On-demand high-capacity ride-sharing via dynamic trip-vehicle assignment

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Ride-sharing services are transforming urban mobility by providing timely and convenient transportation to anybody, anywhere, and anytime. These services present enormous potential for positive societal impacts with respect to pollution, energy consumption, congestion, etc. Current mathematical models, however, do not fully address the potential of ride-sharing. Recently, a large-scale study highlighted some of the benefits of car pooling but was limited to static routes with two riders per vehicle (optimally) or three (with heuristics). We present a more general mathematical model for real-time high-capacity ride-sharing that (i) scales to large numbers of passengers and trips and (ii) dynamically increases optimal routes with respect to online demand and vehicle locations. The algorithm starts from a greedy assignment and improves it through a constrained optimization, quickly returning solutions of good quality and converging to the optimal assignment over time. We quantify experimentally the trade-off between fleet size, capacity, waiting time, travel delay, and operational costs for low- to medium-capacity vehicles, such as taxis and van shuttles. The algorithm is validated with ~3 million rides extracted from the New York City taxicab public dataset. Our experimental study considers ride-sharing with rider capacity of up to 10 simultaneous passengers per vehicle. The algorithm applies to fleets of autonomous vehicles and also incorporates rebalancing of idling vehicles to areas of high demand. This framework is general and can be used for many real-time multivehicle, multitask assignment problems.

Significance

Ride-sharing services can provide not only a very personalized mobility experience but also ensure efficiency and sustainability via large-scale ride pooling. Large-scale ride-sharing requires mathematical models and algorithms that can match large groups of riders to a fleet of shared vehicles in real time, a task not fully addressed by current solutions. We present a highly scalable anytime optimal algorithm and experimentally validate its performance using New York City taxi data and a shared vehicle fleet with passenger capacities of up to ten. Our results show that 2,000 vehicles (15% of the taxi fleet) of capacity 10 or 3,000 of capacity 4 can serve 98% of the demand within a mean waiting time of 2.8 min and mean trip delay of 3.5 min.
Here, we consider the problem of using a fleet of vehicles with varying passenger capacities, and, in contrast to ref. 5, we address both the problems of assigning vehicles to matched passengers and rebalancing—or repositioning—the fleet to service demand. We show how the unified problem of passenger and vehicle assignment can be solved in a computationally efficient manner at a large scale, thereby demonstrating the capability to operate a real-time MoD system with multiple service tiers (shared-taxi, shared-vans, and shared-buses) of varying capacity.

Whereas previous approaches to this problem have focused on heuristic-based solutions (16–18), we present a reactive anytime optimal algorithm. That is, an algorithm that efficiently returns a valid assignment of travel requests to vehicles and then refines it over time, converging to an optimal solution. If enough computational resources are available, the optimal assignment for the current requests and time would be found; otherwise, the best solution found so far is returned.

Traditional approaches that rely on an integer linear program (ILP) formulation, such as ref. 19, also provide anytime guarantees for the multivehicle-routing problem. However, in contrast to our approach, their applicability is limited to small problem instances, which in ref. 19 was 32 requests and 4 vehicles, with a computation cost of several minutes. We also rely on an ILP formulation, but because we do not explicitly model the edges of the road network in the ILP, our approach scales to much larger problem instances. We observe that instances such as New York City, with thousands of vehicles, requests, and road segments, can be solved in real time.

Our approach decouples the problem by first computing feasible trips from a pairwise shareability graph (5) and then assigning trips to vehicles. We show that this assignment can be posed as an ILP of reduced dimensionality. The framework allows for flexibility in terms of prescribing constraints such as (but not limited to) maximum user waiting times and maximum additional delays due to sharing a ride. We also extend the method to proactively rebalance the vehicle fleet by moving idle vehicles to areas of high demand. We quantify experimentally the performance tradeoffs between fleet size, capacity, waiting time, travel delay, and operational costs for low- and medium-capacity vehicles (such as taxis, vans, or minibuses) in a large urban setting. Detailed experimental results are presented for a subset of ~3 million rides extracted from the New York City taxicab public dataset. We show that 3,000 vehicles with a capacity of 2 and 4 could serve 94 and 98% of the demand with a mean waiting time of 3.2 and 2.7 min, and a mean delay of 1.5 and 2.3 min, respectively. To achieve 98% service rate, with comparable waiting time (2.8 min) and delay (3.5 min), a fleet of just 2,000 vehicles with a capacity of 10 was required. This fleet size is 15% of the active taxis in New York City (Movie S1). We also show that our approach is robust with respect to the density of requests and could therefore be applied to other cities.

Our system runs in real time and is particularly suited to autonomous vehicle fleets that can continuously reroute based on real-time requests. It can also rebalance idle vehicles to areas with high demand and is general enough to be applied to other multivehicle, multitask assignment problems.

**Passenger Assignment and Vehicle Routing**

We consider a fleet $V$ of $m$ vehicles of capacity $ν$, the maximum number of passengers each vehicle can have at any given time. We address the problems of both optimally assigning online travel requests to vehicles and finding optimal routes for the vehicle fleet. Each travel request consists of the time of request, a pickup location and a drop-off location. We propose an anytime optimal algorithm for batch assignment of a set of requests $R = \{ r_1, \ldots, r_n \}$ to a set of vehicles $V = \{ v_1, \ldots, v_m \}$, which minimizes a cost function $C$, satisfies a set of constraints $Z$, and allows for multiple passengers per vehicle. A passenger is a past request that has been picked up by a vehicle and that is now en route to its destination. We denote by $P_v$ the set of passengers for vehicle $v \in V$. In a second step, the method also allows to rebalance the fleet of vehicles by driving idle vehicles to areas of high demand, where those vehicles are needed.

[Diagram Fig. 1. Schematic overview of the proposed method for batch assignment of multiple requests to multiple vehicles of capacity $ν$. The method consists of several steps leading to an integer linear optimization that provides an anytime optimal assignment. (A) Example of a street network with four requests (orange human, origin; red triangle, destination) and two vehicles (yellow car, origin; red triangle, destination of passenger). Vehicle 1 has one passenger, and vehicle 2 is empty. (B) Pairwise shareability RV-graph of requests and vehicles. Cliques of this graph are potential trips. (C) RTV-graph of candidate trips and vehicles which can execute them. A node (yellow triangle) is added for requests that cannot be satisfied. (D) Optimal assignment given by the solution of the ILP, where vehicle 1 serves requests 2 and 3 and vehicle 2 serves requests 1 and 4. (E) Planned route for the two vehicles and their assigned requests. In this case, no rebalancing step is required because all requests and vehicles are assigned.]
likely to be required in the future. A schema of the method is shown in Fig. 1.

Our formulation is flexible with respect to physical and performance-related constraints that might need to be added. In our implementation, we consider the following. (i) For each request $r$, the waiting time $\omega_r$, given by the difference between the pickup time $t_i^r$ and the request time $t_i^r$, must be below a maximum waiting time $\Omega$, for example, 2 min. (ii) For each passenger or request $r$ the total travel delay $\delta_r = t_i^r - t_j^r$ must be lower than a maximum travel delay $\Delta$, for example, 4 min, where $t_j^r$ is the drop-off time and $t_i^r = t_j^r + \tau(o_r, d_r)$ is the earliest possible time at which the destination could be reached if the shortest path between the origin $o_r$ and the destination $d_r$ was followed without any waiting time. The total travel delay $\delta_r$ includes both the in-vehicle delay and the waiting time. Finally, (iii) for each vehicle $v$, we consider a maximum number of passengers, $n_{\text{pass}}^v \leq \nu_v$, for example, capacity 10.

We define the cost $C$ of an assignment as the sum of delays $\delta_r$ (which includes the waiting time) over all assigned requests and passengers, plus a large constant $c_{\text{ko}}$ for each unassigned request. Given an assignment $\Sigma$ of requests to vehicles, we denote by $\mathcal{R}_{ak}$ the set of requests that have been assigned to some vehicle and $\mathcal{R}_{ko}$ the set of unassigned requests, due to the constraints or the fleet size. Formally,

$$C(\Sigma) = \sum_{v \in V} \sum_{r \in \mathcal{P}_v} \delta_r + \sum_{r \in \mathcal{R}_{ak}} \delta_r + \sum_{r \in \mathcal{R}_{ko}} c_{\text{ko}}. \tag{1}$$

This constrained optimization problem is solved via four steps (Fig. 1), which are: computing a pairwise request-vehicle shareability graph (RV-graph) (Fig. 1B); computing a graph of feasible trips and the vehicles that can serve them (RTV-graph) (Fig. 1C); solving an ILP to compute the best assignment of vehicles to trips (Fig. 1D); and rebalancing the remaining idle vehicles (Fig. 1E).

Given a network graph with travel times, we consider a function $\text{travel}(v, \mathcal{R})$ for single-vehicle routing. For a vehicle $v$, with passengers $\mathcal{P}_v$, this function returns the optimal travel route $\sigma_v$ to satisfy requests $\mathcal{R}_v$. This route minimizes the sum of delays $\sum_{r \in \mathcal{R}_v} \delta_r$ subject to the constraints $\mathcal{Z}$ (waiting time, delay, and passenger capacity). For low-capacity vehicles, such as taxis, the optimal path can be computed via an exhaustive search. For vehicles with larger capacity, heuristic methods such as Lin–Kernighan (20), Tabu search (21), or simulated annealing (22) may be used. Fig. 2, Right shows the optimal route for a vehicle with four passengers and an additional request.

The RV-graph (Fig. 1B) represents which requests and vehicles might be pairwise-shared and builds on the idea of shareability graphs proposed by ref. 5 but also includes the vehicles at their current state. Two requests $r_1$ and $r_2$ are connected if an empty virtual vehicle starting at the origin of one of them could pick up and drop off both requests while satisfying the constraints $\mathcal{Z}$. A cost $\delta_{r_1} + \delta_{r_2}$ is associated to each edge $e(r_1, r_2)$. Likewise, a request $r$ and a vehicle $v$ are connected if the request can be served by the vehicle while satisfying the constraints $\mathcal{Z}$, as given by $\text{travel}(v, r)$. The edge is denoted by $e(r, v)$.

Next, the cliques of the RV-graph—or regions for which its induced subgraph is complete—are explored to find feasible trips and compute the RTV-graph (Fig. 1C). A trip $T = \{r_1, \ldots, r_n\}$ is a set of $n_p$ requests to be combined in one vehicle. A trip is feasible if all of the requests can be picked up and dropped off by some vehicle, while satisfying the constraints $\mathcal{Z}$.

This step computes feasible trips. There might be several trips of varying size that can service a particular request. In addition, more than one vehicle might be able to service a trip. The assignment step will later ensure that each request and vehicle are assigned to a maximum of one trip. The RTV-graph contains two types of edges: (i) edges $e(r, T)$, between a request $r$ and a trip $T$ that contains request $r$ (i.e., $\exists e(T, r) \iff r \in T$), and (ii) edges $e(T, v)$, between a trip $T$ and a vehicle $v$ that can execute the trip (i.e., $\exists e(T, v) \iff \text{travel}(v, T)$ is feasible). The cost $\sum_{r \in \mathcal{R}_v} \delta_r$, sum of delays, is associated to each edge $e(T,v)$.

The problem is formulated as an ILP, initialized with a greedy assignment obtained directly from the RTV-graph. To compute the greedy assignment $\Sigma_{\text{greedy}}$, trips are assigned to vehicles iteratively in decreasing size of the trip and increasing cost (sum of travel delays). The idea is the maximize the amount of requests served while minimizing the cost (SI Appendix, Algorithm 2).

The optimization problem is formulated in Algorithm 1. A binary variable $\epsilon_{i,j} \in \{0,1\}$ is introduced for each edge $e(T_i, v_j)$ between a trip $T_i \in T$ and a vehicle $v_j \in \mathcal{V}$ in the RTV-graph. If $\epsilon_{i,j} = 1$, then vehicle $v_j$ is assigned to trip $T_i$. We denote by $E_{TV}$ the set of $(i,j)$ indices for which an edge $e(T_i, v_j)$ exists in the RTV-graph, i.e., the set of possible pickup trips. An additional binary variable $\chi_k \in \{0,1\}$ is introduced for each request $r_k \in \mathcal{R}$. These variables are active, i.e., $\chi_k = 1$, if the associated request $r_k$ can not be served by any vehicle and is ignored. The set of variables is then $X = \{\epsilon_{i,j}, \chi_k; \forall e(T_i, v_j) \in \text{RTV-graph and } \forall r_k \in \mathcal{R}\}$.

The cost terms $c_{i,j}$ are the sum of delays for trip $T_i$ and vehicle $v_j$ pickup (stored in the $e(T_i, v_j)$ edge of the RTV-graph) and $c_{\text{ko}}$ is a large constant to penalize ignored requests.
Two types of constraints are included. Line 3 in Algorithm 1 imposes that each vehicle is assigned to one trip at most. Line 4 imposes that each request is assigned to a single vehicle or ignored. In these constraints, three sets appear. The set of trips that can be serviced by a vehicle \( j \), or edges \( e(T_i, v_j) \), is \( T_{V,j} \). The set of trips that contain request \( k \), or edges \( e(T_i, T_k) \), is \( T_{I,k} \). The set of vehicles that can service trip \( i \), or edges \( e(T_i, v_j) \), is \( V_{I,j} \).

This ILP is solved incrementally from the greedy assignment \( \Sigma_{\text{greedy}} \), improving the quality of the assignment over time.

**Algorithm 1. Optimal assignment**

1. Initial guess: \( \Sigma_{\text{greedy}} \)
2. \( \Sigma_{\text{optimal}} := \arg \min_{\Sigma} \sum_{T \in T} \epsilon(T, v) + \sum_{v \in V} \epsilon_{\text{vehicle}}(v) \) subject to:
   \( \sum_{T \in T} \epsilon_{\text{vehicle}}(v) \leq 1 \) for all \( v \in V \)
3. \( \forall T \in T \) \( \sum_{T \in T} \epsilon(T, v) = 1 \) for all \( v \in V \)

This method is well suited for online execution to assign incoming requests \( r(t) \) to a fleet of vehicles for which a pool of requests \( \mathcal{R}_o \) is maintained where \((i)\) new requests are added as they are received and \((ii)\) requests are removed when they are either \( (a) \) picked up by a vehicle or \( (b) \) could not be successfully matched to any vehicle within the maximum waiting time (they are ignored).

Requests are collected during a time window (e.g., 30 s), after which they are assigned in batch to the different vehicles. If a request is matched to a vehicle at any given iteration, its latest pickup time is reduced to the expected pickup time by that vehicle and the cost \( \chi_{\text{vehicle}} \) of ignoring it is increased for subsequent iterations. A request might be rematched to a different vehicle in subsequent iterations as long as its waiting time does not increase and until it is picked up by some vehicle. Once a request is picked up, it remains in that vehicle and cannot be rematched—the vehicle may still pick additional passengers. In each iteration, the new assignment of requests to vehicles guarantees that the current passengers are dropped off within the maximum delay constraint.

After the assignment, due to fleet imbalances, the set \( \mathcal{R}_{\text{idle}} \) of unassigned requests may not be empty, and some empty vehicles \( \mathcal{V}_{\text{idle}} \) may still be unassigned to any request. These imbalances may occur when the idle vehicles are in areas far away from the area of current requests and due to the maximum waiting time and delay constraints and vehicle capacity. Under the assumptions that \((i)\) ignored requests may wait longer and request again, \((ii)\) it is likely that more requests occur in the same are where all requests cannot be satisfied, and \((iii)\) there are not enough requests in the neighborhood of the idle cars, we propose the following approach to rebalance the fleet by moving only the idle vehicles.

To rebalance the vehicle fleet, after each batch assignment, the vehicles in \( \mathcal{V}_{\text{idle}} \) are assigned to requests in \( \mathcal{R}_{\text{ko}} \) to minimize the sum of travel times, with the constraint that either all requests or all of the vehicles are assigned. We first compute the travel time of each individual idle vehicle in \( \mathcal{V}_{\text{idle}} \) to pick each ignored request in \( \mathcal{R}_{\text{ko}} \) and then obtain the optimal assignment via a linear program (SI Appendix, Algorithm 4). In this approach, if all requests can be satisfied, some vehicles may remain idle, saving fuel and distance traveled, which is the case at nighttime.

**Complexity.** The number of variables in the ILP is equal to the number of edges \( e(T, v) \) in the RTV-graph plus the number of requests. In the worst case, the number of variables is of order \( O(mn^2) \) but only reached with complete RV- and RTV-graphs, where all vehicles can serve all requests and all requests can be combined with each other. In practice, the number of variables is orders of magnitude lower and related to the size of the cliques in the RV-graph. The number of constraints is \( n + m \).

**Anytime Optimality.** This method guarantees optimality of the assignment of the currently active requests, while satisfying the constraints \( \mathcal{Z} \), if all of the steps are executed until termination and exploration of all possible trips and assignments. In practice, timeouts can be set both for the amount of time spent generating candidate trips for each vehicle and for the time spent exploring the branches of the ILP. A limit on the number of vehicles considered per request, the number of trips per vehicle, or the optimality gap of the ILP can also be set. These timeouts trade optimality for tractability, and their values will depend on the available resources. We note that the method is reactive, in the sense that it provides anytime-optimality guarantees given the current state of the system and the current requests. To inform the assignment and routing about future demand, an additional cost term could be added to Eq. 1, and future requests could be sampled from historical data. The method allows for parallelization in all steps. Proofs are provided in SI Appendix, III. Theoretical Guarantees.

**Results** We assess the performance of a MoD fleet controller using the proposed algorithm, against real data from an arbitrarily chosen representative week, from 0000 hours Sunday, May 5, 2013, to 2359 hours, Saturday May 11, 2013, from the publicly available dataset of taxi trips in Manhattan, New York City (23). This dataset contains for each day the time and location of all of the pickups and drop-offs executed by each of the 13,586 active taxis. From these data, we extract all of the requests (origin and destination within Manhattan) and consider the time of request equal to the time of pickup. We consider the complete road network of Manhattan (4,092 nodes and 9,453 edges), with the travel time on each edge (road segment) of the network given by the daily mean travel time estimate, computed using the method in ref. 5. Shortest paths and travel times between all nodes are then precomputed and stored in a lookup table.

We perform a simulation of the evolution of the taxi fleet, where vehicles are initialized at midnight at sampled positions from a historical demand distribution and continuously travel to pick up and drop off passengers to satisfy the real requests extracted from the dataset. Requests are collected during a
High vehicle occupancy is achieved in times of high demand, with a large number of the trips being shared. In Fig. 2, we observe that many vehicles are located in mid-Manhattan and contain three or four passengers. Fig. 3 shows that the occupancy depends on the fleet size, capacity, and the maximum waiting/delay time. Lower fleet size, larger capacity and longer waiting/delay times increase the possibilities for ride-sharing and lead to higher mean vehicle occupancy. In Fig. 4, we observe that during peak hours, a small fleet of high-capacity vehicles does indeed operate at high occupancy. For a fleet of 1,000 vehicles of capacity 10, we observe that, during peak time (1800 hours) of a Friday, 10% of the vehicles have eight or more passengers, 40% of the vehicles have six or more, 80% have three or more, and 98% have at least one passenger. For a fleet of 2,000 vehicles of capacity four, we observe that, at the same peak time, over 70% of them have at least three passengers onboard.

We observe that the value of fleets with larger passenger capacities increases with larger \( \Omega \) and \( \Delta \) values, as expected, because passengers are willing to incur a larger personal time penalty. High-capacity vehicles are also more important when the fleet size is smaller, because seating capacity might be a bottleneck with smaller fleets. For instance (Fig. 5.4), a fleet of 1,000 vehicles with a capacity of 10 can satisfy almost 80% of the requests with \( \Omega = 420 \) s, compared with below 30% for a single-rider taxi, for a net gain of over 50%. However, with a larger fleet of 3,000 vehicles and \( \Omega = 120 \) s, the benefit is only about 15%. Interestingly, if longer waiting times and delays are

![Fig. 5.](image-url) Comparison of several performance metrics for varying vehicle capacity (1, 2, 4, and 10 passenger, shown with lines). Each subplot is for a fleet size of 1,000, 2,000, and 3,000 vehicles, and the coordinate axes show increasing maximum waiting time \( \Omega \) of 2, 5, and 7 min. We analyze service rate (percentage of requests serviced) (A), average in car delay \( \delta \) (B), average waiting time \( \omega \) (C), average distance traveled by each vehicle during a single day (D), percentage of shared rides (number of passengers who shared a ride divided by the total number of picked-up passengers) (E), and average computational time for a 30-s iteration of the method (F), in a 24 core 2.5 GHz machine, including computation of the RV-graph, computation of the RTV-graph, ILP assignment, rebalancing, and data writing (higher levels of parallelization would drastically reduce this computational time). The parameters used in the simulation are specified in SI Appendix, III. Theoretical Guarantees, C. Heuristics for Real-Time Execution.

Alonso-Mora et al. PNAS Early Edition | 5 of 6
allowed, $\Omega = 420$ s, a fleet of 3,000 vehicles with a capacity of 2, 4, and 10 could serve 94, 98, and 99% of the demand. To achieve 98% service rate, a fleet of just 2,000 vehicles with a capacity of 10 was required, which represents a reduction of the fleet size to 15% of the active taxi fleet in New York City.

As expected, the in-car travel delay does increase with the increase in vehicle capacity (Fig. 5B). Nonetheless, that increase seems practically negligible—well below 100 s—once ride-sharing is allowed. Furthermore, the mean waiting time does in fact decrease as vehicle capacity is increased (Fig. 5C). For a fleet size of 1,000 vehicles and $\Delta = 420$ s, high-capacity vehicles not only improved the service rate but also achieved a reduction in mean waiting time of over 100 s, which partially offsets the increased in-car delay. In particular, we observe that 3,000 vehicles with a capacity of 2 and 4 could serve 94 and 98% of the demand, with a mean waiting time of 3.2 and 2.7 min and a mean delay of 1.5 and 2.3 min, respectively. To achieve 98% service rate, with comparable waiting time (2.8 min) and delay (3.5 min), a fleet of just 2,000 vehicles with a capacity of 10 was required.

We also observed that increasing the vehicle capacity not only increases the service rate but also reduces the mean distance traveled by the vehicles in the fleet (Fig. 5D), potentially leading to a reduction in costs, congestion, and pollution. We also observe that, with our online method, about 90% of the rides were shared. The number of shared rides slightly increases with $\Delta$ and decreases with the fleet size (Fig. 5E). Finally, we note that our approach is real-time capable (Fig. 5F).

In this paper, we introduced a reactive anytime optimal method with scalable real-time performance for assigning passenger requests to a fleet of vehicles of varying capacity. We quantify experimentally the tradeoff between fleet size, capacity, waiting time, travel delay, and operational costs for low- and medium-capacity vehicles, such as taxis or vans in a large-scale city dataset. Under the assumption of one person per ride, we show that 98% of the taxi rides currently served by over 13,000 taxis could be served with just 3,000 taxis of capacity four. We observe that a vehicle capacity of two is sufficient for ride-sharing when a small trip delay of 2 min is imposed. If a maximum delay of 5 min or more (comparable to the time spent retrieving a car from parking) is allowed, higher-capacity vehicles (i) increase the service rate significantly, (ii) reduce the waiting time, and (iii) reduce the distance traveled by each vehicle. Our analysis shows that a ride-pooling service can provide a substantial improvement in urban transportation systems and that the system parameters such as vehicle capacity and fleet size depend on quality of service requirements and demand.

**Conclusion**

In this paper, we introduced a reactive anytime optimal method with scalable real-time performance for assigning passenger requests to a fleet of vehicles of varying capacity. We quantify experimentally the tradeoff between fleet size, capacity, waiting time, travel delay, and operational costs for low- and medium-capacity vehicles, such as taxis or vans in a large-scale city dataset. Under the assumption of one person per ride, we show that 98% of the taxi rides currently served by over 13,000 taxis could be served with just 3,000 taxis of capacity four. We observe that a vehicle capacity of two is sufficient for ride-sharing when a small trip delay of 2 min is imposed. If a maximum delay of 5 min or more (comparable to the time spent retrieving a car from parking) is allowed, higher-capacity vehicles (i) increase the service rate significantly, (ii) reduce the waiting time, and (iii) reduce the distance traveled by each vehicle. Our analysis shows that a ride-pooling service can provide a substantial improvement in urban transportation systems and that the system parameters such as vehicle capacity and fleet size depend on quality of service requirements and demand.

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