Review

The Material Indices Method in the Sustainable Engineering Design Process: A Review

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Abstract: The material indices method has its application in both the design of construction materials and products. The method has evolved since the 1960s and has been described in German, Russian, Polish, and English scientific literature. In the 1990s, the method was adapted to Design for the Environment with the inclusion of specific energy consumption indicators for various construction materials. The article cites six principles of Design for the Environment and presents specific energy consumption indicators according to various authors. This data was then used in two sample applications of the material indices method to determine the specific energy consumption of product manufacture: of a support structure of the standing frame and a compression spring design. In the conclusions, the significant limitations of the material indices method are emphasized, which are not extensively discussed in the literature on the subject, such as its high sensitivity to the accuracy of the adopted energy consumption indicators for materials in view of the actual production process; not taking into consideration all the negative aspects of the materials’ impact on the environment, or the difficulties associated with predicting the impact of material production technology on the material indices. On the other hand, their simple functional form makes them ideal for incorporation into modern CAD software and in product optimization at the initial stage of concept design.

Keywords: engineering material selection; engineering design process; mechanical design; material indices; environmental impact

1. Introduction

The contemporary engineering design process takes into account the full life cycle of the object being designed. This includes its functions, manufacturability, and economic and environmental factors in the product’s life cycle analysis. Generally, the design process is oriented towards efficient and cost-effective use of resources to ensure a positive environmental effect; work safety and quality of life; adjustment and adaptation to market needs; operation and servicing with a tolerance to errors and risk; as well as the use of renewable resources [1–9]. Such an orientation established a trend for designing structures that fulfilling their functions and are light and often inexpensive at the same time or have a minimal effect on the environment, i.e., production using appropriate materials.

The main objective of this paper is to review the strategies of structural materials selection in mechanical design based on material indices found in the subject literature. These indicators are related to the volume, weight, cost, and environmental indicators of the construction material, thanks to which they take into account the whole life cycle of the designed product.
2. State of the Art in the Use of Material Indices in Mechanical Design

2.1. Evolution of Material Selection Methods in Engineering Design

The material indices method is used to perform a comparative quantitative estimation of various structural materials, taking into consideration the type of load. Every new engineering material can be characterized by calculating its indices and comparing these with those of currently used materials [10]. To the best of the authors’ knowledge, the material indices method has been created by professor Gustav Niemann in 1960 [11], who proposed that the selection of materials should be based on the comparison of volume, mass, and material cost of a given structural member. For example, in the Polish subject literature, when the fundamentals of machine design were referred to for the first time, the compactness index, material consumption index, and cost absorption were introduced in 1964 by professor Stanisław Kocańda [12]. Material indices were also used in 1968 by professor Pavel Orlov [13,14] for the comparison of stiffness, strength, and mass (Table 1) in the four cases of shapes of structural members: a—members of the same shape, demonstrating the same stresses under the same load that exists when a given material is replaced without geometrical changes (cross-sections arranged accordingly to process-related conditions under small stresses); b—members of the same stiffness, the same strains for different cross-sections and stresses; c—members of the same strength, i.e., the same margin of reliability for different cross-sections and stresses proportional to the short-term strength; d—members of the same mass. Cases b and c apply when a material is replaced by another one, and cross-sections of members are changed, with sufficiently accurate stress and strain calculations that are suitable to establish strength and stiffness for different cross-sections. Case d applies when mass is predefined based on the intended use of the member.

| Parameter | Parts with: |
|-----------|-------------|
|           | a) Similar Shapes | b) Equal Stiffness | c) Equal Strength | d) Equal Mass |
| Mass Q    | ρ            | ρ/E          | ρ/Rm        | constans     |
| Stiffness S | E            | constans    | E/Rm         | E/ρ          |
| Strength R = f (x, Fmax) | Rm            | Rm/E          | constans     | E/ρ          |
| Relative stiffness S/Q | Tension/compression | E/ρ          | Bending       | E^1/2/ρ      |
| Relative strength Fmax/R |                 |               |               | Torsion G^1/2/ρ |

In addition, a generalized strength–stiffness index R_e0.2/ρ that characterizes the ability of a member to withstand great loads with a small strain and mass was introduced in the aforementioned publication by Orlov. An extended and modified approach to material indices was provided by professor Witold Korewa in 1974 [15]. Table 2 shows the volume indices ν_v of bars during tension, bending, and torsion for three cases of limit load capacity (as regards the criteria of strength, stiffness, and elasticity).

Mass index c_q and material cost index c_k are determined based on the relationship:

\[ c_q = \frac{c_v}{\gamma} = \frac{c_q}{k} \]

While creating tables with ordered values of the indices for various materials, one must remember that an increase in the calculated values of the indices c_v, c_q, c_k leads to a proportional decrease in volume, mass, and material cost. The compilation of the tables requires the same geometrical values of the shape factor g_k and length factor g_l of the bar and load conditions w. For geometrically-similar bars
with the cross-section shape factor \( g_k = \text{const.} \), the bar length factor \( g_l = \text{const.} \) and the same loads \( F = \text{const.} \), the calculations are simplified.

### Table 2. Volume index \( uv \) of bars for various load capacity criteria as assumed by Korewa et al. in 1974 (source: [15]).

| Bar                  | Strength        | Stiffness       | Elasticity      |
|----------------------|-----------------|-----------------|-----------------|
|                      | \( c_v = m_v \times \frac{g_k}{g_1} \times g_l \) | \( c_v = m_v \times \frac{g_k}{g_1} \times g_l \times \frac{w}{l} \) | \( c_v = m_v \times \frac{g_k}{g_1} \times w \) |
| during tension/compression | \( F = \sigma_{\text{per}} \times 1 \times \frac{1}{l} \) | \( F = E \times 1 \times \frac{1}{l} \times f_{\text{dop}} \times w \) |
| during bending       | \( \frac{\rho_{\text{per}}}{w} = \frac{g_k}{g_1} \times \frac{1}{l} \times \frac{1}{\rho} \times \frac{1}{G_{\text{dop}}} \) | \( \left( W \cdot f_{\text{dop}} \right)^{1/2} \times \frac{\rho_{\text{per}}}{w} \times \frac{W}{G_{\text{dop}}} \times \frac{1}{n} \) |
| during torsion       | \( \frac{\rho_{\text{per}}}{w} = \frac{g_k}{g_1} \times \frac{1}{l} \times \frac{1}{\rho} \times \frac{1}{G_{\text{dop}}} \) | \( \left( W \cdot f_{\text{dop}} \right)^{1/2} \times \frac{\rho_{\text{per}}}{w} \times \frac{W}{G_{\text{dop}}} \times \frac{1}{n} \) |

\( n = 3 \) for a cantilever beam, \( n = 48 \) for a single-span beam with joint fastening, \( n = 192 \) for a single-span beam with rigid fastening.

Taking a beam subjected to bending as an example, when the beam load is determined by strength, beam volume for \( F \cdot g_k \cdot g_l = \text{const.} \) is \( V = (1/\sigma_{\text{per}} \cdot 2^{3/2}) \cdot \text{const.} \) \( 4 \) and its mass is \( Q = V \cdot \gamma = (\gamma/\sigma_{\text{per}} \cdot 2^{3/2}) \cdot \text{const.} \) \( 4 \) and its cost is \( K = Q \cdot k_j = (\gamma \cdot k_j / \sigma_{\text{per}} \cdot 2^{3/2}) \cdot \text{const.} \) \( 4 \). The quantity \( \text{const.} \) 4 has a fixed value in the set of the materials being compared. This means that the creation of relative standardized measures of material values (e.g., for score, or percentage measure relative to the best material) requires only the comparison of given material functions for the above-mentioned relationships in brackets (designated as \( c_v, c_f, c_k \)).

A major advantage of material indices is their simple functional form that can be easily used in practical applications during material selection. For instance, in previous publications by one of the authors of this paper in 1997 ([16, 17]), material indices were used as an aid during material selection using databases of CAD systems designed for optimization, design, and verification calculations of metal helical, flat, and disc springs. Each material was described by 25 quantitative attributes of elasticity, static, and fatigue strength. Material selection was performed in terms of the previously chosen descriptive classification criteria enabling qualitative coding (seven attributes, including technological properties and material cost) or quantitative coding. The assumed criteria of descriptive classification for a spring material are provided in Figure 1, whereas the format of the quantitative code according to the method of material indices developed by Gustav Niemann is presented in Figure 2.

The method of material indices devised by Gustav Niemann was developed in later studies of the Munich school of fundamentals of machine design. In the chapter devoted to lightweight structures in the recent edition of the book “Machine Elements” by Gustav Niemann, Hans Winter, and Bernd Robert Höhn [18], a synthesis of indices was made, together with updated data, including light metals and low-density plastic materials, materials of increased strength and moderate strains or higher wear resistance and fatigue strength. Table 3 presents a set of data relating to structural properties and costs (relative costs) for 21 materials in various forms: metal profiles, simple cast parts, as well as plastic and wood boards. The impact of a material on mass can be illustrated by the quantities of specific volume, strength, and stiffness (the greater the specific volume, the greater the mass):

- specific volume indicating the actual volume (mass) \( L_V = \frac{1}{\rho_{\text{per}}} \left( \frac{dm^3}{N} \right) \);  
- specific strength corresponding to the length of a fixed cross-section bar which breaks under its own weight \( L_R = \frac{E}{\rho_{\text{per}}} \) (km);  
- specific stiffness (elongation) when the deformation is predefined \( L_D = \frac{E}{\rho_{\text{per}}} \) (km).
Figure 1. Criteria of descriptive classification of spring materials in a CAD system for spring design in 1997 (source: [17]).

Figure 2. Quantitative code of the values (standardized in the 0–9 point scale) relating to volume, mass, and material cost of a spring (source [17]).

Table 3. Material and cost data for selected structural materials according to Niemann, Winter, and Höhn. (source: [18]).

| Material | E N/mm² | Rm N/mm² | LV dm³/N | LR km | LD km | Relative Prices |
|----------|---------|----------|----------|-------|-------|-----------------|
|          |         |          |          |       |       |                 |

Note: □ – means that the distinguishing item is irrelevant or unknown
Min CV, Min CQ, Min CK–criteria for volume V, mass Q, and material cost K
Table 3. Material and cost data for selected structural materials according to Niemann, Winter, and Höhn. (source: [18]).

| Material | \(\rho\) kg/dm\(^3\) | \(E\) N/mm\(^2\) | \(R_m\) N/mm\(^2\) | \(L_V\) dm\(^3\)/N | \(L_R\) km | \(L_D\) km | Relative Prices kg dm\(^3\) |
|----------|----------------------|----------------|-----------------|-----------------|---------|---------|---------------------|
| **Metal profiles:** | | | | | | | |
| 1 Steel S235 | 7.85 | 210,000 | 360 | 0.0130 | 4.7 | 2727 | 1.00 |
| 2 Steel E295 | 7.85 | 210,000 | 490 | 0.0130 | 6.4 | 2727 | 1.10 |
| 3 Spring steel Si-Mn | 7.85 | 210,000 | 1300 | 0.0130 | 16.5 | 2727 | 1.67 |
| 4 Pure aluminum (hard) Al | 2.70 | 71,000 | 140 | 0.0377 | 5.2 | 2681 | 1.60 |
| 5 Al-Cu-Mg-Pb | 2.85 | 73,000 | 370 | 0.0358 | 13.2 | 2611 | 1.05 |
| 6 Al-Mg 5 | 2.64 | 72,000 | 250 | 0.0386 | 9.7 | 2780 | 1.31 |
| 7 Mg-Al | 1.80 | 43,000 | 280 | 0.0566 | 15.9 | 2435 | 0.69 |
| 8 Titanium 99.7 | 4.50 | 105,000 | 350 | 0.0226 | 7.9 | 2378 | 31.7 |
| **Simple cast parts:** | | | | | | | |
| 9 EN-GJL-200 | 7.20 | 100,000 | 200 | 0.0141 | 2.8 | 1415 | 2.00 |
| 10 GS 45 | 7.85 | 215,000 | 450 | 0.0130 | 5.7 | 2792 | 4.00 |
| 11 Cast Al alloy | 2.65 | 70,000 | 220 | 0.0385 | 8.5 | 2693 | 0.95 |
| 12 Cast Mg alloy | 1.80 | 42,000 | 240 | 0.0566 | 13.6 | 2378 | 3.10 |
| **Plastic and wood boards:** | | | | | | | |
| 13 Hard PVC up to 55 °C | 1.38 | 3000 | 55 | 0.0739 | 4.0 | 221.6 | 3.33 |
| 14 Polystyrol up to 60 °C | 1.05 | 3200 | 75 | 0.0971 | 7.0 | 310.7 | 0.58 |
| 15 Polyamide up to 90 °C | 1.14 | 1700 | 60 | 0.0894 | 5.3 | 152.0 | 11.7 |
| 16 Polyester resin up to 70 °C with glass fibre (GFK) | 1.90 | 27,000 | 340 | 0.0536 | 18.0 | 1448.6 | 3.44 |
| 17 Reinforced mat (up to 50 °C) | 1.60 | 13,000 | 150 | 0.0637 | 9.4 | 828.2 | 8.33 |
| 18 Reinforced fabric (up to 65 °C) | 2.0 | 33,000 | 630 | 0.0510 | 24.4 | 1682.0 | 9.16 |
| 19 Reinforced roving (up to 70 °C) | 2.082.5 | 1.35 | 7000 | 60 | 0.0755 | 4.5 | 528.6 |
| 20 Hard fabric | 0.72 | 12,000 | 13 | 0 | 0.1416 | 18.0 | 1698.0 |
| 21 Wood (beechwood) | 2.05 | 12,000 | 13 | 0 | 0.1416 | 18.0 | 1698.0 |

Relationships: \(L_V = \frac{l_g}{\rho \sigma_{\text{per}}}\); \(L_R = \frac{E_g}{\rho \sigma_{\text{per}}}\); \(L_D = \frac{G_g}{\rho \sigma_{\text{per}}^2}\).

Computational relationships for the determination of the mass index \(c_q\) under various loads are collected in Table 4, whereas the energy consumption index \(c_e\) will be characterized later in this paper.

Table 4. Mass indices under various loads (based on: [18]).

| Load Type | Limit Value | Mass Index \(c_q\) | Energy Index \(c_e\) |
|-----------|-------------|----------------|-----------------|
| **Tension (compression)** | \(F\) | \(\sigma_{\text{per}}\) per \(\sigma_{\text{per}}\) | \(\rho/\sigma_{\text{per}}\) per \(\rho/E\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| | \(W\) | \(\sigma_{\text{per}}\) | \(\rho/E\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| **Compression (buckling)** | \(F\) | \(S_w\) | \(\rho/E\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| | \(M_g\) | \(\sigma_{\text{per}}\) per \(\sigma_{\text{per}}\) | \(\rho/\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| | \(W\) | \(\sigma_{\text{per}}\) | \(\rho/E\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| **Beam bending** | \(M_g\) | \(\sigma_{\text{per}}\) per \(\sigma_{\text{per}}\) | \(\rho/\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| | \(W\) | \(\sigma_{\text{per}}\) | \(\rho/E\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| **Board bending (b and l–known, t–variable)** | \(M_g\) | \(\sigma_{\text{per}}\) per \(\sigma_{\text{per}}\) | \(\rho/\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| | \(W\) | \(\sigma_{\text{per}}\) | \(\rho/E\sigma^2\) per \(\rho/E\sigma^2\) | \(c_q\) per \(\sigma_{\text{per}}\) |
| **Torsion** | \(T\) | \(\tau_{\text{per}}\) | \(\rho/\tau^2\) per \(\rho/\tau^2\) | \(c_q\) per \(\tau_{\text{per}}\) |
| | \(W\) | \(\tau_{\text{per}}\) | \(\rho/\tau^2\) per \(\rho/\tau^2\) | \(c_q\) per \(\tau_{\text{per}}\) |

The material selection methodology developed by British professor Michael Farries Ashby is highly esteemed (published in 1989–2013, [10,19–22]). In 1989 he indicated 6 classes of engineering materials and 10 basic subsets of material properties [19] (in 1992, he raised that number of material properties to 18 [10]) and has created characteristic plots used to compare these properties for engineering materials.
(metals, ceramics, glasses, elastomers, polymers, and composites); the Ashby plots may be used for solving various design problems with a formal model based on criteria [10]. At the same time, he introduced the so-called performance indices as the basis for the selection of an optimum material. Performance \( p \) shall be understood as a function of three sub-functions of separate parameters: functional requirements \( f_1 \), geometric parameters \( f_2 \), and material properties \( f_3 \) \( (p = f_1 f_2 f_3) \). For a given design task, it is possible to assume the same values of sub-functions of functional requirements \( f_1 \) and geometric parameters \( f_2 \). This means simplification of material selection by the maximization of the sub-function \( f_3 \to \text{max} \). In the aforementioned book by Ashby and the following books by Michael Farries Ashby and John Humphrey Christopher Jones on engineering materials, particular attention was paid to the material selection method based on performance indices with a series of examples [23–26]. In fact, Ashby’s performance indices correspond to Niemann’s material indices. They were creatively developed, but created later and independently of Niemann’s work. The method of the materials science school originating from Cambridge University for material selection using Ashby’s performance indices has been widely applied to solutions for many design problems in the American subject literature on the fundamentals of machine design [27,28]. Figure 3 shows one characteristic Ashby’s plot, simplified by the authors for further analysis. This plot is used for material selection based on the collected parameters of strength and specific energy consumption of specified material families. The guidelines in the plot are used to select materials for robust structures featuring the minimum material consumption index.

![Figure 3](image-url)  
**Figure 3.** A selection chart for strength with minimum production energy (based on Ashby 2005 [20]) (The darker areas in the figure highlight structural materials used for the analysis in the further part of this paper (in Section 3.1)).

Here, it is necessary to point out a certain “intrinsic error” of the material indices method. All calculations performed while determining the strength, stiffness, and work of the elastic strain \( (\sigma = \sigma_{\text{per}}, f = f_{\text{per}}) \) are based on the limit load state \( F \) of the component in question for the volume index \( c_v \) (Table 2).

This limit load state is not typical for mechanical designs or undesirable due to other design limitations that are not accounted for in the material indices method (e.g., process-related, ergonomic limitations). Parameters of the component cross-section are not constant due to load changes...
(e.g., bending moment) along the component length, the limit state of which occurs only locally. Allowable stresses not only result from the strength properties of a material (with the values assumed with a certain spread), but also from the component reliability measured by safety factors under static and fatigue loads. Even in components under tension or compression with a conventionally-fixed distribution of stresses along the component length, increased cross-sections often occur at the points where the loads are applied. The remaining indices of mass, cost, or energy consumption (as discussed later) are derived from the doubtful volume index. Results of such analyses of indices are accompanied by heavily scattered values that correspond to the scattering of values of the cost-absorption and energy consumption indices. The use of the material indices method for material selection in a multi-component design is greatly hindered since non-uniform loads on components are the reason for which material properties in such components are different.

A reasonable approach to material selection in multi-component design is to use contemporary 3D computer-aided design methods. A virtual three-dimensional model of a structure makes it easy to reproduce numerical values of cross-section and mass factors without the simplification that is characteristic for the material indices method. Computer databases facilitate the search and selection of information on material properties [29].

2.2. Material Selection in Design for the Environment

The orientation of engineering design towards the environment is based on the concept of sustainable development. In the process of Design for the Environment, detailed criteria of the environmental impact within the full life cycle of a product are important cornerstones for the structure—from the moment of establishing the design problem, through the process of creating lists of requirements, the process of searching for solutions, evaluating and selecting them to the stage of design engineering [30]. All it means is a new integral approach to the development of products, wherein the approach employs and enriches the former achievements of the design theory. Functions such as safety, durability, reliability, costs, and ergonomics continue to be the main general requirements. Such requirements during the selection of an environmentally-friendly structural material necessitate more thorough analyses of the potential effects of basic phenomena and processes in machines (friction, wear, lubrication, creeping, and material fatigue), toxicity of materials, price availability, process-related processing capabilities, and susceptibility to material recycling. Design for the Environment is one of the design strategies that is currently being widely developed [30–34]. The focal point of these strategies is included in the rules of Design for the Environment [35] that can be characterized as follows:

- **Rule 1.** To ensure sustainable development of resources: to specify renewable and abundant resources; to specify recyclable and recycled resources; to use recycled materials; to employ common and remanufactured components; to specify compatible materials and fasteners for recycling; to minimize the variety of materials in the product or its components; to specify renewable energy sources.

- **Rule 2.** To minimize the use of resources in the production and transportation phase: to change the functions and appeals of packaging during design; to fold and disassemble in a compact state; to apply structural techniques and material technologies that minimize the total volume of material; to provide light materials and components; to specify materials that do not require additional surface treatment or paint; to structure the product to minimize material waste; to minimize the number of components; to ensure clean production processes.

- **Rule 3.** To ensure harmless inputs and outputs: to ensure containment of hazardous substances, substances that are safe to the environmental and user health; to ensure water-based and biodegradable waste; to specify the cleanest source of energy; to ensure easy removal of concentrated toxic components.

- **Rule 4.** To minimize consumption of resources during operation: not to manufacture in a hot-state to prevent material losses; to minimize volume, surface area, and mass of components and materials to which energy is transferred; to specify best-in-class efficiency components; to reduce
power in systems that are not in use by default; to incorporate partial operation to disengage systems that are not in use; to reveal energy and water consumption; to incorporate features that prevent the waste of materials by the user.

- **Rule 5.** To ensure durability of the products and components: to reuse energy; to provide aesthetics of the life cycle; to minimize maintenance; to protect the product from dirt and corrosion; to indicate through the product how parts are maintained; to ensure easy repair and upgrade; to minimize the number of service and inspection tools; to facilitate testing.

- **Rule 6.** To ensure incorporation, disassembly, separation, and cleaning; to indicate through the product how it should be accessed; to ensure that joints and fasteners are accessible; to minimize the number and plurality of fastening elements; to ensure easy cleaning methods and reusability; to create simple part placement that can be restored; to organize in hierarchical modules for end-of-life repair; to implement reusable platforms after replacement of modules; to specify adhesives, labels, surface coatings, and varnishes that are compatible with cleaning; to ensure one disassembly direction without reorientation; to mark materials with reutilization protocol to ensure a shallow or open structure for easy access to sub-assemblies.

Three quantities determine well the environmental impact of materials: embodied energy, carbon footprint, and water demand [36]. Energy consumption by materials during manufacturing and processing may be evaluated using the so-called specific energy consumption per unit volume \( p_v \) \( \text{[GJ/m}^3\text{]} \) or per unit mass \( p_q \) \( \text{[MJ/kg]} \). If the volume \( V \) \( \text{[m}^3\text{]} \) or mass \( m \) \( \text{[kg]} \) of the material is known, its energy consumption \( E = p_v \cdot V \) \( \text{[MJ]} \) or \( E = p_q \cdot M \) \( \text{[MJ]} \) can be determined. While comparing the energy consumption of many materials, it is therefore sufficient to compare values of material indices under a given load (Table 4). Table 5 presents specific energy consumption of frequently occurring materials.

Specific energy consumption is one measure of how use affects the natural environment, without hazards caused by the emission of toxic by-products, recycling difficulties, resistance to biodegradation.

| Material                          | \( p_q \) (MJ/kg) | \( p_q \) (MJ/kg) | \( p_v \) (GJ/m^3) |
|----------------------------------|-------------------|-------------------|-------------------|
| **According to Ashby 1998 [37]  | \( p_q \) (MJ/kg) | \( p_q \) (MJ/kg) | \( p_v \) (GJ/m^3) |
| Metals                           |                   |                   |                   |
| Magnesium alloys                 | 410–420           | 212–490, average 400 | 717–756           |
| Cast irons                       | 60–260            | –                 | 468–1500          |
| Aluminum alloys                  | 290–305           | 142–335, average 190 | 754–884          |
| Stainless steels                 | 110–120           | 46–115, average 70 | 825–972          |
| Copper and its alloys            | 95–115            | 57–120, average 90 | 712–1035         |
| Zinc and its alloys              | 67–73             | 53–145, average 90 | 348–525          |
| Carbon steel                     | 50–60             | 30–72, average 45 | 390–468          |
| Lead and its alloys              | 28–32             | –                 | 300–360          |
| **Polymers**                     |                   |                   |                   |
| Polyamide 66                     | 170–180           | 156–180           | 187–216          |
| Polycarbonate                    | 108–113           | 74–110            | 93–102           |
| Low-density polyethylene         | 103–120           | 75–110            | 97–116           |
| High-density polyethylene        | 80–104            | 85–120            | 73–94            |
| Polystyrene                      | 90–140            | 96–104            | 96–154           |
| Polycrylon chloride              | 67–92             | 57–106            | 87–147           |
| Synthetic rubber                 | 120–140           | 84–150            | 108–126          |
| Natural rubber                   | 5.5–6.5           | –                 | 5–6              |
| **Composites**                   |                   |                   |                   |
| GFRP (Glass Fiber Reinforced Polymer) | 90–120          | 60–150            | 160–220          |
| CFRP (Carbon Fiber Reinforced Polymer) | 130–300          | 300–700           | 230–540          |
| Glass fibres                     | 38–64             | 10–34             | 95–160           |
| Hardwood and softwood            | 1.8–4.0           | 17–46             | 1.2–3.6          |
Table 5 presents specific energy consumption for three groups of construction materials used in the technique (metals, polymers, and composites). The values of individual parameters differ depending on the author and are characterized by a significant dispersion of values. Average values of energy intensity \( p_q \) according to Bey [38] were adopted for further analysis.

### 3. Sample Application of the Energy Consumption Index in Material Selection

#### 3.1. Selection of the Material for a Standing Frame Subject to Bending

The objective here is material selection for a knee support column under bending in a mobile rehabilitation standing frame, i.e., an individual medical device for a physically disabled person. Figure 4 shows the standing frame together with the dimensional system and support column loads \( F = 800 \text{ N}, l = 400 \text{ mm}, a = 500 \text{ mm} \) as well as the dimensions of the cross-section of preliminarily selected aluminum profiles \((60 \times 60 \text{ mm}, \text{section area } A = 20.6 \text{ cm}^2, \text{and index} W_x = 23.5 \text{ cm}^3)\) and steel \((3 \text{ welded rectangular profiles according to EN 10210, \text{section area } A = 5.6 \text{ cm}^2, \text{and index} W_x = 5.9 \text{ cm}^3)\).

The shape factor \( m_v \) of the aluminum section \( m_{vAl} = \frac{W_x}{A} = 0.398 \) considerably differs in its value from the shape factor of the steel section \( m_{vSt} = 0.583 \), which raises doubts as regarding the suitability of the material indices method.

Limit load capacities \( M_{gmax} = W_x \cdot k_g \) of the support column made of aluminum alloys and steel (Table 6) are considerably different and considerably smaller than the actual load \( (M = F \cdot l = 320 \text{ Nm})\).

Table 6. Material data of the support column design.

| Material          | \( E \) (N/mm\(^2\)) | \( \rho \) (kg/m\(^3\)) | \( R_m \) (N/mm\(^2\)) | \( R_e \) (N/mm\(^2\)) | \( k_g = \frac{R_e}{x} \) | \( M_{gmax} \) (Nm) | \( p_q \) (MJ/kg) |
|-------------------|------------------------|---------------------------|------------------------|------------------------|------------------------|------------------|------------------|
| AlMgSi0.5F25 (T6) | 70,000                 | 2700                      | 245                    | 195                    | 55.7                   | 1309             | 190             |
| AlMgSi0.5F19 (T6) | 70,000                 | 2700                      | 190                    | 150                    | 42.8                   | 1006             | 190             |
| St3VC             | 210,000                | 7680                      | 360                    | 235                    | 145                    | 856              | 45              |
| 18G2AC            | 210,000                | 7680                      | 490                    | 355                    | 177                    | 1044             | 45              |

Please note that the verification of the accuracy of the results obtained by the material index method relative to the computational method requires that the ratios of mass material indices be equal to the ratios of component masses for given materials \( c_{qAl} = \frac{m}{m_{min}} \) and the ratios of energy consumption indices be equal to the energy ratios: \( c_{eAl} = \frac{E}{E_{min}} \). These relationships do not apply. This is evidence of the indicative nature of material selection based on the material indices method and confirms the prior critical evaluation of the method. Furthermore, it may be concluded from Table 7 that steel as a structural material has an advantage over aluminum alloys both in terms of the material consumption index and the energy consumption index as indicators of the environmental burden.

Table 7. Data of the material consumption index and the energy consumption index of the support column design.

| Material          | \( c_{q} = \frac{\rho \cdot k_g}{k_{qmin}} \) | \( c_{qAl} \) | \( c_{qSt} \) | \( \frac{m}{m_{min}} \) | \( \frac{E}{E_{min}} \) |
|-------------------|---------------------------------|-------------|-------------|-----------------|-----------------|
| AlMgSi0.5F25 (T6) | 185                             | 2.74        | 1.27        | 528             | 5.33            |
| AlMgSi0.5F19 (T6) | 221                             | 3.27        | 1.27        | 528             | 5.33            |
| St3VC             | 285                             | 1.00        | 1.00        | 99              | 1.00            |
| 18G2AC            | 249                             | 0.87        | 1.00        | 99              | 1.00            |

Please note that the verification of the accuracy of the results obtained by the material index method relative to the computational method requires that the ratios of mass material indices be equal to the ratios of component masses for given materials \( c_{qAl} = \frac{m}{m_{min}} \) and the ratios of energy consumption indices be equal to the energy ratios: \( c_{eAl} = \frac{E}{E_{min}} \). These relationships do not apply. This is evidence of the indicative nature of material selection based on the material indices method and confirms the prior critical evaluation of the method. Furthermore, it may be concluded from Table 7 that steel as a structural material has an advantage over aluminum alloys both in terms of the material consumption index and the energy consumption index as indicators of the environmental burden.
3.2. Comparison of the Energy and Material Consumption Index in the Accurate Calculation Method with the Approximate Indicator Method for Material Helical Compression Springs

In the field of spring design, the use of the material elasticity coefficient has had a long history. Wilhelm Gerolsky made the first compilation of analytical forms of the $V_F/W$ indicator for various bent and twisted springs already in 1918 [39]. Choosing the right material and shape in order to obtain the expected spring parameters, was the main area for the optimization of spring design. The criteria for this selection were the assembly volume ratios of the spring $V_F$ or mass $m$ to stiffness $R$ or the accumulated deformation energy $(W)$ in the spring. In the literature on the subject [10,11,16,17], indicators $m/W$, $m/R$, $V_F/W$, $V_F/R$ were distinguished. Synthetic summaries of applications of the indicator method in spring design, as carried out by prof. B. Branowski [16,17], indicate the possibility of using the accumulated deformation energy to select the optimum type of spring due to the criterion.
represented by the indicator of material selection for specific types of springs. Another indicator (the ratio of accumulated energy \( W \) to volume \( V_M \) of spring material – \( c_M = W/V_M \)) is used by prof. M.F. Ashby [23] to select the best type of spring material.

This paper presents two ways of proceeding in the determination of energy consumption. The first algorithm compares the mass indicators \( c_M \) of three cylindrical helical compression springs with the workload of \( W = 0.5 \cdot F_n \cdot s_n = \text{const} \). Expressing the mass index \( c_M \) as:

\[
c_M = \frac{G \cdot \rho}{\tau_{\text{dop}}^2}
\]

and the derivative energy index will be \( c_E \):

\[
c_E = c_M \cdot \rho_q = \frac{G \cdot \rho}{\tau_{\text{dop}}^2} \cdot \rho_q
\]

In the other algorithm, a strict calculation of energy consumption is performed. In a separate calculation procedure, the geometrical parameters of springs are determined. Each of the three considered cylindrical helical compression springs made of a wire of circular cross-section (marked A, B, C) of the shock absorbers is made of a different material. The springs are made of the following materials: (A) of patented steel wire of unalloyed steel according to DIN 17223 Part 1, type B (EN 10270-1); (B) of stainless steel wire acc. to DIN 17224, type X12CrNi177 (EN 10270-3), (C) of beryllium bronze wire acc. to DIN 17682, type CuBe2 (EN 12166).

The developed calculation algorithm determines the geometric parameters of springs at a given value of deformation work \( W \). Due to the discontinuous nature of the geometric features of spring design (e.g., in Table 8: parameters of wire diameters \( d \) or turn numbers \( n \)), the calculations were carried out using the method of successive approximations using known calculation relationships. The spring parameters given in Table 8 were adopted.

**Table 8. Basic structural properties of springs.**

| Spring | Type of Material                        | Breaking Strength \( R_m \) (N/mm²) | Coefficient of Transverse Elasticity \( G \) (N/mm²) | Density \( \rho \) (kg/dm³) | Specific Energy Consumption \( \rho_q \) (M/J/kg) (Acc. to M.F. Ashby Table 5) |
|--------|----------------------------------------|--------------------------------------|-------------------------------------------------|----------------------------|--------------------------------------------------------------------------------|
| A      | patented steel unalloyed wire          | 1650                                 | 80,400                                          | 7.85                       | 55 on average                                                                  |
| B      | stainless steel wire according to DIN   | 1850                                 | 73,000                                          | 7.80                       | 115 on average                                                                 |
|        | 17224, type X12CrNi177                 |                                      |                                                 |                            |                                                                                                                                     |
| C      | beryllium bronze wire according to      | 1250                                 | 47,000                                          | 8.90                       | 105 on average                                                                 |
|        | DIN 17682, type CuBe2                  |                                      |                                                 |                            |                                                                                                                                     |

Shock absorber springs have similar values of accumulated work \( W = 0.930 \pm 0.044 \) Nm. These are for springs A, B, C, respectively: \( W_A = 0.974 \) Nm, \( W_B = 0.899 \) Nm, and \( W_C = 0.886 \) Nm. When taking into account the permissible torsional stresses \( \tau_{\text{dop}} \approx 0.3 \cdot R_m \), geometric parameters were determined using the following basic design relationships of springs:

- nominal torsional stresses \( \tau_n = \frac{8 \cdot F_n \cdot D}{\pi \cdot d^3} \leq \tau_{\text{dop}} \);
- stiffness \( R = \frac{F_n}{s_n} = \frac{G \cdot d^4}{8 \cdot D^2 \cdot n_t} \);
- accumulated deformation energy \( W = 0.5 \cdot F_n \cdot s_n \);
- wire mass \( M = 10^{-6} \cdot \pi \cdot D \cdot n_t \cdot \frac{\pi \cdot d^2}{4} \cdot \rho \) (kg), \((n_t = n + 1.5)\).

The above limits meet the spring parameters given in Table 9.
1. Literature data (M.F. Ashby [36], N. Bey [38]) shows a large dispersion of the values of specific energy consumption for materials. For example, as given in Table 5, the specific energy consumption of stainless steels varies between \( p_q = 110–120 \text{ MJ/kg} \) according to Ashby and \( p_q = 46–115 \text{ MJ/kg} \) according to Bey and, for copper alloys, between \( p_q = 95–115 \text{ MJ/kg} \) and \( p_q = 57–120 \text{ MJ/kg} \), respectively. Assuming energy consumption limits for specific energy consumption, stainless steel features higher \( p_q \) values than Ashby’s copper alloys, while the opposite is true for Bey. This may change the order of importance for the environment of the compared structures.

The consolidated results of the calculations of energy and material consumption are presented in Table 10 using the accurate method and the material indicator method.

### Table 9. Design parameters of springs (geometrical, elastic, and strength characteristics).

| Spring Parameters | A   | B   | C   |
|-------------------|-----|-----|-----|
| Wire diameter \( d \) (mm) | 2.0 | 2.0 | 2.5 |
| Average diameter of the spring in the non-load condition \( D \) (mm) | 14.0 | 14.0 | 14.0 |
| Total number of turns \( n_t \) | 9.5 | 9.5 | 7.0 |
| Active number of turns \( n \) | 8.0 | 8.0 | 5.5 |
| Locking deflection \( s_{ld} \) (mm) | 19.0 | 19.0 | 17.5 |
| Minimum sum of the inter-turn gaps \( \Sigma_{\text{min}} \) (mm) | 1.6 | 1.6 | 1.4 |
| Spring deflection \( s_n \) corresponding to force \( F_n \) (mm) | 16.5 | 16.5 | 10.8 |
| Spring wire length in the non-load condition \( D \) (mm) | 40.0 | 40.0 | 29.7 |
| Spring wire volume \( V \) (mm\(^3\)) | 1313 | 1313 | 1511 |
| Mass \( M \) (kg) | 0.0103 | 0.0104 | 0.0135 |
| \( s_{ld}/R_m \) ratio | 0.32 | 0.26 | 0.13 |
| Stiffness \( R \) (N/mm) | 7.1 | 7.3 | 15.2 |
| Force \( F_n \) (N) | 118 | 109 | 164 |
| Impact work \( W \) (Nm) | 0.974 | 0.899 | 0.886 |

### Table 10. Comparison of calculation methods for energy and material consumption of springs.

| Spring | \( c_E \) | \( c_E/c_{E_{\text{min}}} \) | \( E \) (MJ) | \( E/E_{\text{min}} \) | \( M \) (kg) | \( M/M_{\text{min}} \) |
|--------|---------|----------------|-------------|----------------|-------|----------------|
| A      | 141.7   | 1              | 0.57        | 1              | 0.0103| 1              |
| B      | 212.6   | 1.50           | 1.20        | 2.1            | 0.0104| 1.01           |
| C      | 312.3   | 2.20           | 1.42        | 2.5            | 0.0135| 1.31           |

The results of the calculations indicate the correct trend of energy consumption increase in the change of spring material from patented carbon steel through stainless steel to beryllium bronze. Large differences in the comparison with the logically occurring similarity of \( c_E/c_{E_{\text{min}}} \) values in the method of material indicators and \( E/E_{\text{min}} \) values in the accurate method result from simplifications of the indicator method. However, the results of the calculations using the indicator method allow for control of the impact of the designed structure on the environment. In designing the geometrical features of A, B, C springs, the permissible torsional stresses (\( \tau_{\text{dop}} = 0.3 R_m \)) were consciously reduced to compensate for the dynamic character of shock absorber spring loads and to reduce stress relaxation.

### 4. Conclusions

The results of the analyses indicate significant limitations of the application of the material indicator method, which is not fully emphasized in the scientific literature. This is a result of antinomy: simplicity of the form of indicators vs. high accuracy of representation of many structural properties of the designed object.

1. Literature data (M.F. Ashby [36], N. Bey [38]) shows a large dispersion of the values of specific energy consumption for materials. For example, as given in Table 5, the specific energy consumption of stainless steels varies between \( p_q = 110–120 \text{ MJ/kg} \) according to Ashby and \( p_q = 46–115 \text{ MJ/kg} \) according to Bey and, for copper alloys, between \( p_q = 95–115 \text{ MJ/kg} \) and \( p_q = 57–120 \text{ MJ/kg} \), respectively. Assuming energy consumption limits for specific energy consumption, stainless steel features higher \( p_q \) values than Ashby’s copper alloys, while the opposite is true for Bey. This may change the order of importance for the environment of the compared structures.
2. The negative impact of materials on the environment may result from factors other than energy consumption in their production (e.g., emissions of nitrogen oxides, sulphur compounds, and solid particles, the demand for water in production).

3. In the calculation example of a bent pole of the standing frame (described in Section 3.1), the results of energy consumption calculations for a pole made of aluminum alloy and a pole made of welded steel profiles were compared. This comparison was carried out using the method of material indicators and the accurate method of calculating mass and energy consumption. Both methods showed a significant advantage of the steel structure over the aluminum structure in terms of environmental loads (energy consumption). Lack of proportionality between the results of the two methods of energy consumption determination (Table 7), as expressed by the ratio $c_{Ei}/E_i$ and ratios $c_{Ei}/c_{E_{min}}$ and $E_i/E_{min}$, confirm the approximate nature of the material indicator method.

4. In the second calculation example (Section 3.2), when comparing the energy and material consumption of helical compression springs made of different materials, similar calculation conclusions were obtained as to the lack of adequacy of the indicator method in relation to the accurate calculation method. The indicator method was used by one of the authors [16,17] to construct a quantitative semantic code of spring materials based on the values of mass and material indicators standardized on a scale of 1–10 at different states of quasi-static and dynamic loading. This code is the basis for the selection of spring material from the computer database. Material indicators were also used in the paper [17] of one of the authors for the selection of the optimum spring type.

5. Material indices are used as some attempts to estimate quantitatively the comparison of structural materials, taking into consideration the type of load. Their major advantage is the functional form that can be easily used operationally in practical applications during material selection in CAD systems. The assumptions made for the use of components made of materials with comparable shape factors create an important restriction on the use of this method in design. A change of technology (e.g., welded structure replaced by a structure with fixing screws) usually changes shape factors. Such limitations are the reason the main importance of the material indices method is associated with materials science and less practically important in design. The use of the material indices method for material selection in a multi-component design, e.g., a support frame made of fixed-section bars, is hindered since non-uniform loading on components results in differently-used material properties.

The evolution of the indices material selection methods has switched from material consumption and cost-absorption indices to energy consumption indices. The literature review presented in this article shows that the method of material indicators may be too simplistic and, in some cases, lead to the selection of non-optimal material (this conclusion is consistent with the conclusions contained in Ref. [40]). This indicates that applying linguistic values (by fuzzy logic) can significantly improve the adequacy of the selected material in engineering design. Especially by describing the material selection problem as a multi-criteria decision-making (MCDM) problem [41].

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Nomenclature

- $\gamma$—specific weight
- $\rho$—volumetric mass density
- $\sigma$—tensile or bending stress
- $\sigma_{per}$—permissible tensile or bending stress
- $\tau_{per}$—permissible torsion stress
- $\phi_{per}$—permissible turning angle
- $A$—cross-sectional area
- $c_e$—energy index
- $c_q$—mass index
- $c_v$—volume index
- $E$—modulus of elasticity
- $F$—force
- $f_1$—sub-function of functional requirements
- $f_2$—sub-function of geometric parameters
- $f_3$—sub-function of material properties
- $f_{per}$—permissible
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