Destruction of Long-period Comets

David Jewitt
Department of Earth, Planetary and Space Sciences, UCLA, Los Angeles, CA 90025-1567, USA; jewitt@ucla.edu
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Abstract
We identify a sample of 27 long-period comets for which both nongravitational accelerations and Ly\textalpha\,-based gas production rates are available. Seven of the 27 comets (i.e., \(\sim 25\%\)) did not survive perihelion because of nucleus fragmentation or complete disintegration. Empirically, the latter nuclei have the smallest gas production rates and the largest nongravitational accelerations, which are both indicators of small size. Specifically, the disintegrating nuclei have a median radius of only 0.41 km, one-quarter of the 1.60 km median radius of those surviving perihelion. The disintegrating comets also have a smaller median perihelion distance (0.48 au) than do the survivors (0.99 au). We compare the order-of-magnitude timescale for outgassing torques to change the nucleus spin, \(\tau_s\), with the time spent by each comet in strong sublimation, \(\Delta t\), finding that the disrupted comets are those with \(\tau_s < \Delta t\). The destruction of near-Sun long-period comets is thus naturally explained as a consequence of rotational breakup. We discuss this process as a contributor to Oort’s long mysterious “fading parameter.”

Unified Astronomy Thesaurus concepts: Comet nuclei (2160); Long period comets (933); Oort cloud (1157)

1. Introduction
Comets are volatile-rich products of accretion in the Sun’s protoplanetary disk. Historically, comets were classified as either short-period or long-period, depending on whether their orbital periods were less or greater than 200 yr. With some complications and subtleties, this division into two dynamical groups has survived to the present day. Most short-period (strictly “Jupiter-family”) comets arrive from the Kuiper Belt, where they have been stored for the past 4.5 Gyr at temperatures \(\sim 40\) K. Long-period comets (LPCs) arrive from equally long-term residence in the Oort Cloud, where the equilibrium temperature is \(\lesssim 10\) K. Both short-period comets and LPCs are thought to have formed in the giant planet region of the solar system and were scattered to their respective storage reservoirs in the final stages of the growth of the planets.

Oort (1950) first examined the distribution of orbital binding energies of LPCs and found that no purely dynamical model could fit the large observed ratio of first-arrival (“dynamically new”) comets to returning comets. He invoked an ad hoc “fading parameter” by which to decrease the brightness of returning comets and thereby depress their number in magnitude-limited surveys. Subsequent work with a much larger comet sample verified both the dynamics and the need for a fading parameter (Wiegert & Tremaine 1999; Levison et al. 2002) but did not identify its physical origin. Observationally, Bortle (1991) reported that intrinsically faint LPCs with small perihelia are less likely to survive perihelion than their brighter counterparts but, again, did not identify the mechanism.

Several practical difficulties are inherent in the observational study of LPCs. Crucially, these objects are generally discovered only a short time before perihelion, and they are soon thereafter lost as they recede from the Sun and fade to permanent invisibility. The observational window for LPCs is consequently short, unlike that of the short-period comets, which can be predictably observed over many orbits. Even worse, LPCs with perihelia \(< 1\) au must be observed at small solar elongation (Sun–Earth–comet) angles, where ground-based telescopes struggle against low elevation and high sky brightness constraints. As a result of these practical difficulties, the nuclei of LPCs are poorly characterized relative to those of short-period comets. Cometary disintegrations, being intrinsically unpredictable and rapidly evolving, are even more difficult to study and rarely reach publication in the refereed literature.

2. The Comet Sample
We are interested in LPCs for which there exist reliable measurements of both the total outgassing rates and the nongravitational accelerations. For this reason, we focus on LPCs discovered since the year 2000, to coincide with the period in which high-quality physical and dynamical measurements have become routinely available from long-term surveys. Specifically, we rely on systematic measurements of the water production rate obtained from \(\text{Ly}\alpha\) observations with the space-borne SWAN ultraviolet spectrometer aboard the Solar and Heliospheric Observatory (SOHO; Bertaux et al. 1997), as well as on all-sky optical surveys (e.g., the Catalina and, recently, Pan-STARRS surveys), which provide precise astrometry over a long timebase. We further restricted the sample to comets with perihelion distances \(q \leq 2\) au.

2.1. Nongravitational Accelerations
We used orbit solutions from JPL’s Horizons\(^1\) website to compile a list of LPCs showing evidence for nongravitational acceleration. The orbital properties of the 27 comets used for this study are listed in Table 1, where we show the estimated original barycentric orbital elements in order to avoid the effects of planetary perturbations. (To find the latter, we used Horizons to compute the osculating orbital elements on 1900 January 1, a time at which all of the comets in the present study were far beyond the planetary region and therefore subject to minimal planetary perturbation). Twelve of the 27 comets are

\(^1\) http://ssd.jpl.nasa.gov/horizons.cgi
Notes.

- Barycentric semimajor axis, in au.
- Eccentricity.
- Inclination, in degrees.
- Perihelion distance, in au.
- Mean Julian Date of perihelion.

\( \alpha_{\text{NG}} = g(r_{\text{HI}})(A_1^2 + A_2^2 + A_3^2)^{1/2}. \) (1)

Function \( g(r_{\text{HI}}) \) is defined by

\[ g(r_{\text{HI}}) = \alpha_M \left( \frac{r_{\text{HI}}}{r_0} \right)^m \left[ 1 + \left( \frac{r_{\text{HI}}}{r_0} \right)^n \right]^{-k}. \] (2)

where \( r_0 = 2.808 \text{ au}, \ m = 2.15, \ n = 5.093, \ k = 4.6142, \) and \( \alpha_M = 0.1113 \) are constants determined from a fit to a model of sublimation and the normalization is such that \( g(1) = 1 \) (Marsden et al. 1973). These constants derive from a model of a sublimating isothermal sphere. While this is logically incorrect (since an isothermal sphere would sublimate isotropically and hence experience no net recoil force), the difference from a physically more plausible hemispheric sublimator is minor, at least at distances \( r_{\text{HI}} \lesssim 3 \text{ au} \), where the bulk of the absorbed energy is used to break hydrogen bonds in water and the sublimation rate is large. The assumed nucleus temperature distribution over the nucleus surface matters more at larger distances, but the sublimation rate falls exponentially, and the resulting recoil force due to distant activity is comparatively small. Values of \( A_1, A_2, A_3, \) and \( \alpha_{\text{NG}} \) are listed for each comet in Table 2. The accelerations are small (the median value at 1 au is \( \alpha_{\text{NG}} = 4 \times 10^{-7} \text{ m s}^{-2} \), about 0.007% of the solar gravitational acceleration).

\[ 2.2. \text{Production Rates} \]

We searched the literature to find reliable measurements of the mass production rates from those LPCs having nonzero nongravitational accelerations. Water molecules dominate the
mass flux and outflow momentum from the nucleus. Direct measurements of the water production rate are impractical, but observations of water photodissociation products provide an accurate alternative. We placed the greatest reliance on a long and spectacular series of measurements of Lyα emission from cometary hydrogen, a photodissociation product of water, made using the SWAN mapping spectrometer instrument on the SOHO spacecraft (Bertaux et al. 1997). These measurements (Combi et al. 2008, 2009, 2011, 2014, 2018, 2019, 2021) have the advantage of internal consistency, being made using a single instrument and, in many cases, providing time resolution sufficient to monitor the heliocentric variation of the water production. Where necessary, we used other published production rate data as listed in Table 2.

Production rates measured as a function of heliocentric distance were interpolated to estimate the production rate at r_H = 1 au, denoted Q_H,O(1), and listed in Table 2. Some comets display significant asymmetry, such that Q_H,O(1) differs before and after perihelion. In these cases we list the average value. We estimate that the values of Q_H,O(1) in the table are accurate to no better than a factor of ∼2. The mass production rate at 1 au, M(1) kg s⁻¹, is related to Q_H,O(1) by M(1) = μm_HQ_H,O(1), where μ = 18 is the molecular weight of the water molecule and m_H = 1.67 × 10⁻²⁷ kg is the mass of the hydrogen atom. For reference, we note that a production rate Q_H,O(1) = 10²⁰ s⁻¹ corresponds to M = 3000 kg s⁻¹. We assume that gas produced on the nucleus surface flows away at the thermal speed V_θ = (8kT/(2πμm_H))¹/₂, where k = 1.38 × 10⁻²³ J K⁻¹ is the Boltzmann constant and T is the temperature of the sublimating ice surface. At 1 au, the temperature is depressed by sublimation to about T = 200 K, giving V_θ = 500 m s⁻¹. The temperature and V_θ change only slightly with heliocentric distance as a result of buffering by sublimation. We ignore solid material (“dust”) expelled simultaneously from the comets because, although the dust and gas mass production rates may be comparable, the dust mass is dominated by large particles that are poorly coupled to the gas flow, travel at speeds ≪V_θ, and so carry only a small fraction of the outflow momentum.

### 3. Results

#### 3.1. Nucleus Radii

We use the production rate and nongravitational acceleration data to estimate the radii of the nuclei in two ways. (a) **Radius from Total Production Rate**: In equilibrium with sunlight, sublimation of cometary ice drives a mass flux, f_s (kg m⁻² s⁻¹), from the surface. Measurements of comets show that sublimation from the nucleus nightside is weak because surface temperatures there are very low. Accordingly, we represent the
nucleus as a sphere, sublimating only from the dayside hemisphere, and we use the energy balance equation to calculate \( f_a \):

\[
\frac{L_\odot (1 - A_B)}{4 \pi R_n^2} = 2[\epsilon \sigma T^4 + f_a(T) H(T)].
\]

(3)

Here the term on the left-hand side is the absorbed solar power \((L_\odot = 4 \times 10^{26} \text{ W} \text{ is the solar luminosity, and } A_B = 0.04 \text{ is the assumed Bond albedo})\), the first term on the right-hand side accounts for radiation cooling \((\epsilon = 0.9 \text{ is the assumed emissivity, } \sigma = 5.67 \times 10^{-8} \text{ W} \text{ m}^{-2} \text{ K}^{-4} \text{ is the Stephan–Boltzmann constant, and } T \text{ is the effective temperature})\), and the second term on the right-hand side represents energy consumed in sublimating ice, the latent heat of which is \( H = 2 \times 10^6 \text{ J kg}^{-1} \). Equation (3) is solved using the Clausius–Clapeyron equation for the pressure versus temperature along the sublimation phase change boundary. At \( r_n = 1 \text{ au} \), for sublimation averaged over the dayside of a spherical ice nucleus, we find \( f_a = 2.1 \times 10^{-4} \text{ kg m}^{-2} \text{ s}^{-1} \).

The mass-loss rate, \( \dot{M} (\text{kg s}^{-1}) \), is then

\[
\dot{M} = 2 \pi n^2 f_a f_e,
\]

(4)

where \( n \) is the nucleus radius. The factor \( f_a \) represents the fraction of the surface area of the nucleus that contributes to the sublimation flux. Empirically, \( f_a \) is a decreasing function of nucleus radius and approaches unity on subkilometer short-period comets (Jewitt 2021). This trend is probably a result of observational bias favoring the detection of small cometary nuclei having large active fractions over those with less active surfaces. Values \( f_a > 1 \) are possible if ice sublimes both from the nucleus and from icy grains ejected from the nucleus. From Equation (4) we obtain the nucleus radius

\[
r_1 = \left( \frac{\dot{M}}{2 \pi n^2 f_a f_e} \right)^{1/2},
\]

(5)

and the nucleus mass

\[
M_n(1) = \rho_n \left( \frac{2}{9 \pi} \right)^{1/2} \left( \frac{\dot{M}}{f_a f_e} \right)^{3/2}.
\]

(6)

As a starting point, and in the absence of evidence regarding \( f_a \) on the long-period nuclei, we take \( f_a = 1 \). Values of \( r_1 \) are listed for each comet in Table 3. If \( f_a < 1 \), as in most short-period comets (A′Hearn et al. 1995), then \( r_1 \) gives an underestimate of the true radius.

(b) Radius from Nongravitational Acceleration: Nongravitational acceleration, \( \alpha_{NG} \), is the result of anisotropic mass loss from sublimating ices on the nucleus. We use it to obtain a second estimate of the mass of the nucleus.

The force on the nucleus is \( k_R \dot{M} V_{\text{th}} \), where \( V_{\text{th}} \) is the outflow speed and \( 0 \leq k_R \leq 1 \) is a dimensionless constant expressing the fraction of the outflow momentum that goes into accelerating the nucleus (for isotropic outgassing \( k_R = 0 \), while for perfectly collimated outgassing \( k_R = 1 \)). Then, force balance on a spherical nucleus of density \( \rho_n \) gives a second relation for the nucleus radius,

\[
r_2 = \left( \frac{3 k_R \dot{M} V_{\text{th}}}{4 \pi \rho_n \alpha_{NG}} \right)^{1/3},
\]

(7)

and the nucleus mass is

\[
M_n(2) = \frac{k_R \dot{M} V_{\text{th}}}{\alpha_{NG}}.
\]

(8)

We take the measured values of \( M \) and \( \alpha_{NG} \) from Table 2, and, as noted above, we adopt \( \rho_n = 500 \text{ kg m}^{-3} \) and \( V_{\text{th}} = 500 \text{ m s}^{-1} \). Measurements from 67P/Churyumov-Gerasimenko give \( k_R = 0.5 \) (Jewitt et al. 2020), which we assume to apply to the LPCs. The resulting values of \( r_2 \) are also listed for each comet in Table 2.

The two estimates of the nucleus radii are compared in Figure 1. Ideally, we would find \( r_1 = r_2 \) (indicated in the figure by the solid diagonal line), but the comets are better described by \( r_1 \sim (5/3) r_2 \) (shown as a dashed black line in the figure). Sosa & Fernández (2011) found a similar result and interpreted it to mean that the LPCs are hyperactive \(( f_a > 1 \text{ in Equation (5)} \text{ acts to reduce } r_1 \)), allowing substantial sublimation from icy grains in the coma in addition to ice in the nucleus. However, the assumption of hyperactivity is only one of several possible reasons for the difference between \( r_1 \) and \( r_2 \). Parameters \( k_R \) and \( \rho_n \) in Equation (7) might also be different from the values assumed, and radius estimate \( r_2 \) can be increased by increasing \( k_R \) and/or decreasing \( \rho_n \). To consider one example, \( r_1 \) and \( r_2 \) could be brought into agreement if the bulk nucleus density in Equation (7) were arbitrarily reduced by a factor \((5/3)^3 \approx 5\) to \( \rho_n \sim 100 \text{ kg m}^{-3} \) instead of \( 500 \text{ kg m}^{-3} \), as assumed. This lower density is by no means ruled out by physics and would still be consistent with values measured in several short-period comets (e.g., 6P/d′Arrest, 19P/Borrelly; Groussin et al. 2019). However, rather than make alternative, weakly justified guesses for some of the parameters in Equations (5) and (7), we conservatively choose the average radius, \( r_\text{av} = (r_1 + r_2)/2 \), as our best estimate of the nucleus radius, and we take the difference between radii \( r_1 \) and \( r_2 \) as a crude measure of the intrinsic radius uncertainty. We feel that this is a good procedure because, if we instead followed Sosa & Fernández (2011) by assuming that \( f_a > 1 \), the conclusions to be reached (described in Section 4) would be changed only by becoming stronger. The mean radii are listed in Column (4) of Table 3.

Figure 1 shows that the disintegrating LPCs (filled red circles representing C/2001 A2, C/2010 X1, C/2012 S1, C/2017 E4, C/2019 Y4, C/2020 F8, and C/2021 A1) have smaller nuclei, on average, than those that survive perihelion (filled yellow circles). Six of the seven disintegrating comets are subkilometer bodies, while the seventh (C/2001 A2 (LINEAR)) is only slightly larger at \( r_\text{av} = 1.4 \pm 0.4 \text{ km} \) (Table 2). The median radius of the disintegrating long-period nuclei is 0.41 km (mean value 0.55 ± 0.15 km, 7 objects), whereas that of surviving nuclei is 1.60 km (mean value 1.96 ± 0.28 km, 20 objects). The nonparametric Kolmogorov–Smirnov (K-S) test was used to assess the likelihood that the two radius distributions are drawn from the same population. This test gave a statistic \( D = 0.807 \), with an associated probability \( p = 0.002 \), consistent with the visual impression that the surviving and disrupted radius distributions are distinct. We also compared the distributions of perihelion distances of the surviving and disrupted comets. The median perihelion distance of the disrupted comets is 0.48 au (mean value 0.48 ± 0.09 au, 7 objects), while that of the survivors is 0.99 au (mean value 0.97 ± 0.10 au, 20 objects). The associated K-S statistics are \( D = 0.697 \) and \( p = 0.007 \), indicating that the hypothesis that the two samples are drawn from the same
parent population can again be rejected, although with less confidence.

Figure 2 compares the two measured quantities, the nongravitational acceleration and the mass-loss rate, both at 1 au. The figure shows that $\alpha_{\text{NG}}(1)$ and $M(1)$ are inversely related, and with a trend that is readily understood. All else being equal, we expect that the mass-loss rate should vary as $M(1) \propto r_n^{-2}$ (Equation (5)), while the nongravitational acceleration should vary as $\alpha_{\text{NG}}(1) \propto M(1)/r_n^3 \propto 1/r_n$ (Equation (7)), giving $\alpha_{\text{NG}}(1) \propto M(1)^{-1/2}$. The black line in Figure 2 has slope $-1/2$ and evidently matches the data well. A least-squares fit of a power law (dashed red line in the figure) to the data gives $\alpha_{\text{NG}}(1) \propto M(1)^B$ with $B = -0.66 \pm 0.17$, consistent with this expectation within one standard deviation. The color-coding in Figure 2 also shows that comets with the largest nongravitational accelerations and the weakest outgassing rates are the most likely to disintegrate, with an approximate separation between disintegrating and surviving comets at $\alpha_{\text{NG}}(1) \sim 10^{-8}$ m s$^{-2}$ and $M(1) \sim 10^3$ kg s$^{-1}$. By Equations (5) and (7), these values correspond to nucleus radii $r_n = 0.5$–0.9 km, consistent with the color-coding in Figure 1 showing that subkilometer LPC nuclei disintegrate.

### Table 3

| Comet | $r_1^a$ | $r_2^b$ | $r^c$ | $\alpha_{\text{NG}}^d$ | $M^e$ | $r_1^f$ | $\Delta r^g$ | Note$^b$ |
|-------|---------|---------|-------|------------------------|------|---------|-------------|---------|
| C/2000 WM1 (LINEAR) | 2.0 | 1.7 | 1.9 | 1.2e+29 | 3628 | 3.13 | 0.96 | F |
| C/2001 A2-A (LINEAR) | 1.8 | 1.0 | 1.4 | 7.3e+28 | 2188 | 1.58 | 1.02 | F |
| C/2001 Q4 (NEAT) | 3.6 | 1.8 | 2.7 | 2.2e+29 | 6691 | 7.15 | 1.05 | F |
| C/2002 T7 (LINEAR) | 4.2 | 2.2 | 3.2 | 4.7e+29 | 14263 | 6.65 | 0.98 | F |
| C/2002 X5 (Kudo-Fujikawa) | 1.3 | 0.8 | 1.1 | 1.2e+29 | 3607 | 0.32 | 0.85 | F |
| C/2003 K4 (LINEAR) | 3.5 | 2.2 | 2.8 | 2.1e+29 | 6252 | 9.79 | 1.07 | F |
| C/2004 Q2 (Machholz) | 3.9 | 2.1 | 3.0 | 2.3e+29 | 6895 | 10.32 | 1.09 | F |
| C/2009 P1 (Garradd) | 3.4 | 1.6 | 2.5 | 1.2e+29 | 3607 | 10.04 | 1.10 | F |
| C/2010 X1 (Elenin) | 0.4 | 0.3 | 0.3 | 6.0e+27 | 180 | 0.07 | 0.94 | F |
| C/2012 K1 (Pan-STARRS) | 2.2 | 1.2 | 1.7 | 8.8e+28 | 2645 | 2.79 | 1.07 | F |
| C/2015 US10 (Catalina) | 2.3 | 1.7 | 2.0 | 1.1e+29 | 3240 | 4.67 | 1.02 | F |
| C/2013 X1 (Pan-STARRS) | 3.7 | 1.7 | 2.7 | 1.7e+29 | 5140 | 9.31 | 1.09 | F |
| C/2014 E2 (Jacques) | 1.8 | 1.0 | 1.4 | 8.3e+28 | 2501.0 | 1.38 | 0.99 | F |
| C/2014 Q1 (Pan-STARRS) | 0.8 | 0.8 | 0.8 | 3.4e+28 | 1010 | 0.43 | 0.89 | F |
| C/2014 Q2 (Lovejoy) | 7.1 | 4.9 | 6.0 | 6.5e+29 | 19569 | 61.01 | 1.10 | F |
| C/2015 ER61 (Pan-STARRS) | 1.4 | 1.3 | 1.4 | 3.4e+28 | 1008 | 3.24 | 1.07 | F |
| C/2015 G2 (MASTER) | 1.1 | 0.9 | 1.0 | 3.2e+28 | 973 | 0.99 | 1.02 | F |
| C/2015 V2 (Johnson) | 2.0 | 1.1 | 1.5 | 3.8e+28 | 1154 | 4.18 | 1.10 | F |
| C/2017 E4 (Lovejoy) | 0.6 | 0.2 | 0.4 | 1.1e+28 | 328 | 0.08 | 0.95 | F |
| C/2001 Y1 (ATLAS) | 0.9 | 0.5 | 0.7 | 7.4e+27 | 223 | 0.98 | 1.09 | F |
| C/2009 Y4 (ATLAS) | 0.6 | 0.6 | 0.6 | 6.7e+27 | 202 | 0.57 | 1.03 | F |
| C/2009 Y4 (ATLAS) | 0.5 | 0.2 | 0.3 | 1.3e+28 | 393 | 0.03 | 0.87 | F |
| C/2009 Y4 (ATLAS) | 0.4 | 0.2 | 0.3 | 4.8e+27 | 143 | 0.04 | 0.92 | F |
| C/2009 Y4 (ATLAS) | 0.3 | 0.2 | 0.3 | 7.1e+27 | 177 | 0.06 | 0.92 | F |
| C/2015 A1 (Leonard) | 0.5 | 0.5 | 0.5 | 9.6e+27 | 577 | 0.27 | 0.98 | F |

Notes.

- $^a$ Nucleus radius from Equation (5), in km.
- $^b$ Nucleus radius from Equation (7), in km.
- $^c$ Mean nucleus radius, in km.
- $^d$ Average production rate when $r_n \leq 3$ au.
- $^e$ Average mass production rate when $r_n \leq 3$ au, in kg s$^{-1}$.
- $^f$ Spin change timescale, from Equation (9), in yr.
- $^g$ Elapsed time with $r_n \leq 3$ au, in yr.
- $^\delta$ D = disintegrated; F = fragmented.

Published examples of well-characterized subkilometer LPCs are few and far between; the compilation by Lamy et al. (2004) lists only two. C/1999 S4 (LINEAR) had $r_n = 0.45$ km (Altenhoff et al. 2002) and $q = 0.765$ au and disintegrated spectacularly at perihelion (Weaver et al. 2001), consistent with our findings here. C/1981 J1 (Sugano-Saigusa-Fujikawa) had $r_n < 0.37$ km (Hanner et al. 1987) and $q = 0.47$ au but was observed only for a few weeks when near Earth, so that its fate is unknown. The paucity of well-studied small nuclei relative to power-law extrapolations from larger sizes (Bauer et al. 2017) may itself be evidence for the efficient destruction of subkilometer LPC nuclei.

### 4. Discussion

Seven of the 27 LPCs in our sample either fragmented or disintegrated, fates that are indicated in Column (9) of Table 3 by the letters “F” and “D,” respectively. These descriptors are purely morphological; in fragmentation the comet splits into two or more discrete objects, typically each retaining a cometary appearance, while in disintegration the comet assumes the appearance of an expanding, diffuse cloud, lacking an obvious source or other embedded structure. The physical
The relationship between fragmentation and disintegration is unclear. We assume that the former is a mild case of the latter, and for simplicity in the following discussion, we use the term "disintegration" to apply to both.

4.1. Disintegration Mechanisms

Given the results in Figures 1 and 2, what mechanisms could be responsible for the disintegration of long-period nuclei?

**Tidal Breakup:** The Roche radius of the Sun for a comet nucleus represented as a fluid body of density $\rho_n = 500 \text{ kg m}^{-3}$ is $\sim 10^{-2} \text{ au}$. In our sample, only C/2012 S1 (ISON) approached the Sun closely enough ($q = 0.012 \text{ au}$) for tidal disruption to be possible. Neither have the remaining comets passed within the Roche spheres of any planet, eliminating tidal breakup as a generally relevant mechanism for this study.

**Sublimation:** Sublimation erosion is typically $\sim 10 \text{ m per orbit}$ (computed from Equation (3)) and thus is too slow to destroy a $\sim 1 \text{ km}$ diameter nucleus in the $\sim 1 \text{ yr}$ spent in strong sublimation while close to the Sun. Moreover, sublimation would naturally produce more steady erosion of the comet, not the catastrophic disintegrations as observed.

**Collisional Disruption:** Interplanetary collisions are very rare. Even in the relatively dense asteroid belt, the collisional disruption timescales of subkilometer bodies are measured in hundreds of Myr, such that the probability of a destructive collision in the $\sim 1 \text{ yr}$ spent by each comet near the Sun is negligible. Moreover, the LPCs have large orbits with random inclinations and disintegrate far above the ecliptic plane, where collisional disruption is even less likely.

**Confined Pressure Explosion:** Samarasinha (2001) invoked the buildup of gas pressure in order to explain cometary disruption. The problem with this mechanism is that the effect of heating by the Sun is confined to a thermal skin that is very thin compared to the radius of the nucleus. For example, cometary material has very small diffusivity, resulting in a thermal skin depth ($\sim 10^{-2} \text{ m}$) that is very small compared to the nucleus radius. Unless the full body of the nucleus is permeated by large interconnected voids (but still sealed from the vacuum of surrounding space), any gas pressure buildup must be confined to a thin surface shell incapable of disrupting the whole nucleus. Likewise, crystallization runaways, although potentially capable of triggering cometary outbursts (Prialnik & Bar-Nun 1992), are necessarily confined by the radial temperature gradient to a surface shell with thickness $\ll r_n$.

**Rotational Instability:** Outgassing exerts a torque on the cometary nucleus capable of substantially changing the spin on a timescale given by

$$
\tau_r = \left( \frac{16\pi^2}{15} \right) \frac{\rho_n r_n^4}{k_T V_{\infty} P} \left( \frac{1}{\bar{M}} \right)
$$

Here $P$ is the instantaneous spin period; $k_T$ is the dimensionless moment arm, equal to the fraction of the outflow momentum that exerts a torque on the nucleus; and $\bar{M}$ is the average value of the mass-loss rate following the comet in its orbit.
(Jewitt 2021). For a weakly cohesive nucleus, the end state of spin-up is rotational disintegration into fragments, which are themselves subject to rapid disintegration because of the strong dependence of $\tau_s$ on $r_n$ (Equation (9)) and because of the sudden exposure of previously buried volatiles.

To calculate $\bar{M}$, we use the facts that water is the dominant volatile and that strong sublimation of water ice is restricted to heliocentric distances $r_{1H} \lesssim 3$ au. Species more volatile than water (notably CO, CO$_2$) can sublimate at lower temperatures and larger distances, but their abundances are poorly constrained in our sample of comets and, in the interests of simplicity, we do not consider them here. Their inclusion would only strengthen our conclusions by amplifying the importance of outgassing torques relative to our water-ice calculation. Accordingly, we computed the average mass-loss rate for each comet using

$$\bar{M} = \frac{\int_{t_0}^{t_0+\Delta t} M(r_{1H}(t))dt}{\Delta t},$$

where $t_0$ is the pre-perihelion time at which $r_{1H} = 3$ au and $\Delta t$ is the time spent with $r_{1H} \leq 3$ au. The instantaneous mass-loss rate $M(r_{1H}(t))$ is computed by solving Kepler’s law for $r_{1H}(t)$ and using Equation (3) to find $M(r_{1H}(t)) = 2\pi R_3 f_3(r_{1H}(t)) \sigma^2$. The average, listed in Table 3, is then substituted into Equation (9) in order to calculate the characteristic spin-up time, $\tau_s$.

We again used values of the quantities $k_T$, $\rho_n$, and $P$ taken from the cometary literature. The median dimensionless moment arm, $k_T = 0.007$, is determined from measurements of the nuclei of short-period comets (Jewitt 2021). Likewise, the average nucleus density, $\rho_n = 480 \pm 220$ kg m$^{-3}$, is known only for the nuclei of short-period comets (Groussin et al. 2019). We adopt $P = 15$ hr, equal to the median rotation period measured in short-period comets (Jewitt 2021). While there are no clear reasons to think that the median $k_T$, $\rho_n$, and $P$ should be different in the long-period versus short-period comets, we are aware of this possibility and eagerly await direct measurements of these parameters in the former population. Given the uncertainties in these quantities, it is obvious that Equation (9) can provide, at best, a value of $\tau_s$ accurate to no better than an order of magnitude.

We set a simple criterion for judging the importance of spin-up torques by comparing $\tau_s$ with $\Delta t$, defined above as the time spent by each comet with $r_{1H} \lesssim 3$ au. If $\tau_s < \Delta t$, then sublimation torques can substantially modify the nucleus spin within a single perihelion passage of the comet, potentially leading to rotational instability and breakup. Otherwise, the outgassing torques are too weak to trigger rotational breakup, at least within a single perihelion passage. Values of $\Delta t$ and $\tau_s$ are listed in Table 3 and plotted for convenience in Figure 3.

Figure 3. Sublimation timescale, $\tau_s$ (Equation (9)), as a function of the time spent with $r_{1H} < 3$ au. Yellow and red filled circles denote nuclei that survived and that were destroyed by the perihelion passage, respectively. The solid black line marks $\tau_s = \Delta t$.

$LPCs$ with reciprocal semimajor axes $a^{-1} < 10^{-4}$ au$^{-1}$ are known as “Oort spike” comets, some but not all of which are dynamically new objects making their first pass through the planetary region. Oort (1950) found that a purely dynamical model of comet delivery from a distant reservoir predicts a larger flux of returning objects, relative to dynamically new comets, than is observed. He introduced an ad hoc “fading parameter” to bring the dynamical model into agreement with the data. The need for this fading parameter has since been confirmed many times (e.g., Wiegert & Tremaine 1999; Levison et al. 2002; Neslušan 2006), but the physical cause of the fading remains unknown. Oort (1950) and others conjecture that it is due to “surface aging” in response to insolation. Levison et al. (2002) concluded from the small number of detections of returning objects in ground-based surveys that a majority of dynamically new comets are destroyed, not merely faded.

The present work shows that disintegration, by removing comets from the observable sample, is a significant fading mechanism. The destruction is size dependent, preferentially afflicting small nuclei, and also perihelion distance dependent,
being more probable at small distances than at large ones. In contrast, published models of the fading parameter instead assume a survival probability that is independent of nucleus size (Wiepert & Tremaine 1999; Levison et al. 2002). Wiepert & Tremaine (1999) examined a sample of comets having median perihelion $q \sim 1$ au, comparable to that of our sample in Table 1. As one of several possible solutions, they found a fading law in which the comets are divided into two groups and supposed that some 95% of LPCs are destroyed within the first six perihelion passages while the remaining 5% survive indefinitely. We conjecture that this empirical division into two groups is an artifact of size-dependent rotational disruption; 95% of the LPCs are subkilometer objects subject to rotational disruption in a few orbits, while 5% are larger and can resist disruption for a much longer time.

The implication that only 5% of LPC nuclei have $r_n > 1$ km at first appears at odds with the radius distribution of the nuclei listed in Table 3, where 17 of the 27 nuclei (62%) are larger than 1 km. However, our sample is highly observationally biased against the inclusion of small nuclei because they produce too little H$_2$O to be detected in the flux-limited Ly$\alpha$ data from SWAN. (The largest comets are also excluded because their nongravitational accelerations are too small to be measured). As a result, the data in Table 3 severely underestimate the abundance of small LPC nuclei and cannot be used to assess the intrinsic size distribution of the nuclei.

Cometary fading has been reported to extend to at least $r_H \sim 10$ au (Królikowska & Dybczyński 2019; Kaib 2022), far beyond the region where outgassing torques from sublimating water ice can alter the nucleus spin. Moreover, a growing number of observations show activity in distant comets (e.g., ~20–25 au in the case of C/2014 UN271Bernardinelli-Bernstein, Farnham et al. 2021; and even 35 au in the case of C/2017 K2 (Pan-STARRS), Jewitt et al. 2021). Fragmentation has also been inferred at very large distances, for example, in comets C/2002 A1 and A2, reported to have split from a common parent when inbound at $r_H \sim 22.5$ au (Sekanina et al. 2003). Water ice is involatile beyond 5 or 6 au, and the sublimation of a more volatile material, perhaps carbon monoxide (CO) ice, is a leading candidate for driving this distant cometary activity. Could fading at large distances be due to torques from CO sublimation?

A definitive answer to this question cannot be reached given our limited knowledge of the surface properties of distant comets, or calculated from first principles. However, order-of-magnitude scaling considerations strongly suggest an answer in the negative, as follows. To first order, the ratio of the timescale for spin-up of a given body through sublimation of CO to that for spin-up through sublimation of water ice is (see Equation (9))

$$\frac{\tau_r(\text{CO})}{\tau_r(\text{H}_2\text{O})} \sim \frac{M(\text{H}_2\text{O}) V_{\text{th}}(\text{H}_2\text{O})}{M(\text{CO}) V_{\text{th}}(\text{CO})}.$$  (11)

We compare the sublimation of CO at 10 au to that of H$_2$O at 1 au. Fortunately, measurements of the two ratios on the right-hand side of Equation (11) are available for the LPC C/1995 O1 (Hale-Bopp). There, $M(\text{H}_2\text{O}, r_H = 1$ au)/$M(\text{CO}, r_H = 10$ au) $\sim 10^3$ (Figure 5 of Biver et al. 2002) and $V_{\text{th}}(\text{H}_2\text{O}, r_H = 1$ au)/$V_{\text{th}}(\text{CO}, r_H = 10$ au) $\sim 3$ (Figure 4(a) of Biver et al. 2002), giving $\tau_r(\text{CO}, r_H = 10$ au)/$\tau_r(\text{H}_2\text{O}, r_H = 1$ au) $\sim 3000$. This factor of 3000 is partly compensated by the longer time spent in the CO sublimation zone. C/1995 O1 had $r_H < 30$ au for 27 yr (compared with $\Delta t \sim 1$ yr for the comets in Table 1) and could have sublimated CO the entire time. Still, based on this scaling argument, spin-up timescales for a given object at 10 au are still two orders of magnitude larger than at 1 au, given C/Hale-Bopp-like outgassing behavior. Substantial spin-up due to CO torques seems unlikely unless the CO/H$_2$O ratios in other LPCs are much larger than measured in C/1995 O1. On this basis we conclude that, while important in the water sublimation zone, spin-up destruction is not an obvious cause of spin-up or fading in any but the tiniest comets beyond it. Oort’s fading parameter thus seems likely to have several physical origins, of which rotational disruption is only one.

For LPCs with $q \lesssim 3$ au, we offer three predictions that will be observationally testable in the foreseeable future given improved population data. First, LPC nuclei larger than a few kilometers in radius should rarely disrupt or disintegrate, unless by another process (e.g., tidal disruption, as may be the case for C/2012 S1 (ISON)). Second, the size distribution of LPCs should be flattened at radii $r_n \lesssim 1$ km, relative to its value at larger radii, owing to the selective loss of small nuclei through rotational instability. Third, accurately bias-corrected data should show that the size distributions of LPC nuclei vary with $q$, reaching “primordial” values only in the outer solar system, where mass loss is negligible.

Lastly, it is reasonable to expect that the imprints of rotational disruption might be found in the Damocloid population, to the extent that these objects (inactive bodies with Tisserand parameters $T_J \leq 2$) are remnants of formerly...
active LPCs. Measurements indeed show a flatter size distribution (Kim et al. 2014), consistent with the preferential destruction of smaller Damocloids, but the available sample is small and undoubtedly subject to its own biases. Future work on these objects may also be revealing.

5. Summary

We examine a sample of 27 LPCs for which both nongravitational accelerations and water production rates are available. Using these two measured quantities, we are able to estimate the nucleus sizes and so explore the systematics of this population. Seven of the 27 comets (∼25%) fragmented or disintegrated.

1. The disintegrating cometary nuclei have systematically smaller radii (median 0.4 km, 7 objects) than those that survive in proximity to the Sun (1.6 km, 20 objects).
2. The disintegrating comets have smaller perihelion distance (median 0.5 au, 7 objects) than those surviving (1.0 au, 20 objects).
3. These size and perihelion distance trends are both consistent with nucleus disintegration through rotational instability, triggered by outgassing torques from sublimating water ice. Specifically, the timescale for outgassing torques to change the spin of subkilometer nuclei is less than the time spent in strong sublimation.
4. Rotational disruption is a cause of the “fading” required to fit the orbital semimajor axis distribution of LPCs.

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