are function of raw coordinates \(x\). The second polynomial with free coefficients \(g_{c,m}\) accounts for exposure-dependent distortions that are function of focal-plane coordinates \(\rho\), computed from the raw coordinates \(x\) using the initial positioning of chips on the focal plane. In this study we adopt a degree 4 for the chip-dependent polynomial, which in practice provides a very good fit to the geometrical distortions of most instruments. We choose a degree 2 for the exposure-dependent polynomial to account for flexures and geometric atmospheric refraction. Note that SCAMP automatically and progressively reduces the degree of both polynomials in cases where the number of free parameters reaches or exceeds the number of constraints: detector failures, shallow exposures, etc.

The cameras involved in this study are often taken off the telescope between runs. Experience shows that the static part of the distortion pattern changes from run to run, sufficiently enough to undermine the global solution. The same goes with filter changes. Therefore the count of “astrometric instruments” entering Eq. (10) far exceeds that of cameras, because what matters is eventually the combination camera/filter/run. Relying on header information and logsbooks, we identified 94 such combinations for the whole dataset, taken with 9 cameras through 30 filters.

For the minimum of \(\chi^2_{\text{astrom}}\) to be unique, the solution must be anchored on the sky. SCAMP does that by forcing one of the catalogs in Eq. (9) to be a catalog of astrometric references with fixed \(\xi\) coordinates. We selected 2MASS (\textit{Skrutskie et al.} 2006) as a reference catalog, because of its suitable depth, good homogeneity, and tight range of observation epochs.

Because instrumental distortions are small at the scale of a chip (typically a few pixels), Eq. (10) can be well approximated by

\[
\xi_{c,e}(x) \approx \xi_{c,e}^{d}(x) + \left( \frac{d \xi_{c,e}^{d}}{dx} \right) \sum_{p} f_{c,i,p}(x) + \sum_{m} g_{c,m}(\rho), \tag{11}
\]

which makes the minimization of Eq. (9) equivalent to solving a system of linear equations.

In SCAMP, the astrometric solution is computed three times. A first, distortion-free solution accurate to about 1" is obtained from the registration of all image exposures. This is sufficient to provide a satisfactory matching of most overlapping detections. A full global solution is then computed, which is used to identify detections with calibrated positions deviating excessively from the mean. Strong deviations may be caused by cross-matching issues such as blending or mismatches, differential chromatic refraction (at high airmass), wavelength-dependent centroids (in galaxies), or large proper motions (in stars). Because of the extended range of epochs and the presence of a nearby star cluster in the data, we opt for a somewhat severe level of clipping, rejecting about 4.5% of all detections at this stage. The final run of the solver on this clipped sample yields the final set of distortion parameters. Figure 7 shows examples of recovered distortion patterns for some of the 94 camera/filter/run combinations.

SCAMP offers the possibility to produce maps of the average residuals in raw coordinates after calibrating the positions with the best-fitting distortion pattern models. These maps tell us of possible position-dependent systematic calibration errors, in particular distortion features that cannot be fitted with a 4\textsuperscript{th} degree polynomial. Two cameras appear to exhibit particularly striking residual patterns with most filter/runs (Fig. 7). A periodic, symmetric pattern is seen for NEWFIRM with amplitude \(\pm 0.05\) pixel, an indication that a 4\textsuperscript{th} degree polynomial is a poor fit to the distortion profile of this instrument. The WFCam data show coordinate jumps up to 0.08 pixel between the 1024\textsuperscript{th} and the 1025\textsuperscript{th} rows and between the 1024\textsuperscript{th} and the 1025\textsuperscript{th} columns. While the most obvious explanation to this feature would be small physical gaps between the four quadrants of the Hawaii-2 detectors (\textit{Cabello et al.} 2000), this “geometrical” hypothesis was dismissed by the Teledyne engineers we contacted, after a careful examination of the original mask used to manufacture the arrays. At the time of writing we remain clueless about the origin of this issue, which is virtually undetectable using the UKIDSS data alone, because of the survey micro-dithering and tiling strategy.

7.7. Differential chromatic refraction

Dispersive elements along the optical path (atmosphere, lenses) have wavelength-dependent refraction indices producing a color dependent shift of the centroid (e.g., \textit{Filippenko} 1982, \textit{Monet et al.} 1992). This effect is known as differential chromatic refraction (DCR). The magnitude of atmospheric DCR depends on zenithal distance and on the source color index.
Fig. 6 Examples of camera distortion patterns, represented by maps of the pixel scale, for 6 of the 94 camera/filter/run combinations.
A prototype of empirical DCR correction is under development. It needs further testing, and has been turned off for the present study. Systematic errors due to DCR are nevertheless expected to be small:

- the vast majority (95%) of the observations used in this study were obtained at airmass <1.4. The resulting absolute DCR offsets for B stars can add up to 30 mas in the V-band, 10 mas in the I-band and <1 mas in the H and K-bands under typical ambient conditions (Stone 2002). It goes down to 8, 7, 2 and <1 mas, respectively, for solar type dwarfs, which corresponds to the high mass end of our sensitivity limit, and rises again to ~25 mas in V and 5 mas in I for late M-dwarfs. Relative offsets within the field-of-view of our instruments are expected to be even smaller.

- the vast majority of the observations were obtained in the red or near-infrared part of the spectrum, where the amplitude of the DCR is smaller.

- several instruments used in this study are equipped with an atmospheric dispersion compensator (Subaru, CTIO/Mosaic2 and KPNO/Mosaic1)

- finally, for many sources, the effect of DCR on the proper motion fit is averaged over the large number of individual measurements (see Fig. 8).

7.8. Charge Transfer Inefficiency

Radiation damage of the CCD detectors can locally alter their charge tranfer efficiency (CTE), producing deformed PSF and affecting the source extraction accuracy. While this effect is im-
important in the space environment, it is expected to be negligible at the level of accuracy of our study in ground based instruments. The complexity of the charge transfer inefficiency (CTI) effects and the large number of CCD instruments used in this study prevent us from attempting a systematic calibration. We nevertheless note that the dithering strategy used in the CCD observations is expected to average out the CTI effects on relative astrometry. Additionally, recent studies demonstrated that even a very low level of background strongly mitigates the CTI effects by filling the traps (Prod'homme et al. 2012). The sky background in ground based CCD observations is several orders of magnitude higher than in space, and is expected to result in negligible CTI induced distortion of stellar images. Finally, a large fraction of the observations presented in this study was obtained with near-infrared detectors which are unaffected by CTI. We checked for a dependence of the residuals of the PSF fit and the astrometric solution with the signal-to-noise ratio and distance to the amplifier, but found no systematic distortion or offset following the behavior expected for CTI effects. For the rest of the analysis, we consider the CTI effects to be negligible.

7.9. Computing proper motions

After the second iteration of the global astrometric calibration is completed, SCAMP performs another cross-matching of all detections, including those that were rejected at the previous step. SCAMP’s cross-matching algorithm matches in priority detections found in two or more successive exposures. We facilitate the cross-identification of moving sources by feeding SCAMP with exposures ordered by instrument and by observation date. We adopt a cross-matching radius of 3″, which defines the maximum proper motion detectable in our study: ≈ 30/ hr for the highest exposure rate found in our sample (one every 10 s).

SCAMP computes proper motions by doing a linear fit (in the weighted $\chi^2$ sense) to source positions as a function of observation dates. No attempt is made to include the effect of trigonometric parallaxes in the fit; annual parallaxes would be poorly constrained for most sources because of observation dates spanning a too short period of time each year. It is not unusual for the position of a source in a given exposure to deviate strongly from the linear trend with time expected from our model. Visual checks indicate that this happens most frequently because of a cosmetics problem (contamination by an electronic glitch, a cosmic ray hit, a fringing pattern or an optical halo) or some deblending issue. To detect and filter out outliers, SCAMP applies a specific procedure to sources with more than two valid epochs and enduring a “bad” fit, i.e. with a reduced $\chi^2$ above 6. The procedure consists of removing from the fit the one detection that decreases the most the reduced $\chi^2$, and iterate until it is less than 6 or a maximum of 20% of points have been removed (or 2 points if less than 10 points remain). With three detections, the the pair that corresponds to the lowest proper motion is selected. The filtering procedure is triggered on less than 5% of sources.

Figure 8 shows the distribution of the reduced $\chi^2$ as a function of the number of measurements NFOS_OK indicated by color. The cut-off at $\chi^2$/d.o.f=6 corresponds to the outlier rejection threshold (see text). For clarity, only 10% of the catalogue is represented.

7.10. Anchoring to an absolute reference frame

The proper motions computed by SCAMP are not explicitly tied to an absolute reference system such as the ICRS (International Celestial Reference System). Linking our measurements to the ICRS can be made by comparing to the Hipparcos catalog. Unfortunately most stars from the Hipparcos and Tycho catalogs present in the Pleiades field are saturated in our data. The resulting large uncertainties on the corresponding position and proper motion measurements prevent us from deriving an accurate off-
set to the ICRS. Nevertheless we can tie our kinematic measurements very closely to the ICRS by computing the offset required to cancel out the apparent proper motion of extragalactic objects. The vast majority of galaxies detected in our sample are resolved under sub-arcsecond seeing conditions, and can therefore be easily and securely identified based on their SPREAD_MODEL value (Fig. 5). Even though the astrometric precision is considerably worse for extended objects compared to point sources, the large number of resolved extragalactic sources allows a statistically meaningful and accurate calculation of the offset to the ICRS. We select all sources with a SPREAD_MODEL indicative of an extended object that display a proper motion less than 30 mas yr\(^{-1}\) in both R.A and Dec (≈379,000 sources), and compute their median proper motion within boxes of 1°×1°. Figure 10 shows the spatial distribution of median apparent proper motions \(\mu_x, \cos \delta\) and \(\mu_\delta\). A gradient pointing towards the galactic plane is clearly seen in both components, which we interpret as the contribution of galactic stars to the overall astrometric solution derived by our algorithm. To correct for these systematic motions, we fit a 4th order polynomial surface to apparent motions in our “extragalactic” dataset and use it to correct all individual measurements. The residuals after correction are <0.2 mas yr\(^{-1}\), and we conservatively add 0.2 mas yr\(^{-1}\) quadratically to the final estimated uncertainty on the absolute proper motion.

As a sanity check, we then compare the proper motions of the 126 quasars from the Million Quasars (MILLIQUAS) Catalogue (v.3.0) with a counterpart in our catalogue. Figure 11 shows the vector point diagram obtained. As expected, the median proper motion is very close to zero (\(\mu_x, \cos \delta, \mu_\delta\) = (0.29, 0.17) mas yr\(^{-1}\).

8. Photometric solution

A global photometric solution is computed for each photometric instrument. A photometric instrument is defined here as a set of instruments sharing a unique photometric behavior. In the case of our study, we chose to define one instrument per combination of telescope plus detector plus filter set. For example, although they are very similar (see Fig. 2) the CFH12K i-band photometric calibration will be treated independently from that of the MegaCam i-band. This choice is made to minimize the effect of color terms between the various physical instruments. Similarly to astrometry, the photometric solution is computed through weighted $\chi^2$ minimization of the quadratic sum of magnitude differences between overlapping detections from pairs of exposures observed with the same photometric instrument. Color terms are ignored and the only free parameters are the magnitude zero-points. Wherever applicable, photometrically calibrated fields act as “anchors” in the final solution. No zero-point correction is applied to isolated fields. No attempt is currently made to derive illumination corrections for the various instruments: a uniform zero-point is computed for each exposure. Finally, the absolute zero-point calibration provided by the observatories or derived using standard fields obtained the same night is accurate to 0.01 to 0.05 mag for images obtained under clear or photometric conditions.

9. Limitations

9.1. Accuracy and sources of errors

The absolute astrometric accuracy is largely limited by the precision of the anchoring onto the extragalactic reference frame, and is described in the previous section. The residuals add up to a maximum of 0.2 mas yr\(^{-1}\) rms over the ≈10° of the survey. The overall “internal” (or relative, image-to-image) accuracy of the calibration is largely limited by the distortion corrections residuals and the variable anisokinetism related to atmospheric turbulences. We also identify a number of sources of errors that can affect the proper motion measurements:

- cosmic rays and bad pixels can make chance coincidences and therefore add noise to the astrometric solution. Their contribution can be greatly minimized by: i) using the most up-to-date bad pixel masks for each instrument, ii) cleaning non-overlapping images using Laplacian edge detection (van Dokkum 2001), iii) filtering abnormal measurements (in particular based on the SPREAD_MODEL of the sources, see Fig. 5), iv) rejecting outliers in the proper motion fit (see section 7.9),
- artefacts produced by saturated stars (such as deformed point spread functions, streaks and bleeding due to pixel over-
flows) will seriously compromise the astrometric solution. This effect is minimized by carefully setting the saturation levels in SExtractor input parameter files. We note that SExtractor PSF fitting module is capable of adjusting a PSF to the non-saturated pixel of a source, extending the dynamic range of our study above the saturation and non-linearity regime of the instruments used in this survey. The corresponding astrometry, although less precise, is nevertheless often good enough to derive relatively accurate proper motion, as illustrated in Fig. 13.

- extragalactic sources and nebulosities are often extended and their centroid position can be wavelength dependent. They can also surround point-like sources. The corresponding chromatic shift between overlapping images obtained in different filters can compromise the proper motion measurements, but also adds noise to the instrumental distortion measurement, and hence to the astrometric solution. The latter effect is minimized by adjusting carefully SExtractor’s parameters and by iteratively selecting only clean point-like sources for the astrometric registration, as described above. In particular, the SPREAD_MODEL filtering is expected to efficiently reject extended sources. Finally, these chromatic shifts are expected to be stochastic in orientation and amplitude, and their effect on the global solution should average out.

- unresolved multiple systems and visual binaries: the orbital motion of true multiple systems and the chromatic shift of blended pairs made of stars of different colors are an additional source of error that cannot be corrected for. Visual multiple systems resolved in a set of images and unresolved in another (e.g. when the seeing or sensitivity are different) can also produce mismatches and errors. They usually result in large reduced-χ² value.

- differential chromatic refraction errors, as discussed in section 7.7

- parallax motion: at an average distance of ≈120 pc (van Leeuwen 2009), the maximum amplitude of the parallax motion of Pleiades members is of the order of ≈8 mas yr⁻¹. Our observations were obtained over yearly periods of approximately 4 months, and Pleiades members possibly display significant parallax motion. This effect is even larger for nearby stars. Our observational strategy and the archival observations were not designed to measure parallaxes, and the multi-epoch images are not suited for a good parallax determination, which also adds noise to the astrometric solution and proper motion fit. We nevertheless verify that most of these sources (and in particular the Pleiades members) are rejected by the 1-σ clipping and their contribution to the astrometric solution is expected to be negligible.

- atmospheric turbulence, as discussed in section 7.5. Using several consecutive observations allows to further average out this effect, and is an additional justification for using individual frames rather than stacked mosaics.

- proper motions themselves: although stars exhibiting large deviations caused by proper motions are clipped, moderate motions (≈5-10 mas yr⁻¹) may degrade the astrometric solution, affecting particularly the distortion patterns derived for the earliest and the latest runs in the observation time range. A new iterative procedure that recomputes the solution after correcting the positions of stars for the derived motions is under development in SCAMP, but it was not judged robust enough in its present state to be applied to this study.
Fig. 12 shows the estimated error of the absolute proper motion fit as a function of the MegaCam i-band magnitude and the maximum time difference used for the fit. As expected, the estimated error is tightly correlated to the maximum time difference and to the luminosity.

10. Comparison with other astrometric catalogues

In the following, we compare our measurements to various astrometric databases found in the literature and check the consistency of our results. Several of these catalogues are not tied to any absolute reference frame (e.g. UCAC4, UKIDSS), and a direct comparison with the DANCe catalogue (anchored on background galaxies) is therefore not strictly correct. We nevertheless note that the difference can in general be approximated to a simple offset.

10.1. Tycho

The Tycho catalogue (Hog et al. 2000) provides proper motion measurements precise to about 2.5 mas yr$^{-1}$ and derived from a comparison of the ESA Hipparcos satellite measurements with the Astrometric Catalogue and 143 other ground-based astrometric catalogues. These catalogues are unfortunately limited to $V_T \leq 12.5$ mag, very close to the saturation or non-linear regime of the datasets used to build the DANCe catalogue. With this limitation in mind, we compare the results obtained for the 3665 common sources. The agreement is good within the large uncertainties, as shown in Fig. 13. As expected, the difference between the Tycho and DANCe measurement displays a clear dependence on the luminosity, fainter sources being in general in better agreement than bright sources.

10.2. UCAC4

The Fourth US Naval Observatory CCD Astrograph Catalog (UCAC4, Zacharias et al. 2010) provides astrometry, photometry and proper motion measurements over the entire sky and covering the luminosity range between $8 \leq R \leq 16$ mag. Uncertainties are typically of the order of $1–10$ mas yr$^{-1}$, depending on magnitude and observing history. Figure 14 shows a comparison of the proper motion measurements in RA for the UCAC4 and DANCe surveys, as a function of 2MASS Ks-band luminosity. Three major groups of sources can be identified:

1. “vertical outliers” are sources with close-to-zero motion in DANCe but significant motion in UCAC4
2. “horizontal outliers” are sources with close-to-zero motion in UCAC4 but significant motion in DANCe.
3. sources with motions in good agreement in both catalogues within the typical uncertainties and to a constant offset

We find that both outlier groups are clearly related to the luminosity of the sources: the “vertical outliers” are in general among the faintest sources, where UCAC4 is less accurate and contains more errors. The “horizontal outliers” are in general bright sources, and we interpret them as erroneous or inaccurate measurements due to saturation and/or non-linearity of the DANCe surveys. As expected, the distribution of sources is asymmetric, with significantly more sources along the direction of the solar antapex ($\mu_\alpha \cos \delta > 0$ and $\mu_\delta > 0$), which coincidently also corresponds to the Pleiades cluster’s mean motion direction.

4 computed as the quadratic sum of the RA and Dec components, and the 0.2 mas yr$^{-1}$ residual related to the anchoring onto the ICRS

10.3. PPMXL

Roese et al. (2010) derived improved mean positions and proper motions on the ICRS system by combining USNO-B1.0 and 2MASS astrometry. The catalog is complete from the brightest stars up to about $V \approx 20$ mag over the entire sky. Typical individual errors of the proper motions range between $4–10$ mas yr$^{-1}$. Figure 15 compares the proper motion measurements in RA and Dec for the PPMXL and DANCe surveys as a function of the PPMXL uncertainty. The same three groups of sources described in Section 10.2 can be seen:

1. “vertical outliers” are sources with close-to-zero motion in DANCe but significant motion in PPMXL. They generally have one or all of the following properties: a) they have the fewest No number of measurements in PPXML, b) they are among the faintest sources and c) they have a flag $ff=1$ in the PPXML catalogue indicative of a problematic fit. On the other hand, they seem to have a reasonable maximum time difference in the DANCe survey, which is in general associated to more reliable proper motion measurements.
2. “horizontal outliers”, with close-to-zero motion in PPMXL but significant motion in DANCe. These sources generally have the smallest maximum time difference and only a few individual measurements in the DANCe catalogue, suggesting that the DANCe proper motion measurements are less reliable.
3. sources with motions in good agreement in both catalogues within the typical uncertainties

We also note that in general, the 2 outlier populations are made of the faintest sources, for which the astrometric precision is expected to be lower.

Figure 15 also shows an offset between the DANCe and PPXML measurements, especially obvious in declination. Figure 11 suggests that the PPXML proper motion measurements are indeed offsetted with respect to the ICRS, as quasars from the MILLIQUAS catalogue do not have an average zero motion in the PPXML catalogue. We note that a similar offset is also reported in the SPM4 catalogue (see Fig. 8 of Girard et al. 2011).

10.4. UKIDSS DR9

The Pleiades cluster was observed as part of the UKIDSS Galactic Cluster Survey. Lodieu et al. (2012) recently presented a photometric and astrometric study based on the corresponding catalogue, which includes proper motion measurements based on the multi-epoch UKIDSS observations. The proper motion measurements given in the UKIDSS DR9 catalogue provide a useful comparison as the DANCe survey includes all the UKIDSS individual images. Figure 16 compares the proper motion measurements in RA for the UKIDSS and DANCe catalogues. Three major groups of sources appear clearly:

1. “vertical outliers” are sources with close-to-zero motion in DANCe but significant motion in UKIDSS. In UKIDSS they generally have a) the fewest number of measurements in PPXML, b) they are among the faintest sources and c) the largest time difference in DANCe
2. sources with motions in good agreement in both catalogues within the typical uncertainties and to a constant offset corresponding to the offset of the UKIDSS measurements to the ICRS.
3. a diffuse group of sources in poor agreement. Most of these sources are detected in the UKIDSS dataset only, and in general have a small maximum time difference resulting in larger uncertainties in the proper motion fit in both catalogues. The lose correlation and dispersion of this group are consistent with the typical uncertainties (>25 mas yr$^{-1}$) of the corresponding measurements in both catalogues.

As the DANCe measurements for the vertical outliers correspond to the most probable extragalactic sources (which are supposed to have no detectable motion, in agreement with the DANCe measurements) and to the measurements with the largest DANCe time baseline (hence more robust in general), we are confident that the DANCe measurements of the vertical outliers are more reliable than their UKIDSS counterparts. We interpret the inconsistency for the vertical outliers’ population as a greater sensitivity of the UKIDSS proper motion fit to deviant individual astrometric measurements. The small number of measurements used in the proper motion fit ($\leq 6$) together with the lack of rejection in the UKIDSS proper motion fit (Lodieu et al. 2012) make it much more sensitive to the presence of deviant and high leverage points and translates into large numbers of errors. The presence of corrupted frames in the UKIDSS DR9 release (discarded by our quality assurance but not by the UKIDSS quality assurance, M. Read private comm.) probably also result in a number of problematic measurements. By using the individual UKIDSS images rather than stacked UKIDSS mosaics, and by including a robust regression algorithm for the proper motion fit,
Fig. 13. Proper motion in RA for the DANCE (x-axis) and Tycho (y-axis) catalogues. The error bars represent the estimated error in the case of the DANCE measurements, and the reported uncertainty in the case of the Tycho measurement. The left panel corresponds to sources with $V_T < 11.5$ mag, and the right panel to sources with $V_T > 11.5$ mag. A dashed line corresponding to a linear relation is represented to guide the eyes. A similar distribution is found in declination.

Fig. 14. Proper motion in RA for the DANCE (x-axis) and UCAC4 (y-axis) catalogues. Only a random subsample corresponding to 10% of the total number of matches is represented for clarity. The left panel corresponds to sources fainter than $K = 13$ mag, and the right panel to sources brighter than $K = 13$ mag. A dashed line corresponding to a linear relation is represented to guide the eyes. A similar distribution is found in declination.
our method is much less sensitive to erroneous individual measurements, as demonstrated by the lack of a clear “horizontal outliers” population.

10.5. On the use of the DANCe and other astrometric catalogues

Large catalogues necessarily contain errors and problems. The comparison of the DANCe measurements to other astrometric catalogues calls for a number of important warnings about their use:

- some proper motion measurements are more reliable than others, and the uncertainty does not always reflect the reliability. Parameters useful to evaluate the reliability of an individual proper motion measurement include in particular (but not exhaustively): the number of astrometric measurements used for the fit, the maximum time baseline, the reduced-$\chi^2$ of the fit
- measurements errors, unknown systematics and problematic measurements present in any large scale astrometric catalogue most likely always affect the completeness of studies based on their proper motion measurements and should be carefully discussed

While a universal rule to assess the quality of a given measurement cannot be given, we have found that the following proper motion measurements should be considered with caution:

- sources close to or above the saturation or linearity limit of the instruments (in the case of the current dataset, $i \approx 13$ mag), or
- sources with small numbers of measurements used for the proper motion fit (NPOS_OK attribute)
- sources with large reduced-$\chi^2$ (CHI2_ASTROM attribute)

In general, and whenever possible, a visual inspection of the individual images is the most robust way to discard problematic measurements.
11. Example of scientific applications

The DANCe catalogue includes accurate photometry and astrometry for 6,116,907 unique sources, and proper motion measurements for 3,577,478 of them, and as such represents a unique opportunity to address various scientific problems. In the following, we give a few examples of direct applications making use of the catalogue.

11.1. The Pleiades cluster

A detailed scientific analysis of the Pleiades cluster kinematics based on the DANCe catalogue will be presented in a future article (Bouy et al., 2012, in prep.). In this section, we give a brief and general overview of the results obtained. Figure 17 shows the vector point diagram of stellar motions obtained with the dataset described above. The group of co-moving cluster members appears clearly around (20,−40) mas yr\(^{-1}\). The DANCe catalogue also offers a unique photometric database. In the case of the Pleiades dataset presented here, a total of 29 photometric instruments covering the spectral range between 0.37 \(\mu\)m (Sloan \(u\)-band) and 2.2 \(\mu\)m (UKIRT \(K\)-band). Figure 18 shows a \(i\) vs \(r−i\) color magnitude diagram using the photometry extracted from the MegaCam and UKIDSS images. The cluster sequence is also visible.

11.2. Solar system bodies

Solar system bodies have typical velocities in the range between \(\approx 2''\) hr\(^{-1}\) (trans-neptunian objects, hereafter TNO) and \(\approx 20''\) hr\(^{-1}\) (main belt asteroids, hereafter MBA). Most observations used in this study are made of several consecutive and dithered images of the same field. Fast moving sources such as solar system bodies can therefore be easily identified. Minor planets are expected to be extremely numerous in the direction of the Pleiades cluster, as it lies close to the ecliptic plane. A detailed analysis of the solar system bodies encountered in the DANCe dataset will be presented in a future article (Bouy et al. in prep) and we only give a brief overview of the capabilities of our algorithms for solar system studies. A basic selection of all sources with a proper motion greater of \(\approx 20''\) hr\(^{-1}\) gave 11,404 candidate minor planets. A request on SkyBot (Berthier et al. 2006) indicates that only 2,837 have a counterpart within a radius of 1' in the database of known solar system bodies as of August 2012, all of them main belt asteroids. A visual inspection of \(\approx 100\) random candidates shows that \(\lesssim 5\%\) are false detections due to artefacts (cosmic ray or ghost coincidence, false detection, etc...). After inspection and rejection of these artefacts, the astrometric and photometric measurements will be submitted to the IAU Minor Planet Center. The high precision astrometry (with a typical accuracy better than \(\lesssim 10\) mas on individual epochs) will be extremely valuable to refine the orbital solutions. The accurate photometry (with typical absolute accuracy \(< 10\%\), and relative accuracy better than \(< < 1\%\)) will be useful to classify the bodies (based on their colors) and in some cases study their rotational periods and geometry. The depth of the datasets allows the discovery of very faint objects, as illustrated in Fig. 19 probing a largely incomplete asteroid size domain.

11.3. Nearby ultracool dwarfs

Nearby ultracool dwarfs can easily be identified in the DANCe catalogues as faint fast moving sources. Figure 20 shows an example of such object discovered in the present survey. A complete analysis will be presented in a future paper, and we here only present the basic properties of one particular source to illustrate the scientific case. The source must be relatively nearby as it moves at \(\approx 200\) mas yr\(^{-1}\). It has a counterpart in the WISE (Cutri & et al. 2012) and its [W1]-[W2] color matches that of known T4−T5 ultracool dwarfs from Kirkpatrick et al. (2011).
11.4. Galactic dynamics

Accurate large scale photometric and astrometric surveys provide a unique opportunity to study the galactic stellar populations. In Fig. [21] we show the distribution of motions in RA and Dec as a function of the $g-r$ color. For this figure, a subset of galactic sources was selected in the DANCe catalogue based on:

- the quality of the proper motion measurement, keeping sources with $g$ magnitude in the range 12–21 mag where the estimated uncertainties are better than $\lesssim 2$ mas yr$^{-1}$ in average.
- the “stellarity”, rejecting all sources with a SPREAD MODEL indicative of an extended source. Although it does not reject unresolved extragalactic sources, the remaining extragalactic contamination on the luminosity range mentioned above should be small enough for the simple purpose if this illustrative example.

A gross bimodal structure in $g-r$ is clearly seen, reflecting the separation of the halo/thick-disk ($g-r \sim 0.5$ mag) and the thin-disk ($g-r \sim 1.3$ mag) populations. The Pleiades population is clearly seen as a small clump around (20,-40) mas, yr$^{-1}$ on top of the general thin disk population. Such observations can provide very important constraints and input to the models of galactic populations.

12. Conclusions and future prospects

We have presented a set of tools capable of deriving high precision relative proper motions using large numbers (several thousands) of ground-based images originating from various instruments. We apply these tools on multi-epoch panchromatic datasets of the nearby Pleiades cluster, and compare to other astrometric catalogues. The results demonstrate our ability to derive accurate proper motion with an estimated accuracy better than $1$ mas yr$^{-1}$ for sources as faint as $i=22-23$ mag, depending on the luminosity and observational history (time baseline, number and quality of the frames, as well as presence and number of reference extragalactic sources for the anchoring on the ICRS).

The DANCe project will use this method to conduct a survey of the most nearby star forming regions and clusters. It aims at complementing the Gaia mission in the substellar regime, and in regions of high extinction. By taking advantage of the wide field surveys performed in the late 90’s and early 2000’s, it will provide high precision proper motion measurements for millions of stars in various nearby associations. In the future, the DANCe project will also take advantage of the growing number of wide and very wide field imagers which will equip various observatories. Large and all-sky surveys are also on-going (e.g. Pan-STARRS, ESO-VST, ESO-VISTA) or foreseen (DES, LSST), ensuring a large flow of high quality images usable for high precision astrometry.

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Fig. 18 $i$ vs $r-i$ color magnitude diagram (MegaCam). Two horizontal lines represent the luminosity of Pleiades members with masses 0.072 and 0.030 $M_\odot$, according to the models of Baraffe et al. (1998) and assuming a distance of 120 pc. The Pleiades sequence is visible.

Fig. 19 Successive CFHTMegaCam images of a main belt asteroid of $g=23.1$ mag. The UT time of observations are indicated. These 3 images are an illustrative subset of 19 images used to measure the proper motion of this source.
Fig. 21 Density maps showing the distribution of proper motion in RA (upper panel) and Dec (lower panel) as a function of the g − r color for galactic sources in the range 12 < g < 21 mag.
