Proton decay from the isoscalar giant dipole resonance in $^{58}$Ni

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Abstract

Proton decay from the $3\hbar\omega$ isoscalar giant dipole resonance (ISGDR) in $^{58}$Ni has been measured using the $(\alpha,\alpha'p)$ reaction at a bombarding energy of 386 MeV to investigate its decay properties. We have extracted the ISGDR strength under the coincidence condition between inelastically scattered $\alpha$ particles at forward angles and decay protons emitted at backward angles. Branching ratios for proton decay to low-lying states of $^{57}$Co have been determined, and the results compared to predictions of recent continuum-RPA calculations. The final-state spectra of protons decaying to the low-lying states in $^{57}$Co were analyzed for a more detailed understanding of the structure of the ISGDR. It is found that there are differences in the structure of the ISGDR as a function of excitation energy.

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I. INTRODUCTION

Experimental studies of direct decay modes of giant resonances can shed light on their microscopic structure and its evolution to a collective behavior. Since most of the giant resonances are located above the particle separation thresholds, particle emission is the dominant decay mode that can take place at different stages of the damping process \[1\]. Particle decay can occur either from the initial \(1p-1h\) state leaving a single-hole state in the \(A - 1\) nucleus, or from the states with partially or completely equilibrated configurations, resulting in an evaporation-like spectrum. Therefore, the branching ratios of particle emission from giant resonances provide us a good means to understand the wave function of the giant resonance.

The main interest in studying isoscalar giant resonances is to investigate the nuclear incompressibility via the determination of the resonance energies of the isoscalar giant monopole resonance (ISGMR) and the isoscalar giant dipole resonance (ISGDR) \[2, 3, 4, 5\].

The incompressibility has a crucial role in the application of the nuclear equation-of-state in model calculations of various astrophysical processes or in descriptions of heavy-ion reactions. These experiments had focused primarily on the ISGMR as the strongest compression resonance ever discovered \[6, 7\], while the ISGDR could be studied in detail only after the first unambiguous evidence for its existence in 1997 \[8\]. Difficulties were mainly caused by the relatively weak excitation of the \(3\hbar\omega\) ISGDR, which, in addition, was distributed with a relatively large width on top of a strong nuclear-continuum and instrumental background. An overlap in excitation energy with the \(3\hbar\omega\) high-energy octupole resonance (HEOR) had to be separated from the ISGDR strength as well.

The problem of separating the background due to the nuclear continuum from the resonance strengths still remained due to the unknown multipole composition. To identify the multipole components, we employ the multipole-decomposition analysis (MDA) to fit the angular distribution of the obtained cross sections, or the difference-of-spectra (DOS) technique, in which pronounced changes and large differences in the shapes of the angular distributions for low multipoles are exploited in measurements at very forward angles, possibly including \(0^\circ\) as well \[8, 9\]. The elimination of the background components was the major difficulty in many of the singles experiments. There remained some ambiguities regarding an appropriate choice of the background-subtraction resulting in a large uncertainty in the shape and the strength of giant resonances. Moreover, measurements at scattering...
angles close to $0^\circ$ often suffered from a substantial contribution of instrumental background in addition to the non-resonant continuum, which is due to quasi-free scattering and pick-up/break-up reactions. The coincidence technique with particle decay gives a useful means to suppress such backgrounds and to isolate resonances strengths. The ISGDR strength can be identified using the DOS analysis provided data are measured in appropriately chosen angular regions where dipole strength dominates over those of other multipolarities (see Fig. 1).

In previous experiments, coincidence measurements with decay particles from high-energy resonances and the subsequent DOS analysis were found to be effective for eliminating both the instrumental background and the non-resonant continuum [10, 11, 12]. The resulting resonance strength and its partial decay branches to single-hole states give detailed information on the microscopic structures of these resonances.

Experiments on the ISGDR in $^{58}$Ni, with a closed shell of 28 protons, performed so far were exclusively singles measurements in which $L=1$ strength distributions were analyzed with MDA techniques over a wide excitation energy range [13, 14, 15]. A fraction of the $L=1$ strength was systematically observed at $E_x \sim 16$ MeV (low-energy part), but the main part of the ISGDR at $E_x \sim 31$ MeV was only found in the latest experiments [13, 15]. Coincidence experiments for the ISGDR have been performed so far only for $^{90}$Zr, $^{116}$Sn and $^{208}$Pb, where gross resonance parameters (energies, widths) and partial branching ratios were determined [10, 11, 12, 16]. We have extended the coincidence studies towards lighter nuclei and investigated the microscopic structures based on the observation of an increasing fragmentation of resonance strengths and decay properties.

Here, we report the first results of a coincidence experiment, in which we aimed at studying the $L=1$ strength distribution in the $3\hbar\omega$ region of $^{58}$Ni, by applying the analysis with the DOS technique, and at deducing its direct proton-decay properties to low-lying proton-hole states of $^{57}$Co.

II. EXPERIMENT

The experiment was carried out at the Ring cyclotron facility of the Research Center for Nuclear Physics (RCNP) in Osaka University, using the $^{58}$Ni(α, α′p) reaction at a beam energy of 386 MeV. We used a $^{58}$Ni target with a thickness of 4 mg/cm². Inelastically scat-
tered α-particles were momentum-analyzed at very forward angles with the high-resolution magnetic spectrometer, Grand Raiden \[17\]. The focal-plane detector system of the spectrometer consisted of two multi-wire drift chambers (MWDC) and two plastic scintillators. The spectrometer enables the detection of ejectiles with a momentum acceptance of $\delta p/p=5\%$ corresponding to an effective excitation-energy range of 15-50 MeV. The spectrometer was set at the scattering angle of $\Theta_{\text{lab}}=2.5^\circ$, with an opening angle of 40 mr both horizontally and vertically defined by the geometry of the entrance slit, which corresponds to an effective angular acceptance of 1.8°-3.8°.

Decay protons were analyzed with a detector array consisting of 13 Si(Li) detectors with a thickness of 5 mm each. These were mounted in the backward hemisphere in the scattering chamber at a radial distance of 12 cm from the target. A total solid angle of 1.6 msr in the range of 100°-220° in the laboratory frame was covered. The resolutions in the $^{58}\text{Ni}(\alpha, \alpha')$ spectrum and in the $^{57}\text{Co}$ final-state spectrum were 200 keV and 400 keV full width at half maximum (FWHM), respectively.

III. DISCUSSION

Energy spectra and angular distributions of inelastically scattered α particles were measured both in singles and in coincidence with protons emitted from the highly excited states in $^{58}\text{Ni}$. Spectra of final-state energy, defined as the excitation energy of the $^{57}\text{Co}$ daughter nucleus, were derived from the excitation energies in $^{58}\text{Ni}$ and proton decay energies.

Singles $(\alpha, \alpha')$ spectra were analyzed to obtain differential cross sections for the ISGDR strength to determine the fraction of the energy-weighted sum rule (EWSR) exhausted. The $(\alpha, \alpha')$ spectra obtained with the opening angle of 40 mr both horizontally and vertically, corresponding to scattering angles $\Theta_{\text{c.m.}} = 1.8^\circ - 3.8^\circ$, were subdivided into two regions of $\Theta_{\text{c.m.}} = 1.8^\circ - 2.5^\circ$ and $3.1^\circ - 3.8^\circ$ by using the ray-tracing technique. These two spectra are given in Fig. 2, both of which show a resonance of the ISGDR in the $3\hbar\omega$ region on top of a nuclear-continuum background. In these spectra the contribution from the instrumental background, which was mainly due to scattering events of the incident beam on the slits defining the opening angle and on various parts of the spectrometer, was eliminated by subtraction. This was possible because it has been observed that these background events at the focal plane had a flat distribution in the vertical position spectrum, while true events were
focused at the focal plane both horizontally and vertically, which allowed their separation from the instrumental background [18].

A remarkable difference between the spectra in Fig. 2 is due to the presence of the $L=1$ excitation strength as expected (see Fig. 1). We also observed that the nuclear-continuum background changed in shape and amplitude. Since the nuclear continuum comprises, in general, a mixture of many multipoles, such changes in the background could be treated by making reasonable assumptions on its shape. To define a background under the resonance, its shape can typically be approximated by simple functions such as polynomials that interpolate the nuclear continuum between the continuum above the $3\hbar\omega$ region, where significant contributions of $4\hbar\omega$ resonances are not expected ($E_x > 40$ MeV), and an intermediate region between the ISGDR and ISGMR (around 23 MeV), where the contributions from the high-energy tail of the latter are assumed to be negligibly small. Various background functions and fitting conditions were tested to give a reliable estimate for the systematic errors of integrated ISGDR cross sections with the $L=1$ strengths at $E_x=23-40$ MeV. As a result, we obtained the cross section values of $24.1\pm1.1$ mb/sr at $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ and $7.1\pm1.0$ mb/sr for $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$. Since the non-resonant continuum background underlying the ISGDR was assumed to be completely removed using different hypothetical functions, only the singles spectrum resulting from the difference-of-spectra (DOS) was plotted for comparison with the spectra obtained with the gate on decay proton events in order to deduce the branching ratios.

The decrease of the DOS below $E_x=20$ MeV is understood as a negative contribution of the ISGMR and ISGQR, as indicated from the angular distributions shown in Fig. 1. A more detailed analysis of singles data was accomplished by multipole decomposition of the resonance structures in the $3\hbar\omega$ region after subtraction of the nuclear-continuum background. Angular distributions were determined by integrating double-differential cross sections at $E_x=23-40$ MeV after subtracting the background functions shown in Fig. 2. The cross sections of the $3\hbar\omega$ resonance structure are compared with the results from the distorted wave Born approximation (DWBA) calculations, and are fitted by using $L=1$ and $L=3$ components. The result is shown in Fig. 3. It is found that the resonance bump at $E_x=23-40$ MeV consists of mainly the $L=1$ ISGDR component and a small contribution of the $3\hbar\omega$ HEOR, at least, at the scattering angles of $\Theta_{c.m.}=1.8^\circ - 3.8^\circ$. Any contributions from the $L=0$ and $L=2$ resonances are not evidenced in the fit.
The analysis of coincidence data started with the identification of prompt and random coincidence events in the timing spectra. Since the timing resolution of 1.9 ns was small enough relative to the repetition period of 19.7 ns for beam bursts, prompt events were well isolated and could be corrected for random coincidences. The real-to-random ratio was found to be \( \approx 10 \) after excluding \( \gamma \)-ray events detected by the Si(Li) detectors. Moreover, since non-resonant quasi-free scattering of protons is strongly forward peaked, its contribution to decay spectra at backward angles, where all proton detectors were placed, was negligibly small.

Angular correlations of decay protons and the \( \alpha \)-particle ejectiles were also extracted and fitted with Legendre polynomials to calculate the yields of proton emission, which were necessary to determine the absolute values of cross sections and branching ratios for proton decay.

Final-state spectra as a function of excitation energy of the daughter nucleus \( ^{57}\text{Co} \) were extracted for the scattering angles \( 1.8^\circ < \Theta_{\text{c.m.}} < 2.5^\circ \) and \( 3.1^\circ < \Theta_{\text{c.m.}} < 3.8^\circ \), and for the excitation-energy range 21-40 MeV where the ISGDR was observed in the singles \( ^{58}\text{Ni}(\alpha, \alpha') \) spectra. The final-state spectra and the spectrum resulting from their subtraction are shown in Fig. 4. The prominent peak due to proton decay from the ISGDR to the \( f_{7/2} \) proton-hole ground state of \( ^{57}\text{Co} \) is clearly observed and is well separated from the other low-lying states. It is evident that the ISGDR decays to the \( f_{7/2} \) proton-hole state in \( ^{57}\text{Co} \) by emitting protons due to the 1p-1h configuration in its wave function. Most of the excited states up to \( E_x = 3 \) MeV in \( ^{57}\text{Co} \) are identified in the final-state spectrum. Due to the energy resolution of 400 keV in the final-state spectrum and due to the increasing level density as a function of excitation energy, the low-lying states at \( E_x \geq 1 \) MeV could not be well resolved. It is worth noting that we observed a weak yield of the ground-state decay from the \( ^{16}\text{O} \) to \( ^{15}\text{N} \) due to oxygen contamination in the target material. However, we conclude that there is no other background contribution at \( E_x < 4.5 \) MeV.

Event yields in both spectra in Fig. 4a show a monotonous increase at \( E_x > 4 \) MeV, which is attributed to the statistical component of decay protons from both the ISGDR and non-resonant continuum to the states in \( ^{57}\text{Co} \) with multi-particle-multi-hole configurations. Statistical decay calculations using the code CASCADE were performed and it was found that the final-state spectra at \( E_x > 4 \) MeV are well described by the statistical-model calculations. On the other hand, the calculation of proton decay for the low-lying final
states becomes strongly model-dependent; still, it is concluded from the statistical decay calculations that proton decay to the ground state in $^{57}$Co proceeds dominantly through the direct process.

The ground state of $^{57}$Co has a simple wave function with a single $f_{7/2}$ proton-hole configuration. This state is readily fed from the resonance with a particle-hole configuration in the proton orbitals. Since knock-out and pick-up/break-up and break-up/pick-up processes lead to very forward emission of protons, measuring proton decay at backward angles ($>90^\circ$) eliminates the contribution of these processes. The remaining underlying non-resonant continuum background due to multistep processes will display a dominant statistical decay with no direct decay component, and a flat angular distribution is expected for this continuum at very forward angles. By gating on decay to the $f_{7/2}$ proton-hole ground state, which does not comprise statistical decay components according to the CASCADE calculations discussed above, resonant structures are selected in the $3\hbar\omega$ region, including the ISGDR, and non-resonant contributions are suppressed from the excitation-energy spectra obtained by the DOS technique. Figure 5a shows the excitation energy spectra in $^{58}$Ni gated on the proton decay to the ground state in $^{57}$Co for the angles $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ and $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$. A significant difference is observed for the spectrum taken at $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ compared to the spectrum taken at $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$. As seen in Fig. 5b, a prominent structure appears after their subtraction in an excitation-energy range of $E_x=20-40$ MeV, where a major fraction of the ISGDR strength exists. In the excitation energy region at the high-energy side of the ISGDR, the background of the nuclear continuum is evidently suppressed, which justifies the validity of the analysis combined with both the DOS technique and the coincidence technique for the observation of the direct particle decay channels.

The spectrum obtained with the DOS technique with a gate on proton decay to the ground state in $^{57}$Co, shown in Fig. 5b, was converted to a strength distribution based on DWBA calculations, and was expressed in terms of the fraction of the EWSR ($dH/dE_x$). The resulting strength distribution is shown in Fig. 6a. Similarly, the singles cross section for the ISGDR obtained by the DOS method (labeled as DOS in Fig. 2) was converted to a strength distribution and expressed as fraction of EWSR rule. This is shown in Fig. 6b. The resonance bump of the ISGDR shown in Fig. 6b now seems to consist of, at least, two components. Firstly, the resonance shape was tested by fitting with a simple Gaussian function covering the whole resonance region. This procedure was not successful in getting
a good fit. Secondly, we tried to fit the resonance using two Gaussian functions for the low- and high-energy parts. This leads to a reduced $\chi^2$ value of 0.94. The resonance parameters for the fit are listed in Table I.

The centroid energy and moments were also derived for the partial strength distribution obtained for the direct proton decay channel to the ground state of $^{57}$Co (see Table I). However, the determination of the strength distributions for all possible decay channels would be essential to obtain the centroid energy and moments of the ISGDR and, consequently, the bulk resonance properties, as well as the incompressibility from centroid energies. Contributions from the direct alpha-decay channels—the alpha-separation threshold is very low ($S_\alpha = 6.400$ MeV)—were, nevertheless, found to be negligible in the excitation energy region of the ISGDR and did not yield significant information on its partial strength distribution. Considerable yields from direct neutron decay comparable to those from proton decay are still expected, since the neutron decay threshold is only around 4 MeV higher than the proton threshold ($S_n = 12.217$ MeV, $S_p = 8.172$ MeV). Therefore, it would be very interesting to extend these studies to measuring neutron decay of the ISGDR.

In medium-heavy nuclei, a fragmented resonance structure reminiscent of the underlying 1p-1h structure is predicted by RPA calculations (see Ref. [19]). This kind of fragmentation could be observed in the coincidence measurements with decay protons, if we can obtain the final-state spectra with considerable statistics and with a resolution good enough to resolve the low-lying final states in $^{57}$Co. It should be noted that in the present experiment, these requirements were not met to obtain the strength distributions of decay protons to the excited final states in $^{57}$Co. Therefore, it becomes difficult to obtain further information on the ISGDR structure from further analyses of the final-state spectrum. In spite of these limitations, it is quite apparent that the ISGDR consists of, at least, two components, with the low- and high-energy parts located at $E_x = 21-27$ MeV and $E_x = 27-38$ MeV, respectively.

Figure 7 shows the difference final-state spectra generated by subtracting the final-state spectra taken at $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ and at $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$ and gated on proton decay from the two ISGDR components in $^{58}$Ni. Therefore, these final-state spectra correspond to proton decay from these two ISGDR components. Some peaks corresponding to the ground state and the low-lying states of $^{57}$Co were fitted with Gaussians. Many other peaks had to be left out in the fitting procedure because of poor statistics and the relatively high level densities that did not allow to resolve individual low-lying states due to a resolution of
400 keV in the final-state spectrum. However, significant differences are found between the spectra in Figs. 7a and 7b. This can be understood by taking into account the fact that the low-lying states in $^{57}$Co have relatively complex wave functions, since $^{58}$Ni has 28 protons and is in the middle of the $fp$-shell, and their structure can be described mostly as one-hole coupled to phonon excitations with further coupling to $n$-particle-$(n+1)$-hole configurations. A reliable interpretation of their population rates would thus require a further improvement in both the experimental data (statistics and resolution) and RPA calculations. If such high-statistics and high-resolution coincidence ($\alpha, \alpha' p$) experiment were successfully performed, one would obtain rich information on the internal structure and evolution of the particle-hole configuration of the ISGDR in order to understand correctly the damping process of the resonance. To demonstrate the differences in proton decay from the two regions of the ISGDR structure to the low-lying states in $^{57}$Co, their relative strength was deduced for each 1 MeV bin of the final-state energy. This quantity can be considered an asymmetry parameter of the ISGDR strength distribution, and used for testing the theoretical models. The results are listed in Table III.

Experimental branching ratios of proton decay to the ground state (g.s.) and to all states below $E_{f,s.}=4$ MeV (including the g.s.) were deduced to be 6.2$\pm$1.4% and 12.9$\pm$2.3%, respectively. These were determined from the total ISGDR strengths in the coincidence and singles difference spectra in the excitation-energy region of $E_x=23$-38 MeV shown in Figs. 6a and b. These values are quite considerable even in comparison with continuum-RPA calculations, which predicted 16.4% for the single-hole $f_{7/2}$ level taking a unit spectroscopic factor [20].

In conclusion, we have reported on coincidence measurements to investigate the proton decay from the ISGDR using the $^{58}$Ni($\alpha, \alpha' p$) reaction at $E_\alpha=386$ MeV. The ISGDR has been observed at $E_x=20$-40 MeV and has been identified by employing difference-of-spectra (DOS) analysis based on the singles and coincidence measurements. The strength distributions of the ISGDR in terms of fractions of the EWSR have been deduced and fitted to determine the gross structure of the ISGDR from both singles and proton-decay data. The gross structure of the ISGDR determined from coincidence measurements shows two components. Significant differences were found in proton decay from these two components of the ISGDR to the low-lying states in $^{57}$Co at excitation energies below 4 MeV. This experimental result indicates that there exist some structural differences in the particle-hole configurations and
damping process of the ISGDR in $^{58}\text{Ni}$ as a function of excitation energy. Partial branching ratios for proton decay to the ground state and the low-lying final states up to 4 MeV in $^{57}\text{Co}$ have been determined. A deeper understanding of the branching ratios and decay patterns of proton decay from the ISGDR would require further development of theoretical models.

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TABLE I: Resonance parameters and fractions of the energy-weighted sum rule (EWSR) determined for the ISGDR based on Gaussian fits and the moments of strength distributions shown in Figs. 6a and b. Moments $m_1$ and $m_0$ were derived for the excitation-energy region of 23-38 MeV. Theoretical values are taken from continuum-RPA calculations. The symbols $\omega$, $\Gamma$ and $H$ denote the centroid energy of the ISGDR, the width and fraction of EWSR in %, respectively, and $m_0$ and $m_1$ are moments of the strength distribution defined by $m_k = \int E^k S ds$ [20].

|                     | singles data | singles data | singles data | coincidence data<sup>a</sup> | theory |
|---------------------|--------------|--------------|--------------|-----------------------------|--------|
|                     | this work    | Ref. [14]    | Ref. [15]    | this work                  | Ref. [20] |

**Gaussian fit**

|                     |               |              |              |                            |        |
|---------------------|---------------|--------------|--------------|---------------------------|--------|
| $\omega$ (MeV)      | 32.9±0.4      | 34.06±0.30   |              | 29.6±1.1                  |        |
| $\Gamma$ (MeV)      | 11.9±1.0      | 19.52±0.41   | 10.8±1.9     |                           |        |
| $H$ (%)             | 63±5          |              |              | 3.4±0.6                   |        |

**Double-Gaussian fit**

|                     |               |              |              |                            |        |
|---------------------|---------------|--------------|--------------|---------------------------|--------|
| $\omega$ (MeV)      |               |              |              | 24.0±1.9, 31.1±1.4        |        |
| $\Gamma$ (MeV)      |               |              |              | 4.3±2.6, 7.8±2.7          |        |
| $H$ (%)             |               |              |              | 0.90±0.17, 2.5±0.4        |        |

**Moments**

| $m_1/m_0$ (MeV)     | 29.5±2.0      | 27.78±0.47   | 30.8±1.7     | 27.9±7.5                  | 27.4   |
| $m_1$ (%)           | 54±8          | 68±20        | 98±4         | 3.4±0.4                   | 75     |

<sup>a</sup>data gated on direct decay to the g.s. of $^{57}$Co.
TABLE II: Ratio of the high-energy part \((E_x=27-38\text{ MeV})\) of the ISGDR to the total \((E_x=21-38\text{ MeV})\), derived as a function of final-state energy in \(^{57}\text{Co}\). The final-state energy has a 1 MeV bin size.

| \(<E_{f.s.}\rangle\) (MeV) | \(H_{HE}/(H_{LE} + H_{HE})\) (%) | \(H_{LE} + H_{HE}\) (%) of EWSR |
|-----------------|-----------------|-----------------|
| 0               | 74±15            | 3.40±0.41       |
| 1               | n/a              | n/a             |
| 2               | 45±25            | 1.15±0.29       |
| 3               | 81±22            | 1.96±0.35       |
| 4               | 63±16            | 2.14±0.32       |
| 5               | 34±18            | 1.67±0.34       |
| 6               | 43±17            | 2.12±0.39       |
| 7               | 30±18            | 1.95±0.42       |

FIG. 1: Differential cross sections of the \(^{58}\text{Ni}(\alpha,\alpha')\) reaction at \(E_\alpha=386\text{ MeV}\) for exciting isoscalar giant resonances in \(^{58}\text{Ni}\). The distorted-wave Born approximation (DWBA) calculations have been obtained by assuming 100% exhaustion of the energy-weighted sum rules (EWSR). The resonance energies have been assumed to be at \(E_x=19, 29, 15\) and \(26\) MeV for the \(L=0, 1, 2\) and 3 resonances, respectively. The regions used for the difference-of-spectra (DOS) analysis are indicated.
FIG. 2: Inelastic α-scattering spectra at $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ and $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$. The resonance structures were separated from the background with functions fitted in the continuum regions at $E_x$=23-40 MeV (see text for more details); the subtracted backgrounds are shown by the solid lines. The difference of the two spectra (DOS) after subtracting the assumed backgrounds is also shown.
FIG. 3: Angular distribution of the cross sections for the resonance structure observed in the $3\hbar\omega$ region. The cross sections for the resonance at $E_x=23-40$ MeV were fitted with the DWBA calculations for $L=1$ and $L=3$. The $L=1$ and $L=3$ cross sections used in the fit are plotted.
FIG. 4: Double-differential cross sections as function of the final-state energy in $^{57}$Co projected for the $3\hbar\omega$ region in $^{58}$Ni. a) Final-state spectra extracted for the scattering angles $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ and $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$. b) DOS showing the feeding pattern to the low-lying states in $^{57}$Co by emitting protons from the ISGDR. Individual final states are partly identified and fitted. Some yield corresponding to the $^{16}$O($\alpha, \alpha'p)^{15}$N.g.s. reaction is also observed due to oxygen contamination in the target.
FIG. 5: a) Double-differential cross sections at $1.8^\circ < \Theta_{c.m.} < 2.5^\circ$ and $3.1^\circ < \Theta_{c.m.} < 3.8^\circ$ plotted as a function of excitation energy in $^{58}\text{Ni}$. The data points have been obtained with a gate on the proton decay to the ground state in $^{57}\text{Co}$. b) DOS representing the $L=1$ strength populating the ground state in $^{57}\text{Co}$. 
FIG. 6: Strength distributions expressed in differential exhaustion factors defined as fractions of the EWSR of ISGDR. The spectra represent the $L=1$ strengths identified with DOS analysis of a) coincidence data gated with proton-decay to the ground state in $^{57}\text{Co}$ (Fig. 5) and b) singles data (Fig. 2). Fit functions and parameters are also indicated.
FIG. 7: Difference final-state spectra plotted as function of the excitation energy in $^{57}$Co. Coincidence conditions are set for a) low- and b) high-energy components of the ISGDR strength in $^{58}$Ni. Fits of individual final states are plotted.