Efficient coding of subjective value

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Preference-based decisions are essential for survival, for instance, when deciding what we should (not) eat. Despite their importance, preference-based decisions are surprisingly variable and can appear irrational in ways that have defied mechanistic explanations. Here we propose that subjective valuation results from an inference process that accounts for the structure of values in the environment and that maximizes information in value representations in line with demands imposed by limited coding resources. A model of this inference process explains the variability in both subjective value reports and preference-based choices, and predicts a new preference illusion that we validate with empirical data. Interestingly, the same model explains the level of confidence associated with these reports. Our results imply that preference-based decisions reflect information-maximizing transmission and statistically optimal decoding of subjective values by a limited-capacity system. These findings provide a unified account of how humans perceive and valuate the environment to optimally guide behavior.

At any given moment, organisms receive much more sensory and interoceptive information than they can physically process. These capacity limitations are thought to have biased brain evolution toward information-processing strategies that are maximally efficient for the control of behavior, an idea known as efficient coding. Such efficient-coding strategies can be observed in sensory systems where the precision with which neural representations encode different states of an environmental variable (for example, different orientations) is proportional to the frequency with which this state is actually encountered. This strategy ensures that the information encoded is as great as possible given the dynamic range of the physical system used to represent it. However, these representations not only need to be efficiently encoded but also need to be decoded and interpreted so that the resulting percepts provide maximally accurate information about the state of the world and the organism. Bayesian statistics imply that optimal perceptual processes would have to combine the representation of the environmental information (that is, the likelihood of a state) with an a priori expectation of these states. While efficient coding and Bayesian decoding theories may appear related, they have only recently been combined in a unified theoretical framework that can account for various low-level perceptual biases. But whether similar encoding and decoding strategies also operate in domains other than low-level perceptual systems remains an open question.

In the domain of preference-based decisions, it is commonly assumed that organisms rely on strategies that maximize the utility of the chosen option, based on stable and accurate representations of preferences that are not systematically affected by processing-resource constraints. However, empirically observed choice behavior often deviates from the predictions of rational choice theory. Purely descriptive theories of such anomalies have been offered, postulating either competition between parallel action-selection processes based on simple heuristics or some type of arbitrary external noise that has no clear psychological or neural basis. While such theories can account for some observed effects of choice variability, biases, or confidence in isolation, a common framework linking these different aspects of behavior is largely missing. Moreover, these models sometimes contain assumptions about value representations that appear implausible given the constraints imposed by the limited-capacity nature of biological systems.

To account for these limitations, recent work has sought to find shared principles in the mechanisms underlying subjective valuation and sensory perception. Theories from this line of research have suggested that subjective value representations may resemble percepts in that they are derived by inference processes that exploit prior information about the relevant distribution of value stimuli in the environment. Moreover, related lines of work suggest that neural reward circuits can flexibly adapt to different value contexts in the environment, possibly consistent with the notion that neural resources are allocated efficiently to the encoding of subjective values. However, it is unknown whether efficient coding and Bayesian decoding principles are indeed used jointly to generate preference representations, and it is unclear whether this information-processing scheme can explain the variability, biases, and confidence in value-based decisions in humans. This lack of knowledge may reflect that the distribution of subjective values in the natural environment is not easily measurable (in contrast to corresponding distributions of sensory signals), since it depends on the long-term experience of each specific organism with the objects in its environment.

Here we propose a way to test whether preference-based decisions are indeed guided by a value representation scheme that combines both efficient coding and Bayesian-decoding principles. We achieve this by introducing a novel approach for studying subjective valuation that takes account of the important fact that neither decision-makers nor experimenters have direct access to the ‘true’ stimulus values underlying all value-related behaviors (for example, ratings and choices). We demonstrate with modeling and behavioral experiments that choice variability, biases, and confidence in human preference-based decisions can all be explained by a single value-inference process. This process maximizes information transmission by optimally allocating limited resources to value representations, based on prior knowledge about the distribution of object values in the individual environment. Our approach accounts comprehensively for several aspects of value judgements and value-based choices and proposes that humans may make value-based choices optimally given resource constraints.

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Results

Efficient coding of subjective value. In studies of perceptual decisions, experimenters usually have complete knowledge of any experimental stimulus value $v$ (for instance, the angular orientation of displayed Gabor patches). This is different in experiments studying value-based choices, since experimenters have no direct access to the ‘true’ value $v$ of the presented object to an observer (Fig. 1a). Here we assume that this ‘true’ value $v$ has been shaped by each observer’s personal history of experiences with this type of object and is therefore entirely subjective. A common strategy adopted by experimenters is thus to first derive an estimate $\hat{v}$ of this subjective value—based on empirical choices or subjective reports (Fig. 1a)—that is subsequently used as input to a decision model. In contrast, if the prior distribution has higher density over low subjective values, lead to higher choice consistency for higher-valued goods (b). In contrast, prior distributions with higher density over high subjective values lead to higher choice consistency for lower-valued goods (b). Red arrows in b and c represent the shifted direction of the center of the prior relative to the indifference subjective value $v = 0$. Behaviors typically have to be given on physically bounded rating scales that can differ across different settings. To account for this, we assume that the individual’s internal subjective scale for $v(r)$ is physically unbounded but can be flexibly mapped via a function $g(\hat{v})$ to any bounded scale in line with experimental demands (Methods).

Inspired by previous work in the perceptual domain, we assume that encoding of subjective values is efficient in the sense that the mutual information between the stimulus values $v$ and the internal response $r$ is maximized. This results in optimal use of the underlying neuronal scale given the expected/learned natural distribution of values in the given environment, that is, the prior $p(v)$. Different from work in the perceptual domain and standard approaches in neuroeconomic studies, we suppose that the experimenter has no knowledge about the specific stimulus value $v_i$ that generated the observed rating scale value $\hat{v} = g(\hat{v})$. However, if the experimenter obtains several value ratings $\hat{v}$ for a given good (and if she repeats this for the full distribution of goods in a given context or environment), then it is possible to infer the stimulus value $v_i$ that is most likely to have generated the observed rating distribution for that good (Methods and Supplementary Fig. 1). Moreover, if individuals employ this encoding approach, then the values $v_i$ inferred based on the rating data should predict subsequent choice behavior in a multichoice task. For instance, in a two-alternative choice task, the optimal strategy is to choose good 1 over good 2 if $\hat{v}_1 > \hat{v}_2$ are the Bayesian posterior means of each good, respectively (see Methods).

One can also make predictions of choice discriminability between two objects based on their position in the rating scale (Fig. 1b,c). If the prior distribution has higher density over low subjective values, then predicted discriminability resembles a U-shaped function, but with higher choice accuracy for lower-valued goods (Fig. 1b). In contrast, if the prior distribution has higher density over high subjective values, then higher choice accuracy should be
observed for higher-valued goods (Fig. 1c). Interestingly, the latter prediction would be diametrically opposite to predictions based on Weber’s law, which generally assumes that higher-value magnitudes should lead to poorer discrimination. Our efficient-coding theory implies that Weber’s law should hold in the case of a particular kind of prior distribution that may be realistic for some sensory magnitudes, but not for the distribution of values for consumption goods assumed here.

Subjective value ratings and choice behavior. In a first behavioral experiment (experiment 1), we presented a set of food items to \( n = 38 \) study participants and asked them to indicate on a continuous rating scale their preference to consume the presented item (Fig. 2a and Methods). Crucially, the participants were familiar with the food products and had seen all of them before the ratings took place, ensuring that they could effectively use the full range of the rating scale. The products (\( M = 64 \) goods) were a representative sample of products typically encountered in the two biggest supermarket chains in Switzerland. Nevertheless, we ensured before testing that participants were indeed familiar with all products (Methods).

We then asked participants to rate the same items a second time, but crucially, they had been unaware that this second rating phase was going to take place, thus allowing a clean estimation of variability in the decoded values (Methods and Fig. 2b). We tested whether this variability actually reflected the value coding/decoding operations rather than just random noise or an artifact of the bounded rating scale. To this end, the same participants underwent a series of incentive-compatible choices in which they selected from pairs of the previously rated food items the one item they preferred to eat. We defined a consistent choice as a trial in which the subject chose the item they had assigned a higher average rating across the two previous ratings. Choice consistency was affected by the value difference between the two items’ prior ratings: the higher the value difference, the more consistent the choices (multiple logistic regression, \( \beta_{\text{difference}} = 0.44 \pm 0.05, P < 0.001; \text{Fig. 2d} \)). This concurs with the long-held notion that stronger evidence leads to more consistent choices. Importantly, choice consistency also depended on the variability in the value ratings: the higher this variability for the items on a given trial, the less consistent the decision (\( \beta_{\text{variability}} = -0.21 \pm 0.05, P < 0.001; \text{Fig. 2d} \)). Extending this trial-to-trial effect of rating variability, we observed that each participant’s average level of variability in the rating task was negatively correlated with the slope of the logistic regression of her individual choices on the items’ mean value difference (\( \beta_{\text{slope}} = -0.77 \pm 0.20, P < 0.001; \text{Fig. 2e} \)). In other words, the higher the variability in the initial value ratings, the less consistent the subsequent choices between the rated items, both compared across trials and across participants. This already suggests that properties of the value coding/decoding operations can somehow affect preference-based choices, but it does not characterize by what mechanisms they may influence the observed decisions.

In the next sections, we will address this question by formal tests of the theoretical framework outlined in our model specification.

In experiment 1, the rating scale was continuous and without numerical cues (Fig. 2a). One may wonder whether rating variability might represent imprecisions in the participants’ assignment of the decoded subjective values to this rating line. We therefore conducted a second experiment (experiment 2, \( n = 37 \)) in which the rating scale was divided into discrete steps with explicitly assigned numerical values (Fig. 2a and Methods). The variability in ratings across this scale clearly resembled the shape observed in experiment 1 (Fig. 2c) and had a similar significant impact on choice behavior (\( \beta_{\text{variability}} = -0.25 \pm 0.05, P < 0.001; \text{Fig. 2d} \)). Again, each participant’s level of variability in the rating task correlated negatively with the slope of the regression of choice consistency on value difference between the goods (\( \beta_{\text{slope}} = -1.2 \pm 0.25, P < 0.001; \text{Fig. 2f} \)). Thus, the influence of rating variability on subsequent choices does not depend on specifics of the rating procedure but may reflect characteristics of the noisy coding/decoding operations used by the observer to estimate the subjective value.

Testing the efficient-coding hypothesis. We now investigate to what extent the observed rating variability in experiments 1 and 2 can be explained by the efficient-coding model. We started by inferring the values \( v_{1,\ldots,M} \) of each good \( m \) that maximized the likelihood of the observed set of ratings for each participant (Methods). In experiments 1 and 2, the rating dataset consisted of \( M = 64 \) and \( M = 61 \) goods, respectively, with \( N = 2 \) ratings for each good. The fitted model successfully captured the empirically observed rating variability (Fig. 2b,c) and the distribution of subjective value estimates \( v \) (Supplementary Fig. 2). We compared the quality of these efficient-coding model fits with those of a simple flexible model that assumes constant Gaussian noise over the rating scale with no prior distribution constraints on the values \( v_{1,\ldots,M} \). For both experiments 1 and 2, the efficient-coding model explained the rating distribution better than the alternative model (Supplementary Fig. 3).

Exploration of the rating data revealed that the distribution of ratings was highly variable across participants (Supplementary Figs. 4 and 5), perhaps indicating that each individual holds different priors over values due to different long-term experience. The inferred prior distributions for both experiments based on our model revealed that the expected value of the prior across the population was shifted toward higher values (Fig. 2b,c). Choice discriminability should therefore resemble the shape predicted in Fig. 1c. If the subjective values of the products are derived using efficient-coding principles, then using the framework described above should allow us to predict each individual’s preference-based decisions. It is important to emphasize that for these prediction analyses, we fixed for each participant the parameters of the prior distribution \( p(v) \) and the stimulus values \( v_{1,\ldots,M} \) to the specific values obtained when fitting the model to the separate rating data. Using these out-of-sample parameters and values, and only adjusting the encoder and external noise, our model did a good job at predicting the choice data (Fig. 2g,h), as suggested by both the qualitative predictions and leave-one-out cross-validation metrics (Methods and Supplementary Note 1). To determine which aspects of the operations formalized in the efficient-coding model are most relevant for explaining behavior, we compared the predictive power of our model to that of alternative models (Supplementary Note 1). For both experiments, the efficient-coding model predicted the data best, as suggested by both the qualitative predictions and leave-one-out cross-validation metrics (Supplementary Note 1).

It may be argued that the specific pattern of choices observed in our experiments could also be captured by a model that does not contain efficient coding but instead fits the full shape of the likelihood function to the observed data, as done for example in previous work on perceptual discrimination. However, it is important to emphasize that our approach does not require us to fit arbitrary shapes of likelihood functions, as these shapes naturally arise from the efficient coding formalized in our model, which only requires fit of one free parameter: noise in the efficient-coding space (for a detailed discussion of this topic see Supplementary Note 2). Thus, the explanatory power of our model does not reflect the general flexibility of Bayesian inference per se but specifically relates to the efficient coding of values embedded in the Bayesian inference process.

The results presented so far suggest that subjective-value representations guiding human preference-based decisions are inferred and employed optimally using both efficient coding and Bayesian decoding. However, it remains unclear whether internal noise due to efficient coding is the main factor explaining fluctuations and potential biases in subjective-value estimations. We investigate this issue in the following section.
Illusions of subjective value. The theory used here predicts in general that for a stimulus with value \(v_i\) near the peak of the prior, the subjective value estimate \(\tilde{v}\) (and the resulting rating \(\tilde{v}\)) should be biased away from the prior, with the strength of this bias determined by the degree of noise in the internal representations used for inference\(^1\). We thus investigated whether a conceptually similar type of bias emerges during subjective-value estimation, reflecting an expectation-induced preference illusion and further supporting efficient coding of subjective value.

The estimation of this valuation bias necessarily requires knowledge of the exact stimulus value \(v_i\) that serves as input on any given trial, which is difficult in our case since the experimenter does not have direct access to \(v_i\) (Fig. 1a). To cope with this problem, we first derived predictions of the estimation bias for different levels of...
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Fig. 3 | Illusion of preference (experiment 3). a, Model-predicted biases for two degrees of internal measurement noise (σ) during subjective-value estimations: high (red, generated by short valuation exposure) and low (black, generated by long valuation exposure). b, Model-predicted differences of the biases for high and low σ across the value-rating scale. c, Difference of the empirical estimates between low and high exposure times (n = 24, mean data are black dots with s.e.m. across participants; blue line interpolates these data for visualization). Note the qualitative and quantitative overlap with the model prediction in b. This suggests that human valuation exhibits complex illusions of subjective preference, as predicted by the Bayesian and efficient-coding hypothesis (see also Supplementary Fig. 7). Lower and upper boxplot hinges correspond to the 25th and 75th percentiles and each semitransparent dot represents the data of one participant. The lower whiskers represent the lowest observed value within Q1 and 1.5×Q1, and upper whiskers represent the highest observed value within Q3 and 1.5×Q3, where Q1 and Q3 are the first and third quartile, respectively.

internal noise σ in the value representations. We assumed that this noise varies with the stimulus presentation times, based on theoretical frameworks postulating that value estimates are constructed using samples from memories/emotions associated with the physical features of the objects. This suggests that a reduction in visual stimulation time should reduce the number of samples that can be drawn and should therefore increase the noise in the internal value representations. To make this intuition explicit, we formulated a mathematical proof confirming that the number of discrete samples (for example, memories) that can be drawn over time is inversely proportional to the level of encoding noise in a capacity-limited system (Supplementary Note 3). Crucially, this proof provides a normative foundation for the theoretical frameworks motivating our approach and confirms the validity of the assumptions underlying our simulations and experimental strategy.

To derive initial qualitative predictions for the value estimation bias for different presentation times—and therefore levels of encoding noise—we performed model simulations using the prior p(ν) obtained in experiments 1 and 2, with the consequence that its peak was slightly shifted to the right of the rating scale (Fig. 2b,c). We selected two levels of encoding noise σ based on the noise levels observed in experiment 1 (see Supplementary Note 4 for a detailed discussion of the relation between encoding noise and the specific bias pattern). The simulations predicted biases for long exposure times (low σ, black line in Fig. 3a) and short exposure times (high σ, red line in Fig. 3a) that are markedly different once the value estimates have been mapped onto the bounded rating scale via g(ν). Crucially, the difference between these two predictions (high and low σ) is independent of νc:

\[
\left(\hat{\nu}_{\text{high}} - \nu_0\right) - \left(\hat{\nu}_{\text{low}} - \nu_0\right) = \hat{\nu}_{\text{high}} - \hat{\nu}_{\text{low}}
\]

Figure 3b shows that simulated rating trials with short exposure time (that is, high σ) have stronger repulsive (‘anti-Bayesian’) biases near the center of the prior (intersection point to the right of the center of the rating scale), but also stronger attraction biases when ν0 is farther away from the peak of the prior. For values close to the prior, this prediction agrees with previous work showing repulsive noise-related biases in perceptual tasks; however, as ν0 moves away from the prior, our simulations predict the opposite tendency (attraction) that would also be expected based on classical Bayesian frameworks.

We devised a behavioral framework (experiment 3) to investigate whether these model-predicted biases are in fact observed for subjective value estimations. Healthy individuals (n = 24) rated goods with similar procedures as in experiment 1. However, for the first round of ratings, a randomly determined half of the goods for each participant were presented for a duration of 900 ms and the other half for a duration of 2,600 ms. Participants did not know whether
Fig. 4 | Confidence (experiment 4). a, Participants (n=28) provided value ratings as in experiments 1 and 2, but also rated their confidence in the value ratings. Participants entered their value and confidence ratings by adjusting the location of a green arrow underneath each rating scale. b, Rating variability plotted as a function of each item’s mean rating across both rounds (solid black dots) was higher for low-rated items (β = −0.18 ± 0.04, P < 0.001). c. Posterior estimates of the expected value of the prior are shifted toward higher rating values (the zero position maps to the center of the rating scale). d. Posterior probability density functions (PDF) were constructed for four symmetric subjective values v (different colors) in the unbounded subjective scale. Groups of densities on the left (light colors) and right (dark colors) reflect low and high subjective values, respectively. Given the expected value of the prior (c), the efficient-coding model predicts lower levels of confidence for low-rated goods (relatively wide posteriors; light colors) than for high-rated goods (relatively narrower posteriors; dark colors). e. Empirical confidence ratings (solid red dots) match the predictions (blue dots) of the best-fitting confidence model (see also Supplementary Table 2) across different value ratings (x axis). Confidence was higher for higher model-predicted subjective values (β = 0.22 ± 0.070, P = 0.002). f. Confidence relates to value-rating variability (shown is the partial correlation after controlling for rating value). As predicted by the model, these two metrics are negatively correlated (r = −0.59, P < 0.001). Dots represent the data of single participants, the blue line represents the identified correlation line, and the shaded area the 95% confidence interval of this line. In all other plots, error bars around data points represent s.e.m. across participants. For the boxplots, lower and upper hinges correspond to the 25th and 75th percentile and each semitransparent dot represents the data of one participant. The lower whiskers represent the lowest observed value within Q1 and 1.5 x Q1, and upper whiskers represent the highest observed value within Q3 and 1.5 x Q3, where Q1 and Q3 are the first and third quartile, respectively. In b and e, *P < 0.005.

Fig. 3 | Temporal order effects. Image presentation times were not randomized, and participants were instructed to then provide their rating as fast as possible (mean reaction times (RTs) of 1.53 ± 0.45 and 1.39 ± 0.4 for low and high exposure times, respectively, see Supplementary Fig. 6). Thus, the effective sampling time (time from the onset of stimulus presentation until response) was 1.53 ± 0.4 s longer for long exposure times (β = 1.4 ± 0.08, P < 0.001; Supplementary Fig. 6), supporting our assumption that participants could draw a higher number of samples (and therefore reduce internal noise in the value representations) for images with long exposure times. We computed the difference in the ratings between short and long durations and plotted this difference as a function of the rating of the long duration (Fig. 3c). The results of this analysis match the non-intuitive quantitative predictions of the efficient-coding model (Fig. 3b), in showing systematic repulsion for the four data points near the peak of the prior and attraction for the other values that are farther away from the prior (Supplementary Fig. 7). Note that the repulsion effect that is both predicted and observed here at the center of the scale is not confined to this location for every possible context; its location and extent over the rating scale depends on the interaction of the three key parameters of our model: the prior location, prior shape, and level of encoding noise (Supplementary Note 4).

Control analyses confirmed that our results are not caused by systematic temporal order effects (no difference in value ratings between the first and second rounds for each of the exposure times; paired t-tests, all P > 0.18). We also compared the accuracy of our model’s predictions to that of control models in which we factorially varied all possible sources of noise that could in principle have affected the ratings (pre-encoding noise, efficient-coding noise, post-encoding noise, and lapses). Models without efficient coding lead to very different predictions that are not supported by our empirical data (Supplementary Fig. 8). To test this quantitatively, we performed a factorial model comparison to quantify the strength of empirical support given by our data for the presence of each noise source (Supplementary Fig. 9 and Supplementary Table 1). This revealed that the only noise source reliably accounting for the variation in subjective value estimation due to time pressure is internal noise in efficient coding (Bayes factor > 100; see Supplementary Fig. 9).
This strongly suggests that the biases in subjective value estimates observed in experiment 3 originate in the efficient-coding operations formalized in our model.

Confidence in subjective valuation. It has been suggested that the perceived confidence in subjective-value reports reflects a second-order judgement (the confidence rating) about a first-order judgement (the subjective-value rating)\(^1\). However, two important issues have remained unaddressed. First, previous work has not explicitly defined a generative model of the encoding and decoding of value representations; second-order statements about these ratings would therefore be subject to the same problems curtailing the validity of the ratings themselves. Second, previous work has remained agnostic about both the information structure of values in the environment and capacity limitations. We therefore tested whether the reported confidence in subjective value estimations can be predicted based on the encoding/decoding process proposed here.

We conducted a new experiment (experiment 4) in which participants provided value ratings as in experiment 1, but they now also gave a confidence rating after each value rating (Fig. 4a). We inferred the subjective values \(\nu(1,\ldots,M)\) exactly as for experiments 1 and 2. Once again, we found a shift of the expected prior (that is, its mean) toward higher values alongside higher rating variability for higher- than lower-rated items (hierarchical linear regression of rating variability for each item versus mean rated value: \(\beta_{\text{RandEffects}} = -0.18 \pm 0.04, P < 0.001\)). Based on these results, we derived three qualitative predictions for the confidence ratings based on the definitions of confidence formulated above. First, confidence should be higher for rating values near the extremes of the rating scale (Fig. 4d), reflecting the transformation from the subjective space to the bounded scale. This prediction is in line with previous work\(^1\). Second, given the shift of the prior density toward higher subjective values (Fig. 4c), the efficient-coding framework predicts that the second-order judgement of the posterior probability perceived in the rating scale should decrease for item values toward the right side of the rating scale; confidence reports should therefore be higher for items with higher subjective value (Fig. 4d). Third, because lower levels of variability in the rating estimates generate narrower posterior distributions, the average variability of each participant’s ratings should be negatively related to her general level of confidence.

The data (Fig. 4e,f) confirm all three predictions. First, confidence increases for values closer to the extremes of the rating scale (quadratic effect \(\beta_{\text{RandEffects}} = 0.41 \pm 0.03, P < 0.001\)). Second, confidence was higher for higher model-predicted subjective values \(\nu_m(\beta_{\text{RandEffects}} = 0.22 \pm 0.070, P = 0.002)\). This runs counter to previous suggestions\(^1\) that confidence ratings should be symmetric with respect to the center of the rating scale: both our model and empirical data reveal that this is not necessarily the case, as the confidence ratings depend on the prior distribution (Supplementary Table 2). Third, across participants, the higher the variability in the subjective value estimations, the less confident the participants are (\(\beta_{\text{RandEffects}} = -0.59, P < 0.0011\)). Crucially, this regression analysis controls for the mean value ratings for each participant (Fig. 4f), thereby confirming our model predictions that confidence relates to rating variability independently of how valuable the participants rated the items. Finally, to test these model predictions more quantitatively for the observed data using our framework, we implemented 11 different proposed models of how confidence may be derived\(^{13,33-34}\) from the posterior distributions of rating values given by our framework (see full details of the model specifications in Supplementary Table 2). Crucially, we fixed both the parameters of the prior distribution and values \(\nu(1,\ldots,M)\) for each participant to the values obtained by fitting the model to her prior rating data. We found that a model based on the statistical definition of confidence (that is, the probability that the rating is correct\(^{33,34}\)) provided the best fit to the empirical confidence reports (Fig. 4e and Supplementary Table 2). These results confirm that our efficient-coding model can capture the value inference processes that underlie not only subjective value estimates but also the reported confidence in these estimates.

Discussion

Our work demonstrates that variability, biases, and confidence in preference-based choices are all consistent with information-maximizing transmission and statistically optimal decoding of values by a limited-capacity system. This suggests that principles governing the encoding and interpretation of low-level sensory signals are also relevant when humans report and choose based on subjective preferences. More specifically, our results support theoretical proposals according to which, just as in the case of sensory systems, subjective value systems optimize the use of limited resources for processing value information and exploit environmental regularities to guide preference-based decisions\(^{16,33,35}\). Thus, our findings provide a fundamental step toward a unified account of how humans perceive and evaluate the environment to optimally guide behavior.

Our work introduces a new framework that may serve to improve the modeling and prediction of preference-based decision-making, and more generally any cognitive process that involves fully subjective value estimations (such as pain\(^1\) and health\(^1\) perception, to mention only two examples). We demonstrate that the common practice of using value ratings as inputs to decision models\(^{1,13,14,16,17,19,20}\) is suboptimal, since these reports should be just as variable and biased as the choices that the experimenter wants to model. This is not a trivial issue, as both ratings and choices can be subject to complex nonlinearities due to the encoding/decoding strategies implemented by the valuation system. Our model provides a solution to this problem, since it makes it possible to employ a single set of ratings to determine both the observer’s subjective values and their underlying prior distribution, while simultaneously accounting for capacity limitations. These parameters and values can then be used to predict fully independent preference-based decisions with higher accuracy than existing standard approaches in the literature. This procedure differs from traditional economic approaches that derive preferences directly from observed choices\(^31\) and that ignore the processes involved in estimating subjective values (and the associated sources of variability). Our results show that this ignorance is not warranted; a detailed understanding of these processes should be a critical aspect to consider in theories of decision-making and economic behavior\(^31\).

In our model specification, variability in subjective value estimates and choices emerges from both internal noise in the coding of value and unspecified (external) noise in the decision process. This perspective is fundamentally different from standard approaches where preference variability is solely attributed to unspecified noise in the decision process (for example, noise added to deterministic value functions\(^33\) through the application of a softmax function or diffusion noise in sequential sampling models\(^{11-13}\)). Based on our empirical and modeling work, we argue that positing unspecified sources of noise in the decision process may be insufficient, given that accounting for noise involved in the coding of value appears to be crucial for deriving more accurate predictions of economic decisions\(^31\). Even though some characteristics of the models used for this purpose (for example, encoding rules and loss functions of the Bayesian encoder) may be refined by future research on both perception\(^31\) and subjective valuation\(^31\), our findings clearly illustrate the general utility of this approach.

In some respects, our model of the coding of value resembles the one posited by decision-by-sampling theory\(^31\). That theory proposes that estimated subjective values directly reflect samples drawn from an internal noisy representation of value, but unlike in our approach, no optimal Bayesian decoding is assumed. As a consequence, decision-by-sampling theory cannot account for our
finding that biases in valuation are changed by time pressure, since drawing fewer samples should lead to value estimates that are noisier, but not different on average. This contrasts with the predictions of the framework presented here, which we show to be fully congruent with the biases observed under time pressure.

Our results support the idea that reported confidence in subjective-value estimations is well captured by a statistical measure of confidence\(^1\). While a recently proposed framework\(^2\) provides an elegant model of confidence judgements for individual value estimates, it does not provide a precise account of what information should actually be encoded but focuses only on what may be decoded. Additionally, that framework does not account for the effects of capacity limitations in information processing and the distribution of object values in the environment. Our work provides a more comprehensive characterization, by demonstrating that the same efficient-coding framework that accounts for biases and variability in subjective value estimates and choices also accounts for the reported confidence in these value estimates. In general, we hope that these results may motivate researchers to further develop explicit process models of metacognition\(^3\). While our work highlights similarities between perceptual and value inference, it has remained agnostic as to how the internal response used for this purpose is derived from low- and high-level sensory signals. Understanding such feature extraction will be important for characterizing how the internal value response may be constructed, for example, by sampling from memory\(^4,5\) and emotion systems\(^6\). While we formally demonstrate that the precision of encoded subjective values in capacity-limited systems may relate to the number of discrete samples that can be drawn (for example, from memory or emotion systems), we have so far only focused on the encoding and readout of simple one-dimensional subjective values associated with an object. However, the framework used here could be parsimoniously extended to incorporate a whole range of lower-level sensory signals and to encompass more complex hierarchical structures. Despite this interesting challenge to further understanding the construction of preferences\(^7\), it is remarkable that a simple normative specification inspired by fundamental principles of low-level sensory perception can capture important aspects of preference-based decisions.

Bayesian models have often been criticized for allowing an arbitrary choice of prior and likelihood functions, as a consequence of which it is suggested that their predictions are vacuous\(^8\). However, in this study, we have shown that by fully constraining the decision model to the distribution of object values—while taking account of capacity constraints—it is possible to accurately capture preference-based choice behavior using a parsimonious model. In line with previous work on low-level sensory perception\(^9\), our results demonstrate that the above-mentioned critique is not always valid. This should motivate researchers to pursue the identification of optimal solutions to computational problems posed by the environment—in both perception and subjective valuation—without ignoring the fact that biological systems are by definition limited in their capacity to process information.

Taken together, our findings suggest that resource-constrained models inspired by models of perception\(^10,11\) may have far-reaching implications not only in neuroscience, but also in psychology\(^12,13\) and economics\(^14,15\). Such models offer the prospect of explaining seemingly irrational aspects of choice behavior, grounded in the need to represent the world with only finite precision. Recent work suggests that features of economic decisions such as risk aversion\(^16\) and preference reversals\(^17\) can be understood as further examples of biases resulting from optimal Bayesian inference from imprecise internal representations of value. This supports our emphasis on the desirability of developing models of decision-making that account simultaneously for the organism’s goals, its environment, and its biological constraints.

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Any methods, additional references, Nature Research reporting summaries, source data, statements of data availability and associated accession codes are available at https://doi.org/10.1038/s41593-018-0292-0.

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**Author contributions**
R.P. and C.C.R. designed the study. R.P. collected and analyzed the data. All authors interpreted the results and wrote the manuscript.

**Competing interests**
The authors declare no competing interests.

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Methods

Participants. The study tested healthy young volunteers (total n = 127, age 19–37 years, 55 females; n = 38 in experiment 1, 17 females; n = 37 new participants in experiment 2 (replication of results obtained in experiment 1), 14 females; n = 24 new participants in experiment 3, 11 females; and n = 28 new participants in experiment 4, 13 females). Participants were randomly assigned to each experiment. No data were excluded from the analyses. Sample size was determined based on previous studies using similar stimuli and tasks. Participants were instructed about all aspects of the experiment and gave written informed consent. None of the participants suffered from any neurological or psychological disorder or took medication that interfered with participation in our study. Participants received monetary compensation for their participation in the experiment, in addition to receiving one food item in the decision-making task (see below).

The experiments conformed to the Declaration of Helsinki and the experimental protocol was approved by the Ethics Committee of the Canton of Zurich. For all experiments, participants were asked not to eat or drink anything for 3 h before the start of the experiment. After the experiment, participants were required to stay in the room with the experimenter while eating the food item that they had chosen in a randomly selected trial of the decision-making task (see below). All experiments took place between 09:00 and 17:00. Our experiments did not include different conditions of the determinant priors by the experimenter, since the participants themselves sorted trials into conditions as a direct consequence of their ratings and choices given during the experiment. Blinding was therefore neither necessary nor possible.

Value rating task. Experiments 1 and 2 consisted of three main phases: (1) rating phase 1, (2) rating phase 2, and (3) the decision-making task. In rating phase 1, we asked the participants to provide subjective-preference ratings for a set of 60 food items using an on-screen slider scale (Fig. 2a). All of the food items were in stock in our lab and participants were notified about this. Importantly, participants saw all food products before the ratings so that they could effectively use the full range of the rating scale. Moreover, participants knew that all products were randomly drawn from the two biggest supermarkets in Switzerland. Based on pilot measurements and previous studies11,51 in our lab, we selected food items that varied all the way from items that most participants would find unappealing (for example, raw broccoli) to items that most participants would find highly appetitive (for example, ice cream). This was important as our model should capture the full range of subjective values that humans typically assign to food items on a daily basis. During the ratings, participants indicated 'how much they wanted to eat the presented food item at the end of the experiment'. The slider scale was continuous in experiment 1 with no numbers displayed (Fig. 2a), whereas the rating scale in experiment 2 was divided in 20 steps of equal size with numbers displayed under each step (Fig. 2a). This was done to ensure that the effects observed in experiment 1 did not depend on the specific choices of reference points in the middle of the rating scale. Participants were informed that the rightmost endpoint would indicate items that they would most love to eat, whereas the leftmost endpoint would indicate items that they would most hate to eat. The initial location of the slider was randomized for each item to reduce anchoring effects.

Rating phase 2 was identical to rating phase 1 and took place immediately after phase 1. The order of the items' presentation was randomized. Crucially, participants were not informed before the rating phase that a second rating phase and a decision-making task would take place. This was important as it prevented participants from actively memorizing the location of the rating in the slider in the first phase, thus providing us with a clean measure of the variability in the value estimates.

In experiment 3, participants provided value ratings as in experiment 1, but for the first round of ratings, half of the goods were presented with a duration of 900 ms and the second half with a duration of 2,600 ms. For the second round of ratings, the presentation durations were inverted for each good. The exposure time (900 ms or 2,600 ms) was pseudo-randomly selected for each good in the first round of ratings, and participants did not know in advance for how long they were going to see each specific food item. The rating scale appeared only once the image disappeared from the screen (see Fig. 1a), and the participants were instructed to provide their rating as fast as possible (mean RTs 1.53 ± 0.45 and 1.39 ± 0.4 for low and high exposure times, respectively). Crucially, participants were not informed in advance about the details of the time manipulations.

In experiment 4, participants provided value ratings as in experiment 1, but indicated after each rating their confidence in their first-order rating (Fig. 4a). Following procedures of previous work2, we informed participants that the leftmost side of the rating scale means 'not at all' confident and the rightmost side means 'totally confident'.

Choice task. For experiments 1 and 2, immediately after the two rating phases, an algorithm selected a balanced set of decision trials divided into four value difference levels on the rating scale (rating difference ~5%, ~10%, ~15%, and ~20% of the length of the rating scale), as defined by the average rating across phases 1 and 2 provided by each participant. Decision-making trials started with central presentation of a fixation cross for 1–2 s. Immediately after this, two food items were displayed simultaneously, one in the upper and one in the lower hemifield (Fig. 2a). The food items were presented until response and participants had up to 4 s to make a choice. Participants were instructed to choose which of the two items (upper or lower) they preferred to consume at the end of the experiment. To make these choices, participants pressed one of two buttons on a standard keyboard with their right-index finger (upper item) or their right thumb (lower item). In experiments 1 and 2, we defined a consistent choice as a trial in which the subject chose the item with a higher mean rating from the prior rating phase. Each experimental session comprised a maximum of 240 trials (this depended on the rating distribution of each participant) divided into 6 runs of 40 trials each. The trials were fully balanced across rating-difference levels (~5%, ~10%, ~15%, and ~20% of the length of the rating scale) and location of consistent response option (up or down).

Model. We assume that the presentation of an object with stimulus value v elicits an internal noisy response v (encoding) that the observer uses to generate a subjective value estimate v (the decoded stimulus value). At the encoding stage, a function F(v) maps the stimulus space to a new space where the Fisher information is uniform over the entire real line. This requires the definition

\[ F(v) = \int_0^\infty p(v|x) dx \quad \text{for} \quad v > 0 \]

(2)

\[ F(v) = -\int_0^\infty p(v|x) dx \quad \text{for} \quad v < 0 \]

(3)

where \( p(v) \) is an improper prior distribution, so that \( F(v) \to \infty \) as \( v \to -\infty \), and \( F(v) \to -\infty \) as \( v \to \infty \). We assume that conditional on the value v, an internal noisy (neural) response is generated

\[ r = F(v) + \delta \]

(4)

with \( \delta \sim N(0, \sigma^2) \), where \( \sigma \) measures the degree of noise in the internal representation that is constant over all possible values F(v). We also note that the prior distribution for possible values of F(v) is uniform on the real line. The posterior mean estimate of F(v) (the estimator that minimizes mean squared error) is then given by

\[ \hat{F}(r) = E[F^{-1}(r + c)] \]

(5)

with \( c = \epsilon - N(0, \sigma^2) \). Here, \( E[.] \) means the expectation over possible values of \( c \). This estimator is a deterministic function that maps each measurement r to an estimated subjective value \( \hat{v}(r) \); this deterministic mapping therefore cannot account for trial-to-trial fluctuation in the value estimates. The variability in the value estimates arises because of the variability in the measurement r on each trial. Accounting for this variability, it follows that for any true stimulus \( v_0 \), the mean estimate should be given by

\[ E[\hat{v}(r)] = E[\hat{v}(F(v_0) + c)] \]

(6)

with \( c = \epsilon - N(0, \sigma^2) \). \( E[.] \) now means the expectation over possible values of \( (c_1 + \epsilon_2) \sim N(0, 2\sigma^2) \). In the small-noise limit, we can take a second-order Taylor expansion:

\[ F^{-1}(F(v_0) + \epsilon) \approx F^{-1}(F(v_0)) + \epsilon^\prime (v_0) + (1/2) \epsilon^\prime\prime (v_0) \epsilon^2 \]

(7)

where \( \epsilon \equiv \epsilon_1 + \epsilon_2 \), \( \epsilon(v_0) \equiv F^{-1}(v_0) \), and the derivatives of \( \epsilon(v_0) \) are evaluated at \( \hat{v}(F(v_0)) \). Taking the expected value over possible realizations of \( c \), we obtain

\[ \hat{v} \approx v_0 + \epsilon^\prime (v_0) \epsilon^2 + (1/2) \epsilon^\prime\prime (v_0) \epsilon^2 + \epsilon^2 \]

(8)

Conditional on a particular stimulus value \( v_0 \), this is a random variable with expected value

\[ E[\hat{v}(v_0)] \approx v_0 + \epsilon^\prime (v_0) \epsilon^2 + \epsilon^2 \]

(9)

and variance

\[ \text{Var}[\hat{v}(v_0)] \approx (\epsilon^\prime (v_0))^2 \epsilon^2 + \epsilon^2 \]

(10)

If we approximate this distribution by a normal distribution with the mean and variance just calculated above, we would obtain a probability density for \( \hat{v} \) given by

\[ p(\hat{v}; v_0, \theta, \sigma) = N(\hat{v}; v_0 + \epsilon^\prime (v_0) \epsilon^2, (\epsilon^\prime (v_0))^2 \epsilon^2 + \epsilon^2) \]

(11)

where \( \theta \) is a set of parameters of the prior distribution (see below). This expression is the likelihood of a given subjective value estimate \( \hat{v} \) conditioned on a true stimulus value \( v_0 \). If one wants to write the joint likelihood of a pair of values \( (\hat{v}, v_0) \) occurring when \( v_0 \) is drawn from the prior, one obtains
\[
\phi(\hat{\theta}, \sigma) = N(\tilde{\theta}, \sigma) = N(\tilde{\theta}, \sigma) = N(\tilde{\theta}_0 + \hat{\mu} \cdot \sigma^2, (\hat{\mu}^2 + \sigma^2) \times F(v))
\]

(12)

In addition to internal noise in the coding of value \( \sigma \), we also account for late noise in the decision stage (that is, post-decoding noise), which may capture any uninformative forms of downstream noise occurring during the response process that are unrelated to valuation per se. We assume this late noise to be normally distributed; therefore, it can be easily added to our model as follows (see Supplementary Note 1 for further discussion on the different sources of noise)

\[
p^\text{late}(\hat{v}; v_{01}, \sigma, \sigma_{\text{ext}}) = N(\tilde{v}, \sigma^2, \sigma_{\text{ext}}^2) = N(\tilde{v}, \sigma^2, \sigma_{\text{ext}}^2) \times F(v)
\]

(13)

The last part of the model defines the probability distribution in the space of the bounded rating scale. Without loss of generality, we assume that this scale is bounded from 0 to 1, with a monotonic mapping of subjective preferences that preserves preference ordering. Transforming the unbounded internal scale to this bounded physical scale requires a mapping that preserves monotonicity. Here we assume that the prior follows a logistic distribution

\[
\phi(\tilde{\theta}) = \frac{1}{1 - e^{-\tilde{\theta}}}
\]

and its first derivative is

\[
\phi'(\tilde{\theta}) = \frac{\tilde{\theta}}{1 - e^{\tilde{\theta}}}
\]

Recall that we are assuming here that the decision-maker maximizes mutual information between the input stimulus and the noisy measurement, therefore \( F(v) \) is defined as the cumulative density function (CDF) of the prior distribution \( \phi(\tilde{\theta}) \).

Here we assume that the prior follows a logistic distribution

\[
p(v; \mu, \sigma) = \frac{1}{4\pi} \text{sech}^2 \left( (v - \mu) / (2\sigma) \right)
\]

(17)

where \( \mu \) and \( \sigma \) represent the mean and scale, respectively. The advantage of using this distribution is that its CDF and both the first and the second derivative of the quantile function have closed-form solutions; however, any similar prior distribution could be used without greatly affecting the quantitative predictions presented here. \( F(v) \), \( \phi(\tilde{\theta}) \), and \( \phi'(\tilde{\theta}) \) are given by

\[
F(v) = \frac{1}{2} \left[ 1 + \text{tan}h \left( \frac{\tilde{\theta} - \mu}{2\sigma} \right) \right]
\]

(18)

\[
\phi(\tilde{\theta}) = \frac{\tilde{\theta}}{1 - e^{\tilde{\theta}}}
\]

(19)

\[
\phi'(\tilde{\theta}) = \frac{2(\tilde{\theta} - 1)}{e^{\tilde{\theta}} - 1}
\]

(20)

Thus, for any experimental dataset consisting of \( M \) goods and \( N \) value ratings for each good, we can find the set of parameters of the prior, the internal valuation noise \( \sigma \), external noise \( \sigma_{\text{ext}} \), and the true subjective values \( v_{(1) \ldots (M)} \) that maximize the likelihood of the observed set of ratings (under the constraint that \( v_{(1) \ldots (M)} \) is distributed following \( p(v) \)).

To compute choice consistency predictions that an experimenter would obtain when performing such analysis in the rating scale (Fig. 1d), we first computed for a fine-grained set of subjective values \( v_i \) their corresponding expected value and variance perceived in the rating scale (if we assume that the experimenter can obtain a large number of ratings for each good) via

\[
\mu_i = \int (v) \times N(0; v_i + \hat{\mu} \cdot \sigma^2, (\hat{\mu}^2 + \sigma^2) \times F(v)) dv
\]

(21)

and

\[
\sigma_i^2 = \int (v) \times \phi(v; \mu_i, \sigma^2, \sigma_{\text{ext}}^2) dv
\]

(22)

where the subscript \( (\cdot) \) reflects the expected value \( (\mu_i) \) and variance \( (\sigma_i^2) \) at position \( v \) in the rating scale. We then looked for expected values \( \mu_i \) closer to the values \( [0.1, 0.11, 0.12, \ldots 0.89, 0.9] \) and used their corresponding variance to approximate the level of choice consistency as follows:

\[
\Phi \left[ \frac{\mu_i - \mu_j}{\sqrt{\sigma_i^2 + \sigma_j^2}} \right] \times \phi \left[ \frac{\mu_i - \mu_j}{\sqrt{\sigma_i^2 + \sigma_j^2}} \right] / 2
\]

(23)

with \( \delta = 0.05 \) (note that different values of \( \delta \) move the accuracy curve up or down but do not affect the general U-shaped curve obtained in our predictions; see Fig. 1b,c).

**Behavioral analyses and statistics.** Preference-rating variability in experiments \( 1 (n = 38), 2 (n = 37) \), and \( 4 (n = 28) \) was computed as the standard deviation for each item across the rating phases 1 and 2. To visualize this effect, we plotted the standard deviation as a function of the mean rating (Figs. 2b and 4b). To investigate the influence of both value difference (VD) and rating variability on the consistency of choices (Fig. 2d), we performed a hierarchical logistic mixed-effects regression of choices (defining consistent \( = 1 \), inconsistent \( = 0 \) on three main regressors of interest, namely: value difference, summed-variability (Var, defined as the sum of the two standard deviations of the two food items presented in each trial), and the summed-value (OV, defined as the sum of the mean rating values of the two food items presented in each trial). All regressors of interest were included in the same model. Similarly, all the population-level regressions described for experiment 4 were based on a hierarchical linear mixed-effects regression approach. All mixed-effects regressions in this study had varying subject-specific constants and slopes (that is, we performed random-effects analyses). Posterior inference of the parameters in the hierarchical models was performed via the Gibbs sampler using the Markov chain Monte Carlo technique implemented in JAGS\(^\text{17}\), assuming flat priors for both the mean and the noise of the estimates. For each model a total of 10,000 samples were drawn from an initial burn-in step and subsequently a total of new 10,000 samples were drawn with three chains (each chain was derived based on a different random number generator engine, and each with a different seed). We applied a thinning of 10 to this final sample, thus resulting in a final set of 1,000 samples for each parameter. We conducted Gelman–Rubin tests\(^\text{18}^\) for each parameter to confirm convergence of the chains. All latent variables in our Bayesian models had \( R < 1.05 \), which suggests that all three chains converged to a target posterior distribution. We checked via visual inspection that the posterior population-level distributions of the final Markov chain Monte Carlo chains converged to our parametrizations. The \( P \) values reported for these regressions are not frequentist \( P \) values but instead directly quantify the probability of the reported effect differing from zero. They were computed using the posterior population distributions estimated for each parameter and represent the portion of the cumulative density functions that lies above/below 0 (depending on the direction of the effect). The regressions across participants reported for experiments 1, 2, and 4 were computed using robust linear regressions using the rfit function\(^\text{19}\) implemented in the statistical computing software R\(^\text{20}\).

To fit the efficient-coding model to the rating data in experiments 1, 2, and 4, we found the stimulus values \( v_{(1) \ldots (M)} \), parameters of the prior \( \tilde{\theta} \), encoding noise \( \sigma \), and external noise \( \sigma_{\text{ext}} \) that maximized the likelihood function \( p(v_{(1) \ldots (M)}; \tilde{\theta}, \sigma, \sigma_{\text{ext}}) \) of the observed set of ratings for each participant under the constraint that \( v_{(1) \ldots (M)} \) is distributed following \( p(v) \) (Supplementary Fig. 1). Alternatively, defining \( \tilde{v} = F(v) \), one can find the value estimates in the efficient space \( \tilde{v}_{(1) \ldots (M)} \) under the constraint that these are uniformly distributed. Using either approach, we found nearly identical results for the fitted parameters, which is expected for correct model specification. Posterior inference of the parameters for this model can be conveniently performed via the Gibbs sampler.

We used the stimulus values \( v_{(1) \ldots (M)} \) and prior parameters \( \tilde{\theta} \) fitted to the rating to predict choices in the two alternative-choice task in experiments 1 and 2. Following our modeling specification, over many trials the probability that an agent chooses an alternative with stimulus value \( v_1 \) over a second alternative with stimulus value \( v_2 \) is given by:

\[
P(v_1 > v_2 | v_1, v_2) = \frac{\text{Var}[\tilde{v}] + \text{Var}[\tilde{v}]}{\text{Var}[\tilde{v}] + 2\sigma_{\text{ext}}^2}
\]

(24)

where \( \Phi() \) is the CDF of the standard normal distribution and the expressions for \( \text{Var}[\tilde{v}] \) and \( \text{Var}[\tilde{v}] \) are given in equations (9) and (10) (see above). In other words, the input values of the choice model are fully constrained by the efficient-coding model based on the fits to the rating data and therefore \( \tilde{\theta}, \sigma, \sigma_{\text{ext}} \). The choice model has only two free parameters, namely the resource noise of the encoder \( \sigma \) and the external noise \( \sigma_{\text{ext}} \). Fits to the choice data were performed via the Gibbs sampler using a hierarchical Bayesian model assuming flat priors for both noise terms. When evaluating different models, we are interested in our model’s predictive accuracy for unobserved data, thus it is important to choose a metric for model comparison that considers this predictive aspect. Therefore, to perform model comparison, we used a method for approximating leave-one-out cross-validation that uses samples from the full posterior\(^\text{21}\). The smaller the
leave-one-out cross-validation, the better the fit. We found that in experiments 1 and 2, the best model was the efficient-coding model. Crucially, this finding is fully replicated when using a different Bayesian metric such as the Watanabe–Akaike information criterion (WAIC). Description of the different choice models tested here is presented in Supplementary Note 1.

**Reporting Summary.** Further information on research design is available in the Nature Research Reporting Summary linked to this article.

**Code availability.** Code to infer subjective values and prior parameters based on rating data is provided in the Supplementary Software.

**Data availability**
The data that support the findings of this study and the analysis code are available from the corresponding author upon reasonable request.

**References**
51. Polania, R., Motisa, M., Opitz, A., Grueschow, M. & Ruff, C. C. The precision of value-based choices depends causally on fronto-parietal phase coupling. *Nat. Commun.* 6, 8090 (2015).
52. Plummer, M. et al. JAGS: a program for analysis of Bayesian graphical models using Gibbs sampling. In *Proc. 3rd International Workshop on Distributed Statistical Computing (DSC2003)* (2003).
53. Gelman, A. et al. *Bayesian Data Analysis*. 3rd edn, (CRC Press, Boca Raton, 2013).
54. Venables, W. N. & Ripley, B. D. *Modern Applied Statistics with S*. (Springer, New York, 2002).
55. R Core Team *R: A Language and Environment for Statistical Computing* (R Foundation for Statistical Computing, Vienna, 2017).
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Reporting Summary

Nature Research wishes to improve the reproducibility of the work that we publish. This form provides structure for consistency and transparency in reporting. For further information on Nature Research policies, see Authors & Referees and the Editorial Policy Checklist.

Statistical parameters

When statistical analyses are reported, confirm that the following items are present in the relevant location (e.g. figure legend, table legend, main text, or Methods section).

- □ [ ] [ ] [ ] n/a
- [ ] [ ] [ ] Confirmed
- [ ] □ The exact sample size (n) for each experimental group/condition, given as a discrete number and unit of measurement
- [ ] □ An indication of whether measurements were taken from distinct samples or whether the same sample was measured repeatedly
- [ ] □ The statistical test(s) used AND whether they are one- or two-sided
- [ ] □ Only common tests should be described solely by name; describe more complex techniques in the Methods section.
- □ [ ] [ ] [ ] A description of all covariates tested
- □ [ ] [ ] [ ] A description of any assumptions or corrections, such as tests of normality and adjustment for multiple comparisons
- □ [ ] [ ] [ ] A full description of the statistics including central tendency (e.g. means) or other basic estimates (e.g. regression coefficient) AND variation (e.g. standard deviation) or associated estimates of uncertainty (e.g. confidence intervals)
- □ [ ] [ ] [ ] For null hypothesis testing, the test statistic (e.g. F, t, r) with confidence intervals, effect sizes, degrees of freedom and P value noted
- □ [ ] [ ] [ ] Give P values as exact values whenever suitable.
- □ [ ] [ ] [ ] For Bayesian analysis, information on the choice of priors and Markov chain Monte Carlo settings
- □ [ ] [ ] [ ] For hierarchical and complex designs, identification of the appropriate level for tests and full reporting of outcomes
- □ [ ] [ ] [ ] Estimates of effect sizes (e.g. Cohen's d, Pearson's r), indicating how they were calculated
- □ [ ] [ ] [ ] Clearly defined error bars
- □ [ ] [ ] [ ] State explicitly what error bars represent (e.g. SD, SE, CI)

Our web collection on statistics for biologists may be useful.

Software and code

Policy information about availability of computer code

| Data collection | Matlab, version 2015a |
|-----------------|-----------------------|
| Data analysis   | R, version 3.4; JAGS, version 4.0 |

For manuscripts utilizing custom algorithms or software that are central to the research but not yet described in published literature, software must be made available to editors/reviewers upon request. We strongly encourage code deposition in a community repository (e.g. GitHub). See the Nature Research guidelines for submitting code & software for further information.

Data

Policy information about availability of data

All manuscripts must include a data availability statement. This statement should provide the following information, where applicable:
- Accession codes, unique identifiers, or web links for publicly available datasets
- A list of figures that have associated raw data
- A description of any restrictions on data availability

The data that support the findings of this study are available from the corresponding author upon request.
Field-specific reporting

Please select the best fit for your research. If you are not sure, read the appropriate sections before making your selection.

- [ ] Life sciences
- [x] Behavioural & social sciences
- [ ] Ecological, evolutionary & environmental sciences

For a reference copy of the document with all sections, see nature.com/authors/policies/ReportingSummary-flat.pdf

Life sciences study design

All studies must disclose on these points even when the disclosure is negative.

| Sample size | Describe how sample size was determined, detailing any statistical methods used to predetermine sample size OR if no sample-size calculation was performed, describe how sample sizes were chosen and provide a rationale for why these sample sizes are sufficient. |
|-------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Data exclusions | Describe any data exclusions. If no data were excluded from the analyses, state so OR if data were excluded, describe the exclusions and the rationale behind them, indicating whether exclusion criteria were pre-established. |
| Replication | Describe the measures taken to verify the reproducibility of the experimental findings. If all attempts at replication were successful, confirm this OR if there are any findings that were not replicated or cannot be reproduced, note this and describe why. |
| Randomization | Describe how samples/organisms/participants were allocated into experimental groups. If allocation was not random, describe how covariates were controlled OR if this is not relevant to your study, explain why. |
| Blinding | Describe whether the investigators were blinded to group allocation during data collection and/or analysis. If blinding was not possible, describe why OR explain why blinding was not relevant to your study. |

Behavioural & social sciences study design

All studies must disclose on these points even when the disclosure is negative.

| Study description | Quantitative experimental study of how humans make subjective value-based decisions |
|-------------------|---------------------------------------------------------------------------------|
| Research sample   | University of Zurich students used as a representative sample of young healthy population. n=127 (55 females), age 19-37 |
| Sampling strategy | Random sampling procedure Sample-size was based on previous studies conducted in our lab (Polania et al, 2014,2015) |
| Data collection   | Visual stimuli were presented on a computer screen. Responses were inserted using a computer keyboard or mouse depending on the experiment |
| Timing            | Data was collected during the years 2015-2017, between 9:00am and 5:00pm |
| Data exclusions   | No data was excluded from the analyses |
| Non-participation | There were no dropouts |
| Randomization     | Participants were randomly assigned to each of the experiments |

Ecological, evolutionary & environmental sciences study design

All studies must disclose on these points even when the disclosure is negative.

| Study description | Briefly describe the study. For quantitative data include treatment factors and interactions, design structure (e.g. factorial, nested, hierarchical), nature and number of experimental units and replicates. |
|-------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Research sample   | Describe the research sample (e.g. a group of tagged Passer domesticus, all Stenocereus thurberi within Organ Pipe Cactus National Monument), and provide a rationale for the sample choice. When relevant, describe the organism taxa, source, sex, age range and any manipulations. State what population the sample is meant to represent when applicable. For studies involving existing datasets, describe the data and its source. |
| Sampling strategy | Note the sampling procedure. Describe the statistical methods that were used to predetermine sample size OR if no sample-size calculation was performed, describe how sample sizes were chosen and provide a rationale for why these sample sizes are sufficient. |
### Data collection
Describe the data collection procedure, including who recorded the data and how.

### Timing and spatial scale
Indicate the start and stop dates of data collection, noting the frequency and periodicity of sampling and providing a rationale for these choices. If there is a gap between collection periods, state the dates for each sample cohort. Specify the spatial scale from which the data are taken.

### Data exclusions
If no data were excluded from the analyses, state so OR if data were excluded, describe the exclusions and the rationale behind them, indicating whether exclusion criteria were pre-established.

### Reproducibility
Describe the measures taken to verify the reproducibility of experimental findings. For each experiment, note whether any attempts to repeat the experiment failed OR state that all attempts to repeat the experiment were successful.

### Randomization
Describe how samples/organisms/participants were allocated into groups. If allocation was not random, describe how covariates were controlled. If this is not relevant to your study, explain why.

### Blinding
Describe the extent of blinding used during data acquisition and analysis. If blinding was not possible, describe why OR explain why blinding was not relevant to your study.

### Field work, collection and transport

| Field conditions | Describe the study conditions for field work, providing relevant parameters (e.g. temperature, rainfall). |
|------------------|--------------------------------------------------------------------------------------------------|
| Location         | State the location of the sampling or experiment, providing relevant parameters (e.g. latitude and longitude, elevation, water depth). |
| Access and import/export | Describe the efforts you have made to access habitats and to collect and import/export your samples in a responsible manner and in compliance with local, national and international laws, noting any permits that were obtained (give the name of the issuing authority, the date of issue, and any identifying information). |
| Disturbance      | Describe any disturbance caused by the study and how it was minimized. |

### Reporting for specific materials, systems and methods

| Materials & experimental systems | Methods |
|---------------------------------|---------|
| n/a | Involved in the study | n/a | Involved in the study |
| ☒ | Unique biological materials | ☒ | ChIP-seq |
| ☒ | Antibodies | ☒ | Flow cytometry |
| ☒ | Eukaryotic cell lines | ☒ | MRI-based neuroimaging |
| ☒ | Palaeontology | ☒ | |
| ☒ | Animals and other organisms | ☒ | |
| ☒ | Human research participants | ☒ | |

### Unique biological materials
Policy information about availability of materials

Obtaining unique materials: Describe any restrictions on the availability of unique materials OR confirm that all unique materials used are readily available from the authors or from standard commercial sources (and specify these sources).

### Antibodies

| Antibodies used | Antibodies used in the study; as applicable, provide supplier name, catalog number, clone name, and lot number. |
|-----------------|--------------------------------------------------------------------------------------------------|
| Validation      | Describe the validation of each primary antibody for the species and application, noting any validation statements on the manufacturer’s website, relevant citations, antibody profiles in online databases, or data provided in the manuscript. |
### Eukaryotic cell lines

**Policy information about cell lines**

| Cell line source(s) | State the source of each cell line used. |
|---------------------|----------------------------------------|
| Authentication      | Describe the authentication procedures for each cell line used OR declare that none of the cell lines used were authenticated. |
| Mycoplasma contamination | Confirm that all cell lines tested negative for mycoplasma contamination OR describe the results of the testing for mycoplasma contamination OR declare that the cell lines were not tested for mycoplasma contamination. |
| Commonly misidentified lines (See ICLAC register) | Name any commonly misidentified cell lines used in the study and provide a rationale for their use. |

### Palaeontology

**Specimen provenance**

Provide provenance information for specimens and describe permits that were obtained for the work (including the name of the issuing authority, the date of issue, and any identifying information).

**Specimen deposition**

Indicate where the specimens have been deposited to permit free access by other researchers.

**Dating methods**

If new dates are provided, describe how they were obtained (e.g. collection, storage, sample pretreatment and measurement), where they were obtained (i.e. lab name), the calibration program and the protocol for quality assurance OR state that no new dates are provided.

- Tick this box to confirm that the raw and calibrated dates are available in the paper or in Supplementary Information.

### Animals and other organisms

**Policy information about studies involving animals; ARRIVE guidelines** recommended for reporting animal research

**Laboratory animals**

For laboratory animals, report species, strain, sex and age OR state that the study did not involve laboratory animals.

**Wild animals**

Provide details on animals observed in or captured in the field; report species, sex and age where possible. Describe how animals were caught and transported and what happened to captive animals after the study (if killed, explain why and describe method; if released, say where and when) OR state that the study did not involve wild animals.

**Field-collected samples**

For laboratory work with field-collected samples, describe all relevant parameters such as housing, maintenance, temperature, photoperiod and end-of-experiment protocol OR state that the study did not involve samples collected from the field.

### Human research participants

**Policy information about studies involving human research participants**

**Population characteristics**

see above

**Recruitment**

Participants were recruited via the online system recruitment platform of the University of Zurich. An important condition to participate in the experiment was that participants were familiar with the food products used in our experiments. The products were selected from the two biggest supermarket chains in Switzerland (Migros and Coop). This selection process was essential to test the hypotheses of our experiments.

### ChIP-seq

**Data deposition**

- Confirm that both raw and final processed data have been deposited in a public database such as GEO.
- Confirm that you have deposited or provided access to graph files (e.g. BED files) for the called peaks.

**Data access links**

For “initial submission” or “Revised version” documents, provide reviewer access links. For your “Final submission” document, provide a link to the deposited data.

**Files in database submission**

Provide a list of all files available in the database submission.

**Genome browser session (e.g. UCSC)**

Provide a link to an anonymized genome browser session for “initial submission” and “Revised version” documents only, to enable peer review. Write “no longer applicable” for “Final submission” documents.

**Methodology**

**Replicates**

Describe the experimental replicates, specifying number, type and replicate agreement.
Flow Cytometry

Plots

- Confirm that:
  - The axis labels state the marker and fluorochrome used (e.g. CD4-FITC).
  - The axis scales are clearly visible. Include numbers along axes only for bottom left plot of group (a 'group' is an analysis of identical markers).
  - All plots are contour plots with outliers or pseudocolor plots.
  - A numerical value for number of cells or percentage (with statistics) is provided.

Methodology

Sample preparation

- Describe the sample preparation, detailing the biological source of the cells and any tissue processing steps used.

Instrument

- Identify the instrument used for data collection, specifying make and model number.

Software

- Describe the software used to collect and analyze the flow cytometry data. For custom code that has been deposited into a community repository, provide accession details.

Cell population abundance

- Describe the abundance of the relevant cell populations within post-sort fractions, providing details on the purity of the samples and how it was determined.

Gating strategy

- Describe the gating strategy used for all relevant experiments, specifying the preliminary FSC/SSC gates of the starting cell population, indicating where boundaries between "positive" and "negative" staining cell populations are defined.

☐ Tick this box to confirm that a figure exemplifying the gating strategy is provided in the Supplementary Information.

Magnetic resonance imaging

Experimental design

Design type

- Indicate task or resting state; event-related or block design.

Design specifications

- Specify the number of blocks, trials or experimental units per session and/or subject, and specify the length of each trial or block (if trials are blocked) and interval between trials.

Behavioral performance measures

- State number and/or type of variables recorded (e.g. correct button press, response time) and what statistics were used to establish that the subjects were performing the task as expected (e.g. mean, range, and/or standard deviation across subjects).

Acquisition

Imaging type(s)

- Specify: functional, structural, diffusion, perfusion.

Field strength

- Specify in Tesla

Sequence & imaging parameters

- Specify the pulse sequence type (gradient echo, spin echo, etc.), imaging type (EPI, spiral, etc.), field of view, matrix size, slice thickness, orientation and TE/TR/flip angle.

Area of acquisition

- State whether a whole brain scan was used or define the area of acquisition, describing how the region was determined.

Diffusion MRI

☐ Used

☐ Not used
### Preprocessing

**Preprocessing software**

Provide detail on software version and revision number and on specific parameters (model/functions, brain extraction, segmentation, smoothing kernel size, etc.).

**Normalization**

If data were normalized/standardized, describe the approach(es) specify linear or non-linear and define image types used for transformation OR indicate that data were not normalized and explain rationale for lack of normalization.

**Normalization template**

Describe the template used for normalization/transformation, specifying subject space or group standardized space (e.g. original Talairach, MNI305, ICBM152) OR indicate that the data were not normalized.

**Noise and artifact removal**

Describe your procedure(s) for artifact and structured noise removal, specifying motion parameters, tissue signals and physiological signals (heart rate, respiration).

**Volume censoring**

Define your software and/or method and criteria for volume censoring, and state the extent of such censoring.

### Statistical modeling & inference

**Model type and settings**

Specify type (mass univariate, multivariate, RSA, predictive, etc.) and describe essential details of the model at the first and second levels (e.g. fixed, random or mixed effects; drift or auto-correlation).

**Effect(s) tested**

Define precise effect in terms of the task or stimulus conditions instead of psychological concepts and indicate whether ANOVA or factorial designs were used.

**Specify type of analysis:**

- [ ] Whole brain
- [ ] ROI-based
- [ ] Both

**Statistic type for inference**

Specify voxel-wise or cluster-wise and report all relevant parameters for cluster-wise methods.

(See Eklund et al. 2016)

**Correction**

Describe the type of correction and how it is obtained for multiple comparisons (e.g. FWE, FDR, permutation or Monte Carlo).

### Models & analysis

**n/a Involved in the study**

- [ ] Functional and/or effective connectivity
- [ ] Graph analysis
- [ ] Multivariate modeling or predictive analysis

**Functional and/or effective connectivity**

Report the measures of dependence used and the model details (e.g. Pearson correlation, partial correlation, mutual information).

**Graph analysis**

Report the dependent variable and connectivity measure, specifying weighted graph or binarized graph, subject- or group-level, and the global and/or node summaries used (e.g. clustering coefficient, efficiency, etc.).

**Multivariate modeling and predictive analysis**

Specify independent variables, features extraction and dimension reduction, model, training and evaluation metrics.