Comments on \(AdS_2\) solutions from M2-branes on complex curves and the backreacted Kähler geometry

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Abstract We consider \(AdS_2\) solutions of M-theory which are obtained by twisted compactifications of M2-branes on a complex curve. They are of a generalized class, in the sense that the non-abelian part of the connection for the holomorphic bundle over the supersymmetric cycle is nontrivial. They are solutions of \(U(1)^2\) gauged supergravity in \(D = 4\), with magnetic flux over the curve, and then uplifted to \(D = 11\). We discuss the behavior of conformal fixed points as a function of the non-abelian connection. We also describe how they fit into the general description of wrapped M2-brane \(AdS_2\) solutions and their higher-order generalizations, by showing that they satisfy the master equation for the eight-dimensional Kähler base space.

1 Introduction

Since the proposal of AdS/CFT correspondence [1], we have witnessed copious examples of \(AdS\) solutions in String/M-theory which are all potentially dual to strongly interacting conformal field theories in various dimensions. The basic examples are of course flat M2, D3 and M5 branes which guarantee maximal supersymmetries in \(D = 3, 4, 6\). Notably, these branes may provide lower-dimensional, less supersymmetric \(AdS\) solutions when partially wrapped on supersymmetric cycles. On the field theory side, this procedure corresponds to topologically twisting the theory [2] through coupling to a combination of R-symmetry currents. The prescription for such configurations in lower-dimensional gauge supergravity theories was first illustrated in [3]. This work considered branes wrapped on 2-cycles in a Calabi–Yau manifold, and the generalization to higher-dimensional cycles was given in e.g. [4,5]. Schematically, one turns on the magnetic fields for bulk gauge fields which encode the twisting of the metric in higher dimensions, so that the effect of curvature on the supersymmetric cycle is canceled. In particular, for Kähler 2-cycles this means we assign precisely the spin connection of the 2-cycle to the diagonal \(U(1)\) part of the bulk gauge field. Then the supersymmetry is retained, albeit the curvature on the world-volume of the brane alone would not allow a constant spinor. Once the branes and supersymmetric cycles are identified, at least in the original prescription [3–7] one obtains unique BPS equations for each wrapped brane configuration when the cycles are hyperbolic space.

For such magnetic brane solutions relevant to 2-cycles, more general solutions were constructed with multiple non-vanishing \(U(1)\) charges, where the sum of magnetic fields still exactly cancel the spin-connection part in the Killing equations [8–10]. Their interpretation as general wrapped branes and the description of the dual conformal field theory are given in [11,12]. For concreteness, let us take a 2-cycle in a Calabi–Yau 3-manifold (CY3). For a holomorphic curve as a Kähler 2-cycle in CY3, locally the geometry is a holomorphic \(\mathbb{C}^2\) bundle over the curve, so in general the connection takes values in \(U(2)\). The supersymmetry constrains the diagonal \(U(1)\) part of the \(U(2)\), leaving the \(SU(2)\) part to one’s disposal. It is pointed out in [12] that choosing the \(SU(2)\) connection appropriately it should be possible to find a solution interpolating CY3 and CY2 as the embedding space. In gauged supergravity the implementation is quite simple: originally for 2-cycles in CY3 we take the diagonal \(U(1)\) among \(SO(4)\) gauge fields (which of course represent the isometry of a \(\mathbb{C}^2 = \mathbb{R}^4\) bundle over the holomorphic curve) and assign it the same value as the spin connection of the 2-cycle. For the generalization we take \(U(1) \times U(1) \subset SO(4)\), and require the sum of two \(U(1)\) connections to be the same as the spin connection of the 2-cycle. This prescription leads to a one-parameter generalization of BPS equations for M5-branes wrapping a 2-cycle in CY3 [11,12], and eventually an infinite number of new \(\mathcal{N} = 1\ AdS_5/CFT_4\) examples. The computation of central charges on both sides match perfectly. This is generalized to D3 branes and also to different supersymmetric cycles in [13–15].

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We note that a very similar idea can be applied also to the case of flat 2-cycles, leading to $AdS \times T^2$ or $AdS \times \mathbb{R}^2$ solutions [16, 17]. These were dubbed magnetic brane solutions and studied further in [18–20]. More generally, black holes of $D = 4$ gauged supergravity with the geometry of $AdS_2 \times \Sigma_2$, with $\Sigma_2 = S^2, H^2, T^2$, have been extensively studied in [21, 22].

In this article we consider M2-branes wrapped on $H^2$, especially the generalization with non-abelian part of connection on $H^2$. The relevant $D = 4$ gauged supergravity has $U(1)^4$ gauge fields and is a consistent truncation of maximal $SO(8)$ gauged supergravity theory. One may consider in this case 2-cycles in CY2, CY3, CY4, and CY5 manifolds. For each of them in the original construction [23] we turn on one, two, three, and four $U(1)$’s, respectively, to cancel out the effect of the spin connection on the 2-cycle. Then it turns out [23] that there exist $AdS_2$ fixed points for CY4 and CY5. The generalization mentioned above leads to a one-parameter family of $AdS_2$ fixed points interpolating CY4 and CY5. We also describe various holographic renormalization group flows between $AdS_4$ and $AdS_2 \times H^2$ solutions.

We will also discuss the uplifted $D = 11$ solutions of $AdS_2 \times H^2$ solutions. Containing an $AdS_2$ factor and being supersymmetric together imply that the solutions can be rewritten in the canonical form, where the internal nine-dimensional space is a warped and twisted circle fibration over an eight-dimensional Kähler space, satisfying [24]

$$\Box_8 R - \frac{1}{2} R^2 + R_{ij} R^{ij} = 0. \quad (1)$$

It is in principle possible to solve this equation first and then, using the geometric data of the Kähler base, to construct the whole $D = 11$ solution. In this paper we start with the uplifted $D = 11$ solution and employ a natural ansatz to check whether the above equation is indeed satisfied.

Supersymmetric solutions written in canonical form can provide useful information more readily. The supersymmetry relations are derived from the existence of Killing spinors and also by exploiting the properties of all spinor bi-linears. As such, solutions in canonical form immediately give full information on the Killing spinors. This can be very useful for instance when one looks for supersymmetric brane embeddings in a given supersymmetric background. References which successfully applied this technique to nontrivial backgrounds are e.g. [25, 26].

In the next section we give the action, the BPS equations and solve for the fixed points. In Sect. 3 we discuss the uplift to $D = 11$, and as a consistency check we verify that the nine-dimensional internal space satisfies the general condition given in [24] and discuss generalization to other dimensions. We conclude in Sect. 4.

### 2 $AdS_2$ solutions

In this section we present multiply charged magnetic brane solutions in $D = 4$ gauged supergravity. As far as we know such solutions are first systematically constructed in [9], especially in Section 8.

The supergravity model we employ here is the $U(1)^4$ truncated action of $\mathcal{N} = 8, D = 4$ gauged supergravity [27, 28]. After truncation, the bosonic field content reduces to a graviton, four vector fields $A_\alpha (\alpha = 1, 2, 3, 4)$, and three real scalar fields $\phi$. The action is

$$\mathcal{L} = \frac{1}{2k^2} \sqrt{-g} \left( R - \frac{1}{2} (\partial \bar{\phi})^2 - 2 \sum_\alpha e^{\alpha/2} F_{\bar{a}}^2 - V \right), \quad (2)$$

where

$$V = - \frac{4}{L^2} (\cosh \phi_{12} + \cosh \phi_{13} + \cosh \phi_{14}). \quad (3)$$

$L$ is a constant which sets the curvature of the $AdS_4$ vacuum solution. The three scalars $\bar{\phi} = (\phi_{12}, \phi_{13}, \phi_{14})$ can be alternatively expressed in terms of $X_\alpha$ in the following way:

$$X_\alpha = \exp (-\bar{a}_\alpha \cdot \bar{\phi}/2), \quad (4)$$

where

$$\bar{a}_1 = (1, 1, 1), \quad \bar{a}_2 = (1, -1, -1), \quad \bar{a}_3 = (-1, 1, -1), \quad \bar{a}_4 = (-1, -1, 1). \quad (5)$$

Note that $\prod_{\alpha=1}^4 X_\alpha = 1$.

It is well known that the maximal gauged supergravity in $D = 4$, and in particular its $U(1)^4$ truncated version, (2), is a consistent truncation of $D = 11$ supergravity. It means that any solution of (2) we may find leads to an exact solution in $D = 11$. The uplifting formula for the metric tensor is

$$\dd s^2 = \Delta^{2/3} \dd s_{4g}^2 + 2L^2 \Delta^{-1/3} \times \sum_\alpha X_\alpha^{-1} (\partial \mu_\alpha^2 + \mu_\alpha^2 (\partial \phi_{a} + 2A_\alpha/L)^2), \quad (6)$$

where $\mu_\alpha$ are angular variables parametrizing $S^4$, i.e. $\sum_{\alpha=1}^4 \mu_\alpha^2 = 1$. The warp factor is $\Delta = \sum X_\alpha \mu_\alpha^2$.

As discussed above, our generalized ansatz interpolates the two $AdS_2$ solutions of M2-branes wrapped on 2-cycles in Calabi–Yau four-folds and five-folds. For the gauge fields,

$$F_1 = F_2 = F_3 = -\frac{zL}{2} \text{vol}(\Sigma), \quad F_4 = -\frac{(1 - 3z)L}{2} \text{vol}(\Sigma). \quad (7)$$

Here we may choose the 2-cycle $\Sigma$ to have constant curvature, like $S^2, T^2$, and $H^2$. $l$ is the scalar curvature of $\Sigma$ and without losing generality we may scale it to be 1, $-1$ when it is nonzero. For $T^2$, we may first rewrite $l \to l/z$ before
solving \( l \) to zero. In particular, for \( T^2 \) we have in general

\[
F_1 = F_2 = F_3 = -\frac{zL}{2} \text{vol}(\Sigma), \quad F_4 = \frac{3zL}{2} \text{vol}(\Sigma). \tag{8}
\]

Now for the rest of the bosonic fields, in order to respect the same symmetry we constrain the scalar fields as follows:

\[
X_1 = X_2 = X_3 = e^{-\phi/2}, \quad X_4 = e^{3\phi/2}. \tag{9}
\]

We note here that \( z = 1/3 \) corresponds to the Calabi–Yau four-fold case, while \( z = 1/4 \) is for the Calabi–Yau five-fold solution in [23]. For the metric our ansatz is

\[
d_{S^4}^2 = e^{2f} (-dt^2 + dr^2) + e^{2\phi} ds^2(\Sigma). \tag{10}
\]

The supersymmetry transformation rules for the \( U(1)^4 \) model can be found for instance in [18,23]. There are four spinor parameters \( \epsilon^\alpha (\alpha = 1, 2, 3, 4) \) and just like the 1/8-BPS condition in [23], we choose \( \epsilon^\alpha = 0 \) for \( \alpha = 2, 3, 4 \). For generic values of \( z \) the BPS equations are given as

\[
e^{-f} f' = -\frac{1}{2\sqrt{2L}} (3e^{-\phi/2} + e^{3\phi/2})
+ \frac{1}{2\sqrt{2}} (3ze^{\phi/2} + (1 - 3z)e^{-3\phi/2}), \tag{11}
\]

\[
e^{-f} g' = -\frac{1}{2\sqrt{2L}} (3e^{-\phi/2} + e^{3\phi/2})
- \frac{1}{2\sqrt{2}} (3ze^{\phi/2} + (1 - 3z)e^{-3\phi/2}), \tag{12}
\]

\[
e^{-f} \phi' = -\frac{1}{\sqrt{2L}} (e^{-\phi/2} - e^{3\phi/2})
+ \frac{1}{\sqrt{2}} (ze^{\phi/2} - (1 - 3z)e^{-3\phi/2}). \tag{13}
\]

One can readily check that for \( z = 1/3 \) our equations are the same as (3.19) of [23] (up to the redefinition \( L = 1/e \) in the notation of [23]). On the other hand, for \( z = 1/4 \) an obvious solution is \( \phi = 0 \) and the rest of the above equations become (3.23) of [23].

In general the above equations determine the holographic RG flow obtained by twisting the maximally supersymmetric \( AdS_4 \) solution. To identify the \( AdS_2 \) fixed points, we demand \( g' = \phi' = 0 \), and it is straightforward to deduce

\[
z e^{4\phi} + (1 - 6z)e^{2\phi} + 1 - 3z = 0. \tag{14}
\]

Solving for \( e^{2\phi} \), we have

\[
e^{2\phi} = \frac{6z - 1 \pm \sqrt{(12z - 1)(4z - 1)}}{2z}. \tag{15}
\]

This equation is essentially the same as the first equation of (8.9) in [9].

Since \( e^{2\phi} > 0 \) by construction, this result provides a constraint for \( z \). One can easily check that the roots are both positive for \( 1/4 < z < 1/3 \), i.e. between the two \( AdS_2 \) solutions in [23]. When \( z \geq 1/3 \) only one of the solutions give a positive value for \( e^{2\phi} \). The result in (15) is independent of \( l \), but when we evaluate \( e^{-2g} \) we find that it is negative if \( l > 0 \).

In Fig. 1 we show the behavior of \( e^{2\phi} \) and \( R_{AdS_2} \) vs. parameter \( z \) for \( AdS_2 \) solutions. The upper (lower) branch is for positive (negative) sign in (15).

3 Uplift to \( D = 11 \) and general description

It is straightforward to construct \( D = 11 \) supergravity solution using the uplifting formula given above in (6). For the
metric, we have
\[ ds_{11}^2 = \Delta^{2/3} \left[ \frac{R_{AdS_2}^2 ds^2(AdS_2) + e^{2\phi} ds^2(H_2)}{\Delta} + e^{-3\phi/2} \frac{L^2}{\Delta} \right] \times \left( e^{2\phi} \sum_{a=1}^{3} (d\mu_a^2 + \mu_a^2 D\phi_a^2) + d\mu_4^2 + \mu_4^2 D\phi_4^2 \right). \]

The radius \( R \) of \( AdS_2 \) part in \( D = 4 \) is given by
\[ \frac{1}{R_{AdS_2}} = \frac{3e^{-\phi/2} + e^{3\phi/2}}{\sqrt{2L}}. \]  

Here it is understood that \( \phi \) is determined by the BPS condition (15). We note that the ratio of radii for \( AdS_2 \) part and \( H^2 \) part is given simply as
\[ \frac{R_{H^2}}{R_{AdS_2}} = 12z - 1. \]  

For our general ansatz, the warp factor is
\[ \Delta = e^{-\phi/2} (\mu_1^2 + \mu_2^2 + \mu_3^2) + e^{3\phi/2} \mu_4^2. \]  

And the twists are such that
\[ d(D\phi_1) = d(D\phi_2) = d(D\phi_3) = -z \text{vol}(H^2), \quad d(D\phi_4) = (3z - 1) \text{vol}(H^2). \]
It is well known that for a pure M2-brane configuration with unbroken supersymmetry and an $AdS_2$ factor, the solution can be always expressed (at least locally) in the following form [24,29]:

$$\mathrm{d}s_7^2 = e^{-2B/3}[\mathrm{d}s^2(AdS_2) + e^B \mathrm{d}s_5^2 + (\mathrm{du} + P)^2].$$  \hfill (21)

Here the eight-dimensional space $\mathcal{M}_8$ with metric $\mathrm{d}s_8^2$ should be Kähler and its Ricci tensor and the scalar curvature satisfy

$$\Box_R - \frac{1}{2} R^2 + R_{ij} R^{ij} = 0.$$  \hfill (22)

Then the entire $D = 11$ supergravity configuration is determined by the data of $\mathcal{M}_8$. In particular, $\mathrm{d}P$ is the Ricci two-form for $\mathcal{M}_8$, i.e. for the Ricci 2-form $\mathcal{R} = \mathrm{d}P$. The four-form gauge field of $D = 11$ supergravity is given by $G_4 = F \wedge \mathrm{Vol}(AdS_2)$. We have

$$\epsilon^B = R/2,$$

$$F = -J + \mathrm{d}[e^{-B} (\mathrm{du} + P)],$$  \hfill (24)

where $J$ is the Kähler form of $\mathcal{M}_8$. The equation (22) was in fact first derived from a study of D3-branes wrapped on Kähler 2-cycle in [30].

One can rewrite the $D = 11$ solutions (16) in a form compatible with (21) and check the supersymmetry conditions given above, in particular (22). The symmetry of the solutions in $D = 11$ imply that the eight-dimensional base manifold should contain factors of $H^2$ and $\mathbb{CP}^2$. Instead of just checking the BPS conditions for our $D = 11$ solutions, we here propose an ansatz suitable for a generalization to arbitrary higher dimensions [29]. The point is that the same equation, (22), when solved for six-dimensional Kähler space, can be used to construct $AdS_3$ solutions in IIB supergravity from D3-branes wrapped on 2-cycles [30]. And it was also shown that there exists a generalization to arbitrary higher dimensions [29], with a gravity action coupled to a vector field, a dilaton, and an associated set of BPS equations. In fact such a generalization was already obtained in [31], for the old wrapped M2-brane $AdS_2$ solutions in [23] and the result here presents a slight generalization.

For the $AdS_2$ solutions from wrapped M2-branes our metric ansatz for Kähler space is

$$\mathrm{d}s^2_{2n+4} = \Delta_1 \mathrm{d}s^2(H^2) + \Delta_2 \mathrm{d}\theta^2 + \frac{\sin^2 2\theta}{\Delta_2} \mathrm{d}\psi^2 + \cos^2 \theta \mathrm{d}s^2(K E^+_n),$$  \hfill (25)

where $K E^+_n$ is $\mathbb{CP}^2$ for wrapped M2-brane solutions. In general they are Kähler–Einstein space with unit radius and satisfy

$$\mathrm{d}\Omega_2 = i P_2 \wedge \Omega_2, \quad \mathrm{d}P_2 = -J_2,$$

$$\mathrm{d}\Omega_{2n} = i P_{2n} \wedge \Omega_{2n}, \quad \mathrm{d}P_{2n} = J_{2n}.$$  \hfill (27)

The nontrivial $U(1)$ fibration $D\psi$ in our metric ansatz is given as

$$D\psi = \mathrm{d}\psi - a P_2 - P_{2n}.$$  \hfill (28)

where $a$ is a constant. Recall that for the old solutions in [23], the uplifted solution has $a = 1$. One may check that $a \neq 1/3$ leads to $a \neq 1$, after straightforward re-phrasing of our uplifted solution (16) into the form of (21).

Obviously the Kähler form should be

$$J_{2n+4} = \Delta_1 J_2 + \sin 2\theta \mathrm{d}\theta \wedge D\psi + \cos^2 \theta J_{2n}.$$  \hfill (29)

From its closure, we easily get ($b$ is a constant)

$$\Delta_1 = a \sin^2 \theta + b.$$  \hfill (30)

We may calculate the Ricci tensor from the exterior derivative of the $(n + 2, 0)$ form $\Omega$.

$$\Omega = e^{-i\psi} \Omega_2 \wedge \cos^a \theta \left(\sqrt{\Delta_1} \Delta_2 \mathrm{d}\theta \right. + i \sqrt{\Delta_1 / \Delta_2} \sin^2 \theta \mathrm{d}\psi \left. \right) \wedge \Omega_{2n}.$$  \hfill (31)

From $\mathrm{d}\Omega = i \Omega \wedge \Omega$, we have

$$P_{2n+4} = \frac{1}{\cos^n \theta \sqrt{\Delta_1 \Delta_2}} \frac{\mathrm{d}}{\mathrm{d}\theta} \left[ \sqrt{\Delta_1 / \Delta_2} \sin 2\theta \cos^n \theta \right].$$  \hfill (32)

It is also straightforward to compute the Ricci scalar and other invariants such as $R_{ij} R^{ij}$ etc.

Not surprisingly, for the most general case the expression for the scalar curvature $R$ for Kähler base space is quite involved. It simplifies greatly if we assume $\Delta_2 = e^2 \Delta_1$, which is of course consistent with our uplifted solution. If we further demand that $R \propto (a \sin^2 \theta + b)^{-1}$ as the identification of warp factor $\Delta$ as $e^{-\theta}$ very clearly shows, we need to set $c^2 = (n + 1)/(a + b)$. Then we have

$$R = \frac{2(2a + (n + 2)b - 1)}{a \sin^2 \theta + b}.$$  \hfill (33)

Furthermore, if we consider the entire expression in (22), we find that it is factorized with a numerical coefficient, so the fourth order differential equation can be reduced to a quadratic equation,

$$a^2 - 2nab - b(n(n + 2)b - 2(n + 1)) = 0.$$  \hfill (34)

One can easily check the old solution of M2-branes wrapped on 2-cycle in CY4 [23,31], which corresponds to $a = 1$, $b = 1/n$.

Although it is a good sign that we again have obtained a quadratic equation, it is not immediately clear that the two quadratic equations (14) and (34) in fact encode the same $D = 11$ solutions. A neat way would be to compare two physically significant quantities. One is the ratio of radii as given in (18), and the other is the ratio of the maximal and minimal values of the warp factor $\Delta_1$ and
equivalently $\Delta$ as a function of $\theta$. By identifying these two quantities, we find the following mapping of parameters:

$$e^{2\phi} = 1 + a/b, \quad z = (a + 2b)/6.$$  \hspace{1cm} (35)

Then it is easy to check the equivalence of (14) and (34).

4 Discussion

In this work we studied $AdS_2$ solutions in M-theory by applying the prescription of [11,12] to M2-branes wrapped on 2-cycles with non-abelian connections. As one varies the parameter $z$, the solutions interpolate CY4 and CY5. As a consistency check we have verified that the uplifted $D = 11$ solutions satisfy the general supersymmetry condition (22) and we also presented a generalization to other dimensions.

With new $AdS$ solutions in String/M-theory in general, it is natural to try to identify the dual conformal field theory and check the validity. For the solutions at hand, the duals are (strongly coupled) quantum mechanics. The problem is, unlike M5- and D3-branes wrapped on 2-cycles, that there is no (strongly coupled) quantum mechanics. The problem is, that there is no (strongly coupled) quantum mechanics. The rule as a maximization [32] or c-extremization [13] is yet to be discovered. It would be certainly very nice if we can establish AdS/CFT duality pairs in a quantitative manner, probably in a way similar to F-maximization [33] where one uses the non-divergent part of the partition function as a function of the $R$-charges. We hope that the one-parameter extensions and their Killing spinor geometry in this paper help to uncover such relations.

The wrapped brane constructions in gauged supergravity theories were generalized to 3- and 4-cycles in [4–6]. It would be interesting to find new solutions which interpolates different wrapped brane $AdS$ solutions with different amount of supersymmetries. We plan to come back to this issue in the near future.

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