ABSTRACT
We explore galaxy properties in general and properties of host galaxies of gamma-ray bursts (GRBs) in particular, using $N$-body/Eulerian hydrodynamic simulations and the stellar population synthesis model, STARBURST99, to infer observable properties. We identify simulated galaxies that have optical star formation rate (SFR) and SFR-to-luminosity ratio similar to those observed in a well-defined sample of 10 host galaxies. Each of the numerical counterparts is found in catalogues at the same redshifts as the observed hosts. The counterparts are found to be low-mass galaxies, with low mass-to-light ratio $M/L$, recent epoch of formation and high ratio between the SFR and the average of the SFR. When compared to the overall galaxy population, they have colours much bluer than the high-mass star-forming galaxy population. Although their SFRs span a range of values, the specific rates of the numerical counterparts are equal to or higher than the median values estimated at the different redshifts. We also emphasize the strong relationships between the specific SFR and quantities known to reflect the star formation history of galaxies, that is, colour and $M/L$: at intermediate redshift, the faintest and bluest galaxies are also the objects with the highest specific rates. These results suggest that GRB host galaxies are likely to be drawn from the high specific SFR subpopulation of galaxies, rather than the high SFR galaxy population. Finally, as indicated by our catalogues, in an extended sample, the majority of GRB host galaxies is expected to have specific SFRs higher than found in the magnitude-limited sample studied here.

Key words: galaxies: evolution – galaxies: formation – large-scale structure of Universe – gamma rays: bursts.

1 INTRODUCTION
Galaxies with a wide variety of properties are observed in the Universe and galaxy subpopulations contribute in a different way to the overall galaxy properties at different redshifts. Important questions in present day cosmology include investigations into how the different subpopulations can be characterized, how subpopulations formed at high redshift evolve into galaxies in the local Universe and how these populations contribute to various properties of the overall galaxy population. In this paper we use a numerical approach to extend our investigation of galaxy properties (Courty, Björnsson & Gudmundsson 2004, hereafter referred to as Paper I) that focused on the specific star formation rate (SFR). While the SFR is a 'snapshot' of the stellar activity in a galaxy, the specific rate is an indicator of how the galaxy forms its stellar mass relative to the total mass that has been assembled through its entire lifetime, via mergers and/or transformation of new accreted gas. The specific rate should therefore give some insight into the star formation history of galaxies, as do other properties, such as colours. The specific SFR has been estimated in a number of observational studies: Guzman et al. (1997) compare the specific SFRs of compact blue galaxies with other galaxy populations, Brinchmann et al. (2004) discuss the star-forming galaxies of the SDSS, Bell et al. (2005) combine infrared (IR) data from the Spitzer Space Telescope with optical data and Feulner et al. (2005) estimate the specific SFR up to $z = 5$.

As in Paper I, we here focus on the properties of a particular population of galaxies, namely the host galaxies of long-duration gamma-ray bursts (GRBs). The nature of the hosts and their evolution with redshift are still open questions. The emphasis over the last few years has been on the host galaxies of long-duration GRBs, which are seen as a powerful tracer of massive star formation in the Universe. It is now well established that at least some long-duration GRBs occur at the death of massive stars (e.g. Hjorth et al. 2003; Stanek et al. 2003) and in a cosmological context massive stars are very short-lived. Because of their extreme brightness, long-duration GRBs are an effective way of locating distant galaxies, most of
which are so faint that they would go undetected in galaxy surveys. In fact, host galaxies fainter than magnitude 29 have already been detected (Jaunsen et al. 2003). In addition, GRBs have been detected out to a redshift higher than \( z = 6 \), and will likely be detected to even higher redshifts. Rather detailed studies of the local star-forming regions in the hosts is therefore possible (Berger et al. 2005, 2006). The most distant burst to date, GRB 050904 at \( z = 6.29 \) (Kawai et al. 2005; Tagliaferri et al. 2005), has already revealed a number of interesting properties of the interstellar medium of the host (Totani 2006), while information about galaxy formation and evolution is yet to be explored in detail, mostly awaiting the increase of the currently modest sample size (around 50 hosts).

From individual studies of host galaxies of GRBs (Fruchter et al. 1999; Frybbo et al. 2003), comparison of host samples with other sources detected in various deep surveys (Le Floc’h et al. 2003), and statistical stellar population synthesis (SPS) of the optical and near-IR (NIR) host properties (Sokolov et al. 2001; Chary, Becklin & Armus 2002; Christensen, Hjorth & Gorosabel 2004), indications are that host galaxies have particular characteristics. These galaxies tend to be optically subluminous, low-mass, blue, starbursting galaxies, with young stellar populations, a modest activity of optical star formation, and perhaps low-metallicity and modest amount of dust obscuration, although this last feature still needs to be firmly established. Le Floc’h et al. (2003) compare a large sample of host galaxies of GRBs, observed in the NIR, with various galaxy surveys and find that the observed \( K \)- and \( R \)-band magnitudes of the hosts are comparable to the field sources selected in optical/NIR deep surveys, but differ significantly from luminous and dusty starburst galaxies observed with ISO and Submillimetre Common-User Bolometer Array (SCUBA). Moreover they show blue \( R - K \) colours typical of the faint blue galaxy population in the field at \( z = 1 \). Also, SCUBA submillimetre observations of GRB host galaxies performed by Smith et al. (2005) suggest that most hosts are not luminous dusty star-forming galaxies. Furthermore, Christensen et al. (2004) have studied a magnitude-limited sample of hosts and estimate the ratio between the rest-frame ultraviolet (UV) SFR and the host optical luminosity. They suggest that the hosts are similar to those HDF galaxies that have the highest SFR-to-luminosity ratios.

In Paper I, we showed that among the population still actively forming stars at low redshift, the high-mass galaxies have much lower specific SFR than the low-mass galaxies. The non-star-forming galaxies, that span the whole galaxy mass range, are old galaxies while most of the stellar populations in the high specific SFR galaxies formed recently. At high redshift the trend of increasing specific SFR with decreasing galaxy mass is also seen, but an interesting point is that the cosmological evolution is much stronger for the high-mass than the low-mass galaxies. These trends agree in general well with the aforementioned observational estimates, to the extent that we concentrate on the qualitative behaviour of the specific SFR. Although not based on observable properties, the results of Paper I for the specific SFR suggest that a subpopulation of faint and blue galaxies, some of the characteristics of the GRB hosts, are likely to belong to the high specific SFR galaxy population, rather than the high-SFR population.

In this paper, we extend the discussion of the properties of GRB host galaxies in Paper I, by combining the results of the same simulations as in that paper with the SPS code, STARBURST99 (Vázquez, Leitherer & Heckman 2005), to infer observable properties. SPS codes allow us to compute the spectral energy distributions (SEDs) of the simulated galaxies at different redshifts. We identify simulated galaxies that have both similar rest-frame UV SFRs and ratios between this SFR and the \( B \)-band luminosity as the 10 observed hosts of a well-defined sample (Christensen et al. 2004, hereafter Chr04). The numerical counterparts of these observed hosts are characterized by a variety of properties, estimated either directly from the simulation or from the computation of the SEDs. In particular, for each galaxy we determine the mass, the ratio between the SFR and the average of the SFH, \( SFR/\langle SFR \rangle \), the specific SFR, the epoch of formation (EoF), the \( R - K \) colour and the mass-to-light ratio (M/L). The properties of the counterparts are then compared to the overall galaxy population, which is characterized through the close relationships between the specific SFR and the colour index and M/L. This comparison is, however, limited by the fact that the observed sample still only includes 10 hosts, spanning a large redshift range.

Although fairly small, the sample of Chr04 is the only available homogeneous sample that estimates the ratio between the optical SFR and the luminosity. Information on other hosts does exist in the literature and other studies, for example, Sollerman et al. (2005), use different SFR estimators such as SFR_{UV} and SFR_{B}, rather than the UV-based indicator adopted in Chr04, but only for a couple of hosts. A comprehensive study of a large host sample using all available information awaits future studies. In Section 3 we also briefly discuss the counterparts of GRB 000911 and 030329, whose SFR_{UV} and \( M_B \) values are available in Masetti et al. (2005) and Gorosabel et al. (2005), respectively.

The paper is organized as follows. In Section 2, we describe briefly the simulation and use of the SPS code. Section 3 contains the main results of the paper. It starts by discussing the observed host sample we use (Section 3.1) and the procedure used to identify the numerical counterparts (Section 3.2). We discuss the observational properties of the counterparts in Section 3.3 and compare their properties with those of the galaxy population in Section 3.4. Section 4 concludes the paper.

### 2 Numerical Procedure

We repeat the simulation used in Paper I in order to obtain galaxy catalogues at the same redshifts as that of the observed GRB hosts in the sample of Chr04. We briefly recall the numerical method and we refer to Paper I for details regarding the simulation. The three-dimensional \( N \)-body/hydrodynamical code couples a PM scheme for computing gravitational forces with an Eulerian approach for solving the hydrodynamical equations. The dominant processes relevant for galaxy formation are included: gravitation, hydrodynamical shocks and radiative cooling processes. Collisional ionization equilibrium is not assumed and the cooling rates are explicitly computed from the evolution of a primordial composition hydrogen–helium plasma. The cosmological scenario adopted is a Lambda cold dark matter model with the following parameters: \( H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}, \Omega_k = 0, \Omega_m = 0.3, \Omega_{\Lambda} = 0.7, \Omega_B = 0.02 \text{ h}^{-2} \) with \( h = H_0/100, \sigma_8 = 0.91 \). The comoving size of the computational volume is \( 32 \text{ h}^{-1} \text{ Mpc} \) and the simulation has \( 256^3 \) dark matter particles and an equal number of grid cells. Galaxy formation is introduced using a phenomenological approach. At each time-step, in cells whose gas satisfies given criteria, a fraction of the gas is turned into a stellar particle of mass \( m_\star \) and EoF \( \alpha_\star \), the scalefactor corresponding to the cosmic time, \( t_* \). The criteria are the following. The cooling time must be less than the dynamical time, \( t_{cool} < t_{dyn} \); the baryonic density contrast, \( (1 + \delta_\rho) \), must be higher than a threshold \( (1 + \delta_\rho_0) = 5.5 \); the mass of the gas must be in a converging flow, \( \nabla \cdot \mathbf{V} > 0 \), and the size of the cell must be less than the Jean’s length, given by \( \lambda_3 = c_s (\pi/G \rho)^{1/2} \). The mass \( m_\star \) is given by \( m_{\text{bg}} (t_\star) \Delta t/t_* \),

\[ \delta_{\text{thresh}} = \left( \frac{c_s}{\sqrt{H_0}} \right)^{1/2} \]
where $\Delta t$ is the time-step, the characteristic time is taken to be $t_c = \max(t_{\text{dyne}}, 10^8 \text{yr})$, and $m_g(t_1)$ is the baryonic mass enclosed within the grid cell. Galaxy-like objects are then defined, at any redshift, by grouping the stellar particles with a friend-of-friend algorithm. A simulated galaxy is therefore a collection of stellar particles of different masses formed at different epochs.

At any redshift, galaxies are characterized by their mass, $M$, defined as the sum of the mass of all the stellar particles the galaxy is composed of an EoF, defined to be the mass-weighted average of the EoF of all its stellar particles; and an SFR, $SFR^\ast$, defined as the amount of stellar material formed in the previous $10^8 \text{yr}$. We also estimate the specific SFR, $\epsilon \equiv \log(10^{12} \text{ yr } SFR^\ast/M)$, a quantity that measures the efficiency of the conversion of the gas into stellar material relative to the galaxy mass. We have, as in Paper I, only considered galaxies with a mass higher than $5 \times 10^9 M_\odot$ in the simulated catalogues. We refer to Paper I for an illustration of the different subpopulations of galaxies obtained.

Considering each stellar particle as a homogenous stellar population, the total SED of a galaxy can be computed from synthesis codes. Evolutionary synthesis codes combine stellar evolutionary theory to describe the time evolution of model stars, stellar atmosphere theory to transform quantities from the theoretical space to the observational one, and the stellar birthrate, giving the number of stars with a given mass formed at a given time. The stellar birthrate comes from the star formation history, which gives the number of stars born in a given time, and the initial mass function (IMF), which gives the relative number of stars born as a function of mass (see Cervino & Luridiana (2005) for a discussion regarding the uncertainties of the synthesis codes). In our procedure, the star formation history of a galaxy comes directly from the formation of its stellar particles, and the stellar birthrate comes from the star formation history, which gives the number of stars born in a given time, and the initial mass function (IMF), which gives the relative number of stars born as a function of mass (see Cervino & Luridiana (2005) for a discussion regarding the uncertainties of the synthesis codes).

The total SED of a galaxy at a given redshift is the sum of all the star-forming galaxies present in the galaxy. The SFR is constant in the later phases on given time-scales. These are roughly $10^7 \text{yr}$ for $H\alpha$ and $10^8 \text{yr}$ for the UV. These coefficients therefore depend on the IMF and its slope, the upper and lower mass cut-off and the metallicity (Boselli et al. 2001). Since one of the purposes of this paper is to find the numerical counterparts of observed host galaxies, we use the same indicator of the SFR as Chr04, and estimate it from the UV continuum at 2800 Å, although the SFRs of the two hosts at the highest redshifts are estimated using the UV continuum at 1500 Å in Chr04. The calibration factor used to convert the luminosity at 2800 Å into SFR is $1.4 \times 10^{-25}$, in units of $(M_\odot \text{ yr}^{-1})(\text{erg } s^{-1} \text{ Hz}^{-1})^{-1}$ (Kennicutt 1998). In our procedure the luminosity at 2800 Å is obtained by averaging the spectrum over 20 Å around 2800 Å. Note that, although our SEDs are determined at subsonic metallicity, we adopt the usual calibration to convert the UV luminosity into SFR that is estimated at solar metallicity. At lower metallicity the calibration increases due to the higher luminosity of low-metallicity stars. The SFR of low-metallicity galaxies when estimated with a calibration at solar metallicity is thus overestimated. The evolution of the calibration associated with different SFR indicators is estimated in Sullivan et al. (2001) and Bicker & Fritze-v. Alvensleben (2005), for instance. At $Z = 0.2 Z_\odot$, the latter paper found that the SFR is overestimated by a factor 1.4, compared to our calibration.

In Fig. 1, we compare the $SFR^\ast$, computed directly from the simulation, with the SFR estimated from the synthetic spectrum of

Figure 1. Comparison of $SFR^\ast$ with $SFR_{UV}$ obtained from the synthetic spectrum for galaxies at $z = 1$. Non-star-forming galaxies are for display purposes plotted at $SFR^\ast = 0.02 M_\odot \text{ yr}^{-1}$. The diagonal dashed line shows $SFR_{UV} = SFR^\ast$.  

1 http://www.stsci.edu/science/starburst99/
In the following sections we consider other quantities to characterize galaxies. The lifetime of a galaxy is estimated at a given redshift, $t(z) - t_{form}$, where $t_{form}$ is the epoch of the formation of the first stellar population. From this the average of the SFR, $\langle \text{SFR} \rangle$, at a given redshift is determined as the amount of stellar material formed over the lifetime of the galaxy. The SFR$^*$ is compared with the average through the ratio $\text{SFR}^*/\langle \text{SFR} \rangle$, that may be seen as analogous to the so-called birthrate parameter, $b$, (Kennicutt, Tamblyn & Congdon 1994). The $M/L$ values in the $B$ and $K$ bands are estimated using the solar magnitudes of $5.45$ and $3.3$, respectively, and the colour $R - K$ using the ‘Cousins $R$’ filter from the GALAXEV package. Finally, the ratio between the rest-frame UV SFR and the luminosity, SFR$_{UV}/(L_B/L_\odot)$, uses the characteristic magnitude or magnitude at the break of the local galaxy luminosity function, $M_\odot^* = -21$. This ratio is sometimes called the specific SFR as, for example, in Chr04, but we will refer to it by the term SFR-to-luminosity ratio and reserve the term specific SFR for the ratio between the SFR and the galaxy mass, as is customary in the literature.

### 3 THE NUMERICAL COUNTERPARTS OF OBSERVED GRB HOST GALAXIES

In this section we attempt to identify numerical counterparts to the host galaxies of the Chr04 sample, explore their properties and compare the host candidate population with the overall galaxy population. We first summarize the relevant properties of the observed sample and our approach to identifying the numerical counterparts. We then discuss their observed properties.

#### 3.1 The observed sample

The sample presented in Chr04 is homogeneous and consists of 10 GRB hosts with redshifts between $z = 2.037$ and $z = 0.433$. The sample is magnitude limited ($R < 25.3$) and ensures that hosts are bright enough to make multicolour photometry possible. The first column in Table 1 lists the hosts under consideration. The observationally determined values of SFR$_{UV}$ and SFR$_{UV}/(L_B/L_\odot)$ are given in tables 4 and 5 of Chr04 and we note that the SFR$_{UV}$ entering the SFR-to-luminosity ratio is not corrected for internal extinction, generally found to be moderate or low. The SFR spans a wide range (between 0.8 and 13 $M_\odot$ yr$^{-1}$), but hosts with redshifts higher than 0.9 have the highest SFR$_{UV}$, more than $\approx 6 M_\odot$ yr$^{-1}$, whereas hosts at lower redshifts have SFR$_{UV} < 2.5 M_\odot$ yr$^{-1}$.

Various observational studies of individual hosts of the Chr04 sample result in slightly different estimates of the same properties [Gorosabel et al. (2003b) for GRB 000418, Gorosabel et al. (2003a) for GRB 000210, Bloom et al. (1999) for GRB 990123, for instance]. We have not attempted to collect all the data existing in the literature, and have only considered the SFR$_{UV}$ and SFR$_{UV}/(L_B/L_\odot)$ given in Chr04. All the hosts in Chr04 are also discussed in Le Floch et al. (2003), giving either their observed $R$ and absolute $B$-band magnitudes or their observed $R$ and absolute $K$ magnitudes and colours, $R - K$. In addition to the Chr04 sample, we also consider two hosts for which the SFRs based on the rest-frame UV flux as well as the $B$-band magnitudes, are available. We can examine such hosts in a similar way as for the Chr04 sample. Masetti et al. (2005) discuss the properties of the host galaxy of GRB 000911 at $z = 1.06$ and derive a $B$-band magnitude of around $-18.4$, giving a $L_B/L_\odot = 0.09$, with our $M_B^*$ (see Section 2), and an extinction-corrected SFR$_{UV}$ of 2.7 $M_\odot$ yr$^{-1}$. Assuming an extinct SFR$_{UV}$ to be a factor of 2.

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**Figure 2.** The mass–magnitude diagrams (upper panel: $K$ band, lower-panel: $B$ band) for the simulated galaxies at $z = 1$. In both panels, dots denote star-forming galaxies while the small dots denote the non-star-forming galaxies. The estimate of $M_\odot^* = -24.7$ around $z = 1$ from the K20 galaxy survey (Pozzetti et al. 2003) is marked by the dotted horizontal line.

![Mass-Magnitude Diagrams](https://example.com/mass-mag.png)
Table 1. Properties of the numerical counterparts corresponding to the GRB hosts listed in column one. Following the redshift of the simulated catalogue in Column 2, the percentage errors in SFR$_{\text{UV}}$ and the SFR-to-luminosity ratio, $\Delta X$ and $\Delta Y$ defined in the text, are given in Columns 3 and 4. Column 5 shows the mass of the counterpart, while Column 6 shows the epoch of its first formed stellar population, $t_{\text{form}}$ (see Section 2 for definition) relative to the Hubble time. The $M/L$ values in the $B$ and $K$ bands, respectively, are given in Columns 7 and 8, followed by the corresponding absolute magnitudes. Then comes the colour index, $R - K$, and the next to last column lists the $(R|AB)$ apparent magnitude. Finally, a reference number for each host is given in the last column.

| GRB    | $z$  | $\Delta X$ | $\Delta Y$ | $M$ (M$_{\odot}$) | $1 - t_{\text{form}}/t_{H}$ | M/L$_B$ | M/L$_K$ | $M_B$ | $M_K$ | $R - K$ | $(R|AB)$ | #  |
|--------|-----|------------|------------|-------------------|-----------------------------|---------|---------|-------|-------|--------|----------|-----|
| 000926 | 2.036 | 0.7        | 0.5        | $1.16 \times 10^{10}$ | 0.76                      | 0.36   | 0.36    | -22.97 | -20.83 | 2.61   | 24.41    | 1   |
| 990123 | 1.592 | 5.6        | 3.2        | $2.41 \times 10^{10}$ | 0.81                      | 0.47   | 0.59    | -23.47 | -21.08 | 3.50   | 24.27    | 2   |
| 000418 | 1.113 | 5.8        | 8.8        | $8.27 \times 10^{9}$ | 0.86                      | 0.35   | 0.32    | -22.63 | -20.57 | 2.47   | 23.24    | 3   |
| 980703 | 0.963 | 1.3        | 0.6        | $3.68 \times 10^{10}$ | 0.88                      | 0.52   | 0.66    | -23.82 | -21.41 | 2.87   | 22.18    | 4   |
| 000210 | 0.843 | 6.5        | 5.7        | $5.16 \times 10^{9}$ | 0.89                      | 0.47   | 0.54    | -21.79 | -19.50 | 2.61   | 23.64    | 5   |
| 970508 | 0.832 | 3.7        | 0.3        | $7.20 \times 10^{8}$ | 0.89                      | 0.30   | 0.25    | -20.14 | -18.18 | 2.22   | 24.84    | 6   |
| 991208 | 0.704 | 1.2        | 0.9        | $1.69 \times 10^{9}$ | 0.90                      | 0.41   | 0.45    | -20.71 | -18.46 | 2.54   | 24.24    | 7   |
| 970228 | 0.695 | 10.8       | 0.5        | $1.60 \times 10^{9}$ | 0.90                      | 0.49   | 0.56    | -20.49 | -18.19 | 2.51   | 24.41    | 8   |
| 010921 | 0.449 | 1.9        | 1.1        | $8.97 \times 10^{9}$ | 0.92                      | 0.68   | 1.01    | -22.01 | -19.42 | 2.58   | 21.93    | 9   |
| 990712 | 0.429 | 3.3        | 2.1        | $1.42 \times 10^{9}$ | 0.92                      | 0.38   | 0.36    | -20.62 | -18.55 | 2.07   | 22.71    | 10  |

The properties that are estimated directly from the simulation output are the SFR SFR$^*$, the specific SFR, the galaxy mass, the ratio SFR$^*/$SFR, the formation epoch of the first stellar population to form in the galaxy, and the EoF of the galaxy as defined in Section 2. From the computation of the SEDs we determine the SFR SFR$_{\text{UV}}$, the SFR-to-luminosity ratio, the magnitudes in the $B$ and $K$ bands, the apparent $R$ magnitude and the colour, $R - K$. The $M/L$ values in the $B$ and $K$ bands are then a combination of the primary simulation outputs and the observable properties.

3.2 Counterpart identification

We generated catalogues of galaxies at the same redshifts as the observed hosts, and looked in each catalogue for simulated galaxies that have both SFR$_{\text{UV}}$ and SFR$_{\text{UV}}$/($L_B/L_K$) nearest to the corresponding values for each observed host. We are able to find a numerical counterpart to each of the 10 observed host of the Chr04 sample, although departures from the observationally inferred values may be large in some cases. The percentage errors in Table 1 quantify how close from these values the counterpart is found. They are defined by $\Delta X = |SFR_{\text{obs}} - SFR_{\text{num}}|/SFR_{\text{obs}}$ and $\Delta Y = |L_{\text{obs}} - L_{\text{num}}|/L_{\text{obs}}$. In this last definition, $L_{\text{obs}}$ denotes the SFR-to-luminosity ratio. The largest departures, when at least one of these quantities is larger than 5 per cent, are seen for counterparts #3, #5 and #8. The first two are noted in Chr04 as having the least acceptable fits to their SEDs. The host of GRB 000418 (#3) is extensively discussed in Gorosabel et al. (2003b) who analyse its SED using a variety of synthetic spectral templates. The adopted SFR does of course depend on the adopted SED. Also, Gorosabel et al. (2003a) find the host galaxy of GRB 000210 (#5) to be brighter than the Chr04 estimate: they find that the $B$-band magnitude is $-20.16$, giving, with their SFR$_{\text{UV}} = 2.1 \text{ M}_{\odot} \text{ yr}^{-1}$, an SFR$_{\text{UV}}/(L_B/L_K)^* = 4.5 \times 10^{-7}$ in Chr04.¹

Each numerical counterpart is characterized by a number of properties that are either tabulated in Table 1 or displayed in Figs 3 and 5. The properties that are estimated directly from the simulation output are the SFR SFR$^*$, the specific SFR, the galaxy mass, the ratio SFR$^*/$SFR, the formation epoch of the first stellar population to form in the galaxy, and the EoF of the galaxy as defined in Section 2. From the computation of the SEDs we determine the SFR SFR$_{\text{UV}}$, the SFR-to-luminosity ratio, the magnitudes in the $B$ and $K$ bands, the apparent $R$ magnitude and the colour, $R - K$. The $M/L$ values in the $B$ and $K$ bands are then a combination of the primary simulation outputs and the observable properties.

3.3 ‘Observed’ properties of the numerical counterparts

From Table 1 we note the following. Low-redshift hosts ($z < 0.9$) are low $B$-band luminosity galaxies, $M_B > -20$. We also see that the counterparts are fainter than $-22$ in the $K$ band at $z < 0.9$. The 10 counterparts are low-mass galaxies with $M < 4 \times 10^{10} \text{ M}_{\odot}$ (the highest mass in the simulation at $z = 1$, being $7.4 \times 10^{11} \text{ M}_{\odot}$). The $B$-band magnitudes and mass of the counterparts can also be seen in Fig. 3 discussed below, where in the upper panel the dotted curves denote values of constant $M_B = -18$ to $-23$ (from left- to right-hand side) and in the lower panel the dashed lines indicate values of constant mass of $10^9$ to $10^{11} \text{ M}_{\odot}$ (from left- to right-hand side). The counterparts have $L_B/L_K$ between $0.074$ and $1.46$ and $L_K/L_B$ between $0.028$ and $0.84$ (with $M_K^* = -24$), making most of them subluminous galaxies. The $M/L$ values in Table 1 are relatively small and more typical of late-type and dwarf galaxies than large spirals or elliptical galaxies.

The counterparts have apparent $R$-band magnitudes between $22$ and $24.4$ and comparison between those and the NIR observational data reported in Le Floc’h et al. (2003) for the same hosts (here referred to as the common sample) shows that the candidate hosts #6 and #9 are the faintest and the brightest, respectively, both of our sample and of the common sample. The apparent $R$-band magnitudes of the counterparts are, however, generally slightly brighter than in Le Floc’h et al. (2003). The bluest of the nine counterparts (#10) for which the $R - K$ colours of the corresponding hosts were estimated in Le Floc’h et al. (2003), is also the bluest of these nine observed hosts. The observed host with the highest colour index corresponds the counterpart with the second highest colour index (after the least blue #2). Globally, we do find that nine counterparts have $R - K$ colours between $2$ and $2.9$ and $3.5$ for #2.

¹The host of GRB 991208 has roughly similar $B$-band magnitude and $A_B$ and has a ratio of non-extinct/extinct SFR within a factor of 2 (Chr04).

²Instead of adopting the nearest counterpart in each catalogue, we could have looked for the second best closest counterparts or the counterparts within a given error box around each observed host. Because of the uncertainties in the observationally determined values and the small number of observed hosts in the sample we consider here, we do think that searching only for the closest counterpart is the most reasonable thing to do.
As noted above, the hosts have various SFRs, be it either the SFR* or the SFRUV, but they have high SFR-to-luminosity ratio and high specific rate, as they all lie in the upper half of both panels in Fig. 3. The specific SFR and the SFR-to-luminosity ratio would be even better correlated if the latter quantity is based on the K-band luminosity, according to the magnitude-mass diagrams in Fig. 2.

3.4 Comparison with the overall galaxy population

Even if some aspects of the simulation may be incomplete, it provides us with catalogues of galaxies at various redshifts in which different galaxy populations may be distinguished. After defining a particular subpopulation of galaxies, for example, similar to the host galaxies of GRBs, an important issue is to compare this particular population to the overall galaxy population. Such a comparison is in the present case limited by the fact that the observed sample includes only 10 hosts, spanning a wide redshift range where cosmological evolution cannot be neglected.

3.4.1 The relationship between the specific SFR and the colour index

We first conduct a qualitative comparison between the counterparts and the overall galaxy population at $z = 1$, focusing on the relationship between the specific SFR and the SFRUV and colour index. By presenting observable properties at this redshift we follow-up on and extend the results and discussion of Paper I.

Fig. 4 presents the SFRUV values and colour index of the whole galaxy population distinguished according to the specific rate ($\epsilon < 1, 1 < \epsilon < 1.3$ and $\epsilon > 1.3$). We also plot the low-mass ($M < 5 \times 10^9 M_\odot$) and high-mass ($M > 5 \times 10^9 M_\odot$) non-star-forming galaxies. We use the same threshold, $\epsilon = 1.3$, as in Paper I. It corresponds roughly to the peak of the probability density function of the specific SFR at $z = 1$. In addition, galaxies with specific rates below or above this value contribute about equally to the total SFR at that redshift. The top panel in Fig. 4 shows the large variation of the SFRUV with respect to the galaxy mass, but there is a clear correlation with the specific SFR (i.e. $\epsilon$). High-mass non-star-forming galaxies have large $M/L_\lambda$, up to about 1, whereas the minimal value for the low-mass high-specific rate galaxies is $\sim 0.15$. The $M/L_\lambda$ in the $B$ band, $M/L_\lambda B$, ranges between $\sim 0.09$ and $\sim 3$, for the overall population. Recalling the results in Table 1, we note that the majority of the counterparts have log $(M/L_\lambda)$ between $-0.5$ and $-0.3$, typical of our low-mass, high specific SFR galaxies, although it should be kept in mind that Fig. 4 is plotted at a single redshift ($z = 1$).

The $colour$–$magnitude$ diagram in the bottom panel in Fig. 4 shows a large variation of the $colour$ index $R - K$, from 1.5 to 4.7, consistent with that seen in the recent K20 galaxy survey (Pozzetti et al. 2003). The high-mass, non-star-forming galaxies, that are also old objects (see Paper I) have the highest colour index, close to the typical value of old elliptical galaxies at $z \gtrsim 1$. In contrast, the majority of the star-forming galaxies have colours around 3. The colour properties correlate with the specific SFR. The bluest objects are also faint galaxies with the highest specific rates. Comparing the data from Table 1 with Fig. 4 shows that the counterparts are clearly bluer than the high-mass star-forming galaxy population, with colour index lower than $\sim 3$. Recalling the correlation between mass and magnitude discussed in the previous section, we note that the colours and $M/L_\lambda$ values are also tightly related (Bell & de Jong 2001). There is also a strong relation, albeit with some dispersion between mass and SFR, resulting in intermediate colours of the

![Figure 3. SFR-to-luminosity ratio versus SFRUV (upper panel) and specific SFR versus SFR* (lower panel) for the star-forming galaxy population at $z = 0.832$. The dotted curves in the upper panel denote constant $M_B$ values from $-18$ to $-23$ (left- to right-hand side). In the lower panel the dotted lines indicate constant mass of $10^9, 10^{10}$ and $10^{11} M_\odot$ (left- to right-hand side). Although at different redshifts, the numerical counterparts of the observed host galaxies (listed in Table 1) are displayed in both panels (solid symbols). In decreasing order of SFRUV, GRB 980703, 000926, 000418, 990123, 002101, 010921, 990712, 970508, 991208, 970228 (the order is the same in the bottom panel with SFR*, except that the host of GRB 970228 is to the left-hand side of GRB 991208). In the upper panel, for each counterpart a short line segment indicates where the corresponding observed host galaxy would be found. In some cases the difference is too small for the line segment to be visible. The two diamonds denote the counterparts at the highest redshifts.](https://academic.oup.com/mnras/article-abstract/376/3/1375/1747654)
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Figure 4. Mass-to-light ratio in solar units in the $K$ band as a function of mass (upper panel) and colour–magnitude diagram (bottom panel) for the simulated galaxy population at $z = 1$. For clarity, only 1000 objects randomly selected from the catalogue, are plotted. The dots indicate non-star-forming, low-mass ($M < 5 \times 10^{10} M_\odot$) galaxies; the filled circles non-star-forming, high-mass ($M > 5 \times 10^{10} M_\odot$) galaxies; the open circles star-forming galaxies with $\epsilon < 1$; the open squares star-forming galaxies with $1 < \epsilon < 1.3$; the filled squares star-forming galaxies with $\epsilon > 1.3$. Galaxies with a mass around $10^{11} M_\odot$, corresponding in Fig. 2 to the characteristic magnitude $M_\star^*_{Ks} = -24.7$ (or $L_\star^*_{Ks} = 1.6 \times 10^{11} L_\odot$), have an $M/L$ of $\log(M/L_K) \sim -0.2$.

Figure 5. Probability density functions of the SFR$^*/\langle SFR \rangle$ (upper panel) and the EoF, when normalized to the Hubble time (bottom panel), for the star-forming galaxy populations at $z = 2.036$ (dotted line) and $z = 0.832$ (dashed line). The counterparts of the hosts in Table 1 are superposed at arbitrary ordinate, but in order of decreasing redshift (from top to bottom).

3.4.2 The star-forming activity of the counterparts

Fig. 5 compares the SFR$^*/\langle SFR \rangle$ and the EoF of the counterparts to that of the star-forming galaxy population at $z = 0.832$ (dashed lines) and $z = 2.036$ (dotted lines), the highest redshift of the host sample. In each panel the counterparts are superposed on the distributions at arbitrary ordinate values, but with a decreasing redshift (from top to bottom). Strictly speaking only two hosts, #1 and 6, should be compared directly to their respective distributions.

The top panel compares the star-forming activity at a given redshift of a galaxy to its average activity since the object started to form its stellar populations. Both distributions peak around unity, but the high-redshift distribution includes more galaxies with SFR$^*/\langle SFR \rangle > 1$, meaning that high-redshift galaxies are more active than present-day galaxies. All hosts except #2 have SFR$^*/\langle SFR \rangle$ close to or above unity (0.85 for #9).

The lower panel shows the EoF normalized to the Hubble time. Comparing the distributions at the two redshifts shows that the low-redshift one is more extended but includes a non-negligible amount of objects with recent epochs of formation. All candidate hosts have ages within 40 per cent of the age of the universe. We remind the reader that the distributions are constructed only from the star-forming galaxies and do not include the old, non-star-forming galaxies. The EoF indicates the epoch at which the galaxy was the most active and is expected to be quite different from the EoF of the first stellar populations, $t_{form}$. Table 1 shows that the EoF of the counterparts are indeed different from $t_{form}$. This particular time is
relatively close to 1 (as defined in Table 1), meaning that the candidate hosts include an early-formed stellar population, although not dominant since they are at the same time young objects.

That the major fraction of the mass of most counterparts was assembled in the recent times is consistently shown by the specific rate, the ratio SFR*/(SFR) and the EoF. We note that the three hosts with the highest SFR*/(SFR) ratios (counterparts #3, 6 and 10), also have the highest specific rates although their SFR* and magnitudes differ widely (GRB 000418, 990712 and 970508, see Fig. 3). They are among the hosts with the youngest epochs of formation, the bluest $R - K$ colours and the lowest $M_{\text{II}}$ values (Table 1), pointing again to the tight correlation between these galaxy properties as discussed above and to the consistency with the GRB host galaxy properties.

3.5 Discussion

Here, we emphasize our main result by comparing the SFR-to-luminosity ratios and specific SFRs of the numerical counterparts to the median values of these quantities in the catalogues they are selected from. These are displayed in Fig. 6. The median value of the specific SFR clearly increases with redshift. Note that at redshifts below $z \sim 0.7$, the minimal specific SFR tends to increase with decreasing redshift. This is due to the fact that the star formation of massive galaxies slows down as the redshift decreases and eventually ceases in an increasing number of them. They therefore disappear from the star-forming galaxy population. Comparing the specific SFRs and the SFR-to-luminosity ratio of the counterparts to the median values at similar redshift shows that the counterparts in all cases except one have values higher than the median. The only exception is the counterpart to GRB 990123 (#2). The SFR $\nu_{\text{UV}}/L_\odot$ of this particular host is the lowest of the Chr04 sample and its observed SED was best fit by a star-forming galaxy spectrum, whereas all of the other hosts were fit by starburst templates. The $B$-band magnitude of this host could however be fainter (Bloom et al. 1999), giving a higher SFR-to-luminosity ratio. Moreover, the $R - K$ colour of this host is as blue as most of the hosts studied in Le Floc'h et al. (2003), whereas it is the reddest one of our sample, as seen above (see Table 1).

It is interesting to note that Chary et al. (2002) estimate the specific SFRs of hosts #2, 4, 6, 7 and 8, although their observational study is based on extinction-corrected SFRs, and their derived specific rates are much higher than our results. The observed hosts #4, 6, 7 and 8 are among those with the highest specific SFR of the whole Chary et al. (2002) sample. They are also found to have higher specific rates than local starburst galaxies. The numerical counterparts to #6, 7 and 8 have specific rates well above the median values (the first three objects on the left-hand side in Fig. 3).

The two squares in Fig. 6 show the SFR-to-luminosity ratio and the specific SFR of the counterparts of the hosts of GRB 000911 and 030329, discussed at the beginning of this section. These counterparts were searched for in catalogues at slightly different redshifts from the host redshifts, $z = 1$ and 0.133, respectively. The counterpart of GRB 000911 ($\Delta X = 0.3$ and $\Delta Y = 5.2$ per cent) is a low-mass, young object ($M = 1.1 \times 10^9 M_\odot$, $1 - \text{EoF}/H_{\text{H(I)}} = 0.37$) with a high specific rate ($\epsilon = 1.87$), blue colour $R - K = 2.12$ and $M/\ell_{\text{K}} = 0.36$. The closest counterpart that we find for the host of GRB 030329 has a lower SFR-to-luminosity ratio than the observed estimate ($\Delta X = 1.7$ per cent but $\Delta Y = 19$ per cent). The candidate host is a low-mass object ($M = 1.4 \times 10^9 M_\odot$), with blue colour $R - K = 2.2$, a specific rate of $\epsilon = 0.7$ and an EoF of $1 - \text{EoF}/i_{\text{H(I)}} = 0.45$. Compared to the overall population these two candidate hosts have SFR-to-luminosity ratios and specific SFRs well above or similar to the median values at the same redshifts.

The fact that the Chr04 sample is magnitude limited and includes bright hosts may explain why the numerical counterparts are not found among the objects with the highest possible specific SFRs. The counterpart of GRB 970508 (#6) is an example. From HST observations and other studies, this host may be described as a blue compact dwarf galaxy (Fruchter et al. 2000). Could this host be a prototype of the general host GRB galaxy population? Interestingly, the counterpart of this host could be found in the sample of compact galaxies at $z \sim 0.7$ analysed in Guzman et al. (1997). The counterpart #6 ($z = 0.83$) with an absolute magnitude $M_{\text{B}} = -18.2$, a mass close to $10^9 M_\odot$ and a specific rate of $\epsilon \sim 1.8$ falls into the fainest and highest specific SFR population of compact galaxies in Guzman et al. (1997) (see their figs 5 and 7). Moreover, Sollerman et al. (2005) discuss three GRB host galaxies and show that they have similar properties as a sample of compact blue galaxies in the local Universe.

4 CONCLUSIONS

In this paper, we have discussed cosmological galaxy properties and the properties of host galaxies of GRBs in particular, using...
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Fully hydrodynamic simulations of galaxy formation and the SPS code, STARBUSt99, to infer observable properties. An important feature of the numerical procedure is that the star formation history of galaxies entering the SPS code, comes directly from the simulation, with each stellar population contained in a given galaxy treated as a homogenous population, that forms instantaneously. We identify objects in the simulation that have optical SFR, SFR$_{UV}$ and SFR-to-luminosity ratio, SFR$_{UV}/(L_B/L_B^*)$, similar to those estimated in a well-defined sample of 10 observed host galaxies (Chr04), the only available homogeneous sample focusing on this ratio. Each numerical counterpart is selected from a simulated catalogue at the same redshift as the corresponding observed host, and is characterized by a number of properties. The SFR$^*$, mass, specific SFR, SFR$^*/(SFR)$, EoF of the first stellar population and EoF of the galaxy object. These are obtained directly from the simulation. In addition, B- and K-band luminosities, R-band apparent magnitude, R − K colour and MIL values are obtained from the SPS or combination of both results. It should be emphasized that some of these properties (e.g. mass and SFR$^*$) are estimated directly from the simulations, making their definition inherently different from those commonly adopted in observations.

The Chr04 sample includes host galaxies with redshifts in the range 0.43 < z < 2.03. The sample is magnitude-limited (R < 25.3), with estimated absolute B-band magnitudes between −21.4 and −18.1. Our counterpart hosts are low-mass galaxies (M < 4 × 10$^{10}$ M$_\odot$), with low MIL values (M/L$_B$ around 0.5); most of them are blue (R − K < 2.9) and young galaxies, with epochs of formation (or ages), within 40 per cent of the age of the universe at the different redshifts. Although the SFR$^*$ of the counterparts varies between −0.4 and 8 M$_\odot$ yr$^{-1}$, the specific SFR is equal to or higher than the median values estimated for the different catalogues, with the lowest value being $\epsilon \sim 1$. Because of its strong correlation with the specific rate, the SFR$^*/(SFR)$ also has high values, around unity or higher. To outline the consistency of such an ensemble of properties, we compare the counterparts to the overall galaxy population at intermediate redshift and discuss the strong relationships between the specific SFR and quantities known to reflect the star formation history of galaxies, that is, colour and MIL. Indeed, the bluest objects are also faint galaxies with the highest specific rates.

Our identification of simulated galaxies with observed hosts has some limitations, both from observational and numerical points of view. Some of the observed hosts may, in other observational studies, be found to have slightly different SFRs or magnitudes, making their SFR-to-luminosity ratios uncertain. Although the general agreement between the simulation and the observations is fairly good, it should be kept in mind that the moderate resolution and somewhat limited number of physical processes included in the simulation may affect the relative number of galaxies in each subpopulation. For instance, these simulations only account for a limited number of 'extreme'-type galaxies, such as extreme starbursts or massive star-forming galaxies. Furthermore, we do not include the effects of dust and, as in Chr04, we only consider extinct SFR$_{UV}$ in the estimate of the SFR$_{UV}/(L_B/L_B^*)$ ratio. That may not be a serious drawback since our focus is on low-mass galaxies that on average suffer less attenuation than the massive ones. In addition, the amount of dust has been shown to be limited in most host galaxies of GRBs (Le Floc’h et al. 2006). The main limitation of this study is the wide redshift range of the 10 observed host galaxies, with only a few galaxies in each narrow redshift bin. The inferences made theretofrom need to be confirmed once the sample size has grown by a factor of 5–10, with a number of hosts at similar redshifts. We should expect to see still higher specific rates in low-mass objects, as the simulated catalogues tend to show. The evolutionary effects displayed in Fig. 6 support this conclusion.

Comparing an expanded host galaxy sample based on Swift data with the simulated catalogues and other well-known galaxy subpopulations, such as compact blue galaxies may be extremely useful. Hosts galaxies should provide a clearer view into the formation and evolution of galaxies and the role of different subpopulations therein. In particular, they will help in investigating the faint end of the galaxy luminosity function. Our results, obtained using a numerical approach, are consistent with and confirm the picture of GRB host galaxies that has emerged lately. They tend to have low mass, be blue in colour and have relatively high specific SFRs. Host galaxies may then belong to the high specific SFR galaxy population, rather than the high SFR population. High-resolution simulations are required to determine, in a more quantitative way, the contribution of the host galaxies to the overall population, and whether hosts are a part of the average normal star-forming galaxy population or a subpopulation of this one, with blue and very low-luminosity objects.

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