The Chaotic History of the Retrograde Multi-planet System in K2-290A Driven by Distant Stars

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Abstract

The equator of star K2-290A was recently found to be inclined by 124° ± 6° relative to the orbits of both of its known transiting planets. The presence of a companion star B at ~100 au suggested that the birth protoplanetary disk could have tilted, thus providing an explanation for the peculiar retrograde state of this multi-planet system. In this work, we show that a primordial misalignment is not required and that the observed retrograde state is a natural consequence of the chaotic stellar obliquity evolution driven by a wider-orbit companion C at >2000 au long after the disk disperses. The star C drives eccentricity and/or inclination oscillations on the inner binary orbit, leading to widespread chaos from the periodic resonance passages between the stellar spin and planetary secular modes. Based on a population synthesis study, we find that the observed stellar obliquity is reached in ~40%–70% of the systems, making this mechanism a robust outcome of the secular dynamics, regardless of the spin-down history of the central star. This work highlights the unusual role that very distant companions can have on the orbits of close-in planets and the host star’s spin evolution, connecting four orders of magnitude in distance scale over billions of orbits. We finally comment on the application to other exoplanet systems, including multi-planet systems in wide binaries.

Unified Astronomy Thesaurus concepts: Exoplanet astronomy (486); Exoplanet dynamics (490); Exoplanet evolution (491); Multiple stars (1081)

1. Introduction

The K2-290A star (EPIC 249624646; an F8 star of 1.19 $M_\odot$) was found to host two transiting planets: a mini-Neptune at a 9 day orbit and a warm Jupiter with an orbital period of 48 days (Hjorth et al. 2019). From adaptive optics imaging and Gaia data, the authors identify two M-dwarf companions at projected separations of ~110 au and ~2500 au. You can find all the relevant parameters in Figure 1.

Furthermore, not only is K2-290 a triple stellar system hosting planets, but it was later found in Hjorth et al. (2021) that both of its planets have retrograde stellar obliquities (124° ± 6° obliquity with respect to their host star spin axis). This retrograde state is unique among the current sample of compact multi-planet systems with nearly a dozen well-aligned ones and a handful of misaligned, still prograde, ones (see the recent discussion in Wang et al. 2021).

The extreme orbital tilt and the unusual presence of two companions stars suggest a peculiar dynamical evolution for K2-290. Other systems with misaligned ($\phi \sim 40^\circ$) multi-planet systems include Kepler-56 (Huber et al. 2013; Otor et al. 2016) and Kepler-129 (Zhang et al. 2021), and may be explained by interactions with the detected distant Jovian-sized planets in the systems (Boué & Fabrycky 2014; Li et al. 2014; Gratia & Fabrycky 2017). A more extreme example is the polar system HD3167 (Dalal et al. 2019), which may still be accommodated by interplanetary interactions by a yet undetected companion (Boué & Fabrycky 2014; Petrovich et al. 2020).

Although retrograde systems do exist, these correspond to lonely short-period planets—hot Jupiters and warm Netpunes. These systems likely acquired their stellar obliquities via a different path, possibly by high-eccentricity migration (e.g., Dawson & Johnson 2018), a process that is forbidden for multi-planet systems like K2-290 (Mustill et al. 2015).

An explanation provided by Hjorth et al. (2021) for the retrograde orbits of K2-290b and c is that the birth protoplanetary disk tilted relative to the host star’s equator (Batygin 2012). Here, an inclined binary companion B would tilt the disk, while the disk dispersal leads to a secular resonance that tilts the host star spin’s axis, sometimes reaching retrograde states (Lai 2014; Spalding & Batygin 2014). Although this may be a reasonable possibility and calculations show that it can reproduce the system’s obliquity for typical parameters, there is a fair amount of uncertainty, including the disk size and dispersal history, planet migration, star–disk coupling, and so on, that may inhibit the occurrence of the resonance (Zanazzi & Lai 2018). Moreover, the questions of whether the stellar obliquity in the disk phase becomes the observed obliquity after billions of years and the role of the third star C remain unaddressed.

Motivated by these questions and by the striking fact that all the relevant precession timescales in the system are comparable, we study the long-term evolution of K2-290A’s stellar obliquity. Our paper is organized as follows. In Section 2 we describe our methods. In Section 3 we show our results, a population synthesis and a physical description of the mechanism that drives obliquity excitation. We discuss our results in Section 4 and present our conclusions in Section 5.
2. Procedure

We simulate the long-term evolution of the system using a secular set of equations described in the Appendix. This allows us to quickly evolve the system for up to 5.6 Gyrs (the upper limit on the age estimate for the central star).

As some parameters are not well constrained (e.g., the mass of planet b, distance to the companion stars, initial rotational period of the central star, etc.) we explore this parameter space and see which combinations reproduce the desired outcome.

2.1. Simplifying the Problem

The K2-290 system is composed of 5 bodies (3 stars, 2 planets), which would mean 10 pair-wise interaction terms. However, only a fraction dominates the dynamics and this allows us to simplify the problem.

The most important simplification is to consider the two planets effectively locked together (i.e., sharing their orbital planes). This coupling is justified using Equation (12) from Lai & Pu (2016):

$$
\epsilon_{b,c} \approx \left( \frac{M_B}{10^3 m_c} \right) \left( \frac{10a_c}{a_B} \right)^3 \left[ \frac{3a_b/a_c}{b_{bc}^{1/2}(a_b/a_c)} \right] \left[ \frac{(a_c/a_B)^{3/2} - 1}{1 + (L_b/L_c)} \right].
$$

which results in $\epsilon_{b,c} \sim 2 \times 10^{-5}$ for the values in Figure 1, assuming $M_B = 7.6 M_\odot$; this means that the two planets are strongly coupled together and their mutual inclination could only reach values in the same order when perturbed by star B.

A similar conclusion is reached comparing with stellar $J_2$. Also, we assume their orbits remain circular as the precession rate $\Omega$ for planet c due to its inner companion is higher than the precession induced by star B even for high values of $e_B \sim 0.99$ (Equation (10) from Denham et al. 2018).

Further simplifications include planets b and c interacting with star C only indirectly via star B, justified since the torque from C is weaker than that of B by a factor of $(b_B/b_C)^3 \sim 10^{-4}$. We also assume that the planets do not torque stars B and C.

\footnote{In Hjorth et al. (2019) there is the possibility for a nonzero eccentricity of planet c, although reported values are for circular orbits and to 3σ they report an upper limit on the eccentricity of 0.241.}

2.2. Precession Frequencies

From the equations of motion in the Appendix, we can evolve the stellar spin axis and planetary angular momentum vectors as

$$
\frac{ds}{dt} = \hat{\Omega}_{b,c} (s \times \hat{j}_{b,c}),
$$

$$
\frac{d\hat{j}_{b,c}}{dt} = \hat{\Omega}_{bc,B} (\hat{j}_{b,c} \times s) + \hat{\Omega}_{bc,S} (\hat{j}_{b,c} \times \hat{j}_B),
$$

where $\hat{j}_{b,c}$ is the unit vector of the angular momentum of both planets and $\Omega$ are precession frequencies. The magnitudes of angular momenta are $L_{b,c} = m_b \sqrt{M_A a_b} + m_c \sqrt{M_A a_c}$ and that of the spin is $S = k_2 M_B R_A^2 \Omega_z$.

The precession frequencies are approximated by

$$
\hat{\Omega}_{bc,S} = \frac{3 J_2 (GM_A^7/2 R_A^2)}{2 \left( m_b \sqrt{a_b} + m_c \sqrt{a_c} \right)^3} \left( m_b/a_b + m_c/a_c \right) \cos(i_{b,c})
\approx 0.28 \text{Myr}^{-1} \left[ 0.5 + 0.45 \left( \frac{3 m_b}{m_c} \right) \left( \frac{J_2}{3 \times 10^{-6}} \right) \cos(i_{b,c}) \right],
$$

where we have used the quadrupole moment of the central star $J_2 \approx \frac{1}{6} k_2^2 (GM_A^7/2 R_A^2)$ (Ward et al. 1976) with $k_2$ its stellar Love number and

$$
\hat{\Omega}_{b,c} = \hat{\Omega}_{bc,c} \left( \frac{S}{L} \right)^{0.45} \left( \frac{6.63 \text{d}}{P_z} \right) \hat{\Omega}_{bc,s},
$$

where $P_z$ is the period of the central star and we have assumed that $k_2 = 0.06$.

In turn, for the planets and star B we get:

$$
\hat{\Omega}_{bc,B} = \frac{3 G^{1/2} M_B a_c^{3/2} \cos(i_{b,c,B})}{4 a_B M_A^{1/2}} \left( 1 - e_B^2 \right)^{3/2}
\approx 0.23 \text{Myr}^{-1} \left( \frac{100 \text{au}}{a_B} \right)^{3/2} \cos(i_{b,c,B}) \left( \frac{1 - e_B^2}{1 - e_B^2} \right)^{3/2},
$$

where we have assumed that the star B only couples to the outer planet c. This is reasonable as the outer planet will precess faster due to B by a factor of $(a_c/a_B)^{3/2} = 5.25$ compared to planet b.
Finally, the A–B binary undergoes nodal precession and/or eccentricity/inclination oscillations due to star C in a von Zeipel–Lidov–Kozai (ZLK) oscillation timescale (von Zeipel 1910; Kozai 1962; Lidov 1962):

\[
\tau_{ZKL} = \frac{2P_{\text{B}}}{3\pi} \frac{(b_{\text{C}}a_{\text{B}})}{a_{\text{B}}} \left( \frac{M_{\text{A}} + M_{\text{B}}}{M_{\text{C}}} \right)
\]

\[
\simeq 1.55\text{Myr} \left( \frac{a_{\text{B}}}{100\text{au}} \right)^{3/2} \left( \frac{b_{\text{C}}}{20a_{\text{B}}} \right) \left( \frac{M_{\text{A}} + M_{\text{B}}}{M_{\text{C}}} \right). \tag{7}
\]

From these estimates we note a crucial result from this paper that *all timescales are in the same order of magnitude* for K2-290. Secular commensurabilities can occur for reasonable values of the system and when they do not, we will show that ZKL cycles can modulate \(e_{\text{B}}\) so that \(\tilde{\Omega}_{bc,B} \propto 1/(1 - e_{\text{B}}^2)^{3/2}\) periodically\(^5\) crosses \(\tilde{\Omega}_{bc,s}\) and/or \(\tilde{\Omega}_{s,\text{bc}}\).

2.3. Spin Down

Even though the current value of the period for star A is known to be 6.63 days, presumably the star started with a shorter period \(P_{\text{a,0}}\) and then, due to magnetic braking it slowed down\(^6\) (e.g., Anderson & Lai 2018). To study the sensitivity of our results on the initial period of the star we assume the Skumanich law for the spin down (Skumanich 1972; Bouvier 2013):

\[
\Omega_*(t) = \frac{\Omega_{*,0}}{\sqrt{1 + \alpha_{\text{MB}} \Omega_0^2 t}}, \tag{8}
\]

where \(\Omega_{*,0}\) is the initial angular velocity of star A and the constant \(\alpha_{\text{MB}}\) was chosen so that the period at the current age of the star (about 4 Gyr) coincides with the current period of star A.

2.4. Planet b Mass

Hjorth et al. (2019) give a mass estimation of 7.6 \(M_{\oplus}\) using the mass–radius relation from Weiss & Marcy (2014). It is worth noting that in Hjorth et al. (2019) this mass could not be observationally constrained and was only found to be 5.8 \(\pm 5.1\) \(M_{\oplus}\). Therefore, we shall vary \(m_{\text{b}}\) in our population synthesis in a wide range of 1–15 \(M_{\oplus}\).

Using the relation from Chen & Kipping (2016) we get a mass of 9.8 \(M_{\oplus}\) which is close to the previously cited value and within the observational constraint. As it will later be shown in Figure 5(d), our results do not depend much on this parameter and so we adopt the mass from Hjorth et al. (2019) as our fiducial value.

3. Results

We show two examples of successful simulations (i.e., achieving obliquities of 124°) in Figure 2 for our fiducial parameters including the von Zeipel–Lidov–Kozai (ZLK) oscillations (von Zeipel 1910; Kozai 1962; Lidov 1962) to emphasize that this is what kicks the system out of the equatorial plane and decouples the inner planets from their star in most cases.

\(^{3}\) Strictly speaking, \(\tilde{\Omega}_{bc,B}\) can cross the other frequencies at points other than the ZKL eccentricity peaks, but these cause the most dramatic changes to the system.

\(^{5}\) Although, given its short period, this effect was probably not significant for star A.

![Figure 2.](image)

**Figure 2.** Evolution of the inclination of the stellar spin axis \((\iota_\star = \cos^{-1}(\hat{j} \cdot \hat{i}))\) and the stellar obliquity \((\iota_{bc,s} = \cos^{-1}(\hat{J}_\star \cdot \hat{j}_s))\) for two examples using the fiducial values given in Figure 1 and final \(J_2 = 10^{-4}\). Panel a shows the case with spin down of the host star from \(P_0 = 2\) days to its current value of 6.63 days, while panel (b) shows the same case without spin down. In panel (c), we show the ZKL cycles of the AB binary and observe that sudden and chaotic changes in the obliquities coincide with the instances where the eccentricity peaks are reached.

3.1. Secular Chaos: Conditions and Available Phase Space

When star C is sufficiently inclined relative to AB, the eccentricity of star B \((e_{\text{B}})\) reaches high values via ZKL oscillations which modulate the precession frequency of the inner planets as peaks in eccentricity translate into peaks in the nodal precession rate \((\tilde{\Omega}_{bc,B} \propto 1/(1 - e_{\text{B}}^2)^{3/2})\). This can be seen in Figure 3 which compares a case of low mutual inclination \((i_{bc})\) to a higher one reaching higher eccentricities. This modulation of the potential can kick the orbit of the planets out of the equatorial plane or decouple them from their star. We can calculate an analytical maximum value of this precession rate by knowing the maximum eccentricity of the cycles and using Equation (6). It is worth noting that the angular momentum of stars B and C is comparable, which is why the effect does not peak at 90° as it would for a test particle system.

Also \(e_{\text{C}}\) plays a role here but is assumed zero to compare with the analytical equation given in Naoz et al. (2013); we later consider the case of \(e_{\text{C}} = 0\) for the population synthesis:

\[
\gamma^2 \left[ \frac{3 + 4\gamma \cos i_{bc}}{2} \right] + \gamma^2 + \gamma \cos i_{bc} - 3 + 5 \cos^2 i_{bc} = 0
\]

where \(\gamma = L_{\text{B}}/L_{\text{C}}\). We can see in Figure 3(b) that for an inclination of 10°, \(\tilde{\Omega}_{bc,B}\) does not cross the other precession
the star B achieves eccentricities close to 0.99 and the system is destroyed as star B approaches too close to the planets ($a_d(1-e_B) \approx a_e$).

Second, the envelopes at large $J_2$ indicate the empty regions where the precession rate of the planets due to star A’s $J_2$ is greater than the one due to star B ($\Omega_{b,c,s} > \Omega_{b,c,B}$). Equating the precession rates from Equations (4) and (6) at the maximum eccentricity $e_{B,max}$, we get the following condition

$$
J_2 \frac{1.9 \times 10^{-5}}{1 - e_{B,\text{max}}^2 (i_{b,c})^2} = 1.
$$

We see this envelope explains very well the observed results from our simulations.

3.2. Population Synthesis

In Figure 5 we explore a parameter space neighboring the observed values in Figure 1 and a range of spin down and $J_2$ histories (the $J_2$ parameter in Figure 5(b) refers to the current value for star A, assuming a period of 6.63 days) with ~50,000 trials.

As in all previous simulations, the planetary system is initially aligned with the stellar equator ($i_{b,c} = 0$). However, the stellar orbits are drawn according to the following properties:

1. The inclinations are isotropically oriented $\cos i \sim U(-1, 1)$, with uniformly distributed longitude of periapsis and longitudes of the ascending nodes.
2. As we had no prior knowledge of the current $J_2$ or initial period of the central star; we assumed a log-uniform and uniform distribution, respectively.
3. The eccentricities of stars B and C were drawn according to the distributions in Tokovinin & Kiyanova (2015), considering that star C has an inner binary:

$$
f(e_B) = 1.2 e_B + 0.4, \quad \langle e_B \rangle = 0.6, \quad (11)
$$

$$
f(e_C) = 0.24 e_C + 0.88, \quad \langle e_C \rangle = 0.52. \quad (12)
$$

4. The semimajor axes $a_B$ and $a_C$ were drawn from a log-uniform distribution, rejecting those that do not satisfy the stability criterion by Mardling & Aarseth (2001):

$$
\frac{a_C (1-e_C) e_B}{a_B} > 2.8 \left(1 + \frac{M_C}{M_B + M_A}\right) \left(1 + \frac{e_C}{1-e_C}\right)^{1/2}. \quad (13)
$$

Finally, we also reject the systems whose orbit-averaged projected distance

$$
D_{\text{proj}} = \frac{a(1-e^2)^{5/2}}{2\pi} \int_0^{2\pi} df \left[1 - \sin^2 f \right]^{1/2} \left[1 + e \cos f\right]^3
$$

does not fall within the observed 1σ error bars of $D_{\text{proj,B}} = 113 \pm 2\text{ au}$ and $D_{\text{proj,C}} = 2467^{+177}_{-155}\text{ au}$ (Hjorth et al. 2019).

We present these results in Figure 5 as the fraction of total simulations achieving the observed obliquity within the estimated age of the system of $4.0^{+0.6}_{-0.5}$ Gyr and find that 56% of the systems could explain K2-290.

Looking into each panel, we see no dependence on initial period (panel (a)). On panel (b) we see the expected trend for $J_2$ as for lower values; the planets are less coupled to their star and are more easily knocked over. This trend was already hinted at...
by the white envelope in Figure 4(c), where for larger \( J_2 \) the inclinations need to be larger to cross the resonances (Equation (10)).

We also observe that the mutual inclination distribution has a dip at \( i_{BC} \sim 100^\circ \) (panel (c)) due to the large eccentricities that disrupt the planetary system, while it reaches two maxima just outside this dip that allow for large \( e_{\text{max}} \) exploring a wider range of nodal frequencies \( \Omega_{\text{bc,B}} \propto (1 - e_B^2)^{-3/2} \) to drive chaos.

In turn, panel (d) shows a slightly higher success rate for lower masses of the inner planet. As this planet represents very little of the angular momentum of the bc system, this is only due to the coupling between bc and the central star where both planets contribute on the same order. Finally, for panels (e) and (f), we see there is a preferred distance for the outer stars. This is more noticeable for star B.

4. Discussion

In this work, we have studied the inclination history of the multi-planet system orbiting K2-290A perturbed by two distant stars and the rotationally induced stellar quadrupole. We show that the stellar obliquity increases chaotically, often reaching retrograde configurations and reproducing the observed value of \( 124^\circ \pm 6^\circ \).
A striking property of K2-290 is that all nodal precession frequencies for the planets and the star’s spin axis are comparable (∼0.2–0.5 Myr⁻¹; Equations (4)–(6)). Thus, secular resonances are often crossed, triggering secular chaos, a process that is assisted by the ZKL oscillations of the AB binary driven by star C.

Other results include:

1. The parameter space where retrograde obliquities are attained grows by including the effect of the distant star C. Without C we cannot reproduce the observed obliquity for our estimated current value of J₂ (Panel (b) of Figure 4), unless \( e_B \) is initially very large. A population synthesis without star C shows a success rate of only 12% (compared to 56% with C) and the successful systems have \( e_B \approx 0.86 \) (Figure 5).

2. We show that a necessary condition for secular chaos is that \( \Omega_{BC} \) is sufficiently large to drive larger values of \( e_{B,\text{max}} \) (see Equation (10) and the envelope in panel c of Figure 4). As such, we expect that B and C are highly inclined relative to each other (see panel (c) in Figure 5).

3. We see some dependence on the final value of J₂ (panel (b), in Figure 5), but no dependence on initial period of the star (panel (a)). In other words, the mechanism is independent on the initial value of J₂. As for the current value, the somewhat evolved star with radius of 1.51R☉ would have had a radius closer to 1.25R☉ during its main sequence; a factor of ∼1.8 lower in the value of J₂.

In what follows, we discuss how our main findings depend on the presence of another planet and how they fit in the bigger picture of obliquity excitation.

4.1. Presence of Other Planets in K2-290

Even though only two planets (K2-290b and K2-290c) have been discovered around K2-290A, there is still the possibility that more planets could be discovered in the future.

Using RV data from HARPS-N, Hjorth et al. (2021) find a radial acceleration for star A of \( \dot{\gamma} = 9 \pm 5 \text{ ms}^{-1}\text{yr}^{-1} \). This acceleration, although compatible with zero within 2σ and with the presence of star B (which would cause an acceleration on the order of 5 ms⁻¹yr⁻¹) within 1σ, could also be caused by other planets orbiting K2-290A with a longer period.

The main effect of this undiscovered planets would be to increase the coupling between the planetary system and star B (increase \( \Omega_{bc,B} \)). Thus, in order to encounter the resonance \( \Omega_{bc,B} \sim \Omega_{bc,c} \), it would demand a larger value of J₂, possibly earlier in the evolution of the star.

4.2. Link to Retrograde Hot Jupiters

The chaotic spin–orbit behavior observed in this work is reminiscent of the work by Storch et al. (2014), Storch & Lai (2015) in the context of Jovians undergoing ZKL cycles and high-eccentricity migration to hot Jupiter orbits. In their work, the Jovian itself plays the role of both the star B undergoing eccentricity oscillations and the planetary system that torques the star.

A qualitative difference occurs when the planet(s) do not have enough angular momentum to torque the star \( |\dot{\Omega}_{bc,B}| \ll \Omega_{bc,B,J} \). If so, the set-up in Storch et al. (2014) with a migrating planet will not drive chaotic obliquity evolution, but just regular oscillations due to the ZKL cycles. Instead, in our model the periodic resonance crossings for the planetary orbits \( \Omega_{bc,s} \sim \Omega_{bc,B} \) may occur at all planetary masses (Equations (4) and (5)). In other words, our model may lead to either chaotic tumbling of the star as in Storch et al. (2014) and/or the planetary orbits, both leading to chaotic obliquity evolution. We have checked this by decreasing the masses of our planets by a factor of 10 or 100.

4.3. Primordial Disk Misalignment or Tertiary-driven Secular Chaos?

As discussed by Hjorth et al. (2021), K2-290 is the first system that provides strong support to the primordial disk misalignment theory (Batygin 2012; Lai 2014; Spalding & Batygin 2014). The companion star B lies at a desired distance of ∼100 au; not too close to suppress planet formation (Moe & Kratter 2021) and not too far to require unrealistically long disk lifetimes.

Unlike the primordial tilting where a resonance crossing is mediated by the dispersing disk, our proposal to cross the resonances relies on the wider-orbit companion star C. This is an important difference as the star C is currently observed and large obliquities are excited by a wide range of orbital distances (∼2000–4000 au, Figure 5(f)) that are consistent with the observations. The chaotic obliquity excitation is then a natural outcome of the observed system, relying just on few-body gravitational dynamics and with a success rate of ∼40%–70% depending on the assumed parameters, mainly the value of J₂. This is a difficult value to estimate as it depends on the internal structure of the star (Batygin & Adams 2013), but we still observe the effect for a wide range of values. As for the disk, involving gas dynamics and evaporation processes, the dynamics is far more uncertain.

Finally, we remark that the primordial tilting and our proposed model can work in tandem. The chaotic obliquity excitation described here starts taking place long after the disk disperses and it is fairly insensitive to the initial stellar obliquity.

4.4. Future Testable Predictions

Figure 5(c) shows this mechanism is more effective when the orbits of stars B and C are almost perpendicular to each other. Although this mutual inclination decreases when \( e_B \) grows, the system spends more time with its large-inclination state, as can be seen in Figure 2(c). Thus, a prediction of our results would be that \( \Omega_{bc} \) should be large, peaking at ∼80° or ∼110°.

As shown by Tokovinin (2017), the orbital planes are uncorrelated for tertiary stars at ∼10³ au (Figure 1 therein), corroborated for larger values of the outer separation (up to 10⁴ au) in Tokovinin (2021).

Given a Keplerian speed for star C (relative to A) of ∼0.7 km s⁻¹, the relative RVs can be measured with current spectrographs. Also, we estimate a proper motion of ∼0.6 mas yr⁻¹ for motion in the sky plane which is above Gaia’s uncertainties.

4.5. Applications to Other Planetary Systems

KOI-5 (Furlan et al. 2017) is a more compact triple star system with a confirmed inclined inner planet (and an unconfirmed outer one). We ran a few simulations to test if the effects previously mentioned could also explain this system and found that with a sufficiently large mutual inclination of the
external star, we can even get retrograde states for KOI-5’s planets.

It is worth noting that there is nothing special about the measured stellar obliquity of 124° in our simulations. In fact, given this mechanism, we could expect to measure stellar obliquity of 124° and any retrograde state.

More generally, the dynamics depend on the outer bodies only through the amplitude of their tidal fields $\propto M/a^3$. Therefore, we may replace the star B in our set-up for a Jovian-mass planet $\sim 10$ times closer to get the same behavior. Correspondingly, making sure star C is close enough to drive ZKL oscillations of such planet (i.e., unquenched by the inner planets).

5. Conclusions

In this work we show that the striking retrograde stellar obliquity of planets K2-290b and c (124° $\pm$ 6°) is a natural outcome of the long-term spin–orbit dynamics driven by the distant stars B and C. Here, the star C drives eccentricity and/or inclination oscillations in the AB orbit, triggering wide-spread chaos in the evolution of the planets’ inclinations and stellar obliquities.

Since our model works for a wide range of initial conditions, independent of the host star’s spin history, we suggest that the previously proposed explanation relying on the primordial tilt of the birth protoplanetary disk may not be required.

Finally, we remark that, for our estimate of $J_2$ for the central star, we can only achieve the observed obliquity if star C is present, and so, the effect of this perturber, even though it is very distant to the planetary system, should not be ignored.

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Appendix

Equations of Motion and Definitions

To describe the orbits of each body we use the vectors of eccentricity $e = e \hat{e}$ and specific angular momentum $j = (1 - e^2)^{1/2} \hat{j}$ with the convention of $\hat{e}$ pointing in the direction of the periapsis and $\hat{j}$ pointing in the direction of the angular momentum. Then, given the potential in terms of these vectors (from Tremaine & Yavetz 2014), we can get their secular evolution:

$$\dot{\phi} = -\frac{\phi_{bc,A}}{2} \left[ (\hat{e} \cdot \hat{j}_{bc})^2 - \frac{1}{3} \right] - \frac{\phi_{bc,B}}{2} \left[ (\hat{e}_{bc} \cdot \hat{j}_{bc})^2 - \frac{1}{3} \right],$$

where the amplitudes are given by:

$$\phi_{bc,A} = \frac{3J_2 GM_a a_B^2}{2} \left( \frac{M_b}{a_b^3} + \frac{M_c}{a_c^3} \right),$$

$$\phi_{bc,B} = \frac{3GM_a M_b}{4a_B^3},$$

$$\phi_{bc,C} = \frac{3GM_a M_B M_C a_B^2}{4(M_a + M_B + M_C)} a_C^3,$$

and $b = a(1 - e^2)^{1/2}$ is the semiminor axis.

We solve the motion using the Milankovitch set of equations (e.g., Tremaine & Yavetz 2014) as

$$\frac{ds}{dt} = \frac{1}{S} (\nabla \phi \times s)$$

$$\frac{dj_k}{dt} = \frac{1}{L_k} (\nabla j_k \phi \times j_k + \nabla e_k \phi \times e_k),$$

$$\frac{de_k}{dt} = \frac{1}{L_k} (\nabla e_k \phi \times j_k + \nabla j_k \phi \times e_k),$$

where the sub-index $k = \{bc, B, C\}$ and $L_{bc} = M_a \sqrt{GM_a a_b} + M_c \sqrt{GM_a a_c}$, $L_B = \frac{M_a M_b}{M_a + M_B} \sqrt{GM_a a_B}$ and $L_C = \frac{M_a (M_B + M_C)}{M_a + M_B + M_C} \sqrt{GM_a a_C}$ are the orbital angular momenta and $S = k_j M_a R_p^2 \Omega$, is the angular momentum spin of the central star.

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\[ \frac{\dot{\phi}_{bc,C}}{2} = \frac{5(e_B \cdot \hat{j}_C)^2 + (\hat{j}_B \cdot \hat{j}_C)^2 + 2e_B^2 - \frac{1}{3}}{2} \]  

\(7\) Except for the eccentricity of the planets. As the potential does not depend on this parameter (which starts at zero), the planetary orbits remain circular, as was required by the fact that both planets are coupled.
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