Evidence for Large Direct $CP$ Violation in $B^\pm \to \rho(770)K^\pm$ from Analysis of the Three-Body Charmless $B^\pm \to K^\pm \pi^\pm \pi^\mp$ Decay

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Decays of $B$ mesons to three-body charmless hadronic final states provide new possibilities for $CP$ violation searches. In decays to two-body final states $(B \rightarrow K\pi, \pi\pi, \text{etc.})$ direct $CP$ violation can be observed as a difference in $B$ and $\bar{B}$ decay rates. In decays to three-body final states that are often dominated by quasi-two-body channels, direct $CP$ violation can also manifest itself as a difference in relative phase between two quasi-two-body amplitudes that can be measured via amplitude (Dalitz) analysis. So far direct $CP$ violation in the $B^\pm \rightarrow K^\pm \pi^\pm \pi^\mp$ channel has been observed only in decays of neutral $K$ mesons [1] and recently in neutral $B$ meson decays [2]. However, large direct $CP$ violation is expected in charged $B$ decays to some quasi-two-body charmless hadronic modes [3].

The search for direct $CP$ violation in the three-body charmless $B^\pm \rightarrow K^\pm \pi^\pm \pi^\mp$ decay described in this Letter is performed by applying a Dalitz analysis technique [4] to a data sample containing 386 million $BB$ pairs, collected with the Belle detector [5] operating at the KEKB asymmetric-energy $e^+e^-$ collider [6] with a center-of-mass (c.m.) energy at the $\Upsilon(4S)$ resonance. These results supersede the results reported in Ref. [2].

Charged tracks are required to have momenta transverse to the beam greater than 0.1 GeV/$c$ and to be consistent with originating from the interaction region. For charged kaon identification we impose a requirement on a particle identification variable which has 86% efficiency and a 7% fake rate from misidentified pions as measured from data. Charged tracks that are positively identified as electrons or protons are excluded. $B$ candidates are identified using two kinematic variables: the energy difference $\Delta E = (\sum_i \sqrt{c^2p_i^2 + m_i^2}) - E_{\text{beam}}^*$, and the beam constrained mass $M_{bc} = \frac{1}{2} \sqrt{E_{\text{beam}}^2 - c^2 \sum_i p_i^2}$, where the summation is over all particles from a $B$ candidate; $p_i$ and $m_i$ are their c.m. three-momenta and masses, respectively; $E_{\text{beam}}^*$ is the beam energy in the c.m. frame. The signal $M_{bc}$ resolution is mainly given by the beam energy spread, and amounts to 2.9 MeV/$c^2$. The signal $\Delta E$ shape is fitted by a sum of two Gaussian functions with a common mean. In fits to the experimental data, we fix the width (35 MeV) and the relative fraction (0.16) of the second Gaussian function to the values obtained from Monte Carlo (MC) simulation. The common mean of the two Gaussian functions and the width of the main Gaussian are allowed to float.

The dominant background is due to $e^+e^-\rightarrow q\bar{q}$ ($q = u, d, s$ and $c$ quarks) continuum events. We reject about 98% of this background while retaining 36% of the signal using variables that characterize the event topology. For more details see Ref. [3] and references therein. From MC studies we find that the dominant backgrounds originating from other $B$ decays that peak in the signal re-
The ∆E distributions for $B^+ \to \bar{D}^0[K^+\pi^-] \pi^+$ and due to $B^+ \to J/\psi(\psi(2S))|\mu^+\mu^-|K^+$ in which muons are misidentified as pions. We veto these backgrounds by applying requirements on the invariant masses of the appropriate two-particle combinations. The most significant backgrounds from charmless $B$ decays originate from $B^+ \to \eta'[^{1}\Sigma^+(1385)]K^+$, $B^+ \to \pi^+\pi^+\pi^-$ where one of the two same-charge pions is misidentified as a kaon, and from $B^0 \to K^+\pi^- \pi^+$ processes.

The ∆E distributions for $B^\pm \to K^+\pi^+\pi^-$ candidates that pass all the selection requirements are shown in Fig. 1. In the fit to the ∆E distribution we fix the shape of the $B\bar{B}$ background component from MC and let the normalization float. The shape of the $q\bar{q}$ background is parametrized by a linear function with the slope and normalization as free parameters of the fit. From these fits we find 2248±79 (2038±76) $B^-$ ($B^+$) signal events; the width of the main signal Gaussian is 15.3±0.5 MeV.

For the amplitude analysis we select events from the $B$ signal region defined as an ellipse around the $M_{bc}$ and ∆E mean values: $|M_{bc} - M_{bc}^0|^2 + |\Delta E|/1000$ MeV$^2 <$1. The total number of events in the signal region is 7757; the relative fraction of signal events is 0.512±0.012. The distribution of background events is determined from analysis of events in the $M_{bc}$−∆E sideband region.

The analysis is performed by means of an unbinned maximum likelihood fit. The distribution of background events is parametrized by an empirical function with 11 parameters. As found in Ref. 2, the three-body $B^\pm \to K^+\pi^+\pi^-$ amplitude is well-described by a coherent sum of $K^*(892)^0\pi^+$, $K_0(1430)^0\pi^+$, $\rho(770)^0K^+$, $f_0(980)K^+$, $f_X(1300)K^+$ and $\chi_{c1}K^+$ quasi-two-body channels and a non-resonant amplitude. The $f_X(1300)K^+$ channel was introduced in order to describe an excess of signal events at $M(\pi^+\pi^-) \approx 1.3$ GeV/c$^2$ (see Fig. 2(b)). The best fit is achieved assuming $f_X(1300)$ is a scalar state; the mass and width determined from the fit (see below) are consistent with those for $f_0(1370)$. Each quasi-two-body amplitude includes a Breit-Wigner function, a $B$ decay form-factor parametrized in a single-pole approximation, a Blatt-Weisskopf factor for the intermediate resonance decay, and a function that describes angular correlations between final state particles. This is multiplied by a factor of $ae^{i\delta}$ that describes the relative magnitude and phase of the contribution. The non-resonant amplitude is parametrized by an empirical function $A_{nr}(K^+\pi^+\pi^-) = a_{12}^\pi e^{-\alpha_{12}^\pi |E|^{2\gamma_{12}^\pi}} + a_{23}^\pi e^{-\alpha_{23}^\pi |E|^{2\gamma_{23}^\pi}}$, where $\alpha$, $a_{12}^\pi$ and $\gamma_{12}^\pi$ are fit parameters, $s_{13} \equiv M^2(K^+\pi^-)$, and $s_{23} \equiv M^2(\pi^+\pi^-)$. In this analysis we modify the model by changing the parameterization of the $f_0(980)$ lineshape from a Breit-Wigner function to a Flatté parameterization and by adding two more channels: $\omega(782)K^+$ and $f_2(1270)K^+$. For $CP$ violation studies the amplitude for each quasi-two-body channel is modified from $ae^{i\delta}$ to $ae^{i(\delta + \epsilon \varphi)}$, where the plus (minus) sign corresponds to the $B^+$ ($B^-$) decay. With such a parameterization the charge asymmetry, $A_{CP}$, for a particular quasi-two-body $B\to f$ channel is given by

$$A_{CP}(f) = \frac{N_+ - N_-}{N_+ + N_-} = \frac{2b \cos \varphi}{1 + b^2}.$$ 

It is worth noting that in this parameterization we assume zero relative phase between $B^-$ and $B^+$ amplitudes.

First we fit the data with $b_1 \equiv 0$ (no $CP$ violation) and determine the parameters of the $f_X(1300)$ ($M = 1.449 \pm 0.013$(stat.) GeV/c$^2$, $\Gamma = 0.126 \pm 0.025$(stat.) GeV/c$^2$), $f_0(980)$ ($M = 0.950 \pm 0.009$(stat.) GeV/c$^2$ and coupling constants $g_{\pi\pi} = 0.23 \pm 0.05$(stat.) and $g_{\pi\pi} = 0.73 \pm 0.30$(stat.)), and the parameter of the non-resonant amplitude $\alpha = 0.195 \pm 0.018$(stat.). We then fix these six parameters and repeat the fit to data with $b$ and $\varphi$ floating for all terms except $B^\pm \to \omega(782)K^\pm$ and the non-resonant amplitudes. Possible effects of these assumptions were studied, and are included in the final results as a part of the model uncertainty. Projections of the fit are shown in Fig 2 and the results are summarized in Table I. We find that the statistical significance of the $B^\pm \to f_2(1270)K^\pm$ signal exceeds 6σ; this is the first observation of this decay mode. The significance of the $B^\pm \to \omega(782)K^\pm$ signal is 2.1σ. The statistical significance of these signals (and the asymmetries quoted in Table I) is calculated as $\sqrt{-2\ln(L_0/L_{max})}$, where $L_{max}$ and $L_0$ denote the maximum likelihood with the nominal fit and with the corresponding amplitude (or asymmetry) fixed at zero, respectively. Note that the significance of the asymmetry is sensitive not only to $b_1 \cos \varphi_1$, but also to $b_1 \sin \varphi_1$, whereas $A_{CP}$ is sensitive only to the former (Eq. 1). Therefore, the significance of the asymmetry should be interpreted as having two degrees of freedom. The only channel where the significance of the asymmetry exceeds the 3σ level is $B^\pm \to \rho(770)^0K^\pm$. Figures 3(a,b) show the $M(\pi^+\pi^-)$ distributions for the $\rho(770) - f_0(980)$ mass region separately for $B^-$ and $B^+$ events. However, the interference term between $B^\to \rho(770)K$ vector and $B^\to f_0(980)K$ scalar amplitudes cancels out when making the $M(\pi^+\pi^-)$ pro-
TABLE I: Results of the best fit to $K^+\pi^+\pi^-$ events in the $B$ signal region. The first quoted error is statistical and the second is the model dependent uncertainty. The quoted CP asymmetry significance is statistical only.

| Channel $(892)\pi\pi$ | Fraction (%) | $\delta$ (°) | $b$ | $\varphi$ (°) | Asymmetry significance ($\sigma$) |
|-----------------------|--------------|---------------|-----|---------------|----------------------------------|
| $K^*(892)\pi\pi$      | 13.0 $\pm 0.8^{+0.7}_{-0.7}$ | 0 (fixed)    | $0.0786_{-0.0031}^{+0.0034}$ | $-18 \pm 44_{-13}^{+13}$ | 2.6 |
| $K_0^*(1430)\pi\pi^*$ | 65.5 $\pm 1.5^{+2.2}_{-2.1}$ | 55 $\pm 4^{+2.1}_{-3.9}$ | $0.069_{-0.030}^{+0.008}$ | $-123 \pm 16_{-5}^{+2.4}$ | 2.7 |
| $\rho(770)K^\pm$      | 7.85 $\pm 0.93^{+0.64}_{-0.59}$ | $-21 \pm 14^{+14}_{-10}$ | $0.28_{-0.09}^{+0.09}$ | $-125 \pm 32_{-85}^{+10}$ | 3.9 |
| $\omega(782)K^\pm$    | 0.15 $\pm 0.12^{+0.03}_{-0.02}$ | 100 $\pm 31^{+38}_{-21}$ | 0 (fixed)    | --           | --     |
| $f_0(980)K^\pm$       | 17.7 $\pm 1.6^{+1.1}_{-1.3}$ | 67 $\pm 11^{+10}_{-13}$ | 0.30 $\pm 0.19^{+0.05}_{-0.10}$ | $-82 \pm 8_{-10}^{+7}$ | 1.6 |
| $f_2(1270)K^\pm$      | 1.52 $\pm 0.35^{+0.22}_{-0.37}$ | 140 $\pm 11^{+18}_{-13}$ | 0.37$^{+0.19}_{-0.16}$$^{+0.11}_{-0.04}$ | $-24 \pm 29_{-20}^{+14}$ | 2.7 |
| $f_0(1300)K^\pm$      | 4.14 $\pm 0.81^{+0.31}_{-0.30}$ | $-141 \pm 10^{+18}_{-9.8}$ | 0.12 $\pm 0.17^{+0.04}_{-0.07}$ | $-77 \pm 50_{-43}^{+48}$ | 1.0 |
| Non-Res.              | 34.0 $\pm 2.2^{+2.1}_{-1.8}$ | $\delta_{\text{nr}} = -11 \pm 5^{+3}_{-3}$ | 0 (fixed)    | --           | --     |

$\chi^{2}/N_{\text{bins}} = 185 \pm 20_{19}^{16}$

$\chi^{2}/N_{\text{bins}} = 1.12 \pm 0.12^{+0.24}_{-0.24}$

$\delta_\text{1} = -11 \pm 5^{+3}_{-3}$

$\delta_\text{2} = -77 \pm 50_{-43}^{+48}$

$\delta_\text{3} = 20_{19}^{16}$

$\delta_\text{4} = 0.15 \pm 0.35^{+0.07}_{-0.05}$

$\delta_\text{5} = 77 \pm 44_{-33}^{+13}$

$\delta_\text{6} = 0.7$

jction for the entire range of the helicity angle $\theta^\pi_{\pi^-}$ of the $\pi^+\pi^-$ system (the angle between the kaon and the pion of the opposite charge in the $\pi^+\pi^-$ rest frame.) Thus only the difference in relative fractions can be observed from comparison of Figs. 3(a) and 3(b). The effect is more apparent in $M(\pi^+\pi^-)$ spectra for the two helicity angle regions $\cos\theta^\pi_{\pi^+}<0$ and $\cos\theta^\pi_{\pi^-}>0$ shown in Figs. 3(c–f). Here the difference in the interference terms for the $B^-$ and $B^+$ decay amplitudes (due to different relative phases between the $B\rightarrow\rho(770)K$ and $B\rightarrow f_0(980)K$ amplitudes) can be distinguished as a difference in the shape of the $M(\pi^+\pi^-)$ spectra for $B^-$ and $B^+$ decays. Results of the branching fraction and $A_{CP}$ measurements are summarized in Table 11 where for intermediate resonance fractions we use world average values [11]. The reconstruction efficiency is $22.4\pm0.2\%$, determined from signal MC simulation in which events are generated according to the matrix elements obtained from the best fit to data.

To assess how well any given fit represents the data, the Dalitz plot is subdivided into non-equal bins requiring that the number of events in each bin exceeds 25. A pseudo-$\chi^2$ variable for the multinomial distribution is then calculated as $\chi^2 = -2 \sum_{i=1}^{N_{\text{bins}}} n_i \ln \left( \frac{n_i}{n_c} \right)$, where $n_i$ is the number of events observed in the $i$-th bin, and $p_i$ is the number of predicted events from the fit. More details are given in Ref. [2]. The $\chi^2/N_{\text{bins}}$ value of the fit to signal events is 182.5/141 (32 fit parameters) and 127.6/120 for the fit to background events.

The following sources of systematic error are found to be dominant in the determination of branching fractions: charged track reconstruction (3% in total); particle identification efficiency (4.5% in total); requirements on event shape variables (2.5%); signal yield determination from the $\Delta E$ fit (3.9%); model dependence (1%); number of produced $BB$ pairs (1%). For the quasi-two-body channels additional sources are the uncertainty in parametrization of the background density function and the uncertainty in secondary branching fractions (2% for $f_2(1270)$, 11% for $K_0^*(1430)$ and 10.8% for $\chi^{0}$ [11]). Note that in the asymmetry calculation most of these systematic uncertainties cancel out. A few remaining sources are uncertainty due to a possible asymmetry in background from charmless $B$ decays (0.6%); the possible bias due to intrinsic detector asymmetry (1.6%); $B^\pm$ signal yields determination (1.1%).

To estimate model uncertainty in the branching fractions and $A_{CP}$ for individual quasi-two-body channels,
we vary the nominal model and repeat the fit to data. The following variations are performed separately: we add one additional channel which is either $K^*(1410)^0 \pi^+$, $K^*(1680)^0 \pi^+$, or $K_2^*(1430)^0 \pi^+$; remove $\omega(782)K^+$ or $f_2(1270)K^+$ channel from the nominal model; fit the data assuming $f_X(1300)$ is a vector ($\rho(1450)$) or excluding this contribution; and use several alternative parameterizations of the non-resonant amplitude $\frac{1}{f^2}$. To cross check the asymmetry observed in $B^\pm \to \rho(770)^0 K^\pm$, we make an independent fit to $B^-$ and $B^+$ subsamples. We also confirm the significance of the asymmetry observed in $B^\pm \to \rho(770)^0 K^\pm$ channel with MC pseudo-experiments where events are distributed according to the matrix element determined from the fit to data. All the cross-checks give consistent results. Finally note that the second solution with a much smaller fraction of the $K^*(1430)\pi$ signal as found in Ref. [8] is confirmed in this analysis. However, comparisons with results on elastic $K^\pi$ scattering [13] and with some theoretical considerations [14] favor the solution with a large $K^*(1430)\pi$ fraction. We find that values of $CP$ parameters $b$ and $\varphi$ are almost solution-independent; variation in their values is considered as a part of the model uncertainty.

In conclusion, we have performed an amplitude analysis of the three-body charmless $B^\pm \to K^\pm \pi^+ \pi^-$ decay. The branching fractions for a number of quasi-two-body channels have been measured; we report the first observation of $B^+ \to f_2(1270)K^+$, a tensor-pseudoscalar decay. We also perform a search for direct $CP$ violation in quasi-two-body intermediate states and find evidence for large direct $CP$ violation in the decay $B^+ \to \rho(770)^0 K^+$. This is consistent with recent results from BaBar [12] and with some theoretical predictions [8]. The statistical significance of the asymmetry is 3.9$\sigma$ and varies from 3.7$\sigma$ to 4$\sigma$ depending on the model used to fit the data. This is the first evidence for $CP$ violation in the decay of a charged meson. Statistical significance of the $A_{CP}$ for the $B^\pm \to \rho(770)^0 K^\pm$ channel is 3.0$\sigma$.

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TABLE II: Summary of branching fraction results. The first quoted error is statistical, the second is systematic and the third is the model uncertainty. Note that $B^+ \to \chi_c0K^+$ contribution is not included in the three-body charmless branching fraction.

| Mode | $B(B^\pm \to RH^\pm \to K^\pm \pi^+ \pi^-) \times 10^6$ | $B(B^\pm \to RH^\mp) \times 10^6$ | $A_{CP}$ (%) |
|------|-----------------------------------------------|---------------------------------|---------------|
| $K^\pm \pi^+ \pi^+$ Charmless | $48.8 \pm 1.1 \pm 3.6$ | $-9.67 \pm 0.64 \pm 0.72 \pm 0.37$ | $+4.9 \pm 2.6 \pm 2.0$ |
| $K^*(892)[K^\pm \pi^+]\pi^\mp$ | $6.45 \pm 0.43 \pm 0.48 \pm 0.25$ | $-51.6 \pm 1.7 \pm 6.8 \pm 1.8$ | $-7.7 \pm 6.5 \pm 2.0 \pm 1.6$ |
| $K_0^*(1430)[K^\pm \pi^+]\pi^\mp$ | $32.0 \pm 1.0 \pm 2.4 \pm 1.1$ | $-3.89 \pm 0.47 \pm 0.29 \pm 0.32$ | $3.33 \pm 0.30 \pm 0.11 \pm 0.20$ |
| $\rho(770)^0[\pi^+ \pi^-]K^\pm$ | $8.78 \pm 0.82 \pm 0.65 \pm 0.55$ | $1.33 \pm 0.30 \pm 0.11 \pm 0.20$ | $+0.06 \pm 0.04 \pm 0.12$ |
| $f_0(980)[\pi^+ \pi^-]K^\pm$ | $0.75 \pm 0.17 \pm 0.06 \pm 0.11$ | $-1.94 \pm 1.3 \pm 1.1$ | $-1.3 \pm 1.1$ |
| Non-resonant | $-1.94 \pm 1.3 \pm 1.1$ | $-1.3 \pm 1.1$ | $-1.3 \pm 1.1$ |
| $\chi_{c0}[\pi^+ \pi^-]K^\pm$ | $0.56 \pm 0.06 \pm 0.04 \pm 0.12$ | $112 \pm 12 \pm 18 \pm 24$ | $-6.5 \pm 20 \pm 2.0 \pm 1.4$ |

FIG. 3: $\pi^+ \pi^-$ mass spectra for $B^-$ (left column) and $B^+$ (right column) events for different helicity regions: (a,b) no helicity cuts; (c,d) $\cos \theta_{K\pi}^\varphi < 0$; (e,f) $\cos \theta_{K\pi}^\varphi > 0$; Points with error bars are data, the open histogram is the fit result and the hatched histogram is the background component.
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