RECURRENT APPROXIMATION AS THE TOOL FOR EXPANSION OF FUNCTIONS AND MODES OF OPERATION OF NEURAL NETWORK

A. Trunov
PhD, Associate Professor, First Vice-Rector
Department of automation and computer-integrated technologies
Petro Mohyla Black Sea State University
68 Marines str., 10, Mykolaiv, Ukraine, 54000
E-mail: trunovalexandr@gmail.com

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1. Introduction

An experience in the automation of complex processes increasingly demonstrates inability of classic methods of the theory of automatic control to effectively resolve the problems of automation of production processes and of management of socio-economic projects [1–3]. Coordination, coordination management [1] as the main principle of functioning in a general control system plays the role of a subsystem of the process stabilization relative to a predetermined strategy that is represented by a trajectory in the space of states [4]. When defining the role of coordination in the process of control, it should be noted that for any intellectual, industrial, social human activity, a necessary characteristic is the procedure of decision making [1, 2, 5, 6]. The latter is presented in one of the forms: values of parameters, functions of controlling influences, formation of productive rules, linguistic terms from the given set [7–10]. For the formation of theoretical principles of the theory of coordination of complex systems, it is necessary to further develop formal methods, mechanisms, tools of coordination that ensure coherence of functions of components of the system and synchronization of objectives as a single entity [2]. At the same time, at present there are successfully operating systems of expert functional diagnosis of complex objects, for example [7, 9]. There are attempts at constructing models of dynamic processes based on the networks of different types [2, 3] created on the methods of conventional and fuzzy logic [4, 8–14]. Modeling of the systems is conducted, which include non-stationary objects [3, 8–10], including the GPSS environments [3]. They examine and analyze the processes of formation of databases [9] and knowledge bases [12–14], formation of productive rules and conclusions based on the Sugeno-Mamdani algorithms and the use of fuzzy neural networks for identification and control of weakly formalized objects, using the Sugeno-Mamdani-Kang network [8]. However, as it is generally known, one of the tools for coordination, which in its initial essence provides coherence of functions of the components of a system and synchronization of objectives as a single entity, is a neural network. It is a means that implements the principle of causation. Its properties especially expand owing to the introduction of recurrent approximation [15], the indicator – vector [16], and development of algorithms for analytical learning [17]. Such recurrent artificial neural networks (RANN) [18] acquire attractive properties and capacities that are not yet fully explored, that is why the implementation of modes of their operation is relevant, including for a new direction of providing coordination control [1, 2] and the indicator – vector [16].

2. Literature review and problem statement

Artificial neural network today is one of the most powerful tools to solve the problems of the information streams processing [1, 19]. As demonstrated in papers [11, 18–20],
the application of recurrent network for the initial data processing creates preconditions and realizes the advantages of a comprehensive approach to the processes of collection, initial processing, accumulation of data, searching for mathematical models, formation of knowledge bases. Development of the structure of such networks, search for and application of convolutions leads to the creation of hybrid and recurrent networks [23]. Their training for interpreting the motions of the highest order that is transformed in the motion of the drive and implements the required trajectory is based on the variants of the theory of optimum control. The application of this approach to biological problems leads to analogies with the chains of cerebral or spinal cord [23]. However, the implementation of these innovative approaches is based on the stepping reverse transitions, which in turn require measuring a signal of sensory feedback and intelligent analysis. Most of the implementations of various stages of the process of intellectual activity are carried out in such networks [2] with the help, first of all, of measuring, then signal processing. Lately, the principles of comparative analysis have been applied more and more for the solution of problems of intellectual activity [5]. However, the need to provide an uncontrolled learning and compression of information by automatic coder, modification of the lost functions and invariance is partially solved in article [24] by changing the structure and formation of parallel links. As demonstrated in papers [8, 10], further development of methods of application of comparative approaches to the analysis leads to the necessity of observing quality attributes of behavior of a physical magnitude by the change in discrete magnitudes. The introduction of indicators [16, 18], which are formed by the comparative rules, demonstrates that they can be used for the formation of productive rules. Development of the systems for initial processing of data using RANN [16, 18], that has recently been implemented in the automated systems [7–9], in industries [12–14] that are rapidly readjusted, and surveillance systems [14], necessitates further development of rapid methods [19–22] of instantaneous learning and qualitative analysis and the methods of formation of results – conclusions based on it [7, 8, 10, 19–22]. As demonstrated in articles [15–17], new types of representation of continuous signal with a simultaneous application of the indicators – vectors [16] and recurrent approximation [15] opens new approaches to diagnosing [15, 16] and creation of RANN.

The main unsolved problems are the decomposition of dynamic signal and its representation through a new tool – the indicator – vector, using recurrent network based on the short-term memory. However, another unsolved problem is the formation of structure for implementation of various modes of RANN operation to solve practical problems of data processing, forming a model and creating productive rules.

3. Aim and tasks of the study

The aim of this work is the formation of structure of recurrent network of information processing with expanded functionality and additional modes of operation based on the indicator vector and recurrent approximation of continuous function.

To accomplish the set goal, the following tasks are formulated:

- to synthesize the structure of recurrent network that is capable to perform calibration, to prepare information on the error of approximation, to solve the problem of minimization;
- to build an algorithm for analytical training a neuron with multiple inputs and to demonstrate its practical effectiveness;
- to synthesize algorithms that provide a necessary set of operating modes and production of controlling rules.

4. Setting and solving the problem of formation of the structure of recurrent network of data processing based on the indicator – vectors and recurrent approximation of continuous function

4. 1. Setting the problem of decomposition of vector function into a Taylor series using the indicator vectors

We will introduce on unlimited orderly set \( \forall Y \in (-\infty, \infty) \) the rule of trigger activation that is defined by two standards \( Y_1, Y_3 \) and the level of permissible deviations \( \delta_1 \) and \( \delta_2 \):

\[
D_Y(y) = \begin{cases} 
-1, & \text{if } Y < Y_1 + \delta_1; \\
0, & \text{if } Y \in [Y_1 + \delta_1, Y_3 - \delta_2]; \\
1, & \text{if } Y > Y_3 - \delta_2. 
\end{cases}
\]

(1)

Note that we introduced operator \( D_Y \), which acts on the scalar function, and its image forms a scalar, which is reflected on the metric space at any magnitude \( \delta_1 \) and \( \delta_2 \), which during configuration may also tend to zero. Under these notes and conditions, the decomposition component of any vector function from vector argument will take the form:

\[
L(\vec{x}_p + \Delta \vec{x}_p) = L(\vec{x}_p) + D_L(\vec{x}_p) \Delta \vec{x}_p + \\
+ \sum^n_{i=1} \frac{\partial L(\vec{x}_p)}{\partial x_i} \Delta x_i + \\
+ \sum^n_{i=1} \sum^n_{j=1} \frac{\partial L(\vec{x}_p)}{\partial x_i \partial x_j} \Delta x_i \Delta x_j.
\]

(2)

This decomposition is realized under conditions of existence of the Fréchet derivatives from the first to the third order, and its accuracy is determined, according to the mean value theorem, by the maximum value of third order derivative module [18].

4. 2. Application of short-long term memory to designing a recurrent network

Under these conditions, the application of recurrent network with memory and structural elements that define the components of the vector-indicator also requires an effective tool for analytical determination of the roots. Fig. 1 demonstrates a fragment of such a RANN, which generalizes the idea of a new decomposition of continuous function \( L(\vec{x}_{\text{init}}) \) in a Taylor series and its practical application for realization of the process of parallel and recurrent signal processing. Thus, if the output from neuron 3 defines reference behavior of system for arbitrary vector of strategies \( \vec{X} \), and from neurons 4 and 17 for \( \vec{X}_i \) and \( \vec{X}_{\text{init}} \), then deviation:

\[
\Delta L(\vec{X}) = L(\vec{X}) - L(\vec{X}_{\text{init}}).
\]

(3)
In turn, this standard element (Fig. 1) also gives a possibility to estimate an error of approximation by comparing magnitudes $L(\vec{X}_{n-1})$, calculated by (4), and the output 17. The latter, in turn, opens up possibilities to perform improvement of the model. This is especially relevant for real systems, in which $L(\vec{X}_{n-1})$ are oscillating nonsmooth functions, since in such cases there occurs a necessity of multipoint approximations. However, as demonstrated in paper [18], the number of points of information delay exceeds by one the order of the higher derivative, so its magnitude is limited. It was also demonstrated that for examining the properties of object, an important condition is the awareness about direction of the change in argument. Applying the comparator to argument growth rate that implements predicate in the form (1), we will obtain from the output of neuron 16, which implements predicate in the form (4), we will create the argument growth. Applying the comparator to the output of neuron 16, which implements predicate in the form (1), we will obtain from the output of neuron 18 the value of additional component of the indicator – vector:
\[ V_i = D_i(\Delta \vec{X}). \]  

4.3. Practical determination of convergence of algorithm for the analytical training of neurons

Analytical training and retraining neurons was proposed and implemented in article [17] for a conditional neural network. It should be noted that the recurrent solutions proposed in [17, 18], under conditions of minimizing the sum of squares of errors, as a fragment of RANN come down to solving the system of nonlinear equations. Let us confine ourselves to a case of finding the coefficients of synaptic weights $\omega_{kj}$ for the j-th neuron of the k-th input and for the magnitude of input $x_{kj}$ of the i-th standard with a total number of standards $I_i$. Under these notations, we will write down the algorithm's key system:
\[ \{ B_k = 0; k = 1, K_k; j = 1, K_j \} \]  
where it is denoted
\[ B_k = \sum_{l=1}^{M} x_k \eta_l Y_l \left(1 + e^{-x_l} \right)^{-2} e^{-x_l} \]  
\[ -\sum_{l=1}^{M} x_k \eta_l \left(1 + e^{-x_l} \right)^{-3} e^{-x_l} \]  
\[ \forall j \text{ if } (k = 1) \text{ then } (x_{k-1, j}) = 1; \]  
\[ \forall j \text{ if } (j = 1) \text{ then } (x_{k-1, j}) = 1; \]  

Using system decomposition (6) by the recurrent approximation method [15] and being limited only by increments of first order, write down the system for determining the synaptic weights $\omega_{kj}$ for the neuron with the number of inputs $K_i$:
\[ \{ B_k = \frac{k_j}{\Delta} \omega_{k-1, j} A_{kj} = 0; k = 1, K_k; j = 1, K_j \} \]  
where it is denoted
\[ A_{kj} = \sum_{k=1}^{M} \sum_{l=1}^{N} (-1)^{l} x_k x_{k, l} Y_l \left(1 + e^{-x_l} \right)^{-2} e^{-x_l} \]  

Numeric results, with detailed analysis of influence on oscillations and the speed of convergence, of both magnitude and sign of the initial approximation $\omega_{kj}$, are represented in paper [18] on the example of neuron with one input and one output. However, to ensure analytical training directly in the process of control, it is necessary to determine the moment of termination of iterative process of approximation.
The availability and quality of such a criterion determines the efficiency of training. Let us derive it as evaluation of error of coefficients of synaptic weights. Suppose that functions $B_k$ are integrated with the square:

$$[B_k] = \sqrt{\int_B (B_k)^2 \, dx}.$$

We receive an error rate by applying operator of rationing to equations (6) and (7), then the evaluation from the bottom and the top will be analytically determined as:

$$\frac{|B_k|}{A_k} \leq \frac{1}{\max_j \left| \frac{A_{kj}}{A_j} \right|} \leq \frac{1}{\min_k \left| \frac{A_{kj}}{A_j} \right|}.$$

The latter gives the assessment of magnitude, which determines the limit of termination of iterations under conditions of the assigned magnitude of permissible error of activation function for standards:

$$\left| \Delta \omega_{j+1} \right| \leq \frac{|B_k|}{A_k} \leq \frac{1}{\min_k \left| \frac{A_{kj}}{A_j} \right|}.$$

**Effect of initial approximation and parameters of system on the evaluation of error of coefficients of synaptic weights for the fifth iteration**

| $N_k$ | $\omega_{10}$ | $\omega_{10}$ | $|B_k|$ | $|B_k|$ | $\sigma$ | $|\Delta \omega_1|$ | $|\Delta \omega_2|$ |
|-------|----------------|----------------|------------|-----------|--------|----------------|----------------|
| 1     | -0.5           | 5              | -6.50E-6   | 5.374E-6  | 0.0075545 | 6.85E-5       | 0.01206       |
| 2     | 0.5            | 5              | 0.009941534 | 1.43196E-5 | 0.007577 | 0.008065   | 0.0080015   |
| 3     | -0.1           | 0.1            | -0.97460387 | 0.017202286 | 0.00788637 | 0.53247 | 0.707926 |
| 4     | 1              | 0.001963412    | 0.018706151 | 0.04438 | 0.009275 | 1.002492 |
| 5     | 0.1            | -0.1           | 0.00658054 | 0.01502513 | 0.03529 | 0.03513 | 0.940764 |

The data of analysis of the effect of initial approximation and the system parameters on the evaluation of error of coefficients of synaptic weights for the fifth iteration are presented in Table 1. According to results of calculations, the solution of the system are the coefficients of synaptic weights $\omega_{10} = -0.40674$, $\omega_{10} = 8.925389$. Thus, for arbitrarily selected five sets of initial approximations $\omega_{10}$, we simultaneously calculated the left parts of the system (6) $|B_k|$, $|B_k|$ and calculated mean squared deviation of error of activation function $\sigma$. As demonstrated by analysis of data from Table 1, initial approximations slightly affect the number of iterations to the assigned mean squared error. In addition, an increase in the number of approximations to eight provides accuracy of the calculations, that is, the relative error is less than tenth of percent.

**5. Discussion of results of simulation of analytical training of RANN**

[Continued discussion]

**5.1. Modes of RANN operation and algorithm of recurrent formation of the model**

**Calibration mode.** To ensure the calibration process in automatic mode of any sensor or measuring device, it is necessary to measure in one point of time three magnitudes: $X_n$ – vector of independent magnitude of argument, the initial magnitude of signal of sensor $L(X_n)$, reference signal $L_r(X_n)$, or, in the automated regime, to read out a reference device indications and enter them to the system. Under these conditions, it is also advisable to register errors of reference indications and argument. Fragment of a recurrent network is displayed in Fig. 2. Calibrating multiplier is determined during calibration and stored in a database as a function of independent magnitude of argument $X_n$:

$$k(X_n) = L(X_n) / L_r(X_n).$$

During calibration, the range of calibration is also defined and saved. In most cases, the calibration mode is provided due to the formation of physical value $X_n$, which in turn is dependent on time. In other words, to implement the idea of calibration, it is necessary to additionally control time. Under conditions of a stable time step $\Delta$, we select a
The action of reg

The main activity of new tools

The latter converts them into the database standard and

neurons 4, 8, 12, 16 are submitted to the controller’s input.

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the sensor arrives directly to the input of neuron 3. By analogy, simultaneously with neuron 3, the same signals are sent to the inputs of neurons 4, 8, 12. Under these conditions, the data from the input of neuron 1 and the outputs from neurons 4, 8, 12, 16 are submitted to the controller’s input. The latter converts them into the database standard and resends to record and store them in it.

where \( L_{ad}(X_n) \) is the signal, which is directly obtained from the output of neuron 3 after correction of zero if the signal from the sensor arrives directly to the input of neuron 3. By analogy, simultaneously with neuron 3, the same signals are sent to the inputs of neurons 4, 8, 12. Under these conditions, the data from the input of neuron 1 and the outputs from neurons 4, 8, 12, 16 are submitted to the controller’s input. The latter converts them into the database standard and resends to record and store them in it.

The mode of formation of evaluation of adequacy by the set of criteria. When implementing this mode, a sequence of values of vector of state is generated, in turn, at the same time a signal is sent to the input of object and the network (to neuron 1). The output of signal from the object is sent to neurons 3, 4, 8, 12. Comparison of the magnitudes of output signals with neuron 3 and 21 makes it possible to obtain the magnitude of error. Upon applying the magnitude of signal of output of neuron 16 and magnitude of two derivatives of the outputs of neurons 8 and 12, we calculate derivative of third order. Thus, using the criteria of adequacy and setting the list of sorted values of \( X_n \) – vector of independent magnitude of argument from the set of range of its change, it is possible to calculate absolute and relative errors of both physical magnitude and its derivatives.

The mode of formation of productive rules and knowledge base. At this stage, data from the database are entered to the network and the behavior of both the physical magnitude that describes the object and its derivatives and errors is examined. Due to the complex of such actions, the productive rules and quantitative criteria are formed that allow selecting the model on the given interval of change in the vector of input.

The mode of formation of productive rules

It is advisable to note such a possibility of using new tools of the indicator vector and properties of recurrent neural network that is built based on recurrent approximation as the formation of productive rules to solve problems: finding a simple root of monotonic function; finding a not simple root of monotonic function; finding a root of oscillating function; selection of controlling influence as a problem on the syn-

5. 2. Modes of finding roots and formation of productive rules

Fig. 3. Fragment of realization of RANN measurement mode

The mode of formation of the model. The main activity of this stage is to find modules and indicator vectors, multiplication and adding of the products afterwards and formation of the difference between the magnitude of this sum and the measured magnitude. In addition, at this stage it is expedient, starting with the fourth point, to calculate the third derivative and enter the data about it to the database.

Fig. 2. Fragment of realization of RANN calibration mode
thesis of controlling influence. Let us consider in stages the peculiarities of solving each of these problems.

Finding a simple root of monotonic function. Assume that the first approximation is taken arbitrarily, and for it, at the outputs from neurons 6, 10, 14, 19, the value of signals is formed. Then the rule that determines the second and other approximations takes the form:

\[ X_{n+1} = X_n - V_1 V_2 \left[ \sum_{k=1}^{n} k! \delta_k (X_k) \right] X_{n-1} \]  

(9)

by information about the first point. However, if one considers that the built network has a shift by \( k+1 \) point, then for this type of cases, limited by the first derivative, the process of finding a root is accelerated. This rule is valid even when the first derivative approaches zero (it has a value less than the accuracy of calculations), since under these conditions \( V_3 = 0 \). Such a rule simplifies the calculation of approximations, but leads to an increase in the number of approximations. Another variant of building a productive rule is the variant (\( K = 1 \)), in which the values of the indicator vector are saved and the derivatives of second or senior orders are used. A rule is built based on the behavior of their increments:

\[ X_{n+1} = X_n - \left[ L(X_n) (V_1 + \Delta V_1) (V_2 + \Delta V_2) \right] \left( \sum_{k=1}^{n} k! \delta_k (X_k) \right) \Delta X_{n-1} \]

This rule is implemented even in the case when the point of approximation reached the point of root. In this case, the value of magnitude \( X_\infty \) simply ceases to grow.

Finding a not simple root of monotonic function. Suppose that in the point of root (the value of function is zero) and the first derivative is also zero, that is, the point of root is also the point of contact, that is, the point of extremum. Assume that the first approximation is taken arbitrarily. For it, at the outputs of neurons 6, 10, 14, 19, the values of signals are formed, then by rule (9) we determine the second and others approximations.

Finding a root of oscillating function. As demonstrated in [16], for non smooth oscillating functions, in the case of selection of such initial value \( X_1 \) that for any of the approximation schemes the next value corresponds to \( X_2 \), for which the indicator vector is equal to \((1, 0, 1)\) or \((1, 1, 0)\), the process of finding out the next approximation must be terminated. Put the following order of actions in accordance with this case:

1. Adopt: \( L(X_1) = L(X_2) \);
2. Find from decomposition:

\[ L(X_1) = L(X_2) + L'(X_2) \Delta + L''(X_2) \Delta^2 / 2 \]

increment

\[ \Delta = -2L'(X_2) / L''(X_2) \];
3. Let us verify – if

\[ \forall \exists X[e] X_0, X_1 \prod(X) \geq L(X_0) = L(X_1) \text{ and } L''(X_1) \neq 0, \]

then the new approximation \( X_3 \), regardless of the peculiarities of behavior of function on the interval, will be found by expression:

\[ X_3 = X_2 - 2L'(X_2) / L''(X_2) \]

One can see from the latter that if one follows the usual pattern, because of the properties of function and selection of the starting point of approximation, one of the approximations is in the interval, on which there is a cycling observed. When following the algorithm 1–2–3, the process of cycling can be predicted and excluded. For improvement and generalization of the above-described rule, we will introduce controlling function \( W \), the magnitude of which will be associated with three components of the indicator vector. Let us represent decomposition in the last point, which starts the process of cycling:

\[ L(X_3) + L'(X_3) \Delta + L''(X_3) \Delta^2 / 2 = L(X_3) W, \]

(10)

where

\[ L(X_3) W = \begin{cases} L(X_3), & \text{if } \{\Delta V_1 = 0 \text{ and } \Delta V_2 \geq 1 \text{ and } V_3 \neq 0\}; \\ 0. & \end{cases} \]

Only under conditions \( \Delta V_1 = 0 \) and when the increment value of the second component, processed by comparator (1) \( \{\Delta V_2 = 1\} \) as well as when the third component is not equal to zero \( V_3 \neq 0 \), then equation (10) is fulfilled, and the next approximation will take the form:

\[ X_{n+1} = X_{n-1} - \frac{L(X_{n-1} - V_1 V_2 V_3)}{L'(X_{n-1})} \frac{(V_{n-1} + \Delta V_{n-1}) (V_{2n-1} + \Delta V_{2n-1})}{2} + \frac{L(X_{n-1}) V_{n-1}^4}{L''(X_{n-1})} \Delta V_{2n+1} \]

(11)

Thus, the process of finding the root is simplified and it comes down to simple calculations without interval of oscillation. The latter is carried out through the introduction of the indicator vector and recurrent networks after the formation of the appropriate set of production rules. Construction of additional logical rules for information processing eliminates the cycling and improves the root search algorithm even for nonmonotonous complex behavior – oscillating function.

Mode of selection of controlling influence as the problem on the synthesis of controlling influence.

Assume that there was set a problem of minimization of objective function under conditions of existence of inequality constraints for a nonlinear object. Suppose also that the object is being observed and the numerator determines:

– vector of deviation of objective function, which describes functioning of the process, from the reference value of deviation by precept;
– the indicator vectors of deviation vector.

Depending on the type of behavior of the deviation vector, the problem comes down to the problem of finding a root. Thus, if one consistently sets the values of the Lagrange function, the value of which is recorded in the database when training the system, and calculates indicators \( V_1, V_2, V_3 \) and indicator of argument change \( V_4 \) and indicator of change in the Lagrange function

\[ V_5 = D \left[ \Delta L(X) \right] = D \left[ L(X) - L(X_{n-1}) \right] \].
then the conditions for the formation of productive rules are formed. Let us write down one of the possible productive rules.

If \( V_2 > 0 \) and \( V_1 > 0 \) and \( V_2 < 0 \), then \( U_{n+1} = U_n - V_1 \Delta U_n \).

According to this rule, the control that provides minimization of the Lagrange function, implements the resulting part of the rule “condition – action” that contains indicator \( V_5 \).

One can see from the latter that if the Lagrange function derivative changes its sign, then indicator \( V_5 \) changes it too and the rule is valid.

One can see from the latter that if the Lagrange function derivative changes its sign, then indicator \( V_5 \) changes it similarly while preserving \( V_4 \), and the rule of determining the effective part works correctly. When implementing the problem of maximization, the sign in front of \( V_5 \) in the last expression of the resulting part of the rule changes from a minus sign to a plus.

Thus, the difference between the current value of any function or Lagrange function and the set of its values from a database allows creating productive rules of the effective part by analogy for the function of controlling influence that will make it possible to find the root of function or to ensure its set value within the permissible deviation. An analysis of root values – the magnitudes of controlling influence, as a solution of the problem on the root, will enable us to find their interval. The latter, by the choice of operator or by the rule “condition-action” will form coordinating and controlling influence and will allow determining amplification factors. The choice of algorithms and the formation of laws of controlling influence and will allow determining amplification factors make such a task relevant for practical application of recurrent networks in the practice of coordinating control. In the case of formation of the Lagrange function with regard to constraints, the system’s capacities expand to the problems of control with limited inequalities.

6. Discussion of results of research into possibilities of formation of new features and modes of operation of RANN

The examined fragments of RANN, due to the proposed extended functions and operating modes, may serve as standard elements of coordinating control system or decision making support system. The examples that are built based on recurrent approximation, demonstrate new possibilities of using the tools of the indicator vector and RANN. Their use is also useful for solving separate applied problems: formation of productive rules for solving the problems of finding simple root of monotonic function, finding a not simple root of a monotonic function, finding a root of oscillating function, selection of controlling influence and the problem on the synthesis of controlling influence. Obtained results continue and complement practical implementation of the idea of recurrent approximation for the solution of problems of modeling and design [15]. The latter, based on the assumption of continuity and differentiation by Fréchet, has limited application. The search for ways of removing these constraints or their circumvention focuses further research on the search for direct and reverse transition from metric to other spaces. The introduction of a set of linguistic variables with a uniform algorithm for constructing the metric on a limited number of standards opens such ways but the problems of the gap, uniqueness and existence give birth to new obstacles at present.

7. Conclusions

1. The structure of recurrent networks of information processing that is formed based on the indicators - vectors and recurrent approximation of continuous function, provides new modes of its operation and extends the functionality. It is capable to realize calibration, to prepare information on the error of approximation, to solve the problem of minimization and act as a module of decision making support system. Its structure forms the information support of the conditional part of the rule “condition-action” and implements effective part in the algorithms of coordination control.

2. The application of the indicators – vectors renders the algorithms for analytical training practically independent of the choice of initial approximation of synaptic weights coefficients, while the network acquires mechanism of re-adjustment during optimal control depending on the changes that occur to the object.

3. The synthesized structure is capable of implementing the algorithms that provide a necessary set of operating modes and production of controlling rules based on the analysis of behavior of the set of the indicator vectors. It is also able to realize simple algorithms for finding roots and control that minimizes or maximizes continuous function or the Lagrange function under conditions of existence of constraints of inequalities for a nonlinear object in accordance with the analytical criteria of evaluation of error of synaptic weights coefficients.

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