Research Article

Dynamic Heating System of Multiphase Flow Digester by Solar-Untreated Sewage Source Heat Pump

Pei Guo,1 Jiri Zhou,1 Rongjiang Ma,2 Nanyang Yu,1, and Yanping Yuan1

1School of Mechanical Engineering, Southwest Jiaotong University, Chengdu 610031, China
2Department of Building Science, Tsinghua University, Beijing 100084, China

Correspondence should be addressed to Nanyang Yu; rhinos@126.com

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The traditional biogas heating system has the disadvantages of a low energy efficiency ratio and high energy consumption. In this study, a solar-untreated sewage source heat pump system (SUSSHPS) was developed for heating a 12 m³ multiphase flow digester (MFD) in Suining, China. To investigate the operating effects, two modes were defined according to the solar fractions in different regions. On the basis of experimental data, thermodynamic calculations and operating simulation analysis were performed, and the solar collector area (A_c) and the minimum length of the sewage double-pipe heat exchanger (L_{min}) for the two modes were calculated. The results indicated that the A_c and L_{min} of mode 2 were larger than those of mode 1 at different solar fractions. Additionally, the results suggested that mode 1 can be used at a solar fraction of <0.33, and mode 2 can be used at a solar fraction of >0.5. Moreover, a comprehensive evaluation of different biogas heating systems was performed. Two evaluation methods were used for modeling calculations, and the results of the two methods were consistent. The SUSSHPS had the largest comprehensive evaluation value among the four systems. The proposed SUSSHPS can play a significant role in improving current biogas heating systems and promoting the development of biogas projects.

1. Introduction

Biogas is a renewable form of energy that is produced by the anaerobic digestion of organic waste at a certain temperature, pH, and concentration [1]. Temperature is one of the factors affecting anaerobic digestion. The temperature variation significantly affects the bacterial digestion process and therefore should not exceed 2–3°C per hour [2]. If the variation in the digestion temperature exceeds 5°C within a short period of time, the biogas production rate can change significantly; thus, a constant digestion temperature is required [3]. Therefore, it is generally accepted that the current biogas project should be equipped with a heating system to ensure stable biogas production during winter.

Traditional heating methods include generation waste heat heating [4], boiler heating [5, 6], active and passive solar heating [7, 8], and heat pump heating [9]. Liu et al. used a groundwater source heat pump to heat a 700 m³ anaerobic digester and found that the fermentation temperature of biogas tanks could be maintained at 33–35°C in winter [10]. Tiwari et al. used a photovoltaic thermal-integrated greenhouse system for biogas heating, and simulation results indicated that the greenhouse room temperature varied between 38 and 47°C [11]. In recent years, for reducing the active energy input and avoiding the high initial cost and unstable defects in the use of single solar energy, solar-integrated source heat pump heating methods have become a popular research topic [12]. These methods include solar-ground source heat pump heating [13], solar-air source heat pump heating [14], and solar-sewage source heat pump heating [15]. However, solar-integrated source heat pump heating methods have many disadvantages, limiting their applications. First, the heating system has a low energy efficiency ratio (EER). Pei et al. used a solar-ground source heat pump to heat a 69.3 m³ anaerobic digester, and the system EER was 2.7 [16]. Another disadvantage of the solar-ground source heat pump heating method is the reduction of the EER over time, which is due to the heat storage imbalance in winter and summer [17]. The disadvantage of the solar-air source heat pump heating method is frosting in winter [18]. Solar-
Table 1: Comparison of different biogas heating systems.

| Heating system                     | Digestion temperature (°C) | CH₄ yield (m³ m⁻³ d⁻¹) | System unit cost* (yuan m⁻³) | EER  | Reference |
|-----------------------------------|----------------------------|-------------------------|-------------------------------|------|-----------|
| Electric boiler                   | 23.5                       | 0.472                   | /                             | 1.38 | [20]      |
| Biogas boiler                     | 35                         | 0.482                   | 2000                          | 1.01 | [19]      |
| Solar+biogas boiler               | 19.82-23.5                 | 0.389-0.472             | 314.39                        | 2.01 | [6]       |
| Solar direct heating system       | 26-37                      | 0.63-1.08               | 2145.16                       | 6.17 | [7]       |
| Solar direct heating system       | 7.02-27.14                 | 0.314-0.569             | 300                           | 5.56 | [21]      |
| Ground source heat pump           | 32                         | 0.6                     | 408.37                        | 2.7  | [9]       |
| Solar-air source heat pump        | 35                         | /                       | 3750                          | 3    | [14]      |

*The value is the system initial cost divided by the volume of the digester.

sewage source heat pump heating is different from the other two methods and has the advantages of a higher EER, a lower initial cost, and easy maintenance. However, the corrosion and blockage of the heat exchangers are significant problems affecting the system application. Additionally, the system is limited to using the primary or secondary water discharged from a sewage treatment plant as a heat source. A comparison of the different biogas heating systems is presented in Table 1.

As shown in Figure 1, a 12 m³ multiphase flow digester (MFD) dynamic digestion system was heated by a biogas boiler near a pig farm at Suining City, Sichuan Province, China [19]. Full-scale field experiments were conducted on the biogas production rate of the system at different temperatures, as well as the dynamic digestion effects and dynamic heating digestion effects of the system. The results for the biogas production rate at different temperatures revealed that the temperature significantly affected the biogas production rate of the MFD system. After long-term operation, although the biogas boiler system had the advantages of convenient operation and easy maintenance, the high energy consumption and low EER reduced the overall efficiency of the biogas project, making it difficult to maintain stable long-term operation.

Accordingly, an integrated solar-untreated sewage source heat pump dynamic heating system for the MFD was developed in this study. A predesigned double-pipe device was used as the heat exchanger, which extracts thermal energy from untreated sewage. The structure of the device avoids the problems of corrosion and blockage, expanding the application scope of the heating system. Additionally, the system does not affect the biochemical treatment of sewage [22]. Furthermore, two operating modes were designed according to the solar fractions in different regions. Through thermodynamic calculations and operating simulation analysis, the variation of the solar collector area (Aₛ) and the minimum length of the sewage double-pipe heat exchanger (lₘₚₑₚₑ) under the two operating modes were obtained, and the application ranges of the operation modes were determined. To quantitatively compare the advantages of the solar-untreated sewage source heat pump system (SUSSHPS) over different heating systems, a comprehensive evaluation of different biogas heating systems was conducted, and calculations were performed using two methods. This study may help promote the use of the integrated solar-untreated sewage source heat pump in the biogas heating field and lead to developments in biogas science research. Moreover, this study can increase the biogas production rate and maintain the stability of biogas projects in winter.

2. System Descriptions and Methods

2.1. System Descriptions. The proposed system (Figure 2) contains two subsystems: the SUSSHPS and the biogas slurry dynamic heating and heat storage system. The SUSSHPS consists of a solar collector, a heat pump unit, a sewage double-pipe heat exchanger, and water pumps. The sewage double-pipe heat exchanger (Figure 3) is a part of the sewage network. Untreated sewage flows in the inner pipe, and chilled water flows in the spiral space between the inner and outer pipes. The thermal energy of the untreated sewage is transferred to the chilled water through the inner pipe wall, which then flows downstream after the heat exchange. Moreover, the solar collectors provide a portion of the heat. Then, the chilled water is pumped into the heat pump unit, and after heat exchange, it is pumped into the sewage double-pipe heat exchanger again. After transmission and conversion by the heat pump unit, thermal energy is transferred to the biogas slurry dynamic heating and heat storage system through the cooling water pump. In the biogas slurry dynamic heating and heat storage system, thermal energy is transferred to the slurry through the slurry double-pipe heat exchanger, and the excess heat is stored in the heat storage tank.

A heat pump unit is used in the system as the heat source for heating. The rated power, rated coefficient of performance (COP), and voltage of the heat pump unit were 1 kW, 4.0, and 380 kV, respectively. To reduce the power of the heat pump unit, a heat storage tank was used. The volume, length, width, and height of the tank were 2 m³, 1.0 m, 1.0 m, and 2.0 m, respectively. The storage temperature was set as 313.15 K. The rated power, rated flow, head, and rotating speed of the chilled water pump and cooling water pump were 0.75 kW, 7 m³ h⁻¹, 12.5 m, and 2000 rpm, respectively.

2.2. Experimental Methods. The digestion material of the MFD is fresh pig manure. The detailed parameters of the MFD dynamic anaerobic digestion system are presented in [2]. Continuous feeding digestion experiments (450 kg per day) were started on February 22, 2016, and performed until
April 20, 2016. The basic characteristics of the biogas slurry used in the experiments are presented in Table 2.

The main measurement parameters include the digestion temperature, pump flow rate, storage temperature, and biogas production, as shown in Table 3.

2.3. System Operating Modes. Figure 4 presents the operating schematic of the SUSSHPS. As shown in Table 4 and Figure 5, the distribution of solar energy resources differs among different regions in Sichuan Province. Under different solar fractions, the necessary thermal energy supplied by the untreated sewage ($Q_{\text{sewage}}$) and solar energy ($Q_{\text{solar}}$) differs. Therefore, the system employs two operating modes. In mode 1, during the daytime, the thermal energy of the MFD dynamic heating and the heat storage tank are supplied by the SUSSHPS ($\circ+\circ\rightarrow\circ+\circ$). At night, the thermal energy of the MFD dynamic heating is supplied by the SUSSHPS and the heat storage tank ($\circ\rightarrow\circ, \circ$). In mode 2, during the daytime, the thermal energy of the MFD dynamic heating and the heat storage tank are supplied by the SUSSHPS ($\circ+\circ\rightarrow\circ+\circ$). At night, the thermal energy of the MFD dynamic heating is supplied by the heat storage.
tank directly (③). To save energy, the heating system runs three times each day and night, for one hour each time. The heat transfer processes for the two modes are shown in Figures 6 and 7.

Similarly, the minimum length of the sewage double-pipe heat exchanger and the solar collector area are different for the two modes. The system heat load includes the heat loss of the slurry tank and the MFD and the heat load of the slurry, which must be heated to reach the target digestion temperature. Ignoring the bioheat and the heat removed by biogas, the system total heat demand can be described as follows [24].

$$Q_{\text{demand}} = Q_1 + Q_2,$$  \hspace{1cm} (1)
where \(Q_{\text{demand}}\) represents the heat duty of the dynamic anaerobic digestion system (in kW), \(Q_1\) represents the heat required for heating the biomass digestive fluid (in kW), and \(Q_2\) represents the heat loss from the MFD and slurry tank (in kW). The specific calculation process is described in [19].

\[
\begin{align*}
12Q_{\text{demand}} + Q_{\text{storage}} &= 3W + 3Q_{\text{sewage}} + 3Q_{\text{solar}}, \\
12Q_{\text{demand}} - Q_{\text{storage}} &= 3W + 3Q_{\text{sewage}}, \\
Q_{\text{sewage}} &= (4Q_{\text{demand}} - W) \times (1 - f), \\
Q_{\text{solar}} &= (8Q_{\text{demand}} - 2W) \times f. 
\end{align*}
\]

Comparing Equation (3) with Equation (5) reveals that the thermal energy supplied by the untreated sewage and the solar irradiation in mode 1 are larger than those in mode 2, indicating that \(A_c\) and \(l_{\text{min}}\) for mode 1 are larger than those for mode 2.

### 2.3.1. Minimum Length of Sewage Double-Pipe Heat Exchanger

Figure 8 presents the measured and calculated untreated sewage temperatures in winter in Suining City. As shown, the temperature of the untreated sewage was 13.4–16.2°C in winter, and the temperature fluctuation was small. Therefore, it is assumed that the sewage temperature was constant at 15°C.

As shown in Figure 2, the water–water heat transfer in the reverse direction is kept in the heat exchanger. The flow of sewage in the inner pipe is natural convection, while the flow of chilled water in the outer pipe is forced convection. The \(l_{\text{min}}\) can be expressed as follows [26]:

\[
\begin{align*}
\text{Figure 4: Operating schematic of the SUSSHPS.} \\
\text{Figure 5: Distribution of solar energy richness in Sichuan [23].} \\
\text{Table 3: Characteristics of the measuring instrument.} \\
\text{Table 4: Recommended data for the solar fractions in Sichuan Province.} \\
\end{align*}
\]
\[ l = \frac{1000Q_{\text{sewage}} \cdot \ln \left( \frac{t_{\text{sewage}} - t_{\text{in}}}{(\pi t_{\text{sewage}} - t_{\text{out}})} \right)}{k_m \cdot \left( t_{\text{sewage}} - t_{\text{in}} \right) - \left( t_{\text{sewage}} - t_{\text{out}} \right)}, \]  

where \( l_{\text{min}} \) represents the minimum length of the sewage double-pipe heat exchanger (in m); \( t_{\text{sewage}} \) and \( t_{\text{in}} \) represent the average inlet and outlet temperatures of the chilled water, respectively (in K); \( k_m \) is the heat transfer coefficient of the heat exchanger (in W m\(^{-1}\) K\(^{-1}\)); \( R_l \) represents the fouling resistance, which is chosen as 0.00017 m K W\(^{-1}\) [27]; \( h_0 \) is the convection heat transfer coefficient of the inner pipe internal surface (in W m\(^{-2}\) K\(^{-1}\)); \( r_i \) represents the inner radius of the sewage double-pipe heat exchanger (in m); \( r_0 \) represents the inner pipe thickness of the inner pipe wall (in m); \( \delta_i \) represents the inner pipe thickness of the outer pipe wall (in m); \( \lambda_0 \) represents the heat conductivity coefficient of the chilled water (in W m\(^{-1}\) K\(^{-1}\)); \( N\nu \) is the Nusselt criterion number; and \( D_e \) represents the characteristic length of the sewage double-pipe heat exchanger (in m). The values of the parameters used in the calculation are presented in Table 5.

2.3.2. Solar Collector Area. After \( Q_{\text{demand}} \) is determined, the solar collector area can be calculated for a specific solar fraction. A direct system was chosen, and \( A_c \) can be expressed as follows [28]:

\[ Q_c = 86.4 \left( 1 + \eta_s \right) Q_{\text{solar}}, \]

\[ A_c = Q_c \times \frac{f}{J_T \times \eta_d \times \left( 1 - \eta_g \right)}, \]  

where \( \eta_g \) represents the overall solar collector efficiency; \( J_T \) is the collector efficiency correction factor; \( \eta_d \) is the collector direct gain fraction; and \( \eta_s \) is the solar fraction (a fraction between 0 and 1).
Table 5: Basic values of the parameters for the sewage double-pipe heat exchanger.

| Parameter                        | Unit | Value          |
|----------------------------------|------|----------------|
| Inner pipe radius                | mm   | 23             |
| Outer pipe radius                | mm   | 39             |
| Thickness of inner pipe wall     | mm   | 2              |
| Thickness of outer pipe wall     | mm   | 3              |
| Average inlet/outlet temperature of chilled water | K    | 280.15/285.15 |

where $A_s$ represents the area of the direct system (in m$^2$); $f$ represents the solar fraction, as shown in Table 3; $I_T$ represents the average daily amount of solar radiation (6.82 MJ m$^{-2}$ d$^{-1}$) [23]; $\eta_d$ represents the average collection efficiency of the solar collector (0.25–0.50; chosen as 0.4 in this study); $\eta_r$ represents the average heat loss rate of the solar collector (0.20–0.30; chosen as 0.2 in this study); $\eta_c$ represents the heat loss efficiency of the direct system (chosen as 0.05); and $Q_s$ represents the heat duty of the solar collector (in MJ d$^{-1}$).

3. Results and Discussion

The proposed SUSSHPS was designed to maintain dynamic anaerobic digestion at 35°C in winter. As indicated by Equation (6), the minimum length of the sewage double-pipe heat exchanger was determined by the heat transfer coefficients of the heat exchanger. Theoretical calculations and a numerical simulation analysis of the heat transfer coefficients of the heat exchanger were performed. As shown in Figure 9, the extended calculated values of the Dittus–Boelter equation and Gnielinski equation [29] were compared with the simulation value obtained using the ANSYS 15.0 software. The results indicated that the differences among the three numerical values were small, and the simulation results were accurate. Therefore, according to Equations (7)–(9), the calculated value of $k_w$ was 292.43 W m$^{-1}$ K$^{-1}$. Figure 10 presents the annual heat duty and heat loss of the SUSSHPS. $Q_{\text{demand}}$ was calculated as 1.01 kW.

Table 6 presents the minimum length of the sewage double-pipe heat exchanger and the solar collector area under the different solar fractions in different modes. As shown, for both modes, with an increase in the solar fraction, the minimum length of the sewage double-pipe heat exchanger decreased, and the solar collector area increased. As shown in Figure 11, with a 0.1 m decrease of the minimum length of the sewage double-pipe heat exchanger, the increases in the solar collector area for modes 1 and 2 were 12.39 m$^2$ and 6.19 m$^2$, respectively. Consequently, the functional relationship between $A_s$ and $l_{\text{min}}$ can be expressed as follows: Mode 1: $Y = 252.76 - 123.86X$ ($R^2 = 0.9996, P < 0.0001$). Mode 2: $Y = 294.03 - 61.87X$ ($R^2 = 0.9996, P < 0.0001$).

The application conditions of the two modes were investigated. Mode 1 can be used in general-solar energy resource areas, where the amount of thermal energy supplied by the untreated sewage is larger than that supplied by the solar irradiation for the SUSSHPS. Conversely, mode 2 can be used in solar energy resource-rich areas, where the amount of thermal energy supplied by the untreated sewage was smaller than that supplied by the solar irradiation for the SUSSHPS. According to Equations (3) and (5), when $Q_{\text{sewage}} = Q_{\text{solar}}$, the solar fractions for modes 1 and 2 are 0.33 and 0.5, respectively. Thus, as shown in Figure 12, the standard deviations are 359.85 m (model 1) and 178.44 m (model 2) for Figure 12(a), and the standard deviations are 34.61 m$^2$ (model 1) and 40.23 m$^2$ (model 2) for Figure 12(b), when the solar fraction is <0.33, mode 1 is more suitable, and when the solar fraction is >0.5, mode 2 is more suitable. Additionally, it was useful to regulate the anaerobic digestion temperature when the solar fraction was between 0.33 and 0.5.

The simulation results were verified. A solar fraction of 0.3 and mode 1 were selected. Figure 13 presents the slurry temperature of the MFD from February 22, 2016, to April 10, 2016. As shown in Figure 13, the slurry temperature was stabilized around 35°C, indicating that the SUSSHPS functioned well and that stable digestion was achieved by the MFD.

4. Evaluation of System Operation

4.1. Establishment of Comprehensive Evaluation System.
To examine the advantages of the SUSSHPS, a comprehensive evaluation of different biogas heating systems
was performed. The original biogas boiler heating system was labeled as “system 1,” the solar direct heating system was labeled as “system 2,” the solar source heat pump heating system was labeled as “system 3,” the SUSSHPS with $l = l_{\text{max}}$ was labeled as “system 4,” and the SUSSHPS with $l = l_{\text{min}}$ was labeled as “system 5.”

Single-calculation analysis methods and software simulation analysis methods have been used in many system-evaluation studies [30]. However, these methods have many disadvantages. The problem of the single-calculation analysis methods affects the comprehensive evaluation of systems, as only the energy saving or economy of the system is considered [31]. The software simulation process simplifies the model indicators, which can cause calculation deviations [32]. Therefore, to evaluate each system quantitatively, a comprehensive evaluation system and a comprehensive evaluation mathematical model based on previous experimental data were constructed. According to the construction
principle of the comprehensive evaluation system, indices with a significant influence on the system performance were chosen. The comprehensive evaluation system included three elements—the operating energy consumption, economy and energy saving, and environmental protection—and six targets. The comprehensive evaluation system for the different biogas heating systems is shown in Figure 14.

4.1.1. Operating Energy Consumption Analysis of Different Biogas Heating Systems. To investigate the operating stability of the different biogas heating systems, an operating energy consumption analysis was performed. The EER of the system can be calculated as follows:

$$EER = \frac{Q_{output}}{Q_{input}}$$  \hspace{1cm} (11)$$

where EER represents the energy efficiency ratio of the system; $Q_{input}$ represents the input energy of the system,

| $f$ | $l_{\text{min}}$ (m) | $A_c$ (m$^2$) | $l_{\text{min}}$ (m) | $A_c$ (m$^2$) |
|-----|-----------------|-------------|-----------------|-------------|
| 0.1 | 1.84            | 25.27       | 4.27            | 29.43       |
| 0.2 | 1.63            | 50.55       | 3.80            | 59.86       |
| 0.3 | 1.43            | 75.82       | 3.32            | 88.29       |
| 0.4 | 1.22            | 101.1       | 2.85            | 117.72      |
| 0.5 | 1.02            | 126.37      | 2.37            | 147.15      |
| 0.6 | 0.82            | 151.64      | 1.90            | 176.58      |
| 0.7 | 0.61            | 176.92      | 1.42            | 206.02      |
| 0.8 | 0.41            | 202.19      | 0.95            | 235.45      |
| 0.9 | 0.20            | 227.47      | 0.47            | 264.88      |
|     | Standard deviation | 0.56       | 69.22        | 1.30       | 80.47       |

**Figure 11:** Ratio of the solar collector area to the sewage heat exchanger minimum length in different modes.

**Figure 12:** (a) Ratio of the solar collector area to the sewage heat exchanger minimum length with respect to the solar fraction. (b) Ratio of solar collector area to the thermal storage volume with respect to the solar fraction.

**Figure 13:** Daily average digestion temperature in the MFD.
including operation energy and heating energy consumption (in MJ d\(^{-1}\)); and \(Q_{\text{output}}\) represents the output energy of the system (in MJ d\(^{-1}\)); the value is 137.66 MJ d\(^{-1}\) as shown in Reference [19].

The operating energy income quantitatively reflects the operating effectiveness of biogas heating systems and was calculated as follows.

\[
Q_{\text{income}} = Q_{\text{output}} - Q_{\text{input}}. \tag{12}
\]

Table 7 presents the calculated EER and operating energy income for the different biogas heating systems by Equations (11) and (12). As shown, system 2 had the largest EER and operating energy income, and the EER of system 2 was six times that of system 1. The EER and operating energy income were the same for systems 3, 4, and 5. The operating energy income of systems 3, 4, and 5 was 21.6 MJ d\(^{-1}\) smaller than that of system 2, and the EER of these three systems was half that of system 2. The results indicate that system 2 is advantageous with regard to the operating energy consumption.

### 4.1.2. Economic Analysis of Different Biogas Heating Systems

It was assumed that the systems were operated continuously. Using the annual cost evaluation method, the annual cost value and the cost current value of the different biogas heating systems were calculated as follows:

\[
PC = M - N,
\]

\[
AC = PC \left[ \frac{s(1 + s)^n}{(1 + s)^n - 1} \right] + C + S, \tag{13}
\]

where \(AC\) represents the annual cost value of the biogas heating system (in yuan); \(PC\) represents the present cost value of the biogas heating system (in yuan); \(M\) represents the initial investment (in yuan); \(N\) represents the net residual value, which was assumed to be 0 yuan; \(C\) represents the annual operating cost (in yuan); \(S\) represents the annual maintenance cost (in yuan); \(s\) represents the annual interest rate of bank deposits (5%–10%); and \(n\) represents the service life, which was set as 20 years.

For convenience, the initial investment for the systems was assumed to consist of the equipment cost and installation cost. The initial investment was 2000 yuan kW\(^{-1}\) for the heat pump unit, 1200 yuan m\(^{-1}\) for the sewage double-pipe heat exchanger, and 200 yuan m\(^{-2}\) for the solar collector. The local electricity price was 0.53 yuan kW\(^{-1}\) h\(^{-1}\). Accordingly, Table 8 presents the \(AC\) and \(PC\) values of the different biogas heating systems. As shown, the \(AC\) and \(PC\) of system 2 were the highest—significantly higher than those of systems 4 and 5—because of the larger solar collector area and higher initial investment for system 2. The \(AC\) and \(PC\) of systems 4 and 5 were lower than those of system 3, indicating that the use of the sewage double-pipe heat exchanger can effectively reduce the solar-collector cost and improve the system economic performance.
where $\eta_i$ represents the energy-saving rate of the biogas heating system relative to system 1 (in %); $H_i$ represents the primary energy consumption of the system (in MJ d$^{-1}$); $\eta_a$ represents the generation efficiency, which was set as 35%; and $\eta_b$ represents the transmission and distribution efficiency, which was set as 90%.

In this study, the small-scale baseline methodology of AMS-IC, which was approved by the Clean Development Mechanism Executive Board of the United Nations Framework Convention on Climate Change, was used to estimate the system CO2 emission reductions [33]. The water heating system using conventional fossil fuels was set as a baseline which does not consider the CO2 emission reduction benefits of the biogas power generation and waste heat recovery in later.

$$ER_y = BE_y - PE_y,$$

(15)

where $ER_y$ represents the CO2 emission reduction of the biogas heating system (in kg d$^{-1}$), $BE_y$ represents the CO2 emissions of the system under baseline conditions (in kg d$^{-1}$), and $PE_y$ represents the CO2 emissions of the system (in kg d$^{-1}$).

$$BE_y = \frac{44 H_1}{12 \eta_a q' \times F_{CO_2}},$$

(16)

where $q'$ is the calorific value of standard coal (29.308 MJ kg$^{-1}$), $F_{CO_2}$ is the carbon emission factor (0.866), and $\eta_a$ represents the efficiency of the conventional energy water heating device (95%).

$$PE_y = 0.278 Q_{input} \times EF_{grid} + V_i \times \rho_{CO_2},$$

(17)

where $EF_{grid}$ is the power grid emission factor (1.0297 kg CO2-(kW h)$^{-1}$) [34], $V_i$ represents the CO2 emission volume of the biogas heating system (in m$^3$), and $\rho_{CO_2}$ is the density of CO2 (1.82 kg m$^{-3}$).

As shown in Table 9, systems 2 and 1 exhibited the best and worst performances, respectively, with regard to the energy-saving rate and CO2 emission reduction.

### 4.2. Establishment of Comprehensive Evaluation Model

#### 4.2.1. Improved Entropy Weight Coefficient Method

The mathematical model of the comprehensive evaluation system was constructed according to the improved entropy weight coefficient method [35]. Because of the different units and dimensions of the indices, it was necessary to normalize the indices using the following equation:

$$r_{ij} = \left\{ \begin{array}{l} x_{ij} - \min_{1 \leq j \leq n} (x_{ij}) \quad (positive \ indices), \max_{1 \leq j \leq n} (x_{ij}) - x_{ij} \\ \frac{\max_{1 \leq j \leq n} (x_{ij}) - \min_{1 \leq j \leq n} (x_{ij})}{(positive \ indices)} \end{array} \right. \quad (18)$$

where $i = 1, 2, \ldots, n; j = 1, 2, \ldots, m; \ n$ is the number of object and $m$ is the number of index; $r_{ij}$ is the $j^{th}$ index of the $i^{th}$ evaluated system after normalization; and $x_{ij}$ is the $j^{th}$ index of the $i^{th}$ evaluated system before normalization.

The $i^{th}$ evaluated system index weight $p_{ij}$ of the $j^{th}$ index is defined as follows:

$$p_{ij} = \frac{r_{ij} + 1}{\sum_{i=1}^{n} (r_{ij} + 1)}. \quad (19)$$

The entropy $E_j$ of the $j^{th}$ index is defined as follows:

$$E_j = -\frac{\sum_{i=1}^{n} p_{ij} \ln p_{ij}}{\ln n}. \quad (20)$$

The objective weight $\theta_j$ of the $j^{th}$ index is defined as follows:

$$\theta_j = \frac{1 - E_j}{m - \sum_{j=1}^{m} E_j}. \quad (21)$$

The objective weight was improved with the combination of the subjective weight. The subjective weights were determined via the Delphi method. The steps of this method are presented in [36]. The subjective weights were calculated using the MATLAB 2015 software (Table 10) and passed the consistency test ($CR = 0.0417 < 0.1$).
The synthetic weight $\gamma_j$ of the $j$th index is defined as follows:

$$\gamma_j = \frac{\theta_j w_j}{\sum_{j=1}^{m} \theta_j w_j}.$$  \hspace{1cm} (22)

The comprehensive evaluation value $\lambda_i$ of the $i$th evaluated system was calculated as follows:

$$\lambda_i = \sum_{j=1}^{m} \gamma_j p_{ij}.$$  \hspace{1cm} (23)

Figure 15 presents the comprehensive evaluation values of the different biogas heating systems. As shown in Table 10, the EER and PC had the largest synthetic weight, and the energy-saving rate had the smallest synthetic weight. The comprehensive evaluation values of the systems decreased in the following order: System 4 > System 5 > System 2 > System 3 > System 1. System 4 had the largest comprehensive evaluation value of 0.2251. Although systems 4 and 5 were not optimal with regard to the EER, system operating energy income, energy-saving rate, and CO$_2$ emission reduction, they were excellent with regard to the system economic performance, particularly the initial investment.

4.2.2. Delphi-Variation Coefficient Combination Weighting Method. The mathematical model of the comprehensive evaluation system was based on the Delphi-variation coefficient combination weighting method [37]. The matrix of normalized indices $R_{ij}$ was constructed using Equation (18).

The variation coefficient is defined as follows:

$$v_j = \frac{\sigma_j}{\bar{x}_j},$$  \hspace{1cm} (24)

where $j = 1, 2, \cdots, m$; $v_j$ is the variation coefficient of the $j$th index; $\sigma_i$ represents the standard deviation of the $j$th index; and $\bar{x}$ represents the average value of the $j$th index.

By normalizing Equation (24), the subjective weight $\theta_j$ of the $j$th index can be described as follows:

$$a_j = \frac{v_j}{\sum_{j=1}^{m} v_j}.$$  \hspace{1cm} (25)

The synthetic weight is defined as follows:

$$\tau_j = \lambda w_j + (1 - \lambda) a_j.$$  \hspace{1cm} (26)

As shown in Table 11 and Figure 15, the EER and PC had the largest impact on the comprehensive evaluation value of the system, and the energy-saving rate had the smallest impact. As shown in Figure 15, the standard deviation is 0.1699 for Delphi-variation coefficient weighting method and is 0.1851 for improved entropy weight coefficient method.
method; the system rankings obtained via the two methods were the same. The comprehensive evaluation values of the systems decreased in the following order: System 4 > System 5 > System 2 > System 3 > System 1. System 4 had the largest comprehensive evaluation value of 0.6864.

4.3. Kendall’s W Test. Different evaluation methods may have different results. Therefore, to investigate whether the conclusions of the two comprehensive evaluation methods were consistent, Kendall’s W coefficient test was conducted [38]. And the coefficient is defined as follows:

\[
R_j = \frac{\sum_{i=1}^{m} r_{ij}}{m},
\]

\[
W = \frac{12 \sum_{i=1}^{n} r_{ij}^2 - 3b^2n(n+1)^2}{bn(n^2-1)},
\]

where \( R_j \) is the rank of the \( j \)th evaluated system; \( b \) is the number of comprehensive evaluation method.

Moreover, using the SPSS software, the evaluation results of the two comprehensive evaluation methods were compared according to Kendall’s W coefficients. The results were Kendall’s \( W = 0 \) and saliency Asymp. Sig. = 1.000, indicating that the evaluation results of the two methods were in good agreement. Therefore, the SUSSHPS was the optimal system among the four heating systems. When the untreated sewage is sufficient, system 4 can be used directly. Conversely, if the untreated sewage is insufficient (\( I_{\text{min}} \leq l \leq I_{\text{max}} \)), solar energy can be used for supplementation. In general, more factors must be taken into account, such as the sewage flow, the construction conditions and difficulty of the sewage double-pipe heat exchanger, and the sewage temperature. The values of the solar collector area and the length of the sewage double-pipe heat exchanger can be defined according to the principle of the maximization of system benefits.

5. Conclusion

For improving the conventional biogas heating system, this paper proposed an SUSSHPS for the MFD dynamic anaerobic digestion system. Two operating modes were defined according to the solar fractions in different regions: mode 1 for general-solar energy resource areas and mode 2 for solar energy resource-rich areas. Based on the thermodynamic calculations and experiments study, the parameters of \( A_x \) and \( I_{\text{min}} \) for the two modes were calculated. And we also clear the suitable conditions of the two modes.

Furthermore, to examine the advantages of the SUSSHPS, a comprehensive evaluation of a biogas boiler heating system, a solar direct heating system, a solar source heat pump heating system, and the SUSSHPS (\( I = I_{\text{min}} \) and \( I = I_{\text{max}} \)) was performed. According to the experimental data and calculated values, a comprehensive evaluation system was constructed, which consisted of three elements and six indices. Moreover, a mathematical model of the comprehensive evaluation system was constructed via the improved entropy weight coefficient method and the Delphi-variation coefficient combination weighting method. The results of the two methods were the same. The biogas boiler heating system and the SUSSHPS exhibited the smallest and largest comprehensive evaluation values, respectively. It is indicated that the SUSSHPS was the optimal system among the four heating systems, exhibiting excellent system economic performance, as well as outstanding energy saving and environmental protection. However, many other factors should be considered, such as the sewage flow and sewage temperature, and the maximization of the system benefits should be the guiding principle in the practical application of the proposed system.

### Nomenclature

- **EER**: Energy efficiency ratio
- **COP**: Coefficient of performance
- **TS**: Total solid concentration of fermentation slurry (%)
- **VS**: Volatile solid concentration of fermentation slurry (%)
- **COD**: Chemical oxygen demand (g L\(^{-1}\))
- **BOD\(_5\)**: Biochemical oxygen demand (g L\(^{-1}\))
- **Q\(_\text{demand}\)**: Heat duty of the dynamic anaerobic digestion system (kW)
- **Q\(_1\)**: Heat required for heating the biomass digestive fluid (kW)
- **Q\(_2\)**: Heat loss from the MFD and slurry tank (kW)
- **T\(_\text{hot}\)**: Temperature of the hot source (K)
- **T\(_\text{cold}\)**: Temperature of the cold source (K)
- **Q\(_\text{storage}\)**: Heat required for heat storage tank (kW)
- **Q\(_\text{sol}\)**: Heat supplied by solar collector (kW)
- **Q\(_\text{untreated}\)**: Heat supplied by untreated sewage (kW)
- **W**: Heat supplied by heat pump unit (kW)
- **f**: Solar fraction (%)
- **l_{\text{min}}**: Minimum length of the sewage double-pipe heat exchanger (m)
- **t_{\text{min}}**: The calculation temperature of the sewage in winter (K)
- **t_{\text{in}}**: Average inlet temperatures of the chilled water (K)
- **t_{\text{out}}**: Average outlet temperatures of the chilled water (K)
- **k_{\text{m}}**: Heat transfer coefficient of the heat exchanger (W m\(^{-1}\) K\(^{-1}\))
- **R**: Fouling resistance (m K W\(^{-1}\))
- **h**: Convection heat transfer coefficient of the inner pipe internal surface (W m\(^{-2}\) K\(^{-1}\))

### Table 11: The variation coefficient and weight of each index.

| Index   | \( \nu_j \) | \( a_j \) | \( w_j \) | \( r_j \) |
|---------|--------------|------------|------------|------------|
| EER     | 0.5059       | 0.1505     | 0.2431     | 0.2175     |
| Q\(_\text{in}\) (MJ d\(^{-1}\)) | 0.5032       | 0.1497     | 0.1231     | 0.1113     |
| PC (yuan) | 0.6766     | 0.2013     | 0.2689     | 0.3001     |
| \( \eta_j \) (%) | 0.6247       | 0.1859     | 0.1328     | 0.1542     |
| \( E_{R_j} \) (kg d\(^{-1}\)) | 0.3269       | 0.0972     | 0.1125     | 0.1097     |
| Standard deviation | 0.1450       | 0.04317    | 0.06998    | 0.07795    |
Conflicts of Interest

The authors declare that they have no conflicts of interest.

Acknowledgments

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Abbreviations

SUSSHPS: Solar-untreated sewage source heat pump system
MFD: Multiphase flow digester.

Data Availability

The data used to support the findings of this study are included within the article.
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