Eukaryotic cells are mechanically supported by a polymer network called the cytoskeleton, which consumes chemical energy to dynamically remodel its structure. Recent experiments in vivo have revealed that this remodeling occasionally happens through anomalously large displacements, reminiscent of earthquakes or avalanches. These cytoskeletal avalanches might indicate that the cytoskeleton’s structural response to a changing cellular environment is highly sensitive, and they are therefore of significant biological interest. However, the physics underlying “cytoquakes” is poorly understood. Here, we use agent-based simulations of cytoskeletal self-organization to study fluctuations in the network’s mechanical energy. We robustly observe non-Gaussian statistics and asymmetrically large rates of energy release compared to accumulation in a minimal cytoskeletal model. The large events of energy release are found to correlate with large, collective displacements of the cytoskeletal filaments. We also find that the changes in the localization of tension and the projections of the network motion onto the vibrational normal modes are asymmetrically distributed for energy release and accumulation. These results imply an avalanche-like process of slow energy storage punctuated by fast, large events of energy release involving a collective network rearrangement. We further show that mechanical instability precedes cytoquake occurrence through a machine-learning model that dynamically forecasts cytoquakes using the vibrational spectrum as input. Our results provide a connection between the cytoquake phenomenon and the network’s mechanical energy and can help guide future investigations of the cytoskeleton’s structural susceptibility.

Significance

The cytoskeleton plays a central role in mechanobiology, serving both as a scaffold to support the cell’s shape and as an engine that allows the cell to exert large-scale mechanical forces. A key feature of the cytoskeleton is that it is dynamic, continually remodeling itself to respond to changing cellular needs. We use computer simulations to study this remodeling process, primarily focusing on fluctuations in the system’s mechanical energy. We observe an avalanche-like tendency for energy to accumulate slowly in the network and then dissipate in large amounts during occasional events that involve large collective network motions. This observation is consistent with recent experiments and suggests that the cytoskeleton is highly responsive to time-varying cellular cues.

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paths (17). Dynamic instability is already an acknowledged feature of certain cytoskeletal components, such as microtubules and filopodia (18). A similar design principle may also apply to larger cytoskeletal structures to allow fast remodeling. For instance, avalanche-like dynamics may serve a useful purpose in the lamellipodia of migrating cells, which probe local chemical gradients and must quickly collapse protrusions in unsuccessful search directions, as well as adaptively remodel their structure in response to changing mechanical loads (2, 19). However, to investigate such possible biological roles, we first need a more detailed account of the underlying causes of the observed large structural rearrangements, which is the subject of this paper.

Here, we perform detailed simulations of a minimal cytoskeletal model system using the software package MEDYAN (Mechanochemical Dynamics of Active Networks) (20). Our main qualitative result is that there is a significant asymmetry between how cytoskeletal networks accumulate and release mechanical energy. While both accumulation and release statistics are heavy-tailed, the magnitudes of energy release are more broadly distributed than those of energy accumulation. Several measures of network dynamics are also found to be distributed asymmetrically for energy release and accumulation, including the network displacement, the localization of tension, and the projection of the network motion onto the vibrational normal modes. These results support an avalanche-like picture of slow energy accumulation punctuated by fast, broadly distributed events of energy release that involve a collective structural rearrangement of the network. The asymmetric energy fluctuations are found to be robust against changes in chemical concentrations and system size, suggesting that avalanches are intrinsic to cytoskeletal network dynamics. We further establish a connection between cytoquakes and mechanical instability, both through the observed spatial delocalization of tension during cytoquakes and the machine-learning-assisted ability to dynamically forecast cytoquakes using the Hessian eigenspectrum of the mechanical energy function. This implies that mechanical instability, as encoded in the Hessian eigenspectrum, precedes incipient cytoquakes, which then act to homogenize tension in the network. At the end of the paper, we pose several open questions based on these results, which can help to guide future investigations into cytoquakes and their possible physiological functions.

Results
Energy Fluctuations Are Asymmetric, Heavy-Tailed, and Self-Affine. We study a subsystem of the full cytoskeleton called an actomyosin network. This consists of semiflexible actin filaments and associated proteins, including active molecular motors (e.g., minifilaments of nonmuscle myosin II A [NMIIA]) and passive cross-linkers (e.g., α-actinin). An actomyosin network as represented in simulation is visualized in Fig. 1. The actin filaments hydrolyze adenosine triphosphate (ATP) molecules in a directed polymerization process, which reaches a steady state called “treadmilling” (21). The myosin minifilaments (~200 nm in length) transiently bind to pairs of actin filaments and also hydrolyze ATP as fuel to walk along the filaments, generating motion and mechanical stresses. These active process drive the network away from equilibrium. The cross-linkers (~35 nm) bind more stably to nearby filaments, serving to transmit the force produced by motors and to both store and, through unbinding, dissipate the resulting energy, heating the environment (22–28). Dissipation of stored mechanical energy also occurs as filaments relax out of strained configurations, in a manner that depends on mutual constraints that filaments exert on each other through bound cross-linkers and motors. Additionally, the rates of motor walking and unbinding, as well as of cross-linker unbinding, depend exponentially on the forces sustained by these molecules, giving rise to nonlinear coupling between the mechanical state of the network and its chemical propensities (29, 30). These processes by which the ability of the network to mechanically relax depends on its current state set the stage for avalanche-like dynamics.

Using MEDYAN, we performed simulations of small cytoskeletal networks consisting of 50 actin filaments in 1-µm³ hard-walled cubic boxes with varying concentrations of α-actinin cross-linkers ([α]) and of NMIIA myosin-motor minifilaments ([M]) (13, 20, 31–33). We omit here other associated proteins, such as the branching agent Arp2/3, finding that our minimal system is sufficient to produce heavy-tailed distributions of event sizes, although it has recently been discovered that branching acts to enhance avalanche-like processes (34). MEDYAN simulations combine stochastic chemical dynamics with a mechanical representation of filaments and associated proteins (see SI Appendix, Description of MEDYAN Simulation Platform for a detailed outline of the MEDYAN model). Simulations proceed...
iteratively in a cycle of four steps: 1) stochastic chemical simulation for a time $\delta t$ (here, 0.05 s), 2) computation of the resulting new forces, 3) equilibration via minimization of the mechanical energy, and 4) updating of force-sensitive reaction rates, such as slip-bonds of cross-linkers, catch-bonds of motors, and motor stalling. Recent extensions to the MEDYAN platform allow calculation of the change in the system’s Gibbs free energy during each of these steps (13, 35), originally applied to study the thermodynamic efficiency of myosin motors in converting chemical free energy to mechanical energy under various conditions of cross-linker and motor concentration. We employ this methodology here and focus on the statistics of the system’s mechanical energy $U$ as it self-organizes.

We first characterize the observed occurrence of avalanche-like dynamics in these simulations. The simulations begin with short seed filaments that quickly polymerize (tens of seconds) to their steady-state lengths. Following this, the slower process (hundreds of seconds) of primarily myosin-driven self-organization occurs, which for most conditions, results in geometric contraction to a percolated network (Movie S1) (26, 36). The mechanical energy $U(t)$ fluctuates near a quasi-steady state (QSS) value, which we analyze as a stochastic process. In Fig. 2A, we display the trajectory of $U(t)$ for condition C33 (with $\alpha$-actin concentration [C] = 2.82 $\mu$m and motor concentration $[M] = 0.04 \mu$M; see Materials and Methods for a description of the experimental conditions). We tracked the net changes of the mechanical energy $\Delta U(t) = U(t + \delta t) - U(t)$ resulting from each complete cycle of simulation steps (1)-(4). The total energy $U$ is a sum over the molecular components in the network, i.e., filaments, motors, and cross-linkers, as well as the excluded volume repulsion between nearby filaments. We show this decomposition of the energy into these components in SI Appendix, Fig. S1. For the purpose of analyzing the observed asymmetric heavy tails in the distribution of $\Delta U$, we treated the negative increments $\Delta U_-$ (energy release) and positive increments $\Delta U_+$ (energy accumulation) as samples from separate distributions with semi-infinite domains. The complementary cumulative distribution functions (CCDFs, or “tail distribution,”) the probability $P(X \geq x)$ of observing a value of the random variable $X$ above a threshold $x$, as a function of $x$ of the observed samples collected from all five runs at QSS are illustrated in Fig. 2B. Both distributions display striking heavy tails relative to a fitted half-normal distribution. The CCDFs are better fit by stretched exponential (Weibull) functions of the form (37)

$$P(X \geq x) = e^{-(x/\eta)^k}.$$  \[1\]

We justify this choice of distribution by constructing Weibull plots, as discussed in SI Appendix, Weibull Plots. We find $k = 0.60 \pm 0.06$ for $|\Delta U_-|$ and $k = 0.83 \pm 0.07$ for $\Delta U_+$ with uncertainty taken over the five runs, indicating shallower tails for energy release compared to energy accumulation. We also measured parameter $\eta$ that indicates non-Gaussianity:

$$\eta = \frac{(x^m)^m}{3 (x^m)^2} - 1,$$  \[2\]

where $(x^m)$ is the $m$th moment about zero; for a half-normal distribution $\eta = 0$, and $\eta > 0$ quantifies heavy-tailedness. We find $\eta = 11.37 \pm 5.37$ for $|\Delta U_-|$ and $\eta = 1.96 \pm 0.58$ for $\Delta U_+$. This, along with the shallower tails of the fitted stretched exponential functions, indicates greater deviation from Gaussianity for energy release compared to energy accumulation. These results support the picture that, typically, energy accumulates comparatively slowly and is released via large occasional events.

We next analyze the temporal correlations of $U(t)$ at QSS. A self-affine stochastic time series $G(t)$, for which $G(t)$ and $|\xi|^H_g G(t/\xi)$ have the same statistics for any scaling parameter $\xi$, has a power spectral density $S(f)$ exhibiting a power-law dependence on frequency $f$: $S(f) \propto f^{-\beta}$, where the spectral exponent $\beta$ is the persistence strength, related to the color of the signal (38, 39). We find $\beta = 1.72 \pm 0.02$ for $U(t)$, as shown in Fig. 2C. With this value of $\beta$, $U(t)$ is classified as a pinkish-brown signal, implying that it is nonstationary and has temporally anticorrelated increments $\Delta U$. Self-affine time series further obey the theoretical relationship $\beta = 2H_a + 1$ when $1 \leq \beta \leq 3$, where $H_a$ is the Hausdorff exponent determined from the scaling of the variogram

$$\gamma(\tau) = \frac{1}{2} \left( G(t+\tau) - G(t) \right)^2 \sim \tau^{2H_a},$$  \[3\]

and where the overbar represents temporal averaging (40, 41). We find that this relationship is satisfied by $U(t)$, as shown in Fig. 2D, yielding $H_a = 0.36 \pm 0.01$ and confirming that $U(t)$ is self-affine. Such non-Markovian and self-affine time series and spatial patterns commonly arise in various complex geophysical
processes (e.g., the temporal variation of riverbed elevation), further supporting the analogy between the cytoskeleton and earth systems (42, 43).

**Distinguishing Features of Cytoquakes.** We find that cytoquakes, defined throughout as simulation cycles for which \( \Delta U < -100 k_B T \), are correlated with several changes in the state of the network. This cutoff at \(-100 k_B T\) is chosen to lie in the tail of the distribution of \( \Delta U \) (Fig. 2), but its specific value does not significantly affect our conclusions. A discussion of the conversion of the numerical \( \Delta U \) data into discrete categories can be found in SI Appendix, Binning. In Fig. 3, we show that rare large events of energy accumulation correspond to a greater than usual number of myosin-motor steps, whereas rare large events of energy release correspond to greater than usual total displacement of the actin filaments and a slightly greater number of linker unbinding events. The displacement between filaments from \( t \) to \( t + \delta t \) is calculated by triangulating the area between the two filament configurations and dividing the area by the filament length, as described in SI Appendix, Filament Displacements. The total filament displacement at time \( t \) is computed as the sum of displacements over all filaments during the time interval \( (t, t + \delta t) \). This quantity is found to be largest during cytoquake events. Furthermore, these large total displacements do not come from highly localized motions. Instead, they depend on many filaments each displacing an unusually large amount, as shown in Fig. 4, where the filaments are ranked according to their displacement during a cycle. For cytoquake events, the typical displacement at almost every rank is greater than the corresponding displacement at that rank for other cycle types. This agrees with the notion of cytoquakes as a large and collective structural rearrangement of the network.

We also observed cytoquakes to induce a spatial homogenization of the tension sustained by the network during large events of energy release, as quantified by changes in the Shannon entropy of the spatial tension distribution \( H(t) \) (Fig. 3D). The tension distribution \( P_{\Delta T} \) is constructed by discretizing the simulation volume of \( 1 \) \( \mu \)m\(^3\) into a grid of \( 10^3 \) voxels indexed by \( i, j, k \) and computing the proportion of the total network tension belonging to the mechanical elements (filament cylinders, cross-linkers, and motors) inside each voxel. Additional details for the calculation of \( H(t) \) can be found in Materials and Methods. The combination of large, collective rearrangement and a spatial homogenization of tension supports the interpretation of cytoquakes as an avalanche-like event of energy release.

**Asymmetric Statistics Are Robust across Concentrations and System Size.** We next discuss how these results generalize to different concentrations of associated proteins and different system sizes.

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Fig. 3. (A) Differences in the total filament displacement between simulation cycles for which \( \Delta U < -100 k_B T \), cycles for which \( \Delta U \in (0 k_B T, 100 k_B T) \), and finally, cycles for which \( \Delta U > 100 k_B T \). To compare these distributions, we first performed a Kruskal-Wallis test on the group, which indicated statistically significant between-group differences. A post hoc two-sided Wilcoxon rank-sum test was then performed on pairs of distributions using a Bonferroni correction factor of 6 on the significance level to account for multiple comparisons. The corrected \( P \) value of the Wilcoxon rank sum test between pairs of cycle types is reported as follows: ‘not significant \((P \geq 0.05)\); *significant at level 1 \((P < 0.05)\); **significant at level 2 \((P < 0.01)\); ***significant at level 3 \((P < 0.001)\) (44). The red bar of the box plots represent the median, and the scatter-plot data represent detected outliers. (B) Differences in the number of motor walking events between the different cycle types as just described. (C) Differences in the number of linker unbinding events between the different cycle types. (D) Differences in the changes in Shannon entropy \( \Delta H \) of the spatial tension distribution of network tension between the different cycle types.
sizes. Five concentrations of α-actinin (ranging from 0.17 to 5.48 μM) and five concentrations of myosin minibundles (ranging from 0.003 to 0.08 μM) were tested with a constant G-actin monomer concentration of 13.3 μM, in the regime of physiological concentrations (45). At the lowest concentrations of cross-linkers and motors, the network did not contract, representing a very different actomyosin phase, to which we omit comparisons. For all of the conditions producing contracting networks, we found that asymmetric heavy-tailed distributions of ∆U persist, with large values of the non-Gaussian parameter for |∆U| (η = 3 - 5) and ∆U (η = 2 - 5), although η for negative increments was observed to decrease with the motor concentration (SI Appendix, Fig. S2). We conclude that the avalanche-like energy fluctuations discussed above are not highly sensitive to associated protein concentrations. These fluctuations may depend on the parameters of the force-sensitive reaction rates (which are taken here to correspond to experimental values), but we leave this interesting question for future work.

We performed a finite-size scaling study by holding the concentrations of condition C5,3 fixed (with α-actinin concentration [α] = 2.82 μM and motor concentration [M] = 0.04 μM) and varying the system volume V. Larger systems reach QSS at later times, and our simulations of larger systems did not reach QSS in the allotted computational time. As a result, we collected samples of ∆U for these systems on the approach to QSS, from 300 to 800 s, once the networks had all nearly fully percolated (i.e., nearly all filaments belonged to a single component connected by cross-linkers) and the relevant scaling behavior could still be observed. Stretch exponential functions approximately fit the distributions of ∆U and ∆U (for all system sizes (see Fig. 5A for the fits of |∆U|)). Larger systems displayed steeper tails, as indicated by the observed power-law decay of η for |∆U| and ∆U (Fig. S5B), although, interestingly, η for |∆U| was larger than that for ∆U by a constant factor of roughly 3 for all systems sizes. The steeper tails were also evidenced by the slow growth of the Kohlrausch exponents k with V (Fig. 5C). Thus, the distributions of energy release and accumulation across the entire network become narrower and more Gaussian for large systems. This, in contrast to driven-dissipative systems that exhibit self-organized criticality (SOC), suggests the existence of some intrinsic and finite scale for avalanche-like releases of energy in cytoskeletal networks. By summing over many local energy fluctuations of this finite scale, the distribution of the fluctuations in the total energy U becomes increasingly Gaussian for large systems, owing to the central limit theorem. This intrinsic scale may be partly determined by the nonconservative transfer (dissipation) of mechanical energy as it spreads through the network during avalanches (24, 46).

**Local vs. Global Metrics.** Existing experimental studies of cytoquakes define them as large local displacements of the cytoskeleton probed using transmembrane-attached microbeads or flexible micropost arrays, rather than as large changes in the cytoskeleton’s total energy, U, as done here (9, 10). To roughly compare our results to experiments, we made the corresponding predictions of the displacements of individual filaments. Rather than summing over all filaments, we tracked each filament individually and measured the set {ηf}t=1Nf (where Nf = 50 is the number of filaments) of the non-Gaussian parameter ηf corresponding to each filament f’s distribution of displacements from 300 to 800 s. The calculation of filament displacements is described in SI Appendix, Filament Displacements. We find that the resulting distributions are heavy-tailed with values of the non-Gaussian parameter for most filaments in the range η ∼ 1 - 5 (Fig. 6). This finding is in semiquantitative agreement with in vivo measurements on micropost arrays, whose displacements have distributions characterized by η ∼ 0 - 7 (10).

We first add the distribution of η itself to be heavy-tailed, also in agreement with the micropost experiments. We next estimated the instantaneous filament speed as the filament displacement divided by ∆t. We find the typical actin filament displacement speeds (∼ 10 nm/s) to be consistent in order of magnitude with separate in vitro experiments on ordered, contractile networks, which estimate this speed as ∼ 10 - 50 nm/s (47). These corroborations with existing measurements suggest that our simulations of a minimal cytoskeletal model system can approximately reproduce experimentally observed cytoskeletal dynamics. We finally mention in connection to experiments that it has recently been argued that more detailed understanding of mechanical dissipation by cytoskeletal networks should help to precisely control traction-based measurements of cellular force production (28). The discovery of avalanche-like dynamics in cytoskeletal networks reported in this and previous studies may help to resolve this experimental difficulty.

The local measurements {ηf}t=1Nf, obtained by tracking each filament individually, can be compared to global measurements, obtained by summing over every filament to obtain the total displacement. The distribution of total displacements is closer to Gaussian, characterized by η ≈ 0 for most volumes tested (Fig. 6). As with the increasing Gaussianity of ∆U for large systems, this can be attributed to the central limit theorem since many filaments were summed over to determine the total displacement. We conclude that in large systems, metrics can be heavy-tailed when measured locally, but Gaussian when measured globally. This distinction between local and global measurements may be important in interpreting future studies of anomalous statistics in cytoskeletal self-organization.

**Normal Mode Decomposition Probes Network’s Mechanical State.** Having described the statistics of the increments ∆U, we next aimed to connect the occurrence of cytoquakes, defined as large values of |∆U|, to the cytoskeletal network’s mechanical stability. To this end, we implemented a method to compute the Hessian matrix $\mathcal{H}$ of the mechanical energy function U. The
Fig. 5. (A) CCDFs of $|\Delta U_\perp|$ normalized by the system volume $V$ collected for five runs for increasing system sizes plotted against the fitted stretched exponential functions. (B) The non-Gaussian parameters $\eta$ for $|\Delta U_\perp|$ and $\Delta U_\parallel$ are plotted with uncertainty taken over the different runs. (C) The Kohlrausch exponents $k$ for $|\Delta U_\perp|$ and $\Delta U_\parallel$.

eigen-decomposition of $H$ is $\Lambda = \{\lambda_k\}_{k=1}^{3N}$, where $3N$ is the number of mechanical degrees of freedom in the system, which comprises $N$ “beads” that are used to discretize the actin filaments. $\Lambda$ is related to the mechanical stability of the cytoskeletal network: The eigenvectors $v_k$ are the normal vibrational modes of the network, and the eigenvalues $\lambda_k$ indicate the stiffness ($|\lambda_k|$) and stability (sgn($\lambda_k$)) of the corresponding mode. Example vibrational modes are illustrated in Movies S2–S5. We drew inspiration for studying $\Lambda$ in the current context from several sources: In single-molecule molecular dynamics studies, the saddle points of $U$ (i.e., points in the landscape with some imaginary frequencies) are associated with transition states (48, 49); studies of polymer networks show that internal stresses produce nonfloppy vibrational modes, even below the isostatic threshold (50); in simulations of glass-forming liquids, the instantaneous normal-mode spectrum allows inference about proximity to the threshold (here 1 pN); this is expected, as it is known from the theory of minimizing loss functions that the ratio of saddle points to true local minima increases exponentially with the dimensionality of the domain (56). We expect that in the space of all possible network topologies (i.e., patterns of cross-linkers and motors binding to filaments), the energy landscape will be rugged, leading to the well-appreciated glassy dynamics of nonequilibrium cross-linked networks (57, 58). For a fixed topology, however, which is the result of the chemical reactions occurring during step (1) of the iterative simulation cycle, the energy landscape should be smooth (i.e., not rugged) with respect to the beads’ positions, with a single nearby local minimum being sought during mechanical minimization in step (3). The residual unstable modes are therefore thought to be an unimportant artifact of thresholded stopping in the conjugate-gradient minimization routine, and not representative of some physical feature of cytoskeletal networks. The observed quantitative dependence of the number of residual unstable modes on $F_T$ supports this conclusion and is illustrated in SI Appendix, Fig. S11.

We quantify the number of degrees of freedom involved in a given normalized eigenvector $v_k$ using the inverse participation ratio (51):

$$r_k = \left( \sum_{i=1}^{N} \sum_{\mu=1}^{3} (v_{k,i\mu})^4 \right)^{-1}. \quad [4]$$

If the eigenmode involves only one degree of freedom, then one component of $v_k$ will be one and the rest will be zero, and $r_k = 1$. 

We briefly digress from the results on cytoquakes to describe some interesting observed trends of metrics defined on $\Lambda$. We distinguish between unstable, stable, soft, and stiff modes: For unstable modes, $\lambda_k < 0$; for stable modes, $\lambda_k \geq 0$, for soft modes $0 \leq \lambda_k < \lambda_T$, and for stiff modes, $\lambda_k \geq \lambda_T$, where we define the threshold $\lambda_T = 40$ pN nm to discriminate between the twin peaks in the density of states (Fig. 7B). The set $\{\lambda_i\}_{i=1}^{3N}$ is visualized with these modes labeled in Fig. 7A for a QSS time point of condition $C_{3,3}$. A very small number of unstable modes persist after each minimization cycle, later iterations stopping once the maximum force on any bead in the network is below a threshold $F_T$ (here 1 pN). Thus, the minimized configurations are, in fact, saddle points of $U$; this is expected, as it is known from the theory of minimizing loss functions that the ratio of saddle points to true local minima increases exponentially with the dimensionality of the domain (56). We expect that in the space of all possible network topologies (i.e., patterns of cross-linkers and motors binding to filaments), the energy landscape will be rugged, leading to the well-appreciated glassy dynamics of nonequilibrium cross-linked networks (57, 58). For a fixed topology, however, which is the result of the chemical reactions occurring during step (1) of the iterative simulation cycle, the energy landscape should be smooth (i.e., not rugged) with respect to the beads’ positions, with a single nearby local minimum being sought during mechanical minimization in step (3). The residual unstable modes are therefore thought to be an unimportant artifact of thresholded stopping in the conjugate-gradient minimization routine, and not representative of some physical feature of cytoskeletal networks. The observed quantitative dependence of the number of residual unstable modes on $F_T$ supports this conclusion and is illustrated in SI Appendix, Fig. S11.
be interesting to investigate in future work how these two aspects of actomyosin networks are interrelated. It may be the case that heavy tails in the distribution of network connectivity can allow for heavier tails in the distribution of $\Delta U$.

We observed that as a network contracts and becomes percolated during the process of myosin-driven self-organization, the stable modes steadily delocalize ($\langle r \rangle$ increases) and stiffen (the geometric mean $\langle \lambda \rangle$ increases), as shown in Fig. 7 E and F. During this process, we also witnessed a qualitative change in the level-spacing statistics of the very soft and delocalized modes ($\lambda_1 < 10 \text{ pN} \cdot \text{nm}$, $r_1 > 100$) from a Poisson to a Wigner–Dyson distribution (SI Appendix, Fig. S3). This indicates that in the percolated state, these vibrational modes interact and exhibit level repulsion, similar to soft particles near the jamming transition (10, 14, 62, 63). Future studies may reveal further similarities between these systems and other marginally stable solids (58, 64).

**Cytoquakes Are Preceded by Mechanical Instability and Deform along Soft Modes.** Can the eigen-decomposition of the Hessian matrix be used to forecast cytoquake occurrence? Intuition suggests that, by analogy with the connection between imaginary frequencies (i.e., unstable modes) and molecular transition states, the vibrational modes of the cytoskeletal network may contain information that a large structural rearrangement is poised to occur (48, 49). To test this idea, and without detailed a priori knowledge about which features in $\Lambda$ would be informative, we implemented a machine-learning model using the eigen-decomposition as the input and outputting the predicted probability of observing a large event of energy release ($\Delta U < -100 \text{ k}_B T$) occurring within the next 0.15 s. As detailed in SI Appendix, Machine Learning Model, we found that, indeed, the Hessian eigenspectrum $\Lambda$ contains sufficient information to forecast cytoquake occurrence with significant accuracy compared to a random model. We first reduced the dimensionality of $\Lambda(t)$ using principal component analysis, finding that 30 dimensions sufficed to explain >95% of the variance across time points, and then used the reduced input in a three-layer feed-forward neural network. We validated our model using receiver operating characteristic curves, achieving an area under the curve (AUC) of 0.70 when using data from five runs of condition C1,3. This improvement in prediction performance over a random model (which would have an AUC of 0.5) implies that mechanical instability, as encoded in the Hessian eigenspectrum, precedes the occurrence of cytoquakes.

To further study the connection between cytoquakes and mechanical stability, we measured the projections of the network’s displacements onto the vibrational normal modes $\{v_k\}_{k=1}^{3N}$. Network displacements $\mathbf{d}(t)$ were found by tracking the movement of each of the $N(t)$ beads during simulation cycles. As a working approximation, beads that depolymerized during a cycle were assigned a displacement of zero, and beads that newly polymerized were not assigned elements in $\mathbf{d}(t)$. The $3N$-dimensional displacement vectors $\mathbf{d}$ were then normalized to have unit length. We define

$$d_k = \mathbf{d} \cdot v_k, \quad [5]$$

as the projections of $\mathbf{d}$ onto the eigenmodes $v_k$, which obey $\sum_k d_k^2 = 1$ owing to the normalization of $\mathbf{d}$ and $v_k$. Thus, the quantity $d_k^2$ is the weight of the displacement $\mathbf{d}$ along the $k$th eigenmode. With this, we define the effective stiffness

$$\lambda_\rho = \sum_k d_k^2 \lambda_k, \quad [6]$$

as the displacement-weighted average of the eigenvalues. In Fig. 8, we display a scatter plot of the pairs $\Delta U(t)$, $\lambda_\rho(t)$ measured

![Fig. 6. Plots for different simulation volumes $V$ of the distributions of non-Gaussian parameter $\eta$ of the distributions of individual filament displacements. The box and whisker plots summarize the distribution of $\eta$ for all filaments in the system, with the median shown as a red bar, the box extending from the first to the third quartiles, and the whiskers extending across the range of $\eta$, omitting outliers. The black diamonds indicate the value of $\eta$ obtained when instead of tracking each filament’s displacement individually, the total summed displacement of all filaments from time point to time point is tracked. These global measurements of displacement are more Gaussian (with $\eta \approx 0$) than the corresponding local measurements obtained from tracking filaments individually.](https://doi.org/10.1073/pnas.2110239118)
Fig. 7. Metrics defined on Hessian eigen-decomposition. (A) Ordered eigenspectrum \( \{ \lambda_k \}_{k=1}^{\infty} \) at a QSS time point for condition \( C_{3,3} \). (B) Scatter plot of the pairs \( |\lambda_k|, r_k \) (circles) plotted against the density of states (solid line), i.e., the proportion of eigenvalues between \( \lambda \) and \( \lambda + d\lambda \). (C) The mean value at QSS of \( \langle r \rangle \) for the stable modes for various conditions \( C_{ij} \). The conditions \( C_{ij} \) with low linker concentrations are not visualized, as these networks did not percolate and obscure visualization for the remaining conditions. The mean is taken over the last 500 s and over different runs. (D) The mean value of the mean node connectivity for various conditions. (E) Trajectories of \( \langle r \rangle \) of the stable modes as the network self-organizes for the conditions \( C_{2,3}, C_{3,3}, C_{4,3}, \) and \( C_{5,3} \), where the color indicates the \( \alpha \)-actinin concentration as in D, and with the mean and SD taken over the different runs. (F) Similar trajectories of the geometric mean of the stable modes \( \langle \lambda \rangle_g \) during QSS for a run of condition \( C_{3,3} \), along with a kernel density estimate of their joint probability density function (PDF). We again distinguish between soft \( (0 \leq \lambda_k < \lambda_T) \) and stiff \( (\lambda_k \geq \lambda_T) \) eigenmodes, where \( \lambda_T = 40 \) pN·nm separates the twin peaks in the density of states (Fig. 7B). The structure of the joint PDF is markedly asymmetric about \( \Delta U = 0 \) and shows that \( \lambda_P \) during cytoquake events is almost always soft, whereas for all other simulation cycles, \( \lambda_P \) could be soft or stiff with similar probabilities. Because soft modes inherently involve a large number of degrees of freedom, as illustrated in Fig. 7B, we also consider

\[
\eta_k = \frac{d_k^2}{r_k} \tag{7}
\]
as the weight of the displacement along eigenmode \( k \) per degree of freedom involved in the eigenmode, where \( r_k \) is the inverse participation ratio defined in Eq. 4. We define \( \eta_{\text{soft}} \) and \( \eta_{\text{stiff}} \) as the mean of \( \eta_k \) over the soft and stiff subsets. Values of \( \eta_{\text{soft}} / \eta_{\text{stiff}} \) for different simulation cycle types are displayed in Fig. 8, Inset, showing that \( \eta_{\text{soft}} > \eta_{\text{stiff}} \) typically only during cytoquakes. Based on this analysis, we conclude that during the large collective rearrangements corresponding to cytoquakes, cytoskeletal networks exhibit enhanced displacement along the soft vibrational modes. We qualify these results by observing that, since cytoquakes involve particularly large network displacements, it may be inappropriate to interpret them using the local harmonic approximation to \( U \) implicit in Hessian analysis (53). In addition,
process, giving $\beta = 3$ for the signal. The observed distribution of $|\Delta U|$ for this system size is fit by a stretched exponential function and has $\beta = 1.72$. Further, the distributions of $|\Delta U|$ become increasingly Gaussian for large system sizes (Fig. 5). We thus conclude that cytoskeletal networks for these physiological conditions display noncritical dynamics, at least as measured by using the global energy release $|\Delta U|$. The motor walking in the system may not be sufficiently slow to yield SOC behavior which requires a sharp separation of time scales between slow driving and fast dissipation, and the nonconservative transfer of mechanical energy between network components may also play a role (13, 24, 46, 67, 68). We note, however, that recent studies have indicated that branched cytoskeletal networks polymerizing against a flexible membrane can produce shape fluctuations of the membrane that exhibit true SOC, leaving open the question of whether criticality is an inherent feature of cytoskeletal dynamics (69, 70).

Instead of scale-free fluctuations, we conjecture that there exists a finite and intrinsic scale for avalanche-like releases of energy that, when summed over sufficiently large systems to obtain the global measure $|\Delta U|$, yields an approximately Gaussian distribution (Fig. 5). An important next question is then what sets this scale and how it may be measured. We expect that the nonconservative transfer of mechanical energy through the network is one factor that attenuates the avalanches. This nonconservation of mechanical energy arises from damping by the cytosol, accounted for in simulation through periodic minimization of the energy following stochastic chemical activity (SI Appendix, Description of MEDYAN Simulation Platform). In the lattice-based Olami–Feder–Christensen model of earthquake systems, nonconservation of energy was shown to introduce a stretched exponential cutoff to the power-law distribution of event sizes, supporting this idea (46, 71). A rough estimate of the intrinsic energy scale of avalanches can be obtained from the SD of the approximately Gaussian distributions of $|\Delta U|$ for large systems. However, a detailed measurement of the spatiotemporal scale will require spatially resolving the measured energy fluctuations, which was not done in this study. In addition, in this study, the temporal extent of avalanches was assumed fixed at the smallest resolved time interval $\delta t = 0.05$ s (see SI Appendix, Dependence on $\delta t$ and $\tau_F$ for a discussion of how varying $\delta t$ affects the distribution of $|\Delta U|$). Characterizing in-depth the spatiotemporal scales of avalanches is thus an important avenue for future work.

In addition to the question of what characterizes the spatiotemporal scale of cytoskeletal avalanches, several other open questions can be posed, based on the results presented here. First, we may ask about the role of force-sensitive reaction rates, including cross-linker unbinding and motor walking and unbinding, in modulating cytoquakes (see SI Appendix, Description of MEDYAN Simulation Platform for details of these reactions). The nonlinear coupling introduced by this force sensitivity between the local tensions in the network and the local relaxation propensities is expected to strongly accentuate avalanche-like dynamics, but in this study, we held the force-sensitive reaction-rate parameters fixed at their physiological values. It would also be interesting to vary the mechanical and geometrical properties of the network, such as the molecular elastic constants and the typical length of the myosin motors. A phase diagram over these parameters would help elucidate the conditions leading to avalanches and how the cell might modulate their occurrence, e.g., by localizing different myosin isoforms to different regions of the cell. Second, we may ask whether the harmonic approximation to the energy implicit in Hessian minimization of the energy following stochastic chemical activity (SI Appendix, Description of MEDYAN Simulation Platform) is correct. This approximation is based on the assumption that the energy is a quadratic function of the deformation, and it is known that this assumption is not always valid (57). A more accurate description of the energy landscape would require a more detailed analysis of the anharmonicity of cytoquake motions, which requires the consideration of higher-order terms in the Taylor expansion of the energy.

Changes in network topology from linker and motor (un)binding cannot be captured using normal mode decomposition of instantaneous network configurations. The eigenspectrum $A(t)$ still informs on the stability of the energy-minimized configuration before a cytoquake, but caution should be used in interpreting the cytoquake motion from $t$ to $t + \delta t$ as decomposing cleanly into noninteracting motions along the normal modes $v_n$. We leave a detailed analysis of the anharmonicity of cytoquake deformations to future work.

Discussion

We have presented evidence supporting the following picture of active cytoskeletal network self-organization: Cytoskeletal networks explore a rugged mechanical energy landscape in a stochastic process characterized by occasional, sudden jumps out of metastable configurations (57, 58). These jumps entail non-Gaussian dissipation of mechanical energy and are accomplished by an avalanche-like process of spreading destabilization, resulting in a collective structural rearrangement and a homogenization of tension. These collective motions have large projections along the soft, delocalized vibrational modes, and, furthermore, properties of these modes can be used to predict when such relaxation events will occur. The key finding supporting the interpretation of cytoskeletal dynamics as avalanche-like is the marked asymmetry about zero in the distribution of $\Delta U$ (Figs. 2B and 5B and C). In addition, several key quantities, including filament displacements (Figs. 3A and 4), tension delocalization (Fig. 3D), and effective stiffness of the motion (Fig. 8), are distributed asymmetrically about $\Delta U = 0$, supporting the picture described above.

An interesting possible interpretation of the heavy tails of $|\Delta U|$ is that cytoskeletal networks are at a point of SOC (40, 41, 65–67). Technical definitions of what constitutes SOC behavior are not universally agreed upon, but we may follow the definition of ref. 41, which states that SOC systems must have event-size distributions that tend to a power law in the limit of an infinite system size and a temporal signal that integrates a pink noise signal into noninteracting motions along the normal modes $v_n$. The motor walking in the system may not be sufficiently slow to yield SOC behavior which requires a sharp separation of time scales between slow driving and fast dissipation, and the nonconservative transfer of mechanical energy between network components may also play a role (13, 24, 46, 67, 68). We note, however, that recent studies have indicated that branched cytoskeletal networks polymerizing against a flexible membrane can produce shape fluctuations of the membrane that exhibit true SOC, leaving open the question of whether criticality is an inherent feature of cytoskeletal dynamics (69, 70).
events and energy-accumulation events (Fig. 8), and a neural network model detected correlations between the Hessian eigen-spectrum and the time-varying likelihood for a cytoquake to occur (SI Appendix, Machine Learning Model). However, as cytoquakes are, by definition, large deformations of the network, we expect that the quadratic approximation will fail to accu-rately describe the energy landscape around a cytoquake event. Higher-order terms in the energy expansion or recently intro-duced nonlinear metrics of the local energy landscape, such as the “flatness parameter,” may be used in future computa-tional investigations (53, 72). Third, we may ask about the role of thermal noise in inducing cytoquake events. In this study, thermal noise enters in the stochastic nonequilibrium chemical dynamics, which are simulated by using a variant of the Gille-spie algorithm over a reaction–diffusion compartment grid (13). However, the mechanical minimization routine is deterministic given the instantaneous chemical state of the network. Chemical reactions including motor walking and filament polymerization are expected to contribute the dominant structural fluctuations in these far-from-equilibrium networks, but the neglected diffu-sive motion of the filaments should also help the network escape from metastable configurations and modulate the frequency and scale of avalanches. Elucidating whether cytoquakes can be ther-mally activated in this way remains another open direction for future work.

Finally, perhaps the most interesting open question regarding cytoquakes pertains to their possible physiological role in cell biology. We proposed here that cytoquakes may be com-itant with a large structural susceptibility, by analogy with well-studied systems like the Ising model that have large sus-ceptibilities to applied fields near their critical point (17, 73). In this argument, the cytoskeleton may undergo large struc-tural changes in response to small changes in the relevant mechanical or chemical signals, an amplification that would serve to enhance cellular sensitivity during dynamic processes, such as chemotaxis. This could also enhance mechanical adaptiv-ity, an increasingly well-documented feature of cytoskeletal networks (19, 74–76). This connection between large cytoskele-tal fluctuations and large susceptibility remains speculative at this stage, however, and would benefit from dedicated study. Recent work has suggested that the branching agent Arp2/3, which was not included in the minimal model studied here, can enhance cytoquake sizes (34). One can ask if by tun-ing the strength of this or other cytoquake-modulating factors, the network is more or less responsive to external perturba-tion. This perturbation could be introduced either mechan-ically, for example, through a simulated or real-force microscopy experiment, or chemically, through a variation of the chemical boundary conditions (33). Such studies should clarify whether large events in cytoskeletal dynamics serve a biologically useful purpose.

Materials and Methods

Simulation Setup and Conditions. To computationally study cytoskeletal networks at high spatiotemporal resolution, we used the simulation platform MEDYAN (13, 20, 31–33). We provide an in-depth discussion of how MEDYAN works in SI Appendix, Description of MEDYAN Simula-tion Platform. MEDYAN simulations combine stochastic chemical dynamics with a mechanical representation of filaments and associated proteins. Simulations move forward in time by iterating through a cycle of four steps: 1) a short burst of stochastic chemical simulation using a variant of the Gillespie algorithm for a time $\delta t$, 2) computation of the new forces resulting from the reactions in step 1), 3) equilibration of the network via minimization of the mechanical energy, and 4) updating of force-sensitive reaction rates. This protocol reflects an assumed separa-tion of time scales between the slow chemical dynamics and the fast mechanical response, such that the mechanical subsystem is assumed to always remain near equilibrium and to adiabatically follow the chemical changes in the network. As argued in ref. 20, supported using exper-imental evidence from refs. 22, 77, and 78, this time-scale separation holds for typical cytoskeletal networks that experience localized force deformations with fast relaxation times compared to the typical waiting time between myosin-motor walking steps and filament-growth-induced deformations.

We performed MEDYAN simulations of small cytoskeletal networks consisting of 50 actin filaments in 1-$\mu$m$^3$ cubic boxes with varying concen-trations of $\alpha$-actinin cross-linkers ($\ell_{\alpha}^i$) and of NMIIA minifilaments ($\ell_{\beta}^i$). The boundaries of the box exert an exponentially repulsive force against the filaments with a short screening length of 2.7 nm. Five concentra-tions of $\alpha$-actinin (ranging from 0.17 to 5.48 $\mu$m) and five concentrations of myosin minifilaments (ranging from 0.003 to 0.08 $\mu$m) were used with a constant G-actin monomer concentration of 13.3 $\mu$m, in the regime of physiological concentrations (45). This led to a steady-state filament-length distribution with mean 0.48 $\mu$m and SD 0.26 $\mu$m. We label these conditions $C_{ij}$, where $i = 1, \ldots, 5$ represents the rank of the cross-linker concentration and $j = 1, \ldots, 5$ represents the rank of the myosin-motor concentration. Five runs of each condition $C_{ij}$ were simulated, each for 2,000 s. The length of the simulation cycle $\delta t$ was chosen as 0.05 s for the results presented in this paper, although we explore dependence on this parameter in SI Appendix, Dependence on $\delta t$ and $F_r$.

Entropy of Spatial Tension Distribution. The simulation volume of 1 $\mu$m$^3$ is discretized into $10^3$ cubic voxels, each 0.1 $\mu$m in linear dimension. Let $i$, $j$, $k = 1, \ldots, 10$ index these voxels, which are an analysis tool and not related to the reaction–diffusion compartments used in MEDYAN. After each simu-lation cycle, the mechanical components of the cytoskeletal network (i.e., the filament cylinders, the myosin motors, and the passive cross-linkers) are each under some compressive or tensile force $T_{\alpha}^j$, where $n$ indexes the mechanical component. There are other mechanical potentials involving these components, but we focus here only on the tensions $T_{\alpha}$. Each mechan-ical component has a center of mass $r_n$ and we define the indicator function $\chi_{jk}(r_n)$, which is equal to one if $r_n$ is inside voxel $i$, $j$, $k$ and zero otherwise. The total tension magnitude inside voxel $i$, $j$, $k$ is

$$|T|_{ijk} = \sum_{\alpha} T_{\alpha}^j \chi_{jk}(r_n).$$

The discrete nonnegative scalar field $|T|_{ijk}$ is converted to a distribution $P_{ijk}$ by normalization:

$$P_{ijk} = \frac{|T|_{ijk}}{\sum_{\alpha} |T|_{ijk}}.$$  

Finally, we introduce the discrete Shannon entropy of this distribution at time $t$ as

$$H(t) = -\sum_{\alpha} P_{ijk}(t) \log P_{ijk}(t).$$

The units of $H$ are nats, and large values indicate a uniform spatial distribu-tion of tension magnitudes throughout the network. Reported trends using this metric are found to be essentially independent of the discretization length.

Constructing the Hessian Matrix. In MEDYAN, semiflexible filaments are repre-sented as a connected sequence of thin cylinders whose joined endpoints (i.e., hinges) are called beads. The set of potentials defining the mechanical energy of the filaments and associated proteins is outlined in SI Appendix, Description of MEDYAN Simulation Platform. The mechanical energy $U$ is a function of these beads’ positions, and elements of the Hessian matrix are defined as

$$H_{\alpha\beta} = \frac{\partial^2 U}{\partial x_{\alpha} \partial x_{\beta}} = \frac{\partial^2 U}{\partial y_{\alpha} \partial y_{\beta}} = \frac{\partial^2 U}{\partial z_{\alpha} \partial z_{\beta}},$$

where $x_{\alpha}$ is the $\alpha$th Cartesian component of the position of the $\alpha$th bead. We have $\mu = x, y, z$ and $i = 1, \ldots, N$, where $N$ is the number of beads in the network, so $H$ is a square symmetric 3N-dimensional matrix. The number of beads $N(t)$ will change as filaments (de)polymerize; in these simulations, at QS, a single filament of length 0.5 $\mu$m comprises ~10 cylinders (11 beads),
each ~50 nm in length. After each mechanical minimization, \( H(t) \) is constructed by numerically computing the derivatives on the right of Eq. 11. The derivative \( \frac{\partial H}{\partial t} \) is found by using a second-order central difference approximation by moving the \( j \)th bead in the \( \pm v \) directions by a small amount and determining the changes in the force component \( F_j \) (79). Due to issues of numerical precision, we do not assume the symmetry of the matrix \( H \), but instead directly compute each component \( H_{j,k} \), and then symmetrize the result: \( \frac{1}{2}(H + H^T) \rightarrow H \).

Data Availability. Trajectories from numerical simulations have been deposited in the Digital Repository at the University of Maryland (DRUM) (80).

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