Ground state and magnetic phase transitions of orthoferrite DyFeO$_3$

Z. Y. Zhao,$^1$ X. Zhao,$^2$[^1] H. D. Zhou,$^{3,4}$ F. B. Zhang,$^1$ Q. J. Li,$^{1,5}$ C. Fun,$^1$ X. F. Sun,$^1$[^2] and X. G. Li$^{1,6}$

$^1$Hefei National Laboratory for Physical Sciences at Microscale, University of Science and Technology of China, Hefei, Anhui 230026, People’s Republic of China

$^2$School of Physical Sciences, University of Science and Technology of China, Hefei, Anhui 230026, People’s Republic of China

$^3$Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996-1200, USA

$^4$National High Magnetic Field Laboratory, Florida State University, Tallahassee, Florida 32306-4003, USA

$^5$School of Physics and Material Science, Anhui University, Hefei, Anhui 230039, People’s Republic of China

$^6$Department of Physics, University of Science and Technology of China, Hefei, Anhui 230026, People’s Republic of China

(Dated: June 10, 2014)

Low-temperature thermal conductivity ($\kappa$), as well as magnetization ($M$) and electric polarization ($P$), of multiferroic orthoferrite DyFeO$_3$ single crystals are studied with $H \parallel c$. When the crystal is cooled in zero field, $M$, $P$, and $\kappa$ all consistently exhibit irreversible magnetic-field dependencies. In particular, with 500 mK < $T$ < 2 K, all these properties show two transitions at the first run of increasing field but only the higher-field transition is present in the subsequent field sweepings. Moreover, the ultra-low-$T$ ($T < 500$ mK) $\kappa(H)$ shows a different irreversibility and there is only one transition when the field is swept both up and down. All the results indicate a complex low-$T$ $H$–$T$ phase diagram involving successive magnetic phase transitions of the Fe$^{3+}$ spins. In particular, the ground state, obtained with cooling to subKelvin temperatures in zero field, is found to be an unexplored phase.

PACS numbers: 75.85.+t, 66.70.-f

I. INTRODUCTION

Magnetic phase transition induced by magnetic field is an outstanding phenomenon in the strongly-correlated electron systems and is associated with many physical interests, such as the unconventional superconductivity, the non-Fermi-liquid behaviors, and the multiferroicity, etc. Multiferroicity induced by spin order has attracted much attention due to its large magnetoelectric (ME) coupling. The spin-current model or the inverse Dzyaloshinsky-Moriya (DM) interaction can explain well the production of electric polarization ($P$) in the non-collinear spin systems, such as the perovskite RMnO$_3$ ($R$ = rare earth)\cite{6,7,8}. When the spins are aligned collinearly, $P$ can also be formed through the exchange striction mechanism, such as in RF$\text{FeO}_3$\cite{9,10}, Ca$_2$CoMnO$_6$\cite{11} and RM$_2$O$_5$\cite{12,13,14}. In these materials, the spin structures are playing a key role in the ME coupling and the formation of the spontaneous electric polarization. The rare-earth-based orthoferrites RF$\text{FeO}_3$ have received a lot of research interests in last several decades, particularly in the manifestations of the spin structures and spin re-orientations\cite{15,16}.

In DyFeO$_3$, the Fe$^{3+}$ moments exhibit $G_xA_yF_z$ ($F_\parallel c$) spin configuration in Bertaut’s notation\cite{20} at room temperature, that is, the main component of the magnetic moment is along the $a$ axis, accompanying with weak ferromagnetism (WFM) along the $c$ axis\cite{21,22}. Upon lowering temperature, the Fe$^{3+}$ spins undergo a Morin transition\cite{23,24} at $T_M$ = 50 K. At this transition the spin configuration changes to $A_xG_yC_z$ (FeII)\cite{24}. Moreover, with an applied magnetic field, $H > H^\text{Fe}_c$, along the $c$ axis the Fe$^{3+}$ spin configuration could change back to Fe$_x$\cite{8,24}. With further lowering temperature, the Dy$^{3+}$ spins develop a long-range antiferromagnetic (AF) order below $T^\text{N}_c$ = 4.2 K\cite{8}. In the AF state, Dy$^{3+}$ spins are confined in the $ab$ plane and the spin configuration can be expressed as $G_xA_y$ with the Ising axis deviating about 33° from the $b$ axis\cite{23,25}. The spin-induced multiferroicity was observed only at $T < T^\text{N}_c$ and when the spin flop of Fe$^{3+}$ moments is introduced by a $c$-axis field\cite{8}. Due to the interaction between Dy$^{3+}$ and Fe$^{3+}$ spins, the Dy$^{3+}$ spins shift towards the layers of Fe$^{3+}$ with opposite spin directions and far away from those with the same spin directions, resulting in a collective displacement of the Dy$^{3+}$ ions and producing a spontaneous $P$. Therefore, both the Dy$^{3+}$ and Fe$^{3+}$ spin structures are crucial for the ME phenomenon. However, the spin structure of Fe$^{3+}$ at low temperatures actually has not been determined. An obvious inconsistency in the early studies is that the Mossbauer spectroscopy suggested a $G_xG_y$ structure\cite{26} while the electric polarization results suggested a $A_xG_yC_z$ structure. Moreover, the ground state and the low-$T$ magnetic phase transitions are actually not known since all the previous works had not studied the physics of DyFeO$_3$ at temperatures lower than 1.5 K.

Heat transport has been proved to be a useful probe for the low-$T$ magnetic transitions\cite{28,35}. In this work, we study the low-$T$ thermal conductivity ($\kappa$), as well as the magnetization ($M$) and electric polarization, of DyFeO$_3$ single crystals with $H \parallel c$ after a zero field cooling (ZFC) process. In particular, the $P$ measurements can be done
at temperatures below 1 K, while the $\kappa$ is measured at temperatures down to several tens of milli-Kelvin. It is found that $M(H)$, $P(H)$, and $\kappa(H)$ all consistently exhibit peculiar low-field irreversible behaviors at $T > 500$ mK with the irreversibility field smaller than $H^*_{Fe}$. At $T < 500$ mK, $\kappa(H)$ shows a different irreversibility with larger $\kappa$ in the field-up process, which is in contrast with the case above 500 mK. The results suggest a complex low-$T$ $H - T$ phase diagram involving successive field-induced magnetic phase transitions of Fe$^{3+}$ spins.

II. EXPERIMENTS

High-quality DyFeO$_3$ single crystals were grown by a floating-zone technique in flowing oxygen-argon mixture with the ratio of 1:4. The crystals were cut precisely along the crystallographic axes after orientation by using back-reflection x-ray Laue photographs. The sample for magnetization measurement is rod-like and the dimension is $1.70 \times 0.75 \times 0.55$ mm$^3$ with the length, width and thickness along the $a$, $c$, and $a$ axis, respectively. The sample for electric polarization measurement is plate-like and the wide face is perpendicular to the $c$ axis with dimension of $2.06 \times 2.14 \times 0.13$ mm$^3$. The dimension of the sample for thermal conductivity measurement is about $2$ K/min from 300 mK to 5 K. In order to stabilize $P$($T$) was measured at a rate of about 2 K/min from 300 mK to 5 K. In order to stabilize temperature in the $P$($H$) measurements, the sweeping-field rate must be slower for lower temperature, which is 0.25, 0.2, 0.15, and 0.1 T/min at 2, 1.4, 1, and 0.7 K, respectively. Thermal conductivity was measured by using a “one heater, two thermometers” technique and three different cryostats$^{20,28}$ (i) in a $^3$He-$^4$He dilution refrigerator at temperature regime of 70 mK–1 K; (ii) in a $^3$He refrigerator at 0.3–8 K, and (iii) in a pulse-tube refrigerator for zero-field data at $T > 5$ K. In all these measurements, the magnetic fields were applied along the $c$ axis.

III. RESULTS AND DISCUSSION

A. Magnetization

The basic magnetic properties of DyFeO$_3$ are characterized by the $M$($T$) and $M$($H$) measurements, of which the representative data are shown in Fig. 1. These results are in good consistency with the earlier works.$^{8,22}$ The temperature dependence of $M$ along the $c$ axis measured in $H = 500$ Oe, shown in Fig. 1(a), has two transitions at 50 and 4.2 K. The AF order of Fe$^{3+}$ spins is known to be formed at a high temperature of $T_N^Fe \sim 645$ K, with a $G_xA_yF_z$ (Fe) spin configuration at room temperature. The transition at 50 K ($T_M$) is a Morin transition, where the Fe$^{3+}$ structure changes to $A_xG_yC_z$ (FeH).$^{22}$ Another transition at 4.2 K ($T^{AF}_N$) corresponds to the AF ordering of Dy$^{3+}$ moments in the $G_xA_y$ configuration. The low-$T$ $M$($H$) curves shown in Fig. 1(b) are consistent with these spin structures.

When the field is applied along the $c$ axis, the transition from Fe$\parallel$ to FeH shifts to lower temperature rapidly with increasing field, but the AF order of Dy$^{3+}$ is robust against the field, as seen in Fig. 1(c). It is known that

FIG. 1: (Color online) Magnetic properties of DyFeO$_3$ single crystal. (a) Magnetic susceptibility in $H = 500$ Oe along the $c$ axis. Inset: Zoom in of the low-$T$ data. The transitions at about 50 and 4.2 K correspond to the Morin transition of Fe$^{3+}$ and the Néel transition of Dy$^{3+}$, respectively. The schematics illustrate the spin structures of Fe$^{3+}$ (bottom, black) and Dy$^{3+}$ (top, blue). (b) Anisotropic magnetization at $T = 2$ K. (c) Representative data of the low-$T$ magnetic susceptibility in different magnetic fields along the $c$ axis. Inset: field dependencies of the transition temperatures of the Dy$^{3+}$ Néel order and the Fe$^{3+}$ spin re-orientation, determined from the $M$($T$) curves.
Dy\(^{3+}\) moments have strong anisotropy and are confined in the \(ab\) plane; therefore, the \(c\)-axis field can hardly change either the Néel transition or the Dy\(^{3+}\) spin orientation. Thus, the irreversible \(M(H), P(H),\) and \(\kappa(H)\) behaviors at low temperatures shown in the following sections are unambiguously related to the successive magnetic transitions of Fe\(^{3+}\) spins.

Figure 2 shows the magnetization of DyFeO\(_3\) single crystal with \(H \parallel c\) after ZFC. With \(T > T_{N}^{Dy}\), \(M\) exhibits an abrupt increase at \(H_{Fe}^{r}\), which corresponds to the spin-flop transition of Fe\(^{3+}\) moments from Fe\(_{II}\) to Fe\(_{II}\). With decreasing temperature, this transition gradually moves to higher field but becomes weaker, and finally evolves into a change of the slope (Fig. 2(a)). With \(T < T_{N}^{Dy}\), there is a lower-field transition shown by a peak at \(H_{m}\) in the differential \(dM/dH\) curves, besides the peak at \(H_{Fe}^{r}\), as shown in Figs. 2(d) and 2(g). Moreover, a peculiar irreversible \(M(H)\) behavior is observed at \(H < H_{Fe}^{r}\), with the irreversibility field slightly larger than \(H_{m}\), as shown in Figs. 2(b-g). Note that this irreversibility is repeatable at \(T > 2 K\) (Figs. 2(c) and 2(d)), which means that the field-up \(M\) for the second time (solid symbol, label 5) is identical to that for the first field-up process (open symbol, label 1). However, with \(T \leq 2 K\), the irreversibility becomes unrepeatable (Figs. 2(f) and 2(g)); that is, the field-up \(M\) for the second time is equal to that in the field-down process (open symbol, label 2). Therefore, there are two transitions in the field-up process and only the higher-field one exists when the field is swept down.

**B. Electric Polarization**

The electric polarization along the \(c\) axis of DyFeO\(_3\) single crystal is measured down to subKelvin temperatures. Figure 3(a) shows the temperature dependencies of \(P\) measured after ME cooling from 5 K to 0.3 K with magnetic field and \(E = 3\) kV/cm along the \(c\) axis. \(P\) is temperature independent at very low temperatures and decreases to zero at around \(T_{N}^{Dy}\), which indicates that the Dy\(^{3+}\) spin order contributes to this electric polarization. The magnitude of \(P\) is enhanced and the transition temperature is slightly suppressed with increasing field. Figures 3(b-e) shows the magnetic-field dependence of \(P\), measured after ME poling from 5 K in 7 T magnetic field and \(E = 3\) kV/cm along the \(c\) axis. At low fields, \(P(H)\) shows a linear ME behavior. With increasing field, the spin-flop transition of Fe\(^{3+}\) from Fe\(_{II}\) to Fe\(_{I}\) causes a change of the slope of \(P(H)\) at \(H = H_{Fe}^{r}\), and the multiferroicity shows up. These results are also in good agreement with the earlier work.\(^8\)

However, \(P(H)\) obtained with the ZFC process (cooling in zero magnetic field and electric field) shows very different behavior (Figs. 4(b-d)). First, the magnitude of \(P\) after ZFC is one or two orders smaller than that after ME poling, which is mainly due to the electric domains. Second and more importantly, an irreversible \(P(H)\) is observed in the linear ME phase. At \(T = 2 K\) (Fig. 4(b)), for example, \(P\) is zero in low fields and exhibits a step-like increase at \(H_{m} \approx 2.5\) T for the first field-up process. In higher-field, \(P(H)\) is reversible and linear with field. Note that \(H_{m}\) increases with decreasing temperature and approaches \(H_{Fe}^{r}\) at 0.7 K (Figs. 4(b-d)). When \(H > H_{Fe}^{r}\) (\(\approx 3.5\) T), the system enters the multiferroic phase due to the spin-flop transition of Fe\(^{3+}\) sublattice.\(^8\) The values of \(H_{m}\) and \(H_{Fe}^{r}\) observed from \(P(H)\) are essentially consistent with those of \(M(H)\). This consistency suggests a...
common origin for the observed irreversibility of $M(H)$ and $P(H)$.

C. Thermal Conductivity

The thermal conductivity of DyFeO$_3$ single crystal is studied for probing the magnetic transitions at even lower temperatures that our $M(H)$ and $P(H)$ measurements cannot be done.

Before presenting the heat transport results of DyFeO$_3$ crystal, we show in Fig. 5(a) the low-$T$ specific heat data. A large and sharp peak is observed at 4.1 K, which is related to the Néel transition of Dy$^{3+}$ spins. It can be seen that the magnetic contributions to the specific heat are important only at very low temperatures and are likely to be negligible above $\sim$ 12 K, where the specific heat data show a minimum. Therefore, the phonon specific heat can be estimated from the high-$T$ data in Fig. 5(a). It is known that in the temperature range $0.02 < T/\theta_D < 0.1$ ($\theta_D$ is the Debye temperature), the phonon specific heat follows a low-frequency expansion of the Debye function, $C = \beta T^4 + \beta_5 T^5 + \beta_7 T^7 + ...$, where $\beta$, $\beta_5$ and $\beta_7$ are temperature-independent coefficients. It is found that this formula fits well to the experimental data at $T > 15$ K, as shown in Fig. 5(a), with the fitting parameters $\beta = 1.28 \times 10^{-4}$ J/K$^4$mol, $\beta_5 = 2.49 \times 10^{-7}$ J/K$^5$mol and $\beta_7 = -1.75 \times 10^{-10}$ J/K$^8$mol.

Figure 5(b) shows the temperature dependencies of the thermal conductivity down to 70 mK in zero field, with the heat current $J_H$ applied along the c axis. For comparison, the data for YFeO$_3$ single crystal are also taken in the same temperature regime. Note that the Y$^{3+}$ ions are nonmagnetic and there is only AF order of Fe$^{3+}$ ions. YFeO$_3$ actually shows a simple and pure phonon heat transport phenomenon at low temperatures: (i) the $\kappa(T)$ curve exhibits a very large peak at about 20 K, with the peak value of 520 W/Km, indicating a very high quality of the single crystal; (ii) the temperature dependence of $\kappa$ is roughly $T^{2.7}$ at subKelvin temperatures, which is close to the $T^3$ boundary scattering limit of phonons. The DyFeO$_3$ data are rather comparable to those of YFeO$_3$, except for two notable differences. At first, the $\kappa$ of DyFeO$_3$ is smaller at high tempera-

![Figure 4](image_url)

FIG. 4: (Color online) Magnetic-field dependencies of the electric polarization of DyFeO$_3$ single crystal measured at (a) 2 K after ME poling and (b-d) at $2 - 0.7$ K after ZFC in $H \parallel c$. The numbers and arrows denote the sweeping-field sequences and directions. In panels (a) and (b), $H_m$ and $H_r$ indicates two transition fields and are the same as those from the magnetization.

![Figure 3](image_url)

FIG. 3: (Color online) (a) Temperature dependencies of the c-axis electric polarization of DyFeO$_3$ single crystal measured after ME poling in magnetic field and $E = 3$ kV/cm electric field, both along the c axis. (b-e) Magnetic field dependencies of $P$ measured after ME poling in 7 T and $E = 3$ kV/cm. The numbers and arrows denote the sweeping-field sequences and directions.
gradually smeared out. Apparently, the magnon spectra using the formula of phonon specific heat, that is, $C = \beta T^3$ is the phonon specific heat at low temperatures. $v_p$ is the average velocity and $l$ is the mean free path of phonons. Using the $\beta$ value obtained from the above specific-heat data, the phonon velocity can be calculated and then the mean free path is obtained from the $\kappa$. The inset to Fig. 5(b) shows the ratio between $l$ and the averaged sample width $W = 2\sqrt{A/\pi}$, where $A = 0.335$ mm. The boundary scattering limit is established.

The field dependence of thermal conductivity after ZFC is measured down to 92 mK and the results are presented in Fig. 6. With decreasing temperature, $\kappa$ exhibits complicated field dependence: (i) with $T > 2$ K, $\kappa(H)$ is reversible and shows a sharp decrease at $H_{c1}$; (ii) with $0.7$ K $\leq T \leq 2$ K, $\kappa(H)$ shows an analogous irreversible behavior; (iii) when temperature is further decreased down to below 500 mK, $\kappa(H)$ exhibits a different irreversible behavior: that is, there is only one dip in the sweeping-field run with a higher location in the field-up process. One notable feature is that the $\kappa$ in the field-up process becomes larger than that in the field-down process, which is opposite to the case above 500 mK.

It has been known from many previous studies on the antiferromagnetic materials that the thermal conductivity could exhibit drastic changes at the magnetic phase transitions or the spin re-orientations. The mechanisms are mostly due to the sudden changes in the population of the magnetic excitations, which can effectively scatter phonons. In some rare case, the magnons well populated at the spin-flop transition can also contribute to the heat transport by acting as heat carriers. In present work, the anomalies of the $\kappa(H)$ curves can be apparently attributed to the transitions of magnetic structures of DyFeO$_3$, which is also a common phenomenon to GdFeO$_3$. However, the hysteresis of $\kappa(H)$ are rather different between these two materials.

**D. Phase Diagram and Magnetic Transitions**

Considering the above experimental results, one can find a common feature for the ZFC $M(H)$, $P(H)$, and...
\( \kappa(H) \) data, that is, an irreversible behavior is observed only in the first field-up process, and it disappears in the following sweeping-field process. One possible reason for the observed irreversibility is the multi-domain effect in the multiferroic materials. Since the crystal is cooled in zero field without ME poling, at zero and low fields, the macroscopic polarization might be zero due to the compensation among different electric domains. With increasing field, the sample gradually changes into a fewer-domain state and the finite magnitude of \( P \) appears, which could be accompanied with some change in the \( M(H) \) curve. However, from our results at \( T \leq 2 \) K, the \( P(H) \) and \( M(H) \) curves are reversible in the subsequent sweeping-field process except for the first one. This is obviously different from the case of the \( P(H)/M(H) \) loop in usual ferroelectric/ferromagnetic materials, in which the loop always exists due to the presence of domains. On the other hand, if the domain effect is the major reason for the observed irreversibility, the phonon scattering by the domain walls should be effective in the whole low-\( T \) range. In the case of GdFeO\(_3\), when the crystal is cooled in zero field, the field-up \( P \) is larger than that in the field-down run, which indicates that there are less ferroelectric domains with increasing field. The larger \( \kappa(H) \) in the field-up process can be attributed to the weak phonon scattering by the domain walls. Similar to the case of GdFeO\(_3\), the \( \kappa(H) \) at \( T > 500 \) mK behaves consistently with the \( M(H) \) and \( P(H) \) curves in DyFeO\(_3\); that is, the ME domain walls are likely playing a role in scattering phonons. However, upon further cooling (\( \leq 300 \) mK) the \( \kappa \) in the field-up process becomes larger than that in the field-down process, which can not be explained by the domain wall scattering on phonons. In a word, although the multi-domain effect could have influence on the magnitudes of \( M(H) \), \( P(H) \), and \( \kappa(H) \), when the crystal is cooled without ME poling, it seems to be not the dominant factor for the observed irreversible behaviors.

The second possible reason for the step-like increase of \( P \) and the consistent low-field irreversibility shown by \( M(H) \), \( P(H) \), and \( \kappa(H) \) is the presence of an unknown zero-field magnetic structure below \( T_N^Dy \) after ZFC, which is metastable in the field and disappears when the field is swept down. Actually, it is a rather common feature of multiferroic materials that a metastable spin configuration is formed in ZFC process while another spin structure is stabilized after ME cooling. A recent example is the field-induced metastable phase in hexaferrites, observed by a neutron scattering. This scenario can easily explain the \( P(H) \) and \( M(H) \) behaviors. Due to the strong out-of-plane anisotropy of Dy\(^{3+} \) spins, the applied field along the \( c \) axis could not change their spin arrangements directly, as the magnetization in Fig. 1(c) indicated. Most likely, only the change of Fe\(^{3+} \) spin structure is involved. Therefore, the zero-field structure of Fe\(^{3+} \) at \( T < T_N^Dy \) should be different from the known Fe\(_I \) at \( T > T_N^Dy \) and is hereafter named as Fe\(_II \). It is also notable that the repeatable irreversibility begins to appear with \( T < T_N^Dy \) and becomes unrepeatable with \( T \leq 2 \) K, the transition from Fe\(_II \) to Fe\(_III \) is therefore a gradual process between \( T_N^Dy \) and 2 K. Another notable feature is that the transition from Fe\(_II \) to Fe\(_I \) at \( T > T_N^Dy \) could cause a sharp increase of \( M \). Due to the presence of irreversibility, this feature gradually vanishes at \( T < T_N^Dy \); instead, two successive magnetic transitions are present, and the higher-field one is from Fe\(_II \) to Fe\(_I \), which is the same as the case at high temperatures.

Based on the above discussions and experimental data of \( M(H) \), \( P(H) \), and \( \kappa(H) \), a low temperature \( H − T \) phase diagram with \( H \parallel c \) and in the case of ZFC is constructed, as shown in Fig. 7. We propose that be-
sides the known Fe\textsubscript{I} and Fe\textsubscript{II}, the phase diagram involves another magnetic phase, Fe\textsubscript{III}. The most important feature is that the Fe\textsuperscript{3+} spins undergo successive transitions: Fe\textsubscript{III} \rightarrow Fe\textsubscript{II} \rightarrow Fe\textsubscript{I} with increasing field and at 500 mK \(< T < T_{N}^{\text{Dy}}\), and only the transition from Fe\textsubscript{III} \rightarrow Fe\textsubscript{II} is present when the field is decreased, which is consistent with the FC results. It is known that there are four Fe\textsuperscript{3+} spin configurations that could produce linear ME response, i.e., $G_x A_y F_z$ (Fe\textsubscript{I}), $A_x G_y C_z$ (Fe\textsubscript{II}), $F_x C_y G_z$, and $C_x F_y A_z$. Since the crystal is cooled without ME poling, it is in principal difficult to judge from the electric polarization whether there is spontaneous $P$ or not in zero field, and accordingly to judge the definite magnetic structure of Fe\textsubscript{III}. This is because that the sample after ZFC could be in a multi-domain phase with spontaneous polarization, even though the measured $P$ is zero. However, since the low-$T$ $P(H)$ loops actually behave rather differently from the usual $P(H)$ hysteresis curves, some kind of magnetic-structure transition other than the multi-domain effect may play a more important role. Nevertheless, we have to leave the definition of the Fe\textsubscript{III} magnetic structure as an open question, and further investigations like neutron scattering studies on single crystals are called for.

This phase diagram could explain the behavior of $\kappa(H)$ down to the lowest temperature. (i) With $T > T_{N}^{\text{Dy}}$, when the field is applied, the Fe\textsuperscript{3+} spin structure changes from Fe\textsubscript{II} to Fe\textsubscript{I}. Accordingly, a sharp decrease of $\kappa$ is observed, due to the phonon scattering by the magnetic excitations\cite{21,32,34}. (ii) With $T \leq 2$ K, the applied field could induce successive transitions from Fe\textsubscript{III} to Fe\textsubscript{II} and then to Fe\textsubscript{I} in the field-up process, and $\kappa(H)$ shows two local maxima due to the weakened scattering of phonons across each transition. The transition from Fe\textsubscript{III} to Fe\textsubscript{II} is absent when the field is decreased, resulting in a larger $\kappa$ below $H_m$. (iii) With further cooling, $H_m$ becomes larger and there is only a first-order transition from Fe\textsubscript{II} to Fe\textsubscript{I} directly with $T < 500$ mK, which results in a different field dependence of $\kappa$. It should be noted that below 500 mK the Fe\textsubscript{II} state is always present in the sweeping-field process. This indicates that the Fe\textsubscript{II} state, which is metastable in sweeping magnetic field above 500 mK, becomes stable at $T < 500$ mK.

In passing, it should be pointed out that, besides the magnon excitations, the paramagnetic spins could also have influence on the phonon thermal conductivity\cite{38,41,42}. Due to the paramagnetic scattering effect, $\kappa(H)$ usually shows a dip-like behavior. From Figs. 6(e-j), the dip around 1 T may be ascribed to the paramagnetic scattering on phonons. The complicated field dependencies at low fields below 0.97 K and 300 mK could be regarded as a superposition of magnon scattering at $H_m$ on the recovery of $\kappa$ due to the paramagnetic scattering, as indicated by the shoulder-like feature around 2 T for both field-up and field-down processes.

FIG. 7: (Color online) ZFC $H-T$ phase diagram of DyFeO$_3$ obtained from the $M(H)$, $P(H)$, and $\kappa(H)$ data. The transition from Fe\textsubscript{III} to Fe\textsubscript{II} is actually a gradual change, as a continuous change of color indicates. Above 500 mK, Fe\textsubscript{III} is a metastable state; that is, it exits when sweeping-up field to the boundary indicated by the dashed line but does not appear when sweeping-down field. Below 500 mK, Fe\textsubscript{II} becomes stable in sweeping field. The crossed red area represents an irreversible region due to the first-order transition from Fe\textsubscript{III} to Fe\textsubscript{I}. The transition temperatures of the Néel order and the spin re-orientation for Dy\textsuperscript{3+} and Fe\textsuperscript{3+}, determined from the $M(T)$ curves (Fig. 1(c)), are also shown.

**IV. SUMMARY**

Our detailed results of magnetization, electric polarization, and thermal conductivity point to a complex magnetic phase diagram of DyFeO$_3$ involving successive field-induced magnetic phase transitions of Fe\textsuperscript{3+} spins. First, the unknown ground state at ultra-low temperatures (Fe\textsubscript{III}) is likely to have no linear ME effect. Apparently, this ground state is determined by the interaction between Dy\textsuperscript{3+} and Fe\textsuperscript{3+} spins. In particular, when the Dy\textsuperscript{3+} sublattice orders antiferromagnetically at $T_{N}^{\text{Dy}}$, the Fe\textsuperscript{3+} spins have to change their orientation. Second, with 500 mK $< T < 2$ K, a low-field irreversibility of the magnetic transitions is observed when the sample is cooled in zero field, which indicates that Fe\textsubscript{III} structure is metastable with sweeping magnetic field. A similar irreversible behavior is probably the one found in another orthoferrite TbFeO$_3$, probed by the capacitance measurement\cite{43}, in which an unknown low-field phase also disappeared with sweeping-down field. It seems that only at very low temperatures ($< 500$ mK), the interaction between Dy\textsuperscript{3+} and Fe\textsuperscript{3+} spins is strong enough to stabilize the Fe\textsubscript{III} structure. The further studies of these mate-
materials and probably other members of orthoferrite RFeO$_3$
cooled to explore their complicated low-T magnetic
structures and related interesting ME effect.

Acknowledgments

This work was supported by the National Natural
Science Foundation of China, the National Basic Re-
search Program of China (Grants No. 2009CB929502,
2011CBA00111, and 2012CB922003), and the Fundamental
Research Funds for the Central Universities (Pro-
grams No. WK2340000035 and WK2030220014).

* Electronic address: xiazhao@ustc.edu.cn
† Electronic address: xsun@ustc.edu.cn
1 B. Lake, K. Lefmann, N. B. Christensen, G. Aeppli, D. F.
McMorrow, H. M. Ronnow, P. Vorderwisch, P. Smeibidl,
N. Mankorntong, T. Sasawa, M. Nohara, and H. Takagi,
Nature Mater. 4, 658 (2005).
2 H. J. Kang, P. Dai, J. W. Lynn, M. Matsuura, J. R.
Thompson, S.-C. Zhang, D. N. Argyriou, Y. Onose, and
Y. Tokura, Nature 423, 522 (2003).
3 H. Pfau, S. Hartmann, U. Stockert, P. Sun, S. Laosberg, M.
Brandl, S. Friedemann, C. Kreller, C. Geibel, S. Wirth,
S. Kirchner, E. Abrahams, Q. Si, and F. Steglich, Nature
484, 493 (2012).
4 T. Kimura, T. Goto, H. Shintani, K. Ishizaka, T. Arima,
and Y. Tokura, Nature 426, 55 (2003).
5 H. Katsura, N. Nagaosa, and A. V. Balatsky, Phys. Rev.
Lett. 95, 057205 (2005).
6 T. Goto, T. Kimura, G. Lawes, A. P. Ramirez, and Y.
Tokura, Phys. Rev. Lett. 92, 257201 (2004).
7 T. Kimura, G. Lawes, T. Goto, Y. Tokura, and A. P.
Ramirez, Phys. Rev. B 71, 224425 (2005).
8 Y. Tokunaga, S. Iguchi, T. Arima, and Y. Tokura, Phys.
Rev. Lett. 101, 097205 (2008).
9 Y. Tokunaga, N. Furukawa, H. Sakai, Y. Taguchi, T.
Arima, and Y. Tokura, Nature Mater. 8, 558 (2009).
10 J.-H. Lee, Y. K. Jeong, J. H. Park, M.-A. Oak, H. M. Jang,
J. Y. Son, and J. F. Scott, Phys. Rev. Lett. 107, 117201
(2011).
11 Y. J. Choi, H. T. Yi, S. Lee, Q. Huang, V. Kryukhin,
and S.-W. Cheong, Phys. Rev. Lett. 100, 047601 (2008).
12 D. Higashiyama, S. Miyasaka, and Y. Tokura, Phys. Rev.
B 72, 064421 (2005).
13 M. Fukunaga, Y. Sakamoto, H. Kimura, Y. Noda, N.
Abe, K. Taniguchi, T. Arima, S. Wakimoto, M. Takeda,
K. Kakurai, and K. Kohm, Phys. Rev. Lett. 103, 077204
(2009).
14 D. Higashiyama, S. Miyasaka, N. Kida, T. Arima, and Y.
Tokura, Phys. Rev. B 70, 174405 (2004).
15 A. V. Kimel, A. Kirilyuk, A. Tsvetkov, R. V. Pisarev,
and T. Rasing, Nature 429, 850 (2004).
16 A. V. Kimel, A. Kirilyuk, P. A. Usachev, R. V. Pisarev,
A. M. Balbashov, and T. Rasing, Nature 435, 655 (2005).
17 A. V. Kimel, B. A. Ivanov, R. V. Pisarev, P. A. Usachev,
A. Kirilyuk, and T. Rasing, Nature Phys. 5, 727 (2009).
18 Y. Tokunaga, Y. Taguchi, T. Arima, and Y. Tokura,
Nature Phys. 8, 838 (2012).
19 K. Yamaguchi, T. Kurihara, Y. Minami, M. Nakajima,
and T. Suemoto, Phys. Rev. Lett. 110, 137204 (2013).
20 E. F. Bertaut, Magnetism, Vol. 3, (Academic Press, New
York, 1963).
21 A. Berton and B. Sharon, J. Appl. Phys. 39, 1367 (1968).
22 G. Gorodetsky, B. Sharon, and S. Shtrikman, J. Appl.
Phys. 39, 1371 (1968).
23 F. J. Morin, Phys. Rev. 78, 819 (1950).
24 L. A. Preloredjco, C. E. Johnson, M. F. Thomas, and B.
M. Wanklyn, J. Phys. C: Solid Stat. Phys. 13, 2567 (1980).
25 L. M. Holmes, L. G. Van Uittert, R. R. Hecker, and G. W.
Hull, Phys. Rev. B 5, 138 (1972).
26 L. M. Holmes and L. G. Van Uittert, Phys. Rev. B 5, 147
(1972).
27 M. Belakhovsky, M. Bogé, J. Chappert, and J. Sivradière,
Solid State Commun. 20, 473 (1976).
28 A. V. Sologubenko, K. Berggöld, T. Lorenz, A. Rosch, E.
Shimshoni, M. D. Phillips, and M. M. Turnbull, Phys. Rev.
Lett. 98, 107201 (2007).
29 A. V. Sologubenko, T. Lorenz, J. A. Mydosh, A. Rosch,
K. C. Shortsleeves, and M. M. Turnbull Phys. Rev. Lett.
100, 137202 (2008).
30 X. F. Sun, W. Tao, X. M. Wang, and C. Fan, Phys. Rev.
Lett. 102, 167202 (2009).
31 X. M. Wang, C. Fan, Z. Y. Zhao, W. Tao, X. G. Liu, W.
P. Ke, X. Zhao, and X. F. Sun, Phys. Rev. B 82, 094405
(2010).
32 Z. Y. Zhao, X. M. Wang, C. Fan, W. Tao, X. G. Liu, W.
P. Ke, F. B. Zhang, X. Zhao, and X. F. Sun, Phys. Rev. B
83, 014414 (2011); ibid. 89, 099903(E) (2014).
33 Z. Y. Zhao, X. M. Wang, B. Ni, Q. J. Li, C. Fan, W. P.
Ke, W. Tao, L. M. Chen, X. Zhao, and X. F. Sun, Phys.
Rev. B 83, 174518 (2011).
34 C. Fan, Z. Y. Zhao, H. D. Zhou, X. M. Wang, Q. J. Li,
F. B. Zhang, X. Zhao, and X. F. Sun, Phys. Rev. B 87,
144404 (2013).
35 F. B. Zhang, Q. J. Li, Z. Y. Zhao, C. Fan, S. J. Li, X.
G. Liu, X. Zhao, and X. F. Sun, Phys. Rev. B 89, 094403
(2014).
36 X. F. Sun, K. Segawa, and Y. Ando, Phys. Rev. Lett. 93,
107001 (2004).
37 T. Yamaguchi and K. Tsushima, Phys. Rev. B 8, 5187
(1973).
38 R. Berman, Thermal Conduction in Solids (Oxford Uni-
versity Press, Oxford, 1976).
39 A. Tari, Specific Heat of Matter at Low Temperatures
(Imperial College Press, 2003).
40 H. B. Lee, Y.-S. Song, J.-H. Chung, S. H. Chun, Y. S.
Chai, K. H. Kim, M. Reehuis, K. Prokes, and S. Mat’aˇ s,
Phys. Rev. B 83, 144425 (2011).
41 X. F. Sun, I. Tsuchada, T. Suzuki, S. Komiya, and Y.
Ando, Phys. Rev. B 72, 104501 (2005).
42 X. F. Sun, A. A. Taskin, X. Zhao, A. N. Lavrov, and Y.
Ando, Phys. Rev. B 77, 054436 (2008).
S. Artyukhin, M. Mostovoy, N. P. Jensen, D. Le, K. Prokes, V. G. de Paula, H. N. Bordallo, A. Maljuk, S. Landgesell, H. Ryll, B. Klemke, S. Paechel, K. Kiefer, K. Lefmann, L. T. Kuhn, and D. N. Argyriou, Nature Mater. 11, 694 (2012).