Unsupervised Learning in Detection of Gene Transfer

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The tree representation as a model for organismal evolution has been in use since before Darwin. However, with the recent unprecedented access to biomolecular data, it has been discovered that, especially in the microbial world, individual genes making up the genome of an organism give rise to different and sometimes conflicting evolutionary tree topologies. This discovery calls into question the notion of a single evolutionary tree for an organism and gives rise to the notion of an evolutionary consensus tree based on the evolutionary patterns of the majority of genes in a genome embedded in a network of gene histories. Here, we discuss an approach to the analysis of genomic data of multiple genomes using bipartition spectral analysis and unsupervised learning. An interesting observation is that genes within genomes that have evolutionary tree topologies, which are in substantial conflict with the evolutionary consensus tree of an organism, point to possible horizontal gene transfer events which often delineate significant evolutionary events.

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1. INTRODUCTION

Evolutionary history of species is now inferred from the evolutionary histories of their genomes. Genomes can be viewed as a collection of genes and whole genome evolution is concluded from the evolution of individual genes. If the majority of genes followed the same evolutionary history, supertree approaches can be used to calculate a majority consensus tree. However, evolutionary trees of individual genes can differ from the majority [1], and in this case, the consensus tree is embedded in a network represented by the histories of the different genes. Evolutionary tree topologies of genes that conflict with the consensus tree are strong indicators of horizontal gene transfer events. Given this, it is clear that organismal evolution cannot be inferred from studying the evolution of just a few genes but must be inferred from studying as many (orthologous) genes as possible.

To construct and evaluate an evolutionary consensus tree based on multiple genes for a set of genomes, it is advisable to construct all possible evolutionary tree topologies for these genomes and measure the support of each topology by the (orthologous) genes within the genomes. Unfortunately, evaluating all possible tree topologies is computationally intractable for any but a very small set of genomes, since the number of possible tree topologies grows factorially with the number of participating genomes. An approach based on the spectral analysis of genomic data using bipartitions [2, 3] allows the inference of consensus trees from smaller quanta of phylogenetic information, side stepping some of the difficult computational issues. Table 1 shows the number of possible trees versus the number of possible bipartitions given a fixed set of genomes. With n taxa there are \((2n-5)!/[2^{n-3}(n-3)!]\) different unrooted tree topologies. The number of possible nontrivial bipartitions for n taxa is given by the formula \(2^{n-1} - n - 1\), and it grows much slower with an increasing number of species than the number of different trees. We refer to the approach based on bipartitions as spectral genome analysis.

It is worth noting that when a single tree is calculated from the combination of all genes, including genes that were horizontally transferred, the topology of the resulting tree might not represent the plurality of gene histories. Therefore, a detailed analysis of the evolutionary histories of the participating genes is of interest. The techniques outlined here support this kind of analysis.

In spectral genome analysis, each set of orthologous genes (a gene family) is associated with a particular set of bipartitions (its spectrum) that define its evolutionary tree.
Thus, we can envision a gene family as a point in the space spanned by all possible bipartitions of a set of genomes. Here, we apply unsupervised learning in the form of self-organizing maps [4] to this space and obtain a visual representation of clusters of gene families with similar spectra. The spectra of the gene families within a particular cluster allow us to infer the consensus tree for that cluster. It is now possible to investigate whether the consensus tree topologies of the clusters are compatible or conflicting with the overall consensus tree. If a cluster of gene families is discovered that conflicts with the consensus tree topology, then this is a strong indication for a horizontal gene transfer event. The advantage of this approach is that we not only see a distinct representation of clusters of gene families with similar spectra. It allows us to infer the consensus tree for that cluster. It is now evident that given any set of nontrivial bipartitions, a bipartition space can be viewed as a $2^{n-3}$ dimensional real vector space. An interesting consequence of this is that we can now measure the distance between spectra as the Euclidean distance between the two corresponding spectrum points in a bipartition space. Let $d_1$

| Number of genomes | Number of unrooted trees | Number of nontrivial bipartitions |
|-------------------|--------------------------|----------------------------------|
| 4                 | 3                        | 3                                |
| 5                 | 15                       | 10                               |
| 6                 | 105                      | 25                               |
| 7                 | 945                      | 56                               |
| 8                 | 10,395                   | 119                              |
| 9                 | 135,135                  | 246                              |
| 10                | 2,075,025                | 501                              |
| 20                | $2.22E+20$               | $5.24E+05$                       |
| 50                | $2.84E+74$               | $5.63E+14$                       |
| $n$               | $(2n - 5)!/[2^{n-3}(n - 3)!]$ | $2^{n-1} - n - 1$ |

2. MATERIALS AND METHODS

2.1. Spectral analysis of evolutionary trees

Given $n$ entities, there are $2^{n-1} - 1$ different ways to assign the entities to two different nonempty sets. That is, there are $2^{n-1} - 1$ different bipartitions of $n$ entities including trivial bipartitions. An (unrooted) tree can be viewed as a model of the evolutionary relationships between $n$ entities or taxa such as species, genes, molecules, and so forth. Trees and bipartitions are related as follows. Each edge in a tree can be seen as dividing the tree into a bipartition: the leaf nodes that can be reached from one end of the edge form one set of taxa and the leaf nodes that can be reached from the other end of the edge form the other set of taxa. A binary tree with $n$ leaf nodes has exactly $2n - 3$ edges. Thus, an evolutionary tree relating $n$ taxa gives rise to $2n - 3$ bipartitions. It is easy to see that $2n - 3 < 2^{n-1} - 1$, that is, the number of bipartitions defined by an evolutionary binary tree of $n$ taxa is much smaller than the number of possible bipartitions of $n$ entities.

Trivial bipartitions, which is bipartitions where one of the partitions is a singleton set, do not contain any phylogenetic information. Thus, given $n$ entities, there are $2^{n-1} - n - 1$ different nontrivial bipartitions. However, in an unrooted binary tree with $n$ leaf nodes there are $n - 3$ interior edges and therefore $n - 3$ nontrivial bipartitions. An interior edge is an edge that is not incident to a leaf node of a tree. It is evident that $n - 3 < 2^{n-1} - n - 1$, that is, the number of nontrivial bipartitions generated by a tree is much smaller than the number of possible nontrivial bipartitions.

Let $t_n$ be an evolutionary tree over $n$ taxa, then we define the bipartitions of $t_n$ as the spectrum of $t_n$, denoted as $S(t_n)$. It is convenient to adopt a vector notation for the spectrum $S(t_n) = (b_1, \ldots, b_{2^{n-1}-1}) = (0, 1, 1, 0, \ldots, 0, 0)$, where $b_k$ denotes bipartition $k$ with $1 < k < 2^{n-1} - 1$. Here, $b_k = 1$ if the spectrum of the tree includes bipartition $b_k$, and $b_k = 0$ otherwise. Note that the vector notation is a representation over all possible bipartitions. Given this, we can now refer to a bipartition space and we can readily see that a spectrum of a particular evolutionary tree $t_n$, represents the coordinates of a point in that space. In our case, where the tree represents the evolutionary relationship between orthologous genes in $n$ genomes, we often refer to the spectrum as the gene family spectrum and therefore a gene family is denoted by a point in bipartition space.

Figure 1(a) is an unrooted tree relating five taxa $A$ through $E$. The arrows indicate branches defining the nontrivial bipartitions in this tree. Figure 1(b) represents a bipartition corresponding to the left arrow in Figures 1(a) and 1(c) represents a bipartition corresponding to the right arrow in Figure 1(a), respectively. Observe that the sub-tree topologies in the bipartitions are unresolved.

By further generalizing and interpreting the values in the spectrum vectors as arbitrary real numbers, as we will do in what follows when we assign confidence values to bipartitions, a bipartition space can be viewed as a $2^{n-1} - 1$ dimensional real vector space. An interesting consequence of this is that we can now measure the difference between spectra as the Euclidean distance between the two corresponding spectrum points in a bipartition space. Let $d_1$,
and its complement \( m_C \) as \( t_L \) and \( t_R \) bipartitions, respectively. Figure 2(c) shows the binary representation of the bipartition in Figure 1(c).

Figure 1: (a) An unrooted tree with 5 taxa, (b) the bipartition corresponding to the left arrow above, (c) the bipartition corresponding to the right arrow above.

### 2.2. Representation of bipartitions

Let \( A \) be a set of \( n \) elements, and \( b \) is a bipartition defined on a set \( A \). Each bipartition \( b \) splits a set \( A \) into two subsets \( m \) and its complement \( m_C \), such that \( A = m \cup m_C \).

We say that two bipartitions are **compatible** if there exists a tree whose spectrum includes both bipartitions. We say that two bipartitions are **conflicting** if they cannot appear in the same spectrum. In set notation, two bipartitions are compatible if a set (either \( m \) or \( m_C \)) of one bipartition is a subset of one of the sets of the second bipartition; or, in other words, bipartitions \( b_1 \) and \( b_2 \) are compatible if and only if one of four possible conditions is satisfied:

\[
(m_1 \subset m_2), (m_1 \subset m_2^c), (m_2^c \subset m_1), \text{ or } (m_2^c \subset m_1^c). \tag{1}
\]

To handle bipartitions computationally in an efficient way, we can represent them effectively as binary masks. Figure 2(a) shows a binary vector indexed by the taxa in Figure 1(a). Figure 2(b) shows the binary representation of the bipartition in Figure 1(b) arbitrarily assigning 1 and 0 to the left and right bipartition, respectively. Figure 2(c) shows the binary representation of the bipartition in Figure 1(c).

Given our binary representation of bipartitions, there is a simple computation to test for compatibility between bipartitions. We say that two bipartitions are compatible if the following returns true:

\[
((b_1 | b_2) = b_1) \parallel ,
((b_1 | b_2) = b_2) \parallel ,
((b_1 \sim b_2) = b_1) \parallel ,
((b_1 \sim b_2) = b_2) \parallel , \tag{2}
\]

where \( b_1 \) and \( b_2 \) denote bipartitions. Here the “\( | \)” operator represents the bitwise OR operation, the “\( \sim \)” operator represents the bitwise negation, the “\( \parallel \)” operator represents the logical OR operation, and “\( = = \)” represents the bitwise equality operator. Given the two masks from Figures 1(b) and 1(c), it is easy to see that they are compatible:

\[
10001 \parallel 11001 = 11001. \tag{3}
\]

On the other hand, the bipartitions 11001 and 10011 are conflicting.

### 2.3. Consensus trees

It is customary to compute confidence values for the edges in an evolutionary tree via bootstrapping [7]. The computed tree represents a consensus tree over the bootstrap samples. The confidence values are typically chosen between 0 and 100. With this, a bipartition derived from a particular edge in the bootstrap consensus tree inherits the confidence value of that edge. This allows us to refine our spectrum vector notation, for example, \( S(t_n) = (0, 67, 85, 0, \ldots, 15, 0) \), where \( t_n \) is now a bootstrapped consensus tree and the values in the vector represent the confidence values for the individual bipartitions.

Figure 3(a) shows a bootstrapped consensus tree with five taxa. The values on the edges represent the bootstrapped confidence values. Figures 3(b) and 3(c) show nontrivial bipartitions of the tree. Notice that the bipartitions inherit the confidence value of the edge that corresponds to the bipartition.

By computing a consensus tree on the bootstrap samples, it is possible to introduce biases due to the fact that phylogenies that do not agree with the plurality are suppressed. This

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**Figure 2:** (a) A binary vector indexed by taxa names, (b) a binary representation of the bipartition in Figure 1(b), (c) a binary representation of the bipartition in Figure 1(c).

**Figure 3:** (a) Bootstrapped consensus tree with 5 taxa, (b) a bipartition with a 95% bootstrapped confidence value, (c) a bipartition with an 85% bootstrapped confidence value.
is particularly critical in our case where the biases of this kind of computation might compound during an analysis. A different approach that avoids computing a consensus tree too early in an analysis is by taking advantage of the spectra of the bootstrap samples. Before we can describe this construction, we need to define what we mean by an average spectrum. Given \( m \) spectra, \( S_1, \ldots, S_m \), in a bipartition space of \( n \) taxa, we define the average spectrum \( S_a \) as

\[
S_a = \frac{1}{m} \sum_{k=1}^{m} S_k.
\]  

The summation of spectra is well defined as vector additions in bipartition space and the multiplication of a scalar and a vector simply scales the components of the vector.

The bootstrap approach can be summarized as follows:

1. For the phylogenetic tree of each bootstrap sample, compute the corresponding spectrum.
2. Compute the average spectrum \( S_a \) over the bootstrap spectra.
3. The values that appear in the vector for the average spectrum can now be interpreted as confidence values.

Observe that computing the consensus tree for the average spectrum is a lossy operation (step 2) as before. However, the advantage of this approach is that we can defer this lossy operation as long as necessary. Note that we need only \( n - 3 \) top nonconflicting bipartitions. If conflicts are singular or minor events, they will not appear in the top \( n - 3 \) bipartitions because their confidence values will be low. If the conflicting bipartitions are among top \( n - 3 \), then the case deserves special attention. If the confidence values for bipartitions are rather small and randomly distributed over the data, this can serve as an indication that the data do not have a clean phylogenetic signal.

An interesting application of this is the construction of a consensus tree of multiple spectra in a bipartition space. If we interpret the spectra \( S_1, \ldots, S_m \) as a cluster in bipartition space, then the average spectrum can be viewed as the centroid of that cluster.

The following constructs a centroid consensus tree of \( m \) given spectra, \( S_1, \ldots, S_m \).

1. Compute \( S_a \) for \( S_1, \ldots, S_m \)
2. Sort the bipartitions in \( S_a \) according to their confidence values.
3. Delete all bipartitions in \( S_a \) that conflict with more strongly supported bipartitions in \( S_a \).
4. Incrementally construct a consensus tree from the remaining bipartitions in \( S_a \), starting with the bipartition with the strongest support to the bipartition with the weakest support.

Note that this is essentially the same algorithm as above with the exception that the spectra, \( S_1, \ldots, S_m \) are not bootstrapped samples but arbitrary points in some bipartition space.

### 2.4. Unsupervised learning in bipartition space

Self-organizing maps [4] were introduced by Kohonen in 1982 and can be viewed as tools to visualize structure in high-dimensional data. Self-organizing maps are considered members of the class of unsupervised machine learning algorithms, since they do not require a predefined concept but will learn the structure of a target domain without supervision.

Typically, a self-organizing map consists of a rectangular grid of processing units. Multidimensional observations are represented as vectors. Each processing unit in the self-organizing map also consists of a vector called a reference vector or reference model. In our case, the multidimensional observations are spectra, where the number of possible bipartitions given \( n \) taxa governs the dimensions of the spectra. The dimensions of processing elements of the map match the dimensionality of the observations.

The goal of the map is to assign values to the reference models on the map in such a way that all observations can be represented on the map with the smallest possible error. However, the map is constructed under constraints in the sense that the reference models cannot take on arbitrary values but are subject to a smoothing function called the neighborhood function. During training the values of the reference models on the map become ordered so that similar reference models are close to each other on the map and dissimilar ones are further apart from each other. This implies that similar observations will be mapped to similar regions on the map. Often reference models are referred to as centroids since they typically describe regions of observations with large similarities.

The training of the map is carried out by a sequential process, where \( t = 1, 2, \ldots \) is the step index. For each observation \( x(t) \) at time \( t \), we first identify the index \( i \) of some reference model which represents the best match in terms of Euclidean distance by the condition

\[
c = \arg \min_i \|x(t) - m_i(t)\| \quad \forall i.
\]  

The quantity \( m_i(t) \) refers to the reference model
at position $i$ on the map at time step $t$. Next, all reference models on the map are updated with the following regression rule where model index $c$ is the reference model index as computed above:

$$m_i(t + 1) = m_i(t) + h_{ci}[x(t) - m_i(t)] \quad \forall i.$$  \hspace{1cm} (6)

Here, $h_{ci}$ is the neighborhood function that is defined as follows:

$$h_{ci} = \begin{cases} 0 & \text{if } |c - i| > \beta, \\ \eta & \text{if } |c - i| \leq \beta, \end{cases}$$  \hspace{1cm} (7)

where $|c - i|$ represents the distance between the best matching reference model at position $c$ and some other reference model at position $i$ on the map, $\beta$ is the neighborhood distance and $\eta$ is the learning rate. It is customary to express $\eta$ and $\beta$ also as functions of time. This computation is usually repeated over the available observations many times during the training phase of the map. Each iteration is called a training epoch.

An advantage of self-organizing maps is that they have an appealing visual representation. That is, the structure of the input domain is graphically represented as a 2-dimensional map. Figure 4 shows a typical map computed in GPX (here the map reconstructed from bipartition matrix of 14 Archaeal species).

Each square in the map represents a reference model. The shading of the map represents the level of quantization or mapping error for the map. Light shading represents a small quantization error; that is, the reference models in those areas match the observations very closely. Dark shading represents a large quantization error; that is, there is a poor match between reference models and observations. Contiguous areas of low quantization error represent clusters of similar entities. Figure 4 shows an interactive cluster layout of the GPX tool. Each cluster contains a set of orthologous families that we put together by the SOM algorithm. By moving a mouse pointer over the map, a user is able to highlight and select clusters of interest and reconstruct phylogenetic trees for the selection.

Here, we make use of this ability of self-organizing maps to visualize high-dimensional spaces in order to visualize similarities and dissimilarities of high-dimensional tree spectra. We would expect points in bipartition space that represent similar spectra to map close together on the visualization and vice versa. Once we have identified clusters of spectra, we can proceed to compute consensus trees for those clusters. Furthermore, we can now compare the trees calculated from individual clusters to the overall consensus tree, and we can investigate whether there exists substantial conflict between the bipartitions of various clusters. Furthermore, the clusters that result from this unsupervised learning allow the biologist to detect trends in the evolutionary histories of the participating genes which might provide insight into events such as horizontal transfers of individual genes or whole metabolic pathways. The fact that the spectra of individual gene families can be visualized as consensus trees and that it is possible to compute the average of several selected spectra and the corresponding majority consensus tree on the fly distinguishes our approach from other spectral approaches (e.g., [3, 8]).

2.5. The construction of gene families

One of the insights of recent evolutionary biology is that it is not sufficient to use one or a few genes to infer phylogenetic relationships among species. Therefore, we propose to use as many genes as possible in our analysis based on the notion of a gene family. A gene family is a collection of genes from different genomes that are related to each other and share a common ancestor. In general, a gene family may include both orthologs and paralogs [9]. Here, we consider only sets of putatively orthologous genes where each species contributes only one gene into a family. The evolutionary history of an individual gene family is a phylogenetic tree.

We select common gene families based on reciprocal best BLAST [10] hit criteria [11] with relaxation (see below). The reciprocal best BLAST hit method requires strong conservative relationships among the orthologs so that if a gene from species 1 selects a gene from species 2 as the best hit when performing a BLAST search with genome 1 against genome 2, then the gene 2 must in turn select gene 1 as the best hit when genome 2 is searched against genome 1. The requirement of reciprocity is very strict and often fails in the presence of paralogs. To select more orthologous sets, we relax the criteria of strict reciprocity by allowing a fixed number of broken connections.

The gene families are aligned with Clustalw version 1.83 using default parameters [12]. For each family, 100 bootstrapped replicates are generated and evaluated with the Phym program [13] using the JTT model, four relative substitution rate categories, and an estimated shape parameter for the gamma distribution describing among site rate variation.

All 100 generated trees are split into their corresponding bipartition spectra and corresponding bootstrap support values are assigned to each bipartition by calculating how many times each bipartition is present in a family (the bootstrap procedure discussed in detail above). The result of these
calculations is a spectrum for each gene family. Observe that
trees calculated from individual bootstrap samples contain
edges that are not part of a majority consensus tree, that is,
the spectrum for a gene family can contain bipartitions that
conflict with other bipartitions in the spectrum. For our pur-
poses, this is important since it prevents information loss and
avoids bias during our analyses.

We can now use the machinery developed above to in-
vestigate the consensus tree of the collection of gene families
and whether there exist spectra that have a significant conflict
with the overall consensus tree.

3. APPLICATION OF GPX

GPX, a tool based on the techniques developed above sup-
ports an active, investigation-style analysis where the user
can interact with the visualization. The user is able to se-
lect centroids on the map and investigate consensus trees and
conflicting bipartitions in the respective spectra. A detailed
description of an experiment using GPX appears in [6]. In a
first experiment, we analyzed 123 gene families of 14 archaea
species. We found that sets of gene families exhibited sub-
stantial conflict with the overall organismal consensus tree
corroborating findings of frequent gene transfers between
organisms sharing the same or similar ecological niches
[14, 15]. In the consensus over all 123 gene families, the rep-
resentative of the Methanosarcinales (Methanosarcina ace-
tivorans) grouped with the Haloarchaean (Haloarcula maris-
mortui and Halobacterium salinarum) as expected from the
analysis of ribosomal RNAs and enzymes involved in trans-
scription and translation [16, 17]. Two clusters of gene fami-
lies were recognized that strongly supported a conflicting bi-
partition that places the homolog from Methanosarcina ace-
tivorans with Archaeoglobus fulgidus. For one of these clus-
ters, the relationships among the other archaea remained
otherwise compatible with the consensus, suggesting gene
transfer events between the ancestors of Methanosarcina and
Archaeoglobus. However, in case of the second cluster formed
by a single gene family, prolyl tRNA synthetases (prolylRS),
the Haloarchaeae grouped at the base of the euryarchaeota.
This placement suggests that the ancestor of the Haloarchaeae
might have acquired this enzyme from outside the archaean
domain, a finding that was corroborated through more de-
tailed phylogenetic analysis (Gogarten, unpublished). While
the haloarchaeal prolylRS are more similar to bacterial than to
archaeal homologs, database searches did not identify any
sequence from an extant organism that is specifically related
to the haloarchaeal prolyl tRNA synthetases. The donor of
the haloarchaeal prolylRS is not a member of any of the bac-
terial or archaean phyla that have prolylRS sequences in the
current nonredundant or environmental databases; possibly
the lineage that donated this enzyme has gone extinct as a
distinct lineage, and only those genes that were donated to
other lineages in the past survived into the presence [18].
These results were obtained by means of an originally de-
developed interactive tool [6], which combines computa-
tionally expensive analysis of complex data with convenient vi-
sual representation of phylogenetic information.

4. CONCLUSIONS

We developed a comparative genomic analysis technique
based on bipartition spectra and unsupervised learning. We
have incorporated the techniques developed here into a web-
based tool and have used this tool successfully in a set of anal-
yses. The tool allows the user to reconstruct the evolution-
ary history shared by the plurality of gene family histories
present within a collection of genomes; gene families with
histories that are in conflict with the plurality are detected,
and families which share conflicting histories can be recog-
nized, thereby facilitating the discovery of major “highways
of gene sharing” [15].

Bipartition spectrum analysis is not restricted to the
SOM algorithm, other clustering algorithms, such as prin-
cipal component analysis (PCA) [19] and local linear em-
bedding (LLE) [20], can be applied to the analysis of large
data sets. A new algorithm, generative topographic map-
ing (GTM) [21], displays maps similar to SOM but uses an
expectation maximization (EM) algorithm instead of
relying on neural network convergence. An alternative-to-
traditional PCA is kernel PCA [22]. This algorithm is based
on support vector machines, which allows it to easily deal
with very wide datasets. ISOMAP [23] is an algorithm sim-
ilar to LLE but distinguishes itself from LLE in that there is
no need to solve a set of linear equations. To make compara-
tive genomic studies a reality, we need to be able to include
large numbers of genomes. This implies that we need to be
able to handle large amounts of data. Future efforts will re-

ake around scaling up methodologies to include as many
species as possible and testing different clustering algorithms
for extraction of important phylogenetic information.

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