Absolutes L-shell ionization and X-ray production cross sections of Lead and Thorium by 16-45 keV electron impact

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The absolute L subshell specific electron impact ionization cross sections near the ionization threshold (16 < E < 45 keV) of Lead and Thorium are obtained from the measured L X-ray production cross sections. Monte Carlo simulation is done to account for the effect of the backscattered electrons, and the final experimental results are compared with calculations performed using distorted wave Born approximation and the modified relativistic binary encounter Bethe model. The sensitivity of the results on the atomic parameters is explored. Observed agreements and discrepancies between the experimental results and theoretical estimates, and their dependence on the specific atomic parameters are reported.

I. INTRODUCTION

Importance of electron impact excitation and ionization data in various materials analysis techniques such as electron probe microanalysis (EPMA), Auger electron spectroscopy (AES), etc. need not be overemphasized. Precise and accurate knowledge of the corresponding cross sections is used as input either in the form of look-up tables or functional dependence on electron impact energies of the electron probe used for such analysis. The inner shell ionization probabilities, extracted from the above-mentioned data, are also pivotal to many other material analysis techniques, apart from their importance in understanding the physical process of ionization in multi-electron bound systems [1].

Inner shells of atoms can be excited by knocking off the bound electrons to the continuum or unfilled quasi-bound orbitals. Vacancies thus created are filled by the electrons from the outer shells, resulting in the emission of photons. In addition, migration of vacancies through Coster-Kronig (CK) transitions among different subshells (L-shell and above) as well as to other inner shells, leads to photon emission with different energies and yields, which are complicated by the fact that the corresponding transition probabilities need to be accurately known. From the observation and quantitative estimation of the related photon yield with high precision, the inner shell ionization cross sections can be obtained, in principle, utilizing the known or pre-determined parameters, such as the fluorescence yield, CK transition probabilities and the sublevel-specific radiative decay probabilities from experiments or theoretical estimates. These important parameters are collectively known as the atomic relaxation parameters.

The above-mentioned relaxation parameters are obtained from experiments or from theoretical estimates [2] and are available from various data bases. However, some of these parameters are quoted with large uncertainties due to various processes involved. For example, the fluorescence yield for a specific subshell depends on the primary vacancy distributions, which in turn depends on the mode of vacancy creation in the subshell. It is also expected that migration of vacancies through CK transition would alter the primary vacancy distributions and hence the fluorescence yield.

Photon emission by electron impact is also possible as a multistep process through Auger transition, followed by creation of vacancy in the inner shells by virtual photons [3]. The above process involving virtual photons can only be accounted for by invoking quantum electrodynamics and the associated electromagnetic interaction between the bound electrons, which involve both Coulomb interaction and the magnetic interaction due to the moving electrons. In case of lighter elements, the motion of inner shell electrons are in the non-relativistic regime (v/c → 0), and therefore, the quantum effects due to magnetic interaction becomes negligible. Thus, inclusion of the Coulomb interaction alone in estimating the electron impact ionization cross sections results in reasonable agreement with the experimental results for the lighter atoms. For heavier atoms like the ones considered in this experiment, the magnetic interaction can no longer be ignored, and related estimates of the electron impact ionization cross sections should take magnetic interaction into account as well. Theoretical estimates based on above has been done in recent times for Gold (Au) [4].

Experiments on electron impact ionization which were done earlier, were focused primarily on K-shell ionization cross section, while L and M shell ionization data were seldom reported [3]. One of the major problems faced in the interpretation of experimental results based on established theories is that the extracted subshell specific
The enhancement factor (k) for the modified relativistic binary encounter (MRBEB) model-based estimates. To the best of our knowledge, the subshell specific ionization cross section for all the L-subshells of Thorium are reported here for the first time at the energy values near the corresponding ionization threshold.

II. EXPERIMENTAL DETAILS

The Experimental set-up consists of an in-vacuum energy dispersive spectrometer with a focusable electron gun (up to 50 keV), electrically cooled silicon PIN diode based X-ray detector, thin film target holder, and Faraday cup. The X-ray detector was placed in the meridian plane at 55° with respect to the beam axis. The pressure maintained inside the vacuum chamber was 5 × 10⁻⁷ mbar. Details of the experimental arrangement are described elsewhere in detail [12].

The targets used in the experiment were made by using two different techniques. Self-supporting Lead targets were made by electron beam vapor deposition. The thickness of the thin film of Lead, deposited on a glass substrate was monitored during deposition using a quartz thickness monitor. Thorium targets were made by electro-deposition on 200 μg/cm² thick Aluminum foil (99.99 % purity). Electro-deposition of Thorium oxide (ThO₂) on the foil cathode from a Thorium nitrate solution in 2-propanol, was monitored by measuring the electrode current and the duration of deposition. Foil thicknesses were measured by an alpha energy loss spectrometer [12] and the measured thicknesses are 78.1 ± 3.8 μg/cm² (Th) and 82.0 ± 4.2 μg/cm² (Pb).

X-rays generated due to electron impact were detected by X-ray detector (model XR-100CR from Amptek, USA), having energy resolution of 165 eV (FWHM) for 5.9 keV photons. Mylar foil of 100 μm thickness was placed in front of the 25.4 μm Beryllium window to reduce flux of M X-rays. The efficiency of the detector was measured by (i) K-shell ionization of Copper by electron impact and (ii) using characteristic X-ray lines from a calibrated 241Am source. The efficiency curve was fitted with equation \( \epsilon(E) = 1.58 \times 10^{-5} + 1.31 \times 10^{-6} E - 8.63 \times 10^{-8} E^2 \). The signal from the detector was fed to a multi-channel analyzer (MCA) through a shaping amplifier. For each data acquisition run, the count rates were kept low (< 300 counts/sec), so that there was no pile-up in the detector and therefore, no dead time correction was required for the MCA.

In the case of targets backed by the thick substrate, the electrons can be back-scattered from the substrate material and re-enter the target. These backscattered electrons can significantly change the original X-ray yield. It is necessary to correct for this enhancement of X-ray yield for the thick film backed targets like the Thorium targets used in this work. Also for obtaining the accurate ionization cross sections, one has to ensure that the target thickness is such that the projectile electrons do not ionize the target atoms more than once, thereby satisfying

In the present work, the \( L_\alpha, L_\beta, L_\gamma \) production cross sections in Lead and Thorium are measured, and the results are converted to the subshell specific ionization cross sections. Because of the finite thickness of the target materials, single collision condition within the target has to be ensured. In arriving at the ionization cross sections from the production cross sections, corrections due to multiple collisions per beam traverse was done using a Monte Carlo simulation procedure. Parameter dependence in extracting the ionization cross sections are also explored to check the sensitivity to parameter variations. The cross sections obtained from experiment are compared with a) theoretical results based on the distorted wave Born approximation (DWBA) including relativistic effects and exchange interactions into account [8], as obtained from the PENELOPE [9] code, and b) the modified relativistic binary encounter Bethe (MRBEB) [10, 11] model-based estimates. To the best of our knowledge, the subshell specific ionization cross section for all the L-subshells of Thorium are reported here for the first time at the energy values near the corresponding ionization threshold.

FIG. 1. Enhancement factor due to the presence of Aluminum backing in Thorium target, as obtained from PENELOPE simulation.
Counts (x10^4)

 CALCULATIONS [8].

The interaction of electrons and photons with matter. Specifically, the effect of electron impact inner shell ionization is taken into account from the numerical differential cross sections (DCS) [13] obtained from DWBA based calculations [8].

While generating simulated X-ray spectra by PENELOPE, the process becomes inefficient and time consuming due to 1) low inner shell ionization and subsequent radiative decay probabilities, and 2) use of thin film media in the experiment. This results in large variance and reduces the predictive power of simulation. To reduce the time spent on computation and to increase the efficiency, it is necessary to use a variance reduction technique, known as interaction forcing. PENELOPE implements the process by artificially reducing the mean free path relevant to the process, but keeping the probability distribution functions for energy loss and angular deflections the same as for the real process. Finally, the biasing introduced by the simulation process is corrected for by applying appropriate statistical weights [2].

Simulation was carried out with a pencil-like electron beam of 2 mm diameter impinging on a thin target at normal incidence. Entry of the projectile electrons into the target, resulting ionization events and emission of X-rays were recorded event by event. From the simulation of a large sample of events, the maximum probability of inner shell ionization per projectile electron was ~0.53 for both the target films used in the experiment. This number, being less than unity, ensures that single collision condition was satisfied in the experiment.

To account for the effect of electron back-scattering in the Thorium target, simulation was done with and without aluminum backing. It was found that up to ~4% of the electrons which ionized the Thorium atoms and subsequently generated L X-rays were back-scattered.
from aluminum. The back-scatter fraction, however, was found to depend on electron energy \((E)\). After obtaining X-ray yield with good statistics from simulation, the corresponding enhancement factor \(k(E)\) was obtained as:

\[
k(E) = \frac{\text{Counts under } L_x \text{ peak for Al backed target}}{\text{Counts under } L_x \text{ peak for unbacked target}},
\]

where \(x\) is \(\alpha, \beta\) or \(\gamma\).

The \(k(E)\)-values, obtained from simulation, are plotted in the Fig. 4 for the \(L\) X-rays. The values of \(k(E)\) lies in the range: 1.005 to 1.095.

### III. DATA ANALYSIS

The X-ray spectra of Lead and Thorium, resulting from electron bombardment at 35 keV, are shown in the Figs. 2 and 3 respectively. Individual \(L_x\) peaks in the observed spectra were fitted with Gaussian profile over the bremsstrahlung background, as shown in the figures, to obtain the corresponding X-ray yield \((N_X)\). The bremsstrahlung background over the region of interest was considered as linear due to small interval of energy spanned by each peak. \(L_\alpha\) and \(L_\beta\) peaks were fitted with single Gaussian functions for both Lead and Thorium. \(L_\beta\) peaks in Thorium could be resolved in \(L_{\gamma 1}\) and \(L_{\beta 2}\), and were fitted with two Gaussian profiles. The \(L_\beta\) peaks could not be resolved for Lead and therefore, a single Gaussian with higher FWHM value was fitted. \(L_\gamma\) peaks in both the targets were resolved into three constituent lines viz., \(L_{\gamma 1}, L_{\gamma 1},\) and \(L_{\gamma 236}\). Fitted \(L_\gamma\) spectra are shown in the insets of Figs. 2(a) and 3(a). The net counts obtained by fitting the spectra were corrected for self-absorption due to finite target thicknesses, assuming the oblique path of the X-rays through the target materials.

The X-ray production cross sections were obtained from the measurements using the formula:

\[
\sigma_i(E) = \frac{N_X A}{e(E') t N_e N_A k(E)},
\]

where, \(\sigma_i(E)\) is the production cross section of \(L_x\) line at projectile electron energy \(E\), \(N_X\) is the net yield of X-rays after self-absorption correction during a time interval \(T\), \(e(E')\) is the effective efficiency of detector at photon energy \(E'\) which is the energy of \(L_x\) line centroid, \(t\) is the thickness of target, \(A\) is the mass number of the target material, \(N_e\) is the total number of electrons impinging on the target during the same interval \(T\), \(N_A\) is the Avogadro number and \(k(E)\) is the enhancement factor defined as above \((k = 1\) for Lead). The effective efficiency of the detector includes the effect of the geometric factor, attenuation due to Mylar and the intrinsic efficiency of the detector.

The experimentally obtained production cross sections were converted to the ionization cross sections using Eqs. 3, 4, 5 given as:

\[
\sigma_{L_1} = \frac{\sigma_{L_{\gamma 236}}}{\omega_1 S_{\gamma 236,1}},
\]

\[
\sigma_{L_2} = \frac{\sigma_{L_{\gamma 1,5}}}{\omega_2 S_{\gamma 1,5,2}} - \sigma_{L_1} f_{12},
\]

\[
\sigma_{L_3} = \frac{\sigma_{L_\alpha}}{\omega_3 S_{\alpha,3}} - \sigma_{L_1}(f_{12} f_{23} + f_{13}) - \sigma_{L_2} f_{23}.
\]

\(S_{\gamma 1,2}\) is the fraction of radiative transition resulting from vacancy created in the \(j^{th}\) subshell associated with the \(L_i\) peak, \(\omega_j\) is the fluorescence yield corresponding to sub-shells \(L_i\), and \(f_{ij}\) is the Coster-Kronig transition probability between the \(L_i\) and \(L_j\) subshells. The production cross sections corresponding to the \(L_{\gamma 1}, L_{\gamma 236}\) and \(L_{\gamma 236}\) transitions are used in the above equations, which is the recommended combination (see ref. [14]), among many other combinations, to find the ionization cross sections. The atomic relaxation parameters, used in the calculations, are taken from the Refs. [15] and [16]. Tables I and II enlist all the parameters used in this work.

| Target    | \(\omega_1\) | \(\omega_2\) | \(\omega_3\) | \(f_{12}\) | \(f_{13}\) | \(f_{23}\) |
|-----------|--------------|--------------|--------------|------------|------------|------------|
| Lead      | 0.1          | 0.397        | 0.343        | 0.064      | 0.61       | 0.119      |
| Thorium   | 0.17         | 0.503        | 0.424        | 0.06       | 0.66       | 0.103      |

#### TABLE I. Fluorescence yield and Coster-Kronig transition probabilities used in this work.

It is evident from Eq. 4 that the \(L_{\gamma 236}\) production cross section is needed to obtain the \(L_1\) sub-shell ionization cross section. However, it is not directly available from experiment due to the limited resolution of the X-ray detector. As mentioned earlier, the \(L_\gamma\) peak is resolved into \(L_{\gamma 1}, L_{\gamma 1},\) and \(L_{\gamma 236}\) lines. Therefore, the production cross section of \(L_{\gamma 236}\) line is obtained by subtracting the contribution of \(L_{\gamma 1}\) from the experimentally obtained \(L_{\gamma 236}\) peak. The contribution of \(L_{\gamma 1}\), in turn, is obtained from the ratio: \(\Gamma_{\gamma 1}/\Gamma_{\gamma 1}\) and the \(L_{\gamma 1}\) peak counts of the fitted spectrum.

The \(L_\gamma\) peaks were not observed at 16 keV electron impact energy for Lead, and at 20 and 22.5 keV energy for Thorium. Also at 25 keV electron beam energy, only \(L_{\gamma 1}\) could be observed for Thorium and therefore, only the \(L_2\) and \(L_3\) ionization cross sections could be obtained. \(L_1, L_2\) and \(L_3\) ionization cross sections were extracted from the data at all energies above 16 keV for Lead and 25 keV for Thorium.

The \(L_\beta\) line of Thorium was resolved into \(L_{\beta 1}\) and \(L_{\beta 2}\) peaks in the obtained spectra. To cross-check and verify the obtained ionization cross sections, attempts were made to extract the \(L_1\) and \(L_2\) ionization cross sections from the \(L_{\beta 1}\) and \(L_{\beta 2}\) production cross sections using the equations 6 and 7 [17].
and \( \sigma \) the calculated (see Ref. [15]) restores good agreement with the results obtained from the sections for \( \sigma \) much deviation in \( L \) from the DWBA estimates. A good reason for using the parameters.

\[
\sigma_{(L_{\beta_1}+L_{\beta_5}+L_{\beta_4})} = S_{\beta_3,3\omega^3} \sigma_{L_{\alpha}} + [S_{\beta_1,2\omega^2} + S_{\beta_5,3\omega^3} f_{23}] \sigma_{L_{\alpha}} + [S_{\beta_1,2\omega^2} + S_{\beta_5,3\omega^3} (f_{13} + f_{12} f_{23}) + S_{\beta_3,1\omega^3}] \sigma_{L_{\alpha}},
\]

\[
\sigma_{(L_{\beta_2}+L_{\beta_6}+L_{\beta_4})} = S_{\beta_{2+6},3\omega^3} \sigma_{L_{\alpha}} + S_{\beta_{2+6},3\omega^3} f_{23} \sigma_{L_{\alpha}} + [S_{\beta_{2+6},3\omega^3} (f_{13} + f_{12} f_{23}) + S_{\beta_3,1\omega^3}] \sigma_{L_{\alpha}}.
\]

IV. RESULTS AND DISCUSSION

The X-ray production cross sections, determined from the experiment and the ionization cross sections, obtained from the experimental data, are shown in Tables \( \text{III} \) and \( \text{IV} \) for Lead and Thorium respectively. The uncertainties in the cross section values are indicated. Overall uncertainties for \( L \) X-rays production cross sections are \( \sim 11 - 12\% \) for both the elements. Contribution to the uncertainties are from 1) detector efficiency (\( \sim 10\% \)), 2) target thickness measurement (\( \sim 5\% \)) and 3) beam current measurement (\( \sim 3\% \)). Considering propagation of errors as per Eqs. \( \text{[3]} \) and \( \text{[5]} \), the uncertainties in the corresponding ionization cross sections are \( \sim 20\% \), and including the uncertainties in the relaxation parameters within their quoted ranges, the errors in the ionization cross sections are larger \( \sim 30\% \).

The experimental results are compared with the two different theoretical estimates based on two different formalisms: 1) MRBEB theory and 2) DWBA formalism. The DWBA theory based analytical formulas for calcu-

| Line | Source shell | Vacant shell | Transition Energy (keV) | Radiative Yield (\( \Gamma \)) | Radiative Yield Fraction (\( S_{\lambda,1} \)) | Transition Energy (keV) | Radiative Yield (\( \Gamma \)) | Radiative Yield Fraction (\( S_{\lambda,1} \)) |
|------|--------------|--------------|-------------------------|---------------------|----------------------|-------------------------|---------------------|----------------------|
| \( l_1 \) | M1 | L3 | 9.184 | 0.085 | 0.0406 | 11.119 | 0.146 | 0.0449 |
| \( l_{02} \) | M4 | L3 | 10.449 | 0.164 | 0.0786 | 12.81 | 0.250 | 0.0765 |
| \( l_9 \) | M1 | L2 | 11.347 | 0.052 | 0.0216 | 14.507 | 0.084 | 0.0215 |
| \( l_{04} \) | N1 | L3 | 12.141 | 0.021 | 0.0101 | 14.973 | 0.037 | 0.0115 |
| \( l_{05} \) | N5 | L3 | 12.623 | 0.293 | 0.1402 | 15.621 | 0.474 | 0.1451 |
| \( l_{04} \) | M2 | L1 | 12.304 | 0.456 | 0.3458 | 15.64 | 0.756 | 0.3588 |
| \( l_{04} \) | M4 | L2 | 12.614 | 1.884 | 0.7808 | 16.202 | 2.951 | 0.7598 |
| \( l_{05} \) | N4 | L3 | 12.601 | 0.032 | 0.0155 | 15.588 | 0.051 | 0.0158 |
| \( l_{04} \) | O4 | L3 | 13.013 | 0.042 | 0.0204 | 16.211 | 0.099 | 0.0305 |
| \( l_{05} \) | O5 | L3 | 13.013 | 0.042 | 0.0204 | 16.211 | 0.099 | 0.0305 |
| \( l_{04} \) | M3 | L1 | 12.791 | 0.501 | 0.3796 | 16.423 | 0.696 | 0.3303 |
| \( l_{05} \) | N1 | L2 | 14.305 | 0.013 | 0.0056 | 18.361 | 0.022 | 0.0058 |
| \( l_{04} \) | N4 | L2 | 14.762 | 0.404 | 0.1677 | 18.982 | 0.685 | 0.1765 |
| \( l_{02} \) | N2 | L1 | 15.099 | 0.120 | 0.0959 | 19.302 | 0.207 | 0.0983 |
| \( l_{03} \) | N3 | L1 | 15.215 | 0.145 | 0.1103 | 19.503 | 0.218 | 0.1036 |
| \( l_{04} \) | O4 | L2 | 15.176 | 0.054 | 0.0227 | 19.596 | 0.133 | 0.0343 |
| \( l_{04} \) | O3 | L1 | 15.775 | 0.052 | 0.0396 | 20.289 | 0.101 | 0.0478 |
| \( l_{04} \) | O2 | L1 | 15.755 | 0.052 | 0.0396 | 20.289 | 0.101 | 0.0478 |

TABLE II. Radiative yields for Lead and Thorium, from Campbell and Wang[16].
| Energy (KeV) | Production cross section | Ionization cross section | Parameters ω \_1 ω \_2 ω \_3 f \_12 f \_13 f \_23 Γ, σ |
|------------|--------------------------|--------------------------|------------------|
|            | \( L_\alpha \) (barn) | \( L_\beta \) (barn) | \( L_\gamma \) (barn) | \( L_1 \) (barn) | \( L_2 \) (barn) | \( L_3 \) (barn) | \% Error |
| 20         | 20.5(2.0)                | 02.8(0.3)                | ..                | ..                | 064.6(8.0)       |
| 22.5       | 46.8(5.6)                | 10.3(1.0)                | ..                | ..                | 147.5(18.4)      |
| 25         | 68.2(8.1)                | 21.9(2.0)                | 2.1(0.3)          | ..                | 213.0(26.8)      |
| 27.5       | 87.6(10.5)               | 31.5(3.1)                | 5.6(0.7)          | 29.2(7.3)         | 417.2(34.7)      |
| 30         | 103.8(12.5)              | 44.6(3.9)                | 6.2(0.8)          | 32.0(8.0)         | 301.1(41.1)      |
| 32.5       | 113.4(13.6)              | 51.7(4.5)                | 6.9(0.8)          | 33.9(8.4)         | 329.2(44.8)      |
| 35         | 114.9(13.8)              | 53.9(4.7)                | 7.7(0.9)          | 36.8(9.3)         | 331.7(45.5)      |
| 37.5       | 122.1(14.6)              | 56.7(5.0)                | 8.0(1.0)          | 36.5(9.1)         | 354.0(48.3)      |
| 40         | 129.5(15.5)              | 62.6(5.4)                | 8.9(1.1)          | 39.8(10.1)        | 374.5(51.3)      |
| 42.5       | 124.9(15.0)              | 59.8(5.3)                | 9.5(1.2)          | 41.0(10.3)        | 358.5(49.5)      |
| 45         | 127.9(15.3)              | 62.9(5.5)                | 8.9(1.1)          | 42.1(10.4)        | 368.0(50.6)      |

TABLE IV. Adopted errors in relaxation parameters.

While comparing with theory, it should be noted that the relaxation parameters, which are used to obtain theoretical production cross sections, can themselves have uncertainties \( \lesssim 50\% \). Table [V] shows the recommended uncertainties in Ref. [13], which are adopted in this work.

The \( L \) X-ray production cross sections of Lead and Thorium are plotted in the Figures [4] and [5] respectively. Corresponding theoretical estimates, based on the DWBA and the MRBEB theories are also plotted on the same graphs. The shaded regions around the DWBA estimates in both the graphs indicate the predicted uncertainty bands arising from the uncertainties in the adopted relaxation parameters.

In case of Lead, the \( L_\alpha \) and \( L_\beta \) X-ray production cross sections, based on measurements done by Wu et al. [18] and Moy et al. [19], are also shown in the Fig. [4]. These two sets of measurements are in good agreement with

\[
\sigma_{L_\beta} = \sigma_{L_1} \left[ \omega_1 S_{\beta,1} + \omega_2 f_{12} S_{\beta,2} + \omega_3 (f_{13} + f_{12} f_{23}) S_{\beta,3} \right] + \sigma_{L_2} \left[ \omega_2 S_{\beta,2} + \omega_3 f_{23} S_{\beta,3} \right] + \sigma_{L_3} \omega_3 S_{\beta,3} \quad (8)
\]

\[
\sigma_{L_\gamma} = \sigma_{L_1} \left[ \omega_1 S_{\gamma,1} + \omega_2 f_{12} S_{\gamma,2} \right] + \sigma_{L_2} \omega_2 S_{\gamma,2} \quad (9)
\]
our corresponding results. The DWBA estimates for the $L_\alpha$ production cross sections of both the elements are in good agreement with all three experimental data sets. The DWBA estimates for $L_\beta$ lines of Lead overpredict the production cross sections across the energy range of interest, but the estimates agree with the experimental results within the predicted uncertainty band. Considering the systematic trend in the experimental data over the energy range, the results of Wu et al. [18] are in better agreement within the uncertainty band. Our results for Lead are systematically on the lower end of the predicted band. The MRBEB theory predicts larger production cross sections in all the cases, with values grazing the upper end of the predicted uncertainty band of DWBA estimates.

No other measurement of the $L$ X-ray production cross sections of Thorium exists to the best of our knowledge. Our results agree with the DWBA estimates for the $L_\alpha$ line (see Fig. 5). Comparison with DWBA estimates for the $L_\beta$ and $L_\gamma$ production cross sections of Thorium indicate the similar trend as that in Lead.

The discrepancy between theory and experiment can be further understood by looking at the $L_1$, $L_2$, and $L_3$ ionization cross sections extracted from our experimental data. The ionization cross sections obtained from our experiment, along with theoretical estimates, are plotted in the Figs. 6 and 7 for Lead and Thorium respectively. In both the elements, the $L_3$ ionization cross section is explained very well by the DWBA theory, specifically for the energies $E > 1.35U$, where $U$ is the ionization threshold for the $L_3$ subshell. Also it is important to note that the $L_3$ subshell ionization cross sections for only a handful of elements in the range from Phosphorus ($Z = 15$) to Uranium ($Z = 92$), measured either directly from electron energy loss spectroscopy (EELS) or indirectly by electron impact spanning energy range from near the ionization threshold to $\sim 1$ MeV, are found to agree reasonably well with the DWBA calculations following Bote...
higher ionization cross sections than the DWBA theory by \( \sim \) \( \frac{L}{100} \). In both the elements studied in our experiment, \( L \) threshold. But in case of \( L \) subshell, \( L \) subshells and the Coster-Kronig factors need to be re-evaluated and experimentally measured.

The \( L \) subshell results are inconclusive due to the fact that the \( \sigma_{L_2} \), obtained from \( \sigma_{L_{1+2}} \) is lower than the theoretical estimates by \( 30 \sim 50\% \), but the \( \sigma_{L_3} \) values, which have almost equal contribution from \( \sigma_{L_2} \) and \( \sigma_{L_3} \), are explained reasonably well by the DWBA theory, specifically for Lead and other high \( Z \) elements[7, 12]. The \( \sigma_{L_3} \) and \( \sigma_{L_0} \) results are explained very well by theory, not only for the Pb and Th, but also for the other high \( Z \) elements[7,12], indicating that the relaxation parameters related to \( L_3 \) subshell are consistent with the underlying theory and related experiments.

From our study, it is evident that the discrepancy between theory and experiment may arise due to errors in fixing some of the relaxation parameters. It is, therefore, important to perform measurements, which require a minimum number of relaxation parameters for extracting ionization cross sections from the experimental data. Clearly, more measurements with wavelength dispersive spectrometer should be done where resolution is so high that even a single transition can be studied, thereby reducing the dependence on the relaxation parameters. Also, very few measurements exist for the \( L \) \( \gamma \) X-ray production cross sections of high \( Z \) elements. As \( L \) transitions relate to the \( L_1 \) and \( L_2 \) subshells, it is important to perform these measurements, specifically in view of the new calculations performed by Pindzola[4,12] by the inclusion of the retarded electromagnetic potential, which significantly changes the ionization cross sections of the \( L_1 \) and \( L_2 \) subshells.

V. CONCLUSION

We have obtained the subshell resolved ionization cross sections from the production cross sections involving the \( L \)-shell in Lead and Thorium. Results are compared with two different theoretical formalisms viz., MRBEB and DWBA. The experimental results are reproduced reasonably well by the DWBA theory for the \( L_3 \) subshell and the \( L_\alpha \) transition, but poor agreement is found for \( L_1 \) and \( L_2 \) subshells and consequently for the \( L_\beta \) and the \( L_\gamma \) transitions in both the elements. MRBEB theory overpredicts the cross sections for all the three subshells in both the elements in the electron impact energy regime explored in our experiment. Discrepancy between DWBA theory and our experiment points to the poor knowledge of the relaxation parameters related to the \( L_1 \) subshell. From our study, we conclude that more

FIG. 6. \( L_1 \), \( L_2 \) and \( L_3 \) subshell ionization cross sections of Lead.

et al.[8], as described in detail in Ref. [20]. The agreement is very limited especially at energies near the ionization threshold. But in case of \( L_2 \) and \( L_1 \) subshells, the agreement between theory and experiment is not at all satisfactory. In both the elements studied in our experiment, the \( L_2 \) and \( L_1 \) subshell ionization cross sections at near-threshold energies are smaller than the DWBA estimates by \( \sim 30 \sim 50\% \). The MRBEB theory predicts \( \sim 20 \sim 30\% \) higher ionization cross sections than the DWBA theory for \( L_2 \) and \( L_3 \) subshells and up to \( 80\% \) higher for \( L_1 \) subshell.

The difference in theory and experiment for \( L_1 \) and \( L_2 \) sub-shell results can be due to the relaxation parameters used in the estimation of these ionization cross sections. A direct indication of the results of relaxation parameter variation is given in Sec. [11] in connection with our attempt in extracting \( \sigma_{L_1} \) and \( \sigma_{L_2} \) for Thorium from the corresponding \( \sigma_{L_m} \) and \( \sigma_{L_n} \). While calculating the \( \sigma_{L_1} \) from the corresponding \( \sigma_{L_{2+3}} \) for both the elements, we have used the radiative yields \( \Gamma_{\gamma_1}, \Gamma_{\gamma_6}, \Gamma_{\gamma_2}, \Gamma_{\gamma_3} \) and the fluorescence yield \( (\omega_1) \). Out of these five relaxation parameters, \( \Gamma_{\gamma_2}, \Gamma_{\gamma_3} \) and \( \omega_1 \) are associated with the relaxation of the vacancy created in the \( L_1 \) subshell, and the remaining parameters are associated with the vacancy in the \( L_2 \) subshell. Thus, our experimental findings indicate that the differences between theory and experiment could be due to the poorly known relaxation parameters, specifically the relaxation parameters related to the \( L_1 \) subshell. It is worth mentioning here that in a review on theories of inner shell ionization by proton impact[21], the author has concluded that the radiative yield related to the \( L_1 \) subshell and the Coster-Kronig factors need to be re-evaluated and experimentally measured.
precise measurements of the corresponding sub-shell resolved cross sections are urgently needed to obtain the relaxation parameters with better precision.

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