LOGICAL RECOGNITION TREE CONSTRUCTION ON THE BASIS OF A STEP-TO-STEP ELEMENTARY ATTRIBUTE SELECTION

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ABSTRACT

Context. A general problem of constructing logical recognition/classification trees has been analyzed. Logical classification trees are the object of the present study. The subject of the study are the relevant methods and algorithms of logical classification trees.

Objective. The goal of this work is to develop a simple and efficient method of constructing logical tree-like models on the basis of classification trees for training discrete information selection characterized by a structure of constructed logical classification trees from elementary attributes estimated on the basis of their informativeness calculation functional.

Method. A general method of constructing logical classification trees is suggested that constructs a tree-like structure for a given initial training selection comprising a set of elementary attributes estimated at each step of constructing a model according to the above selection. In other words, a method of constructing logical classification trees is suggested with the main idea of approximating the initial selection of an arbitrary volume by the elementary attribute set. This method during the current logical tree (node) vertex formation provides selecting the most informative (high-quality) elementary attributes from the initial set. Such approach at constructing the resulting classification tree allows one to reduce essentially the tree size and complexity (i.e. the total number of branches and structural layers) and increase the quality of its further analysis (interpretability). The method of constructing logical classification trees suggested by us enables one to construct the tree-like models for a wide class of artificial intellect theory problems.

Results. The method developed and presented in this work has received a software realization and was studied when solving a problem of classifying the geological type data characterized by a large-dimension attribute space.

Conclusions. Experiments carried out in this work have confirmed the efficiency of the software suggested and demonstrate the possibility of its use for solving a wide spectrum of applied recognition and classification problems. The outlook of the further studies may be related to creating a limited method of logical classification tree by introducing the stopping criterion for the logical tree construction procedure according to the structure depth, its program realization optimization, as well as to the experimental study of this method in a wider circle of applied problems.

KEYWORDS: logical classification tree, image recognition, classification, attribute, branching criterion.

ABBREVIATIONS

TS – training selection;
ST – test selection;
RS – recognition system;
IR – image recognition;
RF – recognition function;
LCT – logical classification tree;
ACT – algorithmic classification tree;
BAS – branched attribute selection.

NOMENCLATURE

G is a certain initial signal set;
R is a certain partition into the classes \( H_i \) preset on the initial set \( G \);
\( W(f) \) is a generalized attribute \( f \) information quality value;
\( f_i \) is a certain fixed generalized attribute;
\( f_R \) is a recognition function;
\( x_i \) are the initial TS discrete objects;
\( b_i \) is a total number of the TS sets, where a certain elementary attribute \( \varphi \) takes the value \( i \).
\( q_i^m \) is a total number of the TS sets, where a certain elementary attribute \( \varphi \) takes the value \( i \) given \( f_R(x) = m \);
\( H_i \) is a set of images (classes) set by the initial TS;
\( (x_i, f_R(x_i)) \) are the training pairs of the initial TS;
\( d_i \) are the ACT constructing stages;
\( r_j \) is a value that the elementary attribute takes from the possible variants of the current problem attribute space;
\( \eta_1, \eta_2, \eta_3 \) are the fixed attribute values that define a certain path in the LCT structure;
\( T_i \) is a path in the logical tree structure that corresponds to the fixed training pair with TS;
\( O_m \) is the function value;
\( k \) is a total number of classes in the set \( G \);
\( n \) is a total number of the problem attributes (attribute space dimension);
\( m_i^j \) is the RF value that ends a certain path \( T_i \), whereas \( j \) is the number of the logical tree construction step;
\( M \) is a total number of training pairs (objects) in the initial TS;
\( M_o \) is a total number of the ST test pairs (objects);
\( S \) is a total number of the TS training pairs, for which the relation \( f_R(x_i) = f \) holds true;
\( \delta \) is the parameter that characterizes training efficiency estimation with respect to the current problem;
\( M_{\eta_1, \eta_2, \eta_3} \) is a total number of all the pairs belonging to the \( \eta_1, \eta_2, \eta_3 \) path of the logical tree structure;

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\[ M_j^{r_1,r_2,r_3} \] is a number of all the pairs belonging to the 
\[ r_1,r_2,r_3 \] path, for which the relation \( f_R(x_1) = j \) holds true;
\[ t_j^{r_1,r_2,r_3} \] are the \( M_j^{r_1,r_2,r_3} \) and \( M_j^{r_1,r_2,r_3} \) relation values;
\[ H_j^{r_1,r_2,r_3} \] is a set of all the pairs of the initial TS that 
belong to a fixed path;
\[ V_r \] is a total number of vertices of constructed LCT;
\[ N_p \] is a total number of attributes used in the constructed 
LCT model structure;
\[ C_{tr} \] is a total number of transfers (links) in the LCT 
model structure;
\[ O_{tr} \] is a total number of resulting values RF (tree 
leaves) in the LCT model structure;
\[ En_{tr} \] is a LCT model error at the TS data array;
\[ Et_{tr} \] is a LCT model error at the ST data array;
\[ Er_{tr} \] is an error at each of the discrete object class;
\[ C_{avg} \] is an average number of transitions per one LCT 
vertex;
\[ N_{fr} \] is a part of elementary attributes used in the LCT 
structure;
\[ O_{fr} \] is a part of the resulting RF values in the general 
LCT structure;
\[ Q_{avg} \] is an average number of the TS sets with respect 
to the resulting RF values (tree leaves) in the LCT 
structure;
\[ l_{main} \] is a general index of the initial TS data generali-
zation LCT model;
\[ Q_{Main} \] is an integral quality index for LCT model.

**INTRODUCTION**

Information technologies based on the mathematical 
image recognition models in a form of LCT (i.e. the tree-
like models) are being widely used in the social, 
economic, environmental and other information 
processing systems. This is explained by the fact that such 
approach allows a set of the classical methods 
shortcomings to be eliminated and a principally new 
result to be achieved by effective and rational use of 
the computing systems capacities [1].

More than 3.500 of recognition algorithms (based on the 
different approaches and concepts) are known today 
having certain limitations in their use (i.e. accuracy, 
speed, memory, versatility, reliability etc). In addition, 
each of the algorithms is limited by a certain specific 
character of application problems, and this is, 
disputably, the most severe bottleneck of not only the 
above algorithms but also the recognition systems based 
on the relevant concepts [2].

The classification (decision) trees are the object of the 
present study.

It is known that presentation of big-volume training 
selections (i.e. discrete information) in a form of the logical 
tree structures has its essential advantages from the view-
point of economic description of the data and efficient 
mechanisms of their application [3]. In other words, the 
training selection covering by a set of elementary attributes 
in the LCT case or that by a fixed set of autonomous rec-
ognition and classification algorithms in the ACT case give 
rise to a fixed tree-like data structure that, to some extent, 
provides even the initial TS data compressing and processing, 
and, thus, allows the apparatus resources of information 
system to be essentially optimized and saved [4].

Note that the field of the use of the LCT concept is 
now extremely extensive, whereas a set of problems and 
tasks solved by the above apparatus could be reduced to 
the following three basic segments, i.e. to the problem of 
description of the data structure, to that of recogni-
tion/classification and to that of regression problem [5].

Thus, the ability of LCT to perform a one-dimensional 
branching to analyze the influence (importance, quality) 
of certain variables allows one to work with various-type 
variables in a form of predicates (in the ACT case – with 
the relevant autonomous classification and recognition 
algorithms) [6]. In this case, the logical tree structure is 
presented in a form of branches and nodes, with certain 
marks (attributes, values) placed on the tree branches
determining the target function (the recognition function in 
the LCT case) and the RF values or the extended transition 
attributes located at the nodes. Note that when con-
structing LCT the issues of choosing the attribute criterion 
(the LCT vertex), where the initial TS partition occurs, 
the criterion of training stopping (the LCT structure con-
struction) and that of rejecting the logic tree branches (the 
LCT sub-trees) remain the crucial ones. Just at this stage, 
a principal question of the LCT theory, i.e. the problem of 
possible construction of all the variants of logical trees 
that correspond to the initial TS and selection of the 
minimal with respect to the depth (layer number) logical 
tree arises [7]. It should be noted here that the above pro-
blem is the \( NP \)-complete one (this was fixed yet by L. 
Highfill and R. Rives), and therefore, has no simple and 
efficient methods of solving.

The methods and algorithms of constructing the logical 
classification trees (the decision trees) are the subject of 
this study.

The principal available methods of training selection 
processing at the recognition function construction do not 
allow the required level of recognition system accuracy to 
be achieved and their complexity in the process of these 
systems construction to be regulated [8]. The methods of 
constructing recognition systems based on the methods 
of logical classification trees (decision trees) are free of such 
shortcoming. In this case, the possibility of complex use 
of a number of known recognition algorithms (methods) 
to solve any particular problem of constructing recogni-
tion scheme is a specific feature of the logical tree (algo-
rithmic classification tree) method. It is based on a single 
methodology, i.e. the optimal approximation of training 
selection by a set of generalized attributes (autonomous 
algorithms) included into a certain scheme (operator) 
constructed in the course of training process [9].
The objective of this work is to develop an efficient and versatile method of constructing classification (recognition) models on the basis of the LCT concept for the discrete information arrays. In addition, the RS schemes obtained have a tree-like structure and elementary attributes as their structural elements.

1 PROBLEM STATEMENT

Let TS be set in a following form (1).

\[
x_1, f_R(x_1), \ldots, x_M, f_R(x_M)
\]

Note that here \( x_i \in G \) (\( G \) is a certain set), and \( RF \) is \( f_R(x_i) \in \{0,1,2,\ldots,k-1\}, (i = 1,2,\ldots,M) \).

Hence, \( f_R(x_i) = l, (0 \leq l \leq k - 1) \) means that \( x_i \in H_l, H_l \subset G \). Here \( f_R \) is a certain finitely many-valued function that assigns the partition \( R \) of the set \( G \) that consists of sub-sets (images, classes) \( H_0, H_1, H_2, \ldots, H_k \).

Thus, TS is a manifold (more strictly, a sequence) of certain sets, and each set is a manifold of certain attribute values and those of certain functions from this set. One may add that the manifold of attribute values is a certain image, whereas the function value correlates this image with the corresponding figure [10].

The task is to build the LCT – L construction based on the initial TS array and determine the values of its structural parameters \( p \) (i.e. \( F(L(p, x_i), f_R(x_i)) \rightarrow opt \)).

2 REVIEW OF THE LITERATURE

Analyzing the problems of tree-like classification and recognition models, one may realize a certain lack of current studies in this field, when the main emphasis is made on the concept of neural network recognition concept [11]. To a great extent, this can be explained by the specific features of just the LCT models, the difficulties of realization moments of the ACT concept (i.e. the highest level of the LCN concept abstraction), the set of the severe rules and restrictions concerning the practical work with such data structures [12].

Present study is a continuation of a cycle of works dedicated to the problem of tree-like discrete object recognition/classification schemes [13–15]. They relate the issues of constructing, using and optimizing the logical trees. It is known [13], that the resulting classification rule (scheme) constructed by an arbitrary method or by means of a branched attribute selection algorithm has a tree-like logical structure. The logical tree consists of the vertices (attributes) grouped in layers and obtained at a certain step (stage) of recognition tree construction [2]. The problem of synthesizing the recognition trees to be represented actually by the algorithm tree (graph) is an important problem [6]. Contrary to available methods, the main peculiarity of tree-like recognition systems is the fact that the importance of certain attributes (attribute/algorithm group) is defined with respect to the function that sets the object partition into classes [16].

For instance, in [17], the principal issues of the decision tree generation for the case of less informative attributes have been analyzed. The ability of LCT to perform a one-dimensional branching to analyze the influence (importance, quality) of certain variables gives a possibility to operate with the various-type variables in a form of predicates (in the ACT case – the relevant autonomous classification/recognition algorithms). Such a concept of logical trees is being used actively in the intellectual data analysis, where the final goal lies in synthesizing the model that predicts the target variable value on the basis of a set of the initial data at the system input [18–20].

Note that today there is a considerable number of algorithms that realize the decision tree concept – CART, C4.5, Sparc, NewID, TRule, CHAID, CN2, Oris and other, but the first ones are the most widely used and popular. It should be noted that the above logical tree algorithm C4.5 uses the so-called theoretical and information criterion as the node (vertex) selection one, whereas the CART algorithm is based on calculating the Gini index that takes into account relative distances between the class distributions [21].

In [2], the important elements of branched attribute selection are proposed and the LCD construction scheme is analyzed on the basis of the logical tree algorithm with a step-by-step estimation of the importance of the discrete attributes according to the TS data. A modified BAS with the one-off estimation of a set of attributes was suggested in [9], while in [22] an algorithm of generating the set (manifold) of random logic classification trees was proposed with a final optimal selection stage.

Because the principal idea of the BAS methods and algorithms could be defined as the optimal approximation of a certain initial TS by the set of elementary attributes (object attributes), their central problem of an efficient branching criterion (vertices, attributes, discrete object attributes) selection becomes the most important. Just these principal problems are considered in [11], where the questions of high-quality estimation of certain discrete attributes, their sets and fixed associations are raised allowing an effective mechanism of branching realization to be implemented.

The LCT structure is characterized by the compactedness, on the one hand, and the layer filling (sparsity) inhomogeneity, on the other hand, as compared to the regular trees (the algorithm with the one-off attribute estimation) [23]. Note that the problem of the BAS method-based LCT construction process convergence and the issues of selecting the logical tree synthesis process stopping (e.g., tree depth or complexity-related restrictions, accuracy restrictions, structure error number restrictions) remain essential [2].

Note that the logical tree concept does not contradict the possibility of using as the LCT attributes (vertices) certain attributes of their combination objects (generalized attribute idea considered in [24]) and sets. However, if one goes further and does not consider as branches the object attributes but selects certain independent recognition algorithms (estimated in accordance with the TS...
3 MATERIALS AND METHODS

The principal scheme of the BAS method algorithms on the LCT concept basis lies in the idea of maximizing the quantity $W_M(f)$ [2]. The latter means that one has to find in the logical tree algorithms such generalized attribute $f$ for the training selection (1), for which the quantity $W_M(f)$ should be as possibly maximal.

Note that the following quantity will be the attribute significance (2).

$$W(q^1_i) = \sum_{i \in M} b_i \rho_i, \quad \text{where } \rho_i = \max_{l \leq m \leq k} \frac{q^m_i}{b_l}. \quad (2)$$

Obviously, the significance of other attributes could be estimated in a similar way. The quantity $\frac{q^m_i}{b_l}$ can be interpreted as the probability of the fact that function $f_R(x)$ takes the value $O_m, (1 \leq m \leq k)$ on condition that the attribute value $q^1_i$ equals to $i$ ($1 \leq i \leq k$). The $\rho_i$ quantity is the maximal of such probabilities. The quantity $\rho_i$ may be said to be information that could be obtained about the $f_R(x)$ function value, knowing that at the $z$ set the attribute $q^1_i$ value is equal to $i$. The quantity $W(q^1_i)$ defined by this equation characterizes information that could be obtained about the $f_R(x)$ function value if the attribute $q^1_i$ value at the $z$ set is known. Obviously, the attribute, for which the above information is maximal, is considered the most important attribute with respect to $f_R(x)$.

Note that selection (1) may have the probability character, i.e. the pairs $(x, f_R(x_i))$, $(i = 1, 2, ..., M)$ may appear in it in accordance with some probability distributions $p(x/H_0), ..., p(x/H_{k-1})$, but the generalized attribute is determinate. Thus, the problem of optimal approximation of the probability selection (1) in general is set using a certain determinate function represented in general case by a generalized attribute $f$. It is obvious that the above problem has a sense when the image (class) character $H_0, H_1, ..., H_{k-1}$ is rather close to the determinate one. The latter means that the main part is occupied by the points (objects) $x$, for which the value $\max[p(x/H_0), ..., p(x/H_{k-1})]$ is close to unit. This value may vary substantially only at the points (objects) that lie on the boundary of several classes $H_0, H_1, ..., H_{k-1}$.

Note that in practice the BAS algorithms work, in general, with the problems where the images (classes) $H_0, H_1, ..., H_{k-1}$ have a character close to the determinate case.

It should be noted that these algorithms possess a following specific feature – each algorithm is a process that consists of certain steps $d_0, d_1, ..., d_i$. Here each step $d_i$ consists, in turn, of two stages (modes), i.e. training and control test.

In the training mode, a certain generalized attribute $f_i$ is formed at the step $d_i$. In the test mode, the efficiency $W_M(f_i)$ with respect to the training selection (1) is calculated for this generalized attribute. If $W_M(f_i) \geq \delta$, then the training process stops, whereas, if $W_M(f_i) < \delta$, then the transition to the step $d_{i+1}$ takes place.

Let us note the peculiarities of selection (1) provision at the training stage. Two cases are possible in practice:

a) Selection (1) is fixed, i.e. it is provided at each training step $d_i$.

b) Selection (1) depends on the step $d_i$, i.e. at each training step $d_i$ another selection is provided.

Case (a) takes place when selection (1) is the data of some experiment (e.g. computer measuring) stored in the read-only memory. The training algorithm in this case is a multiple selection (1) processing. Note that selection (1) may have extremely large volume, therefore, processing algorithms must ensure that selection (1) during operation could not be fed to the read-only memory.

If the case (a) does not occur, and there is no need in storing data in the read-only memory, we deal with the case (b). Here all the pairs processed at the step $d_i$ are not stored and, therefore, at the step $d_{i+1}$ another series of training pairs of the form (1) is fed.

For definiteness, we shall further consider the case (a), i.e. the same TS will be fed at each step $d_i$.

In this LCT construction scheme, a certain elementary attribute $q^1_i$ is chosen. It is required here that the value $W_M(q^1_i)$ with respect to (1) is as maximal as possible. Note once more that $W_M(q^1_i)$ is calculated in accordance with the method specified in [2, 10, 25, 26]. The next steps of the logic tree method are convenient to be interpreted using a tree (Fig. 1).

For definiteness, we shall further consider the case (a), i.e. the same TS will be fed at each step $d_i$.

Note that each LCT vertex (Fig. 1) contains either certain attribute $q^1_i$ or number $m^j_i$ that belongs to the set $\{0, 1, ..., k - 1\}$. The vertex with $m^j_i$, is called a final tree vertex. Two guiding lines (arrows) denoted 0 and 1 go out from the vertex with the attribute $q^1_i$. The guiding line 0 corresponds to the value $q^1_i = 0$, the guiding line 1 – to $q^1_i = 1$. This tree is conditionally divided into layers. The $j$-th layer contains the attributes $q^1_i, q^1_2, ..., q^1_j$.
Any attribute in all the layers, beginning from the first one and ending by the \( n \)-th ones, are the attributes obtained after the \( n \)-steps (stages) of the LCT construction. Note that the attributes located at the \( n \)-th layer are those derived at the \( n \)-th step (stage) of the logical construction process.

Assume that only three steps of the LCT construction are realized, and \( 3, 3, 3, 3, 3, 3 \) are the all attributes obtained as a result of the above steps. The logic tree obtained in this three steps has a following form (Fig. 2).

We shall call the paths corresponding to the case (a) not finished, whereas those in the case (b) will be called finished ones.

If the path \( T_i \) that corresponds to the pair \( (x_i, f_R(x_i)) \) is finished and has at its end the value \( \{1, 0\}, \ldots, \{3, 2, 1\} \), this means that \( f_R(x_i) = m_i^3 \). For instance (see Fig. 2), for any pair \( (x_i, f_R(x_i)) \) that satisfies condition \( \phi_1^3(x_i) = \phi_2^3(x_i) = 1 \), another condition holds true \( f_R(x_i) = m_i^3 \). One may say that for the value \( x_i \) corresponding to the finished path \( T_i \), the complete tree-related recognition is realized (Fig. 2). In other words, the pair \( (x_i, f_R(x_i)) \) belongs to the relevant path \( T_i \).

At the next stages of classification tree construction, the unfinished paths shall be considered only. Then we shall denote each path at the tree under construction by a binary set \( \{1, 0\}, \ldots, \{3, 2, 1\} \). For instance, the binary set 010 at the tree (Fig. 2) shall indicate the path that ends by a final arrow going from the vertex \( \phi_2^3 \) and denoted as 0. Obviously, the set \( \{000, 001, 010, 011, 100, 101\} \) is a manifold of all the unfinished paths at the LCT (Fig. 2).

Let \( M_{n,k} \) be a number of all the pairs \( (x_i, f_R(x_i)) \) of selection (1) that belong to the unfinished path \( 1, r_2, r_3, \ldots, r_j \in \{0, 1\} \). For instance, the binary set 010 at the tree (Fig. 2) shall indicate the path that ends by a final arrow going from the vertex \( \phi_2^3 \) and denoted as 0. Obviously, the set \( \{000, 001, 010, 011, 100, 101\} \) is a manifold of all the unfinished paths at the LCT (Fig. 2).

Let \( M_{n,j}^3 \) be a number of all the pairs \( (x_i, f_R(x_i)) \) of selection (1) that belong to the unfinished path \( 1, r_2, r_3, \ldots, r_j \in \{0, 1\} \). For instance, the binary set 010 at the tree (Fig. 2) shall indicate the path that ends by a final arrow going from the vertex \( \phi_2^3 \) and denoted as 0. Obviously, the set \( \{000, 001, 010, 011, 100, 101\} \) is a manifold of all the unfinished paths at the LCT (Fig. 2).

Let \( M_{n,k}^3 \) be a number of all the pairs \( (x_i, f_R(x_i)) \) of selection (1) that belong to the unfinished path \( 1, r_2, r_3, \ldots, r_j \in \{0, 1\} \). For instance, the binary set 010 at the tree (Fig. 2) shall indicate the path that ends by a final arrow going from the vertex \( \phi_2^3 \) and denoted as 0. Obviously, the set \( \{000, 001, 010, 011, 100, 101\} \) is a manifold of all the unfinished paths at the LCT (Fig. 2).
Let us find the value \( l(r_1, r_2, r_3) \) for which:

\[
l(r_1, r_2, r_3) = \max_j l_{r_1, r_2, r_3}(j), \quad (j = 0, 1, \ldots, k - 1).
\]

Substituting the quantity \( l(r_1, r_2, r_3) \), at the end of each path \( 1, 2, 3 \), at the LCT (Fig. 2), we obtain the following LCT (Fig. 3).

Note that the tree from Fig. 3 realizes some generalized attribute \( f_3(x) \) defined at the set \( G \) and takes the values from the set \( \{0, 1, \ldots, k - 1\} \). The attribute \( f_3(x) \) is calculated as follows. First, for \( x \) we find the entire path \( T_x \) that corresponds to this element (the TS object). For example, if \( \varphi_1^3(x) = 0, \varphi_2^3(x) = 1, \varphi_3^3(x) = 1 \), then \( T_x = 011 \). As the \( f_3(x) \) values we take the element from \( 1, 2, 3 \) that ends the path \( T_x \). For instance, if \( T_x = 011 \), then \( f_3(x) = 101 \). If the object \( x \) corresponds to the finished path \( T_x \), with the number \( m_x, (0 \leq m_x \leq l) \) in the end, we assume that \( f_3(x) = m_x \).

After constructing the attribute \( f_3(x) \), the control test stage starts. In the test mode, the number \( S \) of all the pairs \( (x_i, f_R(x_i)) \) from selection (1), for which relation \( f_R(x_i) = f_3(x_i) \) holds true.

Let us check the condition \( S \geq \delta \). Given this condition met, the process of the tree construction ends, and the generalized attribute \( f_3(x) \) represented by a logical tree (Fig. 3) provides approximation of selection (1). If

\[
l_{r_1, r_2, r_3}^j = \frac{M_{r_1, r_2, r_3}^j}{M_{r_1, r_2, r_3}}, \quad (j = 0, 1, \ldots, k - 1).
\]

When constructing the recognition tree, we shall first select at LCT (Fig. 3) all the values \( l(r_1, r_2, r_3) \) for which relation \( l(r_1, r_2, r_3) = 1 \) is valid. The paths \( r_1, r_2, r_3 \) for which the above relation is valid could be considered finished.

For example, let:

\[
l_{010}^1 = l_{011}^1 = 1; \quad l_{000}^1 < 1;
\]

\[
l_{001}^1 < 1; \quad l_{100}^1 < 1; \quad l_{101}^1 < 1.
\]

In this case, we obtain the tree (see Fig. 4), where \( m_1^3 = l(010), m_2^3 = l(011) \). All the paths \( 000, 100, 101 \) at the tree (Fig. 4) are unfinished. For each of these paths \( r_1, r_2, r_3 \) we consider the sets \( H_{r_1, r_2, r_3} \), where \( H_{r_1, r_2, r_3} \) is the set of all those training selection pairs \( (x_i, f_R(x_i)) \), which belong to the path \( r_1, r_2, r_3 \). The sets \( H_{r_1, r_2, r_3} \) could be considered certain selections. Note that in case of logical tree (Fig. 4) we have the following selections \( H_{000}, H_{001}, H_{100}, H_{101} \). For each selection \( H_{r_1, r_2, r_3} \) we choose the elementary attribute \( \varphi_{r_1, r_2, r_3} \) for which the value \( W_{H_{r_1, r_2, r_3}}(\varphi_{r_1, r_2, r_3}) \) is as maximal as possible. The value \( W_{H_{r_1, r_2, r_3}}(\varphi_{r_1, r_2, r_3}) \) is the efficiency of recognition of the \( r_1, r_2, r_3 \) selection with the help of the attribute \( \varphi_{r_1, r_2, r_3} \). After selecting the attributes \( \varphi_{r_1, r_2, r_3} \), we receive a new LCT shown in Fig. 1. Note that here we shall have as follows:

\[
\varphi_1^4 = \varphi_{000}; \quad \varphi_2^4 = \varphi_{001}; \quad \varphi_3^4 = \varphi_{100}; \quad \varphi_4^4 = \varphi_{101}.
\]

Figure 3 – Logical tree after the three generation steps with fixed paths

Figure 4 – Final LCT

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Then we apply to the tree from Fig. 1 the same process as in case of the tree from Fig. 2.

It is worthy noting that there is no need in forming a separate set of training pairs to realize each selection \( H_{r_1^p, r_2^p, r_3} \). All these selections are realized as follows – the pairs of selection (1) are fed sequentially and only the training selections belonging to the path \( r_1^p, r_2^p, r_3 \) are taken into account. As a result of this process, the selection \( H_{r_1^p, r_2^p, r_3} \) will be realized.

4 EXPERIMENTS

It is obvious that one may construct the LCT set on the basis of one initial TS using the relevant methods and algorithms. For example, using the functional (2) as the branching criterion, we can construct at least two LCTs dependent on the choice – whether it is worthy to evaluate the branching criterion, we can construct at least two LCTs based on the TS and ST data, as well as to each of the selection criteria.

Let us fix at the next stage the main parameters of the LCT model with respect to its characteristics –
\[
C_{\text{avg}} = \frac{C_r}{V_r}, \quad N_r, \quad C_r, \quad O_r, \quad E_n r, \quad E_l r, \quad E_r f .
\]

Let us fix the following list of basic characteristics of the LCT model with respect to its characteristics –
\[
C_{\text{avg}} = \left( C_r / V_r \right), \quad N_r^\prime = \left( N_r / n \right), \quad O_r^\prime = \left( O_r / V_r \right), \quad Q_{\text{avg}} = (M / O_r) .
\]

General index of the initial TS data generalization LCT model is calculated as:
\[
I_{\text{main}} = \frac{M \cdot n}{V_r + 2C_r}.
\]

It is obvious that the patterns \( E_{n r}, \ E_{l r}, \ E_{r f} \) model errors are the critically important LCT model parameters (according to the TS and ST data, as well as to each of the initial partition classes of the current problem set \( G \)).

Note that the question of the reduction of the LCT structure complexity remains a principal moment (here we deal with the following parameters, \( N_r \) being the number of attributes in the LCT structure, \( V_r \) being the number of the LCT model vertices and \( C_r \) being a total number of transitions in the LCT structure; and the memory and processor time loss parameters \( \lambda \) and \( \tau \), respectively).

Note that it is reasonable to increase the parameters \( O_r \) and \( O_{r'} \) in the LCT structure. This will allow the time of making solutions according to this logical tree model to be reduced and the processor time to be saved. It is necessary to maximize the parameter \( I_{\text{main}} \) (the LCT model generalization index) that allows one to reach the most optimal LCT structure and provides the maximal compression of the initial TS data (i.e. to represent the initial data array by the minimally structurally complex logical tree), as well as the parameter \( Q_{\text{avg}} \) (the average number of the TS sets at the resulting RF values, i.e. the LCT leaf) [29–33].

The integral model quality index presented in the following form is an important LCT model index that takes into account the above parameters:
\[
Q_{\text{main}} = \frac{e^{M-M_{tr}}}{N_T \cdot V_{tr} \cdot C_{tr}}.
\]

It should be noted here that this integral LCT model quality index has a sense only in case when the condition \( (E_n r / M) \leq \delta \) holds true. Obviously, in the opposite case it will be zero. This index increase characterizes the growth of the LCT model quality and, vice versa, its decrease testifies to the classification quality worsening.

Thus, having taken, as the basis, the classification tree method and the modularity principle, the software complex Orion III has been developed at the Uzhgorod National University being used to generate the autonomous recognition systems. This system algorithmic library has 11 recognition algorithms including the algorhythm realization of the LCT construction suggested above.

The basic problem here was the construction of the autonomous recognition system on the basis of geological data (the oil-bearing bed partitioning problem). 12 basic elementary attributes and 10 additional ones have been used to recognize objects.

Information concerning the two classes of objects is presented in the TS. At the examination stage, the classification system constructed has to provide an efficient recognition of unknown classification methods with respect to the above two classes. Before starting the work, training selection was automatically checked for correctness (searching for and removing the similar objects of different belonging – the first kind errors), though the system realizes the training and error-correcting scheme for the classification tree (the TEC algorithm) – as generation was carried out in the automatic mode, this algorithm has not been used.

5 RESULTS

Note that training selection consisted of 1.250 objects (756 of them being oil-bearing ones), and the efficiency of constructed recognition system was estimated at the test selection comprising 240 objects. The data of training and test selections have been obtained in accordance with the geological survey on the territory of Transcarpathian province during the period from 2001 to 2011.

It should be noted that a fragment of the main results of the above experiments is presented in Table 1. The LCT models constructed provided a required level of accuracy set by the problem statement, speed and system operating memory consumption.
Note that the suggested LCT model quality estimates fix the most important characteristic of the logical trees and could be used as the optimality criterion in the procedure of LCT construction and final selection from the LCT model set.

It should be noted that this LCT construction scheme was compared to the ACT method showing an acceptable result. The main idea of ACT is its approximation by a set of initial TS algorithms. The ACT structure obtained is characterized by high versatility and relatively compact model structure. However, it requires large apparatus costs to store the generalized attributes and to provide the initial estimation of the TS classification algorithm quality. In contrary, LCT has high classification rule speed, low apparatus costs for storing and tree structure operating and high classification quality.

CONCLUSIONS

In this work, the problem of the LCT construction automation on the basis of TS approximation by a set of elementary attributes has been solved.

The scientific novelty of the results obtained is confirmed by the fact that a simple method of LCT construction has been suggested for the first time on the basis of the elementary attribute selection with a permanent estimation of their importance at each step of the classification tree generation. Here, at each branching step, the influence of any attribute value on the resulting RF value in the tree structure has been taken into account. Note that the functional proposed could be used not only to estimate the informativeness of certain elementary attributes, but also to calculate the importance of the attribute sets and their combinations that allows more optimal structure of synthesized LCT according to the TS initial data to be achieved in future.

We have suggested in the present work a set of general indices that allows the general LCT model characteristics to be presented effectively. This set could be used to select the most optimal LCT from a number of constructed ones (e.g., in the case of the random LCT construction algorithms [22]).

The applied value of the results obtained in the present work means that suggested LCT construction method has been realized in the algorithm library of a universal software system ORION III to solve different applied problems of discrete object array classification/recognition.

Note that practical testing carried out by us has confirmed the performance of suggested LCT models and software. This enables recommendations on the use of the above approach and its software realization to be elaborated for a wide spectrum of applied problems of discrete object array classification/recognition.

The outlook of the further studies could be related to developing the methods of algorithmic trees classification and optimization of the software realization of the suggested LCT construction method and its practical testing at the set of real classification/recognition problems.

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АНОТАЦІЯ

Актуальність. Розглянута загальна задача побудови логічних дерев розпізнавання (класифікації). Об’єктом даного дослідження є логічні дерева класифікації. Предметом дослідження є актуальні методи та алгоритми побудови логічних дерев класифікації.

Мета. Метою даної роботи є створення простого та ефективного методу побудови деревоподібних моделей розпізнавання на основі дерев класифікації для навчальних вибірок дискретної інформації, який характеризується структурою оптимальних логічних дерев класифікації з елементарних ознак оцінених на основі функціоналу розрахунку їх інформативності.
Метод. Пропонується загальний метод побудови логічних дерев класифікації, який для заданої початкової навчальної вибірки буде деревоподібної структури, яка складається з набору елементарних ознак оцінених на кожному кроці побудови моделі за даною вибіркою. Тобто пропонується метод побудови логічного дерева основна ідея якого полягає в апроксимації навчальної вибірки довільного об’єму набором елементарних ознак. Даний метод при формуванні поточної вершини логічного дерева (узла) забезпечує відліки найбільш інформативних (якісних) елементарних ознак з початкового набору. Такій підхід при побудові результату дерев класифікації дозволяє: значно скоротити розмір та складність дерева (загальну кількість гілок та ярусів структури) підвищити якість його наступного аналізу (интерпретабельність). Запропонований метод побудови логічного дерева класифікації дозволяє будувати деревоподібні моделі розпізнавання для широкого класу задач теорії штучного інтелекту.

Результати. Розроблений та представлений в даній роботі метод отримав програмну реалізацію та був досліджений при розв’язанні задач класифікації даних геологічного типу, які характеризуються ознаковим простором великого розмірності.

Висновки. Проведені в даній роботі експерименти підтвердили раціональність запропонованого математичного забезпечення та вказують на можливість його використання для розв’язку широкого спектру практичних задач розпізнавання та класифікації. Перспективи подальших досліджень можуть полягати в створенні обмеженого методу логічного дерева класифікації, який полягає в ведені критерію зупинки процедури побудови логічного дерева за глибиною структури, оптимізації його програмних реалізацій, а також експериментальних дослідженнях даного методу на більш широкі комп'ютерні задачі.

КЛЮЧОВІ СЛОВА: логічне дерево класифікації, розпізнавання образів, класифікація, ознаки, критерій розгалуження.

УДК 001.891:65.011.56

ПОСТРОЕНИЕ ЛОГИЧЕСКИХ ДЕРЕВЬЕВ РАСПОЗНАВАНИЯ НА ОСНОВЕ МЕТОДА ПОШАГОВОЙ СЕЛЕКЦИИ ЭЛЕМЕНТАРНЫХ ПРИЗНАК

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АННОТАЦИЯ

Актуальность. Рассмотрена общая задача построения логических деревьев распознавания (классификации). Объектом данного исследования является логические дерево классификации. Предметом исследования является актуальные методы и алгоритмы построения логических деревьев класификации.

Цель. Целью данной работы является создание простого и эффективного метода построения деревьев классификации для обучающих выборок дискретной информации, которая характеризуется структурой полученных логических деревьев классификации с элементарных признаков оцененных на основе функционала расчета их информативности.

Метод. Предлагается общий метод построения логических деревьев классификации, который для заданной начальной обучающей выборки строит древовидную структуру, состоящую из набора элементарных признаков оцененных на каждом шагу построения модели по данной выборке. То есть предлагается метод построения логического дерева основная идеи которого заключается в аппроксимации начального выборки произвольного объема набором элементарных признаков. Данный метод при формировании текущей вершины логического дерева (узла) обеспечивает выделение наиболее информативных (качественных) элементарных признаков с начального набора. Такой подход при построении результирующего дерева классификации позволяет значительно сократить размер и сложность дерева (общее количество ветвей и ярусов структуры) повысить качество его последующего анализа (интерпретабельность).

Результи. Разработан и представлен в данной работе метод получил программную реализацию и был исследован при решении задач классификации данных геологического типа, характеризующихся признаковыми пространством большой размерности.

Выводы. Проведенные в данной работе эксперименты подтвердили работоспособность предложенного математического обеспечения и показывают возможность его использования для решения широкого спектра практичных задач распознавания и класифікації. Перспективы дальнейших исследований могут заключаться в создании ограниченно моделей логических деревьев по глубине структуры, оптимизации их программных реализаций, а также экспериментальных исследованиях данного метода на более широких круг практических задач.

КЛЮЧЕВЫЕ СЛОВА: логическое дерево классификации, распознавания образов, классификация, признак, критерий разветвления.

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