Measurement of the differential cross sections for isolated direct photon pair production in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV

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We present measurements of direct photon pair production cross sections using 8.5 fb$^{-1}$ of data collected with the D0 detector at the Fermilab Tevatron $p\bar{p}$ collider. The results are presented as differential distributions of the photon pair invariant mass $d\sigma/dM_{\gamma\gamma}$, pair transverse momentum $d\sigma/dp_\gamma^T$, azimuthal angle between the photons $d\sigma/d\phi_{\gamma\gamma}$, and polar scattering angle in the Collins-Soper frame $d\sigma/d(\cos\theta^\prime)$. Measurements are performed for isolated photons with transverse momenta $p_\gamma^T > 18$ (17) GeV for the leading (next-to-leading) photon in the jet, pseudorapidities $|\eta^\gamma| < 0.9$, and a separation in $\eta - \phi$ space $\Delta R_{\gamma\gamma} > 0.4$. We present comparisons with the predictions from Monte Carlo event generators DIPHOX and RESBOS implementing QCD calculations at next-to-leading order, 2$\gamma$NNLO at next-to-next-to-leading order, and SHERPA using matrix elements with higher-order real emissions matched to parton shower.

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Precise knowledge of the direct diphoton (DDP) production differential cross section is a cornerstone of the search for the standard model (SM) Higgs boson by experiments at the Large Hadron Collider [1, 2] and the Tevatron [3, 4]. The term “direct” means that these photons do not result from meson, for example, $\pi^0$, $\eta$, $\omega$, or $K^0_S$ decays. DDP production is also a significant background in searches for Kaluza-Klein [5] or Randall-Sundrum [6] gravitons decaying into two photons, as well as other new phenomena processes, such as decays of heavy resonances [7] or cascade decays of supersymmetric particles [8]. For these searches, DDP production is an irreducible background, and it is crucial to have a detailed understanding of the distributions of key kinematic variables [9].

In addition to investigating physics beyond the SM, DDP production processes are important for studying quantum chromodynamics (QCD) and measuring parton distribution functions (PDFs). DDP production cross sections have been examined at fixed-target [10, 11] and collider experiments [12, 17]. DDP events at the Tevatron $p\bar{p}$ collider are produced predominantly through quark-antiquark annihilation $q\bar{q} \to \gamma\gamma$ and gluon-gluon fusion ($gg \to \gamma\gamma$) via a quark-loop diagram. The matrix element (ME) for the latter process is suppressed by $\alpha_s^2$ relative to $q\bar{q}$ annihilation, but its total production rate at low $\gamma\gamma$ invariant mass ($M_{\gamma\gamma}$) and intermediate $\gamma\gamma$ transverse momentum ($p_\gamma^T$) is quite significant due to the relatively large values of the gluon PDFs in that kinematic region. By the same argument, gluon-gluon fusion becomes even more important at the LHC [18]. DDP events may also originate from processes such as $qg \to q\gamma\gamma$, $q\bar{q} \to g\gamma\gamma$, and $gg \to q\bar{q}$, where a photon with large transverse momentum is radiated from the final state parton. These processes, being nearly collinear, require the introduction of a fragmentation function in perturbative QCD (pQCD) calculations [18]. Photon isolation requirements reduce
the contribution of such fragmentation events. However, their contribution may be still quite large at low $\gamma\gamma$ azimuthal angle difference ($\Delta\phi_{\gamma\gamma}$) and for intermediate $p_T^{\gamma\gamma}$ \[18\,19\], which is the DDP transverse momentum.

In this Letter, we present measurements of differential cross sections of DDP production using the dataset collected at the Fermilab Tevatron D0 experiment between June 2006 and September 2011. The dataset corresponds to an integrated luminosity of $8.5 \pm 0.5$ fb$^{-1}$ \[33\].

Measurements are performed as functions of $M_{\gamma\gamma}$, $p_T^{\gamma\gamma}$, $\Delta\phi_{\gamma\gamma}$, and $|\cos \theta^\gamma|$, the absolute value of the cosine of the polar scattering angle of the diphoton system in the Collins-Soper frame \[20\]. Here we approximate $|\cos \theta^\gamma|$ by $|\tanh((\eta_1 - \eta_2)/2)|$, where $\eta_{1,2}$ are the pseudo-rapidities \[21\] of the leading and next-to-leading photons ranked by $p_T$. These four variables emphasize different phenomena in the diphoton production mechanism. $M_{\gamma\gamma}$ usually serves as a probe for new phenomena searches \[1\,2\,5–7\] and PDFs. The $p_T^{\gamma\gamma}$ and $\Delta\phi_{\gamma\gamma}$ shapes are mostly sensitive to the initial state gluon radiation and fragmentation effects. The $|\cos \theta^\gamma|$ angle is sensitive to PDFs and spin correlations in the final state. In contrast with the previous D0 measurement \[14\], in this analysis we do not impose explicit minimum requirements on $M_{\gamma\gamma}$ or $\Delta\phi_{\gamma\gamma}$, nor do we require that $M_{\gamma\gamma} > p_T^{\gamma\gamma}$, making the measurements more universal. By separating the data into two subsets, with $\Delta\phi_{\gamma\gamma} \geq \pi/2$ and $\Delta\phi_{\gamma\gamma} < \pi/2$, we isolate regions with smaller and larger expected relative contributions from the fragmentation processes.

We compare our results with the theoretical predictions generated using the DPHOX \[18\], RESBOS \[9\,22\,23\], 2$\gamma$NNLO \[24\] and SHERPA \[25\] event generators. The general multipurpose generator approach is to employ interleaved QCD and quantum electrodynamics (QED) parton shower (PS) to describe initial and final state radiation. The SHERPA Monte Carlo (MC) event generator improves this technique by including higher-order real-emission matrix elements.\[26\]. Matching between partons coming from real emissions in the ME and jets from PS is done at some (hardness) scale $Q_{\text{cut}}$ defined following the prescriptions given in Ref. \[26\]. We use events generated with all MEs with two photons and up to two hard partons. However, the ME for gluon-gluon scattering $gg \rightarrow \gamma\gamma$ in SHERPA does not have real parton emissions. As shown in Ref. \[26\] SHERPA provides a good description of the fragmentation function measured at LEP at high fraction of the jet energy carried by the photon, corresponding to tight photon isolation cuts. The loop corrections matching the higher order MEs are missing in SHERPA, which can make predictions significantly scale-dependent and may lead to underestimation of $\gamma\gamma$ rates. In the SHERPA version used in this paper \[23\], the inherent next-to-leading-logarithmic effect of correlated emissions is invoked in parton-shower simulations by appropriately choosing a scale factor for the argument of the running strong coupling constant \[27\].

The DPHOX and RESBOS packages provide predictions at next-to-leading order (NLO) in pQCD, with the $gg \rightarrow \gamma\gamma$ process considered only at the leading order approximation in DPHOX. Also, in DPHOX, explicit single and double parton-to-photon fragmentation processes are included at NLO accuracy, while in RESBOS, rates of fragmentation processes are approximated by a function. Only in RESBOS are the effects of soft and collinear initial state gluon emissions resummed to all orders. \[28\]. The resummation should be important for a correct description of the $p_T^{\gamma\gamma}$ distribution close to zero and the $\Delta\phi_{\gamma\gamma}$ distribution close to $\pi$. The 2$\gamma$NNLO generator, which appeared recently, exploits the $p_T^{\gamma\gamma}$ subtraction formalism \[30\] that handles the unphysical infra-red divergences up to next-to-next-to-leading order (NNLO). It takes into account most diagrams ($q\bar{q}$ and $gg$ scatterings) at $\mathcal{O}(\alpha_s^3)$ accuracy; however, in the current calculations, there is no higher-order correction to the $gg \rightarrow \gamma\gamma$ box diagram and no soft gluon resummation is applied. Additionally, it does not take into account the fragmentation contributions.

The D0 detector, where the DDP measurements are performed, is a general purpose detector described in detail elsewhere \[31\,32\]. The sub-detectors used in this analysis to trigger events and reconstruct photons are the calorimeter, the central tracking system, and the central preshower. The muon detection system is used to compare data and MC simulation sets of $Z \rightarrow \mu^+\mu^- + \gamma$ events to obtain data-to-MC scale factors for reconstruction efficiency. The central tracking system, used to reconstruct tracks of charged particles, consists of a silicon micro-strip detector (SMT) and a central fiber track detector (CFT), both embedded in a 2 T solenoidal magnetic field. The solenoid is surrounded by the central preshower (CPS) detector located immediately before the inner layer of the electromagnetic calorimeter. The CPS consists of approximately one radiation length of lead absorber surrounded by three layers of scintillating strips. The calorimeter is composed of three sections: a central section covering the range of pseudo-rapidities $|\eta_{\text{det}}| < 1.1$ \[21\] and two end calorimeters (EC) with coverage extending to $|\eta_{\text{det}}| \approx 4.2$, with all three housed in separate cryostats. The electromagnetic (EM) calorimeter is composed of four layers of $\Delta\eta_{\text{det}} \times \Delta\phi_{\text{det}} = 0.1 \times 0.1$ cells, with the exception of layer three (EM3) with $0.05 \times 0.05$ granularity. The calorimeter resolution for measurements of the electron/photon energy at 50 GeV is about 3.6%. The energy response of the calorimeter to photons is calibrated using electrons from Z boson decays. Since electrons and photons shower differently in matter, additional corrections as a function of $\eta$ are derived using a detailed GEANT-based \[34\] simulation of the D0 detector response. These corrections are the largest, (2.0–2.5)% at low photon energies ($\approx 20$ GeV). Events satisfying the following trigger requirements are recorded: at least two clusters of energy in the EM calorimeter with a loose
shower shape requirement and a range of $p_T$ thresholds between 15 GeV and 25 GeV. Luminosity is measured using plastic scintillator arrays placed in front of the EC cryostats.

Events are selected with at least two photon candidates with transverse momentum $p_T > 18 (17)$ GeV for the leading (next-to-leading) candidate and pseudorapidity $|\eta| < 0.9$. We require a slight difference between the $p_T$ cutoffs for the two photons to avoid a divergent kinematic region of the NLO calculations [18]. The trigger is more than 90% efficient for these selections.

At high instantaneous luminosities there is more than one $p\bar{p}$ interaction per beam crossing. The photon $p_T$ is computed with respect to the reconstructed $p\bar{p}$ interaction vertex with the highest number of associated tracks, called the event vertex [14]. The event vertex is required to be reconstructed within 60 cm of the center of the detector along the beam axis ($z$), and satisfies this requirement in 98% of events. We correct for effects of detector response to the electron and positron to model DPP production.

Photon candidates are formed from calorimeter towers in a cone of radius $R = \sqrt{\Delta \eta^2 + \Delta \phi^2} = 0.4$ around a seed tower [31]. A stable cone is found iteratively, and the final cluster energy is recalculated from the inner core within $R = 0.2$. The photon candidates are required to: (i) have $\geq 97\%$ of the cluster energy deposited in the EM calorimeter layers; (ii) be isolated in the calorimeter according to $|E_{\text{EM}}(0.4) - E_{\text{EM}}(0.2)|/E_{\text{EM}}(0.2) < 0.07$, where $E_{\text{EM}}(R)$ is the total EM energy in a cone of radius $R$; (iii) have the scalar sum of $p_T$'s of all tracks originating from the event vertex in an annulus of $0.05 < R < 0.4$ around the EM cluster less than 1.5 GeV; and (iv) have an energy-weighted EM shower width consistent with that expected for an electromagnetic shower. To suppress electron misidentification as photons, the EM clusters are required to have no spatial match to a charged particle track or any tracker hit configuration consistent with an electron. The two photon EM clusters are required to be separated by $\Delta R_{\gamma\gamma} > 0.4$.

Additional group of variables exploiting the differences between the photon-initiated and jet activity in the EM calorimeter and the tracker are combined into an artificial neural network (NN) to further reject jet background [38]. In these background events, photons are mainly produced from decays of energetic $\pi^0$ and $\eta$ mesons. The NN is trained on $\gamma$ and jet PYTHIA MC samples. The generated MC events are processed through a GEANT-based simulation of the D0 detector. Simulated events are overlaid with data events from random $p\bar{p}$ crossings to properly model the effects of multiple $p\bar{p}$ interactions and detector noise in data. Care is taken to ensure that the luminosity distribution in the overlay events is similar to the data used in the analysis. MC events are then processed through the same reconstruction procedure as the data. MC events are reweighted to take into account the trigger efficiency in data, and small observed differences in instantaneous luminosity and distribution of the $z$ coordinate of the event vertex. Photon radiation from charged leptons in Z boson decays ($Z \rightarrow \ell^+\ell^-$, $\ell = e, \mu$) is used to validate the NN performance [38]. The NN describes the data well and gives significant extra discrimination against jets. The photon candidates in this analysis are chosen such that their NN output requirement retains 98% of photons and rejects $\approx 40\%$ of jets beyond the rejection provided by the selection described above [14].

We estimate contributions from instrumental $\gamma + jet$ and dijet backgrounds and also the contribution from Z boson/Drell-Yan production events $Z/\gamma^* \rightarrow e^+e^-$ (ZDY). In the instrumental backgrounds, one or more jets are misidentified as photons from jet-forming partons that hadronize into isolated neutral meson(s) ($\pi^0$ or $\eta$) giving rise to two or more photons in the final state. Electrons in the ZDY background can be misidentified as photons due to similarities in the shower shape. The contribution from the ZDY events is estimated from MC simulation with PYTHIA, normalized to the NNLO cross section [39]. On average, 2% of the electrons survive the selection criteria above, mainly due to the inefficiency of matching a charged track to an electron. In data this inefficiency is higher than in MC and the ZDY contribution is corrected for these differences.

The $\gamma + jet$ and dijet instrumental backgrounds are estimated by fitting a two-dimensional (2D) distribution of the leading and next-to-leading photon NN outputs with templates extracted from D0 SHERPA signal and EM-jet PYTHIA MC samples. In the latter, constraints are placed at the generator level to increase the statistics of jet events fluctuating into EM-like objects [40]. For the $\gamma + jet$ template, the photon candidate is taken from either the $\gamma\gamma$ sample or from the EM-jet sample, while for the dijet template, both candidates are taken from the EM-jet sample. Table I shows the numbers of events surviving the selection in data for different $\Delta \phi_{\gamma\gamma}$ regions, as well as the number of data events from each of the four sources as determined by a fit of the signal and background templates to data. The typical DDP purity in the selected data events is around 60%.

| $N_{\gamma\gamma}$ | $N_{\gamma j}$ | $N_{j\gamma}$ | $N_{jj}$ | $N_{ZDY}$ |
|---------------------|----------------|--------------|---------|----------|
| 20255±344           | 10992±344      | 10992±344    | 198±14  | 34020    |
| 198±14              | 327±6        | 195±13      | 2851    | 31169    |
| $N_{\gamma\gamma}$ | $N_{\gamma j}$ | $N_{j\gamma}$ | $N_{jj}$ | $N_{ZDY}$ |
| $\Delta \phi_{\gamma\gamma} < \pi/2$ | $\Delta \phi_{\gamma\gamma} \geq \pi/2$ | $\Delta \phi_{\gamma\gamma} < \pi/2$ | $\Delta \phi_{\gamma\gamma} \geq \pi/2$ | $\Delta \phi_{\gamma\gamma} < \pi/2$ | $\Delta \phi_{\gamma\gamma} \geq \pi/2$ |
| $N_{\gamma\gamma}$ | $N_{\gamma j}$ | $N_{j\gamma}$ | $N_{jj}$ | $N_{ZDY}$ |
| 20255±344           | 10992±344      | 10992±344    | 198±14  | 34020    |
| 198±14              | 327±6        | 195±13      | 2851    | 31169    |
The estimated numbers of DDP events in each bin are corrected for the geometric and kinematic acceptance of the photon, as well as for the photon detection efficiency. Both acceptance and efficiency are calculated using SHERPA MC events. The acceptance is calculated for the events satisfying at the particle level $p_T^\gamma > 18$ (17) GeV for the leading (next-to-leading) photon, $|\eta^\gamma| < 0.9$, and $\Delta R_{\gamma\gamma} > 0.4$. The photon is also required to be isolated by $p_T^{iso} = p_T^{EM}(0.4) - p_T^\gamma < 2.5$ GeV, where $p_T^{EM}(0.4)$ is the scalar sum of the transverse momenta of the stable particles within a cone of radius $R = 0.4$ centered on the photon. The acceptance is driven by selection requirements in $n_{det}$ (applied to avoid edge effects in the calorimeter regions used for the measurement) and $\delta_{det}$ (to avoid periodic calorimeter module boundaries) [31], photon rapidity $\eta^\gamma$ and $p_T$, and bin-to-bin migration effects due to the finite energy and angular resolution of the EM calorimeter. Typically, greater than 80% of events at the reconstruction level remain in the same bin as at the particle level. Choice of an incorrect event vertex leads to a systematic uncertainty on the acceptance, typically $\lesssim 3\%$ for $\Delta \phi_{\gamma\gamma} \geq \pi/2$ and $\lesssim 6\%$ for $\Delta \phi_{\gamma\gamma} < \pi/2$. The systematic uncertainty is estimated by using DDP events simulated with SHERPA in which the event vertex position is randomized according to its distribution in $z$ with respect to the true vertex, and by recalculating all relevant variables of the diphoton system. Possible model-dependent effects are corrected by recalculating the acceptance according to the difference between the photon $p_T$ spectra in data and SHERPA MC. The acceptance grows from 45% in the low $M_{\gamma\gamma}$ region to 80% in the high mass region. The systematic uncertainty on the acceptance varies within $(4-21)\%$. In the regions dominated by fragmentation photons, such as low $\Delta \phi_{\gamma\gamma}$ and intermediate $p_T^\gamma$, the acceptance is lower than in the regions dominated by direct production. The EM clusters reconstructed in the acceptance region are required to pass the photon identification criteria listed above. Small differences between the photon identification efficiencies in data and MC are corrected by using control samples of electrons from $Z$ boson decays and photons from radiative $Z$ boson decays [38, 39]. The overall diphoton selection efficiency is typically about 50% with variations of $\pm 5\%$. The relative systematic uncertainty of the diphoton selection efficiency is about 4%.

The differential cross sections $\sigma/dM_{\gamma\gamma}$, $\sigma/dp_T^\gamma$, $\sigma/d\Delta \phi_{\gamma\gamma}$, and $\sigma/d|\cos \theta^\ast|$ are calculated from the number of data events after the subtraction of background contributions divided by the event selection efficiencies, acceptance, integrated luminosity, and the bin width.

The measured differential cross sections for all considered kinematic regions are presented in Table II. The average value of each variable in a bin was estimated using SHERPA MC events. The statistical uncertainty $\delta_{stat}$ is caused by finite MC statistics used for the efficiency and acceptance calculations and by the statistical uncertainty in data, taking into account statistical correlations with adjacent bins. The latter are estimated using an inverted smearing matrix, following a procedure described in Ref. [41]. The smearing matrix represents the detector resolution function and relates each bin at the particle level to the bins at the reconstruction level. It is constructed for each variable using the DDP MC events simulated with SHERPA.

Figures 1-8 show a comparison of the measured differential cross sections to the theoretical predictions from DIPHOX, RESBOS, $2\gamma$NNLO, and SHERPA. The RESBOS predictions are valid only for the phase space limited by $9 < M_{\gamma\gamma} < 350$ GeV. We take this into account in our calculations and compare RESBOS predictions to $M_{\gamma\gamma}$ measurements up to $\approx 250$ GeV (see Table II), the last mass value below 350 GeV where the cross section is measured. Systematic uncertainties across the bins in the measured cross sections are largely (> 90%) correlated. A common normalization uncertainty of 7.4% re-

### Table II: The measured differential cross sections in bins of $M_{\gamma\gamma}$ and $p_T^\gamma$.

| $p_T^\gamma$ (GeV) | $p_T^{\gamma\gamma}$ (GeV) | $\frac{\sigma}{dM_{\gamma\gamma}}$ (pb/GeV$^2$) | $\delta_{stat}$ | $\delta_{syst}$ | $\delta_{tot}$ |
|------------------|--------------------------|------------------------------------------|----------------|----------------|----------------|
| 0.0–2.5          | 1.4                      | 6.27×10$^{-4}$                          | $+9/9–10/10$   |                |                |
| 2.5–5.0          | 3.6                      | 5.38×10$^{-1}$                          | $+9/9–15/15$   |                |                |
| 5.0–7.5          | 6.2                      | 3.50×10$^{-1}$                          | $+10/9–17/17$  |                |                |
| 7.5–10           | 8.8                      | 3.47×10$^{-1}$                          | $+15/10–22/19$ |                |                |
| 10–12.5          | 11.2                     | 2.35×10$^{-1}$                          | $+12/11–17/17$ |                |                |
| 12.5–15          | 13.7                     | 1.77×10$^{-1}$                          | $+12/11–20/20$ |                |                |
| 15–20            | 17.3                     | 1.26×10$^{-1}$                          | $+12/11–16/15$ |                |                |
| 20–25            | 22.4                     | 6.99×10$^{-2}$                          | $+12/11–15/14$ |                |                |
| 25–30            | 27.4                     | 5.29×10$^{-2}$                          | $+12/10–16/15$ |                |                |
| 30–40            | 34.8                     | 6.32×10$^{-2}$                          | $+12/11–14/14$ |                |                |
| 40–50            | 44.5                     | 5.04×10$^{-2}$                          | $+13/13–16/16$ |                |                |
| 50–60            | 54.7                     | 2.53×10$^{-2}$                          | $+13/12–19/19$ |                |                |
| 60–80            | 67.9                     | 1.04×10$^{-2}$                          | $+12/11–17/17$ |                |                |
| 80–100           | 87.7                     | 3.45×10$^{-3}$                          | $+20/20–26/26$ |                |                |
| 100–120          | 108.4                    | 1.19×10$^{-3}$                          | $+20/19–28/28$ |                |                |
| 120–170          | 139.6                    | 4.75×10$^{-4}$                          | $+20/20–29/28$ |                |                |
FIG. 1: (Color online) The differential cross section as a function of (a) \( M_{\gamma\gamma} \), (b) \( p_{T,\gamma\gamma} \), (c) \( \Delta \phi_{\gamma\gamma} \), and (d) \(|\cos \theta^*|\) for the full \( \Delta \phi_{\gamma\gamma} \) region from data (black points) and theory predictions (curves) are shown in the upper plots. The lower plots show the ratio of data and DIPHOX, RESBOS, and 2\( \gamma \)NNLO predictions to the SHERPA predictions. The inner line for the error bars in data points shows the statistical uncertainty, while the outer line shows the total (statistical and systematic added in quadrature) uncertainty after subtracting the 7.4% normalization uncertainty.

Corrections from luminosity and diphoton selection efficiency is not shown in the plots. The predictions from SHERPA, DIPHOX, and RESBOS are computed using the CTEQ6.6M NNLO PDFs [12], and from 2\( \gamma \)NNLO using MSTW2008 NNLO PDFs [13]. The PDF uncertainty is estimated using DIPHOX and the 44 eigenvectors provided with the CTEQ6.6M PDF set. They are found to be within (3–7)%.

The renormalization \( \mu_R \), factorization \( \mu_F \), and fragmentation \( \mu_f \) scales are set to \( \mu_R = \mu_F = \mu_f = M_{\gamma\gamma} \). The uncertainty due to the scale choice is estimated using DIPHOX via a simultaneous variation by a factor of two of all scales relative to the default values and found to be about 10% for \( d\sigma/dM_{\gamma\gamma} \) and \( d\sigma/d|\cos \theta^*| \), and a maximum of (20–28)% for \( d\sigma/dp_{T,\gamma\gamma} \) at high \( p_{T,\gamma\gamma} \) and for \( d\sigma/d\Delta \phi_{\gamma\gamma} \) at low \( \Delta \phi_{\gamma\gamma} \). All theoretical predictions are obtained using diphoton event selection criteria equivalent to those applied in the experimental analysis (as are those used for the acceptance calculation). In particular, the photon is required to be isolated by \( p_{T,\gamma} < 2.5 \text{ GeV} \).

For DIPHOX, RESBOS, and 2\( \gamma \)NNLO, \( p_{T,\gamma\gamma}^{\text{tot}} \) is computed at the parton level. The cross sections from DIPHOX, RESBOS, and 2\( \gamma \)NNLO are corrected for effects stemming from multiple parton interactions and hadronization, while for SHERPA these effects are handled within the software package. These corrections are estimated using diphoton events simulated by PYTHIA with Tunes A and S0 [37]. The corrections vary within (4–6)% as a function of the measured kinematic variables and are consistent for both
FIG. 2: (Color online) The differential cross section as a function of (a) $M_{\gamma\gamma}$, (b) $p_T^{\gamma\gamma}$, and (c) $|\cos \theta^*|$ for the $\Delta \phi_{\gamma\gamma} < \pi/2$ region. The notations for points, lines and shaded regions are the same as in Fig. 1.

FIG. 3: (Color online) The differential cross section as a function of (a) $M_{\gamma\gamma}$, (b) $p_T^{\gamma\gamma}$, and (c) $|\cos \theta^*|$ for the $\Delta \phi_{\gamma\gamma} \geq \pi/2$ region. The notations for points, lines and shaded regions are the same as in Fig. 1.

Tables [III–V] show that the cross sections in the $\Delta \phi_{\gamma\gamma} \geq \pi/2$ region constitute, on average, about (85–90)% of the cross sections for the full $\Delta \phi_{\gamma\gamma}$ range. From the sub-tables for the $p_T^{\gamma\gamma}$ variable, we observe that at $p_T^{\gamma\gamma} \lesssim 25$ GeV, the cross sections are fully dominated by the $\Delta \phi_{\gamma\gamma} \geq \pi/2$ region, while starting from $p_T^{\gamma\gamma} \gtrsim 30$ GeV, they are significantly dominated (by a factor of 2–4) by the $\Delta \phi_{\gamma\gamma} < \pi/2$ region. The shoulder-like structure observed in the $p_T^{\gamma\gamma}$ distribution around 30–40 GeV should be mainly caused by the fragmentation photons coming from the $\Delta \phi_{\gamma\gamma} < \pi/2$ region, and partially by higher-order (NLO and beyond) corrections [19].

In general, none of the theoretical models considered here provides a consistent description of the experimental results in all kinematic regions. The SHERPA predictions are able to describe most of the phase space relatively well except for the low DDP mass region, very low $\Delta \phi_{\gamma\gamma}$, and with some tension in the $|\cos \theta^*|$ spectrum. A noticeable discrepancy between RESBOS and DIPHOX in some regions of the phase space is due to the absence of all-order soft-gluon resummation ($p_T^{\gamma\gamma}$ close to zero and $\Delta \phi_{\gamma\gamma}$ close to $\pi$) and the fact that the $gg \rightarrow \gamma\gamma$ contribution is calculated only at LO in DIPHOX (small $M_{\gamma\gamma}$). However, RESBOS fails to describe $M_{\gamma\gamma}$, $p_T^{\gamma\gamma}$, and $|\cos \theta^*|$ spectra in the $\Delta \phi_{\gamma\gamma} < \pi/2$ region, where the contributions from the fragmentation diagrams and higher-order corrections are important. The processes with a parton-to-diphoton fragmentation taking place at low masses ($M_{\gamma\gamma} < p_T^{\gamma\gamma}$) are not included yet in any existing calculation [9]. The regions of phase space with a significant contribution from fragmentation photons (very low $\Delta \phi_{\gamma\gamma}$) require ex-
tensive tuning of all of the considered event generators.

In summary, we have presented measurements of differential cross sections of photon pair production in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV as functions of $M_{\gamma\gamma}$, $p_T^{\gamma}$, $\Delta \phi_{\gamma\gamma}$, and $|\cos \theta^*|$ for photons with $p_T > 18(17)$ GeV and $|\eta| < 0.9$ in the full $\Delta \phi_{\gamma\gamma}$ range and for $\Delta \phi_{\gamma\gamma} < \pi/2$, $\Delta \phi_{\gamma\gamma} \geq \pi/2$ separately. The cross sections are compared to the predictions made by the DPHOX, RESBOS, 2YNNLO, and SHERPA MC generators. Overall, SHERPA provides the best description of the measured cross sections. The experimental results show discrepancies with all theoretical predictions in the regions of small $\Delta \phi_{\gamma\gamma}$ and small diphoton mass for $\Delta \phi_{\gamma\gamma} \geq \pi/2$, with minor differences in the shapes of the $|\cos \theta^*|$ distribution. The results are important for understanding of DDP production and tuning of modern generators to study SM phenomena and search for beyond the SM processes.

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![Table III](image)

![Table IV](image)

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TABLE V: The measured differential cross sections in bins of $M_{\gamma\gamma}$, $p_T^\gamma$, and $|\cos \theta^\gamma|$ for $\Delta \phi_{\gamma\gamma} \geq \pi/2$. The columns $\delta_{\text{stat}}$, $\delta_{\text{syst}}$ and $\delta_{\text{tot}}$ represent the statistical, systematic and total uncertainties, respectively.

| $M_{\gamma\gamma}$ (GeV) | $|\cos \theta^\gamma|$ | $d\sigma/d|M_{\gamma\gamma}|$ (pb/GeV$^{-1}$) | $d\sigma/dp_T^\gamma$ (pb/GeV$^{-1}$) | $d\sigma/d|\cos \theta^\gamma|$ (pb) | $\delta_{\text{stat}}$ (%) | $\delta_{\text{syst}}$ (%) | $\delta_{\text{tot}}$ (%) |
|---------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 30-40               | 0.0-0.1          | 2.24 x 10^{-4}  | 1.3 x 10^{-4}   | 6               | +8/8            | +10/10          | +14/10          |
| 30-40               | 0.1-0.2          | 1.86 x 10^{-4}  | 2.0 x 10^{-4}   | 6               | +8/8            | +9/9            | +9/9            |
| 30-40               | 0.2-0.3          | 1.56 x 10^{-4}  | 7               | +9/9            | +11/11          | +16/16          | +21/21          |
| 30-40               | 0.3-0.4          | 1.54 x 10^{-4}  | 6               | +9/9            | +10/10          | +14/14          | +19/19          |
| 30-40               | 0.4-0.5          | 8.0 x 10^{-5}   | 8               | +9/9            | +12/12          | +17/17          | +22/22          |
| 30-40               | 0.5-0.6          | 4.4 x 10^{-5}   | 10              | +11/10          | +15/15          | +20/20          | +25/25          |
| 30-40               | 0.6-0.7          | 0.14            | 17              | +22/22          | +28/28          | +34/34          | +40/40          |

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