Entropic Out-of-Distribution Detection

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Abstract—Out-of-distribution (OOD) detection approaches usually present special requirements (e.g., hyperparameter validation, collection of outlier data) and produce side effects (e.g., classification accuracy drop, slower energy-inefficient inferences). We argue that these issues are a consequence of the SoftMax loss anisotropy and disagreement with the maximum entropy principle. Thus, we propose the IsoMax loss and the entropic score. The seamless drop-in replacement of the SoftMax loss by IsoMax loss requires neither additional data collection nor hyperparameter validation. The trained models do not exhibit classification accuracy drop and produce fast energy-efficient inferences. Moreover, our experiments show that training neural networks with IsoMax loss significantly improves their OOD detection performance. The IsoMax loss exhibits state-of-the-art performance under the mentioned conditions (fast energy-efficient inference, no classification accuracy drop, no collection of outlier data, and no hyperparameter validation), which we call the seamless OOD detection task. In future work, current OOD detection methods may replace the SoftMax loss with the IsoMax loss to improve their performance on the commonly studied non-seamless OOD detection problem.

I. INTRODUCTION

Out-of-distribution (OOD) detection approaches usually use special requirements such as input preprocessing [8], [9], feature extraction combined with metric learning [2], adversarial training [10], hyperparameter validation [11], and collection of additional data [12], [13], [14], [15]. Moreover, current OOD methods commonly show side effects such as classification accuracy drop [16], [9], and slow energy-inefficient inferences [11], [2]. Solutions based on uncertainty (or confidence) estimation (or calibration) present complexity and lead to slow computationally inefficient inferences [17], [18], [19], [20], [21].

We define the seamless OOD detection task, which consists of performing OOD detection under the following restrictions. First, no classification accuracy drop is allowed. Second, the resulting models should produce inferences with the same speed and energy efficiency as those produced by the regularly trained neural networks. Third, no OOD/outlier/additional/extra data may be used. Finally, no hyperparameter validation is required. Improving the performance of neural networks in the seamless OOD detection problem is important from a practical perspective. Additionally, such approaches can be combined in future work with current and novel OOD detection techniques to further improve the performance on the non-seamless OOD detection task.

We argue that the unsatisfactory OOD detection performance of modern neural networks is mainly due to the drawbacks of the SoftMax loss (we follow the “SoftMax loss” expression as defined in [22]). First, the SoftMax loss anisotropy does not incentivize the concentration of high-level representations in the feature space [1], [10], making OOD detection difficult [10] (Fig. 1a). Second, SoftMax loss produces overconfident low-entropy posterior probability distributions [23], which is in disagreement with the maximum entropy principle [24], [25], [26] (Fig. 1h). Therefore, we propose the isotropy maximization loss (IsoMax loss). To fix the SoftMax loss anisotropy, we made IsoMax an isotropic, i.e., exclusively distance-based, loss. To tackle the SoftMax loss overconfidence, we developed the entropy maximization trick, which consists of training with logits multiplied by a high constant that is removed for inference. This technique allows IsoMax loss to produce high-entropy (almost maximum) posterior probability distributions in agreement with the principle of maximum entropy.

We propose to train neural networks replacing the SoftMax loss with the IsoMax loss. The swap of the SoftMax loss with the IsoMax loss requires changes in neither the architecture of the model nor training procedures or parameters. For OOD detection, we use the negative entropy of the neural network output probabilities, which we call the entropic score (ES). Since our solution presents neither special requirements nor side effects, it qualifies as a seamless OOD detection approach as previously defined.

Our contributions are the following. First, we associate the unsatisfactory OOD detection performance of neural networks with the SoftMax loss anisotropy and disagreement with the maximum entropy principle. Second, we propose the IsoMax loss that acts as a SoftMax loss drop-in replacement and may be used as a baseline for building improved OOD detection approaches in future work. We show that the ES produces high performance combined with IsoMax loss. Third, we present the theoretical insight that associates the improved OOD detection performance of the networks trained with IsoMax loss with the principle of maximum entropy. Fourth, we show that our solution produces state-of-the-art performance for the seamless (fast energy-efficient inferences, no classification accuracy drop, no hyperparameter tuning, and no collection of outlier data) OOD detection task. Fifth, despite being unfair since the approaches present different special requirements and side effects, we compare our seamless solution with non-seamless OOD detection methods.
we only consider validation on adversarial samples for non-validation data used for defining hyperparameters should have been removed from the training set, which would presumably lead to an even stronger classification accuracy drop and, consequently, a decrease in OOD detection performance. The authors suggested using two models: one for classification accuracy drop of a few percentage points in some cases. Thus, in our solution, we learn a feature space that is from the start rather than learning a metric from a preexisting feature space, avoiding the need for feature extraction and metric learning postprocessing phases after the neural network training.

A. Isotropy.

To fix the SoftMax loss anisotropy caused by its affine transformation, we forced the logits of the IsoMax loss to depend exclusively on the distances from the high-level features to the class prototypes.

Let $f_\theta(x)$ represent the high-level feature (embedding) associated with $x$, $p_\phi^j$ represent the learnable prototype associated with class $j$, and $d(\cdot)$ represent the nonsquared distance. Additionally, let $\hat{y}^{(k)}$ represent the label of the correct class. Therefore, we construct an isotropic loss by writing:

$$L_1(\hat{y}^{(k)}|x) = -\log \left( \frac{\exp(-d(f_\theta(x), p_\phi^{\hat{y}^{(k)}}))}{\sum_j \exp(-d(f_\theta(x), p_\phi^j))} \right)$$

(1)

Unlike metric learning-based OOD detection approaches, rather than learning a metric from a preexisting feature space, in our solution, we learn a feature space that is from the start consistent with the chosen metric, avoiding the need for feature extraction and metric learning postprocessing phases after the neural network training.

B. Entropy Maximization.

Isotropy improves the OOD detection performance. However, for further performance gains, we need to circumvent the SoftMax loss propensity to produce low-entropy posterior probability distributions. To achieve high-entropy (almost maximum entropy) distributions in agreement with the maximum entropy principle, we introduce the entropic scale, which consists in training using logits multiplied by a constant factor called the entropic scale that is nevertheless removed before inference, enables IsoMax to generate underconfident high-entropy (almost maximum entropy) posterior probability distributions in agreement with the principle of maximum entropy.
The presence of the entropic scale during training does not prevent the loss from approaching zero as required. However, when we remove it prior to the inference, the SoftMax function naturally makes the entropy of the output probabilities increase to almost the maximum value possible if we use a high enough entropic score during training. Thus, returning to Equation (1), multiplying the embedding-prototype distances by an entropic scale $E_s$, and representing the 2-norm of a vector by $||.||$, we write the definition of the IsoMax loss as:

$$L_I(y^{(k)}|x) = -\log \left( \frac{\exp(-E_s \| f_\theta(x) - p_k^\theta \|)}{\sum_j \exp(-E_s \| f_\theta(x) - p_j^\theta \|)} \right)$$

By applying the entropy maximization trick, the inference probabilities for the IsoMax loss may be written as follows:

$$p_I(y^{(i)}|x) = \frac{\exp(-\| f_\theta(x) - p_i^\theta \|)}{\sum_j \exp(-\| f_\theta(x) - p_j^\theta \|)}$$

### C. Prototype Initialization.

We observed that using the Xavier [28] or Kaiming [29] initializations for the prototypes leads to oscillations in performance. Hence, we decided to initialize all prototypes to the zero vector. Weight decay is applied to the prototypes because they are trainable parameters.

### D. Entropic Score.

The entropy has been studied for OOD detection [30]. We show that the output probabilities negative entropy, which we call the entropic score, produces high-performance results when combined with IsoMax loss. Indeed, in such cases, the solution may consider the information provided by all network outputs rather than merely one output. For instance, ODIN and ACET only use the maximum probability.

### E. Implementation Details.

To calculate the losses based on cross-entropy, deep learning libraries usually combine the logarithm and probability into a single computation. However, we experimentally observed that sequentially computing these calculations as standalone operations improves the IsoMax performance. The class prototypes have the same dimension as the neural network last-layer representations. The number of prototypes is equal to the number of classes. The IsoMax loss has fewer parameters than the SoftMax loss because it has no bias to learn.

In addition to avoiding classification accuracy drop compared with the SoftMax loss trained networks, IsoMax loss trained models show higher OOD detection performance (see Table I).

We observed classification accuracy drop and low/oscillating performance when trying to integrate the entropic scale into the SoftMax loss or with cosine similarity [22], [31], [32]. In such cases, the above strategy, i.e., initialization of the loss weights with the zero vector, cannot be performed. The Mahalanobis distance cannot be used because the covariance matrix is not differentiable. Hence, the nonsquared Euclidean distance is the optimal choice for integration with the entropic scale.

### IV. Experiments

All datasets, models, and evaluation metrics used the baseline established in [35] that was followed in the major OOD detection papers [11], [2], [10]. We trained from the scratch 100-layer DenseNet-BC [36] (growth rate $k=12$, 0.8M parameters) and 34-layer ResNets [37] on CIFAR10 [38], CIFAR100 [38] and SVHN [39] using the SoftMax and IsoMax losses.

For both the SoftMax loss and IsoMax loss, we used SGD with the Nesterov moment equal to 0.9, 300 epochs with a batch size of 64, and an initial learning rate of 0.1, with a learning rate decay rate equal to ten applied in epochs 150, 200, and 250. We used a dropout of zero. The weight decay was 0.0001.

We only compared approaches that did not present classification accuracy drop because this facilitates increasing OOD detection performance [40]; moreover, it is particularly undesired from a practical perspective [41]. It is well known that using OOD/outlier/background/additional data improves the OOD detection performance. Therefore, considering that data-based regularization techniques may benefit both SoftMax loss and IsoMax loss, we perform all experiments without outlier exposure [13], [14], background samples [12], or energy-based fine-tuning [15]. The source code is available online.

### V. Results and Discussions

#### A. IsoMax Loss Properties, Ablation Study, and Entropic Scale Value Definition.

To experimentally show that higher entropic scales lead to higher mean entropy probability distributions and consequently

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1. [https://github.com/dlmacedo/entropic-out-of-distribution-detection](https://github.com/dlmacedo/entropic-out-of-distribution-detection)
Fig. 2. (a) SoftMax loss minimizes both the cross-entropy and the mean entropy of the posterior probabilities. (b) IsoMax loss produces low mean entropy posterior probabilities for a low entropic scale ($E_s = 1$). (c) IsoMax loss produces medium mean entropy for an intermediate entropic scale ($E_s = 3$). (d) IsoMax loss produces high mean entropy for a high entropic scale ($E_s = 10$). Therefore, higher entropic scale values are correlated with higher mean entropies as recommended by the maximum entropy principle. Notice that the orange line is almost flat in (d), so the IsoMax loss almost retains the maximum entropy present at the beginning of the training for a high entropic scale. Hence, an entropic scale equal to ten is enough to produce posterior probability distributions with virtually the maximum possible mean entropy $\log(N)$, where $N$ is the number of classes. Consequently, there is no need to increase $E_s$ further. Therefore, we decided to use $E_s = 10$ for IsoMax loss (see also Fig. 3). (e) The left side of the dashed vertical red line presents the classification accuracies. The right side of the dashed vertical red line shows the OOD detection performance using the entropic score and the TNR@TPR95 (true negative rate at 95% true positive rate) metric. We observe that a higher mean entropy produces increased OOD detection performance regardless of the out-of-distribution (out-dist). Isotropy by itself enables the IsoMax loss to exhibit higher performance than the SoftMax loss ($E_s = 1$). IsoMax loss trained models exhibit classification accuracies similar to the classification accuracies presented by SoftMax loss trained networks regardless of the entropic scale.

Fig. 3. AUROC represents the mean AUROC considering all out-of-distribution data. The classification accuracy and the mean OOD detection performance are approximately stable for $E_s = 10$ or higher regardless of the dataset and model. $E_s$ validation cannot significantly improve the OOD detection performance. In fact, this is not even possible because access to the OOD or outlier samples is not allowed in seamless OOD detection. Making $E_s$ learnable did not considerably improve or decrease the OOD detection results.
Improving the OOD detection performance, we trained DenseNets on SVHN using the SoftMax loss and IsoMax loss with distinct entropic scale values. We used the entropic score and the TNR@TPR95 (true negative rate at 95% true positive rate) to evaluate the OOD detection performance (Fig. 2).

Fig. 2 shows that the SoftMax loss generates posterior distributions with lower mean entropy. Fig. 2 illustrates that the unitary entropic scale ($E_s = 1$) does not increase the mean entropy of the probability distributions. In other words, isotropy alone is not enough to produce low mean entropy probability distributions, and the entropy maximization trick is necessary. Nevertheless, Fig. 2 shows that the simple replacement of anisotropic logits based on the affine transformation by isotropic logits is enough to produce low mean entropy probability distributions. In other words, isotropy is necessary.

More importantly, higher entropy posterior probability distributions directly correlate with increased OOD detection performances despite the out-of-distribution data. Hence, the entropy maximization trick enables the migration from low-entropy distributions (Fig. 2b) to high-entropy distributions (Fig. 2d). For a high entropic scale, the IsoMax loss minimizes the cross-entropy while producing high-entropy probability distributions (Fig. 2d). For a high entropic scale, the IsoMax loss minimizes the cross-entropy while producing high-entropy probability distributions (Fig. 2d). For a high entropic scale, the IsoMax loss minimizes the cross-entropy while producing high-entropy probability distributions (Fig. 2d). For a high entropic scale, the IsoMax loss minimizes the cross-entropy while producing high-entropy probability distributions (Fig. 2d). For a high entropic scale, the IsoMax loss minimizes the cross-entropy while producing high-entropy probability distributions (Fig. 2d).

TABLE II

| Model       | Data (training) | OOD (unseen) | Seamless OOD Detection: No Classification Accuracy Drop. No Outlier Data. Fast and Energy-Efficient Inferences. No Hyperparameter Tuning. |
|-------------|-----------------|--------------|----------------------------------------------------------------------------------------------------------------------------------|
| DenseNet    | SVHN            | LSUN         | TNR@TPR95\(^1\) (%) \[^1\] | AUROC\(^2\) (%) \[^1\] | DTACC\(^3\) (%) \[^1\] |
| CIFAR10     | SVHN            | TinyImageNet| 32.2 / 33.2 / 64.5 / 77.0 | 86.6 / 86.9 / 94.6 / 96.6 | 79.9 / 79.9 / 88.1 / 91.6 |
| ResNet      | SVHN            | TinyImageNet| 43.1 / 44.5 / 81.7 / 83.6 | 91.7 / 92.0 / 96.8 / 97.1 | 86.5 / 86.5 / 91.2 / 91.9 |
| CIFAR100    | SVHN            | TinyImageNet| 15.9 / 18.0 / 22.5 / 20.2 | 71.3 / 72.7 / 83.9 / 85.3 | 66.1 / 66.3 / 77.8 / 79.7 |
| SVHN        | CIFAR10         | TinyImageNet| 67.3 / 67.7 / 90.5 / 92.3 | 89.8 / 89.7 / 97.9 / 98.0 | 87.0 / 86.9 / 93.7 / 94.1 |

\(^1\)True negative rate at 95% true positive rate. \(^2\)Area under the receiver operating characteristic curve. \(^3\)Detection accuracy.
They also require previously known optimal adversarial perturbation values for each combination of datasets and models.

ODIN, the Mahalanobis approach, and ACET present hyperparameters that must be validated for each combination of datasets and models. They also require previously known optimal adversarial perturbation values for each combination of datasets and models. 1ODIN uses input preprocessing, temperature calibration, and adversarial validation, i.e., hyperparameter tuning using adversarial examples [11]. 2ACET uses adversarial training, resulting in slower training, possibly reduced scalability for large images, and eventually classification accuracy drop [10]. 3IsoMax+ES means training with IsoMax loss and performing OOD detection using the entropic score (ES). Considering that validating $E_s$ using adversarial examples cannot produce significant gains (Fig. 3), we prefer to keep $E_s=10$ to maintain the simplicity of the solution. 4The Mahalanobis solution uses input preprocessing, feature ensemble, feature extraction followed by metric learning, and adversarial validation [2]. 5 Detection accuracy [3]. The best results are shown in bold (2% tolerance).

| Model   | Data (training) | OOD (unseen) | Non-seamless Out-of-Distribution Detection: Approaches with Different Special Requirements and Side Effects. |
|---------|----------------|--------------|-------------------------------------------------------------------------------------------------------------|
|         |                |              | AUROC (%) [↑] | DTAC [%] [↑] |
|         |                |              | ODIN1 / ACET2 / IsoMax+ES3 (ours) / Mahalanobis4 |
| DenseNet | CIFAR10        | SVHN TinyImageNet LSUN | 92.8 / NA / 96.6 / 97.6 | 86.5 / NA / 91.6 / 92.6 |
|         |                |              | 97.2 / NA / 97.8 / 98.8 | 92.1 / NA / 93.2 / 95.0 |
|         |                |              | 98.5 / NA / 98.8 / 99.2 | 94.3 / NA / 94.9 / 96.2 |
|         | CIFAR100       | SVHN TinyImageNet LSUN | 88.2 / NA / 88.6 / 91.8 | 80.7 / NA / 83.7 / 84.6 |
|         |                |              | 85.3 / NA / 92.6 / 97.0 | 77.2 / NA / 86.6 / 91.8 |
|         |                |              | 85.7 / NA / 94.7 / 97.9 | 77.3 / NA / 89.1 / 93.8 |
|         | SVHN           | CIFAR10 TinyImageNet LSUN | 91.9 / NA / 98.5 / 98.8 | 86.6 / NA / 95.0 / 96.3 |
|         |                |              | 94.8 / NA / 99.1 / 99.8 | 90.2 / NA / 96.1 / 98.9 |
|         |                |              | 94.1 / NA / 99.1 / 99.9 | 89.1 / NA / 95.9 / 99.2 |
| ResNet  | CIFAR10        | SVHN TinyImageNet LSUN | 86.5 / 98.1 / 97.1 / 95.5 | 77.8 / NA / 91.9 / 89.1 |
|         |                |              | 93.9 / 85.9 / 94.6 / 99.0 | 86.0 / NA / 88.3 / 95.4 |
|         |                |              | 93.7 / 85.8 / 96.9 / 99.5 | 85.8 / NA / 91.5 / 97.2 |
|         | CIFAR100       | SVHN TinyImageNet LSUN | 72.0 / 91.2 / 85.3 / 84.4 | 67.7 / NA / 79.7 / 76.5 |
|         |                |              | 83.6 / 75.2 / 92.0 / 87.9 | 75.9 / NA / 85.6 / 84.6 |
|         |                |              | 81.9 / 69.8 / 93.2 / 82.3 | 74.6 / NA / 87.5 / 79.7 |
|         | SVHN           | CIFAR10 TinyImageNet LSUN | 92.1 / 97.3 / 98.0 / 97.6 | 89.4 / NA / 94.1 / 94.6 |
|         |                |              | 92.9 / 97.7 / 98.4 / 99.3 | 90.1 / NA / 94.8 / 98.8 |
|         |                |              | 90.7 / 99.7 / 97.8 / 99.9 | 88.2 / NA / 93.6 / 99.5 |

ODIN, the Mahalanobis approach, and ACET present hyperparameters that must be validated for each combination of datasets and models. They also require previously known optimal adversarial perturbation values for each combination of datasets and models. 1ODIN uses input preprocessing, temperature calibration, and adversarial validation, i.e., hyperparameter tuning using adversarial examples [11]. 2ACET uses adversarial training, resulting in slower training, possibly reduced scalability for large images, and eventually classification accuracy drop [10]. 3IsoMax+ES means training with IsoMax loss and performing OOD detection using the entropic score (ES). Considering that validating $E_s$ using adversarial examples cannot produce significant gains (Fig. 3), we prefer to keep $E_s=10$ to maintain the simplicity of the solution. 4The Mahalanobis solution uses input preprocessing, feature ensemble, feature extraction followed by metric learning, and adversarial validation [2]. 5Detection accuracy [3]. The best results are shown in bold (2% tolerance).

| Model   | Data (training) | Hardware (inference) | Non-seamless Out-of-Distribution Detection: Inference Delays. Presumed Computational Cost and Energy Consumption Rates. |
|---------|----------------|----------------------|------------------------------------------------------------------------------------------------------------------|
|         |                |                      | SoftMax Loss [5] | IsoMax Loss (ours) | ODIN [11], Mahalanobis [2], Generalized ODIN [9] |
|         |                |                      | MPS / ES (ms) [↑] | MPS / ES (ms) [↑] | (ms) [↑] |
| DenseNet | CIFAR10        | CPU / GPU            | 18.1 / 19.4 / 11.6 / 13.0 | 18.0 / 19.2 / 11.6 / 11.5 | 242.4 (≈ 10x slower) / 39.2 (≈ 4x slower) |
|         |                |                      | 18.4 / 19.8 / 12.9 / 11.9 | 18.4 / 19.3 / 11.8 / 11.5 | 261.0 (≈ 10x slower) / 39.6 (≈ 4x slower) |
|         | CIFAR100       | CPU / GPU            | 18.1 / 18.6 / 11.6 / 11.9 | 18.3 / 18.6 / 11.7 / 11.6 | 241.5 (≈ 10x slower) / 39.6 (≈ 4x slower) |
|         | SVHN           | CPU / GPU            | 22.3 / 23.2 / 4.5 / 3.8 | 23.0 / 23.5 / 4.2 / 4.1 | 250.4 (≈ 10x slower) / 15.4 (≈ 4x slower) |
|         |                |                      | 23.3 / 23.1 / 4.3 / 3.9 | 23.3 / 23.8 / 4.3 / 4.2 | 252.6 (≈ 10x slower) / 14.8 (≈ 4x slower) |
|         | SVHN           | CPU / GPU            | 23.1 / 23.4 / 4.2 / 4.0 | 23.4 / 23.3 / 4.0 / 4.0 | 263.8 (≈ 10x slower) / 15.7 (≈ 4x slower) |

MPS means maximum probability score. ES means entropic score. For SoftMax loss and IsoMax loss, the inference delays combine both classification and detection computation. For the methods based on input preprocessing, the inference delays represent only the input preprocessing phase. All values are in milliseconds. The inference delay rates presumably reflect similar computational cost and energy consumption rates.
the OOD detection performance. Table II shows that the IsoMax loss trained models do not show classification accuracy drop.

C. Seamless Out-of-Distribution Detection.

To the best of our knowledge, the proposal presented in [35] and our method are the only solutions that qualify as seamless OOD detection approaches. Table II shows that the models trained with the SoftMax loss using the maximum probability as the score (SoftMax+MPS) always present the worst performance results and that replacing the maximum probability score by the entropic score (SoftMax+ES) produces OOD detection performance gains.

The combination of the models trained using IsoMax loss with the entropic score (IsoMax+ES), which is the proposed solution, significantly improves, usually by several percentage points, the OOD detection performance across almost all datasets, models, out-of-distribution data, and metrics.

The entropic score produces high OOD detection performance when the distributions present high entropy (IsoMax+ES). Indeed, both producing high-entropy distributions and the entropic score contribute to improving the OOD detection performance. However, the contribution of producing high-entropy distributions is considerably more important.

The model does not affect the analyses presented. Indeed, the comments shown above are valid for both DenseNet and ResNet models.

D. Non-seamless Out-of-Distribution Detection.

To tackle non-seamless OOD detection, IsoMax should work as a baseline to be combined with OOD techniques (e.g., outlier exposure, adversarial training, input preprocessing, energy score) rather than competing as a standalone solution. Nevertheless, Table III provides a perspective for how our baseline seamless (standalone) approach compares to non-seamless (composed) solutions.

From a qualitative perspective, ODIN and Mahalanobis use input preprocessing; i.e., to perform OOD detection, each inference requires a first neural network forward pass, a backpropagation, and a second forward pass. They produce slower and less energy-efficient inferences than models trained with IsoMax loss, which are as fast and computationally efficient as the models trained with SoftMax loss. Input preprocessing is indeed a limitation from an economic and environmental perspective.

ODIN requires temperature calibration after neural network training, while the Mahalanobis approach requires feature ensemble and metric learning. Unlike pretraining-based solutions, our approach requires no postprocessing after the neural network training. ACET requires adversarial training, which produces slower training and may limit the application of ACET to large images.

From a quantitative point of view, Table III shows that IsoMax+ES considerably outperforms ODIN in all evaluated scenarios. Therefore, in addition to avoiding hyperparameter tuning and access to the OOD or adversarial samples, the results show that the entropy maximization trick is much more effective in improving the OOD detection performance than temperature calibration, even when the latter is combined with input preprocessing. Furthermore, IsoMax+ES usually outperforms ACET, in some cases by a large margin. Moreover, in most cases, the Mahalanobis method surpasses IsoMax+ES by less than 2%. In some scenarios, IsoMax+ES outperforms the Mahalanobis method.

Table IV presents the inference delays for the SoftMax loss, IsoMax loss, and competing methods using a CPU and GPU. We observe that neural networks trained using the IsoMax loss produce inferences equally as fast as those produced by networks trained using the SoftMax loss, regardless of whether a CPU or GPU is used for inference.

Additionally, the entropic score is as fast as the usual maximum probability score. Moreover, the methods based on input preprocessing were more than ten times slower on the CPU and approximately four times slower on the GPU. These ratios also presumably apply to the computational cost and energy consumption.

To agree with the maximum entropy principle and achieve high performance, rather than generating calibrated maximum probabilities, IsoMax must produce the lowest possible maximum probabilities.

VI. Conclusion

We proposed a seamless OOD detection approach based on logit isotropy and the maximum entropy principle. The proposed IsoMax loss acts as a SoftMax loss drop-in replacement that produces accurate predictions in addition to fast energy- and computation-efficient inferences. No hyperparameter tuning is needed. Hence, no additional procedure other than straightforward neural network training is needed.

OOD detection is performed using the rapid entropic score. Collection of outlier/background data is also not required. To the best of our knowledge, the IsoMax loss does not present any drawbacks compared to the SoftMax loss.

The direct replacement of the SoftMax loss by the IsoMax loss significantly improves the baseline OOD detection performance of neural networks. Therefore, rather than the limitations of the models, the low OOD detection performance of deep networks is due to the SoftMax loss drawbacks, i.e., anisotropy and overconfidence.

In future work, the research community may combine the IsoMax loss with data-based loss regularization techniques to improve the performance. Approaches based on pretrained models or energy-based fine-tuning/score may be applied on IsoMax loss pretrained networks rather than on SoftMax pretrained models.

Thus, rather than competitors, these approaches are actually complementary to IsoMax loss, as they may be combined to achieve even higher overall OOD detection performance. IsoMax loss may replace SoftMax loss as a higher performance baseline for constructing OOD detection solutions.
Another option is to use recent data augmentation techniques. We believe that the simplicity of our solution makes it scalable to large images. Hence, we intend to apply this approach to ImageNet [33]. Finally, since our approach consists of only loss replacement and is based on the general principles of isotropy and maximum entropy, it may be extended to other machine learning methods beyond neural networks.

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