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Observation of in-plane magnetic field induced phase transitions in FeSe

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We investigate thermodynamic properties of FeSe under in-plane magnetic fields using torque magnetometry, specific heat, and magnetocaloric measurements. Below the upper critical field $H_c2$, we observed the field induced anomalies at $H_1 \sim 15$ T and $H_2 \sim 22$ T near $H || ab$ and below a characteristic temperature $T^* \sim 2$ K. The transition magnetic fields $H_1$ and $H_2$ exhibit negligible dependence on both temperature and field orientation. This contrasts to the strong temperature and angle dependence of $H_2$, suggesting that these anomalies are attributed to the field induced phase transitions, originating from the inherent spin-density-wave instability of quasiparticles near the superconducting gap minima or possible Flude-Ferrell-Larkin-Ovchinnikov state in the highly spin-polarized Fermi surfaces. Our observations imply that FeSe, an atypical multiband superconductor with extremely small Fermi energies, represents a unique model system for stabilizing unusual superconducting orders beyond the Pauli limit.

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I. INTRODUCTION

In conventional superconductors, spin polarization can destroy superconductivity when Zeeman energy surpasses the binding energy of Cooper pairs, known as the Pauli paramagnetic limit. In unconventional superconductors, however, exotic superconducting phases have been observed beyond the Pauli limit [1–10], often coexisting with complex magnetic orders. For example, the Fulde-Ferrel-Larkin-Ovchinnikov (FFLO) state was proposed a half century ago [1,2], in which s-wave Cooper pairs acquire a finite center-of-mass momentum to form a spatially modulated superconducting order [3–5]. Alternatively, spin-triplet pairing of field induced quasiparticles can occur particularly in unconventional d-wave superconductors, inducing novel phases with mixture of spin-singlet and spin-triplet pair density waves [6–10]. Growing evidence has revealed that the former and the latter are realized in highly anisotropic organic superconductors and a heavy fermion superconductor CeCoIn$_5$, respectively [10–12]. In both systems, however, the typical field induced spin imbalance $\sigma = (n_\uparrow - n_\downarrow)/(n_\uparrow + n_\downarrow)$, where $\uparrow$ and $\downarrow$ refer to the two spin components with densities $n_\uparrow$, is at most a few percent. Realization of the highly spin-imbalanced superconductivity and possible field induced exotic phases have been remained elusive so far.

Usually in single-band superconductors, Cooper pairs are broken by the orbital pair breaking effect or by the Pauli paramagnetic effect [13]. The orbital pair breaking effect destroys superconductivity at the relatively low upper critical fields $H_c2$ with negligible spin imbalance. Even the orbital effect is largely suppressed, the Pauli paramagnetic effect limits the spin imbalance, typically $\sigma \sim 10^{-2}$. This is because the maximum Zeeman energy $\mu_B H_2$ ($\mu_B$, Bohr magneton) is set by the superconducting gap $\Delta_{SC}$ and usually much smaller than the Fermi energy $E_F$. Multiband superconductors however may host the strongly spin imbalanced state. If the $E_F$ is small in one band with a small $\Delta_{SC}$ and the superconductivity is maintained by the other band with a relatively larger $\Delta_{SC}$ [14,15], spin polarization can be significantly enhanced under high magnetic fields.

Such a candidate is FeSe with $\sigma \sim 10^{-1}$. FeSe is known to be in the so-called BCS-BEC (Bose-Einstein condensate) crossover regime ($\Delta_{SC} \sim E_F$) [16,17] and also in the Pauli limiting regime ($\mu_B H_2 \sim \Delta_{SC}$) [16,18] under in-plane magnetic fields. Possible magnetic field induced phase transitions have been suggested under the out-of-plane fields [16] and very recently, also in the in-plane fields [19]. Therefore FeSe can be a model system to study whether, and if so how, competing magnetic or superconducting instabilities trigger exotic field induced phases in multiband superconductors [20–22] or in the large spin imbalance regime [23–25]. In this work, using torque magnetometry, specific heat, and magnetocaloric measurements, we identified successive anomalies...
with increasing in-plane magnetic field, below \( H_{c2} \) at low temperatures and in the clean limit. These results evidence that unusual superconducting phases are indeed stabilized in FeSe at high in-plane magnetic fields.

II. EXPERIMENTS

Single crystals of FeSe were grown by a KCl-AlCl\(_3\) flux technique [26–28]. The resistivity of single crystals were measured using the standard four-probe method in a Physical Property Measurement System (PPMS-14T, Quantum Design) in order to determine the residual resistivity ratio (RRR). Single crystals with the RRR value higher than 35 were used in the high magnetic field experiments unless otherwise noted (Fig. S3 [29]).

The upper critical field \( H_{c2} \) of FeSe was determined using the resistivity and the tunnel diode oscillator (TDO) frequency measurements at high magnetic fields. We measured the resistive transition under magnetic field up to 30 T in National High Magnetic Field Laboratory (NHMFL), Tallahassee. For resistivity measurements, a room temperature cured silver paste/epoxy was used to connect gold wires to the sample. The TDO measurements up to 30 T were performed in International MegaGauss Science Laboratory in Institute for Solid State Physics (ISSP), University of Tokyo. In the TDO measurements, we recorded the change of the radio frequency in an LC circuit with a crystal wound in a copper coil. For pressure experiments, quasi-hydrostatic pressure was applied up to 35 kbar using a home-made indenter-type pressure cell. The superconducting transition of lead, mounted next to the crystal, typically 100 \( \mu \)m in diameter, was monitored, which is proportional to the magnetic torque acting on the cantilever. The in-plane magnetic field is applied along the sample edge (Fig. S5 [29]).

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The thermodynamic anomalies in the superconducting state were observed using the measurements on torque magnetometry, magnetocaloric effect, and specific heat under magnetic fields up to 30 T at NHMFL. For torque magnetometry measurements, we used a miniature Seiko piezoresistive cantilever. On top of the cantilever we mounted a small single crystal, typically 100 \( \times \) 100 \( \times \) 20 \( \mu \)m\(^3\), extracted from the crystal whose RRR value was determined from the preceding resistivity measurements. During the up- and down-sweeps of the applied magnetic field, the resistance of the piezoelectric cantilever was monitored, which is proportional to the magnetic torque acting on the cantilever. The in-plane magnetic field is applied along the sample edge (Fig. S5 [29]), which is nearly along the diagonal direction of the or-thorhombic lattice. For magnetocaloric effect and specific heat measurements, the samples were mounted on top of a bare chip Cernox or RuO\(_2\) thermometer, suspended by manganin wires (diameter \( \sim \) 10 \( \mu \)m) as shown in Fig. S6 [29]. Detailed information on experiments are available in Ref. [29].

III. RESULTS

A. Characteristics of FeSe

FeSe is the simplest but an atypical member of FeSCs, which has \( T_c \approx 9 \) K and composed of edge-shared FeSe\(_4\) tetrahedra layers in van der Waals (vdW) structure [30]. The observed in-plane upper critical field \( H_{c2}^{ab} \approx 25 \) T is well above the Pauli limiting field \( H_p \approx 15.6 \) T at the BCS limit (\( H_p = 1.847 T_c \)), which indicates that FeSe is in the Pauli limit under in-plane magnetic fields (\( \mu_B H_{c2} \sim \Delta_{SC} \)). In addition, high-quality FeSe single crystals with a high residual resistive ratio (RRR) \( \geq 35 \) are in the clean limit, as confirmed by magnetic quantum oscillations studies [31–34] (Fig. S1 [29]).

More importantly, FeSe has exceptionally small Fermi energies [16,17]. In FeSe, three Fermi surfaces (FSs) exist; one electron band is centered at the \( \delta \) and \( \epsilon \) points and denoted as \( \delta \) and \( \epsilon \), respectively. The Fermi level \( E_F \) is indicated by the dashed line. (c) Fermi surfaces (FSs) of FeSe in the \( \delta \) plane. The gray shades display the anisotropic superconducting gap of each FS. The superconducting gap minima are marked by red arrows. (d) Fermi surfaces of FeSe. [(e) and (f)] Spin imbalance \( \sigma \) (e) and the change of the cross-sectional area \( \Delta A(H) \) in the \( k_z = 0 \) plane (f), as a function of magnetic field. For the hole FS (\( \alpha \)), \( A(H) \) of \( \uparrow \) spins become larger with increasing magnetic field, whereas \( A(H) \) of \( \downarrow \) spins is reduced. The electron FSs (\( \delta \) and \( \epsilon \)) show the opposite field dependence. The in-plane upper critical field \( (H_{c2}) \) is indicated by a grey vertical line.

FIG. 1. (a) Schematic crystal structure of FeSe. Fe atoms form an almost square lattice in the plane, and Se atoms are located above and below the center of Fe\(_4\) plaquettes. The orthorhombic crystal axes, \( a \) and \( b \) are indicated by the arrows. (b) Schematic band structure of FeSe. One hole band is centered at the \( \Gamma \) point and denoted as \( \alpha \), while two electron bands are located at \( X \) and \( Y \) points and denoted as \( \delta \) and \( \epsilon \), respectively. The Fermi level \( E_F \) is indicated by the dashed line. (c) Fermi surfaces (FSs) of FeSe in the \( k_z = 0 \) plane. The gray shades display the anisotropic superconducting gap of each FS. The superconducting gap minima are marked by red arrows. (d) Fermi surfaces of FeSe. [(e) and (f)] Spin imbalance \( \sigma \) (e) and the change of the cross-sectional area \( \Delta A(H) \) in the \( k_z = 0 \) plane (f), as a function of magnetic field. For the hole FS (\( \alpha \)), \( A(H) \) of \( \uparrow \) spins become larger with increasing magnetic field, whereas \( A(H) \) of \( \downarrow \) spins is reduced. The electron FSs (\( \delta \) and \( \epsilon \)) show the opposite field dependence. The in-plane upper critical field \( (H_{c2}) \) is indicated by a grey vertical line.

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and (e) 12 kbar. The external magnetic field was applied along the
temperatures. [(b)–(e)] Magnetic field dependent resistance \(R(H)\) at various temperatures and different pressures of (b) 0, (c) 1.4, (d) 9, and (e) 12 kbar. The external magnetic field was applied along the \(c\)-axis (top) and the \(ab\) plane (bottom).

Table S1 [29]. The Fermi energies for these bands are \(E_F\approx7.9, 6.1\), and 2.9 meV for \(\alpha\), \(\delta\), and \(\epsilon\) pockets, respectively. These values are comparable with their superconducting energies, \(\Delta SC\approx1.64, 1.53\), and 0.39 meV for \(\alpha\), \(\delta\), and \(\epsilon\) pockets, respectively [36,38]. The ratio \(\Delta SC/E_F\approx0.2\) for all the FSs, confirming that FeSe is in the BCS-BEC crossover regime.

Under magnetic fields, the Zeeman effect induces imbalance of spin population as well as momentum mismatch between FSs of \(\uparrow\) and \(\downarrow\) spins. In FeSe with three FSs, spin imbalance and momentum mismatch are different at each FS, as shown in Figs. 1(e) and 1(f). The spin imbalance in three FSs increases with magnetic fields and reaches up to 15% for \(\alpha\) and \(\delta\) FSs and 40% for \(\epsilon\) at \(H_{c2}\approx25\) T s, assuming the \(g\) factor of 2. These values are much larger than the typical value of a few % in other superconductors [16]. The momentum mismatch is also significant and is quantified by the size of \(\alpha\)-FS having a significant \(\Delta A=\alpha F\) and \(\alpha\)-FS with a significant \(\epsilon\)-FS warping [Fig. 1(f) and Fig. S8 [29]]. The \(\alpha\)-FS with \(\uparrow\) spin in the \(k_c=0\) plane may disappear at \(\sim40\) T, resulting in a magnetic Lifshitz transition [39] well above the in-plane \(H_{c2}\).

B. Upper critical fields

Having established that FeSe is simultaneously in the clean limit, in the BCS-BEC crossover regime, and in the Pauli limit under in-plane magnetic fields, we now discuss its magnetic phase diagram. To obtain the magnetic phase diagram, we investigated upper critical fields \(H_{c2}\) of FeSe using the TDO frequency and the resistivity measurements. Figure 2(a) shows the resonant frequency change, \(\Delta F(H)\), of the TDO circuit under magnetic fields up to 35 T for \(H\parallel c\) and \(H\parallel ab\). Figures 2(b)–2(e) display the magnetoresistance (MR) at different temperatures and pressures. Both \(\Delta F(H)\) and \(\rho(H)\) curves shift systematically to lower magnetic fields with increasing temperatures, which reflects the temperature dependence of \(H_{c2}(T)\). It is worth noting that MR is significantly enhanced above \(P_s\approx8\) kbar for \(H\parallel c\), as the long-range AFM order develops and reduces the magnetic scattering [33,40–42]. On the other hands, the MR is much weaker under the in-plane magnetic fields \(H\parallel ab\) reflecting the reduced orbital effect due to the layered crystal structure.

Using the TDO frequency and the resistivity measurements, we obtained upper critical field \(H_{c2}\) as a function of temperature [Fig. 3(a)] and field orientation [Fig. 3(b)], which are consistent with each other and independent of the types of measurements or criteria for determining \(H_{c2}\) (Fig. S2 [29]). For \(H\parallel c\), the zero-temperature upper critical field \(H_{c2}(0)\) is estimated to be \(H_{c2}\approx15\) T. At low temperatures, \(H_{c2}(T)\) data deviate from the conventional Werthamer-Helfand-Hohenberg (WHH) prediction, which is well explained by the two-band model, as found in other FeSCs with significant interband interactions [14,15]. We note that the field induced phase transition [16] observed at \(H\approx15\) T for \(H\parallel ab\) does not affect the \(H_{c2}(T)\) behavior.

In contrast, near \(H\parallel ab\), we observe unusual behaviors of \(H_{c2}\) in both the temperature- and the field angle-dependences. Here the in-plane magnetic field is applied along the diagonal direction of the orthogonal lattice [Fig. 1(a)] and thus denoted as \(H\parallel ab\). In this case, the quasi-2D nature of FeSe suppresses the orbital pair breaking effect and enhances \(H_{c2}(0)\) up to \(\approx25\) T, larger than \(H_{F}\) [Fig. 3(a)]. Usually in FeSCs, the Pauli-limiting effect is more important than the multiband orbital pair breaking effect under in-plane magnetic fields at low temperatures [14,15]. With a large Maki parameter \(\omega_M=\sqrt{2}H_{c2}/H_{F}>1\), where \(H_{c2}\) is the orbital-limiting upper critical field \(H_{c2}(O)=0.69T_c|\Delta H_{c2}/dT|_{T_c}\), \(H_{c2}(T)\) curves of FeSCs, such as LiFeAs [43], KFe\(_2\)As\(_2\) [44], exhibit a saturation behavior at low temperatures and are well described by the single-band WHH model [14,15]. In FeSe, however, we observed a weak but discernible kink in \(H_{c2}(T)\) curve at \(T^*\approx2\) K. Consistently the single-band WHH model with
measurements (open diamond). The WHH model predictions with FeSe, estimated from resistivity (open circle) and TDO frequency $T_c$ by $H_c^\alpha$ the WHH model curves (solid lines) with different Maki parameters overlap with each other. (d) and (e) Pressure dependence of Maki $H_c^\alpha$ parameter. For $H \parallel ab$, strong enhancement of $H_c^\alpha(0)$ below $T_c = 2 K$, indicated by shaded area, cannot be explained by the WHH model.

The pressure dependence of the low-temperature upturn in $H_c^\alpha(T)$ suggests that the observed upturn in $H_c^\alpha(T)$ is intimately related to the Pauli-limiting effect. It has been known that FS reconstruction occurs at a critical pressure $P_c \sim 8$ kbar [33], suggested by quantum oscillations and upper critical field studies. With external pressures below and above $P_c$, we found a systematic variation of $H_c^\alpha(T)$. For $H \parallel c$, $H_c^\alpha(T)$ curves, taken at different pressures and by $H_c^{orb}$, follow the same temperature dependence as clearly shown in Fig. 3(c). This implies that the relative ratios in the sizes or the diffusivity between dominant hole and electron pockets of FeSe are not significantly changed across $P_c$. On contrary, the Maki parameter $\alpha_{M}$, taken from the fit of $H_c^{\alpha}(T)$ curves to the WHH model, is reduced systematically with pressure [Fig. 3(d)]. At high pressures, therefore, the orbital-limiting effect becomes more important for determining $H_c^{orb}$ than the Pauli limiting effect. This is consistent with the fact that the slopes of $H_c^{\alpha}(T)$ at $T_c$, i.e., $dH_c^{\alpha}/dT|_{T_c}$ for $H \parallel ab$, that is proportional to the Fermi velocity along the $c$ axis, is reduced with increasing pressure [Fig. 3(e)] [45]. Concomitantly, the unusual upturn in $H_c^{\alpha}(T)$ at low temperatures is systematically suppressed and eventually disappears for $\alpha_{M} < 1$ [Fig. 3(c)]. These observations suggest the observed upturn in $H_c^{\alpha}(T)$ is not solely due to the multiband effect, but may reflect formation of field induced phase beyond the Pauli limit. In fact, this low-temperature behavior in $H_c^{\alpha}(T)$ resembles those of the unconventional Pauli-limiting superconductors, $\kappa$-(BEDT-TTF)$_2$Cu(NCS)$_2$, and CeCoIn$_5$ [4,10] (Fig. S2 [29]) and is consistent with the recent work on FeSe [19].

C. Magnetic field induced phase transitions

The signatures of unusual phase transitions below $H_c^{\alpha}$ and below $T^* \approx 2$ K are observed in the field-dependent torque magnetometry $\tau(H)$. The torque magnetometry is known to be extremely sensitive to the small changes in the magnetic susceptibility and usually exhibits a large magnetic hysteresis due to vortex pinning in superconductors [46,47] [Figs. 4(a) and 4(c)]. This produces a typical saw-tooth shaped curve of the field derivative $\tau(H)$, $d\tau/dH$, for up- and down-sweeps of magnetic fields. In FeSe, however, we observed two additional anomalies at $H_1 \sim 15$ T and $H_2 \sim 22$ T, as indicated by arrows in Figs. 4(a) and 4(b), well below the irreversible field $H_{irr}$ at which the hysteresis in $\tau(H)$ and $d\tau(H)/dH$ starts to develop. The transition fields $H_1$ and $H_2$ follow the distinct dependence on temperature or field angle from those of $H_{irr} \approx H_2$. Upon increasing temperature or the tilting angle of the magnetic field ($\theta$) from $H \parallel ab$ [Figs. 4(a) and 4(c)], $H_{irr}$ systematically decreases, similar to $H_c^\alpha$ [Figs. 4(a) and 4(b)]. In contrast, the anomalies are pronounced only at low temperatures below $T^*$ and near $H \parallel ab$ with $\theta \approx 15^\circ$. Also the transition fields $H_t$...
and \(H_2\) remain almost the same with variation of temperature or field angle.

These observations allow us to rule out the vortex-related phenomena as a possible origin for the anomalies at \(H_1\) and \(H_2\). It has been well known that the vortex phase transitions, such as melting or modification of the vortex structure and the peak effect, usually share the similar dependence on temperature and field orientation with the upper critical field \(H_c\) [48,49], particularly in highly anisotropic superconductors [48,49], like FeSe [50]. In contrast, the transition fields observed in FeSe are nearly independent of field angle. Instead, this is one of the characteristic features of the field induced exotic phases in e.g. \(\kappa\)-(BEDT-TTF)\(_2\)Cu(NCS)\(_2\) and CeCoIn\(_5\) [3,4,10]. Furthermore, we found that the anomalies at \(H_1\) and \(H_2\) are very sensitive to disorder, whose amount is quantified by the residual resistivity ratio, \(\text{RRR} = \rho(300 \text{ K})/\rho(T_c)\). As shown in Fig. S5 [29], the anomalies at \(H_1\) and \(H_2\) in \(\partial \tau(H)/\partial H\) are present for the crystals with a large \(\text{RRR} \geq 35\). In the crystal with a small \(\text{RRR} \approx 10\), we obtained the typical saw-tooth shaped curves of \(\partial \tau(H)/\partial H\) without additional anomalies. The strong sensitivity to disorder is also consistent with the field induced phase transition in the Pauli-limiting superconductors [3,4,10].

The magnetocaloric effect (MCE) provides further thermodynamic evidence regarding the field induced phase transitions. Once a superconducting sample is placed in a changing magnetic field, difference between the sample temperature \((T)\) and the bath temperature \((T_{\text{bath}})\) is determined by the entropy \((S)\) change and the specific heat \(C_s\) contribution and is described by \(\langle \delta S/\delta H \rangle_T = -(C_s/T)(dT/dH) - \kappa(T - T_{\text{bath}})/TH - (1/T)dQ_{\text{loss}}/dH\). Here, \(\kappa\) is the thermal conductivity between the sample and the environments [51], and \(Q_{\text{loss}}\) corresponds to an additional heat due to the irreversible effect. In our case, the sample is weakly coupled to the bath, due to a relatively low \(\kappa\), i.e., being close to the adiabatic condition. Then the field dependent temperature \(T(H)\) can be considered as an isentropic curve where the decrease (increase) of temperature implies the increase (decrease) of entropy.

With increasing magnetic field, we observed weak but clear anomalies in \(R_T(H)\) [Figs. 4(d) and 4(e)], the resistance of a temperature sensor attached to the crystal, which roughly proportional to the inverse of the sample temperature and becomes similar to the shape of the field dependent entropy, \(S(H)\). In conventional superconductors the monotonous field dependence of \(R_T(H)\) is usually expected with an anomaly only at \(H_c\). However in our experiments we observed additional anomalies in both up- and down-sweeps of magnetic fields at similar \(H_1\) and \(H_2\) (Fig. S6 [29]). With variation of temperature and field orientation, these MCE anomalies appears only below \(T^*\) and near \(H \parallel ab\) with \(\theta \leq 15^\circ\). The transition fields \(H_1\) and \(H_2\) are nearly independent of temperature and field angle, in good agreement with the \(\tau(H)\) results [Figs. 4(a) and 4(c)], as summarized in the magnetic phase diagrams as a function of temperature and field orientation [Figs. 5(a) and 5(b)].

The magnetic field dependent electronic specific heat \(C_s/T\) of FeSe also shows consistent results. In Fig. 4(f), we plot \(C_s/T\), taken at \(0.35\) K, as a function of the normalized magnetic field \(h = H/H_{ab}\) for \(H \parallel c\) and \(H \parallel ab\). In both cases, \(C_s/T\) increases rapidly at low magnetic fields below \(h < 0.3\), which indicates the field induced closing of smaller SC gaps mostly in the \(\delta\)- and the \(\epsilon\)-FSs, consistent with the previous report [38]. Thus at higher magnetic fields, the field dependence of \(C_s/T\) is dominated by the contribution from the \(\alpha\)-FS.
and is expected to follow a nearly linear field dependence below $H_{c2}$ for both $H \parallel c$ and $H \parallel ab$. This would make $C_s(h)/T$ curves collapsed into a single curve, once plotted as a function of the normalized $h$. However in FeSe at higher fields, $C_s(h)/T$ exhibit different behavior depending on the field orientations. For $H \parallel c$, $C_s(h)/T$ increases almost linearly until it is saturated at $H_{c2}$, as expected. In contrast, for $H \parallel ab$, $C_s(h)/T$ deviates from the linear field dependence at $h \approx 0.5$ with a slope change, and then recovers its normal state value at $H_{c2}$. The difference $\Delta C_s(h)/T = C_s(h)/T|_{hfcs} - C_s(h)/T|_{h|lc}$ reveals the anomaly more clearly. The drop of $\Delta C_s(h)/T$ by $\sim 0.4$ mJ mol$^{-1}$ K$^{-2}$ occurs clearly at $h \approx 0.5$, corresponding to $H_1 \approx 15$ T, while the anomaly $H_2 \approx 22$ T appears to be smeared out near $H_{c2}$. Combined with anomalies seen in torque and magnetocaloric measurements, the specific heat anomaly confirms the presence of field induced phases near the in-plane magnetic fields below $H_{c2}$.

IV. DISCUSSION

Now we discuss possible scenarios for the in-plane field induced phase transitions in FeSe. One candidate is the magnetic Lifshitz transition, involving the field induced change of the FS topology. This transition has been proposed to occur in FeSe due to the small $E_F$ [39], which is however unlikely because the following reasons. Firstly, in order to have a magnetic Lifshitz transition at $H \sim 20$ T, e.g., in the $\alpha$-FS having the smallest $A$ at $k_z = 0$, the $g$ factor of FeSe must be $\sim 5$–14, unreasonably large for FeSCs [52]. Secondly, the transition field for magnetic Lifshitz transition is set by electronic structures and is not directly related to the presence of the superconducting order. It is thus expected to occur even

in the normal state, which is not the case in experiments [39]. Experimentally the field induced phase transitions are only observed in the narrow ranges of temperature and field angle within the superconducting phase, and their phase boundaries are never extended to the normal state [Figs. 5(a) and 5(b)].

One possible candidate is then the FFLO phase [3,4]. In this case, the Cooper-pair state $(k \uparrow, -k + q \downarrow)$ is formed with a momentum mismatch $(q)$ between the spin-split FSs, inducing a spatially modulated superconducting order with a characteristic length of $q^{-1}$. In multiband superconductors, the FFLO state with the same global $q$ vector can appear above a transition field on all FSs [20], or each FS can have its own FFLO instability with a different modulation length $q_i^{-1}$ (i, band index), and these instabilities compete with each other, inducing the multiple FFLO orders at different magnetic fields [21,22]. It is however rather unlikely that both transitions observed at $H_1$ and $H_2$ in FeSe are due to the multiple FFLO transitions. Such a multiple FFLO ordering, if exists, is fragile to the interband coupling, because the FFLO instabilities with unequal $q$’s would average the interband pairing energy $\sim \Delta_i \Delta_2 \cos\{(q_2 - q_2) \cdot r\}$ to zero ($\Delta_i$, the superconducting gap at a different band $i$), and strongly reduces $T_c$ under magnetic fields. Therefore, multiple FFLO transitions are allowed only if the interband coupling are drastically suppressed. As discussed below, however, the nesting between spin-split FSs in FeSe are expected to be enhanced near $H_1$ and $H_2$ [Figs. 5(c) and 5(d)]. Furthermore, we found that the entropy is reduced across $H_1$ and $H_2$ for the up-sweep [Figs. 4(d) and 4(e)]. For typical FFLO transitions, entering to the FFLO phase in the up-sweep usually increases the entropy [53,54] because the additional quasiparticles are introduced due to the spatially-inhomogeneous superconducting gap.

FIG. 5. [(a) and (b)] Magnetic phase diagram of FeSe for $H \parallel ab$ as a function of temperature ($a$) and field orientation ($\theta$) with respect to the $ab$ plane (b). The upper critical field $H_{c2}^{\parallel}(T)$ (open symbols) are determined by resistivity (black open circle), TDO frequency (black open diamond), and torque magnetometry (black open star) measurements, while the field induced phase transitions at $H_1$ and $H_2$ are obtained by torque magnetometry (colored open star) and the magnetocaloric effect (colored solid triangle). The inset shows schematics of the possible nesting effect via $(0, \pi)$ or $(\pi, \pi)$ between the spin-split Fermi surfaces (FSs) with anisotropic superconducting gap (gray shade). Near $H_1$, the nesting effect is expected between $\delta \uparrow$ and $\epsilon \downarrow$ FSs via a SDW momentum $q = (\pi, \pi)$ (bottom), while the nesting with $q = (0, \pi)$ is expected near $H_2$ between $\alpha \downarrow$ and $\delta \downarrow$ FSs (top). (c,d) Magnetic field dependent Fermi vectors along two orthogonal directions of $k_x$ (c) and $k_y$ (d) for $\uparrow$ (solid line) and $\downarrow$ (dashed line) spins in the plane of $k_z = 0$. The good matches between the Fermi vectors of $\epsilon \downarrow$ and $\delta \downarrow$ FSs along the $k_x$ direction near $H_1$ and also between those of $\delta \downarrow$- and $\alpha \downarrow$-FSs along $k_y$ direction near $H_2$ are indicated by red and blue circles, respectively. The corresponding nesting conditions between different pairs of the spin-split FSs at $H_1$ and $H_2$ are schematically shown in the insets. The $k_z$ warping of each FS is indicated by different FS cross-section in the planes of $k_z = 0$ (inner line) and $k_z = \pi$ (outer line).
Another promising candidate is the spin-density-wave (SDW) phase of field induced quasiparticles. As it has been discussed for a $d$-wave superconductor CeCoIn$_5$ [10,55,56], the SDW order can be triggered by the nesting effect in the $k$-space near the superconducting gap nodes, where the superconductivity is suppressed by Pauli pair breaking. This nesting effect together with the residual AFM fluctuations is enhanced only in the superconducting state [55,56], allowing the coexisting SDW and superconducting phase. Recent experimental and theoretical studies [35,36,57,58] revealed that the hole ($\alpha$) and the electron ($\delta$ and $\epsilon$) FSs have the opposite in-plane momentum anisotropy in their superconducting gap as shown in Fig. 1(c). Furthermore, two different types of spin fluctuations are dominant in FeSe, the stripe-type spin fluctuation with $q = (\pi, 0)$ and the Neel-type one with $q = (\pi, \pi)$ [59].

Therefore, if the incipient spin fluctuations with $q = (\pi, 0)$ or $q = (\pi, \pi)$ strongly couple the field induced quasiparticles near the superconducting gap nodes or minima, the field induced SDW orders can coexist with the superconducting state and induce the SDW transitions in FeSe. Note that such a SDW order is stable only within the superconducting phase, which is consistent with our phase diagram [Figs. 5(a) and 5(b)] and compatible with the absence of FS reconstruction above $H_{c2}$ [31].

In order to consider the nesting instability of quasiparticles near the superconducting gap nodes or minima, we estimate the magnetic field dependent Fermi vectors $k_F$ in the planes of $k_z = 0$ [Figs. 5(c) and 5(d)] and $k_z = \pi$ (Fig. S9 [29]) along $k_x$ and $k_y$ directions. Unlike other superconductors, FeSe has an exceptionally small $E_F$, and the Zeeman effect with a typical $g$ factor of 2 [52] results in the spin-split FSs much different in size. This produces a large spin imbalance [Fig. 1(d)] and also significantly affects the nesting condition. We found that the nesting via $q = (\pi, \pi)$ nicely matches the $\epsilon$-FS of $\uparrow$ spins with the $\delta$-FS of $\downarrow$ spins along the $k_z$ direction at $H \sim 16$ T [Fig. 5(c)], in good agreement with the observed transition field $H_1 \sim 15$ T. This nesting effect with $q = (\pi, \pi)$ and the resulting interband scattering would suppress the FFLO instability. However, this can couple the field induced quasiparticles near the nodal superconducting gap regions of the $\delta$ and the $\epsilon$ FSs [the inset of Fig. 5(b)] through the Neel-type spin fluctuation [59], leading to the phase transition at $H_1$. In this case, the entropy is expected to be reduced upon entering the SDW phase in the up-sweep due to decrease of the number of degrees of freedom, in agreement with the experiments [Figs. 4(d) and 4(e)]. Moreover the specific heat is also expected to be reduced by the SDW gap formation of quasiparticles, again consistent with experiments [Fig. 4(f)]. The observed reduction of $C_v/T$ by $-0.4$ mJ mol$^{-1}$ K$^{-2}$ [Fig. 4(f)] is $\sim 10\%$ of the total density of states of $\delta$- and $\epsilon$-FSs, indicating that only quasiparticles near the nodal gap region participate the SDW formation.

The higher field phase transition at $H_2 \sim 22$ T appears to be more intriguing than one at $H_1$. We found another nesting condition via $q = (0, \pi)$ at $H \sim 24$ T, close to $H_2$, at which the $\alpha$-FS of $\uparrow$ spins matches well with the $\delta$-FS of $\downarrow$ spins along the $k_y$ direction at $k_z = 0$ [Fig. 5(d)] and also along the $k_z$ direction at $k_z = 0$ (Fig. S9 [29]). In this case, however, this nesting condition involves the states of $\alpha$-FSs with the superconducting gap maxima [the inset of Fig. 5(b)], which does not favor the field induced SDW order. Instead, the FFLO phase due to the intraband superconducting coupling can be a candidate, dominantly in the $\alpha$-FS, which has the largest superconducting gap and is not involved in the possible SDW ordering at $H_1$. Our calculations taking into account the multiband Pauli paramagnetic effect and the FFLO instability, but not the superconducting gap anisotropy, show that the hidden FFLO phase with a common modulation vector in all bands [20,43] can be stabilized at low temperatures (Fig. S7 [29]), supporting this possibility.

We also note that recent thermal conductivity $\kappa(H)$ study under the in-plane magnetic field reveal a clear kink at high magnetic field below $T^* \sim 2$ K, which is attributed to the FFLO phase transition [19]. The transition field, estimated from $\kappa(H)$ measurements coincides with $H_2$ in our work, confirming the presence of field induced transition below $H_{c2}^\phi$. The $\kappa(H)$ measurements more clearly resolve the transition at $\sim H_2$ than at $\sim H_1$, while our torque $\tau(H)$ and specific heat $C_v(H)$ measurements show stronger anomaly at $H_1$ than at $H_2$. Since the SDW or the FFLO orders may be hosted in different FSs, their visibility to the thermal conductivity can differ from that to other thermodynamic probes, depending on the relative scattering rate of quasiparticles at different FSs. In the current stage, the detailed nature of the field induced phase transitions, including possible coexistence of the SDW and the FFLO orders, remains to be clarified. Nevertheless these observations clearly demonstrate that FeSe offers a unique system, in which field induced phase transitions occur in the superconducting state.

V. CONCLUSION

We reported that FeSe undergoes multiple phase transitions under high in-plane magnetic fields below the upper critical fields. The extremely small Fermi energy, comparable with the energy scales of the superconducting gap and the field induced Zeeman effect, is found to be essential to trigger exotic orders with a large spin imbalance, related with either the spin-density-wave or the FFLO phases. These findings add another intriguing aspect to the unique iron-based superconductor FeSe [16–18,30–32,35,36,38] and also pose a challenge to our understanding on the complex interplay between anisotropic superconducting order, incipient magnetic instabilities, and the multi-band effect in the largely spin-imbalanced superconducting systems.

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