Abstract
Decisions made by machine learning systems have increasing influence on the world, yet it is common for machine learning algorithms to assume that no such influence exists. An example is the use of the i.i.d. assumption in content recommendation. In fact, the (choice of) content displayed can change users’ perceptions and preferences, or even drive them away, causing a shift in the distribution of users. We introduce the term auto-induced distributional shift (ADS) to describe the phenomenon of an algorithm causing a change in the distribution of its own inputs. Our goal is to ensure that machine learning systems do not leverage ADS to increase performance when doing so could be undesirable. We demonstrate that changes to the learning algorithm, such as the introduction of meta-learning, can cause hidden incentives for auto-induced distributional shift (HI-ADS) to be revealed. To address this issue, we introduce ‘unit tests’ and a mitigation strategy for HI-ADS, as well as a toy environment for modelling real-world issues with HI-ADS in content recommendation, where we demonstrate that strong meta-learners achieve gains in performance via ADS. We show meta-learning and Q-learning both sometimes fail unit tests, but pass when using our mitigation strategy.

1. Introduction
Consider a content recommendation system whose performance is measured by accuracy of predicting what users will click. This system can achieve better performance by either 1) making better predictions, or 2) changing the distribution of users such that predictions are easier to make. We propose the term auto-induced distributional shift (ADS) to describe this latter kind of distributional shift, caused by the algorithm’s own predictions or behaviour (Figure 1).

ADS are not inherently bad, and are sometimes even desirable. But they can cause problems if they occur unexpectedly. It is typical in machine learning (ML) to assume (e.g. via the i.i.d. assumption) that (2) will not happen. However, given the increasing real-world use of ML algorithms, we believe it is important to model and experimentally observe what happens when assumptions like this are violated. This is the motivation of our work.

Figure 1. Distributions of users over time. **Left:** A distribution which remains constant over time, following the i.i.d assumption. **Right:** Auto-induced Distributional Shift (ADS) results in a change in the distribution of users in our content recommendation environment. (see Section 7.3 for details).

In many cases, including news recommendation, we would consider (2) a form of cheating—the algorithm changed the task rather than solving it as intended. We care which means the algorithm used to solve the problem (e.g. (1) and/or (2)), but we only told it about the ends, so it didn’t know not to ‘cheat’. This is an example of a specification problem (Leike et al., 2017; Ortega et al., 2018): a problem which arises from a discrepancy between the performance metric (maximize accuracy) and “what we really meant”: to maximize accuracy via (1), which is difficult to encode as a performance metric.

Ideally, we’d like to quantify the desirability of all possible means, e.g. assign appropriate rewards to all potential strategies and “side-effects”, but this is intractable for real-world settings. Using human feedback to learn reward functions which account for such impacts is a promising approach to specifying desired behavior (Leike et al., 2018; Christiano et al., 2017). But the same issue can arise whenever human feedback is used in training: one means of improving performance could be to alter human preferences, making them easier to satisfy. Thus in this work, we pursue a complementary approach: managing learners’ incentives.
A learner has an **incentive** to behave in a certain way when doing so can increase performance (e.g., accuracy or reward). Informally, we say an incentive is **hidden** when the learner behaves as if it were not present. But we note that changes to the learning algorithm or training regime could cause previously hidden incentives to be revealed, resulting in unexpected and potentially undesirable behaviour. Managing incentives (e.g., controlling which incentives are hidden/revealed) can allow algorithm designers to disincentivize broad classes of strategies (such as any that rely on manipulating human preferences) without knowing their exact instantiation.\(^1\)

Our goal in this work is to provide insight and practical tools for understanding and managing learners’ incentives, specifically **hidden incentives for auto-induced distributional shift**: HI-ADS. To study the conditions which cause HI-ADS to be revealed, we present unit tests for detecting HI-ADS in supervised learning (SL) and in reinforcement learning (RL). We also create an environment which models ADS in news recommendation, to illustrate the potential effects of revealing HI-ADS in this setting.

The unit tests both have two means by which the learner can improve performance: one which creates ADS and one which does not. The intended method of improving performance is one that does not induce ADS; the other is ‘hidden’ and we want it to remain hidden. A learner “fails” the unit test if it nonetheless pursues the incentive to increase performance via ADS. The SL unit test provides an illustrative example. It is a prediction problem with two targets, mean-zero Gaussians. The intended means of improving performance is to make good predictions (i.e. predict \(\{0, 0\}\)). However we create an incentive for ADS: a prediction of \(>0.5\) for the first target will reduce the variance of the second target, reducing future loss. A learner fails the unit test to the extent it predicts \(>0.5\) for the first target.

In both the RL and SL unit tests, we find that ‘vanilla’ learning algorithms (e.g. minibatch SGD) pass the test, but introducing an outer-loop of meta-learning (e.g. Population-Based Training (PBT) (Jaderberg et al., 2017)) can lead to high levels of failure. We find results consistent with our unit tests in the content recommendation environment: recommenders trained with PBT create earlier, faster, and larger drift in user interests, and for the same level of performance, create larger changes in the user base. These results suggest that failure of our unit tests indicates that an algorithm is prone to revealing HI-ADS in other settings.

Finally, we propose and test a mitigation strategy we call **context swapping**. The strategy consists of rotating learners through different environments throughout learning, so that they can’t see the results or correlations of their actions in one environment over longer time horizons. This effectively mitigates HI-ADS in our unit test environments, but did not work well in content recommendation experiments.

### 2. Background

#### 2.1. Meta-learning and population based training

**Meta-learning** is the use of machine learning techniques to learn machine learning algorithms. This involves instantiating multiple learning scenarios which run in an **inner loop** (IL), while an **outer loop** (OL) uses the outcomes of the inner loop(s) as data-points from which to learn which learning algorithms are most effective (Metz et al., 2019). The number of IL steps per OL step is called the **interval**.

Many recent works focus on multi-task meta-learning, where the OL seeks to find learning rules that generalize to unseen tasks by training the IL on a distribution of tasks (Finn et al., 2017; Ren et al., 2018; Andrychowicz et al., 2016). Single-task meta-learning includes learning an optimizer for a single task (Gong et al., 2018), and adaptive methods for selecting models (Kalousis, 2000) or setting hyperparameters (Snoek et al., 2012). For simplicity in this initial study we focus on single-task meta-learning.

**Population-based training** (PBT; Jaderberg et al., 2017) is a meta-learning algorithm that trains multiple learners in parallel, after each interval \(T\) steps of IL applying an evolutionary OL step which consists of: (1) Evaluate the performance of each learner, (2) Replace both parameters and hyperparameters of 20% lowest-performing learners with copies of those from the 20% high-performing learners (EXPLOIT). (3) Randomly perturb the hyperparameters (but not the parameters) of all learners (EXPLORE).

Two distinctive features of PBT are notable because they give the OL more control than most meta-learning algorithms (e.g. Bayesian optimization (Snoek et al., 2012)) over the dynamics and outcome of the learning process: (1) OL applies optimization to parameters, not just hyperparameters. This means the OL can directly select for parameters which lead to ADS, instead of only being able to influence parameter values via hyperparameters (2) Multiple OL steps per training run.

#### 2.2. Distributional shift and content recommendation

In general, **distributional shift** refers to change of the data distribution over time. In supervised learning with data \(x\) and labels \(y\), this can be more specifically described as
Hidden Incentives for Auto-induced Distributional Shift

3. Auto-induced Distribution Shift (ADS)

Auto-induced distribution shift (ADS) is distributional shift caused by an algorithm’s behaviour: This is in contrast to distributional shift which would happen even if the learner were not present - e.g. for a crash prediction algorithm trained on data from the summer, encountering snowy roads is an example of distributional shift, but not auto-induced distributional shift (ADS).

We emphasize that ADS are not inherently bad or good; often ADS can even be desirable: consider an algorithm meant to alert drivers of imminent collisions. If it works well, such a system will help drivers avoid crashing, thus making self-refuting predictions which result in ADS. What separates desirable and undesirable ADS? The collision-alert system alters its data distribution in a way that is aligned with the goal of fewer collisions, whereas the news manipulation results in changes that are misaligned with the goal of better predicting existing users’ interests (Leike et al., 2018).

In reinforcement learning (RL), ADS are typically encouraged as a means to increase performance. On the other hand, in supervised learning (SL), the i.i.d. assumption precludes ADS in theory. In practice, however, the possibility of using ADS to increase performance (and thus an incentive to do so) often remains. For instance, this occurs in online learning. In our experiments, we explicitly model such situations where i.i.d. assumptions are violated: We study the behavior of SL and myopic RL algorithms, in environments designed to include incentives for ADS, in order to understand when incentives are effectively hidden. Fig. 2 contrasts these settings with typical RL and SL.

4. Incentives

For our study of incentives, we use the following terminology: an incentive for a behavior (e.g. an action, a classification, etc.) is present (not absent) to the extent that the behaviour will increase performance (e.g. reward, accuracy, etc.) (Everitt & Hutter, 2019). This incentive is revealed to a learner if it would, at higher than chance levels, learn to perform the behavior given sufficient capacity and training experience. The incentive is pursued (not eschewed) by a learner if it actually performs the incentivized behaviour. Note even when an incentive is revealed, it may not be pursued, e.g. due to limited capacity and/or data, or simply chance. See Fig 3.

For example, in content recommendation, the incentive to drive users away is present if some user types are easier to predict than others. But this incentive may be hidden from the learner by using a myopic algorithm, e.g. one that does not see the effects of its actions on the distribution of users. The incentive might instead be revealed to the outer loop of a meta-learning algorithm like PBT, which does see the
Incentives may be:

- **present (not absent)**
- **revealed (not hidden)**
- **pursued (not eschewed)**

![Focus of our work](image)

**Figure 3.** Types of incentives, and their relationship to ADS.

Distributional Shift that are hidden from the learner, i.e. incentives for behaviors that cause Auto-induced ADS are

\[ (RL) \]

where moving towards high-reward states is typically intended behavior. Thus managing learners incentives can be intractable to design reward functions that perfectly specify the ultimate goal is desirable. However, for real-world applications of RL, the counter-productive in the context of reinforcement learning (RL), where success is not always possible.

Hiding incentives for ADS may seem counter-intuitive and lead to significant unexpected changes in behavior. For example, hiding the incentive to manipulate users from a content recommendation algorithm can prevent it from influencing users in a way they would not endorse. However, if machine learning practitioners are not aware that incentives are present, or that properties of the learning algorithm are hiding them, then seemingly innocuous changes to the learning algorithm may reveal HI-ADS, and lead to significant unexpected changes in behavior.

Hiding incentives for ADS may seem counter-intuitive and counter-productive in the context of reinforcement learning (RL), where success is not always possible.

**5. Hidden Incentives for Auto-induced Distributional shift (HI-ADS)**

Following from the definitions in Sections 3 and 4, HI-ADS are incentives for behaviors that cause Auto-induced Distributional Shift that are hidden from the learner, i.e., the learner would not learn to perform the incentivized behaviors at higher than chance levels, even given infinite capacity and training experience.

Like ADS, HI-ADS are not necessarily problematic. Indeed, hiding incentives can be an effective method of influencing learner behavior. For example, hiding the incentive to manipulate users from a content recommendation algorithm could prevent it from influencing users in a way they would not endorse. However, if machine learning practitioners are not aware that incentives are present, or that properties of the learning algorithm are hiding them, then seemingly innocuous changes to the learning algorithm may reveal HI-ADS, and lead to significant unexpected changes in behavior.

Hiding incentives for ADS may seem counter-intuitive and counter-productive in the context of reinforcement learning (RL), where moving towards high-reward states is typically desirable. However, for real-world applications of RL, the ultimate goal is not a system that achieves high reward, but rather one that behaves according to the designer’s intentions. And as we discussed in the introduction, it can be intractable to design reward functions that perfectly specify intended behavior. Thus managing learners incentives can still provide a useful tool for specification.

We have several reasons for focusing on HI-ADS: (1) The issue of HI-ADS has not yet been identified, and thus is likely to be neglected (at least sometimes) in practice. Our “unit tests” are the first published empirical methodology for assessing whether incentives are hidden or revealed by different learning algorithms. (2) Machine learning algorithms are commonly deployed in settings where ADS are present, violating assumptions used to analyze their properties theoretically. This means learners could exploit ADS in unexpected and undesirable ways if incentives for ADS are not hidden. Hiding these incentives heuristically (e.g. via off-line training) is a common approach, but potentially brittle (if practitioners don’t understand how HI-ADS could become revealed). In particular, meta-learning algorithms can reveal HI-ADS, and are increasingly popular. (3) Substantial real-world issues could result from improper management of learner’s incentives. Examples include tampering with human-generated reward signals (Everitt & Hutter, 2018) (e.g. selecting news articles which manipulate user interests), and creating “self-fulfilling prophecies” (e.g. driving up the value of a held asset by publicly predicting its value will increase (Armstrong & O’Rorke, 2017)).

**6. Removing HI-ADS via Context Swapping**

We propose a technique called context swapping for removing incentives for ADS revealed by changes to the learning algorithm (e.g. introducing meta-learning). The technique trains N learners in parallel, and shuffles the learners through N different copies of the same (or similar) environments; which copy a given learner inhabits can change at any (or every) time-step. We use a deterministic permutation of learners in environment copies, so that the i-th learner inhabits the j-th environment on time-steps \( t \) where \( j = (i + t) \mod N \), makes an observation, takes an action, and receives a reward before moving to the next environment.

When \( N \) is larger than the interval of the OL optimizer, each learner inhabits each copy for at most a single time-step before an OL step is applied. Under the assumption that different copies of the environment do not influence each other, this technique can address HI-ADS in practice, as we show in Sec. 7.2.1.

**7. Experiments**

In Sections 7.2 and 7.1, we introduce ‘unit tests’ for HI-ADS. Our primary goal with these experiments is to convey a crisp understanding of potential issues caused by revealing HI-ADS. Put simply, our experiments show that you can have a learner which behaves as intended, and just by using meta-learning (e.g. PBT), without changing the performance metric (e.g. loss or rewards), the learner’s behavior...
Figure 4. (a) No context swapping (b) Context swapping. The proposed technique rotates learners through different environments. This removes the incentive for a learner to "invest" in a given environment, since it will be swapped out of that context later and not be able to reap the benefits of its investment.

can change completely.

We also show that context swapping is an effective mitigation technique in these environments. On the practical side, the unit tests can be used to compare learning algorithms and diagnose their propensity to reveal incentives.

In Section 7.3, we model a content recommendation system. The goal of these experiments is to demonstrate how HI-ADS could create issues for real-world content recommendation systems such as news feeds, search results, or automated suggestions. They also validate the usefulness of the unit tests: algorithms failed the unit tests also reveal HI-ADS in this setting. We emphasize that ADS takes place in this environment by construction. The point of our experiments is that meta-learning can increase the rate and/or extent of ADS, by revealing this incentive. We find that context swapping is not effective in this environment, highlighting the need for alternative mitigation strategies.

7.1. HI-ADS Unit Test 1: Supervised Learning

This unit test consists of a simple prediction problem. There are no inputs, only an underlying state \( s \in \{0, 1\} \), and targets \( y \in \mathbb{R}^2 \) with \( y_1, y_2 \sim \mathcal{N}(0, s \cdot s^2), \mathcal{N}(0, 1) \), with corresponding predictions \( \hat{y}_1, \hat{y}_2 \). Additionally, \( s_{t+1} = 0 \) if \( \hat{y}_2 > .5 \). We use Mean Squared Error as the loss function, so the optimal predictor is \( \hat{y}_1, \hat{y}_2 = (0, 0) \). However, predicting \( \hat{y}_2 > .5 \) reduces the variance of \( \hat{y}_1 \), i.e. reduces future loss.

The baseline/IL predictor learns \( \hat{y}_1, \hat{y}_2 \) as parameters using SGD with a learning rate of 0.001. For experiments with meta-learning, PBT is the OL (with default settings, see Section 2.2), used to tune the learning rate, with negative loss on the final time-step of the interval as the performance measure for PBT.

7.2. HI-ADS Unit Test 2: Myopic RL

This unit test is based on a version of the prisoner’s dilemma (Prisner, 2014) where an agent plays each round against its past self. The reward function is presented in Table 1. An agent in this environment has a long-term, non-myopic, incentive for cooperation (with its future self), but a current-time-step, myopic, incentive for defection (from its future self). The unit test evaluates whether a agent reveals the non-myopic incentive even when the agent is meant to optimize for the present reward only (i.e. uses discount rate \( \gamma = 0 \)). Naively, we’d expect the non-myopic incentive to be hidden from the agent in this case, and for the agent to consistently defect; learning algorithms that do so pass the test. But some learning algorithms also fail the unit test, revealing the incentive for the agent to cooperate with its future self. While aiming for myopic behavior may seem odd, myopic learners have no incentives to cause distributional shift, since it can only improve future performance. And while making learners myopic may seem like a ‘brute-force’ guaranteed way to manage HI-ADS, we show it is in fact non-trivial to implement.

Formally, this environment is not a 2x2 game (as the original prisoner’s dilemma); it’s a partially observable Markov Decision Process (Åström, 1965; Kaelbling et al., 1998):

\[
\begin{align*}
    s_t, a_t &= a_{t-1}, \{ \} \\
    a_t &\in \{ \text{defect, cooperate} \} \\
    P(s_t, a_t) &= \delta(a_t) \\
    R(s_t, a_t) &= I(s_t = \text{cooperate}) + \\
    \beta \cdot I(a_t = \text{cooperate}) - 1/2
\end{align*}
\]

where \( I \) is an indicator function, and \( \beta = -1/2 \) is a parameter controlling the alignment of incentives (see Appendix 3.2 for an exploration of different \( \beta \) values.). The initial state is sampled as \( s_0 \sim U(\text{defect, cooperate}) \). Policies are represented by a single real-valued parameter \( \theta \) (initialized as \( \theta \sim \mathcal{N}(0, 1) \)) passed through a sigmoid whose output represents \( P(a_t = \text{defect}) \). We use REINFORCE (Williams, 1992) with discount factor \( \gamma = 0 \) as the baseline/IL optimizer. PBT (with default settings, see Section 2.2) is used to tune the learning rate, with reward on the final time-step of the interval as the performance measure for PBT.

Table 1. Rewards for the RL unit test. Note that the myopic (defect) action always increases reward at the current time-step, but decreases reward at the next time-step - the incentive is hidden from the point of view of a myopic learner. A supposedly myopic learner ‘fails’ the unit test if the hidden incentive to cooperate is revealed, i.e. if we see more cooperate (C) actions than defect (D).

| \( s_t = a_{t-1} = \text{D} \) | \( a_t = \text{D} \) | \( a_t = \text{C} \) |
|-----------------|----------|----------|
| \( s_t = a_{t-1} = \text{D} \) | \(-1/2\) | \(-1\) |
| \( s_t = a_{t-1} = \text{C} \) | \(1/2\) | \(0\) |

7.2.1. HI-ADS Unit Tests Experimental Results and Discussion

We first show that agents trained with PBT fail the unit tests more often than “vanilla” algorithms which do not use meta-learning. We initialize the learning rate log-uniformly between 0.01 and 1.0 for all experiments (whether using
PBT or not). We expect and confirm that the following two factors lead to higher rates of unit test failure: (1) **Shorter intervals**: These give the OL more opportunities to influence the population. (2) **Larger populations**: These make outliers with exceptional non-myopic performance more likely, and OL makes them likely to survive and propagate.

The baseline (no meta-learning) algorithms all pass the unit tests: hidden incentives are almost never revealed - see blue curves in Fig. 5. However, agents trained with meta-learning and large populations often fail the unit tests: see orange curves in top rows of Fig. 5.

We also observe that PBT reveals HI-ADS even when \( T = 1 \), where the explanation that PBT operates on a longer time horizon than the inner loop does not apply. We provide a detailed explanation for how this might happen in Appendix 3, but in summary, we hypothesize that there are at least 2 mechanisms by which PBT is revealing HI-ADS: (1) optimizing over a longer time-scale, and (2) picking up on the correlation between an agent’s current policy and the underlying state. Mechanism (2) can be explained informally as reasonings as: “If I’m cooperating, then I was probably cooperating on the last time-step as well, so my reward should be higher”. As support for these hypotheses, we run control experiments identifying two algorithms (each sharing only one of these properties) that can fail the unit test. Context swapping remains effective.

(1) **Optimizing over a longer time-scale**: replacing PBT with REINFORCE as an outer-loop optimizer. The outer-loop optimizes the parameters to maximize the summed reward of the last \( T \) time-steps. As with PBT, we observe non-myopic behavior, but now only when \( T > 1 \). This supports our hypothesis that exploitation of HI-ADS is due not to PBT in particular, but just to the introduction of sufficiently powerful meta-learning. See Fig. 5 B2.

(2) **Exploiting correlation**: Q-learning with \( \gamma = 0 \) an \( \epsilon = 0.1 \)-greedy behavior policy and no meta-learning. If either state was equally likely, the Q-values would be the average of the values in each column in Table 1, so the estimated \( Q(\text{defect}) \) would be larger. But the \( \epsilon \)-greedy policy correlates the previous action (i.e. the current state) and current action (so long as the policy did not just change), so the top-left and bottom-right entries carry more weight in the estimates, sometimes causing \( Q(\text{defect}) \approx Q(\text{cooperate}) \) and persistent nonmyopic behavior. See Fig. 6 for results, Appendix 4.2 for more results, and Appendix 4.1 for experimental details.

Furthermore, we verify that context swapping significantly mitigates the effect of HI-ADS in both unit tests, decreasing undesirable behavior to near-baseline levels - see bottom rows of Fig. 5. This effect can be explained as follows: Because context swapping transfers the benefits of one learner’s action to the next learner to inhabit that environment, it increases the second learner’s fitness, and thereby reduces the relative fitness (as evaluated by PBT’s EXPLOIT step) of the non-myopic cooperate behavior.

We observe some interesting exceptions with the combination of small populations and short PBT intervals: Although context swapping still significantly decreases the effect of HI-ADS, non-myopic cooperate behavior is observed as much as 20% of the time (for #learners=10, \( T = 1 \); see bottom-left plot).

Figure 5. (A) Values of \( \gamma_2 \) in the supervised learning (SL) unit test. Larger values mean sacrificing present performance for future performance (i.e. non-myopic exploitation of ADS). (B) Average level of non-myopic cooperate behavior observed in the RL unit test for HI-ADS, with two meta-learning algorithms (B1) PBT and (B2) REINFORCE. Lower is better, since the goal is for non-myopic incentives to remain hidden. Despite the inner loop being fully myopic (simple MLP in the SL test, \( \gamma = 0 \) in RL test), in all cases outer-loop (OL) optimizers reveal HI-ADS (top rows). Context swapping significantly mitigates HI-ADS (bottom rows).
We now present a toy environment for modeling content with the illusory truth effect, interest in the topic of the top article (propensity for users of each type to use the platform). At the recommendation system (a classifier) selects which actions stay tightly coupled in the failure cases (col. 1,2,5), while in the cases passing the unit test (col. 3,4) the Q-value of cooperate decreases over time.

7.3. HI-ADS in content recommendation

We now present a toy environment for modeling content recommendation of news articles, which includes the potential for ADS by incorporating the mechanisms mentioned in Sec. 2.2, discussed as contributing factors to the problems of fake news and filter bubbles. Specifically, the environment assumes that presenting an article to a user can influence (1) their interest in similar articles, and (2) their propensity to use the recommendation service. These correspond to modeling auto-induced concept shift of users, and auto-induced covariate shift of the user base, respectively (see Sec. 2.2).

This environment includes the following components, which change over (discrete) time: **User type:** $x^t$, **Article type:** $y^t$, **User interests:** $W^t$ (propensity for users of each type to click on articles of each type), and **User loyalty:** $g^t$ (propensity for users of each type to use the platform). At each time step $t$, a user $x_t^t$ is sampled from a categorical distribution, based on the loyalty of the different user types. The recommendation system (a classifier) selects which type of article to present in the top position, and finally the user ‘clicks’ an article $y^t$, according to their interests. User loyalty for user type $x^t$ undergoes covariate shift: in accordance with the self-selection effect, $g^t$ increases or decreases proportionally to that user type’s interest in the top article. The interests of user type $x^t$ (represented by a column of $W^t$) undergoing concept shift; in accordance with the illusory truth effect, interest in the topic of the top article chosen by the recommender system always increases.

Formally, this environment is similar to a POMDP\(\mathcal{R}\), i.e. a POMDP with no reward function, also known as a **world model** (Armstrong & O’Rourke, 2017; Hadfield-Menell et al., 2017); the difference is that the learner observes the input ($o_{\text{pre}}^t$) before acting and only observes the target ($o_{\text{post}}^t$) after acting. The states $s$, observations $o$, and actions $a$ are computed as follows:

$$s^t = (g^t, W^t, x^t, y^t)$$
$$o_{\text{pre}}^t, a^t, o_{\text{post}}^t = (x^t, y^t, y^t)$$

For further details on this environment, including the state transition function, see Appendix 2.

Our recommender system is a 1-layer MLP trained with SGD-momentum. Actions are sampled from the MLP’s predictive distribution. For PBT, we use $T = 10$ and 20 agents, and use accuracy to evaluate performance. We run 20 trials, and match random seeds for trials with and without PBT. See Appendix 3 for full experimental details.

7.3.1. CONTENT RECOMMENDATION EXPERIMENTAL RESULTS AND DISCUSSION

We find that PBT yields significant improvements in training time and accuracy, but also greater distributional shift (Fig. 7). User base and user interests both change faster with PBT, and user interests change more overall. We observe that the distributions over user types typically saturate (to a single user type) after a few hundred time-steps (Fig 1 and Fig. 7, Right). We run long enough to reach such states, to demonstrate that the increase in ADS from PBT is not transitory. The environment has a number of free parameters, and our results are qualitatively consistent so long as (1) the initial user distribution is approximately uniform, and (2) the covariate shift rate ($\alpha_1$) is faster than the concept shift rate ($\alpha_2$). See Appendix 2 for details.

We measure concept shift (change in $P(y|x)$) as the cosine distance between each user types’ initial and current interest vectors. And we measure covariate shift (change in $P(x)$) as the KL-divergence between the current and initial user distributions, parametrized by $g^t$ and $g^t$, respectively. In Figure 8, we plot concept shift and covariate shift as a function of accuracy. We observe that for both types of ADS, at low levels of accuracy PBT actually causes less shift than occur in baseline agents; HI-ADS are only observed for accuracies above 60%. This suggests that only relatively strong performers are able to pick up on the HI-ADS revealed by PBT (Fig. 8).
Hidden Incentives for Auto-induced Distributional Shift

Figure 7. Content recommendation experiments. **Left**: using Population Based Training (PBT) increases accuracy of predictions faster, leads to a faster and larger drift in users’ interests, $P(y|x)$, (Center); as well as the distribution of users, $P(x)$, (Right). Shading shows std error over 20 runs.

Figure 8. Amount of auto-induced covariate shift (**left**) and auto-induced concept shift (**right**) as a function of performance (accuracy) averaged over all trials, learners, and time-steps. Only relatively strong learners (those which achieve accuracy > 60%) exhibit HI-ADS.

8. Related work

**ADS in practice:** We introduce the term ADS, but we are far from the first to study it. Caruana et al. (2015) provide an example of asthmatic patients having lower predicted risk of pneumonia. Treating asthmatics with pneumonia less aggressively on this basis would be an example of harmful ADS; the *reason* they had lower pneumonia risk was because they had received *more* aggressive care already. Schulam & Saria (2017) note that such predictive models are commonly used to inform decision-making, and propose modeling counterfactuals (e.g. “how would this patient fare with less aggressive treatment”) to avoid making such self-refuting predictions. While their goal is to make accurate predictions in the presence of ADS, our goal is to identify and manage incentives for ADS. Goodfellow (2019) argues that adversarial defenses that do not account for ADS are critically flawed.

**Non-i.i.d bandits:** Contextual bandits (Wang et al., 2005; Langford & Zhang, 2008) are frequently discussed as an approach to content recommendation (Li et al., 2010). While bandit algorithms typically make the i.i.d. assumption, counter-examples exist (Gheshlaghi Azar et al., 2014; Shah et al., 2018); most famously, adversarial bandits (Auer et al., 1995). Closest to our work is Shah et al. (2018), who consider covariate shift caused by multi-armed bandits. Our task in Sec. 7.3 is similar to their problem statement, but more general in that we include user features, thus disentangling covariate shift and concept shift. Our motivation is also different: Shah et al. (2018) seek to exploit ADS, whereas we aim to avoid hidden incentives for ADS.

**Safety and incentives:** Emergent incentives to influence the world (such as HI-ADS) are at the heart of many concerns about the safety of advanced AI systems (Omohundro, 2008; Bostrom, 2014). Understanding and managing the incentives of learners is also a focus of Armstrong & O’Rourke (2017); Everitt (2018); Everitt et al. (2019); Cohen et al. (2019). While Everitt et al. (2019) focus on identifying which incentives are present, we note that incentives may be present and yet not be revealed or pursued - for example, in supervised learning, there is an incentive to make predictions that are over-fit to the test set, but we typically hide the test set from the learner, which effectively hides this incentive. While Carey et al. (2020); Everitt et al. (2019); Armstrong & O’Rourke (2017) discuss methods of removing problematic incentives, we note in practice incentives are often hidden rather than removed. Our work addresses the efficacy of this approach and ways in which it can fail.

**HI-ADS and meta-learning:** As far as we know, our work is the first to consider the problem of HI-ADS, or its relation to meta-learning. A few previous works have some relevance or resemblance. Rabinowitz (2019) documents qualitative differences in learning behavior when meta-learning is applied. MacKay et al. (2019) and Lorraine & Duvenaud (2018) view meta-learning as a bilevel optimization problem, with the inner loop playing a best-response to the outer loop. In our work, the inner loop is unable to achieve such best-response behavior; the outer loop is too powerful (see Fig. 5). Finally, Sutton et al. (2007) note that meta-learning can change learning behavior in a way that improves performance by preventing convergence of the inner loop.

9. Discussion and Conclusion

We have identified the phenomenon of auto-induced distributional shift (ADS), and the problems that can arise when there are hidden incentives for learners to induce distributional shift (HI-ADS). And our experiments demonstrate that using meta-learning can reveal HI-ADS and lead learners to use ADS as a means of increasing performance.

Our work highlights the interdisciplinary nature of issues with real-world deployment of ML systems - we show how HI-ADS could play a role in important technosocial issues like filter bubbles and the propagation of fake news. There are a number of potential implications for our work: (1) When HI-ADS are a concern, our methodology and environments can be used to help diagnose whether and to what
extent the final performance/behavior of a learner is due to ADS and/or incentives for ADS, i.e. to quantify their influence on that learner. (2) Comparing this quantitative analysis for different algorithms could help us understand which features of algorithms affect their propensity to reveal HI-ADS, and aid in the development of safer and more robust algorithms. (3) Characterizing and identifying HI-ADS in these tests is a first step to analyzing and mitigating other (problematic) incentives, as well as to developing theoretical understanding of incentives.

Broadly speaking, our work emphasizes that the choice of machine learning algorithm plays an important role in specification, independently of the choice of performance metric. A learner can use ADS to increase performance according to the intended performance metric, and yet still behave in an undesirable way, if we did not intend the learner to improve performance by that method. In other words, performance metrics are incomplete specifications: they only specify our goals or ends, while our choice of learning algorithm plays a role in specifying the means by which we intend an learner to achieve those ends. With increasing deployment of ML algorithms in daily life, we believe that (1) understanding incentives and (2) specifying desired/allowed means of improving performance are important avenues of future work to ensure fair, robust, and safe outcomes.

10. Acknowledgements

Thanks to the DeepMind and Future of Humanity Institute AI safety teams who gave lots of feedback on these ideas. Thanks to Valentin Dalibard for help with Population Based Training, and Toby Pohlen for help with using Google infrastructure. Thanks to Owain Evans, Audrey Durand, Jacob Buckman, Michael Noukhovitch and Emmanuel Bengio for feedback on drafts.

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Appendices

1. Content recommendation in the wild

Filter bubbles, the spread of fake news, and other technosocial issues are widely reported to be responsible for the rise of populism (Groshek & Koc-Michalska, 2017), increase in racism and prejudice against immigrants and refugees (Noble, 2018), increase in social isolation and suicide (Luxton et al., 2012), and, particularly with reference to the 2016 US elections, are decried as threatening the foundations of democracy (El-Bermawy, 2016). Even in 2013, well before the 2016 American elections, a World Economic Forum report identified these problems as a global crisis (Lee Howell, 2013).

We focus on two related issues in which content recommendation algorithms play a role: fake news and filter bubbles.

1.1. Fake news

Fake news (also called false news or junk news) is an extreme version of yellow journalism, propaganda, or clickbait, in which media that is ostensibly providing information focuses on being eye-catching or appealing, at the expense of the quality of research and exposition of factual information. Fake news is distinguished by being specifically and deliberately created to spread falsehoods or misinformation (Merriam-Webster, 2017; Mihailidis & Viotty, 2017).

Why does fake news spread? It may at first seem the solution is simply to educate people about the truth, but research tells us the problem is more multifaceted and insidious, due to a combination of related biases and cognitive effects including confirmation bias (people are more likely to believe things that fit with their existing beliefs), priming (exposure to information unconsciously influences the processing of subsequent information, i.e. seeing something in a credible context makes things seem more credible), and the illusory truth effect (i.e. people are more likely to believe something simply if they are told it is true).

Allcott & Gentzkow (2017) track about 150 fake news stories during the 2016 US election, and find the average American adult saw 1-2 fake news stories, just over half believed the story was true, and likelihood of believing fake news increased with ideological segregation (polarization) of their social media. Shao et al. (2018) examine the role of social bots in spreading fake news by analyzing 14 million Twitter messages. They find that bots are far more likely than humans to spread misinformation, and that success of a fake news story (in terms of human retweets) was heavily dependent on whether bots had shared the story.

Pennycook et al. (2019) examine the role of the illusory truth effect in fake news. They find that even a single exposure to a news story makes people more likely to believe that it is true, and repeat viewings increase this likelihood. They find that this is not true for extremely implausible statements (e.g. “the world is a perfect cube”), but that “only a small degree of potential plausibility is sufficient for repetition to increase perceived accuracy” of the story. The situation is further complicated by peoples’ inability to distinguish promoted content from real news - Amazeen & Wojdynski (2018) find that fewer than 1/10 people were able to tell when content was an advertisement, even when it was explicitly labelled as such. Similarly, Fazio et al. (2015) find that repeated exposure to incorrect trivia make people more likely to believe it, even when they are later able to identify the trivia as incorrect.

1.2. Filter bubbles

Filter bubbles, a term coined and popularized by Pariser (2011) are created by positive or negative feedback loops which encourage users or groups of users towards increasing within-group similarity, while driving up between-group dissimilarity. The curation of this echo chamber is called self-selection (people are more likely to look for or select things that fit their existing preferences), and favours what Techopedia (2018) calls intellectual isolation. In the context of social and political opinions, this is often called the polarization effect (Wikipedia contributors, 2018).

Filter bubbles can be encouraged by algorithms in two main ways. The first is the most commonly described: simply by showing content that is similar to what a user has already searched for, search or recommender systems create a positive feedback loop of increasingly-similar content (Pariser, 2011; Kayhan, 2015). The second way is similar but opposite - if the predictions of an algorithm are good for a certain group of people, but bad for others, the algorithm can do better on its metrics by driving hard-to-predict users away. Then new users to the site will either be turned off entirely, or see an artificially homogenous community of like-minded peers, a phenomena Shah et al. (2018) call positive externalities.

In a study of 50,000 US-based internet users, Flaxman & Goel (2015) find that two things increase with social media and search engine use: (1) exposure of an individual to opposing or different viewpoints, and (2) mean ideological distance between users. Many studies cite the first result as evidence of the benefits of internet and social media (Robson, 2018; Bakshy et al., 2015), but the correlation of exposure with ideological distances demonstrates that exposure is not enough, and might even be counterproductive.

Facebook’s own study on filter bubbles results show that the impact of the news feed algorithm on filter bubble “size” (a measure of homogeneity of posts relative to a baseline) is almost as large as the impact of friend group composition (Bakshy et al., 2015). Kayhan (2015) specifically study...
the role of search engines in confirmation bias, and find that search context and the similarity of results in search engine results both reinforce existing biases and increase the likelihood of future biased searches. Nguyen et al. (2014) similarly study the effect of recommender systems on individual users’ content diversity, and find that the set of options recommended narrows over time.

Filter bubbles create an ideal environment for the spread of fake news: they increase the likelihood of repeat viewings of similar content, and because of the illusory truth effect, that content is more likely to be believed and shared (Pennycook et al., 2019; DiFranzo & Gloria-Garcia, 2017; Pariser, 2011). We are not claiming that HI-ADS are entirely or even mostly responsible for these problems, but we do note that they can play a role that is worth addressing.

\begin{align*}
\text{incentive-compatible (} \beta = 0.5) \\
\text{incentive-orthogonal (} \beta = 0.0) \\
\text{incentive-opposed (} \beta = -0.5) 
\end{align*}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure9.png}
\caption{Average level of non-myopic (i.e. cooperate) behavior learned by agents in the unit test for HI-ADS. Despite making the inner loop fully myopic (\( \gamma = 0 \)), population-based training (PBT) can cause HI-ADS, leading agents to choose the cooperate action (top row). Context swapping successfully prevents this (bottom row). Columns (from left to right) show results for populations of 10, 100, and 1000 learners. In the legend, “interval” refers to the interval (T) of PBT (see Sec. 2.2). Sufficiently large populations and short intervals are necessary for PBT to induce nonmyopic behavior.}
\end{figure}

\section{Extra experiments and reproducibility details}

\subsection{HI-ADS unit test}

\subsection{Alignment of incentives exploration}

This section presents an exploration of the parameter \( \beta \), which controls the alignment of incentives in the HI-ADS unit tests (see Table 2).

To clarify the interpretation of experiments, we distinguish between environments in which myopic (defect) vs. nonmyopic (cooperate) incentives are opposed, orthogonal, or compatible. Note that in this unit test myopic behaviour (defection) is what we want to see.

1. **Incentive-opposed**: Optimal myopic behavior is incompatible with optimal nonmyopic behavior (classic prisoner’s dilemma; these experiments are in the main paper).

2. **Incentive-orthogonal**: Optimal myopic behavior may or may not be optimal nonmyopic behavior.

3. **Incentive-compatible**: Optimal myopic behavior is necessarily also optimal nonmyopic behavior.

We focused on incentive-opposed environment (\( \beta = -1/2 \)) in the main paper in order to demonstrate that HI-ADS can be powerful enough to change the behavior of the system in an undesirable way. Here we also explore incentive-compatible and incentive-orthogonal environments because they provide useful baselines, helping us distinguish a systematic bias towards nonmyopic behavior from other reasons (such as randomness or optimization issues) for behavior that does not follow a myopically optimal policy.

\subsection{Working through a detailed example for PBT with \( T = 1 \)}

To help provide intuition on how (mechanistically) PBT could lead to persistent levels of cooperation, we walk through a simple example (with no inner loop). Consider PBT with \( T = 1 \) and a population of 5 deterministic agents \( A_1, ..., A_5 \) playing cooperate and receiving reward of \( r(A_i) = 0 \). Now suppose \( A_3 \) suddenly switches to play defect. Then \( r(A_1) = 1/2 \) on the next time-step (while the other agents’ reward is still 0), and so PBT’s \textsc{exploit} step will copy \( A_1 \) (without loss of generality to \( A_2 \)). On the following time-step, \( r(A_2) = 1/2 \), and \( r(A_1) = -1/2 \), so PBT will clone \( A_2 \) to \( A_1 \), and the cycle repeats. Similar reasoning applies for larger populations, and \( T > 1 \).
2.1.3. Q-LEARNING EXPERIMENT DETAILS

We show that, under certain conditions, Q-learning can learn to (primarily) cooperate, and thus fails the HI-ADS unit test. We estimate Q-values using the sample-average method, which is guaranteed to converge in the fully observed, tabular case (Sutton & Barto, 1998). The agent follows the $\epsilon$-greedy policy with $\epsilon = 0.1$. In order to achieve this result, we additionally start the agent off with one synthetic memory where both state and action are defect and therefore $R(\text{defect}) = -0.5$, and we hard-code the starting state to be cooperate (which normally only happens 50% of the time). Without this kind of an initialization, the agent always learns to defect. However, under these conditions, we find that 10/30 agents learned to play cooperate most of the time, with $Q(\text{cooperate})$ and $Q(\text{defect})$ both hovering around $-0.07$, while others learn to always defect, with $Q(\text{cooperate}) \approx -0.92$ and $Q(\text{defect}) \approx -0.45$. Context swapping, however, prevents majority-cooperate behavior from ever emerging, see Figure 12.

2.1.4. Q-LEARNING: FURTHER RESULTS

To give a more representative picture of how often Q-learning fails the unit test, we run a larger set of experiments with Q-learning, results are in Figure 11. It’s possible that the failure of Q-learning is not persistent, since we have not proved otherwise, but we did run much longer experiments and still observe persistent failure, see Figure 10.

Figure 10. The same experiments as Figures 6, 11, run for 50,000 time-steps instead of 3000, to illustrate the persistence of non-myopic behavior.

Figure 11. More independent experiments with Q-learning, exactly following Figure 6. Q-learning fails the unit test in a total of 10/30 experiments (including those from Figure 6).
Hidden Incentives for Auto-induced Distributional Shift

2.2. Content recommendation

2.2.1. Environment details

The environment has the following components:

1. **User type**, $x^t$: categorical variable representing different types of users. The content recommender conditions its predictions on the type of the current user.

2. **User loyalty**, $g^t$: the propensity for users of each type to use the platform. User $x^t$ is sampled from a categorical distribution with parameters given by $\text{softmax}(g^t)$.

3. **Article type**, $y^t$: a categorical variable (one-hot encoding) representing the type of article selected by the user.

4. **User interests**, $W^t$: a matrix whose entries $W^t_{x,y}$ represent the average interest user of type $x$ have in articles of type $y$.

At each time step $t$, a user $x^t$ is sampled from a categorical distribution (based on the loyalty of the different user types), then the recommendation system selects which type of article to present in the top position, and finally, the user selects an article. The goal of the recommendation system is to predict the likelihood that the user would click on each of the available articles, in order to select the one which is most interesting to the user.

User loyalty for $x^t$ then changes in accordance with the self-selection effect, increasing or decreasing proportionally to their interest in the top article. The interests of user type $x^t$ (represented by a column of $W^t$) also change; in accordance with the illusory truth effect, their interest in the topic of the top article (as chosen by the recommender system) always increases. Overall, this environment is an extremely crude representation of reality, but it allows us to incorporate both the effects of self-selection (via covariate shift), and the illusory truth effect (via concept shift).

Formally, this environment is similar to a POMDP\$\setminus\!R, i.e. a POMDP with no reward function, also known as a world model (Armstrong & O’Rourke, 2017; Hadfield-Menell et al., 2017); the difference is that the learner observes the input before acting and only observes the target after acting.

The states, observations, and actions are given below.

$$s^t = (g^t, W^t, x^t, y^t)$$

$$o^t_{\text{pre}}, a^t, o^t_{\text{post}} = (x^t, y^t')$$

Figure 12. More independent experiments with Q-learning, exactly following Figure 6, except also using context swapping. This leads to a 100% success rate on the unit test.
The state transition function is defined by:
\[
g_{x^{t+1}} = g_{x^t} + \alpha_1 W_{x^t}^{t+1},
\]
\[
W_{x^{t+1/2}}^{t+1} = W_{x^t}^{t+1} + \alpha_2 ;
\]
\[
x^{t+1} \sim \text{softmax}(g^{t+1})
\]
\[
y^{t+1} \sim \text{softmax}(W_{x^{t+1}}^{t+1})
\]

Where \( y^t \) is the top article as chosen by the recommender, and \( \alpha_1, \alpha_2 \) represent the rate of covariate and concept shift (respectively). The update for \( W^{t+1} \) merely increases the interest of user type \( x^t \) in article type \( y^t \), then normalizes the interests for that user type.

### 2.2.2. Reproducibility Details

For these experiments, the recommendation system is a ReLU-MLP with 1 hidden layer of 100 units, trained via supervised learning with SGD (learning rate = 0.01) to predict which article a user will select. Actions are sampled from the MLP’s predictive distribution. We apply PBT without any hyperparameter selection (this amounts to just doing the EXPLOIT step), and an interval of 10, selecting on accuracy. We use a population of 20 learners (whether applying PBT or not), and match random seeds for the trials with and without PBT. We initialize \( g^1 \) and \( W^1 \) to be the same across the 20 copies of the environment (i.e. the learners start with the same user population), but these values diverge throughout learning. For the environment, we set the number of user and article types both to 10. Initial user loyalties are randomly sampled from \( N(0, 0.03) \), \( \alpha_1 = 0.03 \), and \( \alpha_2 = 0.003 \).

### 2.2.3. Context Swapping in Content Recommendation

We believe context swapping is not appropriate for the content recommendation environment, since when the environments diverge, optimal behavior may differ across environments. Nevertheless, we ran experiments with it for completeness. The main effect appears to be to hamper learning when PBT is not used, see Figure 13. Notably, it does not appear to significantly influence the rate or extent of ADS when combined with PBT.

### 2.2.4. Exploration of Environment Parameters

In Figure 14, we examine the effect of the rate-of-change parameters \( (\alpha_1, \alpha_2) \) of the content recommendation environment on the results provided in the paper. As noted there, our results are qualitatively consistent so long as (1) the initial user distribution is approximately uniform, and (2) the covariate shift rate \( (\alpha_1) \) is faster than the concept shift rate \( (\alpha_2) \). These distributions are updated by different mechanisms, and are not directly comparable. Concept shift changes the task more radically, requiring a learner to change its predictions, rather than just become accurate on a wider range of inputs. We conjecture that changes in \( P(y|x) \) must therefore be kept smooth enough for the outer loop to have pressure to capitalize on HI-ADS.
Figure 14. Content recommendation results for different values of $\alpha_1, \alpha_2$. 

$\alpha_1 = 0.01, \alpha_2 = 0.001$

$\alpha_1 = 0.1, \alpha_2 = 0.001$

$\alpha_1 = 0.01, \alpha_2 = 0.01$

$\alpha_1 = 0.1, \alpha_2 = 0.01$

$\alpha_1 = 0.01, \alpha_2 = 0.1$

$\alpha_1 = 0.1, \alpha_2 = 0.1$