Strong non-classical induction forces in ion-surface interactions: General origin of Hofmeister effects

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Hofmeister effects continue to defy all-encompassing theories, and their origin is still a matter of debate. We observed strong Hofmeister effects in Ca\(^{2+}/Na^{+}\) exchange on a permanently charged surface over a wide range of ionic strengths. They could not be attributed to dispersion forces, classical induction forces, ionic size, or hydration effects. We demonstrated that another stronger force was active in the ion-surface interactions, and which would create Hofmeister effects in general. The strength of this force was up to 10^4 times that of the classical induction force, and could be comparable to the Coulomb force. Coulomb, dispersion and hydration effects appeared to be interwined to affect the force. The presence of the observed strong non-classical induction force implied that energies of non-valence electrons of ions/atoms at the interface might be heavily underestimated in current theories, and possibly just those underestimated energies of non-valence electrons determined Hofmeister effects.

Hofmeister effects, also known as specific ion effects, were observed over 120 years ago. Even though they are ubiquitous in the physical, chemical and biological literature, their origin is still contested and has been recently brought to the forefront of research. New work in this area may break down barriers between physics and biology.

Ionic sizes, hydration, quantum fluctuations (or dispersion forces), and surface charges are crucial in Hofmeister effects. Nano-scale surfaces and colloidal particles (e.g., DNA, proteins, cells, bacteria, metal oxides, and clay) are usually strongly charged in aqueous solution, and the sign of the charge or the charge number for biological macromolecules will be dependent on pH and ionic strength. In classical theory, the surface charges can set up a strong electric field extending from the surface to several nanometers in solution. Typical surface charge densities and their corresponding electric field strengths include: (1) membrane with surface charge densities of 0.28 C/m^2, and electric fields of 4 \times 10^8 V/m (assuming a planar surface); (2) for natural clay (e.g., illite), it is \sim 0.2895 C/m^2, with an electric field of \sim 4.2 \times 10^8 V/m at the surface; (3) for metal oxides it is 0.3–1.0 C/m^2, with a surface electric field of 10^8–10^9 V/m; (4) for artificially synthesized nano-TiO_2, it is 0.25 C/m^2 and 3 \times 10^8 V/m, respectively. For proteins, surface charge density measurements are primarily based on zeta potentials; therefore, they would be equal to the charge density at the shear plane, which is possibly much lower than the charge density at the surface, especially when considering the strong surface hydration force. At the shear plane, the charge density could reach 0.02–0.35 C/m^2, with an electric field of 10^8–10^9 V/m. Therefore, it is reasonable to expect electric field strengths \sim 10^8 V/m at protein surfaces in aqueous solutions. However, in those calculations, adsorbed counter-ions near the surface are treated as point charges. If their ionic size were taken into account, then the electric field near the surface would be much greater than 10^8 V/m. This is because the finite size of counter ions could weaken their screening effect, as compared with point charges.

Noah-Vanhoucke and Geissler found that, the persistence of electric field in the space near liquid-vapor interface shapes the sensitivity of solute distributions to ion polarizability, and the electric field often plays central role in the influence of ionic polarizability on ion density profiles. Surely, the distribution of the polarized ions would reversely influence the electric field itself. Therefore, at the interface, ionic polarization, ionic distribution and the electric field are interwined. At the solid/liquid interface, however, we often meet strong electric field greater than 10^8 V/m, the effects observed by Noah-Vanhoucke and Geissler might be much stronger and much more complex.
In classical theory, induction forces are much weaker than dispersion forces; thus the contribution of induction forces to Hofmeister effects can be neglected. In strong electric fields of \(10^8 - 10^9\) V/m, however, we must question the validity of classic induction theory for three reasons. First, if an atom or ion is strongly polarized, the binding force of the nucleus to the extranuclear electrons decreases, and, simultaneously, the contribution of the high external electric field to the energy of the electrons is greatly enhanced. The exact additional potential energy of the electrons from the high external electric field should be included in the Hamilton operator. Second, the range of electrostatic forces from surface charges is longer than that from a single ion\(^{26}\), which means that at the surface the additional force on an ion/atom from the external electric field and polarization effects will be long range. Third, there are many counter-ions around the surface and if they are all strongly polarized in the high external electric field\(^{15-16}\), then they will reversibly and strongly influence the external electric field itself. All of these effects must be correctly evaluated.

Because the selectivity coefficient in cation exchange equilibrium varies exponentially with cation-surface interaction energies for the two cation species involved, a slight difference in their respective interaction energies could result in significant differences in selectivity coefficient. Therefore, the ion selectivity coefficient is a useful parameter in quantitative evaluation of Hofmeister effects. For quantitatively evaluate the Hofmeister effects, we should firstly evaluate the contribution of Coulomb interaction to the selectivity coefficient accurately. We recently derived exact analytic solutions for the non-linear Poisson-Boltzmann equation for cation exchange in mixed electrolyte solutions\(^{38}\). This enables accurate evaluations of Coulomb interaction effects on the selectivity coefficient, which in turn allows experimental evaluation of Hofmeister effects on the selectivity coefficient from cation exchange equilibrium data. As a result, a comparison can be made between experimental results and calculated Hofmeister effects that take into account ionic size, hydration, dispersion forces, and classical induction forces.

By analyzing published Ca\(^{2+}\)/Na\(^+\) exchange equilibrium data under a wide range of electrolyte concentrations and ionic strengths \((0.0075 - 0.354\) mol/l\(^2\))\(^{26}\), we found that the observed Hofmeister effects could not be understood in terms of any classical interaction effects noted above, but instead requires a strong new force between cation and surface.

**Results**

**Selectivity coefficient of cation exchange by classical Coulomb force.** For Ca\(^{2+}\)/Na\(^+\) exchange, the selectivity coefficient may be defined as:

\[
K = \frac{a_{Na}N_{Ca}}{a_{Ca}N_{Na}}
\]  
(1)

where \(a_{Na}\) and \(a_{Ca}\) are the activities of Na\(^+\) and Ca\(^{2+}\), respectively, in bulk solution (mol/l), and \(N_{Na}\) and \(N_{Ca}\) are the adsorbed quantities (mmol/g) of Na\(^+\) and Ca\(^{2+}\), respectively, because of the Coulomb force.

An advantage of Eq. 1 is that it can quantitatively evaluate the relative preference between Ca\(^{2+}\) and Na\(^+\). Thus, when \(K > 1\), there is a preference of Ca\(^{2+}\) over Na\(^+\) in exchange; and vice versa for \(K < 1\).

If cation adsorption forces were Coulomb, Eq. 1 gives:

\[
K_C = \frac{a_{Na}N_{Ca}}{a_{Ca}N_{Na}} \int_0^\infty \frac{Z_{CaF}c_{Ca}^0}{Z_{NaF}c_{Na}^0} dx = \frac{\int_0^\infty z_{CaF}c_{Ca}^0 dx}{\int_0^\infty z_{NaF}c_{Na}^0 dx}
\]  
(2)

where \(K_C\) is the selectivity coefficient determined by the Coulomb forces for Ca\(^{2+}\) and Na\(^+\) in cation-surface interactions; \(R\) is the gas constant \((J/mol\cdot K)\); \(T\) is temperature (K); \(F\) is the Faraday constant, \(Z\) is the charge number of cation species; \(\phi(x)\) is the potential at position \(x\) in the diffuse layer; \(S\) is the specific surface area; \(c_i(x)\) is the concentration of the \(i\)th cation species at \(x\); and \(1/\kappa\) is the effective thickness of the diffuse layer (or Debye length).

Liu et al. obtained the exact analytical solution of the non-linear Poisson-Boltzmann equation for 2:1 and 1:1 mixed electrolyte solutions\(^{39}\). From the analytical solution of \(\phi(x)\), we can get the following simple relationships under relatively high surface potential conditions \((\int_0^\infty |Z_i\phi_0| > 0.1V)\):

\[
\int_0^\infty e^{-Z_{CaF}\phi_0} dx = \sqrt{3 + \theta_{Na}/\phi_0} e^{-Z_{CaF}\phi_0}
\]

and

\[
\int_0^\infty e^{-Z_{NaF}\phi_0} dx = \sqrt{3 + \theta_{Na}/\phi_0} e^{-Z_{NaF}\phi_0}
\]

Thus Eq. 2 yields:

\[
K_C = e^{-Z_{CaF}/\kappa_0 - Z_{NaF}/\kappa_0}
\]  
(4)

Taking \(x = 1/\kappa\) to be the upper limit of the integrations in Eq. 2 (meaning \(\phi_{1/\kappa} \to 0\)), we thus have \(Z_iF\phi_0 = Z_iFk [\phi_0 - \phi_{1/\kappa}] (1/\kappa) = -Z_iFE(1/\kappa) = \bar{w}_i(C)\), where \(E = -\kappa [\phi_0 - \phi_{1/\kappa}]\) is the mean electric field strength in the diffuse layer, and \(\bar{w}_i(C)\) is the mean Coulomb potential energy of the \(i\)th cation species in the diffuse layer. Thus Eq. 3 can be expressed as:

\[
K_C = e^{-\phi_0Z_{CaF}/\kappa_0 - \phi_0Z_{NaF}/\kappa_0}
\]  
(5)

According to Eq. 5, it was the mean potential energies of cation species in the diffuse layer that determine the selectivity coefficient \(K_C\).

**Strong Hofmeister effects in Ca\(^{2+}\)/Na\(^+\) exchange.** If we consider Bolt\(^{s2}\) experimental results for Ca\(^{2+}\)/Na\(^+\)-illite exchange equilibria in a solution of NaCl and CaCl\(_2\), there are four relevant aspects: (1) the Ca\(^{2+}/Na^+\) exchange was determined under a wide range of electrolyte concentrations and ionic strengths \((0.0075 - 0.354\) mol/l\); (2) illite particle surfaces can be considered planer; (3) illite surface charges are constant and therefore the surface charge density is independent of pH and ionic strength; (4) the ionic radii of Ca\(^{2+}\) (0.099 nm) and Na\(^+\) (0.095 nm) are almost the same, but the hydration diameter of Ca\(^{2+}\) (0.52 nm) is much larger than that of Na\(^+\) (0.356 nm)\(^{41}\).

Bolt independently determined the surface charge density of illite \((0.2895\) C/m\(^2\)) by the negative adsorption method\(^{21}\). With the Poisson-Boltzmann equation of the mean force, the surface potentials can be estimated from the classical \(\sigma_0 \sim \phi_0\) relationship, where \(\sigma_0\) is surface charge density (C/m\(^2\)), and \(\phi_0\) is surface potential (V). The results were shown in Table 1. We note that ionic interaction energies in bulk solution would influence the distribution of cations in the diffuse double layer; therefore, we used activity instead of concentration for cation species in bulk solution, by using the modified Debye-Hückel equation\(^{42}\).

Using the data in Table 1, \(K_0 = a_{Na}N_{Ca}/a_{Ca}N_{Na}\) \((K_0\) is the experimentally determined \(K\)) and \(K_C\) (Eq. 5) values could be calculated. The values of \(\phi_0\) in Table 1 indicated that the condition \(\sum_i |Z_i\phi_0| > 0.1V\) was satisfied for all \(K_C\) calculations. In Figure 1, it could be seen that the \(K_0\) were higher than the \(K_C\), and the difference increased with surface potential. The difference clearly revealed Hofmeister effects and implied that there are additional adsorption forces other than Coulomb for cation adsorption in Ca\(^{2+}\)/Na\(^+\) exchange. Thus there are strong Hofmeister effects present in Ca\(^{2+}\)/Na\(^+\) exchange, which are strengthened by the increasing surface potential of illite particles.

**Strong Hofmeister effects in Ca\(^{2+}\)/Na\(^+\) exchange based on classical interaction forces.** The effect of dispersion forces. Equation 5 shows...
that selectivity coefficient $K$ is a function of mean potential energy of cation species in the diffuse layer. If dispersion forces were present, Eq. 5 becomes:

$$K_{C+D} = e^{-\frac{\tilde{w}_{(D)}^{i}}{kT}}$$

(6)

where $\tilde{w}_{(D)}^{i}$ was the mean dispersion energy of cation species $i$ in the diffuse layer; the selectivity coefficient $K_{C+D}$ is determined by both Coulomb and dispersion forces.

Considering $\tilde{w}_{(D)}^{i}$ is constant (independent from surface potential), and if the differences between $K_C$ and $K_E$ in Figure 1 come from dispersion forces, then $K_{C+D} = K_E$. From Eqs. 1, 5 and 6, we obtain:

$$\frac{K_E}{K_{C+D}} = e^{-\frac{\tilde{w}_{(D)}^{i} - \tilde{w}_{(D)}^{Na}}{kT}} = \text{constant} (> 1)$$

(7)

Figure 2 plots $K_E/K_C$ vs. $\varphi_0$, which is not constant. Therefore, the differences did not derive from the dispersion forces. The four red dots are $K_E/K_C$ values with very large values of $c_{Na}^{i}/c_{Ca}^{i}$ (red data in Table 1), and will be discussed below.

Only under relatively high electrolyte concentrations is the dispersion force expected to become significant. Therefore, as the electrolyte concentration decreases, the difference between $K_E$ and $K_C$ decreases, and at very low electrolyte concentrations, $K_E/K_C$ will approach 1. However, Figure 2 showed that for decreasing electrolyte concentration (increasing surface potential), the difference between $K_E$ and $K_C$ increased. Therefore, we conclude that strong Hofmeister effects in $Ca^{2+}/Na^{+}$ exchange did not derive from dispersion forces.

The same phenomena are also observed for enzyme activities in <0.2 mol/L solutions of LiCl, NaCl, and CsCl, and for $K^+/Na^+$, $K^+/Li^+$, $Na^+/Li^+$ and $Mg^{2+}/Na^+$ cation exchanges.

The effects of ionic size and hydration. If the hydration effect became important in exchange, it would certainly decrease the preference of $Ca^{2+}$ over $Na^+$ in the exchange since the hydration diameter for $Ca^{2+}$ (0.356 nm) is much larger than that for $Na^+$ (0.35 nm), and then $K_E/K_C < 1$. According to Yan Levin et al., the chaotropic $Na^+$ cation would be more likely adsorbed at particle surfaces, whereas the kosmotropic $Ca^{2+}$ cation would be more likely present in solution. This would decrease the preference of $Ca^{2+}$ over $Na^+$ in the

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**Table 1** | Surface potentials of illite particles for each exchange equilibrium (In the calculation of surface potential, the dielectric constant of water is 8.9 x 10^{-2} C^2/Jm)

| Concentration (×10^3 mol/l) | Activity (×10^3 mol/l) | √I (×10^3 mol/l) | $\alpha_{Na}/\alpha_{Ca}$ | Adsorbed (mmol/g) |
|-----------------------------|------------------------|------------------|---------------------------|-------------------|
| $c_{Na}$ | $c_{Ca}$ | $\alpha_{Na}$ | $\alpha_{Ca}$ | $\sqrt{I}$ | $\alpha_{Na}/\alpha_{Ca}$ | $N_{Na}$ | $N_{Ca}$ | $\varphi_0$ (V) (classical) |
| 0.7 | 0.2 | 0.672 | 0.17 | 36.05 | 3.955 | 0.0054 | 0.111 | -0.1520 |
| 1 | 0.2 | 0.956 | 0.167 | 40 | 5.724 | 0.01 | 0.105 | -0.1522 |
| 3.2 | 0.15 | 2.993 | 0.115 | 60.41 | 26.06 | 0.029 | 0.0985 | -0.1565 |
| 3.2 | 0.56 | 2.964 | 0.412 | 69.85 | 7.188 | 0.012 | 0.1005 | -0.1404 |
| 5.1 | 0.2 | 4.697 | 0.144 | 75.49 | 32.63 | 0.034 | 0.091 | -0.1533 |
| 6 | 1.3 | 5.396 | 0.85 | 99.49 | 6.344 | 0.015 | 0.104 | -0.1310 |
| 9 | 2.3 | 7.89 | 1.361 | 126.1 | 5.800 | 0.019 | 0.1 | -0.1249 |
| 29 | 0.8 | 24.31 | 0.395 | 177.2 | 61.54 | 0.077 | 0.07 | -0.1382 |
| 19 | 9 | 15.45 | 3.933 | 214.5 | 3.928 | 0.019 | 0.0985 | -0.1112 |
| 296 | 0.17 | 60.35 | 0.061 | 280.2 | 34.07 | 0.082 | 0.066 | -0.1245 |
| 95 | 6.8 | 70.57 | 2.071 | 339.7 | 34.07 | 0.084 | 0.064 | -0.1161 |
| 34 | 29.4 | 25.1 | 8.729 | 349.6 | 2.875 | 0.018 | 0.101 | -0.1009 |
| 138 | 0.5 | 100.3 | 0.14 | 373.5 | 718.0 | 0.176 | 0.0175 | -0.1347 |
| 170 | 0.79 | 120.5 | 0.2 | 415.2 | 603.6 | 0.175 | 0.0185 | -0.1301 |
| 238 | 1.1 | 161.8 | 0.235 | 491.2 | 688.9 | 0.17 | 0.017 | -0.1243 |
| 65 | 138 | 40.25 | 20.28 | 692.1 | 1.984 | 0.018 | 0.103 | -0.09010 |
| 296 | 103 | 177.2 | 13.24 | 777.8 | 13.38 | 0.085 | 0.0705 | -0.09245 |

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**Figure 1** | Comparison between calculated (----) and experimental data (●). $K_E$ is the experimental selectivity coefficient; $K_C$ is the calculated selectivity coefficient based on the classical theory.

**Figure 2** | $K_E/K_C$ vs. $\varphi_0$ (V).
Therefore, the hydration effect could not explain the Ca$^{2+}$ interactions between the ions and the surface. I, ionic size, ionic hydration volume, or hydration-adjusted dispersion exchange. One possible reason was that hydration and a hydration-related charge for Na$^+$ exchange because of the stronger dispersion and electrostatic forces per charge for Na$^+$ than that for Ca$^{2+}$, and $K_E/K_C < 1$. In Figure 2, however, $K_E/K_C > 1$ and is not constant vs. surface potential. Therefore, the hydration effect could not explain the Ca$^{2+}$/Na$^+$ exchange. One possible reason was that hydration and a hydration-related dispersion combination may be correct only in relatively weak external electric field conditions of air/water and solid/liquid interfaces. In the dos Santos and Yan Levin study, the surface charge density was merely 0.04–0.06 C/m$^2$. Moreover, only under relatively high electrolyte concentrations would the ionic size (including hydration diameter) effect become significant. Therefore, the difference between $K_E$ and $K_C$ should have decreased with electrolyte concentration, in contrast to Figure 1. Hence, the strong Hofmeister effects in Ca$^{2+}$/Na$^+$ exchange did not come from differences in the ionic size, ionic hydration volume, or hydration-adjusted dispersion interactions between the ions and the surface.

The effect of ionic induction force. Because increasing surface potential strengthened Hofmeister effects, they appear to be independent on dispersion forces, ionic sizes, and hydration effects. If it is the induction force in the electric field of the diffuse layer that was responsible for the large Hofmeister effects, then we have:

$$K_{C+1} = e^{-\frac{[\varphi_{\text{Na}^+} + \varphi_{\text{Ca}^{2+}}] - [\varphi_{\text{Na}^+} + \varphi_{\text{Ca}^{2+}}]}{2\varepsilon}}$$

where $\varphi_{\text{Ca}^{2+}}$ is the mean induction energy of cation species $i$ in the diffuse layer.

Assuming that the dipole orientation near the particle surface is co-directional and parallel with the field direction, then the classical mean induction energy (/mol) of Ca$^{2+}$ ($\varphi_{\text{Ca}^{2+}}$) and Na$^+$ ($\varphi_{\text{Na}^+}$) dipoles can be calculated by the classical equations, and:

$$\varphi_{\text{Ca}^{2+}} = \varphi_{\text{Na}^+} = - P_{\text{Ca}^{2+}} E = - P_{\text{Na}^+} E$$

Table 2 | The calculated $\varphi_0$, $\varphi_{1/\kappa}$, $\beta_{\text{Ca}^{2+}}$, and $\beta_{\text{Na}^+}$ values based on the experimental data

| Activity ($\times 10^4$ mol/l) | $a_{\text{Na}^+}$ | $a_{\text{Ca}^{2+}}$ | $a_{\text{Na}^+}/a_{\text{Ca}^{2+}}$ | $\varphi_0$ (new theory) | $\varphi_{1/\kappa}$ | $\beta_{\text{Ca}^{2+}}$ | $\beta_{\text{Na}^+}$ |
|-------------------------------|------------------|-----------------|----------------------|------------------------|-------------------|-----------------|------------------|
| 0.672                         | 0.17             | 3.953           | -0.1153              | -0.2091                | 1.320             | 0.800           |
| 0.956                         | 0.167            | 5.724           | -0.123               | -0.2215                | 1.235             | 0.765           |
| 2.993                         | 0.115            | 26.06           | -0.1206              | -0.2683                | 1.303             | 0.697           |
| 2.964                         | 0.412            | 7.188           | -0.1061              | -0.2225                | 1.328             | 0.672           |
| 4.697                         | 0.144            | 32.63           | -0.1166              | -0.02724               | 1.323             | 0.677           |
| 5.396                         | 0.851            | 6.344           | -0.1000              | -0.0216                | 1.314             | 0.686           |
| 7.893                         | 1.361            | 5.800           | -0.1003              | -0.02137               | 1.250             | 0.750           |
| 24.31                         | 0.395            | 61.54           | -0.1084              | -0.02801               | 1.302             | 0.698           |
| 15.45                         | 3.933            | 3.928           | -0.09014             | -0.01983               | 1.239             | 0.761           |
| 44.15                         | 1.121            | 39.39           | -0.08014             | -0.02654               | 1.244             | 0.756           |
| 60.35                         | 0.061            | 990.5           | -0.1250              | -0.03241               | 1.316             | 0.684           |
| 70.57                         | 2.071            | 34.07           | -0.09563             | -0.02550               | 1.250             | 0.750           |
| 25.1                          | 8.729            | 2.875           | -0.08082             | -0.01853               | 1.256             | 0.744           |
| 100.3                         | 0.17             | 718.0           | -0.1319              | -0.03171               | 1.276             | 0.724           |
| 120.5                         | 0.2              | 603.6           | -0.1158              | -0.03114               | 1.281             | 0.719           |
| 161.8                         | 0.235            | 688.9           | -0.1243              | -0.03220               | 1.250             | 0.750           |
| 40.25                         | 20.28            | 1.984           | -0.07356             | -0.01731               | 1.232             | 0.768           |
| 177.2                         | 13.24            | 13.38           | -0.08075             | -0.02176               | 1.177             | 0.823           |
theories on dispersion forces, induction forces, and hydration effects might be valid only when the external electric field is weak. In high electric fields \(>4.2 \times 10^6 \) V/m, however, it is possible that new interaction forces are present.

**The general origin of Hofmeister effects at the interface.** Because the differences between \(K_E\) and \(K_C\) sharply increase with surface potential, the unknown interaction force between the cations and the surface must be a function of the potential. Thus two parameters \(\beta_{Ca}\) and \(\beta_{Na}\) are introduced to modify the Coulomb interaction potential energies \((Zp\varphi)\) of \(Ca^{2+}\) and \(Na^+\). Eq. 4 can be changed to \(\beta^{*}\):

\[
K_{modified} = e^{-\frac{(z_{Ca} - z_{Na})\pi e}{\kappa xo_0}}
\]

Using the iteration approach suggested by Li et al.\(^{41}\), \(\beta_{Ca}\) and \(\beta_{Na}\) can be calculated. If \(\varphi_0\) is known, the potential at \(Z = 1/\kappa\) can also be calculated from the analytical solutions of the non-linear Poisson-Boltzmann equation for 1:1 and 2:1 electrolyte solutions. The calculated values of \(\varphi_0\), \(\varphi(1/\kappa)\), \(\beta_{Ca}\) and \(\beta_{Na}\) are in Table 2.

From Table 2, \(\beta_{Ca} > 1\) and \(\beta_{Na} < 1\), which implied that the unknown force for \(Ca^{2+}\) in cation-surface interactions was stronger than that for \(Na^+\). A comparison of surface potentials in Tables 1 and 2 also indicated that the unknown force decreased the surface potential significantly, perhaps because \(Ca^{2+}\) was more effective in screening than \(Na^+\).

We used Table 2 to examine \(\beta_{Ca}\) vs. \(\varphi(1/\kappa)/\varphi_0\) and \(\beta_{Na}\) vs. \(\varphi(1/\kappa)/\varphi_0\). It was surprising that these were unusual linear relationships (with relative error <0.3%):

\[
\begin{align*}
\beta_{Ca} &= 1 + 0.357 - 0.357 \frac{\varphi(1/\kappa)}{\varphi_0} \\
\beta_{Na} &= 1 - 0.357 + 0.357 \frac{\varphi(1/\kappa)}{\varphi_0}
\end{align*}
\]

They were unusual because the slopes were equal to the “1-intercept” for the two cation species. If a new induction force in cation-surface interactions was introduced, Eqs. 12 could be theoretically derived. We tentatively refer to the new surface-potential-dependent force as a non-classic induction force, because it can be explained by the enhanced polarizability in strong external electric field from surface charges of illite particle.

An illite surface charge density of 0.2895 C/m\(^2\) corresponds to an electric field strength of 4\(\times 10^6\) V/m (\(\varepsilon_{water} = 8.9 \times 10^{-2} C/\)m) at the surface. The high external electric field may non-classically and greatly enhance the dipole moments of the two cation species. The dipole moment of a cation species will be more strongly enhanced than others if it has a softer electron cloud and/or prefers to stay near surface of stronger electric field (e.g., a cation with a stronger electrostatic or dispersion force, and/or a chaotropic cation).

If the additional energies do come from the strong non-classic induction force, then:

\[
K_{C + Na} = e^{-\frac{\varphi(1/\kappa)}{\varphi_0}} = e^{-\frac{(z_{Ca} - z_{Na})\pi e}{\kappa xo_0}}
\]

where \(\varphi(1/\kappa)\) and \(\varphi_0\) are the strong non-classical induction energies (J/mol) in the adsorption phase of \(Ca^{2+}\) and \(Na^+\), respectively, which come from the strong polarization of the cations in the high electric field at the surface.

If the dipole orientation of the particle surface was co-directional and parallel with the high external electric field, the mean induction energies of \(Ca^{2+}\) and \(Na^+\) dipoles in the field are:

\[
\begin{align*}
\bar{w}_{Ca(NI)} &= -\bar{p}_{Ca(NI)} E = \bar{p}_{Ca(NI)} K [\varphi_0 - \varphi(1/\kappa)] \\
\bar{w}_{Na(NI)} &= -\bar{p}_{Na(NI)} E = \bar{p}_{Na(NI)} K [\varphi_0 - \varphi(1/\kappa)]
\end{align*}
\]

where \(\bar{p}_{Ca(NI)}\) and \(\bar{p}_{Na(NI)}\) are the mean dipole moments (dm·C/mol) of \(Ca^{2+}\) and \(Na^+\) in the diffuse layer, respectively.

Introducing Eq. 14 into Eq. 13:

\[
K_{C + Na} = e^{-\frac{(z_{Ca} - z_{Na})\pi e}{\kappa xo_0}} = e^{-\frac{(z_{Ca} - z_{Na})\pi e}{\kappa xo_0}}
\]

in which

\[
(Z_{Ca} - Z_{Na})F\varphi_0 + \bar{p}_{Ca(NI)} K [\varphi_0 - \varphi(1/\kappa)] - \bar{p}_{Na(NI)} K [\varphi_0 - \varphi(1/\kappa)]
\]

\[
= Z_{Ca} F\varphi_0 - Z_{Na} F\varphi_0 + \frac{(Z_{Ca} + Z_{Na})(\bar{p}_{Ca(NI)} - \bar{p}_{Na(NI)}) K \varphi_0}{Z_{Ca} + Z_{Na}}
\]

\[
= (Z_{Ca} + Z_{Na})(\bar{p}_{Ca(NI)} - \bar{p}_{Na(NI)}) K \varphi(1/\kappa)
\]

where \(a\) is constant, and \(a = \frac{1}{(Z_{Ca} + Z_{Na}) F k}\). From Eq. 16, we obtained:

\[
K_{C + Na} = e^{-\frac{(z_{Ca} - z_{Na})\pi e}{\kappa xo_0}} = e^{-\frac{(z_{Ca} - z_{Na})\pi e}{\kappa xo_0}}
\]

Comparing Eqs. 17 and 11, we have:

\[
\begin{align*}
\beta_{Ca} &= 1 + a D_{PN(I)} - a D_{PN(I)} K [\varphi(1/\kappa)] \\
\beta_{Na} &= 1 - a D_{PN(I)} + a D_{PN(I)} K [\varphi(1/\kappa)]
\end{align*}
\]

It is very interesting that the fitting equation Eq. 12 for the experimental data could be explained by the theoretical equation Eq. 18. There are several reasons why this is very interesting. The expressions Eq. 18 are the same as Eq. 12; Eq. 18 verifies that \(\beta_{Ca} + \beta_{Na} = 2\); Eq. 18 verifies the “slope = 1-intercept” in Eq. 12; and from Eqs. 18 and 12, \(aD = 0.357\).

By including the strong induction force, the relationship of \(K_{C + Na} \sim \varphi_0\) based on Eq. 17 (where \(a D_{PN(I)} = 0.357\)) fitted the experimental data very well, as shown in Figure 4. It is important to note that if we did not have the specific mathematical form of Eq. 18, the comparison with Eq. 12 could not have been done and the value of \(a D_{PN(I)} = 0.357\).

**Figure 4 | Comparison between theoretical curves of \(K_{C + Na}\) (—) and \(K_E\) (○).**
0.357 would not have been obtained. Therefore the $K_{Ca^+Na^+} \sim \phi_0$ relationship curve based on Eq. 17 is theoretical and not a fitting curve.

In summary, we have shown that a strong non-classic induction force of adsorbed ions in the electric field is the origin of the strong Hofmeister effects in Ca$^{2+}$/Na$^{+}$ exchange.

**Comparison of the strong non-classical and the classical induction energies.** From $a\Delta\tilde{p}_{(NI)} = 0.357$, we have $\kappa \cdot \Delta\tilde{p}_{(NI)} = 0.357 \times 3 \times F = 103337 \text{ C}$ for Ca$^{2+}$ and Na$^{+}$. The differences in the non-classical induction energies between Ca$^{2+}$ and Na$^{+}$ could be calculated from the Ca$^{2+}$/Na$^{+}$ exchange experiments. From Eq. 14, we have:

$$\tilde{w}_{\text{Ca}(NI)} - \tilde{w}_{\text{Na}(NI)} = \left( \tilde{p}_{\text{Ca}(NI)} - \tilde{p}_{\text{Na}(NI)} \right) \kappa \left[ 1 - \frac{\phi \left( \frac{1}{\kappa} \right)}{V_0} \right] V_0 \phi_0$$

$$= 3a\Delta\tilde{p}_{(NI)} \left[ 1 - \frac{\phi \left( \frac{1}{\kappa} \right)}{V_0} \right] F \phi_0$$

$$= 103337 [V_0 - \phi \left( \frac{1}{\kappa} \right)]$$

Thus the experimental values of $\tilde{w}_{\text{Ca}(NI)} - \tilde{w}_{\text{Na}(NI)}$ can be calculated with Eq. 19.

On the other hand, the surface-cation Coulomb force in such a high electric field would be much stronger than that for surface-water (surface hydration) and cation-water (cation hydration) interactions. As a result, the adsorbed cation near the surface might be to some degree dehydrated in the high electric field near the surface. In the extreme case of complete dehydration near the surface, we can use the intrinsic cation polarizability to calculate the dipole moment. Table 3 shows comparisons of $\Delta\tilde{p}$ and $\Delta\tilde{p}$ among the calculated results from cationic excess (Eqs. 9 and 10), the intrinsic polarizabil-

| $a_{\text{Na}}$ | $a_{\text{Ca}}$ | $\Delta w_{(C)}$ (J/mol) | $\Delta w_{(NI)}$ (J/mol) | $\Delta w_{(I)}$ (J/mol) | $\Delta \tilde{w}_{(NI)}$ (D) | $\Delta \tilde{p}_{(NI)}$ (D) | $\Delta \tilde{p}_{(I)}$ (D) |
|-----------------|-----------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| 0.672           | 0.17            | -11125                      | -9754.0                     | 0.054                       | -0.387                      | 448.6                       | -0.0018                     |
| 0.956           | 0.167           | -11906                      | -10463                      | 0.062                       | -0.440                      | 416.3                       | -0.0019                     |
| 2.993           | 0.115           | -11636                      | -9690.0                     | 0.162                       | -1.160                      | 300.5                       | -0.0032                     |
| 2.964           | 0.412           | -10237                      | -8664.9                     | 0.143                       | -1.027                      | 249.6                       | -0.0030                     |
| 4.977           | 0.144           | -11250                      | -9234.2                     | 0.239                       | -1.712                      | 244.0                       | -0.0038                     |
| 5.396           | 0.851           | -9684.7                     | -8101.7                     | 0.257                       | -1.839                      | 179.7                       | -0.0040                     |
| 7.893           | 1.361           | -8677.6                     | -8158.4                     | 0.295                       | -2.108                      | 145.5                       | -0.0043                     |
| 24.31           | 0.395           | -10459                      | -8307.3                     | 0.960                       | -6.872                      | 110.7                       | -0.0053                     |
| 15.45           | 3.933           | -8697.3                     | -7265.7                     | 0.513                       | -3.670                      | 93.59                       | -0.0056                     |
| 44.15           | 1.121           | -9889.9                     | -7849.5                     | 1.053                       | -7.539                      | 80.34                       | -0.0058                     |
| 60.35           | 0.061           | -12061                      | -9568.1                     | 2.360                       | -16.893                     | 73.11                       | -0.012                      |
| 70.57           | 2.071           | -9227.1                     | -7247.1                     | 1.950                       | -13.954                     | 62.90                       | -0.011                      |
| 25.1            | 8.729           | -7798.1                     | -6436.9                     | 0.641                       | -4.587                      | 66.65                       | -0.006                      |
| 100.3           | 0.14            | -11569                      | -9113.3                     | 2.860                       | -20.469                     | 56.61                       | -0.013                      |
| 120.5           | 0.2             | -11173                      | -8748.6                     | 3.170                       | -22.689                     | 51.57                       | -0.014                      |
| 161.8           | 0.235           | -11993                      | -9517.4                     | 4.970                       | -35.357                     | 44.60                       | -0.017                      |
| 40.25           | 20.28           | -7097.6                     | -5812.7                     | 1.242                       | -8.886                      | 46.27                       | -0.009                      |
| 177.2           | 13.24           | -7791.3                     | -6093.9                     | 5.064                       | -36.244                     | 36.05                       | -0.018                      |

Table 3 | Comparison of mean potential energies of cations in diffusion layer producing from Coulomb force, classical induction and non-classical forces respectively
From classical induction theories, $\Delta \rho_{(NI)}^a$ or $\Delta \rho_{(NI)}^p$ decrease with an increase in external electric field (low electrolyte concentration corresponding to high external electric field); and this is not correct because in the classic theories we used constant ionic polarizabilities $x_0^+$ and $x_0^-$ in different electric fields.

The comparison of the observed large non-classical induction energy and the calculated classical induction energy indicated that in a strong external electric field of $10^8$–$10^9$ V/m, the ionic polarizabilities $x_0^+$ and $x_0^-$ would be heavily underestimated by the classical induction theories, and that they would sharply increase with electric field strength (Table 3). Therefore, a new theory to calculate ionic polarization in strong electric fields is required; a successful theory for Hofmeister effects at solid/liquid interfaces should address the statistical mechanics of density fluctuations and their impact on solvent polarization.

There are high electric fields $>10^8$–$10^9$ V/m at the solid/liquid interfaces of clay, oxides, proteins, nanomaterials, and cell membranes. Therefore, the observed strong non-classical induction force will generally be the origin of Hofmeister effects at interface surfaces. In current treatments of Hofmeister effects, however, this important force has been ignored; thus they may be correct only for weak electric fields.

It should be noted that the dielectric constant of water for bulk solution was used in all of the calculations. If it is actually lower near a surface relative to that in the bulk, then the $\Delta \rho_{(NI)}$ values in Table 3 might be overestimated. Even if this was the case, it is unlikely to change the general conclusions of this study.

**An extended analysis of the strong non-classical induction force.**

Table 3 had very large $\Delta \rho_{(NI)}$ values, indicating that adsorbed ions in the electric field of the diffuse layer were strongly polarized. It also indicated that the polarization strength sharply increased with decreasing cation activity and that it was sensitive to the electric field strength in diffuse layer.

To demonstrate the effect of electric field strength in the diffuse layer on the polarization of adsorbed ions, we plotted $\Delta \rho_{(NI)}$ vs. $\phi_0$ in Figure 5.

Even though $\Delta \rho_{(NI)}$ generally increased with $\phi_0$, there was appreciable scatter in Figure 5. However, if the data were divided into three groups according to $d^a_{Na}/d^a_{Ca}$, the relationship of $\Delta \rho_{(NI)}$ vs. $\phi_0$ became more transparent: low values of $d^a_{Na}/d^a_{Ca}$ over the range 1–10; intermediate values over 10–100; and high values over 600–1000.

For low and intermediate values of $d^a_{Na}/d^a_{Ca}$ we found that $\Delta \rho_{(NI)} = P_{Ca(NI)} P_{Na(NI)}$ sharply increased with $\phi_0$. Since the electronic structures for Na$^+$ and Ca$^{2+}$ are, respectively, 1s$^2$2s$^2$2p$^6$ (with a static polarizability $\alpha_{Na} = 0.139 \, \text{Å}^3$) and 1s$^2$2s$^2$2p$^6$3s$^2$3p$^6$ (with a static polarizability $\alpha_{Ca} = 0.4692 \, \text{Å}^3$), the electronic cloud for Ca$^{2+}$ is "softer" than that for Na$^+$. Therefore, quantum fluctuations for Ca$^{2+}$ should be higher than those for Na$^+$. The observation that $\Delta \rho_{(NI)} = P_{Ca(NI)} P_{Na(NI)}$ sharply increased with $\phi_0$ indicated that the difference in random quantum fluctuation between Ca$^{2+}$ and Na$^+$ was strongly and directionally enhanced by the high external electric field.

At a constant surface potential $\phi_0$ (e.g., $-0.12 \, \text{V}$), $\Delta \rho_{(NI)} = P_{Ca(NI)} P_{Na(NI)}$ sharply decreased with increased $d^a_{Na}/d^a_{Ca}$. A larger $d^a_{Na}/d^a_{Ca}$ means more Na$^+$ could be distributed in the inner space of diffuse layer. The electric field was higher in the inner diffuse layer; thus, for larger $d^a_{Na}/d^a_{Ca}$, more Na$^+$ might have random quantum fluctuations directionally enhanced. As a result, $\Delta \rho_{(NI)} = P_{Ca(NI)} P_{Na(NI)}$ decreased.

Even with very high $d^a_{Na}/d^a_{Ca}$ ratios (e.g., 604–991), $\Delta \rho_{(NI)} = P_{Ca(NI)} P_{Na(NI)} > 0$, which implies a strong preference of the surface for Ca$^{2+}$ over Na$^+$. Three key factors will influence that preference: cation charge number (Coulomb force), cation flexibility (dispersion force), and hydration (chaotropic or kosmotropic). Even though Ca$^{2+}$ is kosmotropic and Na$^+$ is chaotropic, the charge number and flexibility of Ca$^{2+}$ are higher than that of Na$^+$, so the surface prefers Ca$^{2+}$ over Na$^+$. Therefore, Coulomb forces, dispersion forces, and hydration effects appeared to be interwined to influence cation distribution at the interface. In Levin theory, only hydration determines that preference.

The difference in quantum fluctuations between Ca$^{2+}$ and Na$^+$ could be strongly and directionally enhanced by the high external electric field that created enormous values of $P_{Ca(NI)} P_{Na(NI)}$. The complex combination of Coulomb, dispersion and hydration effects would also greatly affect the enhancement. In addition, the enhancement would decrease the external electric field because the additional strong non-classical induction force significantly concentrated the counter-ions in the near-surface region.

Similar to London-Lifshiz forces, quantum fluctuations might be the essential origin of the new force. However, unlike London-Lifshiz forces, the random quantum fluctuations might be strongly and directionally enhanced by the high external electric field. Therefore if the quantum fluctuation was the essential cause of the new force, the high electric field would be its external cause. Here, we tentatively refer to this new force as a non-classical induction force, but the induction concept could not exactly describe it. Therefore, we suggest that the new force might derive from the coupling of ionic quantum fluctuations and the high external electric field. The classic Coulomb forces, dispersion forces, ionic size, and hydration effects combine to determine the preference for ion to stay at a surface over others, thus affecting the coupling effect. This concept is schematic.
ally illustrated in Figure 6. We emphasize we are simply illustrating a possible explanation of the new force; a complete description about the nature of the new force is still required.

Conclusions

We have observed a strong non-classical induction force in cation-surface interactions. Hofmeister effects in general may derive from this force, and the results presented here may fundamentally challenge all related theories. Currently, it is believed that Derjaguin-Landau-Verwey-Overbeek theory and the double-layer theory are exact at low electrolyte concentrations; and at high concentrations, dispersion forces, ionic sizes and hydration effects must be taken into account for the explanation of Hofmeister effects. In contrast, our results indicate that the most important forces are not those classical interactions. Instead, they are the strong non-classical induction forces at high and especially at low concentrations for the explanation of Hofmeister effects. The classic Coulomb forces, dispersion forces, ionic size, and hydration effects appeared to be interwined in determining the preference for an ion species to stay at a surface over others, thus affecting the strong non-classical induction forces.

The strong non-classical induction force implies that the energies of non-valence electrons of ion species at the interface might be substantially understated, and that they may profoundly influence the physical and chemical properties of ions, atoms, and molecules. Therefore, to describe Hofmeister effects occurring at interfaces with high electric fields, a combined solution of Schrodinger’s equation and the Poisson-Boltzmann equation would be required, and that the energy produced by the field near the interface should be exactly included in the Hamilton operator.
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**Author contributions**

X.L. and H.L. performed the data analysis and modeling, and wrote the main manuscript text. R.L. prepared Table 1–3. J.N. and D.X. supervised the project. L.W. made a thoroughgoing revision of the manuscript. X.L. and H.L. contributed equally to this work. All authors reviewed the manuscript.

**Additional information**

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