A Deep Learning Approach for Missing Data Imputation of Rating Scales Assessing Attention-Deficit Hyperactivity Disorder

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A variety of tools and methods have been used to measure behavioral symptoms of attention-deficit/hyperactivity disorder (ADHD). Missing data is a major concern in ADHD behavioral studies. This study used a deep learning method to impute missing data in ADHD rating scales and evaluated the ability of the imputed dataset (i.e., the imputed data replacing the original missing values) to distinguish youths with ADHD from youths without ADHD. The data were collected from 1220 youths, 799 of whom had an ADHD diagnosis, and 421 were typically developing (TD) youths without ADHD, recruited in Northern Taiwan. Participants were assessed using the Conners’ Continuous Performance Test, the Chinese versions of the Conners’ rating scale-revised: short form for parent and teacher reports, and the Swanson, Nolan, and Pelham, version IV scale for parent and teacher reports. We used deep learning, with information from the original complete dataset (referred to as the reference dataset), to perform missing data imputation and generate an imputation order according to the imputed accuracy of each question. We evaluated the effectiveness of imputation using support vector machine to classify the ADHD and TD groups in the imputed dataset. The imputed dataset can classify ADHD vs. TD up to 89% accuracy, which did not differ from the classification accuracy (89%) using the reference dataset. Most of the behaviors related to oppositional behaviors rated by teachers and hyperactivity/impulsivity rated by both parents and teachers showed high discriminatory accuracy to distinguish ADHD from non-ADHD. Our findings support a deep learning solution for missing data imputation without introducing bias to the data.

Keywords: ADHD, oppositional behavior, missing data imputation, deep learning, rating scale, continuous performance test, classifications
INTRODUCTION

Attention-deficit/hyperactivity disorder (ADHD) is a common childhood-onset neuropsychiatric disorder with developmentally inappropriate inattention, hyperactivity, and impulsivity (1, 2). The current epidemiological prevalence rate of ADHD is 9.4% in the USA (3) and 8.7% in Taiwan (4). Children and adolescents with ADHD are at increased risk for academic underachievement (5), behavioral problems at school (5, 6), impaired peer (6–8) and parent-child (9, 10) relationships, emotional dysregulation (11, 12), and oppositional and conduct problems (12, 13). Many individuals with ADHD continue to have ADHD symptoms in adulthood (14), suffer from comorbid psychiatric conditions (15), and have persistent executive dysfunctions (16, 17), social impairments (18), and reduced life quality (18) and health conditions (14). Given its high prevalence and long-term impairment, there is a pressing need for early detection, diagnosis, and intervention of ADHD in youth population. Although clinical diagnosis has been recognized as the gold standard for ascertaining ADHD in clinical practice, attention tests and standardized rating scales measuring ADHD and related symptoms are often used to screen for potential cases of ADHD (19), assist in diagnosis (20), and monitor symptom changes over time (21, 22) or in response to treatment (23–27).

Of the core symptoms of ADHD, hyperactivity and impulsivity are more readily observable than attention problems (19, 28). Given this, rating scales covering inattention symptoms may not adequately capture the attention deficits, especially when rating scales are completed by informants other than the subjects themselves. Thus, objective instruments that measure a wide range of attention performance could be helpful in this case. Due to its simplicity and comprehensive coverage of domains in attention and impulsivity, the continuous performance test (CPT) has been widely used in clinical research to aid in assessments of ADHD (29, 30). CPT is designed to engage subjects in a monotonous and repetitive task over an extended time (usually more than 10 min), e.g., letters “A–Z” appear sequentially on the screen and subjects are instructed to respond if any letter other than the target letter (e.g., “X”) shows up on the screen. This task is simple but requires vigilance and sustained attention. Past research has documented that children with ADHD performed worse on CPT than controls (31, 32), despite some concerns about its psychometric properties and ecological validity (33).

Clinical interview with the child and their caregivers is the gold standard for diagnosing ADHD. Direct observations of the child, neuropsychological and cognitive assessment (e.g., with CPT), and the use of self-administered questionnaires completed by parents and/or teachers (31, 33) can sometimes be helpful to aid in the diagnosis of ADHD. Questionnaires and rating scales are a cost-effective and efficient way to screen for ADHD and related symptoms. The Chinese versions of several internationally recognized ADHD instruments (e.g., the Conners Rating Scales and the Swanson, Nolan, and Pelham, Version IV Scale) have been prepared for this purpose, and their psychometric properties had been established in our previous work (19, 21, 22, 34). Whenever feasible, teachers’ reports should be included, as they provide valuable information about the child’s behavior in relation to other same-age peers. Also, teachers may be more likely than parents to identify attention problems in the classroom because they have more opportunities to observe children doing classroom work and tasks that require sustained attention and concentration (35). Despite the low agreement between parent and teacher reports on ADHD symptoms in western studies (35, 36) and our work (37, 38), it is crucial to integrate reports from different informants. Because parents and teachers see the child in different contexts, they each provide unique, valuable cross-context information about the child, which is important when evaluating the cross-context diagnostic requirement of ADHD. Therefore, in this study, we included data from both parent and teacher reports of ADHD symptoms, in addition to clinical interviews conducted by clinicians/psychiatrists as well as children’s performance on the CPT.

A common methodological issue for data collection in a large survey-based or epidemiology study is missing data (39–43). There are several approaches to handling missing data prior to data analysis (44–47). First, the complete-case approach (listwise deletion), which only includes cases with complete data for the analysis, is the simplest to deal with missing data. However, it significantly reduces power for the analysis and can introduce biases if the excluded subjects are systematically different from those included. Second, missing data can be replaced with the mean of the available cases. This is an easily applied approach, but it reduces the data variability and underestimates both the standard deviations (SD) and variances (45, 48). Third, missing values can be imputed using a regression model where available data from other variables are used to predict the value of a particular variable for which data are missing. However, using regression imputation overestimates the correlations between target variable and explanatory variable and also underestimates variances and covariances (48). Fourth, the hot-deck imputation approach, commonly used in surveys, can be used to identify the respondents who share similar characteristics as the non-respondents and then impute missing data from the resembling respondents (49). Fifth, the inverse probability weighting is a method to calculate statistics of a population different from that in which the data collected. Through estimating sampling probability, this method can be used to expand the weight for subjects who have a significant degree of missing data (50). Lastly, multiple imputations, based on multiple regressions, imputes missing data by creating several different plausible imputed datasets and appropriately combining results obtained from each of them (51). Interested readers are referred to the work of Burton and Altman (44), Eekhout et al. (45), Wood et al. (46), and Pigott (47) for the reviews on different methods for handling missing data.

Most of these proposed imputation techniques may bias study results (49, 52). Inverse probability weighting and multiple imputation have been shown to work well when assumptions of missing completely at random (MCAR) and missing at random (MAR) hold (38, 53, 54). Despite great efforts to solve the missing data problem, none of the abovementioned approaches are fully satisfactory. An approach that does not
bias the estimated parameters is needed. In recent years, researchers have started to apply machine learning to missing data imputation, reporting that machine learning methods outperform traditional statistical methods (e.g., mean imputation, hot-deck, multiple imputations) in handling missing data, resulting in better prediction accuracy of patient outcome (55).

Deep learning, a branch of machine learning methods based on artificial neural network (ANN), has been proposed in the early 1980s (56) but limited in use because of the cost in time and computational resources given the hardware constraints at the time. With the availability of large labeled datasets and Graphics Processing Units (GPUs) which greatly accelerate the computing process in deep learning frameworks, deep learning has started to gain popularity in recent years (57). Deep learning has been applied to various domains such as image classification, speech recognition, and language processing, often outperforming traditional machine learning methods such as support vector machine (SVM). The ability of deep learning to infer abstract, high-level representations makes it a promising approach for the prediction of diagnosis, prevention, treatment, and prognosis of mental illness (58, 59). A few studies have used deep learning to classify disorders, including ADHD, Alzheimer’s disease, and dementia (60–64). Deep learning-based approaches have also been shown to perform well as a missing data imputation method in large, high-dimensional datasets (65, 66).

In this study, we propose an approach based on deep learning to impute missing data in ADHD questionnaires. To the best of our knowledge, this work is the first to apply deep learning to clinical data imputation in ADHD. We combined multiple samples from our previous studies to increase the total sample size (N=1220) and used a deep learning approach to impute the missing data in parent- and teacher-rated ADHD scales. We expect deep learning to be able to impute missing values and generate a complete imputed dataset that resembles the original complete dataset (referred to as the reference dataset) as closely as possible in its ability to distinguish ADHD from TD children. In addition, through the process of this deep learning approach, we can rank the questions of the rating scales in terms of the ability of the machine to learn from the data and to predict the missing values accurately. We hypothesized that questions assessing hyperactivity-impulsivity behaviors, particularly from teacher reports, would have high imputation accuracy and discriminating ability based on previous studies suggesting that these symptoms are observable (67) and that teachers may have more opportunities to observe ADHD-related behaviors such as oppositional defiant symptoms than parents do (35).

MATERIALS AND METHODS

Sample and Procedures
The sample consisted of 799 youths with a clinical diagnosis of ADHD (689 boys, 86.2%) according to DSM-IV diagnostic criteria and 421 typically developing (TD) youths (343 boys, 81.5%). The sample came from two separate studies – a longitudinal study of adolescent outcomes in children with ADHD aged 11-16 years (192 ADHD and 142 TD) conducted during 2006-2009 and a genetic, treatment, and imaging study of drug-naïve children and adolescents with ADHD aged 6-18 years (607 ADHD and 279 TD) conducted during 2007-2015. Youths with ADHD were recruited from the child psychiatric clinic in National Taiwan University Hospital (NTUH), Taipei, Taiwan. The TD youths without a lifetime diagnosis of ADHD were recruited from the same school districts as youths with ADHD via the help of school principals and teachers. All the participants and their parents were interviewed using the Chinese version of the Kiddie Epidemiologic Version of the Schedule for Affective Disorders and Schizophrenia (2) to confirm the presence or absence of ADHD diagnoses and other psychiatric disorders. Participants with major medical conditions, psychosis, depression, autism spectrum disorder, or a Full-Scale IQ score less than 70 were excluded from the study.

Participants’ IQ and attention were assessed using the Weschler Intelligence Scale for Children-3rd edition (WISC-III) (68) and Conner’s CPT (CCPT) (69), respectively. Participants’ parents and teachers completed questionnaires assessing the core symptoms of ADHD and related symptoms such as oppositionality by using the Chinese version of the Conners’ parent and teacher rating scales-revised: short form (CPRS-RS/CTRS-RS) (19, 34) and the Chinese version of the Swanson, Nolan, and Pelham, version IV scale (SNAP-IV) reported by parents (22) and teachers (21). These scales have been widely used in the screening for ADHD or measuring the intervention/treatment effect in clinical, community, and research settings (6, 19, 32, 70–76). Given that symptoms of oppositional defiant disorder (ODD) are included in all these scales and ODD symptoms are highly associated with ADHD and easily observed by teachers and parents (77), we included ODD items in the analyses and further hypothesized that ODD symptoms reported by teachers can distinguish ADHD from non-ADHD. These studies were approved by the Research Ethics Committee of National Taiwan University Hospital, Taipei, Taiwan (Approval numbers: 200612114R, 200812153M, 9361700470; ClinicalTrials.gov number: NCT00529906, NCT00916786, NCT00417781) before study implementation. The data were collected after the participants, their parents, and their teachers provided written informed consent.

Measures

The Chinese Version of the Kiddie Epidemiologic Version of the Schedule for Affective Disorders and Schizophrenia (Chinese K-SADS-E)
The K-SADS-E is a semi-structured interview scale for a systematic assessment of both past and current mental disorders in children and adolescents. The Chinese version of K-SADS-E was developed by the Child Psychiatry Research Group in Taiwan (2, 78). To ensure that the DSM-IV diagnostic criteria and language were culturally appropriate and sensitive for the Taiwanese child and adolescent populations, the development of this instrument included two-stage translation and modification of several items with...
psycholinguistic equivalents. This scale has been widely used in child and adolescent clinical research in Taiwan [e.g., (75, 79, 80)].

The Conners’ Continuous Performance Test (CCPT)
The CCPT is a 14-minute, non-X type test design for ages 6 and up (81). Participants are asked to press the space bar when a character (target) shows up on the screen, except when the X (non-target) shows up. There are six blocks in CCPT, with three sub-blocks in each block. Each sub-block has 20-letter presentations. The sub-blocks differ in Inter-Stimulus Intervals (ISIs) of 1, 2, and 4 s, and the sequence of ISI conditions presents randomly. There are 12 indices covering different domains of CCPT performances: (1) Omission errors: the number of times the target is missed; (2) Commission errors: the number of times X is hit; (3) Variability: intra-individual variability in reaction time; (4) Perseveration: a reaction time less than 100 ms; (5) Detectability: the ability to distinguish X from non-X letters; (6) Reaction Time (RT): the period of time between the presentation of the stimulus and the response; (7) Hit RT Standard Errors (Hit RT SE): consistency of response time; (8) Response Style: a function of the ratio of hit target to hit non-target stimuli; (9) Hit RT change by blocks (Hit RT BC): the slope of change in RT over six blocks as the test progresses; (10) Standard error of Hit RT change by blocks (Hit RT SE BC); (11) Hit RT changed by ISIs (Hit RT ISI Change); (12) Standard error of Hit RT changed by ISIs (Hit SE ISI Change). Indices of CCPT can be grouped into several dimensions (82): (1) Focused attention: RT, Hit RT SE, detectability, and omission errors; (2) Sustained attention: Hit RT BC and Hit RT SE BC; (3) Hyperactivity/impulsivity: commission errors, RT, response style, and perseverations; (4) Vigilance: Hit RT ISI Change and Hit SE ISI Change. We used all 12 indices in this study.

The Chinese Version of the Swanson, Nolan, and Pelham, Version IV Scale (SNAP-IV)
The Chinese SNAP-IV form is a 26-item scale rated on a 4-point Likert scale with 0 for not at all (never), 1 for just a little (occasionally), 2 for quite a bit (often), and 3 for very much (very often). There are nine items for inattention (item 1–9) and nine items for hyperactivity/impulsivity (item 10–18) of the core symptoms of ADHD and eight items for the ODD symptoms according to the DSM-IV symptom criteria for ADHD and ODD (77). The psychometric properties of Chinese SNAP-IV Parent (22) and Teacher Form (21) have been established in Taiwan, and the scales have been frequently used to assess ADHD and ODD symptoms in clinical and research settings [e.g., (32, 73–76)].

The Chinese Version of the Conners’ Parent and Teacher Rating Scales-Revised: Short Form (CPRS-R:S/CTRS-R:S)
The Conners’ Rating Scales (CRS), developed in 1969, have been widely used for screening and measuring ADHD symptoms (83–86). We used the short version in this study – the 27-item Conners’ Parent Rating Scales-Revised: Short Form (CPRS-RS) and the 28-item Conners’ Teacher Rating Scales-Revised: Short Form (CTRS-RS). Both forms have four different subscales: Cognitive problems/Inattention, Hyperactivity-Impulsivity, Oppositionality, and ADHD Index. All the items were rated on a 4-point Likert scale with 0 for not at all (never), 1 for just a little (occasionally), 2 for quite a bit (often), and 3 for very much (very often). These scales are reliable and valid instruments for measuring ADHD-related symptoms (6, 19, 70–72).

Quantity of Missing Data
We combined samples from two studies on ADHD. A total of 1220 youths completed CCPT assessments, of which 787 (64.5%) had SNAP-IV parent form, 575 (47.1%) had SNAP-IV teacher form, 995 (81.6%) had CPRS-R:S, and 729 (59.8%) had CTRS-R:S, and 462 (37.9%) had all four rating scales (see Table 1). Our goal is to use the CCPT data and the remaining complete scales to impute missing values for the incomplete scales.

Deep Neural Network for Missing Data Imputation
The interior architecture we used here is deep neural networks (DNN), which stacked modules that have multiple hidden layers and many neurons (87). It is also known as multi-layer perceptron (MLP), which is ANN mimicking human brains (88). DNN uses gradient descent with backpropagation to train the algorithm, making the training process more efficient (89, 90). In this study, we designed an iteration framework to

| TABLE 1 | Data distribution for the ADHD and TD groups. |
|-----------------|------------------|------------------|------------------|
| Number of Scales Completed | ADHD group (n = 799) | TD group (n = 421) |
| | Boys (n = 689) | Girls (n = 110) | Boys (n = 343) | Girls (n = 78) |
| Single scale | CPRS-R:S | 42 | 8 | 20 | 1 |
| | CTRS-R:S | 2 | 1 | 8 | 2 |
| | SNAP-I-P | 11 | 2 | 0 | 0 |
| | SNAP-I-T | 1 | 1 | 0 | 0 |
| Dual scales | CPRS-R:S, CTRS-R:S | 112 | 18 | 54 | 20 |
| | CPRS-R:S, SNAP-I-P | 129 | 22 | 38 | 10 |
| | CPRS-R:S, SNAP-I-T | 0 | 0 | 0 | 0 |
| | CTRS-R:S, SNAP-I-P | 1 | 0 | 0 | 0 |
| | CTRS-R:S, SNAP-I-T | 9 | 0 | 6 | 0 |
| | SNAP-I-P, SNAP-I-T | 42 | 8 | 0 | 0 |
| Triple scales | CPRS-R:S, CTRS-R:S, SNAP-I-P | 15 | 4 | 2 | 0 |
| | CPRS-R:S, CTRS-R:S, SNAP-I-T | 3 | 2 | 0 | 0 |
| | CPRS-R:S, SNAP-I-P, SNAP-I-T | 26 | 4 | 2 | 1 |
| | CTRS-R:S, SNAP-I-P, SNAP-I-T | 6 | 1 | 1 | 0 |
| Quad scales | CPRS-R:S, CTRS-R:S, SNAP-I-P, SNAP-I-T | 222 | 33 | 170 | 37 |
| Completed scales with missing value detected | 68 | 6 | 42 | 7 |

Each element shows the number of participants who completed different scales included in this study. ADHD, attention-deficit/hyperactivity disorder; TD, typically developing; CPRS-R:S, the Chinese version of the Conners’ parent rating scales-revised: short form; CTRS-R:S, the Chinese version of the Conners’ teacher rating scales-revised: short form; SNAP-I-P, the Chinese version of the Swanson, Nolan, and Pelham version IV scale, parent form; SNAP-I-T, the Chinese version of the Swanson, Nolan, and Pelham version IV scale, teacher form.
impute the ADHD data (see Figure 1). We used the 12 indices on the CCPT as the features of the initial training feature to start the imputation process. First, the DNN was used with all the questions of the four ADHD rating scales to identify the question with the highest accuracy to impute the missing values. Then this particular question was merged into the initial training set such that our training set now has one more feature to predict the next question. After these steps, the process moved back to the initial step and identified the next question with the highest predictability, iteratively.

Figure 2 shows our neural network architecture design, which included one input layer, 15 hidden layers, and one output layer. The number of neurons in the input layer started at 12 and increased by one with each iteration. The number of neurons in each hidden layer changed according to the number of input layer’s neurons. There was a total of 15 hidden layers divided into three groups: the beginning five hidden layers had twice the number of neurons of the input layer; the middle five hidden layers had the same number of neurons of the input layer; the last five hidden layers had half the number of neurons of the input layer. Since all scales are on a four-point Likert scale, we had four neurons in the output layer to represent the four possible scores. All layers’ activator, except for the output layer, was the Rectified Linear Unit (ReLU), which is one of the most common activators in deep learning (91), given its calculation speed, convergence speed and that it is gradient vanishing free. For the output layer, we chose the Softmax function, which converted values to probabilities for the four-point classification (92). To evaluate learning performance, we set up an SVM classification (93) to classify ADHD and TD after each iteration.

Deep learning has raised several concerns about hyper-parameters, which affect the speed and quality of the learning process (94, 95). One primary concern about deep learning is overfitting. To prevent this problem, we inserted dropout regularization in every layer (95). It will randomly abandon neurons after updating the weight of each layer. In addition, the iteration was optimized by adding early stopping and changing the batch size. The early stopping has a hyper-parameter called patience. If the training performance stopped improving after a certain number (defined as patience) of the pre-defined epoch (i.e., out of patience), training would stop. The patience of early stopping can significantly affect the whole process time, and batch size can affect model convergence speed; these methods not only can further prevent overfitting but also reduce unnecessary calculation (96). Specifically, we trained the algorithm using different combinations of parameters to find the best combination for our data. First, we used an early stopping function and picked patience on 10 and 100 epochs for this study. Larger epochs give the machine more steps to improve accuracy. Second, we set dropout rate at 20%, 25%, and 50% to evaluate overfitting (95). Lastly, we ran several different batch sizes to examine how batch size influenced deep learning algorithms (97–99). Batch Gradient Descent is where the batch size is equal to the size of the training set; batch size between 1 and the size of the training set is called Mini-Batch Gradient...
Descent (we used batch size=8 for the Mini-Batch). We also used a Stochastic Gradient Descent, where the batch size is one. The gradient and the neural network parameter updated after each batch sample. Because the Stochastic Gradient Descent (with batch size=1) needs lots of time to process, we only ran this with ten epochs for early stopping and 25% dropout rate.

Effectiveness Evaluation
We imputed missing data with the DNN analysis. After that, we conducted SVM classification (93) with the imputed data to distinguish between the ADHD and TD groups. SVM is a reliable machine learning classifier that has been used in many different clinical studies to classify disorders (100–103). By observing the classification score during every iteration, we found that the predictive power changed through our data imputation. After we finished missing data imputation, we used the imputation dataset and the reference dataset to run SVM classification with 10-fold cross-validation and then compared the prediction accuracy of the two datasets by using independent t-tests.

RESULTS

Missing Data Imputation
Classification Accuracy Over Iterations
At the end of each iteration, we conducted SVM classification to classify ADHD and TD and recorded the classification accuracy. The classification accuracy increased from 72% to 90% from the first iteration to the last iteration. Despite some differences in classification accuracy in the middle of the whole iteration process, the accuracy of all the models (with different hyper-parameters) increased throughout iterations and achieved similar accuracy at the end of iterations (see Figure 3A).

Imputation Accuracy Over Iterations
Figure 3B presents the imputation accuracy after each iteration (when a question with the highest accuracy was identified, and its missing value was imputed and merged into the original training set) by different combinations of hyper-parameters. Results showed that accuracy decreased with iterations in all hyper-parameters. The dropout rate was the most influential contributor to the imputation accuracy, i.e., the model with a higher dropout rate had lower accuracy than those with a lower dropout rate in the same iteration. Batch size also influenced the imputation accuracy, i.e., the Stochastic approach has the lowest imputation accuracy even when used with a low dropout rate.

Time Cost
Figure 3C presents the processing time required for each iteration by different combinations of hyper-parameters. Results showed that as batch sizes decreased, the processing time increased. Batch mode was the most time-efficient.

Effectiveness Evaluation
To evaluate the success of imputation, we used SVM classification to examine the ability of the imputed dataset (n =758, 62.1%), estimated with different combinations of hyper-parameters, to classify between the ADHD vs. TD groups. We then conducted independent t-tests to compare the classification accuracy of each of these datasets to that of the reference dataset i.e., the original dataset.
for which all the four scales were complete (n=462, 37.9%). Results showed that different imputed datasets shared similar mean accuracy (0.89 to 0.90), which was not significantly different from the reference dataset (accuracy = 0.89) (see Table 2). Among the imputation datasets, we did not observe much difference in accuracy between datasets imputed with different dropout rates and batch sizes, suggesting that these factors did not influence the predictive power of the imputed data to distinguish ADHD from TD.

### Imputation Order of Questions
All the items (107 in total) in the four scales were categorized into three groups by the imputation order (see Supplementary Table 1): (1) Top group: items that had high discrimination accuracy and were picked up by the machine early (35 items), (2) Bottom group: items that had low accuracy and did not become a target for imputation until other items with higher imputed accuracy were picked (35 items), and (3) Intermediate group (37 items).

Top group: Both parent and teacher reports on questions assessing oppositional behaviors such as “spiteful or vindictive” demonstrated the highest ability to discriminating ADHD from TD. Moreover, questions assessing hyperactive-impulsive symptoms, such as “leaves seat,” “runs about or restless,” and “impatient,” were also included in this group. Some questions reported only by the teachers were also in this group e.g., “argues with adults,” “actively defies or refuses adult requests or rules,”

### TABLE 2 | Classification accuracy of attention-deficit/hyperactivity disorder (ADHD) vs. typically developing (TD) controls in models with different combinations of hyper-parameters (early stopping, batch size, and dropout rate).

| Hyper-parameter | ATCACC       | p-value |
|-----------------|--------------|---------|
| The original group with the completed dataset | 0.8931 ± 0.0215 | 0.415   |
| ES=100, BS=Batch, D=0.25 | 0.8859 ± 0.0142 | 0.523   |
| ES=100, BS=Batch, D=0.5  | 0.8987 ± 0.0139 | 0.585   |
| ES=100, BS=Batch, D=0.25 | 0.8954 ± 0.0164 | 0.484   |
| ES=10, BS=Batch, D=0.25 | 0.8918 ± 0.0113 | 0.906   |
| ES=10, BS=Batch, D=0.25 | 0.8921 ± 0.0010 | 0.216   |

Results presented as means ± standard deviations. Independent t-tests were used to compare the classification accuracy between the imputed and reference datasets. ATCACC, ADHD/TD classification accuracy; ES, early stopping patience; BS, batch size; D, dropout rate.
“is angry and resentful” and “avoids, expresses reluctance about, or has difficulties engaging in tasks that require sustained mental effort (such as schoolwork or homework).”

Intermediate group: Most questions included in this group were about inattention e.g., “cannot pay attention,” “fails to finish work,” “disorganized,” “cannot concentrate,” “distractible,” “not reading up to par,” “poor in arithmetic,” and “forgets things he or she has already learned.” Several impulsive questions, such as “intrudes on others” and “blames others for his or her mistakes,” were also included in this group.

Bottom group: Both parent and teacher reports on questions such as “talks excessively,” “only pays attention to things he/she is interested in,” “loses things,” and “makes careless mistakes” did not have high discriminatory accuracy. In contrast to the high accuracy of teacher reports of several oppositional behaviors, parent reports on these questions fell into this group.

DISCUSSION

The current study, to the best of our knowledge, is the first work using deep learning to impute missing data in ADHD-related rating scales. Three main findings emerged. First, missing data can be imputed using deep learning with high accuracy and that the imputed dataset had a similar, high discriminatory ability to distinguish between the ADHD and TD groups compared to the complete original dataset. Second, our approach generated an imputation order of questions, demonstrating that teacher-reported oppositional symptoms and both teacher- and parent-reported hyperactivity-impulsivity symptoms were highly discriminating symptom clusters to distinguish between the ADHD and TD groups. Third, changing hyper-parameters in deep learning affects the analysis processes and results i.e., deep learning performance is sensitive to hyper-parameters. This study focuses on manipulating batch size, dropout rate, and early stopping. By changing these hyper-parameters, we partially verified some previous findings suggesting that batch size and early stopping have a large effect on processing time and that the dropout rate is the most relevant hyper-parameter for predictive power (97–99, 104).

With our approach, the missing data can be imputed using deep learning, and the imputed dataset has the same high discriminatory ability as the original complete dataset (i.e., the reference dataset). Our results provide strong evidence to support that our imputation not only generated the dataset without missing values but also kept the imputed and reference datasets consistent. Of note, one novelty of this deep learning approach is that we let the machine impute missing data for the whole sample combining the ADHD and TD groups. Previous studies typically only focus on one group imputation at a time, given concerns about biasing the subsequent analyses when combining the case and the control groups during the imputation process (66, 105, 106). For example, combining the two groups may decrease differences and increase the similarity between the case and control groups in terms of the distribution of features. In contrast, imputing missing value separately by groups may introduce bias to the distribution of features, enlarge the group difference (107), and lead to increasing discriminatory ability after imputation. As a result, if new data are added later on, the discriminatory ability might drop because the feature distribution of the imputed dataset is not representative of the original dataset. Our method represents a novel solution to impute missing data while maintaining the discriminatory ability of the imputed dataset to distinguish between the ADHD and non-ADHD groups. This strategy can also ensure that when new data are available at a later time, they can be readily added to and mixed with the imputed data.

This study imputed 45,229 missing values. Each question has a different amount of missing data. About 200 participants had one or two missing questions, and more than 600 participants had missing data in some questions of the four scales. Our result showed that there is no relation between the order of missing data imputation and the amount of missing data in the questions. Even though the original dataset has about 60% missing items across the four scales, our finding showed that the machine could still learn from this dataset. What matters more is to have questions that are highly discriminative between ADHD and non-ADHD. If a question lacks discriminative ability but has minimal amount of missing data, our algorithm would select another question that has higher discriminative ability because the machine would always pick the best feature in each iteration. Our classification accuracy between the ADHD and TD groups increased rapidly at the beginning of the iteration after the missing values for the highly-discriminative questions were imputed. At the end of the iteration, the imputed dataset had the same classification accuracy and distribution compared to the original complete dataset (reference dataset). The most critical issue of data imputation is the bias that it may introduce, ultimately affecting the inferences that can be drawn from the analysis conducted with the imputed dataset. We also compared our classification accuracy with other imputation methods (i.e., interpolate imputation, mean imputation, and multiple imputation). Results indicated that deep learning approach have higher accuracy than traditional statistical imputation methods (see Supplementary Table 2). Our results suggest that deep learning can be a robust and reliable method for handling missing data to generate an imputed dataset resembling the reference dataset and that subsequent analyses conducted with the imputed data showed consistent results with those from the reference dataset.

Imputation order is another important finding of this study. The high-order questions, relative to the low-order ones, are assumed to have higher discriminant validity to differentiate children with ADHD from those without ADHD. Consistent with our hypotheses, our results showed that most of the hyperactivity-impulsivity questions, from both teacher and parent reports, fell into the high-order group. Hyperactive-impulsive behaviors, the “externalizing” features of ADHD, are easily observed in various settings. For example, behavioral descriptions such as “leaves the seat,” “fidgety,” and “runs about or climbs” provide specific...
behaviors for parents and teachers to rate the child in a precise manner. This may be why these hyperactivity-impulsivity questions have high discriminatory validity. However, when hyperactive questions were worded metaphorically such as “restless in the squirmy sense,” “acts as if driven by a motor,” and “talks excessively,” parents and teachers seemed to have a hard time providing valid ratings as indexed by the low discriminatory accuracy of these questions.

Interestingly, we found that almost all oppositional questions from the teacher report were categorized into the high-order group, whereas oppositional questions from the parent report were in the low-order group (67). That is, according to these internationally well-known standardized scales used in our ADHD studies, teacher reports of oppositional symptoms had better discriminant validity in distinguishing ADHD from non-ADHD. One possible explanation is that the classroom teachers, in general, spend more time with the students than parents do and are more likely to observe oppositional symptoms of the index children against a group norm of the same-age peers (6). Given the high co-occurrence between ADHD and ODD symptoms, this may be why teachers’ observations of children’s ODD symptoms had better discriminant validity in distinguishing ADHD from non-ADHD.

Our goal is to impute the missing data of the scales; however, there are some of items in the scales designed for screening ODD symptoms, which are not ADHD symptoms but highly co-occurring with ADHD (CPRS-RS: 2,6,11,16,20,24; CTRS-RS: 2,6,10,15,20; SNAP-IV-P: 19-26; SNAP-IV-T: 19-21,23-26,29). We also conducted analyses without the ODD symptoms (see Supplementary Figure 1). The ADHD/TD classification accuracy showed no difference between our original results with ODD symptoms included and the results with ODD symptoms excluded (see Supplementary Table 3). Comparing the imputation orders with the results with ODD symptoms (see Supplementary Table 1 and Supplementary Table 4) and those without ODD symptoms (see Supplementary Table 3 and Supplementary Table 5), the imputation order of the same items across the two sets of analyses did not change. Our findings of no differences in the imputation orders of other symptoms rather than ODD symptoms between the two analyses suggest that removing ODD items did not affect machine classification, and removing some of the items from the scales did not affect the machine’s ability to learn.

Of note, both parent and teacher reports of inattention questions showed low discriminatory accuracy (108). One possible explanation, as described in the introduction, is that inattention is more difficult to observe than other externalizing symptoms. In addition, every child forgets things or is careless occasionally. Therefore, these types of behaviors may be viewed as normative by parents and teachers (109, 110). However, one exception is that “avoids, expresses reluctance about, or has difficulties engaging in tasks that require sustained mental effort (such as schoolwork or homework)” reported by the teachers on the SNAP-IV was included in the high order group. This suggests that teachers’ evaluation and observation of an index student’s schoolwork and submitted homework as compared to same-age students at the school can distinguish ADHD from non-ADHD.

Our results also showed that changing hyper-parameters (e.g., batch size, dropout rate) in deep learning may affect the performance of the algorithm. We processed with different batch sizes (Batch [size=training set], Mini-batch [size=8], and Stochastic [size=1]) to evaluate the outcomes of the discriminatory accuracy, a hot topic in the deep learning field (97–99, 104). We found that across various sizes of the batch, the discriminative ability to separate ADHD from TD reached the same accuracy after missing data imputation. That is, decreasing batch sizes did not improve the accuracy further, but took much longer to process with deep learning. Batch mode is the most time-efficient. Although Mini-batch requires less memory during processing, hardware advances today have afforded us the memory required for deep learning, making Mini-batch not advantageous over other batch sizes in this aspect. We also processed with Stochastic (batch size=1) to verify the idea of online learning performance (111). The outcome of this showed that the performance was not on par with the mini-batch mode during every iteration of the imputation process, and it took more time to converge than the batch mode. In summary, batch mode allows the machine to compute the gradient over the entire dataset, leveraging an abundant amount of information to find a proper solution more efficiently.

There are several methodological limitations in our study. First, due to the architecture based on the deep learning approach, the larger the size of data is, the more thoroughly the machine can learn. Although our sample size is more than 1,000, this may not be sufficiently large for deep learning. However, for the clinical data with excellent quality and internal validity collected from a single site, our sample size is rather large. Second, our imputation approach combined the ADHD and TD groups, resulting in the machine having to learn more varying values in each feature with a limited sample size. Hence, future research with larger sample sizes is also warranted in this aspect. Third, although our imputed dataset had the same accuracy as the original complete data in classifying the ADHD and TD groups, there is no guarantee that the imputed values are “accurate.” Indeed, our results showed that the predictive power (i.e., the accuracy in predicting the rating scale scores) decreased over time with iterations. This suggests that the machine performed poorly for some items, especially when imputing missing scores for the bottom third of the questions. Fourth, although we used the clinician’s diagnosis (which is based on observations and interviews of the patient as well as interviews with the parent/caregiver) as the outcome to evaluate the effectiveness of imputation and parent questionnaires as part of the features for imputation, the shared variance from parent reports either through answering questions from the clinician or as self-response to the questionnaires is a methodological limitation and potential confounder. Future investigation is warranted to add more features from other informants, e.g., participant’s self-reports, peers reports, or other objective measures. Lastly, although we designed flexible neuron size of each hidden layer to adapt to the number of increasing neurons needed for each input layer, as the number of hidden layers is static, it might lead the last few iterations of imputed output layer to over converge than expected.
CONCLUSIONS
We present a novel approach to impute missing data in ADHD rating scales based on deep learning using participants’ neuropsychological data and ADHD-related behaviors assessed with four scales reported by parents and teachers. Our deep learning approach can impute missing data with both the case and control groups together in the dataset. Our findings provide evidence that our deep learning approach can impute missing data with high accuracy in an aggregated dataset from multiple samples and thus can increase the size of the dataset while maintaining the characteristics and representativeness of the data’s original distribution.

DATA AVAILABILITY STATEMENT
The raw data supporting the conclusions of this article will be made available by the corresponding author only if this request is approved by the Research Ethics Committee of National Taiwan University Hospital, Taipei, Taiwan, according to the current regulation of patient protection in Taiwan.

The datasets used in the analysis were collected using the grants support to the corresponding author (SS-FG) mentioned in the acknowledgments section. The data are available upon request. The studies were preregistered at ClinicalTrials.gov number: NCT00529906 (NSC96-2628-B-002-069-MY3), NCT00916786 (NSC98-2314-B-002-051-MY3), and NCT00417781 (NHRI-EX94-98-9407PC).

ETHICS STATEMENT
The studies involving human participants were reviewed and approved by the Research Ethics Committee of National Taiwan University Hospital, Taipei, Taiwan, according to the current regulation of patient protection in Taiwan. The studies were preregistered at ClinicalTrials.gov number: NCT00529906 (NSC96-2628-B-002-069-MY3), NCT00916786 (NSC98-2314-B-002-051-MY3), and NCT00417781 (NHRI-EX94-98-9407PC).

ACKNOWLEDGMENTS
The data collection is supported by the Ministry of Science and Technology (NSC96-2628-B-002-069-MY3; NSC98-2314-B-002-051-MY3) and the National Health Research Institute (NHRI-EX94-98-9407PC). The manuscript preparation is supported by the Ministry of Science and Technology (MOST106-2314-B-002 -104 -MY3) and the National Health Research Institute (NHRI-EX108-10404PI). We thank all the participants, their parents, and school teachers who participated in our study and the research assistants for their help on data collection.

SUPPLEMENTARY MATERIAL
The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fpsyt.2020.00673/full#supplementary-material

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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