Solar energetic particle drifts in the Parker spiral

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[1] Drifts in the Parker spiral interplanetary magnetic field are known to be an important component in the propagation of galactic cosmic rays, while they are thought to be negligible for solar energetic particles (SEPs). As a result, they have so far been ignored in SEP propagation modeling and data analysis. We examine drift velocities in the Parker spiral within single particle first-order adiabatic theory, in a local coordinate system with an axis parallel to the magnetic field. We show that, in the presence of scattering in interplanetary space, protons at the high end of the SEP energy range experience significant gradient and curvature drift. In the scatter-free case, drift due to magnetic field curvature is present. The magnitude of drift velocity increases by more than an order of magnitude at high heliographic latitudes compared to near the ecliptic; it has a strong dependence on radial distance \( r \) from the Sun, reaching a maximum at \( r \sim 1 \) AU at low heliolatitudes and \( r \sim 10 \) AU at high heliolatitudes. Due to the mass over charge dependence of drift velocities, the effect of drift for partially ionized SEP heavy ions is stronger than for protons. Drift is therefore likely to be a considerable source of cross-field transport for high-energy SEPs.

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1. Introduction

[2] The large-scale structure of the interplanetary magnetic field (IMF) can be approximated as a Parker spiral [Parker, 1958]. Although it is known that this basic structure is altered by turbulence and by a variety of other effects, including the tilt of the magnetic axis with respect to the rotation axis, differential rotation, and transients, a variety of spacecraft measurements have confirmed that the large-scale spatial variation of the IMF broadly follows Parker’s model [e.g., Forsyth et al., 1996].

[3] Energetic charged particles are guided by the IMF in their propagation and scattered by its turbulence. They experience guiding center drifts due to the presence of magnetic field inhomogeneity, curvature, and the solar wind electric field. Drift effects can be treated either by means of single particle first-order guiding center theory [Northrop, 1963; Rossi and Olbert, 1970] or within kinetic theory (for a discussion of these approaches and their connections, see Burger et al. [1985]).

[4] The importance of drifts in the propagation of galactic cosmic rays (GCRs) is well established and is usually modeled by means of the formulation by Jokipii et al. [1977] within the framework of the Parker transport equation. For solar energetic particles (SEPs), characterized by energies lower than GCRs, drift effects are considered to be unimportant. In many instances, SEPs are assumed to be tied to magnetic field lines. This assumption is intrinsic within the majority of SEP propagation models, starting from the formulation of the focussed transport equation [Roelof, 1969] and up to modern efforts based on similar approaches [e.g., Ruffolo, 1995; Lario et al., 1998; Luhmann et al., 2007]. In the latter works, the assumption that particles are tied to magnetic field lines is used to reduce the number of spatial variables required in the modeling to one, the distance traveled along the field line, thus simplifying the problem of solving the corresponding equations.

[5] Single particle first-order guiding center drifts for SEPs in a Parker spiral configuration were considered in two early studies which concluded that they play a negligible role. The first of these studies [Burns and Halpern, 1968] was based on an analytical calculation of drift velocities, while the second used numerical integration [Winge and Coleman, 1968]. Both approaches assumed that particles propagate scatter-free, hence experiencing strong focussing in the IMF, so that in practice a zero particle pitch angle was used in the calculation of drift velocities. In addition, drift velocities were only calculated in the heliographic equatorial plane.

[6] However, spacecraft measurements in interplanetary space clearly show that SEPs can have large pitch angles at locations far away from the Sun. Even during the early phase of SEP events, a fraction of particles have pitch angles close to 90° and this fraction increases greatly during an event, with anisotropies in most cases becoming negligibly small during the peak and decay phases.
[7] In this paper, we investigate single particle first-order drifts in the Parker spiral without assuming a zero pitch angle. On the contrary, we allow for the possibility that particles may be characterized by a broad range of pitch angles while propagating in the interplanetary medium. We analyze the magnitude of drifts as a function of location in the heliosphere. We show that magnitudes of drift velocities are significant for energetic particles at the high-energy end of the SEP range and are a nonnegligible cause of transport across the field.

[8] In section 2, we derive analytical relativistic expressions for single particle first-order drifts in a local reference frame with an axis along the Parker spiral. In section 3, the magnitudes of drift velocities and their spatial variation are analyzed for particles in the SEP energy range. Section 4 presents a discussion of the results and conclusions.

2. Single-Particle Drift Velocities in the Parker Spiral

2.1. Unipolar Parker Field

[9] The Parker spiral interplanetary magnetic field is given by Parker [1958]

\[ B_r = B_0 \frac{r_0^2}{r^2} \] (1)

\[ B_\theta = 0 \] (2)

\[ B_\phi = -B_0 \frac{r_0^2 \Omega \sin \theta}{v_{sw}} \] (3)

where \((r, \theta, \phi)\) are heliocentric spherical coordinates with \(r\) the radial distance, \(\theta\) the colatitude, and \(\phi\) the longitude. Here \(B_0\) is the magnitude of the magnetic field at a reference distance \(r_0\), \(\Omega\) the solar rotation rate (taken as constant) and \(v_{sw}\) the solar wind speed. A solar wind flow that is radial, uniform, and time independent is assumed.

[10] Equations (1)–(3) describe a unipolar field pointing away from the Sun. In reality, the IMF is characterized by at least two domains of opposite polarity, separated by a current sheet. In this section, we analyze drift velocities in the simplified unipolar field given by equations (1)–(3), while the effect of the presence of two polarities will be described in section 2.2.

[11] Due to the motion of the solar wind in the inertial (nonrotating) reference frame, an electric field \(E = -v_{sw}/c \times B\) is present, which, using equations (1)–(3), takes the form

\[ E_r = 0 \] (4)

\[ E_\theta = \frac{\Omega B_0 r_0^2}{c} \frac{\sin \theta}{r} \] (5)

\[ E_\phi = 0 \] (6)

where \(c\) is the speed of light.

[12] Burns and Halpern [1968] (from hereon indicated as BH1968) calculated particle drift velocities in the magnetic and electric fields of equations (1)–(6) analytically in spherical coordinates, for a single particle of nonrelativistic speed and within the assumptions of standard first-order adiabatic theory. The drift velocities consist of an electric field drift \(v_E\), a grad-\(B\) drift \(v_{E_B}\), a curvature drift \(v_c\), and a so-called polarization drift \(v_p\) (given by equations (10), (12), (14), and (15) of BH1968, respectively).

[13] We introduce a local coordinate system \((e_r, e_\phi', e_\phi')\) with an axis parallel to the Parker spiral [Kelly et al., 2012] and calculate the components of the drift velocities in this system. Compared with spherical coordinates, this choice of coordinate system has the advantage that the analytical expressions take a simpler form, as they have at most two nonzero components, both perpendicular to the field. The local coordinate system has an axis \(e_r\) along the direction of the Parker spiral and pointing outward, another axis in the direction of \(e_\phi' = -e_\theta\) with \(e_\theta\) the standard spherical coordinate system unit vector and an axis \(e_\phi'\) completing the right-handed orthogonal system.

[14] In the local Parker system, the electric field drift velocity is given by

\[ v_E = 0 \] (7)

\[ v_{E_\phi'} = \frac{mc}{qB} \frac{v_\perp^2}{(r^2 + a^2)^{3/2}} \frac{r \cot \theta}{(r^2 + 2a^2)^{1/2}} \] (8)

\[ v_{E_\theta} = 0 \] (9)

where \(a\) is a function of colatitude \(\theta\) and is defined as

\[ a = \frac{v_{sw}}{\Omega \sin \theta} \] (10)

The electric field drift is always in the \(e_\phi'\) direction and is independent of particle properties such as speed, charge, and mass. This drift describes the corotation of a particle with the IMF magnetic field lines as the Sun rotates, i.e., it is a corotation drift. Near the Sun, it moves particles in the direction of solar rotation by 14.3° per day.

[15] The grad-\(B\) drift velocity has the expression

\[ v_{B_r} = 0 \] (11)

\[ v_{B_\theta} = \frac{\mu c}{q} \frac{1}{\sqrt{r^2 + a^2}} \frac{r \cot \theta}{(r^2 + a^2)^2} \] (12)

\[ v_{B_\phi'} = -\frac{\mu c}{q} \frac{1}{\sqrt{r^2 + a^2}} \frac{r \cot \theta}{(r^2 + 2a^2)^{3/2}} \] (13)

where \(\mu\) is the particle’s magnetic moment and \(q\) its charge. The grad-\(B\) drift depends on the particle species and on velocity. The direction of the grad-\(B\) drift is opposite for electrons and ions. In the nonrelativistic approximation, the magnetic moment is given by

\[ \mu = \frac{mv_\perp^2}{2B} \] (14)

where \(v_\perp\) is the component of a particle’s velocity in a plane perpendicular to the magnetic field and \(B = |\mathbf{B}|\). Its direct proportionality to \(\mu\), \(v_{B_r}\) is largest for particles with pitch angle \(\alpha = 90°\) and equal to zero for field-aligned (strongly focussed) particles.

[16] The curvature drift has the expression

\[ v_c = 0 \] (15)

\[ v_{c_\phi'} = \frac{mc}{qB} \frac{v_\perp^2}{(r^2 + a^2)^{3/2}} \frac{r \cot \theta}{(r^2 + 2a^2)^{1/2}} \] (16)

\[ v_{c_\theta} = -\frac{mc}{qB} \frac{v_\perp^2}{(r^2 + a^2)^2} \frac{1}{(r^2 + 2a^2)^{3/2}} \] (17)

where \(v_\perp\) is the component of the particle’s velocity parallel to the magnetic field. The curvature drift has a very similar expression to the grad-\(B\) drift, but because of its dependence on \(v_\perp\), it is largest in magnitude for particles with \(\alpha = 0°\)
A generalization of equations (11)–(20) to the case of relativistic particles can be obtained by letting the particle mass $m$ take its relativistic form $m = m_0 \gamma$, where $m_0$ is the particle’s rest mass and $\gamma$ is the relativistic Lorentz factor (see Rossi and Olbert, [1970, equation (5.64)]). We will be adopting relativistic expressions in the following.

[20] Using equation (14) and the expression for the magnitude of $B$ in the Parker spiral

$$B = \frac{B_0 r^2}{r^2 + a^2}^{1/2}$$  \hspace{1cm} (21)

equations (11)–(13) become, in relativistic form

$$v_{\perp B} = 0$$  \hspace{1cm} (22)

$$v_{r B} = \frac{1}{2} m_0 q c \frac{2}{q} v_{\perp f} (r, \theta)$$  \hspace{1cm} (23)

$$v_{\theta B} = \frac{1}{2} m_0 q c \frac{2}{q} v_{\perp f} (r, \theta)$$  \hspace{1cm} (24)

where

$$g(r, \theta) = \frac{a}{B_0 r^2} \frac{x^3 \cot \theta}{(x^2 + 1)^{3/2}}$$  \hspace{1cm} (25)

$$f(r, \theta) = \frac{a}{B_0 r^2} \frac{x^2(x^2 + 2)}{(x^2 + 1)^2}$$  \hspace{1cm} (26)

and $x = x(r, \theta) = r/a(\theta)$. Here $g(r, \theta)$ describes the spatial variation of the $\phi'$ components of the grad-$B$ drift, and $f(r, \theta)$ that of the $\theta'$ components.

[21] Similarly, we can express the curvature drift as

$$v_{\perp} = 0$$  \hspace{1cm} (27)

$$v_{r \phi} = -\frac{m_0 q c v_{\perp}}{q} g(r, \theta)$$  \hspace{1cm} (28)

$$v_{r \theta} = \frac{m_0 q c v_{\perp}}{q} f(r, \theta)$$  \hspace{1cm} (29)

and the polarization drift as

$$v_{\perp} = 0$$  \hspace{1cm} (30)

$$v_{r \phi} = \frac{m_0 q c v_{\perp}}{q} \frac{v_{\perp} v_{\parallel}}{qB} \frac{a r \cot \theta}{(r^2 + a^2)^2}$$  \hspace{1cm} (31)

$$v_{r \theta} = \frac{m_0 q c v_{\perp}}{qB} \frac{v_{\perp} v_{\parallel}}{qB} \frac{a^3}{(r^2 + a^2)^2}$$  \hspace{1cm} (32)

[22] Equations (7)–(9) and (22)–(32) constitute the full set of first-order drift velocities for a relativistic particle of arbitrary pitch angle in the unipolar Parker spiral, expressed in the local Parker coordinate system. This set of equations is equally applicable to SEPs and GCRs.

[23] Due to the dependence on $cot \theta$, the function $g$ and consequently the $\phi'$ components of the grad-$B$ and curvature drift velocities are zero at the heliographic equator (where $\theta = 90^\circ$). Also, $g > 0$ when $\theta \in [0^\circ, 90^\circ]$ and $g < 0$ when $\theta \in [90^\circ, 180^\circ]$, while $f$ is always positive. Figure 1 shows the variation of $f$ and $|g|$ with $\theta$ at four values of $r$. The function $f$, influencing the $\theta'$ components of drift velocities, has a fairly slow variation with $\theta$, so that the magnitude of drift in $\theta'$ does not depend strongly on colatitude. On the other hand, $g$ has a strong $\theta$-dependence, so that the drift in $\phi'$ is zero near the heliographic equator but increases greatly at high heliographic latitudes.

[24] For a unipolar Parker field pointing outward (as in equations (1)–(3)), the directions of the grad-$B$ and curvature drifts for a positively charged ion are as follows. $v_{\perp B}$ is always negative, therefore, in regions not far from the heliographic equatorial plane (where the $e_{\phi'}$ direction points approximately upward), the grad-$B$ drift tends to push particle downward (both above and below the plane). Similarly, the curvature component $v_{r \theta'}$ is always negative, hence...
Figure 2. Absolute values of drift velocity components in the local Parker coordinate system for a 100 MeV proton at latitude \( \delta = 10^\circ \), as a function of \( r \). (left column to right column) gradient, curvature, and polarization drift components. The solid line gives the \( \theta' \) component and the dash dotted line the \( \phi' \) one. In all panels, the dotted line is the corotation speed \( v_{E0} \). Pitch angle \( \alpha = 85^\circ \) (top row); \( \alpha = 5^\circ \) (bottom row).

in the same direction as \( v_{\nabla B \theta'} \). For \( \theta \in [0^\circ, 90^\circ] \) (i.e., \( g > 0 \)), \( v_{\nabla B \theta'} \) is positive (i.e., roughly in the direction of corotation near the equatorial plane), while \( v_{e0'} \) is negative (i.e., roughly opposite corotation near the equatorial plane). The signs of the \( \phi' \) components of the drifts reverse for \( \theta \in [90^\circ, 180^\circ] \).

[25] The directions of gradient-\( B \) and curvature drifts reverse for an electron due to the dependence on \( q \).

2.2. Dipolar Parker Field

[26] Unlike in the unipolar magnetic field of equations (1)–(3), in the solar magnetic field and, consequently, the IMF, two polarities are present. At solar minimum, the IMF’s structure can be broadly described as two hemispheres of opposite polarities, separated by a current sheet, called the Heliospheric Current Sheet (HCS). At solar maximum, a more complex structure consisting of dipolar plus quadrupolar contributions exists. Since the tilt of the magnetic dipole increases as the cycle progresses from minimum to maximum, the tilt angle of the HCS also increases.

[27] In this section, we extend the discussion of energetic particle drifts of section 2.1 to a simplified dipolar IMF, where the HCS coincides with the heliographic equatorial plane, and the magnetic field points outward everywhere in the northern hemisphere and inward everywhere in the southern hemisphere. This configuration is usually described as \( A^+ \) in studies of GCRs, and the one with opposite polarities as \( A^- \).

[28] In an \( A^+ \) configuration, drifts for particles in the northern hemisphere are the same as described in section 2.1. To derive drift directions in the southern hemisphere, we consider how these change when \( -B \) is substituted in place of \( B \) in the expressions for drift velocities. As expected, the electric field drift (corotation drift) remains in the same direction because the electric field direction also reverses. The gradient-\( B \) drift velocity takes opposite signs to those in equations (22)–(24) and so does the curvature drift velocity with respect to equations (27)–(29). Hence, for a positively charged particle in the southern hemisphere (\( \theta \in [90^\circ, 180^\circ] \)), the gradient-\( B \) and curvature drifts will be positive along the \( e_{\phi'} \) direction, thus pushing particles upward at colatitudes not far from the heliographic equator. In the \( e_{\phi'} \) direction, drifts will be opposite compared to those discussed in section 2.1. Therefore, as expected, the directions of drifts from single-particle first-order guiding center theory for an \( A^- \) configuration give rise to the well-known GCR pattern, where positively charged particles drift toward the HCS [Jokipii et al., 1977]. It should be noted that the standard GCR drift expressions are derived for an isotropic particle distribution and do not contain a dependence on pitch angle.

[29] In an \( A^- \) configuration, the gradient-\( B \) and curvature drift patterns are reversed, with positively charged particles drifting from low to high heliolatitudes, i.e., away from the HCS.
If we define a drift velocity \( v_d \) as the sum of the grad-\( B \) and curvature drifts

\[
v_d = v_{\nabla B} + v_c
\]  

Using equations (22)–(24), (27)–(29) and keeping into account the drift directions in the \( \mathcal{A}^+ \) and \( \mathcal{A}^- \) configurations, we can write the following summary expression for \( v_d \), valid in a simple dipolar field with current sheet coinciding with the heliographic equatorial plane

\[
v_d \bigg/ v_{E0} = \text{sgn} \left( \frac{\Delta \phi}{\Delta \phi_c} \right) - \frac{m_0 v_c}{q} \left( \frac{1}{2} \right) \left( 1 + \sin^2 \theta \right) \frac{r}{R_s} \]  

where \( \text{sgn} \) is the sign function, and the colatitude \( \theta \) is expressed in radians.

When particles get within two gyroradii of the heliospheric current sheet, their trajectories are no longer described by adiabatic theory and a separate analysis is required. It can be shown that the effect of a neutral sheet on charged particle motion is to give rise to a drift along the sheet itself and perpendicular to the direction of the magnetic field [Burger et al., 1985]. Current sheet drift is important in the propagation of GCRs, and a number of different approaches for describing it have been proposed (see e.g., Burger and Potgieter [1989] and references therein). Its importance for SEP propagation will need to be established in future work.

**3. Drift Velocities for SEPs**

**3.1. Protons**

As far as we are aware, at present, drifts are not taken into account in most models of SEP propagation and are thought to be unimportant in the SEP energy range.

Figure 2 shows the absolute value of drift velocity components for a 100 MeV proton at heliographic latitude \( \delta=10^\circ \) (i.e., colatitude \( \theta=80^\circ \)). In each row, the panels give, from left to right, \( v_{\nabla B}, v_c, \) and \( v_p \); and the dotted line in all panels represents the corotation velocity \( v_{E0} \). The top row is for a particle of pitch angle \( \alpha=85^\circ \), and the bottom row for one with \( \alpha=5^\circ \). The relativistic factor for a 100 MeV proton is \( \gamma=1.1 \). We use \( v_{sw}=500 \text{ km s}^{-1}, \Omega=2.86 \times 10^{-6} \text{ rad s}^{-1}, \) \( B_0=1.78 \text{ gauss}, \) and \( r_0=1 \text{ r}_s \) with \( r_s \) the solar radius \((r_s=6.96 \times 10^8 \text{ m}); \) this choice of \( B_0 \) and \( r_0 \) ensures that the magnetic field magnitude at 1 AU is 5 nT.

By comparing the top and bottom rows in Figure 2, it is apparent that for a particle with \( \alpha \sim 90^\circ \), the grad-\( B \) drift is dominant, while for \( \alpha \sim 0^\circ \), it is the curvature drift that dominates. The polarization drift is much smaller than the sum of grad-\( B \) and curvature drifts for the case of Figure 2 and all other cases we considered, and will not be further discussed. The magnitudes of the grad-\( B \) and curvature drifts can reach values close to that of the corotation drift. Figure 2 also shows that at \( \delta=10^\circ \), the \( \theta' \) component is dominant, and the largest contribution is from the curvature drift.

Particles that are propagating scatter-free (i.e., for which \( \alpha \) quickly reaches values near zero) will be subject mainly to curvature drift. In the unipolar Parker field of equations (1)–(3), or in the northern hemisphere of a bipolar
3.2. Heavy Ions

[40] The expressions for drift velocities derived in section 2.1 depend on the mass over charge ratio. It is well known from measurements that SEP heavy ions are typically only partially ionized [Klecker et al., 2006], making the value of $m_0/q_i$ large. It is therefore expected that for SEP heavy ions of energies of 100 MeV/nucleon, drift velocities will be larger than those of 100 MeV protons (shown in Figures 2 and 3) by a factor $A/Q$, where $A$ is the ionic mass number and $Q$ the charge number.

3.3. Evolution of SEP Pitch Angle

[41] It is well known that in the absence of scattering, particles injected at the Sun are rapidly focussed by the Parker spiral magnetic field, so that their pitch angle quickly becomes close to zero. If a particle finds itself with pitch angle close to $\alpha=90^\circ$ (e.g., as a result of scattering) at a radial location $r_1$ in interplanetary space (e.g., at 1 AU) and continues to propagate away from the Sun, it will experience focussing; however, this will not be as effective as for a particle injected at the Sun. We study this effect by defining a characteristic focussing radial distance $L_f(r_1)$ as the distance it takes for a particle to focus from $\alpha=90^\circ$ at $r_1$ to $\alpha=5^\circ$. Figure 4 shows the dependence of $L_f$ on the “injection” location $r_1$. The plot shows that a particle starting with pitch angle $\alpha=90^\circ$ near the Sun will be focussed very quickly. However, $L_f$ increases rapidly with radial distance of particle injection, and a particle having $\alpha=90^\circ$ at 1 AU (for example due to scattering) will be focussed to a pitch angle of 5° only by the time it has reached a radial distance of $\sim$80 AU. Consequently, if scattering is present in the interplanetary medium, a significant fraction of particles will be characterized by large and intermediate pitch angles, making the grad-B drift nonnegligible. Due to slow focussing away from the Sun, even a low level of scattering is sufficient to generate a pitch angle distribution with significant population at pitch angles near 90°.

4. Discussion and Conclusions

[42] We analyzed drifts in the Parker spiral IMF using single particle first-order guiding center theory. The drift velocities first derived by BH1968 were calculated in a reference frame with an axis parallel to magnetic field and generalized to the case when scattering is present and to particles of relativistic energies. The resulting equations, equations (7)–(9) and (34)–(36), which include dependence on the particle’s pitch angle, are applicable to SEPs and GCRs.

[43] We have shown that, contrary to current thinking, drift velocities are significant for protons at the upper end of the SEP energy range, and especially for heavy ions.

[44] Particles propagating scatter-free are subject to curvature drift, which near the heliographic equator is essentially a drift in latitude, and at high heliolatitudes includes both a $\phi'$ and a $\theta'$ component. If scattering takes place in the IMF, particles can have a range of pitch angles at large distances from the Sun, and both curvature and grad-B drift can become significant.

[45] Drift velocities vary greatly with location in interplanetary space. Not far above the heliographic equatorial plane, e.g., at latitude $\delta=10^\circ$, the magnitudes of grad-B and...
curvature drifts for 100 MeV protons can be as large as the corotation drift, reaching their maximum value at a distance of about 1 AU from the Sun. At high heliolatitudes, e.g., δ=80°, magnitudes of grad-B and curvature drifts greatly exceed the corotation drift at distances >2 AU and continue to grow with radial distance until ~10 AU.

[46] The large increase in drift velocities at high heliolatitudes is consistent with Ulysses observations of SEPs over the poles of the Sun, which showed that the heliolatitude of the solar event associated with the SEPs is not an important parameter in determining the characteristics of the event [Dalla et al., 2003].

[47] For partially ionized heavy ion SEPs, drift velocities can become much larger than for protons of the same speed, due to the dependence on A/Q.

[48] The overall amount of drift experienced by a particle is determined by how its position and pitch angle vary over time as a result of propagation parallel and perpendicular to the field, focussing and scattering-induced pitch angle changes. Additional transport across the field will be caused by perpendicular propagation associated with turbulence in the IMF, which includes a contribution from field line random walk (see e.g., Laitinen et al. [2013] and references therein). Assessing the relative importance of drift-associated and turbulence-induced perpendicular transport for different particle species and energies will be an important objective of future research.

[49] Results of full orbit test particle simulations of SEP propagation in the Parker spiral are presented in a related paper [Marsh et al., 2013]. The simulations show significant particle drift in agreement with the analytical results obtained in this paper and allow the transport across the field to be quantified.

[50] Drifts should therefore be taken into account in SEP models as a source of cross-field transport and the assumption that particles remain tied to field lines, in-built within many modeling and data analysis approaches, be revised.

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