End-to-end Full Projector Compensation

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Abstract — Full projector compensation aims to modify a projector input image to compensate for both geometric and photometric disturbance of the projection surface. Traditional methods usually solve the two parts separately and may suffer from suboptimal solutions. In this paper, we propose the first end-to-end differentiable solution, named CompenNeSt++, to solve the two problems jointly. First, we propose a novel geometric correction subnet, named WarpingNet, which is designed with a cascaded coarse-to-fine structure to learn the sampling grid directly from sampling images. Second, we propose a novel photometric compensation subnet, named CompenNeSt, which is designed with a siamese architecture to capture the photometric interactions between the projection surface and the projected images, and to use such information to compensate the geometrically corrected images. By concatenating WarpingNet with CompenNeSt, CompenNeSt++ accomplishes full projector compensation and is end-to-end trainable. Third, to improve practicability, we propose a novel synthetic data-based pre-training strategy to significantly reduce the number of training images and training time. Moreover, we construct the first setup-independent full compensation benchmark to facilitate future studies. In thorough experiments, our method shows clear advantages over prior art with promising compensation quality and meanwhile being practically convenient.

Index Terms — Projector compensation, Projector-camera systems, Image warping, Image enhancement

1 INTRODUCTION

With the recent advance in projector technologies, projectors have been gaining increasing popularity with many applications [1], [4], [12], [13], [16], [21], [22], [37], [43], [51], [52], [55], [60]. Existing systems typically require the projection surface (screen) to be planar, white and textureless, and under reasonable environment illumination. These requirements often create bottlenecks for generalization of projector systems. Full projector geometric correction and photometric compensation [2], [4], [17], [44], [51], [52] aims to address this issue by modifying a projector input image to compensate for the projection setup geometry [5], [37], [42], [43], [54] and associated photometric environment [1], [3], [15], [20], [60]. In the rest of the text, we call it full compensation for conciseness. An example from our solution is illustrated in Fig. 1, where the compensated projection result (e) is clearly more visually pleasant than the uncompensated one in (c).

A typical full projector compensation system consists of a projector-camera pair and a nonplanar textured projection surface placed at a fixed distance and orientation (Fig. 1(a)). Most existing methods work in two separate steps: (1) geometric surface modeling, e.g., via a sequence of structured light (SL) patterns [12], [36], and (2) color and texture compensation on top of the geometrically corrected projection, via another sequence of sampling images. Once the camera captures all the projected sampling images, a composite function is fitted to map the input images to the captured images. This function (or its inverse) is then used to infer the compensated image for a new input image.

Although relatively easy to implement, this two-step pipeline has four major issues: (1) Geometric correction is usually performed offline and typically requires additional projected patterns (e.g., Gray-coded SL [12], [36]) that may be disturbed by the projection surface geometry (e.g., reflection, see Fig. 7). It works well when the surface is textureless and the projector-camera system is photometrically calibrated. However, the decoding SL patterns may be imperfect due to photometric disturbance [12], [16], [49] e.g., a textured surface or photometrically uncalibrated projector-camera settings or specular highlight, and thus may lead to an unreliable geometric correction. Then, a second step...
of photometric compensation on top of the erroneous geometric correction may aggravate the suboptimal solution. (2) Moreover, because the geometric correction is assumed independent of the photometric compensation, this two-step pipeline is non-differentiable and thus inaccessible to derivative-based machine learning approaches. (3) Existing solutions (e.g., [13], [15], [38], [48]) usually model the photometric compensation function explicitly, with various simplification assumptions that allow the parameters to be estimated from collected samples. These assumptions, such as context independence (§ 2.2.2), however, are often violated in practice. Furthermore, due to the extremely complex geometric and photometric processes involved in projector-camera systems, it is hard for traditional photometric compensation solutions to faithfully accomplish their task. (4) When projector-camera system setup changes, e.g., replacing the projection surface, changing the projector-camera pose, and adjusting the environment light, the camera exposure or the projector brightness, existing methods must restart the projection-capturing-compensation process from scratch, which is apparently impractical in real life applications.

In this paper, for the first time, an end-to-end full compensation solution is presented to address the above issues. We start by reformulating the compensation problem as a novel form (i.e., disentanglement of geometry and photometry) that can be learned online, as required by the compensation task in practice. This formulation allows us to develop a convolutional neural network (CNN), named CompenNeSt++, to jointly solve both geometric correction and photometric compensation in a unified pipeline solely from the sampling images (i.e., without an additional step of structured light).

By taking into consideration of both geometric and photometric ingredients in the compensation formulation, we carefully design CompenNeSt++ as composed of two subnets. The first subnet is a novel cascaded coarse-to-fine geometric correction subnet, named WarpingNet (Fig. 2), which learns the sampling grid and performs geometric correction; while the second subnet is a novel CNN named CompenNeSt for photometric compensation. CompenNeSt consists of a siamese encoder and a decoder. Such an architecture captures rich multi-level interactions between the camera-captured projection surface image and the projector input image, and allows us to intuitively perform compensation by subtracting the surface features from the projector input image features through skip connections [18]. Moreover, we use two low-level skip connections to carry the high frequency information to the penultimate and the output layers, allowing CompenNeSt to learn the residual features instead of inferring from scratch, thus improving the network convergence.

It is worth highlighting that the two subnets are concatenated directly (Fig. 2), which makes CompenNeSt++ end-to-end trainable/differentiable, i.e., the loss gradients can back-propagate from CompenNeSt module to WarpingNet module, allowing joint optimization of geometry and photometry. In addition, we propose multiple task-specific training strategies, such as projector field of view (FOV)-based WarpingNet weight initialization and projection-free CompenNeSt weight initialization to further improve model convergence.

Another advantage of our CompenNeSt++ is practicability. When setup changes, traditional non-learning based methods have to rerun the compensation process from scratch, which is impractical in real life applications. On the contrary, we propose a Blender [6] rendered synthetic dataset and pre-train CompenNeSt on it, then CompenNeSt++ can be quickly fine-tuned to adapt to new setups. This strategy significantly reduces the number of training images (as few as 8 images) and training time (as short as 3 minutes) and is quite useful in practice. Moreover, during testing/inference, we simplify the WarpingNet to a single sampling grid and the CompenNeSt surface feature branch to biases, and thus further improve the running time efficiency of CompenNeSt++.

Last but not least, an important issue addressed in this paper is the absence of evaluation benchmarks for projector compensation, due mainly to the fact that traditional evaluation is highly setup dependent. More specifically, to evaluate a compensation algorithm, theoretically, its experimental results need to be actually projected and captured and then quantitatively compared with ground truth. This process makes it impractical to provide a shared benchmark among different research groups. In this work, we tackle this issue by deriving a surrogate evaluation protocol that requires no actual projection of the algorithm output. As a result, this surrogate allows us to construct, for the first time, two sharable setup-independent compensation benchmarks, one for full compensation and another for partial photometric compensation. The proposed CompenNeSt++/CompenNeSt is evaluated on the two benchmarks that are carefully designed to cover various challenging factors. In the experiments, CompenNeSt++ demonstrates clear advantages compared with state-of-the-arts.

Our contributions can be summarized as follows:

1) For the first time, an end-to-end trainable solution is proposed for full compensation. Such a solution allows our system to effectively and explicitly capture the complex geometric and photometric interactions involved in the full compensation process.

2) Compared with two-step methods, CompenNeSt++ not only is fully differentiable but also learns the geometric correction without an additional step of structured light and outperforms the traditional two-step methods.

3) Two task-specific weight initializations and two network simplification techniques are proposed to further improve the convergence and running time efficiency of CompenNeSt++.

4) For the first time, a synthetic data-based pre-training method is proposed to significantly improve the practical efficiency of our system.

5) For the first time, a setup-independent full compensation benchmark and a partial photometric compensation benchmark are constructed, which is expected to facilitate future works in this direction.

This paper builds upon preliminary conference papers CompenNet [28] and CompenNet++ [19] and significantly extends them in various aspects. (1) We redesigned the
photometric compensation subnet as removing the surface from the projector input image in the feature space, based on which we propose a novel photometric compensation subnet named CompenNeSt (i.e., the photometric part of CompenNeSt++, the additional “S” stands for siamese). Compared with our previous CompenNet [20] (i.e., the photometric part of CompenNet++ [19]), CompenNeSt is designed with a siamese encoder to explicitly apply the same feature transformation to the surface image and the projector input image, using which we can perform photometric compensation by subtracting the surface pattern from the projector input image in the feature space. Moreover, minor tweaks on skip and transposed convolutional layers are shown to further improve model performance. We show in experimental comparisons that compared with CompenNet++ [19], CompenNeSt++ architecture not only reduces the number of learnable parameters by 27.7% but also significantly improves full compensation accuracy; (2) We perform in-depth ablation studies and show what features are learned by CompenNeSt++ and how the compensation is performed in the feature space. Such studies were not available in our previous papers. (3) We propose a novel pre-training strategy using Blender [6] rendered synthetic dataset, which greatly improves the practicability compared with the naive pre-training method of CompenNet/CompenNet++ [19], [20] and it can significantly reduce the number of training images to 8 and training time to 3 minutes.

For the benefit of the society, the source code, evaluation benchmark and experimental results are publicly available at https://github.com/BingyaoHuang/CompenNeSt-plusplus.

2 RELATED WORKS

In theory, the projector compensation process is a very complicated nonlinear function involving the camera and the projector sensor radiometric responses [38], lens distortion/vignetting [30], perspective transformations [23], [63], surface material reflectance [21], [41], defocus [31], [59], [61] and inter-reflection [53]. A great amount of effort has been dedicated to designing practical and accurate compensation models, which can be roughly categorized into two types: full compensation [4], [17], [44], [49], [51], [52], [58] and partial ones [1], [3], [15], [15], [20], [35], [38], [48], [53].

2.1 Full compensation methods

Full compensation methods perform both geometric correction and photometric compensation. The pioneer work by Raskar et al. [44] creates projection mapping animations on nonplanar colored objects with two projectors. Despite compensating both geometry and photometry, manual registrations using known markers are required. Wetzstein et al. [38] employ a full light transport matrix for full compensation. Despite obtaining accurate global illumination and geometry, it requires an additional radiometric calibration step and capturing and inverting the full light transport matrix is relatively time consuming. Harville et al. [17] propose a full multi-projector compensation method for a white curved screen. The projector-camera pixel correspondences are obtained via 8-12 SL images. Despite being effective to blend multiple projector’s colors, this method assumes a textureless projection surface.

Recently, Siegl et al. [51], [52] perform full compensation on nonplanar Lambertian surfaces for dynamic real-time projection mapping. Similar to [17], they assume the target objects are white and textureless. Asayama et al. [2] attach visual markers to nonplanar textured surfaces for real-time object pose tracking. To remove the disturbance of the markers, photometric compensation is applied to hide the markers from the viewer, and additional IR cameras/emitters are required accordingly. Shahpaski et al. [49] embed color squares in the projected checkerboard pattern to calibrate both the geometry and the gamma function. Although only two shots are required, this method needs a pre-calibrated camera and another planar printed checkerboard target. Moreover, it only performs a uniform gamma compensation without compensating the surface, and thus may not work well on nonplanar textured surfaces.

2.2 Partial compensation methods

Compared to full compensation methods, partial compensation ones typically perform either geometric correction [3], [15], [42], [43], [54] or photometric compensation [1], [3], [15], [20], [60]. Due to the strong mutual-dependence between geometric correction and photometric compensation and to avoid propagated errors from the other part, these methods assume the other part is already performed as a prerequisite. However, this two-step pipeline is non-differentiable and may be subject to suboptimal solutions.

2.2.1 Geometric correction

Without using specialized hardware, such as a coaxial projector-camera pair [10], projector-camera image pairs’ geometric mapping needs to be estimated using methods such as structured light (SL) [5], [42], [43], [54], markers [37] or homographies [20]. Raskar et al. [43] propose a conformal texture mapping method to geometrically register multiple projectors for nonplanar surface projections, using SL and a calibrated camera. Tardif et al. [54] achieve similar results without calibrating the projector-camera pair. The geometrically corrected image is generated by SL inverse mapping. Similarly, Boroomand et al. [5] propose a saliency-guided SL geometric correction method. Narita et al. [37] use IR ink printed fiducial markers and a high-frame-rate camera for dynamic non-rigid surface projection mapping, which requires additional devices as [2].

2.2.2 Photometric compensation

These methods assume that the projector-camera image pairs are registered as a prerequisite and can be roughly categorized into two types: context-independent [13], [15], [38], [48] and context-aware ones [1], [3], [20], [35], [53], where context-aware ones typically assume projector-camera pixels one-to-one mapping while context-aware ones also consider neighborhood/global information. A detailed review can be found in [16]. Context-independent methods typically assume that there is an approximate one-to-one mapping between the projector and camera image pixels, i.e., a camera pixel only
depends on its corresponding projector pixel and the surface patch illuminated by that projector pixel. Namely, each pixel is roughly independent of its neighborhood context. The pioneer work by Nayar et al. [38] proposes a linear model that maps a projector ray brightness to camera detected irradiance with a $3 \times 3$ color mixing matrix. Grossberg et al. [13] improve Nayar’s work and model the environment lighting by adding a $3 \times 1$ vector to the camera-captured irradiance. However, an additional step of the uniform radiometric responses calibration is required for the linearity to hold. Moreover, as pointed out by Juang et al. [30], even with radiometric calibration, the assumption of uniform radiometric response may be violated.

To address this issue, some studies absorb the non-linear radiometric responses in the compensation function, e.g., Sajadi et al. [48] fit a smooth higher-dimensional Bézier patches-based model with $9^3=729$ sampling images. Grundhöfer and Iwai [15] propose a thin plate spline (TPS)-based method and reduce the number of sampling images to $5^3=125$ and further deal with clipping errors and image smoothness with a global optimization step. Other than optimizing the image colors numerically, some methods specifically focus on human perceptual properties, e.g., Huang et al. [24] generate visually pleasing projections by exploring human visual system’s chromatic adaptation and perceptual anchoring property. Also, clipping artifacts due to camera/projector sensor limitation are minimized using gamut scaling.

Despite largely simplifying the compensation problem, the context-independent assumption is usually violated in practice, due to many factors such as perspective projection, lens distortion, defocus and surface inter-reflection [53], [58], [39], [61]. As a result, a projector pixel can illuminate multiple surface patches and a patch can also be illuminated by the inter-reflections of its surrounding patches, and a camera pixel is also determined by rays reflected by multiple patches.

**Context-aware methods** compensate a pixel by considering information from neighborhood context. Grundhöfer and Bimber [14] tackle visual artifacts and enhance brightness and contrast by analyzing the projection surface and input image prior. Li et al. [35] reduce the number of sampling images to at least two by sparse sampling and linear interpolation. Multidimensional reflectance vectors are extracted as color transfer function control points.

Due to the small size of sampling dots, this method may be sensitive to projector defocus and lens vignetting. A simple linear interpolation using those unreliable samples may add to the compensation errors. Besides computing an offline compensation model, Aliaga et al. [1] introduce a run time linear scaling operation to optimize multiple projector compensations. Takeda et al. [53] propose an inter-reflection compensation method using an ultraviolet LED array.

Context-aware methods generally improve over context-independent methods by integrating more information. However, it is extremely hard to model or approximate the ideal compensation process due to complex interactions between the global illuminations, the projection surface and the input image. Moreover, most existing works focus on reducing pixel-wise color errors only rather than jointly improving the color fidelity and structural similarity [57].

### 2.3 Our method

To the best of our knowledge, there exists no previous end-to-end trainable method that performs simultaneous full projector geometric correction and photometric compensation. Our method is inspired by the successes of recently proposed deep learning-based image-to-image translation, such as Pix2pix [27], CycleGAN [65], neural style transfer [11], [25], [29], image super-resolution [9], [32], [34], [56] and image colorization [7], [26], [62]. That said, as the first deep learning-based full compensation algorithm, our method is very different from these studies and has its own special physical domain knowledge. For example, unlike the CNN models above that can be trained once and for all, the projector compensation model needs to be quickly retrained if the system setup changes. However, in practice, capturing training images and training the model are both time consuming. In addition, data augmentation techniques such as random cropping, affine transformation and color jitter are not available for our task, because each camera pixel is strongly coupled with a neighborhood of its corresponding projector pixel and the projection surface patch illuminated by those pixels. Furthermore, general image-to-image translation models do not consider the physical domain knowledge of projector compensation task, e.g., they do not explicitly formulate the complex geometric transformations and spectral interactions between the global lighting, the projector backlight and the projection surface. In fact, the advantage of the proposed method over the classical Pix2pix [27] algorithm is clearly in our evaluations.

In summary, belonging to the full compensation regime, our CompenNeSt++ is the first to jointly learn geometric correction and photometric compensation in an end-to-end framework. The advantage of the proposed CompenNeSt++ over both traditional and deep learning-based two-step methods, is clearly demonstrated quantitatively and qualitatively.

### 3 Deep Full Projector Compensation

#### 3.1 Problem formulation

Our full projector compensation system consists of an uncalibrated projector-camera pair and a non-planar textured projection surface placed at a fixed distance and orientation (Fig. 1(a)). Denote the projector input image as $x$, the composite geometric projection and photometric transfer function as $\pi_p$, and the projector geometric and photometric parameters as $p$. Then, the projected radiance can be denoted as $\pi_p(x, p)$. Let the composite surface reflectance, geometry and pose be $s$, the surface reflection function be $\pi_s$, the global lighting be $g$, camera’s composite capturing function be $\pi_c$, and its composite parameters be $c$. Finally, the camera-captured image $\tilde{x}$ is given by:

$$\tilde{x} = \pi_c(\pi_s(\pi_p(x, p), g, s), c) \quad (1)$$

Note that the composite geometric and photometric process in Eq. 1 is very complex and obviously has no closed form solution. Instead, we find that $p$ and $c$ are constant once the setup is fixed, thus, we disentangle the geometric and photometric transformations and absorb $p$ and $c$ in two

2. We use ‘tilde’ ($\tilde{x}$) to indicate a camera-captured image, see Fig. 2(a).
functions: $T : \mathbb{R}^{H_1 \times W_1 \times 3} \rightarrow \mathbb{R}^{H_2 \times W_2 \times 3}$ that geometrically warps a projector input image to camera-captured image; and $F : \mathbb{R}^{H_1 \times W_1 \times 3} \rightarrow \mathbb{R}^{H_1 \times W_1 \times 3}$ that photometrically transforms a projector input image to an uncompensated camera-captured image (aligned with the projector canonical frontal view). Thus, Eq. 1 can be reformulated as:

$$\hat{x} = T(F(x; g, s)) \quad (2)$$

Full projector compensation aims to find a projector input image $x^*$, named "compensation image" of $x$, such that the viewer-perceived projection result is the same as the ideal desired viewer-perceived image $x'$, i.e.,

$$T(F(x^*; g, s)) = x' \quad (3)$$

where $x'$ is an affine transformed $x$ to match the optimal displayable area (Fig. 5 and Fig. 4). Thus the compensation image $x^*$ in Eq. 3 can be solved by:

$$x^* = F^\dagger(T^{-1}(x')); \quad (4)$$

In practice it is hard to measure $g$ and $s$ directly. For this reason, we implicitly capture them using a camera-captured surface image $\hat{s}$ under the global lighting and the projector backlight:

$$\hat{s} = T(F(x_0; g, s)), \quad (5)$$

where $x_0$ is set to a plain gray image to provide some illumination.

It is worth noting that other than the surface patches illuminated by the projector, the rest part of the surface outside the projector FOV does not provide useful information for compensation (Fig. 2(a) black regions of $\hat{s}$), thus $\hat{s}$ in Eq. 5 can be approximated by a subregion of the camera-captured image $T^{-1}(\hat{s})$ (Fig. 2(b)). Substituting $g$ and $s$ in Eq. 4 with $T^{-1}(\hat{s})$, we have the compensation problem as

$$x^* = F^\dagger(T^{-1}(x'); T^{-1}(\hat{s})), \quad (6)$$

where $F^\dagger$ is the pseudo-inverse of $F$ and $T^{-1}$ is the inverse geometric transformation of $T$.

### 3.2 Learning-based formulation

Obviously, Eq. 6 has no closed form solution and thus we model $F^\dagger$ and $T^{-1}$ jointly with a deep neural network named CompenNeSt++ and learn it using image pairs like $(x^*, x')$ and a camera-captured surface image $\hat{s}$. A key requirement for this solution is the availability of training data, however it is very difficult to obtain the ground truth of the compensation image $x^*$. Fortunately, by investigating Eq. 2 and Eq. 5 we find that:

$$\hat{x} = T(F(x; \hat{s})) \Rightarrow x = F^\dagger(T^{-1}(\hat{x}); T^{-1}(\hat{s})) \quad (7)$$

The equation above follows the same physical process as Eq. 6, indicating that we can train CompenNeSt++ over sampled image pairs like $(\hat{x}, x)$ and a surface image $\hat{s}$, which can be easily obtained (Fig. 3 left).

Another advantage of learning CompenNeSt++ using Eq. 7 instead of Eq. 6 is that we can construct a sharable setup-independent benchmark for model evaluation and comparison without actual projections or captures, see §4.

In the rest of the paper, we abuse the notation $\pi_{\theta}(\cdot; \cdot) \equiv F^\dagger(T^{-1}(\cdot); T^{-1}(\cdot))$ for conciseness, where $\theta = \{\theta_F, \theta_T\}$ are CompenNeSt++’s learnable parameters. By using Eq. 7, we can capture a set of $N$ training pairs, denoted as $X = \{(\hat{x}_i, x_i)\}_{i=1}^N$. Then, with a proper image reconstruction loss $\mathcal{L}$, CompenNeSt++ can be learned by

$$\theta = \arg \min_{\theta} \sum_i \mathcal{L}(\hat{x}_i; \pi_{\theta}(\hat{x}_i; \hat{s}), x_i) \quad (8)$$

where $\hat{x}$ is the compensation of $\hat{x}$ (not $x$, see Fig. 2 network output). Unlike previous methods [15], [48] that use simple
As shown in Fig. 2, WarpingNet consists of three learnable modules (i.e., \( \theta_{\text{aff}} \), \( \theta_{\text{TPS}} \) and \( W_\theta \)), a grid generation function \( G \), a bilinear interpolation-based image sampler \( \phi \), and three generated sampling grids ranked in order of increasing granularity: \( \Omega_{\text{aff}} = G(\theta_{\text{aff}}), \Omega_{\text{TPS}} = G(\theta_{\text{TPS}}), \Omega_r = W_\theta(\Omega_{\text{TPS}}) \).

Specifically, \( \theta_{\text{aff}} \) is a 2x3 learnable affine matrix and it roughly warps the input image \( \tilde{x} \) to the projector canonical frontal view. Similarly, \( \theta_{\text{TPS}} \) contains \((6 \times 6 + 2) \times 2 = 76\) learnable thin plate spline (TPS) \([8]\) parameters and it further nonlinearly warps the rough affine-transformed image \( \phi(\tilde{x}; \Omega_{\text{aff}}) \) to better match the exact projector canonical frontal view. Unlike \([28],[46]\), \( \theta_{\text{aff}} \) and \( \theta_{\text{TPS}} \) are directly learned without using a regression network, which is more efficient and accurate in our case.

Although TPS can approximate nonlinear smooth geometric transformations, its accuracy depends on the number of control points and the spline assumptions. Thus, it may not precisely model geometric deformations involved in the projector-camera imaging process. To address this issue, we design a grid refinement CNN, i.e., \( W_\theta \), to refine the TPS sampling grid. Basically, this module learns a fine-grained displacement for each 2D coordinate in the TPS sampling grid by a residual connection \([18]\), giving the refined sampling grid \( \Omega_r \), higher precisions. The advantages of our CompenNeSt++ over a degraded CompenNeSt++ without grid refinement net (named CompenNeSt++ w/o refine) are evidenced in Tab. 1.

Besides the novel cascaded coarse-to-fine structure with a grid refinement network, we propose a novel sampling strategy that improves WarpingNet efficiency and accuracy. Intuitively, the cascaded coarse-to-fine sampling method should sequentially sample the input \( \tilde{x} \) by

\[
\mathcal{T}^{-1}(\tilde{x}) = \phi(\phi(\phi(\tilde{x}; \Omega_{\text{aff}}); \Omega_{\text{TPS}}); \Omega_r; W_\theta_r(\Omega_{\text{TPS}}))
\]

(10)

However, the three bilinear interpolations (\( \phi \)) above not only are computationally inefficient but also produce a blurred image. Instead, we perform the sampling in the 2D coordinate space, i.e., let the finer TPS grid sample the coarser affine grid followed by a refinement using \( W_\theta_r \), as shown in Fig. 2(b). Thus, the new warped image is given by:

\[
\mathcal{T}^{-1}(\tilde{x}) = \phi(\tilde{x}; W_\theta_r(\phi(\phi(\tilde{x}; \Omega_{\text{aff}}); \Omega_{\text{TPS}})))
\]

(11)

This strategy brings two benefits: (1) only two sampling operations are required and thus it is more efficient; and (2) since the image sampling is only performed once on \( \tilde{x} \), the warped image is sharper compared with using Eq. 10.

Another novelty of WarpingNet is network simplification owing to the sampling strategy above. During testing, WarpingNet is simplified essentially to a single sampling grid \( \Omega_r \) and thus the geometric correction becomes a single bilinear interpolation \( \mathcal{T}^{-1}(\tilde{x}) = \phi(\tilde{x}; \Omega_r) \). This strategy allows us to perform geometric corrections without running grid generation or refinement network, bringing improved testing/inference efficiency (see Fig. 4).

Finally, to improve training convergence and robustness we introduce carefully designed WarpingNet weights initialization techniques in § 3.4.

3.3.2 CompenNeSt \( \mathcal{F}^\dagger \)

CompenNeSt consists of a siamese encoder and a decoder. During training (Fig. 2(b) and Fig. 3 left), it takes two WarpingNet transformed camera-captured images as inputs, i.e.,
a warped surface image $T^{-1}(\tilde{s})$ and a warped sampling image $T^{-1}(\tilde{x})$ and outputs the inferred projector-input image $\tilde{x}$. Both two inputs and the output are 256×256×3 RGB images. Firstly, $\tilde{s}$ and $\tilde{x}$ are fed to the siamese encoder to downsample and to extract multi-level feature maps. Note that in Fig. 2 we give the two encoder branches the same orange color to emphasize that they share weights. Then, the surface’s multi-level and multi-scale feature maps are subtracted from the feature maps of camera-captured image $\tilde{x}$. This design is inspired by the observation that compensation is analogous to removing/canceling the surface $(T^{-1}(\tilde{s}))$ disturbance/patterns/features from the input images ($\tilde{x}'$ or $\tilde{x}$). See how to interpret this physical domain knowledge in §5.2.3.

To improve convergence, we pass low-level interaction information (i.e., feature maps from the first two layers) to high-level feature maps through skip convolutional layers [18]. This design is based on the observation that the output compensated image should look like the projector input image on structure, thus passing the low-level features (i.e., high frequency structural information) to the output layer allows the network to learn residuals on top of a good initial guess thus obviating the need of inferring from scratch.

However, even with the above structure we find it difficult to jointly learn geometric and photometric processes without a proper model initialization, and the output images may become plain gray. To address this issue, we incorporate rich task-specific domain knowledge to weights initialization and training strategies below.

### 3.4 Task-specific domain knowledge and constraints

To improve model convergence and robustness, we leverage rich task-specific domain knowledge of projector-camera systems to initialize and train CompenNeSt++.

#### 3.4.1 Projector FOV mask

According to Eq. 7, full projector compensation’s region of interest is the projector FOV, i.e., Fig. 5 illuminated regions. Thus we can compute a projector FOV mask by automatically thresholding the camera-captured surface images with Otsu’s method [39] followed by some morphological operations (Fig. 5). This mask brings threefold benefits: (1) masking out the pixels outside of the projector FOV improves training stability and efficiency because the image reconstruction loss (Eq. 9) increases significantly when black regions are mis-registered to the ground truth $\tilde{x}$, forcing the WarpingNet to quickly infer a plausible warping grid; (2) the projector FOV mask is the key to initialize WarpingNet affine weights $\theta_{aff}$ in §3.4.2 and (3) to find the optimal displayable area in §3.8.

#### 3.4.2 WarpingNet weights initialization

We further improve the training efficiency by providing a task-specific prior, e.g., the coarse affine warping branch in WarpingNet (Fig. 2(b)) aims to transform the input image $\tilde{x}$ to the projector canonical frontal view, as mentioned in §3.3.1. Thus, the affine parameters $\theta_{aff}$ can be initialized such that the projector FOV mask’s bounding rectangle (Fig. 5 green rectangle) is stretched to fill the warped image. Then, to avoid implausible large displacement from a default random initialization, $\theta_{TPS}$ and grid refinement net $\mathcal{W}_g$ are initialized with small random numbers at a scale of $10^{-4}$, such that they generate identity mappings. These task specific initialization techniques provide a relatively good starting point, allowing CompenNeSt++ to converge stably and efficiently.

#### 3.4.3 CompenNeSt weights initialization

In our end-to-end full compensation pipeline, despite with the training techniques of WarpingNet above, joint training WarpingNet and CompenNeSt may still subject to suboptimal solutions, e.g., the output images become plain gray. Similar to WarpingNet weights initialization, we introduce some photometric prior knowledge to improve CompenNeSt stability and efficiency.

Since our CompenNeSt is has an encoder-decoder-like structure, the weights can be initialized by setting the input surface image $T^{-1}(\tilde{s})$ to zero and training the model in an autoencoder way, i.e., reconstructing the input camera-captured sampling image $T^{-1}(\tilde{x})$. We further simplify the input camera-captured sampling image $T^{-1}(\tilde{x})$ to a projector input image $\tilde{x}$ to avoid actual projection. The training objective function is given in Eq. 12.
§

We train the model on 500 textured sampling images for 2,000 iterations. Then in practice, CompenNeSt can be initialized by loading the saved weights.

### 3.5 Practical compensation using a pre-trained model

Projector compensation requires re-calibration once the setup changes, e.g., replacing the projection surface, changing the projector-camera pose, and adjusting the environment light, the camera exposure or the projector brightness. Previous approaches must re-run the projection-capturing-compensation process from scratch, which is apparently impractical in real-life applications. On the contrary, owing to the end-to-end trainable architecture, our CompenNeSt can be pre-trained and then fine-tuned on new setups using much fewer images and less training time.

Firstly, we render 100 setups with different projector-camera-surface poses, materials, exposures and lightings in Blender [6] (see § 4.2.2). Then, we initialize CompenNeSt using the technique in § 3.4.3 and trained CompenNeSt for 1,500 iterations on two Nvidia GeForce 1080Ti GPUs with a batch size of 48, and it takes about 15 min to finish (without pre-train).

Next, we collect the test set of $N$ samples as $\mathcal{X} = \{(\tilde{x}_i, x_0)\}_{i=1}^N$ and $\tilde{s}$ to train the compensation model $\pi_{0} \approx \{x_0, \tilde{s}\}$ end-to-end (see Fig. 2(b)). Afterwards, as shown in Fig. 4, we simplify the trained CompenNeSt++ to the projector FOV mask $\pi_{0}$ using the techniques in § 3.6. Finally, for an ideal desired viewer-perceived image $z$, we infer its compensation image $z'$ and project $z'$ to the surface.

In practice, $z$ is physically restricted to the surface displayable area, i.e., a subregion of the projector FOV. Similar to [43], we find an optimal desired image $z' = \phi(z; A)$, where $A$ is a 2D affine transformation that uniformly scales and translates the ideal perceived image $z$ to optimally fit the projector FOV as shown in Fig. 5 and Fig. 4.

### 3.7 Implementation and Training Details

CompenNeSt++ is implemented using PyTorch [40] and trained using Adam optimizer [33] with a penalty factor of $10^{-4}$. The initial learning rate is set to $10^{-3}$ and decayed by a factor of 5 at the 1,000th iteration. The model weights are initialized using the techniques in § 3.4. We train the model for 1,500 iterations on two Nvidia GeForce 1080Ti GPUs with a batch size of 48, and it takes about 15 min to finish (without pre-train).

### 3.8 Compensation Pipeline

To summarize, our full projector compensation pipeline consists of three major steps. (1) As shown in Fig. 2(a), we start by projecting a plain gray image $x_0$, and $N$ sampling images $x_1, \ldots, x_N$ to the projection surface and capture them using the camera, and denote the captured images as $\tilde{s}$ and $\tilde{x}_i$, respectively. (2) Then, we gather the $N$ image pairs $\mathcal{X} = \{(\tilde{x}_i, x_0)\}_{i=1}^N$ and $\tilde{s}$ to train the compensation model $\pi_{0} \approx \{x_0, \tilde{s}\}$ end-to-end (see Fig. 2(b)). (3) Afterwards, as shown in Fig. 4, we simplify the trained CompenNeSt++ to the projector FOV mask $\pi_{0}$ using the techniques in § 3.6. Finally, for an ideal desired viewer-perceived image $z$, we infer its compensation image $z'$ and project $z'$ to the surface.

### 4 Benchmark

An issue left unaddressed in previous studies is the lack of public benchmarks for quantitative evaluation, due mainly to the fact that traditional evaluation is highly setup-dependent. In theory, to evaluate a compensation algorithm, its output compensation image $x'$ for input $x$ should be actually projected to the projection surface, and then captured by the camera and quantitatively compared with the ground truth. This process is obvious impractical since it requires the same projector-camera-environment setup for fair comparison of different algorithms.

In this work, motivated by our problem formulation, we derive an effective surrogate evaluation protocol that requires no actual projection of the algorithm output. The basic idea is, according to Eq. 7, we can collect testing samples in the same way as the training samples. We can also evaluate an algorithm in the similar way. Specifically, we collect the test set of $M$ samples as $\mathcal{Y} = \{(y_i, y_1)\}_{i=1}^M$, under the same system setup as the training set $\mathcal{X}$. Then the algorithm performance is measured by averaging over similarities ($i.e.$, PSNR, RMSE and SSIM [57]) between each testing input image $y_i$ and its algorithm output $\hat{y}_i = \pi_{0}(y_i; \tilde{s})$ and reported in Tab. 1.
Our projector compensation system consisted of a Canon 6D camera and a ViewSonic PJD7828HDL DLP projector with resolutions set to 640×480 and 800×600, respectively. In addition, an Elgato Cam Link 4K video capture card is connected to the camera to improve frame capturing efficiency (about 360ms per frame).

The above protocol allows us to construct a projector compensation evaluation benchmark, consisting of $K$ system setups, each with a training set $X_k$, a test set $Y_k$ and a surface image $\tilde{s}_k$, $k = 1, \ldots, K$.

### 4.1 System configuration

Our projector compensation system consisted of a Canon 6D camera and a ViewSonic PJD7828HDL DLP projector with resolutions set to 640×480 and 800×600, respectively. In addition, an Elgato Cam Link 4K video capture card is connected to the camera to improve frame capturing efficiency (about 360ms per frame).

The distance between the camera and the projector varies in the range of 500mm to 1,000mm and the projection surface is around 1,000mm in front of the projector-camera pair. The camera exposure, focus and white balance modes are set to manual; and the global lighting varies for each setup but is fixed during each setup’s data capturing and system testing.

### 4.2 Dataset

#### 4.2.1 Real data

To obtain the sampling colors and textures as diverse as possible, we downloaded 700 colorful textured images from the Internet and use $N = 500$ for each training set $X_k$ and $M = 200$ for each testing set $Y_k$. The experiment results in Tab. 1 show clear improvement of TPS textured over the original TPS method. Our explanations are: (a) Compared with plain color images, the metric process by removing the geometric process involved in WarpingNet. In fact, to abbreviate potential geometry disturbances we investigate CompenNeSt architecture in an ablation study on this dataset, as shown in Tab. 3, Fig. 10 and Fig. 9.

#### 4.2.2 Synthetic data

As mentioned in § 3.5, we propose a pre-training method to improve practicability of CompenNeSt++. Intuitively, it is better to pre-train the model on real data, however, it is difficult and time consuming to capture a real dataset consisting of a wide range of setup parameter variations, such as different lighting, surface material, projector-camera settings, and poses, etc. Instead, we synthesized a dataset using Blender and the virtual projector-camera system consisted of a camera, a projector and a textured surface. As our WarpingNet (the geometric part) is setup-dependent and cannot be pre-trained, we restrict the surface to be planar and focus on photometric compensation i.e., CompenNeSt only. The surface material is modeled using a tunable principle BSDF shader. For each setup, the surface base color is set with different textured images. To increase diversity, random perturbations are applied to the camera parameters and the camera/projector/surface poses.

In total, we render 100 synthetic setups and each setup consists of 500 image pairs for training and 200 for testing. Some representative samples are shown in Fig. 6. Note that in this dataset, both the surface patterns and the projected sampling images are different from the real dataset. Future works can leverage this dataset for model pre-training and network architecture exploration.

### 5 Experimental Evaluations

#### 5.1 Comparison with state-of-the-arts

We compare the proposed full compensation method (i.e., CompenNeSt++) with four two-step baselines, a context-independent TPS model [15], an improved TPS model (explained below), a Fix2pix model [27] and a CompenNeSt model that is without WarpingNet on the proposed evaluation benchmark.

To fairly compare two-step methods, we use the same structured light (SL) warping for geometric correction. We first projected 42 Gray-coded SL patterns [36] to establish projector-camera pixel-to-pixel mapping. Due to strong photometric disturbance, the SL method [36] might suffer from decoding errors and thus we use bilinear interpolation to fill the missing correspondences. Afterwards, we capture 125 pairs of plain color sampling image as used in the original TPS method [15] for photometric compensation, then we warp the sampling images to the projector canonical frontal view using SL and name this method $TPS \text{ w/ SL}$. We also fit the TPS method using SL-warped diverse textured training set $X_k$ and name this method $TPS \text{ textured w/ SL}$.

The experiment results in Tab. 1 show clear improvement of TPS textured over the original TPS method. Our explanations are: (a) Compared with plain color images, the metric process by removing the geometric process involved in WarpingNet. In fact, to abbreviate potential geometry disturbances we investigate CompenNeSt architecture in an ablation study on this dataset, as shown in Tab. 3, Fig. 10 and Fig. 9.

4. Not geometric correction [8], instead using TPS to model the pixel-wise photometric compensation function.
TABLE 1: Quantitative comparison of full compensation algorithms. Results are averaged over $K = 20$ different setups. Note that the metrics for uncompensated images are PSNR=9.5973, RMSE=0.5765 and SSIM=0.0767. The metrics for the original TPS [15] w/ SL (#Train=125) are PSNR=16.7271, RMSE=0.2549 and SSIM=0.5207. See supplementary material for separate measurements for each setup.

| Model                  | #Train=48 PSNR↑ | RMSE↑ | SSIM↑ | #Train=125 PSNR↑ | RMSE↑ | SSIM↑ | #Train=250 PSNR↑ | RMSE↑ | SSIM↑ | #Train=500 PSNR↑ | RMSE↑ | SSIM↑ |
|------------------------|-----------------|-------|-------|-----------------|-------|-------|-----------------|-------|-------|-----------------|-------|-------|
| TPS [15] textured w/ SL| 18.0297         | 0.2199| 0.5390| 18.0132         | 0.2205| 0.5687| 18.0080         | 0.2206| 0.5787| 17.9746         | 0.2215| 0.5830|
| Pix2pix [27]           |                 |       |       |                 |       |       |                 |       |       |                 |       |       |
|                        | 17.7160         | 0.2271| 0.5068| 17.1141         | 0.2468| 0.5392| 16.9236         | 0.2669| 0.5763| 19.4544         | 0.1893| 0.6222|
| CompenNeSt++ [19]      | 19.8552         | 0.1781| 0.6637| 20.7947         | 0.1958| 0.7116| 20.8959         | 0.1581| 0.7227| 21.1127         | 0.1540| 0.7269|
| CompenNet w/ SL        | 20.2788         | 0.1708| 0.6890| 21.0508         | 0.1560| 0.7219| 21.3389         | 0.1508| 0.7376| 21.5184         | 0.1476| 0.7413|
| CompenNeSt++ w/o surf. | 18.1238         | 0.2168| 0.6195| 18.9314         | 0.1974| 0.6623| 19.1256         | 0.1930| 0.6739| 19.2202         | 0.1909| 0.6754|
| CompenNeSt++ w/ o refine| 19.3868        | 0.1934| 0.6372| 20.7373         | 0.1614| 0.7092| 21.0232         | 0.1561| 0.7246| 21.2691         | 0.1516| 0.7322|
| CompenNeSt++           | 19.9377         | 0.1775| 0.6764| 20.8597         | 0.1950| 0.7202| 21.2496         | 0.1518| 0.7393| 21.4868         | 0.1477| 0.7468|

TABLE 2: Quantitative comparison between CompenNeSt w/SL and CompenNeSt++. Results are averaged over $K = 2$ setups with specular highlight surfaces. CompenNeSt++ clearly performs better in this particular case.

| Model                  | #Train=48 PSNR↑ | RMSE↑ | SSIM↑ | #Train=125 PSNR↑ | RMSE↑ | SSIM↑ | #Train=250 PSNR↑ | RMSE↑ | SSIM↑ | #Train=500 PSNR↑ | RMSE↑ | SSIM↑ |
|------------------------|-----------------|-------|-------|-----------------|-------|-------|-----------------|-------|-------|-----------------|-------|-------|
| CompenNeSt w/SL        | 17.1685         | 0.2433| 0.5021| 18.1294         | 0.2173| 0.5569| 18.6915         | 0.2034| 0.5881| 19.9696         | 0.1960| 0.5966|
| CompenNeSt++           | 17.5909         | 0.2302| 0.5444| 18.5610         | 0.2054| 0.6092| 19.1894         | 0.1916| 0.6415| 19.4663         | 0.1851| 0.6459|

textured training images and testing images share a more similar distribution. (b) Although the original TPS method uses $5^3$ plain color images, each projector pixel’s R/G/B channel only has five different intensity levels, training the TPS model using these samples may lead to a suboptimal solution. While our colorful textured samples evenly cover the RGB space at each projector pixel, resulting in a more faithful sampling of the photometric compensation function.

To demonstrate the difficulty of full compensation problem, we compare with a deep learning-based image-to-image translation model Pix2pix [27] trained on the same SL-warped $\mathbf{x}_k$ as TPS textured w/ SL, we named it Pix2pix w/ SL. We train Pix2pix for 12,000 iterations to match the training time of our model. The results show that the proposed CompenNeSt++ outperforms Pix2pix w/ SL, demonstrating that the full compensation problem cannot be well solved by a general deep-learning based image-to-image translation model.

We then compare our method with our partial compensation model CompenNeSt and we train it with the same SL-warped training set $\mathbf{x}_k$ as TPS textured w/ SL and Pix2pix w/ SL, and name this two-step method CompenNeSt w/ SL. The quantitative and qualitative comparisons are shown in Tab. 1 and Fig. 7, respectively.

Tab. 1 clearly shows that CompenNeSt++ outperforms other two-step methods, except for CompenNeSt w/ SL. This indicates that even without an additional structured light step, the geometry correction can be learned directly from the photometric sampling images.

Note that SL may not work well on surfaces with specular highlight, e.g., as shown in Tab. 2 that CompenNeSt++ outperforms CompenNeSt w/ SL by a significant margin on two specular highlight setups extracted from the 20 full compensation setups in Tab. 1. This is because SL suffers from decoding error due to specular highlight and solving full compensation problem separately may lead to suboptimal solution, and thus the two steps should be solved jointly, as proposed by CompenNeSt++. Besides outperforming CompenNeSt w/ SL on specular highlight surfaces, CompenNeSt++ uses 42 fewer images than two-step SL-based methods.

We explain why two-step methods may find suboptimal solution in Fig. 7, where SL decoding errors affect the photometric compensation accuracy. In the 3rd row red zoomed-in patches and the 4th row blue zoomed-in patches, we see unfaithful compensations by the SL-based two-step methods (4th-7th columns), because SL suffers from decoding errors due to specular reflections and establishes false pixel mappings. Then, a second step of photometric compensation based on a false mapping is inevitably error prone. On the contrary, this issue is better addressed by the proposed end-to-end methods CompenNeSt++ pre (i.e., pre-trained and fine-tuned using only 8 sampling images) and CompenNeSt++ (last two columns), where global geometry and photometry information is considered in full compensation and gradients of the image reconstruction loss can be backpropagated to both modules. In summary, CompenNeSt++ not only brings improved performance than two-step SL-based methods, but also waives 42 extra SL projections/captures, and meanwhile being insensitive to specular highlights. Moreover, the pre-trained model CompenNeSt++ pre can work with only 8 sampling images, which further adds to the advantages of our method.

5. https://github.com/junyanz/pytorch-CycleGAN-and-Pix2pix

5.2 Ablation study

In this section, we conduct various ablation studies to show the effectiveness of our novel end-to-end problem formulation, network architecture and further analyze the mechanism of deep projector compensation.
Fig. 7: Qualitative comparison of TPS [15] w/ SL, TPS textured w/ SL, Pix2pix [27] w/ SL, our CompenNeSt w/ SL, our pre-trained CompenNeSt++ fine-tuned using only 8 sampling images, i.e., CompenNeSt++ pre and our CompenNeSt++ on two different surfaces. All models were trained using 500 sampling images (except for CompenNeSt++ pre). The 1st to 3rd columns are camera-captured projection surface, desired viewer-perceived image and camera-captured uncompensated projection, respectively. The rest columns are compensation results of different methods. Each image is provided with two zoomed-in patches for detailed comparison. See supplementary material for more results.

5.2.1 Network architecture exploration

Below we show how we explore the proposed CompenNeSt (the photometric part of CompenNeSt++) architecture and compare it with its degraded versions and our previous photometric compensation model CompenNet [20] on the photometric compensation benchmark to show the effectiveness of our network design. Then, we compare CompenNeSt++ with our previous full compensation model CompenNet++ [19] on the full compensation benchmark to show that by incorporating the improved CompenNeSt, CompenNeSt++ significantly outperforms CompenNet++ [19] (see Tab. 1).

Effectiveness of the siamese structure and improved layers. Compared with CompenNet [20], CompenNeSt has three major improvements: (1) a novel siamese structure (for the orange encoder part, CompenNet does not share weights); (2) symmetric skip connections and thus surface feature subtraction can be performed; (3) replacing the 2×2 filter of the first transposed convolutional layer to a 3×3 filter. To show the effectiveness of our new architecture, we compare with three respective degraded versions, i.e., the original CompenNet [20], CompenNeSt (2×2) and CompenNeSt (2×2, deg. skip) (deg. skip means using degraded CompenNet-like skip connections, the only difference between this model and CompenNet [20] is its siamese structure).

As the quantitative comparisons shown in Tab. 3, the proposed CompenNeSt outperforms all other degraded versions, demonstrating the effectiveness of the siamese structure, the feature subtraction operation and improved layers. Effectiveness of the surface image. To show the effectiveness of our learning-based formulation in Eq. 7 and that the surface image is a necessary model input, we compare the proposed CompenNeSt/CompenNeSt++ with their degraded versions that are without the input surface image and the corresponding encoder branch. We named them CompenNeSt w/o surf. in Tab. 3 and CompenNeSt++ w/o surf. in Tab. 1. Clearly, CompenNeSt and CompenNeSt++ outperform their degraded versions that are without the surface input on the photometric compensation and full compensation benchmark, respectively.

In particular, in Tab. 3 we can see clear improved
Fig. 8: Qualitative comparison of CompenNeSt++ trained with $\ell_1$ loss, $\ell_2$ loss, SSIM loss and $\ell_1$+SSIM loss. Clearly, $\ell_1$ and $\ell_2$ losses are unable to successfully compensate the surface patterns (see the dog head). $\ell_1$+SSIM and the SSIM losses produce similar results, but the cloud in the red zoomed-in patch of SSIM is grayer than $\ell_1$+SSIM and the ground truth.

TABLE 3: Quantitative comparison of the proposed CompenNeSt with CompenNet [20] and three degraded versions that are (1) without the surface image, (2) with CompenNet-like $2 \times 2$ transposed convolutional filters; and (3) additionally with CompenNet-like degraded skip convolutional layers. The models are compared on the photometric compensation dataset using 500 images and 1,000 iterations and the results are averaged over $K = 24$ setups.

| Model                | PSNR $\uparrow$ | RMSE $\downarrow$ | SSIM $\uparrow$ |
|----------------------|------------------|--------------------|------------------|
| CompenNet [20]       | 21.7998          | 0.1425             | 0.7523           |
| CompenNeSt w/o surf. | 20.6123          | 0.1633             | 0.7319           |
| CompenNeSt (2x2)     | 22.1100          | 0.1373             | 0.7698           |
| CompenNeSt (2x2, deg. skip) | 21.9101 | 0.1404             | 0.7595           |
| CompenNeSt            | 22.1292          | 0.1347             | 0.7753           |
| Uncompensated         | 12.1673          | 0.4342             | 0.4875           |

PSNR/RMSE/SSIM when $\tilde{s}$ is included in the model input, showing that our learning-based formulation has a clear advantage over the models that ignore the important information encoded in the surface image. Secondly, in Tab. 1 CompenNeSt++ w/o surf. outperforms TPS w/ SL and TPS textured w/ SL and Pix2pix w/ SL on PSNR/RMSE/SSIM even when $\tilde{s}$ is not included, showing the effectiveness of context-dependent formulation and the importance of the task-specific network design and the problem domain knowledge.

Effectiveness of the grid refinement network. To demonstrate the effectiveness of the sampling grid refinement network $W_{\theta_g}$ (Eq. 11 and Fig. 2), we created a degraded CompenNeSt++ by removing $W_{\theta_g}$, and name it CompenNeSt++ w/o refine. As reported in Tab. 1, CompenNeSt++ clearly outperforms this degraded model, showing the effectiveness of the grid refinement network $W_{\theta_g}$.

5.2.2 Comparison of different loss functions

Previous methods fit the composite compensation function by a pixel-wise $\ell_2$ loss and it is known to penalize large pixel errors while ignores the structural details [57], [64]. We investigated four different loss functions, i.e., pixel-wise $\ell_1$ loss, pixel-wise $\ell_2$ loss, SSIM loss, and $\ell_1$+SSIM loss. The qualitative and quantitative comparisons are shown in Fig. 8 and Tab. 4, respectively. In Fig. 8, compared with SSIM and $\ell_1$+SSIM losses, pixel-wise $\ell_1$ and $\ell_2$ losses cannot well compensate surface patterns, as shown by the dog head in the blue zoomed-in patches. Compared with $\ell_1$+SSIM loss, SSIM loss cannot well compensate the color as shown by the cloud in the red zoomed-in patches.

The quantitative comparisons in Tab. 4 are also consistent with the qualitative comparisons in Fig. 8. Note that SSIM loss alone obtains a worse PSNR/RMSE than $\ell_1$ and $\ell_2$ losses and a worse SSIM value than $\ell_1$+SSIM because it failed to converge on some setups with hard surface geometries and the output becomes plain gray. We further investigated the issue and found that compared with pixel-wise $\ell_1$ and $\ell_2$ losses, SSIM loss alone might encourage smooth plain gray patches. This problem also exists when we train with very few sampling images (see § 5.2.4). Thus, we use $\ell_1$+SSIM loss for CompenNeSt++ training.

Moreover, even when trained with pixel-wise $\ell_1$ loss, CompenNeSt++ outperforms TPS, TPS textured and Pix2pix on PSNR, RMSE and SSIM, this again shows a clear advantage of our task-targeting formulation and architecture.

5.2.3 Interpretation of CompenNeSt photometric compensation mechanism

To interpret the photometric compensation mechanism of CompenNeSt, we conduct two ablation studies.

First, we investigated the features carried by each of the three skip connections by enabling the surface/sampling image features and their corresponding skip connections one-by-one and plot the model output in Fig. 9.

Then, we show how the surface pattern was gradually compensated by sequentially subtracting the surface features...
Fig. 9: Visualization of CompenNeSt photometric compensation mechanism. **Left:** a trained CompenNeSt takes two warped images as input and we investigate the feature maps by enabling the input and the corresponding skip connections once at a time. **Right:** the top and the bottom rows show the network outputs when input the surface image or the sampling image, respectively, and each column shows the output when a specific skip connection and the corresponding layers are enabled. We use gray color to indicate disabled inputs, modules and connections. As shown in the first two columns, the feature maps of the first two layers carry low-level texture information and green/red components. In the 3rd column, we see that the feature maps of the fourth layer carry high-level global information and blue and yellow components.

from the sampling image features via the three skip connections. The network outputs are shown in Fig. 10 columns 4-7. Note that unlike Fig. 9 where the three skip connections are enabled one at a time, in Fig. 10, the three skip connections are gradually enabled, showing how the output (the 7th column) is gradually compensated by subtracting the three surface features.

### 5.2.4 Practicability of the pre-training method

As mentioned before (§ 3.5), projector compensation need to be quickly retrained when setup changes, however all existing methods must rerun the projection-capturing-compensation process from scratch, limiting practicability of projector-camera systems. Below we show our pre-trained CompenNeSt++ can achieve good quality even when only 8 sampling images are available.

We compare our default CompenNeSt++ trained from scratch with a CompenNeSt++ pre-trained on our Blender rendered synthetic dataset. Then we train/fine-tune and evaluate both models on the full compensation benchmark. To demonstrate that the pre-trained model improves performance with limited training pairs and training time, we trained both models for 800 iterations using only 8 samples and 800 iterations with a batch size of 8, and took about 3 minutes.

We compare our default CompenNeSt++ trained from scratch with a CompenNeSt++ pre-trained on our Blender rendered synthetic dataset. Then we train/fine-tune and evaluate both models on the full compensation benchmark. To demonstrate that the pre-trained model improves performance with limited training pairs and training time, we trained both models for 800 iterations using only 8 samples and 800 iterations with a batch size of 8, and took about 3 minutes.

Moreover, even with limited 8 training pairs and 800 iterations, the pre-trained CompenNeSt++ outperforms TPS [15], TPS textured and Pix2pix [27] trained with 250 images on PSNR/RMSE/SSIM in Tab. 1.

Furthermore, CompenNeSt++ has much fewer parameters (0.8M) than Pix2pix’s default generator (54M parameters). This further confirms that projector compensation is a complex problem and is different from general image-to-image translation tasks, and carefully designed models and domain knowledge are necessary.

### 6 Conclusions and Limitations

In this paper, for the first time, we reformulate the full projector compensation problem as a learning problem and propose an accurate and practical end-to-end solution named CompenNeSt++. In particular, CompenNeSt++ jointly learns geometric correction and photometric compensation without an additional structure light step, thus being end-to-end differentiable and waiving 42 extra SL images. The effectiveness of our formulation and architecture is verified by comprehensive experimental evaluations and ablation studies. Moreover, for the first time, we provide the community with two novel setup-independent evaluation benchmark datasets. Our method is evaluated carefully on the benchmarks, and the results show that our end-to-end learning solution outperforms state-of-the-arts both qualitatively and quantitatively by a significant margin. To make
Fig. 10: Output of CompenNeSt when sequentially enabling the three surface skip connections. We start with a trained CompenNeSt and an uncompensated camera-captured sampling image and disable all the skip connections between the surface branch and the backbone network (i.e., s1-s3 in Fig. 9). Then, we sequentially enabled s1 to s3 as shown in columns 4-7. Note that after we disabled a surface skip connection, we subtract its feature mean, e.g., CompenNeSt w/ m means that we disabled s1-s3 but subtracted their corresponding surface feature means from the backbone network. Compared with subtracting the actual feature map, subtracting feature mean only performs a global color and brightness adjustment (see the difference between the 3rd and the 4th columns). Then, when we enabled a surface skip connection, the feature variance/texture information can be better visualized. E.g., comparing the 4th with the 5th/6th columns, we see that s1 and s2 carry low-level surface texture features, subtracting them significantly removes the surface pattern. Comparing the 6th and the 7th columns, we see that s3 carries global color information.

our model more practical, we propose a synthetic dataset and a pre-training method, which allows our model to adapt to new setups with only 8 images and shorter training time, adding to the advantages over the prior works.

**Limitations.** We assume that each single patch of the projection surface can be illuminated by the projector. That said, CompenNeSt++ may not work well on complex surfaces with occlusions (Fig. 11). One potential solution is to use multiple projectors to cover each other’s blind spots. In fact, extending the end-to-end full compensation framework to multiple projectors is an interesting future direction.

**Fig. 11:** CompenNeSt++ is unable to compensate occluded regions such as the pillow fold as pointed by the red arrows.

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