Abstract

We numerically explore synthetic crystal diamond for realizing novel light sources in ranges which are up to now difficult to achieve with other materials, such as sub-10-fs pulse durations and challenging spectral ranges. We assess the performance of on-chip diamond waveguides for controlling light generation by means of nonlinear soliton dynamics. Tailoring the cross-section of such diamond waveguides allows to design dispersion profiles with custom zero-dispersion points and anomalous dispersion ranges exceeding an octave. Various propagation dynamics, including supercontinuum generation by soliton fission, can be realized in diamond photonics. In stark contrast to usual silica-based optical fibers, where such processes occur on the scale of meters, in diamond millimeter-scale propagation distances are sufficient. Unperturbed soliton-dynamics prior to soliton fission allow to identify a pulse self-compression scenario that promises record-breaking compression factors on chip-size propagation lengths.

1. Introduction

Nonlinear diamond photonics provides an attractive technical basis for on-chip photonic applications [1], and has triggered numerous research efforts in recent years. Owing to the unique material properties of diamond [2, 3], given by its large Kerr nonlinearity, wide bandgap, high refractive index, negligible multi-photon loss, and transmission window spanning from the ultraviolet to the far-infrared, impressive demonstrations of photonic devices with novel functionalities have emerged. This includes, e.g., its use as a platform for quantum communication [4], and integrated high-$Q$ optical resonators [5, 1], operating at new wavelengths compared to existing chip-based nonlinear photonic devices for frequency comb generation [6, 3]. It thus exceeds its use in quantum optics applications and is becoming a versatile material for optical devices. A direct transfer of concepts from photonic crystal fibers and silicon-based waveguides [7, 8], such as, e.g., pulse-compression schemes and soliton-effects, to the diamond-based platform seems possible.

Here, we consider the supercontinuum generation process [9, 10, 11, 12], a paradigm of optical pulse propagation in fibers, which has revolutionized optical coherence tomography [13], and frequency metrology [14]. In common silica-based photonic crystal fibers, this process occurs on the lengthscale of several centimeters [15], or even meters [9]. We use the propagation properties of a diamond waveguide surrounded by silica [1], and demonstrate in terms of numerical simulations that the supercontinuum generation process unfolds on a much shorter, millimeter-length propagation scale. In our analysis, we investigate the propagation dynamics of ultrashort optical pulses via the generalized nonlinear Schrödinger equation [10], taking into account higher-order dispersion, pulse self-steepening [16, 17], and the Raman effect [18]. This accounts for various processes that support the generation of widely extended supercontinuum spectra, such as the modulation instability [19], soliton-fission [20, 21], and self-frequency shift of Raman solitons [18]. The initial stage of the supercontinuum generation process allows to identify a pulse self-compression mechanism based solely on soliton-effects [22, 23]. Exploiting this mechanism for higher-order soliton compression, we achieve record-breaking pulse-compression factors, outperforming recent studies in silicon-nitride waveguides [23]. For instance, the compression of a hyperbolic-secant shaped input pulse of 300 fs, corresponding to a higher-order soliton of or-
nder $N = 15$, down to 5.4 fs is achieved on a propagation length of only 6.33 mm. In this respect, diamond allows to consider comparatively high pulse intensities enabling conditions that facilitate high-order soliton propagation effects when pumping in the domain of anomalous dispersion. The fabrication of diamond waveguides with cross-sections that allow to engineer the required dispersion profiles, working at telecom wavelengths and exhibiting the key-feature of a wide domain of anomalous dispersion, is technically feasible [1, 24]. In this regard, since silica-based fibers have clear limitations concerning transparency and convenient dispersion profiles (as described in Sect. 2 below), working with diamond seems beneficial, e.g., the ability to engineer unusual dispersion profiles with several zero-dispersion points leads to the observation of new phenomena [25, 26, 27, 28, 29].

In Sect. 2 we introduce the numerical model for nonlinear pulse propagation in more detail. Section 3 contains the analysis of the supercontinuum generation process and the pulse self-compression scheme in the considered diamond waveguide. Finally, we discuss our results and conclude in Sect. 4.

2. Methods

For the numerical simulation and analysis of the nonlinear z-propagation dynamics of ultrashort laser pulses we use the generalized nonlinear Schrödinger equation (GNLS) [10, 15]

$$\partial_t A = i \sum_{n \geq 2} \beta_n (i \partial_{z})^n A + i \gamma (1 + i \omega_0^{-1} \partial_z) A(z,t) \int R(t') A(z,t-t')^2 \, dt', \quad (1)$$

for a complex-valued field $A \equiv A(z,t)$ on a periodic time-domain of extent $T$ with boundary condition $A(z, -T/2) = A(z, T/2)$. In Eq. (1), $t$ is a retarded time measured in a reference frame moving with the group velocity at $\omega_0$, where $\omega_0$ is a reference frequency with units rad/ps. The real-valued coefficients $\beta_n$ specify the dispersion coefficients of order $n$ with units ps$^n$/m, and $\gamma$ specifies the nonlinear coefficient with units W$^{-1}$/m.

To model dispersive and nonlinear effects in diamond waveguides we use a propagation constant $\beta(\Omega) = \sum_{n \geq 2} (\beta_n / n!) \Omega^n$, where $\Omega = \omega - \omega_0$ defines an angular frequency detuning, characterized by the relative group delay $\beta_1(\Omega) = \beta_2(\Omega)$ shown in Fig. 1(a), and group-velocity dispersion $\beta_2(\Omega) = \beta_2(\Omega)$ shown in Fig. 1(b). This broadband anomalous dispersion profile characterizes a silica embedded diamond waveguide with height $H = 950$ nm and width $W = 875$ nm, extracted from Ref. [1]. This waveguide device was designed for the telecom wavelength range and exhibits a wide domain of anomalous dispersion, bounded by zero dispersion points at $\lambda_{21} \approx 843$ nm and $\lambda_{22} \approx 2340$ nm, see Fig. 1. We further use $\gamma = 9.6 \, \text{W}^{-1}/\text{m}$ [24]. The Raman effect is included via the total response function

$$R(t) = (1 - f_R) \delta(t) + f_R h_R(t), \quad (2)$$

where the first term defines the instantaneous Kerr response, and where the second term specifies a generic two-parameter Raman response function [30, 31]

$$h_R(t) = \frac{\tau_1 \tau_2}{\tau_1 + \tau_2} e^{-t/\tau_1} \sin(t/\tau_1) \Theta(t), \quad (3)$$

with fractional contribution $f_R$, with the Heaviside step-function $\Theta(t)$ ensuring causality. To model the Raman effect in diamond waveguides we here use $f_R = 0.2$, $\tau_1 = 4.0$ fs, and $\tau_2 = 5.7$ fs [32]. Using a discrete sequence of angular frequency detunings $\Omega = \omega - \omega_0 \in 2\pi T^{-1} Z$, the expressions

$$A_\Omega(z) = \frac{1}{T} \int_{-T/2}^{T/2} A(z, t) e^{i \Omega t} \, dt, \quad (4a)$$

$$A(z, t) = \sum_\Omega A_\Omega(z) e^{-i \Omega t}, \quad (4b)$$

Figure 1: Characteristics of the propagation constant of the considered diamond waveguide, reproduced following Fig. 5(a) Ref. [1]. (a) Frequency dependence of the relative group delay (rGD). (b) Frequency dependence of the group-velocity dispersion (GVD), with zero-dispersion points at $\lambda_{21} \approx 843$ nm and $\lambda_{22} \approx 2340$ nm. Domsains of normal dispersion are shaded gray. Top axis in (a) indicates the detuning $\Omega$, related to the wavelength through $\lambda = 2\pi c/(\omega_0 + \Omega)$ with speed of light $c$. 

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specify forward [Eq. (4a)], and inverse [Eq. (4b)] Fourier transforms, relating the field envelopes \( A(z,t) \) to the spectral envelopes \( A_\Omega(z) \). The energy of the field \( A \) can be written in the form \( E(z) = \hbar \sum_\Omega \eta_\Omega(z) (\omega_\Omega + \Omega) \), where \( \hbar \) is the reduced Planck constant, and where the dimensionless quantity \( \eta_\Omega(z) \equiv T[A_\Omega(z)]^2/\{h(\omega_\Omega + \Omega) \} \) specifies the number of photons with energy \( h(\omega_\Omega + \Omega) \). Consequently, the total number of photons is given by

\[
C_{\text{ph}}(z) = \frac{2\pi}{\hbar \Delta \Omega} \sum_\Omega \frac{|A_\Omega(z)|^2}{\omega_\Omega + \Omega}.
\]

Let us note that the GNLS (1) conserves the total number of photons \( C_{\text{ph}} \), but does not conserve the energy \( E \) due to the Raman interaction and self-steepening [30]. The numerical simulations in terms of the GNLS reported below are performed using the variable stepsize “conservation quantity error” (CQE) method [33, 34, 35, 36], with stepsize selection guided by \( C_{\text{ph}} \). To assess time-frequency interrelations within the field \( A \) at a selected propagation distance \( z \), we use the spectrogram [37, 38]

\[
P_s(t, \Omega) = \frac{1}{2\pi} \left| \int_{-T/2}^{T/2} A(z,t')h(t'-t)e^{-i\Omega t'} \, dt' \right|^2,
\]

wherein \( h(x) = \exp(-x^2/2\sigma^2) \) is a Gaussian window function with root-mean-square width \( \sigma \), allowing to localize \( A \) in time.

3. Results

Supercontinuum generation. Below we compare a supercontinuum generation process in a standard silica-based optical fiber with with properties detailed in Ref. [15], to supercontinuum generation in a silica surrounded diamond waveguide exhibiting the dispersion properties detailed in Fig. 1. Results of numerical simulations using initial hyperbolic-secant pulses \( A_0(t) = P_0 \text{sech}(t/t_0) \) with peak power \( P_0 \) and duration \( t_0 \) are shown in Fig. 2 (parameters are detailed below). Starting from the spectrally narrow input pulse, the interplay of linear and nonlinear effects inherent to Eq. (1) leads to an enormous spectral broadening. This involves soliton fission, i.e. the successive breakup of the initial pulse into fundamental solitons, see the insets of Fig. 2(a) and Fig. 2(d), for a silica-fiber and a diamond waveguide, respectively. The pulse breakup is accompanied by the generation of dispersive waves in the domain of normal dispersion, extending the spectrum towards the blue side. Due to the Raman effect these solitons experience a self-frequency shift [Figs. 2(b,e)], extending the red side of the spectrum and resulting in a deceleration of the pulses in the time domain [Figs. 2(a,d)]. Under certain conditions, the ejected solitons form strong refractive index barriers that cannot be surpassed by quasi group-velocity matched dispersive waves in the domain of normal dispersion, resulting in reflection processes that further extend the blue side of the spectrum [15, 39, 40, 41]. Instances of such reflection processes are visible in the spectrograms in Figs. 2(c,f). While both supercontinuum generation processes look very similar regarding the structure of their underlying soliton fission processes, see insets of Figs. 2(a,d), and spectrum, see Figs. 2(b,e), both occur on very different energy scales and propagation distances. Let us note that a fundamental soliton for the silica-based optical fiber with \( \beta_2 = -0.011 \text{ ps}^2/\text{m} \), \( \gamma = 0.1 \text{ W}^{-1}/\text{m} \), and, say, \( t_0 = 0.1 \text{ ps} \), would require a peak power \( P_0 \approx 11 \text{ W} \) and yield a soliton period \( z_s = (\pi/2)L_D \approx 1.4 \text{ m} \) (dispersion length \( L_D = \frac{\gamma t_0^2}{|\beta_2|} \)). Such a fundamental soliton would have energy \( E = 2.2 \text{ pJ} \). In contrast, a diamond waveguide with \( \beta_2 = -0.26 \text{ ps}^2/\text{m} \), \( \gamma = 9.6 \text{ W}^{-1}/\text{m} \), and \( t_0 = 0.1 \text{ ps} \) requires only \( P_0 = 2.7 \text{ W} \) and exhibits \( z_s \approx 0.006 \text{ m} \). In this case, \( E = 0.54 \text{ pJ} \). i.e. the energy required for the fundamental soliton is smaller by about a factor of four. For the supercontinuum generation process shown in Fig. 2, in case of the silica-based optical fiber, the initial pulse had peak power \( P_0 = 10 \text{ kW} \) and duration \( t_0 = 28.4 \text{ fs} \), injected at \( \omega_0 = 2.26 \text{ rad} / \text{fs} \left( \lambda_0 = 835 \text{ nm} \right) \), corresponding to a soliton of order \( N \approx 8.7 \). In case of the diamond waveguide, \( P_0 = 1.66 \text{ kW} \), \( t_0 = 20 \text{ fs} \), and \( \omega_0 = 1.82 \text{ rad} / \text{fs} \left( \lambda_0 = 1035 \text{ nm} \right) \), corresponding to a soliton of order \( N = 7 \). Let us point out that while the supercontinuum generation process in the silica fiber develops on a lengthscale of 12 cm, a similar dynamics in case of the diamond waveguide unfolds on merely 6 mm.

Self-compression scheme. The initial stage of the above supercontinuum generation processes, which is characterized by an enormous spectral broadening, allows to identify a pulse compression scheme, which, in the case of the diamond waveguide [Figs. 2(d-f)], proceeds on a propagation scale of less than a millimeter. Subsequently we discuss this initial self-compression of a higher-order soliton, occurring in the time-domain, in more detail. The narrowing of picosecond pulses in a silica-based single-mode optical fiber in a domain of anomalous dispersion was demonstrated experimentally in Ref. [22]. Therein, pulses with initial duration of \( t_0 \approx 4 \text{ ps} \) (7 ps FWHM according to Ref. [22]) were compressed to about 1/27 of their initial duration within a fiber of length 320 m. The underlying mech-
anism builds upon soliton effects: for a negative value of group-velocity dispersion and for high pulse intensities, exceeding that of a fundamental soliton, the resulting chirp across the pulse leads to pulse narrowing upon propagation; after the pulse attains maximum compression, soliton fission occurs [see Fig. 2(d)]; the higher the initial intensity, the smaller the propagation distance that is required to reach the point of maximum compression. A qualitative analysis of the propagation dynamics of solitons of high order $N$ in terms of the common nonlinear Schrödinger equation (NLS), i.e. Eq. (1) with $f_R = 0$ and nonzero $\beta_2 < 0$ only, resulted in approximate scaling laws for the maximally attainable self-compression (SC) factor [22, 23]

$$F_{SC} = 4.1N,$$  \hspace{1cm} (7)

and the optimal self-compression distance [22, 23]

$$z_{SC} = \frac{L_D}{N} \left( 0.32 + \frac{1.1}{N} \right),$$  \hspace{1cm} (8)

where $L_D = t_0^2/|\beta_2|$ is the dispersion length of the initial pulse and $z_{SC}$ specifies the propagation distance at which the compression factor $F_{SC}$ is achieved.

Subsequently we transfer the concept of this soliton-effect pulse compression scheme to diamond waveguides with dispersive and nonlinear properties detailed in Sect. 2. Specifically, we consider the operating wavelength $\lambda_0 = 1540$ nm ($\omega_0 = 1.212$ rad/fs), at which $\beta_2(\omega_0) \approx -0.59$ ps$^2$/m, and hyperbolic secant pulses of duration $t_0 = 0.3$ ps. Figure 3 summarizes the results of our numerical simulations for soliton orders $N = 10, 15,$ and, $20$. In Figs. 3(a,b) we compare the theoretical predictions of Eqs. (7),(8) with simulations performed in terms of the full GNLS, given by Eq. (1). The good agreement with the above approximate scaling laws does not come as a surprise: during the initial propagation stage, i.e. well before soliton fission sets in, the dynamics is well described by the common NLS. In this regard, an important requirement is that the underlying group-velocity dispersion exhibits a nearly flat anomalous dispersion profile, extending over a wide
wavelength range. Problems concerning the compression limit [42], due to an overlap of the spectrally broadened pulse with the domain of normal dispersion, are thus also reduced. For instance, at $N = 15$, we find that the initial pulse compresses down to 5.4 fs, resulting in a self-compression factor $F_{SC} \approx 0.56$ at the optimal self-compression distance $z_{SC} = 6.33$ mm. Both these values are obtained from pulse propagation simulations in terms of the GNLS (1). Note that for the largest compression factors, the peak intensity might achieve a TW/cm$^2$ level, in which case higher-order effects such as interband-transitions (multi-photon absorption) start to play an increasing role. A visual account of the achieved compression is given in Fig. 3(c), where the pulse intensity at $z_{SC}$ is compared to its initial trace for the above three choices of $N$. Similar as in Ref. [22], we observe that for increasing $N$, an increasingly narrow central peak on top of a broad pedestal emerges. The propagation dynamics for the case $N = 15$ is demonstrated in Figs. 3(d,e): in the propagation range up to $z_{SC}$, the pulse self-compression and increase in peak intensity [Fig. 3(d)], accompanied by spectral broadening [Fig. 3(e)], is clearly evident; immediately beyond $z_{SC}$, soliton fission sets in. Let us emphasize that the considered diamond waveguides support the propagation of ultrashort solitons at rather low pulse intensities. This is a special property enabled by diamond waveguides. Finally, let us note that upon approaching $z_{SC}$, the peak intensity increases at a strongly increasing rate, see Fig. 3(f). This requires an adequate adjustment of the device length or input power to optimally exploit this compression scheme.

4. Discussion and conclusions

In summary, we studied the nonlinear propagation dynamics of optical pulses in diamond waveguides in terms of the generalized nonlinear Schrödinger equation. Specifically, we considered a waveguide device, designed for the telecom wavelength range with a wide domain of anomalous dispersion [1]. We demonstrated that the supercontinuum generation process, which for silica-based optical fibers usually occurs on the scale of centimeters or even meters, occurs already on the scale of millimeters. Owing to the strong optical nonlinearity of diamond and the large negative value of the achievable waveguide group-velocity dispersion, this process not only occurs on much shorter propagation scales, it also requires much lower pulse energies. Recognizing that the propagation dynamics prior to soliton-fission is always characterized by pulse narrowing, directly allows to transfer a simple and efficient pulse compression scheme to the diamond platform, promising record-breaking compression factors on chip-size propagation distances.

This compression scheme, which is solely based on soliton effects in a domain of anomalous dispersion, has recently been studied experimentally within SiN
waveguides [23]. Therein, pulses with initial duration of 1.2 ps and soliton order $N \approx 19$ were compressed to about 1/18 of their initial duration within a low-loss, dispersion engineered waveguide of 40 cm length. This experimentally achieved compression factor is much below the theoretical prediction $F_{\text{SC}} \approx 78$ obtained via Eq. (7). Also, earlier efforts to exploit this self-compression mechanism did not yield compression factors larger than 11 [43, 8, 44]. In our case, the compression factor can simply be increased by starting with an initial pulse duration in the picosecond range and using longer propagation distances. The limitation of this compression scheme is given mainly by the extend of the domain of anomalous dispersion, supporting undisturbed soliton propagation.

While the presented study has a focus on diamond waveguides with a simple geometry, we expect that other waveguide devices fabricated on basis of synthetic diamond, such as angle-etched [45], and fin-shaped structures [46], behave in a qualitatively similar manner. The reported findings are of fundamental interest to nonlinear optics, and provide further insight into the complex propagation dynamics of ultrashort pulses in diamond waveguides.

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