Pressure Transient Analysis for Finite Conductivity Multi-staged Fractured Horizontal Well in Fractured-Vuggy Carbonate Reservoirs

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Abstract: Transient pressure analysis has been considered as a robust method to identify the flow behaviors, estimate reservoir parameters and hydraulic fracturing parameters. Compared with conventional clastic reservoirs, complex pore systems in fractured–vuggy carbonate reservoirs are posing significant research challenges. Although pressure transient analysis (PTA) models for different style wells in carbonate reservoirs have been widely studied, limited study has been conducted for multi-fractured horizontal well (MFHW) in these reservoirs. Thus, this paper is an investigation on PTA for MFHW of fractured-vuggy carbonate reservoirs. Based on source function theory, mirrors reflection and superposition principle, the finite conductive MFHW’s bottom-hole pressure solution for fractured-vuggy carbonate reservoirs is obtained by the Laplace transform and the Stehfest inversion method. Log-log type curves are drawn by numerical algorithms and eight flow regimes are identified. Finally the influences of sensitivity parameters such as fracture number, fracture spacing, half length of fracture, storativity ratio, inter-porosity flow coefficient on unsteady flow behaviors of MFHW are discussed in depth.

Keywords: Fractured-Vuggy Carbonate Reservoir, Multi-fractured Horizontal Well, Finite Conductive, Transient Pressure

1. Introduction

Compared with conventional clastic reservoirs, fractured-vuggy carbonate reservoirs are composed of matrix, fractures, vugs systems. Among these systems, the properties of porosity, permeability and fluid transport behaviors are quite different, which brings a big challenge to study the fluids flow and transport behaviors in these reservoirs [1], [2], [3]. In recent decades, many scholars have made some efforts to study the fluids flow and transport behaviors in fractured–vuggy reservoirs. G. Fuentes-Cruz et al. [4] studied the transient pressure and production decline curve behaviors for partially penetrating wells completed in fractured-vuggy reservoirs. Camacho-Velázquez et al. [5] proposed an unsteady flow analysis model for carbonate reservoirs, and analyzed the transient pressure and production decline curves. Subsequently, the transient pressure of fractured well in fractured-vuggy reservoirs is investigated by Cai and Jia [6]. Cheng et al. [7] used triple media model to establish the well testing model for multi-branch horizontal wells. And the numerical well testing method for carbonate reservoirs is studied by Corbett et al. [8]. However this method is limited for isolated cave. Gulbransen et al. [9] proposed a multi-scale mixed finite element method for modeling of vuggy and naturally fractured reservoirs. Wu et al. [10], [11], [12] proposed a triple-continuum model to describe flow in fractured rock & naturally fractured vuggy reservoirs. Ren et al. [13] proposed a well testing model of inclined well for fractured-vuggy carbonate reservoirs. Jia et al. [14] developed a flowing model of well test analysis for porous-vuggy carbonate reservoirs. After that, a analytical model for wormholes in fractured–vuggy carbonate reservoirs is developed by Wang et al. [15].
element method for modeling of fractured-vuggy reservoirs with large-scale caves and obtained the PTA type curves. Guo et al. [17] and Nie et al. [18] investigated the flow behavior for modeling horizontal well production in fractured-vuggy carbonate reservoirs. However, these aforementioned models were mainly developed for vertical wells, fractured wells and horizontal wells.

According to above mentioned models in fractured-vuggy carbonate reservoirs, two main models are used to describe and study the flow process in fractured-vuggy carbonate reservoirs: (1) triple porosity and single permeability model [15], [19]. The model considers the vug system as a continuum medium, treats fracture system as pathways directly connected to the wellbore, and considers the matrix and vug systems connect to the fracture system. And the inter-porosity flows are considered from the matrix and vug systems to the fracture system; (2) triple porosity and dual permeability model [20]. This model also considers the vug system as a continuum medium, treats fracture system and vug system as pathways directly connected to the wellbore and considers the inter-porosity flows to occur between matrix, fracture and vug systems.

Although series of progress on PTA in fractured-vuggy carbonate reservoirs have been made by using the two models, little study on MFHW of PTA has been conducted in fractured-vuggy carbonate reservoirs. Fortunately, many studies on pressure behaviors of MFHW in clastic and unconventional reservoirs have been performed in recent 20 years [21], [22], [23], [24], [25], [26], [27], which can guide to study PTA of MFHW in fractured-vuggy carbonate reservoirs.

To extend the PTA theory into MFHW in fractured-vuggy carbonate reservoirs, a triple porosity and single permeability model is used in this paper to investigate the transient pressure behavior of finite conductive MFHW. Based on Source function theory, mirrors reflection and superposition principle, the finite conductive MFHW’s bottom-hole pressure solution is obtained by Laplace transform and Stehfest inversion methods. Type curves are drawn by numerical simulations and eight flow regimes are identified. Finally the sensitivity parameters were discussed in depth.

2. Physical Model

Generally speaking, fractured-vuggy carbonate reservoir consists of matrix, fractures and vuggy (Fig. 1). Fluids in the reservoir would flow into wellbore under the pressure drop between wellbore and reservoir pressures, and the triple porosity and sequential single permeability of MFHW flow scheme is shown in Fig. 3.

3. Mathematical Model and Solution

3.1. Mathematical Model

According to the physical model assumptions, the flow equation in porous fractured-vuggy carbonate reservoirs is established as follows:

The reservoir governing equation is:
The formula of interporosity flow from vugsto NFs is:

$$\nabla \cdot \left( \frac{k_{nf}}{\mu} \nabla \Delta p_{nf} \right) + \alpha_{nf} \frac{k_{nf}}{\mu} (\Delta p_{nf} - \Delta p_{nf}^{o}) = \left( V \phi C_{nf} \right)_{nf} \frac{\partial \Delta p_{nf}}{\partial t} \quad (1)$$

The inter flow equation from matrix to vugs is:

$$\left( V \phi C_{m} \right)_{m} \frac{\partial \Delta p_{m}}{\partial t} = -a_{m} \frac{k_{m}}{\mu} (\Delta p_{m} - \Delta p_{v}) \quad (2)$$

Taking the Laplace transform of Eqs.(1)~(3), Eqs.(4)~(6) can be obtained, respectively:

$$\nabla^{2} \Delta \bar{p}_{nf} + \bar{\lambda}_{v} \left( \Delta \bar{p}_{v} - \Delta \bar{p}_{nf} \right) = S_{nf} \Delta \bar{p}_{nf} \quad (4)$$

$$S_{nf} \Delta \bar{p}_{nf} = -\lambda_{n} (\Delta \bar{p}_{m} - \Delta \bar{p}_{nf}) + \lambda_{n} (\Delta \bar{p}_{nf} - \Delta \bar{p}_{v}) \quad (5)$$

$$S_{nf} \Delta \bar{p}_{nf} = -\lambda_{m} (\Delta \bar{p}_{m} - \Delta \bar{p}_{v}) \quad (6)$$

Combining Eqs.(5) ~ (6) and the following dimensionless definitions, Eq. (4) can be written as:

$$\nabla^{2} \bar{p}_{nf} + \bar{u} \bar{\lambda}_{v} (\bar{p}_{v} - \bar{p}_{nf}) = S_{nf} \bar{p}_{nf} \quad (7)$$

In Eq.(7), the expression of $u$ is:

$$u = \bar{\lambda}_{v} + S_{nf} \bar{\lambda}_{m} - \frac{\bar{\lambda}_{v}^{2}}{S_{nf} \bar{\lambda}_{m} + \bar{\lambda}_{v}} \quad (8)$$

All the Dimensionless definitions in the paper are as below:

**Dimensionless distance:**

$$r_{D} = \frac{r}{L}, \quad x_{D} = \frac{x}{L}, \quad y_{D} = \frac{y}{L}, \quad z_{D} = \frac{z}{L}, \quad x_{AD} = \frac{x_{A}}{L}, \quad y_{AD} = \frac{y_{A}}{L}$$

**Dimensionless wellbore storage coefficient:** Dimensionless time:

$$C_{D} = \frac{C}{2\pi \mu \phi_{nf} \rho_{nf}}, \quad t_{D} = \frac{3.6k_{vf}t}{(\phi_{nf} C_{nf})_{nf} L^{2}}$$

**Dimensionless pressure:**

$$p_{D} = \frac{k_{vf} \mu_{nf} h}{1.842 \times 10^{4} \mu_{nf} B} (p_{i} - p_{f}), \quad j = m, n, v, Nf$$

The parameters in Eq. (8) are defined as follows:

**Vug storage capacity ratio:**

$$\omega_{v} = \frac{(V \phi C_{v})_{nf} + (V \phi C_{v})_{m} + (V \phi C_{v})_{f}}{(V \phi C_{vf})_{nf}}$$

**Interporosity flow coefficient from vugs to NFs:**

$$\lambda_{v} = \frac{\omega_{v} k_{vf}}{k_{vf}} L^{2}$$

**Matrix storage capacity ratio:**

$$\omega_{m} = \frac{(V \phi C_{m})_{nf} + (V \phi C_{m})_{v} + (V \phi C_{m})_{f}}{(V \phi C_{mf})_{nf}}$$

**Interporosity flow coefficient from matrix to vugs:**

$$\lambda_{m} = \frac{\omega_{m} k_{mf}}{k_{mf}} L^{2}$$

Based on Eqs.(7) and (8), the flow equation is established by utilizing the point source function and boundary conditions:

$$\begin{bmatrix} \frac{1}{r_{D}^{2}} \frac{d}{dr_{D}} \left( r_{D}^{2} \frac{d\Delta \bar{p}_{nf}}{dr_{D}} \right) - u \bar{p}_{nf} = 0 \\ \Delta \bar{p}_{nf}(r_{D} \to \infty) = 0 \\ \lim_{r_{D} \to 0} 4\pi L^{2} \left( r_{D}^{2} \frac{d\Delta \bar{p}_{nf}}{dr_{D}} \right) = -1 \end{bmatrix} \quad (9)$$

Furthermore, based on Eq. (9), the continuous point source solution[28], [29] of closed top and bottom borders of reservoirs can be obtained by the mirrors reflection and the superposition principle:

$$\bar{p}_{nf} = \frac{4\pi \mu}{2\pi \rho_{nf} h_{nf}} \sum_{n=1}^{\infty} \left( \frac{r_{D}}{r_{D}^{2}} \frac{d\Delta \bar{p}_{nf}}{dr_{D}} \right) \left( \bar{u} \bar{\lambda}_{v} - \bar{\lambda}_{m} \bar{\lambda}_{n} \right) + \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} K_{m,n} \left( \bar{u} \bar{\lambda}_{m} - \bar{\lambda}_{v} \bar{\lambda}_{n} \right) \cos \frac{m\pi x_{AD}}{L} \cos \frac{n\pi y_{AD}}{L}$$

$$\lim_{r_{D} \to 0} 4\pi L^{2} \left( r_{D}^{2} \frac{d\Delta \bar{p}_{nf}}{dr_{D}} \right) = -1 \quad (10)$$

### 3.2. Solution of the Model

The pressure transient solution for MFHW in naturally fractured-vuggy reservoirs is obtained by discretizing fractures (Fig.3) and the use of source function method.
\[ P_D(x_D, y_D, s) = \frac{1}{2C_{f,D}} \int_{\alpha_{in}}^{\alpha_{out}} q_D(\alpha) \cdot K_c(\sqrt{u_0} (x_D - \alpha) + \frac{y_D^2}{\alpha}) \, d\alpha \quad (11) \]

In Eq.(11), \( q_D \) is the Laplace transform of \( q_d(x_D, t_D) \). By writing Eq.(11) for midpoints for all discrete segments, we can get \( m \times n \) equations with \( (m \times n + 1) \) unknowns which are \( P_D(x_D, y_D, s) \) and \( q_{D,i}(u) \). To obtain the pressure responses, one more equation can be written by assuming the flow rate is constant:

\[ \sum_{i=1}^{n} \sum_{j=1}^{s} (x_{D,i+1} - x_{D,i}) \tilde{q}_D(\alpha) \, d\alpha = \frac{1}{s} \quad (12) \]

Considering the skin effect of the fracture wall, the relationship between fracture pressure \( \tilde{P}_D \) and formation pressure \( P_D \) can be written as:

\[ \tilde{P}_{D|D} = P_D \bigg|_{y_D=0} + \tilde{q}_D \cdot S_f \quad (13) \]

Since many proppants will still exist after the well fracturing, which leads to flow resistance in the hydraulic fractures, several previous transient pressure analysis of MFHW assuming infinite conductivity of fractures is not realistic[26]. Thus, the finite conductive fractures of MFHW in carbonate reservoirs is considered.

The flow equations [30] of finite conductive hydraulic fracture ignoring the liquid compressibility can be written:

\[ \frac{\partial^2}{\partial x_D^2} P_{Nd} + \frac{2}{C_{f,D}} \frac{\partial}{\partial y_D} \left. P_{Nd} \right|_{y_D=0} = 0 \quad 0 < x_D < L_{f,D} \quad (14) \]

The boundary conditions are given as follows:

\[ \tilde{q}_D(x_D) = -\frac{2}{\pi} \tilde{P}_{Nd, D} \bigg|_{y_D=0} \quad (15) \]

\[ \frac{\partial \tilde{P}_{Nd}}{\partial x_D} \bigg|_{x_D=0} = -\frac{\pi}{sC_{f,D}} \quad (16) \]

In Eq.(16), the dimensionless conductive coefficient is \( C_{f,D} = (k_D)W_D/(kL) \), \( k_D \) is the fracture permeability, \( W_D \) is the fracture width. Combined with boundary conditions of Eqs.(15)~(16), Eq.(14) can be obtained after integrating.

The flow equations [30] of finite conductive hydraulic fracture ignoring the liquid compressibility can be written:

\[ \tilde{P}_{D,n} - \tilde{P}_{D|D}(x_D) = \pi \frac{S_D}{\alpha_C f_D} \int_{x_D}^{x_D} x_D - \frac{2s}{\pi} \int_{0}^{s} \tilde{q}_D(x') \, dx' \quad (17) \]

Eq. (17) can be rewritten based on Eqs. (11) and (13):

\[ \tilde{P}_{D,n} = \frac{1}{2} \sum_{i=1}^{n} \tilde{q}_D(x') (K_n(x_i - x') \sqrt{u}) + K_n(x_i + x' \sqrt{u}) \, dx' \quad (18) \]

In order to get approximate expansion of Eq.(17), a fracture wing is divided into \( n \) segments by discrete fracture mechanism (see Fig3). Assuming the flow rate of each segment is uniform distributed, Eq.(18) can be expanded by discrete approximate method[30].

\[ \tilde{P}_{D,n} = \frac{1}{2} \sum_{i=1}^{n} \tilde{q}_D(x') (K_n(x_i - x') \sqrt{u}) + K_n(x_i + x' \sqrt{u}) \, dx' \quad (19) \]

Thus the \( n+1 \) equations are composed, \( \tilde{P}_{D,n} \sim \tilde{q}_D \cdot S_f \) can be calculated by numerical method. When the production rate is constant, wellbore storage and skin can be easily added to Eq.(19) as a final step according to Duhamel’s principle [31].

\[ \tilde{P}_{r,D} = \frac{\tilde{P}_{D,n} \cdot \tilde{q}_D \cdot S_f}{1 + s \cdot C_{f,D} \tilde{P}_{D,n}} \quad (21) \]

4. Analyses of Transient Pressure Behaviors

The unsteady pressure characteristic type curves (Fig.4) of finite conductive MFHW for triple porosity and sequential single permeability in fractured-vuggy reservoirs are drawn by converting \( P_{r,D} \) back to \( P_{r, D} \) based on Stehfest numerical inversion [32].

Fig.4 shows that the transient pressure behavior can be divided into eight flow regimes. I: Wellbore storage regime. Curves for both pressure and pressure derivative are in a unite slope trend. II: Transient flow regime between well storage...
and early linear flow which presents a hump. III: Early linear flow regime. The pressure derivative curve is a line with a slope of 0.25; IV: Inter-porosity flow regime from vug to NF. Because vug permeability is higher than NF permeability; there is a characteristic dip. V: Inter-porosity flow regime from matrix to vug. The pressure derivative curve is also a dip controlled by interporosity flow from matrix system to vug system. VI intermediate-time pseudo-radial flow regime around individual fractures which is influenced by the distance between hydraulic fractures. VII: Compound linear flow which represents the linear flow normal to horizontal well axis. VIII: Compound radial flow regime which indicates the pressure of matrix, fracture, and vug systems have arrived at a dynamic balance. The derivative responses of pressure shows a flat behavior.

As is known from Eq. (19), the MFHW well testing typical curves in carbonate reservoirs are mainly influenced by fracture number, distance between fractures, half length of fracture, storage and inter porosity flow.

Fig. 5 illustrates the effects of fracture number on the transient pressure of finite conductive MFHW for triple porosity and sequential single permeability in fractured-vuggy reservoirs. The typical curve characteristics show that with the increase of fracture number, the location of the pressure and pressure derivative curve becomes lower among II~VII regime. The main reason is that the interference between fractures will be stronger as the fracture number increases with other parameters (such as $w_f$, $w_v$, $w_m$, $L_f$, $x_f$, $\lambda_v$, $\lambda_m$, et al.) being constant.

Fig. 6 presents how the fracture distance influences the MFHW well testing curves of triple porosity and sequential single permeability in fractured-vuggy reservoirs. From Fig. 6 we can see that when the distance between fractures increases, compound linear flow emerges later. The reason is that interference between fractures will weaken as the distance between fractures increases.

Fig. 7 illustrates that the half length of fracture mainly affects the early linear flow regime and two inter-porosity flows. Meanwhile, it indicates that the longer the fracture length is, the lower the location of early linear flow regime and two inter-porosity flows regimes in the pressure and pressure derivative curve is.

Fig. 8 and Fig. 9 denote how the vug and matrix interporosity flow coefficient affect the MFHW well testing curves of triple porosity and sequential single permeability in fractured-vuggy reservoirs respectively. It shows that as the interporosity flow coefficient goes higher, the dip appears earlier (Fig. 8). The vug interporosity flow coefficient influences the first dip, while matrix interporosity flow coefficient influences the second one (Fig. 9). Meanwhile, if the value of parameters is inappropriate, the eight flow regimes of the transient pressure behavior of finite conductive MFHW for triple porosity and sequential single permeability in fractured-vuggy reservoirs will not fully emerge (Fig. 8~Fig. 10).
Fig. 9. Effect of matrix interporosity coefficient on the transient pressure of finite conductive MFHW for triple porosity and sequential single permeability in fractured-vuggy reservoirs.

Fig. 10. Effect of storativity ratio on the transient pressure of finite conductive MFHW for triple porosity and sequential single permeability in fractured-vuggy reservoirs.

5 Conclusions

1) Based on the Source function theory, the mirrors reflection and the superposition principle, the finite conductive MFHW’s bottom-hole pressure solution for natural fractured-vuggy carbonate reservoirs is obtained.

2) Well testing typical curves of MFHW in natural fractured-vuggy carbonate reservoirs are drawn, and the ones are characterized by eight flow regimes including wellbore storage regime, transient flow regime, early linear flow regime, inter-porosity flow regime of vug to NF, inter-porosity flow regime of matrix to vug, intermediate-time pseudo-radial flow regime, compound linear flow regime, and compound radial flow regime.

3) The sensitivity parameters of MFHW’s transient pressure well testing curves are discussed. The results indicate that fracture number affects the location of the pressure and pressure derivative curve among II–VII regime; the distance between fractures mainly influence the time compound linear flow emerges; fracture length has a primary effect on the location of the early linear flow regime and two inter-porosity flows regimes; the storativity ratio influences dip’s depth and the interporosity flow mainly affects the time dip emerges.

Nomenclature

- \(k\) = permeability (m\(^2\))
- \(\Delta p\) = Pressure drop (MPa)
- \(\mu\) = oil viscosity (mPa.s)
- \(C_i\) = oil compressibility (MPa\(^{-1}\))
- \(L_f\) = distance between fractures (m)
- \(n_f\) = fracture number
- \(x_f\) = half length of fracture (m)
- \(\alpha\) = shape factor (m\(^{-2}\))
- \(\Phi\) = porosity (decimal)
- \(w\) = storativity ratio
- \(\lambda\) = interporosity flow coefficient
- \(h\) = reservoir thickness (m)
- \(t\) = time (hour)
- \(V\) = volume (m\(^3\))
- \(s\) = time in Laplace space
- \(r_D\) = dimensionless radius
- \(L\) = reference length (m)
- \(x_{D_i}\) = dimensionless x of discrete fracture segment
- \(y_{D_i}\) = dimensionless center point’s y of discrete fracture segment
- \(S_f\) = skin of fracture wall

Subscripts

- NF = natural fracture system
- m = matrix system
- v = vug system
- i = the i-th discrete segment of fracture

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