First-principles study of pressure-induced magnetic phase transitions in ternary iron selenide K\textsubscript{0.8}Fe\textsubscript{1.6}Se\textsubscript{2}

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We have studied the pressure effect on electronic structures and magnetic orders of ternary iron selenide K\textsubscript{0.8}Fe\textsubscript{1.6}Se\textsubscript{2} by the first-principles electronic structure calculations. At low pressure, the compound is in the blocked checkerboard antiferromagnetic (AFM) semiconducting phase, as observed by the neutron scattering measurements. Applying pressure induces two phase transitions, first from the blocked checkerboard AFM semiconducting phase to a collinear AFM metallic phase around 12 GPa, and then to a non-magnetic metallic phase around 25 GPa, respectively. Our results help to clarify the recent experimental measurements under pressure.

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The discovery of iron-based superconductors\textsuperscript{1} has stimulated great interest on the investigation of unconventional superconducting mechanism. A system of particular interest is the recently discovered potassium or other mono-valent element intercalated ternary iron-selenide superconductors A\textsubscript{y}Fe\textsubscript{2}Se\textsubscript{2} (A=K, Rb, Cs, and/or Tl)\textsuperscript{2,3}. These materials show rich magnetic phase diagrams and many unusual physical properties that have not been found in other iron-based superconductors. A thorough investigation may deepen our understanding on the interplay between superconducting and antiferromagnetic fluctuations.

AFe\textsubscript{2}Se\textsubscript{2} has the ThCr\textsubscript{2}Si\textsubscript{2} type crystal structure (Fig. 1a), isotropical to the 122-type iron pnictides\textsuperscript{4}. However, from both experimental and theoretical studies\textsuperscript{6–8}, it was found that the chemically stable phase of A\textsubscript{y}Fe\textsubscript{2}Se\textsubscript{2} is mainly contributed by A\textsubscript{0.8}Fe\textsubscript{1.6}Se\textsubscript{2} with a fivefold expansion of the parent ThCr\textsubscript{2}Si\textsubscript{2} unit cell in the $ab$ plane and a $\sqrt{5} \times \sqrt{5}$ Fe vacancy order (Fig. 1b and 1c). Unlike the collinear\textsuperscript{9,11} or bi-collinear\textsuperscript{12,14} antiferromagnetic (AFM) order found in the parent compounds of other iron-based superconductors, the ground state of A\textsubscript{0.8}Fe\textsubscript{1.6}Se\textsubscript{2} was found to have a novel blocked checkerboard AFM order with a band gap of 400-600 meV\textsuperscript{8,12} and a giant magnetic moment of 3.31 $\mu_B$/Fe formed below a Neel temperature of 559 K.\textsuperscript{8,16} In the blocked checkerboard AFM state, as shown in Fig. 2(a), all four Fe moments within a tetramer are ordered in parallel, while the Fe moments between two neighboring tetramers are ordered in anti-parallel.

The Fe vacancy order and the related distortion in A\textsubscript{y}Fe\textsubscript{2}Se\textsubscript{2} can be altered by chemical doping or by applying pressure. This would in turn affect the stability of different AFM orders in these materials. Unlike chemical doping, an advantage of applying pressure is that it can tune or modify electronic structures and interactions of materials without changing the chemical structures. This provides a unique opportunity to clearly probe the microscopic origin of antiferromagnetic and superconducting pairing interactions, as demonstrated in the study of other iron-based superconductors\textsuperscript{17}. On the other hand, it is very difficult to experimentally characterize the electronic structures and magnetic properties in high pressures by using spectrum probing. This makes theoretical calculations substantially important to study high pressure effect. The recent transport measurements already showed that increasing pressure can suppress the superconducting transition temperature and lead to a semiconducting-to-metallic phase transition at about 9 GPa for A\textsubscript{y}Fe\textsubscript{2}Se\textsubscript{2}\textsuperscript{18}. But no characterization information on the electronic structure and magnetic order is available meanwhile.

To investigate the pressure effect, we have performed first-principles electronic structure calculations on K\textsubscript{0.8}Fe\textsubscript{1.6}Se\textsubscript{2} from 0 to 30 GPa. We find that K\textsubscript{0.8}Fe\textsubscript{1.6}Se\textsubscript{2} undergoes two phase transitions at about 12...
and 25 GPa, respectively. The first transition is from the blocked checkerboard AFM semiconducting state into the collinear AFM metallic state, and the second is from the collinear AFM metallic state into a nonmagnetic metallic state. To our knowledge, such a pressure-induced phase transition between two different magnetic phases has not been found in other Fe-based superconductors.

In our calculations the plane wave basis method was used. We adopted the generalized gradient approximation (GGA) with Perdew-Burke-Ernzerhof (PBE) formula [19] for the exchange-correlation potentials. The ultrasoft pseudopotentials [20] were used to model the electron-ion interactions. The kinetic energy cut-off and the charge density cut-off of the plane wave basis were chosen to be 800 eV and 6400 eV, respectively. A mesh of $18 \times 18 \times 8$ k-points was sampled for the Brillouin-zone integration while the Gaussian broadening technique was used in the cases of metallic states. The lattice parameters and the internal coordinates of all ions were fully optimized by minimizing the enthalpy at a given pressure.

In the calculations, we adopted a $\sqrt{5} \times \sqrt{5} \times 1$ tetragonal supercell, which contains two FeSe layers with total 16 Fe atoms and 4 Fe-vacancies, 20 Se atoms, and 8 K atoms and 2 K-vacancies, to represent $K_{0.8}Fe_{1.6}Se_2$. K atoms can have two inequivalent positions in each supercell. However, from both theoretical calculations [8] and experimental measurements [6], we know that the electronic and magnetic structures of these materials are hardly affected by the different configurations of K atoms.

From the previous calculations [8], we find that the tetramer lattice distortion, of which the four Fe atoms within a tetramer shrink to form a compact square driven by the chemical-bonding between Fe and Se, plays an essential role in stabilizing the blocked checkerboard AFM state. Without such tetramer distortion, the energy of the collinear AFM state (Fig. 2(b)) is in fact about 43 meV/Fe lower than that of the blocked checkerboard AFM state. This collinear AFM state has also a semiconducting gap. But its gap is only of dozens of meV, much smaller than in the blocked checkerboard AFM state. In the collinear AFM state, each pair of next nearest Fe moments are AFM ordered. It suggests that the Se-bridged superexchange AFM interaction dominates over other exchange interactions, similar as in iron-pnictides [10].

To clarify the phase diagram, we have calculated the enthalpy $H$ under pressure. It should be emphasized that it is the minimum of the enthalpy, rather than the minimum of the total energy, that determines the stability of a phase under a pressure at zero temperature. The enthalpy $H$ is defined by $H = E + pV$, where $E$, $p$, and $V$ stand for the total energy (internal energy), pressure, and volume, respectively. In the equilibrium, the pressure is thus equal to the minus derivative of the internal energy with respect to the volume, $p = -dE/dV$. At the transition point between two phases, the derivative of the total energy $E$ with respect to the volume $V$ should be equal for these two phases. Thus the transition pressure can be also determined from the slope of the common tangent lines on the $E$ versus $V$ curves of the two phases.

As there are Fe vacancies in $A_{0.8}Fe_{1.6}Se_2$, K atoms may enter these vacancy positions under high pressures. We have carried out extensive calculations to examine this possibility. However, we find that the enthalpy of the system with Fe vacancies being partially or fully occupied by K atoms is always much higher than that of the system without K occupation on Fe vacancies. Thus we need only to consider the system with the $\sqrt{5} \times \sqrt{5}$-ordered Fe vacancy superstructure.

Figure 3 shows the pressure dependence of the enthalpy in the blocked checkerboard AFM, collinear AFM, and non-magnetic states, respectively. Two phase transitions are observed. In the low pressure regime, the system is in the semiconducting blocked checkerboard AFM phase. At about 12 GPa, a transition from the blocked checker-
In high pressures, the blocked checkerboard AFM state remains in the non-magnetic states, respectively. From the slopes of the two common tangent lines, we find that the critical pressures are about 12 GPa and 25 GPa, respectively. They agree with the values of 12 GPa, 24 GPa, and 27 GPa, respectively. The corresponding separation in the blocked checkerboard AFM phase is about 2.40 Å, 2.30 Å, 2.23 Å, and 2.18 Å at 0 GPa, 12 GPa, 24 GPa, and 27 GPa, respectively. The corresponding separation in the blocked checkerboard AFM phase is 2.44 Å, 2.36 Å, and 2.30 Å at 0 GPa, 12 GPa, and 24 GPa, respectively. Thus the contraction along the c-axis with the pressure is more pronounced in the collinear AFM phase than in the blocked checkerboard AFM phase. It is known that the magnetic moment of Fe is sensitive to the distance between Fe and As or Se[21], thus the magnetic moment should become smaller with increasing pressure. This is consistent with the result shown in Fig. 3. At zero pressure, both the collinear AFM and blocked checkerboard AFM states are semi-conducting, the charge fluctuation is small and each Fe acquires a giant magnetic moment. In high pressures, the collinear AFM state becomes metallic and the charge fluctuation between the conduction and valence bands reduces significantly the effective moment.

In the collinear AFM state at 12 GPa, one can flip some of the Fe spins \( S \) to form different magnetic states. From the energy differences among these states, we have estimated the effective spin exchange interactions and found the nearest neighbor spin exchange constant \( J_1 = -9 \text{ meV}/S^2 \) and the next-nearest neighbor exchange constant \( J_2 = 22 \text{ meV}/S^2 \), similar as in iron-pnictides[10].

Figure 6 shows the electronic band structure of \( K_{0.8}Fe_{1.6}Se_2 \) in the collinear AFM phase at 12 GPa. At this pressure, \( K_{0.8}Fe_{1.6}Se_2 \) is semi-metallic. It contains both electron-type and hole-type charge carriers. From our previous study, we know that at the ambient pressure the collinear AFM state is a meta-stable semiconductor.

![Figure 4](image1.png)

**FIG. 4**: (Color online) The total energy \( E \) versus the volume \( V \) for the blocked checkerboard AFM, the collinear AFM, and the non-magnetic states, respectively. From the slopes of the two common tangent lines, we find that the critical pressures are about 12 GPa and 25 GPa, respectively. They are consistent with the transition pressures determined from the enthalpy, \( P_{B-C} \) and \( P_{C-NM} \), as shown in Fig. 3.

![Figure 5](image2.png)

**FIG. 5**: (Color online) Pressure dependence of the volume (left) and the total energy (right) for the blocked checkerboard AFM, the collinear AFM, and the non-magnetic states, respectively.
with a band gap of 73 meV. High pressure turns it into a metal. In contrast, K$_{0.8}$Fe$_{1.6}$Se$_2$ in the blocked checkerboard AFM phase is always semiconducting with a band gap varying from 600 meV to 300 meV with the increase of pressure up to 24 GPa.

The semiconductor-to-metal transition we find at about 12 GPa between the blocked checkerboard AFM phase and the collinear AFM phases agree qualitatively with the experimental observation\cite{18}. But the transition pressure we obtained is slightly higher than the experimental value (about 9 GPa) for K$_4$Fe$_2$Se$_2$. The difference may result from two reasons. First, the samples used in experimental measurements are not in the perfect K$_{0.8}$Fe$_{1.6}$Se$_2$ composition. They always contain extra Fe and K ions. These extra ions will introduce itinerant charge carriers to the system and reduce the value of the transition pressure. Second, as in all density functional calculations based on the PBE approximation for iron-pnictides and iron-chalcogenides, the magnetic moment of Fe is over-estimated in the collinear AFM metallic states\cite{10}. This means that the charge fluctuation in the collinear AFM state is underestimated, which in turn may result an overestimation for the critical pressure.

In conclusion, we have studied the pressure effect on K$_{0.8}$Fe$_{1.6}$Se$_2$ by performing the first principles electronic structure calculations. Without external pressure, the ground state is in the blocked checkerboard AFM semiconducting phase. By applying a pressure, it undergoes two successive phase transitions, first to the collinear AFM metallic phase at about 12 GPa, and then to the non-magnetic metallic phase at about 25 GPa. Our result agrees qualitatively with the experimental measurement. It suggests that the semiconductor-to-metal phase transition observed by experiments is a transition from the blocked checkerboard AFM phase to the collinear AFM metallic phase. The metallic collinear AFM phase in high pressures shows both electron- and hole-type Fermi surfaces, similar as in iron-pnictides or in FeSe. In analogy to BaFe$_2$As$_2$ or other iron-based superconductors, we believe that the collinear AFM metallic phase of K$_{0.8}$Fe$_{1.6}$Se$_2$ may become superconducting upon pressure and/or electron or hole doping.

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Note added. While in the preparation of this manuscript, we learnt of a paper by C. Cao, M. Fang, and J. Dai on pressure effect on K$_4$Fe$_2$Se$_2$\cite{22}. Unlike what we have done here, they used the total energy rather than the enthalpy to judge the stability of a phase under pressure. Based on such a criterion, they claimed that a so-called Neel-FM state is the most stable in the regime corresponding to the collinear AFM phase in Fig. 3. We have subsequently calculated the enthalpy for this Neel-FM state. But we find that its enthalpy is substantially higher than that of the collinear AFM state up to 25 GPa.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig6}
\caption{(Color online) (a) Electronic band structure of K$_{0.8}$Fe$_{1.6}$Se$_2$ in the collinear antiferromagnetic order (Fig. 2(b)) at a pressure of 12 GPa; (b) Brillouin zone. Here the Fermi energy is set to zero.}
\end{figure}

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