Possible evidence for a common radial structure in nearby AGN tori

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ABSTRACT

We present a quantitative and relatively model-independent way to assess the radial structure of nearby AGN tori. These putative tori have been studied with long-baseline infrared (IR) interferometry, but the spatial scales probed are different for different objects. They are at various distances and also have different physical sizes that apparently scale with the luminosity of the central engine. Here we look at interferometric size information, or visibilities, as a function of spatial scales normalized by the size of the inner torus radius $R_{\text{in}}$. This approximately eliminates luminosity and distance dependence and, thus, provides a way to uniformly view the visibilities observed for various objects and at different wavelengths. We can construct a composite visibility curve over a wide range of spatial scales if different tori share a common radial structure. The currently available observations do suggest, independent of models, a common radial surface brightness distribution in the mid-IR that is roughly of a power-law form $r^{-\alpha}$ as a function of radius $r$ and extends to $\sim 100$ times $R_{\text{in}}$. Taking into account the temperature decrease toward outer radii with a simple torus model, this corresponds to the radial surface density distribution of dusty material directly illuminated by the central engine roughly in the range between $r^{3}$ and $r^{-1}$. This should be tested with further data.

Key words. galaxies: active – galaxies: Seyfert – infrared: galaxies – techniques: interferometric

1. Introduction

Speckle and long-baseline interferometry in the infrared (IR) has started to explore the spatial structure of the putative tori in active galactic nuclei (AGN, e.g. Wittkowski et al. 1998; Weinberger et al. 1999; Swain et al. 2003; Weigelt et al. 2004; Jaffe et al. 2004; Wittkowski et al. 2004; Meisenheimer et al. 2007; Tristram et al. 2007). However, the number of long baselines per object is still generally limited, and a given baseline probes different spatial scales for targets at various distances and having different physical sizes. Here we investigate the possibility of uniformly viewing these interferometric measurements taken for various objects spanning different wavelengths, by studying them as a function of spatial scales in units of torus inner radius.

2. Composite radial structure

2.1. Spatial frequency per inner torus radius

The radius $R_{\text{in}}$ of the inner boundary of the torus dust distribution is thought to be set by dust sublimation. In this case, for a given sublimation temperature and grain size distribution, $R_{\text{in}}$ is expected to be proportional to $L^{1/2}$, where $L$ is the UV/optical luminosity of the central engine (e.g. Barvainis 1987). This proportionality has recently been confirmed by Suganuma et al. (2006) through near-IR reverberation measurements. These provide the inner torus radius as the light travel distance for the time lag between the variability in the optical and the near-IR. It is conceivable that the dust temperature structure within the torus is primarily determined by the illumination from the central source and is, thus, also expected to scale with $L^{1/2}$. In this case, if we view various pieces of interferometric size information as a function of spatial scales normalized by $R_{\text{in}}$, at least the primary luminosity dependence of the data is eliminated, along with the distance dependence.

A direct observable in an interferometric measurement is the visibility, or the normalized Fourier amplitude of the brightness distribution of a source, as a function of spatial scales (or spatial wavelength; see below) given in angular size. Here we normalize the spatial scale by the angular size of $R_{\text{in}}$. More precisely, the Fourier component is studied as a function of spatial frequency, i.e. the number of spatial cycles in a given angular size. Thus we study the visibilities as a function of the number of spatial cycles in $R_{\text{in}}$ or spatial frequency per $R_{\text{in}}$.

For a given projected baseline $b$ in m, observing wavelength $\lambda$ in $\mu$m and $R_{\text{in}}$ in milli-arcsecond (mas), the spatial frequency in cycles per $R_{\text{in}}$, written here as $u \cdot R_{\text{in}}$ (where $u$ is a spatial frequency per mas), is given as

$$u \cdot R_{\text{in}} = 4.85 \times 10^{-3} \frac{b \text{ (m)}}{\lambda \text{ (m)}} \cdot R_{\text{in}} \text{ (mas)} \quad \text{(cycles per } R_{\text{in}}).$$

(1)

The corresponding spatial wavelength $\Lambda$, i.e. the reciprocal of spatial frequency $u$, is given in units of $R_{\text{in}}$ as

$$\Lambda/R_{\text{in}} = 2.06 \times 10^{-2} \frac{\lambda \text{ (m)}}{b \text{ (m)}} \cdot \frac{1}{R_{\text{in}} \text{ (mas)}}.$$

(2)

This corresponds to the representative spatial resolution of the configuration ($b$ and $\lambda$). For simple geometries, the visibility takes the first null at a spatial wavelength $\Lambda$ roughly equal to the characteristic size (e.g. diameter of an uniform disk or a ring). The quantity $\Lambda$ can also be compared directly to the diffraction limit of $2.5 \times 10^{-2}$ (mas) $\lambda(\mu$m)/$D$(m) for a single aperture diameter $D$. We will study visibilities as a function of these two quantities, $u \cdot R_{\text{in}}$ and $\Lambda/R_{\text{in}}$.

An accurate scale length for the inner boundary radius $R_{\text{in}}$ has not been well determined yet. As the most plausible, observationally motivated quantity, we adopt the one obtained from the near-IR reverberation time-lag radii, or if not available, the overall fit to them as a function of UV/optical luminosity $L$ given by Suganuma et al. (2006). In the latter case, the angular size for
the time-lag radius is given as a function of observed flux $f_v$ in $V$-band as (the same as Eq. (4) in Kishimoto et al. 2007)

$$R_{in} = 0.43 \left[ f_v(V)/(50\, \text{mJy}) \right]^{1/2} \text{(mas)} \quad (3)$$

We note that the time-lag radius is actually a factor of $\sim 3$ smaller, for a given luminosity $L$, than the sublimation radius given by Barvainis (1987) assuming graphite grains with radial size $a = 0.05\, \mu$m and sublimation temperature $T_{sub} = 1500\, \text{K}$.

The possible reasons for this difference have been discussed by Kishimoto et al. (2007), including the possibility that $R_{in}$ is determined by much larger grains. As we discuss below, the reverberation radius is supported by the near-IR interferometry of NGC 4151 (Swain et al. 2003). The uncertainty in the time-lag radius is $\sim 0.2\, \text{dex}$, based on the scatter of the fit.

### 2.2. Data

The most suitable data for the radial structure study are those for type 1 AGNs. In these objects, the tori are thought to have much smaller inclinations than in type 2 AGNs, so that the radial structure can be studied without a significant orientation effect. We would also expect that the dependence on the exact PAs of the projected baselines is relatively small (the torus image projected onto the sky would not be far from circular-symmetric; see below). Those type 1 objects for which long-baseline IR interferometric data are found in the literature or archive are listed in Table 1, along with the adopted size for the time-lag radius is given as a function of observed flux $f_v$ in $V$-band as (the same as Eq. (4) in Kishimoto et al. 2007)

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### 2.3. Mid-IR surface brightness distribution

Figure 1 shows the visibility data listed in Table 1 as a function of spatial frequency per inner torus radius. The red/yellow/green colors correspond to from 13 to 8.2 $\mu$m and purple corresponds to 2.2 $\mu$m. The mid-IR data are binned with $\Delta \lambda \sim 0.4\, \mu$m. The arrows are to show that the NGC 1068 data are taken as the lower limit for the visibilities of type 1s at the same spatial frequencies. Visibility curves for various simple geometries are also plotted; three dashed curves, power-law with index $-2.0$, $-2.1$, and $-1.5$ from top to bottom; dotted, Gaussian with HWHM 25 $R_{in}$; dot-dashed, ring with radius $R_{in}$. The flux and correlated flux were estimated from the fluctuation of the measurements over time. For the targets with a few available total-flux measurements, we took weighted means. The errors for the final visibilities were obtained from the estimated errors in the correlated flux and total flux (except for NGC 1068, where the errors were estimated from the scatter of several available visibility measurements).
inclinations), the visibilities are expected to generally decrease, since the bright inner radiation becomes obscured and this effectively makes the overall size of the intensity distribution larger. (Here we are restricting our discussion to the spatial frequencies within the first lobe, i.e., those less than the one at which the visibility reaches the first null.) On the other hand, this decrease is expected to be quite small at long wavelengths, such as in the mid-IR, due to much weaker obscuration effects. Therefore, the mid-IR visibilities of the type 2 AGN NGC 1068 provide a meaningful lower limit for those of the type 1 objects at the same spatial frequencies (indicated by the upward arrows in Fig. 1).

If we put together the lower limit from NGC 1068 with the visibilities observed for the type 1 AGNs in the mid-IR (Fig. 1), the data at different spatial frequencies appear quite coherent, i.e., consistent with the case where these objects roughly share a common radial brightness distribution in face-on inclinations. When compared with various model curves shown in Fig. 1, the mid-IR brightness distribution appears to be consistent with a power-law form, where the index is $\sim -2$ at $\sim 8$ $\mu$m.

The visibility functions for power-law distributions shown in Fig. 1 are for the cases with the outer cut-off radius $R_{\text{out}} = 100R_{\text{in}}$. For the power-law distributions with index $\geq -2$, $R_{\text{out}}$ changes the shape of visibility functions, especially at low spatial frequencies. Here, the data at high spatial frequencies (NGC 1068 and the longer baseline data for NGC 3783) roughly fix the power law index. Then the low spatial frequency data further constrain $R_{\text{out}}$, which corresponds to the outer radius of the mid-IR emission region, to be roughly $\sim 100R_{\text{in}}$ (see also Sect. 3).

To be the least sensitive to the possible dependency of the visibilities on the position angle (PA) of the projected baseline, we would ideally want to compare the visibilities of each object and of different objects measured at the major axis direction of the torus projected on to the sky. The minor axis PA can be estimated from a linear radio jet structure ($\sim 77^{\circ}$ for NGC 4151, Mundell et al. 2003; $\sim 0^{}$ for NGC 1068, e.g. Gallimore et al. 2004) or optical polarization PA ($\sim 136^{}$ for NGC 3783, Smith et al. 2002; $\sim 40^{}$ for Mrk1239, Goodrich 1989). The PA difference between the projected baseline and the expected major axis is listed in Table 1. Unfortunately, these relative PAs are not uniform for the data gathered here; however, they do not seem to disturb the composite visibility diagram shown in Fig. 1, which might indicate that the PA dependence is small as we expect and assumed here for type 1s. Further data are needed to address this issue. The two data sets for the type 2 object NGC 1068 have quite different PAs, which is probably adequate for obtaining lower limits for type 1 visibilities.

The only existing near-IR measurement for type 1 AGNs, i.e. the one for NGC 4151 (Fig. 1, purple cross), is consistent with a ring of radius $R_{\text{in}}$. It is quite expected that the torus shows a much more compact structure in the near-IR than in the mid-IR, since the former reflects the distribution of materials at higher temperatures. For a given inner boundary radius $R_{\text{in}}$, the ring model essentially represents the most compact structure, giving the upper limit for the visibilities. This essentially means that $R_{\text{in}}$ generally cannot be much larger than assumed here; the observed data points would move to the right in Fig. 1 if we adopt larger $R_{\text{in}}$ for each object, which would exceed the upper limit given by the $R_{\text{in}}$ ring. Future near-IR data at high spatial frequencies are crucial to settle this issue.

We should in principle correct the observed visibility for the possible contribution from the unresolved accretion disk in the near-IR to estimate the intrinsic visibility of the torus alone. The correction depends on the estimate of the near-IR flux fraction from the disk, which in turn depends on the assumed near-IR spectral shape of the accretion disk. The correction, however, is estimated to be very small (less than 5% reduction; Kishimoto et al. 2007), as long as the disk spectrum is bluer than observed in the UV/optical, which seems quite likely (e.g. Kishimoto et al. 2008).

All the visibility functions shown in Fig. 1 reach the first null at a spatial wavelength $A \sim a few R_{\text{in}}$ (outside the figure) due to the inner boundary diameter being $2R_{\text{in}}$ in the mid-IR. Detailed intensity distributions in the inner few $R_{\text{in}}$ region will not affect the overall visibility curves significantly, since a major fraction of the mid-IR radiation originates from larger regions. To discuss whether the same model can account for both the mid-IR and near-IR data, we need a physical torus model.

3. Torus model

We aim here to generically describe the torus surface brightness distribution with as few parameters as possible. In various torus models, two types of distributions have been considered; namely, smooth and clumpy distributions (e.g. Pier & Krolik 1992, 1993; Granato & Danese 1994; Efstathiou & Rowan-Robinson 1995; Nenkova et al. 2002; Dullemond & van Bemmel 2005; Schartmann et al. 2005; Hönig et al. 2006; Schartmann et al. 2008). We first consider the latter and assume that the torus consists of various discrete optically-thick dust clouds. The constraints from the alternative case of smooth dust distribution will be considered later below.

The near- and mid-IR torus radiation is primarily dominated by that from those clouds that are directly illuminated by the central engine (e.g. Hönig et al. 2006). We can then approximately parameterize the face-on surface brightness distribution $S_{\nu}(r)$ at an observing frequency $\nu$ as a function of radius $r$ as

$$S_{\nu}(r) = I_{\nu}(T_{\text{max}}(r)) \cdot (r/R_{\text{in}})^{\alpha}. \quad (4)$$

The first term, $I_{\nu}$, is the intensity from an illuminated cloud as a function of $T_{\text{max}}(r)$, which is the maximum temperature of the dust grains at radius $r$ written as

$$T_{\text{max}} = T_{\text{sub}} \cdot (r/R_{\text{in}}) \cdot \frac{1}{\lambda}. \quad (5)$$

This is derived from the thermal equilibrium of a dust grain and involves the wavelength dependency of the absorption efficiency of the grain in the form of its spectral index $\gamma$ in the infrared (Barvains 1987). For the large grain limit, $\gamma = 0$, while $\gamma \sim 1.6$ for the standard interstellar material (ISM) dust grains. The sublimation temperature $T_{\text{sub}}$ is taken here as 1500 K, but our conclusions below are not sensitive to the exact value of $T_{\text{sub}}$. The specific intensity $I_{\nu}$ from an illuminated dust cloud needs to be obtained with a proper radiative transfer calculation, but is approximately of the form

$$I_{\nu} = \int e^{\tau_{B_{\nu}}} B_{\nu}(T(r)) \, d\tau \quad (6)$$

for an optically thick cloud, where $T(r)$ is the temperature of the dust grains at an optical depth $\tau$ from the surface of the cloud, and $B_{\nu}(T)$ is the Planck function. At a given observing frequency, however, we can assume that the intensity distribution over the torus radius, $I_{\nu}(r)$, approximately scales with $B_{\nu}(T_{\text{max}}(r))$. The second term in the expression for $S_{\nu}(r/R_{\text{in}})^{\alpha}$, describes the distribution of the normalized surface density, or the filling factor per unit area, of the illuminated material as a power-law
form. An implicit assumption here is that the dust cloud distribution in the innermost region is opaque so that $S_r(R_\text{in}) = I_\text{v}(T_{\text{sub}})$, and this is the maximum brightness so that $\alpha \leq 0$.

In this way, we can model the visibilities as a function of the parameter $\alpha$ for an assumed dust grain size distribution fixed by $\gamma$. We consider the two cases above, namely, the large grain limit ($\gamma = 0$) and the ISM case ($\gamma = 1.6$). For each case, we can estimate an adequate density index $\alpha$ for roughly reproducing the visibilities observed in the $8-13$ $\mu$m range. We show in Fig. 2 such representative curves where $\alpha$ is taken to be 0.0 and $-0.9$ for the $\gamma = 0$ and 1.6 cases, respectively. We estimate the uncertainties in these indices to be $0.3$, based on the uncertainty in the visibility measurements and also in $R_\text{in}$ ($-0.2$ dex; see Sect. 2.1).

All the curves shown in Fig. 2 have been calculated with an outer boundary of 100 $R_\text{in}$. The results do not change significantly if a larger outer boundary is adopted (the region outside $100R_\text{in}$ contains only a small fractional amount in the mid-IR). Therefore, in the $100R_\text{in}$ cases adopted here, the outer boundary is set almost by the temperature distribution, rather than the density distribution of the illuminated material.

Let us briefly consider the case of smooth dust distribution. If the opening angle of the geometrical distribution is constant over the radii, i.e. if there is no geometrical flaring, the material at large radii is illuminated only by the attenuated radiation from the central engine. Then $I_\text{v}$ would represent the intensity from the dust grains at radius $r$ where the distribution of the maximum temperature $T_{\text{max}}(r)$ is steeper (decreasing more quickly with radius) than considered for the clumpy case above. Therefore, the normalized surface density distribution, $(r/R_\text{in})^\alpha$, has to be shallower, closer to the upper limit of $\alpha = 0$. If there is a geometrical flaring, then we would revert to considering the directly illuminated surface at each radius, leading to essentially the same conclusions as for the clumpy case.

As for the consistency with the near-IR data, the large-grain case produces slightly more compact distributions in the near-IR than the ISM case (because the temperature distribution is steeper), and is marginally consistent with the NGC 4151 data. Thus the large grain case is slightly favored here. We note that the large-grain case is consistent with the small innermost radii suggested by the near-IR reverberations, though other contributing factors are not ruled out (Kishimoto et al. 2007). While we would need a more detailed modeling of the surface brightness distribution for the innermost region, we also need more observational data in the near-IR to constrain such detailed models.

### 4. Conclusions

The long-baseline IR interferometry data for AGN tori are still generally limited in $uv$ coverage for each target. The data for various objects probe different spatial scales. We argue that one way to uniformly study these various data is to view them as a function of spatial frequency per torus inner boundary radius $R_\text{in}$, or spatial scale in units of $R_\text{in}$. In this way, primarily using the data for type 1 AGNs, we tried to construct a composite visibility function over a wide range of spatial scales and investigated the radial structure of the tori. The data obtained so far suggest a common radial distribution of the face-on surface brightness in the mid-IR that approximately has a power-law form with index $-\sim 2$ and extends to $\sim 100R_\text{in}$. Considering the temperature distribution of the dust grains, this corresponds to the surface density distribution of the directly illuminated material ranging approximately between $r^\alpha$ and $r^{-1}$. We aimed here to derive direct constraints with a simple model. Further data are definitely needed over the wavelengths from the near-IR to mid-IR to test the composite visibility function and to further constrain models.

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1 We note that, if indirect heating from the re-emission of dust grains is important, the temperature distribution $T_{\text{max}}(r)$ becomes less steep, so that the constraint difference from the clumpy case will be smaller.