Non-polarizing broadband multilayer reflectors in fish

T. M. Jordan1,2, J. C. Partridge1 and N. W. Roberts1*

Dielectric multilayer reflectors that are non-polarizing are an important class of optical device and have numerous applications within optical fibres1, dielectric waveguides2 and light-emitting diodes3. Here, we report analyses of a biological non-polarizing optical mechanism found in the broadband guanine-cytoplasm ‘silver’ multilayer reflectors of three species of fish. Present in the fish stratum argenteum are two populations of birefringent guanine crystal, with their optical axes either parallel to the long axis of the crystal or perpendicular to the plane of the crystal, respectively. This arrangement neutralizes the polarization of reflection as a result of the different interfacial Brewster’s angles of each population. The fish reflective mechanism is distinct from existing non-polarizing mirror designs4–7 in that, importantly, there is no refractive index contrast between the low-index layers in the reflector and the external environment. This mechanism could be readily manufactured and exploited in synthetic optical devices.

Multilayer reflectors occur extensively in nature. They are used by animals to create iridescent signals for communication8, crypsis for camouflage9 and as reflectors to increase low light sensitivity in many eyes10. Silvery reflections from fish are produced by multilayer ‘stacks’ of high-refractive-index guanine crystals separated by low-refractive-index cytoplasm gaps11. Many fish have two separate forms of these stacks: (i) those in the stratum argenteum, a subdermal layer of the skin, and (ii) those that lie on the surface of teleost scales. We used a digital holographic transmission microscope to measure the ratio of the refractive indices along two planar crystal axes (see Methods for a description of the experimental set-up). We measured the specular component of reflection at an angle of 10° for ideal flat sample to be ~1% by measuring $d(\theta)$ for a glass microscope slide and comparing our measured values to theoretical values for double-image Fresnel equations21 (Fig. 1a). Both fish data sets have maximum polarization values of ~0.35 at $\theta = 60°$, suggesting that the polarization behaviour is near-independent of axis of rotation. At all angles of incidence the reflection spectra are broadband with no gaps in the high reflectance region (Fig. 1b,c). Measurements from samples of S. pilchardus exhibit very similar generic reflection and polarization behaviour (Supplementary Fig. S1).

All previous multilayer models of fish reflectors10,15,19,20 assume that the crystals behave as optically isotropic layers with a refractive index of ~1.83. These crystals, however, are in fact highly birefringent, being a mixture of pure guanine and hypoxanthine, which have refractive indices of (1.93, 1.91, 1.47) and (1.85, 1.78, 1.42)22. The guanine–hypoxanthine ratio varies between fish, with the crystals found in C. harengus reported to have refractive index values of (1.85, 1.81, 1.46)13,22. It has conventionally been thought that the optical axes of the crystals all have a common orientation in the multilayer structure, with the low refractive index value aligned with the short axis of the crystal and the direction of stacking (by convention, the z-axis)13. However, it has recently been demonstrated that the relative axial growth rate of crystals in fish is subject to biological control mechanisms, changing the optic axis of the crystal23. This motivated us to re-examine the optical properties of individual guanine crystals from the stratum argenteum and the inner surface of teleost scales. We used a digital holographic transmission microscope to measure the ratio of the refractive indices along the two planar crystal axes (see Methods for a description of this technique).

In three species of clupeid teleost we identified two distinct populations of guanine crystals that are morphologically identical but have different optical properties. In the stratum argenteum there are both Type 1 and Type 2 crystals, which have planar refractive index ratios of ~1.025 and ~1.250, respectively (Fig. 2 and Supplementary Fig. S2). Under the scales, only Type 1 crystals exist, but these crystals have a different lower-aspect-ratio morphology compared with the crystals from the argenteum. These differences in shape have been reported previously by

\[
d(\lambda, \theta) = \left( \frac{R_s - R_p}{R_s + R_p} \right)
\]

for reflected light. In accordance with previous studies17,18, the polarization by reflection is very different to a Fresnel dielectric with low polarization across all wavelengths and at all angles of incidence. Measurements of $d(\theta)$ at $\lambda = 600\text{nm}$ about the azimuthal (dorsoventral) and latitudinal (rostrocaudal) axes of illumination for C. harengus are shown in Fig. 1a. We estimated the percentage error of the experimental arrangement for an ideal flat sample to be ~1% by measuring $d(\theta)$ for a glass microscope slide and comparing our measured values to theoretical values for double-image Fresnel equations21 (Fig. 1a). Both fish data sets have maximum polarization values of ~0.35 at $\theta = 60°$, suggesting that the polarization behaviour is near-independent of axis of rotation. At all angles of incidence the reflection spectra are broadband with no gaps in the high reflectance region (Fig. 1b,c). Measurements from samples of S. pilchardus exhibit very similar generic reflection and polarization behaviour (Supplementary Fig. S1).

Initially, we used reflectance spectrophotometry to characterize the polarization dependence of the reflectivity from two species of fish, Clupea harengus (Atlantic herring) and Sardina pilchardus (European sardine); see Methods for details of the experimental set-up. We measured the specular component of reflectivity for light polarized perpendicular and parallel to the plane of incidence, $R_p(\lambda, \theta)$ and $R_s(\lambda, \theta)$, and calculated the degree of polarization:

\[
\]
index vectors for each population are given by ratio \( f \) assigned a ‘population state’, with their associated refractive indices. Each crystal layer was randomly in Fig. 3a, illustrating the two populations of guanine crystals and approximated as uniaxial birefringent planar layers with ordinary in the Methods). In this model, the weakly biaxial crystals were two populations of crystals (details of the theory are provided in the reflectivity of a guanine–cytoplasm multilayer containing these measurements of \( \theta \).

Denton and Nicol\textsuperscript{12} and Denton\textsuperscript{13}. It is also worth noting here that although the opercula (gill covers) of both fish species have no scales, the skin contains both physical shapes of the Type 1 crystals as well as Type 2 crystals. In agreement with the literature\textsuperscript{13,22}, our measurements of Type 1 crystals imply that the low refractive index value is aligned with the \( z \)-axis. The measurements for Type 2 crystals are very different from the optical properties reported to date and imply that the low refractive index value is orientated in the \( x\text{-}y \) plane.

We used the anisotropic \( 4 \times 4 \) matrix technique\textsuperscript{24,25} to calculate the reflectivity of a guanine–cytoplasm multilayer containing these two populations of crystals (details of the theory are provided in the Methods). In this model, the weakly biaxial crystals were approximated as uniaxial birefringent planar layers with ordinary refractive index \( n_o \) = 1.83 and extraordinary refractive index \( n_e \) = 1.46. A schematic example of the modelled structure is presented in Fig. 3a, illustrating the two populations of guanine crystals and their associated refractive indices. Each crystal layer was randomly assigned a ‘population state’, with Type 1 crystals having mixing ratio \( f \) and Type 2 crystals having mixing ratio \( 1-f \). Refractive index vectors for each population are given by

\[
\text{Type 1} \quad n_g = (n_o, n_c, n_e)
\]

where \( \phi \) is a uniformly distributed random variable on the interval \([0, \pi]\), and \( n_o \) and \( n_e \) are the ordinary and extraordinary refractive indices, respectively. The isotropic cytoplasm layers and the external environment (water) both have a refractive index of 1.33 (ref. 19).

The broad bandwidth of our reflection spectra are best accounted for by assuming that the thicknesses of the guanine and cytoplasm layers can be modelled as uniformly distributed random variables\textsuperscript{15}. Our model used a thickness sampling interval of \([55, 110] \) nm for the thickness of the guanine crystals\textsuperscript{14}, with the bounds for cytoplasm layer thicknesses allowed to vary freely over physiologically plausible values\textsuperscript{15}. The in \( x\text{-}y \)-plane symmetry of the reflection spectra in Fig. 1a indicates rotational invariance of the macroscopic structure, so we averaged over 500 multilayer structures to account for variation at the microscopic scale (as modelled).

Our optical model predicts that multilayers with only Type 1 crystals \( (f=1) \) have a fully polarizing Brewster’s angle at 67° (black line in Fig. 3b). This polarization behaviour is anticipated by the anisotropic interfacial reflection coefficients for each individual layer\textsuperscript{26}, which have a Brewster’s angle \( \theta_B \) given by the relation

\[
\tan(\theta_B) = \frac{n_{g,c}}{n_{g,z}} \sqrt{\frac{n_c^2 - n_g^2}{n_z^2 - n_g^2}}
\]

where subscripts \( c \) and \( g \) indicate cytoplasm or guanine and subscripts \( x \) and \( z \) indicate Cartesian components\textsuperscript{27}. This is standard Fresnel behaviour and is similar to that occurring if the crystals are assumed to be isotropic, in which case equation (4) reduces to \( \tan(\theta_B) = (n_g/n_c) \) and Brewster’s angle is at 53° (blue line in Fig. 3b). However, when there are two populations of crystal present in the multilayer structure, low-polarization reflections over all angles of incidence can occur. We applied a parametric grid search to the experimental data from C. harengus in Fig. 1a,
The degree of polarization is demonstrated in Fig. 4a, which indicates a monotonic variation in the optical thickness of the layers. Highly birefringent polymers with similar refractive indices to the fish have already been used in multilayer mirror designs, although these studies do not discuss the production of non-polarized reflections through two different populations of birefringent layers.

The polarization properties of a biomimetic design that replaces the two populations of crystals with two uniaxially birefringent populations of layers with refractive indices (1.83, 1.83, 1.33) and (1.33, 1.33, 1.83) are illustrated in Fig. 4c,d. This biomimetic design captures the essential physics of the fish reflective mechanism, but improves the efficiency of polarization neutralization by maximizing the disparity between the interferential Brewster’s angles of the two populations (equation (4)). It is important to be clear that the mechanism of polarization-neutral reflections described here is radically different from that of photonic-bandgap based non-polarizing mirrors. Unlike existing non-polarizing reflectors, the biomimetic design permits the environmental media and low-index layers to be made from the same material, and would provide an advantage in applications where the thermal and mechanical properties of the reflector benefit from being constructed with the same material externally and within the structure.

Figure 3 | Optical structure, modelling and parametric fit to experimental data. a, Schematic illustrating the multilayer model used and the two populations of guanine crystals: Type 1 crystals (purple) and Type 2 crystals (orange). The orientation of the principle refractive indices’ coordinate axes in each crystal layer are indicated. b, Simulations of the degree of polarization $d(\theta)$ at different angles of incidence $\theta$ and at $\lambda = 600$ nm for three classes of multilayer model, including a parametric fit to experimental data from Clupea harengus. The black line is for a multilayer of Type 1 crystals ($f = 1$), the blue line is for isotropic crystals ($n_o = n_e = 1.83$), and the solid red line is a parametric best fit for a mixture of Type 1 and Type 2 crystals with $f = 0.75$. The red crosses are the mean of the azimuthal and latitudinal data from Fig. 1a. Our model explained 95% of the variation in the data, assessed by the $R^2$ from linear regression. There was no systematic difference between model and data (mean pairwise difference and standard deviation (s.d.) = 0.0044 ± 0.0132, $t = 0.7512$, d.f. = 9, $P = 0.472$) (red solid in line in Fig. 3b; see Supplementary Fig. S1 for a similar analysis of data from S. pilchardus). The values of $N$ for the parametric fits for both fish are in excellent agreement with past histological surveys. Figure 3c further shows the similar agreement between the experiment and modelled results for both $\theta = 30^\circ$ (black lines) and $\theta = 60^\circ$ (red lines) as a function of wavelength. The reason underlying this non-trivial polarization behaviour is the different interfacial Brewster’s angles between the isotropic layers and either the Type 1 crystals or the different orientations in the plane of the Type 2 crystals, which can lie anywhere in the interval $[33^\circ, 53^\circ]$ (equation (4)). One further possible explanation for this polarization behaviour that has been considered is polarization mode mixing in the multilayer structure. With changes in polarization occurring due to the changing orientation of the optical axes of the birefringent layers, a contribution might always exist perpendicular to the plane of incidence and therefore be reflected. However, we have both experimentally measured and theoretically calculated (using the best-fit parameters above) both $R_{\sigma \sigma}$ and $R_{\pi \pi}$ for C. harengus (Supplementary Fig. S3). In both the experimental measurements and optical modelling, the contributions of these cross terms are extremely small and cannot account for the polarization response of the structure.

Clearly, the real biological multilayer reflectors of C. harengus and S. pilchardus are weakly polarizing. However, by increasing the number of layers in the multilayer structure, the optical mechanism can produce true polarization-neutral reflections. This property is demonstrated in Fig. 4a, which indicates a monotonic decrease in the degree of maximum polarization with increasing $N$, and Fig. 4b, which shows a reflectance band for both $\sigma$ and $\pi$ polarizations approaching 100% reflectivity at $\theta = 60^\circ$ (which is approximately the angle of highest polarization). Natural photonic structures are proving to be of inspiration for optical technologies, with the organization of birefringent materials in animals leading to the fabrication of novel biomimetic devices. Common to all existing non-polarizing mirror designs is the use of a refractive-index contrast between the low-index layers in the reflector and the external environment (for example, refs 4–7), which enables the reflector to be screened from angles of incidence where polarization occurs. The fish reflective mechanism places no such restriction, and is instead dependent on having both birefringent layers with different interfacial Brewster’s angles and there being a high variation in the optical thickness of the layers. Highly birefringent polymers with similar refractive indices to the fish have already been used in multilayer mirror designs, although these studies do not discuss the production of non-polarized reflections through two different populations of birefringent layers. The polarization properties of a biomimetic design that replaces the two populations of crystals with two uniaxially birefringent populations of layers with refractive indices (1.83, 1.83, 1.33) and (1.33, 1.33, 1.83) are illustrated in Fig. 4c,d. This biomimetic design captures the essential physics of the fish reflective mechanism, but improves the efficiency of polarization neutralization by maximizing the disparity between the interferential Brewster’s angles of the two populations (equation (4)). It is important to be clear that the mechanism of polarization-neutral reflections described here is radically different from that of photonic-bandgap based non-polarizing mirrors. Unlike existing non-polarizing reflectors, the biomimetic design permits the environmental media and low-index layers to be made from the same material, and would provide an advantage in applications where the thermal and mechanical properties of the reflector benefit from being constructed with the same material externally and within the structure.

Figure 3a shows the multilayer model used and the two populations of guanine crystals: Type 1 crystals (purple) and Type 2 crystals (orange). The orientation of the principle refractive indices’ coordinate axes in each crystal layer are indicated. Figure 3b shows simulations of the degree of polarization $d(\theta)$ at different angles of incidence $\theta$ and at $\lambda = 600$ nm for three classes of multilayer model, including a parametric fit to experimental data from Clupea harengus. The black line is for a multilayer of Type 1 crystals ($f = 1$), the blue line is for isotropic crystals ($n_o = n_e = 1.83$), and the solid red line is a parametric best fit for a mixture of Type 1 and Type 2 crystals with $f = 0.75$. The red crosses are the mean of the azimuthal and latitudinal data from Fig. 1a. Our model explained 95% of the variation in the data, assessed by the $R^2$ from linear regression. There was no systematic difference between model and data (mean pairwise difference and standard deviation (s.d.) = 0.0044 ± 0.0132, $t = 0.7512$, d.f. = 9, $P = 0.472$) (red solid in line in Fig. 3b; see Supplementary Fig. S1 for a similar analysis of data from S. pilchardus). Figure 3c further shows the similar agreement between the experiment and modelled results for both $\theta = 30^\circ$ (black lines) and $\theta = 60^\circ$ (red lines) as a function of wavelength. The reason underlying this non-trivial polarization behaviour is the different interfacial Brewster’s angles between the isotropic layers and either the Type 1 crystals or the different orientations in the plane of the Type 2 crystals, which can lie anywhere in the interval $[33^\circ, 53^\circ]$ (equation (4)). One further possible explanation for this polarization behaviour that has been considered is polarization mode mixing in the multilayer structure. With changes in polarization occurring due to the changing orientation of the optical axes of the birefringent layers, a contribution might always exist perpendicular to the plane of incidence and therefore be reflected. However, we have both experimentally measured and theoretically calculated (using the best-fit parameters above) both $R_{\sigma \sigma}$ and $R_{\pi \pi}$ for C. harengus (Supplementary Fig. S3). In both the experimental measurements and optical modelling, the contributions of these cross terms are extremely small and cannot account for the polarization response of the structure.

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In the context of an animal’s visual ecology, to perfectly background-match an axially symmetric light field over all angles of incidence, any vertical dielectric reflector must produce non-polarizing broadband reflections, as well as having high reflectivity. By producing a high degree of polarization neutrality for reflections over all angles of incidence, the mechanism discovered in these species of fish ensures a greater total reflected intensity that more closely matches the open water background light field. Although previous works have emphasized how the spectral properties of biological multilayer structures arise and the relationship that this has to biological function\(^1\), our study exposes the fact that, provided one of the constituent materials has high birefringence, polarization properties, as well as spectral properties, can play a role in their structural organization. It is an intriguing possibility that the selection of polarization properties in the biological reflectors examined in this work are a direct adaptation to better intensity-match the pelagic light environment. It is worth adding that several aquatic animals including fish, cephalopods and crustaceans have polarization vision\(^3\). In an axisymmetric light environment, a consequence of a non-polarizing mechanism of intensity-matching is that the reflector also matches the polarization of the background\(^3\). Finally, it is likely that birefringence is key to the optical properties of other animal multilayer reflectors. The optical properties of silver reflectors in certain cephalopods\(^4\) and the polarizing guanine–cytoplasm structures in the tapeta of some spiders\(^5\) both still require explanation.

**Methods**

*Reflectance spectrophotometry.* Thin areas of fish skin and underlying tissue \(\sim 3 \text{ mm in thickness and } 30 \times 30 \text{ mm}^2\) in size were taken from the vertical lateral flank of each animal and mounted on a black perspex slide. Data were recorded from 300 to 900 nm for the birefringent layers and from 30 to 300 nm for the isotropic layers, with \(f = 0.75\) and the \((1.83, 1.83, 1.33)\) layers being defined as Type 1 in the biomimetic design.

**Figure 4** | A biologically inspired mechanism of polarization-neutral reflection. a–d. Simulated degree of polarization \(\delta(\theta)\) at different angles of incidence \(\theta\) and \(\lambda = 600 \text{ nm for } N = 20, 40, 200, 400 \text{ crystal layers (red, black, blue and green solid lines, respectively) and accompanying reflection and polarization spectra at } 60^\circ\text{ for the fish reflective structure (}a, b\text{) and a biomimetic design (}c, d\text{) with two uniaxial populations of layers with refractive indices given by } (1.83, 1.83, 1.33) \text{ and } (1.33, 1.33, 1.83), N = 400 \text{ in } \textbf{b} \text{ and } N = 200 \text{ in } \textbf{c}. \text{ The black solid line is } R_o(\lambda) \text{ and the green solid line is } \delta(\lambda). \text{ In all plots the layer thicknesses are sampled from uniform distributions on the intervals } [55, 110] \text{ nm for the birefringent layers and } [30, 300] \text{ nm for the isotropic layers, with } f = 0.75 \text{ and the } (1.83, 1.83, 1.33) \text{ layers being defined as Type 1 in the biomimetic design.}

Digital holographic microscopy. We isolated the individual crystals using the methods described by Denton and Land\(^6\). We measured the phase retardation parallel and perpendicular to the long axis of the crystal (indicated by red and black arrows in Supplementary Fig. S2a,b) using a digital holographic microscope. A detailed description of the technique is set out by Colomb and colleagues\(^8\). We made six separate measurements of the phase retardation parallel and perpendicular to the long axis of each crystal, and used the two retardations to calculate the mean planar refractive index ratio. For each species (and sample area) we measured 20 crystals, calculating the mean and standard deviation of measurements (Fig. 2).

Optical modelling. The optical model assumes that the guanine–cytoplasm stack can be approximated as a planar stratified medium with alternating isotropic and uniaxial birefringent layers. The coordinate system was chosen so that the \(z\)-axis was aligned with the direction of stacking and the \(\sigma\) polarization was aligned with the \(y\)-axis. Each crystal layer was orientated at a random planar angle \(\phi\), where \(\phi\) is a uniformly distributed random variable on \([0, \pi]\). The reflectivity was calculated using the \(4 \times 4\) matrix method\(^9,10\). In this formulation, the dielectric properties of each crystal layer are represented by the differential propagation matrix \(D_i\). For the Type 1 crystals this is of the form

\[
D_1 = \begin{pmatrix}
0 & 1 - n^2 \sin^2(\theta) & 0 \\
\varepsilon_{r} & 0 & 0 \\
0 & 0 & \varepsilon_{0} - n^2 \sin^2(\theta)
\end{pmatrix}
\]
and for Type 2 crystals it is of the form

\[ \Delta_2 = \begin{pmatrix} 0 & 1 - n_2^2 \sin^2(\theta) \cos^2(\phi) & 0 & 0 \\ 1 - n_2^2 \sin^2(\theta) \cos^2(\phi) & 0 & \frac{1}{2} (\epsilon_2^e - \epsilon_2^o) \sin(2\phi) & 0 \\ \frac{1}{2} (\epsilon_2^e - \epsilon_2^o) \sin(2\phi) & 0 & 0 & 0 \\ \epsilon_2^o \sin^2(\phi) + \epsilon_2^e \cos^2(\phi) & 0 & 0 & 0 \end{pmatrix} \]

where $\epsilon_2^o = n_2^2 \epsilon_2^e = n_2^2$ and $\eta_2$ is the refractive index of the incident medium, and $\theta$ is the angle of incidence. The isotropic cytoplasm layers have the same form of $\Delta$ matrix as Type 1 crystals, but with $\epsilon_1^o = n_1^2 \epsilon_1^e$ substituted for $\epsilon_2^e$ and $\epsilon_2^o$, respectively. The transfer matrices for each layer were obtained using the procedure described by Azzam and Bashara. The transfer matrix for the overall multilayer system was obtained by taking a matrix product over all layers, and reflectivity coefficients $R_{\pm} = R_{\pm o} + R_{\pm e}$ were then calculated using standard formulae. To equate the microscopic structure with the bulk optical response and simulate a representative model, we sampled and averaged over 500 multilayer structures.

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Author contributions

J.C.P. initiated the study. T.M.J and N.W.R. performed the modelling and experiments. All authors interpreted the data and co-authored the paper.

Additional information

Supplementary information is available in the online version of the paper. Reprints and permission information is available online at http://www.nature.com/reprints. Correspondence and requests for materials should be addressed to N.W.R.

Competing financial interests

The authors declare no competing financial interests.