Research Article

Orthogonal DF Cooperative Relay Networks with Multiple-SNR
Thresholds and Multiple Hard-Decision Detections

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This paper investigates a wireless cooperative relay network with multiple relays communicating with the destination over orthogonal channels. Proposed is a cooperative transmission scheme that employs two signal-to-noise ratio (SNR) thresholds and multiple hard-decision detections (HDD) at the destination. One SNR threshold is used to select transmitting relays, and the other threshold is used at the destination for detection. Then the destination simply combines all the hard-decision results and makes the final binary decision based on majority voting. Focusing on the decode-and-forward (DF) relaying protocol, the average bit error probability is derived and diversity analysis is carried out. It is shown that the full diversity order can be achieved by setting appropriate thresholds even when the destination does not know the exact or average SNRs of the source-relay links. The performance analysis is further extended to multi-hop cooperation and/or with the presence of a direct link where multiple thresholds are needed. By combining the multiple-SNR threshold method with a selection of the best relaying link, a high spectral-efficiency cooperative transmission scheme is further presented. Simulation results verify the theoretical analysis and demonstrate performance advantage of our proposed schemes over the existing ones.

1. Introduction

In most existing wireless communication networks, cable-powered base stations can be easily equipped with spatially separated multiple antennas. On the other hand, mounting multiple antennas in portable mobile terminals is not so practical because of their small-size and limited processing power. Hence, how to fully exploit the diversity benefit of multiple-antenna systems in distributed wireless communication networks has become an important issue. Recently, the concept of cooperation in wireless communications has drawn much research attention due to its potential in improving the efficiency of wireless networks [1–3]. In cooperative communications, users can cooperate to relay each other’s information signals, creating a virtual array of transmit antennas, and hence achieving spatial diversity. Therefore cooperative diversity techniques can dramatically improve the reliability of signal transmission from each user.

In general, relaying transmission strategies can be divided into two main categories: amplify-and-forward (AF) and decode-and-forward (DF). In AF protocol, a relay just amplifies the signal received from the source and retransmits it to the destination or the next node. On the other hand, with the DF protocol, the a relay decodes the signal and remodulates the decoded information before transmitting to the next node. For these two protocols, outage and error performance have been extensively investigated [4–6]. In addition, the DF protocol can be combined with coding techniques and thus forming the so-called coded cooperation [7], which has been further developed in [8].

The uncoded DF protocol is relatively simple and particularly attractive for wireless sensor networks due to the fact that the relays do not rely on any error-correction or error-detection codes and thus the network can afford a severe energy limitation. Unlike coded DF relaying, however, the relays in uncoded DF may forward
erroneous information, and with a conventional combining scheme such as the maximal-ratio combining (MRC), the error propagation degrades the end-to-end (e2e) detection performance. Recently, some works have been done to mitigate error propagation, which can be classified into two main approaches as follows.

The first approach includes selective and adaptive relaying techniques, for example, link adaptive relaying [9] and threshold digital relaying (TDR) [10–13]. Both techniques use the source-relay link SNR to evaluate the reliability of the data received by the relay. In TDR, a relay forwards the received data only when its received SNR is above a threshold value. It has been shown that TDR can achieve the full-diversity order. Different from other full-diversity protocols in the literature, the TDR with relay selection proposed in [12, 13] does not require that the exact or average SNRs of the source-relay links be known at the destination.

In order to mitigate error propagation, the second approach is to develop efficient combining schemes used at the destination [14–17]. In [14], the authors assume that the destination knows the exact source-relay SNR and present the so-called cooperative MRC (C-MRC) scheme that can approximate the maximum likelihood (ML) detection scheme. This scheme is shown to achieve the full-diversity order at the expense of increased signaling overhead to convey the first hop (source-relay link) SNR information to the destination. In [16], in order to reduce the signaling overhead in C-MRC with relay selection, the authors propose a modified combining scheme, called product MRC, which can achieve the same diversity order as the C-MRC. Reference [15] proposes a piecewise linear detector that approximates the ML detector and only requires knowledge of the average SNRs of the first hop. Although transmitting the average link SNRs is less costly than transmitting the instantaneous SNR, the scheme in [15] can only achieve about half of the full-diversity order for networks with more than one relay. In [17], the authors present a simple combining scheme based on hard-decision detection (HDD) with a much lower implementation complexity. However, similar to the scheme in [15], it does not achieve the full-diversity order. All of these abovementioned schemes require the relays to send the instantaneous or average SNRs of source-relay links to the destination. This requirement involves significant signalling overhead and is therefore difficult to fulfill for certain applications such as sensor networks.

This paper is concerned with wireless relay networks that deploy multiple parallel relays communicating with the destination over orthogonal channels in the second phase. We propose and analyze a protocol for relay selection and HDD at the destination based on double SNR thresholds. One SNR threshold is used to select retransmitting relays: a relay retransmits if its received SNR is larger than a threshold; otherwise it remains silent. The other threshold is used at the destination so that the destination makes an HDD for the data received by the relay. In TDR, a relay forwards the received data only when its received SNR is above a threshold value. It has been shown that TDR can achieve the full-diversity order. Different from other full-diversity protocols in the literature, the TDR with relay selection proposed in [12, 13] does not require that the exact or average SNRs of the source-relay links be known at the destination.

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signal \( r_i \), and then forwards the detected result \( s_i \) to the
destination. Therefore the received signal at the destination
from the \( i \)th relay can be written as
\[
y_i = \sqrt{E_i}g_is_i + w_i, \tag{2}
\]
where \( E_i \) is the transmit power of the \( i \)th relay, \( g_i \) is the
channel gain between the \( i \)th relay and destination, which
is modeled as a circularly symmetric complex Gaussian
variable with variance \( N_i^{(1)} \), and \( w_i \) denotes the AWGN at
the destination with zero mean and unit variance. Moreover, \( s_i \)
also has unit average energy.

\[E_i = \cdots = E_R = E = \frac{E_T}{R + 1},\]
where \( E_T \) denotes the total power consumed by the network.

3. BER Performance Analysis

3.1. Performance for the \( i \)th-Relay Link. We first focus on
the performance of the \( i \)th-relay link which is a cascade of
the source-to-\( i \)th-relay link and \( i \)th-relay-to-destination link.
Denote the instantaneous SNRs of these two individual links by
\( y_i^{(1)} \) and \( y_i^{(2)} \). They are given by
\[
y_i^{(1)} = |f_i|E, \quad y_i^{(2)} = |g_i|E. \tag{4}
\]
Let \( p_b(y_i^{(j)}) \), \( j = 1, 2 \), represent the bit error rates (BERs)
of these two individual links as functions of the SNRs \( y_i^{(j)} \).
For a general modulation scheme, it can be approximated as \cite{18}
\[
p_b(y_i^{(j)}) \approx \alpha Q\left(\sqrt{\beta y_i^{(j)}}\right), \tag{5}
\]
where \( \alpha > 0 \) and \( \beta > 0 \) depend on the type of modulation.

Furthermore, for simplicity of analysis (Extension of our
analysis to the more general case is quite straightforward.),
we assume
\[
N_i^{(1)} = \cdots = N_R^{(1)} = N^{(1)},
\]
\[
N_i^{(2)} = \cdots = N_R^{(2)} = N^{(2)},
\]
\[
E_i = \cdots = E_R = E = \frac{E_T}{R + 1}, \tag{3}
\]
where \( E_T \) denotes the total power consumed by the network.

Appendix A provides detailed derivations of the above result.

3.2. Overall Average Bit Error Probability. Consider binary
modulation and let \( P_b(m, k) \) denote the conditional BER that
resulted from the majority voting on the HDDs under the
conditions that (i), among all \( R \) relays, there are \( m \) relays
making binary decisions and \( R - m \) relays making erasure
decisions and (ii), among \( m \) relays making binary decisions,
there are \( k \) relays making correct decisions (i.e., \( m - k \) relays
making error decisions). Obviously, if \( k > m - k \), the final
binary decision is correct and thus \( P_b(m, k) = 0 \). On the
other hand, if \( k < m - k \), the final binary decision is wrong and
thus \( P_b(m, k) = 1 \). If it happens that \( k = m - k \), the
destination makes the final binary decision by chance and hence
\( P_b(m, k) = 1/2 \). Therefore, the conditional BER \( P_b(m, k) \) can be written as
\[
P_b(m, k) = \begin{cases} 0, & k > m - k, \\ \frac{1}{2}, & k = m - k, \\ 1, & m - k >. \tag{12}
\end{cases}
\]
It should be noted that, when \( m = k = 0 \), no information
is sent over the wireless relay network. In such a case, the
conditional BER can be set to 1/2 for further unified analysis.
When nonbinary modulation such as PSK or QAM is used, for all the signals from the received reliable links, the destination first detects the information bits independently and then combines all of the detection results, bit by bit, with a majority voting. Therefore, for any bit in one modulation destination first detects the information bits independently used, for all the signals from the received reliable links, the BER performance at high SNR obtained with the proposed cooperative relay scheme. Then it can be written combining.

signal combining scheme, that is, the maximum likelihood (ML) signal combining scheme based on HDDs and majority combining. Furthermore, similar to [11, 13], we will define the two SNR thresholds as follows:

\[ \Theta_1 = c_1 N^{(1)} \log E, \]

\[ \Theta_2 = c_2 N^{(2)} \log E, \]

where \( c_1 \) and \( c_2 \) are two positive constants, whose values are discussed at the end of this subsection.

With the above definitions of the two SNR thresholds and as the SNR \( E \to \infty \), one has

\[ P_m = 1 - e^{-c \log E / E} \cdot e^{-c \log E / E} = 1 - e^{-c \log E / E} \sim c \cdot \frac{\log E}{E}, \]

where \( c = c_1 + c_2 \). As \( P_m \sim c \cdot \frac{\log E}{E} \), it will be seen later (see (30)) that, in order to achieve the full-diversity order, \( P_m \)

\[ \Lambda(s) \to \sum_{\text{sign}(t_i) = 1} \log \frac{1 - p_i^{(1)}}{p_i^{(1)}} + \sum_{\text{sign}(t_i) = -1} \log \frac{p_i^{(1)}}{1 - p_i^{(1)}}, \] (17)

If the destination only knows all of the average BERs, that is, \( E(p_b(y_i^{(1)})) = G(\Theta_1, N^{(1)} E) = p_i^{(1)}, i = 1, 2, \ldots, m \), at these \( m \) relays, then the LLR of the signal is given by

\[ \Lambda(s) = \sum_{\text{sign}(t_i) = 1} \log \frac{1 - p_i^{(1)}}{p_i^{(1)}} + \sum_{\text{sign}(t_i) = -1} \log \frac{p_i^{(1)}}{1 - p_i^{(1)}} = (2k - m) \cdot \log \frac{1 - p_i^{(1)}}{p_i^{(1)}}. \] (19)

The above LLR metric implies that at high SNR the ML combining scheme is equivalent to the proposed combining scheme based on HDD and majority voting. It should also be noted that the proposed combining scheme does not require that either exact or average SNRs of the source-relay links be known at the destination. Furthermore, when \( P_i^{(1)} = 0 \), it can be readily shown that the ML combining scheme coincides with the conventional MRC scheme. It has also been pointed out in [20] that the performance of the MRC scheme is severely degraded in practical scenario when \( P_i^{(1)} > 0 \), especially when the number of relays increases.

4. Diversity Analysis

4.1. Asymptotic Performance of the ith-Relay Link. In order to present the asymptotic analysis for \( P_a \) and \( P_b \), let us introduce the following two common notations. For two positive functions \( a(x) \) and \( b(x) \), \( a(x) \sim b(x) \) means that \( \lim_{x \to \infty} a(x)/b(x) = 1 \), whereas \( a(x) = O(b(x)) \) means that \( \lim \sup_{x \to \infty} a(x)/b(x) < \infty \). Furthermore, \( \log(\log E) = \Theta(1) \).

\[ \Theta_1 = c_1 N^{(1)} \log E, \]

\[ \Theta_2 = c_2 N^{(2)} \log E, \]

\[ \Lambda(s) = \sum_{\text{sign}(t_i) = 1} \log \frac{1 - p_i^{(1)}}{p_i^{(1)}} + \sum_{\text{sign}(t_i) = -1} \log \frac{p_i^{(1)}}{1 - p_i^{(1)}}, \] (17)

where \( p_i^{(1)} = p_b(y_i^{(1)}) \) and \( t_i = g_i y_i + g_i y_i^* \). Note that, when \( E \to \infty \) and \( \text{sign}(t_i) = 1 \), one has

\[ \log \frac{1 - p_i^{(1)}}{p_i^{(1)}} e_{\sqrt{E} t_i} + p_i^{(1)} + p_i^{(1)} e_{\sqrt{E} t_i} \\
- \log \frac{1 - p_i^{(1)}}{p_i^{(1)}}. \]

On the other hand, when \( E \to \infty \) and \( \text{sign}(t_i) = -1 \), then

\[ \log \frac{1 - p_i^{(1)}}{p_i^{(1)}} e_{\sqrt{E} t_i} + p_i^{(1)} + p_i^{(1)} e_{\sqrt{E} t_i} \\
- \log \frac{p_i^{(1)}}{1 - p_i^{(1)}}, \] (16)

Therefore, when \( E \to \infty \), we have

\[ \Lambda(s) \to \sum_{\text{sign}(t_i) = 1} \log \frac{1 - p_i^{(1)}}{p_i^{(1)}} + \sum_{\text{sign}(t_i) = -1} \log \frac{p_i^{(1)}}{1 - p_i^{(1)}}, \] (17)

Note that the above exact BER calculation of \( \overline{B}_B \) requires to use (6) and (10).

3.3. Near Optimality of the Proposed Combing Scheme. This section shows that, when BPSK modulation is employed, the BER performance at high SNR obtained with the proposed signal combining scheme based on HDDs and majority voting can be close to the BER performance of the optimal combining scheme, that is, the maximum likelihood (ML) combining.

Among all \( R \) relays, it is assumed that \( m \) relays make binary decisions (reliable relays) and \( R - m \) relays make erasure decisions. Without loss of generality, assume that the \( m \) reliable relays are relays \( 1, 2, \ldots, m \). If the destination can know all of the conditional BERs (conditioned on the instantaneous SNR \( y_i^{(1)} \) \( m \) at these \( m \) reliable relays, then the log-likelihood ratio (LLR) for the transmitted signal \( s \) can be computed as (see [19, 20])

\[ \Lambda(s) = \log \frac{f(y_1, y_2, \ldots, y_m \mid s = 1)}{f(y_1, y_2, \ldots, y_m \mid s = -1)} \\
= \sum_{i=1}^{m} \log \frac{1 - p_i^{(1)} e^{-|y_i - \sqrt{E} t_i|^2 / 2} + p_i^{(1)} e^{-|y_i + \sqrt{E} t_i|^2 / 2}}{1 - p_i^{(1)} e^{-|y_i + \sqrt{E} t_i|^2 / 2} + p_i^{(1)} e^{-|y_i - \sqrt{E} t_i|^2 / 2}} \\
= \sum_{i=1}^{m} \log \frac{1 - p_i^{(1)} e^{\sqrt{E} t_i} + p_i^{(1)}}{1 - p_i^{(1)} + p_i^{(1)} e^{\sqrt{E} t_i}}. \] (14)
must decay at least as $O(1/E^2)$ so that each term in the sum in (13) can be expressed asymptotically by $O((\log E/E)^R)$.

Now define

$$\Theta_{\min} = \min\{\Theta_1, \Theta_2\}.$$  \hfill (22)

Then from Appendix A the conditional BER has the following upper bound:

$$P_b \leq ae^{-\beta\Theta_{\min}/2}.$$  \hfill (23)

It follows from (10) that $\Theta_{\min}$ needs to satisfy

$$\beta\Theta_{\min} \geq 2\log E,$$  \hfill (24)

which in turn requires $c_j \ (j = 1, 2)$ to satisfy

$$c_j \geq \frac{4}{\beta} \cdot \frac{1}{N(j)}, \quad j = 1, 2.$$  \hfill (25)

With the definitions of $\Theta_1$ and $\Theta_2$ in (20), (10) can be further simplified to

$$P_b \leq ae^{-2\log E} = \alpha \cdot \frac{1}{E^2},$$  \hfill (26)

which confirms the second diversity order of $P_b$, namely, $P_b \sim O(1/E^2)$. Note that, if there is no threshold, or only one threshold, the diversity order of $P_b$ is only 1; that is, $P_b \sim O(1/E)$.

### 4.2. Diversity Analysis of the Overall Average BER, $\bar{P}_B$

Recall that the diversity order is defined as

$$d = -\lim_{E \to \infty} \frac{\log \bar{P}_B}{\log E}.$$  \hfill (27)

In the following, it is shown that an upper bound on the BER yields $d = R$, which implies that the relay network can achieve the full-diversity.

Since $(1 - P_b)^m \leq 1$ and $(1 - P_b)^k \leq 1$, $\bar{P}_B$ can be upper bounded as follows:

$$\bar{P}_B \leq \sum_{m=0}^{R} \sum_{k=0}^{[m/2]} \left( \begin{array}{c} R \\ m \end{array} \right) \left( \begin{array}{c} m \\ k \end{array} \right) p^r_m p^m_{b-k}.$$  \hfill (28)

Here $[m/2] = m/2$ if $m$ is even, and $[m/2] = (m-1)/2$ if $m$ is odd. It follows from (21) and (26) that

$$\bar{P}_B \leq \sum_{m=0}^{R} \sum_{k=0}^{[m/2]} \left( \begin{array}{c} R \\ m \end{array} \right) \left( \begin{array}{c} m \\ k \end{array} \right) \left( c \log E \right)^{R-m} \left( \frac{\alpha}{E^2} \right)^{m-k}.$$  \hfill (29)

Since $k \leq [m/2]$, one has

$$R \leq R - m + 2(m - k) = R + m - 2k.$$  \hfill (30)

Therefore,

$$\bar{P}_B \leq \left( \frac{\log E}{E} \right)^R \sum_{m=0}^{R} \sum_{k=0}^{[m/2]} \left( \begin{array}{c} R \\ m \end{array} \right) \left( \begin{array}{c} m \\ k \end{array} \right) c^{R-m} \alpha^{m-k} \leq q \left( \frac{\log E}{E} \right)^R,$$  \hfill (31)

where $q$ is a positive constant equal to

$$q = \sum_{m=0}^{R} \sum_{k=0}^{[m/2]} \left( \begin{array}{c} R \\ m \end{array} \right) \left( \begin{array}{c} m \\ k \end{array} \right) c^{R-m} \alpha^{m-k} \leq (c + 1 + a)^R.$$  \hfill (32)

From the above two inequalities, it is obvious that the diversity order of $\bar{P}_B$ is $R$.

Remark 1. If there is no threshold or only one threshold, due to the fact that $P_b \sim O(1/E)$, it can be shown similarly that

$$d = -\lim_{E \to \infty} \frac{\log \bar{P}_B}{\log E} = \left[ \frac{R + 1}{2} \right].$$  \hfill (33)

This means that only about half of the full-diversity order can be achieved.

Since there is no the direct link from the source to the destination, it is possible that an outage event occurs for the network when no information is actually sent to the destination. Based on (21), the outage probability is equal to

$$\bar{P}_{out} = \bar{P}_u^R \sim \left( \frac{\log E}{E} \right)^R.$$  \hfill (34)

Obviously, when $E \to \infty$, $\bar{P}_{out} \to 0$. Therefore, at high SNR region, the outage event has a negligible influence on the BER performance.

### 5. General Cooperation Scenarios

This section first generalizes the results of Section 3 to the following scenarios: (i) multihop cooperation and (ii) cooperation including the direct link. Then a link selection protocol for the general cooperative network including the direct link is also proposed.

#### 5.1. Multihop Cooperation

Consider a general cooperative relay network consisting of $R$ parallel links with each link having $M - 1$ relays. This means that there are $M$ hops from the source to destination. Assume that, for each relay link composing of $M - 1$ relays from the source to the destination, a given relay knows the instantaneous SNR of the channel connected to itself. There are $M$ SNR thresholds to determine the operation of these $M - 1$ relays and the destination on a given relay link. If each relay link has at least one out of $M$ hops whose instantaneous SNR is lower than the corresponding threshold, the whole relay link is called unreliable.

Information transmission over the network is also accomplished in two phases. In the first phase, signals are broadcasted by the source and received by the first relays in all $R$ links. In the second phase, data transmission starts from these first relays and ends at the destination. In order to avoid cochannel interference, all of the involved relay channels are assumed to be orthogonal. Moreover, for any relay link, each relay on the link will send successively a single-bit message informing whether the related part of the relay link is reliable or not. In particular, the first relay first decides independently
whether its channel is reliable by comparing its received SNR to the first threshold value, and informs the second relay by sending a single-bit message indicating whether the first section of the relay link is reliable. Then the second relay sends a single-bit message informing that the first two sections of the relay link are unreliable if it receives the single-bit message from the first relay saying that the first section of the link is unreliable. Otherwise, the second relay first decides independently whether the second channel is reliable by comparing its received SNR to the second threshold value, and informs the third relay by sending a single-bit message. The same procedure repeats for other relays on the link. For any relay link, if the whole link is reliable, then each relay, due to the link unreliability, remains silent. For each of the received signals from the last relays of reliable links, similar to the case of two-hop networks, the destination makes binary hard-decision detections, whereas for the unreliable relay links it makes erasure decisions.

For the \( j \)th hop of the \( i \)th-relay link, denote its instantaneous SNR by \( \gamma_{ij} \), whose second moment is \( \gamma_{ij}^2 \). Similar to the two-hop case, the \( M \) SNR thresholds \( \Theta_j \), \( j = 1, \ldots, M \), introduced for the multi-hop network are defined as

\[
\Theta_j = c_j N_{ij} \log E. \tag{35}
\]

In order to achieve the full-diversity order, the coefficients \( c_j \) should satisfy \( c_j \geq (4/\beta) \cdot (1/N_{ij}) \), which is the same as in the two-hop case.

Extending the analysis in the previous section, the unreliable probability for each relay link is expressed as

\[
P_u = 1 - \prod_{j=1}^{M} \left[ 1 - F_j \left( \Theta_j \right) \right]. \tag{36}
\]

Furthermore, with the definition of \( \{ \Theta_j \} \), it is easily shown that

\[
P_u \sim c \cdot \frac{\log E}{E}, \tag{37}
\]

where \( c = \sum_{j=1}^{M} c_j \).

The exact conditional BER at the destination for the \( i \)th-relay link under the reliable condition can be calculated iteratively based on (10), (11) and the following formula:

\[
P_b = P_b \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M} \right) = \left[ 1 - P_b \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M-1} \right) \right] P_b \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M-1} \right) \]
\[
+ \left[ 1 - P_b \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M-1} \right) \right] P_{M} \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M-1} \right)
\]
\[
= \left[ 1 - G \left( \Theta_j, N_{ij} \right) \right] P_b \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M-1} \right) \]
\[
+ \left[ 1 - G \left( \Theta_j, N_{ij} \right) \right] P_{M} \left( \left\{ \Theta_j, N_{ij} \right\}_{j=1}^{M-1} \right). \tag{38}
\]

Furthermore, it can be shown by induction that the conditional BER for each relay link as a function of \( \{ y_{ij} \}_{j=1}^{M} \) has the following upper bound (see Appendix B for the derivations):

\[
P_b \left( \left\{ y_{ij} \right\}_{j=1}^{M} \right) \leq \sum_{j=1}^{M} aQ \left( \sqrt{\beta \Theta_j} \right) \leq MAQ \left( \sqrt{\beta \Theta_{\min}} \right), \tag{39}
\]

where \( \Theta_{\min} = \min \{ \Theta_j, j = 1, \ldots, M \} \). Then, by making use of the bound \( Q(x) \leq (1/2)e^{-x^2/2} \), it can be shown that \( P_b = O(1/E^2) \). Finally, in the same manner as in the two-hop case, one can verify that the diversity order is also \( R \) since the expression of the overall average BER \( \overline{P}_b \) is the same as that in the two-hop networks, and so is the expression of the outage probability.

5.2. Cooperation Including the Direct Link. First consider separately the performance of the direct link. Assume that the channel gain of the link is \( h \), whose magnitude follows a Rayleigh distribution with a second moment \( N \). For the direct link, we also set an SNR threshold at the destination node and define it similarly as follows:

\[
\Theta = c' N \log E, \tag{40}
\]

where \( c' \) is a constant satisfying \( c' \geq (4/\beta) \cdot (1/N) \). Then the probability that the direct link is unreliable can be expressed as

\[
P'_u = 1 - e^{-c' \frac{\log E}{E}} \sim c' \cdot \frac{\log E}{E}. \tag{41}
\]

On the other hand, under the reliable condition, the conditional BER of the direct link is \( P'_b = G(\Theta, NE) \sim O(1/E^2) \), furthermore, when \( E \to \infty \), it follows that \( P'_u = O(\log E/E) \). This implies that the individual contribution of the direct link on the diversity order is the same as the contribution of single-relay link on the diversity order. Since the direct link can be viewed equivalently as a relay link, the cooperative network with the inclusion of the direct link must have a maximum (or full-) diversity order of \( R + 1 \). Below we will show that this full-diversity order can indeed be achieved with our proposed method.

The overall system average BER can expressed as

\[
\overline{P}_b = (1 - P'_u) \overline{P}_b' + P'_u \overline{P}_b', \tag{42}
\]

where \( \overline{P}_b' \) is given in (13) and \( \overline{P}_b' \) is the conditional BER under the case that the direct link is reliable. The latter probability can be computed as

\[
\overline{P}_b' = \sum_{m=0}^{R} \sum_{k=0}^{m} \binom{R}{m} \binom{m}{k} P_{b}^{m-k}(1-P_{b})^{k} P_{b}(m,k), \tag{43}
\]

where

\[
P'_b(m,k) = P'_b(m+1,k) + (1 - P'_b) P_b(m+1,k+1) \tag{44}
\]

and \( P_b(m,k) \) is given in (12).
To proceed further, the following observations are made.

(1) When the destination makes a correct binary decision for the direct link, \( R - m + 2(m - k) = R + m - 2k \geq R + 1 \) for \( (m + 1) - (k + 1) \geq k + 1 \).

(2) When the destination makes an error binary decision for the direct link, \( 2 + R - m + 2(m - k) = 2 + R + m - 2k \geq R + 1 \) for \( (m + 1) - k \geq k \).

Based on the above observations and similar to the derivations in Section 3, it can be shown that

\[
\tilde{P}_B = O\left(\left(\frac{\log E}{E}\right)^{R+1}\right),
\]

\[
P_B^{(a)} P_B = O\left(\left(\frac{\log E}{E}\right)^{R+1}\right).
\]

Thus the diversity order can finally be computed as

\[
d = - \lim_{E \to \infty} \frac{\log \tilde{P}_B}{\log E} = R + 1.
\]

5.3. Combining Multiple-SNR Threshold Method with a Selection of the Best Relaying Link. In general, any cooperative scheme that involves all the relaying links suffers from a loss in spectral efficiency since multiple time slots or frequency bands (equal to the number of relaying links plus one) are required to retransmit one information symbol. In the two-hop scenario, the best relay selection scheme with high spectrum efficiency is very attractive [21]. In [16, 22], Yi and Kim gave a cooperative scheme by combining C-MRC [14] with the best relay selection and showed that such a combined scheme can also achieve the full-diversity order. In [13], Onat et al. presented a threshold-based relay selection protocol, which can also achieve the full-diversity order. The basic idea in Onat’s protocol is that the destination selects only one link with the best SNR from all of the reliable relay links and the direct link, and performs detection based on the single selected link only. We now extend the link selection ideas to the multihop scenario with multiple-SNR thresholds employed for each indirect link and give a novel cooperative relaying protocol in the following.

Consider a multihop cooperation network with \( R \) parallel relay links. In the first phase, the source broadcasts signals, and the relays and destination receive. In the second phase, the destination first selects only one relay link among all of the reliable relay links. When there exits a reliable relay link among all of the relay links, the relays in the selected link detect the received signal and transmit it to the destination, while all of the other relay links keep silent. Finally the destination performs the MRC with the received signals from the best relay link and the received signal from the direct link. If there is no reliable relay link, all of the relay links remain silent and the destination detects only the received signal from the direct link.

Similar to [13], we also set the SNR threshold as

\[
\Theta = \log E^{2R/\beta}.
\]

Following similar derivations in [13], it is not difficult to show that the proposed link selection protocol can achieve the full-diversity order. The main results are as follows.

Case 1. When there exits a reliable relay link among all of the relay links, the average BER can be expressed as

\[
\overline{P}_B^{(a)} = O\left(\frac{R \log E^{2R/\beta}}{E^{R+1}}\right).
\]

Case 2. When there is no reliable relay link, due to the fact that the MRC combining has the same diversity order as the selection combing [23], the proposed scheme has the same diversity order as Onat’s scheme. The average BER in this case is also given as in Case 1; namely,

\[
\overline{P}_B^{(b)} = O\left(\frac{R \log E^{2R/\beta}}{E^{R+1}}\right).
\]

Therefore, the overall system average BER is

\[
\overline{P}_B = \overline{P}_B^{(a)} + \overline{P}_B^{(b)} = O\left(\frac{R \log E^{2R/\beta}}{E^{R+1}}\right),
\]

which shows the full-diversity order of \( d = R + 1 \).

6. Numerical Results and Comparison

This section provides simulation results to illustrate the performance of the proposed method with multiple-SNR thresholds and multiple hard-decision detections. In all of the simulation curves, SNR denotes the total power, \( E_{I_T} \), since the variance of AWGN is set to one. For simplicity only BPSK modulation is employed in all simulations. We will observe the BER performance of networks with two hops when \( N^{(1)} = N^{(2)} = N = 1 \), and we set all the of thresholds to be the same; namely, \( \Theta_1 = \Theta_2 = \Theta \). In Figures 1–3, we set \( \Theta = c_T \log(1 + E_T/(R + 1)) \), which can satisfy the positive property of SNR thresholds for all values of \( E_T \).

First, we observe the diversity performance for different numbers of relays. Figure 1 plots the BER performance with and without SNR thresholds for \( R = 2, 4, 6 \). Here we set \( c_T = (4/\beta) \cdot (1/N) = 2 \), which meets the inequality in (25). As can be seen, the diversity order with SNR thresholds is higher than the one without thresholds for the same \( R \). It can be also seen that the diversity order with or without SNR thresholds becomes higher as \( R \) increases. These simulation results verify our diversity analysis.

Second, we consider the influence of SNR thresholds on the network average BER performance. Figure 2 plots the BER for different thresholds under the case where there is the direct link. In particular, we consider \( R = 3 \) relays and set the constant coefficient to be \( c_T = K \cdot 2 \), with \( K = 3, 2, 1, 0, 1/2, 1/4, 1/8 \). Note that only with \( K = 3, 2, 1 \) the resulting threshold values meet the inequality in (25). Furthermore \( K = 0 \) means the case without setting SNR thresholds. It can be seen that the network BER performance significantly deteriorates as \( K \) increases (and \( K \geq 1/2 \)). The BER curves with larger SNR thresholds (\( K = 3, 2, 1 \)) are
Figure 1: Diversity performance comparison with and without the SNR thresholds for different numbers of the relays.

Figure 2: BER performance comparison for different SNR thresholds when $R = 3$: with the direct link.

Figure 3: BER performance comparison for different SNR thresholds when $R = 8$: without the direct link.

Figure 4: BER performance comparison between the HDD scheme and several MRC schemes when $R = 3$.

better than the ones without SNR thresholds only at very high-SNR region. On the other hand, the BER curves with smaller SNR thresholds when $K = 1/4, 1/8$ are better than the one without SNR-thresholds in low-to-high-SNR region. In particular, in all of the SNR region from 0 dB to 50 dB, the curve with $K = 1/4$ is always better than any other curves. Similar results can be observed in Figure 3 for the network without the direct link (here $R = 8$). Based on the above observations, in the simulations for Figure 4 the best threshold value $(1/2) \log(1 + E_T/(R + 1))$ when $K = 1/4$ is selected.

Third, Figure 4 compares the BER performances achieved by the proposed HDD scheme and three MRC schemes for the cooperative network including the direct link and with $R = 3$. For the proposed HDD scheme, we make use of the best SNR threshold of $(1/2) \log(1 + E_T/(R + 1))$. For Fan’s MRC scheme [12], we use two thresholds: (i) an SNR threshold of $3 \log(E_T/(R + 1))$ (referred to as Threshold 1 in the figure) as suggested in [12] and (ii) the same SNR threshold of $(1/2) \log(1 + E_T/(R + 1))$ (called Threshold 2 in the figure) as applied in our HDD scheme. From Figure 4 it can be seen that Wang’s C-MRC scheme [14] performs the best, followed by Yi’s product MRC scheme [16]. Both Wang’s and Yi’s MRC schemes perform far better than the two threshold-based schemes (Fan’s and our HDD schemes). However, it is important to be emphasized that Wang’s scheme requires the highest amount of signaling overhead since it requires that the exact SNRs of the source-relay links...
be known at the destination. The product MRC scheme by Yi et al. requires that the relays transmit the amplified signals with the gain determined by the corresponding resource-relay channels. This is not a simple DF transmission. At the practical SNR region, our HDD scheme is better than that of Fan’s. Furthermore, since both our HDD and Fan’s schemes are based on the SNR thresholds, at each SNR value of $E_T$, the average total consumed powers in the threshold-based schemes are in fact smaller than the consumed powers in Wang’s and Yi’s MRC schemes. This is a consequence of the fact that there often exists one or more unreliable links. Specifically, the average power saving of our HDD scheme is equal to $R E_T P_u/(R + 1)$. The perfect agreement between simulation and theoretical results of our proposed HDD scheme is also illustrated in Figure 4.

Finally, we simulate the proposed link selection scheme (Section 5.3) for $R = 3$. In particular, Figure 5 plots the BER curves for different thresholds by setting $\Theta = K R \log(E_T/2)$ with $K = 1, 1/2, 1/3, 1/6, 1/12$. Note that only when $K = 1$ the resulting threshold value meets the equation given in (47). The best performance curve is achieved with $K = 1/3$ and this curve is also plotted in Figure 6 to compare our link selection scheme with existing two relay selection schemes in [13, 22]. For Onat’s scheme [13], the two BER curves correspond to the two SNR thresholds of $\Theta = K R \cdot \log E_T/2$, with $K = 1, 1/3$. The first threshold (called Threshold 1) with $K = 1$ comes from [13], and the second threshold (called Threshold 2) with $K = 1/3$ is the same as that used in our scheme. Obviously, the BER performance with Yi’s selection scheme [22] is the best among all of the three selection schemes under comparison. However, it requires that the exact SNRs of the source-relay links be known at the destination. At low-medium SNR region, our scheme is better than Onat’s scheme with Threshold 1, and close to Onat’s scheme with Threshold 2. On the other hand, at high-SNR region, our scheme is better than Onat’s scheme with Threshold 2, and close to Onat’s scheme with Threshold 1. As discussed before, since both our scheme and Onat’s scheme are based on the SNR thresholds, there is a saving in the total consumed power whenever all of the relay links are unreliable. Precisely, the average power saving for our scheme can be determined to be $E_T(P_u)^K/2$.

## 7. Conclusions

In this paper we have proposed and investigated a cooperative transmission scheme for a wireless cooperative relay network with multiple relays. The proposed scheme employs two signal-to-noise ratio (SNR) thresholds and multiple hard-decision detections (HDDs) at the destination. One SNR threshold is used to select transmitting relays, while the other threshold is used at the destination for detection. We derived the exact average bit error probability of the proposed scheme and showed that it can achieve the full-diversity order by setting appropriate thresholds. The diversity result is significant since our proposed scheme does not require the destination to know the exact or average SNRs of the source-relay links. Performance analysis was further extended to multihop cooperation and cooperation with the presence of a direct link. A high spectral-efficiency cooperative transmission scheme was also presented by combining the multiple-SNR threshold method with a selection of the best relaying link. Simulation results were provided to verify the theoretical analysis and demonstrate performance advantage of our proposed schemes over the previously proposed schemes that have a similar complexity.

## Appendices

### A. Proofs of (10), (11), and (23)

First, with only a direct link, the destination receives a signal from the source and makes a hard decision on the received
signal if its SNR is higher than the SNR threshold \( \Theta \). With the Rayleigh fading model, the channel gain magnitude squared, \( \gamma \), has an exponential distribution with mean value \( \Phi \), pdf \( f(y) \), and cdf \( F(\cdot) \). The conditional pdf of \( \gamma \), conditioned on \( y > \Theta \), is given by

\[
f(y \mid y > \Theta) = \frac{f(y)}{1 - F(\Theta)} = e^{\Theta/\Phi} f(y).
\] (A.1)

Then for a general modulation scheme with parameters \( \alpha \) and \( \beta \) as given in (5), the average BER at the destination can be computed as [18]

\[
G(\Theta, \Phi) = \alpha \int_\Theta^\infty Q(\sqrt{\beta y}) f(y \mid y > \Theta) dy
= \frac{ae^{\Theta/\Phi}}{\sqrt{2\pi}} \int_\Theta^\infty \int_\Theta^y e^{-x^2/2} dx \frac{1}{\Phi} e^{-y/\Phi} dy
= \frac{ae^{\Theta/\Phi}}{\sqrt{2\pi}} \int_\Theta^\infty e^{-x^2/2} \int_\Theta^x e^{-y/\Phi} dy dx
= \frac{ae^{\Theta/\Phi}}{\sqrt{2\pi}} \int_\Theta^\infty \int_\Theta^y e^{-x^2/2} \left( e^{-\Theta/\Phi} - e^{-x^2/\Phi} \right) dx
= \frac{\alpha}{\sqrt{2\pi}} \int_\Theta^\infty e^{-x^2/2} dx
- \frac{ae^{\Theta/\Phi}}{\sqrt{2\pi}} \int_\Theta^\infty \sqrt{2e} e^{-x^2/2} dx
= \alpha Q(\sqrt{\beta \Theta}) - ae^{\Theta/\Phi} \sqrt{2e} Q\left(\frac{\Theta + 2 + \beta \Phi}{\beta \Phi}\right).
\] (A.2)

Next, recall that \( p_b(y_i^{(1)}, y_i^{(2)}) \) represents the BER of \( i \)-th relay link as a function of the SNRs \( y_i^{(1)} \) and \( y_i^{(2)} \). It can be calculated as

\[
p_b(y_i^{(1)}, y_i^{(2)}) = \left[ 1 - p_b(y_i^{(1)}) \right] p_b(y_i^{(2)})
+ \left[ 1 - p_b(y_i^{(2)}) \right] p_b(y_i^{(1)})
= \left[ 1 - aQ\left(\sqrt{\beta y_i^{(1)}}\right)\right] aQ\left(\sqrt{\beta y_i^{(2)}}\right)
+ \left[ 1 - aQ\left(\sqrt{\beta y_i^{(2)}}\right)\right] aQ\left(\sqrt{\beta y_i^{(1)}}\right)
= aQ\left(\sqrt{\beta y_i^{(1)}}\right) + aQ\left(\sqrt{\beta y_i^{(2)}}\right)
- 2a^2 Q\left(\sqrt{\beta y_i^{(1)}}\right) Q\left(\sqrt{\beta y_i^{(2)}}\right).
\] (A.3)

Therefore, it follows from (A.2) and (A.1) that

\[
P_b = \int_\Theta^\infty \int_\Theta^\infty p_b(y_i^{(1)}, y_i^{(2)}) f_i(y_i^{(1)} \mid y_i > \Theta) \times f_i(y_i^{(2)} \mid y_i > \Theta) dy_i^{(1)} dy_i^{(2)}
= G(\Theta_1, N(1)^E) + G(\Theta_2, N(2)^E)
- 2G(\Theta_1, N(1)^E)G(\Theta_2, N(2)^E).
\] (A.4)

To prove (23), first observe that

\[
p_b(y_i^{(1)}, y_i^{(2)}) \leq \alpha Q\left(\sqrt{\beta y_i^{(1)}}\right) + aQ\left(\sqrt{\beta y_i^{(2)}}\right)
\leq \alpha Q\left(\sqrt{\beta \Theta_1}\right) + aQ\left(\sqrt{\beta \Theta_2}\right)
\leq 2\alpha Q\left(\sqrt{\beta \Theta_{\text{min}}}\right),
\] (A.5)

where \( \Theta_{\text{min}} = \min\{\Theta_1, \Theta_2\} \). Based on (A.5) and (A.1), and making use of the bound \( Q(x) \leq (1/2)e^{-x^2/2} \), one has

\[
P_b \leq 2\alpha Q\left(\sqrt{\beta \Theta_{\text{min}}}\right)
\times \int_\Theta^\infty \int_\Theta^\infty f_i(y_i^{(1)} \mid y_i^{(1)} > \Theta_1)
\times f_i(y_i^{(2)} \mid y_i^{(2)} > \Theta_2) dy_i^{(1)} dy_i^{(2)}
\leq 2\alpha Q\left(\sqrt{\beta \Theta_{\text{min}}}\right) \leq a e^{-\beta \Theta_{\text{min}}/2}.
\] (A.6)

**B. Proof of (39)**

The proof of (39) will be carried out by induction. Consider the \( i \)-th relay link with \( M \) hops. When \( M = 2 \), the conclusion is obvious due to (A.5). Suppose that the conclusion also holds for \( M = K \); that is,

\[
p_b\left(\{y_i^{(j)}\}_{j=1}^K\right) \leq \sum_{j=1}^K aQ\left(\sqrt{\beta \Theta_j}\right) \leq K aQ\left(\sqrt{\beta \Theta_{\text{min}}}\right).
\] (B.1)

Then we need to prove that the conclusion holds when \( M = K + 1 \). For a relay link with \( K + 1 \) hops, since the BER for the first \( K \) hops (before the last hop to be completed) equals
\[ p_b (\gamma_j^{(i)})^{K+1}_{j=1} = \left[ 1 - p_b (\gamma_j^{(i)})^{K}_{j=1} \right] p_b (\gamma_j^{(K+1)}) + \left[ 1 - p_b (\gamma_j^{(K+1)}) \right] p_b (\gamma_j^{(i)})^{K}_{j=1} \approx \left[ 1 - p_b (\gamma_j^{(i)})^{K}_{j=1} \right] \alpha Q (\sqrt{\beta \gamma_j^{(i)}}) + \left[ 1 - \alpha Q (\sqrt{\beta \gamma_j^{(K+1)}}) \right] p_b (\gamma_j^{(i)})^{K}_{j=1} \leq p_b (\gamma_j^{(i)})^{K}_{j=1} + \alpha Q (\sqrt{\beta \gamma_j^{(i)}}) \leq K \alpha Q (\sqrt{\beta \gamma_j^{(i)}}) = (K+1) \alpha Q (\sqrt{\beta \gamma_j^{(i)}}). \] (B.2)

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**References**

[1] A. Sendonaris, E. Erkip, and B. Aazhang, "User cooperation diversity—part I: system description," *IEEE Transactions on Communications*, vol. 51, no. 11, pp. 1927–1938, 2003.

[2] J. N. Laneman, D. N. C. Tse, and G. W. Wornell, "Cooperative diversity in wireless networks: efficient protocols and outage behavior," *IEEE Transactions on Information Theory*, vol. 50, no. 12, pp. 3062–3080, 2004.

[3] J. N. Laneman and G. W. Wornell, "Distributed space-time-coded protocols for exploiting cooperative diversity in wireless networks," *IEEE Transactions on Information Theory*, vol. 49, no. 10, pp. 2415–2425, 2003.

[4] P. A. Anghel and M. Kaveh, "Exact symbol error probability of a cooperative network in a rayleigh-fading environment," *IEEE Transactions on Wireless Communications*, vol. 3, no. 5, pp. 1416–1421, 2004.

[5] J.-H. Lee and D. Kim, "BER analysis for decode-and-forward relaying in dissimilar Rayleigh fading channels," *IEEE Communications Letters*, vol. 11, no. 1, pp. 52–54, 2007.

[6] W. Su, A. K. Sadek, and K. J. Ray Liu, "Cooperative communication protocols in wireless networks: performance analysis and optimum power allocation," *Wireless Personal Communications*, vol. 44, no. 2, pp. 181–217, 2008.

[7] A. Nosratinia, T. E. Hunter, and A. Hedayat, "Cooperative communication in wireless networks," *IEEE Communications Magazine*, vol. 42, no. 10, pp. 74–80, 2004.

[8] A. W. Eckford, J. P. K. Chu, and R. S. Adve, "Low complexity and fractional coded cooperation for wireless networks," *IEEE Transactions on Wireless Communications*, vol. 7, no. 5, pp. 1917–1929, 2008.

[9] T. Wang, R. Wang, and G. B. Giannakis, “Smart regenerative relays for link-adaptive cooperative communications,” in *Proceedings of the IEEE Conference on Information Sciences and Systems (CISS ’06)*, pp. 1038–1043, Princeton, NJ, USA, March 2007.

[10] F. A. Onat, A. Adinoyi, Y. Fan, H. Yanikomeroglu, J. S. Thompson, and I. D. Marsland, “Threshold selection for SNR-based selective digital relaying in cooperative wireless networks,” *IEEE Transactions on Wireless Communications*, vol. 7, no. 11, pp. 4226–4237, 2008.

[11] F. Onat, Y. Fan, H. Yanikomeroglu, and J. Thompson, “Asymptotic BER analysis of threshold digital relaying schemes in cooperative wireless systems,” *IEEE Transactions on Wireless Communications*, vol. 7, no. 12, pp. 4938–4947, 2008.

[12] Y. Fan, F. A. Onat, H. Yanikomeroglu, and H. V. Poor, “Threshold based distributed detection that achieves full diversity inwireless sensor networks,” in *Proceedings of the Asilomar Conference on Signals, Systems, and Computerse*, Pacific Grove, Calif, USA, October 2008.

[13] F. A. Onat, Y. Fan, H. Yanikomeroglu, and H. V. Poor, “Threshold based relay selection in cooperative wireless networks,” in *Proceedings of the IEEE Global Telecommunications Conference (GLOBECOM ’08)*, pp. 4810–4814, New Orleans, La, USA, November 2008.

[14] T. Wang, A. Cano, G. B. Giannakis, and J. N. Laneman, “High-performance cooperative demodulation with decode-and-forward relays,” *IEEE Transactions on Communications*, vol. 55, no. 7, pp. 1427–1438, 2007.

[15] D. Chen and J. N. Laneman, “Modulation and demodulation for cooperative diversity in wireless systems,” *IEEE Transactions on Wireless Communications*, vol. 5, no. 7, pp. 1785–1794, 2006.

[16] Z. Yi and I.-M. Kim, “Decode-and-forward cooperative networks with relay selection,” in *Proceedings of the IEEE 66th Vehicular Technology Conference (VTC ’07)*, pp. 1167–1171, Baltimore, Md, USA, October 2007.

[17] Z. Yi and I.-M. Kim, “Decode-and-forward cooperative networks with multiuser diversity,” in *Proceedings of the Military Communications Conference (MILCOM ’06)*, October 2006.

[18] A. Goldsmith, *Wireless Communications*, chapter 6, Cambridge University Press, Cambridge, UK, 2005.

[19] J. N. Laneman and G. W. Wornell, "Energy-efficient antenna sharing and relaying for wireless networks," in *Proceedings of the IEEE Wireless Communications and Networking Conference (WCNC ’00)*, pp. 7–12, Chicago, Ill, USA, September 2000.

[20] B. Djeumou, S. Lasaulce, and A. G. Klein, “Combining decoded-and-forward signals in Gaussian cooperative channels,” in *Proceedings of the 6th IEEE International Symposium on Signal Processing and Information Technology*, pp. 622–627, Vancouver, Canada, August 2006.

[21] A. Bletsas, A. Khisti, D. P. Reed, and A. Lippman, “A simple cooperative diversity method based on network path selection,” *IEEE Journal on Selected Areas in Communications*, vol. 24, no. 3, pp. 659–672, 2006.

[22] Z. Yi and I.-M. Kim, “Diversity order analysis of the decode-and-forward cooperative networks with relay selection,” *IEEE Transactions on Wireless Communications*, vol. 7, no. 5, pp. 1792–1799, 2008.

[23] Z. Wang and G. B. Giannakis, “A simple and general parameterization quantifying performance in fading channels,” *IEEE Transactions on Communications*, vol. 51, no. 8, pp. 1389–1398, 2003.