Geospatial Modeling of Radon-Prone Areas

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Methods for identification of potentially radon-prone areas using geospatial analysis in ArcGIS 10.6 software environment and mathematical modeling in SPSS 19.0 on the example of high background radiation area have been developed. High level of natural radioactivity associated with uranium content in environment objects and natural uranium occurrences, and also the spatial density of faults (reliable and unreliable) and lineaments were taken into account as well as the distance from uranium mine located nearby.

The method of linear discriminant functions was used to make a math model for determining the level of radon hazard. To do this, data on all locations were divided into training and test samples. Determination of predictors of the mathematical model was performed using Fisher’s criterion by their sequential inclusion in discriminant equations. Among the considered 13 factors of radon hazard, seven of them turned out to be informative. For them, canonical coefficients were calculated using the least squares method for first- and second-order polynomials. Based on the values of discriminant functions, a territorial map was constructed to assign the new location to a certain level of radon hazard.

The maps obtained present the correlation of the radon-prone areas with the zones of high spatial density of faults and lineaments, and confirmed by the data of direct indoor radon measurements. In a limited number of measurements, the methods might get a good help in prioritization for round-the-country radon survey. As far as the model for identification of potentially radon-prone areas is mainly based on geological studies, the further research is supposed to be directed to its approbation for a different geological environment of the Ukrainian shield.

Keywords: radon-prone area, geospatial analysis, faults spatial density, spatial density of the 3-4 order lineaments, method of discriminant functions.

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concentrations must be expected for natural reasons and surveys indicate that the percentage of households expected to exceed national reference levels is significantly higher than in other parts of the country. The European Atlas of Natural Radiation (EANR), a collection of maps displaying the levels of natural radioactivity from different sources [2], has not included any data on radon potential for Ukraine yet. At present, there is no national radon action plan. The strategy for public protection against the effects of radon exposure is under development, the methodology for identifying potentially hazardous areas at national level has not been developed yet and therefore these issues remain extremely relevant.

Analysis of previous studies

The issue of geogenic radon potential is widely covered in many European, especially Joint Research Center, publications [2] – [4]. Methodology for radon measurements and research of radon as a source of a significant human health risk is developed, in particular, by specialists from the State Institution «O.M. Marzieiev Institute for Public Health» of the National Academy of Medical Sciences of Ukraine and other experts [5] – [7]. Factors, which lead to formation of radon hazardous areas, are identified by ways of radon entry into the outdoor and indoor atmosphere and described in a wide range of publications, in particular in [8] – [12]. They all come down to the following natural reasons, which are supposed to get emphasized in the present research. The concentration of Rn-222 in the indoor air depends on the content of U-238 and/or Ra-226 in natural environment – rocks, weathering crust of parent material, soils and groundwater, on Rn-222 emanation coefficient from the soil, on the soil properties and condition, on concentration of uranium anomalies in the earth crust, and, consequently, on the concentration of uranium and radium in structural materials. Regarding the outdoor radon, its concentrations can be neglected.

Structural and tectonic geological factors play a significant role: deep-seated faults, fractured zones, zones of milonitization, brecciation, etc. Tectonic zones are considered as radon reservoirs where radon emanation coefficient is increased. When buildings are located above such zones, the likelihood of high concentrations of radon accumulating in them is abruptly increased. Apart from geological factors, buildings’ materials and structures, ventilation, and behavior cultures are also considered [13] – [15]. However, our research is concentrated on the Central Ukrainian Uranium Province of the Ukrainian Shield and uranium mining area, and so we further focus mainly on geological factors.

Setting of research objectives

In [16], the territory of uranium mining and milling facilities legacy sites was outlined and classified (nine legacy sites altogether). The uranium mining has been developed here since the time after the Second World War. The sites of uranium mining (depleted through underground mining and in situ leaching and operating mines) were considered from their radiation hazard and remediation needs [17] – [18].

The presented research objective is to develop a methodology for the radon-prone area identification based on geospatial analysis and mathematical modeling.

Research materials and methods

The input data flow chart for geospatial modeling is presented in Figure 1. The data are borrowed from long-term geological research (1992-2003) archive materials [19] – [20], [26] - geological map of uranium and thorium mineralization of the Ukrainian Shield Precambrian formations of 1: 500 000, geological map of uranium and thorium mineralization of the Ukrainian Shield Ingulskyi megablock of 1:200 000, and also from uranium deposits and ore manifestations database [21] within the central part of the Ukrainian Shield. The map of Pre-Cenozoic deposits, neotectonic map, the soil map for the Kirovohrad district, as well as the relief surface data (SRTM, ALOS), and data on uranium content in different environment objects [20], [22]. Gamma activity of sedimentary rocks cover (µSv/h) [20] and dose rate at 1 m height (µSv/h) [10] were used as supplementary data. Altogether, 13 factors were taken into account (Table 1), and the score was appointed for each of factors so that they could be combined to obtain a comprehensive solution.

Therefore, first, a map of faults spatial density was made over a grid of 5 km x 5 km and analyzed in terms of association of high faults spatial density areas (dark brown colors) and ring structures for the territory outlined (Figure 2). Then, a research territory of the Kirovohrad uranium ore region was allocated for more thorough analysis at local level (40 km x 25 km). The research territory background data on the Michurinske ore field along with the Michurinske uranium deposit located at the intersection of the sub-longitudinal Kirovohrad tectonic zone and the Oleksandrivsko-Pervovzanskiy sub-latitudinal fault, as well as the vicinity of the Kropyvnytskyi city on the one hand, and the oldest Inguliska uranium mine on its south-eastern suburbs on the other hand, justified the choice of this area for research at local level.
Table 1 – Radon hazard levels

| №  | Natural Uranium Deposits, ore Manifestations, Mineralization Points | Uranium Content | Geological Data | Location |
|----|---------------------------------------------------------------|----------------|-----------------|----------|
|    |                                                               | U in Rocks, % | Reliable Faults | Lineaments 3,4 | Distance from SPZ |
|    |                                                               | U in Soils, % | Unreliable Faults |            |          |
| 1  | X1                                                             | 10^-4         |                   |           |          |
| 2  | X2                                                             | 10^-4         |                   |           |          |
| 3  | X3                                                             | 10^-4         |                   |           |          |
| 4  | X4                                                             | 10^-4         |                   |           |          |
| 5  | X5                                                             | 10^-4         |                   |           |          |
| 6  | X6                                                             | 10^-4         |                   |           |          |
| 7  | X7                                                             | 10^-4         |                   |           |          |

Table 1 – Input data flowchart for geospatial modeling
### Fragment of filled in Table 1

| №№ | structural and geological | sedimentary cover | settlements |
|-----|---------------------------|-------------------|-------------|
|     | faults (reliable)         | thickness of sedimentary cover | distance from SPZ, m | dose rate at a height of 1 m, μSv/h |
|     | faults (unreliable)       | gamma dose rate of sedimentary cover μSv/h |                      |                                          |
|     | lineaments                |                                  |                      |                                          |
|     | local 3-4                 | J                               | L                   | M                                         |
|     | detail 6-7-8              | J                               | J                   | M                                         |
|     | thickness of sedimentary cover | J                               | J                   | M                                         |

| №№ | structural and geological | sedimentary cover | settlements |
|-----|---------------------------|-------------------|-------------|
|     | faults (reliable)         | thickness of sedimentary cover | distance from SPZ, m | dose rate at a height of 1 m, μSv/h |
|     | faults (unreliable)       | gamma dose rate of sedimentary cover μSv/h |                      |                                          |
|     | lineaments                |                                  |                      |                                          |
|     | local 3-4                 | J                               | L                   | M                                         |
|     | detail 6-7-8              | J                               | J                   | M                                         |
|     | thickness of sedimentary cover | J                               | J                   | M                                         |

| №№ | structural and geological | sedimentary cover | settlements |
|-----|---------------------------|-------------------|-------------|
|     | faults (reliable)         | thickness of sedimentary cover | distance from SPZ, m | dose rate at a height of 1 m, μSv/h |
|     | faults (unreliable)       | gamma dose rate of sedimentary cover μSv/h |                      |                                          |
|     | lineaments                |                                  |                      |                                          |
|     | local 3-4                 | J                               | L                   | M                                         |
|     | detail 6-7-8              | J                               | J                   | M                                         |
|     | thickness of sedimentary cover | J                               | J                   | M                                         |

### Figure 2 – Faults Spatial Density
Another map of faults spatial density and a map of spatial density of the 3-4 order lineaments (Figure 3) were made over a grid of 1 km x 1 km for the chosen local site in the ArcGIS 10.6 software environment. Then, forty different locations were allocated and considered, so as to smoothly cover zones of different faults and lineaments spatial density (four levels) according to obtained maps. Each location was analyzed in terms of their characterization according to 16 previously proposed factors and database of 40 items was created in the form of a table with the head similar to Table 2.

Mathematical modeling for radon-prone area identification

The method of discriminant functions was used to develop a forecasting model for radon-prone area identification. It is widely applied in various fields of human activities, as well as the other methods of mathematical statistics [23 – 25]. For this purpose, data on all locations were divided into training and testing samples, which included 70 % and 30 % of all observations, respectively. Four levels of potential radon hazard (PRH) were conditionally identified: from the lowest (the 1st) where locations belong to the zone of the lowest spatial faults density to the highest (the 4th) level where locations are concentrated within zones of highest spatial faults and lineaments density.

Each sample included research of all locations, respectively referred to four groups. From a mathematical point of view, all groups were considered as a set of objects with qualitative, varying characteristics. Based on these characteristics, the group to which the object belongs was determined. The mathematical processing of the results was carried out in SPSS 19.0 software environment [26].

Three discriminant functions of the following type are needed to determine the group membership:

\[ \text{DF} = b_{1} \cdot 1 + \ldots + b_{i} \cdot x_{i} + \ldots + b_{p} \cdot x_{p} + C, \]

where \( \text{DF} \) is the discriminant function value; \( x_{i} \) is the quantitative value of the \( i \)-th attribute; \( b_{i} \) is the \( i \)-canonical coefficient of discriminant function (contribution of the \( i \)-th attribute to the function value); \( p \) is the number of attributes; \( C \) is the constant.

The mathematical model predictors were determined using the Fisher Statistics by their sequential inclusion in the discriminant equations. Seven of fifteen considered radon hazardous factors were turned to be informative, and canonical coefficients were calculated for them using the

![Figure 3 – Spatial Density of the 3-4 Order Lineaments](image)
least squares method for the first and second order polynomials. Determination of the mathematical model predictors and the canonical coefficients of the discriminant functions are presented in Table 2.

Therefore, the radon-prone areas identification can be described by the following discriminant functions:

\[
\text{DF}_1(X) = 0.532 \cdot X_1 + 1.746 \cdot X_2 + 1.485 \cdot X_3 + 0.851 \cdot X_4 + 0.153 \cdot X_5 + 0.900 \cdot X_6 + 0.474 \cdot X_7 - 14.871,
\]

\[
\text{DF}_2(X) = 1.588 \cdot X_1 + 0.047 \cdot X_2 + 1.352 \cdot X_3 + 1.338 \cdot X_4 - 0.845 \cdot X_5 + 0.997 \cdot X_7 - 2.208,
\]

\[
\text{DF}_3(X) = -0.053 \cdot X_1 + 1.398 \cdot X_2 - 0.982 \cdot X_3 + 0.195 \cdot X_4 + 0.776 \cdot X_6 + 0.776 \cdot X_7 - 2.934.
\]

Based on the discriminant function values, a territorial map of a new object classification was developed (Figure 4). The territorial map defines the distribution in the area that determines the group affiliation (Table 3). However, within the relevant area, the likelihood of being in this group is higher than for the other groups [27]. Within the areas, the probability for boundary groups is the same.

### Table 2 – Coefficients of canonical discriminant function

| Model's predictors                  | Function | 1  | 2  | 3    |
|-------------------------------------|----------|----|----|------|
| Uranium Deposits and Ore Manifestations |          | 0.532 | 1.588 | -0.053 |
| Uranium Content in Rocks            |          | 1.746 | 0.047 | 1.398 |
| Uranium Content in Soils            |          | 1.485 | 1.352 | -0.982 |
| Reliable Faults Spatial Density     |          | 0.851 | -1.338 | 0.195 |
| Unreliable Faults Spatial Density   |          | 0.153 | -0.845 | -0.983 |
| Local Lineaments Spatial Density    |          | 0.900 | -1.258 | 0.767 |
| Distance from Sanitary Protection Zone |      | 0.474 | 0.997 | 0.776 |
| Constant                            |          | -14.871 | -2.208 | -2.934 |
The correlation coefficients between calculated values of discriminant functions and indicators of group affiliation served a good measure for distribution into groups (Table 4). The obtained eigenvalues are provided in descending order of their values. The value of the eigenvalue is associated with the discriminant capabilities of the function: the higher the eigenvalue, the better the difference. A qualitative estimate of the \( r_{xy} \) link density was established based on the Cheddock scale.

Additionally, the Wilks’ Lambda test was conducted to determine whether the average values of discriminant functions in groups significantly differ among themselves (Table 5).

The obtained discriminant functions allow correct classification of the four groups according to seven predictors. The classification results for the training sample are presented in Table 6.

### Results and discussions

Large-scale studies conducted in Western Europe in the early 1990s have shown that radon produces between 50 % of the collective dose for radon-safe areas and up to 92 % for regions of high radon potential. In the mid-1990s, the State Enterprise «Kirovheolohiia» and other Research Institutions of Ukraine performed radioecological studies on radon in residential areas of the city of Kropyvnytskyi (Kirovohrad) and in the Kirovohrad district [10]. It was determined that 50 % of the surveyed neighborhoods belong to radon-prone areas, including 33.7 % - where indoor radon exceeds 100 Bq/m\(^3\), 11.4 % - 200 Bq/m\(^3\), 0.14 % - 1000 Bq/m\(^3\). In general, it was determined that the number of houses, in which the average annual radon equilibrium equivalent concentration exceeds 100 Bq/m\(^3\) is 53 % of the total number of surveyed houses [10, Kirovheolohiia Archive Materials, 1992-1996].

The research of radon hazard for the Kirovohrad uranium ore region shows the association of the most radon hazardous areas directly with zones of high spatial density of faults and 3-4 order lineaments that is confirmed by high indoor radon values in the neighborhoods of the Kropyvnytskyi city (Figure 5).
Our studies have shown interesting results regarding the joint use of geospatial analysis and mathematical forecasting for zoning of the territory by the radon hazard level in the ArcGIS 10.6 software environment. Spatial faults (reliable and unreliable) density and then spatial density of the 3-4 order lineaments were taken first into consideration as the basic parameters for the initial stage of radon mapping at regional level. Other parameters were added further for a more detailed characterization of the radon hazardous area depending on the chosen location under consideration at local level. The presented technique can be applied to any territories where there is a high level of geological exploration, which allows development of a database of radon hazard factors.

It should be noted that our research confirms that the obtained high indoor radon concentrations are located within the radon-prone areas determined based on geospatial analysis, including the city of Kropyvnytskyi.

Analysis of the mathematical model classification results showed that all objects of groups 1, 2 and 4 were correctly classified. When classifying objects of the group 3, only 90 % of cases were correctly identified and 10 % were assigned to another group. Thus, the accuracy of potential radon hazard level was 97.5 % based on the training sample data.

Analyzing the obtained eigenvalues of the first and the third discriminant functions, equaled to 14,713 and 0,243, one can make a conclusion that the classification capabilities of the first discriminant function are almost 61 times greater than the third one.

When estimating the values of the canonical correlation coefficients, amounted to 0.968 and 0.442, respectively, of the first and third discriminant functions, it is possible to conclude that there is fairly high connection between the radon hazard level and the value of the first discriminant function, which is confirmed by the percentage of this function dispersion – 80.9 %.

During the Wilks’ Lambda test, a very significant result was found between the first and third functions (p <0.001) and a non-significant result between the last functions. Accordingly, it can be concluded that to identify the radon hazard areas, it is sufficient to use the first $DF_1$ and the third $DF_3$ discriminant functions.

When testing the developed mathematical model in the test sample, it was found that the prediction was made correctly for all four groups (Table 7).

Thus, the overall percentage of correct prediction of the radon-prone areas can make up 98.2 %, if the
may be impossible due to various, primarily economic reasons. In a limited number of direct indoor radon measurements, remote methods are supposed to be a good help in identification of potentially radon hazardous level. Therefore, the radon survey can be further prioritized based on potential level identified on geospatial and mathematical modeling data.

As far as our model for identification of potentially radon-prone areas is mainly based on geological studies, the further research is supposed to be directed to its approbation for a different geological environment of the Ukrainian shield, for example, the highly populated Kyiv oblast area.

Thus, the overall rate of correct prediction of the level of potential radon hazard of the territory can be 98.2 %, if the criteria for the selection of a new object of study will be identical to the statistical distribution of data that formed the basis for a mathematical model development. For practical use of the model, it is supposed to determine the degree of conformity of the calculated model to the new object of research. It determines the prioritization or replacement of radon hazard factors (among the proposed 13), or addition of new significant factors, the importance of local characteristics of areas for radon hazard studies, that will require adapting the model and establishing adequacy to the new object.

### Table 7 – Classification of the test sample objects

| Level of Potential Radon Hazard PRH | Predicted Group Membership, % | Total |
|------------------------------------|-------------------------------|-------|
|                                    | first (lowest) level of PRH   |       |
|                                    | second level of PRH           |       |
|                                    | third level of PRH            |       |
|                                    | forth (highest) level of PRH   |       |
| Original, %                        |                               |       |
| first (lowest) level of PRH        | 100                           | 100   |
| second level of PRH                | 0                             | 100   |
| third level of PRH                 | 0                             | 0     |
| forth (highest) level of PRH (potentially radon-prone areas) | 0                             | 0     |

Conclusions

1. In the context of the EU Basic Safety Standards, where radon-prone areas are required to be identified, it is proposed to use remote sensing methods for geospatial modeling of radon-prone areas, first at regional and then at local levels. The basic parameters for the initial mapping stage are supposed to be the faults and the lineaments of the 3rd and 4th level spatial density. Other parameters are added for more detailed analysis, depending on the particular location under consideration.

2. A mathematical model for the level of radon potential identification was developed based on the method of linear discriminant functions. High level of natural radioactivity associated with uranium content in environment objects and natural uranium occurrences, and also the spatial density of faults (reliable and unreliable) and lineaments were taken into account as well as the distance from uranium mine located nearby. The model developed allows classifying the level of radon potential in 98.2 % correctly.

3. As far as in European countries the indoor radon measurements are accepted on unified requirements and on a grid of 10 x 10 km, for countries intending to join the EU radon program, such measurements may be impossible due to various, primarily economic reasons. In a limited number of direct indoor radon measurements, remote methods are supposed to be a good help in identification of potentially radon hazardous level. Therefore, the radon survey can be further prioritized based on potential level identified on geospatial and mathematical modeling data.

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