High oxide-ion conductivity in acceptor-doped Bi-based perovskites at modest doping levels†

Lin Hao Li, Joe Kler, Anthony R. West, Roger A. De Souza and Derek C. Sinclair

A combination of impedance spectroscopy, time-of-flight secondary ion mass spectrometry and literature data are used to show that, (i) the bulk oxide ion conductivity of A-site, alkaline earth-doped BiFeO$_3$ (BF) is independent of the ionic radius of the alkaline earth ion (Ca, Sr, Ba) and, (ii) despite very different A-site environments in (Na$_{1/2}$Bi$_{1/2}$)TiO$_3$ and BF, similar high levels and optimisation of bulk oxide ion conductivity in these Bi-based tilted perovskites is achieved at modest acceptor doping levels of $\sim$1–10%. These results clearly demonstrate that optimisation of oxide ion conductivity in these materials requires concepts beyond a simple crystallochemical approach based on matching the ionic radii of acceptor dopant and host lattice ions.

Introduction

ABO$_3$ perovskite-based oxides have been widely explored for many decades due to their diverse range of functional properties. This spans from Ti$^{4+}$ (d$^0$)-containing polar dielectrics such as ferroelectric BaTiO$_3$ and piezoelectric Pb(Zr,Ti)O$_2$ to Fe$^{3+}$ (d$^5$)-containing multiferroic BiFeO$_3$ and mixed Cu$^{2+}$ (d$^9$) and Cu$^{3+}$ (d$^8$)-containing high temperature superconductors such as YBa$_2$Cu$_3$O$_7$. Oxide-ion conductivity is another well-known phenomenon to occur in the perovskite lattice and many acceptor-doped phases have been investigated for the development of electrolytes and/or electrode materials in applications such as Solid Oxide Fuel Cells (SOFCs), e.g. Sr- and Mg-doped LaGaO$_3$ (LSGM)$^5$ and Sr- and Co-doped LaFeO$_3$ (LSCF)$^6$, respectively. De Souza has collated a wide range of diffusion data on oxygen vacancies in perovskites via Time-of-Flight Secondary Ion Mass Spectrometry (ToF-SIMS) and suggested that there may be a limit for such diffusion in a simple cubic perovskite lattice.$^7$ In 2014 we reported high levels of oxide-ion conductivity in undoped and lightly Mg-acceptor doped Na$_{1/2}$Bi$_{1/2}$TiO$_3$ (NBT).$^8$ Further attempts to increase the oxide-ion conductivity in NBT met with limited success despite the variety of A- and B-site acceptor dopants available.$^9$ A maximum enhancement of less than one order of magnitude was achieved using typically $<$2 at% of either A-site Sr (or Ca) or B-site Mg dopants.$^9$ The conductivity maximum was in good agreement with the model of an oxygen-vacancy diffusivity limit proposed by De Souza.$^7$

The discovery of high levels of oxide ion conduction in NBT was unexpected as it had been investigated primarily as a Pb-free piezoelectric material.$^{10}$ NBT has a rather complex crystal structure, with Na and Bi dispersed on the A-site and ferroelectricity arising from dipoles associated with Bi- and Ti-displacements.$^{11,12}$ The room temperature structure is reported as either rhombohedral (space group R3c)$^{13}$ or monoclinic (C)$^{13}$ with coexistence of rhombohedral (R) and tetragonal (space group P4bnm) polymorphs over a range of temperatures (typically $\sim$255 to 400 °C), before becoming fully tetragonal (T) and then finally cubic at and above $\sim$520 °C. The activation energy ($E_a$) for the oxide-ion conductivity changes on heating from $\sim$0.8 to 0.4 eV at $\sim$325–350 °C$^8$ and has been attributed to changes in volume fraction of co-existing R and T polymorphs.$^{14}$

Various modelling methods and studies$^{15–17}$ have been tried to improve understanding of structure–property relations in NBT with respect to oxide ion conductivity and some trends have emerged. For example, migration energy of oxide ions via saddle points in the lattice associated with two A-site cations and a B-site cation are lowest for Bi located on both A-sites compared to either Na or mixed Na–Bi A-site occupation.$^{15}$ Experimental $E_a$ values agree well with simulations for Na–Bi as the A-site saddle point cations, in good agreement with the (average) disordered arrangement of Na and Bi on the A-sites in NBT. The influence of polymorphism on $E_a$ has$^{16}$ and ordering of Na$^+$ and Bi$^{3+}$ ions on oxygen tracer diffusion$^{17}$ have given further mechanistic insights into the oxide ion conductivity. A complete explanation is still lacking however, owing mainly

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to the complexity of the crystallography and polymorphism of NBT.

These studies on NBT have led to the suggestion that other Bi-based perovskites may show similar behaviour. Unfortunately, very few Bi-based perovskites can be prepared under normal atmospheric conditions; most require high pressure synthesis such as BiMoO₃: M = Al, Sc, Mn. One notable exception is BiFeO₃ (BF) which has been widely studied as a multiferroic. Its electrical properties that include mixed ionic-electronic and oxide ion conductivity in acceptor-doped BF, depend strongly on processing conditions. High levels of oxygen permeability were reported in Sr-doped BF and Impedance Spectroscopy (IS) measurements showed the level of oxide ion conductivity in Ca-doped BF (with 3, 5 and 30 at% replacement of Ca for Bi on the A-site) is as high as that observed in the well-known fluoride-based solid electrolyte, yttrium-stabilised zirconia, YSZ. Ionic conductivity was explained on the basis of A-site Ca-doping compensated by oxygen vacancy creation \( V_0^{**} \) as follows (using Kröger–Vink notation):

\[
2\text{CaO} \xrightarrow{\mathrm{Bi}_2\text{O}_3} 2\text{Ca}^{2+} + 2\text{O}_2^{+} + V_0^{**}
\]

When processed in air, the oxygen vacancies are partially filled by uptake of oxygen from the atmosphere on cooling. This creates electron holes (h) by the following reaction:

\[
V_0^{**} + \frac{1}{2}\text{O}_2(g) \rightarrow \text{O}_2^{+} + 2\text{h}^*
\]

gives rise to high levels of p-type conductivity with \( E_a \sim 0.27-0.45 \) eV. Chemically, the electronic conduction was inferred to arise from partial oxidation of Fe³⁺ to Fe⁴⁺ ions and/or O²⁻ to O²⁻. Oxidation was suppressed by annealing in N₂ at 800 °C with subsequent cooling in N₂. Impedance measurements in N₂ showed a single arc in impedance complex plane, \( Z^* \), plots with a capacitance of a few pF cm⁻¹ for Bi₀.₉₋₀.₀₅Ba₀.₅Fe₀.₉₇₅₋₀.₅O₂. This insensitivity to composition was attributed to reduction in mobile ion diffusivity in perovskites when the acceptor dopants are close in size to that of host cations. Consequently, to predict the macroscopic level of oxide ion transport and choose an optimum dopant remains a challenge.

In this study, we use IS on N₂-annealed samples to show that A-site acceptor-doping BiFeO₃ by 5 at% Ba displays similar behaviour and levels of bulk oxide ion conduction to that reported for N₂-annealed 3–30 at% Ca-doped BF. The presence of a high capacitance, low frequency spike in \( Z^* \) plots for the N₂-annealed samples is taken as an indicator of dominant oxide-ion conductivity. Samples subjected to \(^{18}\text{O}/^{16}\text{O} \) exchange at 500 and 600 °C and subsequent ToF-SIMS analysis yielded high tracer diffusion coefficients, \( D^* \). The Nernst–Einstein equation was used to convert \( D^* \) data into bulk conductivity values, giving good agreement with extrapolated values obtained at lower temperatures by IS and provides direct evidence for oxide ion conductivity. Interestingly, the values of ionic conductivity and \( E_a \) are similar to those of optimised, acceptor-doped NBT. This indicates that, despite the complexities of oxide-ion migration pathways in the non-cubic, Bi-based NBT and BF perovskites, conductivity optimisation may be achieved by modest levels, ~1–10 at%, of A-site acceptor doping by alkaline earth (AE) elements.

### Experimental

Three series of AE-doped BF ceramics were prepared (AE = Ca, Sr and Ba). Full impedance data are given for AE = Ba (5 at%) but the results for AE = Ca, Sr showed similar characteristics and for conciseness only bulk conductivity values at 200 °C for all ceramics are given (see Fig. 6(b)). BiFeO₃ (BF) and Bi₀.₉₋₀.₀₅Ba₀.₅Fe₀.₉₇₅₋₀.₅O₂ (BF-Ba) ceramics were prepared by solid state reaction of Bi₂O₃ (99.9%, Acros Organics), Fe₂O₃ (99.9%, Sigma-Aldrich) and BaCO₃ (99%, Sigma-Aldrich), as appropriate. All reagents were pre-dried before weighing and appropriate mixtures of powders were ball milled. Calcination was carried out at 800 °C for 2 h. Pellets were sintered at 860–925 °C for 1 h depending on composition. For IS measurements, Au paste was coated (850 °C for 2 h) on opposite faces of the pellets. To measure oxide ion conductivity, Au-coated samples were annealed at 800 °C in N₂ for 6 h and cooled to room temperature in N₂ to minimise oxidation and therefore p-type electronic conductivity. IS measurements for N₂-annealed samples were made in 5% H₂, 95% N₂ atmosphere.

Phase purity was examined by X-ray diffraction (XRD) using a high-resolution STOE STADI-P diffractometer equipped with a linear position sensitive detector and Cu Kα₁ radiation. Ceramic microstructure and compositional analysis were analysed using a scanning electron microscope (SEM) Philips XL 30S FEG with an Oxford Link ISIS energy dispersive X-ray (EDS) detector. Variable temperature IS measurements were made in either a non-inductively wound tube furnace or an Oxford cryodrive 1.5 system using Solartron 1260, Solartron Modulab and Agilent E4980A instrumentation. IS data were corrected for sample geometry (thickness/area of pellet) and analysed using ZView software.

Isotope exchange experiments were carried out by first equilibrating samples in O₂ of normal isotopic abundance at the chosen temperature (500 °C or 600 °C) and oxygen partial pressure, \( p_{\text{O}_2} \) of 200 mbar. The duration of the equilibration was ten times that of the exchange, \( t_{\text{eq}} = 10t_{\text{ex}} \). The samples
were quenched to room temperature, annealed in \( ^{18}\text{O}\)-enriched \( \text{O}_2 \) (the isotope fraction in the gas phase being \( n_{x}^{*} = 0.97 \)) at the same temperature and \( p\text{O}_2 \) and quenched again to room temperature.\(^{28}\) The long penetration depths required use of the line scan technique.\(^{29}\) Exchanged samples were cut perpendicular to the original surface, the revealed cross-section was polished and then analysed \(^{30}\) using a ToF-SIMS IV machine equipped with a ToF-SIMS V analyser (IONTOF GmbH, Münster, Germany). The surface was cleaned initially by sputtering with a beam of 2 keV \( \text{Cs}^+ \) (IONTOF GmbH, Münster, Germany). The surface was cleaned initially by sputtering with a beam of 2 keV \( \text{Cs}^+ \) (IONTOF GmbH, Münster, Germany).

The chosen experimental conditions for isotope exchange—surface-limited isotope exchange from a large volume of gas into a semi-infinite medium—result in the following solution to the diffusion equation:\(^{31}\)

\[
n_{x}^{*}(t) = \text{erfc} \left( \frac{x}{2C_{\text{D}^*}^{\text{ex}}t} \right) - \exp \left( \frac{k^*}{D^*}x + \frac{k^*^2}{D^*}t \right) \cdot \text{erfc} \left( \frac{x}{2C_{\text{D}^*}^{\text{ex}}t} + k^* \sqrt{ \frac{t}{D^*} } \right).
\]

This equation expresses the isotope fraction, corrected for gas-phase and background isotope fractions, as a function of position in the solid, \( x \), in terms of the tracer diffusion coefficient of oxygen, \( D^* \), and the oxygen surface exchange coefficient, \( k^* \).

### Results and discussion

XRD patterns at room temperature for undoped BF and BF-Ba ceramics are shown in Fig. S1 (ESI†); both indexed as rhombohedral (space group \( R3cH \)) perovskites. A small amount of \( \text{Bi}_2\text{Fe}_4\text{O}_9 \) (space group \( Pbam \)) was detected in BF ceramics whereas BF-Ba ceramics appeared to be phase-pure. Refined lattice parameters were \( a = 5.572(1) \) Å and \( c = 13.852(3) \) Å for BF and \( a = 5.575(2) \) Å and \( c = 13.840(1) \) Å for BF-Ba. An SEM image shows the grain size in BF-Ba ceramics to be in the range of 0.5 to 2 \( \mu \)m, Fig. S2 (ESI†). The average relative density of sintered BF and BF-Ba pellets was 84 and 92%, respectively. For completeness, the relative density values of all AE-doped ceramics used in Impedance measurements are given in Fig. S3 (ESI†).

IS data were analysed using a combination of \( Z^* \) plots, combined spectroscopic plots of the imaginary components of impedance and electric modulus (\( Z^* \), \( M^* \)) and spectroscopic plots of the real component of the capacitance (\( C^* \)). \( Z^* \) plots were used to overview the dominant impedances in the samples and seek evidence for oxygen diffusion/electrode effects in low frequency data at higher temperatures.\(^{24}\) \( Z^* \), \( M^* \) plots were used to identify unequivocally the bulk response and extract bulk conductivity, \( \sigma_b \), data from \( M^* \) peak maxima.\(^{32}\) \( C^* \) plots gave capacitance values for the different impedance components.

IS data for a sample that was \( \text{N}_2 \)-annealed, BF-Ba(\( \text{N}_2 \)), and subsequently measured in 5% \( \text{H}_2 \), 95% \( \text{N}_2 \), are shown in Fig. 1. \( Z^* \) data show two broad, depressed arcs with an inclined spike at lowest frequencies, Fig. 1(a) and (b). \( Z^* \), \( M^* \) plots in Fig. 1(c) and (d) show a high frequency \( M^* \) peak that is coincident with the high frequency \( Z^* \) peak and therefore, the high frequency \( Z^* \) arc represents the bulk response. \( C^* \) data in Fig. 1(e) and (f) show a high frequency plateau with a value of approximately.

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**Fig. 1** \( Z^* \) plots, combined \( Z^* \) and \( M^* \) spectroscopic plots and \( C^* \) plot for \( \text{N}_2 \) annealed \( \text{Bi}_{0.95}\text{Ba}_{0.05}\text{FeO}_2.975 \) ceramics at 300 °C (a), (c) and (e), 200 °C (b), (d) and (f), respectively.
10 pF cm$^{-1}$ representing the bulk response. At lower frequencies, a broad dispersion terminating in a plateau at about 10 nF cm$^{-1}$ is seen and is attributed to a combination of a grain boundary impedance and the sample-electrode impedance associated with oxygen transfer across the interface. At the lowest frequencies, the $C'$ data show a further increase to values as high as 20 $\mu$F cm$^{-1}$ and are attributed to the onset of a Warburg impedance associated with diffusion of oxygen molecules towards/away from the sample-electrode interfaces.

These $C'$ data demonstrate clearly that the BF-Ba(N$_2$) sample is an oxide ion conductor. Our focus here is on the bulk response and therefore, detailed circuit fitting to extract grain boundary and electrode impedances has not been carried out. This IS response is similar to that reported for Ca-doped BF under similar annealing conditions$^{24}$ which was also attributed to oxide ion conduction. An Arrhenius plot of $\sigma_b$ data obtained from $M''$ spectra for BF-Ba(N$_2$) is shown in Fig. 2 together with $\sigma_b$ data obtained for other AE-doped BF samples prepared in this study and also $\sigma_b$ data reported for Ca doped BF by Maso and West.$^{24}$ The Arrhenius plots for all of these compositions are very similar. $E_a$'s are in the range 0.69–0.95 eV, similar to those for good oxide ion conductors such as 8YSZ.

Results for BF-Ba processed in air, BF-Ba(air), are shown in Fig. 3. There are two main differences from the BF-Ba(N$_2$) data...
sets, Fig. 1. First, the BF-Ba(air) resistances are much lower and consequently, measurements at sub-ambient temperatures were required to show all the features in the $Z^*$ plots, Fig. 3(a–c), and access the high frequency, bulk $M''$ peak (d). Second, the prominent low frequency dispersion in $C'$ data was largely absent, with values smaller than 10 nF cm$^{-2}$/C$^0$, Fig. 3(i). It is concluded that BF-Ba(air) is predominantly an electronic conductor, therefore. The oxide ion conductivity seen in the BF-Ba(N$_2$) data sets is, of course, still present in BF-Ba(air) but is swamped by the much higher electronic conductivity. The only difference between the two samples is their heat treatment history; since BF-Ba(air) was treated in an atmosphere of relatively, much higher $p$O$₂$, the samples had absorbed O$_2$ according to eqn (2) and therefore, their observed bulk electronic conductivity was p-type.

Data for $\sigma_0$ obtained from the bulk $M''$ peaks are shown in Fig. 4, together with $\sigma_0$ data for BF-Ba(N$_2$). The remarkable change in bulk conductivity properties with atmosphere of BF-Ba indicates that, in a plot of $\sigma_0$ vs. $p$O$_2$, the samples would be at the cross-over from the electrolytic domain, BF-Ba(N$_2$) to the p-type domain, BF-Ba(air). The conductivities for the two domains differ by several orders of magnitude, especially at low temperatures because of their different $E_p$. The transport number of oxide ions, $t_o$, in the p-type domain is very small but temperature-dependent and can be estimated from the ratio of the conductivities if it is assumed that the level of oxide ion conductivity is relatively similar in the two samples. For example, at room temperature, the ratio of the extrapolated conductivity values is $\sim 10^4$:1 and therefore, $t_o$ is estimated as $\sim 1 \times 10^{-2}$ in BF-Ba(air).

The behaviour of acceptor-doped BF and NBT materials towards increasing $p$O$_2$ are very different. For BF materials, the onset of p-type behaviour occurs very rapidly if air is not excluded from BF-Ba(N$_2$) samples, for instance during IS measurements. For NBT samples, however, the electrolytic domain extends to much higher $p$O$_2$ and the materials are stable oxide ion conductors in air. The two sets of materials contain oxygen vacancies but only BF-based materials absorb O$_2$ readily. The reason may be the ready availability of the Fe$^{4+}$ state in BF, permitting easy activation of the Fe$^{3+}$/O$_2$ redox couple, whereas there is no corresponding couple associated with Ti$^{4+}$ in NBT. The O$^{2-}$/O$^-$/O$^2-$ couple may also be involved but it is not obvious why this should be activated in BF but not in NBT. A third possibility is that higher levels of the valence band electronic states in BF involve cation–anion hybridisation associated with contributions from the Fe 3d and Bi 6s/6p (lone pair) orbitals as well as O 2p orbitals. The p-type conductivity is an activated process, however, with $E_a$ around 0.2 eV and therefore, the holes are localised rather than delocalised in a valence band.

ToF-SIMS measurements on BF-Ba ceramics that were exchange-annealed in 200 mbar O$_2$ at 500 and 600 $^\circ$C revealed $D^*$ values in the range (1–5) $\times$ 10$^{-8}$ cm$^2$ s$^{-1}$, Fig. 5, with an $^{18}$O penetration depth of $\sim$ 200 microns at 600 $^\circ$C. As the grain size in BF-Ba ceramics is $\sim$ 0.5–2 $\mu$m, Fig. S2 (ESI†), the tracer species encounter numerous grains and grain boundaries. These $D^*$ values are of the same order of magnitude as reported for Mg-doped NBT$^8$ and LSGM.$^{14}$

The conductivity values calculated using the Nernst–Einstein equation on data from $D^*$ at 500 and 600 $^\circ$C for BF-Ba are shown...
in magnitudes of in this study and ref. 24 are shown in Fig. 6(b). The similarity in the mechanism(s) responsible.

... further studies are required to elucidate optimisation of oxide-ion conductivity in these Bi-based tilted perovskites requires concepts beyond a simple crystallochemical approach based on matching the ionic radii of acceptor dopant and host ions, as suggested by Zhang et al. Octahedral tilting, variations in local structure and acceptor-vacancy trapping can all potentially influence the concentration and mobility of the (mobile) oxide ions and further studies are required to elucidate the mechanism(s) responsible.

Conflicts of interest

The authors declare no conflict of interest.

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