Quarkonium Production at the Tevatron through Soft Colour Interactions

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Abstract

The direct charmonium and bottomonium production rate observed at high-$p_T$ in $p\bar{p}$ collisions at the Tevatron is factors of ten larger than predictions based on conventional perturbative QCD. We show that this excess can be accounted for by our model for soft colour interactions, previously introduced to describe in a novel way the large rapidity gap events observed at HERA.
Heavy quarkonia, i.e. bound states of heavy quark-antiquark pairs, are thought to provide a useful testing ground for perturbative Quantum Chromo Dynamics (pQCD). The reason being that the charm and bottom quark masses provide a large scale which makes the short distance behaviour calculable using a perturbative approach whereas the nonperturbative contributions can be factorised into a wavefunction. It was therefore a surprise that measurements by the CDF [1] and DØ [2] collaborations at the Fermilab Tevatron $p\bar{p}$ collider ($\sqrt{s} = 1.8$ TeV) gave cross-sections of direct high-$p_T$ $J/\psi, \psi'$ and $\Upsilon, \Upsilon'$ production far above the expectation from the colour singlet model [3] based on conventional pQCD. The observed excess is generally an order of magnitude and increases to a factor $\sim 50$ with increasing $p_T$.

In the colour singlet model pQCD is used to calculate the production of a $Q\bar{Q}$ pair in a colour singlet state. This forms a quarkonium state with the same angular momentum quantum numbers $^{2S+1}L_J$ by coupling to the non-perturbative wave function at the origin, which is obtained from the leptonic decay width. The striking failure of this model has led to several phenomenological investigations and some new models; for a review see [4]. The colour octet model, which is based on non-relativistic QCD, also takes into account the more abundant perturbative production of $Q\bar{Q}$ pairs in colour octet states. The unknown probability for the transformation into colour singlets due to non-perturbative processes is parametrised with matrix-elements that have to be fitted to data, but are universal so that the model can be tested by studying several different processes. Similarly, in the colour evaporation model [5] a certain fraction of all $Q\bar{Q}$ pairs, independently of their production process and quantum numbers, form a quarkonium state. Thus, both the colour octet model and the colour evaporation model requires fitting to experimental data. In contrast, our soft colour interaction (SCI) model [6] gives a prediction also of the absolute rate which, as will be shown in this Letter, is in good agreement with the Tevatron data.

The SCI model was introduced as a novel way to interprete the rapidity gap events observed in deep inelastic scattering (DIS) at HERA. The model does indeed describe the salient features of the ZEUS [7] and H1 [8] data. The conventional interpretation of these events is in terms of deep inelastic diffractive hard scattering [9] on partons in the pomeron, which is a colourless object exchanged from the quasi-elastically scattered proton. Although phenomenological models based on this idea work quite well to describe the data, there are theoretical problems with the pomeron approach. In particular, the factorisation into a pomeron flux, a pomeron parton density and a hard interaction described by a QCD matrix element may not be universal for all processes, e.g. DIS and hadron collisions. The pomeron-proton interaction is soft and thereby occurs on a long space-time scale. It may therefore be incorrect to consider the pomeron as decoupled from the proton during and after the hard scattering.

It is more natural to expect soft interactions with the proton both before and after the snapshot of the DIS probe. To investigate this line of thinking, we have developed a model [6] with a mechanism for soft colour interactions as an alternative to the approach based on the pomeron and Regge phenomenology.

The basic idea in our SCI model is that there may be additional soft interactions, not previously accounted for, at a scale below the cut-off $Q^2_0$ for perturbative QCD. Obviously, interactions do not disappear below this cut-off. The question is how to take them into account properly and whether conventional hadronization models give a complete descrip-
FIG. 1. Main pQCD processes for production of a $Q\bar{Q}$ pair in (a) leading order and (b) next-to-leading order.

We propose that the quarks and gluons produced by conventional pQCD processes, as described by matrix elements and parton showers, interact non-perturbatively with the colour medium of the proton remnant. This should be a natural part of the process in which ‘bare’ perturbative partons are ‘dressed’ into non-perturbative ones and the formation of the confining colour flux tube in between them. These soft interactions cannot change the momenta of the partons significantly, but they change their colour and thereby affect the colour structure of the event. This in turn will lead to a modified hadronic final state, e.g. with rapidity gaps or quarkonium.

Lacking a proper understanding of non-perturbative QCD processes, we have constructed a model \cite{6} to describe and simulate such soft colour interactions within conventional Monte Carlo (MC) event generators. All partons from the hard interaction plus the remaining partons in the proton remnant are assigned appropriate colour and anticolour charges. Partons from the hard interaction can make a soft interaction with partons in the proton remnant exchanging their colours but not changing their momenta, which may be viewed as soft non-perturbative gluon exchange. Similarly, partons in the proton remnant can exchange colour whereas no direct colour exchanges are allowed between the perturbative partons. Since the process is non-perturbative the exchange probability for a pair cannot be calculated from first principles and is instead described by a phenomenological parameter $R$. The number of soft exchanges will vary event-by-event and change the colour topology. In the Lund string model \cite{10} this corresponds to a modified string stretching that alters the outcome of the hadronization.

The SCI model was first implemented in LEPTO \cite{11} simulating DIS. Here, the main effect producing rapidity gap events at HERA is SCI between the partons from the hard scattering and those in the proton remnant. In particular, with gluon initiated processes at small Bjorken-$x$, the colour octet charge of the produced hard parton system ($q\bar{q}$ plus possible additionally emitted partons) can turn into a colour singlet. This may give a hadronic system $X$ separated in rapidity from a very forward moving proton remnant system of small mass (e.g. a proton or a resonance). The main features of diffractive scattering emerges naturally and the HERA rapidity gap events can be surprisingly well described by this simple model \cite{6}.

This SCI model can be straightforwardly applied to describe heavy quarkonium production in $p\bar{p}$; a colour octet $Q\bar{Q}$ pair from pQCD can be turned into a singlet and thereby form an onium state, provided that the mass is appropriate. In leading order (LO) pQCD heavy
quark production occurs through $gg \to Q\bar{Q}$ (Fig. 1a) and $q\bar{q} \to Q\bar{Q}$. However, higher order processes involving gluon splitting $g \to Q\bar{Q}$ are important. For example, the next-to-leading order (NLO) process $gg \to gQ\bar{Q}$ illustrated in Fig. 1b gives a large contribution because it is an $\alpha_s$ correction to the large cross-section for gluon scattering ($gg \to gg$). Matrix elements with explicit heavy quark masses are available up to NLO. However, since the virtuality of the gluon need not be very large to split, in particular to $c\bar{c}$, still higher orders may be important at Tevatron energies. These can be taken into account approximately through the parton shower approach.

The LO and parton shower production of $Q\bar{Q}$ pairs are available in the MC generator Pythia [12]. On the generated parton level events we apply the above SCI mechanism which will turn some $Q\bar{Q}$ pairs into colour singlets. A quarkonium state is then produced if the invariant mass $m_{Q\bar{Q}}$ is below threshold for open heavy flavour production ($2m_M$). Thus, the cross-section is

$$\sigma_{onium} = \int_{2m_{Q\bar{Q}}}^{2m_M} \frac{d\sigma^1}{dm_{Q\bar{Q}}} dm_{Q\bar{Q}}$$  \hspace{1cm} (1)$$

where the singlet $Q\bar{Q}$ cross-section $d\sigma^1 = d\sigma \otimes \text{SCI}$ is obtained from the application of the SCI model on Pythia events. This is not just a constant fraction of the original $Q\bar{Q}$ cross-section, but depends somewhat on the partonic state and the possible string configurations. Whereas the number of possible string configurations increases with parton multiplicity, the number of string configurations giving a singlet $Q\bar{Q}$ pair is more or less constant. Therefore, the relative probability for a singlet $Q\bar{Q}$ decreases slowly with parton multiplicity. This in turn, implies a slight decrease ($\sim 10\%$ in the observed $p_\perp$-range) of the singlet $Q\bar{Q}$ fraction with increasing $p_\perp$ in the hard scattering process which causes more abundant parton showering.

The invariant mass of the $Q\bar{Q}$ pair is in principle given by the pQCD process. However, we expect this mass to be smeared by the soft colour interactions involving energy-momentum transfers of the order a few hundred MeV. Irrespective of the original $Q\bar{Q}$ mass (below $2m_M$), we therefore divide the quarkonium cross-section onto the different quarkonium states based simply on spin-statistics as suggested by [5]. This should be a good approximation since the heavy quark system is nearly non-relativistic. The cross-section for a given quarkonium state $X$ with total angular momentum $J_X$ is then given by

$$\sigma_X = \frac{\Gamma_X}{\sum_Y \Gamma_Y} \sigma_{onium}$$  \hspace{1cm} (2)$$

where $\Gamma_X = (2J_X + 1)/n_X$ corresponds to a partial width. Here, we have included a suppression of radially excited states, i.e. with the main quantum number $n_X$. This reproduces approximately the differences between different $\psi$ and $\Upsilon$ states regarding their leptonic width and thus the wave function at the origin [13], which should be particularly relevant when the essentially pointlike $Q\bar{Q}$ pair forms an onium state.

The results of this model are shown in Fig. 2 and Table I together with the Tevatron data. The agreement is remarkably good, considering the simplicity of the SCI model and the fact that it was originally constructed for a different physics issue. As mentioned, the absolute normalization is not adjusted to data, but given by the model. The only parameter
in the SCI model, i.e. the probability \( R \) of a colour exchange between two partons, is kept at the value \( R = 0.5 \) chosen to reproduce the rate of rapidity gap events in DIS at HERA. However, as for the rapidity gap rate, the dependence of the onium rate on this parameter is quite small. For example, changing to \( R = 0.1 \) only decreases the cross-section with \( \sim 30 \% \).

There is however a strong dependence on the heavy quark mass \( m_Q \). We have used \( m_c = 1.35 \) GeV and \( m_b = 4.8 \) GeV. Increasing the quark masses by 0.25 GeV decreases the cross-section with a factor 3, whereas a decrease of the quark masses by the same amount increases the cross-section with a factor 2. This is as usual in pQCD heavy quark production close to threshold and can be understood from Eq. (1).

The cross-section also depends somewhat on other features of the Monte Carlo model like the QCD \( \Lambda \) parameter, details in the parton shower model and the choice of parton density parametrizations. These issues are not particular for the SCI model, but of a general character. We therefore do not adjust any of these features, but leave them as they are by default in the PYTHIA MC model which provides a standard for many processes and observables. We note that there are no significant changes in our results when varying the virtuality scale for the parton shower or using different available parton density parametrizations (e.g. MRS or CTEQ) based on recent data. However, including the multiple parton-parton interactions in PYTHIA lowers the total onium cross-section slightly (\( \sim 20 \% \)).

The observed \( p_T \) spectra of the different onium states are also quite well reproduced by the model, as demonstrated in Fig. 2. The contribution from the LO process (shown separately as dashed curves) have a steeper \( p_T \) dependence and only contributes significantly at lower \( p_T \), in particular for \( \psi, \psi' \). Thus, the higher order contributions are most important.

Comparing model and data in detail, there is a tendency for the model to have a slightly flatter \( p_T \) distribution for the \( J/\psi \) production. This may be an effect of using the approximate parton shower gluon splitting \( g \to c\bar{c} \) instead of the NLO matrix element which might be more appropriate at large \( p_T \). It may also be influenced by the detailed contribution of different onium states, since \( J/\psi \) from decays contribute more at smaller \( p_T \).

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The relative rates of \( J/\psi \) from direct production and from decays of higher onium states are given in Table I together with some ratios of cross-sections for different onium states. The model gives good agreement with data in most cases. This shows that simple spin statistics can describe the main effects. The only deviation of some significance is the ratio \( \sigma(\Upsilon(2S))/\sigma(\Upsilon(1S)) \), where the simple suppression of radially excited states seems too strong.

The SCI model provides a mechanism for how a colour octet \( Q\bar{Q} \) pair is turned into a singlet and thereby an absolute normalization of the cross-section for the quarkonium production. In addition, one obtains a direct relation to other manifestations of soft interactions, such as diffraction and rapidity gaps. In the colour octet model the probability to form a singlet is parametrized into matrix elements, but no explicit mechanism for how an octet is turned into a singlet is given.

These models are in clear contrast to the colour singlet model for quarkonium production which cannot explain the large rate observed at the Tevatron. In addition, they differ in the fragmentation function of \( J/\psi \), i.e. \( D_{g\to J/\psi}(z,\mu) \) where \( z \) is the momentum fraction of the \( J/\psi \) relative to the ‘mother’ gluon and \( \mu \) is the factorisation scale. In the colour singlet model the fragmentation function is relatively flat [13], whereas in the colour octet model it is essentially a \( \delta \)-function at \( z = 1 \) [13].

The fragmentation function can be measured by taking the ratio of the transverse mo-
FIG. 2. Transverse momentum spectra of prompt charmonium $J/\psi$, $\psi'$ and bottomonium $\Upsilon$, $\Upsilon'$ in $p\bar{p}$ collisions at the Tevatron energy. Data from CDF [1] (filled symbols) and DØ [2] (open symbols) compared to results from the soft colour interaction (SCI) model applied to $c\bar{c}/b\bar{b}$ production from leading order ($\alpha_s^2$) matrix elements (dashed lines) and with the inclusion of higher order contributions calculated in the parton shower approach (full lines). Production central in pseudorapidity (a) $|\eta| < 0.6$, (b) $|y| < 0.4$ and forward (c) $2.5 < |\eta| < 3.7$ (where an assumed 20% systematic error has been added in quadrature).
TABLE I. Relative rates in % for different onium states in the Monte Carlo model and the Tevatron data [1]. The charmonium cross-sections are in general for $p_{\perp} \geq 5\,\text{GeV}$ and $|\eta| < 0.6$ whereas the bottomonium cross-sections are for $|y| < 0.4$.

|                          | MC model | Data   |
|--------------------------|----------|--------|
| $J/\psi$ direct          | 61       | 64 ± 6 |
| $J/\psi$ from $\chi_c$   | 26       | 30 ± 6 |
| $J/\psi$ from $\psi'$    | 13       | 7 ± 2 ↔ 15 ± 5 |
| $\sigma(\chi_c^2)/\left(\sigma(\chi_c^1) + \sigma(\chi_c^2)\right)$ | 62   | 47 ± 9 |
| $\sigma(\psi'')/\sigma(J/\psi)$ | 32 | 25 ± 6 |
| $\sigma(\Upsilon(2S))/\sigma(\Upsilon(1S))$ | 29 | 46 ± 9 |

† Data are for $p_{\perp} \geq 4\,\text{GeV}$.
‡ Lower (upper) value for $p_{\perp} \sim 5\,\text{(18)}\,\text{GeV}$.
§ Assuming the same fraction of $J/\psi$ and $\psi'$ from $b$ hadron decays.

momentum of the $J/\psi$ and the total transverse momentum in a cone centered at the $J/\psi$ [10]. Following conventional jet algorithms for high energy hadronic collisions, one may choose a cone $\Delta R = \sqrt{\Delta \phi^2 + \Delta \eta^2} \approx 0.7$ in pseudorapidity and azimuthal angle. Applying this to our SCI model results in a fragmentation function for $J/\psi$’s with $p_{\perp} > 5\,\text{GeV}$ which is strongly peaked at $z = 1$. Although its exact form depends on details in the model, it is essentially as expected in the colour octet model and very different from the colour singlet model.

In summary, we have shown that the large rate of direct high-$p_{\perp}$ charmonium and bottomonium in high energy $p\bar{p}$ collisions can be quite well described the Soft Colour Interaction model. The same SCI model also accounts for the rapidity gap events observed at HERA. This indicates that these features of non-perturbative strong interactions are quite general and can be described by a universal model.
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