High-order harmonic generation driven by inhomogeneous plasmonic fields spatially bounded: influence on the cut-off law

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Abstract
We study high-order harmonic generation (HHG) in model atoms driven by plasmonic-enhanced fields. These fields result from the illumination of plasmonic nanostructures by few-cycle laser pulses. We demonstrate that the spatial inhomogeneous character of the laser electric field, in a form of Gaussian-shaped functions, leads to an unexpected relationship between the HHG cutoff and the laser wavelength. Precise description of the spatial form of the plasmonic-enhanced field allows us to predict this relationship. We combine the numerical solutions of the time-dependent Schrödinger equation (TDSE) with the plasmonic-enhanced electric fields obtained from 3D finite element simulations. We additionally employ classical simulations to supplement the TDSE outcomes and characterize the extended HHG spectra by means of their associated electron trajectories. A proper definition of the spatially inhomogeneous laser electric field is instrumental to accurately describe the underlying physics of HHG driven by plasmonic-enhanced fields. This characterization opens up new perspectives for HHG control with various experimental nano-setups.

Keywords: plasmonics, high-order harmonic generation, attosecond pulses

(Some figures may appear in colour only in the online journal)

1. Introduction

Since the seminal experiment performed L’Huillier et al [1], the high-order harmonic generation (HHG) process has constantly increased its relevance and also provides important tools to conduct fundamental experiments in atomic and molecular systems. The nonlinear interaction of ultra-short intense laser pulses with atoms or molecules produces a plethora of phenomena [2–4]. Amongst them, the HHG, i.e. the generation of coherent radiation in the range of extreme ultraviolet to the soft-x-ray spectral range, is one of the most widely experimentally used and theoretically studied. The HHG phenomenon can be condensed using the 3-step model [5–7], namely, (i) in the first step, an electronic wavepacket is sent to the continuum by tunnel ionization through the potential barrier created as a consequence of the non-perturbative interaction between the atom and the laser electric field; (ii) after that, in the second step, the laser-ionized electronic wavepacket propagates in the continuum and is driven back to the vicinity of the parent ion when the laser electric field reverses its direction; (iii) finally, in the third stage of the sequence, this electronic wavepacket has a certain probability to recombine, producing an ultrashort—of the order of hundreds of attoseconds—burst of coherent radiation.

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harmonic radiation after the electron-ion recombination. Both classical and quantum approaches predict that the maximum harmonic order (the so-called HHG cutoff) can be estimated by:

\[ n_c = \frac{3.17U_p + I_p}{\omega}, \tag{1} \]

where \( I_p \) is the ionization potential of the atom or molecule under consideration and \( U_p \) is the ponderomotive energy, given by \( U_p = E_0^2/2 \omega^2 \), \( E_0 \) being the laser electric field peak amplitude and \( \omega \) the laser central frequency. Note that \( U_p \propto I^2 \) where \( I \) and \( \lambda \) are the laser intensity and wavelength, respectively. According to equation (1), there are two possible routes to extend the HHG cutoff \( n_c \) (i.e. to produce photons with much higher energy), namely, (a) to increase the laser wavelength \( \lambda \) [8, 9] or (b) to use more intense lasers. It must be mentioned that, however, longer wavelengths imply a sudden decrease in the HHG efficiency, governed by the well-known \( \lambda^{-5.2} \) law [10–12]. On the other hand, the utilization of more powerful lasers has a fundamental drawback: very rapidly we reach the saturation regime and then the atom or molecule results completely depleted within the leading edge of the laser pulse. This clearly results in a dramatic reduction in the HHG yield (or, in the most extreme case, in a total absence of emitted harmonic radiation) [13–15].

HHG obtained by means of the interaction of ultra-short laser pulses with noble gases has become in the last decade a key phenomenon to produce trains or isolated attosecond pulses [16, 17]. Many efforts have been conducted by the scientific community in order to improve and optimize the HHG process [12, 18–22]; related to this aim, a recent milestone was achieved: by taking advantage of the laser field enhancement obtained by localized plasmons polaritons (LPP), it was shown that it is possible to generate HHG with larger cutoffs. The LPP appears when a metal nanostructure is illuminated by a short laser pulse [23] and the resulting plasmonic-enhanced field presents two main characteristics, namely, (i) it is an amplified replica of the incoming, typically low intensity—\(10^{11}–10^{12} \) W cm\(^{-2} \), driving laser pulse and (ii) it develops spatial variations at a nanometric scale (for a recent review, see e.g. [24]). Besides the initial enthusiasm, the Kim’s experiment is not free of controversies (see e.g. [25–27]) and nowadays there exists a consensus that their setup is not the most viable route to generate HHG with low intensity laser sources. The dispute was, however, partially settled in [28], where low order harmonics were generated with a similar setup, but using a solid piece of material as a driven medium instead of a rare gas. From a theoretical viewpoint, the spatially nonhomogeneous character of the plasmonic-enhanced fields has a tremendous influence in the underlying physics of HHG [29, 30]. The effect of the plasmonic-enhanced electric fields can be accounted for by including a function that models their spatial variation. It was demonstrated that a clear cutoff extension appears and it is mainly due to the spatial inhomogeneous character of the driving field [31–34]. In particular, in [34] it was pointed out that the precise description of the spatial form of the plasmonic-enhanced fields is essential for an accurate prediction of the cutoff extension.

In this contribution, we study the fundamental physics of HHG in a model atom driven by a spatially inhomogeneous plasmonic-enhanced electric field. As was stated, this field results from the interaction between an ultra-short laser pulse and a metal nanostructure. In particular we explore the HHG process by using a realistic fitting of the electric near-field produced by a gold bow-tie shaped nanostructure. The results obtained in this paper are called to be very useful by considering they can clarify some aspects that have not been assessed until now. For instance, the utilization of a Gaussian-shaped and bounded functional form for the spatial variations of the plasmonic-enhanced electric field presents many advantages, that we describe throughout this article. Our quantum mechanical calculations, obtained by solving the one-dimensional time-dependent Schrödinger equation (1D-TDSE), in an argon model atom, are validated by using a pure classical analysis. In addition, further insights about the electron trajectories driven by these spatially bounded inhomogeneous electric fields, joint with the reasons of the HHG cutoff extension, can be extracted from this approach as well.

Our findings can be summarized as follows: we show that (i) the HHG cutoff energy scales with the laser wavelength at a power larger than 3. We also give an explanation of the reasons of this new dependence. We should emphasise, however, that this conclusion is obtained in a limited excitation spectral range and for a particular bow-tie shaped nanostructure; (ii) there exist upper bounds for the HHG cutoff energy and the spatial range of electron’s trajectories. Interestingly, these limits are independent of the excitation wavelength. In contrast, they are strongly dependent on the plasmonic-enhanced electric field spatial distribution; (iii) the field distribution can be designed tailoring the nanostructure geometry. As a consequence, it appears feasible to manipulate the HHG features engineering it. This finding can be extended to any plasmonic-enhanced spatially inhomogeneous field, independently of its origin. Moreover, we stress out that the description of the physics involved in our simulations is performed in a simple and comprehensive manner. In addition, both the quantum and classical results agree very well for the complete set of results obtained.

The rest of the article is organized as follows. In section 2, we discuss the underlying physics of the plasmonic field enhancement and how to compute the spatial shape of the plasmonic-enhanced spatially inhomogeneous field. Our studies include, as much as possible, realistic parameters. In section 3, we briefly describe our quantum mechanical model. We use this approach in section 4 to compute HHG for a large set of parameters. We also discuss here the scaling laws that govern the HHG cutoff in different laser wavelength ranges and what they imply. Finally, in section 5, we summarize the main findings, present our conclusions and give a short outlook. Atomic units are used, unless otherwise stated.

2. Plasmonic-enhanced fields properties

As it is well described in the paper of Kim et al [23], the electric field produced by a bow-tie shaped metal nanostructure, follows the pattern and intensity distribution as sketched in the figure 1(a). As it can be seen, when a laser
light field impinges onto the nanostructure, a bi-dimensional electric near-field is built up, with similar temporal characteristics as the incoming laser pulse, but with an enhanced peak amplitude (around 1–2 orders of magnitude, see e.g. [23]).

Additionally, the local near-field distribution is concentrated around the metallic nanostructure and spatially confined (see figure 1(b) for details). The spatial electric near-field distribution was obtained by using Full Wave, a numerical simulation software based on the finite difference time domain (FDTD) method, under the RSOFT suite [35]. The longitudinal dimension of each bow-tie was set to 175 nm and in figure 1(c) we display the electric near-field amplitude distribution in a range around ±100 nm centered at the middle of the gap. The intensity profile shown in figure 1(c) was calculated for a laser wavelength $\lambda = 800$ nm.

For our purposes, it is enough to reduce the study by considering the cross section between the bow-tie apexes plotted in figure 1(b). This point of view simplifies the representation of the electric near-field in one spatial dimension as it is detailed in figure 1(c), allowing to obtain the HHG yield by means of dimensionally reduced classical and quantum approaches. We have represented the effective near-field in a spatial range where a considerable volume of gas atoms can be ionized and, as a consequence, the HHG yield is strong enough to be experimentally detected. Additionally, it is possible to use the same effective near-field shape for other laser wavelengths, because the numerically calculated field distribution for each wavelength changes only its peak amplitude, leaving its horizontal spatial extension practically unchanged. Finally, note that the plasmonic-enhanced electric near-field oscillates at $\omega$, the frequency of the laser driving field.

Figure 2 shows the one-dimensional dependence of the plasmonic-enhanced electric near-field (note that the field amplitude is normalized at the point A). This curve was constructed by using two Gaussian functions to fit the black curve shown in figure 1(c). As we will show next, an accurate spatial description of the plasmonic driven field is instrumental to understand some of the HHG features.

Point A defines a local minimum of the plasmonic-enhanced electric near-field in the one-dimensional landscape. If we consider that ionization either occurs for both positive or negative electric fields (which correspond in each case to an electron moving to the negative and positive $x$ coordinate, respectively), the electron will always increase its velocity after ionization because at both sides of the point A, the electric field increases/decreases monotonically, depending if the electron moves to the left/right (see the text for more details).
frequencies (larger wavelengths) laser sources travel larger distances in the continuum before recombination (dashed color arrows in figure 2). This indicates they could reach far away regions from their starting initial points and spend larger times in the so-called laser continuum (see e.g. [34] for a detailed study about this aspect). As we will see in the next section, these circumstances are the main responsible of the HHG cutoff extension. This is so by considering that, at larger wavelengths, laser-ionized electrons are moving under the influence of an electric field that increases its intensity as a function of the spatial coordinate. Besides, taking into account a Gaussian-shaped profile for the plasmonic-enhanced driving near-field, the field amplification possesses a ‘natural’ limit, giving thus origin to distinct results.

On the other hand, for the point B, located at ~70 a.u. in our particular example (see figure 2), the electric near-field amplitude increases (decreases) if we move to the right (left) (solid color arrows in figure 2). HHG driven by plasmonic-enhanced near-fields with a spatial restriction to the A–B region was studied in previous works [31–33], where a first order approximation was employed. Below, we will show results that confirm and clarify this description in a more detailed form.

In principle, one would like to model the plasmonic-enhanced HHG process in a complete way, i.e. including both single-atom responses and collective effects. This task, however, is not under the reach of nowadays computational resources. One alternative way to proceed, in order to consider an ‘averaged’ effect of the plasmonic-enhanced field, would be to use a linear or quadratic model to describe the near-field for each position where the model atom is located. In this way the actual shape of the plasmonic-enhanced field would be entirely ‘probed’. A procedure following the latter reasoning was used in [36]. One of the main problems of these simple models, however, is that they would break down for larger wavelengths ($\gtrsim$1500 nm) and higher laser intensities ($\gtrsim$1 $\times$ 10$^{14}$ W cm$^{-2}$).

In fact, laser sources with the latter characteristics are nowadays available and, as a consequence, theoretical models capable to make realistic predictions would be needed.

3. Theoretical models

For a linearly polarized laser field, that is the case of our study, the dynamics of an atomic electron is mainly along the polarization direction. As a result, it is indeed a good approximation to employ the time-dependent Schrödinger equation in one spatial dimension (1D-TDSE). We can thus write (note that we consider the laser linearly polarized along the x-axis):

$$i \frac{\partial \Psi}{\partial t} = \mathcal{H}(t) \Psi(x, t)$$

$$= \left[ -\frac{1}{2} \frac{\partial^2}{\partial x^2} + V_{\text{atom}}(x) + V_{\text{plasm}}(x, t) \right] \Psi(x, t),$$

where $V_{\text{atom}}(x)$ is the atomic potential and $V_{\text{plasm}}(x, t)$ represents the potential due to the oscillating plasmonic-enhanced near-field at laser frequency $\omega$, developed by the nanosource. In here, we use for $V_{\text{atom}}(x)$ the quasi-Coulomb potential:

$$V_{\text{atom}}(x) = - \frac{1}{\sqrt{x^2 + \xi^2}},$$

which was first introduced in [37] and has been widely used in 1D studies of laser-matter processes in atoms. The required ionization potential can be defined by varying the parameter $\xi$ in equation (4). The potential $V_{\text{plasm}}(x, t)$ due to the plasmonic-enhanced electric near-field $E(x, t)$ is given by:

$$V_{\text{plasm}}(x) = - \int E(x, t) \, dx.$$  

Here the spatial dependency of $E(x, t)$ is strong (see figure 2) and we can incorporate it in $E(x, t)$ as follows:

$$E(x, t) = E_0 f(t) h(x) \sin(\omega t).$$  

In equation (6), $E_0$, $\omega$ and $f(t)$ are the electric field peak amplitude, the frequency of the coherent electromagnetic radiation and the pulse envelope, respectively. Furthermore, $h(x)$ represents the functional form of the spatial non-homogeneous part of the plasmonic-enhanced electric near-field. This spatial dependence can be represented as a sum of two Gaussian functions, that in turn can be written as a series of the form:

$$h(x) = \sum_{j=0}^{n} b_j x^j,$$

where the coefficients $b_j$ are obtained by fitting the real electric field shape (see figure 2). This field results from FDTD simulations, considering the real geometry of the bow-tie shaped nanostructure. In order to obtain a good fitting of the function $h(x)$, we have developed the expansion, equation (7), up to the 40th order ($n = 40$). Throughout this work, we use a pulse envelope $f(t)$ of the form:

$$f(t) = \sin^2 \left( \frac{\omega t}{2n_p} \right),$$

where $n_p$ is the total number of cycles, set as $n_p = 6$. We use $\xi = 1.18$ in equation (4) such that the binding energy of the ground state (GS) of the 1D Hamiltonian coincides with the (negative) ionization potential of argon, i.e. $I_0 = -15.76$ eV ($-0.58$ a.u.). Moreover, we assume that the noble gas atom is in its initial GS before ($t = -\infty$) we turn the laser on. Equation (3) is then numerically solved by using the Crank–Nicolson scheme. In addition, to avoid spurious reflections from the spatial boundaries, at each time step, the electron wavefunction is multiplied by a mask function. In our case, both the nanostructure gap (see e.g. [33]) and the spatially bounded character of the plasmonic-enhanced field, limit the electron motion and, in turn, the numerical spatial grid. For instance, at $I = 1 \times 10^{14}$ W cm$^{-2}$ and the largest wavelength employed, $\lambda = 1500$ nm, we have used $x_{\text{lim}} \sim \pm 400$ a.u., with a spatial step of 0.04 a.u. (around 20 000 spatial points). The atomic harmonic yield is then computed by Fourier transforming the so-called dipole acceleration $a(t)$ of its active electron. That is,
Here, $a(t)$ is obtained by using the following commutation relationship:

$$a(t) = \frac{d^2}{dt^2} = \langle \Psi(x, t) | [\mathcal{H}(t), [\mathcal{H}(t), x]] | \Psi(x, t) \rangle.$$  \hspace{1cm} (10)

Here, $\mathcal{H}(t)$ and $\Psi(x, t)$ are the Hamiltonian and the electron wavefunction defined in equation (3), respectively. The function $D(\omega)$ is also called the dipole spectrum, which gives the spectral HHG profile measured in experiments.

4. Results and discussion

The following calculations are made using a laser wavelength $\lambda = 800$ nm and considering an atom located at the point B (see figure 2). In this way, we will first support and validate the linear approximation for the plasmonic-enhanced near-field [33]. This assumption can be considered valid because the movement of the electron, at this laser wavelength, is developed in a tiny spatial region. We show from these results the importance of the sign of the electron motion under spatial inhomogeneous fields. In figure 3, the classical harmonic order versus the ionization/recombination time is shown (for details, see e.g. [30]). The colored arrows detail, for each part of the pulse (figure 3(a)), the trajectories followed by the electrons before and after ionization. It would be worth mentioning that, considering the electron electric charge, a negative electric field pushes the electron far away meanwhile the positive part of the driving pulse brings the electron back to the vicinity of the parent ion (recombination). As a consequence, it is expected that higher-order harmonics can be generated when the electron is ionized by the negative part of the driving pulse. To clarify this phenomenon, different color arrows are used in figure 3(b) to describe the above-mentioned process, at different cycles for the driving pulse. In order to obtain a larger cutoff, it is necessary, in all the cases, to take into account both the intensity and direction for each part of the driving pulse as it is detailed in figure 3. We can also observe from figure 3 that different energies at the recombination are obtained, depending on the direction of electrons movement (see figure 2). As an example, this fact can be clearly observed comparing the energy obtained for electrons ionized by the part of the pulse marked by a red arrow. In this case, the electrons travel to positive $x$ coordinates, where there is a large electric field amplitude, and the recombination energy is higher when compared with that for electrons ionized by the part of the pulse indicated by a black arrow (corresponding to negative $x$ coordinates, where the electric field amplitudes are smaller). The above description put forward the differences between the underlying physics of the HHG driven by spatial homogeneous and inhomogeneous fields. A similar set of results was reported by Shaaran et al. [38] using a quantum orbits analysis.

The next study is performed putting the model atom at $x = 0$ and at a laser-enhanced intensity of $1 \times 10^{14}$ W cm$^{-2}$ (see the point A in figure 2). For all simulations, we have considered a pulse given by equation (6). In order to analyze the evolution of the HHG cutoff with the laser wavelength $\lambda$, we perform quantum simulations at four different $\lambda$ values, i.e. 800, 1100, 1300 and 1500 nm, respectively. These results are compared against those obtained with the classical approach, under the same set of laser parameters.

In figure 4, we can observe the HHG spectra obtained by solving the 1D-TDSE for the four above-mentioned cases. As can be seen, for larger wavelengths a much higher photon energy (cutoff) is reached. This is not surprising, considering the HHG cutoff scales as $\lambda^2$ for spatial homogeneous fields. If we explore, however, the HHG cutoff dependence with the laser wavelength, it could be seen that, as the $\lambda$ increases, the cutoff behaves markedly different for spatial homogeneous and inhomogeneous fields. For $\lambda = 800$ nm (figure 4(a)), the HHG cutoff hardly differs if we use a spatial homogeneous or inhomogeneous field to drive the system. On the contrary, we find that for $\lambda = 1100$, 1300 and 1500 nm the HHG cutoff energy shows an increment reaching values up to $5.17U_p$, $8.47U_p$ and $9.8U_p$, respectively (see figures 4(b)–(d),

\[ D(\omega) \propto \int_{-\infty}^{\infty} dt e^{-i\omega t} a(t), \]  \hspace{1cm} (9)
respectively). It is noticeable that the maximum cutoff energy increases faster than in the case of spatial homogeneous fields, i.e. at a power larger than 2 with respect to the laser wavelength. On the other hand, considering the integration of the Newton–Lorentz equation, we can obtain the maximum energy for the electron at the recombination time with the parent ion. These results are displayed in figure 5. As can be seen, the maximum values of velocity (kinetic energy) reach by the electron follow the same behavior observed in the quantum simulations. This once again supports the particular dependence of the cutoff energy with respect to the excitation laser wavelength.

In order to get more details about the above distinct behavior, we present in figure 6 the dependence of the HHG cutoff, obtained by means of the classical analysis, as a function of the excitation laser wavelength \( \lambda \). We can thus distinguish four different regions, I–IV. In Region I (up to 1100 nm of excitation laser wavelength) the cutoff scales in a similar way as the homogeneous case. This is because at these laser wavelengths the excursion of the laser-ionized electron is small (as a reference, the red line corresponds to the case of a spatially homogeneous laser electric field) and, as a consequence, the spatial variation of the plasmonic-enhanced field is hardly 'probed' by the electron. In Region II, from 1100 to 1600 nm, the cutoff dependence scales with \( \lambda \) at a power above 3; in this region the difference between spatial homogeneous and inhomogeneous fields is much more pronounced.

In Region III, above 1600 nm and up to 3000 nm, we observe a rise in the HHG cutoff lower than the classic law. This fact can be understood considering the limited ionization-acceleration region, as a consequence of the bound electric near-field created by the nanostructure. At these larger wavelengths, the electron excursion is much more extended, so the electron reaches a spatial region where the electric field amplitude is strongly reduced according to the Gaussian-shaped profile fitting (see figure 2).

Finally, in Region IV, defined for laser wavelengths larger than 3000 nm, a sort of saturation in the HHG cutoff energy is observed (compare with the spatial homogeneous electric field case, that follows the \( \lambda^2 \)-law, irrespective of the laser wavelength range). To clarify this point, in figure 7, we show electron trajectories obtained by means of the classical approach. In figure 7(a), we present classical trajectories for a
Figure 5. Classical electron kinetic energy at recombination time as a function of the ionization (red) and recombination (green) times (for more details see e.g [30]). The system is driven by a spatial inhomogeneous field as showed in figure 2 and with the same parameters of figure 4. The model atom is located at point A. The $I_p$ of argon (15.76 eV) and the classical HHG cutoff energy (gray solid line) are shown.

Figure 6. Dependence of the HHG cutoff with the driving laser wavelength $\lambda$ for both spatial homogeneous (red circles) and inhomogeneous (black dots) fields. The Regions I–IV highlight the different functional dependences that describe the HHG cutoff behavior (see the text for more details).

Figure 7. Classical electron trajectories driven by a spatial inhomogeneous field at $\lambda = 3000$ nm (a) and $\lambda = 4000$ nm (b), respectively. It can be observed that the span of trajectories that recombine (shaded region) never overcome $\pm \sim 200$ a.u. (red dashed line).
spatial inhomogeneous field at $\lambda = 3000$ nm, meanwhile in figure 7(b), $\lambda = 4000$ nm. Interestingly, and for both spatial inhomogeneous cases, only few electron trajectories end at the parent ion, i.e. the electron recombination occurs. This means that the efficiency of HHG driven by these long wavelength spatially inhomogeneous near-fields is relatively low. Likewise, when a spatially inhomogeneous field drives the HHG process, two important facts can be extracted from figure 7. On the one side, it is observed that for many electron trajectories there is no recombination. In turn, this fact results in two main physical effects: (i) a low HHG yield and (ii) a large amount of direct electrons in the above-threshold ionization (ATI) process.

Both characteristics are associated with the spatial profile of the plasmonic-enhanced laser electric near-field. On the other side, it can be seen from figure 7 that, independently of the laser wavelength, the electron trajectories that recombine never overcome position values of $\pm 200$ a.u., for this particular electric field amplitude (as indicated by black lines in figure 2). This fact can be confirmed by comparing the electron trajectories for $\lambda = 3000$ and 4000 nm, as it is shown in figures 7(a) and (b), respectively. Additionally, this behavior can be understood taking into account the spatial extension of the electron trajectories developed at larger wavelengths. For these cases, the electron ‘feels’ an electric field of low amplitude (see figure 2) and, as a consequence, a limit in its kinetic energy appears. In summary, in spatially homogeneous fields the electron trajectories do not present limits and, as a consequence, they can reach larger displacements as larger wavelengths are used to drive the electron from the ionization point. In contrast, the trajectories for an electron driven by the studied Gaussian-shaped spatially inhomogeneous field, are constrained up to $\pm \sim 200$ a.u. This is because the plasmonic-enhanced electric near-field generated by the bow-tie shaped nanostructure is spatially bounded.

Additionally, the HHG cutoff energy reached at larger wavelengths, as we explained above, is limited due to the bound electric field, so the kinetic energy gained by the electron cannot overcome an asymptotic value close to $\sim 500$ eV (figure 6).

5. Conclusions and outlook

In conclusion, in this contribution, we reported original features of the HHG driven by a plasmonic-enhanced near-field. On the one side, we observed that the HHG cutoff energy scales with $\lambda$ at a power above 3 in a noticeable range of laser wavelengths. On the other side, in spatial inhomogeneous fields the electron classical trajectories showed several relevant characteristics: (1) the electron displacements are limited by the extension of the bound plasmonic-enhanced spatially inhomogeneous near-field, independently of the excitation wavelength; (2) it is shown that the HHG cutoff energy scales at a power above 3. This fact is directly related to the electric field dependence with the position where the ionization-recombination process takes place and (3) we showed and confirmed, based on classical arguments, that most of the electron trajectories never recombine, so this process would indeed improve the direct-ATI generation. It is worth mentioning that the cutoff behavior described in this work strongly depends on the functional form of the plasmonic-enhanced spatially inhomogeneous near-field proposed. As a consequence, it is expectable a different behavior if plasmonic-enhanced near-fields with other spatial properties are used to drive the HHG process. Summarizing, the results presented in this paper could open new avenues for nanostucture engineering and the exploration of alternative approaches for plasmonic-enhanced HHG.

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References

[1] Ferray M, L’Huillier A, Li X F, Lompre L A, Mainfray G and Manus C 1988 Multiple-harmonic conversion of 1064 nm radiation in rare gases J. Phys. B: At. Mol. Opt. Phys. 21 L31
[2] Protopapas M, Keitel C H and Knight P L 1997 Atomic physics with super-high intensity lasers Rep. Prog. Phys. 60 389
[3] Brabec T and Krausz F 1997 Nonlinear optical pulse propagation in the single-cycle regime Phys. Rev. Lett. 78 3282
[4] Krausz F and Ivanov M 2009 Attosecond physics Rev. Mod. Phys. 81 163
[5] Corkum P B 1993 Plasma perspective on strong field multiphoton ionization Phys. Rev. Lett. 71 1994
[6] Lewenstein M, Balcio P, Ivanov M Y, L’Huillier A and Corkum P B 1994 Theory of high-harmonic generation by low-frequency laser fields Phys. Rev. A 49 2117
[7] Schafer K J, Yang B, DiMauro L F and Kulander K C 1993 Above-threshold ionization beyond the high harmonic cutoff Phys. Rev. Lett. 70 1599

[8] Spielmann C, Burnett N H, Sartania S, Koppitsch R, Schnürer M, Kan C, Lentzner M, Wobrauschek P and Krausz F 1997 Generation of coherent x-rays in the water window using 5-femtosecond laser pulses Science 278 661–4

[9] Popmintchev T et al 2009 Phase matching of high harmonic generation in the soft and hard x-ray regions of the spectrum Proc. Natl Acad. Sci. 106 10516–21

[10] Tate J, Auguste T, Muller H G, Salieres P, Agostini P and DiMauro L F 2007 Scaling of wave-packet dynamics in an intense midinfrared field Phys. Rev. Lett. 98 013901

[11] Frolov M V, Manakov N L and Starace A F 2008 Wavelength scaling of high-harmonic yield: threshold phenomena and bound state symmetry dependence Phys. Rev. Lett. 100 173001

[12] Pérez-Hernández J A, Roso L and Plaja L 2009 Harmonic generation beyond the strong-field approximation: the physics behind the short-wave-infrared scaling laws Opt. Exp. 17 9891–903

[13] Strelkov V V, Sterjantov A F, Shubin N Y and Platonenko V T 2006 XUV generation with several-cycle laser pulse in barrier-suppression regime J. Phys. B: At. Mol. Opt. Phys. 39 577

[14] Pérez-Hernández J A, Roso L, Zair A and Plaja L 2011 Valley in the efficiency of the high-order-harmonic yield at ultra-high laser intensities Opt. Express 19 194430

[15] Moreno P, Plaja L, Malyshhev V and Roso L 1995 Influence of barrier suppression in high-order harmonic generation Phys. Rev. A 51 4746–53

[16] Farkas G and Tóth C 1992 Proposal for attosecond light pulse generation using laser induced multiple-harmonic conversion processes in rare gases Phys. Lett. A 168 447–50

[17] Hentschel M, Kienberger R, Spielmann C, Reider G A, Milosevic N, Brabec T and Krausz F 2001 Attosecond metrology Nature 414 509

[18] Carrera J J, Tong X M and Chu S I 2006 Creation and control of a single coherent attosecond XUV pulse by few-cycle intense laser pulses Phys. Rev. A 74 023404

[19] Chipperfield L E, Robinson J S, Tisch J W G and Marangos J P 2009 Ideal waveform to generate the maximum possible electron recollision energy for any given oscillation period Phys. Rev. Lett. 102 063003

[20] Serrat C and Biegert J 2010 All-regions tunable high harmonic enhancement by a periodic static electric field Phys. Rev. Lett. 104 073901

[21] Neyra E, Videla F, Pérez-Hernández J A, Ciappina M F, Roso L and Torchia G A 2016 Extending the high-order harmonic generation cutoff by means of self-phase-modulated chirped pulses Laser Phys. Lett. 13 115303

[22] Neyra E, Videla F, Pérez-Hernández J A, Ciappina M F, Roso L and Torchia G A 2016 High-order harmonic generation driven by chirped laser pulses induced by linear and non linear phenomena Eur. Phys. J. D 70 243

[23] Kim S, Jin J, Kim Y-J, Park I-Y, Kim Y and Kim S-W 2008 High-harmonic generation by resonant plasmon field enhancement Nature 453 757

[24] Ciappina M F et al 2017 Attosecond physics at the nanoscale Rep. Prog. Phys. 80 054401

[25] Sivis M, Duwe M, Abel B and Ropers C 2012 Nanostructure-enhanced atomic line emission Nature 485 E1–3

[26] Kim S, Jin J, Kim Y-J, Park I-Y, Kim Y and Kim S-W 2012 Kim et al. reply Nature 485 E1–3

[27] Sivis M, Duwe M, Abel B and Ropers C 2013 Extreme-ultraviolet light generation in plasmonic nanostructures Nat. Phys. 9 304–9

[28] Han S, Kim H, Kim Y W, Kim Y-J, Kim S, Park I-Y and Kim S-W 2016 High-harmonic generation by field enhanced femtosecond pulses in metal-sapphire nanostructure Nat. Commun. 7 13105

[29] Pérez-Hernández J A, Ciappina M F, Lewenstein M, Roso L and Zair A 2013 Beyond carbon K-edge harmonic emission using a spatial and temporal synthesized laser field Phys. Rev. Lett. 110 053601

[30] Ciappina M F, Pérez-Hernández J A and Lewenstein M 2014 ClassSTRONG: classical simulations of strong field processes Comput. Phys. Commun. 185 398–406

[31] Husakou A, Im S J and Herrmann J 2011 Theory of plasmon-enhanced high-order harmonic generation in the vicinity of metal nanostructures in noble gases Phys. Rev. A 83 043839

[32] Yavuz I, Bleda E A, Altun Z and Topcu T 2012 Generation of a broadband XUV continuum in high-order-harmonic generation by spatially inhomogeneous fields Phys. Rev. A 85 013416

[33] Ciappina M F, Biegert J, Quindat R and Lewenstein M 2012 High-order-harmonic generation from inhomogeneous fields Phys. Rev. A 85 033828

[34] Ciappina M F, Acimovic S S, Shaaran T, Biegert J, Quindat R and Lewenstein M 2012 Enhancement of high harmonic generation by confining electron motion in plasmonic nanostructures Opt. Express 20 26261–74

[35] FullWAVE-Rsoft User Guide 2008 RSoft Design Group, Inc. 400 Executive Blvd, Suite 100, Ossining, NY 10562

[36] Yavuz I 2013 Gas population effects in harmonic emission by plasmonic fields Phys. Rev. A 87 053815

[37] Su Q and Eberly J H 1991 Model atom for multiphoton physics Phys. Rev. A 44 5997

[38] Shaaran T, Ciappina M F and Lewenstein M 2012 Quantum-orbit analysis of high-order-harmonic generation by resonant plasmon field enhancement Phys. Rev. A 86 023408