Active protection of a superconducting qubit with an interferometric Josephson isolator

Baleegh Abdo1, Nicholas T. Bronn1, Oblesh Jinka1, Salvatore Olivadese1, Antonio D. Córcoles1, Vivekananda P. Adiga1, Markus Brink1, Russell E. Lake2,3, Xian Wu2, David P. Pappas2 & Jerry M. Chow1

Nonreciprocal microwave devices play critical roles in high-fidelity, quantum-nondemolition (QND) measurement schemes. They impose unidirectional routing of readout signals and protect the quantum systems from unwanted noise originated by the output chain. However, cryogenic circulators and isolators are disadvantageous in scalable superconducting architectures because they use magnetic materials and strong magnetic fields. Here, we realize an active isolator formed by coupling two nondegenerate Josephson mixers in an interferometric scheme and driving them with phase-shifted, same-frequency pumps. By incorporating our Josephson-based isolator into a superconducting qubit setup, we demonstrate fast, high-fidelity, QND measurements of the qubit while providing 20 dB of protection within a bandwidth of 10 MHz against amplified noise reflected off the Josephson amplifier in the output chain. A moderate reduction of 35% is observed in $T_{2E}$ when the Josephson-based isolator is turned on. Such a moderate degradation can be mitigated by minimizing heat dissipation in the pump lines.
he capability to perform fast, high-fidelity, single-shot, quantum-nondemolition (QND) measurement of qubits is a critical requirement for the operation of quantum computers. It is needed, for instance, to readout qubits in real-time, track the evolution of quantum states, detect error syndromes, stabilize quantum states, and apply quantum feedback, as required in certain protocols. In the case of superconducting quantum processors, one prominent platform for performing QND measurements is circuit quantum electrodynamics (cQED), in which superconducting qubits are dispersively coupled to superconducting microwave readout resonators, and the qubit state is inferred by measuring the phase shift experienced by a weak near-resonance microwave signal applied to the readout resonator. To perform such fast QND measurements in the cQED architecture, several key microwave components are commonly employed, such as: (1) quantum-limited Josephson amplifiers, which enhance the signal to noise ratio of the output chain while adding minimal amount of noise to the processed signals; (2) Purcell filters, which enable qubits to be coupled to fast readout resonators while inhibiting spontaneous emission of the excitations through the resonators; and (3) non-reciprocal devices, which separate input from output and protect qubits against noise coming from the output chain. However, unlike Josephson amplifiers or Purcell filters, which are compatible with superconducting circuits, have little or no internal loss, and can be miniaturized, nonreciprocal devices, i.e., cryogenic circulators and isolators, which are widely used in state-of-the-art quantum circuits, lack these desired properties. This is primarily because they rely on magneto-optical effects to break the transmission-coefficient symmetry for light under exchanging sources and detectors, which entail using magnetic materials and strong magnetic fields.

In response to the immense challenge of eliminating these magnetic-based nonreciprocal devices, which severely hinder the scalability of superconducting quantum processors, a wide variety of viable alternative nonreciprocal schemes have been proposed and realized recently. Examples of these schemes include: Josephson traveling-wave parametric amplifiers, kinetic-inductance traveling-wave parametric amplifiers, reconﬁgurable directional amplifiers and circulators based on three-mode Josephson devices; Hall-effect-based circulators; interferometric Josephson directional ampliﬁers; circular and directional ampliﬁers that are based on nanomechanical systems; Josephson-array transmission-line isolator; SQUID-based directional ampliﬁers; or SQUID-variant devices, such as Superconducting Low-inductance Undulatory Galvanometer (SLUG) ampliﬁers; and circulators, which rely on variable inductors.

Here, we introduce a Josephson-based isolator, which is devoid of magnetic materials and strong magnets. The device is fully compatible with superconducting circuits and can be integrated on chip. It breaks reciprocity by generating artificial gauge-invariant potential for microwave photons by parametrically modulating the inductive coupling between two modes of the system and achieves unidirectional transmission of propagating signals by creating constructive and destructive wave interference between different paths in the device. The isolator has two key differences, compared to other Josephson-based, microwave-controlled circulators realized recently, it preserves the frequency of the routed quantum signals and can be operated by a single monochromatic microwave drive instead of three. These differences can result in a significant reduction in the overall control hardware resource for operating a larger number of devices. Furthermore, here we test our Josephson-based isolator in a quantum setup. More specifically, we couple it to a superconducting qubit in a fast, high-fidelity measurement setup and demonstrate that, indeed, it provides active protection to the qubit against unwanted noise coming from the output chain.

Results

Nonreciprocity mechanism. To elucidate the basic idea behind the reciprocity-breaking mechanism of our isolator, we qualitatively compare in Fig. 1 a state-of-the-art magnetic-based isolator, whose circuit symbol is shown in Fig. 1a and the Multi-Path Interferometric Josephson ISolator (MPIJIS) realized and measured in this work, whose circuit symbol is introduced in Fig. 1c. While the circuit of the magnetic-based isolator can be realized in several different ways, Fig. 1b exhibits a widely-used commercial realization, which captures the main common attributes of the device. In this realization, a two-port isolator is formed by terminating one port (e.g., port 3) of a three-port, magnetic-based circulator with a matched load (e.g., 50 Ω). As seen in Fig. 1b, the circulator consists of a microstrip metallic junction connected to the center-conductor of the equally-spaced device ports and laid down on a disk-shaped dielectric substrate, which incorporates, at its center, a smaller ferrite disk functioning as a resonant cavity. The circulator circuit also includes a permanent magnet, which induces a magnetic field in the device. As a result of the magnetic bias, the lowest-order resonant mode of the ferrite cavity splits into two modes having different frequencies and nonreciprocal azimuthal phase dependence , which is set by the direction of the applied magnetic field. By engineering the amplitude of these modes, the bias field, a superposition pattern can be generated at the circulator ports, such that microwave signals at falling between the split-resonance frequencies , propagate towards port 2 upon entering port 1, whereas signals entering 2 propagate towards the internal port 3 and dissipate their energy at the matched load.

The MPIJIS relies, in contrast, on different physics. In Fig. 1d, we depict the main components of the device. Unlike the passive magnetic-based isolator shown in Fig. 1b, the MPIJIS consists of two active Josephson mixers coupled together in an interferometric setup formed by two beam-splitters (i.e., 90° hybrids). The two Josephson mixers function as lossless frequency converters (without photon gain) between two signals having frequencies and (green) and (blue), which are supported by the resonance modes of the mixers. By construction, signals at only excite an internal mode of the system. To enable the frequency conversion, the Josephson mixers are driven by a monochromatic microwave pump at frequency . Due to the parametric modulation of the Josephson mixers, an artificial gauge-invariant potential for microwave photons is generated, which depends on the pump-phase difference . The induced potential consequently introduces a nonreciprocal phase shift for the frequency-converted signals, which is exploited in combination with wave interference (enabled by the beam-splitters) for transmitting signals in one direction, i.e., from port 1 to 2, and canceling signals in the opposite direction. Similar to the magnetic-based isolator (Fig. 1b), the canceled signals on the device port 1 are directed towards the MPIJIS internal ports 3 and 4 where they are absorbed by the matched loads.

The device. The MPIJIS realized in this work is shown in Fig. 2. In Fig. 2a, we show a black-box representation of the MPIJIS. It includes two external ports 1 and 2, which support propagating microwave signals at , which fall within the device bandwidth. The MPIJIS receives, for its operation, two monochromatic microwave pumps at , having a certain amplitude and phase difference . The pumps are fed into the MPIJIS through auxiliary ports. In the example of Fig. 2a, the MPIJIS is operated in the forward direction, i.e., propagating signals entering port 1 (input) are transmitted in the...
Almost unity transmission, while significantly attenuating signals propagating in the opposite direction. To break the transmission-coefficient symmetry between source (input) and detector (output), commercial isolators rely on magneto-optical effects, which require magnetic materials and strong magnets. One common realization of such isolators is a three-port circulator in which one of its ports (i.e., 3) is terminated by a 50 $\Omega$ load as shown in b. In this example, signals entering port 1 are directed towards port 2, whereas signals entering port 2 are dissipated in the matched load attached to the internal port 3. c A circuit symbol for the Josephson-based isolator realized and measured in this work, which is based on a different reciprocity-breaking mechanism. In this device, schematically shown in d, two active Josephson mixers are coupled via beam-splitters and driven by a microwave pump source. Unidirectional transmission from port 1 to 2 is generated by constructive and destructive wave interference between different paths in the device. The interference pattern is controlled by the phase difference $\phi = -\pi/2$ between the pumps feeding the two mixing stages. Signals propagating from port 2 to 1 are dissipated in the matched loads connected to the internal ports 3 and 4.
direction of the arrow to port 2 (output) with almost unity transmission, whereas propagating signals entering port 2 are significantly attenuated upon exiting port 1. Figure 2b exhibits a block-circuit diagram of the MPIJIS. It consists of two nominally identical Josephson parametric converters (JPCs)\textsuperscript{46,47}, which serve as lossless, nondegenerate, three-wave mixing Josephson devices as outlined in Fig. 1d. The two JPCs are embedded into an interferometric setup, which couples modes $a$ and $b$ via a 90° hybrid and a short transmission line, respectively. The pump drives are fed to the JPCs via separate physical ports (denoted as P)\textsuperscript{48}. The circuit diagram also reveals two internal ports of the device coupled to ports $b$ and terminated by 50 $\Omega$ loads. A schematic layout of the JPC is shown in Fig. 2c. It consists of two half-wavelength, microstrip resonators ‘a’ and ‘b’, which intersect at the center of a Josephson ring modulator (JRM)\textsuperscript{49}. The JRM consists of four outer-loop Josephson junctions arranged in a Wheatstone bridge configuration. The four internal Josephson junctions inductively shunt the JRM and enable the resonant frequencies $\omega_{ab}/2\pi$ of resonators ‘a’ and ‘b’ to be tuned as a function of the applied external magnetic flux $\Phi_{\text{ext}}$ threading the JRM\textsuperscript{49}. When $0 < |\Phi_{\text{ext}}| < \Phi_0$, where $\Phi_0$ is the flux quantum, the JRM acts as a dispersive nonlinear medium mixing three orthogonal modes with a leading nonlinear term in the system Hamiltonian of the form $\mathcal{H}_{\text{three}} \equiv \hbar g_{ab} (a + a^\dagger) (b + b^\dagger) (c + c^\dagger)$\textsuperscript{40}. Here, $g_{ab}$ is a flux-dependent coupling strength, $a$ and $b$ are the annihilation operators for the differential modes $a$ and $b$, while $c$ is the annihilation operator for the common mode $c$ to both resonators. Each resonator is capacitively coupled, via equal gap capacitors, to two 50 $\Omega$ feedlines, which carry incoming and outgoing signals. The photon decay rates $\kappa_{ab} = 2\pi \gamma_{\text{ph}} \simeq 40$ MHz of resonators ‘a’ and ‘b’ are primarily determined by the impedance mismatch created by the gap capacitors between the feedlines and resonators. In the MPIJIS configuration shown in Fig. 2b, resonator ‘a’ is single ended (i.e., one feedline is shorted to ground) and the pump drive is directly injected to the JRM through a separate on-chip feedline as illustrated in Fig. 2c\textsuperscript{49}. When the JPC is operated as a frequency converter between modes $a$ and $b$, a strong, coherent, off-resonant, common drive is applied at $\omega_{c} \equiv \omega_{c} = \omega_{ab} / \sqrt{2}$\textsuperscript{51,52}. With such a classical drive, we obtain in the rotating wave approximation $\mathcal{H}_{\text{three}} = \hbar g_{ab} (e^{i\phi_{ab}} a b + e^{-i\phi_{ab}} a^\dagger b^\dagger)$, where $g_{ab}$ is a pump-amplitude-dependent coupling strength and $\phi_{ab}$ is the pump phase. On resonance, the transmission amplitude associated with this frequency-conversion process is given by $t = 2\rho/(1 + \rho^2)$, where $\rho = |g_{ab}|/\sqrt{\kappa_{ab} \kappa_b}$. The transmission amplitude varies between 0 (no conversion) and 1 (full conversion). Since this process is unitary, the reflection and transmission amplitudes satisfy the condition $|t|^2 + |r|^2 = 1$. Another crucial property exhibited by $\mathcal{H}_{\text{three}}$ is the pump-phase-dependent, nonreciprocal phase shift imparted on signals undergoing upconversion from mode $a$ to $b$ ($\phi_{ab}$) versus downconversion from $b$ to $a$ ($-\phi_{ab}$). This nonreciprocal phase shift is outlined in Fig. 2d, which shows a signal flow graph for the JPC operated at a special frequency-conversion working point known as the 50:50 beam splitter point, where $r = t = 1/\sqrt{2}$. By coupling the two JPCs in an interferometric setup as shown in the block-circuit diagram depicted in Fig. 2b (or device photons exhibited in Fig. 2c, l), we convert the nonreciprocal phase shift acquired by signals transversing the two JPCs, $\pm \phi$, where $\phi \equiv \phi_{ab} - \phi_{b}$, is the phase gradient between the two pumps feeding the two mixers\textsuperscript{45}, into a nonreciprocal amplitude response via constructive or destructive wave interference between multiple paths in the device. When solving the signal flow graph for the whole device (see Supplementary Note 1 and Supplementary Figs. 1 and 2), we get, on resonance, the following transmission parameters for ports 1 and 2,

$$S_{2\rightarrow 1} = \frac{\sqrt{1 - t^2} + \sqrt{2}t^2 \sin \phi}{1 + t^2},$$

and reflection parameters,

$$S_{1\rightarrow 2} = S_{2\rightarrow 1} = -i\frac{\sqrt{2}t^2 \cos \phi}{1 + t^2}. \quad (2)$$

In the special case in which the JPCs are operated at the 50:50 beam splitter point, i.e., $t = 1/\sqrt{2}$, and the applied pump-phase difference is $\phi = -\pi/2$, we obtain, by substituting into Eqs. (1), (2), total isolation of signals transmitted from port 2 to 1, $S_{1\rightarrow 2} = 0$, and vanishing reflections off ports 1 and 2, $S_{1\rightarrow 1} = S_{2\rightarrow 2} = 0$. Whereas, for signals transmitted from port 1 to 2, we obtain almost unity transmission $|S_{2\rightarrow 1}| = 2\sqrt{2}/3 \simeq 0.94$, which is equivalent to about 0.5 dB loss in signal power. A detailed calculation of the scattering matrix of the MPIJIS as well as key measurement results, i.e., Supplementary Notes 1, 2 and Supplementary Figs. 3 and 4.

It is worth noting that the same isolator circuit presented in Fig. 2b can be used to realize a quantum-limited, phase-preserving Josephson directional amplifier, which has recently been demonstrated in refs. 33,34. One main difference between the two interferometric nonreciprocal devices, relates to the mode of operation of the coupled JPCs. Here, the JPCs are operated in the frequency-conversion mode with no photon gain\textsuperscript{46,51}, whereas in the directional amplifier application, they are operated in the nondegenerate amplification mode, where $\omega_p = \omega_{ab} + \omega_{c}$\textsuperscript{46,47,49}. As a direct consequence of this difference, the two nonreciprocal devices differ in two important aspects, namely, added noise and stability. While the phase-preserving directional amplifier is required by quantum mechanics to add noise equivalent to a half input photon at the signal frequency $n_{\text{add}} = 1/2$, the added noise by the isolator is mainly set by its power attenuation in the forward direction $|S_{2\rightarrow 1}|^2$\textsuperscript{15,16,51}. In the MPIJIS case, the added noise-equivalent-input-photons at the signal frequency is given by $n_{\text{add}} = (1 - |S_{2\rightarrow 1}|^2)/2|S_{2\rightarrow 1}|^2$ (see Supplementary Note 3). For an ideal MPIJIS, whose JPCs are joined by symmetric couplers and operated at the 50:50 beam splitter point, we obtain $n_{\text{add}} = 1/16$ (corresponding to $|S_{2\rightarrow 1}|^2 = 8/9$ on resonance). Moreover, in the directional amplifier case, the amplitude-gain of each JPC is bounded by the amplitude-attenuation of the internal mode $b$. This is to ensure the device stability in the presence of the feedback loop formed between the JPCs\textsuperscript{33,34}. Such a stability requirement is not applicable in the isolation case.

It is also worth noting that the dual operation of the present device, as a directional amplifier or an isolator (depending on the pump frequency, amplitude, and phase), is similar to other nonreciprocal Josephson devices reported recently\textsuperscript{27,29}.

The quantum setup. To demonstrate that the MPIJIS is suitable for quantum applications, we incorporate it into a high-fidelity qubit measurement setup as shown in Fig. 3. The qubit chip used in the measurement consists of two coupled transmons, but only one transmon is measured. Each qubit has its own capacitively coupled control port, which is separate from the readout resonator port used for measurement. To enable fast readout, the qubit is dispersively coupled to a relatively large bandwidth readout resonator which, in turn, is coupled to a superconducting Purcell filter integrated into the same PCB as the qubit chip (see the Methods section). The Purcell filter is added to preserve the qubit lifetime by suppressing spontaneous emission of qubit excitations through the fast resonator. The effective readout bandwidth of the combined resonator-Purcell system is $\kappa/2\pi = 6.6$ MHz. The qubit and readout frequencies are $\omega_q/2\pi = 5.3788$ GHz and $\omega_r/2\pi = 6.8405$ GHz, respectively, while the qubit-state-dependent resonance frequency shift is $\gamma/2\pi = 4.2$ MHz. Another important novelty of this qubit setup is the integration of a custom-made, wideband, superconducting directional coupler to...
Fig. 3 Rapid, high-fidelity, QND measurement setup incorporating the MPIJJS device. The setup, exhibiting only the main components, includes a two-qubit chip in which only one qubit is measured. The measured qubit is read through a single-port, fast readout resonator and controlled via a separate line, which is capacitive-coupled to the qubit. To prevent the qubit from relaxing through the readout resonator, a Purcell filter is added to the resonator port, which connects to the rest of the setup. To enable a reflective measurement of the qubit without utilizing a circulator, a broadband, on-chip directional coupler is incorporated between the Purcell filter and the readout input line. In this configuration, the readout signals input on the directional coupler port, with about 20 dB of attenuation, to the Purcell filter (and readout resonator), whereas the output readout signals reflecting off the readout resonator are transmitted, with a small insertion loss, to a MPIJJS incorporated into the output chain. Following the MPIJJS, a cryogenic circulator is used to route the readout signal to a quantum-limited Josephson amplifier working in reflection (i.e., JPC) and route the amplified reflected signal off the JPC towards the following amplification stage along the output chain, i.e., the HEMT, which is separated from the JPC circulator by two wideband cryogenic isolators, which further protect the qubit from noise coming down the output chain.

couple readout signals into and out of the readout resonator. Compared to conventional qubit setups, which utilize a circulator to measure readout resonators in reflection, using a directional coupler produces two key differences: (1) the input readout signal entering the directional coupler is attenuated by about 18 dB, which can be effectively lumped into the total attenuation of the input readout line, and (2) the directional coupler is reciprocal, therefore, does not protect the qubit against noise coming from the output chain. The main advantages of using a directional coupler over a magnetic circulator are compatibility with superconducting quantum circuits and integrability with other microwave components in the measurement scheme. Further information about the directional coupler performance, fabrication, and packaging can be found in the Methods section. Following the directional coupler, which transmits the output readout signal with minimal attenuation, we incorporate the MPIJJS and a quantum-limited Josephson amplifier (i.e., JPC), separated by a cryogenic circulator. The circulator is crucial, in this case, for three reasons: (1) it separates the weak readout signal input on the JPC from the amplified reflected output signal; (2) it preserves, to a large extent, the output signal power due to its relatively low insertion loss (\(<1 \text{ dB}\) ); and (3) it partially protects the qubit (by about 15–18 dB) against vacuum noise amplified in reflection by the JPC.

Qubit measurements. Figure 4 shows the main results of this work taken with the experimental setup of Fig. 3. Figure 4a–f outlines the six possible measurement configurations of the MPIJJS and the JPC. The graphs, displayed in the four columns, exhibit measurement results taken for each configuration, namely, normalized gain/attenuation of the MPIJJS and JPC versus frequency (first column from the left), readout fidelity histograms of the output chain extracted from the in-phase quadrature (I) of the output field corresponding to the qubit being initialized in the ground ($|g\rangle$) and excited ($|e\rangle$) states (second column), relaxation time $T_1$ (third column), and decoherence time $T_2$ echo of the qubit (fourth column). In configuration a, in which both the MPIJJS and JPC are OFF, we obtain an almost flat transmission parameter because the MPIJJS is transparent for propagating signals and the JPC is totally reflective. Using this configuration, we obtain baseline values for the readout fidelity 0.63, $T_1 = 34 \mu s$ and $T_{2E} = 22.2 \mu s$. Similar readout fidelities and coherence times are measured for this qubit in a separate cooldown when using the conventional high-fidelity setup instead, in which a cryogenic circulator and isolator replace the superconducting directional coupler and the MPIJJS, respectively (see Supplementary Note 4 and Supplementary Fig. 5). In configuration b, we operate the MPIJJS in the forward direction while keeping the JPC OFF. In this case, we observe a small dip in the transmission near resonance of about 0.7 dB, which is close to the ideal value of 0.5 dB. The observed small dip also explains the slight decrease in the readout fidelity to 0.61 (seen in the second column). While we do not observe a decrease in the qubit lifetime due to the operation of the MPIJJS as seen in the third column, we do observe about 35% reduction in $T_{2E} = 14.2 \mu s$, which we attribute to increased qubit dephasing as a result of heat dissipation in the pump lines of the MPIJJS (see Supplementary Note 5 and Supplementary Figs. 6 and 7). In configuration c, we turn off the MPIJJS and turn on the JPC with a gain of 20.7 dB at the readout frequency and a dynamical bandwidth of about 6 MHz, as shown in the first column. As expected in this quantum-limited amplification scenario, the readout fidelity is significantly enhanced $F = 0.95$. However, the enhancement in the fidelity is accompanied by a strong backaction on the qubit state, as seen in the drop of $T_1 = 23.4 \mu s$ and the significant reduction of $T_{2E} = 0.2 \mu s$ by about a factor of 100, compared to configuration a. This backaction is caused by amplified in-band quantum noise, which couples to the resonator-qubit system due to insufficient isolation (i.e., only one isolation stage is present between the qubit and JPC). Next, in configuration d, we keep the JPC ON and operate the MPIJJS in the forward direction. Remarkably, by turning on the active isolation, $T_1 = 32 \mu s$ is almost restored to the baseline-value of configuration a, while $T_{2E} = 4.3 \mu s$ is enhanced by a factor of 22 compared to configuration c (i.e., without the active isolation). Moreover, the observed enhancements in the coherence times of the qubit, compared to configuration c, are achieved without a considerable impact on the total gain 20 dB and readout fidelity $F = 0.9$. In the last two remaining configurations e and f, the MPIJJS is operated in the backward direction, which is attained in situ by shifting the pump-phase difference of the two drives by $\pi$ compared to configurations b and d. In this mode of operation, the MPIJJS effectively mimics an attenuator of about 20 dB in the path of the readout signals as seen in the first column of configuration e for which the JPC is OFF. As expected in the case of heavy attenuation of configuration e, the readout fidelity is diminished $F = 0.51$. A similar effect can also be seen in the poor
signal to noise ratio of the coherence times measurements, which have a large scatter in the data points (despite being averaged more than the other cases). In general, the coherence times measured for the backward-operated isolator $T_1 = 30.2 \mu s$, $T_{2E} = 26 \mu s$ are roughly comparable to those of the forward-operated isolator (i.e., configuration b). Finally, in configuration f, in which the JPC is ON, the amplification of the JPC almost cancels the attenuation of the MPIJIS as seen in the first column, which leads to a slight enhancement of the readout fidelity $F = 0.56$. The coherence times $T_1 = 24 \mu s$, $T_{2E} = 0.2 \mu s$, measured for this case,
are quite similar to configuration c. This is because in both cases the isolator is not shielding the qubit against excess backaction of the preamplifier (JPC).

To quantify the backaction effect on $T_{2E}$ corresponding to the different configurations, we note that because $1/T_{2E} = 1/2T_\phi + 1/T_\phi$ and $T_{2E} < 2T_\phi$, it follows that the qubit coherence time in our case is limited by dephasing, where $T_\phi$ is the dephasing time. One dominant dephasing mechanism in a qubit-resonator system operating in the dispersive coupling regime, such as ours, is photon shot noise in the resonator mode, which causes the qubit frequency to fluctuate due to the AC Stark effect. In this case, the dephasing rate $T_\phi \equiv 1/T_\phi$ is given by $T_\phi = \kappa \chi^2 / (\kappa^2 + \chi^2)$, where $\kappa$ is the average photon number in the resonator, which can be written as $\bar{n} = \bar{n}_{ba} + \bar{n}_{ab}$, where $\bar{n}_{ba}$ and $\bar{n}_{ab}$ are the average thermal and nonthermal (backaction) photon numbers, respectively. Using these relations, we can evaluate $T_\phi$, $\bar{n}_{th}$, and $\bar{n}_{ba}$, summarized in Table 1, for the different configurations a-f exhibited in Fig. 4. Note that in Table 1, we assume that excess dephasing is caused by either an increased thermal photon population in the readout resonator, due to generated heat in the pump lines feeding the MPIJIS (an experimental justification for this assumption is included in the Supplementary Information), and/or by amplified quantum noise reflecting off the JPC port and leaking into the readout resonator, as a result of insufficient isolation (backaction photons). As expected, the largest value for $\bar{n}_{ba} = 0.41$ is obtained for configurations c and f in which the JPC is ON while the MPIJIS is OFF or operated in the backward direction (i.e., in a nonprotective mode). Conversely, a significant reduction in the backaction photon number, by more than one order of magnitude 0.01, is observed when the MPIJIS is operated in the protective forward direction (i.e., configuration d).

Discussion

Based on the results of Fig. 4 and Supplementary Figs. 3, 6, and 7, there are several areas in which the performance of this proof-of-principle MPIJIS can be further improved: (1) the moderate reduction in $T_{2E}$ (of about 35%) when the isolator is ON (Fig. 4b) versus OFF (Fig. 4a). Based on the measurement results of Supplementary Figs. 6 and 7, this reduction can be attributed to increased thermal population in the readout resonator due to heat generated in the pump lines feeding the MPIJIS. Such a heating effect can be mitigated, for example, by replacing the normal-metal directional couplers incorporated into the pump lines at the base-temperature stage (shown in Supplementary Fig. 6b) with superconducting ones and/or dissipating the pump power reflecting off the MPIJIS at a higher-temperature stage; (2) the excess insertion loss observed for on-resonance transmitted signals at certain working points (as seen in Supplementary Fig. 3a,b). This excess loss, which is about 1 dB higher than the ideal-case scenario of 0.5 dB (see device theory in the Supplementary Information), suggests that the constructive interference taking place in the forward direction, for certain working points, is not optimal due to phase and amplitude imbalance of the PCB-hybrid. By substituting the present unoptimized PCB-hybrid with an optimized on-chip version, we believe this figure and the reflections off the device ports (see Supplementary Fig. 3c, d) can be significantly reduced; and (3) the relatively narrow bandwidth of the MPIJIS, which is about 10 MHz and limited by the resonator bandwidths of the JPCs. One method which could be employed to enhance the device bandwidth is impedance-engineering of the JPC feedlines. Applying such a technique in the case of single-port Josephson parametric amplifiers has successfully yielded bandwidths in the range 0.6–0.7 GHz, which correspond to more than 12-fold enhancement compared to standard designs.

Additional enhancements of the device include, (1) reducing its footprint by integrating all components on chip and using lumped-element realization of the JPCs and hybrids; (2) unifying the two external ports of the pumps, as shown in Fig. 2ef. This could be achieved by injecting a single-pump drive into the MPIJIS through an on-chip 90° hybrid whose two output ports connect to the two-stage pump lines, as proposed in ref. 45.

In conclusion, we have introduced and realized a Josephson-based isolator device, which does not rely on magnetic materials or strong magnetic fields and is fully compatible with superconducting quantum circuits. The isolator is comprised of two coupled, nondegenerate, three-wave Josephson mixers embedded in an interferometric scheme. The nonreciprocal response of the device is controlled by the phase gradient of the same-frequency microwave drives feeding the two Josephson mixers. Such a microwave-signal control could enable fast switching of the isolation direction on the fly with a time scale on the order of 15 ns, which is mainly limited by the inverse dynamical bandwidth of the device. The realized isolator exhibits isolation in excess of 20 dB, a dynamical bandwidth of 10 MHz, insertion loss of about 0.7 dB in the forward direction, signal-power reflections off its input and output ports below $-10$ dB, and a maximum input power of $-108$ dBm (see Supplementary Fig. 4). Furthermore, we have validated the applicability of this isolation scheme for quantum measurements by incorporating it into a superconducting qubit measurement setup, which includes a transmon coupled to a fast cavity, Purcell filter, custom-made, broadband, superconducting directional coupler, and a quantum-limited, Josephson parametric amplifier. Using this novel setup, we have demonstrated fast, single-shot, high-fidelity, QND measurements of the quantum state while providing active protection of the

| Table 1 Coherence and backaction comparison |
|-----------------|-----------------|----------------|-----------------|-----------------|-----------------|
| Configuration   | MPIJIS          | JPC T1 (μs)   | JPC T2 (μs)   | JPC $\phi$ (ns) | JPC $\bar{n}_{ab}$ |
| a               | OFF             | 34            | 22.2           | 32.9            | 0.003           |
| b               | OFF             | 35            | 14.2           | 17.8            | 0.005           |
| c               | OFF             | 34.4          | 0.2            | 0.2             | 0.003           |
| d               | OFF             | 32            | 4.3            | 4.6             | 0.005           |
| e               | OFF             | 30.2          | 26             | 45              | 0.002           |
| f               | OFF             | 24            | 0.2            | 0.2             | 0.002           |

Evaluated $T_\phi$, $n_{th}$, and $n_{ba}$ for the different configurations. The symbols F and B correspond to the MPIJIS operated in the forward and backward direction, respectively.
qubit against amplified noise originated by the Josephson parametric amplifier. Owing to its numerous desired properties, an optimized version of this Josephson isolator may play a pivotal role in scalable quantum architectures.

**Methods**

**Qubit measurement parameters.** The frequencies of the pumps applied to the JPC (amplifier) and MPIJS, in the measurements of Fig. 4, are 16.991 GHz and 2.784 GHz, respectively. All qubit data exhibited in Fig. 4 is taken with a readout pulse duration of $t_{\text{r}} = 200$ ns, integration time of $t_{\text{int}} = 200$ ns, and an average photon number in the readout resonator of $n = 2.1$. The qubit data are averaged over 2000 iterations. Using the expression $\tan(\theta/2) = \gamma/\Gamma$, we extract a qubit state-dependent phase shift of the readout signal of $\gamma = 64^\circ$. Furthermore, by substituting the histogram peak location $I/\alpha = 1.7$ for configuration c in Fig. 4 (in which the JPC is ON) in the relation $I/\alpha = \sqrt{2\pi\Gamma\sigma\sin(\theta/2)^2}$, we get an approximate value for the measurement efficiency of our readout chain $\eta \approx 0.3$.

**Scattering parameters of the directional coupler.** The superconducting on-chip directional coupler is realized using coupled coplanar waveguides. The characterization results of the on-chip, wideband, superconducting directional coupler are shown in Fig. 5. A circuit symbol of the directional coupler is shown in the upper-left corner of the figure, which defines the four ports of the device. The characterization measurement is done in a separate cooldown without the qubit setup, where each port of the directional coupler is connected to a three-port, cryogenic circulator with its own input and output lines. A schematic image of the directional coupler chip mounted into a 50 Ω-matched pogo-package is shown in the upper-right corner. As seen in the image, the pogo (pins) inside the package connect the four ports of the directional coupler to designated copper traces in a multilayer PCB. The four copper traces, carrying incoming and outgoing signals, connect to surface-mount SMA connectors at the periphery of the PCB, which in our case define the directional coupler ports. In Fig. 5a–d, we exhibit calibrated measurements of the 16 scattering parameters of the directional coupler in the 4–8 GHz frequency range (limited by the bandwidth of cryogenic, three-port circulators employed in the measurement). The calibration of the transmission parameters is performed using a through measurement of the various pairs of lines used in the characterization of the directional coupler. The direct connection between the different pairs of lines is changed over three consecutive cooldowns. The calibration of the reflection parameters is performed in a fourth cooldown in which the lines used in the characterization are left open ended. Figure 5a exhibits the measured magnitude of the transmission parameters $|S_{11}|^2$ (blue), $|S_{12}|^2$ (orange), $|S_{21}|^2$ (magenta), and $|S_{22}|^2$ (red). The data show that the transmission through the device is close to 0 dB in a wide bandwidth, except for a narrow window around 6.3 GHz, where the minimum transmission between ports 3 and 4 is $-4$ dB. It is worth noting that this measurement includes the insertion loss of the multilayer PCB, whose dielectric material is FR4 ($\varepsilon_r = 3.65$). Figure 5b displays the measured coupling parameters $|S_{12}|^2$ (blue), $|S_{21}|^2$ (orange), $|S_{31}|^2$ (magenta), and $|S_{41}|^2$ (red). The data show that the coupling of the device is approximately flat across the bandwidth with an average value of about $-19$ dB. Figure 5c plots the measured reflection parameters $|S_{11}|^2$ (blue), $|S_{22}|^2$ (orange), $|S_{33}|^2$ (magenta), and $|S_{44}|^2$ (red). The data show that the reflection off the device ports varies across the measurement bandwidth in the $-10$ dB to $-20$ dB range. Finally, Fig. 5d depicts the isolation parameters of the device $|S_{14}|^2$ (blue), $|S_{23}|^2$ (orange), $|S_{31}|^2$ (magenta), and $|S_{43}|^2$ (red). As seen in the figure, the isolation varies between $-25$ to $-40$ dB in the measurement bandwidth, but averages around $-30$ dB.

**Directional coupler package.** To preserve the wideband characteristics of the designed superconducting directional coupler when coupling its pads to 50 Ω PCB transmission lines, we utilize a pogo-package technology detailed in ref. 61, which provides good vertical 50 Ω impedance-matched transitions compared to traditional wirebond technology. A blow-up of the pogo-package used is shown in Fig. 6. It consists of, from bottom to top, a pedestal, an extrusion, a ground board, and an interposer. A cutout is included in the pedestal to push any chip modes to high frequency, and the chip is aligned to the two bosses on the extrusion. The ground board is made to press down on the edges for thermalization and has plating on the inside surfaces of the cutout to avoid exposed dielectric. The tolerances are adjusted such the chip protrudes slightly above the surface of the extrusion to establish positive contact with the ground board. Wirebonds are then added from the ground board to the chip ground plane and across the traces to suppress parasitic modes. The interposer is then clamped on top and spring-loaded pins with 50 Ω dielectrics are used for electrical connections$^{61}$.

**The Purcell filter.** The Purcell filter is realized using five sections of stepped impedance coplanar waveguide (CPW) transmission lines$^{14}$. The CPW sections have alternating characteristic impedances and lengths, i.e., $Z_0 = 25$ Ω of length $\ell_w = 8.5$ mm, and $Z_0 = 120$ Ω of length $\ell_w = 6.5$ mm. The Purcell filter starts and
ends with a low-impedance section. The device functions as a bandpass filter for readout frequencies spanning about 1 GHz of bandwidth around 6.3 GHz. Moreover, it suppresses signals in the frequency range 2–6 GHz. More specifically, it yields an attenuation of about 20 dB near the qubit frequency (~5.2 GHz). The Purcell filter is back-mounted into the same PCB as the qubit-resonator chip using a copper bottom cover. The qubit-resonator chip and the Purcell filter are coupled through a ~10 mm long 50 Ω stripline transmission line within the PCB.

Fabrication process. The qubit-resonator circuit is fabricated on high-resistivity silicon by mixed optical and e-beam lithography. Large features of the superconducting quantum circuit are transferred into a thin film of niobium by optical lithography and reactive ion etch. Subsequently, the Al-Al2O3-Al Josephson junctions are defined by electron beam lithography and deposited by shadow mask evaporation in a Dolan-bridge process. The directional coupler chip is fabricated with a single-layer optical lithography process using sputter-deposited Nb metal on a 3-inch, high-resistivity, float zone silicon substrate. Native oxide is removed from the substrate in situ with an Ar plasma immediately prior to deposition. The photoresist mask is then patterned on the surface of the Nb and the coplanar gaps are etched with SF6 plasma using laser-reflection endpoint detection. The photoresist mask is stripped in hot solvents. Finally, a protective coat of resist is applied before the wafer is diced into dies.

The Purcell filter is implemented using a SiN300 µm thick niobium sputtered on a 4 × 10 mm2 sapphire substrate.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Received: 10 October 2018 Accepted: 20 June 2019
Published online: 17 July 2019

References

1. Devoret, M. H. & Schoelkopf, R. J. Superconducting circuits for quantum information: an outlook. Science 339, 1169 (2013).
2. Vijay, R., Slichter, D. H. & Siddiqi, I. Observation of quantum jumps in a superconducting artificial atom. Phys. Rev. Lett. 106, 110502 (2011).
3. Hatridge, M. et al. Quantum back-action of an individual variable-strength measurement. Science 339, 178 (2013).
4. Campagne-Ibarcq, P. et al. Persistent control of a superconducting qubit by stroboscopic measurement feedback. Phys. Rev. X 3, 021008 (2013).
5. Murch, K. W., Weber, S. J., Macklin, C. & Siddiqi, I. Observing single quantum trajectories of a superconducting quantum bit. Nature 502, 211 (2013).
6. Sun, L. et al. Tracking photon jumps with repeated quantum non-demolition parity measurements. Nature 511, 444 (2014).
7. Vijay, R. et al. Stabilizing Rabi oscillations in a superconducting qubit using quantum feedback. Nature 490, 77 (2012).
8. Wang, J. & Wiseman, H. M. Feedback-stabilization of an arbitrary pure state of a two-level atom. Phys. Rev. A 64, 063810 (2001).
9. Öfek, N. et al. Extending the lifetime of a quantum bit with error correction in superconducting circuits. Nature 536, 441 (2016).
10. Ristè, D., Leewen, J. G., Ku, H.-S., Lehner, K. W. & DiCarlo, L. Initialization by measurement of a superconducting quantum bit circuit. Phys. Rev. Lett. 105, 050507 (2012).
11. Ahn, C., Doherty, A. C. & Landahl, A. J. Continuous quantum error correction via quantum feedback control. Phys. Rev. A 65, 042301 (2002).
12. Blais, A. et al. Quantum-information processing with circuit quantum electrodynamics. Phys. Rev. A. 75, 032329 (2007).
13. Murch, K. et al. Strong coupling of a single photon to a superconducting qubit using circuit quantum electrodynamics. Nature 431, 162 (2004).
14. Walter, T. et al. Rapid high-fidelity single-shot dispersive readout of superconducting qubits. Phys. Rev. Appl. 7, 054020 (2017).
15. Caves, C. M. Quantum limits on noise in linear amplifiers. Phys. Rev. D. 26, 1817 (1982).
16. Clerk, A. A., Devoret, M. H., Girvin, S. M., Marquardt, F. & Schoelkopf, R. J. Introduction to quantum noise, measurement, and amplification. Rev. Mod. Phys. 82, 1155 (2010).
17. Reed, M. D. et al. Fast reset and suppressing spontaneous emission of a superconducting qubit. Appl. Phys. Lett. 96, 203110 (2010).
18. Bronn, N. T. et al. Broadband filters for abatement of spontaneous emission in circuit quantum electrodynamics. Appl. Phys. Lett. 107, 172601 (2015).
19. Collin, R. E. Foundations for Microwave Engineering. 2nd edn (Wiley-Interscience, Hoboken, 2014).
20. Pozar, D. M. Microwave Engineering. 3rd edn (Wiley, Hoboken, 2005).
21. Barzanjeh, S. et al. Clarke, J. & Devoret, M. Noiseless non-reciprocity in a parametric active device. Nat. Phys. 7, 311 (2011).
22. Kamal, A. & Metelmann, A. Minimal Models for nonreciprocal amplification using biharmonic drives. Phys. Rev. Appl. 7, 034031 (2017).
23. Metelmann, A. & Clerk, A. A. Nonreciprocal photon transmission and amplification via reservoir engineering. Phys. Rev. X 5, 021025 (2015).
24. Murch, K. et al. A nearly quantum-limited Josephson traveling-wave parametric amplifier. Science 350, 307 (2015).
25. Zorin, A. B. Josephson traveling-wave parametric amplifier with three-wave mixing. Phys. Rev. Appl. 6, 034006 (2016).
26. Vissers, M. R. et al. Low-noise kinetic inductance traveling-wave amplifier using three-wave mixing. Appl. Phys. Lett. 100, 012601 (2016).
27. Siwa, K. et al. Reconfigurable Josephson circulator/directional amplifier. Phys. Rev. X 5, 041020 (2015).
28. Ranzani, L. & Aumentado, J. Graph-based analysis of nonreciprocity in coupled-mode systems. N. J. Phys. 17, 032024 (2015).
29. Lecoq, F. et al. Nonreciprocal microwave signal processing with a field-programmable Josephson amplifier. Phys. Rev. Appl. 7, 024028 (2017).
30. Viola, G. & DiVincenzo, D. P. Hall effect gyrators and circulators. Phys. Rev. X 4, 021019 (2014).
31. Bosco, S., Haupt, F. & DiVincenzo, D. P. Self-implemented matching easier gyrators and circulators. Phys. Rev. Appl. 7, 024030 (2017).
32. Mahoney, A. C. On-chip microwave quantum hall circulator. Phys. Rev. X 7, 011007 (2017).
33. Abdo, B. et al. Multi-path interferometric Josephson directional amplifier for qubit readout. Quantum Sci. Technol. 3, 024003 (2018).
34. Abdo, B. et al. Josephson directional amplifier for quantum measurement of superconducting circuits. Phys. Rev. Lett. 112, 167701 (2014).
35. Abdo, B., Siwa, K., Frunzio, L. & Devoret, M. H. Directional amplification with a josephson circuit. Phys. Rev. X 3, 031001 (2013).
36. Bernier, N. R. et al. Nonreciprocal reconfigurable microwave optomechanical circuit. Nat. Commun. 8, 604 (2017).
37. Barzanjeh, S. et al. Mechanical on-chip microwave circulator. Nat. Commun. 8, 953 (2017).
38. Malz, D. et al. Quantum-limited directional amplifiers with optomechanics. Phys. Rev. Lett. 120, 023601 (2018).
39. Ranzani, L. et al. Wideband isolation by frequency conversion in a Josephson-function transmission line. Phys. Rev. Appl. 8, 054035 (2017).
40. Kamal, A., Clarke, J. & Devoret, M. H. Gain, directionality, and noise in microwave SQUID amplifiers: Input-output approach. Phys. Rev. B 86, 144510 (2012).
41. Hower, D. et al. High fidelity qubit readout with the superconducting low-inductance undulatory galvanometer microwave amplifier. Appl. Phys. Lett. 104, 152601 (2014).
42. Kerckhoff, J., Lalumiere, K., Chapman, B. J., Blais, A. & Lehnert, K. W. On-chip superconducting microwave circulator from synthetic rotation. Phys. Rev. Appl. 4, 034002 (2015).
43. Fang, K., Yu, Z. & Fan, S. Photonic Aharonov-Bohm effect based on dynamic modulation. Phys. Rev. Lett. 108, 153901 (2012).
44. Fang, K., Yu, Z. & Fan, S. Experimental demonstration of a photonic Aharonov-Bohm effect at radio frequencies. Phys. Rev. B 87, 060301(R) (2013).
45. Abdo, B., Brink, M. & Chow, J. M. Gytor operation using josephson mixers. Phys. Rev. Appl. 8, 034009 (2017).
52. Flurin, E., Roch, N., Pillet, J. D., Mallet, F. & Huard, B. Superconducting
53. Sears, A. P. et al. Photon shot noise dephasing in the strong-dispersive limit of
54. Rigetti, C. et al. Superconducting qubit in a waveguide cavity with a coherence
51. Abdo, B. et al. Full coherent frequency conversion between two propagating
55. Wang, Z. et al. Cavity attenuators for superconducting qubits.
59. Pillet, J.-D., Flurin, E., Mallet, F. & Huard, B. A compact design for the
60. Lu, L.-H., Mohammadi, S., Ponchak, G. E., Bhattacharya, P. & Katehi, L. P. B.
58. Mutus, J. et al. Strong environmental coupling in a Josephson parametric
57. Roy, T. et al. Broadband parametric amplification with impedance
56. Clerk, A. A. & Utami, D. W. Using a qubit to measure photon-number
50. Roch, N. et al. Widely tunable, nondegenerate three-wave mixing microwave
49. Abdo, B., Schackert, F., Hatridge, M., Rigetti, C. & Devoret, M. Josephson
48. Abdo, B., Chavez-Garcia, J. M., Brink, M., Keefe, G. & Chow, J. M. Time-
multiplexed amplification in a hybrid-less and coil-less Josephson parametric
47. Bergeal, N. et al. Phase-preserving amplification near the quantum limit with a
46. Abdo, B., Kamal, A. & Devoret, M. H. Nondegenerate three-wave mixing with
the Josephson ring modulator. Phys. Rev. B 87, 014508 (2013).
45. Abdo, B., Chavez-Garcia, J. M., Brink, M., Keefe, G. & Chow, J. M. Time-
multiplexed amplification in a hybrid-less and coil-less Josephson parametric
44. Phys. Rev. B 86, 082601 (2017).
43. Abdo, B., Schackert, F., Hatridge, M., Rigetti, C. & Devoret, M. Josephson
amplifier for qubit readout. Appl. Phys. Lett. 99, 162506 (2011).
42. Roch, N. et al. Widely tunable, nondegenerate three-wave mixing microwave
device operating near the quantum limit. Phys. Rev. Lett. 108, 147701 (2012).
41. Abdo, B. et al. Full coherent frequency conversion between two propagating
microwave modes. Phys. Rev. Lett. 110, 173902 (2013).
40. Flurin, E., Roch, N., Pillet, J. D., Mallet, F. & Huard, B. Superconducting
quantum node for entanglement and storage of microwave radiation. Phys. Rev. Lett. 114, 090503 (2015).
39. Sears, A. P. et al. Photon shot noise dephasing in the strong-dispersive limit of
circuit QED. Phys. Rev. B 86, 180504(R) (2012).
38. Rigetti, C. et al. Superconducting qubit in a waveguide cavity with a coherence
time approaching 0.1 ms. Phys. Rev. B 86, 100506(R) (2012).
37. Wang, Z. et al. Cavity attenuators for superconducting qubits. Phys. Rev. Appl. 11, 014031 (2019).
36. Clerk, A. A. & Utami, D. W. Using a qubit to measure photon-number
statistics of a driven thermal oscillator. Phys. Rev. A 75, 042302 (2007).
35. Roy, T. et al. Broadband parametric amplification with impedance
engineering: Beyond the gain-bandwidth product. Appl. Phys. Lett. 107, 262601 (2015).
34. Mutus, J. et al. Strong environmental coupling in a Josephson parametric
amplifier. Appl. Phys. Lett. 104, 263513 (2014).
33. Pillet, J.-D., Flurin, E., Mallet, F. & Huard, B. A compact design for the
Josephson mixer: the lumped element circuit. Appl. Phys. Lett. 106, 222603 (2015).
32. Lu, L.-H., Mohammadi, S., Ponchak, G. E., Bhattacharya, P. & Katehi, L. P. B.
Design and implementation of micromachined lumped quadrature (90°)
hybrids. Microw. Symp. Dig. IEEE MTT-S Int. 2, 1285 (2001).
31. Bronn, N. T. et al. High coherence plane breaking packaging for
superconducting qubits. Quantum Sci. Technol. 3, 024007 (2018).

Acknowledgements
B.A. highly appreciates J. Rozen’s help in wiring the dilution fridge. Work pertaining to
the development of the Purcell filter was supported by IARPA under contract W911NF-
10-1-0324 and to the development of the pogo-pin packaging by IARPA under contract
W911NF-16-1-0114-FE and the NIST Quantum Measurements Initiative. Contribution
of the U.S. Government, not subject to copyright.

Author contributions
B.A. designed the isolator device, performed the experiment, and analyzed the data. N.B.
designed the Purcell filter and the PCBs, O.J. designed the device package, coils, and
mounting brackets, S.O. designed and simulated the directional coupler, A.D.C. assem-
bled the qubit measurement setup, M.B., V.P.A. and R.E.L. fabricated the devices, X.W.
performed preliminary characterization of the directional couplers, D.P.P. designed and
provided the package for the directional coupler, J.M.C. supervised the project. B.A.
acted as the principal investigator of the U.S. Government, not subject to copyright.

Competing interests: The authors declare no competing interests.

Peer review information: Nature Communications thanks the anonymous reviewer(s)
for their contribution to the peer review of this work.

Publisher’s note: Springer Nature remains neutral with regard to jurisdictional claims in
published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons
Attribution 4.0 International License, which permits use, sharing,
adaptation, distribution and reproduction in any medium or format, as long as you give
appropriate credit to the original author(s) and the source, provide a link to the Creative
Commons license, and indicate if changes were made. The images or other third party
material in this article are included in the article’s Creative Commons license, unless
indicated otherwise in a credit line to the material. If material is not included in the
article’s Creative Commons license and your intended use is not permitted by statutory
regulation or exceeds the permitted use, you will need to obtain permission directly from
the copyright holder. To view a copy of this license, visit http://creativecommons.org/
lICENSES/by/4.0/.
© The Author(s) 2019