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An Analysis on Hydraulic Loss in a Co-Rotating Bladed Disc Pump

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Abstract: Disc pumps rely on the shear force generated by a co-rotating disc to transport the fluid, the interaction between the fluid and impeller is weak, providing such pumps advantages when handling multi-phase flow. In the present study, a loss analysis is presented on a different kind of disc pump that combines both shear and pressure forces using a co-rotating disc pump and radial blades and that is often applied in marine petroleum engineering for mud-lifting. Experimental measurements on the overall pump performance were performed, and the subsequent hydraulic efficiency analysis shows that similarity laws can be applied for this pump. A particular analysis was specifically performed on the impeller and shows that the resulting loss analysis indicates that the increase in the static pressure is small and that the total pressure increase is mainly contributed to by the dynamic pressure change from the inlet to the outlet impeller sections. In addition, an evaluation of the individual loss levels is proposed in the impeller that is based on one-dimensional assumptions. This type of evaluation has never been proposed for present specific TBD pump designs in the available literature. The obtained results showed that the most important loss levels are roughly equally distributed between the incidence effects, inter-blade leakage, and bolts losses in the impeller, and that all together, they can reach 80% of the total impeller losses, while the blade-loading and friction losses are relatively small. The losses downstream of the impeller are significant, thus, a specific volute design that has been adapted for a disc impeller outlet flow pattern must be considered in order to achieve better performance. The present loss analysis was able to predict the corresponding disc pump performance well, achieving a maximum error rate of ±5% for a rather wide flow coefficient range. The proposed method can be considered to be a useful approach for research or for industrial teams who are working on the same kind of geometry by adopting the same data reduction analysis, allowing them to compare their own results with the present ones.

Keywords: disc pump; performance analysis; experiments; computational fluid dynamics; loss distribution

1. Introduction

With the increasing demand for oil resources, the importance of marine oil drilling technology is becoming more and more prominent due to the huge reserves in the world’s oceans. In deep-sea drilling engineering, a pump system is needed for subsea mud-lifting. However, the composition of subsea mud is complex and is typically a multi-phase fluid that contains large amounts of solid particles and gases. Therefore, conventional centrifugal pumps are limited for subsea mud-lifting due to the strong wear effect, which leads to rapid blade destruction, and the choice of axial flow pumps is also inadequate because...
of the relatively low lift head. Under these circumstances, a special pump design, known as a co-rotating disc pump, is often used for subsea mud-lifting systems [1–5]. Its specific design is derived from the shear pump that was first patented by Nicola Tesla [6], which was only composed of a set of smooth compact discs without blades, as shown in Figure 1.

Figure 1. Tesla disc pump impeller.

Nicola Tesla’s design was later improved by Max [7–9], who enlarged the spacing between the discs and by adding blades on the surface of each disc (also called a Tesla-bladed disc pump, or TBD pump in the present paper). An example is given in Figure 2 [10].

Figure 2. Disc pump model [10].

A distinction must be made between these two types of disc pumps.

- The initial Tesla disc pump only utilizes the viscous force, the internal flow field, and performance analyses presented by Hasinger and Kehrt [11]. Murata et al. [12,13] and Roddy et al. [14] showed that its performance is generally worse than that of a common centrifugal pump, but that the internal flow field is more stable and the streamline between discs almost axisymmetric. Wang et al. [15] analyzed the loss mechanism in the Tesla disc pump and found that the main losses occur downstream of the impeller. Cheremushkin and Polyakov [16] optimized the volute of a Tesla disc pump model, and the optimized model achieved better efficiency compared to the original model.

- In contrast, the TBD pump not only utilizes not the viscous force but also the blade-like structure; moreover, the spacing between discs is much wider, similar to a common centrifugal pump. The pure radial blade shape can be considered to be quite crude in terms of design, especially for something used in impeller inlet conditions, compared to other designs, but this choice has been made to make disc pump more robust according to the transported mixture to be worked with. Therefore, the internal flow field and operating mechanism of the TBD pump are much more complex. The research team at the China University of Petroleum (East China) presented several studies related to TBD pumps that were applied in marine petroleum engineering and used as the mud-lifting pump, and these studies mainly focused on the influence of the geometrical parameters on pump performance [17–19], and the presented studies also showed evidence of the anti-wearability of TBD pumps by finding
that the solid particles mainly concentrated in the bladeless area, which greatly reduced the interaction between the impeller and the solid particles [19–22]. Pei et al. [23] presented an approach to estimate the velocity slip at the impeller outlet, which could be helpful for disc pump performance predictions, but only in situations that are close to design conditions. These studies provided interesting contributions for understanding the overall characteristics of TBD pumps. However, all of the published works that have been found in the available literature on TBD pumps only present overall performances and, more precisely, global efficiency, no information on the hydraulic efficiency of such pumps can be found, and there is also a research gap in terms of the evaluation of the loss distribution in each component of such a specific pump design.

In preliminary studies, authors (Heng et al. [10,24]) have analyzed the performance characteristics of present TBD pumps based on experimental results for several rotational speeds and checked the validity of similarity laws for such unconventional designs. Nevertheless, the objective of the present paper is to first carry out an evaluation of the individual loss sources in different parts of this type of pump before starting future multi-phase flow studies. The present study is therefore divided into two parts: the first part concerns a global performance analysis based on comparisons between the experimental and numerical results determined for the present pump, which were derived from the Discflo™ example from Figure 2, but with a smaller disc spacing. This part is presented in Section 3. The overall CFD results that were obtained on the TBD pump were also used to determine impeller performance.

Hydraulic losses are then analyzed, and an evaluation of their distribution along the different pump components is proposed based on a one-dimensional approach using semi-empirical correlation analytical models. This approach has been widely used and applied for conventional centrifugal pump designs but has never been performed for this specific pump design and is presented in Section 4.

Such an approach was derived from the axial component of the moment of momentum equation applied in a control volume that included the throughflow area between the inlet and outlet sections of the impeller passage. This leads to an evaluation of the theoretical head through the well-known Euler relation based on the one-dimensional assumption that is the basis for the development of the present paper.

2. Presentation of the Present TBD Pump Geometry

The present TBD pump impeller, shown in Figure 3, is directly inserted into an existing industrial volute (Figure 4) pump and replaces a conventional centrifugal impeller that has been previously removed. This set-up was chosen to perform further multi-phase flow tests in the future for ground or sub-see applications. The main geometrical characteristics of the present pump impeller are shown in Figure 5 and Table 1.

![Figure 3. Present TBD pump impeller.](image-url)
Figure 4. Volute assembly.

Figure 5. Driven and dive disc assembly.

Table 1. Main geometrical parameters of present TBD pump.

| Geometric Parameters            | Values  |
|---------------------------------|---------|
| Inlet shroud tip radius $R_{1}$ | 60 mm   |
| Inlet tube radius $R_{1}$       | 50 mm   |
| Outlet radius $R_{2}$           | 100 mm  |
| Number of blades $Z_{B}$        | 8       |
| Number of bolts                 | 8       |
| Bolt diameter                   | 12 mm   |
| Radial bolt location            | 75 mm   |
| Inter blade clearance gap $c_l$ | 8 mm    |
| Blade height $h$                | 4 mm    |
| Blade angle $\beta'$           | 90° (radial blade) |
| Impeller channel width $b$      | 16 mm   |
| Specific speed $\Omega_s$       | 0.8     |
| Specific radius $\Lambda$       | 2.4     |

The driven disc on the shroud side of the impeller is connected to the drive hub disc and is equipped with eight bolts that allow both discs to rotate at the same angular velocity (see Figure 5). The ratio between the two-blade height and the impeller width is kept at 0.5, corresponding to most existing industrial pumps of this type. However, the ratio between the impeller width and the outlet radius is lower compared to other designs.

3. Overall Pump Performances

3.1. Experimental Test Bench and Instruments

A pump test system was built to test pump performance, and the tested fluid media was water. An open 3 m³ volume tank was connected to the inlet and outlet pipes to provide recyclable working fluid. A DZW BT16C-type electrical valve was applied to control
the flow rate of the system, and a YH-LDG-type electromagnetic flowmeter was then used for the real-time monitoring of the volume flow rate, achieving precision of ±0.5% (range: 0–150 m³/h). The TBD pump head $H$ was obtained by the two PTX 5072-type pressure transducers installed on the inlet and outlet pipes, achieving precision of ±0.2% (range: 0–50 m). A torqueometer device was placed between the motor and TBD pump shaft to measure the rotational speed and torque, achieving precision of ±0.1% (range: 0–3000 rpm) and ±0.2% (range: 0–250 N·m), respectively. The test bench can be seen in Figure 6.

![Experimental pump test bench.](image)

**Figure 6.** Experimental pump test bench.

### 3.2. Experimental Results

The performance charts of the present TBD pump are given in Figure 7 along with the evolutions of the pump total head $H$ and global efficiency $\eta_g$ versus the volume flow rate $Q$ for the two rotational speeds 1500 and 2900 rpm.

![Experimental pump total head and global efficiency versus flow rate.](image)

**Figure 7.** Experimental pump total head and global efficiency versus flow rate.

For the measurement uncertainties under the flow rate 100 m³/h and for 2900 rpm, the measurement uncertainties $U_c$ are determined by:

$$U_c = \pm \frac{2.19 \times S}{x \sqrt{n}} \times 100\%$$  \hspace{1cm} (1)

where $S$ is the standard deviation, $x$ is the averaged value of the measured data, and $n$ is the number of times the measurement is repeated ($n = 10$), and they are obtained by following formula:
Based on the measured data, the measurement uncertainty for the flow rate is ±2.5%, for the pump head, it is ±3%, and for the pump efficiency, it is ±4%. These values are also applicable for the hydraulic efficiency, flow coefficient, and head coefficient in relation to Equations (4)–(6).

In Figure 8, these experimental results are presented using the head and flow coefficients defined as follows:

\[ \psi_{t,t,p} = \frac{gH}{\left(U_2\right)^2} \]  

\[ \eta_{hyd,p} = \frac{\rho g Q H}{(\eta_v \eta_m P_s)} \]  

\[ \phi = \frac{Q}{2\pi R b c U_2} \]

where \( \eta_v \) is the volumetric efficiency estimated by taking the leakage flow into account, and \( \eta_m \) is the mechanical efficiency, which is fixed at 0.98 for the present model. The disc friction power, which only depends on the rotational speed, can be estimated according to the following formula (Gülich [25]):

\[ P_{\text{disc}} = k_{\text{disc}} \rho \omega^3 R^2 (1 - (R_1/R_2)^n), \] for one disc.

where \( k_{\text{disc}} \) is the friction coefficient.

**Figure 8.** Experimental total head coefficient and pump hydraulic efficiency versus flow coefficient for 1500 and 2900 rpm.

It was determined that the amount of leakage is small because of the small increase in the static pressure across the impeller, as explained further in Section 4.1. The pump total head coefficient \( \psi_{t,t,p} \) versus the flow coefficients \( \phi \) resulting from two different rotational speeds 1500 and 2900 rpm, respectively, is plotted in Figure 8. Due to the detected cavitation at 2900 rpm, a clear discrepancy can be seen when the flow coefficient \( \phi > 0.08 \). Nevertheless, the rest part of the curve indicates that similarity laws can be applied for this pump for this set of rotational speeds. For the same reason, the hydraulic efficiency \( \eta_{hyd,p} \) versus the flow coefficient is also an invariant, except when cavitation is detected for
high flow rates corresponding to the last three experimental points in Figure 8 obtained for the largest rotational speed value of 2900 rpm. Cavitating flow was roughly detected using the inlet static pressure measurements in front of the pump plus the relative dynamic pressure at the blade impeller inlet section.

Maximum hydraulic pump efficiency $\eta_{\text{hyd,p}}$ occurs for a flow coefficient $\phi_{\text{opt}} \approx 0.068$ and decreases much more gently for higher flow rates compared to lower ones.

Based on the experimental results, the theoretical pump head coefficient $\psi_{\text{th}}$ can be obtained as follows:

$$\psi_{\text{th}} = \psi_{\text{t,t,p}} / \eta_{\text{hyd,p}} \quad (8)$$

The theoretical pump head coefficient is shown in Figure 9 for both rotational speeds. For the maximum flow coefficient, its value is less than 0.7, which is lower than that of a conventional pump design due to bladeless spacing inside the TBD pump impeller. The extrapolated straight line corresponds to the well-known ideal theoretical head coefficient, assuming that there is no inlet swirl and no recirculation.

![Figure 9. Theoretical head coefficient.](image)

For conventional centrifugal pump designs, the value of the head coefficient is equal to 1 for the zero mean flow rate when using the straight-line extrapolation. The corresponding present curve value only reaches 0.8 because the fluid tangential velocity component is always lower than that of conventional full-blade designs and is generally obtained using the slip coefficient evaluation from semi-empirical correlations when a one-dimensional assumption is assumed. Up until now, the corresponding slip factor correlation has not been developed for co-rotating disc pumps. This is the reason why the evaluation of the impeller hydraulic efficiency is the key point for the one-dimensional approach for the loss study conducted in the present paper. It needs both conjugate experimental and numerical data reduction analysis.

### 3.3. Numerical Simulation Set-Up and Results

To determine the local information impeller inlet and outlet flow characteristics that cannot be obtained from local measurement accessibility, Reynolds Average Numerical Simulations (RANS) were performed using a $k-\omega$ SST turbulent model. The 3D fluid domain was created using commercial software UG, as shown in Figure 10. This approach has been widely used thanks to the development of numerical techniques, which have been validated to some extent for specific local studies on cavitation, for example [26], or to obtain more precise information on vibration source detection using unsteady approaches that have been adapted for conventional axial or centrifugal pump designs [27].
The fluid domain corresponding to the inlet pipe was properly extended to ensure stable inlet conditions.

Figure 10. A 3D model of the fluid domain.

Because of the quite simple structure of TBD pumps, structured hexahedral mesh was used to discretize the whole fluid domain, as shown in Figure 11. Leakage fluid domains were considered: the inlet ring area and the back chamber leakage, which is the result of the balance holes on the impeller hub side. Based on the experimental measurements, the inlet average velocity, which is calculated by the flow rate and inlet cross-sectional area, was decided as the inlet boundary condition. The total pressure was imposed as the outlet boundary condition. The impeller was set as a rotary component rotating at exactly the same angular velocity as that measured in the experiments. The wall roughness was determined to be 0.025 mm according to the accuracy of manufacture, and the non-slip wall boundary was applied on all of the wall surfaces.

Mesh sensitivity analysis was performed first, and based on the mesh independency analysis, the results of which are shown in Table 2, a total mesh number of around 8 million was adopted in order to achieve stable pump head and efficiency performance results with a difference of ± 0.6% and ± 0.8%, respectively. Moreover, most of the Y-plus values of the generated rotor mesh are around 10, as shown in Figure 12.

Figure 11. Mesh of fluid domains of the whole pump.
### Table 2. Mesh independency analysis

| Mesh Number (Million) | Inlet and Outlet Pipes | Impeller | Volute and Leaksages | Total | Head | Efficiency |
|-----------------------|------------------------|----------|----------------------|-------|------|------------|
| 1                     | 0.11                   | 0.35     | 0.43                 | 0.89  | 30.89| 25.31      |
| 2                     | 0.33                   | 0.64     | 1.20                 | 2.17  | 30.05| 23.88      |
| 3                     | 0.58                   | 1.40     | 2.59                 | 4.57  | 29.95| 23.82      |
| 4                     | 0.79                   | 2.81     | 4.43                 | 8.03  | 29.77| 23.63      |

**Figure 12.** Y-plus values of the TBD pump impeller.

Numerical simulations were performed for four different flow rates ($Q = 20, 50, 100$ and $150$ m$^3$/h). The pump head coefficient and hydraulic efficiency results are given in Figure 13 and are compared with the experimental ones. Despite the sudden drop in the experimental performance due to cavitation at a large flow rate for 2900 rpm, the head and efficiency values from CFD are quite close to the experimental ones in the vicinity of the maximum efficiency flow rate and above. Considering the objectives of the current paper, it should be considered that the CFD results could be used to determine the impeller performance, which is the main basis of the present investigation.

**Figure 13.** Comparison between experimental and CFD results.

For lower flow rates, the difference in the efficiencies may result from a bad estimation of the mechanical losses and increasing torque measurement uncertainties due to smaller torque values. Vertical error bars correspond to the experimental measurement uncertainties obtained due to the fluctuations in the measured data. Another explanation for the difference between experiments and CFD results at low flow rates is related to
unsteady effects that can be generally correctly modelled using the URANS approach, as already proven in numerous publications for conventional axial and centrifugal pumps.

4. Pump Component Performances and Related Losses

The present loss analysis is based on a one-dimensional approach that is equivalent to conventional pump designs by assuming that the total pump loss coefficient $\zeta_{\text{tot}}$ is equal to the sum of the individual pump component loss coefficients, which are referred to as the inlet loss $\zeta_{\text{inlet}}$, impeller loss $\zeta_{\text{imp}}$, and the volute loss $\zeta_{\text{vol}}$. So that:

$$\zeta_{\text{tot}} = \zeta_{\text{inlet}} + \zeta_{\text{imp}} + \zeta_{\text{vol}}$$  \hspace{1cm} (9)

The individual loss coefficient $\zeta_i$ is defined as the related total pressure loss divided by the outlet impeller rotational speed to the square multiplied by the working fluid density: $\rho U_2^2$,

$$\zeta_i = \frac{(P_{\text{t, out}} - P_{\text{t, in}})}{\rho U_2^2}$$  \hspace{1cm} (10)

where “i” represents one of the pump components (inlet, imp: impeller or vol: volute), and “in/out” is related to the inlet/outlet sections of the corresponding pump component.

They are supposed to depend on the geometry of each pump component and the flow rate and are independent of the rotational speed when the Reynolds number is high enough to assume the turbulent mean flow regime inside the pump flow passage. Total loss coefficient $\zeta_{\text{tot}}$ is obtained from experiments and CFD procedures. Comparisons of both sets of results are given in Section 3. The amount of volute losses is deduced from the pump losses minus the impeller losses.

One must keep in mind that this approach is unable to take several effects, such as unsteadiness, internal and upstream reverse flows, and impeller volute interactions. Its validity for different flow coefficients values will be confirmed.

4.1. Impeller Total Head Coefficient $\psi_{t,t,2}$ versus Flow Coefficient $\phi$

Measurements of the local static pressure at the impeller outlet section cannot be performed because both discs are rotating. Since the CFD results provide rather good overall performance predictions compared to experimental ones (see Figure 13), the mass-average total to static $\psi^*_{t,s,2}$ and total to total $\psi^*_{t,t,2}$ head coefficients for the impeller component alone, resulting from the CFD, are plotted in Figure 14 for several flow coefficients in addition to the experimental total head pump coefficient $\psi_{t,t,p}$, which is reproduced from Figure 8. Each coefficient expression is provided as follows:

$$\psi^*_{t,s,2} = \frac{(P_{s,2} - P_{t,1})_{\text{imp}}}{\rho U_2^2}$$  \hspace{1cm} (1)

$$\psi^*_{t,t,2} = \frac{(P_{t,2} - P_{t,1})_{\text{imp}}}{\rho U_2^2}$$  \hspace{1cm} (2)
Figure 14. Performance curves of the TBD impeller and TBD pump versus the flow coefficient.

It can be observed that the total of the static head gradient inside the impeller is small. For $\phi = 0$, the total of the static head coefficient is equal to $\psi_{t,s,2} = 0.118$, with the corresponding total to total head coefficient $\psi_{t,t,2}$ being equal to $\psi_{t,t,2} = 0.458$. These values come for an extrapolation of the CFD results, which were already presented. (1) These two-limiting couple of values allow us to check if the coherence of these results using the so-called rotary pressure, which can be derived from the energy conservation in the relative frame of reference and can be written as follows (Gülich [25]):

$$P_1 + 0.5 \rho (W_1^2 - U_1^2) = P_{2,\text{id}} + 0.5 \rho (W_2^2 - U_2^2)$$ (3)

along a mean streamline for an ideal transformation. For a real transformation, it can be written as (Gülich [25]):

$$P_1/\rho g + (W_1^2 - U_1^2)/2g = P_2/\rho g + (W_2^2 - U_2^2)/2g + \text{head losses}$$ (4)

or:

$$P_2/\rho g - P_1/\rho g= (U_2^2 - U_1^2)/2g - (W_2^2 - W_1^2)/2g - \text{head losses}$$ (5)

So,

$$\text{head losses} = (U_2^2 - U_1^2)/2g - (W_2^2 - W_1^2)/2g - (P_2 - P_1)/\rho g = 31 \text{ m}$$ (6)

The corresponding loss coefficient is equal to 0.33. The one obtained from the correlation is about 0.36 and corresponds to a 10% difference between the CFD and the model. (2) For $\phi = 0.1183$, the difference between $\psi_{t,t,2}$ and $\psi_{t,s,2}$ can be written as

$$\psi_{t,t,2} - \psi_{t,s,2} = (P_{t,2} - P_{t,1})_{\text{imp}}/\rho U_2^2 - (P_{s,2} - P_{s,1})_{\text{imp}}/\rho U_2^2 = V_{t,2}/2U_2^2 + V_r/2U_2^2$$ (7)

According to the theoretical head coefficient in Figure 9, one can determine that $V_{t,2}/U_2 = 0.56$, so $V_{t,2}/2U_2 = 0.1568$. Then, $V_r/2U_2 = 0.0074$. As such, the estimated value of $\psi_{t,t,2} - \psi_{t,s,2} = 0.1642$. Compared to the value from Figure 14, which corresponds to $\psi_{t,t,2} - \psi_{t,s,2} = 0.1518$, there is a difference of 7.5% that can be considered small according to the simplification adopted to obtain this value. (3) For $\phi = 0$, the difference between the total and static head at the impeller outlet can be written as (Gülich [25]):

$$H_2 - h_2 = V_2^2/2g$$ (8)

and for $\phi = 0$, $V_2 = 0$, and $V_2 = V_{t,2}$.
\[ V_{2g} = \mu \frac{U_{2g}^2}{2g} \]  

(9)

where \( \mu \) is the slip factor, which is equal to \( V_{θ_2}/U_{2g} \), meaning that one can obtain

\[ g(H_2 - h_2)/U_{2g}^2 = 0.5 \]  

(20)

The CFD results give a value of \( \psi_{*t,s,2} - \psi_{*t,t,2} = 0.327 \), which corresponds to a slip factor of 0.808. This corresponds fairly well to the extrapolated value of the experimental results that correspond to the ideal theoretical head coefficient curve without recirculation, which was already obtained in previous works (Heng et al. [10]). The extrapolated value, which was deduced from the experiments in Figure 8, corresponds to 0.8 at \( φ = 0 \). Compared to the one issued from CFD, the difference is only 1%.

4.2. Impeller Internal Flow Loss Evaluation

The internal impeller loss coefficient \( \zeta_{\text{imp}} \) is obtained from the difference \( \psi_{\text{th}} - \psi_{*t,t,2} \), which is the result of a combination of the experimental result (for \( \psi_{\text{th}} \)) and the CFD results (for \( \psi_{*t,t,2} \)). The values are given in Figure 15 versus the flow coefficient.

\[ \zeta_{\text{imp}} = \zeta_{\text{inc}} + \zeta_{\text{bolts}} + \zeta_{\text{cl}} + \zeta_{\text{sf}} + \zeta_{\text{rec}} \]  

(10)

The corresponding values are shown in Figure 15, and the way they are obtained from the loss correlation modelling is presented and detailed in Section 5.

5. One-Dimensional Loss Prediction

5.1. Impeller Loss Model Coefficient

The present analysis takes advantage of existing one-dimensional approaches proposed by several authors, such as Galvas [28] for incidence effects; Jansen [29] for blade-loading and clearance loss models; Johnston and Dean [30] and Coppage and Dallenbach [31] for mixing and recirculation loss models. The incidence loss correlation coefficient can be obtained from the following relationship [28]:

\[ \zeta_{\text{inc}} = (W_1 \cos (β_1 - β_3))/2UL_2^2 \] for a complete blade.  

(11)
The corresponding loss corresponds to the entire kinetic energy associated with the changes in the tangential velocity component from the impeller inlet section. This is because the blade angle $\beta_1 = 90^\circ$ and absolute velocity component is always quite a bit smaller than the rotational velocity $U = \omega R_1$. The corresponding incidence loss coefficient given from the model can be approximated by:

$$\zeta_{\text{inc}} = \frac{U_s^2}{2U^2} = \frac{(R/s/R_2)^2}{2} = \frac{(0.06/0.1)^2}{2} = 0.18 \quad (12)$$

Because the bladed area is half of the total impeller with, the corresponding loss coefficient is equal to 0.08. However, this evaluation is based on a simplified assumption for which the uniform inlet flow is supposed to be present at the impeller inlet section. This is the reason why this value can vary within an uncertainty band of ± 2%. This result can be seen in Figure 15, with additional model loss evaluations for clearance, blade-loading, and skin friction being expressed below.

The losses corresponding to the bolts are modelled using the drag coefficient around the cylinders assuming a local Reynolds number that is based on the bolt diameter and the rotational velocity of the bolts; it is equal to 0.10 for the present disc pump model, within ± 2.5%, depending on the drag coefficient evaluation.

Clearance loss model: This model determines the loss amount due to the fluid leakage from the pressure side to the suction side proposed according to Jansen [29] using the following equation:

$$\zeta_c = 0.6 c_l b_1 V_{\alpha_1} U_{\alpha_1} \left( \frac{R_{\alpha_1}^2 - R_{\alpha_1}^2}{R_{\alpha_1}^2 - R_{\alpha_1}^2} \right)^{\frac{1}{2}} \frac{V_{\alpha_1} V_{\alpha_1}}{U_{\alpha_1}^2} \left( R_{\alpha_1}^2 - R_{\alpha_1}^2 \right) (13)$$

The skin friction loss coefficient ($\zeta_{sf}$), diffusion factor, and related blade-loading loss coefficient ($\zeta_{bl}$) [29–31] are given by Equations (25), (26), and (27), respectively.

$$\zeta_{sf} = 2 G \frac{L_{\text{hyd}} W_{\alpha_1}^2}{b_{\text{hyd}} U_{\alpha_1}^2} \quad (14)$$

$$\zeta_{bl} = 0.05 D^2 \quad (15)$$

and

$$W = \frac{2W_2 + W_{\alpha_1} + W_{\alpha_1}}{4} \quad (16)$$

The diffusion factor $D$ was defined by Whitfield and Wallace [32] and was extended to off-design conditions by Rodgers [33] as follows:

$$D = 1 - \frac{W_2}{W_{\alpha_1}} + 0.6 \psi_{th} \frac{W_2}{W_{\alpha_1}} \left[ \frac{Z_B}{\pi} \left( 1 - \frac{R_{\alpha_1}^2}{R_2^2} \right) + \frac{2R_{\alpha_1}}{R_2} \right]^{-1} \quad (17)$$

The skin friction and blade-loading loss coefficients were found to be small compared to the clearance and incidence losses. The summation of above five loss coefficients is quite close to the CFD results within ± 5% uncertainty, which is an acceptable result based on these correlations. This means that the inlet loss values coming from the inlet pipe can be considered to be negligible.

The recirculation loss coefficient can be estimated using the Coppage and Dallenbach [31] correlation as:

$$\zeta_{\text{rec}} = 0.02 D^2 \cot \alpha_2 \quad (18)$$

The recirculation losses were found to be small for flow coefficients higher than $\phi = 0.05$. However, they increased when the flow coefficient decreased. They correspond to the hatched area shown in Figure 15. This is because the small value of the absolute angle $\alpha_2$ at the impeller outlet $\zeta_{\text{rec}}$ can reach a value of 0.6 for $\phi = 0.02$. This explains the rapid increase in the total loss coefficient of the impeller observed in Figure 15.
Additional loss evaluation due to the presence of bolts is specific to the present geometry since bolts do not exist for conventional designs with complete blades. This evaluation is based on the bolt diameter $d_{\text{bolt}}$ and the bolt rotational speed $U_{\text{bolt}}$, which leads to a turbulent regime since the Reynolds number related to the bolts is equal to $2.7 \times 10^5$.

The corresponding loss level is independent of the flow rate because it is assumed that most of the dynamic local pressure $0.5\rho W_{\text{bolt}}^2$ can be approximated by $0.5\rho U_{\text{bolt}}^2$ with $U_{\text{bolt}} = \omega R_{\text{bolt}}$, with $R_{\text{bolt}} = 0.075$ m.

The corresponding evaluation of the loss coefficient $\zeta_{\text{bolt}}$ is:

$$\zeta_{\text{bolt}} = k (U_{\text{bolt}}/U_2)^2 = k (R_{\text{bolt}}/R_2)^2 = 0.1125, \text{ using } k = 0.2$$  \hspace{1cm} (30)

5.2. Volute Loss Coefficient

Volute losses include mixed losses that generally develop at the inlet part of the volute just after the impeller outlet section. They can be written as the loss coefficient after the impeller being equal to $(\zeta_{\text{mix}} + \zeta_{\text{vol}})$. In this last relationship, $\zeta_{\text{vol}}$ corresponds to the volute loss coefficient with an ideal uniform inlet volute velocity without mixing effects.

The evolutions of $(\zeta_{\text{mix}} + \zeta_{\text{vol}}) = \psi^t, t, t, 2 - \psi_{t, p}$ are given in Figure 16. The corresponding loss coefficient exhibits minimum values for flow coefficient 0.075, for which the maximum efficiency values have been obtained from experiments. The yellow curve should represent the volute loss coefficient evolution that corresponds to ideal uniform inlet conditions at the impeller outlet without recirculation and without wakes.

![Figure 16. Volute and mixed loss coefficients versus flow coefficient.](image)

If this assumption is adopted, then the difference between the ideal curve and the real one corresponds to the mixed loss coefficient, which increases as the flow coefficient decreases.

The mixed losses can be derived from the work of Johnston and Dean [30]:

$$\zeta_{\text{mix}} = \frac{1}{1 + \cot^2 \alpha_2} \left( \frac{1 - \epsilon_W - b^*}{1 - \epsilon_W} \right) \frac{V_2^2}{2U_2^2}$$  \hspace{1cm} (19)

The first term of Equation (31) is small because the absolute angle value is quite small in the present case, regardless of the flow rate. However, the evaluation of the mixed losses strongly depends on the term in brackets, which is quite difficult to evaluate in the present case. However, the mixed loss coefficient can increase to up to one third of the impeller losses in the present case for low flow rates. The large sudden expansion from the impeller outlet width and the volute inlet width should be avoided to reduce these losses.
In a wide range of flow coefficients ranging from 0.6\(\phi_{opt}\) to 2.0\(\phi_{opt}\), these loss evaluations lead us to conclude that the impeller losses reach approximately 85% of the total hydraulic pump losses and that the volute is responsible for 15% of the total amount of pump losses. The individual loss amount inside the impeller compared to the total pump loss corresponds to 20% due to incidence effects, 25% each due to the bolts and the clearance effects, and 15% for blade-loading and skin friction effects. These percentages are obviously different for low flow coefficients because of the significant increase in the total losses due to strong recirculation effects.

An additional important result of this approach is related to the prediction of the optimum flow rate value, which allows the maximum hydraulic efficiency to be obtained. The analysis deduced from the results in Figure 16 tends to indicate that it is strongly related to the volute design parameters. These need to be confirmed using other pump designs in the future if relevant information on detailed geometries and hydraulic efficiencies are given.

6. Conclusions

An experimental analysis on global performance and on flow field inside the impeller of a TBD pump was performed using the CFD approach. Data reduction was performed using the overall data from the experiments to extract several loss coefficients from each element of the pump based on existing loss models that were initially developed for conventional pump designs. This procedure has never been presented before for the present disc pump geometry. The following conclusions can be drawn:

(1) The overall results of the experiments were determined in a specific pump design for two different rotational speeds: 1500 and 2900 rpm. Similarity laws that usually are applied for conventional pump designs can also be applied in the present pump geometry. The maximum global pump efficiency reached 35% for a flow coefficient \(\psi = 0.068\).

(2) The data reduction procedure that was adopted allows that calculation of the pump’s hydraulic efficiency. The maximum hydraulic efficiency value was close to 42%. It is equivalent to conventional semi-open impeller geometries with large clearance.

(3) The present loss correlation evaluation can predict such disc pump performances within a maximum error range of \(\pm 5\%\) for a rather wide flow coefficient range. This procedure also allowed us to have good initial predication for the optimum flow rate value for a given rotational speed. Such a prediction is usually related to the optimum incidence angle for conventional designs but cannot be applied in pure radial blade shapes that are often used in co-rotating disc pumps.

(4) The present loss evaluation can basically be applied to different disc pump geometries since it only relies on geometrical parameters and mean velocity components that can be obtained using one dimensional assumptions and classical similarity laws that are generally used in rotating machinery.

(5) The losses inside the impeller reached 85% of the total pump losses. The impeller efficiency reached a maximum value of 50%. The most important effects come from incidence, inter-blade leakage, and bolts losses. The blade-loading and friction losses inside the impeller were small due to small static pressure increases inside the impeller. Further investigation into the effects of the number of bolts and their location relative to the blade should be an important issue for reducing the related loss levels.

(6) Mixing losses downstream of the impeller are important below maximum flow coefficient values. This means that attention must be taken on the volute design that must be adapted to the present case.

(7) Based on the present results, a comparative study on the relative influence of geometrical parameters, such as the blade height ratio, impeller outlet width, and blade angle should be performed in the future. The authors also recommend providing mor
detailed geometrical information on the bolt diameter and radial location in the impeller. Mechanical and disc friction power must also be evaluated to determine the hydraulic efficiency for the whole flow rate range. Problems related to bolt location and diameter must also be further analyzed due to mechanical stress and disc deformation.

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Nomenclature

- \( b \): impeller channel width (m). \( b = 2h + cl \)
- \( b' \): ratio of diffuser inlet height to impeller outlet height
- \( cl \): inter blade clearance
- friction coefficient
- \( C_f \): friction coefficient
  - \( C_f = 0.0622 Re^{-0.2} \) when \( Re > 3 \times 10^5 \)
  - \( C_f = 2.67 Re^{-0.5} \) when \( Re < 2 \times 10^5 \)
- \( CFD \): related to computational fluid dynamic results
- \( d \): diameter (mm)
- \( D \): diffusion factor
- \( EXP \): related to experimental results
- \( g \): acceleration (m²/s)
- \( h \): blade height (m).
- \( H \): total head (m)
- \( k \): coefficient
- \( L \): length (mm)
- \( n \): repeat times of the measurements
- \( N \): rotational speed (rpm)
- \( P \): pressure (Pa)
- \( P_{disc} \): disc power (W)
- \( P_s \): shaft power (W)
- \( Q \): volume flow rate (m³/s)
- \( R \): radius (m)
- \( U \): rotational velocity (m/s), \( U = \omega R \)
- \( U_c \): measurement uncertainties
- \( V \): absolute velocity (m/s)
- \( W \): relative velocity (m/s)
- \( x \): value of measured data
- \( Z_B \): number of impeller blades (-)
- \( a \): absolute flow angle (°), from tangential direction
- \( \beta \): relative flow angle (°), from tangential direction.
- \( \beta' \): blade angle (°), from tangential direction
- \( \varepsilon_W \): wake blockage coefficient
- \( \eta_g \): global efficiency (%)
- \( \eta_{hyd} \): hydraulic efficiency (%)
| Symbol | Definition |
|--------|------------|
| $\omega$ | angular velocity (rad/s) |
| $\rho$ | fluid density (kg/m³) |
| $\varphi$ | flow coefficient (-) |
| $\psi$ | head coefficient (-) |
| $\psi_n$ | theoretical head coefficient, (-) |
| $\psi_n = \psi / \eta_{hyd}$ |
| $\zeta$ | loss coefficient |
| $\Omega_s$ | specific speed = $\frac{\omega Q^{0.5}}{(gH)^{0.75}}$ |
| $\Lambda$ | specific radius = $\frac{R(gH)^{0.25}}{Q^{0.5}}$ |

**Subscripts**

- 1: impeller inlet section
- 2: impeller outlet section
- bl: blade loading
- bolt: relative to the bolt
- cl: clearance
- disc: relative to the disc
- h: hub
- g: global
- hyd: hydraulic
- id: ideal
- in, inlet: inlet
- inc: incidence
- imp: impeller
- m: mechanical
- mes: related to measurement
- mix: mixing
- opt: related to the optimum efficiency location
- out: outlet
- p: pump
- r: related to the radial component
- rec: recirculation
- s: static, shroud
- sf: skin friction
- t: tip, total
- th: theoretical
- t,s: total to static
- t,t: total to total
- tot: total
- vol: volute
- v: volumetric
- w: wake
- ' : relative to blade geometry
- $\theta$: related to the tangential component

**Superscripts**

- *: average, mean value
- ′: relative to the impeller

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