ISOPHOTE SHAPES OF EARLY-TYPE GALAXIES IN MASSIVE CLUSTERS AT $z \sim 1$ AND 0

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Received 2016 April 5; revised 2016 November 9; accepted 2016 November 10; published 2017 January 6

ABSTRACT

We compare the isophote shape parameter $a_4$ of early-type galaxies (ETGs) between $z \sim 1$ and 0 as a proxy for dynamics to investigate the epoch at which the dynamical properties of ETGs are established, using cluster ETG samples with stellar masses of log($M_*/M_\odot$) $\geq$ 10.5 which have spectroscopic redshifts. We have 130 ETGs from the Hubble Space Telescope Cluster Supernova Survey for $z \sim 1$ and 355 ETGs from the Sloan Digital Sky Survey for $z \sim 0$. We have developed an isophote shape analysis method, which can be used for high-redshift galaxies and has been carefully compared with published results. We have applied the same method for both the $z \sim 1$ and 0 samples. We find similar dependence of the $a_4$ parameter on the mass and size at $z \sim 1$ and 0; the main population of ETGs changes from disky to boxy at a critical stellar mass of log($M_*/M_\odot$) $\sim$ 11.5 with the massive end dominated by boxy. The disky ETG fraction decreases with increasing stellar mass both at $z \sim 1$ and 0, and is consistent between these redshifts in all stellar mass bins when the Eddington bias is taken into account. Although uncertainties are large, the results suggest that the isophote shapes and probably dynamical properties of ETGs in massive clusters are already in place at $z > 1$ and do not significantly evolve in $z < 1$, despite significant size evolution in the same galaxy population. The constant disky fraction favors less violent processes than mergers as the main cause of the size and morphological evolution of intermediate mass ETGs in $z < 1$.

Key words: galaxies: clusters: general -- galaxies: elliptical and lenticular, cD -- galaxies: evolution -- galaxies: photometry -- galaxies: structure

1. INTRODUCTION

Understanding the formation and evolution of early-type galaxies (ETGs) is one of the main topics in modern astronomy because they are important ingredients in the universe. ETGs, also referred to as ellipticals and S0s, are one of the major galaxy populations. The evolution histories of ETGs are imprinted in dynamics, stellar populations, and shapes.

Dynamics of ETGs provide crucial knowledge about their formation and evolution histories. There is a well-known parameter correlation between the luminosity, velocity dispersion, and size, i.e., the Fundamental Plane (Djorgovski & Davis 1987), which combines the correlation between the total luminosity and velocity dispersion (Faber & Jackson 1976), and that between the size and surface brightness (Kormendy 1977). Using integral field spectroscopic (IFS) data of 260 local ETGs (Cappellari et al. 2011a), Cappellari et al. (2013b) obtain a robust stellar mass estimator, and confirm the mass-to-luminosity ratio ($M/L$) variation as a function of velocity dispersion, with which the Fundamental Plane can be interpreted as virial equilibrium (e.g., Djorgovski & Davis 1987; Prugniel & Simien 1996; Forbes et al. 1998), which implies that the Fundamental Plane can be reduced to the mass--size plane (see Cappellari 2015 for a review).

Emsellem et al. (2007, 2011) analyze the IFS data and classify ETGs, using the specific angular momentum, into fast rotators whose dynamics is dominated by rotation and dispersion-dominated slow rotators. Considered on the mass--size plane, the specific angular momentum of ETGs varies as a function of constant velocity dispersion assuming a virial relation. The massive end of ETGs is dominated by slow rotators whereas lower mass systems are basically fast rotators (see Figure 8 in Cappellari et al. 2013a). A similar trend is also found in the tridimensional structure, i.e., massive ETGs are spherical whereas less massive ones are flattened, oblate spheroids (Figure 7 in Cappellari et al. 2013a).

The stellar population is also important to discuss the formation and evolution of ETGs. Local ETGs are known to populate a tight red sequence in the color–magnitude or color–stellar mass diagram (Baum 1959; Faber 1973; Visvanathan & Sandage 1977; Baldry et al. 2004, 2006), because they have rather homogeneous old and metal-rich stellar populations (e.g., Bower et al. 1992; Kodama & Arimoto 1997). Analyzing stellar absorption features obtained from galaxy spectra has revealed that more massive ETGs are older, more metal-rich, and have more $\alpha$ element enhancement, which implies shorter star formation timescales (Worthey et al. 1992; Thomas et al. 2005, 2010). Considered on the mass–size plane, unlike dynamical properties, the stellar population parameters such as the stellar age, metallicity, and star formation timescales (McDermid et al. 2015) as well as molecular gas fraction (Young et al. 2011; Cappellari et al. 2013a) are constant as a function of constant velocity dispersion. On the other hand, with increasing velocity dispersion, the stellar populations become older, more metal-rich and more $\alpha$ element enhanced with shorter formation timescales, and galaxies have lower molecular gas fractions (Cappellari et al. 2013a; McDermid et al. 2015). Because the bulge fraction also increases with increasing velocity dispersion (Cappellari et al. 2013a, and
To explain the different correlation of dynamics and stellar population to the velocity dispersion, a two-phase formation scenario is favored, i.e., a massive compact fast-rotating bulge is formed by dissipative processes such as gas inflow or wet mergers at high redshift ($z > 2$) when the universe is much more gas rich, and dissipationless processes such as dry minor or major mergers increase the galaxy size (e.g., Khochfar et al. 2011; Cappellari et al. 2013a; Dekel & Burkert 2014, and references therein). Because dry mergers reduce angular momentum of the fast-rotating bulge and alter it into slowly rotating ETGs (Khochfar & Burkert 2005; Naab et al. 2006) without changing the stellar population, the dynamical properties vary in the mass–size plane as a function of constant velocity dispersion with the massive end of ETGs dominated by slow rotators while the stellar population becomes constant.

Khochfar et al. (2011) investigate the evolution of the ratio of fast to slow rotators using the semi-analytic galaxy formation model, and present that the ratio evolves in $z < 2$ such that the fast to slow ratio decreases with decreasing redshift due to dry mergers. The size evolution observed in $z < 2$ supports the hypothesis that dry (mainly minor) mergers are at work in this redshift range (e.g., Trujillo et al. 2006, 2007; van Dokkum et al. 2008; Damjanov et al. 2009; Barro et al. 2013; Tadaki et al. 2014). However, Naab et al. (2014) present, using cosmological hydrodynamical simulations of individual galaxies, that there are many paths to create fast- and slowly rotating ETGs and it is not clear when and how ETGs obtained their dynamical properties after the star formation quenching at $z \geq 2$. Moreover, in $z < 2$, secular processes such as fading of disks may play an important role, if we take account of the insufficient merger rate and the evolution of morphology as well as the size evolution (e.g., Oesch et al. 2010; Carollo et al. 2013, 2014; De Propris et al. 2015).

It is important to study the evolution of the dynamical properties of ETGs observationally. However, it is difficult to carry out IFS observations for high-redshift ETGs even with 8-meter class telescopes. The shapes of ETGs provide us with important information, which is related to the dynamics. Although ETGs look featureless and their isophote shapes can be described by perfect ellipses to the zeroth order, their shapes have small but significant deviation from ellipses into “boxy” or “disky” (Lauer 1985a, 1985b, 1985c). Bender & Möllenhoff (1987) and Jedrzejewski (1987) evaluated the deviations of isophote shapes from perfect ellipses using Fourier expansions in the polar angle. They found that the most significant non-zero component is the $a_4$ parameter, the coefficient of the $\cos(4\theta)$ term. The negative sign of the parameter indicates the boxy isophote whereas the positive sign indicates disky.

Bender et al. (1988, 1989) study the isophote shapes and relation to other observed properties using 69 bright E/S0 samples, and have shown that there are significant correlations between $a_4$ and radio, X-ray properties. Boxy ETGs tend to be brighter, supported by random motions with large velocity anisotropy (i.e., slow rotators), and have significant radio and X-ray activities and core nuclear light profiles, while disky ETGs tend to be fainter, supported by ordered rotation with small velocity anisotropy (i.e., fast rotators), lack radio and X-ray activities, and have coreless nuclear profiles (Bender et al. 1989; Ferrarese et al. 1994; van den Bosch et al. 1994; Lauer et al. 1995; Kormendy & Bender 1996; Faber et al. 1997; Rest et al. 2001; Lauer et al. 2005; Kormendy et al. 2009).

Dependence of the isophote shapes on environment is also studied by Shioya & Taniguchi (1993). These isophote shape properties are confirmed by Hao et al. (2006) with a much larger sample of 847 local ETGs using the Sloan Digital Sky Survey (SDSS) data. Pasquali et al. (2007) use the same sample to conclude that isophote shapes may be related to nuclear activities and to group hierarchy. Radial profiles of isophote shape parameters including $a_4$ can also be used to classify galaxy morphology (e.g., Andreon et al. 1996; Andreon & Davoust 1997; Andreon et al. 2016), Naab et al. (1999) and Naab & Burkert (2003) present, by numerical simulations, that nearly equal mass mergers between disk galaxies produce boxy ellipticals whereas minor mergers result in disky ones. Khochfar & Burkert (2005) and Naab et al. (2006) also show that dry mergers also produce boxy elliptical galaxies regardless of the progenitor mass ratio.

In this study, to investigate the epoch at which the dynamical properties of ETGs are established, we analyze the isophote shape parameter ($a_4$), as a proxy for the dynamical properties, of ETGs in massive clusters at $z \sim 1$ and 0. We compare the dependence of the isophote shape parameter on the mass and size as well as the disky ETG fraction between these redshifts. Advantages of studying galaxies in massive clusters are that there are larger number of ETGs than in fields, massive clusters are unique environment which harbors massive ETGs such as central and cD galaxies, and galaxies evolve within the cluster once they enter into such an environment. We have created quiescent ETG samples in massive galaxy clusters with spectroscopic redshifts, using data obtained in the Hubble Space Telescope (HST) Cluster Supernova (SN) Survey for $z \sim 1$ (Dawson et al. 2009, PI-Perlmuter: GO-10496), and SDSS (York et al. 2000) Data Release 12 (DR12, Alam et al. 2015) for $z \sim 0$. We have also developed an isophote analysis method optimized to high-redshift galaxies with low surface brightness and small apparent size.

This paper is organized as follows. In Section 2, we describe the sample selection, and basic properties of the high- and low-redshift quiescent ETG samples. In Section 3, we describe the isophote analysis method. In Section 4, we present the results, which are followed by a discussion in Section 5. Throughout this paper, magnitudes are described in the AB system and are galactic extinction corrected (Schlegel et al. 1998; Schlafly & Finkbeiner 2011). We assume a $\Lambda$CDM cosmology with parameters of $(\Omega_m, \Omega_\Lambda, H_0) = (0.3, 0.7, 70$ km s$^{-1}$ Mpc$^{-1}$).

2. THE GALAXY SAMPLES

In this section, we describe the sample selection and basic properties of our sample galaxies. We create a stellar-mass-limited, high-redshift quiescent ETG sample and low-redshift counterpart for comparison. We first select galaxies with spectroscopic redshift from the HST Cluster SN Survey (Dawson et al. 2009) for the high redshift ($z \sim 1$), and from SDSS (York et al. 2000) DR12 (Alam et al. 2015) for the low redshift ($z \sim 0$). To select quiescent ETGs, we then choose quiescent galaxies using a color–magnitude diagram, impose a stellar mass limit, and select ETGs based on morphological parameters.
2.1. High-redshift Galaxy Sample

In the HST Cluster SN Survey (Dawson et al. 2009) survey, 25 massive high-redshift clusters have been selected from X-ray, optical, and IR surveys (Dawson et al. 2009). The basic properties of the clusters such as redshifts, virial masses, and radii are described in Jee et al. (2011). We have obtained multi-epoch HST imaging data (PID 10496) and follow-up spectroscopic data of galaxies in the clusters.

2.1.1. HST Imaging Data

Imaging data obtained by HST are described in Suzuki et al. (2012) and Meyers et al. (2012), but we briefly describe basic information here. The 25 target clusters were visited by HST four to nine times between 2005 July and 2006 December. Each visit typically consisted of four ∼500 s exposures in the F850LP filter (hereafter $z_{850}$) of the Advanced Camera for Surveys (ACS) Wide Field Camera (WFC; Ubeda 2012) and one ∼500 s exposure in the F775W filter (hereafter $i_{775}$) of the ACS WFC. For galaxies at $z \sim 1$, these two photometric bands cover the wavelength region around the 4000 Å break, an important spectral feature of quiescent galaxies.

In this paper, we use the co-add of exposures from all observation epochs. Four clusters, RDCS J0910+54 (Mei et al. 2006a), RDCS J0848+44 (Postman et al. 2005), RDCS J1252-29 (Blakeslee et al. 2003), and XMMU 2235.3-2557 (Jee et al. 2009), had been previously targeted by ACS in $i_{775}$ and $z_{850}$ (PID9290 and PID9919), and these exposures are also included in our co-added images. We create cutouts of $i_{775}$ and $z_{850}$ images of each galaxy from the co-additions. We use $z_{850}$ cutouts for the morphological classification as well as the isophote shape analysis since the co-added images in $z_{850}$ are much deeper (effective exposure time is ∼10 k sec or more depending on clusters) than in $i_{775}$.

2.1.2. Spectroscopic Redshifts

We select the cluster members confirmed by spectroscopic redshifts. The redshifts of the galaxies are taken from a spectroscopic catalog created in the HST Cluster SN Survey (Meyers et al. 2012). The catalog information is described in Meyers et al. (2012). Briefly, as the HST Cluster SN Survey produced SN candidates, galaxies were spectroscopically targeted with multi-object slits using prescheduled observing time on DEIMOS on Keck II (Faber et al. 2003), and FOCAS on Subaru (Kashikawa et al. 2002), and with Target of Opportunity requests on FORS1 and FORS2 on Kueyen and Antu at the Very Large Telescope (Appenzeller et al. 1998). The FORS1, FORS2, and DEIMOS observations are described in Lidman et al. (2005) and Dawson et al. (2009); the FOCAS observations are described in Morokuma et al. (2010). Galaxy redshifts are measured through cross-correlation with template eigenspectra derived from SDSS spectra (Aihara et al. 2011).

The important spectroscopic features are the 4000 Å break, the absorption of Ca H, K, and the emission lines of [O ii] 3727 Å doublet. The spectroscopic catalog includes these redshifts and additional ones from the literature (Postman et al. 1998; Rosati et al. 1999; Stanford et al. 2002, 2005; Bremer et al. 2006; Brodwin et al. 2006; Demarco et al. 2007; Hilton et al. 2007, 2009; Andreon et al. 2008; Eisenhardt et al. 2008). The equivalent width of [O ii] is also provided for some galaxies (about half of $z \sim 1$ cluster galaxies). Note that the completeness of the spectroscopic sample is not high and varies from cluster to cluster, since many galaxies are additional targets in the HST Cluster SN Survey whose main targets are SNe and their hosts.

In this study, we include 19 clusters with more than two spectroscopically identified members, and exclude other clusters due to too few spectroscopic members. The total number of the included clusters spans from log($M_{200}/M_\odot$) ∼ 14.2 to 14.9, where $M_{200}$ adopted from Jee et al. (2011), is the total mass at the radius, $R_{200}$, inside of which the mean density is 200 times the critical density of the universe at the cluster redshift. We have 301 $z \sim 1$ cluster galaxies with the spectroscopic redshift in total at this stage. The redshift of the selected galaxies spans from 0.90 to 1.48 with the median redshift of $z \sim 1.2$. We later create quiescent ETGs from these 301 galaxies. Of these galaxies, 286 lie within one $R_{200}$ from the cluster center, and another 15 galaxies within 1.5 $R_{200}$, where $R_{200}$ is adopted from Jee et al. (2011). The redshifts of 279 galaxies are within ±0.01 from the cluster redshift, and those of another 22 are within ±0.02.

2.2. Low-redshift Galaxy Sample

To create the low-redshift sample, we make use of SDSS public DR12 (Alam et al. 2015). We refer to the spectroscopic and imaging catalogs provided by SDSS to select low-redshift galaxies, and we use g-band images for the morphological classification as well as the isophote shape analysis because it covers the similar rest-frame wavelength range to $z_{850}$ for $z \sim 1$ galaxies. We create a cutout of the g-band image of each galaxy.

2.2.1. Low-redshift Massive Clusters

We selected nine low-redshift massive clusters, which may be possible descendants of the high-redshift ones based on halo masses ($M_{200}$) and redshifts. Reiprich & Böhringer (2002) study basic properties of low-redshift galaxy clusters such as mass and radius based on X-ray observations. We first select 10 clusters whose redshifts lie in the range of 0.02 < z < 0.05. The redshift range is determined so that the PSF size of SDSS images for $z \sim 0$ galaxies become comparable to that of HST ACS $z_{850}$ images for $z \sim 1$ galaxies in physical scales in order to match the effect of PSF on isophote shape measurements (see Section 3.4). The PSF FWHM of HST ACS $z_{850}$ images, ∼0.9′′1, corresponds to ∼0.75–0.85 kpc at $z \sim 0.8–1.5$, whereas that of SDSS images, ∼1′′3, corresponds to ∼0.5–1.3 kpc at $z \sim 0.02–0.05$.

Then, one low-mass cluster, MKW4 (log($M_{200}/M_\odot$) = 14.1) is excluded from the low-redshift cluster sample. Since the high-redshift clusters are massive (log($M_{200}/M_\odot$) ∼ 14.2–14.9), such a low-mass cluster is not likely to be a descendant of the high-redshift ones. The redshift and mass selection leave us nine clusters, A0119, A1367, COMA, MKW8, A2052, MKW3S, A2063, A2147, and A2199. The halo mass spans from log($M_{200}/M_\odot$) ∼ 14.6 to 15.2. The masses of low-redshift clusters are slightly larger than those of the high-redshift ones. Since the high-redshift clusters with the halo mass of $10^{14.5} M_\odot$ at $z \sim 1$ will evolve into clusters with the mass of $10^{15} M_\odot$ at $z \sim 0$, considering halo mass growth from $z \sim 1$ to 0 (e.g., Zhao et al. 2009), the low-redshift clusters are the possible descendants of the high-redshift ones.
2.2.2. Selection of the Low-redshift Galaxies

We select member galaxies of each cluster using the SDSS spectroscopic catalog. From the spectroscopic catalog, we select all galaxies that lie within one $R_{200}$ radius from the cluster center and within a redshift range of $z_{\text{CL}} - \Delta z \leq z \leq z_{\text{CL}} + \Delta z$, where we set $\Delta z = 0.0067$, which corresponds to 2000 km s$^{-1}$. The cluster radius ($R_{200}$), center, and redshift are referred from Reiprich & Böhringer (2002). We have 3278 galaxies with SDSS spectroscopy ($r < 17.77$ mag) in total at this point with a median redshift of $z \sim 0.029$.

2.3. Selection of the Quiescent Galaxies

We select quiescent galaxies from the spectroscopic members of the high- and low-redshift clusters. We simply select red galaxies for the high-redshift sample. For the low-redshift, we impose more strict selection criteria based on the color–magnitude diagram to choose red-sequence galaxies, which are possible descendants of the high-redshift red galaxies.

2.3.1. High-redshift Quiescent Galaxies

We select the high-redshift quiescent galaxies based on their $i_{775} - z_{850}$ colors. The $i_{775} - z_{850}$ color is measured within a circular aperture of a fixed size. As galaxies, both late- and ETGs (e.g., Tortora et al. 2010; den Brok et al. 2011), often have radial color gradients, we measure the color only in a central region. We set the aperture diameter to 0.022 arcsec, which corresponds to 1.8 kpc at $z = 1.2$ in physical scale. This physical scale is comparable to that of the diameter of the SDSS 3 arcsec fiber at $z \sim 0.03$ with which we later measure the color of low-redshift galaxies.

Because the size of PSF is slightly different between $i_{775}$ and $z_{850}$ images, we prepare PSF-matched images by convolving $i_{775}$ with the PSF of $z_{850}$ and vice versa. The PSF of each band is created in each cluster field as an averaged image of stars. We select $\sim 30$ unsaturated stars, cutout 100 $\times$ 100 pixels around them, and normalize the flux with the central value. Then we oversample the cutout images by 51 times, align the center in the subpixel level, and take an average.

We select red galaxies with $i_{775} - z_{850} \geq 0.7$ as quiescent galaxies. The number of galaxies in the high-redshift quiescent galaxy sample is 224. In Figure 1, we show the color–magnitude diagrams of the high-redshift galaxies in three cluster redshift bins, $z_{\text{CL}} \leq 1.05$, $1.05 < z_{\text{CL}} \leq 1.30$, and $1.30 < z_{\text{CL}}$. We derive the measurement errors of $i_{775} - z_{850}$ color from unconvolved $i_{775}$ and $z_{850}$ images to avoid correlated noise. We run SExtractor (Bertin & Arnouts 1996) on cutout images of $i_{775}$ and $z_{850}$ using two-step (Cold/Hot) method (Rix et al. 2004) to derive total $z_{850}$ magnitudes. The detection parameters in the two steps are optimized by trial and error judged by the successful identification and segmentation of galaxies near cluster cores. We use the Petrosian (Petrosian 1976) magnitudes (MAG_PETRO in SExtractor) as the total $z_{850}$ magnitude because we refer to the the Petrosian magnitudes given in the SDSS catalog for the low-redshift galaxies.

In Figure 1, we also plot the color–magnitude relation of simple stellar population (SSP) models using Bruzual & Charlot (2003, hereafter BC03) with Salpeter initial mass function (IMF). We compute absolute $z_{850}$ magnitudes and $i_{775} - z_{850}$ colors using the observed stellar mass-age and metallicity relation of nearby ETGs (Thomas et al. 2005). As the high-redshift red galaxies form tight red sequence, which is roughly consistent with the SSP models predicted from local red sequence, the evolution of the color would be passive as discussed in previous studies (e.g., Blakeslee et al. 2003; Mei et al. 2006a, 2006b). Although our color selection limit, $i_{775} - z_{850} = 0.7$, is bluer than the modeled red sequence, the selected galaxies should be quiescent because the color limit indicates the SSP equivalent age of older than $\sim 500$, 100, and 300 Myr, respectively, at $z \sim 1.0$, 1.2, and 1.4.

2.3.2. Low-redshift Quiescent Galaxies

We select the low-redshift quiescent galaxies using a color–magnitude diagram of the $u - g$ color and absolute $g$ magnitude. It is not a simple task to select possible descendants of the high-redshift quiescent galaxies as the luminosity and color of the galaxies evolve with redshift. Since the evolution of each galaxy is unknown, we need to assume the evolution. In this study, we assume that the high-redshift quiescent galaxies passively evolve with no mergers. Although we simply select quenched galaxies for high redshift based on one single $i_{775} - z_{850}$ color, we select possible descendants at low redshifts based on the color–magnitude diagram with more strict selection criteria in order not to include newly quenched galaxies in $z < 1$. In Figure 2, we plot the color–magnitude diagrams of the low-redshift galaxies in three cluster redshift bins. We use the magnitude within the SDSS 3 arcsec fiber when we derive the $u - g$ color to reduce the effect of color

![Figure 1](Image1.png)

**Figure 1.** Color–magnitude diagrams of the high-redshift galaxies in three cluster redshift bins, $0.9 \leq z_{\text{CL}} \leq 1.05$, $1.05 < z_{\text{CL}} \leq 1.30$, and $1.30 < z_{\text{CL}} < 1.5$, from left to right. Red circles represent selected galaxies as quiescent while blue squares are unselected galaxies. Error bars indicate median uncertainties. Dashed lines represent the color–magnitude relation of the SSP models with the numbers at the ticks standing for the stellar mass, log($M_*/M_\odot$).
gradients in a galaxy. We refer to the Petrosian magnitude
given in the SDSS catalog as the total g magnitude.

In Figure 2, we also plot the color–magnitude relation by
dashed lines inferred from the stellar mass-age and stellar
mass–metallicity relation of nearby quiescent ETGs (Thomas
et al. 2005) using BC03 with Salpeter IMF. Green solid lines in
the figure are the bluer limit above which a galaxy is selected as
quiescent. We determined the bluer limit as follows. We
decrease the metallicity by three times the intrinsic scatter
(σz/M) ∼ 0.08 dex, see Thomas et al. 2005) from the stellar
mass–metallicity relation and fix the stellar age to 7 Gyr, which
 corresponds to the look-back time to z ∼ 0.9, the lowest
redshift of the high-redshift galaxies. Then, we derived the
color–magnitude relation with these SSP parameters. We
finally fit a linear function of the color–magnitude relation
in the magnitude range of −23 ≤ M_g ≤ −16 to obtain the bluer
limit. As shown in Figure 2, the bluer limit clearly separates
red-sequence galaxies from those in the blue cloud. The
number galaxy in the low-redshift quiescent galaxy sample is 1733.

2.4. Stellar Mass Limits

Next we impose a stellar mass limit. We estimate a stellar
mass of the galaxies by fitting SSP models of BC03 with
Salpeter IMF to color(s) and magnitude. For low-redshift
galaxies, we fit the SSP SED to the Petrosian g magnitude and
SDSS 3 arcsec fiber colors of u − g, g − r, g − i, and g − z.
The free parameters are the stellar mass, age, metallicity. One sigma uncertainty is calculated from errors in the g magnitude
and four colors via the Monte-Carlo simulation.

For high-redshift galaxies, as only i_{775} and z_{850} magnitudes are available, only two free parameters can be constrained by
the fitting. Because our high-redshift quiescent galaxies are largely consistent with red sequence expected from local stellar
mass-age and mass–metallicity relation (see Figure 1), we
relate the stellar age to mass using Equation (3) in Thomas
et al. (2005). Then, independent fitting parameters are the
stellar mass and metallicity. We fit the synthetic SSP SED to the
z_{850} Petrosian magnitude and i_{775} − z_{850} color measured in
the central region (0′′22 diameter aperture) of a galaxy. We
also estimate the stellar mass by assuming the stellar mass–metallicity relation instead of the mass-age relation. We adopt
the absolute value of one half of the difference between stellar
masses obtained in the two different ways as uncertainty of the
stellar mass for the high-redshift galaxies, which is typically
larger than one sigma error arising simply from uncertainties in
i_{775} and z_{850} photometry.

With the estimated stellar masses, we selected galaxies with
log(M_*/M_☉) ≥ 10.5 in order to make the stellar mass range
comparable between low- and high-redshift samples. For quiescent galaxies, the magnitude limit of the high-redshift sample is ∼23–24 mag in z_{850} depending on clusters. For the high-redshift quiescent sample, the stellar mass limit corresponds to the absolute magnitude of M_{z_{850}} ∼ −21.8 and apparent magnitudes of m_{z_{850}} ∼ 22.3, 22.8, and 23.2 respectively at z = 1.0, 1.2, and 1.4. For the low-redshift quiescent galaxies, the stellar mass limit corresponds to M_g ∼ −19.5 and M_r ∼ −20.3 in g and r bands, respectively. The latter becomes the r band apparent magnitude of m_r = 16.4 at z = 0.05 (the upper redshift limit of our low-redshift sample), which is brighter than the magnitude limit of the SDSS spectroscopic sample. We have 158 and 513 galaxies for mass-limited high-
and low-redshift quiescent samples.

We checked possible systematics between stellar masses
obtained from one color and from multi colors. First, we
compared the stellar masses of low-redshift quiescent galaxies.
We computed stellar masses of low-redshift quiescent galaxies from u − g fiber color and g Petrosian magnitude assuming the
mass–age relation (Thomas et al. 2005). We have found that
the stellar masses obtained from a single u − g color tend to be
overestimated by ∼0.5 dex. Then, we compared the stellar
masses of high-redshift quiescent galaxies. For some of our
high-redshift quiescent sample, Delaye et al. (2014) derived stellar masses from four-band photometries, i_{775}, z_{850}, J, and
K_s. We matched our high-redshift quiescent sample and Table
B1 in Delaye et al. (2014), and compared the stellar masses
derived from a single color and three colors (four bands).
Unlike low-redshift samples, the stellar masses derived from a
single i_{775} − z_{850} color are on average underestimated by ∼0.2
dex. Thus, we do not apply any correction to the stellar masses
of our high-redshift galaxies. We note that as Delaye et al.
(2014) use MAG_AUTO magnitudes (i.e., total magnitudes) in
the four filters, negative color gradients cannot explain the
difference in the stellar masses. We would remind readers that
the stellar masses of the high-redshift galaxies may have
uncertainties of ∼0.2 dex.
2.5. Selection of the Quiescent ETGs

We then select ETGs from quiescent galaxies with morphological classification using photometric parameters. We note that our conclusions, e.g., the disky-to-boxy fraction, are stable and have negligible change even if we use a quiescent galaxy sample.

There are various ways to classify galaxy morphology. One is the visual classification, which has a long history in morphological classification (e.g., Sandage 1961; Dressler 1980; Sandage & Tammann 1981; recent studies by Fukugita et al. 2007 for low-redshift with SDSS; Postman et al. 2005 for high-redshift galaxy with HST). There have also been classifications using the concentration (Morgan 1958), and parameter combination of the concentration and mean surface brightness (Doi et al. 1993; Abraham et al. 1996), asymmetry (Abraham et al. 1996), or smoothness (Conselice 2003; Yamauchi et al. 2005). The Gini index is also adopted instead of the concentration parameter (Abraham et al. 2003).

Recently, a machine learning scheme was introduced by Huertas-Company et al. (2011). In this study, we make use of the pair of the concentration parameter and mean surface brightness, which we have found less likely to be affected by signal-to-noise ratios of images than other parameters. In the Appendix, we provide results of simulations comparing the stability of the measurement of the Gini coefficient, asymmetry, concentration index, and mean surface brightness against the signal-to-noise ratio.

Before the morphological classification, we run GALFIT (Peng et al. 2002) on the cutout image of $\xi_{250}$ for high-redshift galaxies and $g$ for low-redshift galaxies to fit a single Sérsic profile (Sérsic 1968; Ciotti & Bertin 1999, for analytical properties of the profile) in order to derive some basic parameters of our galaxies and to create interloper-subtracted images. We constrain the Sérsic index $n$ between 0.2 and 8.0, and we input a PSF image to convolve with its model before fitting to the actual galaxy image. We mask or fit simultaneously nearby objects depending on the degree of overlap. For high-redshift galaxies, the PSF images and SExtractor catalogs of nearby objects are constructed when we derive $t_{775} - \xi_{250}$ colors (see Section 2.3.1). For low-redshift galaxies, we also prepare PSF images and SExtractor catalogs. PSF images are created as for the high-redshift sample, by averaging images of non-saturated $\sim 30$ stars in the original $2k \times 4k$ frame of the target. We make use of the cold/hot method (Rix et al. 2004) as high-redshift, when running SExtractor. We obtained PSF-deconvolved structural parameters such as Sérsic index $n$, effective radius $r_e$, axis ratio $q = b/a$, position angle, and surface brightness $\mu_e$ at $r_e$. We do not use these structural parameters for morphological classification because not all galaxies can be successfully fitted by a single Sérsic profile.

2.5.1. Morphological Classification with $C_{in}$ and $SB_{24.5}$

The concentration index and mean surface brightness are measured in a similar manner as that described in Doi et al. (1993). We first determine an isophote aperture by collecting pixels above cosmological dimming corrected surface brightness of 24.5 mag arcsec$^{-2}$. We use the smoothed images with a Gaussian kernel of $\sigma = 2$ pixel to determine the isophote. The mean surface brightness $SB_{24.5}$ is computed as the total flux within the aperture divided by the total area $A_{aperture}$. We derive the equivalent outer radius as $r_{out} = \sqrt{A_{aperture}/\pi}$ and inner radius as $r_{in} = \alpha r_{out}$, where $\alpha$ is set to 0.3 in this paper. The concentration index $C_{in}$ is defined as the ratio between the fluxes within a circular aperture with $r_{in}$ and that with $r_{out}$.

Doi et al. (1993) present that galaxies with Sérsic indexes of $n = 4$ (ETGs) and $n = 1$ (disk galaxies) can be separated in $C_{in}$-$SB_{24.5}$ plane. However, ETGs with low surface brightnesses ($\mu_e \gtrsim 23$–24 mag arcsec$^{-2}$) and disks with brightnesses of $\mu_e \gtrsim 23$ mag arcsec$^{-2}$ overlap on the plane depending on the PSF size (see Figures 1 and 2 in Doi et al. 1993). Here, $\mu_e$ is the surface brightness at effective radius $r_e$. In our classification criteria described in Doi et al. (1993), $\mu_e$ denotes the central brightness for $n = 1$ galaxies. Because our galaxies reside in massive clusters, we have a certain portion of luminous ellipticals with low surface brightnesses (Kormendy 1977), and these galaxies will drop out from ETG classification if we simply apply the separation criteria described in Doi et al. (1993). Considering that ETGs and disk galaxies have different surface brightness-magnitude relations (see, for example, Figure 20 in Kormendy & Bender 2012), ETGs with $\mu_e \gtrsim 23$–24 mag arcsec$^{-2}$ and disks with $\mu_e \gtrsim 23$ mag arcsec$^{-2}$ would appear in different magnitude ranges.

In Figure 3 (left), the distribution of the low-redshift quiescent mass-limited sample galaxies with Sérsic indexes of $n \geq 3.5$ (left panel) and $n \leq 1.5$ (right panel) on the magnitude and half-light radius plane. Dashed lines indicate a $M_{g} - r_{e}$ relation assuming Sérsic profiles with $n = 4$ (left panel) and $n = 1$ (right panel). $\mu_e$ is set to 24, 23, 22, 21, and 20 mag arcsec$^{-2}$ from top to bottom. Right: same as left but for high-redshift mass-limited quiescent galaxies. The magnitude is given as $M_{g,250}$ instead of $M_{g}$. For the model lines, $\mu_e$ is set to 24, 23, 22, and 21 mag arcsec$^{-2}$ from top to bottom.
brightness ETGs in the fainter region. At the same time, the galaxies with small $n$ and $\mu_e \geq 23$ mag arcsec$^{-2}$ are fainter than $M_e \sim -20.5$. Therefore, we define different selection criteria of ETGs on the $C_{in}$-$SB_{24.5}$ plane for the low-redshift galaxies brighter and fainter than $M_e = -20.5$ so that we can include luminous ETGs with low surface brightnesses simultaneously, excluding disk galaxies.

Figure 3 (right) is the distribution of the high-redshift quiescent mass-limited sample galaxies on the absolute $z_{580}$ magnitude and half-light radius plane. Disk-like galaxies with $n \leq 1.5$ with $\mu_e \gtrsim 23$ only appear in $M_{580} \gtrsim -23$, and luminous ETGs with $\mu_e \gtrsim 23$ in $M_{580} \lesssim -23$. Thus, we set the critical magnitude to $M_{580} = -23.0$ above or below which the selection criteria of ETGs on the $C_{in}$-$SB_{24.5}$ plane are defined differently.

In Figure 4, the distributions of the low- and high-redshift quiescent sample on the $C_{in} - SB_{24.5}$ plane are shown. We also plot the expected positions for model galaxies with $n = 4$ (dashed lines) and $n = 1$ (dotted lines) Sérsic profile convolved with typical PSF. We selected galaxies above the separation line (red solid line) as ETGs. The Sérsic index is shown by the color code. As one can see in the figure, galaxies with $n \gtrsim 2$ are selected as ETGs. The number of galaxies with $\log(M_e/M_\odot) \geq 10.5$ in the low- and high-redshift quiescent ETG sample are 355 and 130, respectively. Note that the majority of the low- and high-redshift quiescent galaxy are ETGs, and this ETG selection hardly affects the result.

2.6. Basic Properties of the Quiescent ETG Samples

We present the basic properties of the quiescent ETG samples such as the stellar mass, size, axis ratio, and Sérsic index measured with GALFIT. Hereafter, when we discuss the structural parameters obtained with GALFIT, we exclude galaxies fitted with $n = 0.2$ and 8.0 because these values are the limits of the parameter constraints and may not be reliable. There are 14 and 23 objects with $n = 0.2$ or 8.0, respectively, in the high- and low-redshift quiescent ETG samples.

In the left panel of Figure 5, the effective radii of the low- and high-redshift quiescent ETGs are plotted against the stellar mass (the mass–size relation). We fit a linear function $\log(r_e/\text{kpc}) = a \times (\log(M_e/M_\odot) - 11) + b$. We fix $a$ to 0.57 following Delaye et al. (2014) and only $b$ is a free parameter. The fitted lines are shown in cyan dashed and magenta solid lines for the low- and high-redshift samples, respectively. We also calculate the mass normalized size $r_e/M_\odot$, which is obtained as $\log(r_e/M_\odot) = \log(r_e/\text{kpc}) - 0.57 \times (\log(M_e/M_\odot) - 11)$. In the right panel of Figure 5, the histograms of $\log(r_e/M_\odot)$ are shown for low- and high-redshift samples. The median mass normalized sizes are $(\log(r_e/M_\odot)) = 0.63 \pm 0.02$ and $0.54 \pm 0.03$ for the low- and high-redshift samples, respectively. The overall distribution shifts toward the larger size from $z \sim 1$ to 0. Kolmogorov–Smirnov (KS) test gives the p-value of 0.001 which indicates that the two samples are statistically different. The size
evolution is basically consistent with the result presented in a previous study (Delaye et al. 2014).

In Figure 6, the axis ratios are plotted against the stellar mass in the left panel, and the histograms of the axis ratios are plotted in the right. The median axis ratios are $\langle q \rangle = 0.71 \pm 0.01$ and $0.68 \pm 0.02$ for the low- and high-redshift samples, respectively. The median axis ratio of the high-redshift sample is smaller than that of the low-redshift one, which is consistent with a previous work (De Propris et al. 2015), but in this study, the KS $p$-value is not small enough ($p = 0.11$) to conclude that the two distributions are statistically different.

In Figure 7, the Sérsic indexes are plotted against the stellar mass in the left panel, and the histograms of the Sérsic indexes are plotted in the right panel. The median Sérsic indexes are $\langle n \rangle = 4.3 \pm 0.01$ and $4.2 \pm 0.2$ for the low- and high-redshift samples, respectively. The median values are consistent within uncertainty. The KS test gives the $p$-value of 0.28, which indicates that the two samples could be drawn from the same sample.

3. MEASURING ISOPHOTE SHAPES

We developed an isophote analysis code that is optimized for high-redshift galaxies with low surface brightness and small angular size, based on Bender & Möllenhoff (1987). The code takes three steps: contour determination; deviated ellipse fit; and estimation of errors. Readers who are not interested in the details of the method, please skip this section.

3.1. Contour Determination

In our code, the number of pixels needed to determine a contour is adjusted adaptively according to the signal-to-noise ratio (S/N) per pixel. This point is different from other isophote analyzing code such as IRAF task ELLIPSE (Jedrzejewski 1987). There are three main challenges in investigating isophote contours of high-redshift galaxies. First, apparent surface brightness of high-redshift galaxy decreases with redshift as $(1 + z)^{-4}$ (cosmological surface brightness dimming). For $z \sim 1$ galaxies, the surface brightness becomes dimmer by $\sim 1/16$, though intrinsic luminosity of a galaxy becomes...
brighter at high redshift due to passive evolution as described in the previous section. Second, small apparent angular size makes isophote shape measurement difficult in that the number of pixels used to determine a contour becomes small. The precision of a contour (or sampling points of the contour, \( x_i, y_j \)) is enhanced by the square root of the number of pixels used to determine the contour for a given surface brightness. As easily imagined, for large, nearby galaxies, low-order isophote shape parameter, e.g., \( a_d \), is rather insensitive to noise per pixel since the typical scale length of \( a_d \sim r \times \pi/4 \), is much larger than pixel size. On the other hand, for distant galaxies with small apparent size, the typical scale length is close to the pixel size, so noise per pixel affects the isophote shape measurement more severely. In addition, the large PSF size compared to the apparent galaxy size may introduce systematic errors, which will be discussed in Section 3.4.

First of all, pixels used in the isophote shape analysis is selected in the following way. Pixels with a flux above a given detection limit is picked up using a smoothed image with a Gaussian kernel of \( \sigma = 1 \) pixel. In this paper, we set the detection limit as one sigma background noise, \( \sigma_{\text{bk}} \), above the background level. Then, from the selected pixels, those contiguous to the initial center of the target are chosen. The position of the initial center is given as an input.

Bright objects close to the target are masked. We make use of the output from GAlFIt. As objects close to the target are simultaneously fitted, we mask the pixel where the modeled flux of nearby objects exceeds that of the target object. We have confirmed that bright nearby objects are successfully masked even in the central region of a galaxy cluster in this way.

We extract pixel annuli from the selected pixels, and isophote contours are sampled from the annuli. In the first step, the center of the target is identified, and pixels that are likely to be affected by PSF are discarded. The center of a galaxy is identified as the intensity peak within the brightest 10% of the pixels. We note that our target of interest is ETGs whose light is concentrated, and the flux peak of a galaxy is not severely affected by noise.

The pixels that may be affected strongly by PSF are discarded in the following way. The faintest pixel within a PSF radius \( r_{\text{PSF}} \) from the center is identified, and pixels within an isophote of the intensity of the faintest pixel are masked and discarded. We refer to these discarded pixels as \((\text{pix}_{\text{dis}}) \) hereafter. In this study, we set \( r_{\text{PSF}} \) to the PSF HWHM, i.e., 1.0 pix for HST images and 1.64 pix for SDSS.

In the next step, the first annulus (the innermost annulus) is determined. The pixels surrounding \((\text{pix}_{\text{in}}) \) are the inner pixels of the first annulus. We refer to these inner pixels as \((\text{pix}_{\text{in}}) \).

Then, of the pixels surrounding \((\text{pix}_{\text{in}}) \), the faintest pixel and its intensity are found, and pixels contiguous to the center above the intensity are noted as \((\text{pix}_{\text{out}}) \). The first annulus, \((\text{pix}_{\text{1,ann}}) \), is defined by the pixels

\[
(\text{pix}_{\text{1,ann}}) = (\text{pix}_{\text{in}}) - (\text{pix}_{\text{dis}}).
\]

The successive annuli are determined in the following way. The inner pixels of \( n \)th annulus is defined as

\[
(\text{pix}_{\text{n,in}}) = (\text{pix}_{\text{n-1,ann}}) - (\text{pix}_{\text{n-1,in}}) \quad (n \geq 2).
\]

Then, of the pixels surrounding \((\text{pix}_{\text{n,in}}) \), the faintest pixel and its intensity are found, and pixels contiguous to the center above the intensity are noted as \((\text{pix}_{\text{n,out}}) \). The \( n \)th annulus, \((\text{pix}_{\text{n,ann}}) \), is defined as

\[
(\text{pix}_{\text{n,ann}}) = (\text{pix}_{\text{n,in}}) - (\text{pix}_{\text{n-1,ann}}) + (\text{pix}_{\text{n,in}}).
\]

Repeating this process until all the pixels defined in the previous subsection are used, successive pixel annuli are determined as described in Figure 8. The annuli tend to be narrow in the high-S/N region, i.e., in the central region, but to be wide in the low-S/N region, i.e., in the outskirt. Because a contour is determined with a larger number of pixels, the sampling points of the contour are not significantly affected by noise even in a low-S/N region.

After pixel annuli are determined, the data points of contours are sampled. First, the isophote level of the \( n \)th contour is calculated as the weighted mean of the pixels in the \( n \)th annulus,

\[
I_n = \frac{\sum_{\text{ann}} I_{\text{xy}} / \sigma_{I_{\text{xy}}}^2}{\sum_{\text{ann}} 1 / \sigma_{I_{\text{xy}}}^2},
\]

where \( I_{\text{xy}} \) and \( \sigma_{I_{\text{xy}}} \) are the intensity and noise per pixel at \((x, y)\), respectively.

Then, each annulus is divided into azimuthal bins, as described in Figure 9. The number of bin is three times the number of pixels in the annulus, or if it is larger than 90, the number of the bin is set to 90. Dividing lines are given so that the ellipse parameter \( t_i \) of the lines becomes equidistant. The ellipse parameter \( t \) is a parameter appearing in the parametric formalization of an ellipse,

\[
x = a \cos(t - \psi), \quad y = b \sin(t - \psi),
\]

where \( a \) and \( b \) are the semimajor and minor axes, and \( \psi \) is the position angle. To define the dividing lines, the position angle, \( \psi \), and axis ratio, \( q = b/a \), are necessary before analyzing isophote shapes. In this step, the position angle, \( \psi \), and axis ratio, \( q = b/a \), are fixed to the value estimated from the intensity-weighted second-order moments (e.g., Stobie 1980; Lupton et al. 2001; Yamauchi et al. 2005) within the brightest 25% of the pixels above \( 1\sigma_{\text{bk}} \) isophote with nearby objects masked.

In each azimuthal bin, the sampling points of the isophote contour are determined using the local radial profile. First, the radius of each pixel in each bin is derived. The radius of the
pixel at \((x, y)\) is calculated as
\[
r_{x,y} = \sqrt{(x - x_0)^2 + (y - y_0)^2},
\]
where \((x_0, y_0)\) is the center of the target. The error of intensity is
scaled by the included area into the bin as
\[
\sigma_{i,x,y}^2 = \frac{\sigma_i^2}{A_{x,y,i}},
\]
where \(\sigma_{i,x,y}\) is the intensity error per pixel, and \(A_{x,y,i}\) is the included area into \(i\)th azimuthal bin. This scaling allows us to
treat the errors as independent, since \(A_{x,y,i}\) is equivalent to the
degree of freedom per pixel included into \(i\)th bin.

We fit a linear function, \(I_{\text{lin}}(r) = \alpha r + \beta\), to the local radial
profile \((r, I)\) using all pixels in each bin by minimizing
\[
\chi^2 = \frac{(I_{x,y} - I_{\text{lin}}(r))^2}{\sigma_{i,x,y}^2},
\]
and derive \(\alpha, \beta\), and the covariance matrix from the scaled
intensity errors \(\sigma_{x,y}^2\). Although a radial intensity profile of a
galaxy is often described by a nonlinear function such as the
Sérsic function (Sérsic 1968), the radial range is small
enough for the local profile to be fitted by a linear function.
We have tested log intensity instead of intensity itself in this
process, but we have not found significant differences.

Then, the radius of the sampling point \(r_{n,i}\) is derived as the
crossing point of the fitting line \(I = I_{\text{lin}}(r)\) and the isophote
level \(I = I_i\). The error of the radius \(\sigma_{r,n,i}\) is calculated from
the covariance matrix, i.e., the propagation of errors from \(\sigma_{x,y}^2\) to
\(\sigma_{r,n,i}\) is calculated. The \((x, y)\) position of the sampling point is
then given as
\[
\begin{align*}
x_{n,i} &= r_{n,i} \cos(\theta_i - \phi) + x_0 \\
y_{n,i} &= r_{n,i} \sin(\theta_i - \phi) + y_0,
\end{align*}
\]
and errors as
\[
\begin{align*}
\sigma_{x,n,i} &= \sigma_{r,n,i} \cos(\theta_i - \phi) \\
\sigma_{y,n,i} &= \sigma_{r,n,i} \sin(\theta_i - \phi),
\end{align*}
\]
where \(\theta_i = (t_i + t_{i+1})/2\). Repeating this process for all
azimuthal bins gives the sampling points for the \(n\)th isophote
contour.

### 3.2. Deviated Ellipse Fit

To each isophote contour, an ellipse is fitted with third-
to sixth-order Fourier deviations. The fitting parameters are five
parameters related to ellipse, center \((x_0, y_0)\), axis ratio \((q)\),
position angle \((\psi)\), and semimajor axis \((a)\), and parameters
related to the deviation, \(a_n\) and \(b_n\) \((n = 3, 4, 5, 6)\). The zeroth
to the second-order deviation terms are not included, since they
degenerate with center, axis ratio, and position angle. First, the
initial values of the five ellipse parameters are derived by
minimizing
\[
\chi^2 = \sum_i ((x_i - x_{e,i})^2 + (y_i - y_{e,i})^2),
\]
where \((x_i, y_i)\) is the sampling point of the contour, \((x_{e,i}, y_{e,i})\) is
the point on the fitting ellipse given as
\[
\begin{align*}
x_{e,i} &= a \cos(\theta_i - \psi) + x_0 \\
y_{e,i} &= b \sin(\theta_i - \psi) + y_0.
\end{align*}
\]
In this step, we iteratively fit the center, axis ratio, and position
angle around the value determined in the previous subsection,
whereas the semimajor axis is fitted around mean value of \(r_i\).

After initial conditions are determined, a deviated ellipse is
fitted. In this process, \((x_{e,i}, y_{e,i})\) is given as
\[
\begin{align*}
x_{e,i} &= (a + \Delta r_i) \cos(\theta_i - \psi) + x_0 \\
y_{e,i} &= (b + \Delta r_i) \sin(\theta_i - \psi) + y_0,
\end{align*}
\]
where \(\Delta r_i\) is the deviation term,
\[
\Delta r_i = \sum_{k=3}^{6} (a_k \cos(k\theta_i - \psi) + b_k \sin(k\theta_i - \psi)).
\]
Finally, zeroth- to sixth-order deviation terms are derived with
ellipse parameters, \((x_0, y_0), q, \psi, a,\) and \(a\), fixed to the values
obtained above.

In Figure 10, an example of measurements of the \(a_4/a\)
parameters of a nearby galaxy NGC4697 is shown. As isophote
shapes of this galaxy have been investigated in Jedrzejewski
(1987) and Bender et al. (1988), we compare our \(a_4\)
measurements with these previous studies. We measure the
isophote shapes using SDSS \(g, r,\) and \(i\) bands. Our measurements
are in good agreement with the previous studies except for the
inner most region where the seeing affects the measurement of
\(a_4\) and three measurements diverge, probably
due to the difference of the seeing. The typical seeing FWHM
in our measurement is \(\sim 1.1 - 1.3\) arcsec estimated from
unsaturated stars, while it amounts to \(\sim 1.5 - 1.9\) arcsec in
Jedrzejewski (1987) and \(\sim 2\) arcsec in Bender et al. (1988).

We reduce the radial profiles of various isophote shape
parameters such as \(q, \psi, a_0 - 6, b_0 - 6\) to mean values in the
following way because it is too complicated to compare the
radial profile between galaxies. The mean value is calculated as

![Figure 9. Example of an annulus divided into an azimuthal bin.](image-url)
an error-inverse-weighted mean. Uncertainty of the mean value is estimated from the propagation of errors, taking account of the correlation between contours. How the errors of isophote shape parameters of each contour are derived is described in the next subsection. We constrain the semimajor axis range in which the mean value of radial profile is calculated between $2d_{\text{PSF}}$ and $2a_b$. Here, $a_b$ is the half-light semimajor axis calculated from $\text{FLUX} _{\text{RADIUS}}$ and $\text{ELONGATION}$ obtained by SExtractor. We have confirmed that taking 1.0 or 1.5 $a_b$ instead does not change our result. Hereafter, the isophote shape parameter (e.g., $a_4$) simply indicates the mean value.

3.3. Estimation of Errors of Isophote Shape Parameters

We estimate statistical errors of isophote shape parameters (e.g., $a_4$) arising from random noise of a flux in each pixel, including photon noise from objects, and background noise such as photon noise due to sky flux and readout noise. We first estimate the random noise in each pixel, then resolve the propagation of noise onto the position of the contour sampling points, and finally, errors of the isophote shape parameters are estimated by the Monte-Carlo simulation.

In the error estimation, the photon noise from objects is estimated from count per pixel by Poisson statistics. The background noise $\sigma_{\text{bg}}$ is estimated from background fluctuation per pixel as we utilize calibrated, sky-subtracted images. The background noise is estimated from a cutout image of each target. All objects detected by SExtractor (see Section 2.3.1) are masked before measuring the pixel to pixel fluctuation. For HST images where background noise per pixel is correlated, $\sigma_{\text{bg}}$ is corrected for the correlated noise using a simple equation described in Section 2.3 in Gonzaga et al. (2012).

Once noise per pixel is calculated for each pixel, the positional error, $\sigma_{\text{pos}}$, or error of radial position $\sigma_{\text{rad}}$, of a sampling point of a contour can be computed as described in Section 3.1. Finally, $1\sigma$ uncertainty is estimated by the Monte-Carlo simulation using the position errors. We resample the sampling points of each contour adding Gaussian random noise to the fitted deviated ellipse with the standard deviation of $\sigma_{\text{rad}}$. We resample the sampling points 100 times and repeat fitting deviated ellipse to derive rms scatter of each isophote shape parameter, which we defined as $1\sigma$ uncertainty.

Figure 10. Example of radial (semimajor axis) profiles of the $a_4$ parameter of a nearby galaxy, NGC4697. Blue shaded region enclosed by solid line represents the result obtained by Jedrzejewski (1987, in B and R band), whereas the red shaded region enclosed by dashed lines indicates the measurements by Bender et al. (1988, in V, R and I band). Blue squares are our measurements in $g$ band, green crosses are in $r$, and red circles are in $i$.

3.4. The Effect of PSF

We evaluate the systematic effect of PSF on the measurement of $a_4$ in a simulation. As mentioned in Pasquali et al. (2006), measured isophote shapes are affected by PSF for galaxies with small apparent sizes compared to PSF. We generated artificial images of low- and high-redshift galaxies, convolved them with typical PSF of low- and high-redshift samples, and measured the $a_4$ parameter in the convolved images. We modeled the galaxies by Sérsic profiles with various combinations of the Sérsic index, axis ratio, and $a_4$ parameter: $n = 1.0, 2.5, 4.0, 6.5$; $q = 0.2, 0.4, 0.6, 0.8; 100 \times a_4/a = -4.0, -2.0, 0.0, +2.0, +4.0$. We also changed the galaxy size. For low-redshift galaxy models, the effective radii are set to $\log(r_e/\text{arcsec}) = 0.0, 0.5, 1.0, 1.5, 2.0$. For high-redshift galaxy models, they are set to $\log(r_e/\text{arcsec}) = -1.0, -0.5, 0.0, 0.5$. We note that 1 arcsec corresponds to 0.62 kpc at $z = 0.031$ and 8.3 kpc at $z = 1.2$, and the ranges of the effective radius well covers the typical sizes of actual galaxies.

A part of the result is shown in Figure 11, where (PSF-convolved) $a_4$ parameters are plotted against the axis ratio, effective radius, and Sérsic index. In the left and central panels, only models with $n = 4.0$ are shown, whereas, in the right panels, only those with $\log(r_e/\text{arcsec}) = 1.0 (0.0)$ are shown for low-redshift (high-redshift) cases, respectively. Also, in the left panels, models with $\log(r_e/\text{arcsec}) = 1.0, 0.5 (0.0, -0.5)$ are shown for low-redshift (high-redshift) cases. In the central and left panels, models with $q = 0.8, 0.4$ are shown.

Apparently, the measured (PSF-convolved) $a_4$ parameters are affected not only by the axis ratio but also by galaxy size and Sérsic index. Moreover, the difference of the measured and intrinsic values of $a_4$ depends on the intrinsic $a_4$ value. The dependence of the PSF effect on these parameters can be summarized as follows. First, the isophote shapes tend to be measured as disky especially for flattened galaxies with $q \lesssim 0.5$. Second, galaxies with the large apparent size are not suffered from the PSF effect, but for small galaxies, the measured isophote shape tends to be round as the relative PSF size to the galaxy becomes larger. Third, for galaxies with larger Sérsic indexes, the isophote shape tends to be rounder, because the flux is more concentrated and affected by PSF more strongly. Finally, the difference of the measured and intrinsic $a_4$ value becomes larger with an increasing absolute value of $a_4$. Pasquali et al. (2006) show the dependence of the PSF effect on the axis ratio for $a_4 = 0$, and our simulation gives the consistent result. We note that only small axis ratios cause systematic effect for disky and boxy classification, i.e., boxy intrinsic shape affected by the PSF may be measured as disky. Other parameters, small sizes, and large Sérsic indices, make the absolute $a_4$ value small, but do not affect the classification.

The effect of PSF on the isophote shape measurement depends on many parameters, and it is rather difficult to correct the $a_4$ value for the effect. However, as we restricted the redshift range of the low-redshift sample so that the PSF size becomes consistent between low and high redshifts, and the sizes, axis ratios, Sérsic indexes do not change between the high- and low-redshift ETG samples very much, the PSF effect is probably similar in both low- and high-redshift samples. Thus, we decided not to correct the measured isophote shape parameters in this study.
4. RESULTS

In this section, we present the results of the isophote shape measurements for the low- and high-redshift samples. In Figure 12, examples of the isophote shape measurement of the low- and high-redshift ETGs are shown. The isophote contours are well fitted by the deviated ellipses.

4.1. Relation between \(a_4\), Mass, and Size

In Figure 13, we show the distribution of the low- and high-redshift ETG samples on the mass--size (\(M_\text{M}--r_\text{e}\)) plane with the \(a_4\) parameter color coded. In this figure, \(a_4\) values are locally averaged around each data point within the plane to see global trends. For both the low- and high-redshift samples, we confirm a well-known correlation between the \(a_4\) parameter and mass, i.e., ETGs tend to be boxy with increasing stellar mass. Both in low- and high-redshift samples, the main population of ETGs changes from boxy to disky at a critical stellar mass of \(\log(M_\text{M}/M_\odot) \approx 11.5\), and the massive end is dominated by disky ETGs. Although the stellar mass of the high-redshift galaxies has a large uncertainty, as we can use only two-band photometry, the critical mass at which the main population of ETGs changes from disky to boxy is in good agreement with the characteristic mass of \(\log(M_\text{M}/M_\odot) \approx 11.3--11.5\) at which the dynamical property of nearby ETGs changes from fast to slow rotators (Emsellem et al. 2011; Cappellari et al. 2013a).

Figure 13 also shows a global trend for low-mass galaxies (\(\log(M_\text{M}/M_\odot) \lesssim 11.5\)) by which they generally become more disky with decreasing size compared at the same mass (i.e., with increasing velocity dispersion) for low- and high-redshift samples. For high-mass galaxies (\(\log(M_\text{M}/M_\odot) \gtrsim 11.5\)), because we do not have galaxies with small \(r_\text{e}\), we cannot examine the size dependence of the \(a_4\) parameter. For the most massive galaxies with \(\log(M_\text{M}/M_\odot) \gtrsim 11.7\), disky galaxies tend to be larger (\(\log(r_\text{e}/\text{kpc}) \gtrsim 1.5\)) in the low-redshift sample. We have one galaxy for the high-redshift sample in this stellar mass and effective radius range and it is disky. Our high-redshift sample lacks massive (\(\log(M_\text{M}/M_\odot) \gtrsim 11.5\)), large (\(\log(r_\text{e}/\text{kpc}) \gtrsim 1.5\)) ETGs (in other words, massive but rather small velocity dispersions of \(\sim 100\, \text{km}\, \text{s}^{-1}\), which is indicative of a disk dominated system). This may be the result of building up of quiescent disk dominated galaxies quenched in \(z < 1\) from blue population at \(z \sim 1\). The situation does not change if we plot this figure with quiescent galaxies before the morphological ETG selection. We have checked the image of massive disky galaxies in our low- and high-redshift ETG samples and found that 3 out of 15 low-redshift galaxies have spiral-like features but none of the 7 high-redshift ones have such features. The incompleteness of spectroscopy for the high-redshift sample is less likely to be the reason for the lack of massive small dispersion galaxies because morphological selection is not applied for the selection of spectroscopic targets.

Figure 13 well illustrates the transition of isophote shapes of ETGs within the mass--size plane as a function of constant velocity dispersion, which is similar to the transition of dynamical properties described in Figure 8 in Cappellari et al. (2013a). We also plot \(M_\text{M}\) and \(r_\text{e}\) of ETGs in the HST ACS Ultra Deep Field at \(z \sim 0.5--1.1\) whose isophote shapes are studied by Pasquali et al. (2006). We estimate the stellar mass from the four-band photometry (\(g, r, i, z\)) presented in Table 1 in Pasquali et al. (2006) using BC03 SSP fit with the Salpeter IMF as for our low-redshift sample, and effective radii is taken from van der Wel et al. (2014). Our high-redshift quiescent ETG sample and those of Pasquali et al. (2006) occupy similar loci on the mass--size plane, though our sample has very large and massive ellipticals because we selected ETGs in massive galaxy clusters.
In Figure 12, we exchange the axes of Figure 13, showing the distribution of the ETG samples on the $M_*-a_4$ plane with the locally averaged effective radius $r_e$ color coded. Disky ETGs are most frequent around $\log(M_*/M_\odot) \sim 10.5$, but are rare in $\log(M_*/M_\odot) > 11.5$ in both low- and high-redshift samples. On the other hand, boxy ETGs appear in all stellar mass ranges. Hence, the transition of the main population from disky to boxy with increasing stellar mass is due to the disappearance of disky galaxies in the massive end. We also plot $a_4$ and $M_*$ of the $z \sim 0.5$–1.1 ETGs from Pasquali et al. (2006). The $a_4$ parameters are taken from Table 2 in Pasquali et al. (2006) where the isophote shape parameter is not corrected for PSF as with ours. Our high-redshift ETG sample and Pasquali et al. (2006) sample have similar $M_*-a_4$ distributions.

In Figure 15, we show the distribution of the ETG samples on the $r_e-a_4$ plane, where the color code indicates the locally averaged stellar mass. As expected from Figures 13 and 14, the majority of ETGs with $\log(r_e/$kpc) \lesssim 0.5$ are disky whereas in $\log(r_e/$kpc) \gtrsim 0.5$, boxy ETGs become frequent in both low- and high-redshift samples. Because there is the size–mass relation, this critical size corresponds to $\log(M_*/M_\odot) \sim 11.5$ (see Figure 13).

4.2. Disky ETG Fraction

In Figure 16, we show the fraction of disky ETGs as a function of stellar mass. We classified ETGs with $a_4 > 0$ as disky. The fraction is calculated in three mass bins, $10.5 \lesssim \log(M_*/M_\odot) < 11.0$, $11.0 \lesssim \log(M_*/M_\odot) < 11.5$, and $11.5 \lesssim \log(M_*/M_\odot)$. The error bars indicate 16th and 84th percentiles computed by 1000-time bootstrap resampling, where the same number of galaxy is randomly resampled and the disky fraction is computed for each resampling. For comparison, we also plot the linear function fit to the disky-to-total fraction of nearby ETGs from Equation (6) in Pasquali et al. (2007), applying our cosmology parameter. The fraction of our low- and high-redshift ETGs is consistent with the linear function. Note that the stellar mass of ETGs in Pasquali et al. (2007) spans from $\log(M_*/M_\odot) \sim 11.0$ to $\log(M_*/M_\odot) \sim 11.7$.

We do not find significant differences in the disky-to-total fraction. For the highest mass bin ($11.5 \lesssim \log(M_*/M_\odot)$), the disky fraction is consistent between low- and high-redshift samples with $\sim 0.09$. The fraction appears higher in low-redshift but the difference is insignificant. If we exclude the three spiral galaxies in the low-redshift sample as contamination (see Section 4.1), the disky fraction of the low-redshift sample becomes 0.41, which is closer to that of the high-redshift (0.43) than the original low-redshift value of 0.52. Therefore, we conclude that the disky fraction for massive ETGs probably stays the same at $z \sim 1$ and 0 in the cluster environment. Since the uncertainty of the disky fraction for massive ETGs arises mainly from the small number of samples (the measurement error of $a_4$ is not large in this mass range), we need a larger sample to confirm the conclusion with higher accuracy.

For the lower mass bin ($10.5 \lesssim \log(M_*/M_\odot) < 11.0$ and $11.0 \lesssim \log(M_*/M_\odot) < 11.5$), one might find that the disky fraction of the high-redshift sample is significantly lower than that of the low-redshift sample. However, the difference may be the result of the large measurement error in $a_4$ of the high-redshift sample, which modifies the shape of the distribution of $a_4$ and can bias the disky fraction into a smaller value. This kind of bias is known as Eddington bias (Eddington 1913; Teerikorpi 2004). In the Appendix, we present the detail of the effect of measurement error of $a_4$ on the disky fraction. If we bring the measurement error of $a_4$ of the low-redshift sample equivalent to that of the high-redshift by adding Gaussian noise to $a_4$ distribution of the low-redshift sample (green open squares in Figure 16), the disky fraction of the low- and high-redshift samples would become consistent within $\sim 0.05$ (see the Appendix). In order to detect possible differences of the disky fraction, we need to increase the sample size of both the low- and high-redshift samples to $\sim 300$, 400, and 800 for...
the highest, intermediate, and lowest mass bins, or, in order to compare the disky fraction without the Eddington bias, we need to reduce the measurement error of $a_4$ of high-redshift galaxies down to an equivalent amount of that of low-redshift galaxies. Thus, we need much deeper imaging of high-redshift galaxies with spatial resolution of space-based telescope, but our imaging data are some of the deepest ones with HST. In the near future, the James Webb Space Telescope will enable us to study isophote shapes for lower mass high-redshift galaxies with much higher accuracy.

4.3. The Uncertainty of the $a_4$ Parameter

We show the measurement error of the $a_4$ parameter as a function of stellar mass in Figure 17. We can see that the error tends to decrease with increasing stellar mass. For the high-redshift quiescent ETGs, the average measurement uncertainties are $100 \times \sigma_{a_4} \sim 0.7$, $0.5$, $0.4$ at $\log(M_*/M_\odot) \sim 10.5$, $11.5$, $12.0$, respectively. For the low-redshift ones, the uncertainties are $100 \times \sigma_{a_4} \sim 0.3$, $0.2$, $0.1$ at $\log(M_*/M_\odot) \sim 10.5$, $11.5$, $12.0$.

4.4. The Relation between the $a_4$ Parameter and the Axis Ratio

In Figure 18, we plot the axis ratio against the isophote shape parameter $a_4$. The absolute value of the $a_4$ parameter tends to be small when the axis ratio is close to unity, and ETGs with small axis ratios tend to be disky for both the low- and high-redshift samples. These trends are already known for nearby ETGs (Bender et al. 1989). We also plot the field ETGs at $z \sim 0.5$–1.1 from Pasquali et al. (2006). Our high-redshift ETGs cover a similar region as theirs.

5. DISCUSSION

We discuss the evolution of ETGs in massive clusters between $z \sim 1$ and 0, based on the isophote shapes as well as other galaxy properties. A theoretical study predicts the dynamical evolution of ETGs (Khochfar et al. 2011), and observational studies have found size evolution and morphological evolution in terms of the axis ratios and Sérsic indices (e.g., Bundy et al. 2010; Damjanov et al. 2011; Cimatti et al. 2012; Newman et al. 2012; Chang et al. 2013a, 2013b; van der Wel et al. 2014; Delaye et al. 2014). However, we do not find significant evolution in the disky-to-boxy fraction between $z \sim 1$ and $\sim 0$, which suggests the isophote shapes and probably the dynamical properties of ETGs are already in place at $z > 1$. We would like to investigate the implication from these observational facts in this section.

5.1. The Effect of PSF on the Disky Fraction

First, we discuss the effect of the PSF on the disky-to-total fraction to make sure that the PSF does not affect the discussion of the evolution of the disky ETG fraction. As we have mentioned in Section 3.4, the measurement of the $a_4$ parameter is affected by the PSF. So, the difference of the PSF between low- and high-redshift samples may introduce some systematics into the evolution of the disky fraction. As the PSF sizes of low- and high-redshift samples are comparable in physical scales, what may matter are different sizes, Sérsic indices, and axis ratios of the sample galaxies.

First, the high-redshift galaxies have, on average, smaller sizes in physical scale than the low-redshift ones. However, smaller sizes only make the absolute value of observed $a_4$ small, and do not change disky to boxy (i.e., the sign of $a_4$) and vice versa.

Second, the high-redshift galaxies have similar Sérsic indices to the low-redshift ETGs in our sample. Although the distribution of the Sérsic index of the high-redshift ETGs seems to spread in a wider range (Figure 7), the Sérsic index does not alter the sign of the $a_4$ parameter.

Finally, the axis ratios of the high-redshift sample is smaller than those of the low-redshift sample; though, the statistical significance is not so high in our samples. This would increase the observed $a_4$ parameter greater for the high-redshift sample than for low-redshift, and the disky fraction of the high-redshift sample may be overestimated. If the disky fraction increases at $z \sim 1$, as predicted in Khochfar et al. (2011), and the smaller axis ratio of the high-redshift galaxy affects the disky–boxy classification, we would observe more significant evolution in the disky fraction, but we do not.

Therefore, even if we take account of the effect of the PSF, it cannot explain the fact that there is no evolution in the disky fraction. Moreover, because the differences of galaxy sizes, Sérsic indices, and axis ratios are very small between the
low- and high-redshift samples, the PSF probably affects the isophote shape measurement equally in low- and high-redshift samples, and does not probably introduce systematics in the evolution of the disky fraction.

5.2. Isophote Shapes of Massive ETGs

In the previous section, we explain that massive ETGs with \( \log(M_{*}/M_\odot) \gtrsim 11.5 \) are basically boxy for both \( z \sim 1 \) and 0 samples. This result indicates that their boxy isophote shapes and probably dynamical properties are already in place at \( z > 1 \). One important point is that the critical mass at which the main population of ETG changes from disky to boxy is consistent between \( z \sim 1 \) and 0 with the value of \( \log(M_{\text{crit}}/M_\odot) \sim 11.5 \). This is consistent with the idea that the origin of boxy ETGs is a kind of mass quenching (see Kormendy et al. 2009, and references therein). When gas accretes onto massive galaxies, a shock develops, the gas is heated to the virial temperature, and star formation is quenched. The hot gas is maintained as hot by additional accretion (Dekel & Birnboim 2006, 2008) and AGN feedback (Best et al. 2006; Best 2007a, 2007b). As a result, any mergers become dry for massive galaxies with \( M_\star \gtrsim M_{\text{crit}} \), and merger remnants tend to be boxy. The idea is supported by observational facts that blue star-forming galaxies are less massive than \( \sim 10^{11} M_\odot \) in the local universe (e.g., Baldry et al. 2004, 2006) and in the intermediate- to high-redshift universe (e.g., Bell et al. 2004; Faber et al. 2007). In addition, existence and nonexistence of X-ray emitting gas in massive and less massive ETGs (Bender et al. 1989; Pellegrini 1999, 2005; Ellis & O’ Sullivan 2006) also make the mass quenching scenario attractive (see Kormendy et al. 2009, for summary).

Theoretical studies done by Dekel & Birnboim (2006, 2008) suggest that the critical halo mass is \( \log(M_{h}/M_\odot) \sim 12 \), which corresponds to the stellar mass of \( \log(M_{*}/M_\odot) \sim 11.2 \) using a baryon-to-total mass ratio of 1/6 (Komatsu et al. 2009) as presented in Kormendy et al. (2009). This mass is in good agreement with the critical mass for the boxy–disky transition. If the mass quenching is the main origin of massive boxy ETGs, the critical mass is basically constant regardless of redshifts. Some authors suggest that these massive ETGs experience a few to several major mergers at \( z < 1 \) (Lidman et al. 2012, 2013; Shankar et al. 2015). These mergers should be dry as wet mergers convert boxy ETGs into disky (Khochfar & Burkert 2005; Naab et al. 2006). It is important to examine whether the critical mass is constant regardless of redshifts even in higher redshifts, but it is beyond the scope of this paper.

The environment may also play a role for the characterization of the isophote shapes (e.g., Shioya & Taniguchi 1993; Hao et al. 2006) and dynamical properties of ETGs (e.g., Cappellari et al. 2011b). Hao et al. (2006) present that boxy ETGs favor denser environments, while disky ETGs favor more isolated environment. IFS studies have revealed that massive, slowly rotating ellipticals are preferentially found in the central region of galaxy clusters (Cappellari et al. 2011b; D’Eugenio et al. 2013; Houghton et al. 2013; Scott et al. 2014). We investigate the disky fraction for ETGs in the inner and outer region of each cluster, separating the high- and low-redshift samples by the cluster centric radius \( r_{\text{CL}} \) with \( \log(r_{\text{CL}}/\text{kpc}) \leq -0.4 \) or \( > -0.4 \). As in the previous section, we calculate the disky fraction in three mass bins. We have confirmed that the disky fraction increases in the outer region in all mass bins for the low-redshift sample. However, we cannot obtain a meaningful result for the high-redshift sample due to the small number of samples, especially in the outer region. For a better understanding about the environmental effect on the disky fraction at high-redshift, we need to increase the number of sample in the outer region of galaxy clusters or less dense environment.

5.3. Morphological Evolution of Less Massive ETGs in the Dense Environment

For less massive ETGs with \( \log(M_{*}/M_\odot) \lesssim 11.5 \), where disky ETG is the dominant population, the disky fraction is consistent between \( z \sim 1 \) and 0 in this mass range, and the higher disky (fast rotator) fraction at high redshift predicted by a theoretical study (Khochfar et al. 2011) is not observed.

Chang et al. (2013a, 2013b) study evolution of the intrinsic shape (oblate or triaxial) of ETGs residing in the field environment using distributions of projected axis ratios. They present that for ETGs with \( 10.5 < \log(M_{*}/M_\odot) < 11.5 \), the fraction of oblate ETGs is higher at \( z > 1 \). If we interpret the oblate-triaxial classification as a disky–boxy (i.e., fast–slow rotator) classification, the fact that no significant increase in the disky fraction is found in this study seems to be inconsistent with the increase of the oblate fraction. However, because our ETGs reside in very massive clusters, we need to take account of the evolution of ETGs in such an environment. For example, evolution of the size of ETGs is different between field and...
cluster environments. Field ETGs at \( z \sim 1 \) smaller sizes than the local counterparts (e.g., Trujillo et al. 2007; Damjanov et al. 2011; Cimatti et al. 2012; Newman et al. 2012; van der Wel et al. 2014). However, Delaye et al. (2014) report that the average size of ETGs living in massive clusters at

\[ 0.8 < z < 1.5 \]

appear to be, on average 1.5 times larger than those residing in the field at similar redshifts when compared at the same mass. We note that Andreon et al. (2016) present an opposite result from Delaye et al. (2014), but this may be due to different morphological selection criteria as noted by the authors: Andreon et al. (2016) apply more strict selection criteria to avoid disk-like quiescent galaxies. The distribution of the axis ratio may also be different between environments. Although axis ratios of our high-redshift ETGs are smaller than those of our low-redshift ones, the axis ratio distribution of the high-redshift sample is not as flat as the field sample at \( z \sim 1 \) in Chang et al. (2013a, 2013b). While the axis ratio histogram of the field sample at \( 1 < z < 2.5 \) in the stellar mass range of \( 10.8 < \log(M_* / M_\odot) < 11.5 \) has a peak around \( q \sim 0.6 \) (see Figure 5 in Chang et al. 2013b), our cluster ETGs at \( z \sim 1 \) have peaks at \( q \sim 0.7 \sim 0.8 \). Thus, the cluster ETG sample probably has a lower oblate-to-triaxial fraction than the field sample. The difference of the sizes and axis ratios between clusters and fields indicates that the morphological evolution of ETGs should be weaker in a dense environment at \( z < 1 \). It may be worthwhile to investigate evolution of isophote shapes of filed ETGs in future work as their morphological evolution is expected to be more pronounced. In the rest of this section, we focus on the evolution of ETGs in a dense environment.

Although the size evolution of ETGs seems to be weak at \( z < 1 \), some authors report the evolution of morphology of ETGs in massive clusters between \( z \sim 1 \) and 0. Mei et al. (2012) present that galaxies in the Lynx super cluster at \( z = 1.3 \) show high fractions of red, bulge-dominated disk galaxies.
Cerulo et al. (2014) claim that the main population of intermediate mass ETGs in massive cluster changes from bulge-dominated disk galaxies at $z \sim 1$ to elliptical galaxies at $z \sim 0$. De Propris et al. (2015) also report the evolution of the axis ratio and the Sérsic index but no size evolution, comparing ETGs in massive clusters at $z \sim 1$ and those in the Virgo cluster. They conclude that ETGs in the dense environment at $z \sim 1$ have similar size but are, on average, more flat and less concentrated than local ones. Bundy et al. (2010) show an increase of massive ($M_* \gtrsim 10^{11} M_\odot$) ETGs and a decline of log($M_*/M_\odot$) $\sim 11$ bulge-dominated spiral galaxies with Sérsic index $1.25 < n < 2.5$ from $z \sim 1$ to $0$, though their sample is taken from the COSMOS field. They infer that at least 60% of the bulge-dominated spiral galaxies are transformed into ETGs (e.g., S0s) on the scale of 1–3 Gyr, and that these transformations might occur as a single major merger event or through multiple evolutionary stages, including disk disruption by minor mergers or accretion of cold gas in star-forming galaxies.

Feldmann et al. (2011) simulated the formation of a group of galaxies, and found that while elliptical galaxies are formed in mergers at $z > 1$, before the merging progenitors fall within the virial radius of the group, unmerged disk galaxies are turned into red-and-dead disks in the group environment due to shutting down of gas accretion and stripping of gas. Thus, based on their simulation, the disk-like ETGs in massive clusters at $z \sim 1$ may originate from quenched disk galaxies. Carollo et al. (2013, 2014) present that quenching and fading of disk galaxies may be responsible for the apparent size evolution of ETGs as a function of time.

Possible mechanisms for fading of disk galaxies into ETGs in a dense environment are not only mergers but also secular evolution. Oesch et al. (2010) found that intermediate mass (log($M_*/M_\odot$) $\gtrsim 11$) disk galaxies are present at $z = 1$ in the COSMOS, but vanish by $z = 0.2$, and suggest that these disk galaxies may be transformed into ETGs by secular evolution because the merger rate is too low to account for the observed decrease in their space densities.

As the disky fraction is consistent between $z \sim 1$ and 0, we suggest that the disk-like ETGs found in massive clusters at $z \sim 1$ (e.g., Cerulo et al. 2014; De Propris et al. 2015), which should simply appear as disky ETGs in this study, are transformed into disky elliptical or S0s in the local universe rather than boxy ETGs. To constrain the process responsible for the evolution, we compare the size–mass relation between the high- and low-redshift samples separately for boxy and disky ETGs within the stellar mass range of $10.5 < \log(M_*/M_\odot) \lesssim 11.5$. In Figure 19, we plot the size–mass relation and histograms of the mass normalized size $r_{e,M_*}$. For boxy ETGs, the median sizes are $\langle \log(r_{e,M_*}/\text{kpc}) \rangle = 0.67 \pm 0.03$ and $0.54 \pm 0.03$ for the low- and high-redshift samples, respectively. For disky ETGs, the median mass normalized sizes are $\langle \log(r_{e,M_*}/\text{kpc}) \rangle = 0.62 \pm 0.03$ and $0.53 \pm 0.06$ for the low- and high-redshift samples, respectively. The KS test gives the $p$-value of 0.0034 and 0.029, respectively, for boxy and disky, which indicates that the differences of the distributions between high- and low-redshift samples are significant. We conclude that both the boxy and disky ETGs grow their size in $z < 1$. The process of the size growth for the ETGs should not be accompanied with the transformation of the isophote shapes and probably dynamical properties, considering the constant disky fraction in $z < 1$.

Considering the constant disky fraction, we suggest that the main cause of the size growth and the morphological evolution of the intermediate mass ETGs in cluster environment may be less violent processes than mergers, such as accretion of low-mass galaxies onto outskirts. Even if mergers occur, the mass ratio should be large enough (i.e., the progenitor mass must be enough unequal) not to convert disky isophote shapes into boxy, as major mergers (Naab et al. 1999; Naab & Burkert 2003) or dry mergers with small mass ratios (Khochfar & Burkert 2005; Naab et al. 2006) can convert disky ETGs into boxy.

We should be cautious about the progenitor bias (e.g., van Dokkum & Franx 1996; Saglia et al. 2010), i.e., blue star-forming disk galaxies at $z \sim 1$ may enter into the quiescent ETG sample at $z \sim 0$. If newly quenched star-forming disks with larger typical sizes appear as disky ETGs at $z \sim 0$, the disky fraction might be constant even if some part of disky ETGs at $z \sim 1$ is converted into boxy, and the size growth in disky ETGs between $z \sim 1$ and 0 may be observed.

To check whether newly quenched galaxies significantly contaminate the low-redshift disky ETGs, we have compared the color of the low-redshift ETGs between disky and boxy. We compute $u - g$ color in two apertures, the Petrosian and the central 3 arcsec apertures. If the low-redshift disky ETGs contain significant fractions of newly quenched galaxies, the average color becomes bluer in disky than in boxy especially in the Petrosian apertures, which contain lights from the outer disk with younger age than the central bulge, assuming that the newly quenched disks become disky ETGs. However, there is no significant difference in the average color and color distribution between disky and boxy ETGs in both Petrosian and 3 arcsec apertures. Thus, we conclude that the low-redshift disky ETGs are not contaminated by newly quenched disks, and the evolution of the disky fraction is not affected by the progenitor bias. This is also supported by the fact that the low-redshift disky and boxy ETGs have similar sizes.

![Figure 19](image-url)
We measured the isophote shapes of ETGs in massive galaxy clusters at redshift $z \sim 1$ and 0 to investigate the evolution of the dynamical properties of ETGs.

We create a high-redshift quiescent ETG sample residing in massive galaxy clusters at $z \sim 1$ using imaging and spectroscopic data obtained in the HST Cluster SN Survey (Dawson et al. 2009). We selected spectroscopic members of the $z \sim 1$ clusters. Then, red galaxies are chosen based on the central $I_{775} - z_{850}$ color as quiescent galaxies. Finally, ETGs are picked up from the quiescent galaxies using the concentration index and surface brightness.

We also prepare the low-redshift quiescent ETG sample in massive clusters at $z \sim 0$ using SDSS DR12 (Alam et al. 2015) for comparison. We selected quiescent galaxies using the color–magnitude diagram with the help of the stellar mass-age and stellar mass–metallicity relation (Thomas et al. 2005) and BC03 SSP models (Bruzual & Charlot 2003). Then, ETGs are selected based on the concentration index and surface brightness.

We develop an isophote shape analysis code, which can be used for high-redshift galaxies with low surface brightness and small apparent sizes based on Bender & Möllenhoff (1987). We have confirmed with a nearby galaxy that our code gives the consistent result to previous studies. We also estimate the effect of PSF on the isophote shape measurement, and find that the small axis ratio makes the measured $a_4$ value larger than the intrinsic one while the galaxy size and Sérsic index only changes the absolute value of the parameter. As the PSF size in physical scales are similar between high- and low-redshift samples, and as the axis ratios, galaxy sizes and Sérsic indices do not change very much between these redshifts, we conclude that the effect of PSF does not introduce systematics to the evolution of the disky fraction.

Our results can be summarized as follows. First, the parameter correlations between $a_4$ and other galaxy properties such as the stellar mass and size are similar between $z \sim 1$ and $z \sim 0$ samples: ETGs tends to be boxy with increasing stellar mass or size. Second, the main population of ETGs changes from disky to boxy at a critical mass of $\log(M_e/M_*) \sim 11.5$ regardless of the redshifts, with the massive end dominated by boxy galaxies. Finally, we do not find significant difference in the disky to total ETG fraction between $z \sim 1$ and 0.

The fact that the massive ETGs ($\log(M_e/M_*) \gtrsim 11.5$) are basically boxy at $z \sim 1$ indicates that the isophote shapes and probably the dispersion-dominated dynamics are characterized at higher redshifts. The constant critical mass between $z \sim 1$ and 0 is consistent with the mass quenching scenario, where shock-heated gas produced in a halo with $\log(M_{\text{halo}}/M_*) \gtrsim 12$ and/or AGN feedback make mergers dry to produce boxy ETGs (Kormendy et al. 2009, and references therein). This halo mass corresponds to the stellar mass of $\log(M_e/M_*) \sim 11.2$ assuming a baryon fraction of 1/6, which is in good agreement with the critical mass of boxy–disky transition of the high- and low-redshift ETGs in our sample.

The environment may also play a role in characterizing isophote shapes and dynamical properties. However, we need a larger number of high-redshift ETG samples especially in the outer regions of galaxy clusters to investigate redshift evolution in the disky fraction.

For less massive ETGs, where the disky galaxy is the dominant population, the morphological evolution and size growth are reported in previous studies. ETGs in massive clusters at $z \sim 1$ tend to be more flattened, less concentrated, in other words, more disk-like, and small. Considering the constant disky ETG fraction, we suggest that disk-like ETGs, which should simply appear as disky ETGs in this study, in massive clusters at $z \sim 1$ are transformed into disky ellipticals or S0s in the local universe. The main cause of the size and morphological evolution should be less violent processes than mergers such as the accretion of low-mass galaxies onto outskirts. Even if mergers occur, the progenitor mass must be unequal enough not to convert disky isophote shapes into boxy, as major mergers (Naab et al. 1999; Naab & Burkert 2003) or dry mergers with small mass ratios (Khochfar & Burkert 2005; Naab et al. 2006) can convert disky ETGs into boxy.

We thank the very helpful referee for comments and suggestions that improved the quality of this paper. We also thank Mitsuru Kokubo for a number of discussions about the bias on the disky fraction. K.M. thanks Masami Ouchi and Stefano Andreon for helpful comments and advice. K.M. also thanks Chris Lidman for encouraging comments. Financial support for this work was provided by NASA through program GO-10496 from the Space Telescope Science Institute, which is operated by AURA, Inc., under NASA contract NAS 5-26555. This work was also supported in part by the Director, Office of Science, Office of High Energy and Nuclear Physics, of the U.S. Department of Energy under Contract No. AC02-05CH11231, as well as a JSPS core-to-core program International Research Network for Dark Energy and by JSPS research grants (20040003, 23340041, 26287029). This work was supported by JSPS Program for Advancing Strategic International Networks to Accelerate the Circulation of Talented Researchers. The authors wish to recognize and acknowledge the very significant cultural role and reverence that the summit of Maunakea has always had within the indigenous Hawaiian community. We are most fortunate to have the opportunity to conduct observations from this mountain. Finally, this work would not have been possible without the dedicated efforts of the daytime and nighttime support staff at the Cerro Paranal Observatory. Funding for SDSS-III has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, and the U.S. Department of Energy Office of Science. The SDSS-III website is http://www.sdss3.org/. SDSS-III is managed by the Astrophysical Research Consortium for the Participating Institutions of the SDSS-III Collaboration including the University of Arizona, the Brazilian Participation Group, Brookhaven National Laboratory, Carnegie Mellon University, University of Florida, the French Participation Group, the German Participation Group, Harvard University, the Instituto de Astrofísica de Canarias, the Michigan State/Notre Dame/JINA Participation Group, Johns Hopkins University, Lawrence Berkeley National Laboratory, Max Planck Institute for Astrophysics, Max Planck Institute for Extraterrestrial Physics, New Mexico State University, New York University, Ohio State University, Pennsylvania State University, University of Portsmouth, Princeton University, the Spanish Participation Group, University of Tokyo, University of Utah, Vanderbilt University, University of Virginia, University of Washington, and Yale University. This research made use of NASA’s Astrophysics Data System. This research made use of the NASA/IPAC...
Extragalactic Database (NED), which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration.

Facilities: HST(ACS), Subaru (FOCAS), KECK:II (DEIMOS), VLT:Kueyen (FORS1), VLT:Antu (FORS2), Sloan (SDSS).

APPENDIX A
EFFECTS OF THE DIFFERENCE OF THE IMAGE QUALITY BETWEEN LOW- AND HIGH-REDSHIFT SAMPLES

Because image quality such as the PSF size and S/N is different between high- and low-redshift samples, it is important to assess how the difference of image quality affects our results. What may matter is the difference of S/N because the size of the PSF is comparable in physical scale between low- and high-redshift samples (see Section 2.2). In this section, we present results of simulations to see how degrading of S/N affects the measurement of some important parameters in this paper. We degraded images of the low-redshift sample galaxies by adding Gaussian noise to make S/Ns comparable to that of high-redshift ones, and then measured morphological and structural parameters such as Gini coefficient, asymmetry, concentration index, surface brightness, effective radius, axis ratio, and Sérsic index as well as isophote shape parameters such as $a_4$.

A.1. Image Degradation of the Low-redshift Galaxies

We degrade images of the low-redshift sample galaxies in the following way. First, we determine the amount of noise added onto the low-redshift galaxy images. The surface brightness becomes fainter by $(1+z)^{-2}$ with increasing redshift due to cosmological dimming. At the same time, galaxies become brighter as they have larger amounts of bright young stars at higher redshift, and the amount of luminosity evolution depends on star formation and assembly history of galaxies.

As star formation and assembly history is complicated, we need some assumptions on the luminosity evolution. Here, we just adopt the difference of average luminosity between high- and low-redshift samples compared at the same stellar mass as the luminosity evolution. In three mass ranges of $10.5 \leq \log(M_*/10^{10} M_\odot) < 11.0$, $11.0 \leq \log(M_*/10^{10} M_\odot) < 11.5$, and $11.5 \leq \log(M_*/10^{10} M_\odot)$, we fit linear functions $M_g(z_{580}) = a(\log(M_*/10^{10} M_\odot)) + b$, where $M_0$ is the lower limit for these mass ranges (i.e., $10.5$, $11.0$, $11.5$), $a$ and $b$ are the fitting parameters.

For low-redshift quiescent galaxies, we obtained the fitting functions, $M_g = -1.14(\log(M_*/10^{10} M_\odot) - M_0) - 19.9$, $-1.43(\log(M_*/10^{10} M_\odot) - M_0) - 20.5$, and $-1.66(\log(M_*/10^{10} M_\odot) - M_0) - 21.2$, respectively, for $10.5 \leq \log(M_*/10^{10} M_\odot) < 11.0$, $11.0 \leq \log(M_*/10^{10} M_\odot) < 11.5$, and $11.5 \leq \log(M_*/10^{10} M_\odot)$. For high-redshift quiescent galaxies, we obtained the fitting functions, $M_g(z_{580}) = -1.11(\log(M_*/10^{10} M_\odot) - M_0) - 21.9$, $-0.896(\log(M_*/10^{10} M_\odot) - M_0) - 22.7$, and $-1.31(\log(M_*/10^{10} M_\odot) - M_0) - 23.3$. Because the difference of the parameter $b$ is $\sim 2.0$ in all stellar mass bins, we adopt $2.0$ mag as the luminosity evolution. This is largely consistent with the luminosity evolution of $\sim 2$--$3$ mag for galaxies with $\log(M_*/10^{10} M_\odot) = 11$--$12$ predicted by BC03 SSP models assuming passive evolution with no merger.

Considering the luminosity evolution of $2.0$ mag and cosmological surface brightness dimming between at $z \sim 1.2$ ($SB_{\text{dim}} = -2.5 \log(1+z)^{-4} \sim 3.4$) and $z \sim 0.031$ ($SB_{\text{dim}} \sim 0.1$), the surface brightness of the low-redshift galaxies in the g band should be observed to be brighter by $0.7$ mag than that of the high-redshift galaxies in $z_{580}$. For example, the surface brightness of $25.0$ mag arcsec$^{-2}$ in $z_{580}$ of a galaxy at $z \sim 1.2$ is intrinsically $21.6$ mag arcsec$^{-2}$ without cosmological dimming. As it would evolve to be fainter by $2.0$ mag at low-redshift, the surface brightness would be $23.6$ mag arcsec$^{-2}$ in $g$ without cosmological dimming. Finally, considering cosmological dimming at $z \sim 0.031$, the observed surface brightness of the low-redshift galaxy is $23.7$ mag arcsec$^{-2}$ in $g$.

We generate the degraded images of the low-redshift galaxies based on the discussion above. The $1\sigma$ background noise level per pixel of our high-redshift sample is equivalent to $\sigma_{\text{bkg,High-z}} = 24.7$ mag arcsec$^{-2}$ in $z_{580}$ on average. Therefore, if the background noise is $\sigma_{\text{bkg,High-z}} = 23.4$ mag arcsec$^{-2} = 2.22 \times 10^{-18}$ erg s$^{-1}$ cm$^{-2}$ Å$^{-1}$ arcsec$^{-2}$, the S/N becomes comparable between high and low redshift at the surface brightness level. Since $\sigma_{\text{bkg,Low-z}}$ of the original $2 \times 2$-binned images of the low-redshift galaxies is $1.05 \times 10^{-18}$ erg s$^{-1}$ cm$^{-2}$ Å$^{-1}$ arcsec$^{-2}$, we create the degraded images by adding Gaussian noise to the original images binned by $2 \times 2$ pixels. One sigma of the added Gaussian noise corresponds to $\Delta\sigma_{\text{bkg}} = \sqrt{\sigma_{\text{bkg,High-z}}^2 - \sigma_{\text{bkg,Low-z}}^2} = 1.96 \times 10^{-18}$ erg s$^{-1}$ cm$^{-2}$ Å$^{-1}$ arcsec$^{-2}$.

A.2. Effects of the Image Degradation on the Morphological Parameters

Using original and degraded images, we measure the Gini coefficient (Abraham et al. 2003), asymmetry (Abraham et al. 1996), concentration index (Doi et al. 1993), and mean surface brightness (Doi et al. 1993), and investigate which parameters are insensitive to the degrading S/N of an image. We use interloper-subtracted images in this procedure. We run SExtractor and GALFIT with the degraded images in the same manner as the original to obtain the interloper-subtracted version of the degraded images.

We measure the Gini coefficients and asymmetry following Meyers et al. (2012). The Gini coefficient is measured within a quasi-Petrosian aperture. First, the preliminary aperture is prepared by collecting all pixels exceeding $1.0\sigma_{\text{bkg}}$ above the background level and contiguous to the center of the target, where $\sigma_{\text{bkg}}$ is $1\sigma$ background noise per pixel. We smooth the image with a Gaussian kernel of $\sigma = 2$ pixels when we take $1\sigma$ isophote. In the preliminary aperture, we compute the quasi-Petrosian flux (Abraham et al. 2007) with the original image rather than the smoothed one. Then, the quasi-Petrosian aperture is created by collecting pixels exceeding the quasi-Petrosian flux in the preliminary aperture with the original image. We calculate the Gini coefficient within this quasi-Petrosian aperture. The error is estimated from bootstrap resampling of the pixels in the aperture (Abraham et al. 2003).
We randomly resample the same number of pixels from the aperture allowing overlaps, then recompute the Gini coefficient with the resampled pixels. We recompute the Gini coefficient this way 1000 times to determine the probability distribution function of the Gini coefficient for each galaxy and record the standard deviation of this distribution as the Gini coefficient error.

The asymmetry with symmetrized aperture consisting of the intersection of the quasi-Petrosian aperture with its 180 deg rotation. The rotation center is iteratively determined so that the measured asymmetry is minimized. Because background noise has some contribution to the measured asymmetry, we estimate the amount of contribution and subtract it from the measured asymmetry. We generate 1000 artificial background images with Gaussian fluctuation with a standard deviation of $s_{bg}$ and measure their asymmetry in the same aperture as for the target. We subtract the average of the 1000 asymmetry measurement of the background, and adopt the standard deviation as an estimate of error because the noise of our image is dominated by background. How we measure the concentration index and mean surface brightness is described in Section 2.5.

In the top panels in Figure 20, we compare the morphological parameters measured in original images and in degraded images. The Gini coefficient tends to be systematically smaller and the asymmetry has a large scatter when measured in the degraded images. On the other hand, the concentration index $C_{in}$ is less affected by the image degradation in the systematic sense. The mean surface brightness $SB_{24.5}$ is less affected than the Gini coefficient and asymmetry; though, a few galaxies have larger value in the degraded images. Considering this, we decided to make use of concentration and surface brightness for ETG selection in this paper (see Section 2.5). The Gini coefficient is also useful for detecting multiple flux peaks (Abraham et al. 2003), e.g., merging systems, but as we simply focus on ETGs, the flux concentration is enough for our purpose, which is another reason why we use the concentration rather than the Gini coefficient. The surface brightness is a useful parameter to classify galaxy morphology as it appears in the Fundamental Plane (Djorgovski & Davis 1987). We note that because we have spectroscopic redshift, we can correct the cosmological surface brightness dimming safely.

A.3. Effects of the Image Degradation on the Structural Parameters

We investigate the effects of the image degradation on the structural parameters such as the effective radius, axis ratio, and Sérsic index measured by GALFIT presented in Section 2.6.

Figure 20. Top panels: comparison of the morphological parameters, the Gini coefficient (a), asymmetry (b), concentration index (c), and mean surface brightness (d), of the low-redshift quiescent galaxies between those measured in original image (x axis) and in degraded images (y axis). Middle panels: comparison of the structural parameters, the effective radius (e), axis ratio (f), and Sérsic index (g) measured by GALFIT of the low-redshift quiescent ETGs between those measured in the original image (x axis) and in degraded images (y axis). Bottom panels: comparison of the isophote shape parameters, $a_4/a$ (h) and axis ratio (i) measured from isophote shapes of the low-redshift quiescent ETGs between those measured in original image (x axis) and in degraded images (y axis). For all panels, green dashed–dotted lines represent $y = x$ for reference, and median measurement uncertainty is given by error bars.
In the middle panels in Figure 20, we compare the structural parameters measured in original images and in degraded images. While effective radii and axis ratios are not affected very much by the image degradation with small scatters, Sérsic indices measured in degraded images have large scatters.

A.4. Effects of the Image Degradation on the Isophote Shape Parameters

We also investigate the effects on the image degradation on the isophote shape parameters presented in Section 4. In the bottom panels in Figure 20, we compare the $a_4$ and axis ratios measured from isophote shape analysis. The $a_4$ parameters have quite large scatter with small systematics $\Delta a_4/a \sim -0.2\%$ compared to the uncertainty when they are measured in the degraded images. However, because large uncertainty affects the shape of the distribution of the $a_4$ parameter, the disky-to-total fraction is affected by large measurement uncertainty, which is presented in the next subsection. The axis ratio measured from isophote shape tends to be large by $\sim 0.04$.

APPENDIX B
THE DISKY FRACTION AFFECTED BY THE UNCERTAINTY OF THE $a_4$ PARAMETER

We present how the distribution of the $a_4$ parameter and the disky-to-total fraction are affected by the measurement uncertainty of $a_4$. We have carried out Monte-Carlo simulations in which the $a_4$ parameters of low- and high-redshift samples are resampled after Gaussian noises are added and then the disky fractions are computed in each resample. We have investigated how the disky fraction changes as functions of the uncertainty of the $a_4$ parameter. In the left panels of Figure 21,
we present the simulated disky fraction as functions of the uncertainty of the a4 parameter. Here the uncertainty (x axis) is computed as the square root of the quadratic sum of the median of the original measurement uncertainty in a stellar mass bin and σ of the Gaussian noises added in the simulations. For the lower stellar mass bins (log(Mσ/MBH) < 11.5), the disky fraction decreases with the increasing uncertainty. We also plot the disky fraction of the low-redshift sample measured with the degraded images with cyan crosses in the figure, which are also smaller than the original value and comparable to the fraction of the high-redshift sample within uncertainty.

The decrease of the disky fraction is probably due to the fact that the shape of the distribution of the a4 parameter is modified by the uncertainty. In the right panels in Figure 21, we present the histograms of the a4 parameter. For the lower stellar mass bins (log(Mσ/MBH) < 11.5), the histograms of the low-redshift sample simulated with equivalent a4 uncertainty to the high-redshift sample (green solid lines) are larger than the original low-redshift sample (blue dashed line) in the boxy bins (a4/a ≤ 0). This bias (Eddington bias, Eddington 1913; Teerikorpi 2004) occurs when the distribution functions (here, the histograms of a4/a) have second- or higher-order differential terms. In the cases in the right panels in Figure 21, when the noises are added, the number of galaxies moving from the disky side to the boxy side is larger than that from boxy to disky. The disky fraction would asymptotically reach 0.5 when we increase the added noises because the distribution would be flat. Taking account of the Eddington bias, i.e., if we compare the disky fractions of the low-redshift sample simulated with equivalent a4 uncertainty to the high-redshift sample, they become comparable to those of the high-redshift within uncertainty. In order to detect possible differences of the disky fraction, we have to increase the sample size of both the low- and high-redshift samples to ∼300, 400, and 800 for the highest, intermediate, and lowest mass bins. In order to compare disky fraction without Eddington bias, we have to decrease the measured uncertainty of the a4 parameter of the high-redshift sample, which will be possible with the next generation of telescopes.

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