1. Introduction
About half of the more than 1000 known transiting exoplanets have orbital periods less than ten days\(^1\). These close-in planets undergo strong tidal effects raised by the parent star. One consequence is that their spins and orbits evolve until an equilibrium configuration is reached, corresponding to coplanarity, circularity, and synchronous rotation (e.g., Hut 1980; Correia 2009). Another consequence is that the shape of these planets differs from a spheroidal body, and it is approximated better by a triaxial ellipsoid (e.g., Chandrasekhar 1987; Correia & Rodríguez 2013). The asymmetry in the mass distribution increases with the proximity to the star, and it is particularly pronounced near the Roche limit (e.g., Ferraz-Mello et al. 2008; Burton et al. 2014).

For simplicity, most observational works on transiting planets assume that its shape is spherical, so they determine an average radius. However, if there is enough precision in the data, it is possible to spot the polar oblateness \(f_p\) signature in the transit light curve (Seager & Hui 2002; Barnes & Fortney 2003; Ragozzine & Wolf 2009; Carter & Winn 2010), which gives us invaluable information on their internal structure. Previous studies have ignored the equatorial prolateness \(f_e\), which is actually more pronounced than the polar oblateness, since the long axis always points to the star, and thus should not be perceptible during the transit. Leconte et al. (2011) and Burton et al. (2014) have shown that failing to account for this distortion would result in a systematic underestimation of the planetary radius, hence of its bulk density. In addition, for planets near the Roche limit, the projected ellipsoid also depends on the inclination to the line of sight and on the rotation angle, which most likely modifies the transit light curve. Unfortunately, there is no comparison of transit light curves for ellipsoidal and spherical planets shown in the works by Leconte et al. (2011) and Burton et al. (2014).

Since a large number of transiting planets are being detected on the verge of tidal disruption (e.g., Valsecchi & Rasio 2014), it becomes important to understand the exact contribution of its shape to the photometric observations. The work by Leconte et al. (2011) is very complete, but as pointed by Burton et al. (2014), it requires complex internal structure models that are difficult to implement and to reconcile with observational parameters. Therefore, Burton et al. (2014) compute the tidal deformation by assuming surfaces of constant gravitational equipotential for the planet that are solely based on observable parameters. Nevertheless, this method is also not easy to implement, since it requires a numerical adjustment, such that the projected area of the model planet during the transit matches those given by the observations. Moreover, we lose the information relative to the internal structure, which is an important complement to the density determination.

In this Letter, we propose a simple analytical model for computing the projected area of close-in planets at any point of its orbit, which is based on the equilibrium surface given by second-order Love numbers. We thus obtain the transit light curve for these planets, which can be used to compare directly with the observations, and infer their internal structure and density.

2. Shape
The shape (or the figure) of a planet is usually described well by a reference ellipsoid (quadrupolar approximation). The standard equation of a triaxial ellipsoid centered on the origin of a Cartesian coordinate system \((X, Y, Z)\) and aligned with the axes is

\[
\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1, \tag{1}
\]

where \(a\), \(b\), and \(c\) are called the semi-principal axes. For the Earth and the gaseous planets in the solar system, we have \(a > b > c\) (oblate spheroids), but usually \(a > b > c\) for the main satellites, where the long axis \(a\) is directed to the central planet.

We let \(\mathbf{R} = (X, Y, Z)\) be a generic point at the surface of the ellipsoid. Then, equation (1) can be rewritten as

\[
\mathbf{R}^T \mathbf{A}_0 \mathbf{R} = 1, \quad \text{with} \quad \mathbf{A}_0 = \begin{bmatrix} a^{-2} & 0 & 0 \\ 0 & b^{-2} & 0 \\ 0 & 0 & c^{-2} \end{bmatrix}, \tag{2}
\]
The first results from the planet’s rotation rate deform under the action of the centrifugal and tidal potentials. a chronous with the orbital mean motion that is, its orbit is circular with radius \( r \), while the second results from the di internal mass di where

\[
\Omega = \frac{1}{a^2} \left( \frac{2}{b^2} + \frac{f_s}{b^3} \right), \quad \text{with} \quad f_s = \frac{a - b}{b}.
\]

Assuming \( a \sim b \sim c \), we can neglect terms in \( f_s^2 \) and \( f_c^2 \) in the previous expressions, and thus

\[
R \approx b \left( 1 + \frac{a}{2} X^2 + \frac{\gamma}{2} Z^2 \right) \approx b + \frac{f_a}{b} X^2 + \frac{f_c}{b} Z^2.
\]

The mass distribution inside the planet is a result of the self gravity, but also of the body’s deformation in response to any perturbing potential \( V_p \). A very convenient way to define this deformation is through the Love number approach (e.g., Love 1911) in which the radial displacement \( \Delta R \) is proportional to the equipotential perturbing surface

\[
\Delta R = -\frac{h_s V_p}{g},
\]

where \( g = Gm/R^2 \) is the surface gravity, \( G \) is the gravitational constant, \( m \) is the mass of the planet, and \( h_s \) is the fluid second Love number for radial displacement. For a homogeneous sphere \( h_s = 5/2 \), but more generally, it can be obtained from the Darwin-Radau equation (e.g., Jeffreys 1976)

\[
I = \frac{2}{3} \left[ 1 - \frac{5}{3} \frac{h_s - 1}{h_s} \right]^{1/2},
\]

where \( I \) is the mean moment of inertia, which depends on the internal mass differentiation.

Like the main satellites in the solar system, close-in planets deform under the action of the centrifugal and tidal potentials. The first results from the planet’s rotation rate \( \Omega \) about the \( c \) axis, while the second results from the differential attraction of a mass element by the nearby star with mass \( m_* \). For simplicity, we consider that the planet reached the final tidal equilibrium; that is, its orbit is circular with radius \( r_0 \), the spin axis is normal to the orbital plane (zero obliquity), and the rotation rate is synchronous with the orbital mean motion \( n \), always pointing the long axis \( a \) to the star (e.g., Ferraz-Mello et al. 2008). Thus, on the planet’s surface, the non-spherical contribution of the perturbing potential is given by (e.g., Correia & Rodríguez 2013)

\[
V_p = -\frac{1}{2} \Omega^2 Z^2 - \frac{3Gm_*}{2r_0^3} X^2.
\]

Replacing the above perturbing potential in expression (7) and comparing with equation (6) for the surface of the ellipsoid, it becomes straightforward that

\[
\frac{f_a}{b} = \frac{3Gm_*}{2gr_0^3} \Rightarrow a = b(1 + 3q),
\]

and

\[
\frac{f_c}{b} = -\frac{h_s}{2g} \Omega^2 \Rightarrow c = b(1 - q),
\]

where \( q = \frac{h_s m_*}{2m} \left( \frac{b}{r_0} \right)^3 \),

where \( \Omega^2 = n^2 \approx Gm_*/r_0^3 \). Since \( q \propto r_0^{-3} \), the closer the planet is to the star, the greater is the difference between the ellipsoid semi-axes. However, there is a maximum value for \( q \), corresponding to the Roche limit, \( r_{\text{RK}} \) (Chandrasekhar 1987)

\[
r_0 \geq r_{\text{RK}} \approx 2.46 \left( \frac{m_*}{m} \right)^{1/3} b \Rightarrow q < q_{\text{max}} \approx \frac{h_s}{30}.
\]

Adopting the maximum value possible for \( h_s = 5/2 \) (Eq. 8) gives

\[
q_{\text{max}} \approx 0.12 \approx 0.08, \quad a_{\text{max}} \approx 1.25 b, \quad \text{and} \quad c_{\text{max}} \approx 0.92 b.
\]

Thus, the approximation used to obtain expression (6) is still valid.

### 3. Transit light curve

We let \((x, y, z)\) be the standard Cartesian coordinate system for exoplanets, centered on the star, where \((x, y)\) are in the plane of the sky and \(z\) is along the line of sight. In this frame, a generic point on the planet’s surface \( r = (x, y, z) \) can be obtained as

\[
r = r_0 + S R,
\]

where \( r_0 = (x_0, y_0, z_0) \) is the position of the center of mass of the planet with respect to the star, and \( S \) is a rotation matrix. When the planet orbits the star in a synchronous circular orbit with zero obliquity, we have

\[
S = S_3(\theta) S_2(\theta) = \left[ \begin{array}{ccc} \cos \theta & -\sin \theta & 0 \\ \sin \theta \cos i & \cos \theta & -\sin i \\ \sin \theta \sin i & \cos \theta \sin i & \cos i \end{array} \right],
\]

where \( \theta \) is the rotation angle, \( i \) is the inclination angle between the normal to the orbit and the line of sight, and \( S_2 \) and \( S_3 \) are the standard \( 3 \times 3 \) rotation matrix about the \( x \) and \( z \) axis, respectively (e.g., Murray & Correia 2010). In this particular tidal equilibrium configuration, for a given time \( t \), we have \( \theta = n(t - t_0) \), and thus \( S = S(t) \). Moreover, the position of the planet in its orbit can also be easily obtained from \( S \) as

\[
r_0 = S R_0 = \left[ \begin{array}{c} \cos \theta \\ \sin \theta \cos i \\ \sin \theta \sin i \end{array} \right], \quad \text{where} \quad R_0 = \left[ \begin{array}{c} r_0 \\ 0 \\ 0 \end{array} \right].
\]

From expression (14) we have

\[
R = S^{-1}(r - r_0) = S^T(r - r_0), \quad \text{and} \quad R^T = (r - r_0)^T S.
\]

Replacing (17) in equation (2), we obtain the equation for the ellipsoidal surface of the planet in the new coordinate system

\[
(r - r_0)^T A(r - r_0) = 1, \quad \text{with} \quad A = S A_0 S^T.
\]

The projection of the ellipsoid in the \((x, y)\) plane of the sky is obtained simply by setting \( z = z_0 \) in previous equation. The result is an ellipse with general equation given by

\[
A(x - x_0)^2 + B(x - x_0)(y - y_0) + C(y - y_0)^2 = 1,
\]

with

\[
A = \cos^2 \theta/\alpha^2 + \sin^2 \theta/\beta^2,
\]

\[
B = (1/\alpha^2 - 1/\beta^2) \sin 2\theta \cos i,
\]

\[
C = (\sin^2 \theta/\alpha^2 + \cos^2 \theta/\beta^2) \cos^2 i + \sin^2 i/c^2.
\]
In the new coordinate system, the diminishing of the stellar flux is then given by the overlap between the planetary ellipse (Eq. 19) and the stellar disk, defined by
\[ x^2 + y^2 = R^2, \]
where we assumed a spherical shape for the star with radius \( R \).
There are many different methods of computing the overlap area.
If the stellar flux is uniform, one easy way is to compute the segment areas (e.g., Eberly 2008; Hughes & Chraibi 2012). In more realistic problems (models that include limb-darkening, stellar rotation, stellar activity, etc.), one can use Monte Carlo integrations (e.g., Press et al. 1992; Carter & Winn 2010).

In Figure 1 we plot the flux difference between the transit light curve of an ellipsoidal and a spherical planet for some real close-in planets, chosen with different inclinations and distances to the star (Table 1). The red line shows the difference obtained with our model (Eq. 19), while the blue line is obtained for an oblate planet with \( a = b \neq c \), both with stellar uniform flux. The dashed line also corresponds to the difference obtained with our model, but using a quadratic stellar limb-darkening correction \( I(\mu)/I(1) = 1 - 0.4830(1 - \mu) - 0.2023(1 - \mu)^2 \), which corresponds to a stellar temperature of 5500 K (Sing 2010).

The effect of an ellipsoidal planet in the transit light curve is also maximized for edge-on orbits (\( \theta = 90^\circ \)). For lower (or higher) inclinations, the planet spends less time in front of the star, so the “bump” increase due to the rotation becomes smaller.

Nevertheless, for almost grazing orbits we can still observe significant differences in the light curve, although the two main features described above are no longer completely individualized (see Fig. A.1, for a Jupiter-like planet at the Roche limit).

4. Inner structure determination

For those systems where the differences in the light curve can be detected, one can use an ellipsoid instead of a sphere to fit the photometric observations (Eq. 19). In addition to the equatorial radius \( b \), the projected ellipsoid only depends on \( q \) (Eqs. 10–12).

Then, when we adjust our model to the observational data, \( q \) is the only supplementary parameter to fit, which accounts for all the observed differences in the transit light curve. In the expression of \( q \) (Eq. 12), all parameters but \( h_t \) are also known from the observational data. It is thus possible to obtain an observational estimation for \( h_t \), which represents an important additional constraint for the inner structure differentiation (Eq. 8).

Seager & Hui (2002) originally showed that the oblateness of transiting exoplanets can be constrained from the variations in the light curve during the ingress and egress phases. However, Barnes & Fortney (2003) noticed that these oscillations are short in time and therefore difficult to observe, although some relatively weak constraints on the Love number were derived for the system HD 189733 (Carter & Winn 2010).
In Figure 1 we observe that the “bump” increase due to the rotation of the progenitor planet is present during the whole transit, not only at ingress and egress phases. As a consequence, the flux differences can be significantly larger than previously thought, increasing our chances of observing the shape of close-in planets. For giant planets near the Roche limit, the flux differences can reach $10^{-5}$, which is above the intrinsic stellar photometric variability on transit timescales, estimated to be around $10^{-3}$ (Borucki et al. 1997). For longer distances to the star, the flux difference can drop below the $10^{-5}$ threshold, so the shape is more difficult to determine. For rocky planets, the flux difference is also smaller than $10^{-5}$. However, since the Roche limit is closer to the star for these planets, the “bump” becomes more prominent, increasing again the chances of detection.

In Figure 1 we also observe that the flux difference is about the same for a stellar uniform flux, or when limb-darkening is considered. The reason is that the differences in the shape of the planet are so tiny with respect to the size of the star that locally the flux can be considered approximately uniform. Therefore, for realistic light curves obtained with non-uniform stellar flux, one can still obtain the correction introduced by the axial asymmetry using a uniform flux model, which is much easier to compute.

5. Density determination

Transiting systems provide a radius $R_i$ for the planet, hence a bulk density, when coupled with the planetary mass determined from radial-velocity measurements. Most studies assume a spherical planet in order to work out the volume $V_i = 4\pi R_i^3/3$, thus providing a spherical bulk density $\rho_i = m/V_i$. However, for close-in planets, the true volume of the ellipsoid is given by $V = 4\pi abc/3$, which gives for the bulk density (Eqs. 10, 11)

$$\rho = \frac{3m}{4\pi abc} = \frac{3m}{4\pi b^3} (1 - 2q) .$$

(24)

When there is enough precision in the data, $b$ and $q$ can be directly adjusted from the transit light curve, instead of $R_i$ (section 4). For low-mass planets such as Kepler-78b, it may be difficult to spot the tiny differences in the light curve with respect to a spherical planet (Fig. 1). In those cases, one can use the spherical model, where $R_i$ is related to the projected ellipsoid (Eq. 19) through

$$\pi R_i^2 = \frac{2\pi}{\sqrt{4AC - B^2}} .$$

(25)

At the center of the transit ($\theta = 90^\circ$), we thus have (Eqs. 20-22)

$$b \approx R_i \left(1 + q/2 - 2q \cos^2 \theta \right) ,$$

(26)

which gives for the bulk density (Eq. 24)

$$\rho \approx \rho_i \left(1 - q/2 + 6q \cos^2 \theta \right) .$$

(27)

Here, $q$ cannot be adjusted from the observations, but it can be estimated from expression (12) using $b \approx R_i$ and adopting the solar system data, $h_1 = 1.5$ for gaseous planets, and $h_2 = 2$ for rocky planets (Yoder 1995).

In Table 1 we compute the relative change in the bulk density, $\Delta \rho = 1 - \rho/\rho_i$, for some close-in planets near the Roche limit ($r_0 < 3r_h$). These corrections agree with those obtained numerically by Burton et al. (2014). The small differences observed between the two methods result from the assumption of different inner structure models. Indeed, an exact match could be obtained using slightly different $h_i$ values in our model.

In Figure 2 we show the relative change in the bulk density as a function of the distance to the star $r_0$. The largest possible correction in the density is $\rho_{\text{max}} \approx 0.7 \rho_i$, obtained from $q_{\text{max}}$ (Eq. 13) with $i = 90^\circ$, which is $30\%$ smaller than the spherical value. However, for realistic cases of planets near the Roche limit ($r_0 \approx r_h$), we get values lower than $20\%$ for rocky planets and lower than $15\%$ for gaseous planets. As in Burton et al. (2014), we also observe that the relative change in the density decreases rapidly with the distance to the star. This correction is less than $5\%$ for planets with $r_0 > 1.5r_h$, which is equivalent to the measurement error on the currently published bulk densities (e.g., Hellier et al. 2011). Therefore, with the current observational precision, a correction in the density determination is only justified for planets that are close to the Roche limit.

Table 1. Observational data (left side) and derived parameters (right side) for some close-in planets near the Roche limit ($r_0 < 3r_h$). All planets listed here were simultaneously detected by transit and radial-velocity techniques.

| Planet       | $r_0$ ($r_h$) | $i$ (deg) | $m_*$ ($M_\odot$) | $R_i$ ($R_\odot$) | $M_i$ ($M_\odot$) | $\rho_i$ ($g/cm^3$) | $h_1$ | $q$ | $a$ | $b$ | $c$ | $\rho$ ($g/cm^3$) | $\Delta \rho$ (%) |
|--------------|--------------|-----------|------------------|-----------------|-----------------|-----------------|-------|----|-----|----|----|----------------|---------------|
| WASP-19b     | 1.09         | 3.27      | 79.4             | 0.97            | 0.99            | 371             | 15.2  | 0.58|     |     |     | 1.5            | 1.29          |
| WASP-12b     | 1.15         | 4.30      | 89.0             | 1.35            | 1.60            | 446             | 19.0  | 0.36|     |     |     | 1.5            | 1.16          |
| WASP-103b    | 1.13         | 3.59      | 86.3             | 1.22            | 1.44            | 473             | 16.8  | 0.55|     |     |     | 1.5            | 0.50          |
| Kepler-78b   | 1.34         | 4.18      | 79.0             | 0.83            | 0.74            | 169             | 1.20  | 5.37|     |     |     | 2.0            | 4.88          |
| WASP-52b     | 1.28         | 3.94      | 85.4             | 0.87            | 0.79            | 146             | 13.9  | 0.30|     |     |     | 1.5            | 0.28          |
| CoRoT-1b     | 1.50         | 3.64      | 85.1             | 0.95            | 1.11            | 327             | 16.3  | 0.41|     |     |     | 1.5            | 0.39          |
| OGLE-TR-56b  | 1.50         | 3.22      | 73.7             | 1.23            | 1.36            | 442             | 15.1  | 0.70|     |     |     | 1.5            | 0.68          |
| WASP-78b     | 1.60         | 4.08      | 87.5             | 1.33            | 2.20            | 283             | 18.6  | 0.24|     |     |     | 1.5            | 0.23          |
| WASP-48b     | 1.60         | 3.47      | 80.1             | 1.19            | 1.75            | 311             | 18.3  | 0.28|     |     |     | 1.5            | 0.27          |
| WASP-4b      | 1.60         | 2.89      | 89.4             | 0.85            | 0.87            | 384             | 14.3  | 0.72|     |     |     | 1.5            | 0.70          |
| HAT-P-23b    | 1.60         | 2.80      | 85.1             | 1.13            | 1.20            | 646             | 15.0  | 1.08|     |     |     | 1.5            | 0.31          |
| WASP-43b     | 1.78         | 1.84      | 82.3             | 0.72            | 0.67            | 646             | 11.4  | 2.43|     |     |     | 1.5            | 3.20          |
| 55 Cnc e     | 2.00         | 1.66      | 82.5             | 0.91            | 0.94            | 781             | 2.17  | 4.18|     |     |     | 2.0            | 4.06          |
| WASP-18b     | 2.29         | 1.90      | 84.8             | 1.24            | 1.15            | 3235            | 16.7  | 3.78|     |     |     | 1.5            | 3.73          |
| Kepler-10b   | 2.43         | 1.49      | 84.8             | 1.07            | 1.07            | 333             | 1.47  | 5.76|     |     |     | 2.0            | 1.67          |
| CoRoT-7b     | 3.01         | 1.22      | 80.1             | 0.91            | 0.82            | 742             | 15.6  | 10.3|     |     |     | 2.0            | 10.3          |

Refs: 1 Bolmont et al. (2006); 2 Fulton et al. (2011); 3 Gillon et al. (2014); 4 Howard et al. (2013); 5 Hébrard et al. (2013); 6 Barge et al. (2008); 7 Adams et al. (2011); 8 Small et al. (2012); 9 Enoch et al. (2011); 10 Gillon et al. (2009); 11 Bakos et al. (2011); 12 Gillon et al. (2012); 13 Smalley et al. (2012); 14 Southworth et al. (2009); 15 Dumasque et al. (2014); 16 Hatzes et al. (2011).
The red curve is relative to gaseous planets ($h_i = 1.5$), while the blue one is relative to rocky planets ($h_i = 2.0$). Both curves are obtained using expression (27) with $i = 80^\circ$. The dots represent the planets listed in Table 1. For $r_0 > 1.5 r_R$, the change is negligible when compared to the present observational errors in the density determination.

### 6. Conclusions

We have presented here a simple model for correcting the transit light curve of close-in planets, which is easy to implement and which allows us to obtain important constraints for the internal structure of these planets. On one hand, it provides a better determination for the bulk density (Eq. 27), which is lower than previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2). For instance, it has been announced that Kepler-78b has an Earth-like density (Howard et al. 2013; previously assumed (Fig. 2).

where $\varepsilon$ is the obliquity (the angle between the equator and the orbital plane), and $\varphi$ is the precession angle. Also, we have now

\[ \Delta \rho = 1 - \rho / \rho_* \]
Fig. A.1. Transit light curves for a Jupiter-like planet orbiting at the Roche limit ($r_0 = r_R = 2.51 R_\odot$) of a Sun-like star with uniform flux (in red). For comparison, we also show the light curve of a spherical planet (dashed line), and the difference between the two curves (bottom figure). The dots correspond to the relative positions shown in the top figure. The shape of the planet in the top figure is obtained with an exaggerated $h_f = 6$, so that we can better spot the modifications in the projected shape, but the transit light curves are obtained with the realistic Jupiter’s value $h_f = 1.5$ (Yoder 1995).

Appendix A: Additional figure