Fracturing in coals with different fluids: an experimental comparison between water, liquid CO₂, and supercritical CO₂

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The present work conducted laboratory experiments of fracturing in fat coals, anthracites, and mudstones. Three different fluids were selected as the fracturing fluids, including water, liquid CO₂ (L-CO₂), and supercritical CO₂ (Sc-CO₂). The resulting fracture morphologies and fracture apertures of the coal specimens were investigated using 3D morphological scanning, and the permeabilities of the samples were measured before and after fracturing. The experimental results showed that the breakdown pressures of Sc-CO₂ fracturing were the lowest among the three fracturing fluids, and the average single fracture apertures of the ScCO₂-induced cracks were the smallest amongst the three fracturing fluids. In addition, the number of cracks and the roughness coefficients induced by Sc-CO₂ fracturing were larger than those caused by water and liquid CO₂. The viscosity of the fracturing fluid and the capillary effect are key factors that affect the crack propagation path and fracture surface topography. The results suggest that Sc-CO₂ has the largest diffusion length, and thus is capable of permeating the coal matrix through small pores and causing more extensive fractures. Additionally, the effective hydraulic apertures of coal specimens produced by Sc-CO₂ fracturing were wider than those induced by water and liquid CO₂. The experimental results indicate that Sc-CO₂ fracturing has huge potential to enhance coalbed methane recovery.

Coalbed methane (CBM) refers to hydrocarbon gases existing in coal seams, whose main component is CH₄. The exploitation and utilization of CBM is of crucial importance to improving the supply of clean energy¹, ensuring safe production in coal mines and reducing greenhouse gas emissions². According to the national coal bed methane resources evaluation report of Ministry of Land and Resources, The amount of prospective resources within 3000 m is 55.20 trillion cubic meters in China, which is the third largest reserves in the world (less than Russia and Canada)³. Nevertheless, the efficiency of CBM exploitation in China has not yet reached to the expected level⁴. The cumulative CBM production was 17.1 x 10^8 m³ by the end of 2015, which is only accounting for about 60% of the total target volume in the plan of the government⁵. One of the primary reasons restricting the efficient exploitation of CBM in China is the low permeability of coal seams (< 1 mD)⁶. Hydraulic fracturing is a commonly used approach for enhancing CBM production in low permeable coals, whose key idea is to inject a large amount of water into ground to create interconnected dense fracture networks⁷. Nevertheless, this technology is not without shortcomings. For example, it results in groundwater contamination by additives that cannot be degraded naturally in the aqueous fracturing liquid⁸. Another main obstacles with hydraulic fracturing is excessive water consumption⁹, which is even more serious considering the situation that the most CBM reservoirs in China are situated in water-deficient areas. In addition, some coal seams in China consist of mudstones interbedded with high clay content, and hydraulic fracturing causes the clays to swell and obstructs gas transport channels, incurring the so-called water block effect.

To surmount the above-mentioned drawbacks, the non-aqueous fracturing technologies are presented by some researchers¹⁰–¹², in which carbon dioxide (CO₂) is considered to be a competitive alternative to water. It is noted that although liquid CO₂ (L-CO₂) is normally injected as fracturing medium in engineering practice, it is highly possible to transit to supercritical state in deep coal seams, where the pressure and temperature exceed the critical point of CO₂ (7.38 MPa and 31.1 °C) (Fig. 1)¹³. Supercritical CO₂ (Sc-CO₂) holds promise as an ideal

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fracturing medium for its low viscosity (similar to CO₂ gas) and high density (similar to liquid CO₂)\(^\text{14}\). Another benefit of Sc-CO₂ fracturing is that it is able to displace the CBM existing as adsorbed form due to the higher adsorption properties of Sc-CO₂ in coals\(^\text{15,16}\) and meanwhile reduces greenhouse gas emissions\(^\text{17}\).

Since its inception, the non-aqueous fracturing with L-CO₂ and Sc-CO₂ has drawn considerable attention\(^\text{18,19}\). Verdon et al.\(^\text{20}\) monitored the seismic wave variations which occurred when aqueous fluid and CO₂ were injected separately into the reservoir. Their results showed that the distinguishable fracturing behaviors of water and Sc-CO₂ arise from their entirely different physical properties. Ishida et al.\(^\text{21}\) compared waterless (including liquid CO₂ (L-CO₂) and Sc-CO₂) and water fracturing in granite. Their experimental results indicated that, compared to water injection, the crack propagation ranges induced by L-CO₂ and Sc-CO₂ were greater and the breakdown pressures were considerably lower. Zhou et al.\(^\text{22}\) conducted Sc-CO₂ fracturing experiments with cylindrical shale samples and used computerized tomography (CT) scanning to characterize the induced fractures. Their experimental results revealed that Sc-CO₂ produced extensive and complex multi-branch fractures in the shale samples. Zhang et al.\(^\text{23}\) performed experiments on Sc-CO₂ fracture initiation and the crack propagation behavior driven by Sc-CO₂ in large shale specimens using acoustic emission (AE) and CT scanning systems, and found that the fracture initiation pressure caused by Sc-CO₂ fracturing was about 50% less than that for water fracturing and that complex fracture networks were more likely to occur in the Sc-CO₂ fractured samples. According to Jia et al.\(^\text{24}\), Sc-CO₂ fracturing induced fractures with rougher and more complex surfaces and higher tortuosity, and increased the permeability of samples to a greater extent compared to water fracturing. Similar conclusions were drawn by Zhou et al.\(^\text{25}\) who carried out Sc-CO₂ fracturing experiments on artificial rock specimens and Cai et al.\(^\text{26}\) who conducted Sc-CO₂ jet fracturing tests on solvent glass specimens. Experimental investigation\(^\text{27–30}\) further revealed that the fracture toughness of coals tends to decrease with the injection of Sc-CO₂, causing cracks in the coal to expand more easily. Parallel to the development in laboratory experiments, some advances are also made in mathematical modelling. Wang et al.\(^\text{31}\) adopted a coupled model of rock fracture mechanics and gas flow to simulate the water, oil, and Sc-CO₂ fracturing processes, finding that Sc-CO₂ fracturing exhibited the lowest breakdown pressure, which is consistent with the experimental results from other studies. Song et al.\(^\text{32}\) presented a multi-field coupling mathematical model to investigate the pressure transmission in the tubing used for Sc-CO₂ fracturing, and Yang et al.\(^\text{33}\) developed a new numerical model to predict the evolution of temperature and pressure during Sc-CO₂ fracturing. These mathematical models offer a theoretical basis for Sc-CO₂ fracturing engineering.

The novelty of the present work lies in that we provide a systematic framework for assessing the performance of different fracturing fluids, in the perspectives of breakdown pressure, number of cracks, and particularly, fracture roughness coefficients and fracture apertures. We performed laboratory fracturing experiments using water, L-CO₂, and Sc-CO₂ as the fracturing fluids on coal core specimens obtained from the main CBM production areas in the Qinshui Basin, China. A triaxial fracturing apparatus designed in-house was employed in the experiments. The permeabilities of the specimens were measured before and after fracturing. Then, the fracture surfaces induced by the different injected fluids were scanned by the 3D morphological scanner and following this, the fracture roughness and apertures are quantified.

**Materials and methods**

The laboratory experiments have undergone the following stages: first, fracturing experiments with the coal specimens were carried out using the different fluids (water, L-CO₂, and Sc-CO₂) under the same operation conditions. Second, after the fracturing the permeabilities of the coal core specimens were measured. Third, the surface topographies of the induced fractures in the coal specimens were studied to compare the fracturing performance of the different fluids. Finally, the fracturing effects were further compared between the three fracturing fluids and analyzed in detail to explain the underlying reasons.
Materials used and sample preparation. Coal rank is a quantity used to describe the degree of coal mineralization in the coal formation process. Generally, coal is divided into anthracite (high-rank coal), bituminous coal (mid-rank coal) and lignite (low-rank coal) according to fixed carbon content, volatile matter, vitrinite reflection and other parameters, which bituminous coal includes long-flame coal, gas coal, fat coal, coking coal and lean coal. In this study, two different rank coals were tested: a mid-rank fat coal and a high-rank anthracite, which were collected from the Changping and Hesi collieries located in the Qinshui Basin. This area is the most important CBM production base in China, accounting for over 66% of China’s total CBM production. Proximate analysis results and mechanical parameters of the coal samples are listed in Table 1. Additionally, mudstone specimens taken from the Changping colliery were used as a control group. The mineral content of the mudstone samples was determined semi-quantitatively using X-ray diffraction (XRD), with a typical XRD pattern as shown in Fig. 2. The results show that the clay mineral content in the mudstone specimens was 34%, including kaolinite and illite, and the rest was composed predominantly of silicon dioxide and potash feldspar. The samples taken from the mine shaft were immediately sealed with paraffin wax to avoid weathering.

The specimens used in the fracturing experiments were cylindrical-shaped. A special coring method was employed to obtain the coal and mudstone specimens to reduce mechanical damage on the samples. The core samples were manufactured using a 1.5 mm carborundum wire saw in a computer numerical control machine tool with lubricating oil coolant. As depicted in Fig. 3a, the core samples of diameter 50 mm were trimmed by saw to a length of approximately 100 mm, and then a central borehole of diameter 5 mm was drilled to a depth of 50 mm. Next, a steel pipe for fluid injection (with external and internal diameter of 3 mm and 2 mm, respectively) was inserted into the borehole to simulate the geometry of CBM fracturing wells. The injection pipe was adhered to the preformed borehole using No. 7102 epoxy glue. A photograph of the coal and mudstone fracturing specimens used in the experiments is shown in Fig. 3b. To observe the integrity of the drilled coal specimens, the CT scanning tests were conducted using the μ-FCB CT test system. Figure 4 shows the CT scanned section images of the borehole of the two types of coal specimens. From Fig. 4, there are no microcracks or defects in the prefabricated holes except for the scratches left by drilling, which means that drilling has not caused significant damage to the coal specimen, and it will not affect the subsequent fracturing test results.

Test apparatus. The fracturing and permeability experiments were carried out on a triaxial fracturing apparatus designed in-house. As illustrated in Fig. 5, the fracturing apparatus was composed of five subsystems: a triaxial loading and control system, a temperature control system, a water fracturing system, a waterless fracturing system (for L-CO₂ and Sc-CO₂ fracturing), and a computer control system. In the triaxial pressure steel kettle,

| Type          | Fat coal | Anthracite | Mudstone |
|---------------|----------|------------|----------|
| Moisture content (%) | 0.63     | 2.54       | –        |
| Ash yield (%)  | 7.90     | 19.37      | –        |
| Volatile matter (%) | 30.35    | 8.02       | –        |
| Fixed carbon (%) | 61.43    | 71.33      | –        |
| Vitrinite reflection (%) | 1.12    | 2.53       | –        |
| Elasticity modulus E (MPa) | 2750     | 3120       | 36,500   |
| Poisson’s ratio ν | 0.28     | 0.29       | 0.32     |
| Tensile strength fₜ (MPa) | 0.57     | 1.12       | 4.52     |

Table 1. Proximate analysis results and mechanical parameters of the coal and mudstone samples.

Figure 2. XRD spectrum of the mudstone used in the experiments.
A silicone rubber sleeve was used around the specimen to facilitate the enforcement of the confining pressure. Axial and confining pressure was applied to the cylindrical specimen using axial and confining servo pumps, respectively, with a control precision of 0.02 MPa. The hydraulic fracturing experiments were conducted using a liquid pressure pump. The waterless fracturing system includes a CO₂ cylinder, a CO₂ liquefaction plant, a duplex plunger pump (for injecting L-CO₂) and a counterbalance valve. The temperature control system mainly consisted of a heating jacket for the triaxial pressure steel kettle and pipeline heater, with a temperature control accuracy of 0.1 °C. When performing Sc-CO₂ fracturing tests, the temperature of the specimen and the pipeline were controlled above the critical temperature (31.10 °C) to ensure that the injected CO₂ was in the supercritical state. Throughout the fracturing experimental procedure, the axial stress, confining pressure, temperature, and fracturing fluid pressure were monitored and recorded in real time by the computer control system.

**Figure 3.** (a) Dimensions of specimens used in the fracturing experiments. (b) Photograph of the coal and mudstone specimens.
Experiment procedure. For the fracturing tests, the coal core samples were placed into the triaxial pressure steel kettle, and the axial and confining pressures were applied alternately at a rate of 2 MPa min\(^{-1}\) to avoid stress damage to the samples. In all the experiments, the axial pressure, \(\sigma_a\), and the confining pressure, \(\sigma_c\), were set to be 10 MPa and 8 MPa, respectively. For the water fracturing tests, the test temperature was set to 40 °C, and water was injected into the borehole at a constant flow rate of 20 ml min\(^{-1}\). The sample was fractured when we observed a rapid drop in the fracturing fluid pressure and a jump in the confining pressure. Prior to the non-aqueous (L-CO\(_2\) and Sc-CO\(_2\)) fracturing experiments, the CO\(_2\) gas was liquefied in the CO\(_2\) liquefaction plant. For the L-CO\(_2\) fracturing tests, the specimen was not required to be heated, and L-CO\(_2\) was injected into the borehole at room temperature (21 °C) using a flow rate of 20 ml min\(^{-1}\). The physical characteristics of Sc-CO\(_2\) are very sensitive to temperature variation\(^3\); therefore, prior to the Sc-CO\(_2\) fracturing experiments, the gas pipeline and core sample were heated to 40 °C, and the temperature was allowed to stabilize over a period of two hours before injecting Sc-CO\(_2\). During all the fracturing experiments, a high-precision pressure sensor recorded the fracturing fluid pressure every 0.1 s. Permeability is one of the most important properties required for evaluating the fracturing effects of different fluids; hence, the permeabilities of the specimens were measured using a steady-state method before and after the fracturing experiments. Finally, the surface topographies of the induced fractures were characterized using a 3-D morphological scanner. The exact conditions under which the different tests were carried out are shown in Table 2. For each type of fracturing fluid, experiments were performed on at least two specimens.

Results and discussion

Breakdown pressures for the different fracturing fluids. The fracturing fluid pressure versus time curves for the fat coal, anthracite and mudstone samples are plotted in Fig. 6 for all three kinds fracturing fluids. As the figure shows, for all the three sample types, the hydraulic pressure increased slowly in the initial stages of water fracturing. When the water is injected, the fluid pressure increased rapidly until fracture occurred. In com-

![CT scan section image of the borehole for (1) the fat coal specimen and (2) the anthracite specimen.](image1.png)

![Experimental apparatus for water, L-CO\(_2\) and Sc-CO\(_2\) fracturing tests.](image2.png)
### Table 2. Experimental conditions for the fluid fracturing experiments.

| Sample number | Specimen type | Fracturing fluid | Axial, confining pressure $\left(\sigma_a/\sigma_c\right)$ (MPa) | Temperature (°C) | Fluid injection rate (mL/min) |
|---------------|---------------|------------------|-----------------------------------------------------------|------------------|-------------------------------|
| $F_1_{water}$ | Fat coal      | Water            | 10/8                                                      | 40               | 20                            |
| $F_2_{water}$ | Fat coal      | Water            | 10/8                                                      | 40               | 20                            |
| $F_1_{L-CO_2}$ | Fat coal      | L-CO$_2$         | 10/8                                                      | 21 (room temperature) | 20                            |
| $F_2_{L-CO_2}$ | Fat coal      | L-CO$_2$         | 10/8                                                      | 21 (room temperature) | 20                            |
| $F_1_{Sc-CO_2}$ | Fat coal      | Sc-CO$_2$        | 10/8                                                      | 40               | 20                            |
| $F_2_{Sc-CO_2}$ | Fat coal      | Sc-CO$_2$        | 10/8                                                      | 40               | 20                            |
| $A_1_{water}$ | Anthracite    | Water            | 10/8                                                      | 40               | 20                            |
| $A_2_{water}$ | Anthracite    | Water            | 10/8                                                      | 40               | 20                            |
| $A_1_{L-CO_2}$ | Anthracite    | L-CO$_2$         | 10/8                                                      | 21 (room temperature) | 20                            |
| $A_2_{L-CO_2}$ | Anthracite    | L-CO$_2$         | 10/8                                                      | 21 (room temperature) | 20                            |
| $A_1_{Sc-CO_2}$ | Anthracite    | Sc-CO$_2$        | 10/8                                                      | 40               | 20                            |
| $A_2_{Sc-CO_2}$ | Anthracite    | Sc-CO$_2$        | 10/8                                                      | 40               | 20                            |
| $M_1_{water}$ | Mudstone      | Water            | 10/8                                                      | 40               | 20                            |
| $M_2_{water}$ | Mudstone      | Water            | 10/8                                                      | 40               | 20                            |
| $A_1_{L-CO_2}$ | Mudstone      | L-CO$_2$         | 10/8                                                      | 21 (room temperature) | 20                            |
| $A_2_{L-CO_2}$ | Mudstone      | L-CO$_2$         | 10/8                                                      | 21 (room temperature) | 20                            |
| $A_1_{Sc-CO_2}$ | Mudstone      | Sc-CO$_2$        | 10/8                                                      | 40               | 20                            |
| $A_2_{Sc-CO_2}$ | Mudstone      | Sc-CO$_2$        | 10/8                                                      | 40               | 20                            |

**Figure 6.** Comparison of fracturing test results with different fracturing fluids for the (a) fat coal, (b) anthracite, and (c) mudstone specimens for different fracturing fluids.
For the waterless fracturing experiments, the increase rate of fluid pressure becomes significantly slower after reaching a certain value and thus it takes longer than hydraulic fracturing to reach the breakdown pressure. A possible explanation is that at the onset of waterless fracturing, the large diffusion coefficients of L-CO₂ and Sc-CO₂ enable them to quickly fill up the borehole of the tested specimens, which results in a rapid increase of fluid stress \( \sigma \). The rock begins to break. Substituting Eqs. (2) and (3) into Eq. (1) allows

\[
\sigma^1 + \sigma^2 = \sigma_t \quad \text{(at } r = R) \tag{1}
\]

where \( r \) and \( \theta \) are the cylindrical coordinates, \( R \) is the radial distance away from the fracturing wellbore at which the rock fractures, and \( \sigma_t \) is the rock tensile strength. The individual stress expressions for \( \sigma^1 \) and \( \sigma^2 \) are:

\[
\sigma^1 = \left(1 + \frac{r^2}{R^2}\right) \frac{R^2}{r^2} \left( \frac{\sigma_a + \sigma_c}{2} \right) - \left( \frac{\sigma_a - \sigma_c}{2} \right) \left(1 + \frac{R^2}{r^2}\right) \cos(2\theta) \tag{2}
\]

\[
\sigma^2 = \frac{R^2}{r^2} P \tag{3}
\]

When \( P \) arrives at the breakdown pressure, \( P_b \), the tangential stress near the fracturing wellbore reaches \( \sigma_t \) and the rock begins to break. Substituting Eqs. (2) and (3) into Eq. (1) allows \( P_b \) to be expressed as follows:

\[
P_b = \sigma_t - (3\sigma_c - \sigma_a) \tag{4}
\]

Equation (4) applies to aqueous fracturing, neglecting the pore pressure variation of the target rock strata near the wellbore. This is because it is difficult for the aqueous medium to permeate into the pores of the rock under fluid pressure, but after that, the fluid pressure accumulated slowly due to the high compressibility of CO₂.

The experimental results of fracturing with all the three fluids are presented in Table 3 for the fat coal, anthracite, and mudstone samples. As the table shows, the breakdown pressures of waterless fracturing were remarkably lower than that of water fracturing. Among the three fracturing fluids, the breakdown pressures in Sc-CO₂ fracturing were the lowest, which are 16.65%, 12.25% and 11.83% lower than L-CO₂ for the fat coal, anthracite, and mudstone samples, respectively, and 38.25%, 30.93% and 25.51% lower than hydraulic fracturing for the mid-rank coal. According to the classical failure criteria in hydraulic fracturing, when the tangential stress near the fracturing wellbore reaches the tensile strength of the coal or rock, the fracture forms and the corresponding fluid pressure in the wellbore is referred to as the breakdown pressure. The critical tangential stress includes the geological stress \( \sigma^v \) resulting from the two principal stresses \( \sigma_a \) and \( \sigma_c \), and the fluid stress \( \sigma^f \) induced by the fracturing fluid pressure, \( P \), in the wellbore. The equation for the stress near the fracturing wellbore is expressed as follows:

\[
\sigma^1 + \sigma^2 = \sigma_t \quad \text{(at } r = R) \tag{1}
\]

\[
\sigma^1 = \left(1 + \frac{r^2}{R^2}\right) \frac{R^2}{r^2} \left( \frac{\sigma_a + \sigma_c}{2} \right) - \left( \frac{\sigma_a - \sigma_c}{2} \right) \left(1 + \frac{R^2}{r^2}\right) \cos(2\theta) \tag{2}
\]

\[
\sigma^2 = \frac{R^2}{r^2} P \tag{3}
\]

Table 3. Fracturing test results for different fracturing fluids in the (a) fat coal (F\#), (b) anthracite (A\#) and (c) mudstone (M\#) specimens.
high stress conditions. Hence the effect of the pore water pressure on the breakdown pressure is not considered in classical hydraulic fracturing models. However, compared to the water, Sc-CO₂ and L-CO₂ have lower viscosity and surface tension, which facilitates penetration into the coal pores⁵⁰. The Sc-CO₂ or L-CO₂ penetration causes additional tangential pore stress, σₜ, around the fracturing wellbore⁵¹:

\[
\sigma_t^3 = \alpha (1 - 2\nu) \left[ \frac{1}{\pi^2} \int_R^\infty p(r)rdr - p(r) \right]
\]

where ν is the Poisson’s ratio of the rock, α is the Biot coefficient, defined as α = 1 – Kᵣ/Kₛ, where Kᵣ and Kₛ are the elasticity moduli of the bulk rock and the rock matrix, respectively, and p(r) is the pore pressure at a distance r from the fracturing wellbore. Based on Terzaghi’s effective stress principle⁴⁰, σₜ can be incorporated into Eq. (1) as follows:

\[
\sigma_t^3 + \sigma_r^2 + \sigma_θ^2 = \sigma_t - p \quad (at \ r = R)
\]

According to Eq. (5), p is equal to P at the fracturing wellbore wall, i.e., r = R. Therefore, σₜ becomes –Pr(1 – 2ν)/(1 – ν). Substituting this expression for σₜ into Eq. (6), the following expression for the breakdown pressure is obtained:

\[
P_b = \frac{\sigma_t - (3\sigma_c - \sigma_a)}{2 - \alpha(2\nu - 1)}
\]

Equation (7) allows the breakdown pressures of waterless fracturing to be calculated. Compared to Eq. (4) for water fracturing, Eq. (7) contains the extra multiplier factor 1/(2 – α(1 – 2ν)/(1 – ν)). Equation (7) shows that for rocks, ν varied between 0 and 0.5, and α is always less than 1 for rocks. Therefore, the factor 1/(2 – α(1 – 2ν)/(1 – ν)) ranges between 0.5 and 1. This explains why the breakdown pressures driven by L-CO₂ and Sc-CO₂ are lower than that induced by water.

**Crack propagation path and fracture surface topography.** Figure 7 compares the crack propagation paths in the three types of samples fractured by each fluid, with sketches of the induced fractures shown alongside photographs of the cylindrical samples for ease of comparison. As the figure shows, for water fracturing, macroscopic through-crack propagation occurred in the samples, whereas several secondary cracks were induced after L-CO₂ fracturing. For Sc-CO₂ fracturing, the number of induced cracks was much more than for the other two fracturing fluids, with a wide and complex fracture network appearing in the fractured specimens.

Measurements of fracture surface morphology were also carried out (Fig. 8). As the figure shows, the fractured specimens were split into two halves by the main crack, and the 3D scanner was used to measure the morphologies of the fractured surfaces in the portions without the fracturing boreholes, thereby mapping the three-dimensional coordinates of the induced fractures. This enabled the areas of the fracture surfaces to be calculated by multi-faceted function fitting of the morphology points. The three-dimensional roughness coefficient, Rₛₛ, of the fracture surface induced by the different fluids is defined as follows:

\[
Rₛ₄ = \frac{A₄}{A₃}
\]

where A₃ is the three-dimensional area of the fracture surface and A₄ is the projection area of the fracture surface. The larger the value of Rₛ₄, the more tortuous the crack surface. The Rₛ₄ values for the scanned specimens are listed in Table 4. As the table shows, for all three sample types the Rₛ₄ values of the fractures induced by Sc-CO₂ were largest and that by water fracturing were the lowest. Hence, the fracture surfaces induced by Sc-CO₂ are rougher and more tortuous. Among the three sample types, the Rₛ₄ values of the fat coal were larger than those of the anthracite for all the three fracturing fluids, and the Rₛ₄ values of mudstones are the lowest, which indicates that the lower the coal rank, the more tortuous the crack surface.

Further, the fracture apertures of the specimens under each experimental condition were determined by positional scanning, using the point-cloud data matching method proposed by Chen et al.⁴¹,⁴². This process is illustrated in Fig. 8. First, the spatial coordinates of the exterior surface of the fractured sample were captured by the 3D scanner (whose precision ranges from 0.01–0.02 mm) and selected as the reference position; next, the sample was opened up and both the fracture surfaces were scanned. By matching the reference position and coordinates of the two surfaces, the fracture aperture can be calculated based on the distances of each grid point:

\[
e_i = z_i^+ - z_i^-
\]

\[
e_m = \frac{\sum_{i=1}^{N} e_i}{N}
\]

where eᵢ is the vertical distance of each grid point, zᵢ⁺ is z-elevation of the top fracture surface and zᵢ⁻ is z-elevation of the bottom fracture surface; eₐ is the average fracture aperture, and N is the total number of grid points of the fracture surface. As shown in Table 4, the average single fracture apertures of the water-induced cracks were the largest among the different fracturing fluids for all three sample types. Compared to the high-rank anthracite coal, the fat coal specimens had wider fracture apertures regardless of fracturing fluid.

The viscosity of the fracturing fluid is one of the most important factors influencing the crack propagation path and fracture surface topography. The fluid with low viscosity is easier to permeate into the micro-pores, and
Figure 7. Crack propagation paths for the (a) fat coal, (b) anthracite, and (c) mudstone samples fractured by water, L-CO$_2$ and Sc-CO$_2$.
Figure 8. Fracture surface morphology and positional scanning.

Table 4. Roughness coefficients and the average fracture apertures for different fracturing fluids in the (a) fat coal (Fx#), (b) anthracite (Ax#) and mudstone (Mx#) specimens.

| Sample number | Fracturing fluid | Roughness coefficients $R_s$ | Average fracture aperture $e_m$ (mm) |
|---------------|------------------|-----------------------------|-------------------------------------|
|               |                  | Test value | Average value | Test value | Average value |
| (a)           |                  |            |               |            |               |
| F1<sub>water</sub> | Water            | 1.217      | 1.256         | 0.692      | 0.732         |
| F2<sub>water</sub> | Water            | 1.295      |               | 0.772      |               |
| F1<sub>L-CO</sub> | L-CO$_2$         | 1.256      | 1.317         | 0.575      | 0.618         |
| F2<sub>L-CO</sub> | L-CO$_2$         | 1.378      |               | 0.661      |               |
| F1<sub>Sc-CO</sub> | Sc-CO$_2$       | 1.433      | 1.506         | 0.401      | 0.426         |
| F2<sub>Sc-CO</sub> | Sc-CO$_2$       | 1.579      |               | 0.451      |               |
| (b)           |                  |            |               |            |               |
| A1<sub>water</sub> | Water           | 1.182      | 1.215         | 0.593      | 0.625         |
| A2<sub>water</sub> | Water           | 1.248      |               | 0.657      |               |
| A1<sub>L-CO</sub> | L-CO$_2$        | 1.203      | 1.276         | 0.488      | 0.513         |
| A2<sub>L-CO</sub> | L-CO$_2$        | 1.349      |               | 0.538      |               |
| A1<sub>Sc-CO</sub> | Sc-CO$_2$      | 1.391      | 1.423         | 0.378      | 0.406         |
| A2<sub>Sc-CO</sub> | Sc-CO$_2$      | 1.455      |               | 0.434      |               |
| (c)           |                  |            |               |            |               |
| M1<sub>water</sub> | Water           | 1.051      | 1.186         | 0.418      | 0.452         |
| M2<sub>water</sub> | Water           | 1.321      |               | 0.486      |               |
| M1<sub>L-CO</sub> | L-CO$_2$       | 1.107      | 1.205         | 0.317      | 0.368         |
| M2<sub>L-CO</sub> | L-CO$_2$       | 1.303      |               | 0.419      |               |
| M1<sub>Sc-CO</sub> | Sc-CO$_2$     | 1.258      | 1.321         | 0.213      | 0.255         |
| M2<sub>Sc-CO</sub> | Sc-CO$_2$     | 1.284      |               | 0.297      |               |
as such leads to the longer crack length and rougher fracture surfaces. Under temperature and pressure conditions of 15 MPa and 40 °C, respectively, the viscosity of Sc-CO₂ (69.56 μPas) is much less than those of L-CO₂ and water (621.56 μPas and 903.62 μPas, respectively)⁴³,⁴⁴. According to Philibert⁴⁵, the diffusion range of fracturing fluids in rocks may be represented by the average diffusion length, \(x_d\), from Einstein’s diffusion equation:

\[
x_d = \sqrt{4D_d \cdot t}
\]

where \(D_d\) is the diffusion coefficient of the fracturing fluid, whose values are \(2.71 \times 10^{-9}\) m²/s, \(1.08 \times 10^{-8}\) m²/s, and \(5.32 \times 10^{-9}\) m²/s for Sc-CO₂, L-CO₂, and H₂O, respectively, and \(t\) is the diffusion time. The \(x_d\) values calculated using Eq. (11) for the three fluids (with the average times taken for fracture initiation following fluid injection in each sample type used as the \(t\) values) were 3453.11 μm, 1916.25 μm, and 1081.85 μm for Sc-CO₂, L-CO₂ and water, respectively. Therefore, the diffusion range of Sc-CO₂ in the samples was much larger than that of water. This is consistent with the observation from Fig. 7, which shows that the Sc-CO₂ caused more widely distributed cracks.

The capillary effect is another important factor determining the propagation of induced cracks, as it affects the intrusion of fracturing fluid into the coal matrix. The fracturing fluids can only enter the pores of coal specimens once the pore diameter exceeds the critical pore diameter, \(d^*\), which is defined as follows:

\[
d^* = \frac{4\sigma_i \cos \theta}{P_e}
\]

where \(\sigma_i\) is the interfacial tension of the fracturing fluid in coal, \(\theta\) is the contact angle, \(P_e\) is the entry pressure. In coals, the entry pressure \(P_e\) is typically ~10 MPa, and the interfacial tensions of Sc-CO₂, L-CO₂, and water are 25 mN/m, 45 mN/m, and 55 mN/m⁴⁶. In addition, the contact angle of Sc-CO₂ and L-CO₂ is ~0°, while that of water is ~16°⁴⁷. From Eq. (12), the threshold diameter of pores for the permeation of Sc-CO₂ is 100 nm, whereas that for water is 211 nm. This suggests that Sc-CO₂ is capable of entering the coal matrix through smaller pores, which may explain why Sc-CO₂ fracturing leads to more extensive fractured areas.

Figure 9 shows scanning electron microscopy (SEM) images of the pore structures of the fat coal and anthracite samples at 43,000× magnification, obtained using a JIB-4700F (JEOL, Japan) instrument. During the SEM analysis, the coal samples were viewed under 15 kV voltage with a spot size of 4.5 under low vacuum mode. As the figure shows, the pore diameters of the two kinds of coals are generally between 100 and 200 nm (the pore diameter of the fat coal sample is about 100 nm, and the pore diameter of the anthracite sample is about 200 nm). Hence, Sc-CO₂ can enter the coal through the pores which can cause more extensive cracking, whereas it is more difficult for water to get into pore structure. Moreover, the pore diameters of the fat coal appear to be larger than those of the anthracite, which may explain the fact that the cracks induced by Sc-CO₂ in the former were more extensive than those in the latter (see Fig. 7).

**Permeability of the fractured coal specimens.** After the fracturing tests, the permeabilities of the fractured specimens were measured by steady-state flow methods⁴⁸,⁴⁹ under the same axial pressure as in the fracturing tests and the confining pressures were set to 4, 6, 8, 10 and 12 MPa. Nitrogen was used for the permeability measurements at a seepage pressure of 2 MPa to avoid absorption effects. Before the formal seepage experiment, Nitrogen is continuously injected into the fractured coal specimen for an hour to remove the fracturing fluid remaining in the fracture. The nitrogen flow in the fractures may be estimated using the following cubic equation⁵⁰:

\[
q = -\frac{e^3 \partial P}{12\mu \partial x}
\]
where $e$ is the fracture aperture, $\mu$ is the fluid viscosity coefficient, and $\partial P/\partial x$ is the pressure gradient of the fluid. Witherspoon et al.\textsuperscript{51} took into account the impact of the fracture roughness to modify Eq. (13), as follows:

$$q = -\frac{e^3 \partial P}{12 \mu} \frac{1}{\partial x} \frac{1}{1 + 6 \left( \frac{\Delta}{e} \right)^{1.5}}$$  \hspace{1cm} (14)

where $\bar{e}$ is the average effective hydraulic fracture aperture, and $\Delta$ is the average height of the coordinate point measured by the 3D scanner. The permeabilities of the cylindrical specimens both before and after the fracturing tests are given by Darcy’s law:

$$q = -\left( \frac{k \cdot A}{\mu} + \frac{1}{W_f} \right) \frac{\partial P}{\partial x}$$  \hspace{1cm} (15)

where $A$ is cross-sectional area of sample along the seepage direction and $k$ is the permeability; $1/W_f$ is the fluid compressibility. Substituting Eq. (14) into Eq. (15), the relationship between $\bar{e}$ and $k$ is established as:

$$\bar{e}^3 \frac{1}{12 + 72 \left( \frac{\Delta}{e} \right)^{1.5}} = k \cdot A$$  \hspace{1cm} (16)

The $\bar{e}$ values for the different specimens calculated using Eq. (16) are plotted in Fig. 10. As the figure shows, for the fat coal specimens, the value of $\bar{e}$ after Sc-CO$_2$ fracturing was 3.05 times greater than that after hydraulic fracturing and 2.18 times greater than after L-CO$_2$ fracturing. Similarly, for the anthracite specimens, the value of $\bar{e}$ after Sc-CO$_2$ fracturing was 3.75 and 2.49 times greater than after hydraulic and L-CO$_2$ fracturing, respectively. This means that Sc-CO$_2$ can greatly increase the permeability of coals compared to the other two fluids, which is beneficial to CBM recovery. There are two possible mechanisms that can explain the greater effective hydraulic apertures induced by Sc-CO$_2$ compared to the other two fluids. Firstly, Sc-CO$_2$ fracturing may release more energy which produces more cracks in coal specimens, resulting in substantial increase in permeability. Secondly, Sc-CO$_2$ can seepage through smaller pore than the other two fluids, causing greater damage and micro-cracking to the solid matrix. This second mechanism works as follows: during the fracturing and crack propagation processes, Sc-CO$_2$ enters small pores and weakens the mineral cementation; as a result, mineral grains may be peeled off from the fracture surface and remain in the induced fractures, thus keeps the cracks open against closure stresses. Moreover, the $\bar{e}$ values of the fat coal specimens were greater than those of anthracite specimens, and showed a steady decrease with increasing effective stress (Fig. 10).

Conclusions
In this study, fracturing experiments were conducted with two different kinds of coal (fat coal and anthracite) and one type of mudstone. Three different fracturing fluids are adopted, including water, liquid CO$_2$ (L-CO$_2$), and supercritical CO$_2$ (Sc-CO$_2$). The fracture surfaces induced by the different fluids were 3D scanned to quantify the roughness and the fracture apertures of the specimens. Furthermore, the permeabilities of the specimens were measured after fracturing. The main conclusions from this study are summarized as follows:

1. The breakdown pressures of waterless fracturing in the coal specimens were significantly lower than that of hydraulic fracturing. Among them, the breakdown pressures of Sc-CO$_2$ fracturing is the lowest, 16.65%, 12.25%, and 11.83% lower than L-CO$_2$ fracturing and 38.25%, 30.93% and 25.51% lower than water hydraulic fracturing for the fat coal, anthracite, and mudstone specimens, respectively. Moreover, the high-rank...
anthracite specimens exhibited higher breakdown pressures than the mid-rank coal fat coal specimens for all three fracturing fluids.

2. Sc-CO$_2$ fracturing induced far more cracks than L-CO$_2$, and formed wide and complex fracture networks. Measurements of fracture surface morphology were carried out, which showed that the three-dimensional roughness coefficient, $R_s$, of the fractures induced by Sc-CO$_2$ were larger than those caused by the other two fracturing fluids for all three samples types. Therefore, the fracture surfaces created by Sc-CO$_2$ are rougher and more tortuous. Meanwhile, the $R_s$ values for the fat coal were greater than those for the anthracite regardless of fracturing fluid, which indicates that more tortuous crack surfaces may take place in lower rank coals. Moreover, the fracture apertures of the specimens were determined by positioning scanning, whose results shows that the average single fracture apertures of the ScCO$_2$-induced cracks were the smallest amongst the three fracturing fluids.

3. Viscosity of the fracturing fluid is the key factors influencing the crack propagation path and fracture surface topography. The diffusion lengths of Sc-CO$_2$, L-CO$_2$, and water were estimated to be 3453.11 µm, 1916.25 µm, and 1081.85 µm, respectively; hence, the diffusion range of Sc-CO$_2$ in the specimens is larger than the other two fluids. The capillary effect is another critical factor that influences the propagation of induced cracks, as it has a bearing on the intrusion of fracturing fluid into the coal matrix. The threshold pore diameters that allow the permeation of Sc-CO$_2$ and water into the coal body were estimated to be 100 nm and 211 nm, respectively, suggesting that Sc-CO$_2$ is more likely than water to permeate into the coal matrix through smaller pores during the fracturing fluid injection. Hence, the more extensive fractured area as seen in the specimens injected with Sc-CO$_2$ may be attributed to these two factors (i.e. diffusion length and capillary effects).

4. For the fat coal specimens, the effective hydraulic aperture, $\varepsilon$, caused by Sc-CO$_2$ fracturing was 3.05 times larger than that caused by water fracturing and 2.18 times greater than that induced by L-CO$_2$ fracturing. Similarly, for the anthracite specimens, the $\varepsilon$ value caused by Sc-CO$_2$ fracturing was 3.75 and 2.49 times greater than water and L-CO$_2$ fracturing, respectively. These results demonstrate that Sc-CO$_2$ fracturing considerably improves the permeability of coals and is therefore beneficial to CBM recovery.

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J.Y. carried out the study and drafted manuscript, H.L. supervised, revised, reviewed and conceptualized the manuscript, and L.L. reviewed and proofread the paper.

Competing interests
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