Research on the Dynamic Compressive Deformation Behavior of 3D-Printed Ti6Al4V

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Abstract: In this paper, the plastic flow and fracture behavior of 3D-printed Ti6Al4V (TC-4) alloy under different temperatures (289–1073 K) and strain rates (0.1–4100 s⁻¹) were studied by using the MTS comprehensive experimental machine (MTS) and split Hopkinson pressure bar (SHPB) equipment. The patterns of the influence of temperature and strain rate on the plastic flow behavior of 3D-printed materials in different printing directions were analyzed and compared with those of the traditional TC-4. Based on the experimental data, the modified Johnson–Cook (J-C) constitutive model of 3D-printed TC-4 alloy was established, and the plastic deformation behavior of the material driven by detonation was studied by X-ray photography. The research results showed that under static loading conditions, the strength of the material (AM-P-TC-4) along the printing direction was much higher than the strength of the material perpendicular to the printing direction (AM-T-TC-4). However, there was no difference in material strength for different directions under dynamic loading. Second, under the same deformation conditions, the strength of the 3D-printed TC-4 alloy was considerably higher than that of the traditional TC-4 alloy, but adiabatic shear fracture could be more easily induced under dynamic compressive deformation conditions for the 3D-printed TC-4 alloy, and its fracture strain was substantially less than that of TC-4 alloys. The modified J-C constitutive model established in this paper could better describe the plastic flow behavior of the AM-P-TC-4 alloy under high temperature and high-strain rate deformation conditions.

Keywords: Ti6Al4V; additive manufacturing; dynamic mechanical properties; high temperature; high strain rate

1. Introduction

The titanium alloy Ti6Al4V, a typical α + β two-phase material, has several advantages, such as low density, high elastic modulus, high strength, and good corrosion resistance and processing performance, and it has been widely used in aerospace, vehicle engineering, shipbuilding, and defense [1,2]. Traditional Ti6Al4V (TC-4) alloy parts are usually prepared in the production process of forging and casting in combination with turning. However, for some large and complex components, the subtractive preparation process has issues of high costs, complex processes, low material utilization, and long processing cycle, which severely hinders the further application of this material in the industrial field. Additive manufacturing is a new industrial technology that emerged in the early 21st century. It mainly involves the use of laser technology to accumulate the spread powder materials layer by layer through computer control to obtain three-dimensional physical products [3]. The processing method adopted by 3D-printing technology is opposite to the traditional subtractive technology, and it can effectively solve production process problems in the manufacturing and preparation of some difficult-to-process, precious-metal and complex parts.

Ti-6Al-4V is a mature titanium alloy material widely used in various industrial fields. Numerous studies have been conducted on the mechanical properties of traditional Ti-
6Al-4V materials [4–8]. Nitin [4] studied the effect of heat treatment on the mechanical properties of Ti-6Al-4V at low strain rates. Lee [7] studied the plastic flow and fracture behavior of Ti-6Al-4V under dynamic deformation conditions using the split-Hopkinson pressure bar (SHPB) method. Thus far, there have been few studies on the mechanical properties of 3D-printed Ti-6Al-4V under dynamic deformation conditions. More studies have focused mainly on the effects of void defects and complex structures within the material on the macro-mechanical behavior of 3D-printed Ti-6Al-4V and the influence of the printing process on the static strength of the material [9–18]. Refael et al. [12,14] studied the effect of holes on the dynamic mechanical properties of 3D-printed Ti6Al4V alloy specimens through dynamic compression and tensile tests. Xiao et al. [16–18] used 3D-printing technology to prepare an open-cell rhombic dodecahedron Ti-6Al-4V lattice structure and studied the macro-mechanical response of this structure under dynamic and static compressive deformation conditions through a series of mechanical experiments. Numerous research data have shown that the strength of 3D-printed Ti-6Al-4V alloy is considerably higher than that of Ti-6Al-4V materials prepared by the traditional technology, but many voids and defects exist inside the 3D-printed Ti-6Al-4V alloy that have negative effects on the mechanical properties of the alloy.

To systematically study and predict the deformation behavior of 3D-printed Ti-6Al-4V materials under high-speed-impact conditions, selective laser melting 3D-printing technology was used in this study to prepare 3D-printed Ti-6Al-4V alloy plates, and the wire electrical discharge machining (WEDM) process was used to cut and obtain mechanical specimens from the longitudinal printing direction (AM-P-TC-4) and transverse printing direction (AM-T-TC-4) of the material. The mechanical response and fracture behavior of the 3D-printed TC-4 material in different printing directions were studied through quasi-static and dynamic compression tests under deformation at different temperatures (289–1073 K) and strain rates (0.1–4100 s\(^{-1}\)), and the results were compared with those of the Ti-6Al-4V alloy (TC-4) prepared via the traditional process. Moreover, based on experimental data, a modified Johnson–Cook (J-C) constitutive model that could predict the dynamic plastic deformation behavior of AM-P-TC-4 and TC-4 was established. Finally, a comparative study of the detonation-driving plastic deformation behaviors of AM-P-TC-4 and TC-4 was performed using a shaped-charge jet warhead.

2. Materials and Test Methods

2.1. Materials

TC-4 (Ti-6Al-4V) produced by the Northwest Institute for Nonferrous Metal Research was used as the traditional forged titanium alloy, and the additively manufactured titanium alloy was prepared based on the selective laser melting (SLM) process. The chemical compositions of the two materials are presented in Table 1. The TC-4 spherical powder for additive manufacturing had a particle size of 15–53 \(\mu\)m.

| Material     | Composition (wt.%): Al | V | O  | Fe | Ti   |
|--------------|------------------------|---|----|----|------|
| TC-4         | 6.30                   | 4.10 | <0.14 | <0.14 | Balance |
| AM-TC-4      | 6.13                   | 4.00 | <0.15 | <0.25 | Balance |

The SLM equipment was developed in-house as shown in Figure 1. A fiber laser with its wavelength at 1070 nm and a maximum power of 500 W was used. The laser spot size on the surface of the powder bed is about 100 \(\mu\)m. To prevent the metal powder from being oxidized during the manufacturing process, argon was used as the protective gas, and the oxygen content was constantly maintained at below 100 ppm (parts per million) during the manufacturing process. A laser power of 340 W, scan speed of 1250 mm/s, and layer thickness of 60 \(\mu\)m were used to produce the samples. The powder bed was heated to
a temperature of 100 °C to reduce the thermal deformation of the samples. The process parameters are presented in Table 2, and the dimensions of the additively manufactured sample were 40 mm × 40 mm × 4 mm. After the additive manufacturing was complete, the sample was subjected to annealing heat treatment (the environmental temperature was raised to 800 °C for 60 min and held for 2 h, followed by air cooling). The final sample after machining is shown in Figure 2. The Leica MC170HD inverted-phase metallographic microscope (Leica, Berlin, Germany) was used to observe the microstructure of the sample under magnifications of 50× and 500×. As shown in the Figure 3, no holes and defects were observed within the microstructure.

Table 2. Selective laser melting process parameters.

| Parameter       | Values  |
|-----------------|---------|
| Laser Power     | 340 W   |
| Scan Speed      | 1250 mm/s |
| Layer Thickness | 60 μm   |

Figure 1. In-house selective laser melting equipment LAS300 with fiber laser.

Figure 2. Additively manufactured TC-4 specimens.
To study the compressive deformation behavior of the final prepared AM-TC-4 alloy and the difference in mechanical properties between this material and the TC-4 alloy prepared via the traditional manufacturing process, the AM-TC-4 alloy and TC-4 alloy specimens (diameter D = 4 mm and thickness L = 2 mm) were prepared via the WEDM process. Among them, AM-TC-4 was sampled along the longitudinal printing direction (AM-P-TC-4) and transverse printing direction (AM-T-TC-4) to study the difference in the mechanical properties of AM-TC-4 in different printing directions; the sampling method is illustrated in Figure 4. Furthermore, the mechanical properties of the two materials under quasi-static and dynamic compressive deformation conditions were studied through the Material Universal Testing Machine (MUTM) and SHPB testing equipment (Figure 5). Specifically, the MUTM was used to compress the two materials at a constant strain rate and 286 K. In the test, the crosshead speeds were 1.2 mm/min and 12 mm/min. An extensometer was used to record the load-deformation relationship during the specimen deformation. The engineering stress–engineering strain and strain rate $\dot{\varepsilon}$ of the specimen were calculated using Equations (1)–(3):

$$\sigma_e = \frac{f}{A_s} \tag{1}$$

$$\varepsilon_e = \frac{\varepsilon}{t} \tag{2}$$

$$\dot{\varepsilon}^* = \frac{V}{T} \tag{3}$$

where $\sigma_e$ is the engineering stress, $\varepsilon_e$ is the engineering strain, $A_s$ is the initial cross-sectional area of the specimen, and $t$ is the deformation. According to the assumption of constant volume, the $\sigma_t$ and $\varepsilon_t$ of the specimen were calculated using Equations (4) and (5).

$$\sigma_t = \sigma_e (1 - \varepsilon_e) \tag{4}$$

$$\varepsilon_t = -\ln(1 - \varepsilon_e) \tag{5}$$

The SHPB equipment was used to study the dynamic compressive deformation behavior of materials under high-temperature and high-strain rate conditions. The selection of mechanical sample size reduces the influence of the inertia effect and stress imbalance on the test data as much as possible [19]. At the same time, in order to eliminate the influence of end face friction on the test results, MoS$_2$ was used as lubricant in the experiment. Figure 5b shows a schematic diagram of the SHPB test device, in which the rod material was 18Ni with 14.5 mm diameter, the bullet length was 400 mm, and the lengths of the incident rod and the transmission rod were 1300 mm; the strain gauges were installed in the middle of the incident rod and the transmission rod.

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{figure3.png}
\caption{Microstructure of 3D-printed specimen: (a) 50×; (b) 500×.}
\end{figure}
strain rate $\dot{\varepsilon}$ of the material during the deformation process were calculated according to the strain signals obtained by the strain gauges on the incident rod and the transmission rod. The equations were as follows:

$$\sigma(t) = \frac{A_b E}{A_s} \varepsilon_{tr}(t)$$  \hspace{2cm} (6)

$$\dot{\varepsilon}(t) = -\frac{2C_b}{l_s} \varepsilon_{re}(t)$$  \hspace{2cm} (7)

$$\varepsilon(t) = \int_0^t \dot{\varepsilon}(t) dt$$  \hspace{2cm} (8)

where $A_b$ is the cross-sectional area of the rod; $l_s$ is the length of the specimen; $\varepsilon_{re}$ and $\varepsilon_{tr}$ are the signals of the incident rod and the transmitted rod, respectively; and $E$ and $C_b$ are the elastic modulus and elastic wave velocity of the rod, respectively. According to Equations (4) and (5), the true stress $\sigma_t$ and true strain $\varepsilon_t$ corresponding to the specimen were calculated.

![Transverse specimens](image1)

![Longitudinal specimens](image2)

**Figure 4.** Sampling method of mechanical specimens.

![Mechanical test equipment](image3)

**Figure 5.** Mechanical test equipment: (a) MTS universal testing machine; (b) SHPB test equipment.
In the SHPB test, it is very important to ensure the stress balance and constant strain rate deformation of materials. Figure 6a,b were, respectively, the waveform diagram and the variation law of stress and strain rate with the strain of the 3D-printed TC-4 material under the deformation conditions of temperature 289 K and strain rate 1200 s\(^{-1}\). According to Figure 6a, the rise time of the incident wave loading section in the experiment is \( T = 16.6 \) μs. The longitudinal wave depth of the TC-4 material was about 5130 m/s. When the loading force of the incident wave on the specimen reached the maximum, the stress wave repeatedly propagated in the specimen about 42 times. Therefore, it could be considered that the stress balance was reached everywhere in the specimen before plastic deformation.

![Figure 6](image)

**Figure 6.** Stress balance and constant strain rate deformation (AM-P-TC-4, 289 K, 1200 s\(^{-1}\)): (a) Waveform, (b) data selection.

In addition, as shown in Figure 6b, in the experiment, a constant deformation strain rate during plastic deformation was ensured. In the process of data processing, only the stress–strain relationship in the constant strain rate deformation range was selected for the next analysis and research, which also reduced the influence of the inertia effect on the accuracy of the test results.

3. Test Results and Discussion

3.1. Stress–Strain Relationship

Using MTS and SHPB test devices, the relationships between the equivalent plastic strain \( (\varepsilon_p) \) and the equivalent stress \( (\sigma) \) for TC-4 and AM-P-TC-4 specimens in the temperature range of 286–1073 K and strain rate of 0.1–4100 s\(^{-1}\) were obtained. With the stress value corresponding to the total strain of 0.05 as the apparent yield strength \( (\varepsilon_Y) \) of the material [20,21], Figure 7 is the schematic diagram of yield point selection. Moreover, the stress–strain relationship of the AM-T-TC-4 specimen at room temperature and a strain rate of 0.1–4100 s\(^{-1}\) were obtained. The results are shown in Figure 8.

![Figure 7](image)

**Figure 7.** Selection of yield point.
Figure 8. Stress–strain relationship of materials (a,c,e) stress–strain curves of TC-4, AM-P-TC-4, and AM-T-TC-4 at 286 K, respectively; (b,d) stress–strain curves of TC-4 and AM-P-TC-4 in high-temperature (473–1073 K) environment.

In addition, 50 TC-4 mechanical samples, 40 AM-P-TC4 samples, and 20 AM-T-TC4 samples were prepared, respectively, and three effective repeated tests were carried out for each deformation condition, and the test data within the constant strain rate range were averaged to ensure the reliability of the data. Figure 8a,b show the $\varepsilon_p - \sigma$ relationship of the TC-4 material prepared via the traditional process under normal-temperature (286 K) and high-temperature (473–1073 K) compressive deformation conditions. Figure 8c,b show the $\varepsilon_p - \sigma$ relationships of AM-P-TC-4 specimens under compressive deformation conditions at room temperature (286 K) and high temperature (473–1073 K), respectively. Figure 8e shows the $\varepsilon_p - \sigma$ relationship of the AM-T-TC-4 specimen under compressive deformation conditions at room temperature (286 K). According to the data in the figure, both materials exhibited certain work hardening and strain rate strengthening effects. The yield strength of the material increased with increasing strain rate, and the flow stress ($\varepsilon > \varepsilon_p$) of the material increased with increasing plastic strain. Moreover, as the environmental temperature increased, the yield strength and flow stress of the material...
gradually decreased. In addition, under dynamic deformation, the heat generated by the material deformation could not be immediately transferred outward, so that the material temperature gradually increased with increasing deformation. Therefore, under high-strain rate deformation, the thermal softening effect reduced the slope of the material stress–strain curve. An additional analysis was performed on the influences of temperature and strain rate on the yield strength and fracture behavior of materials based on the experimental data in Figure 8.

3.2. Effect of Strain Rate on Strength

Figure 9a shows the difference in the yield strength of the 3D-printed TC-4 titanium alloy in the longitudinal and transverse printing directions and the effect of deformation strain rate on the yield strength. The analysis showed that the yield strength of the specimens (AM-T-TC-4) obtained perpendicular to the printing direction under quasi-static deformation conditions (0.1–1 s⁻¹) was between 1240 and 1278 MPa, while the yield strength of the specimen (AM-P-TC-4) obtained along the printing direction was between 1379 and 1434 MPa, and the yield strength was 12% higher than that of AM-T-TC-4. However, as the deformation strain rate increased, the difference in the yield strength of the materials in the two directions gradually decreased; that is, under the condition of dynamic compressive deformation, the compression yield strength of 3D-printed TC-4 in different directions tended to be consistent.

![Figure 9a](image1)

**Figure 9a.** Effect of strain rate on the yield strength of materials: (a) Effect of strain rate on the yield strengths of TC-4, AM-P-TC-4, and AM-T-TC-4 at room temperature; (b) effect of strain rate on the yield strengths of TC-4 and AM-P-TC-4 at different temperatures.

3.3. Effect of Temperature on Strength

Figure 10 shows the relationship between the yield stress of TC-4 and AM-TC-4 materials and the initial environmental temperature under different strain rates. In the temperature range of 289–1073 K, the yield strength of the two materials decreased linearly with increasing environmental temperature. Second, the high-temperature strength of AM-P-TC-4 was also greatly higher than that of TC-4. At a strain rate of 2500 s⁻¹, the initial environmental temperature increased from 289 K to 1073 K, and the yield strength of TC-4 material decreased from 1370.9 MPa to 853.5 MPa, a decrease of about 37.7%. Under the same conditions, the yield strength of the AM-P-TC-4 material decreased from 1557.9 MPa to 1099.7 MPa, a decrease of about 29.4%. It can be seen that the thermal sensitivity of AM-P-TC-4 was lower than that of the TC-4 material; that is, AM-P-TC-4 had higher strength and relatively better thermal stability at high temperatures.

![Figure 10](image2)
Figure 9b shows the yield stress of TC-4 and AM-P-TC-4 materials at different strain rates under different initial environmental temperatures. From the data in the figure, the yield strength of the two materials in the strain rate range of 0.1–4000 s\(^{-1}\) increased linearly with increasing strain rate. In addition, under the same deformation conditions, the yield strength of AM-P-TC-4 was considerably higher than that of the traditional TC-4 material, but the strength of the traditional TC-4 material was more sensitive to the change in strain rate. At the initial environmental temperature of 289 K, the strain rate increased from 0.1 s\(^{-1}\) to 4100 s\(^{-1}\), the yield strength of TC-4 increased from 1122.8 MPa to 1492.2 MPa, and the gain was about 28.6%. Under the same conditions, the yield strength of the AM-P-TC-4 material increased from 1379.1 MPa to 1644.2 MPa, with a gain of about 19.2%. Moreover, under the conditions of a temperature of 289 K and a strain rate of 0.1 s\(^{-1}\), the yield strength of AM-P-TC-4 was 22.8% higher than that of TC-4.

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![Figure 10. Relationship between material yield strength and initial environment temperature.](image)

### 3.4. Fracture Behavior

The above sections focus on the effects of strain rate and temperature on the yield strengths of TC-4, AM-P-TC-4, and AM-T-TC-4 under dynamic compression conditions. The results showed the following: Compared with the traditional TC-4 material, the TC-4 titanium alloy material prepared by additive manufacturing had higher strength under the same deformation conditions. It was found in the experiment that when the material strain accumulated to a certain degree or the deformation strain rate was higher than a certain value, the titanium alloy material would undergo shear fracture during the deformation process. Studies have shown that the fracture behavior of titanium alloy materials is also affected by strain rate and temperature [22,23]. Titanium alloys are prone to adiabatic shear behavior under dynamic impact. As the strain rate increases, the material will produce more adiabatic shear bands and induce the localization of deformation, which makes the material more likely to fracture [23–25]. Therefore, we analyzed the fracture behaviors of TC-4, AM-P-TC-4, and AM-T-TC-4 under dynamic compressive deformation conditions.
Figure 11a–c show the transmission voltage signals of TC-4, AM-P-TC-4, and AM-T-TC-4 under impacts of different strain rates, obtained by SHPB test. According to Equation (6), the transmission voltage signal is positively correlated with the deformation stress of the material. When the material breaks during the stress wave loading process, stress unloading occurs inside the material, which causes the transmission voltage signal to drop sharply in the first loading cycle. As the broken material is further compacted, the subsequent voltage signal rises again. The first inflection point at which the voltage signal appears to fall is taken as the time $t_f$ when the material breaks during the deformation process. The strain $\varepsilon_f$ when the material breaks can be roughly estimated by Equation (9).

$$\varepsilon_f \cong \int_0^{t_f} \varepsilon dt$$

Figure 12 shows the corresponding relationship between the maximum strain of the three materials TC-4, AM-P-TC-4, and AM-T-TC-4 (calculated according to Equation (9)) in the first loading cycle under normal temperature conditions and the deformation strain rate, and the deformation state of the corresponding specimen. Compared with the traditional TC-4 material, the TC-4 titanium alloy material prepared via the 3D-printing process was more prone to fracture due to adiabatic shear under the same deformation conditions. In addition, the maximum fracture strain of the material in different printing directions was also different. Under a strain rate of 2500 s$^{-1}$, the fracture strain of the trad-
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Figure 13 shows the effect of temperature on the fracture behaviors of TC-4 and AM-P-TC-4. Under a strain rate of 2500 s\(^{-1}\), the adiabatic shear fracture behavior of the TC-4 material was suppressed with increasing initial environmental temperature, and its fracture strain gradually increased. When the initial environmental temperature increased to 673 K, the fracture phenomenon of the TC-4 material in the first loading cycle disappeared. However, the fracture behavior of the AM-P-TC-4 material prepared via additive manufacturing was not significantly improved with an increase in the initial environmental temperature.
3.5. Constitutive Relations

The above sections describe the plastic deformation and fracture behavior of TC-4 and 3D-printed TC-4 titanium alloy in the temperature range of 289–873 K and strain rate of 0.1–4100 s\(^{-1}\). The preliminary results showed that the TC-4 material prepared by additive manufacturing had higher strength than the traditionally prepared TC-4 material. However, TC-4 materials prepared by additive manufacturing processes under dynamic deformation conditions are more prone to the localization of deformation caused by adiabatic shear.

In 1983, Johnson and Cook [26] proposed a constitutive model (J-C constitutive) suitable for describing the stress–strain relationship of metallic materials under high-temperature, high-strain rate, and large deformation conditions. The model comprehensively considers the impacts of strain rate effects and temperature on flow stress. The model equation is as follows:

\[
\sigma = \left( A + B\varepsilon_p^m \right) \left( 1 + C \ln\varepsilon^* \right) \left( 1 - T^* m \right) \tag{10}
\]

where \( A, B, n, C, \) and \( m \) are the material constitutive parameters to be determined; \( \varepsilon^* = \frac{\varepsilon^s}{\varepsilon_0} \) (\( \varepsilon_0 \) is the reference strain rate); and \( T^* = \frac{(T - T_r)}{(T_m - T_r)} \), where \( T_r \) is the reference temperature, and \( T_m \) is the material melting point.

Under the reference temperature and the reference strain rate, Equation (11) is used by the J-C constitutive to describe the relationship between the yield strength of the material and the strain rate; that is, when the plastic strain \( \varepsilon_p = 0 \), Equation (10) can be simplified as

\[
\sigma_{0.2} = A \left( 1 + C \ln\varepsilon^* \right) \tag{11}
\]

However, within the strain rate range of 0.01–4100 s\(^{-1}\), the strain rate strengthening behaviors of the TC-4 and AM-P-TC-4 materials used in this study were nonlinear (Figure 14), and the J-C model apparently could not effectively describe the behavior of the materials. Huh and Kang [27] replaced the linear form of the J-C constitutive with a one-variable quadratic form (Equation (12)) considering strain rate-related terms, as shown in Figure 14. Compared with the J-C constitutive, the strain rate-related items proposed by Huh and Kang showed a better correlation with the test data. Therefore, the second term in the J-C constitutive was modified. Equation (12) was used to describe the strain rate strengthening behavior of the two materials, and the modified constitutive form is shown in Equation (13).

\[
\sigma_{0.2} = A \left( 1 + C_1 \ln\varepsilon^* + C_2 \ln\varepsilon^{*2} \right) \tag{12}
\]

\[
\sigma = \left( A + B\varepsilon_p^m \right) \left( 1 + C \ln\varepsilon^* + C_2 \ln\varepsilon^{*2} \right) \left( 1 - T^* m \right) \tag{13}
\]

![Figure 14. Cont.](image-url)
The stress–plastic strain data at the reference temperature $T_r$ and the reference strain rate $\dot{\varepsilon}_0$ were used to determine the parameters $A$ and $B$. The functional relationship of $\sigma_{0.2} - \ln(\dot{\varepsilon}^*)$ at different reference temperatures and strain rates was used to determine $C_1$ and $C_2$. The function relationship of $\ln(1 - \frac{\sigma_{0.2}}{A}) - \ln(T^*)$ at a reference strain rate and different environmental temperatures was used to determine the parameter $m$. Finally, the stress–plastic strain data at different temperatures and different strain rates obtained in the experiment were used to conduct the least-squares optimization for the obtained initial values of the material parameters, and the final constitutive parameters were obtained (Table 3).

Considering the temperature rise of metallic materials due to adiabatic deformation under dynamic conditions [28], the constitutive parameters in Table 3 were used to predict the equivalent stress–equivalent plastic strain data of the two materials at different initial and different strain rates, and the results were compared with experimental data. Figure 15 shows that the modified J-C constitutive model constructed in this paper could effectively predict the mechanical responses of TC-4 and AM-P-TC-4 under high-temperature and high-strain rate deformation conditions, and the experimental data were consistent with the predicted data.

Table 3. Constitutive parameters.

| Description                        | Notations | Values          |
|------------------------------------|-----------|-----------------|
| Density                            | $\rho$ (g/cm$^3$) | 4.459  | 4.120  |
| Yield stress constant              | $A$ (Mpa)  | 1357.2 | 1480.3 |
| Strain hardening constant          | $B$ (Mpa)  | 303.15 | 480.3  |
| Strain rate hardening constant     | $n$        | 0.686  | 0.465  |
| Strain rate hardening constant     | $C_1$      | 0.0519 | 0.0217 |
| Strain rate hardening constant     | $C_2$      | 0.0116 | 0.018  |
| Thermal softening constant         | $m$        | 1.17   | 1.15   |
| Reference strain rate              | $\dot{\varepsilon}_0$ (s$^{-1}$) | 1500   | 1200   |
| Melting temperature                | $T_m$ (K)  | 2110   | 2110   |
| Reference temperature              | $T_r$ (K)  | 289    | 289    |

Figure 14. Strain rate strengthening behaviors of (a) TC-4 and (b) AM-P-TC-4.
3.6. Plastic Deformation Behavior under Extreme Conditions

The previous sections have described the use of the SHPB test to study the temperature (289–1073 K) and strain rate (0.1–4100 s\(^{-1}\)) to systematically analyze the plastic deformation behavior of 3D-printed TC-4 titanium alloy material, and the results have been compared with the traditionally prepared TC-4 titanium alloy. To explore the plastic deformation behavior of the 3D-printed TC-4 material under higher-strain rate conditions, the shaped-charge warhead was used to study the plastic deformation behavior of the 3D-printed TC-4 under more extreme deformation conditions and the difference between this material and the traditional TC-4 materials. The TC-4 and AM-P-TC-4 were separately used as liner materials in the shaped-charge warheads, and the pressure generated by the explosive detonation was up to 30 GPa; the pressure drives the liner materials to collapse and converge inward, thereby forming a high-speed metal jet that moves forward. The deformation strain rate of the material in the whole process was as high as \(10^5\) s\(^{-1}\). Additionally, X-ray photography was used to take images of the jet shape at a specific time after detonation, so that comparative study could be performed on the shaping forms of the rod-shaped jets of TC-4 and AM-P-TC-4 liner materials under the detonation-driving action. Figure 16a shows a schematic diagram of the structure of the shaped-charge warhead used in this study, and Figure 16b shows the images of the shaped-charge warhead prepared with TC-4.
and AM-P-TC-4 titanium alloy as the liner material. For the shaped-charge warhead and X-ray photography experiment, more descriptions can be found in reference [29].

![AM-P-TC-4 and TC-4](image)

**Figure 16.** Shaped-charge warheads: (a) TC-4 and AM-P-TC-4 warheads; (b) structure diagram of shaped-charge warhead.

Table 4 presents the shaping forms, obtained by X-ray photography, of the jets of TC-4 and AM-P-TC-4 liner materials under the driving action of detonation pressure. According to the movement distance of the jet between the two images, the head and tail velocities of the TC-4 jet were 8383 m/s and 2525 m/s, respectively. The head and tail velocities of the AM-P-TC-4 jet were 8185 m/s and 2438 m/s, respectively. Furthermore, the titanium alloy liner collapsed inward under the driving action of high pressure, and converged on the axis, thus forming a high-speed long-rod-shaped jet. However, due to the large velocity difference between the head and tail of the jet, the jet would break during subsequent flights. Compared with the TC-4 material, the jet head formed by the AM-P-TC-4 liner material possessed worse cohesiveness and showed significant expansion and spreading trends during the stretching and forming process.

The results of mechanical tests show that the fracture strain of AM-P-TC-4 material was obviously less than that of TC-4 under the same deformation conditions. At the same time, the increase of ambient temperature did not lead to a significant increase of fracture strain of AM-P-TC-4 material. It led to more severe fracture and breaking behavior of AM-P-TC-4 jet driven by detonation compared to TC-4.

**Table 4.** Comparison of shape-forming of TC-4 and AM-TC-4 jets.

| Liner     | Time (μs) | Jet Pattern |
|-----------|-----------|-------------|
| TC-4      | 40        | ![Jet Pattern](image) |
|           | 60        | ![Jet Pattern](image) |
| AM-P-TC-4 | 40        | ![Jet Pattern](image) |
|           | 60        | ![Jet Pattern](image) |
4. Conclusions

In this study, the Ti6Al4V alloy was prepared based on the selective laser melting 3D-printing process, and the MTS material universal testing machine and SHPB test equipment were used to study the mechanical properties of 3D-printed Ti6Al4V alloy and traditionally prepared Ti6Al4V alloy (TC-4) under high-temperature (289–1073 K) and high-strain rate (0.1–4100 s$^{-1}$) compressive deformation conditions. The mechanical properties of the 3D-printed TC-4 alloy (AM-P-TC-4 and AM-T-TC-4) in different printing directions were compared and investigated. The effects of temperature and strain rate on the material strength and fracture behavior were analyzed, and a modified J-C constitutive model of AM-P-TC-4 and TC-4 was established. Finally, the plastic deformation behavior of AM-P-TC-4 and TC-4 materials driven by detonation was studied through a shaped-charge jet warhead. The research results indicate the following:

1. The TC-4 alloy prepared via 3D printing had higher strength than the traditional TC-4 alloy. However, the 3D-printed TC-4 alloy was more prone to adiabatic shear fracture under dynamic compressive deformation conditions.

2. The TC-4 alloy prepared via 3D-printing technology exhibited certain differences in material properties in different printing directions. The material sampled longitudinally along the printing direction under static conditions had higher strength than the material sampled transversely, but the difference was smaller under dynamic deformation conditions.

3. The established modified J-C constitutive model could effectively describe the stress–strain relationship of the AM-P-TC-4 material under dynamic compressive deformation.

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