A NUMERICAL STUDY OF LONG-RANGE MAGNETIC IMPACTS DURING CORONAL MASS EJECTIONS

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Received 2015 October 21; accepted 2016 February 10; published 2016 March 10

ABSTRACT

With the global view and high-cadence observations from Solar Dynamics Observatory/Atmospheric Imaging Assembly and Solar TErrestrial Relations Observatory, many spatially separated solar eruptive events appear to be coupled. However, the mechanisms for “sympathetic” events are still largely unknown. In this study, we investigate the impact of an erupting flux rope on surrounding solar structures through large-scale magnetic coupling. We build a realistic environment of the solar corona on 2011 February 15 using a global magnetohydrodynamics model and initiate coronal mass ejections (CMEs) in active region 11158 by inserting Gibson–Low analytical flux ropes. We show that a CME’s impact on the surrounding structures depends not only on the magnetic strength of these structures and their distance to the source region, but also on the interaction between the CME and the large-scale magnetic field. Within the CME expansion domain where the flux rope field directly interacts with the solar structures, expansion-induced reconnection often modifies the overlying field, thereby increasing the decay index. This effect may provide a primary coupling mechanism underlying the sympathetic eruptions. The magnitude of the impact is found to depend on the orientation of the erupting flux rope, with the largest impacts occurring when the flux rope is favorably oriented for reconnecting with the surrounding regions. Outside the CME expansion domain, the influence of the CME is mainly through field line compression or post-eruption relaxation. Based on our numerical experiments, we discuss a way to quantify the eruption impact, which could be useful for forecasting purposes.

Key words: magnetohydrodynamics (MHD) – methods: numerical – Sun: corona – Sun: coronal mass ejections (CMEs)

Supporting material: animations

1. INTRODUCTION

The term “sympathetic solar events” refers to sequences of eruptions from distinct regions on the Sun with apparently causal relations. Sympathetic solar events were reported even before the space age (e.g., Richardson 1951; Becker 1958). However, due to a lack of observational evidence, the coupling mechanism remained speculative. With the launch of Solar TErrestrial Relations Observatory (STEREO; Kaiser 2005) and Solar Dynamics Observatory (SDO; Pesnell et al. 2012), we have, for the first time, a (nearly) complete coverage of the Sun from three different perspectives, which gives us an unprecedented opportunity to investigate sympathetic events on a global scale. A dozen solar sympathetic events have been reported so far in solar cycle 24, which are typically in the form of coupled quiescent filament eruptions (e.g., Schrijver & Title 2011; Yang et al. 2012) or coupled active region (AR)/filament eruptions (e.g., Schrijver et al. 2011, 2013; Shen et al. 2012). Compared with the extensively studied initiation mechanisms for isolated events (see, e.g., Forbes et al. 2006; Kliem et al. 2014, and references therein), the mechanisms by which sympathetic events are coupled remain largely unknown. Few allegedly sympathetic events have been extensively analyzed-modeled, so the physical mechanisms of how perturbations propagate from one region to another and how they interact with the background magnetic field and trigger an eruption remain unknown.

Sympathetic events may also present important implications in understanding the space weather, whose two important elements, non-recurrent geomagnetic storms and solar energetic particles (SEPs), are largely attributable to coronal mass ejections (CMEs, see, e.g., Gosling 1993). When propagating into the solar wind, sympathetic events are prone to CME-CME interaction (e.g., Lugaz et al. 2008, 2012; Liu et al. 2014b). Such interactions may significantly modify the structure of the CME-driven shock wave and the properties of the interplanetary CME (ICME), and therefore affect the potential of space weather effects (e.g., Liu et al. 2012, 2014a; Möstl et al. 2012). Interactions between CMEs from the same AR have often been discussed (e.g., Lugaz et al. 2005b, 2007, 2013; Xiong et al. 2006), but CMEs can be spatially extended and those from distant regions may also interact, adding complexity to solar wind data (e.g., Temmer et al. 2012). It is also possible that sympathetic events may play a role in SEP events observed at widely separate locations (e.g., Richardson et al. 2014; Gómez-Herrero et al. 2015).

Statistical studies suggest that coupling between near-simultaneous events likely exists. By investigating all M5 and above flares observed by SDO using superposed-epoch analysis, Schrijver & Higgins (2015) found increased rate of flaring and filament eruptions within the first 4 hr, even at locations more than 20° away from the primary flare. Fu & Welsch (2015) found an increase in the M- and X-class flaring rates following new AR emergence. A recent study finds that 90% and 79% of X-flares occurred in clusters of 2 or more with the mean separation of ~1 day in solar cycle 22 and 23, respectively (A. M. Title 2015, private communication). These studies support the existence of solar sympathy but do not identify the coupling mechanisms. In this study, we would like...
to establish whether such coupling really exists, and if so, the physical mechanisms responsible.

To uncover the coupling mechanisms in solar sympathetic events, two approaches have typically been used in past studies. One approach involves using a topological analysis of the magnetic field, as applied to coronal field extrapolations that employ photospheric magnetograms as boundary conditions (e.g., PFSS: potential field source surface model). One well-studied example is the series of events occurring on 2010 August 1–2. A sequence of apparently coupled eruptions was observed at widely separated locations that spanned a full hemisphere of the Sun. From a comprehensive analysis of the observational data from SDO and STEREO for the 2010 August 1–2 eruptions, Schrijver & Title (2011) argued that the three ARs involved are connected by topological elements present in the magnetic field (i.e., separatix surfaces, separators, and quasi-separatrix layers). A detailed topological analysis of the source-surface background field by Titov et al. (2012) also strongly supports the idea that these structural features were involved in generating sympathetic eruptions for the 2010 August 1–2 events. The other approach is through numerical modeling. Török et al. (2011) reproduce some important aspects of the global sympathetic event on 2010 August 1 using an idealized arrangement of flux ropes in a zero-β simulation, and found that the presence of a pseudo-streamer is important for producing the “twin-filament” eruptions seen in the observations. Also, Lynch & Edmondson (2013) present a 2.5D magnetohydrodynamics (MHD) simulation of sympathetic magnetic breakout eruptions from a pseudo-streamer source region.

One major difficulty in constructing more realistic three-dimensional (3D) global MHD models of sympathetic events is that additional assumptions are needed to establish how unstable the triggered eruption might be. However, these assumptions are very hard to constrain from the available observations. Therefore, instead of building a single realistic case, we build a realistic background coronal environment for 2011 February 15 and investigate quantitatively how the eruption of flux ropes having various strengths and orientations might impact the magnetic structures in the near and remote neighborhood of the eruption. With this study, we can achieve a better understanding about the role of large-scale magnetic coupling during solar sympathetic events and can thereby explore several candidate mechanisms for solar sympathy.

The paper is organized as follows: in Section 2, we describe the global MHD model Alfvén Wave Solar Model (AWSoM) used to construct the background solar wind and Gibson–Low (GL) flux rope model for the CME initiation. In Section 3, we describe the methods that are used for analyzing the simulation data in this study. The simulation results are shown in Section 4, followed by the discussion and summary in Section 5.

2. MODEL

In this study, we utilize the Space Weather Modeling Framework (SWMF) developed at the University of Michigan, which provides a high-performance computational capability to simulate the space weather environment from the upper solar chromosphere to the Earth’s upper atmosphere and/or the outer heliosphere (Tóth et al. 2005, 2012). The framework contains several components that represent different physical domains of the space environment and each physics domain has several models available. We will mainly focus on the Solar Corona (SC), Inner Heliosphere (IH), and Eruptive Event generator components. For SC/IH, the Block-Adaptive-Tree-Solarwind-Roe-Upwind-Scheme (BATS-R-US) code plays a central role in solving the MHD equations that describe the plasmas in the heliosphere (Powell et al. 1999).

2.1. Alfvén Wave Solar Model

The SC model used in this study is the newly developed AWSoM (van der Holst et al. 2014), which is a data-driven model with a domain extending from the upper chromosphere to the corona and heliosphere. A steady-state solar wind solution is obtained with the local time stepping and second-order shock-capturing scheme (Tóth et al. 2012). In order to construct a realistic coronal environment, the inner boundary condition of the magnetic field is specified by a global magnetic map sampled from an evolving photospheric flux transport model (Schrijver & DeRosa 2003). The inner boundary conditions of electron and proton temperature $T_e$ and $T_i$ and number density $n$ are assumed at $T_e = T_i = 50,000$ K and $n = 2 \times 10^{17}$ m$^{-3}$, respectively. The overestimated density at the inner boundary allows chromospheric evaporation to self-consistently populate the upper chromosphere with an appropriately high density, as found on the Sun. The inner boundary density and temperature do not otherwise have a significant influence on the global solution (Lionello et al. 2009). The initial conditions for the solar wind plasma are specified by the Parker solution (Parker 1958), while the initial magnetic field is based on the PFSS model with the Finite Difference Iterative Potential Solver (Tóth et al. 2011).

Alfvén waves are driven at the inner boundary with the Poynting flux scaling with the surface magnetic field. The solar wind is heated by Alfvén wave dissipation and accelerated by thermal and Alfvén wave pressure. Electron heat conduction (both collisional and collisionless) and radiative cooling are also included in the model. These energy transport terms are important for self-consistently creating the solar transition region. In order to produce physically correct solar wind and CME structures, such as shocks, the electron and proton temperatures are treated separately (Manchester et al. 2012; Jin et al. 2013). Thus, while the electrons and protons are assumed to have the same bulk velocity, heat conduction is applied only to the electrons, owing to their much higher thermal velocity. By using physically consistent treatment of wave reflection, dissipation, and heat partitioning between the electrons and protons, the AWSoM showed the capability to reproduce the solar corona environment with only 3 free parameters that determine Poynting flux ($S_A/B$), wave dissipation length ($L_A\sqrt{B}$), and stochastic heating parameter ($h_S$) (van der Holst et al. 2014).

The SC model uses a 3D spherical grid from $1\, R_s$ to $24\, R_s$. The grid blocks consist of $6 \times 4 \times 4$ mesh cells. The smallest radial cell size is $\sim 10^{-3} R_s$ at the Sun, allowing the steep density and temperature gradients in the upper chromosphere to be resolved. The largest radial cell size at the outer boundary of SC is $\sim 1 R_s$. Below $r = 1.7 R_s$, the angular resolution is $\sim 15^\circ$. Above this radius, the grid coarsens by one level to $\sim 2^\circ$. The IH model uses a Cartesian grid to reach $250\, R_s$ with grid blocks consisting of $4 \times 4 \times 4$ mesh cells. The smallest cell size in IH is $\sim 10^{-1} R_s$ and the largest cell size is $\sim 8 R_s$. For both the SC and IH, adaptive mesh refinement is performed
to resolve the heliospheric current sheet (HCS). The number of total cells is $\sim 3 \times 10^6$ in SC, and $\sim 1 \times 10^6$ in IH. In steady-state, both the SC and IH domains are in heliographic coordinates (rotating at the Carrington rotation rate).

2.2. GL Flux Rope Model

In this study, we initiate CMEs using the analytical GL (Gibson & Low 1998) flux rope model implemented in the Eruptive Event Generator Gibson Low module. This flux rope model has been successfully used in numerous studies modeling CMEs (e.g., Manchester et al. 2004a, 2004b, 2014; Lugaz et al. 2005a, 2005b; Schmidt & Ofman 2010). Analytical profiles of the GL flux rope are obtained by finding a solution to the magnetohydrostatic equation $(\nabla \times \mathbf{B}) \times \mathbf{B} - \nabla p - \rho g = 0$ and the solenoidal condition $\nabla \cdot \mathbf{B} = 0$. This solution is derived by applying a mathematical stretching transformation $r \rightarrow r - a$ to an axisymmetric, spherical ball of twisted magnetic flux $b$ with diameter $r_0$ centered relative to the heliospheric coordinate system at $r = r_1$. The field of $b$ can be expressed by a scalar function $\Lambda$ and a free parameter $a_1$ to determine the magnetic field strength. The full derivation of $b$ can be found in the Appendix of Lites et al. (1995). Following the transformation, the GL flux rope field takes the form:

$$\mathbf{B}_{\text{GL}}(r, \theta, \phi) = \left( \frac{\Lambda}{r} \right)^2 b_r(\Lambda, \theta, \phi) \mathbf{e}_r$$

$$+ \left( \frac{\Lambda}{r} \right) \frac{d}{dr} b_\theta(\Lambda, \theta, \phi) \mathbf{e}_\theta$$

$$+ \left( \frac{\Lambda}{r} \right) \frac{d}{dr} b_\phi(\Lambda, \theta, \phi) \mathbf{e}_\phi$$

(1)

where $\Lambda = r + a$. Equilibrium for the transformed state requires the plasma pressure to be:

$$p_{\text{GL}} = \left( \frac{\Lambda}{r} \right)^2 \left( 1 - \left( \frac{\Lambda}{r} \right)^2 \right) \frac{b_r^2}{2 \mu_0} + \left( \frac{\Lambda}{r} \right)^2 a_1 A$$

(2)

and the density be of the form:

$$\rho_{\text{GL}} = \frac{1}{F(r)} \left[ \left( \frac{\Lambda}{r} \right)^2 \left( 1 - \left( \frac{\Lambda}{r} \right)^2 \right) \frac{d}{d\Lambda} \left( a_1 A + \frac{b_r^2}{2 \mu_0} \right) \right.$$

$$+ 2 a_1 A \frac{d}{dr} b_\theta + \frac{d}{r \mu_0} \left( 1 - 2 \left( \frac{\Lambda}{r} \right)^2 \right) b_\theta^2$$

$$\left. + \left( \frac{\Lambda}{r} \right)^2 \left( \frac{a_r^2}{r^2} + \frac{2 a_2}{r \mu_0} b_\theta^2 + \frac{b_\phi^2}{\mu_0} \right) \right]$$

(3)

where $F(r) = GM/r^2$, $G$ is the gravitational constant and $M$ is the solar mass. The transformed flux rope appears as a teardrop shape of twisted magnetic flux. At the same time, Lorentz forces are introduced, which leads to a density-depleted cavity in the upper portion and a dense core at the lower portion of the flux rope. This flux rope structure helps to reproduce the 3-part density structure of the CME in the observation (Ilgra & Hundhausen 1985). However, the dense core in the GL flux rope is not highly structured as is observed. The GL flux rope and contained plasma are then superposed onto the steady-state solar corona solution: i.e., $\rho = \rho_0 + \rho_{\text{GL}}$, $\mathbf{B} = \mathbf{B}_0 + \mathbf{B}_{\text{GL}}$, $p = p_0 + p_{\text{GL}}$. The combined background-flux rope system is in a state of force imbalance (due to the insufficient background plasma pressure to offset the magnetic pressure of the flux rope), and thus erupts immediately when the numerical model is advanced forward in time. There are several advantages of using this unstable flux rope for this study. First, the eruption does not require time for energy to build up that is computationally expensive. Second, the GL flux rope enables us to estimate the total magnetic energy added to the system, therefore facilitates a parameter study.

The initial out-of-equilibrium flux rope eruption does have some artifacts that should be noted. Due to the force imbalance, the initial acceleration process in the source region may not be captured correctly in the simulation. In this study, we focused on the dynamic evolution of surrounding solar structures rather than the eruption itself. The initial arbitrary acceleration in the source region therefore has limited influence on these structures due to the long distance and the cumulative effect of magnetic reconnect falling between the erupting flux rope and the ambient fields. However, we noticed that the strong acceleration in the beginning may lead to stronger fast-mode waves/shock-waves than those in the realistic events. Therefore, the impact caused by waves (see Section 4.2.2) may be overestimated in this study. To overcome this drawback, a more self-consistent modeling of pre-eruptive configurations is needed (e.g., Titov et al. 2014).

The GL flux rope is mainly controlled by four parameters: the stretching parameter $a$ determines the shape of the flux rope, the distance of torus center from the center of the Sun $r_1$ determines the initial position of the flux rope before it is stretched, the radius of the flux rope torus $r_0$ determines the size of the flux rope, and the flux rope field strength parameter $a_1$ determines the magnetic strength of the flux rope. The location (longitude and latitude) and orientation of the flux rope are also specified in the simulation. For this study, we fix three parameters ($a = 0.3$, $r_0 = 0.3$, $r_1 = 1.4$) and location of the flux rope. We conducted a total of 11 runs with different flux rope $a_1$ and orientations. The GL flux rope parameters used in this study are shown in Section 3.

3. METHOD

3.1. Reconstruction of the Solar Corona

By using the global map, as taken from the time-evolving surface flux transport model of Schrijver & DeRosa (2003) on 2011 February 15 00:04:00 UT, and running AWSoM in local time-stepping mode that allows fast convergence, a steady-state MHD solution of the solar corona at that time can be obtained. For a complete list of model parameters of the AWSoM, refer to Table 1 of van der Holst et al. (2014). Here, we use all parameters except $(S_{\text{H}}/B_{\text{H}})$, which controls the Poynting flux passing through the surface of the Sun. A larger value of this parameter increases the level of coronal heating and therefore opens up more field into the heliosphere, leading to larger coronal holes in the synthesized extreme ultraviolet (EUV) images. We chose $(S_{\text{H}}/B_{\text{H}}) = 1.2 \times 10^6$ W m$^{-2}$ sr$^{-1}$ to get a better match between the synthesized and observed EUV images near the Sun. In Figure 1, the model density, temperature, and the instrumental response functions constructed from the CHIANTI 7.1 atomic database (Dere et al. 1997; Landi et al. 2013) are used to synthesize EUV images, which are then compared with the EUV observations.
from SDO/Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) and STEREO/Extreme UltraViolet Imager (EUVI; Howard et al. 2008). Three EUV spectral bands (AIA 211 Å EUVIA 171 Å and EUVIB 195 Å) are selected that cover the temperature range from 1 MK to 2 MK. It is evident in the figure that emission from all the major ARs and coronal holes is reproduced in the synthesized AIA 211 Å image. However, in the synthesized STA/STB images, several ARs are missing due to the outdated far-side magnetic map (STA was ∼87° ahead of Earth and STB was ∼94° behind Earth at that time). Identical log scales are used for both the observed and synthesized images.

In order to further validate the steady-state background solar wind, we also compare the modeled unsigned openflux with that measured at 1 au by the in situ OMNI database. The unsigned openflux is calculated as \[ F_{\text{1 au}} = 4\pi r^2 |B_z| \], where \[ |B_z| \] is averaged over one Carrington rotation. The unsigned openflux in the database is calculated to be \[ 5.73 \times 10^{22} \text{ Mx} \], while the unsigned openflux in the model is \[ 5.33 \times 10^{22} \text{ Mx} \].

In Figure 2, we compare the initial potential field (blue) with the relaxed, steady-state MHD solution (red) from AWSoM. Carrington coordinates are used for all the 3D simulation data in this study. We select the same foot points for both the potential and MHD field lines in the figure. In the left panel, the closed field near the Sun is shown with the isosurface showing the current density \[ |\mathbf{J}| = 2 \times 10^{-7} \text{ A m}^{-2} \]. In general, the PFSS and MHD solutions are very similar for small loops, but the larger loops in the MHD solution are more radially stretched. This result is consistent with a study by Riley et al. (2006). In the right panel, the helmet streamer belt in the two solutions may be compared. The helmet streamer field lines are selected according to the HCS locations at 2.5 \( R_{\odot} \) for PFSS solution and 3.0 \( R_{\odot} \) for MHD solution. In addition to being stretched to a higher altitude, the MHD helmet streamer belt has also reached higher latitudes at certain places than the corresponding potential field solution.
3.2. Quantifying the Eruption Impact

A GL flux rope located within AR 11158 is inserted into the model. The location is marked as “CME” in Figure 3. The insertion of the flux rope adds a mass of $2.4 \times 10^{16}$ g and a magnetic energy $4.1 \times 10^{32}$ erg to the solar corona, both of which are typical parameters associated with X-class flare/CME systems (e.g., Emslie et al. 2005). The simulation is evolved forward in time for 1 hr after flux rope insertion, during which time CME passes through the model corona. The other ARs and filament channels on disk at the time of the eruption are shown in Figure 3. In the following, we briefly describe these solar structures, quantify the eruption impact, and summarize the simulation runs.

3.2.1. Selection of the Solar Structures

The objective is to investigate the impact of a CME on all the ARs (with or without an AR number), filament channels, and some quiet Sun regions on disk at the time of the liftoff of the CME. In total, there are 8 ARs, 5 filament channels, and 2 quiet Sun regions, all of which are labeled in the left panel of Figure 3. The right panel of Figure 3 shows the H$_{\alpha}$ observation, in which the filament channels are evident. Note that the

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*This calculation is based on the Run 1 flux rope parameters in Table 1.*
filament channels in this simulation do not contain flux ropes. Instead, they are modeled by the MHD solution with near-potential fields. Therefore, the filament channels in this study are essentially referred to diffuse region polarity inversion lines (PILs).

3.2.2. Decay Index

To characterize the impact of the eruption on the various structures, we evaluate the decay index $I_{\text{Decay}}$ before and after the eruption:

$$I_{\text{Decay}} = -\frac{d \log B}{d \log h}$$

(4)

where $B$ is the magnetic field strength and $h$ is the height above the solar surface. The decay index represents how fast the overlying field decays with height, which is a key factor for determining when the instabilities happen. Faster decay corresponds to a lesser confining force, which in turn makes eruptions more likely. The critical decay index $I_{\text{crit}}$ above which the flux rope becomes unstable, depends on the flux rope configuration: 1.0 for a straight line current (van Tend & Kuperus 1978) and 1.5 for a toroidal current (Bateman 1978, p. 270). Several observational studies find that ARs with a larger decay index are more likely to generate CMEs (e.g., Liu 2008).

In a statistical study, Filippov & Zagnetko (2008) find that source regions for erupted filaments have a larger decay index than those for stable filaments. Theoretical and numerical studies suggest that a critical decay index between 1.0 and 2.0 is a good approximation for solar corona conditions under various assumptions (e.g., Kliem & Török 2006; Aulanier et al. 2010; Démoulins & Aulanier 2010). In this study, we extract the magnetic field profile above the PIL of different solar structures. We then calculate the decay index for the selected solar structures between 5 and 100 Mm and track its evolution after the eruption, from which we characterize to what extent the solar structures are affected by the CME.

3.2.3. Impact Factor

Because the plasma parameters (e.g., field, velocity, pressure, density) may undergo dramatic changes during the eruption, the decay index alone may not fully characterize the CME’s impact magnitude on different structures. In order to quantify the impact more comprehensively, we introduce the following two impact factors. The first is the sum of relative perturbations in relevant physical quantities:

$$F_{\text{imp1},i} = \frac{1}{7} \cdot \left( \Delta \rho_i + \Delta B_i + \Delta P_i + \Delta F_{\text{Lorentz},i} + \Delta U_i + \Delta I_{\text{Decay},i} + \Delta I_{\text{Final},i} \right)$$

(5)

where $\rho$, $B$, $P$, $F_{\text{Lorentz}}$, and $U$ represent density, total magnetic field, total pressure, Lorentz force, and total velocity, respectively. $\Delta \rho_i = \frac{1}{\text{max}} \sum_{i=0}^{15} \frac{\Delta \rho_i}{\rho_i}$, $\Delta B_i$, $\Delta P_i$, $\Delta F_{\text{Lorentz},i}$, $\Delta U_i$, and $\Delta I_{\text{Decay},i}$ have similar definitions, while $F_{\text{Lorentz}} = |J \times B|/B^2$. $\Delta I_{\text{Final}} = \frac{I_{\text{Decay}} - I_{\text{Final}}}{I_{\text{Final}}}$, where $I_{\text{Final}}$ refers to the decay index derived from the relaxed steady-state solution calculated from the modified inner boundary map, which is comprised of the global magnetic map plus the contribution of the GL flux rope. This term describes how close the decay index (at $t = 1$ hr) is to the final relaxed MHD solution. The impact factor $F_{\text{imp1}}$ thus takes into account changes in 7 different impact quantities over the course of the first hour of evolution. All the values are averaged between 5 and 100 Mm, and are weighted equally.

The second impact factor has a similar definition but is normalized to the maximum relative impact seen within the 15 selected regions. Also a new quantity (penetration height) is added:

$$F_{\text{imp2},i} = \frac{1}{8} \cdot \left( \frac{\Delta \rho_i}{15 \max_i \Delta \rho_i} + \frac{\Delta B_i}{15 \max_i \Delta B_i} + \frac{\Delta P_i}{15 \max_i \Delta P_i} + \frac{\Delta F_{\text{Lorentz},i}}{15 \max_i \Delta F_{\text{Lorentz},i}} + \frac{\Delta U_i}{15 \max_i \Delta U_i} + \frac{\Delta I_{\text{Decay},i}}{15 \max_i \Delta I_{\text{Decay},i}} + \frac{\Delta I_{\text{Final},i}}{15 \max_i \Delta I_{\text{Final},i}} + \frac{1}{H_i} \left( \frac{1}{15 \max_i 1/H_i} \right) \right)$$

(6)

The penetration height $H_i$ is defined as the lowest altitude where the magnetic field magnitude changes by at least 10% relative to the pre-eruption field. This impact factor can vary from 0 (no impact) to 1 (largest impact among structures). As we can see from the equations, the first impact factor is useful when comparing the impact among the set of simulation runs with different initial flux rope parameters. The second impact factor is useful when comparing the impact of the CME on the various structures in the same simulation run.

3.3. Summary of the Simulation Runs

In Table 1, we summarize the various simulation runs, in which the calculations were initialized with different GL flux rope parameters. The two major parameters that we experimented with are the initial orientation angle and the magnetic

| Run Number | $a_i$ | Orientation |
|------------|------|-------------|
| 1          | 50.0 | 128°        |
| 2          | 50.0 | 216°        |
| 3          | 50.0 | 90°         |
| 4          | 50.0 | 156°        |
| 5          | 50.0 | 246°        |
| 6          | 50.0 | 180°        |
| 7          | 50.0 | 270°        |
| 8          | 25.0 | 128°        |
| 9          | 12.5 | 128°        |
| 10         | 12.5 | 270°        |
| 11         | 5.0  | 128°        |
field strength of the flux rope. As shown in Table 1, for Runs 1–7, the flux rope orientation angle varies between 90° and 270°, allowing the study of the dependence of the impact on orientation. For Runs 1, 8, 9, and 11, only the magnetic field strength of the flux rope is varied, which enables the energy dependence of the impact to be assessed. The convention used here is that the orientation angle of 0° means that the foot points of the flux rope are along the east–west direction with the positive polarity at east, while an orientation angle of 180° has the positive polarity to the west. The orientation angle increases in a clockwise fashion.

4. RESULTS

4.1. Dynamic Evolution after the Eruption

The corona evolves dramatically after the eruption. In Figure 4, we show the plasma-β = 2μ₀ (p_e + p_i)/B² at 2.5 Rₑ at (a)–(c) and radial velocity at 42 Mm (d)–(f) for t = 0, 10, and 60 minutes, respectively. In general, the high plasma-β regions at 2.5 Rₑ approximate the HCS location. From the evolution of the plasma-β, we can see clearly that the eruption changes the large-scale magnetic configuration, and thus the HCS, significantly. After an hour of evolution, the HCS has still not relaxed to the original state at t = 0. The major changes occur around ±50° in longitude around the CME source region (AR 11158). In that region, the HCS locations are pushed to higher latitudes both in the north and south hemispheres.

In Figures 4(d)–(f), we show the radial velocity evolution at 42 Mm, which approximately resembles the height of the Dopplergram observed by spectral lines with log T = 5.5–6.0 (Guo et al. 2009). At t = 10 minutes, we can see clearly the strong upward motion inside the expanding CME “bubble,” in front of which the downward motion is evident with a maximum value of ∼100 km s⁻¹ (Figure 4(e)). The downward motion is caused by the downward push of the CME during its expansion into the corona. This same phenomenon was observed to occur in AR 11158 by Harra et al. (2011) and Veronig et al. (2011) using data from the Hinode/EUV imaging spectrometer (Culhane et al. 2007) during an M1.6 flare/CME event on 2011 February 16. The upward motion is induced by the radial propagation of the CME and is more often observed in the Dopplergrams after CMEs (e.g., Harra et al. 2007; Imada et al. 2007; Jin et al. 2009; Tian et al. 2012). At t = 1 hr, the plasma speed has mostly decreased back to the pre-event magnitude, except for a small area around the CME source region where some upward motion is still evident (∼70 km s⁻¹).

In order to illustrate the global magnetic configuration change during the eruption, we further show in Figure 5 the 3D field configuration at t = 0 (left column) and 15 minutes (right column) from three different points of view (an animation is available online). The lines represent flux rope field lines (red),...
Figure 5. Magnetic field configuration from three different point of views at $t = 0$ (left column) and $t = 15$ minutes (right column). Run 1 data is used. The red, white, and green field lines represent flux rope field lines, large-scale helmet streamers, and field lines from surrounding active regions and open field. The coloring of field lines at $t = 15$ minutes is determined by the initial foot point location of individual field lines.

(An animation of this figure is available.)
large-scale helmet streamers (white), and field lines from surrounding ARs/open field (green). At \( t = 15 \) minutes, the flux rope structure is a mix of three different ensembles (colors) of field lines due to magnetic reconnection. Also, the large-scale helmet streamers around the CME flux rope are significantly disturbed, either by field line compression or reconnection.

### 4.2. Different Types of CME Impact

By analyzing the simulation data using the method described in Section 3, we can identify the factors that determine the CME impact. Ideally, we expect that the CME impact is determined by the distance from the source region as well as by the magnetic field strength of the structures. In Figure 6, we show two scatter plots between the impact factors (defined in Section 3) as a function of the distance (Figure 6(a)) and magnetic field strength (Figure 6(b)) based on the data from Run 1. Larger symbol sizes in the figure reflect stronger magnetic field strengths (Figure 6(a)), whereas in Figure 6(b), larger symbols indicate closer distances to the source region. The magnetic field strength is the average value between 5 Mm and 100 Mm in height. For display purposes, the impact factor \( F_{\text{imp1}} \) is normalized by the largest value. The general trend is that stronger CME impacts occur when the target region has weaker field strength, and especially when the target region is closer to the source region. All regions with impact factor larger than 0.2 are located within 400 Mm from the source region, while these regions can have a broad range of magnetic field strengths. We now discuss additional contributing factors such as magnetic field line connectivity and topology.

The CME impact morphologies can be placed into three categories:

#### 4.2.1. Type I: Direct Connection

This type of impact applies to the solar structures that the flux rope expansion can reach directly. Due to the direct interaction between the flux rope magnetic field and the field of the impacted solar structures, the severity of Type I impacts depends strongly on the initial orientation of the flux rope in the simulation. For the simulated CME erupting from AR 11158 discussed here, we find that regions that experience Type I impacts include QR1, AR2, FC1, FC2, and AR8 (marked with red in Figure 3). In Figure 7, we show as an example the Type I impact for AR2 (an animation is available online), in which we compare the magnetic field configuration as well as the decay index with height for two different flux rope orientations (Run 1 and 2).

At around 15 minutes after the eruption, the CME expansion reaches AR2 and starts to interact with the AR2 magnetic field. Figures 7(a) and (b) show the global magnetic field configuration at \( t = 15 \) minutes with selected field lines to represent flux rope (red), large-scale helmet streamers (white), and field lines from surrounding ARs and open field (green). A zoom-in view of AR2 can be found in Figures 7(c) and (d) with the background showing the normalized Lorentz force and the coloring of the field lines showing the height information. In order to distinguish the field line connectivity, the field lines that reconnect with the erupting flux rope are shown in white color. For Run 1, we can see that the flux rope expansion induces more magnetic reconnections than the expansion in Run 2, as indicated by the larger fraction of field lines connecting AR2 and the CME source region in Run 1. As a consequence, the reconnection in Run 1 removes more overlying field from AR2 and leads to a higher decay index with height (Figures 7(e) and (f)). Note that CME-induced reconnection has been observed and simulated by van Driel-Gesztelyi et al. (2014). In the decay index figure, we also show the PFSS solution as well as MHD final solution (new steady-state after flux rope insertion) for comparison. For AR2, the PFSS and MHD final solutions overlap.

In Figure 8, another example of a Type I impact is shown for filament channels FC1 and FC2, which are located southwest of the CME source region. Due to the weaker magnetic field
Figure 7. Panels (a) and (b) show the global magnetic field configuration of AR2 at $t = 15$ minutes for Runs 1 and 2. The red, white, and green field lines represent flux rope field lines, large-scale helmet streamers, and field lines from surrounding active regions and open field, respectively. Panels (c) and (d) show an enlarged view of AR2 as viewed from the side. The background shows the normalized Lorentz force and the coloring of the field lines shows the height. The white field lines represent the field lines reconnected with the erupting flux rope. Panels (e) and (f) show plots of the magnetic field strength and decay index along the height between 5 and 100 Mm (black solid lines). The PFSS and MHD final solutions are shown with blue and red dashed lines (which overlap in this case), respectively. (An animation of this figure is available.)
Figure 8. The magnetic field configuration and decay index of FC1 and FC2 at $t = 30$ minutes under different flux rope orientations (Run 1 and 2). Panels (a) and (b) show the zoom-in view for FC1 and FC2. The background shows the normalized Lorentz force and the coloring of the field lines shows the height. The white field lines represent the field lines reconnected with the erupting flux rope. Panels (c) through (f) show the magnetic field strength and decay index along the height between 5 and 100 Mm (black solid lines). The PFSS and MHD final solutions are shown with blue and red dashed lines, respectively. (An animation of this figure is available.)

In order to further determine the magnitude of the impact as the flux-rope orientation changes, and to characterize when the impact is largest for different solar structures, we conduct a total of 7 simulation runs (Run 1–7) with different flux rope orientations, while keeping the other flux rope parameters fixed, and calculate the impact factor $F_{imp}$ for the solar structures in each run. Figure 9 shows the orientation dependence of CME impact on two structures with type I impacts (AR2 and AR8), and indicates that the magnitude of impact changes significantly in AR2 and AR8 with different flux rope orientations. For AR2, the difference between the largest and smallest impact factor is $\sim 30\%$, whereas for AR8 the difference is $\sim 40\%$. In the left panel of Figure 9, we mark the largest impact configuration for both AR2 (red) and AR8 (blue). The arrows in AR2 and AR8 show the orientation of the AR (pointing from positive to negative polarity), while the arrows in the CME source region show the orientations of the flux rope with the largest impact. The results shown here suggest that the largest impact occurs when the CME flux rope orientation favors reconnection with the impacted solar structures during the expansion phase.

In the numerical simulations, the interaction between the flux rope and the surrounding magnetic structure is traced through 3D field evolution, however such information cannot be easily obtained from observations. To make the simulation results more readily comparable to observations, we now use the simulation data to synthesize time series of EUV images. These synthesized images clearly reveal EUV waves, namely bright fronts that propagate on a global scale, as seen in EUV images from EIT and AIA. Note that the EUV wave in the 2011 February 15 event was studied by Schrijver et al. (2011), Olmedo et al. (2012), and Nitta et al. (2013b). Although there is some debate about the origin of EUV waves, there seems to be a consensus that a single event could consist of both the “wave” (fast MHD wave) and “non-wave” (CME structure) components (see recent reviews by Chen et al. 2005, Patsourakos & Vourlidas 2012, Liu & Ofman 2014, and Warmuth 2015).
Which part of the front represents which processes remains unclear, however. This is where numerical experiments may help reduce the ambiguities of the observations.

We try different flux rope orientations and evaluate the properties of the ensuing EUV waves. For this purpose, we select two simulation runs with moderate flux rope energy and initial orientation of 128° and 270° (Run 9 and 10). A moderate flux rope energy is chosen to approximately match the intensity enhancement of EUV waves in the observation, and the two orientation angles were chosen to correspond to the maximum and minimum impact factors for AR2 shown in Figure 9. Tri-ratio EUV images were then synthesized by dividing two subsequent simulated images in selected wavelengths at times with an appropriate time interval between them ($t = 6$ minutes/$t = 4$ minutes) for both runs, as shown in the left and middle panels of Figure 10. The images are composites of AIA 211 Å (red), AIA 193 Å (green), and AIA 171 Å (blue). The ratio in each channel is scaled to 1 ± 0.3. Because these three filters have the highest signal-to-noise ratio on AIA, the tri-ratio method serves as a useful tool to investigate EUV waves (e.g., Downs et al. 2012) and eruptions (e.g., Nitta et al. 2013a). Comparing the synthesized images in the two runs indicates that the outer front of the EUV waves (marked by blue arrow) is quite similar for the two orientations, while certain areas of the inner front (marked by red arrow) show a marked difference.

These differences can be interpreted with the assistance of 3D field configuration shown in the right panel of Figure 10.
The outer front has a fast-mode wave nature driven by the eruption, which has been simulated in previous studies (e.g., Wu et al. 2001; Cohen et al. 2009; Downs et al. 2011, 2012). The intensity increase in the EUV bands is caused by adiabatic compression, which can be seen as a density increase region in the 3D configuration image (red surface). The inner front represents the expanding volume of the flux rope, where is the main site for reconnection between the flux rope and the surrounding fields. This wave/non-wave nature of EUV waves has also been found in the previous numerical studies (Cohen et al. 2009; Downs et al. 2012). Behind that front is a low density region (blue surface) with most of the flux rope field lines contained inside. The intensity difference of the inner front near AR2 found in the two runs is due to magnetic reconnection between the flux rope and AR2 field. When the flux rope orientation is more favorable to reconnection with AR2, as in Run9, the intensity increases. This effect may be used to identify the reconnection site in observations, and may also help to constrain the orientation of the expanding flux rope. Our result suggests that these numerical models may help us diagnose the origin of the slow and late EUV fronts that brighten due to magnetic reconnection (Guo et al. 2015).

4.2.2. Type II: Indirect Connection

This type of impact includes solar structures that the flux rope cannot reach directly. In contrast to the type I impact, we find that Type II impacts do not significantly depend as much on the orientation of the flux rope. In this study, the structures with Type II impacts include AR1, AR3, AR4, AR5, FC3, FC4, FC5, and QR2 (marked with green in Figure 3). As an example, we show the orientation dependence of the CME impact on AR1 in Figure 9. In contrast to Type I impacts, the calculated impact factor does not depend on the flux rope orientation, and thus does not involve pronounced magnetic reconnection. Instead, the impact is usually caused by field line compression during the eruption (i.e., fast-mode waves). Because no reconnection is involved, the decay index decreases slightly during the compression process and relaxes back to the pre-event state after the wave passage.

Another mechanism that can cause Type II impacts is through the recovery phase evolution. An example is shown in Figure 11, in which we show the magnetic field evolution of AR5 during the hour after the eruption. We can see that after the main phase of CME impact (t = 8 minutes), the field lines start to relax back to the original state. However, the field of AR5 starts to expand again after t = 26 minutes and keeps changing at t = 60 minutes. This evolution is induced by the large-scale structure changing at higher altitudes during the CME propagation. The field lines above AR5 are stretched during this process, which leads to a larger pressure gradient that causes the lower field to expand again in the recovery phase. Our simulation suggests that although the main phase of CME impact only lasts for several minutes, the post-eruption reconfiguration can last for hours after the eruption. The fact that the expansion in the recovery phase causes an increase in the decay index shows that this post-eruption reconfiguration

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Figure 11. Recovery phase evolution of AR5. The background shows the normalized Lorentz force and the coloring of the field lines shows the height in Mm. The eruption occurs at t = 0.
process could play an important role for some of the solar sympathetic events.

4.2.3. Type III: Hybrid Wave-reconnection Coupling

Type III impacts are hybrids between Type I and Type II. Their evolution does depend on the orientation of the flux rope, but the influence is less pronounced than Type I impacts. For example, the effects on AR6 and AR7 (marked with blue in Figure 3), which are not directly connected to the source region, occur as a result of their proximity to AR2, which we classified earlier as having Type I impact. The interaction between Type III structures and the CME often occur via nearby structures possessing Type I impacts. Because the magnetic configuration can be quite different for Type I impacts under different flux rope orientations, this difference may change the magnetic configuration of regions showing Type III impacts as a result. But due to the indirect nature, the influence of orientation is less evident than for the Type I impacts. In Figure 9, we show the orientation dependence of the CME impact on AR 6 as an example.

4.3. Energy Dependence

Another factor that may influence CME impacts is the energy of the eruption. In order to investigate the energy dependence of the CME impact on different structures, we change \( \alpha_1 \) parameter in Equations (2) and (3) while keeping the other parameters fixed. Run 1, 8, 9, and 11 possess four different energy inputs, covering a range spanning a factor of about \( 40^2 \), \( 1.13 \times 10^{31} \), \( 4.12 \times 10^{31} \), \( 1.23 \times 10^{32} \), and \( 4.06 \times 10^{32} \) erg. For each run, we calculate the CME impact on the selected set of structures, as shown in Figure 12. As expected, the magnitude of impact generally increases for larger energy input. An interesting finding is that for most of the structures with Type II impacts, the magnitude of the impact and energy input have a quasi-linear relationship, while for Type I and III structures, that relationship is nonlinear. According to the characteristics of different impact types mentioned in Section 4.2, it suggests that environments that facilitate magnetic reconnection between two regions cause the impact factor to depend nonlinearly on the energy input. If no reconnection is involved in the process, the impact magnitude increases linearly with the CME energy. We also find that all the remote regions feature the same impact types across all energies in this study.

We also try to relate the CME speeds with the corresponding impacts in the simulations. The resulting CME speed for each energy input is shown in Figure 12 in units of km s\(^{-1}\). The CME speed is defined as the average speed of the outmost density enhancement front between 30 and 60 minutes in the simulation. The CME speeds in our simulations range from 411 to 2607 km s\(^{-1}\). We also found that the square of the CME speed has a linear relationship with the magnetic energy of the GL flux rope.

4.4. Influence of Field Topology

In previous sections, the connectivity between the eruptive flux rope and the various target features is determined by tracing and visualizing field lines associated with the unstable flux rope (e.g., in Figures 5 and 7). However, it is unclear how the boundary of the flux rope expansion is determined. Analyzing the large-scale field topology provides additional insight (e.g., Longcope 2005). In this study, we assume that the PFSS solution could be a good estimation for the large-scale configuration of the corona field, which is presumed to be mostly relaxed and thus close to the potential state. In Figure 13, we show the topological structures calculated from the PFSS model, in order to better understand the magnetic environment into which the CME flux rope propagates. Figure 13(a) shows all null points, spine lines, and separatrix surfaces from the PFSS field, while Figure 13(b) shows only those topological domains that directly connect to the CME source region. The methods used to calculate these topological structures are described by Haynes & Parnell (2007, 2010), after adapting for spherical geometries. The very large yellow semi-transparent surface demarcates the boundary between the open and closed flux in the PFSS model. The separatrix surfaces evident underneath are topological domains associated with null points in the coronal volume. The blue line shows the null line on the source surface, and approximates the location of the base of the HCS. A detailed description of these topological features can be found in Platten et al. (2014).

We find that all the Type I impacts identified in the simulations occur within topological domains that have direct connections with the CME source region. Considering the similarity between the PFSS and MHD field solution in this study (shown in Figure 2), this topology analysis suggests that the erupting flux rope does not easily break out of the domain of self-contained field from which it originates. PFSS models seem useful for identifying the different types of impacts on solar structures caused by an erupting flux rope, however, additional regions need to be analyzed in this way in order to more firmly establish this possibility.

5. SUMMARY AND CONCLUSION

We have constructed a global solar coronal model for 2011 February 15, with the aim of analyzing the effects of a flux rope eruption from AR 11158 on the surrounding features visible on the solar disk. Unstable CMEs having different flux rope parameters (e.g., orientation, strength) were inserted into this model, allowing the dependence of the eruption on these parameters to be investigated. The main conclusions are:
1. The impact of a solar eruption on the surrounding solar structures depends on the distance and the magnetic strength of the impacted structures, as well as on the presence (or absence) of a direct coupling mechanism between the CME flux rope and the surrounding large-scale magnetic field. Within the CME expansion domain where the CME flux rope field directly interacts with the solar structures, expansion induced reconnection effectively weakens the overlying field, leading to an increase of decay index. This mechanism may be responsible for coupled eruptions in certain solar sympathetic events. The magnitude of the impact is found to depend on the orientation of the erupting flux rope, with the largest impact occurring when the CME flux rope is favorably oriented for reconnecting with the surrounding regions. Moreover, the magnitude of the impact appears to increase more weakly than linearly with eruption energy.

2. Outside the CME expansion domain, the influence of the CME is mainly through field compression by fast-mode waves, with a magnitude that is roughly proportional to eruption energy. Because no direct reconnection is involved, the decay index in the low corona always decreases during the wave passage and largely relaxes back to the pre-event state thereafter. Even with the energy input of an X-flare/CME, the waves by themselves have limited impact on a distant AR.

3. For certain structures outside the CME expansion domain, the influence of CME can also occur through the post-eruption reconfiguration of the large-scale field that can persist for hours. During this process, although the major impact of the CME has passed, the magnetic field over the structure continues to evolve, causing the decay index to slowly increase. Therefore, it could be an important factor for certain solar sympathetic events.

Based on the results of this numerical study, we can summarize a list of factors that may determine the CME impact on the different solar structures: the distance from the source region, overlying field of the structure, the relative position of the structure to the source region, the relative orientation of source region and impacted structure, the energy of the eruption, and the topology of the large-scale magnetic field. All of the above-mentioned factors are measurable or can be derived from observations. Therefore, it appears possible to establish an empirical relationship to describe the CME impact in future studies. If such an empirical relationship were found, it could be used to determine regions that will experience the greatest influence even before the actual eruption happens, which is potentially useful for the purpose of space weather forecasting.

We are very grateful to the referee for constructive comments that helped to improve the paper. M.J. is supported by UCAR/NASA LWS Jack Eddy Postdoctoral Fellowship. NVN has been supported by NSF grant AGS-1259549. M.J. is grateful for the hosting of Lockheed Martin Advanced Technology Center. M.J. thanks W. Manchester, B. van der Holst, W. Liu, T. Török, and D. Longcope for invaluable discussions. The simulation results were obtained using the Space Weather Modeling Framework (SWMF), developed at the Center for Space Environment Modeling (CSEM), University of Michigan. We are thankful for the use of the NASA Supercomputer Pleiades at Ames and its helpful staff for making it possible to perform the simulations presented in this paper. We also acknowledge the Texas Advanced Computing Center (TACC) at the University of Texas at Austin for providing HPC resources that have contributed to the research results reported within this paper.

SDO is the first mission to be launched for NASA’s Living With a Star (LWS) Program. STEREO (Solar Terrestrial RElations Observatory) is the third mission in NASA’s Solar Terrestrial Probes program (STP). The STEREO/SECCHI data are produced by a consortium of NRL (U.S.), LMSAL (U.S.), NASA/GSFC (U.S.), RAL (UK), UBHAM (UK), MPS (Germany), CSL (Belgium), IOTA (France), and IAS (France).
