Giant magnetoelectric effect in magnetic tunnel junctions coupled to an electromagnetic environment

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We study the magnetization dynamics in ferromagnet|insulator|ferromagnet and ferromagnet|insulator|normal metal ultra-small tunnel junctions, and the associated voltage drop in the presence of an electromagnetic environment assisting the tunneling processes. We show that the environment strongly affects the resulting voltage, which becomes a highly non-linear function of the precession cone angle $\theta$. We find that voltages comparable to the driving frequency $\omega$ can be reached even for small precession cone angles $\theta$, in stark contrast to the case where the environment is absent. Such an effect could be useful for the detection local magnetization precessions in textured ferromagnets or, conversely, for probing the environment via the magnetization dynamics.

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I. INTRODUCTION

Magnetic tunnel junctions (MTJs) are usual tunnel junctions where two metallic ferromagnets are separated by a small insulating barrier. In MTJs the tunneling current depends on the relative orientation of the magnetizations of the two ferromagnetic layers which can be controlled by external magnetic fields, by electrical currents or even by voltages. This phenomenon is called tunneling magnetoresistance (TMR) and it is a consequence of the spin-dependent electron tunneling. There is a plethora of applications utilizing this effect such as, for example, magnetic random access memories and magnetic sensors.

Miniaturization lies at the heart of both electronics and spintronics (electronics with spin). The drawback, however, is that the electronic or spintronic elements become more vulnerable to parasitic effects caused by the surrounding noise sources. For example, by reducing the size of a tunnel junction, the surrounding electromagnetic environment becomes manifest, strongly affecting the electronic transport. One such effect is the dynamical Coulomb blockade (DCB), which means the activation of a Coulomb gap at finite voltage due to inelastic tunneling processes assisted by the environment the tunnel junction interacts with. Along with this effect there are many other physical consequences, such as the zero bias anomaly, single-electron tunneling (SET) oscillations, etc, and for more details we refer the reader to Refs. 8 and 11.

Similarly, by reducing the size of a MTJ one expects that Coulomb interaction effects become important in the presence of an environment (there is always the electronics surrounding the MTJ that can act as an environment, or even the intrinsic electron-electron interactions within the material). Even though typical environments are not spin-dependent, they can still affect the spin-dependent transport, and thus quantities such as the magnetoconductance and current induced spintransfer torques. One important application of MTJs is that they can be efficiently used as magnetization detectors: if one of the two magnet is driven at its ferromagnetic resonance, this results in a dc current flowing through the junction which, in the open circuit, translates into a voltage buildup. For example, by scanning the surface of a textured magnet with the help of a spin-polarized STM tip, one can detect the local magnetization dynamics instead of the global one (e.g. rotation of skyrmions, magnetic vortices, magnetic spirals, etc). The disadvantage of such a detection scheme is that although the signal is proportional to the precession frequency $\omega$, it is also proportional to the square of the precession angle (or cone angle) $\theta$, which is typically very small, of about 1-5 degrees. Thus, the conversion of magnetization dynamics into a voltage is rather inefficient, although some experimental evidences have been put forward. There are several proposals on how to increase such a detection scheme by resorting to various nonlinearities, either by using quantum dots.
to explore the (static) Coulomb blockade, or even by using superconductors in order to take advantage of their singular densities of state. In this paper we take a step forward and analyze the original but in the presence of an environment assisting the tunneling processes.

The paper is organized as follows. In Sec. II we introduce the setup and the system Hamiltonian in the presence of the magnetization dynamics. In Sec. III we calculate the electronic tunneling rates and the charge currents flowing through the MTJ due to the precessing magnetization. In Sec. IV we investigate the magnetization induced voltage in the open circuit for two types of environments, namely single-mode and ohmic, respectively. We show that the coupling to the environment leads, in both cases, to a singular behavior in the electronic transport that dramatically enhances the induced voltage. Here, we also discuss the effect of thermal fluctuations on the induced signal, and demonstrate that the singular features persist at low temperatures. Finally, in Sec. V we end up with some conclusions and outlook on the possible utilization of the effect.

II. SYSTEM HAMILTONIAN

In Fig. I we show a sketch of the system under consideration which consist of a spin-polarized STM tip scanning a (dynamical) textured ferromagnet in the presence of inelastic processes. In the following, however, we assume the tip is fixed at some position \( r_{\text{tip}} \), so that \( m(r_{\text{tip}}, t) = m_i(t), \theta(r_{\text{tip}}) = \theta, \) and \( \omega(r_{\text{tip}}) \equiv \omega \), while \( m_{\text{tip}} \equiv m_R \). The Hamiltonian describing the electrons in the the leads (sample and tip) reads:

\[
H_T = \frac{p^2}{2m} + V(r) + \sum_{i=L,R} \frac{\Delta_i}{2} m_i(r, t) \cdot \sigma, \tag{1}
\]

with \( i = L, R \) (left, right) leads, \( m_i(r, t) \) is the unit vector pointing along the instantaneous magnetization direction in lead \( i \). \( V(r) \) includes any electric-field like potentials, including disorder, external electric fields, crystal, etc, and \( \Delta_i \) is the exchange splitting in the lead \( i = L, R \). Note that for a normal right lead (normal metal tip) we have \( \Delta_R = 0 \). The magnetization direction in the left lead read \( m_L(t) = (\cos \omega t \sin \theta, \sin \omega t \sin \theta, \cos \theta) \), namely it precesses at frequency \( \omega \) and cone angle \( \theta \) around the \( \hat{z} \)-axis. The right ferromagnet instead has its magnetization direction pointing along \( z \), i.e. \( m_R = \hat{z} \).

The leads Hamiltonian needs to be supplemented by the tunneling term

\[
H_T = \sum_{kq\sigma\sigma'} T^k_{\sigma\sigma'} c^\dagger_{k\sigma} c_{q\sigma'} \mathcal{A}_e + \text{h.c.}, \tag{2}
\]

where \( k \) and \( q \) (\( q' \)) are the momentum and spin in the left (right) lead respectively, \( T^k_{\sigma\sigma'} \) is the spin-dependent tunneling matrix element, and \( \mathcal{A}_e \) is an operator that changes the number of electrons \( Q \) on the plates of the tunnel junction by one, i.e. its effect can be formally written as \( \mathcal{A}_e Q A^\dagger_e = Q - e \). We assume that the spin-orbit interaction is absent, so that the only spin dependence of the tunneling matrix elements arise because of the finite magnetization in the leads. Assuming that \( T^k_{\sigma\sigma'} \) does not depend on momentum (as all transport happens around the Fermi level), we are left with the following matrix element:

\[
T^k_{\sigma\sigma'} \equiv t(\sigma|\sigma') = t \left( \delta_{\sigma,\sigma'} \cos \theta + \delta_{\sigma,\sigma'} \sin \theta \right), \tag{3}
\]

where, however, the two spin states are represented in a basis corresponding to the right and left leads magnetizations, respectively. We note that the “displacement” operator is given by \( \Lambda_e = e^{i\phi} \), where \( \phi \) is a phase operator which is conjugate with the charge on the capacitor, i.e. \( [Q, \phi] = ie \). The dynamics of the phase \( \phi \) is dictated by the environment the junction is embedded in, and different environments will be discussed later on. For starters, we only assume that the angle \( \phi \) is a dynamical variable.

The electronic transport in the presence of the magnetization dynamics can be easily tackled by resorting to the rotating wave description, meaning the time-dependent setup can be transformed into a static one. Consequently, we can use usual static tunneling description, such as the Fermi’s golden rule, in order to calculate the charge currents. We will forget altogether about any spin-related processes such as spin pumping and spin accumulations since tunneling times are assumed to be much longer than the spin relaxation times in typical ferromagnetic leads. We then perform the following unitary transformation:

\[
H_{ RW}(t) \rightarrow U^\dagger(t) H_{tot}(t) U(t) - i U^\dagger(t) \partial_t U(t) = H_{tot}(0) - (\omega/2) \sigma_z, \tag{4}
\]

where \( H_{tot} = H_F + H_T \), and \( U(t) = \exp(-i\omega t \sigma_z) \), so that we formally eliminated the time-dependence on the left lead. This results in a shift of the energy levels on the right lead by \( \pm \omega/2 \) for spin up (down), while in the left we obtain the following Hamiltonian:

\[
H_L(t) \rightarrow H_L(0) - (\omega/2) \cos \theta \sigma_\parallel. \tag{5}
\]

Note that \( U(t) \) commutes with any charge degree of freedom, and thus this transformation leaves the environment unaffected. In Fig. 2 we show the resulting levels structure in the rotating frame and the fictitious spin splittings in the the two parts of the setup. Let us provide now the physical picture behind this transformation: in the rotating frame there are static spin biases emerging (or spin-motive forces), which can drive charge currents. For that to occur, there should be spin decaying channels in the leads that act as spin sinks on time scales much shorter than the tunneling time, as mentioned already before.

III. TUNNELING RATES AND ELECTRICAL CURRENT

In the tunneling regime, we can compute the electrical current flowing through the junction by using the Fermi’s golden rule. A sketch of all the tunneling processes and the corresponding fictitious voltages that drive electrons over the tunnel barrier are depicted in Fig. 2. To keep the setup as general
as possible, we also assume that an external bias $V$ is applied over the junction (not taken into account in Fig. 2 for simplicity). The rate from the left to the right lead and from spin $\sigma$ to spin $\sigma'$ (with the corresponding quantization axis in each lead) reads:

$$\Gamma_{LR}^{\sigma \sigma'}(V) = D^L_{\sigma} D^R_{\sigma'} \int_{-\infty}^{\infty} d\epsilon' |T_{\sigma \sigma'}(\epsilon')|^2$$

$$\times f(\epsilon) [1 - f(\epsilon' + eV + eV_{\sigma \sigma'})] P(\epsilon - \epsilon')$$

$$= D^L_{\sigma} D^R_{\sigma'} \int_{-\infty}^{\infty} d\epsilon |T_{\sigma \sigma'}(\epsilon')|^2 \frac{1}{1 - e^{-\beta e \epsilon}} P(eV + eV_{\sigma \sigma'} - e),$$

(6)

which indeed corresponds to the result of Tserkovnyak et al. in Ref. [14] for the case equivalent ferromagnets ($P_L = P_R = P$). Note that if the right ferromagnet is substituted with a normal metal ($P_R = 0$) there is no voltage in the open circuit, which was also shown previously: there is no detection possible in a setup of the form $F|LL|N$. This raises the question whether the presence of environment can lead to a non-zero voltage when the right ferromagnet becomes a normal metal. To make this more transparent, it is instructive to compute the current in the closed circuit at $P_R = 0$ instead of the voltage, which reads:

$$I = \Gamma_{tot} P_L \int_{-\infty}^{\infty} d\epsilon \left\{ \cos^2 \left( \frac{\theta}{2} \right) P(V_+ - \epsilon) - P(V_+ - \epsilon) \sin^2 \left( \frac{\theta}{2} \right) \right\}.$$  

(10)

It is easy to see that in the absence of environment this leads to $I = 0$, as expected, but in general this expression is non-zero. This implies that in the presence of environment the magnetization dynamics detection becomes possible even if the second metal is non-magnetic. The physical picture behind such a non-zero current lies in the fact that the environment, through the inelastic processes, introduces an effective energy-dependent density of states which, in the rotating frame, translates the right normal metal effectively into an ferromagnet.
IV. SPECIFIC ENVIRONMENTS

To get a better understanding on the effect of an environment, we assume in the following two particular types of environments, namely a single electromagnetic mode and an ohmic environment, respectively, coupled to the MTJ.

A. Single-mode environment

The single mode environment simply means an LC circuit, with C being the capacitance of the MTJ (for a sample-STM tip capacitance see, for example, Ref. 23) and \( L \) the inductance of the external circuit. The impedance becomes \( Z_0(\omega) = \frac{i\omega}{[\omega^2 + (\omega - i\epsilon)^2]} \), with \( \omega_0 = 1/\sqrt{LC} \), and \( \epsilon \) a small positive number. Such an impedance results in the following distribution function \( P(E) \) for the environment at finite temperature:

\[
P(E) = e^{-\rho \coth(\beta \epsilon) / 2} \sum_{n=-\infty}^{n=\infty} I_n \left( \frac{\rho}{\sinh(\beta \epsilon) / 2} \right) e^{\rho \epsilon / 2} \delta(E - \epsilon n \omega_0),
\]

where \( \rho = (\pi/\omega_0 CR_0) = E_c/\omega_0 \) is a dimensionless parameter that quantifies the strength of the DCB, i.e. the charging effects versus the environmental excitation energies (here \( E_c = e^2/2C \), \( \beta = 1/k_BT \), and \( I_n(\chi) \) is the modified Bessel function of the first kind. While we cannot extract any analytical expressions for the induced voltage in this case, in Fig. 3 we plot the resulting voltage \( V \) as a function of \( \rho \) by solving the equation \( J = 0 \) for the current in Eq. (8), and using the expression for \( P(E) \) at \( T = 0 \).

The environment strongly affects the induced voltage, and gives rise to a non-monotonic behavior as a function of \( \rho \). This is increased for \( P_R = 0 \) as compared to \( P_L = P_R \), reaching values of the order of \( \omega \) itself (all energies are expressed in terms of \( \omega \)). We mention that this turns out to be the opposite for precessions around \( \theta = \pi \), as one can see from the left plot in Fig. 4. The reason for such a different behavior lies in the fact that the environment affects the spin-dependent density of states \( D_{\uparrow} \) and \( D_{\downarrow} \) by increasing (decreasing) their difference for \( \theta = \pi \) (\( \theta = 0 \)). More importantly, the environment pertains to large values of \( V \) at very small \( \theta \), as seen from Fig. 4, in total contrast to the environment-free case. Such a surprising feature could be very useful in detection of small-angle magnetization dynamics precession without the need of any reference ferromagnet.

Next we discuss briefly the influence of thermal fluctuations. At finite temperatures the effect of the environment is diminished, as depicted in Fig. 5. For temperatures \( T \ll \omega \) the voltage remains rather unaffected, but as the temperature is increased further, the voltage is decreased (increased) in the zero polarized lead case \( P_R = 0 \) (equally polarized leads case \( P_R = P_L \)). Such a behavior is simply due to the fact that thermal excitations wash out the singular spin-polarized density of states induced by the environment.
B. Ohmic environment

As the next example, let us analyze the MTJ in the presence of an Ohmic environment. For such a case, the impedance reads

\[
\frac{\text{Re}[Z(\omega)]}{R_K} = \frac{1}{g} \frac{1}{1 + (\omega/\omega_R)^2},
\]

(12)

where \( g = R_K/R_c \) and \( \omega_R = 1/RC \equiv (g/\pi)E_c \). At finite temperatures, we can write the full correlation function in Eq. (7) as

\[
J(t) = J_q(t) + J_b(t),
\]

with \( J_q(t) \) and \( J_b(t) \) being the quantum (or the magnetic) and thermal contributions, respectively. Here we are interested in the behavior of the junction at energies well below the charging energy \( E_c \), where possible zero-bias anomalies are manifesting. This allows us to consider only the long time limit \( t \to \infty \) characteristic of the correlation function \( J(t) \). More specifically, we assume \( \omega_R t \gg 1 \), which leads to the following expressions:

\[
J_q(t) \approx \frac{2}{g} \left[ \log (\omega_R t) + i \frac{\pi}{2} + \gamma \right],
\]

(13)

\[
J_b(t) \approx \frac{2}{g} \log \left( \frac{\pi \theta}{\sinh (\pi \theta)} \right),
\]

(14)

with \( \gamma = 0.577 \) being the Euler constant. We note that for \( T t \gg 1 \), the thermal contribution becomes \( J_b(t) \approx -\pi T t/8g \), while at short times \( T t \ll 1 \) (but still with \( \omega_R t \gg 1 \)), the correlation function depends quadratically on time, i.e.

\[
J_b(t) \approx -\pi T t^2/8g. \]

The full correlation function \( J(t) \) contains to an exact analytical expression for the \( P(E) \) function defined after Eq. (6), and which characterizes the probability to excite the environment at energy \( E \). However, we will not show the full expression since it is too lengthy to be displayed. Instead, we depict the \( T = 0 \) expression for \( P(E) \), which reads:

\[
P(E) = \frac{e^{-2g/\pi}}{\Gamma(2/g)^2 \pi / g} \left( \frac{E}{g} \right)^{1/2} E_c \]

(15)

\( \Gamma(x) \) being the Gamma function.

Similarly to the the single-mode case, to find the voltage induced by the magnetization dynamics we use Eq. (15) and solve the equation \( I = 0 \) valid for the open circuit. In Fig. 6 we plot the resulting voltage at \( T = 0 \) [using Eq. (15)] as a function of the Ohmic parameter \( g \) and for several polarizations of the right lead \( P_R \), assuming a precession cone angle \( \theta = \pi/10 \). We see that the voltage is non-monotonic as a function of the Ohmic parameter \( g \), reaching a maximum around \( g \approx 1 \) (or \( R \approx R_K \)). Moreover, the voltage decreases with increasing the polarization \( P_R \) of the right lead, meaning that the detection scheme in the presence of the environment is more efficient with a normal metal as a detector instead of a ferromagnet as in the original setup.[14]

In Fig. 7 we plot the \( T = 0 \) voltage as a function of the cone angle \( \theta \) for several values of the Ohmic coupling parameter \( g \). \( P_R = 0 \) (left plot) and \( P_R = P_L \) (right plot). Similarly to the previous case, the voltage reaches values of the order \( \omega \) close to \( \theta = 0 \), again in stark contrast to the environment-free case. Note that the absence of the environment corresponds to \( g \to \infty \), in which case the voltage is zero at \( P_R = 0 \). While the features are very similar to the single-mode environment, this case allows us to extract analytical expressions for the induced voltage, in the limit of small precession angles \( \theta \). For the case of a \( F/I/N \) structure, the polarization of the right lead is \( P_R \equiv 0 \), and we find the following asymptotic expressions (\( V \) is expressed in units of \( \omega \)):

\[
V = \left\{ \begin{array}{ll} 
-\frac{4.25P_L \sin^2 (\theta/2)}{g}, & \text{for } g \to \infty \\
-gP_L, & \text{for } g \to 0
\end{array} \right.
\]

(16)

meaning that the voltage approaches zero as \( 1/g \) as the environment strength is diminished. For a strong environment coupling \( (g \to 0) \), the voltage increases linearly with \( g \), and becomes independent of the angle \( \theta \). Such a behavior, however, is only valid for finite cone angles \( \theta \), while for \( \theta \to 0 \) the
FIG. 8. The amplification function $r$ as a function of the ohmic parameter $g$ and the right lead polarization $P_R$, for a precession cone angle $\theta = \pi/10$ and at $T = 0$. In blue it is depicted the region for which $|r| > 1$, while in light blue we show the region for which $|r| < 1$. Note that the amplification factor $r$ can be both positive and negative over a wide range of parameters.

Next we characterize the voltage gain in the presence of the environment compared to the environment-free case. For that, we define the amplification factor $r$ as:

$$r = \frac{V(g)}{V(\infty)},$$

where $V(\infty)$ is the voltage in the absence of environment in Eq. (9). In Fig. 8 we plot $r$ as a function of $g$ and $P_R$ for a precession cone angle $\theta = \pi/10$. We see that $|r| > 1$, or even $|r| \gg 1$, for a large range of parameters, and thus the detection scheme improves substantially in the presence of environment. Moreover, the amplification factor $r$ can run over both positive and negative values, meaning the voltage can reverse sign, a feature associated again with the effective ferromagnetic density of states induced by environment.

As in the previous case, the thermal fluctuations are expected to smear out the sharp features induced by the coupling to the environment. However, for small enough temperatures so that $T \ll \omega$, the main features remain visible, as shown in Fig. 9. There, we plot the induced voltage as a function of temperature for different ohmic parameters $g$. More specifically, in the main left plot we show the result for $P_R = 0$, while in the main right plot we depict the result for $P_R = P_L$. We mention that in the first case the voltage vanishes as the temperature is increased, while in the second case the voltage reaches the environment-free value for large temperatures, as the singular features are washed out by the thermal fluctuations. In the insets we show the angular dependence of the induced voltage for different temperatures $T$: the black, blue, red, and green curves correspond to $T = 0, 0.1, 0.3$, and 0.5, respectively.

FIG. 9. The voltage as a function of temperature $T$ and angle $\theta$ for a normal metal right lead (left plot) and a ferromagnetic right lead (right plot) for an ohmic environment. The black, blue, red, and green curves correspond to $\theta$ for $g = 3, 5, 10$, respectively. In the insets we plot the angular dependence of the induced voltage for different temperatures $T$: the black, blue, red, and green curves correspond to $T = 0, 0.1, 0.3$, and 0.5, respectively.

voltage vanishes as expected (and as shown in Fig. 7 where the exact expression is plotted). Note that the voltage around $\theta = \pi$ is identical to the $\pi = 0$, but with opposite sign. In the limit of identical ferromagnets on both sides ($P_L = P_R \equiv P$), we obtain

$$V = \begin{cases} 
\frac{2P \sin^2(\theta/2)}{1 + P^2} \left( -\frac{2P \sin^2(\theta/2)}{1 - P^2} \right), & \text{for } g \to \infty \\
\frac{gP}{1 - P^2} \sin^{1/2}(\theta/2) \left( -\frac{gP}{1 + P^2} \right), & \text{for } g \to 0
\end{cases}$$

(17)
corresponding to angles $\theta \approx 0$, while the expression in the brackets represents the expansions around $\theta \approx \pi$. We see that for $\theta \approx 0$ ($\theta \approx \pi$) the voltage is strongly reduced (enhanced) compared to its bare values in the absence of the environment ($g \to \infty$). As before, such a behavior is again due to the effective environmental density of states which tends to reduce (enhance) the difference between $D_L$ and $D_L$ around $\theta = 0$ ($\theta = \pi$).

While the density of states modification by the environment offers an explanation for the non-zero voltage in the $F/I/N$ case, it does not explain why this voltage reaches a maximum comparable to $\omega$ around $\theta = 0$ (or $\theta = \pi$). For a qualitative explanation, we make use of the level structure and electronic transitions depicted in Fig. 2. We see that the transitions are between energy levels separated by $\delta E = \omega(1 \pm \cos \theta)$, which means the environment is interrogated (through the $P(E)$ function) at these two energy scales. When $\theta \to 0$ (or $\theta \to \pi$), the environment is probed at both $E \approx \omega$ and $E \approx 0$. Close to $E \approx 0$, the zero bias anomaly sets in, which reflects a very resistive environment and thus some of the channels for the back-flow charge currents are highly inhibited, leading to an amplification of the voltage.
Finally, let us give some realistic estimates for the induced voltage based on numbers utilized for observing the magnetization dynamics. For example, in Ref. [24] it was reported that $Z_c(\omega) \approx R \sim R_g$ up to frequencies of the order $\omega \sim 1$ GHz, $C \approx 2$ fF, which translates to $E_C \approx 10^{-4}$ eV, and $T = 25$ mK, so that $E_C, \omega \gg k_B T$. These numbers give $g \sim 1$ and lead for a large value of the induced voltage, $eV \approx 0.2 \hbar \omega$. More conservative numbers, such as those in Ref. [26] (tunnel junction) and Ref. [27] (Josephson junction) lead to values of $g$ between $g = 0.1$ and $g = 0.4$, which in turn pertains to a voltage $eV \approx 0.01 \sim 0.15 \hbar \omega$ at small precession angles $\theta = \pi/10$ and for a normal metal as a right lead (the result is $eV = 0$ in the absence of environment in such a case).

V. CONCLUSIONS

In this paper we studied the magnetization dynamics induced voltage in an ultra-small magnetic tunnel junction. We show that in the presence of an electromagnetic environment the electronic transport shows a singular behavior which in turn affects dramatically the induced voltage characteristic. More specifically, we find that the voltage pertaining to the magnetization dynamics can be comparable to the precession frequency $\omega$ even for small precessions angles $\theta \sim 0$, being in stark contrast with behavior of a large MTJ where such a voltage scales as $V \propto \sin^2 \theta$. Moreover, the resulting voltage is finite even when the reference ferromagnet becomes a simple metal, lifting the requirement of using ferromagnets for detection.

The above findings could be extremely useful in view of magnetization dynamics applications. It could provide the means for detecting the magnetization dynamics, for example, on the surface of a 2D ferromagnet by usual STM technique without the need for a spin polarized reference (i.e. spin polarized tip). Turning the tables, the small-angle magnetic dynamics can serve as a nonintrusive spectroscopic probe of the environment itself. By addressing the voltage as a function of $\omega$ one can characterize the nonlinear properties of the environment, possibly even prepared in some given state, or characterize the tunneling into the many-body system itself.

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