A single ion as a three-body reaction center in an ultracold atomic gas

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We report on three-body recombination of a single trapped Rb⁺ ion and two neutral Rb atoms in an ultracold atom cloud. We observe that the corresponding rate coefficient $K_3$ depends on collision energy and is about a factor of 1000 larger than for three colliding neutral Rb atoms. In the three-body recombination process large energies up to several 0.1 eV are released leading to an ejection of the ion from the atom cloud. It is sympathetically recooled back into the cloud via elastic binary collisions with cold atoms. Further, we find that the final ionic product of the three-body processes is again an atomic Rb⁺ ion suggesting that the ion merely acts as a catalyst, possibly in the formation of deeply bound Rb₂ molecules.

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Early on in the quest for ultracold quantum gases three-body recombination played a crucial role as a limiting factor for Bose-Einstein condensation. It was first investigated in spin-polarized hydrogen [1] and somewhat later for alkali atoms [2-5]. For samples with large scattering lengths three-body processes can be resonantly modified through the formation of Efimov states [6]. Recently, three-body recombination was investigated with single atom resolution [7]. Combining ultracold atoms with cold trapped ions is an emerging field where large scattering cross sections naturally come into play due to the comparatively long range $1/r^4$ polarization interaction potential. Two-body collisions between atoms and ions in the low energy regime have been recently studied [8-12]. In this letter, we report on three-body collisions involving two ultracold $^{87}$Rb atoms and a $^{87}$Rb⁺ ion at mK temperatures.

The ion in our experiment can be regarded as a reaction center, facilitating molecule formation through its large interaction radius. For the work presented here, it is essential that we work with ions and atoms of the same species. This renders charge transfer reactions irrelevant, which otherwise would strongly constrain our measurements. Since no accessible optical transition is available for Rb⁺, it is not amenable to laser-cooling and cannot be imaged. We therefore detect the ion and investigate its dynamics in an indirect way, i.e. through its action on the atom cloud. In our experiments, we place a single ion into the center of an atomic sample resulting in a continuous loss of atoms due to elastic atom-ion collisions. This behavior is interrupted when a highly energetic three-body process ejects the ion from the atom cloud. By examining the statistics of ion-induced atom loss in hundreds of repetitions of the experiment, we can investigate a number of important details of the three-body process, such as its quadratic density-dependence, the energy that it releases, its rate coefficient $K_3$ and the dependence of $K_3$ on collisional energy. We also obtain information on the reaction products. As an important byproduct, our measurements also demonstrate sympathetic cooling of an ion from eV energies down to about 1 mK using an ultracold buffer gas.

The atom-ion collision experiments are conducted in a hybrid apparatus (for details see [13]) where a single $^{87}$Rb⁺ ion, trapped in a linear Paul trap, is brought in contact with an ultracold cloud of spin polarized $^{87}$Rb atoms ($F = 1, m_F = -1$). The atom cloud is previously prepared at a separate location from where it is transported to the Paul trap and loaded into a far off-resonant crossed optical dipole trap. The dipole trap is at first spatially separated from the trapped ion by about 50 μm. To start the atom-ion collision experiments it is then centered on the ion with μm precision within a few 100 ms. At this point the atom cloud consists of $N_{\text{at}} \approx 4 \times 10^4$ atoms at a temperature of $T_{\text{at}} \approx 1.2 \mu K$ and a peak density $n_{\text{at}} \approx 1.1 \times 10^{12}$ cm⁻³. At trapping frequencies of (190, 198, 55) Hz this results in a cigar shaped cloud with radial and axial extensions of about 10 μm and 35 μm, respectively.

The single Rb⁺ ion is confined in a Paul trap driven at a frequency of 4.17 MHz resulting in radial and axial trapping frequencies of 350 kHz and 72 kHz, respectively. As the trap is about 4 eV deep, the ion remains trapped on timescales of days and can typically be used for thousands of experimental cycles. It is initially produced by photoionization of an atom from a cold Rb cloud in the Paul trap [14]. Typical kinetic energies $E_{\text{ion}}$ of the ion after sympathetic cooling in the atom cloud are about a few mK-$k_B$ where $k_B$ is the Boltzmann factor. This energy scale is mainly set by two quantities: (1) The excess micromotion (eMM) [15] in the Paul trap whose main part we can control by compensating stray electric fields [14]. (2) Heating effects induced by the interplay of micromotion and elastic collisions [16-18].

As described in [19], an ion immersed in an ultracold atom cloud leads to atom loss by expelling atoms from the shallow optical trap ($\approx 10 \mu K \cdot k_B$ trap depth) via elastic collisions. The radio frequency (rf) driven micromotion is a constant source of energy which drives these loss-afflicting collisions. Figure [19] shows such a decay of an atom cloud at relatively low densities ($\approx 10^{11}$ cm⁻³) and relatively high ion energies ($\approx 35$ mK-$k_B$ [19]). Plotted is the number of remaining atoms after an atom-ion interaction time $\tau$. Each data point corresponds to a single measurement. Overall, the plot shows a relatively smooth decay of the atom cloud with a relative scatter of the atom number of less than 10%. This changes drastically when we carry out the experiments at low ion energies ($\approx 0.5$ mK-$k_B$ [19]) and larger densities ($\approx 10^{12}$ cm⁻³) (Fig [19]). Here, the scatter dramatically increases with $\tau$ and
is on the order of the number of lost atoms. In Fig. 1b, histograms of the data in Fig. 1b are shown. With increasing time $\tau$ the initial normal distribution becomes bimodal as a striking tail towards large atom numbers emerges. At the tips of the tails we find cases where even after interaction times of several seconds barely any atoms have been lost, a signature of missing atom-ion interaction. Apparently, sporadically the atom number over time can follow different paths. The tails we find cases where even after interaction times of several seconds barely any atoms have been lost, a signature of missing atom-ion interaction. We can reproduce the histograms of the data shown in (b). The vertical axis counts the number of incidents for a particular atom number $N_{at}$ and interaction time $\tau$.

In effect, it is a three-body recombination process involving the ion and two neutrals that ejects the ion from the cloud. If, for example, a ground state molecule is formed, binding energies on the order of 0.5 mK $k_B$ and $n_{at} \approx 10^{12}$ cm$^{-3}$. Three-body events ($E_2$, $E_3$) interrupt the atom loss until the atom is recooled and enters the sample at point $R_2$ (Traces $T_2$ and $T_3$). Right: Sketch of the resulting atom number distribution when averaging over many experimental runs. (c) Plot of the probability $P_{\text{threebody}}$ for initial atomic densities $(1.8, 1.1, 0.7, 0.3) \times 10^{12}$ cm$^{-3}$ and atom numbers $(6.5, 4.0, 2.8, 1.6) \times 10^4$, respectively. The solid lines are results of the numerical simulation.

Figure 1b illustrates in a simple picture how the decay of the atom number over time can follow different paths. The solid trace $T_1$ shows the case when only binary atom-ion collisions occur. Such traces result in the narrow peak of the atom number distribution sketched on the right of Fig. 2b. Traces $T_2$ and $T_3$ exhibit three-body collisions at points $E_2$ and $E_3$. At point $R_2$ the ion reenters the atom cloud after recooling. Rare three-body events and long interruption times $t_{\text{out}}$ result in a long tail of the distribution. We can reproduce the histograms in Fig. 1 with a simple Monte Carlo type simulation. We assume an initial normal distribution of the atom number which then decays exponentially with the binary atom-ion collision rate $K_2 n_{at}$. Here, $K_2 \approx 5 \times 10^{-9}$ cm$^3$/s is a rate constant given by the product of the elastic cross section and the ion velocity. A three-body event, occurring at a rate $K_3 n_{at}^2$, interrupts this decay for a period $t_{\text{out}}$. As the ion can only be recooled by the atomic sample, we assume the rate for reentry of the ion into the atom cloud to be proportional to the number of atoms $1/(t_{\text{out}}) = N_{at}/c_{\text{out}}$ with $c_{\text{out}}$ being a constant depending on the trap parameters. In order to fix the model parameters and rate constants it is convenient to carry out a data analysis as follows. We sum up the number of events in the tail of the distributions shown in Fig. 1 for each $\tau$ and divide by the total number of measurements to obtain the probability $P_{\text{threebody}}$ that at least one three-body process takes place within time...
These data are plotted as the filled black circles in Fig. 2 (data set with \( n_{\text{at}} \approx 1.1 \times 10^{12} \text{ cm}^{-3} \)). The corresponding errorbars mainly reflect the difficulty to unambiguously assign data points to the peak or the tail of the distribution where both parts of the bimodal distribution strongly overlap. Besides the data of Fig. 1, Fig. 2 also contains data at three additional atomic densities. All four data sets have in common that the number of three-body events first rapidly increases and subsequently levels off. The leveling off is due to the fact that the probability for a three-body reaction is strongly density-dependent. Closer inspection of the data sets reveals a peculiar feature. In the beginning of the interaction (\( \tau \lesssim 1 \text{ s} \)) only very few three-body events are detected for the lower density samples. We explain this delay by an initial phase of sympathetic cooling of the Rb\(^+\) ion which experiences significant heating during the preparation time of the atom cloud (~30 s). In fact, we observe ion heating specifically during evaporative cooling where the rf is ramped from 70 to 3 MHz. From numerical calculations we estimate that recooling times of about 1 s in atom clouds with \( n_{\text{at}} \approx 10^{12} \text{ cm}^{-3} \) correspond roughly to ion kinetic energies of a few 100 K. According to the calculations the ion will typically undergo several thousand binary collisions with cold atoms until it is sympathetically recooled to mK energies. We are able to describe all four data sets in Fig. 2, consistently with our simple Monte Carlo model (continuous lines). From independent fits to each data set we obtain nearly identical rate coefficients in the range \( K_3 \sim 3.1 - 3.5 \times 10^{-25} \text{ cm}^6/\text{s} \). For each fit the initial cooldown time is accounted for by adjusting the starting time of the simulation. We note that the value for our atom-atom-ion \( K_3 \) rate coefficient is more than three orders of magnitude larger than the three-body coefficient for three colliding neutral \(^{87}\text{Rb} \) atoms [2].

In order to challenge our analysis we have attempted to model the events that send the ion into orbit as two-body processes. The corresponding linear density dependence of the event rate yields much less consistent fit results. The two-body rate coefficients would differ by more than a factor of 3 when comparing the analysis of the data set for the lowest and the highest density. As a cautionary note, we point out that three-body recombination processes to weakly-bound molecular states with binding energies \( \lesssim 10 \text{ meV} \) are not detected in our experiments as the ion will not leave the atom cloud. Thus, the true three-body coefficient may even be significantly larger. From our analysis we also extract an approximate value for the interruption time coefficient \( c_{\text{out}} \approx 1.7 \times 10^5 \text{ s} \). For the typical atom numbers used here this results in several seconds of negligible atom-ion interaction following each ejection of the ion.

In a further experiment, we quantify the kinetic energy \( \Delta E_{\text{ion}} \) gained by the ion in a three-body event. The idea is to lower the depth of the ion trap such that an ion with an energy of a few 0.1 eV escapes while a cold ion remains trapped. The trap depth is reduced to one of 5 values \( U_{\text{red}} \) by lowering one of the endcap voltages of the Paul trap within 300 ms. The voltage is held at this value for 200 ms and ramped back up within 200 ms. The trap depths \( U_{\text{red}} \) are indicated in Fig. 3. They have been computed using methods detailed in [21] for both Rb\(^+\) (bottom abscissa scale) and Rb\(^2+\) (top). A negative trap depth value corresponds to non-trapping. After the trap depth reduction procedure is completed, the presence of the ion in the trap is probed via the loss it induces in a freshly prepared cloud of atoms. Plotted is the remaining atom number. Data points with \( N_{\text{at}} \lesssim 10^3 \) signal the presence of an ion, while data points with \( N_{\text{at}} \approx 4.5 \times 10^3 \) correspond to a lost ion. For better visibility, we have slightly offset in energy the black squares from the grey dots. (b) Ion loss probability \( P_{\text{loss}} \) calculated from the data in (a). The continuous lines are guides to the eye.

![FIG. 3. Measuring the ion energy after a three-body process (black squares) and after purely binary collisions (grey dots). The trap depth is reduced to \( U_{\text{red}} \). (a) If the ion "survives" this procedure in the trap it will subsequently induce atom loss in a freshly prepared cloud of atoms. Plotted is the remaining atom number. Data points with \( N_{\text{at}} \lesssim 10^3 \) signal the presence of an ion, while data points with \( N_{\text{at}} \approx 4.5 \times 10^3 \) correspond to a lost ion. For better visibility, we have slightly offset in energy the black squares from the grey dots. (b) Ion loss probability \( P_{\text{loss}} \) calculated from the data in (a). The continuous lines are guides to the eye.](image-url)
the gained energy $\Delta E_{\text{ion}} \approx 0.4 \text{ eV}$. We note that for trap depths $U_{\text{red}} \lesssim 0.25 \text{ eV}$ the probability of loss is high in general. This suggests that the stability of our trap is compromised at such shallow trapping potentials, limiting the accuracy with which we can determine the energy released in the three-body process. Still, we find a clear splitting between the black and grey data sets. Thus, a resolution of the measurement on the order of 0.1 eV seems plausible.

Mainly two recombination processes come into consideration. In a reaction of the type $\text{Rb} + \text{Rb} + \text{Rb} \rightarrow \text{Rb}_2 + \text{Rb}^+$ the formation of a neutral molecule is catalyzed by the ion which carries away 2/3 of the energy released. If deeply bound Rb$_2$ molecules are produced binding energies of up to $-0.5 \text{ eV}$ are released, in agreement with the measurement. A second possible recombination process, $\text{Rb} + \text{Rb} + \text{Rb}^+ \rightarrow \text{Rb}_2 + \text{Rb}$, produces a molecular ion and a neutral atom. However, as indicated in figure 3, the molecular ion, due to its higher mass, experiences a significantly shallower trap than the atomic ion and would immediately be lost for our parameter range. We thus infer that the ion at hand is Rb$^+$. However, we cannot completely exclude the formation of an intermediate molecular ionic state which may subsequently dissociate.

In a third type of measurement we study the dependence of the three-body coefficient on the ion kinetic energy which we can tune by controlling the ion micromotion. For this we apply a static electric field $\varepsilon$ perpendicular to the axis of the Paul trap and let the ion interact for $\tau = 8 \text{ s}$ with an atom cloud with $n_{\text{at}} \approx 1.0 \times 10^{12} \text{ cm}^{-3}$. We find $P_{\text{threebody}}$ to increase roughly by a factor of 5 when reducing $\varepsilon$ from 3.25 V/m to 0 V/m (Fig. 4b).

In order to express the electric field values in terms of kinetic energy we make use of the relation $E_{\text{EMM}} = c_{\text{trap}} \cdot \varepsilon^2 + E_{\text{res}}$ with $c_{\text{trap}}$ a constant that depends on the trap configuration and the ion mass $[15]$. $E_{\text{res}}$ stands for residual uncompensated micromotion energy, e.g. due to rf phase delay between the trap electrodes. The ion energy can be expressed as $E_{\text{ion}} = c_{\text{dyn}} \cdot E_{\text{EMM}}$ $[19]$. $c_{\text{dyn}}$ is a constant which depends on the atom-ion mass ratio and the spatial extension of the atom cloud and for our experiments can be estimated to be about 2 $[17]$. Since three-body coefficients often follow simple scaling laws, we attempt to describe our data with a power-law dependence of the form $K_3 \propto E_{\text{ion}}^{\alpha}$ within our simulation. We have taken care to also account for the energy dependence of the two-body interactions. Good agreement with the data is achieved for $\alpha = -0.43$, $E_{\text{res}} = 370 \mu \text{K} \cdot \text{Kb}$ and a maximal value for $K_3$ of $2.75 \times 10^{-25} \text{ cm}^6/\text{s}$ (solid trace in Fig. 4b). For comparison, curves for exponents $\alpha = -0.5$ and $\alpha = -0.33$ (dashed and dotted traces, respectively) are shown as well. A residual energy $E_{\text{res}} = 370 \mu \text{K} \cdot \text{Kb}$ is a reasonable value for our current setup and in agreement with other measurements of ours $[14]$.

In conclusion, we have studied three-body recombination involving a single trapped ion and two of its parent atoms at collision energies approaching the sub-mK regime. With a relatively simple model we can understand the two- and three-body collision dynamics and extract corresponding rate coefficients. We observe an increase of the three-body rate coefficient with decreasing collision energy, a behavior that can be expected to become crucial for future experiments targeting even lower temperatures. After a three-body event, ion energies on the order of 0.4 eV were measured, indicating that deeply bound molecules have been created. Since we have not observed Rb$^+_2$ ions, the formation of Rb$_2$ seems probable. The ion would then act as an atomic size catalyzer at mK temperature. It is an interesting question whether such catalyzing action could also be observable close to more massive objects such as carbon nanotubes $[22]$. Finally, as a byproduct of our investigations, we also observe sympathetic cooling of ions from energies in the 0.1 eV range back to mK temperatures.

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