Estimation of Turbulent Heating of Solar Wind Protons at 1 au

G. P. Livadiotis1, M. A. Dayeh1,2, and G. Zank3,4

1 Space Science and Engineering Division, Southwest Research Institute, San Antonio, TX, USA
2 Department of Physics and Engineering Astronomy, University of Texas at San Antonio, San Antonio, TX, USA
3 Center for Space Plasma and Aeronomic Research (CSPAR), University of Alabama in Huntsville, Huntsville, AL 35899, USA
4 Department of Space Science, University of Alabama in Huntsville, Huntsville, AL 35899, USA

Received 2020 October 15; revised 2020 October 26; accepted 2020 October 27; published 2020 December 22

Abstract

The paper presents a new method for deriving turbulent heating of the solar wind using plasma moments and magnetic field data. We develop the method and then apply it to compute the turbulent heating of the solar wind proton plasma at 1 au. The method employs two physical properties of the expanding solar wind plasma, the wave-particle thermodynamic equilibrium, and the transport of entropic rate. We analyze plasma moments and field data taken from Wind S/C, in order to compute (i) the fluctuating magnetic energy, (ii) the corresponding correlation length, and (iii) the turbulent heating rate. We identify their relationships with the solar wind speed, as well as the variation of these relationships relative to solar wind and interplanetary coronal mass ejection plasma.

Unified Astronomy Thesaurus concepts: Space plasmas (1544); Solar wind (1534); Heliosphere (711); Plasma astrophysics (1261)

1. Introduction

We employ two physical properties of the expanding solar wind plasma for improving our understanding of the turbulent heating of solar wind at 1 au, i.e., (a) wave-particle thermodynamic equilibrium (Livadiotis 2019a), and (b) transport of the rate of entropy change (Adhikari et al. 2020).

Recently, it was shown that the energy transfer between plasma particles and waves is governed by a new and unique relationship: the ratio between the energy per particle over the plasma frequency is constant, that is, a large-scale analog of Planck's constant denoted by $h_0$ (Livadiotis & McComas 2013, 2014a, 2014b; Witze 2013; Livadiotis 2013, 2015, 2016, 2017, Ch. 5; Livadiotis & Desai 2016; Livadiotis et al. 2018; Livadiotis 2019a). As an example, Figure 1 demonstrates the large variation of the representative average values and uncertainties of the plasma parameters of 27 space and astrophysical plasmas (Livadiotis 2019a), which are stable and residing at stationary states (Livadiotis 2018a, 2018b), while the respective values of the ratio $E_p/\omega_p$ that approaches the value of $h_0$ remain almost constant.

The wave-particle thermodynamic equilibrium requires that the energy $E_p$ of a plasmon (that is, the quantum of plasma oscillation) to be balanced by the energy per proton $E_p$, i.e., $E_p = E_p$ with:

1. plasmon energy $E_p = \text{energy of quanta } h_0 \cdot \omega_p$
2. energy per proton, $E_p = \text{sum of magnetic energy } B^2/(2\mu_0 n)$, enthalpy $\gamma/(\gamma-1)k_B T$, and turbulent energy $E_t$

The plasma-field coupling in the wave-particle equilibrium constitutes a fine probe for estimating the turbulent energy $E_t$ (which is associated with the turbulent heating and other relevant parameters):

$$E_p = h_0 \cdot \omega_p, \quad E_p = E_p + E_t \quad \text{or}$$

$$E_t = h_0 \cdot \omega_p - E_p^0, \quad \text{with, } E_p^0 = \frac{1}{2\mu_0} B^2/n + \frac{\gamma}{\gamma-1}k_B T,$$

(fundamental plasma oscillation frequency: $\omega_p = [n \cdot e^2 \varepsilon_0^{-1} (m_e^{-1} + m_p^{-1})]^{1/2}$; $m_e$, $m_p$: electron & proton masses; $e$: electron charge; $\varepsilon_0$: permittivity; $\mu_0$: permeability; $k_B$: Boltzmann constant; $\gamma = 5/3$).

Here we use the method provided by the wave-particle equilibrium shown in Equation (1) to derive the turbulent energy $E_t$ at $R = 1$ au with respect to solar wind speed. On the other hand, the turbulent energy is connected with the turbulent heating rate through the formalism of the transport of entropy and its rate of change.

The turbulent heating $S_t$ is necessary for the entropy derivation (Adhikari et al. 2020); the equation that connects the entropy $S = 3/2k_B \ln(P/n_T) + \text{const.}$ with the turbulent heating $S_t$ is given by

$$dS/dR = k_B \cdot S_t/(PV_{sw}),$$

where $P = nk_BT$ is the solar wind proton plasma thermal pressure; $n$ and $T$ are the proton density and temperature; $V_{sw}$ is the solar wind speed.

The turbulent magnetic energy and correlation length affect $E_t$ and $S_t$ according to Adhikari et al. (2020),

$$E_t = m_p \cdot [E_b^{0_1} + E_b^{0_0} \log(f/f_0)] \quad \text{with}$$

$$f \equiv E_b^A \cdot n^{-\frac{1}{2}}, \quad f \equiv f(R), \quad f_0 \equiv f(R_0),$$

$$S_t = \frac{1}{n} \cdot [E_b^{0_1} / \lambda_0^A + \sqrt{2}(E_b^{0_0} / \lambda_0^A \cdot (g/g^0)) \quad \text{with}$$

$$g \equiv (\lambda_0^A)^{-1}(E_b^0)^{-\frac{1}{2}}, \quad g = g(R), \quad g^0 = g(R_0),$$

where the different quantities are (a) the quasi-2D $E_b^{0_1}$, and “Slab” $E_b^A$, fluctuating magnetic energies (in unit mass), and (b) their corresponding correlation lengths, $\lambda_0^A$ and $\lambda_0^A$, respectively.

Figure 2 plots the observed and/or modeled values of (a) fluctuating magnetic energies, (b) correlation lengths, and (c) entropy, as functions of the heliocentric distance $R = 1–75$ au. The observed values were derived from Voyager 2 measurements (Adhikari et al. 2017, 2020); the modeled values were derived from
In this paper, we determine the turbulent heating rate $S_i/n$, and relevant turbulence parameters, such as, the fluctuating magnetic energy $E_{\omega}^m$, and its correlation length $\lambda_{\theta}^m$, by combining the two methods (as shown in Figure 3): (i) wave-particle thermodynamic equilibrium, characterized by the equation connecting the proton and plasmon energies, and (ii) entropy evolution, characterized by the equation connecting the entropic rate with turbulent heating. Section 2 describes the data used in this analysis. Section 3 develops the method for deriving the turbulent heating and its related parameters; in particular, we derive the relationships of turbulent heating rate with entropic rate, wave-particle equilibrium energy, and solar wind speed; we also study the variations of turbulent heating rate and related parameters between the solar

![Image of space & astrophysical plasmas](image)

Figure 1. Average logarithm values of various plasma parameters and of the ratio $E_{\omega}/\omega_{pi}$ for 27 different space and astrophysical plasmas (stable and residing at stationary states), where the variation of all the plotted parameters in contrast to the constancy of $E_{\omega}/\omega_{pi}$ is apparent. The plotted color-coded parameters are (a) density (gray), (b) temperature (light blue), (c) magnetic field strength (magenta), (d) plasma beta (brown), (e) Alfvén speed (yellow), (f) fast magnetosonic speed (deep blue), (g) Debye number (number of particles in a Debye sphere) (green), and (h) the ratio of the energy per proton over the plasma frequency, $E_{\omega}/\omega_{pi}$ (red). All parameter values are normalized to 1 (by dividing each of the 27 values with the maximum between them). The 27 plasmas and their abbreviations are as follows (from left to right in each panel); CIRs (c), coronal loops (cl), AGN (ag), LISM (li), planetary nebula (pn), CMEs (cm), solar wind—Helios (wh), solar wind—ACE (wa), solar wind—Ulysses (wu), solar wind—1 au average (wa), ionosphere (io), Aurora (au), plasma sheet (ps), plasmasphere (pl), sunspot plume (sp), shock example by Burlaga & King (1979) (sb), shock example by Gopalswamy & Yashiro (2011) (sg), magnetosheath (ms), inner heliosheath (ih), magnetosphere—average (ma), magnetosphere—cluster (mc), outer corona (oc), inner corona (ic), coronal holes (ch), Van Allen belts (va), Jovian magnetosphere—average (jm), termination shock (ts). (Taken from Livadiotis 2019a.)

![Image of observed and theoretical values](image)

Figure 2. Observed (blue) and theoretical (red) values of (a) fluctuating magnetic energies $b^{2}\omega^{3}/(A) = E_{\omega}^{m}/(A)\omega_{pi}$, (b) correlation lengths, and (c) entropy $S$ (with an arbitrary choice of the constant so that $S > 0$), plotted as a function of $R$. (Taken from Adhikari et al. 2020.)

![Image of methods](image)

Figure 3. Methods (orange) for computing turbulent heating and relevant turbulence parameters (green).

a system of coupled solar wind and turbulence transport model equations (Zank et al. 1996, 2012; Adhikari et al. 2017; Livadiotis 2019a).

In this paper, we reverse Equation (2), in order to determine the turbulent heating $S_i$ from the entropic rate $dS/dt$, where $V_{\omega}d/dR = d/dt$ (advection speed $V_{\omega} =$ flow speed $V_{sw}$), namely,

$$S_i = P \cdot \frac{d}{dt} \left( \frac{1}{k_B} S \right) = \frac{3}{2} P \cdot \frac{d}{dt} \ln(P/n), \text{ or}$$

$$\frac{1}{n} S_i = \frac{3}{2} k_B T \cdot \frac{d}{dt} \ln(P/n) = \frac{3}{2} k_B T \cdot \frac{d}{dt} \ln(k_B T/n^{\gamma-1}).$$

In this paper, we determine the turbulent heating rate $S_i/n$, and relevant turbulence parameters, such as, the fluctuating magnetic energy $E_{\omega}^m$, and its correlation length $\lambda_{\theta}^m$, by combining the two methods (as shown in Figure 3): (i) wave-particle thermodynamic equilibrium, characterized by the equation connecting the proton and plasmon energies, and (ii) entropy evolution, characterized by the equation connecting the entropic rate with turbulent heating. Section 2 describes the data used in this analysis. Section 3 develops the method for deriving the turbulent heating and its related parameters; in particular, we derive the relationships of turbulent heating rate with entropic rate, wave-particle equilibrium energy, and solar wind speed; we also study the variations of turbulent heating rate and related parameters between the solar

2
wind plasma and an interplanetary coronal mass ejection (ICME). Finally, Section 4 summarizes the conclusions, highlighting the analysis outcome, that is, a method for computing the turbulent heating using simply the plasma moments and magnetic field, and for improving our understanding of the turbulence complexity. (For instance, note that several attempts were made for the description of the complexity of turbulence, based on a new time domain, e.g., Varotsos et al. 2006, 2014, the theory of kappa distributions, e.g., Gravanis et al. 2019, and their connection with the phenomenon of wave-particle thermodynamic equilibrium.) The Appendix demonstrates a toolbox for the derivation of the uncertainty involved in the analysis.

2. Data

We use ∼92 s resolution of long-term observations of solar wind plasma moments (speed $V_{sw}$, density $n$, and temperature $T$ or thermal speed $V_{th} = (2k_{B}T/m_p)^{1/2}$) in conjunction with simultaneous measurements of the interplanetary magnetic field strength $B$, taken from the Solar Wind Experiment (SWE; Ogilvie et al. 1995) and Magnetic Field Investigation (MFI; Lepping et al. 1995) on board Wind S/C, publicly accessible at http://science.nasa.gov/missions. We focus on the first 70 days of 1995 (∼66,000 data samples; see Figure 4) in order to show our method for deriving the turbulent heating. This time period occurred during the declining phase of solar activity cycle 23, and was characterized by ICMEs, which is apparent in increases of the solar wind density and magnetic field magnitude that precede the arrival of the high speed streams at 1 au. ICMEs are identified using in situ measurements of magnetic field, solar wind ions, suprathermal electrons, energetic protons, heavy ion composition, and cosmic rays (Gosling 1996, 1997; Neugebauer & Goldstein 1997; Dayeh et al. 2017, 2018; see also, Gosling et al. 1993; Vorotnikov et al. 2008). ICMEs with high speeds may drive an interplanetary shock, identified as sharp increases in speed, density, temperature, and magnetic field strength (Szabo 1994). (ICME lists are regularly compiled based on Wind & ACE observations; for ICME lists, see Cane & Richardson 2003; Richardson & Cane 2010; see also Jian et al. 2006a, 2006b, 2009; Kilpua et al. 2015.)

3. Results: Derivation of Turbulent Heating Parameters

3.1. Relationship between Turbulent Heating and Entropic Rate

This analysis focuses on $R \sim 1$ au, hence, Equation 3(b) becomes $\frac{1}{2}S_{b} \cong m_{p} \cdot (E_{b}^{02}/\lambda_{b}^{0} + \sqrt{2}E_{b}^{A02}/\lambda_{b}^{A0})$. The second term in Equation 3(b) is much smaller than the first term and can be ignored in the inner heliosphere and especially for $R \sim 1$ au; indeed, as shown in Figures 2(a) and (b), $E_{b}^{0} \gg E_{b}^{A0}$ and $\lambda_{b}^{0} \ll \lambda_{b}^{A0}$ so that $E_{b}^{02}/\lambda_{b}^{0} \gg E_{b}^{A02}/\lambda_{b}^{A0}$; then, for $R \sim 1$ au, we obtain $\frac{1}{2}S_{b} \cong m_{p} \cdot E_{b}^{02}/\lambda_{b}^{0}$. (The second term is given in unit mass.)

First, we use proton plasma moments $n$, $T$, and $P = nk_{B}T$, to derive the entropy $S$, then, the entropic rate $dS/dt$, followed by...
the turbulent heating term $S_t$, then, we calculate $E_b^0 / \lambda_b^0$, i.e., the fraction involving the fluctuating magnetic energy $E_b^0$ and its correlation length $\lambda_b^0$. Therefore, we consecutively find:

(i) $\frac{1}{k_B} S_t = \frac{3}{2} \ln(P/n)$, (ii) $\frac{1}{n} S_t = k_B T \cdot \frac{d}{dt} \left( \frac{1}{k_B} S \right)$,

(iii) $E_b^0 / \lambda_b^0 \approx m_p^{-1} \cdot \frac{1}{n} S_t$.

Figure 5 shows the values of entropy $S$, entropic rate $dS/dt$, and turbulent heating term $S_t$ and rate $S_t/n$, corresponding to the data shown in Figure 4. We examine the relationships of these quantities with the solar wind speed $V_{sw}$. First, we examine the entropic rate plotted against $V_{sw}$.

Figure 6 displays the occurrence frequency of the solar wind speed $V_{sw}$, observed during the 70 day period shown in Figure 4(a), while Figure 6(b) shows the 2D-occurrence frequency of the entropic rate (plotted by its logarithm) taken from Figure 5(b), and plotted against $V_{sw}$. Figure 6(a) demonstrates the nearly bimodal nature of $V_{sw}$ in these observations, i.e., peaks corresponding to slow and fast solar wind streams, with respective averages $\sim 400 \text{ km s}^{-1}$ and $\sim 620 \text{ km s}^{-1}$. For this 70 day period, the separation between the slow and fast solar wind is near $\sim 550 \text{ km s}^{-1}$, i.e., where the distribution in Figure 6(a) has a minimum. Given the sampling distribution of the different solar wind speeds, it is not surprising that the 2D histogram of $dS/dt$ versus $V_{sw}$ in Figure 6(b) also shows two maxima and a minimum, corresponding to the peaks and the valley seen in Figure 6(a).

We therefore normalize the 2D histograms to investigate the actual relationship between $dS/dt$ and $V_{sw}$. Figure 6(c) shows
the 2D histogram normalized by the 1D histogram of $V_{sw}$, which clearly demonstrates that the distribution of entropic rates during this 70 day interval is independent of the solar wind speed. The independence of the entropic rates with respect to $V_{sw}$ is also shown in Figure 6(d). This figure shows the average $dS/dt$ estimated for each of the $V_{sw}$-bins. The 1D histogram in Figure 6(e) indicates that the mean value from all the bins is $\sim -3.22 \pm 0.07$, which is close to the mode of the slightly asymmetric distribution in Figure 6(d).

The entropic rate is calculated by the difference of sequential entropic values divided by the respective time interval. The entropy is given by the logarithm of $P/n^2$; thus, we approximate numerically the infinitesimal deviation of a logarithmic quantity $\ln(x)$ by the (a) difference of logarithms, $d\ln(x) \approx \ln(x_2) - \ln(x_1) = \ln(x_2/x_1)$, or by the (b) standard difference, $d\ln(x) \approx dx/x \approx (x_2 - x_1)/x_1 = x_2/x_1 - 1$ (where $x_1$ and $x_2$ are two sequential points of the quantity $x$). The two approaches are equivalent, as long as $\Delta t$ is small, because of the expansion $\ln(x_2/x_1) = \ln(1 + (x_2/x_1 - 1)) \approx (x_2/x_1 - 1)$. The time resolution of data sets ($\sim 92$ s) is sufficiently small, so that the entropic rate and turbulent heating, determined by either approximation, lead to similar results; indeed, Figure 7 plots $S_t/n$ for both approximations, (a) and (b), while panel (c) gives their percentage difference, $\{S_t^{(b)}/S_t^{(a)} - 1\}$; we observe that the average percentage difference is not larger than $\sim 10^{-1.5} \sim 1/30$.

(Thus, we require all processed $S_t/n$ rates to satisfy $\{S_t^{(b)}/S_t^{(a)} - 1\} < 1/30$.)

3.2. Relationship between Turbulent Heating and Wave-particle Equilibrium Energy

The constancy of the ratio of the energy per proton over the plasma frequency, $E_p^0/\omega_{pl}$ (and thus, the concept of plasma particle–wave thermodynamic equilibrium itself), has been previously confirmed by numerous space plasma measurements. The value of the involved Planck-like constant that characterizes stable space plasmas was found to be (Livadiotis 2017, 2019a):

$$h_\star = (1.16 \pm 0.08) \times 10^{-22} \text{ J s.}$$

The thermodynamic equilibrium characterizing the constancy of $E_p^0/\omega_{pl}$ appears to be violated in the case of the slow solar wind in the inner heliosphere. As has been observed, the ratio $E_p^0/\omega_{pl}$ deviates from the constant value of $h_\star$; this deviation is larger for smaller solar wind speeds. Indeed, Figure 8(c) plots the values of $E_p^0/\omega_{pl}$ versus solar wind speed $V_{sw}$, where we observe that $E_p^0/\omega_{pl}$ undergoes a continuous transition from the slow to the fast solar wind, tending asymptotically toward the known value of $h_\star$. The observed deviation of $E_p^0/\omega_{pl}$ from the constant $h_\star$ is caused by a missing energy that was not originally counted in the particle energy; that is, the turbulent energy $E_t$ (Livadiotis 2019a). Then, we use the total energy per proton $E_p$ that includes the turbulent energy, $E_p = E_p^0 + E_t$, instead of simply the nonturbulent term $E_p^0$. In this way, the wave-particle equilibrium, $E_p = h_\star \omega_{pl}$, constitutes a fine probe for estimating the turbulent energy: $E_t = h_\star \omega_{pl} E_p^0$ (as shown in Equation (1)).

In Figure 8(c), we observe that there are some time intervals, during which $\log(E_0^0/\omega_{pl})$ reaches a peak value of $\sim -22$. However, in other periods, $\log(E_0^0/\omega_{pl})$ decreases by more than one order of magnitude, up to $\sim -23.5$. The existence of strong turbulence determines the conditions where $\log(E_0^0/\omega_{pl})$ deviates from the peak value of $\log h_\star \sim -22$ (Figure 9). Namely, the turbulent energy $E_t$ undergoes a continuous decrease from slow to fast solar wind, tending asymptotically to zero.

The radial profiles of this missing energy $h_\star \omega_{pl} = E_p^0$ and the turbulent energy $E_t$ for the solar wind proton plasma in the inner heliosphere were derived and compared in Figure 10 (Livadiotis 2019a). As shown, the energy difference, $h_\star \omega_{pl} - E_p^0$, provides the turbulent energy $E_t$. The connection of the missing plasmon–proton energy with the turbulent energy provides a new method for estimating and cross-examining the turbulent energy in space and astrophysical plasmas.

Since the paper focuses on $R = R_0 \sim 1$ au, Equation 3(a) becomes $E_t = m_p \cdot E_0^0$, i.e., the second term in Equation 3(a) is negligible. Combining $E_t = m_p \cdot E_0^0 = h_\star \omega_{pl} - E_p^0$ from Equation (1) and $\lambda_0^0 = m_p \cdot E_h^0/(S_t/n)$ from Equation (5), we find the expressions of $E_0^0$ and $\lambda_0^0$ as functions of $h_\star \omega_{pl} - E_p^0$ and $S_t/n$, which can be derived from solar wind plasma moments. Namely,

$$E_0^0 = m_p^{-1}(h_\star \omega_{pl} - E_p^0),$$
$$\lambda_0^0 = m_p^{-1}((h_\star \omega_{pl} - E_p^0) \cdot \left(\frac{1}{n} S_t/n\right)^{-1}).$$

Figure 11 plots the normalized 2D histograms of $E_0^0$ and $\lambda_0^0$ determined as shown by the relationships in Equation (7), and plotted against solar wind speed $V_{sw}$.

In order to identify the physical conditions during such time periods, we first construct the normalized 2D histograms by
and its correlation length plotted versus and because of the turbulent energy (noted as missing energy), which was not originally included in . The plots use solar wind data from Wind S/C during the first 70 day period of 1995, shown in Figure 4. The energy difference, , provides the turbulent energy that was not included in the nonturbulent term (see Equation (1)). This missing energy is the turbulent energy heating of the solar wind. (Modified from Livadiotis & Desai 2016.)

binning the solar wind speed as abscissae and as ordinates. As in Figure 6(c), we normalize the raw 2D histograms by the corresponding 1D histogram of . Then, we generate the data set of , which provides the value of fluctuating magnetic energy , according to Equation (7). As shown in Figure 10(a), we construct the normalized 2D histogram of plotted versus , and determine the dependence (Figure 10).

This analysis has revealed a brand new feature that was not reported in earlier studies—a remarkably smooth transition from slow to fast wind of the turbulent heating rate, , as well as, of other turbulence parameters, such as the fluctuating magnetic energy and its correlation length . For instance, transitions smoothly from values of to as the solar wind speed increases from to (Figure 7). On the other hand, and decrease smoothly and linearly with respect to (on a log–log scale), revealing a power-law anticorrelated dependence (all plotted in Figure 10). The best-fitted expressions are given in Equation (8):

\[
E_b^0 = A_e \cdot V_{sw}^{-\alpha_e}, \quad \lambda_b^0 = A_\lambda \cdot V_{sw}^{-\alpha_\lambda}; \quad A_e = 10^{0.41 \pm 0.06}, \\
A_\lambda = 10^{19.02 \pm 0.22}; \quad a_e = 2.515 \pm 0.025, \quad a_\lambda = 8.14 \pm 0.08,
\]

with units in , in (au), and in (km s\(^{-1}\)).

3.3. Variations of Turbulent Heating Parameters with Solar Wind Speed

We can use the results of Sections 3.1 and 3.2 to understand the effects of the embedded solar wind and ICMEs (or other interplanetary structures) on the derived turbulence parameters, , , and .

As an example, we demonstrate the variations of the turbulence parameters between the solar wind and an ICME (observed for 24 hr at doy-29 of the 70 day period shown in Figure 4). Figure 12 shows the turbulence parameters of the ICME compared to those of solar wind. Clearly, the correlation length, describing the size of the biggest eddies in the turbulent plasma, remains invariant; also, the ICME’s turbulent heating is enhanced, with consequences in space plasma processes and thermodynamics (Verma et al. 1995; Sorriso-Valvo et al. 2007; Vasquez et al. 2007; Marino et al. 2008; Elliott et al. 2019; Livadiotis 2019b). For instance, the temperature rate can be connected with the turbulent heating rate , so that is larger and/or slightly smaller in the examined ICME, rather than in the solar wind.

A similar future analysis of the full ensemble of the structures over two solar cycles will provide insights into the physical processes interwoven with the variations of the turbulence parameters.
4. Conclusions

We employed two physical properties of the expanding solar wind plasma, (a) wave-particle thermodynamic equilibrium, and (b) transport of entropic rate, for improving our understanding of the turbulent heating of solar wind at 1 au.

We analyzed plasma moments and field data sets from Wind S/C, in order to compute (i) the fluctuating magnetic energy $E_b^0$, (ii) the corresponding correlation length $\lambda_b^0$, and (iii) the turbulent heating rate $S_t/n$. We then identified their relationships against the solar wind speed, as well as, the variation of these relationships when compared for the plasmas of solar wind and an ICME.

The wave-particle thermodynamic equilibrium requires the energy of a plasmon, that is, the quantum of plasma oscillation, to be balanced by the energy per proton, which sums the magnetic energy, enthalpy, and turbulent energy; we then express the energy equation in terms of the only unknown, the turbulent energy, which provides a good approximation of the fluctuating magnetic energy $E_b^0$.

On the other hand, the transport of entropy and its rate involves finding the turbulent heating rate, $S_t/n$, which is expressed in terms of $E_b^0$ and the corresponding correlation length $\lambda_b^0$. Our methodology uses the wave-particle thermodynamic equilibrium to compute $E_b^0$, and it is combined with the transport of entropy to compute $S_t/n$ and $\lambda_b^0$.

In summary, the paper results are outlined as follows:

(1) A new method was developed for deriving turbulent heating using plasma moments and magnetic field data.
(2) We computed the turbulent heating and its related parameters, i.e., (i) the fluctuating magnetic energy $E_b^0$, (ii) the corresponding correlation length $\lambda_b^0$, and (iii) the turbulent heating rate $S_t/n$.
(3) We constructed the solar wind speed dependence of the turbulent heating and its related parameters.
(4) The turbulent heating rate, $S_t/n$, was shown to increase with increasing solar wind speed for the slow wind, and tending toward a constant for the fast wind.
(5) An empirical power-law relationship of decreasing $E_b^0$ and $\lambda_b^0$ with increasing solar wind speed was found, where the involved exponents were rather sharp, i.e., $\sim-2.5$ and $\sim-8$, respectively.
(6) An ICME’s turbulent heating rate and fluctuating magnetic energy are enhanced when compared with the solar wind plasma, while the correlation length remains about invariant.
The analysis showed how the turbulent heating and its related parameters can be computed using simply the first plasma moments and the magnetic field; this work made it straightforward that a similar analysis to the full ensemble of the interplanetary structures over two solar cycles will provide insights into the physical processes interwoven with the turbulent heating rate and related parameters.

Authors M.A.D. and G.L. acknowledge partial support from NASA grants 80NSSC19K0079 and 80NSSC20K0290.

Appendix
Uncertainty Toolbox

The uncertainties are derived from propagating the errors of the involved variables and parameters; e.g., the uncertainty of $Y$ that depends on $\{X_i\}$, $i = 1, 2, \ldots$ is $\delta Y = \left[ \sum (\partial Y/\partial X_i)^2 \right]^{1/2}$. The second row of Table 1 shows the propagated (logarithmic) uncertainties of plasma frequency $\omega_{\text{pl}}$, thermal pressure $P$, proton plasma beta $\beta$, entropy $S$, nonturbulent beta $\beta_{\text{nonturb}}$, turbulent beta $\beta_{\text{turb}}$, $\beta_{\text{nonturb}}$, and fluctuating magnetic $E_B^0$ energies, and correlation length $\lambda_B^0$. The plasma density, temperature, and interplanetary magnetic field strength have log-normal distributed errors, which, on average, are $\delta n = \delta n_\text{n} \approx 3\%$, $\delta T = \delta T_\text{T} \approx 8\%$ (Kasper et al. 2006), and $\delta B = \delta B_B \approx 1\%$ (Lepping et al. 1995; Farrell et al. 1996) also $\langle \Delta T \rangle \approx 92\,\text{s}$. These are used for computing the approximations of the third row of Table 1.

ORCID iDs

G. P. Livadiotis https://orcid.org/0000-0002-7655-6019
M. A. Dayeh https://orcid.org/0000-0001-9323-1200
G. Zank https://orcid.org/0000-0002-4642-6192

References

Adhikari, L., Zank, G. P., Bruno, R., et al. 2015, ApJ, 805, 63
Adhikari, L., Zank, G. P., Hunana, P., et al. 2017, ApJ, 841, 85
Adhikari, L., Zank, G. P., Zhao, L.-L., & Webb, G. M. 2020, ApJ, 891, 34
Burlaga, L., & King, J. 1979, JGRA, 84, 6633
Cane, H. V., & Richardson, I. G. 2003, JGRA, 108, 1156
Dayeh, M. A., Desai, M. I., Ebert, R. W., et al. 2018, JPhCS, 1100, 012008
Dayeh, M. A., Desai, M. I., Mason, G. M., Ebert, R. W., & Farahat, A. 2017, ApJ, 835, 155
Elliott, H. A., McComas, D. J., Z Burnett, E. J., et al. 2019, ApJ, 885, 156
Farrell, W. M., Fritzemeier, R. J., Owen, C. J., et al. 1996, GeoRL, 23, 1271
Gopalswamy, N., & Yashiro, S. 2011, ApJL, 736, 17
Gosling, J. T. 1996, ARA&A, 34, 35
Gosling, J. T. 1997, in Coronal Mass Ejections: An Overview, in Coronal Mass Ejections, ed. N. Crooker, J. A. Joselyn, & J. Feynman (Washington, DC: AGU), 9
Gosling, J. T., Bame, S. J., McComas, D. J., et al. 1993, GeoRL, 20, 2789
Gravvanis, E., Akylas, E., Panagiotou, C., & Livadiotis, G. 2019, Entp, 21, 1093
Jian, L., Russell, C. T., Luhmann, J. G., et al. 2009, SoPh, 259, 345
Jian, L., Russell, C. T., Luhmann, J. G., & Skoug, R. M. 2006a, SoPh, 239, 337
Jian, L., Russell, C. T., Luhmann, J. G., & Skoug, R. M. 2006b, SoPh, 239, 393
Kasper, J. C., Lazarus, A. J., Steinberg, J. T., et al. 2006, JGRA, 111, A03105
Kilpua, E. K. J., Lumme, E., Andreouva, K., et al. 2015, JGR, 120, 4112
Lepping, R. P., Acuna, M. H., Burlaga, L. F., et al. 1995, SSRv, 71, 207
Livadiotis, G. 2015, JPhCS, 577, 012018
Livadiotis, G. 2016, ApJS, 223, 13
Livadiotis, G. 2017, in Kappa Distributions: Theory and Applications in Plasmas, ed. G. Livadiotis (Amsterdam: Elsevier)
Livadiotis, G. 2018a, EPL, 122, 50001
Livadiotis, G. 2018b, JGRA, 123, 1050
Livadiotis, G. 2019a, ApJ, 887, 117
Livadiotis, G. 2019b, Entp, 21, 1041
Livadiotis, G., & Desai, M. I. 2016, ApJ, 829, 88
Livadiotis, G., Desai, M. I., & Wilson, L. B., III 2018, ApJ, 853, 142
Livadiotis, G., & McComas, D. J. 2013, Entp, 15, 1118
Livadiotis, G., & McComas, D. J. 2014a, JGRA, 119, 3247
Livadiotis, G., & McComas, D. J. 2014b, in ASP Conf. Ser. 484, Large-scale Quantization in Space Plasmas: Summary and Applications, ed. Q. Hu & G. P. Zank (San Francisco, CA: ASP), 130
Marino, R., Sorriso-Valvo, L., Carbone, V., et al. 2008, ApJL, 677, 71
Neugebauer, M., & Goldstein, R. 1997, in Coronal Mass Ejections, ed. N. Crooker, J. A. Joselyn, & J. Feynman (Washington, DC: AGU), 245
Ogilvie, K. W., Chornay, D. J., Fritzemeier, R. J., et al. 1995, SSRv, 71, 55
Richardson, I. G., & Cane, H. V. 2010, SoPh, 264, 189
Sorriso-Valvo, L., Marino, R., Carbone, V., et al. 2007, PhRvL, 99, 115001
Szabo, A. 1994, JGR, 99, 14737
Varotsos, P. A., Sarris, N. V., & Skordas, E. S. 2014, JGRA, 119, 9192
Varotsos, P. A., Sarlis, N. V., Skordas, E. S., Tanaka, H. K., & Lazaridou, M. S. 2006, PhRvE, 74, 021123
Vasquez, B. J., Smith, C. W., Hamilton, K., et al. 2007, JGRA, 112, A07101
Verma, M. K., Roberts, D. A., & Goldstein, M. L. 1995, JGR, 100, 19839
Vorotnikov, V. S., Smith, C. W., Hu, Q., et al. 2008, SpWea, 6, S03002
Witte, A. 2013, Space Plasmas Share a Secret, https://www.nature.com/news/space-plasmas-share-a-secret-1.13159
Zank, G. P., Dosch, A., Hunana, P., et al. 2012, ApJ, 745, 35
Zank, G. P., Matthaeus, W. H., & Smith, C. W. 1996, JGR, 101, 17093