Exploring the role of conceptual scaffolding in solving synthesis problems

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It is well documented that when solving problems experts first search for underlying concepts while students tend to look for equations and previously worked examples. The overwhelming majority of end-of-chapter (EOC) problems in most introductory physics textbooks contain only material and examples discussed in a single chapter, rarely requiring a solver to conduct a general search for underlying concepts. Hypothesizing that complete reliance on EOC problems trains students to rely on a nonexpert approach, we designed and implemented “synthesis” problems, each combining two major concepts that are broadly separated in the teaching timeline. To provide students with guided conceptual scaffolding, we encapsulated each synthesis problem into a sequence with two preceding conceptually based multiple-choice questions. Each question contained one of the major concepts covered in the subsequent synthesis problem. Results from a small-scale interview study and two large-scale written tests showed that the scaffolding encouraged students to search for and apply appropriate fundamental principles in solving synthesis problems, and that repeated training using scaffolded synthesis problems also helped students to make cross-topic transfers.

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I. INTRODUCTION

An important goal of introductory physics is to train students to be competent problem solvers [1–6]. One feature characteristic of skilled problem solving is successive refinement that begins with a search for fundamental concepts [7–10]. Studies have shown that when solving a problem experts often qualitatively search for underlying concepts, followed by further elaboration at a more detailed level before performing quantitative analysis using mathematical equations [11–16]. In contrast, students frequently begin by searching for formulas and worked-out examples without recognizing deep structure (relevant concepts and principles) [11,12]. Among various types of problem-solving practices, traditional end-of-chapter exercises (EOCs) perhaps are most commonly used in introductory physics courses to train students in learning content. However, these EOCs often are localized, addressing only material covered in a single chapter [2,17]. When solving these problems, students are not motivated to search for underlying concepts, but rather are encouraged to look locally for formulas and worked-out examples and then do plug-and-chug to get a correct answer. As a result, they frequently fail to develop an expertlike approach even after doing a large number of EOCs [18,19].

Researchers have explored various ways to encourage students to rely on underlying concepts to solve physics problems. For example, Larkin [8] used “a programmed booklet, individual testing and remedial instruction” to train students to concentrate on physical principles in solving dc-circuit problems. Reif and Scott [20] designed a computer program entitled “personal assistance for learning” to promote important cognitive skills, including principle-oriented decision making. Dufresne et al. and Mestre and et al. [21,22] created a computer-based “hierarchical analysis tool” to facilitate student recognition of deep structure. Leonard et al. [23] implemented “strategy writing” to explicate underlying concepts involved in physics problems. Kanim employed “bridging exercises” to help students with concepts, thereby encouraging non-formula-driven approaches to electricity problems [24]. Most recently, a study by Singh [25] showed that when answering a qualitative question paired with a preceding isomorphic quantitative question, students could discern their underlying connections, a phenomenon bearing on analogical problem-solving techniques [26]. All of these studies suggest that effective problem-solving skills may be cultivated through target training.

On the basis of these studies, we designed and implemented problems containing multiple concepts that are broadly separated in the teaching timeline to foster effective problem-solving skills among introductory students. These problems, which we name “synthesis problems,” cannot be easily solved by simply invoking locally
A small object attached to a spring of stiffness $k$ is oscillating on a smooth surface, where the frictional force between the object and the surface is negligible. Initially the mechanical energy of the spring-object system is $E_i$. After the block travels a distance of $d$, how does the total mechanical energy of the spring-object system change?

(1) It remains the same: $E_i$
(2) It increases by a value of $kd^2$
(3) It increases, but the increased value is unknown
(4) It decreases by a value of $kd^2$
(5) It decreases, but the decreased value is unknown

A small object attached to a spring is oscillating on a rough surface, where the frictional force between the object and the surface is a constant $f$. Initially the mechanical energy of the spring-object system is $E_i$. After the block travels a distance of $d$, how does the total mechanical energy of the spring-object system change?

(1) It remains the same: $E_i$
(2) It increases by a value of $fd$
(3) It increases, but the increased value is unknown
(4) It decreases by a value of $fd$
(5) It decreases, but the decreased value is unknown

A small ball of mass 0.05 kg is attached to a spring of stiffness 2 N/m, and it oscillates along the x axis on a rough surface. Initially the maximum spring stretch is 1 m. Due to the friction between the ball and the table surface, the maximum stretch of the spring gets smaller. After traveling a distance of 3.8 m, the ball is at the position $x = +0.6$ m. At this moment what is the speed of the ball? The frictional coefficient between the ball and the table surface is $\mu_{\text{kinetic}} = \mu_{\text{static}} = 0.2$.

FIG. 1 (color online). A sequence example: (a) and (b) are two conceptually based multiple-choice questions; (c) is an open-ended problem that synthesizes broadly separated topics in teaching materials. We deliberately used the phrase of “mechanical energy” in (a) and (b) to distinguish it from “energy” of a system, as the former is conserved only in the absence of dissipative forces while the latter is always conserved regardless.
combining this topic with another one that was learned in the 1st quarter physics course: the work-energy theorem. We randomly divided the 12 recruited students into two groups using a blind design: “scaffolding group” (SG) and “plain problem group” (PPG), with 6 in each. Those in the SG group first answered the two conceptual questions in Figs. 1(a) and 1(b) and then solved the subsequent problem [Fig. 1(c)]. Before embarking on the synthesis problem, students were also told that they “may look for underlying connections between the two questions and the problem at hand.” But they were neither confirmatively assured that there must exist a connection nor were they told what the connections, if any, would be. To reduce unnecessary “study availability effects” (due to the proximity in time between scaffolding and test problem) [27], we purposely used a suggestive rather than an imperative statement to point out that students had an option to look for underlying connections. Besides this reminder, no additional feedback of any form (on the scaffolding questions or on the synthesis problem) was provided. Conversely, the PPG students were asked to solve the synthesis problem without being given the preceding questions. Students in both groups were allowed to use their textbooks, notebooks, and calculators.

During the interviews, students were required to talk aloud, and the interviewer provided minimal interventions only for reminding students to keep talking or asking them to clarify explanations not understood by the interviewer. Enough time was given to each student for the required task. Each session was concluded either when a student successfully finished the task or decided to stop. All interview sessions were video recorded and later transcribed. The students’ written work during the interviews was also collected for analysis.

B. Results

The two conceptual questions were shown to be fairly straightforward, and all SG students answered correctly with appropriate reasoning. For brevity and for the purpose of the study, we thereafter concentrate on student performance in solving the open-ended synthesis problem.

The interviews showed that all SG students were able to use the correct fundamental concepts (the work-energy theorem in connection with frictional force in oscillatory motion) to tackle the synthesis problem without referring to their textbooks or notes. Though some students made calculation errors and failed to obtain a correct final answer, all six recognized the connections of the preceding questions with the problem. The average time that the SG students took to identify these connections was 33 sec. In general, these students focused mainly on the fundamental concepts rather than on specific terms or their mathematical expressions. They correctly identified the initial and final states of the ball-spring system, enumerated corresponding energy forms, and attributed the decrease in the system’s mechanical energy to the work done by the frictional force in oscillation. The following excerpt illustrates a typical comment made by the SG students: “We don’t know whether or not this (x = 0.6 m) is when the spring is at its maximum compression... But we can use the ideas from last two questions that mechanical energy may not be conserved, but we can figure out what the work is done by friction. And because of that, then we can figure out what change in kinetic energy is at any point.” Based on these connections, all SG students then used a “forward” strategy [28] to solve the problem, working top-down from the known variables to the unknowns [29].

In contrast, none of the students in the PPG used the fundamental concepts as an initial approach and eventually failed to solve the problem. Although one student struggled to relate the problem to the work-energy theorem in the very late stage of her interview session, she was still unable to use it properly. During the debriefing after the interviews, we asked each PPG student to determine the speed of the ball at some intermediate position in the absence of friction; all could answer it correctly. But combining friction in oscillatory motion and the work-energy theorem proved difficult for them, and they resorted to novicelike strategies [30]. In particular, some students in the PPG immediately began to look into their textbooks or notes after reading the problem. Some specifically searched for formulas of damped oscillation, but soon came to a dead end [31]. They either could not make sense of the variables in the differential equation or could not solve it even if they knew what each variable represented. Some resorted to pattern matching, hoping to find similar worked-out examples in their textbooks [32]. But they quickly realized that this problem was not like the ones they saw in class.

### Table 1. Typical excerpts from the PPG students who approached the problem by equation search, pattern match, or random search.

| Type of search     | Number of students<sup>a</sup> | Typical excerpts                                                                 |
|--------------------|-------------------------------|----------------------------------------------------------------------------------|
| Equation search    | 4                             | “I’m gonna just write down the equation for damped motion.”                       |
| Pattern match      | 2                             | “I’m gonna try to find a problem that’s like this, an example like this...”       |
| Random search      | 2                             | “If I had to start, I would probably just start charting down everything that was relevant and see if anything came out of it. But it’d be just a shot in the dark.” |

<sup>a</sup>Some students used more than one type of search.
Other students aimlessly flipped through their notes, hoping to find hints. (Table I shows typical excerpts for each type of search.) Since these students could not relate the given information with unknowns, they often relied on the “means-ends”[28,33] approach to tackle the problem. Specifically, they started with an equation containing the speed variable and worked backwards to find more equations to solve for other unknowns in the equation. Then they worked forward to replace these unknowns in the preceding equations to finally find the speed of the ball.

One interesting observation was that although the PPG students solved only one problem, the amount of time they spent was comparable to that by the SG students who solved the same problem plus two conceptual questions (~ 20 min). This was largely because the PPG students spent a considerable amount of time thumbing through textbooks and notes for ideas.

IV. STUDY 2: INVESTIGATING IMMEDIATE EFFECTS OF SCAFFOLDING IN A LARGE-SCALE WRITTEN TEST

A. Procedure

A large-scale written test was conducted in the fall of 2008. The goal of this study was twofold. First, we wanted to see if results similar to study 1 would be obtained in a larger sample of students. Second, it was suggested that the effect of conceptual scaffolding used in the interviews might be equivalent to that of direct cueing [34]. If that were the case, then direct cueing alone would be sufficient to help students solve synthesis problems.

The questions and problem shown in Fig. 2 were used in a written test [35]. Here, the open-ended synthesis problem [Fig. 2(c)] addresses both linear and angular momenta—two topics that are taught, respectively, in the middle and at the end of the mechanics sequence at OSU [36]. In total, 360 students from 18 parallel recitation sections of a calculus-based introductory mechanics course took the written test and received credit for participation. We randomly divided these students into three groups by their recitation sections: SG, PPG, and “cuing group” (CG), with 143, 109, and 108 students in each. The SG students were first directed to answer the two conceptual questions in Figs. 2(a) and 2(b) either individually or collaboratively in 5 min. Here, the quantitative nature of the first scaffolding question required students to use learned physics concepts rather than intuitive knowledge to answer it, whereas the second qualitative question avoided asking students to perform similar calculations needed for solving the subsequent synthesis problem. After answering the scaffolding questions, students were then asked to work independently on the synthesis problem within 12 min. Similarly to study 1, the SG students were told that they “may look for underlying connections between the two questions and the problem.” But they were not told whether or not such connections necessarily existed or what they would be.

On a frictionless surface, a car of mass $M$ is moving at a speed of 10 m/s toward another stationary car of mass 2 $M$. Subsequently, they collide and stick together. What is the final speed of the two-car system?

1. 0 m/s
2. 3.3 m/s
3. 5 m/s
4. 6.6 m/s
5. 10 m/s
6. None of the above

A merry-go-round is initially spinning clock-wise around its axis with negligible friction. A child is running at a certain speed towards the merry-go-round, jumps on and stays near its edge. Consider the child and the merry-go-round as a system. How does the angular momentum of the system change after the child jumps on the merry-go-round?

1. Increases
2. Decreases
3. Remains the same
4. Cannot be determined

Tom throws a clay blob of mass $m$ at a massless “black clay catcher” located on the outer rim of a puck which in turn is riding on a horizontal frictionless air table. The clay is moving at a speed of $v$ in a direction tangent to the rim of the puck just before it sticks onto the catcher. Initially stationary, the system of puck plus clay after impact begins moving on the frictionless surface. Tom sees that the metal puck is a uniform disk with a mass of $M$ and a radius of $R$. Remember all uniform disks have a moment of inertia $\frac{1}{2} MR^2$. What is the final total kinetic energy of the moving puck plus clay system?

![FIG. 2. A sequence used for a large-scale written test. (a) and (b) are conceptual questions; (c) is an open-ended synthesis problem.](image-url)
They received no additional feedback (on the scaffolding questions or on the synthesis problem) other than this reminder. Students in the PPG group were given 17 min to solve only the synthesis problem without answering the preceding questions. Similarly, the CG students also were allowed 17 min to solve the problem without answering the questions. But a direct cueing that “Momentum and angular momentum may play a role” was given in the problem statement. All groups were permitted to use their textbooks, notes, and calculators.

Since we were more interested in how students approached the problem than whether they obtained a final correct answer, we judged their written responses against two criteria: consideration and proper application of the conservation laws of linear and angular momenta. Specifically, we used the following rubrics to examine the presence or absence of the criteria.

(1) **Consider fundamental concepts.**—Did the students show written evidence of considering both linear and angular momenta, and did they state that linear and angular momenta are conserved? Responses of any forms, including words, symbols, or diagrams, that contained either general expressions of the conservation laws or specific equations with expanded terms would be considered as meeting this criterion.

(2) **Meaningful expansion.**—Did the students make a meaningful expansion of the fundamental concepts to determine the final linear and angular speed of the system? Given a proper “consideration of fundamental concepts,” efforts to itemize and equate the system’s initial linear or angular momentum to that of the final state would be acceptable. (For example, writing down the initial and final angular momenta and equating them to solve for the final angular speed.) No penalty was given for typographical and computational errors or translation of errors.

Two researchers independently examined student solutions, and agreed on 94% of the cases. The few disagreements were resolved with follow-up discussions.

### B. Results

Student performance on the synthesis problem is depicted in Fig. 3, which shows the percentages of students in each group who considered and made meaningful expansion of the appropriate fundamental principles. As seen, more students in the SG and the CG started with the proper fundamental principles than those in the PPG. [SG: t(250) = 2.85, p = 0.005; CG: t(215) = 2.04, p = 0.042.] However, the percentages were comparable between SG and CG [t(249) = 0.67, p = 0.50]. This suggests that direct cueing and conceptual scaffolding were equally effective in prompting students to consider the relevant underlying principles. (A closer look at student responses further revealed that those who did not consider the conservation laws in the CG almost always dwelled on the definition of linear and angular momenta.) However, Fig. 3 also shows that a larger fraction of students in the SG made a meaningful expansion of the fundamental concepts than in the CG and the PPG. [CG: t(249) = 3.19, p = 0.002; PPG: t(250) = 2.54, p = 0.012.] This indicates that although direct cueing is as helpful as scaffolding in getting students started with the underlying concepts, it is less effective in facilitating a sensible expansion of the cued concepts.

These results notwithstanding, it is possible that the initial assignment of students had been inadvertently biased in favor of the SG. In other words, higher-achieving students by chance had been assigned to the SG. To rule out this possibility, we collected and examined students’ final course grades for the mechanics course they were then attending. As shown in Fig. 4, the average grade point was nearly the same across all groups [F(2, 351) = 0.12, p = 0.891].

To further examine how students of different grade levels performed on the synthesis problem, we divided students of each group into four achievement levels.
This study involved three parallel classes of a calculus-based introductory mechanics course. These classes shared the same course syllabus, materials, demonstrations, labs, recitations, quizzes, homework, midterm exams, and final exam. The instructors of all classes met weekly for more than an hour to compare and review lecture notes. They checked after each lecture to see where the other instructors were. The goal was to cover the same material at the same pace. Lectures of all instructors typically ended in the same place within 10 min or so. In short, the content and delivery were closely monitored to be as nearly as possible similar to what a single instructor might have done. We blindly assigned these classes into three treatment groups: SG, PPG, and control group (CTRL) containing 92, 82, and 90 students, respectively. All classes were given repeated training in the last 2 weeks (reduced to 10 days due to the overlapping of the second week with the Thanksgiving holiday) of a 10-week quarter. During this time, the SG students always received conceptual scaffolding prior to solving a synthesis problem; the PPG students always directly solved the same synthesis problems without conceptual scaffolding; and the students in the CTRL group were consistently required to solve a pair of textbooklike single-concept problems with the same topic coverage as each synthesis problem solved by the SG and PPG students. It is worth noting that the SG and PPG students received synthesis problems only for the 2-week training period. For the remaining 8 weeks of the quarter, students were mostly given traditional EOCs. Further, even during the 2-week training period students were given approximately twice as many EOCs as synthesis problems. Synthesis problems were used to augment rather than entirely replace conventional EOC problems.

In total, we used 10 sets of problem materials for each class in various learning environments, including 5 sets in lectures, 3 sets in recitations, 1 set in lab, and 1 set in homework. Take the SG class for instance: the instructor who had been trained to properly implement the materials used one set in each of the 5 lectures during the 2-week period. He followed similar procedures as outlined in study 1 and study 2, asking students to first answer the conceptual scaffolding questions and then solve a synthesis problem. A reminder to look for underlying connections was also given. Students were given time to first work on their own before the instructor modeled how to focus on deep structure rather than surface features to solve the synthesis problem. This activity took approximately 10 min in each lecture, accounting for 20% of the total lecture time. Anecdotal reports from the instructor showed a nearly 90% class attendance rate during the 2 weeks. Similar approaches were used for labs and recitations except that more time (15 min) was allocated to this activity. Also, students received feedback on how to solve the homework problems from their teaching assistants during a recitation class. Collectively, these problem
materials covered a range of mechanics topics, including force, motion, energy, rotational dynamics, and angular momentum, with an emphasis on the last two topics due to the requirement of the course syllabus. Nevertheless, the linear momentum topic was not covered during the entire training. In all cases except for homework, time on task was controlled to be the same for the three classes.

Four days after the 2-week training, all students took the common final examination in which the synthesis problem shown in Fig. 6 was included. This problem is similar to what was used in study 2 and combines two topics broadly separated in the teaching timeline: conservation of angular momentum (a topic frequently covered in the training) and conservation of linear momentum (a topic not covered in the training). All students, regardless of which treatment class they were from, directly solved this problem without receiving any scaffolding or hints. Subsequently, student solutions were collected, blind-coded (to reduce within-grader error), and analyzed by two researchers independently (to reduce between-grader error) by using the following grading schemes.

1. **Recognition.**—Did the student correctly identify the motion of the disk after collision (linear and angular)? Any words, diagrams, and/or symbols that correctly expressed the motion of the disk would be considered as meeting this criterion.

2. **Consideration.**—Did the student provide any written evidence showing that he or she considered using the correct fundamental principles (the linear and angular momentum conservation laws)? The same criterion as in study 2 was used.

3. **Expansion.**—Did the student make any meaningful expansion of the correct fundamental principles? The same criterion as in study 2 was used.

Analysis results were then compared between the two researchers. It was found that the interrater reliability was 96%, and the remaining divergence was resolved after discussion.

**B. Results**

Since this problem involves two topics, one covered and the other not covered in the training, we illustrate in Fig. 7 students’ performance on each topic individually. As shown, for the topic of linear momentum [Fig. 7(a)] the SG students performed best in all three aspects: identification, consideration, and expansion. Using the control group as a baseline, a $\chi^2$ test indicates that the SG students demonstrated significantly better performance in both considering and expanding the linear momentum conservation law [consideration: $\chi^2(1) = 9.26, p = 0.002$; expansion: $\chi^2(1) = 4.15, p = 0.04$], and a marginally significant better performance in identifying the disk’s linear motion [$\chi^2(1) = 3.61, p = 0.06$]. On the other hand, although a comparable portion of the PPG students could correctly identify the linear motion of the disk, many failed to consider invoking the pertinent conservation law, and the success rate for the PPG students to reach a meaningful expansion of this conservation law was nearly identical to that of the control group. Consequently, there was no
significant difference between the PPG and the control group [identification: $\chi^2(1) = 1.85$, $p = 0.17$; consideration: $\chi^2(1) = 1.52$, $p = 0.22$; expansion: $\chi^2(1) = 0.05$, $p = 0.82$].

As for the angular momentum topic, Fig. 7(b) shows that all classes performed well in recognizing the disk’s rotational motion, a phenomenon likely due to the recency effect[38], as rotational dynamics was the focus of the previous week’s teaching and training. But student subsequent performance quickly diverged. The SG students again displayed the highest success rate in both considering and expanding the angular momentum conservation law. Compared to the baseline control group, the SG students’ better performance was statistically significant [consideration: $\chi^2(1) = 6.75$, $p = 0.009$; expansion: $\chi^2(1) = 7.26$, $p = 0.007$]. Conversely, the PPG students only achieved an intermediate success rate, comparable to that of the control group [consideration: $\chi^2(1) = 1.86$, $p = 0.17$; expansion: $\chi^2(1) = 1.04$, $p = 0.31$].

The above results indicate that in the absence of scaffolding the SG students who were trained with scaffolded synthesis problems performed highest on both topics that were covered and not covered in the training. Nevertheless, a lingering concern was that the SG students in general might have a better course background and therefore outperformed the other two classes on the synthesis problem, a possible bias in the study. To address this concern, we collected and compared students’ mechanics course examination totals (two midterm and one final examination scores) in Fig. 8. As seen, students in all classes demonstrated similar course background with no evidence contesting that our initial assignment was biased in favor of the SG class over the others.

We further investigated how students at different course levels performed on the synthesis problem. We divided students into four quartiles according to their course exam totals. Also, to quantify their performance on the synthesis problem, a measure similar to that in study 2 was employed: a score of “3” was granted for achieving the “expansion” of both pertinent conservation laws, “2” for only reaching the “consideration” stage, “1” for

FIG. 8. Student exam totals for a calculus-based introductory mechanics course.

“recognition,” and “0” for no sensible solution at all. Figure 9 shows the results for students in each quartile of the three classes. As seen, the SG students at all levels outperformed their counterparts in the control group, indicating that the repeated training with scaffolded synthesis problems benefited students at all levels. For the PPG students, however, only the top two quartiles outperformed their counterparts in the control group, and the bottom two quartiles showed no sign of advantage. This suggests that the training using synthesis problems without conceptual scaffolding selectively benefited only the higher-achieving students but not the lower-achieving students.

VI. CONCLUSIONS AND DISCUSSION

We designed and implemented synthesis problems containing concepts that are broadly separated in the teaching timeline. Each problem was encapsulated into a sequence with two preceding conceptual questions which were related to it in terms of the same deep structure (concepts and principles). Prior to solving the problem, students were reminded to seek such relations without being told what the relations were. We implemented these questions, together with the reminder, as guided scaffolding to induce students’ attention to the underlying concepts and prepare them for solving the subsequent synthesis problem.

A small-scale interview study and two large-scale written tests were conducted to explore the role of conceptual scaffolding. Results from the first two studies show that without assistance students had difficulty dealing with synthesis problems, and that using guided scaffolding can prompt students to rely on conceptual knowledge in solving physics problems. Students who answered the preceding questions were more likely to recognize deep structure and thus successfully solve the synthesis problem than those who did not receive the scaffolding. Our studies also indicate that guided conceptual scaffolding is beyond direct cueing. Students who received direct cueing could recall concepts and principles relevant to the problem at
hand, but were less able to make a further sensible expansion than those who received conceptual scaffolding, a finding independent of students’ achievement levels measured by course grades. Here, we consider the cueing on “momentum and angular momentum” as direct because it guided students to narrow their search space from a repertoire of learned knowledge down to a small number of relevant definitions or laws. On the other hand, the conceptual scaffolding used in the studies was considered as less direct, as students were not explicitly informed of any relevant concepts when answering the scaffolding questions or solving the synthesis problem.

In light of the above results, it is worth noting that a direct cue without context is less effective in helping students solve synthesis problems than the contextualized scaffolding used in our studies. One possible explanation for such a result is that the scaffolding provided a level of abstraction more suitable than direct cueing, hence facilitating student application of relevant fundamental principles. It is also possible that because the direct cueing used in the study was decontextualized it failed to provide students an opportunity to make generalization of what was cued. According to Ross and co-workers [27,39,40], being able to generalize from given cues can help solvers use deep structural features to tackle task problems. Moreover, since students receiving scaffolding could choose to work collaboratively to answer conceptual questions before solving a synthesis problem, it is also surmised that students might have benefited from peer coaching in invoking and applying the relevant principles.

Our third study exhibits the sustained effects of conceptual scaffolding on students solving synthesis problems. Students who received two weeks of training with scaffolded synthesis problems demonstrated the highest success rate on a synthesis problem in the final examination, a situation where scaffolding was completely removed. Moreover, these students performed best both on concepts that were covered (conservation of angular momentum) and not covered (conservation of linear momentum) in the training process, indicating that the trained students were better able to make a cross-topic transfer in terms of recognizing and applying deep structure to solve synthesis problems. Our correlation analysis also showed that training with scaffolded synthesis problems benefited students at all levels, whereas the training with omitted scaffolding helped only higher-achieving students. What also is interesting is that the poor performance of the control group again suggests that solving textbooklike problems does not help students to combine their learned knowledge as required for solving synthesis problems.

These results provide useful implications for effective course instruction and future research. If conceptual scaffolding can be frequently used in class to guide students’ attention to deep structure, it is highly probable that they will habitually begin by searching for underlying concepts in solving physics problems. However, it is crucial that students realize and experience the unproductiveness of blind “plug-and-chug.” To achieve this end, some fraction of problems must be designed in a way that students cannot solve by haphazardly grabbing locally introduced formulas. Since our ultimate goal is to train students to be independent proficient problem solvers, it is essential that we continue to seek an optimal way of removing scaffolding to further benefit students. In our studies, a sudden removal of the scaffolding after two weeks of training yielded meaningful positive results. It is conceivable that a gradual removal of the scaffolding can result in equally profitable outcomes. Also, it can be beneficial to further investigate the effects of problem surface features on students’ performance by fine-tuning the similarities between scaffolding questions and synthesis problems [27,39,40]. This work may help identify effective means of manipulating certain features to maximally facilitate students’ access and instantiation of fundamental principles in solving synthesis problems. Moreover, the grading rubrics used in the present study, albeit useful, were rudimentary. In future studies, more detailed grading rubrics [41] may be developed to examine student problem solving at a finer grain level.

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