Evaluation of Product Quality in QFD using Multi Attribute Decision Making (MADM) Techniques in Manufacturing Industry

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Abstract
Every customer wants to purchase the best quality product but the price factor is only the reason due to which most of customers compromise with quality. The main purpose of our study is to find a best suitable method which will be helpful to design such product having good quality with affordable price. Quality Function Deployment (QFD) is the most powerful method for analyzing the customer demands and selection of most important or valuable voice which has to be corrected or modified. The integrated approach of QFD and Optimization techniques (i.e. AHP, TOPSIS, PROMETHEE, etc.) can be used to analyze the product quality manufacturing industry. A QFD optimization methodology is formulated in this study with suitable illustrations and tried to find a best method of product design.

Keywords: Quality Function Deployment, PROMETHEE, AHP, TOPSIS, House of Quality.

1. Introduction
Each customer has different opinion about a product according to his/her demand. In present market many alternatives of many brands are available in the market. When customer feels a demand of anything, he tries to find the availability of such thing/product. Then he tries to search all alternatives available in market and also makes comparison between them. The decision to choose or select any brand is depends on many factors i.e. cost of product, brand name, economic condition of customer, etc. because most of customers try to reduce his expenses. If a product cost is around 20% more than of desired cost then customer can select such product to purchase.

It is not possible to fulfill each desire of customer but we can approach for most customer satisfaction using these techniques. The customer weights to each demand plays very important role and selection of most common weights from them is the most critical task. The optimization techniques are the best option to solve these problems.

QFD is the systemic approach to explore all possible needs of customer and also relate these needs technical parameters of the product.

In order to meet the customer expectations the manufacturing industries are looking for design a product under market oriented approach. QFD is the best approach to identify and prioritize the customer demands using House of Quality (HoQ). QFD introduced in late 1960s and early 1970s in Japan by Akao (1990) the primary functions of QFD at the beginning are product development, quality management and analysis of customer demand. With development, QFD areas expand into more broad areas such as Decision making, Planning, Operations and Engineering Design, among others.

Multilateral decisions (MADM) and multiple decision-making (MODM) are two fundamental aspects of MCDM. There are many methods in each of the mentioned views. Pohekar and Ramachand have emphasized that each method has its own characteristics and that the methods are classified as deterministic, stochastic and false methods. Carlsson and Fuller conducted a comprehensive MCDM study and were classified into four main categories. One category approaches the value and utility theory. This second category is formed by methods that develop different ways of evaluating the relative importance of various attributes and alternatives. Under this category, most of the methods were concentrated on weight determination. The Simple Additional Weighting (SAW), the analytical hierarchy process, the fuzzy conjunction / disjunctive methods, the outranking voluntary methods and the max-min methods. It seems that SAW and fuzzy simple additive weight (FSAW) methods are MCDM methods that use weight decisions and preferences. Churchman et al., the first study used the SAW method to address the portfolio selection problem. The SAW method is advantageous because it is a proportional linear transformation of raw data. This means that the relative order of the magnitude of the standardized scores is the same.

Afshari et al., SAW have been applied in the research to solve problems for Iranian workers. In this paper, the selection of workers is considered a real request, using expert opinion. The data used in this model were collected by five experts. A questionnaire for collecting data from telecommunication companies in Iran was used using scales ranging from 1 to 5. The authors used seven criteria, qualitative and positive, choosing five workers, later in the ranking.
AHP (Analytical Hierarchy Process) is a powerful tool for organizing and analyzing complex problems. In the 1970s Thomas Saaty developed AHP. According to the research, AHP has three steps to structure hierarchy, match comparison, synthesis of results (Saaty 1994, 2008). The AHP has the capacity to make decisions and to measure the coherence of performance (Triantaphyllou, 2000). In traditional AHP, last weightages calculated using vectors. Lootsma (1998) suggested that the values shown in the raw and column normalization are equivalent to the standard Eigen vector. Kwong & Ban (2002) proposed the hierarchy of analytical rigor to calculate the weight of the client's voice and propose a fuzzy-based model to calculate the customer's voices.

TOPSIS (Hwong & Yoon by Ideal Solution by Preliminary Order of similarity by preference) was developed in 1981. In this way, the classification of alternatives will be separated from Ideal Positive and Ideal Negative. The best option is to have the worst positive idea and have the worst negative ideals.

Baky and Abo-Sinna (2013) present TIPSIS to solve the problems of two modules. Rao (2006) proposed a model through the selection of material selection graph theory. Cheng (2008) presented an effective approach to solving TOPSIS in MCDM. Garcia-Cascales & Lamata (2012) Hawang & Yoon proposed the algorithms modified by the TOPSIS method. Zhang & Yo (2012) submit an extended TOPSIS ranking of all alternatives.

Karimi-Nasab and Seyedhoseini (2013) TOPSIS have been applied to the work index of the retail store's classification index. Khademi-Zare et al. FQFD presented two methods in the ranking of the strategic actions of Iranian telecommunication cellular technology, taking into account CA factors with AHP. The Fuzzy Factor was also included in these models. Chen and Tong present with the average weight of the light weight method. Gunasekaran et al. MCDM proposed the optimization of the supply chain using Monte Carlo simulation and FQFD.

2. Methodology
2.1 QFD
Quality Function Deployment (QFD) is a split tool for the development of products from customer needs, resulting in systematic technical specifications which are a guide to manufacturing activities. QFD translates customer needs into appropriate specifications within the company in each of its functional areas, research and development to engineering, production, distribution, sales and service.

2.2 Optimization Techniques
In each phase of optimization different techniques (i.e. SAW, WPS, AHP, TOPSIS, PROMETHEE) can be used. Ranking and priorities may be different for each situation.

2.2.1 Simple Additive Weighting (WAS) Method
SAW is the simplest and widest used method of MADM and this is also called weighted sum method[]. The overall performance score of an alternative is given as:

\[ P_i = \sum_{j=1}^{M} w_j m_{ij} \]

Normalize \( m_{ij} \)

\[ P_i = \sum_{j=1}^{M} w_j (m_{ij})_{normal} \]

Where \( P_i \) is overall score of alternative \( i \) (A\text{\scriptsize{i}}) and \((m_{ij})_{normal}\) represents normalized value of \( m_{ij} \). The highest value of \( P_i \) is considered best alternative among all.

The attributes can be beneficial or non beneficial.

For beneficial attributes normalized values can be calculated by

\[ \left( \frac{m_{ij}}{L} \right)_{K} \]

Where \( \left( \frac{m_{ij}}{L} \right)_{K} \) =L\text{\scriptsize{th}} alternative has the highest measure attribute out of all.

\[ \left( \frac{m_{ij}}{K} \right) = \text{Measure value of attribute for } K\text{\scriptsize{th}} \text{ alternative} \]

For non-beneficial attributes normalized values can be calculated by

\[ \left( \frac{m_{ij}}{L} \right)_{K} \]

Ranking equation:

\[ P_i = \left[ \frac{\sum_{j=1}^{M} w_j (m_{ij})_{normal}}{\sum_{j=1}^{M} w_j} \right] \]
2.2.2 Weighted Product Method (WPM)
This method is similar to simple additive weighting method. The main difference is multiplication is used instead of addition as shown below:

\[ P_i = \prod_{j=1}^{M} \left[ \frac{(m_{ij})_{\text{normal}}}{w_j} \right] \]

Each normalized value of alternative with respect to attribute is raised to the power of relative weight corresponding attribute.

2.2.3 AHP steps
Some calculation steps are essential and explained as follows:

- Establishing the hierarchical structure constructing the hierarchical structure with decision elements, decision-makers are requested to make pairwise comparisons between decision alternatives and criteria using a nine-point scale.
- Calculating the consistency to ensure that the priority of elements is consistent, the maximum eigenvector or relative weights and max λ is calculated.
  \[ \text{I.C.} = \frac{\lambda_{\text{max}} - n}{(n-1)} < 0.10 \]  
  Where n is the number of components evaluated in the pairwise comparison matrix, and λmax is the largest eigenvalue characterizing the previous matrix. When the calculated CR values exceed the threshold, it is an indication of inconsistent judgment. In such cases, the decision makers would need to revise the original values in the pairwise comparison matrix. Finally, it is necessary to aggregate the relative priorities of the decision elements to obtain an overall rating for decision alternatives. The numerical analysis method is employed to calculate the eigen value vector and the maximized eigen value for an understanding of the consistency established and the relative weight among elements.
- Constructing a fuzzy positive matrix a decision maker transforms the score of pair-wise comparison into linguistic variables via the positive triangular fuzzy number (PTFN).
2.2.4 TOPSIS Method

The method is first TOPSIS proposed by Hwang and Lin 1987. In general, TOPSIS has two main functions: one is to calculate the largest distance from the negative ideal solution; another alternative is to choose optimization which has the shortest distance from the ideal solution. In case of the decision problem analysis TOPSIS is an effective and practical method used for hierarchization by preference systems.

TOPSIS method was successfully applied to solve multi-criteria decision making problem in various industrial field. The model of multi-attribute decision making based on TOPSIS was organized for the elimination of logistics information technology decision problem. TOPSIS was used to manage competitive benchmarking in the product design process. TOPSIS integrated with other methods have been developed to handle multipurpose reactive power compensation problem. The method is described below:

Step 1: To determine the objective.
Step 2: Formation of matrix based decision table in which each row of the matrix is allocated to one alternative and each column to one attribute.

\[ A = \begin{bmatrix} C_{11} & \cdots & C_{1n} \\ \vdots & \ddots & \vdots \\ C_{m1} & \cdots & C_{mn} \end{bmatrix} \]

Step 3: Calculate normalized matrix:

\[ R_{ij} = \frac{m_{ij}}{\sqrt{\sum_{j=1}^{M} m_{ij}^2}} \]

Step 4: Decide the relative weights\( (w_{ij}) \) of attributes.

Step 5: Find weighted normalized matrix \( V_{ij} \)

\[ V_{ij} = w_{ij}R_{ij} \]

Step 6: Find the best positive idea and worst negative ideal.

\[ V^+ = \max(V_{1j}, V_{2j}, \ldots, V_{nj}) \quad j = 1, 2, \ldots, n. \]
\[ V^- = \min(V_{1j}, V_{2j}, \ldots, V_{nj}) \quad j = 1, 2, \ldots, n. \]

Step 7: Develop the distances between each alternative. The distances of each alternative from ideal solution can be calculated by the equation given below:

\[ P_{ij}^+ = \frac{1}{M} \sum_{j=1}^{M} (V_{ij} - V_j^+)^2 \]
\[ P_{ij}^- = \frac{1}{M} \sum_{j=1}^{M} (V_{ij} - V_j^-)^2 \]

Step 8: Find the closeness of alternatives

\[ C_i = \frac{P_{ij}^-}{(P_{ij}^+ + P_{ij}^-)} \]

Rank the alternatives the preference order can be find in step 8, which is close to the ideal solution and far from the negative ideal solution. Recommend the best alternative. The preferred alternative is the one with the maximum value of \( C_i \).

2.2.5 PROMETHEE Method:

Step 1: Creating the Data Matrix: \( w = (w_1, w_2, \ldots, w_n) \) k by c with weight \( = (f_1, f_2, \ldots, f_n) \) to the alternative being considered by \( = (a, b, c, \ldots) \) for data matrix.

| Alternatives | Attributes | \( f_1 \) | \( f_2 \) | \( f_3 \) | \ldots | \( f_n \) |
|--------------|------------|---------|---------|---------|--------|--------|
| A            | A          | \( f_1(A) \) | \( f_2(A) \) | \( f_3(A) \) | \ldots | \( f_n(A) \) |
| B            | B          | \( f_1(B) \) | \( f_2(B) \) | \( f_3(B) \) | \ldots | \( f_n(B) \) |
| C            | C          | \( f_1(C) \) | \( f_2(C) \) | \( f_3(C) \) | \ldots | \( f_n(C) \) |
| D            | D          | \( f_1(D) \) | \( f_2(D) \) | \( f_3(D) \) | \ldots | \( f_n(D) \) |
| \ldots       | \ldots     | \ldots   | \ldots   | \ldots   | \ldots | \ldots |
| WEIGHTS      | Wi         | w1      | w2      | w3      | \ldots | wn     |

Step 2: Identification of preferred function Criteria: Six different preference function (Usual, U Type, V Type, Level type, Linear Type) is used for implementation.
Step 3: Determination of Preference Function:

\[ p_a = \begin{cases} 
0, & f(a) \leq f(b) \\
\{ p[f(a) - F(b)], & f(a) > f(b) \}
\end{cases} \]

Step 4: Determine the preferred index: the choice of the Common functions can be determined reference index for each pair of alternatives. \( W(i = 1, 2, \ldots k) \) evaluated by weight by having a \( k \) and \( b \) the alternative preferred index are calculated by equation.

\[
\pi(a, b) = \frac{\sum_{i=1}^{n} w_i \cdot p_i(a, b)}{\sum_{i=1}^{n} w_i}
\]

Step 5: Positive \((\phi^+)\) and Negative \((\phi^-)\) Superiority alternative rule for determining:

\[
\phi^+(a) = \frac{1}{n-1} \sum \pi(a, b)
\]

\[
\phi^-(a) = \frac{1}{n-1} \sum \pi(b, a)
\]

Step 6: Determination of PROMETHEE I Partial Priority for Alternatives: In some cases are involved in the determination of the two alternatives \( A \) and \( B \) for partial priority.

Condition 1. If either of the conditions, a preferable alternative to the alternative \( b \).

\[
\phi^+(a) > \phi^+(b) \text{ and } \phi^-(a) < \phi^-(b)
\]

\[
\phi^+(a) > \phi^+(b) \text{ and } \phi^-(a) = \phi^-(b)
\]

\[
\phi^+(a) = \phi^+(b) \text{ and } \phi^-(a) < \phi^-(b)
\]

Condition 2. If the condition does not allow the following, \( A \) and \( B \) alternative is identical.

\[
\phi^+(a) = \phi^+(b) \text{ and } \phi^-(a) = \phi^-(b)
\]

Condition 3. If either of the following conditions \( A \) alternative, comparable to the \( B \) alternative.

\[
\phi^+(a) > \phi^+(b) \text{ and } \phi^-(a) > \phi^-(b)
\]

\[
\phi^+(a) < \phi^+(b) \text{ and } \phi^-(a) < \phi^-(b)
\]

Step 7: PROMETHEE II complete with identification of priorities for alternatives: The following equation is calculated with the help of exactly the priorities for each alternative. A calculated value of all alternatives with full priority ranking is determined by assessing precisely the same plane.

\[
\Phi(a) = \phi^+(a) - \phi^-(a)
\]

Depending on the exact priority value calculated for \( A \) and \( B \) are two alternative decisions are given below.

If \( (a) > (b) \), \( A \) Alternative is superior.

If \( (a) = (b) \), \( A \) and \( B \) are identical alternatives.

3. Example

An example is considered to demonstrate the methodology of selection of bike.

3.1 AHP Analysis

In survey on these aspects we gave some weight factors according to high or low numbers. The weight factor is an odd number series from 1 to 3,5,7,9 if it’s high and 1 to 1/3, 1/5, 1/7, 1/9 if it’s low. By doing this we will get a comparison matrix.

**Table 2 Comparison Matrix**

|       | Design | Service Availability | Power | Comfort | Price | Mileage |
|-------|--------|-----------------------|-------|---------|-------|---------|
| Design| 1.00   | 0.33                  | 0.33  | 0.14    | 0.20  | 0.11    |
| Service Availability | 3.00   | 1.00                  | 1.00  | 0.20    | 0.33  | 0.14    |
| Power | 3.00   | 1.00                  | 1.00  | 0.33    | 0.20  | 0.14    |
| Comfort | 7.00   | 5.00                  | 3.00  | 1.00    | 0.33  | 0.20    |
| Price | 5.00   | 3.00                  | 5.00  | 3.00    | 1.00  | 0.33    |
| Mileage | 9.00   | 7.00                  | 7.00  | 5.00    | 3.00  | 1.00    |

Then added all the columns and divide each segment with its columns added value to normalize the matrix and this process is called as normalizing the matrix.

|       | Sum | 28.00 | 17.33 | 17.33 | 9.68 | 5.07 | 1.93 |
|-------|-----|-------|-------|-------|------|------|------|


Table 3 Normalized Matrix

| Design    | Service Availability | Power | Comfort | Price | Mileage |
|-----------|-----------------------|-------|---------|-------|---------|
| Design    | 0.04                  | 0.02  | 0.02    | 0.01  | 0.04    | 0.06    |
| Service Availability | 0.11               | 0.06  | 0.06    | 0.02  | 0.07    | 0.07    |
| Power     | 0.11                  | 0.06  | 0.06    | 0.03  | 0.04    | 0.07    |
| Comfort   | 0.25                  | 0.29  | 0.17    | 0.10  | 0.07    | 0.10    |
| Price     | 0.18                  | 0.17  | 0.29    | 0.31  | 0.20    | 0.17    |
| Mileage   | 0.32                  | 0.40  | 0.40    | 0.52  | 0.59    | 0.52    |

Now taking average of each row to get the high weight value and this matrix is called as weight factor matrix

Table 4 Weighted factor Matrix

| Design    | Service Availability | Power | Comfort | Price | Mileage | w |
|-----------|-----------------------|-------|---------|-------|---------|---|
| Design    | 0.04                  | 0.02  | 0.02    | 0.01  | 0.04    | 0.06 | 0.03|
| Service Availability | 0.11               | 0.06  | 0.06    | 0.02  | 0.07    | 0.07 | 0.06|
| Power     | 0.11                  | 0.06  | 0.06    | 0.03  | 0.04    | 0.07 | 0.06|
| Comfort   | 0.25                  | 0.29  | 0.17    | 0.10  | 0.07    | 0.10 | 0.16|
| Price     | 0.18                  | 0.17  | 0.29    | 0.31  | 0.20    | 0.17 | 0.22|
| Mileage   | 0.32                  | 0.40  | 0.40    | 0.52  | 0.59    | 0.52 | 0.46|

Now we can see in above table that “Mileage” is the highest weight value about 0.46 but now to check that is our answer is consistent or not. For that we will do a consistency check.

For consistency we need a weight sum vector named as “Ws”, which is a multiplication of comparison matrix and weight factor matrix.

Table 5 Weight sum vector

| Ws   |
|------|
| 0.19 |
| 0.39 |
| 0.38 |
| 1.05 |
| 1.52 |
| 3.10 |

Now, Taking average of the “Ws dot 1/w” matrix which is 6.42 and this value called as element of consist and shown by λ.

Table 6 Dot product of weight some factor and inverse of weight factor matrix.

| Ws   | I/w   | Ws dot I/w |
|------|-------|------------|
| 0.19 | 32.26 | 6.17       |
| 0.39 | 15.67 | 6.12       |
| 0.38 | 16.20 | 6.20       |
| 1.05 | 6.10  | 6.40       |
| 1.52 | 4.54  | 6.91       |
| 3.10 | 2.18  | 6.74       |

To get consistency index, this formula is applied

\[ \text{Consistency Index (CI)} = \frac{\lambda - n}{n - 1} \]

Where n is the no of alternatives and here we have 6 aspects or alternatives.
So the CI is 0.08and to get the consistency ratio we have to divide the CI by random index “RI” which depends on number of alternatives.

Table 7 Random Index

| N   | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|-----|---|---|---|---|---|---|---|---|---|----|
| RI  | 0 | 0 | 0.58 | 0.9 | 1.2 | 1.24 | 1.32 | 1.41 | 1.45 | 1.49 |

Here for 6 alternatives the value of Random index would be 1.25.
So The Consistency Ratio “CR” is 0.07.
The best consistency ratio would be if it’s less than 0.1 and when it goes equal or higher then it mean the comparison should be rechecked.
Now we got that Average is the aspects which have higher weight value. 
Now the same AHP process would be followed for these three chosen bike models for each alternative. 
So for each alternative we have one weight factor matrix. 
By multiplying all six weight factor matrix with the weight factor matrix from the main comparison matrix. 

| Alternatives         | Design  | Service Availability | Power | Comfort | Price | Mileage | W  |
|----------------------|---------|----------------------|-------|---------|-------|---------|----|
| TVS Star City        | 0.11    | 0.19                 | 0.11  | 0.11    | 0.48  | 0.41    | 0.03|
| Mahindra Centuro     | 0.26    | 0.08                 | 0.26  | 0.26    | 0.41  | 0.48    | 0.06|
| Honda Livo           | 0.63    | 0.72                 | 0.63  | 0.63    | 0.11  | 0.11    | 0.16|

Table 8 Wait matrix multiplication

3.2 SAW Method
Using the above weights the performance score for each attribute is calculated using normalized data.

\[
P_i = \left( \frac{\sum_{j=1}^{M} w_j (m_{ij})_{\text{normal}}}{\sum_{j=1}^{M} w_j} \right)
\]

\[P_1 = (0.11 \times 0.03) + (0.19 \times 0.06) + (0.11 \times 0.06) + (0.11 \times 0.16) + (0.48 \times 0.22) + (0.41 \times 0.46)
\]

\[P_2 = (0.26 \times 0.03) + (0.08 \times 0.06) + (0.26 \times 0.06) + (0.26 \times 0.16) + (0.41 \times 0.22) + (0.48 \times 0.46)
\]

\[P_3 = (0.63 \times 0.03) + (0.72 \times 0.06) + (0.63 \times 0.06) + (0.63 \times 0.16) + (0.11 \times 0.22) + (0.11 \times 0.46)
\]

\[P_1 = 0.3331
\]
\[P_2 = 0.3808
\]
\[P_3 = 0.2755
\]

Ranking- 2-1-3
SAW suggested Bike-B as first choice, Bike-A as second choice, Bike-C as third choice.

3.3 WPM Method
The performance score for bike selection is calculated using same normalized data and weights of attributes using equation:

\[
P_i = \prod_{j=1}^{M} \left[ (m_{ij})_{\text{normal}} \right]^{w_j}
\]

The values of \(P_i\) are:

\[P_1 = 0.11^{0.03} \times 0.19^{0.06} \times 0.11^{0.06} \times 0.11^{0.16} \times 0.48^{0.22} \times 0.41^{0.46}
\]

\[P_2 = 0.26^{0.03} \times 0.08^{0.06} \times 0.26^{0.06} \times 0.26^{0.16} \times 0.41^{0.22} \times 0.48^{0.46}
\]

\[P_3 = 0.63^{0.03} \times 0.72^{0.06} \times 0.63^{0.06} \times 0.63^{0.16} \times 0.11^{0.22} \times 0.11^{0.46}
\]

\[P_1 = 0.2943
\]
\[P_2 = 0.3598
\]
\[P_3 = 0.1947
\]

Ranking- 2-1-3
WPM suggested Bike-B as first choice, Bike-A as second choice, Bike-C as third choice.

3.4 TOPSIS analysis

| Alternatives | Design | Service Availability | Power | Comfort | Price | Mileage |
|--------------|--------|----------------------|-------|---------|-------|---------|
| Bike-A       | .11    | .19                  | .11   | .11     | .48   | .41     |
| Bike-B       | .26    | .08                  | .26   | .26     | .41   | .48     |
| Bike-C       | .63    | .72                  | .63   | .63     | .11   | .11     |

Weights .03 .06 .06 .16 .22 .46
Table 10 Weighted normalized matrix \( (V_{ij} = R_{ij} \times W_{ij}) \)

|       | Design      | Service     | Power       | Comfort     | Price        | Mileage       |
|-------|-------------|-------------|-------------|-------------|--------------|---------------|
| Bike-A | .0033       | .0114       | .0066       | .0176       | .1056        | .1886         |
| Bike-B | .0078       | .0048       | .0156       | .0416       | .0902        | .2208         |
| Bike-C | .0189       | .0432       | .0378       | .1008       | .0242        | .0506         |

\[
\begin{align*}
V^+ & = \begin{bmatrix}
V_1^+ & .0189 \\
V_2^+ & .0432 \\
V_3^+ & .0378 \\
V_4^+ & .1008 \\
V_5^+ & .0242 \\
V_6^+ & .2208 
\end{bmatrix} \\
V^- & = \begin{bmatrix}
V_1^- & .0033 \\
V_2^- & .0048 \\
V_3^- & .0066 \\
V_4^- & .0176 \\
V_5^- & .1056 \\
V_6^- & .0506 
\end{bmatrix}
\end{align*}
\]

Table 11 Separation measures

\[
\begin{align*}
S^+ & = \begin{bmatrix}
S_1^+ & .137059 \\
S_2^+ & .122055 \\
S_3^+ & .170200 
\end{bmatrix} \\
S^- & = \begin{bmatrix}
S_1^- & .138150 \\
S_2^- & .173222 \\
S_3^- & .133140 
\end{bmatrix}
\end{align*}
\]

Relative Closeness:
\[ P_1 = 0.50198 \]
\[ P_2 = 0.58664 \]
\[ P_3 = 0.43891 \]

**Ranking = 2 1 3**

3.5 PROMETHEE Solution

Table 12 Normalized date of example

|       | Design | Service | Power | Comfort | Price | Mileage |
|-------|--------|---------|-------|---------|-------|---------|
| Bike-A | .11    | .19     | .11   | .11     | .48   | .41     |
| Bike-B | .26    | .08     | .26   | .26     | .41   | .48     |
| Bike-C | .63    | .72     | .63   | .63     | .11   | .11     |

Weights: \[ .03 \quad .06 \quad .06 \quad 0.16 \quad .22 \quad .46 \]

\[ \phi = \begin{bmatrix}
1 & .06 & .46 \\
.93 & 1 & .46 \\
.77 & .31 & 1
\end{bmatrix}, \quad \text{Net Flow} = \begin{bmatrix}
1.52 \\
1.39 \\
1.08
\end{bmatrix}, \quad \text{Ranking} = \begin{bmatrix}
3 & -1.18 \\
1.02 \\
0.16
\end{bmatrix} \]

**Ranking: 3-1-2**

Result Summary of Ranking

|        | SAW | WPS | TOPSIS | PROMETHEE |
|--------|-----|-----|--------|-----------|
| Bike-A | 2   | 2   | 2      | 3         |
| Bike-B | 1   | 1   | 1      | 1         |
| Bike-C | 3   | 3   | 3      | 2         |

4. Conclusions
The proposed analysis model has practical application as Bike Section problem shown further more proposed method is also used to solve other optimization problems in many industries. A Methodology based on QFD with optimization tools (AHP, TOPSIS, and PROMETHEE) is suggested for product design and development in
manufacturing industry, which helps in selection of suitable customer needs among large numbers. This approach can also useful to select key column in each phase of QFD and provides best solution for each situation. The method allows assigning values of relative importance to the criterion based on customer preference. Developed models have been proven to allocate weights per demand for the first phase of QFD. These models can be applied to each QFD phase in order to analyze product quality of different industries.

The decision making tools of other criteria can be used for the measurement of product quality and the impact of the developed models can be analyzed. The future direction of a theoretical study is analyzing the similarities and differences between AHP, TOPSIS, PROMETHEE and other MCDA / MCDM methods.

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