1. Introduction

The detection of illegal material at aircraft and landline terminals is an indispensable procedure that prevents the illegal transport of forbidden radioactive material such as uranium between countries. Typically, this type of material is shielded with lead that is undetectable by the image scanner. Therefore, the exposure of the substance can be achieved when the lead is successfully detected. This detection is within the application of high-density and atomic (Z) material. Many techniques based on different rays have been proposed for this detection; however, many challenges halt these because of the high operation cost or incompatibility of facilitations (Procureur, 2017). High-energy electromagnetic rays, i.e. gamma and X-ray, can be used for detection because they rapidly attenuate in a few centimeters of lead but the shielding is expected to be thicker. Familiar charge particles such as Beta and Alpha obtained from radioactive sources are of a short range because of the low energy and they are thus not applicable for the detection. Additionally, although high-energy protons can penetrate enough to be used for the detection, the facilities needed for accelerating them are so expensive and not portable. A more reliable option is the muon particles that reach the Earth’s surface with high energy and sufficient intensity. These particles are free rays that exist everywhere. Muon rays have already been proposed as one of the rays used for radiography (Bogdanov et al., 2006; Bonal et al., 2016; Bonal, Preston, & Dorsey, 2015; Procureur, 2017).

Muons are produced when the protons that come from the universe enter and interact with the upper layers of the atmosphere. They are dominant in the cosmic rays that arrive at the Earth’s surface with an intensity of 1 muon/cm²-min. Interacting muons are like electrons, not with a strong force, but with a larger mass; therefore, they do not rapidly lose energy. Hence, absorption of muons in materials is due to energy dissipation that is attributed to dominating the Coulomb interactions with atomic electrons and multiple scattering by the nuclei. The density of the material and consequently the high atomic number are a crucial factor in the attenuation of the muon particles. Previous studies have shown that muons are more penetrability than other charge particles (Bonal et al., 2016, 2015; Borozdin et al., 2003; Morris et al., 2013). Furthermore, it was demonstrated that high-Z materials can be located and detected using muography by cosmic-ray muons (Priedhorsky et al., 2003).

Cosmic ray muons have a wide range of energy extending from a few MeV up to beyond 100TeV (Brini, Peli, Rimondi, & Veronesi, 1955; Mollerach & Roulet, 2018; Pine, Davisson, & Greisen, 1959; Rastin, 1984). Thus, it is difficult to have an experimental setup with detectors to cover such a wide range. In the interaction
of cosmic rays with matter, photons are produced with different energies depending on the muon energy by Bremsstrahlung also contribute to increasing the electrons because of photoelectric and Compton scattering effects and pair production. Therefore, when the muon is being detected, the counters are affected by the primary and the secondary charged particles and photons of high energy. This makes tracking and identifying the muon by the detector difficult. Only tracking chambers have been successful in tracking the muon and identifying other cosmic rays. It has been conventional that the detection of muons requires tracking detectors. However, the tracks made by the muon and other particles produced are still complicated. Fomin et al. (2017) reported that the muon detector reading is complicated and not precise. It is believed that thousands, millions, or even billions of interactions occur spontaneously until the net energy is equal to zero. Schreiner (2016) reported that the Coulomb multi scattering of muon inside the high-dense material causes potential trajectories that their tracking requires two systems of detectors synchronized with sufficient time resolution. He suggested that the attenuation information could be enough for detection because such a system of this size and complexity is completely impractical for most suggested applications (Schreiner III, 2016). Detection with a huge number of tracks requires high-resolution detectors. Improving the detectors by increasing the resolution leads to the use of very large numbers of readout channels that would be costly (Dixit & Rankin, 2006).

The use of gaseous detectors is relevant for measuring the attenuation of cosmic muon in heavy metals. It has been proven that for measuring muon intensity, gaseous detectors can achieve a higher resolution of detection than scintillation detectors at costs that are still reasonable (Autran, Munteanu, Saoud, & Moinidjé, 2018; Procureur, 2017; Procureur, Dupré, & Aune, 2013). In this work, a telescope of two GM counters was used to detect the high-Z dense material. This telescope was not proposed for muography or for obtaining the dimension of the detected material. Gas detectors such as Geiger-Muller counters were chosen for detecting muons because they detect the intensity of the high energy charged particles well. In our previous work, the validity of the telescope was investigated and a precise count rate was obtained (Altameemi, Hamid, Mohd, Ahmed, & Gopir, 2019). The next step in the research for designing a portable telescope is to determine the absorption (attenuation) coefficient of the detectable high-density material. The theoretical calculation of the muon interaction with matter is usually carried out using the GEANT simulation program; however, the discrepancies in the observation showed that the simulation needs more improvement to describe the interaction of high-energy muons (Apel et al., 2017; Schreiner III, 2016). Experimentally, determining the coefficients of the material using the telescope could be more compatible for future work and this was thus our target in the present work.

Despite recent works focused on obtaining an image of an object using the muon attenuation, comprehension and understanding the muon attenuation in terms of attenuation coefficient is still scant. Tomography is based on attenuation, and many works have focused on the angular distribution of the attenuation to form a clearer picture. The diffusion of muon in shielding material represented by the attenuation curves was studied using Monte-Carlo techniques by Stevenson (1986) who suggested that the problem of muon shielding material required sophisticated and complex computer program that was not available. Morris et al. (2013) reviewed the development and the motivation in radiography and referred to the muon technique as a method for big objects. Further understanding of the complex precipitation sequence in the mechanical strength of Al–Mg–Si alloy was presented using the technique of muon spin relaxation. The technique revealed the existence of defects within the atom-size as vacancies and solute atoms (Mg and Si) (Wenner et al., 2013). Blanpied et al. (2015) presented a method of muon tomography to detect medium and light material (mostly metals) as contraband using GEANT simulation. The electrons produced by muon interacted well with the light material and is the bases of the discrimination of light materials. Based on the data obtained from the KASCADE-Grande observatory, the atmospheric muon attenuation length was measured using the method of high-energy muon shower evolution. The observation was inconsistent with the predictions of the four models of high-energy hadronic interactions that failed to describe the zenith (Apel et al., 2017). Fredrick (2016) experimentally studied the attenuation of the muon spectrum for tomography. The careful measurement showed better attenuation and description by large objects when low energy (110MeV to 1.2 GeV) spectrum of muon was used. He also found the range of muon energy suitable for small objects and measured the attenuation coefficient for aluminum and steel (Schreiner III, 2016). Autran et al. (2018) designed a portable telescope made up of two detectors with efficiency sufficient for measuring the count rate of muon at the sea level to study the variation of muon intensity with the zenithal and azimuthal angles. A review with an emphasis on the recent progress of high-energy cosmic rays was presented by Mollerach and Roulet (2018). An extensive study of cosmic shower contents including the muon content was carried out using cosmic ray propagation through magnetic fields. However, all the above recent studies did not provide the attenuation coefficients of most heavy materials, and thus far, none has measured or calculated them yet. Hence, our aim in the present work is to measure these coefficients.

The present work utilized the telescope proposed by the previous study of Altameemi et al. (2019) in
In order to obtain the attenuation coefficients of the high-density metals (lead, copper, zinc, and aluminum). The count rates of the transmitted muons through different thicknesses were measured and the fitting was applied to calculate the coefficients. In the next section, the experimental setup is presented, and the method of calculation is shown.

2. Attenuation of muons

The exponential attenuation of radiation is mostly conventional in Gamma and then in Beta rays; however, the heavy-charged particles with high energy do not attenuate as well in heavy materials. The theoretical concept of attenuation is based on the decay of the intensity of the transmitted ray through a material. In relation to Gamma interaction with matter, the attenuation is a result of three main interactions, namely photoelectric, Compton scattering and pair production effects. When these three main effects occur through matter, the decay of the ray will be exponential, and the absorber exhibits a linear absorption which is represented by the familiar equation of attenuation:

\[ I = I_0 e^{-\mu x} \]  

(1)

where \( I_0 \) is the incident intensity of the ray in the absence of an absorber of thickness \( x \), \( I \) is the intensity of the transmitted and attenuated ray, and \( \mu \) an attenuation coefficient for the ray. The attenuation coefficient changes with the energy of the incident ray but it becomes linear in lead when the energy of the ray is more than three MeV in which the pair production dominates. The muon cosmic ray of high energy interacts with the material in a very complicated way because of the photonic and particle cascades that cause more secondary interactions, but the domination of the three effects makes the attenuation of the cosmic muon exponential and subjected to Equation (1) (Bertanza & Martelli, 1954; Bogdanov et al., 2006; Hanna, 2012; Procureur, 2017).

The intensity of the cosmic muons can be represented by the measured count rate where the count rate \( R_0 \) is measured by a detector in the absence of the absorber and \( R \) count rate is measured after it has transmitted through the absorber; Equation (1) can then be written in terms of count rate as

\[ R = R_0 e^{-\mu x} \]  

(2)

when the count rate and the thickness of the absorber are measured, the attenuation coefficient can be determined from the slope obtained after the fitting is applied to the linear equation,

\[ \ln(R) = \ln(R_0) - \mu x. \]  

(3)

Equation (3) which is used in the present work is the only classic method that can be used to experimentally determine the attenuation coefficient. The fitting adapted is the least square technique.

3. Experimental setup and measurements

The experiment was conducted with the aim to measure the count rate of muons that penetrate different materials of different thicknesses. It was performed in a laboratory at the School of Applied Physics, Universiti Kebangsaan Malaysia, located at 101.78º E, 2.92º N and 30 m above sea level. The radiation background of this place has been investigated by several previous studies such as Samat and Evans (2011) and Tawalbeh, Samat, and Yasir (2013). The telescope chosen was made from two detectors with a very small solid angle. This telescope has been experimentally investigated and its result has been statistically tested (Altameemi et al., 2019).

The setup is made of two muon telescope (MT). Each telescope as shown in Figure 1 is made up of two Geiger-Muller (GM tubes) of GM1 and GM2 detectors fixed inside the RM60 radiation monitors (RM1, RM2) with 11 cm apart. The axis of the cylindrical chamber of each GM is on one vertical line (Zain, Gopir, Yatim, Sanusi, & Husain, 2010; Zain, Gopir, Yatim, Sanusi, &...
Husaina, 2009) (see Table 1). Both of the RM60 radiation monitors (RM1 and RM2) in the telescope are connected to a coincidence box in order to determine the instantaneous radiation events that occur simultaneously in both of them. The output of the coincidence box is recorded and displayed on a computer monitor that works using Aw-Radw software for the real-time radiation data. The metal sheets with a dimension of 20 cm × 20 cm and different thicknesses used in the experiment are given in Table 2.

The two muon telescopes are fixed apart from each other inside a housing box and the metal sheets are placed on the top of them (Altameemi & Gopir, 2016). The incoming cosmic ray muons from the atmosphere will pass through the reinforced ceiling that is made up of one layer of reinforced concrete consisting of a different element such as iron before impact to the top of the muon telescope placed in the testing room. The reinforced concrete and the walls of the lab are acted as a shielding layer but because concrete has a density of ≈ 2.3 g/cm³ and a relatively small amount of muon absorption with a coefficient α of (0.0001 ± 0.00014)cm⁻¹ as measured in the reinforced concrete building, which has no influence on the count rate of muon within the condition of our experiment. In the experimental setup, two telescopes were chosen, for two measurements for each thickness of an absorber, to obtain less variation. The difference between them is that the next measure in one of them is with thicker absorber whereas the other is thinner. Therefore, this difference may reflect the variance in the count rate due to increasing the absorber thickness while the other, the decreasing. The combination of the two measures from the two telescopes by taking the average could cancel out this variance and obtain more effective count rates.

When slices were chosen as the absorber with a certain thickness, the count rate was collected for 24 h that is long enough to ensure valid measures by the efficient telescope. Starting with the Pb absorber, all slices were placed on the first telescope and zero slice on the second telescope, the measures were taken for 1 day from the two telescopes. Then, several slices of an initial small thickness were moved from the first to the second telescope and the measures were taken again from the two telescopes. We continued moving several slices from one to the other, and with every move, we took the measures from the two telescopes. In the end, all slices were moved to the second telescope. The zero thickness of the absorber (no absorber) was taken twice; one at the beginning using the second telescope and one at the end using the first telescope. Therefore, the two measures were taken on different dates. On the same footing, every thickness of an absorber was taken twice on different dates. All other measurements were achieved through the same method for the slices of the other metals: Cu, Zn, and Al.

### Table 1. The characteristics of muon telescope.

| GM tube | window density | effective diameter | effective area | radiation monitor wall thickness | wall effective length | Telescope distance between the GM tubes (bottom of the upper to the top of the down) | solid angle |
|---------|----------------|--------------------|----------------|---------------------------------|----------------------|-----------------------------------------------------------------|-------------|
|         | 1.5 to 2.0 mg/cm² | 0.91 cm (0.360 inch) | 0.66 cm² (0.102 inch²) | 0.04 cm (0.012 inch) | 3.81 cm (1.5 inch) | 7.19 cm | 0.05 sr. |

### Table 2. Metal sheet thickness.

| Metal | Single sheet/slide thickness | Total thickness (cm) |
|-------|-----------------------------|----------------------|
| Pb    | 140 slides of 0.10 cm each | 14.00                |
| Cu    | 19 slides of 0.15 cm each  | 18.45                |
|       | 78 slides of 0.20 cm each  |                      |
| Zn    | 20 slides of 0.15 cm each  | 17.40                |
|       | 72 slides of 0.20 cm each  |                      |
| Al    | 20 slides of 0.10 cm each  | 20.00                |
|       | 90 slides of 0.20 cm each  |                      |

4. Results, analysis, and discussion

The combination of the count rate measured by the two telescopes with Pb absorber of different thicknesses is shown in Figure 2. A familiar behavior of fast-growing was observed until a point called the transition point, and then the count rate started to exponentially decay. The exponential decay has been well studied and is considered in the present work as exponential attenuation of muon intensity. The shielding dense material of different atomic numbers has a different coefficient of attenuation (George, Jánossy, & McCaig, 1942; Jánossy & Nagy, 1957; Nagy, 1958). Obtaining such a graph for the Pb absorber confirmed the validity of the telescope.

In Figure 2, the transition point of about 1.5 cm is obtained from the position of the peak reading after applying the extreme fitting curve. This value is the same as the transition point of 1.5 cm obtained from early work (George et al., 1942). Such an agreement does not only confirm the capability of the telescope to measure the muon rays but also indicates its efficiency in determining the attenuation coefficients. Using Equation (3) and the least square fitting, the attenuation coefficient of lead was determined as a slope from Figure 2 (bottom) with a value of (0.15 ± 0.01)cm⁻¹. On the same footing achieved for
Figure 2. Attenuation of muon intensity (count rate $R$) through Pb absorber with different depth $x$.

Figure 3. Attenuation of muon intensity (count rate $R$) through Cu absorber with different depth $x$. 
lead, the measurement, analysis and determining the coefficient of others: Cu, Zn, and Al were achieved as shown in Figures 3-5 respectively. The count rate-thickness graphs of the other elements showed clear behaviors with transition points of 3 cm, 4 cm and 9 cm for copper, zinc, and aluminum, respectively. The transition thickness is a specific property of the metal. It shows the capability of the matter to absorb the cosmic muon. Therefore, it depends on the mass density and the atomic number of the metal. Based on Table 3, it is clear that when the atomic number of the absorber increases, the lesser is the transition depth then increase the absorption. Therefore, the higher Z metals and mass density lead to higher capability of absorption.

As mentioned previously, many early works studied the variation of muon count rate with the depth of the penetration; however, none had calculated the attenuation coefficient. Recently, Fredrick (2016) experimentally determined the attenuation coefficient for Al to be 0.09 cm^{-1} and found that the value obtained from the theoretical calculation using the simulation program GEANT is 0.04 cm^{-1} (Schreiner III, 2016). Undoubtedly, such a difference belongs to the energy dependence, the experimental setup and the position of the measured cosmic muon.

The larger value of the attenuation coefficient for lead, Pb (see Table 3) is a good indicator to distinguish between the heavy metal and the light by muon absorption. The coefficients of the metal obtained are very important for the study of attenuation in the future.

5. Conclusion

As aluminum of low atomic weight is the best shield for beta particles, the cosmic muon is similar to gamma ray in that both can be shielded by heavy atomic weight metals like lead. This characteristic of lead for cosmic muon absorption confirms the possibility of the use of the muon telescope to detect lead since it has a very large attenuation coefficient. Since the detection could be extended to more materials, the results showed that the more the atomic weight of the muon absorber, the higher the ability to absorb. The transition depth is a very good reference as beyond it the attenuation starts, and the detection becomes possible. The determined coefficients of attenuation for metals are useful as a reference for...
future work on anisotropic muon absorption in many applications.

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Disclosure statement

No potential conflict of interest was reported by the authors.

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