High-fidelity, broadband stimulated-Brillouin-scattering-based slow light using fast noise modulation

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Abstract: We demonstrate a 5-GHz-broadband tunable slow-light device based on stimulated Brillouin scattering in a standard highly-nonlinear optical fiber pumped by a noise-current-modulated laser beam. The noise-modulation waveform uses an optimized pseudo-random distribution of the laser drive voltage to obtain an optimal flat-topped gain profile, which minimizes the pulse distortion and maximizes pulse delay for a given pump power. Eye-diagram and signal-to-noise ratio (SNR) analysis show that this new broadband slow-light technique significantly increases the fidelity of a delayed data sequence, while maintaining the delay performance. A fractional delay of 0.81 with a SNR of 5.2 is achieved at the pump power of 350 mW using a 2-km-long highly nonlinear fiber with the fast noise-modulation method, demonstrating a 50% increase in eye-opening and a 36% increase in SNR compared to a previous slow-modulation method.

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1. Introduction

Stimulated-Brillouin-scattering (SBS)-based slow light in room temperature optical fibers has attracted extensive research interest over the past few years. A fiber-based slow light system can controllably delay optical pulses and can operate over the entire transparency window of the fiber. However, the narrow ($\sim 35$ MHz) naturallinewidth of the SBS resonance (full width at half magnitude FWHM) in standard single-mode fibers has limited its application to low-data-rate systems. To solve this problem, broadband SBS slow-light techniques were developed. Herráez et al. first used direct current modulation of a semiconductor laser to broaden its spectrum to $\sim 325$ MHz and hence increased the SBS bandwidth to this value. Subsequently, a number of groups have demonstrated broadband SBS slow-light with bandwidths up to tens of GHz, a data rate compatible with modern optical communication systems. In addition to broadening the spectral linewidth of the SBS resonance, a judicious choice of the current modulation waveform can be used to tailor the SBS gain profile, resulting in improved delay performance for the broadband SBS slow light systems. The optimal gain profile that improves the pulse delay under constraints of pulse distortion and pump power is a flat-top gain spectrum with sharp edges. These broadband SBS slow light experiments have extended the application of SBS slow light to broadband all-optical communication devices such as data buffering and data packet synchronization.

Most previously reported broadband SBS slow light experiments control the spectral SBS gain profile by direct modulation of the pump laser using a periodic modulation waveform. The frequency of the waveform is typically chosen to be in the sub-MHz range so that detailed features of the waveform can be reproduced faithfully using an arbitrary waveform generator. However, such modulation induces low-frequency fluctuations in the SBS signal, as we discuss below. Previous research that focused on averaged pulse delay was not affected by these fluctuations because they were averaged out. Nevertheless, these low-frequency fluctuations reduces the signal-to-noise ratio (SNR) for a delayed data sequence and degrades fidelity of the device.

To build an optimal high-fidelity broadband SBS slow light system, we develop a systematic procedure to generate a broadband flat-topped SBS gain profile with direct noise current modulation. Random noise current modulation has been used in previous research on broadband SBS slow light systems. However, due to limited control over the spectral profile, these previous methods generally result in a Gaussian-shaped SBS gain profile. The frequency-dependent gain of a Gaussian profile causes pulse distortion for large delays. Although Yi et al. have discussed shaping the pump spectrum by passing a noise waveform through a saturated electronic amplifier, the control over the SBS gain profile is still limited and highly sensitive to the...
detailed saturation characteristics of the high speed amplifier, which is often hard to characterize. Here, we present an extension of Yi’s method in which the noise distribution is arbitrarily controlled. Compared to Yi’s work, the method described in this paper is superior because we have complete control over the noise waveform in a way that is easily generalized to any DFB laser used as a pump beam in broadband SBS slow light systems. It will be shown that, by controlling the distribution of the noise waveform, we are able to tune the shape of the SBS gain profile and obtain the best flat-topped profile that optimizes the slow light delay and reduces distortion. We also find that using a noise modulation function with a sampling rate $\sim 400$ MHz (fast compared to the phonon lifetime ($\sim 4$ ns) in the fiber) substantially stabilizes the optical signal and improves the data fidelity of the broadband SBS slow light system compared to previous slow modulation methods.

The rest of the paper is organized as follows. Section 2 briefly reviews the dynamics of a distributed feedback (DFB) laser under direct current modulation and describes the procedure to obtain a flat-topped SBS gain profile with two different (slow and fast) modulation waveforms. Section 3 describes and compares the delay performance for a 5-Gb/s return-to-zero (RZ) data sequence using these two methods and quantifies transmission fidelity by eye-opening (EO) and signal-to-noise ratio measurements. Finally, our conclusions are summarized in Sec. 4.

2. Broadband optimal SBS gain profile design with direct current modulation

In broadband SBS slow light systems, a spectrally broadened laser is used as the pump beam. In our experiment, a modulation voltage $V(t)$ is added to the DC injection current of the DFB laser via a bias-T (input impedance = 50 $\Omega$). The DFB laser spectrum is thereby broadened. Broadening of the laser’s spectrum with direct current modulation has been widely used and a quantitative, semiempirical model for the instantaneous spectral shift of the DFB laser output due to direct current modulation $i(t)$ has been established in [14]. The spectral shift $\omega_p(t)$ as a function of time is given by

$$\omega_p(t) = a_0 i(t) - i(t) \otimes h(t),$$

where the first term on the right-hand-side of Eq. (1) represents the linear adiabatic chirp induced by the almost instantaneous current-related changes of the equilibrium carrier density, $a_0$ is a constant coefficient, and the second term describes the slower thermal chirp, which changes the frequency as a result of temperature-related changes of the refractive index and physical length of the cavity. The thermal chirp is characterized by the convolution of $i(t)$ with the impulse response $h(t) = \sum a_n e^{-t/\tau_n}$, where the different time constants $\tau_n$ correspond to thermal conductivities of different layers in the DFB laser. Measurements for our DFB laser reveal that the dominant thermal term has a time constant as short as 7.5 ns [9]. As a result, an analysis of both the thermal and adiabatic chirp is necessary to obtain a precise design of the laser spectrum.

As has been shown in Ref. [11], the SBS gain profile that optimizes slow-light performance under various practical constrains is rectangular-shaped with sharp edges and a flat top. Such a gain profile produces longer delays and reduces pulse distortion. This is because the flat gain profile enables uniform amplification over the different frequency components of the data stream, minimizing the filtering effect and thereby reducing pulse distortion [15]. The rectangular-shaped gain profile also improves the delay. Using the Kramers-Kronig relation, the abrupt-edged gain profile increases the phase shift, which leads to a larger group index and longer delays [8]. Because the broadband SBS gain profile $g(\omega_s)$ (where $\omega_s$ is the signal beam frequency) is given by the convolution of the pump spectrum with the intrinsic narrow Lorentzian lineshape [16], a rectangular-shaped pump laser spectrum with a width much greater than the Lorentzian linewidth produces the desired optimal broadband SBS gain profile.
We start the design of the optimal SBS gain profile by only considering the linear adiabatic term in Eq. (1). In this case, the frequency distribution of the DFB laser is the same as that of the current modulation waveform. This is true when the characteristic time scale of the modulation is faster than any of the time constants of the DFB laser. When the thermal chirp is present, the spectral distribution of the noise must be adjusted using an iterative method, as described below.

To generate the optimal rectangular-shaped pump spectrum, we use a noise waveform $V(t) = 2.5 V \times f(t)$, in which $f(t)$ is a random variable approximately uniformly distributed between -0.5 and 0.5 (Fig. 1(a)). The sampling time interval is set to 2.5 ns for our arbitrary wavefunction generator (Tektronix AFG3251). Figure 1(b) shows the probability distribution $P$ of the modulation waveform as a function of the voltage $V$, which is determined from the histogram of the waveform. The spectrum of the pump beam $p(\omega_p)$ is measured by mixing it with a monochromatic reference beam (New Focus Vortex 6029) on a high-speed detector (New Focus Model 1544b), as shown in Fig. 1(c). We see that the generated pump beam spectrum shows significant improvement compared to a Gaussian profile, but is slightly peaked in the center and shows some asymmetry.

The concentration of the spectrum at the center is due to the thermal chirp. In particular, the current of the laser is constantly fluctuating quickly, leading to fluctuations in the temperature about an equilibrium value. According to Eq. (1), a step change in the current $i(t)$ leads to a sudden adiabatic change in the optical frequency $\omega_p(t)$ followed by thermally induced exponential decay to a stationary value. The fast noise-modulation waveform has a rise time $\sim 2.5$
ns, and has many abrupt changes that can be considered as instantaneous jumps (Fig. 1(a)). After such an abrupt change, the laser spends some time returning towards the previous frequency due to the thermal chirp, which favors frequencies in the middle of the range and causes the center-concentration effect.

To compensate for this effect, we increase the probability distribution in the extrema of the noise distribution, using the function $2.5 \times \tanh(b f(t))$. Figure 1(d)-(f) show the waveform $V(t)$, distribution probability $P$, and resultant pump spectrum $p(\omega_p)$ for $b = 10$. We see that the center-concentration problem in the pump spectrum is solved, but there is still an asymmetry in the profile, as seen in Fig. 1(f). This asymmetric frequency response is induced by the nonlinear contribution to the adiabatic chirp (not accounted for in Eq. (1)) and the additional different thermal time constants [9]. To solve this problem, an asymmetry is needed in the distribution of the modulation waveform. We use $2.5 \times \tanh[b(f(t) + c)]$, in which the parameter $c$ controls the asymmetry of the distribution.

The best parameter values for an optimal pump spectrum are obtained applying an iterative scheme. As we change the parameters in small steps, the pump spectrum is recorded and compared to an optimal flat-top spectrum. The error (root mean square deviation RMSD) is calculated at each step. After a small number of iterations, we find the combination of parameters that minimizes the error using a steepest descent search procedure, which gives us the optimal values $b = 10$ and $c = 0.06$. As shown in Fig. 1(i), modulation with the optimal parameters results in a good flat-topped spectrum profile with reasonably sharp edges. The RMSD for this spectral profile is 0.164 mW/GHz, compared to 0.25 mW/GHz for Fig. 1(c) and 0.173 mW/GHz for Fig. 1(f).

A similar procedure is used to generate a slow modulation waveform following Cabrera-Granado’s approach [9]. We start from a 400-kHz periodic triangular waveform and set the amplitude to 2.73 V (Fig. 2(a)). The resultant pump spectrum (Fig. 2(b)) shows a clear asymmetry, which is corrected by introducing a quadratic term in the triangular waveform (Fig. 2(c)) and

![Figure 2](image-url)

Fig. 2. Pump spectral distribution optimization procedure for the case of slow modulation. Modulation waveform $V(t)$ (left column) and measured pump spectrum profile $p(\omega_p)$ (right column) are shown for triangular modulation (upper row), with the addition of a small quadratic term (middle row), and for the optimum waveform (lower row). The DC injection current is 110 mA.
(d)). However, we still observe peaks at the edge of the spectral profile induced by the thermal chirp at the turning points of the waveform. As a result of the thermal chirp, the instantaneous laser frequency spends more time in these regions. These peaks can be corrected by inducing a current “jump” at the turning points, as shown in Fig. 2(e) and (f). The final modulation waveform is expressed as

\[
V(t) = v_{\text{max}} \times \begin{cases} 
   at^2 + (4/T - aT/4)t & \text{if } t < T/4 \\
   at^2 - (4/T + 3T/4)t + 2 + (2aT^2)/4^2 & \text{if } T/4 < t \leq 3T/4 \\
   at^2 + (4/T - a9T/4)t + (5aT^2)/4 - 4 & \text{if } 3T/4 < t \leq T,
\end{cases}
\]

where \( v_{\text{max}} = 2.73 \) V, and \( a = -30.4 \) \( \mu \)s\(^{-2}\). The parameters are optimized using the same error-minimizing iterative procedure. The RMSD for the optimal spectral profile is 0.069 mW/GHz (Fig. 2(f)), compared to 0.083 mW/GHz for Fig. 2(b) and 0.081 mW/GHz for Fig. 2(d).

We then measure the SBS gain profiles produced by the spectral broadened pump beam using the current modulation waveforms depicted in Fig. 1(g) (the “fast” modulation) and Fig. 2(e) (the “slow” modulation). The experiment setup is shown in Fig. 3. To independently measure the SBS gain profile, we use a weak unmodulated monochromatic signal beam (input power \( P_s \)), and record the amplified signal beam power \( P_s \) at the photoreceiver as we slowly scan the frequency of the signal beam. The SBS power gain \( G \) is given by

\[
G = \ln\left(\frac{P_s}{P_{s0}}\right). \tag{3}
\]

The SBS power gain \( G \) is related to \( g(\omega_s) \) by \( G(\omega_s) = g(\omega_s)L_{\text{eff}} \), where \( L_{\text{eff}} = (1 - e^{-\alpha L})/\alpha = 1.64 \) km is the effective length of the fiber, \( L = 2 \) km is the physical length of the fiber and \( \alpha \) (= 0.9 dB/km) is the attenuation coefficient of the fiber.

![Fig. 3. Experiment setup. Spectrally broadened pump and signal beams counter-propagate in the 2-km-long slow light medium (HNLF, OFS Inc.), where they interact via the SBS process. The SBS frequency shift in the NHLF is 9.62 GHz. A fiber Bragg grating (FBG) is used to filter out the Rayleigh backscattering of the pump beam from the amplified and delayed signal pulse sequence before detection. AWG: arbitrary function generator (Tektronix AFG3251), DFB1: 1550-nm DFB laser diode (Sumitomo Electric, STL4416), EDFA: erbium doped fiber amplifier (IPG Photonics EAD 1K), DFB2: 1550-nm DFB laser diode (Fitel FOL15DCWC), MZM: Mach-Zehnder Modulator, PR: 12 GHz photo-receiver (New Focus 1544b), FPC: fiber polarization controllers, CIR: optical circulator.](image-url)
Figure 4(a) shows the measured SBS gain $G$ profiles for the fast and slow modulation methods. As discussed previously, the SBS gain profile is the convolution of the pump spectrum with the intrinsic narrow Lorentzian lineshape. In our case where the pump spectrum bandwidth (5 GHz) is much larger than the narrow Lorentzian linewidth ($\sim$52 MHz in the NHLF), the resultant SBS gain profile is similar to the pump spectrum, as seen in Fig. 4(a). We see that the SBS gain profile is not as sharp on the edges using the fast noise-modulation waveform, which is due to the fluctuating temperature, as discussed above. On the other hand, the slow triangular-like waveform results in a deterministic value of the laser temperature at any moment. Therefore, the frequency of the laser is well-defined at the edge of the modulation waveform. However, this is not true for the fast noise modulation, where the temperature is affected by the previous history of the modulation and thus has wide fluctuations. However, as shown next, the reduced slope of the edges for the fast noise modulation case does not substantially affect its slow light performance.

![Fig. 4. (a) SBS gain profiles for fast (solid black line) and slow modulations (red dashed line) at $P_p = 70$ mW. (b) SBS gain saturation for fast and slow modulation methods. The black solid line shows the SBS gain $G$ for the fast noise modulation, which grows linearly with pump power $P_p$ until saturated. The red dashed line shows the SBS gain $G$ for the slow modulation, which starts to saturate gradually at a much smaller $P_p$ compared to the fast modulation method.](image)

### 3. Slow-light performance

We next compare the delay performance of the fast and slow modulation methods. First, we use a continuous-wave signal beam ($P_s = 48 \, \mu$W) that is tuned to the SBS resonance to measure the line center SBS gain $G$ at different pump powers. Again, $G$ is obtained from Eq. (3). As shown in Fig. 4(b), both modulation formats result in identical linear growth of $G$ with respect to the pump power $P_p$ when it is low. As $P_p$ increases, we see that the slow modulation method results in an early saturation in comparison to the case for the fast modulation waveform. Saturation takes place when the SBS gain $G$ is large enough so that a great portion of the power in the pump beam is transferred into the signal beam, and the exponential amplification of the signal beam cannot be sustained [17].

The early saturation in the slow modulation case is likely due to fluctuations in $G$. The fluctuation in $G$ is related to the uneven frequency swept rate and the end effect. In the slow modulation method, the frequency of the pump beam is slowly swept. During the modulation period of 2.5 $\mu$s, a monochromatic signal beam is only intermittently amplified during the short time period when the pump-probe frequency difference is equal to the SBS frequency shift within the resonance linewidth. An estimate of the average interaction time period gives 52 MHz/5 GHz $\times 2.5 \, \mu$s = 26 ns. On this small time scale, sweep rate fluctuations result from the short thermal constants of the DFB laser can significantly affect the length of the interaction time...
period and give rise to fluctuations in $G$. Moreover, since the SBS amplification process in the slow modulation method is intermittent, there is an end effect that induces more fluctuations in $G$. In our experiment specifically, the frequency of the pump beam as seen by the signal beam goes through a little less than 8 periods of modulation during the whole propagation time ($\sim 9.7$ $\mu$s) through the 2-km-long HNLF. Since the number of modulation periods during the propagation time is not an exact integer, the signal beam can meet the resonant pump frequency for different times (7 or 8), depending on the relative time when we measure the waveform during the modulation period. As a result of both effects, the output signal beam measured at some particular time is amplified more than others and is more likely to saturate the gain. This behavior results in the gradual early saturation seen in Fig. 4(b).

In the fast modulation method, on the other hand, a monochromatic signal is constantly amplified by the frequency-matching component in the broadband pump beam as it travels through the fiber. The output signal amplification results from the accumulated SBS interaction through the whole fiber and has averaged out short-time fluctuations. Therefore, $G$ is uniform and stable in this case. The fluctuation in $G$ for the slow modulation method is the source of the low-frequency fluctuations that degrades the fidelity of a data waveform, as described next.

To measure the delay and fidelity for a data sequence, we use our 5-GHz broadband SBS slow light system to delay a $2^{12}$ bit-long return-to-zero (RZ) binary data sequence. This data sequence contains all $2^8$ 8-bit-long sequences separated by 8-bits 0s serving as a buffer. In this arrangement, the pattern-dependent delay is averaged. The use of an RZ signal is more reliable in situations with pulse broadening effects, but takes twice as much bandwidth to achieve the same data rate compared to the non-RZ coding. A data rate of 2.5 Gb/s is used for the signal to match the SBS slow light bandwidth of 5 GHz (FWHM), where the width of a single pulse is equal to 200 ps. The data sequence is generated by a pattern generator (HP70004A) and encoded on the signal beam via the 10-GHz Mach-Zehnder Modulator (MZM). We use a small signal power of $P_s = 12 \mu W$ and restrict $P_p < 500$ mW to avoid SBS gain saturation. After propagating through the HNLF, the delayed and amplified signal beam is detected by a 12-GHz photoreceiver and recorded on an 8-GHz digital sampling oscilloscope (Agilent DSO80804B). Slow light performance for the fast and slow modulation methods is evaluated by the well-known fidelity metrics of EO and SNR based on the eye-diagram of the output signal at various pump power levels.

We first generate the output eye diagram, which is essentially an overlap of the time domain output traces for a certain number of bit periods. The EO is measured by the maximum difference between the minimum value of high level and the maximum value of the low level in the eye diagram (shown in Fig. 5). The pattern delay is determined by comparing the position of the maximum eye-opening with and without the pump beam. The SNR at the eye-center is

![Fig. 5. Eye diagrams of delayed and amplified data sequences for (a) slow and (b) fast modulation waveforms at $P_p = 350$ mW. The arrows in the figure show the EO for each case.](image-url)
defined as the ratio of the EO with the quadratic mean of the standard deviations (noise) of the high and low levels.

Figure 6(a) shows the measured pattern delay for both the slow and fast pump modulation formats as a function of \( P_p \). Also shown are the theoretically predicted delay (blue short-dash line), assuming a rectangular-like optimized gain profile [10]. Both modulation formats yield the same delay within the measurement error. The measurements also agree well with the theoretical predictions, indicating that the deviation from a perfect flat-top rectangular profile does not substantially degrade the slow light delay.

![Figure 6(a)](image)

**Fig. 6.** (a) Slow light delay and fidelity metrics of (b) EO and (c) SNR for fast (solid black line) and slow (dashed red line) modulation waveforms, as functions of \( P_p \). The theoretically predicted delay for a rectangular-like optimized gain profile is also shown in blue short-dash line in (a).

Figure 6(b) shows the EO and Fig. 6(c) shows the SNR as functions of \( P_p \). As the output signal beam is amplified with increasing \( P_p \), the signal fidelity first increases as the signal beam overtakes the detector dark noise, then decreases when the SBS gain approaches saturation at high pump power, where amplified spontaneous Brillouin scattering begins to dominate [18]. While both modulation methods result in similar trends for signal quality at different pump power levels, the fast noise-modulation method results in better data fidelity over all pump power levels. In particular, Fig. 5 shows an example of the output eye diagrams for both modulation methods at \( P_p = 350 \) mW. Increased EO and SNR for the fast noise modulation is clearly demonstrated. A fractional delay (ratio of the delay with the width of a single pulse) of 0.81 with a SNR of 5.2 is achieved at \( P_p = 350 \) mW for the fast modulation method. Compared to the slow modulation method, the fast modulation method increases the EO by 50% and SNR by 36%, demonstrating significant enhancement of data fidelity with the same delay.

### 4. Conclusion

We have shown that the signal fidelity is significantly improved in a broadband SBS slow light system using noise current modulation of the pump beam spectrum. By controlling the distribution of the noise-modulation waveform, the SBS gain profile is tailored. We obtain an optimal flat-topped gain profile using an asymmetric bi-peak-distributed noise-modulation waveform. Using this new broadband SBS slow light technique, we significantly improve the signal fidelity compared to previous low-frequency slow synthesized waveform modulation methods. Pattern delays up to 1 pulse width is obtained with high fidelity for RZ data rate of 2.5 Gb/s.

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