Variable stars in the Magellanic Clouds: II. The data and infrared properties

Yoshifusa Ita\textsuperscript{1,2,}\textsuperscript{*}†, Toshihiko Tanabé\textsuperscript{1}, Noriyuki Matsunaga\textsuperscript{1}, Yasushi Nakajima\textsuperscript{3}, Chie Nagashima\textsuperscript{3}, Takahiro Nagayama\textsuperscript{4}, Daisuke Kato\textsuperscript{4}, Mikio Kurita\textsuperscript{4}, Tetsuya Nagata\textsuperscript{4}, Shuji Sato\textsuperscript{4}, Motohide Tamura\textsuperscript{3}, Hidehiko Nakaya\textsuperscript{5} and Yoshikazu Nakada\textsuperscript{1,6}

\textsuperscript{1}Institute of Astronomy, School of Science, The University of Tokyo, Mitaka, Tokyo 181-0015, Japan
\textsuperscript{2}Institute of Space and Astronautical Science, Japan Aerospace Exploration Agency, Sagamihara, Kanagawa 229-8510, Japan
\textsuperscript{3}National Astronomical Observatory of Japan, Mitaka, Tokyo 181-8588, Japan
\textsuperscript{4}Department of Astrophysics, Nagoya University, Chikusa-ku, Nagoya 464-8602, Japan
\textsuperscript{5}Subaru Telescope, National Astronomical Observatory of Japan, 650 North A’ohoku Place, Hilo, HI 96720, U.S.A.
\textsuperscript{6}Kiso Observatory, School of Science, The University of Tokyo, Mitake, Kiso, Nagano 397-0101, Japan

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ABSTRACT
The data of 8,852 and 2,927 variable stars detected by the OGLE survey in the Large and Small Magellanic Clouds are presented. They are cross-identified with the SIRIUS \textit{JHK} survey data, and their infrared properties are discussed. Variable red giants are well separated on the period-\textit{J}–\textit{K} plane, suggesting that it could be a good tool to distinguish their pulsation mode and type.

Key words: galaxies: Magellanic Clouds -- stellar content -- stars: AGB and post-AGB -- variables -- infrared: stars -- surveys

1 INTRODUCTION
Because of their proximity and comparatively well-known distances, the Large and Small Magellanic Clouds (LMC and SMC, respectively) are the ideal places to study stellar evolution. To search for the gravitational lensing events, several projects are now underway monitoring the sky toward the Magellanic Clouds and also the Galactic bulge, where there are a large number of background stars that are potential targets for microlensing. As the natural by-products of these surveys, many variable stars were newly found. The Optical Gravitational Lensing Experiment (OGLE) project is one of such surveys and its \textit{I} band time-series data in the Magellanic Clouds (\textsuperscript{1}Zebru\textsuperscript{2}n et al. 2001) obtained during four years of OGLE-II run (Udalski, Kubiak & Szymanski 1997; January 1997 - November 2000) is now available over the Internet (OGLE homepage: http://sirius.astrouw.edu.pl/~ogle/).

To detect dust-enshrouded variables that have possibly escaped from the ongoing/previous optical projects, we started the \textit{JHK} monitoring survey toward the Large and Small Magellanic Clouds using the InfraRed Survey Facility (IRSF) at the South African Astronomical Observatory Sutherland station. The IRSF consists of a dedicated 1.4m telescope to which is attached a near infrared (NIR) camera SIRIUS, which can observe the sky in the three wave bands (\textit{JHK}_\textsubscript{s}) simultaneously. The filter characteristics are shown in table \textsuperscript{1} The field of view of this system is about 7.7'×7.7' with a scale of 0.453''/pixel. Details of the instrument are found in\textsuperscript{[1]} Nagashima et al. (1999) and\textsuperscript{[2]} Nagayama et al. (2002). This campaign was initiated in December 2000, and so far, many dust-enshrouded variables were found and their light variation data has been steadily accumulating (see\textsuperscript{[3]} Ita et al. 2002 for the first results).

In the previous paper\textsuperscript{[4]} (Ita et al. 2004b) hereafter referred to as Paper I), we cross-identified the OGLE data and the single-epoch SIRIUS \textit{JHK} data from the monitoring survey, and studied the pulsation properties and metallicity effects on period-\textit{K} magnitude relations by comparing the variable stars in the LMC and SMC. In this paper, we present the data of the variable stars in the Magellanic Clouds and discuss their infrared properties.

2 DATA
The total areas covered by the SIRIUS variable star survey are three and one square degrees in the LMC and SMC, respectively. These areas are divided into 27(9) regions of 20' × 20' meshes in the LMC(SMC). Tables \textsuperscript{2} and \textsuperscript{3} define the central coordinates of

\begin{table}[h]
\caption{The filter characteristics.}
\begin{tabular}{|c|c|c|c|}
\hline
 & \textit{J} & \textit{H} & \textit{K}_\textsubscript{s} \\
\hline
Central wavelength [\mu m] & 1.25 & 1.63 & 2.14 \\
Bandwidth [\mu m] & 0.17 & 0.30 & 0.32 \\
\hline
\end{tabular}
\end{table}
them. Each of the $20' \times 20'$ regions is further subdivided into nine sub regions due to the field of view of the SIRIUS, which is about $7.7' \times 7.7'$. We cross-identified OGLE variables in the Magellanic Clouds (Zebrun et al. 2003) with the SIRIUS NIR sources that have been detected at least two of the three ($JHK$) wave bands, and then determined their pulsation periods by using the Phase Dispersion Minimization (PDM) technique (Stellingwerf 1978). Details of the cross-identifications and period findings are described in Paper I. We did not analyze multi-periodic stars (e.g., Bedding et al. 1998) and/or variable stars that show too complex light curves in the phase space (see the bottom panel of figures 4 and 5) to find a predominant period. We made two catalogs presenting data of variable stars in the LMC and SMC. They contain the following information: OGLE name, pulsation period in days, statistical parameter $\theta$ calculated by the PDM, pulsation amplitude ($\Delta = I_{\text{max}} - I_{\text{min}}$), intensity mean $I$ magnitude $< I >$, $JHK$ magnitudes and positional difference $r$ between the SIRIUS coordinate and the OGLE coordinate in arcsec. The $\theta$ is a measure of the regularity of the light variation, being near 0 for the regular variation and near 1 for the irregular variation.

Table 3 is a sample that shows the first five records of the LMC catalog. The full version of the data, including the SMC catalog, is available in the on-line version of this paper. In cases the $JHK$ measurements are saturated or below the detection limit, the corresponding columns contain the value 99.99. The $JHK$ magnitudes in the catalog are referred to the Las Campanas Observatory (LCO) system based on observations of a few dozen stars from Persson et al. (1998) and are not corrected for the interstellar absorption. We used the following colour equations

$$J_{\text{LCO}} = J + \begin{pmatrix} -0.007 \pm 0.002 \\ -0.005 \pm 0.002 \\ -0.003 \pm 0.002 \end{pmatrix}$$

$$H_{\text{LCO}} = H + \begin{pmatrix} 0.016 \pm 0.011 (J-H) \\ 0.009 \pm 0.005 (J-K) \\ 0.000 \pm 0.000 (H-K) \end{pmatrix}$$

$$K_{\text{LCO}} = K + \begin{pmatrix} -0.001 \pm 0.002 \\ -0.002 \pm 0.002 \\ -0.002 \pm 0.002 \end{pmatrix}$$

$$\text{to transform the IRSF instrumental magnitudes to the LCO system based ones. The } J - K \text{ ones were usually used, but } J - H(J - K) \text{ ones were employed if the } K(J) \text{ magnitudes were unavailable. Note that the SIRIUS measures the } K'_s \text{ magnitudes and they were converted to the LCO } K \text{ magnitudes.}$$

To enhance the image quality, we stacked the top 10 best seeing images (typically the seeing ranges from about 0.9" to 1.2" at $K$) that we have been collecting in the ongoing SIRIUS monitoring survey. We used the ISIS.V2.1 package (Alard & Lupton 1998, Alard 2000) to build a composite image that comprises 100 dithered 5 sec exposures. Photometry was performed on the composite image with DoPHOT (Schechter, Mateo & Sahill 1993), and then, the measured magnitudes were calibrated with the single-epoch photometry data by matching the magnitudes of the non-variable stars. Eventually, the photometry has a signal-to-noise ratio (S/N) of about 10 at 17.40, 17.38 and 16.63 mag in $J$, $H$ and $K$, respectively. Also, traditional experiments of adding artificial stars to the composite images revealed that the 90% completeness (detection probability) limits at $J$, $H$ and $K$ are about 17.25, 17.22 and 16.45 mag, respectively (Ita 2004).

### Table 2. Survey regions in the Large Magellanic Cloud

| Name          | Right Ascension | Declination |
|---------------|-----------------|-------------|
| LMC0507-6840  | 05h 07m 00.28s  | -68° 40' 00.00'' |
| LMC0507-6900  | 05h 06m 50.93s  | -69° 00' 00.00'' |
| LMC0507-6920  | 05h 06m 39.97s  | -69° 20' 00.00'' |
| LMC0510-6940  | 05h 10m 26.65s  | -69° 20' 00.00'' |
| LMC0510-6940  | 05h 10m 19.53s  | -69° 40' 00.00'' |
| LMC0511-6900  | 05h 10m 33.53s  | -69° 00' 00.00'' |
| LMC0514-6900  | 05h 14m 16.75s  | -69° 00' 00.00'' |
| LMC0514-6920  | 05h 14m 13.31s  | -69° 20' 00.00'' |
| LMC0514-6940  | 05h 14m 09.77s  | -69° 40' 00.00'' |
| LMC0518-6900  | 05h 18m 00.00s  | -69° 00' 00.00'' |
| LMC0518-6920  | 05h 18m 00.00s  | -69° 40' 00.00'' |
| LMC0522-6920  | 05h 21m 46.67s  | -69° 20' 00.00'' |
| LMC0522-6940  | 05h 21m 50.23s  | -69° 40' 00.00'' |
| LMC0522-7000  | 05h 21m 53.89s  | -70° 00' 00.00'' |
| LMC0526-6920  | 05h 25m 33.35s  | -69° 20' 00.00'' |
| LMC0526-6940  | 05h 25m 40.45s  | -69° 40' 00.00'' |
| LMC0526-7000  | 05h 25m 47.81s  | -70° 00' 00.00'' |
| LMC0529-6920  | 05h 29m 20.01s  | -69° 20' 00.00'' |
| LMC0530-6940  | 05h 29m 30.67s  | -69° 40' 00.00'' |
| LMC0530-7000  | 05h 29m 41.71s  | -70° 00' 00.00'' |
| LMC0533-6940  | 05h 33m 20.91s  | -69° 40' 00.00'' |
| LMC0534-7000  | 05h 33m 35.61s  | -70° 00' 00.00'' |
| LMC0534-7020  | 05h 33m 50.83s  | -70° 20' 00.00'' |
| LMC0537-6940  | 05h 37m 11.13s  | -69° 40' 00.00'' |
| LMC0537-7000  | 05h 37m 29.52s  | -70° 00' 00.00'' |
| LMC0538-7020  | 05h 37m 48.53s  | -70° 20' 00.00'' |

### Table 3. Survey regions in the Small Magellanic Cloud

| Name          | Right Ascension | Declination |
|---------------|-----------------|-------------|
| SMC0050-7250  | 00° 50' 28.95s  | -72° 30' 00.00'' |
| SMC0050-7310  | 00° 50' 23.74s  | -73° 10' 00.00'' |
| SMC0051-7230  | 00° 50' 33.95s  | -72° 30' 00.00'' |
| SMC0055-7230  | 00° 55' 00.00s  | -72° 30' 00.00'' |
| SMC0055-7250  | 00° 55' 00.00s  | -72° 50' 00.00'' |
| SMC0055-7310  | 00° 55' 00.00s  | -73° 10' 00.00'' |
| SMC0059-7230  | 00° 59' 26.04s  | -72° 30' 00.00'' |
| SMC0100-7250  | 00° 59' 31.04s  | -72° 50' 00.00'' |
| SMC0100-7310  | 00° 59' 36.25s  | -73° 10' 00.00'' |

1 These 10 images were taken on different days and hence under the different conditions, and a single image comprises 10 dithered 5 sec exposures.
Table 4. The first 5 records in the LMC catalog. This is a sample of the full version, which is available in the electronic version of Monthly Notices.

| Name            | Period [days] | θ  | ΔI | <I> | J  | H  | K  | t   |
|-----------------|---------------|----|----|-----|----|----|----|-----|
| OGLE050437.94-692217.2 | 0.460         | 0.178 | 1.025 | 19.250 | 99.999 | 16.056 | 16.030 | 2.260 |
| OGLE050438.43-691527.2 | 49.892         | 0.837 | 0.089 | 13.951 | 13.559 | 10.786 | 11.337 | 0.306 |
| OGLE050440.26-693039.7 | 42.783         | 0.866 | 0.160 | 14.189 | 12.786 | 11.880 | 11.599 | 0.466 |
| OGLE050440.29-692708.3 | 39.200         | 0.661 | 0.096 | 14.734 | 13.423 | 12.617 | 12.333 | 0.465 |
| OGLE050440.76-692416.0 | 96.365         | 0.358 | 0.317 | 14.060 | 12.294 | 11.491 | 11.063 | 0.574 |

Figure 1. Variable stars in the LMC (upper panel) and SMC (lower panel) are classified into several groups according to their location on the period-K magnitude plane.

Table 5. Colour mapping table

| Label | Colour | Population |
|-------|--------|------------|
| A^-   | Cyan   | RGB variables & metal poor and old AGB variables |
| A^+   | Yellow | less regularly pulsating AGB variables |
| B^-   | Orange | RGB variables & metal poor and old AGB variables |
| B^+   | Green  | less regularly pulsating AGB variables |
| C^-   | Blue   | Mira variables pulsating in the 1st overtone mode |
| C^-   | Red    | Mira variables pulsating in the fundamental mode |
| D     | Steel-blue | Some obscured variables & Unknown variables |
| F     | Magenta | Cepheid variables pulsating in the fundamental mode |
| G     | Purple  | Cepheid variables pulsating in the 1st overtone mode |

period-K magnitude plane. Refer to Paper I for the details of the grouping. For the easier reading and completeness of this paper, we show the period-K magnitude diagram with classification boxes in figure 1 and also for conciseness, we tabulated the colour mapping chart in table 5. Stars outside the classification boxes are represented by black tiny dots. Throughout this paper, we use the same labels and colours for each group. In the LMC, there is a clump of variables around log P ≲ −0.1 and K ≳ 15.0. This is a group of RR Lyrae variables, which we do not analyze in this paper.

Roughly speaking, five types of variable stars constitute the majority of the catalog: Cepheids, Miras, Semi-regulars, Irregular variables and Eclipsing binaries. However, telling Semi-regulars from Mira variables is rather difficult and there are not necessarily deep physical criteria. Several authors (e.g., Alard et al. 2001; Cioni et al. 2001) use a simple criterion that is based on a certain limiting pulsation amplitude to separate Semi-regulars and Miras. Meanwhile, Kiss & Bedding (2003, 2004) showed that there is a good correlation between the amplitude and mode of pulsation. In this paper, we do not separate Semi-regulars and Miras explicitly. Instead, we distinguish “regularly pulsating variables, (θ ≤ 0.55)” from “less regularly pulsating variables, (θ > 0.55)” relying on the parameter “θ”. In figures 2 and 3 we show the representative light curves of two variable stars on sequence C, having similar periods (~109 and ~126 days) and the same amplitudes (ΔI ~0.490 mag) but different θs.

3.2 Colour-magnitude and colour-colour diagram

The NIR data from the SIRIUS survey enabled us to study the infrared properties of the OGLE variables. Figure 4 and 5 show the NIR colour-magnitude and colour-colour diagram of the OGLE variables. In the inset of the figure 5 we show the colour-magnitude diagram of the SIRIUS data (including non-variables), closing-up around the tip of the first giant branch (TRGB). By comparing the insets and the main diagrams, it is clear that the stars of group A^- and B^- accumulate at the exact location of the TRGB (Ita et al. 2002; Kiss & Bedding 2003, 2004; Ita et al. 2004).

Most of the stars from group D are found at the place a bit brighter than the TRGB. Wood et al. (1999) identified the sequence D with suspected binaries, and Wood et al. (2000) discussed the total mean reddening of E<sub>B-V</sub> = 0.137 and 0.087 as derived by Udalski et al. (1999) for the OGLE's observing fields in the LMC and SMC, respectively. The reddening of the Magellanic Clouds is still somewhat controversial (e.g., Westerlund 1997), and it is certain that this type of statistical average approach cannot account for individual corrections. However, the adopted reddening should not affect any of the conclusions of this paper. The coefficients we calculated in equations 4 to 7 depend on reddening, but the effects should be small.

3.1 Classification of the variable stars on the period-K magnitude plane

Wood et al. (1999) discovered that variable red giants in the LMC form parallel sequences in the period-K magnitude plane and suggested that these sequences can be interpreted as the differences in the pulsation modes (Wood 2000).

In Paper I, we classified variable stars into nine (LMC) and eight (SMC) prominent groups based on their locations on the...
the possible explanations for the $D$ variables. On the other hand, some of the $D$ variables are very red ($J - H > 1.8$, $H - K > 1.5$ and $J - K > 3.2$) and relatively bright ($11.0 \lesssim K \lesssim 12.5$), properties associated with carbon-rich stars and dusty AGB stars (Nikolaev & Weinberg 2000). In the present sample, 14 out of 471 (6 out of 71) $D$ stars in the LMC (SMC) have these properties. A possible explanation for these red stars in the group $D$ is that, these stars could in fact be very dusty AGB stars that are subjected to severe circumstellar extinctions, even in the $K$ band. Whitelock et al. (2003) studied obscured variables in the LMC and showed that the $K$ magnitudes of obscured stars cover a wide range at a given pulsation period. For instance, their data indicates that the difference can be more than two magnitudes in the case of the carbon-rich stars. It is interesting to note that their red stars (those with long periods and $K$ magnitudes fainter than $\sim 11$ mag) clearly locate the brighter part of sequence $D$ on the period-$K$ magnitude plane. In addition, Kiss & Bedding (2003) suggested that there is a group of stars located below the Mira sequence (sequence $C$) and identified them with dusty AGB stars.

### Figure 2

![Figure 2](image2.png)

**Figure 2.** The light curve, theta spectrum and phased light curve (from top to the bottom) of the star OGLE051707.45-692855.3.

3.3 Period-colour diagram

Figure 6 shows the $J - K$ colours of OGLE variables in the Magellanic clouds as a function of their periods. The insets are the close-ups for the sake of clarity. A general trend that the colours get redder with increasing period can be seen.

The dashed lines are the least-square fit of a linear relation to the Cepheid variables ($F$ and $G$ stars), which yields the period-$J - K$ colour relations of

$$J - K[^{\text{mag}}] = 0.147(\pm 0.010) \log P[^{\text{days}}] + 0.248(\pm 0.006)$$

(4)

for the LMC ($\sigma = 0.062$) and

$$J - K[^{\text{mag}}] = 0.167(\pm 0.009) \log P[^{\text{days}}] + 0.272(\pm 0.004)$$

(5)

for the SMC ($\sigma = 0.074$), respectively. The quoted errors are the $1\sigma$ errors of each coefficient. Although the fundamental (group $F$) and first overtone (group $G$) Cepheids are clearly separated in the period-$K$ magnitude plane, we don’t see any significant difference between them in this diagram. This means, if we compare the fundamental and first overtone Cepheids with the same pulsation periods, the stellar radii of first overtone Cepheids should be larger than those of fundamental Cepheids because their stellar temperatures are nearly the same but the first overtone Cepheids are brighter than the fundamental ones. Theories predict exactly the same conclusion (e.g., Bono et al. 2001), and if the stellar radius of the Cepheid variables could be measured accurately, it will help to identify the pulsation modes.

The less regularly pulsating red giants (group $A^\pm$ and $B^\pm$) also follow a tight sequence on the period-$J - K$ colour plane. The thick solid lines in the figure indicate the least-square fit of a linear relation to the stars from the four groups, whose $J - K$ colours and periods are within the ranges, $0.7 < J - K < 1.3$ and $1.2 < \log P < 2.1$. Their period-$J - K$ colour relations are also calculated and they
are,
\[
J - K[\text{mag}] = 0.231(\pm 0.004) \log P[\text{days}] + 0.671(\pm 0.007). \quad (6)
\]
for the LMC ($\sigma = 0.058$) and
\[
J - K[\text{mag}] = 0.272(\pm 0.011) \log P[\text{days}] + 0.560(\pm 0.019). \quad (7)
\]
for the SMC ($\sigma = 0.068$), respectively.

It is obvious that most of the $C$ and $C'$ stars in the LMC, and also some $B'$ stars and most of $C$ stars in the SMC do not follow the extension of these relations. In Paper I, we confirmed the conclusion of Wood & Sebo (1996) and suggested that stars on sequences $C$ and $C'$ are Mira variables pulsating in the fundamental and first overtone mode respectively, by comparing their model calculations with our observational data. Figure 6 clearly shows that $C$ and $C'$ stars behave very similarly on the period-$J - K$ colour plane. This corroborates the idea that the $C$ and $C'$ stars are the same type of stars (i.e., Miras), but only different in the pulsation modes. Also, it is likely that the “some $B'$ stars” in the SMC are the counterparts of the $C'$ stars in the LMC.

In earlier work, Feast et al. (1989), Glass et al. (1995) and Whitelock, Marang & Feast (2000) obtained period-$J - K$ colour relations of Mira variables in the LMC, Sgr I Baade window of the Galactic Bulge and solar neighborhood, respectively. These relations are all based on the SAAO system. The atmospheres of Mira variables are rather complex, making their quantitative comparisons difficult between different filter systems. Thus here we make only qualitative discussions. Just to get a rough idea, we indicated in the upper panel of figure 5 the period-$J - K$ colour relations obtained by Feast et al. (1989) for carbon- (labeled I) and oxygen-rich (labeled II) Miras and by Whitelock et al. (2000) (labeled III) after referring to the LCO system by assuming $(J-K)_{LCO} = 0.928(J-K)_{SAAO} - 0.004$ (Carpenter 2001). Of course we cannot tell exactly which of our stars are carbon- or oxygen-rich, but it is statistically fair to say that stars with $J - K$ colours redder than 1.4 are primarily carbon-rich-stars (Nikolaev & Weimbach 2000). In this point of view, we confirmed the result of Feast et al. (1989) that oxygen- and carbon-rich Miras follow different period-$J - K$ colour relations.

Now that we see the $C$ and $C'$ stars separate on the period-$J - K$ colour plane, it will be interesting to search for the Galactic counterpart of the first overtone Miras ($C'$ stars) by using this tool. Then we can redetermine their distances using their exclusive period-$K$ magnitude relation, which we obtained in Paper I. It will help to understand the differences between the fundamental and first overtone Miras through more detailed studies that are technically difficult in the Magellanic Clouds (i.e., spectroscopic work and mid-infrared observations etc.). Because not only $C$ and $C'$ stars but also the other variables separate on the period-$J - K$ colour plane, the same argument is true for them, such as $D$ stars.

However, before applying this tool to different environments, we should know whether it depends on chemical abundance. Wray, Ever & Paczyński (2004) showed that small amplitude red giant variables in the Galactic Bar can be separated into two groups, and they follow different period-colour relations. Also, they suggest that their $A$ and $B$ stars correspond to type $A^-$ and $B^-$ variables, respectively of Paper I. The insets of the figure 6 clearly confirm their result, showing that $A^-$ and $B^-$ are well separated on the period-$J - K$ colour plane. This infers that the period-$J - K$ relations we derived in equations 6 and 7 are merely the general trends of the

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**Figure 4.** NIR colour-magnitude diagram of OGLE variables in the LMC (upper panel) and the SMC (lower panel). The inset shows the plot of the all SIRIUS data (including non-variables) around the $K$-band luminosity of the TRGB.

**Figure 5.** NIR colour-colour diagram of OGLE variables in the LMC (upper panel) and the SMC (lower panel).
variable red giants, and in fact there are exclusive period-colour relations for each population. Rejkuba et al. (2003) studied infrared properties of long period variables in Cen A. Although they did not mention it, it is likely that there are two groups in their period-colour diagrams (see their figure 10). We suggest that their short-period ($\log P \sim 2.45$) and long-period ($\log P \sim 2.65$) groups could correspond to type $C'$ and $C$ stars in the LMC, respectively. These facts strengthen the idea that, period-colour diagram is a good and universal tool, at least to tell the type of variable stars within a system.

Lebzelter, Schultheis & Melchior (2002) studied the AGAPE-EROS/DENIS variables in the LMC and showed that so-called Semi-regular variables follow a period-colour relation but the "regular" variables do not (see their figure 12). To see the regularity of the light variation quantitatively, we show the relationship between the statistic parameter $\theta$ and period in figure 4. The figure clearly confirmed the Lebzelter’s suggestion and shows that stars that follow period $J - K$ relation ($A^+$ and $B^+$ stars with $\log P \lesssim 2.1$) are less regularly pulsating, and those that don’t ($B^-$ stars with $\log P \gtrsim 2.1$, $C'$ and $C$ stars) are regularly pulsating.

3.4 Period-amplitude ($\Delta I$) and colour-amplitude diagram

Figure 8 is a plot to show the relationship between the pulsation period and amplitude ($\Delta I$). The pulsation amplitude is determined from the OGLE’s $I$ band data, given as $\Delta I = I_{\text{max}} - I_{\text{min}}$. Note that all of the original OGLE light curves were carefully eye-inspected, and we calculated the $\Delta I$ after eliminating the obvious spurious data points.

The figure shows that the fundamental Cepheids show larger amplitude variations than the first overtone Cepheids. Also, the upper envelope of Cepheid amplitude goes down with increasing period. This trend contrasts markedly with that of red giants, because their pulsation amplitudes generally go up with increasing period.

Variables stars with $K$ magnitudes below the TRGB ($A^-$ and $B^-$ stars) pulsate with very small amplitude. With a few exceptions, most of the stars from $D$ group also pulsate with relatively small amplitude. The large amplitude pulsation ($\Delta I \gtrsim 0.9$) seems to occur only among the long-period ($\log P \gtrsim 2.3$) variables. If one had to separate Semi-regular from Mira variables based on pulsation amplitude, the threshold would be about $\Delta I \approx 0.9$, because one can see a discernible gap around there.

Figure 9 shows the relationship between the $J - K$ colour and pulsation amplitude ($\Delta I$). The variable red giants show the clear trend that the amplitude gets larger with increasing colour. According to Nikolaev & Weinberg (2000), obscured carbon-rich AGB stars have the $J - K$ colours redder than about 2.0 mag. Almost all of such dusty carbon-rich stars in the Magellanic Clouds have large pulsation amplitudes. Some of the relatively blue stars ($0.8 \lesssim J - K \lesssim 1.2$) on the sequence $C$ also show large amplitude pulsation. Judging from their $J - K$ colour and being on the sequence $C$, they are likely to be oxygen-rich Mira variables. It is remarkable that the carbon-rich Miras tend to have greater $I$-band amplitudes at redder $J - K$ colour, but the amplitudes of oxygen-rich Miras are almost independent of the colour. This might reflect the difference in the molecular opacities at $I$-band between the two groups.
3.5 Similarities and differences between the LMC and SMC samples

In a large sense, variable stars in the Magellanic Clouds behave similarly in the figures we discussed so far. However, on closer view, there are differences between variable stars in the two galaxies. In the colour-amplitude diagram (figure 9), we see smaller number of oxygen-rich large amplitude Mira variables in the SMC (counterpart of LMC Miras with $J - K$ colours bluer than 1.4) compared to the LMC. This is probably because the difference in average chemical abundance and/or in age between the two galaxies (e.g., Cioni & Habing 2003; Moulhcine & Lancor 2003).

4 SUMMARY

We presented the data of 8,852 and 2,927 variable stars in the Large and Small Magellanic Clouds. Based on these data, we discussed the infrared properties of the variable stars. We showed that period-$J - K$ colour diagram is a good tool to tell the pulsation modes of the Mira variables. A follow-up campaign searching for the Galactic counterpart of the first overtone mode Miras would tell us the difference between them and fundamental mode Miras.

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