Fragment Dynamics in Active Asteroid 331P/Gibbs

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Abstract

We present a dynamical analysis of the fragmented active asteroid 331P/Gibbs. Using archival images taken by the Hubble Space Telescope from 2015 to 2018, we measured the astrometry of the primary and the three brightest (presumably the largest) components. Conventional orbit determination revealed a high degree of orbital similarity between the components. We then applied a fragmentation model to fit the astrometry, obtaining key parameters including the fragmentation epochs and separation velocities. Our best-fit models show that Fragment B separated from the primary body at a speed of ∼1 cm s⁻¹ between 2011 April and May, whereas two plausible scenarios were identified for Fragments A and C. The former split either from the primary or from Fragment B, in 2011 mid June at a speed of ∼8 cm s⁻¹, and the latter split from Fragment B either in late 2011 or between late 2013 and early 2014, at a speed of ∼0.7–0.8 cm s⁻¹. The results are consistent with rotational disruption as the mechanism causing the cascading fragmentation of the asteroid, as suggested by the rapid rotation of the primary. The fragments constitute the youngest known asteroid cluster, providing us with a great opportunity to study asteroid fragmentation and formation of asteroid clusters.

Unified Astronomy Thesaurus concepts: Asteroid belt (70); Solar system (1528); Asteroids (72); Small Solar System bodies (1469); Main-belt comets (2131); Comets (280)

1. Introduction

Active asteroids are a newly discovered class of small solar system bodies having dual characteristics of both comets and asteroids. While their orbits are dynamically asteroidal (Jupiter Tisserand invariant \( T_J \geq 3.08 \); Jewitt et al. 2015), they are observed to show cometary features visually similar to ordinary comets. The existence of active asteroids challenges the traditional view of comets and asteroids as two distinct classes of small solar system bodies. Since the discovery of the prototype active asteroid 133P/Elst-Pizarro (Hsieh & Jewitt 2006), more than two dozen active asteroids have been identified (Jewitt & Hsieh 2022). However, while their cometary morphology unequivocally indicates mass loss, several different physical mechanisms are responsible for the observed activity, including the sublimation of water ice, impact, rotational disruption, and thermal fracturing (e.g., Jewitt & Hsieh 2022). The enigmatic population still remains poorly understood to date.

Active asteroid 331P/Gibbs was discovered in 2012 (Gibbs et al. 2012). Its orbit lies in the outer main belt, with semimajor axis \( a = 3.01 \) au, eccentricity \( e = 0.04 \), and inclination \( i = 9°77 \), corresponding to a Jupiter Tisserand invariant of \( T_J = 3.23 \). The observed mass loss from 331P was at first interpreted to result from an impulsive event, consistent with an impact origin, estimated to have occurred in 2011 July (Stevenson et al. 2012; Moreno et al. 2012). Deep imaging with the Keck telescope in 2014 revealed four fragments embedded in a diffuse particle trail, in addition to the kilometer-sized primary nucleus, the latter with a rotation period of \( 3.26 \pm 0.01 \) hr (Drahus et al. 2015). Deeper imaging with the Hubble Space Telescope (HST) from 2015 to 2018 revealed a wealth of detail, including 19 fragments with radii in the range 0.04–0.11 km (geometric albedo 0.05 assumed), one of which (331P-A) is a likely contact binary (Jewitt et al. 2021). The fragments follow a size distribution with a differential power-law index of \( \gamma = 3.7 \pm 0.1 \) to \( 4.1 \pm 0.1 \), have a combined mass of approximately 1% the mass of the primary, and ejection velocities are crudely estimated as \( \sim 10 \) cm s⁻¹ (Jewitt et al. 2021). Intriguingly, 331P is also a member of a dynamical family with a separation age of \( 1.5 \pm 0.1 \) Myr, but no other active asteroids from the young cluster have been found (Novaković et al. 2014). The relationship between the current mass loss from 331P, and the catastrophic event that gave birth to the asteroid cluster, if any, remains unclear.

In this paper, we analyze the same archival HST observations as in Jewitt et al. (2021) but with the prime objective being to study the dynamics of the fragments. We detail the observations and data reduction in Section 2, present the astrometric and dynamical analyses in Section 3, the results in Section 4, and a summary in Section 5.

2. Observations and Data Reduction

We collected archival HST observations of active asteroid 331P taken under General Observer programs 14192, 14475, 14798, and 15360 (PI: M. Drahus) using the HST Data Search³ in the Mikulski Archive for Space Telescopes. The target was imaged from eight different epochs by HST’s Wide Field Camera 3 (WFC3), which houses two 2k x 4k pixel CCDs separated by a 31 pixel gap and has an image scale of 0°04 pixel⁻¹ in the UVIS channel (Dressel 2022). The long-pass F350LP filter, having effective wavelength 5846 Å, FWHM 4758 Å, and maximum throughput \( \sim 29\% \), was used for all of the images. Because the telescope was tracked at the nonsidereal rate of 331P, background sources are clearly

³ https://archive.stsci.edu/hst/search.php
trailed, and even visibly curved in some of the images, due to the parallactic motion of HST around the Earth. The observing geometry of 331P is given in Table 1.

We started with the calibrated images including charge transfer efficiency correction but no geometric distortion correction. These images were plagued with abundant hot pixels and random cosmic-ray hits. While the hot pixels were flagged and masked in accordance with the data quality arrays accompanying the science images, we applied the L.A. Cosmic algorithm (van Dokkum 2001) to remove cosmic-ray strikes, thereby obtaining much cleaner resulting images. We checked that the pixel counts of the components of 331P and neighboring unsaturated background sources remained untouched by the cosmic-ray removal algorithm. Next, AstroDrizzle (Gonzaga et al. 2012) was used to correct the cleaned images for geometric distortion. In order to further suppress remaining cosmic-ray artifacts and to improve the signal-to-noise ratio of the target, images from the same visits were median combined with alignment on the primary nucleus of 331P. Images in which the active asteroid was strongly influenced or obscured by saturated bright sources were discarded. As a result, most background star trails were effectively removed in the combined stacks.

The combined HST images of 331P have a range of sensitivities, both because of the changing viewing geometry and because different numbers of orbits and total observing times were secured in different visits (Table 1). While a total of 19 fragments, labeled 331P-A through 331P-S, are clearly identified in the data (Jewitt et al. 2021), only the brightest three (Figure 1) can be identified in images taken across the full interval from 2015 December to 2018 July. For this reason, the following analysis applies only to these three fragments, 331P-A, -B, and -C, in addition to the primary body, for which the astrometric data are of sufficient number and quality to permit a useful dynamical analysis.

3. Analysis

3.1. Astrometry

The HST/WFC3 images only contained coarse world coordinate system (WCS) solutions with guide stars in their headers, and therefore updating the solutions using field stars would be necessary before we could determine best-fit orbital solutions for the primary nucleus of 331P and its fragments. Because stars were all trailed significantly in individual HST/WFC3 images, traditional centroiding algorithms that treat stars as point sources could not be used. Instead, we adopted a technique specifically suited for trailed images, in which a source is modeled as a trapezoid in the along-track direction and a Gaussian in the cross-track direction. For each trail, the peak value and pixel coordinates of the centroid, along with the trail length, width, and orientation were free parameters to be fitted. The local sky background was determined using an annulus centered around the corresponding trail, with the inner and outer ranges, respectively, twice and four times the peak value and pixel coordinates of the centroid, along with the trail length, width, and orientation were free parameters to be fitted. The local sky background was determined using an annulus centered around the corresponding trail, with the inner and outer ranges, respectively, twice and four times the dimensions of the trail aperture. For each visit, we picked the image in which the trails of background sources appear to be the most straight by visual inspection, so as to better avoid

Table 1

Observing Geometry of Active Asteroid 331P/Gibbs

| Date          | # Images | $t_{exp}$ (s) | $r_1$ (au) | $\Delta$ (au) | $\alpha$ (°) | $\nu$ (°) | $\theta_{-\nu}$ (°) | $\theta_{+\nu}$ (°) | $\psi$ (°) |
|--------------|---------|--------------|-----------|---------------|-------------|----------|----------------------|----------------------|-----------|
| 2015 Dec 25  | 24      | 368          | 2.906     | 2.011         | 9.7         | 39.3     | 64.7                 | 269.0                 | +3.9      |
| 2015 Dec 28  | 12      | 368          | 2.907     | 2.030         | 10.5        | 39.8     | 66.2                 | 269.0                 | +4.0      |
| 2016 Feb 13  | 24      | 368          | 2.920     | 2.575         | 19.4        | 49.3     | 78.3                 | 269.6                 | +3.6      |
| 2017 Mar 8   | 25      | 438          | 3.059     | 2.111         | 6.2         | 118.8    | 331.1                | 286.2                 | +4.3      |
| 2018 May 17  | 10      | 438          | 3.068     | 2.109         | 5.8         | 123.0    | 70.4                 | 286.7                 | +3.4      |
| 2018 May 26  | 20      | 438          | 3.122     | 2.113         | 1.6         | 197.4    | 169.0                | 274.5                 | −1.5      |
| 2018 Jul 3   | 20      | 453          | 3.115     | 2.402         | 15.2        | 205.3    | 110.0                | 275.2                 | −3.7      |

Notes.

a Individual median exposure time.
b Heliocentric distance.
c Phase angle (Sun-331P-HST).
d True anomaly.
e Position angle of the projected antisolar direction.
f Position angle of the projected negative heliocentric velocity of 331P.
g Orbital plane angle (between HST and orbital plane of 331P).
introduction of a systematic bias due to curvature being unaccounted for in the trail model. We then updated the WCS solutions by a linear fit of the pixel coordinates to the Gaia Data Release 2 catalog (Gaia Collaboration 2018).

Measuring the pixel coordinates of the primary and the brightest fragments of 331P was straightforward in the median-combined images, as each of them was simply treated as a point source to be least-square fitted. Thereby, with the updated WCS solutions, we were able to convert the best-fit pixel coordinates of the primary and components of 331P in the corresponding HST visits to J2000 equatorial coordinates in terms of R.A. and decl. The associated uncertainties were obtained through propagation of the centroid errors and the counterparts in astrometric solutions, with the latter being dominant. We tabulate the astrometry of the components of 331P along with the corresponding uncertainties in Table 2.

3.2. Orbit Determination

In addition to our astrometric measurements, we downloaded astrometry of the primary from the Minor Planet Center Database Search, which covers a much longer observed arc. For our astrometric measurements, we assigned a weighting scheme in accordance with the corresponding measurement errors, whereas we had to debias and weight the counterpart from the Minor Planet Center, following the methods described in Farnocchia et al. (2015) and Vereš et al. (2017), respectively. This is because the astrometry was measured with different star catalogs and no information of their measurement errors is available. We then proceeded to find orbital solutions for the primary and the brightest components of 331P in FindOrb, an N-body orbit determination software package written by B. Gray, which took into account solar gravity, as well as perturbations from the eight major planets, Pluto, the Moon, and the 16 most massive asteroids in the main belt. Positions and masses of the perturbers were adopted from the planetary and lunar ephemeris DE440 (Park et al. 2021). The first post-Newtonian corrections were also implemented in the software package. In a preliminary test, we were aware that almost half of our astrometric measurements from the HST images for the primary had observed-minus-calculated ($O - C$) residuals more than three times larger than the reported measurement errors (no more than ~10 mas), five of which even had residuals over ten times larger. By looking into these measurements more closely, we found that the major discrepancies all existed in the along-track direction. We attempted to refine the astrometric reduction for these images by slightly adjusting the initial guess values in fitting the star trails. However, no improvement beyond the noise level could be achieved. We then visually inspected the images, finding that the star trails appear more curved due to the parallactic motion of the HST orbiting around Earth. Therefore, we concluded that the $O - C$ residuals of these measurements reflected the systematic errors and inflated the measurement errors accordingly. Astrometry of the primary downloaded from the Minor Planet Center with $O - C$ residuals over three times the assigned uncertainties was simply discarded because their $O - C$ residuals can be as enormous as a few arcsec, orders of magnitude greater than those of our worst HST astrometry. We also inflated the measurement errors for the astrometry of the fragments from the same sets of images using the results we obtained for the primary. Consequently, the $O - C$ residuals of the astrometry of the fragments are all consistent with the inflated errors, suggesting the validity of the modification. We summarize the best-fit orbital solutions in Table 3, from which the similarity of the orbits can be readily noticed.

3.3. Fragmentation

The orbital similarities of the components of 331P are indicative of their common origin. We are interested to know whether the fragments 331P-A, -B, and -C were released from the primary at one time, or staggered at different times. In addition, we consider the possibility that some fragments may have been released from other fragments (in so-called “cascading fragmentation”), not directly from the 331P parent body. We address these questions by carefully examining the pairwise separations of the fragments both from the parent and from each other.

We applied two different approaches to investigate the fragmentation of the active asteroid. First, we backtracked the orbits of the components by means of backward integrating the obtained best-fit orbits summarized in Table 3. In order to fully encompass the orbital uncertainties of the components, we applied the Cholesky decomposition method to generate 1000 Monte Carlo (MC) clones for each component based on the corresponding covariance matrices of the orbital elements. We did not attempt to compute and track the mutual distances between the clones of the fragments and those of the primary because we only used results from this approach to guide our attempts using the second approach, to be detailed in the next paragraph. The graphic interface of SOLEX12 (Vitagliano 1997) was utilized to conveniently monitor the backward orbital evolution of the clones of the components, in which the orthogonal Cartesian coordinates of the MC clones of the fragments with respect to the position of the nominal orbit of the primary referenced to the J2000 ecliptic were plotted. We found that around 2011 June, the MC clones of Fragment A formed a highly elongated ellipsoid spatially overlapping with that of the primary body, while the overlap between the MC clones of Fragment B appear to occur in a wider time range between early and mid 2011, due to the larger orbital uncertainty. However, the clones of Fragment C and those of the primary show no more than a partial overlap even during their closest encounter in mid-to-late 2011. On the contrary, its MC clones overlap better with those of Fragment B from 2011 to 2014. This may imply that Fragments A and B separated from the primary, whereas Fragment C possibly split instead from Fragment B. (Another possibility is that a nongravitational acceleration could exist, and so we consider this possibility in the second approach, below.) However, these results from the first approach are highly ambiguous, because the orbital uncertainties in backward integrations (dominated by the systematic errors in the astrometric reduction of field sources in the HST observations) are enormous. Nevertheless, it is interesting that the derived separation times are broadly consistent with the epoch of impulsive activity deduced independently from models of the tail morphology by Moreno et al. (2012) and Stevenson et al. (2012). If we monitored the MC clones further backward in time, we would then observe seemingly acceptable overlaps between the MC clones of the primary and those of Fragments B and C in 2006 again. However, this is due to the orbital periodicity and the growing...
| Time (UTC) | Primary R.A. (h m s) | Decl. (° ′ ″) | Error (″) | R.A. (h m s) | Decl. (° ′ ″) | Error (″) | R.A. (h m s) | Decl. (° ′ ″) | Error (″) |
|-----------|---------------------|---------------|-----------|-------------|---------------|------------|-------------|---------------|-----------|
| 2015 Dec 25 428287 | 04 16 31.2730 | +12 38 01.611 | 0.035 0.006 | 04 16 29.8323 | +12 38 01.542 | 0.031 0.010 | 04 16 30.9851 | +12 38 01.541 | 0.044 0.029 |
| 2015 Dec 25 492963 | 04 16 28.9437 | +12 37 52.882 | 0.094 0.040 | 04 16 27.5046 | +12 37 52.813 | 0.076 0.040 | 04 16 28.6576 | +12 37 52.819 | 0.092 0.040 |
| 2015 Dec 25 559225 | 04 16 26.5694 | +12 37 44.177 | 0.040 0.040 | 04 16 25.1291 | +12 37 44.100 | 0.040 0.040 | 04 16 26.2827 | +12 37 44.114 | 0.040 0.040 |
| 2015 Dec 25 625486 | 04 16 24.1958 | +12 37 35.506 | 0.040 0.040 | 04 16 22.7556 | +12 37 35.424 | 0.040 0.040 | 04 16 23.9109 | +12 37 35.442 | 0.040 0.040 |
| 2015 Dec 28 077894 | 04 15 00.0126 | +12 32 36.090 | 0.006 0.004 | 04 14 58.5905 | +12 32 36.004 | 0.009 0.008 | 04 14 59.7303 | +12 32 36.029 | 0.033 0.034 |
| 2015 Dec 28 143310 | 04 15 57.8805 | +12 32 28.457 | 0.200 0.200 | 04 14 56.4571 | +12 32 28.511 | 0.200 0.200 | 04 14 57.5975 | +12 32 28.552 | 0.200 0.200 |

The R.A. and decl. coordinates are referred to the J2000 equatorial system. The reported errors are formal uncertainties of the astrometric measurements, primarily dominated by systematic errors in the WCS solutions. Technically, the first columns of the errors are uncertainties in the east–west direction at the corresponding J2000 equatorial coordinates.
uncertainty regions with time backwards, and therefore we did not consider possible fragmentation epochs much earlier than 2011.

Our second approach is an application of the fragmentation model first devised by Sekanina (1977, 1978). We have previously succeeded in applying this approach to examine the split event of another active asteroid, P/2016 J1 (PAN-STARRS; Hui et al. 2017). The model simplifies a split event as an instantaneous separation of one component from the other at a fragmentation epoch of \( t_{frg} \). At the instant after the split, a component travels at a separation velocity with respect to the other one referenced to the orbital plane of the latter and expressed in terms of the radial, transverse, and normal (RTN) components (\( \Delta V_R, \Delta V_T, \Delta V_N \)). If no satisfactory gravity-only solution is found, the RTN nongravitational parameters (denoted as \( A_1, A_2, \) and \( A_3 \), respectively; Marsden et al. 1973), are added to the model as additional free parameters to account for a potential nongravitational effect arising from any anisotropic recoil force acting on the fragment. The gravitational interaction between the split components is ignored, but the influence from the Sun as well as massive perturbers such as major planets in DE440 are taken into account. Then, the trajectory and apparent positions of the fragment can be uniquely determined by the above set of split parameters, and can be compared to the astrometric observations. Our code utilizes the Levenberg–Marquardt optimization code MPFIT (Markwardt 2009) to obtain the split parameters that minimize the goodness of fit,

\[
\chi^2(t_{frg}, \Delta V_R, \Delta V_T, \Delta V_N, A_1, A_2, A_3) = \xi^T W \xi,
\]

where \( \xi \) is the vector of the \( O - C \) astrometric residuals, and \( W \) is the diagonal weight matrix of the observations assigned as the inverse square of the astrometric measurement uncertainties. In order to eliminate systematic uncertainties in our absolute astrometric measurements, we fitted the relative astrometry of the paired components. In this way the associated uncertainties arise primarily from errors in the best-fit centroids of the components. These are typically smaller than the overall errors listed in Table 2 by at least an order of magnitude.

We found satisfactory solutions without the need to include nongravitational acceleration terms (the RTN nongravitational parameters were all set to be zero). Given also the statistics of separation speeds of comets (Boehnhardt 2004 and citations therein) and the estimate on the ejection speed of dust based on modeling the dust trail morphology (Jewitt et al. 2021), we confined the magnitudes of the RTN components of the separation velocity to be \( \lesssim 10 \text{ m s}^{-1} \). The Levenberg–Marquardt optimization is only capable of finding local minima, and the fragmentation epoch is the only parameter that could vary substantially. Therefore, we first examined how the goodness of fit changes as a function of the fragmentation epoch by iteratively solving, for the three fragments, their separation velocities with the fragmentation epoch fixed in a \( \pm 6 \) month window from the impulsive activation epoch of (2011 July; Stevenson et al. 2012; Moreno et al. 2012). Once each iteration was completed, we recorded the best-fit separation velocity and the normalized rms residual of the fit, which is the goodness of fit divided by twice the number of observations (so as to get rid of the difference in the numbers of observations between fragments), then incremented the fragmentation epoch by a step size of one day, and started a new fit by repeating the same procedures.

The upper panels of Figure 2 display the resulting relative separation velocities while the lower panel compares the normalized rms residuals of the three fragments. In the 2011–2012 timeframe, there is only a single minimum in the normalized rms residuals for each of the fragments. Two major differences can be readily noticed. First, the minimum of the normalized rms residual of Fragment A is narrow and much better defined than those of Fragments B and C. The Fragment A minimum occurs at \( \sim 2011.45 \) (2011 June 16), consistent with the activation dates 2011 July 7 \( \pm 20 \) inferred from tail measurements (Stevenson et al. 2012). The Fragment B minimum occurs near 2011.3 but, given its width, is consistent with that of Fragment A and with Stevenson et al. (2012). Second, the minima in the normalized rms residuals of Fragments A and B are both \( \lesssim 1 \), representing plausible solutions but, in contrast, the minimum in the computed separation of Fragment C from the primary has a normalized rms \( \sim 10 \). All measurements of the 331P to Fragment C separation from 2015 show \( O - C \) residuals more than ten times larger than the measurement uncertainties, and nearly all observations from 2017 show residuals exceeding the \( 3\sigma \) level. We conclude that while Fragments A and B could both have separated from the primary body and have done so simultaneously, in contrast, the solution for the separation of Fragment C from the 331P primary body is unacceptable.

There are three additional pairwise combinations of the fragments to be investigated, i.e., Fragments A and B,
Fragments A and C, and Fragments B and C. Given the ambiguous results we observed in the backward integration of the MC clones, we examined the possible split epochs in a range still from early 2011 extending to early 2015, almost a year before the earliest HST observation. The above fitting procedures were repeated, except that the step size was increased to four days so as to reduce the computation loads. We present the results in Figure 3, in which we can see that there are two local minima in each of the normalized rms residuals of the solutions for the three pairwise combinations. However, only the pairwise consideration of Fragments B and C has two local minima of comparable depth, with normalized rms $\sim 1$. In comparison, the best fit for the separation between Fragments A and C is worse, in that one observation has an $O-C$ residual of nearly $4\sigma$ and one of almost $3\sigma$, both in the decl. direction. The weighted mean residual in the decl. direction is more than twice the one in the J2000 equatorial east–west direction, which is absent in any other best solutions. More importantly, the best-fit fragmentation epoch (around 2011 May 19) would predate the split events that produced Fragments A and C. Therefore, we conclude that the split between Fragments A and C is implausible and the hypothesis is rejected.

Having known the numbers of local minima in the normalized rms residuals in the time interval, we relaxed the fragmentation epoch as a free parameter and tested with different combination sets of initial guess values for the pairwise combinations of the components of 331P. We found that each best-fit solution would always converge to the same results within the uncertainty levels, as long as the initial guess values for the split epoch is situated within the dip of the normalized rms residual. The individual $O-C$ astrometric residuals of the best-fit solutions for the pairwise combinations of Fragment A and the primary, Fragment B and the primary, Fragments B and A, and Fragments C and B are all consistent with the measured uncertainties. Table 4 tabulates these best-fit solutions, the reported uncertainties are all formal $1\sigma$ errors properly propagated from the astrometric measurement errors. We were fully aware that the derived uncertainties of the split parameters have not incorporated the orbital uncertainties of the paired components. To investigate how strong the influence of the latter would be, we carried out iterative runs with the orbits of the referenced components substituted by the corresponding MC clones. In each run, we obtained the best-fitted fragmentation epoch and the RTN components of the separation velocity and recorded the corresponding goodness of fit and normalized rms residual by fitting the differential astrometry of the fragments. After the whole run was completed, we then computed the standard deviations of the split parameters, finding that, even in the cases with the least certain orbital solutions (for Fragments B and C), the resulting uncertainties are always less than a hundredth, typically less than a thousandth, of the counterparts propagated from the measurement errors alone. Therefore, we believe that the reported uncertainties in Table 4 are trustworthy.

**Figure 2.** Upper three panels: separation velocities decomposed into radial, transverse, and normal components (color coded) of Fragments A (left), B (middle), and C (right) split from the primary of 331P needed in order to best fit the astrometry as functions of fragmentation epoch (here expressed as number of years past J2000). Lower panel: normalized rms residuals (the goodness of fit divided by twice the number of observations) of the best fits for Fragments A, B, and C (distinguished by colors) varied with split epoch. The shaded region represents the range of possible impulsive activation epochs of 331P inferred from the tail morphology by Stevenson et al. (2012; 2011 July $7 \pm 20$), with the nominal value marked by the vertical line. The dotted lines in gray in the upper panels indicate split epochs rendering solutions with corresponding local minimum normalized rms residual. Note the best normalized rms for Fragment C is worse than those for the other two fragments by an order of magnitude.
4. Discussion

One may ask whether or not there can be other fits to the data if nongravitational accelerations are included in the model, and we explored this possibility. Given the fact that the in-plane components of the nongravitational acceleration are usually orders of magnitude larger than the out-of-plane one, we only tested with nonzero $A_1$ and/or $A_2$, while setting $A_3 \equiv 0$ in all cases. We find that acceptable solutions including nongravitational acceleration parameters are possible. For example, we tested the separation of Fragment C from the primary with the inclusion of a radial nongravitational acceleration, $A_1$. We found a solution with goodness of fit even better than any of the gravity-only solutions, having a normalized rms residual of 0.683, provided $A_1 \sim 10^{-12}$ au day$^{-2}$. Another formally acceptable fit was obtained by instead assuming $A_1 = A_3 = 0$ day$^{-2}$, giving a normalized rms residual of only 0.791. However, the apparent improvement of these solutions is almost certainly an artifact of adding more parameters to the fitting model.

Physical measurements of the 331P fragments show no evidence for comet-like outgassing as would be expected in the presence of sublimating ice (Jewitt et al. 2021). In the absence of sublimation, nongravitational accelerations can occur from solar radiation pressure and the Yarkovsky effect, but these are very small. The corresponding radial nongravitational parameter is

$$A_1 = \frac{3(1 + A_B)S_0}{4c\rho R},$$

where $A_B$ is the Bond albedo, $S_0 = 1361$ W m$^{-2}$ is the solar constant, $c \approx 3 \times 10^8$ m s$^{-1}$ is the speed of light in vacuum, and $\rho$ and $R$ are, respectively, the mass density and the radius of the fragment. Substituting the size and mass density estimates (Jewitt et al. 2021) and the Bond albedo $A_B \sim 0$, we find the anticipated radial nongravitational parameter to be $A_1 \sim 10^{-12}$ au day$^{-2}$ for Fragment C. This is two orders of magnitude smaller than the acceleration deduced from the model. We used JPL’s Small-Body Database Query\(^6\) to search for comparably small asteroids with measured $A_2$ values. These small bodies all have $|A_2| \sim 10^{-13}$ au day$^{-2}$, again two orders of magnitude smaller than the value returned by our model. It is unsurprising to find apparently better solutions by adding extra free parameters to the model, but these solutions have no physical significance and gravity-only solutions are just as good.

Given the obtained best-fit fragmentation epochs and the associated uncertainties, we can think of two different possibilities for the fragmentation events that occurred at 331P:

1. Fragments A and B both directly separated from the primary in 2011 mid June at a separation speed of $\sim 8$ cm s$^{-1}$ and between 2011 April and May at $\sim 1$ cm s$^{-1}$, respectively, while Fragment C split from Fragment B at a later epoch, either around late 2011 or between late 2013 and early 2014, at a speed of $\sim 0.7$–0.8 cm s$^{-1}$.

2. Fragment B is the only component that directly fragmented from the primary around April and May in 2011, and it subsequently released Fragment A in 2011 mid June with a separation speed of $\sim 8$ cm s$^{-1}$ and then

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\(^6\) https://ssd.jpl.nasa.gov/tools/sbdb_query.html
Fragment C, either in late 2011, or between late 2013 and early 2014.

We summarize the two possibilities in Figure 4, in which the separation speeds between the components are labeled. The listed uncertainties are formal 1σ errors calculated using the covariance matrices of the split parameters. Unfortunately, other fragments of 331P visible in the HST observations do not have long enough observing arcs, and therefore their fragmentation scenarios cannot be meaningfully constrained.

Admittedly, a drawback of our fragmentation model is that mutual gravitational influences between the components are ignored. However, as the mass, shape, and density distribution will all strongly modify the gravitational potential of a component, all of which are unknown, and treating the components of 331P as multiple massive bodies will almost certainly give rise to chaos in the system of 331P. Given these, in addition to the measurement uncertainties that would otherwise leave too much room for various possible parameter options, we do not see any benefit in taking these extra factors into consideration in the fragmentation model, and we believe that the our results are diagnostic enough. The component separations at different epochs strongly imply that 331P is undergoing cascading fragmentation. Its components form an asteroid cluster that, at just over a decade, is considerably younger than any other known asteroid cluster (Novakovic et al. 2022 and citations therein). Cascading fragmentation has been previously identified in other asteroid clusters (Fatka et al. 2020), including the active asteroid P/2013 R3 (see Figure 12 of Jewitt et al. 2017). Therefore, the ongoing fragmentation at 331P provides us with a great opportunity to study and understand fragmentation of asteroids.

Using the derived separation velocities and times, we qualitatively explore the most likely physical mechanism that led to the cascading fragmentation at 331P. The best-fit separation velocities lie close to the orbital plane of 331P, as the in-plane components were found to be at least around five times larger than the out-of-plane components.

### Table 4

| Quantity                        | Fragment A                  | Fragment B                  | Fragment C                  | Solution I | Solution II |
|---------------------------------|------------------------------|------------------------------|------------------------------|------------|-------------|
| Fragmentation epoch (TDB)       | 2011 Jun 15.62 ± 0.32        | 2011 Apr 26 ± 26             | 2011 Jun 12.15 ± 0.83        | 2011 Dec 10 ± 12 | 2013 Dec 23 ± 18 |
| Separation velocity (cm s⁻¹)    |                              |                              |                              |            |             |
| Radial component                | -5.398 ± 0.012               | +0.04 ± 0.24                 | +5.939 ± 0.026               | -0.723 ± 0.045 | +0.724 ± 0.030 |
| Transverse component            | +6.39473 ± 0.00095           | +1.1767 ± 0.0082             | -5.2422 ± 0.0024             | +0.2715 ± 0.0050 | +0.1661 ± 0.0045 |
| Normal component                | -1.3693 ± 0.0094             | -0.064 ± 0.023               | +1.309 ± 0.027               | -0.001 ± 0.028 | -0.024 ± 0.033 |
| Paired with                     | Primary                      | Primary                      | Fragment A                   | Fragment B  | Fragment B  |
| Normalized rms residual         | 0.834                        | 0.910                        | 0.826                        | 0.761       | 0.750       |

Notes. Our best-fit gravity-only solution for Fragment C in the scenario where it is assumed to split from the primary renders an unacceptably strong systematic trend in the \( O - C \) astrometric residuals, thereby not presented here. The reported uncertainties are 1σ formal errors. The separation velocities are referenced with respect to the corresponding paired components of 331P.

* The corresponding uncertainties are in days.
and \(\sim 0.7 - 8 \text{ cm s}^{-1}\). As per the size estimates of the primary and the three largest fragments by Jewitt et al. (2021), the minimum ejection speeds required to escape the gravitational potential of the primary and that of Fragments A, B, and C are \(\sim 0.7 \text{ m s}^{-1}\) and \(\sim 6 - 10 \text{ cm s}^{-1}\), respectively. Since our fragmentation model neglects the mutual gravitational forces between the components, the measured separation speeds should be seen as the residual speeds at infinity with respect to the pairwise component. Assuming the components are all spherical, we roughly estimate the ejection speed to be

\[
V_\text{ej} = \sqrt{\Delta V^2 + \frac{8}{3} \pi \rho G (R_1^2 - R_1 R_2 + R_2^2)}. \tag{3}
\]

Here, \(G = 6.67 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}\) is the gravitational constant, and \(R_1\) and \(R_2\) are the nucleus radii of the pairwise components. Substituting \(G, R_1,\) and \(R_2\) into the equation, we find \(V_\text{ej} \approx 0.7 \text{ m s}^{-1}\) for Fragments A and B to split from the primary, \(0.1 \text{ m s}^{-1}\) for the split between Fragments A and B, and \(7 \text{ cm s}^{-1}\) for the split between Fragments B and C, all of which are comparable to the respective escape speeds.

The best-fit results from our astrometric model of fragmentation indicate that the split events were spread over several months, inconsistent with an impact origin. In the absence of other plausible mechanisms, we concur with Drahus et al. (2015) and Jewitt et al. (2021) that the fragmentation at the primary of 331P was most likely caused by rotational instability. Separation speeds below the nominal escape velocity, as inferred from the data, are natural products of multibody interactions in a rotationally fissioned asteroid, where delayed ejection of material is also a prominent feature of the models. For example, numerical simulations of rotationally fissioned asteroids reveal complex interactions that produce cm s\(^{-1}\) excess escape velocities in abundance, commonly result in secondary fission, and can have survival lifetimes measured in years (Boldrin et al. 2016).

Future observations at HST resolution and sensitivity are needed to resolve the ambiguities of the present work and will reveal the dynamics of this evolving system more clearly. To explore this, we integrated the motions of the fragments into the future. We find that by 2023, the two possible fragmentation scenarios described for Fragment C, above, will lead to a positional difference of \(\sim 0.3\) (see Figure 5). This is large enough that new measurements from HST (or JWST) will be able to distinguish between the scenarios. New observations of comparable or greater sensitivity may also show the spread of other fragments, and reveal whether the fragmentation cascade continues.

5. Summary

We present an astrometric analysis of the multicomponent active asteroid 331P/Gibbs using data obtained from the Hubble Space Telescope from 2015 to 2018. We applied a fragmentation model to Fragments A, B, and C, which, together with the primary body, 331P, are the brightest and best observed components. The key results are:

1. Fragment B split from the primary in 2011 April–May, with a separation speed of \(1.2 \pm 0.2 \text{ cm s}^{-1}\). This date is in broad agreement with initiation dates determined independently from models of the particle trail in which the fragments appear embedded.

2. We find two plausible solutions for Fragment A, with separation from the primary on 2011 June 15.62 \(\pm\) 0.32 at a relative speed of 8.48 \(\pm\) 0.02 cm s\(^{-1}\), or from Fragment B slightly earlier in 2011 June 12.15 \(\pm\) 0.83 at speed 8.03 \(\pm\) 0.04 cm s\(^{-1}\).

3. We find no acceptable solutions in which Fragment C is released directly from the primary body. Instead, we find two possible scenarios in which Fragment C split from Fragment B, either in late 2011 at 0.77 \(\pm\) 0.18 cm s\(^{-1}\) or near-late 2013 to early 2014 at 0.74 \(\pm\) 0.04 cm s\(^{-1}\).

4. The small fragment separation speeds and the staggered epochs of separation are most compatible with rotational disruption as the mechanism that led to the breakup of 331P starting in 2011.

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Facility: HST/WFC3.

Software: AstroDrizzle (Gonzaga et al. 2012), FindOrb, IDL, L.A. Cosmic (van Dokkum 2001), MPFIT (Markwardt 2009), SOLEX12 (Vitagliano 1997).
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