All of the Sky: HEALPix Density Maps of Gaia-scale Datasets from the Database to the Desktop

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Abstract. The Gaia Archive provides access to observations of around a billion sky sources. The primary access to this archive is via TAP services such as GACS and ARI-Gaia, which allow execution of SQL-like queries against a large remote database returning a result set of manageable size for client-side use. Such services are generally used for extracting relatively small source lists according to potentially complex selection criteria. But they can also be used to obtain statistical information about all, or a large fraction of, the observed sources by building histogram-like results.

We examine here the practicalities of producing and consuming all-sky HEALPix weighted density maps in this way for Gaia and other large datasets. We present some modest requirements on TAP/RDBMS services to enable such queries, and discuss visualisation and serialization options for the results including some new capabilities in recent versions of TOPCAT.

1. Introduction

The primary data access for Gaia (Gaia Collaboration et al. 2016) and several other past and upcoming large-scale surveys is via Table Access Protocol (TAP) services that allow users to execute SQL-like queries against a large remote database. This model of bringing the computation to the data is enforced by the size of these datasets; client-side transportation, storage and processing of the whole dataset is for most purposes impractical or at least highly inefficient.

The remote database engines are typically powerful and can perform fast execution of complex queries. Where the desired result is some kind of source list of limited size, filtered by criteria such as sky position or photometry down to no more than a few thousand or maybe million objects, selection on source criteria works well. But where the requirement is to sample all or a large fraction of the sources in a catalogue in order to obtain statistical information about all or large regions of the sky, the model of retrieving source lists breaks down, since results with very large row counts are disallowed by the service or simply unwieldy to transport to and process at the client.

It is however possible to calculate in the database histograms representing statistical aggregations of all or many data rows. By binning into a tessellating grid of sky tiles, queries can produce weighted or unweighted sky density maps representing source density or other statistical quantities by sky position. Such queries can be executed in reasonable amounts of time and provide result sets small enough to be transported to the client for examination and analysis.
2. Tiling Scheme

Various sky tiling schemes exist, including HTM, Q3C, and HEALPix. We favour the NESTED variant of HEALPix (Górski et al. 2005) which has a number of advantages for this application, including the facts that tiles have equal area, facilitating density map analysis, and that simple SQL-friendly arithmetic (integer division) can be used to degrade pixel index to a lower resolution. The HEALPix grid at order $N$ defines tiles with indices in the range $[0, 12 \times 4^N)$. A sky position within tile $i$ at order $N$ falls within tile $i/4^{N-M}$ at a lower order (coarser resolution) $M$.

3. Service Requirements

The following items must be in place for end-users to be able to construct and use customised weighted or unweighted all-sky density maps for catalogues that would be impractical to download:

**SQL-like access to source catalogue:** Public datasets are increasingly exposed via the Virtual Observatory protocol TAP (Table Access Protocol), allowing remote execution of ADQL (SQL-like) queries.

**HEALPix column or function:** Either the table must have a column giving the index of the HEALPix tile in which the source position falls, or a User-Defined Function must exist that can calculate tile index for each row (e.g. from RA, Dec columns). Most existing TAP services do not currently provide this, but the ARI-Gaia and DaCHS TAP services have introduced such a UDF (this work):

$$\text{ivo_healpix_index(order, ra, dec)}$$

An order-12 HEALPix index is also buried in bits 36–63 of the Gaia source_id column and can be extracted by integer division.

**GROUP BY query:** An SQL query of the form

$$\text{SELECT (agg-func) FROM (table) GROUP BY (healpix-index)}$$

calculates the sky map, returning one row per populated sky pixel. The aggregate function defines the weighting (e.g. $\text{COUNT(\_)}$ gives unweighted source density, $\text{AVG(x)}$ gives the mean value of column or expression $x$) and a $\text{WHERE}$ clause can optionally be added to restrict the selection of sources.

**Query limits:** Limits on query execution time and output size must accommodate execution of these aggregating queries. They typically take very roughly an hour per billion rows, which is long but not unfeasibly so. Million-row outputs are a convenient size for visualisation (HEALPix order 8 has 786 432 tiles) though finer or coarser resolutions can also be useful. Some TAP services impose limits on execution time or output row count that can preclude these queries.

**Semantic markup of HEALPix output:** An undocumented convention exists for serialization of HEALPix maps in FITS files, but not for VOTable, which is the standard output format for TAP. Discussion is ongoing in the IVOA about how best to do this.
Figure 1. $J - K$ colour for 2MASS point sources, using the query: “SELECT ivo_healpix_index(9,raj2000,dej2000) AS hpx9, AVG(jmag-kmag) AS j_k FROM twomass.data WHERE qflg LIKE 'A_A' AND cflg LIKE '0_0' AND xflg = '0' GROUP BY hpx9”. The proposed User-Defined Function is used to calculate HEALPix index from sky position. The upper right half of the image used the WHERE clause above, which selects only sources with good J/K photometry, while the lower left includes all sources (no WHERE clause). With the custom selection the image is cleaner and the values are lower on average, though not uniformly over the sky. This query took 16/39 minutes to scan 163/471 million rows using the GAVO DC TAP service. Plot by STILTS.

Figure 2. Mean isotropic positional error of Gaia DR1 sky positions, using the query: “SELECT source_id/2199023255552 AS hpx9, AVG(SQRT(ra_error*ra_error+dec_error*dec_error)) AS pos_error FROM gaia.dr1 GROUP BY hpx9”. The HEALPix index is recovered from the Gaia source_id column using integer division. This query took 70 minutes to scan 1.1 billion rows using the GAVO DC TAP service. Plot by STILTS.
4. Analysis in TOPCAT and STILTS

Recent releases of the TOPCAT/STILTS table analysis suite (Taylor 2005) include new features for working with HEALPix maps. Tables with an implicit or explicit HEALPix index column can be visualised interactively or exported to bitmapped or vector graphics files. They can be displayed within TOPCAT’s Sky Plot window which offers interactive adjustment of colour maps and grid resolution, pan/zoom navigation, a choice of sky projections and coordinate systems, and the option to overlay multiple plots of different types. Figures 1 and 2 show examples plotted by STILTS. There are also new capabilities to generate HEALPix maps on the client side from local source catalogues and a number of HEALPix-related functions added to the expression language. Since HEALPix maps are tables, these tools can be used to analyse and manipulate them in general, non-visual ways too, for instance calculating statistics and performing joins.

5. Conclusions

An all-sky or wide-field view of quantities aggregated from a large catalogue can sometimes reveal large scale features or trends in astronomical or instrumental behaviour that would be difficult to discern from other data products. Source density maps are the most obvious application, but there are numerous other possibilities.

Although some data centers (including the ESA and ARI Gaia archives) offer for download various pre-calculated all-sky maps in graphical or tabular form, it is often useful for end-users to construct their own, for instance applying custom source selections or weighting functions not foreseen by data centers. Two examples are given in the figures.

We show that this is feasible using TAP services given certain modest requirements. Although this technique is not novel, the lack of required features in most existing TAP services indicate that it is not widely practised.

To enable more widespread use of this technique, we recommend that TAP services should make available the User-Defined Function ivo_healpix_index(order, ra, dec), and should also consider the case of sky map creation when setting query timeout and row output limits. We also encourage the IVOA to standardise the representation of HEALPix tile indices in VOTables.

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