On the alleged duality of the Galactic halo

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ABSTRACT

We examine the kinematics of the Galactic halo based on SDSS/SEGUE data by Carollo et al. (2007, 2010). We find that their claims of a counter-rotating halo are the result of substantial biases in distance estimates (of order 50%): the claimed retrograde component, which makes up only a tiny fraction of the entire sample, prone to contaminations, is identified as the tail of distance overestimates. The strong overestimates also result in a lift in the vertical velocity component, which explains the large altitudes those objects were claimed to reach. Errors are worst for the lowest metallicity stars, which explains the metal-poor nature of the artificial component. We also argue that measurement errors were not properly accounted for and that the use of Gaussian fitting on intrinsically non-Gaussian Galactic components invokes the identification of components that are distorted or even artificial. Our evaluation of the data leads to a revision of the estimated velocity ellipsoids and does not yield any reliable evidence for a counterrotating halo component. If a distinct counterrotating halo component exists it must be far weaker than claimed by Carollo et al. Finally we note that their revised analysis presented in Beers et al. (2011) does not alleviate our main concerns.

Key words: galaxies: haloes - stars: distances - Galaxy: solar neighbourhood - Galaxy: halo - Galaxy: kinematics and dynamics - Galaxy: structure

1 INTRODUCTION

Galactic haloes are an excellent testbed for cosmology and galactic dynamics. Their exploration can constrain the early assembly of galaxies as well as the dynamics of accretion of smaller galaxies. Our Milky Way offers an ideal case for those investigations, as we can directly obtain the detailed parameters like kinematics, elemental abundances and physical properties of single stars surrounding us. New material is still being accreted into the Galactic halo, as the numerous streams and newly discovered dwarf galaxies confirm (see e.g. Ibata et al. [1995], Klement et al. [2006], Belokurov et al. [2007]). As metallicity gradients go in lockstep with star formation, young accreted objects may be more metal-poor than old stars from the inner Galaxy and thus metallicity can not be simply used as a cosmic clock. This would also make it plausible that a later accreted halo component could indeed be on average younger and more metal poor than the older parts. The formation of at least parts of the halo by accretion (combined with later adiabatic contraction) could give rise to difficulties between early more turbulent accretion/collapse processes and later accretion, which might leave an imprint in differences between the inner and outer halo (see e.g. Cooper et al. [2010]). Another possible source of discrepancies between inner and outer halo is dynamical friction, which could be more efficient for prograde than for retrograde infall (Quinn & Goodman [1986], Byrd et al. [1986]). This could give rise to a different rotational signature for accreted material in the outer Galactic halo compared to the inner regions (Murante et al. 2010).

Historically (and as well today), halo stars have been extremely difficult to identify, particularly in local samples, e.g. demonstrated by the historic argument between Oort and Strömgren (Oort [1926], Strömgren [1927]). Like it is practically impossible to get a clean selection into thin and thick Galactic disc based on kinematics (Schönrich & Binney [2009]), we face the analogous problem between thick disc and the prograde stars of the halo. Wrong assumptions about the kinematics of the Galactic disc will thus affect results on the halo component. Soon after the existence of the Galactic halo was established (Schwarzschild [1952], Eggen et al. [1962]), the central question was raised if the stars of the inner and the outer halo had the same properties or if gradients or even breaks in metallicities or kinematics existed with galactocentric radius. Two main strategies to identify and examine halo stars have been used in the past: either stars in the solar neighbourhood are studied, classified according to their kinematics and then conclusions about the structure further away are drawn by extrapolation (e.g. Sommer-Larsen & Zhen [1990]), or the surveys concentrate on bright objects in the outer halo regions, such as RR Lyrae variables or globular clusters (e.g. Sandage [1970]). The second alternative allows to directly map the spatial structure by those standard candles with good distance information (e.g. Saha [1985]). This
strategy implies selection biases: for example the position and presence of RR Lyrae stars on the horizontal branch are correlated with metallicity and age, while it is not known if the formation of globular clusters is representative also for all halo field stars.

Claims of differences between the inner and outer Galactic halo are almost as old as the discovery of the halo itself. After van den Bergh (1967) discussed differences in metallicity and the second parameter between the haloes of the Milky Way and those of its neighbouring galaxies (M31, M33), Searle & Zinn (1978) found that Galactic clusters in the outer regions showed a larger scatter in the ratio of blue to red horizontal branch stars than inner halo globular clusters, which they interpreted as a signature of an age spread.

Preston et al. (1991) found a similar difference in field BHB stars. Differences in kinematics have also been suggested between inner and outer halo globular clusters (Zinn 1993), although precision and reliability of estimates in this respect are limited by the small number of available globular clusters. Various claims of an asymmetry in the halo azimuthal velocity distribution with an extended tail to retrograde orbits have been made (e.g. Norris & Ryan 1989, Majewski 1992) even found the entire halo to be on average counter-rotating. However, not find any significant velocity gradient. Ryan (1992) pointed out that measurements of kinematics based on proper motions were particularly vulnerable to distance errors and showed that overestimated distances for halo stars can lead to false identifications of counter-rotating stars.

In this paper we will revisit the recent claim by Carollo et al. (2007) (hereafter C07) and Carollo et al. (2010) (hereafter C10) that the Galactic halo consists of two components: a more metal-poor counterrotating component with larger scaleheights, distinct from a slightly prgorade component and stars dominating the halo at high altitudes in their analysis. In particular we will carefully re-examine their distance estimation procedures: we will focus on C10 as this paper deviates from its precursor mostly by the larger sample size. To avoid relying on any of the uncertain available distance calibrations, we apply in parallel both the C10 distances and two native SDSS main sequence distance calibrations, checking results additionally with an isochrone method. In Section 2 we outline those methods, discuss the SDSS/SEGUE data used for this purpose and describe how the sample cleaning was performed.

Thereafter (Section 3) we discuss the underlying assumptions and the reliability of gravity estimates used to sort stars into different sequences as well as the actual assumptions for absolute magnitudes by C07 and C10. We will show that their claim to have distances precise to 10−20% is unsupported and that the C10 sample contains a class of stars with significant distance overestimates by being sorted into unphysical positions in the HR diagram. In Section 4 we present statistical proofs of distance biases in the sample and in Section 5 we discuss the implications of different distance schemes on kinematics and the inner-outer halo dissection.

2 THE CALIBRATION SAMPLE OF SDSS AND THE CAROLLO DATASET

All the data used in this paper come from the Sloan Digital Sky Survey (SDSS, York et al. 2000), and consist of spectroscopic observations of stars from both SDSS-I and II and from the SDSS-III/SEGUE survey (Yanny et al. 2009). Stellar parameters for the stars were estimated using the SEGUE Stellar Parameters Pipeline (SSPP, Lee et al. 2008, Allende Prieto et al. 2008).

For this study we use the calibration star sample from SDSS public data release 7 (DR7) 1 As the colour transformations and distances used in C07 and C10 are not part of the public data releases, we draw this information from the sample used by C10, which is a cleaned version of DR7 and which was kindly provided on our request.

The calibration star sample comprises two datasets, namely the photometric calibration star sample and the reddening calibration star sample. Querying the DR7 catalogue for these stars produces a total of 42841 entries, but many refer to identical objects, so that the actual number of unique objects in the database is 33023. The interested reader is referred to the Appendix where we describe how the cleaning of the sample from questionable objects has been performed that cuts down the sample to 28844 stars.

Throughout the paper we make use of two different classes of distance determinations (see Appendix for details): On the one hand the distances used by C07 and C10 and on the other hand two derivations adopted from Ivezic et al. (2008). When using the distances by C07 and C10 we examine the effects of their different sequences by both using their entire sample ("Carollo all") and using exclusively their dwarf stars ("Carollo dwarfs"). For the native SDSS calibrations we restrict ourselves to the dwarf stars, imposing in general a gravity limit of log(g) > 4.1 to reduce the impact of giant and subgiant contamination. We there use two different schemes: An adopted main sequence derivation, where we increase distances defined via their Eq. (A2) and (A3) by accounting for alpha enhancement and additionally decreasing the adopted absolute magnitudes of all stars by 0.1 mag, hereafter termed the adopted main sequence calibration, short "IvzMS". Second the calibration favoured by Ivezic et al. (2008) using Eq. (A7) from their appendix, which is steepened towards the isochrones in order to account for age dependent effects, hereafter called the age dependent calibration (short: "IvzA7"). We would like to point out that we believe neither distance calibration to deliver the full truth, yet they are currently the most commonly used schemes and can give hints on the intrinsic uncertainties of all methods. To have an additional test we cross-checked and confirmed our findings with distances derived directly from using 12.5 Gyr BASTI isochrones (Pietrinferni et al. 2004, 2006; some details are provided in the Appendix). C10 applied two different geometric cuts. The first was a distance cut at an estimated distance of 4 kpc, limiting the errors on velocities caused by proper motion errors. The second was a cut that removed stars differing from the Sun by more than 1.5 kpc in galactocentric radius (i.e. outside 7.0 kpc ≤ R⊙ ≤ 10 kpc with

1 While it is clear that age is one parameter which will cause an older globular cluster to be bluer than a younger one at the same metallicity, whether this is the dominant cause of differences in horizontal branch morphology is still debated (see, for example, Dotter et al. 2010a and Vandenberg 2004, for opposing views.)

2 This dominance of a retrograde component in the outer halo has recently been contested by Deason et al. (2010) although they find a retrograde motion for metal-poor (Fe/H) < −2) and prograde (Fe/H > −2) for metal-rich stars using a HBH sample in the outer Galactic halo. In our view, this issue needs to be further investigated, as they assume constant g band magnitudes for the horizontal branch in a region affected by the blue tail, which spans of order 2 mag in g band luminosity. If a considerable fraction of the halo giants is in the blue tail, their colour and temperature cuts remove a large part of this tail, but still leave HBH members spanning ~ 0.7 magnitudes, as we tested it on SDSS photometry of metal-poor globular clusters known to have such a strong blue tail (M3, M13, M15 and M92) and the BASTI isochrones.

3 http://casjobs.sdss.org/dr7/en/
their value of $R_{\odot} = 8.5$ kpc for the Sun). The latter cut was reasoned from C10 by the use of their applied orbit model, which was adopted from Chiba & Beers (2000) using a St"ackel-type potential from Sommer-Larsen & Zhen (1990). As we do not make use of this orbit calculation, in this work we do not apply the second cut, which removes of order one third of the available stars.

Due to the magnitude ranges in the SEGUE survey the distance cuts imposed by C10 and C07 remove almost all giants from the sample, a minor fraction of subgiants and very few dwarf stars. The effects of both selections depend strongly on the adopted distances and thus the absolute magnitudes of the stars. Applying the C10 distances to the sample, 21600 stars remain within the distance limit of 4 kpc, of which 14763 have surface gravities log($g$) > 8, 0.8, 0.5 and 0.3 (outermost lenses, light blue), contours of the angle term $\eta_\alpha$ in Eq. 7 that quantifies the relative support by the direct line-of-sight velocity measurements. This demonstrates the vulnerability of $V$ velocities in this sample to distance errors as they cannot be found directly from line of sight velocities.

Metallicities are taken from the DR7 pipeline adopted values (Lee et al. 2008a,b). For a discussion of the different metallicity scales of DR7 and C10 the reader is referred to the Appendix. There we also describe in more detail how kinematics are derived from distances, radial velocities and proper motions.

3 ASSESSING THE DISTANCE CALIBRATIONS

The core assumptions in C10 are those about stellar distances. They claim that by using the log($g$) estimates from the SEGUE stellar parameter pipeline stars can be reliably sorted into clean sequences, i.e. main sequence, turn-off and subgiant/giant. The attraction of this idea, laid out in Beers et al. (2000), is that it seems to reduce the distance errors to simple uncertainties in colour and metallicity on well-determined sequences. However, as we will see below, things are more complicated.

3.1 Effects of distance errors

Selecting a star into the wrong position in the colour-magnitude diagram results in a faulty estimate of its absolute magnitude and thus an erroneous distance. As they are the most common population we would naively expect the largest contamination to be main sequence stars mistakenly addressed as turn-off stars. These will be assumed to be far brighter than they are, hence their distance will be overestimated, bringing many of them, especially halo stars, falsely into the retrograde tail of the velocity distribution. This effect happens via the translation of proper motions into velocities and thus prevails for samples that have low support by radial velocities (cf. Section 8 of the Appendix). Fig. 1 depicts the locations of stars (red dots) in Galactic longitude (x-axis) and latitude (y-axis). The SDSS/SEGUE sample is (due to the location of the telescope in the northern hemisphere and the strategy to avoid the high extinction in the Galactic plane) largely concentrated away from the plane and towards the Galactic North Pole. Consequently it has almost no points at directions that would have high support of azimuthal velocities by the direct line-of-sight velocity measurements. The contours in the plot encircle the regions of high line-of-sight velocity support of $V_\alpha$ in the sky. Within the ellipses, the fraction $\eta_\alpha$ (Eq. 7 in the Appendix) of the line-of-sight velocity going into the heliocentric azimuthal velocity $V_\alpha$ is larger than 0.95 (smallest lenses), 0.8, 0.5 and 0.3 (largest lenses). They demonstrate how heavily any analysis of the azimuthal velocities has to rely on the transverse velocity component and thus proper motions and distance estimates.

The effect of distance errors in this process is easily understood: Think of driving a car past a field that has a rabbit sitting on it. As the speed of the car is known, the fact that the rabbit rests on the lawn can be derived by the car driver from its apparent angular speed - if the distance is right. If the natural size of the rabbit is overestimated, so will be its distance and to explain its angular motion one wrongly infers that it moves opposite to the car’s direction of motion. And vice versa a distance underestimate drags the estimated rabbit velocity towards that of the car, i.e. it is wrongly inferred that the rabbit moves in the same direction as the car does. As the Sun moves with a velocity of more than 200 km s$^{-1}$ around the Galactic centre, for this sample a 10% distance overestimate implies that an average halo star in the sample will be wrongly pushed by $\sim 20$ km s$^{-1}$ into retrograde motion, and a larger distance error will entail a proportionately larger retrograde motion.

It should also be mentioned that azimuthal velocities are subject to an error similar to the Lutz-Kelker (1973) bias: Even if there is no net bias on estimated absolute magnitudes and thus of distances, a symmetric magnitude error distribution will cause an asymmetric distribution of estimated distances with a longer tail in the overestimates. As these directly translate to the transverse velocities one will with any magnitude based distance scheme encounter asymmetric velocity errors that give rise to an extended counterrotating tail in the measured halo azimuthal velocity distribution. This may also be related to the asymmetry found by Norris & Ryan (1989).
Fig. 2. The distribution of the “well behaved” stars in the calibration sample (red crosses, without distance cut to make the giants visible) in the dereddened colour-gravity (DR7 pipeline) plane. Horizontal lines mark the cuts adopted by Carollo et al. between the dwarf, turn-off and subgiant/giant regions. Stars that have likely membership in their counter-rotating halo, i.e. with \( V_h < -400 \) km s\(^{-1}\) and fulfilling \( d < 4 \) kpc are marked with blue points.

### 3.2 Gravities

Fig. 2 shows the positions of all cleaned sample stars in the colour - log\( (g) \) plane (red points). The horizontal lines show the selection regions in log\( (g) \) used by C10. Stars with log\( (g) > 4.0 \) are classified as main sequence stars. Those with log\( (g) < 3.5 \) are assumed to be subgiants or giants, while the intermediate objects are classified into their “turn-off” branch. The blue dots mark the objects in the C10 sample that have heliocentric azimuthal velocities, \( V_h < -400 \) km s\(^{-1}\), i.e. they are on highly retrograde orbits and should be in the majority counter-rotating halo objects according to C10. There can be minor differences between the gravities directly from DR7 and their sample, as we use the best determined values when their are double or multiple entries for a star, while their log\( (g) \) values (which we do not have access to) are probably averaged.

The plot reveals one crucial problem with those criteria: although it may be expected that some distinct branches of stars are present, they are not reflected by the SEGUE measurements. While the upper giant branch is apparent, we cannot make out a substantial decrease of densities between the main sequence and subgiant regions. Measurement errors prevail, especially in the turn-off region, and veto against a clean selection of the components.

One possibility is that the measurement errors on log\( (g) \) are so large that it is not possible to use the log\( (g) \) measurements to classify stars into these three categories. Also the true main sequence is inclined in gravity versus colour. In this perspective the constant (colour and metallicity independent) gravity cuts applied by C07 and C10 do not appear well founded. If one aims to select a pure dwarf sample, the tightening of the constant cut relative to the inclined main sequence, is, however, beneficial in reducing the turn-off-contamination.

The accuracy of the DR7 log\( (g) \) values is discussed by Lee et al. (2008b), who show estimated surface gravities for open and globular cluster stars observed by SEGUE for the purpose of calibration of the survey. As demonstrated by Lee et al. (2008b) (see their Fig. 15 if) the low spectral resolution results in a significant scatter in log\( (g) \) values: some turn-off stars have log\( (g) < 3.5 \), and significant numbers of stars with log\( (g) \) measurements in the region assigned by Carollo et al. to the turn-off (3.5 < log\( (g) < 4 \)) are clearly either subgiants or main sequence stars. Thus we have to expect a significant number of main sequence objects in the turn-off band of the Carollo et al. (2007, 2010) samples.

The consequent bias in distance estimation discussed above will give an artificially enhanced fraction of retrograde halo stars residing in the turn-off/subgiant regime. Although Fig. 2 should play this effect down with the red points being drawn from the main sample without distance cuts (to keep the red giant branch visible), while the blue circles satisfy \( d < 4 \) kpc in addition to the velocity cut, this crowding of the counterrotating halo stars into the designated turn-off region is still prominent. The distance cut is responsible for the missing enhancement in the giants.

Carollo et al. also find that their outer counterrotating halo members display significantly lower metallicities than the average of the inner halo. Could this be related to problems with distance estimation as well? It would not be unreasonable to expect the accuracy of the log\( (g) \) estimates to decrease for the stars of lowest metallicity, increasing by this the fraction of fake turn-off stars and subgiants, since the stellar lines become weaker. In fact, Ma et al. (in prep.) find this effect. A better understanding of why the “counter-rotating” component of Carollo et al. has lower metallicity can be achieved from Fig. 3. In its top panel we plot the gravities against the metallicity, again with red points for the entire sample and with blue circles for the strongly retrograde stars. Stars with lower metallicities in the sample get on average assigned lower gravities. This could arise from the fact that determining gravities gets more difficult on the lowest metallicity side. The inclination of the sample in the metallicity-gravity plane favours distance overestimates for metal poor stars, thus lowering the average metallicity of the “counter-rotating” component. This shift in classification of stars is demonstrated in the middle panel of Fig. 3. Almost all identified subgiants are metal-poor, while the average metallicity rises towards the higher surface gravity categories. The bottom panel shows the ratio of the number of turn-off to main sequence stars, \( \rho \), against metallicity. One might argue that the pronounced rise of \( \rho \) towards lower metallicities be caused by the intrinsic rarity of metal-poor objects. As the sample is dominated by magnitude cuts, the different ratios could, however, just be explained by different geometry of the subpopulations, which indeed puts stars with higher scaleheights (e.g. halo) to more remote positions than those with low scaleheights (e.g. disc). Since the C10 sample extends by definition less than 4 kpc away from the plane it is hardly possible to explain how \( \rho \) can rise by a factor of ~ 3 from \( [Fe/H]_{DR7} \sim -1.5 \) to \( [Fe/H]_{DR7} \sim -2.5 \) as the large scaleheight of the halo should veto against relative density variations of the halo populations by this amount.

### 3.3 Absolute magnitudes

Having discussed the surface gravity estimates it is time to turn towards the actual assumptions on absolute magnitudes of stars from which the distances are inferred. The claim by C10 to reach an accuracy of “10 – 20%” in distance estimates is predicated on the ability to cleanly select stars according to their spectroscopically determined gravity into several branches. If such a selection was feasible, it would indeed limit the uncertainties to those caused by
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Figure 3. Top panel: The distribution of the cleaned "all star" sample in the metallicity- surface gravity plane. Horizontal lines mark the cuts adopted by Carollo et al. between the dwarf, "turn-off" and subgiant/giant regions. Stars in the C10 subsample displaying a clear membership to what might be a counter-rotating halo, i.e. with $V_h < -400 \text{ km s}^{-1}$ are marked with blue points. Middle: Metallicity distributions for the different gravity classes used by Carollo et al., showing how low metallicities dominate the "turn-off" and "subgiant" stars. Bottom panel: Ratio of identified "turn-off" stars to dwarf stars as function of $[\text{Fe/H}]_{\text{DR7}}$ using the gravity cuts by Carollo et al. Even between $[\text{Fe/H}]_{\text{DR7}} \sim -1.5$ and $[\text{Fe/H}]_{\text{DR7}} \sim -2.5$ there is a strong uptrend.

Figure 4. The distribution of the sample stars in the $(g - i)_0, M_r$ plane with tiny crosses. Colours give the metallicity $[\text{Fe/H}]_{\text{Car}}$ according to the colour bar on the right. The top panel contains all stars in the C10 sample that pass our quality cuts, while the middle panel exclusively contains stars with $[\text{Fe/H}]_{\text{DR7}} < -1.9$. For comparison we give the BASTI (Pietrinferni et al. 2004, 2006) alpha enhanced isochrones at $[\text{Fe/H}] = -2.14$ of ages 10 and 12.5 Gyrs (green lines) and the Ivezić et al. (2008) absolute magnitude calibration at the same iron abundance (red line). In the bottom panel the metal-poor stars have been enhanced in size and stars with $V_h < -400 \text{ km s}^{-1}$ derived with C10 distances are marked by light blue circles. Red lines show the adopted main sequence calibration (IvzMS) at $[\text{Fe/H}] = -2.14$ and $[\text{Fe/H}] = 0$. Dark blue lines show the BASTI isochrones at solar metallicities for 1, 4, 10 and 12.5 Gyrs, green lines same as in the middle panel. The crosses mark the typical photometric errors and uncertainties in the isochrones.
metallicity, reddening and photometric errors. The reader should bear in mind that the low relative density of the outer halo component found by Carollo et al. implies that even a contamination on the 1% level (i.e. 200 out of ~ 20000 stars) can alter the results.

The sorting into different branches via the formalism of Beers et al. (2000) can be seen in the top panel of Fig. 4. The plot shows all stars in the C10 sample in the $(g - i)_0$, $M_i$ plane that do not have warning flags. The absolute magnitudes were derived directly from the C10 distances using the distance modulus via

$$M_i = r_0 - 5 \log_{10} \left( \frac{d_{Car}}{0.01 \text{ kpc}} \right)$$

(1)

where $M_i$ is the derived absolute magnitude, $r_0$ is the reddening corrected apparent magnitude from the DR7 database and $d_{Car}$ the distance given by Carollo et al. and derived from the Beers et al. sequences.

The three branches, into which the sample stars are selected, can be identified in the figure. Lower metallicity stars are brighter and bluer, but the latter shift dominates. Thus the main sequence gets fainter at the same colour. As the metallicity spread of especially the main sequence in the top panel of Fig. 4 partially obscures the underlying sequences, we restricted the sample to $[\text{Fe/H}]_{DR7} < -1.9$ in the middle panel. For comparison we plot the adopted main sequence calibration at $[\text{Fe/H}] = -2.14$ and the alpha enhanced Basti isochrones (Pietrinferni et al. 2004, 2006) for SDSS colours (cf. Marconi et al. 2006) at $[\text{Fe/H}] = -2.14$ at ages 10 and 12.5 Gys. The main sequence and the giant branch are apparent and between them lies a strong sequence sloping down from (0.2, 3.8) to about (0.8, 4.8). The stars in this band are termed turn-off stars by Carollo et al. as they comprise everything that has gravities $3.5 < \log(g) < 4$. As we can see from the bottom panel, this artificial turn-off sequence comprises the majority of heavily counter-rotating stars (green dots). The reader might ask why we do not see a large number of stars as false identifications in the brightest subgiant branch. As already discussed above the absolute magnitude difference to those stars is, however, so large that by the distance limits most stars sorted into the subgiant and giant branches will be dropped from the sample, as they are deemed to be more than 4 kpc away. This conclusion is verified by the subgiant branch getting much more populated when the distance cut is removed (cf. Fig. 2).

In stellar evolution there exists no unique turn-off branch. Instead there is just a region where stars leave the main sequence and move up to the subgiant branch, and which depends on metallicity and age of the population. Thus the artificial sequence we face here can only be thought of as a compromise for stars in the broad region between main sequence and subgiant branch that intends to describe the average luminosity of these objects. In this perspective, the claim by Carollo et al. to achieve 10 − 20% accuracy in distances is ruled out in this transition region as it intrinsically spans more than one magnitude (at fixed metallicity and colour), i.e a distance uncertainty of more than 50%. Because this "turn-off" branch is constructed to be a compromise between subgiants and main sequence, the gap between the subgiant branch (moving up towards lower metallicity) and the main sequence (moving down, as the colour effect dominates) widens with decreasing metallicity. This aggravates the effects of misassignments on estimated distances for lower metallicity objects.

The worst problem with the "turn-off" stars appears in comparison with stellar models. Comparison of the adopted positions of metal-poor stars in the colour-magnitude diagram with the isochrones at 10 and 12.5 Gys reveals that most objects in the artificial "turn-off" branch reside on the red side of the low metallicity turn-off region. Some of the selected "turn-off" stars are even on the red side of what could be achieved at solar metallicity. In fact the overwhelming majority of strongly retrograde stars is actually claimed to be in a region where according to our knowledge of astrophysics no star of reasonable ages can reside.

3.4 Colour transformation and main sequence comparison

It should be mentioned that the distances used in C07 and C10 were derived using the $B - V$ colour calibration and thus the colour transformation of Lee et al. (2008a) had to be performed to apply them to SDSS colours. Fortunately there are now good isochrones (e.g. BASTI isochrones, Pietrinferni et al. 2004, fiducials An et al. 2008) and photometry in SDSS colours readily available, making such a colour transformation to translate SDSS colours to the former $B - V$ calibration by Beers et al. (2000) unnecessary. The colour transformation may explain some of the scatter and systematic shifts presented in Fig. 5 that shows the comparisons of the absolute magnitudes from C10 to the native SDSS calibrations. The latter is depicted by red lines in Fig. 4 at $[\text{Fe/H}] = -2.14$ and $[\text{Fe/H}] = 0$. Both isochrones and the two main sequence approximations are fainter than the adopted C10 absolute magnitudes, especially at lower metallicities. This can be seen from the middle panel of Fig. 4 and from Fig. 5, which depicts the distribution of differences in absolute magnitudes of C10 towards those derived via the adopted main sequence calibration (top panels) and those derived via the Ivezic et al. (2008) age-dependent relation (bottom panels) for all stars (red), metal poor objects with $[\text{Fe/H}] < -1.9$ (blue) and for the "counter-rotating" stars with $V_b < -400 \text{ km s}^{-1}$ (green crosses and errorbars). Errorbars depict the Poisson noise. On the right side of Fig. 5 we show the same quantities, but exclusively for redder stars with $(g-i)_0 > 0.4$ where the sequences of Beers et al. (2004) have a larger separation, and which also excludes the expected turn-off region (cf. the isochrones in Fig. 4) for the very metal-poor stars. Apart from the observational scatter, the peaks arising from the main sequence $\Delta m \sim 0.3$ and from the "turn-off branch" around $\Delta m \sim 1.0$ are washed out for the whole population, as the sequences shift with metallicity and the main sequence dominates. However, the generally higher intrinsic brightness under the Carollo et al. assumptions is clearly seen in both distance descriptions. On the blue end the age-dependent formulation by Ivezic et al. (2008) is a bit brighter than the adopted main sequence calibration and makes the peak of the "turn-off sequence" in the metal poor and counter-rotating subsamples of C10 merge with the main sequence at blue colours, yet the large offset remains.

For stars that are claimed by C10 to have heliocentric velocities $V_b < -400 \text{ km s}^{-1}$ and thus make up the bulk of what they identify as a counter-rotating halo the two peaks of main sequence and turn-off stars are separated, as the metallicities of these stars are more narrowly distributed. For comparison we show the result of selecting only stars that have $[\text{Fe/H}]_{DR7} < -1.9$ (blue squares in Fig. 5). These distributions look very similar apart from the counter-rotating stars being more inclined to the bright side. Also regard the increased importance of the turn-off band for those populations.

In summary there are two main drivers of overestimated distances in Carollo et al. compared to the native SDSS distance calibrations: The main sequence of C10 for metal-poor stars is brighter than the adopted Carollo et al. assumptions is clearly seen in both distance descriptions. On the blue end the age-dependent formulation by Ivezic et al. (2008) is a bit brighter than the adopted main sequence calibration and makes the peak of the "turn-off sequence" in the metal poor and counter-rotating subsamples of C10 merge with the main sequence at blue colours, yet the large offset remains.
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Figure 5. The distribution of absolute magnitude differences between the Carollo et al. calibration and the other metallicity-dependent colour-magnitude calibrations. In the top row we show the results for the adopted main sequence calibration (“IvzMS”), while in the bottom row we compare to the age-dependent calibration by Ivezić et al. (2008) (“IvzA7”). On the left we show the entire colour range, while we plot only redder objects with \((g - i) > 0.4\) on the right. In the entire sample (red bars) the main sequence by Carollo et al. is brighter by \(\sim 0.15\) mag than in the native SDSS calibrations. The offset gets larger for the counter-rotating (green crosses) and metal-poor (blue squares) stars; note that the Carollo et al. turn-off sequence is very prominent with an offset of about 1 magnitude.

4 SIGNATURES OF MISSELECTION

4.1 Geometric distribution anomaly

Even if the biases in distance assignments were not obvious there are still ways to detect them. As erroneous distance estimates mostly act on the part of motion perpendicular to the line of sight, populations with distance errors will be preferentially found in regions of the sky perpendicular to the velocity component in question, or in other words, if stars end up in one component by misselection this should show up as a bias in sample geometry. Such a bias will not be aligned directly with the Galactic coordinates, but with the part of the biased velocity component covered by proper motion. This is obvious as the largest errors should happen where the uncertainty in the motion is largest, i.e. where the proper motion and distance estimates have the largest impact. For metal-poor stars; most of the designated “turn-off” stars by C10 reside in positions in the colour-magnitude plane that would require unreasonable ages. We thus conjecture that the “counter-rotating” halo as presented by C10 is due to distance uncertainties and the selection of stars into unphysical stellar branches an artifact.

Figure 6. The cumulative distribution of stars on the part of \(V_h\) that is covered by proper motions and not radial velocity measurements. The stars with \(V_h < -400\) km s\(^{-1}\) are drawn with a purple line while the overall sample distribution is drawn with a red line. Beneath is the 0.01 significance level of a Kolmogorov-Smirnov test.
these statistics we make use of the squared angle terms connecting the proper motion to the azimuthal velocity (from now called the "proper motion partition"). We take from eq. (6) in the Appendix the angle terms that connect \( V_{\phi} \) to the proper motions \( l \) and \( b \), square them and add them together:

\[
\xi_{pm,v} = \sin^2(l) \sin^2(b) + \cos^2(l). \tag{2}
\]

Fig. 6 shows the cumulative distribution of stars over the proper motion partition for \( V_\phi \) (red line). The C10 sample is (as the entire SEGUE survey) concentrated towards positions where the azimuthal velocity is mostly covered by proper motions as it is mostly oriented towards high Galactic latitudes. Yet the counter-rotating subsample (purple line) is even more concentrated towards the high proper motion contributions. The average value for \( \xi_{pm,v} \) rises from 0.909 for all stars to 0.933 for the subsample with \( V_\phi < -400.0 \). In other words, the fraction covered by robust radial velocities drops from 0.091 to 0.067. In a Kolmogorov-Smirnov test the probability for equality of the two distributions is well below the 1% level and thus equality is strongly rejected. Again the high values for \( \xi_{pm,v} \) show how vulnerable the sample azimuthal velocities are to any distance errors.

This is of course not a proof of the bias, but a strong indication. Against this argumentation one could raise the objection that stars at low metallicities are located more polewards, as the halo to disc ratio in the sample rises (higher altitudes are reached) and so metal-poor/halo stars show a different spatial distribution. Indeed for lower metallicities the sample distribution shifts polewards reducing the difference, which remains present in all cases, but can become insignificant due to the shrinking sample numbers.

4.2 Linear error analysis and velocity crossovers

A robust approach to prove and quantify the distance errors is presented in Fig. 7 which shows the \( W_\phi \) velocities against \( \sin(l) \sin(b) \cos(b) \) for all stars that should be part of the counter-rotating halo, i.e. have \( V_\phi < -400 \) km s\(^{-1}\). The strong up trend cannot be any stream, which would show up as a narrower band. It appears that the entire halo experiences a lift in \( W \) velocity, which has its origin in the distance errors of the C10 analysis. By wrongly assessing distances the relative motion of stars in the azimuthal direction mixes over the proper motions into the vertical component depending on this angle term. To illustrate this effect think of a star that is seen at \( b = 45^\circ \), \( l = 90^\circ \) and has \( U_\phi = 0 \), \( V_\phi = -500 \) km s\(^{-1}\), \( W_\phi = 0 \). Due to the geometry of the setup the star will have a significant proper motion in \( b \). With a wrong distance estimate the relative impact of line-of-sight velocity and proper motion changes and the star is assigned a non-zero \( W \) velocity. A more detailed description is found in Schönrich et al. (in prep.).

The fitting line has a slope of \( 119 \pm 45 \) km s\(^{-1}\), i.e. the trend is significant at a level of more than 7σ. We can thus state that a significant distance error that is expected from the discussions above is here quantitatively demonstrated. Since the alleged counterrotating halo stars in this subsample (with a cut at \( V_\phi < -400 \) km s\(^{-1}\)) have on average \( V_\phi \sim -470 \) km s\(^{-1}\), we arrive at a distance bias of roughly 40% for the counter-rotating stars, which translates into a magnitude error of around 0.7 mag. It should be mentioned that errors might even be higher: Selecting more strongly retrograde stars the trend estimate gets even higher.

Restricting the sample of stars with \( V_\phi < -400 \) km s\(^{-1}\) further to dwarfs (log(g) > 4.0) and thus removing the largest identified source of distance errors, the numbers of stars in the sample drop by the selection dramatically from 735 stars to 299. The removal of the low gravity stars also gives fewer outliers in the velocity distribution. Only one object has \( |W| > 400 \) km s\(^{-1}\). The lower panel of Fig. 7 shows the remaining stars together with an equivalent linear fit. Again the trend is highly significant, though now more moderate with \( 83.8 \pm 22.5 \) km s\(^{-1}\). The \( \sigma_W \) in the sample is already down from \( 129 \) km s\(^{-1}\) to \( 110 \) km s\(^{-1}\). The more moderate trend corresponds to an error of about 25%. It also fits well into the picture that the distance overestimate for the full sample is larger than for the dwarfs, when we remove the spurious "turn-off" branch. This bias has the effect that the distance overestimates do not only increase the \( W \) velocity directly, but also give rise to an additional contribution to the \( W \) velocity dispersion by turning a part of the large heliocentric azimuthal motion of halo stars into a fake vertical term. We will call this behaviour "velocity crossovers". This effect is even more important in the original analysis by C07 and C10, as they restrict their sample in galactocentric radius, thus increasing the weight around \( l = 90^\circ \) and \( l = 270^\circ \), where \( \sin(l) \) is largest.

5 VELOCITY DISTRIBUTION

How do the described biases and different distance derivations affect the velocity distribution and what might remain of the alleged counter-rotating component halo when we reduce the distance biases that spuriously inflate it? Fig. 8 shows the velocity distributions under different cuts and distance approximation both on a linear scale and on a logarithmic scale that reveals the wings of
the distributions. Error bars give the Poisson noise, but neglect any other sources of error. The velocity distributions of the halo and the Galactic disc can be made out in both plots. The long tail of the counter-rotating halo is clearly visible for the C10 sample (red circles). As already noted above, a restriction to dwarf stars (green crosses) diminishes the counter-rotating tail (around $V < -170$ km s$^{-1}$, which corresponds to $V_h < -400$ km s$^{-1}$). The blue filled squares show what we obtain with the adopted main sequence calibration, and the purple empty circles depict the age-dependent distance calibration by Ivezić et al. (2008). With both native SDSS distance calibrations and the purple empty circles depict the age-dependent distance calibration by Ivezić et al. (2008). With both native SDSS distance calibrations, the sample displays a clean downturn to the low velocity side corresponding to a $V$ velocity dispersion of around $70 - 80$ km s$^{-1}$.

One might argue that the two native SDSS calibrations lead to some contamination by giants that are treated as dwarfs and thus provoke the opposite effect of underestimating distances. To reduce the contamination by evolved stars we use a gravity cut of log($g$) > 4.1 in the following discussions, which mostly helps to reduce the density saddle between the disc and halo component, where halo stars with severe distance underestimates tend to assemble. However, the left tail of the halo distribution does not change significantly on a tightening or loosening of the gravity cut. In the following discussions we will always use the slightly tightened condition log($g$) > 4.1, but we checked that all of our conclusions are valid regardless of the specific choice of the gravity cut. The absence of a significant excessive tail for dwarf stars can in our view only be explained by the fact that strongly counter-rotating halo dwarfs are at the best an extremely rare population. It is highly implausible that the counter-rotating halo consists exclusively of subgiants and giants.

5.1 Kinematics versus metallicities

The reason why Carollo et al. (2007, 2010) get a transition between their inner and outer halo from a local sample is the increasing scaleheight of their populations with lower metallicity, which is linked to the increasing velocity dispersion perpendicular to the plane. According to our above discussion of kinematic fingerprints of distance errors, at least the increase of vertical dispersion by velocity crossovers (Section 4.2) due to distance overestimates should disappear when cutting away the unphysical turn-off stars and further when switching from C10 dwarf distances to the native SDSS calibrations. This is indeed observed in Fig. 9. It shows the values of vertical velocity dispersion against metallicity for different subsamples together with Poisson errors. The full C10 sample (red circles) harbours a prominent uptrend towards lower metallicity, which is at odds with the earlier result from Chiba & Beers (2000). This uptrend almost vanishes in their dwarf subsample (green crosses). Both when using the adopted main sequence calibration (blue filled squares) and when using the [Ivezić et al. (2008)] age-dependent distance estimates (purple empty squares), we see no significant trend with metallicity any more; this finding is robust against changes in the gravity cut. To guide the eye we plot a horizontal line at 85 km s$^{-1}$. There is a suggestion of a subtle increase below [Fe/H]$_{DR7}$ < −1.8, yet numbers are too small to allow for a judgement. A source of uncertainty is the degree of possible giant contamination. It likely rises towards the metal-poor side, which may result in a reduction of measured dispersions. On the other hand the radial velocity support for the vertical velocity component is very high due to the polewards orientation of the sample. So the decrease effected by distance underestimates is relatively weak. Underestimating distances takes a further moderated effect on vertical dispersions: While a distance overestimate both increases the
measured vertical dispersion by direct overestimate of the proper motion part, and a lift via the velocity cross-overs, on distance underestimate the effects have opposite signs, thus to some part balancing each other.

Another way to look at the problem is to plot metallicity distributions as a function of the kinetic energies (by stellar mass) of stars. In Fig. 10 we show the separations in entire kinetic energy ($v^2$, left column) and in vertical kinetic energy ($W^2$, middle column). In the rightmost column we show the vertical kinetic energy, but for retrograde stars ($V < -10$ km s$^{-1}$). As the rotation velocity of disc stars adds to the kinetic energy the disc has its strongest dominance of course not in the lowest energy bin, but at $180^c ({}^3 \text{km s}^{-1})^2 < v^2 < 270^c ({}^3 \text{km s}^{-1})^2$, as most disc stars are on quite circular orbits with an entire velocity close to the circular rotation speed of the Galaxy. The prominent shift especially in the left tail and also peak of the metallicity distributions in the original C10 distance prescription for the full sample (top row) can be seen in both the total and vertical energy separation. However, this already diminishes, when we plot the subsample of the C10 dwarf stars with log($g$) $> 4.0$ (second row). No convincing outer halo signature can be found in either of the native SDSS calibrations (bottom row). At the highest vertical energies a single spike at $[\text{Fe/H}] \sim -2.2$ sticks out. At first glance this could be taken as a hint for an outer halo. However, in this interpretation it should be mirrored by the entire energy distribution, which is not the case. We are tempted to identify this feature at least partly with a prominent metal-poor stellar stream described by Helm et al. (1999) and Keplev et al. (2003), which we expect exactly at these very high vertical energies. This stream can as well serve as explanation for the subtle and insignificant increase of vertical velocity dispersions at $[\text{Fe/H}]_{\text{Dart}} < -1.8$ that was seen in Fig. 9.

There appears also a slight general drift towards lower metallicity at the highest energies, which can be mainly seen in the vertical term. Caution should be exercised, however, due to the varying presence of the Galactic disc (most prominent at the lowest vertical kinetic energies and at total energies corresponding to the rotation speed), which then impacts on the normalization of the halo component and fools the eye because the apparent halo peak can be shifted by the wing of the disc distribution. A quite robust approach is removing all prograde stars from the sample to minimize disc contamination. As this biases kinematics, the overall energy distributions are altered, but the vertical energies (right hand column) should not be affected. In Fig. 10 the entire C10 sample shows a clear signature of lower metallicities in the higher vertical energy bins. When removing the contested turn-off stars (i.e. plotting dwarfs, centre row) no trend apart from the discussed spike can be detected regardless of the applied distance determination.

In summary it can be stated that also in terms of metallicity versus energy the sample has no reliable outer halo signature, neither when using the native SDSS calibrations nor when using the C10 dwarf subsample.

5.2 Component fit

Fig. 11 shows fits to the azimuthal velocity distribution (green data points) for the the four different subsamples and distance calibrations we use. Both columns show the same data, the left column on a linear scale, the right column on a logarithmic scale to examine both centres and wings of the distributions. We apply a simple Gaussian halo and a single non-Gaussian disc component. All fits were done for $-250$ km s$^{-1} < V < 280$ km s$^{-1}$, a limit that stays out of the regions dominated by noise, but reaches on the retrograde side still well into the region where any suspected retrograde halo component would be influential. To account for the observational errors, we folded the underlying distributions with a sum of Gaussians (with a spacing of 1 km s$^{-1}$), of which the relative weights were derived globally for each component from error propagation on the single objects (stars with $V > 50$ km s$^{-1}$ attributed to the disc, objects with $V < 10$ km s$^{-1}$ to the halo) concerning proper motion and radial velocity errors. This treatment is a bit crude and we suspect that it underestimates errors on the left wing of the distribution and overestimates them on the right wing, which we identify as the most likely reason for the overshooting of the model against the data at $V > 270$ km s$^{-1}$. In a second step we folded with another Gaussian magnitude error of 0.25 mag to account for uncertainties in the intrinsic brightness and thus distance of the stars and thereafter a third Gaussian of 7 km s$^{-1}$ to account for velocity crossovers via the distance uncertainties.

For the disc component we make use of the analytic formula of Schönrich & Binney (in prep.). The underlying assumption is that of an isothermal sheet through the Galaxy with increasing velocity dispersions towards the centre, i.e. the stellar populations at each galactocentric radius are given a specific vertical and horizontal energy dispersion. For those populations their likelihood to be in the solar annulus and their scaleheight can be estimated assuming a simple potential with constant rotation speed. We used a solar galactocentric radius $R_0 = 8.0$ kpc, a circular rotation speed of $v_c = 220$ km s$^{-1}$, a disc scalelength of $R_d = 2.5$ kpc, a scalelength for the vertical dispersion of $R_v = 5.0$ kpc and for the horizontal dispersion as $R_h = 7.5$ kpc. The adiabatic correction index (index dependent on the shape of the potential that describes the change of vertical energy along orbits that are extended over different galactocentric radii) was set to 0.5. As we are using the adiabatic correction without a recorrection for energy conservation, the disc local scale height gets moderately underestimated, an effect that we partially cope with by setting the adiabatic correction index to 0.5, slightly below the expected value for the upper disc. To simplify the calculation we summed up disc contributions at equal parts at altitudes $z = 400, 700, 900, 1100, 1400, 1800, 2400$ pc. The Gaussian halo component was set at rest ($V = 0$). The five free parameters of the fit were disc and halo normalization ($N_d = 530, N_d = 16691$ for the entire C10 sample, $N_d = 14403, N_{h} = 312$ for the C10 dwarfs, $N_d = 13031, N_{h} = 262$ for the adopted main sequence calibration, $N_d = 13254, N_{h} = 255$ for the age-dependent calibration), halo azimuthal velocity dispersion ($84.7, 80.9, 65.4, 68.9$ km s$^{-1}$), disc local horizontal dispersion ($\sigma_0 = 43.2, 41.4, 41.5, 40.1$ km s$^{-1}$), and local scaleheight ($h_0 = 571, 499, 466, 439$ km s$^{-1}$). As seen in Fig. 11 apart from a weakness on the high velocity side, which presumably derives from the use of a global observational scatter that could overestimate the uncertainty for disc stars, the two-component approximation gives decent fits (red lines) to the velocity distributions for the dwarf samples. The relative halo normalization varies between the different datasets as the most metal-poor stars are more likely to be classified into the turn-off or subgiant bands.

Of most interest for this discussion is the shape of the (retrograde) halo velocity distribution. For the entire C10 distance sample (left column) we can clearly identify the bump that encouraged C07 and C10 to fit a separate velocity peak starting from around $-200$ km s$^{-1}$. This anomaly becomes especially apparent in the logarithmic plot and is confirmed by Poisson loglikelihood values ruling out equality of the theoretical (simple Gaussian halo) and observed distributions at highest significance.

We point out that even this strong anomaly in the fit alone
Figure 10. Metallicity distributions at different values for kinetic energy in the different distance prescriptions. From top to bottom we show the entire C10 sample, the dwarf stars from C10, the adopted main sequence calibration and the Ivezić et al. (2008) age-dependent calibration. The left column displays a separation by the entire kinetic energy, while the centre column makes only use of the vertical velocity $W$. The right column shows the distributions using the vertical energy part for retrograde stars ($V < -10\, \text{km s}^{-1}$) to reduce the disc contamination. Velocities are taken in km s$^{-1}$. Error bars indicate the Poisson errors.

would not be a sufficient justification for a second physical component, especially not for a retrograde component. There is no reason to firmly believe that the Milky Way halo or its possible components should have a strictly Gaussian velocity structure; the disc certainly can not be adequately described by Gaussian fits (a discussion of this can be found in Strömbäck 1927) and similarly the halo might have a more complex velocity distribution. The only way to cleanly identify a retrograde velocity distortion on the Galactic halo from kinematics would be to prove a difference to the prograde halo tail. As this is, however, impossible at the required accuracy due to the disc contamination, we conclude that without a clean halo-disc separation any attempt to use the azimuthal velocity accuracy due to the disc contamination, we conclude that without a prograde halo tail. As this is, however, impossible at the required accuracy due to the disc contamination, we conclude that without a clean halo-disc separation any attempt to use the azimuthal velocity distribution for proving a retrograde halo component is unreliable.

Besides its doubtful significance for indicating a separate component, the extended retrograde tail anyway diminishes when we turn to the dwarf samples, which do not contain the at least partly unphysical turn-off stars: restricting the C10 sample to their dwarf stars (centre column of Fig. 11) the bump below $-200\, \text{km s}^{-1}$
Figure 11. Velocity distributions for stars (light blue, with Poisson errors) in the calibration sample for different selections and distance prescriptions: From top to bottom: The entire C10 sample, the C10 dwarf stars with $\log(g) > 4.0$, the dwarfs with $\log(g) > 4.1$ using the adopted main sequence calibration distances and the age-dependent formula from Ivezić Z et al. (2008). To show both distribution centre and wings we contrast the linear scale (left) with logarithmic plots of the distributions (right). All distributions are fitted by a simple model (red line) with a Gaussian halo and a single (non-Gaussian) disc component. We did an error propagation from the values given in DR7 which is – together with a magnitude error of 0.25 mag - folded onto the original distribution (light blue). The error broadens the peaks and thus lowers the maximum count rates especially of the disc peak. The dark blue line shows the underlying Gaussian halo component and the purple curve the analytic disc component.
disappears. There is a weak surplus of stars between $-220 \text{ km s}^{-1}$ and $-280 \text{ km s}^{-1}$, which could, however, just be a statistical fluctuation. This is confirmed by statistics, which have the p-level (measured under the assumption of Poisson errors) for equality of the fit and the measured distribution at 0.55 for $-250 \text{ km s}^{-1} \leq V \leq 20 \text{ km s}^{-1}$ (and 0.20 when we extend the range to $-300 \text{ km s}^{-1} \leq V \leq 20 \text{ km s}^{-1}$) meaning that when drawing realisations from the given theoretical distribution, about 55% of the samples would be more different from the theoretical distribution than the current one. Regarding our imperfect treatment of distance errors the quality of the fit is rather surprising. Using the main sequence distance calibration the distribution gets even more contracted due to a weak surplus of about a dozen objects between $V = 280 \text{ km s}^{-1}$ and $V = 75 \text{ km s}^{-1}$, which could, however, just be a statistical fluctuation. It can also be argued that an attempt to fit the disc velocity distribution via a Gaussian fit increase the need for a spurious second halo component, especially as the large (unavoidable) velocity errors limit the information on the real shapes of the underlying velocity distributions: as the disc velocity distribution is naturally skewed towards lower velocities, a Gaussian fit will drop too steeply towards low rotation velocities. This invokes a second Gaussian for the disc (thin-thick discs), which will in most cases show the same problem again, forcing the halo component a little bit up into the prograde regime. This again increases the need for the creation of an artificial retrograde halo component. In this case we avoided this problem by using a more physical fitting formula for the Galactic disc, yet there was still noticeable influence by the disc fit onto the parameters of the simple Gaussian halo component.

Overall we can state that any striking excess of highly retrograde stars disappears from the distribution when we limit the sample to the more reliable dwarf stars. There is a good agreement between fits and data for the dwarf samples, apart from a misfit at high velocities and a slight surplus at the lowest velocities against a Gaussian fit, which, however, rather looks like imperfect error handling or a probable contamination of the sample with misidentifications in between the different catalogues delivering the proper motions or a non-Gaussianity in their contamination. Replacing the questionable Gaussian analysis for the disc by a more physically motivated formula and by applying an error propagation we have shown that neither a second halo nor a second or even third disc component are required for explaining the azimuthal velocity distribution.

5.3 Velocity dispersions

Using the adopted main sequence approximation and restricting the sample to 2020 retrograde stars ($V < -10 \text{ km s}^{-1}$) we can give a tentative estimate for the halo kinematics of $\sigma_r \sim 157 \pm 10 \text{ km s}^{-1}$ and $\sigma_y \sim 75 \pm 8 \text{ km s}^{-1}$. The latter is close to the azimuthal velocity dispersion of $\sigma_r \sim 70 \text{ km s}^{-1}$ from the last section. In these values we accounted for the errors reported in the SEGUE pipeline plus a dispersion of roughly estimated 15% in the distances. These act to reduce the derived velocity dispersions from the actually measured ones. Those values are considerably smaller in V and W than what was given by C10 partly due to the spurious crossover into W velocities having diminished. We point out that these values agree well with the results of Kepley et al. (2007) and Smith et al. (2009). Although we use the same sample with the same distance scale as Smith et al. (2009) we cannot confirm their quoted errors of 2 km s$^{-1}$, since the systematic uncertainties by the distances within the Ivezić et al. (2008) method and sample cleaning are currently too large to assess dispersions on a scale better than 5%.

6 Conclusions

We have described how errors in distance estimates result in an apparent systematic retrograde motion of the Galactic halo, an effect to which the SEGUE/SDSS sample is especially prone by its strong poleward orientation. The general problem of distance biases similarly applies to any study that makes use of proper motion-based estimates. We find that the distance derivation of Carollo et al. (2007) and Carollo et al. (2010) is flawed by sorting stars into unphysical positions in the HR diagram: objects are placed between the subgiant and dwarf sequences in positions that would require stellar ages in excess of the age of the universe. Despite the elegance of the general idea to sort stars into known sequences according to their estimated gravities, the method itself and the used gravity cuts are not well supported by measurements. Moreover there is no "turn-off"-sequence, but turn-off stars are populating a region that spans of order 1 magnitude in luminosity. In this light the statement by C10 to have distances precise to about 10 – 20% is an unsupported claim.

From the distances kindly provided by Carollo et al. we calculated back to their assumed absolute magnitudes and found systematic differences of $\sim 0.2$ to 0.3 mag and a large scatter for metal-poor main sequence stars towards the adopted main sequence calibration as well as towards the age-dependent calibration by Ivezić et al. (2008), also far to the red side of the suspected turn-off region. The adopted main sequence calibration is only slightly fainter than the theoretical BASTI isochrones.

We have shown in Section 5.3 that the claim by C07 and C10 to have found a counter-rotating extended tail of the halo is largely caused by unphysical assumptions about locations of stars in the HR diagram, by magnitude uncertainties in the turn-off stars and by the use of a too bright main sequence calibration. The correctness of this tail can be ruled out by statistical tests, as described in Section 4. The tail diminishes when we limit the C10 sample to dwarf stars and disappears when we make use of the better founded Ivezić et al. (2008) calibrations, which are consistent with fiducials and isochrones. In Section 5.2 we demonstrated that the halo distribution for the dwarf samples regardless of the applied distance determination can be fit by a simple Gaussian component.

We have also shown that in the DR7 pipeline stars with lower metallicities are shifted towards lower gravities, considerably increasing their fraction among the thought-to-be turn-off stars. Further the magnitude difference for their main sequence stars against the Ivezić et al. (2008) main sequence calibration grows towards lower metallicities. The stronger prevalence of distance errors at the metal-poor end of the metallicity distribution will thus give any spurious counter-rotating tail members a biased metallicity distribution.

Finally we have shown that the claim of C10 that the counter-rotating component members reach to higher altitudes can as well
be traced back to distance determinations: the dispersion of the vertical velocity component is significantly increased by their distance errors, though due to the polewards sample orientation this effect would at first order be smaller than for the other velocities. As shown in Section 4 simultaneously the W velocities of the halo stars with distance overestimates are artificially increased by an order 50 km s$^{-1}$ via spurious velocity cross-over terms from the heliocentric azimuthal velocities in the derivation. The effect is strongest for the most strongly retrograde objects (they have the largest heliocentric $V_R$) and is aggravated by their selection for stars in galactocentric radius $7$ kpc $< R < 10$ kpc. This colludes with their metallicity dependent distance bias (see above) to produce their findings of decreasing metallicities at high altitudes. There is a slight excess of more metal-poor stars in a single velocity bin at high vertical velocities, which is not mirrored by the behaviour at high total kinetic energies. We argue that this is most likely a reflection of a well-known local stream that has been identified by Helmi et al. (1999) and Kepley et al. (2007).

Another source of error is the modelling of especially the Galactic disc azimuthal velocity distribution by Gaussian components. It was shown by Strömbärg (1927) that Gaussian modelling of the Galactic disc lead to unphysical results and the identification of spurious components on the low rotation side because of the extended tail. As the skewed V velocity distribution enforces in most cases the introduction of a second Gaussian component, that - being a mere artifact by wrong assumptions - can then be misinterpreted as physical reality, Gaussian modelling of the Galactic disc in a combined disc and halo sample can wrongly force the halo component into the prograde regime to compensate for the two steeply falling disc terms. Consequently this then creates the need for inference of a retrograde component to compensate for the bias.

We also argue that magnitude based distance assessment schemes introduce a velocity bias that resembles the Lutz-Kelker bias: If the error in absolute magnitudes follows a Gaussian distribution, the distance error distribution will thus form an extended tail that grows stronger with increasing dispersions. Via the proper motion part in the determination of space velocities, which is proportional to the estimated distance, measured velocities develop extended tails away from the solar motion. For the V velocity distribution of especially the halo this gives the halo an asymmetric velocity distribution with a longer tail in the retrograde regime, a process that can explain the moderate asymmetries found e.g. by Norris & Ryan (1989).

Finally we note that it is by no means imperative that the halo have a Gaussian velocity distribution. In this light it is rather surprising that our simple Gaussian halo component can fit the data so well. Even if there were deviations from Gaussianity this would alone be no convincing sign for a separate component. A more convincing indication would be a proven difference between the prograde and the retrograde tail of the halo azimuthal velocity distribution, but disentangling this from disc contamination on the prograde side will be difficult.

Recently Carollo and collaborators submitted a rebuttal paper (Beers et al. 2011) claiming that our analysis presented here be wrong. Instead of discussing all our arguments their revised analysis relies on two central claims: They state that the distance scale adopted by us is wrong and that there is an asymmetric halo azimuthal velocity distribution for their metal-poor stars, neither of which we concur with.

Concerning the distance issue we stress that our conclusions are valid for the Carollo et al. (2007, 2010) and both Ivezić et al. (2008) distance calibrations; our work does not rely on a single distance scale in contrast to claims made by Beers et al. (2011). Beers et al. criticize us for adopting the incorrect main sequence calibration of Ivezić et al. (2008) but failed to note that we actually stretched this calibration in the same direction of their preferred one by increasing the luminosities by 0.1 magnitudes and accounting for alpha-enhancement by increasing the measured metallicities by 0.2 dex (Sect. 2). Importantly, we have also made use of their preferred calibration (here denoted 1vzA7) and find no significant differences (e.g. Fig. 11). Finally, we have made use of direct isochrone distances, which fully corroborates our findings.

As for the azimuthal velocity distribution of the most metal-poor stars, we re-emphasize that any magnitude-based distance scheme invokes a bias in the inferred distances and thus an asymmetric azimuthal velocity distribution by definition; this effect is akin to the well-known Lutz-Kelker (1973) bias and is illustrated in Fig. 11. In view of a large magnitude scatter (which their metal-poor stars clearly have, see their Fig. 5) a Gaussian fit is inappropriate due to the missing error handling. In this light it is not surprising that their new revised parameters are quite different from their original results (e.g. for $z_{\text{max}} > 5$ kpc their outer halo mean velocity rose from $-128$ km s$^{-1}$ (cf. Table 1 in C10) to $-59 \pm 20$ km/s). Finally, we argue that moving a considerable fraction of the wrongly identified turnoff stars up to the subgiant/giant branch as done by Beers et al. will make the distance overestimate for misidentified dwarfs among them even more severe.

In summary our criticism of the C07, C10 works remains in full: our in-depth re-analysis of their data with different distance calibrations and a proper error handling reveal no convincing evidence for a dual halo.

The systematic distance uncertainties make it dangerous to draw a definitive conclusion for the strength or existence of a possible counter-rotating halo component. All current distance calibrations have problems and need improvement before a method along the lines used by C07 and C10 can be attempted. We would like to stress that we do not and would not want to rely on either of them. Two central conclusions can, however, be drawn without having to trust any of the different distance calibrations: Even on the C10 or C07 sample using their distances, no reliable detection of any non-Gaussianity in the halo, be it a counter-rotating halo or not, is possible on the examined data set in any of the dwarf samples. If a separate component gets detected on a larger sample in the future, it should be significantly weaker than what was claimed by C10.

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8 APPENDIX

8.1 Kinematics and geometry

We use up-to-date values for the basic constants of our Galaxy. The rotation speed is assumed to be $220 \text{ km s}^{-1}$ in concordance with recent results of Koposov et al. (2010). We apply the recent determinations of solar motion relative to the local standard of rest from Schönrich et al. (2010), which is $\nu_0 = (11.1^{+0.79}_{-0.75}, 12.24^{+0.47}_{-0.57}, 7.25^{+0.37}_{-0.36}) \text{ km s}^{-1}$ with additional systematic uncertainties of $\sim (1, 2, 0.5) \text{ km s}^{-1}$. Neither the Galactic rotation rate nor the solar galactocentric radius $R_{\odot}$ are very well determined, but the angular motion of Sagittarius A* is well constrained (Reid & Brunthaler 2004). The galactocentric radius of $R_{\odot} = 8.5 \text{kpc}$ assumed in C10 is inconsistent with their assumption for the rotation speed. We adopt $R_{\odot} = 8.0 \text{kpc}$, which is in concordance with most measurements, and coincides with the most recent trigonometric parallax determination for Sagittarius B2 (Reid et al. 2009).

8.2 Distance calibrations and metallicities

For adopted distances in SDSS colours two alternatives exist: The Ivezić et al. (2008) calibration (see Appendix therein) or the Beers (2000) calibration. A third possibility would be using the isochrones directly, which would allow for a statistical implementation of the subjulants and also allow for natural shape changes: however, their handling is beyond the scope of this work. The Ivezić et al. (2008) main sequence calibration uses the formula:

$$ M_i (g - r, [\text{Fe/H}]) =$$

$$= 1.65 + 6.29 (g - i)_0 - 2.30 (g - i)_0^2 - 1.11 ([\text{Fe/H}] - 0.18 ([\text{Fe/H}])^2$$

where $M_i$ is the adopted absolute magnitude and $(g - i)_0$ is the reddened SDSS colour index. A short assessment of this formula reveals that it fits the zero age main sequence relatively well in the required colour range at low metallicity. Apart from the short-range behaviour, the subjulants are not considered, the metallicity dependence is not well matched at the high metallicity end. Further, the colour dependence is not perfect at the level of precision required for distances and there are no crossterms between metallicity and colour, i.e. there is no implementation of metallicity-dependent shape changes. Thus this relation has to be used with caution. A comparison with the BASTI isochrones reveals that the Ivezić et al. (2008) calibration at low metallicities is slightly fainter than the isochrones without alpha enhancement. To correct for alpha enhancement we slightly increase the metallicity of all metal-poor stars (with $[\text{Fe/H}]_{\text{DERT}} < -1.0$) by 0.2 dex and let this correction go linearly to zero between $[\text{Fe/H}]_{\text{DERT}} = -1.0$ and $[\text{Fe/H}]_{\text{DERT}} = 0$. In addition we increase all luminosities by 0.1 mag to reconcile the calibration better with the main sequence of M92 according to the fiducials by An et al. (2008), to avoid any suspicion to have buried the counter-rotating tail by a too faint calibration, and as we detected a minor distance underestimate in our statistics without this shift. Further, the calibration is now just slightly brighter than the isochrones as seen in Fig. 3 which is a desired effect at those metallicities, as there are indications that metal-poor isochrones could underestimate the luminosities (or equivalently...
overestimate the effective temperatures) of lower main sequence stars (Casagrande et al. 2007).

To account for age effects Ivezic et al. (2008) also suggested an "age-dependent" calibration, which rises more steeply towards the blue side (Eq. A7 in their appendix). To meet concerns of our referee we show all relevant statistics also in the light of this other calibration. This calibration is steeper in colour than the main sequence calibration, i.e. it is brighter at blue colours and fainter at red colours, following an intention to cope with the steepening of isochrones near the turn-off. However, the steepening of isochrones only applies near the turn-off, while this relation is globally inclined against the main sequence of the isochrones as well as against the main sequence calibration. As this relation thus does not follow the blueward shift of the turn-off towards lower metallicity, a relative overestimate is expected for the distances of the blue stars at lowest metallicity. Vice versa the distances to metal rich turn-off stars might be underestimated.

We tested all our results for the C10 dwarf sample and also for cutting in colour and different gravity selections to delineate the impact by the turn-off region. As can be seen from the central panel in Fig. 4 the difference between the adopted main sequence calibration and the C10 magnitudes persists also to the red side of the turn-off region and is also present for the Ivezic et al. (2008) age-dependent relation.

As an even fourth distance determination we made use of the BASTI isochrones Pietrinferni et al. 2004, 2006. To accomplish that we account again for alpha enhancement with the same grid kindly provided by S. Cassisi for our age determinations in Casagrande et al. 2011. On this isochrone we choose the r-band magnitude from (g-i) on the main sequence. When the turn-off is to the red of the stellar position, we extrapolate from the turn-off point of the isochrone following the shape of the Ivezic et al. (2008) main sequence relation. So these stars are placed at an extrapolated turn-off point. As one can easily see from Fig. 12 in the central statistics there are no significant changes towards the other main sequence calibrations. We confirmed that no real difference was detectable.

C10 used a slightly different metallicity scale from DR7, which was reasoned to balance out a possible metallicity overestimate on the lowest metallicity end:

\[ [\text{Fe/H}]_{\text{DR7}} = -0.186 + 0.765[\text{Fe/H}]_{\text{DR7}} - 0.068[\text{Fe/H}]_{\text{DR7}}^2 \]  

(5)

We argue that their claimed overestimate at low metallicity most likely reflects the impossibility of the pipeline to cope with the faint metal lines in this region, getting lost in the low resolution and low signal-to-noise ratios. This effect is quite similar to the loss of accuracy e.g. in Strömgren photometric metallicities. The formula has the dissatisfaction effect of aggravating the well-known bias of the DR7 pipeline to underestimate the metal content of metal-rich stars. This can be seen by comparison of local stars from the Geneva-Copenhagen Survey Nordström et al. 2004 with high vertical energy, to the metallicity distribution of the SEGUE disc stars. Similarly the ugriz metallicity calibration fails to reproduce metallicities already slightly below solar metallicity as can be seen from Fig. 11 in Arnadóttir et al. 2010. The latter problem is not of major importance for the halo, but applying the formula by Carolo et al. would exacerbate metallicity-induced errors on the disc population. We estimate that distances are only weakly affected by this correction on the low metallicity side (i.e. mostly for halo stars) as the sensitivity of stellar atmospheres to the logarithmic metallicity scale gets lower. This can be seen in VandenBerg et al. 2011 or for comparison in fig. 13 of Casagrande et al. 2011.

We use the DR7 metallicities throughout the paper and do not apply the correction from Eq. (5), but checked that our findings are not significantly affected by switching the distance scale.

8.3 Deriving space velocities

The dataset contains information on magnitudes, colours, the distances, stellar parameters, radial velocities and proper motions. We can thus derive the velocities in the solar/local coordinate system by:

\[
\begin{align*}
U_v &= -d \sin(l) \dot{l} - d \cos(l) \sin(b) \dot{b} + \cos(b) \cos(l) \dot{V} \\
V_v &= d \cos(l) \dot{l} - d \sin(l) \sin(b) \dot{b} + \cos(b) \sin(l) \dot{V} \\
W_v &= d \cos(b) \dot{b} + \sin(b) \dot{V}
\end{align*}
\]

(6)

where \(l, b\) are Galactic longitude and latitude, \(l, b\) are the proper motion components in \(l\) and \(b\) and \(d\) is the assumed distance to the stars. Of special interest is the degree of support of the measurement by radial motions, which are independent of distance biases and have smaller errors. Neglecting the geometrical extension of the sample, the quantity of interest is thus the term connecting the azimuthal velocity in the heliocentric frame \(V_{\phi}\) to the line-of-sight velocity \(V_z\):

\[
\eta_v = [\cos(b) \sin(l)]
\]

(7)

The term \(\eta_v\) is 1 where the \(V_v\) velocity is measured directly from the line-of-sight velocity \(V_z\) i.e. at \(b = 0\) and \(l = 90^\circ, 270^\circ\), its contours on the sample are depicted in Fig. 11.

Due to the extension of the sample to a radius of more than 3 kpc projected on the Galactic plane a small angle approximation cannot be reliably taken. Using the Galactic rest frame velocities in heliocentric coordinate \(U_a = U_b + U_c\), \(V_a = V_b + V_c + V_G\), \(W_a = W_b + W_c\) (where \(V_G\) is the Galactic rotation speed, \(V_b, U_c, W_c\) and \(W_c\) are the components of solar motion relative to the local standard of rest) the correction from the local coordinate system can be done via the Galactic angle

\[
\alpha = \arctan\left( \frac{d \sin(l) \cos(b)}{R_{G0} - d \cos(l) \cos(b)} \right)
\]

(8)
between the line sun-centre to the line star-centre:

\[
\begin{align*}
U &= U_0 \cos \alpha - V_0 \sin \alpha \\
V &= V_0 \cos \alpha + U_0 \sin \alpha - V_G \\
W &= W_a
\end{align*}
\] (9)

Throughout the paper blank letters \(U, V, W\) denote the corrected velocities in a Galactic reference frame, which are useful for assessing kinematics. \(U_0, V_0, W_0\) denote the velocities in the rest frame of the Sun and heliocentric coordinates, which are the native setting for exploring kinematic biases.

### 8.4 Sample cleaning

The DR7 calibration sample contains 42841 spectra. The steps for cleaning the sample and the subsequent reduction of numbers are listed in Table 1, subsamples used in this work and the plots are set in bold font. However, a considerable fraction of these entries is double, i.e. stars whose spectra have been taken several times, some for observational reasons as to improve the signal to noise, some as they were both listed among the photometric calibration stars and the reddening calibration stars. Therefore it is necessary to clean DR7 samples by identifying any measurements that are within 1.5 arcsec of each other in both right ascension and declination or are within an angular distance of 3 arcsec and have a \(g\) band magnitude difference below 0.1 mag. We chose the entry that gives full information on proper motions and the latest measurement in case both contain it. This leaves 33023 unique calibration stars in our DR7 sample. The C10 sample was already cleaned by them and has the 4 kpc distance cut (according to their distances) applied, but not the cut in galactocentric radius (which we do not apply either). Hence the number of unique stars in the C10 sample is only slightly reduced when we demand a cross-match by stellar position on our DR7 table for being less than 2.5 arcsec apart both in right ascension and declination. There are some stars dropping out because of a missing cross-match and there were 52 candidate double entries with identical position in the C10 sample. Among those objects some are \(\sim 0.3\) mag fainter than their second entry and the corresponding entry in DR7. In total we found 41 stars which are \(\sim 0.3\) mag fainter in apparent magnitude than their counterparts in DR7. We checked that none of these differences has a significant impact on the results.

We also removed from the sample the stars with signal to noise ratio \(S/N < 10\) and those which are flagged by the SSPP for spectral abnormalities, for colour mismatches or for being a suspected or proven white dwarf, as well as those with particularly unreliable radial velocity measurements or SSPP parameters. We thus cleaned the C10 sample from \(\sim 1700\) flagged stars. Superficial tests did not show any obvious problems caused by those stars. Following C10, we also included all stars without determined proper motions and "clean" the sample according to Munn et al. (2004) requiring that both \(\sigma_{\text{RA}}\) and \(\sigma_{\text{DEC}}\) < 350 mas, with an additional requirement of those stars to have quoted errors in each proper motion component of \(< 5\) mas yr\(^{-1}\). We checked on the C10 sample that 224 objects in their sample not passing this cut did not cause any noticeable biases. The full cleaning gives a final DR7 sample of 28844 stars, which we will use when plotting "all" stars in DR7. In plots of the full C10 sample we use its counterpart of 21600 stars that already fulfills at their distances the condition of having all distances smaller or equal to 4 kpc.

### Table 1

| condition                     | DR7   | Carollo et al. (2010) |
|-------------------------------|-------|-----------------------|
| original sample entries       | 42841 | —                     |
| cleaned sample by C10         | —     | 23647                 |
| unique & cross-matched        | 33023 | 23553                 |
| unflagged                    | 29585 | 21819                 |
| \(S/N > 10\)                 | 29585 | —                     |
| \(4500 \leq T_{\text{eff}} \leq 7000\) | 29585 | —                     |
| \([Fe/H]_{\text{DR7}}, v_\parallel\) fine | 29585 | —                     |
| prop. motion fine             | 28844 | 21600                 |

| log(g) > 4.0                  | 17365 | 15023                 |
| log(g) > 4.1                  | 13880 | 12120                 |
| \(d_{\text{HIC}} < 4\) kpc, log(g) > 4.0 | 15808 | 14763                 |
| \(d_{\text{HIC}} < 4\) kpc, log(g) > 4.1 | 12678 | 11894                 |
| \(d_{\text{Car}} < 4\) kpc   | —     | 21600\(b\)           |
| \(d_{\text{Car}} < 4\) kpc, log(g) > 4.0 | —     | 15023\(d\)           |

Table 1. Numbers of stars at different cuts in the two samples. The quality cuts are applied cumulatively from the first row until the horizontal line. Below the horizontal line we show selected subsamples with gravity and distance cuts. The cuts down to the quality cut in proper motion are applied successively. Below the horizontal line we show the effects of different distance estimations and cuts on the number of remaining stars. Subsamples used in the paper: \(a\) "all star sample", \(b\) "Ivezic dwarfs", \(c\) Carollo dwarfs.