Validation of a simplified scatter correction method for 3D brain PET with $^{15}$O

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Abstract

Objective Positron emission tomography (PET) enables quantitative measurements of various biological functions. Accuracy in data acquisition and processing schemes is a prerequisite for this. The correction of scatter is especially important when a 3D PET scanner is used. The aim of this study was to validate the use of a simplified calculation-based scatter correction method for $^{15}$O studies in the brain.

Methods We applied two scatter correction methods to the same $^{15}$O PET data acquired from patients with cerebrovascular disease ($n = 10$): a hybrid dual-energy-window scatter correction (reference method), and a deconvolution scatter correction (simplified method). The PET study included three sequential scans for $^{15}$O-CO, $^{15}$O-O$_2$, and $^{15}$O-H$_2$O, from which the following quantitative parameters were calculated, cerebral blood flow, cerebral blood volume, cerebral metabolic rate of oxygen, and oxygen extraction fraction.

Results Both scatter correction methods provided similar reconstruction images with almost identical image noise, although there were slightly greater differences in white-matter regions compared with gray matter regions. These differences were also greater for $^{15}$O-CO than for $^{15}$O-H$_2$O and $^{15}$O-O$_2$. Region of interest analysis of the quantitative parameters demonstrated that the differences were less than 10% (except for cerebral blood volume in white-matter regions), and the agreement between the methods was excellent, with intraclass correlation coefficients above 0.95 for all the parameters.

Conclusions The deconvolution scatter correction despite its simplified implementation provided similar results to the hybrid dual-energy-window scatter correction. We consider it suitable for application in a clinical $^{15}$O brain study using a 3D PET scanner.

Keywords PET • Scatter correction • Brain • $^{15}$O

Introduction

Positron emission tomography (PET) enables the quantification of various biological functions, and the use of $^{15}$O-labeled compounds allows estimates of cerebral blood flow (CBF) and oxygen metabolism [1–3]. The validity of quantitative results depends on the accuracy of the PET acquisition and data processing schemes, which include corrections for detector efficiency, scanner dead-time, random coincidences, photon attenuation, and photon scatter. Currently, all the commercially-available PET scanners employ 3D-acquisition mode in which scatter coincidences are greater than in conventional 2D-acquisition mode, where the scatter effect is marginal. A scatter correction is, therefore, essential to achieve accurate PET data with 3D scanners [4]. However, it is generally difficult to validate the accuracy of the scatter correction for human PET scans, because scatter-free ground-truth results are not known.

PET scatter correction methods fall into two categories: energy-window-based methods [5, 6] and calculation-based methods [4, 7–10]. We have previously validated a 3D-dedicated scanner with a hybrid dual-energy-window...
(HDE) scatter correction (one of the energy-window-based methods), by performing a head-to-head comparison with a conventional 2D scanner on a $^{15}$O study in the brain [6, 11]. However, as the energy-window-based method requires a special setting for two (or more) energy windows and has strict stability requirements because of the narrower energy window [6], calculation-based methods, including a single scatter simulation (SSS) method [9, 10], are utilized in most major clinical PET scanner products. A common drawback of the calculation-based methods is an inability to correct for scatter events originating from radioactivity outside of the field of view (FOV). This may cause a substantial effect in $^{15}$O PET of the brain, where strong radioactivity exists outside of the brain, such as in the lungs, heart, and airways [12, 13].

The aim of this study was to validate the use of the calculation-based method for a clinical PET study using $^{15}$O. We applied a convolution-subtraction scatter correction [4, 7], and compared it with the HDE scatter correction, which we considered as the reference method [11]. The convolution-subtraction method estimates the scatter distribution by convolving the measured sinograms with the scatter kernel. The estimated scatter is subsequently subtracted to obtain the corrected, scatter-free sinograms. This process can be seen as an inverse of the convolution, that is it can be considered a deconvolution; therefore, we refer to the method as deconvolution scatter correction (DEC) [7] in this paper.

Materials and methods

Subjects

PET data from 10 sequential cases acquired between April and June 2014, were analyzed retrospectively. All the patients had occlusion or stenosis of the internal carotid artery (ICA; $n = 5$) or middle cerebral artery ($n = 5$) as demonstrated by MR or CT angiography. This retrospective study was approved by the local ethics committee (No. 15-11, Ethics Committee of Research Institute for Brain and Blood Vessels-Akita).

PET scanner

A SET-3000GCT/M (Eminence SOPHIA; Shimadzu Corp., Kyoto, Japan) dedicated to the 3D-acquisition mode was used [11, 14]. The scanner consisted of 30 gadolinium oxyorthosilicate crystal rings, providing 59 slices, each with a thickness of 2.6 mm. The axial FOV was 156 mm. The lower limit of the energy window (a determinant of the amount of scatter) was set to 400 keV. The scanner was operated in a 64-bit list mode. Three-dimensional sinograms were converted to 2D sinograms using a Fourier rebinning algorithm (FORE). Scatter correction was performed on the 2D sinograms following the description below. Attenuation correction was applied to the scatter-corrected 2D sinograms via transmission scanning (3 min) using a $^{137}$Cs point source and a bismuth germanate transmission detector ring, coaxially attached to the emission detector rings. Reconstruction by filtered back projection with a 6 mm FWHM 3D Gaussian filter resulted in an effective in-plane resolution of 7 mm. All reconstructed images consisted of 59 slices of $128 \times 128$ voxels, with a voxel size of $2.0 \times 2.0 \times 2.6$ mm.

PET protocol

Three emission scans were performed sequentially with inhalation of $^{15}$O-CO, inhalation of $^{15}$O-O$_2$, and injection of $^{15}$O-H$_2$O, with 15-min intervals between the scans.

Fig. 1 Schematic view of deconvolution scatter correction: scatter components in SEW (b) is estimated by convolving the SEW sinograms (a) with the scatter kernel, is subsequently subtracted to obtain the scatter-corrected SEW sinograms (c). SEW standard energy window.
The patient’s head was fixed using pads and a Velcro band tightened around the head and head holder [17]. A removable neck-shield consisting of 7 mm thick lead plates (corresponding to 70% attenuation of 511 keV gamma rays) was used to reduce random and scatter coincidences attributable to radioactivity outside of the FOV [13].

Calibration between the PET scanner and a well counter was performed by scanning a cylindrical phantom (15 cm in diameter) filled with a $^{68}$Ga aqueous solution, and subsequently, a beta detector for measuring an arterial input function was calibrated to the well counter. In this procedure, reconstruction images were generated with HDE and DEC, and calibration factors were separately calculated for HDE and DEC. Scanner count rates with $^{22}$Na point source were measured every day to check the stability of the scanner and to assure the accuracy of the HDE scatter correction, and we confirmed that for the examinations analyzed in the study ($n = 10$), the UEW count rates were within 5% from the baseline (the most recent scanner calibration).

The $^{15}$O-H$_2$O PET study to measure CBF used a 3 min scanning duration with a simultaneously initiated 2 min intravenous infusion of $^{15}$O-H$_2$O (0.37 GBq) by an automatic injector device [3, 18]. The arterial input function was determined with the beta detector system [19], and the CBF was calculated using the autoradiographic method [3, 18]. The $^{15}$O-CO PET study to measure cerebral blood volume (CBV) used a 4 min scan initiated 3 min after a 1 min inhalation of $^{15}$O-CO gas (2.13 ± 0.20 GBq) [20]. The $^{15}$O-O$_2$ PET study with a 3 min scan initiated simultaneously with 1.5 min inhalation of $^{15}$O-O$_2$ (3.39 ± 0.51 GBq) was performed to measure oxygen extraction fraction (OEF) and cerebral metabolic rate of oxygen (CMRO$_2$) [2]. The arterial input function was determined in the same way as the $^{15}$O-H$_2$O PET scan.

**Scatter correction**

The acquired 3D sinograms were sorted into 2D sinograms using FORE. The subsequent 2D sinograms were then scatter-corrected using both the HDE and DEC routines.

![Fig. 2](image1.png)  
*Fig. 2* Representative reconstruction images, scatter-corrected by HDE and DEC, for $^{15}$O-H$_2$O (left), $^{15}$O-O$_2$ (center), and $^{15}$O-CO (right) from a patient with the stenosis of the left internal carotid artery (No. 10) and with three typical slice positions (subject’s native space). *HDE* hybrid dual-energy-window scatter correction, *DEC* deconvolution scatter correction.

![Fig. 3](image2.png)  
*Fig. 3* Patient-averaged reconstruction images, scatter-corrected by HDE and DEC, for $^{15}$O-H$_2$O (left), $^{15}$O-O$_2$ (center), and $^{15}$O-CO (right), with three typical slice positions. The spatially normalized images for each patient were normalized by the counts in GM regions and averaged over the patients. This count normalization was performed to visualize differences in GM-to-WM contrast between DEC and HDE. GM and WM masks, utilized for the analysis (Fig. 4), are also shown. *HDE* hybrid dual-energy-window scatter correction, *DEC* deconvolution scatter correction, *GM* gray matter, *WM* white matter.
HDE scatter correction based on a dual-energy-window acquisition was used as a reference for the comparison. The details of the method have been described previously [6, 11]. In brief, we estimated scatter components in the standard energy window (SEW; 400–624 keV) by combining SEW data and upper energy-window (UEW) data (512–624 keV), in which the scatter contribution is relatively small, and hence, correctable by the DEC method.

The convolution-subtraction scheme was applied in the DEC method [4, 7]: we estimated the scatter components in SEW by convolving the SEW sinograms with the scatter kernel, and subsequently subtracted the estimated scatter to obtain the scatter-corrected SEW sinograms (Fig. 1). The scatter kernel ($S$) is defined as a low-pass filter in the spatial frequency domain of the 2D projection plane of the sinograms (radial-direction $\times$ z-direction for each view angle):

$$S(f) = \frac{1}{1 + \alpha \exp(b|f|^2)},$$

where $f$ represents spatial frequency and $(\alpha, b)$ is a parameter set that determines the amplitude and shape of the scatter kernel. This function was empirically selected to represent the scatter tail of objects. In the current implementation, the parameters $(\alpha, b)$ are varied with the object size to realize the object-dependent scatter kernel. Initially, for both a cylindrical phantom (15 cm in diameter) and an IEC body phantom filled with uniform activity, we optimized the parameters $(\alpha, b)$ by matching the calculated scatter distribution with the tail part of the measured sinograms. Subsequently, the parameters were linearly interpolated and tabulated as a function of the object size. The volume of the object in the FOV is calculated from the segmented-transmission image ($\mu > 0.06$ cm$^{-1}$), and is used as the index of object size.

**Fig. 4** Differences in reconstruction images between DEC and HDE in % unit, defined as $\text{(DEC - HDE)} / \text{HDE} \times 100\%$, are presented as a function of slice position: $^{15}\text{O}-\text{H}_2\text{O}$ (upper), $^{15}\text{O}-\text{O}_2$ (middle), and $^{15}\text{O}-\text{CO}$ (lower). The data were obtained from GM (left) and WM (right) regions, as shown in Fig. 3. Solid lines and dotted lines indicate the results for the patient-average and each patient, respectively.

HDE, hybrid dual-energy-window scatter correction, DEC, deconvolution scatter correction, GM, gray matter, WM, white matter.
Image analysis

All the reconstructed images ($^{15}$O-H$_2$O, $^{15}$O-O$_2$, and $^{15}$O-CO) and parametric maps (CBF, CBV, OEF, and CMRO$_2$) were spatially normalized to the anatomic brain template using the SPM tool (SPM8, http://www.fil.ion.ucl.ac.uk/SPM, Wellcome Trust Centre for Neuroimaging, UCL, London, UK). Thus, the resultant images and maps were in the same data format with an isotropic voxel size of 2 mm.

Whole-brain analysis was performed on the reconstructed images to assess the overall trend of differences between the HDE and DEC methods. Separate masks were created for gray and white-matter (GM and WM) regions by thresholding (at > 0.5) the a priori tissue probability maps available in SPM. The GM and WM masks were applied to the reconstructed images from each patient. Mean values for the masked regions and differences in the mean values between DEC and HDE, (DEC − HDE)/HDE × 100 %, were calculated as a function of slice position.

For the parametric maps, the region of interest (ROI) analysis was performed: ROIs were defined on the template space, drawn bilaterally for each brain region (except for pons and midbrain) in 3 adjacent slices and results were averaged. Elliptical ROIs (16 × 32 mm) were defined for the cerebellar cortex, centrum semiovale, and 4 neocortical regions (frontal, temporal, occipital, and parietal). Circular ROIs (16 mm in diameter) were defined for the pons, midbrain, thalamus, putamen, parahippocampal gyrus, and cingulate gyrus (anterior and posterior parts). Clinical studies frequently use relative rather than absolute parameter values (e.g., relative to values in a normal brain region). We also analyzed the left-to-right ratios of the bilateral ROIs.

Fig. 5 Representative parametric maps, calculated from the reconstruction images scatter-corrected by HDE and DEC, from a patient with occlusion of the left internal carotid artery (No. 3). Five typical slice positions are presented. Regions of interest overlaid on GM probability maps are also shown (left). HDE hybrid dual-energy-window scatter correction, DEC deconvolution scatter correction, GM gray matter.
Intraclass correlation coefficient (ICC) was calculated with a two-way random effects model, ICC(2,1) [21], to evaluate the agreement between DEC and HDE.

Results

Representative reconstruction images from a patient, scatter-corrected by HDE and DEC are shown for $^{15}$O-H$_2$O, $^{15}$O-O$_2$, and $^{15}$O-CO in Fig. 2. Visual assessment indicates that both the scatter correction methods provided similar reconstruction images with near-identical image noise. For detailed delineation of the differences between the methods, the reconstruction images for each patient were normalized by the counts for the whole GM region and then averaged over all the patients. The patient-averaged images, scatter-corrected by HDE and DEC, are shown in Fig. 3. The differences in the WM regions were slightly greater than in the GM regions, and were also greater for $^{15}$O-CO than for $^{15}$O-H$_2$O and $^{15}$O-O$_2$. However, as presented in Fig. 4 as a function of slice position, the differences for $^{15}$O-H$_2$O and $^{15}$O-O$_2$ were approximately 5% in average even in the WM regions. The differences between the HDE and DEC methods were more substantial for $^{15}$O-CO, and showed greater slice-dependence, but values were generally still within 10%, even in the lower slices.

Representative parametric maps calculated from the scatter-corrected reconstruction images from a patient are shown in Fig. 5. Both scatter correction methods provided parametric maps of a similar quality, as was the case with the reconstruction images (Fig. 2). For the patient, whose images are shown (left ICA occlusion), a left hemisphere reduction in CBF and CMRO$_2$, and slight increase in OEF, was visualized similarly by both HDE and DEC. The results of the ROI analysis comparing HDE and DEC are presented in Fig. 6. In addition to the absolute values, the relative values, as left-to-right ratios of each parameter, are also presented in Fig. 7. High ICC values were obtained for both the absolute and relative parameters, with an

![Fig. 6 Correlations between HDE and DEC for CBF, CBV, OEF, and CMRO$_2$. Each dataset has 130 data points (10 subjects × 13 ROIs). Regression line determined by geometric mean regression analysis (solid line), and line of identity (dashed line) are also shown.](image)

HDE hybrid dual-energy-window scatter correction, DEC deconvolution scatter correction, CBF cerebral blood flow, CBV cerebral blood volume, OEF oxygen extraction fraction, CMRO$_2$ cerebral metabolic rate of oxygen
Fig. 7 Correlations of left-to-right ratios between HDE and DEC for CBF, CBV, OEF, and CMRO₂. Each data set has 110 data points (10 subjects × 11 ROIs). Regression line determined by geometric mean regression analysis (solid line), and line of identity (dashed line) is also shown. HDE hybrid dual-energy-window scatter correction, DEC deconvolution scatter correction, CBF cerebral blood flow, CBV cerebral blood volume, OEF oxygen extraction fraction, CMRO₂ cerebral metabolic rate of oxygen.

Table 1 Absolute differences between scatter correction methods: deconvolution (DEC) and hybrid dual-energy window (HDE)

| Region               | Absolute differences (%) in quantitative values | Absolute differences (%) in left-to-right ratios |
|----------------------|------------------------------------------------|-------------------------------------------------|
|                      | CBF   | CBV   | OEF   | CMRO₂ | CBF   | CBV   | OEF   | CMRO₂ |
| Pons                 | 6.3   | 7.3   | 3.5   | 7.6    | –     | –     | –     | –     |
| Cerebellum           | 4.5   | 7.0   | 1.2   | 4.6    | 1.5   | 8.3   | 1.1   | 2.1   |
| Parahippocampal gyrus| 5.6   | 2.3   | 2.3   | 5.3    | 1.7   | 3.5   | 1.6   | 1.6   |
| Midbrain             | 7.3   | 7.1   | 2.9   | 6.8    | –     | –     | –     | –     |
| Putamen              | 6.8   | 4.6   | 2.0   | 8.1    | 1.7   | 5.3   | 1.1   | 1.3   |
| Temporal cortex      | 2.6   | 2.7   | 1.5   | 3.4    | 0.7   | 1.6   | 1.6   | 1.3   |
| Frontal cortex       | 2.0   | 2.2   | 1.6   | 2.8    | 1.2   | 2.8   | 0.8   | 1.1   |
| Anterior cingulate   | 3.5   | 2.9   | 2.1   | 4.3    | 0.7   | 1.7   | 1.1   | 1.0   |
| Thalamus             | 8.0   | 6.3   | 2.8   | 9.5    | 1.8   | 4.9   | 2.4   | 2.1   |
| Occipital cortex     | 6.5   | 2.5   | 1.4   | 6.6    | 1.0   | 1.6   | 1.1   | 1.2   |
| Posterior cingulate  | 7.1   | 5.7   | 1.4   | 7.4    | 0.6   | 1.5   | 0.9   | 0.8   |
| Parietal cortex      | 3.8   | 4.1   | 1.3   | 3.8    | 1.2   | 3.8   | 1.2   | 1.8   |
| Centrum semiovale    | 8.7   | 10.7  | 2.1   | 9.4    | 1.5   | 5.8   | 2.4   | 1.7   |
| Total                | 5.6   | 5.9   | 2.0   | 6.1    | 1.2   | 3.7   | 1.4   | 1.5   |

Absolute differences, DEC/HDE × 100 %, are presented as patient-averaged values.
methods, such as DEC, are practical for a clinical 15O brain studies using 3D PET. However, the SSS method [9, 10, 23], which is implemented in most commercial PET scanners, should be used with caution. Hori et al. [12] demonstrated that the currently implemented version of SSS [23] was inappropriate because of inadequate scaling to account for scatter from outside of the FOV, especially when used for 15O-gas PET. Rather, the original version of SSS, without a compensation procedure for scatter outside of the FOV, provided adequate results in the 15O-gas study [12].

The simplified implementation of DEC, i.e., the spatially-invariant, empirically-defined scatter kernel with optimized parameters for uniform phantoms, has an obvious limitation. Although uncertainty of HDE correction accuracy cannot be ruled out, the simplification and assumptions in DEC cause errors to various degrees. The scatter kernel naturally varies both with position in the scanner FOV and the objects being scanned [4, 7, 24, 25]. In the present study, the maximum differences between DEC and HDE were observed in a white-matter region at the level of the cerebellum in the 15O-CO images. These regions show a lower uptake of radioactivity and are sensitive to errors in the scatter correction because of a greater amount of scatter from surrounding regions with higher activity, such as large vessels. The situation may be more severe for lower parts of the brain with complex structures, on which image-based extraction of an AIF from a large artery (e.g., ICA) is a separate research topic [26–28]. For such regions, the simplified scatter kernel is a potential source of error. Unfortunately, the scanner used had a 156 mm axial FOV and had insufficient sensitivity for detailed investigations of the lower brain parts. A future study using a scanner with a longer axial FOV is desirable.

In the current implementation of DEC, object-size-dependent kernel parameters were applied to deal with objects of various size, and the DEC scatter correction is expected to work well for various applications, including whole-body scanning. In the present study with the 15O-labeled tracers, the phantom-based DEC parameters provided the satisfactory human results. However, there is a possibility of insufficient accuracy of DEC scatter correction for other PET tracers with radioactivity distribution extremely different to the 15O tracers, and further optimization of DEC parameters will be needed. In such a situation, optimization directly using human PET data instead of the uniform phantom data may be suitable although another additional human PET data are required for validation.

Conclusions

The DEC scatter correction method despite its simplified implementation provides similar results to HDE when the fraction of scatter from outside of the FOV is sufficiently small. We consider it suitable for application in clinical 15O brain studies using 3D PET.

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Compliance with ethical standards

Conflict of interest M. Ibaraki, K. Matsubara, K. Sato, and T. Kinoshita declare that they have no conflict of interest.

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