Article
An Integrated Linkage Map of Three Recombinant Inbred Populations of Pea (Pisum sativum L.)

Chie Sawada 1, Carol Moreau 1, Gabriel H. J. Robinson 1, Burkhard Steuernagel 1, Luzie U. Wingen 1, Jitender Cheema 1, Ellen Sizer-Coverdale 2, David Lloyd 3, Claire Domoney 1 and Noel Ellis 1

1 John Innes Centre, Norwich Research Park, Colney Lane, Norwich NR4 7UH, UK; chie.sawada@jic.ac.uk (C.S.); carolj.moreau@gmail.com (C.M.); gabriel.robinson@infarm.com (G.H.J.R.); Burkhard.Steuernagel@jic.ac.uk (B.S.); Luzie.Wingen@jic.ac.uk (L.U.W.); jitender.cheema@jic.ac.uk (J.C.); claire.domoney@jic.ac.uk (C.D.)
2 Institute of Biological, Environmental and Rural Sciences, Aberystwyth University, Plas Gogerddan, Aberystwyth SY23 3EB, UK; eys@aber.ac.uk
3 Germinal Horizon, Institute of Biological, Environmental and Rural Sciences, Aberystwyth University, Plas Gogerddan, Aberystwyth SY23 3EB, UK; david.lloyd@germinal.com
* Correspondence: noel.ellis2@jic.ac.uk
† Current address: Faculty of Medical Sciences, Newcastle University, Newcastle-upon-Tyne NE1 7RU, UK.

Abstract: Biparental recombinant inbred line (RIL) populations are sets of genetically stable lines and have a simple population structure that facilitates the dissection of the genetics of interesting traits. On the other hand, populations derived from multiparent intercrosses combine both greater diversity and higher numbers of recombination events than RILs. Here, we describe a simple population structure: a three-way recombinant inbred population combination. This structure was easy to produce and was a compromise between biparental and multiparent populations. We show that this structure had advantages when analyzing cultivar crosses, and could achieve a mapping resolution of a few genes.

Keywords: pea; genetic map; recombinant inbred population; integrated map

1. Introduction
The three recombinant inbred line (RIL) populations derived from reciprocal crosses between the cultivars Brutus (B), Enigma (E), and Kahuna (K) were generated to provide a set of populations derived from intercultivar crosses of interest to stakeholders of the UK Pulse Crop Genetic Improvement Network [1]. Analysis of early generations of the populations identified genetic regions associated with some traits of interest to pea breeding programs (yield, standing ability, seed size) [1]. Here, we describe a further analysis of these populations, using advanced RILs that were genotyped using 13,204 biallelic SNPs anchored to the pea genome sequence [2], and show the benefit of treating this as a single population for the purposes of genetic mapping.

2. Materials and Methods
2.1. Plant Material
The parents of the segregating populations were the cultivars Brutus (B), Enigma (E), and Kahuna (K). The source of plants used and their relationship to other cultivars are described in Moreau et al. [1]. BrutusAFP 84/384 was bred by DLF Seeds Ltd., and its parents were DP2459/86 and Bohatyr. Enigma was bred by Toft Plant Breeding, and its parents were the cultivars Jackpot and Delta. Jackpot was derived from a cross between Bohatyr and Solara. Brutus and Enigma therefore have some common genetic background derived from the cultivar Bohatyr. Kahuna was also bred by Toft, but with Cebeco as the UK agent, and this variety is currently listed in the UK under Limagrain (pers. comm. with
Jens Christian Nørgaard Knudsen of Nordic Seed and Steve Belcher of PGRO). The RILs derived from the three-way crosses described [1] were advanced by single-seed descent to F13, after which seeds were bulked to support replicated glasshouse and field studies. The three sets of advanced RILs were sown under glasshouse conditions using three or four replicates per line, and phenotypic data were gathered. Seeds were harvested from completely dried and senesced plants.

2.2. SNP Data and Mapping

RILs and their parents were genotyped by Neogen UK, using an Infinium array that detected 13,204 biallelic SNPs. These SNPs were either monomorphic or differed such that two cultivars shared an allele and the third was different. Thus, it was expected that any segregating marker would be scored in two of the three populations, creating the possibility of integrating the maps of these three RIL populations directly, and allowing a more precise association of allelic and phenotypic differences.

Accordingly, the data from the three RIL populations were collated in an Excel file so that all of the data for a single marker were represented as a single row. Each column corresponded to a RIL, and the score was recorded as “B”, “E”, “K”, or “-”, corresponding to the parental origin of the allele, and “-” representing missing data.

Note that for a marker, these three codes refer to just two alleles, but this scoring scheme records the parent of origin of the allele, which is required for genetic mapping. For example, the marker PsCam004787_3611_167 (the top marker on linkage group I) detected a T/C SNP and segregated in BK and EK but not BE, so the B allele in this case was identical to the E allele and different from K. The three possibilities are shown in Table 1.

Table 1. Examples of the three types of allelic calls.

| Marker     | SNP   | Segregates in | Common | Identity |
|------------|-------|---------------|--------|----------|
| PsCam004787| T/C   | BK            | EK     | K        | B = E    |
| PsCam014211| T/G   | BE            | EK     | E        | B = K    |
| PsCam042135| T/G   | BE            | BK     | B        | E = K    |

2.3. Estimates of Relatedness

The fraction of alleles shared between each pair of the parents was calculated directly from the data presented in Table 2. If dBE, dBK, and dEK represent the fractional distances between Brutus and Enigma, Brutus and Kahuna, and Enigma and Kahuna, respectively, then, in Figure 1, the length of the line from the point of trifurcation to Brutus (dBt) is \( \frac{1}{2}(dBE + dBK − dEK) \), etc. Statistical tests of deviation between observed and expected number of marker differences for each linkage group were performed as \( \chi^2 \) tests in which the expected value was in proportion to the total value for all linkage groups.

Table 2. Distribution of markers among populations.

| Linkage Group | Total | Unique to | Shared by |
|---------------|-------|-----------|-----------|
|               | EK    | BK        | EB        | EK & BK  | EK & EB  | BK & EB  |
| LG I          | 550   | 327       | 295       | 461      | 7        | 7        | 3        | 213      |
| LG II         | 726   | 438       | 560       | 444      | 2        | 7        | 1        | 280      |
| LG III        | 975   | 664       | 768       | 518      | 0        | 0        | 0        | 311      |
| LG IV         | 605   | 556       | 530       | 118      | 0        | 4        | 2        | 43          |
| LG V          | 456   | 425       | 206       | 276      | 3        | 1        | 1        | 29        |
| LG VI         | 576   | 398       | 491       | 254      | 2        | 7        | 0        | 28          |
| LG VII        | 668   | 637       | 580       | 107      | 5        | 4        | 3        | 24          |
| total         | 4556  | 3445       | 3430      | 2178     | 19       | 30       | 10       | 1071      |

The numbers of markers per linkage group (LG) are shown for the three populations. Numbers of markers that were unique or shared among populations are given. The shaded entries are those for which the number of distinguishing markers was close to the expectation from the data for all linkage groups; i.e., where the \( \chi^2 \) value was less than 10.
**Figure 1.** Genetic distances between parents. A representation of the genetic differences between Brutus, Enigma, and Kahuna. The relative genetic distances are represented by three linear vectors, each at an angle of 120° with respect to the other two. The differences between individual linkage groups (labeled LG I to LG VII) and the overall difference (labeled All) are given. The sum of the linear vector lengths was constant.

2.4. Construction of Individual Genetic Maps Using ASMap

For genotype data preparation, redundant markers were removed, and initial clustering of markers according to the pairwise Hamming distance between markers was carried out by ThreadMapperStudio [3] for each population. Each cluster was allocated a linkage group (LG) number in line with Table S3 of [4], and markers were labeled with this LG number in the genotype file. The library “ASMap” (v1.0-4) [5] from the R software environment (v4.0.3) was employed for the genetic map construction using a custom-made script (available at https://github.com/wingenl/genetic_mapping_with_ASMap accessed 24 December 2021). Default parameters were applied for the mapping, with the exception of the $p$-value threshold of $10^{-9}$ for the clustering and map distance calculation using the Kosambi mapping function. Subsequently, the orientation of each linkage group was aligned in the direction indicated in Table S8 of [4].

2.5. Construction of An Integrated Map

A total of 4556 markers were mapped in these populations, as summarized in Table 2. A small number of markers were mapped in only one population due to technical problems with allele calling.

Neogen allele calls were converted to “B”, “E”, and “K”, scores as shown above. The positions of 4556 PsCam markers on the seven pseudomolecules of the Caméor v1a assembly were obtained with a blastn analysis using marker sequence information from Supplementary Table 2 of [4] and the Caméor v1a Jbrowse site (https://urgi.versailles.inra.fr/Species/Pisum accessed 24 December 2021). Markers positioned on a pseudomolecule were ordered according to their physical position, and this was used as an initial order for the genetic map. This order was then examined to see whether local rearrangement might minimize the number of close double recombinants that were proposed by the initial order. Markers assigned to scaffolds, or that were not in a position consistent with the genetic map, were positioned with respect to their closest marker. Essentially, this was the
colormapping method of Kiss et al. [6]. The final map data are available in Table S1, and a heat map of all possible pairwise distances between markers within linkage groups is shown in Figure S1.

2.6. Single-Marker Analysis of Quantitative Traits

The average weight of the seed from each RIL was obtained from greenhouse grown plants. These values were then normalized so that each of the three RIL populations had a mean and standard deviation of 0 and 1, respectively. For each marker, the mean and standard deviation of the normalized values was calculated, and a t-test was performed to estimate the significance of the deviation of this difference from the expected value of 0.

3. Results

3.1. Relatedness of the Parental Genomes

Considering only the 4497 markers that were scored in two populations (i.e., where the allelic state was known in the three cultivars), the degree of relatedness between the parents could be estimated, and how this differed among the linkage groups is illustrated in Figure 1. Overall, Kahuna was more distinct from Brutus or Enigma than these were from each other. There were about twice as many markers that distinguished Kahuna from Brutus and Enigma than distinguished either of these from the other two (Table 2). However, this differentiation was not uniformly distributed among linkage groups (Table 2, Figure 1). Kahuna was most distinct for linkage groups IV and VII; while for LG I, it was most similar to the other two lines. Enigma was notably distinct for LG V, and this was statistically the most significant difference (as compared to the overall values).

3.2. The Number of Recombination Events Per RIL

In pea, there are ca. 16 chiasmata per meiosis [7], as crossing over occurs at the four-strand stage. This means that each gamete has, on average, ca. eight crossover events, so in total ca. 16 per individual sporophyte. In the construction of RILs, there were multiple meioses, so in each gamete in each generation, there were ca. eight crossovers. In RILs derived from selfing, in which the fraction of gametes that exhibit a recombination event is $R$, the corresponding fraction of recombination events per meiosis is $r$, and is given by the relationship $r = R/2(1 - R)$ [8]. The frequency distribution of recombination events in the RILs was therefore related to the number of crossovers per meiosis and the number of meioses. If a crossover occurred in a region that was homozygous (distally from the centromere towards the telomere), then the consequences of this event were not observable. Only ca. $\frac{1}{2}$ of crossovers in the F$_2$ led to observable recombination, $\frac{1}{4}$ in the F$_3$, and so on. The total number of recombination events seen to accumulate in the gametes of a RIL, after endless generations, was about twice the number of such events from the F$_1$ meiosis. After endless inbreeding, all gametes from a RIL were identical, so the number of observable recombination events in an RIL was about the same as in an F$_2$; however, in the RIL, they were in the same location in the maternally and paternally derived genomes. Thus, in pea, we expected to see about 16 crossover events per RIL, and the frequency distribution of these would approximate to a Poisson distribution (for which the mean was equal to the variance), as the recombination events were independent of one another. The distribution might have been slightly tighter than a Poisson, because at least one chiasma was required per bivalent for proper chromosomal disjunction (i.e., two out of the four gametes had a recombination event). The observed frequency distributions of recombination events per RIL are shown in Figure 2, and the means and variances are given in Table 3.
Table 3. Mean and variance of the number of recombination events per RIL linkage group.

| Linkage Group | Number of Crossovers |  |  |  |
|---------------|----------------------|--|--|--|
|               | Mean | Variance | Maximum | Variance/Mean |
| I             | 1.56 | 1.26     | 6       | 0.81         |
| II            | 1.76 | 1.39     | 6       | 0.79         |
| III           | 2.13 | 1.64     | 8       | 0.77         |
| IV            | 1.98 | 1.52     | 7       | 0.77         |
| V             | 1.83 | 1.57     | 8       | 0.85         |
| VI            | 1.62 | 1.44     | 6       | 0.89         |
| VII           | 1.96 | 2.14     | 8       | 1.09         |

3.3. The Linkage Map

The length of each linkage group was determined by counting the number of recombination events between adjacent markers, and then using these data to determine the fraction of RILs (\( R \)) that had recombined the parental alleles for the adjacent markers; from this value \( r \), the recombination rate per meiosis was determined as above. The recombination rate was converted to map distance using Haldane’s mapping function [9], which assumed that recombination events were independent of one another. The correlation coefficient between map length (cM) and the average number of recombination events (\( R \)) per linkage group was moderate (\( r^2 = 0.55 \)). Regression analysis gave the relationship cM = 42.4 + (49.3)\( R \), consistent with a requirement for one recombination event per chromosome (enabling proper disjunction) and for each recombination event corresponding to 50 cM. The compiled linkage map is shown in Figure 3.

Extended regions (>10cM) that did not have segregating markers in any of the three populations are marked with a dashed line in Figure 3. These were likely to be regions that were identical by descent (IBD), and may include genes that were selected by breeders; potential candidate genes for these selected traits are discussed below.

Linkage group I. All three parents were afila mutants, i.e., they were homozygous for a recessive \( af \) allele, and this was consistent with the large gap in the map in the region of \( Af \) on LG I; this further suggested that these three varieties carry the same \( afila \) allele.
Figure 3. The integrated genetic map of three RIL populations. The position of genetic markers are indicated as short horizontal bars on the combined linkage map, with horizontal bars to the right of each linkage group indicating the population in which the markers segregated (blue, red, and green for the EK, BK, and BE populations, respectively). Extended segments of the map, of at least 10 cM devoid of markers, which were most likely identical by descent, are indicated by dashed lines; the lengths of these regions are determined by the recombination fraction between the flanking markers. Genes corresponding to classical morphological or physiological phenotypes identified on the pseudomolecules of the Caméor v1a sequence assembly [2] are indicated by name; see Table S2. Approximate positions of genes placed on the map through linked markers are indicated by gene symbols in brackets.

**Linkage group II.** All three parents were white-flowered and carried a recessive allele at the A locus, yet there was no signature of IBD in this region. The data suggested that the a allele of Brutus had a different haplotype from Enigma or Kahuna. There were two large gaps (of presumed IBD) in this linkage group, but only the region including the genes Late1, Rug3, and K had identified genes, and of these, Late1 seemed the most likely to be under selection, as it is involved in photoperiod response [10]. Interestingly, for the Lf gene [11], which is also involved in the regulation of flowering time, but in a different pathway [12], Brutus and Kahuna shared a haplotype that was distinct in Enigma.

**Linkage group III.** This linkage group had two extended IBD regions. One was centered around Hr, another gene involved in the short-day response of pea [13], again suggestive of selection in relation to the control of flowering time. Interestingly, the genes Dne (LG III) and Sn (LG VII), also involved in this pathway [13], did not appear to share identity by descent.

**Linkage group IV.** Although there were several large IBD gaps in this linkage group, there was no obvious selection target identified.

**Linkage group V.** The single large IBD region in this linkage group was associated with the genes Det, R, and Tl, but these were not centrally located in the gap. All three cultivars were round seeded (and so carried a dominant allele at R), but it would seem unlikely that the same R allele would be under selection in independent breeding programs. Berdnikov [14] identified a lethal mutation in the R–Tl interval; this unidentified gene may be under strong selection, but it seems most likely that the locus under selection by breeders has not been identified.
**Linkage group VI.** There were two putative IBD regions in this linkage group. The largest of these, at the top of the linkage group, did not appear to be associated with a clear candidate for selection, but the lower segment was associated with the gene *ANR1a*, which is involved in root development [10], and is a possible candidate.

**Linkage group VII.** This linkage group was notable for the lack of markers segregating in the BE cross; those few markers showing allelic differences between Brutus and Enigma were in three tightly clustered groups (Figures 1 and 3, Table 2). Statistically, this was not the most significant deviation from the expected number of markers, but the combination of their number and marker distribution suggested that most of this linkage group was shared by Brutus and Enigma. This meant that the presumed IBD region for linkage group VII reflected the similarity of two rather than three chromosomes. The same could be argued for linkage group IV, which had a greater statistical significance, but the markers distinguishing Brutus and Enigma were more distributed. This similarity was probably due to shared descent derived from the cultivar Bohatyr (see the Materials and Methods section).

The genes identified as being associated with putative identity by descent regions among these three cultivars were all associated with phenology, flowering time, and plant architecture. This may simply reflect the nature of those genes that have been most intensively studied and were assigned positions on the genetic map. However, it is interesting that those genes assigned positions on the map that were associated with disease resistance (*Dmr, Er1, Sbm1, and Ppi2*) were not associated with IBD regions.

Of the pea NBS LRR genes discussed in [15], only one, AF123702, fell within an IBD region, on linkage group VI close to *Lst*. There were 225 positions on the “Caméor” v1a assembly that corresponded to NBS LRR gene sequences, and an additional 22 mapped to scaffolds (Table S1). Of the 225 that mapped to the pseudomolecules, 12 mapped to positions corresponding to IBD regions. The total map length was 929 cM, and the 13 IBD regions had a total map length of 250 cM, so by chance alone, we would expect 61 NBS LRR genes to lie within these gaps. The underrepresentation of NBS LRR genes within these gaps was statistically significant ($\chi^2 \simeq 52$), and may have reflected breeding selection for diversity at these sites.

### 3.4. Recombination: Map Distance between Recombination Events

A statistical treatment of the frequency distribution of recombination events along a linkage group based on the distribution theory of runs [16] is given in Appendix A. The data, which are plotted in Figure 4, showed a good fit to the expected distribution, which was consistent with recombination events being distributed at random with respect to the genetic map.

### 3.5. Comparison to the Three Individual Genetic Maps

Marker order and linkage group length were broadly conserved between the integrated map and the three separate maps (Figure S1). There were two main differences, the first was that the estimation of length of the putative IBD regions was more difficult where the gaps were longer, and the order of the segments was not easily determined when the gaps were of the order of 50 cM. In addition, there were regions where the marker order was inverted with respect to the integrated map and other individual maps. These were always adjacent to a large gap in the individual map, and presumably the mapping program minimized the number of recombination events between segments of the map that were very distant, and consequently added some double recombinants at the end of a linkage segment (Figures S2 and S3). Note that these were inversions of marker order in the map, not chromosomal inversions.
with their surrounding regions. This supported a recent coancestry of these regions, rather
than exceptionally low rates of recombination.

3.4. Recombination: Map Distance between Recombination Events

In general, the relationship between the genetic map and pseudomolecule assembly followed a sigmoid curve (Figure 5). The nearly vertical sections, where the recombination rate per Mb was very low, corresponded to pericentric regions [2]. Outside these regions, there were extended regions with a slope of roughly 1–3 Mb/cM. The gaps in the curves corresponded to regions of the pseudomolecule where no markers segregated in any of the three RIL populations; these were regions presumed to be identical by descent. These gaps did not seem to correspond to regions with exceptional recombination rates in comparison with their surrounding regions. This supported a recent coancestry of these regions, rather than exceptionally low rates of recombination.

Linkage group V, chromosome 3, had the lowest standard deviation of the cM/Mb ratio, and the recombination rate corresponded to approximately two crossovers per chromosome, but these were unevenly distributed among the two chromosome arms. For the long and short arms, the cM/Mb ratios were 0.35 ± 0.25 and 0.66 ± 0.39, respectively. The long arm was ca. 100 cM, and the short arm ca. 25 cM in length; the long arm had almost four times the number of crossover events of the short arm, and when taking this into account, the recombination rate per unit length of the long arm was about half that of the short arm. This chromosome therefore somehow distinguished the recombination rate on either side of the centromere. This chromosome was reported to have unusual synopsis

Figure 4. The frequency distribution of map distances between recombination events. The expectation for the frequency distribution of map distances between adjacent recombination events in a given individual is described in Appendix A. This distribution is defined by the relationship log $F_L = 2 \log(\epsilon) + L \log(1 - \epsilon) - \epsilon \log(1 - \epsilon)$, where $F_L$ is the frequency of intervals of length $L$ cM and $\epsilon$ ($=L/n$) (see Appendix A). The regression coefficient for the fitted line was 0.94, and the regression line ± one SEM is plotted on the graph. The expected relationship from the number of intervals observed and the total length of these intervals is plotted as the blue dashed line, and the solid red line represents the predicted relationship from the average value of $\epsilon$ from the slope and intercept of the regression line.

3.6. Genetic and Physical Maps

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in the cross JI15xJI399 [7], with severely reduced crossover number, which could be related to the difference in observed recombination rate between both chromosome arms.

Figure 5. Comparing genetic maps with chromosome assemblies. For each linkage group, marker position in cM is plotted on the x-axis against the position of the corresponding sequence on the cognate pseudomolecule (in Mb on the y-axis). In total, 4556 markers were plotted. The five markers that mapped to positions on other pseudomolecules are marked “X” at the top of each graph, and 92 markers that mapped to scaffolds are marked as filled circles at the top of each graph.

3.7. Nonlinear Patterns of Alignment

Linkage group II (chromosome 6) and linkage group VII (chromosome 7) both had extended regions where the mapping between linkage group and pseudomolecule was disturbed (Figure 5). In these regions, markers that were genetically close to each other were far apart on the corresponding pseudomolecule. In both these cases, nonlinearities corresponded approximately to the position of the centromeres. These could be explained as a consequence of misassembly of regions that had a high density of retrotransposons (notably, Tekay and Ogre [2]). Misassembly of the pseudomolecule was not the only possible explanation of this behavior, and it should be noted that these major disruptions to linearity all occurred close to the centromere, where non-recombination has been interpreted as a lack of crossover, but could in fact correspond to double recombination events within the centromere and occasionally in the adjacent segment. Such events would lead to a misassembly of the genetic map.

A second type of nonlinearity in the relationship was seen in the small number of scattered points where the order of markers in the genetic map was different from the order of the corresponding sequence in the pseudomolecule. These may have been errors in either the genetic map or the assembly, and in addition, could be a consequence of gene conversion events, which would appear as close double recombination events in the genetic map.
3.8. Quantitative Traits

The integrated map comprised 621 recombinant inbred lines, so the minimum fraction of lines that were recombinant ($R$) was ca. 1/600, corresponding to a recombination fraction per meiosis ($r$) of ca. 0.08 cM [8]. As the total map length was ca. 900 cM (Table 4), this meant that the resolution was ca. 0.01%, corresponding to a small number of genes. This suggested that the map had the potential to identify candidate genes for quantitative traits.

Table 4. Recombination rates per linkage group and chromosome.

| LG | cM | Total Length Mb | Number of Marker Intervals | cM/Mb | SD |
|----|----|-----------------|--------------------------|-------|----|
| I  | 110| 342 ch2         | 490                      | 0.52  | 1.70 |
| II | 126| 384 ch6         | 611                      | 0.41  | 0.71 |
| III| 151| 463 ch5         | 832                      | 0.32  | 0.32 |
| IV | 132| 357 ch4         | 544                      | 0.52  | 2.07 |
| V  | 126| 438 ch3         | 442                      | 0.36  | 0.29 |
| VI | 138| 298 ch1         | 508                      | 0.40  | 0.76 |
| VII| 145| 393 ch7         | 583                      | 0.46  | 0.68 |
| All| 928| 2675            | 4010                     | 0.42  | 1.09 |

Table 4. The length of the pseudomolecules of the Caméor v1a assembly, taken from https://urgi.versailles.inra.fr/Species/Pisum (accessed 24 December 2021) and not including scaffolds not assigned to pseudomolecules; the corresponding chromosomes are designated ch1 to 7. The recombination rate along each linkage group in cM/Mb was calculated as the mean of the difference in position in cM divided by the difference in position (in Mb) for markers separated by 10 marker intervals. For some pairs, this could not be calculated because the markers were too close to the end of a linkage group, at least one marker was on a scaffold or other pseudomolecule in the v1a assembly. For those markers on the same pseudomolecule that were anomalously far apart, and where this difference was negative, the marker pair was ignored; where the difference was positive, this contributed to an anomalously low cM/Mb value. The recombination rates are plotted in Figure S4.

Previous work with these three populations [1], and a map mainly derived from retrotransposon-based, sequence-specific amplified polymorphism (SSAP) genetic markers, identified QTL for seed size (mean seed weight) on linkage groups I (two loci), III, IV, and V. Using mature seed weight data for the advanced RILs (Table S4), a single-marker analysis of seed weight differences again identified QTL on these linkage groups.

The largest QTL on LG I (Figure 6) close to AGPase [1] (PsCam001055) was identified in the BK subpopulation. The corresponding QTL in the EK subpopulation was in a slightly different location, close to a gene annotated as a transmembrane amino acid transporter (Figure S5). Previously identified QTL on the other end of LG I and LG III in the BE subpopulation (Moreau et al. [1]) were not confirmed by these data. The QTL on LG IV was at PsCam026873, annotated as “Annexin family signature”, and the peak on LG V was at PsCam054756, annotated as “Eukaryotic translation initiation factor 3 subunit 7 (eIF-3)”. The lowest Student’s $t$-value for the BE subpopulation was at PsCam001302, but this was likely to be an artifact, as there were many missing scores for this marker, and it cosegregated with 17 other markers that spanned a 30 Mb region in the pericentric region of chromosome 1 (LG VI, Figure 5). Nevertheless, this block as a whole did have the lowest Student’s $t$-value for BE, suggesting that there was indeed a gene within this pericentric block for which allelic variation contributed to variation in mean seed weight.
pairwise combinations of crosses between three inbred lines could provide useful resources for genetic mapping. This strategy allowed the genetic variation among the three inbreds to be studied coordinately, and the combination of three parents increased the number of markers that could be scored. In addition, the three RIL populations facilitated the generation of a large number of informative RILs, and therefore more overall recombination. Mapping with the integrated populations mitigated some difficulties with determining marker order in individual biparental RIL populations, as was exacerbated by regions of presumed identity by descent. The problem of identity by descent is inevitable in the examination of crosses between related cultivars. Indeed, the differences in marker order as determined by ASMap for the individual subpopulations and the integrated map were all associated with regions of pairwise identity (Figures S2 and S3). The three-way recombinant inbred population structure thus increased both the marker density and the resolution of the genetic map, while the inclusion of a third parent could compensate for some of the difficulties that could arise due to identity by descent.

In this population, we identified several regions of putative identity by descent among all three parents, and pairwise IBD differed among linkage groups (Figures 1 and 3). We ruled out that these regions were caused by an unusual distribution of recombination events (Figures 2 and 6) to support their identity by descent. We hypothesized that breeder selection led to regions identical by descent, and suggested plausible gene candidates as the targets of selection for some regions (Figure 3); however, many IBD regions currently lack gene candidates. The most obvious example of an IBD region explained by a candidate gene was the region encompassing the Aphiia gene; all three cultivars were aphiia mutant types, and presumably carried the same allele at this locus, accounting for the extended

![Figure 6. Mean seed weight analysis. Mean seed weight data were obtained for all RILs (except for one RIL, BK3). These were standardized to a mean of zero and standard deviation of 1 within each RIL population. For each marker, the difference between the means of RILs with contrasting genotypes was calculated, and then the Student’s t statistic was calculated, and this value was plotted on the y-axis, with marker position on the x-axis. Genes close to the maximum or minimum t for each of the three subpopulations are indicated (see also Figure 5). The upper plot shows an expanded linkage group I.](image-url)
region of identity by descent. However, the behavior of the region around the gene A was puzzling. All three cultivars were homozygous for a and were white-flowered; however, the data suggested that recombination occurred close to the A locus in the ancestors of these lines, generating new haplotypes in this region. The contrast between A and Af probably reflected the antiquity of the introduction of white-flowered cultivars [17].

A close examination of the genotypic data showed that recombination events were randomly distributed among RILs. Within the RILs, these were also randomly distributed with respect to the genetic map (Figures 2 and 4). However, this was not the case with respect to the physical map, as we saw extended regions lacking recombination corresponding to the pericentromeres, as has been reported previously [2]. Outside these regions, the recombination rate per unit physical distance was reasonably constant (Figures 6 and S4).

The high marker density and the number of RILs in the combined population enabled a simple single-marker-based approach to determine candidate genes underlying quantitative traits as illustrated by seed size (Figures 6 and S5).

These observations suggested that three-way recombinant inbred populations are a powerful tool for the analysis of genetic variation, especially among cultivated material for which identity by descent can make genetic map construction problematic. For species such as pea, where seeds are large and seed multiplication rates and the number of seed set per cross pollination are low, the production of multparent advanced generation intercross populations [18] is very labor-intensive, while the production of recombinant inbred lines is relatively easy once the initial crosses have been performed. The three-way recombinant inbred combination added more genetic diversity to a mapping population compared to a single RIL population, and the generation of ca. 600 RILs was readily achievable, providing mapping resolution of the order of a few genes.

Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/genes13020196/s1, Figure S1: Heat maps of pairwise inter-marker distances per linkage group, Figure S2: Comparing individual genetic maps with the integrated map, Figure S3. An inverted map segment in the BK linkage group I map, Figure S4. Recombination rates, Figure S5. Candidate genes for a major seed weight QTL, Figure S6. Frequency distribution of the number of intervals between recombination events. Table S1: Genotype data, Table S2: Genomic locations, Table S3: NBS LRR locations, Table S4: Seed weights.

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Appendix A

The frequency distribution of distances between recombination events

The data shown in Figure 2 and Table 3 of the main text were consistent with the recombination events within these populations being distributed at random, close to the expectation of a Poisson distribution, and with a small average number (2 to 3) of crossovers per linkage group. This left the question of whether these were also distributed at random along the linkage groups. This could be examined by following the statistics described in the distribution theory of runs [16], which describes the mean and variance of the length of runs of different classes of object arranged in a line. For two types of object (such as intervals without a crossover vs intervals with a crossover), this can be approximated by the relationship in Equation (A1):

\[ F_n = p^2(1 - p)^n \]
\[ \text{or } \log F_n = 2 \log(p) + n \log(1 - p) \]

(A1)

where \( F_n \) is the frequency of runs of \( n \) markers of allele A flanked on both sides by allele B (i.e., exactly \( n - 1 \) successive intervals without a recombination event bounded by two intervals with recombination events), and \( p \) is the frequency of intervals in which there is a recombination event. In the log form of the equation, the plot is a straight line, and \( p \) can be determined by regression analysis from the slope and intercept. Note that \( p \) can also be determined directly from the data, so the correspondence between the observed and predicted values of \( p \) told us whether the data were a good fit to a random distribution of spacings between recombination events.

The data for all linkage groups were examined, and the number of markers between adjacent crossovers was counted for each RIL. Note that at least 2 crossovers for a linkage group were required in order to define a distance between recombination events, so not all RILs contributed to this analysis (Mood’s statistical treatment accounts for such end effects, but these need to be ignored for this simpler treatment). Some markers were scored “-”, so we cannot know whether there was a recombination event between two adjacent “-” scores, but it was assumed that this was not generally the case. Similarly, in a run of scores such as: AAAA——BBBB, there was clearly a recombination event somewhere within the sequence of “-” scores, but we cannot say where, and therefore could not determine \( n \). A sequence such as: BBBBAAAAAAAA—AAAAABB was considered to have two recombination events, one at the BA transition and the other at the AB transition, and it was assumed that there were no recombination events between the successive markers scored as “-”, so in this case, the total number of markers between the recombination events was the sum of the number of A scores plus the number of “-” scores in the span between the B scores.

The resultable data set corresponded to a total of 3356 spans or runs of markers for which \( n \) could be determined. These included 525,362 intervals, and these were necessarily bounded by intervals where there was a recombination event. Thus, there were in total 532,074 intervals (including 3356 \( \times \) 2 corresponding to the two ends) being considered. Note that if there were three recombination events in a linkage group in an individual RIL, one of these intervals was counted twice.

The resulting frequency distribution is shown in Figure S6, which shows a broad scatter of values, but there was a trend in the data (\( r = 0.83 \)), and the data were a reasonable fit to the theoretical prediction. The slope of the regression line was a little shallower than might be expected from the data points, presumably due to multiple data points with the same value. For the observed value of \( p \), the fraction of intervals with a recombination event in this data set was 0.0063, and the estimated values from the slope and intercept were 0.0045 \( \pm \) 0.0001 and 0.0052 \( \pm \) 0.0001, respectively. For the data set as a whole, \( p \) was 0.0033, lower than above because this included RILs with 0 or 1 recombination event. The difference between the expected and observed values may have been due to combining the data for all linkage groups in a single analysis when there were different numbers of recombination events in the different linkage groups. Furthermore, the regions of identity
by descent corresponded to intervals that were longer than those typical of the map as a whole, so the number of recombination events within these regions may have distorted the analysis.

**Map distance between recombination events**

A problem with considering the number of intervals between recombination events was that the intervals in the map were of a wide range of sizes, in this case notably in the regions of identity by descent. This meant the value of \( p \) in Equation (A1) was an average, and was in fact quite variable. An alternative is to consider the frequency distribution of map lengths between recombination events in each individual. Rather than considering successive intervals, we considered successive elements (\( \epsilon \)) of the map of a fixed length, such that a map length of \( L \) cM corresponded to \( n \) successive intervals of length \( \epsilon \).

In other words: \( L = n \epsilon; n = L/\epsilon \). The chance of finding exactly \( n \) successive elements bounded by a recombination event at either end is therefore represented by Equation (A2):

\[
F_L = \epsilon^2 (1 - \epsilon)^{(L/\epsilon)}
\]

or

\[
\log F_L = 2\log(\epsilon) + L\log(1 - \epsilon) - \epsilon\log(1 - \epsilon)
\]

A plot of \( \log F_L \) vs. map length (\( L \)) therefore should have a slope of \( \log(1 - \epsilon) \) and an intercept of \( 2\log(\epsilon) - \epsilon\log(1 - \epsilon) \), where \( \epsilon = L/n \) is the map length per recombination event in an individual. Note that this was not the same as the map length per recombination event in the population as a whole, which was defined by the genetic map function. This relationship is plotted in Figure 4 of the main text.

**Close double recombination events**

Contrary to common assumptions, close double recombination events are expected when there is no interference. This is obvious in Equation (A1) which had its maximum value at \( n = 0 \). In recombinant inbred lines, only half of the recombination events occurred in the first meiosis, while the remainder were distributed over meioses in successive generations and therefore were not susceptible to interference between generations. If there was some ordering in the position of recombination events with respect to chromosome structure, then there may have been negative interference in recombination events in successive generations; i.e., they tended to occur in similar places. This happens if chiasmata interfere with each other and structural features of the chromosome, as is known to be the case [19].

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