Neutral Higgs Bosons in the SU(3)$_L$⊗U(1)$_N$ model

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Abstract

The SU(3)$_L$⊗U(1)$_N$ electroweak model predicts new Higgs bosons beyond the one of the standard model. In this work we investigate the signature and production of neutral SU(3)$_L$⊗U(1)$_N$ Higgs bosons in the $e^-e^+$ Next Linear Collider (NLC) and in the CERN Linear Collider (CLIC). We compute the branching ratios of two of the SU(3)$_L$⊗U(1)$_N$ neutral Higgs bosons and study the possibility to detect them and the $Z'$ extra neutral boson of the model.

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I. INTRODUCTION

The Higgs sector still remains one of the most indefinite part of the standard model [1], but it still represents a fundamental rule by explaining how the particles gain masses by means of a isodoublet scalar field, which is responsible for the spontaneous breakdown of the gauge symmetry, the process by which the spectrum of all particles are generated. This process of mass generation is the so called Higgs mechanism, which plays a central role in gauge theories. In this process there remains a single neutral scalar, manifesting itself as the Higgs particle. In the standard model only one SU(2) Higgs doublet is necessary and enough to break the gauge symmetry and to generate the particles masses. However, the standard model does not predicts the number of scalar multiplets of the theory, for that reason, there are several extensions of the standard model containing neutral and charged Higgs bosons. The standard model is not able to predicts the mass of the Higgs boson. However, indirect experimental limits are obtained from precision measurements of the electroweak parameters. These measurements are now realized in radiative correction levels, which have a logarithmic dependence of standard Higgs boson mass. From several experiments the present value for the standard Higgs boson mass is $126^{+73}_{-48}$ GeV [2].

Since the standard model leaves many questions open, there are several well motivated extensions of it. For example, if the Grand Unified Theory (GUT) contains the standard model at high energies, then the Higgs bosons associated with GUT symmetry breaking must have masses of order $M_X \sim \mathcal{O}(10^{15})$ GeV. Supersymmetry [3] provides a solution to this hierarchy problem through the cancellation of the quadratic divergences via the contributions of fermionic and bosonic loops [4]. Moreover, the Minimal Supersymmetric extension of the Standard Model (MSSM) can be derived as an effective theory from supersymmetric Grand Unified Theories [5]. Another promissory class of models is the one based on the $SU(3)_C \otimes SU(3)_L \otimes U(1)_N$ (3-3-1 for short) semi-simple symmetry group [6].

These models emerge as an alternative solution to the problem of violation of unitarity at high energies in processes such as $e^- e^- \rightarrow W^- V^-$, induced by right-handed currents coupled to a vector boson $V^-$. The usual way to circumvent this problem is to give particular values to model parameters in order to cancel the amplitude of the process [7], but in [7] was proposed an elegant solution assuming the presence of a doubly charged vector boson. The simplest electroweak gauge model that is able to realize naturally a double charge gauge
boson is the one based on the SU(3) \( \otimes \) U(1) symmetry. As a consequence of the extended
gauge symmetry, the model is compelled to accommodate a much richer Higgs sector.

The main feature of the 3-3-1 model is that it is able to predicts the correct number
of fermions families. This is because, contrary to the standard model, the 3-3-1 model is
anomalous in each generation. The anomalies are cancelled only if the number of families is a
multiple of three. In addition, if we take into account that the asymptotic freedom condition
of the QCD is valid only if the number of generations of quarks is to be less than five, we
conclude that the number of generations is three. Another good feature is that the model
predicts an upper bound for the Weinberg mixing angle at \( \sin^2 \theta_W < 1/4 \). Therefore, the
evolution of \( \theta_W \) to high values leads to an upper bound to the new mass scale between 3
TeV and 4 TeV.

In this work we are interested in a version of the 3-3-1 model, whose scalar sector has
only three Higgs triplets. The text is organized as follow. In Sec. II we give the relevant
features of the model. In Sec. III we compute the total cross sections of the processes and
the Sec. IV contains our results and conclusions.

II. BASIC FACTS ABOUT THE 3-3-1 MODEL

The three Higgs triplets of the model are

\[
\eta = \begin{pmatrix} \eta^0 \\ \eta^- \\ \eta^+ \\ \eta^0 \end{pmatrix}, \quad \rho = \begin{pmatrix} \rho^+ \\ \rho^0 \\ \rho^{++} \\ \rho^0 \end{pmatrix}, \quad \chi = \begin{pmatrix} \chi^- \\ \chi^{--} \\ \chi^0 \end{pmatrix}
\]

transforming as \((3,0), (3,1)\) and \((3,-1)\), respectively.

The neutral scalar fields develop the vacuum expectation values (VEVs) \( \langle \eta^0 \rangle \equiv v_\eta, \langle \rho^0 \rangle \equiv v_\rho \) and \( \langle \chi^0 \rangle \equiv v_\chi \), with \( v_\eta^2 + v_\rho^2 = v_W^2 = (246 \text{ GeV})^2 \). The pattern of symmetry breaking is

\[
\text{SU}(3)_L \otimes \text{U}(1)_N \rightarrow \text{SU}(2)_L \otimes \text{U}(1)_Y \rightarrow \text{U}(1)_{\text{em}}
\]

and so, we can expect \( v_\chi \gg v_\eta, v_\rho \). The \( \eta \) and \( \rho \) scalar triplets give masses to the ordinary fermions and gauge bosons, while the \( \chi \) scalar triplet gives masses to the new fermions and new gauge bosons. The most general,
gauge invariant and renormalizable Higgs potential is

\[
V(\eta, \rho, \chi) = \mu_1^2 \eta^\dagger \eta + \mu_2^2 \rho^\dagger \rho + \mu_3^2 \chi^\dagger \chi + \lambda_1 \left( \eta^\dagger \eta \right)^2 + \lambda_2 \left( \rho^\dagger \rho \right)^2 + \lambda_3 \left( \chi^\dagger \chi \right)^2 + \\
+ \left( \eta^\dagger \eta \right) \left[ \lambda_4 \left( \rho^\dagger \rho \right) + \lambda_5 \left( \chi^\dagger \chi \right) \right] + \lambda_6 \left( \rho^\dagger \rho \right) \left( \chi^\dagger \chi \right) + \lambda_7 \left( \rho^\dagger \eta \right) \left( \eta^\dagger \rho \right) + \\
\]
\[ +\lambda_8 \left( \chi^+ \eta \right) \left( \eta^+ \chi \right) + \lambda_9 \left( \rho^+ \chi \right) \left( \chi^+ \rho \right) + \lambda_{10} \left( \eta^+ \rho \right) \left( \eta^+ \chi \right) + \frac{1}{2} \left( f e^{ijk} \eta_{ij} \chi_k + \text{H. c.} \right). \]

Here \( \mu_i \) (\( i = 1, 2, 3 \)), \( f \) are constants with dimension of mass and the \( \lambda_i \) (\( i = 1, \ldots, 10 \)) are dimensionless constants. \( f \) and \( \lambda_3 \) are negative from the positivity of the scalar masses. The term proportional to \( \lambda_{10} \) violates lepto-barionic number, therefore it was not considered in the analysis of the Ref. [10] (another analysis of the 3-3-1 scalar sector are given in Ref. [11] and references cited therein). We can notice that this term contributes to the mass matrices of the charged scalar fields, but not to the neutral ones. However, it can be checked that in the approximation \( v_\chi \gg v_\eta, v_\rho \) we can still work with the masses and eigenstates given in Ref. [10]. Here this term is important to the decay of the lightest exotic fermion. Therefore, we will keep it in the Higgs potential [2].

As usual, symmetry breaking is implemented by shifting the scalar neutral fieldsas \( \varphi = v_\varphi + i \xi_\varphi \), with \( \varphi = \eta^0, \rho^0, \chi^0 \). Thus, the physical neutral scalar eigenstates \( H_1^0, H_2^0, H_3^0 \) and \( h^0 \) are related to the shifted fields as

\[
\begin{pmatrix} \xi_\eta \\ \xi_\rho \end{pmatrix} \approx \frac{1}{v_W} \begin{pmatrix} v_\eta & v_\rho \\ v_\rho & -v_\eta \end{pmatrix} \begin{pmatrix} H_1^0 \\ H_2^0 \end{pmatrix}, \quad \xi_\chi \approx H_3^0, \quad \zeta_\chi \approx h^0, \quad (3)
\]

and in the charged scalar sector we have

\[
\eta_1^+ = \frac{v_\rho}{v_W} H_1^+, \quad \rho^+ = \frac{v_\eta}{v_W} H_1^+, \quad \eta_2^+ = \frac{v_\chi}{\sqrt{v_\eta^2 + v_\rho^2}} H_2^+, \quad \chi^+ = \frac{v_\eta}{\sqrt{v_\eta^2 + v_\rho^2}} H_2^+, \quad (4)
\]

\[
\rho^{++} = \frac{v_\chi}{\sqrt{v_\rho^2 + v_\chi^2}} H^{++}, \quad \chi^{++} = \frac{v_\rho}{v_\chi} H^{++}, \quad (5)
\]

with the condition that \( v_\chi \gg v_\eta, v_\rho \).

The content of matter fields form the three SU(3)_L triplets

\[
\psi_{aL} = \begin{pmatrix} \nu^a_L \\ \ell'^a_L \\ P^a_L \end{pmatrix}, \quad Q_{1L} = \begin{pmatrix} u'_1 \\ d'_1 \\ J_1 \end{pmatrix}, \quad Q_{aL} = \begin{pmatrix} J'_a \\ u'_a \\ d'_a \end{pmatrix}, \quad (6)
\]

transform as (3, 0), (3, 2/3) and (3*, -1/3), respectively, where \( \alpha = 2, 3 \). In Eqs. (11) \( P_\alpha \) are heavy leptons, \( \ell'_a = e', \mu', \tau' \). The model also predicts the exotic \( J_1 \) quark, which carries 5/3 units of elementary electric charge and \( J_2 \) and \( J_3 \) with -4/3 each. The numbers 0, 2/3 and -1/3 in Eqs. (11) are the U_N charges. We also have the right-handed counterpart of
the left-handed matter fields, $\ell'_R \sim (1,-1)$, $P'_R \sim (1,1)$, $U'_R \sim (1,2/3)$, $D'_R \sim (1,-1/3)$, $J'_{1R} \sim (1,5/3)$ and $J'_{23R} \sim (1,-4/3)$, where $U = u, c, t$ and $D = d, s, b$ for the ordinary quarks.

The Yukawa Lagrangians that respect the gauge symmetry are

\[ L^\ell_Y = -G_{ab}\bar{\psi}_a\ell'_b - G'_{ab}\bar{\psi}_aP'_b\chi + \text{H.c.}, \]
\[ L^q_Y = \sum_a \left[ Q_1L \left( G_{1a}U'_{aR}\eta + \tilde{G}_{1a}D'_{aR}\rho \right) + \sum_\alpha Q_{\alpha L} \left( F_{\alpha a}U'_{aR}\rho^* + \tilde{F}_{\alpha a}D'_{aR}\eta^* \right) \right] + \]
\[ + \sum_\alpha F^J_{\alpha \beta}Q_{J1L}J'_\beta J_1R + GJ_{1L}J_{1R} \quad \text{H.c.} \quad (8) \]

Here, the $G$'s, $\tilde{G}$'s, $F$'s and $\tilde{F}$'s are Yukawa coupling constants with $a, b = 1, 2, 3$ and $\alpha = 2, 3$.

It should be noticed that the ordinary quarks couple only through $H^0_1$ and $H^0_2$. This is because these physical scalar states are linear combinations of the interactions eigenstates $\eta$ and $\rho$, which break the SU(2)$_L \otimes$U(1)$_Y$ symmetry to U(1)$_{em}$. On the other hand the heavy-leptons and quarks couple only through $H^0_3$ and $h^0$ in scalar sector, i.e., through the Higgs that induces the symmetry breaking of SU(3)$_L \otimes$U(1)$_N$ to SU(2)$_L \otimes$U(1)$_Y$. The Higgs particle spectrum consists of seven states: three scalars ($H^0_1, H^0_2, H^0_3$), one neutral pseudoscalar $h^0$ and three charged Higgs bosons, $H^+_1, H^+_2$ and $H^{++}$.

In this work we study the production of a neutral Higgs boson at $e^-e^+$ colliders because of lower backgrounds and since it is one of the most promising in the search for the Higgs. The Higgs $H_i$, where $i = 1, 2$ can be radiated from a $Z$ and $Z'$ boson. The $Z(Z') \rightarrow Z H_1(H_2)$ process is the dominant mechanism at the $Z$ resonance energy. We discuss this process only for on-shell $Z$ production. In this work, we will study the production mechanism for Higgs particles in $e^+e^-$ colliders such as the Next Linear Collider (NLC) ($\sqrt{s} = 500$ GeV) and CERN Linear Collider (CLIC) ($\sqrt{s} = 1000$ GeV).

III. CROSS SECTION PRODUCTION

The main mechanism for the production of Higgs particles in $e^+e^-$ collisions occurs in association with the boson $Z$, and $Z'$ through the Drell-Yan mechanism. The process $e^+e^- \rightarrow H_i Z$ ($i = 1, 2$) takes place through the exchange of bosons $Z$ and $Z'$ in the $s$ channel. Then using the interaction Lagrangian (8) and (2) we obtain the differential cross
section

\[
\frac{d\hat{\sigma}}{d\cos\theta} = \frac{\beta_H e^2 \pi}{32 \sin^4 \theta_W \cos^2 \theta_W s} \times \left( \frac{cZH^2}{(s - M_Z^2 + iM_Z \Gamma_Z)^2} \left( 2M_Z^2 + \frac{2tu}{M_Z^2} - 2t - 2u + 2s \right) \left( g_V^2 + g_A^2 \right) + \right.
\]

\[
+ \frac{cZ'H^2_i}{(s - M_Z^2 + iM_Z \Gamma_Z)^2} \left( 2M_Z^2 + \frac{2tu}{M_Z^2} - 2t - 2u + 2s \right) \left( g_V^{i'} + g_A^{i'} \right) + \right.
\]

\[
+ \frac{2 \ cZH_i cZ'H_i}{(s - M_Z^2 + iM_Z \Gamma_Z) (s - M_{Z_i}^2 + iM_{Z_i} \Gamma_{Z_i})} \times \left. \left( 2M_Z^2 + \frac{2tu}{M_Z^2} - 2t - 2u + 2s \right) \left( g_V^i g_V^{i'} + g_A^i g_A^{i'} \right) \right].
\]

The primes (') are for the case when we take a $Z'$ boson, $\Gamma_Z$ and $\Gamma_{Z'}$ are the total width of the $Z$ and $Z'$ bosons, $g_V^e, g_A$ are the standard lepton coupling constants, $g_{V', A'}$ are the $3-3-1$ lepton coupling constants, $\sqrt{s}$ is the center of mass energy of the $e^-e^+$ system.

For the $Z'$ boson we take $M_{Z'} = (0.5 - 3)$ TeV, since $M_{Z'}$ is proportional to the VEV $v_\chi$ [1, 13]. For the standard model parameters we assume PDG values, i.e., $M_Z = 91.19$ GeV, $\sin^2 \theta_W = 0.2315$, and $M_W = 80.33$ GeV [14], the velocity of the Higgs in the center of mass (CM) of the process is denoted through $\beta_H$, $t$ and $u$ are the kinematic invariants, the $cZZH_i (cZZ'H_i)$ are the coupling constants of the $Z$ boson to $Z(Z')$ bosons and Higgs $H_i$ where $i$ stands for $H^0$, $H^0$, the ch$0$VPM are the coupling constants of the $H^0_i$, where $i$ = 1, 2, to $V^-V^+$, the ch$0$UPP are the coupling constants of the $H^0_i$, where $i$ = 1, 2, to $U^--U^{++}$, and the ch$0$HPP are the coupling constants of the $H^0_i$, where $i$ = 1, 2, to $H^--H^{++}$. We then have that

\[
t = M_Z^2 - \frac{s}{2} \left\{ 1 + \frac{M_Z^2 - M_H^2}{s} + \right. \]

\[
- \cos \theta \left[ \left( 1 - \frac{(M_Z + M_H)^2}{s} \right) \left( 1 - \frac{(M_Z - M_H)^2}{s} \right) \right]^{1/2} \left\} \right., \quad (10)
\]

\[
u = M_H^2 - \frac{s}{2} \left\{ 1 - \frac{M_Z^2 - M_H^2}{s} + \right. \]

\[
+ \cos \theta \left[ \left( 1 - \frac{(M_Z + M_H)^2}{s} \right) \left( 1 - \frac{(M_Z - M_H)^2}{s} \right) \right]^{1/2} \left\} \right., \quad (11)
\]

\[
cZZH_1^0 = -i \frac{g^2}{2\sqrt{3}v_W} \frac{M_Z}{M_W} \frac{v_\eta (6t_W^2 + 1) - v_\rho^2}{\sqrt{1 + 3t_W^2}}, \quad (12)
\]

\[
cZZH_2^0 = i \frac{g^2}{\sqrt{3}} \frac{v_\eta v_\rho}{v_W} \sqrt{1 + 4t_W^2}, \quad cH10VPM = -ig^2 \frac{v_\rho}{v_W}, \quad (13)
\]

\[
\]
\[
cH20VPM = -ig^2 \frac{v_\eta v_\rho}{v_W}, \quad cH10UPP = -ig^2 \frac{v_\eta^2}{v_W}, \quad cH20UPP = ig^2 \frac{v_\eta v_\rho}{v_W}, \quad (16)
\]
\[
cH10HPP = -i 2 \left( (\lambda_6 + \lambda_9) v_\eta^4 + (2\lambda_2 + \lambda_9) v_\eta^2 v_\chi + (\lambda_4 + \lambda_5) v_\eta^2 v_\chi^2 \right) / v_W \left( v_\eta^2 + v_\chi^2 \right), \quad (17)
\]
\[
cH20PP = iv_\eta \frac{2v_\rho \left( (2\lambda_2 - \lambda_4 + \lambda_9) v_\chi^2 + (\lambda_6 - \lambda_5 + \lambda_9) v_\eta^2 \right) - f v_\eta v_\rho v_\chi}{v_W \left( v_\eta^2 + v_\chi^2 \right)}, \quad (18)
\]

where \( \theta \) is the angle between the Higgs and the incident electron in the CM frame, where the coupling constant of the \( Z \) boson to \( Z \) and \( H^0_1 \) are the standard ones and the coupling constant of the \( Z \) boson to \( Z \) and \( H^0_2 \) does not exist.

The total width of the Higgs \( H^0_1 \) into quarks, leptons, \( W^+W^- \), \( ZZ \), \( ZZ' \), \( Z'Z' \) gauge bosons, \( H^0_2 H^0_2 \), \( H^0_1 H^-_1 \), \( H^-_1 H^-_2 \), \( h^0 h^0 \), \( H^0_2 H^0_3 \) Higgs bosons, \( V^-V^+ \) charged bosons, \( U^-U^{++} \) double charged bosons, \( H^0_2 Z \), \( H^0_3 Z' \) bosons and \( H^-H^{++} \) double charged Higgs bosons, are, respectively, given by

\[
\Gamma \left( H^0_1 \rightarrow \text{all} \right) = \Gamma_{H^0_1 \rightarrow q\bar{q}} + \Gamma_{H^0_1 \rightarrow \ell^+\ell^-} + \Gamma_{H^0_1 \rightarrow W^+W^-} + \Gamma_{H^0_1 \rightarrow ZZ} + \Gamma_{H^0_1 \rightarrow Z'Z} + \Gamma_{H^0_1 \rightarrow Z''Z''} + \Gamma_{H^0_1 \rightarrow H^-_1 H^-_1} + \Gamma_{H^0_1 \rightarrow H^-_1 H^-_2} + \Gamma_{H^0_1 \rightarrow h^0 h^0} + \Gamma_{H^0_1 \rightarrow H^0_2 H^0_3} + \Gamma_{H^0_1 \rightarrow V^-V^+} + \Gamma_{H^0_1 \rightarrow U^-U^{++}} + \Gamma_{H^0_1 \rightarrow H^0_2 Z} + \Gamma_{H^0_1 \rightarrow H^0_3 Z'} + \Gamma_{H^0_1 \rightarrow H^-H^{++}}, \quad (19)
\]

where we have for each the widths given above that

\[
\Gamma_{H^0_1 \rightarrow q\bar{q}} = \frac{3 \sqrt{1 - 4M_q^2/M_{H^0_1}^2}}{16\pi M_{H^0_1}^2} \frac{M_q^2}{v_W^2} \left( M_{H^0_1}^2 - 2M_q^2 \right), \quad (20)
\]
\[
\Gamma_{H^0_1 \rightarrow \ell^+\ell^-} = \frac{\sqrt{1 - 4M_\ell^2/M_{H^0_1}^2}}{16\pi M_{H^0_1}^2} M_\ell^2 \left( M_{H^0_1}^2 - 2M_\ell^2 \right), \quad (21)
\]
\[
\Gamma_{H^0_1 \rightarrow W^+W^-} = \frac{\sqrt{1 - 4M_W^2/M_{H^0_1}^2}}{8\pi} \frac{g^2 M_W^2}{M_{H^0_1}^2} \left( 3 - \frac{M_{H^0_1}^2}{M_W^2} + \frac{M_{H^0_1}^4}{4M_W^4} \right), \quad (22)
\]
\[
\Gamma_{H^0_1 \rightarrow ZZ} = \frac{\sqrt{1 - 4M_Z^2/M_{H^0_1}^2}}{8\pi \cos^2 \theta_W} \frac{g^2 M_Z^2}{M_{H^0_1}^2} \left( 3 - \frac{M_{H^0_1}^2}{M_Z^2} + \frac{M_{H^0_1}^4}{4M_Z^4} \right), \quad (23)
\]
\[
\Gamma_{H^0_1 \rightarrow Z'Z'} = \sqrt{\frac{1}{8\pi M_{H^0_1}^2} \left( \frac{M_{Z'}+M_Z}{M_{H^0_1}} \right)^2} \left( cZ' H^0_1 \right)^2 \times \left( \frac{5}{2} + \frac{1}{4} \frac{M_Z^2}{M_{Z'}^2} + \frac{1}{4} \frac{M_{Z'}^2}{M_Z^2} + \frac{1}{4} \frac{M_{H^0_1}^2}{M_Z^2} - \frac{1}{2} \frac{M_{H^0_1}^2}{M_{Z'}} - \frac{1}{2} \frac{M_{H^0_1}^2}{M_{Z}} \right) \times \left( \frac{1}{2} + \frac{1}{4} \frac{M_{Z'}^2}{M_Z^2} + \frac{1}{4} \frac{M_Z^2}{M_{Z'}} + \frac{1}{4} \frac{M_{H^0_1}^2}{M_{Z'}} - \frac{1}{2} \frac{M_{H^0_1}^2}{M_Z} - \frac{1}{2} \frac{M_{H^0_1}^2}{M_{Z'}} \right), \quad (24)
\]
\[
\Gamma_{H^0_1 \rightarrow Z''Z''} = \frac{\sqrt{1 - 4M_Z^2/M_{H^0_1}^2}}{8\pi M_{H^0_1}^2} g^4(1 + 3t_W^2)(12t_W v_\eta^2 (1 + 3t_W) + v_\chi^2)^2 / 576 \pi v_\chi^2 M_{H^0_1}^4
\]
\[ \Gamma_{H^0_i\to H_0^i H_0^i} = \sqrt{1 - 4M_{H_i^0}^2/M_{H_0^i}^2} \left( \frac{\lambda_i(v_\eta^4 + v_\rho^4) + 2v_\eta^3v_\rho^2(2\lambda_4 + 2\lambda_2 + 3\lambda_1)}{v_\chi^2} \right)^2, \]  
\[ \Gamma_{H^0_i\to H_+^0 H_+^0} = \sqrt{1 - 4M_{H_+^i}^2/M_{H_0^i}^2} \left( \frac{\lambda_4 + \lambda_7)(v_\eta^4 + v_\rho^4) + 2v_\eta^3v_\rho^2(\lambda_1 + \lambda_2 + \lambda_7)}{v_\chi^2} \right)^2, \]  
\[ \Gamma_{H^0_i\to H^-_0 H^-_0} = 16\pi M_{H_0^i}^0 \times \left( \frac{(-\lambda_4v_\chi^2 + \lambda_6v_\rho^2)v_\eta^2 - 2(\lambda_5 + \lambda_8)v_\rho^4 - 2(2\lambda_1 + \lambda_8)v_\rho^2v_\chi^2 + f v_\eta v_\rho v_\chi}{v_W(v_\rho^2 + v_\chi^2)} \right)^2, \]  
\[ \Gamma_{H^0_i\to h_0 h_0} = \sqrt{1 - 4M_{h_0}^2/M_{H^0_i}^2} \left( \frac{\lambda_5 v_\rho^2 + \lambda_6v_\eta^2}{v_\chi} \right)^2. \]  
\[ \Gamma_{H^0_i\to V^- V^+} = \sqrt{1 - 4M_{V^\pm}^2/M_{H^0_i}^2} (cH\iota 0 VPM)^2 \left( 3 - \frac{M_{H^0_i}^2}{M_{V^\pm}^2} + \frac{M_{H^0_i}^4}{4M_{V^\pm}^4} \right), \]  
\[ \Gamma_{H^0_i\to U^- U^+} = \sqrt{1 - 4M_{U^\pm}^2/M_{H^0_i}^2} (cH\iota 0 UPP)^2 \left( 3 - \frac{M_{H^0_i}^2}{M_{U^\pm}^2} + \frac{M_{H^0_i}^4}{4M_{U^\pm}^4} \right), \]  
\[ \Gamma_{H^0_i\to H^0_i Z} = 4\pi M_{H^0_i}^0 \times \left( \frac{M_Z^2}{4} + \frac{M_{H^0_i}^2}{4M_{H^0_i}^2} - \frac{M_{H^0_i}^2 M_{H^0_i}^2}{2M_Z^2} + \frac{M_{H^0_i}^4}{4M_Z^2} - \frac{M_{H^0_i}^2}{2} - \frac{M_{H^0_i}^2}{2} \right), \]  
\[ \Gamma_{H^0_i\to H^0_i Z'} = 4\pi M_{H^0_i}^0 \times \left( \frac{M_{Z'}^2}{4} + \frac{M_{H^0_i}^2}{4M_{H^0_i}^2} - \frac{M_{H^0_i}^2 M_{H^0_i}^2}{2M_{Z'}^2} + \frac{M_{H^0_i}^4}{4M_{Z'}^2} - \frac{M_{H^0_i}^2}{2} - \frac{M_{H^0_i}^2}{2} \right), \]  
\[ \Gamma_{H^0_i\to H^- H^+} = \sqrt{1 - 4M_{H^\pm}^2/M_{H^0_i}^2} (cH\iota 0 HPP)^2, \]

where using (15) to (22) and putting \( i=1,2 \), we will have the total width for \( H^0_1 \) and part
of the total width for $H_2^0$. The total width of the Higgs $H_2^0$ into quarks, leptons, $Z$ $Z'$, $Z'Z'$

gauge bosons, $H_1^- H_2^+$, $H_2^- H_1^+$, $h^0 h^0$, $H_2^0 H_3^0$ higgs bosons, $V^- V^+$ charged bosons, $U^- U^+$
double charged bosons, $H_1^0 Z$, $H_1^0 Z'$ bosons and $H^- H^{++}$ double charged Higgs bosons, is given by

\[
\Gamma (H_2^0 \to \text{all}) = \Gamma_{H_2^0 \to \eta \eta} + \Gamma_{H_2^0 \to \eta' \eta'} + \Gamma_{H_2^0 \to Z'Z'} + \Gamma_{H_2^0 \to \eta' H_1^-} + \Gamma_{H_2^0 \to \eta' H_1^+} + \Gamma_{H_2^0 \to \eta' H_2^-} + \Gamma_{H_2^0 \to \eta' H_2^+} + \Gamma_{H_2^0 \to \eta' H_0^-} + \Gamma_{H_2^0 \to \eta' H_0^+} + \Gamma_{H_2^0 \to V^- V^+} + \Gamma_{H_2^0 \to U^- U^+} + \Gamma_{H_2^0 \to H^- H^{++}}.
\]

(37)

where we have for the remaining part of the $H_2^0$

\[
\Gamma_{H_2^0 \to \bar{b}b} = \frac{3 \sqrt{1 - 4 M_b^2 / M_{H_2}^2}}{16 \pi M_{H_2}^2} \frac{M_b^2 v_b^2}{v_W^2 v_H^2} (M_{H_2}^2 - 2 M_b^2), \quad (38)
\]

\[
\Gamma_{H_2^0 \to c\bar{c}(t\bar{t})} = \frac{3 \sqrt{1 - 4 M_c^2 / M_{H_2}^2}}{16 \pi M_{H_2}^2} \frac{M_c^2 v_c^2}{v_W^2 v_H^2} (M_{H_2}^2 - 2 M_c^2), \quad (39)
\]

\[
\Gamma_{H_2^0 \to \tau^- \tau^+} = \frac{\sqrt{1 - 4 M_{\tau}^2 / M_{H_2}^2}}{16 \pi M_{H_2}^2} \frac{M_{\tau}^2 v_{\tau}^2}{v_W^2 v_H^2} (M_{H_2}^2 - 2 M_{\tau}^2), \quad (40)
\]

\[
\Gamma_{H_2^0 \to Z'Z'} = \frac{\sqrt{1 - 4 M_{Z'}^2 / M_{H_2}^2}}{\pi M_{H_2}^2} \frac{M_{Z'}^2 v_{Z'}^2}{v_W^2 v_H^2} \left( \frac{3 - M_{H_2}^2}{M_{Z'}^2} + \frac{1}{4} \frac{M_{H_2}^2}{M_{Z'}^2} \right), \quad (41)
\]

\[
\Gamma_{H_2^0 \to \eta' H_1^-} = \frac{\sqrt{1 - 4 M_{H_2}^2 / M_{H_2}^2}}{4 \pi M_{H_2}^2} \left( v_{\eta} v_{\rho} (\lambda_4 - 2 \lambda_1) v_{a}^2 + v_{\rho}^2(2 \lambda_2 - \lambda_4) \right) \left( v_{\eta} v_{\rho} (\lambda_4 - 2 \lambda_1) v_{a}^2 + v_{\rho}^2(2 \lambda_2 - \lambda_4) \right), \quad (42)
\]

\[
\Gamma_{H_2^0 \to \eta' H_1^+} = \frac{\sqrt{1 - 4 M_{H_2}^2 / M_{H_2}^2}}{16 \pi M_{H_2}^2} \times \left( v_{\eta} v_{\rho} (\lambda_5 + \lambda_6) v_{a}^2 + v_{\rho}^2 v_{\chi}^2 + 2 (2 \lambda_1 - \lambda_4) v_{a}^2 + 2 \lambda_4 v_{a}^2 + f v_{\rho} v_{\chi} \right) \left( v_{\eta} v_{\rho} (\lambda_5 + \lambda_6) v_{a}^2 + v_{\rho}^2 v_{\chi}^2 + 2 (2 \lambda_1 - \lambda_4) v_{a}^2 + 2 \lambda_4 v_{a}^2 + f v_{\rho} v_{\chi} \right), \quad (43)
\]

\[
\Gamma_{H_2^0 \to h_0 h_0} = \frac{\sqrt{1 - 4 M_{h_0}^2 / M_{H_2}^2}}{4 \pi M_{H_2}^2} \left( (\lambda_6 - \lambda_5) v_{a}^2 \right), \quad (44)
\]

\[
\Gamma_{H_2^0 \to H_1^0 Z} = \sqrt{1 - \left( \frac{M_{h_0} + M_Z}{M_{H_2}^2} \right)^2} \left( v_{\eta} v_{\rho} (\lambda_5 - \lambda_6) v_{a}^2 + v_{\rho}^2 v_{\chi}^2 \right) \left( v_{\eta} v_{\rho} (\lambda_5 - \lambda_6) v_{a}^2 + v_{\rho}^2 v_{\chi}^2 \right) \left( g v_{\eta} v_{a}^2 \right) \left( M_{W} v_{\chi} \right), \quad (45)
\]

\[
\Gamma_{H_2^0 \to H_1^0 Z'} = \frac{3 \sqrt{1 - 4 M_{h_0}^2 / M_{H_2}^2}}{4 \pi M_{H_2}^2} \left( v_{\eta} v_{\rho} t_{W}^2 \right) \left( v_{\rho}^2 \sqrt{1 + 3 t_{W}^2} \right),
\]

\[
\end{align*}
\]
\begin{equation}
\times \left( \frac{M_{Z'}^2}{4} + \frac{M_{H_0}^2}{4M_{Z'}^2} - \frac{M_{H_0}^2M_{H^0}^2}{2M_{Z'}^2} + \frac{M_{H^0}^4}{4M_{Z'}^2} - \frac{M_{H^0}^2}{2} - \frac{M_{H^0}^2}{2} \right).
\end{equation}

The total width of the $Z'$ boson, whose one part was already calculated in [12], is

$$\Gamma (Z' \to \text{all}) = \Gamma_{Z' \to \pi^- \pi^+} + \Gamma_{Z' \to \ell^- \ell^+} + \Gamma_{Z' \to \gamma \gamma} + \Gamma_{Z' \to \eta \eta} + \Gamma_{Z' \to H_0^0 H_1^0} + \Gamma_{Z' \to H_2^0 H_1^0} + \Gamma_{Z' \to H_2^0 H_2^+} + \Gamma_{Z' \to H_1^0 H_2^+} + \Gamma_{Z' \to H_0^0 Z} + \Gamma_{Z' \to H_2^0 Z},$$

where $i = e, \mu$ and $\tau$, $X^\pm = V^\pm$ or $U^{\pm \pm}$ and we have for the others particles the relations

$$\Gamma_{Z' \to H_0^0 H_1^0} = \frac{\sqrt{1 - 4M_{H_0}^2/M_{Z'}^2}}{2304\pi M_{Z'}} \left( g_{W_W}^2 + 6v_\eta^2\right) \left( M_{Z'}^2 - 4M_{H_0}^2 \right),$$
$$\Gamma_{Z' \to H_2^0 H_1^0} = \frac{\sqrt{1 - 4M_{H_1}^2/M_{Z'}^2}}{2304\pi M_{Z'}} \left( g_{W_W}^2 + 6v_\eta^2\right) \left( M_{Z'}^2 - 4M_{H_1}^2 \right),$$
$$\Gamma_{Z' \to H_2^0 H_2^+} = \frac{\sqrt{1 - 4M_{H_2}^2/M_{Z'}^2}}{576\pi M_{Z'}} \left( g_{W_W}^2 + 6v_\eta^2\right) \left( M_{Z'}^2 - 4M_{H_2}^2 \right),$$
$$\Gamma_{Z' \to H_1^0 H_2^+} = \frac{\sqrt{1 - 4M_{H_2}^2/M_{Z'}^2}}{576\pi M_{Z'}} \left( g_{W_W}^2 + 6v_\eta^2\right) \left( M_{Z'}^2 - 4M_{H_2}^2 \right).$$

IV. RESULTS AND CONCLUSIONS

In the following we present the cross section for the process $e^- e^+ \to ZH_1^0$ where $i = 1, 2$, for the NLC (500 GeV) and CLIC (1000 GeV). In all calculations it will be taken the following parameters $M_{J_1} = 250$ GeV, $M_{J_2} = 350$ GeV, $M_{J_3} = 500$ GeV, $M_{J_4} = 200$ GeV, $M_{U^{\pm \pm}} = 200$ GeV, $M_{P_n} = 200$ GeV, $M_{Z'} = 600$ GeV, $\lambda_i = 1$ where $i = 1, 2, ..., 9$, $M_{H^0} = 200$ GeV where $i = 1, 2, 3$, $M_{H^\pm} = 200$ GeV where $i = 1, 2$, $M_{H^{++}} = 200$ GeV, $f = -1000$ GeV and the vacuum expectation value $w = 1000$ GeV. The mass of $M_{Z'}$ taken above is in accord with the estimates of the CDF and D0 experiments, which probes the $Z'$ masses in the 500-800 GeV range, [15], while the reach of the LHC is superior for higher masses, that is $1TeV < M_{Z'} \leq 5$ TeV, [16]. With regards to Higgs the LHC is able to discover the Higgs boson with a mass up to 1 TeV and to check its basic properties. In Fig. 1, we show the cross section $e^- e^+ \to ZH_1^0$, this process will be studied in two cases, the one where we put for the vacuum expectation value $v_\eta = 140$ GeV and the other $v_\eta = 240$ GeV, respectively. Considering that the expected integrated luminosity for both colliders will be of order of $6 \times 10^4$ pb$^{-1}$/yr and $2 \times 10^5$ pb$^{-1}$/yr, then the statistics we are expecting are the following. The first collider gives a total of $\approx 3.4 \times 10^4$ events per year for $v_\eta = 140$
FIG. 1: Total cross section for the process $e^-e^+ \rightarrow ZH_1^0$ as a function of $M_{H_1^0}$ for a $\nu_\eta = 140$ GeV at $\sqrt{s} = 500$ GeV (solid line) and $\sqrt{s} = 1000$ GeV (dashed line).

FIG. 2: Total cross section for the process $e^-e^+ \rightarrow ZH_1^0$ as a function of $M_{H_1^0}$ for a $\nu_\eta = 240$ GeV at $\sqrt{s} = 500$ GeV (solid line) and $\sqrt{s} = 1000$ GeV (dashed line).

GeV, if we take the mass of the boson $M_{H_1^0} = 360$ GeV. Considering that the signal for $H_1^0Z$ production will be $t\bar{t}$ and $q\bar{q}$ and taking into account that the branching ratios for both particles would be $B(H_1^0 \rightarrow t\bar{t}) = 3.6\%$ and $B(Z \rightarrow q\bar{q}) = 69.9\%$, see Figs. 5 and 6, we would have approximately 855 events per year. Comparing this signal with the standard model background, like $e^-e^+ \rightarrow W^-W^+, ZZ$, we note that this background can be easily distinguished and therefore eliminated by measuring the transverse mass of the two pairs of jets, see [17], but even so there is another small background, such as $e^-e^+ \rightarrow WWZ$, but
FIG. 3: Total cross section for the process $e^- e^+ \rightarrow Z H^0_2$ as a function of $M_{H^0_2}$ for a $v_\eta = 140$ GeV at $\sqrt{s} = 500$ GeV (solid line) and $\sqrt{s} = 1000$ GeV (dashed line).

FIG. 4: Total cross section for the process $e^- e^+ \rightarrow Z H^0_2$ as a function of $M_{H^0_2}$ for a $v_\eta = 240$ GeV at $\sqrt{s} = 500$ GeV (solid line) and $\sqrt{s} = 1000$ GeV (dashed line).

the cross section for this process is suppressed by at least $\alpha/\sin^2 \theta_W$ relative to the process involving a double gauge boson, so using the COMPHEP \cite{18}, the total cross section for this process will be equal to $4.23 \times 10^{-2}$ pb. The second collider (CLIC) gives a total of $\simeq 2.2 \times 10^4$ events per year if we take the same neutral Higgs mass, that is $M_{H^0_1} = 360$ GeV and considering the same branching ratios for the $H^0_1$ and the Z cited above, we would have nearly 553 events per year, for the signals and backgrounds see also \cite{17}. In Fig. 2, we show the cross section for the production of the same particles as in Fig. 1, in the colliders.
NLC and CLIC for \( v_\eta = 240 \) GeV and with \( M_{H^0_1} = 360 \) GeV. We see from these results that we can expect for the first collider a total of \( \simeq 1.05 \times 10^7 \) events per year. For the second collider, the CLIC, we expect a total of \( 2.9 \times 10^5 \) events per year, that would be more than enough to establish the existence of the \( H^0_1 \). It is interesting to note the difference between the cross section for \( v_\eta = 140 \) GeV and for \( v_\eta = 240 \) GeV, this difference is due to the coupling constant, see (16). In Fig. 3, it is shown the cross section for the production of \( e^-e^+ \rightarrow H^0_2Z \), for \( v_\eta = 140 \) GeV with mass of \( M_{H^0_2} = 360 \) GeV. We see from these results that we can expect for the first collider a total of \( \simeq 6.6 \times 10^4 \) events per year to produce \( H^0_2Z \). Taking into account that the \( H^0_2 \) and \( Z \) will decay in \( t\bar{t} \) and \( \ell^-\ell^+ \), see Figs.
7 and 8, and considering that the branching ratios for them are $B(H_2^0 \rightarrow t\bar{t}) = 21.17\%$ and $B(Z \rightarrow \ell^-\ell^+) = 3.36\%$, then we will have a total of $\simeq 469$ events per year, however this events will be affected by backgrounds such as $e^-e^+ \rightarrow q\bar{q}, WW, ZZ$ production, see [17]. For the second collider, the CLIC, we expect a total of $2.4 \times 10^4$ events per year for the mass of $H_2^0$ equal to 700 GeV and $v_\eta = 140$ GeV, considering now that the channel of decay will be $Z \rightarrow q\bar{q}$ and $H_2 \rightarrow ZZ'$ with $Z \rightarrow b\bar{b}$ and $Z' \rightarrow e^-e^+$, which branching ratios are equal to $B(Z \rightarrow b\bar{b}) = 15.45\%$ and $B(Z' \rightarrow e^-e^+) = 5.9\%$, see Figs. 9 and 10, we will have a total of $\simeq 153$ events per year, that is if we are looking for the signal $jj b\bar{b} e\bar{e}$, we could discover the $H_2^0$ and $Z'$, the backgrounds for this signal can be $WZZ, HZZ$, while the cross sections are
FIG. 9: Branching ratios for the $Z'$ decays as a functions of $M_{Z'}$ for $v_\eta = 140$ GeV.

FIG. 10: Branching ratios for the $Z'$ decays as a functions of $M_{Z'}$ for $v_\eta = 140$ GeV.

so small $\propto 10^{-2}$ a detailed simulation of Monte Carlo must be done in all cases to extract the signal from the background.

Fig. 4 exhibits the total cross section for the production of the same particles as in Fig. 3, in the colliders NLC and CLIC for $v_\eta = 240$ GeV. We see from these results that we can expect for the first collider a total of $\simeq 1.5 \times 10^4$ events per year for $M_{H_2^0} = 360$ GeV. This cross section is smaller compared with that of Fig. 3 by a factor of 0.227. This difference between the cross section for $v_\eta = 140$ and $v_\eta = 240$ is due to the coupling constant (17). If we want to look for a signal such as $e^-e^+ \rightarrow H_2^0 Z \rightarrow t\bar{t} \ell^-\ell^+$ we must multiply $469 \times 0.227$ that gives 106 events. We also have that the CLIC can produce a total of $5.3 \times 10^3$ for
the mass of $M_{H_2} = 700$ GeV and for $\nu_\eta = 240$ GeV, that is, this cross section is smaller by a factor of 0.22 compared with the same process but for $\nu_\eta = 140$ GeV, then the signal $e^- e^+ \rightarrow H_2^0 Z \rightarrow ZZ' Z \rightarrow q\bar{q}(b\bar{b} e^- e^+)$ would give a total of $\approx 34$ events per year. So, we can conclude that the branching fraction measurements could tell us if the Higgs is standard or not.

We can also produce the Higgs bosons via the W-fusion, in which the Higgs bosons are formed in WW collisions and in association with neutrinos, that is

$$e^+ e^- \rightarrow H + \nu\bar{\nu},$$

two mechanisms are responsible for this production, namely, Higgs-strahlung with Z decays to the three types of neutrinos and WW fusion $[17, 19, 20, 21, 22, 23]$, being this last the dominant one for larger Higgs mass. Detailed analysis of this production will be given elsewhere $[24]$.

In summary, we have shown in this work that in the context of the 3-3-1 model the signatures for neutral Higgs bosons can be significant in both the NLC and in the CLIC colliders, however a detailed simulation of Monte Carlo must be done in all cases.

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Figure 1

\[ e^{-}e^{+} \rightarrow ZH_{1}^{0} \]

\[ \sigma \, (\text{pb}) \]

\[ M_{H_{1}} \, (\text{GeV}) \]
Figure 2

\[ e^{-}e^{+} \rightarrow ZH_{1}^{0} \]
Figure 3

$e^-e^+ \rightarrow ZH_2^0$

$\sigma (pb)$

$M_{H_1}(GeV)$

- $\sqrt{s} = 500$ GeV
- $\sqrt{s} = 1000$ GeV
Figure 4

\[ e^-e^+ \rightarrow ZH_2^0 \]

\[ \sigma (\text{pb}) \]

\[ M_{H_2} \ (\text{GeV}) \]
Figure 5

![Graph showing BR(He) vs. M_H (GeV) with various lines representing different processes such as b \bar{b}, c \bar{c}, t \bar{t}, \tau \bar{\tau}, ZZ, W^+ W^-, ZZ, Y^+ Y^-, U^+ U^-)]
Figure 7

![Graph showing BR(H_s) vs. M_{H_s} (GeV) with various decay modes and mass values.](image)
Figure 8

[Graph showing BR(Hz) vs. MH (GeV) with various lines representing different Higgs bosons such as H^+, H^-, H^0, H^0, Z, H^0, Z', and H^+ H^-]
Figure 10