REVISITING THE LONG/SOFT–SHORT/HARD CLASSIFICATION OF GAMMA-RAY BURSTS IN THE FERMI ERA

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ABSTRACT

We perform a statistical analysis of the temporal and spectral properties of the latest Fermi gamma-ray bursts (GRBs) to revisit the classification of GRBs. We find that the bimodalities of duration and the energy ratio ($E_{\text{peak}}$/Fluence) and the anti-correlation between spectral hardness (hardness ratio (HR), peak energy, and spectral index) and duration ($T_{90}$) support the long/soft–short/hard classification scheme for Fermi GRBs. The HR–$T_{90}$ anti-correlation strongly depends on the spectral shape of GRBs and energy bands, and the bursts with the curved spectra in the typical BATSE energy bands show a tighter anti-correlation than those with the power-law spectra in the typical BAT energy bands. This might explain why the HR–$T_{90}$ correlation is not evident for those GRB samples detected by instruments like Swift with a narrower/softer energy bandpass. We also analyze the intrinsic energy correlation for the GRBs with measured redshifts and well-defined peak energies. The current sample suggests $E_{\text{iso}} = 2455 \times (E_{\text{peak}}/10^{55})^{0.59}$ for short GRBs, significantly different from that for long GRBs. However, both the long and short GRBs comply with the same $E_{\text{iso}}$–$L_{\text{iso}}$ correlation.

Key words: gamma-ray burst: general – methods: data analysis

Online-only material: color figures

1. INTRODUCTION

The field of gamma-ray bursts (GRBs) has rapidly advanced in recent years, especially after the launch of NASA missions Swift (in 2004; Gehrels et al. 2004) and Fermi (in 2008; Atwood et al. 2009). A physical classification of GRBs is still a basic open question (e.g., Zhang 2011). According to the traditional classification schemes, GRBs can be divided into long and short ones, based on the well-known bimodal distribution of their durations monitored by the Burst And Transient Source Experiment (BATSE; Meegan et al. 1992), which also show different spectral hardness ratios (HRs; Kouveliotou et al. 1993). The HR in conjunction with the duration provides a means for classification, e.g., the long/soft class constitutes roughly 3/4 of the population and the short/hard class constitutes the other 1/4 for BATSE GRBs (Kouveliotou et al. 1993; Qin et al. 2000). The difference between long and short GRBs is further established by the observations of afterglows and host galaxies. The fact that several nearby long GRBs are associated with Type Ic supernovae (SNe) and most long GRB host galaxies are found to be dwarf star-forming galaxies favors the speculation that most long GRBs are accompanied by massive stellar explosions (see Woosley & Bloom 2006 for a review). Some nearby short GRBs (or short GRBs with a long–soft extended emission) have host galaxies that are elliptical or of early type, with little star formation (Fox et al. 2005; Gehrels et al. 2005; Berger et al. 2005a; Barthelmy et al. 2005). This points toward a different type of progenitor, e.g., compact object mergers (see Nakar 2007 for a review).

This dichotomous picture was soon challenged by some following observations. GRB 060614 and GRB 060505 are two nearby long GRBs that did not have bright SN associations, sharing similar properties to short GRBs (Fynbo et al. 2006; Della Valle et al. 2006; Xu et al. 2009). Three high-z GRBs 080913, 090423, and 090429B have rest-frame durations shorter than 1 s but are likely related to massive stars\textsuperscript{5} (Greiner et al. 2009; Salvaterra et al. 2009; Tanvir et al. 2009; Cucchiara et al. 2011). An observed short GRB 090426 was found in many aspects similar to long GRBs and was also probably linked to the death of a massive star (Antonelli et al. 2009; Levesque et al. 2010; Xin et al. 2011; Thöne et al. 2011; Nicuesa Guelbenzu et al. 2011). These results suggest that certain observational properties (e.g., long versus short duration) do not always refer to certain types of progenitor (see Zhang et al. 2009, and references therein). Moreover, the bimodal duration distribution was not presented in observation for some detectors with a narrow/softer energy bandpass such as HETE-2 and Swift, and the distinction of short/hard and long/soft in the hardness–duration panel is not very clear (e.g., Sakamoto et al. 2011, and references therein; Shao et al. 2011). Recently, Guiriec et al. (2010) analyzed three very bright short GRBs observed by the Fermi Gamma-Ray Burst Monitor (GBM; Meegan et al. 2009) and found that short GRBs are very similar to long ones, but with light curves contracted in time and with harder spectra stretched toward higher energies. They also showed that the hardness evolutions during the bursts follow their flux/intensity variations, similar to long bursts. By studying the composite light curves including both the prompt and afterglow emission of GRBs detected by Swift, Shao et al. (2011) found the similarity of the radiative features between the long and short bursts. They also proposed that the spectral evolution of the prompt emission might be an important factor that determines the correlation between the HR and duration.

Theoretically speaking, the duration may not be a unique indicator for the physical category of a GRB. In the pre-Swift era,\textsuperscript{5} The other possibility, that these high-redshift bursts may be from the super-conducting cosmic strings, has been tightly constrained (Wang et al. 2011).
it was already known that (1) the coalescence of two compact objects can produce either long or short GRBs, depending on the remnant formed in the merger (a short burst is likely if the remnant is a stellar black hole, while a long burst is expected if the remnant is a super-massive neutron star; see Kluźniak & Ruderman 1998, and references therein); and (2) the collapse of a massive star usually produces long GRBs, but the possibility of generating short events cannot be ruled out (Zhang et al. 2003; Fan et al. 2005). One may appeal to multiple observational criteria to judge the correct physical category of the GRB progenitor model that is associated with a certain GRB (e.g., Zhang et al. 2009; Fan et al. 2005; Kann et al. 2011).

Recently, Goldstein et al. (2010) found that the distribution of the $E_{\text{peak}}/\text{Fluence}$ energy ratio has a clear bimodality by analyzing the complete BATSE 5B spectral catalog. An obvious distinction between long and short bursts emerges from this bimodal distribution. This result was further confirmed by an analysis of 382 GRBs from the GBM spectral catalog (Goldstein et al. 2011). Another phenomenological classification method for GRBs was proposed by Lü et al. (2010).

It is urgent to discuss the classification issues further in the Fermi era. The preliminary analysis results of GRBs observed by Fermi-GBM presented by, e.g., Bissaldi et al. (2011), Nava et al. (2011a, hereafter N11), and Shao et al. (2011) confirmed the duration bimodality found in the BATSE data (Kouveliotou et al. 1993). Whether the hardness–duration correlation is also consistent with the BATSE result and the short/hard–long/soft dichotomy classification scheme is robust have not been explored yet. In this paper, we present a systematic analysis of the temporal and spectral properties of Fermi-GBM GRBs cataloged by N11 and analyze the intrinsic energy correlation of GRBs with measured redshift and well-defined peak energy. This paper is structured as follows. The data and sample are presented in Section 2. In Section 3, we revisit the distribution of duration, the correlation between hardness and duration, the distribution of energy ratio, and the intrinsic energy correlation. In Section 4, we give a summary.

2. DATA AND SAMPLE

The Fermi-GBM detected 438 GRBs by the end of 2010 March. The spectral properties of these GRBs have been analyzed and published by N11. Out of the 432 GRBs for which it was possible to perform the spectral analysis, 323 bursts have curved spectra that are well fitted by the Band (Band et al. 1993) or by a cutoff power-law (CPL) model. The remaining 109 bursts are best fitted with a simple power law. In addition, the peak flux spectra of 235 bursts could be extracted and fitted with a Band or a CPL model. The detailed data extraction and analysis can be found in the catalog by N11, which we adopted in the following analysis. Recently, the first two-year Fermi-GBM GRB catalog was released (see Paciesas et al. 2012; Goldstein et al. 2012). The duration ($T_{90}$) of 487 GRBs is reported in the catalog. Combined with the duration data, we separate the 427 GRBs with an analyzed spectrum into different samples (five cases are not included for lack of $T_{90}$ data): 322 GRBs with the curved spectra (Band or CPL model) represent sample 1, while 103 GRBs with the power-law spectra represent sample 2. Furthermore, the 234 GRBs with a fitted peak flux spectrum represent sample 3 (one burst without $T_{90}$ data is excluded).

To analyze the intrinsic energy correlation of the different GRB classes, we collect the GRBs with known redshift and well-defined peak energy up to the end of 2011 May. This sample includes 110 long GRBs and 7 short GRBs detected by BeppoSAX, HETE-2, Swift, Suzaku, and Fermi. Most of the data are taken from Amati et al. (2008, 2009), Nava et al. (2008), Ghirlanda et al. (2009, 2010), and references therein, as well as the GRB Coordinates Network (GCN). The isotropic gamma-ray energy ($E_{\text{iso}}$) and luminosity ($L_{\text{iso}}$) are calculated in the rest frame in the energy range 1–10,000 keV.

3. TEMPORAL AND SPECTRAL ANALYSIS

3.1. Duration and Hardness

Distribution of duration is crucial for the traditional GRB classification. We analyze the distribution of durations of Fermi GRBs in the N11 catalog in detail. As shown in Figure 1, the duration distributions are bimodal either for all the bursts or for samples 1 and 2. The “short” and “long” GRBs are well separated in the log-normal plot, which is consistent with the previous findings (e.g., Bissaldi et al. 2011; N11; Shao et al. 2011). For all the GRBs in N11, we find a central value $\mu_1 = -0.23$ (i.e., $T_{90} \sim 0.59$ s; with a standard deviation $\sigma_1 = 0.47$) and $\mu_2 = 1.42$ (i.e., $T_{90} \sim 26.3$ s; with a standard deviation $\sigma_2 = 0.47$) for short and long bursts, respectively. For sample 1 and sample 2, the best fits yield $\mu_1 = -0.36$ ($T_{90} \sim 0.44$ s; $\sigma_1 = 0.46$) and $\mu_2 = 1.47$ ($T_{90} \sim 29.5$ s; $\sigma_2 = 0.47$) and $\mu_1 = -0.23$ ($T_{90} \sim 0.59$ s; $\sigma_1 = 0.22$) and $\mu_2 = 1.04$ ($T_{90} \sim 11$ s; $\sigma_2 = 0.57$), respectively. These results show that the duration bimodality is not affected by the spectral shape of GRBs, but the duration central value of long bursts in sample 2 is shifted to smaller value and the duration distribution covers a smaller range (see the middle panel of Figure 1). In other

\[ E_{\text{peak}}/\text{Fluence} \]

Figure 1. Distributions of the durations for 322 GRBs with the curved spectra (sample 1, top panel), 103 GRBs with the power-law spectra (sample 2, middle panel), and all 425 GRBs (bottom panel) observed by Fermi. The solid lines show the best fits with two log-normal functions, and the dashed vertical line is 2 s separation line. The $T_{90}$ data are taken from Paciesas et al. (2012).

\[ \text{Number} \]

\[ \log (T_{90}) \text{[s]} \]

\[ 0 \quad 20 \quad 40 \quad 60 \quad 80 \quad 100 \]

\[ 0 \quad 50 \quad 100 \quad 150 \quad 200 \quad 250 \]

\[ -2 \quad -1 \quad 0 \quad 1 \quad 2 \quad 3 \]

\[ \text{log} (T_{90}) \text{[s]} \]

\[ 0 \quad 20 \quad 40 \quad 60 \quad 80 \quad 100 \]

\[ 0 \quad 50 \quad 100 \quad 150 \quad 200 \quad 250 \]

\[ -2 \quad -1 \quad 0 \quad 1 \quad 2 \quad 3 \]

\[ \text{log} (T_{90}) \text{[s]} \]
words, on average, the duration of long GRBs with power-law spectrum is smaller than that of GRBs with curved spectrum. It is well known that the duration strongly depends on the sensitivity and the energy range of the instrument. The bimodal distribution of duration is either a robust result or an instrument selection effect. Using the data of GRBs simultaneously detected by Swift-BAT and Fermi-GBM, Virgili et al. (2011) found that the duration distributions in the BAT and GBM bands are all bimodal. It is essential to make a more detailed study explaining the fact that the bimodal duration distribution is not presented in observations of HETE-2 and Swift. The future work is going to explore it. We also adopt the conventional $T_{90} = 2\,\text{s}$ to separate short and long GRBs.

The spectral hardness is an additional discriminator for the classification of GRBs. In this work, we first explore the correlation between HR and $T_{90}$, where HR defines the fluence ratio between two broad energy bands. We simply divide the GBM energy band (10–1000 keV) into five energy bands, i.e., 10–25, 25–50, 50–100, 100–300, 300–1000 keV. Using the spectral data in N11, we are able to calculate HR in two arbitrary energy bands. We define four different HR measurements, namely, HR1, between the 50–100 keV and the 25–50 keV energy bands, i.e., the typical BAT energy bands; HR2, between the 100–300 keV and the 50–100 keV energy bands, i.e., the typical BATSE energy bands; HR3, between the 300–1000 keV and the 10–300 keV energy bands; and HR4, between the 100–1000 keV and the 25–100 keV energy bands.

We find that the values of HR are significantly different in these energy bands. This is expected, since they strongly depend on the energy bands between which they are calculated. Figure 2 shows HR versus $T_{90}$ for 425 GRBs from N11. From this figure, we find that there is an obvious tendency that short GRBs have harder spectra than long GRBs. The correlations between HR and $T_{90}$ are reported in Table 1. We find that (1) for all 425 GRBs, HR and $T_{90}$ are all anti-correlated for all choices of HR (HR1–HR4), but the correlation coefficients as well as the slopes are different; (2) the values of HR are larger and the HR–$T_{90}$ anti-correlation is stronger in the typical BATSE energy bands (the median value of HR is 2.21, the correlation coefficient is $r = -0.41$, the chance probability is $p = 2.8 \times 10^{-18}$, and the slope is $b = -0.12$) than those in the BAT energy bands (the median value of HR is 1.56, $r = -0.28$, $p = 5.2 \times 10^{-9}$, and $b = -0.06$); and (3) if we consider short and long GRBs separately, the correlations are very weak or even negligible.

In addition, the question arises whether the HR–$T_{90}$ anti-correlation of GRBs depends on spectral shapes. For a comparison with the previous results from the BASTE and BAT observations, the correlations between HR1 and $T_{90}$ and between HR2 and $T_{90}$ for sample 1 and sample 2 are investigated. The results are shown in Figure 3 and Table 1. We find that the anti-correlation between HR and $T_{90}$ indeed depends on the spectral shape of GRBs, and the GRBs with the curved spectra have a clearer correlation than those with the power-law spectra in the same energy bands (for a detailed analysis, see Table 1). Now, the fact that there is no obvious correlation between HR and $T_{90}$ in the Swift-BAT sample, as well as other samples detected by instruments with a narrow/softer energy bandpass such as HETE-2 (Sakamoto et al. 2011), can be easily understood. This is because (1) the HR–$T_{90}$ anti-correlation depends on the energy bands, and the correlation in the typical BAT energy bands is weak; (2) the majority of spectra of BAT GRBs are best fitted by a single power-law model. This is due to the fact that BAT only covers a narrow energy band. The HR–$T_{90}$ anti-correlation for GRBs with the power-law spectra is not obvious; and (3) for a given GRB sample, the values of HR are small and the values of $T_{90}$ are large for a BAT-like softer detector, which makes the HR–$T_{90}$ anti-correlation unclear.
The peak energy and spectral index are also usually adopted to depict the hardness of GRBs. N11 found that, on average, short GRBs have a higher peak energy (~900 keV) and a harder low-energy spectral index (~−0.50) than long GRBs (~160 keV and ~−0.92). We analyze the correlations between $E_{\text{peak}}$ (peak energy in the time-integrated spectra) and $T_{90}$ and between $E_{\text{peak}}^p$ (peak energy in the peak flux spectra) and $T_{90}$ for sample 1, and between $\alpha$ (which represents the spectral index of GRBs best fitted with a power-law model) and $T_{90}$ for sample 2. The results are shown in Figures 4 and 5. We find that $E_{\text{peak}}$ and $T_{90}$, $E_{\text{peak}}^p$ and $T_{90}$, $\alpha$ and $T_{90}$ are all anti-correlated. The detailed correlation analysis is presented in Table 2. The fact that short GRBs have harder spectra and long GRBs have softer spectra is confirmed once again. Recently, Gruber et al. (2011) suggested that the rest-frame peak energy distributions might be the same for the two classes of GRBs based on a small Fermi GRB sample with measured redshift. The different redshift distribution of the two classes of GRBs might be responsible for the different distributions of the observed peak energies (see, e.g., Guetta & Piran 2005). However, we also should note that the redshift distribution that has been found to be different for long and short GRBs might have been strongly affected by the measurement methods. Short GRBs tend to have lower redshift, very similar to those of long GRBs measured by the same method, i.e., spectral analysis of the presumed host galaxies (Shao et al. 2011). Therefore, the distribution of the intrinsic peak energy of the two classes of GRBs and the $E_{\text{peak}}$–$T_{90}$ anti-correlation are needed to further confirm. Moreover, for the short and long classes separately, the $E_{\text{peak}}$–$T_{90}$, $E_{\text{peak}}^p$–$T_{90}$, and $\alpha$–$T_{90}$ anti-correlations do not exist or even are positive correlated. These results are consistent with what was found from the analysis of the correlation between HR and $T_{90}$. Our results indicate that HR, peak energy, and spectral index might be linked to the same physical feature of GRBs. The nature is unknown so far.

### 3.2. Distribution of Energy Ratio

Although the distributions of hardness and duration can be used to classify GRBs, the overlap between these two classes of GRBs cannot be ignored. Moreover, this scheme strongly relies on the subjective choices required for the duration calculation. Recently, Goldstein et al. (2010) showed that the $E_{\text{peak}}$/Fluence energy ratio (which physically represents a ratio of the energy at which most of the gamma rays are emitted to the total energy emitted in gamma rays) can be used as a new GRB classification discriminator. This also has the big advantage that it does not rely on the burst duration estimate. Using the preliminary duration and spectral result of 382 Fermi-GBM GRBs, Goldstein et al. (2011) analyzed the distribution of energy ratio and found that the distribution separated into long bursts and short bursts well. This supports the original claim obtained by Goldstein et al. (2010). Meanwhile, we also analyze the distribution of the energy ratio for sample 1. The fluence in the 10–1000 keV energy band is calculated by using the spectral

| Data | Number | HR | $a$  | $b$  | $r$  | Probability |
|------|--------|----|------|------|------|-------------|
| All  | 425    | HR1| 0.27 | ±0.01| −0.06| ±0.01       | 0.28 | 5.2 $\times$ 10$^{-9}$ |
| All  | 425    | HR2| 0.47 | ±0.02| −0.12| ±0.01       | 0.41 | 2.8 $\times$ 10$^{-18}$ |
| All  | 425    | HR3| −0.15| ±0.05| −0.29| ±0.04       | 0.42 | 6.2 $\times$ 10$^{-20}$ |
| All  | 425    | HR4| 0.68 | ±0.03| −0.25| ±0.02       | 0.44 | 3.0 $\times$ 10$^{-21}$ |
| Short| 77     | HR1| 0.30 | ±0.02| −0.08| ±0.04       | 0.22 | 0.06 |
| Short| 77     | HR2| 0.52 | ±0.02| −0.09| ±0.05       | 0.13 | 0.25 |
| Short| 77     | HR3| 0.03 | ±0.06| −0.09| ±0.13       | 0.04 | 0.74 |
| Short| 77     | HR4| 0.82 | ±0.04| −0.09| ±0.10       | 0.03 | 0.81 |
| Long | 348    | HR1| 0.19 | ±0.02| −0.02| ±0.01       | 0.03 | 0.56 |
| Long | 348    | HR2| 0.35 | ±0.03| −0.05| ±0.02       | 0.11 | 0.03 |
| Long | 348    | HR3| −0.43| ±0.11| −0.11| ±0.07       | 0.14 | 0.009 |
| Long | 348    | HR4| 0.46 | ±0.06| −0.10| ±0.04       | 0.15 | 0.007 |
| S1 All| 322   | HR1| 0.33 | ±0.01| −0.09| ±0.01       | 0.44 | 8.4 $\times$ 10$^{-17}$ |
| S2 All| 103   | HR1| 0.16 | ±0.01| −0.05| ±0.01       | 0.55 | 1.5 $\times$ 10$^{-9}$ |
| S1 All| 322   | HR2| 0.49 | ±0.02| −0.14| ±0.02       | 0.36 | 2.2 $\times$ 10$^{-11}$ |
| S2 All| 103   | HR2| 0.42 | ±0.01| −0.07| ±0.01       | 0.55 | 1.5 $\times$ 10$^{-9}$ |
| S1 Short| 47    | HR1| 0.39 | ±0.02| −0.02| ±0.04       | 0.09 | 0.56 |
| S2 Short| 30    | HR1| 0.19 | ±0.01| 0.02  | ±0.03       | 0.16 | 0.40 |
| S1 Short| 47    | HR2| 0.59 | ±0.04| −0.07| ±0.07       | 0.05 | 0.72 |
| S2 Short| 30    | HR2| 0.45 | ±0.01| 0.02  | ±0.03       | 0.16 | 0.40 |
| S1 Long| 275   | HR1| 0.26 | ±0.03| −0.05| ±0.02       | 0.18 | 0.003 |
| S2 Long| 73    | HR1| 0.13 | ±0.02| −0.03| ±0.02       | 0.20 | 0.09 |
| S1 Long| 275   | HR2| 0.32 | ±0.04| −0.03| ±0.03       | 0.07 | 0.23 |
| S2 Long| 73    | HR2| 0.38 | ±0.03| −0.04| ±0.02       | 0.20 | 0.09 |

**Notes.**
- a: The hardness ratios (HR) are measured between two different energy bands, namely HR1, between the 50–100 keV and the 25–50 keV energy bands; HR2, between the 100–300 keV and the 50–100 keV energy bands; HR3, between the 300–1000 keV and the 50–100 keV energy bands; HR4, between the 100–1000 keV and the 25–100 keV energy bands.
- b: S1 represents sample 1 (316 GRBs with the curved spectra) and S2 represents sample 2 (108 GRBs with the power-law spectra).

The fluence in the peak–$T_{90}$ anti-correlation are needed to further confirm. Moreover, for the short and long classes separately, the $E_{\text{peak}}$–$T_{90}$, $E_{\text{peak}}^p$–$T_{90}$, and $\alpha$–$T_{90}$ anti-correlations do not exist or even are positive correlated. These results are consistent with what was found from the analysis of the correlation between HR and $T_{90}$. Our results indicate that HR, peak energy, and spectral index might be linked to the same physical feature of GRBs. The nature is unknown so far.
parameters in N11, then we obtain the values of $E_{\text{peak}}$/fluence for each of GRBs in sample 1. Figure 6 shows the distribution of the energy ratio. In the top panel, we plot the 316 GRBs included in our sample 1. A bimodal distribution is evident, as previously shown by Goldstein et al. (2011). By using a standard nonlinear least-squares fitting algorithm, we fit the distribution by two log-normal functions. The best fits yield a central value $\mu_1 = -1.34$ with a standard deviation $\sigma_1 = 0.62$, and $\mu_2 = 0.27$ with $\sigma_2 = 0.35$, respectively. In the bottom panel of Figure 6, we present two distributions corresponding to long (unfilled histogram) and short (filled histogram) GRBs. This further confirms the fact that (1) the bimodality of the energy ratio distribution is correlated to that of the burst duration and that (2) the energy ratio is indeed a good discriminator for classifying GRBs. Indeed, it could be used to identify some of the controversial GRBs previously discussed (see Section 3.3).

The energy ratio bimodality can also be easily understood if we note that short GRBs tend to have larger peak energies and smaller fluences (due to their short durations) with respect to the long ones.

To further check the differences between long and short GRBs, we investigate the correlations between the peak flux ($P$) and $T_{90}$ and between the $E_{\text{peak}}^p/P$ ratio (which physically represents a ratio of the energy at which most of the gamma rays are emitted to the total energy emitted in gamma rays in one second at peak of a burst) and $T_{90}$. Those two quantities namely do not depend on the duration of a burst. The detailed results are presented in Figure 7 and Table 2. Both the correlations between $P$ and $T_{90}$ and between $E_{\text{peak}}^p/P$ and $T_{90}$ (shown in the top and bottom panel of Figure 7, respectively) are different for long and short GRBs. An anti-correlation between $P$ and $T_{90}$ and a positive correlation between $E_{\text{peak}}^p/P$ and $T_{90}$ are found for all 234 GRBs with the peak flux curved spectra, although the correlations are not very strong. Likewise, if we consider short and long classes separately, the correlations are negligible or even reversed. This further confirms that the correlation between the hardness and the duration of GRBs is only a general trend between two clusters of GRBs or two types of GRBs and does not apply to either type.

### 3.3. Intrinsic Spectral Energy Correlation

Amati et al. (2002) found a tight correlation between the rest-frame peak energy, $E_{\text{p,rest}}$, and the isotropic equivalent gamma-ray energy, $E_{\text{iso}}$, which was confirmed by later observations (Amati 2006, 2010). However, short GRBs do not follow the correlation, as is true for the peculiarly sub-energetic and close GRB 980425, the prototype of the GRB/SN connection (e.g., Amati 2006, 2010; Piranomonte et al. 2008; Ghirlanda et al. 2009; Gruber et al. 2011). These facts suggest that the $E_{\text{p,rest}}-E_{\text{iso}}$ plane may be used to distinguish between different classes of GRBs and to understand the differences in the physics/geometry of their emission. Here we reanalyze this correlation taking into account the new observational data. Only...
seven short GRBs with redshift, reliable estimate of $E_{\text{peak}}$, and other spectral parameters are available by the end of 2011 May, as listed in Table 3.

The three peculiar/controversial short GRBs (GRBs 071227, 090927, and 100816A; Piranomonte et al. 2008; Amati 2010; Gruber et al. 2011) are excluded for the following reasons. Caito et al. (2010) suggested that GRB 071227 represents another example of a disguised short GRB, after GRB 970228 and GRB 060614, on the basis of their analysis performed in the context of the fireshell scenario. GRB 090927 and GRB 100816A are two short GRBs detected by Fermi and had been analyzed by Gruber et al. (2011). However, the spectrum of GRB 090927 is adequately fitted by a simple power-law function (see Gruber et al. 2009; Nava et al. 2011), which has been confirmed by our current analysis. The category of this GRB hence cannot be further identified due to its inaccurate peak energy measurement. GRB 100816A was simultaneously detected by Swift-BAT, Fermi-GBM, and Konus-Wind, and its duration estimated by these three missions is $2.9 \pm 0.6$ s (15–350 keV), 2 s (50–300 keV), and $\sim 2.8$ s (20 keV–2 MeV), respectively. So it is difficult to determine whether this GRB belongs to the short or to the long class only based on its duration. Fan & Wei (2011) identified a possible wind-like medium surrounding this burst, which suggested a massive star origin (i.e., this
short-like GRB should be a long one). Moreover, this GRB does not deviate from the $E_{\text{p,rest}}$-$E_{\text{iso}}$ region of long GRBs (see also Gruber et al. 2011). We calculate the energy ratio and obtain $\log(E_{\text{p,rest}}/\text{Fluence}) = -1.24$ for GRB 100816A, which is a typical value of long GRBs. Therefore, this event should belong to the long class and has been included in our long GRB sample.

We also collected GRBs observed by Fermi-GBM with the same standard as short GRBs analyzed above from the GCN. Twenty-seven GRBs (including two short ones listed in Table 3) are obtained, as listed in Table 4. Using the same calculation method as Amati et al. (2008), we obtain their isotropic equivalent energies in the energy range 1–10,000 keV (in the bursts’ rest frame). Figure 8 shows the correlation between $E_{\text{p,rest}}$ and $E_{\text{iso}}$. Data reported in Amati (2010) and references therein are also included. We find that the short GRBs are significantly different from the long ones. To obtain a quantitative comparison, we fit the $E_{\text{p,rest}}$-$E_{\text{iso}}$ correlations for the short and long GRBs separately. The best fits yield

$$E_{\text{p,rest}} = 2455 \times \left( \frac{E_{\text{iso}}}{10^{52}} \right)^{0.59\pm0.04}$$

for short GRBs, with a Spearman’s rank correlation coefficient $r = 0.89$ and a chance probability $P = 6.8 \times 10^{-3}$, and

$$E_{\text{p,rest}} = 100 \times \left( \frac{E_{\text{iso}}}{10^{52}} \right)^{0.51\pm0.03}$$

for long GRBs, with $r = 0.85$ and $P = 1.2 \times 10^{-31}$ (see Table 2). For long GRBs, the result is in agreement with that obtained by some authors (e.g., Amati 2010; Ghirlanda et al. 2009, 2010; Gruber et al. 2011).

Wei & Gao (2003) discovered a tight correlation between the rest-frame peak energy and the luminosity ($L_{\text{iso}}$) based on nine GRBs (see their Figure 6). Such a correlation was soon
confirmed by others (e.g., Yonetoku et al. 2004). Recently, further studies showed that although short GRBs are inconsistent with the $E_{\text{p,rest}}-L_{\text{iso}}$ correlation hold by long GRBs, they might follow the $E_{\text{p,rest}}-L_{\text{iso}}$ correlation (e.g., Ghirlanda et al. 2009; Gruber et al. 2011). Such a trend has been confirmed by our analysis with the latest data7 (see Figure 9). The fit to the $E_{\text{p,rest}}-L_{\text{iso}}$ correlation yields

$$E_{\text{p,rest}} = 302 \times \left( \frac{L_{\text{iso}}}{10^{52}} \right)^{0.40 \pm 0.03} \text{ keV},$$

with $r = 0.76$ and $P = 2.3 \times 10^{-23}$. This might imply that the energy dissipation processes powering the prompt gamma-ray emission of short and long GRBs are rather similar, though the progenitors of these two kinds of events are likely different.

### 4. SUMMARY

In this work, we perform a statistical analysis of the temporal and spectral properties of the latest Fermi-GBM-GRBs cataloged by N11 to revisit the classification of GRBs. The traditional short/hard and long/soft classification is supported for these Fermi GRBs by the following facts: (1) the duration of the prompt gamma-ray emission has a clear bimodal distribution. (2) The energy ratio (i.e., $E_{\text{peak}}/\text{Fluence}$) also has a clear

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**Table 3**

| GRB      | $z^a$ | $\alpha$ | Peak Flux Range | $L_{\text{iso}}$ (10$^{52}$ erg s$^{-1}$) | $E_{\text{p,rest}}$ (keV) | Fluence (10$^{-5}$) | Range (keV) | $E_{\text{iso}}$ (10$^{52}$) | Reference |
|----------|-------|----------|-----------------|------------------------------------------|----------------------------|-------------------|-------------|----------------------------|--------|
| 050709   | 0.16  | $-0.53 \pm 0.12$ | $5.1 \pm 0.5E-6$ | 2–400                                    | 0.05 ± 0.01                | 97.4 ± 11.6      | 2–400       | 0.0033 ± 0.0001            | 1      |
| 051221   | 0.5465| $-1.08 \pm 0.13$ | $4.6 \pm 1.3E-5$ | 20–2000                                  | 6.42 ± 0.56                | 620 ± 186         | 20–2000     | 0.3 ± 0.04                 | 1      |
| 061006   | 0.4377| $-0.62 \pm 0.2$  | $2.1E-5$        | 20–2000                                  | 1.78 ± 0.23                | 955 ± 267         | 20–2000     | 0.2 ± 0.03                 | 1      |
| 070714   | 0.92  | $-0.86 \pm 0.1$  | $2.8 \pm 0.3$   | 100–1000                                  | 1.4 ± 0.1                  | 2150 ± 1113       | 15–2000     | 1.1 ± 0.1                  | 1      |
| 090510   | 0.903 | $-0.80 \pm 0.03$ | $80$            | 8–40000                                   | 13.1 ± 0.87                | 8370 ± 760        | 8–40000     | 3.75 ± 0.25                | 2      |
| 100117A  | 0.92  | $-0.14_{-0.31}^{+0.33}$ | $6.1 \pm 0.4$ | 8–10000                                  | 0.41 ± 0.05                | 551 ±142          | 8–10000     | 0.09 ± 0.01                | 3      |
| 101219A  | 0.718 | $-0.22_{-0.25}^{+0.30}$ | $2.8 \pm 0.8E-6$ | 20–10000                                  | 3.78 ± 1.08                | 84_{277}^{+363}   | 20–10000    | 0.49 ± 0.07                | 4      |
| 071227 b | 0.383 | $-0.7$    | $3.5 \pm 1.1E-6$ | 20–1300                                  | 0.25 ± 0.08                | 1384 ± 277        | 20–1300     | 0.1 ± 0.02                 | 5      |

Notes.

* The redshifts are taken from Greiner’s Web site (http://www.mpe.mpg.de/~jcg/grbgen.html).

* Some authors suggested that this GRB is a disguised short one as GRB 060614 (e.g., Caito et al. 2010).

References. (1) Ghirlanda et al. 2008; (2) Guiriec et al. 2009; (3) Paciesas 2010; (4) Golenetskii et al. 2010; (5) Golenetskii et al. 2007.
bimodal distribution and its bimodality is correlated to that of the duration distribution. (3) The anti-correlation between spectral hardness (HR, peak energy, and spectral index) and duration is also confirmed. Moreover, we find out that the correlation between the hardness and the duration is only a general trend between two clusters of GRBs or two types of GRBs and does not apply to either type. Interestingly, there are two leading models for GRBs. One is the collapsar that likely produces long-lasting GRBs. The other is the merger of two compact objects, which is expected to power short-living GRBs. However, it is not always reasonable to argue a collapsar origin for long bursts and a merger origin for short bursts since the possibilities that the collapsar can also produce short GRBs and the merger can generate long GRBs cannot be ruled out, as already realized in the pre-Swift era (e.g., Kluźniak & Ruderman 1998; Zhang et al. 2003; Fan et al. 2005). The observations of some Swift GRBs, such as GRB 060614 and GRB 080503 (e.g., Xu et al. 2009), partly confirm such speculations. Therefore, additional discriminators are highly needed to classify GRBs reliably.

In this work we also find that the anti-correlation between HR and duration depends on the spectral shapes of GRBs and the energy bands. The bursts with the curved spectra in the typical BATSE energy bands (between the 100–300 keV and the 50–100 keV bands) show a tighter anti-correlation than those with the power-law spectra in the typical BAT energy bands (between the 50–100 keV and the 25–50 keV bands). This might explain why the HR–$T_{90}$ correlation is not evident for the Swift-BAT GRB sample, as well as other GRB samples.
detected by instruments with a narrow/softer energy bandpass such as HETE-2 (e.g., Sakamoto et al. 2011; Shao et al. 2011).

Table 4
The Spectral Parameters of 27 Fermi-GBM GRBs with Known Redshifts and Well-measured Peak Energies

| GRB     | $z$  | $\alpha$ | $\beta$ | $E_{\text{peak}}$ (keV) | $\frac{E_{\text{iso}}}{10^{52}}$ (erg) | $L_{\text{iso}}$ (10$^{52}$ erg) | GCN Number |
|---------|------|----------|---------|-------------------------|----------------------------------|---------------------------------|------------|
| 080810A | 0.35 | $-0.91 \pm 0.12$ | ...     | 313.5 $\pm$ 73.6       | 6.9 $\pm$ 0.5                    | 50–300                           | 8100       |
| 080916A | 0.689| $-0.9 \pm 0.1$   | ...     | 109 6 9                  | 15 $\pm$ 5                    | 25–1000                          | 8263       |
| 080916C | 4.35 | $-0.91 \pm 0.02$ | ...     | 424 $\pm$ 24           | 190                             | 8–30000                          | 8278       |
| 081007  | 0.5295| $-1.4 \pm 0.4$   | ...     | 40 $\pm$ 10           | 1.2 $\pm$ 1.4                  | 25–9000                          | 8369       |
| 081222  | 2.77 | $-0.55 \pm 0.07$ | ...     | 134 $\pm$ 9           | 13.5 $\pm$ 0.8                 | 8–10000                          | 8715       |
| 090323  | 3.57 | $-0.89 \pm 0.03$ | ...     | 697 $\pm$ 51           | 100 $\pm$ 1                    | 8–10000                          | 9035       |
| 090328  | 0.736| $-0.93 \pm 0.02$ | ...     | 653 $\pm$ 45           | 80.9 $\pm$ 1                   | 8–10000                          | 9057       |
| 090423  | 8.26 | $-0.77 \pm 0.35$ | ...     | 82 $\pm$ 15            | 1.1 $\pm$ 0.3                  | 8–10000                          | 9229       |
| 090424  | 0.544| $-0.9 \pm 0.02$  | ...     | 177 $\pm$ 3           | 52 $\pm$ 1                     | 8–10000                          | 9230       |
| 090510a | 0.903| $-0.8 \pm 0.03$  | ...     | 4400 $\pm$ 400        | 30 $\pm$ 2                     | 8–40000                          | 9336       |
| 090516  | 4.109| $-1.51 \pm 0.11$ | ...     | 226 $\pm$ 11           | 1.7 $\pm$ 1.1                  | 50–10000                         | 9415       |
| 090618  | 0.54 | $-1.26^{+0.06}_{-0.02}$ | ...     | 155.5$^{+11.1}_{-10.5}$ | 270 $\pm$ 6                   | 8–10000                          | 9535       |
| 090902B | 1.822| $-0.70 \pm 0.06$ | ...     | 341 $\pm$ 4            | 145 $\pm$ 4                    | 8–10000                          | 9933       |
| 090926a | 2.1062| $-0.75 \pm 0.01$ | ...     | 22.2 $\pm$ 9           | 8.7 $\pm$ 3.2                  | 10–10000                         | 9957       |
| 091003a | 0.8969| $-1.13 \pm 0.01$ | ...     | 486.2 $\pm$ 23.6       | 37.6 $\pm$ 0.4                 | 8–10000                          | 9983       |
| 091020  | 1.71 | $-1.2 \pm 0.4$    | ...     | 47.9 $\pm$ 7.1         | 10 $\pm$ 2                     | 8–10000                          | 10095      |
| 091127  | 0.49 | $-1.27 \pm 0.06$ | ...     | 36 $\pm$ 2            | 18.7 $\pm$ 0.2                 | 8–10000                          | 10204      |
| 091208a | 1.063| $-1.48^{+0.05}_{-0.05}$ | ...     | 144.2$^{+18.2}_{-13.9}$ | 5.8 $\pm$ 0.2                  | 8–10000                          | 10266      |
| 10017A  | 0.92 | $-0.14^{+0.33}_{-0.27}$ | ...     | 287$^{+74.9}_{-50}$     | 9.0 $\pm$ 4.1                  | 8–10000                          | 10345      |
| 10041A  | 1.368| $-0.58 \pm 0.01$ | ...     | 627.6$^{+12.5}_{-12.1}$ | 129 $\pm$ 2                   | 8–10000                          | 10595      |
| 10072B  | 2.106| $-0.9 \pm 0.1$   | ...     | 131 $\pm$ 15           | 2.4 $\pm$ 0.1                  | 8–10000                          | 11015      |
| 100814A | 1.44 | $-0.64^{+0.14}_{-0.12}$ | ...     | 106.4$^{+15.3}_{-12.6}$ | 19.8 $\pm$ 0.6                 | 10–10000                         | 10999      |
| 100816a | 0.8049| $-0.31 \pm 0.05$ | ...     | 136.7$^{+4.7}_{-1.7}$  | 3.0 $\pm$ 0.3                  | 10–10000                         | 11124      |
| 100906A | 1.727| $-1.34^{+0.08}_{-0.06}$ | ...     | 106$^{+7.5}_{-20.2}$    | 26.4 $\pm$ 0.3                 | 10–10000                         | 11248      |
| 101219B | 0.55 | $0.33 \pm 0.36$  | ...     | 70 $\pm$ 8            | 5.5 $\pm$ 0.4                  | 10–10000                         | 11477      |
| 110213A | 1.46 | $-1.44 \pm 0.05$ | ...     | 98.4$^{+6.9}_{-6.6}$    | 10.3 $\pm$ 0.3                 | 10–10000                         | 11727      |

Notes. The redshifts are taken from Greiner’s Web site.

\* Two short GRBs.
\* This GRB was classified as a short one by the previous study (e.g., Gruber et al. 2011); we find that it should belong to the long class.

Figure 8. Correlations between the rest-frame peak energy ($E_{\text{peak}}$) and the isotropic total energy ($E_{\text{iso}}$). The squares represent the short GRBs, the triangles represent pre-Fermi long GRBs taken from Amati (2010) and references therein, and the circles represent Fermi long GRBs listed in Table 4. The stars are the two controversial GRBs: GRB 071227 and GRB 100816A. The solid lines are the best-fit correlations: $E_{\text{peak}} = 2455 \times (E_{\text{iso}}/10^{52})^{0.59}$ for short GRBs and $E_{\text{peak}} = 100 \times (E_{\text{iso}}/10^{52})^{0.51}$ for long GRBs.

(A color version of this figure is available in the online journal.)

Figure 9. Correlation between the rest-frame peak energy ($E_{p, \text{rest}}$) and the isotropic peak luminosity ($L_{\text{iso}}$), where the 105 long GRB data are taken from Ghirlanda et al. (2010) and references therein. The other symbols are the same as Figure 8. For combined short and long GRBs, the best fit to the $E_{p, \text{rest}}$-$L_{\text{iso}}$ correlation yields $E_{p, \text{rest}} = 302 \times (L_{\text{iso}}/10^{52})^{0.54 \pm 0.03}$.

(A color version of this figure is available in the online journal.)

We also analyze the intrinsic energy correlation for the different GRB classes and find that all short GRBs deviate significantly from the $E_{p, \text{rest}}$-$E_{\text{iso}}$ correlation hold by long GRBs, and they
might follow another one,
\[ E_{p, \text{rest}} = 2455 \times (E_{\text{iso}}/10^{52})^{0.59} \]

based on the current small sample. Future observations will test our result.

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