Introduction

The replacement of fossil fuels with renewable fuels (e.g., H₂) will be an important part of addressing issues related to CO₂ emission. Anion exchange membrane fuel cells (AEMFCs) are a state-of-the-art technology that efficiently convert chemical energy to electricity without the use of expensive Pt-group electrocatalysts. The alkaline anion exchange membrane (AAEM) and the anion exchange ionomer (AEI), which are both composed of polymeric backbones with pendant cationic functional groups, are critical components in AEMFCs and are responsible for conducting hydroxide anions from the cathode to the anode. Unfortunately, the chemical instability of these cationic polymers towards hydroxide anions remains one of the major obstacles for the development of viable AEMFCs. Both the polymeric backbones and the tethered cations must be stable to alkaline conditions in order to produce durable devices.

Given that cation degradation under alkaline conditions is a major problem, many cationic moieties have been investigated for AAEM applications, including ammonium, phosphonium, imidazolium, and metal-based cations. Model compound studies can shed light on cation stabilities and their mechanisms of degradation. Notably, in 2015, Marino and Kreuer suggested incorporating piperidinium cations within AAEMs due to their outstanding alkaline stability and ease of synthesis. Since then, several groups have developed strategies to synthesize piperidinium-functionalized AAEMs. For example, Jannasch and coworkers prepared a multi-piperidinium-functionalized AAEM with a hydroxide conductivity of 221 mS cm⁻¹ at 80 °C. These results suggest that piperidinium cations are promising structural motifs for high-performance AAEMs.

Alkaline anion exchange membranes (AAEMs) with high hydroxide conductivity and good alkaline stability are essential for the development of anion exchange membrane fuel cells to generate clean energy by converting renewable fuels to electricity. Polyethylene-based AAEMs with excellent properties can be prepared via sequential ring-opening metathesis polymerization (ROMP) and hydrogenation of cyclooctene derivatives. However, one of the major limitations of this approach is the complicated multi-step synthesis of functionalized cyclooctene monomers. Herein, we report that piperidinium-functionalized cyclooctene monomers can be easily prepared via the photocatalytic hydroamination of cyclooctadiene with piperidine in a one-pot, two-step process to produce high-performance AAEMs.

Possible alkaline-degradation pathways of the resultant polymers were analyzed using spectroscopic analysis and dispersion-inclusive hybrid density functional theory (DFT) calculations. Quite interestingly, our theoretical calculations indicate that local backbone morphology—which can potentially change the Hofmann elimination reaction rate constant by more than four orders of magnitude—is another important consideration in the rational design of stable high-performance AAEMs.
oxidative degradation in an operating membrane electrode assembly (MEA). Therefore, it is advantageous to prepare analogous AAEMs free of aromatic substituents. Some aromatic-free AAEMs have been prepared with polyolefin backbones, including polyethylene (PE), polypropylene, polynorbornene, and polytetrafluoroethylene (PTFE). Among these materials, PE-based AAEMs have shown promising chemical stability and mechanical integrity. These materials are conveniently prepared from a ring-opening-metathesis polymerization (ROMP)/hydrogenation sequence of cyclooctene (COE) monomers functionalized with various cations, including ammonium, phosphonium, imidazolium, and cobaltocenium. Despite the outstanding properties of PE-based AAEMs, one of the major limitations of these materials is the laborious synthesis of the cationic monomers, which usually requires four to eight linear steps from commercially available starting materials. To the best of our knowledge, this is the first report of aromatic-free piperidinium- and quinuclidinium-functionalized AAEMs.

Results and discussion

Optimization of monomer synthesis

In our previous report on the photocatalytic hydroamination of olefins, we disclosed that COD could be directly functionalized with piperidine. Although the reported conditions were noteworthy for their high efficiency across a broad scope of substrates, we identified a number of factors that made them less ideal for the large-scale synthesis of AAEM monomers, such as the high loading of photocatalyst [Ir(dF(Me)ppy)2(dtbbpy)] PF6 ([Ir-cat], 2 mol%), the use of commercially unavailable 2,4,6-trisopropylbenzenethiol (TRIP thiol) as H-atom transfer (HAT) catalyst (50 mol%), and the relatively dilute reaction conditions (0.05 M). Seeking to develop an efficient multi-gram synthesis of cyclooctene-piperidine monomers, we commenced optimization studies (Table 1). Using the original conditions, we observed the desired addition product in 76% yield based on piperidine (entry 1), with the major side product resulting from double hydroamination of the alkenes in COD. Increasing the equivalents of COD from 5 to 10 gave a modestly improved yield and markedly decreased the over-hydroamination side products (entry 2). Increasing the reaction concentration from 0.05 M to 0.2 M in toluene reduced the reactivity of the system (entry 3), but an accompanying reduction in photocatalyst loading boosted the yield to 86% (entry 4). We were also pleased to find that the reaction still worked efficiently with only 15 mol% HAT catalyst (entry 5). Switching to thiophenol as a simpler HAT catalyst proved to be slightly less efficient (entry 6), but in weighing the practicality of the reaction we opted to move forward with this system.

We then evaluated the possibility of a telescoped sequence to directly isolate the quaternary ammonium monomers. After the optimized hydroamination reaction described above (Table 1, entry 6), the toluene, unreacted piperidine, COD, and thio-phenol catalyst were removed under reduced pressure. The residue was refluxed with 2 equiv. of MeI in THF for 2 hours providing white solid 1 in 81% yield after trituration in Et2O. This one-pot, two-step approach can be used to prepare monomers expediently in at least 1.5 gram scale (see the ESI† for more details). Similar strategies were applied to synthesize other piperidinium-functionalized monomers, including ethyl (2), n-butyl (3), and n-octyl (4) derivatives (Scheme 2A). Quinuclidinium monomer 5 was prepared in 30% yield over two steps via hydroamination of COD with 2-(piperidin-4-yl)ethanol followed by an Appel reaction (Scheme 2B).
Membrane synthesis and properties

With various functionalized cyclooctene monomers in hand, a series of piperidinium-functionalized AAEMs (i.e. PEPM, PEPE, PEPB, PEPO, and PEQ) membranes from monomers 1–5, respectively) were prepared via a ROMP/hydrogenation sequence (Table 2). The functionalized monomers were first copolymerized with cis-COE by adapting our previous ROMP procedures. The molar ratio of cis-COE to Grubbs II catalyst was 800 : 1, and the incorporation of the ionic monomers can be easily tuned by changing their loading (Table 2). The resulting copolymers were then hydrogenated using Crabtree’s catalyst and H2 to produce AAEMs with PE backbones. After hydrogenation, the AAEM thin films were cast via a melt-pressing method, and the anions were exchanged to hydroxide in a 1 M KOH aqueous solution before measuring hydroxide conductivity (σ(OH−)22 °C), water uptake (WU), and dimensional change (ΔL) (Table 2). Their ion exchange capacities (IECs) were determined by comparing integration ratios in 1H NMR spectra (Table 2), and the results were consistent with monomer feeding ratios and Mohr titration results (see the ESI Table S4† for more details). When R = Me, both the hydroxide conductivity and WU increased with IEC, and it was found that the cation incorporation ratio in the range of 20–23% allowed
for a good balance between the two properties ($\text{PEPM}_{20}$ and $\text{PEPM}_{23}$) (Fig. 1A). Therefore, we controlled the cation incorporation ratio in substituted piperidinium (Et ($\text{PEPM}_{20}$), iBu ($\text{PEPM}_{23}$), and nOct ($\text{PEPM}_{28}$)) and quinuclidinium ($\text{PEQ}_{20}$) AAEMs to be approximately 20 mol% ($\text{PEPE}_{20}$, $\text{PEPB}_{18}$, $\text{PEPO}_{23}$, and $\text{PEQ}_{20}$, respectively). Excellent WU (within 40%) and $\Delta L$ (within 11%) performance was observed for all membranes with different alkyl substituents. $\text{PEPB}_{18}$ and $\text{PEPO}_{23}$ exhibited relatively low hydroxide conductivity, but they became significantly more conductive after 1 M KOH treatment at 80°C for 3 days (vide infra, see Fig. 2). This is likely because their hydrophobic side chains slowed down the anion exchange process, so that longer time and higher temperatures were required for thorough hydroxide exchange. The hydroxide conductivities at 80°C of AAEMs with methyl substituents were found to be in the range of 74–95 mS cm$^{-1}$ (Fig. 1B), which are comparable to previously reported piperidinium functionalized AAEMs with similar IECs.$^{39-42,45-53,76}$

**Membrane alkaline stability**

In line with previously observed mechanisms for cation degradation,$^{16,24-18,77}$ we expected there to be two major degradation mechanisms (i.e., nucleophilic substitution and Hofmann elimination) at three different sites in these piperidinium-functionalized AAEMs (i.e., the piperidinium ring, the alkyl substituent, and the PE backbone). Since nucleophilic substitution at the methine center of the polymer backbone should be relatively unlikely, we anticipated the five possible degradation pathways summarized in Scheme 3. Pathways a and b arise from nucleophilic substitution, while pathways c, d, and e derive from $\beta$-hydrogen Hofmann elimination.

The membranes were soaked as strips in 1 M KOH at 80°C for 30 days, and their alkaline

![Fig. 1](A) Membrane hydroxide conductivity and water uptake of PEPMs with different ionic contents. (B) Membrane hydroxide conductivities of PEPMs under different temperatures.

| Samples     | Ionic monomer | mol% of 1–5 | IEC$^b$ (mmol I$^-$/g) | $\sigma^c$ (OH$^-$, 22°C) (mS cm$^{-1}$) | WU$^d$ | $\Delta L^e$ |
|-------------|---------------|-------------|------------------------|--------------------------------------|------|-------------|
| $\text{PEPM}_{0.16}$ | 1             | 16%         | 1.09                   | 26 ± 1                               | 22%  | 4%          |
| $\text{PEPM}_{0.20}$ | 1             | 20%         | 1.31                   | 35 ± 2                               | 26%  | 7%          |
| $\text{PEPM}_{0.23}$ | 1             | 23%         | 1.41                   | 43 ± 2                               | 54%  | 8%          |
| $\text{PEPM}_{0.28}$ | 1             | 28%         | 1.61                   | 53 ± 2                               | 92%  | 9%          |
| $\text{PEPE}_{0.20}$ | 2             | 20%         | 1.23                   | 36 ± 2                               | 28%  | 6%          |
| $\text{PEPB}_{0.18}$ | 3             | 18%         | 1.12                   | 16 ± 1                               | 24%  | 6%          |
| $\text{PEPO}_{0.23}$ | 4             | 23%         | 1.23                   | 15 ± 5                               | 40%  | 8%          |
| $\text{PEQ}_{0.20}$ | 5             | 20%         | 1.23                   | 35 ± 1                               | 36%  | 11%         |

$^a$ See the ESI for more details. $^b$ Determined by $^1$H NMR analysis before hydrogenation. $^c$ Determined from the average of three trials ± standard deviation. $^d$ Water uptake at 22°C = 100 × [mass$_{\text{wet}}$ − mass$_{\text{dry}}$]/mass$_{\text{dry}}$%. $^e$ Dimensional change at 22°C = 100 × [length$_{\text{wet}}$ − length$_{\text{dry}}$]/length$_{\text{dry}}$%.
stabilities were evaluated by both changes in hydroxide conductivities (Fig. 2) and Fourier-transform infrared (FT-IR) spectroscopy (Fig. 3). The methyl-substituted piperidinium PEPM$_{20}$ and quinuclidinium PEQ$_{20}$ showed the best conductivity stability (80% and 71% retained conductivity, respectively). The hydroxide conductivities of PEPB$_{18}$ and PEPO$_{23}$ boosted during the first three days with the plausible reasons discussed above, while drastic conductivity decreases were observed afterwards (21% and 40% remaining, respectively). AAEMs with ethyl substituents (PEPE$_{20}$) exhibited obvious conductivity loss from the beginning of the stability tests (42% remaining after 30 days). These overall stability trends agreed well with previous reports.$^{38,39}$ One of the most stable AAEMs, PEPM$_{30}$, was further evaluated for its mechanical stability before and after the alkaline treatment (Fig. S38†). It was found that the as-synthesized membrane PEPM$_{30}$ (fully hydrated in the iodide form) was strong and ductile (22 MPa stress and 330% strain at break), then the membrane became relatively weaker (15 MPa) yet more ductile (357% strain) after soaking in 1 M KOH$_{aq}$ at 80 °C for 30 days. Their excellent mechanical properties were comparable to Nafion™ N115 (32 MPa stress and 310% strain at break).$^{29}$ The elongation properties of these PE-based AAEMs significantly outperformed the rigid AAEMs derived from poly(aromatic)s.$^{34,35}$

To interrogate the degradation pathways, we used FT-IR spectroscopy to study the structural changes in these membranes before and after the alkaline treatment (Fig. 3). Piperidine-functionalized PE (PEP$_{26a}$) was also prepared from the HCl adduct of the hydroamination intermediate (compound S1†) using an analogous ROMP copolymerization strategy followed by deprotonation to mimic some of the proposed degradation products (pathways b and c in Scheme 3, see ESI† for more details).$^{25}$ Since the as-prepared PE-based AAEMs cannot be dissolved in common organic solvents, solid-state characterization methods such as FT-IR are advantageous. Originally, we proposed that the piperidinium AAEMs would give extremely clear FT-IR spectra, as there are only three types of bonds in these aromatic-free polymers (i.e., C–C, C–H, and C–N bonds). However, as shown in Fig. 3 and S39† we noticed that the signals of C–N bonds were too weak to be confidently assigned in comparison to the strong C–H bond signals (1460 cm$^{-1}$ and 2800–3000 cm$^{-1}$). The small hump peaks at 1650 cm$^{-1}$ and 3300 cm$^{-1}$ were from water in membranes.$^{80}$ The FT-IR spectra of PEP, PEPM, PEPE, PEPB, PEPO, and PEQ were almost the same (Fig. S39†) suggesting that FT-IR spectroscopy might not be sensitive enough to distinguish piperidine and piperidinium in these polymer samples. A new peak at 964 cm$^{-1}$ possibly suggested the presence of alkene groups in the polymer after alkaline treatment (the red trace in Fig. 3), yet it is hard to clearly assign it as pathways d or e in Scheme 3. As an important note, we observed that when we performed the stability studies in soda lime glass vials, there were always new broad peaks around 1050 cm$^{-1}$ in FT-IR spectra for all the samples after alkaline treatment (see the blue trace in Fig. 3 and S40†). These peaks were attributed to Si–O bonds from glass etching, as we measured the weight of the glass vials dropping by near 0.5 g after the stability studies (Table S5†). We also observed relatively slower conductivity decrease in glass vials (Fig. S41†). Although similar glass etching problems have been observed in alkaline stability studies,$^{81,82}$ this is the first spectroscopic evidence to prove that the detached Si–O substances could be adsorbed by polymer samples to affect their ionic...
conductivities. Plastic containers made from PP and PTFE are recommended to perform aqueous alkaline stability tests.\textsuperscript{18}

To gain more insight into the degradation mechanism, we decided to use solution-based \textsuperscript{1}H NMR analysis, as it can provide quantitative degradation kinetics and clearer degradation product assignments. Our group has previously conducted alkaline stability studies under accelerated degradation conditions by treating model compounds or polymers with KOH solutions in CD\textsubscript{3}OH using 3-(trimethylsilyl)-1-propanesulfonic acid sodium salt as the internal standard at 80 °C in sealed NMR tubes.\textsuperscript{10,25,26,36} As a side note, control experiments showed that borosilicate glass NMR tubes were more resistant to basic corrosion and there were almost no changes to their weights after the KOH/methanol stability studies (Table S5†).\textsuperscript{10} One requirement of this NMR stability protocol is that the studied model compounds or polymers must be soluble in methanol. Fortunately, we can easily tune their solubilities by changing the cation incorporation ratio and molecular weight during the ROMP copolymerization process. For example, to get the cation incorporation percentage was slightly lower than expected in these oligomers, and monomers 1–5 gave rise to oligomers PEPM\textsubscript{52}, PEPE\textsubscript{54}, PEPEB\textsubscript{58}, PEPO\textsubscript{64}, and PEQ\textsubscript{55}, respectively (see ESI† for more details).

We then subjected five cationic oligomers and a small molecule model compound N-hexyl-N-methylpiperidinium bromide (6) to the accelerated alkaline degradation conditions: 2 M KOH in CD\textsubscript{3}OH at 80 °C for 30 days (Fig. 4). The use of CD\textsubscript{3}OH makes anions ([OH\textsuperscript{−}] and [OCD\textsubscript{3}\textsuperscript{−}]) more reactive due to a smaller hydration sphere, and also prevents potential H/D exchange reactions.\textsuperscript{18,36} We found that cationic model compound 6 had very good alkaline stability (94% remaining after 30 days), and detected small amounts of byproducts from both nucleophilic demethylation (3%) and Hofmann elimination (2%).\textsuperscript{81} However, we observed much faster cation degradation in oligomers with the general trend being PEQ ≈ PEPM > PEPE > PEPB > PEPO. Oligomers PEPM\textsubscript{52}, PEPEB\textsubscript{58}, and PEPO\textsubscript{64} decomposed mostly through backbone Hofmann elimination (e) under these accelerated KOH/methanol conditions, as large quantities of N-alkylpiperidines were detected as byproducts (Fig. 4). We observed 27%, 55%, and 66% N-methyl-, N-butyl-, and N-octyl-piperidine compared to 41%, 87%, and 93% degradation from the corresponding PEPM\textsubscript{52}, PEPEB\textsubscript{58}, and PEPO\textsubscript{64}, respectively. In all these cases, we also detected a broad single peak around 5.4 ppm, which is consistent with internal alkene peaks. The trend of increasing length of alkyl chains facilitating Hofmann elimination elsewhere is consistent with what Jannasch and coworkers demonstrated for their piperidinium-functionalized AAEs, although they observed ring-opening Hofmann elimination as the major degradation pathway due to rigid substituents on the piperidinium ring.\textsuperscript{19} Ring-opening Hofmann elimination and nucleophilic ring opening degradation may also occur under our conditions, but these minor degradation pathways are extremely difficult to be accurately quantified by \textsuperscript{1}H NMR analysis in the complicated reaction system. Interestingly, a volatile degradation byproduct, ethylene, was detected from the degradation of PEPE\textsubscript{54} oligomer (31% remaining). The backbone elimination (22%, e) and ethyl elimination (26%, c) gave similar rates under the testing conditions. Quinuclidinium PEQ\textsubscript{55} gave 30% nucleophilic ring-opening degradation out of its 35% cation degradation, probably owing to the ring strain in this bicyclic scaffold. It is noteworthy that for all these oligomer studies in sealed NMR tubes, we observed the formation of dark insoluble materials, which likely formed as the oligomers became electroneutral and less polar after degradation, diminishing their solubility in methanol. These findings highlight the importance of using an internal standard to track polymer alkaline stabilities through \textsuperscript{1}H NMR analysis, as key information about volatile and insoluble byproducts could be easily missed otherwise.

To provide additional insight into the degradation mechanisms of these piperidinium- and quinuclidinium-functionalized AAEs, we used dispersion-inclusive hybrid density functional theory (DFT) in conjunction with an implicit
solvent model to compute free-energy barriers ($\Delta G^\ddagger$) for the degradation pathways in Scheme 3 under the experimental conditions (2 M KOH/CD$_3$OH, 80 °C). To do so, we constructed models of the PEPM, PEPE, and PEQ systems (i.e., model-PEPM, model-PEPE, and model-PEQ) in which the PE backbone was truncated to include only seven carbon atoms (see Fig. 5B for a graphical depiction of model-PEPM; see Theoretical and computational methods for a detailed description of the computational protocol).

For model-PEPM, $\Delta G^\ddagger$ values associated with Hofmann elimination (d, e) were lower than that of $\text{SN}_2$ (a, b) by ca. 4–6 kcal mol$^{-1}$, which suggests that these nucleophilic substitution channels were not the primary degradation modes in this system (see Table 3). When comparing amongst the Hofmann elimination pathways, DFT predicted that d was preferred over e by $\Delta \Delta G^\ddagger = \Delta G^\ddagger_d - \Delta G^\ddagger_e = 1.2$ kcal mol$^{-1}$. This $\Delta \Delta G^\ddagger$ value corresponds to a factor of ca. 5.5 in the relative degradation rate constants (i.e., $k_d/k_e = \exp[(19.8 \text{ kcal mol}^{-1}) -$

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**Fig. 4** Alkaline stability evaluation of model compound 6 and oligomers under 2 M KOH/CD$_3$OH conditions at 80 °C for 30 days: degradation kinetics by $^1$H NMR analysis (left) and byproduct assignment (right).

**Fig. 5** (A) Free-energy barriers ($\Delta G^\ddagger$ in kcal mol$^{-1}$) corresponding to the degradation pathways in Scheme 3 for model-PEPM as a function of an applied force (F in nN) to the distance (D) between $\gamma$-carbons on the polymer backbone. All barrier heights were computed with CH$_3$O$^-$ as the nucleophile and base (i.e., at the experimental conditions of 2 M KOH/CD$_3$OH, 80 °C) using the EFEI approach in conjunction with dispersion-inclusive hybrid DFT and an implicit solvent model. (B) Top: Graphical depiction of model-PEPM. Bottom: Tabulated statistics describing the model-PEPM backbone as a function of F. Even with the largest forces considered in this work (F = ±0.25 nN), the average backbone C–C bond length ($\langle d_{cc}\rangle$) and C–C–C bond angle ($\langle \theta_{ccc}\rangle$) remained largely unchanged from their force-free (F = 0 nN) values.
21.0 kcal mol⁻¹)/RT] = 5.5 at T = 80 °C in accordance with transition state theory (TST), see Theoretical and computational methods. As described above, ¹H NMR analysis indicated that byproducts from e comprised 66% of the PEPM degradation (i.e., 27% of the total 41% degradation; see Fig. 4), while the remaining 34% remained unassigned (potentially due to solubility issues, vide supra). According to the theoretical results in Table 3, this unassigned portion most likely resulted from d, as the Sn2 pathways have substantially higher ΔG² values. Although DFT errors in the prediction of relative barrier heights can exceed 1.0 kcal mol⁻¹,⁴⁴ our calculations on model-PEPM suggested that d should be the dominant degradation pathway, while ¹H NMR analysis showed a slight preference for e.

To further explore this issue, we investigated one aspect of the experiment that was not accounted for in the theoretical ΔG² in Table 3, namely, how the local conformation of the polymer backbone affects degradation kinetics in piperidinium-based AAEMs. To do so, we sampled both compressed and extended backbone conformations in model-PEPM, and computed ΔG² for each degradation pathway as a function of backbone geometry (see Fig. 5). This was accomplished by applying a small tensile force (F) to the distance (D) between the γ-carbons (Cγ) in model-PEPM via the external forces explicitly included (EFEI) approach.⁴⁵ In doing so, we explored a wide range of backbone conformations without perturbing the backbone C–C bond lengths (and C–C–C bond angles) in model-PEPM, thereby mimicking the distribution of local polymer morphologies present in PEPM. From the plot in Fig. 5A, backbone geometry had little to no effect on ΔG² for the Sn2 pathways (a, b) as well as the Hofmann elimination on the piperidinium ring (d). However, Hofmann elimination along the backbone (e) was strongly dependent on the backbone conformation and became increasingly facile for extended, and increasingly difficult for compressed model-PEPM backbones. According to our calculations, this effect was remarkably large (i.e., modifying ΔG² by ca. 7 kcal mol⁻¹) and can potentially change the TST rate constant by up to four orders of magnitude!

This finding is consistent with the Hofmann elimination (E2) mechanism, which proceeds more favorably when Hβ–Cβ is anti-periplanar to Cα–N, i.e., θHβCβCαN > 150° or θHβCβCαN < -150°. For compressed backbone conformations (in which Cγ–Cβ tended to be anti-periplanar to Cα–N), the observed increase in ΔG² resulted from unfavorable torsional rearrangement in the transition state to access the required anti-periplanar Hβ–Cβ–Cα–N orientation. For extended backbone conformations, Hβ–Cβ was naturally anti-periplanar to Cα–N, hence e could proceed with relative ease. Since PEPM exists as an ensemble of backbone conformations, accounting for the effects of local backbone morphology on ΔG² (via an appropriately weighted Boltzmann average over the ΔG² values in Fig. 5) could yield a very different picture of the degradation kinetics than that provided by the ΔG² (F = 0) values alone. As such, one explanation that is consistent with both our experimental and theoretical data is that the distribution of backbone conformations tends to be more extended in PEPM; this would lead to a more favorable ΔG² for e, making this pathway competitive with (or even more favorable than) d.

To investigate how the substitution of R = Me (PEPM) for R = Et (PEPE) affected the stability of these piperidinium-based AAEMs, we also computed barriers for the analogous model-PEPE system. Again, we found that the Sn2 pathways (a, b) had higher barriers than the Hofmann elimination pathways (c, d, e), thereby suggesting that nucleophilic substitutions were not the primary degradation modes in PEPE as well. ¹H NMR analysis attributed ca. 38% and 32% of the total PEPE degradation to c and e (i.e., 26% and 22% of the total 69% degradation; see Fig. 4); with higher Sn2 barriers, we again hypothesized that the remaining 30% (unassigned) likely resulted from d. Since local backbone morphology substantially influenced ΔG² for e in model-PEPM (see Fig. 5), we expect the same in model-PEPE; if extended backbone conformations were favored in PEPE, e could again be competitive with d, which was observed experimentally.

Since rotation about Cα–Cβ in the ethyl moiety of model-PEPE was largely unhindered, one would expect that any one of the three corresponding β-hydrogens would be in the anti-periplanar position preferred by Hofmann elimination. DFT calculations on model-PEPE strongly agreed with these expectations and predicted ΔΔG² values for c (with respect to the other pathways) that were tantamount to >99% of the degradation proceeding through this channel. As mentioned above, ¹H NMR indicated that c was only responsible for 38% of the PEPE degradation, in stark contrast to the theoretical result. Since the model-PEPE backbone conformation was unlikely to affect ΔG² for c, theoretical arguments based on local polymer morphology alone are insufficient to explain why c seems to be severely hindered in PEPE. Notably, a similar discrepancy also occurs in (even simpler) tetraalkylammonium systems, wherein experimental characterization of the kinetics associated with ethyl-based Hofmann elimination also yields markedly different results from the theoretical ΔΔG² values (cf. Table 3 of ref. 38 with Fig. 6 of ref. 86). In this case, experimental Hofmann
elimination rates, i.e., half-life (τ) data, obtained by Marino and Kreuer88 for ethyltrimethylammonium (ETM) and propyl-
trimethylammonium (PTM) correspond to a ΔΔG‡ = ΔG‡ETM −
ΔG‡PTM = −RT ln [PTM/ETM] = −RT ln [33.2 h/2.8 h] =
−2.1 kcal mol−1 at T = 160 °C (assuming pseudo-first order
kinetics in 6 M NaOH and no side reactions), while the
theoretical calculations of Long et al.87 yield ΔΔG‡ = ΔG‡ETM −
ΔG‡PTM = 17.5 kcal mol−1 − 22.9 kcal mol−1 = −5.4 kcal mol−1
under the same conditions. As such, the (relative) rate of ethyl-
based Hofmann elimination in tetraalkylammonium salts also
seems to be markedly attenuated with respect to the theoreti-
cally predicted ΔΔG‡ values. Since a deeper understanding of
this degradation pathway can be leveraged in the rational
design of robust next-generation AAEMs for alkaline fuel cell
applications, the underlying reason(s) (e.g., the use of TST,
approximate treatment of electronic structure and solvent
effects, etc.) for this apparent discrepancy is currently under
investigation in our group.

For model-PEQ, the H3P-C6 in the bicyclic (quinuclidinium)
ring cannot easily access an anti-periplanar position with C6−N6,
thereby making Hofmann eliminations via the ring (c, d) less
viable degradation pathways (Table 3). In direct contrast to
model-PEPM and model-PEPE, the ring-opening S2,2 reactions
(a, b) have much lower ΔG‡ values (most likely due to ring
strain) and now become competitive pathways in model-PEQ.
1H NMR analysis indicated that these S2,2 reactions (a, b;
experimentally indistinguishable) and the remaining Hofmann
elimination (c) were indeed the primary degradation pathways,
with a corresponding assignment of 86% (a, b) and 14% (c) of
the PEQ byproducts (i.e., 30% and 5% of the total 35% degra-
dation, respectively; see Fig. 4). In this case, there is strong
experimental (cf. relative degradation kinetics for c for all
polymers in Fig. 4) and theoretical (cf. relative ΔG‡ values for
model-PEQ in Table 3) evidence that degradation through e was
attenuated in PEQ. Taking local backbone morphology into
consideration, these findings might be indicative of a prefer-
ence for compressed backbone conformations in PEQ (in
contrast to PEPM and PEPE). As such, this morphological
picture of PEQ shares some similarities with the stacked layer
model proposed by Trigg et al. for precisely sulfonated poly-
ethylene materials.87

Conclusions

In this work, we demonstrate that a photocatalytic hydro-
amination reaction enables the facile synthesis of significant
quantities of a piperidinium-cyclooctene monomer, which is
quickly converted through a ROMP/hydrogenation sequence to
materials for alkaline fuel cell applications. These materials are
the first aromatic-free, piperidinium- and quinuclidinium-
functionalized AAEMs with PE backbones. This strategy not
only expediently produced AAEMs with strong mechanical
properties, high hydroxide conductivity, and good alkaline
stability, but also enabled us to perform systematic studies to
compare different alkaline stability testing conditions
(containers) and different characterization techniques. By
employing a combination of FT-IR, 1H NMR, and DFT analysis,
we have identified the primary degradation pathways in these
AAEMs, and elucidated the crucial role played by polymer
backbone conformations in regulating degradation pathways
based on Hofmann elimination along the PE backbone. In
doing so, we find that methyl-substituted-piperidinium- and
quinuclidinium-functionalized AAEMs (PEPE and PEQ) gave
the highest alkaline stability. Due to the ease of their prepara-
tion, we propose that these cation-functionalized PE materials
should be excellent candidates for anion exchange membranes
with broader applications beyond AEMFCs.

Theoretical and computational methods

All calculations were performed using the Q-Chem (v5.2) software
package.88 Geometry optimizations employed the dispersion-inclusive hybrid B3LYP+D389−91 density functional
approximation in conjunction with the 6-31G* basis set for C,
H, and N (and the more diffuse 6-31+G∗ basis set for the O in
the charged nucleophilic species); this mixed basis set will be
denoted as 6-31G+[HCN]/6-31+G*[O] below. Vibrational
frequency calculations were used to confirm the nature of all
stationary points, wherein all minima contained no imaginary
frequencies and all transition state (TS) structures each con-
tained a single imaginary frequency connecting the reactants
(i.e., a local optimized reaction complex of the charged nucle-
ophilic species with model-PEPM, model-PEPE, or model-PEQ)
and the respective degradation products. Since the degradation
experiments in this work were performed in 2 M KOH/CD3OH at
T = 80 °C, methoxide (CH3O− or CD3O−) is expected to be the
primary and preferred reactive species (over OH−) due to its
higher nucleophilicity and basicity. In this and previous work,
we successfully identified the CD3O− addition byproducts.81
In all of the theoretical calculations performed herein, CH3O− was
therefore used as the nucleophilic (and basic) species. In many
cases, the frozen string algorithm92,93 aided in the search for TS
structures. Thermal contributions to the internal energy (Ei,
enthalpy (Hi), entropy (S), and free energy (G)) were computed at
T = 80 °C using partition functions derived within the ideal gas
(IG), rigid rotor (RR), and harmonic oscillator (HO) approxima-
tions. Entropic contributions from low-frequency vibrational
modes (present in both the reactants and TS structures) were
computed using the quasi-RHOO correction as outlined by
Grime (with α = 4, ωb = 100 cm−1, and BAv, set to the geometric
mean of the principal moments of inertia (I1, I2, I3) for each
system).94 Higher-level single-point corrections to the electronic
component of the internal energy (Edec) were obtained using the
ωB97X-VD density functional approximation and the cc-pVTZ88
basis set for C, H, and N (and the more diffuse aug-cc-pVTZ88
basis set for the O in the charged nucleophilic species); this
mixed basis set will be denoted as cc-pVTZ[HCN]/aug-cc-pVTZ88
[O] below. All calculations were performed in the integral
equation formalism polarizable continuum model (PCM) with
a dielectric constant of 23.9, which corresponds to methanol
extrapolated to T = 80 °C.97–100 To investigate the effect of local
backbone morphology, a small tensile force (∼0.25 nN ≤ F ≤
+0.25 nN) was applied in increments of 0.05 nN to the distance (D) between the γ-carbons in the polymer backbone via the external forces explicitly included [EFEI] approach.69

As such, the following working expression was used when computing G for a given reactant \(G_{\text{react}}\) or TS species \(G_{\text{TS}}\):

\[
G(F) = E_{\text{elec}} + H - TS + V_{\text{EFEI}}(F) - RT \ln g. \tag{1}
\]

In this expression, \(E_{\text{elec}}\) is the electronic (or DFT) energy computed at the \(\omega B97X-V/\text{cc-pVQZ}[\text{HCN}]/\text{aug-cc-pVQZ}[\text{O}]/\text{PCM}\) level. In practice, the \(E_{\text{elec}}\) term in this expression is evaluated as \(nRT\) in accordance with the IG approximation. \(S\) is the analogous entropic contribution given by:

\[
S = S(T) = S_{\text{trans}}(T) + S_{\text{rot}}(T) + S_{\text{vib}}(T), \tag{3}
\]

in which \(S_{\text{trans}}(T)\), \(S_{\text{rot}}(T)\), and \(S_{\text{vib}}(T)\) are the translational, rotational, and vibrational contributions to the entropy, and have been computed using the IG, RR, and HO approximations, respectively, at the B3LYP+D3/6-31G* [HCN]/6-31+G* [O]/PCM level. In practice, the \(pV\) term in this expression is evaluated as \(nRT\) in accordance with the IG approximation. \(S\) is the analogous entropic contribution given by:

\[
S = S(T) = S_{\text{trans}}(T) + S_{\text{rot}}(T) + S_{\text{vib}}(T), \tag{3}
\]

in which \(S_{\text{trans}}(T)\), \(S_{\text{rot}}(T)\), and \(S_{\text{vib}}(T)\) are the translational, rotational, and vibrational contributions to the entropy, and have been computed using the IG, RR, and quasi-RHf approximations, respectively, at the B3LYP+D3/6-31G* [HCN]/6-31+G* [O]/PCM level. \(V_{\text{EFEI}}(F) = -F \times D\) is an additional potential energy contribution that arises when an external force with magnitude \(F = |F|\) is applied to the system using the EFEI approach,69 and \(D\) is the distance between γ-carbons in the polymer backbone resulting from a geometry optimization of the system (in the presence of \(F\)) at the B3LYP+D3/6-31G* [HCN]/6-31+G* [O]/PCM level. Here, we stress that all geometry optimizations (and subsequent vibrational frequency analyses) were performed by minimizing \(E_{\text{DFT}} + V_{\text{EFEI}}(F)\) (instead of just \(E_{\text{DFT}}\)) with respect to the nuclear coordinates in the system; as such, all resulting minima (and TS structures) did not contain any spurious imaginary frequencies. The final term in \(G(F)\) accounts for the number of chemically equivalent \(S_{\text{eq}}\) or E2 sites in degradation pathways a, d, and e (vide infra); in this term, \(g\) is the corresponding degeneracy factor and takes on values of \(g = 1\) for all reactants and \(g = 1\) or \(g = 2\) for all TS structures considered herein.

Since the primary purpose of the theoretical calculations in this work is to assess the relative viability among a set of competing degradation pathways (with the same reactants), all free-energy barriers \(\Delta G^2 = G_{\text{TS}} - G_{\text{react}}\) were computed with respect to a single reference, \(i.e.,\) the global minimum reactant complex on the corresponding potential energy surface (PES), instead of the reactant complex directly connected to each TS via the intrinsic reaction coordinate (IRC). Doing so explicitly accounts for the equilibrium (Boltzmann) population of the corresponding IRC-based reaction complex—which is potentially a local minimum reaction complex on the PES—in each \(\Delta G^2\) value provided herein, and therefore allows for a fairer comparison among competing degradation pathways.

Due to the potential errors that arise when computing free-energy barriers with DFT (which often exceed 1.0 kcal mol\(^{-1}\))68 we avoid discussing absolute reaction rates throughout this work, and instead compare and contrast \(\Delta G^2\) values corresponding to different degradation pathways \(\Delta G_1\) and \(\Delta G_2\) in relative terms, \(i.e.,\) \(\Delta \Delta G^2 = \Delta G_2 - \Delta G_1\). We also discuss the relative differences between \(\Delta G^2\) values in terms of the corresponding reaction rate constants \(k_i\), which have been estimated using the Eyring equation of transition state theory (TST):

\[
k_i = \frac{k_B T}{h} e^{-\Delta G^2_i/RT}, \tag{4}
\]

in which \(k_i\) is the transmission coefficient (assumed to be unity throughout this work), \(k_B\) is the Boltzmann constant, and \(h\) is Planck’s constant. For two different degradation pathways that yield the same products \(c.f.\) Table 3), one can define an effective rate constant \(k_{\text{eff}} = k_1 + k_2\) and use the Eyring equation to derive a corresponding effective barrier height \(\Delta G^2_{\text{eff}}\) via

\[
e^{-\Delta G^2_{\text{eff}}/RT} = e^{-\Delta G^2_1/RT} + e^{-\Delta G^2_2/RT}, \tag{5}
\]

which can be rearranged to give:

\[
\Delta G^2_{\text{eff}} = \Delta G^2_1 - RT \ln[1 + e^{-(\Delta G^2_2 - \Delta G^2_1)/RT}]. \tag{6}
\]

For identical degradation pathways \(c.f.\) with two chemically equivalent \(S_\text{eq}\) or E2 sites, \(\Delta G^2_1 = \Delta G^2_2\) and this expression simplifies to:

\[
\Delta G^2_{\text{eff}} = \Delta G^2_1 - RT \ln 2, \tag{7}
\]

which comprises the degeneracy correction to \(G(F)\) used above in eqn (1).

All calculations were performed using the following convergence criteria: \(10^{-8}\) au for the DIIS error and \(10^{-11}\) au for the integral thresholding value during self-consistent field (SCF) optimizations; \(3.0 \times 10^{-6}\) hartree per bohr for the maximum gradient component, \(1.2 \times 10^{-5}\) bohr for the maximum atomic displacement, and \(1.0 \times 10^{-8}\) hartree for the energy change between successive steps during geometry optimizations (with convergence reached after satisfying any one of these criteria). A detailed breakdown of the free-energy components (Table S6†) as well as the optimized geometries for each species are included in the ESL†

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This work was primarily supported as part of the Center for Alkaline-based Energy Solutions (CABES), an Energy Frontier Research Center funded by the U.S. Department of Energy, Office of Science, Basic Energy Sciences under Award #DE-
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