Proposal of an Equal-Stiffness and Equal-Stroke 2D Micro-Positioning Platform Driven by Piezoelectric Actuators

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Abstract: Micro-positioning platform plays an important role in the field of precision positioning such as microelectronics, robotics and biomedicine. This paper proposes an equal-stiffness and equal-stroke 2D micro-positioning platform, which is driven by piezoelectric actuators. The overall structure of the 2D micro-positioning platform adopts a nested structure and the displacement magnification mechanism adopts two hourglass displacement magnification mechanisms. The displacement magnification ratio of the hourglass displacement magnification mechanism was studied, and its structural parameters were optimized. Static stiffness analysis and simulation analysis of the micro-positioning platform were carried out. The simulation stiffness of the micro-positioning platform in the XY direction is 46873 N/m and 46832 N/m respectively. The experimental prototype of the micro-positioning platform was built. Through the measurement experiment with the prototype, the maximum stroke of the micro-positioning platform in the XY direction is 489 µm and 493 µm respectively; the maximum coupling ratio in the XY direction is 2.38% and 2.70% respectively. The research indicates that the micro-positioning platform had the characteristics of small size, equal long stroke, equal stiffness and low coupling ratio in the XY direction.

Keywords: micro-positioning platform; hourglass displacement amplification mechanism; long stroke; piezoelectric actuators; equal stiffness

1. Introduction

In recent years, the micro-positioning technology plays an increasingly important role in microelectronics manufacturing, biomedical engineering, optical, micro-assembly, ultraprecision machining and other fields [1–4]. For example, in the field of biomedicine, the operational precision requirements of processing techniques such as cell separation, dissection, and extraction are constantly improving. Under normal circumstances, it is easy to damage the cells during the clamping contact, and it is difficult to handle micron-level particles. The optical micro-manipulation technology based on the precision positioning platform came into being, and scientists can obtain high-quality images of cells on the microscope stage more quickly [5]. While micro-mechanical execution technology is a key technology to realize micro-positioning. At the same time of high positioning accuracy, the working stroke of the micro-positioning platform must be satisfied. Therefore, the current hot topic is to study micro-positioning platforms with longer stroke, greater scope of application and higher flexibility [6–9].

At present, the long stroke micro-positioning platform is mainly divided into single-stage driving positioning platform and two-stage driving positioning platform [10]. The single-stage drive positioning...
platform refers to the positioning by a single driving method. For example, Mikio Muraoka developed a long-stroke two-dimensional positioning platform based on the principle of triangular amplification and piezoelectric actuators, with the maximum coupling displacement of 0.2 mm [11]. Liu XR et al. proposed a nano two-dimensional positioning platform with a maximum working stroke of 43 µm and a maximum coupling ratio of 11.7% [12]. The single-stage drive positioning platform has advantages of compact structure, but it also has some disadvantages of coupling and short stroke.

The two-stage drive positioning platform realizes large-stroke positioning through the macro drive mechanism and the micro drive device is arranged at the end of the macro drive mechanism to achieve high-precision positioning as an error compensation. For example, Liu DQ et al. developed a micro and macro dual-drive precise positioning platform based on servo motor and piezoelectric ceramic actuator [13] and Zhang LF et al. developed a high-speed positioning platform based on voice coil motor and piezoelectric ceramic [14]. However, the problem with such positioning platforms is that they are too large, which limits their application to some extent. In addition, the nonlinear dynamic characteristics, hysteresis effect and vibration coupling effect of macro and micro positioning platform in the process of macro movement into micro movement also lead to the reduction of positioning accuracy [15,16]. In the micro-positioning platform, stiffness, stroke and mechanical coupling are also important characteristics that determine the performance of the micro-positioning platform [17]. The micro-positioning platform has the equal-stiffness, equal-stroke and lower mechanical coupling in the direction of movement, which is not only beneficial to the manufacture of the micro-positioning platform, but also further improve the accuracy and the application range of the positioning platform [18]. Some commercial micro-positioning platform, such as Thorlabs of the United States, have done very well in the stroke and accuracy of the micro-positioning platform, but have not seen any reports on the micro-positioning platform of equal-stiffness and equal-stroke [19].

Piezoelectric actuators are important parts of micro-positioning platform. As driving elements, they have the characteristics of strong electromechanical coupling, fast response and high accuracy. Piezoelectric actuators can be divided into piezoelectric bending actuators [20] and piezoelectric stack actuators. The piezoelectric bending actuators can produce bending displacement, so they can be used as the driving element of the inertial driving mechanism [21]. Under the condition of achieving more degrees of freedom, the number of driving elements required is reduced. For example, Audelia G. Dharmawan et al. designed a novel legged piezoelectric Miniature Robot, which drives by a single piezoelectric unimorph actuator. By utilizing the difference of bending vibration mode of piezoelectric bending under different driving frequencies and designing the specific position of robot leg to generate similar differential drive mechanism, underdrive motion is realized, and the robot is manipulated to turn left, right and forward [22]. The piezoelectric stack actuators have a single-direction output displacement, which are smaller in size and more rigid than the piezoelectric bending actuators [23]. In this paper, the driving elements of the micro-positioning platform need to have a single-direction input displacement, higher stiffness and smaller size, so we choose the piezoelectric stack actuators.

The amplification principle of the displacement amplification mechanism in the micro-positioning platform mainly includes three kinds of hydraulic amplification, lever amplification and triangular amplification [24–27]. The principle of triangular amplification overcomes the shortcomings of low frequency response of the hydraulic amplification mechanism and the shortcomings of arc-shaped output displacement of the lever amplification mechanism. In order to overcome the shortcomings of short stroke, unequal stiffness and large size of 2D positioning platform, this paper develops an equal-stiffness and equal-stroke 2D micro-positioning platform driven by piezoelectric actuators. This 2D micro-positioning platform combines the advantages of a single-stage driven micro-positioning platform and uses an hourglass displacement amplification mechanism based on the triangle principle. In this paper, we propose an hourglass displacement amplification mechanism based on the principle of triangular amplification, which not only overcomes the shortcomings of the traditional displacement amplification mechanism [28], but also can provide a certain pretension for the piezoelectric actuators and the structure is more compact. For example, Cunman Liang et al. [29] and Mingxiang Ling et al. [30]
designed the diamond displacement amplification mechanism based on the triangle principle, although they have stable amplification performance, the hourglass displacement amplification mechanism has a more compact structure under the same amplification ratio. The displacement amplification ratio and structural parameters of the hourglass displacement amplification mechanism are studied. The static analysis of the 2D micro-positioning platform was carried out and the stiffness of the 2D micro-positioning platform was studied. The magnification of the positioning platform was simulated and compared with the experimental results. The micro-positioning platform experiment system was built to test the maximum output displacement and coupling ratio of the micro-positioning platform. The results show that the equal-stiffness and equal-stroke 2D micro-positioning platform driven by piezoelectric actuators realizes the requirements of low coupling ratio, equal stiffness, small size and long stroke. This 2D micro-positioning platform can be widely used in the field of micro-positioning technology.

2. Design and Analysis of Micro-Positioning Platform

In this paper, an equal-stiffness and equal-stroke 2D micro-positioning platform driven by full-piezoelectric drive is designed by combining the hourglass displacement amplification mechanism and the elastic plate displacement transmission mechanism. Figure 1 is the structure diagram of the micro-positioning platform, which is composed of outer substrate 1, hourglass displacement amplification mechanism 2 in the X direction, hourglass displacement amplification mechanism 3 in the Y direction, inner substrate 4, the elastic plate displacement transmission mechanism 5 in the X direction, the elastic plate displacement transmission mechanism 6 in the Y direction and stage 7. 8 is the structure of the nested part, the hourglass displacement amplification mechanism in the Y direction is nested in the X direction, and the nested part is driven by the hourglass displacement amplification mechanism in the X direction to move in the X direction. 9 is a piezoelectric actuator, which is produced by Harbin Soluble Core Technology Co., Ltd. The piezoelectric actuator model is Rp150/7 × 7/50 and the size is 7 × 7 × 42 mm. The piezoelectric actuator and the Hourglass displacement amplification mechanism are connected by an interference fit and fixed with metal glue. The entire micro-positioning platform adopts 7075 aluminum alloy on the material to have high abrasion resistance, high elongation, high yield strength and sufficient elastic deformation, and the elastic modulus E of 7075 aluminum alloy is 71.5 Gpa. The micro-positioning platform performs overall machining on the wire EDM machine to make the whole structure without mechanical clearance, no idle running and compact structure. The overall size of the micro-positioning platform is 140 mm × 100 mm × 10 mm. The nested structure is used to fix the micro-positioning structure in the Y direction to the inner substrate, so that the motions of the micro-positioning platform in the X and Y directions do not interfere with each other, and the micro-positioning platform uses a symmetrically arranged hourglass displacement amplifying mechanism and displacement transmission mechanism in the XY direction, so that the platform has equal stiffness in the XY direction and improves the range of application of the positioning platform.
2.1. Working Principle of Micro-Positioning Platform

As can be seen from the structure diagram of the micro-positioning platform, the inner layer portion of the micro-positioning platform moves in the Y direction, while the outer layer portion moves in the X direction. The working principle of the two-direction movement of the micro-positioning platform X and Y is the same. Taking the X-direction movement of the micro-positioning platform as an example, the working principle of the micro-positioning platform is introduced, as shown in Figure 2.

![Figure 2](image)

**Figure 2.** The working principle diagram of micro-platform in the X direction.

The piezoelectric actuator is vertically elongated \( \Delta x \), after the voltage is applied, and the two inner bumps of the hourglass displacement amplification mechanism are subjected to the driving force \( F_x \) of the piezoelectric actuator, and the hourglass elastic plate hinge generates a swing angle of \( \Delta \alpha_x \). The elastic plate is elastically deformed, resulting in \( \Delta y_x \) displacement deformation and \( \Delta \theta_x \) angular deformation, effective amplification the piezoelectric actuator output displacement \( \Delta x \), and pulling the inner substrate to realize the X-direction movement in combination with the guiding function of the transfer mechanism of displacement, thereby realizing the movement of the micro-positioning platform in the X direction.

2.2. Design and Optimization of Hourglass Displacement Amplification Mechanism

2.2.1. Hourglass Displacement Amplification Mechanism

Through the design and analysis of the hourglass displacement amplification mechanism to effectively amplify the driving volume of piezoelectric actuators. Figure 3 shows an hourglass displacement amplification mechanism, which is mainly composed of inner bump, connector, piezoelectric actuator and elastic plate hinges. The piezoelectric actuator is connected to the inner bump.

![Figure 3](image)

**Figure 3.** Hourglass displacement amplification mechanism.
2.2.2. Working Principle of Hourglass Displacement Amplification Mechanism

The working principle of the hourglass displacement amplification mechanism is shown in Figure 4a. Figure 4b is an elastic plate hinge motion model of the hourglass displacement magnification mechanism. The hourglass displacement amplification mechanism provides a certain preloading force for the piezoelectric actuator to be clamped horizontally between the two inner bumps of the amplification mechanism. The bump can increase the stiffness of the hourglass displacement amplification mechanism and reduce the displacement loss. When the piezoelectric actuator inputs the driving amount of $\Delta x$ to the amplifying mechanism at point A, the driving volume $\Delta x$ causes the elastic plate hinge to elastically deform and generates $\Delta \alpha$ turning angle at points A and B, thereby causing the amplified displacement $\Delta y$ at point B to be generated.

![Figure 4. The schematic of hourglass amplification mechanism. (a) Working principle diagram of hourglass displacement amplification mechanism; (b) Motion model of quarter hourglass amplification mechanism.](image)

2.2.3. Magnification Ratio of Hourglass Displacement Amplification Mechanism

The elastic plate hinge is the core component of the hourglass amplification mechanism and the elastic deformation of the elastic plate hinge provides displacement deformation and angular deformation to amplification mechanism. The elastic plate hinge structure of the hourglass amplification mechanism is composed of flexible plates with length $l$, width $b$ and thickness $t$.

The force model of the hourglass displacement amplification mechanism is shown in Figure 5. When the piezoelectric actuator is applied with voltage extension, the two inner bumps of the hourglass are subjected to the force $F$ and the elastic plate hinge undergoes a certain elastic deformation, the amplification mechanism produce displacement $\Delta y$ in the Y direction.

![Figure 5. Force model of hourglass displacement amplification mechanism.](image)
$F_A$ and $F_B$ are the horizontal tensile force of the inner bump and the connector acting on the elastic plate hinge, respectively. According to the principle of force balance, $F_A = F_B = F$. As shown in Figure 4b, the elastic plate hinge generates $\Delta \alpha$ turning angle at points A and B during the movement, so that the moment $M_A$ is generated at the hinge A and B. $k_\alpha$ is the rotation stiffness of the elastic plate hinge at points A and B. With the hinge $B$ as the restraining end, the moment of the elastic plate hinge $AB$ is:

$$Fl \sin \alpha = 2M_\alpha = 2k_\alpha \Delta \alpha$$  \hspace{1cm} (1)

where $l$ is the length of the $AB$ elastic plate hinge; $\alpha$ is the angle between the elastic plate hinge and the horizontal X-axis; $\Delta \alpha$ is the rotation angle of the elastic plate hinge; $k_\alpha$ can be expressed as follows:

$$k_\alpha = \frac{Ebt^3}{6l}$$  \hspace{1cm} (2)

where $E$ is the elastic modulus of the material. Decompose the horizontal tensile force $F$ at point $A$ into the force $F_m$ along the direction of the elastic plate hinge:

$$F \cos \alpha = F_m = k_m \Delta l$$  \hspace{1cm} (3)

where $\Delta l$ is the elongation length of the elastic plate hinge, and $k_m$ is the tensile stiffness of the elastic plate hinge. $k_m$ can be expressed as follows:

$$k_m = \frac{Ebt}{l}$$  \hspace{1cm} (4)

The point $A$ of the elastic plate hinge produces a displacement of $\Delta x$ under the action of the horizontal tension force $F$, and the work done by the horizontal tension force $F$ is:

$$F \Delta x = F_m \Delta l + 2M_\alpha \Delta \alpha$$  \hspace{1cm} (5)

After substituting Equations (1) and (2) into Equation (3), horizontal displacement can be derived as:

$$\Delta x = \frac{2k_\alpha \cos^2 \alpha}{k_m l \sin \alpha} \Delta \alpha + l \Delta \alpha \sin \alpha$$  \hspace{1cm} (6)

The displacement of point $B$ in the vertical direction is $\Delta y$, which can be expressed as:

$$\Delta y = \Delta l \cos \alpha$$  \hspace{1cm} (7)
Therefore, the displacement amplification ratio equation of the hourglass displacement amplification mechanism can be derived as:

\[
\frac{\Delta y}{\Delta x} = \frac{3l^2 \sin \alpha \cos \alpha}{l^2 \cos^2 \alpha + 3l^2 \sin^2 \alpha}
\]  

(8)

2.2.4. Optimization of Structural Parameters of Hourglass Displacement Amplification Mechanism

According to Equation (8), the amplification ratio of the hourglass displacement amplification mechanism is mainly affected by the elastic plate hinge length \(l\), the hourglass hinge tilt angle \(\alpha\), and the hinge thickness \(t\). Reasonable optimization of the three structural parameters of the hourglass displacement amplification mechanism can make the hourglass displacement amplification mechanism have better amplification effect.

The relationship between the elastic plate hinge length \(l\) of the hourglass displacement amplification mechanism, the tilt angle \(\alpha\) of the elastic plate hinge and the magnification ratio is shown in Figure 7. As can be seen from the Figure, the displacement magnification ratio of the hourglass displacement amplification mechanism increases as the length of the elastic plate hinge increases. With increasing tilt angle of the elastic plate hinge, the magnification ratio decreased after an initial increase. When the angle of the elastic plate hinge is 1\(^\circ\), the displacement magnification of the hourglass displacement amplification mechanism is the largest. When the tilt angle is too small, the output force of the hourglass displacement amplification mechanism will be reduced, so that the overall working stroke of the platform is reduced and the tilt angle is too small will also reduce the stiffness of the hourglass displacement amplification mechanism, so the tilt angle is taken as \(\alpha = 3.5^\circ\). In theory, the length of the elastic plate hinge is as long as possible, However, considering that the overall size of the platform cannot be too large and the stiffness of the hourglass displacement amplification mechanism must be sufficient, the length of the elastic plate hinge is taken as \(l = 30.5\) mm. The thickness \(t\) of the flexible hinge is generally 1 mm. If the thickness is too thin, the stiffness of the platform will be insufficient, and if it is too thick, the elastic deformation of the hinge will be reduced, so the thickness \(t\) of the elastic plate hinge of the hourglass displacement amplification mechanism is taken as 1 mm. Finally, \(l = 30.5\text{ mm}, \alpha = 3.5^\circ, t = 1\text{ mm}\) and the magnification ratio is 14.9.

![Figure 7. Effects of hinge length and tilt angle on magnification.](image)

2.3. Static Analysis of Micro-Positioning Platform

According to the knowledge of elastic mechanics and related literature [31], the elastic plate hinge of the hourglass displacement amplification mechanism and the elastic plate transfer mechanism of displacement can be simplified as an elastic plate spring. The elastic plate spring can be equivalent to two antisymmetric cantilever beam models, and the half-beam model method is used to derive the stiffness formula \(k_1\) the transfer mechanism of displacement and the stiffness formula \(k_2\) of the
hourglass displacement amplification mechanism. Therefore, the relationship between the piezoelectric actuator output force $F$ and the output displacement of the micro-positioning platform can be derived:

$$F_x \sin \alpha \cos \alpha = (k_{1x} + k_{2x})x$$

(9)

$$F_y \sin \alpha \cos \alpha = (k_{1y} + k_{2y})y$$

(10)

Among them:

$$k_{1x} = \frac{2Eb^3}{l_{x1}^3}$$

(11)

$$k_{2x} = \frac{Eb^3}{l_x^3}$$

(12)

$$k_{1y} = \frac{2Eb^3}{l_{y1}^3}$$

(13)

$$k_{2y} = \frac{Eb^3}{l_y^3}$$

(14)

where $\alpha$ is the angle between elastic plate hinge of hourglass displacement amplification mechanism and horizontal X-axis; $b$ is the width of elastic plate hinge of hourglass displacement amplification mechanism and transfer mechanism of displacement; $t$ is the thickness of elastic plate hinge of hourglass displacement amplification mechanism and transfer mechanism of displacement; $F_x$ and $F_y$ are respectively the vertical output forces of the X and Y direction piezoelectric actuators for the hourglass displacement amplification mechanism; $x$ and $y$ are respectively the displacement of the stage in the X and Y directions; $k_{1x}$ and $k_{1y}$ are the stiffness of transfer mechanism of displacement in the X and Y directions, respectively; $k_{2x}$ and $k_{2y}$ are the stiffness of the hourglass displacement amplification mechanism in the X and Y directions, respectively; $l_{x1}$ and $l_{y1}$ are 1/2 lengths of transfer mechanism of displacement in the X and Y directions, respectively; $l_x$ and $l_y$ are the lengths of the elastic plate hinges of the hourglass displacement amplification mechanism in the X and Y directions, respectively; $E$ is the elastic modulus of the material.

Bringing the platform size parameters into Equations (11)–(14) can obtain the stiffness of the micro-positioning platform hourglass displacement amplification mechanism, the stiffness of the displacement transmission mechanism, and the overall stiffness of the micro-positioning platform in the X and Y directions, as shown in Table 1. Where: $l_{x1} = l_{y1} = 42$ mm, $l_x = l_y = 30.5$ mm, $b = 10$ mm, $t = 1$ mm.

Table 1. Micro-positioning platform theoretical stiffness table.

| Stiffness Analysis                        | Stiffness in X Direction (N/m) | Stiffness in Y Direction (N/m) |
|-------------------------------------------|--------------------------------|--------------------------------|
| Hourglass magnification $k_2$            | 25,376                         | 25,376                         |
| Displacement transmission mechanism $k_1$ | 19,436                         | 19,436                         |
| Micro-positioning platform $k_1 + k_2$   | 44,812                         | 44,812                         |

In ANSYS/Workbench, 100 N, 200 N and 300 N driving forces were respectively applied to the X and Y directions of the micro-positioning platform for simulation analysis. The force acts on the mounting surface of the piezoelectric actuator and the displacement amplification mechanism, and the direction of the force is the same as the extension direction of the piezoelectric actuator. Figure 8 shows the output displacement on the path of the displacement transmission mechanism under the driving force in the X direction, and Figure 9 shows the output displacement on the path of displacement transmission mechanism under the driving force in the Y direction.
Table 3. Comparison of theoretical value and simulation value of micro-positioning platform stiffness.

| Stiffness Analysis | Stiffness in X Direction(N/m) | Stiffness in Y Direction(N/m) |
|--------------------|-------------------------------|-------------------------------|
| Theoretical value  | 44,812                        | 44,812                        |
| Simulation value   | 46,873                        | 46,832                        |

The percentage difference between theory and simulation 4.5% 4.5%

Figure 8. Relationship between force and displacement curve of micro-platform in the X direction.

Figure 9. Relationship between force and displacement curve of micro-platform in the Y direction.

According to Figure 8, Figure 9 and the stiffness calculation formula, the simulation stiffness of the micro-positioning platform in the X and Y directions can be obtained, as shown in Table 2.

Table 2. Micro-positioning platform simulation stiffness table.

| Driving Force (N) | Stiffness in X Direction (N/m) | Stiffness in Y Direction (N/m) |
|-------------------|--------------------------------|--------------------------------|
| 100               | 46,872                         | 46833                          |
| 200               | 46,874                         | 46,831                         |
| 300               | 46,874                         | 46,831                         |

The elastic deformation of the material under different driving forces will slightly change the structure of the platform, resulting in different stiffness under different driving forces. Taking the average of three simulation results, the stiffness of the micro-positioning platform in the X direction is 46,873 N/m and the stiffness in the Y direction is 46,832 N/m. The comparison between the theoretical analysis and the simulation analysis of the stiffness of the micro-positioning platform is shown in Table 3.
It can be seen from the table that the theoretical analysis values of the stiffness in the X and Y directions of the micro-positioning platform are only 41 N/m different from the simulation analysis values, which is about 0.08%, thus verifying that the stiffness in the X and Y directions of the micro-positioning platform is equal. The difference between the theoretical stiffness value and the simulated stiffness value is 4.5%, which further verifies the reliability of the theoretical calculation.

In ANSYS/Workbench, 3D solid elements are used to simulate the displacement of the micro-positioning platform in the X and Y directions. Figure 10 is the boundary conditions of the simulation. Under standard earth gravity, the outer substrate of the micro-positioning platform is fixed and the mounting surface BC, DE of the piezoelectric actuator is subjected to an input displacement of 50 µm. Figure 11 shows the mesh division of the micro-positioning platform. The mesh size is set to 1mm and the mesh type is Hex Dominant. The relevance center of mesh is fine and the smoothing of mesh is high. The results are shown in Figures 12 and 13. When the piezoelectric actuator drive volume is up to 50 µm, the maximum working stroke in the X direction of the micro-positioning platform is 498 µm, the displacement magnification is 9.96; the maximum working stroke in the Y direction is 497 µm, and the displacement magnification is 9.94. Thus, the stroke and magnification ratios of the X and Y directions of the micro-positioning platform are also equal.

**Figure 10.** Boundary conditions for simulation of micro-positioning platform.

**Figure 11.** The mesh of micro-positioning platform.
3. Experimental Analysis

In order to verify the performance of the micro-positioning platform, a micro-positioning platform experimental test system was built, as shown in Figure 14. Figure 15 is a prototype of the micro-positioning platform. The experimental system consists of a micro-positioning platform, Rp150/7 × 7/50 stacked piezoelectric actuator with a maximum driving voltage of 150 V, a displacement of 50 μm at the maximum driving voltage, a drive power, an eddy current sensor, a dSPACE1104 controller and a computer. The controller is dSPACE1104 produced by the dSPACE Ltd. in Paderborn, Germany. The stacked piezoelectric actuator Rp150/7 × 7/50 and the drive power supply RH13 are produced by Harbin Soluble Core Technology Co., Ltd. in Harbin, China. The eddy current sensor is produced by Japan AEC Corp in Kawasaki-City, Kanagawa, Japan, the model is PU-05.

![Figure 12. The displacement simulation of micro-positioning platform in the X direction.](image)

![Figure 13. The displacement simulation of micro-positioning platform in the Y direction.](image)

In order to verify the accuracy of the simulation results, the convergence of the mesh is discussed. Table 4 is the simulation results of the micro-positioning platform in the XY direction under different mesh qualities. It can be seen from Table 4 that the simulation results gradually converge with the improvement of the mesh quality and the number of elements. When the mesh size is 1 mm, the results have converged, so the simulation results are more reliable.

| Number of Nodes | Number of Elements | Mesh Size | Simulation Results in the X Direction | Simulation Results in the Y Direction |
|----------------|--------------------|-----------|--------------------------------------|--------------------------------------|
| 794,198        | 177,222            | 0.8 mm    | 498.53 μm                            | 496.77 μm                            |
| 407,840        | 88,292             | 1 mm      | 498.25 μm                            | 496.6 μm                             |
| 258,154        | 55,044             | 1.2 mm    | 497.28 μm                            | 495.89 μm                            |
| 176,847        | 37,704             | 1.4 mm    | 496.08 μm                            | 495.64 μm                            |

![Table 4. The simulation results of the micro-positioning platform in the XY direction under different mesh qualities.](image)
3.1. Micro Positioning Platform Maximum Output Displacement Test

In the micro-positioning platform experimental test system, the piezoelectric actuator has a maximum output displacement of 50 µm at a driving voltage of 150 V. Taking the step voltage of 15 V and applying 0–150 V voltage to the X and Y directions of the micro-positioning platform, respectively. The voltage-displacement curves in the X and Y directions are as shown in Figure 16.

In the voltage range of 0–150 V, the simulated output displacement of the micro-positioning platform is slightly higher than the experimental output displacement, and the overall trend is consistent. According to the experimental test, the maximum output displacement of the micro-positioning platform in the X direction is 489 µm, and the maximum output displacement in the Y direction is 493 µm.

Table 5 shows the comparison of the maximum output displacement of the micro-positioning platform simulation and experiment. It can be seen from the table that the experimental output displacement is slightly higher than the experimental output displacement, and the overall trend is consistent.
displacement of the micro-positioning platform in the X/Y direction is basically consistent with the simulated output displacement.

Table 5. Platform output displacement comparison table.

| Direction of Movement | Simulation Analysis | Experiment Analysis |
|-----------------------|---------------------|---------------------|
| X direction           | 498 µm              | 489 µm              |
| Y direction           | 497 µm              | 493 µm              |

### 3.2. Micro-Positioning Platform X/Y Direction Coupling Experiment

At present, a major problem in the 2D micro-positioning platform is that the motion interference and coupling are serious in XY directions. Therefore, it is necessary to carry out experimental tests on the coupling displacement of the micro-positioning platform in X and Y directions. A driving voltage of 0–150 V with a step size of 15 V is applied in the X and Y directions, respectively, and the coupling displacement in the Y and X directions is measured.

Figures 17 and 18 are coupling displacement diagrams in Y and X directions. According to Figures 17 and 18, the maximum coupling ratio in the Y direction is 2.38% and the maximum coupling ratio in the X direction is 2.70% when we applied 15 V driving voltage in the X and Y directions, respectively (Coupling ratio in the Y direction = Coupling displacement in the Y direction/Output displacement in the X direction). The coupling is caused because the displacement amplification mechanism and the elastic plate displacement transmission mechanism of the micro-positioning platform generate machining defects and elastic deformation during the machining process. This can result in coupling displacements in undesired directions. In general, the micro-positioning platform has a low coupling ratio in the X and Y directions.

![Figure 17. Y-direction coupling displacement when moving in the X direction of the platform.](image1)

![Figure 18. X-direction coupling displacement when moving in the Y direction of the platform.](image2)
4. Conclusions

The hourglass displacement amplification mechanism proposed in this paper can effectively amplify the micro-displacement of the piezoelectric actuator, which is the key to realize the long stroke of the micro-positioning platform. The nested structure of the micro-positioning platform makes the movements in the X and Y directions do not interfere with each other. The design of the micro-positioning platform with equal stiffness in XY direction improves the positioning accuracy and reduces the coupling displacement of the micro-positioning platform. After experimental test, the maximum output displacement of the micro-positioning platform in the X direction is 489 µm, and the maximum output displacement in the Y direction is 493 µm and the maximum coupling rate is 2.7%. The micro-positioning platform achieves the purpose of equal-stiffness, equal-stroke, small size and low coupling. The above studies still have some shortcomings, such as repeated positioning accuracy and the minimum resolution of the micro positioning platform, which will be reported in subsequent studies.

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