Local signaling with molecular diffusion as a decoder of Ca$^{2+}$ signals in synaptic plasticity

Honda Naoki, Yuichi Sakumura and Shin Ishii*

Graduate School of Information Science, Nara Institute of Science and Technology, Takayama, Ikoma, Nara, Japan
*Corresponding author. Graduate School of Information Science, Nara Institute of Science and Technology, 8916-5 Takayama, Ikoma, Nara 630-0192, Japan.
Tel.: +81 743 72 5984; Fax: +81 743 72 5989; E-mail: ishii@is.naist.jp

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Synaptic plasticity is induced by the influx of calcium ions (Ca$^{2+}$) through N-methyl-D-aspartate receptors (NMDARs), and the direction and strength of the response depend on the frequency of the synaptic inputs. Recent studies have shown that the direction of synaptic plasticity is also governed by two distinct NMDAR subtypes (NR1/NR2A, NR1/NR2B). How are the different types of regulation (frequency-dependent and receptor-specific) processed simultaneously? To clarify the molecular basis of this dual dependence of synaptic plasticity, we have developed a mathematical model of spatial Ca$^{2+}$ signaling in a dendritic spine. Our simulations revealed that calmodulin (CaM) activation in the vicinity of NMDARs is strongly affected by the diffusion coefficient of CaM itself, and that the local CaM diffusion system works as a dual decoder of both the frequency of Ca$^{2+}$ influxes and their postsynaptic current shapes, generated by two NMDAR subtypes, implying that spatial factors may underlie the complicated regulation scheme of synaptic plasticity.

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Introduction

Ca$^{2+}$ ions play a role in triggering signal transduction pathways that regulate a variety of neurobiological processes including synaptic plasticity, one of the major mechanisms underlying learning and memory. In a neuron, Ca$^{2+}$ signaling is spatiotemporally regulated both globally, within a cellular compartment such as a dendritic spine, and locally at the site of Ca$^{2+}$ entry. Thus, the differences between local and global Ca$^{2+}$ signaling must be elucidated in order to fully understand the spatial regulation of signal transduction cascades.

The frequency of synaptic inputs, and hence the frequency of Ca$^{2+}$ influxes caused by N-methyl-D-aspartate receptor (NMDAR) activation, is thought to dictate the direction and strength of synaptic plasticity (Dudek and Bear, 1992; Markram et al, 1997; Johnston et al, 2003). It was reported recently, however, that the direction of synaptic plasticity is also governed by NR2A- and NR2B-containing NMDAR subtypes; the induction of long-term potentiation (LTP) is blocked by antagonists of NR2A but not of NR2B, whereas the induction of long-term depression (LTD) is blocked by antagonists of NR2B but not of NR2A (Liu et al, 2004a; Massey et al, 2004). This implies a controversial ‘receptor-specific regulation’ of synaptic plasticity (Bliss and Schoepfer, 2004; Rusakov et al, 2004; Wong et al, 2004). How the distinct characteristics of synaptic plasticity (i.e., frequency-dependent and receptor-specific regulation) are realized simultaneously has yet to be elucidated.

With respect to global Ca$^{2+}$ signaling within an entire dendritic spine, there is a potential problem with receptor-specific regulation. Because Ca$^{2+}$ diffusion is very rapid, and the volume of a dendritic spine is relatively small (<1 μm$^3$), the Ca$^{2+}$ concentration should, in effect, become instantaneously uniform within a spine. If so, downstream signals originating from different Ca$^{2+}$ sources are likely to become entangled. This problem could be avoided if the downstream signaling works specifically in the so-called Ca$^{2+}$ nanodomain, an area with a relatively high Ca$^{2+}$ concentration localized near Ca$^{2+}$ channels (Augustine et al, 2003).

Studies in hippocampal neurons have indicated that molecular regulation in local Ca$^{2+}$ signaling is associated with changes in synaptic weight. An electrophysiological study using two different exogenous Ca$^{2+}$ buffers, BAPTA and EGTA, provided circumstantial evidence of local Ca$^{2+}$ signaling around NMDARs during the induction of LTP (Hoffman et al, 2002). Moreover, a Ca$^{2+}$ imaging experiment has shown that L-type voltage-sensitive Ca$^{2+}$ channels do not contribute measurably to increasing Ca$^{2+}$ levels in spines, but instead to activating calcium/calmodulin (CaM)-dependent kinase II (CaMKII), suggesting the existence of local Ca$^{2+}$ signaling (Yasuda et al, 2003). Immunohistochemical studies have shown that plasticity-related molecules, such as CaMKII and protein phosphatase 1 (PP1), are localized at the postsynaptic densities (PSDs) just below synaptic membranes (Sheng and Lee, 2000; Winder and Sweatt, 2001; Blackstone and Sheng, 1998).
The significance of local Ca$^{2+}$ signaling can also be predicted computationally in simulation studies of Ca$^{2+}$ signaling. When the signaling pathway was modeled as a uniform system, the computed level of CaM activation was low and insufficient to upregulate CaMKII (Bhalla, 2002a, b), probably due to the lack of spatially localized reactions. Despite this evidence of local Ca$^{2+}$ signaling, its role in the regulation of synaptic plasticity has not yet been clarified.

The diffusion of Ca$^{2+}$ is so rapid that it is probably difficult to regulate local Ca$^{2+}$ signaling in small components such as dendritic spines. In this study, we focus on local signaling mediated by CaM instead of Ca$^{2+}$ itself, because CaM diffuses relatively slowly, and hence allow for flexible control on the signaling. CaM, a Ca$^{2+}$ effector protein, is a primary transducer that mediates the Ca$^{2+}$-regulated inductions of synaptic plasticity (Xia and Storm, 2005).

The effects of molecular diffusion must be considered as local regulation, because molecular diffusion should be physically and chemically impeded if proteins accumulate to a high level in a local space. In fact, the abundance of actin filaments and PSD-95 (a scaffolding protein) under synaptic membranes is a remarkable aspect of dendritic spines (Kennedy, 2000; Matus, 2000). Furthermore, the in vivo suppression of molecular diffusion has been reported in neurons and smooth muscle cells (Popov and Poo, 1992; Luby-Phelps et al, 1995); this impedance should contribute to the local molecular regulation of synaptic plasticity.

To examine the contributions of local reactions in the Ca$^{2+}$ nano-domain and the impeded diffusion of CaM to the regulation of synaptic plasticity, we have constructed a mathematical model of spatial Ca$^{2+}$ signaling in a dendritic spine, in which Ca$^{2+}$ flows into the cytoplasm and interacts with diffusing CaM. To clarify the molecular basis of the frequency-dependent and receptor-specific regulation of synaptic plasticity, in particular, we have examined the response of local Ca$^{2+}$ signaling while taking into account the frequency and postsynaptic current shapes of Ca$^{2+}$ influxes generated by two NMDAR subtypes (Erreger et al, 2005). First, we show that local Ca$^{2+}$ signaling is regulated in a different manner from global signaling. Second, we shed light on a significant dependence of local CaM dynamics on CaM diffusion, suggesting that to achieve a sufficient level of local CaM activation, the system requires a moderate CaM diffusion coefficient. Third, we demonstrate that as long as CaM is able to diffuse, local Ca$^{2+}$ signaling can process different features of synaptic inputs: the frequency and current shapes of Ca$^{2+}$ influxes. Moderate CaM diffusion enables local Ca$^{2+}$ signaling to act as a ‘dual decoder’ to translate these input features into the correlated level of CaM activity. We also show that these local dynamics are highly robust to various Ca$^{2+}$-regulating factors, such as the buffering system and excretion by Ca$^{2+}$ pumps, and hence that the decoding properties are preserved under any conditions. These findings suggest that a ‘local CaM diffusion system’ functions as the molecular basis of the complicated regulation scheme of synaptic plasticity.

**Results**

To simulate local dynamics of Ca$^{2+}$ signaling, we constructed a model of spatial Ca$^{2+}$ signaling in a dendritic spine (1 μm$^3$), which included Ca$^{2+}$ influx through NMDARs, Ca$^{2+}$ uptake by pumps, leakage through the membrane, buffering by Ca$^{2+}$-binding proteins, and CaM activation (Figure 1A; for details, see Materials and methods and Supplementary Figure 1). To pay attention to the locality of Ca$^{2+}$ signaling, we assumed radial diffusion from a Ca$^{2+}$ source consisting of a cluster of NMDARs.

**The difference between local and global Ca$^{2+}$ signaling**

To examine the characteristic difference between local and global Ca$^{2+}$ signaling, we investigated the spatiotemporal details of Ca$^{2+}$ and CaM responding to Ca$^{2+}$ influxes injected through NMDARs. When Ca$^{2+}$ influxes were applied to the

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**Figure 1** A scheme of a model spine and a local Ca$^{2+}$ profile. (A) The model spine is composed of hemispherical elements and has a volume of 1 μm$^3$. Ca$^{2+}$ ions were injected through NMDARs as a point source located at the center of the spine (red arrow). Diffusing molecules were assumed to diffuse radially from the NMDARs. Ca$^{2+}$ influx, Ca$^{2+}$ uptake by pumps, leakage from the membrane, and buffering by Ca$^{2+}$-binding proteins were all incorporated into the model. To compare local and global signaling, we focused on the concentrations of Ca$^{2+}$ and CaM in the local and global areas as indicators of the degree of signaling activity at the PSD and in the whole spine, respectively. (B) The spatiotemporal Ca$^{2+}$ profile when a sequence of 10 Ca$^{2+}$ influxes was injected at 50 Hz (upper panel) into the model. Each injected current was biologically realistic (amplitude=9 pA, Ca$^{2+}$ fraction=11%, period=10 ms) (Pina-Crespo and Gibb, 2002; Nimchinsky et al, 2004). The horizontal axis denotes the elapsed time from the onset of current injection, and the vertical axis denotes the distance from the site of the NMDARs (lower panel).
model spine, a high Ca$^{2+}$ concentration (>90 μM) was localized at the Ca$^{2+}$ nano-domain, which is within 50 nm of the influx source (β scale of PSDs) (Figure 1B), and its transient time course formed rectangular shapes (Figure 2A, upper panel), reflecting the shapes of the influx time course (Figure 1B, upper panel) (Supplementary Figure 2 shows the case when triangular-shaped currents were applied). Such transient responses of Ca$^{2+}$ in the local area are considered to occur owing to the rapid formation of a Ca$^{2+}$ steady gradient resulting from fast Ca$^{2+}$ diffusion. In contrast to these local Ca$^{2+}$ dynamics, the global Ca$^{2+}$ response was rather slow and cumulative (Figure 2A, lower panel). The cumulative effect of Ca$^{2+}$ depended on the distance from the NMDARs (Figure 2B), as has been suggested by a modeling study of a presynaptic system for the facilitation of vesicle release (Tang et al., 2000).

Responding to such Ca$^{2+}$ profiles, CaM was highly activated in the local area, but only weakly activated in the global area (Figure 2C). This high CaM activity in the local area was sufficient to upregulate CaMKII, a CaM effector protein (Supplementary Figure 3). A particularly important aspect of local CaM activation is the accumulation of input stimuli, which is not realized by the local Ca$^{2+}$ concentration. The slower diffusion of CaM than of Ca$^{2+}$ (Figure 2D) induces the accumulation of activated CaM in the local area. In contrast, the obtained global CaM activity was small, less than 0.75 μM, which was insufficient to upregulate CaMKII (Supplementary Figure 3). This activation was due to diffusion of activated CaM from the local area, and actually CaM was not activated in the global area when the CaM diffusion was blocked (Supplementary Figure 4). These observations suggest that the regulation of Ca$^{2+}$ signaling should be treated as a spatial system, rather than as a uniform system, which ignores spatial factors, even in a tiny spine.

The behavior of simulated global Ca$^{2+}$ is consistent with biological data. In our simulation, peak concentration was around 1 μM and decay time constant was around 23.5 ms (Figure 2A, lower panel). Comparable values were measured by Ca$^{2+}$ imaging studies in dendritic spines (Murthy et al., 2000; Holthoff et al., 2002; Sabatini et al., 2002) (see the comparison of Ca$^{2+}$ decay behavior with experimental data in Supplementary Figure 5). If a Ca$^{2+}$ indicator (Fluo-4, 200 μM) was added to the model spine in a simulation experiment, peak Ca$^{2+}$ decreased and the decay of global Ca$^{2+}$ concentration became slower (Supplementary Figure 6). To show the adequacy of the model behaviors from a different perspective, we reproduced the experimentally observed effects of exogenous Ca$^{2+}$ buffers, BAPTA and EGTA, on local and global Ca$^{2+}$ signaling (Supplementary Figure 7) (Hoffman et al., 2002). Moreover, we checked the robustness of local and global Ca$^{2+}$ signaling against variation in buffering systems, excretion by Ca$^{2+}$ pumps, and spine morphology such as size and geometry. To summarize the results, global Ca$^{2+}$ signaling was sensitive to most of those factors, but local Ca$^{2+}$ signaling was highly robust (Supplementary Figures 8–12).

![Figure 2](image_url)

**Figure 2**  The details of local and global Ca$^{2+}$ signaling. (A) The time courses of Ca$^{2+}$ in the local area (25–50 nm away from the NMDARs, upper panel) and in the global area (>350 nm from the NMDARs, lower panel). These curves were extracted from Figure 1B. (B) Accumulation effect of Ca$^{2+}$ response, dependent on the distance from NMDARs. Peak Ca$^{2+}$ responses are plotted against the number of input pulses in a burst stimulus (10 pulses) so that each Ca$^{2+}$ peak value at the onset is normalized at 1. (C) The time courses of CaM activation in the local (upper panel) and global (lower panel) areas, induced by Ca$^{2+}$ influxes. (D) Temporal changes of Ca$^{2+}$ (upper panel) and CaM (lower panel) activities are plotted against the distance from NMDARs. Red, black, blue, and green lines indicate the time of 0, 1, 10, and 60 ms, respectively, elapsed after Ca$^{2+}$ stimulation was finished at 190 ms.
The effects of molecular diffusion on local Ca$^{2+}$ signaling

Local diffusion of CaM may be impeded not only chemically by interaction with CaM effectors, but also physically by the cytoskeleton and scaffolding proteins, because PSDs in dendritic spines contain an abundance of proteins. Indeed, it was found that the diffusion coefficient of receptors moving two-dimensionally on the plasma membrane decreases exponentially as scaffolding proteins accumulate (Nakada et al., 2003). To examine the effects of this restricted molecular diffusion on local Ca$^{2+}$ signaling, we investigated CaM activation in the Ca$^{2+}$ nano-domain using various diffusion coefficients for CaM. CaM activation resulting from the high Ca$^{2+}$ level in the local area depended strongly on the diffusion coefficient of CaM (Figure 3B). When the CaM diffusion coefficient estimated in vitro (Yang et al., 2001) was used, CaM activity was close to zero, as observed in previous simulation studies based on a uniform system (Bhalla, 2002a, b), whereas nondiffusible CaM resulted in CaM activation that exceeded the level required for 100% CaMKII autophosphorylation (Figure 3A and B and Supplementary Figure 3). When the diffusion coefficient of CaM was set to the value observed in vivo (Luby-Phelps et al., 1995), the level of CaM activation in the local area lay within the controllable range for CaMKII autophosphorylation (green line in Figure 3A and B). Local CaM activation was thus found to relate inversely to the diffusion coefficient of CaM (Figure 3C). These results suggest that CaM must diffuse at a moderate rate, as has been observed in vivo, to be activated and controlled in the local area. Moreover, these results imply that the cytoskeleton may regulate local signal transduction by influencing molecular diffusion in the area.

A local CaM diffusion system as a dual decoder

The dependence of Ca$^{2+}$ signaling dynamics on frequency and current shapes of Ca$^{2+}$ influxes was examined. First, three kinds of Ca$^{2+}$ bursting influxes were applied to the model spine (Figure 4A). To see solely the effect of frequency here, each burst contained the same number of Ca$^{2+}$ influxes and hence the same quantity of Ca$^{2+}$ ions. As shown in Figure 2A and B, there was no cumulative effect in local Ca$^{2+}$ (Figure 4C), whereas both global Ca$^{2+}$ and local active CaM accumulated depending on the frequency (Figure 4B and D). Next, the shape of Ca$^{2+}$ influxes is another important characteristic because it is known that current shape depends on the two main subtypes of NMDARs, NR2A- and NR2B-containing NMDA receptors; the current produced by NR2A-containing NMDARs has a higher amplitude and a shorter duration than that produced by NR2B-containing receptors (Erreger et al., 2005). To investigate the effect of current shape on Ca$^{2+}$ signaling, we prepared three current shapes including the same quantity of Ca$^{2+}$ (Figure 4E). Different current shapes induced different peak values of Ca$^{2+}$ concentration (Figure 4F) and CaM activation (Figure 4H) in the local area, but the difference was not very prominent for global Ca$^{2+}$ (Figure 4F).

In the induction of synaptic plasticity, the direction and strength depend on the frequency of Ca$^{2+}$ influxes (Dudek and Bear, 1992; Markram et al., 1997; Johnston et al., 2003) and NMDAR subtypes (Liu et al., 2004a; Massey et al., 2004). This frequency-dependent and receptor-specific regulation is evidence that Ca$^{2+}$ signaling simultaneously transfers both the frequency and influx rate signals to downstream cascades (‘dual decoder’) in levels of Ca$^{2+}$, CaM, or CaM effectors. We propose that such a dual regulation can be explained by
integrating the results of Figure 4. To examine if responses of Ca\(^{2+}\) and CaM in local and global area correlated with the frequency and influx rate signals, peak responses of Ca\(^{2+}\) signaling to these two input features are summarized in Figure 5. Here, for simple representation of the influx rate, the shape of a rectangular current was characterized by the amplitude and time width for a fixed total quantity of Ca\(^{2+}\) ions.

The Ca\(^{2+}\) level in the global area depended on the frequency of Ca\(^{2+}\) influxes, but not significantly on the influx rate (Figure 5A and C, left panels), suggesting that the dual decoder does not work in global Ca\(^{2+}\) signaling. In contrast, the local Ca\(^{2+}\) level was proportional to the influx rate but independent of the frequency (Figure 5A and C, right panels). For local CaM activation, the frequency of the influxes and the influx rate were directly proportional to the amount of activated CaM.
The influx rate is characterized as the current amplitude. The duration of the current varied inversely with the amplitude of the current to keep the total quantity of Ca$^{2+}$ ions. (A) Peak plots of the Ca$^{2+}$ concentration in the local area (left panel) and in the global area (> 350 nm from the NMDARs) (right panel). (B) Peak plots of the CaM-4Ca$^{2+}$ concentration in the local area for the nondiffusible CaM model (left panel) and the diffusible CaM model using the CaM diffusion coefficient observed in vivo (Luby-Phelps et al. 1995) (right panel). Red lines indicate the cases in which the affinity dependence of CaM for Ca$^{2+}$ on CaM effector proteins was considered, as shown in (F). (E) A summary of the decoding abilities of Ca$^{2+}$ and CaM. If the peak response correlated linearly with the frequency or the influx rate, decoding is regarded as success (an open circle), otherwise, as failure (a filled circle). Correspondence to subfigures is also shown; for example, ‘A, left’ means this decoding success can be observed in the left panel of subfigure (A). (F) Dose–response curve of CaM for Ca$^{2+}$. This curve is derived from kinetic parameters of CaM using CaM4Ca = CaM$_{total}$K$_{i}$K$_{j}$K$_{k}$K$_{l}$Ca$^{2+}$/(1 + K$_{i}$Ca$^{2+}$ + K$_{j}$K$_{k}$K$_{l}$Ca$^{2+}$ + K$_{i}$K$_{j}$K$_{k}$K$_{l}$Ca$^{2+}$), K$_{i}$ = K$_{i}$/K$_{i}$ (i=1-4). Black and red lines indicate the cases without and with the kinetic parameter values of backward reaction in the third and fourth binding of Ca$^{2+}$ being one-tenth; the red-colored condition represents the increase in the affinity of CaM for Ca$^{2+}$ due to the interaction with CaM effector proteins.

One or two Ca$^{2+}$-bound CaM molecules interact with CaM effector proteins such as CaMKII and adenylate cyclase, and the interactions increase the affinity of CaM for Ca$^{2+}$ by reducing the dissociating reaction rate rather than by increasing the binding reaction rate (Johnson et al. 1996). When we introduced an increased affinity, by employing a one-tenth value for the kinetic parameter, to the backward reaction in the third and fourth binding of Ca$^{2+}$ (Figure 5F), little effect was found on the local CaM activity (red lines in Figure 5B and D, right panels), whereas global CaM activation was facilitated as CaM diffusion coefficient measured in vivo was used (Figure 5B and D, right panels), but not when CaM was prevented from diffusing (Figure 5B and D, left panels) (the time course of nondiffusible CaM activity is shown in Supplementary Figure 13). Thus, this local CaM diffusion system is necessary for Ca$^{2+}$ signaling to be able to dual-decode the frequency of influxes and the shape of currents (Figure 5E). In particular, the ability to detect the influx rate (current shape) may be the basis of receptor-specific regulation of synaptic signal transduction.
Figure 6  Reproduction of frequency- and NMDAR subtype-based regulation of synaptic plasticity. (A) The peak concentrations of CaM-4Ca\(^{2+}\) in the local area, computed after 100 identical Ca\(^{2+}\) influxes were applied to the model spine, are displayed. The frequency (horizontal axis) and the influx rate (vertical axis) of the Ca\(^{2+}\) influxes were varied in each trial. (B) Synaptic plasticity was modeled by a U-shaped function of the CaM-4Ca\(^{2+}\) concentration. The plasticity factor is expressed as positive and negative values for LTP and LTD, respectively. The boundary between LTD and LTP was set at 30 \(\mu\)M CaM-4Ca\(^{2+}\), which corresponds to the concentration necessary for around 65% CaMKII activity at equilibrium (see Figure 3A). (C) The resultant synaptic plasticity computed from the peak CaM-4Ca\(^{2+}\) concentration (A) using the U-shaped function (B). The meaning of labels (i–iv) is explained in the text. (D) An illustration of the regulation of synaptic plasticity by the subtypes of NMDARs. The labels (i–iv) correspond to those in (C). (E) The dependence of synaptic plasticity on the frequency of Ca\(^{2+}\) influxes for two influx rate values, corresponding to NR2A- and NR2B-containing receptors. These data are extracted from (C). The blue and red curves are schematic, each roughly interpolating the circles. (F) The relationship between synaptic plasticity and the global Ca\(^{2+}\) level in the model spine. The plasticity factor is obtained by applying the U-shaped function (B) to the local CaM-4Ca\(^{2+}\) concentration (A), not to the global Ca\(^{2+}\) concentration.
expected (Supplementary Figure 14). This result implies that dual decoding is not influenced by CaM affinity. Moreover, the dual decoding was found to be robust against variations in the buffering, excretion system, spine morphology, and current shapes of injected Ca\(^{2+}\) influxes (see Supplementary Figures 15–19).

**Synaptic plasticity induced by local CaM activity**

The dependence of CaM activation on the frequency and current shapes of Ca\(^{2+}\) influxes is comprehensively evaluated in Figure 6A. For the bridge between CaM activation (Figure 6A) and the expression of LTP and LTD (represented by the plasticity factor), we assumed that the plasticity factor is defined by a U-shaped function of the CaM-4Ca\(^{2+}\) concentration (Figure 6B).

The U-shaped function was mathematically derived from the network structure of downstream cascade (CaMKII/calci-neurin-PP1 system) (D’Aicam et al., 2003), based on the idea that the change in synaptic weight regulated by neurin-PP1 system) (D’Aicam et al., 2003) (D’Alcantara et al., 2003), based on the idea that the change in synaptic weight regulated by phosphorylation of AMPA receptors is determined by a balance between kinase (CaMKII) and phosphatase (calci-neurin, PP1) activities (Lisman, 1989). In great details of signaling cascades involving the regulation of synaptic plasticity, CaM behaves as a hub and is believed to integrate Ca\(^{2+}\) signals (Xia and Storm, 2005). Then, it is reasonable to evaluate synaptic plasticity outcomes with respect to CaM activity.

Applying this U-shaped function to the calculated levels of activated CaM obtained from burst stimulations with variable frequencies and influx rates resulted in two-dimensional synaptic plasticity as shown in Figure 6C. The parameter space can be divided into four regions: (i) the stimulations induced LTP, (ii) the stimulations induced LTD, and (ii) and (iv) no plasticity was induced.

We propose here that our model can explain the NMDAR subtype-specific regulation of synaptic plasticity (Liu et al., 2004a; Massey et al., 2004) (Figure 6C and D). Under control conditions, high-frequency stimulation (HFS) causes both subtypes of NMDARs to respond in this spine, leading to plasticity factor values in regions (i) and (ii), whose combination results in LTP. If the NR2A subtypes are blocked, only region (ii) remains and no plasticity is induced. If the NR2B subtypes are blocked, only region (i) remains and LTP is induced. On the other hand, low-frequency stimulation (LFS) results in plasticity factor values in regions (iii) and (iv) thereby inducing LTD. If the NR2B subtypes are blocked, region (iii) disappears and no plasticity is generated. Conversely, if the NR2A subtypes are blocked, only region (iv) disappears and LTD is induced.

In addition, our model reproduced the dependence of synaptic plasticity on the frequency of synaptic inputs being U-shaped (Figure 6C) (Dudek and Bear, 1992; Johnston et al., 2003). Furthermore, consistent with the observation that during neuronal development, the NR2A/NR2B ratio in NMDARs increases (Liu et al., 2004b) and LTP gradually becomes dominant over LTD (Puyal et al., 2003), we found that LTP became dominant when a high influx rate was applied to the model (Figure 6E). We also found a U-shaped relationship between the global Ca\(^{2+}\) concentration and synaptic plasticity (Figure 6F). This reminds us of the conventionally discussed relationship between plasticity and the spatially averaged Ca\(^{2+}\) level, which has been observed in Ca\(^{2+}\) imaging studies (Hansel et al., 1997; Cormier et al., 2001; Johnston et al., 2003).

It should be noted here that the plasticity factor in our model was determined by local CaM activity and not by global Ca\(^{2+}\) levels (Figure 6B).

**Discussion**

The connections between spatial factors in signal transduction and specific biological functions have not been sufficiently investigated. We have shown the significance of spatial factors, such as local reactions within the Ca\(^{2+}\) nano-domain and the diffusion of Ca\(^{2+}\) effector proteins, to the Ca\(^{2+}\) signaling required for synaptic plasticity.

Ca\(^{2+}\) nano-domain (≥ 90 μM, < 50 nm) appeared during the application of Ca\(^{2+}\) influxes (Figure 1B). This high Ca\(^{2+}\) concentration activated CaM excessively because of inherent strong affinity of CaM for Ca\(^{2+}\) when CaM could not diffuse (Figure 3B). Such excessive CaM activation was, however, prevented by diffusion of CaM itself, as shown in Figure 3B and C. As long as CaM diffuses at a moderate rate as in vivo, local CaM activity remains in an appropriate range, which is useful to control downstream signaling (Figure 3A). This ‘local CaM diffusion system’ functions as a ‘dual decoder’ of both the frequency of Ca\(^{2+}\) influxes and the current shapes generated by two distinct NMDA receptor subtypes (Erreger et al., 2005) (Figure 5B and D, right panels). Frequency decoding is realized by CaM diffusion transferring transient frequency-indep-endent Ca\(^{2+}\) responses into accumulated responses of CaM, whereas influx rate decoding is realized by means of Ca\(^{2+}\) levels before the signals are transduced into the CaM activity. The dual decoding in local Ca\(^{2+}\) signaling is strongly robust, regardless of how global Ca\(^{2+}\) behaves.

Previous studies proposed that CaMKII detects the stimulation frequency by becoming autophosphorylated, thereby translating the frequency level into the strength of LTP. CaMKII was observed to act as a frequency decoder of Ca\(^{2+}\) stimulation in vitro and in vivo (De Koninck and Schulman, 1998; Eshete and Fields, 2001). On the other hand, a biochemical study revealed that the phosphorylation state of CaMKII at equilibrium depends on the Ca\(^{2+}\) concentration (Bradshaw et al., 2003), hence on CaM activity (Figure 3A). In our simulation, the phosphorylation level of CaMKII was in effective determined by the peak concentration of active CaM, because the local concentration of active CaM was rapidly increased and saturated as Ca\(^{2+}\) stimulation and the saturated level depended on the frequency and the influx rate of Ca\(^{2+}\) stimulation. This is the reason why we evaluated the decoder’s ability in relation to the peak response of active CaM, but not to its temporal integration. Therefore, our results indicate that the local CaM diffusion system, rather than CaMKII, plays the main role in decoding the information of synaptic stimulation (Figure 5).

The dual decoding by the local CaM diffusion system provides a mechanism for both the frequency-dependent and NMDAR subtype-specific regulation of synaptic plasticity (Figure 6C); our model of local Ca\(^{2+}\) signaling with
constrained molecular diffusion successfully realized the receptor-specific regulation, which could not be accomplished by global Ca$^{2+}$ signaling. Moreover, our model reproduced the observed developmental shift from LTD to LTP (Figure 6E).

We also found that the relationship between the global Ca$^{2+}$ concentration and the synaptic plasticity induced by local CaM activity was U-shaped (Figure 6F). Currently, it is thought that synaptic plasticity is simply determined by the Ca$^{2+}$ concentration in a U-shaped fashion (Hansel et al., 1997; Yang et al., 1999; Cormier et al., 2001; Johnston et al., 2003); high and moderate Ca$^{2+}$ concentrations induce LTP and LTD, respectively. In this simplified scheme, however, the Ca$^{2+}$ concentration is averaged over the entire spine, and hence does not reflect local Ca$^{2+}$ signaling. On the other hand, recent experimental studies showed that local Ca$^{2+}$ signaling around Ca$^{2+}$ channels regulates the induction of LTP (Hoffman et al., 2002; Yasuda et al., 2003), suggesting that synaptic plasticity cannot be explained simply by the averaged Ca$^{2+}$ concentration, and that local Ca$^{2+}$ signaling must be taken into account. We, therefore, speculate that the conventional ‘global Ca$^{2+}$ hypothesis’ is too macroscopic to allow us to understand the complicated regulation scheme of synaptic plasticity.

Local CaM activation was found to be strongly affected by the diffusion coefficient of CaM itself (Figure 3C). CaM diffusion may be regulated by cytoskeletal structures such as actin filaments. The polymerization of actin is affected by the diffusion coefficient of CaM itself (Figure 3C). CaM activation was found to be strongly affected by the diffusion coefficient of CaM itself (Figure 3C).

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cylindrical approximation (Holmes and Levy, 1990; Zador et al., 1990). Compared with the cylindrical approximation, our model pays more attention to locality of Ca2⁺ signaling around a localized cluster of NMDARs: NR2A-containing NMDA receptors are localized specifically in synaptic clefts, whereas those containing NR2B tend to be localized far from the release sites of presynaptic vesicles (Collingridge et al., 2004; Liu et al., 2004).

Ca²⁺ regulation

Ca²⁺ ions were injected through a number of NMDARs as a point source located at the center of the first shell (Figure 1A and Supplementary Figure 1). Ca²⁺ influx was given as a rectangular shape (Figure 1B, upper panel) and the concentration change was defined by

\[
\frac{d(Ca^{2+}\text{in})_{n-1}}{dt}_{\text{influx}} = -\gamma I/(2FV_{\text{n-1}})
\]

where \(\gamma\) denotes the fraction of current I carried by Ca²⁺ through the NMDARs and F is the Faraday’s constant. Because the estimated number of NMDARs opens in a single spine by a synaptic spike is three (Nimchinsky et al., 2004) and the current through a single channel was measured at 3 pA (Pina-Crespo and Gibb, 2002), I was set at 9 pA (10 ms), except when examining the effect of Ca²⁺ influx rate on local Ca²⁺ signaling (Figures 4–6).

Extrusion of Ca²⁺ from the spine was modeled by three types of Ca²⁺ pumps (SERCA, Na⁺/Ca²⁺ exchanger, and PMCA) situated only at the outermost (15th) shell (Figure 1A and Supplementary Figure 1). The Ca²⁺ extrusion process was described by Hill’s equation:

\[
\frac{d(Ca^{2+}\text{out})_{n-1}}{dt}_{\text{pump}} = -v_{\text{max}} \frac{(Ca^{2+}\text{out})_{n-15}}{K_n + (Ca^{2+}\text{out})_{n-15}}
\]

where \(v_{\text{max}}\) is the maximal velocity of Ca²⁺ clearance, \(K_n\) is the half-maximal concentration of Ca²⁺ for each pump, and \(n\) is the Hill coefficient. Leak Ca²⁺ flow was also added into the outermost shell with the leak constants \(v_{\text{extracell}}\) and \(L_{\text{ER}}\) (Figure 1A and Supplementary Figure 1):

\[
\frac{d(Ca^{2+}\text{extracell})_{n-15}}{dt}_{\text{leak}} = -v_{\text{extracell}}(Ca^{2+}\text{extracell})_{n-15} - (Ca^{2+}\text{extracell})_{n-15}
\]

\[
-L_{\text{ER}}(Ca^{2+}\text{ER})_{n-15} - (Ca^{2+}\text{ER})_{n-15}
\]

where \((Ca^{2+}\text{extracell})_{n-15}\) and \((Ca^{2+}\text{ER})_{n-15}\) are Ca²⁺ concentrations outside the model spine and in the endoplasmic reticulum, respectively.

For Ca²⁺ buffering, we distributed five kinds of Ca²⁺-binding proteins uniformly into the model spine: four kinds of immobile, and very-slow CBPs. The kinetic parameters of immobile CBPs (fast CBP, medium CBP, slow CBP, and very-slow CBP) followed the previous models (Markram et al., 1998; Franks et al., 2001). Mobile CBPs, which are likely to contribute to Ca²⁺ dynamics, are diffusible and their diffusion coefficients are independent of Ca²⁺ binding in the model. Binding of Ca²⁺ ions to CBPs was modeled by the association and dissociation reactions:

\[
\frac{d(Ca^{2+}\text{CBP})_{n}}{dt}_{\text{CRP}} = -k_2(Ca^{2+}\text{CBP})_{n} + k_3(Ca^{2+}\text{CBP})_{n}
\]

where \(k_2\) and \(k_3\) are the association and dissociation rates, respectively.

Calmodulin regulation

CaM has four binding sites for Ca²⁺ ions (two sites in each of the C- and N-terminal domains) and its transducer function was assumed to emerge when all four sites are occupied (CaM-4Ca²⁺). Each Ca²⁺ binding step in this fourth-order reaction was calculated by

\[
\frac{d(Ca^{2+}\text{CM})_{n}}{dt}_{\text{CM}} = k_{12}(Ca^{2+}\text{CM})_{n} - (k_{2} + k_{3} + k_{4})(Ca^{2+}\text{CM})_{n} + k_{4}(Ca^{2+}\text{CM})_{n}
\]

where \([CaM\cdot zCa^{2+}]_{n}\) denotes the concentration of CaM bound by \(z\) Ca²⁺ ions, and \(k_{1}, k_{2}, k_{3}, k_{4}\) are the association and dissociation rates in the zth step reaction \((z=0, 1, 2, 3, 4)\). Note that the association rate of N-terminal domains used in the model was one-tenth that measured in vitro (Luby-Phelps et al., 1995), because Ca²⁺ binding is interfered owing to the interaction of CaM with Mg²⁺ and K⁺ ions, and the effective rates then decrease (Linse et al., 1991; Malmendal et al., 1999). The concentration of CaM was set at 200 μM in the model spine. For the diffusion coefficient of CaM, we used the value previously measured in smooth muscle cells (Luby-Phelps et al., 1995), except when examining model behaviors against various values of the diffusion coefficient (Figure 3C). The diffusion coefficient of CaM was assumed to be independent of Ca²⁺ binding.

In this biochemical model, we did not distinguish the kinetic parameters of Ca²⁺ binding with CaM free or trapped by CaM effector proteins. The rate constants were adopted from an in vitro experimental report; to use these experimentally measured values, which should be a mixture of the rate constants of free and trapped CaM, implicitly incorporates the effect of interaction between CaM and CaM effector proteins (Johnson et al., 1996). Furthermore, in the diffusion process, we did not model differential diffusions between free CaM and trapped CaM, and we adopted the diffusion coefficient measured in vitro (Luby-Phelps et al., 1995); this experimental value should also include the effect of interaction between CaM and CaM effector proteins. Therefore, recruitment of the reaction rate constants and diffusion coefficient measured in vivo represents the average dynamics of signaling mediated by free CaM and trapped CaM.

All parameters used in the control condition of our model are listed with their values in Supplementary Table 1. Simulations were performed using MATLAB (The Mathworks Inc., MA).

Supplementary information

Supplementary information is available at the Molecular Systems Biology website (www.nature.com/msb).

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