Diquark resonance and single top production at the Large Hadron Collider

Durmus Karabacak, S. Nandi and Santosh Kumar Rai

Department of Physics and Oklahoma Center for High Energy Physics,
Oklahoma State University, Stillwater, OK 74078, USA

Abstract

New physics at the TeV scale is highly anticipated at the LHC. New particles with color, if within the LHC energy reach, will be copiously produced. One such particle is a diquark, having the quantum numbers of two quarks, and can be a scalar or a vector. It will decay to two light quarks, or two top quarks, or a top and a light quark, (up or down type depending on the quantum number of the produced diquark). If singly produced, it can be looked for as a dijet resonance, or as giving extra contribution to the single top production or $tt$ production. In this work, we consider a color sextet vector diquark having the quantum number of $(ud)$ type, its resonance production, and the subsequent decay to $tb$, giving rise to excess contribution to the single top production. Even though the diquark mass is large, its strong resonance production dominate the weak production of $tb$ for a wide range of the diquark mass. Also its subsequent decay to $tb$ produce a very hard $b$-jet compared to the usual electroweak production. In addition, the missing energy in the final state event is much larger from the massive diquark decays. Thus, with suitable cuts, the final state with $b, \bar{b}$ and a charged lepton together with large missing energy stands out compared to the Standard Model background. We make a detailed study of both the signal and the background. We find that such a diquark is accessible at the 7 TeV LHC upto a mass of about 3.3 TeV with the luminosity 1 fb$^{-1}$, while the reach goes up to about 4.3 TeV with a luminosity of 10 fb$^{-1}$.

1Email address: durmas@ostatemail.okstate.edu
2Email address: s.nandi@okstate.edu
3Email address: santosh.rai@okstate.edu
1 Introduction

After more than one year of successful running of the Large Hadron Collider (LHC) at CERN, the data released by the two experiments, ATLAS and CMS have not only improved on some of the limits set by the Tevatron experiments, but has already started giving some insights into the TeV scale. So far the results have proved to be consistent with predictions from the Standard Model (SM) with not much deviation which means that the LHC data is already pushing the energy frontier of any Beyond Standard Model (BSM) physics predictions. As expected the LHC data would be most sensitive to the strongly interacting sector with strong limits obtained from resonant searches of new physics exchanged in the s-channel. As the initial states at hadron colliders are colored particles, the most dominant contributions would be through new colored resonances as their couplings would be typically of the order of $\alpha_s$. Such colored particles are predicted in many class of BSM theories such as “squarks” in R-Parity violating supersymmetric theories [1], “diquarks” in super-string inspired $E_6$ grand unification models [2], “excited quarks” in composite models [3–6], models with color-sextet fermions [7,8], color-octet vectors such as axigluons [7,9] and colorons [10–13], models with color-triplet [14], color-sextet [15–17] or color-octet scalars [18,19].

These resonant states when produced will decay to two light jets leading to modification of the dijet differential cross-section at large invariant mass. Both ATLAS and CMS collaborations have looked at the dijet signal and already put strong constraints on such resonances [20–23]. The most current bounds reported by the ATLAS experiment with data corresponding to 1.0 fb$^{-1}$ integrated luminosity at 95% C.L. are 2.99 TeV for excited quarks, 3.32 TeV for axigluons and 1.92 TeV for color-octet scalars [22] while the CMS collaboration with the same amount of data reports lower bounds of 3.52 TeV for the $E_6$ diquarks, 2.49 TeV for the excited quarks, 2.47 TeV for the axigluons and colorons [23].

We note that another interesting prospect other than the dijet signal at LHC would be the modifications to the top quark signal due to exchanges from such colored particles. We are interested in particular with particles of the “diquark” type which carry non-zero baryon number and couple to a pair of quarks or anti-quarks. A lot of studies exist in the literature for such diquarks and their resonant effects in the dijet signals [24–31] and pair production of top quarks [32,35] at the LHC. Scalar triplet diquark contributions have been previously considered in single top quark production at the LHC [36]. We focus on the case of vector...
diquarks which are sextets of $SU(3)_C$ with charge $Q_e = \frac{1}{3}$. Such particles will be copiously produced as s-channel resonances and thus contribute to the dijet final state. It is worth noting that these diquarks will also contribute to the single top quark production leading to significant enhancement in the production cross-section for the process which is the main thrust of this work. An important property of the top, in contrast to lighter quarks, is that it decays before hadronization and thus the single top quark production at the LHC can prove to be an ideal channel to probe for new physics.

For our study of the vector diquark we follow the formalism presented in Ref [29]. In Sec. 2 we present the formalism and give the basic interaction Lagrangian relevant for our study and in Sec. 3 we discuss the single top production cross-section at the LHC and give our results for the signal coming from the diquark exchange and present a detail analysis by comparing the signal with the SM background for the single top channel. In Sec. 4 we discuss the LHC reach for diquark contribution in the single top channel and in Sec. 5 we give our conclusions with future outlook.

2 Formalism

We are interested in new elementary particles that couple to a pair of quarks directly which would imply that they carry exotic baryon number. As the LHC is a proton-proton machine, the initial states comprised of the the valence quarks would lead to enhanced flux in the parton distributions for the collision between a pair of valence quarks such as $uu, dd$ or $ud$. Any new particle that couples to these pairs would carry a baryon number $B = \frac{2}{3}$ and will be charged under the SM color gauge group $SU(3)_C$. Such states are generally referred to as "diquarks". We follow the formalism presented in Ref [29] where the states are classified according to their charges under the SM gauge group $SU(3)_C \times SU(2)_L \times U(1)_Y$ and their spin ($J$). We follow the notation of group structure

$$(SU_3, SU_2)^J_{Q_e},$$

where $Q_e$ indicates the electric charge ($T_3 + Y$). The colored exotics (diquarks) that couple to the valence quark pairs can be either color anti-triplets or sextets. Writing them in the notation
given by Eq. 2.1 we have

$$\Phi \sim (3 \oplus 6, 3)^{0}_{-4/3,2/3,-1/3}, \quad \Phi_q \sim (3 \oplus 6, 1)^{0}_{q} \quad (q = -1/3, 2/3, -4/3),$$

$$A^\mu_U \sim (3 \oplus 6, 2)^{1}_{-1/3,-4/3} \quad A^\mu_D \sim (3 \oplus 6, 2)^{1}_{2/3,-1/3},$$

(2.2)

plus their charge conjugates. The gauge invariant Lagrangian describing the interaction of the above states is given by [29]

$$\mathcal{L}_{qqD} \sim K^j_{ab} \left[ y_{\alpha\beta} \bar{Q}_a^\gamma \sigma_2 \Phi^j \gamma_\mu Q_{b\lambda} + \kappa_{\alpha\beta} \bar{Q}_a^\gamma \sigma_2 \Phi^j \gamma_\mu Q_{b\lambda} \right. $$

$$\left. + \lambda^{1/3} U_{\alpha\beta} \Phi^j \gamma_\mu U_{\beta\lambda} + \lambda^{2/3} u_{\alpha\beta} \Phi^j \gamma_\mu U_{\beta\lambda} + \lambda^{4/3} \bar{Q}_a^\gamma \sigma_2 \gamma_\mu A^\mu_{U\beta} \right] + \text{h.c.}, \quad (2.3)$$

where $$\Phi^j = \frac{1}{2} \sigma_k \Phi^j_k$$ with $$\sigma_k$$ the $$SU(2)_L$$ Pauli matrices and $$K^j_{ab}$$ are $$SU(3)_C$$ Clebsch-Gordan coefficients with the quark color indices $$a, b = 1−3$$, and the diquark color index $$j = 1−N_D$$, $$N_D$$ is the dimension of the $$(N_D = 3)$$ triplet or $$(N_D = 6)$$ antisextet representation. C denotes charge conjugation, and $$\alpha, \beta$$ are the fermion generation indices. The color factor $$K^j_{ab}$$ is symmetric (antisymmetric) under $$ab$$ for the $$6$$ ($$3$$) representation.

After electroweak symmetry breaking, the states in Eq. (2.2) mix and reclassify themselves according to color ($$3, 6$$) and electric charges ($$-4/3, 2/3, -1/3$$). We are only interested in the couplings of the vector diquark and thus keep only terms that involve the vector fields which we denote as $$V_{2U}^{N_D}, V_{U}^{N_D}, V_{D}^{N_D}$$, where the subscripts $$2U, U, D$$ in the fields indicates their electric charge $$|Q|$$ of two up type quarks, one up and one down type quark respectively. The relevant interactions among the physical vector states (diquarks) are then described by the following effective Lagrangian density

$$\mathcal{L}_{qqD}^{V} = K^j_{ab} \left[ \lambda^{2U}_{\alpha\beta} V_{2U}^{ij} \bar{w}_{\alpha\gamma} \gamma_\mu P_R u_{\beta\lambda} + \lambda^{U}_{\alpha\beta} V_{U}^{ij} \bar{w}_{\alpha\gamma} \gamma_\mu P_R d_{\beta\lambda} + \lambda^{D}_{\alpha\beta} V_{D}^{ij} \bar{w}_{\alpha\gamma} \gamma_\mu P_L d_{\beta\lambda} \right] + \text{h.c.} \quad (2.4)$$

where $$P_\tau = \frac{1}{2}(1 \pm \gamma_5)$$ with $$\tau = L, R$$ representing left and right chirality projection operators and superscript $$\mu$$ is the Lorentz four vector index. Note that we have suppressed the dimension index $$(N_D)$$ which is common to all the states as the interaction for the triplet and antisextet are similar. The more general form of the Lagrangian can be found in Ref. [29].

The coupling $$\lambda$$'s involved in Eq. (2.1) are completely arbitrary and can be large as long as they remain perturbative $$\left(\frac{\lambda^2}{4\pi} < 1\right)$$. However most of them are tightly constrained by flavor physics. In our case we find that the more stringent constraints come from collider data such as
the Tevatron and LHC. We focus on the contribution coming from the interaction vertex that involve the vector diquark $V_D$ which will mediate the production of top quark at the LHC and modify the event rates for single top quark production. The diquarks can couple to the initial state valence partons in the proton and are only constrained by their coupling strengths. Thus they will contribute to the dijet production at the LHC which is enhanced for lighter mass and will be possible to study through the invariant mass distribution in the dijet channel. Both the CMS \cite{23} and ATLAS \cite{22} experiments at LHC have looked for such narrow resonances in the dijet channel and effectively lead to strong constraints on such massive resonances. It is worth noting that these colored states do not have direct coupling to a pair of gluons and thus the production cross section for such particles is limited by the flux of the initial partons in the proton at the LHC.

3 Single top production at the LHC

We study the single top-quark production at the LHC where the new physics effects on the single top production come from the exchange of the vector diquark ($V_D$) in the s-channel. The single top production in the SM can proceed in three different channels as shown in Fig. 1. We

![Figure 1: The leading order (LO) Feynman diagrams for the $t$-channel, $s$-channel, and $tW$ production mode for the single top at hadron colliders.](image)

can have the (a) $t$-channel production of the top quark with a light quark in the final state, (b) $s$-channel mode where the top quark is produced with $\bar{b}$-quark via exchange of a $W$-boson and (c) the associated production of the top quark with the $W$-boson via initial state gluon-bottom fusion. The $t$-channel processes, $qb \rightarrow q't$ and $\bar{q}b \rightarrow \bar{q}'t$, are significantly large than the $s$-channel processes, $qq' \rightarrow \bar{b}t$ at LHC. The associated production of a top quark with a $W$ boson, $bg \rightarrow tW^-$, has a smaller cross-section compared to the $t$-channel processes, but is significantly larger than the $s$-channel processes. The approximate theoretical cross-sections for the 7 TeV LHC for the single top processes calculated at NNLO \cite{37,39} are shown in Table 1.

\begin{table}
\centering
\begin{tabular}{|c|c|}
\hline
Process & Cross-section (pb) \\
\hline
$qb \rightarrow q't$ & $X$ \\
$\bar{q}b \rightarrow \bar{q}'t$ & $Y$ \\
$qq' \rightarrow \bar{b}t$ & $Z$ \\
$bg \rightarrow tW^-$ & $W$ \\
\hline
\end{tabular}
\caption{Theoretical cross-sections for single top processes at NNLO.}
\end{table}
Table 1: The approximate NNLO cross-sections for single top (anti-top) production of mass $m_t = 173$ GeV at the LHC with 7 TeV center-of-mass energy. Note that the cross section for $\bar{t}W^+$ production is identical to that for top.

| Channel                  | NNLO cross-section (pb) |
|-------------------------|-------------------------|
| $t$-channel top         | $41.7^{+1.6}_{-0.2} \pm 0.8$ |
| $t$-channel anti-top    | $22.5 \pm 0.5^{+0.7}_{-0.9}$ |
| $s$-channel top         | $3.17 \pm 0.06^{+0.13}_{-0.10}$ |
| $s$-channel anti-top    | $1.42 \pm 0.01^{+0.06}_{-0.07}$ |
| $tW^-$                  | $7.8 \pm 0.2^{+0.5}_{-0.6}$ |

For our purposes, we are interested in the corrections to the $s$-channel production mode for the single top through the vector diquark exchange. The Feynman diagram contributing to the production mode is shown in Fig. 2. Note that the final state has a $b$-quark instead of the $\bar{b}$ unlike the $s$-channel mode in SM. The anti-top production through the charge-conjugated vertices would be significantly suppressed and different because of the small flux of the anti-partons in the colliding protons. Although the top and anti-top production can be distinguished through the charged lepton identification coming from the decay, it is practically impossible to distinguish the $b$ from the $\bar{b}$ at LHC. Thus we focus only on the production mode $pp \rightarrow tb$ which will show an effective increase in the $s$-channel single top production. As the final state distinctly differs from the SM subprocess, there are no interference term contributions. Thus we can simply evaluate the new physics contributions by calculating the subprocess $ud \rightarrow V_D^* \rightarrow tb$ at LHC and convolute it with the appropriate parton density functions (PDF) for the initial colliding partons.

The amplitude for the subprocess $ud \rightarrow V_D^* \rightarrow tb$ using the interaction vertices from the
The production cross-section for \( pp \rightarrow tb + X \) at LHC as a function of the diquark mass \( M_D \) for two values of the center-of-mass energy, \( E_{CM} = 7 \) and 14 TeV. Note that we have chosen \( \lambda'_{\alpha\alpha} = 1 \) and \( Q = m_t \), the mass of the top-quark.

The total production cross-section at the LHC for the subprocess through the vector diquark exchange in the \( s \)-channel is given by

\[
\sigma(pp \rightarrow tb + X) = \sum_{i=1}^{2} \int dx_1 \int dx_2 \mathcal{F}_{u_i}(x_1, Q^2) \times \mathcal{F}_{d_i}(x_2, Q^2) \times \hat{\sigma}(u_id_i \rightarrow tb) \tag{3.7}
\]

where \( \mathcal{F}_{u_i} \) and \( \mathcal{F}_{d_i} \) denote the PDF’s for the up-type and down-type quarks in the colliding protons, while \( Q \) is the factorization scale. We plot the leading-order production cross section for the process \( pp \rightarrow tb + X \) at LHC for the center-of-mass energies of 7 TeV and 14 TeV as a
function of the diquark mass in Fig. 3. We have set the factorization scale $Q = m_t$ and used the CTEQ6L1 parton density functions \cite{40}. We have used $\lambda'_{\alpha\alpha} = 1$ for evaluating the production cross-section in Fig. 3. Note that for the diquark mass $M_D < 4$ TeV the contribution is more than $0.1$ pb at the current LHC center-of-mass energy for order $\lambda' = 1$ couplings. However the couplings are severely constrained for the first two generations from the dijet data at the LHC and thus effective cross-sections would be actually smaller for the low values of diquark mass. For the diquarks of mass greater than $1$ TeV we can assume the top quark as massless and in this limit the total decay width $\Gamma_D$ (for decays to $ud + cs + tu$) is given as
\begin{equation}
\Gamma_D = \frac{\lambda'^2 M_D}{8\pi}.
\end{equation}
As the diquark exchange in the $s$-channel would contribute to the dijet cross-section there are strong constraints on its mass and coupling strength \cite{22,23}. For order one coupling the current bound is $3.52$ TeV for the $E_6$ diquarks. However, we must note that the coupling strength of the diquark to the third generation $\lambda'_{33}$ is unconstrained by the dijet data and thus the direct bounds on the diquark mass can be relaxed for smaller values of the couplings. The $\lambda'_{33}$ coupling is however constrained from the upper bound on the single-top cross-section in the $s$-channel which is $< 26.5$ pb at $95\%$ C.L. using a cut-based analysis \cite{41}. For our analysis, we have assumed that the couplings to all generations are the same and thus we use the constraints given by the upper bound on the cross-section times branching ratio ($\sigma \times B$) on the dijet rate \cite{23} to evaluate the cross-sections for different values of the diquark mass.

As pointed out before, we would like to see the effect of the diquark contributions to the $s$-channel production of single top-quark. To analyze this we focus on the semileptonic decay mode of the produced top quark leading to the following final state:
\begin{equation}
pp \rightarrow (t \rightarrow bW^+) b \rightarrow (W^+ \rightarrow \ell^+ \nu_\ell) bb \rightarrow \ell^+ bb E_T
\end{equation}
where we restrict ourselves to the choice of $\ell = e, \mu$ for the charged lepton. As it is very difficult to differentiate between a $b$ and $\bar{b}$ even with the heavy flavor tagging of the jets in the final state, we are looking at a final state with one positively charged lepton ($\ell^+$) and two hard $b$-jets and missing transverse momenta. A similar final state is expected in the SM from the $s$-channel single top production as well as various other subprocesses which can lead to similar final state topology. At the LHC the significant contributions in the SM to this final state come from the
following processes:
\[
p p \rightarrow W^+Z, \ t\bar{t}, \ t\bar{b}, \ W^+b\bar{b}
\]
\[
\rightarrow t\bar{j}, \ W^+jj, \ (tW^- + tW^+), \ W^+W^-(3.10)
\]
where the processes in the upper row of Eq. [3.10] give two b-jets while the processes in the lower row lead to light quarks in the final state which are identified as b-jets because of mistag. For our parton-level analysis, we choose a b-tagging efficiency of 50% while the mistag rate for light quarks tagged as b-jets is taken as 1%. We must point out that the b-tag efficiency and the mistag rates are dependent on the transverse momenta \( p_T \) and rapidity \( \eta \). Our choice does not include these effects. However, to do such detailed analysis one would also need to include various other systematics including showering and hadronization effects at the LHC and detector-level simulations which is beyond the scope of this work. So we assume that our choice for the efficiencies and the mistag rate is a good approximation when averaged over the entire range of transverse momenta for the quarks within the allowed rapidity gap.

To select the particles in the final state we demand that they satisfy some basic kinematic selection cuts.

- For the two b-jets we demand that they have a minimum transverse momenta given by \( p_T^b > 20 \text{ GeV} \) and are within the rapidity gap \( |\eta_b| < 2.5 \).

- The charged lepton \((\ell^+ = e^+, \mu^+)\) is required to have a minimum transverse momenta given by \( p_T^{\ell^+} > 20 \text{ GeV} \) and is within the rapidity gap \( |\eta_{\ell^+}| < 2.5 \).

- The final states must account for a minimum missing transverse momenta given by \( \not{E}_T > 50 \text{ GeV} \).

- To resolve the final states in the detector they should be well separated. To achieve this we require that they satisfy \( \Delta R_{ij} > 0.2 \) with \( i, j \) representing the b-jets and the charged lepton. The variable \( \Delta R_{ij} \) defines the separation of two particles in the \((\eta, \phi)\) plane of the detector with \( \Delta R_{ij} = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2} \), where \( \eta \) and \( \phi \) represent the pseudo-rapidity and azimuthal angle of the particles respectively.

- To suppress large contributions of gluon splitting into two \((b)\) jets we demand that the minimum invariant mass of two b-jets satisfy \( M_{b_1b_2}^{inv} > 10 \text{ GeV} \).
• We also demand that there are no additional jets with $p_T > 20$ GeV or additional charged leptons with $p_T > 10$ GeV.

With these basic selection cuts and efficiency rates for $b$-tagging we evaluate the contributions to the final state within the SM using the event generator MadGraph 5 [12]. The contributions from the different processes are collected in Table 2. We note that while the $s$-channel single top quark process gives a significant rate, the most dominant contribution comes from the QCD induced process $pp \rightarrow W^+ b \bar{b}$. Summing over all significant contributions we find that the LO SM cross-section at LHC with $\sqrt{s} = 7$ TeV, for the final state of $\ell^+ + 2b + \mathcal{E}_T$, is $\approx 141$ fb. We calculate the contributions for the above final state coming from the single

| Sub-process | $\sigma(\ell^+ + 2b + \mathcal{E}_T)$ (fb) |
|-------------|---------------------------------|
| $pp \rightarrow WZ$ | 7.33 |
| $pp \rightarrow Wjj$ | 9.97 |
| $pp \rightarrow Wb\bar{b}$ | 87.55 |
| $pp \rightarrow tW$ | 0.53 |
| $pp \rightarrow tt$ | 5.51 |
| $pp \rightarrow tj$ | 6.24 |
| $pp \rightarrow tb$ | 23.32 |

Table 2: The total SM background cross section for the dominant sub-processes contributing to the final state $\ell^+ + 2b + \mathcal{E}_T$ estimated at the parton-level, using the event generator MadGraph 5. Note that we have included a $b$-tagging efficiency of 50% for the $b$-jets and a mistag rate of 1% for the light quarks to be tagged as $b$-jets for the final cross sections shown in the table.

top production via the exchange of a vector diquark in the $s$-channel for two different values of the diquark mass, viz. $M_D = 2$ TeV and $M_D = 3$ TeV. The effective couplings (assuming equal couplings to all generations) for the two choices of the diquark mass are restricted by the dijet data and given by the upper bound on $\sigma \times B(pp \rightarrow qq) < 0.121$ pb for $M_D = 2$ TeV and $\sigma \times B(pp \rightarrow qq) < 0.021$ pb for $M_D = 3$ TeV which lead to the upper bound on the effective $\lambda'$ coupling as 0.24 and 0.3 respectively. Using the maximum allowed couplings, we estimate the cross-section $\sigma(\ell^+ + 2b + \mathcal{E}_T)$ with the selection cuts and efficiency rates as 2.95 fb for $M_D = 2$ TeV and 0.42 fb for $M_D = 3$ TeV. However, we must note that these upper bounds are relaxed as there are no severe constraints on the diquark coupling to the third generation quarks. The
dominant constraint comes from the upper bound of the $s$-channel single top-quark production cross-section at LHC \cite{41} which puts an upper bound on the product of the couplings as $\lambda_3^t \lambda_3^t \lambda_3^t \lambda_3^t \leq 0.45$. This allows the $\lambda_3^t \approx 1$ which would imply that the 2 TeV and 3 TeV diquark contributions to the $\ell^+ + 2b + E_T$ final state can be as large as 51 fb and 4.7 fb respectively. The relative significance of the diquark contributions can be enhanced by selecting events through additional kinematic cuts suited to suppress the SM background without effecting the new physics signal. To understand the kinematic characteristics of the final state events coming from the SM processes and the diquark mediated process we plot the normalized differential distributions of the cross-section as a function of a few kinematical variables in Fig. 4.

![Figure 4](image)

Figure 4: Normalized differential distribution of the cross section as a function of the transverse momenta ($p_T$) of the visible particles in the final state for the SM background and the signal for two different values of the mass of the diquark $M_D = 2$ TeV and $M_D = 3$ TeV.

In Fig. 4 we plot the normalized differential distribution of the cross-section with respect to the transverse momenta ($p_T$) of the visible particles in the final state, viz. the two $b$-jets and the charged lepton for the combined SM background and for the individual diquark contributions of mass $M_D = 2$ TeV and 3 TeV respectively. The $b$-jets are arranged according to their $p_T$’s and so the leading $b$-jet ($b_1$) from the diquark mediated process comes almost always from the decay of the heavy diquark and thus peaks in the high $p_T$ region when compared to the SM distribution which falls very rapidly as the $b$-jets get harder. As the diquark mass is increased we can see that the $b$-jet $p_T$ peaks at much higher value (corresponding to the Jacobian peak at $\approx \frac{M_D}{2}$). Again for the diquark mediated process the sub-leading $b$-jet ($b_2$) comes from the decay of a highly boosted top-quark and thus carries large $p_T$ as shown in Fig. 4 (b). The charged lepton ($\ell^+$) also shows similar behavior like the sub-leading $b$-jet as it also carries the
boost of the top-quark from which it originates.

In Fig. 5 we plot the normalized differential distribution of the cross-section with respect to the isolation parameter $\Delta R$ between a pair of visible particles. Note that the characteristic behavior of particles coming from the decay of heavy resonance would be that they are produced back-to-back in the transverse plane and are well separated which would imply peaking at large values of $\Delta R$. This is the feature expected between the leading $b$-jet ($b_1$) and sub-leading $b$-jet ($b_2$) as well as the charged lepton ($\ell^+$) when the events correspond to the process mediated by the diquark as evident in Fig. 5 (a) and (b). However, when the pair of particles originate from the decay of the highly-boosted top quark ($b_2$, $\ell^+$) the relative separation between them would be much smaller as seen in the distributions shown in Fig. 5(c). The SM background does not have these characteristic features and shows a relatively uniform distribution in the $\Delta R$ variable because of contributions from multiple processes smoothening away any distinct effects of an individual contribution.

Another important kinematic variable relevant for any resonant production mode is the invariant mass of a pair of visible particles which reconstructs the mass of the resonant particle. In our case the heavy diquark decays to $tb$ where the top decays further semileptonically. Thus we focus on the invariant mass distributions of the visible decay products. In Fig. 6 we plot the normalized differential distribution of the cross-section with respect to the invariant mass between a pair of visible particles. We note that the reconstructed invariant mass $M_{b\ell E_T}$ will
Figure 6: Normalized differential distribution of the cross section as a function of the invariant mass of a pair of visible particles in the final state for the SM background and the signal for two different values of the mass of the diquark $M_D = 2\, \text{TeV}$ and $M_D = 3\, \text{TeV}$.

give us a good but approximate estimate of the diquark mass, which we have not shown here. As shown in Fig. 6 (a) and (b), the distributions for the diquark mediated process for the invariant mass of the two $b$-jets ($b_1b_2$) and the leading $b$-jet with the charged lepton ($b_1\ell$) would peak for larger values and drop rapidly as it approaches the diquark mass which acts as an upper bound for the invariant mass value. The SM contributions however fall off very rapidly for large invariant mass in these particle pairs which is remnant of the fact that there are no heavy TeV mass particle in SM that can cause such a behavior. However, the invariant mass distribution for the sub-leading $b$-jet and the charged lepton has an upper cut-off at the top mass ($m_t$) for the diquark mediated process since the two particles almost always originate from the decay of the top quark and so the invariant mass of the decay products can never be greater than the mass of the mother particle. This can be seen in Fig. 6 (c). Note that the SM distribution has a long tail as there are other contributions which get superposed on the single top channel contribution making it significantly different from that of the diquark mode.

The dependence of the differential cross section on the different kinematic variables gives us a hint as to what should be the additional kinematic selection on the final state events which would make the diquark effects stand out against the SM contributions. We find that the most effective selection turns out to be the transverse momenta of the leading $b$-jet which originates from the decay of the diquark itself. We find that a more stringent requirement that the leading $b$-jet satisfies $p_T > 400\, \text{GeV}$ is very helpful in achieving a greater suppression of the SM background without affecting the diquark contributions significantly. With this additional
cut, the SM background is reduced to \( \simeq 0.59 \text{ fb} \) while the contribution for the diquark with mass \( M_D = 2 \text{ TeV} \) is reduced only by 7% and that with mass \( M_D = 3 \text{ TeV} \) is reduced only by 4%, thus significantly increasing the sensitivity to the diquark effects in the single top channel. The other promising variables are the \( \Delta R \) and the invariant mass distribution of the two \( b \)-jets and that between the leading \( b \)-jet and the charged lepton which show significant difference between the diquark contribution and the SM background and will increase the signal significance with appropriate selection cuts when combined with the \( p_T \) selection.

4 LHC Sensitivity

We have simulated the events for diquark contribution and the SM background for the final state \( \ell^+ + 2b + \not{E}_T \) at LHC with \( \sqrt{s} = 7 \text{ TeV} \) for two values of the integrated luminosity of 1 \( \text{ fb}^{-1} \) and 10 \( \text{ fb}^{-1} \). The statistical significance is calculated using \[ S = \sqrt{2 \times \left[ (s + b) \ln(1 + \frac{s}{b}) - s \right]} \] (4.11)

where \( s(b) \) is the number of diquark (SM background) events for the corresponding integrated luminosity. We show the sensitivity of the LHC to the diquark mass as a function of its coupling in Fig. 7. We have assumed that the vector diquark couples to all generations of SM quarks with the same strength such that \( \alpha_\lambda \equiv \lambda'^2_{ii}/4\pi \). However \( \alpha_\lambda \) in Fig. 7 can also be redefined as \( \alpha_\lambda \equiv \lambda'_{ii} \lambda'_{33}/4\pi \) where \( \lambda'_{ii} = \lambda'_{11} = \lambda'_{22} \) which means that we can treat \( \lambda'_{33} \) which is unconstrained by dijet data separately. In Fig. 7 (a) we show the sensitivity of LHC in the \( (\alpha_\lambda, M_D) \) parameter plane at 3\( \sigma \) statistical significance using the basic selection cuts discussed in Sec. 3. For \( \lambda'^2 = 4\pi \alpha_\lambda \sim \mathcal{O}(1) \), we find that the LHC can rule out diquark of mass \( M_D \simeq 2.8 \text{ TeV} \) with data corresponding to 1 \( \text{ fb}^{-1} \) of integrated luminosity while the reach becomes \( M_D \simeq 3.65 \text{ TeV} \) with data corresponding to 10 \( \text{ fb}^{-1} \) with the same set of cuts. This reach is improved if we include the strong cut on the transverse momenta of the leading \( b \)-jet of \( p_T > 400 \text{ GeV} \), which we show in Fig. 7 (b). We find that with an integrated luminosity of 1 \( \text{ fb}^{-1} \) which is already collected by each of the two experiments at LHC, the vector diquark mass accessible to LHC at 3\( \sigma \) statistical significance would be \( M_D \simeq 3.25 \text{ TeV} \) while the reach expands to \( M_D \simeq 4.3 \text{ TeV} \) with \( L = 10 \text{ fb}^{-1} \). Thus we find that the single top channel with the appropriate cuts competes quite well with the dijet channel and can prove to be an improvement over the dijet channel if the coupling of the diquarks to the third generation quarks is larger

13
Figure 7: Illustrating the reach for the LHC running at 7 TeV center-of-mass energy in the single top channel for the diquark mass and its coupling to SM quarks. The reach is shown for two values of the integrated luminosity where (a) shows the reach with the basic cuts used for the single top analysis while (b) shows the reach with a stronger cut of $p_T > 400$ GeV on the leading b-jet.

than its coupling to the first two generations.

5 Summary and Conclusions

In this work we have studied the single top quark production at the LHC running at $\sqrt{s} = 7$ TeV. We have considered the effects of a vector diquark resonance on the single top quark production ($pp \rightarrow tb$) and compared it with the SM background for the $\ell^+2b \not{E}_T$ final state, where the top decays semileptonically. We find that there could be large enhancements in the single top quark production at LHC and find that various kinematic distributions effectively capture the essence of a heavy particle exchange which distinguish it from SM background. We have shown that the use of specific selection cuts on the kinematics of the final states can lead to improved significance for the effects of the diquark exchange and increase the LHC sensitivity to heavier diquark mass. We also note that for the vector diquark coupling more strongly to the third generation quarks than the first two generations, the LHC can be sensitive to higher values of the diquark mass when compared to the dijet channel.

In this work, we have restricted ourselves to the study of the sextet vector diquark exchange
and we note that similar results can be also obtained for the triplet vector diquark or the scalar diquarks [36] which contribute to the single top quark production at the LHC. The vector diquark effects on the top quark polarization would be different from that of a scalar diquark exchange [34] as the Lorentz structure at the interaction vertices will be different which can prove to be a good discriminant in distinguishing the vector from the scalar exchange [44, 45].

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