Purpose: The aim of this study was to compare the wave-CAIPI (controlled aliasing in parallel imaging) trajectory to the Cartesian sampling for accelerated free-breathing 4D lung MRI.

Methods: The wave-CAIPI k-space trajectory was implemented in a respiratory self-gated 3D spoiled gradient echo pulse sequence. Trajectory correction applying the gradient system transfer function was used, and images were reconstructed using an iterative conjugate gradient SENSE (CG SENSE) algorithm. Five healthy volunteers and one patient with squamous cell carcinoma in the lung were examined on a clinical 3T scanner, using both sampling schemes. For quantitative comparison of wave-CAIPI and standard Cartesian imaging, the normalized mutual information and the RMS error between retrospectively accelerated acquisitions and their respective references were calculated. The SNR ratios were investigated in a phantom study.

Results: The obtained normalized mutual information values indicate a lower information loss due to acceleration for the wave-CAIPI approach. Average normalized mutual information values of the wave-CAIPI acquisitions were 10% higher, compared with Cartesian sampling. Furthermore, the RMS error of the wave-CAIPI technique was lower by 19% and the SNR was higher by 14%. Especially for short acquisition times (down to 1 minute), the undersampled Cartesian images showed an increased artifact level, compared with wave-CAIPI.

Conclusion: The application of the wave-CAIPI technique to 4D lung MRI reduces undersampling artifacts, in comparison to a Cartesian acquisition of the same scan time. The benefit of wave-CAIPI sampling can therefore be traded for shorter examinations, or enhancing image quality of undersampled 4D lung acquisitions, keeping the scan time constant.

Keywords
free-breathing, lung, self-gated, wave-CAIPI
1 | INTRODUCTION

The lung is an especially challenging organ to image with MR, as the acquisition is typically impaired by respiratory and cardiac motion. In addition, the fast $T_2^*$ decay of the MR signal and the inherently low proton density of lung tissue complicates lung MRI. The easiest way to avoid artifacts arising from respiration is a breath-hold examination. However, patients often have a limited breath-hold capability, posing a severe restriction to the available acquisition time. Another approach is respiratory gating by means of image-based methods, or using additional external hardware. In addition, the center of k-space can be exploited as a navigator signal. Although some non-Cartesian k-space trajectories inherently measure this (direct current) DC signal in each repetition, a small increase in measurement time has to be invested in Cartesian and in wave-CAIPI (controlled aliasing in parallel imaging). The big advantage of these self-gating techniques is that they do not require any additional hardware, which saves time during patient preparation and increases patient comfort. Furthermore, retrospective gating allows for individual adjustment of gating parameters after the acquisition. Finally, the implementation of retrospective self-gating requires only minor modifications to existing pulse sequences. However, even with respiratory self-gating, acquisition times should be kept as short as possible, as long scan times bear an increased risk of involuntary patient movement, ultimately leading to degraded image quality. Furthermore, as available time slots in clinical routine are very limited, acceleration of the acquisition enables a higher patient throughput.

The Cartesian k-space trajectory is used most prominently in clinical routine. However, other k-space trajectories may be better suited for accelerated imaging, which is of utmost importance to improve patient comfort. Recently, wave-CAIPI has been proven to be a very effective method for volumetric acquisitions, accelerated by parallel imaging. In this work, the wave-CAIPI k-space trajectory is used in a self-gated FLASH pulse sequence for dynamic lung imaging, to make better use of receive coil sensitivity variations in all three spatial dimensions.

A key difference to previous reports that used the wave-CAIPI technique is—apart from the target application—the phase-encoding scheme. The wave-CAIPI k-space trajectory is typically combined with a regular, 2D CAIPI-shifted undersampling pattern. In a work by Chen et al., a variable density sampling and radial view ordering scheme was used. To avoid large gaps in k-space after retrospective gating, the phase-encoding scheme in this work was randomized using a nonuniform density distribution that oversamples the center of k-space.

This work combines a randomized self-gated FLASH pulse sequence with the wave-CAIPI k-space trajectory to acquire high-quality, dynamic 3D images of the human lung during free breathing. The proposed method is especially interesting for radiotherapy treatment planning, as respiration-induced tumor motion needs to be carefully evaluated before treatment. For different acquisition times, the wave-CAIPI sequence is compared to a Cartesian sequence with, apart from the k-space trajectory, identical parameters.

2 | METHODS

2.1 | Setup

The wave-CAIPI k-space trajectory was implemented in a 3D FLASH pulse sequence by playing out sinusoidal gradient oscillations on both phase-encoding axes during readout. The oscillations were shifted with respect to one another by a phase of $\pi/2$, leading to helically shaped readout lines in k-space. In this work, a fixed number of gradient oscillations $N_{\text{wave}} = 4$ and a maximum gradient wave amplitude $A_{\text{wave}} = 6 \text{ mT/m}$ was chosen. To acquire the k-space center signal (“DC signal”), which was used as a respiratory navigator signal, the ADC was opened for a short time immediately after the nonselective RF excitation pulse. A schematic pulse sequence diagram is shown in Figure 1A.

For all examinations, both wave-CAIPI and Cartesian reference scans were performed, using identical sequence parameters, apart from the additional gradient oscillations for the wave-CAIPI technique. Images were acquired with an isotropic resolution of 2.23 mm and a k-space matrix of size $224 \times 224 \times 112-144$. Further relevant sequence parameters were FOV = $500 \times 500 \times 250-321 \text{ mm}^3$, TR = 4.8 ms, TE = 1.9 ms, flip angle = 5º, readout bandwidth = 350 Hz/pixel, corresponding to a readout duration of 2.86 ms. Readout was always chosen to be in the head–foot direction. All examinations were performed with an 18-channel body coil array, in combination with a spine coil array with 12-16 channels activated.

The order of the phase-encoding steps was randomized with respect to nonuniformly distributed, 2D pseudo-random numbers, to avoid synchronization between phase encoding and breathing motion. Hence, 2D pseudo-random numbers within the 2D range of $([0, 1], [0, 1])$ were generated by a Mersenne-Twister algorithm, as implemented in the C++ standard library, using a normal distribution with a width of $\sigma = 0.3$. The resulting distribution was rescaled by the number of phase-encoding steps in both dimensions. The density distribution that was used is displayed in Figure 1C. A typical full sampling pattern of an 8-minute acquisition before respiratory gating is shown in Figure 1D.

To quantitatively evaluate and compare image quality, 4D lung MR scans were performed on 5 healthy volunteers, using both sampling strategies. In addition, 1 patient (male, 65 years old) with known squamous cell carcinoma in the lung was examined, and respiration-induced tumor movement was assessed. For both samplings, wave-CAIPI and Cartesian, the total acquisition time was set to $T_{\text{Acq}} = 08:01-10:18$ minutes,
leading to a moderate average undersampling rate of $R \approx 1.5$ in the images after respiratory self-gating, which was considered to provide adequate reference images for the later comparison with accelerated scans. For the calculation of sensitivity maps, a low-resolution, Cartesian reference scan with increased FOV in the coronal plane was performed.

All measurements were performed on a 3T clinical scanner (MAGNETOM Prisma®; Siemens Healthcare, Erlangen, Germany). The in vivo study was approved by our institution’s ethics committee, and informed, written consent was obtained from each subject before measurement.

### 2.2 Reconstruction

Regardless of the used k-space trajectory, the first step for image reconstruction is sorting the data, acquired in pseudo-random order, into different breathing states. To this end, the DC signal measured by the ADC directly after the excitation pulse is used as a navigator signal. In the absence of spatial encoding, this signal is proportional to the total amount of protons within the imaged object, weighted by the sensitivity profiles of the respective receive coils. The signal of a single receive coil near the lung/liver interface was manually selected and band-pass-filtered to smooth the signal and to remove signal variations corresponding to the periodic cardiac motion. The remaining signal variations of that coil then arise from tissue (liver) moving in and out of the range of sensitivity of the coil, and therefore serve as a respiratory navigator. An exemplary self-gating signal is displayed in Figure 2 for a volunteer examination. The measured data were binned into partially overlapping breathing states, with the requirement that all breathing states contain about 21% of all acquired data. The respiratory cycle was resolved in eight breathing states, which is a typical range for dynamic 3D lung acquisitions. This approach ensures that all k-space bins (corresponding to the breathing states) contain a sufficient amount of data for a stable parallel imaging reconstruction. Before respiratory gating, the first 2500 readouts were discarded, to be sure to achieve a steady-state magnetization.

Gradient system imperfections cause gradient discrepancies, such that the actually played-out sinusoidal gradient oscillations of the wave-CAIPI are a distorted version of the nominal gradients (ie, as designed in the pulse program).
Depending on the gradient axis, the real sinusoidal gradient oscillations differ from the theoretical waveforms by a time delay in the order of 6 µs and magnitude alterations of about 1%. The discrepancy between the theoretical input gradient and the gradient that is actually played out leads to inaccuracies in the k-space trajectory (as displayed in Figure 1B), consequentially deteriorating the image quality of the wave-CAIPI acquisitions. The gradient system transfer function characterizes this gradient system behavior and can therefore serve as a correction of the latter problem during reconstruction.\textsuperscript{19-22} The gradient system transfer function of the MR scanner was determined in additional phantom measurements. To this end, the phase evolution of the MR signal was measured in two parallel slices, while triangular input gradients were played out on the gradient axis perpendicular to the excited, parallel slices. Separate measurements for the three individual gradient axes were performed. A good estimate of the true k-space trajectory can be obtained by using only the self-terms of the gradient system transfer function.

After retrospective data sorting into breathing states and k-space trajectory correction, the images were reconstructed using an iterative CG SENSE approach.\textsuperscript{23,24} Sensitivity maps were calculated using the Berkeley Advanced Reconstruction Toolbox.\textsuperscript{25} Reconstruction times were between 45 and 90 minutes for eight breathing phases, depending on the degree of undersampling. Especially for comparisons of two different imaging techniques, a fair choice for the regularization parameter, in this case, the stopping criterion for the iterative SENSE reconstruction, needs to be defined. In this work, a criterion based on the actual image noise was formulated. From an additional scan, noise correlations in the different receiver coil elements were calculated for all volunteer examinations. For the noise measurement, the same pulse sequence setup as for actual imaging was used, with the RF amplitude set to zero. Therefore, only noise was measured in each receive channel. This measurement of noise correlations can be performed in only a few seconds. Subsequently, properly correlated, artificial noise can be generated using the method proposed by Robson et al.\textsuperscript{26} From the noise-only data, a noise covariance matrix describing noise correlations between the individual channels was calculated. The noise covariance matrix was used to generate artificial but authentic noise samples, to simulate a fully sampled, multichannel, noise-only scan with the same k-space matrix as for actual imaging. To obtain the image noise estimate from the noise-only k-space, a Fourier transformation was performed, and coil combination was done, taking into account the coil sensitivity maps. The noise estimate \( r_{\text{Noise}} \) is then calculated as the \( L^2 \)-norm of the coil-combined noise image, as follows:

\[
 r_{\text{Noise}} = \sqrt{\sum_{i=1}^{N_{\text{ch}}} \sum_{k=1}^{N_{\text{ch}}} m_{ik} C^*_k},
\]

where \( C^* \) is the complex conjugate transpose of the coil sensitivity matrix; \( m \) denotes the individual coil images; \( N_{\text{ch}} \) is the number of channels; and \( N_{\text{px}} \) is the number of image pixels. Iterations of the CG SENSE algorithm were performed until the CG residual \( r_{\text{CG}} \) obeyed \( r_{\text{CG}} < c \cdot r_{\text{Noise}} \), where the factor \( c \) dictates the compromise between residual aliasing artifacts and image noise. For the in vivo studies, the parameter was set to be in the range of 0.3-0.5, whereas for the phantom-based SNR calculations, \( c = 0.3 \) was chosen. The same value of \( c \) was chosen for the respective Cartesian and wave-CAIPI reconstructions. Based on the proposed criterion, the algorithm was stopped in the transition phase of the typical L-shaped function of the logarithm of the CG residual, plotted against the iteration number, as suggested in the work by Qu et al.\textsuperscript{27}

\[2.3 \quad \text{Image analysis}\]

The wave-CAIPI and Cartesian acquisitions were retrospectively accelerated. For this purpose, shorter scans were simulated by discarding data acquired at the end of the measurement, such that only a certain period of time (starting after establishing a steady-state magnetization) was kept. To assess the image quality for different accelerations, the normalized mutual information (NMI) and the RMS error (RMSE) were calculated for each breathing state as a function of acquisition time and used to quantify image similarity between retrospectively accelerated acquisitions and their respective references.\textsuperscript{15,28,29} The reference images were chosen to be the images of the individual breathing states, before retrospective acceleration. For this approach to work, the initially determined gating windows were kept fixed for all accelerations. The normalized mutual information of two discrete variables \( X \) and \( Y \) was calculated as

\[
\text{NMI}(X, Y) = \frac{I(X, Y)}{\sqrt{H(X) \cdot H(Y)}},
\]

where \( I(X, Y) \) is the mutual information between \( X \) and \( Y \), and \( H(X) \) and \( H(Y) \) denote the entropy of \( X \) and \( Y \), respectively. The NMI describes the amount of information that can be obtained about variable \( X \) by measuring the variable \( Y \). It is therefore suited as a similarity measure to compare different accelerated images with their respective reference. In addition to the NMI, the RMSE between the reference image and the accelerated images was calculated.

The SNR ratio \( r_{\text{SNR}} = \text{SNR}_{\text{wave-CAIPI}} / \text{SNR}_{\text{Cartesian}} \) and g-factors were calculated on a pixel-by-pixel basis for accelerated wave-CAIPI and Cartesian phantom experiments by means of the pseudo multiple replica method.\textsuperscript{26} To this end, 100 reconstructions were performed, each time adding artificial, properly correlated, and scaled noise to the acquired data. The phantom images were acquired using the same

\[
\text{SNR} = \frac{\mu}{\sigma},
\]

where \( \mu \) is the mean of the signal, and \( \sigma \) is the standard deviation of the noise.
density-weighted sampling scheme as for the dynamic lung images. The sampling pattern was adapted to mimic a typical k-space sampling pattern for a 1-minute 4D-lung MRI after respiratory gating (fraction of missing k-space lines ~92%). The phantom consisted of two stacked canisters, containing NaCl and NaH$_2$PO$_4$*2H$_2$O in water, respectively. As the phantom is not representative for actual lung tissue, absolute SNR values do not necessarily correspond to SNR in in vivo measurements. However, the SNR ratio, comparing wave-CAIPI and Cartesian sampling, is not affected by relaxation parameters and provides an adequate measure of SNR gain. The SNR calculation was performed using phantom measurements, as the final undersampling patterns of in vivo scans are different using retrospective self-gating. The same undersampling pattern was used for the wave-CAIPI and the Cartesian reconstruction. This avoids any possible effects due to different sampling patterns and is not possible for retrospectively gated in vivo data. The phantom-based approach also prevents errors in $f_{SNR} = \frac{SNR_{wave-CAIPI}}{SNR_{Cartesian}}$ due to motion, and enables a comparison on a pixel-by-pixel basis.

Furthermore, g-factor maps were calculated for accelerated wave-CAIPI and Cartesian 4D lung scans, also using the pseudo multiple replica method. To assess differences between wave-CAIPI and Cartesian sampling in the g-factor maps, the same undersampling pattern was simulated for the in vivo images as follows: The respective full data sets (without retrospective acceleration; scan time ~8 minutes) were reconstructed using the CG SENSE algorithm. The resulting artifact-free images were resampled retrospectively, to simulate a fully sampled in vivo scan. These artificially fully sampled data sets were then undersampled, using the same random undersampling pattern for both sampling techniques.

3 | RESULTS

Using the self-terms of the gradient system transfer function, image artifacts arising from gradient imperfections were effectively suppressed, as demonstrated in Figure 3 for a sagittal slice of a volunteer measurement.

A comparison of retrospectively accelerated images for Cartesian and wave-CAIPI sampling is shown in Figure 4. For an acquisition time of 8:01 minutes, both techniques result in good image quality. Especially in the case of high acceleration (down to 1 minute), the Cartesian images exhibit visible residual undersampling artifacts, whereas the artifact level is reduced using the wave-CAIPI technique. A more detailed comparison of accelerated images in three different orientations is displayed in Figure 5 for an acquisition time of 2 minutes.

Figure 6A-E presents box plots of calculated NMI values for all 5 healthy volunteer examinations; the average of NMI values was determined over the eight different breathing states. Median NMI values of the wave-CAIPI acquisition are consistently higher than the Cartesian NMI medians. Scatterplots of the NMI and the RMSEs of all volunteer measurements are shown in Figure 7. Most (91%) of the calculated RMSE values of the accelerated wave-CAIPI images are lower than the RMSEs for the Cartesian images; most of the individual RMSE values lie below the identity line in Figure 7A. As shown in Figure 7B, 97% of the individual NMI values lie above the identity line (ie, wave-CAIPI scans exhibit higher NMI values). Especially for small acquisition times, which correspond to higher RMSE and lower NMI levels, the difference between the two sampling schemes is more pronounced. For the images with an acquisition time of 2 minutes, the mean RMSE value for wave-CAIPI is $6.51 \pm 1.78$ and for Cartesian sampling, and the mean RMSE is $7.82 \pm 1.79$, in arbitrary signal intensity units. On average, RMSE values were $18.9\% \pm 13.2\%$ lower, and NMI values were $10.2\% \pm 7.3\%$ higher for the wave-CAIPI, compared with Cartesian sampling.

Figure 8A,B show 4D MR and PET/CT images of a patient with squamous cell carcinoma in the lung. The 3-minute wave-CAIPI 4D MRIs show superior image quality, compared with the 3-minute Cartesian acquisitions. No relevant respiratory motion-induced displacement of the tumor can be observed, as displayed in Figure 8C for the 3-minute wave-CAIPI MRI. As a result, in the process of radiotherapy...
treatment planning, the safety margins around the tumor do not need to be increased due to respiration.

The SNR ratio \( r_{\text{SNR}} = \frac{\text{SNR}_{\text{wave-CAIPI}}}{\text{SNR}_{\text{Cartesian}}} \) that was calculated in the phantom for the two trajectories is presented in Figure 9A, binned according to the Cartesian g-factor in the corresponding pixels. An exemplary slice of the median-filtered SNR ratio map is displayed in Figure 9B. The average SNR gain of wave-CAIPI was \( r_{\text{SNR}} = 1.14 \pm 0.31 \). Calculations of the g-factor (using the same set of replicas as for the SNR measurement) yielded an average g-factor of \( g_{\text{mean}} = 1.21 \) for wave-CAIPI in the phantom. In the Cartesian case, the average g-factor was \( g_{\text{mean}} = 1.34 \) in the phantom. g-Factor maps for a simulated 2-minute in vivo scan are presented in Figure 9C.
FIGURE 6  A-E, Box plots of the normalized mutual information (NMI) between accelerated images and their respective references for 5 volunteer examinations. The average is performed over the individual breathing states. Median NMI values of the wave-CAIPI are consistently above the Cartesian NMI values.
DISCUSSION

The results of the patient examination indicate that, using the wave-CAIPI sampling, the image quality of accelerated acquisitions can be enhanced while keeping the scan time constant. In the presented case, no relevant displacement of the tumor could be observed during respiration. An important application of the proposed method would be in the context of radiotherapy treatment planning. It is very important in radiotherapy not only to ensure tumor coverage with the prescribed dose but also to spare organs at risk (e.g., lung, liver, heart). For this purpose, safety margins around the tumors are used in the target volume definition process to guarantee coverage. If tumor motion is not considered at all, very large margins have to be used, resulting...
in a high probability of radiation-induced pneumonitis, for example.30 Different treatment planning concepts are used to create target volumes that are influenced differently by more extreme respiration states.30,31 Tumor delineation depends substantially on image quality. Consequently, accelerated images acquired with the wave-CAIPI sampling technique are superior over Cartesian ones. In the present case, safety margins around the tumor do not need to be increased due to respiratory motion. Moreover, the superior soft-tissue contrast compared with CT can lead to further dose reductions, especially for the identification of moving lesions in the pancreas, for example.32

The calculated normalized mutual information as a function of acquisition time is used as a quantitative measure to capture the similarity of the accelerated images to their respective references (initial full-duration scan; no retrospective scan-time reduction). For each breathing state, a series of images with decreasing acquisition time is generated and the NMI is calculated. The respiratory gating windows are fixed for all accelerated images, to ensure comparability of images with different acquisition times. Median NMI values of the wave-CAIPI scans lie consistently above those of the Cartesian scans, indicating a lower loss of image information due to acceleration. The scatterplots of RMSE and NMI in Figure 7 show that the accelerated wave-CAIPI images exhibit smaller discrepancies to the reference images compared with the Cartesian case. This is supported by phantom-based SNR ratio calculations. The SNR advantage of \( r_{SNR} = 1.14 \pm 0.31 \) for the wave-CAIPI approach leads to a more well-posed CG SENSE reconstruction, which reduces residual noise enhancement in the final images. In Figure 9A, the SNR ratio in the individual pixels of the phantom images are binned according to the Cartesian g-factor in the respective pixel. The SNR gain by using the wave-CAIPI is larger in regions where the Cartesian image exhibits a large g-factor. In the phantom, g-factor calculations of the used setup yielded average g-factors of \( g_{wave} = 1.21 \) for the wave-CAIPI, compared with \( g_{Cartesian} = 1.34 \) for the Cartesian imaging. The g-factor maps of the simulated 2-minute 4D-lung imaging.
which would further decrease the g-factor.\textsuperscript{10,33} Regarding
MR scanner would allow higher gradient wave amplitudes,
wave-CAIPI parameters. The slew-rate limits of the used
Further optimization potential of the present work lies in the
compared with
the readout direction always fully sampled. As a result, the
are involved in undersampling. In contrast, undersampling in
missing k-space samples, as all three dimensions in k-space
undersampling results in a more homogeneous distribution of
voids in k-space. Due to the helically shaped readout lines,
are visible in the accelerated Cartesian images, which compli-
cates vessel identification and delineation.
In Breuer et al,\textsuperscript{15} full coverage of the lung was achieved in
3 minutes, using a randomized, self-gated and density-
weighted Cartesian sequence. Calculations of the normal-
ized mutual information displayed in Figure 6 and the image
comparison in Figure 4 indicate that the image quality of a
3-minute Cartesian scan is comparable to the image quality
of a 2-minute wave-CAIPI scan. Thus, the benefit of using
the wave-CAIPI k-space trajectory can be traded for a re-
duced acquisition time or enhanced image quality, keeping
the scan time constant. Using the wave-CAIPI technique, the
SNR benefit could also be traded for higher temporal resolu-
tion of the respiratory cycle. Keeping the scan time constant,
a higher number of (independent) breathing states implies an
increased undersampling rate.
An interesting extension of the presented work would be
to play out phase-encoding steps according to the actual cur-
rent breathing state, as determined by the DC signal. Instead
of prospectively defining a suitable order of the phase-
encoding steps, the sampling patterns in each breathing state
could thereby be adjusted as desired. Such an approach would,
however, come at the expense of an unpredictable scan time.

5 | CONCLUSIONS

Quantitative image analysis, involving calculations of SNR,
normalized mutual information and RMSE, demonstrated an
enhanced image quality for the wave-CAIPI technique, com-
pared with the Cartesian sequence in free-breathing, self-gated
4D lung MRI. The combination of density weighting and the
wave-CAIPI k-space trajectory enables full coverage of the
human lung in eight breathing states in only a few minutes.

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CONFLICT OF INTEREST
J. A. J. Richter and M. Stich are now employees of Siemens
Healthcare, Erlangen, Germany. Their contribution to the
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Siemens Healthcare.

DATA AVAILABILITY STATEMENT
The source code for the iterative Conjugate Gradient SENSE
reconstruction is publicly available at https://github.com/
expRad/4d_lung. A volunteer 4D-lung MRI data set can
be downloaded from zenodo.org (https://doi.org/10.5281/
zenodo.3765168).
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