NUMERICAL SIMULATIONS OF RADIATIVE MAGNETIZED HERBIG–HARO JETS: THE INFLUENCE OF PRE-IONIZATION FROM X-RAYS ON EMISSION LINES

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ABSTRACT

We investigate supersonic, axisymmetric magnetohydrodynamic jets with a time-dependent injection velocity by numerical simulations with the PLUTO code. Using a comprehensive set of parameters, we explore different jet configurations in the attempt to construct models that can be directly compared to observational data of microjets. In particular, we focus our attention on the emitting properties of traveling knots and construct, at the same time, accurate line intensity ratios and surface brightness maps. Direct comparison of the resulting brightness and line intensity ratios with observational data of microjets shows that a closer match can be obtained only when the jet material is pre-ionized to some degree. A very likely source for a pre-ionized medium is photoionization by X-ray flux coming from the central object.

Keywords: Herbig–Haro objects – ISM: jets and outflows – magnetohydrodynamics (MHD) – methods: numerical – shock waves

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1. INTRODUCTION

Jets from young stellar objects (YSOs) derive their emission from gas that has been heated and compressed by shocks. In fact, the actual jet matter is invisible for most of its extension, and only the cooling zones behind the shocks emit a variety of lines that can be revealed with great accuracy and are rich sources of diagnostic indications on the post-shock physical parameters such as temperature, density, ionization fraction, and radial velocity. We refer especially to the so-called microjets like HH 30, DG Tau, and RW Aur (Bacciotti & Eisloffel 1999; Hartigan & Morse 2007; Bacciotti et al. 2002; Melnikov et al. 2009), where the line emission is limited to a region of the jet going up to about 4″–5″ from the forming star. Therefore, a careful study of shock formation and evolution is crucial to understand the physical processes at work and to constrain jet parameters that cannot be directly observed, such as the magnetic field intensity, the pre-shock density and temperature, and the jet velocity.

Radiative shocks have been studied in steady-state conditions by several authors (e.g., Cox & Raymond 1985; Hartigan et al. 1994), who derived the one-dimensional (1D) post-shock behavior of various physical parameters (temperature, ionization fraction, electron density, etc.) as functions of the distance from the shock front. More recently, Massaglia et al. (2005a) and Teşileanu et al. (2009a) have carried out 1D numerical studies of the time-dependent evolution of radiating, magnetized shocks. They have applied the results to the cases of DG Tau and HH 30, with the goal to reproduce the observed behavior of the line intensity ratios along the jet.

These studies, as discussed by Raga et al. (2007) as well, brought about the problem of the numerical resolution that is needed for a correct treatment of the post-shock region, especially as far as the reproduction of the line ratios is concerned. To solve this problem the authors have employed adaptive mesh refinement (AMR) techniques, which allow one to follow with great accuracy the sudden temperature drop behind the shock front and save computational time.

Teşileanu et al. (2009a) also discussed the influence on the results of the cooling function details. They concluded that the use of a detailed treatment of radiative emissions and ionization/recombination processes in the jet material, as well as adequate numerical resolution are very important for the reproduction of emission line ratios, which are extremely sensitive parameters. Instead, to describe the general morphology of the jet and integrated emission line luminosities, an approximation of the total radiative losses gives good results, provided the numerical resolution is sufficient to minimize numerical dissipation effects (Raga et al. 2007; Teşileanu et al. 2009).

Even though these results were obtained in the 1D limit, they can nonetheless serve as a guideline for the multidimensional case, where additional physical effects, such as rotation (Bacciotti et al. 2002), can affect the shock evolution. Teşileanu et al. (2009b) and Mignone et al. (2009) have carried out preliminary studies of the evolution of two-dimensional (2D) shocks traveling along a jet, deriving synthetic emission maps, full synthetic spectra, and position–velocity (PV) diagrams of single lines.

Previous theoretical investigations (e.g., Shull & McKee 1979) focused on stationary shock models where strong shocks were able to produce, via the UV radiation emission, the ionization of the pre-shock material, affecting the emission properties. Another approach was the one of Hartigan et al. (1987), which provided for the interpretation of observational data a set of plane-parallel shock models, including some with a totally ionized pre-shock medium, with the relative emission line fluxes. It was noticed, at that time, that large differences in the emission properties are related to the pre-ionization state of the pre-shock medium.

In this paper, we consider the axisymmetric evolution of a train of shocks as they travel along a jet, differently from Massaglia et al. (2005a) and Teşileanu et al. (2009a) who studied a single shock.

These shocks are produced by imposing a sinusoidal perturbation on the jet structure, otherwise in radial equilibrium.
with the external environment. The use of AMR allows a careful treatment of the post-shock region, providing (at the highest level of refinement) a minimum grid size corresponding to about 0.02 AU. The emissivity distribution obtained by numerical simulations with the PLUTO code (Mignone et al. 2007, 2011) is convolved with a point-spread function (PSF) similar to the one of the observing instruments for comparison with observations. As we shall see, a substantial improvement in reproducing the observed emission features can be achieved by introducing a pre-ionization of the jet material. Indeed, as recently pointed out (Güdel 2011), regions surrounding protostars are subject to the action of X-rays able to ionize jet material to an important degree, that, due to the low recombination rates, lasts up to large distances from the jet origin.

The plan of the paper is as follows. In Section 2 we discuss the initial equilibrium, perturbation, pre-ionization, and parameters and the adopted techniques to model the problem; in Section 3 we present the results for a different choice of parameters; the conclusions are drawn in Section 4.

2. THE MODEL

Our model consists of a stationary jet model with a superimposed time-dependent injection velocity that produces a chain of perturbations eventually steepening into shock waves. In what follows, the fluid density, velocity, magnetic field, and thermal pressure will be denoted, respectively, by \( \rho, \mathbf{v} = (v_r, v_\phi, v_z), \mathbf{B} = (B_r, B_\phi, B_z), \) and \( p. \) The gas pressure depends on the plasma density \( \rho, \) temperature \( T, \) and composition through the relation \( p = \rho k_B T / (\mu m_H), \) where \( \mu \) is the mean molecular weight and \( k_B \) is the Boltzmann constant. Simulations are carried out by solving the time-dependent magnetohydrodynamic (MHD) equations in cylindrical axisymmetric coordinates \( r, z: \)

\[
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0, \\
\frac{\partial (\rho v_r)}{\partial t} + \nabla \cdot (\rho \mathbf{v} \otimes \mathbf{v} - \mathbf{B} \otimes \mathbf{B}) + \frac{\partial p}{\partial r} = \frac{\rho v_r^2 - B^2_r}{r}, \\
\frac{\partial (\rho v_\phi)}{\partial t} + \nabla \cdot (\rho \mathbf{v} \otimes \mathbf{v} - r \mathbf{B} \otimes \mathbf{B}) = 0, \\
\frac{\partial (\rho v_z)}{\partial t} + \nabla \cdot (\rho \mathbf{v} \otimes \mathbf{v} - \mathbf{B} \otimes \mathbf{B}) + \frac{\partial p}{\partial z} = 0, \\
\frac{\partial B_r}{\partial t} - \frac{\partial \phi}{\partial z} = 0, \\
\frac{\partial B_\phi}{\partial t} + \frac{1}{r} \frac{\partial (r \phi)}{\partial r} = 0, \\
\frac{\partial B_z}{\partial t} + \frac{\partial \phi}{\partial z} = 0, \\
\frac{\partial E}{\partial t} + \nabla \cdot [(E + p) \mathbf{v} - \mathbf{v} \otimes \mathbf{v} \otimes \mathbf{B}] = S_E, \\
\]

where \( \rho \) is the mass density, \( \mathbf{v} = (v_r, v_\phi, v_z) \) is the velocity, \( \mathbf{B} = (B_r, B_\phi, B_z) \) is the magnetic field, \( p = p + B^2 / 2 \) denotes the total pressure, \( \mathbf{E} = -\mathbf{v} \times \mathbf{B} \) is the electric field, and \( E \) is the total energy density for an ideal gas:

\[
E = \frac{\rho}{\Gamma - 1} + \frac{\rho v^2}{2} + \frac{B^2}{2},
\]

with \( \Gamma = 5/3 \) the specific heat ratio.

The source term \( S_E \) accounts for radiative losses and is directly coupled to the ionization network described in Teșileanu et al. (2008):

\[
\frac{\partial (\rho X_{\kappa,i})}{\partial t} + \frac{1}{r} \frac{\partial (\rho X_{\kappa,i} v_r)}{\partial r} + \frac{\partial (\rho X_{\kappa,i} v_z)}{\partial z} = \rho S_{\kappa,i},
\]

where \( \kappa \) and \( i \) identify the element and its ionization stage, respectively, and \( S_{\kappa,i} \) is a source term accounting for ionization and recombination processes. Given the range of temperature and density, we include the first three ionization stages of C, O, N, Ne, S besides hydrogen and helium.

Numerical simulations have been performed in the computational domain defined by \( r \in [0, 400] \) and \( z \in [0, 1200] \) AU covered by a base grid of \( 128 \times 384 \) cells, with six additional levels of refinement with consecutive grid jump ratios of \( 2 : 2 : 4 : 2 : 2 : 2, \) thus yielding an effective resolution of \( 16,384 \times 49,152 \) cells. Computations are performed using the AMR version of the PLUTO code with the HLLC Riemann solver together the spatially and temporally second-order accurate MUSCL-Hancock scheme. See Mignone et al. (2011) for a detailed description of the code and implementation methods.

2.1. Model Parameters and Simulation Cases

A cylindrical jet equilibrium model is constructed by first prescribing radial profiles for density, velocity, and magnetic field, and then by solving the radial balance momentum equation for the gas pressure. The details of this equilibrium configuration are outlined in the Appendix.

The resulting radial profiles define a family of jet models characterized by the hydrogen number density \( n_H \), longitudinal velocity \( v_j \), temperature \( T_j \), jet to ambient density contrast \( \eta = n_H / n_a \), and peak rotation velocity \( v_\psi^{\text{max}} \). In the present context we restrict our attention to purely toroidal configurations and leave models with helical magnetic fields (i.e., \( B_\phi \neq 0 \)) to forthcoming studies. Since the ambient temperature is prescribed to be \( T_a = 1000 \) K, the maximum value of \( B_\phi \) is not a free parameter but depends on the rotation velocity. Finally, the parameter that controls the degree of pre-ionization of the jet material at the base of the jet is the X-ray luminosity \( L_X \) of the central object, for which the ionization at photoionization equilibrium is computed as explained in Section 2.3.

Along with the equilibrium magnetized models we also consider purely hydro configurations that, due to an overpressurized beam, cannot establish equilibrium with the environment. In this case, a conical structure is formed during the propagation.

In the simulations reported here we set the jet radius, initial jet temperature, velocity, and density contrast to the values \( r_j = 20 \) AU, \( T_j = 2500 \) K, \( v_j = 110 \) km s\(^{-1}\), and \( \eta = 5 \), respectively. Table 1 summarizes the chosen set of simulation cases while we plot in Figure 1 the radial profiles for density, temperature, velocity, and magnetic field. Within each set (labeled by a capital letter), the X luminosity of the central object, the period, and amplitude of the perturbation are allowed to vary.

Set \( A \) is characterized by no rotations and a relatively weak magnetic field and density. As a special case, we also include set \( AB \) consisting of purely HD 2D simulations. In these cases, the conical expansion favors the formation of a decreasing density along the longitudinal direction. Set \( B \) has stronger rotation and (consequently) magnetic field. Sets \( C \) and \( D \) are identical to \( A \) and \( B \) (respectively) except that the beam is five times heavier. Finally, the last set \( E \) has a maximum rotation velocity \( v_\psi^{\text{max}} = 15 \) km s\(^{-1}\) and peak magnetic field of 725.2 \( \mu \)G.
since the conditions in which the second and the third shock was justified by two main reasons. 

In the present work, however, a time-dependent velocity fluctuation is prescribed at the boundary (after a steady configuration has been reached) as

$$\delta v_y = A \sin \left( \frac{2\pi t}{\tau} \right),$$

where $\tau$ is the period of perturbation (in years). This choice is justified by two main reasons.

1. The formation of the pair of forward–reverse shocks elongates the high-intensity line emission area and leads to a better agreement with the morphology of the observed emission knots.

2. Our aim of approaching simulation results to observational data benefits from less strict conditions on the perturbation parameters.

Moreover, we limit ourselves to three perturbation periods since the conditions in which the second and the third shock propagate are quite similar.

### Table 1

| Set | $n_H$ | $v^\varphi_{\max}$ (km s$^{-1}$) | $B^\varphi_{\max}$ ($\mu$G) |
|-----|-------|-----------------|-----------------|
| A($L_X, \tau, \delta v$) | $10^4$ | 0 | 196.7 |
| Ab($L_X, \tau, \delta v$) | $10^4$ | 0 | ... |
| B($L_X, \tau, \delta v$) | $10^4$ | 10 | 505.2 |
| C($L_X, \tau, \delta v$) | $5 \times 10^4$ | 0 | 196.7 |
| D($L_X, \tau, \delta v$) | $5 \times 10^4$ | 10 | 505.2 |
| E($L_X, \tau, \delta v$) | $5 \times 10^4$ | 15 | 725.2 |

**Notes.** Different simulation cases are distinguished by the hydrogen density $n_H$, peak rotation velocity $v^\varphi_{\max}$, and magnetic field $B^\varphi_{\max}$, respectively, given in the second, third, and fourth column. Each set defines a family of models with varying $X$ luminosity $L_X$ of the central object, period, and amplitude of the perturbation $\tau$ and $\delta v$. In all simulation cases, the jet radius, temperature, velocity, and density contrast are the same and equal to $r_j=20$ AU, $T_j=2500$ K, $v_j=110$ km s$^{-1}$, and $\eta=5$, respectively.

### 2.3. Pre-ionization Fraction

We analyze the effect of the jet base irradiation by X-rays coming from the central T Tauri star. Our goal is not to model this region in detail, but is limited to gaining information on reasonable values of the ionization of the jet medium at the distance where observations and our simulations start, i.e., at $r_s=0.1$ corresponding to $2 \times 10^{14}$ cm. Detailed numerical calculations of the combined dynamical, heating–cooling, and photoionization processes in YSO jets are underway and will be published in a forthcoming paper.

Protostellar objects show X-ray luminosities $10^{28}$–$10^{32}$ erg s$^{-1}$, depending on their mass and possibly originating from the magnetized stellar corona (Glassgold et al. 2000; Preibisch & Neuhauser 2005), with possible contributions from the jet itself, as discussed recently by Skinner et al. (2011) for RY Tau-HH 938 and by Güdel et al. (2011) for DG Tau. The interaction of an X-ray photon, in the keV energy range, with an atom or molecule results in the production of a fast photoelectron, the primary, that in turn generates, collisionally, a deal of secondary electrons (Glassgold et al. 1997). We follow the treatment by Shang et al. (2002) that ignores the contribution of the primary electrons and considers the dominant secondary electrons only. We write the energy input $\mathcal{H}_X$ by X-rays (energy per unit volume per unit time) and the photoionization rate $\xi_X$ as

$$\mathcal{H}_X = \frac{n_H(r)}{4 \pi r^2} \int_{E_0}^{\infty} L_X(E) \sigma_{pe}(E) e^{-\xi_X} \gamma_{\text{heat}} \, dE,$$

$$\xi_X = \frac{1}{4 \pi r^2} \int_{E_0}^{\infty} \frac{L_X(E)}{\epsilon_{\text{ion}}} \sigma_{pe}(E) e^{-\xi_X} \, dE.$$

In the expression above $L_X(E)$ is the energy-dependent X-ray luminosity, $E_0(=0.1$ keV) is the low-energy cutoff, $\sigma_{pe}(E)$ is the cosmic photoelectric absorption cross section per H nucleus, $\gamma_{\text{heat}}$ is the absorbed fraction of the X-ray flux, $\epsilon_{\text{ion}}$ is the energy to make an ion pair, and $r$ is the optical path in spherical symmetry. Since $\gamma_{\text{heat}}$ and $\epsilon_{\text{ion}}$ (given by Shang et al. 2002) can be considered nearly independent of energy, we have

$$\mathcal{H}_X = n_H(r) \gamma_{\text{heat}} \epsilon_{\text{ion}} \xi_X,$$

where (Shull & van Steenberg 1985)

$$\frac{1}{\epsilon_{\text{ion}}} = \frac{\gamma_H}{I(H)} + \frac{\gamma_{\text{He}}}{I(\text{He})},$$

with

$$\gamma_H = 0.3908 \left(1 - x_e^{0.4092}\right)^{1.7592},$$

$$\gamma_{\text{He}} = 0.1516 \left(1 - x_e^{0.4092}\right)^{1.7592}.$$
\[ y_{\text{He}} = 0.0554 \left( 1 - x_e^{0.4614} \right)^{1.666}. \]

In the above relationships, \( I(H) \) and \( I(\text{He}) \) are the ionization potentials of \( \text{H} \) and \( \text{He} \), \( x_e \) is the hydrogen ionization fraction, and

\[ y_{\text{heat}} = 0.9971 \left[ 1 - (1 - x_e^{0.2663})^{1.3163} \right] \]

specifies the heating fraction.

The X-ray optical depth \( \tau_X \) can be written as

\[ \tau_X = \sigma_{\text{pe}}(k T_X)N, \quad N = \int_0^\infty n_{\text{H}} d\nu', \quad (9) \]

where \( \sigma_{\text{pe}}(E) = \sigma_{\text{pe}}(k T_X)(k eV/E)^\eta \) and \( \sigma_{\text{pe}}(1 \text{ keV}) = 2.27 \times 10^{-22} \text{ cm}^2 \). \( k T_X = 1 \text{ keV} \), and the exponent \( p = 2.485 \) is for solar abundances.

Note that for a thermal spectrum the ionization rate (Equation (6)) becomes

\[ \xi = \frac{L_X \sigma_{\text{pe}}(k T_X)}{4\pi r^2 \epsilon_{\text{ion}} \int_0^\infty \xi^{-p} \exp \left[ -(\xi + \tau_X \xi^{-p}) \right] d\xi', \quad (10) \]

where \( L_X \) is the total X-ray luminosity and \( \xi = E/k T_X \).

We consider the region close to the inner disk, where the disk-wind jet component originates, and above the extended stellar atmosphere, where the stellar-wind jet component is being launched (see the discussion in Matsakos et al. 2009). The medium there is heated and ionized by an X-ray flux of luminosity \( L_X \). This region extends from a distance \( r = R_X \sim 10^{12} \text{ cm} \) to \( 1 \text{ AU} \), the stellar corona outer radius, up to about 1 \text{ AU}, i.e., the inner disk. The radial velocities there are small enough and the ionization, recombination, heating, and cooling timescales fast enough that we can assume energetic and ionization/recombination equilibria:

\[ \mathcal{H}_X - \mathcal{L} = 0, \quad (11) \]

\[ \left( c_i + \frac{\xi X}{n_e} \right) f_n - c_i (1 - f_n) = 0, \quad (12) \]

with \( f_n \) the number fraction of neutral hydrogen atoms, \( n_e = n_{\text{H}}(1 - f_n + Z) \) the electron density, \( n_{\text{H}} \) the total hydrogen density, and \( Z = 0.001 \) the metal abundance by number, \( c_i, c_f \) are the ionization and recombination rate coefficients, respectively (see Dopita & Sutherland 2003), and \( \mathcal{L} \) represents the energy loss term (energy per unit volume per unit time). The loss term is modeled according to the SNEq cooling model by Teşileanu et al. (2009a).

If we assume a very moderate X-ray luminosity \( L_X = 10^{29} \text{ erg s}^{-1} \) and a particle density of \( 10^6 \text{ cm}^{-3} \), at \( r = R_X \) we obtain, according to Equations (11) and (12), equilibrium temperature \( \approx 12,000 \text{ K} \) and ionization fraction \( \approx 40\% \) close to the jet axis and drops to about 5% at 1 \text{ AU}, at the jet initial lateral border. The ionization/recombination timescales are of the order of months, while the heating/cooling ones are of an order of magnitude smaller. The matter is then funneled into the jet by dynamical and MHD processes, expands and accelerates reaching velocities of 100–200 km s\(^{-1}\) in a few AU’s (Zanni et al. 2007; Tzeferacos et al. 2009). One may expect a substantial drop in temperature by cooling, but the ionization fraction, due to the long recombination timescale, \( t \sim 1/c_i n_e \), would remain close to the equilibrium one. Thus, the assumption of a residual ionization fraction in the central spine of the jet of about 10%–20% at 0.1 is a quite reasonable one.

2.4. Post-processing and Data Analysis

The output from numerical simulations, which includes the chemical/ionization network and radiative cooling losses, cannot be directly compared with observations. Density, velocity, and ionization fraction distribution must be in fact transformed into surface brightness maps, line ratios, and PV diagrams in a post-processing phase.

The first step in this process is the computation of 2D emissivity maps at wavelengths corresponding to atomic transitions of interest, selected by the user. In the five-level atom model considered by the cooling treatment implemented in the PLUTO code, there are a few hundred selectable emission lines. For these computations, the ionization state of the matter and the temperature in each simulation cell must be known. The simulation code PLUTO delivers the detailed ionization state for the atomic species H, He, C, N, O, Ne, and S. The temperature is computed from the pressure, density, and ionization state in each cell.

The second step is the three-dimensional (3D) emissivity integration, in cylindrical symmetry, done by rotating the 2D emissivity maps previously obtained around the \( z \)-axis. The 3D structure is then projected onto a plane perpendicular on the line of sight (the emitted power in each emission line is integrated over lines parallel to the line of sight), in order to obtain a surface brightness map similar to the ones observed. A simulation of the effects of the PSF of the instrument is also added, the simulations usually having much higher resolutions than the observational data (in order to capture the physics within). The PSF assumes a Gaussian form, with user-defined half-width \( \sigma \). For the 2D surface brightness maps presented in this work, a PSF that is roughly 1/4 of the one of \textit{Hubble Space Telescope (HST)} was employed (HST has a resolution of approximately 0’1, that means 14 AU at the distance of Taurus-Aurigae where the sources are located). We have chosen to use this smaller PSF in order to have, at this stage, a better resolution of the output jet structures. In drawing the plots of line ratios and surface brightness along the axis of the simulated jet, the resolution was reduced to approximately that of HST.

The two steps leading from the PLUTO output data to simulated maps of surface brightness are illustrated in Figure 2.

After the second step of post-processing, a longitudinal or transversal slit of arbitrary size can be defined on the computed surface brightness map, used to compute synthetic spectra and PV diagrams. The synthetic spectra include the natural and Doppler line broadening, and consist of all emission lines selected for processing, with customizable spectral range and resolution. The resulting PV diagrams can be directly compared to the ones derived from observations. PV diagrams taken with a slit parallel to the jet axis and stepped across the jet or a slit perpendicular on the jet axis are particularly useful for simulations that include the rotation of the jet. This is expected from models of jet generation, and indications of rotation have been detected in several microjets in recent works (Bacciotti et al. 2002; Woitas et al. 2005; Coffey et al. 2004, 2007).

It is also possible to extract velocity channel maps in custom velocity channels and emission lines, to be compared with observations. These velocity channel maps are of paramount importance in the investigation of jet structure.

3. RESULTS

We discuss the results of the numerical simulations and compare these with observations of emission knots of the
three sources, for which high-quality observational data are available in the literature. The jets obtained with the numerical simulations have been projected at an angle of 45° with the line of sight, taking as a reference the case of the RW Aurigae jets.

3.1. Shocked Jet Emission

In the simulation set A, the equilibrium of a cylindrical jet is guaranteed by the toroidal component of the magnetic field vector and the density along the jet remains uniform, thus the first shock propagates in a constant density environment. In contrast, the second and the third shocks in the array travel in the decreasing density zone following the propagation of the previous shock, ensuring a longer time span for intense line emission. Indeed, following the evolution of the shocks over time, one can note the different behavior of the second shock with respect to the first one, being brighter over a larger distance.

Figure 3 shows surface brightness maps in three emission lines from [S ii], [O i], and [N ii], respectively, for a simulation type A. In this case the jet variability period is 10 years, the perturbation amplitude 50 km s$^{-1}$ and the temperature of the jet material 2500 K (hydrogen mostly neutral before the shock). We can see in this figure the sharp decrease of the brightness after the peak of about four orders of magnitude over a distance of 50 AU. This leaves large dark spaces between emission knots that are not seen in observations. We note that an attempt to alleviate this problem by diminishing the time periodicity of the perturbations that evolve in shock waves, leads to a decrease in the maximum knot brightness, explained by the lower mass flux entering each shock.

When an X-ray-induced pre-ionization of the pre-shock medium is considered (about 19% in hydrogen), Figure 4, the emission areas behind the shocks are extended compared to previous case, Figure 3 (in the figures being presented the same moment in the evolution), and the maximum values of the brightness are higher as well. This configuration provides surface brightness maps more similar to observational data, with elongated emission knots because of the higher background ratio of ionized elements in the jet material.

Moreover, the presence of pre-ionization leads to the increase in the peak surface brightness with factors between two and four. This is due to the fact that a pre-existing increased number of free electrons hasten the collisional ionization and excitation, enhancing the total brightness.

In Figure 5, we show a comparison among the simulated surface brightness of the shocked jet in [N ii] 6548 Å for four different simulation sets (A, B, C, and D from top to bottom panels), including the pre-ionization of the jet material.
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Figure 4. Simulation in A configuration, pre-ionization 19%, perturbation amplitude 50 km s\(^{-1}\), period 10 years, surface brightness in [S\(\text{ii}\)] 6716 Å (top), [O\(\text{i}\)] 6300 Å (middle), and [N\(\text{ii}\)] 6583 Å, units of erg cm\(^{-2}\) arcsec\(^{-2}\) s\(^{-1}\), log\(_{10}\) maps.

(A color version of this figure is available in the online journal.)

by X-rays. For consistency, the maps are drawn at the same evolutionary stage and the “variable” parameters were set to the same values.

The top panel shows the surface brightness map for a simulation in setup A, with rather compact emission knots and low-intensity gaps between them. The B simulation (second panel from top) includes the jet rotation with a maximum velocity of 10 km s\(^{-1}\), and produces maximum surface brightness lower than in the corresponding A cases, but with a reduced decrease in brightness in the regions between two successive emission peaks. In case C (third panel in Figure 5), the propagation of the knots is slightly faster with respect to the previous cases because of the higher density (5 \(\times\) 10\(^4\) cm\(^{-3}\) instead of 10\(^4\) cm\(^{-3}\)). In addition, the maximum value of the surface brightness is higher than in the otherwise very similar results of case A. The results of case D have been obtained by setting the jet rotation at 10 km s\(^{-1}\) and density at 5 \(\times\) 10\(^4\) cm\(^{-3}\), and from Figure 5, bottom panel, we see that the morphology of the line emission is similar to the one of case B, but with higher emission intensities due to the increased amount of mass load of the jet.

The purely hydrodynamic case Ah is characterized by a larger lateral expansion, thus both the maximum surface brightness and the length of the high-intensity zone are lower than in the corresponding MHD cases, so it was excluded from the comparison in Figure 5. The results in the E cases were very similar to the ones obtained in the D setup, thus not displayed.

3.2. Comparison with Observations

3.2.1. Observational Constraints

We refer to HST (Space Telescope Imaging Spectrograph (STIS) instrument) observations of RW Aurigae jets, Melnikov et al. (2009); for DG Tau, Bacciotti et al. (2002) and Lavalley-Fouquet et al. (2000); and for HH30, Hartigan & Morse (2007).

In Figure 6, we show the observed surface brightness along the jet axis in the three emission doublets of [O\(\text{i}\)] (6300 Å and 6363 Å), [N\(\text{ii}\)] (6548 Å and 6583 Å), and [S\(\text{ii}\)] (6716 Å and 6731 Å).
6731 Å) for the three sources quoted above. Hereafter, where no wavelength is specified, the square brackets notation refers to the sum of both lines of the respective doublet.

One can note the overall higher brightness of the three emission doublets for DG Tau, in agreement with both the higher Doppler velocities measured for this source and the presence of an X-ray emission discovered by the *Chandra Observatory* (e.g., Schneider & Schmitt 2008), as possibly indicative of stronger shock waves. Working in the approximation of an optically thin plasma, the higher values for the RW Aurigae redshifted jet with respect to HH30 jet, despite the similar flow and shock velocities, may be explained by the higher declination angle of the former with respect to the line of sight and the different toroidal magnetic field strength.

### 3.2.2. Surface Brightness

As discussed in the previous section, the surface brightness variation with distance along the jet differs depending on the case considered. Without including pre-ionization (i.e., with the ionization fraction taken in collisional equilibrium at 2500 K ahead of the shocks), the distribution of surface brightness along the jet (Figure 7) has variations of many orders of magnitude and lower peak values with respect to the pre-ionized cases (and much lower than observations).

The rotating jet simulated in configuration D is a good candidate for the comparison with observations, the decrease of brightness between the high intensity being less pronounced than in the corresponding non-rotating case (A)—see Figure 8.

An important increase in brightness is also important for the comparison with observations—shocks with higher-amplitude perturbations (higher than 50 km s\(^{-1}\)) are not likely for “slow” jets such as HH30 and RW Aur, so the pre-ionization provides a way of enhancing brightness without going with the simulations beyond the most probable parameter range.

The decreasing trend of the peak brightness with the traveled distance from the jet origin is visible both in simulations and observations: at angular distances larger than 2′, the decrease is approximately one order of magnitude (Figures 6 and 8). This suggests that the knots observed in many jets (e.g., HH 34 and HH 111) at distances of a few tens of arcseconds from the source are likely to arise from other mechanisms, i.e., jets shear-layer instabilities.

### 3.2.3. Line Emission Ratios

The line emission ratios are indispensable ingredients in methods for deriving the physical parameters of space plasmas from observations. In the case of stellar jets, the forbidden emission doublets of [S\(\text{II}\)], [O\(\text{I}\)], and [N\(\text{II}\)] between 6000 and 7000 Å are used (’BE’ technique; Bacciotti & Eislöffel 1999) for this purpose. For this reason, the comparison between the observed and simulated line ratios is a powerful method of validation for both the numerical code and the correct interpretation of observational data.

In the previous 1D analyses, we considered the emission of a single shock at different times while propagating along the jet, instead we are now taking snapshots at given times of the whole length of the jet and study the behavior of the line ratios as a function of the longitudinal coordinate. The high numerical resolution achieved thanks to the AMR technique allows us to follow not only the values in the emission peaks, but also their evolution in the post-shock zone as the gas cools. We draw in Figure 9 the results of the calculations, without...
pre-ionization, of three line ratios of forbidden lines in comparison with the observed line ratios (symbols) for the first part of the redshifted jet from the RW Aurigae pair. We see that the values of the calculated line ratios approach observations only for short distances after the shocks.

In Figures 10 and 11 we show a simulation from the $A$ and $B$ sets, respectively, with pre-ionization included. In both cases the behavior of the calculated line ratios is much more consistent with observational data, the variations between knots remaining in the observed ranges.

### 3.3. Position–Velocity Diagrams

In order to illustrate the distribution in velocities of the emitting material, the PV diagrams are widely used. A spectrum is generated for each pixel along the spectrograph slit, and the results are plotted in units of surface brightness at a certain wavelength on a PV map.

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**Figure 10.** Line ratios between the three doublets of $[\text{S}\text{ ii}]$ 6716+6731 Å, $[\text{O}\text{ i}]$ 6300+6363 Å, and $[\text{N}\text{ ii}]$ 6548+6583 Å, log10 scale plot on the jet axis from simulation type $A$ with pre-ionization and observations. (A color version of this figure is available in the online journal.)

**Figure 11.** Line ratios between the three doublets of $[\text{S}\text{ ii}]$ 6716+6731 Å, $[\text{O}\text{ i}]$ 6300+6363 Å, and $[\text{N}\text{ ii}]$ 6548+6583 Å, log10 scale plot on the jet axis from simulation type $B$ with pre-ionization and observations. (A color version of this figure is available in the online journal.)

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If Figure 12, the output from the PLUTO post-processing routines is shown. The top panel is a surface brightness map in one of the lines of the $[\text{S}\text{ ii}]$ doublet, with the user-defined slit from where the data for the PV diagram will be taken. The bottom panel displays the resulting PV diagram, in units of surface brightness. The distribution of brightness is concentrated to the right half of the image, corresponding to positive velocities, due to the declination angle between the jet axis and the line of sight. The enhanced emission knots can be clearly seen in the PV diagram, concentrating around radial velocities of $90 \text{ km s}^{-1}$.

The PV diagrams are a powerful tool in the modern study of the structure of stellar jets, providing more accurate information on the velocity distribution of the emitting material. From the differences in the radial velocity and asymmetries between opposite parts of the jet, their rotation (predicted by models) can be inferred (Coffey et al. 2007). Consequently, as both the spatial and spectral resolutions of observational data increased, these diagrams were also generated from the jet models, in order to be compared to the ones derived from observations (Cerqueira et al. 2006; Smith & Rosen 2007). Arrays of models were devised (Kajdic et al. 2006).

An interesting study underway, where PV diagrams from multiple slits will be employed, focuses on DG-Tau and RW Aurigae, in the search for rotation signatures.

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**Figure 12.** Surface brightness (top panel) with the defined slit 0.4 wide (at the distance of Taurus) and position–velocity diagram (bottom) for $[\text{S}\text{ ii}]$ 6731 Å. (A color version of this figure is available in the online journal.)

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4. CONCLUSIONS AND SUMMARY

Starting from numerical MHD simulations that include ionization network and detailed radiative cooling, we have obtained synthetic emission maps of surface brightness at various wavelengths relevant for observations of HH microjets. The comparison with observations was not limited to surface brightness (along the jet, integrated in velocity), we have also tried to match
the observed line ratios for different values of the simulation parameters.

We have shown the crucial role assumed by the pre-existing ionization in the jet medium, prior to the passage of the shock wave, for the line emission properties of the corresponding “knot.” We believe that pre-ionization will be a key ingredient in future work. This relatively high ionization fraction is likely to come from the X-ray photoionization of the atoms at the jet base, being advected away with the flow conserving its value because of the low recombination rate. The pre-ionization increases the number of free electrons in the gas and speeds up the processes of ionization and excitation at the passage of the shock wave.

Among the simulations performed during this work, the $B$ and $D$ sets, which include a toroidal magnetic field, rotation of the jet, and pre-ionization, seem to compare well with observations. Future analyses will address the problem of the contrast between the knots and intra-knots brightness, which remains higher than observed, for performing simulations aiming to reproduce in greater detail the emission features of particular objects, with the goal to constrain the jet physical parameters and better understand the physical mechanisms at work. Moreover, a challenging but potentially insightful investigation will be the 3D case that could address the shock misalignment.

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APPENDIX

RADIAL EQUILIBRIUM SOLUTION

The equilibrium solution is constructed by considering the radial force balance between pressure, magnetic, and centrifugal forces under the assumption $v_r = B = 0$. The equilibrium condition is expressed through the steady-state radial component of the momentum equation, which reads

$$dp = \frac{ρv_r^2}{r} - \frac{1}{2} \left[ \frac{1}{r^2} \frac{d(rB_θ)^2}{dr} + \frac{dB_z^2}{dr} \right]. \quad (A1)$$

In the present context, we ignore the effect of a poloidal field component and simply consider cases with $B = 0$. Density and longitudinal velocity profiles can be chosen to smoothly match their ambient values for $r > R_j$ while the azimuthal component of magnetic field is prescribed by

$$B_θ(r) = \frac{B_m}{(r/r_j)} \sqrt{1 - \exp\left[-(r/a)^2\right],} \quad (A2)$$

where $a = 0.9r_j$ is the magnetization radius and $r_j$ is the jet radius. This choice guarantees that at large radii the field becomes essentially force free whereas close to the axis the electric current $J \approx -2B_mr_j/a^2$ is approximately constant. A convenient profile for the azimuthal velocity is

$$v_θ(r) = \frac{rr_j}{a^2} \frac{2\exp\left[-(r/a)^2\right]}{ρ} \sqrt{\frac{1}{r}} \frac{d(rB_θ)^2}{dr} + \frac{dB_z^2}{dr} \right], \quad (A3)$$

where the constant $α$ sets the amount of rotation and the relative importance of the centrifugal to the Lorentz force. With these assumptions Equation (A1) can be integrated giving

$$p(r) = p_j + \frac{2}{α} \left[ a^2 \frac{B_m^2}{(r/r_j)^2} \right] \exp\left[-(r/a)^2\right], \quad (A4)$$

where $p_j$ is the jet pressure on the axis. Clearly, when $α > B_m$, the gas pressure increases monotonically with $r$ while the opposite is true for $α < B_m$. The condition $α = B_m$ yields exact balance between rotations and magnetic forces.

The actual value of $α$ can be expressed in terms of the maximum rotation velocity $v_θ^{\max}$ which, in the limit of constant density, becomes

$$α \approx v_θ^{\max} \left(\frac{a}{2r_j}\right) \frac{1}{ρ} \sqrt{\frac{r_j}{ρ_j}}. \quad (A5)$$

Finally, in order to specify the magnetic field strength $B_m$, we note that, by assigning the equilibrium ambient temperature $T_a = \frac{ρ_aμ_a}{ρ_jk_B}$ (where $ρ_a$ is the ambient density), Equation (A4) may be solved for the magnetic field strength $B_m$ giving

$$B_m^2 = α^2 + \frac{2k_B}{\pi m_a} \left(\frac{a}{r_j}\right)^2 \frac{ρ_j}{μ_j} \left(T_j - T_a/μ_a\right). \quad (A6)$$

where $k_B$ is the Boltzmann constant, $m_a$ is the atomic mass unit, $ρ_j$ is the jet density, $η = ρ_j/ρ_a$ is the jet to ambient density contrast, and $μ_j$ and $μ_a$ are the mean molecular weights in the jet and in the ambient medium, respectively. Equation (A6) immediately shows that, for $T_a < T_j$, the magnetic field has a lower threshold value and its strength always increases with rotation.

REFERENCES

Bacciotti, F., & Eisloeffel, J. 1999, A&A, 342, 717
Bacciotti, F., Ray, T. P., Mundt, R., Eisloeffel, J., & Sofi, J. 2002, ApJ, 576, 222
Cerqueira, A. H., Velázquez, P. F., Raga, A. C., Vasconcelos, M. J., & de Colle, F. 2002, ApJ, 576, 426
Coffey, D., Bacciotti, F., Ray, T. P., Eisloeffel, J., & Woitas, J. 2007, ApJ, 663, 350
Coffey, D., Bacciotti, F., Woitas, J., Ray, T. P., & Eisloeffel, J. 2004, ApJ, 604, 758
Dopita, M. A., & Sutherland, R. S. 2003, Astrophysics of the Diffuse Universe (Berlin: Springer)
Glassgold, A. E., Feigelson, E. D., & Montmerle, T. 2000, Protostars and Planets IV, ed. V. Mannings, A. P. Boss, & S. S. Russell (Tucson, AZ: Univ. Arizona Press), 429
Güdel, M. 2011, BAAS, 43, 104.05
Güdel, M., Audard, M., Bacciotti, F., et al. 2011, arXiv:1101.2700v1
Hartigan, P., & Morse, J. 2007, ApJ, 660, 426
Hartigan, P., Morse, J. A., & Raymond, J. 1994, ApJ, 436, 125
Hartigan, P., Raymond, J., & Hartmann, L. 1987, ApJ, 316, 323
Kajdic, P., Velázquez, P. F., & Raga, A. C. 2006, RevMexAA,42, 217
Lavalley-Fouquet, C., Cabrit, S., & Dougados, C. 2000, A&A, 356, L41
Lavalle-Fouquet, C., Cabrit, S., & Dougados, C. 2000, A&A, 356, L41
Massaglia, S., Mignone, A., & Bodo, G. 2005a, A&A, 442, 549
Matsakos, T., Massaglia, S., Trussoni, E., et al. 2009, A&A, 502, 217
Melnikov, S. Y., Eisloeffel, J., Bacciotti, F., Woitas, J., & Ray, T. P. 2009, A&A, 506, 763
Mignone, A., Bodo, G., Massaglia, S., et al. 2007, ApJS, 170, 228
Mignone, A., Tešileanu, O., & Zanni, C. 2009, in ASP Conf. Ser. 406, Numerical Modeling of Space Plasma Flows: ASTRONUM-2008, ed. N. V. Pogorelov, E. Audit, P. Colella, & G. P. Zank (San Francisco, CA: ASP), 105
Oliva, B., & Glassgold, A. E. 1997, ApJ, 480, 344
Güdel, M., Najita, J., & Igea, J. 1999, ApJ, 480, 344
Güdel, M., Audard, M., Bacciotti, F., et al. 2011, arXiv:1101.2700v1
Hartigan, P., & Morse, J. 2007, ApJ, 660, 426
Hartigan, P., Morse, J. A., & Raymond, J. 1994, ApJ, 436, 125
Hartigan, P., Raymond, J., & Hartmann, L. 1987, ApJ, 316, 323
Kajdic, P., Velázquez, P. F., & Raga, A. C. 2006, RevMexAA,42, 217
Lavalley-Fouquet, C., Cabrit, S., & Dougados, C. 2000, A&A, 356, L41
Massaglia, S., Mignone, A., & Bodo, G. 2005a, A&A, 442, 549
Matsakos, T., Massaglia, S., Trussoni, E., et al. 2009, A&A, 502, 217
Melnikov, S. Y., Eisloeffel, J., Bacciotti, F., Woitas, J., & Ray, T. P. 2009, A&A, 506, 763
Mignone, A., Bodo, G., Massaglia, S., et al. 2007, ApJS, 170, 228
Mignone, A., Tešileanu, O., & Zanni, C. 2009, in ASP Conf. Ser. 406, Numerical Modeling of Space Plasma Flows: ASTRONUM-2008, ed. N. V. Pogorelov, E. Audit, P. Colella, & G. P. Zank (San Francisco, CA: ASP), 105
Mignone, A., Tešileanu, O., Zanni, C., Težerac, P., et al. 2011, ApJS, in press (arXiv:1110.0740)
Preibisch, Th., & Neuhauser, R. 2005, ApJS, 160, 390
Raga, A. C., De Colle, F., Kajdić, P., Esquivel, A., & Cantó, J. 2007, A&A, 465, 879
Schneider, P. C., & Schmitt, J. H. M. M. 2008, A&A, 488, L13
Shang, H., Glassgold, A. E., Shu, F. H., & Lizano, S. 2002, ApJ, 564, 853
Shull, J. M., & McKee, C. F. 1979, ApJ, 227, 131
Shull, J. M., & van Steenberg, M. E. 1985, ApJ, 298, 268
Skinner, S. L., Audard, M., & Güdel, M. 2011, ApJ, 737, 19
Smith, M. D., & Rosen, A. 2007, MNRAS, 378, 691

Teşileanu, O., Massaglia, S., Mignone, A., Bodo, G., & Bacciotti, F. 2009a, A&A, 507, 581
Teşileanu, O., Mignone, A., & Massaglia, S. 2008, A&A, 488, 429
Teşileanu, O., Mignone, A., & Massaglia, S. 2009b, in Astrophysics and Space Science Proc., Protostellar Jets in Context, ed. T. P. Ray, K. Tsinganos, & M. Stute (Berlin: Springer), 447
Tzeferacos, P., Ferrari, A., Mignone, A., et al. 2009, MNRAS, 400, 820
Woitas, J., Bacciotti, F., Ray, T. P., et al. 2005, A&A, 432, 149
Zanni, C., Ferrari, A., Rosner, R., Bodo, G., & Massaglia, S. 2007, A&A, 469, 811