Countering the Deleterious Effects of Electromagnetic Pulse

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Robot systems like automated shipping swinging robots, wire transducer sensors and even computer indigenous time sensors (amongst others) often use oscillating circuits such as the famous van der Pol system, while this manuscript investigates protection of such sensor circuitry to spurious voltage spikes accompanying an electromagnetic pulse. These spurious voltages can lead to uncontrolled robot motion and even debilitation. A very brief discussion of electromagnetic pulses yields design parameters to evaluate circuit responses to realistic disturbing pulses. Recent research in nonlinear-adaptive methods to protect circuits are described to highlight the proposed novelty: utilization of feedback rules as adaptive mechanisms to modify the otherwise nonlinear feedforwards systems improving the results in recent literature. Feedback is iterated to select adaption parameters that simultaneously produce favorable circuit performance in addition to effective parameter identification inherent in the adaption (to provide meaningful parameter estimates to unspecified future applications). Spurious voltages were rapidly rejected with a mere 0.3% trajectory deviation, stabilizing quickly with a final (steady state) deviation of 0.01%. The demonstrated abilities to reject the deleterious spurious effects are compared to nominal figures of merit for timing accuracy of various computer systems to conclude the proposed methods are effective for some applications, but insufficient for others.

Keywords: control theory, learning systems, intelligent control systems, sensors and signal processing, robotics and applications, interpretation of sensor data, sensor electronics, robustness to electromagnetic pulse

INTRODUCTION

Robotic systems often use the chaotic van der Pol oscillator. Dutra et al. (2003) and Naoki et al. (2008a) and Roy and Demiris (2005) each articulate van der Pol used for bipedal locomotor robotics, where the implementation in (Naoki et al., 2008b) regards myriapod robots. Veskos and Demiris (2005) illustrates utilization of the van der Pol equation for swinging robots. Jasni et al. (2012) illustration van der Pol manifest as central pattern generation for quadrupled robots. Amongst the ubiquitous robotic applications of the chaotic, nonlinear van der Pol equation, this manuscript will select robotic computer systems’ indigenous timing circuits to evaluate the efficacy of the proposed methods and comparison will be made to typical capabilities of computers-usage to discern practical applicability of the achieved robustness performance. The IEEE-1588 precision timing-protocols (PTP) are a proven technology that synchronizes the internal clocks of PTP-enabled Ethernet devices such as robots, control systems, and components to create synchronized, systemwide timestamps (Harris, 2021a) The protocol is also used for time synchronization in modular collaborative robots (Gutiérrez et al., 2018). The most common way to sync robot time is with the Network Time Protocol (NTP) (David, 2014). The impact on these protocols and devices and others will be evaluated with imposition of electromagnetic pulse.
This section introduces electromagnetic pulse and very briefly describes the factors influencing the resulting voltages on distant systems and subsequently studies adaptive methods to protect electronic system timing circuits from the deleterious effects of the voltage imposition. The description of electromagnetic pulse (Electromagnetic Pulse) is intentionally abbreviated to emphasize the proposed methods to counter the resultant deleterious effects. The effects will manifest as displaced circuit timing and the displacement will be compared to figures of merit presented in Results for the aforementioned devices and protocols to ascertain the ability to continue operations despite the imposition of electromagnetic pulse.

**Electromagnetic Pulse**

Electromagnetic pulses are produced in lightning events and in nuclear detonations (Nanevicz et al., 2021). Reference (Nanevicz et al., 2021) and (Rabinowitz, 1986) describe the various kinds of electromagnetic pulse, while (Zhou et al., 2019) elaborates on effects of lighting-induced electromagnetic pulse on Korean power systems. This manuscript investigates mitigation of any investigated effects of electromagnetic pulse on Korean power systems. This manuscript investigates mitigation of any application utilizing a certain class of electronics.

Electromagnetic pulse as often characterized by relatively slow (lasting \( \leq 102 \) s) pulse called magnetohydrodynamic (with energies \( E \leq 10^{-1} \) V/m) plus a quick pulse often referred to transient electromagnetic pulse, “TEMP.” Since the prompt gamma rays create transient electromagnetic pulse by creating Compton recoil electrons, the total energy of the transient electromagnetic pulse cannot exceed the total energy of the prompt gamma rays (Rabinowitz, 1987). The total electric field strength, \( E \) in the pulse from (Rabinowitz, 1987) is displayed in Eq. 1 where \( E_0 = 52.5 \times 10^3 \) V/m, \( \alpha = 4.0 \times 10^9 / \text{sec} \), \( \beta = 4.78 \times 10^8 / \text{sec} \), whose results are displayed in Figure 1.

In accordance with Eq. 2 of reference (Rabinowitz, 1987), the power per electron is on the order of \( 3 \times 10^7 \) W/sec, and this power attenuates with distance from the event and varies with height of the event (in the atmosphere).

“At any instant the energy radiated by the ensemble of Compton electrons is stored equally in the electric and magnetic fields in the oscillating electromagnetic waves. This energy cannot exceed the accumulated earth-directed part of the gamma energy at any instant of time.” (Rabinowitz, 1987).

From (Rabinowitz, 1987), the total energy density delivered in time, \( t \) by the transient electromagnetic pulse is the integral of the Poynting vector, while energy balance the total energy release can be used to find the total gamma energy. The power radiated per (nonrelativistic accelerated) electron is such that electrons orbit circularly with roughly constant pitch and radius and if acting independently radiate at most about \( 4 \times 10^{-22} \) Watts, where roughly \( 2 \times 10^{13} \) electrons act in the so-called cone of influence (a very narrow cone of base \( \approx 400 \) km and area of \( 1 \) m\(^2\) whose vertex is centered at the burst) with a transient electromagnetic pulse power per electron of \( 3 \times 10^{-7} \) W electron.

The Compton electrons have energy equally stored in magnetic and electric fields, establishing a reasonable fundamental limit of electromagnetic pulse energy, which cannot exceed the earth-directed portion of accumulated gamma energy at any time, \( t \). The skin depth of charge on the impinged object is affected by the atmospheric conductivity (affecting the energy reaching the object) and the conductivity of the impinged object. The electric field strength, \( E(t) \) in the pulse as a function of time is given in Eq. 1, where \( E_0 = 52.5 \times 10^3 \) V/m, \( \alpha = 4.0 \times 10^9 / \text{sec} \) and \( \beta = 4.78 \times 10^8 / \text{sec} \).

\[
E(t) = E_0(e^{\alpha t} - e^{\beta t})
\]  

(1)

Considering realistic limitations on voltages imparted by electromagnetic pulse energy at a distance, the research in this manuscript utilizes a conservative imposition of a megavolt in a microsecond (notice the time of imposition in Figure 1A’s plot of Eq. 1’s time-evolution of energy) and seeks to assess the ability of adaptive van der Pol timing circuits to resist the deleterious effects of the imposed voltages. Particularly, notice in Figure 1 the movement towards roughly steady state prior to 1 microsecond.

**Electronic System Timing Circuits**

Timing circuits (for example those in Figure 2) (Timer Circuits: Digital C, 2021; Sekikawa et al., 2011; Van der Pol oscillator La, 2021) utilize capacitors as their basis, where the time constant of the capacitor is the product of the resistance and capacitance producing predictable capacitor charge and discharge curves for both voltage and current, and their governing equations are highly nonlinear and are often described as “chaos” as depicted in Figure 1B, where the bifurcation or transition from a fixed-point to limit cycle behavior is called a Hopf bifurcation (Patil et al., 2020). Cooper et al. (2017) introduced adaptive notions of controlling chaos [with respect to the van der Pol oscillator in Eq. 2, and this manuscript evaluates the use of those methods to provide resiliency to the deleterious effects of electromagnetic pulse induced voltages. The van der Pol oscillator is applicable to several fields of endeavors including brain science (Patil et al., 2020) and even dynamics of phase synchronization between solar polar magnetic fields (Savostianov et al., 2020), so the proposed methods in this manuscript become generalizable. Using the proposed methods, the goal is to force the system to respond with a perfect circle in phase space rather than the chaotic limit cycle displayed in Figure 1B, despite the imposition of a large, rapid voltage spike from an electromagnetic pulse.

\[
\frac{d^2x}{dt^2} + \mu(1-x^2)\frac{dx}{dt} + x = F(t)
\]  

(2)

**MATERIALS AND METHODS**

**Adaptive Methods to Protect Electronic System Timing Circuits**

Protection from electromagnetic pulse is ubiquitously achieved by shielding efforts (Lee et al., 2020; Jang et al., 2020), whereas this manuscript proposes passive mitigation by adopting adaptive electronics capable of counteracting the effects of the transient voltages. Following the successful implementation of nonlinear adaptive methods to spacecraft attitude control (Sands et al.,
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, Cooper et al. (2017) utilize the inherent dynamic of the van der Pol oscillator (in a feedforward-only sense) governed by electrodynamic physics to establish a forcing function (Eq. 3) to achieve a repeatable, predictable state space trajectory. Reference (Sands et al., 2007) evaluates a new energy function that facilitates a nonlinear stability proof where feedforward and feedback may be separately tuned, while references (Sands et al., 2009; Sands et al., 2012) illustrate variations theoretically (Sands et al., 2009) and experimentally (Sands et al., 2012) on laboratory hardware. In the feedforward, the governing dynamics are used directly where the states are replaced with the desired states and the parameter to be estimated \( \mu \) is replaced by estimate \( \hat{\mu} \), and this equation is proposed to quickly adapt to the imposition of impinging voltages generated by transient electromagnetic pulses, where \( \hat{\mu} \) is determined by an adaption rule with proportional derivative and integral components [as first described by Minorsky (1922) according to Flügge-Lotz, (1971)], multiplied by gains \( K_p, K_d, \) and \( K_i \) for proportional, derivative, and integral components respectively.

\[
\frac{d^2x}{dt^2} - \mu(1-x^2)\frac{dx}{dt} + x = F(t) \equiv \frac{d^2x_d}{dt^2} - \hat{\mu}(1-x^2_d)\frac{dx_d}{dt} + x_d \quad (3)
\]

This section provides a concise and precise description of the experimental (simulation) results, their interpretation, as well as the experimental conclusions that can be drawn. Simulations were created in MATLAB/SIMULINK software version R2020A with variable step size and automatic solver selection. Eq. 3 is encoded with the desired trajectories (subscripted \( d \)) described with sinusoids per (Cooper et al., 2017) and a standard proportional, integral, derivative controller used as the adaption rule of (presumed) unknown parameter \( \mu \). After 30 seconds of transient followed by steady-state operation, 1 MV is imposed on the timing circuit over 1 microsecond (conservatively representing a sample case described briefly in Adaptive Methods to Protect Electronic System Timing Circuits of this manuscripts) inducing a second transient and convergence to steady-state. The results permit assessment of resiliency to the deleterious transient embodied in the parameters of the transient (e.g., trajectory deviation, impact on timing to complete the circular oscillation, etc.).

Adaptive Methods to Protect Electronic System Timing Circuits first illustrates gain tuning of the parameters in the adaption rule and the selected adaption rule gains are used in Results's comparison of adaptive circuit performance estimating unknown parameter \( \mu \) and the resulting impacts on timing circuit performance.
Estimation by Adaption Rule With Proportional, Derivative, and Integral Components

This section illustrates iterative adaption gain tuning in 3 degrees displayed in Figures 3A,B, while Figure 3C displays the results of the chosen adaption gain selection. For ease of reading, each subfigure’s caption contains a mini table containing relevant information for each respective iteration corresponding to the figure.

Figure 4 compares nominal circuit performance to the case of imposition of a megavolt over a microsecond. Figures 4A,B depict nominal performance with the abscissa of Figure 4B zoomed to amplify the initial transient response (which is duplicated in the first period less than 30 s in Figure 4B). Figures 4C,D display timing circuit performance with event imposition at 30 seconds. Notice the comparison of Figures 4A,C. The topmost and lowest portions of the circular trajectory have identical transient startup, while the upper (middle) portion of the circular trajectory includes a new additional transient associated with the disturbance at 30 seconds.

Qualitatively, the circuit seems quite resilient in the fact the nominal circular trajectory is merely mildly disturbed. The deviation off the circular path produces an incrementally longer time-period to complete the circle, and this time-period embodies the deleterious effects. If this additional time results in loss of clock synchronization, for example, the electronic system using this timing circuit could be rejected from network access with other systems using the same time synchronization.

RESULTS

Comparison of Nominal Results (No Electromagnetic Pulse) and Results With Electromagnetic Pulse

Running identical simulations for 60 s affords an opportunity for direct comparison to reveal the timing impacts of the transient electromagnetic pulse. While Figure 4D displays the resulting tracking error, Figure 5 displays the accuracy of identification of \( \mu \) illustrating the duration of deleterious effects. At the termination of each simulation, the voltage trajectory ends at a specific point along the planned trajectory that establishes chip timing. Tables 1–4 display the two simulations’ final adapted value of \( \mu \) and final state and rate illuminating quantitative impacts.

Impacts on Timing Circuit Performance

Comparison of Nominal Results (No Electromagnetic Pulse) and Results With Electromagnetic Pulse revealed timing disruption was substantially overcome by the proposed adaptive circuit, but the disruption was not zero, as displayed in Figure 6. The period of oscillation was delayed 1.55 milliseconds and trajectory deviation was essentially stabilized during the transient electromagnetic pulse exhibiting a mere 0.3% trajectory deviation stabilizing quickly with a final (steady-state) deviation of 0.01%. This section compares the simulated timing disruption to figures of merit for timing maintenance of various systems utilizing timing circuits amongst other timing sources. A 2014 white paper published by MicroSemi includes many such figures of merit for representative systems.

“Most network operations (e.g., online security, log file updates) require accuracy on the order of 1–10 milliseconds. Depending on the specific application, electric utilities may require time measured in microseconds. Most financial and general business applications require accuracy in the 100 millisecond to 10 s range—even if only to accurately establish the order of events. Even if set to an absolutely accurate time reference, a PC clock may still be off by 50 milliseconds at the very instant when it is set. Then, once set, the clocks in computers will start to drift, some by as much as several minutes a day. It is possible for a workstation to achieve consistent accuracy of half-a-millisecond, but only if its clock is reset repeatedly over the course of a day.” (Microsemi White Paper, 2014).

Consider the electric power industry “…operators have to phase synchronize generators running hundreds of miles apart. In addition, they also must monitor the power grid for events such as voltage spikes or equipment outages using systems known as SCADA (supervisory control and data acquisition). SCADA systems are heavy users of time synchronization technology—specifically GPS time servers—and timestamps are
a major reason why. Timestamps from these servers provide the critical evidence needed to identify the causes of power failures, such as the one that crippled the Northeastern United States and Ontario in August 2003.** (Microsemi White Paper, 2014).

“On a WAN, NTP client time accuracy can be as good as 10–50 milliseconds on average, whereas individual time corrections can frequently vary by quite a bit more. However, if UTC is provided via GPS to the LAN, NTP can usually distribute UTC locally with an accuracy of one to 2 milliseconds to the clients. (GPS time stamp accuracy inside the time server is typically about a few microseconds to UTC). That means for most organizations, and for most applications, a GPS referenced time server is sufficient to deliver time to the local net and distribute time to client machines once available.” (Microsemi White Paper, 2014).

While Table 4 indicates a representative 1.5 milliseconds impact to oscillation period, Table 5 lists several instance of typical timing synchronization capabilities and requirements to bestow intuition on the ability of the proposed method to maintain nominal performance amidst an electromagnetic pulse event and quickly re-establish nominal performance.

Several application areas have timing requirements for synchronization that indicate efficacy of the proposed method (e.g., WAN networks, personal computers) and some applications that require such tight timing abilities or requirements to render the proposed method ineffective (e.g., IEEE 1588 Precision Time Protocol, and GMR1000 Master Clocks).

**DISCUSSION**

Use of the van der Pol chaotic equation is perhaps ubiquitous in robotics, e.g., automated shipping swinging robots, wire transducer sensors and even computer indigenous time sensors (amongst others). This manuscript proposed a new method to increase robustness of these applications to the deleterious effects of spurious environmental electromagnetic fields, while focusing on robot computer systems for comparison, since figures of merit are readily available without needing to model and simulate other potential applications. The results presented using the proposed adaption mechanism indicate efficacy for some applications (e.g., particularly personal computer and network electronics) while not sufficient for others (e.g., applications requiring IEEE 1588 Precision Time Protocol and industrial automation applications requiring accuracy akin GMR1000 master clock).
The main strength seems to be the robust rejection of the transient voltages with minimal deviation potentially preventing loss of timing synchronization following an electromagnetic impulse event from solar sources, lightning, nuclear detonations, etc.

Cooper, et al. used Eq. 2 to formulate Eq. 3 in accordance with principles of so-called physics-based controls as taught by Lorenz (2021a), Lorenz (2021b) and attempted to augment the physics-based feedforward with classical feedback optimized in a linear-quadratic sense, but the augmentation performed very poorly. Thus, this manuscript instead sought to use classical feedback principles (not yet optimized) to perform the function of parameter adaption rather than to formulate the feedback control signal. Future research should investigate the burgeoning application of deterministic artificial intelligence methods (D.A.I.) (Sands, 2020) which seem to promise improved performance over nonlinear adaptive methods (Sands et al., 2007; Sands et al., 2009; Sands et al., 2012) like the one proposed here. D.A.I. re-introduces optimization in the feedback learning channel whose instantiation constitutes a key difference between nonlinear adaption as utilized here and D.A.I. as taught at Cornell University (Sands, 2020; Shah and Sands, 2021).

Comparison to Alternatives
Having illustrated efficacy of the proposed method to counter deleterious effects of the imposition of a megavolt in a microsecond, Table 6 displays comparison of the results validated in Results to the efficacies of alternatives. Three alternatives are examined: surge protectors, unregulated power strips, and electromagnetic pulse shields. Surge protectors are arguably ubiquitously known, since they are common household devices protecting home electronics against sudden voltage spikes on the order of hundreds of volts imposed over microseconds after a few nanoseconds delay. Unregulated power strips are often described differently than surge protectors, since many do not truly use grounding techniques similar to surge protectors.

Electromagnetic pulse shields are very recently touted as capable or protection against electromagnetic pulse generated by lightning by comparison to military standards for such protection, although subsequent publications highlight the issue that protection should not be claimed too broadly. Protection against the effects of electromagnetic pulse generated by high altitude nuclear detonations necessitates rejection of very high voltages. A noteworthy validation was experimentally performed and the capabilities are coarsely summarized in Table 6. The proposed methodology indicates efficacy at much higher voltage levels.

Conclusion
This manuscript proposed, analyzed, and validated in simulation where spurious voltages were rapidly rejected with a mere 0.3% trajectory deviation, stabilizing quickly with a final (steady state) deviation of 0.01%. The demonstrated abilities to reject the deleterious spurious effects are compared to nominal figures of merit for timing accuracy of various computer systems to conclude the proposed methods are effective for some applications, but insufficient for others. The proposed method illustrated capabilities to reject a megavolt, while typical alternatives reject hundreds of volts.
TABLE 6 | Efficacies of typical alternatives to deal with sudden voltage spikes (1, 2, 3, 4).

| Voltage                  | Imposition time | Ground method               |
|--------------------------|-----------------|-----------------------------|
| Surge protectors         | 3–4 times nominal voltage | 1–3 microseconds after delay of few nanoseconds | Blocking, shorting, or release as heat |
| Unregulated power strips | ~100 coulomb-volt (~5,000 amps, ~100 s V) | 25 nanosecond delay | Dissipation in circuit |
| EMP shield               | ~100 s of volts | ~1 microsecond | Dissipation in circuit |
| Proposed                 | ~1 MV           | ~1 microsecond | Dissipation in circuit |

1https://en.wikipedia.org/wiki/Surge_protector.
2Experimentally (hardware) demonstrated, 2019. Available online: https://www.empshield.com/ (accessed 8 July 2021); https://markets.businessinsider.com/news/stocks/emp-shield-llc-develops-the-world-s-emp-shield (accessed 8 July 2021); https://www.empshield.com/wp-content/uploads/2019/11/EMP_Shield_Military_Testing_16_March_2019_Public.pdf (accessed 9 July 2021).
3The author con
4Acknowledgments

The foremost development at the heart of the methods proposed in this manuscript arise from the physics-based methodology taught by Professor Robert Lorenz (Lorenz R., 2021) who recently posthumously was named a Fellow of the National Academy of Engineering in the United States. Readers may see this methodology at the heart of several methods, not at least nonlinear adaptive control (Sands et al., 2007; Sands et al., 2009; Sands et al., 2012) and deterministic artificial intelligence (Cooper et al., 2017; Sands, 2020).

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DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

The author confirms being the sole contributor of this work and has approved it for publication.

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