The phenomenon of time-reversal violating generation of static magnetic and electric fields is a basis of a new method for measurement of the electron EDM and T-odd P-odd constants of electron interaction with a nucleon beyond Standard Model

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(Dated: March 26, 2022)

It is shown that in the experiments for search of EDM of an electron (atom, molecule) the T-odd magnetic moment induced by an electric field and the T-odd electric dipole moment induced by a magnetic field will be also measured. It is discussed how to distinguish these contributions.

PACS numbers: 32.80.Ys, 11.30.Er, 33.55.Ad

Nowadays there is an appreciable progress in development of methods for measurement of ultra weak magnetic and electric fields. Therefore, new experiments for measurement of an electric dipole moment(EDM) $d$ of electrons are being prepared.

The EDM of a particle exists if parity (P) and time-reversal (T) invariance are violated. Investigation of the EDM existence could provide knowledge about physics beyond the Standard Model [1-4].

F.L. Shapiro’s idea to measure the electron EDM by applying a strong electric field to a substance that has an unpaired electron spin is being used for the EDM search [1, 6].

The interaction $W_E$ of the electron electric dipole moment $\vec{d}$ with an electric field $\vec{E}$ depends on their orientation:

$$W_E = -d\vec{E}, \quad (1)$$

where $d = d_J^L$, $J$ is the atom spin, $d$ is the EDM.
Spins of electrons (atoms) at low temperature appear to be polarized due to similar to the polarization (magnetization) of electrons by a magnetic field in paramagnetic substances due to the interaction $W_B$ of an electron (atom) magnetic moment $\vec{\mu}$ with a magnetic field $\vec{B}$

$$W_B = -\vec{\mu} \cdot \vec{B}. \tag{2}$$

Spins of electrons (atoms) polarized by an electric field induce the magnetic field $\vec{B}_E$ (Fig. 2) and change in the magnetic flux $\Phi$ at the surface of a flat sheet of material [1]:

$$\Delta \Phi = 4\pi \chi A d E^*/\mu_a, \tag{3}$$

$$B_E = \frac{\Delta \Phi}{A} = 4\pi \chi \frac{d}{\mu_a} E^*, \tag{4}$$

where $\chi$ is the magnetic susceptibility, $\chi \approx \frac{\rho \mu_a^2}{3k_B T}$, $\rho$ is the number density of spins of interest, $k_B$ is Boltzmann’s constant and $T$ is the sample temperature. In the cases where simple Langevin paramagnetism is applicable, $E^*$ is the effective electric field at the location of the spins, $\mu_a = g \sqrt{J(J+1)} \mu_B$ where $\mu_B$ is the Bohr magneton, $\mu_a$ is the atomic or ionic magnetic moment, $g$ is the Lande factor and $A$ is the sample area.
If an external magnetic field acts on either a para- or a ferromagnetic material, the spins in the substance become polarized due to substance magnetization. Therefore, the electric dipole moments appears polarized, too. This results in the induction of an electric field $\vec{E}_B$ (Fig. 3) (see ref. D.DeMille in [1]):

$$E_B = 4\pi \rho d P(B),$$

where $P$ represents the degree that the spins are polarized in the sample.

According to the analysis [1], modern methods for measurement of $B_E$ and $E_B$ provide sensitivity for electric dipole moment measurement about $10^{-32} e \, cm$ and in some cases even $10^{-35} e \, cm$.

It is important to pay attention to another mechanism of time-reversal violating generation of magnetic and electric fields, which have been discussed in [1]. According to the idea of [1], an induced magnetic moment $\vec{\mu}(\vec{E})$ (and, as a result, a magnetic field (Fig.4)) of a particle appears due to the action of a field $\vec{E}$ under conditions of violation of P- and T-invariance (and similar, an induced electric dipole moment $\vec{d}_B$ (an electric field Fig.5) of a particle appears due to the action of a field $\vec{B}$). This new effect does not depend on temperature. An effect magnitude is determined by a P-odd T-odd tensor polarizability $\beta_{ik}^T$ of a particle (atom, molecule, nucleus, neutron, electron and so on). For an atom (molecule), $\beta_{ik}^T$ arises due to P- and T-odd interaction of electrons with a nucleus. For the stationary state of an atom (molecule) $|N_0\rangle$ the tensor $\beta_{ik}^T$ is as follows:

$$\beta_{ik}^T = \sum_F \frac{\langle N_0|\vec{d}_i|F\rangle \langle F|\vec{\mu}_k|N_0\rangle + \langle N_0|\vec{\mu}_i|F\rangle \langle F|\vec{d}_k|N_0\rangle}{E_F - E_{N_0}},$$

where $|F\rangle$ is the wave function of a stationary state of the atom, considering T-odd interaction $V_w^T$, $E_F$ and $E_{N_0}$ are the energies of the atom (molecule) stationary states, $\vec{d}$ and $\vec{\mu}$ are
the operators of electric dipole moment and magnetic moment, respectively and \( i, k = 1, 2, 3 \) correspond to the axes \( x, y, z \).

Let us place an atom (molecule) into an electric field \( \vec{E} \). The induced magnetic dipole moment \( \vec{\mu}(\vec{E}) \) appears in this case:

\[
\mu_i(\vec{E}) = \beta_{ik} E_k,
\]

(7)

The tensor \( \beta_{ik} \) (like any tensor of rank two) can be expanded into scalar, symmetric and antisymmetric parts.

The antisymmetric part of the tensor \( \beta_{ik} \) is proportional to \( e_{ikl} J_l \), where \( e_{ikl} \) is the totally antisymmetric tensor of rank three. The symmetric part of the tensor \( \beta_{ik} \) is proportional to the tensor of quadrupolarization \( Q_{ik} = \frac{3}{2J(2J-1)}[J_i J_l + J_k J_l - \frac{2}{3} J(J+1) \delta_{ik}] \). As a result

\[
\beta_{ik} = \beta_s \delta_{ik} + \beta_v e_{ikl} J_l + \beta_t Q_{ik},
\]

(8)

where \( \beta_s, \beta_v, \beta_t \) are the scalar, vector and tensor P-, T-odd polarizabilities of the particle, respectively. For a substance with the nonpolarized spins \( S_p \rho(J) \vec{J} = 0 \) and \( S_p \rho(J) Q_{ik} = 0 \) (here \( \rho(J) \) is the atom (molecule) spin density matrix). As a result for such a substance, \( \beta_{ik}^T \) appears to be a scalar \( \beta_{ik}^T = \delta_{ik} \beta_s^T \).

Placement of a nonpolarized atom (molecule, nucleus) into an electric field induces the magnetic dipole moment \( \vec{\mu}_E \):

\[
\vec{\mu}(\vec{E}) = \beta_s^T \vec{E},
\]

(9)

where \( \beta_s^T = \sum_F \frac{(N_0|\hat{d}_z|F) \langle F|\hat{\mu}_z|N_0 \rangle + (N_0|\hat{d}_z|F) \langle F|\hat{\mu}_z|N_0 \rangle}{E_F - E_{N_0}} \), \( \hat{d}_z \) and \( \hat{\mu}_z \) are the \( z \) components of the operators of the electric dipole moment and magnetic moment, respectively, axis \( z \) is parallel to the electric field \( \vec{E} \). It should be emphasized that for strong fields (when the distance between atom (molecule) levels is comparable with the energy of interaction with an electric \( \vec{E} \) (magnetic \( \vec{B} \)) field) \( \beta_s^T \) depends on \( \vec{E} \) (\( \vec{B} \)).

Weak interaction is much weaker than strong and electromagnetic interactions. Therefore, to find the wave function \( |F\rangle \), the perturbation theory can be applied:

\[
|F\rangle = |f\rangle + \sum_n \frac{\langle n|V_T^w|f\rangle}{E_f - E_n} |n\rangle = |f\rangle + \sum_n \eta_n^T |n\rangle,
\]

(10)

where \( |f\rangle \) is the wave function of an atom in the absence of weak interactions and the mixing ratio is \( \eta_n^T = \frac{\langle n|V_T^w|f\rangle}{E_f - E_n} \). It should be mentioned that for theoretical analysis of \( \beta_s^T \)
in a substance it is necessary to find a wave function of an excited state of an atom in the
substance which is difficult to do.

It follows from (9) that in a substance placed into electric field the magnetic field is
induced [7]:

\[ \vec{B}_{\text{ind}}^E = 4\pi \rho \beta_s^T \vec{E}^*. \]  

(V11)

Vice versa, if an atom (molecule, nucleus) is placed into a magnetic field, the induced electric
dipole moment \( d(B) \) appears [7],

\[ d_i(B) = \chi_{ik}^T B_k, \]

(12)

where the tensor polarizability \( \chi_{ik}^T \) is \( \chi_{ik}^T = \beta_{ki}^T \). The dipole moment \( d(B) \) leads to the
induction of an electric field in the substance: \( E_{i}^{\text{ind}}(B) = 4\pi \rho \beta_{ki}^T \vec{B}_k^* \), where \( \vec{B}_k^* \) is the local
magnetic field, acting on the considered particle in the substance.

If an atom is found in a point with the cubic symmetry (or in a liquid), then \( \langle Q_{ik} \rangle = S_{pp}(J)Q_{ik} = 0 \) and \( \langle \vec{\mathcal{J}} \rangle = S_{pp}(J) \vec{\mathcal{J}} \parallel \vec{B}_k^* \). As a result the terms including \( \beta_v^T \) and \( \beta_t^T \) turn
to zero \( (e_{ikl} \langle J_l \rangle B_k^* = e_{ikl} B_k^* B_k^* = 0) \).

As a consequence, in this case

\[ E_{\text{ind}}(B) = 4\pi \rho \beta_s^T \vec{B}_k^*, \]

(13)
FIG. 5:

Hence, analyzing the results of the experiment proposed in [1], one should consider that the appearance of the induced magnetic and electric fields is caused by:

1. A magnetic field is induced due to interaction of the electric dipole moment of an atom with an external electric field (see (3),(4))

2. A magnetic field is induced due to mechanism (see (11))

3. A magnetic field appears as a result of polarization (magnetization) of atom magnetic moments by the local induced magnetic field $\vec{B}_{loc}$ due to interaction $W$ of the magnetic dipole moment of an atom with this field

$$W = -\vec{\mu}_a \vec{B}_{loc}. \quad (14)$$

The local field $\vec{B}_{loc}$ is the sum of two contributions:

$$\vec{B}_{loc} = \vec{B}_{E loc} + \vec{B}_{ind}^{loc}, \quad (15)$$

where the field $\vec{B}_{E loc}$ is the local magnetic field acting on an atom from the polarized (by mechanism [1,5], see (3),(4)) magnetic moments of the other atoms of the sample. This field depends on temperature and its contribution could be neglected for those temperature values, which provide $\chi \ll 1$. But for temperature $T < 1K$ the susceptibility $\chi \sim \frac{1}{T}$ becomes comparable with 1 and higher, and the energy of interaction of two magnetic dipoles for neighbour atoms occurs of order of $k_B T$ and greater. Thus, in this case, the collective effects, well-known in the theory of phase transition in magnetism, should be taken into account while considering magnetization by an electric field.
The field $\vec{B}_{\text{ind}} = \vec{B}_{\text{ind}}^1 + \vec{B}_{\text{ind}}^2$ does not depend on temperature.

The field $\vec{B}_{\text{ind}}^1 = \chi_{\text{loc}}^T \vec{E}^*$ is the local magnetic field produced in the point of the considered atom location by the magnetic moments of atoms of the substance (except for the considered atom) induced by the aid of mechanism [7] (see (6),(8)); $\chi_{\text{loc}}^T \sim \rho \beta_s^T$ is the local P-,T-odd susceptibility of the substance. In general case $\chi_{\text{loc}}^T$ is a tensor, but if atom surrounding possesses cubic symmetry, then the principal contribution to this tensor is made by its scalar part ($\chi_{\text{loc}}^T$ depends on the substance density and sample shape: for sphere $\chi_{\text{loc}}^T = \frac{8\pi}{3} \rho \beta_s^T$; for cylinder $\chi_{\text{loc}}^T = 4\pi \rho \beta_s^T$).

The field $\vec{B}_{\text{ind}}^2$ is the self-induced magnetic field of the considered atom. The magnetic moment (T-odd current) of the atom induced by an electric field acting on the atom due to mechanism [7,8] causes appearance of the magnetic field inside the atom:

$$\vec{H}_E^T(\vec{r}) = \text{rot} \, \vec{A}_E^T(\vec{r})$$

with the vector potential $\vec{A}_E^T(\vec{r}) = \frac{1}{c} \int \frac{j_T(\vec{r})}{|\vec{r} - \vec{r}'|} d^3r'$. $j_T^T(\vec{r})$ is the T-odd part of the transition current density operator for an atom (molecule) placed in an electric field [7] (it is calculated by the use of wavefunctions (10)). The magnetic interaction Hamiltonian of an atom with the field $\vec{A}_E^T$ can be expressed as [9]:

$$W_{2\text{ loc}} = -\frac{1}{2c} \int (\vec{j}(\vec{r}) \vec{A}^T(\vec{r}) + \vec{A}^T(\vec{r}) \vec{j}(\vec{r})) d^3r,$$

where $\vec{j}(\vec{r})$ is the atom transition current density operator calculated with the atom wavefunction without consideration of P-,T-odd interactions, $\vec{j}(\vec{r}) = c \text{rot} \vec{\mu}(\vec{r})$ and $\vec{\mu}(\vec{r})$ is the operator of the atom magnetic moment density. If the atom is found in a point with the cubic symmetry (or in a liquid) then we may omit contributions from atom multipoles.

In this case the above expression can be written as:

$$W_{2\text{ loc}} = -\vec{\mu}_a \cdot \vec{B}_{\text{ind}} = -\chi_{\text{at}}^T \vec{\mu}_a \cdot \vec{E}_{\text{loc}}^*,$$

where $\vec{\mu}_a = \mu_a \vec{J}$ and $\chi_{\text{at}}^T$ is the T-odd atom susceptibility, which does not depend on the substance density and sample shape, $\chi_{\text{at}}^T \sim \beta_s^T \frac{1}{a^3}$ (here $a$ is the typical radius of distribution density of the magnetic moment induced by an electric field in the atom [7]).

As a result one obtains:

$$\vec{B}_{\text{loc}} = (\chi_{\text{loc}}^T + \chi_{\text{at}}^T) \vec{E}_{\text{loc}}^* = \chi_{\text{loc(subst)}}^T \vec{E}_{\text{loc}}^*,$$

$$\chi_{\text{loc(subst)}}^T = \chi_{\text{loc}}^T + \chi_{\text{at}}^T.$$
The interaction of the magnetic moment of an atom with the induced magnetic field causes the appearance of the magnetic field due to different population of magnetic levels of the atom in the field $\vec{B}_{\text{loc}}$ in thermal equilibrium

$$\vec{B}_{\text{ind}}^{\prime} = 4\pi \chi \vec{B}_{\text{loc}} \approx 4\pi \chi \vec{B}_{\text{loc}}^{\text{ind}} = 4\pi \frac{\mu_a^2}{3k_B T} \chi_{\text{loc(subst)}} \vec{E}^*,$$

the field $\vec{B}_{\text{loc}} = \vec{B}_{E \text{ loc}} + \vec{B}_{\text{ind loc}}$, but $\vec{B}_{E \text{ loc}}$ contribution could be neglected for those temperature values, which provide $\chi \ll 1$, and it is omitted here.

Therefore, the flux $\Delta \Phi$, which is going to be measured in the experiment proposed in [1] should be written as:

$$\Delta \Phi = AB_E = 4\pi A(\chi \frac{d}{\mu_a} + \rho \beta_s^T + \chi T_{\text{loc(subst)}}) \vec{E}^* =$$

$$= 4\pi A[\chi(\frac{d + \mu_a \chi_T}{\mu_a}) + \chi T_{\text{loc}}] \vec{E}^*;$$

$$\vec{B}_E = 4\pi [\chi(\frac{d + \mu_a \chi_T}{\mu_a}) + \chi T_{\text{loc}}] \vec{E}^*;$$

(23)

where $\chi = \frac{\mu_a^2}{3k_B T}$.

FIG. 6: The magnetic field that is observed in an experiment is the sum of magnetic fields produced by the polarized spins of particles and induced by the external electric field ($\sim \beta_T$)

It should be noted that the quantity $d + \mu_a \chi_T$ is the electric dipole moment of an atom available for measurement in conventional EDM experiments studying atom (molecule) spin precession in an external electric field. It is well known that the atom EDM is arisen from several mechanisms: the contribution proportional to $d_e$, the contribution due to T-,P-odd
interaction of atom electrons with nuclear nucleons (dependent and independent on nuclear spin) (d also contains contribution $\sim \beta^T_s \alpha^T$ induced according to [12] by the magnetic field $\sim \mu_a^T$, which is produced inside the paramagnetic atom by its electrons).

According to [18,23] there is one more addition to the EDM $\sim \mu_a \chi a$. Note that the contribution to the atom EDM proportional to the nucleus spin $I$ is equal to zero if the sample temperature is high ($\langle I \rangle = 0$ at high temperatures).

Let us consider now the experiment to detect the electric dipole moment of the electron by means of measurement of the electric field [1] (see (5)). In this case we also should take into consideration the effect [7] of EDM induction by the magnetic field (12).

$$d$$ is the atom EDM containing contribution $\sim \beta^T_s \alpha^T$ induced according to [12] by the magnetic field $\sim \mu_a^T$, which is produced inside the paramagnetic atom by its electrons.

So, measurement of $\Delta \Phi$ and $E_B$ provides knowledge about the atom EDM and $\beta^T_s$. To distinguish these contributions one should consider the fact that $\chi$ and $P(B)$ depend on temperature, while $\beta^T_s$ does not. Therefore, studying $B_E$ and $E_B$ dependence on temperature allows one to evaluate contributions from the EDM and $\beta^T_s$ to the measured effect.

It should be particularly emphasized that $\Delta \Phi$ and $E_B$ differs from zero even when the electron EDM $d_e$ is equal to zero.

It should be also emphasized that the polarizability $\beta^T_s$ differs from zero even for atoms with the zero spin, for which EDM is absent. In this case (as well as for high temperatures

Thus, the electric field measured in the experiment [1] is as follows (see (9),(10), Fig.7):

$$E_B = 4\pi \rho (d_a P(B) + \beta^T_s B^*),$$

(24)

$E_B$ is the atom EDM containing contribution $\sim \beta^T_s \alpha^T$ induced according to [12] by the magnetic field $\sim \mu_a^T$, which is produced inside the paramagnetic atom by its electrons.

So, measurement of $\Delta \Phi$ and $E_B$ provides knowledge about the atom EDM and $\beta^T_s$. To distinguish these contributions one should consider the fact that $\chi$ and $P(B)$ depend on temperature, while $\beta^T_s$ does not. Therefore, studying $B_E$ and $E_B$ dependence on temperature allows one to evaluate contributions from the EDM and $\beta^T_s$ to the measured effect.

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FIG. 7:
when the average atom spin \( \langle \vec{J} \rangle = 0 \) only the effect \( \mathcal{J}_7 \), described by the terms \( \mathcal{J}_7 \) proportional to \( \beta_s^T \), contributes to the induced electric and magnetic fields. If the substance consists of several types of atoms, then their contribution to the induced field is expressed as a sum of contributions from different atoms:

\[
\vec{B}_E = 4\pi \rho \sum_n c_n \beta_{ns}^T \vec{E}_n^*, \quad \vec{E}_B = 4\pi \rho \sum_n c_n \beta_{ns}^T \vec{B}_n^*,
\]

(25)

where \( c_n \) is the concentration of atoms of the type \( n \), \( \vec{E}_n^* \) and \( \vec{B}_n^* \) are the local fields acting on atoms of the type \( n \).

Now let us consider what information about constants of T-,P-odd interaction of an electron with a nucleus can be obtained from studying the effect \( \mathcal{J}_7 \) of time-reversal violating generation of fields \( \vec{E}_B \) and \( \vec{B}_E \) (describing by (25)).

According to [1] we can expect a magnetic induction sensitivity about \( 3 \times 10^{-15} \text{G/} \sqrt{\text{Hz}} \). In ten days of averaging the sensitivity is \( \sim 10^{-18} \text{G} \). This leads to the sensitivity for \( d_e \) measurement of about \( 10^{-32} \text{e cm} \).

Such sensitivity of magnetic induction measurement provides for polarizability \( \beta_s^T \) measurement the sensitivity \( \beta_s^T = \frac{B_E}{4\pi \rho \rho E} \sim 10^{-43} \text{cm}^3 \) (it is supposed that \( \rho \approx 2 \div 3 \cdot 10^{22} \) and \( E^* \sim 10 \text{ kV/cm} \), for example, for liquid and solid Xe \( \rho \approx 2 \cdot 10^{22} \)).

Let us consider now the possibilities given by the experiment studying the electric field, which is induced by a magnetic field \( \mathcal{J}_7 \) for measurement of the polarizability \( \beta_s^T \). Analysis [1] shows that existing methods of the electric field measurement allow to measure electric fields \( E \sim 10^{-13} \div 10^{-14} \text{V/cm} \sim 3 \cdot 10^{-16} \div 3 \cdot 10^{-17} \text{ CGSE} \) in ten days operation. Therefore, for \( \beta_s^T = \frac{E_B}{4\pi \rho B} \) we can get the estimation \( \beta_s^T \approx 10^{-43} \div 10^{-45} \text{cm}^3 \) (\( \rho \approx 2 \cdot 10^{22}, B \approx 10^4 \div 5 \cdot 10^4 \text{ Gauss} \)).

The obtained evaluation for \( \beta_s^T \) \( (\beta_s^T \sim 10^{-43} \div 10^{-45} \text{cm}^3) \) and the expressions (6,10) allow us to evaluate the mixing ratio \( \eta_{nf}^T \). Recall that conventional T-,P-even polarizability of an atom can be expressed similar (6) with replacement of the matrix element \( \mu \) by the matrix element \( d \) (and \( \eta_{nf}^T = 0 \)). Therefore, we can estimate \( \beta_s^T \sim \beta_s \alpha \eta_T \), where \( \beta_s \) is the conventional T-,P-even polarizability of the atom, \( \alpha = \frac{1}{137} \) is the fine structure constant and \( \eta_T \) is some average value for the coefficient of mixing of opposite parity levels \( \eta_{nf}^T \). The estimation for \( \eta_T \) follows from the above: \( \eta_T \sim \frac{\beta_s^T}{\beta_s \alpha} \approx 10^{-17} \div 10^{-19} \) (the atom polarizability is of the order \( \beta_s \sim 10^{-24} \text{cm}^3 \), for example, for Xe according to [10] \( \beta_s = 2.7 \cdot 10^{-24} \text{cm}^3 \)).

Two types of T-,P-odd interactions contribute to the constant of mixing of opposite parity
levels $\eta_{nT}^T$: the interaction of the electron EDM with the coulomb field of the nucleus and the T-,P-odd interaction of the electron with the nucleus nucleons.

The spin-independent part of the T-,P-odd interaction of an electron with nucleons is described by two constants $k_{1p}$ describes interaction with protons and $k_{1n}$ describes interaction with neutrons. For example, calculation adduced in $^8$ for Cs provides $\eta_T = 3.7 \cdot 10^{-11} (0.41k_{1p} + 0.59k_{1n})$, where the sum $(0.41k_{1p} + 0.59k_{1n}) < 5 \cdot 10^{-4}$. Therefore, for Cs $\eta_T \lesssim 10^{-14}$. The same limits for the sum $k_{1p}$ and $k_{1n}$ were obtained from EDM measurements for $^{129}$Xe (0.4$k_{1p} + 0.6k_{1n}) \lesssim 10^{-4}$.

Let us note that in the experiment $^2$ planned to measure the EDM of Cs atoms trapped in optical lattices is expected to obtain sensitivity of Cs EDM measurement of about $d_{Cs} \approx 3 \cdot 10^{-25} e \cdot cm$. This value of the atom EDM provides to improve estimation for $\eta_T$ and to get limits $\eta_T \lesssim 10^{-16}$ and the sum of $k_{1p}$, $k_{1n} \lesssim 5 \cdot 10^{-6}$.

As it was shown above the experiments studying $\beta_{T}^{s}$ provide for mixing coefficient the value $\eta_T \lesssim 10^{-17} \div 10^{-19}$. Therefore, these experiments give hope to reduce (three orders) the estimations for the sum $k_{1p}$, $k_{1n}$ (it is expected to be $\lesssim 10^{-7} \div 10^{-9}$). This value for $k_{1p}$, $k_{1n}$ is significantly lower than the limitation which could be obtained from the results of measurements of atom dipole moment that have been done earlier (see, for example, $^8$) and from the proposed experiment $^2$.

Let us consider now what limits for the electron EDM $d_e$ can be obtained from study of the effect $^7$. To estimate contribution from $d_e$ to polarizability $\beta_{T}^{s} \sim \beta_{s}\alpha\eta_T$ let us use connection of mixing coefficient $\eta_T$ (caused by the electron EDM $d_e$) with the atom EDM $d_A$ induced by the electron EDM $d_e$: $d_A \sim \epsilon\alpha\eta_T \sim Rd_e$ $^8$, $R$ is the atomic EDM enhanced factor. Therefore, $\eta_T \sim \frac{Rd_e}{\epsilon\alpha}$. Using the mentioned estimations for $\beta_{T}^{s}$ and $\eta_T$ we obtain $d_e \sim \frac{a\beta_{T}^{s}}{\epsilon\alpha R} e \cdot cm$ i.e. $d_e \sim 10^{-27} \div 10^{-30} e \cdot cm$ ($\beta_{T}^{s} \approx 10^{-43} \div 10^{-45} cm^3$, $R \approx 10^2 \div 5 \cdot 10^2$).

Let us remind that the upper limit $d_e \lesssim 1.6 \cdot 10^{-27} e \cdot cm$ follows from the experiments with Tl $^4$.

Thus, experimental study of the effect $^7$ provides to get more (three or four orders) strict limits for constants, which describe T-,P-odd interactions of an electron with nucleons and for $d_e$. Such improvement of estimations constrains theories beyond the Standard Model. To study effect $^7$ one could use different atoms (molecules) and substances (for example, ferroelectric crystals providing very high electric fields for heavy atoms) and this study does not require target cooling to ultralow temperatures (1 K and lower). Spins of atoms
(molecules) can be nonpolarized or atoms (molecules) can be spinless.

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