SIMPLER IS BETTER: SPECTRAL REGULARIZATION AND UP-SAMPLING TECHNIQUES FOR VARIATIONAL AUTOENCODERS

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ABSTRACT

Full characterization of the spectral behavior of generative models based on neural networks remains an open issue. Recent research has focused heavily on generative adversarial networks and the high-frequency discrepancies between real and generated images. The current solution to avoid this is to either replace transposed convolutions with bilinear up-sampling or add a spectral regularization term in the generator. It is well known that Variational Autoencoders (VAEs) also suffer from these issues.

In this work, we propose a simple 2D Fourier transform-based spectral regularization loss for the VAE and show that it can achieve results equal to, or better than, the current state-of-the-art in frequency-aware losses for generative models. In addition, we experiment with altering the up-sampling procedure in the generator network and investigate how it influences the spectral performance of the model. We include experiments on synthetic and real data sets to demonstrate our results.

1. INTRODUCTION

Generative deep neural network models such as the Generative Adversarial Network (GAN) [11] and the Variational Autoencoder (VAE) [2] have in recent years gained a lot of attention in e.g. face generation [3,4,5], image-to-image translation or style-transfer [6,7,8] tasks. The wide applicability of generative models has fostered a large body of research that aims to improve generative network architectures to enhance the quality of the generated images. Most of this work has focused on proposed variations of spatial loss terms in the objective functions, which has led to a multitude of different GAN and VAE architectures, see e.g. [9,10,11,8,12,13]. Although current methods generate very realistic-looking natural images, see e.g. [3,4,5], generative neural network models are in general not able to reproduce the spectral distribution of natural images adequately. Generated images still suffer from blurriness and lack of sharp details. This issue is illustrated in columns (a) and (b) of Fig. 1 where the first column, (a), shows an original sample from the CelebA dataset [14], and (b) is a blurry reconstruction of the same sample image from a VAE trained with a traditional spatial objective function.

The lack of high-frequency content can be partially explained by the spectral bias of neural networks [15]; neural networks prioritize low-frequency components of the data in the early stages of learning. A growing body of research has investigated these findings, see e.g. [16,17,18,19], and ways to utilize this in e.g. deep-fake detection [20,21,22,23]. Others propose different ways to resolve, work around, or reduce the effects of a bias towards the low-frequency components [21,24,22,25,24,17,26]. Another partial explanation for the discrepancy in the frequency content of generated images is the transposed convolution operation used in the up-sampling components of generative models. Durall et al. [21] argue that the transposed convolution operation is causing the models’ inability to learn the high-frequency content of the data and propose to append spectral regularization (SR) to the spatial objective function to mitigate the effects caused by the up-sampling strategy. Others, see e.g. [17,26], suggest to replace the last up-sampling operation in the architecture.

In this work we show that a simple frequency-aware loss that forces the generative model to focus on agreement of the overall spectral content of the data is equally effective, and sometimes better than the current state-of-the-art-in SR [21].

Fig. 1: A sample from the CelebA dataset [14]. Top row: (a): real image, (b): Vanilla VAE reconstruction and (c): reconstruction from VAE with spectral regularization. Bottom row: FFT spectrum of the corresponding images. We note the discrepancies at the highest frequencies of the 2D Fourier spectrum in (b), compared to (a), and the lack of details in the spatial representation of the image. A simple 2D FFT regularization (c) achieves less blurriness in the spatial domain and less discrepancies in the Fourier spectrum. Figure is best viewed online.
1.1. Related Work

Many works have illustrated the problems of generative models and spectral reconstruction. Several theories exist, but the most notable are spectral bias [15, 16] and issues related to the up-sampling operations in the final layers of the generator network [21, 26]. Karras et al. [4] generate high-resolution images by first letting their network focus on low-resolution images and then progressively shift the training to consider higher-resolution images. However, as pointed out by Khayatkhoei and Elgammal [16], application of the StyleGAN2 [4], which samples at high frequencies, might avoid the spatial frequency bias without actually solving the issue: high-frequency components, such as sharp details, are not preserved to the same extent in data that has been sampled at very high frequency [16]. Moreover, access to high-definition or high-resolution images is not always possible, especially not when working with e.g. remote sensing data or medical data. Very deep architectures might also be unsuitable when considering available computational power or computation time in specific applications and projects.

There are numerous works in the last two years that either try to explain the frequency discrepancy from a theoretical perspective, such as [24, 18], or acknowledge this drawback by proposing ways to resolve or reduce the effects of the spectral bias. Particularly important is the work by Durall et al. [21], which illustrates how standard up-sampling methods such as bilinear interpolation followed by traditional convolution. Results from our experiments show promising results by replacing the last transposed convolution layer with either zero-insert scaling, nearest interpolation, or bilinear interpolation followed by traditional convolution.

2. METHODOLOGY

This section briefly introduces variational autoencoders and the proposed frequency-aware loss function used in this work. A section describing the commonly used up-sampling procedures in convolutional neural networks is also included.

2.1. Variational Autoencoders

A variational autoencoder is a Bayesian generative model configured in an autoencoding fashion, with an encoder mapping the data, \( x \), into a latent variable, \( z \), and a decoder that maps the latent variable back to the original data space. As usual in a Bayesian setup, the problem of inference is to find the posterior distribution \( p(z|x) \). Since the evidence \( p(x) \) is typically intractable, a lower bound is optimized using variational inference [2]:

\[
\arg \min_{\phi, \theta} \mathbb{E}_{q_\phi(z|x)} \left\{ \log p_\theta(x|z) \right\} - \beta \text{KL}(q_\phi(z|x)||p(z)).
\] (1)

For full derivations, see [29] or [30]. Both \( q_\phi(z|x) \) (encoder) and \( p_\theta(x|z) \) (decoder) are modeled via neural networks. \( p(z) \) is the prior over the latent variable \( z \), which is commonly assumed to be multivariate Gaussian distributed. Furthermore, identifying \( \log p_\theta(x|z) \) as the negative BCE loss, we can replace this with an energy-based model, \( p(x|z) \propto \exp(-L(x, \mu_x(z))) \) where \( L \) is any function that leads to a proper probability density function [24]. This formulation allows alternative reconstruction losses, such as the Watson perceptual loss used in [24].
We employ three different datasets with increasing complexity for the evaluation: a simple gray-scale version of the Shape dataset by Jing et al. [33], the grey-scale MNIST dataset [34], and the RGB CelebA dataset [14] of celebrity faces. The Shape and MNIST datasets were analyzed at 32x32 resolution, while the CelebA dataset was analyzed at 64x64 resolution. We choose to employ the simple VAE networks from [33]. The focus of this work is to evaluate how SR, either alone or combined with last layer up-sampling [17], can enhance image quality. The influence of different network architectures on the models’ ability to reproduce the high-frequency content of the data is beyond the scope of this work and has therefore been omitted. The interested reader could consult [3, 4, 5] for examples of generative model architectures focused on generating high-resolution images from low-resolution images. To evaluate the performance of the models, we use the root mean squared error (RMSE) and azimuthal (polar coordinate) integration of the Fourier spectrum. Since the AI loss focuses on alignment in the 1D representation of the Fourier power spectrum, the Vanilla-VAE on the alignment in the spatial domain, and our FFT loss on the alignment in the 2D representation of the Fourier spectrum, we choose to compute the RMSE in all these three domains. RMSE metrics for the Watson-DFT loss on the Shape dataset have been omitted from the reported results of Sec. 3.1 and Sec. 3.2 since these models did not work correctly. We argue that this could be an effect of the Shape dataset being too simple for a more complex loss, but did not investigate this further since the Shape dataset was included only to compare how different losses generalize from simple to more complex datasets.

3.1. Spectral regularization with transposed convolution

Firstly, we trained VAE models for each of the three different datasets with the baseline Vanilla-VAE, and then with the added Watson-DFT, AI or the FFT loss by employing traditional transposed convolution up-sampling. Our purpose was to compare the three different ways to achieve SR against each other and the baseline. Based on this, we evaluated if our contribution, the FFT loss, can compete against the Watson-DFT and the AI loss. Tab. [1] summarizes the quantitative results from the empirical investigation, while Fig. 2a and Fig. 2b show the average azimuthal integration of the power spectrum for models trained with the different objective functions. The quantitative RMSE metrics in Tab. [1] show that our proposed FFT loss performs well in generating images that resemble the true images. The only exception is when the RMSE is computed in the AI-domain, where the Watson-DFT loss has a smaller RMSE than our FFT loss for the CelebA dataset. This is also shown in Fig. 2b.

3.2. Different last-layer up-sampling procedures

Secondly, we changed the up-sampling of the last layer of the VAEs from the traditional transposed convolution to ‘N.1.5’,
(d) CelebA+up

Fig. 2: Average azimuthal integration power spectrum computed for images in a test batch of either the MNIST [34] (first column) or the CelebA dataset [14] (second column) by applying either the Vanilla-VAE, Watson-DFT, AI or the FFT loss. Results for models trained with the traditional transposed convolution up-sampling operation are shown in (a) and (b). Corresponding results with the 'N.1.5' up-sampling [17] are shown in (c) and (d).

as introduced in Sec. 2.3 and repeated the experiments from Sec. 3.1. Tab. 2 summarizes the quantitative results from the empirical investigation, while Fig. 2c and Fig. 2d show average azimuthal integration of the power spectrum for models trained with the Vanilla-VAE, Watson-DFT, AI and FFT loss in combination with 'N.1.5' up-sampling in the last layer. In all cases, results in Tab. 2 show that models trained with our proposed FFT loss resemble the true data distribution better than any of the other evaluated objective functions. Comparing the rightmost parts of Fig. 2c and Fig. 2d to Fig. 2e and Fig. 2d, it can be noted that the change in up-sampling to ‘N.1.5’ improves the alignment of the high frequencies for all generative models. However, it should be noted that the change in up-sampling does not always imply lower RMSE, compare e.g. Watson-DFT for CelebA in the AI-domain in Tab. 1 with the corresponding value in Tab. 2. For the AI loss and CelebA we can verify the results from [17]; changing the up-sampling to ‘N.1.5’ reduces the RMSE in both the AI-domain and the 2D Fourier transform-domain. However, this result is not consistent for all datasets, over all tested SR losses, nor for the baseline Vanilla-VAE. This indicates that a change in the up-sampling procedure is one possible way to improve the performance of generative models, but the effect is not consistent, and we urge more research on this topic.

| Objective function | Dataset      | AI          | 2D FT       | Spatial domain |
|--------------------|--------------|-------------|-------------|----------------|
| Vanilla-VAE:      | Shape        | 1.2226 ± 0.8317 | 1.1791 ± 0.3184 | 0.0004 ± 0.00088 |
| AI:                | Shape        | 0.8892 ± 0.4943 | 1.0642 ± 0.3549 | 0.0003 ± 0.00055 |
| FFT:               | Shape        | 0.4447 ± 0.1671 | 1.0543 ± 0.3289 | 0.0001 ± 0.00021 |
| Vanilla-VAE:      | CelebA       | 3.5091 ± 0.8265 | 1.7278 ± 0.1319 | 0.0001 ± 0.00013 |
| Watson-DFT:       | CelebA       | 3.9728 ± 0.9607 | 1.8497 ± 0.0962 | 0.0004 ± 0.00028 |
| AI:                | CelebA       | 3.5084 ± 0.9108 | 1.7274 ± 0.1194 | 0.0009 ± 0.00028 |
| FFT:               | CelebA       | 2.8764 ± 0.5774 | 1.7270 ± 0.1249 | 0.0002 ± 0.00017 |
| Vanilla-VAE:      | CelebA       | 9.2300 ± 1.8732 | 4.3506 ± 0.7480 | 0.0123 ± 0.0136 |
| Watson-DFT:       | CelebA       | 6.7433 ± 2.7038 | 4.0370 ± 0.7803 | 0.0028 ± 0.00356 |
| AI:                | CelebA       | 9.5100 ± 2.0860 | 4.3345 ± 0.6696 | 0.0116 ± 0.0137 |
| FFT:               | CelebA       | 8.3239 ± 1.5421 | 3.5406 ± 0.6743 | 0.0237 ± 0.0303 |

Table 1: Mean ± std RMSE (lower is better, marked in bold) computed in AI-domain, 2D Fourier Transform (FT) domain and spatial domain, for experiments in Sec. 3.1 for Vanilla-VAE, Watson-DFT loss, AI loss, and the FFT loss with transposed convolution up-sampling.

| Objective function | Dataset      | AI          | 2D FT       | Spatial domain |
|--------------------|--------------|-------------|-------------|----------------|
| Vanilla-VAE:      | Shape        | 1.3893 ± 0.3328 | 1.1983 ± 0.3240 | 0.0004 ± 0.00035 |
| AI:                | Shape        | 0.8041 ± 0.4916 | 1.0940 ± 0.3186 | 0.0002 ± 0.00046 |
| FFT:               | Shape        | 0.1394 ± 0.1013 | 1.0325 ± 0.3248 | 2.6892±0.65 ± 0.0065 |
| Vanilla-VAE:      | CelebA       | 3.4711 ± 1.0887 | 1.8513 ± 0.1008 | 0.0084 ± 0.00234 |
| Watson-DFT:       | CelebA       | 3.6987 ± 1.2195 | 1.9171 ± 0.1164 | 0.0100 ± 0.00278 |
| AI:                | CelebA       | 3.1655 ± 0.9568 | 1.8270 ± 0.0848 | 0.0085 ± 0.00236 |
| FFT:               | CelebA       | 2.9276 ± 0.9551 | 1.7041 ± 0.0958 | 0.0071 ± 0.0189 |
| Vanilla-VAE:      | CelebA       | 9.4452 ± 3.7583 | 4.3022 ± 0.4761 | 0.0315 ± 0.0373 |
| Watson-DFT:       | CelebA       | 6.0802 ± 2.5990 | 4.0807 ± 0.8466 | 0.0290 ± 0.0059 |
| AI:                | CelebA       | 8.5200 ± 4.0594 | 3.6181 ± 4.3116 | 0.3156 ± 0.0367 |
| FFT:               | CelebA       | 5.8252 ± 2.5366 | 3.5917 ± 0.6925 | 0.0245 ± 0.0315 |

Table 2: Mean ± std RMSE for experiments in Sec. 3.2 for Vanilla-VAE, Watson-DFT loss, AI loss, and the FFT loss, with ‘N.1.5’ up-sampling in the last layer, following [17].

4. CONCLUSION AND FUTURE WORK

In this paper, we have shown that a simple spectral regularization term based on the 2D Fourier transform performs better than more complex regularization methods for improving the image quality of the VAE generative model. Moreover, our results show that changing the up-sampling procedure in the last layer from transposed convolution to nearest-neighbor interpolation followed by standard convolution gives more ambiguous results than indicated by previous research. Clearly, more research is needed to untangle the true spectral properties of neural generative models.

5. ACKNOWLEDGEMENTS

We thank Stian Normann Anfinsen at NORCE and Robert Jenssen at UiT for their valuable feedback. This work was financially supported by the Research Council of Norway (RCN), through its Centre for Research-based Innovation funding scheme (Visual Intelligence, grant no. 309439), and Consortium Partners.
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