Improving sensitivity to low-mass dark matter in LUX using a novel electrode background mitigation technique

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This paper presents a novel technique for mitigating electrode backgrounds that limit the sensitivity of searches for low-mass dark matter (DM) using xenon time projection chambers. In the Large Underground Xenon (LUX) detector, signatures of low-mass DM interactions would be very low-energy (~keV) scatters in the active target that ionize only a few xenon atoms and seldom produce detectable scintillation signals. In this regime, extra precaution is required to reject a complex set of low-energy electron backgrounds that have long been observed in this class of detector. Noticing backgrounds from the wire grid electrodes near the top and bottom of the active target are particularly pernicious, we develop a machine learning technique based on ionization pulse shape to identify and reject these events. We demonstrate the technique can improve Poisson limits on low-mass DM interactions by a factor of 1.7–3 with improvement depending heavily on the size of ionization signals. We use the technique on events in an effective 5 tonne-day exposure from LUX’s 2013 science operation to place strong limits on low-mass DM particles with masses in the range $m_{\chi} \in 0.15$–10 GeV. This machine learning technique is expected to be useful for near-future experiments, such as LUX-ZEPLIN and XENONnT, which hope to perform low-mass DM searches with the stringent background control necessary to make a discovery.

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I. INTRODUCTION

Numerous astrophysical observations suggest $\sim$25% of the energy density of the Universe is composed of a non-luminous, gravitationally interacting material known as dark matter (DM) [1,2]. A class of weakly interacting massive particles (WIMPs) with masses $m_{\chi} \in 10$ GeV–10 TeV is consistent with observational evidence [3], but without confirmation via direct detection [4–6], the community has begun to more seriously consider well-motivated, lower-mass alternatives [7].

The Large Underground Xenon (LUX) experiment has reported world-leading WIMP-nucleon scattering limits using 95 live days of data from 2013 (WS2013) [8–11] and final limits with increased exposure [5,12]. Although LUX is most sensitive to $m_{\chi} \gtrsim 5$ GeV, there are analysis techniques that can be used to reduce the threshold, allowing us to search for low-mass dark matter using the existing data sets [13–15].

This paper presents a new analysis of WS2013 data, utilizing the smallest signals recorded by the instrument. This is done by incorporating events that contain only ionization signals, which remain robust at very low energies where there are usually no detectable scintillation signals. While this approach improves LUX’s sensitivity to $m_{\chi} \in 0.15$–5 GeV, it introduces a complex set of low-energy backgrounds that have been observed in similar analyses in this class of detectors [15–18]. Recently, much progress has been made to characterize these backgrounds (see e.g. [19–21] and references therein), but it remains the case that advanced analysis techniques will be required to mitigate them adequately. In this paper, we utilize a unique pulse-shape-based machine learning technique to address the most pernicious background, namely, electron pulses originating from the grids. We discuss how this might be further improved upon in near future experiments, such as LUX-ZEPLIN (LZ) and XENONnT, to aid a possible low-mass dark matter discovery.

The LUX detector, now retired, was a two-phase, xenon time projection chamber (TPC) that was operated at the Sanford Underground Research Facility (SURF). Particles scattering in the 250.9 ± 2.1 kg [22] of active liquid xenon mass can produce scintillation photons and free atomic electrons that are converted into two signals called $S1$ and $S2$. The $S1$ is created when the prompt scintillation is detected by 122 photomultiplier tubes (PMTs) located above and below the xenon, as illustrated in Fig. 1. The $S2$ is formed when the electrons drift upward in an electric field produced by gate and cathode wire grid electrodes near the top and bottom of the liquid. A stronger electric field across the liquid-vapor interface extracts the electrons into the gas phase creating proportional scintillation (electroluminescence) that is also detected by the PMTs [23]. With an average amplification of 24.5 photons detected (phd) for every electron, the detector was sensitive to single electrons [21].

LUX has powerful background rejection capability, because of its two signal readout. Radiogenic backgrounds occurring primarily near the edges of the xenon can be cut

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based on their three-dimensional position. The horizontal coordinates of interaction vertices are reconstructed from the $S2$ hit pattern in the top PMTs ($x_{S2}, y_{S2}$), and the vertical coordinate is calculated from the product of drift velocity ($v_{\text{drift}} = 0.152 \pm 0.001 \text{ cm/} \mu \text{ s}$) and time delay between $S1$ and $S2$ ($t_d$). Additionally, discrimination between different types of incident particles is possible using the $S2/S1$ ratio. For example, $\beta$ particles and $\gamma$ rays scatter primarily on atomic electrons, producing relatively less scintillation and more electrons than DM scatters on nuclei for a given observed signal size [24,25]. In the graphical space defined by $S2/S1$ and $S1$, the result is a distinguishable electron recoil (ER) band appearing above a nuclear recoil (NR) band.

In this work, we lower the LUX energy threshold close to the limit of the instrument by accepting events with only an $S2$, in addition to those with both an $S1$ and $S2$. The impact of this choice is illustrated in Fig. 2, which compares the low $S1 + S2$ and the high $S2$ detection efficiencies in the energy range of xenon nuclear recoils produced by low-mass DM. The curves are calculated using the Noble Element Simulation Technique (NEST) version 2.0.1 [26] to simulate the liquid xenon microphysics of signal production and detector physics of signal collection. Below 6 keV$_{nr}$, the $S1 + S2$ detection efficiency tapers off because low light collection efficiency of the PMTs ($\sim 10\%$ averaged over the active volume) prevents the small scintillation signals of nuclear recoils in this energy regime from producing $S1$s that pass LUXs two PMT coincidence criteria (described further in Sec. II). When the requirement that events contain an $S1$ is dropped, efficiency remains high down to 1 keV$_{nr}$. At this point, the small number of electrons produced by nuclear recoil events are sometimes lost due to capture by impurities while drifting (a 0%–30% effect referred to as “electron lifetime”) or remain trapped at the liquid surface due to the 49% extraction efficiency observed in WS2013. (Further details on the additional efficiency curves presented in Fig. 2 are discussed in Sec. II.)

An important side effect of incorporating events with only an $S2$ is that background rejection based on $S2/S1$ ratio and $z$ coordinate becomes impossible. As a consequence, there are elevated rates of low-energy background events from multiple sources.

We observed three categories of electron emission trailing preceding $S1$s and $S2$s (studied in detail in a previous publication [21]). There was photoionization and the photoelectric effect induced by xenon luminescence, delayed emission of electrons trapped under the liquid surface, and capture and release of drifting electrons by impurities. The first category of emission dominates up to 325 $\mu$s following $S1$s or $S2$s (the length of time for an electron to drift the full length of LUX’s TPC), but disappears after this point. These emissions are not a major source of $S2$-only backgrounds because their short time delays allow us to easily to associate them with preceding...
pulses—however, they do complicate event selection, discussed in Sec. II numbered point 1. The last two categories of emission decay over long time scales and generate significant S2-only backgrounds within second-wide time windows following high-energy events that produce many electrons.

In addition to emissions that trailed preceding pulses, we identified two, particularly prevalent categories of events originating on the gate and cathode grids (referred to here as “electrode events”). There was grid electron emission and radiogenic events occurring on/in the grid wires. The former is a process that produces single or multiple electron S2s whose intensities correlate with the electric field magnitude near grid wires [19,20]. These events were observed to occur at hot spots on the grids that intermittently emit electrons for periods of time up to a few tens of seconds and are also expected to occur in less conspicuous patterns continuously throughout the run. The latter are backgrounds from $^{238}\text{U}/^{232}\text{Th}$ contamination inherent to grid wires and plate-out of $^{222}\text{Rn}$ daughters on wire surfaces. Plate-out occurs primarily during construction when components are exposed to air with typical quantities of $^{222}\text{Rn}$. However, it also occurs during operation when charged $^{222}\text{Rn}$ daughters in the xenon drift along electric field lines that terminate on wire surfaces. Small amounts of these isotopes are continuously absorbed in the xenon during normal operation conditions. Specifically, in LUX, they were introduced during a 150 Bq $^{222}\text{Rn}$ injection [28].

After an initial plate-out event, the short-lived daughters quickly decay away leaving only $^{210}\text{Pb}$, with a 22-year half-life, and its two daughters $^{210}\text{Bi}$ and $^{210}\text{Po}$. The most harmful decay products are emitted at low energies. They include $^{210}\text{Pb}$ and $^{210}\text{Bi}$ $\beta$ decays, and recoils of $^{206}\text{Pb}$ nuclei following $^{210}\text{Po}$ $\alpha$ decays in which the $\alpha$ particle travels into the wire.

After applying a set of data selection criteria to minimize most backgrounds, we observed a remaining excess of electrode events. To reduce the excess, a machine learning technique was developed to identify and reject events based on S2 pulse shape, which was observed to differ between S2s originating on the electrodes and those originating in the bulk xenon. In this paper, we show this technique can be used to significantly improve limits in an analysis including S1 + S2 and S2-only events. We suggest refining the technique in near future experiments, such as LZ and XENONnT.

II. DATA SELECTION AND ANALYSIS

To achieve maximum DM sensitivity in an “S1-agnostic” analysis, we introduced new cuts and vetoes that address background challenges not present in previous analyses requiring both an S1 and S2 [9–11,29]. The event selection criteria, exposure, and software threshold are described in further detail in the number points below.

1. Candidate DM events are interactions in the active xenon volume that generate one burst of scintillation and one localized cloud of ionization, as would a single scatter of a DM particle on a xenon nucleus. The corresponding S1 and S2 pulses are grouped in 1 ms event windows by LUX’s standard waveform processing software. Within each window, there may be small secondary pulses from a variety of sources. The most significant contributors are single electron S2s from photoionization and the photoelectric effect of the interactions’ luminescence, and single photon S1s from thermionic dark counts of the PMTs and fluorescence induced when xenon luminescence photons are absorbed by the reflective polytetrafluoroethylene (PTFE) walls surrounding the TPC [13,21]. In addition, to secondary S2s induced by the interaction itself, there can be significant rates of secondary S2s induced by previous large events; however, these pulses are mitigated with a veto detailed in point 4(b).]

Several criteria, similar to those described in [5,8,9], are applied to efficiently select single scatter events containing secondary pulses. S1s were required to have a two PMT coincidence to distinguish them from a single photon; S2s were required to have greater than 55 spikes in their pulse waveform; and event windows were required to contain exactly one S2 preceded by one or zero S1s which pass the second and first conditions, respectively. The S2 condition utilizes a variable called “spike count,” an alternative measure of pulse size sometimes used in place of area in sparse pulses. It corresponds to approximately 2.2 detected electrons as measured using pulse area, 5 $\cdot \sigma$ greater than the mean pulse area of a single electron.

The single scatter detection efficiency, shown in Fig. 2, was measured using tritium $\beta$ decay calibration data as a robust sample of low-energy events in the liquid xenon bulk [30]. The efficiency is $\sim 1$ for events with S2s above the software threshold discussed in the next point.

2. An S2 software threshold of 3.5 detected electrons ($S2 = 85.75$ phd) was selected because efficiency measurements that use tritium calibration data are robust for events with S2s larger than this size. Below 3.5 detected electrons, the calibration data were found to contain non-negligible quantities of background events from delayed emission of electrons trapped under the liquid surface, and capture and release of drifting electrons by impurities.

3. Backgrounds from radioactive contamination on the electrodes and detector walls were mitigated with cuts on event position.

(a) Electrode events with S1s were removed with a drift time cut at $7 < t_{d} < 321$ $\mu$s, whose boundaries correspond to 5 mm below the gate and 2 mm above the cathode.
(b) Due to the geometry of the detector, S2s produced at the junction of the wall and cathode, a starting radius of \( r_{S2} \approx 24 \text{ cm} \), drift upward with a slight radial bias exiting the liquid at a reconstructed radial coordinate of \( r_{S2} \sim 20 \text{ cm} \) [31]. At this exit radius, S2s just above the software threshold have an uncertainty of \( \sigma_{r_{S2}} \sim 1.5 \text{ cm} \) [32]. A cut of \( r_{S2} < 16 \text{ cm} \), greater than \( 2 \cdot \sigma_{r_{S2}} \) from the exit radius, was selected to remove the vast majority of these events.

The 124 kg of xenon mass delimited by the two cuts was calculated from the fraction of accepted \(^{83m}\text{Kr} \) events (a calibration source that distributes itself uniformly in the active mass when injected into the detector). The uncertainty on the calculation has two major contributors. The first is a \( \pm 0.8\% \) contribution from estimates of xenon volume and density used in the active mass calculation from [22]. The second is introduced by the drift cut which can only be applied to events that do have an S1 and, therefore, a determinate \( t_d \). We estimate an additional 2\% contribution to the uncertainty from the mass increase that would occur if the drift cut were to be removed.

4. Three data quality vetoes were used to remove WS2013 data taken under unstable detector conditions or during periods of time with high rates of S2-only backgrounds.

(a) Data taken during April 2013, the beginning of the WS2013 data set, were removed from the analysis because of unstable electron lifetime during this period of time.

(b) A 50 ms veto following large events with a full waveform area greater than \( 1 \times 10^5 \text{ phd} \) was implemented to reduce backgrounds from delayed emission of electrons trapped under the liquid surface, and capture and release of drifting electrons by impurities. In [21], it was shown the intensities of these backgrounds correlate with the size of preceding S2s and decay with exponential and power law-like time dependencies, respectively. Furthermore, their positions in the horizontal plane correlate highly with the location of the S2s. These behaviors suggest previous S2 size, time delay, and position might be used to optimize the veto; however, preliminary tests incorporating this information showed little improvement in the background rate above the 3.5 detected electron analysis threshold. In this region of the spectrum, our fixed “large event veto” maximally reduced the background rate while preserving 93\% of the live time. Below the threshold, however, these background sources are expected to contribute significantly to the event rate. Reference [21] showed a more aggressive veto using previous S2 size and time delay was able to significantly reduce the single electron rate beyond what was attained by our fixed veto, but only with a great reduction of the live time. This aggressive veto had no effect on the rate of S2s above the analysis threshold indicated these pulses originate from other sources, namely, the electrodes.

(c) Periods of time with an unusually high rate of S2s below the analysis threshold were removed because they correlated with high rates of S2s just above the threshold originating from hot spots on the electrodes [19,20]. The below threshold S2s were required to appear in events with a full waveform area less than 2000 phd, to mitigate backgrounds from photoionization and the photoelectric effect induced by xenon luminescence, which are significant in large events. The remaining S2s were required to be composed of greater than 1.2 detected electrons, because a large fraction of S2s failing this cut were observed to be delayed emissions of electrons trapped under the liquid surface, and captures and releases of drifting electrons by impurities [discussed just above in point 4(b)].

After applying these cuts, the average below threshold S2 rate was just a few Hz. The data were grouped in 1 hour long bins and 6\% of bins with the highest S2 rates were rejected. We note that the differences in time and position of consecutive S2s could be used to optimize this veto. Preliminary tests incorporating this information showed potential for reducing the loss of live time from this veto—which was expected considering LUX’s hot spots emitted electrons for burst of only a few tens of seconds while our veto bins are 1 hour in length. However, the tests showed little improvement in the background rate above the analysis threshold.

When combined, the three vetoes have the effect of reducing the live time from the original 95-day exposure to 81 days.

5. The April 2013 data set was scrutinized to identify several categories of pathological events. Multiple cuts on parameters derived by the LUX waveform processing software were designed to remove these events while maintaining >90\% efficiency as measured with tritium data.

(a) There were two types of pathological events associated with the extraction region between the gate and anode: those from interactions occurring in the vapor and those from interactions just below the liquid surface. These events produce proportional scintillation almost immediately after the energy deposition resulting in small or nonexistent time delays between their S1s and S2s. They create S2-only backgrounds when the
waveform processing software mistakenly identifies only a single $S2$ pulse from the combined $S1 + S2$ trace. Because of the attached $S1$, these pulses often have bimodal shapes or reach a maximum very close to their beginning edge. They were tagged and removed using multiple cuts on a set of pulse shape defining parameters (these parameters are discussed in more detail in the context of electrode backgrounds in Sec. III).

(b) Many vapor events have wide, degraded $S2$s due to their electrons traveling through atypical, electroluminescence paths—not simply from liquid surface to anode—and extended $S1$s because of the long lifetime of the scintillation-producing triplet xenon dimer state in the gas phase. The waveform processing software tends to divide the waveforms of these events into many pulses labeling just one an $S2$. They were removed with a cut on “badarea,” a parameter defined as the integrated area of the waveform trace minus the area of the $S1$ and $S2$ pulses. To a smaller extent, the badarea cut removes backgrounds from delayed emission of electrons trapped under the liquid surface, and capture and release of drifting electrons by impurities; however, the “large event” veto described in point 4(b) removes most of these backgrounds prior to application of this cut.

(c) Another fraction of the vapor events occurs just above or below an anode grid wire causing an unusually large fraction of electroluminescence to reach the top or bottom PMTs. These events were mitigated with cut on the asymmetry of $S2$ light collected by top and bottom PMTs.

(d) A small fraction of events from radiocantamination on the detector walls have poor $x_{S2}$, $y_{S2}$ position reconstruction causing them to pass the radial cut defined in point 3(b). Because wall activities are $\sim 10^2$ greater than the bulk, this pathology can be significant. These events were removed using a cut on the chi-squared value of the Mercury position reconstruction algorithm. Multiple scatters with interaction vertices at the same vertical position, but differing horizontal positions, are also removed via this cut.

The effectiveness of the $S2$ quality cuts is quantified in Table I which compares the combined acceptance of relevant vetoes/cuts with the event rate in the region just above the software threshold that most greatly determines sensitivity to low-mass DM.

### Table I

| Description of cut/veto | Signal acceptance | Events 3.5 < $n_e$ < 4.5 |
|-------------------------|-------------------|--------------------------|
| Starting events         | 100%              | 100%                     |
| Large event veto        | 93%               | 28%                      |
| $S2$ quality            | 85%               | 3.5%                     |
| Electrode hot spot veto | 79%               | 0.3%                     |

6. Events with $S2/S1$ ratios outside the 1% and 99% contours of the NR band were rejected for having the wrong recoil type.

7. Populations of $S2$-only events with a single photon pulse preceding the $S2$ by 0–7 $\mu$s or 321–326 $\mu$s are almost entirely composed of gate and cathode backgrounds that have $S1$s with too few photons to pass the two PMT coincidence requirement described in point 1. Because LUX’s waveform processing software only records information about 10 pulses in each event, some of the single photons are not recorded in the final data set forcing us to identify and reject these backgrounds by eye.

Occasionally, the waveform of a genuine bulk event will contain a thermionic PMT dark count or PTFE fluorescence photon preceding the $S2$ by the aforementioned time windows, thus causing the event to be falsely identified as an electrode background. A $1.6 \pm 0.1\%$ efficiency loss due to this random coincidence was calculated from WS2013 average single photon rate measurements for top and bottom PMTs from [13]—a LUX publication describing a detailed study of single photon $S1$ pulses.

### III. Machine Learning Technique for Removing Electrode Backgrounds

#### A. Mitigation with a boosted decision tree

The data selection criteria described in the previous section greatly reduce the background rate, but leave significant populations of events originating on the gate and cathode. This is evident in Fig. 3(top), which shows events in the dark matter search region that do have an $S1$ and, therefore, a determinate $z$ position.

Figure 3(bottom) shows the $S2$ pulse width distributions of LUX’s gate, bulk xenon, and cathode events defined by the drift time cuts $t_d < 7 \mu s$, $7 \mu s < t_d < 321 \mu s$, and $321 \mu s < t_d$. The bulk distribution shows a $\sqrt{t_d}$ trend that is consistent with expectations from diffusion of drifting electrons. If $S2$-only background events from interactions on the gate and cathode followed this trend, they could be removed using a pulse width cut. However, the gate and cathode distributions have a significantly broader spread than what is observed in the bulk, indicating that efficient removal of electrode backgrounds requires a more sophisticated cut. (Note that, in this analysis, we use a pulse half-width parameter instead of full width. It is defined from the
leading edge of the pulse and avoids asymmetric tails occurring on the trailing edge of some pulses due to electron emission and instrumental effects.)

The discrepancy between electrode and bulk xenon S2 width distributions can be explained by the differences in pulse shape summarized in Fig. 4. Panels (a)–(e) contain skew-Gaussian fits of S2 pulses typically found in the WS2013 data. The top panels are fits to bulk xenon S2s from the top, middle, and bottom of the TPC (drift times $\sim10$, $\sim150$, and $\sim300 \mu$s). The S2s are symmetric and have widths that grow predictably with $\sqrt{t_d}$. Some electrode S2s are indistinguishable from those in the bulk xenon, but others are asymmetric and/or sharply peaked like the fits shown in panels (d) and (e). This variety of electrode S2 pulse shapes impairs the accuracy of typical pulse width metrics resulting in broader width distributions.

The phenomenon generating the odd S2 pulse shapes is electric field fringing around grid wires. Figure 4(f) shows a typical electric field profile around a single gate wire (reproduced from [33]). The field lines do not point uniformly in the $z$ direction; instead, they stretch away from the wire surface in arcuate patterns. Furthermore, very

FIG. 3. All WS2013 events in range $3.5 < n_e < 50.5$ containing both an S1 (passing the two PMT coincidence requirement) and S2 pulse, and passing all vetoes/quality cuts applied to S2-only events. Gate, bulk, and cathode events are defined by drift time cuts: $t_d < 7 \mu$s, $7 \mu$s < $t_d$ < $321 \mu$s, and $321 \mu$s < $t_d$. The event rate is vastly higher at the gate and cathode drift times suggesting electrode events are the dominant source of backgrounds.

FIG. 4. Panels (a)–(e) show typical S2 pulse shapes obtained from skew-Gaussian fits to LUX data. The top panels have symmetric shapes that are characteristic of bulk events near the top, middle, and bottom of the TPC (drift times $\sim10$, $\sim150$, and $\sim300 \mu$s). Panels (d) and (e) show asymmetry characteristic of gate S2s whose electrons travel through a range of electric fields. Panel (f) shows a typical electric field profile around a single gate wire (reproduced from [33]). Electric field profiles of cathode wires have a similarly wide range of magnitudes although most field lines, except those at the very top of the wire, point downward. The five red circles in panels (a)–(e) are parameters ($t_{10}$, $t_{25}$, $t_{50}$, $t_{75}$, and $t_{90}$) that mark the times at which the pulse attains 10%, 25%, 50%, 75%, and 90% of its total area. These parameters were used as input to the machine learning algorithm along with maximum pulse height, the time at which the pulse attains its maximum height, and the times at which the rising and falling edges of the pulse reach 0 phd/sample. Note the bulk event profiles on the top panels can also occur for gate and cathode S2s originating on the top of a wire where field curvature is less dramatic.

near the wire surface, the electric field magnitude is proportional to $\sim1/r_w$, where $r_w$ is the wire’s radial coordinate. A two-dimensional COMSOL model was used to calculate the electric field magnitude near the gate and cathode wires in LUX. They are a factor of $\sim10^2$ greater than in the bulk xenon.

When an interaction occurs in a region with electric field fringing, it creates a cloud of electrons that is contorted such that it produces an odd S2 pulse shape. As the electrons drift, they experience drastic changes in electric field that cause their velocity to vary and, thus, the distance between adjacent electrons to stretch or contract. Additionally, sufficiently far apart electrons can experience differences in path length that significantly alter their proximity. The latter effect is most significant near the bottom of gate wires where the curvature of field lines is most dramatic. Events near the cathode wires usually do not produce S2s, because their electrons drift downward along field lines that terminate on the electrode that shields the bottom PMTs. Only 16% of field lines near cathode wires
extend upward and those that do stem from the top of the wire where field curvature is less dramatic. Despite this, some $S_2$s originating on the cathode, as well as those on the gate, were observed to have visibly asymmetric shapes.

Fortunately, the odd $S_2$ shapes created by field fringing can be successfully tagged by holistically quantifying pulse shape. For this reason, we used a machine learning algorithm to design a cut on the full set of LUX parameters that quantify shape. Some examples of these parameters are provided in Figs. 4(a)–4(e). The five red circles along the horizontal axis are the points at which the pulse attains 10%, 25%, 50%, 75%, and 90% of its total area. The varying distances between red circles in panels (a)–(e) are evidence that pulse shape asymmetry is encoded in these quantities. Other shape quantifying parameters are the maximum pulse height, the time at which the pulse attains its maximum height, and the times at which the rising and falling edges of the pulse reach 0 phd/sample.

Out of the many available machine learning methods, we choose a boosted decision tree (BDT) for ease in understanding how the algorithm uses and values input parameters. This algorithm is implemented in PYTHON through the scikit-learn library’s AdaBoost (Adaptive Boosting [34]) classifier. The output is a discriminator score that indicates whether an $S_2$ is more bulk- or electrodelike.

AdaBoost builds a sequence of weak classifiers that focus on different subsets of the training data. In our case, the weak classifiers are decision trees that perform cuts on input parameters to decide whether each data point should be assigned a value of $+1$ (bulklike) or $-1$ (electrodelike). When the $n$th tree has been trained, the data points are reweighted so that misclassified points are given higher importance during training of the $(n+1)$th tree. This iterative procedure is repeated until the desired number of trees have been trained. Although the prediction of each tree is binary, the final discrimination score may take on continuous values from $-1$ to $+1$. It is calculated by averaging the predictions of the decision trees with weights that vary depending on the classification accuracy of the tree [35].

The training and testing data were selected to include $S_2$s of all sizes in the dark matter search range of 3.5–50.5 detected electrons (Fig. 5). Bulklike events were sourced from the tritium calibration data set. They were required to pass all selection criteria outlined in Sec. II. Gate- and cathodelike events were sourced from WS2013. They were required to have both an $S_1$ and $S_2$, pass all vetoes/quality cuts applied to $S_2$-only events, and pass gate or cathode drift time cuts of $t_d < 7 \mu s$ or $321 \mu s < t_d$. Because these criteria produced many more cathode than gate events, the radial cut was relaxed for the latter, to generate a sufficiently large training sample. This choice could potentially make the training data less representative of the backgrounds in WS2013, but this only affects how optimally the BDT removes grid backgrounds and not how conservative the final limit is (which is determined by the Yellin procedure, Sec. IV).

Despite the electric field profile around cathode wires preventing most events from producing $S_2$s, there are many more cathode than gate training events. This is not reliable evidence of greater $^{222}$Rn daughter contamination or a higher electron emission rate on the cathode. Instead, it is primarily a result of detector conditions that tend to enlarge $S_2$s originating on the gate to sizes greater than the 50.5 detected electron upper threshold used in this analysis. Primarily, the larger average electric field near gate wires ($52 \text{ kV/cm}$ compared to $18 \text{ kV/cm}$ on the cathode) enhances the charge yield. Additionally, electrons originating on the cathode drift through the full length of the detector over which they have a 30% chance of being captured by a xenon impurity, while those originating on the gate drift a very short distance and have a very low capture probability. This causes more cathode events to appear in the signal region below 50.5 detected electrons.

The gate, cathode, and tritium training data were weighted to share the same flat $S_2$ area spectrum with a single step at 12.5 detected electrons. Below the step, where both the DM signal spectrum and the April 2013 background spectrum are strongest, the training data were weighted more heavily. Keeping the same spectrum for bulk- and electrodelike classes ensures the algorithm does not rely on $S_2$ area as a means of discrimination, through residual correlation with input parameters. It is necessary because the shapes of the gate and cathode background spectra are unknown, due to the lack of $S_1$s for most events.
Tests on the April 2013 data that were excluded from the final analysis but pass the selection criteria outlined in Sec. II were performed to find the ratios of gate:cathode:tritium events (scale factors multiplying the weighted S2 area spectra) that lead to near-optimal reduction in event rate at fixed signal efficiency. The selected gate:cathode and electrode (gate + cathode):tritium ratios were both 1:1.

Finally, cross-validation on multiple subsets of the training data was used to optimize the BDT’s hyper-parameters, such as maximum decision tree depth and number of trees. The optimal number of trees found was 100, with an optimal maximum depth of 2, though the performance was fairly robust across a wide range of hyperparameter values.

The BDT training performance is best summarized with receiver operating characteristic (ROC) curves. These are plots of signal [tritium (bulk)] acceptance ($e_s$) vs electrode background leakage ($e_b$) calculated by placing a threshold on the discriminator scores of the testing data points at successive values spanning the range $(-1, +1)$. In this space, the diagonal $e_s = e_b$ corresponds to no discrimination (random guessing) and $e_s = 1$ to perfect discrimination. The greater the area under the curve, the greater the discrimination power.

Families of ROC curves generated from gate and cathode training data with differing cuts on S2 size are shown in Fig. 6. It is immediately clear the BDT is more adept at removing gate events compared to cathode events. This outcome was expected, as electron clouds from the cathode experience additional diffusion that erases initial S2 shape information. Discrimination power also increases with S2 size, because larger numbers of electrons form more recognizable pulse shape patterns. This trend is weaker for gate events, which can be efficiently identified and rejected even with few detected electrons.

The ROC curves can be used to estimate a BDT discriminator threshold that maximizes sensitivity to dark matter signals. To aid understanding of these curves, we consider two simple benchmark scenarios where the sensitivity of the analysis is a simple analytic function of the signal and background efficiencies, the quantities plotted in the curves. The background-subtracted scenario models a rare event search analysis with both an assumed signal and a background model (e.g., a profile likelihood ratio). In this case, the sensitivity scales as $e_s / \sqrt{e_b}$, because the mean of the background spectrum can be subtracted, leaving only statistical fluctuations. The second scenario is a na"ive Poisson limit with no background subtraction, in which case the sensitivity scales as $e_s / e_b$. In order to improve the sensitivity relative to an analysis with no grid background cut, the ROC curves must exceed thresholds at $e_s = \sqrt{e_b}$ (background subtracted) or $e_s = e_b$ (Poisson).

The present analysis uses Yellin’s $p_{\text{max}}$ test statistic [36] to calculate sensitivity, as described further in Sec. IV. This approach is expected to scale somewhere between the Poisson and background subtracted extremes, because it takes into account the difference in shape of the data and signal energy distributions, but makes no assumptions about the shape of the background distribution. Given this, both $e_s = \sqrt{e_b}$ and $e_s = e_b$, the thresholds that must be exceeded by the ROC curves for a BDT discriminator threshold to improve sensitivity in a Poisson or background subtracted DM analysis. Stars indicate the points of optimal $e_s / \sqrt{e_b}$.

**FIG. 6.** ROC curves for (a) bulk tritium vs cathode and (b) bulk tritium vs gate test data. The curves can be used to estimate a BDT discriminator threshold that maximizes sensitivity to dark matter signals in an extreme scenario where only gate or cathode backgrounds are present. Two additional curves are plotted to guide the eye: $e_s = e_b$ and $e_s = \sqrt{e_b}$, the thresholds that must be exceeded by the ROC curves for a BDT discriminator threshold to improve sensitivity in a Poisson or background subtracted DM analysis. Stars indicate the points of optimal $e_s / \sqrt{e_b}$. 
backgrounds are present, or cathode backgrounds with \( n_e > 12.5 \).

In our analysis, the discriminator cut was designed to be signal model agnostic by requiring signal acceptance be constant with respect to event energy. It was chosen considering the points of maximum \( \epsilon_s/\sqrt{\epsilon_b} \), indicated as stars on the ROC curves. Based on the clustering of these points, a flat 60\% signal acceptance was imposed by selecting a different discriminator threshold for each of the \( S_2 \) size bins. At this signal acceptance, all ROC curves pass the \( \epsilon_s/\sqrt{\epsilon_b} \) requirement except those from the cathode with \( S_2 \)s of \( n_e < 12.5 \).

To evaluate the effectiveness of the discriminator cut, it was repeatedly modified to produce various choices of \( \epsilon_s \) then applied to April 2013 data passing the selection criteria outlined in Sec. II. In each case, the observed data leakage matched the background leakage calculated from training data with 1:1 gate to cathode ratio, albeit subject to statistical fluctuations in a limited data set. This result substantiates our conjecture that a significant fraction of the \( S_2 \)-only events remaining after the Sec. II cuts/vetoes are electrode backgrounds. Additionally, it is evidence that the gate and cathode training data are representative of the \( S_2 \)-only electrode backgrounds in that the \( S_2 \)s have similarly asymmetric/sharply peaked shapes.

The signal acceptance and background rejection of the discriminator cut (calculated from the training data) are plotted in Fig. 7. By design, the signal acceptance remains near 60\% at all \( S_2 \) sizes. The background rejection slightly improves with \( S_2 \) size as is expected from the trends observed in the ROC curves. Additionally, gate and cathode rejection is similar for \( S_2 \)s with \( n_e > 12.5 \), but cathode rejection falls short of gate rejection by \( \sim 15\% \) for \( n_e < 12.5 \).

**Table II.** Importance of parameters in the BDT. Only the top five (of twelve) are tabulated, for brevity. Here, \( t_s \) corresponds to the time at which the pulse attains \( x\% \) of its total area, as illustrated in Fig. 4, while \( V_{\text{max}} \) is the maximum pulse height.

| Variable        | Importance |
|-----------------|------------|
| \( t_{75} - t_{50} \) | 0.212      |
| \( V_{\text{max}} \)    | 0.153      |
| \( t_{25} - t_{10} \)  | 0.148      |
| \( t_{90} - t_{75} \)  | 0.131      |
| \( t_{50} - t_{25} \)  | 0.083      |

**B. Effectiveness of boosted decision tree**

An understanding of the parameters most useful to the BDT can be gained by looking at the “importances” of the input parameters presented in Table II. For a single decision tree, a parameter’s importance is the fraction of training events separated by each branching node using the parameter, weighted by the reduction of impurity at each node. For a BDT, the overall importance of a parameter is an average of the individual decision tree importances with weights that vary depending on the classification accuracy of the tree (the same weights used in the calculation of the discriminator score). For our training data, the time differences outlining the middle of the pulse (e.g., \( t_{75} - t_{50} \)), as well as the pulse height, are more important than the time differences outlining the tails (not shown in Table II). This inclination of the BDT could be a result of \( S_2 \) waveform noise from photoionization and ionization phenomena that more readily appear at the edges of \( S_2 \) pulses. For example, the trailing edge of \( S_2 \)s can overlap with electron signals produced by the quantum efficiency of electroluminescence incident on the gate. These electrons will obscure the original shape of the \( S_2 \)’s trailing edge.

![FIG. 7. Signal acceptance and background rejection capability of the boosted decision tree used to tag and remove gate- and cathodelike events. The cut is not applied below the software threshold.](image1)

![FIG. 8. Half-width distributions of training data before and after applying a discriminator cut tuned to 60% signal efficiency.](image2)
Figure 8 shows the half-width distributions of training data before and after applying the selected discriminator cut. As designed, the cut greatly reduces the gate and cathode distributions while mostly preserving the tritium (bulk) distribution. While the averages of all three distributions shift toward central (bulklike) values, there are tails remaining at small and large half-widths. These tails are evidence the BDT is finding new features, more subtle than half-width, that are useful for discriminating between electrode and bulk events.

To characterize improvement of limits from using LUX’s full set of shape quantifying parameters compared to just half-width, a second BDT was run using half-width as the only input parameter. Training hyperparameters were also varied for this BDT, with minimal effect on performance. Figure 9 compares the ROC curves of the “total” and “half-width” BDTs for the smallest and largest S2 size bins using the combined training + testing data set. For the cathode, both bins have similarly shaped total and half-width ROC curves suggesting diffusion experienced by cathode S2s has the effect of washing away pulse shape information other than pulse width. For the gate, the ROC curves of the smallest bin show the same lack of improvement. However, in the largest bin, the total ROC curve sits far above the half-width ROC curve indicating a large improvement from the addition of extra shape parameters.

The points of maximum improvement for background subtracted and Poisson limits are indicated as stars and circles in Fig. 9. Poisson limits are maximized at equal or lower $\epsilon_s$ than background subtracted limits. Because they have a greater dependence on $\epsilon_b$ than background subtracted limits, Poisson limits favor lower values of $\epsilon_b$ despite the accompanying decrease in $\epsilon_s$.

Figure 10 uses the combined training + testing data set to show the effectiveness of the BDT as it depends on S2 size. It shows the maximum expected limit improvement for each S2 size bin considering extreme cases of only gate backgrounds or only cathode backgrounds. Poisson limit improvement factors are in the range 1.7–3 demonstrating our machine learning technique is effective at improving limits based solely on comparing signal and observed event spectra. Poisson limit improvement is a factor of 1.3–2 greater than that calculated for background subtracted limits, which can be explained by the Poisson limits’ greater dependence on $\epsilon_b$. For all gate background scenarios, the limit improvement increases by a factor of 1.5–2

![Figure 9](image_url)

**FIG. 9.** ROC curves of training + testing data for a BDT using all shape quantifying parameters compared to a BDT using only half-width. Points of maximum limit improvement are shown by stars and circles for background subtracted and Poisson cases, respectively.

![Figure 10](image_url)

**FIG. 10.** Predicted maximum improvement in exclusion limits for background subtracted ($\epsilon_s = \sqrt{\epsilon_b}$) and Poisson ($\epsilon_s = \epsilon_b$) scenarios, calculated separately for extreme cases of only gate backgrounds or only cathode backgrounds. Points of maximum improvement correspond to the stars and circles from Fig. 9 for the BDT using all parameters. Since we do not know the energy spectrum of the background, distinct values are given for each S2 size bin; the final improvement would be a weighted average of the values shown.
An increase is expected due to the greater amount of pulse shape information encoded in larger pulses.

**IV. RESULTS AND SENSITIVITY**

The final WS2013 data, after applying all cuts described in Sec. II and the BDT discriminator cut in Sec. III (A), are plotted in Fig. 12. The spectrum rises near the analysis threshold, though this is significantly mitigated by the BDT cut, which reduces the observed event rate by a factor of $\sim 4$ while retaining approximately 60% signal efficiency independent of $S_2$ size. This background reduction factor is consistent with the approximately 75% background rejection expected from the training model (Fig. 7). This outcome demonstrates a substantial and efficient removal of electrode backgrounds using only $S_2$ pulse shape information, which is useful even for small $S_2$ of only a few detected electrons. The residual rate of events just above the 3.5 detected electron software threshold is approximately 7 events/tonne/day/electron, after correcting for cut efficiencies.

Two DM signal hypotheses were tested against the data presented in Fig. 13. First was the traditional spin-independent (SI) elastic scatter of DM on a xenon nucleus whereafter the nucleus recoils, ionizing and exciting neighboring xenon atoms in its path. Detection through this NR channel is limited to dark matter particles with $m_\chi \gtrsim 2$ GeV which are able to transfer enough momentum

![FIG. 11. Sensitivity calculations employed NEST v2.0.1 NR and ER charge yield models (solid black curves), with a hard cutoff in yield below 0.3 keV$_{nr}$ and 0.186 keV$_{ee}$, respectively. Charge yield measurements for NRs are from [37,38], while those for ERs are from [30,39–41].](image)

![FIG. 12. DM search data from May through September 2013 before and after applying the BDT cut and hand scanning to remove events that originated on the electrodes. The BDT cut reduces the observed event rate by a factor of $\sim 4$ while retaining approximately 60% signal efficiency independent of $S_2$ size. DM spectra at the 90% confidence interval cross-section limit are overlaid for comparison.](image)

![FIG. 13. Upper limits on the spin-independent DM-nucleon cross section at 90% C.L. The result of the $S_2$-only analysis with an NR signal model is shown in black, and the result of the $S_2$-only analysis with a signal model based on the Migdal effect is shown in gray. Also shown are limits from DarkSide-50 [18] (S1-only, binomial fluctuation assumption), CDMSlite [48], CRESST-III [49], XENON100 S2-only [16], XENON1T S1 + S2 [6], XENON1T S2-only [17] (NEST 2.0.1 yields), XENON1T S2-only with Migdal effect [47], and past LUX searches using S1 + S2 events [5], including S1s with single photons using double photoelectron emission (DPE) [13], and the Migdal effect [11].](image)
to a heavy xenon nucleus to produce S2s above the analysis threshold. In a small fraction of DM scatters, a second signal type is expected to be produced via the “Migdal effect” [42,43]. It arises when the recoiling xenon nucleus induces a change in atomic energy levels, forcing the emission of a ~keV electron that also ionizes and excites neighboring atoms. Although rare, this type of ER signal enables DM detectors to probe lower DM masses than those possible via the traditional NR channel. A small fraction of sub-GeV DM scatters are calculated to produce an above-threshold S2 via the Migdal effect, even when the NR signal is undetectable. While there has been no experimental confirmation of the Migdal effect to date, various experiments have applied the theory in DM searches [44–47]. Details of the Migdal signal model applied in this work are published in [11], which outlines a search for DM via this channel using WS2013 data with both an S1 and S2.

The detectors responses to the traditional NR and Migdal signals were modeled with NEST v2.0.1—assuming a DM velocity distribution calculated from the Standard Halo Model as in [50]. NEST relies on NR and ER charge yield models that are fit to empirical data, as shown in Fig. 11. Below the lowest experimental data points at 0.3 keVnr and 0.186 keVee, the charge yields are conservatively assumed to be zero. The overall signal efficiency is modeled according to Fig. 2, with an additional ~60% reduction from the BDT cut.

NR and Migdal upper limits presented in Fig. 13 were calculated using Yellin’s pmax test statistic [36]. The limits are an unbinned comparison between the set of WS2013 events passing all cuts and a signal model of one variable, in this case the S2 size. Unlike a simple Poisson analysis, this type of limit utilizes the difference in shape between the signal and observed spectra allowing for stronger exclusion limits without requiring a known background model.

A potential source of uncertainty in the signal model is introduced by the electrode cut. Because the gate and cathode are at the top and bottom of the detector, the cut has a greater tendency to remove signal-like events at short and long drift times compared to those at intermediate times. This can, in principle, affect the signal spectrum through the dependence of S2 size on drift time. This uncertainty was investigated by generating two versions of the signal spectra: one uniform in drift time and a second generated according to a Gaussian distribution narrowly focused at the center of the detector. The limits generated by these two models differ by less than 4% at all DM masses, a negligible change. The curve in Fig. 13 is produced by the uniform distribution.

The low-threshold, S1-agnostic analysis described in this paper provides increased sensitivity to low-mass DM, compared to LUX’s standard S1 + S2 analyses of NR and Migdal signals [5,11]. This improvement is primarily due to inclusion of events with S2s smaller than 10 detected electrons and no S1s. In this signal regime, one can see from Fig. 7 that gate events are rejected with greater efficiency than those from the cathode.

Through a combination of lower threshold, reduced inherent detector backgrounds, and careful removal of electrode events, LUX has been able to substantially improve on previous DM-nucleon scattering cross-section limits from XENON100 [16], an experiment with a target mass similar to LUX. The present sensitivity is approximately comparable to that obtained by the DarkSide-50 experiment [18], though we note that the DarkSide-50 analysis relies on a broad spectrum energy calibration in the crucial regime below about 7 keV. Other measurements in this regime suggest an approximately 30% lower electron yield [51,52] that lessens with decreasing recoil energy. New, direct measurements are urgently needed to confirm those results. Finally, we note that the present results are not as stringent as those obtained by the larger XENON1T experiment [17], whose exposure is approximately a factor of 4 greater than that of LUX.

Electrode events are likely to remain a challenge for LZ and other xenon experiments searching for low-mass dark matter, as well as coherent neutrino-nucleus scattering of solar 8B neutrinos. Because the machine learning technique introduced in this paper is highly dependent on S2 size, it is expected to be of equal or greater success in LZ due to low-energy signals containing greater numbers of electrons (primarily a result of a greater extraction efficiency, predicted to be 95% in LZ compared to 49% in LUX WS2013). The technique works in concert with treatments used to reduce electron emission rates from LZ grid wires. In particular, acid passivation was demonstrated by [20] to bring about order-of-magnitude reductions of emission rate by improving the quality of the oxide layer on wire surfaces.

Although LZ expects a higher event rate than what was measured in LUX, thus a greater intensity of electron emissions trailing previous events, we anticipate these backgrounds will remain manageable in the region of the spectrum above a few electrons. LZ’s larger size will allow selection of a low background region near the center of the active mass with a significantly attenuated γ-ray intensity, the greatest source of high-energy backgrounds in this type of detector. Furthermore, previous S2 size, position, and time delay information can be used to design a more advanced veto than what was used in this LUX analysis. We also note that LZ’s improved extraction efficiency will mitigate backgrounds from delayed emission of electrons trapped at the liquid surface, the only source of multiple electron S2s identified in [21] apart from those originating at the electrodes or radiogenic events within the xenon.

Finally, we suggest the success of the machine learning technique might be improved further by feeding entire S2 waveforms from each PMT into a convolutional neural

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network or similar algorithm intended for low-level input, instead of just 12 shape-defining parameters. We note that such an approach would introduce additional computing burden, but it would likely lead to a significant improvement in discrimination power considering the substantial increase in potentially useful information.

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