Abstract

Pseudo-LiDAR 3D detectors have made remarkable progress in monocular 3D detection by enhancing the capability of perceiving depth with depth estimation networks, and using LiDAR-based 3D detection architectures. The advanced stereo 3D detectors can also accurately localize 3D objects. The gap in image-to-image generation for stereo views is much smaller than that in image-to-LiDAR generation. Motivated by this, we propose a Pseudo-Stereo 3D detection framework with three novel virtual view generation methods, including image-level generation, feature-level generation, and feature-clone, for detecting 3D objects from a single image. Our analysis of depth-aware learning shows that the depth loss is effective in only feature-level virtual view generation and the estimated depth map is effective in both image-level and feature-level in our framework. We propose a disparity-wise dynamic convolution with dynamic kernels sampled from the disparity feature map to filter the features adaptively from a single image for generating virtual image features, which eases the feature degradation caused by the depth estimation errors. Till submission (November 18, 2021), our Pseudo-Stereo 3D detection framework ranks 1st on car, pedestrian, and cyclist among the monocular 3D detectors with publications on the KITTI-3D benchmark. The code is released at https://github.com/revisitq/Pseudo-Stereo-3D.

1. Introduction

Detecting the 3D objects from monocular image enables the machine to perceive and understand the 3D real world, which has a wide applications including virtual reality, robotics and autonomous driving. Monocular 3D detection is a challenging task because of the lack of accurate 3D information in a single image. However, the huge potential in such a cheap and easy-to-deploy solution to 3D detection attracts more and more researchers. Remarkable progress has been made in Pseudo-LiDAR detectors [11, 29, 34, 43, 52] that use a pre-trained depth estimation network to generate Pseudo-LiDAR representations, e.g. pseudo point clouds and pseudo voxels, and then feed them to LiDAR-based 3D detectors. It shows that enhancing the capability of perceiving depth can improve monocular 3D detection performance. However, there is a huge performance gap between Pseudo-LiDAR and LiDAR-based detectors because of the errors in image-to-LiDAR generation [32].

Apart from LiDAR-based detectors, the stereo 3D detectors [9, 17] can also accurately localize 3D objects. Also, the gap in image-to-image generation for stereo views is much smaller than that in image-to-LiDAR generation, which is a cross-modality conversion. Instead of Pseudo-LiDAR, we propose a novel Pseudo-Stereo 3D detection framework for monocular 3D detection. Our Pseudo-Stereo 3D detection framework generates a virtual view from a single input image to compose Pseudo-Stereo views with the generated virtual view and the input view. Then, we feed the Pseudo-Stereo views to stereo 3D detectors for detecting 3D objects from the single input image. We use one of the most advanced stereo 3D detectors, LIGA-Stereo [17], as the base detection architecture. Thus, the virtual view generation is the key to our Pseudo-Stereo 3D detection framework.

We take KITTI-3D as an example only to explain how to generate a virtual view. Note that the virtual view does not require the ground-truth actual view in the dataset for training. In KITTI-3D, the monocular 3D detection is performed on the left image from the stereo views. Our aim

Figure 1. Overview of our Pseudo-Stereo 3D detection framework with novel virtual view generation methods: (a) Image-level to use the generated disparity map for forward warping the input left image into a virtual right image. (b) Feature-level to convert the left features into virtual right features. A feature conversion baseline is to clone the left features as the special case in stereo views.
is to construct Pseudo-Stereo views by generating the virtual right view from the input left view in either image-level or feature-level for monocular 3D detection. As shown in Figure 1, we propose two types of virtual view generation: (a) image-level to generate the virtual right image from the input left image and (b) feature-level to convert the left features into virtual right features. In image-level, we convert the estimated depth map from the input left image into disparities and use them to forward warp the input left image into a virtual right image to compose the Pseudo-Stereo views with the input left view. In feature-level, we propose a disparity-wise dynamic convolution with dynamic kernels sampled from disparity feature map to filter the left features adaptively for generating virtual right features, which eases the feature degradation caused by the depth estimation errors. Also, a simple feature conversion is to clone the left features as the virtual right features, which is the special case of stereo views that the virtual right view is the same as the left view. We summarize our contributions:

- We propose a Pseudo-Stereo 3D detection framework with three novel virtual view generation methods, including image-level generation, feature-level generation and feature-clone, for detecting 3D objects from a single image, achieving significant improvements in monocular 3D detection. The proposed framework with feature-level virtual view generation ranks 1st among the monocular 3D detectors with publications across three object classes on KITTI-3D benchmark.
- In our framework, we analyze two major effects of learning depth-aware feature representations, including the estimated depth map and the depth loss as the depth guidance. It is very interesting to find that the depth loss is effective in feature-level virtual view generation only and the estimated depth map is effective in both image-level and feature-level for depth-aware feature learning.
- In our feature-level virtual view generation method, we propose a disparity-wise dynamic convolution with dynamic kernels from disparity feature map to adaptively filter the features from a single image for generating virtual image features, which avoids the feature degradation caused by the depth estimation errors.

### 2. Related Works

The architectures for monocular 3D object detection can be mainly categorized into two groups: Pseudo-LiDAR based methods [11, 34, 43] that use pre-trained depth networks to generate pseudo LiDAR representations, e.g. pseudo point clouds and pseudo voxels, and then feed them to LiDAR-based 3D detectors, and the rest monocular 3D detection methods that use 2D feature learning from a single image with optional 3D cues matching, concatenating or guiding for 3D perception [24, 26, 31, 38, 39, 54, 57].

#### Monocular 3D Detection

There are a few monocular 3D detectors use 2D feature learning in 2D backbone with optional 3D cues concatenated or matched to 2D features for 3D perception. Chabot et al. [6] estimate the similarity between the detected vehicle and a pre-defined 3D vehicle shape template used as 3D cues in 2D backbone. They solve the 3D location and 3D rotation angle of the detected vehicle in a standard 2D/3D matching algorithm [22]. Barabanau et al. [2] use 2D features to predict the rotation and key points of a car in a 2D backbone. Then, they use a geometric reasoning between the key points and the corresponding points in CAD models to get the depth and 3D locations of the car. But it is difficult to get CAD models of all object classes. GrooMeD-NMS [21] extracts 2D features for monocular 3D detection, with a differentiable NMS selecting the best 3D box candidate. GS3D [23] uses a specifically designed 2D backbone to extract the surface features for tackling the representation ambiguity between 2D bounding box and 3D bounding box. MonoEF [56] employs a 2D backbone with a camera extrinsic parameter aware module to deconstruct camera extrinsic parameters from 3D detection parameters. M3D-RPN [4] extracts 2D image feature to predict both 2D and 3D bounding boxes directly by minimizing the distance error between the 2D projection of the predicted 3D bounding box and the predicted 2D bounding box. Following M3D-RPN [4], many works [28, 33, 35] enhance the 2D feature learning with the 2D-3D detection head for monocular 3D detection.

Some methods aggregate the 2D image feature and the depth features extracted from the depth map to get 2D depth-aware features [12, 33]. D4LCN [12] employs a depth-guided convolution with the weights and the receptive fields learning from the estimated depth for depth-aware feature extraction. DDMP-3D [47] uses a depth-conditioned propagation based on graph to learn 2D depth-aware features for monocular 3D detection. DD3D [33] adds a depth prediction head to the 3D detection head and uses a depth loss to learn 2D features that are sensitive to depth information for monocular 3D detection. DD3D also pre-trains the depth prediction head on a large-scale dataset and fine-tunes the overall network on monocular 3D detection task. Other methods extract 2D features and construct 3D feature volume from the transformation of 2D features to improve 3D perceiving capacity. CaDDN [38] uses the estimated depth distributions to construct a frustum feature grid. Then, the frustum feature is converted into a voxel grid using known camera calibration parameters to construct 3D voxel feature volumes. ImVoxNet [39] uses 2D backbone to extract 2D image feature and projects the 2D features into 3D feature volumes following [31]. Then, the 3D feature volumes go through 3D backbone to enhance the 3D features for monocular 3D detection.

**Pseudo-LiDAR.** Pseudo-LiDAR architecture converts
3. Preliminaries of Stereo 3D Detector

Volume-based stereo 3D detectors aim to generate 3D anchor space from stereo image [37] and localize 3D objects from 3D feature volume [9, 17, 48]. DSGN [9] follows the widely used 3D cost volume construction in stereo matching [16, 45, 50] with 3D geometric information encoding. The depth loss in stereo matching branch helps learn depth-aware features for the detection branch, improving the detection accuracy. Wang et al. [48] use a direct construction of 3D cost volume to reduce the computational cost. Based on DSGN [9], LIGA-Stereo [17] achieves significant improvements against other methods [3, 9, 53] in stereo 3D detection. Thus, we use LIGA-Stereo [17] as our base stereo 3D detection architecture and feed the Pseudo-Stereo views to LIGA-Stereo. We focus on how to generate the virtual right view from the input left view and learn Pseudo-Stereo features that are sensitive to depth information. Thus, we introduce the stereo image feature extraction and the 3D feature volume construction in LIGA-Stereo [17].

Stereo Image Feature Extraction. Given an image pair \((I_L, I_R)\) from stereo views, the LIGA-Stereo [17] first extracts the left features and the right features via a ResNet-34 [18] with shared weights as the 2D image backbone. The strides of the output feature map in the five blocks are 2, 2, 4, and 4, respectively. The channels of the output feature map in the five blocks are 64, 64, 128, 128 and 128. Then, we denote the left and the right features as \(F'_L\) and \(F'_R\) that are the input to the spatial pyramid pooling (SPP) module [7] with shared weights for getting the final left features \(F_L\) and right features \(F_R\). The strides of the final left features \(F_L\) and right features \(F_R\) are 1, and the channels of the final left features \(F_L\) and the right features \(F_R\) are 32.

The 3D Feature Volume Construction. With the left features \(F_L\) and the right features \(F_R\), the stereo volume \(V_{st}\) is built by concatenating the left features \(F_L\) with the re-projected right features \(F_{R→L}\) at every candidate depth level. Thus, the stereo volume construction can be formulated with camera parameters as:

\[
V_{st}(u, v, w) = \text{concat}[F_L(u, v), F_{R→L}(u, v)]
\]

\[
F_{R→L}(u, v) = F_R(u - \frac{f}{z_{min}} v, v) = F_R(u, v) - \frac{f h}{w} \text{, } v
\]

\[
d(w) = w \cdot v_d + z_{min}
\]

where \((u, v)\) are the pixel coordinates, \(w \in [0, 1, ...]\) indicates the depth index, \(S\) is the stride of the feature map, \(v_d\) is the depth interval, \(z_{min}\) indicates the minimal depth value, \(f\) is the camera focal length, and \(b\) represents the baseline of the stereo camera pair. After the stereo volume \(V_{st}\) is filtered by a stereo network 3D Hourglass [17], we get a re-sampled stereo volume \(V_{st}'\) and a depth distribution volume \(P_{st}\). The \(P_{st}\) describes the depth probability distribution of pixels for all the candidate depth levels described in \(d(w)\).

A depth loss is computed between the depth map regressed from the re-sampled stereo volume \(V_{st}'\) and the ground-truth depth map to guide the depth-aware learning of \(V_{st}'\).

4. Method

As shown in Figure 2, we propose three novel methods to generate the virtual right view from the input left view and construct the Pseudo-Stereo views in (a) image-level in Section 4.2, (b) feature-level in Section 4.3, and (c) feature-clone as the baseline of feature-level generation in Section 4.4. We describe the loss function in Section 4.5. In Section 4.6, we analyze the depth-aware feature learning in the proposed Pseudo-Stereo 3D detection framework.

4.1. Pseudo-Stereo 3D Detection Framework

We use LIGA-Stereo [17] as our base stereo 3D detection architecture and replace the stereo image feature extraction block with our Pseudo-Stereo image feature extraction block. As shown in Figure 2, we propose three virtual right view generation methods and extract Pseudo-Stereo image features from the input left view and the generated virtual right view. Then, we feed the Pseudo-Stereo image features to LIGA-Stereo for detecting 3D objects from the input left image only.
Figure 2. Overview of our virtual view generation methods: (a) Image-level that uses the generated disparity map for forward warping the input left image into a virtual right image, (b) Feature-level that converts the left features into virtual right features via the proposed disparity-wise dynamic convolution (DDC), (c) Feature-clone that simply duplicates the left features as the virtual right features.

4.2. Image-level Generation

In image-level, we generate a virtual right image $\hat{I}_R$ from the input left image $I_L$ using the estimated disparity map as shown in Figure 2(a). Then, we extract Pseudo-Stereo image features from the Pseudo-Stereo pair $(I_L, \hat{I}_R)$. With a pair of pixel correspondences $x_l$ and $x_r$ in the left image $I_L$ and the right image $I_R$, the disparity $d$ between the pair of pixel correspondences can be computed as:

$$d = x_l - x_r$$  \hspace{1cm} (4)

Given the depth value $z$ for the pixel $x_l$ in the input left image and the camera calibration parameters, the relationship between the disparity $d$ and its corresponding depth value $z$ can be formulated as:

$$d = \frac{f \cdot b}{z}$$  \hspace{1cm} (5)

where $f$ and $b$ are the camera focal length and the baseline of the stereo camera pair, respectively.

To get the virtual right image, we first use a pre-trained DORN [13] to estimate the depth map $Z$ from the input left image $I_L$. Then, we convert the depth map $Z$ to a disparity map $D$ according to Eqn. 5 with camera parameters. Following Eqn. 4, we use the disparity map to forward warp the left image $I_L$ [40] into the virtual right image $\hat{I}_R$ as shown in Figure 3. To address ‘blurry’ edges, occlusions, and collisions, we sharpen the disparity map by identifying the flying pixels and applying a Sobel edge filter response of greater than 3 to the disparity map on those flying pixels [19, 49]. In image-level generation, we embed the estimated depth information extracted from the left image into the virtual right image for Pseudo-Stereo 3D detection. Then, we use a ResNet-34 [18] with shared weights followed by a spatial pyramid pooling (SPP) module with shared-weights to extract the left features $F'_L$ and the virtual right features $\hat{F}'_R$ from the Pseudo-Stereo pair $(I_L, \hat{I}_R)$. We can use the Pseudo-Stereo image features to construct the stereo volume $V_{st}$ as detailed in Section 3.

4.3. Feature-level Generation

Generating the virtual right image is a time-consuming process because of the forward warping [19, 49]. To overcome this, we propose a differentiable feature-level method for generating the virtual right features from the left features and the disparity features as shown in Figure 2(b). We convert the estimated depth map into a disparity map and use two ResNet-34 [18] to extract the left features $F'_L$ from the left input image and the disparity features $F_D$ from the disparity map. The two ResNet-34 are not with shared weights.

Instead of computing the offsets to compensate the left view as the virtual right view, we propose a disparity-wise dynamic convolution (DDC) to filter the left feature map $F'_L \in \mathbb{R}^{W \times H \times C}$ adaptively by the dynamic kernels from the disparity feature map $F_D \in \mathbb{R}^{W \times H \times C}$ for generating the virtual right feature map $\hat{F}'_R \in \mathbb{R}^{W \times H \times C}$, where $W$, $H$ and $C$ are the width, height and channel of the feature map, respectively. As shown in Figure 4, the adaptive filtering process use a $3 \times 3$ sliding window to cover all the
feature points in \( F_D \) and \( F'_L \):

\[
\hat{F}_R(i, j) = \frac{1}{3 \times 3} \sum_{i' \in \{i - 1, i, i + 1\}} \sum_{j' \in \{j - 1, j, j + 1\}} F_D(u', v') \cdot F'_L(u', v')
\]

(6)

where \( u' \in \{i - 1, i, i + 1\} \) and \( v' \in \{j - 1, j, j + 1\} \) are the coordinates of the feature points in the sliding window. We need to apply \( W \times H \) times sliding window to cover the whole feature map, which is not efficient. Instead, we use a grid shifting operation that can cover the whole feature map with 9 times shifting. After padding, we shift a \( W \times H \) window following the direction and the step size represented in a \( 3 \times 3 \) grid \((g_i, g_j)\), \( g \in \{-1, 0, 1\} \) on \( F_D \) and \( F'_L \) for getting the kernel \( F_D^{(g_i, g_j)} \in \mathbb{R}^{W \times H \times C} \) and the feature map \( F_L^{(g_i, g_j)} \in \mathbb{R}^{W \times H \times C} \), respectively. When \( g_i = 0 \) and \( g_j = 0 \), the \( W \times H \) window covers the original feature map that is without padding as shown in black dot box of Figure 4. Thus, we can get the virtual right features \( \hat{F}_R \) by filtering \( F_L^{(g_i, g_j)} \) adaptively by the kernels \( F_D^{(g_i, g_j)} \):

\[
\hat{F}_R = \frac{1}{3 \times 3} \sum_{g_i, g_j} F_L^{(g_i, g_j)} \odot F_D^{(g_i, g_j)}
\]

(7)

where the grid shifting operation is applied nine times to cover the whole feature map. For more details, please refer to supplementary materials. We feed \( F'_L \) and \( \hat{F}_R' \) to SPP module with shared weights using strides of 4 for getting the final left features \( F_L \) and virtual right features \( \hat{F}_R \).

Compared with the image-level generation, the feature-level generation is faster without forward warping and more adaptive using the proposed disparity-wise dynamic convolution. Also, by embedding the estimated depth information into high dimensional feature space and using the embedded depth information to filter the left features, it mitigates the degradation of depth-aware representations and the depth-aware representations can strengthen the embedded depth information with extra depth guidance, achieving significant improvements in monocular 3D detection.

4.4. Image Feature Clone

We clone the left features as the virtual right features as shown in Figure 2(c). This can be seen as the special case of Pseudo-Stereo views that the virtual right view is the same as the left view. Also, feature cloning is used as the baseline of feature-level generation. With different Pseudo-Stereo views, the proposed framework can improve the representations of 3D feature volume with the paired pixel-correspondence constraints or the feature-correspondence constraints converted from the estimated depth map. However, cloning feature does not need a pre-trained depth estimation network in our Pseudo-Stereo 3D detection framework, leading to better generalization capability.

4.5. Loss Function

Since we use LIGA-Stereo [17] as our base stereo 3D detection architecture and replace the original stereo image feature extraction block with the proposed three variants of Pseudo-Stereo image feature generation block as shown in Figure 2, we employ the same loss function as LIGA-Stereo [17], including the detection loss \( L_d \) for the regression of all detection parameters, the depth loss \( L_{depth} \) as the additional depth guidance for the re-sampled stereo volume \( V'_t \) and the knowledge distillation loss \( L_{kd} \) to transfer the structural knowledge from a LiDAR-based detector as described in LIGA-Stereo [17]. The overall loss can be formulated as:

\[
L = \lambda_d L_d + \lambda_{dep} L_{depth} + \lambda_{kd} L_{kd}
\]

(8)

where \( \lambda_d, \lambda_{dep}, \) and \( \lambda_{kd} \) are the regularization weights for the detection loss, the depth loss, and the knowledge distillation loss, respectively. The knowledge distillation adopted in LIGA-Stereo is well studied in [17]. Please refer to LIGA-Stereo [17] for more details. We focus on how to generate the virtual right view from the input left view and improve the capability of perceiving depth in features.

4.6. Learning Depth-aware Features

The depth-aware feature learning in our framework lies in two aspects: the estimated depth map and the depth loss. We convert the estimated depth map as the disparity map and use it in either image space or feature space. By comparing the performance of the two methods, we can study the effect of the estimated depth map used for depth-aware feature learning in both image-level and feature-level. The depth loss \( L_{depth} \) is used as the additional depth guidance for the re-sampled stereo volume \( V'_t \) to improve the depth awareness in features, improving monocular 3D detection performance. Although both the estimated depth map and the depth loss can improve the depth awareness in feature learning, the interaction between the two factors is not well studied for monocular 3D detection before this work.

For the image-level generation in Section 4.2, we use a Pseudo-Stereo image pair to extract the Stereo image features, where the virtual right image is generated from the left image with the help of the estimated depth map. The monocular depth estimation is an ill-posed problem, which makes it difficult to get high-quality depth maps for virtual right image generation. Thus, the pixel-correspondence
constraints of the generated Pseudo-Stereo pairs may have large offsets against the ground truth because of the depth estimation errors. Learning with the virtual right image warped from the inaccurate pixel-correspondences causes feature degradation. Since there is a huge gap between the ground-truth depth and the degraded feature, forcing the network to fit the ground-truth depth map using the depth loss with the degraded feature impairs the overall performance. For feature-level generation in Section 4.3, the virtual right features are generated from the left features and the disparity features. Unlike image-level generation, where the forward-warping is a non-learning process from image to image, the feature-level generation is an adaptive learning process with disparity-wise dynamic convolutions from feature to feature. Also, the estimated depth information is embedded into high dimensional feature space and the embedded depth information is used to filter the left features in the feature-level generation. This eases the degradation of depth-aware representations, mitigating the gap between the ground-truth depth and the feature. Thus, the feature representations can evolve and refine the depth information with extra depth guidance, for example, a depth loss. For feature-clone in Section 4.4, we duplicate the left features as the pseudo-Stereo image features without the estimated depth map. The depth loss alone can improve the depth awareness of features, improving the detection performance.

5. Experiments

5.1. Dataset and Evaluation Metric

Dataset. KITTI 3D object detection benchmark [15] is the most widely used benchmark for 3D object detection. It comprises 7481 training images and 7518 test images, along with the corresponding point clouds captured around a mid-size city from rural areas and highways. KITTI-3D provides 3D bounding box annotations for 3 classes, Car, Cyclist and Pedestrian. Commonly, the training set is divided into training split with 3712 samples and validation split with 3769 samples following that in [12], which we denote as KITTI train and KITTI val, respectively. All models in ablation studies are trained on the KITTI train and evaluated on KITTI val. For the submission of our methods, the models is trained on the 7481 training samples. Each object sample is assigned to a difficulty level, Easy, Moderate or Hard according to the object’s bounding box height, occlusion level and truncation.

Evaluation Metric. We use two evaluation metrics in KITTI-3D, i.e., the IoU of 3D bounding boxes or BEV 2D bounding boxes with average precision (AP) metric, which are denoted as AP_{3D} and AP_{BEV}, respectively. Following the monocular 3D detection methods [2,12,54], we conduct the ablation study on Car. KITTI-3D uses the AP_{R11} with 40 recall points instead of AP_{R40} with 11 recall points from October 8, 2019. We report all the results in AP_{R40}.

5.2. Experiment Settings

Input Setting. We use the pre-trained model of DORN [14] to estimate the depth map. Then, we transform the depth maps into disparity maps with the camera calibration parameters. The virtual right images in image-level generation are generated before training to reduce the training time. For feature-level generation, the disparity map is normalized by μ=33.20, σ=15.91. The μ and σ indicate the mean and variance of disparity map calculated from the training set.

Training Details. The network is trained with an AdamW [25] optimizer, with β1=0.9, β2=0.999. We train the network with 4 NVIDIA RTX 3090 GPUs. The batch size is set to 4. For the regularization weights of the training loss, λ_d=1.0, λ_kd=1.0. The regularization weight λ_{dep} for depth loss L_{depth} is set to 0 or 1, representing whether the depth loss is used or not. We use a single model to detect objects in different classes (Car, Cyclist and Pedestrian) together. Other hyper-parameters are set as the same as LIGA-Stereo [17].

| Exp. | Methods     | L_{dep,t} | Easy AP_{3D}/AP_{BEV} | Moderate | Hard |
|------|-------------|-----------|------------------------|----------|------|
| 1    | Image-level | ✓         | 31.43 / 41.82          | 21.53 / 29.00 | 18.47 / 25.21 |
| 2    | Image-level | ✓         | 31.81 / 42.87          | 22.36 / 30.16 | 19.33 / 26.38 |
| 3    | Feature-level | ✓         | 35.18 / 45.50          | 24.15 / 32.03 | 20.35 / 27.57 |
| 4    | Feature-level | ✓         | 22.04 / 31.10          | 16.18 / 22.55 | 14.31 / 20.56 |
| 5    | Feature-clone | ✓         | 28.46 / 37.66          | 19.15 / 25.78 | 16.56 / 22.47 |
| 6    | Feature-clone | ✓         | 24.33 / 32.99          | 17.09 / 23.77 | 14.61 / 20.81 |

Table 1. Ablation studies of three proposed Pseudo-Stereo variants and L_{depth} at IOU threshold 0.7. Exp. is the experiment tag.

5.3. Ablation Study

As shown in Table. 1, we conduct ablation studies on the KITTI val for the three proposed Pseudo-Stereo variants: image-level, feature-level and feature-clone generation.

Image-level. As shown in Exp.1 and Exp.2 in Table. 1, with the depth loss, the overall performance of the image-level generation method decreases by (-0.38%, -0.83%, -0.86%) for AP_{3D} and (-1.05%, -1.16%, -1.17%) for AP_{BEV}. The pixel-correspondence constraints of the generated Pseudo-Stereo pairs may have large offsets against the ground truth because of the depth estimation errors. Learning with the virtual right image warped from the inaccurate pixel-correspondences causes the feature degradation. Forcing the degraded feature to fit the ground-truth depth map with the depth loss impairs the overall performance.

Feature-level. As can be seen from Exp.3 and Exp.4 in Table. 1, the feature-level generation with the depth loss achieves significant improvements on AP_{3D} (+13.04%, +7.97%, +6.04%) and AP_{BEV} (+14.4%, +9.48%, +7.01%). The forward-warping used in image-level generation is a non-learning process from image to image, while
the feature-level generation is an adaptable and differentiable learning process with disparity-wise dynamic convolutions from feature to feature. The virtual right features are generated from the left features and the disparity features. Thus, the feature degradation caused by the depth estimation errors is mitigated by embedding the estimated depth information into high dimensional feature space and using the embedded depth representations to filter the left features dynamically in the feature-level generation. The gap between the ground-truth depth and the feature is mitigated with the extra depth guidance from the depth loss, the depth representations can strengthen the embedded 3D measurements in feature-level, achieving much better performance.

**Feature-clone.** From Exp.5 and Exp.6 in Table 1, it shows that the feature-clone achieves significant improvements with the depth loss on $AP_{3D}$ (+4.13%, +2.06%, +1.95%) and $AP_{BEV}$ (+4.67%, +2.01%, +1.66%). This lies in the fact that feature-cluster does not require depth estimation network and the depth loss alone can improve the awareness of depth information in features.

**Estimated Depth Map.** From the comparison among Exp.2, Exp.4 and Exp.6 in Table 1, with the estimated depth map used in both image-level (Exp.2) and feature-level (Exp.4), the models achieve better performance than the model without using the estimated depth map (Exp.6), which implies that the estimated depth map is effective in both image-level and feature-level in our framework. In image-level, the degraded feature caused by inaccurate pixel-correspondences is not forced to fit the ground-truth depth without the depth loss, and the estimated depth map improves the capability of perceiving depth information in the image input level, improving performance for monocular 3D detection. In feature-level, the feature degradation is eased by the proposed DDC in high dimensional feature space and the estimated depth map improves the capability of perceiving depth information in features, thereby achieving better performance than the image-level methods.

**DDC.** By comparing the performance feature-level and feature-clone methods with and without depth loss, we find that the depth loss is essential in feature-level generation to monocular 3D detection. We use the feature-clone method with depth loss as the baseline and add DDC to the baseline (Exp.3 in Table. 1) to shown the effect. Feature-level generation with the proposed DDC achieves significant improvements against the baseline, indicating that the proposed DDC is effective in generating the virtual right view in feature level for monocular 3D detection. This lies in the fact that the proposed DDC uses the embedded depth representations to dynamically filter the left features, deriving depth-aware feature learning and achieving significant improvements in monocular 3D detection.

### 5.4. Quantitative and Qualitative Results

We evaluate the three proposed Pseudo-Stereo variants: image-level generation, feature-level generation and feature clone, on KITTI test and val set. From the above ablation studies, we choose the strategy with better performance for each method: image-level generation without depth loss (Ours-im), feature-level generation with depth loss (Ours-fld) and feature-clone with depth loss (Ours-fcd).

**Results on test set.** Table 2 shows the performance comparison for Car on KITTI test server and Table 3 shows the performance comparison for Pedestrian and Cyclist on KITTI test server. DD3D [33], GUPNet [27] and MonoPSR [20] rank 1st on Car, Pedestrian and Cyclist, respectively, for monocular 3D detection in KITTI-3D benchmark beh-

| Methods       | Reference | Easy  | Moderate | Hard    | Easy  | Moderate | Hard    |
|---------------|-----------|-------|----------|---------|-------|----------|---------|
| MonoDIS [44]  | ICCV 2019 | 10.37 | 7.94     | 6.40    | 17.23 | 13.19    | 11.12   |
| AM3D [30]     | ICCV 2019 | 16.50 | 10.74    | 9.52    | 25.03 | 17.32    | 14.91   |
| M3D-RPN [4]   | ICCV 2019 | 14.76 | 9.71     | 7.42    | 21.02 | 13.67    | 10.23   |
| D4LCN [12]    | CVPR 2020 | 16.65 | 11.72    | 9.51    | 22.51 | 16.02    | 12.55   |
| MonoPair [10] | CVPR 2020 | 13.04 | 9.99     | 8.65    | 19.28 | 14.83    | 12.89   |
| MonoFlex [55] | CVPR 2021 | 19.94 | 13.89    | 12.07   | 28.23 | 19.75    | 16.89   |
| MonoEF [56]   | CVPR 2021 | 21.29 | 13.87    | 11.71   | 29.03 | 19.70    | 17.26   |
| GrooMeD-NMS [21] | CVPR 2021 | 18.10 | 12.32    | 9.65    | 26.19 | 18.27    | 14.05   |
| CaDDN [38]    | CVPR 2021 | 19.17 | 13.41    | 11.46   | 27.94 | 18.91    | 17.19   |
| DDMP-3D [47]  | CVPR 2021 | 19.71 | 12.78    | 9.80    | 28.08 | 17.89    | 13.44   |
| MonoRUn [8]   | CVPR 2021 | 19.65 | 12.30    | 10.58   | 27.94 | 17.34    | 15.24   |
| DFR-Net [58]  | ICCV 2021 | 19.40 | 13.63    | 10.35   | 28.17 | 19.17    | 14.84   |
| MonoRCNN [42] | ICCV 2021 | 18.36 | 12.65    | 10.03   | 25.48 | 18.11    | 14.10   |
| DD3D [33]     | ICCV 2021 | 23.22 | 16.34    | 14.20   | 30.98 | 22.56    | 20.03   |
| Ours-im       | –         | 19.79 | 13.81    | 12.31   | 28.37 | 20.01    | 17.39   |
| Ours-fld      | –         | 23.74 | 17.74    | 15.14   | 32.84 | 23.67    | 20.64   |
| Ours-fcd      | –         | 23.61 | 17.03    | 15.16   | 31.83 | 23.39    | 20.57   |

Table 2. Performance for Car of three methods on KITTI test at IOU threshold 0.7. The best results are **bold**, the second best underlined.
Table 3. Performance for Pedestrian and Cyclist on KITTI test at IOU threshold 0.5. The best results are bold, the second best underlined.

Table 4. Performance for Car on KITTI val set at IOU threshold 0.7. The best results are bold, the second best underlined.

fore this work. As shown in Table. 2 and Table. 3, Ours-fld achieves better performance than DD3D [33], GUPNet [27] and MonoPSR [20] across all three object classes on both $AP_{3D}$ and $AP_{BEV}$ for monocular 3D detection using single model only. Moreover, our three methods achieve 18/18 best results and 15/18 second-best results across all three object classes on both $AP_{3D}$ and $AP_{BEV}$. Note that Ours-fld achieves 17 out of 18 best results except the hard level of car, where the best is Ours-fld. This implies that the proposed Pseudo-Stereo 3D detection framework is very effective in monocular 3D detection.

Results on val set. As shown in Table. 4, Ours-fld outperforms state-of-the-art methods on KITTI val set. Figure 5 shows the qualitative results of Ours-fld, the best model, on KITTI val set.

Generalization Capability. Usually, there is a large gap between the monocular 3D detection performance on val set and test set because of over-fitting. As shown in Table. 2 and Table. 4, the performance gap for Ours-fld is much smaller than Ours-im and Ours-fld. This lies in the fact that feature-clone method does not require the estimated depth map for training, leading to better generalization capability. Note that we provide both options in our framework.

6. Conclusion

We propose a Pseudo-Stereo 3D detection framework with three novel virtual view generation methods, including image-level generation, feature-level generation and feature-clone, for detecting 3D objects from a single image, achieving significant improvements in monocular 3D detection. The proposed framework with our feature-level virtual view generation method ranks 1st among the monocular 3D detectors with publications across three object classes on KITTI-3D benchmark. In feature-level virtual view generation, we propose a disparity-wise dynamic convolution with dynamic kernels from disparity feature map to filter the features adaptively from a single image for generating virtual image features, which eases the feature degradation and achieves significant improvements. We analyze two major effects of depth-aware feature learning in our framework.

Broader Impacts. Our Pseudo-Stereo 3D detection framework has the potential to provide a new perspective of monocular 3D detection with Pseudo-Stereo views to our community. Also, our analysis of depth-aware feature learning in Pseudo-Stereo frameworks may give an inspiration to mitigate the performance gap between monocular and stereo 3D detectors.

Acknowledgement: This work was supported by the National Key Research and Development Program of China (2018YFE0183900). Hang Dai would like to thank the support from MBZUAI startup fund (GR006).
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