DECIBEL: Improving Audio Chord Estimation for Popular Music by Alignment and Integration of Crowd-Sourced Symbolic Representations

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Abstract

Automatic Chord Estimation (ACE) is a fundamental task in Music Information Retrieval (MIR), which has applications in both music performance and in research on other MIR tasks. The ACE task consists of segmenting a music recording or score and assigning a chord label to each segment. ACE has been a task in the MIREX competition for 10 years, but is not yet a solved problem: current methods seem to have reached a glass ceiling. Moreover, many recent methods are trained on a limited data set and consequently suffer from overfitting. In this study, we propose DEcibel\textsuperscript{1} (DEtection of Chords Improved By Exploiting Linking symbolic formats), a novel system that utilizes multiple symbolic music representations in addition to audio in order to improve ACE on popular music.

The main input for DEcibel not only consists of the audio file, but also contains a set of MIDI and tab files that are obtained through web scraping and manually matched to the audio file. Given the audio file and matched MIDI and tab files, the system first estimates chord sequences from each file, using a representation-dependent method. For audio files, DEcibel uses existing state-of-the-art audio ACE techniques: in our experiments, we use the output of the nine ACE submissions from MIREX 2017 and/or 2018, as well as a commercial state-of-the-art method. MIDI files are first aligned to the audio file, using a Dynamic Time Warping-based method; subsequently, chord sequences are estimated from the re-aligned MIDI files using an algorithm based on template matching. Tab files are first parsed, resulting in untimed chord sequences and then aligned to the audio, using an existing algorithm based on a Hidden Markov Model. In a final step, DEcibel uses a data fusion method that integrates all estimated chord sequences into one final output sequence.

The main contributions of this study are twofold. First, by aligning different symbolic formats to audio, DEcibel automatically creates a heterogeneous harmonic representation that enables large-scale cross-version analysis of popular music. Second, our results show that DEcibel’s data fusion method improves each of the ten evaluated state-of-the-art audio ACE methods in terms of estimation accuracy. Exploiting the musical knowledge that is implicitly incorporated in MIDI and tab files, it breaks the observed glass ceiling, without requiring a lot of additional training, thereby prohibiting further overfitting to the existing chord annotations.

\textsuperscript{1}An implementation of DEcibel is available on https://github.com/DaphneO/DEcibel.
Chapter 1

Introduction

Automatic Chord Estimation (ACE)\(^1\) is a fundamental problem in Music Information Retrieval. The ACE task is concerned with estimating chords in audio recordings or symbolic representations of music. Basically, ACE segments a song in such a way that the segment boundaries represent chord changes and each segment has a chord label. This is typically represented by a sequence of (start time, end time, chord label) 3-tuples.

Figure 1.1 shows an example of such a chord sequence. We see that the first 2.6 seconds of this song do not contain any chords, hence the no-chord symbol N. This no-chord segment is followed by a 8.8 second segment in which an E major chord sounds, followed by an A major chord, etcetera.

\[
\begin{align*}
0.000000 & \quad 2.612267 \quad N \\
2.612267 & \quad 11.459070 \quad E \\
11.459070 & \quad 12.921927 \quad A \\
12.921927 & \quad 17.443474 \quad E \\
17.443474 & \quad 20.410362 \quad B \\
20.410362 & \quad 21.908049 \quad E \\
21.908049 & \quad 23.370907 \quad E:7/3 \\
23.370907 & \quad 24.856984 \quad A \\
24.856984 & \quad 26.343061 \quad A:min/b3 \\
26.343061 & \quad 27.840748 \quad E \\
27.840748 & \quad 29.350045 \quad B
\end{align*}
\]

Figure 1.1: Chord sequence annotation for the beginning of the Beatles song *I Saw Her Standing There*. This is a sequence of (start time, end time, chord label) 3-tuples.

A chord can be defined as multiple notes that sound simultaneously. As we will see in Section 2.4.1, any chord can efficiently be represented by a text string (for example the chord labels in Figure 1.1: E, A, B, E:7/3 and A:min/b3). The progression of chords through time defines the harmonic structure of a piece of music. Therefore, the estimation of chords in a music piece has many applications in both music performance and in Music Information Retrieval (MIR), as described below.

For music students, it is common to play along with songs on on-line streaming services like YouTube (Stowell and Dixon, 2011). ACE can make this easier for the less experienced musician. Chordify\(^2\) is a web-service that uses ACE techniques to display the chords of any audio file to the user. From the fact that Chordify is used by 1.5 million users every month (Bountouridis et al., 2016), we can conclude that there is great interest in systems using ACE.

Chord sequences have also been used by the MIR research community in high-level tasks such as cover song identification (Khadkevich and Omologo, 2013), key detection (Papadopoulos and Tzanetakis, 2012), genre classification (Ajoodha et al., 2015), lyric interpretation (Kolchinsky et al., 2017) and audio-to-lyric alignment (Mauch et al., 2012). To conclude, a well-performing ACE system, which estimates reliable chord sequences, would be of great use for both music performers and MIR researchers.

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\(^1\) ACE is also referred to as Chord Recognition, Automatic Chord Transcription or Automatic Chord Detection.

\(^2\) https://chordify.net/
1.1 Stagnation and subjectivity

Fujishima (1999) was the first who considered ACE as a problem on its own and since this pioneering publication, many researchers have worked on the task. Despite these efforts in the past two decades, ACE is not yet a solved problem.

ACE has been a task in the annual benchmarking evaluation Music Information Retrieval Evaluation eXchange (MIREX) since 2008. The main evaluation measure is Weighted Chord Symbol Recall (WCSR), which reflects the proportion of correctly labeled chords in a data set, weighted by the total length of the data set. State-of-the-art ACE methods yield WCSR of around 80%, given a chord vocabulary of major and minor chords. However, from recent MIREX results, Humphrey and Bello (2015) observe a stagnation in ACE performance. Scholz et al. (2016) give two suggestions to recover from this stagnation: ACE methods should either make better use of musical expert knowledge, or they should use new techniques, for example deep learning, instead of relying on the small set of commonly used techniques.

Besides, Humphrey and Bello (2015) throw light on another issue of ACE: chord annotations are inherently subjective. Even between musically trained human annotators, there can be a discrepancy of over 15% in the chord annotation of a song. This subjectivity matter was earlier identified by Ni et al. (2013), who asked 5 musicians to each annotate the same 20 songs and show a 10% discrepancy between the annotations. More recently, Koops et al. (2019) introduced a 50-song data set of popular music, annotated by 4 professional musicians, and found only 73% overlap on average for the traditional major-minor vocabulary. The currently common practice to evaluate ACE by comparing the results to a single reference annotation is disputed by Humphrey and Bello (2015); Ni et al. (2013) and Koops et al. (2019). Ni et al. (2013) and Koops et al. (2019) even claim that modern ACE systems have started to overfit the MIREX data set, mimicking the subjective aspects of MIREX’s reference annotations. Although none of these papers presents a practical, scalable solution to the subjectivity issue, it becomes clear that subjectivity in ACE is an important issue that is often overlooked in existing research.

In conclusion, there is need for a new strategy that overcomes existing stagnation in ACE without further overfitting to existing (subjective) data sets. In this study, we propose a novel method that uses MIDI and tab files, which implicitly contain crowd-sourced musical knowledge, to improve existing state-of-the-art methods, requiring a minimal amount of additional training.

1.2 Research goal

The aim of this research is to show that audio ACE can be improved by exploiting symbolic representations of popular music. For this purpose, we designed and implemented DECIBEL (DEtection of Chords Improved By Exploiting Linking symbolic formats). DECIBEL is a novel system that exploits multiple heterogeneous symbolic music representations for improving ACE. MIDI and tab files can be considered as crowd-sourced note and chord transcriptions respectively. By using these symbolic representations, DECIBEL implicitly integrates musical knowledge into existing ACE methods, which may be a strategy to overcome the stagnation issue identified in the previous section. As DECIBEL only relies to a small extent on training on reference annotations, our method prohibits further overfitting to existing data sets. To evaluate DECIBEL, we compare its performance to state-of-the-art ACE systems submitted in the MIREX competitions of 2017 and 2018, as well as a commercial ACE method. DECIBEL improves each of the tested ACE systems.

1.3 Related work

Our work builds on previous approaches to integrate symbolic music and audio in the chord estimation task, as we will see in this section.

Ewert et al. (2012) introduce a cross-version analysis framework for comparing harmonic analysis results from different musical domains. After collecting a MIDI file for each audio file in a 112-song subset of the Isophonics
(Mauch et al., 2009; Harte, 2010) data set, they use two state-of-the-art chord recognition methods for MIDI data and align each MIDI file to the corresponding audio recording. This way, they create a harmonic representation for each of the 112 songs, which contains three chord label sequences: the ground truth labels and the re-aligned outputs that were obtained by the two MIDI chord recognition systems. They show that this harmonic representation can be used for quantitative evaluation of MIDI chord recognition methods, using annotations for corresponding audio recordings. In addition, by visualizing this harmonic representation, they demonstrate how it can be used for qualitative error analysis of automatically generated chord labels, and by that contribute to the understanding of an ACE algorithm’s behavior and the properties of the underlying music material. The research by Ewert et al. lays the foundation for the work proposed in this study, in which we expand the harmonic representation with chord labels from multiple MIDI and tab files for each audio recording and show how this enriched harmonic representation can be used to improve ACE.

The integration of tab files and audio with respect to chord estimation was earlier researched by McVicar and De Bie (2010) and McVicar et al. (2011a,b). In these three papers, they show that a HMM-based system for audio ACE can be significantly improved by incorporation of external information from guitar tabs. In a preprocessing step, they obtain a set of tab files by a web scrape and consequently parse them. In the resulting format, to which they refer as Untimed Chord Sequences (UCSSs), only the chord labels and line information of each tab is retained. As a next step, they align each UCSS to the corresponding audio file. For this purpose, the authors introduce four variations on the traditional Viterbi algorithm. The most promising variation is Jump Alignment, which aligns the UCSS to the audio file, thereby allowing jumps from the end of any annotation line to the beginning of any line. We implemented Jump Alignment as part of the DECIBEL system and will explain the implementation more thoroughly in Section 6.2.

The integration of heterogeneous output of multiple ACE algorithms was proposed by Koops et al. (2016). The authors experiment with three different techniques to combine chord sequence estimates from different sources (the MIREX 2013 ACE submissions, applied to the Billboard data set) into one final output sequence for each song. They show that their data fusion method yields the best results in terms of WCSR. Also, they show that the output sequence found by their data fusion method is an improvement to the best scoring team. In our study, we use a similar data fusion method to combine the chord labels obtained from audio, MIDI and tab files.

1.4 Outline

The remainder of this study is structured as follows: Chapter 2 provides the required music theory and terminology information in order to understand the concepts that will be used in the remainder of this study. In Chapter 3, we describe DECIBEL’s framework. As we will see in this chapter, DECIBEL consists of four subsystems: three of these subsystems compute chord labels in their own representation-specific way and the fourth subsystem combines these results in a data fusion step. The audio, MIDI and tab subsystems are described in Chapters 4, 5 and 6 respectively. DECIBEL’s data fusion strategy is described in Chapter 7. Finally, we will present our conclusions in Chapter 8.
Chapter 2

Musical background

This chapter gives an introduction to pitch, music notation, intervals and chords. The material in Section 2.1 to 2.4 is based on Taylor (1989) and (Müller, 2015, Chapter 1 and 5). Section 2.5 describes the three music representations we consider in this research: audio, MIDI and tabs.

2.1 An introduction to pitch

Music consists of tones, and each tone has some properties, for example its duration, start time and pitch. Pitch refers to the degree of highness of sound. If you hit a key on the left side of the piano and subsequently strike a key on the right, the second produced tone will be higher pitched than the first one. Similarly, men’s voices are generally lower pitched than women’s voices and a tuba sounds lower than a piccolo.

2.1.1 Pitch in physics: waves and frequencies

From a physical point of view, sound is generated by vibrating objects, for example the string and soundboard of a violin or the vocal cords of a singer. These vibrations cause displacements and oscillations of air molecules, resulting in local regions of compression and rarefaction. This alternating pressure travels through the air as a longitudinal wave, from its source to a perceiver.

The change in air pressure at a certain location can be graphically represented by a waveform of the sound. A waveform plots the deviation of the air pressure from the average air pressure over time.

If the points of high and low air pressure repeat in an alternating and regular fashion, the resulting waveform is called periodic. The period is defined as the amount of time that is required for completing a cycle. The frequency is the reciprocal of period, and is measured in Hertz (Hz). For example, a period of 2.5 ms corresponds with a frequency of \( \frac{1}{0.0025} = 400 \text{ Hz} \). The higher the frequency of a sinusoidal wave, the higher the corresponding tone sounds.

However, real-world sounds, such as the tones that are produced by a musical instrument, are much more complex than a pure tone resulting from a single sinusoid. A musical tone can be described as a superposition of sinusoids, each with their own frequency. A partial is any of the sinusoids by which a musical tone is described. The frequency of the lowest partial present is called the fundamental frequency of the sound. The pitch of a musical tone is usually determined by the fundamental frequency.

Two tones with fundamental frequencies in a ratio equal to any power of two, are perceived as similar. All tones with this kind of relation can be grouped in the same pitch class. The distance between one musical tone and another tone with half or double its fundamental frequency is called an octave. For example, a tone with a frequency of 440 Hz sounds similar to a tone with a frequency of 220 Hz. These tones are an octave apart and belong to the same pitch class.
2.1.2 Twelve-tone equal-temperament

We have seen that pitch and frequency are closely related, but musicians typically do not specify the height of a tone in Hertz. Instead, the space of all different pitches is discretized using a tuning system. Although many different tuning systems have been suggested and used in history, the standard tuning in modern Western music, which is the tuning used in this research, is twelve-tone equal-tempered tuning. This tuning system is the standard system used as basis for tuning the piano.

In the twelve-tone equal-tempered tuning system, an octave is divided into twelve scale steps - often simply referred to as tones. The fundamental frequencies of these steps are equally spaced on a logarithmic frequency axis, as the human perception of pitch is logarithmic in nature. This means that the frequency ratio of two subsequent scale steps is constant and equals $2^{\frac{1}{12}} \approx 1.059463$. The distance, or interval, between two subsequent scale steps is called a semitone. In other words, if we multiply the frequency of an arbitrary pitch by $2^{\frac{1}{12}}$, this pitch is raised by a semitone.

These semitones can be further divided into cents. By definition, each octave is divided into 1200 cents, so a semitone consists of 100 cents. The frequency ratio of two subsequent cents equals $2^{\frac{1}{1200}} \approx 1.0005777895$. Note that both the cent and the semitone are logarithmic measures of distance between pitches.

2.1.3 Note names and octave numbers

In Section 2.1.1, we have seen that two tones that differ in pitch by one or more octaves can be grouped in the same pitch class and in Section 2.1.2 we learned that the twelve-tone equal-tempered tuning system divides the octave into twelve steps of one semitone. We can therefore deduce that there are twelve pitch classes.

In modern Western music notation, each pitch class has a pitch class name or note name, which consists of a letter and possibly an accidental. There are seven pitch classes which can be named by just one letter from \{A, B, C, D, E, F, G\}. These pitch classes correspond to the white keys of the piano, as illustrated in Figure 2.1. The remaining five pitch classes are named by a combination of a letter and an accidental. An accidental raises or lowers the corresponding note. The most common accidentals are the sharp (♯) and flat (♭), which respectively raise and lower the note with a semitone. So the black key on the piano positioned between the C- and D-keys produces a note that can be denoted by either C♯ or D♭. Similarly, the other “black-key” pitch classes can be referred to by either \{D♯, F♯, G♯ and A♯\} or \{E♭, G♭, A♭ and B♭\}. We see that two different names can refer to the same pitch class. This phenomenon is called enharmonic equivalence.

Following Scientific Pitch Notation, a pitch is not only specified by the pitch class name, but also by an octave number. The higher the octave number, the higher the pitch. For instance, an A1 sounds an octave higher than an A0, which is the lowest tone that can be produced by most pianos. The note A4 has a frequency of 440 Hz in modern twelve-tone equal-tempered tuning and is used as a reference note for tuning.

Note that the distance between notes denoted by two subsequent letters is not always the same. For example, D4 and E4 differ by two semitones: in Figure 2.1 we see that there is a distance of two piano keys, so two semitones, between D and E. On the other hand, E4 and F4 are just one semitone apart: there is no black key on the piano between these notes.
2.2 Music notation

Music is notated on a staff, which consists of five parallel horizontal lines, counted from the bottom, see Figure 2.2. Notes can be notated on the lines or between them. The pitch of a note is determined by its vertical position on the staff, combined with the clef. The two most common clefs are the treble clef or ‘G’ clef (♮) and the bass clef or ‘F’ clef (♭). The working of these clefs is illustrated in Figure 2.3: if there is a treble clef at the beginning of the staff, this means that the note on the second line is G4. By way of illustration, this note is colored red. When using the bass clef, the note that is placed on the fourth line is F3 - colored blue.

If notes lie above or below the limits of the staff, short additional lines called ledger lines are used. We see for example that we need one ledger line for the notation of C4 in the treble clef as well as in the bass clef. As ledger lines deteriorate the readability of sheet music, it is common to use the treble clef for high notes (C4 and higher) and use the bass clef for lower notes.

2.3 Intervals

Now that we have become acquainted with tones, pitches and their notation, it is time to introduce the notion of intervals. An interval is the distance between two pitches. We already know that, assuming twelve-tone equal-tempered tuning, we can divide the octave in twelve semitones. Based on the notion of semitone, we can specify other intervals that are used in Western music theory.

Interval names consist of a number and a quality. In counting the number, both notes are included. For example when determining the interval from C4 to F4, we count four notes (C4, D4, E4, and F4), so this interval is called a fourth. Similarly, the interval from E4 to C5 is a sixth. The interval from one note to another note with exactly the same pitch is a unison.

Traditionally, intervals are named on the basis of the major scale, which consists of seven notes and an eighth note one octave apart from the first note. In the major scale, there is only one semitone difference between note 3 and 4 and between note 7 and 8, while there are two semitones difference between all other subsequent notes. An example of a major scale is C major: C - D - E - F - G - A - B - C. In Figure 2.4 we see the full names of all intervals between C, which is the root note of the scale, and each of the other notes. In each major scale, the intervals unison, fourth, fifth and octave get the quality “perfect”, while the intervals second, third, sixth and seventh get the quality “major”.

Using only perfect and major intervals, we cannot express all different intervals. For instance, we have no name yet for an interval of three semitones. We can solve this by raising or lowering the upper note of the interval
Figure 2.4: The eight intervals of the major scale. Note that the distance between the third (E) and fourth (F) note and between the seventh (B) and eighth (C) note is only one semitone.

with a semitone, following these rules:

- Given a perfect or major interval: if either the upper note is raised a semitone or the lower note is lowered a semitone, the interval becomes **augmented**;
- Given a major interval: if either the upper note is lowered a semitone or the lower note is raised a semitone, the interval becomes **minor**;
- Given a perfect or minor interval: if either the upper note is lowered a semitone or the lower note is raised a semitone, the interval becomes **diminished**.

Figure 2.5 shows all possible major, minor, augmented and diminished intervals in (or just beyond) the octave, with their distance in semitones. Note that two different interval names can refer to the same difference in semitones, e.g. both the augmented fourth and the diminished fifth consist of six semitones. These intervals are enharmonically equivalent.

### 2.4 Chords

A **chord** can be loosely defined as a group of tones sounding at the same time. Most researchers agree that a chord should consist of tones from at least three distinct pitch classes.

Chords that consist of tones from three pitch classes are called **triads**. In Western music, most triads can be stacked in thirds and consist of the note on which the triad is based (root), plus the third and the fifth above it. The root note determines the name, while the quality of the other intervals determines the type of chord. For example: a C with a major third and a perfect fifth forms a C major chord, and a D with a minor third and a perfect fifth is a D minor chord. It is possible to extend chords by stacking more thirds upon them. **Seventh** chords consist of a “normal” triad and an added seventh, forming a tetrad. The most common seventh chord is the dominant seventh, made out of a major tetrad and a minor seventh. Figure 2.6 summarizes the most used triad and tetrad chords in Western music.

For one chord, there are many variations possible. First, there exist multiple **inversions** for each interval. When the chord’s lowest note is its root (like in the examples of Figure 2.6), the chord is said to be in **root position**. When the lowest note is the third, for example the E in a C major chord, this chord is in **first inversion**. When the lowest note is the fifth, the chord is in **second inversion**. A seventh chord can even be in **third inversion** if the seventh is the lowest note. Second, notes of the same pitch class may be doubled, for example in a C major chord consisting of C3, E3, F3 and C5. This is called **octave doubling**. Third, the notes of a chord may not be played simultaneously, but after each other. In this case, we speak of a **broken chord**.

The concept of harmony and chords is enriched by the existence of **non-harmonic tones**. These tones are not part of the chord. Instead, they are used to create a smooth melody line, to prepare the transition to another chord or to add a dissonant element, creating musical tension. Though non-harmonic tones certainly contribute to the beauty of music, they provide a challenge for ACE systems as it is difficult to automatically determine whether a given note is either harmonic of non-harmonic.
Figure 2.5: Major, minor, augmented and diminished intervals, with their distance in semitones
Figure 2.6: The most common chords based on triads and tetrads
2.4.1 Chord notation and representations

There exist various notations for chords, which can differ between and even within genres. (Taylor, 1989) In baroque music for example, the chord notation consists of a bass line with figures written underneath the notes. This notation is called figured bass and is illustrated in Figure 2.7. The figures represent the intervals that should be played above the bass note. For example: the first bar is the figured bass notation for a C major chord in root notation, and can be played like the second bar in Figure 2.7. Similarly, the figured-bass notation in the third bar means that we should add the third and the sixth to the bass note. The bass note is an E, so we add a G and C to the bass note, resulting in a C major chord in first inversion - as written out in the fourth bar. The fifth and sixth bar represent a second-inversion C major chord in figured bass and full notation respectively.

Figure 2.7: Three inversions of the C chord in figured bass notation

In Classical Harmony Analysis, chords are studied and notated in relation to the current key. This notation is called Roman numeral notation and is, unsurprisingly, characterized by Roman numerals under the chords. These Roman numerals indicate the scale degree on which the chord is built, as illustrated in Figure 2.8. In this figure, we see seven chords in the key of C major. The first chord is a C major chord. The interval between the key C and the root note of the chord (C) is a unison, so we need the Roman equivalent of the digit “1”. As a rule, major chords are capitalized, so the correct Roman numeral for this chord in this key is “I”. The second chord is a D minor chord. The key (C) and the root note of the chord (D) are a second apart and the chord is in minor, so the corresponding numeral is “ii”. The final bar in our example piece is a diminished B chord. Diminished chords are indicated with a small “0” after the Roman numeral. Similarly, augmented chords (not present in this example) are indicated with a small “+” after the Roman numeral. Note that the Roman numeral that a chord gets, is dependent on the key in which it occurs. In Figure 2.9, we see for example that a G major chord gets the Roman numeral “V” in the key of C major, while “I” is the right numeral in the key of G major.

Figure 2.8: Seven chords in the scale of C major in Roman numeral style notation notation

Yet another chord representation is used in jazz and popular music. These genres are characterized by improvisation in performance. The basic harmonies are generally quite simple, so the main purpose of the chord representation is to be easy to read and interpret. As we will see in Section 2.5.3, this chord representation is common in tabs (an alternative for regular sheet music). Figure 2.10 shows some variations of the C chord and their chord notation in jazz and other forms of popular music. The letter name of the root of the chord is shown as a capital letter. A chord is assumed to be major unless stated otherwise. Minor chords get a “m” after the chord letter; “+” or “aug.” stands for an augmented chord and a chord with a “0” or “dim.” is diminished. It is unusual to specify the bass note, so a chord without bass indication can be in any inversion. In the rare cases where the bass note is specified, it is notated with a slash after the letter name of the root of the chord.
like in the last two bars of our example. It is important to notice that there exist multiple variations of chord notation in jazz and pop music, and some of them cause ambiguity issues. For example: some musicians use the symbol $\Delta$ for major chords, so $C\Delta$ is a C major chord and $C\Delta^7$ is a C major seventh chord. Others use the $\Delta$ symbol as a synonym for major seventh chords, so they would notate the C major seventh chord as $C\Delta$. To interpret chords like $C\Delta$ correctly, one should therefore be well aware which variation of notation is applied.

![Figure 2.10: Major, minor, augmented and diminished C chords in root position; Major C chords in first and second inversion](image)

Each of the three chord notations is suitable for the genre or field of study in which they are used. However, none of them is well-suited for the chord annotations which we need in order to train and test ACE systems: they are either hard to write in flat text, key-dependent or ambiguous. **ACE chord annotations** require a unambiguous, context-independent notation that is easy to write and intuitive to interpret. Harte et al. (2005) propose a chord grammar in which millions of chords can be defined unambiguously, whereas they give a succinct short-hand notation for the most common chords. Chords names are based on their root note, independent of the present key. In this notation, the C minor chord can either be represented by its components, like $C:(b3,5)$, or by a shorthand string: $C:\text{min}$. We can also compose more complex chords using the component notation: $A:(3,5,b7,9)$ is a dominant ninth chord, consisting of A, C#, E, G and B. The asterisk is used as “omit symbol”, so $D:\text{maj7}(\ast3)$ would be equivalent to $D:(5,7)$. The bass can be specified with a slash, followed by the interval from root to bass note. A D diminished seventh chord in third inversion would be represented as $D:(b3,b5,bb7)/bb7$ or $D:\text{dim7}/bb7$. This chord grammar has become the standard notation for ACE reference annotations, including the Isophonics annotations (Mauch et al., 2009; Harte, 2010) which we use in this project.

### 2.5 Music representations

Apart from sheet music, there exist multiple other music representations. Each of them has its own way of storing pitch or chord information. In this section, we investigate the three music representations that are used in DECIBEL: audio, MIDI and tabs.

#### 2.5.1 Audio representation

Sound is generated by vibrations and travels through the air as a longitudinal wave, which can be graphically represented by a waveform (see Section 2.1.1). This waveform plots the deviation of the air pressure from the average air pressure over time. A **digital** audio representation (e.g. a .wav or .mp3 file) is an approximation of this waveform, in which the sound wave of the audio signal is digitized by sampling and quantization. (Müller, 2015, Chapter 2).

**Sampling** refers to the process of reducing a continuous-time (CT) signal to a discrete-time (DT) signal, which is defined only on a discrete subset of the time axis. The typical sampling rate for CD recordings is 44.1 kHz, so a CD has 44100 samples per second.

In **quantization**, the continuous range of possible amplitudes is replaced by a discrete range of possible values. For CD recordings, a 16-bit coding scheme is used, which allows representation of $2^{16} = 65536$ possible values.

Although the tones that are present at a given time cannot be read directly from the waveform, there exist methods to estimate them. Remember from Section 2.1.1 that a musical tone is basically a superposition of sinusoids, each with their own frequency. Using **Fourier analysis**, we can decompose our signal (the digitized waveform) into the sinusoids it consists of - and their frequencies. In the remainder of this section, we give a short summary of the discrete Fourier transform, short-time Fourier transform and Constant-Q transform. A
Figure 2.11: Three different signals (a, b, c) with the same frequency distribution yield identical Fourier transforms (d, e, f)

detailed explanation of Fourier analysis is beyond the scope of this study. For more information about Fourier transforms, we refer the reader to Müller (2015, Chapter 2).

The Fourier transform converts a signal that depends on time into a representation that depends on frequency. The formula for the discrete Fourier transform is given in Equation 2.1. $X_k$ is the $k$th Fourier coefficient, which is the amount of frequency $k$ that is present in a signal $x$. The signal $x$ consists of $N$ time samples.

$$X_k = \sum_{n=0}^{N-1} x(n) \exp\{-2\pi i kn/N\} \quad (2.1)$$

The magnitude of the Fourier transform tells us about the signal’s frequency content: if $X_k$ is high for a frequency $k$, then this frequency $k$ is important in the signal. However, we cannot infer at which time the frequency content occurs. This is illustrated in Figure 2.11: each of the three signals at the top consist of a low note (3Hz) that sounds for 5 seconds and a higher note (9Hz) that sounds for the other 5 seconds. However, signal a starts with the higher note, while in signal b this note sounds in the middle and in signal c the high note is placed at the end. Though the signals would sound different, the magnitude of the Fourier transform is exactly the same: we see peaks at 3 and 9 Hz.

The short-time Fourier transform (STFT) (Gabor, 1946) offers a solution for this problem. The STFT considers only a small part of the signal, which is dependent on the window function $w$. $w$ is a function with $w(n) \in \mathbb{R}$ if $n \in \{0, N-1\}$ and $w(n) = 0$ otherwise. $N - 1$ is the window size. The window is shifted every $H$ samples. $H \in \mathbb{N}$ is the hop size. In general, a smaller hop size gives more precise results, but is computationally more expensive than a large hop size. The choice for the perfect hop size value is therefore dependent on the application.

$$X_{m,k} = \sum_{n=0}^{N-1} x(n + mH)w(n) \exp\{-2\pi i kn/N\} \quad (2.2)$$

The formula for the STFT is given in Equation 2.2. In Figure 2.12, we see an example of the STFT with a rectangular window of 200 samples (2 seconds with a sampling rate of 100 Hz). The hop size is 200. These window and hop sizes are way to large for real-life applications, but are chosen in order to be visible in the figure.
We can visualize the intensity of frequencies over time in 2D using a spectrogram. A spectrogram is the squared magnitude of the STFT:
\[ S(m, k) = |X_{m,k}|^2 \] (2.3)

Figure 2.13 shows the spectrogram of *I Saw Her Standing There* by The Beatles. For this spectrogram, we chose a sampling rate of 22050Hz, window size of 2048 samples and hop size of 512 samples. Each point in the spectrogram represents the frequency intensity at a given time point. The warmer the color, the higher the frequency.

The STFT is a common method to extract feature information from a signal. Nevertheless, this method has some problematic properties: first, one needs to specify a window function. The window must be large enough to capture the lowest frequencies. On the other hand: the larger the window, the lower the time resolution. Another disadvantage of the STFT is that the frequencies calculated by the STFT are separated by a constant frequency difference, while we have seen that the frequencies of notes of a scale of Western music increase...
Figure 2.14: CQT spectrogram of *I Saw Her Standing There* by The Beatles. In this spectrogram, the frequencies are placed logarithmically on the *y*-axis, because the octave numbers increase linearly.

Figure 2.15: CQT chromagram of *I Saw Her Standing There* by The Beatles. In this representation, octave information is discarded, but pitch class information is retained.

exponentially. Therefore, the frequencies from the STFT do not map directly to the frequencies of music notes.

In the **Constant-Q transform** (Brown, 1991), the window size is not constant, but dependent on the coefficient \( k \): the window \( N_k \) grows with higher frequencies. Also, the frequency filters \( f_k \) are not spaced linearly (like in the STFT), but logarithmically: the \( k \)'th filter is \( f_k = \left(2^{1/b}\right)^k f_{\text{min}} \).

\[
X_{m,k} = \sum_{n=0}^{N_k-1} x(n + mH)w(k,n)\exp\left\{-2\pi i n/N_k\right\}
\]

The formula of the Constant-Q transform is given in Equation 2.4. Note the differences with Equation 2.2: the window function now has two parameters \( k \) and \( n \); the window size \( N_k \) is dependent on \( k \) and we normalize by \( N_k \) to compensate for high values at high frequencies. When choosing the right values for \( f_{\text{min}} \) (the lowest frequency we can detect) and \( b \) (the number of bins per octave), the Constant-Q transform maps directly to frequencies of musical notes.

In Figure 2.14, we see the spectrogram of the same Beatles song, but now calculated from the Constant-Q transform with \( f_{\text{min}} = 65.4\text{Hz} \) (the note C2) and \( b = 12 \). Note that the frequencies are placed logarithmically on the *y*-axis because the octave numbers increase linearly, so it is easier to see which pitches sounded at each time instance in the song. Almost every pitch has a strictly positive intensity: the lion’s share of the spectrogram’s colors is not dark blue. Many of those pitches were not played intentionally by The Beatles’ band members, but are caused by partials (any of the sinusoids of which a complex tone is composed, see Section 2.1.1).

For most MIR tasks concerning pitches, octave information can be discarded. This is also the case for **ACE**: the octave numbers are irrelevant in determining the chord from the pitches of which it is composed; we only need the pitch classes. **Chroma features** aggregate all spectral information that relates to a given pitch class into a single coefficient. There exist many variations of Chroma features, and they can be calculated from both the STFT and the Constant-Q transform. Basically, a Chroma feature is a 12-dimensional vector that can be
Figure 2.16: Structure of a MIDI file. A MIDI file has a header chunk and a number of track chunks. Each track chunk has a number of \(\langle\text{delta-time}, \text{event}\rangle\) pairs. The most interesting events for our application are note on and note off events.

obtained by summing all frequencies. Figure 2.15 shows a visualization of the chroma features of our example song. Here, we see for example that the pitch classes E and G# have high chroma values in the beginning of the song. Indeed, the song starts with a E major chord.

### 2.5.2 MIDI representation

MIDI is an abbreviation for Musical Instrument Digital Interface. It is a protocol which allows electronic instruments and other digital musical tools to communicate with each other, by sending event messages. Such an event message can for example instruct a synthesizer to start playing a certain note (by a note on event), stop playing a note (note off event) or change to another instrument sound (program change event). A MIDI file is a sequence of MIDI messages, organized in a specific format.

The information stored in MIDI files is therefore fundamentally different from the information stored in audio files: as we have seen in the previous section, audio files represent the waveform of a sound. Conversely, a MIDI file stores a list of instructions for a synthesizer, just like a musical score in a way stores instructions for a musician. The MIDI file itself does not contain any audio signals, but audio can be synthesized based on the MIDI event messages. MIDI files can thus be considered as a compact way to store a musical score and form therefore a symbolic music representation. Compared to audio, it is way easier to extract note information from MIDI. This makes MIDI particularly interesting for research in MIR and musicology.

Another difference between MIDI and audio is the file size: as MIDI stores music on a note level instead of on a sample level, MIDI files are typically much smaller than audio files. For instance, the .wav file of *I Saw Her Standing There* which we use in our data set has a size of 92.6 megabytes, while our MIDI files of the same song have file sizes ranging from just 27.3 to 28.8 kilobytes. This storage efficiency hugely contributed to the popularity of MIDI files before the advent of the compressed file format MP3. Up until now, MIDI files are still used in resource-scarce settings such as karaoke machines. This has lead to an abundance of MIDI files today. Recently, Raffel (2016) obtained as much as 178,561 MIDI files with unique MD5 checksums (i.e. a widely used 128-bit hash that is computed on a file) trough a large-scale web scrape, resulting in the “Lakh MIDI Dataset”.

The structure of a MIDI file is illustrated in Figure 2.16. A MIDI file consists of a header chunk and a number of track chunks. The header chunk specifies the number of track chunks and the duration of a tick, which is the default time unit in a MIDI file. Each track chunk has a number of \(\langle\text{delta-time}, \text{event}\rangle\) pairs. The delta-time is the time that has passed since the previous event, measured in ticks. An event is either a MIDI event, system exclusive (sysex) event or meta event. For a detailed description of these events and MIDI in general, we refer the reader to Guérin (2009). In this section, we will only consider a subset of events. The most common MIDI events in an average MIDI file are note on, note off and program change events. Note on and note off events respectively specify the start and end of a note and have a channel, pitch and velocity. Both pitch and velocity are integers between 0 and 127. A larger pitch value results in a higher sound: a pitch of zero corresponds to a C0, while the highest possible pitch (127) is the G10. If the velocity is high, a loud sound will be heard.
while a velocity of zero only produces silence. A channel can be seen as a part in a full score: each channel is at any time mapped to a program number. These programs, or patches, determine the instrument sound. For example, program 1 is the acoustic grand piano, while a channel with program 59 will play the tuba for us. The program of a channel can be changed by program change events.

Based on note on and note off events, we can easily extract a piano-roll representation of a MIDI file. This is a time-frequency visualization that strongly reminds of piano rolls for pianola or reproducing piano. The piano-roll representation of a MIDI for the Beatles song *I Saw Her Standing There* is shown in Figure 2.17. When comparing this figure to the CQT-spectrogram in Figure 2.14, it becomes clear that the piano-roll representation is much “cleaner”: thanks to the absence of partials, it is way easier to extract notes from MIDI than from audio.

Raffel and Ellis (2016a) describe the sources of information available in a MIDI file. First, MIDI files are naturally suited to be used as transcriptions of pieces of music, thanks to the way they are specified. At each position in the file, we can infer exactly which instrument plays which note. To extract this kind of information, various software libraries were developed, for example the MIDI Toolbox (Eerola and Toiviainen, 2004) and pretty_midi (Raffel and Ellis, 2014) Second, we can gather timing information from MIDI files, as there exist events for tempo changes and time signatures. Third, all 24 possible major and major keys can be specified in a key change event. Fourth, lyrics can be added to MIDI transcriptions by the use of lyrics meta-events. Finally, software libraries like jSymbolic (McKay and Fujinaga, 2006) and music21 (Cuthbert and Ariza, 2010) can be used to compute higher-level features.

To summarize, in this section we have seen that MIDI files are a symbolic music representation from which we can extract all kinds of musical information, including a note transcription, using one of the software libraries developed for this purpose. Thanks to their storage efficiency, MIDI files abound on the Internet. This makes MIDI files particularly interesting for ACE research.

### 2.5.3 Tab representation

Guitar tablatures and chord sheets are collectively known as “tabs”. In contrast to traditional musical scores, (guitar) tablature indicates the instrumental fingering rather than musical pitches. These tablatures are usually represented using an ASCII text notation, in which each line represents a string of the instrument. As reading tablature requires little musical training and tabs can be written and read without any specific software, they are very popular: millions of guitar tablature files can be found on websites like Ultimate Guitar\(^1\) (Macrae and Dixon, 2011). Figure 2.18 shows an example of guitar tablature. Chords can be extracted from tabs very easily. For example, above the word “seventeen” we see the fingering combination (0, 3, 1, 2, 2, 0), which means that a chord is played using open E strings, the third fret on the B string, the first fret on the G string and the second fret on the D and A string. This way, the notes E4, D4, G#3, E3, B2 and E2 are played on the six strings. These notes form the seventh chord E7, as they consist of the notes E, G#, B and D. In many tablatures, including the example in Figure 2.18, chords are represented twice by also adding a chord. This makes it even easier to extract chord information from guitar tablature. However, note that tablature does not contain any timing information, in contrast to audio and MIDI representations.

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\(^1\)https://www.ultimate-guitar.com/
A **chord sheet** is a lyric sheet, in which chord symbols are placed above the lyric syllables with which they have to be timed. Chord sheets can also be very compactly represented in ASCII text notation. They can be found in abundance on the Internet. Figure 2.19 is a fragment from a chord sheet for *I Saw Her Standing There*. We see that chord information can be extracted directly from the chord sheet. However, similar to guitar tablature, there is no timing information available in chord sheets. In addition, it is quite common for chord sheets to represent only a single verse and chorus, as the chords of other verses and choruses in pop songs are often the same.

In summary, tabs consist of guitar tablatures and chord sheets. Both types are created by music enthusiasts and can be found in abundance on websites like Ultimate Guitar. However, as there are no restrictions on the authorships of tabs, many tabs are erroneous or incomplete. Therefore, it is not trivial to select only the high-quality tabs.

## 2.6 Summary of musical background

This chapter provided an introduction to the concepts of pitch, music notation, intervals, chords and music representations. The **pitch** of musical tones refers to the degree of highness of sound and that the frequency is the number of vibrations in the sound wave. A tuning system discretises the space of all different pitches. In this study, we use twelve-tone equal-tempered tuning, in which the frequency ratio between of two subsequent scale steps equals $2^{1/12}$. A distance of twelve semitones is called an octave. We can group tones that are an octave apart in the same pitch class. In modern Western music notation, tones are given note names based on a pitch class name (i.e. one letter from {A, B, C, D, E, F, G}, possibly combined with an accidental) and an octave number. The reference note A4 has a frequency of 440 Hz. Music is **notated** on a staff. The pitch of each note is determined by its vertical position on the staff. **Intervals** are defined as the distance between two pitches and are based on the notion of semitone. **Chords** are groups of notes sounding at the same time, consisting of tones from at least different pitch classes. Most chords are built by stacking stacks of thirds on a root note. Triads are chords that consist of tones from three pitch classes and consist of the root, plus the third and fifth above it. Seventh chords, or tetrads, consist of the root, third, fifth and seventh. There exist multiple inversions for each chord, which are dependent on the relation of root note and bass note. We have seen various notations for chords. In this project, we use the chord grammar proposed by Harte et al. (2005) as this grammar is unambiguous, context-independent and easy to use.

In Section 2.5 we discussed the three different music representations which are used in this research project. The audio representation is an digitization of the waveform, obtained by sampling and quantization. **Pitch** information cannot be read from the audio directly, but can be estimated using Fourier analysis. **Midi** files are another music representation which, thanks to their storage efficiency, abound on the Internet. Interestingly, Midi files are defined in such a way that we can easily extract all kinds of musical information, including pitch information. The third and final music representation we study are tabs, which is an umbrella term for guitar tablature and chord sheets. Tabs can be found in abundance on the Internet. Chords can be extracted almost directly from tabs, although tabs do not contain timing information and the chord labels are not always reliable.
Chapter 3

Framework of proposed system “DECIBEL”

In this chapter, we present the framework of DECIBEL: the proposed system for the Detection of Chords Improved By Exploiting Linked symbolic formats. In Chapter 1 we have seen that existing chord estimation techniques that are only based on audio have some limitations: the performance of the MIREX ACE submissions seems to have reached a glass ceiling and some modern systems suffer from overfitting to subjective reference annotations. In Section 2.5 we saw that the symbolic representations MIDI and tab have the convenient property that it is very easy to extract notes and chords from them. DECIBEL exploits this property by aligning MIDIs and tabs to the corresponding audio file, extracting chord sequences from each of the representations and using data fusion to combine the resulting chord sequences. DECIBEL’s framework is summarized in Figure 3.1 and will be explained concisely in this section.

3.1 DECIBEL’s framework in a nutshell

The DECIBEL system has a data set of audio, MIDI files and tabs at its disposal. MIDI files and tabs are obtained by a web scrape. These files are manually matched, based on meta-data. The dataset and matching process are described in Section 3.2.

For each song, each of the three representations (audio, MIDI and tabs) is mapped to an audio-timed chord sequence, which is a sequence of chord events. Chord events are 3-tuples, consisting of a start time, end time and chord label. The possible chord label values are specified by the chosen chord vocabulary. The method for this chord estimation step depends on the representation: we used three different methods for audio, MIDI and tab representations, as specified below:

Audio: DECIBEL estimates chords from audio data using existing audio ACE techniques.

MIDI: In order to estimate chords from MIDI, DECIBEL first aligns each MIDI file to the audio recording using audio-symbolic alignment techniques. Then, chords are extracted from the audio-aligned MIDI file using a pattern-matching technique for chord estimation in symbolic music. This way, DECIBEL obtains the chord sequences with the correct start and end times for the original audio file.

Tabs: For the tabs, DECIBEL can easily find the chord labels by parsing the ASCII text. Consequently, the system aligns them to the audio using Jump Alignment.

Each of the three procedures for representation-dependent extraction of audio-timed chord sequences can be considered as a subsystem of DECIBEL. In Chapters 4, 5 and 6, we will describe the audio, MIDI and tabs subsystems in detail.

At this point, we have a rich harmonic representation, consisting of possible chord sequences for the song, obtained from symbolic and audio representations. As a final step, we use data fusion to combine these chord sequences into one final chord sequence. The data fusion method is treated in Chapter 7.

In the remainder of this section, we describe the collection of the data set in detail in Section 3.2. Also, we de-
Figure 3.1: Diagram of decibel’s framework. The M represents the matching between different representations of the same song. Data formats are depicted by rectangles; procedures are represented as rounded rectangles. The grey elements show how decibel extends existing audio ACE methods.

scribe the performance evaluation measures, which are used to test both the representation-specific subsystems as well as the data fused result, in Section 3.3.

3.2 Collection of data set

Decibel uses a data set of audio, MIDI files and tabs. This data set is based on a subset of the Isophonics Reference Annotations (Mauch et al., 2009). The Isophonics data set contains chord annotations for 180 Beatles songs, 20 songs by Queen, 7 songs by Carole King and 18 songs by Zweieck. In this project, we only use the songs by the Beatles and Queen, as there were no MIDI or tabs for Zweieck available and there were some inconsistencies in the Carole King annotations. Using this 200 song data set has three advantages: (1) the music by The Beatles and Queen is popular music and therefore the correct genre for our dataset; (2) thanks to the popularity of the two bands, it is easy to find MIDI and tab files for the songs in the data set; and (3) the chord labels have been carefully checked and have been used for many years by the MIR community.

We used the audio as provided on the CDs in Table 3.1. A complete list of all song names and the index that we assigned to them, is given in Appendix A. After collecting the audio files and annotations, we need to find MIDI and tab files and match them to the songs in our data set. First, we searched on the Internet for MIDI files of the aforementioned 200 songs. We downloaded MIDI files from 9 websites123456789. This way, we found 770 MIDI files with unique MD5-checksums, so multiple MIDI files (3.85 on average) map to a single audio file. We matched the MIDI and audio files by hand, based on the MIDI file name. Furthermore, we obtained tabs from Ultimate Guitar10. We first automatically scraped all tabs from The Beatles and Queen from Ultimate Guitar’s website. Then, we matched the tabs to the audio files by hand, based on song title. Tabs from songs

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1http://beatlesnumber9.com
2http://bmh.webzdarma.cz
3http://davidmidim.com
4http://earlybeatles.com/midi
5http://en.midimelody.ru
6http://queen.wz.cz/midi
7http://www.angelfire.com
8http://www.dongrays.com
9http://www.rppmf.com
10https://www.ultimate-guitar.com
Table 3.1: Isophonics Reference Annotations

| Artist       | Album                              | ID            | # songs |
|--------------|------------------------------------|---------------|---------|
| The Beatles  | Please Please Me                   | CDP 7 46435 2 | 14      |
| The Beatles  | With the Beatles                   | CDP 7 46436 2 | 14      |
| The Beatles  | A Hard Day’s Night                 | CDP 7 46437 2 | 13      |
| The Beatles  | Beatles For Sale                   | CDP 7 46438 2 | 14      |
| The Beatles  | Help!                              | CDP 7 46439 2 | 14      |
| The Beatles  | Rubber Soul                        | CDP 7 46440 2 | 14      |
| The Beatles  | Revolver                           | CDP 7 46441 2 | 14      |
| The Beatles  | Sgt. Pepper’s Lonely Hearts Club Band | CDP 7 46442 2 | 13      |
| The Beatles  | Magical Mystery Tour               | CDP 7 48062 2 | 11      |
| The Beatles  | The Beatles (the white album)      | CDS 7 46443 8 | 30      |
| The Beatles  | Abbey Road                         | CDP 7 46446 2 | 17      |
| The Beatles  | Let It Be                          | CDP 7 46447 2 | 12      |
| Queen        | Greatest Hits I                    | Parlophone, 0777 7 8950424 | 14      |
| Queen        | Greatest Hits II                   | Parlophone, CDP 7 7979712 | 6       |

that were not in the dataset, were discarded. This resulted in 1668 matched tabs (974 chords and 694 guitar tablature files).

Some statistics on the data set are shown in Figure 3.2. A typical song in our data set has a duration of 2 to 3 minutes, consists of 50-100 chord segments and is matched to 3 to 5 MIDI files and 5 to 10 tabs.

### 3.3 Performance evaluation

In order to evaluate both the performance of decibel’s representation-specific subsystems and its final output chord sequence, we need evaluation measures. The quality of a chord sequence is usually determined by comparing it to a ground truth created by one or more human annotators. Commonly used data sets with chord annotations, which are also used in the MIREX ACE contest, are Isophonics\(^{11}\), Billboard\(^{12}\), RobbieWilliams\(^{13}\), RWC-Popular\(^{14}\) and USPOP2002Chords\(^{15}\). As stated before, decibel uses the Isophonics data set, augmented with matched MIDI and tab files.

The standard quality measure to evaluate the quality of an automatic transcription is chord symbol recall (csr) (Harte, 2010). This measure is also used in the MIREX ACE contest\(^{16}\). Csr is the summed duration of time periods where the correct chord has been identified, normalized by the total duration of the song. Until 2013, MIREX used an approximate, frame-based csr calculated by sampling both the ground-truth and the automatic annotations every 10 ms and dividing the number of correctly annotated samples by the total number of samples. Since 2013, MIREX has used segment-based csr, which is more precise and computationally more efficient. The formula for segment-based csr is given in Equation 3.1. We consider the ground-truth annotation \(A\) as a sequence of segments \(S_A\) and the estimated annotation \(E\) as a sequence of segments \(S_E\). The duration of a segment is notated as \(|·|\).

\[
CSRT(S_E, S_A) = \frac{\sum_{S_i^A} \sum_{S_j^E} |S_i^E \cap S_j^A| \cdot M_T(S_i^A, S_j^E)}{\sum_{S_i^A} |S_i^A|} \tag{3.1}
\]

\(M_T\) is a matching function as defined by Equation 3.2, in which \(T\) denotes the comparison method used to evaluate the result of the matching function.

\(^{11}\)http://isophonics.net/datasets

\(^{12}\)http://ddmal.music.mcgill.ca/research/billboard

\(^{13}\)https://www.researchgate.net/publication/260399240_Chord_and_Harmony_annotations_of_the_first_five_albums_by_Robbie_Williams

\(^{14}\)https://github.com/tmc323/Chord-Annotations

\(^{15}\)https://labrosa.ee.columbia.edu/projects/musicsim/uspop2002.html

\(^{16}\)http://www.music-ir.org/mirex
(a) Song durations  
(b) Number of chord segments per song  
(c) Number of MIDI files and tabs per song. Note that some songs (e.g. song number 208) are not matched to any MIDI or tab file. These are songs on the Queen CD's for which there were no reference annotations in the Isophonics data set.

Figure 3.2: Data set statistics. A typical song in our data set has a duration of 2 to 3 minutes, consists of 50-100 chord segments and is matched to 3 to 5 MIDI files and 5 to 10 tabs.
| Ground Truth | C | F | G | C |
|--------------|---|---|---|---|
| Annotation A | C | B | C | F# | C | F | B | F | B | G | C |
| Annotation B | | | Am | | F | G | C |

$t = 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9 \quad 10 \quad 11 \quad 12 \quad 13$

Figure 3.3: Annotation A has a CSR of $9/13 = 69.2\%$ and Annotation B has a CSR of $8/13 = 61.5\%$. However, Annotation B is the preferred chord sequence.

$$M_T = \begin{cases} 1 & \text{if } X \text{ matches } Y \\ 0 & \text{otherwise} \end{cases} \quad (3.2)$$

The comparison method is dependent of the chord vocabulary: both the chord labels ground truth annotations and the estimated annotations are mapped to a limited set of chord labels, as specified by the chord vocabulary. MIREX uses the following five chord vocabularies:

1. Only the chord root note (C, D, ..., B), or no-chord (N);
2. Major and minor: \{N, maj, min\};
3. Seventh chords: \{N, maj, min, maj7, min7, 7\};
4. Major and minor with inversions: \{N, maj, min, maj/3, min/b3, maj/5, min/5\};
5. Seventh chords with inversions: \{N, maj, min, maj7, min7, 7, maj/3, min/b3, maj7/3, min7/b3, 7/3, maj/5, min/5, maj7/5, min7/5, 7/5, maj7/7, min7/b7, 7/b7\}.

Two chords match if and only if they are mapped to exactly the same chord label in the vocabulary. For example, the mapping to chord vocabulary 1 only preserves the root note. The chords C:maj and C:min will both be mapped to a C chord, so these chords would match in the first chord vocabulary. However, in all other vocabularies they would be mapped to C:maj and C:min, which do not match.

For results that are calculated for the whole data set, we weigh the CSR by the length of the song when computing an average for a given corpus. This final number is referred to as the weighted chord symbol recall ($\text{wcsr}$). Calculating the WCSR is basically the same as treating the data set as one big audio file, and calculating the CSR between the concatenation of all ground-truth annotations and the concatenation of all estimated annotations.

The CSR correctly indicates the accuracy of an ACE algorithm in terms of whether the estimated chord for a given instant in the audio is correct. It is therefore widely used in the evaluation of ACE systems. However, the annotation with the highest CSR is not always the annotation that would be considered the best by human listeners. As an example, examine Figure 3.3. Here we see two estimated annotations. Although Annotation A has the higher CSR, most musicians would prefer Annotation B: Annotation A is clearly over-segmented, which makes it difficult to play and unnatural to listen to. On the other hand, human listeners would consider the 5 seconds with the wrong chord in Annotation B as just one major mistake.

Just measuring the (weighted) chord symbol recall is therefore not enough: we also need a metric for chord segmentation quality. For this purpose, Mauch (2010) proposed the use of the directional hamming distance $h(S, S^0)$. It describes how fragmented segmentation $S$ is with respect to segmentation $S^0$, according to Equation 3.3:

$$h(S, S^0) = \frac{N_{\text{inc}}}{\sum_{i=1}^{N_{\text{inc}}}} \left( |S_i^0| - \max_j |S_i^0 \cap S_j| \right) \quad (3.3)$$

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In our example, let Annotation A be $S^A$, let Annotation B be $S^B$ and let the ground truth be $S^G$. Then, $h(S^A, S^G)$ is a measure of over-segmentation of $S^A$ with respect to $S^G$. Indeed,

$$h(S^A, S^G) = \sum_{i=1}^{N_{SG}} \left( |S^G_i| - \max_j |S^G_i \cap S^A_j| \right) = (5 - 1) + (3 - 1) + (2 - 1) + (3 - 3) = 7$$

This is a high value, so the directional Hamming distance shows that $S^A$ is over-segmented. A high Hamming distance in the opposite direction indicates under-segmentation.

$$h(S^G, S^A) = \sum_{i=1}^{N_{SA}} \left( |S^A_i| - \max_j |S^A_i \cap S^G_j| \right) = 13 * (1 - 1) = 0$$

so $S^A$ is not under-segmented. The segmentation of Annotation B is identical to the ground truth:

$$h(S^B, S^G) = h(S^G, S^B) = 0$$

We can easily transform the directional Hamming distance into a quality measures for over-segmentation and under-segmentation using the following equations:

$$\text{OverSegmentation}(S_E, S_A) = 1 - \frac{h(S_E, S_A)}{\sum_{i=1}^{N_{SA}} |S_A_i|} \in [0, 1] \tag{3.4}$$

$$\text{UnderSegmentation}(S_E, S_A) = 1 - \frac{h(S_A, S_E)}{\sum_{i=1}^{N_{SA}} |S_A_i|} \in [0, 1] \tag{3.5}$$

OverSegmentation or UnderSegmentation values near 0 correspond to highly under- and over-segmented annotations respectively. High values indicate good segmentation quality. Equations 3.4 and 3.5 can be combined into an all-in-one segmentation measure using Equation 3.6. We use the minimum, so an annotation only gets a high segmentation quality if neither under-segmentation nor over-segmentation is dominant.

$$\text{Segmentation}(S_E, S_A) = \min \left\{ \text{OverSegmentation}(S_E, S_A), \text{UnderSegmentation}(S_E, S_A) \right\} \tag{3.6}$$
Chapter 4

Automatic Chord Estimation on audio

In this chapter, we focus on the subsystem of DECIBEL that extracts chord sequences from the audio representation, which is schematically summarized in Figure 4.1. There exist multiple methods to extract chord labels from audio data. In Section 4.1, we give an overview of existing methods for ACE in audio, showing a variety in implementations. Ten state-of-the-art systems are used in the audio ACE subsystem of DECIBEL, as described in Section 4.2. Finally, we evaluate these ten systems on our 200 song data set in Section 4.3 and conclude in Section 4.4.

4.1 Related work on audio ACE

This section gives an overview of existing methods for ACE on audio. Fujishima (1999) was the first who considered ACE as a task on its own. Since then, a lot of researchers have buckled down to this subject.

Most methods use the following pipeline (McVicar et al., 2014): first, audio data is partitioned into a training set and a test set and features are calculated on both partitions. Subsequently, the features from the training set are used to train the parameters of a model. The chord labels for the test set are then estimated using this trained model. Finally, the performance of the system is evaluated by comparing the labels calculated by the model to the reference (ground truth) chord labels. Feature extraction and models are described in Sections 4.1.1 and 4.1.2 respectively. The standard pipeline is illustrated in Figure 4.2.

4.1.1 Feature extraction for audio ACE

The first step in audio chord estimation is feature extraction. Features are extracted for both the audio in the training set and the audio in the test set, as shown in Figure 4.2.

The first operation most ACE methods perform in feature extraction, is to calculate (a variation of) the chromagram (Wakefield, 1999). As we have seen in Section 2.5.1, the chromagram describes the pitch class salience over the duration of the audio, i.e. it represents which notes are present in each audio frame. For calculating the chromagram, the audio is first transformed to the frequency domain using either the Short Time Fourier Transform (STFT) or Constant-Q transform.

In many ACE systems, the spectrogram is preprocessed before calculating the chromagram. For example, Mauch (2010) removes background noise by median filtering of the spectrogram; Reed et al. (2009) remove the
percussive elements of the spectrum and Pauws (2004) removes harmonics. As some popular music songs are not tuned at the standard pitch of A₄ = 440 Hz, many methods compensate for tuning issues by computing the spectrogram at a multiple of the required frequency resolution: Sheh and Ellis (2003) doubled the frequency resolution of the spectrogram and Harte and Sandler (2005) even used the triple frequency resolution. As a next step, some authors remap the spectrogram, so it represents the human perception of pitch saliences more closely. Ni et al. (2012) for example use A-weighting, i.e. a technique to express the loudness as perceived by the human ear, to calculate loudness-based chromagrams. Finally, almost all methods discard octave information, as this is not relevant in chord estimation: the pitch A₄ has the same function in a chord as the pitch A₃ or A₅.

Given the chromagram, some **post-processing** steps may help to prevent frequent chord changes in the predicted chord sequence. Fujishima (1999) used smoothing techniques as post-processing, while Bello and Pickens (2005) introduce beat-synchronous chromagrams, in which the chromagram is averaged between beat segments.

Some methods however use **other representations** than traditional chromagrams: Harte et al. (2006) introduce the Tonal Centroid feature; Mauch and Dixon (2008) calculate a distinct bass chromagram and in more recent work, Wu et al. (2017) calculate a 36-dimensional binary acoustic feature using a Deep Residual Network, trained on MIDI data. Sigta et al. (2015) use Deep Neural Networks and Korzeniowski and Widmer (2016a,b) train a Convolutional Neural Network to automatically learn musically interpretable features from the spectrogram. Müller and Ewert (2010) introduce chroma DCT-reduced log pitch (CRP) features, which improve timbre invariance. These CRP features are implemented in the **ace** system by O’Hanlon et al. (2017).

In this subsection, we saw various ways of extracting features from audio. These features are extracted from the audio of both the training set and the test set, and serve as an input for a model, as we will see in the next session.
4.1.2 Audio ACE models

As a next step, we need to estimate chord labels, given the feature vectors of the test set. Although early methods for calculating the chord labels from feature vectors rely on template matching, recent works typically use statistical models or neural networks. Usually, these models are first trained on the training set, which is a subset of the data set for which ground truth chord labels are known. The model is then evaluated on the other partition of the data set: the test set. This section briefly indicates the variety of models used in audio ACE.

Shehan and Ellis (2003) were the first to use the Hidden Markov Model (HMM) and Expectation-Maximization algorithm to train a model for ACE, in which the chord labels are represented by hidden states and the features correspond to the observed states. HMMs model the joint probability distribution \( P(X, y) \) over the feature vectors \( X \) and the chord labels \( y \). We will have a more detailed look at HMMs in Section 6.2.2, as this type of model is also used in the Jump Alignment algorithm (with which DECIBEL aligns tabs to audio). Some methods, for example the system proposed by Shenoy and Wang (2005), incorporate key information in a two-chain HMM. Scholz et al. (2009) introduce higher-order HMMs, in order to better model the complexity of music.

An alternative model is the Dynamic Bayesian Model (DBM), which is a Bayesian network that relates variables to each other over adjacent time steps. It was introduced for ACE by Mauch and Dixon (2010). This model has hidden nodes for metrical position, chord, bass note and musical key and observed nodes for bass and treble chromagrams. Thanks to its design, the DBM is able to integrate multiple pieces of musical context in a single model.

Burgoyne et al. (2007) used different variations of Conditional Random Fields (CRF). CRF is a discriminative model: it models \( P(y|X) \), which is the conditional distribution of chord labels given a sequence of feature vectors. Linear-chain CRFs were also used in the system of Korzeniowski and Widmer (2016b).

In recent work, we see a trend towards using Artificial Neural Network models. This class of models is inspired by biological neural networks in our brains: they consist of a collection of connected nodes or neurons, often arranged in layers. Each of the neurons processes a signal that it receives from neurons of the previous layer, calculates some non-linear function on the sum of these inputs and passes the result on to the neurons in the next layer. The neurons and edges between them typically have weights that are adjusted in the training phase. This way, neural networks can learn a function that maps feature vectors to chord labels without modeling a probability distribution - provided that there is sufficient training data. Neural networks come in many flavors. For example, Sigtia et al. (2015) use a hybrid Recurrent Neural Network (RNN) model and Wu et al. (2017) combine a Bi-direction LSTM Network and CRFs.

4.2 Selected systems

In order to evaluate DECIBEL, we experiment with ten different audio ACE systems: the nine submissions for the MIREX 2017 and/or 2018 ACE competition, together with the Chordify algorithm. We selected these ten systems as they are state of the art. It is therefore, in contrast to inferior audio ACE systems, not trivial that we can improve these systems by incorporating information from MIDI files and tabs. The implementation of the selected systems is summarized below.

**CHF:** The exact details of the Chordify algorithm are not public, but the current implementation is based on Koops et al. (2017). CHF uses a deep convolutional-recurrent model for automatic chord recognition from the CQT spectrogram.

**CM2 (2017) / CM1 (2018):** CM2 is the algorithm implemented in the Chordino plugin in Sonic Visualiser (Cannam et al., 2017). First, NNLS chroma features are extracted from the CQT spectrogram. Then, a fixed dictionary of chord profiles is used to calculate frame-wise chord similarities. Finally, the chord labels are computed using a HMM. CM2 was resubmitted in 2018 as CM1.
JLW1, JLW2 (2017): Both JLW algorithms are based on the random forest model, which is a collection of decision trees (Jiang et al., 2017). First, the signal is separated into a harmonic and percussive signal, using HPSS. Then the harmonic part is transformed to the frequency domain and NNLS chroma features are calculated on the result. Consequently, a random forest model is trained on these features. This results in a chordogram, which is a matrix that represents the emission probability for chord $c$ at frame $n$. As a final step, the result is smoothed, and this is where versions JLW1 and JLW2 differ. JLW1 uses a HMM, similar to the one used by Chordino. JLW2 uses a beat tracking CRF model that only allows chord changes on beats or at half-beat positions.

KBK1, KBK2 (2017)/ FK2 (2018): Each of the two KBK algorithms is based on neural networks and only recognizes chords in the Major/Minor alphabet. KBK1 uses a deep neural network to extract chroma vectors, as shown in (Korzeniowski and Widmer, 2016a), while KBK2 learns features automatically by a fully convolutional neural network (Korzeniowski and Widmer, 2016b). Then, in both versions, the chord sequence is decoded using a linear-chain Conditional Random Field (CRF) as described in Korzeniowski and Widmer (2016b) and chords segments are aligned to beats using a beat tracker. KBK2 was resubmitted in 2018 as FK2.

WL1 (2017): In WL1, the acoustic features are first calculated from the spectrogram of each music signal with a deep residual network. Then, the feature vectors are fed as a sequence into a Bidirectional Long Short Term Memory network, and a class likelihood vector is calculated for each frame. Finally, the class likelihood sequence is passed on to the trained CRF layer to decode the optimal label sequence. (Wu et al., 2017)

JLCX1, JLCX2 (2018): Both JLCX1 and JLCX2 are based on a model that represents a chord label by its root, triad and bass. Then, a classifier based on a Recurrent Convolutional Neural Network (RCNN) is trained to recognise all subparts given the audio feature. Finally, labels of these subparts are reassembled to form the final chord label. The difference between JLCX1 and JLCX2 is that JLCX2 restricts the chord transition to align with beat positions, while JLCX1 allows chord transitions at any location. (Jiang et al., 2018)

SG1 (2018): The approach of SG1 (Gasser and Strasser, 2018) is based on previous year’s MIREX submission KBK2. SG1 uses a convolutional neural network as well, and augments the training data by applying pitch shifts and detuning. However, they train the network on three objectives: root note, chord description and inversion.

4.3 Evaluation of audio ACE

In this section, we evaluate the ten audio ACE systems, of which we described the implementation in the previous section, on our data set\(^1\). Figure 4.3 shows the performance of all ten systems in terms of CSR and segmentation measures. From the figure we see that the CSR of all ten systems is quite high, with a median value of at least 80%. JLCX2 is the best performing system, but given these high CSR scores we can already conclude that all ten systems are state of the art. We also observe some outliers for all systems, which are songs for which the CSR is very low. Some outliers are song-specific, that is: (almost) all audio ACE systems perform badly on this song. Other outliers are specific for an ACE system.

First, we will look at song-specific outliers, which have low CSRs due to problems in the audio recording or in the ground truth labels. Some songs have tuning issues. This is for example the case in the song Lovely Rita from the Beatles. The song was originally performed in E major, but during mixdown the tape machine ran at a lower frequency, resulting in a pitch drop of a quarter tone (Lewisohn, 1989). Without this background information, it would be very hard to decide if the song is in E major or in E♭ major. From Figure 4.4 it becomes clear that all ten audio ACE systems choose the E♭ major key: the chord labels of the ACE systems are quite consistently one semitone lower than the ground truth chord labels. This results in very low CSRs for all ten audio ACE systems, ranging from 0% (e.g. JLW2) to 20% (e.g. KBK2). The Beatles song Wild Honey Pie has tuning issues as well, resulting in CSRs from 0% (JLW1) to 42% (KBK2). Wild Honey Pie is a short, experimental song, characterized by Indian influences, played with a lot of vibrato. The Queen song Another One Bites The Dust has some tuning issues too, albeit to a lower extent than Lovely Rita and Wild Honey Pie.

\(^1\)Note that the results are not exactly the same as the MIREX evaluation on the Isophonics data set, as we use a subset of this data set, consisting of the Beatles and Queen songs.
Figure 4.3: Comparison of performance measures for Chordify (CHF) and MIREX 2017/2018 ACE submissions. For a description of these performance measures, see Section 3.3. KBk2 is the best performing system in terms of CSR. CHF and CM2 tend to oversegment the song. On the other hand, WL1 inclines to undersegmentation.
Figure 4.4: Chord sequences from ten different audio ACE systems on the Beatles song *Lovely Rita*, which has tuning issues. CsR = Chord Symbol Recall; OvS = oversegmentation; UnS = undersegmentation; and Seg = segmentation.

In two other songs (*The Continuing Story of Buffalo Bill* and *Don’t Pass Me By*), the chord labels of the nine MIREX chord ACE systems are shifted in time compared to the ground truth data, as shown in Figure 4.5. This is probably due to the use of different audio versions in chord annotation and evaluation.

Figure 4.5: Chord sequences from ten different audio ACE systems on the Beatles song *Don’t Pass Me By*, in which the chord labels are shifted in time. CsR = Chord Symbol Recall; OvS = oversegmentation; UnS = undersegmentation; and Seg = segmentation.
The Beatles song *Revolution* has another song-specific issue. This song is a sound collage: an experimental recording that is glued together from sound fragments, many of which are non-harmonic. Accordingly, we see in Figure 4.6 that a large part of the ground truth is represented with black, corresponding to the no-chord symbol. However, most audio ACE systems do not correctly recognize non-harmonic content as they are trained on tonal music.

![Figure 4.6](image)

Figure 4.6: Revolution 9 is a sound collage, consisting of many non-harmonic sounds. CSR = Chord Symbol Recall; OvS = oversegmentation; UnS = undersegmentation; and Seg = segmentation.

Apart from song-specific problems (like tuning issues, shifted recordings and non-harmonic notes), there are also audio ACE-specific issues. From Figure 4.3a, we can see that KBK2 performs the best, while CM2 performs the worst in terms of CSR. CHF and CM2 tend to oversegment the song, considering the relatively low values for oversegmentation in Figure 4.3b. On the other hand, WL1 inclines to undersegmentation. We see this for example in Figure 4.7: in this example we see that CHF and CM2 create too many segments and correspondingly get relatively low oversegmentation scores. On the other hand, WL1 creates too few segments, resulting in undersegmentation: WL1 here has a undersegmentation score of only 0.53.
Figure 4.7: Chord sequences from ten different audio ACE systems on the Beatles song *Another Girl*. CSR = Chord Symbol Recall; OvS = oversegmentation; UnS = undersegmentation; and Seg = segmentation.

4.4 Conclusion

In this chapter, we have described the implementation and performance characteristics of ten systems for audio ACE. By evaluating the audio ACE systems on our 200 song data set, we learned that all ten systems are state of the art, as they have high chord symbol recalls. However, different ACE systems behave differently: some systems tend to undersegment the chord sequence, while others tend to oversegmentation. In this study, we will use of each of these systems: we will compare the performance of the original audio ACE system to the data fused result, which incorporates not only the audio ACE system but also information from MIDI and tab files.
Chapter 5

Automatic Chord Estimation on MIDI

In this chapter, we discuss the subsystem of DECIBEL that detects an audio-timed chord sequence based on a MIDI file. This subsystem is illustrated below, in Figure 5.1. In order to receive audio-timed chord labels from a MIDI file, DECIBEL first finds an optimal alignment from the MIDI file to the audio file, realigns the MIDI file using this alignment and then uses a MIDI chord recognizer to estimate the chord labels on the realigned MIDI file. In Section 5.1 we will explain the alignment step and in Section 5.2 the MIDI chord recognition step. We then have audio-timed chord labels for each MIDI file. However, there may be MIDI files that are unsuitable to use, because they are bad transcriptions (i.e. the notes in the MIDI file are not consistent with the notes in the audio file), because they are in a wrong transposition or because they are a transcription of just one part of the song. It may help to exclude these MIDI files from the data fusion step. We experiment with MIDI selection methods in Section 5.3 and conclude in Section 5.4.

5.1 MIDI-to-audio alignment

Music alignment is the procedure which, given any position in one representation of a piece of music, determines the corresponding position within another representation. It is also called music synchronization. In the MIDI subsystem, DECIBEL aligns each of the MIDI representations to the corresponding audio representation. This section explains the MIDI-to-audio alignment procedure. MIDI-to-audio alignment is an important task in MIR: a lot of research has already been conducted on this subject. Therefore, we will first study related work on alignment in Section 5.1.1. We can then make a well-grounded choice for the alignment system implemented in DECIBEL. This alignment system is described in Section 5.1.2 and evaluated in Section 5.1.3.

5.1.1 Related work on MIDI-to-audio alignment

There are two variants of MIDI-to-audio alignment: on-line and off-line alignment. In off-line alignment, the full performance is accessible for the alignment process. By contrast, in on-line alignment, the aligner processes the data in real-time as the signal is acquired. On-line alignment is also known as score following and has applications such as automatic accompaniment, audio editing and automatic turning of score pages. In

Figure 5.1: Diagram of DECIBEL’s MIDI subsystem; the M between Audio File and MIDI file indicates that they are manually matched.
general, off-line techniques work better than on-line systems, because they do not need to calculate the alignment in real-time and they can access the full performance at all times. For our project, the full performance is accessible from the beginning of the alignment process and the alignment does not have to be calculated in real-time. Therefore, we use off-line audio-symbolic alignment techniques.

The alignment method is typically based on either statistical approaches (for example HMMs, as used by e.g. Cuvillier and Cont (2014)) or Dynamic Time Warping (Carabias-Orti et al., 2015; Raffel and Ellis, 2016b; Arzt, 2016; Lajugie et al., 2016). In this project, we focus on Dynamic Time Warping (dtw) approaches, as the dtw algorithm is efficient, is conceptually simple and calculates an easily interpretable alignment confidence score.

In the remainder of this section, we first give a general introduction to dtw. Subsequently, we see how dtw can be applied to alignment of music.

An introduction to Dynamic Time Warping

In dtw (Sakoe and Chiba, 1978) we try to find the optimal alignment path between two sequences of feature vectors \( X \in \mathbb{R}^{M \times D} \) and \( Y \in \mathbb{R}^{N \times D} \), in which \( M \) and \( N \) are the lengths of vectors \( X \) and \( Y \) respectively and \( D \) is the dimension of the feature vector. For example: for chroma vectors, \( D = 12 \). An alignment path is defined as two nondecreasing sequences \( p \in \mathbb{N}^L \) and \( q \in \mathbb{N}^L \), that satisfy the following three conditions:

- Boundary condition: \( p[1] = 1, q[1] = 1, p[L] = N \) and \( q[L] = M \);
- Monotonicity condition: \( p[1] \leq p[2] \leq \ldots \leq p[L] \) and \( q[1] \leq q[2] \leq \ldots \leq q[L] \);
- Step size condition: \( (p[l+1] - p[l], q[l+1] - q[l]) \in \{(1,1), (1,0), (0,1)\} \) for \( l \in [1, L-1] \).

In the alignment path \( p, q \), \( p[i] = n \) and \( q[i] = m \) implies that the \( n^{th} \) feature vector in \( X \) is matched to the \( m^{th} \) feature vector in \( Y \). The optimal alignment path is the path with the lowest total cost, in which the total cost is defined as the sum of local costs \( c \) between each pair of features \( (X[p[i]], Y[q[i]]) \) on the alignment path. Finding the optimal path \( p, q \) can thus be defined as the following minimization problem:

\[
\begin{align*}
(p, q) &= \text{argmin}_{p,q} \sum_{i=1}^{L} c(X[p[i]], Y[q[i]])
\end{align*}
\]  

(5.1)

As an example, consider two sequences \( X = [0, 1, 2, 3, 2, 1] \) and \( Y = [1, 2, 3, 2, 0] \) and define the cost function as the absolute distance, i.e. \( c(X[p[i]], Y[q[i]]) = |X[p[i]] - Y[q[i]]| \). The optimal alignment path is illustrated in Figure 5.2. In this path, the first two elements of \( X \) are aligned to the first element of \( Y \); the third element of \( X \) is aligned to the second element of \( Y \); the fourth element of \( X \) is aligned to the third element of \( Y \), etcetera. Therefore, the optimal path is \( p, q = [1, 2, 3, 4, 5, 6], [1, 1, 2, 3, 4, 5] \). This path has length \( \sum_{i=1}^{6} c(X[p[i]], Y[q[i]]) = c(0, 0) + c(1, 1) + c(2, 2) + c(3, 3) + c(2, 2) + c(1, 0) = 0 + 1 + 0 + 0 + 0 + 1 = 2 \).

\[
\begin{align*}
X: & \quad 0 \quad 1 \quad 2 \quad 3 \quad 2 \quad 1 \\
Y: & \quad 1 \quad 2 \quad 3 \quad 2 \quad 0
\end{align*}
\]

Figure 5.2: Alignment of \( X = [0, 1, 2, 3, 2, 1] \) and \( Y = [1, 2, 3, 2, 0] \)

To determine the optimal alignment path, one could compute the total cost of all possible warping paths and then return the path with the lowest cost. Unfortunately this is not feasible for large sequences, because the number of possible warping paths is exponential in the length of the sequences. Luckily, there exist other methods to find the optimal alignment path.

Consider a path \( p_n, q_m \), with length \( k \) that is a prefix of the alignment path. That is: \( p_n, q_m \) fulfills all requirements of the alignment path, except for the last part of the boundary criterion. So:
Also, note that the optimal path
Likewise, we do need to minimize for calculating the cost of any path
The Dynamic Time Warping algorithm uses Equations 5.2, 5.3 and 5.4 to efficiently compute the optimal full alignment path \( p_n, q_m \) in constant time, using the following equation:

\[
\text{cost}(p_n, q_m) = \min_{p_n, q_m} \sum_{i=1}^{k} c(X[p_n[i]], Y[q_m[i]])
\]

\[
= c(X[p_n[l]], Y[q_m[l]]) + \min\left\{ \sum_{i=1}^{k-1} c(X[p_n[i]], Y[q_m[i]]) \right. \\
\left. \sum_{i=1}^{k-1} c(X[p_n[i]], Y[q_m[i]]) \right. \\
\right. \sum_{i=1}^{k-1} c(X[p_n[i]], Y[q_m[i]])
\]

All paths \( p_n, q_1 \) have the special property that they must exclusively consist of horizontal steps, i.e. \( (p_n[l+1] - p_n[l], q_1[l+1] - q_1[l]) = (1, 0) \) for \( l \in [1, k - 1] \). Therefore, we can calculate their cost without minimization:

\[
\text{cost}(p_n, q_1) = \min_{p_n, q_1} \sum_{i=1}^{k} c(X[p_n[i]], Y[q_1[i]])
\]

\[
= \sum_{i=1}^{n} c(X[p[i]], Y[q[1]])
\]

Likewise, we do need to minimize for calculating the cost of any path \( p_1, q_m \):

\[
\text{cost}(p_1, q_m) = \min_{p_1, q_m} \sum_{i=1}^{k} c(X[p_1[i]], Y[q_m[i]])
\]

\[
= \sum_{i=1}^{m} c(X[p[1]], Y[q[i]])
\]

Also, note that the optimal path \( p_n, q_m \) with \( n = N \) and \( m = M \) equals the optimal full alignment path \( p, q \).

The Dynamic Time Warping algorithm is given in Algorithm 1. The algorithm takes a cost matrix \( C[n, m] = c(X[n], Y[m]) \). Any entry \( D[n, m] \) contains the cost of the optimal path \( p_n, q_m \), so after running the algorithm \( D[N, M] \) contains the minimum cost of \( p, q \). We can find the optimal alignment path \( p, q \) by following the arrows backwards from \( P[N, M] \).

Let us now test the DTW algorithm on our example \( X = [0, 1, 2, 3, 2, 1] \) and \( Y = [1, 2, 3, 2, 0] \) from Figure 5.2. First, we calculate the cost matrix \( C \). Remember that in our example, \( c \) is defined as the absolute difference. For example, \( C[4,1] = c(X[4], Y[1]) = |X[4] - Y[1]| = |3 - 1| = 2 \). The resulting cost matrix \( C \) is given in Figure 5.3a. Figures 5.3b and c show the accumulated cost matrix \( D \) and the path matrix \( P \) respectively, which are calculated by the algorithm. We indeed find the optimal alignment path \( (p, q = [1, 2, 3, 4, 5, 6], [1, 1, 2, 3, 4, 5]) \) by following the arrows back from \( P[N, M] \) and read from \( D[N, M] \) that its total cost truly equals 2.

**Dynamic Time Warping in music alignment**

In the previous subsection, we saw an example of DTW on a one-dimensional signal. When aligning two music representations, the features typically have more dimensions. For example, chroma features would be a sensible
Algorithm 1 Pseudocode of the DTW algorithm

1: function dtw(Cost Matrix $C$ of size $N \times M$)
2: Initialize Accumulated cost Matrix $D$ of size $N \times M$
3: Initialize Path Matrix $P$ of size $N \times M$.
4: $D[1, 1] = C[1, 1]$
5: $P[1, 1] = \cdot$
6: for all $n \in [2, N]$ do
7: \hspace{1em} $D[n, 1] = C[n, 1] + D[n - 1, 1]$
8: \hspace{1em} $P[n, 1] = \leftarrow$
9: end for
10: for all $m \in [2, M]$ do
11: \hspace{1em} $D[1, m] = C[1, m] + D[1, m - 1]$
12: \hspace{1em} $P[1, m] = \downarrow$
13: end for
14: for all $n \in [2, N]$ do
15: \hspace{1em} for all $m \in [2, M]$ do
16: \hspace{2em} $s = \min D[n - 1, m - 1], D[n, m - 1], D[n - 1, m]$
17: \hspace{2em} if $s \equiv D[n - 1, m - 1]$ then
18: \hspace{3em} $D[n, m] = C[n, m] + D[n - 1, m - 1]$
19: \hspace{3em} $P[n, m] = \leftarrow$
20: \hspace{2em} else if $s \equiv D[n, m - 1]$ then
21: \hspace{3em} $D[n, m] = C[n, m] + D[n, m - 1]$
22: \hspace{3em} $P[n, m] = \downarrow$
23: \hspace{2em} else
24: \hspace{3em} $D[n, m] = C[n, m] + D[n - 1, m]$
25: \hspace{3em} $P[n, m] = \leftarrow$
26: end if
27: end for
28: end for
29: end function

Figure 5.3: Cost matrix and DTW output for the alignment of our toy example $X = [0, 1, 2, 3, 2, 1]$ and $Y = [1, 2, 3, 2, 0]$
choice: they can be calculated from both the audio and the synthesized MIDI. In that case, the features are
twelve-dimensional. Chroma features are for example used for alignment by Hu et al. (2003). Prätzlisch and
Müller (2016) and Wang et al. (2014) also use chroma based-features, but those are combined with features
capturing onset information. Other methods, those designed by Dixon and Widmer (2005) and Raffel and Ellis
(2015), use the result from a Constant-Q transform.

As we have seen in Section 2.5.1, we need to set a time scale for the feature vectors. Some methods, for
example Dixon and Widmer (2005), compute feature vectors over short, overlapping frames of audio. Other
methods, like Raffel and Ellis (2015) use beat-synchronous feature vectors, obtained by aggregating the original
feature vectors between two beats.

Multidimensional features require an appropriate cost function. A common choice (used by e.g. Turetsky and
Ellis (2003); Wang et al. (2014); Raffel and Ellis (2015)) is the cosine distance. The cosine distance between
two \(d\)-dimensional features \(x\) and \(y\) is defined as:

\[
c(x, y) = 1 - \frac{\langle x | y \rangle}{||x|| \cdot ||y||} = 1 - \frac{\sum_{i=1}^{d} x_i \cdot y_i}{\sqrt{\sum_{i=1}^{d} x_i^2} \cdot \sqrt{\sum_{i=1}^{d} y_i^2}}
\]  

(5.5)

Some methods use a penalty to discourage non-diagonal moves (Raffel and Ellis, 2015). That is, Equation 5.1
is replaced by Equation 5.6, in which \(\Phi(i) \leq 0\) if \(p[i] = p[i - 1]\) or \(q[i] = q[i - 1]\).

\[
p, q = \text{argmin}_{p,q} \sum_{i=1}^{L} c(X[p[i]], Y[q[i]]) + \Phi(i)
\]  

(5.6)

In music alignment, it is not always necessary that the alignment path \(p, q\) spans the entirety of feature vectors
\(X\) and \(Y\). For instance, sometimes we want to match only a part of a MIDI file to the audio recording. In order
to enable subsequence matching, we drop the boundary condition \((p[1] = 1, q[1] = 1, p[L] = N \text{ and } q[L] = M)\)
and relax it to the more flexible condition that either \(g \cdot N \leq p[L] \leq N\) or \(g \cdot M \leq q[L] \leq M\). \(g\) is the gully
parameter and determines the proportion of the subsequence that must be successfully matched. Raffel and Ellis
(2015) for example choose a gully of 0.95, allowing for some tolerance that the beginning or ending of a
MIDI file is incorrect.

To conclude, some methods place global constraints (Müller, 2015, Chapter 3) on the alignment path. These
global constraints reduce complexity of the DTW algorithm and prevent paths that diverge too much from the
diagonal line. A global constraint only allows points on the warping path inside the global constraint region
\(R \subseteq [1 : N] \times [1 : M]\). Two well-known constraints are the Sakoe-Chiba band (Sakoe and Chiba, 1978) and the
Itakura parallelogram (Itakura, 1975). The Sakoe-Chiba band constrains the path to lie within a fixed distance
of the diagonal, as shown in Figure 5.4a. The Itakura parallelogram is illustrated in Figure 5.4b and constrains
the path to lie within a parallelogram around the diagonal of the matrix.

![Figure 5.4: Global constraint regions](image)

\(\text{Figure 5.4: Global constraint regions}\)

5.1.2 Selected system

As we have seen in Section 5.1.1, Dynamic Time Warping (DTW) is a common technique to align two feature
vectors, for example two representations of the same song. We also learned that there are many variations of
the DTW algorithm: one can use different features, time scales, cost functions, penalties, gully parameters and
global constraints. In this section, we will explain the MIDI-to-audio alignment method we selected for DECIBEL.
For alignment between MIDI files and audio recordings, DECIBEL uses a DTW algorithm by Raffel and Ellis (2016b). We selected this algorithm for a couple of reasons. In the first place, it benefits from the two advantages of DTW: the algorithm calculates an easily interpretable alignment confidence score, which gives a good indication of the alignment quality. Furthermore, the algorithm is conceptually simple and easy to implement. Typically, the performance of DTW heavily relies on the chosen parameters. An advantage of this specific system is that the optimal parameter setting is trained on a synthetically trained data set of 1000 MIDI files which were transcriptions of Western popular music songs, using Bayesian optimization.

Before we look at the specific parameter settings, let us first consider the outline of the algorithm. The outline is illustrated with an example in Figure 5.5. First, all MIDI files are synthesized using the fluidsynth\(^1\) software synthesizer with the FluidR3\_GM soundfont. Now we have a waveform representation for both the audio (Figure 5.5a) and the MIDI file (Figure 5.5b). Note that our example MIDI file starts with silence, while in the audio recording the music starts immediately. Also, the MIDI file has a longer duration, as the MIDI file repeats the chorus an additional time, compared to the audio file. Then, the Constant-Q transform is calculated for both the audio (Figure 5.5c) and the synthesized MIDI waveform (Figure 5.5d). Features are found by aggregation over the Constant-Q transform vectors. Then, the optimal path between the audio file and the synthesized MIDI is calculated using DTW. This results in an optimal path and the alignment confidence score, as illustrated in Figure 5.5e. In this figure, we see that the alignment path starts not in the coordinate (0, 0), but a bit to the right: the silence at the start of the MIDI file is not mapped to any position in the audio file. The same goes for the end of the MIDI file, which is a superfluous repetition of the chorus. Finally, this alignment path is used to remap the MIDI file to the audio recording (see Figure 5.5f).

DECIBEL uses the unchanged parameter setting reported in the paper by Raffel and Ellis (2016b). The parameters are listed in Table 5.1. We did not experiment with alternative parameter settings as the parameters were already optimized for a dataset in the same genre as mine. In the optimal parameter setting, the features are represented by log-magnitude Constant-Q transform. This is the Constant-Q transform we have seen in Section 2.5.1, but the log of the features is calculated to mimic human perception more closely. An optimal hop size of 1024 samples is found, which corresponds to a time scale of 46 milliseconds, given the sampling rate of 22050 Hz: \(\frac{1024}{22040} = 0.046s\). Feature vectors are normalized by L2 norm before calculating the local distances. This is equivalent to using the cosine distance. An penalty of the median distance between all pairs of frames is found to give the best results. In the optimal system, the gully parameter is 0.96 and there is no band path constraint.

The output of the DTW system is an optimal path and its alignment confidence score. The path specifies which time point, measured in seconds, in the MIDI file is aligned to which time point in the audio file. We use this path to recompute the times in the MIDI file using the pretty\_midi package (Raffel and Ellis, 2014). This gives us the “audio-aligned MIDI file” we will use in the chord estimation step. The alignment confidence score is the mean distance between all pairs of frames over the entire aligned portion of both feature sequences. A qualitative evaluation on 500 real word MIDI/audio pairs by Raffel and Ellis (2016b) shows that the alignment confidence score is a reliable measure for the quality of the alignment in most cases, although there were a few outliers which had a low (good) alignment confidence score despite being aligned badly. In general, MIDI/audio pairs with an alignment confidence score below 0.85 are aligned well. In the next section, we will do a similar evaluation for to verify if the alignment confidence score is a good indicator for the alignment quality in our data set.

\(^{1}\text{http://www.fluidsynth.org/}\)

| Parameter                  | Setting                                      |
|----------------------------|----------------------------------------------|
| Feature representation     | log-magnitude Constant-Q transform           |
| Time scale                 | every 46 milliseconds                         |
| Cost function              | cosine distance                              |
| Penalty                    | median distance of all pairs of frames        |
| Gully                      | 0.96                                         |
| Band path constraint       | none                                         |

Table 5.1: Parameter settings of audio-MIDI DTW alignment algorithm
Figure 5.5: Illustration of the alignment procedure
5.1.3 Evaluation of MIDI-to-audio alignment

After aligning all MIDI files in the data set to the corresponding audio file, we found an average alignment confidence score of 0.768. In order to verify if the results found by (Raffel and Ellis, 2016a) are applicable to our data set, we evaluated the performance of the DTW system on a random sample of 25 MIDI files. For each MIDI file, we synthesized the realigned MIDI version and played it simultaneously with the original audio file in Sonic Visualiser, listening to the realigned MIDI file on the left earphone and the original audio on the right earphone. In this listening test, we classified each MIDI into one of three alignment quality categories: bad alignments; alignments with minor issues; or good alignments. The results of this evaluation can be found in the Appendix, in Table B.1 and is also depicted in a violin plot in Figure 5.6. A violin plot (Hintze and Nelson, 1998) is an alternative for the box plot that reveals density information from the data. Our evaluation confirmed Raffel’s observation that alignments with a low alignment confidence score are good, while high alignment score (above 85%) have major issues. These problems are mostly due to MIDI files in a wrong transposition or MIDI files that were bad transcriptions, for example because they only represented one part of the song.

5.2 Chord estimation on MIDI

In the previous section we saw how DECIBEL aligns MIDI files to audio recordings. As a next step, we need a chord estimator to calculate the chord sequences from this realigned MIDI file. In this section, we give an overview of related work on MIDI ACE in Subsection 5.2.1 and describe DECIBEL’s MIDI chord estimation method in Subsection 5.2.2. This method will be briefly evaluated in Subsection 5.2.3.

5.2.1 Related work on chord estimation on MIDI

Chord estimation in MIDI files is the task of dividing a MIDI file into segments, in such a way that each segment boundary corresponds to a chord change, and assigning a chord label to each segment. In contrast to audio chord estimation, only few methods have been proposed that extract chords from symbolic music like MIDI.

In a pioneering paper, Winograd (1968) proposes a grammar-based approach to perform automatic tonal (roman numeral) analysis. This type of analysis identifies chords in their harmonic context. Maxwell (1992) developed a rule-based expert system that performs harmonic chord function analysis for tonal music, for example Bach keyboard pieces. Temperley and Sleator (1999) present a computational system for analyzing both metrical and harmonic structure. The system is based on eight preference rules, which are criteria for selecting the best alignment confidence scores for each rating in our qualitative evaluation.
Pardo and Birmingham (2001, 2002) propose another method for segmentation and chord labeling. They segment the score using partition points (the set of all start and end points, excluding duplicates). Then, the score for each segment is calculated by computing the minimum of the distance between the segment and any of the 180 (template, root) pairs. An example of a template is \((0, 3, 7)\), corresponding to a major chord. The authors give 15 different templates and 12 possible roots - one for each pitch class. In case of a tie, the best (template, root) pair is found using tie breaking rules. Inspired by aforementioned research by Pardo and Birmingham, Scholz and Ramalho (2008) propose COCHONUT: a new way to recognize chords from symbolic MIDI guitar data in bossa nova music, which is also dealing with complex chords like ninth and suspended chords. Chord estimation is split into three steps: (1) run a segmentation algorithm; (2) apply a utility function to identify the most probable chords for each segment and build a graph representing them; and (3) choose the best chord label for each segment, considering contextual information.

Raphael and Stoddard (2003, 2004) use probabilistic models to perform functional harmonic analysis on MIDI data. The analysis is performed on a fixed musical period, for example a measure. They use 12 pitch classes. A chord is specified by the tonic, mode and chord. For example, \((t, m, c) = (2, \text{major}, \text{II})\) would represent a triad in the key of D major built on the second scale degree. So this chord contains the pitches E, G and B (e minor). The most likely chord sequence is computed with a HMM using the Baum-Welch algorithm.

Radicioni and Esposito (2010) perform chord estimation using a HMPerceptron model, in which the domain knowledge is modeled in Boolean features. As chord vocabulary, they consider chords with 12 possible root nodes, 3 possible modes and 3 possible added notes, resulting in 108 possible chord labels.

In more recent research, Masada and Bunescu (2017) propose a machine learning model for chord estimation that uses semi-Markov Conditional Random Fields (semi-CRFs) to perform a joint segmentation and labeling of symbolic music.

In this section, we have seen that the number of algorithms for MIDI chord recognition is limited. Each of these algorithms would require modification and/or labelled training data in order to be used in DECIBEL: (1) rule-based systems (Winograd, 1968; Maxwell, 1992; Temperley and Sleator, 1999) are designed for a specific music genre (usually classical music); (2) some algorithms (Winograd, 1968; Maxwell, 1992; Temperley and Sleator, 1999; Raphael and Stoddard, 2004) recognise functional harmony instead of chord labels; and (3) other systems (Radicioni and Esposito, 2010; Masada and Bunescu, 2017) are based on machine learning, which requires a lot of labelled training data that is not available for MIDI files of popular music. Therefore, we designed Cassette (Chord estimation Applied to Symbolic music by Segmentation, Extraction and Tie-breaking TEmplate matching). Cassette is a template-matching based algorithm for MIDI chord recognition that is easy to implement and understand and does not require any training. It is based on Pardo and Birmingham (2002), but we adapted the segmentation method and use alternative tie breaking rules.

### 5.2.2 Implementation of Cassette

In Section 5.2.1 we have seen that the existing algorithms for MIDI chord recognition are not suitable for direct use in our DECIBEL system. Therefore, we designed Cassette (Chord estimation Applied to Symbolic music by Segmentation, Extraction and Tie-breaking TEmplate matching). Cassette is a template-matching based algorithm for MIDI chord recognition that is easy to implement and understand. Similar to the good old cassette tapes, this algorithm is certainly not state of the art. However, it is simple to implement and does not require any training.

Cassette recognizes chords in a three-step procedure: first, it segments each audio-aligned MIDI file. Then, it calculates a weighted chroma feature for each of the segments, based on the notes that are present within the segment. Finally, Cassette matches the features of each segment to the features of a predefined chord vocabulary and assigns each segment to the most similar chord. In the remainder of this section, we zoom in on each of these three steps.

Cassette segments the MIDI both on the bar and on the beat level. In many cases, segmentation on the bar level is sufficient, as chord changes in popular music often are placed on the downbeat, i.e. on the first beat of a bar. An advantage on segmentation on the bar level is that non-harmony notes, which are typically short, are
less problematic in the template matching step as they have relatively lower weights than the (typically longer) harmony notes. On the other hand, segmentation on the bar level does not work well for songs that have chord changes at other positions than the start of a bar. That is why CASSETTE segments the MIDI file on the beat level as well. This typically results in a chord sequence with more chord changes, although some of which are based on non-harmony notes. For segmentation, CASSETTE uses the pretty_midi package by Raffel and Ellis (2014). Bar segments are found with the get_downbeats function, while the algorithm finds beat segments with the get_beats function.

After segmentation, the next step is feature extraction on each of the segments of the MIDI file. For each segment, CASSETTE extracts the notes sounding between its start and end time. From these notes, we calculate weighted chroma, a feature that is similar to A-weighted chroma as used by Bonvivi (2014, Section 4.1). In order to calculate the weighted chroma feature for a given segment, CASSETTE computes for each note the product of the MIDI velocity and the proportion of the bar during which this note sounds, and sums this product over all notes in the same pitch class. For example, the weighted chroma of a quarter note C in a 4/4 bar with MIDI velocity of 100 is [25, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]. In the resulting vector, both the louder notes (with high velocity) and the longer notes (with higher duration) in the MIDI file are relatively more important, compared to softer or shorter notes. CASSETTE normalizes the weighted chroma vector by dividing each element by the total sum of all its elements. This makes the feature invariant to the total loudness and duration of the notes in the segment.

As a third and final step, we need to find the best matching chords for each segment. Therefore, CASSETTE calculates the template similarity score between the feature of the segment and the feature of each template in our chord vocabulary. In this project, we use a vocabulary of 24 chords, consisting of all 12 major chords and all 12 minor chords, and the no-chord. The chroma-like feature of each template is a 12-dimensional vector, in which each value is 1 if the corresponding note occurs in that chord and the value is 0 otherwise. For example: the D minor chord consists of a D, F and an A. The corresponding chroma would be [0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1]. The score function that measures the similarity between the chroma of the segment and the chroma template is based on earlier work by Pardo and Birmingham (2002). The template similarity score $S$ is calculated with the formula

$$S = P - (N + M).$$

$P$ is the positive evidence: the sum of the weights of the chroma of the bar which match a template element. $N$ is the negative evidence: the sum of the weights of the chroma of the bar which does not match a template element. $M$ stands for misses: the count of template elements not matched by any note. High scores correspond to well-matched templates. For each bar, CASSETTE finds the chord with the highest template similarity score. If the score is -3 or lower, the algorithm assigns a no-chord, as there is no evidence for any chord if three notes or more from the template are missing. Furthermore, CASSETTE applies a single tie-breaking rule: if multiple templates have the same template similarity score, it selects the template whose root pitch has the greatest weight in the segment’s chroma.

### 5.2.3 Evaluation of CASSETTE

In the previous section, we have seen how CASSETTE estimates chords from MIDI files. For the evaluation of the system, we run into a minor issue: a suitable data set with chord annotations for MIDI files of popular music does not yet exist. As a solution, we selected 50 well-aligned MIDI files from our data set and tested them against the Isophonics annotations, as described below.

First, we needed a subset of MIDI files for which the timing information was consistent with the Isophonics annotations. In Section 5.1.3 we observed that MIDI/audio pairs that are aligned well typically have a low alignment error. Therefore, we selected the 50 MIDI files with the lowest alignment error. This subset had alignment confidence scores ranging from 0.459 to 0.602, so we can reasonably expect that these MIDI files are well aligned to the audio.

Then, we ran the CASSETTE algorithm on the audio-aligned versions of these 50 MIDI files and calculated the WCSR for each of the resulting chord label sequences. The results are shown in Table 5.2. Note that particularly the beat-based MIDI chord recognition method performs quite well in terms of WCSR with a 80.0% score. Compared to the bar-based MIDI chord recognition method, beat-based chord recognition has minor oversegmentation issues, while the bar-based method is undersegmenting. This also explains the lower WCSR score of 70.9% of the bar-based method. We can conclude that CASSETTE, despite its simplicity, performs quite well on our data set with popular music and a limited chord vocabulary.

Another interesting property of CASSETTE is that it computes template similarity scores, which we can use
to calculate an approximation score for the quality of the output chord sequences. The template similarity score for each segment gives an indication of the fit of the chord label to this segment: a high score indicates a well-fitting chord label while a low-score segment probably has a less suitable chord label. This may be the case when the actual chord label is more complex than the best fitting chord in our simplified vocabulary. When we average the scores over all segments, we get an approximation score for the quality of the chord label. We call this score the Average Template Similarity (ATS) and we will see its advantages in the next section.

5.3 MIDI file selection

In the previous section we showed that CASSETTE, our MIDI chord recognition method, was quite successful for a 50-song subset of well-aligned MIDI files. Yet extending the aforementioned experiment to the full data set showed a considerably worse performance: when comparing the chord sequences found by MIDI file alignment and chord recognition system on all MIDI files, we found a WCSR of 62.9% for beat-based chord recognition and 60.3% for bar-based chord recognition. These results are not competitive to the performance of other (audio) chord recognition systems. However, these poor results are partly due to low-quality MIDI files. Table 5.3 shows that MIDI quality highly influences the ACE performance. If the worst MIDI file for each song is chosen, then the WCSR for our data set is 45.2% (beat) and 43.9% (bar); if the best MIDI file for each song is chosen, then the WCSR for our data set is 78.9% (beat) and 75.0% (bar).

In this section, we describe a method to select the estimated best MIDI file for each song. Since we cannot calculate the CSR for unlabeled data, we use a proxy measure based on the AES and ATS scores.

As reported in Section 5.1, some MIDI files are badly aligned. Accordingly, these files will typically not yield good chord labels. Therefore, we discarded all MIDI files with an AES higher than 85%. This leads to a great shift in performance: the WCSR on all MIDI files that are sufficiently aligned, is 72.7% (beat) and 69.3% (bar).

After this MIDI selection step based on alignment quality, we have 592 out of our initial 770 MIDI files left. Since we still have multiple MIDI files per song, we do an additional selection step. For this, we use the ATS score that is calculated by CASSETTE. The CSR correlates with the ATS: the Pearson correlation coefficient is 0.483 for beat segmentation and 0.597 for bar segmentation. For most songs, the CSR of the MIDI with the highest ATS is (almost) as good as the CSR of the actual best MIDI, as shown in Figure 5.7. In this scatter plot, each point belongs to a song from our data set. The CSR of the estimated best MIDI of the song corresponds with its position on the x-axis and the CSR of the actual best MIDI corresponds with its position on the y-axis. Points on the diagonal line (where x = y) are songs for which the best MIDI file was estimated correctly. The plot shows that there are very few songs for which there is a big difference between CSR of the best MIDI and CSR of the estimated best MIDI: there are only three songs for which the difference is higher than 0.5. In two of these songs, the estimated best MIDI was a semitone transposed, compared to the original audio. In the third song, the estimated best MIDI is only a transcription of part of the song. However, in the vast majority of songs, the difference in CSR between the estimated and actual best MIDI files is small: most points are close to the diagonal line. We conclude that the ATS is a suitable score measure to select the estimated best MIDI file for each song. This is also reflected in the performance shown in Table 5.3: the chord sequences from MIDS selected with our proposed selection method (Estimated best) have WCRSs of 75.7% and 72.9% and thereby outperform the performance of all well-aligned MIDI files with three percentage points.

Figure 5.8 shows the CSR distribution for all MIDI files in grey and all estimated best MIDI for each song in a darker shade. It shows that MIDI files corresponding to the poorest chord estimates (grey peaks at the left) are typically not selected.

| Sementation method | WCSR | OvS | UnS | Seg |
|--------------------|------|-----|-----|-----|
| Beat               | 80.0% | 83.0% | 89.1% | 80.8% |
| Bar                | 70.9% | 95.4% | 67.1% | 67.1% |

Table 5.2: Results of MIDI chord recognition for the 50 MIDS with the lowest alignment error.
Figure 5.7: Csr of the real best MIDI compared to the CSR of the estimated best MIDI for both beat and bar segmentation. Points on the diagonal line (i.e. $x = y$) correspond to songs for which the best MIDI file was estimated correctly. The distance in $y$ direction between each point and the line is the difference between the CSR of the best MIDI and the CSR of the estimated best MIDI file.

Figure 5.8: Histograms showing the distribution of CSR for (A) MIDI files with bar segmentation; (B) MIDI files with beat segmentation; and (C) tab files.
Table 5.3: Performance comparison of five MIDI selection methods in terms of WCSR, oversegmentation, undersegmentation and segmentation as defined in Harte (2010).

|               | WCSR  | OvSeg | UnSeg | Seg  |
|---------------|-------|-------|-------|------|
|               | Beat  | Bar   | Beat  | Bar  | Beat  | Bar   | Beat  | Bar   |
| Min CSR       | 45.2% | 43.9% | 75.5% | 88.6%| 75.4% | 62.2% | 65.9% | 60.8% |
| All           | 62.9% | 60.3% | 78.9% | 91.4%| 81.7% | 66.9% | 72.6% | 66.0% |
| Well-aligned  | 72.7% | 69.3% | 80.2% | 93.1%| 86.6% | 71.0% | 76.8% | 70.4% |
| Estimated best| **75.7%** | **72.9%** | **81.3%** | **93.2%**| **87.2%** | **73.3%** | **77.6%** | **72.5%** |
| Max CSR       | 78.9% | 75.0% | 82.3% | 93.2%| 87.2% | 72.9% | 78.6% | 71.9% |

5.4 Conclusion

In this section, we have examined the MIDI subsystem of DECIBEL. This subsystem extracts chord sequences from MIDI files by first aligning the MIDI file to the audio file and then running a simple chord estimation method on the re-aligned MIDI file. In our data set, we have collected multiple MIDI files for each song. The subsystem computes a chord sequence for each MIDI file, so we obtain multiple chord sequences per song. We have seen that we can select “good” (and in many cases the best) MIDI files for each song by (1) ignoring MIDI files with a high alignment error and (2) selection of the MIDI with the highest Average Template Similarity (ATS). This resulted in WCSRs of 75.7% for the beat segmentation and a 72.9% for bar segmentation.
Chapter 6

Automatic Chord Estimation on tabs

In the previous chapters we have seen how our system estimates audio-timed chord labels from audio representations and MIDI files. In this chapter, we will look at DECIBEL’s third subsystem, which uses tab files for estimating chord labels. As we have seen in Section 2.5.3, there exist two types of tabs and we can easily extract chord symbols from both of them: guitar tablature indicates the instrumental fingering, which directly maps to the notes of a chord; in a chord sheet, the chord symbols are represented explicitly, together with the lyric syllables with which they have to be timed. In this chapter, we will explain how DECIBEL uses tabs from either of these two types in order to estimate audio-timed chord labels. The outline of this subsystem is also illustrated in Figure 6.1. First, the tabs are parsed and the chord information is extracted. This step is described in Section 6.1. As a next step, DECIBEL aligns the chord information to the audio file, as described in Section 6.2. This gives us multiple chord estimates: one for each tab file of the corresponding song. In Section 6.3, we explain how DECIBEL selects the expected best tab file for each song. Finally, we summarize the chapter in Section 6.4.

6.1 Tab parsing

Before DECIBEL can align the tab files to the audio, it first needs to parse them and extract the chord information. The used tab parsing method is explained in Section 6.1.1 and evaluated in Section 6.1.2.

6.1.1 Tab parsing methodology

DECIBEL parses the tabs in a similar way to the parser proposed by Macrae (2012). First, it classifies each line in the tab file to a line type. Then, it segments the tab by splitting on empty lines. As a next step, all systems in each segment are identified. We define a system as a set of subsequent lines that belong to each other. For example: a tab system is very common in guitar tablature files and consists of exactly six subsequent tab files. In chord sheets, a common system is the alteration between chord lines and lyrics lines. From these systems, DECIBEL can then extract the chord labels. Thereby, the system retains line information (i.e. the line of the chord in the text file), as this will be used in the tab-audio alignment step. The steps of line type classification,

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**Figure 6.1:** Diagram of DECIBEL’s tab subsystem; the M between Audio File and Tab File indicates that they are manually matched.
segmentation and system and chord extraction are explained more thoroughly in the remainder of this section.

**Line type classification**

For each line in the tab file, DECIBEL estimates its line type using a set of heuristics. We distinguish the following line types: empty, chords, tuning definition, capo change, structural marker, chord definition, tablature, lyrics and combined chord and lyrics.

- A line has the **empty** line type if it is empty or consists only of a space.
- To determine if a line has the **chords** line type, the system first splits the line by spaces. Then it checks if each element of the line matches the chord pattern. An element is a chord if:
  - It consists of at most 10 characters;
  - The first character is a note letter (a, b, c, d, e, f or g);
  - The element does not contain sequences of four digits (as this would indicate a chord definition);
  - The element does not contain symbols; and
  - Any three letter sequence is in the following list: min, add, aug, dim, maj, sus, flat.

- A line has the **tuning** line type if it contains the word “tuning”.
- A line is a **structural marker** if it contains the word “verse”, “chorus” or “bridge”.
- A line is a **tablature line** if it contains at least 10 characters which are a digit, hyphen, vertical bar, slash, letter ‘h’, ‘b’ or ‘p’ or a space and the number of hyphens is larger than the number of spaces.
- A **lyrics line** fulfills each of the following conditions:
  - It does not contain square brackets, the equals sign or the at sign;
  - It contains at most 10 hyphens;
  - Either:
    * It consists of just one word, which has only letter characters and contains at least three of the same letters after each other, like ‘ooooh’ or ‘aaah’; or
    * It contains at least two words.

- To find out if a line is a **combined chords and lyrics** line, DECIBEL first extracts all characters between square brackets ([ and ]). If these characters form a chord, it removes all characters between each pair of square brackets. If the remaining line is a lyrics line, we can conclude that our original line was a combined chords and lyrics file.

- If a line does not satisfy any of these requirements, the parser assigns the line type **undefined**.

**Segmentation**

At this point, we have line types for each line in the tab. As a next step, our parser divides the tab file into segments. A **segment** is simply defined as the lines between lines of the empty line type. In a typical tab, verses and choruses are separated by empty lines and therefore are designated to their own segment.

**System and chord extraction**

Now we have our tab file divided into segments, and we know the line type of each of the lines in a segment. We want to extract the chord labels, but we only extract them from a suitable system. A **system** consists of all of lines that should be played or sung together at the same time. For example, in a typical chord sheet, we will find a lot of systems consisting of a **chord line** above a **lyrics line**, as the chords in the chord line should be
Table 6.1: System types and their chord extraction methods

| System type                        | Chord Extraction                                      |
|------------------------------------|--------------------------------------------------------|
| Combined chords and lyrics line    | Parse chords from combined chords and lyrics line      |
| Chord line                         | Parse chords from chord line                          |
| Exactly six tablature lines        | Parse chords from chord line                          |
| Chord line                         | Parse chords from six tablature lines                  |
| Exactly six tablature lines + 1 to 3 lyrics lines | Parse chords from six tablature lines                  |

DECIBEL assigns each line to the largest possible system. Consider for example a segment consisting of three chord definition lines, followed by a chord line, six tablature lines and one lyrics line. Our parser finds only one system, consisting of a chord line, six tablature lines and a lyrics line. In this case, the six tablature lines do not form a system on their own, as the chord line and lyrics line are also played and sung at the same time. This has to do with the very reason why we consider systems: we only extract one chord sequence from a system, to prevent duplicate chord sequences. This is particularly important in guitar tablatures, as they often have a chord line directly followed by six tab lines with exactly the same chord information. In that case, the parser ignores the six tab lines and extract the chords from the chord line only. For each of the systems, the chord extraction method is displayed in the second column of Table 6.1. We see that there are basically three chord extraction methods:

- **Parse chords from combined chords and lyrics line**: our parser extracts all characters between square brackets ([ and ]), so we have a list of strings, in which each string represents a chord. Then it parses each string by splitting it into a root note, chord type and optional bass note using regular expressions. For example, the chord string “D7/F#” has root note “D”, chord type “7” (dominant seventh chord) and bass note “F#”. Based on these three substrings, the parser now converts the chord string to Harte’s chord notation (Harte et al., 2005). It also saves the line number and character index of the start of the chord string.

- **Parse chords from chord line**: the parser extracts chord strings from the chord line by splitting on spaces and “|” characters. Then it parses each string and converts it to Harte’s chord notation, line numbers and character indices, as described above.

- **Parse chords from six tablature lines**: for each character index (x-value), the parser extracts the six characters that are notated above each other. If all characters are either a digit of an ‘x’, a chord is played at this position. The parser then derives the notes played at the same time based on these characters and their string - for example: if a digit ‘1’ appears on the B string line, the corresponding chord is a C; the digit ‘2’ on the B string corresponds to a C#. Finally it finds the nearest chord from our chord vocabulary (based on cosine distance). Again, it also saves line number (of the first tab line) and character index.

6.1.2 Tab parsing evaluation

In this section, we describe the evaluation of the tab parsing algorithm. For the evaluation of the tab parsing algorithm, we used a random sample of 25 tabs from the data set, as listed in Appendix C. For these 25 tabs, we annotated the untimed chord sequence by hand. Then, we ran DECIBEL’s tab parsing algorithm on these 25 tabs and compared the result to the annotation.

The results are shown in Figure 6.2, in which the height of each bar corresponds to the number of chords in the annotation of a tab file. The True Positives (TP) are the chords in the annotation which are also in the parsed results. In the figure, we see them as the blue part of the bar. The orange part of the bar corresponds
Figure 6.2: Recall of chords in our sample of 25 tab files.

to the False Negatives (FN): the chords that are in the annotation of a tab file, but not found by our parser. As we see in this figure, the parser finds (almost) all chords in most of the songs, as the orange part is very small. There were no chords in either the annotation or the parser output of the third, tenth and 23rd song. For the other songs, chords were missing in the tab output for the following reasons:

- The parser does not recognize chords that are glued after each other (without a separator) in the tab file;
- The parser does not recognize chords in a line with more text or strange symbols, as such a line is not classified as a chord line;
- The parser does not recognize chords in guitar tablature systems when there are no digits or 'x' in all six lines.

In some songs, text that was actually not a chord was misinterpreted as chords. This happened in one tab file which added some rhythm information by for example putting a 'Q' above a chord symbol for quarter note durations and an 'E' for eighth note durations. Our parser falsely detected a line of eighth notes as a sequence of E chords. In another line, chord vocabulary information was falsely detected as a chord line.

Still, in most songs we see that the tab parser performs quite well, as there are no missing chords in 15 of the 25 songs.

6.2 Jump Alignment

Having completed the tab parsing step, we have extracted the chord labels and their corresponding line and word numbers from the tab file. However, tab files retain no timing information, so we need an additional step to align the chord labels to the audio file. As we have seen in Section 1.3, there already exist four different algorithms by McVicar et al. (2011b) that incorporate tab information into a HMM-based system for audio chord estimation. To the best of our knowledge, these are the only algorithms that use tabs in audio ACE. The most promising of these four algorithms is Jump Alignment. In this section, we describe and evaluate our implementation of Jump Alignment.

Jump Alignment is based on a Hidden Markov Model (HMM). A HMM models the joint probability distribution \( P(X, y|\Theta) \) over the feature vectors \( X \) and the chord labels \( y \), where \( \Theta \) are the parameters of the model. In Section 6.2.1, we describe the preprocessing steps that are used for extraction of the features \( X \) and the chord labels \( y \). Section 6.2.2 gives an introduction to the HMM. The details on the Jump Alignment algorithm are treated in Section 6.2.3.
6.2.1 Preprocessing

First, the audio file needs to be preprocessed. For this purpose, we use the python package librosa (McFee et al., 2018). First, we convert the audio file to mono. Then, we use the HPSS function to separate the harmonic and percussive elements of the audio. Then, we extract chroma from the harmonic part, using constant-Q transform with a sampling rate of 22050 and a hop length of 256 samples. Now we have chroma features for each sample, but we expect that the great majority of chord changes occurs on a beat. Therefore, we beat-synchronize the features: we run a beat-extraction function on the percussive part of the audio and average the chroma features between the consecutive beat positions. The chord annotations need to be beat-synchronized as well. We do this by taking the most prevalent chord label between beats. Each mean feature vector with the corresponding beat-synchronized chord label is regarded as one frame. Now we have the feature vectors \( X \) and chord labels \( y \) for each song, which we feed to our HMM.

6.2.2 Hidden Markov Model

As we have seen in Section 4.1.2, a HMM models the joint probability distribution \( P(X, y|\Theta) \) over the feature vectors \( X \) and the chord labels \( y \), where \( \Theta \) are the parameters of the model. The HMM is an extension of the Markov chain in which the states are not directly observable (but hidden). In this section, we give a summary of the Hidden Markov Model, based on the tutorial by Rabiner (1989) and Section 5.3.2 from Müller (2015).

In a Markov chain, we make the assumption that the probability from the current state \( s_t \) to the next state \( s_{t+1} \) only depends on the current state, and not on any of the previous states. Formally:

\[
P(Y_{t+1} = s_{t+1}|Y_1 = s_1, Y_2 = s_2, \ldots, Y_t = s_t) = P(Y_{t+1} = s_{t+1}|Y_t = s_t)
\]

This assumption is called the Markov property. In our implementation, states are represented by chord labels. Any chord label is an element from the discrete set of chords from our chord vocabulary. Although we could use any chord vocabulary, we use the vocabulary with all major and minor chords and the no-chord symbol. Our vocabulary thus consists of 25 items. Thanks to the Markov property, we can efficiently model the probability that chord \( j \) occurs after chord \( i \) by the transition probability \( P_{tr}(y_t = j|y_{t-1} = i) \). Given a chord vocabulary of 25 items, we can model all transition probabilities in \( 25 \cdot 25 = 625 \) probability values, that can be efficiently stored in the matrix \( P_{tr} \).

The first chord of a chord progression cannot be computed from its previous chord. This information is specified by the initial state probabilities. There are 25 initial state probability values, stored in the vector \( P_{ini} \), in which \( P_{ini}(y_1 = c) \) is the probability that the first chord is chord \( c \).

Based on the Markov chain, we could now compute the probability for a given chord label given a sequence of chord labels, or compute the probability of any chord label sequence. However, in a ACE scenario, we cannot directly observe the chord labels, but we do observe a sequence of chroma features that is related to the chord labels. We thus need to expand our model, by adding emission probabilities. The resulting model is a Hidden Markov Model. The emission probability \( P_{obs}(X_t|y_t) \) equals the probability of an observation (chroma feature vector) \( X \) given a chord label \( y \) at time \( t \). In contrast to transition and initial state probabilities, the emission probabilities cannot be represented by a matrix, as chroma features are continuous. Instead, they are modeled by continuous probability density functions: the observation probability distribution for each of the 25 chord labels \( a_i \) in the vocabulary as a 12-dimensional Gaussian with 12-dimensional mean vector \( \mu_i \) and 12 × 12 covariance matrix \( \Sigma_i \). We can now find our emission probabilities for any observed chroma feature vector \( x_t \) and any chord label \( a_i \), using the Gaussian with parameters \( \mu_i \) and \( \Sigma_i \):

\[
P_{obs}(x_t|\mu_i, \Sigma_i) = \frac{1}{(2\pi)^{6}|\Sigma_i|^{1/2}} \exp\left[-\frac{1}{2}(x_t-\mu_i)^T\Sigma_i^{-1}(x_t-\mu_i)\right]
\]

We now have seen that a HMM is parametrized by transition, initial state and emission probabilities. We define \( \Theta \) as the set of these parameters:

\[
\Theta = \{P_{tr}, P_{ini}, \{\mu_i\}_{i=1}^{25}, \{\Sigma_i\}_{i=1}^{25}\}
\]

There exist different ways of estimating \( \Theta \). We adopt the machine learning approach, that is, we train the probabilities on a subset of our data set. In our case, the training set is a 100-song random sample of our
HMMs can be used to solve three basic problems, as pointed out in Rabiner (1989). One of these problems,\( X \)

Now we know all elements of the HMM, we can represent the joint representation for the chroma feature vectors \( X \) and chord labels \( y \) mathematically in the following equation:

\[
P(X, y|\Theta) = P_{\text{init}}(y_1|\Theta) \cdot P_{\text{obs}}(x_1|y_1, \Theta) \cdot \prod_{t=2}^{\|y\|} P_{\text{tr}}(y_t|y_{t-1}, \Theta) \cdot P_{\text{obs}}(x_t|y_t, \Theta)
\]  

(6.4)

HMMs can be used to solve three basic problems, as pointed out in Rabiner (1989). One of these problems, which is called the uncovering problem or decoding problem, is the relevant problem for our purpose: automatic chord estimation. The goal of the uncovering problem is to find the state (chord) sequence that best explains the observed (chroma) feature sequence. Formally: we want to find the chord label sequence \( y^* \) where

\[
y^* = \arg\max_y P(y|X, \Theta).
\]

Note that this is equivalent to finding \( y^* = \arg\max_y P(y, X|\Theta) \).

Note that the optimal chord sequence for an observation sequence of \( n \) elements starts with the optimal chord sequence for the observation sequence of the first \( n - 1 \) elements. The Viterbi algorithm efficiently solves the uncovering problem by exploiting this property. The pseudocode of Viterbi is given in Algorithm 2. In each iteration, the algorithm computes the indices \( i_1, i_2, \ldots, i_T \) to the optimal chord sequence for \( X_1, X_2, \ldots, X_T \) (i.e. the first \( t \) steps of the observation sequence \( X \)) ending with chord label \( y_t \). The result is then stored in the matrices \( V \) and \( B \) in \( V \), the algorithm keeps the likelihood of the current path, while the chord index is stored in \( B \). When calculating a chord sequence of length \( n \), the likelihoods of the optimal chord sequences of length \( n - 1 \) can be efficiently retrieved by reading the corresponding value from matrix \( V \). In the termination phase, we can read the final chord index \( i_T \) by maximizing over the last column of \( B \) and find the full optimal chord sequence by following the backpointers in \( B \) back in time. We can also read the likelihood of the full optimal chord sequence from \( V[i_T, T] \).

**Algorithm 2** Pseudocode of the Viterbi algorithm

1. \textbf{function} \textsc{Viterbi}(Observation Sequence \( X_1, X_2, \ldots, X_T \), HMM specified by \( \Theta \), Chord alphabet \( y_1, y_2, \ldots, y_{25} \))
2. \hspace{1cm} Initialize Viterbi Matrix \( V \) of size \( 25 \times T \) \hspace{1cm} \text{▷ Initialization}
3. \hspace{1cm} Initialize Backpointer Matrix \( B \) of size \( 25 \times (T - 1) \).
4. \hspace{1cm} for all \( i \in [1, 25] \) do
5. \hspace{2cm} \( V[i, 1] = P_{\text{init}}[y_i] \cdot P_{\text{obs}}(y_i|X_1) \)
6. \hspace{1cm} end for
7. \hspace{1cm} for all \( t \in [2, T] \) do
8. \hspace{2cm} for all \( i \in [1, 25] \) do
9. \hspace{4cm} \( V[i, t] = \max_{j=1}^{25} V[j, t-1] \cdot P_{\text{tr}}[y_j, y_i] \cdot P_{\text{obs}}(y_i|X_t) \)
10. \hspace{2cm} \( B[i, t-1] = \arg\max_{j=1}^{25} V[j, t-1] \cdot P_{\text{tr}}[y_j, y_i] \)
11. \hspace{2cm} end for
12. \hspace{1cm} end for
13. \hspace{1cm} \( i_T = \arg\max_{j=1}^{25} V[j, T] \) \hspace{1cm} \text{▷ Termination}
14. \hspace{1cm} for all \( t \in [T-1, 1] \) do
15. \hspace{2cm} \( i_t = B[i_{t+1}, t] \)
16. \hspace{1cm} end for
17. \hspace{1cm} return Chord Sequence \( y_{i_1}, y_{i_2}, \ldots, y_{i_T} \) and Likelihood Value \( V[i_T, T] \)
18. \textbf{end function}

### 6.2.3 Jump Alignment

Jump Alignment is an extension to the HMM described in the previous section, which utilizes the chords that are parsed from tabs. Following McVicar et al. (2011b), we refer to these chords parsed from tab files as Untimed Chord Sequences (UCSs). Compared to the original HMM, in the Jump Alignment algorithm the state space and transition probabilities are altered in such a way that it can align the UCSs to audio, while allowing for jumps to the start of other lines. We will explain how this works in the remainder of this section.
Let us assume that we have an audio file and tab file from the same song. Let $e = e_1, e_2, \ldots, e_L$ be the UCS we extracted from the tab file, applying the parsing algorithm described in Section 6.1. Because we want an alignment between the audio file and this UCS $e$, we define a new set of hidden states: $Y' = \{1, 2, \ldots, L\}$ corresponds to the indices of the chords in $e$. For example, given a (very small) chord vocabulary $[C, D, E]$ and the UCS $[C, E, D, E, D, C, E]$, our hidden state set $Y'$ would be $[1, 3, 2, 3, 2, 1, 3]$. Note that different hidden states can now refer to different occurrences of the same chord, in contrast to our original state space.

We also need to alter the transition probability distribution $P'_{tr}$, as we only want to allow chord sequences that are alignments of $e$, our Untimed Chord Sequence. However, McVicar et al. (2011b) showed that exact alignment of $e$ to audio results in a decrease in performance compared to the original HMM, because repetition cues (like “play this verse twice”) are not interpreted by the tab parser. In addition, some tabs do not specify the chords of all verses. Therefore, Jump Alignment allows jumps from the end of a line in the tab file to the beginning of any line (the current one, of any of the previous or subsequent lines). The new transition probability distribution is expressed as:

$$
P'_{tr}(j|i, \Theta, e) = \begin{cases} 
\frac{1}{Z_i}P_{tr}(e_i, e_j) & \text{if } j \in \{i, i+1\}, \\
\frac{b_f}{Z_i}P_{tr}(e_i, e_j) & \text{if } i < j \text{ and } i \text{ is the end and } j \text{ is the beginning of a line}, \\
\frac{b_b}{Z_i}P_{tr}(e_i, e_j) & \text{if } i > j \text{ and } i \text{ is the end and } j \text{ is the beginning of a line}, \\
0 & \text{otherwise.} 
\end{cases} \tag{6.5}
$$

$Z_i$ is a normalization factor, which is used to re-normalize $P'_{tr}$ so that the transition probabilities $P'_{tr}(y_j|y_i, \Theta, e)$ sum to one. $p_f$ is the probability of jumping forward when this is allowed. Likewise, $p_b$ is the probability of a jump backwards, provided that this is allowed.

The forward probability $p_f$ and backward probability $p_b$ need to be specified. We estimate the optimal $p_f$ and $p_b$ as follows: first, we manually select a subset of 22 songs for which we are sure that they are in the right key (so we do not need to consider transpositions). Appendix D lists these songs. Then, we run the Jump Alignment algorithm with all combinations of forward and backward probabilities between 0 and 1 in steps of 0.05 and evaluate the resulting chord label sequences in terms of CSR. We will use the $p_f$ and $p_b$ with the highest average CSR.

Figure 6.3 shows the average CSR for our 22-song subset, given a ($p_f, p_b$) parameter setting. We see that positive forward or backward probabilities improve CSR compared to a strict alignment (in which $p_f = 0$ and $p_b = 0$): particularly non-zero backward probabilities yield considerably better chord label sequences than $p_b$‘s of zero. However, if the forward and backward probabilities become too large, the average CSR decreases as the importance of the order of lines in the tab file decreases. We find an optimal parameter setting of $p_f = 0.05$ and $p_b = 0.05$. This is the parameter setting that we use in our implementation of Jump Alignment.

Tabs are often notated in a transposed key compared to the original audio file, because some keys are easier to play on the guitar than others. In order to correct for such “simplified” tabs, Jump Alignment considers the tab files in all 12 transpositions and chooses the transposition with the highest likelihood.

### 6.3 Tab file selection

The performance of the jump alignment algorithm is dependent on the quality of the tab file. Following McVicar et al. (2011b), we select for each song the tab file for which the log-likelihood was the highest. The results for our full 200 song dataset are shown in Table 6.2. If we would take the average CSR of all tabs for a song, the WCSR is 72.4%. The upper limit for the selection method is a WCSR of 78.7%: this is what we would get if we selected the best tab. Since we do not know the CSR for unlabelled data, we select the expected best tab-file for each song based on the log-likelihood, following McVicar et al. (2011b). By choosing the tab file with the highest log-likelihood for each song, the resulting WCSR improves to 75.3%. The distribution of CSRs of selected tab files compared to all tab files is also shown in Figure 5.8.
Figure 6.3: Average CSR for 22-song subset given $p_f$ and $p_b$. We find an optimal parameter setting of $p_f = 0.05$ and $p_b = 0.05$.

| Table 6.2: WCSR of all songs, with different tab file selection methods |
|---------------------------------------------------------------|
| **WCSR**                                                       |
| Worst CSR of all tabs                                         | 59.1% |
| Average CSR of all tabs                                       | 72.4% |
| Best log-likelihood of all tabs                               | 75.3% |
| Best CSR of all tabs                                          | 78.7% |

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6.4 Conclusion

In this section, we have examined the last of the three representation-specific subsystems of DECIBEL: the tab subsystem. This subsystem consists of a parser that extracts Untimed Chord Sequences (UCSs) from guitar tablature or chord sheets, thereby retaining line information. This is then input for the Jump Alignment algorithm, which aligns the UCSs to the audio recording. When selecting the estimated best tabs for each song, based on log-likelihood, this subsystem reaches a WCSR of 75.3% on the Isophonics data set.
Chapter 7

Data fusion

DECIBEL estimates chord label sequences from different music representations, i.e. audio, MIDI and tab files, as we have seen in the previous three chapters. This results in a set of chord label sequences for each song in our data set. This set of chord labels forms a rich harmonic representation that is already interesting in itself, as we will see in Section 7.1. However, in order to answer our research question we need to combine these chord label sequences into one final sequence (and compare the resulting chord sequence to the sequence obtained by using only an audio ACE method). DECIBEL achieves this using a data fusion step. In this chapter, we motivate the chosen data fusion method by a literature study and an evaluation of various methods.

![Diagram of DECIBEL's data fusion subsystem](image)

Figure 7.1: Diagram of DECIBEL’s data fusion subsystem. The set of MIDI- audio- and tab-based audio-timed chord label sequences forms a rich harmonic representation. Our data fusion combines all chord label sequences for a song into a single output chord label sequence.

7.1 A rich harmonic representation

In the previous chapters we have seen how DECIBEL’s subsystems estimate chord label sequences from audio, MIDI and tab representations of a song. These three representations store musical content of the same song in fundamentally different ways: as we have seen in Section 2.5, audio files are obtained by digitizing the waveform; MIDI files are a series of note on and note off events; whereas tab files show the guitar fingering or chord labels, aligned to the lyrics. The timing information in audio is represented in seconds, based on the underlying performance; in MIDI files, timing is measured in ticks; in tabs, timing information is missing. Also, the source of information differs: audio files are recordings of a performance; MIDI files are either score-based or transcriptions of a recording; tabs can be considered as (untimed) chord label sequences, manually annotated by music enthusiasts.

However, the chord label estimation and synchronization steps performed by DECIBEL’s subsystems transform these three heterogeneous representations into a homogeneous format, i.e. as a series of (start time, end time, chord label) 3-tuples. The combination of the set of chord label sequences from each of the representations of a song results in a rich harmonic representation.
This rich harmonic representation is a very interesting by-product of the DECIBEL system, as it allows for cross-version analysis, i.e., comparing analysis results from different representations. The chord label sequences can easily be visualized, which makes it very easy to see the consistencies and inconsistencies in chord labels between different representations. As identified earlier in research by Ewert et al. (2012) and Konz et al. (2013), having such a unified view of different analysis results deepens the understanding of both the algorithm’s behavior and the properties of the underlying musical material.

Consider for example the visualization of the chord label sequence for the Beatles song *Golden Slumbers* in Figure 7.2. In our data set, we have matched three MIDI files and eight tab files to the audio version of the song. CASSETTE, our MIDI ACE method, analyzes the chords both on a bar and a beat level, so we have six chord label sequences based on the three MIDI files. In combination with the eight chord label sequences based on the tab files and a single analysis by the Chordify algorithm based on the audio file, we have $6 + 8 + 1 = 15$ chord label sequences. Each of these estimated chord sequences, as well as the ground truth, is visually represented by a horizontal bar in which the color represent the chord label and time in seconds can be read from the position on the $x$-axis. In this example, we observe there are some parts of the song for which (most of) the 15 estimated chord sequences agree on the labels, e.g., the D minor chord starting after 11 seconds; the G major chord sounding immediately thereafter or the C major chord that starts at 32 seconds. However, in other musical passages there is some disagreement. If there is a single deviating chord sequence estimation, this is typically either due to some error in the MIDI or tab file or due to an error in the estimation method. For example, when estimating the chord sounding in the 38th second from our third MIDI file, using CASSETTE on the bar level, we falsely find a F major chord instead of a C major chord. In some passages, we observe multiple “clusters” of possible chord labels, i.e., different perspectives on the harmonic content of a musical passage, each of them supported by multiple chord label estimations. For example, we can consider the start of the song either as a long A minor chord or as a sequence of A minor and C major chords. Also, there exist different perspectives on the chord in the 23rd second (is it a C major, E major, F minor or something else?) and the modality of the A (major or minor) chord starting after 62 seconds.

MIDI and tab files implicitly incorporate musical knowledge, as they are (in the popular music genre) typically transcriptions made by music enthusiasts. Therefore, the comparison of analysis results from different music representations reveals passages in the music for which there are multiple possible perspectives. Studying these passages can give us a deeper understanding of subjectivity issues in the musical material.

In this section, we have seen that the chord label sequences estimated on different music representations of the same song together form a rich harmonic representation. Visualization of this harmonic representation can give valuable insights in different perspectives on chord labels within a specific segment of the song. This makes large-scale cross-version analysis feasible. Moreover, it bridges the gap between technical, audio-oriented, musical signal processing and non-technical, score-oriented musicology. A detailed analysis on the different harmonic perspectives on the Beatles and Queen songs from our data set is beyond the scope of this research, but would be an interesting direction of future work which would provide better insights in the subjectivity issues in harmonic analysis of popular music.

### 7.2 Related Work on data fusion

In the remainder of this chapter, we study data fusion methods to combine chord label sequence obtained from DECIBEL’s audio, MIDI and tab subsystems into a single output sequence. The integration of heterogeneous output of multiple ACE algorithms using data fusion is a new idea, which was recently proposed by Koops et al. (2016). In this study, the authors experiment with three different techniques to combine chord sequence estimates from different sources (the MIREX 2013 ACE submissions, applied to the Billboard data set) into one final output sequence for each song. They show that their proposed data fusion method yields the best results in terms of WCSR. Also, they show that the output sequence found by their data fusion method is an improvement to the best scoring team, with an increase between 3.6 percentage point and 5.4 percentage point compared to the best team.

The three techniques used for combining chord label sequences are random picking (RND), majority voting (MV) and data fusion (DF). In all three techniques, the system proposed in Koops et al. (2016) first samples the chord label sequence from each source in segments of 10 milliseconds. In the RND technique, the output chord label for each segment is found by picking the corresponding label from a randomly chosen source. For MV, the output chord label for each segment is the most frequent label of all sources. If multiple labels are most
The source accuracy \( A(S_i) \) is the arithmetic mean of the probabilities of all chord labels a source \( S_i \) provides. Initially, these chord label probabilities may be based on a frequency count. A source with a high source accuracy inherently has a lot of chord labels that agree with other sources, and therefore can be considered more trustworthy. Assuming that the sources are independent, the source accuracy is the probability that a source provides the appropriate chord. On the other hand, the probability that a source provides an inappropriate chord can be computed with \( 1 - \frac{A(S_i)}{n} \), given \( n \) possible inappropriate chord labels. The source vote count \( V.S(S_i) \) combines these probabilities and is computed as follows: \( V.S(S_i) = \ln \frac{n \cdot A(S_i)}{1 - A(S_i)} \). Chord labels of sources with higher source vote counts are more likely to be picked than labels of sources with low source vote counts, as we will see shortly.

The goal of the data fusion method is to determine the most likely chord label for each segment, given a number...
of sources. To this end, the data fusion method computes a chord label vote count \( VC(\mathcal{L}) \) for each chord label \( \mathcal{L} \). The chord label vote count is dependent on both the number of sources with a matching chord label and the source vote count of these sources, as expressed in the formula \( VC(\mathcal{L}) = \sum_{\sigma \in S^L} V S(\sigma) \), in which \( S^L \) is the set of sources with chord label \( \mathcal{L} \).

From the label vote counts, we can compute chord label probabilities for each chord label \( \mathcal{L} \) by \( P(\mathcal{L}) = \frac{\exp(VC(\mathcal{L}))}{\sum_{\mathcal{L} \in D} \exp(VC(\mathcal{U}))} \). As we divide the chord label vote count of our chord label by the chord label vote count of all possible chord labels \( D \), this results in a probability value between 0 and 1.

The data fusion method proposed by Koops et al. (2016) also takes the dependency between sources into account, following the intuition that sources that are dependent of each other share many uncommon chord labels. Based on the number of shared uncommon chords with other sources, the authors compute a source dependency weight \( I(S_i, \mathcal{L}) \), which represents the probability that a source \( S_i \) provides a chord label \( \mathcal{L} \) independently.

We now have seen the definitions of chord label probabilities, source accuracy and source dependency. Note that they are all defined in terms of each other. As a solution to this paradoxical situation, Koops et al. (2016) propose to initialize the chord label probabilities with equal probabilities and iteratively compute source dependency, chord label probabilities and source accuracy until convergence is reached. Finally, their data fusion method selects for each segment the chord label with the highest chord label probability.

In their experiments, the authors compare the performance of DF to RND and MV for two subsets of the Billboard data set. Each of these three chord sequence combination methods is computed on all twelve MIREX 2013 ACE submissions for both Billboard subsets. The Billboard annotations serve as ground truth. Their results show that the DF method significantly outperforms both the RND and MV methods as well as each of the individual submissions. We can conclude that combining chord label sequences from multiple sources using data fusion is a promising strategy to improve ACE.

### 7.3 Data fusion experiments

In the previous section, we have seen that the heterogeneous output of multiple ACE systems can be integrated into a single output chord sequence, using data fusion. Although the results obtained in previous work are solely based on audio data, the data fusion method can also be applied to chord label sequences that are based on symbolic data. This is exactly what DECIBEL’s data fusion subsystem does: the subsystem uses the chord sequences from audio, MIDI and tabs and integrates them in a final output sequence. In contrast to earlier work, in our case the number of sources differs per song. That is why we experiment with a selection strategy that elects only one source per representation. In this section, we will explain DECIBEL’s data fusion implementations.

In order to test if DECIBEL improves current audio ACE systems, we need to combine these chord label sequences into one final sequence. DECIBEL achieves this using a data fusion step. In this section, we motivate the chosen data fusion method by an evaluation of various methods. These methods are based on earlier work by Koops et al. (2016). In contrast to earlier work, DECIBEL needs to combine a varying number of sources per song. That is why we experimented with a selection strategy that selects only one source per representation. We compare two selection strategies in combination with three different integration methods. The two selection strategies are ALL and BEST: ALL takes the chord sequences of all tabs and MIDI files as sources. BEST only uses the sources of the expected best tab and MIDI file for each song, as described in Section 5.3 and 6.3. There are eight songs for which no MIDI is selected, since all MIDs were badly aligned. For these songs, BEST only combines the audio and tab sequences.

The three integration methods are based on earlier work (Koops et al., 2016). We first divide each input chord sequence in 10 millisecond samples. Then we integrate the sources, selected using ALL/BEST, with either random picking (RND), majority voting (MV) or data fusion (DF). The implementations of RND and MV are unchanged compared to Koops et al. (2016): given a specific sample, RND takes the chord label of an arbitrary source, while MV assigns the chord label used by most of the sources.

Our implementation of the DF technique takes into account both the expected accuracy of sources and the probability of the labels provided by the sources. Let \( \mathcal{X} \) be the set of samples, \( \mathcal{V} \) be the chord vocabulary, \( S \) be the sources selected by the integration method and let \( \mathcal{L} : S \times \mathcal{X} \times \mathcal{V} \mapsto \{0, 1\} \) be a labelling function such
that $\mathcal{L}(s, x, v) = 1$ if source $s$ assigns chord $v$ to segment $x$ and 0 otherwise.

The source accuracy $A[s]$ is the probability that a source $s$ provides appropriate chords; the chord label probability $P[x, v]$ is the probability of chord label $v$ at segment $x$, given the chord labels of the sources. The chord label probability is defined based on the labelling $\mathcal{L}$ and the chord label vote count $VC[x, v]$. This value determines the influence of each source on the final label, based on its source accuracy. These values are iteratively computed as follows:

\begin{align*}
A[s] &= \frac{\sum_{x \in X} \sum_{v \in V} P[x, v] \cdot \mathcal{L}(s, x, v)}{|X|} \\
VC[x, v] &= \sum_{s \in S} \mathcal{L}(s, x, v) \cdot \ln \frac{(|V| - 1)A[s]}{1 - A[s]} \\
P[x, v] &= \frac{\exp VC[x, v]}{\sum_{v' \in V} \exp VC[x, v']}
\end{align*}

$A[s]$, $VC[x, v]$ and $P[x, v]$ are defined in terms of each other. Therefore, we use an alternative equation for the initial computation of the chord label probability $P_0[x, v]$: 

\begin{equation}
P_0[x, v] = \frac{\sum_{s \in S} \mathcal{L}(s, x, v)}{|S|}
\end{equation}

The final chord labelling for DF is obtained by first computing Equation 7.4 and then repeatedly updating Equations 7.1–7.3. Whereas Koops et al. (2016) repeat until a fixed point is reached, we always repeat 5 times. After this, we assign the chord label $v$ with the highest probability $P[x, v]$ to each segment $x$ to obtain the final DF chord sequence.

### 7.4 Data fusion results

We now compare the performance of each of the six combinations of integration methods and selection strategies (i.e., RND-ALL, RND-BEST, MV-ALL, MV-BEST, DF-ALL and DF-BEST), applied to each of our ten audio ACE systems. Friedman tests (Friedman, 1937) for each of these ten audio ACE show that the integration methods and selection strategies give significantly different results in terms of CSR. Consequently, we perform a Tukey’s Honest Significant Difference post-hoc test (Tukey, 1949) to identify which integration-selection combinations are significantly different. The results are visually represented in Figure 7.3. In these figures, we can easily observe which differences are significant because the corresponding horizontal lines do not overlap in the $y$-direction. Consider for example Figure 7.3a. Here we see that both RND methods are significantly worse than the original audio ACE system (CHF). There is no significant difference between CHF and DF-ALL. MV-ALL is better than CHF, but the difference is not found significant by Tukey’s HSD test. MV-BEST and DF-BEST perform significantly better than the original CHF system, and DF-BEST turns out to be the winner.

When examining the test results for all ten audio ACE systems for all ten state-of-the-art audio ACE systems in combination with all two selection strategies and all three integration methods, we make four observations.

**First**, the random picking integration method always performs worse than the original audio ACE system, regardless of the chosen selection strategy. This is consistent with findings in earlier work (Koops et al., 2016). From this observation, we conclude that agreements between sources should be taken into account.

**Second**, the BEST selection method always performs better than the ALL selection method. The explanation for this is as follows: given a poor MIDI or tab file, DECIBEL’s MIDI or tab subsystem will find a poor chord label sequence. In the ALL selection method, this chord label sequence will, to a greater or lesser extent, be integrated in the final output sequence, which deteriorates the output sequence’s quality, whereas the BEST selection method (hopefully) ignores this poor chord label sequence.

**Third**, we observe that the difference between BEST and ALL is even larger for the DF integration method than for MV. A possible explanation for this is that chord label sequences from tabs are often undersegmented, for
Figure 7.3: Visual representation of the differences in terms of Chord Symbol Recall between different data fusion methods, for CHF and each of the MIREX 2017 and/or 2018 ACE submissions. For each of the horizontal lines that do not overlap in the y-direction, the difference in CSR between the corresponding data fusion methods is significant.
example because chord changes in instrumental parts or very short chords are often not detected. This is typical for tabs and therefore can occur at multiple (independent) tabs of the same song. Consequently, suboptimal chord sequences from tabs could get a high source accuracy in DF-ALL, and therefore substantially influence the final output sequence. DF-BEST only considers the expected best tab and MIDI file. If the expected best tab is undersegmented, it will probably get a low source accuracy, because chord sequences from MIDI and audio have less undersegmentation issues. The difference between MV-ALL and MV-BEST is smaller, as MV does not use source accuracies.

Our fourth and final observation is that DF-BEST performs better than MV-BEST, although the difference is not always significant. However, DF-BEST is always better than the original audio ACE system. As shown in Table 7.1, the improvement is significant for all tested audio methods except JLCX1 and JLCX2.

When comparing the oversegmentation measure for our integration methods, we can do another observation: RAND and MV tend to oversegment, in contrast to DF. This becomes clear when looking at the chord sequences for the song Things We Said Today in Figure 7.4. Note that both RND chord sequences have way too many chord changes, resulting in a low oversegmentation score. Both MV chord sequences are oversegmented as well, albeit to a lower degree. On the other hand, we see no oversegmentation issues in the DF chord label sequence.

![Figure 7.4: Chord label sequences for the Beatles song Things We Said Today. CSR = Chord Symbol Recall; OvS = oversegmentation; UnS = undersegmentation; and Seg = segmentation. Note that RAND and MV tend to oversegment, in contrast to DF.](image)

From these observations, we can conclude that DF-BEST is the best selection-integration combination. Table 7.1 shows a comparison between the WCSR of each of the ten audio ACE systems and DF-BEST applied to each system. The table shows that using DF-BEST improves ACE WCSR on average by 3.05%.

Finally, let us look at the song-wise performance of DF-BEST compared to the original audio file. Figure 7.5
Table 7.1: WCSR of audio ACE systems and DF-BEST. Note that two of the 2017 systems were resubmitted in MIREX 2018. Significant improvements are shown in bold. Using DF-BEST improves ACE WCSR on average by 3.05%.

| Audio ACE | MIREX | Audio WCSR | DF-BEST WCSR | Improvement | DF-GT-BEST WCSR |
|-----------|-------|-------------|---------------|-------------|-----------------|
| CHF       | -     | 82.0%       | 84.6%         | 2.6%        | 86.3%           |
| CM2/CM1   | 2017, 2018 | 75.7%      | 81.7%         | 6.0%        | 84.1%           |
| JLW1      | 2017  | 79.0%       | 83.2%         | 4.2%        | 84.6%           |
| JLW2      | 2017  | 78.5%       | 83.0%         | 4.5%        | 84.3%           |
| KBK1      | 2017  | 82.8%       | 85.5%         | 2.6%        | 86.8%           |
| KBK2/FK2  | 2017, 2018 | 87.3% | 88.2%         | 0.8%        | 88.9%           |
| WL1       | 2017  | 79.9%       | 83.6%         | 3.8%        | 85.0%           |
| JLCX1     | 2018  | 86.3%       | 87.1%         | 0.9%        | 88.1%           |
| JLCX2     | 2018  | 86.5%       | 87.1%         | 0.6%        | 88.1%           |
| SG1       | 2018  | 79.5%       | 84.0%         | 4.6%        | 85.8%           |

shows the difference between the CSR of the chord label sequence obtained by DF-BEST and the CSR of the chord label sequence found by the original audio ACE system. The song keys are given on the y-axis, and the length of the horizontal bars correspond to the difference in CSR. If a bar is located on the right side of x = 0, then the chord label sequence found by DF-BEST is better than the sequence found by the original audio ACE system. We see that this is the case for the vast majority of songs in our dataset. On the other hand, if a bar is located on the left side of x = 0, DF-BEST performs worse than the original audio ACE system. From all ten plots, we see one song for which DF-BEST performs considerably worse. This is song number 174, Let it be by The Beatles. This song has an issue similar to Don’t pass me by, as we saw in Figure 4.5: the audio file that we used was shifted compared to the audio file that was used in the MIREX competition. That is why the chord label sequence found by DF-BEST is shifted and therefore is not consistent with the Isophonics annotations any more. We see another ‘peak’ to the left at song 196, We will rock you by Queen, for the CHF algorithm. The reason for this difference is that CHF estimates the chord label sequence for this song quite well, as shown in Figure 7.6. However, the best found MIDI and tab file find very different chord labels for the first 90 seconds of the song and therefore the result found by DF-BEST is based on the tab file, which apparently had the highest source accuracy. In practice, this song starts with a lot of percussion and little harmonic content. Therefore, it is not so surprising that there are multiple views on the chord labels for this song.

In this section we have seen that DF-BEST is the best combination of the selection strategy and integration method. DF-BEST performs better than the original audio algorithm in terms of WCSR and does not suffer from oversegmentation.
Figure 7.5: CSR of df-BEST compared to the CSR of the original audio ACE system for each song in the dataset. The difference between the CSR of df-BEST and the CSR of the original audio ACE system is given on the x-axis; the y-axis gives the index of the song in our data set. Horizontal lines on the right side of \( x = 0 \) correspond to songs for which df-BEST improves the original system in terms of CSR, while the horizontal lines on the left side of \( x = 0 \) correspond to songs for which the original ACE system produced better results in terms of CSR.
Figure 7.6: Chord label sequences for the Queen song *We will rock you*. Note: CSR = Chord Symbol Recall; OvS = oversegmentation; UnS = undersegmentation; and Seg = segmentation.
Chapter 8

Conclusion

The goal of this study was to test whether exploiting MIDs and tabs improves Automatic Chord Estimation (ACE). The ACE task is concerned with estimating chords in audio recordings or symbolic representations of music and has applications in both music performance and in Music Information Retrieval (MIR). Many systems for audio ACE exist, but ACE is not yet a solved problem: as we have identified in Section 1.1, existing methods suffer from stagnation and overfitting to subjective annotations. There is need for a new strategy that overcomes existing stagnation in ACE without further overfitting to existing (subjective) data sets. An improved system for ACE would have positive consequences for millions of performers and MIR systems for e.g. cover song identification and genre classification.

For this purpose, we created a new system, DECIBEL, that (1) aligns MIDI and tab files to audio recordings and uses representation-specific chord estimation techniques for both symbolic and audio formats to estimate chord sequences for each file; and (2) integrates the resulting heterogeneous chord sequences into one final output sequence. In this concluding chapter, we will give an overview of our contributions and some directions for future work.

8.1 Contributions

The main contributions of this research are twofold: we designed a system that automatically extracts a rich harmonic representation and used this representation to improve state-of-the-art audio ACE systems. In addition, we extended the existing Isophonics Reference Annotations with a large set of MIDI and tab files, which we manually matched to the annotations. As a final contribution, we made the implementation of our system available on GitHub.

8.1.1 Rich harmonic representation

As we have seen in Chapters 4, 5 and 6, DECIBEL has three subsystems that estimate chord label sequences from audio, MIDI and tab files, using representation-specific ACE and alignment techniques. The resulting chord label sequences form a rich harmonic representation that is a contribution by itself, as it can easily be visualized and enables large-scale cross-version analysis of popular music, giving more insights on subjectivity issues. The potential use of this rich harmonic representation is described in Section 7.1.

8.1.2 Improvement of state-of-the-art audio ACE systems

In Chapter 7, we described our experiments on data fusion. DECIBEL uses data fusion methods to combine the chord label sequences from the aforementioned rich harmonic representation into a single output sequence. The method DF-BEST turned out to be the best-performing method. Using this data fusion method, DECIBEL improves each of the ten original state-of-the-art audio ACE systems. The average WCSR improvement is as
much as 3.05%. Supported by statistical tests, we can confirm the hypothesis that audio ACE can be improved by integrating symbolic music formats.

Although DECIBEL needs a data set of symbolic formats and has a longer calculation time than the original audio ACE systems, it also has two major advantages beyond the WCSR improvement. As a first advantage, by using MIDI and tab files that are scraped from the Internet, DECIBEL implicitly incorporates musical knowledge: MIDI and tab files can be considered as human-made transcriptions of musical notes and chords. As a second advantage, DECIBEL requires a minimum amount additional training and therefore prohibits overfitting to subjective data sets. There is little training needed for the HMM used by Jump Alignment, but apart from that, neither the tab or MIDI subsystem needs to be trained.

8.1.3 Extended Isophonics data set

As a third contribution, we extended the widely used Isophonics Reference Annotations with 770 MIDI files and 1668 tabs. These symbolic music files are scraped from the Internet and manually matched to the corresponding song in the Isophonics data set. In this research project, we learned that MIDI files and tabs are highly useful for the ACE task. We expect that the extended data set can also contribute to advances in other MIR tasks, such as structural segmentation or lyrics-to-audio alignment.

8.1.4 Python implementations

As a fourth and final contribution, we made our Python implementation of DECIBEL available to the MIR community. The complete code repository can be found on https://github.com/DaphneO/DECIBEL. As part of the complete DECIBEL system, this repository contains new Python implementations for existing algorithms, such as Jump Alignment (McVicar et al., 2011b) and data fusion (Koops et al., 2016), as well as implementations for new algorithms, such as our MIDI chord recognizer CASSETTE and a tab parser.

8.2 Future work

From the results of this research project, we can conclude that the integration of multiple symbolic formats and audio for the improvement of ACE is an interesting research direction that deserves more attention in the future. In this section, we give some directions for future work.

As a first suggestion for future work, it would be interesting to test DECIBEL’s performance on a larger data set, for example the Billboard data set. The Isophonics data set was convenient to use, because there were myriad MIDI files and tabs available for music by The Beatles and Queen. DECIBEL’s performance may drop when testing on less popular or more modern artists, because there may be less symbolic formats available for their songs. It would also be interesting to test DECIBEL on music of another genre, for example jazz music. Very recently, a new data set for jazz, consisting of 113 tracks, was released by Eremenko et al. (2018). In the accompanying paper, Eremenko et al. (2018) evaluate two audio ACE methods on their new data set and observe that the CSR’s for these methods were quite low. Extending the data set with MIDI and tab files for these jazz songs and running the DECIBEL system on the extended data set may give better results.

As a second suggestion, we recommend using a larger chord vocabulary in future work. It would be interesting to see if the integration of symbolic formats also helps in recognizing more complex chords, such as seventh chords. Using MIDI and tab files might be very helpful in recognizing complex chords, as these representations directly encode notes and chord labels respectively.

Our third suggestion for future work is to experiment various techniques for DECIBEL’s subtasks. In the current implementation, we decided to use state-of-the-art audio ACE methods in combination with relatively simple methods for alignment and MIDI chord estimation. The rationale behind this is as follows: the audio ACE methods should be as “good” as possible, as it may be trivial to improve a poorly performing audio ACE method. On the other hand, the techniques for tab alignment, MIDI alignment and MIDI chord recognition should be simple: if we can show that simple methods already improve the audio ACE method, we can assume that more
sophisticated techniques will give even better results. Besides, simpler methods are easier to understand and implement, and typically do not require a lot of training. However, as we now know that applying simple techniques on MIDI and tab files already improves audio ACE, it would be interesting to see how much we can improve our results by using more sophisticated techniques. For example, a MIDI chord recognizer that takes the musical context into account will probably give better results than our proposed CASSETTE algorithm.

As a fourth and final suggestion for future work, we propose to test DECIBEL’s performance by doing user tests. We saw that DECIBEL improves each of the ten tested state-of-the-art audio ACE systems. Based on these results, we expect that performers prefer DECIBEL’s estimated chord label sequences to the sequences found by audio ACE systems. However, recall from Section 3.3 that WCSR is not always a good measure for the quality of a chord sequence. Therefore, it would be good to verify the improvement by doing user tests.
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## Appendix A

### Data set

| Index | Song title                        | Album                      |
|-------|-----------------------------------|----------------------------|
| 1     | I Saw Her Standing There          | *The Beatles - Please Please Me* |
| 2     | Misery                            |                            |
| 3     | Anna (Go To Him)                  |                            |
| 4     | Chains                            |                            |
| 5     | Boys                              |                            |
| 6     | Ask Me Why                        |                            |
| 7     | Please Please Me                  |                            |
| 8     | Love Me Do                        |                            |
| 9     | P. S. I Love You                  |                            |
| 10    | Baby It’s You                     |                            |
| 11    | Do You Want To Know A Secret      |                            |
| 12    | A Taste Of Honey                  |                            |
| 13    | There’s A Place                   |                            |
| 14    | Twist And Shout                   |                            |

| Index | Song title                        | Album                      |
|-------|-----------------------------------|----------------------------|
| 15    | It Won’t Be Long                  | *The Beatles - With the Beatles* |
| 16    | All I’ve Got To Do                |                            |
| 17    | All My Loving                     |                            |
| 18    | Don’t Bother Me                   |                            |
| 19    | Little Child                      |                            |
| 20    | Till There Was You                |                            |
| 21    | Please Mister Postman            |                            |
| 22    | Roll Over Beethoven               |                            |
| 23    | Hold Me Tight                     |                            |
| 24    | You Really Got A Hold On Me       |                            |
| 25    | I Wanna Be Your Man               |                            |
| 26    | Devil In Her Heart                |                            |
| 27    | Not A Second Time                 |                            |
| 28    | Money                             |                            |

| Index | Song title                        | Album                      |
|-------|-----------------------------------|----------------------------|
| 29    | A Hard Day’s Night                | *The Beatles - A Hard Day's Night* |
| 30    | I Should Have Known Better        |                            |
| 31    | If I Fell                         |                            |
| 32    | I'm Happy Just To Dance With You  |                            |
| 33    | And I Love Her                    |                            |
| 34    | Tell Me Why                       |                            |
| 35    | Can’t Buy Me Love                 |                            |
| 36    | Any Time At All                   |                            |
| 37    | I’ll Cry Instead                  |                            |
| Index | Song title                             |
|-------|----------------------------------------|
| 38    | Things We Said Today                  |
| 39    | When I Get Home                       |
| 40    | You Can’t Do That                     |
| 41    | I’ll Be Back                           |

*The Beatles - Beatles for Sale*

| Index | Song title                             |
|-------|----------------------------------------|
| 42    | No Reply                               |
| 43    | I’m a Loser                            |
| 44    | Baby’s In Black                       |
| 45    | Rock and Roll Music                   |
| 46    | I’ll Follow the Sun                   |
| 47    | Mr. Moonlight                          |
| 48    | Kansas City- Hey, Hey, Hey, Hey       |
| 49    | Eight Days a Week                     |
| 50    | Words of Love                          |
| 51    | Honey Don’t                           |
| 52    | Every Little Thing                    |
| 53    | I Don’t Want to Spoil the Party       |
| 54    | What You’re Doing                     |
| 55    | Everybody’s Trying to Be My Baby      |

*The Beatles - Help!*

| Index | Song title                             |
|-------|----------------------------------------|
| 56    | Help!                                  |
| 57    | The Night Before                      |
| 58    | You’ve Got To Hide Your Love Away     |
| 59    | I Need You                             |
| 60    | Another Girl                           |
| 61    | You’re Going To Lose That Girl         |
| 62    | Ticket To Ride                         |
| 63    | Act Naturally                          |
| 64    | It’s Only Love                         |
| 65    | You Like Me Too Much                  |
| 66    | Tell Me What You See                  |
| 67    | I’ve Just Seen a Face                  |
| 68    | Yesterday                              |
| 69    | Dizzy Miss Lizzy                       |

*The Beatles - Rubber Soul*

| Index | Song title                             |
|-------|----------------------------------------|
| 70    | Drive My Car                           |
| 71    | Norwegian Wood (This Bird Has Flown)  |
| 72    | You Won’t See Me                      |
| 73    | Nowhere Man                            |
| 74    | Think For Yourself                    |
| 75    | The Word                               |
| 76    | Michelle                              |
| 77    | What Goes On                           |
| 78    | Girl                                   |
| 79    | I’m Looking Through You                |
| 80    | In My Life                             |
| 81    | Wait                                   |
| 82    | If I Needed Someone                    |
| 83    | Run For Your Life                      |

*The Beatles - Revolver*

| Index | Song title                             |
|-------|----------------------------------------|
| 84    | Taxman                                 |
| 85    | Eleanor Rigby                          |
| 86    | I’m Only Sleeping                      |
| 87    | Love You To                            |
| 88    | Here, There And Everywhere             |
| Index | Song title                                      |
|-------|-----------------------------------------------|
| 89    | Yellow Submarine                               |
| 90    | She Said She Said                              |
| 91    | Good Day Sunshine                              |
| 92    | And Your Bird Can Sing                         |
| 93    | For No One                                     |
| 94    | Doctor Robert                                  |
| 95    | I Want To Tell You                             |
| 96    | Got To Get You Into My Life                    |
| 97    | Tomorrow Never Knows                            |

*The Beatles - Sgt. Pepper’s Lonely Hearts Club Band*

| Index | Song title                                      |
|-------|-----------------------------------------------|
| 98    | Sgt. Pepper’s Lonely Hearts Club Band         |
| 99    | With A Little Help From My Friends            |
| 100   | Lucy In The Sky With Diamonds                 |
| 101   | Getting Better                                 |
| 102   | Fixing A Hole                                  |
| 103   | She’s Leaving Home                             |
| 104   | Being For The Benefit Of Mr. Kite!            |
| 105   | Within You Without You                        |
| 106   | When I’m Sixty-Four                           |
| 107   | Lovely Rita                                    |
| 108   | Good Morning Good Morning                      |
| 109   | Sgt. Pepper’s Lonely Hearts Club Band (Reprise)|
| 110   | A Day In The Life                              |

*The Beatles - Magical Mystery Tour*

| Index | Song title                                      |
|-------|-----------------------------------------------|
| 111   | Magical Mystery Tour                           |
| 112   | The Fool On The Hill                           |
| 113   | Flying                                         |
| 114   | Blue Jay Way                                   |
| 115   | Your Mother Should Know                         |
| 116   | I Am The Walrus                                |
| 117   | Hello Goodbye                                  |
| 118   | Strawberry Fields Forever                      |
| 119   | Penny Lane                                     |
| 120   | Baby You’re A Rich Man                         |
| 121   | All You Need Is Love                           |

*The Beatles - The Beatles*

| Index | Song title                                      |
|-------|-----------------------------------------------|
| 122   | Back in the USSR                               |
| 123   | Dear Prudence                                  |
| 124   | Glass Onion                                    |
| 125   | Ob-La-Di, Ob-La-Da                             |
| 126   | Wild Honey Pie                                 |
| 127   | The Continuing Story of Bungalow Bill          |
| 128   | While My Guitar Gently Weeps                   |
| 129   | Happiness is a Warm Gun                        |
| 130   | Martha My Dear                                 |
| 131   | I’m So Tired                                   |
| 132   | Black Bird                                     |
| 133   | Piggies                                        |
| 134   | Rocky Raccoon                                  |
| 135   | Don’t Pass Me By                               |
| 136   | Why Don’t We Do It In The Road                 |
| 137   | I Will                                         |
| 138   | Julia                                          |
| 139   | Birthday                                       |
| 140   | Yer Blues                                      |
| 141   | Mother Nature’s Son                            |
| 142   | Everybody’s Got Something To Hide Except Me and My Monkey |
| Index | Song title                           |
|-------|--------------------------------------|
| 143   | Sexy Sadie                           |
| 144   | Helter Skelter                       |
| 145   | Long Long Long                       |
| 146   | Revolution                           |
| 147   | Honey Pie                            |
| 148   | Savoy Truffle                        |
| 149   | Cry Baby Cry                         |
| 150   | Revolution                           |
| 151   | Good Night                           |

*The Beatles - Abbey Road*

| Index | Song title                                             |
|-------|--------------------------------------------------------|
| 152   | Come Together                                         |
| 153   | Something                                              |
| 154   | Maxwell’s Silver Hammer                                |
| 155   | Oh! Darling                                            |
| 156   | Octopus’s Garden                                       |
| 157   | I Want You                                            |
| 158   | Here Comes The Sun                                    |
| 159   | Because                                               |
| 160   | You Never Give Me Your Money                           |
| 161   | Sun King                                               |
| 162   | Mean Mr Mustard                                        |
| 163   | Polythene Pam                                          |
| 164   | She Came In Through The Bathroom Window                |
| 165   | Golden Slumbers                                        |
| 166   | Carry That Weight                                     |
| 167   | The End                                                |
| 168   | Her Majesty                                            |

*The Beatles - Let It Be*

| Index | Song title                                             |
|-------|--------------------------------------------------------|
| 169   | Two of Us                                              |
| 170   | Dig a Pony                                             |
| 171   | Across the Universe                                    |
| 172   | I Me Mine                                              |
| 173   | Dig It                                                 |
| 174   | Let It Be                                              |
| 175   | Maggie Mae                                             |
| 176   | I’ve Got A Feeling                                     |
| 177   | One After                                              |
| 178   | The Long and Winding Road                              |
| 179   | For You Blue                                           |
| 180   | Get Back                                               |

*Queen - Greatest Hits I*

| Index | Song title                                             |
|-------|--------------------------------------------------------|
| 181   | Bohemian Rhapsody                                     |
| 182   | Another One Bites The Dust                             |
| 184   | Fat Bottomed Girls                                    |
| 185   | Bicycle Race                                           |
| 186   | You’re My Best Friend                                  |
| 187   | Don’t Stop Me Now                                      |
| 188   | Save Me                                                |
| 189   | Crazy Little Thing Called Love                         |
| 190   | Somebody To Love                                       |
| 192   | Good Old Fashioned Lover Boy                           |
| 193   | Play The Game                                          |
| 195   | Seven Seas Of Rhye                                     |
| 196   | We Will Rock You                                      |
| 197   | We Are The Champions                                   |

*Queen - Greatest Hits II*
| Index | Song title                     |
|-------|-------------------------------|
| 198   | A Kind Of Magic               |
| 201   | I Want It All                 |
| 202   | I Want To Break Free          |
| 206   | Who Wants To Live Forever     |
| 211   | Hammer To Fall                |
| 212   | Friends Will Be Friends       |
# Appendix B

## Alignment listening test results

| MIDI file | Alignment error | Listening test result | Error description |
|-----------|-----------------|------------------------|------------------|
| 128-005   | 0.723           | 2 - Good alignment, no fade out in MIDI |                  |
| 014-003   | 0.762           | 2 - Good alignment, MIDI cut off too soon at the end |                  |
| 095-002   | 0.636           | 2 - Good alignment, but seems to be a bit shifted |                  |
| 047-001   | 0.934           | 1 - Very bad alignment |                  |
| 063-004   | 0.764           | 3 - Good alignment |                  |
| 098-004   | 0.850           | 3 - Good alignment |                  |
| 196-001   | 0.656           | 3 - Good alignment |                  |
| 099-002   | 0.959           | 1 - Very bad alignment |                  |
| 195-001   | 0.723           | 2 - Good alignment with minor issues at the end |                  |
| 036-002   | 0.903           | 1 - First verse and chorus missing in MIDI, issues at the end |                  |
| 184-001   | 0.720           | 3 - Good alignment |                  |
| 078-003   | 0.654           | 2 - Good alignment, no fade out in MIDI |                  |
| 042-001   | 0.815           | 2 - Good alignment, but sometimes seems to be a bit shifted |                  |
| 152-002   | 0.705           | 2 - Good alignment, no fade out in MIDI |                  |
| 181-005   | 0.964           | 1 - Very bad alignment (transcription with only piano) |                  |
| 002-001   | 0.644           | 2 - Good alignment, no fade out in MIDI |                  |
| 061-002   | 0.762           | 2 - Good alignment, minor issues at the end |                  |
| 155-001   | 0.880           | 1 - Mediocre alignment, last 50s of the audio missing in MIDI file |                  |
| 073-004   | 0.760           | 2 - Good alignment, but seems to be a bit shifted |                  |
| 055-002   | 0.712           | 3 - Good alignment |                  |
| 003-001   | 0.771           | 2 - Good alignment, but seems to be a bit shifted |                  |
| 010-001   | 0.709           | 2 - Good alignment, no fade out in MIDI |                  |
| 125-002   | 0.784           | 3 - Good alignment |                  |
| 202-005   | 0.641           | 3 - Good alignment |                  |
| 212-001   | 0.532           | 3 - Good alignment |                  |

Table B.1: Results of the alignment listening test
Appendix C

Tabs in parsing evaluation set

The annotated subset for the tab parsing evaluation consists of these 25 songs:

1. Let It Be (ver 6) Tabs
2. A Hard Days Night (ver 10) Chords
3. You’re My Best Friend solo Tabs
4. Savoy Truffle (ver 2) Chords
5. Strawberry Fields Forever Acoustic Chords
6. A Taste Of Honey (ver 2) Chords
7. What You’re Doing Chords
8. A Hard Days Night (ver 3) Tabs
9. Let It Be (ver 4) Chords
10. Love You To Tabs
11. Cry Baby Cry (ver 4) Chords
12. For You Blue Chords
13. Getting Better (ver 5) Chords
14. Help (ver 8) Chords
15. No Reply (ver 4) Chords
16. Happiness Is A Warm Gun Tabs
17. I’ll Be Back (ver 2) Tabs
18. Tell Me Why Tabs
19. Get Back (ver 5) Tabs
20. Anna (ver 2) Chords
21. A Day In The Life Tabs
22. You Never Give Me Your Money Tabs
23. Eleanor Rigby (ver 3) Tabs
24. I’ll Be Back (ver 7) Chords
25. Yesterday Chords
Appendix D

Tabs in forward and backward training set

The following 22 songs were used for training forward and backward probabilities:

1. Misery Chords
2. Please Mister Postman Chords
3. You Really Got A Hold On Me (ver 2) Chords
4. And I Love Her Tabs
5. I’ll Cry Instead Tabs
6. I’ll Be Back Tabs
7. Mr Moonlight Tabs
8. Help (ver 6) Chords
9. I Need You Tabs
10. You’re Going To Lose That Girl Chords
11. Act Naturally (ver 3) Tabs
12. Norwegian Wood (ver 4) Chords
13. Think For Yourself Chords
14. Girl Acoustic Chords
15. Good Day Sunshine Chords
16. Sgt Peppers Lonely Hearts Club Band Reprise (ver 2) Chords
17. Penny Lane (ver 6) Chords
18. Come Together Chords
19. Mean Mr Mustard (ver 2) Chords
20. Golden Slumbers Chords
21. A Kind Of Magic Chords
22. I Want To Break Free Chords