FE Modelling and Analysis of Beam Column Joint Using Reactive Powder Concrete

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Abstract: Reactive powder concrete (RPC) is used in the beam-column joint region in two out of four frames. Finite element modeling of all specimens is developed by using ABAQUS software. Displacement controlled analysis is used rather than load control analysis to obtain the actual response of the structure. The prepared models were verified by using experimental results. The results showed that using RPC in the joint region increased the overall strength of the structure by more than 10%. Moreover, it also helped in controlling the crack width. Furthermore, using RPC in the joint region increased the ductility of the structures. Comparisons were made by varying the size of the mesh and viscosity parameter values. It was found that by increasing the mesh size and viscosity parameter value, analysis time and the number of steps during analysis were reduced. This study provides a new modeling approach using RPC beam-column joint to predict the behavior and response of structures and to improve the shear strength deformation against different structural loading.

Keywords: reactive powder concrete; beam-column joint; FE modeling; crack; concrete

1. Introduction

The beam-column joint is a sensitive and crucial part of a structure, where a failure in it can cause the sudden collapse of a building [1]. It is the most seismically vulnerable component in a structure that is typically designed for gravity loads [2]. Recently, extensive research has been on the behavior of reinforced concrete (RC) beam-column joints brought under monotonic loading [3–5]. It was found that many beam-column joints designed with the concept of strong column weak beam concept undergo severe shear force during a seismic event causing joint failure [6].

Shear failures are brittle and more vulnerable causing the catastrophic collapse of structures. To achieve ductile design, ductile material or appropriate reinforcement should be used to improve shear capacity. The latter technique is mostly done by providing stirrups and ties in beams and columns, respectively, with appropriate spacing for good bonding between concrete and reinforcement [7]. Shear capacity can also be enhanced by following various techniques. De Corte and Boel [8] examined the use of rectangular spiral reinforcement (RSR) by testing RC beams under continuous four-point test and results showed increased shear capacity. Yang, Kim [9] explored the effectiveness of Spiral type wire rope as a shear reinforcement by testing three two-span reinforced concrete T-beams in the four-point test under static loading conditions, and results demonstrated increased...
ductility and controlled crack width. Similarly, Al-Nasra and Asha [10] utilized swimmer bars as transverse reinforcement with three types of connection (weld, bolt, and U-link bolt), and results depicted that it is a convenient method for improving shear strength, ductility, and controlling crack width. Another research by Ghobarah and Said [11] suggested different retrofitting and reinforcing techniques for improving shear resistance of beam-column joints by using concrete jacketing, bolted steel plates, and corrugated steel sheets, etc. [12]. Moreover, Gencoglu and Mobasher [13] concentrated on the use of external steel plates on each side of the column face by bolting it through epoxy bonding and steel angles welded to the plates and the joint region inflated with concrete fillet in a two-way beam column slab system to provide additional strength to structure against different loadings. As the columns were prefabricated, these approaches were extremely beneficial in terms of construction time. All these methods were very effective in enhancing the shear strength of a beam-column joint, but such techniques are neither cost-effective nor time-efficient.

Reactive powder concrete (RPC) exhibiting strain hardening processes can be utilized to improve beam-column joint strength. During the 1990s, ultra high strength performance mortar known as reactive powder concrete was developed having the compressive strength of 200 MPa [14]. The RPC concept was first developed in 1990 by P. Richard and M. Cheyrezy [15]. It was first utilized in 1997 for the construction of the Sherbrooke bridge in Canada [16]. RPC provides many advanced and high strength and ductility properties in comparison to conventional concrete [17]. RPC constituents include cement, sand, silica fumes, quartz powder, superplasticizers, and steel fibers (optional) [18]. The compressive strength of the RPC used in high prestressed bridge girders is more than 200 MPa while its flexural strength is 50 MPa with high workability. Moreover, it possesses strong ductility and energy absorption characteristics [19]. These properties of RPC make it a significant material. Therefore, RPC is widely used in the construction industry for the construction of different structures like prestressed girders, sewer pipes, blast resistance structures, and high-pressure pipes [20]. Experimental investigation on RPC showed significant improvement in the strength, ductility, strain capacity, and energy dissipation of structures. Furthermore, during the uniaxial compression test, RPC sustained a significant amount of load after initial cracking [21]. The presence of silica fumes and fine particles in the material provides pozzolanic characteristics, agitating the hydration reaction and increasing strength [14]. RPC sometimes shows brittle behavior due to its ultra-high strength. This can be mitigated by adding steel fibers. RPC is gaining momentum and recently has been used in a number of construction fields including bridge erection, mining engineering and high-rise buildings [22,23].

RPC can be used for retrofitting structures. Al-Jubory [24] evaluated the bond strength and durability of RPC using as a repairing material. The addition of silica fume and quartz powder to RPC improved temperature resistance and rendered the structure impermeable. Furthermore, employing RPC as a retrofitting material increased the structure’s compressive and flexural strength by more than 12%. It was observed that the abrasion coefficient of RPC was 7.58% more than ordinary concrete. Results indicated no drastic declination for RPC which proved it to be more durable than reinforced concrete.

The experimental study was employed on reinforced RPC (having 1% and 2%) with and without steel fibers. On both of these samples, several strength tests were performed, including compressive strength, tensile strength, and flexural strength. It was discovered that the inclusion of steel fibers increases compressive strength, flexural strength, and split tensile strength by more than 10%. Compressive strength for samples without and with reinforcement was 50–67 MPa and 74.5 MPa, respectively. Low values indicated the presence of higher calcium aluminate content. Experimental results showed that RPC has 250 times greater durability and 200% more compressive strength and 150% more flexural strength than conventional and high strength mortar (HSM). Furthermore, RPC has an abrasion coefficient that is eight times that of normal and four times that of HSM. Freeze and thaw cycles have less effect on RPC which makes it more durable. All these factors lead RPC to be one of the best retrofitting materials [25].
RPC has improved material usage in the concrete industry by providing economic benefits and builds considerably strong, efficient, and durable structures. Experimental research on RPC is conducted by many researchers, however, there is little study on modeling of RPC beam-column joints. This research focused on the numerical modeling of RPC beam-column joint besides experimental work. Numerical modeling provided complete diagnoses about the cause and extent of damage to the structures. Moreover, it is an efficient technique, and it is gaining momentum as it is not only cost-effective but also time efficient. The numerical modeling of the beam-column joint was done using ABAQUS software which is capable of simulating the nonlinear behavior and gives more realistic results in comparison to other software. The experimental results obtained were validated against the numerical results.

2. Experimental Investigation

Four triangular frames as shown in Figure 1 were cast and tested under simple monotonic loading for the determination of tensile strength of beam-column joints. Two out of four frames consisted of conventional concrete. RPC was used in the beam-column joint in the remaining two frames.

![Triangular Frame](image)

**Figure 1.** Triangular frames of 2′ × 2′.

The cross-section and long section details of specimens are shown in Figures 1 and 2. Column and beam dimensions are 4″ × 4″ × 24″ and 4″ × 6″ × 24″, respectively, with a cover of 0.5″ from all sides. All the frames were brought under a monotonic loading machine for testing. During the application of load, roller support was provided to the beam and the column was kept fixed. Sensors were installed both at the joints and the beam ends.

![Column and Beam Section](image)

**Figure 2.** Cross-section and reinforcement detailing of beam and column.
Constituents of RPC are shown in Table 1. RPC mix requires a higher cement quantity as compared to conventional concrete. The quality of cement is also of immense significance in this case [26]. Previous studies have employed high-performance cement with a low sodium oxide and low calcium aluminate content [27–30]. Reinforcement of grade 60 (60 ksi) was used in the specimens. RPC specimens in this study were made with low C3A Portland cement Type V complying with ASTM C150-2. Silica fume was utilized as an auxiliary binder. This was done as RPC requires a pozzolanic substance containing microparticles to reduce small voids in the paste. It also contributed to enhancing the strength and durability properties of the mix as a result of improved dense packing. According to ASTM C 494, a superplasticizer was used to recompense for the decreased water/cement ratio [31]. In the end, quartz mineral was employed to produce high-performance RPC. As the attributes of RPCs not only depend mainly on the order in which the components are inserted into the combination, but also on the speed and length of the process of mixing [32–34]. Approximately 7 min of gradual mixing of dry materials made out of silica fume, Portland cement, and quartz. The superplasticizer was added to water and the whole combination from the superplasticizer with water was added to the components immediately. The blend was then mixed up at around 10 min of progressively escalating speed. Beam column joint for two out of the four frames were left (4 inches for beam and 6 inches for column) for RPC concrete as shown in Figure 3. Joints were cast using RPC concrete monolithically with the conventional concrete as shown in Figure 4. The burlap curing method was adopted. In this method, the triangular specimens were kept under a burlap that was kept wet. Both controlled conventional concrete and RPC specimens were brought under a monotonic loading machine having a capacity of 200 tons as depicted in Figures 5 and 6. In monotonic load testing, the load is steadily escalated at a constant rate, with no reversals from test start to ultimate fracture. Casting and testing of RPC frames are shown in Figures 3–6.

| Ordinary Portland Cement | Silica Fume | Quartz | Fine Aggregate | W/C Ratio | Steel Fibers | Superplasticizers |
|-------------------------|------------|--------|---------------|-----------|--------------|------------------|
| 1                       | 0.25       | 0.4    | 1.1           | 0.17      | 0.03         | 0.015            |

Figure 3. Joint left for RPC.
As seen in Figures 7–10, shear cracking was the primary cause of failure in all the specimens. The distribution of cracks in the RPC sample was distributed uniformly due to the presence of steel fibers. As no coarse aggregates were involved in the case of RPC specimens, beam-column joint resulted in decreased stiffness as discussed in the results.
section of the article. RPC resulted in an increase of 10–15 percent of the tensile strength (the ability of a material to stretch when pulled apart) as compared to controlled conventional concrete samples.

**Figure 7.** Failure of the conventional concrete specimen (CC_S1) after application of load.

**Figure 8.** Failure of the conventional concrete specimen (CC_S2) after application of load.

**Figure 9.** Failure of RPC specimen (RPC_S1) after application of load.
Table 2 shows the values of experimental results. Strength ($f'c$), Elastic modulus ($E_c$), maximum load, and displacement for all the specimens were studied. RPC specimens reached ultimate strength at a later stage and have shown higher $E_c$. Moreover, the load taken by RPC specimens was greater in comparison to controlled concrete specimens.

Table 2. Experimental results.

| Specimens | $f'c$ (MPa) | $E_c$ (MPa) | Max Load in Experimental (N) | Max Displacement Experimental (mm) |
|-----------|-------------|-------------|-------------------------------|-----------------------------------|
| CC_S1     | 21.03       | 27,497.88   | 15,500                        | 35.98                             |
| CC_S2     | 21.03       | 27,497.88   | 13,330                        | 46.28                             |
| RPC_S1    | 45.24       | 37,433.67   | 18,000                        | 40.15                             |
| RPC_S2    | 45.24       | 37,433.67   | 16,020                        | 43.33                             |

3. Modelling

Recently, numerical modeling has been increasingly adopted to simulate the damaging effect of structures. These numerical models can predict the failure events by analysis of nonlinear behavior such as buckling, large displacements, cracking, and inter-surface contacts. Finite element analysis (FEA) model-based software ABAQUS was used to model and to simulate and determine the response of RPC in improving the shear strength deformation of vulnerable beam-column joint. Different parameters for linear and nonlinear analysis were taken from experimental work of shear strength-deformation improvement of vulnerable beam-column connection using RPC.

3.1. Finite Element Modeling of Nonlinear Behavior of Beam-Column Joint

3.1.1. Finite Element Method

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3.1. Finite Element Modeling of Nonlinear Behavior of Beam-Column Joint

3.1.1. Finite Element Method

The finite element method (FEM) is the most widely used in numerical simulation of structures [35]. Finite element models have the potential to solve a wide range of complex problems from elastic linear models for linear elements to highly plastic models for nonlinear and solid elements. FEM is one of the leading methods to simulate all types of structures (timber, steel, concrete, masonry) [36].

3.1.2. Abaqus Software

To perform numerical simulation of beam-column joint using RPC a FEM-based software ABAQUS/CAE was selected, which is general-purpose analysis software having the capability of solving the elastic and inelastic problems of the static and dynamic response of components [37].

ABAQUS/CAE 6.14-1 VERSION was used for modeling and analysis of beam-column joint using RPC.

3.1.3. Concrete Damage Plasticity Model

The concrete damage plasticity (CDP) model was selected as it has the capability and potential for modeling reinforced concrete and other quasi-brittle material for different types of structure. CDP model can define the nonlinear behavior of the RPC beam-column joint. Additionally, it takes into account the isotropic damage elasticity concepts with isotropic tensile and compressive plasticity. It also considers the degradation of elastic stiffness produced by plastic straining both in compression and tension [38]. The CDP model can show damage characteristics of a material. The main failure mechanism that this model assumes is the tensile cracking and the compressive crushing [39].

Different parameters required in the CDP model were studied and selected based on available literature both for conventional as well RPC specimens. The dilation angle for the model was taken as $36^\circ$. It is the angle obtained due to a change in volumetric strain produced due to plastic shearing. It depends on the angle of internal friction. Dilation angle controls the amount of plastic volumetric strain produced due to plastic shearing. Normally dilation angle is taken between $30^\circ$ and $40^\circ$ for concrete to avoid large variation between experimental work and numerical modeling. For the seismic design of reinforced concrete, the value of dilation angle is normally between $35^\circ$ to $38^\circ$ [40]. Moreover, eccentricity is the deviation from the center. The default value for eccentricity was taken, i.e., 0.1. If the value
is increased by 0.1 the curvature of flow potential is increased. If the value is decreased from the default value, the convergence problem may occur if confinement pressure is not high enough. Furthermore, the ratio of biaxial loading \( f_b \) to uniaxial loading \( f_{c0} \) is normally taken as 1 or greater than 1. In this case default value was taken i.e., \( f_b / f_{c0} = 1.16 \). K is the shape factor and default value for K = 0.667 [41]. The viscosity parameter shows the amount of flow potential in a material. A lower viscosity parameter value is better as higher values result in a high force of reaction. Therefore, the viscosity parameter, in this case, was taken as 0.001 [42].

### 3.2. Compressive and Tensile Behavior Determination by Using Eurocode

Compressive behavior and tensile behavior of both normal concrete and RPC were determined by using EN 1992 Eurocode 2: Design of concrete structures part 1–1 [43]. It describes different principles and requirements for the safety, serviceability, and durability of concrete structures with specific provisions of buildings. Eurocode 2 applies to the design of civil engineering works such as buildings, roads, bridges, etc. It is applied to plain, reinforced, and prestressed concretes. It complies with the specifications and requirements given in EN 1992-1-1 about safety, serviceability of the structures, the basis of their design, and verification of structures given in EN 1990; basis of structural design [38]. Compressive and tensile stress-strain curves are shown in Figures 11 and 12, respectively. The limitation of the Eurocode 2 for concrete structures is that it is concerned only with the requirements for resistance, safety, serviceability, durability, and fire resistance of the structures. Moreover, it does not consider the other requirements like thermal or sound insulation, etc. [38].

![Figure 11](image1.png)

**Figure 11.** Stress-strain diagram for analysis of concrete using Eurocode 2 [43].

![Figure 12](image2.png)

**Figure 12.** Tensile stress-strain curve of concrete from Eurocode [43].
3.2.1. Compressive Behavior

The compressive behavior of concrete was calculated by using the relations of Eurocode [43] given in Equation (1).

\[ E_{cm} = 22(0.1f_{cm})^{0.3} \]  

where:
- \( f_{cm} \) (MPa) is the compressive strength
- \( E_{cm} \) (GPa) is the modulus of elasticity

Other values showing the position of characteristics points are strain \( \varepsilon_{c1} \) at average compressive strength and ultimate strain \( \varepsilon_{cu} \) at 0.

\[ \varepsilon_{c1} = 0.7(f_{cm})^{0.31} \]  
\[ \varepsilon_{cu} = 0.35\% \]  

where:
- \( \varepsilon_{c1} \) is the strain at peak stress
- \( \varepsilon_{cu} \) is the ultimate strain at which concrete fails

Equations (2) and (3) are only pertinent to concrete having a cylindrical compressive strength of 50 MPa and cube compressive strength of 60 MPa at the most. On the basis of a list of the experimental results, Kmiecik and Kamiński [44] proposed the quite accurate approximating Equations (4) and (5):

\[ \varepsilon_{c1} = 0.0014[2 - \exp(-0.024f_{cm}) - \exp(0.140f_{cm})] \]  
\[ \varepsilon_{cu} = 0.004 - 0.0011[1 - \exp(-0.0215f_{cm})] \]  

Knowing the values of the output in Equations (4) and (5) one can determine the points at which the graphs intersect. Compressive stress values can be determined at any point using these relations [43].

According to Eurocode EN 1992-1-1

\[ \sigma_c = f_{cm}(k\eta - \eta^2)/(1 + (k - 2)\eta) \]  

where:

\[ k = 1.05 \times E_{cm} \left( \frac{\varepsilon_{c1}}{f_{cm}} \right) \]  

and:

\[ \eta = \frac{\varepsilon_c}{\varepsilon_{c1}} \]  

3.2.2. Tensile Behaviors

The tensile behavior of concrete was calculated by using the Equations (9)–(12).

If \( \varepsilon_t \leq \varepsilon_{cr} \)

\[ \sigma_t = E_c \times \varepsilon_t \]  

and if \( \varepsilon_t > \varepsilon_{cr} \)

\[ \sigma_t = f_{cm}(\frac{\varepsilon_{cr}}{\varepsilon_t})^{0.4} \]  
\[ f_t = 0.33 \times f_{c}^{0.5} \]  
\[ f_{tr} = 0.30f_{ck}^{2/3} \]  

For the determination of the complete stress-strain curve for compressive behavior and the tensile behavior of normal concrete and RPC, Eurocode has been used which is capable of determining the actual response of structures closer to the experimental setup. As RPC is a composite material and there is no official code for RPC developed yet, therefore small
modifications based on literature have been made in normal concrete formulas for the determination of stress-strain curves of RPC.

Simple modifications were incorporated into the Equations (1), (3), and (12). These equations were utilized in assigning material properties during numerical modeling in ABAQUS to obtain more realistic results of RPC concrete. Modified equations are shown in Equations (13)–(15).

\[
E_{cm} = 22(0.13f_{cm})^{0.3} \\
\epsilon_{cu} = 0.40\% \\
f_t = 0.40 \times f_c^{0.5}
\]

3.3. Steps and Boundary Conditions

After the completion of assembly, a step was formed. In steps, a time period was provided for which the load is applied to the assembly. The load was then applied to the designated location according to the magnitude of the sample and boundary conditions were applied according to experimental work in which two specimens (CC_S1 and RPC_S1) have hinge boundary condition, i.e., \((U_1 = U_2 = UR_3 = 0)\) while the other two specimens have fixed boundary condition \((U_1 = U_2 = U_3 = UR_1 = UR_2 = UR_3 = 0)\) at column end while roller support \((U_1 = UR_2 = UR_3 = 0)\) at the beam end in all specimens. “U” refers to translatory motion while “UR” refers to rotation of the support. Both the boundary conditions for the column were studied and their effect on the strength and load values were observed.

3.4. Meshing

Meshing is the process of dividing the whole finite element model into a smaller number of chunks by the formation of different nodes at different points. Meshing is an important process as it allows us to apply load and find displacement or any other desired result at any point in the model. The greater the size of the mesh, the smaller will be the number of iterations taken to analyze the whole model and vice versa. In a greater size mesh, a lesser number of nodes are formed, hence the number of iterations and time of analysis is reduced. In our case, the size of the mesh taken was 25 mm, 40 mm, and 50 mm. Independent types of meshing for concrete and steel are selected in Figures 13–15 [42].

![Figure 13. Meshing of 25 mm size for concrete.](image)
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Figure 13. Meshing of 25 mm size for concrete.

Figure 14. Meshing of steel embedded in concrete.

Figure 15. Typical view of Abaqus model of reinforcement.

3.5. Load

A series of analysis was performed on conventional concrete controlled specimens and RPC specimens to simulate and predict the actual response of linear and nonlinear behavior on beam-column joint and to show the behavior of RPC in improving the shear strength deformation against different structural loading. A monotonic load of 0 to 20 kN was applied at the top of the exterior joint for all specimens till the specimens reached the ultimate value. After the application of load, step was created for static analysis. Time period and increment values were given to all specimens. Figures 16 and 17 show the analysis of RPC samples with fixed and hinge boundary conditions, respectively. As seen in Figure 16, a small amount of buckling was observed when the column boundary condition was kept fixed, whereas no buckling was observed in the case of hinge column conditions as seen in Figure 17.
Figure 15. Typical view of Abaqus model of reinforcement.

3.5.Load-Displacement Curve

A series of analysis was performed on conventional concrete controlled specimens experimental results of shear strength-deformation improvement for vulnerable beam-column connection using RPC were used to validate the developed FEM approach. Different parameters from experimental work were used in numerical modeling. This approach provided a more realistic response simulation of the actual beam-column joint. The numerical results were compared with experimental results for the verification of the model as shown in Table 3. There was a negligible deviation of numerical results from experimental results for controlled concrete samples in case of maximum loads. It was 1.13% and 0.63% for CC_S1 and CC_S2, respectively. For RPC samples, the divergence was comparatively higher. It was 6.05% for RPC_S1 and 6.73% for RPC_S2. Maximum displacement variation was 7.06%, 4.18%, 3.12%, and 6.54% for CC_S1, CC_S2, RPC_S1, and RPC_S2, respectively. The maximum variation observed was 7.06% for CC_S1 for displacement. This shows that numerical results were in strong agreement with the experimental results.

Table 3. Comparison of load and displacement between experimental and modeling.

| Specimens | f'c (MPa) | Ec (MPa) | Max Load in Experimental (N) | Max Load in Modeling (N) | Max Displacement Experimental (mm) | Max Displacement Modeling (mm) | Difference b/w Modeling and Experimental Max Values (mm) |
|-----------|-----------|---------|-------------------------------|--------------------------|-----------------------------------|-------------------------------|--------------------------------------------------------|
| CC_S1     | 21.03     | 27,497.88 | 15,500                       | 15,675.21                | 35.98                             | 33.44                         | 2.54                                                   |
| CC_S2     | 21.03     | 27,497.88 | 13,330                       | 13,413.50                | 46.28                             | 48.21                         | 1.93                                                   |
| RPC_S1    | 45.24     | 37,433.67 | 18,000                       | 19,090.02                | 40.15                             | 38.89                         | 1.25                                                   |
| RPC_S2    | 45.24     | 37,433.67 | 16,020                       | 17,097.80                | 43.33                             | 40.50                         | 2.83                                                   |

Figure 16. Analysis of RPC with fixed column boundary condition.

Figure 17. Analysis of concrete with hinge column boundary condition.

4. Results and Discussion

Experimental results of shear strength-deformation improvement for vulnerable beam-column connection using RPC were used to validate the developed FEM approach. Different parameters from experimental work were used in numerical modeling. This approach provided a more realistic response simulation of the actual beam-column joint. The numerical results were compared with experimental results for the verification of the model as shown in Table 3. There was a negligible deviation of numerical results from experimental results for controlled concrete samples in case of maximum loads. It was 1.13% and 0.63% for CC_S1 and CC_S2, respectively. For RPC samples, the divergence was comparatively higher. It was 6.05% for RPC_S1 and 6.73% for RPC_S2. Maximum displacement variation was 7.06%, 4.18%, 3.12%, and 6.54% for CC_S1, CC_S2, RPC_S1, and RPC_S2, respectively. The maximum variation observed was 7.06% for CC_S1 for displacement. This shows that numerical results were in strong agreement with the experimental results.
4.1. Load Displacement Curve

4.1.1. Conventional Concrete Controlled Specimens

The comparison of the load-displacement curve obtained from experimental and ABAQUS simulations are shown in Figures 18–21. The shape of the ABAQUS simulations curves is quite close to the experimental curves. The maximum average discrepancy between modeling and experimental results of conventional concrete was 3–7%. Almost linear behavior was obtained using ABAQUS modeling for CC_S1 whereas in experimental work the pattern of the graph showed nonlinearity which might be due to non-uniform increment of load in the experimental setup.

Figure 18. Displacement at beam end (roller support) with a hinge boundary condition at column end for CC_S1 (mesh size 25 mm).

4.1.2. RPC Specimens

The maximum discrepancy between modeling and experimental results of RPC in the case of RPC_S1 was 6.05% while that of RPC_S2 was 6.7%. The deviation of experimental results from modeling in RPC_S1 was due to non-uniform increment of load and time period in the experimental setup while RPC_S2 showed quite accurate results. Mesh size effect was studied for RPC specimens and compared with the experimental results Figures 22 and 23. Mesh size 25 was considered for RPC_S1 and mesh size 40 for RPC_S2 for comparison with the experimental values.

Figure 19. Displacement at beam end (roller support) with a fixed boundary condition at column end for CC_S2 (mesh size 25 mm).
4.2. Comparison between Conventional Concrete and RPC Specimens

Comparison between conventional concrete and RPC specimen is shown in Figures 22 and 23. RPC specimens took 10–15% more load as compared to conventional concrete-controlled specimens. Delayed peaks were obtained for RPC specimens which shows delayed damaging effect in the samples.
4.3. Stiffness of Concrete and RPC Specimens

For the validation of the model, the stiffness of all specimens was calculated. It can be seen from Tables 4 and 5 that the initial stiffness in the RPC specimens is low in comparison to conventional concrete. Moreover, it can be observed that as the load increased the structure lost its rigidity and stiffness (the ability of a structure to resist deformation when subjected to the applied force). However, after 20% of loading RPC was still taking more load in comparison to conventional concrete as shown in Tables 4 and 5. It can also be observed from Figures 24–26 that the initial stiffness of RPC specimens is low compared to controlled concrete specimens. Figures 25 and 26 depict that as the load was increased to 25% and 50% of the ultimate load, RPC showed to have high stiffness comparatively.
Table 4. Stiffness of all specimens from experimental work.

| Specimens |
|-----------|
| CC_S1 |
| CC_S2 |
| RPC_S1 |
| RPC_S2 |

| Specimens | Stiffness (kN/mm) | Stiffness (kN/mm) | Stiffness (kN/mm) | Stiffness (kN/mm) |
|-----------|------------------|------------------|------------------|------------------|
| CC_S1     | 21.36            | 19.18            | 14.66            | 14.19            |
| CC_S2     | 2.24             | 3.23             | 4.59             | 4.38             |
| RPC_S1    | 1.48             | 1.96             | 2.53             | 2.43             |
| RPC_S2    |                  |                  |                  |                  |

Table 5. Stiffness of all specimens at different loading rates (numerically).

| Specimens |
|-----------|
| CC_S1 |
| CC_S2 |
| RPC_S1 |
| RPC_S2 |

| Specimens | Stiffness (kN/mm) | Stiffness (kN/mm) | Stiffness (kN/mm) | Stiffness (kN/mm) |
|-----------|------------------|------------------|------------------|------------------|
| CC_S1     | 18.561           | 20.82            | 15.76            | 15.98            |
| CC_S2     | 12.67            | 17.49            | 12.23            | 12.76            |
| RPC_S1    | 5.42             | 7.18             | 8.88             | 8.48             |
| RPC_S2    | 3.45             | 4.31             | 5.44             | 5.73             |
| CC_S1     | 2.50             | 3.06             | 4.11             | 4.03             |
| CC_S2     | 1.99             | 2.38             | 3.10             | 2.88             |
| RPC_S1    | 1.42             | 1.34             | 1.98             | 1.56             |
| RPC_S2    | 1.09             | 0.97             | 1.03             | 1.29             |
| CC_S1     | 0.88             | 0.76             | 0.85             | 0.81             |
| CC_S2     |                  |                  |                  |                  |

Figure 24. Initial stiffness of all specimens at 5% of ultimate loading.
4.4. Ductility of Concrete and RPC Specimens

The ductility displacement factor (R), as depicted in Figure 27, according to the Committee Euro International Du Beton, 1996, is defined as the ratio between failure displacement and yield displacement. The yield displacement is the lateral displacement at 80% of the ultimate load at ascending part of the curve while the failure displacement is the lateral displacement at 80% of the ultimate load at descending part of the curve [26]. Ductility factor R and ductility displacement (DD) can be obtained from Equations (16) and (17), respectively.

\[
R = \frac{\Delta f}{\Delta y} \tag{16}
\]

where \( \Delta f \) = failure displacement \( \Delta y \) = yield displacement

\[
DD = \frac{\Delta i}{\Delta y} \tag{17}
\]

where \( \Delta i \) = maximum displacement in any cycle \( \Delta y \) = yield displacement

![Figure 25](image1.png)

Figure 25. Stiffness of all specimens at 25% of ultimate loading.

![Figure 26](image2.png)

Figure 26. Stiffness of all specimens at 50% of ultimate loading.
Table 6 displays ductility factor R and displacement ductility (DD) for all the specimens both for experimental and numerical modeling. Experimental results showed an increase of 27% and 11% in R for S1 and S2, respectively. Similarly, DD for RPC was enhanced by 29% and 12% for S1 and S2, respectively. The same trend was shown by numerical modeling results.

Table 6. Ductility factor and ductility displacement.

| Sample | Experimental | Modeling |
|--------|--------------|----------|
|        | Ductility Factor (R) | Displacement Ductility (DD) | Ductility Factor (R) | Displacement Ductility (DD) |
| CC_S1  | 4.91         | 4.78     | 4.671       | 4.699         |
| CC_S2  | 5.56         | 5.71     | 5.18        | 5.33          |
| RPC_S1 | 6.257        | 6.19     | 6.03        | 6.153         |
| RPC_S2 | 6.2          | 6.39     | 5.98        | 6.13          |

5. Conclusions

A series of analysis were performed on conventional concrete and RPC beam-column joint specimens. Following conclusions were made based on experimental and numerical testing.

1. The use of RPC only in the joint region increased the overall strength of the structure by 10–15% and also delayed the crack propagations.
2. The maximum average discrepancy between modeling and experimental results of conventional concrete and RPC was 3–7%. This discrepancy was due to the non-uniform increment of load and time period in the experimental setup.
3. It was observed that with an increment in the mesh size, a reduction in the number of analysis increments occurred. This caused variation of modeling results from experimental results. Therefore, finer mesh size is recommended.
4. Increasing the value of viscosity reduced the analysis time but produced more errors in results. The lower value of the viscosity parameter is better as higher values cause a high peak of reaction force. Therefore, smaller values are preferable i.e., 0.001, 0.002, 0.003, or 0.005 etc.
5. Fixed column end conditions caused an increase in column stresses which resulted in buckling of column. No buckling was observed for hinged column conditions. Maximum deformation was observed at the beam end irrespective of the column end conditions.
6. To obtain actual results, displacement control analysis should be used rather than load control analysis. With displacement control analysis it is easier to obtain the converged solutions in ABAQUS in case of highly nonlinear problems.

6. Recommendations

Based on this research following recommendations can be used for future research work.

In the case of RPC, a decrease in the initial stiffness of the specimen was observed in the joint region as coarse aggregates were not used. Therefore, the use of suitable size of coarse aggregate will not only increase the initial stiffness but also increase the strength of the structure.

Steel fibers of a longer length should be used so that they can help in controlling the crack from widening. In the case of RPC, shear cracking was observed in the joint region. Combining the RPC technique with some other technique will convert the failure mechanism from the joint to the beam through their combined effect.

Besides the CDP model smeared crack modeling and brittle concrete modeling of the RPC can be used to determine the complex behavior of RPC in structure.

As there is no official Eurocode for RPC. Therefore, the development of Eurocode for RPC with and without steel fibers will enable us to clearly understand the complicated behavior of the material.

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