Abstract

We present a new online boosting algorithm for adapting the weights of a boosted classifier, which yields a closer approximation to Freund and Schapire’s AdaBoost algorithm than previous online boosting algorithms. We also contribute a new way of deriving the online algorithm that ties together previous online boosting work. We assume that the weak hypotheses were selected beforehand, and only their weights are updated during online boosting. The update rule is derived by minimizing AdaBoost’s loss when viewed in an incremental form. The equations show that optimization is computationally expensive. However, a fast online approximation is possible. We compare approximation error to batch AdaBoost on synthetic datasets and generalization error on face datasets and the MNIST dataset.

1 Introduction

Most practical algorithms for object detection or classification require training a classifier that is general enough to work in almost any environment. Such generality is often not needed once the classifier is used in a real application. A face detector, for example, may be run on a fixed camera data stream and therefore not see much variety in non-face patches. Thus, it would be desirable to adapt a classifier in an online fashion to achieve greater accuracy for specific environments. In addition, the target concept might shift as time progresses and we would like the classifier to adapt to the change. Finally, the stream may be extremely large which deems batch-based algorithms to be ineffective for training.

Our goal is to create a fast and accurate online learning algorithm that can adapt an existing boosted classifier to a new environment and concept change. This paper looks at the core problem that must be solved to meet this goal which is to develop a fast and accurate sequential online learning algorithm. We use a traditional online learning approach, which is to assume that the feature mapping is selected beforehand and is fixed while training. The paradigm allows us to adapt our algorithm easily to a new environment. The algorithm is derived by looking at the minimization of AdaBoost’s exponential loss function when training AdaBoost with \( N \) training examples, then adding a single example to the training set, and retraining with the new set of \( N + 1 \) examples. The equations show that an online algorithm that exactly replicates batch AdaBoost is not possible, since the update requires computing the classification results of the full dataset by all the weak hypotheses. We show that a simple and approximation that avoids this costly computation is possible, resulting in a
fast online algorithm. Our experiments show that by greedily minimizing the approximation error at each coordinate we are able to approximate batch AdaBoost better than Oza and Russell’s algorithm.

The paper is organized as follows, in section 2 we discuss related work. In section 3 we present AdaBoost in exact incremental form, then we derive a fast approximation to this form, and discuss issues that arise when implementing the approximation as an algorithm. We also compare our algorithm with Oza and Russell’s algorithm [8]. We conclude with experiments and a short discussion in section 4.

2 Related Work

The problem of adapting the weights of existing classifiers is a topic of ongoing research in vision [3, 4, 9, 13]. Huang et al’s [3] work is most closely related to our work. They proposed an incremental learning algorithm to update the weight of each weak hypothesis. Their final classifier is a convex combination of an offline model and an online model. Their offline model is trained solely on offline examples, and is based on a similar approximation to ours. Our model combines both their models into one uniform model, which does not differentiate between offline and online examples. This allows us to continuously adapt regardless of whether or not the examples were seen in the offline or online part of the training. Also, by looking at the change in example weights as a single example is added to the training set, we are able to compute an exact update to the weak hypotheses weights, in an online manner, that does not require a line search as in Huang et al’s work.

Our online algorithm stems from an approximation to AdaBoost’s loss minimization as the training set grows one example at a time. We use a multiplicative update rule to adapt the classifier weights. The multiplicative update for online algorithms was first proposed by Littlestone [7] with the Winnow algorithm. Kivinen and Warmuth [6] extended the update rule of Littlestone to achieve a wider set of classifiers by incorporating positive and negative weights. Freund and Schapire [2] converted the online learning paradigm to batch learning with multiplicative weight updates. Their AdaBoost algorithm keeps two sets of weights, one on the data and one on the weak hypotheses. AdaBoost updates the example weights at each training round to form a harder problem for the next round. This type of sequential reweighting in an online setting, where only one example is kept at any time, was later proposed by Oza and Russell [8]. They update the weight of each weak hypothesis sequentially. At each iteration, a weak hypothesis classifies a weighted example, where the example’s weight is derived from the performance of the current combination of weak hypotheses. Like our algorithm, Oza and Russell’s algorithm has a sequential update for the weights of the weak hypotheses, however, unlike ours, theirs includes feature selection. Our algorithm is also derived from the more recent AdaBoost formulation [11]. We show how the Online Coordinate Boosting algorithm weight update rule can be reduced to Oza and Russell’s update rule with a few simple modifications.

Both our and Oza and Russell’s algorithms store for each classifier an approximation of the sums of example weights that were correctly and incorrectly classified by each weak hypothesis. They can be seen as algorithms for estimating the weighted error rate of each weak hypothesis under memory and speed constraints. Another algorithm that can be seen this way is Bradley and Schapire’s FilterBoost algorithm [1]. FilterBoost uses nonmonotonic adaptive sampling together with a filter to sequentially estimate the edge, an affine transformation of the weighted error, of each weak hypothesis. When the edge is estimated with high probability the algorithm updates its classifier and continues to select and train the next weak hypothesis. Unlike our and Oza and Russell’s algorithm, FilterBoost cannot adapt already selected weak hypotheses weights to drifting concepts.

3 Online Coordinate Boosting

We would like to minimize batch AdaBoost’s bound on the error using a fast update rule as examples are presented to our algorithm. Let \((x_1, y_1), \ldots, (x_{N+1}, y_{N+1})\) be a stream of labeled examples \(x_i \in \mathbb{R}^M, y_i \in \{-1, 1\}\), and let a classifier be defined by a linear combination of weak hypotheses \(H(x) = \text{sign}(\sum_{j=1}^{m} \alpha_j h_j(x))\), where the weights are real-valued \(\alpha_j \in \mathbb{R}\) and each weak hypothesis \(h_j\) is preselected and is binary \(h_j(x) \in \{-1, 1\}\). We use the term coordinate as the index of a weak hypothesis. Let \(m_j = y_j h_j(x_i)\) be defined as the margin which is equal to 1 for correctly classified examples and -1 for incorrectly classified examples by weak hypothesis \(j\).
Throughout training, AdaBoost maintains a weighted distribution over the examples. The weights at each time step are set to minimize the classification error according to batch AdaBoost [10]. Adding a single example to the training set changes the weights of the examples, and the weights of the entire classifier. AdaBoost defines the weight of example \( i \) as \( d_{i,j} = e^{-\sum_{j=1}^{m_{i,j}} \alpha_j m_{i,j}} \), which implies \( d_{i,j} = d_{i,j-1} e^{-\alpha_j m_{i,j-1}} \). Furthermore, the weight of a weak hypothesis \( J \) is defined as \( \alpha_J = \frac{1}{2} \log W_j^+ / W_j^- \), where the sums of correctly and incorrectly classified examples by weak hypothesis \( j \) are defined by \( W_j^+ = \sum_{i: m_{i,j}=+1} d_{i,j} \) and \( W_j^- = \sum_{i: m_{i,j}=-1} d_{i,j} \) correspondingly. We define \( \mathbf{1}_i \) as the indicator function.

We use superscript to indicate time, which in the batch setting is the number of examples in the training set. Adding a single example to the training set changes the weights of the examples, and the weights at each time step are set to minimize the classification error according to batch AdaBoost [10]. Throughout training, AdaBoost maintains a weighted distribution over the examples. The weights of each weak hypothesis from \( d_{i,j} \) represent the sign of the margin of the examples being grouped by the cumulative sum. Formally, we will break these subsets to subsets over \( N \) weights \( \{d_{1,j}, \ldots, d_{N,j}\} \), and the weight of the last ex-

3.1 AdaBoost in exact incremental form

AdaBoost’s loss function \( Z_{j+1} = \sum_i d_{i,j} e^{-\alpha_j m_{i,j}} \) bounds the training error. It has been shown [10, 11] that minimizing this loss tends to lower generalization error. We are motivated to minimize a fast and accurate approximation to the same loss function, as each example is presented to our algorithm. Similarly to AdaBoost, we fix all the coordinates up to coordinate \( J \), and seek to minimize the approximate loss at the \( J \)th coordinate. The optimization is done by finding the update \( \Delta \alpha_j^N \) that minimizes AdaBoost’s approximate loss with the addition of the last example. More formally, we are given the previous weak hypotheses weights \( \alpha_1^N, \ldots, \alpha_J^N \) and their updates so far \( \{\alpha_1^N, \ldots, \alpha_{J-1}^N\} \) and wish to compute the update \( \Delta \alpha_J^N \) that minimizes \( Z_{J+1} \). The resulting update rule is the change we would get in coordinate \( J \)’s weight if we trained batch AdaBoost with \( N \) examples and then added a new example and retrained with the larger set of \( N+1 \) examples. Looking at the derivative of batch AdaBoost’s loss function when adding a new example, we get the update rule for \( \Delta \alpha_j^N \):

\[
Z_{j+1} = \sum_{i=1}^{N+1} d_{i,j} e^{-\alpha_j^{N+1} m_{i,j}} = \sum_{i=1}^{N+1} d_{i,j} e^{-(\alpha_j^N + \Delta \alpha_j^N) m_{i,j}} 
\]

\[
\frac{\partial Z_{j+1}}{\partial \alpha_j^N} = -\sum_{i=1}^{N+1} d_{i,j} e^{-(\alpha_j^N + \Delta \alpha_j^N) m_{i,j} m_{i,j}} 
\]

\[
= \sum_{i: m_{i,j}=-1} d_{i,j} e^{(\alpha_j^N + \Delta \alpha_j^N)} - \sum_{i: m_{i,j}=+1} d_{i,j} e^{-(\alpha_j^N + \Delta \alpha_j^N)} 
\]

\[
= W_{j+1}^N e^{(\alpha_j^N + \Delta \alpha_j^N)} - W_{j+1}^N e^{-(\alpha_j^N + \Delta \alpha_j^N)}. 
\]

Setting the derivative to zero and solving for \( \Delta \alpha_j^N \) we get:

\[
\Delta \alpha_j^N = \frac{1}{2} \log \frac{W_{j+1}^N}{W_{j+1}^{N+1}} - \alpha_j^N = \alpha_j^{N+1} - \alpha_j^N. 
\]

The update \( \Delta \alpha_j^N \) that minimizes \( Z_{j+1} \) is dependent on two quantities \( W_{j+1}^N \) and \( W_{j+1}^{N+1} \). These are the sums of weights of examples that were respectively classified correctly and incorrectly by weak hypothesis \( J + 1 \), when training with \( N + 1 \) examples.

We rewrite these sums in an incremental form. The incremental form is derived by separating the weight of the last example that was added to each of the sums from the rest of the sum. This will allow us later on to compute a fast incremental approximation to them, resulting in our online algorithm. We combine the analysis of both sums by incorporating the parameter \( \sigma \in \{-1, +1\} \), which represents the sign of the margin of the examples being grouped by the cumulative sum. Formally, we will break these subsets to subsets over \( N \) weights \( \{d_{1,j}, \ldots, d_{N,j}\} \), and the weight of the last ex-
ample $d_{N+1, j}$ which is added to the appropriate sum using the function $g_j^N = d_{N+1, j} \mathbf{1}_{[m_{N+1, j} = \sigma]}$:

$$
W_{j}^{N+1} = \sigma \sum_{i: m_{i, j} = \sigma} d_{i, j} = \sum_{i'} d_{i', j} + g_j^N = \sum_{i'} \prod_{j=1}^{J-1} e^{-\alpha_j^{N+1} m_{i, j}} + g_j^N
$$

$$
= \sum_{i'} \prod_{j=1}^{J-1} e^{-(\alpha_j^N + \Delta \alpha_j^N) m_{i, j}} + g_j^N = \sum_{i'} d_{i', j}^{N} \prod_{j=1}^{J-1} e^{-\Delta \alpha_j^N m_{i, j}} + g_j^N.
$$

We define the subsets of examples as $i'_j = \{i | (m_{i, j} = \sigma) \land (i \leq N)\}$. We partition the indices of the first $N$ examples to two subsets: a subset of correctly classified examples, where $\sigma = +1$, and incorrectly classified examples, where $\sigma = -1$.

### 3.2 A fast approximation to the incremental form

Equation 7 is a sum product expression which is costly to compute and requires that the margins of all previous examples be stored. In order to make this an online algorithm which stores only one example in the memory, we approximate each term in the product with a term that is independent of all previous terms. The approximation error at each coordinate is approximated by new terms that are independent of $q_j$.

**Theorem 1**: The approximation forms give us a way to compute the exact error for any choice of $m_{i, j}$. However, the exact error expression may have $2^J$ terms and exactly minimizing it may be costly. Instead, by taking a greedy approach and looking at a part of the error terms we are able to minimize the approximation error at each coordinate. We formulate the problem as follows: nature chooses a set of margins $m_{ij}$ and the booster chooses $q_{i', j}^N, \ldots, q_j^N$ to minimize the approximation error of the boosted classifier at each coordinate. Let $\delta_j = e^{-\Delta \alpha_j} - e^{\Delta \alpha_j}$, then for each weak hypothesis, if nature chooses the margin $m_{ij} = -1$, according to 10, the squared error at coordinate $j$ is $(q_j^N)^2 \delta_j^2$. If nature chooses a margin $m_{ij} = +1$, then according to 11, the squared error at coordinate $j$ is $(1 - q_j^N)^2 \delta_j^2$. We look at squared error to avoid negative errors. Regardless of the choice of margin, we can only make one type of error since the margins are binary.

**Theorem 1** gives us the solution for parameters $q_j^N$ using a greedy minimization of the weighted squared approximation error at each coordinate.
Theorem 1. Let the weighted squared approximation error at coordinate \( j \) and sign \( \sigma \) be defined by
\[
e_j^2 = \sum_{i_j^\sigma} d_{i_j}^N \left( 1_{[i:m_{i_j}=-1]}(q_{i_j}^\sigma)^2 \delta_j^2 + 1_{[i:m_{i_j}=+1]}(1-q_{i_j}^\sigma)^2 \delta_j^2 \right).
\] (12)

Then, the minimizer \( q_{j}^\sigma \) of the weighted approximation error at coordinate \( j \) is:
\[
q_{j}^\sigma = \frac{\sum_{i_j^\sigma \land m_{i_j}=+1} d_{i_j}^N}{\sum_{i_j^\sigma} d_{i_j}^N}.
\] (13)

Proof. Using a greedy approach and looking at the weighted squared approximation error at a single coordinate \( j \) given the weights of the examples at coordinate \( J \), we solve for \( q_{j}^\sigma \). Since the error function is convex, we can take derivatives and solve to find the global minimum:
\[
\frac{\partial e_{j}^\sigma}{\partial q_{j}^\sigma} = 2\delta_j^2 \sum_{i_j^\sigma} d_{i_j}^N \left( 1_{[i:m_{i_j}=-1]}q_{i_j}^\sigma - 1_{[i:m_{i_j}=+1]}(1-q_{i_j}^\sigma) \right).
\] (14)

We solve for \( q_{j}^\sigma \) by setting the derivative to zero. We can divide by \( \delta_j \) since all the example weights are positive and therefore \( \delta_j \neq 0 \).
\[
q_{j}^\sigma = \frac{\sum_{i_j^\sigma \land m_{i_j}=+1} d_{i_j}^N}{\sum_{i_j^\sigma} d_{i_j}^N} = \frac{\sum_{i_j^\sigma \land m_{i_j}=+1} d_{i_j}^N}{\sum_{i_j^\sigma} d_{i_j}^N}.
\] (15)

\[\square\]

Theorem 1 has a very natural interpretation. The minimizer \( q_{j}^\sigma \) can be seen as the weighted probability of weak hypothesis \( j \) producing a positive margin and weak hypothesis \( J \) producing a margin \( \sigma \) (either positive or negative).

3.3 Implementing the approximation as an algorithm

Initialization: The recursive form of equation 9 requires us to define a setting for \( W_0^\sigma \). Let \( W_0^\sigma = |i_0^\sigma| \) be the count of examples with a \( \sigma \) margin with the first weak hypothesis. This is equivalent to setting the initial weight of each example to one, which gives all the examples equal weight before being classified by the first weak hypothesis.

Weight updates: Theorem 1 shows that calculating the error minimizer requires keeping sums of weights which involve two weak hypotheses \( j \) and \( J \). Similarly to our approximation of the sums of weights \( W_j^{\sigma N+1} \), we need to approximate \( q_{j}^\sigma \) as examples are presented the online algorithm. Applying the same approximation to estimate \( q_{j}^\sigma \) yields a similar optimization problem, however the approximation error minimizers for this problem involves three margins. We avoid calculating this new minimizer, and instead use the same correction we used for \( W_j^{\sigma N+1} \) (see Algorithm 1.)

Running time: Retraining AdaBoost for each new example would require \( O(N^2 J^2) \) operations, as the classifier needs to be fully trained for each example. By using our approximation we can train the classifier in \( O(N J^2) \), where the processing of each example takes \( O(J^2) \). A tradeoff between accuracy and speed can be established by only computing the last \( K \) terms of the product, and assuming that the others are equal to one. This speedup results in running time complexity \( O(N J K) \), where \( K \) will be defined as the order of the algorithm. Algorithm 1 shows the Online Coordinate Boosting algorithm with order \( K \).

3.4 Similarity to Oza and Russell’s Online algorithm

Let us compare Oza and Russell’s algorithm [8] to our algorithm. Excluding feature selection, there are two steps in their algorithm. The first adds the example weight to the appropriate cumulative sum, and the second reweights the example. Step one is identical to the addition that our algorithm performs if we assume that all the terms in the product in equation 9 are equal to one, or equivalently...
Algorithm 1 K-order Online Coordinate Boosting

Input: Example classifications $M \in \{-1, 1\}^{N \times J}$ where $m_{ij} = y_i h_j(x_i)$
Order parameter $K$
Smoothing parameter $\epsilon$

Option 1: Initialize $\alpha_j = 0, \Delta \alpha_j = 0$ where $j = 0, \ldots, J$
$W_j^+ = \epsilon, W_j^- = \epsilon$ where $j, k = 0, \ldots, J$

Option 2: Initialize using AdaBoost on a small set.

for $i = 1$ to $N$ do
    $d = 1$
    for $j = 1$ to $J$ do
        $j_0 = \max(0, j - K)$
        $\pi^+_j = \prod_{j=0}^{j-1} \left( \frac{W_j^+}{W_j^-} e^{-\Delta \alpha_k} + (1 - \frac{W_j^+}{W_j^-}) e^{\Delta \alpha_k} \right)$
        $\pi^-_j = \prod_{j=0}^{j-1} \left( \frac{W_j^-}{W_j^+} e^{-\Delta \alpha_k} + (1 - \frac{W_j^-}{W_j^+}) e^{\Delta \alpha_k} \right)$
        for $k = 1$ to $j$ do
            $W_{jk}^+ \leftarrow W_{jk}^+ \pi^+_j + d 1_{[m_{ik} = +1]} \cdot 1_{[m_{ij} = +1]}$
            $W_{jk}^- \leftarrow W_{jk}^- \pi^-_j + d 1_{[m_{ik} = -1]} \cdot 1_{[m_{ij} = -1]}$
        end for
        $\alpha_{ij} = \frac{1}{2} \log \frac{W_j^+}{W_j^-}$
        $\Delta \alpha_j = \alpha_j - \alpha_j^{i-1}$
        $d \leftarrow d e^{-\alpha_j m_{ij}}$
    end for
end for

Output: $\alpha_1^N, \ldots, \alpha_J^N$

that $\Delta \alpha_j = 0$. At step two, reweighting the example, Oza and Russell break the update rule to two cases, one for each type of margin:

$$m_{ij} = +1 : \quad d \leftarrow d \frac{W_j^+ + W_j^-}{2W_j^+} = \frac{d + d \left( \frac{W_j^-}{W_j^+} \right)}{2} \quad (16)$$

$$m_{ij} = -1 : \quad d \leftarrow d \frac{W_j^+ + W_j^-}{2W_j^-} = \frac{d + d \left( \frac{W_j^+}{W_j^-} \right)}{2} \quad (17)$$

The two cases can be consolidated to one case when we introduce the margin into the equations. Interestingly, this update rule smooths the examples weights by taking the average between the old weight and the new updated weight that we would get by AdaBoost’s exponential reweighting [11]:

$$d \leftarrow d + \frac{d + d \left( \frac{W_j^+}{W_j^-} \right)}{2} = d + \frac{d e^{-\alpha_j m_{ij}}}{2} \quad (18)$$

If we do not perform corrections to the W’s, and only add the weight of the last example to them, we reduce our algorithm to a form similar to Oza and Russell’s algorithm. Since Oza and Russell use an older AdaBoost update rule, when put in an online framework, the weights in their algorithm are squared and averaged compared to our weights.

4 Experiments and Discussion

We tested our algorithm against modified versions of Oza and Russell’s online algorithm. The only modification was the removal of the weak hypothesis selection process. Instead we fixed a predefined set of ordered weak hypotheses. Three experiments were conducted, the first with random
data, the second with the MNIST dataset, and the third with a face dataset. Throughout all our experiments we initialized our algorithm with the cumulative weights that were produced by running AdaBoost on a small part of the training set. We needed to initialize our algorithm to avoid divide-by-zero errors when only margins of one type have been seen for small numbers of training examples. We similarly initialized Oza and Russell’s algorithm, however, since our training sets are large, it had little influence on their algorithm’s performance compared to a non-initialized run.

(a) Synthetic: Average approximation error as the number of training examples is increased. Concept drift every $10K$ examples. Averaged over 5 runs. Accuracy improves with higher order.

(b) MNIST: Combined classifier test error as the number of training examples is increased. OCB and AdaBoost achieve lower test error rates than Oza and Russell’s algorithm.

(c) Face data: Average normalized approximation error as the number of training examples is increased. Averaged over 10 permutations of the training set. OCB best approximates AdaBoost.

(d) Face data: Average 1-AUC as the number of training examples is increased. OCB and AdaBoost have almost identical performance on 100K test set.

Figure 1: Approximation and Test error experiments

**Synthetic data:** The synthetic experiment was set up to test the adaptation of our algorithm to concept change, and the effects of the algorithm’s order on its approximation error. We created synthetic data by randomly generating multiple margin matrices $M_t$ which contain margins $m_{ij}$. Each matrix was created one column at a time at which we draw a random number between zero and one for each column. The random number gives us the probability of the weak hypothesis classifying an example correctly. To simulate concept drift, each matrix $M_t$ was generated by perturbing the probabilities of the previous matrix by a small amount and sampling new margins accordingly. We consider the normalized approximation error of the classifier learned by the online algorithms and the equivalent boosted classifier. Let the normalized approximation error between AdaBoost’s weight vector and another weight vector be defined by $err(\alpha_{ada}, \alpha) = 0.5 \| \frac{\alpha_{ada}}{\|\alpha_{ada}\|} - \frac{\alpha}{\|\alpha\|} \|_1$. We compared the approximation error for each example that was presented to the online algorithms with the equivalently trained batch classifier. The experiment was repeated 5 times with different margin generation probabilities. Each experiment comprised of three $M_t$ matrices of size $10,000 \times 20$, thereby simulating concept drift every 10,000 examples. Figure 1(a) shows the average approximation error as the number of training examples is increased. Increasing our algorithm’s order shows improvement in performance. However, we have witnessed that a tradeoff exists when training large classifiers, where the approximation deteriorates as the order is increased too much. The tradeoff exists since $q_{ij}^*$ is a greedy error minimizer, and might not optimally minimize the total approximation error.

**Face data:** We conducted a frontal face classification experiment using the features from an existing
face detector. These weak hypotheses are thresholded box filter decision stumps. The trained face detector contains 1520 weak hypotheses, which were learned using batch AdaBoost with resampling [5, 12]. Using the existing set of weak hypotheses, we compared the different online algorithms for approximation and generalization error on new training and test sets. Both our training and test sets consist of 93,000 non-face images collected from the web, and 7,000 hand labeled frontal faces all of size $24 \times 24$. We created 10 permuted training sets by reordering the examples in the original training set 10 times. The experimental results were averaged over the 10 sets. This was done to verify that our algorithm is robust to any ordering. Our algorithm was initialized with the cumulative sums of weights obtained by training AdaBoost with the first 5000 examples in each training set. Initializing Oza’s algorithm did not improve its performance. We compared the online algorithms to AdaBoost’s while training for every 10,000 examples. The training results in figure 1(d) show that our online algorithm with order 400 achieves better average AUC rates than Oza and Russell’s algorithm.

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