Validation of Models for the Calculation of Sun Positions and mapped Radiation on inclined Surfaces

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Abstract. In order to validate building simulation programs and to identify sources of errors in implemented models, it is necessary to evaluate individual physical effects step by step. For building simulations, the radiation load that hits buildings is a significant boundary condition. In order to reproduce these loads as accurately as possible, sun position models and weather data adapted to them are necessary. With the help of sun position models, the radiation data (usually available in horizontal or normal radiation) are mapped onto inclined and oriented surfaces. This paper examines a possible validation. For the analysis, different building simulation tools (NANDRAD, Radiance, IDA ICE, Modelica, TRNSYS, ETU Simulation) are compared with different time steps for specific dates using the result data azimuth and altitude. The locations are distributed over the northern and southern hemispheres, inside and outside the tropics and polar circles, and with large deviations from the standard meridian, thus allowing errors to be found in the implemented sun position models. In the following step, these building simulation platforms are compared with regard to their minutely radiation loads on building façades. Errors in the radiation mapping on inclined surfaces are hereby determined.

1 Introduction to Solar Loads

1.1 Room Energy Balance

Fig. 1 shows the boundary conditions for the energy balance equation for indoor air nodes in thermal building simulations.

Fig. 1. Room Energy Balance Variables depending on solar radiation loads highlighted red

The red highlighted boxes in the figure contain variables of the balance equation that are directly or indirectly dependent on solar radiation loads. For thermal building simulations the solar radiation loads have a big impact on heating and cooling demand or thermal behaviour of the building.

This makes it clear that the correct calculation and mapping of these loads on a surface is important and that a detailed investigation is necessary. A possible validation approach for solar radiation loads is described and documented in detail in this paper. This approach has already been carried out within the SIMQUALITY[1] research project and the data presented here are derived from it. Subsequently, the solar radiation loads are described in more detail. After that the validation procedure is shown including the result data for different simulation programs. Finally, possible problems and questions are explained.

1.2 Definition of the Sun Position

To calculate a solar radiation load on a surface the exact sun position for each time step must be calculated. To describe the position of the sun several different systems exist. In this paper, the horizontal coordinate system is used to describe the position of the sun with azimuth and altitude as shown in Fig. 4.

The azimuth gives the direction of the sun with the fixed point at North and a positive count towards east. The Altitude describes the elevation angle of the sun above the horizon with positive sign. To determine the exact sun position the latitude lat., the longitude lon and the time zone tz of the location are to be calculated.
1.3. Calculation of the sun position

The following equations show a possible model for the calculation of the sun position for each time step of a year [2][3]. The sun position model described below is implemented in the CCM-Library[4]. It is used in NANDRAD[5] to calculate the sun position.

Standard longitude \( \text{lon}_{\text{Standard}} \):
\[
\text{lon}_{\text{Standard}} = tz \cdot 15^\circ
\]  
(1)

Longitude deviation to standard meridian correction \( \Delta t_{\text{long}} \):
\[
\Delta t_{\text{long}} = \Delta t_{\text{lon}} \frac{4 \text{ min}}{\text{deg}}
\]  
(2)

Corrected time with longitude, \( t_d \) apparent solar time:
\[
t_d = t_a + \Delta t_{\text{long}}
\]  
(3)

Correction of day length due to eccentricity and earth’s orbit around sun \( \Delta t_{\text{exc}} \):
\[
B = 2\pi \frac{t_d - 81}{365}
\]  
(4)

Equation of time ET:
\[
\text{ET} = t_d + \Delta t_{\text{long}} + \Delta t_{\text{exc}}
\]  
(5)

Equation of Time

Altitude of sun \( \gamma_s \):
\[
\sin(\gamma_s) = \sin(\text{lat}) \cdot \sin(\delta) + \cos(\text{lat}) \cdot \cos(\delta) \cdot \cos(h)
\]  
(10)

Azimuth of sun \( \alpha_s \):
\[
\tan(\alpha_s) = -\sin(h) \cdot \frac{\tan(\delta) \cdot \cos(\text{lat}) - \sin(\text{lat}) \cdot \cos(h)}{\cos(h)}
\]  
(11)

1.3 Calculation of Solar Radiation Loads on inclined surfaces

To calculate the exact solar radiation on an inclined surface the position of the sun at each time step has to be known. Subsequently the solar radiation loads from the climate file mapped onto the surface are calculated.

The following equations show a possible model to calculate the radiation load for any randomly inclined and rotated surface. There is only an isotropic model for calculating the diffuse radiation noted. The documented model is implemented in the CCM-Library and thus in NANDRAD.

- \( \alpha_s \): Azimuth of sun
- \( \gamma_s \): Altitude (elevation angle) of sun
- \( \alpha_p \): Azimuth of the inclined surface
- \( \beta_p \): Tilt angle / inclination angle of the surface
- \( \theta \): Declination angle

Equation for Direct Radiation:
\[
Q_{\text{rad,dir,hor}} = \frac{Q_{\text{rad,dir,hor}}}{\sin(\gamma_s)}
\]  
(12)

Equation for Diffuse Radiation (isotropic model)
\[
Q_{\text{rad,dir,hor}} = \frac{Q_{\text{rad,dir,hor}}}{\sin(\gamma_s)} \cdot \frac{Q_{\text{rad,dir,hor}}}{\sin(0.5\beta_p) \cdot Q_{\text{dir,hor}} + Q_{\text{diff,hor}}}
\]  
(13)
2 Validation of Solar Radiation Loads

In this section, a possible validation approach for correct solar radiation loads will be proposed. This means that first the sun position model and afterwards the solar radiation mapping on an inclined surface will be validated. For each validation test, a program will be set as the reference in order to carry out cross-platform checks. For each validation however it still needs to be discussed which program or data should be set as reference. It will only show a certain methodology for a possible validation approach.

2.2 Validation of sun position models

In the first step, the sun position model of each will be validated. The test case for the validation is described in detail below.

2.1.1 Participating programs

| Program       | Version          |
|---------------|------------------|
| NANDRAD[5]    | 1.4              |
| Radiance      | 5.2.0            |
| IDA ICE       | 4.8.0.1          |
| TRNSYS        | 1.8              |
| ETU Simulation| 4.1              |
| ETU HottCAD   | 5.1.x.19         |
| Modelica      | Dymola Ver 4.1   |
|               | AixLib 0.7.3[9]  |
| TAS           | 9.3              |

All programs shown in Table 1 take part in this validation task. Since some programs show deviations in the validation task and are currently working on improving the results only anonymised results are shown.

2.1.2 Locations

| Location   | Longitude in ° | Latitude in ° | Time-zone | Note                                           |
|------------|----------------|---------------|-----------|------------------------------------------------|
| Barrow     | -156.78        | 71.30         | -9        | Inside the northern polar circle               |
| Denver     | -104.86        | 39.76         | -7        | Small distance to the standard meridian        |
| Lima       | -77.12         | -12.00        | -5        | In the southern hemisphere and within the southern solstice circle |
| Potsdam    | 13.067         | 52.383        | 1         | Small distance to the standard meridian on the east side |
| Shanghai   | 121.43         | 31.17         | 8         | Short distance from the standard meridian      |
| Kaxgar     | 75.98          | 39.47         | 8         | Very large distance to the standard meridian (same time zone as Shanghai) |
| Singapore  | 103.98         | 1.37          | 8         | Small distance to the equator and within the northern solstice circle |
| Melbourne  | 144.83         | -37.67        | 10        | In the southern hemisphere outside the solar tropic |

2.1.3 Dates

To get a broad insight into the sun positions yearly output with an hourly step size and 5 different days with minutely output will be investigated. These dates are chosen by the ASHRAE 140 BESTest[11] and have been extended to cover the whole year.

The calculation results are compared for the following days with minutely output:

- 5. March
- 27. July
- 22. September
- 24. October
- 17. December
2.1.4 Results

Fig. 6 shows the azimuth and altitude for the 22nd of September for the location of Barrow and Fig. 7 shows the azimuth and altitude for the 24th of October for the location of Lima. Fig. 6 shows that the individual models certainly lead to different solar elevations. This also happens for locations such as Lima where the sun is close to the zenith shown in Fig. 7. For program 6 and 9 only the sun position angles are given when the sun is over the horizon (\(\gamma_s > 0^\circ\))

![Graph showing azimuth and altitude for Barrow on September 22nd](image1)

Fig. 6. Azimuth and Altitude for 22nd of September for Barrow

![Graph showing azimuth and altitude for Lima on October 24th](image2)

Fig. 7. Azimuth and Altitude for 24th of October for Lima

2.1.5 Evaluation

A cross checking of the altitude and azimuth is not working for altitude angles that get closer to the zenith (\(\gamma_s = 90^\circ\)) as the position of the sun at the sky is the same whereas the azimuth angle can diver strongly.

To find a better criteria to cross check the sun position, the vector of the sun ray in the Cartesian coordinate system will be determined for each calculated time step (minute, hour) from the specified azimuth and altitude. Subsequently the determined vector is compared with the vector of the reference program at the same time step. For this purpose, the angle spanned by both vectors is determined via the scalar product and considered to be deviating from a value of more than 3 degrees. The reference values for the comparison are taken from program 4. For the respective whole day and for the hours in which the sun is above the horizon (sunshine hours) the sum of all minutes with deviation over the comparison period is determined.

Table 3 Number of minutes with deviation between the reference program (program 4) and the evaluated programs.

(only programs with deviation shown)

| Location | Date   | Program 2 | Program 5 |
|----------|--------|-----------|-----------|
| Barrow   | Jul27  | 1         | 86        |
| Denver   | Dec17  |           | 1         |
| Kaxgar   | Dec17  |           | 1         |
| Lima     | Mar5   | 1         | 1         |
|          | Jul27  | 1         |           |
|          | Sep22  | 1         |           |
|          | Oct24  | 1         |           |
|          | Dec17  | 1         |           |
| Melbourne| Mar5   | 1         | 2         |
|          | Jul27  | 1         | 2         |
|          | Sep22  | 1         | 3         |
|          | Oct24  | 1         | 9         |
|          | Dec17  | 1         | 1         |
| Shanghai | Dec17  | 1         |           |
| Singapur | Jul27  | 1         |           |
|          | Dec17  |           | 1         |

Table 3 shows the sum of all deviations between program 4 and the regarded program for all tested dates and locations. Only program 2 and program 5 are shown since the other tested programs had no deviation to program 4. In Table 4 the validation of program 2 is shown. Table 3 indicates that program 2 has often only one minute at some days that deviates from the reference program which is considered as a cosmetic problem. Program 5 shows at the location Barrow around midnight a faulty altitude angle (0 degree) when the sun is still up. Therefore it is not validated for Barrow. All other locations with small
deviations are considered to be cosmetic and are therefore validated.

| Date   | Barrow | Denver | Lima | Potsdam | Shanghai | Kanger | Singapore | Melbourne |
|--------|--------|--------|------|---------|----------|--------|-----------|-----------|
| Mar5   |◼       |◼       |◼     |◼        |◼         |◼       |◼          |◼          |
| Jul27  |◼       |◼       |◼     |◼        |◼         |◼       |◼          |◼          |
| Sep22  |◼       |◼       |◼     |◼        |◼         |◼       |◼          |◼          |
| Oct24  |◼       |◼       |◼     |◼        |◼         |◼       |◼          |◼          |
| Dec17  |◼       |◼       |◼     |◼        |◼         |◼       |◼          |◼          |
| Validation |◼       |◼       |◼     |◼        |◼         |◼       |◼          |◼          |

### 2.2 Validation of solar radiation on inclined surfaces

In the second step of the here described validation procedure, the mapped radiation on an inclined surface will be validated. In order to take part in this validation it is necessary to pass the validation of the sun position model. This validation approach is described in detail below.

#### 2.2.1 Programs

Since not every program took part in the sun’s position validation, only the programs shown in Table 5 are investigated in this research. Some programs show deviations in the validation task and are currently working on improving the results of the validation task and therefore only anonymised results are shown.

| Program          | Diffuse Radiation Model |
|------------------|-------------------------|
| NANDRAD          | Isotrop                 |
| IDA ICE          | Anisotrop (Perez)       |
| TRNSYS (1)       | Isotrop                 |
| TRNSYS (2)       | Anisotrop (Perez)       |
| ETU Simulation   | Anisotrop               |
| Modelica AixLib  | Isotrop                 |

As program 6 is highly developed concerning the solar radiation models it will be chosen as the reference for this test case.

#### 2.2.2 Model

In order to validate the different models that map the radiation a surface with an area of 1m² having different inclinations and orientations are defined. Table 6 shows an overview of the different surfaces that must be modelled in this test case.

To validate radiation loads on differently inclined and orientated directions this paper will only focus on two surfaces – an east oriented surface with 90° inclination (E90) and a west oriented surface with 30° inclination (W30).

#### 2.2.3 Locations

Concerning the location Potsdam was chosen for this test case. Since the validation of the sun position already showed possible inaccuracies or model errors at different locations there is no need to test several locations. The test reference year of 2010 TRY2010 of Potsdam in the epw-format is taken.

#### 2.2.4 Dates

For the validation the same dates as used in the validation of the sun position will be taken.

#### 2.2.5 Results

In Fig. 9 diffuse, direct and global Solar Radiation is shown for the surface oriented West with an inclination of 30° on the 27th of July and in Fig. 9 diffuse, direct and global Solar Radiation is shown for the surface oriented East with an inclination of 90° on the 22nd of September.

To get a better overview, the daily energy integral is moreover shown. It becomes obvious that all programs calculate very different curves for the solar radiation over the day and the deviations are therefore significant. Program 1 has very jagged radiation loads over the day program 4 has a constant offset to the back. Program 6 usually shows the highest maxima during the day. Program 2 always lies in between. The possible effects are discussed hereafter in the evaluation section.
**Fig. 9.** Radiation Loads on the surface oriented West with an inclination of 30° for 27th of July (W30)

**Fig. 10.** Radiation Loads on the surface oriented East with an inclination of 90° for 22nd of September (E90)
2.2.6 Evaluation

Fig. 11. Radiation Loads Evaluation (direct, diffuse and global) for the surface oriented East with an inclination of 90°

Fig. 12. Radiation Loads Evaluation (direct, diffuse and global) for the surface oriented East with an inclination of 90°

Table 7. Validation overview for the solar radiation daily energy integral on surface E90 and W30 for program 4

| Program 4 | E90 | W30 |
|-----------|-----|-----|
| Mar5      | ■   | ■   |
| Jul27     | ■   | ■   |
| Sep22     | ○   | ■   |
| Okt24     | ○   | ■   |
| Dec17     | ■■  | ■   |

Validation

For surface E90 the evaluation results are shown in Fig. 11 and for surface W30 the evaluation results are shown in Fig. 12.

In this test case, the evaluation for all programs with isotropic or anisotropic radiation model as shown in Table 8 are split up. As mentioned before program 6 serves as the reference program for isotropic radiation model types and program 5 as the reference for anisotropic radiation model types.

Table 8. Reference programs for the validation tasks

| Model       | Reference | programs  |
|-------------|-----------|-----------|
| Anisotropic | program 5 | program 1, program 2 |
| Isotropic   | program 6 | program 3, program 4 |

The deviation of each program is based on the reference program. To validate the solar radiation load on the surfaces the solar radiation energy integral for all dates will be calculated and the deviation should not be over 10% from the reference. It is to be questioned how the qualitative course of the radiation loads is to be evaluated. As Fig. 9 and Fig. 10 show, the difference between the individual programs is significant. This question needs to be discussed further.

Fig. 13. Comparison of all programs regarding the distribution of the radiation values from the climate file. Diffuse radiation on a horizontal surface is shown

These deviations can have several reasons. One particular cause is the interpretation of the solar radiation data from the climate file as shown in Fig. 13. In this the course of the diffuse solar radiation on a horizontal surface is shown so that the mapping of the radiation data to the sun position does not affect the comparison. Program 6 interprets the radiation values from the climate file as an hourly integral and then calculates the course over the
day, so that the hourly integral at the end of each hour step fits to the solar radiation value from the climate file. Program 1 interprets the radiation data as constant values for each hour and therefore the curves are jagged. Program 4 interprets the radiation values from the climate file as momentary values and therefore it is shifted to the back and its integrals are usually too small since the sun position does not fit to the radiation value from the climate file. Program 3 calculates a strongly attenuated radiation pattern throughout the day and the maximum hourly integral values are not reached either. The situation is similar for program 2. It calculates the radiation intensities based on the radiation values from the climate file and shifts the course by about half an hour to the front. However, this means that the hour integrals also deviate and do not fit to the climate file.

2.3 Validation results

Table 9 shows an overview of the complete validation approach for the solar radiation loads. It shows that program 2, 3, 5 and 6 are the only thermal simulation programs that are able to pass the validation approach. Program 1 and 4 have either difficulties with the sun positioning or the mapping of radiation loads on an inclined surface.

Table 9. Validation overview for all programs

|                  | Program 1 | Program 2 | Program 3 | Program 4 | Program 5 | Program 6 |
|------------------|-----------|-----------|-----------|-----------|-----------|-----------|
| Sun position model | ■         | ■         | ■         | ref       | ■         | ■         |
| Solar Radiation on inclined surfaces | □         | ■         | ■         | □         | ref       | ref       |
| Validation       | □         | ■         | ■         | □         | ■         | ■         |

3 Conclusion

In this paper, a possible cross-program validation approach was explained and carried out to compare solar radiation loads for thermal building simulation programs. First the position of the sun and after that the radiation on an inclined surface were calculated. In order to test the sun position model profoundly, several worldwide spread locations and dates distributed over the year were calculated and compared with output data in minute steps. Furthermore, the solar radiation on several inclined planes was compared for the location of Potsdam. In order to provide a wide range of different simulation programs, various tools that modelled the test cases within the research project SIMQUALITY[1] were compared.

It was shown that the calculated sun positions of the individual programs are very close together. Moreover, the solar loads on the inclined surfaces were compared. The results show that there are big differences between all programs concerning the interpretation and mapping of solar radiation loads from the climate file onto an inclined surface.

That demonstrates the importance of a stepwise validation of every single physical effect in thermal building simulation programs. The more complex models become and the more parameters influence them, the more difficult it becomes to detect possible model or implementation errors. Hence, there is a need for well-elaborated and accurate validation procedures for single physical effects to get correctly working programs. In this paper a procedure for the validation of solar radiation loads has been developed and described.

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