ULTRAFAIN DARF S—ST A R F ORM AT I ON A ND CHEMICAL EVOLUTION IN THE SMALLEST GALAXIES

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ABSTRACT

In earlier work, we showed that a dark matter halo with a virial mass of 10^7 M⊙ can retain a major part of its baryons in the face of the pre-ionization phase and supernova (SN) explosion from a 25 M⊙ star. Here, we expand on the results of that work, investigating the star formation and chemical evolution of the system beyond the first SN. In a galaxy with a mass Mvir = 10^7 M⊙, sufficient gas is retained by the potential for a second period of star formation to occur. The impact of a central explosion is found to be much stronger than that of an off-center explosion both in blowing out the gas and in enriching it, as in the off-center case most of the SN energy and metals escape into the intergalactic medium. We model the star formation and metallicity, given the assumption that stars form for 100, 200, 400, and 600 Myr, and discuss the results in the context of recent observations of very low-mass galaxies. We show that we can account for most features of the observed relationship between [α/Fe] and [Fe/H] in ultra-faint dwarf galaxies with the assumption that the systems formed at a low mass, rather than being remnants of much larger systems.

Key words: dark ages, first stars, reionization -- galaxies: abundances -- galaxies: dwarf -- galaxies: formation -- stars: Population II

Online-only material: color figures

1. INTRODUCTION

The origin of the smallest galaxies (M_300 < 10^7 M⊙) is an unresolved question. Some are likely to be remnants of much larger (∼10^9 M⊙) systems that have been stripped of a large percentage of their baryons and dark matter (Mayer et al. 2001), but others may have formed as low-mass systems. The discovery of examples of this latter class of systems would boost our understanding of the early baryonic systems, as they are likely to have preserved chemical signatures of the first generations of stars. Small systems are simpler and are likely to have undergone fewer enrichment events, leaving these signatures relatively intact (Bland-Hawthorn et al. 2010; Karlsson et al. 2012; Frebel & Bromm 2012; Karlsson et al. 2013).

The Sloan Digital Sky Survey (York et al. 2000) discovered a number of very faint Local Group dwarf galaxies. These galaxies have luminosity L_⊙ < 10^6 L⊙ and are known as ultrafaint dwarfs (UFDs). The halo masses of these systems are uncertain and highly model-dependent; however, the masses within the half-light radius are better constrained. Wolf et al. (2010) found that the half-light masses of the UFDs ranged from 6 × 10^5 to 1.2 × 10^7 M⊙. Segue 2 (Belokurov et al. 2009) contains less than 1.5 × 10^7 M⊙ within the half-light radius.

Early UFD studies such as Simon & Geha (2007) studied chemistry using [Fe/H] histograms, but more recent works (Frebel & Bromm 2012; Vargas et al. 2013; Kirby et al. 2013a) have added an extra dimension through observations of [α/Fe]. Tinsley (1979) suggested that enhanced [α/Fe] in halo stars could be explained by the time delay between Type II and Type Ia supernovae (SNe), and this idea is now widely used in chemical modeling. Type II SNe eject many more alpha elements relative to iron than Type Ia and can occur early in the lifetime of a galaxy because their progenitors are short-lived high-mass stars, while Type Ia SNe do not form until much later. This means that the enrichment is initially dominated by Type II SNe such that [α/Fe] is initially high, but declines after ∼100 Myr due to the effect of Type Ia SNe. The value of [Fe/H] at which [α/Fe] begins to decline is linked to the number of Type II SNe in the first 100 Myr and is therefore an approximate measure of the star formation rate in a system. If there is no decline, it is likely that star formation lasted less than 100 Myr. However, as we will show, the stochastic nature of star formation in small systems means that the average time between Type Ia SNe can be as much as 50 Myr and it is therefore possible for a system to form stars for significantly longer than 100 Myr without a Type Ia SN.

Frebel & Bromm (2012) investigated six UFDs and found that Ursa Major II was a good candidate for having no Type Ia enrichment, while Coma Berenices and Bootes I were reasonable candidates given uncertainties in r-process predictions. Vargas et al. (2013) found that Segue I and Ursa Major II do not show any low [α/Fe] stars and, therefore, star formation likely lasted less than 100 Myr. However, five other UFDs do show a decline in [α/Fe] with increasing [Fe/H], and therefore likely had longer star formation histories. While total halo masses are difficult to constrain, the galaxies studied in these two works have (baryon+dark) masses of the order of 10^5–10^7 M⊙ within the half-light radius, suggesting that their virial masses range from slightly lower than the M_vir = 10^7 M⊙ models we present here, to significantly higher.

Tolstoy et al. (2009) emphasize that dwarf galaxies are not special systems and that the only reason for classifying them separately is to study galaxy formation and evolution on a smaller scale. However, in the early universe, there are two effects that can prevent galaxies from forming or surviving in low-mass dark matter halos. The first is the epoch of reionization, when the light from the first stars photoionized much of the neutral gas in the early universe, such that neutral gas could not cool and settle in small halos. The usual assumption is that the threshold halo mass exceeds ∼10^8 M⊙.

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(Rees 1986; Barkana & Loeb 1999; Gnedin 2000; Okamoto et al. 2008). However, as noted in Bland-Hawthorn et al. (2014, referred to as Paper I), the timescale for the evaporation of gas is long enough that the star-forming gas in the inner region is protected and can form stars while the gas in the outer regions evaporates. Recent simulations support this view, finding that at least some halos with masses \( \sim 10^7 M_\odot \) can survive the epoch of reionization and continue forming stars (Bovill & Ricotti 2009; Ricotti 2009; Bovill & Ricotti 2011).

The second process that can remove neutral gas from galaxies is the energy output of massive stars. In the two-dimensional axisymmetric models of Mac Low & Ferrara (1999), the energy from central SN explosions was found to couple efficiently with the interstellar medium (ISM) and all the neutral gas was blown out from systems with \( \lesssim 10^8 M_\odot \). Mac Low & Ferrara (1999) assumed a constant rate of energy input, with the lowest rate corresponding to an SN every 3 Myr.

In Paper I, we presented three-dimensional hydrodynamical models demonstrating that systems with virial masses of \( 10^{5.5} - 10^7 M_\odot \) retain nearly all of their gas in the face of wind, pre-ionization, and SN from a 25 \( M_\odot \) star. This suggests that gas survival is common in these systems, because under typically assumed initial mass functions (IMF; e.g., Kroupa 2001), 80\% of stars massive enough to end their lives as SNe are less massive than 25 \( M_\odot \). The most important difference between the models in Paper I and previous works is that a single SN is assumed. In systems as small as these, the low star formation rate results not only in a low SN rate, but also a high degree of stochasticity such that long gaps between SNe are plausible. This means that the gas in some systems has sufficient time to recover from the effects of one SN before it is disrupted by another. Furthermore, an SN event temporarily suppresses star formation such that massive stars, with their associated winds and SNe, are less likely to form in the period and location in which the gas is disrupted. Halos with low masses are common in the early universe, and while many of the systems we study will lose nearly all of their star-forming gas before a significant amount of stars can form, the stochasticity of star formation is such that at least some systems will have their massive stars spaced far enough apart in space and time for dense gas to be retained and star formation to continue.

Our work also differs from previous works in that we assume an inhomogeneous medium, which assists in the survival of systems, as energy can escape through low-density channels. Paper I also investigates the effect of the location of the SN, finding that if the SN occurred away from the center, the impact of the SN was smaller because most of the energy escaped through the lower density regions away from the center. Finally, we included the effects of the early-phase photoionization of the star before it explodes, finding that the energy output from a 25 \( M_\odot \) star over its lifetime is comparable to the SN’s explosive energy.

Our models form after the first generation of stars, but before or at the early stages of the epoch of reionization. They are considered to form in isolation and we do not seek to model their interaction with the Galaxy. This paper builds on the work of Paper I by considering what happens after the first SN. Using a probabilistic method based on that of Argast et al. (2000) and the output from the simulations described in Paper I, we simulate star formation and chemical evolution in galaxies with masses of \( 10^7 M_\odot \). We also discuss \( 10^{6.5} M_\odot \) systems and find that a 25 \( M_\odot \) star is sufficient to terminate star formation. We compare our results for \( [\alpha/Fe] \) versus \( [Fe/H] \) to the UFDs from Vargas et al. (2013) as well as Segue 2, which is the least massive known galaxy (Kirby et al. 2013a).

Section 2 discusses the numerical models and simulations performed, although we will refer to Paper I for a more detailed explanation of the single SN simulations. Section 3 will outline our star formation prescription. Section 4 analyzes the distribution of mass, location, and frequency of SNe, and the results of extending the simulation beyond the first SN are discussed in Section 5. Section 6 will compare to observed UFDs, followed by our conclusions in Section 7.

2. METHODS

2.1. Single Supernova Simulations

We do not seek here to model the formation of the first stars in minihalos with masses of \( 10^5 M_\odot \), which is dealt with in other works (Abel et al. 2002; Yoshida et al. 2008), but instead assume that the first stars have enriched the intergalactic medium (IGM) to \([Fe/H] = -4\) (Madau et al. 2001; Bromm & Larson 2004), the lower limit of the available gas cooling functions (Sutherland & Dopita 1993). Evidence for such low metallicities originally came from the metal-poor stars in the Galactic halo (Karlsson et al. 2013). But gas phase metallicities as low as \([Fe/H] = -4\) have now been observed in the IGM at \( z \sim 3-3.5\) (Fumagalli et al. 2011). This is therefore an appropriate starting metallicity for our model, although the threshold could be lower if early galaxy winds fail to enrich the IGM, as in the simulations of Muratov et al. (2013). \([Fe/H] = -4\) is close to the limit at which sufficient dust can form for low-mass star formation to be possible. We therefore allow only high-mass stars to form in unenriched gas, with low-mass stars beginning to form in gas that is enriched even slightly from its initial state. Subsequent star formation is modeled by the prescription described in Section 3.

The simulations are described in detail in Paper I, but here we provide an explanation of the features of the first star, both during its lifetime and once it explodes. For simplicity, throughout the paper, the \( 10^7 M_\odot \) model will be referred to as M70 and the \( 10^{6.5} M_\odot \) model as M65.

2.1.1. Modeling the Photoionization Around the SN Progenitor

The pre-ionization of the gas by the SN precursor plays a key role in the loss or survival of gas after the SN explosion, particularly in low-mass dark matter halos. In Paper I, we consider in detail the impact of an ionized H II region that forms around the progenitor star prior to the explosion. The key parameters of this model are the effective temperature \( (T_{\text{eff}}) \), the luminosity \( (L) \), and the associated stellar atmospheres. These give the ionizing photon flux as a function of time up to the SN event. Transforming the grid coordinates to spherical coordinates around the star, radial summations to approximate the optical depth integrals are performed, resulting in thermal and ionization structures calculated from the \textsc{Mapping IV} ionization code. These are then mapped back to Cartesian coordinates and used in the \textit{Fyris} fluid computations. It was necessary to perform this remapping for every timestep in the fluid dynamics simulation in order to track the evolution in opacity. This slowed the code by a factor of 5–10 and was therefore only performed on specific cases of the M65 and M70 where gas had been observed to survive without pre-ionization. We considered both clumpy and smooth external media with and without gas cooling.
We model the SN progenitor with a low-metallicity star of $25 M_\odot$ since 80% of all SN events in a conventional IMF have lower mass and therefore weaker ionizing radiation fields. We use the evolutionary tracks of (Meynet & Maeder 2002, hereafter MM02) for a rapidly rotating, low-metallicity massive star. Their $[\text{Fe/H}] = -3.7$ tracks are the closest published tracks for the metallicity threshold used here. The $25 M_\odot$ track was missing from that work, and so we have interpolated the main sequence phase of this model from the other stellar models. We used the tabulated main sequence lifetime of 6.1 Myr from MM02. The interpolation is shown in Figure 1. For the above model, we adopt a stellar spectrum at $[\text{Fe/H}] = -4$ using an ATLAS9 ZAMS stellar atmosphere (Castelli & Kurucz 2004) shown in Figure 2.

To avoid the complexities of rapid post-main sequence evolution, we assume that the star simply explodes as an SN at the end of the main sequence. Ekström et al. (2006) showed that mass loss during the main sequence in similar stars at very low metallicity may only amount to 1% of the initial mass, and Kudritzki (2002, 2005) showed that the stellar wind luminosities of low-metallicity ($[\text{Fe/H}] \leq -4.0$) O stars are typically $10^{38}$ erg s$^{-1}$ or less, several magnitudes below an equivalent solar metallicity star. We combine these values to get a mean wind velocity for a main sequence mass loss of 1%:

$$v_w \approx 880 \left( \frac{L_w}{10^{34} \text{erg s}^{-1}} \right)^{1/2} \left( \frac{M}{25 M_\odot} \right)^{-1/2} \left( \frac{t_{\text{MS}}}{6.1 \text{Myr}} \right)^{-1/2} \text{km s}^{-1}. \tag{1}$$

This wind is included in the pre-SN evolution, but the small mass flux and low ram pressure meant that it had negligible effect on the simulations. Once the H II region pressurized the surrounding region, the stellar wind was unable to blow a wind bubble of any significant size.

The key parameter for these near-zero metallicity O stars is their unusually high effective temperatures for a given mass. 40,000 K (see, for example, Meynet & Maeder 2000, and more recently, Georgy et al. 2012). This means the star will be more effective as a source of ionizing photons than the equivalent star at the same mass in similar stars at very low metallicity. To convert the evolutionary tracks, $T_{\text{eff}}(t)$ and $L(t)$, to an ionizing photon luminosity, we used the ATLAS9 (Castelli & Kurucz 2004) atmospheric grid, which uniquely contains a set of atmospheres for $[\text{Fe/H}] = -4.0$ with alpha element abundance enhancements, perfectly matching the initial gas composition in our simulations. The interpolated stellar temperature, luminosity, and ionizing fluxes are shown in Figure 3. For comparison, a photon flux assuming a blackbody instead of the stellar atmosphere is included.
2.2. Multiple Supernovae

The simulations outlined in Paper I followed the evolution of the system in the face of the energy output from a single massive star and it was found that for systems more massive than $10^{6.5} M_\odot$ gas will be retained and further star formation is possible. The goal of this paper is to model this subsequent star formation and chemical enrichment, allowing the production of $[\alpha/Fe]$ versus $[Fe/H]$ plots to compare with observed UFDs. The simulation method described in the previous section is computationally intensive, and the boundary conditions begin to have an effect even at 60 Myr. A significantly larger grid would be required to run the full simulation for hundreds of Myr. Instead, we use the 60 Myr of data from the first SN to simulate the effects of later SNe.

We run a simulation for 600 Myr with a resolution of 0.5 Myr. Stars are allowed to form using a Kroupa IMF and an adaptation of the Argast et al. (2000) stochastic method, where stars are formed in a cell with a probability proportional to the square of the gas density as described in Section 3. The gas recovers within 30 Myr of an SN explosion from a $25 M_\odot$ star, so the density in each cell of the single SN simulations from Paper I at 35 Myr is taken as representing the undisturbed density. If a star more massive than $20 M_\odot$ is formed sufficiently close to the center to have a significant impact on the system, the density is reset to the $r = 0$ value and allowed to evolve forward through the frames of the single SN simulation. If a star with a mass between 8 and $20 M_\odot$ is formed, the simulation keeps moving forward through the frames during the lifetime of the star, then resets to the 6 Myr state, which is the time at which the SN occurs in the single-SN simulation. This has the effect of removing the pre-ionization phase, which is less significant for stars less than $20 M_\odot$. Note that the impact of an SN will be lessened in the absence of a pre-ionization phase, so this may slightly underestimate the amount of star formation for a few megayears after the SN. Opposing this effect is the fact that...
the gas will not always recover completely before the next SN occurs, so an SN from a less massive star will sometimes occur in a pre-ionized environment.

A similar method is used to calculate \([\text{Fe}/\text{H}]\), except that instead of resetting, as is done for density, each SN enriches the gas, so \([\text{Fe}/\text{H}]\) increases. As can be seen in Figure 6, by 40 Myr after the SN, the \([\text{Fe}/\text{H}]\) in the densest cells and the central cells is close to constant, so this value can be used to calculate the iron output of a single SN. Models of Type II SN yields such as in Nomoto et al. (2006) note that the iron yield from Type II SNe is nearly independent of stellar mass. Therefore, after each SN, we reset the \([\text{Fe}/\text{H}]\), as was done for density above, but with the addition of the iron from a single SN multiplied by the number of previous SNe. This is only an approximation, and the true Fe yield may be slightly higher or lower depending on the state of the gas, as was noted for density above. \([\alpha/\text{Fe}]\) is calculated in the same way as \([\text{Fe}/\text{H}]\), with the \(\alpha\) abundance defined as the sum of the abundances of Ca, Mg, Si, and Ti. The yields used are from Woosley & Weaver (1995), interpolated and extended to 8 \(M_\odot\). They are seven times the amount of iron that a typical Type II SN produces, and it therefore only takes a few Type II SNe to significantly reduce \([\alpha/\text{Fe}]\).

### 3. STAR FORMATION PRESCRIPTION

A realistic prescription of star formation is required to predict the observational properties of our simulated systems. The amount and location of star formation are the most important factors in the length of time stars will form before there are multiple SNe close enough in location and time to turn off star formation. Particularly important is whether the system survives for the 100 Myr it takes for the first Type Ia SNe to occur, which shows up observationally in decreased \([\alpha/\text{Fe}]\).

The first step was to choose the criteria for a cell in the simulation to form a star. The simulations do not include self-gravity and molecular cooling, so the gas does not cool to star-forming temperature, which is much less than 100 K. Recent work by Hopkins et al. (2013) outlines several possible methods for specifying the amount and position of stars in high-resolution simulations. They find that the best results are given by an “overdensity” criterion,

\[
\alpha = \beta \frac{|\nabla \cdot \mathbf{v}|^2 + |\nabla \times \mathbf{v}|^2}{G\rho} < 1,
\]

where the density of the gas, \(\rho\), is compared to the sum of the square magnitudes of the divergence and curl of the velocity field \(\mathbf{v}\), which account for the local velocity dispersion and the internal rotation and shear of the gas. \(\beta \sim 0.5\) is a constant relating to geometry.

However, Hopkins et al. (2013) note that for systems where the average density is much less than the typical densities at which stars form, a simple density criterion works nearly as well. This is certainly the case for our modeled systems, and a test of both criteria over 10 Myr adjusted for a chosen star formation rate did not show significant differences in the spatial distribution of star formation.

The density criterion is simpler than the Hopkins overdensity criterion, and we therefore adapt the method of Argast et al. (2000). At each time step, \(5 \times 10^4\) cells are selected...
at random from the 2163 L1 grid, and each is given a probability of forming a star that is proportional to the square of the density of the cell. This introduces stochasticity to the method, ensuring that the star formation is not completely dominated by the cells in the center, which have the highest density. Changing the proportionality coefficient and the number of cells gives two free parameters that allow the rate of star formation and the distribution of densities at which stars form to be specified.

The critical metallicity at which the IMF switches from top-heavy to bottom-heavy is believed to be $Z_{\text{crit}} \sim 10^{-6} - 10^{-3.5} Z_\odot$ (Bromm & Yoshida 2011). Given that the metallicity in the first galaxies is likely to be similar to the upper end of this range (Bromm et al. 2003; Frebel et al. 2007), we allow low-mass stars to form only in gas that has been enriched by our first SN. We note that some simulations (Johnson et al. 2008; Greif et al. 2010) find that the metallicity of the first galaxies could be as high as $[\text{Fe/H}] = -3$, which would have the effect of increasing our total star formation. The masses of stars are selected by sampling a Kroupa IMF (Kroupa 2001) with a mass range of 0.1–50 $M_\odot$, with the restriction that if the mass of the star is less than 8 $M_\odot$ and the metallicity at the location the star is to be formed is $[\text{Fe/H}] \leq -4$, the star does not form.

We start with a reference model to find the baseline star formation rate, allowing us to calculate the disrupting effect of the SN, as well as providing a check that our star formation criteria are reasonable. This is the star formation rate for the undisturbed gas if no SNe occurred, assuming the Kroupa IMF at all metallicities. The mean star formation rate is $1.3 \times 10^{-5} M_\odot \text{yr}^{-1}$ for M70 and $5.7 \times 10^{-6} M_\odot \text{yr}^{-1}$ for M65. This corresponds to $1.4 \times 10^{-4} M_\odot \text{yr}^{-1}$ kpc$^{-2}$ within the scale radius of M70 and $1.8 \times 10^{-4} M_\odot \text{yr}^{-1}$ kpc$^{-2}$ for M65, which is within an order of magnitude of the observed star formation rates in starbursts in larger dwarf galaxies such as Carina (Bigiel et al. 2008).

We then take the single-SN model and assume that a $25 M_\odot$ star forms at $t = 0$. The proportion of dense gas retained is compared in Figure 5, while Figure 7 shows how the distribution of metals changes over time after the SN. In the M70CC case, the metals mix with the gas in the center and the regions with dense gas become enriched. In the M70OC case, the gas in the center remains unenriched and therefore no low-mass stars are formed. An SN explosion closer to the center is therefore required for low-mass stars to form.

The variation in star formation rate, given the wind and SN from this $25 M_\odot$ star, is shown in Figure 8 for M70CC. The star formation rate dips as much of the dense gas is blown out by the energy from the stellar winds and SN, but eventually much of the gas returns to the center of the galaxy, meaning that there are enough dense regions for the star formation rate to recover to 50% of the pre-SN level. The M70 off-center explosion does not form low-mass stars because the dense gas is not enriched. The M65 models quickly lose all of their dense gas, so they never form low-mass stars.

In the M65 model with a central explosion, dense gas is rare by the time the SN occurs, and the SN blows out the remaining 10%. By 15 Myr, the amount of gas denser than $n_H = 10$ cm$^{-3}$ is negligible. The off-center M65 model survives the pre-SN ionization with about half of its dense gas intact. However, the SN explosion blows out the rest of the dense gas, and by 25 Myr a negligible amount of gas remains, with $n_H > 10$ cm$^{-3}$. The mean total star formation with the enrichment condition relaxed is $16 M_\odot$ for the central model, while the mean for the off-center model is $27 M_\odot$.

In this section we discussed only the impact of the first high-mass star and found that for the M70 model, after the first central explosion, low-mass stars are able to form, while an off-center
explosion has only a small impact on the system. This means that the system will survive and form stars until there are multiple SNe close to the center and not spaced too far apart in time. In the next section, we will discuss the distribution of the masses, location, and timing of subsequent stars that will end their life as an SN, all of which affect how long star formation continues in the system.

4. MASS, LOCATION, AND TIMING OF SUPERNOVAE

For the multi-SN simulation, we require estimates of how frequently massive stars form, how massive they are, and where they occur. Here, we use the output of the single SN simulations to estimate these parameters. We also identify effects that separate massive stars in location and in time, supporting the
For various stellar masses from Schaerer (2002) for $Z = 0$ and $Z = 0.02 Z_\odot$. At lower metallicity, the lifetimes are shorter. The starting metallicity in our simulations is $10^{-4} Z_\odot$, so the lifetimes and $Q$ in our simulations will be somewhere between these two extremes.

4.2. Timing

The probability $p_{\text{form}}$ that at least one star with a mass greater than $8 M_\odot$ has formed since $t = 0$ is

$$p_{\text{form}}(t, M > M_{\text{crit}}) = 1 - 0.994^n,$$

where $n$ is the number of stars that have formed by time $t$, $M_{\text{crit}} = 8 M_\odot$ is the threshold for a star to end its life as an SN, and the probability $p_{\text{SN}}$ that a SN explosion has occurred before time $t$ is

$$p_{\text{SN}}(t) = 1 - \sum_{M = M_{\text{crit}}}^{50} \left(1 - p_M(t - t_M)dMight),$$

where $t_M$ is the lifetime of a star of mass $M$ and $p_M$ is given by Equation (2).

Figure 9 shows the cumulative probability of a second SN with time following the formation of a $25 M_\odot$ star at $t = 0$. For the centered case, while a second massive star is likely to form within 10 Myr, there is only a ~30% chance that the SN from the star will occur before the gas recovers at $t \sim 20$ Myr. For the second explosion to occur within 20 Myr of the first, the second star must have a mass of at least $12 - 30 M_\odot$. This supports our assumption that the gas usually recovers after an SN before the next SN disrupts it again, meaning that the system is likely to survive at least its first two SN explosions.

4.3. Location

Figures 4(a) and (b) show the effects of a $25 M_\odot$ star on an M70 halo. Over the first 6 Myr, the star pushes gas out as well as ionizing the surrounding gas, creating a region where there

**Table 1**

| Mass ($M_\odot$) | Prob | $Z = 1/50 Z_\odot$ | $Z = 0$ |
|-----------------|------|-----------------|--------|
|                 | Z    | Lifetime (Myr) | $ar{Q}$ (photon s$^{-1}$) | Lifetime (Myr) | $ar{Q}$ (photon s$^{-1}$) |
| 8–10            | 0.28 | 38–27 | 0.2–1.5 $\times 10^{46}$ | 25–18 | 2.3–4.7 $\times 10^{47}$ |
| 10–12           | 0.17 | 27–21 | 1.5–6.5 $\times 10^{46}$ | 18–14 | 4.7–8.5 $\times 10^{47}$ |
| 12–15           | 0.16 | 21–15 | 0.7–3.0 $\times 10^{47}$ | 14–10 | 0.9–1.7 $\times 10^{48}$ |
| 15–20           | 0.15 | 15–11 | 0.3–1.4 $\times 10^{48}$ | 10–7.5 | 1.7–3.8 $\times 10^{49}$ |
| 20–25           | 0.084 | 11–8.3 | 1.4–5.9 $\times 10^{49}$ | 7.5–6.1 | 3.8–6.8 $\times 10^{49}$ |
| 25–30           | 0.053 | 8.3–7.0 | 3.9–7.6 $\times 10^{49}$ | 6.1–5.2 | 0.7–1.1 $\times 10^{50}$ |
| 30–35           | 0.036 | 7.0–6.1 | 0.8–1.2 $\times 10^{50}$ | 5.2–4.6 | 1.1–1.6 $\times 10^{51}$ |
| 35–40           | 0.026 | 6.1–5.5 | 1.2–1.8 $\times 10^{51}$ | 4.6–4.2 | 1.6–2.1 $\times 10^{52}$ |
| 40–45           | 0.019 | 5.5–5.0 | 1.8–2.3 $\times 10^{52}$ | 4.2–3.9 | 2.1–2.8 $\times 10^{53}$ |
| 45–50           | 0.015 | 5.0–4.7 | 2.3–2.9 $\times 10^{53}$ | 3.9–3.7 | 2.8–3.4 $\times 10^{54}$ |
is no dense neutral gas for star formation to occur. This region forms a Strömgren sphere and has a radius

\[ r_{\text{strom}} = \left( \frac{3 Q(H)}{4\pi \beta_2 n^2} \right)^{1/3}, \]  

(6)

where \( Q(H) \) is the photon flux from the star and \( n \) is the gas density. At low metallicities, the recombination rate \( \beta_2 \) to all levels other than the ground state is \( \beta_2 = 1.84 \times 10^{-13} \times (T/1.5 \times 10^4 \text{ K})^{-0.78} \) (Dopita & Sutherland 2003).

The gas density is not constant, but decreases as radius increases and is also inhomogeneous such that it is not constant at a given radius. In the case where the star is not at the center, this means that the ionized region can be highly asymmetric, as the Strömgren radius is smaller in the direction of the dense gas in the center and much larger in other directions.

In the central case, the region is nearly symmetrical, and we use the mean density of the gas. The extent of the Strömgren sphere increases with time, because the region surrounding the star becomes less dense. Figure 10(a) shows how the radius increases for a 25 \( M_\odot \) star at the center of the M70 system. The values of temperature and photon flux are from MM02, as described in Section 2.1.1. This Strömgren radius can be considered an exclusion radius within which no stars will form. The maximum radius of 74 pc at 6 Myr is very close to the half gas-mass radius where we form the star in the off-center model.

The above effect can aid the survival of small galaxies. Two massive stars cannot form close together in location, as the first will create an ionized region that prevents the second from forming. The more massive the first star to form, the bigger the effect. Figure 10(b) shows the Strömgren radius as a function of mass just after the star has formed. Two metallicities are shown, \( Z = 0 \) and \( Z = 1/50 \ Z_\odot \), while the metallicity in our model lies between these two values.

While a 25 \( M_\odot \) star has a Strömgren sphere that covers half the scale radius, lower mass stars have a much smaller effect. Figure 1 shows a sharp fall in photon flux for stars below 25 \( M_\odot \). At \( Z = 10^{-2} \ Z_\odot \), the radiation from a 12 \( M_\odot \) star over its entire 20 Myr lifetime is the same as a 25 \( M_\odot \) star emits in 200 kyr.

The pre-ionization phase for such a star can be neglected for simplicity, as it will only affect a few cells.

5. RESULTS AND DISCUSSION

Figure 11 shows how the total star formation rate varies with time. The overall average is \( \sim 5 \ M_\odot \ \text{Myr}^{-1} \), but with a large amount of noise due to the stochasticity of star formation. The effective Type II SN rate (including only the SNe close enough to the center to have a significant impact on the system) is 0.05 SN Myr\(^{-1}\), or 1 SN/20 Myr. The effective Type Ia SN rate is set to be 1 SN/20 Myr based on Jimenez et al. (2014), such that after 100 Myr Type Ia SNe are as common as Type II.

5.1. Description of a Typical Simulation Run

In this section, we describe a sample simulation run, the results of which are shown in Figure 12. For the first 6 Myr, corresponding to the lifetime of the initial 25 \( M_\odot \) star, \( [\text{Fe/H}] \approx -4 \) everywhere in the gas. As discussed in Section 3, we do not allow low-mass stars to form at this metallicity. At \( t = 6 \) Myr, the 25 \( M_\odot \) star explodes and begins to enrich the gas. The first low-mass stars form at around 17 Myr and have a wide range of \( [\text{Fe/H}] \) from \(-3.8\) to \(-2\), while \( [\alpha/\text{Fe}] \) shows very little scatter and is \( \approx 0.85 \). This is higher than the expected long-term average \( [\alpha/\text{Fe}] \) from Type II SNe, because a 25 \( M_\odot \) star is more massive than 80% of Type II SN-forming stars and more massive stars have higher \( \alpha \) yields relative to iron. In this run, the first star with greater than 8 \( M_\odot \) forms at 32 Myr, which is slightly higher than the median time of 25 Myr. This star has a mass of 9.7 \( M_\odot \), corresponding to a lifetime of 29 Myr. At 38 Myr, a 9.0 \( M_\odot \) star forms, which will explode just after the gas has recovered from the previous SN, and this is followed by a 10 \( M_\odot \) star forming at 46 Myr. The combined effect of this is a period of low star formation from 60-100 Myr, although a few stars do form at a lower \( [\alpha/\text{Fe}] \) \( \sim 0.5 \) on the side opposite to the later SNe. Note that in Figure 12, these stars are at low \( [\text{Fe/H}] \), as the gas with higher \( [\text{Fe/H}] \) has not yet recovered from the multiple SNe that enriched it.

Between 100 and 200 Myr, enrichment from Type Ia SNe results in a decline in \( [\alpha/\text{Fe}] \) with increasing \( [\text{Fe/H}] \). A few stars form with \( [\alpha/\text{Fe}] < 0 \) in regions that are well away from the locations of all previous Type II SNe, but close to one or
more Type Ia SNe. By 200 Myr, stars with $[\text{Fe}/\text{H}] > -2$ are becoming common and the mean $[\text{Fe}/\text{H}]$ is $-2.9$, increasing to $-2.3$ at 400 Myr. We terminate star formation at 600 Myr, as it is likely that star formation will be switched off by closely spaced SNe or the epoch of reionization at some time before this. The simulation ends with 2950 $M_\odot$ of stars having formed, and there have been 29 Type II and 25 Type Ia SNe close enough to the center to significantly disrupt and enrich the gas.

The above description is an example only, and given that we assume star formation will occur stochastically, with variations in the number, mass, and location of stars, different runs of the simulation can give quite different results. The total star formation and therefore number of SNe over the 600 Myr does not vary much between runs, meaning that the stars in the clump at $[\text{Fe}/\text{H}] \sim -1.5$ are a typical feature, although they can have slightly higher or lower $[\alpha/\text{Fe}]$ due to variation in the relative number of Type Ia and Type II SNe. The mean $[\text{Fe}/\text{H}] = -2.10 \pm 0.09$ and the mean $[\alpha/\text{Fe}] = 0.28 \pm 0.03$. Note that these errors are simply the statistical errors based on a number of runs and do not take into account uncertainties in our star formation rate, IMF, and Type Ia SN frequency.

The large scatter in $[\alpha/\text{Fe}]$ at $[\text{Fe}/\text{H}] \approx -2.5$ is a result of stars forming in regions that have been affected by very few SNe. At lower $[\text{Fe}/\text{H}]$ there is little scatter because all stars have been affected by only a single SN, while at higher $[\text{Fe}/\text{H}]$ there have been enough SNe that significant variations from the mean are uncommon.

6. COMPARISON TO OBSERVED SYSTEMS

We now compare the results of our simulations to the UFDs discovered by Simon & Geha (2007) and Simon et al. (2011), which were studied in $[\alpha/\text{Fe}]$ by Vargas et al. (2013), as well as to the mass–metallicity relation (Kirby et al. 2013b). The Vargas UFDs have masses ranging from $6 \times 10^5 M_\odot$ to $1.2 \times 10^7 M_\odot$ within the half-light radius (Wolf et al. 2010). The total halo masses are uncertain, but may be significantly greater than this, such that the virial halo masses are likely to range from being similar to the $10^7 M_\odot$ in our model to being many times greater. In Figure 13, we plot the $[\text{Fe}/\text{H}]$ versus $[\alpha/\text{Fe}]$ data from the Vargas et al. (2013) study on the results of one of our simulation runs and determine whether our model can explain these systems. Vargas et al. (2013) note that the galaxies show evidence of old stellar populations without intermediate-age stars, indicative of a single burst of star formation lasting less than 2 Gyr.

Vargas et al. (2013) give abundance ratios for 61 red giant branch stars in 8 UFDs, the largest sample of alpha abundances in galaxies this faint. They found that six of the eight show on average reduced $[\alpha/\text{Fe}]$ at higher $[\text{Fe}/\text{H}]$, meaning that stars have likely formed for longer than 100 Myr. Figure 13 shows $[\alpha/\text{Fe}]$ versus $[\text{Fe}/\text{H}]$ for the complete Vargas sample, as well as Segue 2 from Kirby et al. (2013a) with our model prediction superimposed. In this section, we discuss whether our simulations can explain these systems. The definition of $[\alpha/\text{Fe}]$ for the observed values uses the same four elements

Figure 12. Plots of $[\alpha/\text{Fe}]$ vs. $[\text{Fe}/\text{H}]$ for stars after 100 (top), 200, 400, and 600 Myr. The dashed vertical lines in each panel are to the right of 90% of the points and can be considered a typical value of $[\text{Fe}/\text{H}]$ at which stars form at that time.
as used to define \( \alpha \) in our models, although our method has the effect of giving a greater weight to [Si/Fe] and [Mg/Fe], which are the more abundant elements, and a very low weight to [Ti/Fe]. Titanium is underproduced in the Woosley & Weaver (1995) nucleosynthetic models with respect to the solar values, while the Ca, Si, and Mg yields are consistent with the solar values and each other.

6.1. Systems Showing no Evidence of Type Ia Supernovae

Segue 1 (plotted in red in Figure 13) has a mass of \( 5.8^{+8.2}_{-3.1} \times 10^7 M_\odot \) within the half-light radius. Only five stars were observed by Simon et al. (2011), with four having \( [\alpha/Fe] \) between 0.6 and 0.9 and the other 0.4. Frebel et al. (2014) observed two more stars in Segue 1 with \( [\text{Fe/Fe}] \approx -3.5 \) and suggested that it was the least evolved known galaxy. The two stars with \( \text{[Fe/H]} \approx 0.5 \) are unusual, being two of only three stars in the Vargas sample at \( \text{[Fe/H]} \approx 2 \) with \( [\alpha/Fe] > 0.4 \). Our models show very few stars with \( \text{[Fe/H]} > -2 \) forming in the first 100 Myr of the evolution of the system.

Ursa Major II (dark blue in Figure 13), which has a half-light radius mass of \( 7.9^{+3.6}_{-3.1} \times 10^6 M_\odot \) (Wolf et al. 2010), also shows no evidence of a decline in \([\alpha/Fe]\). Given sufficient Type II SNe and the absence of Type Ia SNe, \([\alpha/Fe]\) will eventually settle around 0.35 (Frebel & Bromm 2012). The stars in Ursa Major II are clustered around \([\alpha/Fe] = 0.4\), with all but one of the stars having \([\text{Fe/H]} < -2.5\). The exception is a star with \([\text{Fe/H]} = -1.1\) and \([\alpha/Fe] = 0.4\); however, this may be a foreground star rather than a member of the system (Frebel et al. 2010).

Leo IV (yellow in Figure 13) has a half-light radius mass of \( 1.2^{+0.5}_{-0.9} \times 10^6 M_\odot \) (Wolf et al. 2010) and contains only four observed stars, all with large uncertainties in their abundance ratios. More stellar abundances are required to determine whether \([\alpha/Fe]\) decreases with increasing \([\text{Fe/H]}\) in this system. Leo IV has a luminosity of 8700 \( L_\odot \), suggesting a factor of 40 more star formation than in our models for a typical mass-to-light ratio and a Kroupa IMF (e.g., Martin et al. 2008) if it formed stars for \( <100 \) Myr. The system may be a closer match to our models if the period of star formation was longer. Brown et al. (2012) gives the constraint that the spread of stellar ages is less than 2 Gyr.

The stars from these three systems are plotted on an example run of our simulation after 100 Myr in the top panel of Figure 13. Segue 1, with its low luminosity and half-light radius mass, is the best fit to our models; however, two stars do not appear to fit with star formation times of \( <200 \) Myr. We note that there are large uncertainties associated with the star formation rate, the Type Ia SN rate, and the time of the first Type Ia SN. We therefore test increasing the star formation rate by a factor of two and evolving for 200 Myr without allowing Type Ia SNe. The results are shown in Figure 14. Increasing the undisturbed star formation rate has only a small effect on the total enrichment, because it leads to SNe occurring more quickly after the gas is used up, which leads to a period of low or no star formation. A larger halo mass would be required to maintain a higher average star formation rate. Frebel et al. (2014) calculated the initial stellar mass for Segue 1 to be \( \sim 1500 M_\odot \), which suggests a star formation rate a factor of two to three higher than for our models if the length of star formation was 100–150 Myr. However, this is not a large enough factor to explain the outliers at \([\text{Fe/H]} \approx -1.5\).

6.2. Systems Showing Evidence of Type Ia Supernovae

The remaining systems show evidence of Type Ia SNe, containing stars with solar or sub-solar \([\alpha/Fe]\). These galaxies have masses in the range \( 6 \times 10^7–1.2 \times 10^8 M_\odot \) within the half-light radius (Wolf et al. 2010). All show lower \([\alpha/Fe]\) for higher \([\text{Fe/H]}\), which is interpreted as the effect of Type Ia SNe, which yield much more iron relative to \( \alpha \) elements compared to Type II SNe. The decline in \([\alpha/Fe]\) may commence before the first Type Ia SNe due to Type II SNe from lower mass (8–15 \( M_\odot \))
stars. Averaged over a Kroupa IMF, the yield from Type II SNe \([\alpha/Fe] \approx 0.35\) is significantly lower than for many stars in the Vargas et al. (2013) sample.

In the Vargas et al. (2013) sample, nine stars are observed in Coma Berenices, of which seven show \([Fe/H] < -2.5\), with six of these clustering around \([\alpha/Fe] \approx 0.8\). The other two stars show \([Fe/H] < -2\) and \([\alpha/Fe] \approx 0.2\). This could be explained by a few high-mass stars affecting the system in the first 100 Myr, followed by a small number of Type Ia SNe, after which star formation quickly ends. The observed stars in Coma Berenices (darker green in 13) have a mean \([Fe/H] \approx -2.7\) and we therefore compare it to our 200 Myr plot in Figure 13, which has mean \([Fe/H] = -2.9\). The metallicity observations fit well, suggesting that Coma Berenices may have formed stars for \(\sim 200\) Myr. The luminosity of 3700 \(L_\odot\) suggests \(\sim 5-10\) times more star formation than for our model if this is the case. The mass within the half-light radius is \(2.0^{+0.9}_{-0.6} \times 10^6 M_\odot\) (Wolf et al. 2010) and it does not show evidence of tidal disruption (Muñoz et al. 2010).

Leo T is shown in the third panel of Figure 13. There are only five stars, four of them with \(-2.0 < [Fe/H] < -1.5\), consistent with a system that formed stars for \(\sim 400\) Myr. The star with \([Fe/H] = -1.8\) and \([\alpha/Fe] = 0.7\) is rare in our models and requires enrichment by multiple Type II SNe from high-mass stars without significant enrichment from Type Ia SNe. Leo T is the most luminous system in the Vargas sample and the only one that shows evidence of star formation at late times.

The rest of the Vargas systems are shown in the bottom panel of Figure 13 along with Segue 2 from Kirby et al. (2013a). All contain stars with \([Fe/H] > -1.5\) and some show stars with \([Fe/H] > -1.1\).

These systems have star formation histories of less than 2 Gyr (Vargas et al. 2013). Ursa Major I and Hercules, with their luminosities of >\(10^4 L_\odot\) and their half-light halo masses of \(\sim 10^7 M_\odot\), are likely significantly more massive than our modeled systems. Canes Venatici II, with a half-light radius mass of \(1.4^{+1.0}_{-0.6} \times 10^6 M_\odot\) and a luminosity of \(7.9^{+4.4}_{-3.4} \times 10^3 L_\odot\) (Wolf et al. 2010), is a closer fit, although the implied \(>10^4 M_\odot\) of stars is still more than in our model.

The remaining systems do not contain stars with \([Fe/H] < -3\), but other features match well with our model, with nearly all observed stars lying close to regions with a high density of modeled stars. The low-metallicity stars in Hercules do not fall on the clump of modeled stars, but can be explained by the effects of one or more early Type II SNe from lower mass stars, which would have the effect of reducing \([\alpha/Fe]\). The large scatter in \([\alpha/Fe]\) near \([Fe/H] = -2.5\) in the model is seen in Ursa Major I and Canes Venatici II, although not in Hercules or Segue 2. In our simulation, the scatter results from the range of \(\alpha\) enrichment from different-mass Type II SNe, as well as the commencement of Type Ia SNe.

Within each galaxy there is much less scatter in \([\alpha/Fe]\) than in \([Fe/H]\), especially at low \([Fe/H]\), which is expected for the reasons outlined in Frebel & Bromm (2012). Ursa Major I contains a star at \([Fe/H] = -2.6\) with approximately solar \([\alpha/Fe]\), which could be indicative of a low star formation rate resulting in lower enrichment for the first 100 Myr, but could also be explained simply by a case where fewer SNe occur in the first 100 Myr due to the stochastic nature of stellar masses.

Segue 2 is the least massive known galaxy, with \(<1.5 \times 10^5 M_\odot\) within the half-light radius, a luminosity of \(900 L_\odot\), and a stellar mass of \(1000 M_\odot\). This is much less massive than our modeled systems. Belokurov et al. (2009) give a total halo mass of \(5.5 \times 10^5 M_\odot\), but they noted that this is highly model-dependent and the true mass could be higher.

Kirby et al. (2013a) discuss two possibilities, the first being that the galaxy formed at a mass similar to the observed mass, and the second being that the system formed with a mass \(\sim 10^6 M_\odot\), but that 99.7% of the stars have been stripped. The second scenario requires a highly eccentric orbit (50:1; Peñarrubia et al. 2008). This would be a highly unusual object, and Kirby et al. (2013a) note that it would be the first known galaxy to have lost its dark matter halo without being completely disrupted. While Segue 2 is the only significant outlier from the stellar mass—metallicity relation (Kirby et al. 2013b), which supports the tidal stripping scenario, Chen et al. (2014) suggest that the stellar mass—metallicity relation becomes flat or even changes direction below \(M_{\text{vir}} = 10^7 M_\odot\), because lower mass halos are less efficient in accreting metal-poor gas. The current observational data cannot distinguish between the possible origins of Segue 2.

The observed stars from Segue 2 are plotted in orange on the bottom panel in Figure 13. Six of the eight stars show \([\alpha/Fe] > 0.3\) and \([Fe/H] < -2.2\). One of the remaining stars is at \([Fe/H] = -1.9\) and solar \([\alpha/Fe]\), while the other is at \([Fe/H] = -1.3\) and sub-solar \([\alpha/Fe]\).

We also tested a scenario without enrichment from Type II SNe, where the Type Ia SN rate was increased such that the total SN rate remained the same. The implicit assumption made here is that intermediate-mass (3–8 \(M_\odot\)) stars can form at our starting metallicity of \([Fe/H] = -4\). The results are shown in Figure 15 and show that the decline in \([\alpha/Fe]\) is too rapid to explain UFD observations. Within 200 Myr, most stars formed in our simulation have lower \([\alpha/Fe]\) than any observed stars. We therefore conclude that enrichment from Type II SNe is required to explain the metallicity of stars in the UFDs observed to date. However, given the results of Paper I, a \(10^{-5} M_\odot\) galaxy would likely survive a single Type Ia SN, which does not have the pre-ionization phase associated with Type II SNe. The star formation rate of M65 in its undisturbed state is \(5.7 M_\odot\) Myr\(^{-1}\), which corresponds to an average of 10 stars per Myr. In the Kroupa IMF, 1 in 270 stars is greater than 8 solar masses, so the average SN rate if the gas is not disturbed is 1 per 27 Myr; however, the stochastic nature of star formation means that

![Figure 14. Observations of Segue 1 from Vargas et al. (2013, red points) compared to a 200 Myr run of our model where star formation is doubled and Type Ia supernovae are not allowed.](image-url)
in 15% of cases no stars with greater than 8 $M_\odot$ will form within 50 Myr and in 2% of cases none will form within the first 100 Myr. Such systems could therefore experience one or more prompt Type Ia SNe (Mannucci et al. 2006) before any Type II SNe.

Only a few hundred stars would form in such a system, and they may be beyond the reach of current telescopes. Future detections of stars in such systems are likely to show very low [$\alpha$/Fe] relative to [Fe/H] because the surviving systems will be those that lacked the $\alpha$-enriching massive stars. Systems that form with a high enough metallicity for immediate low-mass star formation may show a few very low [Fe/H] stars with high [$\alpha$/Fe]. Such stars would form in gas enriched only by Population III stars.

6.3. Scaling Relations

Dwarf galaxies observed to date obey a tight relationship between stellar mass and metallicity,

$$[\text{Fe}/\text{H}] = -1.69 + 0.30 \log \left( \frac{M_\star}{10^5 M_\odot} \right). \quad (7)$$

with an rms of 0.16 (Kirby et al. 2013b).

After 400 Myr in our model, the stellar mass is $\approx 2000 M_\odot$ and [Fe/H] $= -2.3 \pm 0.1$. Assuming that due to stellar evolution the stellar mass observed today would be half of its original value (as calculated for Segue 1 by Frebel et al. 2014), the mass–metallicity relation gives [Fe/H] $= -2.59 \pm 0.16$. The discrepancy is larger at 600 Myr, where [Fe/H] $= -2.1 \pm 0.1$ for our model, compared to [Fe/H] $= -2.54 \pm 0.16$ from the mass–metallicity relation.

However, our models do fit well with the simulations of Chen et al. (2014), who suggest that there is a change of slope in a number of scaling relations at $M_{\text{vir}} \sim 10^8 M_\odot$ resulting from the inefficiency of low-mass halos in accreting metal-poor gas.

The mean stellar metallicity of $-2.1$ at 600 Myr in our model is slightly lower than they find for a $M_{\text{vir}} = 10^7 M_\odot$ halo, although it is still within their range of uncertainty. They find that the total stellar mass is equal to

$$\log M_\star = 3.5 + 1.3 \log (M_{\text{vir}}/10^7 M_\odot). \quad (8)$$

This gives $M_\star = 3200 M_\odot$, which is similar to the stellar mass of $3000 M_\odot$ from our models.

7. SUMMARY

We have simulated star formation and chemical enrichment in systems with dark matter halo masses of $10^7 M_\odot$, which is a mass similar to many of the recently discovered UFDs. We use the single SN simulations of Paper I as a starting point and evolve the system for 600 Myr. Using a simple model of star formation, we find the following.

1. A single star with a mass of $25 M_\odot$ is sufficient to permanently stop star formation in a system with a mass of $10^{6.5} M_\odot$, even if the star is as much as 0.5 scale radii (50 pc) from the center.
2. In systems with $10^7 M_\odot$, massive stars farther than 0.5 scale radii (75 pc) from the center have little impact on the system as most of the energy and metals escape.
3. Systems with $10^7 M_\odot$ recover from the first SN explosion and form low-mass stars for more than 100 Myr.
4. The assumption that star formation occurs at the same rate as in the Carina dwarf (scaled for the size of our modeled systems) predicts a turnover of [$\alpha$/Fe] at [Fe/H] $\sim -2.5$.
5. Our models predict $> 1$ dex of scatter in [$\alpha$/Fe] close to the turnover, but that away from this value of [Fe/H] the scatter should be $< 0.5$ dex.
6. In terms of stellar and halo mass, Segue 1 is the closest observed match to our modeled systems. The stellar mass of
~1500 $M_\odot$ calculated by Frebel et al. (2014), along with the lack of evidence of enrichment from Type Ia SNe, suggests a star formation rate a factor of three to four times higher than for our models, while the halo mass estimate from Simon et al. (2011) suggests the system is ~3 times more massive than our M70 model. With better instruments, we expect the detection of many systems similar to Segue 1, which is currently the least luminous known galaxy. This paper provides support to the suggestion of Bovill & Ricotti (2009) that at least some such systems are fossil galaxies that formed in the early universe with halo masses $<10^5 M_\odot$, then experienced only a single burst of star formation.

7. We find that systems with $M_{\text{vir}} = 10^{6.5} M_\odot$ and lower cannot survive the feedback from their star formation. This suggests that if Segue 2 has a virial mass of $<10^6 M_\odot$ as suggested by Kirby et al. (2013a), it could not have formed with its present halo mass, but rather must have experienced at least some tidal stripping. However, if its true virial mass is $\gtrsim 10^6 M_\odot$, it is consistent with the stellar mass–metallicity relation of Chen et al. (2014) and may therefore be an intrinsically very low-mass system.

8. All observed stars in the rest of the Vargas UFDs have metallicities that are consistent with our model, although our model predicts stars with lower metallicities than have been observed. This discrepancy may result from the starting metallicity of $[\text{Fe/H}] = -4$, or the metallicity floor for low-mass star formation.

We have assumed our systems are formed and evolve in isolation and have not addressed the complex issues of accretion, ram pressure stripping, dark matter halo stripping, and other effects that may affect the evolution of the galaxy. While our modeled systems are in isolation, the UFDs compared to in this work have been affected by the M31 and Milky Way effects that may affect the evolution of the galaxy. While our work provides support to the suggestion of Bovill & Ricotti (2011) suggests the system is currently the least luminous known galaxy. This paper provides support to the suggestion of Bovill & Ricotti (2009) that at least some such systems are fossil galaxies that formed in the early universe with halo masses $<10^5 M_\odot$, then experienced only a single burst of star formation.

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~1500 $M_\odot$ calculated by Frebel et al. (2014), along with the lack of evidence of enrichment from Type Ia SNe, suggests a star formation rate a factor of three to four times higher than for our models, while the halo mass estimate from Simon et al. (2011) suggests the system is ~3 times more massive than our M70 model. With better instruments, we expect the detection of many systems similar to Segue 1, which is currently the least luminous known galaxy. This paper provides support to the suggestion of Bovill & Ricotti (2009) that at least some such systems are fossil galaxies that formed in the early universe with halo masses $<10^5 M_\odot$, then experienced only a single burst of star formation.

7. We find that systems with $M_{\text{vir}} = 10^{6.5} M_\odot$ and lower cannot survive the feedback from their star formation. This suggests that if Segue 2 has a virial mass of $<10^6 M_\odot$ as suggested by Kirby et al. (2013a), it could not have formed with its present halo mass, but rather must have experienced at least some tidal stripping. However, if its true virial mass is $\gtrsim 10^6 M_\odot$, it is consistent with the stellar mass–metallicity relation of Chen et al. (2014) and may therefore be an intrinsically very low-mass system.

8. All observed stars in the rest of the Vargas UFDs have metallicities that are consistent with our model, although our model predicts stars with lower metallicities than have been observed. This discrepancy may result from the starting metallicity of $[\text{Fe/H}] = -4$, or the metallicity floor for low-mass star formation.

We have assumed our systems are formed and evolve in isolation and have not addressed the complex issues of accretion, ram pressure stripping, dark matter halo stripping, and other effects that may affect the evolution of the galaxy. While our modeled systems are in isolation, the UFDs compared to in this work have been affected by the M31 and Milky Way effects that may affect the evolution of the galaxy. While our work provides support to the suggestion of Bovill & Ricotti (2011) suggests the system is currently the least luminous known galaxy. This paper provides support to the suggestion of Bovill & Ricotti (2009) that at least some such systems are fossil galaxies that formed in the early universe with halo masses $<10^5 M_\odot$, then experienced only a single burst of star formation.

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