Quality and size assessment of quantized images using K-Means++ clustering

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ABSTRACT
In this paper, an amended K-Means algorithm called K-Means++ is implemented for color quantization. K-Means++ is an improvement to the K-Means algorithm in order to surmount the random selection of the initial centroids. The main advantage of K-Means++ is the centroids chosen are distributed over the data such that it reduces the sum of squared errors (SSE). K-Means++ algorithm is used to analyze the color distribution of an image and create the color palette for transforming to a better quantized image compared to the standard K-Means algorithm. The tests were conducted on several popular true color images with different numbers of K value: 32, 64, 128, and 256. The results show that K-Means++ clustering algorithm yields higher PSNR values and lower file size compared to K-Means algorithm; 2.58% and 1.05%. It is envisaged that this clustering algorithm will benefit in many applications such as document clustering, market segmentation, image compression and image segmentation because it produces accurate and stable results.

Keywords:
Color quantization
Image compression
K-Means++
Machine learning
True color image

1. INTRODUCTION
The development of information and communication technologies favors an increasing need for image and video data, which require large storage space and high transmission bandwidth. Image processing technology has undergone significant growth. Therefore, to save up existing storage devices and transmission channels, methods which are able to compress data are widely investigated [1, 2]. A true-color image consists of 24-bit of storage, where 8 bits for red, 8 for green, and 8 for blue [3]. This kind of image has a big number of pixel data which can represent up to 16,777,216 colors and makes its display, processing, transmission, and storage problematic. As a result, color quantization is used to solve for many image processing and graphics problems. In the past, color quantization was needed due to the limitations of graphics capabilities of display hardware. Color quantization still maintains its practical value even though 24-bit display hardware has become common [4-6].

Color quantization is a preprocessing technique that is used to reduce the number of colors in images such that the reconstructed image should be visually close to the original image. It is able to eliminate unnecessary information from images. For instance, unnecessary color information in topographic maps needs to be eliminated so as to accurately construct digital evaluation model (DEM). Color quantization plays a critical role in many other digital applications such as segmentation,
color texture analysis, content-based retrieval, watermarking, text detection, and non-photorealistic rendering, and. In general, this technique is done by performing two steps. The first is to select the palette design from the colors in the original image. The second step is pixel-mapping, it is done by changing each color with the color in the palette. Color quantization is an implementation of lossy image compression [7-10]. Figure 1 shows the representation between a 24-bits original image and 64 colors of quantized image.

Currently, there are two algorithms for palette design, clustering-based and splitting-based. Some well-known splitting algorithms are the median-cut [11], center-cut [12], Octree [13], variance-based [14], RWM-cut [15], and binary splitting [16]. The splitting-based algorithms generally split the color space of the color image into two disjoint groups according to their splitting criteria. Then, the splitting is iterated until the wanted number of groups is achieved. Finally, the cluster center of each group is chosen as the palette color [17]. Clustering-based algorithms include Hierarchical Clustering, K-Means, and K-Medoids [18]. The performance of clustering-algorithm-based techniques varies greatly depending on how the K representative colors are chosen. These techniques have to make a tradeoff between their computational efficiency and minimization of the distortion measure. For example, the standard K-Means algorithm can minimize the quantization error efficiently if enough number of iterations are allowed [19, 20]. K-Means clustering algorithm [21] was originally proposed for pattern recognition. It is commonly recognized as a sub-optimal quantization technique that can also be applied to color vision, image segmentation, and vector quantization. For image vector quantization, the generalized Lloyd algorithm, also called the LBG algorithm, is identical to the standard K-means algorithm [22].

K-Means++ was proposed by David Arthur and Sergei Vassilvitski in 2007. It is an improvement to the standard K-Means in order to surmount the random selection of the initial cluster centers. This algorithm uses the squared distance weighting method to select the next center. This algorithm also reduces the fluctuation happening in K-Means and provide better and stable clustering results [23]. Authors in [24] found that the K-Means++ algorithm has proved to be more accurate than the standard K-Means in crime document clustering. Therefore, we investigate the PSNR and file size of quantized images using K-Means++ compared to the standard K-Means.

The rest of the paper is organized as follows; Section 2 describes the research method, including the K-means++ algorithm, and PSNR as the quality assessment method. Section 3 presents the results and analysis. Finally, Section 4 explains the conclusions and future work.

2. RESEARCH METHOD

In this experiment, the image is converted to a collection of RGB color values as X. Identify the number of clusters (K value) that is desired to represent the image. The numbers of clusters proposed are 32, 64, 128, and 256. The number of clusters must be less than the actual number of colors that exist in

Figure 1. The different representation between, (a) An original image in 24-bits RGB color, (b) Quantized image is reduced to a palette of 64 colors

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the image. The next step is to choose K colors to represent the original image. The chosen colors would act as the centroids to classify all the colors in the original image. Then proceed the following K-Means++ Clustering algorithm [25]:

- Select a center \( c_1 \), which is chosen uniformly at random from \( X \).
- Select a new center \( c_p \) by choosing \( x \in X \) with probability \( \frac{D(x)^2}{\sum_{x \in X} D(x)^2} \).

\( D(x) \) denotes the shortest distance from a data point to the closest center we have already chosen.

\[
D(x) = (x_1 - c_{11})^2 + (x_1 - c_{12})^2 + \ldots + (x_1 - c_{ir})^2
\]

Repeat Step 2, \( k \) centers have been taken altogether.

For each \( i \in \{1,...,k\} \), set the cluster \( C_i \) to be the set of points in \( X \) that are closer to \( c_i \) than they are to \( c_j \) for all \( j \neq i \).

For each \( i \in \{1,...,k\} \), set \( c_i \) to be the center of mass of all points in \( C_i \): \( c_i = \frac{1}{|C_i|} \sum_{x \in C_i} x \).

Repeat Step 4 and 5, until \( C \) no longer changes.

After the algorithm is done, each color is looped through and replaced with the center color that has the closest distance to it. This step is known as color remapping in color quantization. Then, the remapping process would reproduce an image that is visually similar to the original image, but only with \( K \) colors exist in it.

Color quantization algorithms efficiency is measured by PSNR (Peak-to-Signal Noise Ratio), where a higher PSNR means the quantized image is closer to the original visually [26].

\[
PSNR = 10 \log_{10} \left( \frac{M^2}{MSE} \right)
\]

where \( M \) is the original image’s maximum value. The typical value of PSNR for lossy compressed images are between 30-50 dB [27]. MSE measures the distortion or deviation between the original image and its reconstructed image (quantized image) [28].

\[
MSE = \frac{1}{MN} \sum_{x=1}^{M} \sum_{y=1}^{N} (S_{xy} - C_{xy})^2
\]

3. RESULTS AND DISCUSSION

To evaluate the PSNR value and file size of K-Means++ clustering algorithm, 4 (four) popular images from USC-SIPI University Image Database (http://sipi.usc.edu/database/); “Baboon”, “Fruits”, “Lena”, and “Pepper” are used. The images are 512x512 pixels sized. The original image file sizes are as follows 624 KB, 464 KB, 464 KB, and 528 KB. Figure 2 shows the tested images.

![Figure 2. The test images. (a) Baboon, (b) Fruits, (c) Lena, (d) Peppers](image)

Experiments are implemented using Java programming language on an i7 7700HQ 2.8GHz processor, 8GB RAM, and NVIDIA GeForce GTX 1050Ti 4GB VGA. K-Means++ is compared to the standard K-Means clustering algorithm. The tests were done 3 times for each ‘K’ value. Table 1 depicts...
the average PSNR values and file sizes of the tested images. Figure 3 shows the quantization results of “Fruits”. Figure 4 shows the comparison between K value and PSNR, while Figure 5 shows the comparison between K value and file size.

| No. | Image | Number of colors | Size (KB) | K   | K-Means++ | K-Means+ | PSNR (dB) | Size (KB) | PSNR (dB) | Size (KB) |
|-----|-------|------------------|-----------|-----|-----------|----------|-----------|-----------|-----------|-----------|
| 1   | Baboon| 230427           | 622       | 32  | 27.07     | 129      | 26.31     | 130.67    | 27.07     | 129.67    |
|     |       |                  |           | 64  | 28.95     | 169.67   | 28.39     | 170       | 28.95     | 169.67   |
|     |       |                  |           | 128 | 30.89     | 215      | 29.93     | 218       | 30.89     | 215      |
|     |       |                  |           | 256 | 32.67     | 273.33   | 30.80     | 275.33    | 32.67     | 273.33   |
| 2   | Fruits| 49451            | 461       | 32  | 30.25     | 61.67    | 29.90     | 62        | 30.25     | 61.67    |
|     |       |                  |           | 64  | 32.85     | 82       | 32.53     | 83.33     | 32.85     | 82       |
|     |       |                  |           | 128 | 35.25     | 110.33   | 34.14     | 110.67    | 35.25     | 110.33   |
|     |       |                  |           | 256 | 37.06     | 137.67   | 36.86     | 138.67    | 37.06     | 137.67   |
| 3   | Lena  | 148279           | 462       | 32  | 30.82     | 93.67    | 31.00     | 95        | 30.82     | 93.67    |
|     |       |                  |           | 64  | 33.81     | 129.67   | 32.26     | 130       | 33.81     | 129.67   |
|     |       |                  |           | 128 | 34.88     | 161      | 32.68     | 163.33    | 34.88     | 161      |
|     |       |                  |           | 256 | 35.08     | 175.67   | 35.05     | 176       | 35.08     | 175.67   |
| 4   | Peppers| 183525           | 526       | 32  | 28.56     | 82.67    | 28.15     | 84        | 28.56     | 82.67    |
|     |       |                  |           | 64  | 30.95     | 117.67   | 30.06     | 120       | 30.95     | 117.67   |
|     |       |                  |           | 128 | 33.40     | 159.33   | 32.34     | 163.33    | 33.40     | 159.33   |
|     |       |                  |           | 256 | 34.90     | 207      | 34.87     | 208.67    | 34.90     | 207      |

Figure 3. Quantized images of “Fruits”, (a) K=32, (b) K=64, (c) K=128, (d) K=256

Figure 4. The comparison between K value and PSNR

Figure 5. The comparison between K value and file size

Based on the results depicted in Table 1, the quantized images altogether have the average PSNR more than 30 dB on K value of 128 and 256. The smallest average file size produced is 61.67 KB on Fruits image with K value of 32 and the biggest is 273.33 KB on Baboon image with K value of 256. The average file sizes have a scale of 2 to 7 times smaller than the original size. The PSNR and file sizes of K-Means++
clustering are better than K-means clustering with PSNR and file size percentage decreases for 32, 64, 128, and 256 clusters are 2.19% and 1.2%, 2.59% and 1%, 3.93% and 1.39%, 1.61% and 0.61%. The standard K-Means algorithm initializes the cluster centers uniformly at random, whereas K-Means++ tends to initialize near the center of the squares. Therefore, the results given by the standard K-Means are different in every run. In this case, the colors chosen as the centers could have adjacent RGB values. So, the PSNR and file sizes obtained by the standard K-Means are worse than the K-Means++. Based on Figure 4 and 5, more clusters (K) produce a better PSNR and file size, while the file sizes are still much lower than the original size. If the number of clusters gets bigger, then the mass of pixels that have similarities with the cluster centers produce quantized image that is closer to the original.

4. CONCLUSION
By using K-Means++ algorithm, the quantized images altogether have the average PSNR more than 30 dB on K value of 128 and 256. The average file sizes have a scale of 2 to 7 times smaller compared to the original size. The PSNR and file size increase as the K value gets bigger. In addition, the average PSNR and file size produced of each quantized image achieves better results compared to the original K-Means algorithm; 2.58% and 1.05%. K-Means++ algorithm has been proved to be better and more accurate that K-Means, in color quantization. The reason is because the fact that K-Means algorithm initializes the cluster centers uniformly at random, whereas K-Means++ tends to initialize near the center of the squares. Based on the research conducted, different distance metrics can be used to make a representation of the images so that it can be compared in terms of weighting. It is also recommended that the extension of this work can be done for images with bigger resolutions.

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