Crystal structure of $\eta''$-Fe$_3$Al$_{7+x}$ determined by single-crystal synchrotron X-ray diffraction combined with scanning transmission electron microscopy

Norihiko L. Okamoto$^{a,b,c}$, Masaya Higashi$^a$ and Haruyuki Inui$^{a,b}$

$^a$Department of Materials Science and Engineering, Kyoto University, Kyoto, Japan; $^b$Center for Elements Strategy Initiative for Structural Materials (ESISM), Kyoto University, Kyoto, Japan; $^c$Institute for Materials Research, Tohoku University, Sendai, Japan

ABSTRACT
The crystal structure of $\eta''$-Fe$_3$Al$_{7+x}$, the low-temperature phase of $\eta$-Fe$_2$Al$_5$ with a composition on the Fe-rich side of the solid solubility range, has been determined by synchrotron X-ray single-crystal diffraction combined with scanning transmission electron microscopy. The $\eta''$ phase possesses commensurate long-period-ordered superlattice structures (space group $Pmcn$) based on the parent orthorhombic unit cell of $\eta$-Fe$_2$Al$_5$, consisting of twin domains (orientation variants) alternately stacked along the long-periodicity axis. Each of the twin domains possesses a motif structure belonging to the base-centered monoclinic space group $C2/m$, with a cell volume twice that of the parent orthorhombic unit cell (space group $Cmcm$). One-fourth of the $c$-axis chain sites corresponding to Al$_2$- and Al$_3$-sites in the $\eta$ phase are respectively occupied by both Fe and Al atoms and exclusively by Al atoms in a regular manner. This regularity is disturbed in the twin-boundary region, giving rise to structural/compositional modulation. Because of the different chemical compositions between the motif structure and twin-boundary region, the $\eta''$ phase with various compositions can be constructed only by changing the number of the parent orthorhombic unit cells to be stacked along the orthorhombic $c$-axis, without changing the atomic arrangements for the motif structure or the twin boundary to account for the observed solid solubility range. The chemical formula of the $\eta''$ phase can thus be expressed as Fe$_3$Al$_{7+x}$ under a simple assumption on the occupancies for Al/Fe atoms in the $c$-axis chain sites.

ARTICLE HISTORY
Received 7 March 2019
Revised 26 April 2019
Accepted 26 April 2019

KEYWORDS
Intermetallic compound; superlattice structure; orientation variants; nanoscale twins; icosahedron

CLASSIFICATION
10 Engineering and Structural materials; 106 Metallic materials; 212 Surface and interfaces; 302 Crystallization / Heat treatment / Crystal growth; 503 TEM, STEM, SEM; 504 X-ray / Neutron diffraction and scattering

1. Introduction
Aluminized steels have received increasing attention in recent years, because of their excellent resistance to corrosion and oxidation at high temperatures as well as high optical reflectivity, leading to good design properties. They have been widely used in fields such as automobile exhaust systems, household appliances, and building materials in severe environments that Zn-coated steels cannot tolerate [1–6]. The global depletion of Zn resource
has also driven the transition from Zn- to Al-coated steels [7,8]. Hot-dip aluminized steels are produced by immersing steel strips into a molten Al or Al-Si bath, followed by heat treatment to alloy the Al coating over the Fe substrate through thermal diffusion. A thin aluminum oxide layer formed on top of the coating is believed to act as a diffusion and thermal barrier, enhancing the corrosion and thermal resistance [2,3]. Below the aluminum oxide layer, the brittle intermetallic compound \( \eta - Fe_2Al_3 \) forms as the major phase in the reaction layer, especially when the molten bath is pure Al, exhibiting a columnar texture elongated along its orthorhombic [001] direction [9–11]. Therefore, the \( \eta - Fe_2Al_3 \) phase is expected to play a decisive role in determining the mechanical and other properties of hot-dip aluminized steels [12,13]. Furthermore, the \( \eta - Fe_2Al_3 \) phase is also known to act as an inhibition layer during the galvanizing/galvannealing process to suppress the excessively rapid reaction of the Zn coating with the Fe substrate [14]. Thus, understanding the structural [11,15,16], thermodynamic [17–21], and mechanical [9,12,13] properties of \( \eta - Fe_2Al_3 \) is indispensable for the development of Al- and Zn-coated steels.

According to Burkhardt et al. [15], the crystal structure of \( \eta - Fe_2Al_3 \) belongs to the orthorhombic space group \( Cmcm \), consisting of an FeAl2 framework structure (Fe and Al1 sites with full occupancies) and a chain of six Al sites with partial occupancies (0.32 and 0.24 for Al2 and Al3 sites, respectively) along the orthorhombic \( c \)-axis (Figure 1). The relatively wide solid solubility range (Al-27 to 31 at.% Fe) reported for the \( \eta \) phase [19–21] is usually assumed to be realized by varying Al occupancies in the \( c \)-axis chain sites. However, Becker et al. [22,23] have recently reported that not only Al but also Fe atoms occupy the \( c \)-axis chain sites in the \( \eta \) phase with Fe-rich compositions, suggesting that the number density of atoms in the \( c \)-axis chain does not depend much on the alloy composition in the solubility range, unlike the expectation from the crystal structure model by Burkhardt et al. [15]. Very recently, a few research groups including ours have independently found that there are several different low-temperature phases having crystal structures based on the \( \eta \) phase, with the Al/Fe atoms arranged in ordered manners in the orthorhombic \( c \)-axis chain [22–24]. On the Al-rich side of the solubility range (~Al-27.3 at.%Fe), Al atoms in the \( c \)-axis chain are arranged in an ordered manner to form a new phase (\( \eta^* - Fe_2Al_3 \)) with a tripled superlattice structure based on the parent \( \eta \) structure [24]. We have found that in the \( \eta^* \) phase, one-third of the \( c \)-axis chain sites corresponding to the Al3 sites in the \( \eta \) phase are occupied exclusively by Al atoms, while those corresponding to the Al2 sites are completely vacant. As a result, a total of two-ninths of the \( c \)-axis chain sites are occupied in an ordered manner [24]. Becker et al. [22,23] have reported, on the other hand, that when the alloy composition is on the Fe-rich side of the solubility range (~Al-29.4 at.%Fe), Al and Fe atoms in the \( c \)-axis chain are arranged in an ordered manner to form another low-temperature phase (\( \eta'' \)) [23]. Those authors believed that the \( \eta'' \) phase has an incommensurately modulated crystal structure of long periodicity along the orthorhombic \( c \)-axis [23]. However, neither the occupation behavior of the Fe and Al atoms in the \( c \)-axis chain (i.e. their fractions at each of the Al2 and Al3 sites) nor the origin of the incommensurability/modulation was clarified. It is of particular interest to know the preferential sites for Fe/Al atoms and the manner of their ordered arrangement in the \( c \)-axis chain (if any), in view of the established principle for Al atoms in the \( c \)-axis chain in the \( \eta^* \) phase on the Al-rich side of the solubility range [24].

In the present study, we investigate the crystal structure of the \( \eta'' \) phase with two different compositions, by using single-crystal synchrotron X-ray diffraction (SXRD) and electron diffraction combined with atomic-resolution scanning transmission electron microscopy (STEM), as we have successfully applied to the crystal structure refinement of a series of intermetallics of the Fe-Zn system formed on galvanized/galvannealed steels [25–31].

2. Experimental procedures

Ingots with two different nominal compositions, Al-30.0 and 31.0 at.%Fe, were prepared by arc-melting Fe and Al (4N purity) under an Ar gas flow. Mass loss after the arc-melting was less than 0.1%. The solidified ingots encapsulated in a quartz ampoule with Ar gas were heat-treated under two different conditions: (i) at 900°C for 1 day and then at 300°C for 28 days followed by iced-water quenching, and (ii) at 1000°C for 1 day followed by iced-water quenching. The microstructures and chemical compositions of phases present in the specimens were examined by scanning electron microscopy (SEM).
and transmission electron microscopy (TEM). Thin foils for TEM observations were prepared by twin-jet electro-polishing in a solution of perchloric acid and methanol (1:9 by volume) at −40°C and 10 V. Bright-field images and electron diffraction patterns were obtained with a JEOL JEM-2000FX TEM operated at 200 kV, while atomic-resolution images were obtained with a spherical-aberration-corrected JEOL JEM-ARM200F STEM operated at 200 kV. The probe convergence angle and the inner/outer detector angles for high-angle annular dark-field (HAADF) imaging were 22 and 90/370 mrad, respectively. Energy dispersive X-ray spectroscopy (EDS) was employed in atomic-resolution STEM observation. Simulations of STEM images and electron diffraction patterns were performed with the WinHREM software package [32] and CaRIne software [33], respectively. SXRD experiments were carried out at 300 K with a large cylindrical image-plate camera installed at BL02B1 of SPring-8 synchrotron radiation facility. A columnar specimen was machined from the η″ phase in the Al-31.0 at.%Fe alloy quenched from 300°C with a JEOL JIB-4000 focused ion beam (FIB) apparatus at an operating voltage of 30 kV. The size of the columnar specimen was approximately 18 μm in diameter and 20 μm in length. The crystal structure was solved by SHELXT [34] and refined by full-matrix least-squares techniques on F² (SHELXL-97) [35] within the WinGX crystallographic software package [36,37].

3. Results

3.1. SEM and TEM observations

Figure 2(a–d) shows SEM back-scattered electron images (BEIs) of microstructures in the two alloys with different nominal compositions quenched from different temperatures. While specimens with the Al-30.0 at.%Fe composition quenched from 300 and 1000°C both exhibit the η″ single-phase microstructure (Figure 2(a,b)), those with the Al-31.0 at.%Fe composition quenched from these two temperatures exhibit two-phase microstructures consisting of the major η″ phase (dark region) and the secondary ζ phase (bright region) (Figure 2(c,d)). This phase identification is based on electron diffraction analysis.
(not shown). Hence, the Fe-rich side boundary of the \(\eta\)"-phase solid solubility region is between Al-30.0 and 31.0 at.%Fe.

Figure 2(e–h) shows bright-field TEM images of the \(\eta\)" phase with the [100]\text{Cmcm} incidence.\(^1\) All the four specimens exhibit lattice fringes parallel to the (001)\text{Cmcm} plane, with a spacing of approximately 6 and 8 nm for the Al-30.0 and 31.0 at.%Fe alloys, respectively. Figure 2(i–n) shows selected-area electron diffraction (SAED) patterns obtained from the \(\eta\)" phase with the [100]\text{Cmcm} and [102]\text{Cmcm} incidences, respectively. All the SAED patterns contain superlattice diffraction spots in addition to those from the \(\eta\) phase with the space group \text{Cmcm} (Figure 2(o,p)). These superlattice diffraction spots appear at nearly the mid positions between the 000 and the 002, 021, and 021 fundamental spots for the [100]\text{Cmcm} incidence, and between the 000 and the 201 fundamental (forbidden) spots for the [102]\text{Cmcm} incidence, respectively, as indicated by the yellow circles. Close inspection of the SAED patterns with the [100]\text{Cmcm} incidence (Figure 2(i–l)) indicates, however, that these superlattice diffraction spots are not located exactly at these mid positions, but rather split into two or more spots along the \(c^*\) direction (as shown in the enlarged patterns in the bottom left of Figure 2). The split distance of these superlattice diffraction spots at the mid position between the 000 and the 002 fundamental spots (2\(\Delta^*\)) is twice that between the 000 and the 021 fundamental spots (\(\Delta^*\)). The split distance, 2\(\Delta^*\), is approximately 1/15 and 1/19 the distances between the 000 and 002 fundamental spots (2\(c^*\)) for the Al-30.0 and 31.0 at.%Fe alloys, respectively. As will be described in the following sections, the splitting of these superlattice reflections is due to structural/compositional modulation in the superlattice structure of the \(\eta\)" phase. Specifically, the observed split distances indicate that the magnitude of the superlattice unit cell dimension of the \(\eta\)" phase is respectively 15 and 19 times that of the \(c\)-axis of the parent orthorhombic unit cell of the \(\eta\) phase (0.42 184 nm). The spacing of the lattice fringes parallel to the (001)\text{Cmcm} plane (Figure 2(e–h)) is indeed fairly comparable to the magnitude of the superlattice periodicity (6.3 and 8.0 nm respectively for the Al-30.0 and 31.0 at.%Fe alloys) estimated from the split distance of the superlattice diffraction spots.

In the next two sections, we will describe the results of crystal structure refinement for the \(\eta\)" phase in two steps: first determination of the motif structure without structural/compositional modulation (Section 3.2) and then determination of the long-period unit cell structure with structural/compositional modulation (Section 3.3).

3.2. Motif structure of the \(\eta\)" phase without modulation

3.2.1. Electron diffraction

The unit cell dimension of the motif structure of the \(\eta\)" phase without modulation could be deduced from the positions of superlattice diffraction spots observed in the SAED patterns (Figure 2(i–n)) by ignoring their splitting. Figure 3(a) shows the unit cell dimension (outlined in green) and interplanar spacing of (021), (021), (201), and (201) lattice planes (indicated respectively with red, blue, yellow, and purple lines) of the \(\eta\) phase in the projection along the [100]\text{Cmcm} and [010]\text{Cmcm} incidences, which are orthogonal with each other. Since the superlattice diffraction spots are
observed very near the mid positions between the 000 and ±21 or ±201 fundamental spots (accompanied by splitting) (Figure 2(i–n)), interplanar distances for these four planes should be doubled in the \( \eta'' \) phase (Figure 3(b)). Intersections of these four lattice planes (dark blue circles) then form a body-centered orthorhombic lattice with a doubled \( c \)-axis lattice dimension. Therefore, the unit cell of the motif structure of the \( \eta'' \) phase is assumed to belong to the body-centered orthorhombic system possessing a unit cell volume twice that of the \( \eta \) phase. However, the atomic arrangement in the FeAl\(_2\) framework structure consisting of Fe and Al\(_1\) sites with full occupancy cannot be reproduced with any of the nine body-centered orthorhombic space groups (\( \text{Immm} \) and so on) listed in the International Tables for Crystallography [38]. Therefore, crystal symmetry of the motif structure in the \( \eta'' \) phase should be lower than body-centered orthorhombic (i.e. either monoclinic or triclinic). After symmetry considerations, we found it to be the base-centered monoclinic space group \( \text{C2/m} \), which is equivalent to the ‘quasi’ body-centered orthorhombic space group \( \text{I2/m1} \) (\( \beta = 90^\circ \)) listed in the International Tables for Crystallography [38]. We have also confirmed that the base-centered space group \( \text{C2/m} \) (\( \beta = 127^\circ \)) has the highest symmetry among all possible space groups.

Since the number of symmetry operations of the space group \( \text{Cnmc} \) (16) is twice that of \( \text{C2/m} \) (8), the \( \eta'' \) phase with the space group \( \text{C2/m} \) should have two orientation variants if it is formed from the \( \eta \) phase through solid–solid phase transformation upon cooling. These two orientation variants (designated as A and B) are generated by taking the principal axis \( (b\text{-axis}) \) of the monoclinic unit cell parallel (A) and anti-parallel (B) to the \( a \)-axis of the parent orthorhombic unit cell (Figure 3(c)). Since these two orientation variants are symmetric with each other with respect to the \( \{001\}_{\text{Cnmc}} \) mirror plane, they are twins.

The Miller index transformation from the \( \eta \) phase (\( \text{Cnmc} \)) to the \( \eta'' \) phase (\( \text{C2/m} \)) for orientation variants A and B is expressed as follows:

**Directions:** \([uvw]_{\text{Cnmc}} \rightarrow [UVW]_{\text{C2/m}}\)

\[
U = w, \quad V = 2u, \\
W = 2v + w \quad (\text{orientation variant A}) \quad (1)
\]

\[
U = w, \quad V = -2u, \\
W = -2v + w \quad (\text{orientation variant B}) \quad (2)
\]

**Planes:** \(\{hkl\}_{\text{Cnmc}} \rightarrow \{HKL\}_{\text{C2/m}}\)

\[
H = -k + 2l, \quad K = 2h, \\
L = k \quad (\text{orientation variant A}) \quad (3)
\]

\[
H = k + 2l, \quad K = -2h, \\
L = -k \quad (\text{orientation variant B}) \quad (4)
\]

SAED patterns with the \([010]_{\text{C2/m}}\) and \([111]_{\text{C2/m}}\) incidences calculated for orientation variant A (corresponding respectively to the \([100]_{\text{Cnmc}}\) and \([102]_{\text{Cnmc}}\) incidences for the \( \eta \) phase) are shown in Figure 2(q,r), respectively. The experimental SAED patterns (Figure 2(i–n)) are well reproduced by the calculation (Figure 2(q,r)), except for the splitting of superlattice diffraction spots.

The approximate lattice parameters and atomic coordinates of the \( \eta'' \) phase with the space group \( \text{C2/m} \) (i.e. the motif structure without modulation) are derived based on those of the parent \( \eta \) phase [15] (left part of Table 1), and tabulated in the right part of Table 1. Each of the Fe, Al\(_1\), Al\(_2\), and Al\(_3\) sites in the \( \eta \) phase with the space group \( \text{Cnmc} \) splits into a few different Wyckoff sites in the \( \eta'' \) phase with the space group \( \text{C2/m} \).

### 3.2.2. STEM observation

Figure 4(b) shows an atomic-resolution HAADF-STEM image of the \( \eta'' \) phase with the \([100]_{\text{Cnmc}}\) incidence. The corresponding \([100]_{\text{Cnmc}}\) projection of the crystal structure for the \( \eta \) phase reported by Burkhardt et al. [15] is shown in Figure 4(a). While Fe atoms in the Fe sites and Al atoms in the Al\(_1\) sites with full occupancy forming the FeAl\(_2\) framework structure exhibit a well-defined asymmetric dumbbell pattern (Fe: brighter, Al\(_1\): darker), Al atoms at the Al\(_2\) and Al\(_3\) sites with partial occupancy in the \( c \)-axis chain do not exhibit any noticeable brightness contrast in the image. In the HAADF-STEM image of the \( \eta'' \) phase (Al-30.0 at.%Fe) with the equivalent \([010]_{\text{C2/m}}\) incidence (Figure 4(c)), on the other hand, bright spots are observed at positions corresponding to every fourth of the Al\(_2\) sites along the \( c \)-axis chain for the \( \eta \) phase, as indicated by yellow arrows. This is a clear indication that the Al (and Fe) atoms are arranged in the \( c \)-axis chain in an ordered manner, forming the monoclinic unit cell of the motif structure of the \( \eta'' \) phase with the space group \( \text{C2/m} \), as outlined with magenta lines in Figure 4(c). The positions of these bright spots, indicated by yellow arrows, correspond to the Wyckoff 2\( a \) sites in the doubled monoclinic unit cell of the motif superlattice structure (right part of Table 1). As will be described later in Section 3.3.2, SXRD indicates that a part of the Al\(_3\) sites is also occupied by Al atoms in an ordered manner, although they are not visible in the HAADF-STEM image of Figure 4(c) due to their large atomic displacement parameters (Figure 6(c)).

### 3.3. Crystal structure of the \( \eta'' \) phase with modulation

#### 3.3.1. STEM observation

Figure 5 shows an HAADF-STEM image of the Al-30.0 at.%Fe alloy quenched from 300°C taken along
Direction. In addition to the asymmetric dumbbell pattern corresponding to Fe and Al atoms in the FeAl₄ framework structure, there are clearly bright spots arranged in an ordered manner in the c-axis chain as highlighted by white arrows. These bright spots correspond to the Wyckoff sites in the doubled monoclinic unit cell of the motif superlattice structure, as described in the previous section. Close inspection of Figure 5 indicates that there are two domains with different arrangements of these bright spots as outlined by yellow dotted rectangles (Supplementary Figure S1). These two domains are obviously symmetric with each other with respect to the (001) mirror plane, and thus they are the twin variants described in Section 3.2.1. Surprisingly, the thickness of each twin variant is fairly constant when measured along the c-axis of the orthorhombic unit cell of the parent η phase, being 7.5 times the orthorhombic c-axis lattice constant (~3.16 nm) for this composition (Al-30.0 at.% Fe). Then, the total thickness of a pair of twin variants A and B is 15 times the c-axis lattice constant of the parent orthorhombic unit cell (M value: 15) [39–41], amounting to approximately 6.3 nm, which is virtually identical to the spacing of lattice fringes (~6 nm) observed in the bright-field images of Figure 2(e,f).

Thus, the crystal structure of the η″ phase can be described as consisting of twin (orientation) variants A and B alternately stacked along the c-axis of the orthorhombic unit cell of the parent η phase, with structural and compositional modulation at the twin boundary. Details of the structural/compositional modulation will be fully described in Section 4.2.

### 3.3.2. Single-crystal SXRD

Table 1. Unit cell dimensions and atomic coordinates for (left) the parent η-Fe₅Al₅ phase [15], and (right) the motif structure in the η″ phase. The cell dimensions and atomic coordinates for the motif structure are simply derived from Ref [15]. The refined parameters are tabulated in Supplementary Table S2.

| Space group | a (nm) | b (nm) | c (nm) | β (deg.) | Cell volume (nm³) |
|-------------|--------|--------|--------|----------|------------------|
| Cmcm | 0.76559 | 0.64154 | 0.42184 | -127.25 | 0.20719 |
| C2/m | 1.0599 | 0.7656 | 0.6415 | 127.25 | 0.4144 |

Table 1. Unit cell dimensions and atomic coordinates for (left) the parent η-Fe₅Al₅ phase [15], and (right) the motif structure in the η″ phase. The cell dimensions and atomic coordinates for the motif structure are simply derived from Ref [15]. The refined parameters are tabulated in Supplementary Table S2.

| Atom | Wyck. | Occ. | x | y | z | Atom | Wyck. | Occ. | x | y | z |
|------|-------|------|---|---|---|------|-------|------|---|---|---|
| Fe1  | 4c    | 1    | 0 | 0.8277 | 1/4 | Fe1  | 4i   | 1    | 0.125 | 0  | 0.453 |
| Al1  | 8g    | 1    | 0.1880 | 0.1467 | 1/4 | Al1  | 8j   | 1    | 0.125 | 0.312 | 0.271 |
| Al2  | 4b    | 0.32 | 0 | 0.500 | 0  | Al2  | 2d   | 0    | 0.750 | 0  | 0.250 |
| Al3  | 8f    | 0.24 | 0 | 0.034 | 0.830 | Al3  | 4i   | 0    | 0.085 | 0  | 0.051 |
|      |       |      |   |       |     |      |       |      |   |       |     |

*Al21 site is occupied by both Fe and Al atoms in the compositionally and structurally modulated structure of the η″ phase.

Figure 4. (a) Atomic arrangement of the η phase reported by Burkhardt et al. [15] projected along the [100] Cmcm orientation. HAADF-STEM images of the (b) η and (c) η″ phases taken along the [100] Cmcm direction, which corresponds to the [010] C2/m direction for the monoclinic motif structure of the η″ phase.

Reproduced with permission of the International Union of Crystallography.
Figure 5. HAADF-STEM image of the $\eta''$ phase in the 30.0 at.%Fe alloy quenched from 300°C taken along the [100]$_{Cmcm}$ orientation. Regions with slightly bright contrast in the c-axis chain are highlighted by white arrows. The monoclinic unit cell of the motif structure of the $\eta''$ phase is indicated by magenta and green parallelograms.

$Pnma$ (the 5th setting of $Pnma$) of the highest symmetry is assigned to the $\eta''$ phase. The c-axis lattice constant of the $\eta''$ phase is 8.01655 nm. This value is exactly 19 times that of the parent $\eta$ phase (0.42184 nm) [15], and this is in good agreement with the spacing of lattice fringes (~8 nm) observed in Figure 2(g,h) as well as the long periodicity estimated with the splitting distance of superlattice diffraction spots (Figure 2(l)). In further structure refinement, we employed the following procedures. At first, the Fe1–Fe19 and Al1–Al19 sites constituting the FeAl$_3$ framework structure were assumed to be occupied exclusively by Fe and Al atoms, respectively, with full occupancy and isotropic displacement parameters. Meanwhile, the 14 different sites (Al21–Al25 and Al31–Al39) comprising the c-axis chain were assumed to be occupied exclusively by Al atoms. Then, mixed occupancies of Al and Fe atoms were allowed in each of the 14 different c-axis chain sites for the occupancy determination. Only one of the 14 chain sites was refined in each fitting procedure to avoid divergence of the fitting, and the site to be refined was changed one by one until the occupancies for all the c-axis chain sites were converged. As a result, we found that the Al31–Al39 sites are occupied almost exclusively by Al atoms (96 ± 7% on average) while the average Fe occupancy at the Al21–Al25 sites is as high as 27 ± 12% (Supplementary Table S1). Thus, the c-axis chain sites in the $\eta''$ phase are occupied by not only Al but also Fe atoms. This agrees with the result of crystal structure refinement for the $\eta''$ phase by Becker et al. [22,23], but is quite different from that of the $\eta'$ phase (Fe$_3$Al$_6$) reported in Ref [24] where the c-axis chain sites are exclusively occupied by Al atoms in an ordered manner. Finally, anisotropic displacement parameters for all the 52 sites were refined. Supplementary Table S1 gives the atomic coordinates and equivalent isotropic displacement parameters refined for the $\eta''$ phase in the present study.

The refined atomic structure of the $\eta''$ phase in the Al-31.0 at.%Fe alloy is shown in Figure 6(a). This compound possesses a long-period superlattice structure based on the parent $\eta$-phase structure (space group $Cmcm$) with a peculiar ordered arrangement of Fe/Al atoms in the c-axis chain sites. While the orthorhombic unit cell of the $\eta$ phase stacks along the c-axis to form a long-period superlattice unit cell of the $\eta''$ phase (M = 19 for Al-31 at.%Fe), almost every fourth of the c-axis chain sites is occupied in an ordered manner by Fe/Al or Al atoms, so that the unit cell consists of two twin-related domains alternately stacked along the orthorhombic c-axis. The top and bottom quarters of the unit cell correspond to the orientation variant A, while the central half of the unit cell corresponds to the orientation variant B in Figure 6(a). In other words, each of the twin domains is formed with the motif structure having the doubled unit cell dimension described in Section 3.2, and they comprise the unit cell of the $\eta''$ phase with the twin boundaries corresponding to the diagonal glide planes at $z = 1/4$ and $3/4$. Importantly, it is the twin boundary that gives rise to the structural/compositional modulation that leads to the splitting of superlattice reflections. This is evident from the fact that while every fourth of the c-axis chain sites is ‘regularly’ occupied with the occupied-site sequence of ...Al2/Al3/Al2/Al2/Al3/... within the twin domains, this regularity is disturbed in the twin boundary region where the occupied-site sequence is ...Al3/Al2/Al3/Al3/... The composition derived from the present structure refinement for the $\eta''$ phase is Al-29.2 at.%Fe, which is slightly lower in Fe content than the nominal alloy composition (Al-31.0 at.%Fe). Crystal structures of the $\eta''$ phase with different compositions can be constructed only by changing the number (M value) of the parent orthorhombic unit cells to be stacked along the orthorhombic c-axis (e.g. M = 15 for Al-30.0 at.%Fe), with identical atomic arrangements for the motif structure and the twin boundary.

Figure 6(b) shows an HAADF-STEM image calculated based on the refined structural model (Figure 6(a)) for the Al-31.0 at.%Fe alloy. It reproduces most
Table 2. Summary of crystallographic data and structure refinement for the long-period ordered structure of the η" phase in the Al-31.0 at.%Fe alloy quenched from 300°C.

| Crystal data                          | Fe$_{20}$Al$_{40.3}$ (Al-29.2 at.%Fe) |
|---------------------------------------|--------------------------------------|
| Refined chemical formula              |                                       |
| Space group                           | Pmcn (the 5th setting of Pnma)        |
| Z                                     | 4                                    |
| Lattice constants, a (nm)             | 0.7660(3)                            |
| b (nm)                                | 0.6428(1)                            |
| c (nm)                                | 8.0165(24)                           |
| Cell volume (nm$^3$)                  | 3.9477                               |
| Density (calculated) (Mg/m$^3$)       | 4.146                                |
| Formula weight                        | 2464.11                               |
| Absorption coefficient (mm$^{-1}$)    | 7.925                                |
| Crystal size (mm$^3$)                 | 0.018 × 0.018 × 0.020                |
| Data collection                       |                                       |
| Wavelength (nm)                       | 0.04981                               |
| θ range for data collection (degree)  | 0.356 – 38.508                       |
| Index ranges                          | -19 ≤ h ≤ 16                         |
|                                       | -16 ≤ k ≤ 16                         |
|                                       | -99 ≤ l ≤ 173                        |
| Reflections collected                 | 93,050                                |
| Independent reflections               | 26,355                                |
| Independent reflections (l > 20l)     | 3042                                  |
| Completeness to F$_{max}$             | 99.9%                                 |
| R$_{int}$                             | 0.1137                                |
| Refinement                            |                                       |
| Refinement method                     | Full-matrix least-squares on F$^3$    |
| Number of reflections used            | 26,355                                |
| Number of refined parameters          | 379                                   |
| Goodness-of-fit on F$^2$               | 0.977                                 |
| R$_1$, l > 20l                       | 0.0868                                |
| wR$_2$, l > 20l                      | 0.2262                                |
| R$_1$, all data                      | 0.3270                                |
| wR$_2$, all data                     | 0.2795                                |
| Largest diffraction peak and hole (10$^{-3}$ e$^-$ nm$^{-2}$) | 9.322/-5.552 |

Computer programs used: WinGX [36,37], SHELXT [34], and SHELXL embedded in SHELX [35].

features in the experimental HAADF-STEM image for the Al-30.0 at.%Fe alloy (Figure 5), except for the difference in M value. Al atoms at the Al31 – Al39 sites are hardly visible in either the calculated or experimental images, because of the large atomic displacement of the corresponding sites (Figure 6(c)) [42,43]. Interestingly, the crystal structure of the η” phase can also be described by the packing of distorted Al$_{10}$Fe$_2$ icosahedra whose center is preferentially occupied by an Fe atom (Al21–Al25 sites) as shown in Figure 6(d). This is very similar to the Fe–Zn intermetallic compounds (Γ′-Fe$_2$Zn$_{13}$, Γ$_1$-Fe$_{11}$Zn$_{40}$, δ$_{1p}$-Fe$_{12}$Zn$_{120}$, and ζ-Fe$_6$Zn$_{13}$), whose crystal structures are described by the packing of the common structural unit (Fe-centered Zn$_{12}$ and/or Fe-centered (Zn,Fe)$_{12}$ icosahedron) [25–31].

3.3.3. EDS elemental mapping

Figure 7(a) shows an HAADF-STEM image of the η” phase in the Al-31.0 at.%Fe alloy taken along the [001]$_{Cmcm}$ direction. In the projection along this direction, atomic columns forming the c-axis chain can clearly be observed without disturbance by other atoms, as seen in the schematic crystal structure of Figure 7(b). In addition to bright spots corresponding to Fe atoms (red circles) and Al atoms (blue circles) in the FeAl$_2$ framework structure, those corresponding to the atomic columns of the c-axis chain (green circle) are clearly seen with the brightness between those of Fe and Al atoms in the FeAl$_2$ framework structure. An Fe-elemental map obtained using atomic-resolution EDS is shown in Figure 7(c). Areas enriched with Fe are located at the c-axis chain sites, in addition to those at Fe atoms in the FeAl$_2$ framework structure. This is a clear indication that the c-axis chain sites in the η” phase are indeed occupied by not only Al but also Fe atoms.

4. Discussions

4.1. General description of crystal structures of the η” phase

In the present study, we determined that the η” phase (the low-temperature phase of η-Fe$_2$Al$_5$ with Fe-rich side compositions) possesses an orthorhombic long-period superlattice structure (space group Pnmcn), based on the parent orthorhombic unit cell (space group Cmcm) of the η phase. The superlattice structure consists of M unit cells of the parent orthorhombic lattice stacked along the orthorhombic c-axis, with a peculiar ordered arrangement of Fe/Al atoms in the c-axis chain sites. As a result, the unit cell of the η” phase consists of two twin-related domains alternately stacked along the orthorhombic c-axis with two twin boundaries at z = 1/4 and 3/4, corresponding to the diagonal glide planes. Each of the twin domains is comprised of
the motif structure with doubled unit cell dimension (Section 3.2). Based on the building principle described above, we can construct the crystal structures of the η" phase with various compositions only by changing M among several values as shown in Figure 8(a). All these structures are commensurate with the modulation 'regularly' occurring at the interval of half the long periodicity. Indeed, the split distance (2Δ*) of superlattice diffraction spots in the SAED patterns with the [100]_{Cmcm} incidence calculated for the structural models of Figure 8(a) is consistently 2c*/M, as shown in Figure 8(b). This clearly confirms the validity of our
structure refinement result for the \( \eta'' \) phase (see also Supplementary Figure S2).

Becker and Leineweber [23] have recently reported that the \( \eta'' \) phase possesses incommensurately modulated structures using powder X-ray diffraction. The approximant structures\(^3\) they derived for the \( \text{Al-29.3 and 29.4 at.}\%\text{Fe} \) alloys without taking the structural incommensurability into account are shown in Figure 8(c). These approximant structures are similar to the commensurate long-period structures determined in the present study in at least two aspects. First, the approximant/superlattice structures are based on the stacking of the parent orthorhombic unit cell of the \( \eta \) phase along the orthorhombic \( c \)-axis (the two structural models of Figure 8(c) can be expressed with \( M = 13 \) and 21). Second, the twin domains are stacked along the \( c \)-axis, with the diagonal glide planes at \( z = 1/4 \) and 3/4 being the twin boundaries. The key difference between the models of Becker and Leineweber [23] and ours (Figure 8(c) vs. 8(a)) is thus in how the Al/Fe atoms occupy the \( c \)-axis chain sites. The average distances of atoms located in the \( c \)-axis chain in these approximant structures (0.29 ± 0.02 and 0.29 ± 0.05 nm respectively for \( M = 13 \) and 21) are almost identical to that (0.29 ± 0.01 nm) in the commensurate long-period structure with \( M = 19 \) refined by SXRD in the present study (Figure 6(a)). This indicates that the atom packing density in the \( c \)-axis chain sites in these two structural models does not significantly differ from each other. However, their atomic arrangements along the \( c \)-axis chain sites are quite dissimilar. In

---

**Figure 8.** (a) Schematic illustration of the atomic arrangement in the commensurate long-period \( \eta'' \)-phase structures for \( M = 7–23 \). For simplicity, it is assumed that the Al3-equivalent sites are occupied exclusively by Al atoms, while the Al2-equivalent sites are occupied evenly by Fe and Al atoms (50%:50%), except for the Al2-equivalent site closest to the twin boundaries that are occupied exclusively by Al atoms. The positions of the Al2- and Al3-equivalent sites (orange and green circles) are schematically arranged in a straight line for simplicity. (b) 00l systematic row in the SAED pattern with the \([100]_{\text{cocom}}\) incidence, calculated with the above atomic arrangement. (c) Approximant structures of the incommensurately modulated structures of the \( \eta'' \) phase with \( M = 13 \) (Al-29.3 at.%Fe) and \( M = 21 \) (Al-29.4 at.%Fe) as deduced by Becker and Leineweber [23].

---

\(^3\) The approximant structures derived by Becker and Leineweber [23] are consistent with the commensurate long-period structures determined in the present study.
Table 3. Average, minimum, and maximum distances between Fe/Al atoms in the c-axis chain sites in the η" phase.

| M value | 19" | 21" |
|---------|-----|-----|
| Average (nm) | 0.29 ± 0.01 | 0.29 ± 0.02 |
| Minimum (nm) | 0.268 | 0.256 |
| Maximum (nm) | 0.307 | 0.323 |

*Al-31.0 at.%Fe alloy refined by SXRD (present study).
*Al-29.3 at.%Fe alloy refined by powder X-ray diffraction [23].
*Al-29.4 at.%Fe alloy refined by powder X-ray diffraction [23].

our model, almost every fourth of the c-axis chain sites is ‘regularly’ occupied with the sequence of ... Al2/Al3/Al2/Al3/Al2/Al3... (except for the twin-boundary regions), so that the motif structure is defined within twin domains for our commensurate structures (Figure 6(a) and 8(a)). However, such regularity in the occupied-site sequence is lost in the approximant structures deduced by Becker and Leineweber [23]. This is evident from the fact that the atomic distance in the c-axis chain in their approximant structures ranges widely, from 0.256 to 0.323 nm for M = 13 and from 0.217 to 0.354 nm for M = 21 (Figure 8(c) and Table 3). Clearly, the atomic arrangement within each of twin regions varies significantly depending on the M value, so that no motif structure can be defined in the approximant structures deduced by Becker and Leineweber [23]. We speculate that the contradiction between these two studies comes from the difference in the analyzed sample size. Becker and Leineweber [23] may have deduced the incommensurately modulated structures because their powder sample included various crystallites with different M values. This is evidenced by the significant broadening of superlattice diffraction spots, which they had noticed [23]. On the contrary, our STEM and SXRD experiments were performed on a very limited volume (~100 nm³ for STEM and ~0.005 mm³ for SXRD) compared to that of conventional powder X-ray diffraction (usually ~10 mm³).

As a result, in both our STEM and SXRD analyses, the structure was homogeneous throughout the small volume of specimen, and as a result no broadening of superlattice diffraction spots was noticed (Section 3.3.2).

4.2. Composition dependence of crystal structures of the η" phase

The unit cell of the η" phase consists of two twin-related domains alternately stacked along the orthorhombic c-axis. Each domain is formed with the motif structure having a fixed composition (Fe₆Al₁₆ or Fe₃Al₉). Meanwhile, the twin boundary region has a different fixed composition (Fe₆Al₁₆ or Fe₃Al₉), which gives rise to structural and compositional modulation to cause the splitting of superlattice reflections. Since the chemical compositions of the motif structure and twin boundary region are different from each other, that of the η" phase may vary with the M value (i.e. how frequently the twin boundary region appears along the c-axis stacking direction).

The numbers of atomic sites in the commensurate long-period structure with an arbitrary M value can be expressed as a function of M:

(i) Fe sites comprising the FeAl₂ framework: 4M
(ii) Al sites comprising the FeAl₂ framework: 8M
(iii) c-axis chain sites equivalent to Al₂ sites in the parent orthorhombic structure: M + 1
(iv) c-axis chain sites equivalent to Al₃ sites in the parent orthorhombic structure: 2(M-1)

In total, there exist 15M-1 atomic sites per unit cell. As revealed by the SXRD analysis (Sections 3.3.2 and 4.1), the c-axis chain sites equivalent to Al₂ sites in the parent orthorhombic structure (hereafter called Al₂-equivalent sites) are occupied almost exclusively by Al atoms while those equivalent to Al₃ sites (hereafter called Al₃-equivalent sites) are occupied by both Fe and Al atoms. The exception is the Al₂₅ site, closest to the twin boundary, where the occupancy of Fe toms is

Table 4. Numbers of Fe/Al atoms at each of the sites, and the chemical composition in the long-period η"-phase structures for several M values.

| M value | 7   | 9   | 11  | 13³ | 15   | 17   | 19³ | 21³ | 23³ |
|---------|-----|-----|-----|-----|------|------|-----|-----|-----|
| FeAl₂ framework sites, 12M | Fe, 4M | 28 | 36 | 44 | 52 | 60 | 68 | 76 | 84 | 92 |
| Al, 8M | 56 | 72 | 88 | 104 | 120 | 136 | 152 | 168 | 184 |
| Al₂-equivalent sites, M + 1 | Al², 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| Fe (50%), (M-3)/2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| Al (50%), (M-3)/2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| Al₃-equivalent sites, 2(M-1) | Al (100%), 2(M-1) | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 | 44 |
| Total Fe | (9M-3)/2 | 30 | 39 | 48 | 57 | 66 | 75 | 84 | 93 | 102 |
| Total Al | (2M-1)/2 | 74 | 95 | 116 | 137 | 158 | 179 | 200 | 221 | 242 |
| Total Fe + Al | 15M-1 | 104 | 134 | 164 | 194 | 224 | 254 | 284 | 314 | 344 |
| Chemical composition (at.%Fe) | (9M-3)/(30M-2)*100 | 28.85 | 29.10 | 29.27 | 29.38 | 29.46 | 29.53 | 29.58 | 29.62 | 29.65 |

*Nearest to the twin boundary.
*Al-29.3 at.%Fe alloy refined by powder X-ray diffraction (Becker and Leineweber [23]).
*Al-30.0 at.%Fe alloy observed by STEM (present study).
*Al-31.0 at.%Fe alloy refined by SXRD (present study).
*Al-29.4 at.%Fe alloy refined by powder X-ray diffraction (Becker and Leineweber [23]).
less significant compared with other Al2-equivalent sites (Figure 6(a)). Therefore, it is reasonable to assume that the Al3-equivalent sites are occupied exclusively by Al atoms while the Al2-equivalent sites are occupied evenly by Fe and Al atoms (50%:50%), except for the Al2-equivalent site closest to the twin boundary that are occupied exclusively by Al atoms. The numbers of Fe/Al atoms in each of the sites for several M values (from 7 to 23) are given in Table 4. As a result, the Fe content (chemical composition) in the compound is expressed as (9M-3)/(30M-2), increasing from 28.85 for M = 7 to 29.65 at.%Fe for M = 23 (bottom line in Table 4) and with the limit of 30.0 at.%Fe for M → ∞. A similar conclusion can be drawn by considering the compositions of the motif structure and twin-boundary region with their respective layer thicknesses expressed with the M value. Since the layer thicknesses of the motif structure and the twin-boundary region are respectively M-3 times and three times the c-axis constant of the parent orthorhombic structure (Figure 9), the overall composition is expressed as (Fe3Al2)3M-9(Fe3Al8)8 = Fe9M-3Al21M+1. This tendency qualitatively agrees with our results: Al-30.0 at.%Fe for M = 15 and 31.0 at.%Fe for M = 19. Because the η" phase always appears with twin-related domains (with fringe contrast in bright-field TEM images) regardless of the M value, they should be enriched in Al compared to the motif structure (Fe3Al2) by the incorporated amount of the twin boundary (Fe3Al8), and so the overall chemical composition is expressed as Fe3Al7+x.

4.3. Comparison of the crystal structures of the η, η′, and η" phases

Although the crystal structures of the η′ and η" phases are both superstructures based on the parent orthorhombic unit cell (space group Cmcm) of the η phase, the ordered manner in which Al/Fe atoms arrange in the c-axis chain sites is quite different from each other. Since the irregular atomic arrangement occurs in the twin boundary region, only the motif structure with the chemical formula of Fe3Al2 is considered for the η" phase. In the η" phase, one-third of the Al3-equivalent sites are occupied exclusively by Al atoms. In the η" phase, on the other hand, one-fourth of the Al2-equivalent sites are occupied by both Fe and Al atoms, while one-fourth of the Al3-equivalent sites are occupied exclusively by Al atoms.

Figure 9. Comparison of the atomic arrangement in the c-axis chain sites, between the commensurate structure determined in the present study and the approximant structure deduced by Becker and Leineweber [23].
(bottom right of Figure 10), giving rise to the doubled superlattice structure and the stoichiometric composition of Fe₃Al₂⁻. Of the 12 Al₂⁻ and Al₃-equivalent sites in the c-axis chain, the 1st, 5th, and 9th sites (i.e. every fourth of the 12 sites) are occupied by both Fe and Al atoms. This confirms that Fe atoms also occupy the c-axis chain sites when the Fe content increases in the low-temperature phases (from η′ to η″ phases), as observed in the high-temperature η phase by Becker and Leineweber [23]. Interestingly, once the Fe atoms start to occupy the c-axis chain sites, the Fe atoms prefer to occupy the Al₂⁻ equivalent sites while the Al atoms change to prefer to the Al₂⁻ equivalent sites together with Fe atoms.

5. Conclusions

(1) The η″ phase (the low-temperature phase of η-Fe₂Al₅) exhibits commensurate long-period superlattice structures (space group Pmcn) consisting of twin domains (orientation variants) alternately stacked along the long-periodicity axis parallel to the orthorhombic c-axis.

(2) Each of the twin domains possesses a motif structure belonging to a base-centered monoclinic-ordered structure (space group C2/m), with a cell volume twice that of the parent orthorhombic unit cell of η-Fe₂Al₅ (space group Cmcm).

(3) One-fourth of the c-axis chain sites corresponding to Al₂⁻ and Al₃-sites in the η phase are respectively occupied by both Fe and Al atoms and exclusively by Al atoms in a regular manner, while this regularity is disturbed in the twin boundary region to give rise to structural/compositional modulation.

(4) Because of the different chemical compositions in the motif structure and twin boundary region, the η″ phase with various compositions can be constructed only by changing the number (M) of the parent orthorhombic unit cells to be stacked along the orthorhombic c-axis, without changing the atomic arrangements for the motif structure or the twin boundary region.

(5) The chemical formula of the η″ phase can be expressed as Fe₃Al₂₋ₓ under a simple assumption about the occupancies for Al/Fe atoms in the c-axis chain sites.

3. Approximant structures are commensurately approximated structures of the incommensurately modulated structures and derived by finding a small rational component close to the irrational component of the incommensurately modulated structures [23].

Disclosure statement

No potential conflict of interest was reported by the authors.

Funding

This work was supported by JSPS KAKENHI [grant numbers 15H02300, 16K14415, 16H04516, and 16K14373], and the Elements Strategy Initiative for Structural Materials (ESISM) from the Ministry of Education, Culture, Sports, Science and Technology (MEXT) of Japan. It was supported in part by Advanced Low Carbon Technology Research and Development Program (ALCA) from the Japan Science and Technology Agency (JST). It was also supported by JKA and its promotion funds from KEIRIN RACE and Program for Advanced Technology, Kansai Research Foundation for Technology Promotion, as well as the 24th Research Promotion Grant from the Iron and Steel Institute of Japan (ISIJ). The synchrotron radiation experiments were performed at the BL02B1 of SPring-8 with the approval of the Japan Synchrotron Radiation Research Institute (JASRI, Proposal Nos. 2016B1096, 2017A1243, and 2019A1568).

ORCID

Norihiko L. Okamoto @ http://orcid.org/0000-0003-0199-7271

References

[1] Richards RW, Jones RD, Clements PD, et al. Metallurgy of continuous hot-dip aluminizing. Int Mater Rev. 1994;39(5):191–212.
[2] Abro MA, Lee DB. Microstructural changes of Al hot-dipped P91 steel during high-temperature oxidation. Coatings. 2017;7(2):31–40.
[3] Abro MA, Lee DB. High temperature corrosion of hot-dip aluminized steel in Ar/1%SO₂ Gas. Met Mater Int. 2017;23(1):92–97.
[4] Lemmens B, Gonzalez-Garcia Y, Corlú B, et al. Study of the electrochemical behaviour of aluminized steel. Surf Coat Technol. 2014;260:34–38.
[5] Xue ZY, Hao XY, Huang Y, et al. Wear resistance and wear mechanism of a hot dip aluminized steel in sliding wear test. Surf Rev Lett. 2016;23(2):1550098.
[6] Zhang QY, Zhou Y, Liu JQ, et al. Wear Behavior and Mechanism of Fe-Al Intermetallic Coating Prepared by Hot-Dip Aluminizing and Diffusion. Metall Mater Trans A. 2016;47A(5):2232–2242.
[7] Boryczko B, Holda A, Kolenda Z. Depletion of the non-renewable natural resource reserves in copper, zinc, lead and aluminium production. J Clean Prod. 2014;84:313–321.
[8] Lee CH. Formulation of resource depletion index. Res Cons Rec. 1998;24(3–4):285–298.
Determined by Scanning Transmission Electron Microscopy, Acta Mater. 2014;81:345–357.

Okamoto NL, Inui H, Yasuhara A, et al. Crystal structure determination of the Γ phase in the Fe-Zn-Al system by single-crystal synchrotron X-ray diffraction combined with scanning transmission electron microscopy. J Alloys Compd. 2015;644:287–296.

Okamoto NL, Inomoto M, Adachi H, et al. Micropillar compression deformation of single crystals of the intermetallic compound ζ-FeZn13. Acta Mater. 2014;65:229–239.

Okamoto NL, Kashioka D, Inomoto M, et al. Compression deformability of Γ and ζ Fe–Zn intermetallics to mitigate detachment of brittle intermetallic coating of galvannealed steels. Scripta Mater. 2013;69(4):307–310.

Inui H, Okamoto NL, Yamaguchi S. Crystal structures and mechanical properties of Fe-Zn intermetallic compounds formed in the coating layer of galvannealed steels. ISIJ Int. 2018;58(9):1550–1561.

Okamoto NL, Michishita S, Hashizume Y, et al. Fracture toughness of the Fe-Zn intermetallic compounds measured by bend testing of chevron-notched single-crystal microbeams. ISIJ Int. 2018;58(9):1569–1577.

Ishizuka K. A practical approach for STEM image simulation based on the FFT multislice method. Ultramicroscopy. 2002;90(2–3):71–83.

CaRIne crystallography 3.1; [cited 2019 Mar 6]. Available from: http://carine.crystallography.pagespero-orange.fr/index.html

Sheldrick GM. SHELXT - Integrated space-group and crystal-structure determination. Acta Crystallogr A. 2015;71:3–8.

Sheldrick GM. A short history of SHELX. Acta Crystallogr A. 2008;64:112–122.

Farrugia L. WinGX suite for small-molecule single-crystal crystallography. J Appl Crystallogr. 1999;32(4):837–838.

Farrugia L. WinGX and ORTEP for Windows: an update. J Appl Crystallogr. 2012;45(4):849–854.

Hahn T. International Tables for crystallography, Vol. A: space-group symmetry. 5th ed. Dordrecht: Springer; 2005.

Fujime S, Ogawa S, Fujiwara K, et al. Intensity of satellite reflections in electron diffraction patterns from evaporated alloy films with CuAu II type superstructure. J Phys Soc Jpn. 1964;19(10):1881–1892.

Ogawa S, Watanabe D. Electron diffraction study on the ordered alloy CuAu. J Phys Soc Jpn. 1954;9(4):475–488.

Ogawa S, Watanabe D, Watanabe H, et al. The direct observation of the long period of the ordered alloy CuAu(II) by means of electron microscope. Acta Crystallogr. 1958;11(12):872–875.

Harada S, Hoshikawa H, Kuwabara K, et al. Crystal structure refinement of ReSi13.75 with an ordered arrangement of silicon vacancies. Philos Mag. 2011;91(23):3108–3127.

Harada S, Tanaka K, Kishida K, et al. Direct observation of vacancies and local thermal vibration in thermoelectric rhenium silicide. Appl Phys Express. 2012;5(3):035203.