Hierarchical \{332\} < 113 > twinning in a metastable β Ti-alloy showing tolerance to strain localization

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ABSTRACT

A hierarchical \{332\} < 113 > twinning system is studied in a metastable beta Ti-12Mo-10Zr (wt%) alloy, which shows strong twinning-induced plasticity (TWIP) effect due to a three-level twinning mechanism. In-situ digital image correlation (DIC) indicates a good tolerance to strain localization until \(\varepsilon_{\text{max}} = 0.4\) thanks to TWIP hardening effect. The local shear misfit due to the intersection between the matrix slip bands and the primary twin boundaries is accommodated by the formation of secondary and tertiary sub-twinning structures. The strain accommodation postpones crack nucleation at the slip-twin intersections, contributing to the high tolerance of the strain localization.

IMPACT STATEMENT

The metastable Ti-12Mo-10Zr alloy displays a high tolerance to strain localization in tension thanks to the dynamic strain-hardening effect and local strain accommodation by the hierarchically self-organized triple \{332\} < 113 > deformation twinning.

Commercial Ti-alloys have been widely used in the fields of aerospace, biomedical, automotive and petrochemical industries. However, low strain-hardenability and insufficient damage tolerance are the two major weaknesses that limit the use of Ti-alloys when comparing to steels. Recently, new strategies inspired from TRIP (transformation-induced plasticity) and TWIP steels have been followed to overcome these weaknesses in β metastable Ti-alloys. In the last decade, by tuning the simultaneous or sequential activation of deformation modes among dislocation slips, deformed twins (DTs) and stress-induced martensitic transformation (SIMT), a new family of TRIP/TWIP β Ti-alloys [1–6] has been developed, exhibiting excellent combination of high strength, large ductility and improved strain-hardening rate. The relationships among the three deformation mechanism and their effects on mechanical performances in the TRIP/TWIP Ti-alloys have been studied in detail. Interestingly, some hierarchical substructures such as secondary SIMT and secondary/tertiary DTs are reported in TRIP/TWIP Ti-alloys as accommodation mechanisms [7,8]. Regarding the triple twinning structure, hierarchical lengthscales have been observed in pure titanium [9]. In the Ti-alloys dominated by single \{332\} < 113 > DT mode (hereafter termed as 332T), the occurrence of hierarchically self-organized structures...
and their impact on mechanical properties become of great interest for TWIP Ti research. In this work, we report a study of hierarchical microstructure of a three-level deformation and the mechanism of its impact on the alloy’s tolerance to strain localization. The TWIP Ti-alloy used in this study is a metastable beta Ti-12Mo-10Zr (wt%) alloy designed by ‘d-electron’ strategies [10]. The microstructural characterization of hierarchical structure was analysed by electron backscatter diffraction (EBSD) and transmission electron microscopy (TEM) techniques. The 2D full-field strain distribution was analyzed by the in-situ optical digital image correlation (DIC) technique.

The cylindrical ingot of Ti-12Mo-10Zr (160 mm in diameter) was prepared by vacuum arc-melting under a high-purity Ar atmosphere using Ti-Mo master alloy and high purity Ti and Zr sponges. The processing of samples is the same as our previously reported method [1]. DIC technique with a camera recording was used during the tensile test. A 2D full-field strain map was recorded at a rate of 3 frames/second. The details of the technique can be found in reference [11]. The tensile test was conducted using an INSTRON 5967 machine at a constant strain rate of $10^{-3}$ s$^{-1}$. The strain maps were processed by Instron® DIC Replay Software. Phase characterization was carried out by X-ray diffraction (XRD) using Bruker D8 ADVANCE with Cu Kα radiation operating at 40 kV and 40 mA. Deformation microstructures were analysed by EBSD scans performed on a scanning electron microscope (SEM) operating at 20 kV. A JEOL 2100 microscope operating at 200 kV was used to carry out fine microstructural analysis.

Figure 1(a) displays the stress–strain curves of Ti-12Mo-10Zr and the DIC strain-distribution maps at different strain levels. The yield stress and ultimate tensile stress are about 730 and 1090 MPa, respectively, which represent much higher values than the Ti-12Mo strength reported elsewhere [1]. This can be attributed to the full suppression of SIMT and the solution strengthening effect provided by the zirconium addition [4]. A series of frames of the DIC video shows the 2D full-field strain maps at different strain levels (Figure 1(a)). It can be seen that a shear zone [12] (indicated in Figure 1(a)) occurs at the onset of plasticity ($\epsilon = 0.02$). With increasing tensile strain to $\epsilon = 0.05$, the shear zone spreads in width along the sample length. From $\epsilon = 0.05$ until fracture, the plastic zone stays at the same location, contributing to higher local tensile strain ($\epsilon_{\text{max}}$) than overall $\epsilon$. This phenomenon, according to Considère’s criterion, usually leads to rapid decreasing stability with respect to necking in many BCC metals which lack sufficient strain-hardenability. Similarly, in the present alloy, the strain localization occurred at the very beginning of the plastic regime (Figure 1(b), $\epsilon = 0.02$) due to the weak hardening rate (730 MPa) is almost equal to the yielding strength near Considère’s criteria line. However, instead of necking, the stable plastic flow was immediately restored by the rapid increasing of hardening rate until $\epsilon = 0.12$, then maintained by the decreasing of the hardening rate to $\epsilon = 0.25$ ($\epsilon_{\text{max}} = 0.4$) before the hardening rate drops below the Considère’s criteria line. The stabilized plastic flow suggests a dynamic strain-hardening mechanism of the alloy in addition to the conventional dislocation slip mechanism in BCC alloys. The initial structure of Ti-12Mo-10Zr is presented in Supplementary Figure 1.

Figure 2 shows EBSD analysis results concerning the deformation structure of Ti-12Mo-10Zr on a macroscale. The grain boundaries are clearly visible in EBSD inverse pole figure (IPF) map (Figure 2(a)). The high density of parallel or interlaced deformation bands with different colour contrast are observed in each grain marked as Grain 1 ~ 5, suggesting that both fast multiplication
and thickening of the deformation bands occurred with the continuous accumulation of strain. The crystallographic relationship between the bands and matrix are identified to correspond to \{332\} <113> system. Two examples of the misorientation measurements are shown in Figure 2(c), the characteristic 50.5° (CSL \Sigma 11) is confirmed. The sizes of these 332Ts are in the range of a few micrometers. The activation of different 332T variants can be seen in some grains, depending on their orientation with respect to the external stress. It can be seen from image quality (IQ) maps (Figure 2(b)) that some slip bands intersect with the 332T bands. It is worth noting that no SIMT $\alpha'$ was observed in this alloy, consistently with XRD results shown in Supplementary Figure 1(b). The observed 332Ts are directly formed from the matrix, denoted as 'primary 332T' hereafter, intersecting the slip planes of the matrix, thus reducing the mean-free path of dislocation slip. The primary 332T can be also proved by TEM observation. Supplementary Figure 2 shows an overview of TEM images of primary 332T (1st 332T) and secondary 332T (2nd 332T). According to the Hall-Petch effect, the primary 332T is a strain-hardening mechanism resulting from the dynamical reduction of dislocation mean free path during its multiplication. In addition to the efficient hardening effect due to the primary 332 T boundaries as dislocation slip barriers, accommodation mechanisms to relax strain localization and damage at these intersections are of great importance to postpone the premature crack nucleation.

Careful TEM investigations are performed on the 332 T and its interfaces. Interestingly, a tertiary \{332\} <113> twin (3rd 332 T) was identified in the 2nd 332 T by TEM, where the 2nd to 3rd 332 T follows the same crystallographic orientation relationship as the 1st to 2nd 332 T system. Figure 3 shows TEM analysis of the hierarchical \{332\} <113> twinning structures at multiple length scales. Figure 3(a) shows a primary deformation band (about 2 $\mu$m in width) with several secondary bands (about 100–300 nm in width). The secondary deformation bands and their internal tertiary bands were visible in the higher magnification TEM image, as shown in Figure 3(b). The above deformation bands are identified to be 332-type DT with habit plane parallel to the common twin 332 planes between parent and twin product, consistently with previous reports [1]. In this work, the TEM foil was tilted to \{101\} zone axes (ZA) of the primary deformation band, as the reference orientation. The orientation relation between the primary and secondary deformation bands (Figure 3(e)) is in agreement with the $\Sigma 11$ coincidence site lattice of \{332\} <113> twinning system [13]. By using the similar method, the secondary 332 T bands and tertiary 332 T bands were also identified by the corresponding selected-area electron diffraction (SAED) pattern (Figure 3(e–f)). However, as the matrix is a few degrees deviated from its \{101\} ZA, the corresponding SAED pattern of the matrix near [315] ZA is shown in Figure 3(c). By reconstructing the crystallographic projection, it is found that the primary twin plane is \{332\}_\text{Matrix}, which is not orientated at edge-on conditions in our characterization (about 10° inclined from beam axis). The same trace analysis method is also used to identify the possible planes of slip band contrast in the
Figure 3. TEM images of the hierarchical structure of triple 332 T. (a) Bright-field image of triple 332 T (Lower magnification overview); (b) Close-up bright-field image of selected-area b in (a): matrix (M), primary 332 T, secondary 332 T and tertiary 332 T. The traces in the matrix and primary 332 T analysed by the trace method [14] were presented in (a). The selected-areas c, d, e and f were also highlighted by the dotted circle in (a) and (b); (c–f) SAED of selected-areas c, d, e and f, respectively. The zone axes (ZA) of the matrix is near [315]β, and the common ZA of [101]β is shared by primary, secondary and tertiary 332 T.

Based on the TEM imaging results, Figure 4 shows a schematic illustration of the 3D view and cross-section views concerning the formation sequence of primary 332 T (1st T), secondary 332 T (2nd T) and tertiary 332 T (3rd T). The 3D view is reproduced based on the TEM images (Figure 4(a–b)) by illustrating the ‘hidden’ planes in the foil thickness to understand the inter-plane geometries discussed. And the cross-section views are intended to explain the proposed mechanisms by showing relative positions of the planes and their notations used in this work. A coincidence is found between the incoming slip band (132)[111]matrix and the 2nd 332 T, that they share the common intersection line (indicated in 3D view of Figure 4) on the 1st 332 T interface. The geometry measurements show that their habit planes are almost parallel, and the angle between the Burgers vector of the
Figure 4. Schematic illustration of the 3D view and cross-sectional views concerning the formation sequence of primary 332 T, secondary 332 T and tertiary 332 T.

slip band (Burgers vector is $a/2[\bar{1}\bar{1}1]$) and the twinning direction is about 40°. The Geometric Criterion (GC) [15] can be used, as an index to be minimized as possible, to predict which slip or twinning system could be activated at an interface in response to an incoming slip band. The present GC index is about $-0.77$, which is one of the lowest values among all combinations of the slip and twinning systems on either side of the interface. Based on this finding, it is presently thought that the localized shear strain due to dislocation pile-up at the 1st 332 T boundary may be accommodated by the formation of an appropriate 2nd 332 T variant. Some details of the accommodation process can be discussed with regard to the slip-interface interaction [16]. Here, the 332 T interface can be characterized as $\Sigma 11$ (332) boundaries, which act as effective obstacles for slip transfer, leading to dislocation pile-up at the left-hand side of the interface [15]. Stress concentrations consequently happen at both sides of the interface close to the pile-up site. On the right-hand side, the stress concentration points act as sources of new dislocation slips or twinning operations to accommodate the slip strain [17]. In the present case, the 2nd 332 T bands are formed to relax the stress concentration. At the intersection between slip band and 332 T, it can be observed that the interface orientation is tilted from the original 332 T orientation (observed in Figure 3(a–b) and illustrated in Figure 4), which demonstrates the magnitude of shear deformation. A perfect shear compatibility can be established when the total shear strain '$\gamma_{\text{slip band}}$' induced by slip band equals to the shear strain '$\gamma_{\text{2nd 332 T}}$' provided by the thickening of the 2nd 332 T band (Figure 4). However, the balance is about to break when '$\gamma_{\text{slip band}}$' continues to increase locally in the slip band along with the plastic flow.

It should be pointed out that the 2nd twinning operation has changed interface structure at the intersection (from $\Sigma 11$ to mixed type, indicated in Figure 4). The change of the interface structure associates with the change of slip-interface interaction [16,18]. One pair of slip systems, ($\bar{1}32$)[111]_{matrix} and ($\bar{2}31$)[111]_{2nd 332 T}, is found likely to fulfill the direct slip transfer criterion. The Geometric Criterion index is about $-0.8$, the lowest among all combinations. However, the direct slip transfer usually involves a trapping process of the incoming dislocation at interface, leading again to stress accumulation [17,19]. Previous experimental study has shown that a high resolved shear stress, about 2 times higher than the yielding stress, is required to push the dislocation out of the boundary [18]. In TWIP Ti-alloys, such stress level is largely sufficient to activate 332 T. As a matter of fact, the 3rd twinning structures are indeed observed in most of the 2nd twin bands (Figure 3). Therefore, it would be reasonable to suggest that when '$\gamma_{\text{slip band}}$' > '$\gamma_{\text{2nd 332 T}}$', a compressive stress is likely accumulated in the 2nd 332 T along the slip transfer direction, resulting in the formation of the 3rd 332 T as a supplementary accommodation mechanism.
Some discussions can be addressed to the relation between the hardening mechanism by 1st 332T and the accommodation mechanism. The synergetic cooperation of these two mechanisms is thought to be one of the reasons for the macroscopic tolerance to strain localization. Analogous to the Ti-alloys operating in TWIP/TRIP [1,5], similar synergy may exist between twinning and martensitic transformation, which play roles for strain-hardening and for strain misfit accommodation, respectively. As a result, these alloys also present very stable plastic flow accompanied by strong strain hardening effect. Furthermore, the activation of the 1st deformation mechanism is determined by the chemical stability of β phase. The activation sequence has been reported to be SIMT-332T-112T when increasing the β phase. It is assumed that the stability of solution-treated Ti-12Mo-10Zr should be situated between Ti-12Mo and Ti-13Mo-18Zr, because the 1st deformation mechanism of Ti-12Mo is TRIP + TWIP 332T [1,20] and the Ti-13Mo-18Zr is TWIP 332T + 112T mode [4]. Similarly in the selection of 2nd/3rd accommodation mechanisms, the Ti-12Mo presents 2nd martensite and 2nd/3rd 112T in the 1st 332T, whereas the TWIP Ti-13Mo-18Zr presents low volume fraction of 2nd 332 twinning and the formation of a special [5 8 11] twinning [4]. Comparing to the triple 332T observed in the Ti-12Mo-10Zr, these differences might suggest that the selection of 2nd and 3rd accommodation mechanisms is also affected by the β chemical stability.

The hierarchical structures of primary, secondary and tertiary 332T, at multiple length scales, construct a 'composite band' [1] under the uniaxial tensile load in Ti-12Mo-10Zr. The 332T bands have been proved to contribute to the strain hardening effect in TWIP Ti-alloys, which probably results from both the dynamic reduction of the mean free path for dislocation glide by the growing twinning network [2,4] and the mechanical contrast effect of the twins/matrix [4]. The shear strain concentration starting at a strain of 0.02 until 0.32 suggests that intensive dislocation slip and 332T happened in the same volume of the sample all along the tensile deformation to fracture. The 332T interface intersects the dislocation slip along (110), (112) or (123) planes as effective barriers, leading to intense stress concentration at the twin/matrix interfaces. In the absence of an efficient accommodation mechanism, such concentration will lead to damage and early nucleation of cracks at the twins/matrix interfaces. The proposed accommodation mechanism in Ti-12Mo-10Zr is a hierarchical sub-twinning mechanism to maintain the plastic flow strain up to $\epsilon_{\text{max}} = 0.5$ before fracture. The strain-hardening effect reflects the incremental dislocation density, which associates to the slip-twin interaction and the simultaneous augmentation of 1st 332T density. The hierarchical 332T twinning shows an auto-accommodated microstructure at each twinning level. It suggests that this hierarchical twinning mechanism can be comparable to the hierarchical microstructure reported in TRIP/TWIP Ti-Mo and Ti-V-Cr-Al alloy, in which 2nd martensite formed in the 1st 332T plays the role of accommodation to the local strain misfit [1,5]. In another Ti-Mo-Zr alloy with higher Zr content (Ti-13Mo-18Zr), this hierarchical twinning mechanism has also been observed as one of the accommodation mechanisms in addition to the [5 8 11]-type twinning at 332T boundaries [4]. These facts suggest that the activation of the hierarchical 332T could probably be dependent to alloy chemical composition. Owing to the hierarchical twinning accommodation, the Ti-12Mo-10Zr presents high tolerance to localized stress concentration.

**Disclosure statement**

No potential conflict of interest was reported by the author(s).

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