Chirality and topology are intimately related fundamental concepts, which are heavily explored to establish spin-textures as potential magnetic bits in information technology. However, this ambition is inhibited since the electrical reading of chiral attributes is highly non-trivial with conventional current perpendicular-to-plane (CPP) sensing devices. Here we demonstrate from extensive first-principles simulations and multiple scattering expansion the emergence of the chiral spin-mixing magnetoresistance (C-XMR) enabling highly efficient all-electrical readout of the chirality and helicity of respectively one- and two-dimensional magnetic states of matter. It is linear with spin-orbit coupling in contrast to the quadratic dependence associated with the unveiled non-local spin-mixing anisotropic MR (X-AMR). Such transport effects are systematized on various non-collinear magnetic states – spin-spirals and skyrmions – and compared to the uncovered spin-orbit-independent multi-site magnetoresistances. Owing to their simple implementation in readily available reading devices, the proposed magnetoresistances offer exciting and decisive ingredients to explore with all-electrical means the rich physics of topological and chiral magnetic objects.
Electric readout of chirality has rarely been possible with conventional technologies based on current perpendicular-to-plane (CPP) geometries. Resting on tunnel magnetoresistance (TMR), which requests two magnetic electrodes, spin-polarized scanning tunneling microscopy/spectroscopy (STM/STS) was so far the only technique successful in detecting the chirality of spin spirals and sub-10 nm skyrmions\cite{30-35}. The challenge resides in the highly non-trivial full control of the magnetization direction of the readout electrode and the sensing efficiency, dictated by the relative alignment of the magnetization of two electrodes. Obviously, the realization of all-electrical chiral detection, i.e., readout with a non-magnetic electrode, would enable a remarkable leap forward on the basis of a robust practical implementation. However, the known MR effects such as the anisotropic MR (AMR)\cite{36-39} and the recently discovered highly efficient spin-mixing MR (XMR)\cite{40,41} are expected to be transparent to the main attributes of topological structures: chirality or helicity. With an efficiency of a few percent, the AMR originates from spin-orbit coupling (SOC) and is by nature an on-site effect that depends on the local quantization axis of the magnetization relative to the crystal lattice. The X in XMR stands for spin-mixing since the XMR effect has been proposed to mainly arise from the spin-mixing of the electronic states as a result of a non-local mechanism driven by electron scattering at atoms having canted magnetic moments independently from SOC\cite{40,41}. Intriguingly, the precise nature of the dependence of measured signals on the opening angles of the underlying spin-textures remained so far elusive\cite{42}.

In contrast to CPP geometries, all-electrical chiral and topological characterization is in principle possible with current-in-plane (CIP) transport concepts such as the topological Hall effect\cite{43} or the recently proposed chiral\cite{44} and non-collinear\cite{45} Hall effects.
effects. However, these effects are fairly small in general and have to be disentangled from a large Hall background. Moreover, the required Hall bar junction complicates their integration in standard device structures.

In this work, we unveil the existence of a rich family of MR effects enabling the all-electrical perpendicular readout of distinct chirality or helicity characteristics of spin-textures. We utilize multiple scattering concepts and intensive systematic first-principles simulations of atomically resolved transport measurements as probed within STM/STS on magnetic textures generated in a prototypical material: fcc-PdFe bilayer deposited on Ir(111) surface (see Methods). The chosen substrate is well known to host isolated Néel-type skyrmions with a few nanometers diameter.

The discovered set of MRs are categorized in terms of the presence (or not) of non-collinear magnetism, SOC and their concomitant intertwining, as schematically illustrated in Fig. 1h. Purely non-collinear magnetism, i.e., without SOC, gives rise to an isotropic MR induced by the spin-mixing of electronic states due to the misalignment of the atomic magnetic moments, which is the transport phenomenon usually discussed in Refs. 40,41. We name it here I-XMR since it is isotropic and transparent to SOC-related phenomena, as shown from our analytical derivations and systematic ab-initio simulations. We identify the MR chiral in nature, the chiral XMR effect (C-XMR), which is linear in SOC and requires non-collinear magnetism as well as broken inversion symmetry similarly to the conditions giving rise to DMI. C-XMR reaches large efficiencies permitting to distinguish and spatially probe the chiral nature of a given magnetic object. Traditional AMR is quadratic in SOC and emerges in a collinear magnetic environment upon a global rotation of the spin moments. In our study, however, we found a spin-mixing AMR (X-AMR) effect, which is also quadratic in SOC but it is non-local and depends on the canting angle between magnetic moments. In contrast to AMR, its magnitude can be as large as conventional MR efficiencies. The peculiar angular and spatial dependencies characterizing each of the different MR mechanisms enable their straightforward experimental detection and project a plethora of opportunities for basic and applied research of chiral and topological magnets.

**Results**

**Impact of helicity on the XMR signal.** According to the Tersoff–Hamann model54, the local density of states (LDOS) decaying from a particular site \( i \) into the vacuum is proportional to the differential conductance \( dI/dV \) at a bias voltage \( V_{\text{bias}} \) relative to the highest occupied state of the sample measured with STM employing a non-magnetic tip. The latter is assumed in the second vacuum layer above the Pd substrate, as shown in Fig. 1g. The efficiency of the XMR effect is calculated as the ratio between the deviation of the conductance on top of a skyrmion from that of a reference point, which we choose to be the collinear magnetic region (see Methods section):

\[
\text{XMR}(E) = \frac{\text{LDOS}_C(E) - \text{LDOS}_N(E)}{\text{LDOS}_C(E)},
\]

where \( C \) and \( N \) correspond to the collinear and non-collinear magnetic areas, respectively, as shown in Fig. 1, while \( y \) indicates the helicity of the skyrmion.

As understood currently, the XMR effect results mainly from the non-collinearity of the magnetic moments without invoking spin-orbit coupling. The latter, however, can affect the measured XMR signal due to AMR. As aforementioned, both effects are chiral- or helicity-independent. This implies that XMR should be unaltered when switching the sense of rotation of the magnetic moments. This particular scenario is investigated by comparing the energy-resolved XMR ratios to the I-XMR one obtained by switching-off SOC, as illustrated in Fig. 2a. For a systematic comparison, the relative angles are maintained fixed to that obtained from full self-consistency of the skyrmion with \( y = 0 \). The sense of rotation of moments has been switched to realize the skyrmion with \( y = \pi \) (see Fig. 1a, b). The spectra were obtained on top of the core of a Néel-type skyrmion with diameter \( D_{\text{sky}} = 2.2 \text{ nm} \). While at first sight, the XMR\(^{\pi} \) and XMR\(^{-\pi} \) signals seem to have a similar shape, they remarkably do not lay on top of each other. Taking as an example the tunneling energy of 1.27 eV (see dashed line in Fig. 2a), we find that SOC enhances XMR\(^{\pi} \) by a factor of three in strong contrast to the drastic reduction and even change of sign imposed on XMR\(^{\pi} \). Such discrepancy is not limited to the core of the skyrmion but is a general effect, as demonstrated in the spatial maps plotted in Fig. 2c–e. The three maps are indeed very different, with the signal collected on XMR\(^{\pi} \) being the largest. At an energy of 0.61 eV (dot-dashed line in Fig. 2a), SOC seems now to reduce the XMR emanating from both skyrmions but favoring the observation of the skyrmion with helicity \( y = 0 \) instead of the one with \( y = \pi \). Impressively, the XMR signal without SOC peaks up at a value of \( \approx 35 \% \), but with SOC the XMR efficiency crashes down to \( \approx 24 \% \) for \( y = \pi \). The patterns found for XMR\(^{\pi,0,\pi} \) cannot be explained by the hitherto known mechanisms: merely SOC-independent non-collinear magnetism or chiral-insensitive AMR. Overall, this evidences the existence of new MR effects at play.

The alteration of the XMR signals results certainly from the change in the electronic structure imposed by the reversal of the skyrmion’s helicity as illustrated in Fig. 2b, where a comparison is displayed between the LDOS measured on top of the skyrmionic (core) and collinear configurations. For the particular bias voltages addressed earlier, SOC reduces the predicted \( dI/dV \) amplitude at 0.61 eV and enhances at 1.27 eV the signal pertaining to the skyrmion with \( y = \pi \) without affecting that of the zero-helicity skyrmion. In general, the shape, linewidth, and energy of the electronic states depend simultaneously on SOC and on the chirality of the underlying magnetic configuration. Clearly, SOC enables electronic hybridization channels sensitive to the sense of rotation of the magnetic moments.

**Multi-site isotropic, chiral, and anisotropic XMR signals.** A deeper understanding of the unveiled observations can be unraveled by scrutinizing the different contributions to the LDOS, which are enabled by the rotation of magnetic moments. In the process of building up the electronic structure at a given site, electrons scatter in the lattice and hope between neighboring magnetic atoms, picking up various information. Using multiple scattering theory (for details see Supplementary Information 2), we demonstrate that local and non-local multi-site contributions of different nature emerge: isotropic (independent from SOC), chiral (linearly dependent on SOC), and anisotropic achiral (quadratically dependent on SOC), which are strongly contingent to the underlying magnetic texture. We find that the all-electrical XMR signal at a site \( i \) is a sum of four terms:

\[
\text{XMR}(E) = I\text{-XMR}(E) + C\text{-XMR}(E) + X\text{-AMR}(E) + \text{Ani-XMR}(E).
\]
our discussion here to nearest neighbors. This indicates that the magnetoresistance should change in a cosine fashion upon rotation of the moments, with a maximum expected when the moments are aligned antiferromagnetically. In the adiabatic approximation, i.e., when the skyrmions are large, it is then expected that the isotropic contribution should be quadratic with the rotation angle between two magnetic moments. Similarly to the extended Heisenberg Hamiltonian, one can identify an additional biquadratic contribution

\[ \gamma_{\text{XMR}}(E) = \frac{1}{2} \mathbf{S}_i \cdot \mathbf{S}_j \]  

and even other higher-order terms.

Besides the isotropic contributions, we uncover a chiral term, C-XMR, linear with SOC and directly proportional to the chiral product between the spin-moment \( \mathbf{S}_i \) and its neighboring moments:

\[ \gamma_{\text{C-XMR}}(E) \mathbf{S}_i \cdot (\mathbf{S}_i \times \mathbf{S}_j) \], where \( \mathbf{c} \) is analogous to the DM vector and obeys therefore similar symmetry rules. Owing to the chiral nature of this term, rotating the moments clockwise or counter-clockwise modifies the LDOS in an opposite fashion. The largest contribution arises if the rotation angle is \( \pi/2 \). For large skyrmions, the angular dependence is linear with the angle between moments. Obviously, since the remaining contributing terms are achiral, by switching the helicity of the skyrmion (or the chirality of a spin-spiral or a domain wall), one can immediately extract the chiral XMR:

\[ \gamma_{\text{XMR}}^{\gamma}(E) = -\gamma_{\text{C-XMR}}^{\gamma}(E) = \frac{1}{2} \gamma_{\text{XMR}}^{\gamma=}(E) - \gamma_{\text{XMR}}^{\gamma=\pi}(E) \]  

The usual AMR is quadratic in SOC and is local by nature since it only depends on the orientation of moment \( \mathbf{S}_i \).

Conventionally, it is written as

\[ \gamma_{\text{AMR}}(E) = \mathbf{S}_i \cdot (\mathbf{c} \cdot \mathbf{S}_j) \]  

assuming that the anisotropy field responsible for the AMR effect points along the cartesian direction \( z \). In our multiple scattering expansion, however, we uncover non-local (multi-site) dependencies generalizing the AMR to what we dub spin-mixing AMR (X-AMR) effect. The latter is proportional to \( \gamma_{\text{X-AMR}}(E) = \mathbf{S}_i \cdot (\mathbf{c} \cdot \mathbf{S}_j) \) instead of the expected local angular dependence \( \cos^2 \theta_i \), where \( \theta_i \) is the polar angle pertaining to moment \( \mathbf{S}_i \). Furthermore, we find a SOC-correction to the isotropic two-site term:

\[ \gamma_{\text{X-AMR}}(E) \mathbf{S}_i \cdot \mathbf{S}_j \].

Owing to the distinct angular dependence of each of the identified MRs, it is possible to fit the spatial maps and extract the magnetoresistance weights associated to each mechanism. We can expand Equation (2):

\[ \text{XMR}(E) = \sum_{ij} \text{XMR}_{ij}(E) \]  

with the sum

Fig. 2 Impact of the helicity on the XMR signal. a Comparison of energy-resolved XMR signals with different helicities and without SOC measured on top of the skyrmion’s core. b Sum of spin-resolved electronic structure in the vacuum on top of the core of a Néel-type skyrmion with diameter \( D_{sk} \approx 2.2 \text{ nm} \) for different helicities and above the collinear configuration. The dashed and dotted-dahed lines indicate, respectively, the tunneling energies \( E_{\text{bias}} = 1.27 \text{ eV} \) and \( 0.61 \text{ eV} \) at which a spatial map of the whole skyrmion is plotted for c, f \( \text{XMR}^{\gamma=0} \), d, g \( \text{XMR}^{\gamma=\pi} \) and e, h l-XMR signals.
limited to the nearest neighbors and:

\[
\text{XMR}_{ij} = \left[ \gamma_{2\text{-spin}}^{2\text{-spin}} I\text{-XMR} + \gamma_{\text{Ani-XMR}} \right] \mathbf{S}_i \cdot \mathbf{S}_j + \gamma_{4\text{-spin}}^{4\text{-spin}} I\text{-XMR} (\mathbf{S}_i \cdot \mathbf{S}_j)^2 + \gamma_{C\text{-XMR}} \mathbf{C} \cdot \mathbf{S}_i \times \mathbf{S}_j + \gamma_{\text{X-AMR}} \mathbf{e} \cdot \mathbf{S}_i (\mathbf{e} \cdot \mathbf{S}_j),
\]

where the energy dependence is omitted for simplicity.

We expect the spatial map of each contribution to show distinctive patterns depending on the underlying spin-texture. The overlap of all terms can be complex and hinged on the MR weights magnitude and sign. In Table 1, we list the weight distributions for three bias energies: 0.56, 0.61, and 1.27 eV as obtained for the skyrmion studied in Fig. 2 (see Supplementary Note 3–5 for further details). One immediately remarks that all contributions can be of the same order of magnitude, with their sign and size being energy-dependent. We note that in contrast to the AMR weight, the contribution of the rest of the parameters will be enhanced due to the non-local nature of their associated MRs. On the fcc-111 surface, the maximum enhancement factor of 6 is expected due to the number of nearest neighboring pairs. Remarkably, the weight pertaining to X-AMR is larger than that of the conventional AMR. Even if quadratic with SOC, it can directly compete with the weight characterizing C-XMR, which is linear with SOC. The SOC-independent XMR seems to provide the largest contribution to the electrical signal, however, the unveiled SOC-driven MRs are significant. We note that at 1.27 eV, the signal is dominated by C-XMR with a weight of opposite sign to the conventional I-XMR.

Before proceeding to the skyrmion case, it is instructive to explore the behavior of the different MRs for the case of a homogeneous spin-spiral (see Fig. 3) utilizing MR weights provided in Table 1 at an energy bias of eV_{bias} = 0.56 eV. A systematic comparison of the different XMR components along the x-direction is provided in (e, f). The ratio cos^2 \theta / AMR_{total} is shown in (g) for spirals of wave vectors 0.2 \pi/a, 0.3 \pi/a, and 0.5 \pi/a to visualize the contribution of the new X-AMR.

### Table 1 Energy-dependent weights of the various unveiled spin-mixing magnetoresistances.

| Energy (eV) | \( \gamma_{2\text{-spin}}^{2\text{-spin}} I\text{-XMR} \) | \( \gamma_{4\text{-spin}}^{4\text{-spin}} I\text{-XMR} \) | \( \gamma_{C\text{-XMR}} \) | \( \gamma_{\text{AMR}} \) | \( \gamma_{\text{X-AMR}} \) | \( \gamma_{\text{Ani-XMR}} \) |
|------------|----------------|----------------|----------------|----------------|----------------|----------------|
| 0.56       | -6.4190        | 0.0361         | 3.7392         | -0.9416        | 4.7319         | 0.0107         |
| 0.61       | 12.4692        | -0.1588        | 2.0918         | 0.7079         | -3.3460        | 0.1750         |
| 1.27       | -1.0456        | 0.0045         | 3.1518         | 0.0206         | 0.0442         | -0.0443        |

The tunneling energies are given in eV units.
to the total AMR (Fig. 3e). At first sight, they look all similar (Fig. 3b–d), but a closer inspection of their angular dependence reveals differences owing to their local versus non-local nature (Fig. 3f). By dividing the conventional $\cos^2(\theta)$ characterizing the traditional AMR by the total AMR, one can identify the signature of X-AMR as exemplified in Fig. 3g for different spiral pitches. Increasing the wave vector of the spiral enlarges the rotation angle of the magnetic moments, which enhances (diminishes) the contribution of the X-AMR (conventional AMR). The latter provides a well-defined path for the experimental detection of X-AMR.

In contrast to spin-spirals, skyrmions are inhomogenous spin-textures that trigger spatial modulations of all XMR components. This is visualized in Fig. 4 for the various MR patterns hosted by a Néel skyrmion at 0.61 eV (see Supplementary Note 6 for the MR patterns of different skyrmionic structures). The dissimilarity of the shape, extension, and sign of the plotted efficiencies is remarkable. On the one hand, the C-XMR and I-XMR culminate to their maximum value (respectively $-10.2\%$ and $-34.4\%$) at the skyrmion core (Fig. 4a, b). On the other hand, C-XMR experiences a change of sign close to the skyrmion’s edge, contrary to I-XMR. Interestingly, the total AMR contrast is positive and narrower than the negative ones obtained for I-XMR and C-XMR (Fig. 4d). Keeping in mind that the sign of C-XMR switches with the change of helicity, this is a nice example demonstrating how different MRs can counter-act each other when reading chiral magnetic objects. The total AMR signal exhibits a maximum of 19% slightly off-centered from the skyrmion’s core. At the latter location, the total AMR value drops down to 17.6%, which is expected to be zero, i.e., similar to that of the ferromagnetic background, when counting only on the traditional local AMR. In this particular case, the non-local contribution X-AMR, which is two orders of magnitude larger than the conventional AMR or the Ani-XMR (Fig. 4e–g), dominates the total AMR efficiency. While at 0.61 eV the SOC-driven signals, i.e., C-XMR and total AMR, are equally important, albeit different sign, we identify in Fig. 4c the energy window ranging from 0.7 to 1.4 eV where the MR is mostly of chiral origin. At about $-1.36$ eV, the total AMR dominates the scene by reaching an impressive efficiency of 24.7%.

Other chiral spin textures. For completeness, we have expanded our investigations to other skyrmionic structures such as Bloch skyrmions and antiskyrmions (Fig. 5d–f). Henceforth, we focus on the C-XMR effect, which is a primary tool to distinguish chiral spin textures. We assume the anisotropy fields associated with the Néel skyrmion of zero helicity and plot in Fig. 5a–c the spatial C-XMR patterns at 1.27 eV. On the one hand, the C-XMR of the Néel-type skyrmion is isotropic, reaches a maximum value at its core, and reduces in magnitude when approaching the edge. On the other hand, the C-XMR patterns obtained for the Bloch-type skyrmions and antiskyrmions are strongly anisotropically with off-centered maxima, reflecting their chiral texture as described by $\mathbf{c}_1 \cdot (\mathbf{S}_1 \times \mathbf{S}_2)$. Here regions of zero C-XMR arise within the skyrmionic area contrary to what is observed in Néel skyrmions. In the Bloch skyrmion, one finds a sequence of six large-amplitude lobs separated by zero-lines whenever the chiral signal changes...
In this particular case, the dot product of spin-chirality vector and the underlying DMI vector switches within each row of atoms when passing across the skyrmion’s core (see the box shown in Fig. 5f). This explains the emergence of lobes of opposite sign facing each other, which surround the central region that carries a vanishing signal due to the perfect cancellation of chiral contributions. In the antiskyrmion case, one notices four lobes: two of positive sign merging atop the skyrmion core, which separate the two lobes carrying negative chiral contrast. Here the spin-chirality along the x-axis passing through the core of the skyrmion is of opposite sign than that along the y-axis. Surprisingly, the symmetry characterizing the antiskyrmion is not transmitted to the C-XMR signal: the upper (left) half part is different from the lower (right) one. This originates from the electronic contribution of the Pd overlayer, where the atoms sit on a triangular lattice following the ABC stacking characterizing the assumed fcc(111) surface.

Discussion

The chirality or topological nature of spin-textures plays a crucial role in determining their physical properties as well as their potential practical use. Those aspects are difficult to address with current readout technologies based on the CPP geometries. Here, we discovered a rich family of spin-mixing magnetoresistances that enables an all-electrical reading of non-collinear magnetic states. Based on systematic first-principles simulations and multiple scattering based concepts, we demonstrated the existence of a highly efficient chiral spin-mixing magnetoresistance, linear with SOC and directly induced by the chiral nature of the underlying spin-texture. We uncovered the contributions of terms quadratic with SOC that give rise to the conventional local anisotropic magnetoresistance and the newly found non-local anisotropic magnetoresistance. The latter is found to be orders of magnitude larger than the conventional anisotropic magnetoresistance and competes directly with the chiral or SOC-independent spin-mixing magnetoresistance in shaping the final electrical signal. The patterns emerging from each of the unveiled magnetoresistance terms as well as their distinct dependence on the misalignment of the magnetic moments can be utilized to identify their respective amplitude and probably explain previously reported intriguing behaviors.

We envisage the scenario of topological spin-textures driven in a racetrack equipped with a non-magnetic detecting electrode, which can either offer atomic resolution, as possible with an STM tip, or not as it is the case in more conventional CPP devices (see Fig. 6). STM enables the atom-by-atom exploration of the signal dependence on the angles between the magnetic moments. Currently, in such experiments, the measured spectra are deconvoluted assuming dependencies expected from TMR (if the tip is magnetic), AMR and XMR but assuming for the latter that the signal is directly proportional to the angle between adjacent moments. Our findings demonstrate that the contributing phenomena are richer than assumed so far and clearly lead to complex interference patterns, which can be disentangled owing to the distinctive simple dependencies of each of the contributing effects on the direction of the magnetic moments. This is analog to the procedure followed when dissecting Hall signals in transversal resistivity measurements. The overall signal can include the anomalous, topological, and quantum Hall effects besides the ordinary one. The different effects have a distinct origin, each signaling very different physics. They do interfere and it is only through their specific dependence with respect to various parameters, such as the magnetic field and magnetization direction, that one can extract them and make conclusions on important physics of the probed materials.

Fig. 5 C-XMR signals on various chiral skyrmions. On the upper panel the C-XMR signal at a bias energy of $eV_{bias} = 1.27$ eV is shown for (a) Néel type and (b) Bloch type skyrmions and for (c) antiskyrmions. On the lower panel d-f the corresponding skyrmion magnetic textures with diameter $D_{sk} \approx 2.2$ nm are shown. The rectangular boxes are used in the text to address the change of chirality across the different skyrmions.

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The chirality or topological nature of spin-textures plays a crucial role in determining their physical properties as well as their potential practical use. Those aspects are difficult to address with current readout technologies based on the CPP geometries. Here, we discovered a rich family of spin-mixing magnetoresistances that enables an all-electrical reading of non-collinear magnetic states. Based on systematic first-principles simulations and multiple scattering based concepts, we demonstrated the existence of a highly efficient chiral spin-mixing magnetoresistance, linear with SOC and directly induced by the chiral nature of the underlying spin-texture. We uncovered the contributions of terms quadratic with SOC that give rise to the conventional local anisotropic magnetoresistance and the newly found non-local anisotropic magnetoresistance. The latter is found to be orders of magnitude larger than the conventional anisotropic magnetoresistance and competes directly with the chiral or SOC-independent spin-mixing magnetoresistance in shaping the final electrical signal. The patterns emerging from each of the unveiled magnetoresistance terms as well as their distinct dependence on the misalignment of the magnetic moments can be utilized to identify their respective amplitude and probably explain previously reported intriguing behaviors.

We envisage the scenario of topological spin-textures driven in a racetrack equipped with a non-magnetic detecting electrode, which can either offer atomic resolution, as possible with an STM tip, or not as it is the case in more conventional CPP devices (see Fig. 6). STM enables the atom-by-atom exploration of the signal dependence on the angles between the magnetic moments. Currently, in such experiments, the measured spectra are deconvoluted assuming dependencies expected from TMR (if the tip is magnetic), AMR and XMR but assuming for the latter that the signal is directly proportional to the angle between adjacent moments. Our findings demonstrate that the contributing phenomena are richer than assumed so far and clearly lead to complex interference patterns, which can be disentangled owing to the distinctive simple dependencies of each of the contributing effects on the direction of the magnetic moments. This is analog to the procedure followed when dissecting Hall signals in transversal resistivity measurements. The overall signal can include the anomalous, topological, and quantum Hall effects besides the ordinary one. The different effects have a distinct origin, each signaling very different physics. They do interfere and it is only through their specific dependence with respect to various parameters, such as the magnetic field and magnetization direction, that one can extract them and make conclusions on important physics of the probed materials.
In our context, the existence of spin spirals in materials hosting skyrmions permits to distinguish in the measured spectra the non-local anisotropic magnetoresistance $X$-AMR, $\propto \cos \theta_i \cos \theta_j$, from the local one, $\propto \cos^2 \theta_i$, where $\theta_i$ is the polar angle associated with moment $S_i$ (assuming an out-of-plane anisotropy field). On one hand, the C-XMR behaves like $c_{ij} / C S_i \cdot S_j$, which for small angles is proportional to the average angle between a given moment and its nearest neighbors, as extracted experimentally ($c$ being the analog of the DM vector and obeys similar symmetry rules). As an example, Fig. 6a illustrates the C-XMR signals pertaining to different skyrmions (note the opposite sign for Néel skyrmions of different helicity). On the other hand, the I-XMR gives rise to a dot product dependence, $S_i \cdot S_j$.

If the detecting electrode lacks atomic resolution, one could rely on the total signal sensed from the underlying area encompassing the skyrmion. Here, the amplitude of the various MRs hinges on their respective origin and simultaneously on the size of the confined spin-textures, which can be controlled by an external magnetic field. To have an overview, Fig. 6b shows the bias-resolved total XMR signal for different skyrmions which can be compared to that emanating from the I-XMR. In general, spatial oscillations lead to interferences that affects the magnitude of the overall signal. One notices blue, red, and white bands corresponding to positive, negative, and transparent MR efficiencies, which are not identical for the different magnetic objects. The I-XMR, X-AMR and AMR being the same for the particular considered cases, the differences in the total XMR efficiency originate from the C-XMR due to the associated helicities. In Fig. 6d, e, one clearly sees that the skyrmions give rise to disparate total XMR induced by C-XMR, as obtained at a tunneling energy of $eV_{bias} = 1.27$ eV. An overview of the bias-resolved total C-XMR is shown in Fig. 6c, where one notices that MR pertaining to the Bloch and antiskyrmions vanishes as a result of the competing oscillations (lobs) shown for example in Fig. 6a. This occurs due to the chiral vector $c_{ij}$ associated with C-XMR, that does not match the directions of the DM vectors that should stabilize the Bloch and antiskyrmions.

Overall, the unveiled phenomena enforce our view that such reading mechanisms represent a new avenue for further fundamental studies of the very rich physics of chiral and topological magnetism. We envision the use of the new magnetoresistances in readily available all-electrical readout device architectures to...
sense, distinguish and categorize the ever increasing number of predicted and discovered non-collinear spin-textures.

Methods

Computational details. The simulations are based on density functional theory (DFT) and the local spin density approximation as implemented in the full-potential scalar-relativistic Korringa-Kohn-Rostoker (KKR) Green function method with spin-orbit coupling included self-consistently. The method enables the embedding of single magnetic skyrmions in a real-space approach that does not require the use of periodic supercells. The approach is based on two steps: first, self-consistent calculations of the skyrmion-free ferromagnetic slab with periodic boundary conditions are performed. The associated Green function, \( G_0 \), is extracted and utilized to solve the Dyson equation, schematically written as \( G = G_0 + G\Delta VG \), in order to obtain the new Green function \( G \). \( \Delta V \) represents the potential changed after injecting the magnetic skyrmion. The magnetic textures are obtained in a self-consistent fashion till convergence is achieved.

The PdFe bilayer on Ir(111) surface is simulated with a slab consisting of a layer of Pd atop Fe, which is deposited on 34 layers of Ir. We assumed an fcc-stacking for all layers with atomic positions obtained from ab-initio. The embedded cluster consists of a total of 165 atoms, including 37 Fe atoms (see Refs. and references therein for details). We assume an angular momentum cutoff at \( I_{\text{tot}} = 3 \) for the orbital expansion of the Green function and when extracting the LDOS a k-mesh of \( 200 \times 200 \) is considered.

Data availability

The data that support the findings of this study are provided in the Supplementary Information and in the main manuscript.

Code availability

The KKR code is a rather complex ab-initio DFT-based code, which is in general impossible to use without proper training on the theory behind it and on the practical utilization of the code. We are happy to provide it upon request.

Received: 12 July 2021; Accepted: 1 March 2022; Published online: 24 March 2022

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Acknowledgements
This work is supported by the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation program (ERC-consolidor grant 681405- DYNASORE and Grant No. 856538, project “3D MAGiC”) and the Deutsche Forschungsgemeinschaft (DFG) through SPP 2137 “Skyrmionics” (Projects LO 1659/8-1, BL 444/16-2). We acknowledge the computing time granted by the JARA-HPCC Vergabegremium and VSR commission on the supercomputers JURECA at Forschungszentrum Jülich and at the supercomputing center of RWTH Aachen University.

Author contributions
S.L. initiated, designed, and supervised the project. I.L.F. performed the first-principles calculations and post-processed the data. S.L. provided the analytical derivations of the various magnetoresistance effects. I.L.F., S.B., and S.L. discussed the results and helped writing the manuscript.

Competing interests
The authors declare no competing interests.

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