Nickel-Rich Outflows Produced by the Accretion-Induced Collapse of White Dwarfs: Lightcurves and Spectra

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ABSTRACT

The accretion-induced collapse (AIC) of a white dwarf to form a neutron star can leave behind a rotationally supported disk with mass of up to \( \sim 0.1 \, M_\odot \). The disk is initially composed of free nucleons but as it accretes and spreads to larger radii, the free nucleons recombine to form helium, releasing sufficient energy to unbind the remaining disk. Most of the ejected mass fuses to form \(^{56}\text{Ni}\) and other iron group elements. We present spherically symmetric radiative transfer calculations of the transient powered by the radioactive heating of this ejecta. We estimate the ejecta composition using nucleosynthesis calculations in the literature and explore the sensitivity of our results to uncertainties in the ejecta kinematics. For an ejecta mass of \( 10^{-2} \, M_\odot \left( 3 \times 10^{-3} \, M_\odot \right) \), the lightcurve peaks after \( \lesssim 1 \) day with a peak bolometric luminosity \( \gtrsim 2 \times 10^{41} \, \text{ergs} \, \text{s}^{-1} \) (\( \sim 5 \times 10^{40} \, \text{ergs} \, \text{s}^{-1} \)); the decay time is \( \sim 4 \) (2) days. Overall, the spectra redden with time reaching \( U - V \sim 4 \) after \( \sim 1 \) day; the optical colors (\( B - V \)) are, however, somewhat blue. Near the peak in the lightcurve, the spectra are dominated by Doppler broadened Nickel features, with no distinct spectral lines present. At \( \sim 3 - 5 \) days, strong Calcium lines are present in the infrared, although the Calcium mass fraction is only \( \sim 10^{-4.5} \). If rotationally supported disks are a common byproduct of AIC, current and upcoming transient surveys such as the Palomar Transient Factory should detect a few AIC per year for an AIC rate of \( \sim 10^{-2} \) of the Type Ia rate. We discuss ways of distinguishing AIC from other rapid, faint transients, including Ia’s and the ejecta from binary neutron star mergers.

Key words: supernovae – nucleosynthesis, abundances – accretion disks

1 INTRODUCTION

As an accreting white dwarf (WD) approaches the Chandrasekhar mass, it suffers one of two fates: (1) collapse to form a neutron star (NS) or (2) explosion as a Type Ia supernova (SN). Which of these end states is realized depends on the relative densities required for electron captures on Ne makes accretion-induced collapse (AIC) of a WD to a neutron star possible, and thus O-Ne WDs, rather than C-O WDs, preferentially undergo AIC (Nomoto 1984; Miyaji et al. 1980; Canal & Gutiérrez 1997 for a review). The composition of the WD is, however, a critical factor: the relatively low densities required for electron captures on Ne makes accretion-induced collapse (AIC) of a WD to a neutron star possible, and thus O-Ne WDs, rather than C-O WDs, preferentially undergo AIC (Nomoto 1984; Miyaji et al. 1980; Canal et al. 1994; Canal et al. 1993; Gutiérrez et al. 1996; Gutiérrez et al. 2005; Wann et al. 2006). AIC may result both from accretion following Roche-lobe overflow from a non-degenerate companion (the “single degenerate” AIC channel; e.g. Nomoto et al. 1979; Nomoto & Kondo 1991), as well following the merger of two WDs in a binary system (e.g. Yoon et al. 2007).

There is no direct observational evidence for AIC and so its rate remains uncertain. Numerical simulations of AIC find that it is accompanied by a weak explosion (\( \sim 3 \times 10^{49} \) ergs) that synthesizes only a very small amount of Ni (\( < 10^{-3} \, M_\odot \) in current models) (Woosley & Baron 1992; Dessart et al. 2006; Abdikamalov et al. 2014), unless there is a strong, large-scale magnetic field in the progenitor white dwarf (Dessart et al. 2007; Metzger et al. 2008). The neutrino-driven wind from the proto-neutron star does produce \( 3 \times 10^{-3} \, M_\odot \) of neutron-rich elements (specifically, matter with an electron fraction \( < 0.4 \); Dessart et al. 2006). The low total abundance of such elements in the galaxy implies an AIC rate of \( \lesssim 1\% \) of the Type Ia rate, if the calcu-
The radiative transfer calculations are motivated by the model presented in Metzger et al. (2009a). They argued that the observational signature of AIC can, in some circumstances, be dominated by the ejecta produced by an accretion disk around the newly formed neutron star, rather than by the weak SN that accompanies the AIC itself. To motivate our radiative transfer calculations, we first summarize Metzger et al. (2009a)'s calculation of the disk's evolution and nucleosynthesis (§2.1). We then describe our radiative transfer calculations (§2.2) and the composition and structure of the disk ejecta (§2.2.1). Our main results are presented in §3. We conclude by discussing the key properties of AIC, and comparing them to other predicted faint, rapid transients (§3).

1.1 Summary of the Model

Depending on the rotation profile of the WD prior to collapse, and in particular the degree of differential rotation (Saio & Nomoto 2004; Yoon & Langer 2004; Piran 2008), the neutron star formed during AIC is surrounded by a rotationally supported disk (Dessart et al. 2006, 2007; Abidakalbayev et al. 2010). For even modest differential rotation (that does not significantly change the Chandrasekhar mass), the disk mass is $M_D \sim 10^{-2} - 0.1 M_\odot$. However, if the WD is uniformly rotating, the disk mass is significantly lower, even if the WD is rotating near break-up (Abidakalbayev et al. 2010).

Most of the rotationally supported material is initially just outside the proto-neutron star at a radius of $R_D \sim 100$ km. The disk is born sufficiently hot that nuclei are dissociated into free nucleons and weak interaction processes have time to change the neutron to proton ratio. Under these conditions, the composition of the disk can be usefully described using the electron fraction

$$Y_e = \frac{n_p}{n_n + n_p}$$

where $n_p$ and $n_n$ are the proton and neutron densities, respectively. Weak interactions in the disk are dominated by the pair capture reactions

1. $e^+ + n \rightarrow \bar{\nu}_e + p$ $(2)$
2. $e^- + p \rightarrow \nu_e + n$ $(3)$

where the resulting neutrino emission is also the dominant coolant for the disk material because the photons are trapped and cannot escape on the timescales of interest. Although the disk is formed very hot, electron degeneracy suppresses the formation of electron/positron pairs. The resulting electron excess favors electron captures (eq. 3) over positron captures (eq. 2), thus driving the composition neutron rich (e.g. Pruet et al. 2003)

As the accretion onto the proto-neutron star, the remaining mass spreads to larger radii in order to conserve angular momentum. As the disk spreads, the temperature drops (for the majority of the mass) and thus the neutrino cooling and weak reactions become less efficient. When the bulk of the disk reaches $R_D \sim 1000$ km, the disk has cooled to $T \sim 10^{10}$K, and weak interactions freeze out (Metzger et al. 2009a). Absent a central neutron star — as is the case for analogous disks formed during binary neutron star mergers — weak interactions freeze out when the material is still quite neutron rich, with $Y_e \sim 0.2 - 0.4$. During AIC, however, the proto-neutron star emits copious neutrinos in the first few seconds after formation (Burrows & Lattimer 1983), which irradiate the disk as it spreads. Because the neutron star is depletonizing, electron neutrinos dominate the emission and the rate of neutrino captures $\nu_e + n \rightarrow p + e^-$ becomes comparable to the rate of pair captures (eqs. 2-3). For a significant fraction of the mass, this increases the electron fraction at freeze-out to $Y_e \gtrsim 0.5$.

As the disk continues to spread, the free nucleons in the disk recombine to form heavy nuclei once $T \sim \text{few} \times 10^9$ K. The formation of He alone releases $\sim 7$ MeV per nucleon, which is larger than the gravitational binding energy of the disk when fusion commences ($\sim 2$ MeV per nucleon). As a result, the disk is unbound, with its slow viscous spreading transformed into a supersonic outflow that reaches $v \sim 0.1$ c. The end state of the fusion that initiates the disk’s destruction is determined by the density, temperature, and electron fraction (the latter because weak interactions have frozen out); the parameters are such that the ejecta is nearly in nuclear statistical equilibrium (NSE). Since there are roughly equal numbers of protons and neutrons, a significant fraction of the unbound disk fuses to form $^{56}$Ni, the decay of which can power a supernova-like transient once the ejecta expands sufficiently that photons may diffuse out. In the remainder of this paper, we calculate the lightcurves and spectra of this transient.

2 ASSUMPTIONS & MODEL PARAMETERS

2.1 Radiative Transfer Calculations

We calculate lightcurves and spectra using the time-dependent radiative transfer code SEDONA, a detailed description of which can be found in Kasen et al. (2006). SEDONA solves the radiative transfer problem in a homologously expanding atmosphere described by a velocity-time
grid. We include the gamma ray energy emitted from the decay chain $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{58}\text{Fe}$ and evolve the composition accordingly. We modified SEDONA to treat $^{56}\text{Ni}$ as distinct, allowing us to include other Ni isotopes in the opacity without evolving their composition or including their decay energy. All line information is from Kurucz & Bell (1995).

SEDONA tracks the emitted gamma rays from radioactive decay and determines the resulting heating through Compton scattering and photoelectric absorption. The opacities are first calculated using the input density and composition, the calculated energy deposition, and an initial temperature guess. The dominant opacities are electron scattering and bound-bound line transitions. Our calculations assume local thermodynamic equilibrium (LTE), although SEDONA supports non-LTE opacity calculations as well. The source function for the lines is calculated in the two-level form of the Planck function, $B_{\lambda}$, through

$$S_{\lambda} = (1 - \varepsilon)J_{\lambda} + \varepsilon B_{\lambda} \quad (4)$$

where the degree of line scattering is encapsulated in the thermalization parameter, $\varepsilon$, which equals the ratio of absorption opacity to total opacity. We fixed $\varepsilon = 0.3$, motivated by the calculations of Kasen et al. (2006). Given the opacity and ionization states in LTE, the temperature profile is determined from the condition of radiative equilibrium, balancing the rate of thermal emission with the rate of photon absorption and radioactive energy deposition. The synthetic spectrum is determined using a Monte Carlo calculation. The spectrum and temperature profile are iterated on until the temperature structure converges. The final synthetic lightcurves and spectra are determined on the last iteration by recording the photons that escape the outflow. We set the velocity and time bin resolutions in our calculations to $200 \text{ km s}^{-1}$ and 0.1 day, respectively.

### 2.2 Outflow Properties

Although the outflows produced during AIC are likely to be asymmetric (albeit axisymmetric), we use a 1D spherically symmetric model to study the lightcurves and spectra. Given current uncertainties in the properties of the unbound accretion disk and the interaction between the disk and the AIC supernova, we believe that this approximation is a reasonable first step.

The bulk speed of the outflow is $\simeq 0.1 \text{ c}$, determined by the nuclear energy released as the disk is unbound. Given the likely order unity fluctuations about this fiducial speed, we set the density distribution of the homologously expanding outflow to be

$$\rho = \begin{cases} a e^{v/v_c} & \text{if } 0 < v < 0.05 \text{ c} \\ b v^{-\alpha} & \text{if } 0.05 \text{ c} \leq v < 0.2 \text{ c} \end{cases}$$

where $C$ parameterizes the density profile of the outflow. The constants $a$ and $b$, which in general are functions of time, are determined by continuity of density at $v = 0.05 \text{ c}$ and by fixing the total outflow mass, $M_{\text{tot}}$. The e-folding velocity, $v_c$, is included to ensure that there is not an artificially abrupt cutoff in the density at small velocity/radii (which can affect the photosphere at late times), but the exact value is not crucial; we take $v_c = 500 \text{ km s}^{-1}$. Equation (5) implies that the bulk of the mass in the outflow has $0.05c \lesssim v < 0.2c$. The precise value of the density power law index $C$ within this velocity range does not significantly affect the observational signatures of AIC. We will focus on $C = 4$ but we carried out calculations for $C = 2$ and 4, which covers the full range of possibilities, from most of the mass being at high velocity ($C = 2$) to most of the mass being at smaller velocity ($C = 4$). The lightcurves in the models with smaller C peak somewhat earlier ($\Delta t = 0.2 \text{ d}$ between $C = 2$ and $C = 4$) and fall more rapidly after the peak, as would be expected since more of the mass is at high velocity. Nonetheless, the peak bolometric luminosity remains nearly the same. The spectra at early times are relatively independent of $C$, but there are some differences at $t \gtrsim 3$ days when individual spectral features begin to become more prominent. We will highlight these differences below, but we focus on the case of $C = 4$.

| Table 1. Mass Fractions in the Three Fiducial Models. |
|---------------------------------------------|
| Element | $Y_{e}$ range | $Y_{e}$ range | $Y_{e}$ range |
| Ca      | $3.60 \times 10^{-5}$ | $4.55 \times 10^{-5}$ | $1.68 \times 10^{-5}$ |
| Sc      | $1.38 \times 10^{-5}$ | $1.99 \times 10^{-5}$ | $3.24 \times 10^{-6}$ |
| Ti      | $5.63 \times 10^{-5}$ | $2.55 \times 10^{-5}$ | $4.44 \times 10^{-5}$ |
| V       | $1.40 \times 10^{-5}$ | $1.77 \times 10^{-5}$ | $2.52 \times 10^{-5}$ |
| Cr      | $2.24 \times 10^{-3}$ | $1.16 \times 10^{-4}$ | $7.61 \times 10^{-5}$ |
| Fe      | $1.87 \times 10^{-2}$ | $1.12 \times 10^{-2}$ | $1.07 \times 10^{-2}$ |
| Co      | $2.95 \times 10^{-3}$ | $3.73 \times 10^{-3}$ | $1.76 \times 10^{-3}$ |
| Ni      | $8.59 \times 10^{-1}$ | $9.00 \times 10^{-1}$ | $9.87 \times 10^{-1}$ |
| Cu      | $5.03 \times 10^{-3}$ | $4.52 \times 10^{-3}$ | $2.21 \times 10^{-4}$ |
| Zn      | $1.03 \times 10^{-1}$ | $7.31 \times 10^{-2}$ | $5.90 \times 10^{-2}$ |
| Ga      | $1.42 \times 10^{-4}$ | $1.40 \times 10^{-4}$ | $0.00$ |
| Ge      | $3.86 \times 10^{-3}$ | $4.23 \times 10^{-3}$ | $0.00$ |
| As      | $5.60 \times 10^{-6}$ | $7.08 \times 10^{-6}$ | $0.00$ |
| Se      | $5.97 \times 10^{-4}$ | $5.42 \times 10^{-4}$ | $0.00$ |
| Rb      | $1.69 \times 10^{-4}$ | $1.25 \times 10^{-5}$ | $0.00$ |
| Sr      | $2.86 \times 10^{-3}$ | $1.12 \times 10^{-3}$ | $0.00$ |
| Y       | $1.84 \times 10^{-4}$ | $2.19 \times 10^{-4}$ | $0.00$ |
| Zr      | $9.46 \times 10^{-4}$ | $1.20 \times 10^{-3}$ | $0.00$ |
| Mo      | $3.40 \times 10^{-6}$ | $4.30 \times 10^{-6}$ | $0.00$ |

| Table 2. Mass Fraction of $^{56}\text{Ni}$ in the Three Fiducial Models. |
|---------------------------------------------|
| $X_{\text{Ni}}$ | $Y_{e}$ range | $Y_{e}$ range | $Y_{e}$ range |
|--------------|----------------|----------------|----------------|
| $X_{\text{Ni}}$ | $5.38 \times 10^{-1}$ | $6.49 \times 10^{-1}$ | $9.97 \times 10^{-1}$ |
\[ Y_e = 0.425 - 0.55 \] are the most realistic because the disk models in [Metzger et al. (2009b)] in general have a range of \( Y_e \) at different radii and times. However, the differences between these three different models give an indication of the systematic uncertainties in our predictions introduced by uncertainties in the outflow composition. Lacking a hydrodynamic calculation of the disk evolution and its transition to the ejecta phase, we take the composition of the ejecta to be uniform at all radii/velocities.

Given the electron fraction in the ejecta, we determined the composition of each model using the nucleosynthesis calculations of [Woosley & Hoffman (1992) and Seitenzahl et al. (2008)], averaging over the range of \( Y_e \) in our model, and using the solar system abundances from Arnett (1996) to determine absolute abundances. Table 1 summarizes the composition of each of the models and Table 2 gives the mass fraction of \( ^{56}\text{Ni} \) in each model. In determining the composition of our models, we used the calculations of Woosley & Hoffman (1992) and Seitenzahl et al. (2008) with thermodynamic properties most similar to AIC ejecta. Specifically, for \( 0.425 < Y_e < 0.5 \), we used the finite entropy abundances calculated from the \( \alpha \)-process with \( T = 10^{10} \text{K} \) and \( \rho = 2 \times 10^4 \text{g cm}^{-3} \) in Table 3 of Woosley & Hoffman (1992), corresponding to a mild \( \alpha \)-rich freeze-out. The entropy and expansion time scale used in these calculations are similar to those expected in the disk when \( \alpha \)-particles form and outflows begin. For \( 0.5 < Y_e \leq 0.55 \), we use the abundances calculated from NSE with \( T = 3.5 \times 10^9 \text{K} \) and \( \rho = 10^6 \text{g cm}^{-3} \) in Figure 3 of Seitenzahl et al. (2008). Because AIC outflows likely possess a moderate entropy \( \sim 3 - 10 \text{keV baryon}^{-1} \) [Metzger et al. (2009a)], and hence may undergo a mild \( \alpha \)-rich freeze-out, the pure NSE calculations in Seitenzahl et al. (2008) do not strictly apply. However, by extrapolating the results of full nucleosynthesis calculations by [Pruet et al. (2004)] to the relevant entropy regime, we find that the yield of \( ^{56}\text{Ni} \), the dominant isotope in this composition range, is well-approximated by its NSE abundance.

Since the nuclei are in their post-decay phase in Woosley & Hoffman (1992), we converted the entire fraction of \( ^{56}\text{Fe} \) to its parent \( ^{56}\text{Ni} \). Although some matter with \( Y_e < 0.425 \) may be present in AIC ejecta, we did not include in our models due to the uncertain and contradictory nucleosynthesis information in Seitenzahl et al. (2008) and Hartmann et al. (1985). We also did not include Br and Kr in our calculations due to lack of line information in Kurucz & Bell (1993). Finally, our calculations only include heating due to the decay of \( ^{56}\text{Ni} \), although other radioactive isotopes are produced and may contribute to the light curve. In particular, we find that \( ^{57}\text{Ni} \) (half-life \( \tau_{1/2} = 35.6 \text{ hr} \)) and \( ^{62}\text{Zn} \) (\( \tau_{1/2} = 9.2 \text{ hr} \)) produce specific heating rates that are a factor \( \sim 6 \) and \( \sim 12 \) times higher, respectively, than \( ^{56}\text{Ni} \) on timescales \( t \lesssim \tau_{1/2} \). However, in most cases the much lower mass fractions of these isotopes relative to \( ^{56}\text{Ni} \) implies that their contribution to the total heating is relatively minor. One exception is the mass fraction of \( ^{62}\text{Zn} \) in our \( Y_e = 0.425 - 0.55 \) model, which we estimate is only a factor \( \sim 4 \) less than \( ^{56}\text{Ni} \) and thus could contribute appreciably to the very early light curve.

As discussed in [Metzger et al. (2009b)] determined the mass of unbound disk material to be a few times \( 10^{-2} \text{M}_{\odot} \) using collapse calculations from Dessart et al. (2006, 2007), but the ejecta mass could be significantly lower if the WD is more uniformly rotating [Abdkalamov et al. (2010)]. We studied a range of total masses for the ejecta but focus on \( M_{\text{tot}} = 3 \times 10^{-3} \text{M}_{\odot} \) and \( M_{\text{tot}} = 10^{-2} \text{M}_{\odot} \) here because this is the range of masses for which the disk ejecta produces an observationally interesting luminosity. The lightcurves and spectra have similar behaviour for different total masses, simply shifted to somewhat earlier times and shorter wavelengths for lower total mass, as would be expected using analytic estimates based on Arnett’s law [Arnett (1982)].

3 RESULTS

Figure 1 shows the bolometric and R-band lightcurves produced by AIC ejecta for the three different compositions summarized in Tables 1 and 2, and for two different total masses. The lightcurve evolution is consistent with analytic expectations based on the competition between expansion and diffusion [Arnett (1982)]. The low mass and high speed of the ejecta imply that the rise time is extremely fast \( \sim \text{few days} \); the subsequent decay is somewhat slower, with the luminosity decaying significantly after \( \lesssim 4 - 5 \text{ days} \) for \( M_{\text{tot}} = 10^{-2} \text{M}_{\odot} \) and \( \gtrsim 2 - 3 \text{ days} \) for \( M_{\text{tot}} = 3 \times 10^{-3} \text{M}_{\odot} \). The peak bolometric luminosity is \( \sim 1 \times 10^{41} \text{ ergs s}^{-1} \) for \( M_{\text{tot}} = 10^{-2} \text{M}_{\odot} \) and a factor of \( \sim 3 \) lower for \( M_{\text{tot}} = 3 \times 10^{-3} \text{M}_{\odot} \). This is a factor of \( \sim 100 \) fainter than a typical Type Ia supernova, which is consistent with the much smaller Ni masses produced during AIC.

For a given total mass, Figure 4 shows that the models with smallest range in electron fraction \( (Y_e = 0.5 - 0.55) \) are the brightest and broadest. The dependence on the composition is, however, modest and is reasonably degenerate with a different total mass for the ejecta. This implies that the uncertainty in the detectability of AIC is due primarily to uncertainty in the total mass of the disk ejecta, not the composition of the material. The dependence on \( Y_e \) in Figure 4 arises because only matter with \( Y_e \gtrsim 0.48 \) produces significant Ni, which both powers the lightcurve and contributes to the opacity of the ejecta. Lower \( Y_e \) material ends up as higher Z elements which do not contribute to the radioactive heating (note that for even lower \( Y_e \gtrsim 0.1 - 0.3 \), the decay of neutron-rich ejecta can produce a heating rate similar to that of Ni [Metzger et al. 2010]).

The bumps in the AIC lightcurves in Figure 1 arise because only matter with \( Y_e \gtrsim 0.48 \) produces significant Ni, which both powers the lightcurve and contributes to the opacity of the ejecta. Lower \( Y_e \) material ends up as higher Z elements which do not contribute to the radioactive heating (note that for even lower \( Y_e \gtrsim 0.1 - 0.3 \), the decay of neutron-rich ejecta can produce a heating rate similar to that of Ni [Metzger et al. 2010]).

The bumps in the AIC lightcurves in Figure 1 have the same physical cause as those seen in some Type Ia SNe (see Pinto & Eastman 2000 and Kasen 2003 for a discussion of the latter). As the ejecta expands, the matter cools, and ions begin to recombine. Singly ionized ions have a greater number of lines in the optical and infrared part of the spectrum, and are therefore more efficient at fluorescing photons from bluer to redder wavelengths. Because the ejecta is more transparent at redder wavelengths, this redistribution effect allows the radiation energy stored in the ejecta to escape more rapidly, leading to a rise in the bolometric light curve.

Figure 2 shows the U-B, B-V, B-J, and R-I colors as a function of time for the \( M_{\text{tot}} = 10^{-2} \text{M}_{\odot} \) models from Figure 1. We define the colors here using the ratio of the luminosities \( \lambda_i \) at the centers of the appropriate bands, with \( \lambda_U = 3611 \AA, \lambda_B = 4611 \AA, \lambda_V = 5851 \AA, \lambda_R = 7011 \AA, \lambda_I = 8111 \AA, \) and \( \lambda_J = 12351 \AA \). Figure 2 shows that AIC is predicted to become increasingly red in the first
The Lightcurves and Spectra of AIC

Figure 1. Predicted bolometric and R-band lightcurves of AIC transients, calculated for different values of the total ejected mass $M_{\text{tot}}$. The R-band center was taken as $\lambda_R = 7011$ Å. Thick and thin lines correspond to $M_{\text{tot}} = 10^{-2}M_\odot$ and $3 \times 10^{-3}M_\odot$, respectively. Different linestyles correspond to different ejecta compositions, specifically different assumptions about the range of electron fraction in the ejecta (see Tables 1 and 2).

\[ Y_e : 0.425 - 0.55 \]
\[ Y_e : 0.45 - 0.55 \]
\[ Y_e : 0.5 - 0.55 \]

(a) Bolometric Lightcurves

(b) R-Band Lightcurves

\[ M_{\text{tot}} = 10^{-2}M_\odot \]
\[ M_{\text{tot}} = 3 \times 10^{-3}M_\odot \]

The spectra at 1 day and 5 days are shown in Figure 3 for the $M_{\text{tot}} = 10^{-2}M_\odot$ models. Near the peak of the lightcurve (\( \sim 1-3 \) days), the emission peaks at \( \sim 3000-6000 \) Å and is reasonably red, consistent with Figure 2. At 1 day, individual spectral features are not discernible: given the high speeds, the lines have Doppler broadened and merged. Spectral lines do become more apparent at later times. In particular, at \( \sim 3 - 5 \) days the calcium triplet at \( \sim 9000 \) Å produces a luminosity comparable to the total luminosity of the ejecta, despite the fact that the mass fraction of Ca is \( \sim 3 \times 10^{-5} \). This is the most prominent individual spectral feature seen in any of our calculations, although we note that the actual strength of the Ca II line may be somewhat overestimated due to our LTE assumption. The spectra are generally Ni dominated but Doppler broadening makes it very difficult to identify individual spectral features. Although the results in Figure 3 are for $M_{\text{tot}} = 10^{-2}M_\odot$ and $\rho \propto v^{-4}$ in equation (6), the general conclusions about the spectra of AIC drawn here are reasonably robust and also apply to the other calculations we have carried out. In particular, the lower mass models with $M_{\text{tot}} = 3 \times 10^{-3}M_\odot$ have similar spectra at day 1. Models with different density profiles have similar spectra at day 1, but steeper velocity profiles (larger C) retain the Ca II triplet line and the peak at \( \sim 5000 \) Å to later times, simply because more mass is concentrated at lower velocities.

Our predicted color evolution may be sensitive to non-LTE effects. In particular, the red colors are primarily due to the fact that in these models a significant fraction of the mass is in iron and nickel even at the highest velocities. The outer layers of the ejecta are cooler, and in a lower ionization state, and so they very strongly blanket the bluer wavelengths. Non-thermal ionization from the decay products of $^{56}$Ni could in principle keep the outer layers of the ejecta more ionized. This would reduce the degree of line blanketing in the blue part of the spectrum (and the fluorescence to redder wavelengths) leading to an overall less red spectrum. This possibility will be studied in future work.

The predicted bolometric and R-band lightcurves of AIC transients, calculated for different values of the total ejected mass $M_{\text{tot}}$. Different linestyles correspond to different ejecta compositions, specifically different assumptions about the range of electron fraction in the ejecta (see Tables 1 and 2).
Figure 2. U-B, B-V, B-J, and R-I color evolution for the model with ejecta mass $M_{\text{tot}} = 10^{-2} M_{\odot}$. The models with the wider range of electron fraction are, we believe, more physical ($Y_e = 0.425 - 0.55$ and $Y_e = 0.45 - 0.55$); see text. These initially become redder with time in U-B, with little evolution after a few days. The spectra at 1 and 5 days are shown in Figure 3. The colors are defined using the ratio of the luminosities $\lambda L_{\lambda}$ at the following wavelengths: $\lambda_U = 3611$ Å, $\lambda_B = 4611$ Å, $\lambda_V = 5851$ Å, $\lambda_R = 7011$ Å, $\lambda_I = 8111$ Å, and $\lambda_J = 12351$ Å (chosen to match the wavelength bins used in the radiative transfer calculation).

4 DISCUSSION

Although the theoretical possibility of AIC has been recognized for decades (Canal & Schatzman 1976; Nomoto et al. 1979), only recently have transient surveys had sufficient depth, field of view, and cadence to potentially detect and characterize these events. The identification of AIC, or the ability to place meaningful constraints on its rate, would have important implications for a variety of astrophysical problems, including degenerate binary evolution, the progenitors of Type Ia SNe, and the formation channels of globular cluster NSs (Grindlay 1987). low mass X-
ray binaries (van den Heuvel 1984), and millisecond pulsars (Grindlay & Bailyn 1988).

Because AIC transients are powered by the decay of $^{56}\text{Ni}$, they have many qualitative similarities to Type Ia SNe. Although the observed lightcurves are too dim to perform cosmology, characterizing the correlation between peak luminosity and decay timescale (i.e., the Phillips 1993 relation) for AIC would be useful for observationally identifying these events. For example, the duration and peak luminosity of AIC transients increases with the ejecta mass, which probably increases in proportion to the initial mass of the accretion disk (Metzger et al. 2009b). The disk mass, in turn, is set by the angular momentum and rotational profile of the WD prior to collapse (Dessart et al. 2006; Abdikamalov et al. 2010), which also determines whether AIC is expected to be a powerful source of gravitational waves (Ott 2009). Everything else being equal, more luminous AIC transients are thus more likely to be accompanied by a detectable gravitational wave, making AIC transients a promising electromagnetic counterpart to events detected with ground-based interferometers such as Advanced LIGO.

We now briefly address the prospects for the “blind” detection of AIC with current and future transient surveys. Although the rate of AIC is uncertain, the amount of rare elements produced by the neutron-rich SN ejecta constrains the rate $R_{\text{AIC}}$ to be $\lesssim 10^{-4}$ yr$^{-1}$ per Milky Way-type galaxy (or $\lesssim 10^{-2}$ of the SN Ia rate) if the AIC calculations of Dessart et al. (2006) are representative. Assuming that the AIC rate is proportional to the blue stellar luminosity (Kopparapu et al. 2008), a Galactic rate of $R_{\text{AIC}} = 10^{-4}$ R$_{-4}$ yr$^{-1}$ corresponds to a volumetric rate of $10^{-6}$R$_{-4}$ Mpc$^{-3}$ yr$^{-1}$. For an ejecta mass of $M_{\text{ej}} = 10^{-2}$M$_{\odot}$, we find that AIC results in an optical transient with a peak luminosity $L_{\text{peak}} = 10^{41}$ ergs s$^{-1}$ (Fig. 4). The resulting luminosity distance is $600(400)[100]L_{41}^{1/2}$ Mpc for a magnitude limit of 25(24)[21], where $L_{41} = L_{\text{peak}}/10^{41}$ ergs s$^{-1}$. The PanSTARRs Medium Deep Survey (MDS; Kaiser et al. 2002), which covers $\sim 84$ deg$^2$ in $g$ and $r$ down to AB magnitude $\sim 25$, should thus detect $\sim 2L_{41}^{3/2}$ R$_{-4}$ AIC transients per yr. The 5-day cadence survey of the Palomar Transient Factory (PTF; Law et al. 2009), which surveys an active area $\sim 2700$ deg$^2$ to a limiting AB magnitude of 21, will detect $0.3L_{41}^{3/2}$ R$_{-4}$ yr$^{-1}$. Thus, for $R_{\text{AIC}} \sim 10^{-4}$ yr$^{-1}$ and $L_{41}$ few we conclude that MDS and PTF should detect $\sim 1 - 3$ AIC per year. As we discuss below, identifying AIC transients for follow-up observations will be challenging, so these estimates are probably optimistic and motivate faster cadence surveys such as the Palomar P60-FasTING survey (Kasliwal et al. 2011). Prospects for detection are better with the Large Synoptic Survey Telescope (LSST: Strauss et al. 2010), which will image the entire sky down to a limiting magnitude $\sim 24.5$ every 3–4 nights and should detect AIC events at a rate $\sim 10^3 L_{41}^{3/2}$ R$_{-4}$ yr$^{-1}$. Unfortunately, the fraction of AIC that have ejecta masses of $\sim 10^{-2}$M$_{\odot}$, and thus peak luminosities of $L_{\text{peak}} = 10^{41}$ ergs s$^{-1}$, is very difficult to predict given uncertainties in the differential rotation of the progenitor WD. Absent additional theoretical progress, it will thus not be easy to turn upper limits from transient surveys into constraints on the rate of AIC.

Although the prospects for upcoming transient surveys will detect AIC are promising, their identification will be challenging due to the deluge of other transients that will be discovered (and, indeed, are already being discovered). Other thermal transients predicted to occur on $\lesssim$ few day timescales include the failed deflagrations of C/O WDs (Livne et al. 2003), “Ia” SNe due to unstable thermonuclear He flashes from WD binaries (Bildsten et al. 2007; Shen et al. 2010), shock breakout from Type 1a supernova (Piro et al. 2010), and radioactively-powered transients from NS mergers (Metzger et al. 2010). Although NS mergers and other WD-related explosions may originate from a similar stellar population as AIC, a defining characteristic of AIC is that the majority of the ejected material is processed through NSE. This means that few low or intermediate-mass elements are likely to be pro-

Figure 3. Spectra for the model with ejecta mass $M_{\text{tot}} = 10^{-2}$M$_{\odot}$. At early times the spectra are dominated by Doppler-broadened Nickel features, with no individual spectral features identifiable. At 5 days, however, the Ca triplet at 9000 Å is quite prominent. This line is generally present at late times (\(\approx 2 - 5\) days) in all of our models.
duced (such as He, O, C, and Ti), in contrast to what is expected from Ia's or the failed detonation of a WD. We note, however, that trace amounts of Ca and Ti are produced in some of our models (see Table 1), which still may produce strong lines despite their low abundances (e.g. the Ca triplet at $\sim 9000$ Å; Fig. 2). A perhaps more dramatic difference between AIC transients produced by a disk around the newly formed NS and other WD-related events are the large outflow speeds $\sim 0.1c$ in AIC, which leads to highly velocity-broadened lines.

The speed of the ejecta from NS mergers, as in AIC, is expected to be large. A distinguishing feature in this case, however, is that NS merger ejecta is more neutron-rich than AIC ejecta, because in AIC the accretion disk material that ultimately becomes unbound is first irradiated by electron neutrinos from the proto-neutron star (Metzger et al. 2009b). Although the current line data for the $r$-process nuclei produced in NS merger ejecta is insufficient to make concrete spectroscopic predictions, it is safe to say that NS mergers are unlikely to resemble any spectral class of SNe yet detected. AIC and NS merger transients may also be distinguished by their light curve evolution. In Figure 3 we compare the bolometric light curves from AIC (this paper) and NS mergers (from Metzger et al. 2010) assuming a ejecta mass $M_\odot = 10^{-2} M_\odot$ in both cases. Although the overall brightness and late-time evolution is similar, the NS merger light curve shows an earlier, more pronounced peak. This difference results from the different radioactive heating rate in the two cases. AIC transients are powered by the decay of $^{56}$Ni, which produces an approximately constant heating rate prior to the $^{56}$Ni half-life $\sim 6$ days. NS merger transients, by contrast, are powered by a large number of decaying nuclei with a wide distribution of half-lives, resulting in a total heating rate that decreases approximately as a power-law $E \propto t^{-1.2-1.4}$. NS merger transients peak earlier simply because the radioactive heating is concentrated at early times. Distinguishing between NS mergers and AIC based on light curve evolution alone would thus probably require catching the event prior to maximum.

Several sub-luminous, rapidly-evolving Type I supernovae have recently been discovered, which could in principle be related to AIC. These include SN 2008ha (Valenti et al. 2009; Foley et al. 2009; Foley et al. 2010), 2005E (Perets et al. 2009), and 2002bj (Poznanski et al. 2010). In all of these events, the low $^{56}$Ni masses inferred from their peak luminosities ($\sim 10^{-3} - 0.1M_\odot$) are largely consistent with the quantity predicted from AIC. However, the presence of low and intermediate mass elements (e.g. Ca, C, O, He) in the spectra of these events with relatively low velocities ($\sim 200 - 10000$ km s$^{-1}$) rules out the standard Ni-rich AIC scenario outlined in this paper.

As discussed by Metzger et al. (2009b), the timescale, velocity, and composition of the AIC transient can be modified if a substantial quantity of WD material remains at large radii following AIC, either because the WD is still collapsing or because some matter remains centrifugally supported in a remnant disk created by a super-$M_\odot$, WD-WD merger (e.g. Yoon et al. 2007). In the latter case, depending on the mass and composition of the WDs, up to $\sim 0.1M_\odot$ in C, O, Ne, or He could remain at a radius $\sim 10^9$ cm. Once the SN explosion or Ni disk wind impacts the remnant material, it will (1) shock heat the material to a few times $10^8$ K, which may synthesize intermediate mass elements but will not disassociate the Ni and will leave some unburned WD material; (2) slow the ejecta from $v \sim 0.1c$ to a few thousand km s$^{-1}$. A combination of slower ejecta and higher opacity would lengthen the duration of the light curve, making such an event easier to detect. Such an “enshrouded AIC” scenario may therefore still be capable of explaining events such as SN 2008ha, 2005E, and 2002bj. In order to make a quantitative comparison to observations, however, hydrodynamic simulations will be required to determine the dynamics and nucleosynthetic yield of the complex interaction between the prompt SN, the Ni-rich disk wind, and the remnant WD material. Moreover, the timescale of AIC relative to the WD-WD merger itself is uncertain; any significant delay would likely lead to less debris at large radii and a “cleaner” event analogous to that calculated in this paper.

On this note it is also important to distinguish between AIC due to accretion from a binary companion, as considered in this paper, and electron-capture supernova in AGB stars with O-Ne-Mg cores (for recent work, see Kitaura et al. 2006; Wanajo et al. 2009). Although the collapse mechanism in these two cases is similar, an important difference in the AGB case is the presence of an extended hydrogen envelope. This additional overlying material both increases the $^{56}$Ni yield of the explosion and extends the duration of the supernova due to its larger opacity (Wanajo et al. 2009). Although the lack of hydrogen in the spectra of SNe 2008ha, 2005E, and 2002bj rules out electron capture SNe in these events, electron capture events may explain slower evolving sub-luminous SN such as 2008S (e.g. Prieto et al. 2008; Thompson et al. 2009; Pumo et al. 2009).

Our calculations could be improved in a number of ways. In particular, future work will require more realistic

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**Figure 4.** Comparison of the bolometric light curves of the transients from AIC (this paper) and NS mergers (Metzger et al. 2010). Both models were calculated for a total ejecta mass of $M_{\text{ej}} = 10^{-2} M_\odot$. The NS-NS merger transient is produced by the decay of a large number of neutron-rich nuclei created by $r$-process nucleosynthesis in the ejecta; Metzger et al. 2010 estimated a thermalization efficiency of $\epsilon_{\text{therm}} \sim 0.5$ for these decays. This figure highlights that distinguishing NS merger and AIC transients using lightcurve evolution alone will likely require early-time observations at $\lesssim 1$ day.
multi-dimensional models in which the composition is calculated from a hydrodynamic simulation of the disk evolution beginning with free nucleons. This is important for determining the final composition as a function of radius, which in turn can influence the spectroscopic predictions.

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