Composition Optimization, High-temperature Stability and Thermal Cycling Performance of Sc-doped Gd2Zr2O7 Thermal Barrier Coatings: Theoretical and Experimental Studies

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Composition optimization, high-temperature stability and thermal cycling performance of Sc-doped Gd$_2$Zr$_2$O$_7$ thermal barrier coatings: theoretical and experimental studies

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Abstract

Sc was doped into Gd$_2$Zr$_2$O$_7$ for expanding the potential for thermal barrier coating (TBC) applications. According to first-principles calculation, the solid solution mechanism of Sc in Gd$_2$Zr$_2$O$_7$ lattice was revealed, i.e., Sc first occupies the lattice interstitial sites followed by substituting for Gd, and the interstitial Sc concentration is less than 11.11%. By considering the mechanical and thermophysical properties comprehensively, the optimum Sc doping content was determined to be 16.67%, and this composition was selected to produce TBCs by air plasma spraying with YSZ as a bottom ceramic coating (Gd-Sc/YSZ TBC). After sintering at 1400 °C for 100 h, Gd-Sc coatings remain phase and structural stability indicative of excellent sintering resistance. By thermal cycling tests, Gd-Sc TBCs fails due to the low toughness and the interface reaction between Gd-Sc and bonding coatings, while Gd-Sc/YSZ TBCs exhibit
much longer thermal cycling lifetime, and the failure mode is YSZ coating cracking.

**Keyword:** Thermal barrier coatings; First-principles calculation; Solid solution mechanism; High-temperature stability; Thermal cycling.

1. **Introduction**

Thermal barrier coating (TBC) is a kind of high temperature protective coating used for aero turbine engine blades, prolonging blade working lifetime, improving thrust weight ratio and thermal efficiency [1-3]. TBCs are generally composed of a ceramic top coating, thermally grown oxide (TGO), bond coating and superalloy substrate. The ceramic top coating generally has the properties of low thermal conductivity, high chemical stability and thermal expansion coefficient (TEC) to meet the requirements of reducing the surface temperature of the substrate and reducing the thermal stress between the substrate and the adhesive layer [4-5]. The traditional ceramic top coating material is Y₂O₃ partially stabilized ZrO₂ (YSZ), which has good thermal and mechanical properties [6-8]. However, a transition from metastable tetragonal phase (t') to monoclinic phase (m) occurs when YSZ is in long-term service above 1200 °C, which is often accompanied by volume expansion, resulting in coating spallation; in addition, YSZ has sintering shrinkage and other problems during long-term service, which greatly reduces the thermal insulation performance of the coating [4, 9-10].

In recent years, rare earth zirconate (RE₂Zr₂O₇, RE = rare earth element) have been
widely concerned by many scholars. Because of their low thermal conductivity, high TEC and good phase stability, they are a series of good candidates for TBC applications. Among the rare earth zirconates, Gd$_2$Zr$_2$O$_7$ has the lowest thermal conductivity and the highest TEC, so it is regarded as one of the most promising thermal barrier coating materials [11]. In addition, Gd$_2$Zr$_2$O$_7$ has low oxygen permeability and structural stability at higher temperature [12]. However, the mechanical properties and toughness of Gd$_2$Zr$_2$O$_7$ are poor, which limits its application.

Gd$_2$Zr$_2$O$_7$ has two crystal structures, namely pyrochlore structure and defect fluorite structure, both of which are face centered cubic space lattice [13-14]. Gd$^{3+}$ and Zr$^{4+}$ lattice sites can be replaced by other ions, and some small ions could also enter the interstitial sites. Therefore, the thermal conductivity of Gd$_2$Zr$_2$O$_7$ can be further reduced by selectively doping other ions in a single Gd$_2$Zr$_2$O$_7$, which makes it possible to improve its thermophysical properties and mechanical properties. It is reported that the TEC of RE$_2$Zr$_2$O$_7$ increases with the decrease of RE$^{3+}$ (rare earth) size [15]. Zhang [16] et al. found that the fracture toughness of Gd$_2$Zr$_2$O$_7$ can be increased by doping Yb$^{3+}$. Lee [17] et al. found that the Y$^{3+}$ can significantly improve mechanical properties and insulation performance in Gd$_2$Zr$_2$O$_7$. These results show that doping small RE$^{3+}$ in GZO is beneficial to improve mechanical properties and thermophysical properties. Among the RE$^{3+}$, Sc has the smallest atomic radius [18]. Our previous research results show that Sc$^{3+}$ can increase the fracture toughness and TEC of Gd$_2$Zr$_2$O$_7$ [19]. However, in previous studies, the doping amount of Sc was not optimized, and the solid solution
mechanism of Sc in GZO lattice was not clarified theoretically.

Thermal shock resistance behavior, sintering resistance and phase stability of TBCs at high temperature are of great theoretical significance for the optimization design of aeroengine. Rare earth zirconate coating is resistant to sintering at high temperature, and is not easy to undergo phase transformation, but its fracture toughness and thermal expansion coefficient are relatively low, which will lead to poor thermal shock lifetime. M. Karabas [20] found that the thermal cycle life of La$_2$Zr$_2$O$_7$ can be improved by doping rare earth elements. Guo [21] et al. studied the high temperature stability and thermal shock resistance of (Gd$_{0.9}$Yb$_{0.1}$)$_2$Zr$_2$O$_7$, and found that (Gd$_{0.9}$Yb$_{0.1}$)$_2$Zr$_2$O$_7$ can still maintain good phase stability at 1600 °C, and the thermal cycle life is more than 3700 times. Other studies have shown that the design of double-ceramic-layer (DCL) TBCs structure can also improve the thermal shock lifetime, and YSZ coating can effectively mitigate the thermal shock effect [22-24]. According to the above report, rare earth zirconate materials have good phase stability at high temperature, and the thermal shock resistance can be improved by doping rare earth elements.

The first-principles calculation method based on density functional theory has developed into an important method to predict the properties of materials in recent years, and has been used by many scholars to study the effect of rare-earth doping on the properties of rare earth zirconate. Li [25] et al. found by first-principles calculation that doping Sm$^{3+}$ in La$_2$Zr$_2$O$_7$ could improve the mechanical and thermal properties, and
LaSmZr$_2$O$_7$ has the optimal mechanical and thermal properties when the doping rate is 50%. Zhao [26] et al. used density functional theory and found that the Young’s modulus, Debye temperature and thermal conductivity of Gd$_2$Zr$_2$O$_7$ decrease with the Th content. Xiao [27] et al. used first-principles calculation method and found that the Young's modulus of Gd$_2$Zr$_2$O$_7$ decreases by 22.2-59.9 GPa with the Ce content, and the thermal conductivity decreases by 21% after completely replacing Ce at Zr site.

Sc has been proved to be a very effective dopant, which can significantly improve the mechanical and thermal properties of Gd$_2$Zr$_2$O$_7$, but the solution mechanism and the optimal doping amount are still unclear. For TBC applications, its thermal shock and sintering behavior need to be investigated. Therefore, this study intends to clarify the solution mechanism of Sc doped Gd$_2$Zr$_2$O$_7$ by first-principles method and optimize the doping amount of Sc through the change of mechanical and thermophysical properties, and investigate its thermal shock resistance behavior and sintering behavior under long-term heat treatment conditions.

2. Theoretical calculation methods and experimental procedure

2.1 Theoretical calculation method

The theoretical calculations were carried out by the Vienna Ab initio Simulation Package (VASP) software based on density functional theory (DFT) [28]. The projector augmented wave (PAW) method was used to describe the interaction between electrons and ions, and the generalized gradient approximation (GGA) was used to describe the
electron exchange correlation potential [29, 30]. In all calculations, the plane wave cutoff energy was set to 500 eV and the k point is 3×3×3. The convergence criterion of structural optimization was that the stress of each atom was less than 0.01 eV/atom. In this work, Gd$_2$Zr$_2$O$_7$ pyrochlore structure was first established, and then several possible models of Sc doped Gd$_2$Zr$_2$O$_7$ solid solution was examined. For the strong interactions caused by the 4f electrons of Gd, we did not adopt the Hubbard U correction method, but as the core states, because 4f electrons do not affect the calculated results of mechanical and thermodynamic properties [31, 32].

In order to elucidate the solid solution mechanism of Sc atom in Gd$_2$Zr$_2$O$_7$ lattice, the defect formation energies of different doping models were calculated based on the following equation:

$$E_f=E_{\text{tot}}[\text{defect}]-E_{\text{bulk}}[\text{perfect}]-\sum_n n_i \mu_i$$  \hspace{1cm} (1)

where $E_{\text{tot}}[\text{defect}]$ is the energy of the crystal after doping, $E_{\text{bulk}}[\text{perfect}]$ is the energy of an undoped perfect crystal, $n_i$ is the number of doping atoms i, and if this atom is added to the system, $n>0$, if this atom is removed from the system, $n<0$; and $\mu$ is the chemical potential of the corresponding atom.

After calculating the mechanical property parameters, the thermophysical properties were obtained, including longitudinal sound velocity $v_l$, transverse sound velocity $v_t$, average sound velocity $v_m$, Debye temperature $\Theta$ and minimum thermal conductivity $k_{\text{min}}$. The formulas used are as follows:
\[ v_l = \sqrt{\frac{B + \frac{4}{3} G}{\rho}} \]  \hspace{1cm} (2)
\[ v_t = \sqrt{\frac{G}{\rho}} \]  \hspace{1cm} (3)
\[ v_m = \left[ \frac{1}{3} \left( \frac{2}{v_l} + \frac{1}{v_t} \right) \right]^{\frac{1}{3}} \]  \hspace{1cm} (4)
\[ \Theta = \frac{h}{k_B} \left[ \frac{3n}{4\pi} \left( \frac{N_A}{M} \right) \right]^{\frac{1}{3}} v_m \]  \hspace{1cm} (5)

The minimum thermal conductivity is calculated by Clarke's model and Cahill's model respectively, with the following formulas:

\[ k_{\text{min}}^{\text{Clarke}} = 0.87k_B M_a \left[ \frac{1}{3} E^2 \rho^6 \right] \]  \hspace{1cm} (6)
\[ k_{\text{min}}^{\text{Cahill}} = \frac{k_B}{2.48} \left( \frac{n}{V_m} \right)^{\frac{2}{3}} (v_l + 2v_t) \]  \hspace{1cm} (7)

Where B is bulk modulus, G is shear modulus, E is Young's modulus, \( \rho \) is density, \( n \) is the number of atoms in the crystal, \( V_m \) is the volume of unit cell, \( h \) is Planck constant, \( N_A \) is Avogadro constant, \( k_B \) is Boltzmann constant, \( M \) is Molar mass, and \( M_a \) is the average mass per atom.

2.2 Experimental procedure

Sc-doped Gd\(_2\)Zr\(_2\)O\(_7\) (Gd-Sc) powders were prepared by a chemical precipitation and calcination method [33, 34]. Firstly, Gd\(_2\)O\(_3\) and Sc\(_2\)O\(_3\) were dissolved into excessive concentrated nitric acid to obtain Gd(NO\(_3\))\(_3\) and Sc(NO\(_3\))\(_3\), and ZrOCl\(_2\)·8H\(_2\)O was dissolved in deionized water. Then the solutions were mixed evenly and slowly into excessive ammonia water with mechanically stirring and ultrasonic oscillated to obtain white precipitation, which was filtered and washed several times with deionized water and anhydrous ethanol until PH 7 was reached. The obtained powders were dried at 120 °C for 10 h and calcined at 900 °C for 5 h for crystallization.
Gd-Sc coating and Gd-Sc/YSZ double-ceramic-layer coating (DCL) TBCs were produced by air plasma spraying (APS), and the bond coating and the substrate were NiCoCrAlY and Ni-based superalloy, respectively. Gd-Sc and YSZ powders were agglomerated into microscopic particles by a spray drying method before spraying. When preparing double layer coating, YSZ coating was first sprayed on the bond coating, followed by the Gd-Sc coating.

Thermal shock tests were conducted by a water quenching method. When the temperature of the furnace was reached 1050 °C, Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs were put into the furnace and held for 10 minutes, followed by putting it into deionized water to room temperature. This process was defined as a thermal cycle and the termination condition was that the spallation area of the coating surface exceeds 20%. The sintering behavior of Gd-Sc coatings were investigated at 1400 °C in a furnace (SK-G08163, China) for 20h, 50h, 100h and 200h.

Phase compositions were determined by a D8 Advance Bruker diffractometer using Cu Kα radiation, the parameters were as follows: the voltage and current was 40 kV and 40 mA, and the scanning range of 2θ was 20°–80° with a rate of 6 °/min. The high temperature stability of Gd-Sc powders was examined by STA449C thermal analyzer, with the parameters as follows: the heating rate is 10 °C/min and the temperature range is from room temperature to 1450 °C. The surface morphologies, cross-sectional
microstructure and composition analysis were observed by scanning electron microscope (SEM; Nanosem 430, FEI, USA) equipped with energy dispersive spectroscopy (EDS, IE 350).

3. Results and discussion

3.1 Structural properties of Gd$_2$Zr$_2$O$_7$

The optimized Gd$_2$Zr$_2$O$_7$ model is shown in Fig. 1. The structure exhibits a typical pyrochlore structure with 16 Gd, 16 Zr and 56 O atoms. In the lattice, Gd occupies 16d (0.5, 0.5, 0.5), Zr occupies 16c (0, 0, 0), and the O has two types of sites, i.e., 48f (x, 0.125, 0.125) and 8b (0.375, 0.375, 0.375). In addition, there is an unoccupied oxygen vacancy of 8a (0.125, 0.125, 0.125) in Gd$_2$Zr$_2$O$_7$ lattice.

The two most important parameters for describing the structure of pyrochlore are the lattice constant $a_0$ and the atomic coordinate parameter $x_{O-48f}$. The $x_{O-48f}$ is an important parameter for the degree of structural disorder, with a value between 0.3125 and 0.375 [33]. When $x=0.3125$, it is an ideal pyrochlore structure, while when $x=0.375$, the system exhibits a disordered fluorite structure, that is, a larger value of $x_{O-48f}$ means a more disordered lattice structure [36]. After completing structural relaxation, the results of $a_0$, $x_{O-48f}$ and density of the Gd$_2$Zr$_2$O$_7$ model are obtained as shown in Table 1, which are 10.600 Å, 0.3386 and 6.79 g/cm$^3$, respectively, showing agreement with the published values [37-40]. The above part demonstrates the reliability of our calculation results.
3.2 Solid solution mechanism of Sc-doped Gd$_2$Zr$_2$O$_7$

In Gd$_2$Zr$_2$O$_7$ lattice, the doped Sc has two possible sites, i.e., interstitial site and substitution for Gd. In order to determine the solid solution mechanism of Sc in the lattice, we established models with one Sc atom, two atoms, three atoms and four atoms, which were named GdSc-1-inter and GdSc-1-sub, GdSc-2-inter and GdSc-2-inter+sub, GdSc-3-inter and GdSc-3-2-inter+1-sub, and GdSc-4-2-inter+2-sub, respectively, as listed in Table 2 and shown in Fig. 2. The subscripts of inter and sub stand for a Sc atom occupying an interstitial site and substituting for Gd, respectively. The interstitial sites are 32e (0.25,0.25,0.25), which is the most stable interstitial site in pyrochlore structure [41]. The Gd site farthest from the 32e is selected as the substitution site.

Defect formation energy is an important parameter to determine the mechanism of point defect formation. The smaller the value, the easier the doped atom can enter the lattice. The calculated formation energy values of above models are shown in Table 2. According to the calculation results, the solution mechanisms of Sc atoms in the Gd$_2$Zr$_2$O$_7$ lattice are analyzed as follows: one Sc atom is easier to enter the interstitial site of the lattice, because the formation energy of GdSc-1-inter (0.141) is obviously smaller than that of GdSc-1-sub (1.269), which is also consistent with our previous experimental results [17]. It is found that the formation energy of GdSc-2-inter is slightly lower than that of GdSc-2-inter+sub, which indicates that the lattice may accommodate two interstitial Sc atoms but the second atom has some tendency to substitute for Gd. However, when three Sc atoms were added, we found that the formation of GdSc-3-inter
significantly increased, which means that the $\text{Gd}_2\text{Zr}_2\text{O}_7$ lattice has no ability to accommodate three interstitial Sc atoms; in the case of $\text{GdSc-3-2inter+1-sub}$ model, the formation energy decreases significantly, suggesting that the third atom has to substitute for Gd.

The calculated lattice constant values are also listed in Table 2, and shown in Fig. 3 with variation of the Sc contents. The lattice constant increases to 10.646 when the Sc content is below 11.11%, followed by a decrease. The increase is due to the presence of interstitial Sc atoms causing lattice expansion, and the decrease could be attributed to the smaller Sc substitution for Gd. Note that when the Sc content is above 5.88%, the increase rate of lattice constant is reduced. This indicates that the second Sc atom has some possibility to substitute for Gd, offsetting the lattice expansion, which agrees with the formation energy calculation results. As a result, one could conclude that the interstitial Sc concentration in $\text{Gd}_2\text{Zr}_2\text{O}_7$ lattice might be less than 11.11%, which is consistent with our previous experimental results [17].

According to the change trend of the defect formation energy and lattice constant, the solid solution mechanism of Sc in $\text{Gd}_2\text{Zr}_2\text{O}_7$ lattice might be clear: when the Sc content is 5.88%, the Sc atom enter the interstitial sites (32e) in the lattice; when the Sc content is 5.88%-11.11%, the interstitial Sc atoms reach saturation, after that the doped Sc begin to substitute for Gd.
3.3 Mechanical and thermophysical properties of Sc-doped Gd$_2$Zr$_2$O$_7$

Based on the fully optimized model, we calculated the mechanical properties of Sc doped Gd$_2$Zr$_2$O$_7$ with Gd$_{2-}$inter, Gd$_{2-}$2-inter, Gd$_{2-}$3-2-inter+1-sub, and Gd$_{2-}$4-2-inter+2-sub, including elastic constants, bulk modulus $B$, shear modulus $G$ and Young's modulus $E$. For cubic system, there are three independent elastic constants $C_{11}$, $C_{12}$ and $C_{44}$. The calculated results are shown in Table 3. For Gd$_2$Zr$_2$O$_7$, there are some differences between our calculated results and values in the literature [27, 32]. The reason may be that the pseudopotential we used is different from that in the literature. For the ceramic system, we did not consider the spin polarization in the calculation process, while the results in the literature considered it [27, 32]. However, for the bulk elastic modulus $B$, shear elastic modulus $G$ and Young's elastic modulus $E$, our calculated results are in good agreement with the experimental values, which reveals the reliability of our calculated results.

For the cubic system, the elastic constants $C_{11}$, $C_{12}$ and $C_{44}$ must meet the following three criteria to be mechanically stable: $C_{11}+2C_{12} > 0$; $C_{44} > 0$; $C_{11}-C_{12} > 0$ [42]. According to the calculation results in Table 3, all models are mechanically stable. The variation trend of elastic constant and elastic modulus with the Sc content is shown in Fig. 4. It can be seen from Fig. 4a that $C_{11}$, $C_{12}$ and $C_{44}$ have the lowest value when the Sc doping amount is 5.88%. Fig. 4b shows the bulk modulus $B$, shear modulus $G$ and Young's modulus $E$. When the Sc content is 5.88%, bulk modulus $B$ decreases to the lowest value, and then increases slowly with the increase of Sc content. The shear
modulus G decreases gently with the increase of Sc content, which is consistent with
the research results of Th-doped Gd\textsubscript{2}Zr\textsubscript{2}O\textsubscript{7}, Ti-doped Gd\textsubscript{2}Zr\textsubscript{2}O\textsubscript{7} and La-doped Gd\textsubscript{2}Zr\textsubscript{2}O\textsubscript{7} [26, 27]. Note that doping Sc atom could reduce Young's modulus E by 50-73 GPa. This
is because doping smaller Sc atom into Gd\textsubscript{2}Zr\textsubscript{2}O\textsubscript{7} lattice introduce size and coupling
force mismatch, which causes fluctuation of strain field and lattice softening, resulting
in a significant decrease of Young's modulus [43]. For TBC applications, a low Young's
modulus is desirable, which means large stain tolerance of coatings beneficial for
thermal shock resistance of TBCs [44].

The calculated results of Pugh’s indicator(G/B) and Poisson ratios (σ) of Sc doped
Gd\textsubscript{2}Zr\textsubscript{2}O\textsubscript{7} with Gd\textsubscript{Sc-1-inter}, Gd\textsubscript{Sc-2-inter}, Gd\textsubscript{Sc-3-2-inter+1-sub}, and Gd\textsubscript{Sc-4-2-inter+2-sub} are listed in
Table 4. G/B is an important index to describe brittle toughness of materials, with a
critical value of 0.5, above which the material exhibits brittle [45]. In other words, the
lower the G/B is, the better toughness the material has. Poisson's ratio σ is also another
an important parameter to describe the toughness of materials. For ductile materials,
the Poisson's ratio is 0.33, while for strong covalent crystals, the Poisson's ratio is 0.1
[46]. In other words, a higher the Poisson's ratio means better toughness of materials.
The calculated G/B and Poisson’s ratios of Gd\textsubscript{2}Zr\textsubscript{2}O\textsubscript{7} are 0.545 and 0.269, which are in
good agreement with the literature values [26, 47]. Fig. 5 shows the variation of Pugh’s
indicator(G/B) and Poisson ratios (σ) with the Sc content. With the increase of the Sc
content, G/B decreases first followed by an increase when the doping content reach
16.67%, while σ increases first and then shows a decrease. At a Sc doping level of
16.67%, G/B has the lowest value of 0.408, and σ has the highest value of 0.32, suggesting that the material with this composition has the highest toughness.

The thermophysical properties of different Sc-doped Gd$_2$Zr$_2$O$_7$ models are listed in Table 5. The calculated Debye temperature of Gd$_2$Zr$_2$O$_7$ is 508.506 K, which is close to the calculated value of 520.7 K by Zhao et al. [26] and the experimental 513.4 K by Shimamura et al. [47]. After doping Sc atoms into Gd$_2$Zr$_2$O$_7$, longitudinal sound velocity $v_l$, transverse sound velocity $v_t$ and average sound velocity $v_m$ all decrease, which leads to the decrease of Debye temperature. The variation of Debye temperature $\Theta$ (a) and thermal conductivity (b) with the Sc content is shown in Fig. 6. 5.88 % Sc doping into Gd$_2$Zr$_2$O$_7$ lattice reduces the Debye temperature by 72 K, while there is a slight increase in the Debye temperature when the doping content reach 11.11%, and then it decreases again. Debye temperature of a material can reflect its TEC [49]. A low Debye temperature suggests weak interaction between atoms in the lattice, which indicates a high coefficient of thermal expansion [27]. For TBC materials, a high coefficient of thermal expansion benefits to reduce the thermal mismatch between the coating and substrate.

The minimum thermal conductivities were calculated based on Cahill’s model and Clarke’s model as listed in Table 5, which are present in Fig. 6b as the function of the Sc content. The calculated thermal conductivities of Gd$_2$Zr$_2$O$_7$ are 1.23 W/m·K by Clarke’s model and 1.35 W/m·K by Cahill’s model, which are agreed with the
calculated value of 1.29 W/m·K and 1.35 W/m·K by Zhao et al. [26, 27]. Our calculated results are also within the experimental results range of 1.0-1.6 W/m·K [50-52]. It can be seen from Fig. 6b that the minimum thermal conductivity calculated by Cahill’s model is slightly higher than that by Clarke’s model, which is also in line with the calculation trend of other scholars [26, 27]. Comparing curves in Fig. 6a and 6b, it could be found that the variation trend of thermal conductivity is similar with that of Debye temperature with the increase of Sc content. Compared with Gd$_2$Zr$_2$O$_7$, 5.88 % Sc doped Gd$_2$Zr$_2$O$_7$ has a significant decrease in the minimum thermal conductivity, but further increasing the Sc doping content enhances the thermal conductivity; when the Sc content is above 11.11%, the minimum thermal conductivity has a decline trend, but the decrease rate becomes slow at higher doping levels. It can be seen from the variation of Debye temperature and thermal conductivity that too much Sc doping has no obvious effect on increasing TEC and decreasing thermal conductivity.

Thermal conductivity is closely related to phonon scattering [21]. When the Sc content is 5.88%, Sc atoms enter the interstitial sites of Gd$_2$Zr$_2$O$_7$, which enhances phonon scattering. However, in order to balance the charge, oxygen vacancies are consumed, which would reduce the phonon scattering, but the thermal conductivity is still greatly reduced, which indicates that interstitial doping atoms play a significant role in enhancing phonon scattering. With the increase of Sc content, Gd is gradually replaced by Sc$^{3+}$. Due to the smaller Sc$^{3+}$ replaces Gd$^{3+}$, resulting in Sc$^{3+}$ is loosely bound in an oversized atomic cage and does not easily vibrate with other phonons, acting like a local
"rattler", which enhances the scattering of phonons and leads to a decrease in thermal conductivity, but its enhancement effect is not as significant as that brought by interstitial atoms, which leads to a slow decline in thermal conductivity [53].

According to the theoretical calculation, the mechanical and thermophysical properties of Gd$_2$Zr$_2$O$_7$ can be designed by Sc doping. When the Sc content is less than 11.11%, all Sc atoms enter the interstitial sites of Gd$_2$Zr$_2$O$_7$ lattice. Then, the Gd$^{3+}$ sites would be gradually replaced by Sc$^{3+}$ with the increase of Sc content. Young's modulus decreases by 50-64 GPa after doping Sc atom, which benefits the thermal shock resistance and high temperature stability of the coating. However, when the content of Sc exceeds 16.67%, the decreasing trend slows down. The toughness of the material can be improved obviously by doping Sc atoms, but when Sc content exceeds 16.67%, the toughness begins to decrease. Similarly, the downward trend of Debye temperature and thermal conductivity begins to slow down after Sc content exceeds 16.67%. Therefore, when the content of Sc is about 16.67%, all aspects of the performance may be the most suitable.

3.4 Preparation of Gd-Sc TBCs and their sintering behavior

The XRD patterns of the prepared Gd-Sc powder, Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs are shown in Fig. 7a. All the patterns exhibit similar appearance, which have diffraction peaks ascribed to disordered defect fluorite. This indicates that during plasma spraying processes, Gd-Sc powder keeps phase stability, and our spraying
parameters are suitable. Fig. 7b shows the DSC curve of Gd-Sc powder at a temperature range of 25 °C to 1450 °C. There is an endothermic peak at 388 °C, which may be caused by evaporative heat absorption of crystalline water. No other heat absorption or exothermic peaks can be observed during the whole heating process, which indicates that Gd-Sc can maintain good high temperature stability up to 1450 °C. This is beneficial for Gd-Sc coatings used at elevated temperatures.

Cross-sectional microstructures of Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs are shown in Fig. 8a and Fig. 8b, respectively. The Gd-Sc coating and YSZ coating show a typical layered structure, and both types of TBCs have integral interface, where there are no obvious defects such as gaps and cracks. In Gd-Sc TBCs, the thickness of the Gd-Sc coating is ~120 μm. In Gd-Sc/YSZ DCL TBCs, the thickness of Gd-Sc coating is ~80 μm and that of YSZ coating is ~150 μm.

The XRD patterns of Gd-Sc/YSZ coatings after heat treatment tests at 1400 °C are shown in Fig. 9. It can be seen that the patterns of the annealed coatings are similar to that of the as-fabricated coating except that the peaks become sharp, which indicates the crystallization degree of the coatings increases after heat treatments. No new phases are formed in the coatings during sintering, indicating that Gd-Sc coating has excellent phase stability at 1400 °C.

The surface morphologies of Gd-Sc coatings after heat treatments at 1400 °C are shown
in Fig. 10. During the first 100 h heat treatment, the coating surface morphologies have little change indicative of excellent sintering resistance. Prolonging the heat treatment to 200 h, many micro-cracks disappear and some large cracks appear, and in the enlarged image (Fig. 10d), one can found that the grains have some growth. This indicates that the coating experiences some sintering during long-term heat treatment at 1400 °C, but the sintering degree is not severe, and the coating almost keeps its original morphology.

The fracture surface morphology of Gd-Sc coatings after heat treatments at 1400 °C are shown in Fig. 11. It can be seen that the layered structure can be clearly observed in the coatings after 20 h, 50 h and 100 h heat treatments. When the heat treatment time is extended to 200 h, the lamellar structure is not obvious, microcracks and pores are closed, and some vertical cracks begin to appear, which indicates that the coating turns to sintering. The reason for the vertical cracks may be that sufficient temperature and time provide driving force for the growth of grains during heat treatment. At the beginning of sintering, grains contact with each other, resulting in sintering neck, microcracks and voids gradually heal; with the extension of time to the later stage of sintering, the micro-cracks and voids disappear, which reduces the strain tolerance and thermal insulation of the coating. The thermal stress accumulated during long-term heat treatment couldn’t be released through micro-cracks and voids, resulting in stress concentration, which results in cracks during the cooling phase. This will not benefit the thermal shock resistance, corrosion resistance and other properties of the coating,
and greatly reduces the service life of the coating.

3.5 Thermal cycling behavior of Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs

The macroscopic morphologies evolution of Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs during thermal cycling tests are shown in Fig. 12. Both types of TBCs spalled from the edge. After 75 and 215 thermal cycles, the spallation area of Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs reaches 20% of the total area, respectively. The superalloy substrates become black, which indicates that substrate oxidation takes place during the thermal cycling test. By comparison, Gd-Sc/YSZ DCL TBCs exhibits much longer lifetime than that of Gd-Sc TBCs, revealing that double-layer design could significantly improve the thermal shock resistance of TBCs.

The XRD patterns of the Gd-Sc TBCs and Gd-Sc/YSZ DCL TBCs after thermal cycling tests are shown in Fig. 13. During the tests, Gd-Sc coatings undergo no phase decomposition, indicating that the coatings have excellent phase stability. AlNi$_3$ is detected for the Gd-Sc TBCs after 75 thermal cycles, which is the component of the bonding coating [54, 55]. It could be presumed that some regions of Gd-Sc coating have spalled off, leaving the bond coating outside. After 215 thermal cycles, t’-ZrO$_2$ and NiO are detected in the Gd-Sc/YSZ DCL TBCs. This indicates that the spallation may occur near the bond coating, causing the TGO being detected.

The spalling edge region and adjacent region of Gd-Sc TBCs and Gd-Sc/YSZ DCL
TBCs are marked as A, B, C and D, respectively, as shown in Fig. 12b and d. Fig. 14a shows the cross-sectional morphology of region A. After 75 thermal cycles, the Gd-Sc coating has spalled, and there is a large delamination crack in the coating. The cross-section morphology of region B is shown in Fig. 14b. It can be seen that the coating delamination starts from the region near the bond coating. It has been reported that Gd$_2$Zr$_2$O$_7$ can react with TGO during heat treatment, which causes stress growth and crack formation at the interface between Gd$_2$Zr$_2$O$_7$ coating and the bond coating [22]. For Gd-Sc coating, it also has large possibility to react with TGO, resulting in delamination crack in the coating region near the bond coating. Additionally, although Gd-Sc has improved toughness compared with Gd$_2$Zr$_2$O$_7$, its toughness is still not high enough to resist the thermal stress generated in the thermal cycle process, which inevitably leads to the formation of cracks in the Gd-Sc coating.

Fig. 15a shows the cross-sectional microstructure of region C. After 215 thermal cycles, the interface between Gd-Sc and YSZ coatings is well bonded, without any defect, and both coating maintains good structural integrity. However, a larger delamination crack forms in the YSZ coating, above which the coatings are spalled. The cross-sectional morphology of region D is shown in Fig. 15b. Although the coatings here are not spalled, some delamination cracks can be found in the YSZ coating, which could cause coating spallation like Fig. 15a by further thermal shock. At the interface between the YSZ coating and the bond coating, some dark contrast products are observed, which are denoted as E. EDS analysis results show that the product is mainly composed of Ni, Al,
O and a small amount of Cr. Combined with the XRD results, we can determine that the products in this region are mainly NiO, as well as some Cr and Al oxides, which is the component of TGO.

Based on the results of SEM and EDS, the failure mechanisms of Gd-Sc/YSZ DCL TBCs could be analyzed as follows: since the bottom and side of the substrate are not covered with the coating, and the thickness of the bond coating is thin, which results in serious oxidation of the alloy substrates and the bond coating during thermal cycling. The thickness of the TGO increase and accompany by a larger volume expansion, thereby producing a large stress concentration near the oxidation product, resulting in the initiation and propagation of cracks, which cause the YSZ coating cracking. Note that Gd-Sc coating still maintains good structural integrity and the interface with YSZ coating is intact. This is because the doping of Sc improves the toughness and TEC, and reduces the Young’s modulus, which ensures the tolerance in the process of thermal cycle, and has a good thermal match with YSZ. YSZ coating plays a good buffer role during thermal cycling, and prevent the reaction of Gd-Sc with the bond coating to form GdAlO$_3$ phase. Therefore, Gd-Sc/YSZ DCL TBCs have better thermal shock resistance.

Thermal cycling life is an important index to evaluate the practical performance of TBCs. Long thermal cycle life is more suitable as a candidate material for TBCs. There are many factors that affect the thermal cycle life, such as cooling rate, temperature, high temperature dwell time and so on. Under similar experimental conditions, the
thermal cycling life of La$_2$Zr$_2$O$_7$/YSZ-TBCs is 160 times, GdPO$_4$/YSZ-TBC is 70 times and (La$_{0.8}$Eu$_{0.2}$)$_2$Zr$_2$O$_7$/YSZ-TBC is 32 times [56-58]. The thermal cycling life of these new thermal barrier coatings is less than that of Gd-Sc/YSZ DCL TBCs. In particular, compared with Gd$_2$Zr$_2$O$_7$, the thermal cycling life is increased by 55% [59]. Therefore, Gd-Sc has excellent thermal shock resistance and good application prospects in the newly developed thermal barrier coating materials.

4. Conclusions

In this work, the first-principles method is used to study the solid solution mechanism of Sc atom in Gd$_2$Zr$_2$O$_7$ lattice, and the variation of mechanical and thermophysical properties of Sc-doped Gd$_2$Zr$_2$O$_7$ (Gd-Sc) with the Sc content, based on which the Sc doping content was optimized. Then, Gd-Sc TBCs and Gd-Sc/YSZ TBCs were produced by air plasma spraying, and the phase composition, microstructure, sintering behavior and thermal cycling performance of the coatings were investigated. Following conclusions can be drawn:

(1) When the content of Sc is 5.88%, Sc atoms occupies the interstitial sites in the Gd$_2$Zr$_2$O$_7$ lattice because the formation energy of interstitial doping is significantly lower than that of substitution doping. The variation trend of the lattice constant shows that the Sc interstitial concentration might be less than 11.11%. After that, Gd would be gradually replaced by Sc with the increase of the doping content.

(2) Compared with Gd$_2$Zr$_2$O$_7$, Gd-Sc has lower Young's modulus and Pugh's indicator (G/B) and a higher Poisson ratio (σ) suggesting better thermal shock
resistance and higher toughness. At the Sc doping level of 16.67%, Gd-Sc exhibited the lowest G/B and the highest σ indicative of the highest toughness. With the increase of the Sc content, the Debye temperature and thermal conductivity have similar variation trends, which have a significant decrease when doping 5.88 % Sc, and then increase slightly followed by a decrease with further doping. When the Sc content exceeds 16.67%, the decreasing trend of Debye temperature and thermal conductivity reduce. Therefore, the Sc doping content in Gd$_2$Zr$_2$O$_7$ is optimized to be 16.67%.

(3) Gd-Sc coatings maintain excellent phase and structural stability after heat treatment at 1400 °C for 100 h. The thermal shock resistance of Gd-Sc/YSZ DCL TBCs is better than that of Gd-Sc TBCs. Due to the improvement on the toughness and thermal expansion coefficient and the decrease in Young's modulus, Gd-Sc coatings have good structural integrity and excellent matching with YSZ coating during thermal cycling. In addition, YSZ coating plays a good buffer role during thermal cycling and prevents the reaction of Gd-Sc with the bond coating. Gd-Sc coatings reveal excellent thermal shock resistance and sintering resistance, which has a promising application prospect.

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Figure Captions

Fig. 1. Crystal structure of Gd$_2$Zr$_2$O$_7$

Fig. 2. Solid solution mode of Sc in Gd$_2$Zr$_2$O$_7$ lattice with different doping contents

Fig. 3. The variations of lattice constants with the Sc content

Fig. 4. The variations of (a) Elastic constants C$_{11}$, C$_{12}$, C$_{44}$ and (b) Bulk modulus B, Shear modulus G and Young's modulus E with the Sc content

Fig. 5. The variations of Pugh’s indicator(G/B) and Poisson ratios (σ) with the Sc content

Fig. 6. The variation of Debye temperature Θ (a) and thermal conductivity (b) with the Sc content

Fig. 7. XRD patterns of Gd-Sc powders and coatings (a), and DSC curve of Gd-Sc powders (b)

Fig. 8. Cross-section microstructures of the Gd-Sc TBC (a) and the Gd-Sc/YSZ DCL TBC (b)

Fig. 9. XRD patterns of Gd-Sc coatings after different heat treatment time

Fig. 10. Surface morphologies of Gd-Sc coatings after heat treatment at 1400 °C for (a) 20 h, (b) 50 h, (c) 100 h and (d) 200 h

Fig. 11. Fracture surface morphologies of Gd-Sc coatings after heat treatment at 1400 °C for (a) 20 h, (b) 50 h, (c) 100 h and (d) 200 h

Fig. 12. Macroscopic morphologies evolution of Gd-Sc TBCs (a and b) and Gd-Sc/YSZ DCL TBCs (c and d) during thermal cycling tests

Fig. 13. XRD patterns of Gd-Sc TBCs (a) and Gd-Sc/YSZ DCL TBCs (b) after thermal
cycling tests

Fig. 14. Cross-sectional microstructures of regions A (a) and B (b) of Gd-Sc TBCs after 75 thermal cycles

Fig. 15. Cross-sectional microstructures of regions C (a) and D (b) of Gd-Sc/YSZ DCL TBCs after 215 thermal cycles
Table 1

The structural parameters of Gd$_2$Zr$_2$O$_7$

|         | $a_0$  | $x_{O-4f}$ | $\rho$ (g/cm$^3$) |
|---------|--------|------------|-------------------|
| Gd$_2$Zr$_2$O$_7$ | 10.600 | 0.3386     | 6.79              |
| Cal. [37] | 10.682 | 0.338      | 6.629             |
| Cal. [27] | 10.452 | 0.342      |                   |
| Cal. [38] | 10.66  | 0.339      |                   |
| Exp. [39] | 10.54  | 0.344      | 6.8 [40]          |

Table 2

Lattice constants and formation energy calculations of Sc-doped Gd$_2$Zr$_2$O$_7$

| Sc content         | $a_0$  | $E_f$  |
|--------------------|--------|--------|
| GdSc-sub           | 6.25%  | 10.581 | 1.269  |
| GdSc-inter         | 5.88%  | 10.646 | 0.141  |
| GdSc-2-inter       | 11.11% | 10.663 | 0.659  |
| GdSc-2-inter+sub   | 11.76% | 10.632 | 0.745  |
| GdSc-3-inter       | 15.79% | 10.758 | 3.347  |
| GdSc-3-2inter+1-sub| 16.67% | 10.647 | 0.953  |
| GdSc-4-2-inter+2-sub| 22.22%| 10.623 | 1.621  |

Table 3

Elastic constant and elastic modulus of Sc-doped Gd$_2$Zr$_2$O$_7$

|         | $C_{11}$ | $C_{12}$ | $C_{44}$ | $B$ | $G$  | $E$  |
|---------|----------|----------|----------|-----|------|------|
| Gd$_2$Zr$_2$O$_7$ | 296.521  | 101.943  | 86.824   | 166.803 | 90.869 | 230.712 |
| Cal. [27] | 324.7    | 125.3    | 94       | 191.8 | 96.2 | 247.3 |
| Cal. [32] | 277      | 110      | 52       | 165   | 63   | 214   |
| Exp. [47] | -        | -        | -        | 174   | 93   | 236   |
| Exp. [48] | -        | -        | -        | 153   | 80   | 205   |
| GdSc-inter | 263.328  | 69.894   | 48.769   | 123.007 | 66.713 | 169.497 |
| GdSc-2-inter | 285.407  | 81.656   | 55.201   | 147.880 | 69.716 | 180.745 |
| GdSc-3-2inter+1-sub | 281.431  | 99.205   | 58.998   | 154.205 | 62.964 | 166.263 |
| GdSc-4-2-inter+2-sub | 273.801  | 86.689   | 53.527   | 140.88 | 60.089 | 157.827 |
Table 4

Pugh’s indicator (G/B) and Poisson ratios (σ) of Sc-doped Gd$_2$Zr$_2$O$_7$

|          | G/B  | σ    |
|----------|------|------|
| Gd$_2$Zr$_2$O$_7$ | 0.545 | 0.269 |
| Cal. [26]  | 0.500 | 0.285 |
| Exp. [47]  | 0.530 | 0.273 |
| GdSc-inter | 0.542 | 0.270 |
| GdSc-2-inter | 0.471 | 0.296 |
| GdSc-3-2inter+1-sub | 0.408 | 0.32  |
| GdSc-4-2-inter+2-sub | 0.427 | 0.313 |

Table 5

Thermophysical properties of Sc-doped Gd$_2$Zr$_2$O$_7$

|          | $v_1$  | $v_l$  | $v_m$   | $\Theta$ | $k_{\text{Clarke}}$ | $k_{\text{Cahill}}$ |
|----------|--------|--------|---------|----------|----------------------|----------------------|
| GZO      | 6512.44 | 3658.179 | 4070.692 | 508.506  | 1.23                 | 1.35                 |
| Cal. [26] | 4108.0  | 520.7  |          |          | 1.29                 | 1.42                 |
| Exp.     | 513.4[47] |        | 1.0-1.6 [50-52] |        |                      |                      |
| GdSc-inter | 5595.406 | 3139.157 | 3493.509 | 436.277  | 1.06                 | 1.16                 |
| GdSc-2-inter | 5955.415 | 3204.201 | 3577.345 | 447.505  | 1.17                 | 1.21                 |
| GdSc-3-2inter+1-sub | 5968.192 | 3068.724 | 3436.649 | 430.97   | 1.06                 | 1.20                 |
| GdSc-4-2-inter+2-sub | 5809.301 | 3029.188 | 3389.289 | 425.403  | 1.05                 | 1.17                 |
Figure 1

Crystal structure of Gd2Zr2O7
Figure 2

Solid solution mode of Sc in Gd2Zr2O7 lattice with different doping contents
Figure 3

The variations of lattice constants with the Sc content
Figure 4

The variations of (a) Elastic constants $C_{11}$, $C_{12}$, $C_{44}$ and (b) Bulk modulus $B$, Shear modulus $G$ and Young's modulus $E$ with the Sc content.
Figure 5

The variations of Pugh's indicator (G/B) and Poisson ratios (σ) with the Sc content
Figure 6

The variation of Debye temperature $\Theta$ (a) and thermal conductivity (b) with the Sc content.
Figure 7

XRD patterns of Gd-Sc powders and coatings (a), and DSC curve of Gd-Sc powders (b)
Figure 8

Cross-section microstructures of the Gd-Sc TBC (a) and the Gd-Sc/YSZ DCL TBC (b)
Figure 9

XRD patterns of Gd-Sc coatings after different heat treatment time
Figure 10

Surface morphologies of Gd-Sc coatings after heat treatment at 1400 °C for (a) 20 h, (b) 50 h, (c) 100 h and (d) 200 h
Figure 11

Fracture surface morphologies of Gd-Sc coatings after heat treatment at 1400 °C for (a) 20 h, (b) 50 h, (c) 100 h and (d) 200 h
Figure 12

Macroscopic morphologies evolution of Gd-Sc TBCs (a and b) and Gd-Sc/YSZ DCL TBCs (c and d) during thermal cycling tests
Figure 13

XRD patterns of Gd-Sc TBCs (a) and Gd-Sc/YSZ DCL TBCs (b) after thermal cycling tests
Figure 14

Cross-sectional microstructures of regions A (a) and B (b) of Gd-Sc TBCs after 75 thermal cycles
Figure 15

Cross-sectional microstructures of regions C (a) and D (b) of Gd-Sc/YSZ DCL TBCs after 215 thermal cycles