Retinal adaptation and invariance to changes in higher-order stimulus statistics

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(Dated: December 21, 2013)

Adaptation in the retina is thought to optimize the encoding of natural light signals into sequences of spikes sent to the brain. However, adaptation also entails computational costs: adaptive code is intrinsically ambiguous, because output symbols cannot be trivially mapped back to the stimuli without the knowledge of the adaptive state of the encoding neuron. It is thus important to learn which statistical changes in the input do, and which do not, invoke adaptive responses, and ask about the reasons for potential limits to adaptation. We measured the ganglion cell responses in the tiger salamander retina to controlled changes in the second (contrast), third (skew) and fourth (kurtosis) moments of the light intensity distribution of spatially uniform temporally independent stimuli. The skew and kurtosis of the stimuli were chosen to cover the range observed in natural scenes. We quantified adaptation in ganglion cells by studying two-dimensional linear-nonlinear models that capture well the retinal encoding properties across all stimuli. We found that the retinal ganglion cells adapt to contrast, but exhibit remarkably invariant behavior to changes in higher-order statistics. Finally, by theoretically analyzing optimal coding in LN-type models, we showed that the neural code can maintain a high information rate without dynamic adaptation despite changes in stimulus skew and kurtosis.

I. INTRODUCTION

Adaptation is ubiquitous in the nervous system, from synaptic depression (Abbott et al., 1997; Tsodyks & Markram, 1997) and single neuron spiking (Adrian, 1928; Partridge & Stevens, 1970), to the activity of neural modules (e.g. Müller et al., 1999)). In sensory systems, it has been suggested to be a key design principle of the neural code (Wark et al., 2007), which may allow for optimal information coding by matching the neural responses to stimulus statistics (Attick, 1992; Attick & Redlich, 1990; Attneave, 1954; Barlow, 1961). The retina is one of the most studied highly adaptive neural circuits, in which the mapping between stimuli and neural response changes to match the statistics of the mean light intensity (Shapley & Enroth-Cugell, 1984), temporal and spatial contrast and spatial scale (Baudoin et al., 2007; Chander & Chichilnisky, 2001), and pattern distributions with tunable amounts of skewness and kurtosis (Srinivasan et al., 1982), and contrast adaptation in the vertebrate and fly visual systems (Brenner et al., 2000; Chander & Chichilnisky, 2001; Laughlin, 1981; Shapley & Victor, 1979; Smirnakis et al., 1997; Victor, 1986) have been characterized as gain-control mechanisms that serve to efficiently encode the variation of the stimulus around the mean into a limited dynamic range of firing rates at the output. It has been further shown that neural systems adapt not only to various stationary stimuli, but also to dynamic changes in stimulus distributions taking place across multiple timescales (Fairhall et al., 2001; Ulanovsky et al., 2004; Wallach et al., 2008).

Despite its ubiquitous presence, it is still not clear what are the limits to adaptation, and in particular, which stimulus changes should lead to adaptive responses and which should not. Moreover, by its nature, adaptation comes with an inherent caveat or cost (Fairhall et al., 2001): adaptive code is ambiguous, which requires the decoder to keep some knowledge of the coding context. Since most studies of adaptation analyzed neural systems’ response to first- and second-order spatio-temporal statistics in the stimulus, we addressed here the nature of neural response to changes in higher-order structure of visual stimuli; such higher-order structure is characteristic of natural scenes (Geisler, 2008; Simoncelli & Olshausen, 2001) and is perceptually salient (Chubb et al., 2004; Portilla & Simoncelli, 2000; Tkacik et al., 2011).

To characterize adaptation and invariance to stimulus statistics beyond luminance and contrast, we studied retinal responses to spatially uniform stimuli where light intensities were drawn independently from distributions with tunable amounts of skewness and kurtosis. We analyzed salamander retinal ganglion cell responses

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using maximally informative dimensions, and quantified the encoding properties of the neurons using 2D linear-nonlinear (LN) models. We found clear signatures of contrast adaptation in the rescaling of nonlinearities to these stimuli, but also that the same neurons display striking encoding invariance to changes in stimulus skewness or kurtosis, even when they are exposed to strongly bimodal stimulus distributions.

II. MATERIALS AND METHODS

Natural image statistics. To sample the range of naturally occurring values for contrast, skewness and kurtosis, we took a sample of 501 calibrated grayscale images from the Penn Natural Image Database (PNIDb) (Tkacik et al. 2011). From each image we selected 400 random patches each 200×200 pixels in size, which corresponds in area to the angular size of about 3 degrees, roughly the size of the center receptive field of a salamander retinal ganglion cell. Averaging over each patch to get the mean luminance in that patch, we computed the contrast, skewness and kurtosis of the distribution of patch luminances in a given image. Repeating the process over all images in our selection (containing shots of Baobon habitat in Okavango delta in Botswana, including landscape images, some with horizon, closeups of the ground, and a small selection of man-made objects in that habitat), we accumulated natural distributions of contrast, skewness and kurtosis.

In our analyses, contrast is defined as $C = \sigma_L/\mu_L$, where $L$ is the mean luminance, $\sigma_L = \sqrt{\langle (L - \bar{L})^2 \rangle}$ is the std of the luminance distribution $P(L)$ and brackets denote averaging over this distribution; skewness $S = (\langle (L - \bar{L})^3 \rangle/\sigma_L^3); \text{ and kurtosis } K = ((L - \bar{L})^4/\sigma_L^4 - 3$. Note that kurtosis is defined to be 0 for Gaussian distributions.

Electrophysiology. Multi-electrode array recordings were performed on adult tiger salamander (Ambystoma tigrinum) (Meister et al. 1994). All experiments were done according the regulation of Ben Gurion University of the Negev and the laws of the State of Israel. Prior to the experiment the salamander was adapted to bright light for 30 minutes. Retinas were isolated from the eye and peeled from the sclera together with the pigment epithelium. Retinas were placed with the ganglion cell layer facing a multielectrode array with 252 electrodes (Ayaio Biosystems, Switzerland) and superfused with oxygenated (95% O2, 5% CO2) Ringer medium which contained 110mM NaCl, 22mM NaHCO3, 2.5mM KCl, 1mM CaCl2, 1.6mM MgCl2, and 18mM glucose, at room temperature. The electrode diameter was 10μm and electrode spacing varied between 40 and 80 μm. Recordings of 24-30 hours were achieved consistently. Extradurally recorded signals were amplified (MultiChannel Systems, Germany), digitized at 10 kHz on four personal computers and stored for off-line spike sorting and analysis. Spike sorting was done by extracting from each potential waveform the amplitude and width, followed by manual clustering using an in-house program written in MATLAB.

Stimulation. The stimulus was projected onto the salamander retina from a CRT video monitor (ViewSonic G90H) at a frame rate of 60Hz such that each stimulus frame was presented twice in a row (for a stimulus sampling rate of 30Hz) using standard optics. The stimulus intensity was presented in grayscale and was gamma corrected for the monitor. Gaussian stimulus distributions with the desired variance were generated using MATLAB random number generator. We refer to all non-Gaussian stimuli as HOS (higher-order statistics) stimuli, which we generated with the statistics given in Table I as follows. The kurtotic distributions were sums of two equal-variance Gaussian distributions of equal weight and displaced means. The skewed stimuli are sums of two Gaussian distributions with unequal variances. All resulting distributions have the same mean luminance of $\bar{L} \approx 225$ lux.

We performed two experiments. In the first (23 cells), all 9 stimuli were displayed in long, non-repeated sequences (52202 frames of 33.33 ms each for each of the 9 stimuli), allowing us to infer LN models precisely; we used the Gaussian stimulus to fit LN models using both the spike-triggered average / covariance and maximally informative dimensions, to check how closely the two inference methods agree. In the second experiment (40 cells), the two Gaussian stimuli were absent, while for the 7 remaining HOS stimuli each non-repeated sequence was followed by a repeated sequence (30 repeats, 602 frames at 33.33 ms for each repeat), used to validate our models.

| Stimulus $S$ | symbol | contrast $C$ | skewness $S$ | kurtosis $K$ |
|-------------|--------|-------------|-------------|-------------|
| Gaussian    | $C+$   | 0.097       | 0           | 0           |
|             | $C+$   | 0.177       | 0           | 0           |
| Skewed      | $S-$   | 0.170       | -1.9        | 5.1         |
| (HOS)       | $S-$   | 0.172       | -1.0        | 6.0         |
|             | $S+$   | 0.175       | 1.0         | 5.2         |
|             | $S+$   | 0.178       | 1.9         | 5.2         |
| Kurtotic    | $K-$   | 0.177       | 0           | -1.8        |
| (HOS)       | $K-$   | 0.176       | 0           | -0.9        |
|             | $K+$   | 0.173       | 0           | 5.3         |

TABLE I Stimuli $S$ used in the experiment (see main text for the definition of the statistics $C, S, K$). The shorthand symbol for the stimulus starts with the C/S/K (for contrast, skew, kurtosis) and is followed by $--, +, +, +, +, +, +, +$ (small magnitude and negative, large magnitude and negative, small magnitude and positive, large magnitude and positive); therefore, $S = \{C+, C++, S--, S-, S+, S++, K--, K-, K+\}$. Parameters in the table denoted in bold were varied in each of the three stimulus categories.

Linear filters. In inferring LN encoding models, reverse correlation techniques cannot directly be applied to non-Gaussian stimuli because they lead to biased filter estimates. Instead, we used maximally informative dimensions (MID) (Sharpee et al. 2004). To look for a single significant filter $k_1$, one performs the following maximization over possible linear filters $k_1$, constrained to unit norm ($\|k_1\cdot k_1\| = 1$):

$$I_{\text{spike}} = \max_{k_1} D_{KL}(P(k_1 \cdot \text{spike}) \| P(k_1 \cdot 0) . \tag{1}$$

Here $D_{KL}$ is the Kullback-Leibler divergence (Cover & Thomas 1991) between the spike-triggered distribution and the prior distribution of stimulus fragment projections onto $k_1$, and $a$ are stimulus fragments (those preceding the spike for the spike-triggered distribution, and all fragments for the prior distribution). To look for 2D models, we repeated the same optimization with two filters $\{k_1, k_2\}$; the spike-triggered and prior distributions are two-dimensional in this case. For all neurons, the single most informative filter $k_1$ was contained in the space of the 2 filters $\{k_1, k_2\}$; for further analysis, we rotated the system of reference such that the first filter was the single most informative filter $k_1$ (which mostly corresponded to the spike-triggered average for those cells that were exposed to Gaussian stimulus), while the second filter $k_2$ spanned the $\{k_1, k_2\}$ subspace together with $k_1$, and formed an orthonormal basis, $k_1 \cdot k_2 = 0, k_2 \cdot k_2 = 1$.

The filters extended over 600 ms and were sampled on 36 equidistant points, with temporal resolution of 16.67 ms. We expressed the filters as a combination of 16 basis functions, $k_{1,2} = \sum_{\mu=1}^{16} a_{\mu,1} b_{\mu,2}$, where $b_{\mu}$ are unit-area Gaussian bumps with 40 ms
width, uniformly tiling the 600 ms span of the filters, and \( \alpha \) are the expansion coefficients; we maximized \( I_{\text{spike}} \) in the space of parameters \( \alpha \). This expansion made the filters smooth and very slightly improved generalization performance, but the results were stable even if we inferred directly in the space of \( k \).

For performance reasons we estimated \( D_{KL} \) during MID optimization runs using kernel-smoothing estimation; for final results we used the context-weighted-tree (CTW) estimator \( [\text{Sadeghi} 2009] \), the two estimators agreed without bias and to within 4% for final filters across all cells and stimuli. Optimization was done using custom stochastic gradient descent code that can avoid local maxima. We performed two optimization runs for each cell and each stimulus, and the values of information per spike between the two runs differed by 1% on average, 98.6% of the runs had a difference smaller than 5%.

To quantitatively compare the shapes of the filters across stimuli in experiment 1, we needed to ensure that each stimulus condition had enough spikes for good filter inference. We required each cell to have an average firing rate of at least 1.5 Hz; 15 out of 23 cells passed this cut. In experiment 1 we displayed Gaussian stimuli in addition to HOS stimuli, and we computed spike-triggered averaged average / covariance to extract STA and the next most significant filter (orthogonal to the STA) from Gaussian segments. To judge the significance of the eigenvectors in the STC analysis we used bootstrapping with subsets of recorded spikes following \( [\text{Bialek & de Ruyter van Steveninck} 2005] \).

Nonlinearities and PSTH prediction. After having reconstructed the linear filters \( \{k_1, k_2\} \), we estimated the nonlinearities as follows: \( N(v_1, v_2) = f \cdot P(v_1, v_2|\text{spike})/P(v_1, v_2) \), where \( v_{1,2} = k_{1,2} \cdot s \) are the projections of the stimulus onto the two linear filters, and \( f \) is the mean firing rate of the neuron in a given stimulus condition. For 2D nonlinearities, we binned \( \{v_1, v_2\} \) values on a 16 × 16 grid; for estimating 1D projections of the full 2D nonlinearity, we binned into a number of bins that was adaptively dependent on the number of spikes, and used kernel smoothing to approximate the probability distributions. Prediction performance was only slightly changed when 2D nonlinearities were sampled over 32 × 32 domain, and in general dropped due to overfitting when 64 × 64 bins were used. We used 2D LN models fit on the nonrepeated segment of the stimulus to predict the PSTH for the repeated segments, using the time resolution of 16.67 ms, half the stimulus refresh rate. The fit was quantified by computing the Pearson cross-correlation between the true and predicted PSTH.

Information captured by the models. In the framework of LN encoding models, one assumes that only a small number \( K \) of linear projections \( \{v_1, v_2, \ldots, v_K\} \) of a high-dimensional stimulus \( s \) determine whether a neuron spikes or not \( (\text{Agüera y Arcas & Fairhall 2003}) \). In other words, the neuron is viewed as implementing a probabilistic dependency chain: \( s \rightarrow \{v_1, v_2, \ldots, v_K\} \rightarrow N(v_1, v_2, \ldots, v_K) \rightarrow \text{spike} \), which implies a chain of information processing inequalities: \( I_{\text{spike}}(s; \text{spike}) \geq I_{\text{spike}}(v_1, v_2, \ldots, v_K; \text{spike}) \geq I_{\text{spike}}(N(v_1, v_2, \ldots, v_K); \text{spike}) \). It is possible to estimate \( I_{\text{spike}}(s; \text{spike}) \) from repeated presentations of the same stimulus. If \( r(t) = (\sum_{\mu=1}^{N(\rho)} \delta(t - t_{\mu}) \text{repeats}) \) is the time-dependent firing rate, where \( \rho = 1, \ldots, R \) indexes the repeats, \( t_{\mu} \) is the time of \( \mu \)-th spike in repeat \( \rho \), and \( t \in [0, T] \) denotes time within the repeat of length \( T \), the estimate for true information per spike is given by \( [\text{Brenner et al. 2009}] \):

\[
I_{\text{spike}}^{ub} = \frac{1}{T} \int_0^T dt \frac{r(t)}{\bar{r}} \log_2 \frac{r(t)}{\bar{r}},
\]

where \( \bar{r} = 1/T \int_0^T dt \ r(t) \) is the average firing rate across the repeated stimulus segment. This quantity is an upper bound to the information quantities defined above for LN models. The fraction, e.g. \( I_{\text{spike}}(v_1, v_2; \text{spike})/I_{\text{spike}}^{ub} \) (between 0 and 1), tells us how well the two stimulus projections capture the full dependence of spiking on the stimulus. Similarly, \( I_{\text{spike}}(N(v_1, v_2); \text{spike})/I_{\text{spike}}^{ub} \) (which needs to be lower or equal to the information in the two projections for the same neuron and stimulus) quantifies how much information is further lost when compressing the description of spike-dependence from two projections into a single nonlinear combination.

The information was estimated from Eq 2 with rates computed in 16.67 ms bins (matching the time resolution of the temporal filters and the sampling used to calculate \( D_{KL} \) in Eq 1), and was corrected for small-sample bias by repeatedly estimating the information on random subsets of stimulus repeats of varying sizes, plotting the information estimates against 1/\( N_{\text{repeats}} \) and extrapolating to infinite number of repeats; we also applied the correction for the difference between mean firing rates in the repeated and non-repeated stimulus segments \( [\text{Fairhall et al. 2006}] \). The expected extrapolation error is below 1%. To obtain an upper bound for the systematic error due to short repeat length, we split the repeated segment in half and estimated the information separately on each half, which resulted in relative differences with a std of 8%; we expect the true error to be smaller. Information rates were estimated by computing the information per spike and multiplying by the mean firing rate.

For all neurons recorded in experiment 2 (with non-repeated and repeated stimuli), we computed several information-theoretic quantities: (i+ii) \( I_{\text{spike}}(v_1, v_2; \text{spike}, S)/I_{\text{spike}}^{ub}(S) \) is the information fraction captured by 2 (and 1, respectively) linear filter(s), fit separately to each stimulus condition \( S \); (iii+iv) \( I_{\text{spike}}(N(v_1, v_2; \text{spike}, \text{global})/I_{\text{spike}}^{ub}(S) \) are the fractions captured by the nonlinear combination of 2 (and 1, respectively) projection(s) fit separately to each stimulus condition \( S \); (v+vi) \( I_{\text{spike}}(v_1, v_2; \text{spike}, \text{global})/I_{\text{spike}}^{ub}(S) \) and \( I_{\text{spike}}(N(v_1, v_2; \text{spike}, \text{global})/I_{\text{spike}}^{ub}(S) \) are the fractions captured by a single 2D model (by two projections and their nonlinear combination, respectively) that has been fit globally to all stimulus stimuli \( S \). These quantities were all estimated using CTW estimator for Kullback-Leibler divergence. When estimated on spike trains that have been shuffled with respect to the stimulus, the estimator yields negligible values below \( 10^{-3} \) bits.

Predicted information rate of LN models. To computationally simulate the effect that the (lack of) adaptation would have on the information rate when the stimulus statistics changes, we used the LN models inferred at high contrast C++ to predict the firing rate \( r(t) \) for stimuli with contrasts \( C < C++ \) and ask how much information such neurons would carry per spike in the absence of any adaptation. This information in the predicted rate, \( I_{\text{rate}} \), was evaluated using Eq 2 and expressed as a fraction of information captured by the two relevant filters (which does not depend on contrast and only serves as a normalization). We similarly asked how the same quantity would behave when the global models (single LN models for all cells that are fit across all stimuli, and therefore have no adaptation) were used to encode information into the rate for each of the skewed stimuli.

III. RESULTS

To characterize how the retina encodes higher-order statistics (HOS) of the luminance distribution, we presented it with a set of 9 synthetic spatially homogenous stimuli \( S \), where the light intensity of each stimulus frame was drawn independently from distributions \( P_S(L) \) that were matched in mean \( \bar{L} \) (see Materials and Methods). The stimuli differed systematically in contrast, skewness, and kurtosis, as depicted in Fig 1H. The particular values
were chosen to span the range of skewness and kurtosis which are found in natural scenes, as shown in Fig. 2A-E. To span these ranges, contrast values $C$ had to be chosen in the low range, due to the hardware limitations of the stimulus display.

To quantify how retinal neurons change their code when contrast, skewness, or kurtosis of the stimulus change, we constructed accurate encoding models for the recorded neurons, and compared their properties under the different stimuli. We thus followed [Fairhall et al. 2003], who have shown that for spatially uniform Gaussian stimuli in the salamander retina, linear-nonlinear (LN) models with one or two linear filters often suffice to describe the cells’ encoding scheme with high accuracy. Moreover, [Agüera y Arcas & Fairhall 2003] and Bialek & de Ruyter van Steveninck (2005) also provided an interpretation of the filtering operations as dimensionality reduction on the stimulus space, the success of which can be quantified with information theory. Here we extended their framework to non-Gaussian stimuli and analyzed how information is encoded beyond linear filtering stage, in the nonlinear response, and finally in the spiking rate. We could then characterize adaptation and invariance quantitatively, and compare the behavior of real neurons with computational models that either have or lack adaptation.

1. Linear filters of retinal ganglion cells do not adapt to changes in higher-order stimulus statistics

We recorded from 23 retinal ganglion cells that were presented with 9 types of non-repeated stimuli (2 Gaussian + 7 higher-order statistics) in experiment 1, and from 40 cells presented with non-repeated and repeated stimuli of 7 types with higher-order statistics (see Materials and Methods) in experiment 2. Figure 2A shows the estimated information rate of the neurons as a function of their firing rate. Consistently with previous reports [Balasubramanian & Sterling 2009], the information rate $I$ scaled weakly sub-linearly with the mean firing rate $\bar{r}$ ($I \propto r^{0.76}$). There were no other large systematic dependencies in transmitted information across cells and stimulus classes.

Next, we inferred the best linear filters for each cell, and each of the stimulus condition $S$, separately. We used maximally informative dimensions (MID) for learning the filters for all stimuli, and for the Gaussian stimuli we additionally used spike-triggered average and spiketriggered covariance. We also inferred a global model for each cell, where a single filter (or a single pair of filters) was fit across all stimulus conditions (see Materials and Methods). In cross-validation on test data, the prediction performance of the models of essentially all cells (97% of cell/stimulus combinations) increased when using two filters (2D LN models), compared to one-dimensional LN models, but in some cases the contribution of the second filter was very small. The linear filters inferred using MID for one of these cells are shown in Fig. 3B for 9 stimulus conditions; overlaid is the leading eigenvector of the spike-triggered covariance matrix computed for the C++ stimulus, and the best global filter learned by MID (all filters are scaled to unit norm). The filters show very strong overlap, indicating that their shape does not adapt to the stimulus distribution. We emphasize that computing the naive STA estimates gives a systematic change in filter shape with the stimulus skew, as shown in Fig. 3C, but this is simply an artifact of the STA estimation on non-spherically-symmetric stimuli, and is not indicative of any adaptation process.

Figures 3D-E show a typical cell for which a model with two linear filters is needed. We again observe a high overlap between the filters inferred using MID in 9 stimulus conditions, the filter pair computed using STC in the Gaussian condition, and the single global best pair of filters inferred across all conditions using MID. 15 of the 23 cells in experiment 1 have an average firing rate above 1.5 Hz for every stimulus, permitting reliable filter estimation. Out of those, a single-filter model in the Gaussian condition suffices for 8 cells (i.e. the single-filter model accounts for more than 90% of the information per spike of the two-filter model), and for 7 cells two filters are needed. To measure the agreement between inferred filters across conditions for each cell, we compute the Pearson cross-correlation between the STC derived filter(s) in the Gaussian condition, and the filters derived using MID for each stimulus condition $S$. The average correlation across the group of cells with a single linear filter is 97% ± 2%, while the average correlation across the group of cells with 2 filters is 86% ± 5% (error bar = std across cells); the decrease in the later case is mainly attributable to the difficulty of inferring jointly 2 filters using MID with a limited number of spikes.

We quantified the effects of changing the higher-order statistics on the shape of the linear filters by computing the balance index $b$, defined as the ratio between the total (signed) area under the filter and the absolute area: $b = \sum k_\mu/\sum |k_\mu|$, where $\mu$ indexes the temporal components of the filter. The balance index across the recorded population was $b = -0.0350 \pm 0.13$ (n=40 cells from experiment 2), where the mean and error bar (std) are taken across all cells, conditions and both filters. Broken down across conditions, there is a small systematic modulation of $b$ with the stimulus, which is smaller than 10% (Fig 4); additionally, there is substantial scatter across the recorded population.

To ask whether these slight variations in filter shape across stimuli matter for encoding, we compared the performance of global filters (constant for each cell across all the stimuli) with filters inferred separately for each stimulus. We estimated the information captured by the single-filter model, by a two-filter model, and by a two-filter global model (where a single pair of two filters is inferred for all stimuli for each cell). Single-filter models (fit to each stimulus separately) captured 69% ± 12% of the information per spike (averaged across cells and stim-
FIG. 1 Synthetic stimuli used to probe salamander retinal ganglion cells. The probability densities, $P_S(L)$, for all 9 stimuli $S$ used, grouped into 3 categories (cyan = Gaussian, magenta = skewed, and yellow = kurtotic). All stimuli are matched in mean (225 lux), and all except for C+ have the same contrast; for details, see Table I.

FIG. 2 Higher-order statistics in natural scenes. A,B) Two example images from the Penn Natural Image Database. The grayscale images are calibrated into units of cd/m$^2$. The yellow circle represents the typical size of the salamander retinal ganglion cell center. Luminance was averaged in patches of this size, and contrast ($C$), skewness ($S$) and kurtosis ($K$) were computed for the distribution over many patches from each image. The distributions $P(L)$ for the two example images are shown as insets, and the corresponding values for $C,S,K$ are displayed in the two image panels. C,D,E) The distribution of contrast, skewness and kurtosis, respectively, over 501 natural images. Colored squares represent the values of the three parameters used in synthetic stimuli (color coded as in Fig 1). 2 cyan stimuli differ in contrast $C$ but have constant $S$ and $K$; 4 magenta stimuli differ in skew $S$ but have constant values of $C$ and $K$; and 3 yellow stimuli differ in kurtosis $K$ but have constant $C$ and $S$ (see Table I).
FIG. 3 Linear filters and higher-order statistics stimuli in retinal ganglion cells. A) Estimated information rate (see Methods) as a function of the mean firing rate. Each dot represents one of the 40 cells in experiment 2 exposed to one of the 7 HOS conditions (skewed stimuli in magenta, kurtotic in yellow). The growth in information is slightly sublinear, with no obvious systematic dependence on the stimulus type. B) A cell whose behavior is captured well by a single linear filter. Shown in light blue are the filters for all 9 (2 Gaussian, 7 HOS) stimuli reconstructed using maximally informative dimensions; in black the spike-triggered average computed on the Gaussian stimulus C++; in red, a single global filter inferred using MID across all stimuli conditions simultaneously. C) Biased STA filter estimates for 5 skewed stimuli (thicker lines mean increasing skewness) for the same cell as in B (note the difference in the time axis). D,E) A cell whose behavior is described well by two linear filters (light blue = the most informative dimension; dark blue = the second most-informative dimension). Other symbols the same as in B). F) Information captured by two filters (across stimuli, horizontal axis), as a fraction of the total information per spike; mean and std across 40 cells in experiment 2. The average performance of global models (the same pair of filters across all stimuli for each cell) is plotted as red squares.

and kurtosis vary across the range observed in natural scenes.

2. Nonlinearities of retinal ganglion cells responding to higher-order statistics stimuli

Completing the LN description of the ganglion cells is the mapping from the linear projection(s) of the stimulus into the cell’s firing rate. We estimated these 2D nonlinear functions from the data by binning \( P(v_1, v_2|\text{spike}) \), where \( v_i = k_i \cdot s \) are the projections of the stimulus onto the two filters, \( k_1, k_2 \), as explained in Materials and Methods. This was done for each neuron and each condition separately, or for all conditions jointly using the global pair of filters, to yield a single 2D global LN model for every cell. Figure 5A shows a global nonlinear function for an example neuron. In Fig. 5B we explicitly show, for that same neuron, the prior ensembles for all 7 higher-order statistics stimuli (gray), with overlaid spike-triggered ensembles for skewed (magenta) and kurtotic (yellow) stimuli, along with the marginal projections of these distributions. The number of spikes is in general insufficient to reliably sample and then systematically compare the 2D nonlinear functions across cells and stimuli. We therefore decided to base our comparisons directly on the firing rate prediction performance. The 2D models for cells in experiment 2 are fit on the non-repeated segments, and are subsequently tested by predicting PSTH in response to repeated stimulus presentations for which we could measure the true PSTH; here, too, the prediction was done either with models fit separately at each condition, or with the global model, where 2 linear filters and the nonlinearity were fit simultaneously across all stimuli, as shown in Fig. 5C.

FIG. 4 The dependence of the balance index on the stimulus type. The balance index \( b \) is a ratio between the total (signed) area under the filter, normalized by the absolute area; balanced filters have \( b = 0 \), fully unbalanced \( b = \pm 1 \). Shown are averages (±1 std error bars) for 40 cells in experiment 2, computed across both linear filters for each cell.
sparse K+ stimulus condition (where the spike rate is the lowest); there was essentially no drop for other stimulus conditions in performance of global vs. separate models. Our simulations show that the limitations to the performance of LN-based models in predicting the firing rate are due to the inability of these models to capture the refractory and spike-feedback effects (which would be possible with e.g. generalized linear models (Pillow et al., 2008) or Keat-type models (Keat et al., 2001)).

We reiterate, however, that the prediction performance was used here solely as a differential measure, to evaluate the significance of the changes in linear filters and nonlinearities with the stimulus condition.

Finally, we can ask how successfully the global models recapitulate the overall firing rate changes with the stimulus statistics. Figure [A] shows the relative change in firing rates for cells from experiment 2 for 7 HOS stimuli; the cells have been sorted to reveal the dominant pattern, where cells that prefer left-skewed stimuli respond less strongly to the other stimuli, while cells that respond strongly to right-skewed stimuli also respond to negative kurtosis. We can use a global 2D LN model fit for every cell to predict the mean firing rate in response to all of the 7 stimuli. These models (without any adaptation) reproduced very well the mean firing rate for each stimulus and cell, as depicted in Fig. [B], and therefore also the pattern of changes in the firing rate (not shown).

3. Adaptation to changes in contrast and invariance to changes in higher-order statistics

We observe that the encoding properties of salamander ganglion cells do not depend on the higher-order statistics of the luminance levels. To establish this, we compared the shape of linear filters across the stimulus conditions directly (by measuring their overlap), by information-theoretic measures (information per spike captured), and through the impact on the prediction performance; similarly, we assessed the changes in the nonlinearity by measuring their impact on the prediction performance. In all cases—with the possible exception of highly kurtotic (K+) stimuli—we found that global models, i.e. models with invariant pair of filters and invariant nonlinearity, account for the neural behavior equally well as the models fit to different stimuli separately. Since neurons are nonlinear dynamical systems coupled to the stimulus, we find this extent of invariance surprising—we expected that higher-order statistics in the stimuli would “interact” with the photoreceptor-bipolar-RGC cascade to yield a notable change in the effective encoding properties, especially for heavily skewed or bimodal stimuli.
when the stimulus contrast changes, retinal ganglion cells adjust their gain, matching the variation of the signal about the mean to the dynamic range of the firing rate at the output, thereby keeping the information rate high. Without adaptation, the information rate would drop because the neurons have a limited output range and they are noisy. “Noise” in the context of LN encoding models is the stochasticity related to the spike generation: from the stimulus $s$ to spike, $s \rightarrow \{v_1, v_2\} \rightarrow N(v_1, v_2) \rightarrow$ spike, it arises when the nonlinear function $N$ is interpreted as the mean firing rate of a Poisson point process. To explore the effects of the presence or absence of adaptation, we generated spikes according to this LN prescription in response to various stimuli, and measured the information in such synthetic spike trains using Eq. (2). By using the true inferred (adapting) models for low and high contrast, we found that in both conditions the real spiking neuron can retain $\sim 90\%$ of the information extracted from the stimuli by the linear filters. On the other hand, when using the model inferred at high contrast, holding it fixed (no adaptation), and probing it with stimuli of progressively lower contrast, the information rate dropped significantly, as shown in Fig. 7B. The situation is very different for skewness (or kurtosis): Fig. 7C shows that no such drop in information is observed when the global model is used to generate spikes in case of skewed stimuli, making adaptation unnecessary and invariant encoding possible.

This effect is easy to understand if we compare the extent to which the 9 stimulus distributions differ a priori, after filtering by the neuron’s linear filters, and after passing through the nonlinear function. Figure 8A shows a $9 \times 9$ matrix of the Kullback-Leibler distances $D_{KL}(p_j(s)||p_i(s))$ between all pairs of stimuli $i,j = \{C+,C++,S--,S-,S+,S++,K--,K-,K+\}$ (2 Gaussian, 7 higher-order statistics). The bimodal stimulus $K--$ is clearly distinct from the others. After linear filtering (Fig. 8B), however, the low contrast stimulus $C+$ differs the most from the others, which are all matched in contrast. Because linear filters, as we have shown, do not change in shape, this is simply a consequence of the central limit theorem: the filters sum up (with weights) samples drawn independently from the stimulus distributions $P_\mathbf{s}$, so the filter outputs must converge to Gaussian distributions with variances that are related to the variance (or contrast) of the input. In other words, the invariant linear filters remove the signatures of higher order statistics and “equalize” different stimuli with the exception of their contrast. In the last, nonlinear stage (Fig. 8C), the nonlinearity adapts to contrast as well, ultimately yielding LN model outputs whose distributions are very similar across the range of stimuli differing in contrast, skewness and kurtosis.

4. Should the linear filters adapt to changes in higher-order statistics?

We previously established that the retinal ganglion cells do not adapt their linear filtering properties to changes in stimulus skewness and kurtosis. Taking this invariance of linear filters as given, we next showed that linear filtering and contrast adaptation together can successfully remove the signatures of higher-order statistics from the distribution of neural firing rates. Here we re-
FIG. 7 The benefits of contrast and higher-order statistics adaptation. A) Inset. The 1D nonlinearity, $N(v_1)$, for an example neuron (E0C4) inferred at high contrast (C++, light blue), and at low contrast (C+, dark blue). The low contrast nonlinearity can be aligned to the high contrast one by (i) rescaling the stimulus (horizontal) axis by the ratio of the two contrasts, and (ii) rescaling the firing rate (vertical) axis by the ratio of the two average firing rates, yielding the red line. Main panel. Scatter plot of the nonlinearity at high vs nonlinearity at low contrast (black, 19 neurons from experiment 1; the coordinates of each point are the high / low C nonlinearity values at the same value of the projection $v_1$ for a particular neuron). After rescaling, the nonlinearities align (red). The scaling breaks down for rates above 30 Hz (rarely observed at low contrast). B) The information in the spiking pattern of a LN model neuron, normalized by the information captured by the two linear projections of the corresponding stimulus. Cyan circles = inferred models for 19 neurons for high and low contrast (C++, C+) stimulus. Green line = computational prediction obtained by taking 19 high contrast models and dialing down the stimulus contrast without any adaptation in the model (error bars = std across the neurons). C) Analogous analysis for changes in skewness (note the difference in scale); magenta = models inferred separately for each skewed stimulus; green = invariant (and therefore non-adapting) global models for every cell.

FIG. 8 Neurons with contrast adaptation yield similar distributions of firing rates in response to very different distributions of inputs. A) Kullback-Leibler distance matrix, $D_{KL}$ (bits), between all 9 pairs of stimulus distributions (cyan = 2 Gaussian, magenta = 4 skewed, yellow = 3 kurtotic distributions). Bimodal K-- distribution is most different from the others. B) The difference between the respective 2D linear projections of the 9 stimulus distributions (shown are the averages over $D_{KL}$ matrices for 19 neurons in experiment 1). Linear filtering of IID stimuli washes out most of the higher-order structure (but not the second order), and the most distinct stimulus type at this stage is C+, since its variance is different from the other distributions of projections. C) $D_{KL}$ (average over 19 neurons) between the nonlinear transformations of the respective linear projections. Since the nonlinearity adapts to contrast, this step equals the low contrast (C+) with the other stimuli.

turn to the observation of invariant linear filters to ask whether such invariance should be expected on theoretical grounds.

In a one-dimensional LN model neuron, the probabil-
ity of spiking was assumed to be a saturating nonlinear function of the filtered stimulus:

$$P(\text{spike}|s) = \frac{1}{2} \tanh(k(S) \cdot s + \theta(S)) + \frac{1}{2}, \quad (3)$$

where the linear filter $k$ and the spiking threshold $\theta$ may depend on the stimulus type $S$. We simulated spike sequences $\sigma$ of this model neuron in response to repeated presentations of the stimulus, whose value in each time bin was drawn independently from from $P_S(L)$: $\sigma(r, t) = \{0, 1\}$ was ‘0’ when the neuron was silent in time bin $t$ and during repeated presentation $r$ of the stimulus, and ‘1’ if it spiked. To quantify how well such a neuron encodes information about the stimulus into spike trains, we estimated the information rate $I$ (in bits per second) between the stimuli and the response, using the direct method (Strong et al., 1998).

For stimulus types $S$ of varying skewness, we found the optimal filter $k$ and the threshold $\theta$ that would maximize the information rate $I$ that the neuron would convey. If real neurons were adapting in such a way, this procedure would then predict how their filters would change with the stimulus distribution. For computational reasons, our model was simplified: (i) the linear filter was biphasic, with a “fast” lobe of amplitude $A_f$, and a “slow” lobe of amplitude $A_s$, whose widths and the positions were fixed, so the filter was fully specified by the two amplitude parameters $\{A_s, A_f\}$ as schematized in Fig. 9A; (ii) we maximized the information rate $I$ for a fixed average firing rate $r$; (iii) the effective noise of the neuron, or fraction of output entropy that is lost to noise, $\eta = S_{\text{noise}}/S_{\text{total}}$, was fixed.

Figure 9 shows the dependence of the information rate on the shape of the stimulus filter: left-skew distributions ($S--$) slightly favor OFF cells (negative fast lobe, positive slow lobe, Fig. 9B), while right-skew distributions ($S++$) slightly favor ON cells (not shown). This conclusion was robust to noise in the neuron $\eta$ ranging from $\sim 0$ to 0.5. For a specific choice of $\eta = 0.2$ in Fig. 9C, Fig. 9D shows the dependence of information rate on the ratio of the fast to slow lobe amplitude, $\tan \phi = A_f/A_s$. For each stimulus ($S++$ and $S--$), there are two local maxima, one for an ON-like and one for an OFF-like cell, which differ in the transmitted information by less than 10%. Importantly, however, the maxima are not achieved at the same value of $\phi$ in both stimulus conditions – this means that while an adapting ON or OFF cell can maintain the same rate of information transmission when the stimulus changes, it will need to modify the filter shape by adjusting the ratio $A_f/A_s$.

Focusing on the case of an OFF cell, we found that an optimally adapting cell would increase the area under the fast (negative) lobe and would decrease the area under the slow (positive) lobe with increasing skewness. We used the balance ratio $b$, introduced previously, to quantify this change. Figure 9E shows significant changes in the filter shape with skew that range from $b = 0.3$ for $S--$ to $b = -0.3$ for $S++$ (as expected, the optimal filter for the Gaussian stimulus is balanced ($b = 0$), with equal and opposite areas under the two lobes). However, these substantial changes in the filter shape only lead to moderate changes in the amount of encoded information: in the case shown in Fig. 9, the information gain of the adaptive neuron relative to the case of no adaptation is always less than 10%. While the exact number varies with the chosen constraints ($r, \eta$, the locations and widths of the filter lobes), two qualitative observations remain true: (i) the neurons should adjust the biphasic linear filter away from the balanced configuration (optimal for Gaussian stimuli) by systematically adjusting the weight under the fast and slow lobes so that, e.g. in case of the OFF cell, negative skew favors larger weight in the slow lobe; but also that (ii) these adaptive changes would only lead to small relative information gains.

IV. DISCUSSION

We explored the limits of retinal adaptation, by analyzing the responses of salamander retinal ganglion cells to temporally uncorrelated and spatially uniform stimuli with Gaussian, skewed and kurtotic luminance distributions. While the retina is highly adaptive to changes in first and second order statistics, we found invariance of neural encoding to changes in stimulus skewness and kurtosis in both the linear filtering stage and the nonlinear stage. [Bonin et al. (2008)] reported a similar result in the cat LGN for spatially structured stimuli, using 1D LN models inferred using reverse correlation; we see an analogous invariance to skew and kurtosis for spatially uniform stimuli in the retina, for 2D models inferred using a theoretically unbiased method, while exploring a substantially wider range of skewness and kurtosis values. Taken together, these results suggest that adaptation in the early visual system is not sensitive to changes in commonly measured higher-order statistics.

From an information optimization point of view it is not immediately clear why the retina does not adapt to such higher-order changes. Moreover, since neurons are nonlinear dynamical systems coupled to their inputs, a large change in the statistical structure of the input would, on general grounds, be expected to influence the neuron’s effective encoding properties, even if it did not lead to an increase in information transmission. Thus, invariant encoding in the face of substantial changes in the stimulus statistics is not an obvious a priori expectation.

Adaptive code is necessarily ambiguous. The same response from an adapting neuron can, for example, signal two different light intensities, depending on the stimulus history. Downstream neurons must therefore rely either on keeping track of the adaptive state of the encoding neuron, or on using diversity in the neural population in a proper way to estimate the stimulus. Moreover, non-trivial processing is required also on the encoding side: the adaptive neuron needs to infer from the stimulus itself whether some underlying property of the stimulus...
FIG. 9 Finding optimal filters for an LN model neuron for stimuli with negative skew (S--). A) The biphasic filter with two parameters determining the amplitudes of the fast and slow lobes, \( \{A_f, A_s\} \). Each of the amplitudes can be positive or negative. When \( A_s \) is positive and \( A_f \) is negative, the cell is an OFF cell; when \( A_s \) is negative and \( A_f \) is positive, the cell is an ON cell. B) Information about the stimulus encoded in the spike train (bits per second, color scale), as a function of the fast lobe amplitude \( A_f \) and the slow lobe amplitude \( A_s \). The ON and OFF types have been denoted in the 2 corresponding quadrants of the plot. C) Fraction of entropy lost to noise, \( \eta \), as a function of \( \{A_f, A_s\} \). Points in the plane that have \( \eta \sim 0.2 \) are shown in white, and lie on a circular locus of points; we are only interested in the models with fixed value of \( \eta \). We parametrize such points by their angle, \( \phi \); these values are extracted from B) along the \( \eta = 0.2 \) contour. Green points correspond to ON cells, cyan points to OFF cells. There are two peaks in information, one (slightly higher) peak for the OFF type cell and one for the ON type cell. In all plots, the optimal OFF cell is denoted by a magenta dot. D) Information on the locus of points \( \eta \sim 0.2 \) as a function of \( \phi \); these values are extracted from B) along the \( \eta = 0.2 \) contour. Green points correspond to ON cells, cyan points to OFF cells. There are two peaks in information, one (slightly higher) peak for the OFF type cell and one for the ON type cell. In all plots, the optimal OFF cell is denoted by a magenta dot. E) Theoretical prediction for the shape of the optimal biphasic OFF filters for stimuli with different skewness values. As skewness increases from negative (S--, green) to positive (S++, blue), the negative lobe becomes more prominent and the positive lobe becomes less prominent. For the symmetric Gaussian stimulus (C++, red) the optimal filter is balanced. These changes are quantified by the balance index \( b \) (see text), which measures the difference in area between the lobes, normalized to the total absolute area under the filter. For the simulations in this figure, the stimulus refresh time is 10 ms and mean firing rate is held fixed at 5 Hz (results are qualitatively unchanged for rates up to fourfold higher).

(such as the mean luminance or contrast) has changed and thus an adaptive response needs to be triggered (but c.f. also [Borst et al. 2005]). In short, adaptive codes incur computational costs that invariant codes do not.

These considerations suggest that there exist changes in stimulus statistics for which the benefits of adaptation outweigh the costs. It also implies the existence of changes where the encoding properties should remain invariant, even if other equally good encoding strategies were available to the cell, thereby making the code easy and unambiguous to decode. Such changes would be those where, even without adaptation, the information rate would not drop precipitously when the stimulus distribution changes.

Our results lead us to believe that an encoding model with non-adapting linear filter(s) and a nonlinearity, which adapts to contrast but not to higher-order statistics, is an efficient strategy that reduces the inherent ambiguity in the code. Contrast adaptation is necessary to prevent a severe drop in the information rate after a contrast change. If in addition the linear filters are invariant, the filtering, together with the central limit theorem, can remove higher-order statistics. This would leave the luminance and the contrast as the only target statistics for adaptation, while simultaneously maintaining a high information rate and minimizing the code ambiguity.

We did not observe any adaptive changes in the filter shape either for skewed and kurtotic stimuli, or after the change in contrast. Small changes in filter shape have been previously reported by [Smirnakis et al. 1997] in response to large changes in contrast, beyond the values we used here (“faster” filters at high contrast values). It is not clear how one could assess the cost of adding an adaptive mechanism that modifies the retinal ganglion cell filters for higher-order statistics; we can ask, however, how much information would be gained by it. Our toy model simulations show that while it would be theoretically possible to increase the transmitted information by adjusting the shape of the linear filter to the stimulus, the gains in information would be very modest (around 10% for a robust range of realistic parameter choices, much less than the gain due to contrast adaptation), despite significant changes in the shape of the optimal linear filter.

One explanation for the lack of dynamic adaptation to higher-order statistics is therefore that it does not yield much gain in information, while potentially increasing the coding cost and complexity. It is possible, then, that instead of implementing an adaptation mechanism able to dynamically change the filter shape on an individual cell basis in response to stimulus skew, the neural population is structurally adapted to the overall luminance distribution of natural scenes, by properly partitioning the population between ON- and OFF-like cells [Ratliff et al. 2010].

Another explanation for invariant coding in response to higher-order statistics could be that the ability to adapt is limited by the ability to detect a change in the underlying statistical structure of the stimulus. For example, to detect reliably a change in kurtosis, the neuron...
would need to receive some minimal number of independent stimulus samples, but this minimum might still be large, making such inferences hard. More fundamentally, it is not clear what are the actual statistics that the neurons are adapting to. Perhaps then, the retina (and other neural systems) may be using other estimators for contrast-, skew-, and kurtosis-like statistics?

Some of these important issues could be addressed by extending our analysis either by using temporally correlated stimuli, or by heavy-tailed (or naturalistic) luminance histograms – if they can be reproduced in the lab using display hardware with a larger dynamic range. Both of these extensions would affect the central limit theorem argument above: in the case of temporally correlated stimulus, the samples would no longer be independently drawn and thus might not (quickly) converge to a Gaussian; in the second case, the linear filter will not be able to “erase” the signatures of higher-order statistics, should the decay of the luminance distribution be too shallow. As both extensions would bring the stimuli closer to the true naturalistic ones, they could provide us with a more complete window into the nature of retinal adaptation to natural scenes.

Acknowledgments

We thank Vijay Balasubramanian, Kristina Simmons, and Jason Prentice for stimulating discussions. GT wishes to thank the faculty and students of the “Methods in Computational Neuroscience” course at Marine Biological Laboratory, Woods Hole. This work was supported by The Israel Science Foundation and The Human Frontiers Science Program.

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