Linguistic Annotation of Neo-Latin Mathematical Texts: a Pilot-Study to Improve the Automatic Parsing of the Archimedes Latinus

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Abstract
This paper describes the process of syntactically parsing the Latin translation by Jacopo da San Cassiano of the Greek mathematical work The Spirals of Archimedes. The Universal Dependencies formalism is adopted. First, we introduce the historical and linguistic importance of Jacopo da San Cassiano’s translation. Subsequently, we describe the deep Biaffine parser used for this pilot study. In particular, we motivate the choice of using the technique of treebank embeddings in light of the characteristics of mathematical texts. The paper then details the process of creation of training and test data, by highlighting the most compelling linguistic features of the text and the choices implemented in the current version of the treebank. Finally, the results of the parsing are discussed in comparison to a baseline and the most prominent errors are discussed. Overall, the paper shows the added value of creating specific training data, and of using targeted strategies (as treebank embeddings) to exploit existing annotated corpora while preserving the features of one specific text when performing syntactic parsing.

Keywords: Dependency parsing, Latin mathematical language, Universal Dependencies

1. Introduction
Jacopo da San Cassiano (1395-1494) translated most of the archimedean corpus from Ancient Greek to (Neo-)Latin around 1450 probably on the orders of Pope Nicholas V (d’Alessandro and Napolitani, 2012). The works of Archimedes, alongside Euclides’ Elements, are considered a pillar of Hellenistic, and, in general, Greek mathematics (Heath, 1921). Jacopo’s translation became a crucial medium for the rediscovery of Greek mathematics (Heath, 1921). Jacopo’s translation was considered necessary to properly understand such a difficult work. Unlike modern mathematical texts, that rely heavily on symbolic notation, Ancient Greek mathematical texts are entirely written in plane natural language. Expressions that nowadays are rendered as ‘AB:CD=DE:EF’ were expressed as ‘the line AB has to the line CD the same proportion that DE has to EF’. This creates an extremely peculiar variety of Ancient Greek (Acerbi, 2011; Acerbi, 2012; Netz, 2003), translated to Latin by Jacopo adopting the same style. The study of the linguistic features of Jacopo’s translation hasn’t been undertaken until now. Nonetheless, the creation of a treebank of this corpus is promising for different reasons:

• The text features a variety of Latin rarely targeted by linguistic studies and underrepresented in linguistic resources.

• The adaptation of the Latin language for translating the Greek of mathematics poses unique challenges.

• The availability of linguistically annotated Renaissance texts is still limited.

By creating the Archimedes Latinus treebank we aim at investigating the syntactic peculiarities of mathematical (Neo)-Latin. Given the success of the Universal Dependencies (UD) initiative (Nivre et al., 2016), and the large treebank availability (160), the Latin Archimedes treebank adopts the UD formalism. In addition, the recently created UDante treebank (Cecchini et al., 2020a) represents a milestone for Latin UD annotation. In fact, it is the first “native” UD treebank and its creation has generated the first (not-yet complete) language-specific guidelines for Latin. Regularity is one of the most striking features of mathematical language, since a handful of terms and syntactic structures, indicating mathematical objects and relations, constitute the bulk of the text. Hence, we aim at verifying whether a syntactic parser, trained on a part of Jacopo’s translation, can successfully parse the rest of the corpus, or at least reach results that significantly accelerate the post-correction for the treebank creation. This paper is structured as follows: section 2 describes the syntactic parser that we have finetuned for this study and introduces the concept of treebank embedding; section 3 describes the creation of training and test data; section 4 discusses the results of the parsing.

2. Parser
Treebank (or dataset) embeddings have been developed by (Stymne et al., 2018) on the ground of (de Lhoneux et al., 2021).
et al., 2017), in order to tackle the problem of training a monolingual dependency parser using heterogeneous treebanks. In fact, different UD treebanks for the same language might differ on specific aspects of the UD formalism: for instance, on the choice of the PoS for non clear-cut categories such as DET and PRON (see discussion below). Such inconsistencies might cause poor performances of parsers trained on multiple treebanks (Stymne et al., 2018). Treebank embeddings are used to prioritize, when parsing a new text, the conventions of one of the treebanks used for the training. To this goal, during training, a treebank embedding is concatenated to each word and thus one representation is learned for each of the treebank used. The representation is the same for every token of one treebank and differs from one treebank to another. When parsing a new text, a treebank identifier is given and the sentences get parsed following the ‘style’ of the chosen treebank. This method allows to take advantage of large training sets without overlooking treebank-specific features. The same method has been exploited to use treebanks of related languages during the training of a dependency parsing model (Smith et al., 2018). By applying this method to our case, we aim at verifying whether the parser picks up the specific, ‘regular’, features of the mathematical text while taking advantage of other existing treebanks. Hence, we train a multitask model to predict Parts-of-Speech (POS) and parse the text. We use the deep biaffine parser (Dozat and Manning, 2017) implementation of MaChAmp (van der Goot et al., 2021) with the use of dataset embeddings in the encoder introduced in (van der Goot and de Lhoneux, 2021). The parser uses mBERT (Devlin et al., 2019) as an encoder, and a dataset embedding is concatenated to the embedding of each wordpiece before it is passed to the decoder.

3. Data Creation

3.1. Text extraction and tokenization

B. Sisana, a scholar specializing on Jacopo’s work, has shared the critical edition of the whole corpus of Jacopo’s archimedean translations, as contained in the the manuscript Nouv. Acq. Lat. 1538 (Paris, Bibliothèque nationale) identified as the autograph (d’Alessandro and Napolitani, 2012). The text is edited using MauroTeX, a specific mark-up language developed for the edition of mathematical text. Via a Python script, the text of the Spirals (on which this pilot study focusses) was extracted from the TeX file. The tokenization and an automated PoS tagging have been performed using the Pie Latin LASLA+ model 0.0.6 (Manjavacas et al., 2019), fine-tuned on ca. 1,500,000 tokens taken from the LASLA Latin corpus (Clérice, 2021).

3.2. Creating training data and test data

A training and test sets of sentences of The Spirals have been created. They both qualify as Gold Standard since they have been manually annotated by a Latin philologist. The training set consists of the first 48 sentences of the book (1307 tokens), while the test set consist of 30 sentences taken from Propositions XIX and XX of the same book (913 tokens). The automatic PoS tagging of the Pie Latin LASLA+ model 0.0.6 has been corrected using Pyrrha, a language independent post correction app for PoS and lemmatization (Clérice et al., 2019). The PoS tagset used in Pyrrha has been converted to the Universal PoS tagset (Petrov et al., 2012) adopted in the UD initiative. At this point, the annotation of mathematical letters remains an open challenge. In fact, to indicate points, lines, circumferences and other mathematical objects, Ancient Greek authors use letters, in expression such as ‘the line AB’, often reduced to ‘the AB’. In Greek manuscripts, a line is traced on the top of the letters. Jacopo follows the same convention, adding to dots around the string of letters, as visible in Figure 1. Recent studies have argued that these (groups of) letters have the purely linguistic anaphoric value of labels, since they allow to refer unambiguously to the same mathematical object across the same proof (Acerbi, 2020). This goes against the theory according to which their primary goal is to identify specific points in a diagram. It is thus not obvious whether the string of letters can be considered as a single token and what PoS should be assigned to it. Based on the graphic evidence of the manuscripts, we decided to keep the forms as a single token, instead of considering each letter as separate token corresponding to a point. The PoS has been left undetermined at this stage (X), but will be assigned either to NOUN or SYM following additional discussions with UD experts. In fact, UD guidelines assign the PoS SYM to

\[ \text{in tempore } gk \]

Figure 1: Snippet of the Nouv. Acq. Lat. 1538 ‘in tempore gk’
of the head is arbitrary since the two words do not hold a head-modifier relation. The length of sentence represents a second challenge: the digitized text is, in fact, the direct transcription of a Renaissance manuscript. Manuscripts tend to record only minimal punctuation (Parkes, 1992), and the transcription sticks to the original layout. This entails extremely long sentences, whose clauses are rarely separated by commas: in the test set, the median length is of 21.5 words with a maximum of 104, resulting in syntactic trees with a median depth of 5.5 layers. This will be addressed for the final version of the treebank, by adding punctuation as modern editors regularly do. The lack of punctuation entails additional difficulties in analyzing the role of Latin particles in the sentence. Words such as enim (‘namely’, ‘indeed’), autem (‘however’, ‘on the other hand’), rursus (‘on the contrary’), can both linking clauses belonging to the same sentence or link one sentence with the preceding one, structuring the discourse (Kroon, 1995). In very long sentences composed of a number of juxtaposed clauses, it is challenging to establish whether the tuple (verb, particle) should receive the DEPREL ‘cc’ in case the particle functions as coordinating conjunction, or ‘discourse’ when functioning as discourse marker.

4. Training and evaluation

Once the training data and test data have been created, the Biaffine parser is again trained on the cluster of ancient languages described above, with the addition of the newly created mathematical training data. For the prediction of the PoS tags, the mathematical training data, the treebanks, and the UD versions of the LASLA corpus are used as training data. The model is trained for 80 epochs. The Unlabeled Attachment Score (UAS) measures the correctness of the syntactic structure (EDGES), whereas the Labeled Attachment Score (LAS) includes also the evaluation of the label attached to the dependency (DEPRELS obl, obl:cmpr and obl:arg all count as obl). Table reports the LAS and UAS scores computed on the test data processed with this.

few exceptions will be corrected in the final version of the Treebank.

The LASLA corpus is a morphosyntactically manually annotated corpus of Latin classical texts (Denooz, 1978), see http://web.philo.uig.ac.be/lasla/presentation-du-laboratoire/. The LASLA data were converted to UD by Flavio M. Cecchini, CIRCSE, Università Cattolica di Milano. A sample of these data has been used in the frame of Evalatin2022, https://circse.github.io/L4HALA/2022/Evalatin.

The model will be shared soon.

For this pilot study, the LAS was computed on first-level relations only, without considering any subrelation (e. g., the DEPRELS obl, obl:cmpr and obl:arg all count as obl).

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1. https://universaldependencies.org/guidelines.html
2. In particular, Flavio M. Cecchini, CIRCSE, Università Cattolica di Milano.
3. https://universaldependencies.org/u/dep/
4. https://universaldependencies.org/u/dep/flat.html
5. https://universaldependencies.org/u/dep/flat.html
6. The UD guidelines indicate that the first of the two words linked by the ‘flat’ DEPREL should be used as head. The
parser (‘Archimedes’) and with UDPipe using the UD v. 2.6 for Latin (baseline).

| Model     | PoS | UAS   | LAS   |
|-----------|-----|-------|-------|
| Biaffine  | 91.25 | 72.43 | 59.85 |
| Archimedes|      |       |       |
| IT-TB     | 68.60 | 55.03 |       |
| Perseus   | 68.16 | 50.44 |       |

Table 1: UPOS, UAS and LAS score of different parsers

The results show a significant gain with respect to the UDPipe IT-TB model, 3.83 UAS points and 4.82 LAS points. The results can still be improved significantly: at the moment such procedure can only be effectively use as a first step to accelerate the following manual annotation. Nevertheless, it seems that a multi-task learning setup is well suited to using multiple sources of data to facilitate the annotation of a new dataset. Additionally, dataset embeddings facilitate annotating new data in the style of a specific treebank.

In order to measure the impact of the addition of mathematical texts and the use of the ‘mathematical embedding’ on the performance of the Biaffine parser, we also evaluated the performance of the Biaffine parser with the training described in Section 3.2 on a very brief portion of text (ca 400 tokens, propositions VII-VIII). The results on UAS and LAS (resp. 70.56 and 58.63) outperform UDPipe, but are lower than those obtained in the final stage. However, we should mention that this test-set might not be representative, since some complex sentences had to be removed due to editorial issues. The annotation of PoS scores quite high (95.6): the result, higher than with the addition of mathematical texts, can be explained by the absence, in this portion of text, of the term spiralis (‘spiral’), which is the main source of errors for the final test-set (see below).

5. Error analysis

To complement the scores, we performed an analysis of the errors on the POS, dependencies and labels. The confusion matrix of the PoS is shown in Figure 2. The most frequent error is due to the mislabeling of spiralis (‘spiral’) as NOUN in the expression linea spiralis (‘spiral line’), where it is an ADJ. The second most frequent source of errors is the confusion between DET and PRON, which is mostly due to linguistic ambiguity, given that the same words, such as ille (‘that’, ‘that person’) or iste (‘this’, ‘this person’), can be used with both functions.

Out of the 253 cases of wrong head assignment, 57 concern mathematical labels, which is a highly specific feature of our text. In the subset of corrected predicted dependency, the most common error in DEPRELS assignment (15 times out of 127 errors) is ‘nmod’ instead of ‘flat’, always between a mathematical term and its label. As it appears, most of the errors generate from the mathematical content of the text.

6. Conclusion

The linguistic annotation of non-classical, non-literary varieties of Latin poses major challenges, both because of the difficulty of adapting existing guidelines to these texts and because of the lack of well-suited annotated data and tools to automate the process. In this pilot study we have shown the added value of creating specific training data, and of using targeted strategies (as treebank embeddings) to jointly exploit existing annotated corpora without losing the features of one specific text. Such strategy beats baseline results, and appears promising for the future. As next steps, the performance of the parser will be improved by assigning PoS to mathematical labels in the training data and by increasing the amount and variety of training data from Jacopo’s translation of different work of Archimedes. In a second stage, we will manually correct the output of the parser to provide a treebank of Jacopo’s translation of at least one complete work of Archimedes. Finally, the completion of such project will result in the...
contribution to the guidelines for the UD-style annotation of Latin, in particular scientific Latin.

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