Production of Very Light Elements and Strontium in the Early Ejecta of Neutron Star Mergers

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Abstract

We study the production of very light elements (Z < 20) in the dynamical and spiral-wave wind ejecta of binary neutron star mergers by combining detailed nucleosynthesis calculations with the outcome of numerical relativity simulations. All our models are targeted to GW170817 and include neutrino radiation. We explore different finite-temperature, composition-dependent nuclear equations of state, and binary mass ratios, and find that hydrogen and helium are the most abundant light elements. For both elements, the decay of free neutrons is the driving nuclear reaction. In particular, ∼0.5−2 × 10^{-6} M_⊙ of hydrogen are produced in the fast expanding tail of the dynamical ejecta, while ∼1.5–11 × 10^{-6} M_⊙ of helium are synthesized in the bulk of the dynamical ejecta, usually in association with heavy r-process elements. By computing synthetic spectra, we find that the possibility of detecting hydrogen and helium features in kilonova spectra is very unlikely for fiducial masses and luminosities, even when including nonlocal thermodynamic equilibrium effects. The latter could be crucial to observe helium lines on very few days after merger for faint kilonovae or for luminous kilonovae ejecting large masses of helium. Finally, we compute the amount of strontium synthesized in the dynamical and spiral-wave wind ejecta, and find that it is consistent with (or even larger than, in the case of a long-lived remnant) the one required to explain early spectral features in the kilonova of GW170817.

Unified Astronomy Thesaurus concepts: Neutron stars (1108); R-process (1324); Explosive nucleosynthesis (503)

1. Introduction

Binary neutron star (BNS) mergers are primary sites for the production of heavy elements in the universe through the rapid neutron capture process (r-process, e.g., Symbatsy & Schramm 1982; Eichler et al. 1989; Freiburghaus et al. 1999). This association was confirmed by the detection of the kilonova AT2017gfo (Arcavi et al. 2017; Coulter et al. 2017; Drout et al. 2017; Evans et al. 2017; Kasliwal et al. 2017; Nicholl et al. 2017; Pian et al. 2017; Smartt et al. 2017; Soares-Santos et al. 2017; Tanvir et al. 2017) as the electromagnetic (EM) counterpart of the BNS gravitational wave (GW) signal GW170817 (Abbott et al. 2017a, 2017b). The luminosity evolution of the UV/visible/IR transient AT2017gfo is indeed in agreement with the heating rate and opacity expected from a distribution of freshly synthesized r-process elements (e.g., Kasen et al. 2017; Perego et al. 2017; Villar et al. 2017; Tanaka et al. 2017; Wollaeger et al. 2018). A few days after merger the spectrum of AT2017gfo reveals emission and absorption features qualitatively compatible with the forest of lines expected for matter rich in heavy elements (in particular, lanthanides and actinides). However, the firm identification of spectral features attributable to specific elements whose mass number is larger than A ∼ 100 has so far not been robust (see, however, Smartt et al. 2017; Gillanders et al. 2021, for interesting attempts). The main difficulties here lie in the huge number of possible bound-bound and bound-free transitions that provide the bulk of the photon opacity in matter enriched in heavy elements, and in our still poor knowledge of these atomic transitions. Additionally, the high expansion speed of the matter expelled by BNS mergers (ejecta) and its nonuniform spatial distribution are...
expected to cause a significant and nontrivial line broadening. However, in the early kilonova phases most of the ejecta are still opaque to radiation: only the fastest ejecta have become transparent and form an atmosphere that can alter the thermal emission coming from the underlying photosphere. The composition of this thin atmosphere could actually provide spectral features whose origin is possibly easier to identify. Indeed, the spectrum at 1.5 days of AT2017gfo resembles a blackbody emission with a significant residual around 8000 Å whose analysis suggested the presence of strontium (Watson et al. 2019), a light r-process element whose production in the universe is however dominated by the slow neutron capture (see, e.g., Prantzos et al. 2020).

The discovery of EM counterparts of BNS mergers detected in GWs is a challenge that often requires prolonged observations of multiple candidate transients, due to the uncertainties in the sky localization of the source. The identification of lines in their spectra and the comparison with the expected abundances can help discriminate between more and less plausible candidates. This approach heavily relies on detailed theoretical modeling of the ejecta from BNS mergers and of the subsequent early kilonova emission. Different mechanisms, acting on different timescales, are responsible for multiple ejecta components, whose properties mainly depend on the still uncertain equation of state (EOS) of nuclear matter and on the binary mass ratio (see, e.g., Radice et al. 2020, and references therein). The dynamical (see, e.g., Korobkin et al. 2012; Bauswein et al. 2013; Palenzuela et al. 2015; Sekiguchi et al. 2015; Foucart et al. 2016; Lehner et al. 2016; Radice et al. 2016; Sekiguchi et al. 2016; Bovard et al. 2017; Radice et al. 2018) and spiral-wave wind (Nedora et al. 2019, 2021) ejecta are the earliest and fastest ejecta, thus becoming transparent within the very first days and possibly providing key spectral features. Larger amounts of matter are expelled later in the form of baryonic disk winds (see, e.g., Fernández & Metzger 2013; Perego et al. 2014; Metzger & Fernández 2014; Siegel et al. 2014; Just et al. 2015; Martin et al. 2015; Lippuner et al. 2017; Fujibayashi et al. 2018; Siegel & Metzger 2018; Fernández et al. 2019; Miller et al. 2019). In these cases the ejection mechanisms are, for example, turbulent viscosity of magnetic origin, neutrino irradiation, magnetic pressure. This larger amount of mass expanding with lower speed (compared to the dynamical ejecta) is expected to become transparent only after a few days.

In this paper, we investigate in a systematic way the production of very light elements (lighter than calcium) in BNS mergers, focusing in particular on hydrogen and helium, based on detailed merger simulations. For the first time, we directly connect the thermodynamics conditions for their production to the binary properties (mass ratio and EOS), and we study their early detectability in kilonova spectra. The presence of hydrogen in the dynamical ejecta of BNS mergers has already been predicted by Metzger et al. (2015) and Just et al. (2015). Indeed, in these works it was noticed that the head of the dynamical ejecta can contain $\sim 10^{-3} M_\odot$ of free neutrons expanding at $\geq 0.4c$, not captured by seed nuclei due to their sudden drop in density. In addition to producing peculiar neutron-powered precursors of kilonovae (Metzger et al. 2015), this fast expanding matter would provide an envelope of hydrogen around the ejecta. In this paper, we want to check the amount of hydrogen with respect to the inclusion of weak interactions in merger simulations and in the modeling of the merger through full general-relativistic simulations (see also Ishii et al. 2018; George et al. 2020). Moreover, we want to test if hydrogen can give possible spectral features. Also the production of helium has been reported in the analysis of the abundances obtained in the dynamical ejecta of BNS mergers (see, e.g., Wanajo et al. 2014). However, its origin and its dependence on the binary parameters and on the EOS have never been investigated, as well as its spectral detectability.

In addition to the very light elements, we also study the production of strontium since this element was claimed to be detected in AT2017gfo. We want to test if its inferred amount is compatible with our predictions and if this information can help discriminate between different merger models of GW170817.

The paper is structured as follows. In Section 2, we present the methods used in our analysis: in particular, the BNS merger simulations in Section 2.1, the nucleosynthesis calculations in Section 2.2, and the kilonova spectrum model in Section 2.3. Our results are presented in Section 3, focusing first on the nucleosynthetic yields in Section 3.1, then on the nuclear processes responsible for their production in Section 3.2, and on the analysis of the ejecta conditions in Section 3.3, and finally on the kilonova spectral features in Section 3.4. We summarize and discuss our results in Sections 4 and 5.

2. Method

2.1. BNS Merger Simulations

Nucleosynthesis in BNS mergers depends mainly on three physical parameters: the specific entropy ($s$), the electron fraction ($Y_e$), and the expansion timescale ($\tau$) (Hoffman et al. 1997). BNS merger ejecta cannot be characterized by a single value of these parameters. A distribution in the $(s, Y_e, \tau)$ space is instead expected.

In this work, we consider results of numerical relativity (NR) simulations performed with the WhiskyTHC code (Radice & Rezzolla 2012; Radice et al. 2014a, 2014b). The latter is an NR code that solves the Einstein’s equations in the 3 + 1 Z4c free-evolution scheme (Bernuzzi & Hilditch 2010; Hilditch et al. 2013) coupled to general-relativistic hydrodynamics on adaptive mesh-refinement grids. WhiskyTHC employs high-resolution shock capturing algorithms and implements finite-temperature, composition-dependent nuclear EOSs, an approximate neutrino transport scheme (Radice et al. 2016, 2018), and the general-relativistic large eddy simulation method for turbulent viscosity of magnetic origin (Radice 2017, 2020). The code was specifically designed to model the late inspiral, merger, and post-merger phases of BNS mergers.

We consider three models whose chirp mass is targeted to the GW170817 event (Abbott et al. 2017a) labeled as BLh_equal, BLh_unequal, and DD2_equal. The first and the third ones have $M_1 = M_2 = 1.364 M_\odot$, while the second one has $M_1 = 1.856 M_\odot > M_2 = 1.020 M_\odot$. The BLh_equal and BLh_unequal models employ the softer BLh nuclear EOS (Logoteta et al. 2021), a hadronic EOS whose high density part has been derived using the finite-temperature extension of the Brueckner–Bethe–Goldstone quantum many-body theory in the Brueckner–Hartree–Fock approximation. This EOS predicts a maximum mass of $2.10 M_\odot$ for a cold, nonrotating NS. The DD2_equal model uses the stiffer HS(D2) EOS (Typel et al. 2010; Hempel et al. 2012). This EOS was derived in the framework of relativistic mean field models, uses density-
dependent couplings at high density, and predicts a maximum	ns mass of 2.42 $M_\odot$. Both these EOSs are consistent with
current nuclear and astrophysical constraints and roughly
bracket uncertainties in the properties of matter above nuclear
densities.

For all simulations the adaptive mesh refinement is
caracterized by seven nested grids with 2:1 refinement level.
Each physical setup is run at least at two different resolutions,
sometimes even at three. The linear resolution in the
finest level is of $\sim$246, $\sim$187, and $\sim$125 m for the low, standard,
and high-resolution cases, respectively. We denote the three cases as LR,
SR, and HR, respectively. All models include neutrino
radiation, and in particular, neutrino absorption in optically
thin conditions. The latter is crucial to correctly predict the
composition of the dynamical ejecta (Wanajo et al. 2014;
Foucart et al. 2016; Radice et al. 2018). For each model we
consider both simulations with and without turbulent viscosity.
All the simulations employed in this work were presented in
Perego et al. (2019), Nedora et al. (2019), Bernuzzi et al.
(2020), and Nedora et al. (2021) where more details can be
found.

Tidal torques and shock waves produced by the bouncing
remnant unbind matter within a few milliseconds (the so-called
dynamical ejecta). For equal mass binaries, a softer EOS
produces stronger shocks and larger shock-heated ejecta, while
tidal ejection within a crescent across the equatorial char-
acterizes very unequal mass mergers. The dynamical ejecta are
obtained by applying the geodetic extraction criterion. A
summary of the amount of dynamical ejecta for the three
different models, as well as a list of the employed simulations,
can be seen in the upper part of Table 1. The mass values are
computed as the arithmetic average of the distribution of the
ejecta masses obtained by considering the different available
resolutions and by including both viscous and unviscous
simulations. The (possibly asymmetric) errors correspond to
the minimum and the maximum differences between the
average and distribution of the actual masses. Additionally, the
DD2_equal and BLh_equal simulations were extended up to
several tens of milliseconds after merger (and in particular, up
to $\sim$90–100 ms post merger in the SR cases) showing the
development of an $m = 1$ spiral arm in the central remnant.
The spiral arm propagates into the disk, transporting angular
momentum outward and producing a matter outflow in the
form of a spiral-wave wind. The presence of this wind is
directly related to the presence of a non-collapsed remnant in
the center (this justifies why we did not compute the wind for
the BLh_unequal model, in which a prompt BH formation
occurs). Moreover the corresponding ejection rate did not show
signs of attenuation at the end of the simulations. We decided to
estimate the ejection rate in the form of a spiral-wave wind
by considering the longest simulations available, i.e., the SR
ones. The SR simulations of the BLh_equal model produce
$1.08 \times 10^{-2} M_\odot$ around 105 ms for the simulation without
viscosity, and $1.61 \times 10^{-2} M_\odot$ around 90 ms for the viscous
simulation of spiral-wave wind ejecta, obtained by using the
Bernoulli extraction criterion. The SR simulations of the
DD2_equal model produce $1.23 \times 10^{-2} M_\odot$ around 80 ms post
merger for the simulation without viscosity, and $1.58 \times 10^{-2} M_\odot$ around 107 ms post merger for the viscous
simulation. When considering that this wind develops starting
10 ms after merger, we estimate the spiral-wave wind ejecta
rate, $R_{\text{wind}}$, to be $(1.57 \pm 0.42) \times 10^{-1} M_\odot$ s$^{-1}$ and
$(1.58 \pm 0.04) \times 10^{-1} M_\odot$ s$^{-1}$ for the BLh_equal and DD2_equal
model, respectively (see the bottom part of Table 1). Once
again, for each model the actual values and their uncertainties
have been computed using the average and the differences between the two available simulations.

### 2.2. Nucleosynthesis

To compute time-dependent yield abundances we use the
publicly available nuclear network SkyNet, including 7843
isotopes up to $^{337}$Cs (Lippuner & Roberts 2017). We employ
the latest JINA REACLIB database (Cyburt et al. 2010) while
using the same setup as in Lippuner & Roberts (2015) for the
other input nuclear physics. In particular, strong inverse rates

### Table 1

**Properties of the Dynamical Ejecta (Top) and of the Spiral-wave Wind Ejecta (Bottom)**

#### Dynamical Ejecta

| Model      | M1 $[M_\odot]$ | M2 $[M_\odot]$ | Viscosity and resolution | $m_{\text{ej}}$ $[10^{-3} M_\odot]$ | $m_{\text{H}}$ $[10^{-3} M_\odot]$ | $m_{\text{He}}$ $[10^{-3} M_\odot]$ | $m_{\text{Sr}}$ $[10^{-3} M_\odot]$ |
|------------|----------------|----------------|--------------------------|-------------------------------------|----------------------------------|----------------------------------|----------------------------------|
| BLh_equal  | 1.364          | 1.364          | vis: (LR, SR); no-vis: (LR, SR, HR) | $1.37^{+0.29}_{-0.25}$ | $1.52^{+0.05}_{-0.05}$ | $3.87^{+0.31}_{-0.21}$ | $3.01^{+0.47}_{-0.53}$ |
| BLh_unequal| 1.856          | 1.020          | vis: (SR, HR); no-vis: (SR, HR) | $9.1^{+0.14}_{-0.15}$ | $0.78^{+0.20}_{-0.33}$ | $9.25^{+0.52}_{-0.84}$ | $0.25^{+0.14}_{-0.14}$ |
| DD2_equal  | 1.364          | 1.364          | vis: (LR, SR, HR); no-vis: (LR, SR, HR) | $1.36^{+0.78}_{-0.13}$ | $1.70^{+0.19}_{-0.57}$ | $3.12^{+0.99}_{-1.43}$ | $2.91^{+0.85}_{-1.34}$ |

#### Spiral-wave Wind Ejecta

| Model      | M1 $[M_\odot]$ | M2 $[M_\odot]$ | Viscosity and resolution | $R_{\text{wind}}$ $[10^{-1} M_\odot$ s$^{-1}$ | $X_{\text{H}}$ $[10^{-8}$ | $X_{\text{He}}$ $[10^{-7}$ | $X_{\text{Sr}}$ $[10^{-7}$ |
|------------|----------------|----------------|--------------------------|-------------------------------------|----------------------------------|----------------------------------|----------------------------------|
| BLh_equal  | 1.364          | 1.364          | vis: (LR, SR); no-vis: (LR, SR) | $1.57 \pm 0.42$ | $0.92^{+0.40}_{-0.33}$ | $9.86^{+0.12}_{-0.28}$ | $2.12^{+0.31}_{-0.49}$ |
| DD2_equal  | 1.364          | 1.364          | vis: (LR, SR, HR); no-vis: (LR, SR) | $1.58 \pm 0.04$ | $6.64^{+0.49}_{-0.37}$ | $4.57^{+0.34}_{-0.20}$ | $3.58^{+0.05}_{-0.07}$ |

*Note.* For each BNS merger model we indicate the masses of the two NSs ($M_1$ and $M_2$) and the corresponding set of available simulations, differing by resolution and physical viscosity of turbulent origin. For the dynamical ejecta, we report the total, H, He, and Sr ejected masses. For the spiral-wave wind ejecta, we report the average ejection rate and the H, He, and Sr mass fractions. The reported numbers are the mean values, averaged over the set of simulations, while the errors correspond to the distance between the average and the largest or smallest values.

### Note

For each BNS merger model we indicate the masses of the two NSs ($M_1$ and $M_2$) and the corresponding set of available simulations, differing by resolution and physical viscosity of turbulent origin. For the dynamical ejecta, we report the total, H, He, and Sr ejected masses. For the spiral-wave wind ejecta, we report the average ejection rate and the H, He, and Sr mass fractions. The reported numbers are the mean values, averaged over the set of simulations, while the errors correspond to the distance between the average and the largest or smallest values.
are computed assuming detailed balance. Spontaneous and neutron-induced fission rates are taken from Frankel & Metropolis (1947) and Panov et al. (2010), adopting fission barriers and fission fragment distributions from Mammadou et al. (2001), Wahl (2002). The default version of SkyNet does not include β-delayed fission reactions. However, we do not expect them to affect the synthesis of light elements, but only of neutron-rich heavy nuclei and therefore the final abundances near the second r-process peak (see, e.g., Mumpower et al. 2018). Also, they do not significantly alter the abundances of nuclei surviving to fission after neutron freeze-out and undergoing α decay, and so we also assume that their contribution to He abundance in low Y_e conditions is negligible. Nuclear masses are taken from the REACLIB database, which includes experimental values where available and theoretical masses from the finite-range droplet macroscopic model (Möller et al. 2016) otherwise.

SkyNet requires time-dependent trajectories of Lagrangian fluid elements to predict the temporal evolution of the abundances. We initialized all trajectories in NSE at \( T_0 = 6\) GK. For a given electron fraction and entropy, the NSE solver determines the corresponding initial density, \( \rho_0 \), by considering a fully ionized ideal gas of ions, electrons, and photons. After that, matter density evolves first through an exponential phase and then to a homologous expansion (Lippuner & Roberts 2015):

\[
\rho(t) = \begin{cases} 
\rho_0 e^{-t/\tau} & \text{for } t \leq 3\tau, \\
\rho_0 (3\tau/(et))^3 & \text{otherwise.}
\end{cases}
\]

The tracer temperature is evolved consistently to the expansion, accounting for nuclear heating. The tracer and the abundances of all relevant nuclear species are evolved up to \( 10^9 \) s.

To cover the relevant intervals we perform extensive nucleosynthesis calculations over wide ranges of \( \tau, Y_\alpha \), and \( s \), namely, \( 0.5 \leq \tau [\text{ms}] \leq 200, \ 1.5 \leq s \{b_{\text{baryon}}^{-1}\} \leq 300, \) and \( 0.01 \leq Y_\alpha \leq 0.48, \) by constructing an \( 18 \times 26 \times 25 \) regular grid (approximately logarithmic in the two former quantities and linear in the latter). The above ranges span the relevant expected intervals for the ejecta properties of compact binary mergers.

We finally obtain time-dependent abundances from the convolution of the yields tabulated with SkyNet with the distribution of ejecta properties from the simulations. From each BNS simulations we extract the mass weighted distribution of the ejecta in the \( (s, Y_\alpha, v_\infty) \) space by inspecting the properties of the unbound matter on a coordinate sphere of radius 294 km. The solid angle is discretized in \( N_\theta = 51 \) polar and \( N_\phi = 93 \) azimuthal angular bins, uniform in both the \( \theta \) and \( \phi \) angles. We stress that we do not perform any averaging procedure over the angular variables, \( v_\infty \) is the asymptotic velocity computed as \( v_\infty = c(1 - \gamma^{-2})^{1/2}. \) In the case of the geodetic criterion, \( \gamma = u_2 \) is the time component of the four-velocity, while for the Bernoulli criterion, \( \gamma = u_h, \) where \( h \) is the relativistic specific enthalpy per baryon. The expansion timescale is computed starting from the density and velocity obtained from the simulations at the extraction radius, following the procedure introduced in Radice et al. (2016, 2018).

2.3. Kilonova Spectra

The possible presence of light elements in BNS merger ejecta raises the question of whether they can produce recognizable features in the observable spectra. To address this issue, we use the open-source spectral synthesis code TARDIS (Kerzendorf & Sim 2014) to produce spectral models for the predicted ejecta abundances and physical conditions. TARDIS is a Monte Carlo radiative-transfer code that operates in one dimension assuming the ejecta are spherically symmetric. In particular, it prescribes a thermal emission at the photosphere and then predicts the spectrum emerging after the radiation has interacted with the above atmosphere at a certain time after merger. Matter within the atmosphere is discretized by Lagrangian radial mass shells of monotonically increasing speed in velocity space. The code inputs include the luminosity at the photosphere, the density profile and the composition of the ejecta between the photosphere and the head of the ejecta. A set of atomic data for the relevant ions and the adopted approximations in computing the ionization/excitation state of the atoms in the ejecta, as well as the handling of matter-radiation interactions, are also required (see references in Kerzendorf & Sim 2014; Boyle et al. 2017; Vogl et al. 2019).

The presence of lanthanides and actinides significantly increases matter opacity in BNS merger ejecta (Kasen et al. 2013; Tanaka & Hotokezaka 2013) such that radiation drives the expanding ejecta toward local thermodynamical equilibrium (LTE) conditions (Kasen et al. 2017). However, we cannot exclude the possibility that the H and He lines are boosted by nonlocal thermodynamical equilibrium (NLTE) effects similar to those observed in the ejecta of supernovae (SNe). Indeed, helium excitation, and ionization rates in supernova ejecta are strongly affected by nonthermal electron collisions, produced by \( \gamma \)-rays resulting from the radioactive decay of \( ^{56}\text{Ni} \) (Graham 1988; Lucy 1991; Mazzali & Lucy 1998; Hachinger et al. 2012). The significant sensitivity of He to these effects is due to the large energy gap (20 eV) between the He I ground state and its first excited state, and to the metastability of its first two excited states. Since He in BNS merger ejecta is often embedded in radioactive material and the \( Q \)-value of \( ^{56}\text{Ni} \) decay is comparable to the one of \( r \)-process element decays during the kilonova timescale, it is reasonable to assume that similar effects could occur also in kilonovae.

TARDIS models LTE conditions between matter and radiation, but it also offers a variety of approximate NLTE treatments of ionization and excitation (for example, the nebular approximation for the ionization balance). Among them, TARDIS includes an analytical approximation for the NLTE helium level population that was developed for the He-rich ejecta of double detonation type Ia SNe (Boyle et al. 2017).

Additionally, strong departures from LTE can arise even without the presence of high-velocity electrons. The radiation field above the photosphere is typically dilute compared to that of a blackbody. In these conditions, the rate of collisions with thermal electrons is often too low to establish LTE populations for the low densities in the outer layers of the ejecta. The resulting NLTE effects significantly affect the hydrogen line strengths, as observed in type II SNe (Takeda 1990, 1991; Duschinger et al. 1995). To model these effects, we use the TARDIS version presented in Vogl et al. (2019), which has already been applied to modeling H-rich ejecta in NLTE conditions (Vogl et al. 2020). This version of the code includes
a more complete treatment of radiation-matter interactions including bound-free and free–free processes, as well as collisions between ions and thermal electrons. The modified code solves the statistical equilibrium equations for the ion and level number densities without relying on the Boltzmann and Saha equations.

In addition to the nucleosynthesis yields provided by our BNS and nucleosynthesis calculations, we require a model for the ejecta profile and photosphere evolution. In accordance with the symmetry employed by TARDIS, we consider the analytic spherically symmetric model presented in Wollaeger et al. (2018). In particular, we assume a homologously expanding layer of ejecta of total mass $M$, average expansion speed $v_{\text{avg}}$, and uniform gray opacity $\kappa$. The latter should be intended as an effective, average opacity related to the more physical and detailed energy-dependent one and to the relevant radiation spectrum. Typical values of $\kappa$ for kilonovae range between 1 and a few square centimeters per gram, depending on the matter composition (see, e.g., Tanaka et al. 2020). The density profile is described by

$$\rho(t, r) = \rho_0 \left(\frac{t}{t_0}\right)^{-3} \left(1 - \frac{r^2}{(v_{\text{max}} t)^2}\right)^3,$$

where $v_{\text{max}} = 128 v_{\text{avg}} / 63$ and $\rho_0 = 315 M / (64 \pi v_{\text{max}}^3)$. The time-dependent photospheric radius, $R_{\text{ph}}(t)$, is defined by the condition

$$\int_{R_{\text{ph}}(t)}^{R_{\text{max}}(t)} \rho(t, r) \kappa \, dr = \frac{2}{3},$$

while the mass outside the photosphere is computed as

$$M_{r>R_{\text{ph}}(t)} = 4\pi \int_{R_{\text{ph}}(t)}^{R_{\text{max}}(t)} \rho(t, r) r^2 \, dr.$$

Each fluid element expands with constant radial speed $v$ and the relation between the (Lagrangian) velocity coordinate and the (Eulerian) radial coordinate is $v = rt$.

3. Results

3.1. Nucleosynthesis: Overview

In Figure 1 we present number abundances of selected elements in the ejecta of the three considered models, 2 days after merger. For each model, the abundance values are obtained as the averages over all available simulations, while the error bars are the maximum and minimum difference with respect to the average. Among the lightest elements ($Z < 20$), H and He are the most abundant species, while all the elements between lithium and potassium are usually several orders of magnitude less abundant ($Y \lesssim 10^{-5}$). When considering the dynamical ejecta, the production of H and He appears robust and their abundances vary only within one order of magnitude even when changing the EOS stiffness or the binary mass ratio. H and He abundances are comparable to (or even larger than) lanthanides and actinides, as well as to Sr abundance, unless the binary is very asymmetric. Light element production is less significant in the spiral-wave wind ejecta, where the production of the first and second $r$-process peak elements is favored. However, we stress that the spiral-wave wind ejecta, where the production of H and He varies from the same model. In the case of a long-lived remnant, due to the larger spiral-wave wind contribution, H and He tend to be slightly underproduced with respect to Sr and heavy $r$-process elements.

In addition to the number abundances, our simulations can provide the masses of the different elements. In the upper part of Table 1 we report the masses of H, He, and Sr in the dynamical ejecta for the different merger models. Once again, the central values correspond to the arithmetic averages while the uncertainties to the largest difference between the average and the distribution of the actual values. Since the spiral-wave wind ejecta have not saturated at the end of our equal mass simulations and the precise amount of ejecta depends on the central remnant lifetime, in the bottom part of Table 1 we provide the mass fraction of the above elements in the spiral-wave wind ejecta.

Matter ejection from BNS mergers is not isotropic and from our models we can extract the angular distributions for the different atomic species. In Figure 2 we present the polar distribution factor for an element $i$, $f_i(\theta)$, defined as

$$f_i(\theta) = \frac{4\pi}{M_i} \int_0^{2\pi} dM_i \, d\Omega \, d\phi,$$

i.e., the ratio between the actual angular distribution of the mass of a certain element (averaged over the azimuthal angle) and the equivalent isotropic one ($M_i / 4\pi$). This factor measures how much the obtained ejecta distributions differ from an isotropic distribution. For the dynamical ejecta expelled by equal mass mergers (left panels), the total amount of mass (black solid line) shows a larger distribution at lower latitudes and a clear decrease (more pronounced in the case of the stiffer DD2 EOS) moving toward the poles. This is consistent with previous results (see, e.g., Radice et al. 2018) and testifies that, despite being emitted over the entire solid angle, the dynamical ejecta are not isotropic. H and He are distributed at all latitudes but in associations with different elements: close to the equator, together with heavier elements (e.g., with lanthanides and actinides); at high latitude, with lighter $r$-process elements (as Sr). This suggests a distinct origin, especially for He. For the
dynamical ejecta produced by very asymmetric mergers (top-right panel), most of the ejecta is concentrated across the equator (Lehner et al. 2016; Sekiguchi et al. 2016; Bernuzzi et al. 2020), where heavy elements and He are significantly synthesized, while H and Sr are produced at higher latitudes, where the amount of ejecta is significantly smaller or even negligible. Finally, for the spiral-wave wind ejecta (bottom-right panel), matter ejection happens predominantly at low latitudes, but in this case the production of heavy nuclei and He is more limited to the region across the equator ($70^\circ \lesssim \theta \lesssim 110^\circ$), H is negligible everywhere (since $f_{\text{He}}(\theta)$ is maximum when $f_{\text{total}}(\theta)$ is minimum), while light r-process elements, like Sr, trace well the overall ejecta distribution, with a significant excess/deficiency at very high/low latitudes, respectively.

3.2. Nucleosynthesis: Analysis

We investigate the origin of very light elements and of Sr first by presenting their abundances in Figure 3, alongside with the sum of the lanthanides and actinides ones. These abundances were obtained by considering individual trajectories characterized by broad ranges of $Y_e$ and $s$, and two expansion timescales that bracket the relevant scales for dynamical and spiral-wave wind ejecta, namely, $\tau = 1$ ms and $\tau = 11.4$ ms, corresponding to $v_\infty \lesssim c$ and $v_\infty \approx 0.1c$, respectively. Despite the fact that in Figure 1 we presented also the sum of the elements with $3 \leq Z \leq 19$, we do not report here their detailed abundances since they are subdominant and they do not produce any relevant feature on the presented scales.

3.2.1. Hydrogen

The presence of H in the ejecta is related to high-s and low-$Y_e$ matter that expands very rapidly, as visible in the top-left panel of Figure 3 (see also Metzger et al. 2015; Ishii et al.
In these conditions, H is produced as a decay product of free neutrons within a few tens of minutes. Indeed the ejecta at NSE freeze-out is composed mostly of free $n$'s, several percent in the mass of $\alpha$ particles and very few heavier seed nuclei ($A \lesssim 100$). Due to the extremely fast density drop, a large fraction of $n$'s do not participate in the $r$-process (Lippuner & Roberts 2015). The larger the abundance of H is, the smaller the abundance of heavy elements is, with a narrow intermediate regime of comparable abundances. For $\tau \gtrsim 10$ ms, H production becomes always negligible, unless for combinations of extremely high and low values of entropy and electron fraction, respectively.

### 3.2.2. Helium

As visible in Figure 3, the production of He can happen both in the absence of and in association with heavy elements, as also suggested by the simulation yields. The former case is realized for $Y_e \gtrsim 0.45$, when most neutrons are locked inside strongly bound nuclei (including $\alpha$'s) at NSE freeze-out, and the ratio between free neutrons and seed nuclei is not large enough to guarantee $r$-process nucleosynthesis beyond the second peak. The latter case takes place in two different regimes: (i) at high entropy ($s \gtrsim 60$ $k_B$ baryon$^{-1}$) for a broad range of electron fractions ($Y_e \lesssim 0.4$); (ii) at low entropy ($s \lesssim 60$ $k_B$ baryon$^{-1}$) for relatively low electron fractions ($Y_e \lesssim 0.23$). The high-$s$ regime was considered for many years as the main scenario for $r$-process nucleosynthesis in supernova winds (e.g., Woosley et al. 1994; Farouqi et al. 2010; Arcones & Martínez-Pinedo 2011). High-$s$ conditions favor the production of $\alpha$ particles and fewer heavier seed nuclei at NSE freeze-out ($\alpha$-rich freeze-out). The free neutrons are captured by the few seed nuclei to produce the heaviest elements, while for $Y_e \gtrsim 0.40$ the neutron-to-seed ratio becomes too small for this process to occur. In the low-$Y_e$, low-$s$ regime, He production correlates with the production of heavy $r$-process elements, particularly of actinides. In these

![Abundances at 2 days for $\tau = 1.0$ ms (top) and $\tau = 11.4$ ms (bottom) trajectories](image)

**Figure 3.** Number abundances of hydrogen, helium, strontium, and lanthanides and actinides summed together, as a function of $Y_e$ and $s$, for $\tau \sim 1.0$ ms (top) and $\tau \sim 10$ ms (bottom), at 2 days after merger, as obtained by our parametric nucleosynthesis calculations.
In the previous expressions $Y_{(A,Z)}$ is the number abundance of a nucleus with atomic number $Z$ and mass number $A$, $\langle \sigma v \rangle_{ZA}$, $\lambda_{\gamma,ZA}$ and $\lambda_{n,ZA}$ are the corresponding neutron capture rate, photodisintegration ($\gamma$, n) rate, and $\alpha$-decay rate, respectively, $\langle \sigma v \rangle_{t+t}$ represents the t + t reaction rate, while $\langle \sigma v \rangle_{d+t}$ the d + t reaction rate. Helium is initially depleted to form heavier iron group nuclei in expanding matter under NSE conditions, up to the point when charged-particle freeze-out occurs ($T > 3$ GK). Despite the initially larger $\alpha$ abundance, in the $Y_e = 0.35$ trajectory, due to the lower neutron abundance, (n, $\alpha$) reactions are inefficient in producing He that is instead effectively destroyed through ($\alpha$, n) reactions, thus reducing $Y_{\text{He}}$ more significantly than for smaller $Y^*$'s. After NSE freeze-out, (n, $\gamma$)-($\gamma$, n) equilibrium guarantees a high neutron density and neutron-to-seed ratio, and starting from seed nuclei with $A \geq 100$ drives the formation of heavier nuclei through the $r$-process nucleosynthesis, far from the valley of stability. The high abundance of free neutrons provides also an almost steady supply of free protons (through n-decay) and thus the efficient formation of d and t. Reactions such as $t + t \rightarrow n + n + ^4\text{He}$ and $d + t \rightarrow n + ^4\text{He}$ are not in equilibrium with their inverse.

As a consequence, He nuclei accumulate and increase their abundance until (n, $\gamma$)-($\gamma$, n) equilibrium freezes-out (visible in the figure when $Y^* \lesssim 10^{-4}$). When $Y_{\alpha}$ drops, tritium and deuterium are no more produced and the production of He is halted. As visible in the lower panels of Figure 4, $\tau_{\text{He}}$ is accounted by $\tau_{d+t}$ and especially $\tau_{t+i}$ in the time window between the end of NSE and the drop of $Y_{\alpha}$, clearly demonstrating that these two reactions are the main He production channel. At later times ($t > 2$ s), $\alpha$-decay of translead nuclei (if produced) becomes significant and $Y_{\text{He}}$ increases further. Lower initial $Y_e$ (i.e., a larger $Y_e \approx 1 - Y_{\alpha}$) results in (i) a wider time window over which t and d can be efficiently produced and converted into He, and (ii) a larger abundance of $\alpha$-decaying translead nuclei. This picture is further confirmed by the fact that if n decay is artificially removed from Skynet $Y_{\text{He}}$ stays initially frozen, before increasing only at $t > 2$ s due to $\alpha$ decays. When present ($Y_e \lesssim 0.2$), $\alpha$ decays can change He abundance by a factor of 2 on a timescale of several days after merger, comparable to the kilonova timescale. The relative importance between charged reactions and $\alpha$ decays has been analyzed in more detail in Appendix A.

### 3.2.3. Elements from Lithium to Potassium

For all elements between lithium and potassium, the predicted abundances are usually below $10^{-5}$ over the whole parameter space. Only for a few elements (namely, beryllium,}

![Figure 4: Evolution of a few selected abundances (top) and some relevant reaction timescales (bottom) for three low-entropy trajectories. For all trajectories, $s = 10^6$ baryon$^{-1}$ and $\tau = 10$ ms, while $Y_e = 0.15$, 0.25, and 0.35 moving from left to right. Before n freeze-out, reactions involving deuterium and tritium account for $\alpha$ particle production, while after $\alpha$ decay of translead nuclei. Vertical dotted lines correspond to the time at which the temperature drops below 3 GK, roughly corresponding to the NSE freeze-out, and to the time when $\alpha$ decays become effective. The point when $Y_{\alpha} = 10^{-4}$ is also presented as a freeze-out. For $0.2 \lesssim Y_e \lesssim 0.45$ the faster freeze-out and the lack of translead nuclei produce a lower $Y_{\text{He}}$.](image-url)
nitrogen, oxygen, and neon), abundances can be slightly above $10^{-5}$ in corners of the parameter space (usually, $Y_e \lesssim 0.3$ and high entropy). In the case of high-entropy ejecta, at NSE freeze-out the densities are rather low ($\lesssim 10^5$ g cm$^{-3}$). In the resulting $\alpha$-rich freeze-out conditions, the building of light elements through $\alpha + \alpha + n$ and triple-$\alpha$ reactions is very inefficient (unless the density of free neutrons can partially compensate). In the case of low entropy and possibly low $Y_e$ conditions, the nuclei distribution at NSE freeze-out is dominated by neutron-rich seed nuclei around the iron group (with $A \sim 70$–90). This distribution extends also toward lower mass numbers, but it is lower-bounded by the $N = 20$ and $Z = 20$ magic numbers. The subsequent $r$-process nucleosynthesis produces nuclei with $A \gtrsim 40$. For low electron fractions, $N$ can be significantly larger than $Z$, but the high-neutron-to-seed ratio drives the nucleosynthesis far from calcium isotopes. For relatively large $Y_e$ ($Y_e \gtrsim 0.4$), the starting seeds are close to the valley of stability and $\beta$ decays are not effective in significantly lowering the atomic number. All this prevents the efficient formation of nuclei below calcium and other than H and He both in high and low-entropy $r$-process nucleosynthesis.

3.2.4. Strontium

Figure 3 shows how the production of elements of the first $r$-process peak and immediately above it (as Sr) crucially depends on the ejecta $Y_e$. Indeed, for $0.2 \lesssim Y_e \lesssim 0.38$ Sr is robustly produced for entropy lower than $\sim 100 k_B$ baryon$^{-1}$. In these conditions, a weak $r$-process nucleosynthesis occurs: at NSE freeze-out, typical seed nuclei are in the mass range of $A = 50$–80 and the neutron-to-seed ratio is of a few tens. The subsequent neutron captures produce nuclei up to $A \sim 90$, including Sr, but the nucleosynthesis does not reach the second $r$-process peak. Within this regime, a significant increase of $Y_{Sr}$ is observed only for $0.35 \lesssim Y_e \lesssim 0.38$, while at relatively large entropy ($20 \lesssim s [k_B$ baryon$^{-1}] \lesssim 80$) Sr is produced with a lower threshold $Y_e (\lesssim 0.20)$. For $s \gtrsim 100$ $k_B$ baryon$^{-1}$ or $Y_e \gtrsim 0.48$, $\alpha$-rich freeze-out occurs. Sr can be also produced in $\alpha$-rich freeze-out conditions (see, e.g., Hoffman et al. 1997; Freiburghaus et al. 1999), but only for $20 \lesssim s [k_B$ baryon$^{-1}] \lesssim 120$ and $Y_e \gtrsim 0.4$. Indeed, for lower entropy the neutron-to-seed ratio decreases too much and the nucleosynthesis stops at the first $r$-process peak, while for larger entropy the density at NSE freeze-out is too low to allow three-body reactions and most of the $\alpha$ particles do not further interact.

3.3. Ejecta Conditions

We are now in the position to understand in which dynamics and thermodynamics conditions the abundances presented in Figure 1 have been synthesized by convolving the thermodynamic distribution of the ejecta from the simulations with the distribution of abundances computed as a function of the ejecta conditions, as visible in Figure 3. In Figures 5 and 6, we present the normalized, mass weighted histograms as extracted from three of the simulations considered in this work, one for each BNS model. We tested that the overall features discussed below depend neither on the resolution nor on the inclusion of physical viscosity. For each angular bin, the 3D distributions have been marginalized either with respect to $\tau$ (first and third columns) or $Y_e$ (second and forth columns). Since the ejection of matter is usually anisotropic, we consider two representative polar angles, one close to the polar axis (top panels) and one to the equatorial plane (bottom panels), while we integrate along the azimuthal direction. The bulk of the ejecta have low entropy ($s < 40 k_B$ baryon$^{-1}$) and is very neutron-rich, with equatorial ejecta being usually characterized by lower $Y_e$ and lower entropy. However, at both angles a high-entropy tail (with $s > 60 k_B$ baryon$^{-1}$) expanding at high speeds ($\tau \lesssim 5$ ms) is visible. This high-entropy, high-velocity tail in the ejecta is a signature of the so-called shock-heated ejecta, produced by the bouncing remnant. This tail is more important for softer nuclear EOS, producing more violent mergers and stronger shocks. In the case of very different colliding NS masses the properties of the ejecta are qualitatively different. In this case, the dynamical ejecta are mainly produced by the tidal disruption of the lightest NS. Polar ejecta are almost absent and the equatorial ejecta are dominated by low-entropy, low $Y_e$ matter that expand with $\tau \sim 10$ ms. The high-entropy, high-velocity tail in their ejecta distribution is almost absent.

For equal mass mergers, in the case of the softer BLh EOS most of the H and He are efficiently synthesized in the high-$s$, fast expanding tail of the shock-heated component of the dynamical ejecta, while the subdominant He synthesized in low-$s$, low-$Y_e$ conditions roughly traces the less abundant heavy $r$-process element distributions. For the stiffer DD2 EOS, the merger is less violent. The high-$s$ tail of the shock-heated dynamical ejecta is thus less relevant and its contribution to the He production becomes comparable to the low-$s$, low-$Y_e$ contribution. H is still produced, but slightly less efficiently. For the same merger model, the spiral wind ejecta have a pronounced, narrow peak in the velocity-entropy space, around $\tau \approx 8$ ms and $s \approx 20 k_B$ baryon$^{-1}$, and a broad $Y_e$ distribution with a peak around $\gtrsim 0.3$, but extending down to 0.1. Thus, the production of H is suppressed while He is synthesized less efficiently than in the dynamical ejecta and in association with the more abundant lanthanides and actinides. For the unequal mass case, because of the lack of the high-entropy tail, low-$s$, low-$Y_e$ matter is the main source of He, tracing the presence of heavy $r$-process elements, more abundant than He by a few.

Strontium is synthesized in the high-latitude dynamical and in the spiral-wave wind ejecta. In these ejecta, neutrino irradiation plays a fundamental role in increasing $Y_e$ above the production threshold. The larger entropy and $Y_e$ obtained in the case of spiral-wave winds or softer EOS enhance its production by a factor of a few. On the contrary, the equatorial ejecta that characterize very unequal mass merger are efficiently shielded from neutrino irradiation, preventing Sr production.

3.4. Kilonova Spectra

To test whether the H and He synthesized in the early ejecta of BNS mergers can produce features, we compute synthetic kilonova spectra using TARDIS, initialized with the ejecta properties derived in our models. We consider a fiducial ejecta model characterized by $1.5 \times 10^{-3} M_\odot$ of dynamical ejecta and $1.95 \times 10^{-2} M_\odot$ of spiral-wave wind ejecta (obtained by considering $R_{\text{wind}} = 0.15 M_\odot s^{-1}$ acting for $\Delta t_{\text{wind}} = 0.13$ s). The dynamical ejecta expand at an average speed of 0.22$c$, while the spiral-wave wind ejecta at 0.15$c$. We assume that the two ejecta have interacted producing a single homologously expanding profile, which however retains information about the ejecta stratification in the composition (i.e., we assume no large
scale mixing on the kilonova timescale). The expanding ejecta are thus described by the profile Equation (2), where $M$ is the sum of the two ejecta masses and $v_{\text{avg}}$ is obtained by imposing linear momentum conservation, i.e., it is the mass weighted speed. We assume $10^{-6} \, M_\odot$ of H, located at the top head of the ejecta and moving at $\sim 0.33c$. We note that this speed is $\sim 30\%$ lower than the speed of the fast expanding tail of the dynamical ejecta as extracted from our simulations at $\sim 10$ ms after merger. This is a consequence of the adoption of a single profile for the whole ejecta at the kilonova timescale. Since this produces a possibly denser H layer, the following analysis should be intended as an upper limit on the explored effects. We further assume that H is produced in association with heavy elements with a mass fraction of $X_H = 0.5$ (see, e.g., Metzger et al. 2015). Below it, we consider a mixture of $r$-process elements, inside which He is uniformly distributed inside the top part of the ejecta, corresponding to the dynamical ejecta only (i.e., we consider no He in the underlying spiral-wave wind ejecta). For the sake of concreteness, we consider low latitude emission (to which a larger solid angle is associated) and we assume $\kappa = 10 \, \text{cm}^2 \, \text{g}^{-1}$. Based on Equations (3) and (4), we estimate the amount of ejecta (and thus of H and He) in optically thin conditions and the speed of matter at the photosphere. Additionally, we consider representative values of the luminosity at the photosphere, based on time-dependent bolometric luminosity models fitted against AT2017gfo (Smartt et al. 2017), ranging from $1.6 \times 10^{39} \, \text{erg s}^{-1}$ a few hours after merger to $4 \times 10^{41} \, \text{erg s}^{-1}$ at 2–3 days. The set of all these values are considered as baseline values, while we test the robustness of our results both with respect to the H and He masses, and to the bolometric luminosity. The results of our investigation are reported in Table 2.

We first consider the spectra obtained by considering LTE conditions in the ejecta. For all explored configurations, i.e., starting from the baseline models and increasing the H or the He mass, and the photosphere luminosities up to a factor of 20, we do not observe any observable feature in the spectrum at $\sim 5$ and 8 hr, and at 2 and 3 days for H and He, respectively. We choose these times because the range 0.2–3 days is the time interval when we expect the outer H-rich shell to become optically thin. For helium, we investigate 2 and 3 days after merger, since these are the times when we expect $\sim 50\%$ and $\sim 100\%$ of He to be above the photosphere in our models. These results can be understood by considering that for the density and temperature conditions expected during a kilonova and assuming LTE, H, and He recombine to atomic form very rapidly, see Appendix B. Only for slowly expanding ejecta, ionized states are present up to a few hours after the merger. In fact, while a few hours after explosions the ejecta temperature reaches $10^7 \, \text{K}$, already at 0.5 day the temperature drops to $10^5 \, \text{K}$. In these conditions, the small predicted masses of H and He are not expected to produce persistent lines. These results depend very weakly on the specific trajectory.

We explore the possible impact of NLTE excitations by using the analytical approximation for the NLTE He level population developed inside TARDIS for the He-rich ejecta of double detonation type Ia SNe (Boyle et al. 2017). The predicted He line strength changes dramatically with the NLTE treatment. In these explorations, we also test the case of photospheric luminosities lower than the baseline value. While for the fiducial values of He mass and luminosity no clear features can be observed, a larger amount of He can produce a visible broad He I $\lambda 10831$ line. In particular, using our baseline photospheric luminosity at 2 days ($4 \times 10^{41} \, \text{erg s}^{-1}$), an absorption feature becomes visible for $m_{\text{He}} > 8 \times 10^{-5} \, M_\odot$. Lower masses (of the order of $4 \times 10^{-6} \, M_\odot$, comparable with our baseline value) of He can produce the He I $\lambda 10831$ feature for days if the kilonova is fainter than our reference case. For example, at 2 days we obtained the same He I $\lambda 10831$ feature if the luminosity is between $2.7 \times 10^{40}$ and $9.6 \times 10^{40} \, \text{erg s}^{-1}$, while at 3 days if $L = 3.8 \times 10^{40} - 1.5 \times 10^{41} \, \text{erg s}^{-1}$, see Figure 7. These ranges in the photospheric luminosity can be

**Figure 5.** Mass weighted, normalized histograms of the $(Y_e, s, \tau)$ conditions for the dynamical ejecta extracted from the SR, viscous simulation of the BLh_equal model (left four panels), and of the BLh_unequal model (right four panels). For each simulation, we distinguish between the $(Y_e, s)$ (left panel) and $(\tau, s)$ (right panel) planes, and a high (top panel) and a low (bottom panel) latitude angle.
understood since for too high luminosity He is fully ionized and lines are not produced.

We also checked the possible impact of NLTE effects for H. None of the tested baseline configurations including NLTE effects in TARDIS as in Vogl et al. (2019) produce noticeable H lines at optical wavelengths. For the baseline luminosity, at 0.3 days $10^{-3} M_\odot$ of H (thus, 10 times more than predicted by our models) are necessary to produce weak Lyman lines below 1000 Å, Balmer lines are visible only for an even (and probably implausible) larger amount of H, $\gtrsim 10^{-3} M_\odot$, with first hints at $\sim 10^{-4} M_\odot$. The temperatures are initially so high that there is very little neutral hydrogen. A smaller luminosity mitigates this effect, but the H mass required to produce visible Balmer lines is still around $10^{-3} M_\odot$.

4. Discussion

Watson et al. (2019) estimated between 1 and $5 \times 10^{-5} M_\odot$ of Sr to explain the observed spectral feature attributable to the Sr II line in the early spectrum of AT2017gfo. As discussed in great detail in that work, this estimate must be taken with care due to a few simplifications contained inside the underlying kilonova model (for example, the usage of a spherically symmetric model, or of a single photosphere or the lack of possible NLTE effects). However, keeping in mind these important caveats, we can compare our finding with their inferred mass. On the one hand, the amount of Sr produced in the dynamical ejecta of our equal mass models is compatible with the inferred one, even when anisotropic production is taken into account and all Sr is assumed to be transparent within a few days. Indeed, since AT2017gfo was most probably observed from high latitudes ($15^\circ \lesssim \theta \lesssim 30^\circ$) and Sr is mainly produced at those latitudes in the dynamical ejecta, an equivalent spherically symmetric model would require about twice as much total dynamical ejecta ($f_{Sr} \sim 2$ for $\theta \sim 20^\circ$, as visible for example in the top-left panel of Figure 2). On the other hand, in the case of very unequal mass models, Sr is produced in a more isotropic way. The required Sr mass is however significantly larger than the one obtained in the dynamical ejecta of our corresponding simulations. In addition to the dynamical ejecta, for models that do not form quickly a BH, the spiral-wave wind is an efficient mechanism to unbind matter from the disk (Nedora et al. 2019, 2021). For example, assuming an emission rate of $0.15 M_\odot \text{s}^{-1}$, a timescale of $\Delta t_{\text{wind}} \sim 0.13 \text{s}$ would be required to unbind $\sim 0.02 M_\odot$ (this is the amount usually required by kilonova models to explain the blue component of AT2017gfo, see, e.g., Cowperthwaite et al. 2017; Kasen et al. 2017; Perego et al. 2017; Villar et al. 2017; Rosswog et al. 2018; Breschi et al. 2021). Based on the total Sr mass fraction obtained in our models, these ejecta would translate to $4\times8 \times 10^{-4} M_\odot$ of additional Sr. However, the production of Sr is very asymmetric in this wind, and in particular, for a high-latitude viewing angle ($\theta \sim 20^\circ$), the amount of Sr of an equivalent spherically symmetric model should be about 20% of the its actual amount, meaning $8\times16 \times 10^{-5} M_\odot$ of additional Sr in the spiral-wave wind ejecta, as visible in the bottom-right panel of Figure 2. This amount is still larger than the inferred one, but only by a factor of a few. While the many uncertainties in the spectrum calculation and the assumption that all Sr was above the relevant photosphere at the time of interest for the spectrum can possibly weaken this discrepancy, our results may suggest that the timescale over which a spiral-wave wind could have been active in GW170817 remnant should be not significantly larger than 100 ms, otherwise the corresponding ejecta would imply a much larger amount of Sr than the one reported by Watson et al. (2019).

In Figure 7, we also report the 2.5 and 3.5 day spectra of AT2017gfo (Pian et al. 2017) showing a broad absorption at 810 nm that was explained by a blueshifted transition of Sr II (Watson et al. 2019). Interestingly, based on the velocity profile only, this feature could be consistent also with the He 10831 line in the ejecta expanding at 0.25$c$. However, the lower
At early times after merger

Note.

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Table 2
Summary of the Kilonova Spectra Results Obtained Using TARDIS

| Time (days) | \(m_H\) or \(m_\text{He}\) (10^{-6} M_\odot) | \(f_{\text{He}}\) (-) | \(L_{\text{ph}}\) (10^{41} erg s^{-1}) | \(v_{\text{ph}}\) (c) | (N)LTE | Notes | Effects |
|-------------|-----------------|-----------------|-----------------|-----------------|--------|--------|--------|
| 0.2–0.3     | 1.0             | 1.0             | 16              | 0.3             | LTE    | Baseline | None   |
| 0.2–0.3     | 1–20            | 1.0             | 16–320          | 0.3             | LTE    | Sensitivity | None   |
| 0.2–0.3     | 1.0             | 1.0             | 16              | 0.3             | NLTE   | Baseline | None   |
| 0.2–0.3     | 1–20            | 1.0             | 1–320           | 0.3             | NLTE   | Sensitivity | Hα line for \(L_{\text{ph}} \lesssim 2.15\) and \(m_H \gtrsim 10\) |

Helium

| Time (days) | \(m_H\) or \(m_\text{He}\) (10^{-6} M_\odot) | \(f_{\text{He}}\) (-) | \(L_{\text{ph}}\) (10^{41} erg s^{-1}) | \(v_{\text{ph}}\) (c) | (N)LTE | Notes | Effects |
|-------------|-----------------|-----------------|-----------------|-----------------|--------|--------|--------|
| 2           | 4               | 0.52            | 4               | 0.25            | LTE    | Baseline | None   |
| 2           | 4–80            | 0.51            | 4–80            | 0.25            | LTE    | Sensitivity | None   |
| 3           | 4               | 1.0             | 4               | 0.235           | LTE    | Baseline | None   |
| 3           | 4–80            | 1.0             | 4–80            | 0.235           | LTE    | Sensitivity | None   |
| 2           | 4               | 0.52            | 4               | 0.25            | NLTE   | Baseline | None   |
| 2           | 4–80            | 0.51            | 0.2–80          | 0.25            | NLTE   | Sensitivity | He I feature for \(0.27 \lesssim L_{\text{ph}} \lesssim 0.96\) and \(m_\text{He} = 4\) |
| 3           | 4               | 1.0             | 4               | 0.235           | NLTE   | Baseline | None   |
| 3           | 4–80            | 1.0             | 0.2–80          | 0.235           | NLTE   | Sensitivity | He I feature for \(m_\text{He} > 40\) and \(L_{\text{ph}} = 4\) \(\text{He I feature for } 0.48 \lesssim L_{\text{ph}} \lesssim 1.5\) and \(m_\text{He} = 4\) |

Note. At early times after merger (top, 0.2–0.3 days) we consider tiny kilonova atmospheres rich in H, while at later times (bottom, 2–3 days) larger atmospheres with He. For each time, we consider a baseline model characterized by a certain amount of H or He, \(m_H\) and \(m_\text{He}\), a certain transparency factor, \(f_{\text{He}}\), corresponding to the fraction of the element mass outside the photosphere, a photospheric luminosity and velocity, \(L_{\text{ph}}\) and \(v_{\text{ph}}\), respectively. We study the sensitivity of our results with respect to LTE versus NLTE, and with respect to the element masses and photospheric luminosity.

luminosities (with respect to the one deduced by AT2017gfo spectra assuming a distance of \(d_L = 40\) Mpc) required to observe significant NLTE effects seem to disfavor the interpretation of this feature as caused by He rather than Sr. More luminous kilonovae, more compatible with AT2017gfo and closer to our baseline model, require He masses significantly larger than our baseline value (\(\gtrsim 10\)) to produce similar effects. This discrepancy is possibly mitigated by the anisotropy in the ejection of He at polar latitudes, see Figure 2, but only by a factor of \(\sim 2\), if we consider \(\theta \sim 20^\circ\).

In addition to producing H, the decay of free neutrons at the forefront of the dynamical ejecta can power an EM precursor of the kilonova (Metzger et al. 2015). However, the amount of free neutrons available to decay and to power such a precursor (which can be identified with the amount of H in the dynamical ejecta, see Table 1) is between one and two orders of magnitude smaller than the one used by Metzger et al. (2015) and obtained by Just et al. (2015). We stress that neutrino effects were not considered in those simulations, while their impact on the amount of free neutrons is crucial, as visible in our results and as also discussed by Ishii et al. (2018) and George et al. (2020). Indeed, our results agree within a factor of a few with those reported in these latter papers. Since the precursor luminosity is expected to be proportional to the free neutron mass, the predicted magnitude in the UV bands is likely to be more than 3.5 magnitudes smaller than the one suggested in Metzger et al. (2015) even within the first hour after merger (where the peak is expected to occur, as suggested by Ishii et al. 2018). For those conditions, it is unclear if this contribution will be visible or if it will be dominated by the rising kilonova emission.

Dynamical and spiral-wave wind ejecta from BNS mergers are not the only environment where H and He can be synthesized in association with r-process elements. In the case of BH-NS mergers, dynamical ejecta conditions are very similar to the ones observed in very unequal BNS mergers, with possibly larger average expansion velocities (e.g., Just et al. 2015; Fernández et al. 2017; Roberts et al. 2017; Kyutoku et al. 2018). Thus, in this case we expect a significant He production in association with heavy r-process nucleosynthesis, as visible in some of the nucleosynthesis results of the above works. Since H is significantly produced in the high speed tail of the dynamical ejecta and these ejecta are mainly produced in shock-heated conditions, H is expected to be even less abundant in BH–NS mergers. Both in the case of BNS and BH–NS mergers, neutrinos, viscosity, and magnetic processes can drive matter ejection on the viscous timescale expanding at significantly smaller velocity than the dynamical ejecta, \(v_{\infty} \lesssim 0.1c\) (see, e.g., Metzger et al. 2009; Fernández & Metzger 2013; Perego et al. 2014; Metzger & Fernández 2014; Siegel et al. 2014; Martin et al. 2015; Just et al. 2015; Wu et al. 2016; Lippuner et al. 2017; Radice et al. 2018; Fujibayashi et al. 2018; Fernández et al. 2019; Miller et al. 2019). The possible presence of He in these ejecta and their potential spectroscopical relevance was already anticipated by Fernández & Metzger (2013), based on analytical estimates (Hoffman et al. 1997). Detailed numerical simulations (see, e.g., Fernández & Metzger 2013; Just et al. 2015; Fujibayashi et al. 2018) show the possible presence of a significant high-entropy tail in the ejecta distribution, especially close to the polar axis, where the production of He in α-rich freeze-out conditions occurs. This tail is particular prominent in the case of GRMHD simulations (Fernández et al. 2019). For BNS mergers, if the central massive NS survives on a timescale comparable to or larger than the viscous timescale, \(\nu\) irradiation can increase \(\nu_{\alpha}\) even above 0.45, producing efficiently He in α-rich freeze-out conditions. Thus, also these ejecta can host significant He production (Lippuner et al. 2017). We stress,
however, that these slower ejecta are expected to become transparent at later times, when the presence of heavy elements and stratified ejecta can substantially increase the spectrum complexity.

### 5. Conclusions

In this paper, we have analyzed the production of very light elements (between H and K) in the early ejecta expelled by BNS mergers, and we have investigated their detectability in kilonova spectra. In particular we have focused on the nucleosynthesis occurring in the dynamical and spiral-wave wind ejecta obtained by detailed numerical relativity simulations targeted to the GW170817 event, and we have explored their dependence on the mass ratio and nuclear EOS.

We found that H and He can be robustly synthesized in the dynamical ejecta, with a mass fraction ranging between $10^{-3}$ and $10^{-2}$, while their production is negligible in spiral-wave wind ejecta. The total amount of H ranges between $\sim 0.5$ and $2 \times 10^{-5} M_\odot$, while the one of He is between $\sim 2$ and $10 \times 10^{-6} M_\odot$. Hydrogen is mostly produced in the high speed tail of the dynamical ejecta (see, e.g., Just et al. 2015; Ishii et al. 2018) while the production of He can happen both in high-entropy, high-$Y_e$, and in low-entropy, low-$Y_e$ conditions. In the latter case, the presence of He is associated with the production of heavy r-process elements and its amount can increase by a factor of $\sim 2$ during the kilonova timescale, due to $\alpha$ decays. With the exception of the He produced by $\alpha$ decay of very heavy elements, neutron decay is the driving nuclear process behind the nucleosynthesis of both these elements. Indeed, in addition to producing H from unburned free neutrons on timescales comparable to the free neutron lifetime, the early (i.e., within the first second) decay of free neutrons in very neutron-rich environments produces deuterium and tritium that immediately fuse to produce He.

Based on the masses and on the ejecta properties computed in our model, we produced synthetic spectra with TARDIS to test whether dynamical ejecta enriched in H or He can leave an observational signature in the observed kilonova spectrum. Our analysis suggests that no effects are visible if LTE conditions are assumed. NLTE effects are required to produce a significant He I $\lambda 10831$ spectral feature at $t \gtrsim 2$ days after merger, while they do not produce any clear H feature for our fiducial configurations. Then, we further explored the luminosity and mass parameter spaces to define admissible ranges allowing for the He I $\lambda 10831$ spectral feature in the spectrum. Considering the baseline luminosity, a He mass at least one order of magnitude larger than our fiducial value is required to produce a significant feature. However, a lower He mass, comparable to our reference value, could be sufficient to produce an observable feature between 2 and 3 days if the kilonova is fainter than our reference value by one order of magnitude and a factor of a few ($0.27 - 1.5 \times 10^{41}$ erg s$^{-1}$). Significant H features (e.g., Balmer lines) require two or three orders of magnitude more H mass than predicted.

The production of elements between Li and K is negligible in all relevant kinds of ejecta. This very robust feature is due to the presence of $Z = N = 20$ magic nuclear numbers, which prevents seeds nuclei formed in the iron group region to reach elements below calcium. Due to their low abundances, their observational impact in the early spectrum is also negligible.

Besides these very light elements, we investigated the production of strontium in our models, a light r-process element (whose cosmological production is however dominated by the s-process, see, e.g., Prantzos et al. 2020), which has been possibly identified in the spectrum of AT2017gfo.
In agreement with previous findings (see, e.g., Wanajo et al. 2014; Radice et al. 2018; Nedora et al. 2021), we found that Sr is produced both in the dynamical and spiral-wave wind ejecta. In the former case, Sr production happens in the high-$Y_e$ high-latitude ejecta, and its amount ranges between 1 and $5 \times 10^{-5} M_e$ (including our estimates of the uncertainties of numerical origin). In the latter case, a significant amount of Sr is synthesized at all angles due to the relatively large $Y_e$, with a possible exception of the region very close to the equator. Sr production is very efficient and its typical mass fractions (integrated over the whole spiral-wave wind ejecta) are between 1.5% and 4.5%. The amount of Sr in the dynamical ejecta is comparable to the one required to explain the spectral features in AT2017gfo. Since the spiral-wave wind can efficiently produce even more Sr, our results suggest that the central object in GW170817 should have collapsed within $\sim 100$ ms.

Since H and He are often observed in EM transients, our results could be relevant to organize and prioritize future observational campaigns for EM counterparts of GW events during the first days, when dynamical ejecta become transparent and kilonova spectra are still close to blackbody. We remark that in this work we have limited our analysis to very light elements, up to potassium. However, it has been recently shown that calcium, for example, could provide a visible signature in kilonova spectra (Domoto et al. 2021). An extension of this study to elements heavier than potassium will be the subject of a future work. Our results are robustly grounded on state of the art, first-principle simulations of BNS mergers and nucleosynthesis calculations. We have shown that the usage of a finite-temperature, composition-dependent nuclear EOS is key to predict the correct amount of ejecta and its angular distribution. Moreover, the inclusion of weak interactions and neutrino irradiation are essential to correctly model the relative amount of neutrons and protons, and ultimately, to predict detailed nucleosynthesis yields to be compared with observations. Nevertheless, several limitations and weaknesses still affect our results. Our partial knowledge of the nuclear EOS and the still large uncertainties in the modeling of neutrino radiation, in addition to the lack of a robust numerical convergence of the ejecta properties, represent the largest limitation to our capability of predicting with accuracy the properties of the ejecta emerging from a BNS merger. Additionally, our limited knowledge of the relevant atomic opacities and the many uncertainties and approximations still present in the radiative transfer behind kilonova predictions still limit our predictive capacity. Our work underlined also the possible relevance of NLTE effects in shaping kilonova spectra. However, our approach mostly relied on supernova modeling, while NLTE effects in kilonovae have not been studied in details. A strong effort in linking models to observations will be required to fill all these gaps in the years to come.

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**Appendix A**

**Origin of Helium: Fusion versus Decay Reactions**

In this appendix, we quantify the relative importance between charged reactions and $\alpha$ decays, together with their temporal evolution. To do that, we compare $Y_{He}$ at the end of our calculations ($Y_{He(\text{final})}$) with $Y_{He}$ at and after neutron freeze-out. In figure Figure 8, we show $Y_{He(t)}/Y_{He(\text{final})}$ for different times (namely, the neutron freeze-out time, 1 hr, 1 day, and 10 days). In the top and bottom panels we consider subsets of the trajectories we presented in Section 3.1 characterized by $s = 9.0 k_B$ baryon$^{-1}$ and $\tau = 8.6$ ms, respectively. We focus on $Y_e \lesssim 0.2$ since for larger $Y_e$ there are no $\alpha$-decaying nuclei and all He is produced at $n$ freeze-out. For $0.1 \lesssim Y_e \lesssim 0.2$, between $\sim 20\%$ and $\sim 40\%$ of the final He is already produced at neutron freeze-out. For $Y_e < 0.1$ the relative amount tends to increase up to $\sim 70\%$. Since many $\alpha$ decays happen on timescales of several days, $\lesssim 40\%$ ($\lesssim 25\%$) of $Y_{He}$ is produced after the first (10th) day after merger.

**Appendix B**

**Ion Abundances in Kilonova Ejecta Under LTE Conditions**

In this appendix, we present H and He ion abundances under LTE conditions by solving the Saha equation for a mixture of atoms and ions, as predicted by representative tracer particles. In computing the atomic partition functions, we restricted ourselves only to the ground states, while for the ionization energies and spins we considered the publicly available
In practice, for H we consider the full abundances produced by a tracer characterized by $\tau = 1 \text{ ms}$, $s = 100 \text{ kB baryon}^{-1}$, and $Y_e = 0.15$, while for He by $\tau = 10 \text{ ms}$, $s = 10 \text{ kB baryon}^{-1}$, and $Y_e = 0.15$. We calculated the abundances of atomic and ionized H and He over a wide range of matter densities and temperature, namely, $10^{-16} \lesssim \rho [\text{g cm}^{-3}] \lesssim 10^{-8}$ and $100 \lesssim T [\text{K}] \lesssim 5 \times 10^5$. Doubly ionized helium dominates for $T \gtrsim 3 \times 10^4 \text{ K}$, while atomic He for $T \lesssim 10^4 \text{ K}$. We tested the sensitivities of our results to the specific nuclear abundances by changing the entropy by one order of magnitude, without noticing qualitative differences. To explore conditions that are relevant for the kilonova emission, we consider profiles of density and temperature suitable to describe homologously expanding ejecta according to the following relationships:

$$
\rho(t) = \rho_0 \left( \frac{t}{t_0} \right)^{-3} \quad \text{and} \quad T(t) = T_0 \left( \frac{t}{t_0} \right)^{-1}.
$$

While we keep $T_0 = 1 \text{ GK}$, we vary $\rho_0$ and $t_0$ to account for ejecta of different kinds. In particular, we consider $t_0 = 0.02 \text{ s}$ and $\rho_0 = 10^6 \text{ g cm}^{-3}$, for fast and slow expanding ejecta, respectively. As shown in Figure 9, for the density and temperature conditions expected during a kilonova and assuming LTE, H and He recombine to atomic form very rapidly. Only for slowly expanding ejecta, ionized states are present up to a few hours after the merger. In fact, while a few hours after explosions the ejecta temperature reaches $10^5 \text{ K}$, already at 0.5 day the temperature drops to $10^4 \text{ K}$. In these conditions, the small predicted masses of H and He are not expected to produce persistent lines, at least for LTE level.
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