Magnetic field inference in active region coronal loops using coronal rain clumps

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ABSTRACT

Aims. We aim to infer information about the magnetic field in the low solar corona from coronal rain clumps using high-resolution spectropolarimetric observations in the Ca\textsc{ii} 8542 Å line obtained with the Swedish 1-m Solar Telescope.

Methods. The weak-field approximation (WFA) provides a simple tool to obtain the line-of-sight component of the magnetic field from spectropolarimetric observations. We adapted a method developed in a previous paper in order to assess the different conditions that must be satisfied in order to properly use the WFA for the data at hand. We also made use of velocity measurements in order to estimate the plane-of-the-sky magnetic field component, so that the magnetic field vector could be inferred.

Results. We have inferred the magnetic field vector from a data set totalling 100 spectral scans in the Ca\textsc{ii} 8542 Å line, containing an off-limb view of the lower portion of catastrophically cooled coronal loops in an active region. Our results, albeit limited by the cadence and signal-to-noise ratio of the data, suggest that magnetic field strengths of hundreds of Gauss, even reaching up to 1000 G, are omnipresent at coronal heights below 9 Mm from the visible limb. Our results are also compatible with the presence of larger magnetic field values such as those reported by previous works. However, for large magnetic fields, the Doppler width from coronal rain is not that much larger than the Zeeman width, thwarting the application of the WFA. Furthermore, we have determined the temperature, \(T\), and microturbulent velocity, \(\xi\), of coronal rain clumps and off-limb spicules present in the same data set, and we have found that the former ones have narrower \(T\) and \(\xi\) distributions, their average temperature is similar, and coronal rain has microturbulent velocities smaller than those of spicules.

Key words. Sun: corona – Sun: magnetic fields

1. Introduction

As the history of the observations of prominences unfolded, they were classified into different categories of a similar phenomenon. One class of prominence that could be seen in the surroundings of active regions was named the Class IV prominence by Pettit (1943).\textsuperscript{1} This type of prominence contained material that was falling in the shape of streamers of coronal material or, as Pettit (1943) called them, ‘coronals’. Coronals can be observed in \textsc{h}\alpha and Ca\textsc{ii} H and K lines falling into the upper chromosphere with velocities of 100 – 200 km s\textsuperscript{-1}, several of them being along a common path. One of the first works to coin the term ‘coronal rain’ to characterise material falling into the chromosphere was the classification of prominences developed by Menzel & Evans (1953), although they interpreted that the precipitating material originated from condensations of coronal plasma and that the phenomenon occurred outside of active regions. Only recently has it been shown that coronal rain is in fact a phenomenon that should be differentiated from prominences due to the very specific conditions under which it occurs (e.g. Antolin et al. 2010).

Some numerical simulations show that under the influence of a steady, uniform heating, coronal loops are found to be in a state of thermal equilibrium (see, for example, Mikić et al. 2013, and the references therein). This equilibrium is either static or consists of a steady flow of material from one end of the loop to the other. However, there are certain situations for which no possible equilibrium can be achieved, even in the presence of a constant or high frequency impulsive heating. This state is called thermal nonequilibrium (TNE; Antiochos & Klimchuk 1991; Klimchuk & Luna 2019). The heating of the loop in these situations is mainly concentrated at the footpoints, and the dynamics of the plasma are constantly evolving in response to the energy imbalance present in the loop due to the inefficiency of thermal conduction to compensate for the radiative losses in the uppermost part of the loop. This imbalance leads the temperature and density to reach critical values, a phenomenon known as ‘catastrophic cooling’ (Antiochos et al. 1999; Antiochos & Klimchuk 1991). The radiative losses increase as the density grows and the temperature decreases. This evolution can sometimes lead to the formation of cold, high-density condensations of plasma inside coronal loops because, locally, thermal instability can take place and drive the local accretion of plasma into high-density clumps. This condensed material can later fall back along the loop to the chromosphere in the form of coronal rain (Schrijver 2001; Müller et al. 2004; Antolin et al. 2010). If the conditions are maintained over a timescale of the order of the radiative timescale, the coronal rain events can happen periodi-

\textsuperscript{1} Pettit’s classes IIIa and IIIb may also correspond to coronal rain material, but the evidence presented by this author is inconclusive.
Coronal rain can appear mainly in two situations (Antolin 2020). It can take place during the gradual phase of a flare, within the flaring loops at the late stage of their cooling phase, or, more commonly, in active region loops. Another coronal rain scenario has been recently identified in the quiet Sun, associated with null point topologies high up in the corona, where magnetic field dips are naturally formed and where material can accumulate (Mason et al. 2019; Li et al. 2018). The appearance of the clumps heavily depends on the spectral line used to observe them. They have a very wide temperature range, from a few $10^2$ K up to several times $10^5$ K, so they can be seen both in chromospheric and transition region lines. When observed in chromospheric lines, coronal rain appears clumpy and is seen to have a smaller length (hundreds of kilometers) measured along the direction of the flow than when seen through transition region lines, for which much longer lengths (up to tens of megameters) are observed (Antolin et al. 2010, 2015; Antolin & Rouppe van der Voort 2012). However, thinner and more elongated clumps are also seen in lines such as Hα, and we have also spotted several of them in our observations in the Ca ii 8542 Å line.

The structure of coronal rain clumps is assumed to consist of a cool core, surrounded by a thin transition region of a higher temperature that envelops the clump and serves as a boundary between the condensed material and the corona (Antolin 2020). Multiple individual coronal rain clumps can fall along the same coronal loop or bundle of loops at the same time, so the appearance of what can be perceived as one individual coronal rain clump can change with time given the possible superposition of multiple clumps when viewed with a coarse spatial resolution instrument. Instruments that provide higher spatial resolution, such as the Daniel K. Inouye Solar Telescope (DKIST; Rimmelle et al. 2020), will likely reveal that the widths of the clumps have a distribution of even smaller values than those measured with current instruments (Scullion et al. 2014; Antolin et al. 2015).

The plasma that constitutes coronal rain consists of both neutrals and ions, and we assume them to be in a state of strong coupling, which is predominantly achieved through collisions between the ions and the neutral particles (Oliver et al. 2016). This means that even when observed through neutral lines such as Hα, the motion of coronal rain clumps can be safely assumed to take place along the magnetic field lines of the coronal loop. The implications of this fact are cardinal to the study of the morphology and structure of the magnetic field in coronal loops. Coronal rain has already been used to map the topology of the magnetic field of coronal loops (Antolin & Rouppe van der Voort 2012). With spectropolarimetric observations of coronal rain clumps, it is also possible to set further constraints on the magnetic field strength of coronal loops.

Direct inferences of magnetic fields of coronal loops from spectropolarimetric observations are rather scarce. Schad et al. (2016) employed observations obtained using the Facility Infrared Spectropolarimeter (FIRS; Jæggl et al. 2010) at the 0.76 m Dunn Solar Telescope (DST; Dunn 1964; Dunn & Smartt 1991) in the He i 10830 Å line in order to study the magnetic field topology and structure of a coronal loop filled with cold material. The data had a spatial sampling of 0.29″ pixel$^{-1}$, which equaled the size of each scan step. A total of 218 steps were scanned in an observation which took 32 minutes to generate, resulting in a 60″ × 70″ field of view. The magnetic field vector along a coronal loop was inferred using the inversion code HELIX$^+$ (He-Line Information Extractor$^+$; Lagg et al. 2004; Lagg 2007). With the results from the first part of the inversion, accounting only for the Zeeman effect, these authors were able to study the variation with respect to the height above the solar surface of the magnetic field component along the line of sight ($B_{\text{LOS}}$). Under the assumption that the magnetic field and the plasma flow are aligned with the orientation of the triangulated loop, the total magnetic field strength was calculated. We note that $B$ and $B_{\text{LOS}}$ strengths higher than 1000 G were inferred at a height of 9 Mm above the limb, with $B$ decreasing to only a few Gauss at coronal heights above 50 Mm. The full magnetic field strength was also inferred using the ‘Hanle-slab’ model of the HELIX$^+$ code applied to the highly redshifted He i component. These authors report that the only coherent results obtained using this method were for heights ranging between 14 and 50 Mm, because outside this range the strength of the linear polarisation signal was not sufficient to yield reliable results. The type of solutions that yielded a magnetic field aligned with the coronal loop geometry turned out to be those that were most similar to the results inferred in the first step of the analysis, using the triangulated loop to obtain the magnetic field strength.

Kuridze et al. (2019) used observations of coronal loops filled with material that evaporated as a result of a flare event in order to infer $B_{\text{LOS}}$ values using the weak-field approximation (WFA; Landi Degl’Innocenti & Landolfi 2004; Centeno 2018). The spectropolarimetric observations used to carry out the inference were obtained with the Crisp Imaging SpectroPolarimeter (CRISP; Scharmer et al. 2008) at the Swedish 1-m Solar Telescope (SST; Scharmer et al. 2003) in the Ca ii 8542 Å line. The spatial sampling of the observations was 0.057″ pixel$^{-1}$, with a cadence of about 32 s. In order to increase the signal-to-noise ratio ($S/N$), a spatial average was done, resulting in a $0.23″$ pixel$^{-1}$ spatial resolution. We note that $B_{\text{LOS}}$ values were inferred up to heights of 18 Mm above the visible limb, with values at lower heights (up to 9 Mm) peaking at two values, 150 G and 300 G, because of the presence of different structures in the field of view. At upper heights, the inferred $B_{\text{LOS}}$ values were lower, ranging from 50 G to 180 G, having a median of 90 G.

In a previous paper (Kriginsky et al. 2020, hereafter Paper I), we developed a method to infer the $B_{\text{LOS}}$ value using the WFA through a Bayesian scheme, which was applied to off-limb and on-disc spicules in observations obtained in the Ca ii 8542 Å line with CRISP. We were able to study the $B_{\text{LOS}}$ value both in the vicinity of active regions and in quiet Sun regions. The study in both cases yielded an abundance of magnetic fields of hundreds of Gauss in these structures.

In this paper, we used spectropolarimetric observations (Sect. 2) in the Ca ii 8542 Å line of the low coronal portion of an active region loop bundle in order to infer the total magnetic field strength from the coronal rain clumps that were falling towards the chromosphere. We adapted the method developed in Paper I, combining the use of the WFA with velocity measurements to infer the magnetic field strength in the lower corona (Sect. 3). Magnetic field strengths of hundreds of Gauss were abundantly inferred (Sect. 4), with the possibility of even higher values being present. Concluding remarks are presented in Sect. 5.
2. Observations

The observations used in this work were obtained with the CRISP instrument at the SST on 03 June 2016 and consisted of imaging spectropolarimetry in the Ca\textsc{ii} 8542 Å line and in the hydrogen H\textalpha line with a pixel scale of 0.057″ pixel\(^{-1}\). The spectral sampling was 0.05 Å in the line centre and 0.25 Å at the wings, with a total of 15 spectral positions for the calcium observations. The spectral sampling of the H\textalpha observations was 0.1 Å at the line centre and 0.25 Å at the wings, totalling 18 spectral positions. Data reconstruction made use of the Multi-Object Multi-Frame Blind Deconvolution (MOMFBD; Van Noort et al. 2005) method. The CRISP data reduction pipeline (CRISPRED; de la Cruz Rodríguez et al. 2015) was used for additional data reduction, including the cross-correlation method of Henriques (2012). The resulting temporal cadence was 36.33s.

The data set analysed consisted of observations obtained between 16:27 UT and 17:27 UT, totalling 100 frames of spectropolarimetric observations of off-limb chromospheric structures near active region NOAA AR 12551, as it was approaching the solar west limb. Due to the presence of an active region, coronal rain was easily seen off-limb as small clump-like features falling through the low corona. Given their density and size, the Ca\textsc{ii} 8542 Å intensity signal from these structures can be much lower than the average intensity of the visible disc when looking at an intensity image. Figure 1 shows a temporal frame in the Ca\textsc{ii} 8542 Å line together with a simultaneous image in the H\textalpha line. The movie associated with Fig. 1 shows the superposed Ca\textsc{ii} 8542 Å and H\textalpha intensity over the course of the observations.

One would normally expect that pixels outside the solar disc and off-limb features such as coronal rain, prominences, or spicules would have no signal; however, due to scattering in the Earth’s atmosphere and stray light in the telescope, there is a presence of diffuse stray light (Chae et al. 1998; Rouppe van der Voort 2019). This stray light is averaged over the Sun and it produces a normal spectrum and hence an absorption line. When the level of stray light was averaged over time in each pixel, a declining gradient as a function of the distance from the limb was clearly seen. With this declining gradient, the level of stray light was estimated and removed from the Ca\textsc{ii} 8542 Å intensity.

3. Data analysis

In this section, we describe the different methods used to infer several physical parameters from the observational data.

3.1. Line-of-sight magnetic field component

The main goal of this study was to apply the same method developed in Paper I using the WFA to infer the value of $B_{\text{LOS}}$. The method is based on the expression that relates the intensity and the Stokes $V$ profile,

$$V(\lambda) = -4.67 \times 10^{-13} \bar{\gamma} f \lambda_0^2 B_{\text{LOS}} \frac{\partial I(\lambda)}{\partial \lambda},$$

where $f$ is the magnetic filling factor (Landi Degl’Innocenti & Landolfi 2004; Asensio Ramos 2011), $\bar{\gamma}$ is the effective Landé factor of the line (Landi Degl’Innocenti 1982), $\lambda_0$ is the wavelength of the transition (in angstroms), and $B_{\text{LOS}}$ is given in Gauss. Two conditions need to be satisfied in order to correctly use the WFA: The Zeeman width must be much smaller than the Doppler width, and the magnetic field needs to be uniform along
the line of sight (LOS). The first condition is mathematically expressed as

$$\frac{\Delta l_z}{\Delta I_0} \ll 1,$$

(2)

where $\Delta l_z$ is the Doppler width of the line and $\Delta I_0$ is the Zeeman splitting. The Zeeman splitting (in angstroms) is given by the expression

$$\Delta l_z = 4.67 \times 10^{-13} I_0^2 B,$$

(3)

where $B$ is the field strength (in Gauss). The Doppler width, assuming that the instrument width for CRISP is negligible, is expressed as

$$\Delta I_0 = \frac{I_0}{c} \sqrt{1.663 \times 10^{-2} \frac{T}{\mu} + \xi^2},$$

(4)

where $T$ is the temperature (in Kelvin), $\xi$ is the microturbulent velocity (in km s$^{-1}$), $c$ is the speed of light, and $\mu$ is the atomic weight of the atom from which the spectral line originates. By inserting Eq. (3) into Eq. (2), we arrive at the requirement that

$$B \ll \frac{\Delta I_0}{4.67 \times 10^{-13} \Delta l_z^2}.$$

In Paper I, it was not possible to infer the value of $B$. This prevented these authors from checking whether Eq. (5) was satisfied, so they used typical values for $T$ and $\xi$ in order to estimate, with the help of Eq. (4), an upper limit for the values of $B$ that could be safely inferred, arriving at the expression

$$B \ll 2650 \text{ G}.$$

In this study, we were able to go a step further because we inferred $B$ and not just $B_{\text{LOS}}$ for some of the coronal rain clumps. By fitting the intensity profile in each inference with a Gaussian model, we approximated the value of the fitted width ($\sigma_f$) as the value of the Doppler width. This allowed us to check in every inference, for which $B$ could be obtained, whether Eq. (5) was satisfied. If the inferred value of $B$ was larger than 15 % the value of the right-hand side of Eq. (5), the result was discarded.

The second necessary condition for the application of the WFA concerns the uniformity of the magnetic field along the LOS. A gradient of the magnetic field along the LOS can produce asymmetries in the shape of the Stokes $V$ profile, and the method developed in Paper I limits the allowed amplitude asymmetry to only those cases when it could be caused by the noise present in the data. This method was carried out pixel by pixel with a procedure that analysed the correlation between $V$ and $\partial I/\partial \lambda$ and the amplitude asymmetry of $V$, before proceeding with the inference of $B_{\text{LOS}}$. A Bayesian inference scheme was developed in order to obtain a posterior probability distribution of $B_{\text{LOS}}$, from which the mode and the 95% highest posterior density (HPD) interval were extracted as statistical results. In Paper I, this analysis was applied to spicules and was carried out for each pixel; however, given the weakness of the Stokes $I$ and $V$ signals present in coronal rain pixels and the rigorous inference scheme developed, a pixel-by-pixel study applied to coronal rain yielded no pixels satisfying the criteria imposed. A modification of the method devised by these authors was developed in order to circumvent this issue. Both the Stokes $I$ and $V$ profiles of each pixel (or set of pixels, see next paragraph) inside a clump were fitted with model functions. In the case of Stokes $I$, the model profile was a Gaussian function, while the Stokes $V$ profiles were fitted with the derivative of a Gaussian profile. The Stokes $I$ fit had three free parameters: the amplitude ($\sigma_I$), the width ($\sigma_V$), and the position of the peak ($\lambda_I$) of the Gaussian profile. The Stokes $V$ fit had two free parameters: the amplitude ($\sigma_V$) and the width ($\sigma_I$) of the Gaussian profile. The position of the peak of the $V$ fit was held fixed at the position that resulted from fitting the $I$ profile ($\lambda_V = \lambda_I$). Two criteria were imposed on the results of both fits. The first criterion was to set an upper limit of $10^{-3}$ for the sum of the difference between the value of the fitted $V$ profile and the observed $V$ profile. The second criterion was based on the similarity between the resulting widths of both fits. When they were too dissimilar, the relation between $V$ and $\partial I/\partial \lambda$ was seen to take an ‘8’ shape (see Fig. 2). We tried to

![Fig. 2.](a) Plot of $V$ as a function of $\partial I/\partial \lambda$ displaying the shape of an ‘8’ due to the discrepancy between $\sigma_V$ and $\sigma_I$, whose values are given on top of the frame. (b) Same as (a), but for a case in which the most significant digit of $\sigma_V$ and $\sigma_I$ is the same.)
Fig. 3. Example of a coronal rain clump present in the observations and the averaging of the Stokes $I$ and $V$ profiles in groups of adjacent pixels. (a) Coronal rain clump at $-0.75$ Å from the line centre from an image taken at 16:40:55 UT. (d) Magnified view of the red rectangle of panel (a) in order to enhance the view of the clump. (b), (c), (e), and (f) Stokes $I$ and $V$ profiles normalised to their respective maxima as they appear when averaging the signal from one, two, three, and four pixels, respectively. The colour of the $I$ profile matches the colour of the pixel (or group of pixels) on which the signal is averaged in order to generate the profile as shown on (d). The continuous lines reflect the observed profiles, while the dashed lines depict the profiles that result from fitting $I$ and $V$ with a Gaussian profile and the derivative of a Gaussian profile, respectively.

This analysis was first carried out pixel by pixel, but given the small number of results, a spatial averaging of neighbouring pixels was done. For each clump, the set of pixels inside it was determined, and all the possible groups of $n$ connected pixels (with $n = 1, 2, 3,$ and $4$) was used to obtain average Stokes $I$ and $V$ profiles. These profiles were then subjected to the analysis described above. Figure 3 shows an example of the type of profiles that resulted when performing this analysis for all the values of $n$. The normalisation of the profiles shown in Fig. 3 depends on their maximum value, which is different for the various values of $n$. As a result, it is not visually obvious that this averaging leads to an increase in the S/N as $n$ is increased. Nevertheless, in general, performing a spatial average increased the ratio of the extrema of the $V$ lobes to the extrema of the noise that was present at wavelengths located far from the intensity peak.

A single pixel could pertain to a group of any $n$ pixels at the same time. Furthermore, groups with common pixels, but with a different value of $n$ were considered different groups. This was done to maximise the different possible outcomes and to avoid the need to single out the best set of groups of $n$ pixels that had no overlapping pixels between groups, which is something that could prove difficult to realise with an automatic criterion.

### 3.2. Velocity measurement

The line-of-sight velocity component ($v_{LOS}$) was estimated from the Doppler shift of the intensity profile for each clump. A mean intensity profile was obtained by averaging over the intensity signal of the pixels in the clump, and a Gaussian fit was performed in order to estimate the position of the intensity peak. The error in this parameter value was estimated from the covariance matrix of the fit, and it was then propagated to the error in $v_{LOS}$.

If a coronal rain clump could be spotted unequivocally at least twice, the plane-of-the-sky component of the velocity ($v_{POS}$) was estimated by measuring its displacement on the field of view. For this purpose, the centre of mass of the clump was estimated by weighting each pixel according to its peak intensity:

\[
X_{CM} = \frac{\sum_{k=0}^{N} x_k i_k}{\sum_{k=0}^{N} i_k}, \quad Y_{CM} = \frac{\sum_{k=0}^{N} y_k i_k}{\sum_{k=0}^{N} i_k},
\]

where $N$ is the total number of pixels in the clump, $x_k$ and $y_k$ are the coordinates of each pixel on the plane of the sky, and $i_k$ is...
the peak intensity of each pixel, and $X_{\text{CM}}$ and $Y_{\text{CM}}$ are the clump centre-of-mass coordinates. Assuming a straight trajectory, the displacement of the centre of mass divided by the elapsed time gives an approximation of $v_{\text{POS}}$. The error in this measurement was propagated from the error in $i_k$, which in turn comes from the Gaussian fit and by approximating the uncertainty of the $x$- and $y$-coordinates of each pixel to be one pixel.

3.3. Plane-of-the-sky magnetic field component

Assuming that the plasma moves along magnetic field lines, after obtaining $v_{\text{LOS}}$, $v_{\text{POS}}$, and $B_{\text{LOS}}$, we estimated the plane-of-the-sky magnetic field component ($B_{\text{POS}}$) with the following relation:

$$B_{\text{POS}} = B_{\text{LOS}} \frac{v_{\text{POS}}}{v_{\text{LOS}}}.$$  (8)

3.4. Magnetic field strength

Once the plane-of-the-sky magnetic field component was obtained, the magnetic field strength was inferred as follows:

$$B = \sqrt{B_{\text{LOS}}^2 + B_{\text{POS}}^2} = B_{\text{LOS}} \sqrt{1 + \left(\frac{v_{\text{POS}}}{v_{\text{LOS}}}\right)^2}.$$  (9)

Equation (9) was introduced in the Bayesian scheme developed in Paper I in order to obtain a posterior distribution of $B$ and its 95% HPD interval. As is explained in Sect. 3.3, the errors in $v_{\text{POS}}$ and $v_{\text{LOS}}$ were propagated into the value of their squared ratio as it appears in Eq. (9), which was then introduced as a new parameter into the Bayesian scheme with a uniform prior bounded by its minimum and maximum values according to its uncertainty.

4. Results and discussion

In this section, we present the results of the analysis of the different physical parameters described in Sect. 3.

4.1. Behaviour and shape

Throughout the whole duration of the observations, which added up to an hour, clumps of multiple shapes were seen to mainly fall in a localised region of the field of view, following a very similar path (see movie accompanying Fig. 1). Their most common shape displayed a bright centre with fading tails both in front or behind them along their trajectory. Sometimes they displayed nearly circular shapes, and it was also common to observe the complete lack of a bright centre in favour of a much longer thin structure that covered the whole path usually followed by the clumps. Several clumps also varied in shape along their trajectory, becoming more or less elongated as they fell into the chromosphere, which is a phenomenon that was also observed in Hα spectroscopic observations by Antolin & Rouppe van der Voort (2012).

Although the actual number of visible clumps was much larger, we only analysed and identified those that were mostly isolated, omitting those that were packed too closely together to discern a visible boundary between them. A total of 37 clumps were identified, mostly along a common path with a few exceptions, as Fig. 4 shows.

The appearance of clumps in the Ca ii 8542 Å line and in the Hα line is very different. As Fig. 1 shows, when seen in Hα, the rain has a stronger signal compared to the disc intensity. The rain is also much more abundant in this spectral line than in the Ca ii and in several cases an elongated clump is seen in Hα, while only its dense core is seen in the corresponding Ca ii observation. This disparity arrives at the extreme case of some clumps clearly spottable in Hα, while not being visible in Ca ii.

4.2. Stray light

In order to quantify the importance of the removal of the average stray light profile from the observations, we calculated the ratio of this average profile to the $I$ profile at the position of the intensity peak for the pixels used in the magnetic field inference. The Ca ii 8542 Å results are shown in green and the Hα results are shown in blue.
in these two spectral lines. The results are shown in Fig. 5. The stray light profile amounted up to 23% of the observed profile for the Ca\textsc{ii} 8542 Å, while it only amounted up to 15% for H\textsc{α}, in most cases being less than 5%. Therefore, stray light correction appears to be a more important effect when studying coronal rain in the Ca\textsc{ii} 8542 Å line.

### 4.3. Intensity width

In order to study the average width of the coronal rain intensity profiles, we obtained the full width at half maximum (FWHM) by performing a Gaussian fit to the Ca\textsc{ii} 8542 Å Stokes I. Additionally, we performed Gaussian fits to the intensity profiles of the spicules present in the data set analysed here\(^2\). The results are shown in Fig. 6. We found that the ratio of the average width of the intensity profile of spicules to that of the intensity profile of the coronal rain clumps for the Ca\textsc{ii} 8542 Å line was 1.7, while its value for the H\textsc{α} line was 1.1. The difference in ratios between the Ca\textsc{ii} 8542 Å and H\textsc{α} lines could be caused by the fact that, for a given temperature, the thermal component of the Doppler width is a factor of 40 larger for H\textsc{α} because of the difference in atomic mass between hydrogen and calcium atoms.

\(^2\) The data set of this paper is #8 of Paper I.

Making use of Eq. (4), we employed a similar method as the one described by Froment et al. (2020) to measure the temperature and microturbulent velocity of coronal rain clumps using the combined observations in the Ca\textsc{ii} 8542 Å and H\textsc{α} lines, assuming equal temperatures and microturbulent velocities for both lines. The results are shown in Fig. 7. The measured temperatures were of the order of tens of thousands of kelvin, with an average value of 20 500 K, while the microturbulent velocity ranged from 1 to 13 km s\(^{-1}\), with an average value of 6 km s\(^{-1}\).

The method of Froment et al. (2020) to measure \(T\) and \(\xi\) was also used for the spicules present in the data set. The temperature range was broader than that of coronal rain clumps, with an average value of 19 900 K, while the microturbulent velocity had an average value of 13 km s\(^{-1}\), approximately two times the value measured for coronal rain. This difference in non-thermal effects could explain the disparity between the measured values of the FWHM between spicules and coronal rain in the Ca\textsc{ii} 8542 Å line described before.

### 4.4. Velocities

The identified clumps provided a total of 57 \(v_{\text{LOS}}\) measurements using the method described in Sect. 3.2. Given the necessity for the clumps to be spotted at two different times and the limited

\[\text{Counts}\]

\[\text{Counts}\]

\[\text{Counts}\]

\[\text{Counts}\]

\[\text{Counts}\]
off-limb field of view, a $v_{\text{POS}}$ measurement could be determined for only 19 of these clumps. Another reason for the limited number of $v_{\text{POS}}$ measurements was the cadence of the data, which resulted in a large motion of the clumps between two consecutive temporal frames. The results are displayed in Fig. 8. The values of $v_{\text{LOS}}$ ranged from a few km s$^{-1}$ up to about 35 km s$^{-1}$, peaking at around 25 km s$^{-1}$. The total velocity values were calculated with the expression

$$v = \sqrt{v_{\text{LOS}}^2 + v_{\text{POS}}^2},$$

and they ranged between 70 and 120 km s$^{-1}$, with a mean value of 95 km s$^{-1}$. These values are in excellent agreement with previous studies (Antolin & Rouppe van der Voort 2012; Schrijver 2001; de Groof et al. 2005). The fact that the total velocity achieved values that were much larger than the inferred $v_{\text{LOS}}$ values indicates that the trajectory followed by most of the clumps was almost parallel to the plane of the sky with a small component in the direction of the observer. Hence, $B_{\text{LOS}}$ values much smaller than $B$ values were expected.

### 4.5. Magnetic field inference

Using the method detailed in Sect. 3, we performed the inference of $B_{\text{LOS}}$ for different values of $n$ (1, 2, 3, and 4). We also performed the inference of $B$ for those clumps that had a $v_{\text{POS}}$ value assigned. As Fig. 4 shows, most of the observed clumps were falling along a common path. This fact, combined with the observation that the measured ratio of $v_{\text{LOS}}$ values to the $v_{\text{POS}}$ values was located mostly between 0.2 and 0.3, with an average of 0.23, allowed us to use this average as a representative value for the clumps falling along this common path, but that are only seen in one scan. The results are shown in Fig. 9. The inferred $B_{\text{LOS}}$ values were found to be between 40 and 430 G, mostly between 100 and 220 G. The distribution of $B$ ranged from 170 up to 980 G. The average inferred $B$ value was 550 G. As evidenced by Fig. 9, $B$ values as large as 2085 G were originally inferred. However, many of the results, especially those corresponding to large values of $B$, had to be discarded in order to satisfy Eq. (5).

The distributions displayed in Fig. 9 combine the total results for all the different values of $n$. Table 1 summarises the results separately for each $n$ and for all $n$ combined. Except for the average inferred value of $B$ for $n = 2$, it seems that the inferred values of both $B_{\text{LOS}}$ and $B$ decrease as the value of $n$ increases. One of the possibilities could be the superposition effects that can take place when combining signals from different pixels, which is something that was explored in detail in Paper I when applying this analysis on signals originating from spicules. These authors concluded, albeit for spicular material, that when spatial or temporal averages are undertaken, the inferred values of the magnetic field strength tend to decrease.

Comparing the values of $B_{\text{LOS}}$ inferred using our inference method with the results presented by Schad et al. (2016) or Kuridze et al. (2019) is challenging because they are heavily influenced by the orientation of the loop with respect to the observer and, therefore, they can vary strongly depending on the observational data used. We do, however, infer similar values to those reported by Kuridze et al. (2019) using a different method to ours but also employing the WFA, which is something that indicates that both studies report the abundance of magnetic field values of hundreds of Gauss. As mentioned in the Introduction, Schad et al. (2016) inferred the values of $B$ in two different ways: from the inferred $B_{\text{LOS}}$ values using the HELIX$^*$ code combined with the triangulated geometry of the loop and using the Hanle-slab part of the HELIX$^*$ code. Unfortunately, these authors report that the values of $B$ inferred using the second method are not reliable for heights above the visible surface lower than 14 Mm, so it would be unwise to compare our inference results with those obtained through that method because we were only capable of detecting clumps up to 9 Mm above the limb. However, it is possible to compare our results with those obtained using the geometry of the loop combined with the $B_{\text{LOS}}$ inference. Inspecting Fig. 8 of Schad et al. (2016) while considering the large error in their reported height measurements, we can estimate that the values inferred by those authors at the heights correspond-

![Fig. 8. Occurrence of the different values of (a) $v_{\text{LOS}}$ and (b) $v_{\text{POS}}$ as inferred from the Gaussian fit of the intensity and (c) inferred values of the total velocity calculated with Eq. (9)].

| $n$ | $B_{\text{LOS}}$ | HPD($B_{\text{LOS}}$) | $B$ | HPD($B$) |
|-----|-----------------|----------------------|----|----------|
| 1   | 210 [201, 215]  | 585 [543, 636]       |    |          |
| 2   | 190 [178, 196]  | 507 [490, 545]       |    |          |
| 3   | 174 [164, 181]  | 564 [538, 611]       |    |          |
| 4   | 156 [149, 161]  | 542 [518, 586]       |    |          |
| 1, 2, 3, 4 | 167 [158, 173]  | 548 [523, 592]       |    |          |
We have used spectropolarimetric observations in the
5. Conclusions
are present in the coronal rain clumps studied in this work.
WWFA and the Ca\textsc{ii} in coronal rain clumps, they cannot be safely inferred using the
as those reported by Schad et al. (2016) can very well be present
applicable. This means that even though magnetic fields as large
larger than 1000 G. The highest $B$ value that we inferred with
our method was around 1000 G, with most values centred around
500 G. Nevertheless, we were limited to inferring magnetic field
values using the method described in Sect. 3.1. (b) Inferred values of the total magnetic field for the cases in which $\theta_{\text{POS}}$
could also be obtained. The colours of panel (b) indicate whether Eq. (5)
was satisfied (green) or not (red).

Fig. 9. (a) Inferred $B_{\text{LOS}}$ values using the method described in Sect. 3.1. (b) Inferred values of the total magnetic field for the cases in which $\theta_{\text{POS}}$
could also be obtained. The colours of panel (b) indicate whether Eq. (5)
was satisfied (green) or not (red).

ing to those of our observations (heights lower than 9 Mm) are
larger than 1000 G. The highest $B$ value that we inferred with
our method was around 1000 G, with most values centred around
500 G. Nevertheless, we were limited to inferring magnetic field
values that are compatible with the conditions for the WFA to be
applicable. This means that even though magnetic fields as large
as those reported by Schad et al. (2016) can very well be present
in coronal rain clumps, they cannot be safely inferred using the
WFA and the Ca\textsc{ii} 8542 Å line. The distribution of values of $B$
in Fig. 9 could lead us to believe that values higher than 1000 G
are present in the coronal rain clumps studied in this work.

5. Conclusions
We have used spectropolarimetric observations in the
Ca\textsc{ii} 8542 Å line with the CRISP instrument installed at
the SST in order to study the magnetic field of the low coronal
portion of catastrophically cooled active region coronal loops
by using coronal rain clumps as magnetic tracers. We have
employed the WFA as a simple and computationally inexpensive
tool to paint a picture of the type of magnetic fields that are
found in this part of the solar atmosphere. However, the WFA
can only be applied when certain conditions about the plasma
and the magnetic field are satisfied. This means that we needed
to make sure that the conditions for its applicability were
carefully assessed. The method employed here was a variation
in the method developed by Kriginsky et al. (2020), adding a
few extra steps related to the goodess of the fit that was
performed to the observed Stokes $I$ and $V$ profiles and using
velocity measurements to infer the magnetic field strength.

Given their density and size, it is a challenging task to ob-
tain spectropolarimetric signals in coronal rain clumps with the
observational capabilities of current instruments. We needed to
overcome this issue in order to obtain profitable results by per-
forming spatial averages of multiple connected pixels. We con-
structed groups of up to four pixels, which were generated ran-
domly inside each clump. By performing these averages, we
were able to increase the S/N of the data, increasing the possibil-
ity of obtaining magnetic information from coronal rain clumps.
This exercise proves that although it is a challenging task, it
is possible to obtain spectropolarimetric signals in these struc-
tures with the available instrumentation. We expect that with the
arrival of telescopes such as DKIST we will be able to gather
even more information with better resolution and S/N and paint
a more complete picture of the dynamics of coronal rain clumps.

One of the biggest limitations we have faced, besides the
presence of noise in the data, was the cadence. With a small
off-limb field of view and structures that follow a path mostly
parallel to the plane of the sky with velocities of 100 km s$^{-1}$,
a cadence of 36.33 s is far from ideal. It was difficult to spot a
significant number of clumps more than once in time and space
in order to approximate their magnetic field strength with the aid
of the velocity vector, so the results were limited. Additionally,
with a better cadence, we would have been able to obtain more
precise information about the geometric structure of the multiple
coronal loops that were present in the data, and that would have
allowed for a precise study of the variation in the magnetic field
strength with height.

We were also limited by the range of applicability of the
WFA regarding the values of the magnetic field strengths that we
could be safely inferred. As its name suggests, it can only be ap-
plied on weak-field regimes and, beyond a certain limit, we can-
not fully trust the values that were inferred. This circumstance
hindered our ability to compare our results with those of other
authors. It seems clear that a complementary inference method
needs to be used parallel to the WFA in order to obtain results
regarding the larger magnetic field values suggested by the right
tail of the distribution of Fig. 9b. What we have shown is that
the WFA is useful to determine the lower to medium range of
magnetic field values that seem to be present near the feet of
catastrophically cooled coronal loops. Since the magnetic field
strength is expected to decrease with height, the WFA should
also be applicable above the 9 Mm limit of our data.

Regardless of the limitations of the method and the observa-
tional challenges that we have faced, it seems clear that there is
an abundant presence of magnetic fields of hundreds of Gauss
in the lower coronal part of catastrophically cooled active region
coronal loops, and coronal rain clumps can indeed serve as tools
not only to map out the geometry of the loops with their motion,
but also as sources of information about the actual magnetic field
values in this part of the solar corona.

As shown in Sect. 4.3, we have estimated the temperature
and microturbulent velocity of coronal rain clumps and spicules
using the method described by Froment et al. (2020). Using this
method entailed the assumption that the temperature and micro-
turbulent velocity of the plasma seen in the Ca ii 8542 Å and Hα lines are the same. This is an approximation that must be considered when addressing the results obtained. The average temperature of coronal rain clumps and spicules was found to be very similar, albeit the temperature distribution of spicules was much broader. There was a noticeable difference in the measured microturbulent velocity, with the average value for spicules being about two times larger than that of coronal rain clumps. Considering the assumptions made in order to obtain these results, the next step would be to compare them to the results obtained with different approaches, such as the use of non-local thermodynamic equilibrium inversion codes.

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