Faint Quasars Live in the Same Number Density Environments as Lyman Break Galaxies at $z \sim 4$

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Received 2019 November 26; revised 2020 October 19; accepted 2020 October 21; published 2020 December 21

Abstract

Characterizing high-$z$ quasar environments is key to understanding the coevolution of quasars and the surrounding galaxies. To restrict their global picture, we statistically examine the g-dropout galaxy overdensity distribution around 570 faint quasar candidates at $z \sim 4$, based on the Hyper Suprime-Cam Subaru Strategic Program survey. We compare the overdensity significances of g-dropout galaxies around the quasars with those around g-dropout galaxies, and find no significant difference between their distributions. A total of 4 (22) out of the 570 faint quasars, $0.7 - 0.4(3.9^{+6.8}_{-4.8})\%$, are found to be associated with the $>4\sigma$ overdense regions within an angular separation of 1.8 (3.0) arcmin, which is the typical size of protoclusters at this epoch. This is similar to the fraction of g-dropout galaxies associated with the $>4\sigma$ overdense regions. This result is consistent with our previous work in which $1.3^{+0.9}_{-0.7}$ and $2.0^{+1.1}_{-1.0}\%$ of luminous quasars detected in the Sloan Digital Sky Survey exist in the $>4\sigma$ overdense regions within $1.8$ and $3.0$ separations, respectively. Therefore, we suggest that the galaxy number densities around quasars are independent of their luminosity, and most quasars do not preferentially appear in the richest protocluster regions at $z \sim 4$. The lack of an apparent positive correlation between the quasars and the protoclusters implies that (i) the gas-rich major merger rate is relatively low in the protocluster regions, (ii) most high-$z$ quasars may appear through secular processes, or (iii) some dust-obscured quasars exist in the protocluster regions.

Unified Astronomy Thesaurus concepts: Quasars (1319); Galaxy evolution (594); Lyman-break galaxies (979); Protoclusters (1297); Galaxy formation (595)

1. Introduction

High-$z$ quasars are powered by mass accretion onto supermassive black holes (SMBHs). According to the $M - \sigma$ relation (Magorrian et al. 1998; Kormendy & Ho 2013), the black hole mass is strongly correlated with the bulge mass, and thus the halo mass of the host galaxy. If the local deterministic relation is valid even at a high redshift, high-$z$ quasars are expected to reside in massive halos. In fact, at $z > 3$, the quasar halo mass is massive: $M_h \sim (4 - 6) \times 10^{12} h^{-1} M_\odot$ (Shen et al. 2007). In terms of the hierarchical structure formation, galaxies may frequently experience gas-rich mergers in galaxy overdense regions (e.g., Hine et al. 2016). The central SMBH can be fed by sufficient gas to evolve into a quasar (“merger scenario”; e.g., Hopkins et al. 2008). Thus, high-$z$ quasars are speculated to reside in galaxy overdense environments such as protoclusters.

However, a consistent picture regarding the environments of $z > 3$ quasars has not yet been achieved, despite numerous intensive studies (for details, see Overzier 2016). For instance, there is supportive evidence that $z > 3$ quasars exist in galaxy overdense regions (e.g., Zheng et al. 2006; Kashikawa et al. 2007; Utsumi et al. 2010; Husband et al. 2013; Morselli et al. 2014; Balmaverde et al. 2017; Decarli et al. 2017; Garcia-Vergara et al. 2019; Neeleman et al. 2019; Mignoli et al. 2020). On the other hand, several previous studies reported that quasars do not live in galaxy overdense regions at $z > 3$ (e.g., Toshikawa et al. 2016; Kikuta et al. 2017; Marino et al. 2018; Ota et al. 2018; Lupi et al. 2019; Marinello et al. 2020; Uchiyama et al. 2019; Yoon et al. 2019). The characterization of high-$z$ quasar environments is challenging owing to the rarity of high-$z$ quasars and protoclusters. The number densities of protoclusters and quasars are expected to be $\sim 1$ deg$^{-2}$ at $z \sim 4$ (Toshikawa et al. 2018; Uchiyama et al. 2018). Cosmic variance and the different physical-scale density measurement as well as the low statistics have prevented us from obtaining a global picture of the high-$z$ quasar environment.

In recent years, Uchiyama et al. (2018, hereafter U18) statistically examined whether 151 Sloan Digital Sky Survey (SDSS) quasars were correlated with 179 Hyper Suprime-Cam
(HSC)-detected protoclusters at $z \sim 4$ (Toshikawa et al. 2018), the number of which is approximately 10 times higher than previously known protoclusters. This more systematic study led to high statistics and low cosmic variance effects. As a result, the majority of the quasars at $z \sim 4$ are likely not associated with protoclusters. Only $\sim1\%$ of the SDSS luminous quasars were found to be associated with protoclusters. The SDSS quasar halos at $z \sim 4$ were likely to evolve into group-like halos.

The quasars used in U18, however, were limited to luminous ones with UV absolute magnitudes of $M_{UV} \lesssim -26$, corresponding to $\sim M_{UV}^* - 0.5$ (Akiyama et al. 2018) at $z \sim 4$. The galaxy density around the less luminous quasars is likely to be higher than that around the luminous ones owing to photoevaporation effects, which could make the surrounding galaxy densities lower (e.g., Kashikawa et al. 2007; Dashyan et al. 2019; Johnson & Aykutalp 2019; Uchiyama et al. 2019).

On the other hand, it is known that the clustering strength of quasars at $z \sim 4$ is likely to be higher than that around the less luminous quasars owing to photoevaporation effects, which could make the surrounding galaxy densities lower (e.g., Kashikawa et al. 2007; Dashyan et al. 2019; Johnson & Aykutalp 2019; Uchiyama et al. 2019). This more systematic study of U18, we could clarify the possible dependency on the quasar luminosity for their surrounding environments, and we could provide more statistically robust results as our quasar sample size was approximately four times larger than that in the previous study of U18.

The paper is organized as follows. In Section 2, we describe the HSC Subaru Strategic Program (HSC-SSP) survey, and the construction of the HSC-detected protoclusters and quasars. In Section 3, we investigate the environments of the HSC quasars. The implications of our results are discussed in Section 4. Finally, in Section 5, conclusions and a summary of our findings are provided. We assume the following cosmological parameters: $\Omega_M = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, and magnitudes are given in the AB system.

2. HSC-SSP Survey and Sample Selection

2.1. Subaru HSC-SSP Survey

The HSC-SSP survey started in early 2014 and will include 300 nights until its completion by 2020. The HSC is equipped with 116 2$K \times 4K$ Hamamatsu fully depleted CCDs, among which 104 CCDs are used to obtain scientific data over a field of view of 1.5$^2$ in diameter. The detailed system design is summarized by Miyazaki et al. (2018). For the CCD dewear and camera system design, one should refer to Komiyama et al. (2018). This study is based on the Wide layer of the HSC-SSP, which has wide-area coverage and high sensitivity through five optical bands ($g$, $r$, $i$, $z$, and $y$) with transmission functions (Kawanomoto et al. 2018) that are roughly similar to the SDSS filter curves. The total exposure times are 10 minutes in the $g$ and $r$ bands and 20 minutes in the $i$, $z$, and $y$ bands. The on-site quality assurance system for the HSC (OSQAH; Furusawa et al. 2018) is used in the HSC-SSP observations. The HSC data (DR S16A; Aihara et al. 2018b) in the Wide layer have already produced an extremely wide field image of $>200$ deg$^2$ with a median seeing value of 0''6-0''8. The survey design is presented in Aihara et al. (2018a). Data reduction is performed with the dedicated pipeline hscPipe (version 4.0.2, Bosch et al. 2018), which is a modified version of the Large Synoptic Survey Telescope software stack (Ivezic et al. 2008; Axelrod et al. 2010; Juric et al. 2015). The astrometric and photometric calibrations are associated with the Pan-STARRS1 system (Schlafly et al. 2012; Tonry et al. 2012; Magnier et al. 2013). The fluxes and colors of the sources are measured with cModel, which is achieved by fitting two-component, point-spread function (PSF)-convolved galaxy models to the source profile (Abazajian et al. 2004).

2.2. HSC Protocluster Sample

We use the $z \sim 4$ protocluster candidate catalog constructed from DR S16A (Toshikawa et al. 2018). We briefly summarize the key steps of the catalog construction here.

First, the $g$-dropout candidates were selected from five independent fields: W-XMMiLSS (R.A. = $1^{d}36^{m}00^{s}$ $\sim 3^{d}00^{m}00^{s}$, decl. = $-6^{d}00^{m}00^{s}$ $\sim -2^{d}00^{m}00^{s}$), W-Wide12H (R.A. = $11^{d}40^{m}00^{s}$ $\sim 12^{d}20^{m}00^{s}$, decl. = $-2^{d}00^{m}00^{s}$ $\sim 2^{d}00^{m}00^{s}$), W-GAMA15H (R.A. = $14^{d}00^{m}00^{s}$ $\sim 15^{d}00^{m}00^{s}$, decl. = $-2^{d}00^{m}00^{s}$ $\sim 2^{d}00^{m}00^{s}$), W-HECTOMAP (R.A. = $15^{d}00^{m}00^{s}$ $\sim 17^{d}00^{m}00^{s}$, decl. = $42^{d}00^{m}00^{s}$$\sim 45^{d}00^{m}00^{s}$), and W-VVDS (R.A. = $22^{d}00^{m}00^{s}$ $\sim 23^{d}20^{m}00^{s}$, decl. = $-2^{d}00^{m}00^{s}$$\sim 3^{d}00^{m}00^{s}$). Here, the following criteria were used, as provided in van der Burg et al. (2010):

\begin{align}
1.0 &< g - r, \\
| r - i | &< 1.0, \\
1.5 | r - i | &< (g - r) - 0.80, \\
r &\leq m_{lim,3\sigma}, \\
i &\leq m_{lim,5\sigma},
\end{align}

where $m_{lim,3\sigma}$ and $m_{lim,5\sigma}$ are $3\sigma$ and $5\sigma$ limiting magnitudes, respectively. If the objects were not detected in the $g$-band filter at $3\sigma$, their $g$-band magnitudes were replaced with the corresponding $3\sigma$ limiting magnitudes. The red galaxies at intermediate redshifts and dwarf stars could satisfy the color selection criteria. The contamination rate from these objects was evaluated as a maximum of 25\% at $i < 25.0$ (Ono et al. 2018). The $g$-dropout selection completeness window was estimated to be $z = 3.8^{+0.9}_{-0.3}$ by the Monte Carlo method (Ono et al. 2018), as illustrated in Figure 1.

Owing to the sky conditions in the observation, the depth over the entire regions is inhomogeneous, which causes large scatter in the number of detected objects in the different fields, leading to difficulties in comparing the number densities among their fields. Thus, only homogeneous depth regions were used, where the $g$, $r$, and $i$-band $5\sigma$ limiting magnitudes were fainter than 26.0, 25.5, and 25.5 mag, respectively. The resultant effective area after removing the masked region around the bright objects was 121 deg$^2$. In this area, 259,755 g-dropouts down to $i < 25.0$ were detected.

Subsequently, the fixed aperture method was applied to determine the surface density contour maps of the g-dropout
galaxies. Apertures with a radius of 1′/8, corresponding to 0.75 physical Mpc (pMpc) at $z \sim 4$, were distributed in the sky of the HSC Wide layer. This aperture size is comparable with the typical protocluster size at this epoch with a descendant halo mass of $\gtrsim 10^{14} M_\odot$ at $z = 0$ (Chiang et al. 2013). The resolution of the density map was 1 × 1 arcmin$^2$. The overdensity significance was defined by $(\langle N-N \rangle)/\sigma$, where $N$ is the number of g-dropout galaxies in an aperture, and $\langle N \rangle$ and $\sigma$ are the average and standard deviation of $N$ over all of the fields, respectively. $(\langle N \rangle, \sigma)$ was estimated to be (6.4, 3.2) (Toshikawa et al. 2018). It was assumed that the number density of the g-dropout galaxies in the masked areas was the same as the average. However, the apertures in which $>50\%$ of the area was masked were excluded. As the contaminants of foreground objects distribute randomly over the sky, the overdensity significance should not be greatly affected by the contamination (Toshikawa et al. 2012).

The protocluster candidates were defined as overdense regions with $>4\sigma$ overdensity significance. Although large scatter exists owing to projection effects, the surface overdensity significance is closely correlated with the descendant halo mass at $z = 0$. Toshikawa et al. (2016) demonstrated that $>76\%$ of $>4\sigma$ overdense regions of g-dropouts were expected to evolve into dark matter halos with masses of $>10^{14} M_\odot$ at $z = 0$, whereas overdense regions with less than $4\sigma$ significance could not be distinguished from fields owing to the projection effect. According to Toshikawa et al. (2018), as a result of the projection effect, the protocluster sample is biased to the richest structure, the average descendant halo mass of which is expected to be $\sim 5 \times 10^{14} M_\odot$, with a high purity ($>76\%$) but low completeness ($\sim 6\%$). By clustering analysis, their mean halo mass at $z \sim 4$ was estimated to be $2.3^{+0.5}_{-0.3} \times 10^{13} h^{-1} M_\odot$, which is comparable to galaxy group halo mass (Toshikawa et al. 2018). It should be noted that the success rate of this technique has already been established by a previous study on the $\sim 4$ deg$^2$ of the CFHTLS Deep Fields, as the precursor of this HSC protocluster research, followed by Keck/DEIMOS and Subaru/FOCAS spectroscopy (Toshikawa et al. 2016). The authors carefully checked each $>4\sigma$ overdense region, and removed 22 fake detections of mainly the spiral arms of local galaxies (Aihara et al. 2018b). As a result, 179 protocluster candidates at $z \sim 4$ in the HSC Wide layer with overdensity significance ranging from 4 to 10$\sigma$ were obtained.

### 2.3. HSC Quasar Sample

The $z \sim 4$ quasar sample was constructed from the same DR S16A as used in Akiyama et al. (2018). We present the essence of the selection below.

The authors selected the quasar sample conservatively in the effective survey area of 172.0 deg$^2$, which is covered by grizy-bands and masked around bright objects ($i < 22$) to avoid possible failure of the HSC pipeline deblending process for faint objects in the outskirts of the bright objects (Akiyama et al. 2018). Stellar objects were extracted when their second-order adaptive moments (Hirata & Seljak 2003) were comparable to the PSF size.

The $z \sim 4$ quasar candidates were selected by using the griz-band color–color selection,

$$
\begin{align*}
 r - z &= 0.65 (g - r) - 0.30, \\
 r - z &= 3.50 (g - r) - 2.90, \\
 g - r &= 1.50,
\end{align*}
$$

and izy-band color–color selection,

$$
\begin{align*}
 z - y &= -2.25 (i - z) + 0.400, \\
 -0.3 &< i - z.
\end{align*}
$$

The latter izy-band criterion was applied to remove contaminations such as red galactic stars and several outliers. Akiyama et al. (2018) limited the sample to $i > 20$ because bright objects ($i < 20$) are affected by saturation or nonlinearity effects. They carefully removed objects around bright stars and galaxies, as well as those close to faint halos and satellite tracks around bright stars to prevent unreliable photometry.

A total of 1668 quasar candidates, with photometric redshifts of $z = 3.9^{+0.4}_{-0.3}$ (Figure 1), were detected. The UV absolute magnitudes of the HSC quasars lie in the range of $-26$ to $-22$. The faintest UV magnitude is $\sim 4$ mag fainter than that of the SDSS quasars selected at $z \sim 4$ by Akiyama et al. (2018). The contamination rate of the HSC quasars is $<40\%$ at $i < 23.5$, and $>50\%$ at $i > 23.5$. We confirm that our results do not change, even if the sample is limited to bright quasars with $i < 23.5$ (Section 3). The completeness is higher than $80\%$ at $i < 23.0$ and decreases to $\sim 40\%$ at $i = 24$. Note that the survey area is wider than that of our g-dropout galaxies.

#### 2.4. Cross-matched Effective Area

We cross-match the effective areas used in the protocluster and quasar searches to examine their possible correlation fairly. As a result, a cross-matched effective area of $\sim 98$ deg$^2$ is established. In total, 146 protoclusters (210,627 g-dropout galaxies with $i < 25.0$) and 570 HSC quasars in the effective area are obtained. As the redshift distribution of the HSC quasars is slightly narrower than that of the g-dropout galaxies, as illustrated in Figure 1, we aim to determine not whether the g-dropout overdense regions host the HSC quasars, but whether the number density environments around the HSC quasars are overdense regions.
3. Results

3.1. Overdensity Distribution around Quasars

We derive the distribution of the local maxima of the overdensity significances within a typical protocluster radius centered on the HSC quasars. This simple approach is sufficient to understand whether or not the quasars reside in the protoclusters. Note that in this approach, we cannot assess the possible local clustering signal within \(<1/8\) radius from the quasars, as the overdensity significances are calculated by using apertures with a radius of \(1/8\).

The distributions of the maximum overdensity significances within circles with radii of \(a = 1'\) centered on the quasars and random points are illustrated in the upper panel of Figure 2. Here, the random points are 570 points distributed uniformly on the cross-matched effective area, and their overdensity significance distribution is estimated by taking the average of 10,000 realizations. We find that the HSC quasars tend to reside in denser regions than the random points. In fact, the \(P\)-value in the Kolmogorov–Smirnov (KS) test for their distributions is estimated to be \(\sim 0\).

To obtain a quantitative understanding of the number density-based environment of the HSC quasars, we also compare the overdensity distributions around the HSC quasars with those around the g-dropout galaxies. The probability distribution of the maximum overdensity significances within the \(a = 1'\) radius centered on the g-dropout galaxies is also depicted in the upper panel of Figure 2. The overdensity significance distribution of the quasars is found to be significantly the same as that of the g-dropout galaxies. Their KS test \(P\)-value is 0.09. This result implies that the clustering strength of quasars and g-dropout galaxies is similar at least at the scales probed herein (i.e., \(1/8\) and \(3'\)).

As shown in Figure 3, we also find that only 4 out of 570 (=\(0.7\pm 0.4\)\%), where the error is assumed as Poisson error) HSC quasars are associated with the \(>4\sigma\) overdense regions within \(1/8\) separation.\(^{13}\) The positions of the protoclusters associated with the quasars are summarized in Table 1. Among the 570 randomly selected g-dropout galaxies, the fraction of those associated with the \(>4\sigma\) overdense regions within the separation radius of \(1/8\) is \(0.5\pm 0.3\%\). Here, the error is estimated by random sampling with replacement of the 570 g-dropout galaxies 10,000 times (bootstrap method). As a result, this ratio is the same as that of the HSC quasars within \(1\sigma\) error. This

\(^{13}\) Additionally, \(2.3\pm 0.6(10\pm 1.3)\%\) of the HSC quasars, are associated with the overdense regions with \(>5\sigma\ (>2\sigma)\) overdensity significances within \(1/8\) separation.
suggests that the HSC quasars do not preferentially appear in the richest protoclusters.

Note that the radial size of the protocluster at $z \sim 4$ could extend to a maximum of $\sim 3'0$ (Chiang et al. 2013). Even if we use a radius of $a = 3'0$ (1.2 pMpc) to evaluate the local maximum distribution of the overdensity significance, no significant difference of the overdensity significance distributions between the quasars and the $g$-dropout galaxies is found, as indicated in the lower panel of Figure 2. The KS test $P$-value for their distributions is 0.15. Moreover, only 22 out of 570 ($=3.9^{+0.8}_{-0.5}\%$) quasars reside in the $>4\sigma$ overdense regions.

Again, the ratio is consistent with that of the $g$-dropout galaxies within $1\sigma$ error; among the 570 randomly selected $g$-dropout galaxies, the fraction of those associated with the protoclusters within the $3/0$ separation is $4.4^{+0.9}_{-0.75}\%$. The results do not change even if the HSC quasar sample is limited to $i < 23.5$ bright ones as shown in Figure 2.

In our analysis, we can ignore quasar contaminants in the $g$-dropout galaxy sample as the quasar fraction of the $g$-dropout galaxies is only $\sim 0.01$. Here, this value is estimated by using the $g$-dropout luminosity function, $f$, and the galaxy fraction, $w$, given by Ono et al. (2018), and taking a weighted-average of $(1-f)$ with weight $w$ on a magnitude range of $i < 25$. In fact, even if we use a subsample of the faintest $g$-dropout galaxies with $i > 24$, where the quasar contamination is much lower (Ono et al. 2018), to measure the overdensity distribution, our results do not change (Figure 2).

3.2. Stacking Overdensity Maps around Quasars

We stack overdensity significance maps around the HSC quasars and the $g$-dropout galaxies with a radial scale of $10'$ ($\sim 4$ pMpc) to examine the possible difference in the galaxy density environments between the HSC quasars and $g$-dropout galaxies at any scale. Figure 4 presents the radial profiles of the stacked overdensity significance maps centered on the HSC quasars and the $g$-dropout galaxies. For a fair comparison of their density environments, we exclude the 570 HSC quasars from the $g$-dropout galaxy sample. We find that the galaxy density profile around the HSC quasars is statistically identical to that of the $g$-dropout galaxies at all scales within a 95% confidence interval.
Figure 4. Stacked radial profile of overdensity significance distribution centered on HSC quasars/g-dropouts. The blue points indicate the stacked overdensity profile of the HSC quasars. The green points, which are offset by +0.25σ over the horizontal axis for improved visualization, indicate those of all g-dropout galaxies. The error bars represent the 95% confidence interval based on the standard error of the mean of the overdensity significances in each bin. The logarithmic and the linear scale of the vertical axis are shown in the top and bottom panels respectively.

4. Discussion

4.1. Environment and Halo Mass of the Quasar at \( z \sim 4 \)

We found that 4 (22) out of the 570 HSC quasars; that is, 0.72% (3.94%) of the HSC quasars, are associated with the overdense regions with >4σ overdensity significances within 1.8 (3.0) arcmin separation at \( z \sim 4 \) (but see the caveat explained in Section 4.2). Now, we need to confirm that this ratio is consistent with the perspective of the quasar halo mass.

We use the extended Press–Schechter (EPS) model (Press & Schechter 1974; Bond et al. 1991; Bower 1991; Lacey & Cole 1993) to examine whether or not the quasar halos at \( z \sim 4 \) evolve into the cluster halos at \( z \sim 0 \), or, in other words, their quasars can belong to protoclusters at \( z \sim 4 \). According to the EPS model, the conditional probability \( P_2(M_{12}, z_2|M_{11}, z_1) \) that a halo with a mass of \( M_{11} \) at a redshift of \( z_1 \) evolves into a halo with a mass of \( M_{12} \) at a later redshift of \( z_2 \) is estimated as follows (Hamana et al. 2006):

\[
P_2(M_{12}, z_2|M_{11}, z_1) \, dM_{12} = \frac{1}{\sqrt{2\pi} \delta c_1 \delta c_2} \left[ \frac{\sigma_1^2}{\sigma c_1^2 - \sigma c_2^2} \right]^2 \exp \left[ -\frac{1}{2} \frac{(\sigma c_1^2 - \sigma c_2^2)^2}{\sigma_1^2 \sigma c_1^2 - \sigma_2^2} \right] \, d\sigma c_2 \, dM_{12},
\]

(11)

where \( \delta c_1 \) and \( \delta c_2 \) are the rms density fluctuation smoothed over spheres of a mass of \( M_{11} \) at \( z_1 \) and the critical overdensity threshold to collapse at \( z_1 \), respectively. Subsequently, the conditional mass function \( n_2(M_{12}, z_2|M_{11}, z_1) \) is estimated from

Equation (11) (Hamana et al. 2006):

\[
n_2(M_{12}, z_2|M_{11}, z_1) \, dM_{12} \propto \frac{1}{M_{12}} P_2(M_{12}, z_2|M_{11}, z_1) \, dM_{12},
\]

(12)

He et al. (2018) estimated the average halo masses of \( 1.46^{+1.71}_{-1.01} \times 10^{12} h^{-1} M_\odot \) for the HSC quasars at \( z = 3.9^{+0.4}_{-0.3} \) by means of clustering analysis. We set \( M_{11} = 1.46^{+1.71}_{-1.01} \times 10^{12} h^{-1} M_\odot, \ z_1 = 3.9^{+0.4}_{-0.3}, \) and \( z_2 = 0.0 \). Thereafter, the halo mass distribution at \( z = 0 \) can be calculated from Equations (11) and (12). We find that 8.4%–14.6% of the halos with a mass of \( 1.46^{+1.71}_{-1.01} \times 10^{12} h^{-1} M_\odot \) at \( z = 3.9 \) are expected to evolve into halos with a mass of \( >10^{14} h^{-1} M_\odot \) at \( z = 0 \). The ratio is almost the same, with 1.2σ (0.7σ) significance, as that of the HSC quasars associated with the >4σ overdense regions out of the entire sample within 1.8 (3.0) arcmin separation. This means that our findings are consistent with the expected halo mass growth.

4.2. Signal Dilution Over Redshift Space

Our overdense region sample exhibits high incompleteness owing to the large redshift error of the g-dropout galaxies (Section 2.2). We quantitatively evaluate to what extent the possible clustering signals around the HSC quasars are diluted by this projection effect.

A quasar is assumed to exist in a typical protocluster-scale cylinder, with a diameter of 1.5 (1 + \( z \)) comoving Mpc (cMpc) along the celestial sphere direction and a height of 1.5 (1 + \( z \)) cMpc along the line-of-sight (LoS) direction at \( z = 3.9 \), which corresponds to the median redshift of the HSC quasars. The cylinder space is assumed to be an overdense region with \( n \) times the average galaxy density (cMpc\(^{-3}\)) at the cylinder scale. By integrating the g-dropout selection function (Figure 1), the redshift window width of the g-dropout galaxy is estimated to be >10 times the cylinder scale (protocluster scale) along the LoS direction. Thus, a cylinder with \( n > 20 \) times the average density can be achieved for our >4σ overdense regions, using the definition of the overdensity significance (\( N-N \))/\( \sigma \) (Section 2.2). Conversely, if the vicinity of a quasar is an overdense region with < 20 times the average density, the density region is not detected as our protocluster sample. This implies that few >4σ overdense regions (the most prominent ones) are detected (the completeness is ~6%; see Section 2.2), and therefore, a higher fraction of quasars may be associated with protoclusters.

4.3. Comparison with SDSS Luminous Quasars

In order to examine the possible dependency of the quasar environments on their luminosities, we compare our findings with the results of U18, in which the g-dropout galaxy number density environments of luminous quasars at \( z \sim 4 \) were investigated by using HSC-detected protoclusters. The method for selecting the g-dropout galaxies and the protoclusters were the same as in the present study. The quasars were extracted from the SDSS quasar catalog based on SDSS DR12 (Pâris et al. 2017). The SDSS DR12 quasar catalog is the final SDSS-III quasar catalog, which contains 297,301 spectroscopically confirmed quasars over a wide redshift range of 0.041 < \( z < 6.440 \) in an area covering approximately 10,200 deg\(^2\).
of the sky. A total of 151 SDSS quasars are found in the effective areas of the HSC protocluster search within the g-dropout redshift range of \( z = 3.3-4.2 \). The UV absolute magnitudes of this sample are brighter than \( \sim -26 \). For details, please refer to U18.

We find that our results in the present study support our previous study of U18; 2 and 3 out of 151 SDSS quasars (1.3\(^{+0.9}_{-1.1}\)% and 2.0\(^{+1.1}_{-1.1}\)%), where these errors are assumed to be Poisson errors) are found to be spatially associated with the \( >4\sigma \) overdense regions within 1/8 and 3/0 separations, respectively. Their ratios are consistent, within a 1\( \sigma \) error, with the case of the HSC quasars. This fact suggests that the number densities of the g-dropouts around the quasars are expected to be independent of their luminosity over a wide range of their UV absolute magnitudes, \( M_{\nu} = -28 \sim -22 \). This may arise from the fact that the halo mass is almost independent of the quasar luminosity (e.g., Eftekhary et al. 2015). In fact, He et al. (2018) found that the halo masses of the HSC quasars were consistent with those of the SDSS quasars.\(^{13} \)

4.4. Environment of Quasar Pairs at \( z \sim 4 \)

As illustrated in Figure 3, two out of the four HSC quasars associated with the \( >4\sigma \) overdense regions, namely QSO1 and QSO2, could constitute possible quasar pairs with their projected separations of 9/6 (\( \sim 4 \) pMpc). In Onoue et al. (2018), a quasar pair was defined as two quasars with their separation closer than the size of massive protoclusters that are expected to evolve into the descendant halos with halo masses of \( 10^{15} M_{\odot} \) at \( z = 0 \). Concretely, they extracted the quasar pairs with their projected proper distance of \( R_{\perp} < 4 \) pMpc and velocity offset of \( \Delta V < 3000 \text{ km s}^{-1} \). We define the two quasars with their projected proper distance \( R_{\perp} < 4 \) pMpc as the “possible quasar pairs,” as we have no information regarding the velocity offset in the HSC quasar sample. Our finding is likely to relate to the results found in the SDSS quasars by Onoue et al. (2018), whereby the SDSS quasar pairs tended to reside in the galaxy overdense regions at \( z \sim 4 \). Spectroscopy is required for our possible quasar pairs to confirm the reality of the quasars and to measure their redshift differences.

4.5. Triggering Mechanism of Quasar

Our findings show no preference of quasar activity in the \( z \sim 4 \) richest protocluster environment, where gas-rich galaxy major mergers are expected to occur frequently (e.g., Gottlöber et al. 2001; Stewart et al. 2009; Jian et al. 2012; Hine et al. 2016). This fact is likely to be against the simple expectation that almost all gas-rich major mergers result in quasars. We show some implications for our results below.

First, the major merger rates in our protocluster regions may not be so high that we cannot confirm the enhancement in our statistical accuracy. The projection effect discussed in Section 4.2 prevents the detection of the possible enhancement. The major merger rates can be diluted to be \( <0.1 \) times owing to the effect. Using Hubble Space Telescope imaging combined with spectroscopic observation for the quasar-hosted protoclusters is necessary to estimate the exact merger rates (Hine et al. 2016).

Second, if the major mergers occur with nonnegligible probability in the protocluster regions, they may not appear through the major mergers but secular processes (e.g., Fanidakis et al. 2012). Several recent observations have provided no evidence that quasar activity is enhanced by major mergers. Mechtley et al. (2016) examined whether or not quasar hosts exhibit distortions owing to major mergers by comparing 19 quasar host galaxies to 84 inactive galaxies at \( z \sim 2 \). These authors found that there was no significant difference in the distortion fractions between the quasar hosts and inactive galaxies, meaning that the triggering mechanism of the quasars was not always a major merger. According to Yang et al. (2018), the accretion rates of SMBHs are strongly dependent on the stellar masses of the host galaxies, independently of their sub-Mpc or global 1–10 Mpc scale environment. Ricarte et al. (2019) also found that the relation between the black hole accretion rate and star formation rate does not depend on the host galaxy environments, and identified no evidence of a connection between black hole growth and galaxy mergers (but see Yoon et al. 2019). Trakhtenbrot et al. (2017) determined diverse host galaxy properties of luminous quasars at \( z \sim 5 \) in terms of SMBH fueling mechanisms, suggesting that a galaxy merger may not be a necessary condition for either process, and other mechanisms that are not related to major mergers may drive the rapid growth of the most massive BHs. Ito et al. (2019) recently found that extreme UV-bright galaxies that are expected to have experienced a starburst phase caused by frequent mergers exist in our protocluster regions. Third, our optical observation might miss some quasars in the rich protoclusters owing to the quasars being in the dust-obscured phase, which appears immediately after experiencing a major merger (Hopkins et al. 2008). Recently, Kubo et al. (2019) stacked the Planck images of the same HSC protocluster regions as those used in the present study, and found a significant (>5\( \sigma \)) excess at mid-IR wavelengths, suggesting that the richest protoclusters at \( z \sim 4 \) may also contain a significant population of obscured AGN. Combining these results with our findings appears to be challenging for the merger scenario (e.g., Hopkins et al. 2008), which predicts that quasars are the descendants of obscured AGNs. This study combined with that of Kubo et al. (2019) simply leads to the inconsistent argument that the progenitors and descendants are not in the same environment, although many uncertainties should be taken into account, such as the quasar duty cycle, and the duration between the major merger and quasar activation. Perhaps not all obscured AGNs will evolve into quasars. Moreover, some of them tend to evolve into high-\( z \) radio galaxies (HzRGs) in the most overdense regions (the most massive halos) because frequent mergers build up spins of the SMBHs and cause them to launch radio jets (Fanidakis et al. 2013; Hatch et al. 2014; Orsi et al. 2016). The quasar activity, which is maintained by the gas cooling and accretion onto a central SMBH, will be suppressed by radio-mode feedback in a massive halo (e.g., Fanidakis et al. 2013). As a result, HzRGs are expected to be associated with the richest protoclusters. Clustering measurements are absolutely essential for exact interpretations of the major merger scenario. We will conduct the clustering analysis of HzRGs and protoclusters based on the HSC-SSP data in forthcoming research.

\(^{13}\) For example, using the maximum likelihood method fitting to a power-law model, the halo masses of the HSC quasars and the SDSS quasars were estimated to be $\log M_\text{h}/10^{15} M_\odot = 12.20^{+0.33}_{-0.40}$ and $\log M_\text{h}/10^{15} M_\odot = 11.43^{+0.18}_{-0.20}$, respectively. For details, please refer to He et al. (2018).
One should refer to the possible enhancement of quasar activity due to cosmic cold gas. Cosmic cold gas inflow in the early universe could also provide a significant amount of gas supply to the SMBHs preferentially in large-scale overdense environments, so that quasar activity could be enhanced in the overdense regions in contrast to our observational results (e.g., Kereš et al. 2005; Dekel & Birnboim 2006; Di Matteo et al. 2008; Ocvirk et al. 2008; Sijacki et al. 2009; Costa et al. 2014). According to Dekel & Birnboim (2006), cold streams at \( z > 2 \) should still not be fully disrupted in rare massive halo objects with \( >10^{12} M_{\odot} \), even if they are diluted by a hot medium heated by quasar feedback. However, recent cosmological hydrodynamic simulations (e.g., Di Matteo et al. 2008) demonstrated that strong feedback on massive halos with \( >10^{12} M_{\odot} \), at \( z \sim 6 \) stop the cold stream to penetrate into the central BH. These authors mentioned that even at \( z < 6 \) in massive halos the feedback energy clearly affects the inflowing cold gas.

5. Conclusion

We examined the \( g \)-dropout galaxy overdensity distribution around 570 faint quasar candidates (HSC quasars) at \( z \sim 4 \). The possible correlation between the \( g \)-dropout overdense regions, especially protoclusters and the HSC quasars was examined. The protoclusters constructed by Toshikawa et al. (2020) were de

from the JSPS (grant 20K14530). R.A.O. received support from CNPq and the Visiting Scholar Program of the Research Coordination Committee of the National Astronomical Observatory of Japan (NAOJ).

This work was based on data collected by the Subaru Telescope and retrieved from the HSC data archive system, which is operated by the Subaru Telescope and Astronomy Data Center at the NAOJ.

The HSC collaboration includes the astronomical communities of Japan and Taiwan, and Princeton University. The HSC instrumentation and software were developed by the NAOJ, the Kavli Institute for the Physics and Mathematics of the Universe (Kavli IPMU), the University of Tokyo, the High Energy Accelerator Research Organization (KEK), the Academia Sinica Institute for Astronomy and Astrophysics in Taiwan (ASIAA), and Princeton University. Funding was provided by the FIRST program from the Japanese Cabinet Office, the Ministry of Education, Culture, Sports, Science and Technology (MEXT), the Japan Society for the Promotion of Science (JSPS), the Japan Science and Technology Agency (JST), the Toray Science Foundation, NAOJ, Kavli IPMU, KEK, ASIAA, and Princeton University.

This study made use of software developed for the Large Synoptic Survey Telescope (LSST). We thank the LSST Project for making their code available as free software at http://dm.lsst.org.

The Pan-STARRS1 Surveys (PS1) have been made possible through the contributions of the Institute for Astronomy, the University of Hawaii, the Pan-STARRS Project Office, the Max-Planck Society and its participating institutes: the Max Planck Institute for Astronomy, Heidelberg and the Max Planck Institute for Extraterrestrial Physics, Garching, Johns Hopkins University, Durham University, the University of Edinburgh, Queens University Belfast, the Harvard-Smithsonian Center for Astrophysics, the Las Cumbres Observatory Global Telescope Network Incorporated, the National Central University of Taiwan, the Space Telescope Science Institute, the National Aeronautics and Space Administration under grant No. NNX08AR22G, issued through the Planetary Science Division of the NASA Science Mission Directorate, the National Science Foundation under grant No. AST-1238877, the University of Maryland, and Eotvos Lorand University (ELTE) and the Los Alamos National Laboratory.

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We thank the referee for helpful comments that improved the manuscript. N.K. acknowledges support from the JSPS (grant 15H03645). T.N. acknowledges support from the JSPS (grants 16H03958, 19H00697, 20H01949). M.K. acknowledges support
