Role of Chemistry and Crystal Structure on the Electronic Defect States in Cs-Based Halide Perovskites

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Abstract: The electronic structure of a series perovskites ABX$_3$ (A = Cs; B = Ca, Sr, and Ba; X = F, Cl, Br, and I) in the presence and absence of antisite defect X$_B$ were systematically investigated based on density-functional-theory calculations. Both cubic and orthorhombic perovskites were considered. It was observed that for certain perovskite compositions and crystal structure, presence of antisite point defect leads to the formation of electronic defect state(s) within the band gap. We showed that both the type of electronic defect states and their individual energy level location within the bandgap can be predicted based on easily available intrinsic properties of the constituent elements, such as the bond-dissociation energy of the B–X and X–X bond, the X–X covalent bond length, and the atomic size of halide (X) as well as structural characteristic such as B–X–B bond angle. Overall, this work provides a science-based generic principle to design the electronic states within the band structure in Cs-based perovskites in presence of point defects such as antisite defect.

Keywords: perovskite; electronic structure; defect properties

1. Introduction

ABX$_3$ (A = monovalent organic or inorganic cation, B = bivalent metal, and X = halide) type perovskites have received much attention as candidate materials for various electronic and opto-electronic applications ranging from solar cells to light-emitting diodes [1–3]. The chemistry and crystal structure of these perovskites determine the band structure needed for the application. For example, the chemical bonding between the metal (B) and the halogen (X) atoms are linked to the valance band maxima (VBM) and conduction band minima (CBM) with anti-bonding X p and non-bonding B p states having major contributions at VBM and CBM, respectively [4]. The extent and nature of such orbital overlap is linked to intrinsic properties of the B and X atoms, such as the atomic radius [5] and the electronegativity (EN) differences between B and X [5,6]. The higher EN difference between B and X reportedly causes the widening of bandgap [7,8]. In an ionic bond, where the electronegativity difference between metal and halogen is high, the electronic charge cloud is less dispersed along the bond and localized near the nuclei, limiting the overlap between atomic orbitals and resulting in a large bandgap in ionic perovskite. Further, the size of the atom significantly influences the atomic orbital overlap in a bond. For example, in a covalent bond involving smaller sized atoms, the nucleus strongly pulls the electron cloud making it unable to form a covalent bond, and instead, forms an ionic bond with the other atoms. Further, atomic size approximates the energy of the orbitals that are participating in the bonding that leads to the band structure. Hence, the VBM and CBM positions vary systematically based on the atomic size. The effect of atomic size and electronegativity on the electronic structure of halide perovskites can be well understood from the bandgaps of MAPbX$_3$ (X = I, Br, and Cl), a widely studied perovskite system used mainly for photovoltaic applications. The experimental bandgap of MAPbX$_3$ (X = I, Br, and Cl) changes systematically from 1.55 eV [9], 2.00 eV [10], and 2.88 eV [11] with decreasing atomic size and increasing electronegativity from I, Br to Cl, respectively.
In addition to the atomic size and electronegativity, arrangement of atoms within a lattice can also significantly alter the positions of the VBM and CBM, and the band structure in general. In a typical halide perovskite structure, B metal is bonded with the neighboring six halides forming a [BX₆]⁴⁻ octahedral, and the relatively larger A cation occupies the volume between two corner-sharing octahedra [12]. Based on the atomic arrangement, halide perovskites are mainly found in three temperature-dependent crystal structures: cubic, tetragonal, and orthorhombic. For instance, all MAPbI₃ show a high-temperature cubic phase (α) followed by a tetragonal phase (β) at intermediate temperatures, and an orthorhombic phase (γ) at low temperatures [13]. These crystal structures in ABX₃ perovskites differ in terms of their symmetry, or more precisely, on the lattice parameter and B–X–B bond angle in the [BX₆] octahedra [12]. In the cubic structure, the [BX₆] octahedra is oriented in such a way that all the B–X–B bond angles are 180°, whereas, in the tetragonal and orthorhombic phases, the octahedra is tilted with B–X–B bond angles less than 180°. A vast number of studies have claimed that a distortion of the [BX₆] octahedra or B–X–B bond angles below 180° can change the bandgap in perovskites [14,15]. The deviation of the B–X–B bond angles from 180° in the ideal cubic structure reduces the antibonding interaction between the B and the X atoms, which lowers the energy of the VBM and increases the bandgap [15]. Xiao and co-workers reported that for CsPbI₃, as the Pb–I–Pb bond angle (180°) in the cubic structure is reduced to 136.4° in the distorted structure, the bandgap increases to 1.66 eV from 1.48 eV [15].

Point defects, such as cation or halide vacancy, the interstitial and antisite defects produced during the synthesis of perovskite compounds, also affect the band structure. Frequently, these point defects introduce additional electronic states within the band structure which can affect the transfer of charge carriers across the bands. For example, cation and halide vacancy can form a state near the VBM and CBM (shallow state), whereas the antisite defect, which is formed usually at high halide concentrations, produces mid-gap localized states (trap state) [16,17]. In particular, both experimental and computational reports have linked the formation of localized electronic states to antisite point defect in lead halide perovskites [18–20].

In this paper, we performed density functional theory (DFT) calculations to systematically investigate the electronic structure of a series of theoretically and experimentally observed perovskites ABX₃ (A = Cs; B = Ca, Sr, and Ba; X = F, Cl, Br, and I) in the presence and absence of antisite defect X₈ (where one B atom is replaced by one X atom). It is notable that previous electronic structure calculations [21,22] on the Cs-based halide perovskites were mostly focused either on the defect formation energy or elemental contribution on the band structure. In this manuscript, we aim to establish a fundamental link between features of the perovskite electronic structure, such as band gap and the position of the localized electronic states w.r.t band edges, with the intrinsic atomic properties and crystal structure. An understanding of these relationships will help predict electronic band structure features for an arbitrary B and X combination based on easily available intrinsic features, such as EN, bond dissociation energy (BDE), and covalent radius of the B and X atoms. We restrict our study to the s-block perovskites (B = Ca, Sr, and Ba) as an alternative to Pb-based perovskites, which exhibit negative environmental impacts [23]. It is notable that both Pb-based and s-block perovskites exhibit similar elemental contribution toward band structure i.e., the valence and conduction band edges are formed by X and the B atoms, respectively [24,25].

2. Computation Details

Electronic structure calculations of ABX₃ (A = Cs; B = Ca, Sr, and Ba; X = F, Cl, Br, and I) with and without point defect were performed using the Vienna ab-initio Simulation Package (VASP) [26]. It is notable that among the 12 possible chemical combinations of B and X, CsCaBr₃ [27], CsCaF₃ [28], and CsSrF₃ [29] were experimentally observed in the cubic phase. Initial structures for other compositions are obtained from previous computational studies [30,31] and the materials project database [32]. The DFT calculations
were based on the Perdew, Burke, and Ernzerhof (PBE) [33] generalized gradient approximation (GGA). Our calculations did not include the effect of spin-orbit coupling due to the absence of the spin-orbit effect for the $s$-block metals. The cutoff energy for the plane wave basis was set to 400 eV. We allowed the system to relax ionic positions, cell volume, and cell shape during structure relaxation until the maximum force on each atom was less than 0.01 eV/Å. Cubic and orthorhombic crystal structures were investigated for all the perovskite compositions. We used $3 \times 3 \times 3$ supercells with 135 atoms in the cubic systems and $2 \times 2 \times 1$ supercells with 80 atoms in the orthorhombic systems. For structural relaxation, we used a $3 \times 3 \times 3$ k-points in the cubic systems, whereas we used a $2 \times 2 \times 3$ k-points in the orthorhombic structures. An $8 \times 8 \times 8$ and $8 \times 8 \times 12$ r-centered k-point grid was used for the density of states (DOS) calculation for the cubic and orthorhombic structures, respectively. VESTA software was used to visualize the charge densities and crystal structures [34]. LOBSTER [35] software was used to extract the bonding information between the atoms using the concept of the crystal orbital overlap population (COOP). We note that for the bonding interactions, the orbital overlap between the orbitals is considered positive, and for the antibonding interaction, the overlap between orbitals is considered negative. Hence, for the antibonding interaction, value of COOP factor is negative.

3. Results and Discussion

3.1. Atomic Structure and Electronic Properties of Cubic Perovskites

We start with the atomic and band structure calculations with cubic CsCaBr$_3$, an experimentally observed perovskite, which serves as a representative of the $s$-block ABX$_3$ perovskite. It is notable that our calculated lattice parameter and band gap for defect free CsCaBr$_3$ was 5.77 Å (see Table S3 in the Supplemental Information) and 4.40 eV (Figure 1a), respectively, which is in good agreement with the experimentally measured lattice constant and band gap of 5.69 Å and 4.39 eV [27], respectively. The VBM consists of Br $4p$ states while the Ca $3d$ orbitals are the major contributor of the CBM. The Cs atom had no significant contribution at VBM or CBM, which is also commonly observed in both $s$-block and $p$-block halide perovskites [27,36]. In the case of CsCaBr$_3$ with an antisite defect, a localized electronic defect is observed within the bandgap at the position $L = 0.56$ eV, higher than the VBM (see partial DOS plot in Figure 1b and its magnified version in Figure 1c). To investigate the origin of the localized electronic defect in the CsCaBr$_3$ with an antisite defect, we calculated partial electronic charge density at the energy level where the localized electronic defect was formed, as shown by the yellow regions in Figure 1d. The charge density plot shows that that the localized electronic state originated from the columbic interaction between the defect bromine atom at the center and the six surrounding bromine atoms, with the defect bromine atom making the major contribution. Further, the negative value of crystal orbital overlap population (COOP) in our analysis indicates the presence of an antibonding interaction between the $4p-4p$ orbitals of the antisite Br atom and the surrounding Br atoms (see Figure S1 in the Supplementary Information). From the molecular orbital theory, we know the energy of antibonding orbitals is higher than the energy of the individual atomic orbital [37]. For this reason, the defect state forms at a higher energy level compared to the VBM. In addition, we found that the bond-length between the defect Br atom and the surrounding Br atoms was 2.4% higher than the initial Ca–Br bond-length in defect-free case (see Table S1 in the Supplemental Information). The bigger size of the Br atom compared to the Ca atom, as well as the repulsion generated by the negative charges of the Br atoms, caused the bond-length to increase.
We hypothesized that the energy level position of the localized defect state created by the antisite defect strongly depends on the antibonding interactions between the $p$-orbitals of halogen atoms and the size of halogen atom. Hence, the position of the localized defect can be predicted based on the intrinsic properties of elements, such as the atomic size of X [38] and the bond dissociation energy (BDE) of B–X [39]. Halogens atomic size reflects the energy of the outer orbital that are taking part in bonding or antibonding interactions. Similarly, a bond’s BDE value provides information about the bond’s strength or the quantitative measure of the orbital interactions between molecular orbitals participating in the bond. In addition, in a perovskite system with a large BDE of the B–X bond, creating an antisite defect will require a greater amount of energy. Therefore, the energy of the electronic state that arises by breaking the B-X bond will surely be a function of the BDE of the B–X bond.

To test our hypothesis, we calculated the band structure of a series of cubic ABX$_3$ (A = Cs; B = Ca, Sr, or Ba; X = I, Cl, or F) structures with antisite defects. It is important to note that all of the B and X elements we used in our calculations belong to the same group in the periodic table. Therefore, the natures of the VBM and CBM are equivalent to the CsCaBr$_3$ structure, i.e., the VBM consists of X $n^p$ and the CBM is composed of B $nd$ orbitals, where $n$ is the principal quantum number, and the higher the value of $n$, the higher the energy of the orbital. Based on our hypothesis, we expected that for a fixed B metal with decreasing sizes of halogen atoms from I to F, the position of the localized electronic defect will shift gradually towards the VBM as the energy of the outermost orbital decreases from I(5p) > Br(4p) > Cl(3p) > F(2p). For example, the CsCaCl$_3$ structure with a
smaller sized Cl atom (99 pm) [38] and higher BDE of the Ca–Cl bond (398 kJ/mol) [32] will produce a localized defect closer to the VBM when compared to the CsCaI₃ structure with a bigger I atom (133 pm) [38] and lower BDE of the Ca–I bond (285 kJ/mol) [39] in presence of an antisite defect. Figure 2a,b show the calculated relative position of the electronic defect state (L) as a function of the BDE of the B–X bond and the size of X atom, respectively. The individual density of state calculations for all the cubic ABX₃ for both pristine and the structures with X₃ antisite defects are shown in the Supplementary section (see Figures S4–S14 in the Supplemental Information). As theorized earlier, for each B = Ca, Sr, and Ba, the value of L decreased gradually from I to F making the localized defect state nearer to the VBM. For all calculations with fluorine (except B = Ca), the defect state merges with the VBM, and we consider L as zero. Figure 2 clearly shows that the energy gap L is strongly correlated with the BDE of the B–X bond and the size of X. Therefore, it is essential to understand how intrinsic properties are related to the position (L) of the localized electronic state.

![Figure 2](image-url)

**Figure 2.** Dependence of cubic CsBX₃ (B = Ca, Sr and Ba and X = I, Br, Cl and F) defect position with respect to VBM on (a) BDE of B–X bond and (b) atomic size of X. Dotted lines are for eye-guiding the trend.

The higher the BDE of B–X, the stronger the interaction between B and X, as BDE is a measure of the strength of a bond. The formation of the X₃ antisite defect requires breaking a B–X bond and replacing the B atom with a defect X atom. The defect X atom interacts with the surrounding X atoms to produce the localized defect state as mentioned earlier. For a given X atom, a stronger B–X bond reduces the X atom’s interaction with the defect X atom, and the localized defect state forms at a lower energy level with respect to the VBM. For instance, the Cl(3p)–Cl(3p) interaction energy will be much lower than that of I(5p)–I(5p). The BDE and bond-length are directly related to each other. Shorter bonds have a higher BDE and vice versa.

To test our hypothesis, we measured the bond-length between the antisite defect atom and the surrounding halogen atoms and compared them to the Ca–X bond-length for the structure with no defect for the CsCaX₃ systems. We observed the maximum bond-length increase for CsCaI₃ (3.5%) and the minimum for CsCaF₃ (1.3%), which corresponds to the L values for these systems (see Table S1 in the Supplemental Information). Again, the localized electronic defect state originated from the np–np antibonding interaction between the halogen atoms. The energy of the interacting p-orbitals plays an important role in determining the position of the localized electronic defect state. The energy of the outermost p-orbitals followed the order F(2p) < Cl(3p) < Br(4p) < I(5p). Therefore, the localized electronic state originated from the I(5p)–I(5p) antibonding interaction in CsCaI₃ located at the higher L value compared to the position of the electronic defect state due to Cl(3p)–Cl(3p) interaction in CsCaCl₃.

To further establish the relationship between the energy of the halogen orbitals and the position of the localized electronic defect state in CsCaBr₃, we substituted a Cl atom on
the Ca atom site (Cl\(_{\text{Ca}}\)), instead of a Br on a Ca site, as it was done for an antisite defect in CsCaBr\(_3\). We found that the chlorine atom doping creates a localized electronic defect near to the VBM (\(L_{\text{Cl}} = 0.34\) eV) in comparison to the localized electronic defect state that forms due to Br\(_{\text{Ca}}\) (\(L_{\text{Br}} = 0.56\) eV) (see Figure 3b,c). The lower energy of Br\((4p)\)–Cl\((3p)\) antibonding interaction in Cl\(_{\text{Ca}}\) compared to the Br\((4p)\)–Br\((4p)\) interaction in the Br\(_{\text{Ca}}\) antisite defect caused the localized electronic defect to form near to the VBM. Hence, halide perovskites doped with smaller size halogen atoms or a mixed-halide perovskite should show fewer tendencies to form deep trap states.

In summary, for the cubic structures, the position of the localized electronic defect state is a function of the BDE of the B–X bond and the size of the defect X atom. The higher BDE of the B–X bond and the lower size of X create a localized electronic defect closer to VBM. The position of the localized electronic state can be controlled by choosing an appropriated-sized halogen atom.

3.2. Atomic Structure and Electronic Properties of Orthorhombic Perovskites

Depending on the temperature, the perovskites may exhibit structures with less symmetry than the cubic structures. In the case of the highly symmetric cubic structure, the B–X bond distances are isotopic and remain so when an antisite substitution changes the bond distances and results in only one localized electronic state at a singular location within the band structure. However, for a less symmetrical crystal of the same ABX\(_3\) composition, the B–X bond distances can be anisotropic. In those cases, we hypothesized that, unlike the cubic crystal structure, the presence of an antisite defect in a less symmetrical crystal

![Figure 3.](image-url)
structure can create electronic defect states at two or more different positions within the band gap. To test this hypothesis, we introduced an antisite defect within orthorhombic CsSrI$_3$ (a = 4.81 Å, b = 15.78 Å, and 12.37 Å), a frequently studied s-block perovskite structure with a Cmcm space group (space group No. 63) [30,40]. This orthorhombic structure differs from the symmetric cubic structure due to (a) a different arrangement of atoms and (b) the tilted octahedra of [SrI$_6$] compared to the undistorted octahedral network in a cubic structure. The octahedra consist of one central Sr atom with four equatorial iodine atoms in the same plane (equatorial) with the Sr atom and two apical iodine atoms located out of the plane (see Figures S2 and S3 in the Supplemental Information). The measured Sr–I–Sr bond angles in the orthorhombic structure are 94.5° (equatorial) and 141.8° (apical) as compared to the 180° Ca–Br–Ca bond angle in the cubic CsCaBr$_3$. Figure 4a,b represent the electronic DOS of orthorhombic CsSrI$_3$ without and with antisite defect, respectively. Our study revealed that, unlike the cubic structures, the antisite defect within orthorhombic structure creates localized electronic defect states at two different energy level positions within the bandgap, which we named defect-1 and defect-2. Defect-1 and defect-2 lie at the energy level $L_1 = 0.58$ eV and $L_2 = 1.6$ eV above VBM, respectively. To find the origin of both defect-1 and defect-2, we plotted the charge densities at the energy levels where they are formed as shown in Figure 4d,e, respectively. Similar to the cubic case, the yellow regions depict the electronic charge contributions from all the atoms at that energy level. The charge density plot shows two different kinds of iodine associations which account for the formation of the defect states $L_1$ and $L_2$.

Figure 5 shows the two different groups of iodine atoms present in the orthorhombic structure with the defect. I1 is the antisite defect. I4, I5, I6, and I7 are bonded with I1 in the equatorial plane, and the I2, I3, and I1 are bonded along the c-axis (apical). Resembling the cubic structure, the bond-distance between I1 and I4, I5, I6, and I7 (3.81 Å) increased compared to the Sr–I bond-distance (3.33 Å) in the structure with no defect. In contrast, the bond-distance between I1 and I2, I3 (2.94 Å) was lower than the Sr–I bond-distance (3.28 Å) in the defect-free structure. These observations relate to the formation of two different iodine associations and correlate well with the previous discussion of the effect of the I$_{Pb}$ antisite defect on the MAPbI$_3$ (001) surface [41].
Figure 4. The partial DOS of orthorhombic bulk CsSrI$_3$ (a) without defect and (b) with the antisite defect. (c) magnified portion of the plot (b) indicating the $L_1'$ (eV) and $L_2'$ (eV) value and the electron charge density isosurface plot for the energy range (d) −0.9 to 0.1 eV and (e) 1 to 1.2 eV corresponding with (b).

Figure 5. Antisite defect (I1) with all the neighboring atoms at a maximum distance of 4Å. I4, I5, I6, and I7 are in an equatorial plane with the I1. Atoms I2 and I3 located at the apical positions with respect to I1.

The Sr-I bond is ionic in nature due to the large electronegativity differences between Sr (EN~0.95) and I (EN~2.66). In the presence of the antisite defect (ISr), the bond between Sr and I breaks at the defect site and the negative charge cloud shifts towards the I atom. These I atoms with an excess negative charge tends to share the charge with the newly introduced I atom by forming covalent bonds. To verify the presence of covalency between the iodine atoms, we performed the Bader charge analysis and measured the distance between the...
antisite defect and the surrounding I atoms, as shown in Table 1. The Bader charge analysis uses electron density to calculate the electronic charges present on individual atoms [42]. The average charge on the iodine atoms in the structure with no defect was $-0.776e$. In the presence of the antisite defect I$_1$, all of the iodine atoms surrounding the I$_1$ had decreased negative charges, whereas the charge on I$_1$ was $+0.193e$. The positive charge on the I$_1$ and the decrease in charges of the surrounding iodine atoms indicates the sharing of charge and, hence, the presence of covalency between them. The I$_2$ and I$_3$ atoms show the maximum reduction of the negative charge (~48%), and the other four iodine atoms, which are aligned in the equatorial plane with I$_1$, show ~15% reduction. The different measures of charge sharing, or reductions of negative charges are correlated to the two kinds of bond distances between the I$_1$ and the six neighboring iodine atoms. The covalency, or sharing of negative charge, resulted in the shorter bond-length between the I$_1$ and the surrounding six I atoms. The shorter bond-distance of 2.94 Å between I$_1$, I$_2$, and I$_3$ is very close to the bond distances between I atoms in the I$_2$ molecule (2.7 Å).

Table 1. Bader charge and distance analysis of defect Iodine and neighboring I atoms for CsSrI$_3$ bulk with Sr$_I$ defect. I$_1$ is the antisite defect. The average charge on I atoms before introducing defect was $-0.776e$.

| Iodine (I) | Charge (e) in the Defect-Free Structure | Charge (e) in Presence of the Defect | Percent Change in Charge (%) | Distance from I$_1$ (Å) |
|-----------|----------------------------------------|-------------------------------------|----------------------------|------------------------|
| I$_1$     | +0.193                                 | -0.394                              | 48.90                     | 2.94                   |
| I$_2$     | -0.772                                 | -0.394                              | 48.90                     | 2.94                   |
| I$_3$     | -0.772                                 | -0.394                              | 48.90                     | 2.94                   |
| I$_4$     | -0.777                                 | -0.660                              | 15.00                     | 3.81                   |
| I$_5$     | -0.777                                 | -0.660                              | 15.00                     | 3.81                   |
| I$_6$     | -0.680                                 | -0.660                              | 15.38                     | 3.81                   |
| I$_7$     | -0.780                                 | -0.660                              | 15.38                     | 3.81                   |

In addition, the distance between I$_1$ and I$_4$, I$_5$, I$_6$, and I$_7$ (3.81 Å) is comparable to the van der Waals bond-length of I$_2$ (3.96 Å). The shorter bond-length between the first group of atoms (I$_1$, I$_2$, and I$_3$) compared to the second group of atoms (I$_1$, I$_3$, I$_4$, I$_5$, and I$_6$) is due to the higher extent of sharing the negative charge (greater covalency). We named the first group as trimer and the second group as pentamer. The COOP results show that the defect-1 originated because of the antibonding interaction in the iodine pentamer whereas defect-2 forms because of the antibonding interaction in the iodine trimer (see Supplemental Information). Defect-1 forms near the VBM at a lower energy on the bandgap, and the defect-2 forms at the higher energy level on the bandgap. The different positions of defect-1 and defect-2 can be correlated with the antibonding energy. In addition, the antibonding energy is related to bond-distances between the atoms. It has been reported that shorter metal-halide bonds favor stronger antibonding interactions [43]. For instance, the Sn–Cl bond (2.81 Å) in CsSnCl$_3$ has a stronger antibonding interaction energy of 2.469 eV compared to 1.213 eV for the Pb–Cl (2.87 Å) bond in CsPbCl$_3$ [36,43]. Therefore, the shorter bond-length in the iodine trimer caused the defect-2 to form at the higher level on the bandgap when compared to defect-1.

From these findings, it is reasonable to link the covalent bond distances of the halogen molecules to the location of defect states within the bandgap. To test this hypothesis, we consider all of the s-block orthorhombic ABX$_3$ (A = Cs; B = Ca, Sr, and Ba; X = F, Cl, Br, and I) for our band structure and atomic structure calculations (see Figures S15–S25 in the Supplemental Information). As the origin of defect-1 is equivalent to the localized electronic defect in the cubic case, we linked $L_1$ with the BDE of the B–X bond and the atomic size of X (Figure 6a,b). In Figure 6c,d, $L_2$ is plotted as a function of two interlinked intrinsic properties, BDE of the X–X bond and the covalent bond-distance of X$_2$. For defect-1, we observed the similar dependency of $L_1$ on BDE of the B-X bond and atomic size of X.
that we observed in the cubic structure for the parameter $L_1$, i.e., compounds with lower BDE of B–X and larger atomic sizes correspond to larger values of $L_1$. Conversely, defect-2 compounds with higher BDE of X–X or smaller covalent bond-distance of $X_2$ show higher values of $L_2$. For example, CsSrCl$_3$ shows a higher $L_2$ value (2.21 eV) due to a greater BDE of Cl–Cl (436.3 kJ/mol) and a smaller covalent bond-distance of Cl$_2$ (198 pm) when compared to the CsSrI$_3$, where the $L_2$, the BDE of I–I, and the covalent bond-distance of I$_2$ is 1.40 eV, 152.2 kJ/mol, and 266 pm, respectively. We were not able to investigate similarly for cases with fluorine, i.e., CsBF$_3$ (B = Ca, Sr, and Ba) systems, because the defect-1 merges with the VBM and measuring $L_1$ i.e., difference of energy from the VBM was not feasible. Our data as presented above shows that the formation and position of the electronic defect states within the band gap in halide perovskites in the presence of an antisite defect are linked to the intrinsic properties of the constituent atoms as well as the crystal structure. Therefore, the energy level where the electronic defects will form in the presence of any other commonly observed point defects, such as cation or anion vacancies, interstitials etc., can be predicted with the basic understanding of the material chemistry and the crystal symmetry. For example, for a B metal vacancy X–X covalent bond length change or the BDE of X–X can play an important role in determining the position of the electronic defect state on the bandgap. Additionally, lower symmetrical crystal structures (e.g., monoclinic or rhombohedral) with two or more different bond distances between B and X will likely produce localized electronic states at multiple energy levels on the bandgap in presence of an antisite defect.

![Figure 6](image-url)

**Figure 6.** Dependence of orthorhombic CsBX$_3$ (B = Ca, Sr and Ba and X = I, Br, Cl and F) defect-1 position ($L_1$) with respect to VBM on (a) BDE of B–X bond and (b) atomic size of X and defect-2 position ($L_2$) on (c) BDE of X–X bond and (d) covalent bond length of X–X. Dotted lines are for eye-guiding the trend.
4. Conclusions

In summary, we present a DFT-based first-principles study on the electronic structure of ABX$_3$ (A = Cs; B = Ca, Sr, and Ba; X = F, Cl, Br, and I) perovskites with cubic and orthorhombic phases in presence of antisite point defect. We observed that the presence of an antisite defect within the cubic perovskite leads to the formation of a localized electronic defect state within the bandgap. The higher BDE of the B–X bond and the lower size of X atom shifts the electronic defect state closer to VBM as much as it merges with VBM in case of CsBaF$_3$, a composition with high B–X BDE and smaller sized of halide atom. This implies that the position of the localized electronic state can be controlled by choosing an appropriate cubic perovskite chemistry including mixed halides. Unlike the highly symmetry cubic perovskite structure with 180° B–X–B bond angle, presence of two non-180° B–X–B bond angle leads to the formation of two localized electronic defects in orthorhombic perovskites, a lower symmetric structure. Among the two electronic defects in case of orthorhombic perovskites, interestingly the electronic defect closer to the VBM is linked to the BDE of the B–X bond and the atomic size of X as observed in case of cubic perovskite. However, for the second electronic defect, it was observed that higher BDE of the X–X bond and higher covalent bond-length shift the localized electronic defect away from the VBM band edge. Overall, our calculations provide generic principles to design electronic states of Cs-based perovskites in presence of point defects in terms of readily available intrinsic features of the elements, such as bond-dissociation energy, atomic size, and covalent bond-distance as well as structural characteristic such as B–X–B bond angle. The fundamental principles presented in this research can be extended to screen materials with for a desired electronic structure in wide variety of experimentally observed perovskite crystal structures and point defects.

Supplementary Materials: The following are available online at https://www.mdpi.com/1996-1944/14/4/1032/s1, Figure S1: Crystal orbital overlap population (COOP) analysis for (a) Br$_{Cs}$ antisite defect with surrounding Br atoms in cubic CsCaBr$_3$ and (b) I$_{Cs}$ antisite defect with surrounding I atoms in the orthorhombic CsSrI$_3$; Table S1: Change in the bond-length of Ca–X (X = F, Cl, Br, I) before and after introducing the X$_{Ca}$ antisite defect; Figure S2: Representation of (a) Cubic (Pnmm) and (b) Orthorhombic (Pnma) ABX$_3$; Figure S3: (a) Axial and (b) Apical bonds in orthorhombic CsSrI$_3$; Table S2: The optimized lattice parameter (Å) of cubic ABX$_3$ (A = Cs, M = Ca, Sr, Ba and X = F, Cl, Br, I); Table S3: The optimized lattice parameter (Å) of orthorhombic ABX$_3$ (A = Cs, M = Ca, Sr, Ba and X = F, Cl, Br, I); Figure S4: The partial DOS of bulk cubic CsCaI$_3$ (a) without defect and (b) with antisite defect; Figure S5: The partial DOS of bulk cubic CsCaCl$_3$ (a) without defect and (b) with antisite defect; Figure S6: The partial DOS of bulk cubic CsCaF$_3$ (a) without defect and (b) with antisite defect; Figure S7: The partial DOS of bulk cubic CsSrCl$_3$ (a) without defect and (b) with antisite defect; Figure S8: The partial DOS of bulk cubic CsSrBr$_3$ (a) without defect and (b) with antisite defect; Figure S9: The partial DOS of bulk cubic CsSrF$_3$ (a) without defect and (b) with antisite defect; Figure S10: The partial DOS of bulk cubic CsSrCl$_3$ (a) without defect and (b) with antisite defect; Figure S11: The partial DOS of bulk cubic CsBaCl$_3$ (a) without defect and (b) with antisite defect; Figure S12: The partial DOS of bulk cubic CsBaBr$_3$ (a) without defect and (b) with antisite defect; Figure S13: The partial DOS of bulk cubic CsBaF$_3$ (a) without defect and (b) with antisite defect; Figure S14: The partial DOS of bulk orthorhombic CsCaCl$_3$ (a) without defect and (b) with antisite defect; Figure S15: The partial DOS of bulk orthorhombic CsCaBr$_3$ (a) without defect and (b) with antisite defect; Figure S16: The partial DOS of bulk orthorhombic CsCaF$_3$ (a) without defect and (b) with antisite defect; Figure S17: The partial DOS of bulk orthorhombic CsSrCl$_3$ (a) without defect and (b) with antisite defect; Figure S18: The partial DOS of bulk orthorhombic CsSrBr$_3$ (a) without defect and (b) with antisite defect; Figure S19: The partial DOS of bulk orthorhombic CsSrF$_3$ (a) without defect and (b) with antisite defect; Figure S20: The partial DOS of bulk orthorhombic CsSrCl$_3$ (a) without defect and (b) with antisite defect; Figure S21: The partial DOS of bulk orthorhombic CsSrF$_3$ (a) without defect and (b) with antisite defect; Figure S22: The partial DOS of bulk orthorhombic CsBaI$_3$ (a) without defect and (b) with antisite defect; Figure S23: The partial DOS of bulk orthorhombic CsBaBr$_3$ (a) without defect and (b) with antisite defect; Figure S24: The partial DOS of bulk orthorhombic CsBaCl$_3$ (a) without defect and (b) with antisite defect; Figure S25: The partial DOS of bulk orthorhombic CsBaF$_3$ (a) without defect and (b) with antisite defect.
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