Probing millicharge at BESIII

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We propose to search for millicharged particles at the BESIII detector which is operated at the Beijing Electron Positron Collider. We compute the monophoton signal events at the BESIII detector due to millicharged particle production, as well as due to standard model irreducible/reducible backgrounds. By utilizing all the data accumulated at the BESIII detector since 2011, we derive new leading upper limits on millicharge, \(\varepsilon \lesssim (0.86 - 2.5) \times 10^{-3}\), for the mass range, 0.1 GeV \(\lesssim m \lesssim 1\) GeV. Furthermore, projections with more data to be collected at the BESIII detector are also made. Our analysis significantly reduces the parameter region of millicharge to account for the anomalous 21 cm absorption signal near redshift \(z \simeq 17\) recently observed by the EDGES experiment.

Introduction. Electric charge quantization is an empirical fact. Charge quantization is also theoretically related to the magnetic monopole, because if any magnetic monopole exists in the Universe, it quantizes the electric charge \cite{1}. However, so far, there is no clear experimental evidence to support the existence of the magnetic monopole. Thus we do not know yet what mechanism leads to electric charge quantization.

A number of experiments have been carried out to detect the non-integer charge of particles in the standard model (SM), and very stringent limits have been obtained. For example, the charge of hydrogen atom and neutron are measured to be smaller than \(10^{-21}\)e, where \(e\) is the magnitude of the electron charge \cite{2–5}. There are also searches for new particles beyond the standard model that carry electric charge, and very strong constraints on electrically charged new particles have been imposed from various laboratory experiments and astrophysical processes \cite{6–8} for the review on the constraints. The electrically charged particles beyond SM are referred as millicharged (or minicharged) particles, since usually only new particles with very small electric charge are allowed.

To parameterize the extremely weak coupling between a millicharged fermion and the SM photon, we employ the following interaction Lagrangian

\[
\mathcal{L}_{\text{int}} = e\varepsilon A_\mu \bar{\chi} \gamma^\mu \chi, \tag{1}
\]

where \(\chi\) is the millicharged particle, \(A_\mu\) is the SM photon, and \(\varepsilon\) is the millicharge (normalized to the magnitude of the electron charge). There are viable theoretical models in which millicharged particle can naturally occur. For example, millicharged particles may be present in models in which a kinetic mixing term is introduced between different \(U(1)\) gauge fields \cite{9, 10}. Millicharged particles can also arise in Stueckelberg extensions of the standard model in which mass terms generated by the Stueckelberg mechanism mix the SM \(U(1)_Y\) gauge boson and new Abelian gauge bosons in the hidden sector beyond SM \cite{11, 12}. In this paper, we only consider the millicharged particle and the interaction given by Eq. (1); we decouple all other particles that appear in a specific model and do not consider any additional interaction between millicharged particles with SM.

Recently, an anomalous absorption signal near redshift \(z \simeq 17\) in the cosmological 21 cm spectrum was observed by the EDGES experiment \cite{13}. To explain such a signal, a number of papers have used millicharged dark matter (DM) particles to cool the hydrogen atom in the Universe. Millicharged DM is a good candidate to explain the 21 cm anomaly, since the interaction cross section between DM and baryons exhibits a \(e^{-4}\) behavior which is consistent with cosmological observations. Our analysis in this paper has direct implications to the parameter space of millicharged particles that can explain the 21 cm anomaly \cite{14–16}.

In this paper, we propose to search for millicharged particles below GeV at the BESIII detector which is operated at the Beijing Electron Positron Collider (BEPCII). The existing laboratory constraints for MeV-GeV millicharged particles include bounds from the SLAC electron beam-dump experiment \cite{17}, bounds from the SLAC MilliQ searches \cite{18}, bounds from the E613 experiment \cite{19}, and bounds from MiniBooNE \cite{20}. Recently, CMS collaboration \cite{21} excludes particles with electric charge \(2e/3 \ (e/3)\) below 310 (140) GeV. There is also a proposed experiment at the LHC aiming to detect millicharged particles \cite{22}. Here we use the monophoton signal to probe the MeV-GeV millicharged particles by analyzing the BESIII data of \(\sim 15\) fb. The monophoton signature has been considered previously in DM searches at \(e^+e^-\) colliders \cite{23–28}. Here we first carry out a detailed analysis at the BESIII detector by taking into account various backgrounds. We derive the BESIII sensitivity to the millicharge, and show that the BESIII detector can probe the parameter region that has not been constrained by previous experiments.

Signals of millicharged particles at electron colliders. Millicharged particle can be produced at particle colliders via its coupling with the standard model photon. However, if the millicharge is very small, the produced millicharged particle is often undetectable in practice,
because only a feeble signature inside particle detectors could be produced. Thus one relies on final state particles produced in additional to the millicharged particle for the detection, which is analogous to most dark matter searches at particle colliders.

At the electron-positron collider, we use the monophoton signal to search for the millicharged particles. The Feynman diagram for the production process of the single photon in association with millicharged particles, $e^+e^- \rightarrow \chi \gamma$, is shown in Fig. (1), where $\chi$ stands for the millicharged particle.

The differential cross section for the $e^+e^- \rightarrow \chi \gamma$ process is given by

$$\frac{d\sigma}{d\gamma dE_\gamma} = \frac{8\alpha^3 s^2 (1 + 2m_\chi^2/s_\gamma)}{3s E_\gamma (1 - z_\gamma^2)} \left[ 1 + \frac{E_\gamma^2}{s_\gamma} (1 + z_\gamma^2) \right], \tag{2}$$

where $E_\gamma$ is the energy of the final state photon, $z_\gamma \equiv \cos \theta_\gamma$, with $\theta_\gamma$ being the relative angle between the final state photon and the beam direction of the initial state electron, $s$ is the square of the center-of-mass energy, $m_\chi$ is the mass of the millicharged particle, $s_\gamma = s - 2\sqrt{s}E_\gamma$, and $\beta_\chi = (1 - 4m_\chi^2/s_\gamma)^{1/2}$. Here we have integrated over all possible momenta for the two final state millicharged particles and neglected the electron mass.

The irreducible background. The major irreducible standard model background processes to the monophoton signal at the electron-positron collider are the $e^+e^- \rightarrow \nu_\tau \bar{\nu}_\tau \gamma$ processes, where $\nu_\tau = \nu_\tau, \nu_\mu, \nu_\tau$ are the three standard model neutrinos. The corresponding Feynman diagrams are displayed in Fig. (2). For electron neutrinos, both the $Z$-boson and the $W$-boson diagram contribute; whereas the muon and tau neutrinos are only produced via the $Z$-boson diagrams. For electron colliders operated at the GeV scale, the diagram mediated by two $W$ bosons are significantly smaller than those with a single $W$ or $Z$ mediator. Thus we do not consider the diagram with two $W$ mediators for our analysis in the electron colliders running with GeV beam energy. The differential production cross section for the $e^+e^- \rightarrow \nu_\tau \bar{\nu}_\tau \gamma$ processes mediated by a single $W/Z$ boson is given by [31] [29]

$$\frac{d\sigma}{d\gamma dE_\gamma} = \frac{\alpha G_F^2 s_\gamma^2}{4\pi^2 s E_\gamma (1 - z_\gamma^2)} f(s_W) \left[ 1 + \frac{E_\gamma^2}{s_\gamma} (1 + z_\gamma^2) \right], \tag{3}$$

where $G_F$ is the Fermi constant, $s_W \equiv \sin \theta_W$ with $\theta_W$ being the weak mixing angle, and $f(s_W) = 8s_W^4 - 4s_W^2/3 + 1$. Here we have integrated over the momenta of the final state neutrinos and summed all three neutrino flavors. As shown in Fig. (3), the monophoton cross section due to the irreducible SM background grows with the colliding energy; however, the monophoton cross section due to millicharged particle production in the $m_\chi = 0.1$ GeV case increases when the colliding energy decreases. Thus, electron collider with smaller colliding energy has a better sensitivity to kinematically accessible millicharged particles.

There are other irreducible SM backgrounds due to semi-invisible meson decays; for example the decay mode $J/\psi \rightarrow \nu_\tau \bar{\nu}_\tau \gamma$ contributes to the irreducible background if the colliding energy is tuned to coincide with the mass of the $J/\psi$ meson. However, the branching ratio of these decay modes are typically very small, for instance, $\text{BR}(J/\psi \rightarrow \nu_\tau \bar{\nu}_\tau \gamma) = 0.7 \times 10^{-10}$ in SM [32]. Thus we exclude these irreducible backgrounds in meson decays in

Figure 1. Feynman diagram for the process $e^+e^- \rightarrow \chi \gamma$. The diagram with photon radiated by the positron is included in the analysis, but not drawn here. The diagrams with photon radiated by millicharged particles are not considered since they are suppressed by $\varepsilon$.

Figure 2. Feynman diagrams for the process $e^+e^- \rightarrow \nu_\tau \bar{\nu}_\tau \gamma$, where $\nu_\tau = \nu_\tau, \nu_\mu, \nu_\tau$ [29, 30].

Figure 3. The monophoton cross sections of the irreducible SM background and of millicharged particles as a function of $\sqrt{s}$ in the BEPCII energy range, $2.0 \text{ GeV} \leq \sqrt{s} \leq 4.6 \text{ GeV}$. The kink in the $m_\chi = 0.1 \text{ GeV}$ curve is due to the maximum energy measured in the EMC at BESIII which is 2 GeV.
our analysis.

Reducible backgrounds at the BESIII detector. Next we want to investigate the reducible backgrounds at the BESIII detector, which is located at the double-ring BEPCII with the beam energy ranging from 1.0 GeV to 2.3 GeV [33]. The reducible backgrounds are present due to the limited detection capability of the BESIII subdetectors. The main drift chamber (MDC), the innermost subdetector of BESIII, that determines the momentum of a charged particle, covers the polar angle $|\cos\theta| < 0.93$ [33]. The electromagnetic calorimeter (EMC) that measures the energies and positions of electrons and photons consists of the barrel with angle coverage $|\cos\theta| < 0.83$ and the endcap with angle coverage $0.85 < |\cos\theta| < 0.93$ [33]. The Time-of-Flight (TOF) sub-detector which is placed between the drift chamber and the electromagnetic calorimeter measures the flight time of charged particles. The TOF consists of the barrel with angle coverage $|\cos\theta| < 0.83$ and the endcap with angle coverage $0.85 < |\cos\theta| < 0.95$ [33].

One of the most important reducible backgrounds arises from the radiative Bhabha scattering, $e^+e^- \rightarrow e^+e^\gamma$, where neither of the two final state electrons is detected. The Bhabha scattering can be mediated by either an s-channel or a t-channel virtual photon; because any of the four external fermion legs can radiate a photon, there are eight diagrams in the radiative Bhabha scattering. Two of the radiative Bhabha diagrams are shown in Fig. (4).

![Feynman diagram](image)

Figure 4. Feynman diagram for the process $e^+e^- \rightarrow e^+e^\gamma$. Here diagrams mediated by a virtual Z boson are neglected.

We further consider the $e^+e^- \rightarrow ff\gamma$ background where the final state $f$ fermion ($f \neq e$) escapes detection, and the $e^+e^- \rightarrow \gamma\gamma\gamma$ process where only one of the three final state photons is detected. There are also reducible backgrounds from meson decays in which a final state photon is undetected due to the limited detection capability. We consider all these reducible backgrounds in our analysis.

Detector simulation. We simulate signal events and different SM background events for various BESIII running energies, which are shown in Table (11). For the signal process $e^+e^- \rightarrow \chi\bar{\chi}\gamma$ and the irreducible background $e^+e^- \rightarrow \nu\bar{\nu}\gamma$, we generated one million points from the analytic differential cross sections, Eq. (2) and Eq. (3), in the $E_\gamma-Z_\gamma$ plane using Monte-Carlo methods; each point has a weighted differential cross section.

There are several singularities associated with the radiative Bhabha scattering. For the final state photon, neither infrared divergence nor the collinear singularity is relevant since the photon has to be detected. However, because the final state $e^\gamma$ has to be undetected in order to contribute to the background, the collinear singularity ($e^\gamma\gamma\gamma\gamma$ going along the beam directions) cannot be removed. This arises in the t-channel photon processes as shown in Fig. (4). Although the electron mass makes this collinear singularity finite, it is still difficult to numerically compute the scattering cross section in the collinear region of the phase space which, however, dominates the total cross section [34-37]. We use FeynArts [38] and FORM-CALC [39] packages to numerically evaluate the cross section for the process $e^+e^- \rightarrow e^+e^-\gamma$ where the final state $e^\pm$ has $|\cos\theta| > 0.95$ which is beyond the coverage of the TOF, as well as MDC and EMC. FeynArts and FORM-CALC packages output weighted scattering cross sections for different phase space points. We found that MADGRAPH [40] cannot sample the phase space efficiently due to the collinear singularity. We carry out similar calculations for $e^+e^- \rightarrow \mu^+\mu^-\gamma$ and $e^+e^- \rightarrow e^+e^-\gamma\gamma$. We impose $E_\gamma > 1$ MeV [41] to remove the infrared divergence in $e^+e^- \rightarrow \gamma\gamma$.

We use EvtGen [42, 43] to simulate reducible background coming from meson decays. We generate $2 \times 10^8$ meson decay events for $J/\psi$, $10^8$ events for $\psi(3683)$, $10^8$ events for $\psi(3770)$, and $3 \times 10^7$ events for $\psi(4040)$.

The energy and position information of photon and electron are determined by the EMC. The energy resolution of the EMC at the BESIII detector is [33]

$$\sigma(E)/E = 2.3%/\sqrt{E/\text{GeV}} \pm 1\%.$$  (4)

The angular resolution also depends on the energy of the particle; we provided the following fitted function which gives a nice approximation to the angular resolution [44]

$$\sigma(\theta) = (0.024/\sqrt{E/\text{GeV} - 0.002}) \text{(rad).}$$  (5)

To simulate the detector effects on the final state particles, we smear the energy and the polar angle for the final state electron and photon using Gaussian distributions which take into account the resolution functions, Eq. (4) and Eq. (5).

Detector cuts. The energy measurement for electrons or photons in the EMC at the BESIII detector ranges from 20 MeV to 2 GeV. We follow the cuts used by the BESIII Collaboration [45]: (hereafter the basic cuts) photon candidates must satisfy $E > 25$ MeV in the barrel ($|\cos\theta| < 0.8$) or $E > 50$ MeV in the end-caps (0.86 < $|\cos\theta| < 0.92$).

However, after the basic cuts, the reducible background due to $e^+e^- \rightarrow e^+e^-\gamma$ is still very large, as shown in Fig. (5) where we display $E_\gamma - z_\gamma$, normalized distributions for both the monophoton events due to millicharged
particle production process and the $e^+e^- \rightarrow e^+e^-\gamma$ process. To suppress the big reducible backgrounds, we further impose the following cuts (hereafter the advanced cuts) on top of the basic cuts:

$$E_{\gamma}/\text{GeV} > a z_i^2 + b_i$$

where $a$ and $b$ are free parameters to be fixed by maximizing the significance. The advanced cuts are motivated by the fact that the final photon in the central region ($|\cos \theta| < 1$) cannot have a sufficient large energy due to energy conservation in the $e^+e^- \rightarrow e^+e^-\gamma$ process with both final $e^\pm$ going along the beam directions. The $e^+e^- \rightarrow \mu^+\mu^-\gamma$ and $e^+e^- \rightarrow \gamma\gamma\gamma$ background processes exhibit similar distributions. As shown in Table (I) and in Fig. (5), the advanced cuts are very efficient in eliminating these reducible backgrounds.

| Cuts    | $\chi\chi\gamma$ | $\nu\bar{\nu}\gamma$ | $e^+e^-\gamma$ | $\mu^+\mu^-\gamma$ | $\gamma\gamma\gamma$ | $S$    |
|---------|------------------|------------------------|----------------|---------------------|---------------------|-------|
| Basic   | 32.3             | 1.39                   | $6.9 \times 10^3$ | $2.6 \times 10^3$  | $4.5 \times 10^3$  | 0.0038 |
| Advanced| 6.58             | 0.022                  | 0              | 0                   | 0                   | 2.56  |

Table I. The cross sections (in unit of fb) of the signal and SM background processes after each cut, and the corresponding significance $S = S/\sqrt{S+B}$. The integrated luminosity is $L = 1 \text{ fb}^{-1}$ and the running energy is $\sqrt{s} = 4.18 \text{ GeV}$. We choose $m_\chi = 0.1 \text{ GeV}$ and $\varepsilon = 0.01$ for the millicharged particle. The advanced cut here is $E_\gamma/\text{GeV} = 0.99 z_i^2 + 0.99$.

We optimize the advanced cuts for each BESIII running energy by choosing the $a$ and $b$ values that maximize the significance for the case in which $m_\chi = 0.1 \text{ GeV}$ and $\varepsilon = 0.01$. Four SM backgrounds are considered in the optimization, including $e^+e^- \rightarrow \nu\bar{\nu}\gamma$, $e^+e^- \rightarrow e^+e^-\gamma$, $e^+e^- \rightarrow \gamma\gamma\gamma$, and the reducible background in meson decays. Table (II) shows the optimized $a$ and $b$ values for each running energy at BESIII. We have checked that under the optimized advanced cuts, the $e^+e^- \rightarrow \mu^+\mu^-\gamma$ process does not contribute any background event.

| Year | $\sqrt{s}$ (GeV) | $L$ (fb$^{-1}$) | $a$ | $b$ | $\varepsilon_{95}$ |
|------|------------------|----------------|-----|-----|------------------|
| 2015 | 2.125            | 0.5           | 0.52 | 0.53 | 0.015           |
| 2012 | 3.097            | 0.5           | 0.68 | 1.12 | 0.015           |
| 2017 | 3.515            | 0.5           | 0.79 | 0.86 | 0.0095          |
| 2011 | 3.554            | 0.5           | 0.84 | 0.86 | 0.044           |
| 2012 | 3.686            | 0.5           | 0.95 | 1.21 | 0.013           |
| 2011 | 3.773            | 1.99          | 0.89 | 0.94 | 0.0051          |
| 2017 | 3.872            | 0.2           | 0.90 | 0.96 | 0.016           |
| 2011 | 4.009            | 0.5           | 0.92 | 0.98 | 0.011           |
| 2016 | 4.18             | 3.1           | 0.99 | 0.99 | 0.0060          |
| 2013 | 4.23             | 1.05          | 1.00 | 1.01 | 0.011           |
| 2013 | 4.26             | 0.83          | 1.01 | 1.02 | 0.013           |
| 2017 | 4.28             | 3.9           | 1.04 | 1.04 | 0.0063          |
| 2012 | 4.36             | 0.5           | 1.06 | 1.05 | 0.019           |
| 2014 | 4.42             | 1             | 1.02 | 1.08 | 0.014           |
| 2014 | 4.6              | 0.5           | 1.04 | 1.14 | 0.024           |
| 11-17 | -               | 15.024        | -   | -   | $8.6 \times 10^{-4}$ |

Table II. The center-of-mass energy and corresponding luminosities collected since 2011 at the BESIII detector, and the corresponding optimized $a$ and $b$ parameters for the advanced cuts. $\varepsilon_{95}$ is the 95% C.L. upper limit on millicharge $\varepsilon$ for the $m_\chi = 0.1 \text{ GeV}$ case. Data before 2017 are given by [46], and information about 2017 data is provided by [47]. The last row shows the limit combining all data between 2011 and 2017.

**Methodology of combining data.** A large amount of data have been accumulated by the BESIII detector at various running energies since 2011 when the monophoton trigger was implemented [48]. A summary of the BESIII data is presented in Table (II) where the data are arranged by the center-of-mass energy $\sqrt{s}$. To probe the millicharge, we carry out a likelihood analysis to combine all the data collected at various running energies as shown in Table (II). We first define a chi-square at each running energy

$$\chi_i^2 = \frac{S_i}{\sqrt{S_i + B_i}},$$

where $S_i$ ($B_i$) is the number of signal (background) events at the running energy labeled by the index $i$. Here $B_i$ includes the SM irreducible background, the SM reducible backgrounds, and other possible background events caused by instruments. We further build a likelihood function $L_i$ for each running energy as follows

$$L_i = \exp(-\chi_i^2/2).$$

The total likelihood function $L$ for combining all the running energies can be built via

$$L = \Pi_i w_i L_i,$$
where \( w_i \) is the weight for each running energy. The test-statistic (TS) is related to the total likelihood via

\[
TS = -2 \ln \mathcal{L}.
\]

The 95% confidence level (C.L.) exclusion limit on the millicharge \( \varepsilon \) is obtained by demanding that the corresponding TS is larger by 2.71 than that in SM. In our analysis, we set \( w_i = 1 \) for all data points.

Results. Fig. (6) shows the combined 95% C.L. exclusion upper limits on millicharge \( \varepsilon \) for various masses, by using the data presented in Table (II). Here we further consider other possible background events that are caused by instruments; a simple Monte-Carlo algorithm is used to assign these instrumental background events to various running energy points according to the integrated luminosity. As shown in Fig. (6), the current BESIII data can probe millicharge down to \( \varepsilon \lesssim 0.86 (2.5) \times 10^{-3} \) for the \( m_\chi = 0.1 \) (1) GeV case. Fig. (6) further shows pre-existing experimental constraints in the 0.01 GeV \( \lesssim m_\chi \lesssim 1 \) GeV mass range, which include bounds from the SLAC electron beam-dump experiment [17], bounds from the SLAC MilliQ searches [18], bounds from E613 [19], and bounds from MiniBooNE [20]. Thus, BESIII data can provide new leading upper limits to the millicharged particle in the mass range, 0.1 GeV \( \lesssim m_\chi \lesssim 1 \) GeV. The new limits significantly reduce the parameter space in which one can use 1% millicharged DM to explain the 21 cm anomaly [14–16].

Projections are made under the assumption that additional 10 fb\(^{-1}\) data are to be collected in the future BESIII runs. Two different projected limits are drawn on Fig. (6) for collecting 10 fb\(^{-1}\) more data at \( \sqrt{s} = 2.125 \) GeV and \( \sqrt{s} = 4.6 \) GeV; realistic data takings with more running energies can be interpolated between these two projected limit lines.

Summary. In this work, we have proposed a search for millicharged particles via the monophoton signature at the BESIII detector at BEPCII. We found that by using the current BESIII data, one can provide new leading constraints on the millicharged particle in the mass range, 0.1 GeV \( \lesssim m_\chi \lesssim 1 \) GeV. We also systematically analyzed the irreducible and reducible SM backgrounds for the monophoton signature that are essential for dark matter searches at the BESIII detector which was lacking in the literature to our knowledge.

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