Disjoint connectivity of wireless sensor network

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ABSTRACT
Growing ramification in WSN contemplations are not restricted to routing, construction of protocols, dynamic of mobile nodes and infrastructure of the network. Although transcended to geometric level demonstrated as computational and dynamical geometries in spite of graph theory. In this paper we present step forward recognition features of a network devoted to solve the problem of reconstructing the disconnected network by connecting any disconnected chains. It considers geometrical properties of random depletion nodes deviated from unit grid. Number of chains and number of nodes in each chain are calculated with the average number of connections to a total nodes and longest chain. Histogram represented number of chains and numbers of nodes for each chain are used to show fragmentation of the network. Algorithm included a method to translate adjacent matrix to chain matrix and vice versa to check the agreement of initial case with the results. The amount of chain deviation and average connections per node for longest connected chain and for the total network are drawn as bar charts and conduct interpretations.

KEYWORDS
networks, WSN, disjoint connectivity, matLab, random depletion

1. INTRODUCTION

WSN is one of active and operational subjects, although the extended care to apply it [1, 2], many levels of studies are considered like infrastructure technology, electronics, microprocessors, digital signal processors DSP, communications, battery production technology and others of power sources [3–6]. Additional subjects are involved as network management, routing, types of protocols applied. Estimating capacity of transmitted data, network lifetime, maintenance, and fault tolerance are topics of important role in studying and implementing WSN [7–9].

Infrastructure of network includes methods of how the node distributed in the range of interest (RoI) and sometimes accesses the exact coordinates of each node (two or three dimensions). Knowing exact coordinates of nodes plays an important role especially in applications like indicating fire in a forest or a leakage in a petroleum pipe. The mechanism of allocated node position called localization while applying statistical information about node position, the number of connections between nodes may give approximate information about the efficiency and capacity of the network. The way of depletion nodes across RoI may play an important factor to all performants of the network and affects connectivity, coverage, routing and traffic of packets as the capacity of the node system.

WSN from geometric point of view is important like other studies, almost all scientists or engineers working on WSN do not give geometry of network any consideration according to replace the whole routing problem to topology and tree connection between nodes or depend on statistical information and leave geometry as a losing end especially when position of node is relevant to the application [10–12]. Although geometry of a network is connected to a graph theory and computational geometry, these branches of mathematics lead to dynamic geometry that will bring network geometry to new fields and interact with more general aspects and concepts in both ways [13, 14]. Beginning with localization is a keystone to solve
problems of network. Ubiquitous software is applied for simulation of WSN, like opnet, C++ and MATLAB programs, they are working over different levels of obligations and complexity. Estimating packet transfer capacity acting with different structures of protocols and verity of node connection methods are one level. Simulating the details of electronic block diagram circuit defined each WSN node, reading communication patterns and capability of transmission, then time response and synchronization of all that are another level [15, 16].

Prim topics in WSN are connectivity and coverage. Connectivity is about determining the connection between nodes – homogeneous or heterogeneous – and finding losing end chains or isolated nodes, although calculating area coverage is a complementary topic to connectivity [6, 17] and a way to notice the efficiency of WSN to handle, calculating area coverage need to discriminate chains and isolated nodes, which is the topic of this paper, then find area coverage for each.

In this paper we encounter estimating number of chains (connected nodes but disjoint from other nodes), number of nodes in each chain and average connections to a longest one and compare that with the average connections to all nodes in the network, this is done with different number of nodes, different densities and verity of maximum transmission distances. Within many years of research, we did not find any independent attempt to find geometric properties of WSN. Studding included chains in the network is an algorithm used to predict efficient routing; this algorithm recognizes many chains in the network with predefined number of nodes, then selects suitable node within each chain and discriminates it as prime node. It is used as a connected node to main node or connected to a sink node. This algorithm simplifies routing techniques for the network [18, 19]. Defined number of chains and the length of each chain gives important parameters to evaluate the properties of network and it is a step to word find algorithms to connect these chains in a proper way, also estimating average connection of nodes in chain and in a total graph indicate side of the properties of the network [20]. Detecting many chains in the network and the longest chain length is small fraction of the total nodes (diversity is about one) this network is of poor efficiency and cannot be used to any communication tasks, while if a diversity near zero indicates that more nodes are connected to main chain then transmission rate will be better. If network is disconnected a suitable technique may be used like network control, increasing transmission radius, or repositioning mobile nodes to establish connections to fragmented or insulated parts, the two methods are actually used [21].

2. FIND THE LONGEST CHAIN ALGORITHM

2.1. Algorithm attended

To find the longest chain in connected graph of simulated wireless sensor network algorithm that is written to simulate random depletion of nodes and find connected graph within maximum transmission radius then new method is written to find connected chains of nodes and estimate the longest one, and the algorithm is used to find statistical results for connected nodes in random distributed WSN.

The details of algorithm are explained in the following steps:

Step1: Estimate arbitrary coordinate matrix XY0:
(a) Set uniform grid x & y coordinates of a pre-defined grid step.
(b) Add random normal distribution of x & y coordinates of zero mean value and variation of 1 or 2 grid step.

Step2: Find connected matrix by calculating distance between nodes and connect (α0 = 1) then if distance (dij) < maximum transmission radius (R0) to generate connected matrix [22].

Step3: Find connected chain matrix by constructing a sequence of connected nodes to current node, these groups of nodes may be connected to each other and construct a chain Part of Mat-LAB m-file to generate chain matrix from connected [23].

Step4: Find optimization connected group matrix by checking each sequence with the previous, if any common node combining the two sequences without repeated nodes.

Step5: Change maximum transmission radius (R0) and repeat from step2.

Step6: Draw longest chain on original connected graph as shown in Fig. 1.

Step7: Create histogram in Mat-LAB m-file if number of chains has the same number of nodes and draw it for each maximum transmission radius.

![Fig. 1. Sample of Plot of original connected graph and longest chain marks with different color](image-url)
Step 8: Calculate:

- Diversity factor \( \frac{1}{C_0} \) where \( C_0 \) is the number of nodes in the longest chain.
- Average connections in graph \( \frac{\text{no. connections in network}}{\text{number of nodes in total network}} \)
- Average connections in longest chain \( \frac{\text{no. connections in longest chain}}{\text{number of nodes in longest chain}} \)

Step 9: Using Microsoft Excel program to collect data of diversity factor and average connections for total network and longest chain and draw bar charts for collected data for each collected case with different maximum transmission radius and deviations.

2.2. Applied algorithm

Algorithm created above is achieved using Matlab m-files and executed with:

1. Uniform grids 5 x 5 or 10 x 10 units with step value 1 or 2.
2. Deviation of 0.5, 1, and 2 units.
3. Density of 1, 4, and 9 node/unit squared.
4. Radius of 0.95, 1.2, 1.5, and 1.95 for density 1 node/unit squared, radius of 0.475, 0.6, 0.75, 0.975, and 1.25 for density 4 nodes/unit squared, and radius of 0.13667, 0.4, 0.65, and 0.8333 for density 9 nodes/unit squared.

Application success of algorithm includes two stages:

1. Number node connected matrix is produced from adjacent matrix making chain connections according to the applied algorithm, then adjacent matrix is reproduced from new matrix, comparisons are achieved by drawing

| Density (nodes/Unit Squared) | \( R_{\text{max}1} \) | \( R_{\text{max}2} \) | \( R_{\text{max}3} \) | \( R_{\text{max}4} \) | \( R_{\text{max}5} \) | Remarks |
|-----------------------------|------------------|------------------|------------------|------------------|------------------|---------|
| 1                           | 0.95             | 1.2              | 1.5              | 1.95             | 2.5              | \( R_{\text{max}} \) |
| 4                           | 0.475            | 0.6              | 0.75             | 0.975            | 1.25             | \( R_{\text{max}} / \sqrt{4} \) |
| 9                           | 0.35             | 0.4              | 0.5              | 0.65             | 0.733            | \( R_{\text{max}} / \sqrt{9} \) |

*Fig. 2. Connected graph and the longest chain obtained with \( R_0 = \) (a) 0.95 (b) 1.2 (c) 1.5 and (d) 1.95 units*
old and new adjacent matrices connected graphs, both graphs are matched. This test helps to accurate algorithm mechanism from bugs and miscalculations.

2. Longest chain in network is redrawn on original connected graph, so match of the longest chain is ensured directly on graph. Therefore, redrawing new adjacent matrix is no longer important since no new information can be noticed any more.

To ensure accuracy of the algorithm small network is used as examples to check results with manual calculations and estimations, like number of nodes in a longest chain, number of chains formed, and number of connections per chain. All examples fit the results.

Many equations are used to define magnitude of chain deviations:

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**Fig. 3.** Histogram of number of chains have any number of connected nodes for 100 nodes with node density 1 node/unit squared and unit diversity factor for different maximum transmission distances $R_0$ (a) 0.95 (b) 1.2 (c) 1.5 & (d) 1.95 units

**Fig. 4.** Diversity factor with different deviations and maximum transmission radius $R_0$

**Fig. 5.** Average connection per node in longest chain with different $D$ and $R_0$
3. THE RESULTS OF FINDING LONGEST CHAIN ALGORITHM

First: The average connections of nodes in longest chain are always more (or equal only when all nodes in network are connected to longest chain) than average connections of the network, see Table 1. This is self-evident, since in network many nodes are single or with few connections, contrary to connected chain.

Second: Deviations of chains in a network is big when maximum transmission radius is less than grid step. It seems that a dramatic change will occur when radius of maximum transmission is greater than three fourth of the grid step, \( R_0 > 0.75 \cdot D \) as shown in Fig. 2a, b, c, and d.

Third: Histograms of the four cases previously mentioned are drawn, these histograms emphasize clearly

\[
\text{Diversity Factor} = \frac{\text{No. of Nodes in Longest Chain}}{\text{No. of Nodes in Total Graph}}
\]

\[
\text{Average Connections in Longest Chain} = \frac{\text{No. Connections in Longest Chain}}{\text{No. Nodes in Longest Chain}}
\]

\[
\text{Average Connections in Total Graph} = \frac{\text{No. Connections in Total Graph}}{\text{No. Nodes in Total Graph}}
\]

\[
\text{Fig. 6. No. of node in longest chain for different } D \text{ and } R_0
\]

\[
\text{Fig. 7. Connected graph for } 10 \times 10, 4 \text{ nodes/unit squared with } R_0 = (a) 0.457 \text{ (b) 0.6 (c) 0.75 (d) 0.975 units}
\]
what graph plots of connected nodes show. Many different
node number short chains occur when maximum trans-
mission radius is small compared to grid step and many
single nodes also as shown in Fig. 3a and b. While at
maximum transmission radius greater than three fourth of
grid step a clear long chain of nodes occurs, as shown in
Fig. 3c and d.

Forth: Diversity factor (the percentage ratio of number
of connected nodes in longest chain to the total number
of overall nodes in area) and average number of connections
per node for longest chain and overall nodes are estimated
according to Eqs (1) and (2) with respect to different
maximum transmission radius. Bar chart created by Excel
shows that a large disperse of chains occur when small
maximum transmission radius is used. While, when radius
of transmission being larger than three fourth of grid step
disperses will be rapidly decreases and connections of
longest chain may cover all nodes especially when maximum
transmission radius approaches full step of grid. When the
magnitude of deviation about grid crosses tends to change
the behavior of connections are the same for different
diversities with small differences. In large deviation more
nodes on edges of the area may be deviated far from age and
not connected to their neighbors, as shown in the first series
in Fig. 4 for deviation of two units, although maximum
transition radius is large, deviation still has effect the
connections.

Any longer transmission radius will case more and more
power dissipation and shorter battery and network life. Also,
there will be more and more average connections to longest
chain in the network, so the average of number of connect-
ions of longest chain also depends on measuring the quality
of services (QoS) of the network. Average number of con-
nections per connected node in a longest chain is recorded
and drawn as an Excel bar chart. Figure 5 shows that when
depletion deviation is equal to one unit, results will be med-
ium compared with smaller or larger deviations. Also
connections will be greater if the deviations of nodes are
smaller when maximum transmission radius is at three
fourth of grid step, that is local factors act between nodes,
while when maximum transmission radius is bigger, this
case will disappear, and adjacent nodes of different grid
crossing have the domination effects as shown in Fig. 6.

Fifth: For dense depletion nodes a smaller maximum
transmission radius is needed. Since connections between
nodes depend on the mean distances between them, the
expectation maximum transmission radius will be reduced
as a square root of a uniform increasing in depletion density
especially the area under consideration is squared. So to keep
comparisons between radii of different density depletions it

Fig. 8. Connected graph for $10 \times 10$, 9 nodes/unit squared with $R_0 = (a) \ 0.31667 \ (b) \ 0.4 \ (c) \ 0.5 \ (d) \ 0.65 \ units$
is more logical to compare radii of inverse relation with the square root of depletion density to each other:

\[ R_{\text{max}} = \frac{R_0}{\sqrt{D_n}} \]  

(7)

Where \( R_0 \) is maximum transmission radius for depletion density \( D_n = 1 \) and \( R_{\text{max}} \) is equivalent maximum transmission radius for larger densities.

Basic \( R_{\text{max}} \) and related radii for different densities obeying relation 7 are shown in Table 1.

Network with 4 nodes per unit squared density and different maximum transmitted radios are plotted as shown in Fig. 7.

Network with 9 nodes per unit squared density and different maximum transmitted radios are also plotted as shown in Fig. 8.

The Longest connected chain in both densities in graphs show the same behavior as in lower node density where the connections are dominant for maximum radius of transmission greater than grid spacing divided by square root of node density as in Eq. (7). Then scaling of node densities can be confirmed for the same area of depletion.

Also, no significant signs are found and the minor differences in graph due to deviations may also be scaled. Number of nodes connected are scaled, while average connections per node about the same values as shown in Figs 9 and 10.

4. CONCLUSIONS AND FUTURE WORKS

Wireless Sensor Networks are still a hot topic especially in mobile network and because it is part of more sophisticated articles dealing with the Internet of thing (IoT), (FOG) and CLOUD systems and technologies, since multiple objects must be connected with each other, and these relations must be geometrical, routing and smart connections. So that studying wireless sensor network as theoretical and geometrical properties will always support manufacturing and applying WSN in real world. Estimating the longest chain in connected network as a simple geometric configuration is one of many in this trained to study behavior and efficiency of network therefore to control, optimize network and so on. Knowledge of node coordinates in random depletion method is a partly solved problem and needs to be more researched in the future. The project simulates network as a simple disk model, while almost all WSNs are clustering configurations and it is important to upgrade model to deal with clustering configuration by using different maximum transmission radii for different nodes. Using different network models can be done in future works and may include elliptical or multi-hop transmission patterns.

No real efforts are found for finding longest node connected chain as a target method to compare, this trained of searching need to consider especially for data analysis and pattern recognition, this paper tries to give chain properties of nodes in a network more attentions.

Random distributed method in use is deviate \( X \) and \( Y \) coordinates from uniform grid with predefined step length, using different depletion methods can be helpful for more realistic presentations.

Find solutions to connect discriminated chains by inserting, mobile few nodes or increasing maximum transmission range of specific nearest nodes between disconnected chains, these solutions may the topic of future projects.

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