The initial period function of late-type binary stars and its variation

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ABSTRACT

The variation in the period distribution function of late-type binaries is studied. It is shown that the Taurus-Auriga pre-main-sequence population and the main-sequence G dwarf sample do not stem from the same parent period distribution with better than 95 per cent confidence probability. The Lupus, Upper Scorpius A, and Taurus-Auriga populations are shown to be compatible with being drawn from the same initial period function (IPF), which is inconsistent with the main-sequence data. Two possible IPF forms are used to find parent distributions to various permutations of the available data, which include Upper Scorpius B (UScB), Chameleon, and Orion Nebula Cluster pre-main-sequence samples. All the pre-main-sequence samples studied here are consistent with the hypothesis that there exists a universal IPF that is modified by binary-star disruption if it forms in an embedded star cluster leading to a general decline of the observed period function with increasing period. The pre-main-sequence data admit a log-normal IPF similar to that arrived at by Duquennoy & Mayor (1991, A&A, 248, 485) for main-sequence stars, provided the binary fraction among pre-main-sequence stars is significantly higher. However, for consistency with proto-stellar data, the possibly universal IPF ought to be flat along the log-P or log-semi-major axis and must be similar to the K1 IPF form derived by means of inverse dynamical population synthesis, which has been shown to lead to the main-sequence period function if most stars form in typical embedded clusters.

Key words. binaries: general – stars: formation – stars: late-type

1. Introduction

The initial distribution of orbital periods of binary-star systems, i.e. the initial period function (IPF), poses an important constraint on star-formation theory as well as being a necessary input for modelling stellar populations. Constraining its form, and its possible variation with star-forming conditions, is thus of fundamental importance. Observations of late spectral-type systems (stellar masses ≤2 $M_\odot$) have shown that many young populations have a higher binary proportion than old Galactic-field populations (Mathieu 1994; Zinnecker & Mathieu 2001, for reviews; and more recently Duchêne et al. 2007a,b; Connelley et al. 2008), at least within a certain range of binary star periods. Duchêne (1999) performed a comprehensive comparison of various young stellar groups in terms of their binary properties and concluded that very young star-forming regions are very likely to have a binary excess compared to the field or star clusters. This conclusion is enhanced by the study of proto-stars by Connelley et al. (2008).

However, variations between young populations also appear to be evident, such as when comparing the Taurus-Auriga (Köhler & Leinert 1998) and Orion Trapezium Cluster populations (Prosser et al. 1994; Petr et al. 1998; Petr 1998; Simon et al. 1999) that have a similar age (≈1 Myr). Connelley et al. (2008) even study the possible variation in the shape of the proto-stellar period function as proto-stars transcend the various stages of their spectral energy distribution evolution. The source of these variations must be understood to unearth any possible systematic variations with the boundary conditions of their birth environment.

In this contribution, we postulate the existence of a universal IPF and test it against observations of binary period distributions for various star-forming regions.

1.1. Binary formation

In this subsection we discuss the theoretical understanding of binary-star formation and of the limitations thereof.

The formation of binary systems remains an essentially unsolved problem theoretically (e.g. Maury et al. 2010). Fisher (2004) shows analytically that isolated turbulent cloud cores can produce a (unknown) fraction of binary systems with the very wide range of orbital periods as observed. However direct cloud collapse calculations are very limited in predicting binary-star properties owing to the severe computational difficulties of treating the magneto-hydrodynamics together with correct radiation transfer and evolving atomic and molecular opacities during collapse. Available results obtained by applying the necessary computational simplifications suggest the preference of a typical period, around $IP \approx 4$, but such a narrow period distribution cannot be transformed to the observed wide range of periods, $0 \leq IP \leq 10$ (Kroupa & Burkert 2001).

The currently most advanced hydrodynamical simulations were reported by Moeckel & Bate (2010). They allow a turbulent SPH cloud to collapse forming a cluster of 1253 stars and brown dwarfs amounting to 191 $M_\odot$. The cluster has a radius of about 0.05 pc and contains a substantial binary and higher-order
multiple stellar population with a large spread in semi-major axis, $a$, that however peaks at a few AU. After dynamical evolution with or without expulsion of the residual gas, the distribution of orbits remains quite strongly peaked at a few AU with a significant deficit of orbits with $a > 10$ AU compared to the main-sequence population (their Fig. 11). This state-of-the-art computation therewith confirms the above stated issue that it remains a significant challenge for star-formation theory to account for the Gaussian-type distribution of a spanning $10^5 - 10^8$ AU as observed by Duquennoy & Mayor (1991) and Raghavan et al. (2010) for G-dwarfs, by Mayor et al. (1992) for K-dwarfs, and by Fischer &Marcy (1992) for M-dwarfs in the Galactic-field. One essential aspect still missing from these computations is the stellar feedback that starts to heat the cloud as soon as the first proto-stars appear. These heating sources are likely to counter the gravitational collapse such that in reality the extreme densities are not achieved allowing a much larger fraction of wide binaries to survive.

More general theoretical considerations suggest that star formation in dense clusters ought to have a tendency towards a lower binary proportion in warmer molecular clouds (i.e. in cluster-forming cores) because of the reduction in the available phase-space for binary-star formation with increasing temperature (Durisen & Sterzik 1994, hereinafter DS). On the other hand, an enhanced binary proportion for orbital periods $IP \lesssim 5.6$ may be expected in dense clusters owing to the induction of binary formation by means of tidal shear (Horton et al. 2001, hereinafter HBB), thus possibly compensating for the DS effect. The initial period distribution function (IPF) may thus appear similar in dense and sparse clusters, apart from deviations at long periods caused by encounters and the cluster tidal field. A certain fraction of stars form in small-$N$ systems, and the dynamical decay of these is likely to affect the final distribution of $IP \lesssim 5$ binaries (Sterzik & Durisen 1998), giving rise to a non-uniform jet activity (Reipurth 2000), but again, quantification of this is next-to-impossible given the neglect of the hydrodynamical component. However, the binary formation channel must vastly dominate over the formation of non-hierarchical higher-order multiples because otherwise even low-density pre-main-sequence stellar populations would have a large fraction of single stars because initially non-hierarchical multiple systems decay on a core-crossing timescale ($\approx 5 \times 10^5$ yr, Goodwin &Kroupa 2005). The low preponderance of high-order multiple proto-stars in observational surveys is noteworthy in this context (Duchêne et al. 2007a).

1.2. On the existence of a universal IPF

This subsection deals with the question whether the existence of a universal IPF can be deduced from observational data.

Assuming binary systems emerge, by whatever process, with a universal IPF consistent with the pre-main-sequence data, and that most stars form in embedded clusters of modest density, Kroupa (1995a, hereinafter K1, 1995b, hereinafter K2) shows that the IPF evolves on a few cluster crossing time scales to the observed Galactic-field, or present-day period function (PDPF). Applying this approach to dense embedded clusters, Kroupa et al. (1999, hereinafter KPM) and Kroupa et al. (2001, hereinafter KAH) find consistency with the observed period function in the Orion Nebula Cluster despite assuming the universal K1 IPF. This suggests that observed variations in the pre-main-sequence-star period function may be attributed to the dynamical history of the respective population, and that there may formally exist a universal parent IPF that emerges from the binary-star formation process and from which the observed pre-main-sequence and main-sequence cases can be generated.

We note that this universal IPF is strictly speaking not observable because of the rapid evolution after binary star birth, but the formal concept of a parent IPF is useful for synthesizing binary star populations. This concept is equivalent to that of a universal IMF. Given that the parent distribution of stellar masses that emerges after the proto-stellar phase has been found to be invariant, it is natural to state theInvariant Initial Binary Population Hypothesis (Kroupa 2011). Indeed, given that it is known that the stellar IMF is invariant over a large region of physical star-forming regime, it would be expected that a universal IPF ought also to exist. This is because the mass of a star is the last quantity to be established in the star-formation process, with the binary property of a stellar system being established, essentially, at a prior formation stage. Discarding the notion of a universal IPF, the above star-cluster work at least shows that the dynamical history of a population needs to be taken into account before discussing variations in the period distributions.

There are two general processes driven by fundamentally different physics that evolve an IPF with time. On the one hand, system-internal processes such as the tidal circularisation, star-disk interactions, and decay of small-$N$ proto-systems affect binaries with periods $IP \lesssim 5$. K2 referred to this collectively as a pre-main-sequence eigenevolution of the orbital parameters. Eigenevolution leads to period-eccentricity and period-mass-ratio correlations. On the other hand, binaries with $IP \gtrsim 5$ are affected by encounters in embedded clusters (stimulated evolution of the period function). Stimulated evolution does not significantly evolve the eccentricity distribution of a population, but leads to a depletion of the initial period and mass-ratio distribution function for companions with weak binding energy (e.g. K1; K2; Parker et al. 2009).

The aim of this contribution is to quantify the significance of the variation in the observed period distribution of various populations of binary systems in order to allow an improved assessment of a possible underlying parent distribution of orbital periods or equivalently of semi-major axes. In doing so, we test whether there is an invariant IPF and which form this IPF would have. Two IPF forms are studied, namely the K1 IPF (Eq. (4) below), which was previously suggested to unify the pre-main-sequence and main-sequence binary populations, and a log-normal IPF.

The IPF conceived here is a formal initial period distribution function established after the proto-stellar phase has finished. As such, it may not be observable because pre-main-sequence eigenevolution affects the shorter-period binaries on timescales of about $10^5$ yr, while stellar-dynamical and tidal-field influences affect it at longer binary-star orbital periods on the dynamical timescale of the star-forming system. The IPF is therefore as much a theoretical construct as the IMF is, which is also not observable (see the Cluster IMF Theorem, Kroupa 2008). The notion of a formally invariant IPF is very powerful. If this notion were verified to be consistent with observational data, it would be important as a boundary condition for star-formation theory (e.g. Fisher 2004), and also for the generation of theoretical initial stellar populations, such as for $N$-body experiments of embedded clusters and “classical” binary population synthesis (e.g. de Kool 1996; Johnston 1996), and for dynamical population synthesis (K2; Marks & Kroupa 2011).
The observational data sets used here are briefly presented in the subsections below.

In general, the binary star data provide for each detected binary system, the observed projected separation, $\Delta$ (in AU), which we transform to an estimate of the true semi-major axis, $a$, via $a = \Delta/0.95$ (Leinert et al. 1993). The values of $a$ are then converted to an orbital period using Kepler’s third law, $P_{\text{sys}} = a^3/M_{\text{sys}}$, where $P_{\text{sys}} = P/365.25$ is in yr and $a$ in AU, assuming the system mass $M_{\text{sys}} = 1.3 M_\odot$. This transformation is valid only statistically and not on an individual-object basis. A system mass of $1.3 M_\odot$ is chosen here to reflect the primary being of solar mass with a typical secondary star, which we assume to be of the average stellar mass. Leinert et al. (1993) used a system mass of $1.3 M_\odot$, but this difference amounts to only about 10 percent in log mass and is thus of no consequence for the present analysis. In the case of the DM main-sequence sample and the pre-main-sequence binaries with $IP < 4$ (data by Mathieu 1994; and Richichi et al. 1994), the published $IP$ values are adopted here.

For each observational sample of $N_{\text{obs,sys}}$ systems (each of which may be a binary or a single star), the list of IP values thus obtained is binned into $nb$ bins over the interval $[IP_1, IP_2]$ covered by the observational survey (obtained from the survey interval in AU, $a_1$ to $a_2$, using Kepler’s third law as above). The so constructed histogram has a bin-width $\delta IP = (IP_2 - IP_1)/nb$ (in most cases equal for all bins except where noted otherwise), and in each bin $i$ of width $\delta IP$, there are $N_{\text{obs,bin}}(IP_i)$ binaries. The observational estimate of the true period distribution function, expressed as the binary proportion per unit IP interval, is thus obtained from

$$f_{\text{obs}}(IP_i) = N_{\text{obs,bin}}(IP_i)/N_{\text{obs,sys}} \delta IP_i,$$

with an associated binomial uncertainty (Petr et al. 1998),

$$\epsilon_{\text{obs}}(IP_i) = \left( \frac{f_{\text{obs}}(IP_i) [1 - f_{\text{obs}}(IP_i)]}{N_{\text{obs,sys}} \delta IP_i} \right)^{1/2}.$$

(2)

Binomial uncertainties are used here rather than Poisson uncertainties, $\epsilon_{\text{obs}}(IP_i) = (f_{\text{obs}}(IP_i)/N_{\text{obs,sys}} \delta IP_i)^{1/2}$, since the typical situation at hand is that of observing $N_{\text{obs,bin}}(IP_i)$ successes in $N_{\text{sys}}$ trials, each trial having a probability $f(IP_i)$ of success, whereby $f_{\text{obs}}(IP_i)$ is an estimate of $f(IP_i)$. We note that $\epsilon_{\text{obs}}(IP_i) < \epsilon_{\text{obs}}(IP_i)$.

2.1. Main-sequence data (canonical; can.ms)

The data by Duquennoy & Mayor (1992) is defined as the canonical main-sequence sample because it comprises until recently the largest, and most detailed, multiplicity survey among low-mass main-sequence stars. It mainly consists of G-dwarf stars, but K- and M-dwarf main-sequence binaries have essentially the same period distribution (Fischer & Marcy 1992; Mayor et al. 1992; and Fig. 1 in K1). The characteristics of the DM study that qualify them for the “canonical” main-sequence sample are the large and complete sample of solar-type stars within 22 pc of the Sun, and that all periods are covered. A key finding of the DM study is that the frequency distribution of the binary stars’ orbital periods is unimodal and shows a well-defined log-normal distribution. In this analysis, their published and incompleteness-corrected histogram of IP values, which is based on $N_{\text{obs,sys}} = 164$, is adopted. The range in period covered in the study is $-1.0 \leq IP \leq 10$ with $\delta IP = 1.0$, and $nb = 11$.

A more recent survey of the multiplicity properties of solar-type stars was presented by Raghavan et al. (2010). This survey comprises a sample that is about 2.5 times larger than the DM study and reaches larger distances. In contrast to the DM survey, it is not based on a consistent 13-year spectroscopic survey but uses a compendium of observations from various sources. Raghavan et al. derive a period-distribution that they fit very well using a log-normal form with a peak at $\log_{10} IP = 5.03$ and standard deviation of $\sigma(\log_{10} IP) = 2.28$. The DM log-normal distribution peaks at $\log_{10} IP = 4.8$ and has a standard deviation of $\sigma(\log_{10} IP) = 2.3$. The Raghavan et al. study leads therefore to very similar results, and for the time being we continue to use the DM survey as the canonical one.

2.2. Pre-main-sequence (PMS) data (canonical, can.pms): Taurus-Auriga

The “canonical” PMS sample, is composed of results obtained from multiple star surveys in the Taurus-Auriga star-forming region.

For short orbital periods, i.e. for $IP < 2$, binaries detected by the spectroscopic survey of Mathieu (1992, 1994) are considered. Visual binaries in Tau-Aur, with $4.5 \leq IP \leq 7.5$, were extensively searched and studied by Ghez et al. (1993), Leinert et al. (1993), and Köhler & Leinert (1998), and the data from the latter two publications are included in the “canonical” PMS sample. Slightly shorter period binaries (with $3 \leq IP \leq 4$) were addressed by Richichi et al. (1994), using lunar occultation measurements. Hence, the “canonical” PMS sample covers a significantly wide range of orbital periods, from $IP = 0.5$ to $IP = 7.5$, although not continuously (see lower panel in Fig. 1). All stars included in the “canonical” PMS sample are low-mass stars, similar to the stars included in the “canonical” MS sample. The PMS sample includes classical T Tauri stars and weak-line T Tauri stars that show indistinguishable binary-star period distributions (Köhler & Leinert 1998), and are thus considered as one population in our “canonical” PMS data. Table 1 lists the details for each dataset in terms of, e.g. how many targets, $N_{\text{obs,sys}}$, have been observed, which are the lower and upper survey limits (expressed in lower and upper semi-major axis), or what distance to the region has been assumed.

In the context of a possible dynamical evolution of the binary stars’ period, it is important to note that the average surface density of young stars in Taurus-Auriga is relatively low (Gomez et al. 1993). Variations or changes in the overall period distribution caused by encounters over the age of the current Taurus-Auriga PMS population, which is ~1 Myr, are expected to be small. Only during the earliest evolutionary phases of the systems, i.e. just after the formation of the stars, is some stimulated dynamical evolution conceivable (Kroupa & Bouvier 2003).
2.3. Other pre-main-sequence data

Beside Taurus-Aurigae, the orbital period distribution of binary stars surveyed in the star-forming regions of Lupus, Chamaeleon, Upper Scorpius, and the Orion Trapezium Cluster (Table 1) are considered here. By necessity the binary fractions per separation range as published by the respective researchers are adopted such that here no re-analysis of possible contamination is performed as it would go beyond the scope of this contribution.

As for the canonical Tau-Aur PMS data, the surveys comprise low-mass stars with a mixture of weak-line T Tauri and classical T Tauri stars. Although it cannot be completely ruled out that some older ZAMS stars might be included in the samples, the vast majority of the surveyed targets have been confirmed to be of PMS nature (e.g. Covino et al. 1997). Moreover, the orbital period distributions of the samples do not change significantly if the samples are restricted to confirmed PMS stars (e.g. Köhler 2001). None of the surveyed PMS populations in the analysed regions are older than a few Myr. The Orion Trapezium Cluster, with an age of \( \sim 1 \) Myr (Hillenbrand et al. 1997), is likely the youngest region, while Upper Scorpius is the oldest with \( \sim 5 \) Myr (Preibisch et al. 2002). The star-forming regions Chamaeleon and Lupus have ages in-between those of the Orion TC and Upper Scorpius (Chamaeleon: 2 Myr, Luhman 2004; Lupus: \( \sim 2–5 \) Myr, Wichmann et al. 1997; Makarov 2007).

The surveyed regions do have significantly different characteristics with respect to their average stellar densities. Nakajima et al. (1998) analysed the average surface density of companions, which was taken as an indicator of the clustering strength, and found that Lupus is the least clustered region, while the Orion TC is quite strongly clustered. The stellar density in the Orion TC was found to be \( \sim 5 \times 10^4 \) stars/pc\(^3\) (McCaughrean & Stauffer 1994). Chamaeleon is considered as a loose stellar aggregate, similar to Lupus, but with a somewhat higher average stellar density (Nakajima et al. 1998). The region Upper Scorpius is part of the Sco-Cen OB association and does not show such a very high stellar density as the Orion TC, although it is very likely that the original configuration of Upper Sco was much denser than today, but that the stars have dispersed with time. The stellar populations in Upper Scorpius are typically divided into Upper Scorpius A (UScA) and Upper Scorpius B (UScB), as these two regions show spatially distinct distributions. Both regions are found at very similar distances (de Zeeuw et al. 1999) and we assume the same overall distance value of 145 pc as adopted in the binary survey paper of Köhler et al. (2000). A notable difference between UScA and UScB is that UScA contains several high-mass (B-type) stars, while no

### Table 1. Details of binary survey data used in this paper.

| Star-forming region | \( N_{\text{obs,sys}} \) | \( nb \) | \( a_1 \) [AU] | \( a_2 \) [AU] | Adopted distance [pc] | References |
|--------------------|----------------|-------|-------------|-------------|-----------------------|------------|
| Tau-Aur (can.PMS)  | 91             | 2     | \( lP = 0.5 \) | \( lP = 1.5 \) | 140                   | (a)        |
| Tau-Aur (can.PMS)  | 30             | 1     | \( lP = 3.5 \) | \( lP = 3.5 \) | 140                   | (b)        |
| Tau-Aur (can.PMS)  | 178            | 4     | 19.5        | 1832        | 140                   | (c), (d)   |
| Lupus              | 127            | 4     | 18.3        | 1348        | 160                   | (e)        |
| Chamaeleon assoc.  | 77             | 4     | 11.6        | 460         | 160                   | (f)        |
| UScA               | 68             | 3     | 18.0        | 460         | 145                   | (g), (h)   |
| UScB               | 51             | 3     | 18.0        | 460         | 145                   | (g), (h)   |
| Orion TC           | 62             | 1     | 214         | 625         | 450                   | (i), (j)   |
|                    | 109            | 1     | 72.9        | 214         | 450                   | (i), (j)   |
This is a non-parametric test, making no assumptions about the form of the underlying populations, such as there being a well-defined mean and variance, as opposed to using the \( \chi^2 \) statistic, which makes such assumptions about the underlying distributions. The WSR test assesses the likelihood of observing a certain fraction of the data being asymmetrically distributed about a reference data set. To construct the WSR statistic, the differences \( f_{pms}(IP) - f_{ms}(IP) \) are ordered according to their absolute values. These are ranked, and the ranks associated with the positive differences are added to form the test statistic \( T^+ \). The statistic is symmetrical, that is, the same result is obtained by considering the negative differences. For the data in Table 2, \( T^+ = 21 \) with \( n = 6 \) data points. Obtaining such a large or larger \( T^+ \) has a significance probability \( P = 0.016 \) (Table 10 in Bhattacharyya & Johnson 1977). The null hypothesis is thus only supported with a confidence of 1.6 per cent, confirming the above conclusion. Using only the data with \( IP \geq 5 \) gives \( n = 3 \) differences, which is too small for this non-parametric test to allow significant conclusions, in contrast to the \( \chi^2 \) test used above, because the latter relies on additional information about the populations.

The Kolmogorov-Smirnov test cannot be applied here nor later in this paper, because the data sets cover different \( IP \) ranges, and \( f_{rms} \) was estimated by DM after applying incompleteness corrections, that is there exists no list of complete \( IP \) values from which a cumulative distribution can be generated.

### 3. Main-sequence versus pre-main-sequence

We estimate the statistical significance of the difference between the observed main-sequence and the pre-main-sequence binary star period distributions by focussing on the “canonical” main-sequence and pre-main-sequence distributions as defined in Sect. 2. The binary proportion per unit log\(_10\) \( P \) interval is given by Eq. (1) \( f(IP) = \frac{N_{bin}(IP)}{N_{sys}} \), where \( N_{bin}(IP) \) is the number of binaries in the \( i \) th log-period interval \( \delta IP_i \) (=1 here), and \( N_{sys} \) is the total number of systems in the survey, whereby each single star and each binary count as a system. To obtain matching data sets, the main-sequence histogram plotted in Fig. 1 of KPM is linearly interpolated to obtain three \( IP \) bins with unit width for \( IP = 5.0, 6.0, 7.0 \) (i.e. covering the interval \( 4.5 \leq IP \leq 7.5 \)). The resulting data are listed in Table 2.

The well-tried \( \chi^2 \) statistic is applied to test the null hypothesis that both observed distributions stem from the same underlying parent distribution, by calculating

\[
\chi^2 = \sum_{i=1}^{6} \frac{(f_{rms}(IP) - f_{pms}(IP))^2}{e_{rms}^2(IP) + e_{pms}^2(IP)}
\]

(3)

to obtain \( \chi^2 = 15.7 \) with \( v = 6 \) degrees of freedom. Obtaining this large value, or larger, has a significance probability 0.01 < \( P < 0.02 \), so that one can be less than 2 per cent confident that the null hypothesis holds true. Excluding the \( IP < 4 \) bins where the main-sequence and pre-main-sequence data agree within the uncertainties, and concentrating instead only on the more recent Taurus-Auriga data (Köhler & Leinert 1998), we find that \( \chi^2 = 13.2, v = 3 \) with 0.001 < \( P < 0.01 \). The null hypothesis can thus be rejected with approximately 99 per cent confidence. It may be concluded that the two observed distributions stem from different parent distributions.

To obtain an additional assessment of the confidence in this result, the Wilcoxon-Signed-Rank (WSR) test (e.g. Bhattacharyya & Johnson 1977) provides a welcome alternative.

### 4. Standard period functions

After establishing with a high level of confidence that the canonical pre-main-sequence and main-sequence period distributions differ significantly, one can proceed to begin inquiring as to how the parent distributions of the two data sets may be described. In the literature, two analytic forms of possible parent distributions for the two data sets have been used.

#### 4.1. Initial period functions (IPFs) and present-day period functions (PDPFs)

For pre-main-sequence binary systems, K1 suggests an IPF,

\[
f_k(IP) = f_{pms} \frac{\eta}{\delta + (IP - IP_{min})^2},
\]

(4)

using the canonical pre-main-sequence and main-sequence data as constraints. This does not contradict the results of the previous section since one takes into account through extensive N-body modelling that the main-sequence distribution results from the pre-main-sequence distribution if most stars form in modest (embedded) clusters. K1 found that \( \eta = 3.5 \) and \( \delta = 100 \) provide good fits to the pre-main-sequence data, and to the main-sequence data after passing through a typical star cluster\(^7\) assuming that the overall primordial binary proportion is \( f_{pms} = 1 \), and setting the minimum orbital period to 1 d (\( IP_{min} = 0 \)). As seen in Fig. 1, we note in particular that \( f_k(IP) \) is essentially flat for \( IP \geq 4.5 \) (\( \eta \geq 20 \) AU). With the above parameters Eq. (4) is referred to as the K1 IPF, and IPFs constructed with different values of the parameters are said to be of the K type.

\(^7\) The typical star cluster is the birth site of most stars in the Galaxy. According to K1, it contains typically 200 binaries in a characteristic radius of about 0.8 pc, while Adams & Myers (2001) find that most stars would originate from compact 10–100 member groups. This estimate can be argued to correspond to the previous one if residual gas loss and subsequent expansion with loss of stars from the modest embedded cluster are taken into account.
K2 constructed a more elaborate model based on the above
K1 IPF, but including eigenevolution for the correct correlation
between eccentricity, period, and mass ratio of short-period bi-
naries. This model has $IP_{\text{min}} = 1, \eta = 2.5, \delta = 45$ and is required to
reproduce and predict the period- and mass-ratio-distribution
functions and the distribution of orbits in the eccentricity-period
diagram for realistic stellar populations. These details are, how-
ever, not required in the present treatment and would not lead to
different results. A useful feature of Eq. (4) is that it can be
easily converted to a period-generating function (Eq. (11b) in K1)

\[ IP(X) = IP_{\text{min}} + \left[ \delta \left( e^{\frac{X}{\delta}} - 1 \right) \right]^{\frac{1}{\gamma}}, \]

where \( X \in [0, 1] \) is a uniform random variate, and with
\( \int_{IP_{\text{min}}}^{IP_{\text{max}}} f_{K1}(IP) dIP = f_{\text{rms}} \). The maximum allowed log-period,
\( IP_{\text{max}} \), follows from Eq. (5) with \( X = 1 \). Equation (5) allows the
efficient construction of a pre-main-sequence population, as in
\( N \)-body calculations of the evolution of embedded clusters (e.g.
KPM; KAH).

For the PDPF, the Gaussian distribution in \( IP \) describes the
observed period distribution of local G-dwarfs very well (DM)

\[ f_{\text{DM}}(IP) = f_{\text{rms}} \kappa \frac{1}{\sqrt{2\pi} \sigma_{IP}} e^{-\left( \frac{\sqrt{\sigma_{IP}}}{\sigma_{IP}} \right)^{2}}, \]

where \( \sqrt{\sigma_{IP}} \) and \( \sigma_{IP} \) are, respectively, the variance in \( IP \) and
the average-\( IP \), and \( \int_{IP_{\text{rms}}}^{IP_{\text{max}}} f_{\text{DM}}(IP) dIP = f_{\text{rms}} \) is enforced by ad-
justing \( \kappa \), since \( \int_{IP_{\text{rms}}}^{IP_{\text{max}}} f_{\text{DM}}(IP) dIP = f_{\text{rms}} \). DM measured an over-
all binary proportion of \( f_{\text{rms}} = 0.58, \sigma_{IP} = 2.3, \) and \( \sigma_{IP} = 4.8 \).
This is referred to as the DM PDPF, and period functions con-
structed according to Eq. (6) but with different values for the
parameters are referred to as being of the DM type. A simple
period-generating function cannot be written down; we resort
instead to the Box-Muller method for generating \( IP \)s (e.g. Press
et al. 1994).

### 4.2. The tests

We test the confidence with which the IPF (the K1-distribution,
Eq. (4) with \( \eta = 3.5, \delta = 100 \) and \( f_{\text{rms}} = 1 \)) or the
PDPF (the DM-distribution, Eq. (6) with \( \sigma_{IP} = 2.3, \) \( \sigma_{IP} = 4.8 \) and
\( f_{\text{rms}} = 0.58 \)) can represent each data set of Sect. 2.

For each observational sample, the theoretical distributions
are converted to matching histograms by generating \( N_{\text{th,sys}} = 10^{6} \) periods and binning these into the same \( IP \)-bins as in the
respective observational sample, obtaining (Eq. (1))

\[ f_{\text{th}}(IP_{i}) = f_{o} N_{\text{th,bin}}(IP_{i}) / (N_{\text{th,sys}} \delta IP_{i}), \]

where \( f_{o}(IP_{i}) \) is either of the K (\( f_{o} = f_{\text{rms}} \)) or the DM (\( f_{o} = f_{\text{rms}} \)) type. Given the size of an observa-
tional sample, \( N_{\text{obs,sys}}, \) the expected number of binaries in each
\( IP \) bin is

\[ N_{\text{exp,bin}}(IP_{i}) = f_{o}(IP_{i}) N_{\text{obs,sys}} \delta IP_{i}, \]

with the associated expected binomial uncertainty

\[ \epsilon_{N_{\text{exp,bin}}(IP_{i})} = \left[ f_{o}(IP_{i}) \right] \left( 1 - f_{o}(IP_{i}) \right) \delta IP_{i} N_{\text{obs,sys}} \frac{1}{2}. \]

To quantify the goodness-of-fit, the \( \chi^{2} \) statistic for the K or
DM distribution becomes

\[ \chi^{2}_{K(\text{DM})} = \sum_{i=1}^{\text{nb}} \left( \frac{N_{\text{exp,bin}}(IP_{i}) - N_{\text{obs,bin}}(IP_{i})}{\epsilon_{N_{\text{exp,bin}}(IP_{i})}} \right)^{2}. \]

### 4.3. Results

The above procedure is applied to all the data and the results
are shown in Fig. 1. The conclusion with very high confidence
(at the 99.5 per cent level or better) is that the canonical main-
sequence data are inconsistent with the K1 IPF (upper panel),
and that the canonical pre-main-sequence data are inconsistent
with the DM PDPF (lower panel). This does not change even if
\( IP = 9.5 \) main-sequence value is ignored in the upper panel
(giving \( \chi^{2} > 43 \) with \( P = 0.00 \) for the K1 IPF). This result is
consistent with that of Sect. 2, where it was shown that the canonical main-sequence and pre-main-sequence data differ signif-
ically.

The results of applying this procedure to each of the pre-
main-sequence data sets are presented in Fig. 2. It is evident
that the Taurus-Auriga, Lupus, and UScA populations are consis-
tent with the hypothesis that they be drawn from the K1 IPF.
The Cham pre-main-sequence population is marginally consis-
tent with the hypothesis that the parent distribution is the K1 IPF
at the 5 per cent confidence level, whereas the full UScB sam-
ple is only consistent with the K1 IPF at the 3 per cent confi-
dence level. UScB becomes consistent at the 19 per cent confi-
dence level with the K1 IPF if three of the widest binaries are
removed from the sample, assuming these are significantly
closer (<90 pc) than the bulk of UScB stars at ~145 pc. Their
apparent brightness is clearly brighter than expected for their
spectral type when placed at 145 pc, and proper motion mea-
surements confirm nearby distances for at least two of the wide
binary systems (Perryman et al. 1997; Salim & Gould 2003).

On the other hand, an alternative hypothesis is that the data
sets be drawn from the DM PDPF. This hypothesis can be dis-
carded with very high confidence for the Taurus-Auriga, Lupus,
and UScB pre-main-sequence populations. It cannot be dis-
carded for the Cham, UScA, and ONC populations. The Cham
and UScA populations can, in fact, be drawn from either period
function. The higher significance probability for the hypothesis
that Cham be drawn from the DM PDPF is however consistent
with the hypothesis that Cham started off in a clustered mode
with a K1 IPF, the Cham population possibly being an evolved
version of the canonical pre-main-sequence population. This is
also true for the ONC sample as shown by KPM and KAH.

### 5. Parent period distribution functions

In Sect. 4.3, the K1 IPF and the DM PDPF were compared with
all the available data sets individually.

In this section, data sets are combined and more general solu-
tions for possible parent distributions of the K and DM types
(Eqs. (4) and (6) respectively) are sought by scanning the pa-
rameter spaces \( \eta, \delta \) and \( \sigma_{IP}, \) \( \sigma_{IP} \) using suitable increments by
evaluating Eq. (9) and the associated significance probability \( P \).
This procedure is demonstrated in Figs. 3 and 4 by first of all
finding all admissible solutions to the canonical data sets. The
solutions found in this way agree with the known solutions
(the K1 IPF and DM PDPF), and one may have confidence in
the algorithm.
Fig. 2. Similar to Fig. 1 but for all pre-main sequence samples. In all panels, the dotted continuous curves are the model distributions (K1 IPF upper curves, DM PDPF lower curves), whereas the model histograms are shown as solid lines with expected binomial uncertainties as dotted error-bars. Thick histograms are the data (Sect. 2). The $\chi^2$ value and probability, $P$, of observing such a large or larger $\chi^2$ is written in each panel (upper numbers for testing the data against the K1 IPF, lower numbers for testing against the DM IPF). For UScB, the lower set of numbers refers to the dotted histogram, which corresponds to the results after removing the three widest binaries from the sample.
When combining $n_{\text{dat}}$ data sets under a common hypothesis, the combined $\chi^2_{\text{comb}}$ and number of degrees of freedom, $n_{\text{bf,comb}}$, are computed as to be

$$n_{\text{bf,comb}} = \sum_i n_{\text{bf}_i},$$

$$\chi^2_{\text{comb}} = \sum_i \chi^2_{i},$$

(10)

where $\chi^2_i$ and $n_{\text{bf}_i}$ are the chi-square and number of degrees of freedom of data set $i$. Possible data sets are $i = \text{Lupus, Cham, UScA, UScB, ONC, canonical pre-main-sequence (=can.pms), and canonical main sequence (=can.ms)}$. The significance probability, $P_{\text{KorDM}}$, of obtaining $\chi^2 \geq \chi^2_{\text{comb}}$, is evaluated as above (Eq. (9)), and $P_{\text{K}}, P_{\text{DM}}$ are the resulting combined confidence probabilities when using the K and DM type PFs, respectively, for testing the hypotheses set up in the following. A hypothesis is deemed consistent with the data if $P_{\text{KorDM}} \geq 5 \times 10^{-2}$, i.e., if the significance probability is 5 per cent or better.

The following hypotheses are tested:

1. A PF of the K type is the parent distribution of all combined data sets ($n_{\text{dat}} = 7$).
   Assuming $f_{\text{ms}} = 1$ and scanning the parameter space, as above, yields no solutions at all in agreement with the data at the 0.001 per cent level or better ($P_{\text{K}} \leq 10^{-5}$). Thus, the hypothesis can be discarded at the 99.999 per cent level.
   Assuming $f_{\text{ms}} = 0.8$ and $f_{\text{ms}} = 0.6$ also leads to the rejection of this hypothesis with $P > 99.999$ per cent confidence.
   The general conclusion, stated with a confidence better than 99.999 per cent, is thus that there is no single parent distribution of the K type for all data sets combined.

2. A PF of the DM type is the parent distribution of all combined data sets ($n_{\text{dat}} = 7$).
   Assuming $f_{\text{ms}} = 0.58, 0.8, 1.0$ and scanning the parameter space, as above, yields no solutions at all in agreement with the data at the 0.001 per cent level or better ($P_{\text{DM}} \leq 10^{-5}$).
   Thus, there is no single Gaussian parent distribution of all data sets combined. The hypothesis is rejected with a confidence of higher than 99.999 per cent.

3. A PF of the K type is the parent distribution of the combined canonical pre-main-sequence and canonical main-sequence data sets ($n_{\text{dat}} = 2$).
   The relevant confidence is determined from Eq. (10) with $[i = \text{can.pms, can.ms}]$. The result is that there is no solution with a confidence better than $P_{\text{K}} = 10^{-5}$ for $f_{\text{ms}} = 1, 0.8, 0.6$, so that this hypothesis can be discarded with a confidence of higher than 99.999 per cent.

4. A PF of the DM type is the parent distribution of the combined canonical pre-main-sequence and canonical main-sequence data sets ($n_{\text{dat}} = 2$).
   The relevant confidence is determined from Eq. (10) with $[i = \text{can.pms, can.ms}]$. There is no solution with confidence better than $P_{\text{DM}} = 10^{-5}$ for $f_{\text{ms}} = 0.6$. For $f_{\text{ms}} = 0.8$, the parameter region $\sigma lP = 2.5 \pm 0.4, \sigma lP = 5.1 \pm 0.2$ has $P \leq 0.1$ per cent, while for $f_{\text{ms}} = 1.0$ the parameter region $\sigma lP = 2.6 \pm 0.4, \sigma lP = 5.2 \pm 0.2$ has $P \leq 0.05$ per cent. This hypothesis can thus be discarded with 99.9 per cent confidence.

5. A PF of the K type is the simultaneous parent distribution of the canonical pre-main-sequence data, as well as of the Lupus and UScA pre-main-sequence data sets ($n_{\text{dat}} = 3$).
   The relevant confidence is determined from Eq. (10) with $[i = \text{can.pms, Lupus, UScA}]$. These are chosen because
Testing hypothesis 5 with \( f_{\text{pms}} = 1.0 \). Survey of \( \eta, \delta \) parameter space for solutions of the K type with \( f_{\text{pms}} = 1 \) (Eq. (4)) for the canonical pre-main-sequence data, together with the Lupus and UScA pre-main-sequence data sets. Open circles and small dots delineate models consistent with the data at the 1 and 5 per cent confidence level, respectively. The K1 IPF is shown as the thick cross, and the straight line is as in Fig. 3. The thick solid dots show models consistent at the 50 per cent level or better.

Testing hypothesis 6 with \( f_{\text{ms}} = 1.0 \). Survey of \( \sigma_{lP}, a_{lP} \) parameter space for solutions of the DM type (Eq. (6)) to the canonical pre-main-sequence data, together with the Lupus and UScA pre-main-sequence data sets. Open circles and small dots delineate models consistent with the data at the 1 and 5 per cent confidence level, respectively. The DM PDPF is shown as the thick cross.

A PF of the DM type is the simultaneous parent distribution of the canonical pre-main-sequence data, the Lupus, and UScA pre-main-sequence data sets (\( n_{\text{dat}} = 3 \)). Scanning \( \sigma_{lP}, a_{lP} \) parameter space leads to solutions with \( P_{\text{DM}} > 10^{-2} \) if \( f_{\text{ms}} = 1.0 \) (Fig. 7), whereas \( P_{\text{DM}} < 5 \times 10^{-4} \) if \( f_{\text{ms}} = 0.8 \) and \( P_{\text{DM}} < 10^{-5} \) if \( f_{\text{ms}} = 0.6 \). Thus, a simultaneous Gaussian parent distribution is only possible, with a significance probability better than 5 per cent, if the pre-main-sequence binary-star fraction is significantly larger than the main-sequence value of 60 per cent (note that \( f_{\text{ms}} \) in Eq. (6) is here the binary-star fraction required for the combined pre-main-sequence samples).

A PF of the K type is consistent with all pre-main-sequence data (canonical, Lupus, UScA, Cham, UScB, and ONC) (\( n_{\text{dat}} = 6 \)). No parent distribution of the K-type can be found with 0.1 per cent confidence or better. This suggests that these pre-main-sequence data sets may either have different IPFs, or that they stem from the same IPF but were modified, as would be expected for example for the ONC data (KPM, KAH). UScB, however, forms a definite outlier, since it has a significant surplus of binary stars at long periods (Fig. 2), when taking the observational results at face value as we do here for all datasets. After removing possible non-members (cf. Sect. 4.3), a surplus of binary stars at long periods persists although being less significant, which cannot be understood in terms of binary-star disruption in embedded clusters.

A PF of the DM type is consistent with all pre-main-sequence data (canonical, Lupus, UScA, Cham, UScB, and ONC) (\( n_{\text{dat}} = 6 \)). No DM-type PF exists with \( P_{\text{DM}} > 5 \times 10^{-4} \), so that this hypothesis can be rejected with 99.95 per cent confidence.
6. A revised IPF

In the previous section, the tests of hypotheses 5 and 6 yielded parameter ranges for Eqs. (4) and (6) that are consistent with the combined data at the 5 per cent confidence level or better. These parameter ranges are shown in Figs. 5 and 6 for K-type solutions, and in Fig. 7 for DM-type solutions. The data sets were selected according to which appeared to be the least evolved, using the a priori knowledge gained in K1 and K2.

It is noteworthy that the K-type solutions ($\eta \approx 2.5$–3, $\delta \approx 40$–70) are consistent within a 5 % confidence level with the K1 IPF ($\eta = 3.5$, $\delta = 100$), thus corroborating the results obtained in K1. This is particularly interesting because here we used data sets including more than one pre-main-sequence population, while in K1 only older Taurus-Auriga data were available but no functional fitting to these data was performed such as here. The K1 IPF was instead obtained using inverse dynamical population synthesis by performing approximate (eye-ball) fits to the pre-main-sequence data, and to the main-sequence data after star-cluster disintegration. The present purely statistical approach confirms the K1 IPF ($\eta \approx 3.5$, $\delta \approx 100$, $f_{\text{pms}} \geq 0.8$, with enhanced confidence probability for larger $f_{\text{pms}}$).

A new result obtained here (Fig. 7) is that a log-normal function in orbital period $P$ can also be considered a parent distribution of the same pre-main-sequence data as above. These data are consistent, at the 5 per cent confidence level or better, with being drawn from a parent distribution of the DM-type, if this PF has parameters indistinguishable from those of the DM PDPF ($\sigma L P \approx 2.3$, $a_{\text{il}} P \approx 5$) but with a significantly larger binary proportion, $f_{\text{pms}} = 1.0$.

The result is thus that either the K1 IPF (Eq. (4)), a K-type solution with $\delta \approx 29.52 \eta$ (straight line in Fig. 5), or the Gaussian PF (Eq. (6)) with the above parameters can be parent distributions of pre-main-sequence binary systems with indistinguishable confidence probabilities. This is illustrated in Fig. 8.

7. Conclusions

A fresh look has been taken at the variations evident in the period distribution of binary stars in various stellar populations. The most notable such difference, noted by many authors, lies between the canonical pre-main-sequence population of Taurus-Auriga and the canonical Galactic-field local G-dwarf population. The difference is significant (Sect. 3), but can be understood to result from the stimulated evolution of an initial Taurus-Auriga-type population if most Galactic-field stars originate in modest embedded clusters (K1). That work arrives at a possible initial period function, the K1 IPF (Eq. (4)), which is nearly flat for $a \geq 20$ AU.

The variation between pre-main-sequence populations is also studied here, with the result that significant differences are evident, notably between the canonical pre-main-sequence population and the ONC and UScB samples. Stimulated evolution in the dense Orion Nebula Cluster efficiently depletes a K1 IPF to the observed data (KPM, KAH), so that the former difference can be readily accounted for. The latter difference, which results from a significant apparent surplus of long-period binaries in UScB, may indicate that the IPF of the UScB population was very different to that in Taurus-Auriga, as noted by Brandner & Köhler (1998). Noteworthy in this context is that UScA, in which mostly binaries with small separations are present, contains several high-mass (B-type) stars, while no high-mass stars are present in UScB, which appears to contain primarily wider binaries. This is qualitatively consistent with UScA perhaps stemming from denser embedded stellar groups that are already dispersed after dynamical evolution and the expulsion of residual gas by the massive stars. Discarding three of the widest binaries in the UScB data set yields a binary population consistent with the K1 IPF (Sect. 4.3), leaving the ONC as the only pre-main-sequence population that clearly differs from the canonical pre-main-sequence population. In any case, among the data sets used in this paper the UScB data has the lowest number of systems surveyed for binarity, and the region is most likely more affected by containing dispersed mixed populations of stars with...
different distances and ages than the other data. Hence, the observed orbital-period distribution of binaries in USCB remains to be confirmed.

The (canonical) Taurus-Auriga, Lupus, and UScA populations appear to be the least-evolved and are consistent with being drawn from a common parent IPF if the binary proportion is higher than on the main sequence. The set of possible IPFs shown in Figs. 5–7, where the K1 IPF is included. Three possible IPFs, all with indistinguishable confidence probabilities, are presented in Fig. 8. While no formal decision can be made based on $P_{\text{KoDM}}$ as to which of the three IPFs plotted in Fig. 8 are to be preferred, the a priori knowledge gained in K1 favours the K1 IPF, because (i) it is consistent with the data at the 10 per cent confidence level; (ii) it is the precursor of the Galactic-field PDPF for a reasonable library of embedded clusters; and (iii) the revised K-type IPF shown as the thin solid line in Fig. 8 leads to a deficit of Galactic-field binaries with $IP \lesssim 6$ (Fig. 8 in K1). Inverse dynamical population synthesis will have it becomes readily apparent that a flat distribution function for a traditional description of the data. Parker et al. (2009) and does suggest that the K1 IPF (Eq. (4)) is a more appropriate description of the data. Parker et al. (2009) come to a similar conclusion and stress that a $a > 10^4$ AU binaries cannot survive in any clustered environment. They may however form during cluster dissolution (Kouwenhoven et al. 2010).

We note that the above three pre-main-sequence populations, and in addition the Cham and ONC populations, are all consistent with a monotonically decreasing PF with increasing IP (Figs. 2 and 8). This may suggest that all known pre-main-sequence populations have already suffered some degree of stimulated evolution, and may have begun with the same (universal) IPF. This notion allows reconstruction of the properties of the embedded clusters from which the pre-main-sequence populations might have originated (inverse dynamical population synthesis). Explicit modelling of this evolution has been performed for the ONC IPF: KAH; Parker et al. 2009) and sparse embedded clusters (K1; K2, Kroupa & Bouvier 2003; Parker et al. 2009).

Thus, at present it cannot be confirmed whether the IPF depends on the star-forming conditions, that is, the presently available data are consistent with an invariant birth or initial binary population.

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