Detailed Examination of a Single Conduction Event in a Potassium Channel

Philip W. Fowler, Oliver Beckstein,† Enrique Abad,‡ and Mark S. P. Sansom* 

Department of Biochemistry, University of Oxford, South Parks Road, Oxford OX1 3QU, United Kingdom

Supporting Information

ABSTRACT: Although extensively studied, it has proved difficult to describe in detail how potassium ion channels conduct cations and water. We present a computational study that, by using stratified umbrella sampling, examines nearly an entire conduction event of the Kv1.2/2.1 paddle chimera and thereby identifies the expected stable configurations of ions and waters in the selectivity filter of the channel. We describe in detail the motions of the ions and waters during a conduction event, focusing on how waters and ions enter the filter, the rotation of water molecules inside the filter, and how potassium ions are coordinated as they move from a water to a protein environment. Finally, we analyze the small conformational changes undergone by the protein, showing that the stable configurations are most similar to the experimental crystal structure.

SECTION: Biophysical Chemistry and Biomolecules

ion channels are proteins that control the flow of ions across polarized cell membranes. The voltage-gated sodium (Nav) and potassium (Kv) channels are central to the generation of action potentials and hence are of tremendous physiological importance.1 Both families of channels have been extensively studied thanks to the exquisite sensitivity of single-channel electrophysiology and recent successes in elucidating atomic-resolution structures by X-ray diffraction. 

Long et al.2 elucidated the structure of the tetrameric Kv1.2/2.1 paddle chimera (Kvchim - Figure 1A), which is functionally similar to Shaker, the canonical voltage-gated potassium ion channel.3 The central pore domain, common to all potassium channels, is surrounded by four voltage-sensing domains. The pore-lining helices are kinked, opening the intracellular gate wide enough that it is thought to be open.2,4

The extracellular third of the pore forms a narrow constriction, the selectivity filter (Figure 1B), made from four loops each with the highly conserved sequence TVGYG, one from each monomer. The loops are arranged so that the backbone carbonyl oxygens point toward the pore axis, creating a series of octahedral cages (labeled $S_0$–$S_4$) that can coordinate a cation or a water molecule. The selectivity filter is sufficiently narrow that potassium ions must dehydrate to enter and can only move through in single-file.5 The prevailing view is that inside the filter there is always a single water ($w$) between each ion (K), leading to what we call the KwK mechanism.6 The energetics so are finely tuned that sodium ions are excluded, yet over half a billion of potassium ions can pass through per second. Immediately below the selectivity filter is the central cavity, which contains water molecules and cations,7 and in the Kvchim structure this is contiguous with the intracellular medium. How can we examine the conduction of potassium ions by Kvchim in atomic detail? This is difficult to do by experiment alone because the process of conduction is fast and occurs in a confined, highly optimized space that is very sensitive to perturbation8 and there is no experimental technique with the sufficient spatial and temporal resolution to resolve a single selectivity filter. Computer simulation can complement experiment provided one is careful to validate the results. Molecular
dynamics simulations have been used to study different aspects of the behavior of potassium ion channels, including how potassium ions and water move through the selectivity filter. One defines several collective variables so that the conduction process can be followed; these are usually the displacements of the ions and waters along the pore axis. Although a fast process, the energetic barriers are sufficiently high that biased simulations methods have typically been applied. These methods apply forces to the ions and waters to ensure that the required region of collective variable space is sampled. A multidimensional potential of mean force (PMF) contains a considerable amount of information; for example, stable configurations of the selectivity filter can be identified. Berneche and Roux used this approach to examine the conduction of potassium through the selectivity filter of the first, low-resolution structure of KcsA. Other potassium and related channels have been studied, including KirBac1.1, Kv1.2, the high-resolution structure of KcsA, NaK, and sodium channels. The sensitivity and reproducibility of conduction PMFs have been examined. More recently, computer power has increased to the point at which it has become possible to simulate multiple conduction events by “brute force” simulations if very high electric fields are applied. Although such unbiased simulations are intuitively appealing, it perhaps remains more efficient and informative to use biased approaches to investigate conduction. From the resulting PMFs one can, in theory, (i) make a direct connection to analytical and hierarchical theories and thereby calculate the conductance of the channel and (ii) examine a conduction event in more detail. We discuss the feasibility of the former in another paper.

We instead examine the net permeation of a single potassium ion through the Kv1.2/2.1 paddle chimeric channel. Not only do we study the energetics but we also study conduction from the perspective of the permeating species and determine how the conformation of the selectivity filter and its surrounding residues change during a conduction event.

We simulated only the pore domain of the Kvchim paddle chimera. This is reasonable because it has been shown that the pores of unrelated K channels can be spliced into a Kv channel, suggesting that Kv channels are modular in nature. We placed potassium ions and waters at alternate sites within the selectivity filter, and a third potassium ion (ion3) was placed in the central cavity below the selectivity filter. The resulting structure was embedded in a lipid bilayer and equilibrated using classical molecular dynamics.

The positions of the permeant species, and hence the configuration of the selectivity filter, was followed using the same collective variables as previous studies. Harmonic potentials were then separately applied to the center of mass of the two ions in the filter (ion12, z12) and the incoming ion (ion3, z3). By running 125 × 0.5 ns simulations, each with the harmonic potentials centered on a different value of (z12, z3), we were able to sample nearly an entire conduction event using stratified umbrella sampling. Three independent sets of umbrella simulations were run, making a total of 375 simulations.
Because we have implicitly assumed that there is always a water between any two potassium ions in the selectivity filter, we checked whether this was true for all umbrella simulations. The water between the two potassiums in the selectivity filter occasionally managed to squeeze past one of the ions. This occurred in 8% of frames (Figure S1 and Table S1 in the Supporting Information). All of these frames were removed, thereby ensuring our simulations followed the KwK mechanism. This process reduced the overlap in certain regions of \((z_{12}, z_{23})\) coordinate space, preventing us from calculating the three separate PMFs. Instead we combined all data to ensure adequate sampling of \((z_{12}, z_{23})\) space and calculated a single 2D PMF. We explicitly determined when the 2D PMFs were converged and, after discarding that portion of the data, estimated the correlation time and thereby calculated the errors (Figures S2–S4 in the Supporting Information).

The final result is a complex landscape with several minima (Figure 2) corresponding to the expected stable configurations of the selectivity filter: \(wwKwK(K)\), \(wKwKw(K)\), and \(KwKwK\). The landscape suggests that the KwKwK configuration is more stable than the \(wwKwK(K)\) configuration by \(4.0 \pm 0.5 \text{ kcal/mol}\) (Table S2 in the Supporting Information). Using shorter umbrella simulations, we have previously identified the same stable configurations and estimated that the KwKwK configuration is more stable than the \(wwKwK(K)\) configuration by \(5–8 \text{ kcal/mol}\).

To validate the above 2D PMF, we calculated the free energy required to move a potassium ion from the cavity into the S0 site, \(\Delta G_{\text{cavity-S0}}\), and vice versa, using thermodynamic integration (Figure S5 in the Supporting Information). resulting in \(\Delta G_{\text{cavity-S0}} = 8.6 \pm 0.2 \text{ kcal/mol}\) and \(\Delta G_{\text{S0-cavity}} = -8.1 \pm 0.2 \text{ kcal/mol}\). The forward and reverse calculations therefore agree with one another to within the estimated error and confirm that the three-ion configuration (KwKwK) is indeed more favorable than the \(wwKwK(K)\) configuration. The difference between the above values and our previous estimate \(\Delta G_{\text{S0-cavity}} = -8.1 \pm 0.2 \text{ kcal/mol}\) may be due to the two free energies not being directly comparable, or it may indicate that one or both calculations are, despite the results of our analyses, not yet converged. We conclude that the three-ion configuration (KwKwK) is more favorable than the \(wwKwK(K)\) configuration by \(4–8 \text{ kcal/mol}\).

The minimum free-energy path (MFEP) represents the most probable conduction mechanism (Figure 2). It has three major minima (points 1, 5, and 8) corresponding to the \(wwKwK(K)\), \(wKwKw(K)\), and \(KwKwK\) configurations of the selectivity filter, two barriers (points 3 and 6), and three possible intermediates (points 2, 4, and 7) (Table S2 in the Supporting Information). The depth of two of the possible intermediates is less than the estimated error so should be ignored. Only the configuration (point 4) can be considered to be metastable. Here both ion1 and ion2 appear to be in the process of moving between sites and are held in the plane of carbonyl oxygens. The heights of the barriers are in the range 3.5–7.9 kcal/mol (Table S3 in the Supporting Information) and seem rather too high to match the experimental order of magnitude of conductance properties for this channel in the framework of standard electrodifusion theory. These barrier heights are consistent with a previous study where we methodically examined the reproducibility and sensitivity to changes in the force field of such 2D PMFs.

In the remainder of this letter we shall examine in detail a single conduction event. Let us start with a solvated potassium ion (ion3) in the central cavity and two potassium ions (ion1 and ion2) bound at S2 and S4, with water molecules at S1 and S3. As ion3 approaches and enters the selectivity filter the average water persistence time (i.e., how long a water molecule stays within its solvation shell) increases (Figure 3A, B). Log–linear histograms of the water persistence times as a function of \(z_3\) (Figure 3C) show that when ion3 is in the central cavity \((-12 < z_3 \leq -13 \text{ Å})\) the solvating waters rapidly exchange with other waters in the central cavity and hence the persistence time is \(<140 \text{ ps}\). But as ion3 comes closer to the hydroxyl side chains of Thr370 that define the entrance to the filter, some waters persist for longer and longer until, when in the region \(-6 < z_3 \leq -7 \text{ Å}\), several waters persist for the entire equilibrated region of the trajectory (400 ps).

The nonlinear increase in the water persistence time along the pore axis strongly suggests that the entry of permeating species into the selectivity filter is a complex process and there is no clear boundary, one side of which a water is ‘outside’ the filter and the other is ‘inside’ the filter. Instead there are wide regions at the base of the filter (and probably also at the top) where the water is transitioning from being ‘outside’ to being ‘inside’. It is therefore incorrect to consider the selectivity filter as a hollow cylinder and the ions and waters as hard spheres.

Likewise, our observation that waters can occasionally squeeze past ions in the selectivity filter suggests that even when definitely inside the filter the persistence time for waters is long but not infinite.

As ion3 approaches the hydroxyl side chains of Thr370, all of the species in the filter move up one site in a concerted manner (‘knock-on’), and a water then enters site S4 (points 3–4, Figure 4A). A second ‘knock-on’ event (points 6–7) then
occurs and ion3 enters the filter, leading to the KwKwK configuration. The optimum coordination number of a potassium ion is 6–9.\textsuperscript{27} During conduction the coordination numbers of ion1 and ion2 are 8–9, except during both knock-on events when they are reduced. The coordination number of ion1 remains low (∼7) after the second knock-on event as it is in S0, which has only four carbonyl oxygens coordinating the cation with the remainder of the coordinating oxygens coming from water molecules. The incoming ion, ion3, is initially solvated by waters in the central cavity, but as it approaches Thr370 there is a gradual substitution of water oxygens by protein oxygens until ion3 is fully stabilized in site S4 and the filter achieves the KwKwK configuration (point 8). The coordination number of ion3 remains stable at 6–7 until ion3 enters the selectivity filter, whereupon it increases to 7–9, consistent with that experienced by ion2 at the start of the MFEP.

![Figure 4](https://example.com/figure4.png) Figure 4. Detailed look at a conduction event. (A) Average displacement of the conducting species along the minimum free energy path (MFEP). The nine points labeled correspond to those in Figure 2. The position of water23 is not well-defined until it enters the filter, which is assumed to occur after point 2. (B) Examining the ion coordination numbers ion shows that ions 1 and 2 are coordinated by oxygens from both the protein and water, with the former dominating, leading to coordination numbers in the region 6–9. Lower values occur outside of stable configurations. Ion3 is initially entirely coordinated by water, but there is a gradual increase in the amount of coordination provided by the protein as it approaches S4 from the central cavity. (C) Average angles of the intervening waters along the MFEP. Also shown are the distances between the waters and ions within the selectivity filter. (D) Examining the RMSD of the filter along the MFEP shows how the selectivity filter is most similar to the crystal structure when ions and waters are stably bound (points 1, 5, and 8). The RMSD is calculated relative to the crystal structure of Kvchim2 and compares the backbone heavy atoms (C\(_\alpha\), C, N, O) as well as the C\(_\beta\) atoms of the entire selectivity filter (the sequence TVGYG).

A water molecule trapped between two potassium ions can coordinate only one ion at a time. This is seen in the average angles made by the two waters in the filter (Figure 4C). With ion3 in the central cavity, water12 is oriented (∼20°) to solvate ion1, which is above it in site S2. This is energetically favorable because ion2, which is below the water in site S4, can be solvated by waters from the central cavity, whereas ion1 cannot. As a result the average distance between ion1 and water12 is less than the distance between ion2 and water12. During the first ‘knock-on’, ions1 and 2 and water12 get squeezed together and water12 adopts an average angle of ∼90°, presumably indicating that it coordinates both ions equally. Water23 now enters the selectivity filter and rotates (∼150°) during the second knock-on to coordinate ion3 as it subsequently enters the filter. Water12 then starts to rotate back to ∼20° (points 5–6), so it is once again coordinating ion1 (in S0), again resulting in the distance between ion2 and water12 increasing. During this movement the distance
between water23 and ion3 starts to increase until (point 7) water23 suddenly moves to coordinate ion2 rather than ion3 by simultaneously rotating (~20°) and moving up in the filter. The stable KwKwK configuration is thereby attained with both ‘trapped’ waters coordinating the ions above them in the selectivity filter. Because each water is an electrical dipole the external electric field could affect these rotations in subtle ways.

The selectivity filter subtly changes conformation during the conduction event, as shown by the root-mean-square deviation (RMSD) of the selectivity filter (Figure 4D and Figure S6 in the Supporting Information). The RMSD is smallest when the filter is in one of the stable configurations, suggesting that, as we might expect, the crystal structure is a spatial average of proteins with stable configurations of their selectivity filters. To probe how the selectivity filter changes conformation, we measured the distances between the opposing oxygens that line the filter and the backbone dihedral angles (Figure S7 in the Supporting Information). The opposing oxygen distances show how the filter has to first open slightly at Thr370 and then close to ‘swallow’ first water23 (points 3–5) and then ion3 (points 6–8). There is no clear correlation between any single dihedral angle and the individual opposing oxygen distances, suggesting that the ‘swallowing’ effect observed is driven by multiple small changes in dihedral angles along the backbone of the selectivity filter.

All K channels have a network of hydrogen bonds around the selectivity filter (Figure S8 in the Supporting Information). For example in Kvchim, Ser367 can form a hydrogen bond with the backbone carbonyl of Tyr363 and the hydroxyl group of Tyr373. It has been shown that mutating either tryptophan or the residue equivalent to Ser367 (a threonine) in the Shaker channel prevents expression, consistent with the hypothesis that these interactions help stabilize the selectivity filter. The propensity of all hydrogen bonds investigated remained approximately constant during the conduction event, and there was no correlation between the fluctuations and the movement of the conducting species, further suggesting that these hydrogen bonds simply stabilize the selectivity filter.

In conclusion, we have calculated a 2D PMF characterizing nearly an entire conduction event through the selectivity filter of the Kv1.2/2.1 chimeric voltage-gated channel, assuming the KwK mechanism is correct. This identifies the expected stable configurations of the selectivity filter (wwKwK(K), wKwKw(K), and KwKwK; Figure 2). We have described in detail the motions of the ions and waters during two ‘knock-on’ events, have shown how the filter is able to smooth the transition of a potassium ion from water into the narrow constriction of the selectivity filter, and have investigated the small conformational changes that occur during a conduction event. This is the first study to combine in this fashion the calculation of PMFs with detailed structural analysis.

**REFERENCES**

1. Hille, B. *Ion Channels of Excitable Membranes*, 3rd ed.; Sinauer Associates, Inc: Sunderland, MA, 2001.
2. Long, S. B.; Tao, X.; Campbell, E. B.; MacKinnon, R. Atomic Structure of a Voltage-Dependent K+ Channel in a Lipid Membrane-Like Environment. *Nature 2007*, 450, 376–382.
3. Tao, X.; MacKinnon, R. Functional Analysis of Kv1.2 and Paddle Chimera Kv Channels in Planar Lipid Bilayers. *J. Mol. Biol.* *2008*, 382, 24–33.
4. Fowler, P. W.; Sansom, M. S. P. The Pore of Voltage-Gated Potassium Channels Is Strained When Closed. *Nat. Commun.* *2013*, 4, 1872.
5. Hodgkin, A. L.; Keynes, R. D. The Potassium Permeability of a Giant Nerve Fibre. *J. Physiol.* *1955*, 128, 61–88.
6. Zhou, Y.; MacKinnon, R. The Occupancy of Ions in the K+ Selectivity Filter: Charge Balance and Coupling of Ion Binding to a Protein Conformational Change Underlie High Conduction Rates. *J. Mol. Biol.* *2003*, 333, 965–975.
7. Zhou, Y.; Morais-Cabral, J. H.; Kaufman, A.; MacKinnon, R. Chemistry of Ion Coordination and Hydration Revealed by a K+ Channel-Fab Complex At 2.0 Å Resolution. *Nature 2001*, 414, 43–48.
8. Yifrach, O.; MacKinnon, R. Energetics of Pore Opening in a Voltage-Gated K+ Channel. *Cell 2002*, 111, 231–9.
9. Maffe, C.; Bhattacharya, S.; Yoo, J.; Wells, D.; Aksimentiev, A. Modeling and Simulation of Ion Channels. *Chem. Rev.* *2012*, 112, 6250–6284.
10. Tai, K.; Fowler, P. W.; Mokrab, Y.; Stansfeld, P.; Sansom, M. S. P. In *Methods in Cell Nano Biology*, 1st ed.; Jena, B. P., Ed.; Elsevier B.V.: Boston, 2008; Vol. 90, Chapter 12, pp 233–265.
11. Bernèche, S.; Roux, B. Energetics of Ion Conduction Through the K+ Channel. *Nature 2004*, 414, 73–7.
12. Doyle, D.; Cabral, J.; Pfuetzner, R.; Kuo, A.; Gulbis, J. M.; Cohen, S. L.; Chait, B. T.; MacKinnon, R. The Structure of the Potassium Channel: Molecular Basis of K+ Conduction and Selectivity. *Science 1998*, 280, 69–77.
13. Domene, C.; Klein, M. L.; Branduardi, D.; Gervasio, F. L.; Parrinello, M. Conformational Changes and Gating at the Selectivity Filter of Potassium Channels. *J. Am. Chem. Soc.* *2008*, 130, 9474–9480.
14. Furini, S.; Domene, C. A atypical Mechanism of Conduction in Potassium Channels. *Proc. Natl. Acad. Sci. U. S. A.* *2009*, 106, 16074–16077.
15. Treptow, W.; Tarek, M. K+ Conduction in the Selectivity Filter of Potassium Channels Is Monitored by the Charge Distribution Along Their Sequence. *Biophys. J.* *2006*, 91, L81–L83.
(16) Bastug, T.; Kuyucak, S. Comparative Study of the Energetics of Ion Permeation in Kv1.2 and KcsA Potassium Channels. Biophys. J. 2011, 100, 629–636.

(17) Egwolf, B.; Roux, B. Ion Selectivity of the KcsA Channel: A Perspective from Multi-Ion Free Energy Landscapes. J. Mol. Biol. 2010, 401, 831–842.

(18) Furini, S.; Domene, C. Gating at the Selectivity Filter of Ion Channels that Conduct Na⁺ and K⁺ Ions. Biophys. J. 2011, 101, 1623–1631.

(19) Corry, B. Na⁺/Ca²⁺ Selectivity in the Bacterial Voltage-Gated Sodium Channel NavAb. PeerJ 2013, 1, e16.

(20) Furini, S.; Domene, C. On Conduction in a Bacterial Sodium Channel. PLoS Comput. Biol. 2012, 8, e1002476.

(21) Fowler, P. W.; Abad, E.; Beckstein, O.; Sansom, M. S. P. Energetics of Multi-Ion Conduction Pathways in Potassium Ion Channels. J. Chem. Theor. Comput. 2013, submitted.

(22) Khalili-Araghi, F.; Tajkhorshid, E.; Schulten, K. Dynamics of K⁺ Ion Conduction Through Kv1.2. Biophys. J. 2006, 91, L72–4.

(23) Jensen, M. O.; Borhani, D. W.; Linderf-Larsen, K.; Maragakis, P.; Jogini, V.; Eastwood, M. P.; Dror, R. O.; Shaw, D. E. Principles of Conduction and Hydrophobic Gating in K⁺ Channels. Proc. Natl. Acad. Sci. U. S. A. 2010, 107, 5833–5838.

(24) Jensen, M. O.; Jogini, V.; Borhani, D. W.; Leffler, A. E.; Dror, R. O.; Shaw, D. E. Mechanism of Voltage Gating in Potassium Channels. Science 2012, 336, 229–233.

(25) Jensen, M. O.; Jogini, V.; Eastwood, M. P.; Shaw, D. E. Atomic-Level Simulation of Current-Voltage Relationships in Single-File Ion Channels. J. Gen. Physiol. 2013, 141, 619–632.

(26) Lu, Z.; Klem, A. M.; Ramu, Y. Ion Conduction Pore Is Conserved Among Potassium Channels. Nature 2001, 413, 809–813.

(27) Bostick, D. L.; Brooks, C. L. Selectivity in K⁺ Channels Is Due to Topological Control of the Permeant Ion’s Coordinated State. Proc. Natl. Acad. Sci. U. S. A. 2007, 104, 9260–5.

(28) Fowler, P. W.; Tai, K.; Sansom, M. S. P. The Selectivity of K⁺ Ion Channels: Testing the Hypotheses. Biophys. J. 2008, 95, S062–72.