Mathematical Modelling of a Novel Hetero-junction Dual SIS ZnO-Si-SnO Solar Cell

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Abstract

For the last few decades scientists across the world have achieved significant improvement in performance of conventional silicon p-n junction solar cell. Sophisticated high temperature doping technology is unavoidable in the fabrication of these solar cells. Back in 1970s scientists proposed an alternative solar cell technology with Schottky barrier which can cut down the burden on thermal budget of manufacturing process. Later the metal-semiconductor Schottky barrier further modified with hetero junction semiconductor-semiconductor solar cells. A thin intrinsic layer sandwiched between semiconductor-semiconductor junctions can repair the junction defects efficiently. These SIS solar cells became popular for its low thermal budget and considerable efficiency. In this paper we have tried to propose a mathematical model of a novel dual side SIS solar cell which is basically a multi junction solar cell. We have introduced a third semiconductor layer (SnO) at the back side of the cell which can provide an inversion layer similar to PERT solar cell. This structure is first of its kind and thus a theoretical analysis is required before implementation. We have studied the effect of this back field on the performance of the cell and propose a mathematical model based on reciprocity theorem of charge collection. The efficiency of conventional ZnO-pSi SIS solar cell was computed ~5.2% while the back SnO p+ layer is expected to enhance the efficiency up to ~7.9% according to our mathematical model. We have concluded with significant mathematical justification to implement this structure with proposed electro-chemical experiments.

Keywords: SIS solar cell; ZnO; SnO; MATLAB; hetero junction; Silicon

1. Introduction

In 1883 Fritts reported a non-conventional solar cell with very poor efficiency (~1%) replacing the silicon homojunction with metal-semiconductor Schottky junction [1]. In later years scientists have significantly improved the efficiency of Schottky barrier solar cell by optimizing the metal layer thickness and introducing an insulator layer in between the metal-semiconductor to minimize the junction interface crystal defect [2][3]. The basic principle of operation of these MIS solar cells later inspired scientists to adopt the similar technology in semiconductor-insulator-semiconductor hetero-junction solar cells (SIS). The choice of different semiconductor combinations and different layer deposition techniques like enhanced the efficiency of the solar cell in following years. Metal oxide semiconductors like SnO\textsubscript{2} [4], TiO\textsubscript{2} [5], ITO [6], ZnO [7] became popular in investigating the performance of SIS solar cell. Modern layer deposition techniques like sputtering, CVD, ALD immensely helped this technology to grow. The latest development of SIS solar cell using ITO-SiO\textsubscript{2}–n-Si was reported as 16.6% efficiency by Untila et al in 2020 [8]. Still the major trailing factor for SIS solar cell in race of solar cell technology is its poor efficiency but this SIS technology seems to be the winner for its extremely low thermal budget in comparison with conventional crystalline Si solar cell. Different metal oxide semiconductors layer can be grown over Si even by room temperature CBD or Sol-gel process [9]. On the other hand the recent advancement of Si solar cell is designed with PERT technology where rear surface is totally passivated by back surface field. Highly efficient PERT Si solar cell (~24.5\%) has been reported by Zhao et al [10]. Inspiration of our design of novel dual SIS solar cell is to adopt the PERT technology in SIS solar cell by introducing a rear surface passivated field. This filed was designed by another SIS junction at the back. The semiconductor materials for these two SIS junctions (front surface and back surface) were chosen considering their carrier concentration and electron affinity. The semiconductor properties of the metal oxides used in our proposed cell structure were sourced from existing experimental data published elsewhere.

Fig. 1 Dual SIS structure

The proposed dual SIS collar cell structure is depicted in Fig. 1. We have considered p type mono crystalline Si as the substrate. The front surface is totally passivated by ITO layer which is an n type semiconductor further modified with SnO p+ layer. On the back side of the cell SnO layer is introduced which provides the inversion layer. ZnO layer is added on top of SnO layer for its low thermal budget. The proposed model was simulated by a numerical method in MATLAB.
Si(semiconductor) where the back surface field is designed with another SIS field consisting with p-Si(Semiconductor)-Al₂O₃(Insulator)-SnO(Semiconductor). All the layers can be grown over the p-Si substrate by suitable CBD or Sol-gel or low temperature thermal process [11][12][13][14]. The thermal budget reduction is a major advantage of our proposed structure. We have theoretically estimated the performance of the proposed solar cell. The collection probability of the minority carrier was formulated for different sections of the proposed cell by solving the Poisson’s equation and applying reciprocity theorem condition. Further the layer thickness was varied and estimated the effect on voltage-current profile.

2. Band Diagram and carrier flow

The energy band diagram and the corresponding band bending of the proposed solar cell structure is shown in Fig.2.

![Energy band diagram of dual SIS structure](image)

Fig. 2 Energy band diagram of dual SIS structure

Here the we have are referring prefix 1, 2 and 3 for associated parameters of ZnO, p-Si and SnO respectively. Different material properties required for the mathematical modelling of this dual SIS solar cell are considered from different experimental works reported elsewhere. The parameters that we have considered are listed below in Table 1.

| Parameter                        | ZnO (n-type) | Si (p-type) | SnO (p⁺-type) |
|----------------------------------|--------------|-------------|---------------|
| Energy band gap (eV)             | Eₘ₁ = 3.37[15]| Eₘ₂ = 1.124[16]| Eₘ₃ = 2.4[17]  |
| Electron affinity (eV)           | χ₁ = 4.5[15]  | χ₂ = 4.05[16] | χ₃ = 3.7[18]  |
| Effective mass of electron (mₑ) | mₑ₁ = 0.24[19]| mₑ₂ = 1.08   | mₑ₃ = 0.4[20] |
| Effective mass of hole (mₚ)     | mₚ₁ = 0.59[19]| mₚ₂ = 0.81   | mₚ₃ = 0.9[20] |
| Electron mobility (cm²/V-s)      | μₑ₁ = 200[19] | μₑ₂ = 1400   | μₑ₃ = 3[21]   |
| Hole mobility (cm²/V-s)          | μₚ₁ = 50[19]  | μₚ₂ = 470    | μₚ₃ = 7[17]   |
| Electron lifetime (s)            | τₑ₁ = 2.8×10⁴[23]| τₑ₂ = 10×10⁴[22]| τₑ₃ = 4×10⁹[21] |
| Hole lifetime (s)                | τₚ₁ = 2.8×10⁷[23]| τₚ₂ = 10×10⁶[22]| τₚ₃ = 4×10⁹[21] |
| Electron concentration (cm⁻³)    | Nₑ₁ = 4.8×10¹⁸[24]| Nₑ₂ = 6.7×10⁴| Nₑ₃ = 5×10¹⁸[25] |
| Hole Concentration (cm⁻³)        | Nₚ₁ = 10¹⁵     | Nₚ₂ = 10¹⁵   | Nₚ₃ = 5×10¹⁸[25] |

When the device reaches its equilibrium the Fermi level has to be constant throughout the device. The actual position of the Fermi level depends upon the majority carrier concentration. In case of metal oxide semiconductors the carrier concentration depends upon its deposition process and temperature. We have considered the different concentration for ZnO for different layer deposition techniques as reported. Then we have studied the effect of the deposition process on the performance of the solar cell which is discussed later in this paper. The band bending and junction notch approximation is done by solving the Maxwell’s equations at the junction boundary. For the ZnO-
Si(p-type) junction the built in potential can be estimated from the band diagram as shown in equation 1.

$$\Psi_1 = \frac{1}{q} \left[ (\chi_2 + E_{C2} - E_F) - (\chi_1 + E_{C1} - E_F) \right] \ldots \ldots \ldots (1)$$

Here $E_{C}$ is the conduction band energy and $E_F$ is the Fermi energy level of the device. Further applying the Fermi-Dirac statistical distribution of electron we can get[26],

$$E_{C1} - E_F = k_BT \ln \left( \frac{N_{C1}}{N_{d1}} \right) \ldots \ldots \ldots (2)$$

$$E_{C2} - E_F = E_{G2} - (E_F - E_{V2}) = E_{G2} - k_BT \ln \left( \frac{N_{V2}}{N_{a2}} \right) \ldots \ldots \ldots (3)$$

$E_V$ is the valence band energy. Substituting equation 2 and 3 in equation 1 we can get the expression for built in potential as,

$$\Psi_1 = \frac{1}{q} \left[ \chi_2 - \chi_1 + E_{G2} - k_BT \ln \left( \frac{N_{V2}N_{C1}}{N_{a2}N_{d1}} \right) \right] \ldots \ldots \ldots (4)$$

The notch height for this junction will be the difference in conduction band energy, i.e.

$$\Delta E = E_{C2} - E_{C1} \ldots \ldots \ldots (5)$$

Then the band bending is drawn obeying the Matsuura equation.[27]

The second junction creates a back surface p-p* field. The band bending will occur due to the change in concentration gradient of acceptors. Since SnO shows a good high density p type semiconductor (~10^{19}/cm^3)[25] and the p-Si substrate is chosen with 10^{15}/cm^3 acceptor concentration. This results a considerable band bending and back surface field to enhance the collection probability of the solar cell. The band diagram in this case is drawn with the same approach as ZnO(n-type) and p-Si junction. The built in junction potential in this case can be written from equation 4. We have considered $E_{G2}$ to match the datum voltage level with $\Psi_1$.

$$\Psi_2 = \frac{1}{q} \left[ \chi_2 - \chi_1 + E_{G3} - E_{G2} - k_BT \ln \left( \frac{N_{V3}N_{C2}}{N_{a3}N_{d2}} \right) \right] \ldots \ldots \ldots (6)$$

This field sweeps away the light generated carriers to reach the junction 1 and hence get collected. We have considered the insulation layer in each junction 10 Å. Which is thin enough to allow the carrier to pass due to tunnelling effect. The pinning of carriers as an effect of same energy state tunnelling is shown in the band diagram by small pinning lines.

The photon entering through the front surface ZnO layer creates photo generated carriers in different part of the solar cell. The location of absorption of photon depends up on the energy of the photon and attenuation constant of the material. Most of the photon gets attenuated before reaching the second junction hence a very few carrier will be collected by the second junction. But the rear junction field provide a drift to the generated carrier to reach to the junction before recombination. As shown in the energy band diagram the electron flow will be towards the negative slope and hence we can have a net photo generated current from left to right in the device.

3. Dark saturation current

In our design of dual SIS structure we have considered two junctions of different carrier concentration. This results two depletion region and two built in potential as equated in equation 4 and 6. The photo generated current due one junction depends upon the voltage across other junction. The total photo generated current depends on the collection probability which is discussed in the next section. The built in potential for two different junctions are cumulative and thus the voltage drop across the equivalent diodes must be in series. The dark saturation current is controlled by this built in potential of the cell. The dark saturation current densities for two junctions can be calculated as a function of acceptor and donor carrier concentrations, diffusion coefficient and diffusion length [28].

$$J_0 = qe^{-\phi/\mu} \sqrt{N_{a2} \frac{D_{p2}}{\tau_{p2}} + N_{d1} \frac{D_{n2}}{\tau_{n2}}} \ldots \ldots \ldots (7)$$

In equation 7, $\phi$ is the built in potential. For a single SIS (ZnO-Si) cell $\phi = \Psi_1$. Where as, for the proposed dual SIS (ZnO-Si-SnO) cell the built in potential $\phi = \Psi_1 + \Psi_2$.

The diffusion coefficient D was estimated from Einstein relationship

$$D = \frac{kT}{q} \mu \ldots \ldots \ldots \ldots \ldots (8)$$

4. Photo generated current
The photo generated current basically involves with two mechanisms, one is the carrier generation due to absorption of photon, and other is the collection of the carrier drifted due to the effect of depletion region electric field. As we have discussed earlier in dual SIS cell we have two depletion region electric fields in front and rear junction. So the collection of the photo current will be due to simultaneous effect of these two built in fields. All the generated carriers do not get collected by the junction. A factor called collection probability \( (C_p) \) plays an important role to determine the ratio of generated to collected carrier. In 1985 Donolato published his path-breaking proposition to estimate the collection probability of photo generated minority carrier under photo illuminance, which is well recognized as reciprocity theorem \([29]\). Later he reconstructed the theorem in 1994 for two dimensional application \([30]\). The theorem can be approximated in one dimensional and stated as “The current collected by p-n junction as a unit carrier point charge is generated at a point \( P(x) \) (where \( x \) is the distance of point P from surface) is quantitively same as excess minority charge density at point \( P(x) \) due to unit density of carrier at the p-n junction edge”. This novel observation was mathematically expressed by him in the transport equation,

\[
D \nabla^2 C_p(x) - \frac{1}{\tau} C_p(x) = 0 \quad \text{(9)}
\]

We have incorporated this theorem to solve for the collection probability for our proposed solar cell. We are having three different material regions in this design.

![Fig. 3 Different semiconductor region in dual SIS structure](image)

In Fig. 3 different semiconductor regions is shown with their dimension. We have applied the reciprocity theorem for these three regions. The general solution of equation 9 can be given as,

\[
C_p(x) = Ae^{-x/L} + Be^{x/L} \quad \text{(10)}
\]

Where, \( L \) is the diffusion length.

\[
L = \left( D \tau \right)^{1/2}
\]

Different boundary conditions were taken for three different regions to find the constant \( A \) and \( B \) and then we solved the equation 9 to get the expression of \( C_p(x) \).

Region I: ZnO layer

The two boundary conditions are taken as,

\[
C_p(d_f) = 1 \quad \text{(11)}
\]

At the edge of the depletion region, all the carriers are collected. The collection of charges at the front surface is characterized by the reduced surface recombination velocity \( s_f = S_f/Dp_1 \). As explained by Donolato we got the second boundary condition.

\[
\frac{\partial C_p(0)}{\partial n_f} = s_f C_p(0) \quad \text{(12)}
\]

Solving this we get the expression for \( C_p(x) \). The complete solution of equation 9 under these conditions can be
found by reforming the solution as described by Hermele et al.\cite{31}

\[ C_{p1}(x) = \frac{\cosh\left(\frac{W_d - d_1 + x}{L_{p1}}\right) + L_{p1}s_f \sinh\left(\frac{W_d - d_1 + x}{L_{p1}}\right)}{\cosh\left(\frac{W_d}{L_{p1}}\right) + L_{p1}s_f \sinh\left(\frac{W_d}{L_{p1}}\right)} \quad \text{for} \quad d_1 \geq x \geq 0 \] \hspace{1cm} (13)

The surface recombination velocity \( (S_0) \) for ZnO surface was taken as \( 1 \times 10^5 \) cm/s \cite{32}.

Region II: p-Si layer

In the Si region if the photo carriers are generated at any of the junction edges that will be immediately collected.

This gave us two boundary conditions,

\[ C_p(d_1) = 1 \quad \text{.......}(14) \]

and

\[ C_p(d_2) = 1 \quad \text{.......}(15) \]

Solving transport equation with these conditions we got the solution for region II.

\[ C_{p2}(x) = \left(1 - \frac{L_{n3}}{L_{n2}}\right) e^{-\frac{x}{L_{n2}}} + e^{\frac{x}{L_{n2}}} \quad \text{for} \quad d_2 \geq x \geq d_1 \] \hspace{1cm} (16)

We have assumed that all the carriers can tunnel through the insulator layer, sandwiched between the semiconductors.

Region III: SnO layer

The boundary conditions for the p* layer was taken from the similar argument of region I.

\[ C_p(d_2) = 1 \quad \text{.......}(17) \]

and

\[ \frac{\partial C_p(W)}{\partial n_b} = s_n C_p(W) \quad \text{.......}(18) \]

We get the solution similar to region I.

\[ C_{p3}(x) = \frac{\cosh\left(\frac{W + d_2 - x}{L_{n3}}\right) + L_{n3}s_n \sinh\left(\frac{W + d_2 - x}{L_{n3}}\right)}{\cosh\left(\frac{W}{L_{n3}}\right) + L_{n3}s_n \sinh\left(\frac{W}{L_{n3}}\right)} \quad \text{for} \quad d_2 \geq x \geq W \] \hspace{1cm} (19)

Here the surface recombination velocity is taken as 400 cm/s \cite{33}. The surface recombination velocity can be controlled by appropriate passivating layers.

The total photo generated current density thus can be calculated as,

\[ J_L = q \int_{0}^{d_1} \int_{\lambda = 280nm}^{370nm} \left( (1 - R(\lambda)) \alpha_1(\lambda) H_0(\lambda) e^{-\alpha_1 x} d\lambda \right) C_{p1}(x) dx \]

\[ + q \int_{d_1}^{d_2} \int_{\lambda = 280nm}^{370nm} \left( (1 - R(\lambda)) \alpha_2(\lambda) H_0 e^{-\alpha_2 x} d\lambda \right) C_{p2}(x) dx \]

\[ + q \int_{d_2}^{d_1} \int_{\lambda = 370nm}^{1100nm} \left( (1 - R(\lambda)) \alpha_3(\lambda) H_0 e^{-\alpha_3 x} d\lambda \right) C_{p2}(x) dx \]

\[ + q \int_{d_2}^{w} \int_{\lambda = 280nm}^{370nm} \left( (1 - R(\lambda)) \alpha_4(\lambda) H_0 e^{-\alpha_4 x} d\lambda \right) C_{p3}(x) dx \]

\[ + q \int_{d_2}^{w} \int_{\lambda = 370nm}^{460nm} \left( (1 - R(\lambda)) \alpha_4(\lambda) e^{-\alpha_4 W_n} e^{-\alpha_3 x} d\lambda \right) C_{p3}(x) dx \] \hspace{1cm} (20)

The bandgap of ZnO is 3.37 eV. The photons having lesser energy than bandgap energy will not get absorbed by the ZnO layer. As a result for the majority of the wavelengths of the light ( >370 nm) ZnO layer will act like transparent
window layer. Similarly wavelengths greater than 460 nm will not get absorbed by SnO layer. Here $\alpha$ is the absorption coefficient of the media. Absorption coefficient of ZnO layer was formulated from the experimental result provided by Park et al. [34]

$$\alpha_1(\lambda) = 6.64 \times 10^5 \times \sqrt{\frac{hc}{\lambda} - E_{g1}} \quad \text{.........(21)}$$

Absorption coefficient of Si layer for the spectra was considered as the data provided Green et al [35]. The absorption coefficient for SnO layer was considered from the experimental result reported by Liu et al. [36]

$$\alpha_3(\lambda) = 4.2 \times 10^5 \times \sqrt{\frac{hc}{\lambda} - E_{g3}} \quad \text{.........(22)}$$

The photon flux data was fed to equation 24 from AM 1.5 irradiance standard data. $R(\lambda)$ was taken from the micro textured surface reflectance data [37].

5. Series and shunt resistance
The series resistance arises from emitter resistance, base resistance and contact resistance.

$$R_s = R_b + R_e + R_c \quad \text{.........(23)}$$

In proposed dual SIS structure the base is SnO layer while the emitter is ZnO layer. The base and emitter resistance was calculated from the following equations.

$$R_b = \frac{W - d_i}{A\sigma_3} \quad \text{.........(24)}$$

$$R_e = \frac{d_i}{q\mu_{e1}N_{d1}} \quad \text{.........(25)}$$

The contact resistance as calculated as a function of ZnO layer carrier concentration from graph obtained by Schroder et al [38].

$$R_c = 10^{(-5\log_{10}(N_{d1})+96.6)} \times 0.1 \times 10^4 \quad \text{.........(26)}$$

Here all the resistances were calculated per unit area and the contacts were assumed to cover 10% of total area. As the ideality factors were considered to be unity the shunt resistance also considered to be very high as 1.5k ohm.

6. Result and discussion
The conventional V-I equation of the solar cell can be derived from its equivalent circuit.

$$I = aJ_L - aJ_0 \exp \left[ \frac{q(V + aJ_LR_S)}{nkT} \right] - \frac{V + aJ_LR_S}{R_{St}} \quad \text{.........(27)}$$

$a$ is the surface area of the cell. Here we are considering the edge recombination to be negligible and the operating voltage is large enough to consider the ideality factor $n = 1.39$.

All the parameters that are mentioned in equation 27 was computed with MATLAB. We have plotted different parameters for different sections of the device and for different wavelengths. The result helped us to analyze the performance and improvement of the proposed dual SIS (ZnO-p Si-SnO) cell with respect to single SIS(ZnO-p Si) cell. The simulated results showed a significant improvement on open circuit voltage and short circuit current. This resulted a higher efficient dual SIS solar cell than single SIS structure. Improvement of short circuit current depends on the light generated current. The back surface field enhance the collection probability as discussed earlier.
Fig. 4 Collection probability

Fig 4 shows the collection probability of photo generated carriers inside the device. We have considered the thickness of both ZnO and SnO film 150 nm and the p-Si substrate of thickness 500 micron. The improvement of collection probability in dual SIS cell seems much overwhelming over the single SIS cell as shown in Fig 4. The major enhancement of collection probability can be observed as the light penetrates deeper inside the cell. Here we must acknowledge the fact that as photon beams are penetrated more inside the cell it gets attenuated. The attenuation depends upon $\alpha$ which is a function of the wavelength. The attenuation constant $\alpha$ is very high for lesser wavelengths. Thus almost all the photon flux gets attenuated as infra red wave penetrates through the cell. Almost no photon flux remains where the effective collection probability is improved for the back surface field. So the region where collection probability is largely enhanced there is no more generated carrier to get collected. For the higher wavelengths of the spectra the attenuation is less. This implies that photon flux can get inside deeper in the cell without losing much of its strength. The advantage of higher collection probability near the back surface field is more effective for ultra violet range of the spectra.

Fig. 5 Photo generated current for different wavelength

In Fig 5 we can see the simulated output of Photo generated current for different wavelength of the spectra. This
result is justifying our analysis. We can observe the improvement of photo-generated current is prominent only for higher wavelength photons. A significant improvement can be observed beyond the visual range of the spectra. A total increment of 2.8224% of photo-generated current has been computed in dual SIS structure with respect to single SIS structure without back surface SnO layer. The proposed solar cell performs better for ultra violet range whereas there is not any significant change in photo current for lower wavelength range of spectra.

![](comparison_of_V-I_characteristics.png)

**Fig. 6 V-I characteristics of dual and single SIS cell**

The V-I characteristics was simulated for a 1 cm² cell with and without back SnO film.

|                      | J_{SC} in mA/cm² | V_{OC} in volt | Form Factor (FF) | % Efficiency (η) |
|----------------------|------------------|----------------|------------------|------------------|
| Dual SIS solar cell  | 0.0186           | 0.4565         | 0.7903           | 6.6928           |
| Single SIS solar cell| 0.0180           | 0.3780         | 0.7611           | 5.1908           |

A comparative performance index table is shown in Table 2. We can see a significant improvement in both open circuit voltage and short circuit current. As a result the efficiency is expected to raise up to ~6.7% from ~5.2%. The result for single SIS solar cell is quite close by the experimental result obtained by Untila et al [40]. The improvement of the J_{SC} is the result of the change in collection probability for p-p⁺ depletion region at p Si-SnO junction. Whereas the additional built in potential improved the open circuit voltage.
We have further varied the effective hole concentration of back surface SnO film. We have contemplated the effect of hole concentration of SnO layer in computed efficiency. Different values of hole concentration was taken into consideration as reported by other groups of scientists earlier. Different methods of deposition were considered with different physical conditions. Guo et al reported the effective concentration of hole carrier in 25°C and 300°C [25]. Hsu et al reported properties of deposited SnO by sputtering [41]. Bu reported sol gel deposition of p-type Sno:Mn:K film for solar cell application [42]. All the data of these reports were interposed in our mathematical model to get the efficiency of the proposed dual SIS solar cell. In Fig 7 we can observe efficiency increases exponentially as the carrier concentration increases. We observed that the efficiency was lesser for dual SIS structure than single Sis cell when the hole concentration of the back surface layer is less than that of the p-Si substrate. When the hole concentration of SnO is less than that of p-Si layer a reverse field is to be created which acts in opposition to the ZnO-Si junction. This makes the overall efficiency lower than single ZnO-p Si SIS solar cell. The simulated result shown in Fig 7 leads us to an important expression of efficiency as a function of effective hole concentration of the back surface p+ layer.

\[ \eta = m \ln \left( \frac{N_a}{N_{ref}} \right) \]  

Where the constants \( m = 0.4122473 \) and \( N_{ref} = 8.148582 \times 10^{11} \) cm\(^{-3} \) were computed from the graph. \( N_a \) is the hole concentration of SnO in cm\(^{-3} \).

**7. Conclusion**

In this mathematical model we are proposing a very new hetero junction dual SIS solar cell which has 28.93% to 52.23% improvement in efficiency over the single SIS solar cell. We have approximated the efficiency as a function of carrier concentration of back surface layer carrier concentration. This shows a exponential increment of efficiency with carrier concentration. Though the overall efficiency is much lesser than the crystalline Si solar cell but the
process involved in depositing the layers on front and back surface was considered to be done with some simple chemical process mostly conducted in room temperature. This can avoid expensive annealing and diffusion process. This proposed cell thus has much opportunity to perform well in low energy and low budget applications. In this paper we are proposing a very new hetero junction structure with significant mathematical justification and low cost electro chemical experimentation. Since the SnO layer is shown to be beneficial for the solar cell application this paper indicates a green signal for the further development of dual SIS solar cell.

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