Deterministic strain-control of stability and current-induced motion of skyrmions in chiral magnets

Phuong-Vu Ong, Tae-Hoon Kim, Haijun Zhao, Brandt A. Jensen, Lin Zhou, and Liqin Ke

1 Ames Laboratory, U.S. Department of Energy, Ames, Iowa 50011, USA
2 School of Physics, Southeast University, Nanjing 211189, China

External magnetic field, temperature, and spin-polarized current are usually employed to create and control nanoscale vortex-like spin configurations such as magnetic skyrmions. Although these methods have proven successful, they are not energy-efficient due to high power consumption and dissipation. Coupling between magnetic properties and mechanical deformation, the magnetoelastic (MEL) effect, offers a novel approach to energy-efficient control of magnetism at the nanoscale. It is of great interest in the context of ever-decreasing length scales of electronic and spintronic devices. Therefore, it is desirable to establish a comprehensive framework capable of predicting effects of mechanical stress and enabling deterministic control of magnetic textures and skyrmions. In this work, using an advanced scheme of multiscale simulations and Lorentz transmission electron microscopy measurements we demonstrate deterministic control of topological magnetic textures and skyrmion creation in thin films and racetracks of chiral magnets. Our investigation considers not only uniaxial but also biaxial stress, which is ubiquitous in thin-film devices. The biaxial stress, rather than the uniaxial one, was shown to be more efficient to create or annihilate skyrmions when the MEL coefficient and strain have the same or opposite signs, respectively. It was also demonstrated to be a viable way to stabilize skyrmions and to control their current-induced motion in racetrack memory. Our results open prospects for deployment of mechanical stress to create novel topological spin textures, including merons, and in control and optimization of skyrmion-based devices.

I. INTRODUCTION

Nanoscale vortex-like spin configurations, i.e., magnetic skyrmions [1], are promising information carriers for future magnetic memories [2, 3]. Investigations on these real-space topological states are usually devoted to their creation or annihilation via external magnetic field, temperature [4–11], and spin-polarized current control [12]. Although these methods have proven successful, they require high power consumption with high power dissipation in the form of heat. Coupling between magnetic properties and mechanical deformation, or magnetoelastic (MEL) effect, promises energy-efficient control of magnetism at the nanoscale. Moreover, the integration of skyrmions into current semiconductor technology is highly likely to rely on thin-film heterostructures, in which large stresses are often presented due to the lattice mismatch between substrate and component layers. Therefore, it is necessary to understand the effects of MEL coupling and strain on magnetization dynamics, in general, and on skyrmions, in particular, and the mechanism which ensures their stability in strained systems.

Studies have shown that uniaxial stress can deform skyrmions from circular to elliptic shape in FeGe thin plates [13]. It can also fine-tune skyrmion crystals (SkXs) phase region in MnSi [14, 15] and Cu2OSeO3 crystals [16]. Different mechanisms have been proposed to explain the observed phenomena, including strained-induced magnetic anisotropy (MA) along the stress direction [15, 17] and strained-induced anisotropy of Dzyaloshinski-Moriya interaction (DMI) [13]. It is worth mentioning that even for the uniaxial stress, the concomitant strain is induced in all three orthogonal directions. As a result, an effective MEL field is induced not only in the direction along the stress axis, but also perpendicular to it. This is a unique feature of stress-induced MA, and it is important to consider the combined effect of the effective MEL fields in all directions. Moreover, these studies indicated that different types of stress, i.e., tensile or compressive, is required to stabilize skyrmions in different materials. Therefore, it is crucial to establish a principle that allows deterministic control of topological spin textures in materials with given physical properties. Lastly, biaxial stress, as opposed to the uniaxial one, is ubiquitous in modern electronic devices, which are based on stacking of multilayers. Therefore, a complete and practical understanding of the stress effect should include the biaxial stress.

Here, we propose a theoretical framework for study of the stress effects, which includes the second-order (in strain) MEL effect and enables a deterministic control of topological spin textures and their dynamics. Based on this framework, we report results of advanced multiscale simulations and Lorentz transmission electron microscopy observation on the effects of both uniaxial and biaxial stress on magnetization dynamics and skyrmions in thin films and racetracks of chiral magnets. MnSi and β-Mn-type Co-Zn-Mn were employed as two typical model materials. Our results elucidate the relationship between MEL properties, types of stress, and their effects. It was found that the biaxial stress, rather than the uniaxial one, is more efficient to stabilize skyrmions and to control their dynamics in thin films and racetracks.
where \( \ell \) which we are interested takes the form of the Landau-Lifchitz-Gilbert (LLG) equation for the inter/intracrystal magnetocrystalline interactions (DMI), the initial boundary value problem for the Landau-Lifchitz-Gilbert (LLG) equation which we are interested takes the form

\[
\begin{align*}
\frac{\partial \mathbf{m}}{\partial t} - \alpha \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t} &= -\mathbf{m} \times \mathbf{H}_{\text{eff}} \\
&\quad \text{in } \Omega \times (0, \infty), \\
2\ell_{\text{ex}}^2 \nabla \cdot \mathbf{m} &= -\ell_{\text{dm}} \mathbf{m} \times \mathbf{n} \quad \text{in } \Gamma \times (0, \infty), \\
\mathbf{m}(0) &= \mathbf{m}^0 \quad \text{in } \Omega,
\end{align*}
\]

where \( \ell_{\text{ex}} = \sqrt{2A/\mu_0 M_s^2} \) and \( \ell_{\text{dm}} = 2D/\mu_0 M_s^2 \) are exchange and DMI lengths, respectively, in which \( A \) and \( D \) are exchange interaction and DMI parameter, respectively; \( \alpha \) is the Gilbert damping parameter; \( \mu_0 \) is the vacuum magnetic permeability; \( \Gamma \) is the domain boundary and \( \mathbf{m}^0 \) is initial magnetization. Note that the LLG equation in (1) is in the dimensionless form. The effective field, \( \mathbf{H}_{\text{eff}} \), is determined by the first derivative of total energy functional, \( \mathcal{E}[\mathbf{M}] \), with respect to the magnetization vector \( \mathbf{M} \), more precisely

\[
\mathbf{H}_{\text{eff}} = -\frac{1}{\mu_0 M_s} \frac{\delta \mathcal{E}[\mathbf{M}]}{\delta \mathbf{M}} = \ell_{\text{ex}}^2 \Delta \mathbf{m} + \mathbf{H}_d + \mathbf{H}_{\text{ext}}
\]

\[
+ Q(e\mathbf{m} - \ell_{\text{dm}} \nabla \times \mathbf{m}) + \mathbf{H}_{\text{mel}}
\]

where \( \mathbf{H}_d \) and \( \mathbf{H}_{\text{ext}} \) are effective demagnetizing and external fields, respectively. The descriptions of these conventional terms can be found in Refs. [19, 20]; \( Q = 2K/\mu_0 M_s^2 \) is the MA coefficient, in which \( K \) is uniaxial MA energy. We focus on the new term, \( \mathbf{H}_{\text{mel}} \), which describes the MEL effect and can be determined from the MEL energy functional [21, 22]:

\[
U_{\text{mel}}[\mathbf{M}] = \int_{\Omega} \left( B_1 \sum_i m_i^2 e_{ii} + \frac{1}{2} B_2 \sum_{i \neq j} m_i m_j e_{ij} \right) \left( 1 + \frac{1}{2} D_{11} \sum_i m_i^2 e_{ii}^2 \right) \, dr
\]

where \( m_i, i = x, y, \) or \( z, \) are the Cartesian component of the normalized magnetization \( \mathbf{m} \), \( B_1 \) and \( B_2 \) are the first-order, and \( D_{11} \) is the second-order MEL coefficients, and \( e_{ij} \) is strain tensor. Mechanical deformation induced by lattice mismatch usually does not involve changes in crystallographic angles. Therefore, shear strain will not
be considered in the present work, i.e., \( e_{ij} \approx 0 \) for \( i \neq j \). With this in mind, we calculated the first functional derivative of the equation (3) with respect to \( \mathbf{M} \) and obtained the effective MEL field:

\[
\mathbf{H}_{\text{mel}}[\mathbf{M}] = -\frac{1}{\mu_0 M_s^2} \left[ (2B_1 + D_{11} e_{xx}) m_x e_{xx} \hat{x} + (2B_1 + D_{11} e_{yy}) m_y e_{yy} \hat{y} + (2B_1 + D_{11} e_{zz}) m_z e_{zz} \hat{z} \right]
\]

where \( \hat{x}, \hat{y}, \) and \( \hat{z} \) are the unit basis vectors of the Cartesian coordinate system.

For the FEA of MnSi skyrmion racetrack with the current-in-plane configuration, the Zhang-Li spin torque term [23] will be added to the effective field [23]:

\[
\mathbf{H}_{ZL}[\mathbf{M}] = [\mathbf{m} \times (\mathbf{u} \nabla)] + \xi (\mathbf{u} \nabla) \mathbf{m}
\]

\[
\mathbf{u} = \frac{1}{1 + e^2 |e| \mu_0 |\mathbf{M}|^2} \mathbf{m}
\]

where \( e, g_e, \) and \( \gamma \) are electron charge, \( g \)-factor, and gyromagnetic ratio, respectively, \( \mu_B \) is Bohr magneton. Nonadiabatic spin torque parameter, \( \xi \), is typically an order of magnitude larger than the damping parameter \( \alpha \) [24].

B. Uniaxial and biaxial strain in isotropic materials

For an isotropic materials, we have the following relations between stress tensor \( (e_{ij}) \) and strain tensor \( (\sigma_{ij}) \) [25],

\[
e_{xx} = \frac{1}{E} [\sigma_{xx} - \nu(\sigma_{yy} + \sigma_{zz})]
\]

\[
e_{yy} = \frac{1}{E} [\sigma_{yy} - \nu(\sigma_{zz} + \sigma_{xx})]
\]

\[
e_{zz} = \frac{1}{E} [\sigma_{zz} - \nu(\sigma_{xx} + \sigma_{yy})]
\]

where \( E \) is Young’s modulus, \( \nu \) is Poisson’s ratio, \( \sigma_{xx}, \sigma_{yy}, \sigma_{zz} \) are stress along, \( x, y, \) and \( z \) directions.

In the case of uniaxial stress, \( \sigma_{xx} = \sigma \) and all other stress components vanish. From (7)-(9), we have

\[
e_{xx} = \frac{\sigma}{E}
\]

\[
e_{yy} = -\nu e_{xx}
\]

\[
e_{zz} = -\nu e_{xx}
\]

In the case of biaxial stress, \( \sigma_{xx} = \sigma_{yy} = \sigma \) and \( \sigma_{zz} = 0 \), we have,

\[
e_{xx} = (1 - \nu) \frac{\sigma}{E}
\]

\[
e_{yy} = e_{xx}
\]

\[
e_{zz} = -\frac{2\nu}{1 - \nu} e_{xx}
\]

For metals, typical value of Poisson’s ratio is \( \nu \approx 1/3 \) [26]. Therefore, from (13)-(15) we have \( e_{xx} = e_{yy} \approx -e_{zz} \) for the biaxial stress.

For materials with nonlinear MEL property such as MnSi, we performed finite element analysis (FEA) of the problem (1) using the Commins (COMputational MicroMagnetICS) code [27], modified to include the MEL field [23]. We are not aware of any micromagnetic codes, which are capable of calculating the nonlinear MEL effects. The FEA was performed using the (almost) second-order tangent plane scheme. Within this scheme, numerical solution of the LLG has been proved to converge toward the weak solution within an error of (almost) second-order in time-step size [29] [28]. The FEA implementation is based on the multiphysics finite element software Netgen/NGSolve [29].

For MnSi thin films and racetracks, the FEA was performed using Delaunay tetrahedralization with maximal global mesh-size of 6.0 nm was employed. Time-step size was set to 0.1 ps. Thickness of the thin films and racetracks was fixed at 18.0 nm. Damping parameter was \( \alpha = 0.02 \). Material physical parameters are obtained from the experiments for a 17.6-nm thick MnSi thin film [30]. In particular, exchange stiffness \( A = 0.76 \times 10^{-12} \) J/m; bulk DMI coefficient \( D_{11} = 0.34 \times 10^{-3} \) J/m²; saturation magnetization \( M_s = 0.16 \times 10^6 \) A/m; uniaxial MA \( K = 0.9 \times 10^5 \) J/m²; the first order and second order MEL coefficients were \( B_1 = 1.0 \times 10^8 \) J/m⁴ and \( D_{11} = -7.8 \times 10^7 \) J/m³, respectively. It was found that most of these parameters are independent of or weakly dependent on thickness, except to uniaxial MA [30].

For simulations of MnSi racetrack with an applied in-plane spin-polarized current, we set \( \xi = 0.2 \). Degree of spin-polarization \( P \) was set to the experimental value of 0.1 [31]. Electron current density \( j_e = 5.0 \times 10^{10} \) A/m² was employed. We note that \( j_e \) denotes direction of electron motion, which is opposite to motion of positive charge.

On the other hand, the alloy Co₈Zn₄₅Mn₃₅ is a linear MEL material (as shown below). Moreover, it hosts skyrmions with relatively large radii and thus requires a large simulation area (~ \( 2.5 \times 10^3 \) µm). Therefore, micromagnetic simulations were carried out using the finite-difference code mumax [32]. The simulations were performed on a sample of area \( 2.5 \times 2.5 \) µm² and thickness 190 nm with discretization cell size of \( 5 \times 5 \times 190 \) nm³. External magnetic field was \( B_{ext} = 0.15 \) T and damping parameter was \( \alpha = 0.02 \). Cubic MA constant was set to \( K = 0.5 \times 10^4 \) J/m³. DMI coefficient was set to \( D_{11} = 0.7 \times 10^{-3} \) J/m², which is greater than the experimental value for the Co₈Zn₄₅Mn₃⁵ bulk (0.53 \times 10^{-3} J/m²) [33], but found to give the simulated period of the helical stripes in agreement with our experimental value for the Co₈Zn₄₅Mn₃ thin plate. For other material physical parameters, we adopted the experimental values for Co₈Zn₄₅Mn₄ alloy. In particular, exchange stiffness \( A = 9.2 \times 10^{-12} \) J/m [33] and saturation magnetization \( M_s = 0.35 \times 10^6 \) A/m² [34].
C. Density functional theory (DFT) calculation of the MEL coefficient

To calculate the MEL coefficients and Poisson’s ratio $\nu$ of the Co-Zn-Mn alloy, we performed DFT calculations based on the projector augmented-wave formalism for electron-ion potential[34], as implemented in the Vienna Ab initio Simulation Package[35]. Exchange-correlation interaction was treated within the Perdew-Burke-Ernzerhof functional form of the generalized gradient approximation (GGA)[36]. The binary parent alloy Co$_{10}$Zn$_{10}$ has a simple cubic structure (space group number 213), in which the 8c sites are mainly occupied by Co atoms and the 12d sites are mainly occupied by Zn and also randomly occupied by the remaining Co atoms (Fig. 1a) [38]. In a derived alloy Co$_x$Zn$_{y}$Mn$_z$ alloys ($x + y + z = 20$), Mn atoms mainly occupy the 12d sites, but also share the 8c sites with Co atoms[39, 40]. To avoid complications due to the randomness of site occupancies in the Co$_x$Zn$_y$Mn$_z$ alloys, we employed a simplified model based on the binary alloy Co$_{10}$Zn$_{10}$. The model has 10 Co atoms (8 at the 8c sites and 2 at two arbitrary 12d sites) and 10 Zn atoms at the 12d sites.

Uniaxial stress was applied along the x axis. At each strain $e_{xx} = \varepsilon_u$, geometry optimization, magnetic, and atomic relaxation were performed until the change in the total energy between two ionic relaxation steps is smaller than 10$^{-6}$ eV. Then, the corresponding strain $e_{yy}$ and $e_{zz}$ along the y and z directions, respectively, can be determined as a function of $e_{xx}$ (Fig. 1b, right ordinate). The MA was calculated as the total-energy difference between the two magnetic states in which the magnetization is aligned along the [100] or [100] directions, respectively. The obtained data is shown in Fig. 1b (left ordinate).

In the phenomenological theory, MA can be determined by the following expression:

$$MA = f_M(e_{ij}, m_z = 1) - f_M(e_{ij}, m_z = 1)$$

where the magnetic energy density functional $f_M$ is expressed by:

$$f_M(e_{ij}, m_i) = K(1 - m_i^2) + B_1 \sum_{i = x, y, z} e_{ii} m_i^2 + B_2 \sum_{i \neq j} e_{ij} m_i m_j$$

(17)

Since shear strain will not be considered, i.e., $e_{ij} = 0$ for $i \neq j$. Substituting (17) into (18) we obtain:

$$MA = -K + B_1 (e_{xx} - e_{zz})$$

(18)

For uniaxial stress, $e_{zz} = -\nu e_{xx}$. Therefore, with putting $e_{xx} = \varepsilon_u$ we obtain

$$MA = -K + B_1 (1 + \nu) \varepsilon_u$$

(19)
FIG. 3. Finite element analysis of the MnSi thin film under in-plane uniaxial and biaxial stress. Sample area is 500×500 nm² and thickness is 18 nm. External magnetic field is 0.2 mT along the film normal. (a, b, c) Equilibrium magnetization in the xy-plane viewed from the top under the uniaxial stress with ε_u = 0, -2.0, and 2.0% after the simulation duration of 15 ns, 5 ns, and 10 ns, respectively. The uniaxial stress axis (u) is along the x axis, as indicated by the double headed arrow in (c). (d) The propagation vector q of the helical phase is rendered perpendicular to the stress axis when the magnetoelastic coefficient B_1 and strain have opposite signs (B_1 ε_u < 0). (e) Magnetic texture featured by magnetization in the xy-plane in most of the perimeter region of the vortices, while still pointing downward in the core regions under the biaxial compressive stress (ε_b = -2%) after 10.0 ns. (f) Skyrmion crystal under the biaxial tensile stress (ε_b = 2.0%) after 35.3 ns.

G2-F20 operating at 200 kV of accelerating voltage. A Hysitron PI 95 TEM PicoIndenter enables quantitative uniaxial tensile testing in the LTEM experiments. Real-time applied force and displacement were measured. By subtracting the PTP device portion from the measured force, actual force applied to the specimen was calculated. As a result, a linear stress-strain relation with Young’s modulus of 85.52 GPa was obtained. An external magnetic field was applied along the electron beam direction by partially exciting the objective lens. The in-plane magnetization maps of magnetic structures were obtained by the LTEM Fresnel images with a phase-retrieval QPt software on the basis of the transport of intensity equation.[41].

III. RESULTS AND DISCUSSION

A. The uniaxial and biaxial stress effects on a nonlinear MEL chiral magnet

Due to the lack of space-inversion symmetry, DMI is induced in MnSi and makes it a material of choice for study of topological spin textures[4]. In a thin film form, MnSi exhibits nonlinear MEL behavior with the first- and second MEL coefficients of B_1 = 1.0 × 10^6 J/m³ and D_{11} = –7.8 × 10^7 J/m³, respectively[20].

Fig. 3 shows the FEA results for a 18-nm-thick MnSi thin film under an external magnetic field of 0.2 T. In the strain free condition, the system shows short stripes and skyrmions of various shapes with an average diameter of about 58 nm (Fig. 3a).

For a uniaxial stress along the x axis, the relationships between strains along the x, y, and z axes are ε_{xx} = ε_u and ε_{yy} = ε_{zz} = –νε_u, as inferred from equations (10)-(12). Under the uniaxial compressive stress (ε_u = –2.0%), these skyrmions elongate and merge to form a helical phase with the spin-spiral propagation (or q-) vector perpendicular to the stress direction (Fig. 3b). In contrast, the uniaxial tensile stress does not induce a helical phase, but only the elongation and alignment perpendicular to the stress axis (Fig. 3c).

Underlying mechanism of the stress-induced formation of the helical phase can be explained on the basis of strain-induced MA. For a uniaxial stress along the x axis, the effective MEL field [4] is equivalent to the following
field up to addition by a field parallel to \( \mathbf{m} \)

\[
H_{\text{mel}}^u[\mathbf{M}] = -\frac{1}{\mu_0 M_s^2} \left[ 2(1+\nu)B_1 \varepsilon_u + (1-\nu^2)D_{11}\varepsilon_z^2 \right] m_x \hat{x}
\]

(20)

This effective MEL field has the same nature as a MA field along the \( x \) axis. We note that the field (20) can be made parallel to the stress direction (\( x \)) only by combination of the effective MEL fields induced not only in the direction along the stress axis, but also perpendicular to it. Under the compressive stress, due to \( B_1 \varepsilon_u < 0 \) and \( D_{11} < 0 \) the field (20) is parallel to \( \hat{x} \) and thus induces an increase in the magnetization component \( |m_x| \). As a result, the skyrmions and short stripes are elongated along the stress direction. These elongated skyrmions and stripes combine to form longer ones and eventually helices (Fig. 3b). Due to the finite size along the thin film normal a helical phase with \( q \)-vector oriented along the \( z \) axis is prohibited. The reason is that it will result in a lamellar structure of ferromagnetic layers parallel to the \( xy \)-plane, which is a relatively unstable configuration. As a result, the \( q \)-vector can be oriented only along the \( y \) axis (Fig. 4).

We found that including the second order term (due to the finite \( D_{11} \)) is necessary for the formation of purely helical phase, which otherwise contains discontinuous helices and an isolated skyrmion (Fig. 4). This second order effect can be understood in term of the additional field \( \left( -\frac{(1-\nu^2)D_{11}\varepsilon_z^2}{\mu_0 M_s^2} \right) m_x \hat{x} \) in (20), which, for \( D_{11} < 0 \), is parallel to \( \hat{x} \) and thus enhances the in-plane MA. Therefore, it further promotes the elongation and merging of skyrmions and hence the formation of helices.

On the other hand, for tensile stress (\( B_1 \varepsilon_u > 0 \)) the field (20) points opposite to \( \hat{x} \). Therefore, it drives magnetization equally likely in the \( y \) and \( z \) directions. Due to the above mentioned asymmetry between the \( y \) and \( z \) axes, skyrmion elongation occurs along the \( y \) axis. In this case, a helical phase could, however, not be formed (Fig. 3). The reason is that the field (20) now induces an enhancement in the perpendicular MA (PMA), which tends to stabilize magnetization along the \( z \) direction. This is shown by the noticeable increase in the \( m_z \) components, as indicated by the enhanced color contrast in Fig. 3b, compared with that in Fig. 3a. Therefore, the enhanced PMA limits the elongation and suppresses the merging, and thus stabilizes the (elongated) skyrmions.

For thin films, it is often more relevant to consider biaxial stress, which is caused by the lattice mismatch between a thin film and the underlying substrate or between the component layers in a heterostructure. Under the biaxial stress, the \( x \) and \( y \) directions are equivalent and, therefore, skyrmion elongation effect will not occur. The effective MEL field (4) is now equivalent to

\[
H_{\text{mel}}^b[\mathbf{M}] = \frac{1}{\mu_0 M_s^2} \left[ 2\left( \frac{1+\nu}{1-\nu} \right) B_1 \varepsilon_b + \frac{(1+\nu)(1-3\nu)}{(1-\nu)^2} D_{11}\varepsilon_z^2 \right] m_x \hat{z}
\]

(21)

where \( \varepsilon_b \) is strain along the \( x \) and \( y \) directions (see equations (13)-(15)). Given that for most metals the Poisson’s ratio \( \nu \) is about \( \approx 1/3 \), the equation (21) implies that the second order term is negligibly small, owing to the factor \( (1-3\nu) \) and also the second order in strain \( (\varepsilon_z^2) \). For the compressive stress (\( B_1 \varepsilon_b < 0 \)), this field reduces PMA of the MnSi film. As a result, magnetization is driven to the \( xy \) plane in most of the perimeter regions of the vortices, while still pointing downward in the core regions (Fig. 3d). This magnetic configuration resembles that of merons, which are vortex-like spin textures with winding number \( n = -1/2 \) [42], except that there are still finite out-of-plane magnetization components in some finite parts of the perimeters. Nevertheless, the result gives rise to a possibility of creating merons and their crystal with a biaxial stress if magnetic field and temperature can be fine-tuned into a proper condition.

Under the biaxial tensile stress (\( B_1 \varepsilon_b > 0 \)), PMA is enhanced, leading to a transformation of the short stripes into skyrmions and a reduction of skyrmion diameter. After a simulation time of 10.0 ns, the system was found to become all skyrmions with a diameter of about 50 nm. These skyrmions were found to keep moving and reorganizing themselves in a relatively slow process. Fig. 3 shows the skyrmion system after 35.3 ns. It is expected that a hexagonal SkX will form after a sufficiently long simulation time.

As discussed above, the out-of-plane (along the \( z \) axis) MEL field plays a key role in stabilization, creation, or annihilation of skyrmions. Comparing the first order terms in the equations (20) and (21) for the uniaxial
FIG. 5. Finite difference simulations of the Co$_x$Zn$_{x+\delta}$Mn$_{3.5}$ thin plate under in-plane uniaxial stress. Sample area and thickness are 2.5×2.5 $\mu$m$^2$ and 190 nm, respectively. Simulation duration is 100ns. (a, b) Helical and SkX phases in the $xy$-plane viewed from the top in the zero strain condition under the external magnetic field $B_{ext} = 0$ and 0.15 T, respectively, along the $z$ direction. (c) Elongation and alignment of skyrmions at strain $\varepsilon_u = 0.53\%$ under the field $B_{ext} = 0.15$ T. The uniaxial stress axis ($u$) is along the $x$ axis, as indicated by the double headed arrow. Solid lines indicate lattice distortion due to edge dislocations (dashed lines) or skyrmion vacancy (dotted circle). (d) Total winding number of the system as a function of strain $\varepsilon_u$ and magnetic field.

and biaxial stress, respectively, reveals a difference by a factor of $\left(\frac{1}{1-\nu}\right)$. Most of materials have $\nu$ ranging between 0.0 and 0.5. For the typical case of $\nu = 1/3$, this translates into a strain-induced PMA either larger or smaller by 50% for the biaxial stress, compared with that induced by the corresponding uniaxial one. Based on the above discussed results, we proposed the following criteria for efficient creation and control of skyrmions with mechanical stress: i) the applied stress should be biaxial; ii) the MEL coefficient $B_1$ and strain have to be in the same sign. Moreover, due to the factor $\left(\frac{1}{1-\nu}\right)$ the relative efficiency of the biaxial stress depends on the Poisson’s ratio $\nu$. A higher $\nu$ value leads to a higher efficiency of the mechanical control with biaxial stress, as opposed to the uniaxial one.

B. The magnetoelastic sign effect on skyrmion elongation and helical phase formation

As can be inferred from the effective MEL fields (20) and (21), the strain $\varepsilon_u$ always appears in the forms of products $B_1\varepsilon_u$ and $D_{11}\varepsilon_u$. From the above mentioned mechanism of stress effect, it is clear that formation and orientation of the elongated skyrmions and helical phase relative to the stress direction depend on sign of the MEL coefficient $B_1$. Therefore, they can vary from one material to another.

To further demonstrate the deterministic control of magnetic texture, we apply our micromagnetic framework to a $\beta$-Mn-type Co$_x$Zn$_{y}$Mn$_{z}$ alloy with $x + y + z = 20$. This class of chiral magnets can host skyrmions beyond room temperature [7]. As shown above, our DFT calculations predict that the $\beta$-Mn-type Co-Zn-Mn alloy has linear MEL behavior with the negative MEL coeffi-
FIG. 6. Phase diagram and magnetic textures in the 190 nm (100) Co₈Zn₅.5Mn₃ thin plate and effect of uniaxial stress along a [110] direction. (a) A contour plot of skyrmion density at room temperature under the strain free condition as deduced from LTEM observation. Color scale indicates skyrmion phase fraction (in %) of the observed area. (b,c) Underfocused LTEM image of helical spin texture and the corresponding fast Fourier transform (FFT), respectively, in a strain free sample under zero field. (d,e) Skyrmion crystal and its FFT, respectively, in a strain free sample under 70 mT. (f) Skyrmions elongated and aligned along the uniaxial stress direction [110] under 70 mT and strain εᵤ = 0.53%. (g) The corresponding FFT of (f) exhibits an elliptic shape with major-axis perpendicular to the stress direction.

cient B₁, i.e., opposite to that for MnSi, and thus makes it an ideal choice for a further test of the framework.

To obtain the magnetic texture in the zero magnetic field and strain free condition, we carried out simulation at high temperature and then slowly decreased it to zero, i.e., employed simulated annealing simulation to accelerate the convergence process toward the ground state. The magnetic texture exhibits discontinuous helical stripes with different orientations and an average stripe period of about 156 nm (Fig. 5a).

Under the external magnetic field Bₑₓt = 0.15 T along the thin plate normal, polydomain SkX is formed with an average skyrmion diameter of about 150 nm (Fig. 5b). A uniaxial tensile stress with εᵤ = 0.53% is then applied along the x direction. The stress effect is twofold: first, it induces elongation of skyrmions; and second, it renders skyrmions aligned along the stress directions, and thus induces a polydomain-to-monodomain phase transition (Fig. 5c). The monodomain SkX has edge dislocations (dashed lines) and a skyrmion vacancy (dotted circle). It is worth mentioning that the local distortion induced by the vacancy is especially strong for the SkX, in sharp contrast to that for a solid crystal.

A topological magnetic texture is characterized by a winding number or topological charge defined as

\[ n = \frac{1}{4\pi} \int \mathbf{m} \cdot (\partial_x \mathbf{m} \times \partial_y \mathbf{m}) dx dy \]  

which is a negative integer for the Co-Zn-Mn thin plate under the external magnetic field parallel to the z axis. Fig. 5d shows absolute value of total winding number |N| of the system as a function of strain and magnetic field below 0.3 T. Three variation regimes of |N| can be identified: first, it is slowly decreased or unaltered with increasing strain; then at a certain strain value depending on the applied field, it is rapidly reduced; after that, it slowly decreases toward zero. In the first regime, the main processes are elongation and alignment of skyrmions and short stripes, which do not involve change in topology of the magnetic texture. In the second regime, merging of elongated skyrmions and short helical stripes becomes active. Moreover, in this regime strain is also sufficiently large to align magnetization along the stress direction in most of the thin plate area, leading to local transitions to ferromagnetic (FM) states, which are topologically trivial. These effects together cause the rapid decrease in |N|. For strong magnetic fields on the verge of a FM transition (∼0.30 T), the stress-induced elongation and merging of skyrmions are suppressed for strain below a critical value. Above the critical strain, the system changes di-
rectly from a skyrmion phase to a FM phase. Therefore, for the magnetic field of 0.3 T the total winding number |N| falls sharply at the strain value \( \varepsilon_u = 1.38\% \).

For the Co-Zn-Mn thin plate, the elongation and alignment of skyrmions (Fig. 5a) is at 90 degree with respect to those for the MnSi thin film under the same type of strain (tensile, Fig. 3a). This is due to the opposite signs of the first order MEL coefficients for the two materials. Based on the results for both of the systems, the following rule can be drawn: for a thin plate or thin film under uniaxial stress, if the product \( B_1 \varepsilon_u \) is negative, skyrmion elongation and alignment will be parallel to the stress direction. Moreover, the stress diminishes PMA of the elongation will be limited due to the stress-induced enhancement of PMA.

**C. Experimental confirmation**

Based on LTEM observation at room temperature, a phase diagram was established for the observed rectangular area under increasing external magnetic field, \( B_{ext} \). Transitions from helical to skyrmion phase and from skyrmion to FM phase occurs at \( B_{ext} \sim 20 \) and 130 mT, respectively (Fig. 3h). Fig. 3b shows helical texture in the zero field condition. These helical stripes have different orientations and average period of about 160 nm, resembling the simulation result for the zero field and zero strain condition (Fig. 5d). Under \( B_{ext} = 70 \) mT, a SkX can be observed with average skyrmion diameter about 140 nm (Fig. 5h), compared to the simulation result of 150 nm.

Elliptic skyrmions aligned along the stress direction can be observed at strain \( \varepsilon_u = 0.53\% \) (Fig. 3f). The corresponding fast Fourier transform of the LTEM image has an elliptic shape with the major axis perpendicular to the stress direction (Fig. 5g), confirming the skyrmions are elongated along the stress direction. This agreement between the experimental and simulation results also confirms the DFT prediction of the negative MEL coefficient \( B_1 \) for this alloy.

**D. Stress control of skyrmion motion on MnSi racetrack**

To demonstrate a practical application of our findings, we consider a 900-nm long, 60-nm wide, and 18-nm thick MnSi racetrack under a perpendicular magnetic field of 0.15 T. An in-plane electron-current density \( j_e = 5.0 \times 10^{11} \text{ A/m}^2 \) is passed through the track along the long (x) axis. The current is found to induce elongation of a skyrmion. The skyrmion can grow into a long stripe of up to 260 nm in 10.0 ns (Fig. 7b-f). Shorter stripes are also induced around the middle of the racetrack (Fig. 7c and d). As a result, the current-induced motion of skyrmions is suppressed. As the stability of skyrmions and their steady flow are essential prerequisites for operation of skyrmion racetrack devices, such skyrmion elongation and magnetic stripes would have a detrimental effect on the devices.

Under the biaxial compressive stress (\( \varepsilon_b = -2\% \)),
these stripes are transformed into skyrmions (indicated by 2 and 3 in Fig. 7a-j). As a result, the skyrmions are unblocked and start to flow following the electron current. The skyrmions 1 and 2 are in free motion during time between \( t = 13.0 \) to 14.5 ns (Fig. 7a and j) and \( t = 12.0 \) to 13.0 ns (Fig. 7i and i), respectively. We note that their motion also has finite transverse components (indicated by the double headed arrows for the skyrmion 1 in Fig. 7a-j). This is the observed skyrmion Hall effect caused by the magnetic Magnus force, which is induced by the skyrmion topological charge and is perpendicular to the current and the magnetic field directions.\(^{[13]}\)\(^{[44]}\) The transverse motion is limited due to the narrow width and reflection at the racetrack boundary. Average horizontal velocity is estimated to be 80.0 m/s, which is comparable to the experimental and predicted values for Pt/CoFeB/MgO and Pt/Co thin films, respectively.\(^{[45]}\)\(^{[46]}\)

Stability of skyrmions is a major challenge for their applications at room-temperature. Our results demonstrate that the biaxial stress can be employed to efficiently create, stabilize, and control skyrmions. This can be achieved, for example, by growth of the racetrack on a piezoelectric substrate, which will facilitate an energy-efficient control of strain via an applied voltage or electric field. This strain-mediated approach has already been proved to assist magnetization switching in magnetoelectric memories.\(^{[17]}\)\(^{[49]}\) Such a device structure can be employed to control and enhance stability of skyrmion-based racetrack memories and sensors. Another advantage of such a multiiferroic heterostructure is that skyrmions can also be controlled by manipulating the ferroelectric polarization of the substrate.

To summarize, we have demonstrated theoretically and experimentally the mechanical control of topological magnetic textures and their dynamics in thin films and thin plates of chiral magnets. Based on the magnetoelectric coupling, our theoretical framework elucidates the relationship between magnetoelectric properties of materials, types of stress (tensile or compressive), and their effects, and thus enables a deterministic control of the topological spin textures. It was found that the biaxial stress, rather than the uniaxial one, is more efficient to annihilate, create, and stabilize skyrmions. Moreover, creation or annihilation occurs when the magnetoelastic coefficient and strain have the same or opposite signs, respectively. Stress can induce a rich variety of topological spin textures, possibly including merons. Biaxial stress was also demonstrated to be a viable way to stabilize skyrmions and to control their current-induced motion in racetrack memory. We hope our findings stimulate further research and open prospects for deployment of mechanical stress in control and optimization of skyrmion-based devices.

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