CellBIC: bimodality-based top-down clustering of single-cell RNA sequencing data reveals hierarchical structure of the cell

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ABSTRACT

Single-cell RNA sequencing (scRNA-seq) is a powerful tool to study heterogeneity and dynamic changes in cell populations. Clustering scRNA-seq is essential in identifying new cell types and studying their characteristics. We developed CellBIC (single Cell Bi-modal Clustering) to cluster scRNA-seq data based on modality in the gene expression distribution. Compared with classical bottom-up approaches that rely on a distance metric, CellBIC performs hierarchical clustering in a top-down manner. CellBIC outperformed the bottom-up hierarchical clustering approach and other recently developed clustering algorithms while maintaining the hierarchical structure of cells. Importantly, CellBIC identifies type 2 diabetes and age-specific β cell signatures characterized by SIX3 and CDH2, respectively.

INTRODUCTION

The advent of high capacity single cell RNA-seq (scRNA-seq) allows the characterization of large number of single cell transcriptomes (1–6). Clustering is an important step to study cell heterogeneity and characterize previously unknown cell sub-populations. For clustering cell-to-cell distance is usually used to identify cells with similar expression profiles. A classical hierarchical clustering method uses the cell-to-cell distance to reconstruct a tree structure, where each branch represents a sub-type (2–10). Accordingly, the choice of an appropriate metric and a linkage criterion influences the clustering results. Also, a hierarchical clustering method often fails to find a large group in the process of collecting small groups to reconstruct a tree structure due to the conflict between similarity across multiple groups (11,12). Ensemble approaches have been developed for scRNA-seq clustering to compensate biases from using a metric or a criterion (13,14). SC3 (13) uses a consensus of k-means clustering results followed by hierarchical clustering. SIMLR (14) provides a similarity metric learned by combining multiple kernels. Even though successful, these approaches still rely on the choice of a metric and a linkage criterion.

Dimension reduction approaches such as principle component analysis (PCA) and t-distributed stochastic neighbor embedding (t-SNE) have been widely applied for clustering in order to handle multi-dimensional scRNA-seq data efficiently by visualizing cells in a two or three dimensional space (2,4,5,6,8–10,15–20). Subsequently, clustering is performed by grouping cells based on the proximity in the reduced dimension. However, these approaches can fail to identify cell types when cells are intermingled in the reduced domain.

Here, we developed CellBIC (single Cell Bi-modal Clustering), a novel clustering approach for scRNA-seq. Compared with a classical ‘bottom-up’ hierarchical clustering approach that builds up a tree from a distance matrix, CellBIC implements a ‘top-down’ approach by performing clustering by dividing the dataset recursively to reconstruct a hierarchical structure (21). While a top-down hierarchical clustering method requires additional computation time for identifying an optimal division point (22), it can provide a better clustering performance and interpretation than bottom-up algorithms (21–25). A top-down clustering equips with a simple flat clustering to divide datasets into large sub-groups (22). Often, a K-means algorithm has been used as a flat clustering due to its execution speed (22). Instead of using a K-means algorithm, we designed a new flat clustering approach for scRNA-seq data using multi-modal patterns in gene expression. Multi-modality is an intrinsic characteristic observed in heterogeneous scRNA-seq data. For instance, if the expression levels of a gene are high in a cell type and low in other...
cell type, its distribution in the mixed population will show a bimodal distribution in scRNA-seq. Bimodality in expression is also previously observed in the scRNA-seq from mouse bone-marrow-derived dendritic cells due to the potential cell specificity of a sub-population in responding to lipopolysaccharide (26).

CellBIC identifies cellular clusters by considering a bimodal expression pattern in a top-down manner. By dissecting cells based on bimodal memberships recursively, CellBIC reconstructs a hierarchical tree structure. We applied CellBIC to various scRNA-seq data including human pancreas (3,6), mouse cortex (4), and mouse lung (5). CellBIC shows a superior performance for clustering of scRNA-seq data over traditional bottom-up clustering algorithms as well as other state-of-the-art clustering algorithms. The hierarchical structure that CellBIC identified reconstructed the developmental lineages of the pancreas. Applying CellBIC further to pancreatic β cells, we identified genes in β cells associated with type 2 diabetes (T2D) and aging.

**MATERIALS AND METHODS**

**Clustering evaluation**

t-SNE (27) and density-based spatial clustering of applications with noise (DBSCAN) (28) were implemented in MATLAB 2017b. Bottom-up hierarchical clustering was performed by two MATLAB functions ‘linkage’ and ‘dendrogram’. For t-SNE and bottom-up clustering, we used genes whose log2 transformed TPM > 1 in >25% cells and the coefficient of variation of the log2 transformed TPM > 1. For SC3 and SIMLR, we used their default parameters.

To benchmark clustering algorithms, each obtained cluster was assigned to a cell type with the best matching cell type. By comparing the assigned cell type with the gold standard, we calculated adjusted rand index (ARI) for each clustering result. We considered the maximum ARI of the clustering results for different numbers of clusters and for five repeats as the ARI of each clustering algorithm. ARI was calculated by a MATLAB function ‘rand_index’in a package Adjusted Rand Index version 1.0 with ‘adjusted’ option using MATLAB 2017b (https://www.mathworks.com/matlabcentral/fileexchange/49908-adjusted-rand-index).

CellBIC uses bimodal distribution in scRNA-seq for clustering

A multi-modal distribution in expression is often observed in scRNA-seq data from a mixed cell population. For instance, insulin (INS) expression levels in the scRNA-seq from human pancreas showed a bimodal distribution: the higher mode for β cells (INS+) the lower mode for other cells (INS−) regardless of the donors (Supplementary Figure S1). This suggests a potential use of modality for scRNA-seq clustering.

Hypothesizing that cells that belong to a mode in a bimodal distribution consistently across multiple genes share similarity, we designed a top-down hierarchical clustering approach. To implement clustering, we obtain Boolean membership of cells (High/Low or 0/1) after fitting the distribution of expression levels of each gene with a Gaussian mixture model (Figure 1A). To obtain bimodal distribution, we used a Gaussian mixture model with two modes. We only consider a gene as a candidate based on t-statistics (t > 10). In CellBIC, genes that do not make cells belong to a membership are discarded (Figure 1B). For this, CellBIC calculates the Hamming distance using the Boolean membership. The Hamming distance (Hij) of two Boolean vectors i and j is defined by the ratio of the number of mismatch. The absolute Hamming distance (AHij) between i and j is defined as follows:

\[
AH_{ij} = \begin{cases} 
H_{ij} & \text{if } H_{ij} < 0.5 \\
1 - H_{ij} & \text{otherwise}
\end{cases}
\]

In this configuration, the Hamming distance of 1 is for the perfect mismatch for a gene pair and 0.5 for a random match. Two genes with maximum Hamming distance are selected as the top seed gene pair. We limited that the seed gene pair has a distance larger than 0.7 to remove seed gene pairs weakly mismatching each other. We further confirmed that the performance was robust to the Hamming distance cutoff for a seed gene pair (Supplementary Figure S2). Then, we selected genes showing consistent or contrasting Boolean membership with the selected two seed genes. A gene is added if average absolute Hamming distance with the existing genes is below 0.2 (correlation test P-value <0.01, and binomial test P-value < 1e−25), which provided robust clustering performances for several independent scRNA-seq datasets (Supplementary Figure S3).

The collective membership will show two groups of cells aligned with the seed gene pair (Figure 1C).

**Dissecting cells using the hamming code table**

The Hamming codes for the aligned genes were represented in the membership matrix. The matrix is composed of two gene groups aligned to the two seed genes, respectively. The Boolean values were switched (0 to 1 and 1 to 0) when appropriate. The maximum of the moving standard deviation (window = 1/15 of the total number of cells) on the column sum of the matrix determines the dissection point of the two groups of cells. Consequently, the dissecting point and the genes aligned to the seed two genes form four quadrants in the membership matrix. The majority values of the two crossing quadrants are same. For instance, the majority value of the second and the fourth quadrants in Figure 1C is 0 and the other two quadrants (first and third quadrants in Figure 1C) is 1. If the majority component is not observed in an alternative manner from the first to the fourth quadrant, dissection is discarded and the clustering stops. To prevent CellBIC from falling into a local minimum, this procedure is repeated using the top 5 seed genes (Supplementary Figure S4). When selecting the aligned gene sets with the seed genes, genes used for previous dissection are not considered for the alignment with the next seed genes. Genes that provide best dissection among them is selected based on the following clustering score C.

\[
C = \left( \frac{E}{4} - 0.7 \right) N
\]

where E denotes the sum of the ratios of ‘1’ in the second and the fourth quadrants and the ratios of ‘0’ in the first
Figure 1. CellBIC implements top-down hierarchical clustering using bimodal pattern. (A) Step 1: Boolean membership is obtained using a Gaussian mixture model. (B) Step 2: A gene group is selected based on the Boolean membership. Only genes observed in one mode significantly are included. (C) Step 3: A membership matrix is obtained using the selected gene set. Cells are divided into two groups based on the membership matrix. (D) A top-down clustering is performed by applying A-C recursively. (E) A membership matrix obtained by CellBIC when using human pancreatic α/H9251 and β/H9252 cells (3). (F) A classical bottom-up hierarchical clustering using human pancreatic α and β cells (3). The point to cut the tree is not well defined for the bottom-up hierarchical clustering.

and third quadrants of the membership matrix, \( N \) denotes the number of the genes aligned to the two seed genes, and 0.7 is clustering score weight. The clustering score weight was determined after testing various weight values using the benchmarking data (Supplementary Figure S5). This algorithm is recursively applied to the subgroups until every dissection is discarded (Figure 1D) or the minimum number of cells in the cluster is less than a cutoff value. The CellBIC performance was robust to the change of the minimum number of cells especially with the cell number <50 (Supplementary Figure S6).

Gene ontology (GO) and Kyoto Encyclopedia of Genes and Genomes (KEGG) analysis

All the GO (29) and KEGG (30) pathways analyses were implemented using Enrichr 2017 version (31).

RESULTS

A top-down clustering better dissects cells than the classical hierarchical clustering

To test the usefulness of using modality in clustering scRNA-seq data, we prepared a well-characterized cell groups composed of human pancreatic α and β cells (3). Applying CellBIC to this dataset, we identified Glucagon (GCG) and INS as the top pairing seed genes, which are the marker for α/H9251 and β/H9252 cells, respectively (Figure 1E). Along with GCG, we found classical α cell markers such as ARX (32) and IRX2 (33) were aligned with GCG (Fisher’s exact test \( P\)-value = 3.11e–28 and 1.33e–38, respectively). Also, β cell markers such as PDX1 (34) and MAFA (35) were aligned well, as expected, with INS (Fisher’s exact test \( P\)-value = 7.27e–28 and 5.45e–43, respectively).

The classical bottom up clustering approach identified pre-defined α and β cell groups as well. However, it did not provide a well-structured tree. When a tree is cut, the hi-
Hierarchical clustering approach did not clearly distinguish α against β cells, which could mislead the subsequent analysis (Figure 1F). Our test demonstrates that the top-down clustering identified functional sub-cell types and can better be applied to clustering scRNA-seq data.

**CellBIC showed outstanding clustering performance in the comprehensive benchmarking tests**

For comprehensive benchmarking, we compared the performance of CellBIC with various clustering approaches for scRNA-seq data including the classical hierarchical clustering and t-SNE (27) followed by DBSCAN (28). We also included recently developed SC3 (13) and SIMLR (14) for the comparison.

For this benchmarking we used scRNA-seq data for (i) 668 cells from human pancreas (3), (ii) 2544 cells from human pancreas (6), (iii) 3005 cells from mouse cortex (6) and (iv) 201 cells from mouse lung (5). We used the annotation of cells provided by each study as a gold standard. If a cell is not defined, we left it as undefined. Supplementary Table S1 summarizes the composition of cells that we used.

From the transcriptome of 668 human pancreas cells, CellBIC identified α, β, pancreatic polypeptide (PP), ductal, acinar, and mesenchymal cells successfully (Figure 2A). The classical bottom-up hierarchical clustering method successfully identified α, β, PP, ductal and mesenchymal cells. However, many α cells were misclassified. The t-SNE approach identified α, β, duct, acinar and mesenchymal cells, but it misclassified most of β cells. This is because of the difficulties in dissecting α against β cells that are located closely in the reduced dimension, where DBSCAN only selected the subset of β cells (Supplementary Figure S7). SC3 identified α and β cells well. However, SC3 failed to distinguish PP cells from α cells. SIMLR almost perfectly separated 4 types of endocrine cells, but it failed to distinguish ductal, acinar, and mesenchymal cells (Figure 2A).

With another 2544 cells from human pancreas, SIMLR showed similar identification performance to CellBIC (Figure 2B). However, both hierarchical clustering and t-SNE+DBSCAN failed in identifying α cells against β cells. SC3 missed or misclassified considerable proportions of α and β cells (Figure 2B). For mouse cortex cells, CellBIC, hierarchical clustering, t-SNE+DBSCAN, and SC3 showed comparable performance (Figure 2C). SIMLR, however, failed in distinguishing interneurons and two pyramidal cells (CA1 and S1). For mouse lung cells, only CellBIC and SIMLR distinguished E16 stage cells (Figure 2D) but SIMLR misclassified a considerable number of cells.

Figure 2E summarizes the overall performance using ARI for the datasets we used. Overall, CellBIC showed best or at least comparable results with other classifiers. CellBIC’s performance was robust for all the tested datasets (ARI > 0.7) SC3 showed comparable performance with CellBIC for 3 independent datasets. However, it performed poorly when using 2544 human pancreas cells. Our results demonstrate that clustering using modality may overcome the potential algorithmic biases in calculating distance between cells and/or subsequent analysis.

**CellBIC reconstructs hierarchical cluster trees**

We further investigated the hierarchical structure identified by CellBIC. From human pancreatic tissues (3), we first obtained two large cell groups. Gene ontology (GO) of the first group (left) showed terms related with endocrine function of pancreas such as ‘Maturity onset diabetes’ (adjusted P-value = 1.50×10⁻⁶) and ‘Insulin secretion’ (adjusted P-value = 7.94×10⁻⁶) (Figure 3 and Supplementary Table S2). The other group (right) showed terms related with exocrine function of pancreas such as ‘Hippo signaling pathway’ (adjusted P-value = 6.37×10⁻³) (36,37) (Figure 3 and Supplementary Table S3). Endocrine cells were further divided into a group containing α (GCG+) and PP (PPY+) cells and the other group containing β (INS+ and δ (SST+) cells. This is consistent with the view that PP and δ cells are similar with α and β cells, respectively (38,39). The exocrine cells divided into mesenchymal cells expressed genes related with ‘ECM-receptor interaction’ (adjusted P-value = 1.73×10⁻²) and a group expressed genes related with ‘ Tight junction’ (adjusted P-value = 3.63×10⁻⁴) (Figure 3 and Supplementary Tables S4–S5). The second group was further divided into ductal and acinar cells. In sum, CellBIC identified a structure of pancreatic cell types in a hierarchical form. We also obtained similar results from the scRNA-seq dataset for 2544 cells from human pancreatic tissues (6) (Supplementary Figure S8 and Supplementary Tables S6–S11).

CellBIC also reconstructed a hierarchical structure using the scRNA-seq data from mouse cortex (4). At the top level, mouse cortex cells were dissected into two large groups, one with a function related with ‘Myelination’ (adjusted P-value = 2.92×10⁻²) and the other ‘SOMATIC transmission’ (adjusted P-value = 2.62×10⁻⁴), suggesting non-neuronal and neuronal cells, respectively (Supplementary Figure S9 and Supplementary Tables S12–S13). The neuronal cells were separated by the order of the interneurons and pyramidal neurons from two different sources including somatosensory (S1) and hippocampal CA1 region (Supplementary Figure S9 and Supplementary Tables S14–S15). The non-neuronal cells were separated by the order of oligodendrocytes, endothelial-mural cells, astrocyte-ependymal cells and microglia (Supplementary Figure S9 and Supplementary Tables S16–S19).

**CellBIC identified the characteristics of β cells associated with T2D and aging**

We further questioned the sub-clusters in the β cells composed of 98 adult and 20 child pancreatic β cells (3). CellBIC identified a group of cells with higher expression levels of SIX3 and CD14 (Figure 4A). While these cells showed strong INS expression levels, we found majority of cells high with SIX3 and CD14 were from T2D donors (Fisher’s exact test P-value: 1.56×10⁻⁴). To confirm this, we used an independent scRNA-seq data from normal and T2D β cells (18) (Figure 4B). In these independent datasets, genes highly expressed in SIX3+ cells (CD14, NEFM, SIX3, ITGB3BP) also had significantly higher expression in the cells from T2D donors (Wilcoxon rank sum test P-value < 1.0×10⁻²). Also, genes exclusively observed in SIX3+ cells such as CPBI and CPA2 were expressed significantly less frequently
Figure 2. CellBIC outperforms in the benchmarking tests. The pre-defined sets (gold standard) are compared with the predicted cell types by CellBIC, bottom-up hierarchical clustering, t-SNE+DBSCAN clustering, SC3, and SIMLR. (A, B) two human pancreata (3,6), (C) a mouse cortex (4) and (D) a mouse liver dataset (5). (E) Performance evaluation of five clustering algorithms for four scRNA-seq datasets using ARI.

Figure 3. CellBIC reconstructs a top-down hierarchical structure from 668 human pancreatic cells (3). The entire human pancreatic cells were divided into endocrine and exocrine cells. Endocrine cells were further divided into a group containing α (GCG+) and PP (PPY+) cells and another group containing β (INS+) and δ (SST+) cells. The exocrine cells were divided into mesenchymal cells and a group consisting of ductal and acinar cells. Finally, CellBIC reconstructed the hierarchical structure for the pancreatic sub-types.

in normal β cells (Wilcoxon rank sum test P-value < 1.0e-4).

Interestingly, a previous genome-wide association study also showed a potential role of SIX3 in β cell maturation and a relevance of SIX3 with type 1 diabetes (T1D) and T2D risk (40). Furthermore, a subset of β cells expresses CD14, which is associated with the immune surveillance (41) and β cell viability (42). Our study may suggest CellBIC can be used to identify β cell markers associated with diabetes risk.

The clustering using the top second seed pair identified another β cell sub-type marked by N-cadherin (CDH2) (Figure 5A). We found CDH2+ cell group is populated with cells obtained from adult donors (Fisher’s exact test P-value = 2.71e-16, Figure 5A). The age-dependent gene expression of two seed genes LCN2 and CDH2 is also supported by a published bulk RNA-seq data obtained from human adult and fetal pancreatic β cells (43) (Wilcoxon rank sum test P-value < 0.01, Figure 5B). The validation using the two scRNA-seq datasets from donors with various ages (6,18) showed significantly positive correlations (correlation test P-value = 3.05e-4 and P-value = 3.12e-4, respectively, Figure 5C and D). Previous staining study identified the expression of CDH2 in human β cells (44,45). We also found that CDH2 is expressed only in adult β cells in the two independent scRNA-seq datasets (3,18) (Supplementary Figure S10). The negligible CDH2 expression in adult α cells from the same donor further showed that CDH2 expression in adult β cells are not from contamination such as doublet...
Figure 4. CellBIC identifies genes associated with T2D from β cell sub-clustering. (A) A membership matrix of sub-clustering of β cell shows SIX3 and CD14 are highly expressed in β cells from T2D donors. (B) Evaluation of the gene expression using the β cell scRNA-seq dataset from normal and T2D patients (18).

Figure 5. CellBIC identifies genes associated with aging from β cell sub-clustering. (A) A membership matrix of sub-clustering of β cell show CDH2 is highly expressed in adult β cells. (B) LCN2 and CDH2 expression shows age-dependency in the bulk RNA-seq data obtained from fetal and adult pancreas (43). Violin plots show age-dependent CDH2 expression in the two β cell scRNA-seq datasets by (C) Segerstolpe et al. (18) and (D) Enge et al. (6).
cells. Our study suggests that CDH2 may be a β cell aging marker.

DISCUSSION
Clustering scRNA-seq data provides an unbiased way to characterize cells. CellBIC newly implemented a top-down hierarchical clustering approach for scRNA-seq data. To dissect cell groups, CellBIC designed a new flat clustering algorithm in a top-down clustering based on modality. Unlike its competitors, it does not require a calculation of cell-to-cell distance from the expression values directly. In the series of benchmarking tests, CellBIC outperformed the classical bottom-up hierarchical clustering approach. This may be because a simple distance metric the bottom-up clustering relies cannot deal with multi-dimensional data effectively. Ensemble approaches such as SIMLR and SC3 were designed to overcome potential biases using a single metric. Our benchmarking tests demonstrated that CellBIC outperformed the bottom-up hierarchical clustering approach as well as ensemble-based approaches. The robust performance of CellBIC in clustering four independent scRNA-seq datasets shows the advantages of using the distribution of data instead of using cell-to-cell distances.

Modality has been used for a number of studies using scRNA-seq data. MAST (46), SCDE (47), and scDD (48) utilized bimodal characteristics of gene expression in scRNA-seq to identify differentially expressed genes. These studies indicate that a gene with a bimodal expression pattern across single cells could be a good marker for distinguishing a cell state of cell type.

Previously, single cell based approaches identified CFAP126 (also known as Fltp), CD9, and ST8SIA1 as the β cell sub-type markers (49,50). We did not identify them in our analysis. However, CellBIC identified SIX3 and CDH2 as a marker for T2D and aging, respectively. These are obtained from the top 2 seed gene pairs. Interestingly, the other four algorithms could not identify these two β cell subtype markers using their default options (Supplementary Figures S11–S13). Interestingly, SC3 found a group of cells depleted with SIX3 and CDH2 expression when it was forced to identify more than three clusters (Supplementary Figure S12). Our results exhibit that there are algorithmic advantages of using the modality for cell clustering.

Even though we used bimodal pattern for our clustering, a multi-modal pattern will be observed if multiple cell types are observed in scRNA-seq. Multi-modal pattern can be identified using mixture of multiple Gaussian. CellBIC cannot currently use the multi-modal patterns. Clustering using multi-modal pattern requires large cell number for assigning membership to each mode and it may not be easy each to reconstruct the hierarchical structure. Instead, CellBIC identifies clusters by recursively identifying for bimodal patterns.

DATA AVAILABILITY
Input files for the benchmarking datasets and a MATLAB source code for CellBIC are available at https://github.com/neocaleb/CellBIC.

SUPPLEMENTARY DATA
Supplementary Data are available at NAR Online.

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CONFLICT OF INTEREST STATEMENT
None declared.

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