Effect of PYTHIA8 tunes on event shapes and top-quark reconstruction in $e^+e^-$ annihilation at CLIC

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Abstract

This paper describes the effect of PYTHIA8 tunes on event simulation of $e^+e^-$ collisions with center-of-mass (CM) energies of 380 GeV and 3 TeV at the proposed CLIC collider. Event shapes, such as thrust, thrust major, thrust minor, oblateness, as well as particle multiplicities have been analyzed and relative differences with respect to the default PYTHIA8 tune were determined. The effect of tunes on top-mass reconstruction in the resolved and boosted regimes was analyzed. No statistically significant variation for reconstructed top masses using invariant masses of three jets was found for events with a CM energy of 380 GeV. For the fully boosted top reconstruction at a CM energy of 3 TeV, a significant shift in reconstructed top mass of about 700 MeV for the “Montull” tune was observed. This shift correlates with an increase in particle multiplicity compared to all other PYTHIA8 tunes.

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1 Introduction

High-precision measurements at future $e^+e^-$ collisions require a good understanding of hadronisation, which involves non-perturbative QCD physics. Currently, modeling of this stage in particle production can be successfully achieved using Monte Carlo simulations. Such simulations have a number of free parameters that have to be tuned to experimental data using different techniques. This can lead to uncertainties that can affect final measurements when such Monte Carlo simulations are used for unfolding detector effects and various corrections.

The effect of Monte Carlo tunes on hadronic final states in $e^+e^-$ annihilation at the CLIC collider [1] can be studied using the PYTHIA8 Monte Carlo generator [2]. It has seven tunes dealing with hadronization, particle (flavor) composition and time-like showering aspects. The tunes use different sets of the LEP1-LEP2 data. The default setting used by PYTHIA8 is the so-called Monash 2013 [3] tune, which can be applied to both $e^+e^-$ and $pp/p\bar{p}$ data. More information on other PYTHIA8 tunes can be found in Ref.[2].

This paper discusses the PYTHIA8 tunes and their impact on hadronic-final states in $e^+e^-$ annihilation at the centre-of-mass (CM) energies planned for the CLIC collider. In particular, effects on top-mass reconstruction were studied using the resolved and boosted top reconstruction techniques.

2 Simulations

In this study two million events per PYTHIA8 tune were generated and compared against the Monash 2013 tune (default). Events were simulated for two CM energies, 380 GeV and 3 TeV. For the event-shape studies, the generated processes are $e^+e^- \rightarrow Z^*/\gamma \rightarrow q\bar{q}$, where $q$ ($\bar{q}$) are quark (anti-quark), which includes all quark flavors but the top quarks. To study top reconstruction, the events were generated for the process $e^+e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$, where one top quark decays to $Wb$, followed by $W^\pm \rightarrow l^\pm \nu$, while the second $W$ decays to two jets. The initial-state photon radiation was turned off for the event shape studies, but switched on for top reconstruction studies to obtain the most realistic case for top-quark reconstruction. Event shapes and jets were reconstructed from stable particles, which are defined as having a lifetime $\tau$ larger than $3 \times 10^{-10}$ seconds. Neutrinos were excluded from consideration. No kinematic cuts have been applied to stable particles.

In this paper, tunes for different simulations will be indicated as "$T[N]"$, where "$[N]"$ is an integer number corresponding to the PYTHIA8 parameter “Tune:ee” which specifies the implemented tune used to generate events. In the following, the default (“Monash 2013”) tune is indicated with $T0$. Other tunes, with $N$ running from 1 to 6, are described in [2].

All files generated for this study are available from the HepSim public repository [4]. The CLIC detector response was not simulated, thus the effect of the tunes on reconstructed variables gives an upper limit of the possible impact on event shapes and top-mass measurements, without expected smearing due to detector effects and beam backgrounds.

3 Effect from tunes on hadronic final states

3.1 Multiplicity distributions

One simple variable that is potentially sensitive to hadronisation and particle-event composition is particle multiplicity per collision event. The study of the effect of PYTHIA8 tunes on particle multiplicity was done using the $e^+e^- \rightarrow Z^*/\gamma \rightarrow$ hadrons process, excluding top production. Figure 1 shows the neutral- and charged-particle multiplicity distributions for 380 GeV and 3 TeV CM energy, respectively. The result indicates that the tune $T2$, which corresponds to the “Montull” setting, shows the largest increase
in particle multiplicity. A similar observation was made using the multiplicity distribution of charged particles (not shown).

Figure 2 shows the distribution of particle multiplicity for 380 GeV and 3 TeV CM energy for the $e^+e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$ (all decays) process. The conclusion stays the same as in the case of inclusive production, i.e. the effect of tunes can be as large as 100% for the large multiplicity tail, with the largest enhancement coming from the Montull tune.

3.2 Event shapes

Event shape variables are used for studies of global features of particle flows in events. Studies of the energy flows in hadronic final states of $e^+e^- \rightarrow Z^*/\gamma \rightarrow \text{hadrons}$ process have allowed tests of perturbative QCD. Some of the event shape variables have been discussed in the recent review [5]. This study uses several popular variables defined below:

- Thrust of an event is defined as $T = \max_{\vec{n}} \frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|}$, where $|\vec{n}| = 1$. The sum runs over three-momenta of all final state particles (charged and neutral). The thrust axis is defined by the vector $\vec{n}_T$ for which the maximum is obtained.

- Thrust major is defined as $T_M = \max_{\vec{n}_M} \frac{\sum_i |\vec{p}_i \cdot \vec{n}_M|}{\sum_i |\vec{p}_i|}$, assuming the additional condition that $\vec{n}_M$ should lie in the plane perpendicular to $\vec{n}_T$;

- Thrust minor is defined as $T_m = \frac{\sum_i |\vec{p}_i \cdot \vec{n}_m|}{\sum_i |\vec{p}_i|}$, where $\vec{n}_m = \vec{n}_T \times \vec{n}_M$. The thrust minor is perpendicular to both the thrust and the major axis.

- Oblateness, $O_{bl} = T_M - T_m$.

For convenience, we use the $1 - T$ variable, instead of $T$. Such a re-definition leads to a falling distribution, similar to the other three event-shape variables, $T_M$, $T_m$ and $O_{bl}$. In the limit of two narrow back-to-back jets, $1 - T$ is close to 0, while a value of 1/2 corresponds to events with a uniform distribution of momentum flow in all directions.

Figure 3 shows the distribution of the trust values $1 - T$ for two different CM energies of the $e^+e^- \rightarrow Z^*/\gamma \rightarrow \text{hadrons}$ process. It indicates that the $T2$ (“Montull”) setting shows the largest deviation from the central tune in the limit of small values of $1 - T$. This deviation is close to 4 – 5% for the ratio with default tune. Large values of the $1 - T$ distribution suffer from low statistics, therefore, it is difficult to make a conclusive statement on contributions from different tunes.

Figure 4 shows the values of the major thrust for 380 GeV and 3 TeV CM energies. Similarly, Fig. 5 shows the values of the minor thrust. The difference between different tunes was found to be smaller compared to the multiplicity distributions discussed before, with the largest deviation of 10% for the T2 tune.

Figure 6 shows the distribution of the values of oblateness for different CM energies. As in the case of major and minor thrust values, no significant effect from the use of different tunes was found.

Figures 7, 8, 9 and 10 show the event-shape variables for the $e^+e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$ (all decays) process. As expected, these distributions for top production have different shapes compared to the $e^+e^- \rightarrow Z^*/\gamma \rightarrow \text{hadrons}$ process, indicating more uniform distributions of momentum flow in all directions. As before, the effect of different tunes was found to be smaller compared to the multiplicity distributions shown in Fig. 2. The observed variations in the event shape distributions are at the level of 5 – 10% compared to the default tune.
4 Effect on top reconstruction

4.1 Resolved reconstruction

The effect of the PYTHIA8 settings described in the previous section was studied in the context of top reconstruction. Semi-leptonic $t\bar{t}$ decays in $e^+e^-$ annihilation were selected as candidates for three-jet mass reconstruction using events with a lepton from the W decays. The jets were reconstructed using the anti-$k_T$ algorithm [6] as implemented in the FastJet package [7]. The input for the jet reconstruction excludes neutrinos and the lepton from the W decays. This jet algorithm used a distance parameter of $R = 1.0$. Note that the recent CLIC studies [8] of the top reconstruction in $e^+e^-$ at 500 GeV suggest even a larger jet size ($R = 1.3$). For the generator-level studies presented in this paper, we did not find significant improvements in top reconstruction for larger jet sizes.

Hadronic jets were reconstructed in the exclusive mode by requiring exactly four jets in an event. Jets that originate from $b-$quarks were identified by matching jet four-momenta with the momenta of $b-$quarks from the truth-level particle record using a cone algorithm defined in rapidity ($y$) and the azimuthal angle ($\phi$) with a size of 0.3. When reconstructing the top mass for the 380 GeV events, light flavoured jets were merged to build the W-boson mass. The two-jet mass combinations were then constrained to fall within 20 GeV of the nominal W mass value of 80.385 GeV. Such two-jet combinations correspond to W boson candidates. $b$-jets that shared a mother particle with the leptonic W were excluded, and the remaining $b$-jets were combined with the W-boson candidates to calculate the top mass.

Figure 11(a) shows the dijet invariant mass distribution for light-flavour jets. A clear peak at around 80 GeV was observed, which corresponds to the W boson mass. The effect of different tunes is indicated in the ratio plot to the default PYTHIA8 tune.

Figure 11(b) shows the reconstructed mass of three-jet combinations, after combining the W-boson candidates reconstructed from two jets with the third jet identified as the $b-$jet. This figure shows that the effect from different tunes on this distribution is negligible. For a quantitative assessment of the mass shifts, a Breit-Wigner function was used to fit the three-jet mass distribution around the peak position of this distribution. Generally, the fit function does not describe well the asymmetric distribution shown in Figure 11(b). Nevertheless, restricting the fit range to $\pm 4$ GeV around the peak leads to a good value of $\chi^2/\text{ndf} \simeq 1$, and helps a quantitative assessment of shifts in the peak position. It was determined that the shifts in the peak position of the Breit-Wigner distribution with respect to the default PYTHIA8 tune are within 80 MeV for all implemented tunes. At this moment, this value has a non-negligible contribution from statistical uncertainties, therefore, the actual effect can be smaller than this value.

4.2 Boosted reconstruction

The resolved top reconstruction described above has a low reconstruction efficiency for the boosted regime at 3 TeV CM energy. For this large CM energy, the transverse momenta of top quarks are large enough that $b$-jets overlap with light-flavour jets making the differentiation of light-flavour and $b-$jets difficult.

For the boosted-top studies, jets were reconstructed using the anti-$k_T$ algorithm [6] with a distance parameter of $R = 1.2$. The events were forced to have two jets. A larger jet size of $R = 1.2$, compared to $R = 1.0$ for the resolved case, was found to have a better reconstruction efficiency in the boosted regime. This effect is expected since the larger jet size is more appropriate for collecting the decay products of boosted top quarks. Then, the mass of the leading jet was calculated for each PYTHIA8 tune.

Figure 12 shows the mass of the leading jets in the boosted regime. As for the resolved case, the peak position for each PYTHIA8 tune was determined using the fits with the Breit-Wigner distribution. Generally, the Breit-Wigner distribution is too simple for the description of the asymmetric jet-mass distribution. However, it is sufficient for quantitative estimates of the observed shift after restricting the fit range to $\pm 4$ GeV around the peak position of the jet mass distribution. It was found that the largest
shift for jet mass with respect to the PYTHIA8 default is due to the Montull tune. This shift is about 700 MeV. The observed large effect on jet masses is not totally surprising since our previous studies have indicated the significant effect of the Montull tune on particle multiplicities, and jet masses are known to be sensitive to the number of jet constituents.

5 Conclusions

We have performed an analysis of PYTHIA8 tunes for $e^+e^-$ annihilation and their effect on several event shape distributions and on top-mass reconstruction using resolved and boosted techniques. This study was performed for two CM energies, 380 GeV and 3 TeV, anticipated for the CLIC collider.

Most tunes of PYTHIA8 show small effects on hadronic final states of $e^+e^-$. The largest change on the reconstructed variables was found for the Montull tune to the LEP1 particle composition. The effect is significant for multiplicity distributions, where the difference between the Montull and the default (“Monash”) parameter sets can be as large as 100% for events with large multiplicities of final-state particles. The Montull tune is directed towards the flavour composition, and care should be taken considering it for future studies since it is rather outdated [9].

Compared to the multiplicity distributions, the effect of PYTHIA8 tunes is significantly smaller for the event shape variables considered in this paper. A typical effect of about 5% was found for small values of $1 - T$. The Montull tune shows the largest shift (of about 10%) for the minor and major thrust values. However, it is difficult to determine systematic trends for large event-shape values due to limited statistics.

The reconstruction of the top mass from dijets in semi-leptonic top decays using different PYTHIA8 tunes does not indicate significant mass shifts with respect to the default PYTHIA8 settings. The observed mass shifts were found to be less than 80 MeV at the CM energy of 380 GeV.

For the boosted top reconstruction using 3 TeV CM energy, a shift in jet mass from boosted top decays was found to be of the order of 700 MeV. This shift originates from the use of the Montull tune, and it is qualitatively consistent with the observed increase in particle multiplicity for this tune. If the Montull tune is used for future CLIC studies, the observed mass shift can have an impact on various searches and other measurements in the boosted regime.

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Figure 1: The distribution of particle multiplicity (including charged and neutral particles) for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies of $e^+e^-$ annihilation with hadronic decays of $Z^*/\gamma$ (excluding $t\bar{t}$). The bottom plot shows the ratios of different tunes with the default $T0$ (“Monash”) tune.
Figure 2: The distribution of particle multiplicity (charged and neutral) for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+ e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$ (all decays).
Figure 3: The distribution of the thrust values \((1 - T)\) for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in \(e^+e^- \rightarrow Z^* / \gamma \rightarrow \text{hadrons}\) (excluding \(t\bar{t}\)).
Figure 4: The distribution of the major thrust values for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^-\rightarrow Z^*/\gamma \rightarrow \text{hadrons (excluding } t \bar{t}).$
Figure 5: The distribution of the minor thrust values for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^- \rightarrow Z^*/\gamma \rightarrow$ hadrons (excluding $t\bar{t}$).
Figure 6: The distribution of the oblateness for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^-\rightarrow Z^*/\gamma\rightarrow$ hadrons (excluding $t\bar{t}$).
Figure 7: The distribution of the thrust values $(1 - T)$ for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^- \rightarrow Z^* / \gamma \rightarrow t\bar{t}$(all decays).
Figure 8: The distribution of the major thrust values for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^- \rightarrow Z'/\gamma \rightarrow t\bar{t}$ (all decays).
Figure 9: The distribution of the minor thrust values for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$ (all decays).
Figure 10: The distribution of the oblateness for different PYTHIA8 tunes at 380 GeV and 3 TeV CM energies in $e^+e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$ (all decays).
Figure 11: Jet invariant masses for two-jet and three-jet combinations at 380 GeV CM energy for semileptonic top decays in $e^+e^- \rightarrow Z^*/\gamma \rightarrow t\bar{t}$. 
Figure 12: Jet masses for boosted top reconstruction in semi-leptonic top decays at 3 TeV CM energy in $e^+ e^- \rightarrow Z'/\gamma \rightarrow t\bar{t}$, together with the fit to determine the peak positions.