Model gradient coil employing active acoustic control for MRI

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Abstract  Results are presented for a model three-axis gradient coil incorporating active acoustic control which is applied to the switched read gradient during a single-shot rapid echo-planar imaging (EPI) sequence at a field strength of 3.0 T. The total imaging acquisition time was 10.6 ms. Substantial noise reduction is achieved both within the magnet bore and outside the magnet. Typical internal noise reduction over the specimen area is 40 dBA whereas outside the acoustic chamber the noise level is reduced by 60–67 dBA. However these results are relative to a control winding which is switched in phase, adding 6 dBA in its non-optimized mode, which is included in the quoted figures.

Keywords MRI · Acoustic control · Gradient coils · Reduced acoustic noise · EPI

Introduction

With the advent of more-powerful magnets and faster imaging regimes in magnetic resonance imaging (MRI) a major concern is the high levels of noise generated during scanning. This noise arises within the cylindrical structure of the gradient coil and is proportional to the driving current and the strength of the static magnetic field. This current generates Lorentz forces that induce vibrations in the coil structure, thereby generating substantial noise.

The general trend for increased static field strengths and faster imaging techniques have made the noise situation worse. The acoustic noise problem has now reached the point where it poses a significant health risk not only to the patient but also to medical staff working in close proximity to scanners. For example, in ultra-high-speed imaging such as echo-planar imaging (EPI) and echo-volumar imaging (EVI), because of the high maximum gradient amplitudes employed and extremely rapid slew rates used in these techniques, noise levels can approach 130 dBA [1–3], which is well above the safety levels permitted in the workplace. While adult patients can be protected to some extent against the dangers of acoustic noise, infants and foetuses in utero cannot be so easily protected. The same is true for animals in veterinary practice.

Various approaches have been explored to try to ameliorate the acoustic noise problem, including the development of special pulses for use in EPI [4, 5], and also gradient shielding techniques [6]. Presently the most common approach is to seal the gradient coil in a vacuum chamber [7].

As an alternative approach, active acoustic control for gradient coils was introduced by Mansfield and Haywood [8] in an attempt to ameliorate the acoustic noise problem by controlling the vibrational modes generated in the coil structure. In this novel approach the gradient coil structure comprises flat rectangular plates or flat arcuate sectors, in which the gradient field winding and an additional control winding are embedded in the flat plate structure in order to control the vibrational mode of the structure, thereby reducing the noise. The use of either rectangular or arcuate sectors simplifies somewhat the theory of noise propagation.

The purpose of the control winding is to prevent the production of compressional and bending vibration modes in the coil structure that result from the opposing forces applied to the coil former segments by the opposite currents in the gradient and return arcs of the coil. It achieves this by decoupling these two currents. Each coil segment consists of two plates separated by a small gap. Around this gap a second,
control winding is placed which carries a current $I_1^e e^{i\phi}$ for the
plates with a gradient field winding current $I_1$, and $I_2^e e^{i\phi}$ for
the plates with a gradient field winding current $I_2$. The two
halves of the former can then move independently, thereby
reducing considerably the compressive and bending forces.
These forces cannot be eliminated entirely as the former is
not infinitely rigid. To assist this process further the control
winding is activated so that the currents flowing on each side
of both sections are acting in unison. Simple theory indicates
that the current and phase in the control windings should be
equal to those in the gradient windings. Due to the finite velo-
city of sound in the formers greater acoustic attenuation is
achieved by modifying slightly the amplitude and phase of
the current in the control windings.

In the work presented here, as a first step in demonstrating
the principle of active acoustic control, a scaled-down model
two-axis gradient coil was constructed and used to obtain a
single-shot image using EPI. The coil consists of a number of
sectors, each comprising flat rectangular plates with embed-
ded straight wire windings for the transverse gradient, $G_y$,
used as the read gradient, together with embedded straight
wire secondary control windings for active acoustic control
of this switched gradient. The same method of flat rectangu-
lar plates with embedded straight wire gradient windings was
used for the $G_z$ gradient but without the control winding. The
longitudinal gradient, $G_z$, used a traditional Maxwell pair.

**Magnetic field gradient calculations**

The field gradient in the $z$-direction, $G_z$, has components [2]

$$G_x = \frac{\partial B_z}{\partial x},$$

$$G_y = \frac{\partial B_z}{\partial y},$$

$$G_z = \frac{\partial B_z}{\partial z}. \tag{1c}$$

In our coordinate system $G_x$ is the equivalent to the gener-
ation of $G_y$ but with rotation of the gradient assembly through
90° about the $z$-axis. In this work we concern ourselves enti-
lessly with the generation of $G_y$.

A magnetic field gradient, $G_y$, of the required strength and
extent can be produced by at least four parallel straight wires
placed at the corners of a rectangle with all wires carrying
equal currents flowing in the same direction. By increasing
the number of parallel wire pairs and by appropriately chan-
ging the spacing of the wires along the $z$-axis the region of
linearity of the field gradient produced can be enlarged.

Starting with the impractical infinite wire case for our
calculations, following Zupancic and Pirš [9], we express
the $z$-component of the magnetic field for six wires, each
carrying current $I$, as

$$B_z(y, z) = \frac{\mu_0 I}{4\pi} \sum_{n=0}^{\infty} \left( \frac{\xi}{r} \right)^n A_n,$$  \tag{2}

where

$$A_n = \exp[-i(n+1)\phi], \tag{3}$$

where the displacement $\xi$ in Eq. (2) is given by

$$\xi = y + iz, \tag{4}$$

and where $r$ and $\phi$ are the cylindrical coordinates of a wire,
and $y$ and $z$ are the coordinates of a point at which the field
is calculated.

If Eq. (2) is expanded one can readily see that all even
powers of $\xi$ vanish. When $z = 0$ the first term in Eq. (2),
when differentiated with respect to $y$, yields a linear gradient
$G_y$. For six wires, the region of linearity can be made larger
when both $A_3$ and $A_5$ are zero.

Let the current in the corner wires be $I_1$, and that in the
center wires be $I_2$. We find, after some calculation, that $I_2/I_1$
is 0.8:1 with an angle $\delta$ between the diagonals of the corner
plate pairs of 66.6°.

An infinite wire design is impractical. All wires that form
the windings have to fit inside the magnet, as do the control
wires.

Field of finite parallel wires

The optimum angle between the diagonal corner wires for
an infinite wire system has been calculated. We now use this
angle in magnetic field gradient calculations for a practical
coil design with finite wire lengths. The magnetic field $B(r)$
at a distance $r$ from a wire displaced $r_w$ from the origin and
which carries a current $I$ along a wire path $w$ is given by the
Biot–Savart expression

$$B(r) = \frac{\mu_0 I}{4\pi} \int \frac{(r - r_w) \times dr_w}{|r - r_w|^3}, \tag{5}$$

where $\mu_0$ is the free-space magnetic permeability and $dr_w$ is
a wire element.

The vector displacements required later are written in
Cartesian coordinates as

$$r = ix = jy = k z \tag{6}$$

and

$$r_w = i x_w + j y_w + k z_w. \tag{7}$$

For a finite wire parallel to the $x$-axis the elements $dy_w = 0$
and $dz_w = 0$. The $B_x$ component of Eq. (5) is

$$B_x(x, y, z) = 0. \tag{8}$$
Similarly the $B_y$ and $B_z$ components are

$$B_y(x, y, z) = \frac{\mu_0 I}{4\pi} (z - D_1) g$$ \hspace{1cm} (9)

and

$$B_z(x, y, z) = \frac{\mu_0 I}{4\pi} (y - A_1) g,$$ \hspace{1cm} (10)

where the current $I = 1,000$ A, the permeability of free space $\mu_0 = 4\pi \times 10^{-7}$ N/A$^2$, $D_1 = A_1 \tan \beta$ is the spacing along the $z$-axis between the wires in the plate pairs, and $A_1$ is the distance between the wires in the $y$-axis to the center (see Fig. 1).

The integral $g$ is given by

$$g = \int_{-B_1}^{B_1} \frac{dx_w}{[(x - x_w)^2 + (y - A_1)^2 + (z - D_1)^2]^{3/2}} ,$$ \hspace{1cm} (11)

and can be solved exactly [9], giving

$$g = \frac{(x + B_1)/\left[(x + B_1)^2 + (y - A_1)^2 + (z - D_1)^2\right]^{1/2}}{(y - A_1)^2 + (z - D_1)^2}$$

$$- \frac{(x - B_1)/\left[(x - B_1)^2 + (y - A_1)^2 + (z - D_1)^2\right]^{1/2}}{(y - A_1)^2 + (z - D_1)^2}.$$ \hspace{1cm} (12)

By combining Eqs. (9) and (10) with Eq. (12) and with appropriate values of $A_1$ and $D_1$, we obtain the magnetic field of six parallel finite length wires. The component $B_x$ is zero everywhere and the component $B_y$ is zero over the $xy$-plane, which can be chosen as the imaging plane.

Gradient field strength and linearity

The gradient strength and linearity were calculated for the $G_y$ gradient coil design, comprising six current-carrying loops together with six control winding loops. The coil thickness was given by $2D_1 = 2A_1 \tan \beta$. The length of the plates $2B_1$ was fixed at $\pm 0.30$ m. The width of the plate pairs, $s$, was fixed at 0.217 m, this value being the maximum allowable in the magnet. The optimum angle, $\beta$, for the wire positions was also fixed to give maximum linearity. Figure 1 shows a sketch of the $G_y$ gradient coil arrangement and a detailed sketch of an individual plate pair or sector making up the coil is shown in Fig. 2. A plot of the calculated magnetic field strength and gradient linearity is shown in Fig. 3.

Effect of the control windings

Calculations were carried out to determine whether the additional gradient field produced by the control windings would compromise the magnetic efficacy of the $G_y$ gradient. The calculations showed that the strength of the field produced by the control windings is determined by the size of the gap between them. By keeping the gap as small as possible, the field produced by the control winding is kept small compared to the $G_y$ gradient field. From calculations for our coil configuration, with a gap of 0.005 m between the control windings, it was found that the control windings added only 3.5% to the $G_y$ gradient field.

The control winding current and relative phase are equal to those supplied to the $G_y$ gradient when the coil is operating in the noise cancellation mode. From the results of the
calculations above, the small contribution from the control winding to the overall gradient field affects the linearity of the $G_y$ gradient field by a negligible amount and stays within 1.5% over the region of interest (ROI) (see Fig. 3).

Field of view and resolution

To match the acoustically controlled gradient coil system with the imaging parameters of the 3 T system a field of view (FOV) of 6.4 cm$^2$ with a resolution of 2 mm along both image axes was chosen.

Fabrication of the gradient coil plate pairs

The flat plates used for the actively acoustically controlled transverse read gradient, $G_y$, were constructed by cutting sheets of approximately 11.5-mm-thick Tufnol 10 G 40 glass fabric–epoxy resin laminated plastic to the required dimensions. The plate resonant frequency varied linearly with the plate thickness and served as a way to tune all the plates to a common resonant frequency. Figure 4 shows a frequency sweep and acoustic response of a plate pair of equal thickness. To broaden the resonant peak and give a larger operating area half the plates were machined down to a thickness of 11 mm and the other half were machined down to a thickness of 10.7 mm so that, when placed together to form a plate pair, they would have the desired frequency response. Grooves 2.5 mm wide and 6.0 mm deep were machined into each half of the plate pair along both edges so that the gradient winding could be inserted along the outer edge and the control winding on the inner edge of the front face of the plate pair. Two layers of round 2 mm diameter shellacked copper wire were placed on top of each other into each groove and then covered with approximately 2 mm of epoxy resin to embed the wires into the plates. The plate pairs were then assembled by placing two plates, one 11 mm and one 10.7 mm thick, together. To hold individual plate halves together as plate pairs, 30-mm-wide cross-bars were fitted at the back of the plate pairs with a 1.0 mm gap between the plates, running the length of the plates. The wire ends on the plates were then soldered together to form a single continuous two-turn outer winding to provide the main gradient field and a continuous two-turn inner winding to provide acoustic control. A diagram of the plate-pair arrangement is shown in Fig. 2. The response of each plate pair was measured acoustically in the magnet. The results of each plate pair showed a double-peaked response in which the amplitudes of each plate pair differed slightly. However there were areas in each plate pair response where the amplitudes overlapped and would be ideally suited for a common operating frequency. For all six plate pairs the overlap occurred at around 3.2 kHz, so an operating frequency of 3.205 kHz was chosen, as it corresponded to one of the MR system’s digital sampling frequencies.

Experimental procedure

With the three banks of gradient amplifiers available on the 3.0T system, demonstration of the imaging capabilities of the coil at the same time as application of acoustic control was not possible. The high gradient field strength required for such short imaging times meant that large currents were required for imaging. These could only be achieved by employing a bank of eight Techrons to power the gradients via a resonant circuit. This circuit consisted of a bank of high-power capacitors connected in series with the gradient coil windings. At our operating frequency of 3.205 Hz and with the measured inductance of 52 µH ideally we required a capacitance of 47.4 µF to tune the coil. With the capacitors available we were able to achieve a measured capacitance of 45.4 µF, which was sufficient to achieve the required current in the switched gradient coil.
With only three sets of power supplies and one bank of capacitors available it was almost impossible to carry out noise reduction experiments while imaging, without dispensing with slice selection thus freeing the third bank of Technrons to supply power to the acoustic control winding. As active acoustic control requires almost identical currents in both the control and gradient wires it was necessary to reduce the imaging field to approximately one third of its original size in order to compensate for the lower power capability in the control winding amplifier that consisted of only four Technrons with no second bank of capacitors to operate them in resonant mode. This would have meant most of the image detail would be lost. Consequently the experiment had to be split into two parts. The first part was to obtain an image from the coil utilizing all three gradient axes, but with no acoustic noise cancellation. The second part, after reconfiguring the gradient amplifiers, was the noise cancellation experiment.

The whole three-axis gradient coil assembly, including the cylindrical frame, the six-plate \( G_y \) gradient coil arrangement, the four-plate \( G_x \) coil, the Maxwell pair, the sample, and the radiofrequency (RF) coil consisting of a simple two-turn transmit and receive coil tuned to 127.7 MHz, were placed in the center of the magnet bore. Before imaging, the main magnetic field was shimmed to reduce any \( B_0 \) inhomogeneity effects due to susceptibility differences caused by the gradient system and the imaging sample. The magnet bore was lined with a layer of sculpted foam in order to achieve a degree of acoustic isolation. A similar lining covered the end caps at each end of the magnet enclosing the magnet bore volume. At one end of the acoustic chamber was a linear array of electret microphones (RS Components Ltd., Corby, UK, stock no. 283–4748, with an input port diameter of 8 mm and an approximately omnidirectional cardioid response over \( \pi \) radians), which was placed either within the acoustic chamber a distance 1.20 m from the gradient plate assembly and facing the front plane of the gradient coil or outside the chamber at a further distance of 10 cm. In the latter position the linear array of microphones was used to detect the acoustic output across the diameter of the magnet approximately 1.3 m from the surface of the gradient coil. The linear array was comprised of 11 microphones, equally spaced 5 cm apart. Each microphone output was fed separately to a circuit switching arrangement, allowing manual interrogation of each microphone signal via a Hewlett Packard network analyzer. The numerical results were obtained by manually stepping through the microphone outputs, recording both the signal amplitude and phase. This procedure was used when operating in a spot frequency mode. In other experiments only the central microphone was used and the acoustic frequency stepped through a predetermined range of frequencies. The geometry of the coil design was such that a high degree of acoustic cancellation occurs along the central axis of the magnet and the acoustic noise here is consequently automatically low, as shown in Fig. 9. In addition, the length of the coil compared to the imaging region is such that the variation in the acoustic output vertically is expected to be small in comparison with the transverse variation. Consequently, the microphones were positioned along this transverse axis. The acoustic signal amplitudes, measured using the microphone array and network analyzer correspond to A-weighted sound pressure level (SPL) measurements in dB\( \text{A} \). (For details of our calibration method see Ref. [10].)

**Results**

Slice selection was set to give a coronal slice through the phantom approximately 9 mm thick. From the modulus image obtained, the FOV spanned 32 pixels in the frequency-encode direction and 64 pixels in the phase-encode direction. This gave the image a true resolution of 32 mm \( \times \) 64 mm. The image was Fourier interpolated by zero filling to double the resolution along the frequency-encode axis. The structure within the phantom can be discerned down to a resolution of 2 mm in both directions. The image was easily corrected for the common EPI artefact of Nyquist ghosting by manually applying a first-order phase correction in the image formed from the odd echoes.

Following imaging the gradient amplifiers were reconfigured for the acoustic control experiments. The experiment was optimized by adjusting the phase and amplitude of the current in the control winding to give a noise reduction across the whole of the \( x \)-axis. Acoustic noise levels from the coil system were obtained using the central microphone of the array and these are plotted as a function of the current supplied to the gradient coil. Figure 5 shows the acoustic noise output in dB\( \text{A} \) versus log \( I \), where \( I \) is the current in amps for the whole coil together with specific results on the whole coil at particular currents, namely 20 and 40 A and on a single plate pair. A least-squares fit of all the data gives the straight line \( y = [21.92x + 47.018] \text{dB}_\text{A} \) with a slope of 21.92 dB\( _\text{A} /\log(I) \). This demonstrates the high degree of linearity of the acoustic response with current over three orders of magnitude. The graph shows that this relationship holds for individual plate components, individual plate pairs, and the coil system as a whole.

The current required for imaging with an image acquisition time of 10.6 ms was 253 A, or log \( I \) = 2.40. From Fig. 5 it is noted that this current corresponds to an acoustic noise output of 95.8 dB\( _\text{A} \) at the operating frequency of 3.205 kHz.

Figure 6 shows the complete three-axis gradient coil assembly with a central access of 10 cm. Figure 7 shows a detailed sketch of the full gradient assembly. Figure 8a is a diagram of the phantom, and Fig. 8b shows the image produced. The phantom comprised a water-filled circular chamber with a diameter of 5.6 cm, immersed within which
Fig. 5  Acoustic noise output in dBA versus log I, where I is the current in amps flowing at 3.205 kHz for a number of coil arrangements. Closed circles show the whole coil with the full current capability. The open circle shows the whole coil with an input of 20 A. The open square shows the whole coil response with a 40 A input. The closed squares show a plate pair and its response over a restricted current range.

is a block of material in which various shapes and holes are machined. The water chamber is 10 mm thick. It can be seen in Fig. 8b that there is very good agreement of the image with the small detail in the phantom. This is a one-shot image. All experiments were carried out within an acoustically lined chamber forming the inside bore of the 1 m-bore 3.0 T magnet.

Figure 9 shows graphs of acoustic noise output versus microphone position for the complete gradient coil system shown in Fig. 6 when placed within the lined magnet bore and immersed in a 3.0 T static magnetic field. This noise output is measured using a linear array of 11 microphones placed across the magnet diameter, 1.2 m from the gradient coil face. Figure 9a corresponds to an acoustic operating frequency of 3.3125 kHz with a current of 20 A, and Fig. 9b corresponds to an acoustic operating frequency of 3.3780 kHz with a current of 40 A. In both graphs, curves A and B correspond, respectively, to the anti-optimized high-noise output when the control current phase is φ = π and the optimized low-noise output when the control current phase is φ = 0; in both graphs the currents in the control winding and main winding were equal. The red line through curve A indicates the average acoustic noise signal. Curves C and D show the measured noise output when the microphone array was placed outside the acoustic chamber at a distance of 1.3 m from the gradient coil face and correspond, respectively, to the anti-optimized output when the control current phase φ = π and the optimized low-noise output.
Fig. 8  a Plan view of the phantom. b Snapshot image response for the phantom, which has a machined block with cutouts and is let into the flooded water compartment. The internal diameter is 52 mm. The circular dots have diameters of 3, 6, and 13 mm. The image acquisition time was 10.6 ms

output when the control current phase \( \phi = 0 \). The red line through curve D shows the average acoustic noise signals. In this case approximately 20 dBA of further acoustic noise reduction is achieved and is attributable to the acoustic foam used within the acoustic chamber. The overall noise reductions achieved are substantial, amounting to 67 dBA in Fig. 9a and 60 dBA in Fig. 9b relative to the control winding, which is switched in phase and in its non-optimized mode accounts for 6.0 dBA of the quoted noise reductions.

These results are of course for noise reduction outside the magnet and indicate the effect of noise on the environment, particularly for those people standing near the magnet when in operation. However, looking in more detail at Fig. 9a, b we see that curves B in both diagrams indicate a substantial reduction in acoustic noise within the lined bore of the magnet. Typically we see a noise reduction within the acoustic chamber corresponding to 40 dBA noise attenuation over a central shaft equal to the sample diameter of 5.2 cm. This is shown on both subfigures as the central region of curve B. Again this figure includes the 6 dBA quoted above.
Fig. 10 a The tailored EPI pulse as used with active acoustic control, consisting of a truncated three-lobe sinc function employing five frequencies within the narrow range over which the active acoustic reduction operates. This results in a pulse that consists of a modulated sinusoidally switched gradient at the central frequency, in this case 3.205 Hz. b One half of the central part of the symmetric tailored pulse. Allowing a two-echo redundancy before and after the necessary image data, the sampling region consists in total of 68 gradient half-cycles within the relatively flat region which is +3.1% of the median value.

Discussion

In our acoustic experiments we compared all signals with those obtained for the anti-optimum acoustic noise output level. This process seemed reasonable experimentally since it required a phase flip from the anti-optimum state to the optimum state. However this process has added an extra 6 dB_A to the results, which has arguably made our results appear better.

Active acoustic control has been developed specifically to work at, or close to, the acoustic plate resonance. At frequencies far from the plate resonance we have found that the ratio of currents can deviate significantly from unity and the phase of the control current relative to the main gradient current can deviate significantly from zero. However, with the selection of suitable operating frequencies we have previously demonstrated that significant acoustic control is still possible within most regions of the acoustic spectrum [10].

As active acoustic control operates over a narrow band of frequencies a tailored switched gradient pulse was employed consisting of a few frequencies within this band (Fig. 10). This produces good active acoustic noise reduction while simultaneously providing a practical sinusoidal switching gradient for high-speed EPI. Using tailored pulses of this kind has been shown to result in considerable noise reduction in individual plate pairs commensurate with that obtained in single-frequency experiments [5]. As we were not employing active acoustic control during the imaging process a simple sinusoidal switching gradient was employed in the blipped EPI sequence (Fig. 11).

The main purpose of the model coil design employed in this paper was to produce a small working coil with active acoustic control. It is impractical for use in the majority of scanners as the utilizable imaging volume is too small. While it would be possible to produce a magnetically screened version of our coil, such screening was not necessary in the present instance. Were a more practical concentric arcuate design to be implemented, including active acoustic control, then it would become essential to incorporate magnetic screening.

The greatest acoustic noise reduction occurs in the central region through the mechanism of destructive interference from each side of the coil structure, which theory tells us extends principally along the central magnet z-axis and gradient x-axis. However from our earlier work [10] it would appear that, by a suitable choice of plate material and by operating at a somewhat lower frequency commensurate with a larger object size, it will be possible to extend the gradient set, using arcuate sectors, to allow at least human head scanning and possibly whole-body imaging.

Conclusion

We have designed and built a model coil system incorporating acoustic control. This has been used to produce a snapshot image using EPI with an imaging time of 10.6 ms.
The gradient coil uses rectangular plate sectors that restrict the object size. The acoustic noise reduction measured over the specimen area is approximately 40 dB_A as presented, or approximately 34 dB_A if the acoustic control winding is not activated. Acoustic noise outside the magnet was reduced by 60–66 dB_A or 54–60 dB_A if the acoustic control winding is not activated.

In the future a more practical concentric arcuate design for head imaging or for whole-body access, incorporating acoustic control as well as active magnetic screening, could be built. Such a design would enable a useful comparison to be made with other whole-body gradient coil designs.

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