Universal optical line terminal encoding and decoding architecture in two-code keying for noncoherent spectral amplitude coding optical code division multiple access systems

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Abstract. We propose a new code family, called extended shifted prime codes, and the universal encoding architecture for spectral amplitude coding optical code division multiple access systems using a two-code keying scheme. The proposed system can eliminate multiuser interference and suppress phase-induced intensity noise. In addition, we design the ESP codes to be an encoding/decoding architecture based on the array waveguide grating architecture and reduce the power loss and the complexity of the optical line terminal. The numerical results demonstrate that the proposed system with ESP codes outperforms the existing one-dimensional shifted prime codes system.© The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.OE.53.1.016104]

Keywords: array waveguide grating; optical code division multiple access; phase-induced intensity noise; passive optical network; shifted prime codes.

Paper 130750 received May 21, 2013; revised manuscript received Nov. 24, 2013; accepted for publication Dec. 6, 2013; published online Jan. 6, 2014.

1 Introduction

Optical code division multiple access (OCDMA) can provide high-speed connections with bandwidth sharing and secure communications in next-generation optical access networks. Spectral amplitude coding (SAC) in OCDMA systems has been exploited in the optical networking units of passive optical networks (PONs). However, in the on-off keying, the codewords are unidimensional and require the codewords power of bit “1” and the zero codewords power of bit “0” to control the unequal power to accommodate more simultaneous users in PONs. The codewords in two-code keying (TCK) are a better event because the codewords power of bit “1” and the codewords power of bit “0” control the equal power. In addition, the performance of OCDMA systems is limited by the multiuser interference (MUI). To address this issue, shifted prime (SP) codes with TCK are proposed to remove MUI. In this letter, we propose extended shifted prime (ESP) codes with TCK to further reduce the phase-induced intensity noise (PIIN) and support more simultaneous users. The variance of PIIN current is effectively reduced by employing the proposed ESP codes. We also propose a novel array waveguide grating (AWG) architecture to decrease the power loss and complexity of the optical line terminal (OLT).

In the following sections, we first review the SP codes. The SP codes are designed to eliminate MUI without chip stuffing of the codes. A code sequence of the SP code is denoted as $C_{m,n} = \{c_{m,n}(0), c_{m,n}(1), \ldots, c_{m,n}(p^2-1)\}$, where $m = 0, 1, \ldots, p-1, n = 0, 1, \ldots, p-1$, and $C_{m,n} \in \mathbb{F}_p$. The $p^2$ represents the set of all $p$-tuples over GF($p$). The corresponding codeword is denoted as $X_{m,n} = [x_{m,n}(0), x_{m,n}(1), \ldots, x_{m,n}(p^2-1)]$. Therein, we set $x_{m,n}(i) = 1$ as $i = c_{m,n}(b) + bp$ and $b = 0, 1, \ldots, p-1$, where $c_{m,n}(b) = m \cdot b \oplus n$. Otherwise, $x_{m,n}(i) = 0$. The $\cdot$ and $\oplus$ are the modulo-$p$ multiplication and addition, respectively. The codewords $X_{m,n}$ with the same value $m$ belong to the same code group. The cross-correlations between the two SP codewords $X_{m,n}$ and $X_{q,r}$ are $X_{m,n} \otimes X_{q,r} = p$ as $m = q, n = r$, $X_{m,n} \otimes X_{q,r} = 0$ as $m \neq q, n \neq r$, or $X_{m,n} \otimes X_{q,r} = 1$ as $m \neq q, n \neq r$, where $\otimes$ is the dot product of two vectors.

2 1-D ESP Codes with TCK

In the letter, we design ESP codes to reduce PIIN and increase the number of simultaneous users. Specifically, we describe the ESP codes as follows: $x_{e,m,n}(j) = 1$, for $j = (e-1)p + c_{e,m,n}(b) + bNp$, $b = 0, 1, \ldots, p-1$; otherwise, $x_{e,m,n}(j) = 0$, where $e \in \{1, 2, \ldots, N\}$. The code weight is $p$, the code length is $Np^2$, the number of codewords is $M = Np^2$, and the code size is $M = N/(p^2 - p)/2$. Table 1 uses an example with $N = 2, p = 3, M = 18$, and $M = 6$. The cross-correlations of the ESP codes are specified as follows: $X_{e,m,n} \otimes X_{f,q,r} = p$ as $e = f, m = q, n = r$, $X_{e,m,n} \otimes X_{f,q,r} = 0$ as $e \neq f, m = q, n \neq r$, or $X_{e,m,n} \otimes X_{f,q,r} = 1$ as $e \neq f, m \neq q$. Moreover, we let any two codewords $(X_{e,m,n}$ and $X_{e,m,n})$, which belong to the same code group, assigned to the same user for TCK. It is set as $X_{e,m,n} = X_{e,m,n+1}$ in this letter. Table 1 uses a codeword $X_{e,m,n}$ or $X_{e,m,n}$ as the encoding of information bit “0” or “1”. The modified cross correlations in ESP codes for TCK are derived as follows:
Table 1 Extended shifted prime (ESP) codes for $N = 2$, code weight $p = 3$, and code size $M_s = 6$.

| $e$ | $m$ | $n$ | $X_{e,m,n}$ |
|-----|-----|-----|-------------|
| 1   | 0   | 0   | 100 000 100 000 100 000 |
| 1   | 0   | 1   | 010 000 010 000 100 000 |
| 1   | 0   | 2   | 001 000 001 000 001 000 |
| 1   | 1   | 0   | 100 000 010 000 001 000 |
| 1   | 1   | 1   | 010 000 001 000 100 000 |
| 1   | 1   | 2   | 001 000 100 000 010 000 |
| 1   | 2   | 0   | 100 000 001 000 100 000 |
| 1   | 2   | 1   | 010 000 100 000 010 000 |
| 1   | 2   | 2   | 001 000 010 000 100 000 |
| 2   | 0   | 0   | 000 100 000 100 000 100 |
| 2   | 0   | 1   | 000 010 000 010 000 010 |
| 2   | 0   | 2   | 000 001 000 001 000 001 |
| 2   | 1   | 0   | 000 100 000 100 000 001 |
| 2   | 1   | 1   | 000 010 000 001 100 000 |
| 2   | 1   | 2   | 000 001 100 000 010 000 |
| 2   | 2   | 0   | 000 100 000 010 000 010 |
| 2   | 2   | 1   | 000 010 000 100 000 001 |
| 2   | 2   | 2   | 000 001 000 010 000 100 |

$$X_{e,m,n} \odot X_{f,q,r} \cdot X_{e,m,n} \odot X_{f,q,r}$$

$$= \begin{cases} p, & e = f, m = q, n = r, \\ -p, & e = f, m = q, n = r, \\ 0, & \text{otherwise}. \end{cases}$$

The proposed transmitter encodes ESP codes in the electrical domain, the same as the literature, and it has been shown that the OLT can transfer the electrical domain into the optical domain.\(^{12}\)

In Fig. 2, the modulation voltage $V_m$ is the input of EOM, and the optical transmitted intensity $I_n$ is the output of the EOM, where the optical transmitted intensity $I_n = I_{n0} + \psi V_m$. If $V_m = 0$, the optical transmitted intensity
is $I_{00}$. The EOM transfers the modulation voltage $V_m$ into optical transmitted intensity $I_m$. Therefore, the ratio of transmission factor is $\gamma = I_m/V_m$. Figure 2 presents the transformation from the electrical domain to optical domain with the environment described in Table 1, where $N = 2$ in ESP codes with the code weight $p = 3$ and the code size $M = 6$.

We first describe the matrix operation circuit in the electrical domain with $H = 1/p \times S \times \text{BIT}$, where $H = [h_0, h_1, \ldots, h_{M-1}]^T$, $S = [X^T_{1,0,0}, X^T_{1,0,1}, \ldots, X^T_{N,p-1,p-1}, X^T_{N,p-1,p-2}]$, and $\text{BIT} = [\text{bit}_0, \text{bit}_1, \ldots, \text{bit}_{M-1}, \text{bit}_{M-1}]^T$. The codes are then transformed to the waveform as follows. Let $h_0$ denote the element of $H$. If code $X_{1,0,0}$ is transmitted and $\text{bit}_0$ is 1, $h_0$ is 1/3. In contrast, if the codes $X_{1,0,0}$ and $X_{1,1,0}$ are transmitted and $\text{bit}_0$ is 1, $h_0$ will be 2/3. If the codes $X_{1,0,0}$, $X_{1,1,0}$, and $X_{1,2,0}$ are transmitted and $\text{bit}_0$ is 1, $h_0$ becomes 1. If the codes without $X_{1,0,0}$, $X_{1,1,0}$, and $X_{1,2,0}$ are transmitted and $\text{bit}_0$ is 1, $h_0$ is 0. Let $V_{m,max}$ denote the maximum value of modulation voltage $V_m$. Afterward, $h_1$ is included in the voltage setting in the transformation to the waveform, i.e., $V_m = -V_{m,max} + 2V_{m,max}h_1$.

Figure 3 shows the receiver structure of the proposed ONU($\tau$) with ESP codes for TCK in an OCDMA system. The ONU($\tau$) comprises two sets of fiber Bragg gratings (FBGs), one balanced detector, and an integrator. The two FBG sets are constructed based on the codewords $X_{e,m,n}$ and $X_{e,m,n'}$. The upper output part is connected to the input part of the photodetector (PD) as PD0, and the lower output part is connected to the input part of PD1. The balanced detector is connected to an integrator. The two cross-correlation results $X_{e,m,n} \odot X_{f,q,r}$ and $X_{e,m,n'} \odot X_{f,q,r}$ lead to the output of PD0s 0 to 1 in the balanced detector.

The principles of the FBG-based decoder are based on the cross-correlation described as in Eq. (1). The code sequences $X_{f,q,r}$ are first received by the FBG-based decoder. Then, the signature code $X_{e,m,n}$ achieves the modified cross correlation as shown in Fig. 3. The input of the correlator $r_1$ represents the spectral components. The first output of the correlator $r_1$ is connected to the FBG for the code sequence $X_{e,m,n'}$. The second output of the correlator $r_1$ is connected to the PD1. The spectral components with the FBG for the code sequence $X_{e,m,n'}$ are reflected back toward the PD1 to obtain the photocurrent $I_{1,bit=0}$. The other spectral components are passed through the FBG for the code sequence $X_{e,m,n}$.

The other spectral components are connected to the correlator $r_0$. The first output of the correlator $r_0$ is connected to the FBG for the code sequence $X_{e,m,n}$. The second output of the correlator $r_0$ is connected to the PD0. The spectral components with the FBG for the code sequence $X_{e,m,n}$ are reflected back toward the PD0 to acquire the photocurrent $I_{0,bit=1}$. The other spectral components are passed through the FBG for the code sequence $X_{e,m,n}$. The average photocurrent is $I_{1,bit=0} = I_{0,bit=0} - I_{1,bit=0}$ and $I_{1,bit=1} = I_{0,bit=1} - I_{1,bit=1}$ corresponding to Eq. (1). Therefore, the principles of the FBG-based decoder are based on the cross-correlation.

Moreover, we eliminate the MUI with Eq. (1) according to the difference between the two correlations. Now, Table 2 compares the optical power budget for the conventional OLT using SP codes and the proposed OLT. Since the proposed OLT does not include splitter and combiner, which generally have high insertion loss, the power loss of the proposed OLT is much smaller than that of the conventional ones. This replaceable word is the insertion loss of A. The insertion loss of AWG is 3 dB according to the existing work. By contrast, the insertion losses in this paper are improved to 5 dB for the 1 x 49 AWG multiplexer and 5 dB for the 49 x 1 AWG demultiplexer, respectively. The total insertion loss is 10 dB. This replaceable word is the insertion loss of B and insertion

![Fig. 2](https://www.spiedigitallibrary.org/journals/Optical-Engineering/2014/53(1)/16104-3/Images/Fig_02.png)  
**Fig. 2** The modulation voltage versus the optical transmitted intensity of the electro-optic modulator (EOM).

![Fig. 3](https://www.spiedigitallibrary.org/journals/Optical-Engineering/2014/53(1)/16104-3/Images/Fig_03.png)  
**Fig. 3** The receiver structures of the ESP codes for TCK in an optical network unit (OUN, $\tau$).

### Table 2: Comparison of optical power budgets for conventional OLT with SP codes and proposed OLT with ESP codes.

| Items | Code W | n | Optical PB (Ref. 6) | n | Optical PB |
|-------|--------|---|---------------------|---|------------|
| Code W | $p = 7$ |  | $p = 7$ |
| Ins. A | 0 | 0 dB | 1 | 10 dB |
| Ins. EOM | 0 | 0 dB | 1 | 2 dB |
| Ins. B | 1 | 4 dB | 0 | 0 dB |
| Ins. C | 1 | 4 dB | 0 | 0 dB |
| Ins. D | 1 | 0.9 dB | 0 | 0 dB |
| Ins. E | 1 | 11 dB | 0 | 0 dB |
| Ins. F | 1 | 11 dB | 0 | 0 dB |
| Total | 30.9 dB | 12 dB |

Note: Optical PB: Optical Power Budget; Code W: Code Weight; Insertion loss of: Ins.; A: 1 x 49 and 49 x 1 AWG (DE)MUX; B: 1 x 7 Coarse AWG; C: 7 x 7 Fine AWG; D: 2 x 1 Optical Switch; E: 1 x 7 Splitter; F: 7 x 1 Combiner.
loss of C. The insertion loss of AWG is 3 dB according to the literature.14 The insertion loss of 7 × 7 AWG is 2.4 dB according to the literature.15 By contrast, the insertion losses in this paper are improved to 4 dB for the 1 × 7 coarse AWG multiplexer and 4 dB for the 7 × 7 fine AWG, respectively. This replaceable word is the insertion loss of D. The insertion loss of the optical switch is 0.7 dB according to the literature.16 By contrast, the insertion losses in this paper are improved to 0.9 dB for the optical switch. This replaceable word is the insertion loss of E and insertion loss of F. The insertion loss of the optical splitter (and optical combiner) is 11 dB according to the Ref. 17. Therefore, the insertion loss is 11 dB for the optical splitter (and optical combiner). This replaceable word is the insertion loss of EOM. The insertion loss of the EOM is 1.2 dB according to the existing work.18 By contrast, the insertion loss in this paper is improved to 2 dB for the EOM. The power budget difference will be increased with the value of p. Therefore, as p = 7, the optical power budget (dB) decreases from 30.9 dB in the SP codes in Ref. 6 to 12 dB in the proposed OLT.

3 System Performance

We first describe the signal-to-noise ratio (SNR) and bit error rate (BER) of the proposed scheme. The photocurrent noise variances are derived according to independent noise variances, i.e., $<i_{\text{noise,bit}=0}^2> + <i_{\text{PIN,bit}=0}^2> + <i_{\text{shot,bit}=0}^2> + <i_{\text{thermal,bit}=0}^2> = <i_{\text{shot,bit}=1}^2> + <i_{\text{shot,bit}=1}^2> + <i_{\text{thermal,bit}=1}^2>$. Therefore, the average photocurrents in the received signals are $I_{0,\text{bit}=0} = I_{1,\text{bit}=0} = I_{0,\text{bit}=1} = I_{1,\text{bit}=1}$. Note that the cross-correlation between $X_{1,0,0}$ and $X_{f,q,r}$ corresponds to the cross-correlation of the PD current $I_{0,\text{bit}=0}$ and $I_{1,\text{bit}=0}$, with information bit = “x”. Therefore, if the information bit is “0,” the two cross-correlations are $I_{0,\text{bit}=0}$ and $I_{1,\text{bit}=0}$. If the information bit is “1,” the two cross-correlations are $I_{0,\text{bit}=1}$ and $I_{1,\text{bit}=1}$. Before obtaining $\text{SNR}_{\text{bit}=0}$ and $\text{SNR}_{\text{bit}=1}$, and BER, below we first derive the number of type-I simultaneous users, probability density function of the cross-correlation value, total cross-correlation, auto-correlation, and photocurrent noise variances.

First, we derive the number of type-I simultaneous users. Let $W$ denote the number of simultaneous users, and we randomly choose one of them as the major simultaneous user, which selects $X_{1,0,0}$ code, whereas other ($W - 1$) simultaneous users will select other codes. The number of type-I simultaneous users is $[(W - 1)/N]$ because $[(W - 1) - (W - 1)/N]$ simultaneous users have the cross-correlation as “0.”

Second, we derive the probability density function of the cross-correlation value with “1” and “0.” The code weight is $p$, and $p$ is odd. ($p-1$) is the even because we adopt ($p-1$) divided by 2 from the TCK, and the remainder is zero. The code size is $M_p = N(p^2 - p)/2$ in TCK. The probability density function of the cross-correlation value with “0” is $[p - 1]/(p^2 - p)/2 - 1 - (p-1)/2 - 1]$. The probability density function of the cross-correlation value with “1” is $[1 - (p-1)/2 - 1]/(p^2 - p)/2 - 1]$. Third, we derive the total cross-correlation. Before the derivation of the PD current, the total cross-correlation is $\lambda = [(W - 1)/N] - [(W - 1)/N]/(p - 1)/(p^2 - p)/2 - 2$, where the cross-correlation value is “0” and “1,” the number of type-I simultaneous users is $[(W - 1)/N]$, and the probability density function of the cross-correlation value is set with “0” and “1.”

Fourth, we derive the auto-cross correlation. ($p + \lambda$) is the auto-cross correlation adding to the total cross-correlation. The code length ($Np^2$) is incorporated in ($p + \lambda$)/($Np^2$). The average photocurrents $I_{0,\text{bit}=0} = I_{1,\text{bit}=0}$, $I_{0,\text{bit}=1}$, and $I_{1,\text{bit}=1}$ are originated as follows. For information bit = “0” we develop $I_{0,\text{bit}=0}$ and $I_{1,\text{bit}=0}$ as $I_{0,\text{bit}=0} = R_Ps\sqrt{p + \lambda}/(Np^2)$ and $I_{1,\text{bit}=0} = R_PS_{\text{sr}}\sqrt{\lambda}/(Np^2)$. For information bit = “1” we develop $I_{0,\text{bit}=1}$ and $I_{1,\text{bit}=1}$ as $I_{0,\text{bit}=1} = R_Ps\sqrt{\lambda}/(Np^2)$ and $I_{1,\text{bit}=1} = R_Ps\sqrt{p + \lambda}/(Np^2)$. As the information bit = “0” and “1,” the average photocurrent is as follows:

$$I_{r,\text{bit}=0} = I_{0,\text{bit}=0} - I_{1,\text{bit}=0} = R_Ps/(Np)$$
$$I_{r,\text{bit}=1} = I_{0,\text{bit}=1} - I_{1,\text{bit}=1} = -R_Ps/(Np),$$

Therefore, the BER is obtained as $\text{BER} = \text{erfc}(\sqrt{SNR_{\text{bit}=0}/SNR_{\text{bit}=1}}/2)/2^6$. Moreover, the variance of the thermal noise current is as:

$$<i_{\text{thermal,bit}=0}^2> = <i_{\text{thermal,bit}=1}^2> = 4K_bT_bR_L.$$
4 Conclusion
We propose ESP codes and demonstrate that the effects of PIIN are effectively suppressed. Compared with the existing SP codes, our numerical results show that ESP codes can effectively increase the number of simultaneous users under 2.5-Gbps data transmission. Moreover, a universal OLT encoding architecture can be operated with other code families. Then, we also devise a AWG architecture for ESP codes to reduce the power loss and the complexity for OLT in PONs.

Acknowledgments
The authors wish to thank the High Speed Intelligent Communication (HSIC) Research Center at the Chang Gung University, Taiwan, for providing facilities and financial support which were crucial to our study.

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