Charge and frequency resolved isochronous mass spectrometry in storage rings: First direct mass measurement of the short-lived neutron-deficient $^{51}$Co nuclide

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Revolution frequency measurements of individual ions in storage rings require sophisticated timing detectors. One of common approaches for such detectors is the detection of secondary electrons released from a thin foil due to penetration of the stored ions. A new method based on the analysis of intensities of secondary electrons due to penetration of the stored ions. A new method based on the analysis of intensities of secondary electrons

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Ion storage rings are versatile facilities ideally suited for performing precision experiments with rare ions [1]. One prominent example of such experiments is the measurement of masses of short-lived nuclides [2]. The masses of exotic nuclei are indispensable quantities for nuclear structure and astrophysics as well as for investigations of fundamental symmetries [3–6]. Huge efforts are undertaken worldwide, both in theory and experiment, to extend the knowledge of nuclear masses to the outskirts of the chart of nuclides. However, since the nuclides with presently unknown masses are as a rule short-lived and/or have tiny production rates, their measurements require very sensitive and fast techniques [7, 8]. One of such techniques is the isochronous mass spectrometry (IMS) applied to nuclei of interest stored in a storage ring [9].

The property of the IMS, which was pioneered at the experimental storage ring (ESR) facility of GSI [10–13], is that the revolution time difference $t_r$ is directly related to its mass-over-charge ratio difference $\Delta(m/q)$ by the following expression [9,10]:

$$\frac{\Delta t}{t_r} = \frac{1}{\gamma} \frac{\Delta(m/q)}{(m/q)\Delta\gamma},$$  \hspace{1cm} (1)

where $\gamma$ denotes the transition point of the storage ring. From Eq. (1) it follows that for a mass measurement it is required to achieve accurate determination of revolution times (frequencies) of stored ions. Such determinations require sophisticated detection setups. The revolution frequencies of stored relativistic ions are typically in the MHz range, which translates into MHz count rate on the detector. Furthermore, since the storage rings are operated under ultra-high-vacuum conditions of $10^{-10} - 10^{-12}$ mbar, the detectors have to be bake-able. Detectors employing secondary electrons released from a thin foil by the penetrating ions are routinely employed in IMS experiments [14, 15].

In this Letter we present a method which allows for, in addition to the precise measurements of revolution times, a simultaneous determination of the nuclear charge of the stored ions. Taken into account the high count rates (several MHz) and high timing accuracy (about 50 ps), this method may be of a broad interest not only for storage-ring-based nuclear and atomic physics experiments, but also for beam diagnostics, particle identification, and detectors for space missions, etc. Furthermore, we present the first mass measurement of the short-lived $^{51}$Co nuclide ($T_{1/2} = 68.8 (1.9)$ ms [16]). Since the $^{51}$Co$^{27+}$ and $^{34}$Ar$^{18+}$ ions have a very close mass-over-charge ratio $(\Delta(m/q)/(m/q) \approx 5 \times 10^{-6}$), they cannot be resolved by their revolution times (see Eq. (1)). However, due to different atomic numbers of Co and Ar ions, the mass of $^{51}$Co could
The experiment was performed at the HIRFL-CSR accelerator complex in the Institute of Modern Physics (IMP), Chinese Academy of Sciences (CAS), with the combination of a heavy ion synchrotron CSRm, an in-flight fragment separator RIBLL2 and the experimental storage ring CSRe [17]. The aim was to measure the masses of short-lived \( T_e = -3/2 \) nuclei in the \( fp \) shell. For this purpose, the \(^{58}\text{Ni}^{19+}\) primary beams at an energy of 463.36 MeV/u provided by the CSRm were fragmented in an \( \sim 15 \) mm beryllium target placed at the entrance of RIBLL2. The \( T_e = -3/2 \) fragments centred around \(^{47}\text{Mn}\) were transmitted through the RIBLL2 and injected into the CSRe. The RIBLL2 and CSRe were set to a fixed magnetic rigidity of \( Bp = 5.6770 \text{Tm} \). All fragments within a \( Bp \)-acceptance of \( \sim \pm 0.2\% \) were injected into the CSRe. The beam energy was chosen such that the fragments of interest have the energy after the production target corresponding to \( \gamma = \gamma_0 = 1.395 \), namely the isochronous condition [8, 10]. At this energy the fragments emerged from the target predominantly as bare ions.

Typically, about ten ions were stored simultaneously in one injection into the CSRe. The revolution frequencies of stored ions were about 1.6 MHz. In order to measure the revolution times, a dedicated timing detector equipped with a 19 \( \mu \text{g/cm}^2 \) carbon foil of 40 mm in diameter was installed inside the CSRe. The detector design and its operation were described in detail in Ref. [15]. When a stored ion passed through the timing detector, secondary electrons were released from the foil. The electrons were guided isochronously by perpendicularly arranged electrostatic and magnetic fields to a set of micro-channel plates (MCP). The signals from the MCP detector were directly put into a fast digital oscilloscope, sampled and stored for off-line analysis. The time resolution was about 50 ps, and the detection efficiency varied from 20% to 70% depending on the type and the number of stored ions [15].

The recording time was set to 200 \( \mu \text{s} \) for each injection which corresponds to \( \approx 320 \) revolutions of the ions in the CSRe. A sequence of timing signals obtained for simultaneously stored \(^{13}\text{N}^{7+}\) and \(^{54}\text{Ni}^{28+}\) single ions is illustrated in Figure 1. Five revolutions corresponding to the recording time of 3 \( \mu \)s are depicted.

The timing signals for each individual ion are periodic. This property was used to determine the revolution times \( t_i \) of each stored ion (see Ref. [8] for more details). Only those particles which were stored for more than 300 revolutions in the CSRe were used in the analysis. This condition is important for the precise determination of the corresponding revolution times. All obtained revolution times were put into a histogram thus forming a revolution time spectrum. Figure 2 illustrates a part of the revolution time spectrum zoomed in a narrow time window of 616 ns \( \leq t \leq 618 \) ns. The temporal instabilities of the magnetic fields discussed in Refs. [8, 18, 19] have been corrected for.

Good isochronous conditions are fulfilled in a limited range of revolution times [20, 21]. In this experiment we analysed the range lying within 608 ns \( \leq t \leq 620 \) ns [19], which is characterised by the standard deviations of 2-5 ps and the optimal mass resolving power of \( \Delta m/m \approx 180000 \) for the revolution-time peaks. The revolution time spectrum zoomed in 608 ns \( \leq t \leq 620 \) ns is illustrated in Figure 1 of Ref. [19].

The revolution time spectrum was calibrated by using the nuclides with accurately known masses present simultaneously in the same spectrum. Fourteen such nuclides were used to fit \( m/q \) versus \( t \) employing a third order polynomial function:

\[
\frac{m}{q}(t) = a_0 + a_1 \cdot t + a_2 \cdot t^2 + a_3 \cdot t^3 \tag{2}
\]

where \( a_0, a_1, a_2 \) and \( a_3 \) are free parameters. The masses determined in this experiment were included into the latest Atomic Mass Evaluation AME’12 [22].

The peaks of \(^{51}\text{Co}^{27+}\) and \(^{40}\text{Ar}^{18+}\) ions in Figure 2 can not be resolved in the spectrum due to very similar mass-over-charge ratios. The standard deviations of the revolution time peaks in this range lie within 2-4 ps. From the systematic trends of production yields for \( T_e = -3/2 \) nuclides, one would expect a significant amount of short-lived \(^{51}\text{Co} \) ions to be injected and stored in the CSRe.
and $-64 \text{ mV}$ are assigned to $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ and neighbouring ions. Note that $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ can not be resolved by their revolution times (see Figure 3) but have been nicely resolved by different signal amplitudes.

As seen in Figure 1, signal amplitudes for ions with a larger atomic number ($^{27}\text{Ar}^{28+}$ ions) are on average larger than the signals for ions with a smaller atomic number ($^{18}\text{Ar}^{17+}$ ions). The emission of secondary electrons is well studied, see, e.g., Refs. [23, 24]. The difference in the amplitudes can be understood as a difference of ion energy loss in the detector foil, which scales in first order with $q^2$ [13].

To determine the mass of $^{51}\text{Co}$, we employed this $q$-dependence to resolve the peaks of $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ ions. For this purpose we analyzed the average signal amplitudes for each ion obtained from all its revolutions in the CSRe. A two-dimensional spectrum has been produced, where the three axis are the averaged signal height (amplitude), the revolution time, and the number of ions. The spectrum of $^{51}\text{Co}^{27+}$, $^{34}\text{Ar}^{18+}$ and neighbouring ions is depicted in Figure 3. One can see in this figure that the stored ions with $T_z = -1/2, -1$, and $-3/2$, including the $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ couple, can clearly be resolved by their signal amplitudes. The spectrum in Figure 3 is a storage ring analog of the well-known identification plots obtained in in-flight separator (see, e.g., Figure 1 in Ref. [25]).

The signal height distributions for $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ ions are presented in Figure 4a. We assume that the events with average signal amplitudes larger than 64 mV belong to $^{51}\text{Co}^{27+}$ ions, while those peaks with amplitudes smaller than 64 mV are assigned to $^{34}\text{Ar}^{18+}$ ions. Then, by setting these gates on each ion, the mean revolution times for $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ ions could be extracted as shown in Figure 4c. The corresponding revolution time difference was found to be merely $1.63(35)$ ps.

Unfortunately, the peaks of $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ ions could not be completely separated from each other in the signal height distributions (see Figs. 3 and 4a). The remaining overlap can introduce an error in the extraction of the revolution times which in turn can lead to an additional systematic error in the mass determination. To estimate this influence, we investigated the signal height distributions for $^{52}\text{Co}^{27+}$ and $^{35}\text{Ar}^{18+}$ ions. The revolution times of these ions are very different as can be seen in Figure 4d and an unambiguous distribution of the averaged signal amplitudes can be extracted for the two ion species by gating on the corresponding revolution time peak. The latter is shown in Figure 4b. We emphasize that these two ion species were injected and stored simultaneously with $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$ ions. By studying the obtained signal height distribution, we find that 10 (43) out of the 2402 (440) $^{35}\text{Ar}^{18+}$ ($^{52}\text{Co}^{27+}$) ions have an averaged signal height larger (smaller) than 64 mV. Since the signal amplitude depends on $q$ of the ions, it is reasonable to assume that distribution for the $^{35}\text{Ar}^{18+}$ / $^{52}\text{Co}^{27+}$ couple shall be the same as for the $^{34}\text{Ar}^{18+}$ / $^{51}\text{Co}^{27+}$ couple. Hence, we can estimate that $0.4\%$ ($10\%$) of the total number of $^{34}\text{Ar}^{18+}$ ($^{51}\text{Co}^{27+}$) events may erroneously be assigned to $^{51}\text{Co}^{27+}$ ($^{34}\text{Ar}^{18+}$). On the basis of this estimation, we concluded that in the 704 (144) $^{34}\text{Ar}^{18+}$ ($^{51}\text{Co}^{27+}$) events, which were used to calculate the mean revolution time of $^{34}\text{Ar}^{18+}$ ($^{51}\text{Co}^{27+}$) ions, there could present $15(3)$ contaminating counts from $^{51}\text{Co}^{27+}$ ($^{34}\text{Ar}^{18+}$) corresponding to $\sim 2\%$ of the total statistics for $^{51}\text{Co}^{27+}$ (144 events) and $^{34}\text{Ar}^{18+}$ (704 events). This mis-assignments can cause an average shift of $0.03 \sim 0.04$ ps in the mean revolution times, which is negligible compared to the statistical error of the obtained time difference of $1.63(35)$ ps.

The masses of $^{51}\text{Co}$ and $^{34}\text{Ar}$ nuclei were deduced by interpolating the calibration curve defined by Eq. (2) to the corresponding revolution time of $^{51}\text{Co}^{27+}$ and $^{34}\text{Ar}^{18+}$. The mass-excess values $ME(^{51}\text{Co}) = -27342(48)$ keV and $ME(^{34}\text{Ar}) = -18379(15)$ keV were obtained. We note that our re-determined mass excess for $^{34}\text{Ar}$ nuclide is in excellent agreement with the independently measured value of

![Figure 4](image-url)
\[ \Delta CDE(A, T) = M(A, T_{Z>}) - M(A, T_{Z<}) + 2T_{Z<} \cdot \Delta_{alt} \] (3)

where \( M(A, T_{Z>}) \) and \( M(A, T_{Z<}) \) are the masses of mirror nuclei with the larger and the smaller charge, respectively. \( \Delta_{alt} = 782.6466(5) \) keV is the neutron-hydrogen mass difference \([22]\). Expressed differential \( \Delta CDE \) values, \( \Delta CDE(A, T) = CDE(A + 2, T) - CDE(A, T), \) for \( T = 3/2 \) in the \( sd\)- and lower \( fp\)-shell nuclei are plotted in Figure 5 together with predictions by often-used mass models. Microscopic Hartree-Fock-Bogoliubov with BSk21 interaction (HFB-21) \([29]\) model as well as macroscopic-microscopic WS-3.6 (WS) \([30]\) and Finite-Range Droplet Model (FRDM) \([31]\) were considered. We note that the WS model, whose \textit{rms} deviation from 2149 known nuclear masses is merely 336 keV, reproduces very well the experimental data for the whole chain of Co isotopes. The success of this model has been attributed to a better consideration of residual correlations and isospin and mass dependence of the model parameters \([30, 32, 33]\).

One clearly sees in Figure 5 that the staggering of the ACDE values, superimposed on a monotonic decreasing curve, persists up to \( A = 43 \), but the effect is washed out for the heavier ones \((A = 45 - 51)\). The \( ^{51}\text{Co} \) mass value is decisive here since it contributes two new data points. It is striking that all considered mass models fail to describe the experimental staggering of the ACDE values. The staggering is basically not present in the WS3.6 calculations and the HFB-21 and FRDM produce even the opposite staggering phases.

Kaneko \textit{et al.}, in a study of \( T = 1/2 \) CDE and \( T = 1 \) TDE (triplet displacement energy) \([34]\), pointed out the necessity of the isospin-nonconserving (INC) nuclear interactions for the \( f_{1/2} \)-shell. Now we study CDE for the \( T = 3/2 \) isospin chain by performing similar shell-model (SM) calculations as in Ref. \([34]\). As seen in the insert of Fig. 5 the results without the INC forces indicate some staggering of ACDE values for \( A = 45 - 51 \) while the experimental data do not show any significant staggering. By including the INC-forces, the description of the experimental data is improved considerably. Although not unambiguous, these results point to the presence of INC-forces in the \( p_{f/2} \)-shell. This conclusion is consistent with the recent calculation for the \( T = 1/2 \) chain \([34]\), where the staggering pattern was observed in the \( T = 1/2 \) isospin chain, but with a notable exception for the \( f_{1/2} \)-shell nuclei with masses \( A = 42 - 52 \). Moreover, both the experimental data and the predictions show a similar drop at \( A = 53 \), where one nucleon occupies the \( p_{3/2} \) orbital. Note, that the current shell-model calculations include INC only for the \( f_{1/2} \)-shell. Our SM results show that the staggering pattern persists beyond \( A = 55 \). Whether and how \( T = 3/2 \) CDE in the upper-\( p\)-shell depends on INC is an important question to be addressed by future mass measurements of heavier \( T = 3/2 \) nuclei.

In summary, we measured for the first time the mass of short-lived \( ^{51}\text{Co} \) nucleus by applying the isochronous mass spectrometry on \( ^{58}\text{Ni} \) projectile fragments in the storage ring CSRe in Lanzhou. The stored \( ^{51}\text{Co}^{27+} \) and \( ^{34}\text{Ar}^{18+} \) ions cannot be resolved by their revolution times due to very similar mass-over-charge ratios. Therefore, we developed a new method in which we analysed the average amplitudes from the timing detector as a function of atomic number of the ions. This enabled us to resolve \( ^{51}\text{Co}^{27+} \) and \( ^{34}\text{Ar}^{18+} \) ions by their charge and thus to extract their revolution times. The newly developed method may be considered in future measurements of \( Z = N \) nuclides.

The extracted proton separation energy indicates that \( ^{51}\text{Co} \) is probably the lightest proton-bound even-\( N \) Co isotope. The behaviour of the staggering of differential ACDE values was used to investigate the importance of INC interactions in the \( fp\)-shell nuclei. The new mass of \( ^{51}\text{Co} \) is essential for this study since it belongs to the region \((A = 45 - 51)\) where shell model calculations turned out to be sensitive to the inclusion of INC forces. The obtained results point to the necessity to include INC interactions in the calculations of \( fp\)-shell nuclei.

FIG. 5: (Colour online) Experimental and theoretical \( \Delta CDE \) values. The insert shows a zoom on the heavier mass region together with shell model calculations without (SM) and with (SM+INC) isospin-nonconserving nuclear forces.
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