Research Article
Pathogens, Social Networks, and the Paradox of Transmission Scaling

Matthew J. Ferrari,1 Sarah E. Perkins,1,2 Laura W. Pomeroy,1,3 and Ottar N. Bjørnstad4

1 Center for Infectious Disease Dynamics, Department of Biology, The Pennsylvania State University, University Park, PA 16802, USA
2 Cardiff School of Biosciences, Cardiff University, Biomedical Sciences Building, Museum Avenue, Room C7.29, Cardiff CF10 3AX, UK
3 Department of Veterinary Preventative Medicine, The Ohio State University, Columbus, OH 43210, USA
4 Center for Infectious Disease Dynamics, Departments of Biology and Entomology, The Pennsylvania State University, University Park, PA 16802, USA

Correspondence should be addressed to Matthew J. Ferrari, mferrari@psu.edu

Received 24 September 2010; Revised 26 December 2010; Accepted 15 January 2011

Academic Editor: Katia Koelle

Copyright © 2011 Matthew J. Ferrari et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Understanding the scaling of transmission is critical to predicting how infectious diseases will affect populations of different sizes and densities. The two classic “mean-field” epidemic models—either assuming density-dependent or frequency-dependent transmission—make predictions that are discordant with patterns seen in either within-population dynamics or across-population comparisons. In this paper, we propose that the source of this inconsistency lies in the greatly simplifying “mean-field” assumption of transmission within a fully-mixed population. Mixing in real populations is more accurately represented by a network of contacts, with interactions and infectious contacts confined to the local social neighborhood. We use network models to show that density-dependent transmission on heterogeneous networks often leads to apparent frequency dependency in the scaling of transmission across populations of different sizes. Network-methodology allows us to reconcile seemingly conflicting patterns of within- and across-population epidemiology.

1. Introduction

Transmission is the driver of host-pathogen interactions and the most important determinant of disease dynamics. The patterns and dynamics of transmission within any given host population depend on how infectious and susceptible hosts interact, both spatially and socially [1]. Ultimately, pathogen transmission at the population level is determined by patterns of mixing at the individual level. Network science has highlighted that the mean and variance in transmission among individuals is key to the dynamics of spread within a given population network [2–5]. Predictions of disease dynamics, however, often require that we make projections from one population to another. Population size (i.e., counts), and possibly density, is a common metric with which to characterize differences among populations. Thus, a central challenge in infectious disease ecology is to understand how the distribution of contacts scales across populations of varying size.

Classically, the complex biology of host mixing has been characterized using select formulations from a small number of candidate mathematical models (e.g., [6–11]). If we consider only the increase in infected individuals (i.e., due to disease transmission), then the rate of increase in the number of infected individuals (I), $dI/dt$, is given by the number of susceptible hosts, $S$, times the force of infection (the per capita rate of infection). The force of infection, in turn, is the product of the rate of contacts among individuals, the probability of a contact being with an infectious host, and the probability of that contact giving rise to an infection. The first and third terms are commonly combined into a transmission term, $\beta$. In the simplest case, the rate of contact among hosts is assumed constant (i.e., independent of both population size and density). In a well-mixed population, the
probability of any given contact being infected is then $I/N$, where $N$ is the population size (i.e., count), and the rate of increase of infected individuals in the population is given by
\[ \frac{dl}{dt} = \beta S \frac{l}{N}. \]

This formulation is commonly referred to as frequency-dependent transmission (note that there has been extensive discussion of the appropriate terminology for these models; here, we defer to the derivations and terminology of Begon et al. [10]). Alternatively, if transmission scales linearly with population density (i.e., $\beta = \theta N/A$, where $A$ is area occupied by the population) then we arrive at the density-dependent transmission model:
\[ \frac{dl}{dt} = \beta SI. \]

Though the derivation of (2) is stated in terms of population density, the dependence on area is commonly suppressed by assuming that area is constant through time [10], and thus population size and density are equivalent measures. Begon et al. [10] caution, however, that this simplification in interpreting the two models leads to challenges in comparing dynamics across different populations that presumably occupy ranges of a different area. The frequency- and density-dependent transmission models are extreme special cases. While a variety of alternative or intermediate models have been proposed on theoretical or empirical grounds (see [9–11]), these remain the dominant archetypes in the literature.

Both models assume homogeneous mixing (“mean field”) with no explicit spatial or social structure. While the mechanism of transmission is not explicitly considered in the derivation of (1) and (2), the choice between these two models is often motivated by the mode of transmission. Vector-borne and sexually transmitted diseases are generally assumed to be transmitted in a frequency-dependent manner because the mean number of contacts is independent of population density (if the number of sexual partners or vector attack rates are constant, e.g., [12]). Directly transmitted diseases, in contrast, are typically expected to spread in a density-dependent manner (because the number of encounters may increase with density and/or population size). Alternatively, the density-dependent transmission model has been equated with homogeneous or uniformly random mixing among individuals in contrast to frequency-dependent transmission, which is taken to reflect some degree of local heterogeneity in the population (i.e., in sexual partners) [13]. Begon et al. [10], however, have argued that heterogeneity of the contact structure is orthogonal to the distinction between density- and frequency-dependent transmission.

For host populations of constant size, occupying ranges of constant area, and pathogens that do not cause mortality, the frequency- and density-dependent formulations are equivalent. One may think of both as having a force-of-infection (= per susceptible rate of infection) equal to $\beta l$, where $\beta' = \beta/N$ for the former and $\beta' = \beta$ for the latter. However, they make very different predictions about dynamics and control—such as targets for vaccination coverage and culling [9, 14]—when the host population size varies as a result of extrinsic forces or disease-induced mortality because of their implicit scaling-laws. In the frequency-dependent model, the realized population-level per capita (per susceptible-and-infected) transmission rate ($\hat{\beta} = dl/Sldt$) declines with increasing population size ($N$). As a consequence, the basic reproductive ratio, $R_0$—which defines the epidemic invasion criterion ($R_0 > 1$) —remains constant across varying population sizes. In contrast, the density-dependent model predicts a constant per capita transmission rate across population density. In this model, $\hat{\beta}$ is independent of population size, so consequently $R_0$ increases with $N$. The difference in the predictions of the two models leads to important and divergent predictions for dynamics: the frequency-dependent model has no threshold density for invasion [15] and predicts that moderately infectious pathogens ($R_0 > 2$) that result in lethal infections should lead to extinction of the host and the pathogen [14, 16] while the density-dependent model predicts a critical host density for pathogen invasion and long-term persistence and coexistence of the host and pathogen [17]. Further, for endemic, immunizing pathogens of hosts with a relatively long lifespan, $L$, the mean age-of-infection is predicted to be approximately $L/R_0$ [17, 18]. Thus, based on these models, we expect that frequency-dependent pathogens should exhibit constant mean age-of-infection and proportion of the population that is susceptible while, with density-dependent pathogens, mean age-of-infection and susceptible proportion decay with host population size.

Though the theoretical predictions of the frequency- and density-dependent transmission models are clearly distinct, the empirical patterns that emerge when transmission rates (or $R_0$) have been estimated in real populations are less clear [11]. When reviewing the literature, we find that the patterns do not align with the classic dichotomy between directly transmitted pathogens and sexually or vector transmitted pathogens (Table 1). The different theoretical predictions with respect to the scaling of dynamics with population size are particularly relevant, as we often observe disease processes at one scale (or location) and make inference about the behavior at another. As such, understanding how transmission scales across populations of different sizes is critical to making valid predictions.

Numerous empirical observations have provided direct measures of $R_0$ and/or $\hat{\beta}$ from collections of host populations that vary in size geographically, or individual populations that vary in size through time (Table 1). For example, two directly transmitted pathogens within the morbilliviridae have had $\hat{\beta}$ estimated for a broad range of population sizes: both measles [19] (Figure 1) and phocine distemper virus [20] found $\hat{\beta}$ to be inversely related to population size, and as a consequence, $R_0$ to be relatively invariant. These scaling patterns are as predicted by the frequency-dependent model, despite these pathogens being directly transmitted (and not “frequency-dependent” STDs or vector-borne pathogens).
for which density dependence is normally expected. Other empirical studies are ambiguous in their model support when scaled across populations (Table 1). For example, $R_0$ was concluded to be invariant across population sizes for Aujeszky’s disease virus in pigs [21], supporting a frequency-dependent model; Begon et al. [22] found equal support for frequency- and density-dependent transmission models in cowpox data in rodents; Smith et al. [19] found support for model that is intermediate to the density-dependent model. Begon et al. [22] argued that support of the density- versus frequency-dependent models based on an analysis of long-term time series from the same system. Bucheli and Shykoff [23] argued that support of the density-versus frequency-dependent model depended on the spacing of the host plants in pollinator-vectored anther smut. Klepac et al. [24] found that while the density-dependent model fitted the observations of the 2002 phocine distemper virus outbreak in the Dutch Wadden Sea better than a frequency-dependent model, the observed dynamics in juvenile and adult seals (which are less social) was better explained by a frequency-dependent model.

Table 1: Empirical examples from the published literature of $R_0$ measured in host populations differing in size, indicating the empirical observations and the likely mean-field scaling model.

| Host-pathogen system          | Empirical observations                                      | Model supported       | Reference |
|-------------------------------|------------------------------------------------------------|-----------------------|-----------|
| Humans-measles                | Found $R_0$ to be relatively invariant across population sizes. | Frequency dependent   | [15]      |
| Humans-pertussis              | Transmission was inverse of population size                 | Frequency dependent   | [58]      |
| Humans-diphtheria             | Transmission was independent of flock sizes                 | Frequency dependent   | [59]      |
| Humans-scarlet fever          | $R_0$ was invariant across different population sizes       | Frequency dependent   | [21]      |
| Harbor seals-phocine distemper virus (PDV) | Density-dependent scaling did not explain differences in transmission between different-sized seal haul-out sites | Frequency dependent   | [20]      |
| Rana mucosa-chytridiomycosis  | Transmission rate increases and saturates with density of infected individuals | Frequency dependent   | [33]      |
| Tasmanian devil—devil facial tumor disease | Maintenance of high prevalence following population decline | Frequency dependent   | [34]      |
| Brushtail possums-leptospira interogens | Density-dependent model fit experimental infection rates | Density dependent     | [60]      |
| Elk-brucellosis               | Population density was associated with an increase in seroprevalence but could not differentiate among linear and nonlinear effects of host density. | Nonlinear density dependent | [61]      |
| Rodents-cowpox                | Both models fit to incidence time series; support for both equivocal. | Frequency and density dependent | [22]      |
| Rodents-cowpox                | Transmission term lies between density- and frequency-dependent and varies seasonally. | Model is intermediate  | [11]      |
| Indian meal moth-granulosis virus | A decline in transmission with increasing density of infectious cadavers | Neither               | [26]      |
| Possum-tuberculosis           | Transmission did not fit frequency- or density-dependent models | Neither               | [62]      |
| Tiger salamander-Abystomatigrinum virus | Transmission was best modeled by a power or negative binomial function, that is, nonlinear density dependence. | Neither               | [63]      |
| Badgers-Mycobacterium bovis   | Negative relationship between host abundance and infection prevalence | Neither               | [64]      |
an extinction risk. Rachowicz and Briggs [17] predict that moderately lethal pathogens can lead to extinction of the host. Under the density-dependent model, the reduction of the susceptible population below a threshold level drives the effective transmission rate below 1 and leads to extinction of the pathogen only. The successful application of this principle, for example, rabies [35], smallpox [36], and foot-and-mouth disease [37] is consistent with density-dependent transmission.

Measles and phocine distemper, which have been well-studied both within and across populations, are exemplary of the paradoxical predictions of the mixing models. Both exhibit scaling of transmission rates across populations that is consistent with frequency dependence but local dynamics that are consistent with density dependence [19]. We believe that this paradox arises from the application of the same mean-field transmission model to describe both the within-population transmission and the implicit scaling between populations. We need to revisit the assumption of random host mixing in the face of the strong social and spatial structuring that may limit the interactions between individuals [1]. The dynamics of within-population transmission depend on both the mode of transmission and the structure of transmission network [2-4]; however, the scaling of transmission across populations hinges on the social and spatial structuring of the host population, somewhat independent of the mode of transmission. Note that this point was already raised by De Jong et al. [15]. In the next section, we use network models to show that the equivocal support of the classical models can be resolved by explicit considerations of the contact networks of social and spatial contact patterns.

2. Epidemics and Social Networks

Network models have become very popular methods to relax the assumption of complete mixing among individuals (see [5] for a general review). In most natural populations and particularly those with strong social or spatial structure, individuals interact with only a small proportion of the population. We first introduce the network formalism to capturing social organization, and then we discuss the emergent scaling of pathogen transmission on three classes of social networks.

Epidemic network models differ from the mean-field models in that individuals only interact within their local social neighborhood. We can use these models to investigate the scaling of the realized per capita transmission rate, \( \hat{\beta} \), with host population size in relation to both the mean neighborhood size (\( \langle k \rangle \) = mean degree) and the heterogeneity of contacts. Cellular automata models have similarly been used to study the distinction between local transmission and global dynamics (e.g., [38-41]). However, the nature of cellular automata models limit the range of social structures that can be studied to those that can be reasonably collapsed to 2 dimensions (i.e., a lattice). Contact network models

\[ \text{Figure 1: Scaling of measles transmission. The estimated mean transmission rate (}\beta)\text{ of measles in England and Wales plotted against increasing city size in thousands. Reproduced from [19].} \]
allow the flexibility to study a wide range of social structures with a complex mix of both local and global interactions [42].

Various characteristics of contact network topology (i.e., clustering, assortativity, etc.) may vary with population size. However, there are few empirical studies of the scaling of network properties on social networks of various sizes. Here, we focus simply on the scaling of the mean number of contacts with network size, both because of its straight forward interpretation and its parallels with the classic formulations of the density- and frequency-dependent mean-field models. The classic mean-field models make explicit assumptions about the way the mean rate of contacts scales with population density, but are restricted by implicit assumptions of how the variance in contacts scales with density. Contact network models make explicit the relationship between the mean and variance of contacts in the choice of the degree distribution. Further, contact network models relax the assumption that population density or size is a proxy for the contact rate, which is implicit in the mean-field models.

Host social organizations that have constraints on group size (e.g., classroom size for school children, harem size for some social mammals) may be adequately represented by a Poisson distribution of social contacts (i.e., a variance to mean ratio near 1, Figure 2(a)) [2]. In contrast, many animal species exhibit skewed social contact networks with few individuals having many contacts, and the majority having few contacts (i.e., a variance to mean ratio \( \gg 1 \), Figure 2(b)) [43, 44]. Following established theory, these social interactions are commonly characterized by truncated power laws [45, 46].

We generated networks of size \( N = 100, 500, 1000, 2000, 5000, \) and 10000 nodes (individuals) for which the mean number of contacts scaled in one of 3 ways: (1) the mean number of contacts was independent of population size \( \langle k \rangle = 6 \), (2) the mean number of contacts increased slower than linearly with population size \( \langle k \rangle = 0.06 \sqrt{N} \), and (3) the mean number of contacts increased linearly with population size \( \langle k \rangle = 0.06 \times N \). Note that all networks have the same mean when \( N = 100 \). The constant and linear scaling functions are analogous to the assumptions of the classic frequency- and density-dependent transmission functions in the mean-field models when area is held constant. The intermediate function represents an intermediate setting where, for example, the number of contacts increases initially with population size (e.g., larger cities lead to larger workplaces), but the total number of contacts is limited by time or typical home range. In these models, we base the scaling of contacts on the population size rather than density. While in many settings it may be reasonable to assume that the probability of a contact depends on spatial proximity [47], the complexity of empirical contact networks has highlighted that space is not always a reasonable proxy for social proximity [48].

We considered the effect of local heterogeneity of contacts by generating networks with Poisson, exponential, and truncated power law contact distributions. The Poisson contact distribution reflects a setting with relatively low variance in the number of contacts and thus approximates the homogeneous contact structure of the mean-field models [10]. The power law contact distributions reflect extreme heterogeneity in local contacts that is seen in many empirical contact networks. The exponential contact distribution represents an intermediate case. Networks were generated using the algorithm described by Molloy and Reed [49]. We approximated a power law degree distribution using a negative binomial distribution with dispersion parameter, \( \theta = 0.1 \). The presence of highly connected individuals, so-called "super spreaders" [43], has been consistently shown to have large impacts on the threshold conditions and final size of outbreaks [4, 50]. Thus, under the assumption of constant mean contacts for networks of increasing size, we might expect emergent scaling of dynamics for the three degree distributions as larger networks will better sample the degree distribution, which would mean a greater proportion of rare “super spreaders” in the exponential and power law distributed networks.

For all three families of edge distributions, nodes were connected at random with the restriction that self-loops (nodes connected to themselves) and double edges between nodes were disallowed. Thus, individuals cannot infect themselves and cannot infect another in the population more than once.

We simulated epidemics on the contact networks according to a discrete time, stochastic susceptible-infected-removed ("chain-binomial") [51] model. Susceptible hosts become infected in each time step with probability \( p_j = 1 - \exp(-\beta T_j) \), where \( T_j \) is the number of infected individuals within the local neighborhood of individual \( j \) at a given time point. Thus, infection depends on the local density of infected hosts, where density is relative to the social neighborhood rather than a fixed neighborhood in Euclidean space (i.e., transmission is locally density dependent). Infected individuals were removed from the population in each time step with probability \( 1 - \exp(-\gamma) \), thus leading to a geometrically distributed infectious period—the discrete
time equivalent of the standard SIR assumptions. Removed individuals were assumed to be permanently immune and thus unable to be subsequently infected; in practice, these nodes in the network are “turned off”, so while the total number of nodes remains constant, the effective number of nodes in the epidemiologically active portion of the network declines (i.e., thus, for this model equivalent to disease-induced mortality). In an important contrast to the mean-field models, the removal of infected nodes results in reduced contacts for their remaining neighbors. Thus, for structured contact networks (as has been well explored for cellular automata models [38, 39]), the local and global impact of the removal of infected individuals can be quite different. However, in contrast to nonnetwork models (e.g., cellular automata and small-world models for which only local connections are explicit), variance in the distribution of contacts leads to a structured cascade of infection from highly connected individuals to less well-connected individuals, which results in a decline in the per capita realized transmission. This effect is equivalent to the frailty effect discussed in mathematical demography [19]. The rate and magnitude of this decline depends explicitly on the distribution of the underlying transmission network [52].

For each configuration, we generated 30 networks and simulated epidemics seeded by a single infection. In each time step, the probability of transmission across an edge was assumed to be 0.1, and the probability that an infected node recovered was 0.1. We calculated, for each configuration and each time step, the realized per capita (per infected) transmission rate, \( \hat{\beta}t \):

\[
\hat{\beta}t = I_t - I_{t-1} \frac{S_t}{I_t},
\]

where \( I_t \) and \( S_t \) are the total number of infectious and susceptible nodes on the network at time \( t \). The selective removal of highly connected nodes early in the epidemic results in a decrease in the realized transmission rate as the epidemic progresses [52]. To generate time-weighted realized per capita rates, we, therefore, calculated \( \hat{\beta} \) as the intercept of the regression of \( \hat{\beta}t \) on time. Thus, we are describing the scaling of the rate of transmission at the initiation of an epidemic. Calculations using the time-course average yields similar scaling results and are, therefore, not included (Ferrari et al., unpublished results).

We find that the realized \textit{per capita} transmission rate \((\hat{\beta})\) decreased with population size despite local transmission being modeled as a density-dependent process (Figures 3(a), 3(c), and 3(e)). Only when the mean number of contacts is assumed to increase linearly with population size is \textit{per capita} rate \((\hat{\beta})\) constant across networks (Figures 3(a), 3(c), and 3(e)). Social group sizes that increase slower-than-linearly with community size yield intermediate results; \( \hat{\beta} \) decays but slower than \( 1/N \). In all cases, the local scale transmission remains constant across network sizes; that is, the number of new infections per susceptible-infected pair remains constant regardless of network size or configuration (Figures 3(b), 3(d), and 3(f)). Surprisingly, these scaling relationships are remarkably constant across the three classes of networks despite the difference in the variance in local contacts. For a given network size and mean number of contacts, the per capita transmission rate was lowest for the Poisson networks and greatest for the scale-free networks, in agreement with the standard observation that transmission is positively correlated with variance in the contact distribution. The critical finding from our analysis is that we need to distinguish between the \textit{mode} of transmission within-populations (frequency versus density dependent) and the \textit{scaling} of transmission between populations.

3. Discussion

Classically, the choice of model to describe disease dynamics was based on the transmission route of the pathogen, with little regard to empirical patterns. Even though this method may accurately describe local transmission between individual hosts, as evidenced by the wealth of empirical examples and the success of the resultant theory in disease management, it is not evident that these models will scale correctly to describe transmission across socially or spatially distinct populations (see examples in Table 1). In the above example, we have shown that the scaling pattern of pathogen transmission among distinct populations can be determined by the structure and scaling of the local host contact network and that the scaling pattern is independent of the mode of transmission. The scaling relationship depends explicitly on the heterogeneity in contacts and how the average connectivity changes with population size. In general, the scaling of transmission is likely to depend on the particular nature of host mixing and contact network structure—pathogen transmission biology may not play a large role.

In all the models, the heterogeneity in the contact structure leads to a structured cascade of infection from highly connected individuals to less connected individuals [52], which results in a decline in the realized per capita transmission rate that is consistent with the predictions of the mean-field density-dependent model. (Note that the constant, or increasing, per capita transmission rate that is predicted by the mean-field, frequency-dependent model requires that new contacts be formed among individuals remaining in network model to overcome this frailty effect.) However, we only observed density-dependent scaling with population size in network models when the mean number of contacts is proportional to population size. This phenomenon is rarely observed in the literature (Table 1), possibly due to natural constraints on the number of contacts as populations grow, due to limited time or space. Presumably, for some very well-mixed systems such as phases in bacterial emulsions, density-dependent scaling with population size may be possible. Despite locally density-dependent transmission, the network models predict \( \hat{\beta} \) to scale in a pattern consistent with the frequency-dependent mean-field model when the mean number of social contacts is independent of population size or increases at a decelerating rate. We would expect this scaling pattern when social forces place constraints on the number of contacts independently of population size; for
example, measles, for which school classroom sizes tend to be reasonably constrained [19], and phocine distemper virus in harbor seals, for which spatial constraints limit the number of seals on haulouts [18].

We further found that the scaling relationship was independent of the variance in the edge distribution of the contact network. Thus, the choice of the mean-field, density-dependent model to represent populations with
homogeneous mixing [13], is not justified and would impose a scaling relationship that is only consistent with the extreme case where the mean number of contacts scale linearly with population size. As such, this observation corroborates the heuristic argument of Begon et al. [10] that the degree of local heterogeneity in the contact structure is “orthogonal to the distinction between density- and frequency-dependent contact rates and transmission.”

The network models we present here are necessarily simplistic in that they presume that epidemic dynamics are fast relative to ecological dynamics, so we can ignore births, nondisease mortality, and the formation of new connections following node removal (i.e., in the event that node removal is interpreted as mortality rather than lasting immunity). In principle, these should not impact our general observations providing that births and deaths are not biased with respect to the connectivity of nodes, an assumption implicit in the mean-field models. In practice, however, it is likely that births and deaths are biased with respect to network characteristics (e.g., [53]) or that connections are dynamic (connections accrue or change as nodes age [54]). Understanding these mechanisms that generate contact processes is an important ecological challenge and the efficient algorithms to incorporate these dynamics into model representations remain an important technical challenge.

The density- and frequency-dependent, mean-field models make explicit assumptions about how the mean contact rate should scale with population density (or size if area is held constant as is the common assumption). As Begon et al. [10] point out, the direct application of these models across populations presents a challenge, as it requires the presumption that either area is comparable among populations of different size, or that the relationship between density and contact rate is consistent across populations. A variety of more flexible mean-field models have been proposed that allow for more intermediate, nonlinear relationships between density and contact rate [11]. However, while these intermediate relationships may provide better fit to observed dynamics, they are difficult to interpret in terms of explicit mechanisms, as there may be a range of candidate explanations for the nonlinear relationship between density and contacts [11].

Contact network models, while occasionally limiting in their complexity, present a useful tool for understanding the role of the social contact structure in generating observed dynamics. The focus on explicit characteristics of the contact structure provides a mechanistic explanation for the resulting dynamics compared with the phenomenological representations of contact rate assumed in the mean-field models. Here, we have shown the flexibility of these models to retain commonly observed within-population dynamics (i.e., the decline in realized transmission due to contact frailty) and a range of scaling patterns across population sizes as a function of the relationship between the contact distribution and the network size. We have presented only relatively simple examples where the mean and variance of the contact distribution scale with network size. However, it is reasonable to presume that a variety of additional, higher-order characteristics of contact networks (i.e., clustering, assortativity) may also scale with population size or density. The challenges of projecting even simple mean-field models across populations highlights the need for a greater understanding of how the characteristics of contact network correlate with more directly measureable metrics such as population size and density in order to make the lessons from contact network epidemiology predictive.

In conclusion, we must understand the local mixing dynamics of the host population rather than assume an implicit mixing structure defined by the pathogen in order to make predictions about epidemic dynamics across scales. Both experimental and theoretical work is needed to resolve the uncertainty about the scaling of transmission with population size and density. Experimentally, proper model systems will permit exploration of the effects of population size and density on mixing behavior and epidemic dynamics. Critically, this may depend strongly on behavioral responses to population size or density at the scale of individuals (e.g., [28]) that give rise to important deviations from the simple scaling models. Theoretically, method development and application will allow the study of contact network properties from field-sampled data on real populations. Network models in physics and epidemiology have provided great insights into the effect of heterogeneities and network topology on epidemic dynamics; however, connecting these insights to dynamics in real systems is challenging because of the need for fully censused populations to recreate contact networks and the assumption that network topology is static (though see [55]). The development of statistical methods to conduct inference on social network models [56] may prove useful to understand network assembly rules and for generating candidate networks for investigation of epidemic dynamics through simulation; in particular, how models of host movement and interaction among individuals give rise to scaling rules—be they network properties or mean-field approximations—for population mixing [57]. Overall, increasing the comprehension of host contact and mixing dynamics—through experimental and theoretical methods—will permit a more complete understanding of epidemic dynamics.

References

[1] S. Altizer, C. L. Nunn, P. H. Thrall et al., “Social organization and parasite risk in mammals: integrating theory and empirical studies,” Annual Review of Ecology, Evolution, and Systematics, vol. 34, pp. 517–547, 2003.

[2] L. A. Meyers, B. Pourbohloul, M. E. J. Newman, D. M. Skowronski, and R. C. Brunham, “Network theory and SARS: predicting outbreak diversity,” Journal of Theoretical Biology, vol. 232, no. 1, pp. 71–81, 2005.

[3] M. E. J. Newman, “Spread of epidemic disease on networks,” Physical Review E, vol. 66, no. 1, Article ID 016128, 11 pages, 2002.

[4] R. Pastor-Satorras and A. Vespignani, “Epidemic spreading in scale-free networks,” Physical Review Letters, vol. 86, no. 14, pp. 3200–3203, 2001.

[5] S. Bansal, B. T. Grenfell, and L. A. Meyers, “When individual behaviour matters: homogeneous and network models in
epidemiology,” *Journal of the Royal Society Interface*, vol. 4, no. 16, pp. 879–891, 2007.

[6] R. M. Anderson and R. M. May, “Regulation and stability of host-parasite population interactions I. Regulatory processes,” *Journal of Animal Ecology*, vol. 47, pp. 219–247, 1978.

[7] M. C. M. de Jong, “Mathematical modelling in veterinary epidemiology: why model building is important,” *Preventive Veterinary Medicine*, vol. 25, no. 2, pp. 183–193, 1995.

[8] G. Dwyer, J. S. Elkington, and J. P. Buonaccorsi, “Host heterogeneity in susceptibility and disease dynamics: tests of a mathematical model,” *American Naturalist*, vol. 150, no. 6, pp. 685–707, 1997.

[9] H. McCallum, N. Barlow, and J. Hone, “How should pathogen transmission be modelled?” *Trends in Ecology and Evolution*, vol. 16, no. 6, pp. 295–300, 2001.

[10] M. Begon, M. Bennett, R. G. Bowers, N. P. French, S. M. Hazel, and J. Turner, “A clarification of transmission terms in host-microparasite models: numbers, densities and areas,” *Epidemiology and Infection*, vol. 129, no. 1, pp. 147–153, 2002.

[11] M. J. Smith, S. Telfer, E. R. Kallio et al., “Host-pathogen time series data in wildlife support a transmission function between density and frequency dependence,” *Proceedings of the National Academy of Sciences of the United States of America*, vol. 106, no. 19, pp. 7905–7909, 2009.

[12] P. H. Thrall, J. Antonovics, and D. W. Hall, “Host and pathogen coexistence in sexually transmitted and vector-borne diseases characterized by frequency-dependent disease transmission,” *American Naturalist*, vol. 142, no. 3, pp. 543–552, 1993.

[13] A. B. Lockhart, P. H. Thrall, and J. Antonovics, “Sexually transmitted diseases in animals: ecological and evolutionary implications,” *Biological Reviews of the Cambridge Philosophical Society*, vol. 71, no. 3, pp. 415–471, 1996.

[14] F. De Castro and B. Bolker, “Mechanisms of disease-induced extinction,” *Ecology Letters*, vol. 8, no. 1, pp. 117–126, 2005.

[15] M. C. M. De Jong, O. Diekmann, and H. Heesterbeek, “How does transmission of infection depend on population size?” in *Epidemic Models: Their Structure and Relation to Data*, D. Mollison, Ed., pp. 84–94, Cambridge University Press, Cambridge, UK, 1995.

[16] W. M. Getz and J. Pickering, “Epidemic models: thresholds and population regulation,” *The American Naturalist*, vol. 121, pp. 892–898, 1983.

[17] R. M. Anderson and R. M. May, *Infectious Diseases of Humans: Dynamics and Control*, Oxford University Press, Oxford, UK, 1991.

[18] J. Swinton, J. Harwood, B. T. Grenfell, and C. A. Gilligan, “Persistence thresholds for phocine distemper virus infection in harbour seal Phoca vitulina metapopulations,” *Journal of Animal Ecology*, vol. 67, no. 1, pp. 54–68, 1998.

[19] O. N. Bjørnstad, B. F. Finkenstädt, and B. T. Grenfell, “Dynamics of measles epidemics: estimating scaling of transmission rates using a Time series SIR model,” *Ecological Monographs*, vol. 72, no. 2, pp. 169–184, 2002.

[20] J. Swinton, J. Harwood, and A. Hall, “Scaling of phocine distemper virus transmission with harbor seal community size,” *Ecology*, vol. 30, pp. 231–240, 1999.

[21] A. Bouma, M. C. M. de Jong, and T. G. Kimman, “Transmission of pseudorabies virus within pig populations is independent of the size of the population,” *Preventive Veterinary Medicine*, vol. 23, no. 3–4, pp. 163–172, 1995.

[22] M. Begon, S. M. Feore, K. Bown, J. Chantrey, T. Jones, and M. Bennett, “Population and transmission dynamics of cowpox in bank voles: testing fundamental assumptions,” *Ecology Letters*, vol. 1, no. 2, pp. 82–86, 1998.

[23] E. Bucheli and J. A. Shykoff, “The influence of plant spacing on density-dependent versus frequency-dependent spore transmission of the anther smut Microbotryum violaceum,” *Oecologia*, vol. 119, no. 1, pp. 55–62, 1999.

[24] P. Klepac, L. W. Pomeroy, O. N. Bjørnstad, T. Kuiken, A. D. M. E. Osterhaus, and J. M. Rijks, “Stage-structured transmission of phocine distemper virus in the Dutch 2002 outbreak,” *Proceedings of the Royal Society B*, vol. 276, no. 1666, pp. 2469–2476, 2009.

[25] C. J. Ryder, K. M. Webberley, M. Boots, and R. J. Knell, “Measuring the transmission dynamics of a sexually transmitted disease,” *Proceedings of the National Academy of Sciences of the United States of America*, vol. 102, no. 42, pp. 15140–15143, 2005.

[26] J. A. Shykoff, “The influence of plant spacing on density-dependent versus frequency-dependent spore transmission of the anther smut Microbotryum violaceum,” *Oecologia*, vol. 119, no. 1, pp. 55–62, 1999.

[27] P. Klepac, L. W. Pomeroy, O. N. Bjørnstad, T. Kuiken, A. D. M. E. Osterhaus, and J. M. Rijks, “Stage-structured transmission of phocine distemper virus in the Dutch 2002 outbreak,” *Proceedings of the Royal Society B*, vol. 276, no. 1666, pp. 2469–2476, 2009.

[28] M. J. Smith, S. Telfer, E. R. Kallio et al., “Host-pathogen time series data in wildlife support a transmission function between density and frequency dependence,” *Proceedings of the National Academy of Sciences of the United States of America*, vol. 106, no. 19, pp. 7905–7909, 2009.

[29] P. H. Thrall, J. Antonovics, and D. W. Hall, “Host and pathogen coexistence in sexually transmitted and vector-borne diseases characterized by frequency-dependent disease transmission,” *American Naturalist*, vol. 142, no. 3, pp. 543–552, 1993.

[30] A. B. Lockhart, P. H. Thrall, and J. Antonovics, “Sexually transmitted diseases in animals: ecological and evolutionary implications,” *Biological Reviews of the Cambridge Philosophical Society*, vol. 71, no. 3, pp. 415–471, 1996.

[31] F. De Castro and B. Bolker, “Mechanisms of disease-induced extinction,” *Ecology Letters*, vol. 8, no. 1, pp. 117–126, 2005.

[32] M. C. M. De Jong, O. Diekmann, and H. Heesterbeek, “How does transmission of infection depend on population size?” in *Epidemic Models: Their Structure and Relation to Data*, D. Mollison, Ed., pp. 84–94, Cambridge University Press, Cambridge, UK, 1995.

[33] W. M. Getz and J. Pickering, “Epidemic models: thresholds and population regulation,” *The American Naturalist*, vol. 121, pp. 892–898, 1983.

[34] R. M. Anderson and R. M. May, *Infectious Diseases of Humans: Dynamics and Control*, Oxford University Press, Oxford, UK, 1991.

[35] J. Swinton, J. Harwood, B. T. Grenfell, and C. A. Gilligan, “Persistence thresholds for phocine distemper virus infection in harbour seal Phoca vitulina metapopulations,” *Journal of Animal Ecology*, vol. 67, no. 1, pp. 54–68, 1998.

[36] O. N. Bjørnstad, B. F. Finkenstädt, and B. T. Grenfell, “Dynamics of measles epidemics: estimating scaling of transmission rates using a Time series SIR model,” *Ecological Monographs*, vol. 72, no. 2, pp. 169–184, 2002.

[37] J. Swinton, J. Harwood, and A. Hall, “Scaling of phocine distemper virus transmission with harbor seal community size,” *Ecologie*, vol. 30, pp. 231–240, 1999.

[38] A. Bouma, M. C. M. de Jong, and T. G. Kimman, “Transmission of pseudorabies virus within pig populations is independent of the size of the population,” *Preventive Veterinary Medicine*, vol. 23, no. 3–4, pp. 163–172, 1995.

[39] M. Begon, S. M. Feore, K. Bown, J. Chantrey, T. Jones, and M. Bennett, “Population and transmission dynamics of cowpox in bank voles: testing fundamental assumptions,” *Ecology Letters*, vol. 1, no. 2, pp. 82–86, 1998.
