Optimizations of force-field parameters for protein systems with the secondary-structure stability and instability

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We propose a novel method for refining force-field parameters of protein systems. In this method, the agreement of the secondary-structure stability and instability between the protein conformations obtained by experiments and those obtained by molecular dynamics simulations is used as a criterion for the optimization of force-field parameters. As an example of the applications of the present method, we refined the force-field parameter set of the AMBER ff99SB force field by searching the torsion-energy parameter spaces of $\phi$ (N-C$^\alpha$-C-N) and $\psi$ (C$^\beta$-C$^\alpha$-C-N) of the backbone dihedral angles. We then performed folding simulations of $\alpha$-helical and $\beta$-hairpin peptides, using the optimized force field. The results showed that the new force-field parameters gave structures more consistent with the experimental implications than the original AMBER ff99SB force field.

I. INTRODUCTION

In the field of molecular simulations of protein systems, force fields are widely used. The force field is represented by a sum of potential-energy terms, which are given by functions and their parameters based on classical mechanics. There are several well-known force fields, such as AMBER\textsuperscript{6,7}, CHARMM\textsuperscript{8,9}, OPLS\textsuperscript{10}, GROMOS\textsuperscript{11}, and ECEPP\textsuperscript{11}. When many researchers perform molecular simulations of protein systems, these force fields are utilized extensively. Generally, the force-field parameters are determined based on experimental results for small molecules and theoretical results using quantum chemistry calculations of small peptides such as alanine dipeptide.

In a force field, the potential energy is usually composed of the bond-stretching term, bond-bending term, torsion-energy term, and nonbonded energy term. In these energy terms, it is known that the torsion-energy term is the most problematic. For instance, the ff94\textsuperscript{12} and ff96\textsuperscript{13} versions of AMBER differ only in the backbone-torsion-energy parameters. Nevertheless, these secondary-structure-forming tendencies are quite different\textsuperscript{14–16}. Therefore, many researchers have studied this energy term and its force-field parameters. Recently, new force-field parameters of the backbone torsion-energy term about $\phi$ and $\psi$ angles have been developed, which are, e.g., AMBER ff99SB\textsuperscript{14}, AMBER ff99SB\textsuperscript{15}, CHARMM 22/CMAP\textsuperscript{2} and OPLS-AA/I\textsuperscript{2}. Newly proposed methods of the force-field refinement also mainly concentrate on the torsion-energy terms. These modifications of the torsion energy are usually based on quantum chemistry calculations\textsuperscript{17,21}. We have also proposed a force-field refinement method in the previous works\textsuperscript{14–16,22–25}. These methods are based on the Protein Data Bank (PDB) and minimize some score functions in the force-field parameter space. One of the methods consists of minimizing the sum of the square of the force acting on each atom in the proteins with the structures from the PDB\textsuperscript{14–16,24,25}. Other approaches use the root-mean-square deviation between the original PDB structures and the corresponding minimized structures as the score function\textsuperscript{22,23}.

In this article, we introduce a novel optimization method for force-field parameters, which searches the lowest value of a score function defined by the sum of numbers of amino acids, which have secondary-structure conformations. As an example, we applied this approach to AMBER ff99SB force field and determined new force-field parameters for $\psi$ (N-C$^\alpha$-C-N) and $\zeta$ (C$^\beta$-C$^\alpha$-C-N) angles. Here, we are using the Greek letter $\zeta$ for the dihedral angle defined by C$^\beta$-C$^\alpha$-C-N.

In Methods section the details of the methodology are given. In Results and Discussion section the results of applications of the optimization method to the AMBER ff99SB force field are presented. The last section is devoted to conclusions.

II. METHODS

A. Force-field parameters

The existing force fields for protein systems such as AMBER\textsuperscript{6,7}, CHARMM\textsuperscript{8,9}, and OPLS\textsuperscript{10} use essentially the same functional forms for the potential energy $E_{\text{conf}}$ except for minor differences. The conformational poten-
tial energy $E_{\text{conf}}$ can be written as,

$$E_{\text{conf}} = E_{\text{BL}} + E_{\text{BA}} + E_{\text{torsion}} + E_{\text{nonbond}}, \quad (1)$$

where, $E_{\text{BL}}$, $E_{\text{BA}}$, $E_{\text{torsion}}$, and $E_{\text{nonbond}}$ represent the bond-stretching term, the bond-bending term, the torsion-energy term, and the nonbonded energy term, respectively. Each force field has similar but slightly different parameter values. For example, the torsion energy is usually given by

$$E_{\text{torsion}} = \sum_{\text{dihedral angle } \Phi} \sum_{n} V_n \left[ 1 + \cos(n\Phi - \gamma_n) \right], \quad (2)$$

where the first summation is taken over all dihedral angles $\Phi$ (both in the backbone and in the side chains), $n$ is the number of waves, $\gamma_n$ is the phase, and $V_n$ is the Fourier coefficient. Namely, the energy term $E_{\text{torsion}}$ has $n$, $\gamma_n$, and $V_n$ as force-field parameters.

B. Optimization method of force-field parameters

We now describe our new method for optimizing the force-field parameters. In this method, we prepare $M$ protein structures, which are some experimentally determined conformations. For these proteins, we perform MD simulations, which start from the experimental conformations, by using a trial force field. We try to perform MD simulations with varied values of force-field parameters. After that, we estimate the “$S$” value defined by the following function from the trajectories of the $M$ proteins obtained from the trial MD simulations:

$$S = \sum_{i=1}^{M} \left( \frac{n_{i}^{S\rightarrow U}}{N_{i}^{S}} + \frac{n_{i}^{U\rightarrow S}}{N_{i}^{U}} \right), \quad (3)$$

Here, $n_{i}^{S\rightarrow U}$ is the number of the amino acids in protein $i$ where their structures in PDB (initial conformation) had some secondary structures (such as $\alpha$-helix, $3\alpha$-helix, $\pi$-helix, and $\beta$ structures) but transformed into unstructured, coil structures without any secondary structures after a short MD simulation. Likewise, $n_{i}^{U\rightarrow S}$ is the number of amino acids in protein $i$ where their structures in PDB had coil structures but transformed to have some secondary structures after a MD simulation. $N_{i}^{S}$ is the total number of amino acids in protein $i$ which have some secondary structures in PDB, and $N_{i}^{U}$ is the total number of amino acids in protein $i$ which have coil structures in PDB.

When we calculate the $S$ values for the conformations obtained from MD simulations by using trial force-field parameters, the parameter set, which yields the minimum $S$ value, is considered to give the optimized force field. We remark that we want the number of proteins $M$ and the total number of time steps of each MD simulation to be as large as possible in order to reduce the effects of experimental and systematic errors. In practice, the available computer power decides them.

III. RESULTS AND DISCUSSION

A. Applications of the optimization method

We present the results of the applications of our optimization method presented in the previous section to the AMBER ff99SB force field. We first chose 31 PDB files ($M = 31$) with resolution 2.0 Å or better, with sequence similarity of amino acid 30.0 % or lower, and with from 40 to 111 residues (the average number of residues is 86.7) from PDB-REPRDB. Namely, the PDB IDs of these 31 proteins are 1LDD, 1HBK, 1Y02, 1I2T, 1U84, 2ERL, 1TQG, 1OSD, 1LQ, 1WHO, 1CQY, 1H75, 1GMX, 1IB, 1VC1, 1AY7, 1KAF, 1KPF, 1BM8, 1MK0, 1EW4, 1OSD, 1VCC, 1OPD, 1CYO, 1CTF, and 1N9L (these structures are shown in Fig. 1). We added hydrogen atoms to the PDB coordinates by using the AMBER11 program package. We then performed short potential energy minimizations while restraining the coordinates of the heavy atoms. We used the obtained conformations as the initial structures. These initial conformations were used as reference experimental structures in the definition of $S$ in Eq. (3). For short MD simulations, the unit time step was set to 2.0 fs and the bonds involving hydrogen were constrained by the SHAKE algorithm. Each simulation was carried out for 40.0 ps (hence, it consisted of 20,000 MD steps) by using Langevin dynamics at 300 K. The nonbonded cutoff of 20 Å were used. As for solvent effects, we used the GB/SA model included in the AMBER program package ($\sigma = 5$). For all the calculations, we used the AMBER11 program package.

As the target force-field parameters, we used the parameters $V_1$ of $\psi$ (N-C\textsuperscript{$\alpha$}-C-N) and $\zeta$ (C\textsuperscript{$\beta$}-C\textsuperscript{$\alpha$}-C-N) angles for the torsion-energy term in Eq. (2). We performed the simulations by using 14 and 15 different values of the $V_1$ parameters of $\psi$ and $\zeta$, respectively, and each simulation with a fixed set of parameter values was repeated five times by changing the initial velocities of atoms in the 31 proteins. Namely, we calculated $n_{i}^{S\rightarrow U}$ and $n_{i}^{U\rightarrow S}$ in Eq. (3) as the average numbers of $n_{i}^{S\rightarrow U}$ and $n_{i}^{U\rightarrow S}$ of 10 conformations from the last 20.0 ps (within 40.0 ps) for each simulation (the total number of conformations was thus 50 for each protein). The results are shown in Fig. 2. We determined the optimized force-field parameters in order of $\zeta$ and $\psi$, by searching the minimum value of $S$ in Fig. 2. The optimized $V_1$ value for $\zeta$ is $-1.60$ (while the original value is 0.20), and the optimized $V_1$ value for $\psi$ is 0.31 (while the original value is 0.45).

B. Test simulations of two peptides

In order to test the validity of the force-field parameters obtained by our optimization method, we performed the folding simulations using two peptides, namely, C-terminal fragment of streptococcal protein G, which is some-
times referred to as G-peptide. The C-peptide has 13 residues and its amino-acid sequence is Lys-Glu−Thr-Ala-Ala-Ala-Lys+−Phe-Glu-Arg+−Gln-His+−Met. This peptide has been extensively studied by experiments and is known to form an α-helix structure. Because the charges at peptide termini are known to affect helix stability, the N and C termini of the peptide was blocked with acetyl and N-methyl groups, respectively. The G-peptide has 16 residues and its amino-acid sequence is Gly-Glu−Trp-Thr-Tyr-Asp−Asp−Ala-Thr-Lys+−Thr-Phe-Thr-Val-Thr-Glu+. The termini were kept as the usual zwitter ionic states, following the experimental conditions. This peptide is known to form a β-hairpin structure by experiments.

For test simulations, we used replica-exchange molecular dynamics (REMD). The unit time step was set to 2.0 fs, and the bonds involving hydrogen were constrained by the SHAKE algorithm. Each simulation was carried out for 30.0 ns (hence, it consisted of 15,000,000 MD steps) with 32 replicas by using Langevin dynamics. The replica exchange was tried every 3,000 steps. The temperature was distributed exponentially: 600, 585, 571, 557, 544, 530, 517, 505, 492, 480, 469, 457, 446, 435, 425, 414, 404, 394, 385, 375, 366, 357, 348, 340, 332, 324, 316, 308, 300, 293, 286, and 279 K. As for solvent effects, the N and C termini of the peptide was kept as the usual zwitter ionic states, following the experimental conditions. This method can optimize force-field parameters using the AMBER program package (igb = 5). These simulations were performed with different sets of randomly generated initial velocities.

In Fig. 3, α-helicity and strandness of two peptides obtained from the REMD simulations are shown. For the original AMBER ff99SB force field, the α-helicity is clearly larger than the strandness in not only C-peptide but also G-peptide. Namely, the original AMBER ff99SB force field clearly favors α-helix structure and does not favor β structure. On the other hand, for the optimized force field, in the case of C-peptide, the α-helicity is larger than the strandness, and in the case of G-peptide, the strandness is larger than the α helicity. We can see that results obtained from the optimized force field are in better agreement with the experimental results than the original force field.

In Fig. 4, 310 helicity and π helicity of two peptides obtained from the test simulations are shown. For 310 helicity, the optimized force field does not favor it, while the original force field favors it to some extent. π helicity has almost no value in the both cases of the original and optimized force fields for the two peptides. As the both peptides have no 310-helix and π-helix in the experimental results, these results of the optimized force field also have better secondary-structure-forming tendencies than those of the original force field.

In Fig. 5, the 32 lowest-energy conformations of C-peptide obtained from the REMD simulations for each replica in the case of the original and optimized force fields are shown. In the case of the original force field, 27 conformations have helix structures; 15 of them are α-helix and 12 are 310-helix. In the case of the optimized force field, on the other hand, 14 conformations have helix structures, and all of them are α-helix. Moreover, five conformations are β structures. Both force fields favor helix structures more than β structures. The original force field also has some tendency to favor 310-helix structures, while the optimized force field does not. This result is consistent with the results of 310 helicity in Fig. 4.

In Fig. 6, the 32 lowest-energy conformations of G-peptide obtained from the REMD simulations for each replica are shown. As in the case of C-peptide, 27 conformations obtained from the simulations with the original force field have helix structures; 11 of them are α-helix, 15 are 310-helix, and one is π-helix. In the case of the optimized force field, 11 conformations have helix structure (nine are α-helix and two are 310-helix), and 16 conformations have β structures. We see that the optimized force field slightly favors β structure in agreement with the experimental implications.

IV. CONCLUSIONS

In this work, we proposed a new optimization method of force-field parameters and, as an example, optimized some torsion-energy parameters of the ff99SB force field. This method can optimize force-field parameters using PDB structures. We applied these optimization method using 31 protein molecules from the Protein Data Bank. We then performed folding simulations of α-helical and β-hairpin peptides. We found that the 310 helicity of the optimized force field decreases for both peptides and that the strandness of the optimized force field increases for β-hairpin peptide in comparison with those of the original ff99SB. The results therefore showed that the optimized force-field parameters gave structures more consistent with the experimental implications than the original ff99SB force field. Moreover, the results also showed that the secondary-structure-forming tendencies depend strongly on only two parameters of backbone-torsion-energy term. We are now testing the validity of our method by the folding simulations of larger proteins.

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1Cornell, W. D.; Cieplak, P.; Bayly, C. I.; Gould, I. R.; Kenneth M. Merz, J.; Ferguson, D. M.; Spellmeyer, D. C.; Fox, T.;
FIG. 1. Structures of 31 proteins from PDB, which were used in the optimization of force-field parameters. The figures were created with VMD.
FIG. 2. $S$ values (defined in Eq. 2) obtained from MD simulations of 31 proteins with the force fields which have different $V_1$ parameter values for $\zeta (C^\beta-C^\alpha-C-N)$ (a) and $\psi (N-C^\alpha-C-N)$ (b) angles.
FIG. 3. $\alpha$ helicity (a-1) and strandness (a-2) of C-peptide and $\alpha$ helicity (b-1) and strandness (b-2) of G-peptide as functions of the residue number. These values were obtained from the REMD simulations at 300 K. Dotted and normal curves stand for the original AMBER ff99SB and the optimized force field, respectively.
FIG. 4. $3_{10}$ helicity (a-1) and $\pi$ helicity (a-2) of C-peptide and $3_{10}$ helicity (b-1) and $\pi$ helicity (b-2) of G-peptide as functions of the residue number. These values were obtained from the REMD simulations at 300 K. Dotted and normal curves stand for the original AMBER ff99SB and the optimized force field, respectively.
FIG. 5. Lowest-energy conformations of C-peptide obtained for each replica from the REMD simulations. (a) and (b) are the results of the original AMBER ff99SB and the optimized force field, respectively. The conformations are ordered in the increasing order of energy. The figures were created with DS Visualizer.
FIG. 6. Lowest-energy conformations of G-peptide obtained for each replica from the REMD simulations. (a) and (b) are the results of the original AMBER ff99SB and the optimized force field, respectively. The conformations are ordered in the increasing order of energy. The figures were created with DS Visualizer.