Complete breakdown of the Debye model of rotational relaxation near the isotropic-nematic phase boundary: Effects of intermolecular correlations in orientational dynamics

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The Debye-Stokes-Einstein (DSE) model of rotational diffusion predicts that the rotational correlation times $\tau_l$ vary as $[l(l+1)]^{-1}$, where $l$ is the rank of the orientational correlation function (given in terms of the Legendre polynomial of rank $l$). One often finds significant deviation from this prediction, in either direction. In supercooled molecular liquids where the ratio $\tau_1/\tau_2$ falls considerably below three (the Debye limit), one usually invokes a jump diffusion model to explain the approach of the ratio $\tau_1/\tau_2$ to unity. Here we show in a computer simulation study of a standard model system for thermotropic liquid crystals that this ratio becomes much less than unity as the isotropic-nematic phase boundary is approached from the isotropic side. Simultaneously, the ratio $\tau_2/\eta$ (where $\eta$ is the shear viscosity of the liquid) becomes much larger than hydrodynamic value near the I-N transition. We have also analyzed the break down of the Debye model of rotational diffusion in ratios of higher order rotational correlation times. We show that the break down of the DSE model is due to the growth of orientational pair correlation and provide a mode coupling theory analysis to explain the results.

I. INTRODUCTION

The rotational diffusion model of Debye [1,2] was proposed originally to explain dielectric relaxation of polar molecules and to relate the observed relaxation time to viscosity by the use of the Stokes-Einstein relation. The Debye-Stokes-Einstein (DSE) model is primarily devised to model the Brownian motion in orientational degrees of freedom. The DSE model provides the following amazingly simple expression for the decay of the $l$-th rank orientational correlation function $C_l^s(t)$

$$C_l^s(t) = \exp(-t/\tau_l),$$

with

$$\tau_l^{-1} = l(l+1)k_BT/\zeta_R,$$

where

$$\zeta_R = 6\etaV$$

In the above expression of rotational friction, $V$ is the volume of the molecule in question, $\eta$ is the viscosity of the liquid, $k_B$ is Boltzmann constant and $T$ is the temperature. The above expressions predict the ratio of the first and second-rank rotational correlation times, $\tau_1/\tau_2$, to be equal to three. The higher rank rotational correlation times also vary following the $[l(l+1)]^{-1}$ dependence. In the past, different aspects of DSE relationship have been tested namely, (a) the shape dependence [3,4,5], (b) the viscosity dependence, and (c) the rank dependence of the orientational relaxation, in simple as well as complex liquids.

In many cases, the ratio $\tau_1/\tau_2$ is found to fall below three. In particular, in supercooled liquids, the ratio is known to approach unity at low temperatures and related issues (like translation-rotation decoupling) that have given rise to considerable amount of discussion [6,7,8,9,10,11,12,13,14,15,16,17]. One often invokes the breakdown of Debye diffusion model, which requires small angle Brownian rotational motion for its validity, due to the emergence of large scale hopping involving large angular jumps. The basic idea is that a large jump leads to the decay of $C_l^s(t)$ of all rank $l$ at the same time, so that all of them have similar correlation times corresponding to the average waiting time for this large jump to occur.

The case of $\tau_1/\tau_2$ deserves particular attention because it is the oft discussed one. The sensitivity of these two correlation times (and hence the respective correlation functions) to intermolecular interactions is different. When the rotating molecule has dipolar interactions with the surrounding molecules, one expects the first rank rotation to be more affected than the second rank one. This is a manifestation of intermolecular correlation which is reflected in the orientational pair correlation functions. Thus, if we consider dipolar spheres (such Stockmayer liquid), we should expect the ratio $\tau_1/\tau_2$ to be larger than three. On the other hand, if the intermolecular interaction has up-down symmetry (as in the case of molecules with ellipsoid of revolution), the reverse could be true. Thus, one may need to include the role of intermolecular correlation to generalize the DSE model appropriately.

One ideal candidate to test the above argument regarding the role of equilibrium pair correlations is a system of model mesogens undergoing the isotropic-nematic (I-N) phase transition. The isotropic phase is both positionally and orientationally disordered while the nematic phase is still positionally disordered but orientationally ordered. Earlier experimental and simulations studies
have demonstrated that existing of the orientational relaxation of nematogens near I-N transition have similarities with that observed in the supercooled liquids. The orientational order parameter is defined by $S = \langle P_2(\cos(\theta)) \rangle$, where $\theta$ is the angle of the orientation of the molecular axis with the director. In the isotropic phase, $S = 0$ for infinitely large systems while it is non-zero (around 0.5) in the nematic phase. The important point is that orientational correlation undergoes rapid increase as the I-N phase boundary is approached from the isotropic side. This large growth in correlation would provide a testing ground of the rotational diffusion model and the role of intermolecular correlations.

Different molecular models have been used to test the DSE in molecular simulations. In a molecular dynamics simulation study using the Gay-Berne intermolecular potential [25], de Miguel et al. found the ratio $\tau_1/\tau_2$ to be always less than three in the isotropic phase. They found that the departure from the Debye limit was pronounced when density was reduced or temperature was increased; this deviation is a manifestation of the inertial decay which gives a ratio $[l + 1/l]$ for $\tau_1/\tau_{l+1}$. Vasanthi et al. [26] in extensive molecular dynamics simulations using the same model have studied the aspect ratio dependence of the DSE relationship [24]. Recently Jose and Bagchi have studied the breakdown of the DSE relationship near the I-N phase transition in a system of Gay-Berne ellipsoids of revolution [27]. They have shown that the relation between the rotational friction and viscosity breaks down near the I-N phase transition.

The motivation of the present work comes partly from recent reports of the observed similarity in the orientational relaxation between supercooled liquids and liquid crystals [18, 19, 20, 21, 22, 23, 24]. The deviation of the rank dependence from the Debye model (Eq.2) has been often discussed in the context of supercooled liquids. As discussed earlier, this is attributed to the existence of large angular jumps at low temperatures. In this work, we investigate the rank dependence of the rotational diffusion near the isotropic-nematic phase boundary. We find that the ratio $\tau_1/\tau_2$ becomes much less than unity as the isotropic-nematic phase boundary is approached from the isotropic side. Simultaneously, the ratio $\tau_2/\eta$ (where $\eta$ is the shear viscosity of the liquid) becomes much larger than hydrodynamic value near the I-N transition. We have also analyzed the breakdown of the Debye model of rotational diffusion in ratios of higher order rotational correlation times. Theoretical analysis shows that the breakdown of the DSE model can be attributed to the growth of orientational pair correlation. We provide a mode coupling theory analysis to explain the results. Thus, the present analysis seems to suggest that one need not always invoke large scale jump diffusion to explain the decrease of the ratio $\tau_1/\tau_2$ from the Debye limit. This view raises some interesting questions which we address in the Conclusion.

In the next section, we describe the system and simulation details. Results of our molecular dynamics simulation study of a system of ellipsoids of revolution with an aspect ratio equal to three along an isotherm and an isochores across the I-N phase transition is presented in the section III. These results show that the ratio $\tau_1/\tau_2$ can become much less than unity. This section also includes results for higher rank orientational time correlation functions (OTCF). In section IV we present a theoretical analysis which can explain theoretical aspects of these results. Section V provides a summary of our results and concluding remarks.

II. SYSTEM AND SIMULATION DETAILS

Here we consider a system of molecules with axial symmetry interacting with the Gay-Berne (GB) pair potential that has served as a standard model in the simulation studies of thermotropic liquid crystals. In the GB pair potential [28, 24], each molecule is assumed to be an ellipsoid of revolution having a single-site representation in terms of the position $r_i$ of its center of mass and a unit vector $e_i$ along its principal axis of symmetry. The GB interaction between molecules $i$ and $j$ is given by

$$U_{ij}^{GB}(r_{ij}, e_i, e_j) = 4\epsilon(r_{ij}, e_i, e_j)(\rho_{ij}^{-12} - \rho_{ij}^{-6})$$

where

$$\rho_{ij} = \frac{\mathbf{r}_{ij} - \sigma(r_{ij}, e_i, e_j) + \sigma_0}{\sigma_0} \cdot \frac{\sigma_0}{\sigma}.$$  \hspace{1cm} (5)

Here $\sigma_0$ defines the cross-sectional diameter, $r_{ij}$ is the distance between the centers of mass of molecules $i$ and $j$, and $\mathbf{f}_{ij} = \frac{r_{ij}}{r_{ij}}$ is a unit vector along the intermolecular separation vector $r_{ij}$. The molecular shape parameter $\sigma$ and the energy parameter $\epsilon$ both depend on the unit vectors $e_i$ and $e_j$ as well as on $\mathbf{f}_{ij}$ as given by the following set of equations:

$$\sigma(r_{ij}, e_i, e_j) = \sigma_0 \left[1 - \frac{\chi}{2} \left(\frac{(e_i \cdot f_{ij} + e_j \cdot f_{ij})^2}{1 + \chi(e_i \cdot e_j)} + \frac{(e_i \cdot f_{ij} - e_j \cdot f_{ij})^2}{1 - \chi(e_i \cdot e_j)}\right)\right]^{-1/2}$$  \hspace{1cm} (6)
with \( \chi = (\kappa^2 - 1)/(\kappa^2 + 1) \) and

\[
\epsilon(\hat{r}_{ij}, e_i, e_j) = \epsilon_0[\epsilon_1(e_i, e_j)]^{\nu}[\epsilon_2(\hat{r}_{ij}, e_i, e_j)]^\mu
\]

where the exponents \( \mu \) and \( \nu \) are adjustable, and

\[
\epsilon_1(e_i, e_j) = [1 - \chi^2(e_i \cdot e_j)^2]^{-1/2}
\]

and

\[
\epsilon_2(\hat{r}_{ij}, e_i, e_j) = 1 - \frac{\chi'}{2} \left[ \frac{(e_i \cdot \hat{r}_{ij} + e_j \cdot \hat{r}_{ij})^2}{1 + \chi'(e_i \cdot e_j)} + \frac{(e_i \cdot \hat{r}_{ij} - e_j \cdot \hat{r}_{ij})^2}{1 - \chi'(e_i \cdot e_j)} \right].
\]

with \( \chi' = (\kappa' \cdot 1/\mu - 1)/(\kappa' \cdot 1/\mu + 1) \). Here \( \kappa = \sigma_{ss}/\sigma_{ee} \) is the aspect ratio of the molecule with \( \sigma_{ee} \) denoting the molecular length along the major axis and \( \sigma_{ss} = \sigma_0 \), and \( \kappa' = \epsilon_{ss}/\epsilon_{ee} \), where \( \epsilon_{ss} \) and \( \epsilon_{ee} \) are the depth of the minima of potential for a pair of molecules aligned parallel in a side-by-side configuration and end-to-end configuration, respectively. It follows that the GB pair potential defines a family of potential models, each member of which is characterized by a set of four parameters \( (\kappa, \kappa', \mu, \nu) \). In the present work, we employ the Gay-Berne pair potential with the original and most studied parametrization \( (3, 5, 2, 1) \).

All quantities are given in reduced units defined in terms of the Gay-Berne potential parameters \( \epsilon_0 \) and \( \sigma_0 \): length in units of \( \sigma_0 \), temperature in units of \( \epsilon_0/k_B \), and time in units of \( (m\sigma_0^2/\epsilon_0)^{1/2} \), \( m \) being the mass of the ellipsoids of revolution. We set the mass as well as the moment of inertia of the ellipsoids equal to unity. The simulation is run in a microcanonical ensemble with the system in a cubic box with periodic boundary conditions. Further details of the simulation can be found elsewhere [22].

The system of Gay-Berne ellipsoids of revolution with aspect ratio 3 is studied separately along an isotherm with density variation and along an isochore with temperature variation across the I-N transition. As compared to the density driven transition, the temperature driven I-N transition in the present system is known to be rather diffuse [30]. Next we present the results of our study.

### III. RESULTS

#### A. Density variation along an isotherm

In figure 1 we show the orientational order parameter with density as a system of 576 Gay-Berne ellipsoids of revolution transits across the I-N transition along an isotherm at temperature \( T^* = 1 \). The phase transition is found to occur over a range of density between 0.305 and 0.315. In figures 2(a) and 2(b), we show the decay of the single-particle orientational correlation function for the first eight ranks in the isotropic phase and near the I-N phase boundary, respectively. The \( l \)th rank single-particle orientational time correlation function (OTCF) is defined as

\[
C_l^l(t) = \frac{\sum_i P_l(\hat{e}_i(0), \hat{e}_i(t))}{\sum_i P_l(\hat{e}_i(0), \hat{e}_i(0))}.
\]

where \( \hat{e}_i(0) \) is the unit vector along the symmetry axis of the \( i \)th ellipsoid of revolution. The DSE model is found to hold good for all ranks of the single-particle orientational time correlation functions shown in Fig. 2(a) in the isotropic phase. As the rank of the correlation function increases, the relaxation time decreases.

Near the I-N phase boundary, as shown in Fig. 2, the relaxation of the single-particle OTCFs slows down considerably for all ranks. However, \( C_l^l(t) \) gets affected differently for different \( l \) values. The even and the odd \( l \)-th \( C_l^l(t) \) behave differently with the appearance of a pronounced plateau in \( C_2^l(t) \) and \( C_4^l(t) \). Interestingly, a similar decay behavior has been observed in supercooled liquids [3, 13].

Figure 2(b) shows that although the initial decay of \( C_2^l(t) \) and \( C_4^l(t) \) is faster than that of \( C_1^l(t) \) and \( C_3^l(t) \),

![Image of Figure 1: The evolution of the orientational order parameter with density along the isotherm at temperature \( T^* = 1 \).]
respectively, the decay becomes slower at longer times. The even \( l \)-th correlation functions both develop a rather long and distinct plateau. The decay of \( C_4(t) \) is particularly revealing because it shows all the four phases of decay – the initial Gaussian, followed by the exponential, then the crossover to the plateau and the final exponential decay.

In figure 3 we show the evolution of the ratios \( \tau_1/\tau_2 \), \( \tau_1/\tau_3 \), and \( \tau_1/\tau_4 \) as increase in density drives the system across the I-N transition. Note that away from the I-N phase boundary in the isotropic phase, the ratios remain close to what are predicted by the Debye rotational diffusion model. However, as the I-N phase boundary is approached from the isotropic side, it is evident that the Debye rotational diffusion model breaks down completely.

In figure 4 we show the ratios between the second-rank orientational correlation time and the higher rank orientational correlation times across the I-N transition. The circles represent the data for \( \tau_2/\tau_3 \) and the triangles for \( \tau_2/\tau_4 \). The ratios are scaled by the corresponding Debye predictions.

FIG. 2: The time evolution of the single-particle orientational time correlation functions, whose rank range from 1 to 8, shown in a log-log plot at two densities corresponding to (a) \( \rho^*=0.285 \); (b) \( \rho^*=0.315 \). The curves are arranged in the decreasing order of ranks from the left to the right in each plot.

FIG. 3: The density variation of the ratios between the first-rank orientational correlation time and the second, third, and fourth rank orientational correlation times across the I-N transition. The circles represent the data for \( \tau_1/\tau_2 \), the diamonds for \( \tau_1/\tau_3 \) and the triangles for \( \tau_1/\tau_4 \). The ratios are scaled by the corresponding Debye predictions.

FIG. 4: The ratios between the second-rank orientational correlation time and the higher rank orientational correlation times across the I-N transition. The triangles represent the data for \( \tau_2/\tau_3 \) and the circles for \( \tau_2/\tau_4 \). The ratios are scaled by the corresponding Debye predictions.

present work. Figure 4 shows a cusp like behavior which is well-known in the study of equilibrium critical phenomena of finite sized systems. Its appearance in dynamics suggests the existence of large scale fluctuations in the orientational order parameter \[31\]. Since the second rank orientational correlation function is associated with the optical response of the system which undergoes dramatic increase near the I-N transition \[31, 32\], the most affected orientational memory function is the second-order one.

Microscopically this phenomenon may be understood qualitatively in terms of the molecular field theory of...
Maier and Saupe [31, 32, 33], where the molecule is confined in an effective field created by its neighbors. This effective potential is given by the expression

\[ u_i = -\frac{A}{V^2}\frac{1}{2}S(3\cos^2(\theta_i) - 1) \]  

where \( A \) is constant independent of the temperature, volume, and pressure, \( V \) is the molecular volume and \( \theta_i \) is the angle between molecular axis with a preferred axis. This effective potential grows as the order parameter increases. Note that a \( \pi \) rotation of the molecular axis relaxes \( C_i^1(t) \) but not \( C_i^2(t) \). This effect is manifested in the higher order orientational correlation functions also. However, a random orientation of the smaller angle less than \( \pi/2 \) is only required for the relaxation of the \( C_l^i(t) \) with \( l \geq 3, 4, \ldots \) etc. Hence the slow down of relaxation at these ranks appears as \( S \) becomes significantly large. In section IV, we present a quantitative theory to describe these effects.

Another important aspect of the DSE which has been a subject of intense study in the literature of supercooled liquids is the viscosity (\( \eta \)) dependence of the time constant (\( \tau_i \)) of orientational correlation function. In figure 5, we present the semi-log plot of this ratio against density. The ratio remains a constant in the isotropic phase of the liquid crystals, in agreement with hydrodynamic prediction. This is also in accordance with the earlier simulation [27] which shows the ratio between the rotational friction and the viscosity also shows similar behavior.

Note that unlike in supercooled liquids, the growth in the viscosity of the nematogens near the I-N transition is not rapid [27]. Therefore, the ratio between \( \tau_i \) and \( \eta \) deviates from the DSE prediction only due to the growth of \( \tau_i \). It is also evident that the violation of the DSE is found to be different for the odd and the even values of \( l \). In figure 5, the ratio between \( \tau_i \) and \( \eta \) for even \( l \) values grows more dramatically than that for odd \( l \) values.
time. From the corresponding integral orientational correlation function to decay by the Debye limit as shown by the dot-dashed line. The prime is used to distinguish it from the temperature below which the orientational correlation time is beyond the scope of the present simulation study. The poor data quality at long times with the present run length restricts us from having a reasonable fit of the long-time decay. In order to have an estimate of the second-rank orientational correlation time for the sake of comparison of the rank-dependent orientational correlation times, we define a correlation time for the sake of comparison of the rank-dependent memory function. The above difference arises because temperature variation leads only to small changes in density because of the dominance of the repulsive part of the potential in determining the liquid structure.

**IV. THEORETICAL ANALYSIS OF ORIENTATION RELAXATION**

Here we present a mode coupling theory (MCT) analysis of the above relaxation behaviour. MCT has a long and honorable history in describing dynamics near phase transitions [34, 35, 36]. Our starting point of the theoretical analysis is the Zwanzig-Mori continued fraction representation of the frequency dependent orientational time correlation function, $C_l(z)$ [37, 38, 39, 40],

$$C_l(z) = \frac{1}{z + \frac{l(l+1)\tau_2 \tau_l}{\tau(z+\Gamma_l(z))}} \quad (12)$$

where $I$ is the moment of inertia and $\Gamma_l(z)$ is the Laplace frequency ($z$) and rank dependent memory function. The latter is determined by the torque-torque correlation function. In general, it is very difficult to determine this correlation function from first principles, but as a first approximation, we would combine input from the mode coupling theory with that from the time dependent density functional theory to obtain an expression for the memory function, $\Gamma_l(z)$, which can be used to understand the reasons for the breakdown of the DSE model. Near the I-N transition the memory function $\Gamma(z)$ can be written as a sum of two parts

$$\Gamma_l(z) = \Gamma_{bare} + \Gamma_{sing}(z), \quad (13)$$

where the bare part of the memory function is assumed to be rank and frequency independent. This can be described by the two-body (binary) collision model. Note that in conjunction with Eq.12 $\Gamma_{bare}$ leads to the DSE
behaviour. The singular part of the memory function contains effects of intermolecular correlation and is rank dependent. It is given by \[18\] .  

\[ \Gamma^{s\ell m(g)}_{l}(z) = \frac{3k_{B}T_{\rho}}{8\pi^{2}I} \int_{0}^{\infty} dt \, e^{-zt} \int_{0}^{\infty} dk \, k^{2} \sum_{m} c^{2}_{\ell m}(k) F_{l m}(k, t). \]  

(14)

In the above equation, \( \Gamma_{l} \) is the rank and frequency dependent memory function. This is a function of the \( l, l, m \) component of the wavevector dependent direct correlation function \( c_{\ell m}(k) \) (in the inter molecular frame). \( F_{l m}(k, t) \) is the \( l, m \) component of the orientation dependent self-intermediate scattering function. The \( F_{l m}(k, t) \) is defined in terms of the spherical harmonics as  

\[ F_{l m}(k, t) = \left\langle e^{i(k(\mathbf{r}(t) - \mathbf{r}(0)))} Y_{l m}(\Omega, 0) Y_{l m}(\Omega, t) \right\rangle. \]  

(15)

The single particle position and orientation dependent \( \Gamma(\mathbf{r} - \mathbf{r}', \mathbf{t} - t', \Omega, \Omega') \) memory function is related to the torque-torque correlation function through the density functional theory by following the fluctuation dissipation theorem \[18, 19, 40\]. Note that \( \Gamma^{s\ell m(g)}_{l}(z) \) contains the integration over the wave vector dependence. The slow down of the relaxation of single particle orientational correlation function is related to the nature of the component of the dynamics structure factor.

It is important to note that the rotational friction depends on the rank of the orientational correlation function and this friction differs from rank to rank because of vastly different wave vector dependence of \( F_{l m}(k, t) \), for different \( \ell \), particularly at low wavenumbers. Near the I-N transition, due to existence of large wave length fluctuations, the \( k \to 0 \) component of the \( F_{20}(k, t) \) undergoes a very slow decay and this is responsible for the slow down of the relaxation of the \( C_{2}^{0}(t) \). In this limit, the expression for \( F_{2m}(k, t) \) is given by \[15\] .

\[ F_{l m}(k, t) = S_{l m}(k) e^{-\frac{(k^{2}+D_{R}^{2}t^{2})^{\ell m}}{2S_{l m}(k)}}; \]  

(16)

where \( S_{l m}(k) \) is the orientation dependent structure factor and \( D_{R} \) is the rotational diffusion coefficient. The \( S_{l m}(k) \) is given by the expression  

\[ S_{l m}(k) = \left\langle e^{i(k(\mathbf{r}(t) - \mathbf{r}(0)))} Y_{l m}(\Omega, 0) Y_{l m}(\Omega, t) \right\rangle. \]  

(17)

Near the I-N transition, \( S_{20}(k) \) grows as \( 1/B^{2}k^{2} \) (\( B = \frac{\rho^{3}}{\pi^{2}} \left( \frac{S_{l m}(k)}{c_{l m}(k)} \right) \)). The growth of orientational pair correlation with the approach of the I-N transition is evident in figure 8. Note that the starting from density \( \rho^{*} = 0.305 \), the orientational pair correlation function becomes non-zero even at large intermolecular separations. This is reflected in the rapid growth of \( S_{20}(k) \) as \( k \to 0 \) near the I-N transition.

Combination of the above factors provides the following simple expression for the frequency dependence of the singular part of the memory kernel  

\[ \Gamma^{s\ell m(g)}_{2}(z) = A/\sqrt{z} \]  

(18)

where \( A \) is a numerical constant \[18\]. Note that such a power law dependence is absent from all odd \( \ell \)-th \( \Gamma_{\ell} \) but in principle present in all the even \( \ell \). However, as \( \ell \) increases, the decay becomes increasingly inertial and the role of intermolecular correlation becomes weak beyond \( \ell = 4 \). But for \( \ell = 2 \) and \( \ell = 4 \), the inverse square root dependence of the rotational memory function leads to a markedly slower, power law decay, as seen from figure 2(b).

Physically, this power law is a manifestation of the growth of the pseudo-nematic domains near the I-N phase boundary. A particle inside this domain feels a localizing potential which makes its rotation difficult. However, even within such a domain, a rotation of an individual particle by \( 180^{\circ} \) (that is, by \( \pi \)) is possible because of the up-down symmetry of the particle. However, in contradiction to the conceptualization prevalent in supercooled liquid literature, here such a half-cycle rotation relaxes only the odd rank correlation functions, leaving the even ranked ones unchanged. In the MCT description, the influence of the localizing potential enters through the two particle direct correlation function \( c_{l m}(k) \) and the static structure factor \( S_{l m}(k) \). Just as in the Maier-Saupe theory, the present mean-field theory description can capture the rank dependence of the effective localizing potential.

The above mode coupling theory analysis is by no means complete, but it provides a semi-quantitative explanation of the observed rank dependence of the orientational correlation time near the I-N transition, in terms of the rapid growth of equilibrium orientational pair correlation function.
V. CONCLUDING REMARKS

Let us first summarize the main results presented here. We study a system of Gay-Berne model mesogens along an isotherm and an isochore separately across its isotropic-nematic phase transition to investigate the rank dependent single-particle orientational relaxation from the perspective of the Debye behavior. Our results demonstrate that orientational correlation that starts growing near the I-N transition as it is approached from the isotropic side induces a marked deviation from the Debye behavior. Instead, our analysis randomizes and thereby leads to the decay of correlation of all ranks with the same rate. Instead, our analysis attributes the non-Debye rank dependence to the rapid growth of equilibrium orientational pair correlation function.

As already mentioned, an earlier onset of stretching in the even rank correlation functions than in the corresponding odd rank functions has been observed in supercooled liquids as well. This similarity is indeed interesting and deserves further study.

In view of the results presented here, a comparative study between dielectric relaxation (which essentially measures the $\ell = 1$ correlation function) and light scattering or fluorescence depolarization or even NMR (all of these measure the $\ell = 2$ correlation function) should be worthwhile. In fact, a detailed theoretical analysis of dielectric relaxation near the I-N phase boundary seems to be lacking.

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