CNN-AIDED FACTOR GRAPHS WITH ESTIMATED MUTUAL INFORMATION FEATURES FOR SEIZURE DETECTION

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ABSTRACT
We propose a convolutional neural network (CNN) aided factor graphs assisted by mutual information features estimated by a neural network for seizure detection. Specifically, we use neural mutual information estimation to evaluate the correlation between different electroencephalogram (EEG) channels as features. We then use a 1D-CNN to extract extra features from the EEG signals and use both features to estimate the probability of a seizure event. Finally, learned factor graphs are employed to capture the temporal correlation in the signal. Both sets of features from the neural mutual estimation and the 1D-CNN are used to learn the factor nodes. We show that the proposed method achieves state-of-the-art performance using 6-fold leave-four-patients-out cross-validation.

1. INTRODUCTION
Epilepsy is a highly common neurological disorder, causing recurrent episodes of the involuntary movement known as epileptic seizures [1]. Based on the place in the brain where seizure starts and the intensity of the abnormal signals, patients with epilepsy may suffer from different symptoms such as auras, repetitive muscle contraction, and loss of consciousness. [2]. Epileptic seizure severely affects the patient’s quality of life and can have other social and economic impacts; for instance, some activities, including swimming, bathing, and climbing a ladder, become dangerous as a seizure during that activity might result in unpredictable injuries and even death. Therefore, early detection of epilepsy can notably improve the patient’s quality of life. A leading tool to diagnose seizure is based on electroencephalogram (EEG) monitoring, being economical, portable, and non-invasive [3]. However, the review of EEG recordings is a time-consuming expert-dependent process due to contamination by physiological and non-physiological resources [4], and similarity of epileptic spikes to normal EEG waveforms.

The challenges associated with EEG monitoring gave rise to a growing interest in machine learning aided automatic seizure detection. A common approach is to train a model, typically a convolutional neural network (CNN), applied to features extracted from the Wavelet or Fourier transform of the signal [5–10], typically involving careful feature engineering. Other seizure detection methods process the raw EEG signals directly. We then use a 1D-CNN to extract extra features from the EEG signals and use both features to estimate the probability of a seizure event. Finally, learned factor graphs are employed to capture the temporal correlation in the signal. Both sets of features from the neural mutual estimation and the 1D-CNN are used to learn the factor nodes. We show that the proposed method achieves state-of-the-art performance using 6-fold leave-four-patients-out cross-validation.

2. PROBLEM STATEMENT AND PRELIMINARIES
2.1. Seizure Detection Problem
In this paper, seizure detection refers to the identification and localization of the ictal (i.e., the seizure) time intervals from EEG recordings of patients with epilepsy [21]. To formulate this mathematically, let \( X = \{X_1, X_2, \ldots, X_N\} \) be the EEG recordings of a patient, where \( N \) represents the number of channels. Each measured channel \( X_i \) is comprised of \( n \) consecutive blocks, e.g., blocks of 1-second recordings, and we write \( X_i = [x_i^{(1)}, x_i^{(2)}, \ldots, x_i^{(n)}] \), where \( x_i^{(t)} \) is the signal corresponding to the \( t \)-th EEG channel during the \( i \)-th
block. The seizure state for each block is represented as a binary vector \( s = [s_1, \ldots, s_n] \), where \( s_t \in \{0, 1\} \) models whether or not a seizure occurs in the \( t \)-th block. Our goal is to design a system which maps the EEG recordings \( X \) into an estimate of \( s \), which is equivalent to finding the time indices where seizure occurs.

To model the relationship between the EEG signals \( X \) and the seizure states \( s \), it is needed to consider both inter-channel correlation as well as temporal correlation that the recordings exhibit. The former stems from the fact that when the seizure starts, the epileptic activity propagates to other areas in the brain [22] which affects the patterns of other channel recordings [23]. This manifests high dependence between different channels, i.e., between \( x_i^{(t)} \) and \( x_j^{(t)} \), when \( t \) is at the beginning and during ictal phase. Temporal correlation results from the fact that seizures typically span multiple recording blocks, and thus the probability of observing a seizure at time instance \( t \) depends on the presence of a seizure in the previous block, such that the entries of \( s \) can be approximated by a Markovian structure [16]. Our proposed solution, detailed in Section 3, exploits this statistical structure using factor graphs.

2.2. Factor Graph Inference

Factor graphs are a representation of factorizable multi-variable functions, such as probability distributions, as a bipartite graph. These graphical models facilitate inference at reduced complexity via message passing algorithms, such as the sum-product methods [24]. Consider an observed sequence \( Y = [y_1, \ldots, y_n] \) encapsulating a latent state sequence \( s = [s_1, \ldots, s_n] \) whose entries take values in a finite set \( S \), as a form of a hidden Markov model (HMM). In such cases, the joint distribution of \( y, s \) obeys

\[
P(s, y) = \prod_{k=1}^{n} P(s_k | s_{k-1}) P(y_k | s_k), \tag{1}
\]

which can be represented as factor graph with variable nodes \( \{s_k\}_{k=1}^{n} \) and function nodes \( \{f_k\}_{k=1}^{n} \), where \( f_k(s_k, s_{k-1}) := P(s_k | s_{k-1}) P(y_k | s_k) \).

The factor graph representation allows one to compute the maximum a-posteriori probability (MAP) decision rule with a complexity that only grows linearly with \( n \) as opposed to exponentially with \( n \). This is achieved by evaluating the marginal distribution \( P(s_k, y) \) for each \( k \in \{1, \ldots, n\} \) via message passing over the factor graph. In this case, the forward messages are recursively updated via

\[
\mu_{f_k \rightarrow s_k}(s_k) = \sum_{\{s_1, \ldots, s_{k-1}\}} \prod_{j=1}^{k} f_j(s_j, s_{j-1}), \tag{2}
\]

and the backward messages via

\[
\mu_{f_{k+1} \rightarrow s_k}(s_k) = \sum_{\{s_{k+1}, \ldots, s_n\}} \prod_{j=k+1}^{n} f_j(s_j, s_{j-1}). \tag{3}
\]

Then, the desired marginal distribution, which is maximized by the MAP rule, is given by

\[
P(s_k, y) = \mu_{f_k \rightarrow s_k}(s_k) \cdot \mu_{f_{k+1} \rightarrow s_k}(s_k). \tag{4}
\]

Intuitively (2)-(3) are interpreted as an aggregate of neighboring information. Once all neighbors have communicated (i.e., messages have propagated the entirety of the graph) the product of the forwards and backward messages determines the marginal probability.

3. MICAL Seizure Detection Algorithm

In this section, we present the proposed MICAL algorithm. MICAL is comprised of three main components: neural MI estimator quantifying the instantaneous dependence between different channels at each EEG block to capture the inter-channel correlation (see Subsection 3.1); a 1D CNN which generates a latent representation of the raw EEG block plus a soft estimate of the seizure state using the joint features from the 1D-CNN and the neural MI estimator (see Subsection 3.2); and factor graph inference utilizing the soft estimates as learned function nodes to incorporate temporal correlation (see Subsection 3.3). A high-level illustration of the flow of MICAL is depicted in Fig. 1.

3.1. Neural Mutual Information Estimation

MI is a measure of the statistical dependence between two random variables. While cross-correlation measures linear dependence, MI can capture higher-order statistical dependence [25], and is thus able to capture nonlinear relationship between signals, which is likely to exist between EEG signals during seizure [22, 23]. The MI between the random variables \( x_1, x_2 \) taking values in \( \mathcal{X} \times \mathcal{X} \) with a joint distribution \( P_{X_1 X_2} \) and marginals \( P_{X_1} \) and \( P_{X_2} \) is defined as

\[
I(X_1; X_2) = D_{KL}(P_{X_1 X_2} \parallel P_{X_1} P_{X_2}), \tag{5}
\]

where \( D_{KL} \) is the Kullback-Leibler (KL) divergence.

Using (5) to compute MI as a measure of statistical dependence for EEG samples, with unknown probability distributions is a challenging task [26]. To address this issue, it was recently shown that neural networks can be trained to estimate MI, based on the Donsker-Varadhan representation

\[
D_{KL}(P_{X_1 X_2} \parallel P_{X_1} P_{X_2}) = \sup_{T: X \rightarrow Y} E_{P_{X_1 X_2}}[T(x_1, x_2)] - \log \left( E_{P_{X_1} P_{X_2}} \left[ e^{T(x_1, x_2)} \right] \right), \tag{6}
\]

where a neural model with parameters \( \phi \) denoted by \( T_\phi \) is used to represent the function \( T \) in (6). To maximize the right hand side of (6) gradient descent can be used to find the maximizing set of parameters \( \phi \) [27]. To overcome the limitations imposed by the estimation variance, [28] proposed the Smoothed MI Lower-bound Estimator (SMILE), which learns to estimate MI by training a neural network to maximize the objective function

\[
\hat{I}_\phi(X_1; X_2) = E_{P_{X_1 X_2}}[T_\phi(x_1, x_2)] - \log E_{P_{X_1} P_{X_2}} \left[ \text{clip}(e^{T_\phi(x_1, x_2)}, e^{-\tau}, e^\tau) \right], \tag{7}
\]

where \( \text{clip}(v, l, u) := \max\{\min(v, u), l\} \) and \( \tau \) is a hyperparameter.

The resulting neural estimator was shown to learn to reliably predict MI under various distributions.

In MICAL, we apply SMILE to estimate \( I(x_i^{(j)}; x_j^{(i)}) \) at each EEG block \( t \) for each channel pair \( i, j \). Since MI is symmetric, i.e., \( I(x_i^{(j)}; x_j^{(i)}) = I(x_j^{(i)}; x_i^{(j)}) \), we only estimate the MI for \( j > i \). We set \( T_\phi \) to be a fully-connected network with two hidden layers and ReLU activations, and train it with \( \tau = 0.9 \) in the objective (7). The numerical results from neural estimator satisfy the underlying hypothesis of high correlation among recordings during seizure state. This is illustrated in Fig. 2, where it is observed that the trained estimator outputs higher MI values during seizure compared to non-seizure blocks.
resented as an HMM. Similar modelling was shown to faithfully reproduce the probability of the presence of a seizure, thereby enabling the prediction of future seizures.

3.2. 1D CNN

In parallel to the neural MI estimator, each raw EEG signals block is also processed using a dedicated 1D CNN to extract relevant features from the block. The resulting vector $y_t$, representing the stacking of these extracted features and the estimated MI at EEG block $t$, is used to produce a probabilistic estimate of the presence of a seizure. We develop a 1D CNN architecture to extract meaningful features from raw EEG signals and combine these features with the MI estimation results. Compared to 2D CNNs; specifically, the baseline model proposed by Boonyakitanont et al. [12], 1D CNN can evaluate all EEG channels at a given time instance, but in 2D CNNs only the channel indexes that are close together are processed together.

To have a comparable configuration with the baseline model, we use the same number of filters. Unlike previous studies, we design the kernel size such that our 1D CNN will have a high receptive field of 1 second of the recording, compared to approximately 33 ms in prior works. This feature of the architecture leads to capturing low-frequency components of the signals and long-term temporal correlation within the 4-second blocks in EEG signals. The details of the proposed CNN model is shown in Fig 1.

3.3. Factor Graph Inference

The resulting seizure state probability using only the MI estimates and the features from 1D CNN does not exploit the presence of temporal correlation. Therefore, as proposed in [17] for sleep state tracking, we exploit the presence of temporal correlation by utilizing the block-wise soft decisions not for prediction, but as learned function nodes in a factor graph. We incorporate temporal correlation by assuming that the relationship between the extracted features $y_1, \ldots, y_n$ and the underlying seizure state $s_1, \ldots, s_n$ can be represented as an HMM. Similar modelling was shown to faithfully capture the temporal statistics in EEG-based seizure detection [16]. For such models, one can compute the MAP rule with linear complexity using sum-product inference over the resulting factor graph, as described in Subsection 2.2. However, to evaluate the messages (2)-(3), one must be able to compute the function nodes $\{f_k\}_{k=1}^n$, given by

$$ f_k(s_{tk}, s_{tk-1}) = P(s_{tk} | s_{tk-1})P(y_{tk} | s_{tk}). \ (8) $$

In MICAL, we utilize the block-wise soft decisions as estimates of the conditional distribution $P(y_{tk} | s_{tk})$. The transition probability $P(s_{tk} | s_{tk-1})$, which is essentially comprised of two values, can be obtained from histogram, or manually tuned as we do in our numerical study in Section 4. The obtained marginal distributions (4) are compared to a pre-defined threshold $T$ for detection. The resulting seizure detection algorithm is summarized as Algorithm 1.

Algorithm 1: MICAL seizure detection

| Step | Description |
|------|-------------|
| 1 Inputs: | SMILE and 1D CNN networks, estimated $P(s_{tk} | s_{tk-1})$, EEG signals $X$, threshold $T$ |
| 2 Feature extraction: | for $k = 1, \ldots, n$ do |
| 3 | Compute $\{f_k\}$ from soft decisions via (8); |
| 4 | Apply 1D CNN to obtain combined features $y_{tk}$ and obtain soft decision; |
| 5 | end |
| 6 Factor graph inference: | Compute $\mu_{f_{tk} \rightarrow s_k} \{0, 1\}$ via (2); |
| 7 | Compute $\mu_{f_{tn-k+2} \rightarrow s_{n-k+1}} \{0, 1\}$ via (3); |
| 8 | end |
| 9 Detect seizure at $t_k$ if $\mu_{f_{tk} \rightarrow s_k}(1) \mu_{f_{tk+1} \rightarrow s_k}(1) > T$. |

4. NUMERICAL RESULTS

We evaluate MICAL\footnote{The source code and hyper-parameters can be found on GitHub.} using the CHB-MIT dataset [20]. The data is comprised of scalp EEG recordings from 24 pediatric subjects with intractable seizures, sampled at a frequency of 256 Hz where seizure start and end times are labeled. In order to balance and denoise the dataset, few simple pre-processing steps are included. Sample recordings with at least one seizure are selected and a notch filter is applied to remove the noise from power line. Due to the short...
seizure duration, for each recording file, we reduce non-seizure samples to 10 times before and 10 times after seizure time. Therefore, for every second of seizure data, there are 20 seconds of non-seizure data. The seizures are estimated for every second. To estimate the probability of seizure over the t-th second, the past 32 seconds of recording is used to solve the optimization that estimates MI. This window size has demonstrated the best results over the dataset. The past 4 seconds of recording is used as input to the 1D CNN for estimating the features. The value of 4 seconds is selected to satisfy a good trade-off between the number of samples in a block and the stationarity of the observed signals over a block. In our experiments, seven models are used for comparison. The 2D CNN used in [12] and spectrogram detector of [10] as two baseline models since they reported the best results compared to prior works. For MICAL, we tune the transition probability to $P(s_t = 1|s_{t-1} = 1) = 89.54\%$ and $P(s_t = 1|s_{t-1} = 0) = 17.90\%$. To evaluate the contribution of each individual component of MICAL, we conduct a complete ablation study. We predict seizure probability based solely on input block through 1D CNN features as well as combined features from MI estimator and CNN. We also add two different structures, including GRU cells and factor graph to the 1D CNN features to exploit temporal correlation without incorporating the inter-channel correlation. All detectors use decision threshold of $T = 0.5$.

For considering variability among patients, a 6-fold leave-4-patients-out evaluation is conducted. To examine the performance of the proposed hybrid algorithm, three metrics are measured: area under ROC curve (AUC-ROC) which shows the capability to distinguish between seizure and non-seizure samples, area under precision recall curve (AUC-PR) that is the indicative of success and failure rates, and F1 score representing the harmonic mean between precision and recall.

The results for three performance measures are summarized in Table 1. The represented values for all metrics show the average across 6 folds. As presented in Table 1, the 1D CNN used by MICAL achieves almost 5% improvement compared with the baseline models, specifically for AUC-ROC and AUC-PR. As indicated, considering only temporal or inter-channel correlation has no significant effect on the model performance. Therefore, the incorporation of MI estimation and factor graph inference by MICAL yields the highest performance measures, 83.8% and 50.38% for AUC-ROC and AUC-PR, respectively and 93.42% for F1 score. The results indicate that our algorithm admits the hypothesis of existing high correlation among signals during seizure states. Furthermore, exploiting temporal correlations in a principled manner through factor graphs is shown to facilitate learning an accurate detector, compared to using a black-box RNNs, at a much reduced computational complexity.

|     | AUC-ROC | AUC-PR | F1 score |
|-----|---------|--------|----------|
| 2D CNN [12] | 77.81 ± 0.08 | 37 ± 0.17 | 88.3 ± 0.03 |
| Spectrogram [10] | 75.4 ± 0.11 | 37.66 ± 0.10 | 92.77 ± 0.09 |
| 1D CNN | 82.12 ± 0.04 | 42.23 ± 0.12 | 91.47 ± 0.02 |
| 2D CNN | 82.28 ± 0.03 | 44.43 ± 0.10 | 90.42 ± 0.06 |
| 1D CNN | 83.15 ± 0.05 | 44.50 ± 0.12 | 92.35 ± 0.02 |
| 1D CNN-SMILE | 83.10 ± 0.04 | 48.30 ± 0.11 | 92.47 ± 0.01 |
| MICAL | 83.85 ± 0.04 | 50.38 ± 0.13 | 93.42 ± 0.01 |

Table 1. Summary of results

5. CONCLUSION

We proposed MICAL, which is a data-driven EEG-based seizure detector designed to exploit both inter-channel and temporal correlations. For this, MICAL estimates the MI between each pair of EEG channels to capture the non-linear correlation among recordings observed during seizure times. The estimated MI is combined with a carefully designed 1D CNN to provide a soft estimate for each signal block. Instead of using these features for prediction, they are utilized to evaluate the function nodes of an underlying factor graph, allowing it to infer at linear complexity while exploiting temporal features between EEG blocks. We demonstrate that MICAL achieves notable improved performance compared to previously proposed methods.

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