Galaxy Clusters in the Line of Sight to Background Quasars: II. Environmental effects on the sizes of baryonic halo sizes

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ABSTRACT
Based on recent results on the frequency of Mg\textsc{ii} absorption line systems in the “QSO behind RCS clusters” survey (QbC), we analyse the effects of the cluster environment on the sizes of baryonic haloes around galaxies. We use two independent models, i) an empirical halo occupation model which fits current measurements of the clustering and luminosity function of galaxies at low and high redshifts, and ii) the GALFORM semi-analytic model of galaxy formation, which follows the evolution of the galaxy population from first principles, adjusted to match the statistics of low and high redshift galaxies. In both models we constrain the Mg\textsc{ii} halo sizes of field and cluster galaxies using observational results on the observed Mg\textsc{ii} statistics. Our results for the field are in good agreement with previous works, indicating a typical Mg\textsc{ii} halo size of $r_{\text{Mg} \textsc{ii}} \approx 50h_{71}^{-1}\text{kpc}$ in the semi-analytic model, and slightly lower in the halo occupation number approach. For the cluster environment, we find that both models require a median Mg\textsc{ii} halo size of $r_{\text{Mg} \textsc{ii}} < 10h_{71}^{-1}\text{kpc}$ in order to reproduce the observed statistics on absorption line systems in clusters of galaxies. Based on the Chen & Tinker (2008) result that stronger systems occur closer to the Mg\textsc{ii} halo centre, we find that strong absorption systems in clusters of galaxies occur at roughly a fixed fraction of the cold-warm halo size out to $1h_{71}^{-1}\text{Mpc}$ from the cluster centres. In contrast, weaker absorption systems appear to occur at progressively shorter relative fractions of this halo as the distance to the cluster centre decreases. These results reinforce our conclusions from Paper I and provide additional independent support for the stripping scenario of the cold gas of galaxies in massive clusters by the hot intracluster gas, e.g., as seen from X-ray data.

Key words: galaxies: clusters, galaxies: general, galaxies: structure, galaxies: haloes

1 INTRODUCTION
Understanding the influence of environment on galaxy evolution either in the field or in galaxy clusters, provides important missing clues on the interplay of internal and external mechanisms that shape the galaxy population. In this work we concentrate on the statistics of Mg\textsc{ii} absorption systems in galaxies associated with high-redshift clusters, as recently obtained by Lopez et al. (2008; hereafter 'Paper I'). Our aim is to confront those statistics with different galaxy models in order to constrain the sizes of the cold-warm baryonic component of cluster galaxies. Ever since the first studies of QSO absorption lines, Mg\textsc{ii} was recognized as an excellent tracer of high-redshift galaxies (Bergeron & Stasinska 1986; Petitjean & Bergeron 1990; Steidel & Sargent 2002; Churchill et al. 2000; Lanzetta, Turnshek & Wolfe, 1987, Tytler et al., 1987, Steidel & Sargent, 1992). These seminal works were then followed by numerous studies (Churchill et al. 1999; Nestor, Turnshek &

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\footnote{The temperature of the Mg\textsc{ii} gas is expected to be a few $10^4$ K, and therefore is termed here cold-warm gas. Notice that in some other cases, e.g., in Chen & Tinker (2008), Mg\textsc{ii} is referred to as cold gas.}
Building upon the results presented in Paper I, we perform a theoretical study of Mg\textsc{ii} absorption systems using models to determine how the size of the cold-warm baryonic halo depends on environment. In order to do this we use two different models, (i) a HO model, constructed empirically by Cooray (2006), adopting a ΛCDM cosmology, and (ii) a semi-analytic model by Bower et al. (2006, a version of the GALFORM model by Cole et al., 2000) which follows the evolution of galaxies in a ΛCDM Universe from first principles, tuned to reproduce the observed galaxy population at a wide range of redshifts (other semi-analytic models include Baugh et al., 2005, Croton et al., 2006, Lagos et al., 2008, among others). We then concentrate on determining the cold-warm baryonic halo sizes and their dependence on galaxy environment, without modeling the distribution of gas in a direct way, but instead establishing the required cold-warm halo size needed to reproduce the observed Mg\textsc{ii} absorber statistics presented in Paper I for clusters of galaxies. For simplicity, we start assuming a unity covering fraction and then discuss the implications of this choice.

Throughout this paper the cosmological model adopted is characterised by the “concordance” parameters in line with estimates from the large-scale distribution of galaxies and the temperature fluctuations in the cosmic microwave background (Sánchez et al., 2006), namely, Ω_m = 0.25, Ω_Λ = 0.75, Ω_b = 0.045, a Hubble constant H_0 = 71 × h_{71}km/s/Mpc, with h_{71} = 1, n = 1 and σ_8 = 0.9.

The paper is organised as follows. In Section 2 we briefly review the observational results from Paper I and the additional refinements applied to them to take into account the contamination from the field and the large-scale structure. Section 3 presents the two models in detail. Section 4 describes the results, and a discussion is presented in Section 5. Our conclusions are summarised in Section 6.

2 OBSERVATIONS

In this section we describe the available datasets used for the present work and the corrections we have made to account for contamination from the field and large-scale structures.

2.1 The data

In Paper I we used the Red sequence Cluster Survey (RCS, Gladders & Yee, 2005) to perform a search of clusters in the LOS to background quasars, and constructed two different sets of cluster-QSO pairs. The first set includes 46 high-resolution QSO spectra, and the second comprises lower resolution spectra (these numbers do not include restrictions on signal-to-noise ratios). In all cases, the maximum physical distance between the line-of-sight to QSOs and the cluster centres was set to 2h_{71}^{-1}Mpc, for a total sample of 529 cluster-QSO pairs.

We estimate the median mass of RCS clusters in the sample using the B_{500} parameter (Gilbank et al., 2007) which can be used to estimate individual cluster masses, and correlation functions. All other non-HO models assuming statistical distributions for observational quantities will be referred to simply as Monte-Carlo simulations.
For this work we only take into account results from clusters with at least a 2 - σ detection of $B_{\text{GzR}}$ (that is, 2 - σ away from zero). For this subsample of RCS clusters (all of which are paired to a background QSO for a total of 212 pairs) we find a median mass of $1.64 \pm 0.355 \times 10^{14} h_7^{-1} M_\odot$ (errors correspond to the 20 and 80 percentiles of the mass distribution) which we will use in the remainder of this work.

Clusters in the RCS survey are identified using a likelihood method which fits simultaneously for a projected cluster density profile and a red sequence at different redshifts (see Paper I for more details); this method produces an estimate of the cluster photometric redshift as a by-product. A Mg II system is associated to a RCS cluster when the redshift of the absorption falls within a 1 - σ interval around the cluster photometric redshift. In some cases a given absorption system can satisfy this criterion for more than one cluster, in which case we test two different options, to assign the absorption system (i) to the closest cluster in projection (referred to as "nearest cluster", and (ii) to the farthest cluster in projection ("farthest cluster"). We will show that this choice does not affect our results in a significant way, respectively.

Our subsamples are defined via lower limits of equivalent width (EW). This is particularly important since without a clear modeling of the dependence of the line strength in our models we cannot exclude the occurrence of strong lines, particularly when taking into account indications that these occur closer to the centre of the absorbing galaxy (Chen & Tinker, 2008). We construct (i) sample S:WS (weak and strong systems) which includes all QSO-Cluster pairs from the high resolution spectra, and (ii) sample S:St (strong systems only) which consists of QSO-Cluster pairs selected from the low-resolution data. Notice that sample S:St includes the QSO-Cluster pairs from S:WS (all the available pairs), but only considers absorption systems with EW above the lower limit of 1Å. We define hits in the same fashion as in Paper I, i.e., absorption systems within $\pm \Delta z$ of a cluster redshift, where $\Delta z$ is the uncertainty in the cluster redshift.

Notice that in order to maximize the number of hits, we do not impose the constraints on EW completeness or on pair redshifts used in paper I to correct for cluster completeness. As we show below, these more relaxed sample definitions introduce variations in our results that are negligible when compared to the field and clustering corrections.

### 2.2 Correcting for systematic effects in the Cluster-QSO pair information

The number of hits, $N_{\text{hits}}$, varies with the impact parameter to the cluster centre (see Tables 1 and 2). The number of QSO-cluster pairs is larger than the number of QSOs with measured spectra since in many cases there are two or more clusters in the QSO line-of-sight. Given that a Mg II absorption is associated to a cluster only if the redshift difference is within the cluster photometric redshift error, $\Delta z$, there is a chance that some of these hits will have actually taken place in the field (which corresponds to the average environment including voids and clusters, statistically) rather than in the associated RCS cluster. Therefore, we make a first correction to the number of hits by setting,

$$N_{\text{hits}}^{\text{field}} = N_{\text{hits}} - N_{\text{field}},$$

where the correction from the field takes the form,

$$N_{\text{field}} = \frac{dN}{dz}(z) \times 2\Delta z,$$

with $z$ being the photometric redshift of the cluster, $2\Delta z$ is summed over all clusters considered in a given sample, and $dN/dz$ is the field estimate from the literature. For S:WS, $dN/dz$ is given by

$$\frac{dN}{dz} = 1.9306 + N_{c}(1+z)^{\alpha} \exp\left(\frac{W_{0}}{W_{c}}(1+z)^{-\beta}\right),$$

where the first term corresponds to the Churchill et al. (1999) estimate extended to $0.015A < W_{\text{3796}} < 0.3A$, and the second term corresponds to the Nestor, Turnshek & Rao (2005) estimate for absorbers with EWs higher than $W_{0}$, which in this case is set to $W_{0} = 0.3A$; their published parameter values are $N_{c} = 1.001(\pm 0.132)$, $\alpha = 0.226(\pm 0.170)$, $W_{c} = 0.443(\pm 0.032)$, $\beta = 0.634(\pm 0.097)$ (uncertainties are shown only to illustrate the accuracy of the fit). For sample S:St $dN/dz$ is given by the second term with $W_{0} = 1A$. The adopted redshift corresponds to the median redshift of the RCS cluster sample, median($z$) = 0.6. The field corrections are listed in column 3 of Tables 1 and 2.

It is well known that clusters occupy biased density peaks in the distribution of matter which are characterised by a high amplitude cluster-mass cross-correlation function (see for instance, Croft et al., 1997, Padilla et al., 2001). Hence, a correction has to be introduced to take into account the enhanced matter density around clusters which would increase the occurrence of Mg II absorbers from the field in the surrounding few Mpc around each cluster.

We then proceed to calculate the effect of clustering in the region surrounding the clusters, for which we propose a correction of the form,

$$N_{\text{hits}} = N_{\text{hits}}^{\text{corr}} - N_{\text{corr}},$$

where $N_{\text{corr}}$ includes the expected excess of field hits due to the overdensity around our cluster sample,

$$N_{\text{corr}} = I \times N_{\text{field}},$$

where the factor $I$ is calculated using the cluster-mass cross-correlation function as

$$I = \frac{\int_{r_{\text{cm}}(z) - Y_{c}}^{r_{\text{cm}}(z) + Y_{c}} n(b, y') \langle n \rangle dy + \int_{r_{\text{cm}}(z) + Y_{c}}^{r_{\text{cm}}(z) + Y_{c}} + n(b, y') \langle n \rangle dy}{\int_{r_{\text{cm}}(z) - Y_{c}}^{r_{\text{cm}}(z) + Y_{c}} dy + \int_{r_{\text{cm}}(z) + Y_{c}}^{r_{\text{cm}}(z) + Y_{c}} dy - 1},$$

where the comoving distance in the redshift path is $Y_{c} = \sqrt{r_{\text{0}} - b^2}$, $r_{\text{cm}}$ indicates comoving distance, $r_{\text{0}} = 1.92h_{7}^{-1} \text{Mpc}$ is the median of the radius containing 90 percent of the cluster galaxies for our sample of RCS clusters, $\langle n \rangle$ is the average galaxy density, and $n(b, y')$ is the galaxy density calculated using

$$n(b, y') = \langle n \rangle (1 + \xi_{M}(b, y')).$$

In the last expression, $\xi_{M}(b, y')$ is the cluster-mass cross-correlation function,

$$\xi_{M}(x, y) = \xi_{M}(\sqrt{x^2 + y^2}) = \frac{\chi}{r_{\text{0}}} \gamma,$$

where $r_{\text{0}} = 5h^{-1}\text{Mpc}$ and $\gamma = -1.8$ parametrise the correlation function of the mass (see for instance Padilla et
fourth column includes the effects of clustering for the correction; the fifth column shows the total number of QSO-Cluster pairs.

The third column contains the number of hits corrected from the contribution from the Field; the fourth column includes the effects of clustering for the correction; the fifth column shows the total number of QSO-Cluster pairs.

Table 1. Number of Mg II doublet hits in the S:WS sample (second column) for different ranges of impact parameter to the cluster centre (indicated in the first column). The third column contains the number of hits corrected from the contribution from the Field; the fourth column includes the effects of clustering for the correction; the fifth column shows the total number of QSO-Cluster pairs.

| range in b/h\(^{-1}\)Mpc | N\(_{hits}\) | Field corrected | Clustering corr. | Number of QSO-Cluster pairs |
|--------------------------|---------|-----------------|-----------------|----------------------------|
| 0.0 to 0.5               | 8       | 4.79            | 4.22            | 11                         |
| 0.5 to 1.0               | 5       | 2.41            | 2.05            | 12                         |
| 1.0 to 1.5               | 1       | 0.47            | 0.37            | 13                         |
| 1.5 to 2.0               | 1       | 0.48            | 0.40            | 10                         |

Table 2. Number of Mg II doublet hits in the S:St sample. Columns are as in Table 1.

| range in b/h\(^{-1}\)Mpc | N\(_{hits}\) | Field corrected | Clustering corr. | Number of QSO-Cluster pairs |
|--------------------------|---------|-----------------|-----------------|----------------------------|
| 0.0 to 0.5               | 1       | 0.96            | 0.95            | 14                         |
| 0.5 to 1.0               | 7       | 6.73            | 6.70            | 32                         |
| 1.0 to 1.5               | 2       | 1.92            | 1.91            | 55                         |
| 1.5 to 2.0               | 1       | 0.95            | 0.94            | 66                         |

3.1 Notation and definitions

In the models we will make reference to two distinct types of objects, (i) cluster-mass dark-matter haloes, (ii) and galaxies residing within these clusters. In all cases, the impact parameter will refer to the projected distance in physical units at the comoving distance to the cluster between the QSO line-of-sight and the centre of the cluster (real or simulated); we will use the notation b for this impact parameter. In the case of individual galaxies, we will refer to two separate quantities, (i) the scale-length of the gaseous disk, \(r_{\text{disk}}\), and (ii) the extent of the Mg II halo capable of producing a Mg II absorption feature above a minimum equivalent width, \(W_{\lambda 5796}\), that will be accordingly specified. The Mg II halo in the model galaxies is assumed to be a uniform cloud of constant density with no holes (filling factor of unity; see Section 5.2 for a discussion of the effects of a different value). Finally, in all cases the observational sample to be compared with the models will be characterised by its median equivalent width.

3.2 Halo Occupation Monte-Carlo simulations

The HO model is used in the literature to test whether the properties of individual galaxies depend on their host halo mass (e.g., Cooray, 2005); its parameters can be adjusted using observed galaxy properties such as their clustering (see for instance Zehavi et al., 2004) and luminosity functions in different bands (Cooray, 2006). A HO model does not include physical prescriptions for galaxy evolution, although it can be used to infer the evolution of the population of galaxies in haloes via comparison with observations at various redshifts.

In this first approach we use a HO model with parameters adjusted by Cooray (2006) to match the luminosity function of Sloan Digital Sky Survey (Abazajian et al., 2005) galaxies brighter than r-band absolute magnitudes \(M_r = -17\). This HO model assumes that the number of galaxies per halo depends on the halo mass such that haloes with masses above a minimum value \(M_{\text{min}} = \ldots\)
The figure shows the expected number of hits per QSO-cluster pairs for clusters with median masses of $10^{13.8} M_\odot$ (top panels), increasing to $10^{15.3} M_\odot$ (bottom panels). We show the results for 1, 2 and 3 simultaneous hits (solid, dashed and dotted lines) in the LOS of one target quasar as a function of the median impact parameter, $b_m$, calculated at the median redshift of the RCS cluster sample, median($z$) = 0.6. In this case, we assume two values for the median Mg\textsc{ii} halo sizes, $r_{Mg\textsc{ii}} = 50$ and 80$ h_{71}^{-1}$ kpc (left and right panels, respectively), which correspond to a range of sizes consistent with estimates from absorption systems of field galaxies in QSO spectra (Churchill, 2001, Churchill & Vogt, 2001, Nestor, Turnshek & Rao, 2005). The models show that it is easier to obtain more events of multiple hits when observing more massive clusters as well as when choosing background QSOs closer to the cluster centres. Also, a larger Mg\textsc{ii} halo will produce more hits, as expected. These plots allow us to study the particular case of LOS number 14 from Paper I, where two Mg\textsc{ii} absorption systems overlap with the allowed ranges of photometric redshifts of 6 individual RCS clusters. Using the expected frequency for single and double hits for the median mass of our RCS cluster sample, the resulting likelihood that both Mg\textsc{ii} systems overlap with the allowed ranges can be calculated.

$$r_{Mg\textsc{ii}} = \sqrt{\frac{N_{\text{hits}}}{\pi \sigma(b) N_{\text{LOS}}}}$$

(9)

where we have assumed that all galaxies have equal Mg\textsc{ii} halo sizes.

Figure 1 shows the expected number of hits per QSO-cluster pairs for clusters with median masses of $10^{13.8} h_{71}^{-1} M_\odot$ (top panels), increasing to $10^{15.3} h_{71}^{-1} M_\odot$ (bottom panels).
correspond to only one out of the six clusters is $\simeq 10^4$ times lower than the case where the individual absorptions are associated to two different clusters (out of the available 6). This calculation corresponds to the average impact parameter $b_n = 1200h_{71}^{-1}$kpc, characterising this LOS, and considers the measured median masses of the RCS clusters in our sample (in the case where the double hit and single hit are equally likely, the former are only $\simeq 5$ times less likely to happen than the latter for this LOS). Therefore, from this point on we consider this case as two single hits (Table 1 is constructed accordingly). This would not be the case if the multiple absorption system was consistent with the photometric redshift of a single RCS cluster. This particular LOS offers an excellent laboratory for follow-up spectroscopy of absorbers.

We estimate the relative errors in Mg\textsc{ii} halo sizes, $\Delta r_{\text{Mg}\textsc{ii}}/r_{\text{Mg}\textsc{ii}}$, assuming Poisson statistics and using the frequency of single hits and samples of different total number of QSO-cluster pairs. For this calculation we adopted fixed values of cluster mass, $M = 1.64 \times 10^{14}h_{71}^{-1}M_{\odot}$, and impact parameter, $b = 1339h_{71}^{-1}$kpc, corresponding to the median values in our full sample of QSO-RCS cluster pairs. In Figure 2 we show the variation of $\Delta r_{\text{Mg}\textsc{ii}}/r_{\text{Mg}\textsc{ii}}$ for three different Mg\textsc{ii} halo sizes as a function of the number of QSO-cluster pairs. The vertical grey line indicates the expected errors in the Mg\textsc{ii} halo size for the total number of 529 pairs in sample S:St, and indicates that for sizes larger than $\simeq 50h_{71}^{-1}$kpc, the uncertainties would be below a 25 percent of the inferred size.

We will use this model to infer the typical size of the Mg\textsc{ii} halo and its associated measurement error in the observational data described above.

In what follows, we introduce the details of the additional model which uses a cosmological numerical simulation in combination with a semi-analytic model of galaxy formation.

### 3.3 GALFORM Semi-analytic galaxies

This model differs from the HO in that it follows the evolution of galaxies using a number of physical prescriptions for the different galaxy components, including cold gas, stars, metallicity of stars and gas (hot and cold), and the properties of the central super-massive black hole. However, there is a strong observational component to the model since its parameters are tuned to match the observed galaxy population at various redshifts.

The main advantage in using a semi-analytic model relies on the following. The global properties of large concentrations of matter either in simulations or in observations are well known on average; however, the complex nature of the non-linear collapse that formed virialised objects has important consequences on their diversity, even for objects of similar masses. The properties that are not included in a general description of clusters include their asphericity, substructure and formation history, and their relation to the surrounding environment. Therefore, the use of a cosmological-numerical simulation allows us to include this diversity in the population of cluster-size dark-matter haloes, an effect that is very difficult to include in the model presented in the previous subsection, which relies on Monte-Carlo modeling.

In this work we use the Bower et al. (2006) GALFORM galaxy catalogue which conforms a complete sample of galaxies down to a magnitude $M_r = -17$. These galaxies populate the Millennium Simulation (Springel et al., 2005), which follows the evolution of $\simeq 1 \times 10^{11}$ collisionless dark-matter particles from $z = 50$ to the present on a box of $704.2h_{71}^{-1}$Mpc a side, for a mass resolution per particle of $1.21 \times 10^9h_{71}^{-1}M_{\odot}$. This simulation allows to identify bound dark-matter structures and to follow their descendants at different redshifts. This, in turn, can be used to infer the galaxy population within each dark-matter halo, via various assumptions regarding the different processes that shape the formation and evolution of galaxies in a semi-analytic model (Croton et al., 2007, Malbon et al., 2007, Lagos, Cora & Padilla, 2008, De Lucia et al., 2006).

It is important to note that these galaxies do not include a description of their Mg\textsc{ii} content, and therefore can only be used in a similar way to the HO model procedure. Given that the model follows the evolution of the disk scale-length, $r_{\text{disk}}$ of each individual galaxy with time, we assume that the radius of the Mg\textsc{ii} halos will be,

$$r_{\text{Mg}\textsc{ii}} = A \times r_{\text{disk}},$$

where $A$ is a proportionality constant that will be varied in order to match the observed frequency of Mg\textsc{ii} absorption events. This is an important hypothesis that we will adopt throughout this work, namely, that the size of the Mg\textsc{ii} halo is proportional to the disk size.

Our sample of simulated clusters is constructed by selecting all systems above a minimum mass such that the median mass equals that present in our RCS cluster sample.
3.3.1 Simulated composite cluster

In order to study the frequency of galaxies in front of background QSOs in the numerical model, we construct a composite cluster using all the objects within our sample of simulated clusters. We do this by stacking all the clusters using their most bound particle as their centres; the semi-analytic model by Bower et al. (2006) uses this position to place the central galaxy of each halo. The stacking procedure erases all cluster membership information. Therefore our simulated composite cluster cannot be used to study multiple absorption events from individual clusters. As was mentioned above, the multiple hit candidate present in the data from paper I is considered as two single hits due to its low probability of occurrence.

Given that the population of background QSOs is at a very large distance behind the clusters in our sample, we assume that the former are distributed at random within $2h_{71}^{-1}$ Mpc from the cluster centres, in projection.

3.3.2 Morphological types

Among the information available for each galaxy in the semi-analytic model are the stellar mass in the disk and bulge components. Therefore, it is possible to separate a population of elliptical and spiral galaxies, which may prove important in light of previous results suggesting the presence of strong Mg$\text{II}$ absorption systems mainly in spiral systems (Zibetti et al., 2007).

Therefore, our analysis of number of galaxies in the line-of-sight of background QSOs is done to a first approximation only on spiral galaxies selected so that the stellar content in their bulges is only up to 70 percent of the total stellar mass (Bertone et al., 2007).

We bear in mind that Zibetti et al. (2007) also show that there may be dependencies of the Mg$\text{II}$ absorption on galaxy colour and morphology. Given the simplicity of the approach we follow in this work, we will not attempt to model this dependency but instead will offer estimates on the expected impact of the morphological selection on our results in Section 5.2.

4 RESULTS

In this section we provide separately the results obtained using the two models presented in the previous section, firstly from the observationally motivated Halo Occupation model, and secondly from the semi-analytic model galaxies in the Millennium simulation (Springel et al., 2005).

4.1 HO Model

We use Eq. 9 to determine the sizes of galaxy Mg$\text{II}$ haloes that would produce the rate of hits shown in Table 1 (only calculated for the S:WS sample), for clusters with median mass $1.64 \times 10^{14} h_{71}^{-1} M_{\odot}$. We show the resulting typical sizes in Figure 3 for the total number of hits in the S:WS sample (open squares) and also for the corrected counts by the expected contamination from the field (open pentagons) and clustering (open triangles). The results when considering the “farthest cluster” variant of our S:WS sample fall within the errorbars of these estimates, and therefore are not shown. Errorbars are calculated by assuming Poisson statistics. The points along the abscissa correspond to the middle of the bin in $b$, with small shifts for the different cases, added to improve clarity.

An important change in the inferred Mg$\text{II}$ halo sizes is produced when one of the cluster members is placed at the centre of the cluster (i.e. a central galaxy). This affects the innermost region for which it is straight-forward to infer the expected fraction of line-of-sights that would pass through the central galaxy Mg$\text{II}$ halo once its typical size, $r_{\text{Mg II}}$, is known. This is an iterative process which converges rapidly after three iterations. When taking this into account, the results change quite dramatically for the low impact parameter bin as it is shown by the open star symbols in Figure 3. These results indicate that near the cluster centres, the Mg$\text{II}$ halo of a galaxy could either be as large as $r_{\text{Mg II}} \approx 16 h_{71}^{-1}$ kpc, or as small as $r_{\text{Mg II}} \approx 2 h_{71}^{-1}$ kpc, depending on whether a central galaxy is assumed to lie exactly at the observationally determined cluster centre (which is subject to uncertainties).

Our results show that the typical size of the Mg$\text{II}$ halo tends to increase towards the outskirts of the cluster. This result is independent of the corrections applied to the observational data, and is not sensitive to the presence of a central

![Figure 3. HO Model: Mg$\text{II}$ halo sizes as a function of impact parameter, according to the HO model results. Open squares show the results for the total number of hits in the S:WS sample, open pentagons correspond to the number of hits corrected by the expected field hits, and open triangles show the results from adding the correction for clustering. The open star symbols indicate the resulting sizes when one of the cluster members is positioned at the centre of mass of the cluster. The horizontal solid line indicates the radius of Mg$\text{II}$ haloes in the field obtained from the HO model.](image-url)
galaxy at the centre of mass of the cluster. This is also in reasonable agreement with previous studies that report that the cold/cold-warm gas halo sizes around galaxies may be stripped off by the hot intracluster gas (see for instance Heinz et al., 1999). We also use the HO model to estimate the typical Mg II halo size in the field, which is indicated by the horizontal grey solid line in Figure 3. We estimate this size by integrating over the full range of halo masses where dark-matter haloes are expected to have at least one galaxy with $M_\text{vir} < -17$, for the EW range corresponding to sample S:WS. As can be seen, our estimate of $r_{\text{Mg}\ II} \approx 30h_{71}^{-1} \text{kpc}$ (in broad agreement with observational estimates, e.g. Churchill et al., 1999) is slightly larger than our findings for the inner cluster environment, in agreement with the stripping scenario in clusters. For reference, the galaxy number density in the HO model is $n = 7.639 \times 10^{-3}/h_{71}^{-3} \text{Mpc}^3$. Notice that this result corresponds to the HO model; the results from the analysis of the semi-analytic model for the field are presented in the following subsection.

4.2 GALFORM semi-analytic model

Given the better description of individual clusters allowed by the combination of a numerical simulation and a semi-analytic model, the results from the composite cluster may provide further clues regarding the dependence of Mg II halo on the distance to the cluster centre.

We start by studying the expected typical halo size in the field. In order to do this, we randomly select positions in the simulation and take all the galaxies within $2h_{71}^{-1} \text{Mpc}$ in projection from these centres stacked together. This stack is characterised by a comoving length which we convert to a redshift path. We then place one QSO in the background and sort all the galaxies in the stack with respect to their projected distance to the QSO, and assume that their Mg II halo sizes will be directly proportional to their disk scale-lengths, as was mentioned in Section 3.3. All the Mg II haloes defined this way that contain the LOS to the QSO are counted. We then vary the constant $A$ until the simulation reproduces the same counts per unit redshift path, $dN/dz$, reported by the study of the field by Churchill et al. (1999).

Figure 4 shows the results of the semi-analytic approach. It depicts the distribution of disk scale-lengths in the field (lower x-axis label), where galaxies show a wide range of values with a peak at $r_{\text{disk}} = 6h_{71}^{-1} \text{kpc}$. The top x-axis label shows the resulting Mg II halo sizes, with a distribution peak at a value of $r_{\text{Mg}\ II} \approx 50h_{71}^{-1} \text{kpc}$, well in agreement with the observational estimate of Churchill et al. (1999) for EW $> 0.02 \text{A}$. Also note that our estimate from this approach is only slightly higher than the results from the HO presented in the previous section. This difference arises from the different EW limits assumed in each case (otherwise both results agree with each other).

The analysis of the composite cluster constructed from the GALFORM model also provides useful insights on the size of the Mg II haloes in the cluster environment, and particularly as a function of distance to the cluster centre. In the semi-analytic model, galaxy disk scale-lengths show smaller typical sizes near the cluster centres as can be seen in Figure 5 where we show the median size of galaxy disks (points; errorbars indicate the error of the mean assuming Poisson statistics). This is a first indication that the model indeed includes important environmental effects on the galaxy population (notice that these values are not to be compared to the field Mg II region sizes denoted as $r_{\text{Mg}\ II}$). In the GALFORM semi-analytic model, the physical process driving the environmental changes within clusters is the removal of the hot gas reservoir around galaxies once they enter a new dark-matter halo; this process effectively stops the cooling of gas onto the galactic disk halting its growth.

Following the procedure used to infer the typical sizes of Mg II haloes in the field, we also find the proportionality constant that multiplied by the disk scale-lengths gives a
Figure 6. Semi-analytic model: Histogram of galaxy disk scale-lengths (lower x-axes) and Mg\textsc{ii} galaxy haloes (upper x-axes) needed to reproduce the number of hits in the observations, for different ranges of impact parameter \( b \), shown in the key (increasing values from left to right panels) for the S:WS and S:St samples (top and bottom panels, respectively).

Figure 7. Semi-analytic model: Median sizes of Mg\textsc{ii} haloes as a function of projected distance to the cluster centre. Errorbars show the error of the median.
show the error of the median) for the S:WS (triangles) and S:St (circles) samples. As can be seen from both figures, the trend of a larger galaxy size at larger distances from the cluster centre is clearly found in both samples with values ranging from $r_{75}^{\text{Mg II}} \simeq 2 - 6h_{71}^{-1}\text{kpc}$ at $b < 0.5h_{71}^{-1}\text{Mpc}$ to $r_{75}^{\text{Mg II}} \simeq 25h_{71}^{-1}\text{kpc}$ for $b > 1.5h_{71}^{-1}\text{Mpc}$, in good agreement with the HO results with a central galaxy. The corresponding inferred size for typical Mg II haloes in the field for the range of EW in sample S:WS for the semi-analytic model is $40h_{71}^{-1}\text{kpc}$ (notice that this value differs slightly with the result from Figure 4, due to the different EWs considered).

We remind the reader that these results are motivated by the observational frequency of Mg II absorption systems in our samples of RCS cluster-QSO pairs (the proportionality constant in Eq. 10 depends on the impact parameter). Therefore, the trends of smaller Mg II halo (cf. Fig. 5) and disk sizes (cf. Fig. 6) towards the cluster centres are independent results. Furthermore, the reasonable consistency between the results from the HO model and the semi-analytic simulation provides further reliability to the findings on the trends of Mg II halo size with the distance to the cluster centre.

5 DISCUSSION

In the previous section we studied the inferred typical Mg II halo sizes using two different models, the HO and the output from a semi-analytic simulation. We find that both models are able to reproduce the observed frequency of Mg II absorption events found in observational data in Paper I. More importantly, our results indicate that the Mg II halo sizes tend to increase from relatively low values of $r_{75}^{\text{Mg II}} \simeq 2 - 6h_{71}^{-1}\text{kpc}$ to $r_{75}^{\text{Mg II}} \simeq 25h_{71}^{-1}\text{kpc}$ for $b = 0.5h_{71}^{-1}\text{Mpc}$ to $b > 1.5h_{71}^{-1}\text{Mpc}$; both models produce consistent results.

In what follows, we present a study of the fraction of the Mg II halo responsible for producing different Mg II absorption line strengths, and an analysis of possible systematic effects present in our current measurements.

5.1 Regions of strong Mg II absorption line systems

We take full advantage of the additional information available in the semi-analytic model regarding the galaxy disk scale-lengths, and combine this with previous results by Chen & Tinker (2008) who find that stronger absorption systems are produced by clouds closer to the galaxy centre to study the typical size of the regions in the Mg II halo responsible for different absorption line strengths.

In our analysis of the semi-analytic model we maintain a record of the distance, $d$, between each QSO line-of-sight and each galaxy centre. Therefore, after finding the proportionality constant $A$ (Eq. 10) that reproduces the frequency of hits found in Paper I, we can sort the galaxies with respect to $d$. Then, for different ranges of cluster-centric impact parameter, we study the observed fractions of different line-strengths, and find the galacto-centric distance out to which the same fractions of model galaxies are included. Such a distance is then identified as the maximum distance out to which a given line-strength would be produced in the model. Figure 8 presents the resulting fraction of the Mg II halo size out to which a given line-strength occurs, as a function of distance from the cluster centre. This rescaling is adopted in order to factor out the measured variation of the global Mg II halo size with the impact parameter to the cluster centre. Open and solid symbols represent high ($W_0^{T796} > 2\text{Å}$) and low ($W_0^{T796} < 2\text{Å}$) equivalent width absorption systems, respectively; triangles correspond to results from the S:WS sample, circles to S:St. In the case of the high equivalent width results, the large errorbars only allow a possible rejection of an increase of the Mg II halo region producing such absorption events. However, there is a mild indication that the low equivalent width absorption systems (all from S:WS) tend to occur at increasingly larger distances from the galaxy centre in terms of the Mg II halo size towards the outskirts of clusters. These results are again in good agreement with the stripping scenario, where the low density Mg II clouds within a given galaxy would be more easily removed than the denser Mg II regions nearer the galaxy centre that would be responsible for high equivalent width absorption systems.

5 Notice that the Mg II halo size at $b > 1.5h_{71}^{-1}\text{Mpc}$ is not expected to resemble the Mg II halo size inferred for the field since this sample contains only galaxies in high mass dark-matter haloes, and therefore does not include a representative sample of field galaxies, even in the cluster outskirts.

6 In their terminology this would be a halo centre, which can be applied to each galaxy in the semi-analytic model since these are located at the centres of bound substructures (or sub-haloes) in the numerical simulation.
5.2 Possible systematic effects

The parametrisation of both models, HO and semi-analytic, used to mimic the observational procedure carried out in Paper I, depends on a number of parameters, assumptions and measurements that can induce systematic effects.

For instance, the results shown in the previous sections were obtained for clusters of a median mass corresponding to the estimates for the RCS clusters. In order to assess the possible systematic biases arising from errors in these cluster mass measurements we change the adopted median mass by factors of 4 and 0.25, approximately 0.6dex in the cluster mass. The results in the HO and semi-analytic models are affected by very similar relative variations, which do not show a dependence with the distance to the cluster centre. When the lower value for the median mass is adopted, the inferred median sizes of the Mg\textsc{ii} haloes increases by \(\sim 10\) percent; alternatively, a higher median mass produces a decrease in the inferred size by a \(20 - 25\) percent. Given that the effect does not vary with the distance to the cluster centre, our conclusions would not be significantly affected by this source of systematic uncertainties.

It should also be taken into account that in our modeling, we have considered spherical Mg\textsc{ii} haloes. Given the lack of detailed information on the thickness of cold gas disks, we do not venture into assuming a given disk thickness in this work, as has also not been done in previous works studying the size of Mg\textsc{ii} absorption regions in the field as in Churchill et al. (2001).

It has been argued that a unity covering fraction for Mg\textsc{ii} haloes is rather unlikely (Bechtold & Ellingson, 1992, Tripp & Bowen, 2005, Chen & Tinker, 2008, Kacprzak et al., 2008). Since the models we have adopted here assume a fixed value for the covering fraction (which we have chosen to be \(C = 1\)), we cannot study a possible dependence with environment. However, it is easy to see that a different covering fraction will change our results on the Mg\textsc{ii} halo sizes according to \(r_{\text{Mg\textsc{ii}}} \propto r_{\text{gal}}\).

Finally, the effect from considering absorption from low gas content galaxies should also be taken into account. In the semi-analytic model, the fraction of elliptical galaxies changes as a function of the distance to the cluster centre. This is specially true for \(r/r_{\text{vir}} < 1\), where the fraction of model elliptical galaxies (see Section 3.3.2) increases from \(\sim 15\) percent to \(\sim 50\) percent at \(r/r_{\text{vir}} = 0.015\), measured in projection (these fractions are in good agreement with results from the SDSS from Goto et al., 2003). At larger distances from the cluster centres, the fraction of elliptical galaxies remains practically unchanged. For sample S:WS (and similarly for sample S:St), considering an absorption from elliptical galaxies in the semi-analytic model would increase by a factor of \(\sim 1.43\) the number of potential absorbers and therefore decrease our estimate of the typical Mg\textsc{ii} halo size inside clusters by \(16\) percent. Our estimates at larger distances from the cluster centre will be equally affected by a decrease of approximately \(7.8\) percent. The latter estimate would also change our estimates for the typical Mg\textsc{ii} halo size inferred for the field accordingly in both, the semi-analytic and HO models. In consequence, our conclusions do not change significantly due to this effect.

6 SUMMARY AND CONCLUSIONS

In this paper we have presented a theoretical study of Mg\textsc{ii} halo sizes of galaxies in clusters and in the field, by comparing recent observational results on the incidence of Mg\textsc{ii} absorption systems in RCS cluster-QSO pairs by Lopez et al. (2008), and the predicted systems from the Halo Occupation and Semi-analytic models.

As a first step in our analysis we applied corrections to the observed frequency of absorption events to take into account possible contaminations from the field, and effects of the Large-Scale Structure.

The results from the HO and semi-analytic models indicate that the typical field Mg\textsc{ii} halo is \(r_{\text{gal}} \approx 39 - 50 h_{71}^{-1}\) kpc (for EW > 0.02\(\AA\)), a value in broad agreement with previous results pointing towards \(r_{\text{gal}} \approx 50 - 100 h_{71}^{-1}\) kpc found for similar absorber EWs (Churchill et al., 2001, Zibetti et al., 2007, Chen & Tinker, 2008, Kacprzak et al., 2008).

The HO model also indicates that the Mg\textsc{ii} halo tends to be smaller near the cluster centres, reaching values of \(r_{\text{gal}} \approx 16 h_{71}^{-1}\) kpc. When one of the cluster members occupies the centre of mass of the cluster, the Mg\textsc{ii} halo size can be as low as \(\approx 2 h_{71}^{-1}\) kpc. This result is obtained assuming a fixed galaxy size for all the cluster members. The results from the Semi-analytic model are consistent with those from the HO showing a clear decrement in the typical Mg\textsc{ii} size towards the cluster centres. An interesting by-product of this analysis is that the galaxy disk scale-lengths in the model also show a clear increase towards the outskirts of clusters, in accordance with the scenario where strong interactions strip galaxies of their outer disks in cluster environments.

We also used the semi-analytic model to estimate the radii of Mg\textsc{ii} haloes producing different strengths of absorption. In order to do this we assumed that stronger lines are produced nearer the centres of galaxies (following Chen & Tinker, 2008). We found that in terms of the Mg\textsc{ii} halo size, the strong absorption regions occur out to a rather fixed value, independent of the distance to the cluster centre. However, weaker absorption line systems show a tendency to occur at larger distances from the galaxy centre (in units of their global Mg\textsc{ii} halo radius) towards the outskirts of clusters. This trend could explain the flatter EW distribution found in paper I, that included all impact parameters within \(b < 2 h_{71}^{-1}\) Mpc.

Our results indicate that the effect of the cluster environment on galaxies is extremely important and can produce a decrement of up to a 90 percent of the Mg\textsc{ii} halo size with respect to galaxies in more gentle environments such as the field.

7 This is an upper limit for the contribution of ellipticals to the projected galaxy number density at a median impact parameter of \(b/r_{\text{vir}} = 0.17\). This value corresponds to the first bin in our measurements of \(r_{\text{Mg\textsc{ii}}}\), \(b < 500 h_{71}^{-1}\) kpc, for the median virial radius of the clusters, \(r_{\text{vir}} = 775 h_{71}^{-1}\) kpc.

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