Machine Learning-Based Analysis of Free-Text Keystroke Dynamics

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Abstract

The development of active and passive biometric authentication and identification technology plays an increasingly important role in cybersecurity. Keystroke dynamics can be used to analyze the way that a user types based on various keyboard input. Previous work has shown that user authentication and classification can be achieved based on keystroke dynamics. In this research, we consider the problem of user classification based on keystroke dynamics features collected from free-text. We implement and analyze a novel a deep learning model that combines a convolutional neural network (CNN) and a gated recurrent unit (GRU). We optimize the resulting model and consider several relevant related problems. Our model is competitive with the best results obtained in previous comparable research.

1 Introduction

Recently, passive biometric authentication and identification techniques have received considerable attention. In this research, we consider such a passive biometric based on keystroke dynamics. The resulting technique is applicable to the authentication problem, and can also potentially play a role in intrusion detection.

Keystroke dynamics are based on typing behavior, such as the duration of keyboard events, the duration of key presses, the time difference between key presses, and so on. Such data can be collected from a standard keyboard by monitoring input and recording the time intervals between each keystroke. Keystroke dynamics may not be strong enough too be used as a standalone authentication system and hence it is typically combined with another type of authentication, such as a password. In its role as an IDS, keystroke dynamics may be competitive with other techniques.

Compared with most other biometric technologies (e.g., fingerprint), keystroke dynamics has advantages. For example, no special hardware is required to collect

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keystroke features, and keystroke data can be obtained in a passive manner, which reduces the burden on users. In addition, keystroke dynamics can be used as part of a real-time intrusion detection system (IDS)—in contrast to a typical username and password authentication system, where ongoing monitoring is not a realistic option. In addition to playing a role in authentication, keystroke dynamics can serve to enhance security after a user has been authenticated.

Disadvantages of keystroke dynamics based authentication might arise if a user has an injured hand, a user is distracted, or the hardware (e.g., keyboard) has changed. We believe that that these—and related—disadvantages can be overcome, and we expect that the use of keystroke dynamics in security applications will increase in the future.

In this paper, we analyze free-text keystroke dynamics data and train deep learning models to distinguish between users. The features we consider are related to keystroke timing, and are all obtained from standard keyboards. Furthermore, we do not utilize the characters that are typed, and hence user privacy is maintained.

We focus primarily on a novel model architecture that combines a convolutional neural network (CNN) and a gated recurrent unit (GRU). We experiment with non-timing features and we employ concepts from Siamese networks [9], and we experiment with pre-trained models and attention.

Here, we only consider free-text data [2]. Specifically, for our free-text dataset, we use [30], which contains keystroke data from 148 participants. The primary goal of this research is to achieve a high accuracy from a biometric system that uses features derived from keystroke dynamics. Among other desirable properties, we would ideally like our models to be scalable and robust.

The following sections of this paper are organized as follows. Section 2 discusses relevant background topics, with the focus on a survey of previous work. Section 3 describes the dataset used in our experiments and outlines the machine learning techniques that we employ. Our free-text experimental results are presented in Section 4, while Section 5 summarizes our main results, and include suggestions for future work.

2 Background

In this section, we discuss keystroke dynamics and we provide a selective survey of previous work in this field. We also introduce the machine learning models that we employ in this research.

2.1 Keystroke Dynamics

According to [22], “keystroke dynamics is not what you type, but how you type.” Most previous work on typing biometrics can be divided into either classification that relies on fixed-text or authentication based on free-text data [25]. For fixed-text, the text used to model the typing behavior of a user and to authenticate
the user is the same (e.g., a password). This approach is usually applied to short text sequences. Classification is generally based on timing features related to the character typed [6]. An thorough discussion of the fixed-text problem can be found in [25].

For the free-text case, the text used to model typing behavior of a user and the text used to authenticate the same user is, in general, not the same. Free-text usually implies long text sequences, and can be viewed as a continuous form of authentication or as part of an IDS.

In the past, distance based methods were popular for the analysis of keystroke dynamics. More recently, machine learning techniques have come to the fore, including support vector machines (SVM), recurrent neural networks (RNN), hidden Markov models (HMM), $k$-nearest neighbors ($k$-NN), multilayer perceptrons (MLP), and so on [33].

Next, we discuss relevant previous work. Then, in the subsequent section, we the dataset and learning techniques used in our experiments.

## 2.2 Previous Work

In this section, we first consider distance-based methods. Then we discuss more recent work that is based on a wide variety of (mostly) modern machine learning techniques.

### 2.2.1 Distance Based Research

The concept of keystroke dynamics can be traced back to the 1970s, at which time the analysis was focused on fixed-text data [7]. Subsequently, Bayesian classifiers based on the mean and variance in time intervals between two or three consecutive key presses were applied to keystroke dynamics data [23]. For example, in [23] the authors claim an accuracy of 92% over a dataset consisting of 63 users.

Typical of relatively early work in this field are nearest neighbor classifiers based on distance measures. Euclidean distance or, equivalently, the $L_2$ norm was often used. More success was found using the $L_1$ norm (i.e., Manhattan distance), which makes it easier to single out the contribution made by individual components. In addition, the $L_1$ norm is more robust with respect to outliers. In [18], the best result obtained from a distance-based technique uses a nearest neighbor classifier based on a scaled Manhattan distance. Subsequently, statistical-based distance measures—such as Mahalanobis distance—were used with success in keystroke dynamics research [3].

The equal error rate (EER) is a point on the ROC curve where the sum of the false accept rate (FAR) and false rejection rate (FRR) is minimized. The EER is a commonly used measure of success for biometric systems—the lower the value of EER, the better the performance of a system. For example, in [18] the authors achieve an equal error rate (EER) of 0.096.
2.2.2 Machine Learning Based Research

Recently, research in keystroke dynamics has been dominated by machine learning techniques. Such techniques include $K$-nearest neighbors ($k$-NN) [32], $K$-means clustering [15], random forests [19], fuzzy logic [10], Gaussian mixture models [13], and many, many more.

In comparison to the fixed-text problem, the number of research studies involving free-text data is much smaller. In [31] it is claimed that the amount of research done with fixed-text was eight times as much as that for free-text, as of 2013.

Free-text presents several challenges as compared to fixed-text. For example, in free-text, the number of keys typed can differ greatly. There may also be word-specific dependencies in free-text [28] that would not be relevant in fixed-text.

As an aside, we note that other keystroke features might be of interest. For example, keystroke acoustics are considered in [27], where a dataset containing 50 users yields an EER of 11%. This results shows that acoustic-based typing information can be useful for authentication. However, an advantage of keystroke dynamics based on timing features is that such information can be easily collected from any standard keyboard.

3 Implementation

In this section, we first introduce the keystroke dynamics dataset considered in this research. Then we discuss the various learning techniques that we have applied to this free-text dataset.

3.1 Dataset

For our free-text data, we choose to use the so-called Buffalo dataset [30], which was collected by researchers at SUNY Buffalo. This dataset contains long fixed-text and free-text keystroke data from 157 subjects, with each subject using the keyboard over three sessions [30]. For the fixed-text, users were requested to type Steve Jobs’ Stanford commencement speech, which was split into three pieces. In free-text, users are requested to answer two survey style questions and one scene description. The time duration within each session was about 50 minutes, with about 5700 keystrokes, on average, and hence over 17,000 for the three sessions combined. Furthermore, there was a 28 day time interval between sessions, and four different types of keyboards were used. In this paper, we only consider the Buffalo free-text keystroke data.

Note that the Buffalo free-text dataset is divided into two subsets, referred to as a “baseline” subset and a “rotation” subset. In the baseline subset, there are 75 users using the same type of keyboard across all three sessions. For the rotation subset, there are 74 users using three different types of keyboard across their three sessions. The data collected on each keystroke consists of the name of the key, the key event (key-down or key-up), and a timestamp (measured in milliseconds).
3.2 Techniques Considered

In our free-text experiments, we also employ machine learning models that are somewhat more complex and experimental in nature, as compared to those typically used in comparable research. Next, we briefly discuss both of the models we consider.

3.2.1 BERT

Bidirectional encoder representations from transformers (BERT) is a language model developed by Google [5] that is designed to serve as an encoder in an encoder-decoder model. The BERT encoder converts words into vector representations that a corresponding decoder can then use to generate the output. BERT training is divided into two major steps which are known as pre-training and fine-tuning. In the pre-training phase, Google has used a large amount of text data to train the model in an unsupervised manner. In fine-tuning, labeled training data is used to adapt the model to a specific problem. In our experiments, we use the pre-trained model and the fine-tuning is performed based on the words typed by a user.

3.2.2 CNN-GRU Model

We propose a novel hybrid CNN-GRU model that is designed to learn from a sequence of individual keystroke features. This model was inspired by related work in [17].

The core idea of using a GRU is that it can take advantage of sequential information in a user’s typing behavior. Since a GRU is a type of recurrent neural network, it has the ability to learn the current characteristics of the input based on previous characteristics. In addition, we use a CNN before the GRU, with the aim of providing enhanced features to the GRU. In effect, this CNN step can be viewed as a form of feature engineering. In our CNN, the length of the convolutional kernel corresponds to the number of sequences that are covered. The convolution operation has the ability to produce a “higher-level” keystroke signature. Subsequently, these signatures serve as the input to the GRU. After training the GRU, a user’s keystroke behavior pattern is obtained.

We also implement dropout within the proposed model. The idea of dropout was introduced in [29] as a regularization technique for deep neural network. As the name indicates, for dropouts we randomly drop nodes (neurons) along with their connections from the neural network during training. This has the effect of training each mini-batch over a different network. Dropouts serve to prevent overfitting by forcing nodes that would likely otherwise atrophy to be active in the learning process.

For this proposed model, we use the BCEWithLogitalLoss activation function, as opposed to the more typical sigmoid. According to [24], BCEWithLogitalLoss is more stable than sigmoid or BCELoss.
4 Free-Text Experiments

This section provides our experiments and results for the machine learning techniques discussed above when applied to the Buffalo free-text dataset. We also provide some analysis of our experiments.

The Buffalo free-text dataset contains three different sessions. Thus, we perform 3-fold cross validation with each session serving as a fold. We use the notation s01-train-s2-test to mean that we use sessions 0 and 1 for training, with session 2 reserved for testing—the notation for the other folds is analogous.

4.1 Text-Based Classification

First, we attempt to classify based on the text typed by users. Ultimately, we want to classify users based on their keystroke dynamics, but by first focusing solely on the characters typed, we can see how much information is contained in users’ differing responses, as opposed to their typing characteristics.

For our text-based experiment, we use BERT for multi-classification of the 148 users in the free-text part of the Buffalo dataset, based on words typed. This experiment, which we refer to as BERT-word, was complicated by various typos that had to be corrected.

The result of this experiment is extremely poor, and testing loss does not decrease significantly. One problem may be that the dataset is too small, as the training data for each user consists of only about 15 lines of words, with 2 lines for testing. Note that each line contains about 18 words. In a typical NLP application, we would have hundreds of times more data for training and testing.

The bottom line here is that we are not able to classify users based on the actual text that was typed with an accuracy greater than guessing. Although additional experiments might be helpful, it appears that there is little useful information contained in the raw text. We now turn our attention to keystroke dynamics based models.

4.2 Keystroke Dynamics Models

Here, we apply and analyze our novel CNN-GRU architecture, which we outlined in Section 3.2.2, above. This model is based only on keystroke dynamics, as opposed to the actual text typed by a user.

The goal here is to build a model that could be used as part of an ongoing intrusion detection system (IDS). That is, the model would be used to periodically verify the identity of a user in real time.

For our dataset, we employ the baseline subset of the Buffalo free-text, in which each of 75 users typed across three sessions. After determining the basic parameters of our model, we consider a wide variety of modifications.
4.2.1 Features

We consider three types of features in our experiments, namely, timing features, rate features (discussed below), and “fusion.” For the fusion case, we simply combine the timing and rate features.

First, we consider timing features only. In this case, we transform the free-text keystroke data into a fixed-length keystroke sequence, then further convert the sequence into a keystroke vector. The format of the keystroke vector is presented in Figure 1, where \( x \) and \( y \) are consecutive keystrokes. Note that \( x \) and \( y \) are simply numeric values representing the position in the keystroke sequence—the key that was pressed in not recorded. That is, we do not use what was typed as a feature, just how it was typed. This assures that a user’s typing is not revealed by our analysis.

The notation \( H[x] \) is the hold duration of the key, \( U[x] \) is the key-up time (the timestamp when key is released), and \( D[x] \) is the key-down time (the timestamp of the key was pressed). Therefore, \( D[x]U[x] \) is the time duration that a key was pressed until it was released, and \( D[x]D[y] \) is the time duration between two consecutive keys being pressed. In all cases, \( x \) and \( y \) indicate any key being pressed.

| ID\([x]\) | ID\([y]\) | H\([x]\) | H\([y]\) | D\([x]\)U\([y]\) | D\([x]\)D\([y]\) |

Figure 1: Keystroke timing feature vector

After obtaining the keystroke vectors, we normalize the timing features. As discussed in [34], this normalization results in features with mean 0 and variance 1.

Next, we consider “rate” features. Traditionally, keystroke dynamics is based on timing, as discussed above. However, other typing habits can also serve as indicators of typing behavior. For example, features that relate to the use of the left and right hands may help the model to distinguish between users.

In addition to conventional timing features, we further consider seven features consisting of the rate at which various keys are pressed. Specifically, we consider rate at which each of the delete, left shift, right shift, left caps, right caps, control key, and the combination of left and right arrow keys are pressed. These features will surely be useful for distinguishing a user’s handedness, but they may also be useful as more general indications of typing style.

As a first experiment, we consider different numbers of key-strokes for analysis. Specifically, we consider conventional key-length 100 and rate features with key-length 500. For each user, we append the rate features after the timing features. We have tested models with three different kinds of features, namely, timing only, rate only, and combined. The accuracy of the timing feature only is 84.72%, while the accuracy improves to 90.82% after combining with the rate features.

For some users, the rate features make a large difference, but for others they actually make the results worse. For example, user 1 with timing feature alone has an accuracy is only about 60%. But if we combine with the rate feature, accuracy increases to 95%. In this case, the mixed features seem to be effective. However,
for user 7, the timing feature alone yield an accuracy of 82%, but if we include the rate features, the accuracy drops to 50% for the fusion case, while considering rate alone, the accuracy is 87.5%. In some cases it is better to use timing alone while in some other cases, it is better to combine both, and yet other cases it is best to just use rate features. But in most cases, the accuracy is increased when using the combined features. The result of first seven users is shown in Figure 2.

Finally, we consider feature “fusion,” that is, we combine timing and rate features, using the same key length for both. We have also experimented with independent key-lengths, but this does not improve on the results presented here.

Next, we combine the rate features with the timing feature using the idea from Siamese network [9]. A Siamese network has two inputs, which are fed into two neural networks that, respectively, map the inputs into a new space. A distance-related loss function is used to train the network parameters, so that the trained network can measure the similarity of the two inputs. For the rate features, we apply a linear transformation using the torch.nn.Linear() module from PyTorch, while conventional features use a multi-kernel CNN-GRU. We then concatenate the two features together and pass them through a fully connected layer to obtain the desired output.

The results of our fusion experiments are summarized in Table 1. We observe that when we apply longer key lengths, the result tend to improve. However, the reason we stop at key length 250 is that some users typed much less than was typically the case. Regardless, these experiments show that the this fusion approach is effective, and achieves very high accuracy for this authentication problem.
Table 1: Feature fusion for different key lengths

| Model   | Parameters | Test session | Average |
|---------|------------|--------------|---------|
|         | kernel     | key-length   | s0      | s1      | s2      |
| CNN-GRU | 2,2,2      | 50           | 89.2%   | 89.7%   | 89.6%   | 89.5%   |
|         | 2,2,2      | 150          | 92.5%   | 93.1%   | 93.7%   | 93.1%   |
|         | 2,2,2      | 200          | 93.4%   | 93.6%   | 94.3%   | 93.8%   |
|         | 2,2,2      | 250          | 94.6%   | 94.1%   | 93.8%   | 94.2%   |

4.2.2 Parameter Tuning

Next, we perform parameter tuning on our CNN-GRU model. The hyperparameters that we vary include the learning rate, kernel size of the CNN, and keystroke length, among others. Since our model is implemented in Cuda [11], we are able to efficiently test many parameter values.

As discussed above, our original model uses a single kernel CNN-GRU model and achieves an average accuracy of 84.7%. We consider a multi-kernel CNN, where the kernel is a list so that different combinations can be tested. When we include the rate features, we obtain a best average accuracy of 92.1% using the model parameters in Table 2.

Table 2: Best result for parameter tuning of kernel

| Model   | Parameters | Accuracy |
|---------|------------|----------|
|         | kernel     | out-channel | RNN-size |         |
| CNN-GRU | 2,2,2      | 32        | 8        | 92.0%    |

In a multi-kernel model, when the kernel sizes differ, features are observed on different scales—when the kernel size is large, the receptive field is bigger and more of the input is observed. The tradeoff is that larger kernel sizes tend to result in overfitting. Furthermore, when we combine different kernels together, padding issues arise. The purpose of padding is to make the size of the feature map consistent with the size of the original image, with padding determined by the size of the filter and the size of the stride. Padding enables us to use all of the actual data.

Our multi-kernel experiment results are given in Table 3. None of these results improve on our best previous accuracy of 92.3%.

Another parameter of interest in our CNN is the “out channel” which is the number of channels produced by the convolution. The results obtained when experimenting with this parameter are given in Table 4. Here, we obtain a marginal improvement on our previous best accuracy.

We also conduct experiments varying the depths of convolutional layers. These experimental results for three to nine layer modes are summarized in Table 5. Somewhat surprisingly, these result indicate that higher layer models do not seem to
Table 3: Parameter tuning CNN kernel

| Model   | Kernel | Test session | Average |
|---------|--------|--------------|---------|
|         |        | s0 | s1 | s2 |
| CNN-GRU | 2      | 85.0% | 85.6% | 83.5% | 84.7% |
|         | 2,4,6  | 89.2% | 90.1% | 90.7% | 90.0% |
|         | 2,4,6,8 | 87.9% | 88.1% | 87.9% | 88.0% |
|         | 2,2,2  | 91.7% | 92.4% | 92.3% | 92.1% |
|         | 4,4,4  | 89.6% | 90.4% | 90.0% | 90.3% |

Table 4: Parameter tuning CNN out channel

| Model   | Parameters | Test session | Average |
|---------|------------|--------------|---------|
|         | kernel     | out-channel  |         |
| CNN-GRU | 2          | 16 | 90.9% | 90.4% | 90.7% | 90.6% |
|         | 2          | 32 | 92.4% | 92.1% | 91.4% | 92.0% |
|         | 2          | 48 | 92.6% | 92.4% | 91.8% | 92.3% |
|         | 2          | 64 | 92.6% | 92.2% | 91.8% | 92.2% |
|         | 2          | 96 | 91.6% | 92.3% | 92.3% | 92.1% |
|         | 2          | 128 | 92.1% | 92.5% | 91.6% | 92.1% |

improve over our 3-layer model. In the realm of future work, it would be interesting to experiment with other deep networks, such as ResNet, DenseNet, and SENet.

Table 5: Parameter tuning CNN convolution

| Model   | Parameters | Test session | Average |
|---------|------------|--------------|---------|
|         | Conv. Learning rate | s0 | s1 | s2 |
| CNN-GRU | 3        | 0.001 | 91.1% | 90.6% | 89.9% | 90.5% |
|         | 3        | 0.01  | 91.6% | 92.3% | 91.6% | 91.8% |
|         | 6        | 0.01  | 92.1% | 92.1% | 91.8% | 91.8% |
|         | 9        | 0.01  | 91.5% | 92.1% | 90.8% | 91.5% |

Next, we experiment with an attention mechanism in both the single kernel and multi-kernel cases. When using conventional features only, we obtain a marginal improvement, as summarized in Table 6.

After experimenting with additional parameter tuning, we find the best model uses the parameters in Table 7. These parameters will be used in all subsequent experiments.

4.2.3 Fine Tuning

In this section, we consider a model for multi-classification of all 75 users (as discussed above) and then use this model in a pre-trained mode to construct a binary
classification model. We refer to this two-step process as “fine tuning.”

Note that here we consider binary classification of each user, and hence each user will have their own model. We then consider the average case for each of the resulting 75 models to obtain our accuracy results. In the multi-classification stage, we construct a single model among 75 users that we then use as a pre-trained model to construct each of the binary classifiers via “fine-tuning.”

We have experimented with a wide variety of parameters at the multi-class stage. We obtain a best result of 76.96% using the parameters shown in Table 8.

After obtaining our best pre-trained model, we further apply it in a binary classification model to obtain a best accuracy is 97.2%, as summarized in Table 9.

It can be seen from the result in Table 10 that the ratio of positive samples to negative samples in the validation and test sets is roughly equal, which means that we have data with similar distributions for evaluation and testing. In Table 10, we consider user IDs from 1 to 5.

In addition, both the training and validation sets use random sampling, while the test set runs on all samples. Therefore, in the test set, the number of samples for label 0 (not users) is much more than the number of samples for label 1 (users). The results shown in Table 11 indicate that a model that can better discriminate samples with label 0 will be stronger.

### Table 6: Analysis of attention layer

| Model     | Parameters kernel | Attention | Test session s0 | s1 | s2 | Average |
|-----------|------------------|-----------|-----------------|----|----|---------|
| CNN-GRU   | 2                | —         | 90.16%          | 88.37% | 88.54% | 89.02%  |
|           | 2                | ✓         | 89.91%          | 89.17% | 88.92% | 89.00%  |
|           | 2,2,2            | —         | 91.70%          | 92.40% | 92.30% | 92.10%  |
|           | 2,2,2            | ✓         | 92.00%          | 92.40% | 92.50% | 92.30%  |

### Table 7: Attention and rate features (baseline subset)

| Model     | Hyperparameter | Value | Test session s0 | s1 | s2 | Average |
|-----------|----------------|-------|-----------------|----|----|---------|
| CNN-GRU   | CNN kernel     | 2     | 95.4%           | 94.5% | 94.0% | 94.6%   |
|           | CNN out        | 48    |                 |    |    |         |
|           | RNN size       | 8     |                 |    |    |         |
|           | learning rate  | 0.001 |                 |    |    |         |
|           | weight-decay   | 0.00001 |               |    |    |         |
|           | step-scheduler | 70    |                 |    |    |         |
|           | key-length     | 250   |                 |    |    |         |
|           | epochs         | 80    |                 |    |    |         |
|           | attention      | yes   |                 |    |    |         |
|           | rate features  | 7     |                 |    |    |         |

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| Model      | Hyperparameter       | Value  | Test session |
|------------|----------------------|--------|--------------|
|            |                      |        | s0 | s1 | s2 |
| CNN-GRU    | CNN kernel-size      | 3      | 77.74% | 77.38% | 76.96% |
|            | CNN out-channel      | 192    |      |     |    |
|            | RNN size             | 32     |      |     |    |
|            | learning rate        | 0.01   |      |     |    |
|            | weight-decay         | 1e-5   |      |     |    |
|            | step-scheduler       | [80,350,390] |    |     |    |
|            | key-length           | 250    |      |     |    |
|            | epochs               | 400    |      |     |    |

Table 9: Fine-tune results (baseline subset with freeze)

| Model      | Parameters | Test session | Average |
|------------|------------|--------------|---------|
|            | freeze     | s0 | s1 | s2          |     |
| Fine-tune  | —          | 0.01| 96.7% | 97.4% | 97.1% | 97.1% |
|           | —          | 0.001| 97.3% | 97.3% | 96.9% | 97.2% |
|           | —          | 0.0001| 94.5% | 95.2% | 94.6% | 94.7% |
|           | ✓          | 0.01| 94.4% | 94.7% | 93.6% | 94.2% |
|           | ✓          | 0.001| 94.0% | 93.9% | 94.0% | 94.0% |
|           | ✓          | 0.0001| 84.5% | 84.5% | 85.1% | 84.7% |

Table 10: Test and validation ratios

| User ID | Test pos | Test neg | Test ratio | Validation pos | Validation neg | Validation ratio |
|---------|----------|----------|------------|----------------|----------------|------------------|
| 1       | 310      | 12,797   | 0.02422    | 2643           | 115,319        | 0.0229           |
| 2       | 182      | 12,925   | 0.01408    | 1673           | 116,289        | 0.0144           |
| 3       | 248      | 12,859   | 0.01929    | 2109           | 115,853        | 0.0182           |
| 4       | 173      | 12,934   | 0.01338    | 1697           | 116,265        | 0.0146           |
| 5       | 184      | 12,923   | 0.01424    | 1607           | 116,355        | 0.0138           |

Table 11: Test and validation

| Data    | Test session | Average |
|---------|--------------|---------|
| val     | 89.67% | 87.98% | 87.70% | 88.45% |
| test    | 94.74% | 89.22% | 90.05% | 91.34% |
We further analyze the precision, recall, F1 score, and perform parameter adjustments for the labels 0 and 1. Note that originally, label 1 is used as the positive label (user). However, since the data is so imbalanced, we swap the positive and negative label to observe the result on the multi-kernel (2-2-2) model. These label switching results are shown in Table 12. We observe that this model has a strong ability to detect intruders—the precision in the best case is virtually 100%. This experiment indicates that our model would work well as an IDS.

Table 12: Label-swap

| Metric | Test session | Average |
|--------|--------------|---------|
|        | s0  | s1  | s2  |       |
| Accuracy | 94.74% | 89.22% | 90.05% | 91.34% |
| Precision | 99.60% | 99.58% | 99.49% | 99.57% |
| Recall  | 95.05% | 89.45% | 90.40% | 91.63% |
| F1 Score | 97.25% | 94.04% | 94.46% | 95.25% |

4.2.4 GRU with Word Embedding

In addition to keystroke features, we experiment with some text-base features in our GRU model. This does raise security concerns, since we must record what a user actually types, as opposed to simply using keystroke dynamics. But, we want to determine whether this additional level of detail can result in an improved model.

We use the `nn.Embedding` for word vectors in PyTorch, which provides a mapping between words and their corresponding vectors. The embedding weights can be trained, either by random initialization or by pre-trained word vector initialization. This technique can be used to determine the positional relationship of two keys on the keyboard. For example, keys that are positioned next to each other can be classified as adjacent, and their vector should be similar. Furthermore, other relationships can be determined, such as keys that are pressed with the left hand, as compared to those that are pressed with the right hand.

We implement this word embedding in our GRU model. Note that no CNN model is used in this experiment. We compare the experimental results for different dimensions of word embedding vectors with and without attention. The result of these experiments are summarized in Table 13. Note that embedding weights are trained by random initialization. Unfortunately, this model suffers from overfitting, as can be seen from the graphs in Figure 3.

In an attempt to deal with this overfitting issue, we use Word2Vec [20, 21] to generate vector embeddings. Specifically, we train on a sentence in two directions with random text length from 6 to 12 characters. We find that keys that are close together result in a higher score. For example, A and S, which are adjacent on a standard QWERTY keyboard, have a cosine similarity of 0.9918, while A and P, which are on opposite ends of the keyboard, have a cosine similarity of 0.7891.
The experimental results obtained of comparing random initialization and initialization with pre-trained vectors using a GRU model are shown in Table 14. Again, these results still clearly result in overfitting. When embedding is used, the model can reach a training accuracy of about 0.998, but the loss during testing increases.

When we apply word embedding in the CNN-GRU model, the overfitting issue is resolved—these results are given in Table 15. However, the result of word embedding do not outperform our previous experiment. This result is significant, since it shows that for our free-text dataset, there is nothing to be gained by using the actual text typed by a user, as compared to simply using keystroke dynamics. Since using the text would raise serious privacy concerns, it is beneficial that we do not have to use such data to obtain optimal results.
### Table 15: Word embedding for CNN-GRU

| Model          | Test session | Average |
|----------------|--------------|---------|
| Word-CNN-GRU  | 2            | 91.28%  |
| CNN-GRU       | 2,2,2        | 91.34%  |

#### 4.2.5 CNN-Transformer

Next, we experiment with a transformer technique on our CNN-GRU model, which we refer to as the CNN-Transformer model. Specifically, we apply positional encoding before the encoder layer—the result of this experiment is shown in Table 16. This result is significantly worse than our previous best model, so we do not pursue this approach further.

| Model     | Test session | Average |
|-----------|--------------|---------|
| CNN-Encoder | 89.89% 86.22% 84.97% | 87.03% |

### Table 16: CNN-transformer results

#### 4.2.6 CNN-GRU-Cross-Entropy-Loss

Cross entropy can be used to determine how close the actual output is to the expected output. This loss function combines the two functions of `nn.LogSoftmax()` and `nn.NLLLoss()`. This function is considered useful when dealing with an imbalanced training set, and we have such a dataset.

In this experiment, we change the activation function from `BCEWithLogitsLoss` to `CrossEntropyLoss`. Furthermore, we calculate the output during training and testing with `softmax` and `argmax`, respectively. The result for this experiment is given in Table 17. We see that this is a strong model, indicating that imbalance may be an issue that we should address. Nevertheless, this experiment does not improve on our best results.

| Model                                  | Test session | Average |
|----------------------------------------|--------------|---------|
| CNN-GRU-Cross-Entropy                  | 98.3% 96.7% 95.2% | 96.7%   |
4.2.7 Rotation Subset

To this point, our best model uses the fine-tuning technique discussed in Section 4.2.3. Based on this model, we also consider the so-called rotation subsets of the Buffalo free-text dataset, in which 73 users use different keyboards in different sessions.

In this experiment, we build a multi-classification model on the rotation subset and obtain the result shown in Table 18. Compared to our previous multi-classification results, the classification here is much worse. This is to be expected, since each session of the data is obtained from a different keyboard.

| Model    | Parameters | Accuracy  |
|----------|------------|-----------|
|          | kernel     | out-channel | RNN-size | epochs |           |
| CNN-GRU  | 2          | 96         | 8        | 120,240 | 58.22%   |
|          | 16         | 192        | 64       | 40,80   | 49.16%   |

Next, we use a multi-classification model as a pre-trained model to build binary classifiers, analogous to the fine-tuned models discussed above. The fine-tune results based on the rotation subset is shown in Table 19.

| Model    | Learning rate | Test session | Average |
|----------|---------------|--------------|---------|
|          |               | s0  | s1  | s2  |          |
| CNN-GRU  | 0.001         | 86.9%| 83.7%| 91.1%| 87.2%    |
|          | 0.01          | 89.8%| 86.7%| 93.2%| 89.9%    |

From these results, we observe that the use of different keyboards will likely create serious difficulties for modeling based on keystroke dynamics. Thus, we conclude that different models will be needed for the same user when using different keyboards.

4.2.8 Robustness

We also want to consider the robustness of our models. There are various definitions of robustness, but in general, we want to quantify the effect of a changing environment on a model. There is no standard way to measure robustness for keystroke dynamics. Here, we use a technique known as synthetic minority oversampling technique (SMOTE) to generate synthetic data that has similar characteristics to the training data. We then measure robustness in the sense of how well our models perform on this SMOTE-generated data.
SMOTE is typically applied as a data augmentation technique to an imbalanced dataset. The idea behind SMOTE is to generate similar samples to the training data using a straightforward interpolation approach [8]. The concept of SMOTE is illustrated in Figure 4, where the hollow circles on the right-hand side represent augmented data points that are obtained by interpolating between actual data points.

![Figure 4: SMOTE illustrated](image)

In this set of experiments, we use $6 \times 250$ dimensional array as the feature vector, and use the `imbalance-learn` package in Python package to generate SMOTE data points. First, we use SMOTE to increase the positive samples and apply a “smoothing ratio” of 0.1 which means that we increase in the number of positive samples to 0.1 times the number of negative samples. We also experiment with a smoothing ratio of 0.5. The training and validation results of these experiment are summarized in Table 20.

| Model     | Parameters   | Result        | Test session | Average |
|-----------|--------------|---------------|--------------|---------|
|           | SMOTE ratio  |               | s0  s1  s2   |         |
| CNN-GRU   | 2 2 2        | Validation    | 89.57% 87.56% 87.66% | 88.26% |
|           |              | Test          | 94.74% 89.22% 90.05% | 91.34% |
| 8 0.1     | Validation   | 79.76% 77.91% 77.93% | 78.35% |
|           | Test         | 98.05% 97.39% 96.50% | 97.31% |
| 8 0.5     | Validation   | 73.47% 71.02% 71.32% | 71.94% |
|           | Test         | 98.49% 98.32% 98.07% | 98.26% |

The performance on the SMOTE data shows that after augmenting, the accuracy decreases on the validation set, while the performance on the test set has improved. We speculate that SMOTE adds noise to the positive labels, which worsens the ability of the model to judge positive cases. Moreover, when adding a higher proportion of SMOTE data, the performance on the validation set reduces further, while performance on the test set improves.

We also perform experiments for different ratios of under sampling. That is, we reduce the number of negative samples to a specified proportion of the positive samples. The results of these experiments are shown in Table 21. As expected, these results show minimal change, as compared to the corresponding base models.
Table 21: SMOTE results for CNN-GRU with undersampling

| Model   | Parameters          | Result     | Test session | Average |
|---------|---------------------|------------|--------------|---------|
|         | Parameters          |            | s0           | s1      | s2      |         |
|         | kernel SMOTE ratio  |            |              |         |         |         |
| CNN-GRU | 2,2,2                | Validation | 89.57%       | 87.56%  | 87.66%  | 88.26% |
|         |                     | Test       | 94.74%       | 89.22%  | 90.05%  | 91.34% |
|         | 8                   | Validation | 82.82%       | 81.40%  | 80.80%  | 81.67% |
|         | .1 under            | Test       | 93.61%       | 89.90%  | 90.47%  | 91.33% |
|         | 8                   | Validation | 82.70%       | 80.64%  | 80.49%  | 81.28% |
|         | .5 under            | Test       | 93.38%       | 91.11%  | 89.96%  | 91.48% |
|         | 8                   | Validation | 82.60%       | 81.09%  | 80.77%  | 81.49% |
|         | 1.0 under           | Test       | 93.03%       | 91.17%  | 90.01%  | 91.40% |

We further analyze the precision, recall and F1 score of our models. Note that in these experiments we also perform label switching. As discussed above, label switching may provide a better indication of the utility of a model in the IDS case. The results of these experiments are given in Table 22.

Table 22: SMOTE ratio 0.5 with label-switching

| Metric    | Test session | Average |
|-----------|--------------|---------|
|           | s0           | s1      | s2      |
| Accuracy  | 98.49%       | 98.22%  | 98.08%  | 98.26% |
| Precision | 98.81%       | 98.79%  | 98.81%  | 98.80% |
| Recall    | 99.67%       | 99.42%  | 99.24%  | 99.44% |
| F1 Score  | 99.24%       | 99.10%  | 99.02%  | 99.12% |

Comparing the result for the "label-switch" case in Table 12, we conclude that the higher the SMOTE ratio, the higher the recall, and the lower the precision. This implies that the model is more capable of capturing data with label 0 (which, due to label switching, represents the positive case), but the accuracy of the model’s judging label as 0 is also lower.

4.2.9 Explainability

Next, we briefly consider the “explainability” of our model. That is, we would like to gain some insight into how the model is actually making decisions. Most machine learning techniques are relatively opaque, in the sense that it is difficult to understand the decision-making process. This is especially true of neural network based techniques, and since our model combines multiple techniques, it is bound to be even harder it interpret directly.
Here, we consider local interpretable model-agnostic explanations (LIME) [26] to try to gain insight into the role of the various features in our model. LIME perturbs the input and compares the corresponding outputs. If a small change in an input feature causes the classification to switch, then we can judge the importance of a specific feature to the model’s decision-making process.

The concept behind LIME is illustrated in Figure 5, where the solid black circles and hollow red circles represent two categories, and the blue curve is the decision boundary between the classes. LIME uses a simplified linear model—represented in the figure by the dashed line—to predict the classes. Locally, this linear model will likely be very accurate, although it would typically fail badly globally. By using a simple linear model, we can, for example, more easily determine the most relevant features.

In our LIME experiment, we select user 46 and the “s12-train-s0-test” case. For this experiment, the best validation accuracy we obtain is 96.88% and the best test accuracy is 99.31%.

For the sake of brevity, we omit the details of our LIME experiments but, in summary, we find that LIME indicates that our model focuses more on holding time and difference time. In general, it appears that a good model focuses less on key-id, which indicates that it may not be a good feature to distinguish users.

4.2.10 Equal Error Rate

The equal error rate (EER) is an objective standard to measure classifiers. In a biometric system, the false accept rate (FAR) is the rate at which a user can authenticate as someone else, whereas the false reject rate (FRR) is the rate at which a user cannot authenticate as themselves. When these rates are equal, the value is called equal error rate. The lower the EER value, the higher the accuracy of the biometrics system. In practice, we would likely not set the system parameters so that the FAR is equal to the FRR. For example, in a financial application that requires high security, the FAR should be very low, which necessitates a somewhat higher FRR. Nevertheless, the EER allows us to easily compare different biometric systems.
Here, we use a sigmoid function for output, so that we can obtain the prediction result in the form of a probability. Then we use the prediction and ground-truth to calculate the confusion matrix. After obtaining labels, we construct an ROC curve to obtain the FPR and TPR and, finally, we determine the EER from the ROC curve.

The EER results with s01 for training and s2 for testing for various models discussed above are provided in Table 23. The best EER we obtain is 0.0386, and when we use this model over all sessions we obtain an average EER of 0.0394.

| Model                                      | s01-train-s2-test |
|--------------------------------------------|-------------------|
| Pre-trained word embedding with CNN-GRU    | 0.1091            |
| CNN-Transformer-encoder                   | 0.1257            |
| CNN-GRU-cross-entropy-loss                 | 0.1502            |
| CNN-GRU-without-sampler-at-best-val        | 0.0609            |
| CNN-GRU-without-sampler-at-best-eer        | 0.0611            |
| CNN-GRU-without-sampler-at-non-best-val    | 0.0594            |
| CNN-GRU-with-sampler                       | 0.0826            |
| CNN-GRU-without-sampler-fine-tune          | 0.0412 (0.7187-multi) |
| CNN-GRU-without-sampler-fine-tune          | 0.0386 (0.7599-multi) |

After determining the best result on the baseline subset, we then apply this model to all 148 users. The resulting EER for all subset for different models is shown in Table 24. However, we see that the result is poor, which is apparently due to the rotation subset, where different keyboards are used across sessions, and the fact that some users do not type much data in the baseline subset. Thus, it is more realistic to set a threshold for the key length with different users—in this case, we obtain a best EER result in Table 25. From the last two lines in Table 25, we observe that the model that has the higher multi-classification accuracy results in a lower EER for the fine-tuned case.

| Model                                      | s01-train-s2-test |
|--------------------------------------------|-------------------|
| CNN-GRU-attention-without-sampler          | 0.1389            |
| CNN-GRU-attention-non-without-sampler      | 0.1239            |
| CNN-GRU-fine-tune                          | 0.1029            |

### 4.2.11 Knowledge Distilling

Knowledge distilling is somewhat analogous to explainability. In knowledge distillation we “compress” a model, in the sense that we try to replace a complex model...
with a much simpler one that achieves comparable results. The goal is to extract the essence of a complex model within a much simpler form.

This method knowledge distilling was first proposed in [4]. Then in [12] a “teacher” and “student” model was proposed from the concept of mentoring. The output of the teacher network is used as a soft label to train a student network. For our model, the EER results obtained based on teacher-student knowledge distilling with different parameters are shown in Table 26.

4.2.12 Weighted Loss
In the CNN-GRU fine-tune model, we select BCEWithLogitsLoss as our criterion to calculate the loss. However, we did not specify the parameter of pos-weight which is the weight of positive samples in the original experiment. In this experiment, we use the fine-tune model as a backbone and try to tune the positive weights and compare with our previous results. The results of these experiments are given in Table 27.

Note that the results in Table 27 are average among the three different test sessions. From the result in Table 27, we observe that when the value of pos-weight is 0.1, the precision is best, while the recall rate decreases, as compared to the

### Table 25: Best model for EER (all subsets)

| Model                                      | Test session | Average |
|--------------------------------------------|--------------|---------|
| CNN-GRU-without-sampler-fine-tune          | s0 0.0690 s1 0.0841 s2 0.0557 | 0.0696  |

### Table 26: EER results for knowledge distilling

| Model                      | s01-train-s2-test |
|----------------------------|-------------------|
| Student-1-Teacher-1        | 0.1333            |
| Student-1.5-Teacher-0.5    | 0.1409            |
| Student-1.99-Teacher-0.01  | 0.1762            |
| Student-0.99-Teacher-0.01  | 0.1355            |
| Student-0.5-Teacher-1.5    | 0.0864            |
| Student-0.5-Teacher-1.99   | 0.1097            |
| Student-0.01-Teacher-1.99  | 0.0925            |

Note that in this experiment, we simply use a multi-classification model as the teacher and the corresponding binary classification as the student model. With this type of approach, we hope to see that the teacher can improve the results given by the student model, as indicated by a low EER. However, in our experiments the EER is not competitive with our fine tuning model. Hence, we cannot draw any strong conclusions from this experiment, but this is worth pursuing as future work.
Table 27: Results for tuning pos-weight (baseline subset)

| Metric      | Fine-tune | pos-weight |
|-------------|-----------|------------|
|             |           | 0.1 | 2   | 10  | 50  |
| ERR         | 0.0395    | 0.0428 | 0.0413 | 0.0392 | 0.0813 |
| Accuracy    | 99.33%    | 99.41% | 99.21% | 99.03% | 96.81% |
| Precision   | 78.46%    | 84.57% | 74.82% | 67.51% | 50.87% |
| Recall      | 76.88%    | 69.45% | 78.92% | 83.28% | 82.77% |
| F1 Score    | 74.63%    | 72.92% | 73.40% | 71.64% | 56.64% |
| AUC         | 98.84%    | 98.74% | 98.87% | 98.88% | 98.28% |

original fine-tune model. Moreover, when the value of pos-weight is higher, the precision decreases while the recall increases, which nicely illustrates the inherent trade-off between these measures. Based on these results, we can adjust the value of pos-weight depending on different application scenarios.

4.2.13 Ensemble Models

In this section, we consider three ensemble models which include various combinations of fine-tuning, softmax, and transformer. The results for these cases are given in Table 28. Note that the results in Table 28 are each an average among three different test sessions. Since the results for the softmax and transformer models are much worse than the fine-tune model, the resulting ensembles only improve slightly in terms of precision and recall, and only for some users.

Table 28: Result for ensembles (baseline subset 1)

| Metrics    | Ensemble |
|------------|----------|
|            | fine-tune | softmax | transformers |
| ERR        | 0.082    | 0.0395  | 0.1644       | 0.1449 |
| Accuracy   | 99.28%   | 99.33%  | 96.80%       | 87.03% |
| Precision  | 76.71%   | 78.46%  | 41.69%       | 19.10% |
| Recall     | 78.34%   | 76.88%  | 71.30%       | 76.26% |
| F1 Score   | 74.29%   | 74.63%  | 47.46%       | 23.21% |
| AUC        | 95.18%   | 98.84%  | 84.23%       | 93.37% |

We further ensemble the models with different pos-weight values, with the fine-tune model as the backbone. The parameters of the three ensembles considered, which we denote as models $\mathcal{A}$, $\mathcal{B}$, and $\mathcal{C}$, are specified in Table 29. Note that the results in Table 30 represent the average among the three different test sessions. We observe that the EER, precision, and recall rates all improve with these ensemble techniques.
Table 29: Various model combinations

| Model | Combination                      |
|-------|----------------------------------|
| A     | fine-tune, pos-w 0.1, pos-w 2, pos-w 10, pos-w 50 |
| B     | fine-tune, pos-w 0.1, pos-w 2, pos-w 10 |
| C     | fine-tune, pos-w 0.1, pos-w 10 |

Table 30: Results for ensembles (baseline subset 2)

| Metrics | fine-tune | Model | A | B | C |
|---------|-----------|-------|---|---|---|
| ERR     | 0.0395    | 0.0285| 0.0312 | 0.0322 |
| Accuracy | 99.33% | 99.41% | 99.69% | 99.37% |
| Precision | 78.46% | 81.31% | 82.98% | 82.32% |
| Recall  | 76.88% | 80.92% | 78.79% | 77.99% |
| F1 Score | 74.63% | 78.67% | 78.31% | 77.75% |
| AUC     | 98.84% | 99.28% | 99.24% | 99.18% |

4.2.14 Discussion

Figure 6 summarizes the results of our free-text experiments, both in terms of EER and accuracy. Note that the best accuracy and the best EER were both achieved with the CNN-GRU-without sampler-fine-tune model.

In our experiment, we have applied a sampler to train so as to deal with the situation of imbalanced data. As for feature engineering, we transform the data into a vector which includes the label of the key and the timing features. Then, we compute the mean and variance and center the data, which enable us to achieve better performance.

We perform parameter tuning on the models and obtain a great improvement in accuracy. The result shows that longer keystroke sequence and larger out-channel size generally result in higher accuracy, while more convolutions do not improve our model. After parameter tuning, we apply an attention layer on the outputs of the GRU and find that some users’ accuracy slightly improves. Moreover, we expand the keystroke dynamics features to include rate features. Although the accuracy result of do not greatly improve, the EER does achieve better performance.

We also use a multi-classification model as a pre-trained model for binary classification. The results indicate that such a pre-trained multi-classification model can achieve higher accuracy and a lower EER for the corresponding binary classification model.

Finally, we compare our free-text experiments to previous work. From the results in Table 31, we see that our best model is competitive with the best EER previously obtained, while the accuracy of several of our models exceed 99%.
Figure 6: Accuracies and EER of models (baseline subset)

Table 31: Comparison to previous work for Buffalo free-text dataset

| Research           | Models               | Accuracy | EER  |
|--------------------|----------------------|----------|------|
| Lu, et al. [17]    | CNN-RNN              | —        | 0.0236 |
| Ayotte, et al. [1] | ITAD metrics         | —        | 0.0530 |
| Huang, et al. [14]| SVM                  | —        | 0.0493 |
| Our research       | fine-tune CNN-GRU    | Greater than 99% | 0.0690 |

5 Conclusion and Future Work

In this paper, we developed and analyzed machine learning techniques for biometric authentication based on free-text data. We focused on a novel CNN-GRU architecture, and we experimented with an attention layer, rate features, pre-trained models, ensembles, and so on. The maximum multiclass classification accuracy that we achieved with our model was 99.31%, with an EER of 0.069. As far as we are aware, this is the best accuracy attained to date for the Buffalo free-text dataset, and our EER is competitive with the best results previously obtained. In addition, for our CNN-GRU model, we considered “explainability” and knowledge distillation, among many other relevant topics.

The high accuracy and low EER for our free-text results indicate that passive authentication and intrusion detection may be practical, based on keystroke dy-
namics. That is, in addition to an initial authentication at login time, a user can be periodically re-authenticated by passively monitoring typing behavior. In this way, intrusions can be detected in real-time, with a minimal burden placed on users.

There are many avenues available for future work. For example, we plan to perform extensive model optimization and model fusion. For model optimization, we will consider techniques from contrastive learning and self-supervised technique to see whether these approaches can improve our model.

As another example of possible future work, we plan to evaluate the robustness of our technique using an algorithm known as POPQORN [16]. The idea behind this technique is to observe the effect of outside disturbances to the model and thereby determine its robustness.

Of course, more and better data is always useful, and this is especially true in free-text analysis. Having more realistic and longer-term free-text datasets over a larger number of users would add credence to the results obtained in any research.

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