Influence of local strain caused by cycloaddition on the band gap control of functionalized single-walled carbon nanotubes†

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Fine control of the band gap of single-walled carbon nanotubes (SWNTs) has been achieved by the functionalization with dibromoalkanes, namely, 1,3-dibromopropane (1a), 1,4-dibromobutane (1b), 1,5-dibromopentane (1c), and 1,8-bis(bromomethyl)naphthalene (1d). Red-shifted photoluminescence (PL) peaks observed at 1215–1242 nm were assigned to the local band gaps of the chemically functionalized SWNTs 2a, 2b, 2c, and 2d, respectively. Density functional theory (DFT) and time-dependent DFT calculations for 2a–2d suggest that “local strain” induced by cycloaddition plays an important role in tuning the local band gap energies of functionalized SWNTs.

Introduction

Single-walled carbon nanotubes (SWNTs) have attracted significant interest due to their remarkable mechanical stability and intrinsic optical and electrical properties.1–3 Their various electronic states based on the diameter and helicity make SWNTs attractive as the building blocks of electronic and optical nanodevices.4 In 2002, near-infrared (NIR) photoluminescence (PL) of semiconducting SWNTs was observed in individually dispersed SWNTs.5 PL measurements of SWNTs have been used as a useful analytical method to assign SWNT structures because the first (E11) and second (E22) optical transition energies can be identified from the excitation and emission energies. As NIR photoluminescence materials, SWNTs are expected to be of practical use in the imaging of biological tissues, telecommunications, and other applications.6–8 Recently, it has been reported that the chemical functionalization of SWNTs, such as photooxidation, arylation, and alkylation, induces bright and red-shifted NIR PL peaks.9–19 Based on density functional theory (DFT) calculations, it was proposed that the new PL peak is derived from splitting of the frontier orbitals of SWNTs by sidewall functionalization.20 Miyauchi et al. reported that the PL quantum yield of SWNTs (typically ~1%) was increased by at least one order of magnitude (to ~18%) by oxidation at a moderate functionalization degree.21

Wang et al. reported the observation of new PL peaks in the range of 1110–1148 nm (PL) from arylated (6,5) SWNTs depending on the substituents of the phenyl group. A good correlation was found between this emission wavelength and Hammett’s constant, which revealed that the electronic effect of the substituent is one of the factors in emission wavelength control.13 Furthermore, Wang et al. reported that the emission wavelength can be controlled by the number of fluorine atoms in fluoroalkylated SWNTs.22 Recently, we reported that the dialkylation of (6,5) SWNTs using butyllithium and butyl bromide and their subsequent thermal treatment resulted in a new strong PL peak at around 1220 nm (E11 PL).15 Additionally, (6,5) SWNTs functionalized using 1,2-bis(bromomethyl)benzene predominantly resulted in a new PL peak at 1231 nm.15 These results indicate that controlling the distance of the addition site carbons on the SWNTs is another factor that controls the emission wavelength. The contribution of the addition site carbons on the SWNTs is another factor controlling the emission wavelength of functionalized SWNTs. Yang et al. reported theoretical studies showing that the electronic states of pristine SWNTs varied with strain and that the changes in the band gap depend on their chirality and deformation mode.22,23 Pioneering experimental work on tuning the electronic properties of pristine SWNTs with mechanical strain by monitoring the change in band gap and PL in response to applied strain have also been reported.24–26
The introduction of a cyclic addenda on the SWNT can be expected to produce local strain depending on the alkyl chain length. In addition, changes in the local band gap energy can be measured with high sensitivity by PL measurements. In the present study, we functionalized SWNTs using dibromoalkanes, 1a–1d, to clarify the influence of the local strain induced by cyclic addenda on the red-shifted PL wavelength of functionalized SWNTs. These dibromoalkanes have been used for the synthesis of cyclization products of fullerene C60.27,28

**Experimental**

**General information**

The (6,5)-enriched SWNTs (SG 65i), used in this work, were purchased from Sigma-Aldrich. Reagent-grade dibromoalkanes were purchased from commercial suppliers. 1d was synthesized according to literature procedure.29 Optical absorption spectra were recorded by using a spectrophotometer (V-670; Jasco Corp.) equipped with a Pyrex cell with a 10 mm path length. In addition, Raman spectra were measured under excitation at 514.5, 561, and 633 nm, by using a spectrophotometer (LabRAM HR-800; Horiba Ltd.). These spectra were normalized relative to the G band. Photoluminescence spectra were obtained by using a spectrophotometer equipped with a 450 W lamp and a Symphony-II CCD detector (Nanolog; Horiba Ltd.). The excitation and emission wavelengths were varied from 500–1000 nm and 827–1400 nm, respectively, in 1 nm steps. The excitation and emission slit widths were 10 nm. The PL intensity was corrected to the data correction time of each sample. For absorption and PL measurements, the samples were dispersed in D2O containing 1 wt% sodium dodecylbenzene sulfate (SDBS) by ultrasound irradiation in a bath sonicator (B2510J-MT ultrasonic cleaner; Branson) and centrifuged at 140 000 g. Scanning electron microscopy (SEM) was conducted using a Hitachi Ltd.). Thermogravimetric analysis (TGA) of the samples was performed at a heating rate of 10 °C min−1 and washed with tetrahydrofuran, methanol, and distilled water by the dispersion/filtration process. The resulting films were analyzed with Raman spectroscopy and used for preparation of SWNT dispersion.

**Computational details**

A single unit of pristine (6,5) SWNT passivated with hydrogen at the terminals was utilized as the computational model. SWNT-C8H8, SWNT-C12H10, SWNT-C16H10, and SWNT-C20H10 adducts were calculated at the ortho and para positions in three different directions (L−33, L87, L27), as shown in Fig. 2. The ground state of these derivatives was optimized by DFT using the B3LYP functional with 6-31G*.31–33 The TD-DFT calculations of the vertical transition energies and the optimization of excited states were performed at the B3LYP/3-21G level of theory. To evaluate the effects of the distortion of the nanotube and π-conjugation of the C12H10 adduct on the transition energy, we also examined SWNT-(CH3)2 with the same nanotube structure as SWNT-C12H10. Aliphatic addenda were also examined in the same manner. All DFT calculations were conducted using the Gaussian 09 suite of programs version E.01.34

**Results and discussion**

The alkylation of SWNTs was conducted using commercially available (6,5) SWNT-enriched SWNTs, sodium naphthalenide, and dibromoalkanes (1), as shown in Scheme 1.35,36 The functionalization degree of the alkylated SWNTs (2) was evaluated by the characteristic absorption peak intensity at ~980 nm (E11) and the intensity ratio of the D band to the G band (D/G ratio: [D/G]) in the Raman spectra (Fig. 1).37 The E11 abs. ratio is used as an index for the degree of functionalization of SWNTs, and is defined by the relative peak intensity, [E11 absorption intensity of 2/absorption intensity of local minimum near 775 nm of 2]/[E11 absorption intensity of SWNTs/absorption intensity of local minimum near 775 nm of SWNTs]:

\[
E_{11} \text{ abs. ratio} = \frac{\text{Relative } E_{11} \text{ peak intensity of 2}}{\text{Relative } E_{11} \text{ peak intensity of SWNTs}} \quad (1)
\]

The local minimum at ~775 nm was selected for the normalization because there is no characteristic absorption peak at that wavelength, and the absorbance of the characteristic peaks changed only in the photoreaction of SWNTs with aliphatic amines.38 As shown in Table 1, higher D/G values and a larger decrease of the E11 abs. ratio were observed for 2a and

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**Table 1**

| SWNTs | Sodium Naphthalenide | Alkylated SWNTs |
|-------|---------------------|-----------------|
| 1a    | 2                   | 1               |
| 1b    | 3                   | 2               |
| 1c    | 4                   | 3               |
| 1d    | 5                   | 4               |

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**Figure 1**

[Diagram showing the chemical structure of SWNTs and alkylated SWNTs with functionalization degree.]
2b than for 2c and 2d, indicating that 2a and 2b have higher functionalization degree than 2c and 2d. It is well known that in the cyclization reaction of alkenyl radicals, the yields increase in the order of the formation of 7-, 6-, and 5-membered rings. The high functionalization degrees of 2a and 2b are consistent with the typical radical cyclization (Scheme 1).

Fig. 1c shows the PL spectra of 2a–2d normalized to the \( E_{11} \) PL peaks. \( E_{11} \) PL peaks were observed in the spectra of 2a–2d, as dominant peaks, at 1215, 1230, 1231, and 1242 nm, respectively. The excitation spectra of these emissions are in good agreement with the absorption spectra of (6, 5) SWNTs, indicating that the PL peaks assigned to the functionalized (6, 5) SWNTs (Fig. 1d). When bromoalkane was used for the reaction, an \( E_{11} \) PL peak at approximately 1100 nm and an \( E_{11} \) PL peak emerged as a function of the reaction.

Independently, Shiraki and Nakashima et al. reported that two new PL peaks at 1129 and 1253–1258 nm emerged in the reaction of SWNTs with reagents having two reactive benzene diazonium moieties. The selective emergence of the \( E_{11} \) PL peaks in 2a–2d, similar to that in SWNTs functionalized using 1,2-bis(bromomethyl)benzene, indicates that a highly selective cyclization addition was proceeded in the reaction of SWNTs with 1a–1d.

It is noteworthy that the \( E_{11} \) PL peaks in 2a–2d were observed to vary in the range of 1215–1242 nm when changing the alkyl chain length. Wang et al. reported that the emission energy of functionalized (6,5) SWNTs by mono-substituted phenyl group can be controlled between 1110 and 1148 nm depending on the introduced electron withdrawing and electron donating groups in the phenyl groups. The difference in the electronic effects of 1a–1c is presumed to be small because difference of 1a–1c is the number of methylene units. It was reported that the wave-number of Raman peaks is sensitive to the doping and mechanical strain of SWNTs. No significant difference of the

### Table 1

| SWNTs   | \( E_{11} \) abs. ratio | 514.5 nm | 561 nm | 633 nm | \( E_{11} \) PL peak |
|---------|--------------------------|---------|-------|-------|---------------------|
| 2a      | 0.45                     | 0.44    | 0.32  | 0.40  | 1215 nm             |
| 2b      | 0.40                     | 0.46    | 0.36  | 0.35  | 1230 nm             |
| 2c      | 0.61                     | 0.28    | 0.24  | 0.23  | 1231 nm             |
| 2d      | 0.66                     | 0.28    | 0.26  | 0.24  | 1242 nm             |
wavenumber corresponding to the red shifted PL peaks was observed for 2a–2d (Fig. S2†), supporting that the addenda influence locally at the addition sites. Previously, we reported the PL properties of butylated SWNTs having different functionalization degree.41 Two butylated SWNTs have a large difference in the functionalization degree, but a small difference in new red-shifted PL wavelength (Fig. S5†). In contrast, 2a–2d have a small difference in the functionalization degree compared to butylated SWNTs, but a large difference in the PL wavelength, suggesting that the effect of the functionalization degree on the new PL peak wavelength is small in 2a–2d.

Therefore, the differences in the PL wavelength in 2a–2c might be due to the local strain of the SWNTs induced by the cyclic addenda. The effect of the naphthyl unit on the Stokes effect of 2d compared with that of 2c was considered by theoretical calculation which is discussed later.

To clarify the PL properties of 2, we performed DFT and TD-DFT calculations. We considered six model structures of cyclized adducts with different addition positions. These isomers are distinguished using the abbreviations reported by Htoon and coworkers (Fig. 2a).23 The optimized structures of the isomers 2a–2d are shown in Fig. 2c. The calculation results showed that the ortho L–33 isomer is the most stable isomer, regardless of the functional groups (Fig. 2d). To address the local distortion of 2a–2c, we focus on the bond angles defined in Fig. 2b. The sum of the three bond angles (\(a_1 + a_2 + a_3\)) approaches the value of the ideal sp\(^3\) carbon in the order of SWNT < SWNT-(C\(_3\)H\(_6\)) < SWNT-(C\(_4\)H\(_8\)) < SWNT-(C\(_5\)H\(_10\)) regardless of the addition position (Fig. 3, Tables S2 and S3†). The results indicate that the number of methylene units in the cyclic addenda affects the degree of local strain of the SWNT skeleton.

The absorption energies of ortho L–33, ortho L–87 and ortho L–27 isomers were calculated using TD-DFT with B3LYP/3-21G. As shown in Fig. 3 and Table 2, the calculated absorption energies strongly depend on their addition position, and increase in the order of SWNT-(C\(_{12}\)H\(_{10}\)) < SWNT-(C\(_4\)H\(_8\)) < SWNT-(C\(_5\)H\(_10\)) when compared at the same addition position. Because of the high computational cost of the geometry optimization of the excited state, we calculated the emission energies of ortho L–33 isomers as selected examples. The calculated emission energies showed a similar tendency to the calculated absorption energy with similar Stokes shifts regardless of the adducts (Table S4†). In order to evaluate the influence of alkyl chain length of acyclic addenda, estimation of absorption energies of SWNT-(C\(_3\)H\(_6\)Br), SWNT-(C\(_4\)H\(_8\)Br), H-SWNT-(C\(_3\)H\(_6\)Br), and H-SWNT-(C\(_4\)H\(_8\)Br) was conducted. The calculated absorption energies of SWNT-(C\(_4\)H\(_8\)Br) and SWNT-(C\(_5\)H\(_10\)Br) show no significant difference, which is also found in those of H-SWNT-(C\(_3\)H\(_6\)Br) and H-SWNT-(C\(_4\)H\(_8\)Br) (Table S7†). These theoretical calculation results agree well with the experimental results and show that the PL wavelength of SWNTs can be effectively controlled by the alkyl chain length of the cyclic addenda.

To evaluate the effect of the naphthyl unit of 2d, the absorption energy of SWNT-(CH\(_2\))\(_2\) was calculated. The structure of SWNT in SWNT-(CH\(_2\))\(_2\) was taken to be the same as that in SWNT-(C\(_{12}\)H\(_{10}\)) (Fig. 2c). Thus, the distortion of the SWNT in SWNT-(CH\(_2\))\(_2\) is identical to that in SWNT-(C\(_{12}\)H\(_{10}\)).

The optimized structures of the cyclized adducts (Table S4†) were calculated using TD-DFT with B3LYP/3-21G. Different orientations in ortho adducts are marked in the same manner as in Fig. 2.

![Fig. 3](image)

**Fig. 3** Sum of bond angles at the addition sites in functionalized (6,5) SWNTs (black lines represent the addition position “a”, and red lines represent the other addition position in ortho adducts). Calculated absorption energy of functionalized (6,5) SWNTs (blue line) using TD-DFT with B3LYP/3-21G. Different orientations in ortho adducts are marked in the same manner as in Fig. 2.

### Table 2: Calculated absorption wavelength of functionalized (6,5) SWNTs using TD-DFT with B3LYP/3-21G

| Addition positions | SWNT-(C\(_3\)H\(_6\)) | SWNT-(C\(_4\)H\(_8\)) | SWNT-(C\(_5\)H\(_10\)) | SWNT-(C\(_{12}\)H\(_{10}\)) | SWNT-(CH\(_2\))\(_2\)\(^a\) |
|--------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| ortho L–33         | 880                  | 885                  | 892                  | 896                  | 889                  |
| ortho L–87         | 920                  | 934                  | 936                  | 941                  | 935                  |
| ortho L–27         | 1099                 | 1120                 | 1121                 | 1130                 | 1119                 |

\(^a\) The structure of SWNT in SWNT-(CH\(_2\))\(_2\) was taken as the same as that in SWNT-(C\(_{12}\)H\(_{10}\)).
Fig. 4 Frontier molecular orbital diagrams of ortho and para adducts for SWNT-(C\textsubscript{5}H\textsubscript{10}) (B3LYP/6-31G*, isovalue = 0.02).

The absorption energy of SWNT-(CH\textsubscript{3})\textsubscript{2} is similar value to that of SWNT-(C\textsubscript{6}H\textsubscript{10}), indicating that the naphthyl unit of 2d contributes to the larger red-shift of 2d than 2c.

Focusing on the frontier orbitals, the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) of the ortho L\textsubscript{25} isomer are the most localized in the ortho isomers (Fig. 4, S12 and S13\textsuperscript{†}). In the para isomers, HOMO and LUMO orbitals of para L\textsubscript{33} are the most localized. The degree of localization of the frontier orbital correlates well with the trends in the HOMO-LUMO gap energies, which are shown in Table S5.\textsuperscript{†} This result is consistent with the results of hydrophenylated SWNT isomers reported by Htoon et al.\textsuperscript{42}

**Conclusions**

In conclusion, we studied the PL properties of functionalized SWNTs using dibromoalkanes. After functionalization, new PL peaks were emerged as a dominant peak in the range of 1215–1242 nm depending on the alkyl chain length of the dibromoalkane used. The functionalization degree of the alkylated SWNTs were strongly influenced by the alkyl chain length of the addenda. The DFT calculations showed that the structural changes in the SWNTs increased with increasing alkyl chain length of the cyclic addenda. In addition, theoretical calculations revealed that the naphthyl unit and the length of the alkyl group in the addenda influence the absorption and emission energy of functionalized SWNTs. We expected that these findings will broadly impact the fundamental understanding of the intrinsic PL properties of SWNTs and will be useful for the development of photonic devices, bioimaging, strain sensing, and other applications.

**Conflicts of interest**

There are no conflicts to declare.

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