Biotechnology and Industrial Microbiology

Growth kinetic models of five species of Lactobacilli and lactose consumption in batch submerged culture

Fazlollah Rezvani\textsuperscript{a}, Fatemeh Ardestani\textsuperscript{b,}\textsuperscript{*}, Ghasem Najafpour\textsuperscript{c}

\textsuperscript{a} Islamic Azad University, Shahrood Branch, Department of Chemical Engineering, Shahrood, Iran
\textsuperscript{b} Islamic Azad University, Qaemshahr Branch, Department of Chemical Engineering, Qaemshahr, Iran
\textsuperscript{c} Babol Nooshirvani University of Technology, Faculty of Chemical Engineering, Biotechnology Research Lab., Babol, Iran

\textbf{A R T I C L E  I N F O}

Article history:
Received 7 June 2015
Accepted 20 September 2016
Available online 3 January 2017
Associate Editor: Maricê Nogueira de Oliveira

Keywords:
Bacterial growth
Exponential kinetic model
Contois model
Lactobacilli

\textbf{A B S T R A C T}

Kinetic behaviors of five Lactobacillus strains were investigated with Contois and Exponential models. Awareness of kinetic behavior of microorganisms is essential for their industrial process design and scale up. The consistency of experimental data was evaluated using Excel software. L. bulgaricus was introduced as the most efficient strain with the highest biomass and lactic acid yield of 0.119 and 0.602 g g\textsuperscript{-1} consumed lactose, respectively. The biomass and carbohydrate yield of L. fermentum and L. lactis were slightly less and close to L. bulgaricus. Biomass and lactic acid production yield of 0.117 and 0.358 for L. fermentum and 0.114 and 0.437 g g\textsuperscript{-1} for Lactobacillus lactis were obtained. L. casei and L. delbrueckii had the less biomass yield, nearly 11.8 and 22.7% less than L. bulgaricus, respectively. L. bulgaricus (R\textsuperscript{2} = 0.9500 and 0.9156) and L. casei (R\textsuperscript{2} = 0.9552 and 0.8401) showed acceptable consistency with both models. The investigation revealed that the above mentioned models are not suitable to describe the kinetic behavior of L. fermentum (R\textsuperscript{2} = 0.9367 and 0.6991), L. delbrueckii (R\textsuperscript{2} = 0.9493 and 0.7724) and L. lactis (R\textsuperscript{2} = 0.8730 and 0.6451). Contois rate equation is a suitable model to describe the kinetic of Lactobacilli. Specific cell growth rate for L. bulgaricus, L. casei, L. fermentum, L. delbrueckii and L. lactis with Contois model in order 3.2, 3.9, 67.6, 10.4 and 9.8-fold of Exponential model.

© 2017 Sociedade Brasileira de Microbiologia. Published by Elsevier Editora Ltda. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/licenses/by-nc-nd/4.0/).

\textbf{Introduction}

Kinetic models are useful tools in design and control of biotechnological processes to obtain improved knowledge about microbial growth behavior using mathematical models along with specifically accurate and repeatable detailed experiments. Cell growth time-courses are involved individual growth phases: lag phase, exponential growth phase, stationary phase and the phase with exponential decay. Nonlinear mathematical models used to identify growth parameters.\textsuperscript{1}

\textsuperscript{*} Corresponding author.
E-mails: f.ardestani@qaemiau.ac.ir, Ardestani_fatemeh@yahoo.com (F. Ardestani).
http://dx.doi.org/10.1016/j.bjm.2016.12.007
1517-8382/© 2017 Sociedade Brasileira de Microbiologia. Published by Elsevier Editora Ltda. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/licenses/by-nc-nd/4.0/).
Lactobacillus is a genus of gram-positive facultative anaerobic bacteria also known as one of the main groups of probiotic organisms involved in functional foods. A common feature of these microorganisms is their antagonistic activity against some pathogens such as salmonella spp., Escherichia coli, Listeria monocytogenes, Clostridium perfringens and Helicobacter hepaticus. The capability of L. plantarum and L. reuteri in phytic acid hydrolysis is valuable in bread processing technology. Inoculating hetero-fermentative lactic acid bacteria to alfalfa silages cause to increase the production of lactic and acetic acids, hence decrease pH, reduce the number of yeasts and moulds, and inhibit Enterobacterium and Klebsiella pneumoniae. Lactobacilli are widely applied in industrial enzyme production processes, for example glucose-forming amylase and lactase. Different strains of Lactobacilli are the main fermentative lactic acid and γ-aminobutyric acid producers used in commercial processes as well as starters in dairy products.

Kinetic behavior of Lactobacilli was studied by some previous researchers. Ghaly et al. reported that high lactose concentrations had an inhibitory effect on L. helveticus growth rate. They also emphasized that adding yeast extract to culture medium and using micro aeration could cause to increase the specific growth rate and lactose consumption of Lactobacilli. Vasudha and Hari investigated Gompertz and Logistic kinetic models for L. plantarum NCDC 414. The viable cell counts increased from 4 × 10^6 to 7 × 10^10 CFU mL\(^{-1}\) at 24 h. Cock and Stouvenel studied lactic acid production by L. lactis subs lactis and showed that up to 35 g L\(^{-1}\) lactic acid was obtained in fermentation with using 60 g L\(^{-1}\) of initial glucose. Amran evaluated the growth kinetic of L. helveticus on whey permeate. He characterized and described five separate phases during L. helveticus growth. L. rhamnosus cell dry weight was obtained; which was equal to 23 g L\(^{-1}\) after 18 h incubation at appointed bioreactor conditions. Gupta et al. found that L. plantarum cell growth rate was improved with an increase in agitation speed. It was also found that malic acid as carbon source enhanced the specific growth rate of L. plantarum from 0.2 to 0.34 h\(^{-1}\). The study of cell growth and substrate utilization kinetic of L. casei and L. rhamnosus showed as strong exponentially dependent on product inhibition at low lactic acid concentrations. In our best of knowledge, there is not any documented report on Lactobacilli kinetics with Contois and Exponential kinetic models. In this article, kinetic behavior, cell growth and substrate consumption trends of five different strains of Lactobacilli were investigated. Based on Contois and Exponential kinetic models in a batch submerged culture whey as the main nutrients of the medium was used. In each case, influential kinetic parameters were determined.

Materials and methods

Microorganisms and inoculum preparation

Lactobacillus species: L. casei subsp. casei PTCC1608, L. delbrueckii subsp. delbrueckii PTCC1333, L. delbrueckii subsp. bulgaricus PTCC1757, L. fermentum PTCC1744 and L. delbrueckii subsp. lactis PTCC1743 were prepared from Iranian Research Organization for Science and Technology.

The stock culture of each strain was separately prepared on MRS medium. Inoculated cultures were incubated at 37°C for 48 h and then stored in a refrigerator at 4°C. Batch submerged fermentation process was performed in separate laboratory shake flasks contained of deproteinized sterile whey as the main substrate. The culture media was enriched by adding some growth factors including (gL\(^{-1}\)): lactose, 50; yeast extract, 10; sodium acetate, 5; KH\(_2\)PO\(_4\), 2; MgSO\(_4\), 0.2; MnSO\(_4\), 0.05; FeSO\(_4\), 0.03; peptone, 10.

Culture preparation

100 mL of deproteinized and enriched sterile whey was added to a 250 mL shake flask. Before autoclaving, pH was adjusted to 6.5 by a 2 M NaOH solution or 2 N HCl. To prevent undesired reactions, deproteinized whey and the enrichment media were separately autoclaved at 121 °C for 15 min and then were mixed together in sterile conditions to obtained 100 mL final culture medium in each shake flask.

Batch submerged fermentation

Inoculation was performed by adding 2.5 mL of Lactobacillus stock culture to each shake flask. Then, the flasks were incubated at 37 °C mixed with agitation speed of 50 rpm for 50 h. At this period, samples were removed at proper 5 h intervals to assay lactic acid, lactose and cell dry weight concentrations.

Assessments

Lactic acid and lactose concentrations were analyzed by high performance liquid chromatography (HPLC, Perkin Elmer 200, Shimadzu, Japan) with Aminex HX-87H column. The mobile phase consisted of 5 mM sulfuric acid solution at 40 °C and flow rate of 0.6 mL min\(^{-1}\) was used.

Cell dry weight was assayed using a spectrophotometer (Shimadzu, 1601, Japan) at a wavelength of 480 nm. Standard dilute solutions of bacterial cell were prepared from stationary phase of cell growth. To determine cell dry weight calibration curve, 15 mL of each standard sample was passed through a cellulose acetate filter with 0.45 micron pore size. Filters then washed with distilled water and dried at 100 °C for 24 h. Cell dry weight was calculated based on differences between the initial and the final filter weights. For each Lactobacillus species, a separate standard curve of cell dry weight versus absorption value was recorded; which was applied to determine cell dry weight in actual experimental samples.

Kinetic models

Contois (Eq. (1)) is an un-structured kinetic model based on substrate and biomass concentration and Exponential (Eq. (2)) kinetic models is another un-structured kinetic model based on only substrate concentration.

\[
\mu = \mu_{\text{max}} \frac{S}{K_S + S} \quad (1)
\]

\[
S = S_0 + S_1 \left[1 - \exp(\mu_{\text{max}} \cdot t)\right] \quad (2)
\]
where $\mu$ and $\mu_{\text{max}}$ is the specific growth rate and the maximum specific growth rate of bacterial strain in term of h$^{-1}$, respectively. $K_s$, $S_0$, $S_1$, $X$ and $X_m$ is the semi-saturated coefficient, the limiting substrate (lactose) concentration, initial lactose concentration, required lactose for initial cell biomass forming, cell dry weight and the maximum cell dry weight in term g.L$^{-1}$, respectively.

Results

Cell growth

Five different Lactobacilli species were studied for cell growth evaluation for incubation period of 50 h. Deproteinized whey as carbon sources was used in a submerged batch culture. Almost for all studied strains, a 6 h lag phase period and 25–45 h (depend on the strain) exponential growth phase was observed. Table 1 presents biomass production and lactic acid consumption trends for five different strains of Lactobacilli.

Fig. 1 presents cell dry weight and lactic acid production as well as lactose consumption profile for L. delbrueckii subsp. bulgaricus PTCC1737. After incubation period of (the real end of the exponential growth phase) maximum cell dry weight (5.1 g.L$^{-1}$) was obtained. The rate of biomass productivity was calculated as 0.17 g.L$^{-1}$h$^{-1}$ for this strain. Maximum produced lactic acid by L. delbrueckii subsp. bulgaricus PTCC1737 was defined to be 26.6 g.L$^{-1}$. For this strain, maximum lactic acid yield and productivity was determined of 0.602 g.g$^{-1}$ consumed lactose (after 52 h incubation) and 0.804 g.L$^{-1}$h$^{-1}$ (after 24 h incubation), respectively. Results showed that cell dry weight was increased from 0.9 to 5.1 g.L$^{-1}$ (more than 466% increase in cell density) at a period of 18 h in exponential growth phase.

Similar behavior, of course with lower efficiency was observed for L. casei subsp. casei PTCC1608 (Fig. 2). For this strain, produced cell biomass has reached to 3.4 g.L$^{-1}$ after 36 h incubation. Biomass productivity of L. casei subsp. casei PTCC1608 was calculated 0.119 g.L$^{-1}$h$^{-1}$. Maximum lactic acid concentration of 24.2 g.L$^{-1}$was obtained. For this strain, maximum lactic acid yield and productivity was determined as 0.586 g.g$^{-1}$ consumed lactose (48 h after incubation) and 0.696 g.L$^{-1}$h$^{-1}$ (after 24 h incubation), respectively. However, cell dry weight was increased from 0.8 to 4.3 g.L$^{-1}$ (more than 437% increase in cell density) at a period of 24 h in exponential growth phase.

L. delbrueckii subsp. lactic PTCC1743 reached to its end of exponential growth phase after 24 h incubation. At this time, cell dry weight was 3.1 g.L$^{-1}$ and then, remained constant for a period of 18 h. But at the end of the stationary phase (after 48 h incubation) suddenly increased to 3.9 g.L$^{-1}$ and then decreased again to 3.1 g.L$^{-1}$ after 52 h incubation (Fig. 3). Biomass productivity of L. delbrueckii subsp. lactic PTCC1743 was evaluated equal to 0.081 g.L$^{-1}$h$^{-1}$ after 48 h. In exponential growth phase, cell dry weight was increased from 0.6 to 3.1 g.L$^{-1}$ (more than 416% increase in cell density) at a period of 12 h. Maximum lactic acid concentration was obtained as 14.7 g.L$^{-1}$ at after 42 h incubation. Maximum lactic acid yield and productivity was obtained 0.437 g.g$^{-1}$ consumed lactose (after 42 h incubation) and 0.47 g.L$^{-1}$h$^{-1}$ (after 30 h incubation), respectively.

L. delbrueckii subsp. delbrueckii PTCC1333 had an extended exponential growth phase until 42 h after incubation. At this time, cell dry weight reached to 3.2 g.L$^{-1}$ (Fig. 4). Biomass productivity of L. delbrueckii subsp. delbrueckii PTCC1333 was obtained as 0.076 g.L$^{-1}$h$^{-1}$ after 52 h incubation. Lactic acid production was observed both at exponential and the stationary growth phases. Maximum lactic acid concentration (13.2 g.L$^{-1}$) was obtained after 52 h incubation (end of the stationary phase). Maximum lactic acid yield and productivity was obtained 0.351 g.g$^{-1}$ consumed lactose (after 52 h incubation) and 0.317 g.L$^{-1}$h$^{-1}$ (after 36 h incubation), respectively.

Fig. 1 – Cell dry weight and lactic acid production as well as lactose consumption profile for Lactobacillus delbrueckii subsp. bulgaricus PTCC1737 in a submerged batch culture of deproteinized whey at 37 °C with 50 rpm agitation speed for 52 h.

Fig. 2 – Cell dry weight and lactic acid production as well as lactose consumption profile for Lactobacillus casei subsp. casei PTCC1608 in a submerged batch culture of deproteinized whey at 37 °C with 50 rpm agitation speed for 52 h.

Fig. 3 – Cell dry weight and lactic acid production as well as lactose consumption profile for Lactobacillus delbrueckii subsp. lactic PTCC1743 in a submerged batch culture of deproteinized whey at 37 °C with 50 rpm agitation speed for 52 h.
Fig. 254

Table 1 - Biomass and lactose concentrations and specific growth rate for five studied Lactobacilli in a submerged batch culture medium of lactose fortified whey at 37 °C with 50 rpm agitation speed for 52 h.

|        | Time (h) 0 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 52 |
|--------|------------|---|----|----|----|----|----|----|----|----|----|
| L. bulgaricus | X (g L⁻¹) | 0.2 | 0.9 | 2.5 | 4.2 | 5.1 | 5.1 | 5.1 | 5.1 | 5.2 |
|         | S (g L⁻¹) | 47.9 | 40.1 | 26.6 | 13.5 | 7.3 | 7 | 6.7 | 6.1 | 5.8 |
|         | µ (h⁻¹)   | - | 0.250 | 0.210 | 0.169 | 0.135 | 0.108 | 0.089 | 0.077 | 0.071 |
| L. casei | X (g L⁻¹) | 0.2 | 0.8 | 2.6 | 3.9 | 4.2 | 4.3 | 4.3 | 3.8 |
|         | S (g L⁻¹) | 48.2 | 42.1 | 31.9 | 17.8 | 10.5 | 9.2 | 9.1 | 8.7 | 8 |
|         | µ (h⁻¹)   | - | 0.231 | 0.214 | 0.165 | 0.127 | 0.102 | 0.085 | 0.072 | 0.064 |
| L. lactis | X (g L⁻¹) | 0.2 | 0.6 | 1.9 | 3.1 | 3.2 | 3.1 | 3.4 | 3.9 | 3.1 |
|         | S (g L⁻¹) | 49.2 | 38.8 | 27.3 | 21.4 | 19.6 | 18.2 | 16.4 | 15.8 | 13.2 |
|         | µ (h⁻¹)   | - | 0.183 | 0.188 | 0.152 | 0.115 | 0.091 | 0.079 | 0.071 | 0.059 |
| L. delbrueckii | X (g L⁻¹) | 0.2 | 0.6 | 1.7 | 2.4 | 2.6 | 2.9 | 3.2 | 3.1 | 3 |
|         | S (g L⁻¹) | 48.1 | 36.4 | 25.3 | 22.1 | 18.2 | 16.4 | 15.1 | 13.6 | 12.4 |
|         | µ (h⁻¹)   | - | 0.183 | 0.178 | 0.138 | 0.107 | 0.089 | 0.077 | 0.077 | 0.058 |
| L. fermentum | X (g L⁻¹) | 0.1 | 0.7 | 2.1 | 2.5 | 2.7 | 2.9 | 3.3 | 3.5 |
|         | S (g L⁻¹) | 49.3 | 44.2 | 35.6 | 29.1 | 26.8 | 25.3 | 23.2 | 22.6 | 20.1 |
|         | µ (h⁻¹)   | - | 0.324 | 0.254 | 0.179 | 0.137 | 0.110 | 0.093 | 0.083 | 0.077 |

L. fermentum PTCC1744 had the longest exponential growth phase; after 52 h incubation period, maximum cell dry weight of 3.5 g L⁻¹ was obtained (Fig. 5). In addition, its biomass productivity was 0.067 g L⁻¹ h⁻¹. Lactic acid production was observed at both exponential and the stationary growth phases. Maximum lactic acid concentration (10.7 g L⁻¹) was obtained at the end of the stationary phase. Maximum lactic acid yield and productivity was defined as 0.358 g g⁻¹ consumed lactose (after 52 h incubation) and 0.29 g L⁻¹ h⁻¹ (after 30 h incubation), respectively.

**Contois kinetic**

In order to evaluate the consistency of five studied strains with Contois kinetic model, experimental data of lactose consumption and cell dry weight production in exponential growth phase were used (Table 1). Fig. 6 represents the linear fitted experimental data using Contois kinetic model for five investigated Lactobacilli strains.

Maehus law explains the exponential growth phase of Lactobacillus species in a batch culture (Eq. (3)). Integration of Eq. (3) using suitable initial condition (X = X₀ at t = t₀) resulted in Eq. (4) that demonstrates specific cell growth rate (µ). The values for initial biomass concentration and lag phase time delay (X₀ and t₀) were considered 0.2 g L⁻¹ and 6 h, respectively.

\[
\frac{dX}{dt} = \mu X
\]

\[
\mu = \frac{\ln \left( \frac{X}{X_0} \right)}{t - t_0}
\]

Specific cell growth rate values were calculated according to the cell dry weight as biomass concentration (X) and average lactose concentration as limiting substrate concentration (Savg) for the exponential growth phase using Eq. (4). Kinetic constant coefficients (µ_max, Ks) were calculated using the curve fitting method.

**Exponential model**

The consistency of the practical data for the cell growth and lactose consumption of five studied Lactobacillus species with
Exponential kinetic model is presented in Fig. 7. $F(S)$ was defined as Eq. (5).

$$F(S) = \left( \frac{S_0 + S_1 - S}{S_1} \right)$$  \hspace{1cm} (5)

Specific cell growth rate was calculated for each of studied Lactobacilli in exponential and the stationary growth phases are presented in Table 1.

**Discussion**

The analysis of obtained results (presented in Table 1) showed that *L. delbrueckii* subsp. *bulgaricus* PTCC1737, *L. fermentum* PTCC1744 and *L. delbrueckii* subsp. *lactis* PTCC1743 had the highest biomass yield of 0.119, 0.117 and 0.114 g g$^{-1}$ of consumed lactose, respectively. *L. casei* subsp. *casei* PTCC1608 showed...
and L. delbrueckii subsp. delbrueckii PTCC1333 showed lower biomass production yield, relatively 11.8 and 22.7% less than L. delbrueckii subsp. bulgaricus PTCC1737, respectively. Fig. 1 represents that lactic acid production rate in exponential growth phase was higher than the stationary phase. Biomass productivity of L. casei subsp. casei PTCC1608 was calculated 30% less than L. delbrueckii subsp. bulgaricus PTCC1737. Maximum lactic acid concentration was 9% less than L. delbrueckii subsp. bulgaricus PTCC1737. For this strain, maximum lactic acid yield and productivity was in order of 2.65 and 8.7% less than L. delbrueckii subsp. bulgaricus PTCC1737. Biomass productivity of L. delbrueckii subsp. lactis PTCC1743 was 52.35% less than L. delbrueckii subsp. bulgaricus PTCC1737. Maximum lactic acid concentration was approximate 45% less than L. delbrueckii subsp. bulgaricus PTCC1737. Maximum lactic acid yield and productivity was in order of 27.4 and 41.5% less than L. delbrueckii subsp. bulgaricus PTCC1737. Cock and Stouvenel\textsuperscript{21} found 35 g L\textsuperscript{-1} lactic acid productions by L. lactis sublactis. In the present work, maximum lactic acid concentration was obtained as 26.6 g L\textsuperscript{-1} by L. delbrueckii subsp. bulgaricus PTCC1737. Biomass productivity of L. delbrueckii subsp. delbrueckii PTCC1333 was 55.3% less than L. delbrueckii subsp. bulgaricus PTCC1737 and approximately near to L. delbrueckii subsp. lactis PTCC1743. Lactic acid production was observed at exponential and the stationary growth phases. Maximum lactic acid concentration was obtained after 52 h.
incubation (end of the stationary phase), half of *L. delbrueckii* subsp. *bulgaricus* PTCC1737. Maximum lactic acid yield and productivity was in order 41.7 and 60.6% less than *L. delbrueckii* subsp. *bulgaricus* PTCC1737. *L. fermentum* PTCC1744 had the longest exponential growth phase. Its biomass productivity was 60.6% less than *L. delbrueckii* subsp. *bulgaricus* PTCC1737. This strain was the same as previously mentioned strain, lactic acid production was observed at both exponential and the stationary growth phases. Maximum lactic acid concentration was about 60% less than *L. delbrueckii* subsp. *bulgaricus* PTCC1737. Maximum lactic acid yield and productivity was in order of 40.5 and 63.9% less than *L. delbrueckii* subsp. *bulgaricus* PTCC1737. Polak-Berecka et al., reported 23 g L\(^{-1}\) of dry cell weight after 18 h for *L. rhamnosus*, much more than our studied strains. This indicate that strain type and culture composition have considerable impact on biomass production. Reported data by Berry et al., on *L. rhamnosus* ATCC10863 growth characteristics and its lactic acid production in batch culture of a defined medium showed a yield of 0.84 g lactic acid g\(^{-1}\) of consumed substrate. Bustos et al., studied lactic acid production by *L. pentosus* ATCC8041 from vinegar trimming wastes. They reported a production yield of 0.77 (g lactic acid g\(^{-1}\) consumed substrate) that is relatively less than our obtained data. It was found that the quality of substrate and type of organism species are key parameters in product yield. The main reason might be due to existence of high mineral concentration in the whey. Kim et al., reported 13.7 g L\(^{-1}\) lactic acid concentrations in a 48 h fermentation using *L. lactis* ssp. lactis that is much lower than our obtained data using glucose as the main substrate.

Results showed that *L. delbrueckii* subsp. *bulgaricus* PTCC1737 and *L. casei* subsp. *casei* PTCC1608 had good acceptable consistency using Contois kinetic model. R-square, \(\mu_{\text{max}}\) and \(K_a\) for the first strain were in order of 0.95, 0.265 h\(^{-1}\) and 1.34 g L\(^{-1}\) and for the second one were 0.9552, 0.299 h\(^{-1}\) and 3.85 g L\(^{-1}\), respectively (Table 2). *L. delbrueckii* subsp. *delbrueckii* PTCC1333 also showed an acceptable fitting with Contois kinetic model. For this strain R-square, \(\mu_{\text{max}}\) and \(K_a\) were 0.9493, 0.311 h\(^{-1}\) and 13.11 g L\(^{-1}\), respectively. *L. fermentum* PTCC1744 was fitted to Contois model with a good R-square (0.9367) and the greatest amounts of specific cell growth rate (2.591 h\(^{-1}\)). But its Contois semi-saturated coefficient \(K_a\) was the greatest obtained value of 188.33 g L\(^{-1}\). Therefore, it is perceived that Contois kinetic model may not be desired to describe the cell growth and substrate consumption behavior of *L. fermentum* PTCC1744. Results indicated that the consistency of *L. delbrueckii* subsp. *lactic* PTCC 1743 with Contois kinetic model is the less than all other investigated strains. For this strain, R-square was determined to be as low as 0.873.

Vasudha and Hari studied the Gompertz and Logistic kinetic models for *L. plantarum* NCDC 414. They found that the viable cell counts increased from 4 \times 10^8 to 7 \times 10^10 CFU mL\(^{-1}\), lactic acid concentration increased by about 4.5 folds and 44% w/v of substrate consumption was occurred at an incubation period of 24 h. In this work, significant lactic acid production observed for the exponential and stationary phases. In addition, the cell dry weight increased by about 10–15 folds (depend on the strain) in 24 h. Alvarez et al., studied the kinetics of cell growth, lactic acid production and substrate utilization of *L. casei* var. *rhamnosus*. They reported a strong exponentially dependent product inhibition at low lactic acid concentrations. Their results indicated that lactic acid production rate was partially associated with biomass growth as this work demonstrated.

Based on the calculated kinetic parameters (Table 2), *L. delbrueckii* subsp. *bulgaricus* PTCC1737 and *L. casei* subsp. *casei* PTCC1608 had good acceptable consistency with Contois kinetic model too. R-square and \(\mu_{\text{max}}\) for the first strain were in order 0.9156 and 0.0824 h\(^{-1}\) and for the second strain were 0.8401 and 0.0757 h\(^{-1}\), respectively (Table 2).

It was found that other studied strains did not have an acceptable consistency with Exponential kinetic model. Thus, Exponential kinetic model is not a well desired model to describe the cell growth and substrate consumption behavior of these three strains. The obtained specific growth rate for *L. delbrueckii* subsp. *bulgaricus* PTCC1737 with Exponential kinetic was about 70% less than the obtained value with Contois kinetic model. Also, for *L. casei* subsp. *casei* PTCC1608, 75% decline was documented in this work.

### Conclusion

This is the first report on the cell growth and substrate utilization kinetic of five different strains of *Lactobacilli* with respect to Contois and Exponential kinetic models. *L. delbrueckii* subsp. *bulgaricus* PTCC1737 was introduced as the desired strain in fields of biomass and lactic acid production yield. *L. delbrueckii* subsp. *bulgaricus* PTCC1737 and *L. casei* subsp. *casei* PTCC1608 showed acceptable consistency with both Contois and Exponential kinetic models. We found, Contois is better than Exponential model to describe cell growth and lactose consumption behavior of *L. strains*.

### Conflicts of interest

The authors declare no conflicts of interest.

---

**Table 2 – A comparison of Contois and Exponential kinetic constants for five different species of Lactobacilli.**

| Strain                | R\(^2\) | \(\mu_{\text{max}}\) (h\(^{-1}\)) | \(K_a\) (g L\(^{-1}\)) |
|-----------------------|---------|---------------------------------|-------------------------|
| *L. delbrueckii* subsp. *bulgaricus* PTCC1737 | 0.9500  | 0.8401                          | 3.58                    |
| *L. casei* subsp. *casei* PTCC1608       | 0.9552  | 0.265                           | 1.34                    |
| *L. delbrueckii* subsp. *lactic* PTCC1743 | 0.8730  | 0.311                           | 12.72                   |
| *L. delbrueckii* subsp. *delbrueckii* PTCC1333 | 0.9493  | 0.333                           | 13.11                   |
| *L. fermentum* PTCC1744                   | 0.9367  | 2.591                           | 188.33                  |
Acknowledgments

The authors wish to thank the Offices of Vice Chancellors in Research at Islamic Azad University, Qaemshahr Branch for their support of valued experimental and analytical work conducted during the course of present research.

REFERENCES

1. Vazquez JA, Murado MA. Unstructured mathematical model for biomass, lactic acid and bacteriocin production by lactic acid bacteria in batch fermentation. J Chem Tech Biotechnol. 2008;83:91–96.
2. Panchenika EFR, Maziero MT, Rodriguez-Leon JA, Parada JL,Spiere MR, Soccol CR. Molecular characterization and biomass metabolite production of Lactobacillus reuteri LPB P01-001: a potential probiotic. Braz J Microbiol. 2012;43:135–147.
3. Sule J, Korosi T, Hacker A, Variga L. Evaluation of culture media for selective enumeration of bifidobacteria and lactic acid bacteria. Braz J Microbiol. 2014;45:1023–1030.
4. Turchi S, Mancini S, Fratini F, et al. Preliminary evaluation of probiotic potential of Lactobacillus plantarum strains isolated from Italian food products. World J Microbiol Biotechnol. 2013;29:1913–1922.
5. Yu Z, Zhang X, Li S, Li C, Li D, Yang Z. Evaluation of probiotic properties of Lactobacillus plantarum strains isolated from Chinese sauerkraut. World J Microbiol Biotechnol. 2015;29:489–498.
6. Riaz S, Nawaz SK, Hasnain S. Bacteriocins produced by L. fermentum and L. acidophilus can inhibit cephalosporin resistant E. coli. Braz J Microbiol. 2010;41:645–648.
7. Scapin D, Grando WF, Rossi EM, Perez KJ, Malheiros PS, Tondo EC. Antagonistic activity of Lactobacillus acidophilus LA10 against Salmonella enterica serovar Enteritidis SE86 in mice. Braz J Microbiol. 2013;44:57–61.
8. Appukuttan S, Kadirvelu J. Optimization of nutritional and non-nutritional factors involved for production of antimicrobial compounds from Lactobacillus pentosus SJ65 using response surface methodology. Braz J Microbiol. 2014;45:81–88.
9. Bian L, Molan AL, Maddox L, Shu Q. Antimicrobial activity of Lactobacillus reuteri DPC16 supernatants against selected food borne pathogens. World J Microbiol Biotechnol. 2011;27:991–998.
10. Zhang M, Zhang H, Li Y, Qi W, Wang Z, Wang J. Inhibitory effect of Lactobacillus acidophilus on Helicobacter hepaticus in vitro. World J Microbiol Biotechnol. 2013;29:499–504.
11. Bendjeddou K, Fons M, Strocker P, Sadoun D. Characterization and purification of a bacteriocin from Lactobacillus paracasei subsp. paracasei BMK2005, an intestinal isolate active against multidrug-resistant pathogens. World J Microbiol Biotechnol. 2012;28:1543–1552.
12. Didar Z, Haddad Khodaparast MH. Effect of different lactic acid bacteria on phytic acid content and quality of whole wheat toast bread. J Food Biosci Technol. 2011;1:1–10.
13. Zhang T, Li L, Wang XF, Zeng ZH, Hu YG, Cui ZJ. Effects of Lactobacillus buchneri and Lactobacillus plantarum on fermentation, aerobic stability, bacteria diversity and ruminal degradability of alfalfa silage. World J Microbiol Biotechnol. 2009;25:965–971.
14. Ilori MO, Amund OO, Omidiji O. Short communication: purification and properties of a glucose-forming amylase of Lactobacillus brevis. World J Microbiol Biotechnol. 1995;11:595–596.
15. Akolkar SK, Sajgure A, Lele SS. Lactase production from Lactobacillus acidophilus. World J Microbiol Biotechnol. 2005;21:1119–1122.
16. Nancib A, Nancib N, Boudrant J. Production of lactic acid from date juice extract with free cells of single and mixed cultures of Lactobacillus casei and Lactococcus lactis. World J Microbiol Biotechnol. 2009;25:1423–1429.
17. Givry S, Prevot V, Duchiron F. Lactic acid production from hemi cellulose hydrolyzate by cells of Lactobacillus fermentans immobilized in Ca-alginate using response surface methodology. World J Microbiol Biotechnol. 2008;24:745–752.
18. Qian L. Submerged fermentation of Lactobacillus rhamnosus YS9 for γ-aminobutyric acid (GABA) production. Braz J Microbiol. 2013;44:183–187.
19. Ghaly AE, Tango MSA, Mahmoud NS, Avery AC. Batch propagation of Lactobacillus helveticus for production of lactic acid from lactose concentrated whey whey with microaeration and nutrient supplementation. World J Microbiol Biotechnol. 2004;20:65–75.
20. Vasudha Sh, Hari NM. Un-structured kinetic modeling of growth and lactic acid production by Lactobacillus plantarum NCDC 414 during fermentation of vegetable juices. IWT – Food Sci Technol. 2014;59:1123–1128.
21. Cock LS, de Stouvenel AR. Lactic acid production by a strain of Lactococcus lactis sublactis isolated from sugar cane plants. Elect J Biotechnol. 2006;9:41–45.
22. Amrane A. Analysis of the kinetics of growth and lactic acid production for Lactobacillus helveticus growing on supplemented whey permeate. J Chem Technol Biotechnol. 2005;80:345–352.
23. Polak-Berecka J, Marsico AR. Application of response surface methodology to enhancement of biomass production by Lactobacillus rhamnosus E/N. Braz J Microbiol. 2011;42:1485–1494.
24. Gupta S, Abu-Ghannam N, Scannell AGM. Growth and kinetics of Lactobacillus plantarum in the fermentation of edible Irish brown seaweeds. Food Bioprod Process. 2011;89:346–355.
25. Passos FV, Fleming HP, Hassan HM, Mc Feeters RF. Effect of malic acid on the growth kinetics of Lactobacillus plantarum. Appl Microbiol Biotechnol. 2005;63:207–211.
26. Alvarez MM, Aguillere-Ezkuriartza EJ, Ramirez-Medrano A, Rodriguez-Sanchez A. Kinetic analysis and mathematical modeling of growth and lactic acid production of Lactobacillus casei var. rhamnosus in milk whey. J Dairy Sci. 2010;98:5552–5560.
27. Koizumi K. Chapter 3: HPLC of carbohydrates on graphitized carbon columns. J Chrom. 2002;66:103–119.
28. Berry AR, Franco CMM, Zhang W, Middelberg APF. Growth and lactic acid production in batch culture of Lactobacillus rhamnosus in a defined medium. Biotechnol Lett. 1999;21:163–167.
29. Bustos G, Muleses AB, Cruz JM, Domínguez JM. Production of fermentable media from vine-trimming wastes and bioconversion into lactic acid by Lactobacillus pentosus. J Sci Food Agr. 2004;84:2105–2112.
30. Kim Woonjin S, Ren J, Dunn Noel W. Differentiation of Lactococcus lactis subspecies lactis and subspecies cremoris strains by their adaptive response to stresses. FEMS Microbiol Lett. 1995;171:57–65.