Hybrid Chirp Signal Design for Improved Long-Range (LoRa) Communications

Md. Noor-A-Rahim, M. Omar Khyam, Apel Mahmud, Xinde Li, Dirk Pesch, H. Vincent Poor

Long-range (LoRa) communication has attracted much attention recently due to its application for many Internet of Things applications. However, one of the key problems of the LoRa technology is it is vulnerable to noise/interference due to the use of only up-chirp signals during modulation. In this paper, to solve this problem, unlike the conventional LoRa modulation scheme, we propose a modulation scheme for LoRa communication based on joint up- and down-chirps. A fast Fourier transform (FFT) based demodulation scheme is devised to detect modulated symbols. To further improve demodulation performance, a hybrid demodulation scheme, comprised of FFT and correlation-based demodulation is also proposed. The performance of the proposed scheme is evaluated through extensive simulation results. Compared to the conventional LoRa modulation scheme, we show that the proposed scheme exhibits over 3 dB performance gain at bit error rate of $10^{-4}$.

Index Terms—LoRa, LoRaWAN, IoT, LPWAN, Chirp Modulation.

I. INTRODUCTION

The Internet-of-Things (IoT) has become the key technology to connect the physical world with the cyber world. The IoT now connects billions of devices embedded into the physical world to the Internet and allows us to share the data generated by them. Low-Power Wide-Area (LPWA) technologies are one of the key machine-type communications (MTC) technologies enabling IoT networks with low energy consumption and reasonable reliability. In recent years, a number of LPWA network (LPWAN) technologies have been proposed, including Sigfox, Narrow-Band IoT (NB-IoT), and LoRa, to name a few [1]. Of them, LoRa has attracted much attention because of its openness and flexibility, which has led to exceptional commercial growth of LoRa based offerings among the evolving LPWANs [2]. Furthermore, LoRa offers several benefits over conventional communication schemes thanks to its chirp spread spectrum modulation technique, which includes a constant signal envelope, energy-efficient long-range communication, robustness against narrow-band interference, and Doppler effect [3]. Despite its advantages, interference poses a significant problem for LoRa modulation as it uses ISM bands, where a number of other wireless technologies share the same spectrum [4]. In this light, the co-existence of both LoRaWAN or other LPWA networks has been studied extensively in recent years. For example, coded [5] or independent [6] message replications through time diversity have been proposed for both LoRaWAN or other LPWA networks. Co-existence of LoRa with Sigfox and IEEE 802.15.4g has also been studied in [7] and [8], respectively.

Since LoRa is popular technology, multiple independent LoRa networks are expected to be used in close vicinity. Therefore, LoRa signals are also vulnerable to the same spreading factor interference, particularly for large scale LoRa IoT deployments. The demodulation of LoRa under such a condition (known as capture effect) has been analyzed with mathematical models in [9]. Spreading factor allocation strategies have been used to enhance LoRa capacity in [10]. The physical layer of LoRa has been modeled mathematically in [11], while a closed-form approximation of LoRa modulation BER performance is presented in [7].

Despite significant efforts towards mitigating noise/interference effects on LoRa-based systems, interference still poses a significant problem for LoRa modulation. And the technical reason behind the noise/interference in the LoRa modulation scheme is it uses either up-or down-chirp as a basis to encode data in a cyclic manner, where a chirp is divided into two sub-chirps (Fig. 1). As a result, when the symbol value $(k)$ increases, the bandwidth of the first sub-chirp decreases (Fig. 1). In this situation, when demodulation is performed, the strength of the demodulated signal becomes weaker [12]. Therefore, in the presence of the interference/noise, a false peak is detected. A detailed description of the LoRa demodulation is given in Section II.

In this paper, we propose a modulation scheme for LoRa communication based on joint up- and down-chirps to solve this problem. The proposed system is inspired by the ultrasonic indoor positioning systems proposed in [13], [12], which demonstrated a system that uses both up-and-down-chirps at the same time is more resilient against noise/interference. The advantage of the proposed modulation scheme is that the bandwidth of the sub-chirps within a chirp does not reduce significantly with a higher symbol value (e.g., Fig. 2(d))

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compared to the conventional design (e.g., Fig. 1(d)).

To demodulate symbols in the proposed scheme, we propose a Fast Fourier Transform (FFT)-based demodulation scheme and develop a hybrid demodulation scheme for further enhancing the demodulation performance. We show that the proposed scheme significantly outperforms the conventional LoRa modulation scheme with and without interference scenarios.

The remainder of the paper is organized as follows. In Section II we briefly present the modulation and demodulation strategies for traditional LoRa communication. The proposed and enhanced modulation schemes are presented in Section III. The performance of the proposed schemes is presented and compared in Section IV. Finally, we conclude in Section V.

II. PRELIMINARIES

A. LoRa Modulation

Chirp spread spectrum modulation is used in LoRaWAN to generate the LoRa signal. In LoRa modulation, \( S \) bits are mapped into a LoRa modulated symbol, where \( S \) is the spreading factor. Hence, we need to create \( 2^S \) symbols to accommodate all possible bit combinations. The time-domain LoRa signal for one symbol period can be written as [14]:

\[
\begin{align*}
x_k(t) = &\begin{cases}
A e^{j2\pi((f_1+kB)t+Bt)\frac{B}{2T}} & \text{if } t \leq \tau \\
A e^{j2\pi((f_1+kB-B)t+Bt)\frac{B}{2T}} & \text{if } t > \tau
\end{cases}
\end{align*}
\]

(1)

where \( k \in \{0,2^S-1\} \) is the decimal representation of \( S \) bits\(^1\) in \( \text{d} \). \( A \) and \( T \) represent the amplitude and symbol duration of one LoRa signal, respectively. The bandwidth \( B \) of the LoRa signal is defined by \( B = f_h - f_i \), where \( f_h \) and \( f_i \) are maximum and minimum frequencies, respectively. Each LoRa modulated symbol satisfies the time-bandwidth constraint \( BT = 2^S \). The time of frequency hopping in one LoRa symbol period \( \tau \) is defined by \( \tau = T - \frac{k\tau}{2^S} \). The spreading factor establishes a trade-off between the data rate and coverage range. The instantaneous frequency of \( x_k(t) \) can be calculated as:

\[
\begin{align*}
f_{x_k}(t) = &\begin{cases}
f_1 + \frac{kB}{2T} + \frac{B}{2T} t & \text{if } t \leq \tau \\
f_1 + \frac{kB}{2T} - B + \frac{B}{2T} t & \text{if } t > \tau
\end{cases}
\end{align*}
\]

(2)

A simple example of the traditional LoRa modulation scheme is presented in Fig. 1 for \( S = 2 \) where each \( k \) represents a different bit.

B. LoRa Demodulation

The received signal in the presence of interference and noise is given by:

\[
y_k(t) = x_k(t) + \tilde{x}_k(t) + w(t),
\]

(3)

where \( \tilde{x}_k(t) \) is an interference signal (with spreading factor same or different to \( x_k(t) \)) and \( w(t) \) represents the complex white Gaussian noise with zero mean and variance \( \sigma^2_w \). The demodulation of a received LoRa signal is generally performed either through matched filtering or de-chirping. In the former one, the received signal is cross-correlated with all possible combinations of the signature signals. A high correlation peak implies that the desired signature signal is presented within the received signal and the index of the peak denotes the starting of the desired signature signal, which is also useful to determine range information between the transmitter and receiver. Although this approach has several advantages, including high range resolution and enhanced SNR [15], the major problem of this approach is high computational complexity.

The underlying principle of the later one involves multiplying the received signal with a synchronized raw down-chirp having the same \( S \) and \( B \). Assuming no noise and interference, the multiplied signal becomes:

\[
z_k(t) = x_k(t) \times A e^{j2\pi(f_i t - \frac{B}{2T})},
\]

(4)

where the second term in the multiplication represents raw down-chirp signal. The instantaneous frequency of the multiplied signal can be given as follows:

\[
f_{z_k}(t) = \begin{cases}
f_1 + f_h + \frac{kB}{2T} & \text{ if } t \leq \tau \\
(f_1 + f_h + \frac{kB}{2T}) - B & \text{ if } t > \tau
\end{cases}
\]

(5)

Equation (5) implies that the demodulated signal comprises two intervals, each consists of a constant frequency. In both intervals, the frequency linearly depends on the offset and the difference between the levels is \( B \). Now, suppose the signal is downsampled at the rate of \( B \) Hz. In that case, the instantaneous frequency turns into a continuous frequency over the entire chirp and, after subtracting the term \( f_1 + f_h \), is proportional to the shift \( k \). As a result, the resultant sampled signal becomes a pure sinusoid. When FFT is performed on that sinusoid, that response is obtained with the peak shifted by the \( k \) value [16]. The above process can be summarized by the following equation:

\[
\hat{k} = \arg \max F(z_k(t)) - f_l - f_h
\]

(6)

where \( \hat{k} \) is an estimate of the transmitted symbol’s index \( k \) and \( F(z_k(t)) \) gives frequency domain representation after performing down-sampling on \( z_k(t) \) at the rate of \( B \) Hz. More details on the down-sampling and frequency domain representation can be found in [17].
III. PROPOSED MODULATION SCHEME

In previous studies, it was shown that the chirp signal design based on joint up- and down chirps always exhibits better performance compared to the chirp signal composed of only up- or down-chirp. For example, in the context of indoor positioning, the scheme based on joint up- and down-chirps provides better location accuracy than the one based on only either up- or down-chirp schemes. Motivated by this, we propose a LoRa modulation scheme using both up- and down-chirp in contrast to the conventional, either up- or down-chirp approach. In our proposed scheme, we represent the first half only either up- or down-chirp schemes. Motivated by this, we propose a LoRa modulation scheme where only two frequency components are observed (as described in Subsection II-B), while is composed of multiple frequency components, where the signal power is distributed among the frequency components. As a result, after FFT, the peak of the frequency spectrum obtained from will be much higher than the peak of the frequency spectrum obtained from. Note that a similar phenomenon can be observed when the down-chirp based received signal is multiplied by a synchronized raw down-chirp, the frequency of the resultant signal becomes:

\[
z_{kd}(t) = \begin{cases} 
Ae^{2\pi(2f_1 + \frac{kB}{2\pi} - Bt)t} & \text{if } t \leq \tau_{ku} \\
Ae^{2\pi(2f_1 + \frac{kB}{2\pi} + Bt)t} & \text{if } t > \tau_{ku}
\end{cases}
\]

(10)

By examining the peak of the frequency spectrum obtained from and , one can determine that the received signal corresponds to an up-chirp based transmitted signal. We observe that is similar to the traditional demodulation scheme where only two frequency components are observed (as described in Subsection II-B). While is composed of multiple frequency components, where the signal power is distributed among the frequency components. As a result, after FFT, the peak of the frequency spectrum obtained from will be much higher than the peak of the frequency spectrum obtained from. Note that a similar phenomenon can be observed when the down-chirp based received signal is multiplied by a synchronized raw down- and up-chirp, respectively. Mathematically the process can be described in the following manner. Firstly, we find the estimates of the index () of the up-chirp-based transmitted symbol and the corresponding amplitude () by the following manner:

\[
\hat{k}_u = \arg \max_i F_k(z_{ku}(t)) - f_t - f_h
\]

\[
F_k = \max (F_k(z_{ku}(t)))
\]

Similarly, for the down-chirp-based transmitted symbol, we find the index () and the corresponding amplitude () by the following manner:

\[
\hat{k}_d = \arg \max_i F_k(z_{kd}(t)) - f_t - f_h
\]

\[
F_k = \max (F_k(z_{kd}(t)))
\]

The estimated index of the transmitted symbol is given by:

\[
\hat{k} = \arg \max_i (F_i)
i \in \{k_u, k_d\}
\]

B. Hybrid Demodulation

In this section, we propose a hybrid demodulation algorithm to further improve the performance of the proposed FFT based demodulator. In the presence of noise/interference, sometimes the FFT demodulator incorrectly detects the transmitted up-chirp (down-chirp) based signal as a down-chirp (up-chirp) based signal. To tackle this ambiguity, we perform two cross-correlation operations after performing the FFT based demodulation, as cross-correlation-based demodulation provides optimum detection. After performing the multiplication

\[2\]
of the received signal with raw down- and up-chirp signals, we find one up-chirp based candidate transmitted LoRa symbol and one down-chirp based candidate transmitted LoRa symbol. Then we perform cross-correlation between the received signal and the candidate symbols from where the best matched symbol is considered as the transmitted symbol. The proposed hybrid demodulation scheme is summarized in Algorithm 1.

**Algorithm 1 Hybrid Demodulation Technique**

1. Find $z_{k_u}(t)$ and $z_{k_d}(t)$ from (1) and (2), respectively.
2. Following (3) and (4), find the estimates of up- and down-chirps-based transmitted symbol’s indexes i.e., $\hat{k}_u$ and $\hat{k}_d$, respectively.
3. Perform cross-correlation between the received signal and the LoRa symbols with indexes $\hat{k}_u$ and $\hat{k}_d$ and find the absolute cross-correlation values $X_{\hat{k}_u}(\ell)$ and $X_{\hat{k}_d}(\ell)$, respectively.

$$X_{\hat{k}_u}(\ell) = \left| \int_{-\infty}^{\infty} y_k(t) \cdot x_{\hat{k}_u}^*(t-\ell) \, dt \right|$$

$$X_{\hat{k}_d}(\ell) = \left| \int_{-\infty}^{\infty} y_k(t) \cdot x_{\hat{k}_d}^*(t-\ell) \, dt \right|$$

4. Find the estimated index of the transmitted symbol by the following equation:

$$\hat{k} = \arg \max_{i \in \{k_u, k_d\}} \{X_i(0)\}$$

![Fig. 3: Performance comparison between the proposed and traditional LoRa modulation schemes with different spreading factors.](image)

**IV. Numerical Results and Discussion**

In this section, we present the performance evaluation of our proposed LoRa modulation and demodulation scheme. In the simulation, we set $B = 125$ KHz and a packet size of 200 bits. In Fig. 3, we present the performance comparison between our proposed scheme and the traditional scheme in the presence of additive white Gaussian noise (AWGN). The bit error rate (BER) performance is presented for $S = \{6, 8, 10\}$. As expected, the improved BER performance is observed as $S$ increases. We observe that the proposed LoRa modulation scheme outperforms the traditional LoRa modulation scheme for all scenarios. The proposed scheme exhibits over 3 dB improvement at a BER of $10^{-4}$ compared to the traditional scheme. A further improvement over the proposed FFT based demodulation is observed by applying the proposed hybrid demodulation scheme, since the correlation performed in the hybrid demodulation eliminates the ambiguity in nature (up/down) of the received signal. For different spreading factors, in Table I, we present the required signal-to-noise ratio (SNR) to obtain a packet error rate $\leq 0.01$. For each case, we observe a significant improvement in SNR threshold with our proposed modulation and demodulation schemes.

Now we present the performance of the proposed schemes in the presence of interference, where the desired LoRa signal collides with another LoRa signal. For interference signals with spreading factors $S = \{6, 8, 10\}$, the BER performance comparison is presented in Fig. 3. In the simulation, we set the noise as Gaussian distributed with variance $\sigma^2 = 1$. We consider unit received power for desired LoRa signal, while vary the received power of the interference LoRa signal to vary the signal-to-interference and noise ratio (SINR). Again, the BER performance improves as the $S$ increases except in the scenario where the interference signal has the same spreading factor as the desired signal, for which the worst performance is observed. Similar to the results shown in Fig. 3, we observe a performance improvement for all the scenarios with the proposed schemes. For all combinations of reference signals and interference signals, the SINR threshold comparison is presented in Table I. Again, we find the minimum SINR required for each combination to achieve a packet error rate of 0.01. From the table, we observe that in most cases, the proposed schemes exhibit a better SINR threshold compared to the traditional scheme.

**V. Conclusion**

In this paper, we have proposed novel modulation and demodulation schemes for LoRa communications. The modulation scheme is designed based on up- and down-chirp signals. A FFT based demodulation scheme is proposed to detect the proposed modulated symbols. For further enhancement, a hybrid demodulation scheme is also presented, which comprises FFT and correlation-based operations. With and without interference, simulation results show that the proposed schemes exhibit better bit error rate performance compared to the conventional LoRa modulation scheme.

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TABLE I: SNR (in dB) threshold comparison.

| Sp. Fac | S = 6 | S = 7 | S = 8 | S = 9 | S = 10 | S = 11 | S = 12 |
|---------|-------|-------|-------|-------|--------|--------|--------|
| Traditional | -3    | -6    | -9    | -12   | -15    | -19    | -22    |
| Proposed (FFT) | -6    | -11   | -13   | -16   | -19    | -22    | -25    |
| Proposed (Hybrid) | -8    | -11   | -14   | -17   | -19    | -22    | -26    |

Fig. 4: Performance comparison of different LoRa signals in the presence of interference.

TABLE II: SINR (in dB) threshold comparison. Traditional, proposed, and hybrid schemes are presented by green, blue, and red circles, respectively.

| Des | S = 6 | S = 7 | S = 8 | S = 9 | S = 10 | S = 11 | S = 12 |
|-----|-------|-------|-------|-------|--------|--------|--------|
| Int |       |       |       |       |        |        |        |
| 0   | 0     | 0     | -1    | -2    | -3     | -3     | -4     |
| 1   | -3    | -4    | -5    | -5    | -6     | -6     | -7     |
| 2   | -6    | -7    | -8    | -8    | -9     | -9     | -9     |
| 3   | -10   | -10   | -10   | -10   | -10    | -11    | -11    |
| 4   | -12   | -12   | -12   | -12   | -12    | -13    | -13    |
| 5   | -15   | -15   | -15   | -15   | -15    | -16    | -16    |
| 6   | -17   | -17   | -18   | -17   | -18    | -18    | -18    |

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