Why Do Torus-unstable Solar Filaments Experience Failed Eruptions?

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Abstract

We study the magnetic field and 3D conﬁguration of 16 ﬁlament eruptions during 2010 July–2013 February in order to investigate the factors that control the success and/or failure of solar eruptions. All of these events, i.e., eruptions that failed to be ejected and become coronal mass ejections, have ﬁlament maximum heights exceeding 100 Mm. The magnetic ﬁeld of ﬁlament source regions is approximated by a potential ﬁeld extrapolation method. The ﬁlament 3D conﬁguration is reconstructed from three vantage points by the observations of Solar Terrestrial Relations Observatory Ahead/Behind and Solar Dynamics Observatory spacecraft. We calculate the decay index at the apex of these failed ﬁlaments and ﬁnd that in seven cases, their apex decay indexes exceed the theoretical threshold (n_{crit} = 1.5) of the torus instability (TI). We further determine the orientation change or rotation angle of each ﬁlament top during the eruption. Finally, the distribution of these events in the parameter space of rotation angle versus decay index is established. Four distinct regimes in the parameter space are empirically identiﬁed. We ﬁnd that all the torus-unstable cases (decay index n > 1.5) have large rotation angles ranging from 50° to 130°. The possible mechanisms leading to the rotation and failed eruption are discussed. These results imply that, in addition to the TI, the rotation motion during the eruption may also play a signiﬁcant role in solar eruptions.

Key words: instabilities – Sun: corona – Sun: coronal mass eruptions (CMEs) – Sun: ﬁlaments, prominences

Supporting material: animation

1. Introduction

Coronal mass eruptions (CMEs) are spectacular bursts of plasma and magnetic ﬁeld in the Sun’s corona. They are frequently associated with solar ﬂares. CMEs and ﬂares are considered to be two observational aspects of the same physical process in a solar eruption (Harrison 1996; Zhang et al. 2001, 2004; Priest & Forbes 2002).

Magnetic ﬂux ropes (MFRs), a set of coiled magnetic ﬁeld lines winding more than once around a common axis, are believed to be the fundamental structure of CMEs. Coronagraph images of CMEs and in situ measurements of magnetic ﬁeld validate the fact that the MFR conﬁguration of CMEs exists after the solar eruption (Burlaga et al. 1981; Vourlidas et al. 2013). However, whether an MFR is present in the corona prior to an eruption or is formed during the eruption process is still a subject of debate. Some observational features may contain hints related to the MFRs, including ﬁlaments, sigmoidal, and hot channels (Kuperus & Raadu 1974; Rust & Kumar 1994; McKenzie & Canﬁeld 2008; Zhang et al. 2012; Cheng et al. 2013). These features may be different manifestations of MFRs, depending on different observational selection effects (e.g., sensitive to different temperatures), perspectives, as well as magnetic environments (Cheng et al. 2017). Filaments are made of cold and dense plasma suspended in the magnetic dips of an MFR conﬁguration (Guo et al. 2010; Mackay et al. 2010). Filaments are therefore a good tracer of MFRs in the corona (Schmieder et al. 2013; Zhou et al. 2017).

However, MFR eruptions are not always associated with CMEs. For a so-called “failed” ﬁlament eruption, a strong deceleration appears in the wake of the initially eruptive-like acceleration. The eruptive ﬁlament reaches a maximum height as the mass in the ﬁlament threads drains back toward the Sun (Ji et al. 2003), and there is no propagating CME in the white-light coronagraph images. Popular belief attributes such failure to the criteria for the torus instability (TI, in general terms: a sufﬁciently steep decrease of the overlying ﬁeld in height) is not met at or above the eruption site (e.g., Török & Kliem 2005; Kliem & Török 2006; Liu 2008; Liu et al. 2012; Song et al. 2014). The critical value is generally suggested to be typically in a range of 1.1–1.5 (e.g., Kliem & Török 2006; Démoulin & Aulanier 2010; Olmedo & Zhang 2010; Zuccarello et al. 2015). Some ﬁlament eruptions exhibit a strong rotation motion about its ascending direction and display a characteristic “inverse γ” shape, which is referred to as the Kink instability (e.g., Hood & Priest 1979; Török & Kliem 2005). However, kink instability is not an effective mechanism for full solar eruptions. It often needs to cooperate with a TI (e.g., Kliem & Török 2006; Liu 2008; Schmieder et al. 2013; Vemareddy & Zhang 2014).
Recently, an experimental result has demonstrated that torus-driven eruptions can fail under a weak kink onset condition (Myers et al. 2015). Using solar observations, Jing et al. (2018) pointed out that the TI onset criteria is not a necessary condition for CMEs, some TI-stable MFRs can manage to break through the strong “strapping” field and evolve into CMEs. The eruption is additionally influenced by other factors, such as the $T_\alpha$ (twist number in the MFRs; Myers et al. 2015; Liu et al. 2016), $\Delta \varphi$ (the change of orientation of the polarity inversion line (PIL) as a function of height; Baumgartner et al. 2018). Meanwhile, with a strong writhe, the erupting MFR may experience a dissolution by magnetic reconnection with the overlying flux, resulting in a failed eruption (Hassanin & Kliem 2016). Anyway, most of the previous observational studies of failed eruptions could not reveal the exact mechanism associated with it.

Uncovering what prevents an evolving eruption from becoming ejective surely improves our understanding of the requirements for a solar eruption. Using the 3D reconstruction by exploiting observations of multiple views and the potential field source surface (PFSS) model (Schrijver & De Rosa 2003), we have investigated 16 failed filament eruptions. We find out that the writhe of failed filament eruption varies significantly from event to event, and the amount of writhe depends on the decay index of strapping magnetic field. In Section 2, we describe our event sample as well as the data and methods used. The details of the analysis are described in Section 2, and the obtained results and discussions are presented in Section 3.

### 2. Observation and Analysis

#### 2.1. Instruments

The twin Solar TERrestrial RELations Observatory (STEREO) A (Ahead), B (Behind) and Solar Dynamics Observatory (SDO) provide us with an unprecedented opportunity to observe filaments in a multiview setting. The Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) on board SDO can observe a filament in narrow extreme-UV (EUV) passbands including 304 Å (formation temperature $T_f = 10^5$ K) and 193 Å ($T_f = 1.58 \times 10^5$ K) with a high cadence (12 s), high spatial resolution (0.64 pixel per pixel), and large field of view (FOV; 1.3R$_\odot$). Meanwhile, the Extreme Ultraviolet Imager (EUVI) on board STEREO provides another view of the filament at similar wavelengths, i.e., 304 Å (from FOV of 1.7R$_\odot$) and 195 Å ($T_f = 1.4 \times 10^6$ K) with an FOV of 1.7R$_\odot$ (Howard et al. 2008). For a failed filament eruption, evolutions of height and velocity have exactly the same trend as the hot-channel prior to it ceasing to rise (Cheng et al. 2014). Utilizing these multiview observations, we apply 3D reconstruction to obtain the 3D configuration and evolution of filaments of study. The Helioseismic and Magnetic Imager (HMI; Schou et al. 2012), also on board SDO, provides photospheric vector magnetic field data with a cadence up to 45 s and a pixel size of 0.64. We have employed three different coronagraphs, Solar and Heliospheric Observatory (SOHO)/Large Angle and Spectrometric Coronagraph (LASCO)-C2 (Brueckner et al. 1995) and STEREO/Sun Earth Connection Coronal and Heliospheric Investigation (SECCHI)-COR1 A and B (Howard et al. 2008), to determine whether a filament eruption results in CME or not, i.e., a successful eruption or a failed eruption.

#### 2.2. Selection of Events

Sixteen failed filament eruptions are selected in this study (Table 1) according to the following criteria (e.g., Figure 1): (1) It is a failed filament eruption, i.e., no corresponding CME is captured in LASCO/C2 or SECCHI/COR1 (Figure 1(b)). (2) The source region of the filament should be located on the solar disk in the view of SDO/AIA to allow for the coronal magnetic field extrapolation, as well as in the limb view of STEREO/
EUVI as is necessary for 3D reconstructions (e.g., Figures 1(c), (d)). (3) The terminal height of the filament can be exactly determined. In this study, we only consider the cases in which the maximum height exceeds 100 Mm. An erupting filament that stops at a lower altitude is inclined to be torus-stable in its later evolution due to the "relatively high probability" of a small decay index at the lower heights. Since the purpose of this study is to examine the nature of failure of torus-unstable events, the choice of high heights makes our selection of event unambiguous.

Based on these criteria, we examine SDO/AIA and STEREO/EUVI data to search for suitable filament eruption events from 2010 July to 2013 February, during which the near-quadrature configuration of STEREO A/B allows for the best 3D view of a solar eruption (see Figure 1(a)). We have successfully identified 16 such events, which are listed in Table 1. Through browsing the evolution of these 16 filament eruptions, we find out part of these cases show a strong rotation motion, hence we focus on the relationship between the rotation motion and filament eruption.

Figure 1. The selection criteria of failed filaments. Panel (a) displays the paths of the STEREO-A (red arc) and B (blue arc) and position of SDO (green dot) in the ecliptic plane during the period from 2010 July 22 to 2013 February 07. The blue and red circles indicate the positions of STEREO-A/B on 2012 May 5 when a failed filament eruption occurred. The black dot on the Sun marks the filament source region, which appears on the solar disk when viewed from SDO, on the limb from STEREO-B, and on the backside of the Sun from STEREO-A. Panel (b) shows no obvious CME signal in STEREO-B COR1 and EUVI 304 and 195 Å composite image acquired during the filament eruption. Panels (c) and (d) provide observations of the prominence morphology during the eruption from the limb view in STEREO-A EUVI 304 Å and the disk view in SDO/AIA 304 Å, respectively. An animation of the two views of the eruption process in the 304 Å passband is available online. The animation runs from ∼17:00 UT to 18:26 UT. (An animation of this figure is available.)
2.3. Decay Index and Rotation Angle

For the 16 selected events, we create a parameter space that characterizes the TI and the writhing morphological change. The critical parameter for the TI is the decay index \( n = -d \ln B_{\text{ex}} / d \ln h \), where \( B_{\text{ex}} \) is the horizontal component of external field perpendicular to the radial component \( B_r \) in spherical coordinates. Here we employ the PFSS model to calculate the coronal magnetic field based on the synoptic map of the photospheric radial field. It should be noted that only the transverse component of the extrapolated potential field is used, because the radial component does not contribute to the downward confinement onto the erupting MFRs. The final decay index is an average value along the main PIL. We use the 2012 May 5 event (No. 9 in Table 1) as an example to demonstrate how the decay index at its maximum height is calculated.

![Fig 2](image)

**Figure 2.** Calculation of the decay index at the maximum height of the failed erupted filament. The white plus symbols in panels (a) and (b) depict the prominence spine. The green triangle symbol denotes the same point viewed in two different angles (from SDO and STEREO-B). Panel (c) shows the line-of-sight magnetic field in the source region of the filament, and black asterisks mark out the projected location of the filament before the eruption. A cyan line denotes the PIL near this filament. In panel (d), the decay index \( n \) as a function of the height \( h \) above the surface in units of Mm. The vertical and horizontal lines indicate the maximum height and the corresponding decay index.

The final decay index is an average value along the main PIL. We use the 2012 May 5 event (No. 9 in Table 1) as an example to demonstrate how the decay index at its maximum height is calculated. Figures 2(a) and (b) show the erupted filament stopping at a certain height in SDO and STEREO-B view angles. We reconstruct the 3D coordinates of several selected points along the erupted filament axis using scc_measure.pro routine, which is available in SolarSoftWare (Freeland & Handy 2012). The maximum height of the filament is thus determined to a good degree. We sample the segment of the PIL directly underneath the filament by clicking on the segment as uniformly as possible to get sufficient representative points (marked by cyan line in Figure 2(c)), and then calculate the decay index \( n \) at different heights for each selected point. In Figure 2(d), we plot \( n \) as a function of \( h \), which is averaged over all selected points, with the error bar indicating the standard deviation. The filament final decay index corresponding to the maximum height can be found through interpolation of these discrete \( n(h) \) nodal values, the uncertainty of the final decay index can also be estimated by interpolation.

For this case, we obtain that the decay index at maximum height \( n_{\text{max}h} = 2.20 \pm 0.09 \). Note that the threshold value of TI is believed to be 1.5 for a toroidal current channel (Kliem & Török 2006). Thus, this derived \( n_{\text{max}h} \) is significantly larger than the theoretical critical value. In the meantime, \( n \) increases monotonically as the height increases, so there is no local torus-stable confinement (Wang et al. 2017). Obviously, this filament eruption is in the torus-unstable state but failed.

Here, we look into the writhing morphological change during the eruption of these events. The writh is proportional to the difference in angle between the tangent vector at the top and the line connecting the footpoints (Török et al. 2010). To evaluate the writh during the eruption, we calculate the rotation angle \( \varphi \) from the reconstructed filament. The same case is employed as the example. We project the erupted filament
onto the solar disk from the top view (See Figure 3(a)). Here we use the line connecting the elbows as the proxy of the tangent vector at the top. Four points (white asterisks in Figures 3(a)–(b)) selected near the two elbows are used for fitting. The projected filament top is represented by a fitted regression line. \( \varphi \) is then given as the difference in angle between the fitted regression line and the line connecting the footpoints. The image sequence (Figure 1(d)) also shows that the rotation is clockwise (CW; viewed from above) for this filament eruption. For this case, we calculated the rotation angle and its corresponding error (\( \varphi = 130^\circ \pm 1^\circ.6 \)). Its error originates from the uncertainty of the elbow’s location.

3. Results and Discussion

Figure 4 shows the scatter diagram of TI parameters \( n \) versus rotation angle \( \varphi \) (with estimated uncertainties) for the 16 failed filament eruptions. The failed events with decay index \( n \) less than 1.5 (9 out of 16 cases) may be consistent with the present understanding of the TI. In the TI model, an erupting filament cannot evolve into a CME when its decay index has not achieved the theoretical expectation (\( n \geq n_{\text{crit}} = 1.5 \)) (Kliem & Török 2006). However, exceptions to this theory do exist. The decay indexes of the other seven cases (red color events in Figure 4) exceed more than 1.5, but they do not result into CMEs. This result argues against this conception that the TI is a sufficient condition for a full eruption. Here we call these exceptions torus-unstable failed eruptions. Interestingly, all these torus-unstable events show a strong rotation during the eruptions. Their rotation angles (\( \varphi \)) exceed 40\(^\circ\) with an average value of 89\(^\circ\). The critical rotation angle, \( \varphi \sim 40^\circ \), discriminates best between those torus-stable and torus-unstable failed filament eruptions. There is not a single case located in the region of the large decay index (\( n \geq 1.5 \)) and small rotation angle (\( \varphi \leq 40^\circ \)) regime. Thus four distinct regimes can be empirically identified in the parameter space as shown in Figure 4.

Apparently, the rotation motion of a filament has a certain correlation with the failed eruption. Previous models concerning the writhing of MFRs have opposite effects for an eruption: On one hand, the writhing of the MFR’s upper part into the orientation of the overlying arcade is energetically favorable for passing through the overlying arcade to become a CME (Sturrock et al. 2001; Fan 2005). On the other hand, the helical deformation facilitates interchange reconnection between filament flux and ambient flux (Hassanin & Kliem 2016) and/or reconnection between the legs of the rope (Alexander et al. 2006; Liu & Alexander 2009; Kliem et al. 2010), such reconnection progressively decrease the flux content of the rope, up to its full destruction. This interaction is signified by the brightenings and nonthermal sources near the body or the crossing point of the filament (Karlický & Kliem 2010; Cheng et al. 2018). When only considering the torus-unstable failed eruptions, the reconnection caused by the MFR writhing seems
dominant, an intense brightening in the body of the filament supports this possibility (see the brightening pointed by green arrow in 17:36 UT of Figure 1(c)). The simulation of Török et al. (2010) pointed out that confined MFR eruptions tend to show stronger writhing at low heights than ejective eruptions (CMEs). Hassanin & Kliem (2016) further inferred that if an eruption is halted, then the magnetic tension of the erupting flux can no longer be relaxed by expansion but only by further writhing, resulting in a tendency for confined eruptions to develop a strong writhing.

In summary, 16 failed filament eruptions are studied with both the AIA on board the SDO and EUVI on board STEREO. Their decay indexes are obtained from the PFSS model and rotation angle are calculated with the help of the 3D reconstruction. Thus we establish the scatter diagram of TI parameters $n$ versus rotation angle $\varphi$. Seven cases are theoretically in the torus-unstable state. Meanwhile, they all show strong writhing motions during the eruptions with rotation angle $>40^\circ$. It seems that writhing and failed eruption show a complex coupling relationship. The possible reconnection due to the filament rotational motion may ruin the architecture of the MFR, resulting in a failed eruption. Simultaneously, this confinement induces a strong rotation instead of a further expansion. More detailed observational analysis, theoretical considerations, and numerical simulations are necessary toward a comprehensive understanding of the MFR eruption.

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References

Ahrens, J., Geveci, B., & Law, C. 2005, in The Visualization Handbook, ed. C. D. Hansen & C. R. Johnson (Cambridge, MA: Academic Press), 717
Alexander, D., Liu, R., & Gilbert, H. R. 2006, ApJ, 653, 719
Ayachit, U. 2015, The ParaView Guide: A Parallel Visualization Application (Clifton Park, NY: Kitware)
Baumgartner, C., Thalmann, J. K., & Veronig, A. M. 2018, ApJ, 853, 105
Brueckner, G. E., Howard, R. A., Koomen, M. J., et al. 1995, SoPh, 162, 357
Burlaga, L., Sittler, E., Mariani, F., & Schwenn, R. 1981, JGR, 86, 6673
Cheng, X., Zhang, J., Ding, M. D., Liu, Y., & Poomvises, W. 2013, ApJ, 763, 43
Cheng, X., Ding, M. D., Zhang, J., et al. 2014, ApJL, 789, L35
Cheng, X., Guo, Y., & Ding, M. 2017, ScChE, 60, 1383
Cheng, X., Kliem, B., & Ding, M. D. 2018, ApJ, 856, 48
Démoulin, P., & Aulanier, G. 2010, ApJ, 718, 1388
Fan, Y. 2005, ApJ, 630, 543
Freeland, S. L., & Handy, B. N. 2012, SolarSoft: Programming and data analysis environment for solar physics, Astrophysics Source Code Library, ascl:1208.013
Guo, Y., Schmieder, B., Démoulin, P., et al. 2010, ApJ, 714, 343
Harrison, R. A. 1996, SoPh, 166, 441
Hassanin, A., & Kliem, B. 2016, ApJ, 832, 106
Hood, A. W., & Priest, E. R. 1979, SoPh, 64, 303
Howard, R. A., Moses, J. D., Vourlidas, A., et al. 2008, SSRv, 136, 67
Ji, H., Wang, H., Schmahl, E. J., Moon, Y.-J., & Jiang, Y. 2003, ApJL, 595, L135
Jing, J., Liu, C., Lee, J., et al. 2018, ApJ, 864, 138
Klimchý, M., & Kliem, B. 2010, SoPh, 266, 71
Klim, B., Linton, M. G., Török, T., & Karlický, M. 2010, SoPh, 266, 91
Klim, B., & Török, T. 2006, PhRvL, 96, 255002
Kuperus, M., & Raadu, M. A. 1974, A&A, 31, 189
Lemen, J. R., Title, A. M., Akin, D. J., et al. 2012, SoPh, 275, 17
Liu, R., & Alexander, D. 2009, ApJ, 697, 999
Liu, K., Wang, Y., Shen, C., & Wang, S. 2012, ApJ, 744, 168
Liu, R., Kliem, B., Titov, V. S., et al. 2016, ApJ, 818, 148
Liu, Y. 2008, ApJL, 679, L151
Mackay, D. H., Karpen, J. T., Ballester, J. L., Schmieder, B., & Aulanier, G. 2010, SSRv, 151, 333
McKenzie, D. E., & Canfield, R. C. 2008, A&A, 481, L65
Myers, C. E., Yamada, M., Ji, H., et al. 2015, Natur, 528, 526
Olmedo, O., & Zhang, J. 2010, ApJ, 718, 433
Priest, E. R., & Forbes, T. G. 2002, A&ARv, 10, 313
Rust, D. M., & Kumar, A. 1994, SoPh, 155, 69
Schou, J., Scherrer, P. H., Bush, R. L., et al. 2012, SoPh, 275, 229
Schmieder, B., Démoulin, P., & Aulanier, G. 2013, AdSpR, 51, 967
Schrijver, C. J., & de Rosa, M. L. 2003, SoPh, 212, 165
Song, H. Q., Zhang, J., Cheng, X., et al. 2014, ApJ, 784, 48
Sturrock, P. A., Weber, M., Wheatland, M. S., & Wolfson, R. 2001, ApJ, 548, 492
Török, T., Berger, M. A., & Klim, B. 2010, A&A, 516, A49
Török, T., & Kliem, B. 2005, ApJL, 630, L97
Venem HY, & Zhang, J. 2014, ApJ, 797, 80
Vourlidas, A., Lynch, B. J., Howard, R. A., & Li, Y. 2013, SoPh, 284, 179
Wang, D., Liu, R., Wang, Y., et al. 2017, ApJL, 843, L9
Zhang, J., Cheng, X., & Ding, M.-D. 2012, NatCo, 3, 747
Zhang, J., Dere, K. P., Howard, R. A., Kundu, M. R., & White, S. M. 2001, ApJ, 559, 452
Zhang, J., Dere, K. P., Howard, R. A., & Vourlidas, A. 2004, ApJ, 604, 420
Zhou, Z., Zhang, J., Wang, Y., Liu, Y., & Chintzoglou, G. 2017, ApJ, 851, 133
Zuccarello, F. P., Aulanier, G., & Gilchrist, S. A. 2015, ApJ, 814, 126