Emerging spin–phonon coupling through cross-talk of two magnetic sublattices

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Many material properties such as superconductivity, magnetoresistance or magnetoelectricity emerge from the non-linear interactions of spins and lattice/phonons. Hence, an in-depth understanding of spin–phonon coupling is at the heart of these properties. While most examples deal with one magnetic lattice only, the simultaneous presence of multiple magnetic orderings yield potentially unknown properties. We demonstrate a strong spin–phonon coupling in SmFeO3 that emerges from the interaction of both, iron and samarium spins. We probe this coupling as a remarkably large shift of phonon frequencies and the appearance of new phonons. The spin–phonon coupling is absent for the magnetic ordering of iron alone but emerges with the additional ordering of the samarium spins. Intriguingly, this ordering is not spontaneous but induced by the iron magnetism. Our findings show an emergent phenomenon from the non-linear interaction by multiple orders, which do not need to occur spontaneously. This allows for a conceptually different approach in the search for yet unknown properties.
The richness of physical phenomena in correlated oxides roots in the interaction and competition of coexisting properties and instabilities. A fundamental facet in materials with magnetic ions is the coupling of magnetic spins, the crystal lattice and lattice vibrations. From this interaction fascinating phenomena emerge, such as superconductivity\(^1\), multiferroicity\(^2,3\), giant thermal Hall effect\(^4\) or ferroelectric phase transitions\(^5\). The presence of two magnetic ions in different sublattices makes the interaction particularly complex, but likewise intriguing. For instance, the cross-talk of transition-metal and rare-earth ions (\(R^{3+}\)) in complex oxides leads to phenomena such as spin-reorientations, magnetic compensation\(^6,7\), solitonic lattices\(^8\) or multiferroicity\(^9,10\), including domain inversion\(^11\) and interconversion of domains and domain walls\(^12,13\). At first sight, these phenomena seem to be of magnetic nature only. However, upon closer inspection, the coupling to the crystal lattice and related lattice vibrations turns out to be vital. For instance, multiferroicity entails an ionic displacement and tilts of the oxygen octahedra can give rise to a net-magnetization by a canting of the spins and thereby steer the rare-earth magnetism induced by the transition-metal ion\(^14\). Hence, the combination of the primary magnetic and structural orders is considerably more than the sum of its parts, manifesting in the emergence of enhanced or additional properties.

Despite the important interactions of magnetism and structure, spin–phonon coupling arising from the cross-talk of two magnetic ion subsystem remains largely unexplored. The observation and understanding of such cross-talk are at the heart of the present work. We show how the interaction of two magnetic sublattices in SmFeO\(_3\) leads to the rise of an extraordinarily strong coupling between spins, lattice and lattice vibrations. First, for the high-temperature regime, we reveal a softening of the elastic moduli during the spin reorientation. Second, below room temperature, an unprecedentedly strong spin–phonon coupling arises from the non spontaneouse ordering of the \(Sm^{3+}\) spins thanks to the exchange-field of the iron magnetism. Here we find strong indications that this “spin-spin–phonon” coupling gives rise to a phase change in SmFeO\(_3\). Hence, the interaction of both magnetic sublattices drives a strongly non-linear material response—entirely absent for the individual magnetic sublattices.

**Results and discussion**

SmFeO\(_3\) crystallizes in a perovskite-type structure with the space group \(Pnma\)^\(^7\). The primary structural distortions from the ideal perovskite structure are tilts of the oxygen octahedra, \(ab^+a^-\) in Glazer’s notation\(^15\) (Fig. 1a). At \(T_N = 680\) K, the iron spins order antiferromagnetically along the \(c\)-axis (\(G_2\)-type)\(^1\). A spin canting induces a weak-ferromagnetic moment along the \(b\)-axis \((F_y)\) and an \(A\)-type component along the \(a\)-axis (expressed in Bertaut’s notation\(^16\)) (Fig. 1b). Between 450 K and 480 K, the iron-spin lattice experiences a spin reorientation to a \(C,G,F\)-type ordering triggered by the anisotropy change of the samarium moments\(^1\). Subsequently, the samarium spins align in the exchange field of iron. This becomes clear from magnetic measurements as a decline of the overall magnetization below 140 K\(^17,18\) with a full compensation at 3.9 K\(^19\). Staub et al. showed that the Fe\(^{3+}\) magnetism can even induce an antiferromagnetic order on the rare-earth sublattices below spin-reorientation\(^20\). Warshil et al. showed that this low-temperature ordering involves the formation of a cluster glass rather than a discrete transition\(^21\). The high temperatures of the magnetic ordering \(T_N\) and the spin-reorientation allow us to disentangle high- and low-temperature phenomena. This makes SmFeO\(_3\) a model material, unlike other rare-earth transition-metal ions, in which most magnetic interactions occur far below room temperature.

To assess the interaction of spins and phonons, we performed Raman scattering complemented with resonant ultrasound spectroscopy (RUS) from 800 K down to 4 K. Both are excellent probes for detecting and tracing even subtle structural and magnetic changes\(^22,23\). Raman spectroscopy probes directly the optical phonons. Thanks to a recent work\(^24\), we can assign all 24 Raman active phonons \((\Gamma = A_g + 5 B_{1g} + 7 B_{2g} + 5 B_{3g})\) to their specific vibrational patterns (see Fig. 2a and Supplementary Note 1). RUS provides a highly sensitive probe of static and dynamical lattice distortions that accompany relaxation processes and phase transitions\(^26,27\). In an RUS experiment, variations of elastic moduli scale with the square of the frequencies of individual resonances which are dominated by shearing motions, and acoustic loss is expressed in terms of the inverse mechanical quality factor, \(Q^{-1}\). Combining both techniques provides access to the form and strength of both spin–phonon and spin-lattice coupling.

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**Fig. 1 Magnetic properties of SmFeO\(_3\).** a Rare-earth orthoferrite \(Pnma\) structure\(^55\). Oxygen, iron and rare-earth ions are given in red, green and turquoise, respectively, FeO\(_6\) octahedra in pale blue. Solid and dashed lines describe the orthorhombic unit cell and the pseudo-cubic setting, respectively. b Evolution of the magnetization (data taken from Ref. \(^19\)) at the Néel temperature \(T_N\), the Fe\(^{3+}\) spins order in a \(A,F,G\)-type fashion. At the spin reorientation, the magnetic order changes to \(C,G,F\). The spin canting leads to a net-magnetization. Both Fe\(^{3+}\) spin structures are sketched in pseudo-cubic settings. At low temperatures, the iron magnetism induces the magnetic \(Sm^{3+}\) sublattice with a net-magnetic moment (turquoise arrows) aligning antiparallel to the iron moments, which leads to a magnetic compensation point \(T_{comp}\) at 3.9 K.
ultrasound resonance bands; see Supplementary Figs. 5 and 6). To 700 K, thus above the magnetic ordering (this behavior is alike for all deviation in elastic moduli. Softening through the reorientation transition. scales with some combination of single crystal elastic moduli, showing a temperature evolution of the complete Raman spectra, the phonon frequencies parentheses indicate polarization of incident and scattered light, respectively. Parentheses denote the propagation direction, while symbols inside the 850 K, across the spin reorientation

\[ T(N) = 450 \text{ to } 480 \text{ K}. \] With decreasing temperature, the magnetic Sm\textsuperscript{3+} anisotropy changes. This change in anisotropy induces a rotation of the iron spin system\(^7\) (Fig. 1b) marking the incipient cross-talk between the iron and the samarium magnetism. Unlike at \( T(N) \), the RUS data show elastic softening by up to a few percent and a closely correlated increase in acoustic loss between 460 and 480 K, before \( f^2 \) reverts to the same trend below 460 K as observed above 480 K (Fig. 2c–g, Supplementary Figs. 4–6). Observing the same temperature evolution of resonance frequencies before and after the onset of magnetic order means that the magnetic order parameter can only be very weakly coupled to strain – or that magnetoelastic coupling is completely absent, consistent with the literature and our findings at \( T(N) \). Further, this lack of coupling of the magnetic order parameters with macroscopic strains together with the inverse correlations between the variations of \( f^2 \) and \( Q^{-1} \), indicates that softening in the transition interval is due to anelastic relaxation.

The mechanism responsible for the concomitant changes of elastic moduli and acoustic losses is not known other than it involves anelastic relaxations of magnetoelastic origin. Strain relaxation of the structure in response to a dynamic stress is required, and one possibility is the existence of local regions with monochoric distortions. However, although a monoclinic phase could be local monoclinic symmetry in these two phases\(^3,34,35\) has not been detected by X-ray diffraction in orthoferrites\(^3,32,33\). Evidence from NMR spectroscopy that there could be local monoclinic symmetry in these two phases\(^3,34,35\) has also been disputed\(^33\). (For further information see Supplementary Note 4).

In contrast to the strong RUS anomaly, frequencies of the optical Raman phonons show no observable change through the spin reorientation (Fig. 2b, c). This is consistent with the absence of changes in strain and the timescale of relaxational effects in the order of \( \sim 10^{-6} \) s (ultrasound frequency), which would not be detected on the phonon timescale of \( \sim 10^{-12} \) s. The FWHM (Supplementary Note 2) is characterized by a stagnation around the spin reorientation, and, in turn, the phonon lifetime does not lengthen any further. This indicates a reduced phonon correlation-length arising from a non-collective rotation of the iron spins and the competition of both magnetic phases (for further discussion see Supplementary Note 2). There is no evidence for a collective rotation and a resulting symmetry breaking on the phonon length scale, i.e., the intermediate length scale between the strictly local scale of NMR and the macroscopic length scale of X-ray diffraction.

To conclude the high temperature analysis, we find that the elastic moduli of SmFeO\(_2\) soften significantly during the spin reorientation by a magnetoelastic relaxation mechanism present only in the reorientation state driven by the Fe\textsuperscript{3+}-Sm\textsuperscript{3+}-interplay. The magnitude of any macroscopic strains coupled with the
magnetic order parameter remains small throughout the full temperature range, including through the Neel point and the spin-reorientation transition.

**Induced Sm$^{3+}$ ordering ($T < 300$ K).** Having observed emergent magnetoelastic properties as the samarium acts on the magnetic order of iron, we now turn to the reverse case with iron acting on samarium. Upon cooling below the spin reorientation, the iron magnetism induces a non-spontaneous ordering of the Sm$^{3+}$ spins. Our Raman spectra reveal two types of spectral anomalies in this regime. First, the frequency evolution of several vibrational bands dramatically deviates with temperature from a typical anharmonic behavior (Fig. 3). Second, we observe the emergence of new Raman features (Fig. 4). In comparison with the Raman results, RUS is virtually featureless with only subtle anomalies at 250 K that could be consistent with magnetoelastic coupling (see Supplementary Note 8).

The observed deviations of the Raman frequencies from a typical thermal behavior are unprecedentedly strong in perovskites. While spin–phonon coupling commonly leads to Raman shifts of a few wavenumbers at most$^{29,30,36}$, we observe deviations of over 10 cm$^{-1}$ and up to 8%. To understand the underlying mechanism of the deviations, we take a closer look at the vibrational pattern of the affected Raman modes. The low frequency $\Gamma_{6g}(1)$ and $A_g(2)$ modes are pure samarium vibration modes along the $y$- and $z$-axis, respectively, while $B_{1g}(2)$, $A_g(3)$, and $B_{2g}(3)$ are rotation modes of the octahedra, which include samarium displacements. The anomalies of the pure samarium vibrations ($B_{1g}(1)$ and $A_g(2)$) are a clear sign of a modification of the Sm$^{3+}$ sublattice emerging from the non-spontaneous alignment of the samarium spins. Changes of the tilt vibrations, $B_{1g}(2)$, $A_g(3)$, and $B_{2g}(3)$, are, at first sight, less intuitive to relate to the Sm$^{3+}$ spin ordering. However, in the same way as the rotations of the octahedra affect the interaction of neighboring iron spins, FeO$_6$ rotations alter the Fe-O-Sm coupling path. The orientation of the samarium-spin sublattice is steered by the trilinear coupling of Fe$^{3+}$ spins, Sm$^{3+}$ spins and the octahedral tilt system, as proposed theoretically by Zhao and co-workers$^{14}$.

Hence, the effective field acting on the Sm$^{3+}$ spins is of magneto-structural origin and links the samarium magnetism to the rotations of the octahedra. The FWHM that are commonly more susceptible to coupling phenomena show anomalies for all phonon modes below 350 cm$^{-1}$, i.e. modes that include Sm$^{3+}$ motions. Only motions in $x$-direction are not affected, which epitomises the naturally anisotropic character of the Sm$^{3+}$-Fe$^{3+}$ spin interaction. For a further discussion see Supplementary Note 2. Overall, the interaction between Sm$^{3+}$ and Fe$^{3+}$ gives rise to the emergence of spin–phonon coupling, which we probe as a strong anomaly of samarium and octahedron vibrations.

New Raman features are highlighted in Fig. 4 as red-shaded areas. These features are not observed at ambient conditions but emerge gradually with decreasing temperature at 112 and 224 cm$^{-1}$ in $z(xy)yz$ as well as 130, and 287 cm$^{-1}$ in $y(xz)yz$ configuration, using Porto’s notation$^{37}$. To better illustrate the emergence, we show in Fig. 4e how the features at 130 and 287 cm$^{-1}$ gain in intensity with decreasing temperature. (For further emergent feature see Supplementary Note 3).

To understand the consequences that come with the emergence of new Raman features, we need to identify their nature. Firstly, the new bands cannot be previously masked vibration modes, since all vibrational bands of $Pnma$ symmetry in SmFeO$_3$ have been identified$^{24}$. We need to consider the following typical origins for the new features:

(i) **Sm$^{3+}$ crystal-field excitations:** Because of the non-centrosymmetric position of Sm$^{3+}$ ions, the ground-state energy of samarium is split. The interaction between rare-earth and iron can impact these low energy levels as earlier investigations of ReFeO$_3$ show$^{38–43}$. However, such bands have only been observed by submillimeter spectroscopy and low frequency Raman modes are limited to the well-known magnon excitations of the Fe$^{3+}$ spin$^7$. Overall, electronic Sm$^{3+}$ excitations are expected at frequencies below 100 cm$^{-1}$, much lower than the position of our new Raman active features. Therefore, we exclude low energy Sm$^{3+}$-transitions as origin of the new features.

(ii) **Two-magnon bands result from scattering of two magnetic excitations not only at the $\Gamma$-point but also at the zone boundary. Therefore, they can be found at higher frequencies. Resulting
The phonon spectrum (deviations $< 0.5$ cm$^{-1}$) try breaking and induced ferroelectricity are barely detectable in spontaneous ordering of both, the Gd$_3$TbMnO$_3$, the symmetry breaking can only be hypothesized from characteristics. With the ordering of the magnetic Gd$_3$TbMnO$_3$ NATURE COMMUNICATIONS | https://doi.org/10.1038/s41467-021-27267-8 ARTICLE

The changes to the Raman spectra, however, show identical anomalies of the vibrational modes. Excluding the previous processes, see for example in TbMnO$_3$ upon the transition into the incommensurate multiferroic phase$^{44}$. However, since the single-magnon bands do not show an anomalous behavior below room temperatures, a magnonic nature of the new bands is unlikely (see Supplementary Note 7).

(iii) New phonons: The shape of the emerging bands at 112, 224 and 287 cm$^{-1}$ strongly resemble the neighboring phonon modes. In addition, these features emerge simultaneously with the anomalies of the vibrational modes. Excluding the previous options, we therefore assign these bands as new phonon bands.

To put these findings into context, we compare them with well-known systems that experience a magnetically induced phase transition. In collinearly antiferromagnetic RMn$_2$O$_4$ the symmetry breaking and induced ferroelectricity are barely detectable in the phonon spectrum (deviations $< 0.5$ cm$^{-1}$) and no new Raman bands are observed$^{45-48}$. Likewise, phonon deviations in spin-spiral systems are below the resolution limit, e.g. in MnW$_2$O$_7$.$^{49}$ In TbMnO$_3$, the symmetry breaking can only be hypothesized from shifts of the vibration frequencies smaller than 1.5 cm$^{-1}$ and new extremely broad features are assigned to two-magnon excitations$^{50}$. Overall, anomalies in SmFeO$_3$ driven by the interplay of iron and samarium exceed these examples by one order of magnitude. Furthermore, it is instructive to compare SmFeO$_3$ to its ferroelectric sibling GdFeO$_3$. Unlike SmFeO$_3$ where the Sm$^{3+}$ sublattice order is induced, the ferroelectric phase transition in GdFeO$_3$ results from the independent and spontaneous ordering of both, the Gd$^{3+}$ and the Fe$^{3+}$ sublattices. The changes to the Raman spectra, however, show identical characteristics. With the ordering of the magnetic Gd$^{3+}$ spins, Gd$^{3+}$ and octahedral tilt vibrations show the same anomalous deviations as in SmFeO$_3$ and the emergence of new bands$^{51}$. These similarities reinforce the assignment of the new features as phonons. Yet, the physical origins of the phenomena in GdFeO$_3$ and SmFeO$_3$ are strikingly different resulting from classical spontaneous Gd$^{3+}$-Gd$^{3+}$ ordering, as opposed to non-spontaneous, but iron-induced Sm$^{3+}$ ordering. Therefore, in GdFeO$_3$, the anomalies are limited to the ferroelectric phase below 2.5 K$^9$, while in SmFeO$_3$ they occur at two orders of magnitude higher temperatures.

Furthermore, the emergence of new phonon bands itself, in direct analogy to GdFeO$_3$, provides evidence for a change of phase in SmFeO$_3$ through a symmetry lowering. Raman spectroscopy does not allow for an identification of the symmetry. From the evolution of the phonon modes and the lattice constants (see Supplementary Note 9), we can estimate, however, that the material remains orthorhombic with the possible point groups 222 or mm2. This consequence of the Fe$^{3+}$-Sm$^{3+}$-interplay is astonishing and goes beyond a rise of strong spin–phonon coupling.

In conclusion, we scrutinized the spin–phonon coupling in SmFeO$_3$, a model material for the interaction of two magnetic ions, throughout all magnetic phases. Any coupling between the magnetic order parameters of iron alone and strain is weak, such that there are no obvious anomalies in the evolution of elastic moduli through the Néel critical point, on either side of the spin reorientation transition, or associated with the magnetic cluster glass formation. This is a reflection, primarily, of the fact that Fe$^{3+}$ is not Jahn-Teller active. On the other hand, there is a significant anelastic effect through the temperature interval of the spin reorientation transition, which is ascribed to relaxational magnetoelastic effects of locally strained regions that might possibly be monoclinic.

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**Fig. 4 Emerging of new phonon modes.** Raman spectra for $y(xz)\bar{y}$, a and $z(xy)\bar{z}$, c and d, configurations at 40 and 293 K, respectively. e Temperature dependent Raman spectra in $y(xz)\bar{y}$ configuration. The colored areas indicate new Raman-active bands.
Once the Sm$^{3+}$ and Fe$^{3+}$ spins start interacting, however, a strong spin–phonon coupling emerges. This coupling manifests in the anomalous evolution of vibrational bands and in the emergence of new Raman active modes. It is activated by the non-spontaneous, though intrinsic ordering of the Sm$^{3+}$ spins in the exchange field of the magnetic Fe$^{3+}$ sublattice. We observe strong indications—identical to the ferroelectric phase transition in GdFeO$\text{3}$—that this non-spontaneous ordering induces a phase change in SmFeO$\text{3}$. In addition, our findings support the theoretical prediction of the trilinear coupling between Fe$^{3+}$ and Sm$^{3+}$ spins and the FeO$_{6}$ tilt vibrations.\(^5\) While this seminal theoretical work focuses on the influence of the tilts on the magnetism, we demonstrate here the reverse-effect of the magnetism on the structural vibrations.

We have shown how the non-linear interplay of two magnetic orders can trigger significant variations of lattice motions. We expect that the presented effects are not limited to SmFeO$\text{3}$, but likely exist in a vast variety of systems like rare-earth manganites, ferrites or chromites, where magnetic transition-metal sublattices impose a magnetic ordering on rare-earth sublattices. We have shown that such non-linear coupling of magnetic orders can give rise to enhancement phenomena and even new phases exceeding by far the sum of the initial properties. We expect that such phenomena are not limited to magnetic orders but may play a role for a large number of interacting orders. Importantly, these effects emerge just below room temperature and are not limited to cryogenic temperatures which makes them attractive for potential applications. This work motivates the specific search for hidden non-linear material responses, in experiment and theory, to achieve a conclusive picture of the microscopic interaction mechanisms at play and their potential exploration in technology applications.

**Methods**

**Sample preparation.** SmFeO$\text{3}$ single crystal samples were grown in a four-mirror optical floating-zone furnace (FZ-T-10000-H-VI-P-SH, Crystal Systems Corp.) as described elsewhere.\(^6\) Crystals of all three orthorhombic orientations were prepared, lapped to a thickness of 80 $\mu$m and polished optically flat.

**Raman spectroscopy.** Raman spectroscopy measurements were performed with an inVia Renishaw Reflex Raman Microscope in micro-Raman mode with a 633-nm He-Ne laser. We avoided sample heating by limiting the laser power. Frequencies and FWHM of the phonon modes were obtained by fitting the Raman spectra with Lorentzian functions. During the Raman scattering experiments, the temperature of the crystals was controlled using a Linkam THMS600 stage and an Oxford Instruments Microstat for cryogenic temperatures.

**Resonant ultrasound spectroscopy.** The technique of Resonant Ultrasound Spectroscopy (RUS) involves the measurement of acoustic resonances of mm-sized samples between two piezoelectric transducers and has been described in detail by Migliori and Sarrao.\(^7\) The first transducer excites mechanical vibrations, typically in the frequency range 0.01–1 MHz, and the second detects resonances at frequencies which depend on the size, shape and density of the sample and on the values of its elastic moduli.

Individual peaks in the primary spectra are fitted to determine their frequency, $f$, and width at half maximum height $\Delta f$. Each resonance is typically dominated by shear vibrations and the square of the resonance frequencies scales with different combinations of the (predominantly shear) elastic moduli. Acoustic loss is expressed in terms of the inverse mechanical quality factor, $Q^{-1}$, which is taken to be $\Delta f/f$. Two different instruments were used for measurements above and below room temperature. In the low temperature instrument, the sample sits directly between the transducers and the holder is lowered into a helium flow cryostat. A few mbars of helium are added to the sample chamber to assist thermal equilibration between the sample and the cryostat. In the high temperature instrument, the sample sits between the tips of alumina buffer rods which are inserted into a horizontal resistance furnace with the transducers attached to the ends of the rods, outside the cryostate.

An irregular fragment with dimension $1 \times 1 \times 1 \text{mm}^3$ and mass 0.0158 g was selected for study on the basis that it did not show any externally visible cracks. Spectra containing 65,000 data points were collected in automated cooling/heating sequences using a settle time of 20 min at each set point to allow for thermal equilibration. Liquid nitrogen was used for cooling down to $-110 \text{K}$. For the high temperature measurements, the sample was held in an argon atmosphere. Selected peaks in the primary spectra were fitted with an asymmetric Lorentzian function to extract values of $f$ and $\Delta f$ as a function of temperature, using the software package Igor (Wavemetrics).

**Data availability**

The Raman spectroscopy and Resonant Ultrasound Spectroscopy data generated in this study have been deposited in the Research Collections database of the ETH Zurich under accession code https://doi.org/10.3929/ethz-b-0005124054.

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