Effects of Response Format on Psychometric Properties and Fairness of a Matrices Test: Multiple Choice vs. Free Response

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Reasoning is regarded to be an essential facet of fundamental cognitive abilities. As examinee characteristics may affect performance in Reasoning tests, concern about maintaining fairness is expressed. The purpose of the current study was to examine effects of response format on psychometric properties and fairness of a matrices test according to examinee's sex, risk propensity, and test anxiety. A total of 433 German-speaking pupils (aged 14–20) were randomly assigned to either a multiple choice or a free response version of the same 25-item test. Data analysis yielded Rasch-homogeneous 23-item versions, with higher reliability, but lower criterion validity for the free response test. No interactions between response format and sex, test anxiety, or risk propensity were revealed, but a significant main effect of sex: men out-performed women in reasoning irrespective of response format. Results are discussed with reference to attributes of the test situation and sample characteristics.

Keywords: reasoning, response format, multiple choice, free response, fairness

INTRODUCTION

The question regarding the most appropriate response format to gain valid information concerning test takers' characteristics is currently becoming a “hot topic” within the assessment of personality in the job context with reference to the newly emerged forced choice format (see Usami et al., 2016; Lin and Brown, 2017; O'Neill et al., 2017; Brown and Maydeu-Olivares, 2018; Wetzel and Greiff, 2018). However, studies addressing response formats within the domain of the assessment of knowledge, skills, and abilities with stem-equivalent items are rare. One reason for this may lay in the fact that innovative and promising developments of response formats are scarce. As regards the constructed response format, often also called free response (FR), its standard application is obviously easier to implement into a test design when responses can be verbalized (e.g., Sebrechts et al., 1991; Edwards and Arthur, 2007). When presenting item material based on complex and abstract figures, new ways of FR formats are required. Within the current study, we compared a new FR version with a multiple choice (MC) version for the assessment of figural reasoning (Piskernik, 2013) with reference to their psychometric properties.

Reasoning has been considered to be a crucial aspect of fundamental thinking abilities or general intelligence (Carroll, 1993). Valid, reliable and fair measurement of reasoning should provide information about a test taker's general intelligence level, which revealed as a strong predictive value not only for academic and professional success, but also for success in life and health (Carroll, 1993; Mittring and Rost, 2008; Danner et al., 2016; Schmidt et al., 2016). However, the
robustness of test scores with reference to method bias has been questioned by past research, as, for example, by studies comparing an adaptive and a fixed item version of the same matrices test (Ortner and Caspers, 2011; Ortner et al., 2014) or by a study investigating achievement differences between students with and without reading difficulties in varying response formats (Collins et al., 2018). Identifying tests’ psychometric features and test takers’ personal and environmental characteristics that may contribute to the emergence of test bias is hence a highly relevant task for psychological research.

As regards test design, most published matrices tests are based on MC format (e.g., Raven et al., 1998; Hossiep et al., 1999; Formann, 2002; Booth and Horn, 2004). Previous research demonstrated significant group differences in various MC tests in scores partially based on systematically differing personality characteristics beyond the assessed target construct. This was found, for example, for men and women (Irving and Lynn, 2005), for people who are more or less likely to take risks (Rowley, 1974; Alnabhan, 2002; Rubio et al., 2010) and for more or less test anxious persons (Benjamin et al., 1981; Crocker and Schmitt, 1987). Taking into consideration that achievement tests aim to assess individuals’ maximum performance, systematic decrement in performance due to construct-irrelevant sources of score variance related to group membership may diminish validity of a test in certain groups, and may jeopardize test fairness (Zieky, 2016).

Comparisons of test scores between persons are valid when these scores indicate equal psychological meanings between individuals (Van de Vijver and Poortinga, 1997). On the other hand, test bias describes systematic error that differentially impairs the validity of test scores in identified groups of persons (Reynolds, 2000). Test fairness has been described as one of the fundamental psychometric standards for designing, developing and administering psychological tests (Dorans and Cook, 2016). With reference to test design, the Standards for Educational and Psychological Testing of the AERA, APA, and NCME have stated that “fairness is a fundamental validity issue and requires attention throughout all stages of test development and use” (p. 49; AERA, 2014). According to Helms’ Individual-Differences (HID) model (2006), test fairness was defined as identification and removal of systematic variance in test results which is irrelevant for the construct and can be attributed to these psychological characteristics.

Ever since the MC format was developed, its pros and cons over the FR format have been discussed and studied empirically (e.g., Kastner and Stangl, 2011; Bonner, 2013; Hudson and Treagust, 2013; Schult and Lindner, 2018; Schult and Sparfeld, 2018; Liou and Bulut, 2020). Economy and efficiency for administrators of tests emerged as advantages of the MC format (McCoubrie, 2004), with test takers indicating preferences for the MC format as this was rated as easier. Nevertheless, there are also test administrators and subjects who prefer the FR format (McCoubrie, 2004; Powell, 2012; Mingo et al., 2018). They argue that higher level cognitive processes are required in order to answer FR questions compared to MC tests, where retrieving learned facts and other sources besides learning success or high cognitive performance can contribute to a high score, as, for example, test wiseness (Rowley, 1974; Birenbaum and Tatsuoka, 1987; Martinez, 1999; McCoubrie, 2004; Heyborne et al., 2011; Powell, 2012).

However, several studies (as reviewed by Rodriguez, 2003; Simkin and Kuechler, 2005; Bonner, 2013) empirically compared various MC modes (e.g., true/false, assignment tasks, MC with varying numbers of options, single correct answer, multiple correct answers, with the option “none of the above is true,” with the option “I don’t know the answer”) as well as different FR modes (e.g., clozes, sentence completion, short answer, essay) within several domains (e.g., mathematics, reading comprehension, vocabulary). Various study designs like within- and between-subjects designs as well as stem-equivalent and non-stem-equivalent items were employed in these studies. Even though test scores gained for both response formats revealed mostly high correlation coefficients when related to each other (e.g., 0.92 with stem-equivalent items, 0.85 with non-stem-equivalent items; Rodriguez, 2003), some variability on account of response format has not yet been empirically explained (Rodriguez, 2003; Simkin and Kuechler, 2005; Bonner, 2013; Woodcock et al., 2019).

The present study aimed to contribute (1) to the question of differential effects of response format not only regarding psychometric properties of tests, but also (2) concerning test fairness in terms of differential effects of response format according to test takers’ personality characteristics. Especially two aspects of personality revealed as relevant with reference to response format in the literature: Risk propensity (e.g., Rubio et al., 2010) and test anxiety (e.g., Crocker and Schmitt, 1987). Risk propensity has been defined as willingness to show behavior that involves an unknown probability of danger and negative consequences, but also the possibility of winnings or benefits (Leigh, 1999). Risk propensity is represented by a continuum with a certain amount of risky behavior being adaptive but becoming maladaptive at extreme levels (Dahne et al., 2013). In order to assess risk propensity, self-report questionnaires represent the most frequently employed approach (e.g., Johnson et al., 2004). In addition, objective tests (see Lejeune et al., 2002; Ortner and Proyer, 2015; Kyllonen and Kelly, 2018) assess test takers’ behavior in standardized miniature situations and quantify risky behavior in terms of behavior samples. Numerous studies have shown a higher tendency for test takers possessing higher levels of risk propensity to guess in MC tests when they were unsure about items, while people with low risk propensity preferred to skip those questions (Alnabhan, 2002; Rubio et al., 2010; Baldiga, 2013). As the probability of guessing correctly in a MC test with eight response options is 12.5%, or even more if some distractors can be excluded, high risk-taking individuals have a significantly higher likelihood of achieving more points in MC tests than low risk-taking subjects (Rowley, 1974; Alnabhan, 2002; Rubio et al., 2010; Stenlund et al., 2018). Research showed that even when test takers were required to answer all items in a test based on MC format, persons with higher scores in the willingness to risk a penalty in a test situation outperformed those with lower risk scores (Rowley, 1974). Studies furthermore revealed men to score higher in MC tests while women showed higher omission rates of items...
This was explained by gender differences in guessing tendencies. Risk propensity may play a role in test taking when tactics can be relevant, such as guessing instead of omitting. As guessing is less or not possible in the FR format, possessing a higher level of risk propensity could be less advantageous. As a consequence, we expected test takers with high risk propensity to outperform test takers with low risk propensity at MC format while there are no differences between the two groups at FR format.

The second personality characteristic that we addressed with reference to response format was test anxiety. Test anxiety, defined as the tendency to extreme fear of being rated negatively in upcoming tests (Zeidner, 1998), has been acknowledged as a major disruptive factor for academic careers: severe test anxious pupils and students often failed in tests and achieved lower mean grades than less test anxious ones (Hembree, 1988; Zeidner, 1998; Von der Embse et al., 2013; Stenlund et al., 2018). Several studies reported sex differences in test anxiety (e.g., Putwain and Daly, 2014; Núñez-Peña et al., 2016; Lowe, 2019) and it has been identified as a source of bias for underperformance in standardized testing (as reviewed by Zeidner, 1998; McDonald, 2001). Taking different response formats into account, it seems easier for test takers to identify a solution by selecting it compared to constructing it. With reference to anxiety in a test situation, test takers could be more relaxed by knowing that they could identify the correct solution in a MC test also by chance, which is not possible in a FR test. We therefore presumed that test anxiety could represent a relevant characteristic when investigating these two response formats for the first time with reference to reasoning ability. However, surprisingly few studies examined if test anxious people are more disadvantaged by one of the response formats. Two studies revealed that test takers who reported higher scores in test anxiety performed relatively better at MC sections than at FR items. It was hypothesized that test-related worries have a distracting impact and make it easier to recognize a correct answer than constructing it (Benjamin et al., 1981; Crocker and Schmitt, 1987). As MC tests were often considered to be less frightening than FR tests by pupils and students (Birenbaum and Feldman, 1998; Zeidner, 1998), test anxiety could be especially detrimental in FR studies. Therefore, we expected high test anxious persons to perform at an inferior level compared with low test anxious people in the FR format while fewer differences should arise in the MC format.

Both mentioned aspects of personality—risk propensity and, as referred to above, test anxiety—are known to interact with sex (e.g., Zeidner, 1990; Byrnes et al., 1999; Farooqi et al., 2012; Bulgan, 2018), which has also been mentioned with reference to response format. Two meta-analyses of sex differences in the widely applied progressive matrices test (Raven et al., 1998) with 57 included studies (Lynn and Irwing, 2004), respectively 22 included studies (Irving and Lynn, 2005) showed men generally outperforming women ($d = 0.33$ resp. $d = 0.31$): This sex difference was replicated in different European countries (e.g., Lynn et al., 2004; Mackintosh and Bennett, 2005), South America (e.g., Rosseti et al., 2009), Asia and South Africa (e.g., Lynn, 2002; Lynn and Tse-Chan, 2003; Abdel-Khalek and Lynn, 2006). Nevertheless, some studies did not report significant differences between men and women in progressive matrices (e.g., Rushton and Cvorovic, 2009; Savage-McGlynn, 2012; Flores-Mendoza et al., 2013). Whereas, all of these results on sex differences were derived from matrices tests based on MC response format, only few studies have employed matrices tests based on FR format so far. They reported small sex differences in favor of men (e.g., Becker et al., 2014) or no significant differences between men and women (e.g., Piskernik, 2013). To examine the potential role of response format for the emergence of sex differences, matrices tests must be presented in an item-equivalent MC and FR version. Within the present study, we realized this design for the first time.

Regarding research on specific cognitive abilities or factual knowledge, data showed that men often outperformed women in the MC version, while both sexes performed approximately the same in the FR version, or women performed even better: these interaction effects were demonstrated, for example, in mathematics and languages (Bolger and Kellaghan, 1990; Reardon et al., 2018), history (Bridgeman and Lewis, 1994) as well as in natural sciences (DeMars, 1998; Stanger-Hall, 2012). In contrast, Bonner (2013) reported no interaction between sex and response format in crystallized intelligence. Consequently, these results may suggest that previously reported sex differences in the domain of matrices tests may also be related to effects of the MC response format.

The present study was designed to provide new insights into the role of response format in matrices tests with reference to sex differences, related to aspects of personality—risk propensity and test anxiety—and psychometric properties. In line with these research aims, the first objective of the current study was to investigate possible effects of response format on the matrices test's Rasch model fit, difficulty, reliability by means of internal consistency, as well as influences on the test's criterion validity. The second objective of this work was to examine possible effects of response format on the results of matrices tests according to an examinee's sex, risk propensity and test anxiety.

**MATERIALS AND METHODS**

**Sample**

A sample of 433 German-speaking pupils (65.60% female, 34.40% male) between the ages of 14 and 20 ($M = 16.62, SD = 1.24$) participated voluntarily. Pupils from different Austrian secondary schools were invited to take part either in the context of psychology tuition or in their free time. An information letter about the experiment was given to all participants and written informed consent was obtained from the parents of under 16-years-olds as well as from all the pupils themselves.

**Materials**

**FRM**

The computerized Free Response Matrices test (FRM; Piskernik, 2013) consisted of 25 items representing an incomplete $3 \times 3$ matrix with figures. Each figure was made up of 5 x 5 squares either colored black or white (see an item example in Figure 1). The items were constructed according to rules, as for example, the rule *addition*, where the matrix components of the first and second figure had to be summed up in the third figure of every
row or column, and the rule *intersection*, where only matrix components that were present in the first as well as in the second figure, might be present in the third figure of every row or column. These underlying rules had to be found and applied correctly to complete the matrix with the missing pattern. Test takers were instructed to create the missing figure by clicking on the squares (or coloring the squares with a marker in the paper-pencil version). The items were scored dichotomously (correct = 1, incorrect = 0). The author reported an internal consistency of Guttman's $\lambda^2 = 0.88$, a correlation coefficient of $r = 0.81$ with Raven’s Advanced Progressive Matrices and Rasch model fit for the original FRM version (Piskernik, 2013). An internal consistency of $\alpha = 0.73$ was shown in this study.

**FRM With MC Format**

In order to investigate the influence of response format, we created a MC version of the FRM with stem-equivalent items. Following Preckel (2003), a rule taxonomy for distractor generation was created and seven distractors for each of the 25 FRM items were constructed and ordered randomly. Reliability was $\alpha = 0.57$ in the current study. **Figure 2** shows a sample item in the MC version.

Research by Mittring and Rost (2008) revealed that the correct solution of some matrices items (e.g., the APM; Raven et al., 1998) can be determined by simple counting of matrix components and analysis of sets, subsets or intersections, without looking at the item stem. A distractor analysis revealed that only 8% ($n = 2$) of the newly constructed MC items could potentially be solved by counting distractor components (in comparison to around 50% of the APM; Mittring and Rost, 2008). One or more distractors could potentially be excluded by applying the counting strategy in 56% ($n = 14$) of the new FRM MC items, and for 36% ($n = 9$) of the items no exclusion of distractors was possible without looking at the item stem.

**DOSPERT-ES**

To measure subjective risk propensity, the subset *ethics* of the Domain-Specific Risk-Taking Scale in its German version (DOSPERT-G, Johnson et al., 2004) was adapted for pupils and students. The test takers were supposed to rate how likely they would follow a risky activity or behavior on a Likert scale from 1 (very unlikely) to 5 (very likely). As Item 2 “... not declare a significant amount of income in the tax return” seemed inappropriate for pupils, it was replaced by the new item “... use a neighbor’s unsecured Wi-Fi without permission.” To make the scale even more appropriate for the research objective of current study, the additional item “... guess in a test, even if I don’t know the answer” was inserted. Overall, the new subset “ethics for pupils” (DOSPERT-ES) consisted of 9 items. Scores represent the scale mean from 1 to 5. An internal consistency of $\alpha = 0.73$ was shown in current study. Correlations between the original version of DOSPERT and self-reported frequencies...
of risky behavior (e.g., financial, ethical and social risk-taking) demonstrated construct validity (Weber et al., 2002).

BART

In the computerized test sessions we employed the Balloon Analogue Risk Task (BART; Lejuez et al., 2002) to assess objective risk propensity. Within this behavior based approach, test takers were instructed to virtually inflate 15 balloons on the screen with mouse clicks as far as possible without exploding. They saw a small red balloon accompanied by a balloon pump button labeled Pump up the balloon, a reset button labeled Collect $$$, potential earnings, balloon number, numbers of pumps and total winnings. Each click on the pump inflated the balloon 1° (about 0.125 in. [about 0.32 cm]) in all directions. With each pump, 0.5 points were accumulated in a temporary bank. The probability that a balloon could explode was fixed at 1/128 for the first pump. If the balloon did not explode after the first pump, the probability for explosion was 1/127 on the second pump, 1/126 on the third pump, and so on, until the 128th pump at which point the probability of an explosion was 1/1 (i.e., 100%). When a balloon was pumped to its individual explosion point, it disappeared and all points in the temporary bank were lost. At any point during each balloon trial, participants could stop pumping the balloon by clicking the Collect $$$ button. This click transferred all the points from the temporary bank to the permanent bank. Instructions were given based on Lejuez et al. (2002, pp. 78–79), with no precise information about the probability of explosion given. Participants were told the following: “It is your choice to determine how much to pump up the balloon, but be aware that at some point the balloon will explode.” The corrected average number of pumps (0–128), which is the average of clicks per unexploded balloon, served as a score for risk propensity. To incite the subjects, a small gift was given to the six participants with the most points. A reliability coefficient of $r = 0.87$ was reported (Ronay and Kim, 2006). With reference to criterion validity, BART scores were positively associated with self-reported risk-related behaviors, such as smoking ($r = 0.36$), gambling ($r = 0.44$), drug and alcohol consumption (both $r = 0.28$) as well as risky sexual behaviors ($r = 0.25$; Lejuez et al., 2002).

TAI-G

A short form of the Test Anxiety Inventory–German version (TAI-G; Hodapp, 1991), a questionnaire consisting of 15 items (Wacker et al., 2008) was employed to assess four dimensions of test anxiety: worry (five items), excitement (four items), lack of confidence (three items), and interference (three items). The mean total score (1–4) was applied to test the hypotheses. In this study, an internal consistency of $\alpha = 0.87$ was shown. The TAI-G has been shown to assess more trait-related stable individual differences than situational effects (Keith et al., 2003).

Further Measures

Demographic data including age, sex, and type of secondary school were provided by the subjects. Additionally, school grades in mathematics from 1 (highest grade) to 5 (lowest grade) of the last four school reports were surveyed on a voluntary basis to calculate the test’s criterion validity. Math grades were chosen as they showed the highest correlations with matrices in previous research (e.g., Heller et al., 1998; Pind et al., 2003). In total, 297 pupils declared their grades. A reliability coefficient of $\alpha = 0.90$ was calculated in the current study.

Procedure

We employed an experiment with between-subjects design. Pupils were randomly assigned to either the FR ($n = 203; 46.90\%$) or the MC ($n = 230; 53.10\%$) version. Furthermore, 53.30% worked on all tests and questionnaires in a computerized mode, 46.70% in a paper-pencil mode (except the BART, it was omitted in the paper-pencil condition). Data collection took place in quiet rooms at school or at the laboratory of the Department of Psychology. Each test taker worked about 50 min on all test and questionnaire items. Participants received a code and were given the opportunity to indicate if they wanted to receive anonymous feedback on their results.

Statistical Analyses

In a first step, we estimated the dichotomous Rasch model fit of the two response format modes separately in R by using the package TAM (Robitzsch et al., 2018). We further calculated person ability parameters ($\theta$) and extracted descriptive statistics for our data and correlations between all relevant variables using SPSS 21.

In the next step, a $2 \times 2$ ANOVA with response format (FR vs. MC) and sex as fixed factors was employed in SPSS 21 with PROCESS macro (Hayes, 2013) to assess the question of a sex $\times$ response format interaction on test scores. In order to address the flaw of Null Hypothesis Significance Testing that only evidence against the null hypothesis can be gathered and not in favor of it, we also followed the Bayesian approach as an alternative to frequentist statistics (see Wagenmakers et al., 2018). Using JASP 0.8 with the default scaling factor of 0.5 of the Cauchy distribution, we computed the Bayes factor which describes the ratio of one hypothesis’ likelihood to the likelihood of another. For an additional evaluation of interactions between personality characteristics and response format, moderated regression analyses with subjective and objective risk propensity as well as test anxiety as predictors and response format as moderator were computed.

Furthermore, we employed item response theory (IRT) analyses using performance median, sex, and age median as split criteria and extracted IRT item difficulty estimates in $R$ with the package TAM (Robitzsch et al., 2018) in order to reveal possible effects of response format on the Rasch model fit and the difficulties of the two modes. One claim of the Rasch model fit is the independency of item parameters from the particular sample of persons tested, which can be examined by checking whether item difficulties are dissimilar in specific groups (e.g., women vs. men, high or low ability groups). We used the $R$ package difR (Magis et al., 2010) for testing of differential item functioning (DIF). In detail, we employed the four DIF detection methods “TID” (Transformed Item Difficulties), “MH” (Mantel-Haenszel), “Std” (standardization) as well as “Logistic” (logistic regression), and applied “majority voting” for deciding whether
DIF was present or not (i.e., if three or more of the four tests suggested significant DIF on the \( p < 0.01 \), we concluded that DIF was present in the respective item). Finally, analyses of internal consistency in terms of Cronbach’s alpha were applied in SPSS 21 to compare reliability between both response formats, and criterion validity of the two test modes was estimated with Spearman correlation coefficients between FRM test scores and mathematics grades.

**RESULTS**

**Effects of Personality on Performance With Reference to Response Format**

Descriptive statistics for our data are listed in Table 1. The ANOVA with response format and sex as fixed factors revealed a significant main effect for sex in both response formats \( [F(1, 429) = 17.07, p < 0.01, \eta^2 = 0.03] \) with males \((M = 0.27, SD = 1.04)\) outperforming females \((M = −0.14, SD = 1.10)\). No significant main effect for response format \( [F(1, 429) = 0.18, p = 0.67, \eta^2 < 0.01] \) or interaction between sex and response format was revealed \( [F(1, 429) = 1.62, p = 0.20, \eta^2 < 0.01] \). When we analyzed this model in a Bayesian fashion, Bayes factors suggested that the model considering only the main effect for sex \((B_{10} = 94.11)\) was 29.32 times more likely than the model considering both main effects and the interaction between sex and response format \((B_{10} = 3.21)\) and 9.35 times more likely than the model comprising only the main effects sex and response format.

No significant interactions were shown between response format and subjective risk propensity in moderation analyses \( [\Delta R^2 < 0.01] \) when including the interaction term, \( F(1, 372) = 0.06, p = 0.81 \), between response format and objective risk propensity \( [\Delta R^2 < 0.01, F(1, 217) = 0.19, p = 0.67] \), and between response format and test anxiety \( [\Delta R^2 = 0.01, F(1, 372) = 0.42, p = 0.52] \).

**Effects of Response Format on Psychometric Properties**

In our Rasch model fit analysis, we dropped Item 7 from further analyses as all pupils had solved that item in the FR version and we removed item 19 due to significant outfit \((t = 3.64, p < 0.01)\) as well as infit \((t = 2.13, p = 0.03)\) in the FR scale. Significant outfit and infit of items in IRT analyses suggested a deviation from the assumed unidimensionality. The remaining 23-item model revealed satisfactory fit in the FR as well as in the MC data. Additionally, the models displayed good to sufficient Expected- A-Posteriori (EAP) reliability in both samples (FR: \( 0.73, MC: 0.57 \)). EAP reliability coefficients in IRT analyses were based on a Bayesian-adjusted posterior ability distribution and informed about the amount of reduced measurement uncertainties in the person ability parameters. When testing for DIF; all items showed good outfit (FR: all \( t < 1.52, p > 0.13 \); MC: all \( t < 1.39, p > 0.17 \)) and infit (FR: all \( t < 1.64, p > 0.10 \); MC: all \( t < 1.14, p > 0.26 \)) with performance median as split criterion. Employing age median and sex as split criteria revealed no DIF in both response formats, which means that the items did not function in different ways for the respective groups of test takers in either response format.

Analyses of IRT-based item difficulties of the FR \((M = −1.14, SD = 2.59)\) and the MC \((M = −1.29, SD = 1.75)\) version illustrated similar difficulties overall \([t(3863) = 0.23, p = 0.82, \eta^2 < 0.01] \), with only some items differing slightly between the two modes (see also Figure 3). Analysis of internal consistency revealed higher coefficients (see Table 1) for the FR version of the 23-item scale \((\alpha = 0.73)\) as compared to the MC version \((\alpha = 0.57)\). In contrast, \( \theta \) gained by the MC version \((r = −0.40, p < 0.01, \eta^2 = 0.16) \) showed a significantly higher Spearman correlation coefficient \((p < 0.01, q = 0.29)\) with average mathematics grades of the last four school reports compared to \( \theta \) gained by the FR version \((r = −0.13, p = 0.14, \eta^2 = 0.02)\). Negative correlation coefficients represent positive correlations in this case as school grades in Austria are coded contrary to \( \theta \).

**Further Results**

Exploratory analysis revealed a large significant main effect of response format \([F(1, 198) = 34.39, p < 0.001, \eta^2 = 0.15; B_{10} = 2,727,000.00] \) on the number of skipped items in a \( 2 \times 2 \) ANOVA with response format and sex as fixed factors, with more omitted items in the FR version \((M = 1.78, SD = 1.92)\) than in the MC

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**Table 1**

| Measures | \( n \) | \( \alpha \) | Women \((n = 284)\) | | | | | All \((n = 433)\) | \( \eta^2 \) |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| | | | \( M \) | \( SD \) | \( M \) | \( SD \) | \( M \) | \( SD \) | |
| FRM | 433 | | | | | | | | 0.03** |
| FRM_FR | 203 | 0.73 | 16.31 | 3.05 | 17.43 | 2.58 | 16.70 | 2.94 | |
| FRM_MC | 230 | 0.57 | 15.62 | 3.12 | 16.94 | 2.65 | 16.08 | 3.03 | 0.04** |
| DOSPERT | 376 | 0.73 | 16.92 | 2.86 | 17.86 | 2.45 | 17.24 | 2.76 | 0.02* |
| BART | 221 | 0.87a | 2.08 | 0.51 | 2.49 | 0.68 | 2.21 | 0.60 | 0.10** |
| TAI-G | 376 | 0.87 | 2.31 | 0.54 | 2.03 | 0.46 | 2.22 | 0.53 | 0.06* |
| AGE | 433 | | 16.67 | 1.31 | 16.51 | 1.08 | 16.62 | 1.24 | <0.01 |
| GRADES | 297 | 0.90 | 2.63 | 0.99 | 2.82 | 1.01 | 2.69 | 1.00 | <0.01 |

(\( \alpha \) = internal consistency parameter; \( \eta^2 \) = internal consistency for the BART is reported according to analyses of Ronay and Kim (2006).)

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*p < 0.05. **p < 0.01.
version \((M = 0.43, SD = 1.07)\). No significant main effect of sex \([F(1, 198) = 0.25, p = 0.619, \eta^2 < 0.01; B_{10} = 0.16]\) or interaction between sex and response format was found \([F(1, 198) = 0.53, p = 0.469, \eta^2 < 0.01; B_{10} = 133.386.95]\).

Significant correlations between FRM time and performance \((r = 0.41, p < 0.001)\), test anxiety \((r = −0.20, p = 0.002)\), and subjective risk propensity \((r = 0.20, p = 0.003)\) indicated that time spent on solving the FRM items was positively related to \(\theta\), lower test anxiety and higher subjective risk propensity. Males \((M = 18.78 \text{ min}, SD = 6.76)\) spent significantly more time \([F(1, 229) = 6.67, p = 0.010, \eta^2 = 0.03; B_{10} = 3.42]\) on the FRM than females \((M = 16.20 \text{ min}, SD = 7.05)\).

**DISCUSSION**

The present study was the first to systematically investigate psychometric properties and fairness of two stem-equivalent response formats of a matrices test with reference to personality characteristics. Therefore, we constructed a MC version of a FR matrices test which proved to be less prone to counting strategies than former reasoning tests. Overall, different psychometric indicators revealed a heterogeneous picture: whereas two items of the FR scale violated model fit with reference to the dichotomous model of Rasch and were removed, no items had to be dropped for the MC scale. The present data revealed the MC version as being significantly superior with reference to criterion validity, employing school grades in mathematics as external criterion as suggested by previous research (e.g., Heller et al., 1998; Pind et al., 2003). In contrast, the FR matrices items revealed higher internal consistency and EAP reliability indicators than the MC items. This result is in line with a recent report by Schult and Sparfeldt (2018) with reference to international student assessment tests. The possibility to employ strategies based on test wisdom in these kinds of items (e.g., elimination of distractors, guessing) may serve as an explanation for the somewhat lower reliability coefficients revealed for the MC items. Especially with reference to more difficult MC items, evoking more clueing strategies in certain test takers, random error and therefore reduced reliability may result. Even though item parameters of the two versions reached comparable difficulty values, some of the easier items in the FR version turned out to be more difficult in the MC version, whereas several of the most difficult items revealed as relatively easier in the MC mode, maybe caused by guessing.

As men often outperformed women in MC versions of performance tests while test takers of both sexes performed approximately equal in FR versions according to recent studies (e.g., DeMars, 1998; Stanger-Hall, 2012; Reardon et al., 2018), we hypothesized an interaction between sex and response format. According to our data, male pupils outperformed female pupils in both response formats, whereas sex and response format did not interact significantly. Previous demonstrations of interaction effects between sex and response format were based on tests measuring similar contents with non-stem equivalent items (e.g., Bridgeman and Lewis, 1994; Stanger-Hall, 2012), leading to the assumption that item and test design features, other than response format, may have induced the detected interaction effects.

Sex differences in general intelligence have been a controversial issue in psychological research for many years (see...
Arendasy and Sommer, 2012) with numerous demonstrations of men outperforming women in matrices tests (e.g., Lynn and Irving, 2004; Mackintosh and Bennett, 2005; Rosseti et al., 2009) and only a few findings of equal performances (e.g., Savage-McGlynn, 2012; Flores-Mendoza et al., 2013). As no DIF for sex was revealed in both response formats of the current study, our data aligned with previous findings of sex differences in favor of men, irrespective of response format. This result could either support Lynn’s (1994) hypothesis that men actually develop higher average intelligence than women from the age of about 15, or further item features, aside from response format, could lead to test bias. As proposed by Colom et al. (2004), the visuo-spatial format of matrices tests could be accountable for higher male performance, since men tend to achieve superior scores in spatial abilities as compared to women. Moreover, salience of item elements, i.e., the perceptual complexity of geometrical shapes (Arendasy and Sommer, 2012), as well as “stereotype threat” in terms of women automatically tending to confirm the negative stereotype that they commonly perform at an inferior level to men in certain standardized tests (Miller and Halpern, 2014), are potential factors leading to sex differences in general intelligence.

Regarding effects of personality variables on cognitive test results, neither effects of test anxiety nor of risk propensity revealed significant differences, even though interactions between these characteristics and response format have been suggested by earlier research (e.g., Rowley, 1974; Benjamin et al., 1981; Crocker and Schmitt, 1987; Alnabhan, 2002; Rubio et al., 2010). As previous studies revealed effects of subjects’ test anxiety and risk propensity on test scores particularly within high-stakes assessments (Segool et al., 2013; Knekta, 2017; Stenlund et al., 2018), aspects of the test situation (low-stakes) could have contributed to this finding. Given the small personal relevance of the test outcome for the pupils in the current study, test anxiety and risk propensity may not have influenced the subjects substantially in this test situation. Furthermore, some of the effects reported in other studies could have been influenced by test takers’ ages. Within this study, the median age of subjects was between 16 and 17 years and therefore below the age of most test takers in previous studies.

Further results revealed a significantly higher amount of omitted items in the FR version, indicating that considerably more guessing occurred in the MC mode, consistent with previous research (e.g., Bonner, 2013), possibly resulting in less valid data. The longer pupils worked on the FRM items, the higher their performance turned out to be. Interestingly, males spent significantly more time on solving the test than females. On the one hand, these results could indicate that test takers with higher ability needed more time to complete the test; on the other hand pupils with higher scores—i.e., male pupils—could have achieved higher performance by persistently trying instead of giving up at an early stage. Test takers who declared higher risk propensity—i.e., male pupils—took more time to solve the items as well, leading to the assumption that risk-taking pupils spent more time on trying to guess the correct option than risk-averse ones, as suggested by recent studies (Alnabhan, 2002; Rubio et al., 2010; Baldiga, 2013). Pupils who indicated lower test anxiety—i.e., male pupils—also spent longer time on the items, suggesting that highly test anxious subjects aimed to work their way through the test rapidly.

Psychometric advantages of the FR format could be argued due to the fact that the FR items were originally selected out of an item pool according to their properties. However, data suggest an advantage of MC items with reference to the important aspect of criterion validity. Future studies may address effects of response format on psychometric properties and fairness of matrices tests by including further relevant constructs. It seems, for example, possible, that the FR version requires more working memory capacity in order to remember the item creation rules or creativity.

DATA AVAILABILITY STATEMENT

The dataset for this study can be found in the Open Science Framework (https://osf.io/5ru9q/).

ETHICS STATEMENT

This study was carried out in accordance with the recommendations of the statutes of the University of Salzburg (part XI), Ethic Committee of the Paris Lodron University of Salzburg. All subjects gave written informed consent in accordance with the Declaration of Helsinki.

AUTHOR CONTRIBUTIONS

SB and TO conceptualized the research. SB co-developed the MC version, organized and conducted the data collection. TS and SB performed the statistical analyses. SB wrote the first draft of the manuscript. TO supervised the research, provided the theoretical input for the Introduction and Discussion sections, and revised the earlier versions of the manuscript. All authors contributed to manuscript revision, read, and approved the submitted version.

ACKNOWLEDGMENTS

We thank Bernhard Piskernik for his advice concerning the conceptualization of this research and Manuela Wagner for co-developing the MC version. We thank the Schuhfried GmbH for providing software and items of the FRM test. Furthermore, we thank Freya Gruber and Verena Eberle for their help during the data collection. Finally, we thank all teachers and pupils who agreed to take part in the research.
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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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