Modeling the Infrared Interstellar Extinction

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Abstract

How dust scatters and absorbs starlight in the interstellar medium (ISM) contains important clues about the size and composition of interstellar dust. While the ultraviolet (UV) and visible interstellar extinction is well studied and can be closely fitted in terms of various dust mixtures (e.g., the silicate-graphite mixture), the infrared (IR) extinction is not well understood, particularly, the mid-IR extinction in the 3–8 \( \mu \)m wavelength range is rather flat (or “gray”) and is inconsistent with the standard Mathis, Rumpl, & Nordsieck (MRN) silicate-graphite dust model. We attempt to reproduce the flat IR extinction by exploring various dust sizes and species, including amorphous silicate, graphite, amorphous carbon and iron. We find that the flat IR extinction is best explained in terms of micrometer-sized amorphous carbon dust which consumes \( \sim 60 \) carbon atoms per million hydrogen atoms (i.e., C/H \( \approx 60 \) ppm). To account for the observed UV/visible and near-IR extinction, the silicate-graphite model requires Si/H \( \approx 34 \) ppm and C/H \( \approx 292 \) ppm. We conclude that the extinction from the UV to the mid-IR could be closely reproduced by a mixture of submicrometer-sized amorphous silicate dust, submicrometer-sized graphitic dust, and micrometer-sized amorphous carbon dust, at the expense of excess C available in the ISM (i.e., this model requires a solid-phase C abundance of C/H \( \approx 352 \) ppm, considerably exceeding what could be available in the ISM).

Keywords: Infrared, Extinction, Dust, Model

1. Introduction

The interstellar extinction is one of the primary sources of information about the interstellar dust size and composition. The interstellar extinction varies from one sightline to another in the ultraviolet (UV) and optical
wavelength range. This variation in the Milky Way galaxy can be described by a single parameter, i.e., $R_V$ (Cardelli et al. 1989; hereafter CCM). The average extinction law for the Galactic diffuse interstellar medium (ISM) corresponds to $R_V \approx 3.1$. Based on the interstellar extinction curve observed for the diffuse ISM $R_V \approx 3.1$, Mathis et al. (1977) constructed a simple interstellar dust model to fit the interstellar extinction observed over the wavelength range of $0.11 \mu m < \lambda < 1 \mu m$. This classic model — known as the “MRN” model — consists of silicate and graphite grains and takes a simple power-law size distribution $dn/da \propto a^{-\alpha}$ with $\alpha \approx 3.5$ for the size range of $50 \AA < a < 0.25 \mu m$, where $a$ is the radius of the dust which is assumed to be spherical. This model was further developed by Draine & Lee (1984) who extensively discussed the optical properties of “astronomi-

\footnote{1}R_V \equiv A_V/E(B-V)$ is the total-to-selective extinction ratio, where $E(B-V) \equiv A_B - A_V$ is the reddening which is the difference between the extinction in the blue band ($A_B$) and the extinction in the visual band ($A_V$).

\footnote{2}Hoyle & Wickramasinghe (1962) first proposed that graphite grains of sizes a few times $0.01 \mu m$ could condense in the atmospheres of cool N-type carbon stars, and these grains would subsequently be driven out of the stellar atmospheres and injected into the interstellar space by the stellar radiation pressure. Similarly, Kamijo (1963) suggested that nanometer-sized SiO$_2$ grains could condense in the atmospheres of cool M-type stars. Gilman (1969) argued that grains around oxygen-rich cool giants could mainly be silicates such as Al$_2$SiO$_5$ and Mg$_2$SiO$_4$. Silicates were first detected in emission in M stars (Woolf & Ney 1969, Knacke et al. 1969). After blown out of the stellar atmospheres and injected into the interstellar space, silicates could become an interstellar dust component. Hoyle & Wickramasinghe (1969) first modeled the interstellar extinction in terms of a mixture of silicate grains of radii $\sim 0.07 \mu m$ and graphite grains of radii $\sim 0.065 \mu m$. Wickramasinghe & Nandy (1970) found that a mixture of silicate, graphite, and iron grains achieved a rough fair fit to the interstellar extinction curve at $\lambda^{-1} < 8 \mu m^{-1}$.

\footnote{3}To be precise, the MRN model actually derived a wider size range of $50 \AA < a < 1 \mu m$ for the graphite component and a narrower size range of $0.025 \mu m < a < 0.25 \mu m$ for the silicate component (and for other components such as SiC, iron and magnetite), with $\alpha \approx 3.3$–3.6. In the literature, the MRN model is customarily taken to be a mixture of silicate and graphite with $\alpha = 3.5$ and $50 \AA < a < 0.25 \mu m$. This is probably because (1) in their Figure 4 the demonstrated model fit to the observed UV/visible extinction was provided by the olivine-graphite mixture with $\alpha = 3.5$ and $50 \AA < a < 0.25 \mu m$ for both dust components; and (2) Draine & Lee (1984) also derived $\alpha = 3.5$ and $50 \AA < a < 0.25 \mu m$ for both dust components using improved optical constants for these two substances. The sudden cutoff at $a_{\text{min}} = 50 \AA$ and $a_{\text{max}} = 0.25 \mu m$ is not physical. Kim et al. (1994) and WD01 adopted a more smooth size distribution function which extends smoothly to $a > 1 \mu m$. But the dust with $a > 1 \mu m$ takes only a negligible fraction of the total dust mass.
cal” silicate and graphite materials. Subsequent developments were made by Draine and his coworkers (Weingartner & Draine 2001 [hereafter WD01], Li & Draine 2001) who extended the silicate-graphite grain model to explicitly include polycyclic aromatic hydrocarbon (PAH) molecules to explain the so-called “unidentified infrared emission” (UIE) bands at 3.3, 6.2, 7.7, 8.6, and 11.3 µm (see Léger & Puget 1984, Allamandola et al. 1985).

With the wealth of available data from space-borne telescopes (e.g., Infrared Space Observatory [ISO] and Spitzer Space Telescope) and ground-based surveys (e.g., Two Micron All Sky Survey [2MASS]) in the near- and mid-infrared, in recent years we have seen an increase in interest in the infrared (IR) extinction. Understanding the effects of dust extinction in the IR wavelengths is important to properly interpret these observations. While the UV/optical extinction has been extensively observed for a wide variety of environments and modeled in terms of various dust models, our understanding of the near- and mid-IR extinction is still somewhat poor and controversial, despite that in this spectral domain many advances have been made in the past few years (see §1 of Wang et al. 2013).

As shown in Figure 1, WD01 silicate-graphite grain model predicts a power-law of $A_\lambda \propto \lambda^{-1.74}$ for the IR extinction at $1 \mu m < \lambda < 7 \mu m$, while the MRN model predicts a steeper power-law of $A_\lambda \propto \lambda^{-2.02}$. The model IR extinction curves reach their minimum at $\sim 7 \mu m$ where the extinction power-law intersects the blue-wing of the 9.7 µm silicate absorption band.

Rieke & Lebofsky (1985) measured the IR extinction from 1 µm to 13 µm for the lines of sight toward o Sco, a normal A5II star behind the edge of the ρ Oph cloud obscured by $A_V \approx 2.92$ mag$^5$ and toward a number of stars in the galactic center (GC). Rieke & Lebofsky (1985) derived a power-law of $A_\lambda \propto \lambda^{-1.62}$ for $1 \mu m < \lambda < 7 \mu m$ for o Sco and the GC sources. Draine (1989) compiled the IR extinction observed for a range of galactic regions including diffuse clouds, molecular clouds, and HII regions. He derived a power-law of $A_\lambda \propto \lambda^{-1.75}$ for $1 \mu m < \lambda < 7 \mu m$. More recently, Bertoldi et al. (1999) and Rosenthal et al. (2000) also derived a power-law extinction of $A_\lambda \propto \lambda^{-1.7}$ for $1 \mu m < \lambda < 7 \mu m$.

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$^4$At $\lambda > 7 \mu m$, the extinction increases because of the 9.7 µm silicate Si–O stretching absorption band.

$^5$The extinction toward o Sco at $\lambda > 0.55 \mu m$ can be well described by the $R_V = 3.1$ extinction law. At $\lambda < 0.55 \mu m$, the observed colors of o Sco are much bluer than expected from those of a normal A5II star obscured by $A_V = 2.92$ mag with the $R_V = 3.1$ extinction law, leading to the assignment of $R_V \approx 4.0$ (see Rieke & Lebofsky 1985).
Figure 1: Comparison of the IR extinction observed for various interstellar regions with that predicted from the MRN (red dot-dashed line) and WD01 (black solid line) silicate-graphite models for the diffuse ISM of which the UV/optical extinction is characterized by $R_V \approx 3.1$. The little bump at 6.2 $\mu$m arises from the C–C stretching absorption band of PAHs (see Li & Draine 2001).

$$A_\lambda \propto \lambda^{-1.7}$$ for $2 \mu$m $< \lambda < 7 \mu$m for the Orion molecular cloud (OMC).\footnote{The OMC extinction also displays an absorption band at 3.05 $\mu$m attributed to water ice.}

However, numerous recent observations suggest the mid-IR extinction at $3 \mu$m $< \lambda < 8 \mu$m to be almost "universally" flat or "gray" for both diffuse and dense environments (see §1.4 of Wang et al. 2013 for a summary), much flatter than that predicted from the MRN or WD01 silicate-graphite model for $R_V = 3.1$ (see Figure 1).

Lutz et al. (1996) derived the extinction toward the GC star Sgr A* between 2.5 $\mu$m and 9 $\mu$m from the H recombination lines. They found that the GC extinction shows a flattening of $A_\lambda$ in the wavelength region of $3 \mu$m $< \lambda < 9 \mu$m, clearly lacking the pronounced dip at $\sim 7 \mu$m predicted from the $R_V = 3.1$ silicate-graphite model (see Figure 1). This was later confirmed by
Lutz (1999), Nishiyama et al. (2009), and Fritz et al. (2011).

Indebetouw et al. (2005) used the photometric data from the 2MASS survey and the Spitzer/GLIMPSE Legacy program to determine the IR extinction. From the color excesses of background stars, they derived the $\sim 1.25 – 8 \mu m$ extinction laws for two very different lines of sight in the Galactic plane: the $l = 42^o$ sightline toward a relatively quiescent region, and the $l = 284^o$ sightline which crosses the Carina Arm and contains RCW 49, a massive star-forming region. The extinction laws derived for these two distinct Galactic plane fields are remarkably similar: both show a flattening across the 3–8 $\mu m$ wavelength range, consistent with that derived by Lutz et al. (1996) for the GC.

Jiang et al. (2006) derived the extinction at 7 and 15 $\mu m$ for more than 120 sightlines in the inner Galactic plane based on the ISOGAL survey data and the near-IR data from DENIS and 2MASS, using RGB tip stars or early AGB stars (which have only moderate mass loss) as the extinction tracers. They found the extinction well exceeding that predicted from the MRN or WD01 $R_V = 3.1$ model.

Flaherty et al. (2007) obtained the mid-IR extinction laws in the Spitzer/IRAC bands for five nearby star-forming regions. The derived extinction laws at $\sim 4 – 8 \mu m$ are flat, even flatter than that of Indebetouw et al. (2005).

Gao et al. (2009) used the 2MASS and Spitzer/GLIMPSE data to derive the extinction in the four IRAC bands for 131 GLIMPSE fields along the Galactic plane within $|l| \leq 65^o$. Using red giants and red clump giants as tracers, they also found the mean extinction in the IRAC bands to be flat.

Wang et al. (2013) determined the mid-IR extinction in the four Spitzer/IRAC bands of five individual regions in Coalsack, a nearby starless dark cloud, spanning a wide variety of interstellar environments from diffuse and translucent to dense clouds. They found that all regions exhibit a flat mid-IR extinction.

All these observations appear to suggest an "universally" flat extinction law in the mid-IR, with little dependence on environments.\footnote{We should note that an “universally” flat mid-IR extinction law does not necessarily mean an identical mid-IR extinction law for all regions, instead, it merely means a flattening trend of $A_\lambda$ with $\lambda$ in the mid-IR. Chapman et al. (2009), McClure (2009), and Cambrésy et al. (2011) found that the shape of the mid-IR extinction law appears to vary with the total dust extinction. But also see Román-Zúñiga et al. (2007) and Ascenso et al. (2013) who found no evidence for the dependence of the mid-IR extinction law on the environment.} While rapid
progress has been made in observationally determining the mid-IR extinction and numerous IR extinction curves have been accumulated both for the Milky Way and for the Magellanic Clouds (e.g., see Gao et al. 2013a), theoretical understanding of the nature and origin of the flat mid-IR extinction lags well behind the observations. We plan to model the interstellar extinction from the far-UV to the far-IR for a wide range of interstellar environments. In this work we present our first attempts to understand the nature of the flat mid-IR extinction. In §2 we summarize the current status in interpreting the flat mid-IR extinction. §3 describes our model. §4 presents the results and discussions.

Figure 2: Comparison of the IR extinction observed for various interstellar regions with that predicted from the WD01 model for $R_V = 5.5$ (black solid line) and the iron needle model (red dot-dashed line) of Dwek (2004) which is a combination of the $R_V = 3.1$ silicate-graphite model of Zubko et al. (2004; green dashed line) and iron needles (blue dashed line).

total dust extinction.
2. Modeling the Mid-IR Extinction: Where Do We Stand?

To the best of our knowledge, only WD01 and Dwek (2004) have closely reproduced the flat mid-IR extinction. Using a mixture of amorphous silicate dust and carbonaceous dust, WD01 fitted the UV/optical and near-IR extinction curves of different values of $R_V$ in the wavelength range of $0.125 \mu m < \lambda < 2.86 \mu m$. Draine (2003) extended the WD01 model of $R_V = 5.5$ into the IR up to $\lambda < 30 \mu m$. It is amazing that the WD01 $R_V = 5.5$ model closely reproduces the flat mid-IR extinction observed toward the GC (Lutz et al. 1996; also see Figure 2). The success of the WD01 $R_V = 5.5$ model and the failure of the WD01 $R_V = 3.1$ model in fitting the flat mid-IR extinction suggest that the flat mid-IR extinction implies a population of large dust, although the exact size and quantity of this dust population are not known.

Generally speaking, denser regions tend to have flatter extinction curves in the UV and higher values $R_V$: increased $R_V$ is attributed to tilt in size distribution to decrease numbers of small grains, and increase of numbers of large grains due to grain growth primarily through coagulation (Draine 2011).

However, the flat mid-IR extinction is not only seen in dense regions. As discussed in §1, the flat mid-IR extinction has been seen in various interstellar environments, including diffuse clouds (e.g., the low-density lines of sight in the Galactic midplane [see Zasowski et al. 2009], and the diffuse and translucent regions of the Coalsack nebula [see Wang et al. 2013]). The $R_V = 5.5$ size distribution is more appropriate for dense regions.

Dwek (2004) hypothesized that metallic needles may play an important role in accounting for the flat mid-IR extinction. As shown in Figure 2, Draine (2004) argued that, combined with the silicate-graphite mixture for the $R_V = 3.1$ model (Zubko et al. 2004), metallic needles with a typical length ($l$) over radius ($a$) ratio of $l/a \approx 600$ and a needle-to-H mass ratio of $\sim 5 \times 10^{-6}$ could explain the flat mid-IR extinction derived by Lutz (1999).

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8The carbonaceous grain population was assumed to extend from grains with graphitic properties at radii $a > 0.01 \mu m$, down to particles with PAH-like properties at very small sizes (see Li & Draine 2001).

9The idea of metallic needles was originally brought up by Hoyle et al. (1968) and Wickramasinghe et al. (1975) to explain the 2.7 K cosmic microwave background (CMB). They argued that the 2.7 K CMB might have arisen from the radiation of “Population III” objects thermalized by long slender conducting cosmic whiskers or “cosmic needles”.
for the GC. However, it is not clear if metallic needles are indeed present in
the ISM (see Li 2003). It would be interesting to study their generation and
evolution in the ISM and their optical properties.

Gao et al. (2013b) have also attempted to fit the \( \sim 1–19 \mu m \) IR extinction
curve toward the GC derived by Fritz et al. (2011). Their best-fit model for
the GC IR extinction constrains the visual extinction to be \( A_V \sim 38–42 \) mag.
But their model could not simultaneously reproduce both the relatively steep
\( \sim 1–3 \mu m \) near-IR extinction and the flat \( \sim 3–8 \mu m \) mid-IR extinction. They
suggested that the extinction toward the GC could be due to a combination of
dust in different environments: dust in diffuse regions (characterized by small
\( R_V \) and steep near-IR extinction), and dust in dense regions (characterized
by large \( R_V \) and flat UV extinction).

3. Our Model

We aim at simultaneously reproducing the observed UV/optical and near-
and mid-IR extinction. Following MRN and WD01, we assume a mixture of
amorphous silicate dust and graphite dust. The optical constants of amor-
phous silicate dust and graphitic dust are taken from Draine & Lee (1984).
Since the flat mid-IR extinction is seen both in diffuse clouds and in dense
clouds, we consider the UV/optical and near-IR extinction curves of different
\( R_V \) values: \( R_V = 3.1, 4.0, \) and 5.5.

We adopt an exponentially-cutoff power-law size distribution for both
dust components: \( \frac{dn}{da} \propto a^{-\alpha} \exp \left( -\frac{a}{a_c} \right) \) for \( a_{\min} < a < a_{\max} \), where \( a \)
the spherical radius of the dust (we assume the dust to be spherical), \( \alpha \) is the
power exponent, and \( a_c \) is the cutoff size. Following MRN, the lower cutoff
of the dust size is initially taken to be \( a_{\min} = 50 \) Å. But for the \( R_V = 4.0, 5.5 \)
curves, we find that \( a_{\min} = 25 \) Å is more favorable. The upper cutoff is set
at \( a_{\max} = 2.5 \mu m \).

We have five parameters: \( \alpha_S \) and \( a_{c,S} \) for the silicate component, \( \alpha_C \) and
\( a_{c,C} \) for the carbonaceous component (i.e., graphite), and \( f_{C2S} \), the mass
ratio of graphite to silicate dust. The ratio of the total model extinction at
wavelength \( \lambda \) to the column density of H nuclei is calculated from

\[
\frac{A_\lambda}{N_H} = 1.086 N_S' \times C_{\text{ext}}(\lambda),
\]

\[
C_{\text{ext}}(\lambda) = \int_{a_{\min}}^{a_{\max}} C_{\text{ext},S}(a, \lambda) a^{-\alpha_S} \exp \left(-\frac{a}{a_{c,S}} \right) da
\]
\[ (N'_C/N'_S) \int_{a_{\text{min}}}^{a_{\text{max}}} \frac{C_{\text{ext},C}(a, \lambda)}{a} a^{-\alpha_C} \exp \left(-\frac{a}{a_{c,C}}\right) \, da , \quad (2) \]

\[ N'_S = \sum_{j=1}^{N_{\text{obs}}} \left\{ (A_\lambda/N_H)_{\text{obs},j} \times \frac{C_{\text{ext}}(\lambda_j)}{\sigma_{\text{obs},j}^2} \right\} \]

\[ / \left[ 1.086 \sum_{j=1}^{N_{\text{obs}}} \{ C_{\text{ext}}(\lambda_j)/\sigma_{\text{obs},j} \}^2 \right] , \quad (3) \]

\[ N'_C/N'_S = f_{\text{C2S}} \times \left( \frac{\rho_S}{\rho_C} \right) \times \int_{a_{\text{min}}}^{a_{\text{max}}} a^{3-\alpha_S} \exp \left(-\frac{a}{a_{c,S}}\right) \, da / \int_{a_{\text{min}}}^{a_{\text{max}}} a^{3-\alpha_C} \exp \left(-\frac{a}{a_{c,C}}\right) \, da , \quad (4) \]

where \( N'_S \) and \( N'_C \) are respectively proportional to the column densities of the silicate and graphite dust, \( \rho_S = 3.5 \, \text{g cm}^{-3} \) and \( \rho_C = 2.24 \, \text{g cm}^{-3} \) are respectively the mass densities of the silicate and graphite dust, \( C_{\text{ext},S}(a, \lambda) \) and \( C_{\text{ext},C}(a, \lambda) \) are respectively the extinction cross sections of the silicate and graphite dust of size \( a \) at wavelength \( \lambda \), \( C_{\text{ext}}(\lambda) \) is the extinction at wavelength \( \lambda \) of the silicate-graphite mixture per silicate dust column, and \( (A_\lambda/N_H)_{\text{obs},j} \) and \( \sigma_{\text{obs},j} \) are respectively the “observed” extinction and uncertainty at wavelength \( \lambda_j \). For the UV/optical and near-IR extinction, we follow WD01 to fit the CCM extinction characterized by \( R_V \) between 0.35 and 8 \( \mu \text{m}^{-1} \) and evaluate the extinction at \( N_{\text{obs}} = 100 \) wavelengths \( \lambda_j \), equally spaced in \( \ln \lambda \).

As will be shown later in §4, although this simple grain model could closely reproduce the observed UV/optical and near-IR extinction, it could not fit the flat mid-IR extinction. Guided by the fact that dust scatters starlight most effectively at wavelengths comparable to its size (i.e., \( 2\pi a/\lambda \sim 1 \); see Wang et al. 2014), we will add an extra population of large, micrometer-sized dust to account for the flat mid-IR extinction. For this large, \( \mu \text{m} \)-sized dust population, we will consider amorphous silicate, graphite, amorphous carbon, and metallic iron. We adopt the optical constants of the “ACAR”-type amorphous carbon of Rouleau & Martin (1991). The optical constants of iron are taken from Li (2003).

For the mid-IR extinction, we compare the model results with the observational data for the following regions as a whole: the Galactic center...
(Lutz 1999, Nishiyama et al. 2009), the Galactic plane (Indebetouw et al. 2005, Jiang et al. 2006, Gao et al. 2009), nearby star-forming regions (Flaherty et al. 2007), and the Coalsack nebula (Wang et al. 2013). Ideally, the CCM UV/optical extinction should be combined only with the IR extinction for the regions characterized by the same $R_V$. However, the regions for which the mid-IR extinction has been measured are not well characterized and their $R_V$ values are not well determined.

Nonetheless, as illustrated in Figure 1, the mid-IR extinction for different regions does not appear to differ substantially from each other and on average, a flat mid-IR extinction is well established. It is interesting to note that, as shown in Wang et al. (2013) for the Coalsack nebula, the mid-IR extinction of diffuse regions seems to be even somewhat flatter than that of dense regions. Therefore, we intend to compare our model results with the mid-IR observations as a whole, instead of an individual region.

In modeling the UV/optical extinction, we perform a grid-search by minimizing $\chi^2$ (see eq. 8 of WD01) with the weights given by WD01. We fit the mid-IR extinction by eye as we do not know how the mid-IR extinction data points should be weighted compared to the UV/optical extinction. We fit the UV/optical segment and the mid-IR segment separately but requiring that the addition of the mid-IR model extinction to the total extinction does not distort the fit to the UV/optical part.

4. Results and Discussion

To testify our model, we first fit the UV/optical and near-IR extinction curve of $R_V = 3.1$. We assume that silicate and graphite have the same size distribution (i.e., $\alpha_S = \alpha_C$, $a_{c,S} = a_{c,C}$). Figure 3 shows the best-fit results. The best-fit model parameters are listed in Table I. The abundances of the dust-forming heavy elements locked up in the dust can be derived from the following equation:

$$[X/H] = \frac{4\pi}{3} \times \rho_X/m_H \times N_X/\mu_X$$

For example, the line of sight toward the Galactic center is often considered as a sightline of diffuse clouds as revealed by the presence of the 3.4 $\mu$m C–H aliphatic hydrocarbon stretching absorption feature which is not seen in molecular clouds (Pendleton & Allamandola 2002, Mennella et al. 2002). However, the Galactic center sightline must also contain molecular cloud materials as revealed by the presence of the 3.1 $\mu$m and 6.0 $\mu$m H$_2$O ice absorption features (e.g., see McFadzean et al. 1989).
Figure 3: Fitting the $R_V = 3.1$ UV/optical and near-IR extinction with a simple mixture (black solid line) of amorphous silicate (green dashed line) and graphite dust (blue dashed line). The black solid line plots the model fit, while the red solid line plots the $R_V = 3.1$ extinction curve observed for diffuse regions. See §3 for details.

\[ \times \int_{a_{\text{min}}}^{a_{\text{max}}} N'_X a^{3-\alpha_X} \exp \left( -a/a_{c,X} \right) da , \]  

where $m_H = 1.66 \times 10^{-24}$ g is the mass of a hydrogen atom, $\rho_X$ and $N'_X$ are respectively the mass density and column density of the dust species containing element X, and $N_X$ and $\mu_X$ are respectively the number of X atoms in and molecular weight of a molecule of the dust species containing element X. We consider elements Si and C and dust species amorphous silicate and graphite: $\mu_C \approx 12$, $N_C = 1$, $\mu_S \approx 172$, and $N_{Si} = 1.111$. We derive the C and Si abundances required to be locked up in dust to be $[C/H]_{\text{dust}} \approx 292$ ppm and $[Si/H]_{\text{dust}} \approx [Mg/H]_{\text{dust}} \approx [Fe/H]_{\text{dust}} \approx 34$ ppm (ppm refers to “parts per million”).

For the dust-forming element X, let $[X/H]_{\text{ISM}}$ be the “interstellar abun-
Figure 4: Fitting the $R_V = 3.1$ UV/optical, near- and mid-IR extinction with a simple mixture (thin black solid line) of amorphous silicate (green dashed line) and graphite dust (blue dashed line), together with a population of large, $\mu$m-sized dust: (a) amorphous carbon of $a \approx 1.5\,\mu$m and C/H $\approx 60$ ppm, (b) graphite of $a \approx 1.5\,\mu$m and C/H $\approx 92$ ppm, (c) amorphous silicate of $a \approx 3.0\,\mu$m and Si/H $\approx 21,000$ ppm, and (d) iron of $a \approx 1.5\,\mu$m and Fe/H $\approx 84$ ppm. The thick red solid line plots the model fit, while the symbols plot the observed extinction: the magenta open triangles plot the $R_V = 3.1$ UV/optical/near-IR extinction, the other symbols plot the mid-IR extinction. See [4] for details.

dance” – the total abundance of this element in the ISM, both in gas and in dust; and $[X/H]_{\text{gas}}$ be the gas-phase abundance of this element. The abundance of this element in dust is $[X/H]_{\text{dust}} = [X/H]_{\text{ISM}} - [X/H]_{\text{gas}}$. The gas-phase Mg, Si and Fe abundances are negligible (i.e. these rock-forming elements are almost completely depleted from the gas phase; see Li (2005) and references therein). Therefore, for Si we have $[\text{Si/H}]_{\text{dust}} \approx [\text{Si/H}]_{\text{ISM}}$.

The interstellar abundance of Si (i.e. $[\text{Si/H}]_{\text{ISM}}$) is not known. Traditionally, one often adopts the solar photospheric abundances (e.g. Asplund et al.
of heavy elements as their interstellar abundances. However, Lodders (2003) argued that the currently observed solar photospheric abundances (relative to H) must be lower than those of the proto-Sun because helium and other heavy elements have settled toward the Sun’s interior since the time of the Sun’s formation some 4.55 Gyr ago. She further suggested that protosolar abundances derived from the photospheric abundances by considering settling effects are more representative of the solar system elemental abundances.

On the other hand, it has also been argued that the interstellar abundances might be better represented by those of B stars and young F, G stars (because of their young ages) which are just \(\sim 60-70\%\) of the solar values (i.e., “subsolar”; Snow & Witt 1996, Sofia & Meyer 2001). However, Li (2005) showed that if the interstellar abundances are indeed “subsolar” like B stars and young F, G stars, there might be a lack of raw material to form

Figure 5: Same as Figure 4 but for \(R_V = 4.0\).
the dust to account for the interstellar extinction. We also note that Przybilla et al. (2008) derived the photospheric abundances of heavy elements for six unevolved early B-type stars in the solar neighborhood OB associations and the field using NLTE techniques. They found that the photospheric abundances of those B stars are in close agreement with the solar values. Nieva & Przybilla (2012) further derived the photospheric abundances of 29 slowly-rotating early B-type stars. These stars exhibit <10% abundance fluctuations and their abundances are also similar to that of the Sun.

The Si abundance of the Sun, proto-Sun, and early B stars are respectively \([\text{Si/H}]_{\odot} \approx 32 \text{ ppm} \) (Asplund et al. 2009), 41 ppm (Lodders 2003), and 32 ppm (Przybilla et al. 2008, Nieva & Przybilla 2012). The model which best fits the UV/optical extinction requires \([\text{Si/H}]_{\text{dust}} \approx 34 \text{ ppm} \), consistent with the solar, proto-Sun or B stars Si abundance.

For C, it is more complicated since the gas-phase C abundance is recently
under debate. Earlier studies reported \([\text{C}/\text{H}]_{\text{gas}} \approx 140 \text{ ppm}\) from the weak intersystem absorption transition of \(\text{C II}\) at 2325 \(\text{Å}\) (Cardelli et al. 1996; Sofia et al. 2004). Very recently, Sofia et al. (2011) derived \([\text{C}/\text{H}]_{\text{gas}} \approx 100 \text{ ppm}\) for several interstellar sightlines from the strong transit ion of \(\text{C II}\) at 1334 \(\text{Å}\). They argued that the oscillator strength for the \(\text{C II}\) transition at 2325 \(\text{Å}\) previously used by Cardelli et al. (1996) and Sofia et al. (2004) to obtain \([\text{C}/\text{H}]_{\text{gas}} \approx 140 \text{ ppm}\) might have been underestimated.

The solar \(\text{C}\) abundance and proto-Sun \(\text{C}\) abundance are respectively \([\text{C}/\text{H}]_{\odot} \approx 224 \text{ ppm}\) (Asplund et al. 2009) and 288 ppm (Lodders 2003). The \(\text{C}\) abundance of the early B stars which are thought to be ideal indicators for the present-day interstellar abundances since they preserve their pristine abundances is close to the solar \(\text{C}\) abundance: \([\text{C}/\text{H}]_{\star} \approx 214 \pm 20 \text{ ppm}\) (Przybilla et al. 2008) and \([\text{C}/\text{H}]_{\star} \approx 209 \pm 15 \text{ ppm}\) (Nieva & Przybilla 2012). If the interstellar \(\text{C}\) abundance is like that of the early B stars (i.e., \([\text{C}/\text{H}]_{\text{ISM}} \approx 209 \text{ ppm}\)) or that of the proto-Sun (i.e., \([\text{C}/\text{H}]_{\text{ISM}} \approx 288 \text{ ppm}\)), with the gas-phase \(\text{C}\) abundance of \([\text{C}/\text{H}]_{\text{gas}} \approx 100 \text{ ppm}\) (Sofia et al. 2011) subtracted, there will be only \(\sim 109 \text{ ppm}\) or \(\sim 188 \text{ ppm}\) of \(\text{C}\) available to make the carbonaceous dust. However, the model which best fits the UV/optical extinction requires \([\text{C}/\text{H}]_{\text{dust}} \approx 292 \text{ ppm}\), substantially exceeding what would be available to be locked up in dust.

As shown in Figure 3, the silicate-graphite mixture model with \([\text{Si}/\text{H}]_{\text{dust}} \approx 34 \text{ ppm}\) and \([\text{C}/\text{H}]_{\text{dust}} \approx 292 \text{ ppm}\) closely reproduces the observed UV/optical/near-IR extinction. However, it fails in fitting the flat 3–8 \(\mu\text{m}\) mid-IR extinction (see Figure 4a). According to light scattering theory, dust absorbs and scatters starlight most effectively if its size is comparable to the starlight wavelength. Therefore, the dust which dominates the mid-IR extinction at \(\sim 3–8 \mu\text{m}\) should be in micrometer size scale, as inferred from the consideration of \(a \sim \lambda/2\pi\). This leads us to add an extra population of large, \(\mu\text{m}-\text{sized dust to account for the mid-IR extinction. We explore the size of the dust ranging from } a = 0.5 \mu\text{m to } a = 3.5 \mu\text{m. For simplicity, we only consider dust of sin-}

\[\text{We note that, except the composite dust model of Mathis (1996) which only requires [C/H]_{dust} \approx 155 \text{ ppm} (and [Si/H]_{dust} \approx 31 \text{ ppm, but see Dwek 1997)}, all interstellar grain models consume more C than the available value of } \sim 109 \text{ ppm or } \sim 188 \text{ ppm in the ISM: [C/H]_{dust} \approx 194 \text{ ppm} (and [Si/H]_{dust} \approx 20 \text{ ppm}) of Li & Greenberg (1997), [C/H]_{dust} \approx 231 \text{ ppm} (and [Si/H]_{dust} \approx 48 \text{ ppm}) of WD01, [C/H]_{dust} \approx 244 \text{ ppm} (and [Si/H]_{dust} \approx 36 \text{ ppm}) of Zubko et al. (2004), [C/H]_{dust} \approx 233 \text{ ppm} (and [Si/H]_{dust} \approx 50 \text{ ppm}) of Jones et al. (2013).} \]
gle sizes. In principle, we could assume a log-normal size distribution or the WD01-type size distribution for this \( \mu \)m-sized dust population. But we do not expect that a distribution of dust sizes would affect the conclusion drawn from the single-size model. A distribution of sizes would remove the ripple structures in the extinction curve of single-sized dust. The observed mid-IR extinction is commonly derived from broad-band photometry and therefore could tolerate the wavy ripples.

As shown in Figure 4a, the \( R_V = 3.1 \) model together with spherical amorphous carbon dust of radius of \( a \approx 1.5 \mu \)m and \( C/H \approx 60 \) ppm could closely fit the mid-IR extinction. These \( \mu \)m-sized amorphous carbon grains, with \( 2\pi a/\lambda \gg 1 \), are “gray” in the UV/optical wavelength regime. Therefore, the addition of \( \mu \)m-sized dust does not distort the fit to the observed \( R_V = 3.1 \) extinction curve provided by the silicate-graphite model. In total, this model requires \( [C/H]_{\text{dust}} \approx 352 \) ppm to account for the observed extinction from the UV to the mid-IR, with \( \sim 17\% \) of the C atoms locked up in the \( \mu \)m-sized amorphous carbon component.

We have also considered \( \mu \)m-sized graphite, amorphous silicate, and iron dust. As shown in Figure 4b, graphite of radius of \( a = 1.5 \mu \)m is also capable of reproducing the flat mid-IR extinction. However, the \( \mu \)m-sized graphite population requires \( C/H \approx 92 \) ppm. Therefore, amorphous carbon, with \( C/H \approx 60 \) ppm, seems more favorable since the \( R_V = 3.1 \) silicate-graphite model already encounters a “carbon crisis” problem: the model consumes more \( C/H \) than what is available.

As shown in Figure 4c, amorphous silicate could not fit the mid-IR extinction for two reasons: (1) the best-fit model with \( a = 3 \mu \)m predicts a prominent dip at \( \lambda \approx 8 \mu \)m which is not seen in the observed mid-IR extinction; this dip is due to the onset of the 9.7 \( \mu \)m Si–O stretch at \( \lambda \approx 8 \mu \)m; (2) this model requires Si/H \( \approx 21,000 \) ppm to be locked up in the \( \mu \)m-sized silicate dust, which is far more than the available amount of \([\text{Si/H}]_{\text{ISM}} \approx 32–41 \) ppm in the ISM.

Figure 4d shows the fit obtained with Fe/H \( \approx 84 \) ppm in iron spheres of \( a = 1.5 \mu \)m. Although the fit to the mid-IR extinction is excellent, this model requires a total depletion of Fe/H \( \approx 116 \) ppm, while the Fe abundance of the Sun, proto-Sun, and early B stars is only \([\text{Fe/H}]_\odot \approx 27.5 \) ppm (Asplund

\[13\] To account for the UV/optical extinction, the submicrometer-sized amorphous silicate component consumes Fe/H \( \approx 32 \) ppm.
et al. 2009), $[\text{Fe}/\text{H}]_{\odot} \approx 34.7$ ppm (Lodders 2003), and $[\text{Fe}/\text{H}]_{\star} \approx 28$–33 ppm (Przybilla et al. 2008, Nieva & Przybilla 2012), respectively.

Table 1: Model parameters for fitting the UV/optical and near-IR extinction.

| Extinction Type | $A_{\text{Ks}}/N_{\text{H}}$ $(10^{-23} \text{mag cm}^2)$ | $\alpha_{\text{S}}$ | $\alpha_{\text{C}}$ | $a_{\text{c,S}}$ $(\mu\text{m})$ | $f_{\text{C2S}}$ | $N'_{\text{S}}$ (cm$^{-2}$) | $[\text{Si}/\text{H}]_{\text{dust}}$ (ppm) | $[\text{C}/\text{H}]_{\text{dust}}$ (ppm) |
|----------------|---------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $R_V = 3.1$   | 6.26                            | 3.2             | 3.2             | 0.14            | 0.6             | $4.687 \times 10^{-24}$ | 34.0            | 292             |
| $R_V = 4.0$   | 6.85                            | 2.7             | 2.7             | 0.12            | 0.6             | $1.669 \times 10^{-21}$ | 30.7            | 264             |
| $R_V = 5.5$   | 7.40                            | 2.1             | 3.0             | 0.16            | 0.3             | $1.047 \times 10^{-18}$ | 40.0            | 172             |

We have also considered models for the $R_V = 4.0$ and $R_V = 5.5$ extinction curves since the flat mid-IR extinction has also been seen in dense regions (see Table 1). For the $R_V = 4.0$ case, we also assume that both silicate and graphite have the same size distribution. The results are shown in Figure 5 and Table 1. It is seen that both amorphous carbon of $a \approx 1.6 \mu\text{m}$ and graphite of $a \approx 1.5 \mu\text{m}$ could fit the flat mid-IR extinction. Again, amorphous carbon is preferred since it requires $\text{C}/\text{H} \approx 72$ ppm, less than that of graphite of $\text{C}/\text{H} \approx 92$ ppm. For the $R_V = 5.5$ case, we could not fit the UV/optical/near-IR extinction if we assume the same size distribution for both silicate and graphite. We therefore set $a_{\text{c,S}} = a_{\text{c,C}}$, but allow silicate and graphite to have different $\alpha$ values (i.e., $\alpha_{\text{S}} \neq \alpha_{\text{C}}$). The best-fit results are shown in Figure 6 and the model parameters are tabulated in Table 1. Similar to the $R_V = 3.1$ and $R_V = 4.0$ models, $\mu\text{m}$-sized amorphous carbon and graphite could closely fit the mid-IR extinction, with amorphous carbon being preferred since it does not consume as much C/H as graphite.

Finally, we note that it is not clear how $\mu\text{m}$-sized interstellar dust is formed. However, there are several pieces of evidence suggesting its presence in the ISM: (1) measurements by dust impact detectors on the interplanetary spacecrafts Ulysses and Galileo appear to indicate a substantial flux of interstellar particles with masses $> 10^{-12}$ g (corresponding to $a > 0.4 \mu\text{m}$ for silicate and $a > 0.5 \mu\text{m}$ for graphite) entering the heliosphere (see Landgraf et al. 2000, Krüger et al. 2007); (2) Taylor et al. (1996) reported radar detection of $a \approx 30 \mu\text{m}$ particles entering the Earth’s atmosphere on solar-hyperbolic trajectories implying that they are arriving from interstellar space. Socrates Draine (2009) discussed the detectability of very large interstellar grains of $a \sim 1 \text{mm}$ (“pebble”) through optical scattered light halos.
5. Summary

The mid-IR extinction curves of a wide variety of interstellar regions (including both diffuse and dense environments) exhibit a flat or “gray” behavior in the wavelength region of $\sim 3-8 \mu$m. This flat mid-IR extinction is hardly accounted for by the standard MRN silicate-graphite dust model. To explain the flat mid-IR extinction, we have considered various dust sizes and species, including amorphous silicate, graphite, amorphous carbon, and iron spheres. We find that $\mu$m-sized amorphous carbon dust best fits the flat mid-IR extinction. The observed extinction from the UV to the mid-IR could be closely reproduced by a mixture of submicrometer-sized amorphous silicate dust, submicrometer-sized graphitic dust, and micrometer-sized amorphous carbon dust. However, this mixture requires a solid-phase C abundance of $C/H \approx 352$ ppm, considerably exceeding what could be available in the ISM.

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