Abstract. We propose a new way to detect individual bright Ultra-High Energy Cosmic Ray (UHECR) sources above background if the Galactic Magnetic Field (GMF) gives the main contribution to UHECR deflections \[1\]. This method can be directly applied to maps given by experiments. It consists in starting from at least two high energy events above \(6 \times 10^{19}\) eV, and looking at lower energy tails. We test the efficiency of the method and investigate its dependence on different parameters. In case of detection, the source position and the local GMF deflection power are reconstructed. Both reconstructions are strongly affected by the turbulent GMF. With the parameters adopted in this study, for 68% of reconstructed sources, the angular position is less than one degree from the real one. For typical turbulent field strengths of \(4 \mu G\) at the Earth position and 1.5 kpc extension in the halo, one can reconstruct the deflection power with 25% precision in 68% of cases.

Keywords: ultra-high energy cosmic rays, magnetic fields, Galaxy.

I. INTRODUCTION

The HiRes experiment first observed the cutoff in the spectrum \[2\]. The UHECR sources are still unknown. Some possible candidates can be studied from the point of view of acceleration mechanisms -see for example Refs. \[3\], \[4\], \[5\].

Their detection is difficult due to the UHECR deflections in the extragalactic and Galactic magnetic fields. One can either wait for enough data at the highest energies to find a class of UHECR sources, or search for the first individual brightest sources. In this study, we investigate this second possibility.

We propose here a method to find Ultra-High Energy (UHE) proton or light nuclei sources on top of background and reconstruct their positions. We show that one has to start from at least two events with energies above \(10^{19.5}\) eV \(-\sim 6 \times 10^{19}\) eV before looking at lower energy tails, in order to avoid confusion by the background. We investigate the performance of this method depending on the different relevant parameters.

We assume as in \[6\] that UHECR deflections due to the extragalactic magnetic fields are negligible compared to those due to the GMF. For an example of non negligible extragalactic contributions, see \[7\]. The GMF is divided into two components: regular and turbulent. For the regular one, we take the Prouza and Smida model \[8\], \[9\]. It consists of a thick disk, and of toroidal and dipolar fields. Following the latest knowledge on the GMF \[10\], \[11\], we modify some parameters and take an exponentially decaying profile along the Galactocentric radius. The field strength close to the Sun is \(B_{\text{reg}} = 1 - 3 \mu G\) (currently admitted strength: \(B_{\text{reg}} \approx 2 \mu G\)). The model for the turbulent component is described in \[11\]. The root mean square (RMS) value of the turbulent field decays as \(1/r\) along the Galactocentric radius \(r\), and exponentially along the direction orthogonal to the Galactic plane. The plane thickness is set here to 1.5 kpc. The turbulent field strength close to the Sun is \(B_{\text{turb}} = 2 - 8 \mu G\) (currently admitted strength: \(B_{\text{turb}} \approx 4 \mu G\)).

For source events, we assume power law acceleration spectra, with a power law index equal to 2.2 and a maximum energy set to \(10^{21}\) eV. In most cases, we take a proton source and set its distance to the Earth to \(50 - 100\) Mpc. In the most cases, we take a proton source and set its distance to the Earth to \(50 - 100\) Mpc. Protons are propagated to the observer by using the results of Ref. \[12\] for energy losses, which creates a “bump” in the source spectrum \[12\]. Then, the generated cosmic rays (CR) are deflected in the regular GMF (see e.g. \[14\]), and in the turbulent GMF. For more details on turbulent GMF deflections, see Refs. \[15\], \[11\]. The effects of both components are shown in Fig. 1.
The regular component deflects the CR along a curve and the turbulent one spreads them “randomly” around it in a sector-shaped region. When there are many events with the same energies, they are not spread uniformly, as discussed in References [14], [15], [16]. Results depend on many parameters of the model and on the considered location on the sky. However, in practice, there are only two essential parameters: The local deflection powers -see Ref. [1]- of the regular GMF (denoted $D$) and of the turbulent GMF. Background events are simulated according to the energy spectrum measured by HiRes [2] and the exposure of Telescope Array [7].

II. METHOD

The following work is done on sky maps which only display events with energies bigger than a given threshold, $E_{th}$. The idea is to look for tails of lower energy events around at least two nearby events with energies $E > 10^{19.8}$ eV.

We start by taking a circle around an event with $E_1 > 10^{19.8}$ eV. Its radius $R$ can be optimized and the value we take depends, among others, on $E_{th}$ and $D$. We will call $R$ an “internal” parameter of the method. The tail of lower energy events is searched by assuming that all events from the source are located in a sub-region of the circle, that has a sector shape with a central axis given by the second highest energy event. The energy $E_2 \leq E_1$ of the second highest energy event is above a given threshold $E_2 \geq E_{2\text{min}}$, and its distance to the highest energy event must be compatible with an emission from the same source. This distance should be lower than $\beta D/E_2 - D/E_1$, where $\beta$ is another internal parameter, and $D$ is the value initially assumed for the local deflection power. Fig. 2 shows the probability to detect the source and the probability to be confused by some background. Results presented for a source of luminosity above $10^{19.6}$ eV equal to 2.6% of the total luminosity in UHECR, $E_{th} = 10^{19.3}$ eV, 5000 events above $10^{19}$ eV in the whole sky, $B_{\text{reg}} = 2 \mu$G and $B_{\text{turb}} = 4 \mu$G.

![Fig. 2: Dependence on $E_{2\text{min}}$, the minimum energy for the second highest energy event. Thick solid line for the probability to detect the source. Thin solid line for the probability to detect some background. Results presented for a source of luminosity above $10^{19.8}$ eV equal to 2.6% of the total luminosity in UHECR, $E_{th} = 10^{19.3}$ eV, 5000 events above $10^{19}$ eV in the whole sky, $B_{\text{reg}} = 2 \mu$G and $B_{\text{turb}} = 4 \mu$G.](image)

III. STUDY OF THE PARAMETER SPACE

We study below how the efficiency of the method presented above changes with values of physical or experimental parameters. There are two requirements for source detection. First, the probability to detect the source doublets has to be large enough, in order not to remove too much source signal. Second, the probability to be confused by some background has to be low enough compared to the probability to detect the source signal.

We define here a “cluster” as a group of at least three nearby events with very high energies, $E > 10^{19.8}$ eV. The probability to have a cluster of background events is very low in case of reasonable statistics and no -or low- anisotropy. For example it is $\sim 1\%$, with 5000 events in the whole sky above $10^{19}$ eV and no anisotropy. On the contrary, the probability to have a background doublet of very high energy events is, in most cases, not negligible compared to the probability to have a source doublet. That is why we separate the two cases -doublet or cluster- below. In case of a doublet, we apply the method depicted in the previous section, whereas in case of a cluster, we do not need it since the source is already detected in $\sim 99\%$ of cases. Applying the method reduces the background more than the signal from the source, but its side-effect is to reduce the signal from the source in any case. That is why it is not worth applying it when the probability to be confused by some background is already very low. However, when statistics increase, or in case of a large anisotropy above $6 \times 10^{19}$ eV, background clusters become more frequent and the method would then also
that even for the largest field strengths in these ranges, the ability of the method to detect the source is still quite acceptable. The difference between the dashed and the thin solid lines shows the efficiency to remove the background. The difference between the dashed-dotted and the thick solid lines is smaller: The source signal is less removed than the background. The difference between dotted and dashed-dotted lines corresponds, in practice, to cases when the source is already detected thanks to clusters of events.

These results are computed for an isotropic sky, even at the highest energies. We checked that for reasonable values of anisotropies (if all events with energies above $10^{19.8}$ eV are located in a fraction of the sky larger than 25%), results would be affected in a linear way. For example, in the case of a 25% fraction, the probabilities to have a background doublet and to detect it would be both approximately multiplied by 4.

We have studied the dependence on source parameters. We show in Ref. [1] results for the dependence on the source luminosity. We point out that with a regular GMF deflection power, for example close to $D \sim 5^\circ \times 10^{19.6}$ eV for protons, one can still detect a light nuclei source, but only by looking for clusters if the source luminosity is sufficient. In this case, the ratio “signal/background” for doublets would be too small to detect such sources. We have also presented results on the dependence on experimental statistics. There is no clear and no general best energy threshold $E_{th}$ to look for lower energy tails of events. When $E_{th}$ is decreased, the probability to detect a source doublet through the method increases, but the probability to be confused by a background doublet increases with a larger rate. For the example considered in Ref. [1], $E_{th} = 10^{19.6}$ eV $\approx 4 \times 10^{19}$ eV is a good compromise between sufficient source detection and sufficient background rejection.

The impact of the total amount of experimental data mostly affects the way the detection should be done, depending on the source luminosity. For example, with a bright source and large statistics like $10^4$ events above $10^{19}$ eV, clusters of source events appear more often and looking for them becomes a more efficient way to track the source than applying the method for doublets. However, when the amount of data still increases, the method used previously for doublets will also start to be needed for clusters, so as to reject background ones.

IV. RECONSTRUCTION OF THE SOURCE POSITION AND OF THE REGULAR GMF DEFLECTION POWER

In this section, we discuss the ability of the method to reconstruct the source position and the local regular GMF deflection power $D$.

With the assumptions considered here, and $B_{turb} = 4 \mu G$, the position of a source located in a region of the sky where $D \sim 5^\circ \times 10^{19.6}$ eV can be reconstructed with an accuracy of 1 degree in about 68% of cases - see distribution with thick solid line in Fig. 5. Thus, the angular resolution of this method for the source position

The figures 3 and 4 show the dependence of results on the regular and turbulent GMF strengths. Fig. 3 is computed for different strengths of $B_{reg}$ between 1 and 3 $\mu G$, and with a constant ratio between regular and turbulent field strengths. For Fig. 4 $B_{reg} = 2 \mu G$ and the turbulent field strength $B_{turb}$ varies between 2 and 8 $\mu G$. The internal parameters of the method have been optimized for each field strength. The dotted line is the probability that a proton source of luminosity above $10^{19.8}$ eV is located in a fraction of the sky larger than 26%. The dotted line shows the efficiency to remove the background. The difference between the dashed-dotted and the thick solid lines is smaller: The source signal is less removed than the background. The difference between dotted and dashed-dotted lines corresponds, in practice, to cases when the source is already detected thanks to clusters of events.

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For these lower
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68% of cases, as shown in Fig. 6—see thick solid line.

The above results are mainly spoiled by the turbulent
ponent can be reconstructed with up to 25% precision in
68% of cases. The local deflection power can be known
in a region of the sky where $D \sim 5 \times 10^{19.6}$ eV. Thin solid
line for no turbulent component ($B_{turb} = 0 \mu G$), dashed line
for $B_{turb} = 2 \mu G$, and thick solid line for $B_{turb} = 4 \mu G$.


Fig. 6: Distribution of reconstructed deflection powers in $^\circ \times 10^{19.6}$ eV. Same parameters and line types as in Fig. 5.

reconstruction is of the order of the experimental angular
resolution.
Another noticeable result is that, in the same conditions,
the local deflection power $D$ of the regular GMF component can be reconstructed with up to 25% precision in
68% of cases, as shown in Fig. 6—see thick solid line.
The above results are mainly spoiled by the turbulent
field. For comparison, we put in the same plots the
distributions with $B_{turb} = 0 \mu G$ (thin solid line) and
$B_{turb} = 2 \mu G$ (dashed line). The lower the turbulent
field strength, the better the precision on both results.
For these lower $B_{turb}$ strengths, the distance on the sky
between the reconstructed and the real sources would be
mostly affected by the experimental angular resolution
and not by the method.
The strength of the regular field (for $B_{reg} = 1 - 3 \mu G$
at the Sun position) does not change the precision on
the reconstruction of $D$, but the precision on the source
position reconstruction is better for low $B_{reg}$ values.
If we simulate the experimental resolution on energies
by taking values such as $\Delta E/E \sim 20\%$ instead of
$\Delta E/E = 0$ (theoretical energies), no noticeable change
can be seen in our results.

V. CONCLUSION

We have proposed and studied here an alternative
way to detect individual bright UHECR sources, if
the UHECR deflections due to the turbulent GMF are
not too large compared to the deflections due to the
regular component. We generated two sets of events:
Events from a source with a $1/E^{2.2}$ injection spectrum
that we propagated from the source to the Earth, and
events from some background generated according to
the HiRes spectrum and the Telescope Array exposure.
We mixed both sets of events, tried to detect the source
and checked how often we got confused by detecting
some background.
We showed that one should look for doublets of events
with $E > 10^{19.8}$ eV, when using the depicted method.
We studied in section III the dependence on several
parameters: Unknown parameters from the magnetic
fields, the source, the sky anisotropy at high energies and
the experimental statistics. We showed in section IV
that with the parameters and assumptions adopted here,
the precision on the source reconstruction would be
dominated by the current experimental angular resolution
in 68% of cases. The local deflection power can be known
up to 25% in 68% of cases.
In the future, this method can be applied to experimental
data so as to find bright UHECR proton or light nuclei
sources.

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