Imputation of spatially-resolved transcriptomes by graph-regularized tensor completion

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Abstract

High-throughput spatial-transcriptomics RNA sequencing (sptRNA-seq) based on in-situ capturing technologies has recently been developed to spatially resolve transcriptome-wide mRNA expressions mapped to the captured locations in a tissue sample. Due to the low RNA capture efficiency by in-situ capturing and the complication of tissue section preparation, sptRNA-seq data often only provides an incomplete profiling of the gene expressions over the spatial regions of the tissue. In this paper, we introduce a graph-regularized tensor completion model for imputing the missing mRNA expressions in sptRNA-seq data, namely FIST, Fast Imputation of Spatially-resolved transcriptomes by graph-regularized Tensor completion. We first model sptRNA-seq data as a 3-way sparse tensor in genes (p-mode) and the (x, y) spatial coordinates (x-mode and y-mode) of the observed gene expressions, and then consider the imputation of the unobserved entries or fibers as a tensor completion problem in Canonical Polyadic Decomposition (CPD) form. To improve the imputation of highly sparse sptRNA-seq data, we also introduce a protein-protein interaction network to add prior knowledge of gene functions, and a spatial graph to capture the spatial relations among the capture spots. The tensor completion model is then regularized by a Cartesian product graph of protein-protein interaction network and the spatial graph to capture the high-order relations in the tensor. In the experiments, FIST was tested on ten 10x Genomics Visium spatial transcriptomic datasets of different tissue sections with cross-validation among the known entries in the imputation. FIST significantly outperformed the state-of-the-art methods for single-cell RNAseq data imputation. We also demonstrate that both the spatial graph and PPI network play an important role in improving the imputation. In a case study, we further analyzed the gene clusters obtained from the imputed gene expressions to show that the imputations by FIST indeed capture the spatial characteristics in the gene expressions and reveal functions that are highly relevant to three different kinds of tissues in mouse kidney.
Author summary

Biological tissues are composed of different types of structurally organized cell units playing distinct functional roles. The exciting new spatial gene expression profiling methods have enabled the analysis of spatially resolved transcriptomes to understand the spatial and functional characteristics of these cells in the context of eco-environment of tissue. Due to the technical limitations, spatial transcriptomics data suffers from only sparsely measured mRNAs by in-situ capture and possibly missing spots in tissue regions that entirely failed fixing and permeabilizing RNAs. Our method, FIST (Fast Imputation of Spatially-resolved transcriptomes by graph-regularized Tensor completion), focuses on the spatial and high-sparsity nature of spatial transcriptomics data by modeling the data as a 3-way gene-by-(x, y)-location tensor and a product graph of a spatial graph and a protein-protein interaction network. Our comprehensive evaluation of FIST on ten 10x Genomics Visium spatial genomics datasets and comparison with the methods for single-cell RNA sequencing data imputation demonstrate that FIST is a better method more suitable for spatial gene expression imputation. Overall, we found FIST a useful new method for analyzing spatially resolved gene expressions based on novel modeling of spatial and functional information.

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Introduction

Dissection of complex genomic architectures of heterogeneous cells and how they are organized spatially in tissue are essential for understanding the molecular and cellular mechanisms underlying important phenotypes. For example, each tumor is a mixture of different types of proliferating cancerous cells with changing genetic materials [1]. The cancer cell sub-populations co-evolve in the micro-environment formed around their spatial locations. It is important to understand the cell-cell interactions and signaling as well as the functioning of each individual cell to develop effective cancer treatment and eradicate all cancer clones at their locations [2]. Conventional gene expression analyses have been limited to low-resolution bulk profiling that measures the average transcription levels in a population of cells. With single-cell RNA sequencing (scRNA-seq) [3–5], single cells are isolated with a capture method such as fluorescence-activated cell sorting (FACS), Fluidigm C1 or microdroplet microfluidics and then the RNAs are captured, reverse transcribed and amplified for sequencing the RNAs barcoded for the individual origin cells [6, 7]. While scRNA-seq is useful for detecting the cell heterogeneity in a tissue sample, it does not provide the spatial information of the isolated cells. To map cell localization, earlier in-situ hybridization methods such as FISH [8], FISSEQ [9], smFISH [10] and MERFISH [11] were developed to profile up to a thousand targeted genes in pre-constructed references with single-molecule RNA imaging. Based on in-situ capturing technologies, more recent spatial transcriptomics RNA sequencing (sptRNA-seq) [12–15] combines positional barcoded arrays and RNA sequencing with single-cell imaging to spatially resolve RNA expressions in each measured spot in the spatial array [12, 16–18]. These new technologies have transformed the transcriptome analysis into a new paradigm for connecting single-cell molecular profiling to tissue micro-environment and the dynamics of a tissue region [19–21].

With in-situ capturing technology, RNAs are captured and sequenced in the spots on the spatial genomic array aligned to the locations on the tissue. For example, spatial transcriptomics
technology based on 10x Genomics Visium kit reports the number of copies of RNAs by counting unique molecular identifiers (UMIs) in the read-pairs mapped to each gene [22]. There are still significant technical difficulties. First, in-situ capturing has a low RNA capture efficiency. The earlier spatial transcriptomics technology’s detection efficiency is as low as 6.9% and 10x Genomics Visium has only a slightly improved efficiency [23]. In addition, the sample preparation requires highly specific handling of tissue sections. The spots in some tissue regions might entirely fail to fix and permeabilize RNAs due to various possible issues in preparing tissue sections. A few examples of such regions are shown in S1 Fig. Thus, sptRNA-seq data often only provides an incomplete profiling of the gene expressions over the spatial regions of the tissue. Similarly, in scRNA-seq data analysis, the missing gene expressions are called dropout events, which refer to the false quantification of a gene as unexpressed due to the failure in amplifying the transcripts during reverse-transcription [24]. It has been shown in previous studies on scRNA-seq data that normalizations will not address the dropout effects [22, 25]. In the literature, many imputation methods such as Zero-inflated factor analysis (ZIFA) [26], Zero-Inflated Negative Binomial-based Wanted Variation Extraction (ZINB-WaVE) [27] and BISCUIT [25] have been developed to impute scRNA-seq. While these methods are also applicable to impute the spatial gene expressions, they ignore a unique characteristic of sptRNA-seq data, which is the spatial information among the gene expressions in the spatial array, and do not fully take advantage of the functional relations among genes for more reliable joint imputation.

To provide a more suitable method for imputation of spatially-resolved gene expressions, we introduce FIST, Fast Imputation of Spatially-resolved transcriptomes by graph-regularized Tensor completion. FIST is a tensor completion model regularized by a product graph as illustrated in Fig 1. FIST models sptRNA-seq data as a 3-way sparse tensor in genes (p-mode) and the (x, y) spatial coordinates (x-mode and y-mode) of the observed gene expressions (Fig 1A). As shown in Fig 1B, a protein-protein interaction network models the interactions between pairs of genes in the gene mode, and the spatial graph is modeled by a product graph of two chain graphs for columns (x-mode) and rows (y-mode) in the grid to capture the spatial

![Fig 1. Imputation of spatial transcriptomes by graph-regularized tensor completion.](https://doi.org/10.1371/journal.pcbi.1008218.g001)
relations among the \((x, y)\) spots. The Cartesian product of these graphs with prior knowledge of gene functions and the spatial relations among the capture spots are then introduced as a regularization of tensor completion to obtain the Canonical Polyadic Decomposition (CPD) of the tensor. The imputation of the unobserved entries can then be derived by reconstructing the entries in the completed tensor shown in Fig 1C. In the experiments, we comprehensively evaluated FIST on ten 10x Genomics Visium spatial genomics datasets by comparison with widely used methods for single-cell RNA sequencing data imputation. We also analyzed a mouse kidney dataset with more functional interpretation of the gene clusters obtained by the imputed gene expressions to detect highly relevant functions in the clusters expressed in three kidney tissue regions, cortex, outer stripe of the outer medulla (OSOM) and inner stripe of the outer medulla (ISOM).

### Materials and methods

In this section, we first describe the task of spatial gene expression imputation, and next introduce the mathematical model for graph-regularized tensor completion problem. We then present a fast iterative algorithm FIST to solve the optimization problem defined to optimize the model. We also provide the convergence analysis of proposed algorithm in S1 File. Finally, we provide a review of several state-of-the-art methods for scRNA-seq data imputation, which are also compared in the experiments later. The notations which will be used for the derivations in the forthcoming sections are summarized in Table 1.

### Imputation of spatial gene expressions by tensor modeling

Let \(T \in \mathbb{R}^{n_x \times n_y \times n_z} \) be the 3-way sparse tensor of the observed spatial gene expression data as shown in Fig 1A, with the missing gene expressions represented as zeros, where \(n_p\) denote the total number of genes, \(n_x\) and \(n_y\) denote the dimensions of the \(x\) and \(y\) spatial coordinates of the spatial transcriptomics array. Our goal is to learn a complete spatial gene expression tensor \(\hat{T} \in \mathbb{R}^{n_x \times n_y \times n_z}\) from \(T\) as illustrated in Fig 1C. However, it is computationally expensive and often infeasible to compute or store a dense tensor \(\hat{T}\), especially in high spatial resolutions with millions of spots. Therefore, we propose to compute an economy-size representation of

| Notation | Definition |
|----------|------------|
| \(G_x, G_y\) | Spatial chain graphs of \((x, y)\) coordinates |
| \(G_p\) | Protein-protein interaction (PPI) network |
| \(n_x, n_y, n_p\) | Number of vertices in \(G_x, G_y\) and \(G_p\) |
| \(W_x \in \mathbb{R}^{n_x \times n_x}, W_y \in \mathbb{R}^{n_y \times n_y}\) | Adjacency matrix of \(G_x, G_y\) |
| \(L_x \in \mathbb{R}^{n_y \times n_y}, L_y \in \mathbb{R}^{n_x \times n_x}\) | Graph Laplacian of \(G_x, G_y\) |
| \(\Theta(x, y, p)\) | Cartesian product of \(G_x, G_y\) and \(G_p\) |
| \(\mathcal{M}(x, y, p) \in \mathbb{R}^{n_x \times n_y \times n_z}\) | Adjacency matrix of \(\Theta(x, y, p)\) |
| \(\mathcal{L}(x, y, p) \in \mathbb{R}^{n_x \times n_y \times n_z}\) | Graph Laplacian of \(\Theta(x, y, p)\) |
| \(T \in \mathbb{R}^{n_x \times n_y \times n_z}\) | Incomplete spatial gene expression tensor |
| \(\hat{T} \in \mathbb{R}^{n_x \times n_y \times n_z}\) | Complete spatial gene expression tensor |
| \(M \in \mathbb{R}^{n_x \times n_y \times n_z}\) | Binary mask tensor |
| \(\hat{A}_x, \hat{A}_y, \hat{A}_p \in \mathbb{R}^{n_x \times n_x}, \hat{A}_x, \hat{A}_y, \hat{A}_p \in \mathbb{R}^{n_y \times n_y}\) | CPD component matrices of \(\hat{T}\) |
| \(\text{vec}(T) \in \mathbb{R}^{n_x \times n_y \times n_z}\) | Rearrange \(T\) to be a vector |

[https://doi.org/10.1371/journal.pcbi.1008218.t001](https://doi.org/10.1371/journal.pcbi.1008218.t001)
\( \hat{T} \) via an equality constraint \( \hat{T} = \{\hat{A}_p, \hat{A}_y, \hat{A}_s\} \), which is called Canonical Polyadic Decomposition (CPD) [28] of \( \hat{T} \) defined below

\[
\hat{T} = \{\hat{A}_p, \hat{A}_y, \hat{A}_s\} = \sum_{p=1}^{r}[\hat{A}_{i,j}] \circ [\hat{A}_{j,i}] \circ [\hat{A}_{s,i}],
\]

where \( r \) is the rank of \( \hat{T} \), and \( \circ \) denotes the vector outer product. Here, \([\hat{A}_{i,j}]\) is the \( i \)-th column of the low-rank matrix \( \hat{A}_x \in \mathbb{R}^{n_x \times n_y \times n_z} \), which can be similarly defined for \([\hat{A}_{j,i}]\) and \([\hat{A}_{s,i}]\). By utilizing the tensor CPD form, we replaced the optimization variables from \( \hat{T} \) to \( \hat{A}_p, \hat{A}_y \) and \( \hat{A}_s \), reducing the number of parameters from \( n_p n_y n_z \) to \( r(n_p + n_y + n_z) \). The advantage of the tensor representation is to incorporate the 2-D spatial \( x \)-mode and \( y \)-mode such that the grid structure is preserved within the columns and the rows of the spatial array in the tensor, which contains useful spatial information. Next, we introduce the tensor completion model over \( \hat{A}_p, \hat{A}_y \) and \( \hat{A}_s \).

### Graph regularized tensor completion model

The key ideas of modeling the task of spatial gene expression imputation are i) the inferred complete spatial gene expression tensor \( \hat{T} \) is regularized to integrate the spatial arrangements of the spots in the tissue array and the functional relations among the genes; ii) the observed part in \( T \) is also required to be preserved in \( \hat{T} \) as the completion task requires; and iii) the inferred tensor \( \hat{T} \) is compressed as the economy-size representation \( \hat{T} = \{\hat{A}_p, \hat{A}_y, \hat{A}_s\} \) for scalable space and time efficiencies. The novel optimization formulation is shown below in Proposition 1,

\[\text{Proposition 1. The complete spatial gene expression tensor } \hat{T} \in \mathbb{R}^{n_x \times n_y \times n_z} \text{ can be obtained by solving the following optimization problem:} \]

\[
\begin{align*}
\text{minimize} & \quad \frac{1}{2} ||M \odot (T - \hat{T})||_F^2 + \frac{\lambda}{2} \text{vec}(\hat{T})^T \mathcal{L}(x, y, p) \text{vec}(\hat{T}) \\
\text{subject to} & \quad \hat{T} = \{\hat{A}_p, \hat{A}_y, \hat{A}_s\} \\
& \quad \hat{A}_p \geq 0, \hat{A}_y \geq 0, \hat{A}_s \geq 0,
\end{align*}
\]

where \( \lambda \in [0, 1] \) is a model hyperparameter; \( \odot \) denotes the Hadamard product; and \( ||.||_F \) denotes the Frobenius norm of a tensor.

There are two optimization terms in the model defined in Eq (2), consistency with the observations (the first term) and Cartesian product graph regularization (the second term), which are explained below.

- **Consistency with the observations**
  We introduce a binary mask tensor \( M \) to indicate the indices of the observed entries in \( T \). The \((i, j, k)\)-th entry \( M_{ijk} \) which is defined below, represents whether the \((i, j, k)\)-th element in \( T \) is observed or not.

\[
M_{ijk} = \begin{cases} 
1 & \text{if } T_{ijk} \text{ is observed}, \\
0 & \text{otherwise}.
\end{cases}
\]

By introducing the squared-error in \( F \)-norm \( ||M \odot (T - \hat{T})||_F^2 \) in the model, we ensure
the inferred spatial gene expression tensor $\tilde{T}$ is consistent with its observed counterparts in $T$.

- **Cartesian product graph regularization**

Two useful assumptions to introduce prior knowledge for inferring the tensor are 1) the spatially adjacent spots should share similar gene expressions, and 2) the expressions of two genes are likely highly correlated if they share similar gene functions [29, 30]. We introduce a spatial graph and a protein-protein interaction (PPI) network into the model.

We first encode the spatial information in two undirected unweighted chain graphs $G_x = (V_x, E_x)$ and $G_y = (V_y, E_y)$, where $V_x$ and $V_y$ are vertex sets and $E_x$ and $E_y$ are edge sets. There are $|V_x| = n_x$ vertices in $G_x$ where $n_x$ is the number of the spatial coordinates along the $x$-axis of the spatial array. Two vertices in $G_x$ are connected by an edge if they are adjacent along the $x$-axis. The connections in $G_y$ can be similarly defined to encode the $y$-coordinates of the tissue.

We also incorporate the topological information of a PPI network download from BioGRID 3.5 [31] to use the functional modules in the PPI network. We denote the PPI network as $G_p = (V_p, E_p)$ which contains $|E_p|$ experimentally documented physical interactions among the $|V_p| = n_p$ proteins. We then use the Cartesian product graph [32] $\mathcal{G}(x, y, p) = (V, E)$ of the three individual graphs $G_x$, $G_y$, and $G_p$ to regularize the elements in $\tilde{T}$, where $|V| = n_x n_y n_p$. The $(v_x, v_y, v_p)$-th vertex in $V$ represents a triple of vertices $v_x \in V_x$, $v_y \in V_y$, $v_p \in V_p$ from each of the three graphs. The $(a_x, a_y, a_p)$-th and $(b_x, b_y, b_p)$-th vertices in $V$ are connected by an edge iff for any $i, j \in \{x, y, p\}$, $(a_i, b_i) \in E_i$ and $a_i = b_i \in V_i$ for all $i \neq j$. For a graph $G_i = (V_i, E_i)$ where $i \in \{x, y, p\}$, we denote its adjacency matrix as $W_i$, degree matrix as $D_i$, and graph Laplacian matrix as $L_i = D_i - W_i$. The adjacency and graph Laplacian matrices of $\mathcal{G}(x, y, p)$ are obtained as $\mathcal{L}(x, y, p) = W_x \oplus W_y \oplus W_p$ and $\mathcal{L}(x, y, p) = L_x \oplus L_y \oplus L_p$ respectively, where $\oplus$ denotes the Kronecker sum [33].

By introducing the term $\mathbf{vec}(\tilde{T})^T \mathcal{L}(x, y, p) \mathbf{vec}(\tilde{T})$ in Eq (2), the inferred gene expression values in $\tilde{T}$ are ensured to be smooth over the manifolds of the product graph $\mathcal{G}(x, y, p)$, such that a pair of tensor entries $\tilde{T}_{a_x, a_y, a_p}$ and $\tilde{T}_{b_x, b_y, b_p}$ share similar values if the $(a_x, a_y, a_p)$-th and $(b_x, b_y, b_p)$-th vertices are connected in $\mathcal{G}(x, y, p)$. A connection implies that the $x$-coordinate $a_x$ and $b_x$ is adjacent or $y$-coordinate $a_y$ and $b_y$ is adjacent or gene $a_p$ and gene $b_p$ are connected in the PPI, with the two other dimensions fixed. Using Cartesian product graph is a more conservative strategy to connect multi-relations in a high-order graph as we have shown in [34] since only replacing one of the dimensions by the immediate neighbors is allowed to create connections. Note that it also possible to use tensor product graph or strong product graph [34] but there could be too many connections to provide meaningful connectivity in the product graph for helpful regularization. It is known that genes’ connectivities in PPI network correlate with their co-expressions. We also justified this hypothesis on the spatial transcriptomics data by examining the relation between the connectivity in PPI network and the co-expression in spatial locations among the genes in the 10 different 10x Genomics Visium spatial genomics datasets used in this study. The results of this analysis are shown in S2 Fig.

We observed higher co-expressions between the genes that are connected with less hops in the PPI, which clearly supports our assumptions.

**FIST Algorithm**

The model introduced in Eq (2) is non-convex on variables $\{\hat{A}_x, \hat{A}_y, \hat{A}_p\}$ jointly, thus finding its global minimum is difficult. In this section, we propose an efficient iterative algorithm Fast Imputation of Spatially-resolved Transcriptomes by graph-regularized Tensor completion
(FIST) to find its local optimal solution using the multiplicative updating rule [35], based on derivatives of \( \hat{A}_p, \hat{A}_y \) and \( \hat{A}_x \). Without loss of generality, we only show the derivations with respect to \( \hat{A}_p \), and provide the FIST algorithm in Algorithm 1.

We first bring the equality constraint \( \hat{T} = [\hat{A}_p, \hat{A}_y, \hat{A}_x] \) in Eq (2) into the objective function, and rewrite the objective function as

\[
J = J_1 + \lambda J_2
\]

\[
J_1 = \frac{1}{2} \| \mathcal{M} \otimes (T - [\hat{A}_p, \hat{A}_y, \hat{A}_x]) \|^2
\]

\[
J_2 = \frac{1}{2} \text{vec}(\hat{A}_p \hat{A}_y \hat{A}_x)^T \Omega(\mathbf{x}, \mathbf{y}, \mathbf{p}) \text{vec}(\hat{A}_p \hat{A}_y \hat{A}_x)
\]

(3)

The partial derivative of \( J_1 \) with respect to \( \hat{A}_p \) can be computed as

\[
\frac{\partial J_1}{\partial \hat{A}_p} = (\mathcal{M}_i \otimes \hat{T}_i) - (\mathcal{M}_i \otimes \hat{T}_i)(\hat{A}_p \otimes \hat{A}_y),
\]

where \( \hat{T}_i \in \mathbb{R}^{r \times n \times n} \) denotes the matrix flattened from tensor \( T_i \otimes \) denotes the Khatri–Rao product [28]. Note that the term \( \mathcal{M}_i \otimes \hat{T}_i \) in Eq (4) implies we only need to compute the entries in \( \hat{T}_i \) which correspond to the non-zero entries (indices of the observed gene expression) in \( \mathcal{M} \). The rest of the computation in Eq (4) involves the well-known MTTKRP (matricized tensor times Khatri-Rao product) [36] operation, which is in the form of \( M \) operation, and can be computed in \( O(r|\mathcal{X}|) \) if \( \mathcal{X} \) is a sparse tensor with \( |\mathcal{X}| \) non-zeros, and \( \hat{A}_p \) and \( \hat{A}_y \) have \( r \) columns. Thus, the overall time complexity of computing Eq (4) is \( O(r|\mathcal{X}|) \).

Following the derivations in [34], we obtain the partial derivatives of the second term \( J_2 \) as

\[
\frac{\partial J_2}{\partial \hat{A}_p} = \hat{A}_p (\Phi_i \otimes \Theta_j + \Phi_j \otimes \Theta_i) + L_p \hat{A}_y (\Phi_i \otimes \Theta_j),
\]

(5)

where \( \Phi_i = \tilde{\hat{A}}_i \tilde{\hat{A}}_x \) and \( \Theta_j = \hat{A}_j \hat{A}_y \), for all \( i \in \{x, y \} \). It is not hard to show that the complexity of computing the Eq (5) is \( O(\sum_{i \in \{x, y \}} (r^2n_i + rn_j^2)) \).

Next, we combine \( \frac{\partial J_1}{\partial \hat{A}_p} \) and \( \frac{\partial J_2}{\partial \hat{A}_p} \) to obtain the overall derivative as

\[
\frac{\partial J}{\partial \hat{A}_p} = \frac{\partial J_1}{\partial \hat{A}_p} + \lambda \left( \frac{\partial J_2}{\partial \hat{A}_p} \right)
\]

\[
= \begin{pmatrix}
\frac{\partial J_1}{\partial \hat{A}_p} \\
\frac{\partial J_2}{\partial \hat{A}_p}
\end{pmatrix} + \lambda \left( \begin{pmatrix}
\frac{\partial J_2}{\partial \hat{A}_p} \\
\frac{\partial J_1}{\partial \hat{A}_p}
\end{pmatrix}^T \right) - \lambda \left( \begin{pmatrix}
\frac{\partial J_2}{\partial \hat{A}_p} \\
\frac{\partial J_1}{\partial \hat{A}_p}
\end{pmatrix}^T \right),
\]

(6)

where \( \begin{pmatrix}
\frac{\partial J_1}{\partial \hat{A}_p} \\
\frac{\partial J_2}{\partial \hat{A}_p}
\end{pmatrix}^T \) and \( \begin{pmatrix}
\frac{\partial J_2}{\partial \hat{A}_p} \\
\frac{\partial J_1}{\partial \hat{A}_p}
\end{pmatrix}^T \) are non-negative components in \( \frac{\partial J}{\partial \hat{A}_p} \), which are defined below as

\[
\begin{pmatrix}
\frac{\partial J_1}{\partial \hat{A}_p} \\
\frac{\partial J_2}{\partial \hat{A}_p}
\end{pmatrix} = (\mathcal{M}_i \otimes \hat{T}_i)(\hat{A}_x \otimes \hat{A}_y),
\]

(7)

\[
\begin{pmatrix}
\frac{\partial J_2}{\partial \hat{A}_p} \\
\frac{\partial J_1}{\partial \hat{A}_p}
\end{pmatrix} = (\mathcal{M}_i \otimes \hat{T}_i)(\hat{A}_y \otimes \hat{A}_x),
\]

(8)
which only requires the space of the tensor graph and tensors, and break down the calculus into the computation on the efficient tensor computation in Eqs (7)–(10), the algorithm can avoid computing the full Car-plexus representation of the complete spatial gene expression tensor.

\[
\left[ \frac{\partial \mathcal{J}_2}{\partial \hat{A}_p} \right]^- = \hat{A}_p (\Phi_x \odot \Theta_p^x + \Phi_y \odot \Theta_p^y) + D_p \hat{A}_p (\Phi_x \odot \Phi_y), \tag{9}
\]

\[
\left[ \frac{\partial \mathcal{J}_2}{\partial \hat{A}_p} \right]^- = \hat{A}_p (\Phi_x \odot \Theta_p^x + \Phi_y \odot \Theta_p^y) + W_p \hat{A}_p (\Phi_x \odot \Phi_y), \tag{10}
\]

where \( \Theta_i^x = \hat{A}_x D_i \hat{A}_x \) and \( \Theta_i^y = \hat{A}_y W_i \hat{A}_y \), for all \( i \in \{x, y, p\} \). According to Eq (6), the objective function \( \mathcal{J} \) objective will monotonically decrease under the following multiplicative updating rule,

\[
[\hat{A}_p]_{a,b} \leftarrow \frac{[\hat{A}_p]_{a,b}}{\gamma_{a,b}} + \lambda \frac{[\gamma_{a,b}]^-}{\gamma_{a,b}}
\]

where \( [\hat{A}_p]_{a,b} \) denotes the \((a, b)\)-th element in matrix \( \hat{A}_p \). Similarly, we can derive the update rule for \( [\hat{A}_x]_{a,b} \) and \( [\hat{A}_y]_{a,b} \) as follows,

\[
[\hat{A}_x]_{a,b} \leftarrow \frac{[\hat{A}_x]_{a,b}}{\gamma_{a,b}} + \lambda \frac{[\gamma_{a,b}]^-}{\gamma_{a,b}}
\]

\[
[\hat{A}_y]_{a,b} \leftarrow \frac{[\hat{A}_y]_{a,b}}{\gamma_{a,b}} + \lambda \frac{[\gamma_{a,b}]^-}{\gamma_{a,b}}
\]

We then propose an efficient iterative algorithm FIST in Algorithm 1 to find the local optimum of the proposed graph regularized tensor completion problem with time complexity \( O(r|M| + \sum_{i \in \{x, y\}} (e_i n_i + \eta_i n_i)) \). FIST takes the incomplete spatial gene expression tensor \( T \), PPI network and spatial chain graphs as input (line 1-2 in Algorithm 1), and outputs the inferred CPD representation of the complete spatial gene expression tensor \( \hat{T} \) (line 9 in Algorithm 1), via solving the optimization problem defined in Proposition 1 with the multiplicative updating rule (line 5-7 in Algorithm 1) based on the tensor calculus in Eqs (7)–(10). With the efficient tensor computation in Eqs (7)–(10), the algorithm can avoid computing the full Cartesian product graph and tensors, and break down the calculus into the computation on the individual graphs and the sparse tensors. Therefore, FIST is proven to be a scalable method, which only requires the space \( O(|T| + |M|) \) to store the sparse tensors, \( O(\sum_{i \in \{x, y\}} |E_i|) \) to store the graphs, and \( O(\sum_{i \in \{x, y, p\}} |E_i| + \eta_i n_i) \) to store the factor matrices. Thus, the overall space complexity is \( O(|T| + |M| + \sum_{i \in \{x, y\}} (|E_i| + \eta_i n_i)) \). The theoretical convergence analysis of FIST is also given in S1 File.

**Algorithm 1** FIST: Fast Imputation of Spatially-resolved Transcriptomes by graph-regularized Tensor completion

1: **Input:** 1) spatial gene expression tensor \( T \in \mathbb{R}^{n_x \times n_y \times n_p} \), 2) binary mask tensor \( M \in \mathbb{R}^{n_x \times n_y \times n_p} \) which indicates the observed part in \( T \), 3) protein-protein interaction (PPI) network \( G_p \) and 4) hyper parameter \( \lambda \).

2: **Construct** the spatial chain graphs \( G_x \) and \( G_y \) as described in the text.
3: Randomly initialize $\tilde{A}_p \in \mathbb{R}_+^{n_p \times r}$, $\tilde{A}_y \in \mathbb{R}_+^{n_y \times r}$ and $\tilde{A}_x \in \mathbb{R}_+^{n_x \times r}$ as non-negative matrices.

4: while not converge do
5: update $\tilde{A}_p$ by Eq (11).
6: update $\tilde{A}_y$ by Eq (12).
7: update $\tilde{A}_x$ by Eq (13).
8: end while
9: Output: the low-rank matrices $\tilde{A}_p$, $\tilde{A}_y$, and $\tilde{A}_x$, which forms the CPD representation of the inferred spatial gene expression tensor $\tilde{T} = [\tilde{A}_p, \tilde{A}_y, \tilde{A}_x] \in \mathbb{R}_+^{n_p \times n_y \times n_x}$.

Related methods for comparison
To benchmark the performance of FIST, we compared it with three matrix factorization (MF)-based methods (with graph regularizations) and a nearest neighbors (NN)-based method, which have been applied to impute various types of biological data including the imputation of dropouts in single-cell RNA sequencing (scRNA-seq) data. Note that NMF-based methods have been shown to be effective for learning latent features and clustering of high-dimension sparse genomic data [37].

- **ZIFA**: Zero-inflated factor analysis (ZIFA) [26] factorizes the single cell expression data $Y \in \mathbb{R}^{N \times D}$ where $N$ and $D$ denote the number of single cells and genes respectively, into a factor loading matrix $A \in \mathbb{R}^{K \times D}$ and a matrix $Z \in \mathbb{R}^{N \times K}$ which spans the latent low-dimensional space where dropouts can happen with a probability specified by an exponential decay associated with the expression levels. The imputed matrix can be computed as $\hat{Y} = ZA + \mu$, where $\mu \in \mathbb{R}^{1 \times D}$ is the latent mean vector.

- **REMAP**: Since ZIFA is a probabilistic MF model which does not utilize the spatial and gene networks, we therefore also compare with REMAP [38], which was developed to impute the missing chemical-protein associations for the identification of the genome-wide off-targets of chemical compounds. REMAP factorizes the incomplete chemical-protein interactions matrix into the chemical and protein low-rank matrices, which are regularized by the compound similarity graph and protein sequence similarity (NCBI BLAST [39]) graph respectively.

- **GWNMF**: Both ZIFA and REMAP are only applicable to the spot-by-gene matrix which is a flatten of a input tensor $T$. Such flattening process assumes the spots are independent from each other, and thus loses the spatial information. To keep the spatial arrangements, we also apply MF to each $n_x \times n_y$ slice in tensor $T$. Specially, we adopt the graph regularized weighted NMF (GWNMF) [40] method to impute each $n_x \times n_y$ gene slice. We let GWNMF use the same x-axis and y-axis graphs $G_x$ and $G_y$ as described in the previous section to regularize the MF.

- **Spatial-NN**: It has been observed that in sparse high-dimensional scRNA-seq data, constructing a nearest neighbor (NN) graph among cells can produce more robust clusters in the presence of dropouts because of taking into account the surrounding neighbor cells [41]. Such rationale has be considered in the clustering methods such as Seurat [42] and shared nearest neighbors (SNN)-Cliq [41], and can also be adopted to impute the spatial gene expression data. We introduce a SNN-based baseline Spatial-NN using neighbor averaging to compare with FIST. Specifically, to impute the missing expression of a target spot, Spatial-
NN first searches its spatially nearest spots with observed gene expressions, then assigns their average gene expression to the target spot.

We used the provided Python package (https://github.com/epierson9/ZIFA) to experiment with ZIFA, and the provided MATLAB package (https://github.com/hansaimlim/REMAP) to experiment with REMAP. To apply both methods, we rearranged the data tensor $T \in \mathbb{R}^{n_x \times n_y \times n_p}$ to a matrix $T \in \mathbb{R}^{N \times n_p}$, where $N = n_x \times n_y$ denotes the total number of spots. The spatial graph of REMAP is constructed by connecting two spots if they are spatially adjacent. REMAP adopts the same PPI network as the gene graph $G_p$ as used by FIST. We used MATLAB to implement GWNMF and Spatial-NN ourselves to impute each gene slice $T_i \in \mathbb{R}^{n_x \times n_y}$ in $T$. In the comparisons, the graph hyperparameter $\lambda$ of FIST is selected from $\{0, 0.01, 0.1, 1\}$. The graph hyperparameters of REMAP and GWNMF are set by searching the grids from $\{0.1, 0.5, 0.9, 1\}$ and $\{0, 0.1, 1, 10, 100\}$ respectively as suggested in the original studies. Note that different methods use different scales of graph hyperparameters since the gradients of their variables with respect to the regularization terms are in different scales. The optimal hyper-parameters are selected by the validation set for each method. For FIST, REMAP and GWNMF, we applied PCA on matrix $T \in \mathbb{R}^{N \times n_p}$ to determine the rank $r \in [200, 300]$ of the low-rank factor matrices, such that at least 60% of the variance is accounted for by the top-$r$ PCA components of $T$. The latent dimension $K$ of ZIFA is set to 10 since it is time consuming to run ZIFA with a larger $K$. We also observed that increasing $K$ from 10 to 50 does not show clear improvement on the imputation accuracy.

Results

In this section, we first describe data preparation and performance measure and then show the results of spatial gene expression imputation. We also analyzed the results by the gene-wise density of the gene expressions and regularization by permuted graphs. Finally, we analyzed the imputed spatial gene expressions in the Mouse Kidney Section dataset to show several interesting gene clusters revealing functional characteristics of the three tissue regions, cortex, OSOM and ISOM.

Preparation of spatial gene expression datasets

We downloaded the spatial transcriptomic datasets from 10x Genomics (https://support.10xgenomics.com/spatial-gene-expression/datasets/), which is a collection of spatial gene expressions in 10 different tissue sections from mouse brain, mouse kidney, human breast cancer, human heart and human lymph node as listed in Table 2. All the sptRNA-seq datasets were

| Dataset | Tissue section | Tensor dimensions | Density |
|---------|----------------|-------------------|---------|
| HBA1    | Human Breast Cancer (Block A Section 1) | $13,426 \times 60 \times 77$ | 0.093 |
| HBA2    | Human Breast Cancer (Block A Section 2) | $13,470 \times 58 \times 75$ | 0.100 |
| HH      | Human Heart    | $7,487 \times 63 \times 70$ | 0.049 |
| HLN     | Human Lymph Node | $12,368 \times 61 \times 78$ | 0.088 |
| MKC     | Mouse Kidney Section (Coronal) | $12,264 \times 41 \times 56$ | 0.103 |
| MBC     | Mouse Brain Section (Coronal) | $13,570 \times 49 \times 74$ | 0.110 |
| MB1P    | Mouse Brain Serial Section 1 (Sagittal-Posterior) | $15,404 \times 62 \times 67$ | 0.115 |
| MB2P    | Mouse Brain Serial Section 2 (Sagittal-Posterior) | $12,497 \times 63 \times 65$ | 0.077 |
| MB1A    | Mouse Brain Serial Section 1 (Sagittal-Anterior) | $12,658 \times 59 \times 66$ | 0.105 |
| MB2A    | Mouse Brain Serial Section 2 (Sagittal-Anterior) | $12,295 \times 63 \times 66$ | 0.082 |

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We applied 5-fold cross-validation to evaluate the performance of imputing spatial gene expressions from each of the 10 datasets into a 3-way tensor (1-10 cells per spot). To fit a tensor model on the spatial gene expression datasets, we organized the expression data in a perfect grid in earlier spatial transcriptomic arrays and the rows and columns in the grid can be used directly as the coordinates \((n_x,n_y)\). In the Visium array slide, the spots are arranged in a hivegrid. To map the spatial coordinates \((n_x,n_y)\), we shifted the odd-numbered rows by a half of a spot for a convenient arrangement of the spots in the tensor without loss of generality. We set the entries in \(T\) to zeros if their UMI counts is lower than 3. We then removed the genes with no UMI counts across the spots, and removed the empty spots in the boundaries of the four sides in the H&E staining from \(T\). The log-transformation is finally applied to every entry of \(T\) as \(T_{ijk} \leftarrow \log(1 + T_{ijk})\). The sizes and densities of the 10 different spatial gene expression tensors after preprocessing are summarized in Table 2. Finally, we downloaded the full Homo sapiens and Mus musculus protein-protein interactions (PPI) networks from BioGRID 3.5 [31] as the gene network \(G_p\) to match with the genes in each dataset.

**Evaluations and performance measures**

We applied 5-fold cross-validation to evaluate the performance of imputing spatial gene expressions by spatial spots or genes as follows:

- **Spot-wise evaluation**: We chose 4-fold of the non-empty spatial spots for training and validation, and held out the rest 1-fold non-empty spatial spots as test data. When evaluating the expressions \(T_{ijk} \in \mathbb{R}^{n_x \times n_y}\) in the \((k,j)\)-th spatial spot, we set the vectors \(T_{ij\cdot}\) and \(M_{ij\cdot}\) in the input tensor \(T\) and mask tensor \(M\) to zeros to indicate that the expressions in this spot are unobserved; next, we use the learned low-rank matrices \(A_p\), \(A_i\), and \(A_j\) to construct the predicted gene expressions \(\hat{T}_{ij\cdot}\) as described in Eq (1).

- **Gene-wise evaluation**: For each gene, we chose 4-fold of its observed expressions (non-zeros in \(T\)) for training and validation, and held out the rest 1-fold observed expressions as test data. When evaluating the 1-fold expressions in the \(i\)-th gene \(T_{i\cdot\cdot} \in \mathbb{R}^{n_x \times n_y}\), we set the corresponding entries in \(T_{i\cdot\cdot}\) and \(M_{i\cdot\cdot}\) in the input tensor \(T\) and mask tensor \(M\) to zeros, to indicate the expressions in this fold are unobserved; next, we use the learned low-rank matrices \(A_p\), \(A_i\), and \(A_j\) to construct the predicted gene expressions \(\hat{T}_{i\cdot\cdot}\) as described in Eq (1).

The hyper-parameter \(\lambda\) is optimized by the validation set for FIST and baseline methods. Denoting vectors \(t \in \mathbb{R}^{n_x \times 1}\) and \(\hat{t} \in \mathbb{R}^{n_x \times 1}\) as the true and predicted expressions in the held-out spatial spot \(T_{ij\cdot}\) or the held-out entries in gene \(T_{i\cdot\cdot}\), the imputation performance is evaluated by the following three metrics,

- **MAE (mean absolute error)** = \(\frac{1}{n} \sum_{i=1}^{n} |t_i - \hat{t}_i|\),

- **MAPE (mean absolute percentage error)** = \(\frac{1}{n} \left( \sum_{i=1}^{n} \frac{|t_i - \hat{t}_i|}{|t_i|} \right)\),

- **R² (coefficient of determination)** = \(1 - \frac{\sum_{i=1}^{n} (t_i - \hat{t}_i)^2}{\sum_{i=1}^{n} (t_i - \bar{t}_i)^2}\)\(^{-1}\).

We expect a method to achieve smaller MAE and MAPE and larger R² for better performance.
FIST significantly improves the accuracy of imputing spatial gene expressions

The performances of FIST and the baseline methods except for ZIFA in the spot-wise evaluation are compared in Fig 2. ZIFA was excluded from this spot-wise evaluation as it does not allow empty rows (spots) in the implementation of its package, and thus is not applicable to the prediction of the held-out test spots. The average performances of all the spatial spots using each of the 10 sptRNA-seq datasets are shown as bar plots. FIST consistently outperforms all the baselines with lower MAE and MAPE, and larger $R^2$ in all the 10 datasets. We further applied right-tailed paired-sample $t$-tests on $R^2$ values to test against the alternative

![Fig 2. Spot-wise cross-validation on 10x Genomics data. The performances of the four compared methods on the 10 tissue sections are measured by 5-fold cross-validation. Each bar shows the mean of the imputation performance of one method on all the spatial spots. The result on each of the 10 datasets is shown in one vertical column separated by dashed lines. The means are also compared between FIST and each of the baseline methods in S1 Table by paired-sample $t$-tests.](https://doi.org/10.1371/journal.pcbi.1008218.g002)
hypothesis that the $R^2$ produced by FIST has a larger mean than the mean of those produced by each of the baseline methods; and we also applied left-tailed paired-sample $t$-tests on MAE and MAPE values to test against the alternative hypothesis that the MAE and MAPE produced by FIST have a smaller mean than the mean of those produced by each of the baseline methods. The $p$-values in S1 Table show that comparing with the baseline methods, FIST has significantly lower MAE and MAPE in each of the 10 datasets, and larger $R^2$ in all comparisons but one, in which FIST performed only slightly better than GWNMF on HB2P dataset by $R^2$.

The performances of FIST and the baseline methods in the gene-wise evaluation are compared in Fig 3. The average and standard deviation of the prediction performances across all the genes are shown as error bar plots in Fig 3. Similar to the spot-wise evaluation, FIST clearly outperforms all the baselines with more robust performances across all the genes, as the variances in all the three evaluation metrics are also lower than the other compared methods. To examine the prediction performance more closely, we also showed the distributions of MAE, MAPE and $R^2$ of individual genes in the 10 datasets in S3–S5 Figs, respectively. The result is consistent with the overall performance in Fig 3. The observations suggest that FIST indeed performs better than the other methods in the imputation accuracy informed by the spatial information in the tensor model. It is also noteworthy that GWNMF, the MF method regularized by the spatial graph applied to each individual gene slice in tensor $T$, outperforms the other baselines in almost all the datasets. This observation further confirms that the spatial patterns maintained in each gene slice is informative for the imputation task. It is clear that FIST
outperformed GWNMF with better use of the spatial information coupled with the functional modules of the PPI network \( G_p \) and the joint imputation of all the genes in the tensor \( T \).

**Cartesian product graph regularization plays a significant role**

To demonstrate that the Cartesian product graph regularization in FIST significantly improves the imputation accuracy, we showed in Fig 4 the performance of FIST in each of the 10 datasets by varying the graph hyper-parameter \( \lambda \) in the spot-wise evaluation. By increasing \( \lambda \) from 0 to 0.1 to put more belief on the graph information, we observe an appreciable reduction on the MAE and MAPE, and increase on \( R^2 \) across all the 10 datasets. The observation strongly suggests that the predictions by FIST are improved by leveraging the information carried in the CPG topology, and the belief on the graph information can be effectively optimized by using a validation set in the cross-validation strategy.

To further understand the associations between the CPG regularization and characteristics of the expressions of the genes, we analyzed the genes that are benefiting most from the regularization by the CPG in the gene-wise evaluation. In particular, in the grid search of the optimal \( \lambda \) weight on the CPG regularization term by the validation set, we count the percentage of the genes with optimal \( \lambda = 0.01 \) rather than 0, which means completely ignore the regularization. To correlate the improved imputations with the sparsity of the gene expressions, we divided all the genes into 4 equally partitioned groups (L1-4) ordered by their densities in the sptRNA-seq data, where L1 and L4 contain the sparsest and the densest gene slices, respectively. For each of the four density levels, we count the percentage of gene slices that benefit from the CPG regularization and plot the results in Fig 5A. In the plots, there is a clear trend that the sparser a gene slice, the more likely it benefits from the CPG regularization in all the 10 datasets. In the densest L4 group, as low as 20% of the genes can benefit from the CPG regularization versus more than 50% in the sparest L1 group. This is understandable that there is less training information available for sparsely expressed genes (with more dropouts) and the spatial and functional information in the CPG can play a more important role in the imputation by seeking information from the gene’s spatial neighbors or the functional neighbors in the PPI network. This observation is also consistent with the fact that the performance of

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**Fig 4. Analysis of Cartesian product graph regularization with varying network hyper-parameter in spot-wise evaluation.** The plots show the imputation performance of FIST on the ten 10x Genomics datasets with varying network hyper-parameters in \([0, 0.1, 1]\) by MAE, MAPE and \( R^2 \).

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tensor completion tends to degrade severely when only a very small fraction of entries are observed [43, 44], and therefore those sparser gene slices tend to benefit more from the side information carried in the CPG.

We also compared the performance of FIST using the CPG of $G_x$, $G_y$, and $G_p$ with the one using a randomly permuted graph from the CPG. To generate the random CPG, we first generated three random graphs by permuting $G_x$, $G_y$, and $G_p$ individually which also preserves the degree distributions of the original graphs, by randomly swapping the edges in each graph while keeping the degree of each node. Then we measured the performances of FIST using the original CPG and the CPG obtained from the permuted graphs by MAE reduction, which is the total reduction of MAE on all the genes by varying hyperparameter $\lambda$ from 0 to 0.01 meaning not using the graph versus using the graph. The comparisons across all the 10 datasets are shown in Fig 5B. We observe that the FIST using the original graphs receives much higher MAE reduction than the FIST using the permuted graphs. This observation suggests the topology in the original CPG carries rich information that is helpful for the imputation task beyond just the degree distributions preserved in the random graphs.

**FIST imputations recover spatial patterns enriched by highly relevant functional terms**

To demonstrate that imputations by FIST can reveal spatial gene expression patterns with highly relevant functional characteristics among the genes in the spatial region, we performed comparative GO enrichment analysis of gene clusters detected with the imputed gene expressions. We conducted a case study on the Mouse Kidney Section data to further analyze the associations between the spatial gene clusters and the relevance between their functional characteristics and three kidney tissue regions, cortex, outer stripe of the outer medulla (OSOM) and inner stripe of the outer medulla (ISOM).

To validate the hypothesis that the imputed sptRNA-seq tensor $\tilde{T}$ given below

$$\tilde{T} = (1 - \mathcal{M}) \odot \hat{T} + T$$

can better capture gene functional modules than the sparse sptRNA-seq tensor $T$ does, we first rearranged both sptRNA-seq tensors into matrices $\tilde{T} \in \mathbb{R}^{N \times n_y}$ and $T \in \mathbb{R}^{N \times n_y}$, where $N = n_x n_y$.
denotes the total number of spots. We then applied K-means on each matrix to partition the genes into 100 clusters. Next, we used the enrichGO function in the R package clusterProfiler [45] to perform the GO enrichment analysis of the gene clusters. The total number of significantly enriched gene clusters (FDR adjusted p-value < 0.05) in each of the 10 tissue sections are shown in Fig 6, which clearly tells that K-means on the imputed sptRNA-seq data produces much more significantly enriched clusters across all the 10 tissue sections than the sparse sptRNA-seq data without imputation.

Finally, we conducted a case study on the Mouse Kidney Section and present the highly relevant functional characteristics in different tissues in mouse kidney detected with the imputations by FIST. For each of the 100 gene clusters generated by K-means as described above, we collapsed the corresponding gene slices in $\mathcal{T}$ into a $n_x \times n_y$ matrix by averaging the slices to visualize the center of the gene cluster. The enrichment results of all the 100 clusters are given in S2 Table. We focus on 3 kinds of representative clusters in Fig 7 which match well with three distinct mouse kidney tissue regions: cortex, ISOM (inner stripe of outer medulla) and OSOM (outer stripe of outer medulla). By investigating the enriched GO terms by the clusters (p-values shown in Table 3), we found their functional relevance to cortex, ISOM and OSOM regions. We found that the spatial gene cluster 9 which is highly expressed in cortex specifically enriched biological processes for the regulation of blood pressure (GO:0008217, GO:0003073, GO:0008015 and GO:0045777) and transport/homeostasis of inorganic molecules (GO:0055067 and GO:0015672). The spatial gene cluster 23 and 28 which are also highly expressed in cortex enriched cellular pathways that are critical for the polarity of cellular membranes (GO:0086011, GO:0034763, GO:1901017, GO:0032413 and GO:1901380) and the transport of cellular metabolites (GO:1901605, GO:0006520, GO:0006790 and GO:0043648),

Fig 6. Enrichment analysis on the sparse and imputed sptRNA-seq data. The total number of significantly enriched clusters (with at least one enriched GO term with FDR adjusted p-value < 0.05) in the 10 tissue sections are shown.

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respectively. These observations are consistent with previous studies reporting the regulation of kidney function by above listed biological processes in cortex [46–49]. In contrast, the pattern analysis of spatial gene expression in cluster 4, 8, 25 and 52 which are highly expressed in OSOM in kidney showed that catabolic processes of organic and inorganic molecules are specifically enriched such as GO:0015711, GO:0046942, GO:0015849, GO:0015718, GO:0010498, GO:0043161, GO:0044282, GO:0016054, GO:0046395, GO:0006631, GO:0072329, GO:0009062 and GO:0044242. These cellular processes are known to be active in renal proximal tubule which exists across cortex and OSOM [50–55]. Distinctively, the spatial gene clusters highly expressed in ISOM enriched pathways for nucleotide metabolisms (GO:0009150, GO:0009259 and GO:0006163) in cluster 3 and renal filtration (GO:0097205 and GO:0003094) in cluster 5. Collectively, these observations demonstrate that FIST could identify physiologically relevant distinctive spatial gene expression patterns in the mouse kidney dataset. Further, it suggests that FIST can provide a high-resolution anatomical analysis of organ functions in sptRNA-seq data.

**Experiments on additional low-resolution spatial gene expression datasets**

To demonstrate that FIST is broadly applicable to impute the spatial gene expression data generated with different platforms, we performed additional experiments on spatial transcriptomics datasets from 3 replicates of mouse tissue (olfactory bulb) provided from an earlier study [56]. Developed before 10x Genomics Visium Spatial protocol, the spatial transcriptomics technology [56] applies an aligned array to profile tissue with both lower spot density and larger spot size (1,007 spots in total, and 200 μm between spots). The design achieves a resolution of 100 μm (10-40 cells per spot). Similar to the experiments on the 10x Genomics data, we organized each of the 3 tissue replicates into a tensor \( T \in \mathbb{R}^{n_x \times n_y \times n_z} \), where \( n_x = 33 \) and \( n_y = 35 \) in all the 3 replicates, and \( n_p \) is 14,198, 13,818 and 138,40, respectively in replicate 1, 2 and 3. The \((i, j, k)\)-th entry in \( T \) is the RPKM value of the \(i\)-th gene at the \((k, j)\)-th coordinate in the array.

We performed the spot-wise 5-fold cross-validation as we did in the 10x Genomics data to compare the performances of FIST and the same baseline methods. The distributions of MAE, MAPE and \( R^2 \) on all the spatial spots in each of the 3 tissue replicates are shown in Fig 8.
Table 3. Functional terms enriched by spatial gene clusters (most significantly relevant functions).

| Region | Cluster | Significantly Enriched GO terms |
|--------|---------|---------------------------------|
| Cortex | Cluster 9 | GO:0003073—regulation of systemic arterial blood pressure (p = 9.1 × 10\(^{-6}\))
| | | GO:0008217—regulation of blood pressure (p = 1.0 × 10\(^{-5}\))
| | | GO:0055067—monovalent inorganic cation homeostasis (p = 4.3 × 10\(^{-5}\))
| | | GO:0008015—blood circulation (p = 5.3 × 10\(^{-5}\))
| | | GO:0045777—positive regulation of blood pressure (p = 5.8 × 10\(^{-5}\))
| | | GO:0015672—monovalent inorganic cation transport (p = 2.3 × 10\(^{-2}\))
| | Cluster 23 | GO:0086011—membrane repolarization during action potential (p = 2.2 × 10\(^{-3}\))
| | | GO:0034763—negative regulation of transmembrane transport (p = 2.2 × 10\(^{-3}\))
| | | GO:1901017—negative regulation of potassium ion transmembrane transporter activity (p = 2.4 × 10\(^{-3}\))
| | | GO:0032413—negative regulation of ion transmembrane transporter activity (p = 2.7 × 10\(^{-3}\))
| | | GO:1901380—negative regulation of potassium ion transmembrane transport (p = 3.4 × 10\(^{-3}\))
| | Cluster 28 | GO:1901605—alpha-amino acid metabolic process (p = 4.8 × 10\(^{-16}\))
| | | GO:0006520—cellular amino acid metabolic process (p = 6.4 × 10\(^{-9}\))
| | | GO:0006790—sulfur compound metabolic process (p = 3.1 × 10\(^{-8}\))
| | | GO:0043648—dicarboxylic acid metabolic process (p = 8.4 × 10\(^{-8}\))
| OSOM | Cluster 4 | GO:0015711—organic anion transport (p = 7.7 × 10\(^{-7}\))
| | | GO:0046942—carboxylic acid transport (p = 1.1 × 10\(^{-6}\))
| | | GO:0015849—organic acid transport (p = 1.1 × 10\(^{-5}\))
| | | GO:0015718—monocarboxylic acid transport (p = 5.0 × 10\(^{-5}\))
| | Cluster 8 | GO:0010498—proteasomal protein catabolic process (p = 1.3 × 10\(^{-9}\))
| | | GO:0006497—protein lipidation (p = 1.3 × 10\(^{-8}\))
| | | GO:0042158—lipoprotein biosynthetic process (p = 1.3 × 10\(^{-8}\))
| | | GO:0043161—proteasome-mediated ubiquitin-dependent protein catabolic process (p = 1.3 × 10\(^{-8}\))
| | Cluster 25 | GO:0044282—small molecule catabolic process (p = 5.5 × 10\(^{-14}\))
| | | GO:0016054—organic acid catabolic process (p = 1.0 × 10\(^{-14}\))
| | | GO:0046395—carboxylic acid catabolic process (p = 1.0 × 10\(^{-14}\))
| | | GO:0006631—fatty acid metabolic process (p = 2.9 × 10\(^{-14}\))
| | | GO:0072329—monocarboxylic acid catabolic process (p = 9.6 × 10\(^{-14}\))
| | | GO:0009062—fatty acid catabolic process (p = 1.0 × 10\(^{-13}\))
| | | GO:0044242—cellular lipid catabolic process (p = 4.7 × 10\(^{-13}\))
| | Cluster 52 | GO:0006732—coenzyme metabolic process (p = 1.2 × 10\(^{-10}\))
| | | GO:0006520—cellular amino acid metabolic process (p = 1.6 × 10\(^{-10}\))
| | | GO:1901605—alpha-amino acid metabolic process (p = 2.3 × 10\(^{-9}\))
| | | GO:0044282—small molecule catabolic process (p = 2.1 × 10\(^{-9}\))
| | | GO:0000906—sulfur amino acid metabolic process (p = 2.3 × 10\(^{-9}\))
| ISOM | Cluster 3 | GO:009150—purine ribonucleotide metabolic process (p = 7.4 × 10\(^{-8}\))
| | | GO:0009259—ribonucleotide metabolic process (p = 7.4 × 10\(^{-8}\))
| | | GO:0006163—purine nucleotide metabolic process (p = 7.4 × 10\(^{-8}\))
| | | GO:0019693—ribose phosphate metabolic process (p = 7.4 × 10\(^{-8}\))
| | | GO:0072521—purine-containing compound metabolic process (p = 7.4 × 10\(^{-8}\))
| | Cluster 5 | GO:0048872—osteogenesis of number of cells (p = 4.5 × 10\(^{-8}\))
| | | GO:0030218—erythrocyte differentiation (p = 3.2 × 10\(^{-8}\))
| | | GO:0034101—erythrocyte homeostasis (p = 3.2 × 10\(^{-8}\))
| | | GO:0003094—glomerular filtration (p = 3.2 × 10\(^{-8}\))
| | | GO:0097205—renal filtration (p = 3.2 × 10\(^{-8}\))

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Consistent with the observations in the previous Figs 2 and 3, FIST clearly outperforms all the baselines with lower MAE and MAPE, and larger $R^2$ in all the 3 replicates. The results suggest that FIST has a potential to be applied to various spatial transcriptomics datasets of different resolution and sparseness to achieve better imputation performance by modeling the spatial data as tensors, and including the prior knowledge with the CPG regularization.

To confirm that the imputation accuracy of FIST is significantly improved by the CPG regularization, we showed in Fig 9 the performance of FIST in each of the 3 replicates by varying the graph hyper-parameter $\lambda$ in the spot-wise evaluation. It is also consistent with the observation in the previous Fig 4, we can observe remarkable reduction on the MAE and MAPE and improvement on $R^2$ by increasing $\lambda$ to 0.1. The observation also verifies that the CPG topology is informative for the imputation task.

Discussions

In this study, we propose to apply tensor modeling of multidimensional structure in spatially-resolved gene expression data mapped by the 2D spatial array. To the best of our knowledge, this is the first work to model the imputation of spatially-resolved transcriptomes as a tensor completion problem. Our key observations in the experiments with the ten 10x Genomics Visium spatial transcriptomic datasets are that 1) the imputation accuracy is significantly improved by leveraging the tensor representation of the sptRNA-seq data, and 2) by incorporating the spatial graph and PPI network, the accuracy the imputation and the content of the

Fig 8. Spot-wise imputation performance on mouse tissue replicates. The performances of the four compared methods on the 3 replicates are measured by 5-fold cross-validation. The performance on each spatial spot is denoted by one dot in the box plots. The performances of different methods are shown in different colors.

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functional information in the imputed spatial gene expressions can be further improved significantly.

We observed that the genes that are more sparsely expressed can benefit more from the adjacency information in the spatial graph and the functional information in the PPI network. These genes can be empirically detected with a validation set to tune the only hyper-parameter $\lambda$ for deciding if the regularization by the product graph is needed for the imputation of a gene. Thus, we expect a low risk of overfitting in applying FIST to other datasets. In addition, the functional analysis of the spatial gene clusters detected on the Mouse Kidney Section data further confirms that FIST detects gene clusters with more spatial characteristics that are consistent with the physiological features of the tissue.

Overall, we concluded that FIST is an effective and easy-to-use approach for reliable imputation of spatially-resolved gene expressions by modeling the spatial relation among the spots in the spatial array and the functional relation among the genes. The imputation results by FIST are both more accurate and functionally interpretable. FIST is also highly generalizable to other spatial transcriptomics datasets with high scalability and only one hyper-parameter needed to tune.

Although our experiments mainly focused on medium density 10x Genomics Visium kit array (5000 spots or 1000 spots), we also plan to further develop variations of FIST for high-resolution spatial transcriptomics datasets with millions of spots generated by high-definition spatial transcriptomics (HDST) [14]. The HDST datasets from the study includes 3 mouse tissue sections from olfactory bulb and 3 human tissue sections from breast cancer using hexagonal array to profile tissue with a high density (1,467,270 spots in total) to achieve a resolution of 2 $\mu$m. The imputation tasks on the HDST datasets are quite different due to two reasons: First, each cell spans multiple spots. Simple imputation of each spot is not a
well-defined learning problem. Thus, the segmentation of the spots into each individual cell might be necessary as a pre-processing step. Second, the capture efficiency of HDST is as low as 1.3%, which leads to much sparser data for imputation. Our preliminary analysis indicate that the gene expression on the spots are too sparse to be meaning unless they are aggregated among the spots in a larger region. We plan to develop variations of FIST to overcome these additional challenges.

Another interesting future direction is to develop a variation of FIST for imputing spatial gene expressions with additional information from matched single-cell RNA sequencing data. For example, probabilistic graphical models have been introduced for imputing spatial gene expressions by integration with scRNA-seq data [57]. With the integration of PPI network and tensor modeling, FIST has a great potential to achieve better scalability as well as better accuracy for imputation of transcriptome-wide spatial transcriptomics data.

Supporting information

S1 Fig. Spatial regions with failed RNA fixing and permeabilization. The H&E images are shown on the left, and the heatmaps of the total RNA count at each spot are shown on the right. The regions with irregularly low RNA count are annotated by the circles.
(PDF)

S2 Fig. PPI co-expression analysis. The Pearson correlation coefficients between expression values of k-hop gene pairs from PPI network are shown as box plots. The Pearson correlation coefficients of different hop is shown in each column.
(PDF)

S3 Fig. Gene-wise imputation performance by MAE. The performances on the imputations of each gene are shown as box plots. The MAE of every gene slice is denoted by one dot. The performance of each method is shown in each colored box plot.
(PDF)

S4 Fig. Gene-wise imputation performance by MAPE. The performances on the imputations of each gene are shown as box plots. The MAPE of every gene slice is denoted by one dot. The performance of each method is shown in each colored box plot.
(PDF)

S5 Fig. Gene-wise imputation performance by $R^2$. The performances on the imputations of each gene are shown as box plots. The $R^2$ of every gene slice is denoted by one dot. The performance of each method is shown in each colored box plot.
(PDF)

S1 Table. $p$-values of paired-sample $t$-tests. The means of performance (measured by MAE, MAPE and $R^2$ as in Fig 2) for predicting all the spot fibers are compared between FIST and each of the baseline methods, using paired-sample $t$-tests.
(XLSX)

S2 Table. Enriched GO terms of spatial gene clusters. The GO terms significantly enriched by the genes in each spatial gene cluster (FDR adjusted p-value <0.05) are shown in the spreadsheet tables.
(XLSX)

S1 File. Convergence of FIST.
(PDF)
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References

1. Heppner GH. Tumor heterogeneity. Cancer research. 1984; 44(6):2259–2265. PMID: 6372991
2. Schmidt F, Efferth T. Tumor heterogeneity, single-cell sequencing, and drug resistance. Pharmaceuticals. 2016; 9(2):33. https://doi.org/10.3390/ph9020033 PMID: 2732289
3. Jaitin DA, Kenigsberg E, Keren-Shaul H, Elefant N, Paul F, Zaretsky I, et al. Massively parallel single-cell RNA-seq for marker-free decomposition of tissues into cell types. Science. 2014; 343(6172):776–779. https://doi.org/10.1126/science.1247651 PMID: 24531970
4. Macosko EZ, Basu A, Satija R, Nemesh J, Shekhar K, Goldman M, et al. Highly parallel genome-wide expression profiling of individual cells using nanoliter droplets. Cell. 2015; 161(5):1202–1214. https://doi.org/10.1016/j.cell.2015.05.002 PMID: 26000487
5. Klein AM, Mazutis L, Akartuna I, Tallapragada N, Veres A, Li V, et al. Droplet barcoding for single-cell transcriptomics applied to embryonic stem cells. Cell. 2015; 161(5):1187–1201. https://doi.org/10.1016/j.cell.2015.04.044 PMID: 26000487
6. Hebenstreit D. Methods, challenges and potentials of single cell RNA-seq. Biology. 2012; 1(3):658–667. https://doi.org/10.3390/biology10300658 PMID: 24832513
7. Liu S, Trappnell C. Single-cell transcriptome sequencing: recent advances and remaining challenges. F1000Research. 2016; 5. https://doi.org/10.12688/f1000research.7223.1 PMID: 26949524
8. Lubeck E, Coskun AF, Zhiyentayev T, Ahmad M, Cai L. Single-cell in situ RNA profiling by sequential hybridization. Nature methods. 2014; 11(4):360. https://doi.org/10.1038/nmeth.2892 PMID: 24681720
9. Lee JH, Daugharty ER, Scheiman J, Kalhor R, Yang JL, Ferrante TC, et al. Highly multiplexed subcellular RNA sequencing in situ. Science. 2014; 343(6177):1360–1363. https://doi.org/10.1126/science.1250212 PMID: 24578530
10. Shah S, Lubeck E, Schwarzkopf M, He TF, Greenbaum A, Sohn CH, et al. Single-molecule RNA detection at depth by hybridization chain reaction and tissue hydrogel embedding and clearing. Development. 2016; 143(15):2862–2867. https://doi.org/10.1242/dev.138560 PMID: 27342713
11. Chen KH, Boettiger AN, Moffitt JR, Wang S, Zhuang X. Spatially resolved, highly multiplexed RNA profiling in single cells. Science. 2015; 348 (6233). https://doi.org/10.1126/science.aaa6090 PMID: 25858977

12. Vickovic S, Stähl PL, Salmén F, Giatrellis S, Westholm JO, Mollbrink A, et al. Massive and parallel expression profiling using microarrayed single-cell sequencing. Nature communications. 2016; 7(1):1–9. https://doi.org/10.1038/ncomms13182 PMID: 27739429

13. Nawy T. Spatial transcriptomics. Nature Methods. 2018; 15(1):30–30. https://doi.org/10.1038/nmeth.4542

14. Vickovic S, Eraslan G, Salmen F, Klughammer J, Stenbeck L, Schapiro D, et al. High-definition spatial transcriptomics for in situ tissue profiling. Nature methods. 2019; 16(10):1897–900. https://doi.org/10.1038/s41592-019-0454-y PMID: 31501547

15. Berglund E, Maaskola J, Schultz N, Friedrich S, Marklund M, Bergensträhle J, et al. Spatial maps of prostate cancer transcriptomes reveal an unexplored landscape of heterogeneity. Nature communications. 2019; 9(1):1–13. https://doi.org/10.1038/s41467-018-04724-5 PMID: 29925878

16. Smith EA, Hodges HC. The spatial and genomic hierarchy of tumor ecosystems revealed by single-cell technologies. Trends in cancer. 2019; 5(7):411–425. https://doi.org/10.1016/j.trecan.2019.05.009 PMID: 31311656

17. Liang SB, Fu LW. Application of single-cell technology in cancer research. Biotechnology advances. 2017; 35(4):443–449. https://doi.org/10.1016/j.biotechadv.2017.04.001 PMID: 28390874

18. Prabhakaran S, Azizi E, Carr A, et al. Dirichlet process mixture model for correcting technical variation in single-cell gene expression data. In: International Conference on Machine Learning; 2016. p. 1070–1079.

19. Stegle O, Teichmann SA, Marioni JC. Computational and analytical challenges in single-cell transcriptomics. Nature Reviews Genetics. 2015; 16(3):133–145. https://doi.org/10.1038/nrg3833 PMID: 25628217

20. Prabhakaran S, Azizi E, Carr A, et al. Dirichlet process mixture model for correcting technical variation in single-cell gene expression data. In: International Conference on Machine Learning; 2016. p. 1070–1079.

21. Pierson E, Yau C. ZIFA: Dimensionality reduction for zero-inflated single-cell gene expression analysis. Genome biology. 2015; 16(1):241. https://doi.org/10.1186/s13059-015-0805-z PMID: 26527291

22. Hwang T, Tian Z, Kuang R, Kocher JP. Learning on weighted hypergraphs to integrate protein interactions and gene expressions for cancer outcome prediction. In: 2008 Eighth IEEE International Conference on Data Mining. IEEE; 2008. p. 293–302.

23. Chatr-Aryamontri A, Oughtred R, Boucher L, Rust J, Chang C, Kolas NK, et al. The BioGRID interaction database: 2017 update. Nucleic acids research. 2017; 45(D1):D369–D379. https://doi.org/10.1093/nar/gkw1102 PMID: 27980099
32. Sayama H. Estimation of Laplacian spectra of direct and strong product graphs. Discrete Applied Mathematics. 2016; 205:160–170. https://doi.org/10.1016/j.dam.2015.12.006
33. Horn RA, Horn RA, Johnson CR. Topics in matrix analysis. Cambridge university press; 1994.
34. Li Z, Zhang W, Huang RS, Kuang R. Learning a Low-Rank Tensor of Pharmacogenomic Multi-relations from Biomedical Networks. In: 2019 IEEE International Conference on Data Mining (ICDM). IEEE; 2019. p. 409–418.
35. Lee DD, Seung HS. Algorithms for non-negative matrix factorization. In: Advances in neural information processing systems; 2001. p. 556–562.
36. Smith S, Ravindran N, Sidiropoulos ND, Karypis G. SPLATT: Efficient and parallel sparse tensor-matrix multiplication. In: 2015 IEEE International Parallel and Distributed Processing Symposium. IEEE; 2015. p. 61–70.
37. Kim H, Park H. Sparse non-negative matrix factorizations via alternating non-negativity-constrained least squares for microarray data analysis. Bioinformatics. 2007; 23(12):1495–1502. https://doi.org/10.1093/bioinformatics/btm134 PMID: 17483501
38. Lim H, Polekscic A, Yao Y, Tong H, He D, Zhuang L, et al. Large-scale off-target identification using fast and accurate dual regularized one-class collaborative filtering and its application to drug repurposing. PLoS computational biology. 2016; 12(10):e1005135. https://doi.org/10.1371/journal.pcbi.1005135 PMID: 27716836
39. Camacho C, Coulouris G, Avagyan V, Ma N, Papadopoulos J, Bealer K, et al. BLAST+: architecture and applications. BMC bioinformatics. 2009; 10(1):421. https://doi.org/10.1186/1471-2105-10-421 PMID: 20003500
40. Gu Q, Zhou J, Ding C. Collaborative filtering: Weighted nonnegative matrix factorization incorporating user and item graphs. In: Proceedings of the 2010 SIAM international conference on data mining. SIAM; 2010. p. 199–210.
41. Xu C, Su Z. Identification of cell types from single-cell transcriptomes using a novel clustering method. Bioinformatics. 2015; 31(12):1974–1980. https://doi.org/10.1093/bioinformatics/btv088 PMID: 25805722
42. Satija R, Farrell JA, Gennert D, Schier AF, Regev A. Spatial reconstruction of single-cell gene expression data. Nature biotechnology. 2015; 33(5):495–502. https://doi.org/10.1038/nbt.3192 PMID: 25867923
43. Tomoka R, Suzuki T, Hayashi K, Kashima H. Statistical performance of convex tensor decomposition. In: Advances in neural information processing systems; 2011. p. 972–980.
44. Narita A, Hayashi K, Tomoka R, Kashima H. Tensor factorization using auxiliary information. Data Mining and Knowledge Discovery. 2012; 25(2):298–324. https://doi.org/10.1007/s10618-012-0280-z
45. Yu G, Wang LG, Han Y, He QY. clusterProfiler: an R package for comparing biological themes among gene clusters. Omics: a journal of integrative biology. 2012; 16(5):284–287. https://doi.org/10.1089/omi.2011.0118 PMID: 22455463
46. Crowley SD, Gurley SB, Oliverio MI, Pazmino AK, Griffiths R, Flannery PJ, et al. Distinct roles for the kidney and systemic tissues in blood pressure regulation by the renin-angiotensin system. The Journal of clinical investigation. 2005; 115(4):1092–1099. https://doi.org/10.1172/JCI200523378 PMID: 15841186
47. Coffman TM, Crowley SD. Kidney in hypertension: guyton redux. Hypertension. 2008; 51(4):811–816. https://doi.org/10.1161/HYPERTENSIONAHA.105.063936 PMID: 18332286
48. Veroulti SN, Boscardin E, Hummer E, Frateschi S. Regulation of blood pressure and renal function by NCC and ENaC: lessons from genetically engineered mice. Current opinion in pharmacology. 2015; 21:60–72. https://doi.org/10.1016/j.coph.2014.12.012 PMID: 25613995
49. Brown D, Wagner CA. Molecular mechanisms of acid-base sensing by the kidney. Journal of the American Society of Nephrology. 2012; 23(5):774–780. https://doi.org/10.1681/ASN.2012010029 PMID: 22362904
50. Yanase H, Takebe K, Nio-Kobayashi J, Takahashi-Iwanaga H, Iwanaga T. Cellular expression of a sodium-dependent monocarboxylate transporter (Slc5a8) and the MCT family in the mouse kidney. Histochernistry and cell biology. 2008; 130(5):957–966. https://doi.org/10.1007/s00418-008-0490-z PMID: 18751721
51. Nagamori S, Wiriyasermkul P, Guarch ME, Okuyama H, Nakagomi S, Tadagaki K, et al. Novel cystine transporter in renal proximal tubule identified as a missing partner of cystinuria-related plasma membrane protein rBAT/SLC3A1. Proceedings of the National Academy of Sciences. 2016; 113(3):775–780. https://doi.org/10.1073/pnas.1519959113 PMID: 26739563
52. Zalups RK. Organic anion transport and action of γ-glutamyl transpeptidase in kidney linked mechanistically to renal tubular uptake of inorganic mercury. Toxicology and applied pharmacology. 1995; 132 (2):289–298. https://doi.org/10.1006/taap.1995.1110 PMID: 7785056
53. Anzai N, Jutabha P, Enomoto A, Yokoyama H, Nonoguchi H, Hirata T, et al. Functional characterization of rat organic anion transporter 5 (Slc22a19) at the apical membrane of renal proximal tubules. Journal of Pharmacology and Experimental Therapeutics. 2005; 315(2):534–544. https://doi.org/10.1124/jpet.105.088583 PMID: 16079298

54. Tojo A, Sekine T, Nakajima N, Hosoyamada M, Kanai Y, Kimura K, et al. Immunohistochemical localization of multispecific renal organic anion transporter 1 in rat kidney. Journal of the American Society of Nephrology. 1999; 10(3):464–471. PMID: 10073596

55. Hwang JS, Park EY, Kim W, Yang CW, Kim J. Expression of OAT1 and OAT3 in differentiating proximal tubules of the mouse kidney. Histology and histopathology. 2010. PMID: 19924639

56. Ståhl PL, Salmén F, Vickovic S, Lundmark A, Navarro JF, Magnusson J, et al. Visualization and analysis of gene expression in tissue sections by spatial transcriptomics. Science. 2016; 353(6294):78–82. https://doi.org/10.1126/science.aaf2403 PMID: 27365449

57. Lopez R, Nazaret A, Langevin M, Samaran J, Regier J, Jordan MI, et al. A joint model of unpaired data from scRNA-seq and spatial transcriptomics for imputing missing gene expression measurements. arXiv preprint arXiv:190502269. 2019.