An s-d model for local and non-local spin dynamics in laser-excited magnetic heterostructures

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Abstract

We develop a joint microscopic theory for the laser-induced magnetization dynamics and spin transport in magnetic heterostructures based on the s-d interaction. Angular momentum transfer is mediated by scattering of itinerant s electrons with the localised (d electron) spins. We calculate the rate equations perturbatively and focus on a spin one-half d electron system. We find an analytical expression for the dynamics of the local magnetization that is coupled to an equation for the non-equilibrium spin accumulation of the s electrons, which converges to the microscopic three-temperature model in the limit of a strong s-d coupling. The equation for the spin accumulation is used to introduce diffusive spin transport. The presented numerical solutions show that during the laser-induced demagnetization in a ferromagnetic metal a short-lived spin accumulation is created that counteracts the demagnetization process. Moreover, the spin accumulation leads to the generation of a spin current at the interface of a ferromagnetic and non-magnetic metal. Depending on the specific magnetic system, both local spin dissipation and interfacial spin transport are able to enhance the demagnetization rate by providing relaxation channels for the spin accumulation that is build up during demagnetization in the ferromagnetic material.
I. INTRODUCTION

Exciting magnetic systems with ultrashort laser pulses gives rise to fascinating physics. First, it was shown that a femtosecond laser pulse can quench the magnetization of a ferromagnetic thin-film on a subpicosecond timescale [1]. Later, all-optical magnetization switching was discovered in GdFeCo alloys [2], which proved the high potential of using ultrashort laser pulses for future data writing technologies. Moreover, it was demonstrated that the laser pulse generates a spin current [3, 4]. In non-collinear magnetic heterostructures the ultrafast generated spin current exerts a spin-transfer torque [5, 6], leading to the excitation of Terahertz standing spin waves [7, 8]. Understanding all these ultrafast phenomena paves the way towards faster magnetic data technologies, and bridges the boundaries between photonics, spintronics and magnonics.

Despite the vast experimental developments within the field, the microscopic origin of the observed demagnetization rates is still heavily debated. Various microscopic processes have been proposed as being the dominant mechanism, such as (i) the coherent interaction between the photons and the spins [9, 10], (ii) spin-dependent transport of hot electrons [11], and (iii) local spin dynamics as triggered by laser heating or excitation [1, 12–20]. In the latter case, the models often rely on the assumption that heating of the electrons increases the amount of spin-flip scattering events, resulting in the transfer of angular momentum. An example of this type of models is the microscopic three-temperature model (M3TM) [15], where it is assumed that the magnetization dynamics is dominated by Elliott-Yafet electron-phonon scattering. Arguably, other types of scattering mechanisms can also account for the observed demagnetizations rates, such as Elliott-Yafet electron-electron scattering [14] and electron-magnon scattering [18]. The latter stems from the $s$-$d$ interaction in ferromagnetic transition metals, that couples the local magnetic moments ($d$ electrons) and free carriers ($s$ electrons). Similar models were derived to describe the ultrafast magnetization dynamics in semiconductors [21] and ferrimagnetic alloys [22].

Another important question is what mechanism drives the optically induced spin currents in magnetic heterostructures. First, it could be directly related to the proposed superdiffusive spin currents created in the magnetic material [11, 23]. Secondly, the laser-induced thermal gradients can generate a spin current resulting from the spin-dependent Seebeck effect [24, 25]. Recently, it was proposed that the spin-polarized electrons are generated at
a rate given by the temporal derivative of the magnetization \cite{5}. Interestingly, this implies that the demagnetization and the generated spin current are driven by the same physical mechanism. The \textit{s-d} interaction, which mediates angular momentum transfer between the local magnetic moments and itinerant electrons, is a principal candidate \cite{5,18,26}.

In this work, we present a model for laser-induced magnetization dynamics including spin transport based on the \textit{s-d} interaction. The model describes that during demagnetization an out-of-equilibrium spin accumulation is created in the \textit{s} electron system, which leads to the generation of a spin current in magnetic heterostructures. The numerical solutions of the rate equations that we derive show a qualitative agreement with the experiments and suggest that indeed the \textit{s-d} interaction could be the main driving force of the observed ultrafast phenomena. Furthermore, the crucial role of the spin accumulation is emphasized, namely (i) the generated spin accumulation has a negative feedback on the demagnetization process and (ii) this bottleneck can be removed by either local spin-flip processes or by electron spin transport. Hence, both local and non-local processes play a crucial role in the magnetization dynamics. Finally, we discuss the limit in which the newly presented model becomes equivalent to the M3TM, and we conclude with an outlook.

We start with the derivation of the model in Section II. In Section III, we model the demagnetization experiments and discuss the role of the spin accumulation. We describe the laser-induced dynamics in a collinear magnetic heterostructure in Section IV. We explain how the different demagnetization rates of the parallel and anti-parallel configuration can be understood from the presented theory. In Section V, we describe a bilayer consisting of a ferromagnetic and non-magnetic metallic layer. Here, we introduce diffusive spin transport. We investigate the role of the layer thickness on the magnetization dynamics and we analyse the temporal profile of the injected spin current in the non-magnetic layer.

II. MODEL

Analogous to Ref. \cite{18}, we define the ferromagnetic transition metal in terms of two separate electronic systems, corresponding to the \textit{3d} and \textit{4s} electrons. A schematic overview of the model is presented in Fig. 1(a). The \textit{d} electrons are the main contributor to the magnetic properties of the system and are relatively localised. Therefore, we approximate the \textit{d} electron system as a lattice of localised spins. At each lattice site there is only one spin
and the atomic magnetic moment is given by $\mu_{at} = 2S \mu_B$, where $\mu_B$ is the Bohr magneton and $S$ is the spin quantum number. We neglect the orbital angular momentum.

In this work, we describe the localised spin system within a Weiss mean field approach, similar to the description used in the M3TM \cite{15}. The Hamiltonian of the $d$ electrons is expressed as

$$\hat{H}_d = \Delta \sum_j \hat{S}^d_{j,z},$$

where $\hat{S}^d_{j,z}$ is the $z$ component of the spin at lattice site $j$ and $\Delta$ is the exchange splitting. Hence, each spin corresponds to a system of $2S + 1$ energy levels splitted by energy $\Delta$.

The $s$ electrons are described as a free electron gas. They are coupled to the localised spins through the on-site $s$-$d$ interaction, given by

$$\hat{H}_{sd} = J_{sd} \sum_j \hat{S}^d_{j} \cdot \hat{s}(r_j).$$

Here, $J_{sd}$ is the $s$-$d$ exchange coupling constant, $V_{at}$ is the atomic volume, $\hat{S}^d_{j}$ is the spin operator of the spin at lattice site $j$, and $\hat{s}(r_j)$ is the spin density operator of the $s$ electrons at position $r_j$ of lattice site $j$.

We express $\hat{s}(r_j)$ in terms of the electron creation and annihilation operators in momentum space. Now we have

$$\hat{H}_{sd} = \sum_j \sum_{kk'} \left[ J^s_{jkk'} c^\dagger_{k\uparrow} c_{k\downarrow} \hat{S}^{d+}_{j} + \text{h.c.} \right],$$

where the coupling strength is parametrized by the matrix element $J^s_{jkk'}$. $\hat{S}^{d+}_{j}$ corresponds to the spin ladder operator for the spin at lattice site $j$. The operator $c^\dagger_{k\sigma}$ ($c_{k\sigma}$) creates (annihilates) an $s$ electron with momentum $k$ and spin $\sigma$. In the transition from Eq. (2) to Eq. (3) the terms proportional to the $z$ components are omitted and rewritten in terms of a mean-field energy shift in the Hamiltonian for the $s$ electrons \cite{18}. The similar energy shift in the $d$ electron system (a shift of $\Delta$) plays a minor role and is neglected.

Equation (3) describes the spin-flip scattering of $s$ electrons with the localised spins, which mediates angular momentum transfer between the $s$ and $d$ electron systems, but conserves
Figure 1. Schematic overview of the model. (a) The system is divided into a subsystem of localised 3d electrons and itinerant 4s electrons. The laser pulse heats up the s electrons. Angular momentum is transferred between the s and d subsystems by the s-d interaction. Secondly, angular momentum can dissipate out of the combined system by additional spin-flip processes in the s system, e.g., Elliott-Yafet electron-phonon scattering. Figures (b)-(d) schematically show the occupation of the energy levels in the d and s subsystems during the laser heating (for $S = 1/2$). Figure (b) indicates the ground state ($T_e = 0$ K). Figure (c) shows that the broadening of the Fermi-Dirac distribution allows spin-flip transitions around the Fermi level. This process is accompanied by a spin-flip of a local d spin. The s electrons thermalize rapidly and a non-zero spin accumulation $\mu_s$ is created, as is indicated in Fig. (d).

the total angular momentum. Hence, these scattering events change the total spin in the $z$ direction of the d electron system. To calculate the resulting magnetization dynamics, we apply perturbation theory using the density matrix formalism. We only show the most important steps, for more details we refer to Ref. [21], where an equivalent calculation is presented for semiconductors. In contrast to Ref. [21], our system does include a direct (d-d) exchange interaction between the localised spins, as represented by Eq. [1].

First, we assume that the density matrix of the complete system can be factorized in terms of a density matrix $\hat{\rho}^C$ for the carriers (s electrons) and $\hat{\rho}^S$ for the localised spins (d electrons). Secondly, we assume that after excitation there is no coherence between the spins. In other words, the time scale at which the spins dephase is the shortest time scale
within the system, such that the density matrix \( \hat{\rho}^S \) is diagonal. The diagonal elements of \( \hat{\rho}^S \) are given by the occupation numbers \( \rho_{m_s}^S = f_{m_s} \) for each energy level \( m_s \) of a single spin, where \( m_s \) corresponds to the \( z \) component of the spin. In this Boltzmann approach, the ensemble average of the spin in the \( z \) direction is given by \( \langle \hat{S}^{d,z} \rangle = \sum_{m_s=-S}^{S} m_s f_{m_s} \).

In order to find the magnetization dynamics, we calculate the time derivative of all occupation numbers \( f_{m_s} \). The mathematical description follows from the Liouville-von Neumann equation, and a coarse-grained description of the time evolution of the density operator [27]. The coarse-graining step size, interval \( \delta t \), determines the time resolution of the model and should be sufficiently small compared to the observed demagnetization time \( \tau_M \). Moreover, we assume that the time interval \( \delta t \) satisfies the conditions for the Markov approximation, i.e., \( \delta t \) should be much larger than the correlation time of the electrons and the density matrix changes slowly relative to \( \delta t \) [17, 21]. Secondly, it is assumed that the time interval is much larger than the time scale associated with the energy transfer, in this case that yields \( \delta t \gg \hbar/\Delta \). This is the standard limit underlying Fermi’s golden rule, i.e., the condition leads to the transitions having a well-defined energy conservation represented by the Dirac delta function. Hence, we should have that \( \hbar/\Delta \ll \delta t \ll \tau_M \). Since \( \hbar/\Delta \sim 10 \text{ fs} \) and \( \tau_M \) is of the order of \( \sim 100 \text{ fs} \), the validity of this limit is not trivial. However, it is expected that the role of all the approximations is relatively weak and only affects the results quantitatively.

Finally, using the diagonality of the density matrix \( \hat{\rho}^S \) and the explicit form of the interaction Hamiltonian \( \hat{H}_{sd} \) we find [21]

\[
\frac{df_{m_s}}{dt} = -(W_{m_s-1,m_s} + W_{m_s+1,m_s}) f_{m_s} + W_{m_s,m_s-1} f_{m_s-1} + W_{m_s,m_s+1} f_{m_s+1},
\]

where \( W_{m_s \pm 1, m_s} \) are the transition rates from level \( m_s \) to \( m_s \pm 1 \). The transition rates are calculated using Fermi’s golden rule, analogous to the derivation of the M3TM [15]. We assume that the \( s \) electrons thermalize rapidly due to Coulomb scattering and can be described by Fermi-Dirac statistics. Here, the distributions for the spin up and spin down \( s \) electrons have a common temperature \( T_e \), but are allowed to have a distinct chemical potential for which the difference is defined as the spin accumulation \( \mu_s = \mu_\uparrow - \mu_\downarrow \). In the limit that the Fermi energy is much larger than all other energy scales, we find [21, 22]
\[
W_{m_s \pm 1, m_s} = \frac{\pi}{2\hbar} J_{sd}^2 S_{m_s} \rho_{sd} \frac{\exp \left( \frac{\Delta - \mu_s}{2k_B T_C} \right)}{2 \sinh \left( \frac{\Delta - \mu_s}{2k_B T_C} \right)}.
\]  

(5)

Here, \(S_{m_s} = S(S + 1) - m_s(m_s \pm 1)\) and \(D_{\uparrow \downarrow}\) (in units eV\(^{-1}\)atom\(^{-1}\)) is the density of states at the Fermi level for the spin up and spin down \(s\) electrons respectively. Equation (5) mathematically quantifies the amount of available phase space for transitions induced by the \(s\)-\(d\) interaction. Figures 1(b)-1(d) schematically show the changes to the occupation of the \(d\) and \(s\) electron states as a result of laser heating the system. Figure 1(c) shows that the thermal broadening of the Fermi-Dirac functions allows for transitions between the two spin directions of the \(s\) electrons, which is accompanied by a flip of a localised \(d\) electron spin. The \(s\) electrons thermalize rapidly and the new distributions have a shifted chemical potential, i.e., a non-zero spin accumulation is created, as is depicted in Fig. 1(d).

The dynamics of the spin accumulation \(\mu_s\) can be derived analogously and directly follows from spin angular momentum conservation. Now we define the normalized magnetization \(m_d = -\langle \hat{S}_d^{\pm z} \rangle / S\) of the localised magnetic moments. In equilibrium, the experimentally detectable magnetization is dominated by \(m_d\). This is not straightforward after excitation because of the induced exchange of angular momentum between the \(s\) and \(d\) electrons. In general, the magneto-optical signal in typical pump-probe experiments is a linear superposition of the contribution of the \(s\) and \(d\) electrons. For a \(S = 1/2\) system we have \(\Delta = 2k_B T_C m_d\), and the dynamics is described by the two equations

\[
\frac{d\mu_s}{dt} = \rho_{sd} \frac{dm_d}{dt} - \frac{\mu_s}{\tau_s},
\]

(6)

\[
\frac{dm_d}{dt} = \frac{1}{\tau_{sd}} \left( m_d - \frac{\mu_s}{2k_B T_C} \right) \left[ 1 - m_d \coth \left( \frac{2m_d k_B T_C - \mu_s}{2k_B T_e} \right) \right].
\]

(7)

We defined the constant \(\rho_{sd} = \bar{D}^{-1} - J_{sd}/2\), with \(\bar{D} = 2D_{\uparrow} D_{\downarrow}/(D_{\uparrow} + D_{\downarrow})\). Note that the term proportional to \(J_{sd}\) results from the energy gap between the spin up and spin down \(s\) electrons arising from the \(s\)-\(d\) interaction (as was introduced in the transition from Eq. (2) to Eq. (3)), which can be both positive and negative depending on the sign of \(J_{sd}\). Moreover, we defined \(\tau_{sd}^{-1} = (\pi/\hbar) J_{sd}^2 D_{\uparrow} D_{\downarrow} k_B T_C\), which is closely related to the demagnetization rate. We introduced the phenomenological term proportional to \(\tau_{sd}^{-1}\), which describes all spin-flip
scattering processes that dissipate angular momentum out of the combined electronic system [18], e.g., this term includes Elliott-Yafet electron-phonon scattering.

Equation (7) clearly shows the similarities with the standard form of the equation for the longitudinal magnetization relaxation of a spin $S = 1/2$ system within a mean-field approach. For instance, in the limit $\tau_s \rightarrow 0$ the spin accumulation directly vanishes and the equilibrium condition is given by $m_d = \tanh(m_d T_C/T_e)$. In this limit there is no net spin polarization, i.e., the $s$ electrons can be considered as spinless, which is exactly the assumption underlying the M3TM [15]. We note that although this expression closely resembles the expression presented in Ref. [15], the pre-factor corresponds to a completely different physical mechanism. More details about the relation with the M3TM will be discussed below.

Although we have a simple definition of the parameters $\rho_{sd}$ and $\tau_{sd}$, the estimation of these parameters is far from straightforward. We approximated the $d$ and $s$ electrons as two distinct systems, localised and itinerant electrons. In the real system there is no such clear separation because of $s$-$d$ hybridization. Effectively, we separated the ‘band-like’ and ‘local magnetic’ properties of the combined electronic system ($d$ and $s$), which makes it complex to estimate the relevant value of $\bar{D}$. Hence, it is convenient to treat both $\tau_{sd}$ and $\rho_{sd}$ as effective parameters. In the upcoming sections, we interpret $\tau_{sd}$ as the experimentally retrieved demagnetization time and we choose the constant $\rho_{sd} = 1$ eV. The exact values should be retrieved from carefully fitting the model to the experiments, which is beyond the scope of this theoretical paper.

Finally, $D^{-1}$ $(D_{1/2}^{-1})$ scales with the width of the conduction band and is typically much larger than $J_{sd}/2$, i.e., we have $\rho_{sd} = \bar{D}^{-1} - J_{sd}/2 \approx \bar{D}^{-1}$. Then, we can define the magnetization of the total spin system ($s$ and $d$ electrons) as $m_{tot} = m_d - \rho_{sd}^{-1} \mu_s$, which is conserved by the $s$-$d$ interaction and will be used in the following analyses.

In the next section we discuss the important role of the spin accumulation by describing the laser-induced demagnetization experiments using the numerical solutions of Eqs. (6)-(7).

III. ULTRAFAST DEMAGNETIZATION

In order to investigate the typical laser-induced dynamics of the local magnetization and spin accumulation specifically, we consider a system with magnetic parameters $\tau_{sd} = 0.2$ ps and $T_C = 1000$ K. To model the laser heating we define the temporal profile of the laser
Figure 2. Ultrafast demagnetization described by the $s$-$d$ model. Figure (a) shows the temporal profile of the $s$ electron temperature $T_e$ and phonon temperature $T_p$, after laser-pulse excitation at $t = 0$ with $P_0 = 12 \cdot 10^8$ Jm$^{-3}$. Figures (b)-(d) present the laser-induced dynamics of the spin systems, using $T_C = 1000$ K and $\tau_{sd} = 0.2$ ps. Here, the line types indicate the calculations for different values of $\tau_s$, which are given in the figure. Figure (b) shows the resulting magnetization dynamics in the $d$ electron system. Figure (c) shows the temporal profile of the spin accumulation $\mu_s$ and Fig. (d) shows the dynamics of the total magnetization $m_{tot}$.

pulse as $P(t) = (1/(\sigma \sqrt{\pi})) \exp[-(t - t_0)^2/\sigma^2]$, where $P_0$ is the absorbed laser pulse energy density and $\sigma$ determines the pulse duration, which is set to 50 fs. We use the standard two-temperature model to find the dynamics of the $s$ electron temperature $T_e$ and phonon temperature $T_p$ [28]. We include a heat dissipation term that transfers heat out of the phonon system on a time scale $\tau_D = 20$ ps. For the heat capacities and the electron-phonon coupling constant we use the values for Cobalt given in Ref. [15]. We calculate the dynamics of the magnetization and spin accumulation by solving Eqs. (6)-(7) numerically. We do this for multiple values of $\tau_s$. The results are presented in Figs. 2(a)-(d).
Figure 2(a) shows the laser heating of the \( s \) electrons and the equilibration of the electron temperature with the phonon temperature. Figures 2(b)-(d) display the laser-induced dynamics of the spin systems for different values of the spin-flip scattering time \( \tau_s \), as indicated by the different line types. Figure 2(b) shows the magnetization of the \( d \) electrons \( m_d \) as a function of time. The temporal profile of the spin accumulation \( \mu_s \) is presented in Fig. 2(c). Finally, Fig. 2(d) displays the total magnetization \( m_{tot} \) as a function of time. Figures 2(b) and 2(d) clearly show that the demagnetization of \( m_d \) and \( m_{tot} \) is maximized for the smallest \( \tau_s \).

Figure 3. The \( s-d \) model in the limit of a strong \( s-d \) coupling \( (\tau_{sd} \to 0) \), compared to the microscopic three-temperature model (M3TM) [15]. The plot shows the magnetizations \( m_d \) (red) and \( m_{tot} \) (green) as a function of time after laser-pulse excitation at \( t = 0 \) with \( P_0 = 1 \cdot 10^8 \text{ Jm}^{-3} \) and \( \sigma = 50 \text{ fs} \). The remaining magnetic parameters are given by \( T_C = 1000 \text{ K} \) and \( \tau_s = 0.2 \text{ ps} \). The dotted black line indicates the magnetization calculated with the basic M3TM (using demagnetization time scale \( \tau_M = \tau_s = 0.2 \text{ ps} \) [29]).

The calculations show that the creation of a spin accumulation has a negative feedback effect on the demagnetization (of both \( m_d \) and \( m_{tot} \)), i.e., the short-lived spin accumulation acts as a bottleneck [18, 21]. The bottleneck can be removed by the additional spin-flip relaxation processes in the \( s \) electron system, which happen at a rate given by \( \tau_s^{-1} \). This means that in the limit \( \tau_{sd} \ll \tau_s \) the demagnetization rate strongly depends on \( \tau_s \). In the extreme case \( \tau_{sd} \to 0 \), which corresponds to an infinitely strong \( s-d \) interaction, \( m_d \) and \( \mu_s \) are equilibrated instantaneously and their relation can be found by setting Eq. (7) equal to zero. Now the \( d \) and \( s \) electrons can be treated as a single spin system with magnetization \( m_{tot} \) of which the subsequent dynamics is governed by \( T_e \) and the additional spin-flip scattering processes of the \( s \) electrons. These additional scatterings include Elliott-Yafet electron-
phonon scattering. Hence, in analogy with the M3TM [15], the system behaves as a single spin system with a characteristic demagnetization rate that is associated with Elliott-Yafet electron-phonon scattering. More specifically, in the low-fluence limit \( m_{\text{tot}}(t) \) converges to the magnetization dynamics from the M3TM, which is visualized in Fig. [3]. Here, \( m_d(t) \) and \( m_{\text{tot}}(t) \) follow from the \( s-d \) model using \( P_0 = 1 \cdot 10^8 \text{ Jm}^{-3} \) and \( \tau_s = 0.2 \text{ ps} \) in the limit of a strong \( s-d \) coupling (\( \tau_{sd} \rightarrow 0 \)). All other system parameters are kept equal to the calculations of Fig. [2]. The dotted black line is the magnetization described by the M3TM for the same system, using the demagnetization time scale \( \tau_M = \tau_s = 0.2 \text{ ps} \) [29], which shows a clear overlap with the total magnetization \( m_{\text{tot}} \).

On the other hand, in the limit \( \tau_{sd} \gg \tau_s \) the spin accumulation relaxes efficiently and the bottleneck effect is negligible. In this limit, the magnetizations \( m_d \) and \( m_{\text{tot}} \) converge and their dynamics can be well described by Eq. (7) without the terms involving \( \mu_s \) (similar to the limit \( \tau_s \rightarrow 0 \)). Up to a pre-factor, the magnetizations \( m_d \) and \( m_{\text{tot}} \) are now described by the same mathematical expression as in the M3TM. However, the physical origin of the ultrafast demagnetization is different.

In conclusion, in both regimes there is a clear relation with the M3TM. Nevertheless, in a real system it is expected that \( \tau_{sd} \) and \( \tau_s \) can be of the same order and a short-lived spin accumulation influences the magnetization dynamics. Finally, Fig. [2(c)] shows that for a decreasing \( \tau_s \) the spin accumulation becomes directly proportional to the temporal derivative of the magnetization \( m_d \), as can be mathematically derived from Eq. (6) in the limit \( \tau_s \rightarrow 0 \). These typical curves for \( \mu_s \) resemble the measurements in the experimental investigations of the optically generated spin currents at the interface of a ferromagnetic and non-magnetic metal [5].

In the following sections we investigate the role of spin transport on the demagnetization process.

IV. F/N/F STRUCTURES: PARALLEL VERSUS ANTI-PARALLEL

In the previous section we showed that during laser-pulse excitation a spin accumulation is generated that counteracts the demagnetization process. In this section, we show that spin transport can act as an additional mechanism for removing this bottleneck effect. We model the experiments with collinear magnetic heterostructures [3, 30]. More specifically, we
address the results presented in Ref. [3], in which a magnetic heterostructure is investigated that consists of two identical Co/Pt multilayers separated by a Ru spacer layer. The authors present a comparison of the demagnetization of the parallel and anti-parallel aligned states of the heterostructure. The measurements showed that the anti-parallel configuration has a larger demagnetization rate and amplitude, which can be explained by the generation of a spin current that enhances the demagnetization process. In the following, we will show that these results can be understood and reproduced by the presented $s$-$d$ model.

Hence, we consider a system containing two identical ferromagnetic (F) layers with a non-magnetic (N) layer in between. We further refer to this system as the F/N/F structure. We investigate the different laser-induced demagnetization rates for the parallel and anti-parallel configuration of the F/N/F structure. The systems are schematically depicted in the inset of Fig. 4. By definition, F layer 1 is pointing up in both configurations, whereas F layer 2 is pointing in the up and down direction for the parallel and anti-parallel configuration respectively.

We assume all the layers to be very thin, such that we can take the temperature, magnetization and spin accumulation homogeneous within each layer. We define a magnetization $m_{d,i}$ and $\mu_{s,i}$ for each F layer $i$. Because of the very small thickness of the N layer we assume
that the electron transport is in the ballistic regime. In that case, we can approximate that
the spin transport in the non-magnetic layer is purely driven by the difference in the spin
accumulation of both F layers. Within these limits the spin accumulations satisfy

\[ \frac{d \mu_{s,i}}{dt} = \rho_{sd} \frac{dm_{d,i}}{dt} - \frac{\mu_{s,i}}{\tau_{s,i}} - \frac{\mu_{s,i} - \mu_{s,j}}{\tau_{B}}, \]  

(8)

where \( i \neq j \) and \( i, j \in \{1, 2\} \). The last term represents the spin transfer between the F
layers driven by ballistic electron transport. The prefactor, which has the units of time, is
defined as \( \tau_{B} \). We use that \( \tau_{B} \sim 1 \) fs based on the assumptions that the Fermi velocity is
\( v_{F} \sim 10^{6} \text{ ms}^{-1} \) and the thickness of the N layer is \( d_{N} \sim 1 \text{ nm} \). Note that the transport
term depends on the spin accumulation at the same time coordinate, i.e., the distinct F
layers feel changes in the opposing layer instantaneously. In the real experiment there might
be a small delay. However, we expect that this effect can be neglected in our calculations.
Finally, we stress that this particular form of the transport term can only be used for two
strictly identical F layers, as was the case in Ref. [3].

For the F layers we use the magnetic parameters \( \tau_{sd} = 0.1 \) ps, \( \tau_{s} = 0.02 \) ps and \( T_{C} = 600 \) K, which are approximated values corresponding to the Co/Pt multilayers used in the
experiments [3]. Furthermore, we apply a low-energetic laser pulse with \( P_{0} = 1 \cdot 10^{8} \text{ Jm}^{-3} \)
and assume that the system is heated homogeneously. In this specific case, we set the pulse
duration to \( \sigma = 70 \) fs [3]. For convenience, we still use the heat capacities and electron-
phonon coupling constant of pure Cobalt [15].

The results are displayed in Fig. 4. The red and blue curves show the magnetization \( m_{d} \)
of F layer 1 for the parallel and anti-parallel configuration respectively. It is verified that
\( m_{\text{tot}} \) (not shown) behaves very similar. In agreement with the experiments, we observe a
larger demagnetization rate and amplitude for the anti-parallel configuration. This can be
easily understood from the transport term in Eq. (8). In the parallel configuration we have
\( \mu_{s,1} = \mu_{s,2} \) at any time and the transport term vanishes. In contrast, for the anti-parallel
configuration we have \( \mu_{s,1} = -\mu_{s,2} \); the transport does not vanish and behaves as an extra
channel for angular momentum transfer. This extra channel assists the reduction of the
spin accumulation, thereby leading to a larger demagnetization. Equivalently, in the anti-
parallel configuration the spin current in the non-magnetic layer is non-zero and has exactly
the correct polarisation to enhance the demagnetization rates in both F layers. Finally,
The laser-induced magnetization dynamics in an F/N structure. The magnetic parameters of the ferromagnetic layer are given by $\tau_{sd} = 0.3$ ps, $\tau_s = 0.2$ ps and $T_C = 1388$ K. (a) The maximum demagnetization $\Delta m_d$ as a function of the ferromagnetic layer thickness $d_F$. The non-magnetic layer thickness is set to $d_N = 200$ nm and we used $P_0 = 30 \cdot 10^8$ Jm$^{-3}$. The inset shows the system schematically. (b) The maximum demagnetization $\Delta m_d$ as a function of $P_0$ for $d_F = 5$ nm (blue) and $d_F = 20$ nm (red). For both systems we have $d_N = 200$ nm. The black dashed line indicates the demagnetization of the bulk ferromagnet in the absence of an F/N interface ($d_F = \infty$ and $d_N = 0$).

Fig. 4 also shows that the demagnetization curves of the two configurations converge at $t \sim 400$ fs, which is in agreement with the experiments [3].

In the next section, we analyse the temporal profile of the spin current generated in an F/N structure in the diffusive regime. Furthermore, we investigate the role of the thickness of the layers.

V. F/N STRUCTURES: DIFFUSIVE SPIN TRANSPORT

Finally, we show that in magnetic heterostructures spin diffusion within the s electron system can significantly enhance the demagnetization rate. Here, we model a system consisting of a ferromagnetic (F) layer and a non-magnetic (N) layer. As indicated in the inset of Fig. 5(a), we define the thickness of the F layer and N layer as $d_F$ and $d_N$ respectively. Spin transport is described in the diffusive regime, where both layers are treated on an equal footing. We assume that the interface is transparent for spins, such that the spin accumulation is continuous at the interface [31, 32]. We write
\[
\frac{\partial \mu_s}{\partial t} = \frac{\partial}{\partial x} \left[ D \frac{\partial \mu_s}{\partial x} \right] - \frac{\mu_s}{\tau_s},
\]

(9)

where \( x \) is the spatial coordinate, the interface is at \( x = 0 \), and we assumed that the system is homogeneous in the lateral directions. Here, \( D \) corresponds to the diffusion coefficient. Furthermore, we set the spin currents at the edges equal to zero \( j_s(-d_F) = j_s(d_N) = 0 \). For convenience, we assume that the system is heated homogeneously, i.e., there are no thermal gradients present. Hence, the demagnetization of the F layer is the only source of the spin current and there is no spin-dependent Seebeck effect included in this calculation.

Equation (9) is solved numerically, where we discretized the system using a finite difference method. Note that the spatial derivative of the diffusion coefficient \( D \) is only non-zero at the interface. In these calculations, the F layer corresponds to pure Cobalt for which we use the diffusion coefficient \( D = 250 \text{nm}^2\text{ps}^{-1} \) [26]. Furthermore, we use \( \tau_{sd} = 0.3 \text{ps} \) and \( \tau_s = 0.2 \text{ps} \). For the N layer we take \( D = 9500 \text{nm}^2\text{ps}^{-1} \) and \( \tau_s = 25 \text{ps} \), which correspond to the diffusion coefficient and spin-flip relaxation time for Copper [26].

Figure 5(a) shows a calculation of the F/N structure excited with a laser pulse with energy density \( P_0 = 30 \cdot 10^8 \text{Jm}^{-3} \) and pulse duration \( \sigma = 50 \text{fs} \), where we used the heat capacities and electron-phonon coupling constant of Cobalt [15]. The diagram shows the maximum demagnetization \( \Delta m_d = m_{d,0} - m_{d,\text{min}} \) as a function of the F layer thickness \( d_F \), where \( m_{d,0} \) is the initial (equilibrium) value of \( m_d \), and \( m_{d,\text{min}} \) is the minimum of \( m_d \) after excitation. The thickness of the N layer is kept constant and set to \( d_N = 200 \text{nm} \). It clearly shows that the demagnetization becomes larger when the F layer thickness decreases. Intuitively, the injection of spins into the non-magnetic layers can enhance the demagnetization significantly as long as the F layer is relatively thin. This conclusion is corroborated by the results presented in Fig. 5(b), which shows the demagnetization \( \Delta m_d \) as a function of \( P_0 \). The results are plotted for \( d_F = 5 \text{nm} \) and \( d_F = 20 \text{nm} \). The dashed line indicates the demagnetization of a bulk ferromagnet in the absence of an N layer \( (d_F = \infty \text{ and } d_N = 0) \). The calculations show that for a relatively thin F layer spin injection into the N layer can lead up to \( \sim 30\% \) more demagnetization.

Now we discuss the dynamics of the injected spin current itself. We do this by calculating the spin accumulation at the outer edge of the N layer \( \mu_s(d_N) \). The results are shown in Fig. 6 which displays the spin accumulation as a function of time for three different values
Figure 6. The diffusive spin current injected in the non-magnetic (N) layer with thickness $d_N$, coupled to a ferromagnetic (F) layer with thickness $d_F$. The diagram shows the spin accumulation at the outer edge of the N layer (position $x = d_N$, indicated by the red dotted line in the inset) as a function of time. Furthermore, we set $P_0 = 20 \cdot 10^8$ Jm$^{-3}$ and $\sigma = 50$ fs. The magnetic parameters are identical to the values used in Fig. 5. The line types indicate the results for three different values of $d_N$. The thickness of the F layer is kept constant and set to $d_F = 10$ nm.

of $d_N$ that are given in the figure. The F layer thickness is kept constant at $d_F = 10$ nm. In agreement with the experimental investigations [5, 26], the diagram clearly shows that for an increasing $d_N$ the minimum of $\mu_s(d_N)$ shifts in time and is reduced. This behaviour can be understood from the diffusive character of the spin transport. Here, the temporal profile of $\mu_s(d_N)$ is highly sensitive to the specific material that composes the F layer and the corresponding effective parameters, as is expected from the experimental investigation using various materials for the F layer [26].

A more quantitative comparison with the experiments would require addressing spin transport beyond the diffusive regime and implementing a finite penetration depth of the laser pulse in the modelling. However, we focused our discussion on the dynamics that stems from the $s$-$d$ interaction and we specifically investigate the role of $\mu_s$ independent of the thermal properties of the system. In that case, the model shows that in the presence of only the $s$-$d$ interaction, the typical experimental observations can be explained and show a qualitative agreement.
VI. CONCLUSION AND DISCUSSION

In conclusion, we presented a simplified s-d model that is used to describe laser-induced magnetization dynamics in magnetic heterostructures. The presented numerical calculations show the critical role of the spin accumulation. During demagnetization a spin accumulation is created, which counteracts the demagnetization process. Both local spin-flip scatterings and spin transfer to a non-magnetic layer can reduce this spin accumulation effectively and, depending on the system, can both play a dominant role in the characterization of the demagnetization rate. Importantly, the model shows that even in the absence of any other interaction, the s-d interaction could account for the typically observed ultrafast phenomena.

The presented s-d model provides a versatile description of ultrafast magnetization dynamics, which converges to the M3TM for a strong s-d coupling and possesses the additional feature that spin transport can be included straightforwardly. However, one needs to keep in mind that the presented model is a simplified description of the underlying physics. As was earlier discussed, the d electrons are not perfectly localised. Moreover, the d electron spins are described using a Weiss model, i.e., spin wave excitations are neglected. In a more complete description, the d electrons are described as a magnonic system and the s-d interaction corresponds to electron-magnon scattering [18]. That has the advantage that spin transport driven by magnon transport can be included, which is expected to give a non-negligible contribution to the spin transport at the interface between a ferromagnetic and non-magnetic metal [32]. In that case, the electronic and magnonic contribution to the spin transport can be treated on an equal footing by introducing a magnon chemical potential [32, 33]. This description should allow for both chemical potential gradients and thermal gradients. For instance, thermal gradients can be induced by a finite penetration depth of the laser pulse and can drive a spin current via the electronic spin-dependent Seebeck effect [24, 25] and the magnonic spin Seebeck effect [34, 35]. Nevertheless, we expect that the dominant contributions to the dynamics can be well described by the presented model and it provides a useful pathway to investigate the underlying physics.

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