Laser Nanopatterning of Colored Ink Thin Films for Photonic Devices

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Supporting Information

ABSTRACT: Nanofabrication through conventional methods such as electron beam writing and photolithography is time-consuming, high cost, complex, and limited in terms of the materials which can be processed. Here, we present the development of a nanosecond Nd:YAG laser (532 nm, 220 mJ) in holographic Denisyuk reflection mode method for creating ablative nanopatterns from thin films of four ink colors (black, red, blue, and brown). We establish the use of ink as a recording medium in different colors and absorption ranges to rapidly produce optical nanostructures in 1D geometries. The gratings produced with four different types of ink had the same periodicity (840 nm); however, they produce distant wavelength dependent diffraction responses to monochromatic and broadband light. The nanostructures of gratings consisting of blue and red inks displayed high diffraction efficiency of certain wavelengths while the black and brown ink based gratings diffracted broadband light. These gratings have high potential to be used as low-cost photonic structures in wavelength-dependent optical filters. We anticipate that the rapid production of gratings based on different ink formulations can enable optics applications such as holographic displays in data storage, light trapping, security systems, and sensors.

KEYWORDS: Holography, laser ablation, diffraction gratings, printing, photonic devices

INTRODUCTION

Nanofabrication techniques such as electron beam lithography (EBL) or Focused Ion Beam (FIB) milling can produce meticulous nanostructures with 2−5 nm resolution. However, they require high-power energy supplies, have long producing times, and involve complex setups and equipment. In addition, they are not amenable for a variety of materials which can be directly processed. Coloration of different nanomaterials as metasurfaces is highly desirable to produce multifunctional and miniaturized optoelectronic devices. These devices may comprise metallic nanostructures with high polarization-independent reflection, strong contrast, fast response time, and long-term stability. In addition they may have controllable optical absorption of a nanostructured polymer film to diffract light. However, these devices require layers with specific arrangement as short-range ordered nanoholes in a gold film, which affect the total cost and time, and these devices can be only used in reflection mode. Nanoparticle (NP) assemblies can also be used to create functional optical/electrical devices for sensing, electronics, displays, and catalysis. Sophisticated design patterns, high intensity and wide angle-independent structural colors are the key features of the NP-based optical devices. Ejecting ink from the nozzle, wetting, sputtering, spreading, and retracing processes can affect the precisions of the final structure of the printed nanostructures. The localized surface plasmon resonance of silver nanoplate (SNP) substrates can be tuned from 500 to 800 nm in the visible spectrum. These devices have selective optical absorption and scattering behavior based of specific nanoparticle sizes. However, they required complex chemical syntheses processes. Moreover, the colors of silver films lead to strong electromagnetic scattering. Cubic liquid-crystal structures have been developed for electronic and photonic
Figure 1. Fabrication of 1D patterns through nanosecond DLIP in holographic Denisyuk reflection mode. (a) Nd:YAG laser beam (532 nm, 3.5 ns) was directed to a dielectric mirror and passed through a dye-based ink medium and reflected back from a plane mirror to ablate a localized region of the recording medium. Four dye-based ink mediums are (b) black, (c) red, (d) blue, and (e) brown. The light transmission measurement for each medium added on each color. Scale bar = 200 μm.

Many advanced reflective photonic applications could be achieved based on the patterned crystallographic orientation of the cubic soft lattice of a blue phase liquid crystal (BPLC). The BPLC could be produced with UV irradiation and photomask which are complex and high cost. In addition, photolithography has been widely used to make various nanostructures for optical devices operating in the visible region. However, using pulsed laser ablation requires low energy and rapid production. Recently, direct laser interference patterning (DLIP) has been used to produce nanostructures in thin materials. Such nanostructures can be patterned into 1/2/3D geometries and complex patterns such as Fresnel lenses and filters. The expansion of this platform to a wide range of low-cost materials is highly desirable for large-scale production.

Here, we show a holographic ablation based on direct laser interference patterning method to rapidly create low-cost optical nanostructures. A Nd:YAG laser (532 nm) was used in holographic Denisyuk reflection mode to create ablative interference fringes. We utilized different synthetic dye-based inks, which have different optical properties, to produce 1D photonic nanostructures. Tested ink media consisted of four ink colors (black, red, blue, and brown). Holographic DLIP allowed forming constructive antinode fringes of electromagnetic field from the standing wave to create gratings in dye-based inks. Using thick film of material (ink) causes multiple laser wave interference fringes to form the gratings. A thick amplitude grating invariably describes an absorption grating. Usually a thick holographic grating can be expressed as a sinusoidal absorption grating and it has different characteristics of diffraction compared to conventional gratings with sharp edges. This is because the shape and the thickness of the recording medium influences the transmission profile. Such dye-based ink gratings can be used in a myriad of devices to produce light deflection, guidance, or coupling. In the present work, the nanostructures based on the four dye-based ink gratings have been spectrally analyzed and angle-resolved measurements were performed to characterize their optical properties. This is the first demonstration of laser based nanopatterning of multiple ink formulations and their usage for wavelength dependent optical devices. The work demonstrates the possibility of nanopatterning organic and fluorescent materials which cannot be processed through methods such as photolithography and electron beam lithography.

**MATERIALS AND METHODS**

**Preparation of the Ink Recording Media.** Black, red, blue and brown ink colors (Staedtler Lumocolor) have refractive indexes of 1.6, 1.65, 1.59, and 1.62 respectively. Diluted ink solutions (1:8, v/v in ethanol) were spin coated on a 1 mm thick glass slides at 200 rpm for 35 s. The inks used were permanent and had a long-term durability.

**Fabrication of the Diffraction Gratings in ink.** Holographic direct laser interference patterning was used in Denisyuk reflection mode. Laser beams (λ = 532 nm) initially directed by a mirror traveled to an ink-based recording medium and reflected from a plane mirror to ablate the localized regions of the medium. The exposure angle of all ink films was set to 18° from the surface plane of the plane mirror (object).

**Spectroscopic Measurements of the Ink Gratings.** The diffraction of light from 1D gratings of the four inks (black, red, blue and brown) were analyzed by normally illuminating the periodic samples with violet (λ = 405 nm), green (λ = 532 nm), and red (λ = 635 nm) laser beams and observing the transmitted light perpendicularly on a flat screen, placed 17 cm away.

**Angle-Resolved Measurements of the Gratings.** halogen light source (HL-2000, Ocean Optics) and a goniometer setup were used to carry out angle-resolved measurements of the diffraction efficiency of the ink gratings. Diffraction spots from the ink nanostructures were analyzed in transmission mode. Each sample was placed 17 cm away from the optical probe to analyze the diffraction wavelengths. A motorized rotating stage was used for broadband spectroscopic analysis of the rainbow diffraction through the nanostructure gratings. The rotation stage had 0.5° steps from ranging from −90° to +90°.
**RESULTS AND DISCUSSION**

**Holographic Fabrication of 1D Nanostructures.** Figure 1a shows the diagram of the hologram recording setup in Denisyuk ablation mode. The laser beams initially directed by a mirror traveled to an ink-based recording medium and reflected from a plane mirror to ablate the localized regions of the medium. To form the gratings, the four dye media were used: black ink (a combination of blue, red, and yellow dyes) (Figure 1b), red ink (Figure 1c), blue ink (Figure 1d), and brown ink (a combination of green, yellow, and red dyes) (Figure 1e).

A halogen light source was used to analyze the transmission of each ink-based recording medium (insets in Figure 1). The transmitted halogen light generated the visible range wavelengths from 400 to 850 nm. For thick materials, the recording media could be described in terms of light absorption percentage (Absorption % = 1 - Transmission %). The black ink had the most absorption of light in the visible range, absorbing more than 75% of all wavelengths (Figure 1b). The red ink had low absorption (20–45%) of light in the visible range and it allowed 80% light transmission over 620 nm wavelengths (Figure 1c). On the other hand, the blue ink has shown high light transmission below 500 nm and above 700 nm (Figure 1d). Brown ink consisted of different dye compositions, showing high light transmission at all wavelengths. As a result, red and blue inks had sharp absorption dips in the visible spectrum; however, the black and brown inks were highly absorbent in the visible spectrum since they were composed of many colors.

Holographic DLIP was performed to produce a well-ordered grating in each ink medium, where the size of the grating pattern ranged from 0.2–1.0 cm in diameter (roughly the size of laser beam). The four ink media received the same laser beam energy (210 mJ) and they produced the same 1D nanostructures. The red ink had low peak absorption at 532 nm so it produced the same 1D nanostructures fabricated by holographic DLIP. Gratings having periodicities of 840 nm in (a) black, (b) red, (c) blue, and (d) brown inks. SEM grating image of (e) black, (f) blue gratings. The light transmission graphs of each ink were integrated for normalization. Scale bar = 10 μm. SCALE bar scale bar = 1 μm.

**Optical Characterization of the Gratings.** The created nanostructures were amplitude gratings. However, different absorption regions of the ink produced different diffraction responses. Although the standing wave field had the same source wavelength, different dye inks formed different diffraction patterns. The black grating had the same spacing as the other inks but it has different diffraction responses when illuminated with different laser beams (Figure 3). The black ink based grating and the analytical solution was 2% (eq 5). The period of grating spacing can be controlled by the exposure angle (θ) between the laser beam and the tilt angle from the surface plane of the mirror (eq 5).20

The formation of gratings on the four colored inks has increased the broadband light transmission. The average transmission ranges between 3 and 20% (Figure 2a–d). The highest percentage of transmission change was in the red ink while the lowest one was in the brown ink, whereas the transmission increased by 8% and 10% for blue and black inks, respectively (Figure 2). In general, transmission of light changed in all the ink media operating between 400 and 650 nm except for red ink which remained in the entire visible spectrum. The highest absorption zone of the red ink was at 559 nm, close to the laser beam wavelength of 532 nm. SEM images show magnified images for the nanostructures of black and blue gratings (Figure 2e,f).

![Holographic Fabrication of 1D Nanostructures](image)
has generated additional diffraction spots.\textsuperscript{27} The violet laser beam illumination (405 nm) of the grating resulted in diffraction of the first order at 27° and the second order at 73°, which agreed with the theoretical diffraction spots (eq 6). In addition, the secondary wave diffracted two more spots (Figure 3a). The laser beam (532 nm) produced diffraction of the first order at 39°, which was similar to the theoretical diffraction angle, whereas the secondary wave created two additional spots at 18° and 63° (Figure 3b). Additionally, the red laser beam (635 nm) resulted in the diffraction of light at 47° with 2° difference as compared to the theoretical diffraction value and the secondary wave diffraction was at 24° (Figure 3c). The additional diffraction spots resulted from the high absorption of black ink and subsequent secondary standing wave. The black dye-based ink received one of the standing beam stronger (532 nm) than the other (1064 nm). The two wavelength could electromagnetically induce diffraction intensity based on the thickness and the medium of the grating.\textsuperscript{27,28} Although the black ink generated additional diffraction spots from the secondary standing wave, another experiment has been conducted on black ink with Nd:YAG laser beam 1064 nm and there was no sign of secondary grating diffraction (ESI Material, Supporting Information (SI) Figure S1).

The red and brown inks showed resemblance in the diffraction of the first order (Figure 3e,f, k,l). However, there was a slight change in the (405 nm) laser diffraction of the second order from the two ink gratings (Figure 3d−j). The red ink has generated diffraction at 68° and the brown ink diffraction was at 71° due to

Figure 3. Diffraction from nanostructures upon illumination from three monochromatic light sources (405 nm, 532 and 635 nm) on patterned ink gratings (Λ = 0.84 nm) (a−c) Black, (d−f) red, (g−i) blue, and (j−l) brown inks. Scale bar = 5 cm.
The intensity of the intensity of the diffraction order (m) can be theoretically estimated:

\[ \Lambda = \frac{\lambda m}{\sin(\theta)} \]  

where \( \Lambda \) is the wavelength of the incident light, \( m \) is the diffraction order, and \( \theta \) is the angle of diffraction. The variation in monochromatic light wavelengths to illuminate ink gratings changed diffraction efficiency. The diffraction efficiency (\( I_{\text{diff}} \)) of each ink grating was considered from the relation of the intensity of first order \( I_1 \) and the zero-order intensity \( I_0 \) (\( I_{\text{diff}} = I_1/I_0 \)). The black ink had three equal monochromatic diffraction spots of the first order because of its absorption behavior of the broad wavelengths. However, the diffraction efficiencies of the three laser beams were not the same because some of the ink-based gratings had different light transmissions at zero-order (Figure 4a). The light diffraction efficiency of the red ink at 635 nm was the lowest because most light transmitted in the zero-order as the same wave color (Figure 4b). On the other hand, this was not the case for the blue ink. The light at 405 nm had high diffraction efficiency due to the two waves (primary and secondary) creating a higher sinusoidal absorption grating with small waves to produce a phase grating diffraction in the same position of the first order (eq 6). The brown ink light diffraction efficiency was the lowest because it had low light absorption (Figure 4d). The ink thickness had an important role on light diffraction based on absorption parameter (\( Q' \)) and refractive index effect can be calculated as

\[ Q' = 2\pi n \Lambda \cos \theta \]
\[ Q' = \frac{m}{2 \sin \theta} \]

where \( Q' \) is the thickness parameter, \( h \) is the grating thickness, and \( n_o \) is the refractive index of the grating vector. \(^{24,29}\) Black ink was selected to test the effect of the thickness because it had equal transmission for three monochromatic laser lights. The laser light (635 nm) was used to test the transmission profile of different thicknesses.

The black ink was spin-coated on 1 mm thick glasses at a speed of (200—1200 rpm). The transmission decreased with lower spin-coating speed and higher thickness (Figure 4e). Addition-

**Figure 5.** Angle-resolved measurements of the diffraction gratings fabricated via holographic DLIP. (a) The spectroscopy system contained the diffraction of a broadband light beam that passed through 1D ink sample on a motorized stage to measure the rainbow pattern. The rainbow grating diffraction pattern of (b) black, (c) red, (d) blue, and (e) brown inks. Rainbow pattern length from the grating diffraction of (f) black, (g) red, (h) blue, and (i) brown light diffraction. Spectroscopy measurements of (j) black, (k) red, (l) blue, and (m) brown dye-based inks. Scale bare = 5 cm.
ally, the diffraction intensity of first order increased with increasing thickness of the ink layer (Figure 4f). However, the secondary grating diffractions did not follow the first order trend and showed different responses in diffraction intensity. The first order diffraction is commonly used in optical applications because it has the highest efficiency, and in the present analysis, it can be the primary evaluation parameter. The thickness of the ink medium was being controlled by the spin-coating speed (Figure 4g). In addition, the ink layer thickness had a significant effect in light absorption (Figure 4h). As a result, increasing the ink thickness reduced the transmission, which enhanced the diffraction efficiency. The refractive index and absorption parameters at different thicknesses were calculated by (eq 7 and 8); and therefore, 915 nm thickness was chosen as the best medium thickness for the subsequent experiments. Using laser interference in Denisyuk reflection mode, the material thickness must be reasonable to allow the laser waves to pass through any substrate to produce the ablative reflection waves. If the material does not transmit the laser waves, the medium would burn it or not respond. In addition, if the absorption reaches zero or 100% transmission, the target material would not interact with laser wave.\textsuperscript{17,20} For these reasons, the ink thickness was sufficient to have reasonable absorption, in particular the black and blue inks.

A goniometer controlled spectroscopy setup was used for angular measurements and the distribution of the rainbow diffraction pattern from each ink grating was recorded (Figure 5a). The angle-resolved diffraction measurements of the four ink gratings were measured at a maximum broadband light intensity to quantify the highest value of diffracted wavelength distribution. The maximization enabled to have the same bandwidth of grating diffraction within the range of 400–850 nm. The rainbow diffraction of each ink grating had different arcs and number of orders. The length measurements were based on placing a screen at 30 cm away from diffraction samples. The black ink grating had the widest dispersion pattern as compared to the other inks, and it produced two diffraction orders with a total angular diffraction of 43° from one side of the rotation stage (0° to +90°). The total length of the two orders was 22.83 cm (Figure 5b–f). The red and brown ink gratings had the same total angular diffraction having a width of 19° to (10 cm long) (Figure 5c–g and 5e–i). However, the blue ink formed a different shape of the rainbow to create a thinner width at the green region with a total diffraction of 23° and 12.7 cm long (Figure 5d–h). The black ink generated two rainbow patterns: the first order was 17°–22° and the second order was at 21°–60° from the two laser waves (Figure 5f). The black ink had the highest diffraction intensity of all light waves due to high light absorption (Figure 5i), but 11% of light waves was diffracted at the first order (ESI Material (SI) Figure S2). However, the red ink diffracted less light from the rainbow pattern because it had low light absorption (Figure 5g) and diffraction concentrated at the peaks at 490 to 625 nm based on its absorption zone (Figure 5k). The blue ink grating had the highest diffraction intensity of 73% because of the light absorption between the two peaks (Figure SI). Nevertheless, the lowest intensity of wavelength distribution was with the brown ink, reaching a maximum of 28% diffraction (Figure S1). This is because brown medium lost most of light to transmission at the zero-order that led to a low percentage of overall light diffraction (Figure 5m) (ESI Material, SI Figure S3). Consequently, the four ink gratings showed a different response on the rainbow diffraction pattern. The blue and red grating inks indicated that both of them were able to create single wavelength low-cost photonic structures with wavelength dependence.

However, the black and brown inks were not able to generate specific wavelength filtering because both inks diffracted light in all wavelengths.

**Applications of the Ink-Based Gratings.** The dye-based inks on glass substrates could be used as low-cost wavelength filters. Their thickness of the ink layer could be controlled to adjust the percentage of light transmission and to create different photonic effects (Figure 6a1–a4). The numbers of laser pulses were varied on the dye-based inks to filter transmission but this process ablated most of the ink medium to create ~90%. The laser energy and the thickness of the recording medium should be controlled to finely tune the optical properties of the wavelength filter transmission. In addition, the hydrophobicity measurements were carried out on the ink gratings with deionized water (Figure 6b). The nanopatterned gratings were created on the four ink types (Figure 6c) to show the visible effect of nanostructures and to create 1D structures (800 nm periodicity) for the hydrophobicity measurements. The hydrophobicity has increased after the nanostructure formation on the

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**Figure 6.** Hydrophobic properties and applications of dye-based ink gratings. (a1) black, (a2) red, (a3) blue, and (a4) brown ink wavelength filters. (b) Hydrophobicity measurements on the dye-based inks. (c) The nanopatterned gratings in array form. (d,e) hydrophobicity contact angle change. (f1,f2) Blue ink based 1D grating personal security signature. (g1,g2) Black ink based surface grating University of Birmingham logo. Scale bar = 5 mm.
dye-based inks, but possibility of less than 10% of difference from dye ink gratings color and instrument accuracy precision. We also demonstrate this capability by creating 1D nanostructures in blue ink (Figure 6d,e). In addition, there are many other optical applications that can be achieved with dye-based ink gratings. Multiple laser exposures were conducted to ablate the ink substrate in a x−y linear movement stage at 15° to produce a 1D diffraction grating in the form of a signature. A 1D grating based signature with blue ink can be used to create a high security feature (Figure 6f1,f2). According the manufacturer, the inks have long-term durability. In these experiments, there was no change in sample quality after a year. The sample shown in Figure 6f1 is one year older than the sample in Figure 6f2, and they both have comparable optical performances. Moreover, a 1D diffraction grating based logo of "University of Birmingham" was created by ablating black ink as examples of sophisticated design of trademark and brands for diverse commercial applications (Figure 6g1,g2). Their applications in optical devices include holographic displays, data storage, filters, light trapping, security systems, and sensors.1,13,31

■ CONCLUSIONS

We report the production of optical nanostructures based on economical dye-based inks. The diffraction from these gratings depended on the ink’s refractive index and incident wavelength. The black ink based nanostructures displayed additional diffraction spots from its secondary grating, whereas the phase grating in the blue nanostructure enhanced light diffraction of the same wavelength. Moreover, with increasing ink thickness, the light diffraction is enhanced and the effective transmission is decreased. In addition, the ink based gratings can be used as a wavelength-dependent filter and their thickness can be controlled to adjust the percentage of transmission. In particular, the blue and red ink nanostructures have the potential to be used as low cost wavelength-dependent photonic structures, which have application in displays, fiber optics, and biosensors. Furthermore, hydrophobicity measurements were performed on the four ink gratings to show the increase in the contact angle due to the topology of the nanostructures. To demonstrate the utility, the blue ink based grating was demonstrated as an example of an advanced personal security signature, and a black ink grating was patterned to display "University of Birmingham" as a distinctive logo. The DLIP patterning method described herein has wide potential applications in commercial diffraction optics.

■ ASSOCIATED CONTENT

Supporting Information

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Additional information as noted in the text (PDF)

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Notes
The authors declare no competing financial interest.

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