Verification of Query Completeness over Processes
[Extended Version]

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Abstract. Data completeness is an essential aspect of data quality, and has in turn a huge impact on the effective management of companies. For example, statistics are computed and audits are conducted in companies by implicitly placing the strong assumption that the analysed data are complete. In this work, we are interested in studying the problem of completeness of data produced by business processes, to the aim of automatically assessing whether a given database query can be answered with complete information in a certain state of the process. We formalize so-called quality-aware processes that create data in the real world and store it in the company’s information system possibly at a later point. We then show how one can check the completeness of database queries in a certain state of the process or after the execution of a sequence of actions, by leveraging on query containment, a well-studied problem in database theory.

1 Introduction

Data completeness is an important aspect of data quality. When data is used in decision-making, it is important that the data is of good quality, and in particular that it is complete. This is particularly true in an enterprise setting. On the one hand, strategic decisions are taken inside a company by relying on statistics and business indicators such as KPIs. Obviously, this information is useful only if it is reliable, and reliability, in turn, is strictly related to quality and, more specifically, to completeness.

Consider for example the school information system of the autonomous province of Bolzano in Italy, which triggered the research included in this paper. Such an information system stores data about schools, enrolments, students and teachers. When statistics are computed for the enrolments in a given school, e.g., to decide the amount of teachers needed for the following academic year, it is of utmost importance that the involved data are complete, i.e., that the required information stored in the information system is aligned with reality.

Completeness of data is a key issue also in the context of auditing. When a company is evaluated to check whether its way of conducting business is in accordance to the law and to audit assurance standards, part of the external audit is dedicated to the analysis
of the actual data. If such data are incomplete w.r.t. the queries issued during the audit, then the obtained answers do not properly reflect the company’s behaviour.

There has been plenty of work on fixing data quality issues, especially for fixing incorrect data and for detecting duplicates \cite{10,6}. However, some data quality issues cannot be automatically fixed. This holds in particular for incomplete data, as missing data cannot be corrected inside a system, unless additional activities are introduced to acquire them. In all these situations, it is then a mandatory requirement to (at least) detect data quality issues, enabling informed decisions drawn with knowledge about which data are complete and which not.

The key question therefore is how it is possible to obtain this completeness information. There has been previous work on the assessment of data completeness \cite{12}, however this approach left the question where completeness information come from largely open. In this work, we argue that, in the common situation where the manipulation of data inside the information system is driven by business processes, we can leverage on such processes to infer information about data completeness, provided that we suitably annotate the involved activities with explicit information about the way they manipulate data.

A common source of data incompleteness in business processes is constituted by delays between real-world events and their recording in an information system. This holds in particular for scenarios where processes are carried out partially without support of the information system. E.g., many legal events are considered valid as soon as they are signed on a sheet of paper, but their recording in the information system could happen much later in time. Consider again the example of the school information system, in particular the enrolment of pupils in schools. Parents enroll their children at the individual schools, and the enrolment is valid as soon as both the parents and the school director sign the enrolment form. However, the school secretary may record the information from the sheets only later in the local database of the school, and even later submit all the enrolment information to the central school administration, which needs it to plan the assignment of teachers to schools, and other management tasks.

In the BPM context, there have been attempts to model data quality issues, like in \cite{7,13,2}. However, these approaches mainly discussed general methodologies for modeling data quality requirements in BPMN, but did not provide methods to assess their fulfilment. In this paper, we claim that process formalizations are an essential source for learning about data completeness and show how data completeness can be verified. In particular, our contributions are (1) to introduce the idea of extracting information about data completeness from processes manipulating the data, (2) to formalize processes that can both interact with the real-world and record information about the real-world in an information system, and (3) to show how completeness can be verified over such processes, both at design and at execution time.

Our approach leverages on two assumptions related to how the data manipulation and the process control-flow are captured. From the data point of view, we leverage on annotations that suitably mediate between expressiveness and tractability. More specifically, we rely on annotations modeling that new information of a given type is acquired in the real world, or that some information present in the real world is stored into the information system. We do not explicitly consider the evolution of specific values for
the data, as incorporating full-fledged data without any restriction would immediately make our problem undecidable, being simple reachability queries undecidable in such a rich setting [9,14]. From the control-flow point of view, we are completely orthogonal to process specification languages. In particular, we design our data completeness algorithms over (labeled) transition systems, a well-established mathematical structure to represent the execution traces that can by produced according to the control-flow dependencies of the (business) process model of interest. Consequently, our approach can in principle be applied to any process modeling language, with the proviso of annotating the involved activities. We are in particular interested in providing automated reasoning facilities to answer whether a given query can be answered with complete information given a target state or a sequence of activities.

The rest of this paper is divided as follows. In Section 2, we discuss the scenario of the school enrolment data in the province of Bozen/Bolzano in detail. In Section 3, we discuss our formal approach, introducing quality-aware transition systems, process activity annotations used to capture the semantics of activities that interact with the real world and with an information system, and properties of query completeness over such systems. In Section 4, we discuss how query completeness can be verified over such systems at design time and at runtime, how query completeness can be refined and what the complexity of deciding query completeness is.

2 Example Scenario

Consider the example of the enrollment to schools in the province of Bolzano. Parents can submit enrollment requests for their child to any school they want until the 1st of March. Schools then decide which pupils to accept, and parents have to choose one of the schools in which their child is accepted. Since in May the school administration wants to start planning the allocation of teachers to schools and take further decisions (such as the opening and closing of school branches and schools) they require the schools to process the enrollments and to enter them in the central school information system before the 15th of April.

A particular feature of this process is that it is partly carried out with pen and paper, and partly in front of a computer, interacting with an underlying school information system. Consequently, the information system does not often contain all the information that hold in the real world, and is therefore incomplete. E.g., while an enrollment is legally already valid when the enrollment sheet is signed, this information is visible in the information system only when the secretary enters it into a computerised form.

A BPMN diagram sketching the main phases of this process is shown in Fig. 1, while a simple UML diagram of (a fragment of) the school domain is reported in Fig. 2. These diagrams abstractly summarise the school domain from the point of view of the central administration. Concretely, each school implements a specific, local version of the enrolment process, relying on its own domain conceptual model. The data collected on a per-school basis are then transferred into a central information system managed by the central administration, which refines the conceptual model of Fig. 2. In the following, we will assume that such an information system represents information about children and the class they belong to by means of a pupil\((pname, class, sname)\) rela-
Parents can submit enrolment applications, which are then decided upon by the School Administration. Once accepted, enrolments are recorded and the School information system generates statistics and assigns resources. Fig. 1. BPMN diagram of the main phases of the school enrollment process.

Fig. 2. UML diagram capturing a fragment of the school domain.

When using the statistics about the enrollments as compiled in the beginning of May, the school administration is highly interested in having correct statistical information, which in turn requires that the underlying data about the enrollments must be complete. Since the data is generated during the enrollment process, this gives rise to several questions about such a process. The first question is whether the process is generally designed correctly, that is, whether the enrollments present in the information system are really complete at the time they publish their statistics, or whether it is still possible to submit valid enrollments by the time the statistics are published. We call this problem the design-time verification.

A second question is to find whether the number of enrollments in a certain school branch is already complete before the 15th of April, that is, when the schools are still allowed to submit enrolments (i.e., when there are school that still have not completed the second activity in the school lane of Fig. 1), which could be the case when some schools submitted all their enrollments but others did not. In specific cases the number can be complete already, when the schools that submitted their data are all the schools that offer the branch. We call this problem the run-time verification.

A third question is to learn on a finer-grained level about the completeness of statistics, when they are not generally complete. When a statistic consists not of a single number but of a set of values (e.g. enrollments per school), it is interesting to know for which schools the number is already complete. We call this the dimension analysis.
3 Formalization

We want to formalize processes such as the one in Fig. [1] which operate both over data in the real-world (pen&paper) and record information about the real world in an information system. We therefore first introduce real-world databases and information system databases, and show then how transition systems, which represent possible process executions, can be annotated with effects for interacting with the real-world or the information system database.

3.1 Real-world Databases and Information System Databases

We assume an ordered, dense set of constants $dom$ and a fixed set $\Sigma$ of relations. A database instance is a finite set of facts in $\Sigma$ over $dom$. As there exists both the real world and the information system, in the following we model this with two databases: $D^{rw}$ called the real-world database, which describes the information that holds in the real world, and $D^{is}$, called the information system database, which captures the information that is stored in the information system. We assume that the stored information is always a subset of the real-world information. Thus, processes actually operate over pairs $(D^{rw}, D^{is})$ of real-world database and information system database. In the following, we will focus on processes that create data in the real world and copy parts of the data into the information system, possibly delayed.

Example 1. Consider that in the real world, there are the two pupils John and Mary enrolled in the classes 2 and 4 at the Hofer School, while the school has so far only processed the enrollment of John in their IT system. Additionally it holds in the real world that John and Alice live in Bolzano and Bob lives in the city of Merano. The real-world database $D^{rw}$ would then be $\{pupil(John, 2, HoferSchool), pupil(Mary, 4, HoferSchool), livesIn(John, Bolzano), livesIn(Bob, Merano), livesIn(Alice, Bolzano)\}$ while the information system database would be $\{pupil(John, 2, HoferSchool)\}$.

Where it is not clear from the context, we annotate atoms with the database they belong to, so, e.g., $pupil^{is}(John, 4, HoferSchool)$ means that this fact is stored in the information system database.

3.2 Query Completeness

For planning purposes, the school administration is interested in figures such as the number of pupils per class, school, profile, etc. Such figures can be extracted from relational databases via SQL queries using the COUNT keyword. In an SQL database with a table $pupil(name, class, school)$, a query asking for the number of students per school would be written as:

\[
\begin{align*}
\text{SELECT} & \text{ school, COUNT(*) as pupils_nr} \\
\text{FROM} & \text{ pupil} \\
\text{GROUP BY} & \text{ school.}
\end{align*}
\]

In database theory, conjunctive queries were introduced to formalize SQL queries. A conjunctive query $Q$ is an expression of the form $Q(\bar{x}) :\neg A_1, \ldots, \neg A_n, M$, where $\bar{x}$ are
called the distinguished variables in the head of the query. \( A_1 \) to \( A_n \) the atoms in the body of the query, and \( M \) is a set of built-in comparisons \( \Pi \). We denote the set of all variables that appear in a query \( Q \) by \( \text{Var}(Q) \). Common subclasses of conjunctive queries are linear conjunctive queries, that is, they do not contain a relational symbol twice, and relational conjunctive queries, that is, queries that do not use comparison predicates. Conjunctive queries allow to formalize all single-block SQL queries, i.e., queries of the form “SELECT \ldots FROM \ldots WHERE \ldots”. As a conjunctive query, the SQL query \( \Pi \) above would be written as:

\[
Q_{\text{pupil}}(\text{schoolname}, \text{count(name)}):= \text{pupil(name, class, schoolname)}
\]

(2)

In the following, we assume that all queries are conjunctive queries. We now formalize query completeness over a pair of a real-world database and an information system database. Intuitively, if query completeness can be guaranteed, then this means that the query over the generally incomplete information system database gives the same answer as it would give w.r.t. the information that holds in the real world. Query completeness is the key property that we are interested in verifying.

A pair of databases \( (D^w, D^s) \) satisfies query completeness of a query \( Q \), if \( Q(D^w) = Q(D^s) \) holds. We then write \( (D^w, D^s) \models \text{Compl}(Q) \).

Example 2. Consider the pair of databases \( (D^w, D^s) \) from Example 1 and the query \( Q_{\text{pupil}} \) from above (2). Then, \( \text{Compl}(Q_{\text{pupil}}) \) does not hold over \( (D^w, D^s) \) because \( Q(D^w) = \{(\text{HoferSchool}, 2)\} \) but \( Q(D^s) = \{(\text{HoferSchool}, 1)\} \). A query for pupils in class 2 only, \( Q_{\text{class2}}(n):= \text{pupil}(n, 2, s) \), would be complete, because \( Q(D^w) = Q(D^s) = \{\text{John}\} \).

3.3 Real-world Effects and Copy Effects

We want to formalize the real-world effect of an enrollment action at the Hofer School, where in principle, every pupil that has submitted an enrolment request before, is allowed to enroll in the real world. We can formalize this using the following implication: \( \text{pupil}^w(n, c, \text{HoferSchool}) \iff \text{request}^w(n, \text{HoferSchool}) \), which should mean that whenever someone is a pupil at the Hofer school now, he has submitted an enrolment request before. Also, we want to formalize copy effects, for example where all pupils in classes greater than 3 are stored in the database. This can be written with the following implication: \( \text{pupil}^w(n, c, s), c > 3 \rightarrow \text{pupil}^s(n, c, s) \), which means that whenever someone is a pupil in a class with level greater than three in the real world, then this fact is also stored in the information system.

For annotating processes with information about data creation and manipulation in the real world \( D^w \) and in the information system \( D^s \), we use real-world effects and copy effects as annotations. While their syntax is the same, their semantics is different. Formally, a real-world effect \( r \) or a copy effect \( c \) is a tuple \((R(\vec{x}, \vec{y}), G(\vec{x}, \vec{z}))\), where \( R \) is an atom, \( G \) is a set of atoms and built-in comparisons and \( \vec{x}, \vec{y} \) and \( \vec{z} \) are sets of distinct variables. We call \( G \) the guard of the effect. The effects \( r \) and \( c \) can be written as follows:

\[
\begin{align*}
r &: R^w(\vec{x}, \vec{y}) \iff \exists \vec{z} : G^w(\vec{x}, \vec{z}) \\
c &: R^w(\vec{x}, \vec{y}), G^w(\vec{x}, \vec{z}) \rightarrow R^s(\vec{x}, \vec{y})
\end{align*}
\]
Real-world effects can have variables \( \bar{y} \) on the left side that do not occur in the condition. These variables are not restricted and thus allow to introduce new values.

A pair of real-world databases \((D_1^w, D_2^w)\) conforms to a real-world effect \(R^w(\bar{x}, \bar{y}) \iff \exists \bar{z} : G^w(\bar{x}, \bar{z})\), if for all facts \(R^w(\bar{c}_1, \bar{c}_2)\) that are in \(D_2^w\) but not in \(D_1^w\) it holds that there exists a tuple of constants \(\bar{c}_3\) such that the guard \(G^w(\bar{c}_1, \bar{c}_3)\) is in \(D_1^w\). The pair of databases conform to a set of real-world effects, if each fact in \(D_2^w \setminus D_1^w\) conforms to at least one real-word effect.

If for a real-world effect there does not exist any pair of databases \((D_1, D_2)\) with \(D_2 \setminus D_1 \neq \emptyset\) that conforms to the effect, the effect is called useless. In the following we only consider real-world effects that are not useless.

The function \(\text{copy}_c\) for a copy effect \(c = R^w(\bar{x}, \bar{y}), G^w(\bar{x}, \bar{z}) \rightarrow R^w(\bar{x}, \bar{y})\) over a real-world database \(D^w\) returns the corresponding R-facts for all the tuples that are in the answer of the query \(P_c(\bar{x}, \bar{y}) : R^w(\bar{x}, \bar{y}), G^w(\bar{x}, \bar{z})\) over \(D^w\). For a set of copy effects \(CE\), the function \(\text{copy}_{CE}\) is defined by taking the union of the results of the individual copy functions.

**Example 3.** Consider a real-world effect \(r\) that allows to introduce persons living in Merano as pupils in classes higher than 3 in the real world, that is, \(r = \text{pupil}^w(n, c, s) \iff c > 3, \text{livesIn}(n, \text{Merano})\) and a pair of real-world databases using the database \(D^w\) from Example 1 as \((D^w, D^w \cup \{\text{pupil}^w(\text{Bob}, 4, \text{HoferSchool})\})\). Then this pair conforms to the real-world effect \(r\), because the guard of the only new fact \(\text{pupil}^w(\text{Bob}, 4, \text{HoferSchool})\) evaluates to true: Bob lives in Merano and his class level is greater than 3. The pair \((D^w, D^w \cup \{\text{pupil}^w(\text{Alice}, 1, \text{HoferSchool})\})\) does not conform to \(r\), because Alice does not live in Merano, and also because the class level is not greater than 3.

For the copy effect \(c = \text{pupil}^w(n, c, s), c > 3 \rightarrow \text{pupil}^w(n, c, s)\), which copies all pupils in classes greater equal 3, its output over the real-world database in Example 1 would be \(\{\text{pupil}^w(\text{Mary}, 4, \text{HoferSchool})\}\).

### 3.4 Quality-Aware Transition Systems

To capture the execution semantics of quality-aware processes, we resort to (suitably annotated) labelled transition systems, a common way to describe the semantics of concurrent processes by interleaving \([5]\). This makes our approach applicable for virtually every business process modelling language equipped with a formal underlying transition semantics (such as Petri nets or, directly, transition systems).

Formally, a (labelled) transition system \(T\) is a tuple \(T = (S, s_0, A, E)\), where \(S\) is a set of states, \(s_0 \in S\) is the initial state, \(A\) is a set of names of actions and \(E \subseteq S \times A \times S\) is a set of edges labelled by actions from \(A\). In the following, we will annotate the actions of the transition systems with effects that describe interaction with the real-world and the information system. In particular, we introduce quality-aware transition systems (QATS) to capture the execution semantics of processes that change data both in the real world and in the information system database.

Formally, a quality-aware transition system \(\hat{T}\) is a tuple \(\hat{T} = (T, re, ce)\), where \(T\) is a transition system and \(re\) and \(ce\) are functions from \(A\) into the sets of all real-world effects and copy effects, which in turn obey to the syntax and semantics defined in Sec. 3.3.

Note that transition systems and hence also QATS may contain cycles.
Example 4. Let us consider two specific schools, the Hofer School and the Da Vinci School, and a (simplified version) of their enrolment process, depicted in BPMN in Fig. 3(a) (in parenthesis, we introduce compact names for the activities, which will be used throughout the example). As we will see, while the two processes are independent from each other from the control-flow point of view (i.e., they run in parallel), they eventually write information into the same table of the central information system.

Let us first consider the Hofer School. In the first step, the requests are processed with pen and paper, deciding which requests are accepted and, for those, adding the signature of the school director and finalising other bureaucratic issues. By using relation \( \text{request}^{rw}(n, \text{HoferSchool}) \) to model the fact that a child named \( n \) requests to be enrolled at Hofer, and \( \text{pupil}^{rw}(n, 1, \text{HoferSchool}) \) to model that she is actually enrolled, the activity \( \text{pH} \) is a real-world activity that can be annotated with the real-world effect \( \text{pupil}^{rw}(n, 1, \text{HoferSchool}) \sim \text{request}^{rw}(n, \text{HoferSchool}) \). In the second step, the information about enrolled pupils is transferred to the central information system by copying all real-world enrolments of the Hofer school. More specifically, the activity \( \text{rH} \) can be annotated with the copy effect \( \text{pupil}^{rw}(n, 1, \text{HoferSchool}) \rightarrow \text{pupil}^{rw}(n, 1, \text{HoferSchool}) \).

Let us now focus on the Da Vinci School. Depending on the amount of incoming requests, the school decides whether to directly process the enrolments, or to do an entrance test for obtaining a ranking. In the first case (activity \( \text{pD} \)), the activity mirrors that of the Hofer school, and is annotated with the real-world effect \( \text{pupil}^{rw}(n, 1, \text{DaVinci}) \sim \text{request}^{rw}(n, \text{DaVinci}) \). As for the test, the activity \( \text{tD} \) can be annotated with a real-world effect that makes it possible to enrol only those children who passed the test: \( \text{pupil}^{rw}(n, 1, \text{DaVinci}) \sim \text{request}^{rw}(n, \text{DaVinci}), \text{test}^{rw}(n, \text{mark}), \text{mark} \geq 6 \). Finally, the process terminates by properly transferring the information about enrolments to the central administration, exactly as done for the Hofer school. In particular, the activity \( \text{rD} \) is annotated with the copy effect \( \text{pupil}^{rw}(n, 1, \text{DaVinci}) \rightarrow \text{pupil}^{rw}(n, 1, \text{DaVinci}) \). Notice that this effect feeds the same \( \text{pupil} \) relation of the central information systems that is used by \( \text{rH} \), but with a different value for the third column (i.e., the school name).

Fig. 3(b) shows the QATS formalizing the execution semantics of the parallel composition of the two processes (where activities are properly annotated with the previously discussed effects). Circles drawn in orange with solid line represent execution states where the information about pupils enrolled at the Hofer school is complete. Circles in blue with double stroke represent execution states where completeness holds for pupils enrolled at the Da Vinci school. At the final, sink state information about the enrolled pupils is complete for both schools.

3.5 Paths and Action Sequences in QATSs

Let \( T = (T, re, ce) \) be a QATS. A path \( \pi \) in \( T \) is a sequence \( t_1, \ldots, t_n \) of transitions such that \( t_i = (s_{i-1}, a_i, s_i) \) for all \( i = 1 \ldots n \). An action sequence \( \alpha \) is a sequence \( a_1, \ldots, a_m \) of action names. Each path \( \pi = t_1, \ldots, t_n \) has also a corresponding action sequence \( \alpha_{\pi} \) defined as \( a_1, \ldots, a_n \). For a state \( s \), the set \( Aseq(s) \) is the set of the action sequences of all paths that end in \( s \).

Next we consider the semantics of action sequences. A development of an action sequence \( \alpha = a_1, \ldots, a_n \) is a sequence \( D^w_0, \ldots, D^w_n \) of real-world databases such that each pair \( (D^w_j, D^w_{j+1}) \) conforms to the effects \( re(\alpha_{j+1}) \). Note that \( D^w_0 \) can be arbitrary.
Consider the QATS in Figure 3(b) and recall that the action Compl(seq) in action sequence satisfies it. A state satisfies query completeness for Hofer school, because in all models of real-world databases (developments), there exists a unique trace $D_0^{rw}, \ldots, D_n^{rw}$ of real-world databases (developments), where $D_0^{rw}$ may contain additional pupil facts at the Hofer school w.r.t. $D_0^{rw}$ because of the real-world effect of action $a_1$, and $D_n^{rw} = D_n^{rw}$. Each such development has a uniquely defined trace $D_0^{rw}, D_1^{rw}, D_2^{rw}$ where $D_0^{rw} = D_0^{rw}$ by definition, $D_1^{rw} = D_0^{rw}$ because no copy effect is happening in action $a_1$, and $D_2^{rw} = D_1^{rw} \cup \text{copy}_{\text{cel}(a_1)}(D_1^{rw})$, which means that all pupil facts from Hofer school that hold in the real-world database are copied into the information system due to the effect of action $a_1$. Thus, the state $s_2$ satisfies Compl($Q_{\text{Hofer}}$) for a query $Q_{\text{Hofer}(n)} := \text{pupil}(n, c, \text{HoferSchool})$, because in all models of the action sequence the real-world pupils at the Hofer school are copied by the copy effect in action rH.

3.6 Completeness over QATSS

An action sequence $\alpha = a_1, \ldots, a_n$ satisfies query completeness of a query $Q$, if for all developments of $\alpha$ it holds that $Q$ is complete over $(D_0^{rw}, D_n^{rw})$, that is, if $Q(D_0^{rw}) = Q(D_n^{rw})$ holds. A path $P$ in a QATS $\tilde{T}$ satisfies query completeness for $Q$, if its corresponding action sequence satisfies it. A state $s$ in a QATS $\tilde{T}$ satisfies Compl($Q$), if all action sequences in $\text{Aseq}(s)$ (the set of the action sequences of all paths that end in $s$) satisfy Compl($Q$). We then write $s \vDash \text{Compl}(Q)$.

Example 5. Consider the QATS in Figure 3(b) and recall that the action pH is annotated with the real-world effect pupil($n, 1, \text{HoferSchool} \leftarrow \text{request}(n, \text{HoferSchool})$, and action rH with the copy effect pupil($n, 1, \text{HoferSchool} \rightarrow \text{pupil}(n, 1, \text{HoferSchool}$). A path $\pi = ((s_0, pH, s_1), (s_1, rH, s_2))$ has the corresponding action sequence (pH,rH).

It's models are all sequences $(D_0^{rw}, D_1^{rw}, D_2^{rw})$ of real-world databases (developments), where $D_0^{rw}$ may contain additional pupil facts at the Hofer school w.r.t. $D_0^{rw}$ because of the real-world effect of action $a_1$, and $D_2^{rw} = D_2^{rw}$. Each such development has a uniquely defined trace $D_0^{rw}, D_1^{rw}, D_2^{rw}$ where $D_0^{rw} = D_0^{rw}$ by definition, $D_1^{rw} = D_0^{rw}$ because no copy effect is happening in action $a_1$, and $D_2^{rw} = D_1^{rw} \cup \text{copy}_{\text{cel}(a_1)}(D_1^{rw})$, which means that all pupil facts from Hofer school that hold in the real-world database are copied into the information system due to the effect of action $a_1$. Thus, the state $s_2$ satisfies Compl($Q_{\text{Hofer}}$) for a query $Q_{\text{Hofer}(n)} := \text{pupil}(n, c, \text{HoferSchool})$, because in all models of the action sequence the real-world pupils at the Hofer school are copied by the copy effect in action rH.
4 Verifying Completeness over Processes

In the following, we analyze how to check completeness in a state of a QATS at design time, at runtime, and how to analyze the completeness of an incomplete query in detail.

4.1 Design-Time Verification

When checking for query completeness at design time, we have to consider all possible paths that lead to the state in which we want to check completeness. We first analyze how to check completeness for a single path, and then extend our results to sets of paths.

Given a query \( Q(\bar{x}) \) \( = \) \( R_1(\bar{t}_1), \ldots, R_n(\bar{t}_n), M \), we say that a real-world effect \( r \) is risky w.r.t. \( Q \), if there exists a pair of real-world databases \((D_1^w, D_2^w)\) that conforms to \( r \) and where the query result changes, that is, \( Q(D_1^w) \neq Q(D_2^w) \). Intuitively, this means that real-world database changes caused by \( r \) can influence the query answer and lead to incompleteness, if the changes are not copied into the information system.

\[ \text{Proposition 1 (Risk effects). Let } r \text{ be the real-world effect } R(\bar{x}, \bar{y}) \iff G_1(\bar{x}, \bar{z}_1), Q \text{ be the query } Q : R_1(\bar{t}_1), \ldots, R_n(\bar{t}_n), M \text{ and } \bar{v} = \text{Var}(Q). \text{ Then } r \text{ is risky wrt. } Q \text{ if and only if the following formula is satisfiable:} \]

\[ G_1(\bar{x}, \bar{z}_1) \land (\bigwedge_{i=1}^{n} R_i(\bar{t}_i)) \land M \land (\bigvee_{R_i=\bar{v}} (\bar{x}, \bar{y}) = \bar{t}_i) \]

\[ \text{Proof. } \Rightarrow: \text{ If the formula is satisfied for some assignment } \delta, \text{ this satisfying assignment directly yields an example showing that } r \text{ is risky wrt. } Q \text{ as follows: Suppose that the disjunct is satisfied for some } i = k. \text{ Then we can construct databases } D_1^w \text{ and } D_2^w \text{ as } D_1^w = G_1(\delta \bar{x}, \delta \bar{z}_1) \cup \{ \bigwedge_{i=1}^{n}, j \neq k R_i(\delta \bar{t}_i) \} \text{ and } D_2^w = D_1^w \cup \{ R_k(\delta \bar{t}_k) \}. \text{ Clearly, } (D_1^w, D_2^w) \text{ satisfies the effect } r \text{ because for the only additional fact } R_k(\delta \bar{t}_k) \text{ in } D_2^w, \text{ the condition } G_1 \text{ is contained in } (D_2^w). \text{ But } Q(D_1^w) \neq Q(D_2^w) \text{ because with the new fact, a new valuation for the query is possible by mapping each atom to itself.} \]

\[ \Rightarrow: \text{ Holds by construction of the formula, which checks whether it is possible for } R-\text{facts to satisfy both } G_1 \text{ and } Q. \text{ Suppose } r \text{ is risky wrt. } Q. \text{ Then there exists a pair of databases } (D_1^w, D_2^w) \text{ that satisfies } r \text{ and where } Q(D_1^w) \neq Q(D_2^w). \text{ Thus, all new facts in } D_2^w \text{ must conform to } G_1 \text{ and some facts must also contribute to new evaluations of } Q \text{ that lead to } Q(D_1^w) \neq Q(D_2^w). \text{ Thus, each such facts implies the existence of a satisfying assignment for the formula.} \]

\[ \text{Example 6. Consider the query } Q(n) := \text{pupil}(n, c, s), \text{livesIn}(n, \text{Bolzano}) \text{ and the real-world effect } r_1 = \text{pupil}(n, c, s) \iff c = 4, \text{ which allows to add new pupils in class 4 in the real world. Then } r_1 \text{ is risky w.r.t. } Q, \text{ because pupils in class 4 can potentially also live in Bolzano. Note that without integrity constraints, actually most updates to the same relation will be risky: if we do not have keys in the database, a pupil could live both in Bolzano and Merano and hence an effect } r_2 = \text{pupil}(n, c, s) \iff \text{livesIn}(n, \text{Merano}) \text{ would be risky w.r.t. } Q, \text{ too. If there is a key defined over the first attribute of } \text{livesIn}, \text{ then } r_2 \text{ would not be risky, because adding pupils that live in Merano would not influence the completeness of pupils that only live in Bolzano.} \]
We say that a real-world effect \( r \) that is risky w.r.t. a query \( Q \) is repaired by a set of copy effects \( \{c_1, \ldots, c_n\} \), if for any sequence of databases \( (D_1^w, D_2^w) \) that conforms to \( r \) it holds that \( Q(D_2^w) = Q(D_1^w) \cup \text{copy}_{c_1, \ldots, c_n}(D_2^w) \). Intuitively, this means that whenever we introduce new facts via \( r \) and apply the copy effects afterwards, all new facts that can change the query result are also copied into the information system.

**Proposition 2 (Repairing).** Consider the query \( Q := R_1(\bar{t}_1), \ldots, R_n(\bar{t}_n), M \), let \( \bar{v} = \text{Var}(Q) \), a real-world effect \( R(\bar{x}, \bar{y}) \Leftrightarrow G_1(\bar{x}, \bar{z}_1) \) and a set of copy effects \( \{c_1, \ldots, c_m\} \). Then \( r \) is repaired by \( \{c_1, \ldots, c_m\} \) if and only if the following formula is valid:

\[
\forall \bar{x}, \bar{y}: \left( \exists \bar{z}_1, \bar{v}: \left( G_1(\bar{x}, \bar{z}_1) \land \bigwedge_{i=1}^n R(i) \land M \land \bigvee_{R_i = R} (\bar{x}, \bar{y}) = \bar{t}_i \right) \Rightarrow \bigvee_{j=2}^m \exists \bar{z}_j: G_j(\bar{x}, \bar{z}_j) \right)
\]

**Proof.** "\( \Leftarrow \)" Straightforward. If the formula is valid, it implies that any fact \( R(\bar{x}) \) that is introduced by the real-world effect \( r \) and which can change the result of \( Q \) also satisfies the condition of some copy effect and hence will be copied.

"\( \Rightarrow \)" Suppose the formula is not valid. Then there exists a fact \( R(\bar{x}) \) which satisfies the condition of the implication (so \( R(\bar{x}) \) can both conform to \( r \) and change the result of \( Q \)) but not the consequence (it is not copied by any copy effect). Thus, we can create a pair \( (D_1^w, D_2^w) \) of databases as before as \( D_1^w = G_1(\bar{x}, \bar{z}) \cup \{ \bigwedge_{i=1}^n R(i) \} \) and \( D_2^w = D_1^w \cup \{ R(\bar{t}_i) \} \) which proves that \( Q(D_2^w) \neq Q(D_1^w) \cup \text{copy}_{c_1, \ldots, c_n}(D_2^w) \). \( \square \)

This implication can be translated into a problem of query containment, a well-studied topic in database theory \[11, 8, 14, 12\]. In particular, for a query \( Q(\bar{z}) := R_1(\bar{t}_1), \ldots, R_n(\bar{t}_n) \), we define the atom-projection of \( Q \) on the \( i \)-th atom as \( Q_i(\bar{z}) := R_1(\bar{t}_1), \ldots, R_{i-1}(\bar{t}_{i-1}), R_i(\bar{t}_i), \bar{z} = \bar{t}_i \). Then, for a query \( Q \) and a relation \( R \), we define the \( R \)-projection of \( Q \), written \( Q^R \), as the union of all the atom-projections of atoms that use the relation symbol \( R \), that is, \( \bigcup_{R_i = R} Q_i^R \). For a real-world effect \( r = R(\bar{x}, \bar{y}) \Leftrightarrow G(\bar{x}, \bar{z}) \), we define its associated query \( P_r \) as \( P_r(\bar{x}, \bar{y}) := R(\bar{x}, \bar{y}), G(\bar{x}, \bar{z}) \).

**Corollary 1 (Repairing and query containment).** Let \( Q \) be a query, \( \alpha = a_1, \ldots, a_n \) be an action sequence, \( a_i \) be an action with a risky real-world effect \( r \), and \( \{c_1, \ldots, c_m\} \) be the set of all copy effects of the actions \( a_{i+1} \ldots a_n \).

Then \( r \) is repaired, if and only if it holds that \( P_r \cap Q^R \subseteq P_{c_1} \cup \ldots \cup P_{c_m} \).

Intuitively, the corollary says that a risky effect \( r \) is repaired, if all data that is introduced by \( r \) that can potentially change the result of the query \( Q \) are guaranteed to be copied into the information system database by the copy effects \( c_1 \) to \( c_m \).

The corollary holds because of the direct correspondence between conjunctive queries and relational calculus \[1\].

We arrive at a result for characterizing query completeness wrt. an action sequence:

**Lemma 1 (Action sequence completeness).** Let \( \alpha \) be an action sequence and \( Q \) be a query. Then \( \alpha \models \text{Compl}(Q) \) if and only if all risky effects in \( \alpha \) are repaired.

**Proof.** "\( \Leftarrow \)" Assume that all risky real-world effects in \( \alpha \) are repaired in \( \alpha \). Then by Lemma 1 any fact introduced by a real-world effect \( r \) which can potentially also influence the satisfaction of \( \text{Compl}(Q) \) also satisfies the condition of some later copy effect,
Lemma 2 (Duplicate removal). makes the analysis more difficult. We first introduce a lemma that allows to remove repeated action sequences more in detail in Section 4.4.

We discuss the complexity of query containment and hence of completeness entailment to each other in linear time.

Before discussing complexity results in Section 4.4 we show that completeness entailment over action sequences and containment of unions of queries have the same complexity. A query language is defined by the operations that it allows. Common sublanguages of conjunctive queries are, e.g., queries without arithmetic comparisons (so-called relational queries), or queries without repeated relation symbols (so-called linear queries).

For a query language \( \mathcal{L} \), we call \( \text{EntC}(\mathcal{L}) \) the problem of deciding whether an action sequence \( \alpha \) entails completeness of a query \( Q \), where \( Q \) and the real-world effects and the copy effects in \( \alpha \) are formulated in language \( \mathcal{L} \). Also, we call \( \text{ContU}(\mathcal{L}) \) the problem of deciding whether a query is contained in a union of queries, where all are formulated in the language \( \mathcal{L} \).

**Theorem 1.** Let \( \mathcal{L} \) be a query language. Then \( \text{EntC}(\mathcal{L}) \) and \( \text{ContU}(\mathcal{L}) \) can be reduced to each other in linear time.

**Proof.** “\( \Rightarrow \)”: Consider the characterization shown in Lemma 1. For a fixed action sequence, the number of containment checks is the same as the number of the real-world effects of the action sequence and thus linear.

“\( \Leftarrow \)”: Consider a containment problem \( Q_0 \subseteq Q_1 \cup \ldots \cup Q_n \), for queries in a language \( \mathcal{L} \). Then we can construct a QAATS \( \mathcal{F} = (S, s_0, A, E, re, ce) \) over the schema of the queries together with a new relation \( R \) with the same arity as the queries where \( S = \{s_0, s_1, s_2\} \), \( A = \{a_1, a_2\} \), \( re(a_1) = (R^n(\bar{x}) \iff Q_0(\bar{x})) \) and \( ce(a_2) = \bigcup_{i=1..n}(Q_i(\bar{x}) \rightarrow R^i(\bar{x})) \). Now, the action sequence \( a_1, a_2 \) satisfies a query completeness for a query \( Q' \) exactly if \( Q_0 \) is contained in the union of the queries \( Q_1 \) to \( Q_n \), because only in this case the real-world effect at action \( a_1 \) cannot introduce any facts into \( D^\alpha_{\text{rw}} \) of a development of \( a_1, a_2 \), which are not copied into \( D^\alpha_{\text{rw}} \) by one of the effects of the action \( a_2 \).

We discuss the complexity of query containment and hence of completeness entailment over action sequences more in detail in Section 4.4.

So far, we have shown how query completeness over a path can be checked. To verify completeness in a specific state, we have to consider all paths to that state, which makes the analysis more difficult. We first introduce a lemma that allows to remove repeated actions in an action sequence:

**Lemma 2 (Duplicate removal).** Let \( \alpha = \alpha_1, \bar{a}, \alpha_2, \bar{a}, \alpha_3 \) be an action sequence with \( \bar{a} \) as repeated action and let \( Q \) be a query. Then \( \alpha \) satisfies \( \text{Compl}(Q) \) if and only if \( \alpha' = \alpha_1, \alpha_2, \bar{a}, \alpha_3 \) satisfies \( \text{Compl}(Q) \).
Proof. ".\Rightarrow": Suppose \( \alpha \) satisfies Compl(\( Q \)). Then, by Prop. \[1\] all risky real-world effects of the actions in \( \alpha \) are repaired. Let \( a_r \) be an action in \( \alpha \) that contains a risky real-world effect \( r \). Thus, there must exist a set of actions \( A_r \) in \( \alpha \) that follows \( a_r \) and contains copy effects that repair \( r \). Suppose \( A_r \) contains the first occurrence of \( \bar{a} \). Then, this first occurrence of \( \bar{a} \) can also replaced by the second occurrence of \( \bar{a} \) and then the modified set of actions also appears after \( a_r \) in \( \alpha' \).

"\(\Leftarrow\)". Suppose \( \alpha' \) satisfies Compl(\( Q \)). Then, also \( \alpha \) satisfies Compl(\( Q \)) because adding the action \( \bar{a} \) earlier cannot influence query completeness: Since by assumption each risky real-world effect of the second occurrence of \( \bar{a} \) is repaired by some set of actions \( A_r \) that follows \( \bar{a} \), the same set \( A_r \) also repairs each risky real-world effect of the first occurrence of \( \bar{a} \).  

\( \square \)

The lemma shows that our formalism can deal with cycles. While cycles imply the existence of sequences of arbitrary length, the lemma shows that we only need to consider sequences where each action occurs at most once. Intuitively, it is sufficient to check each cycle only once. Based on this lemma, we define the normal action sequence of a path \( \pi \) as the action sequence of \( \pi \) in which for all repeated actions all but the last occurrence are removed.

Proposition 3 (Normal action sequences). Let \( \bar{T} = (T, re, ce) \) be a QATS, \( \Pi \) be the set of all paths of \( T \) and \( Q \) be a query. Then

1. for each path \( \pi \in \Pi \), its normal action sequence has at most the length \( |A| \),
2. there are at most \( \sum_{k=1}^{(|A|)\cdot |A|!} < (|A| +1)! \) different normal forms of paths,
3. for each path \( \pi \in \Pi \), it holds that \( \pi \vDash \text{Compl}(Q) \) if its normal action sequence \( \alpha' \) satisfies Compl(\( Q \)).

The first two items hold because normal action sequences do not contain actions twice. The third item holds because of Lemma \[2\] which allows to remove all but the last occurrence of an action in an action sequence without changing query completeness satisfaction.

Before arriving at the main result, we need to show that deciding whether a given normal action sequence can actually be realized by a path is easy:

Proposition 4. Given a QATS \( \bar{T} \), a state \( s \) and a normal action sequence \( \alpha \). Then, deciding whether there exists a path \( \pi \) that has \( \alpha \) as its normal action sequence and that ends in \( s \) can be done in polynomial time.

The reason for this proposition is that given a normal action sequence \( \alpha = a_1, \ldots, a_n \), one just needs to calculate the states reachable from \( s_0 \) via the concatenated expression \( (a_1, \ldots, a_n)^+, (a_2, \ldots, a_n)^+, \ldots, (a_{n-1}, a_n)^+ \). This expression stands exactly for all action sequences with \( \alpha \) as normal sequence, because it allows repeated actions before their last occurrence in \( \alpha \). Calculating the states that are reachable via this expression can be done in polynomial time, because the reachable states \( S_{\gamma} \) can be calculated iteratively for each component \( (a_i, \ldots, a_n)^+ \) as \( S_{\gamma} \) from the reachable states \( S_{\gamma} \) until the previous component \( (a_{i-1}, \ldots, a_n)^+ \) by taking all states that are reachable from a state in \( S_{\gamma} \) via one or several actions in \( (a_i, \ldots, a_n) \), which can be done with a linear-time graph traversal such as breadth-first or depth-first search. Since there are only \( n \) such components, the overall algorithm works in polynomial time.
**Theorem 2.** Given a QATS $\bar{T}$ and a query $Q$, both formulated in a query language $L$, checking “$s \not\models \text{Compl}(Q)$” can be done using a nondeterministic polynomial-time Turing machine with a $\text{ContU}(L)$-oracle.

**Proof.** If $s \not\models \text{Compl}(Q)$, one can guess a normal action sequence $\alpha$, check by Prop. 4 in polynomial time that there exists a path $\pi$ from $s_0$ to $s$ with $\alpha$ as normal action sequence, and by Thm. 1 verify using the $\text{ContU}(L)$-oracle that $\alpha$ does not satisfy $\text{Compl}(Q)$. $\square$

We discuss the complexity of this problem in Section 4.4

### 4.2 Runtime Verification

Taking into account the concrete activities that were carried out within a process can allow more conclusions about completeness. As an example, consider that the secretary in a large school can perform two activities regarding the enrollments, either he/she can sign enrollment applications (which means that the enrollments become legally valid), or he/she can record the signed enrollments that are not yet recorded in the database. For simplicity we assume that the secretary batches the tasks and performs only one of the activities per day. A visualization of this process is shown in Fig. 4. Considering only the process we cannot draw any conclusions about the completeness of the enrollment data, because if the secretary chose the first activity, then data will be missing, however if the secretary chose the second activity, then not. If however we have the information that the secretary performed the second activity, then we can conclude that the number of the currently valid enrollments is also complete in the information system.

Formally, in runtime verification we are given a path $\pi = t_1, \ldots, t_n$ that was executed so far and a query $Q$. Again the problem is to check whether completeness holds in the current state, that is, whether all developments of $\pi$ satisfy $\text{Compl}(Q)$.

**Corollary 2.** Let $\pi$ be a path in a QATS and $Q$ be a query, such that both $Q$ and the real-world effects and the copy effects in the actions of $\pi$ are formulated in a query language $L$. Then “$\pi \models \text{Compl}(Q)$” and $\text{ContU}(L)$ can be reduced to each other in linear time.

The corollary follows directly from Theorem 1 and the fact that a path satisfies completeness if and only if its action sequence satisfies completeness.

Runtime verification becomes more complex when also the current, concrete state of the information system database is explicitly taken into account. Given the current
state $D$ of the database, the problem is then to check whether all the developments of $\pi$ in which $D^\pi_n = D$ holds satisfy $\text{Compl}(Q)$. In this case repairing of all risky actions is a sufficient but not a necessary condition for completeness:

**Example 7.** Consider a path $(s_0, a_1, s_1)$, $(s_1, a_2, s_2)$, where action $a_1$ is annotated with the copy effect $\text{request}^\pi(n, s) \rightarrow \text{request}^\pi(n, s)$, action $a_2$ with the real-world effect $\text{pupil}^\pi(n, c, s) \leftarrow \text{request}^\pi(n, s)$, a database $D^\pi_n$ that is empty, and consider a query $Q(n) : \neg \text{pupil}(n, c, s)$, $\text{request}(n, s)$. Then, the query result over $D^\pi_n$ is empty. Since the relation $\text{request}$ was copied before, and is empty now, the query result over any real-world database must be empty too, and therefore $\text{Compl}(Q)$ holds. Note that this cannot be concluded with the techniques introduced in this work, as the real-world effect of action $a_2$ is risky and is not repaired.

The complexity of runtime verification w.r.t. a concrete database instance is still open.

**4.3 Dimension Analysis**

When at a certain timepoint a query is not found to be complete, for example because the deadline for the submissions of the enrollments from the schools to the central school administration is not yet over, it becomes interesting to know which parts of the answer are already complete.

**Example 8.** Consider that on the 10th of April, the schools “Hofer” and “Da Vinci” have confirmed that they have already submitted all their enrollments, while “Max Valier” and “Gherdena” have entered some but not all enrollments, and other schools did not enter any enrollments so far. Then the result of a query asking for the number of pupils per school would look as in Fig. 5 (left table), which does not tell anything about the trustworthiness of the result. If one includes the information from the process, one could highlight that the data for the former two schools is already complete, and that there can also be additional schools in the query result which did not submit any data so far (see right table in Fig. 5).

Formally, for a query $Q$ a dimension is a set of distinguished variables of $Q$. Originally, dimension analysis was meant especially for the arguments of a GROUP BY expression in a query, however it can also be used with other distinguished variables of a query. Assume a query $Q(\bar{x}) : \neg B(\bar{x}, \bar{y})$ cannot be guaranteed to be complete in a specific state of a process. For a dimension $\bar{w} \subseteq \bar{x}$, the analysis can be done as follows:
1. Calculate the result of $Q'(\vec{w}) \leftarrow B(\vec{x}, \vec{y})$ over $D^\sigma$.
2. For each tuple $\vec{c}$ in $Q'(D^\sigma)$, check whether $s, D^\sigma \models \text{Compl}(Q[\vec{w}/\vec{c}])$. This tells whether the query is complete for the values $\vec{c}$ of the dimension.
3. To check whether further values are possible, one has to guess a new value $\vec{c}_{\text{new}}$ for the dimension and show that $Q[\vec{w}/\vec{c}_{\text{new}}]$ is not complete in the current state. For the guess one has to consider only the constants in the database plus a fixed set of new constants, hence the number of possible guesses is polynomial for a fixed dimension $\vec{v}$.

Step 2 corresponds to deciding for each tuple with a certain value in $Q(D^\sigma)$, whether it is complete or not (color red or green in Fig. 5 right table), Step 3 to deciding whether there can be additional values (bottom row in Fig. 5 right table).

### 4.4 Complexity of Completeness Verification

In the previous sections we have seen that completeness verification can be solved using query containment. Query containment is a problem that has been studied extensively in database research. Basically, it is the problem to decide, given two queries, whether the first is more specific than the second. The results follow from Theorem 1 and 2 and are summarized in Figure 6. We distinguish between the problem of runtime verification, which has the same complexity as query containment, and design-time verification, which, in principle requires to solve query containment exponentially often. Notable however is that in most cases the complexity of runtime verification is not higher than the one of design-time verification. The results on linear relational and linear conjunctive queries, i.e., conjunctive queries without selfjoins and without or with comparisons, are borrowed from [12]. The result on relational queries is reported in [14], and that on conjunctive queries from [11]. As for integrity constraints, the result for databases satisfying finite domain constraints is reported in [12] and for databases satisfying keys and foreign keys in [8].

### 5 Conclusion

In this paper we have discussed that data completeness analysis should take into account the processes that manipulate the data. In particular, we have shown how process models can be annotated with effects that create data in the real world and effects that copy data.
from the real world into an information system. We have then shown how one can verify the completeness of queries over transition systems that represent the execution semantics of such processes. It was shown that the problem is closely related to the problem of query containment, and that more completeness can be derived if the run of the process is taken into account.

In this work we focussed on the process execution semantics in terms of transition systems. The next step is to realize a demonstration system to annotate high-level business process specification languages (such as BPMN or YAWL), extract the underlying quality-aware transition systems, and apply the techniques here presented to check completeness. Also, we intend to face the open question of completeness verification at runtime taking into account the actual database instance.

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References

1. Abiteboul, S., Hull, R., Vianu, V.: Foundations of databases. In: Addison-Wesley (1995)
2. Bagchi, S., Bai, X., Kalagnanam, J.: Data quality management using business process modeling. In: Services Computing, 2006. SCC’06. IEEE International Conference on (2006)
3. Bagheri Hariri, B., Calvanese, D., De Giacomo, G., De Masellis, R., Felli, P.: Foundations of relational artifacts verification. In: BPM. pp. 379–395. Springer (2011)
4. Bagheri Hariri, B., Calvanese, D., De Giacomo, G., Deutsch, A., Montali, M.: Verification of relational data-centric dynamic systems with external services (2013)
5. Baier, C., Katoen, J.P.: Principles of Model Checking. The MIT Press (2008)
6. Bilenko, M., Mooney, R.J.: Adaptive duplicate detection using learnable string similarity measures. In: ACM SIGKDD. pp. 39–48 (2003)
7. Bringel, H., Caetano, A., Tribollet, J.M.: Business process modeling towards data quality: A organizational engineering approach. In: ICEIS (3) (2004)
8. Calì, A., Lembo, D., Rosati, R.: Query rewriting and answering under constraints in data integration systems
9. Damaggio, E., Deutsch, A., Hull, R., Vianu, V.: Automatic verification of data-centric business processes. In: Proc. of the 9th Int. Conference on Business Process
10. Hernández, M.A., Stolfo, S.J.: Real-world data is dirty: Data cleansing and the merge/purge problem. Data mining and knowledge discovery 2(1), 9–37 (1998)
11. van der Meyden, R.: The complexity of querying indefinite data about linearly ordered domains. In: PODS. pp. 331–345 (1992)
12. Razniewski, S., Nutt, W.: Completeness of queries over incomplete databases. In: VLDB (2011)
13. Rodríguez, A., Caro, A., Cappiello, C., Caballero, I.: A BPMN extension for including data quality requirements in business process modeling. In: BPMN (2012)
14. Sagiv, Y., Yannakakis, M.: Equivalence among relational expressions with the union and difference operation. In: VLDB. pp. 535–548 (1978)