Production and absorption of exotic bottomonium-like states in high energy heavy ion collisions

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We investigate the production and absorption of $Z_b (10610)$ and $Z_b' (10650)$ states in a hadronic medium, via the processes $\bar{B}^* (B^*) \rightarrow \pi Z_b^{1/2}$ and the corresponding inverse reactions. We use effective field Lagrangians based on an SU(4)-extension of the hidden gauge formalism to account for the couplings between light and heavy mesons, and a phenomenological Lagrangian involving the $B^* B^{*1/2} Z_b^{1/2}$ vertices. The absorption cross sections are found to be much larger than the production ones.

I. INTRODUCTION

In recent years we have witnessed the discovery of many new states, indicating that the heavy-hadron spectrum is much richer than expected in conventional constituent quark models. The benchmark in this new era of spectroscopy was the discovery of the state $X(3872)$ in 2003 by the Belle Collaboration \cite{Belle}. Since then, more than twenty candidates of exotic hadron states have been observed by several collaborations. For a review, see references \cite{review1,review2,review3}.

Among these many states, we find two charged bottomonium-like resonances, $Z_b\bar{b}$ (10610) and $Z_b\bar{b}'$ (10650) (denoted hereafter as $Z_b^\pm$ and $Z_b'^\pm$), observed in the processes $\Upsilon (5S) \rightarrow \Upsilon (nS) \pi^\pm (n = 1, 2, 3)$ and $\Upsilon (5S) \rightarrow \pi^\pm h (mS) (m = 1, 2)$ \cite{Belle,Belle2}. The reported masses and decay widths averaged over the mentioned channels are $m_{Z_b^\pm} = 10607.2 \pm 2.0$ MeV, $\Gamma_{Z_b^\pm} = 18.4 \pm 2.4$ MeV and $m_{Z_b'^\pm} = 10652.2 \pm 1.5$ MeV, $\Gamma_{Z_b'^\pm} = 11.5 \pm 2.2$ MeV. Due to their charged nature and favored quantum numbers ($J^P = 1^+ (1^+)$), they cannot be pure $b\bar{b}$ states and must contain at least four quarks. Another relevant property is that, similarly to other exotic states, they are close to thresholds of heavy-meson bound states: $Z_b$ and $Z_b'$ are near $BB^*$ and $B^* B^*$ thresholds, respectively. Thus, a natural interpretation extensively used is to suppose that they are $S$-wave deuteron-like states of bottomed mesons \cite{deuteron}. Accordingly, we assume here that the components of $Z_b$ and $Z_b'$ are $S$-wave molecular states of $\frac{1}{\sqrt{2}}(BB^* - B^* B)(3S_1)$ and $B^* B^{*1/2}(3S_1)$, respectively \cite{deuteron,deuteron2}.

Although plausible, the meson molecule interpretation of these exotic bottomonium states is not yet firmly established. It can be argued that, due to the larger masses, these multiquark states should be more compact and a tetraquark configuration, i.e. two quarks and two antiquarks in a compact “bag”, should be favored.

In order to arrive at a consistent picture of these states, we must take advantage of all the experimental information already existent and still to be obtained. We have already data on the $Z_b$ and $Z_b'$ masses and decay widths coming from $e^+ e^-$ collisions. More information can be obtained from the hadron colliders, in particular from the production cross section measured in proton-proton, proton-nucleus and nucleus-nucleus collisions. In the case of the much more investigated $X(3872)$, the attempt to explain the measured production cross section in proton-proton collisions led to the conclusion that it is very difficult to understand this state as a meson molecule. According to the calculations presented in \cite{X3872}, the $X$ can be better understood as a mixture with both a molecular and a $c\bar{c}$ component. It will be interesting to see if the same conclusion holds for the $Z_b$ and $Z_b'$.

The experimental study of $X(3872)$ production in hadron colliders (already started \cite{X3872}) and in heavy ion collisions (HICs) will complement the accumulated information and help in discriminating between different pictures of the state. The same can be said about the $Z_b$ and $Z_b'$ states discussed above. The advantage of working with heavy ions is that we have a much higher production rate of heavy quarks. Moreover in HICs there is a quark gluon plasma (QGP) phase, where the quarks can move freely and form more easily multiquark states, specially in the hadronization transition. The disadvantage is that it is more difficult to identify these states experimentally, in the middle of an extremely large number of produced particles. Another disadvantage is that in HICs there are a number of effects and possibilities which have to be considered, for which the theoretical treatment is still incomplete. In this work we concentrate on one of such aspects: the interaction of these multiquark states (more specifically of the $Z_b$ and $Z_b'$) with the light particles forming the hot hadronic medium which is produced after the cooling and hadronization of the QGP. We will follow closely and extend the previous works on the subject, where the interactions of the $X(3872)$ were addressed \cite{X3872}.

After being produced at the end of the quark gluon plasma phase, the $Z_b$ and $Z_b'$ interact with other hadrons during the expansion of the hadronic matter. Therefore, they can be destroyed in collisions with the comoving
light mesons, but they can also be produced through the inverse reactions \[27, 34\]. Since the cross sections depend on the spatial configuration of these states, the strength of these interactions depends ultimately on the internal structure of the \(Z_b\) and \(Z'_b\) and the measurement of their multiplicity would be very useful to determine their structure.

Inspired by evaluations of the \(X(3872)\) abundance mentioned above, in this work we study the interactions between \(Z_b\) and \(Z'_b\) and light hadrons. More precisely, we consider the production of \(Z_b\) and \(Z'_b\) through the processes \(BB \to \pi Z_b^{(i)}\), \(B^*B \to \pi Z_b^{(i)}\), and \(B^*B^* \to \pi Z_b^{(i)}\) and absorption of these exotic states through the inverse processes \(\pi Z_b^{(i)} \to \bar{B}B\), \(\pi Z_b^{(i)} \to \bar{B}^*B\) and \(\pi Z_b^{(i)} \to \bar{B}^*B^*\). We obtain the amplitudes and cross sections related to these processes for \(Z_b^{(i)+}\) within the framework of \(SU(4)\) effective Lagrangians \[22, 27\]. Also, following Refs. \[13, 21, 24\], we assume that the \(Z'_b\) couples to the components \((B^0B^* + B^*B^*)\), while the \(Z_b^{(i)+}\) only couples to \((B^0B^*)\).

The paper is organized as follows. In Section II we describe the formalism, and determine the production and absorption amplitudes and cross sections. Then, in Section III we present and discuss our results. Finally, in Section IV we draw the concluding remarks.

II. FORMALISM

The analysis of the processes involving the \(Z_b^{(i)}\) production and absorption will be done in the effective field theory approach. Accordingly, the Lagrangians carrying the couplings between light- and heavy-meson fields are built within the framework of an \(SU(4)\)-extension of the hidden gauge formalism: it consists of an effective theory in which the vector mesons are identified as the dynamical gauge bosons of the hidden \(U(3)^V\) local symmetry in the \(U(3)_L \times U(3)_R/U(3)^V\) non-linear sigma model \[27, 33, 34\]. The Lagrangians are given by

\[
\mathcal{L}_{PPV} = -ig_{PPV}(V^\mu [P, \partial_\mu P]),
\]

\[
\mathcal{L}_{VVVP} = \frac{g_{VVVP}}{\sqrt{2}} \epsilon^{\mu \nu \rho \sigma} \langle \partial_\mu V_\nu, \partial_\rho V_\sigma P \rangle,
\]

where \(PPV\) and \(VVVP\) denote pseudoscalar-pseudoscalar-vector and vector- vector-pseudoscalar vertices, respectively; the symbol \(\langle \ldots \rangle\) stands for the trace over \(SU(4)\)-matrices; \(V_\mu\) represents a \(SU(4)\) matrix, which is parametrized by 16 vector-meson fields including the 15-plet and singlet of \(SU(4)\),

\[
V_\mu = \begin{pmatrix}
\omega \rho^0 + \frac{\rho^0}{\sqrt{2}} & \rho^+ & K^{0+} & B^{0*} \\
\rho^- & \rho^- \frac{\rho^0}{\sqrt{2}} & K^{00} & B^{*+} \\
K^{*(0)} & K^{*(0)} \phi & B^{**} & B^*_s + Y \\
B^0 & B^+ & B^{*+} & \eta_s
\end{pmatrix}.
\]

\(P\) is a matrix containing the 15-plet of the pseudoscalar meson fields, written in the physical basis in which \(\eta, \eta'\) mixing is taken into account,

\[
P = \begin{pmatrix}
\frac{\eta}{\sqrt{3}} + \frac{\eta'}{\sqrt{2}} & \frac{\pi^0}{\sqrt{2}} & \frac{\pi^+}{\sqrt{2}} & K^+ & B^0 \\
\frac{\eta}{\sqrt{3}} - \frac{\eta'}{\sqrt{2}} & K^0 & K^0 & B^- \\
-\frac{\eta}{\sqrt{3}} + \sqrt{\frac{2}{3}} \eta' & \sqrt{\frac{2}{3}} \eta' & \phi & B^*_s + Y \\
\end{pmatrix}.
\]

The coupling constants \(g_{PPV}\) and \(g_{VVVP}\) in Eq. (1) are related to pseudoscalar-pseudoscalar-vector and vector-pseudoscalar vertices, respectively, and are given by \[27\],

\[
g_{PPV} = \frac{m_V}{2f_\pi}, \quad g_{VVVP} = \frac{3m_V^2}{16\pi^2 f_\pi^3}
\]

with \(m_V\) being the mass of the vector meson, which we take as the mass of the \(\rho\) meson, and \(f_\pi\) the pion decay constant. The coupling \(g_{PPV}\) is the strong coupling of the \(B^0\) meson to \(B\). Noticing that the decay \(B^* \to B\) is kinematically forbidden, it is not possible to determine \(g_{PPV}\) from experiments. We then use the experimental information from the charm sector and from heavy quark symmetry \[27\], which engenders an effective \(g_{PPV}\) for the vertices involving \(B\) and \(B^*\) mesons as

\[
g_{PPV} = \frac{m_V}{2f_\pi} m_{B^*}.
\]

The \(m_{B^*}/m_{K^*}\) factor present in the above coupling has its origin in the heavy quark symmetry (as in Ref. \[27\]), with which the \(D^* \to D\) width is correctly reproduced. It must be added that our \(PPV\) coupling also coincides with the value used in Ref. \[20\] where the same is determined using the heavy quark symmetry. Further, the same \(PPV\) coupling has been used in Ref. \[40\] where \(\rho - B\) and \(\rho - B^*\) interactions are studied. A comparison of the \(PPV\) coupling in Ref. \[40\] with the value obtained in Ref. \[11\] within a lattice simulation shows that the two values are compatible. It is also worth to mention that our \(VVVP\) coupling is also comparable with the value obtained within the heavy quark symmetry in Ref. \[20\]. This is so because we only make use of one aspect of \(SU(4)\), which is the connection between the different coupling constants. As shown in Ref. \[12\], without using any equality of masses for the light and \(c\) quarks, for the case of the charm sector (where one could think that \(SU(4)\) would give meaningless coupling constants) wherever the connection between couplings can be tested or compared with other approaches, the corresponding \(SU(4)\) relations give very similar results.

Next, we can introduce the couplings of the \(Z_b^{(i)}\) to \(B^{(i)}\)-meson fields. We emphasize that in the present approach we treat \(Z_b^{(i)}\) as an elementary degree of freedom, with quantum numbers \(J^P = 1^+\). Also, following Refs. \[3, 19, 24\], we assume that \(Z_b^+ (10610)\) couples to the components \((B^0B^* + B^*B^0)\), while \(Z_b^0 (10650)\) couples only to the channel \((B^*B^0)\). Then, the phenomenolog-
The Lagrangians involving the \(Z_b^{(i)}B^*B^{(\ast)}\) vertices are

\[
\mathcal{L}_{ZBB^*} = g_{ZBB^*}(BZ_{\mu}B_{\mu}^* + B^*_{\mu}Z_{\mu}B^*),
\]

\[
\mathcal{L}_{Z^*BB^*} = ig_{Z^*BB^*}\epsilon^\alpha\beta\gamma\delta B_{\alpha}\partial_\beta Z_{\gamma}B^*_{\delta},
\]

where \(g_{ZBB^*}\) and \(g_{Z^*BB^*}\) are the coupling constants of the \(ZBB^*\) and \(Z^*BB^*\) vertices, respectively; \(B = B^-\), \(B^\ast_{\mu} = B^\ast_{\mu} - \) and \(Z_{\mu}^{(i)} = Z_{\mu}^{(i)}\) and the greek letters indicate Lorentz indices.

Now we can determine the transition amplitudes for the processes \(B\bar{B} \rightarrow \pi Z_b^{(\ast)}\), \(B^*\bar{B} \rightarrow \pi Z_b^{(\ast)}\) and \(B^*B^* \rightarrow \pi Z_b^{(\ast)}\), by using the Lagrangians in Eqs. (1) and (5). In Figs. 1 and 2 we show the diagrams associated to the mentioned processes at leading order, with the specification of the charges of the incoming bottomed mesons and of the particles in the final state, keeping in mind that the diagrams in Figs. 1 and 2 are related to the processes involving \(Z_b^{(i)}\) production, while diagrams in Figs. 4 and 5 to the \(Z_b^{(i)}\).

The amplitudes associated to the \(t\)-channel diagrams shown in Figs. 1 and 2 for the \(B\bar{B}, B^*\bar{B}, B^*B^* \rightarrow \pi Z_b\) processes are, respectively,

\[
\mathcal{T}_1^{(Q_1,Q_2)} = T_1^{(Q_1,Q_2)} g_{PV}\mathcal{L}_{ZBB^*} \frac{1}{t - m_B^2}
\times \left[(p_1 + p_3)_\mu + \frac{m_B^2 - m_{Z}^2}{m_{Z}^2} p_2\mu\right] \epsilon_{Z}^\mu(p_4);
\]

\[
\mathcal{T}_2^{(Q_1,Q_2)} = T_2^{(Q_1,Q_2)} g_{PV}\mathcal{L}_{Z^*BB^*} \frac{1}{t - m_B^2}
\times \epsilon^{\mu\nu\alpha\beta} p_{1\mu}p_{3\alpha}e_B\cdot \nu(p_1) \epsilon_{Z}^\beta(p_4);
\]

\[
\mathcal{T}_3^{(Q_1,Q_2)} = T_3^{(Q_1,Q_2)} g_{PV}\mathcal{L}_{Z^*BB^*} \frac{1}{t - m_B^2}
\times p_{3\mu} \epsilon_{B^*}(p_1) \epsilon_{B^*}(p_2) \epsilon_{Z}^\mu(p_4);
\]

while the amplitudes associated to the \(u\)-channel diag-
grams shown in Figs. 1 and 4 are, respectively,
\[
\mathcal{U}_{1}(Q^{11},Q^{21}) = U_{1}(Q^{11},Q^{21}) g_{PPV} g_{ZBB} \frac{1}{u - m_B^2} \times \left[ (p_2 + p_3) \epsilon + \frac{m_B^2 - m_\pi^2}{m_B^2} p_1 \right] \epsilon^*_Z (p_4);
\]
\[
\mathcal{U}_{3}(Q^{11},Q^{21}) = U_{3}(Q^{11},Q^{21}) g_{PPV} g_{ZBB} \frac{1}{u - m_B^2} \times p_3 \epsilon'_{B_2}(p_2) \epsilon'_{B_1}(p_1) \epsilon'_{Z_2}(p_4).
\]

The quantities \(T_{5}(Q^{11},Q^{21})\) and \(U_{r}(Q^{11},Q^{21})\) appearing in Eqs. (6) and (7) are isospin coefficients of the scattering amplitudes for \(t\) and \(u\)-channels, respectively, and are defined in Table I (\(Q^{11},Q^{21}\) denotes the charges of particles in the initial state; \(p_1, p_2, p_3, p_4\) represent the momentum of the particles in the initial (final) states; \(m_B, m_{B'}, m_{B''}, m_{\pi}\) and \(m_{\pi}\) are average masses of the \(B, B', B''\) and \(\pi\) mesons; \(\epsilon_B(p_1)\) and \(\epsilon_{Z_2}(p_4)\) are the polarization vectors of \(B\) mesons and \(Z_b\) states, respectively.

In the case of \(Z_b^+\) production, we note that there is no diagram contributing to \(\bar{B} B \rightarrow \pi Z_b^+\) reaction, since there is no \(B B' Z_b^+\) vertex. Thus, the amplitudes related to the \(t\)-channel diagrams shown in Fig. 5 for the \(\bar{B} B' \rightarrow \pi Z_b^+\) process are,
\[
T_{5}(Q^{11},Q^{21}) = T_{5}(Q^{11},Q^{21}) g_{PPV} g_{ZBB} \frac{1}{t - m_B^2} \times \epsilon^{\mu \nu \alpha \beta} \epsilon^\alpha_{Z_2} p_1 \epsilon^\beta_{Z_2} \epsilon^\mu_{Z_2} \epsilon^\nu_{Z_2} (p_4);
\]
while the amplitudes for the \(u\)-channel diagrams in Figs. 4 and 5 associated to the \(\bar{B} B' B'' \rightarrow \pi Z_b^+\) processes are, respectively,
\[
U_{4}(Q^{11},Q^{21}) = U_{4}(Q^{11},Q^{21}) g_{PPV} g_{ZBB} \frac{1}{u - m_B^2} \times \epsilon^{\mu \nu \alpha \beta} \epsilon^\alpha_{Z_2} p_4 \left[ (p_2 + p_3)_\alpha + \frac{m_B^2 - m_\pi^2}{m_B^2} p_{1\alpha} \right] \times \epsilon_{B'}(p_1) \epsilon_{Z_2} (p_4);
\]
\[
U_{5}(Q^{11},Q^{21}) = T_{5}(Q^{11},Q^{21}) g_{PPV} g_{ZBB} \frac{1}{u - m_B^2} \times \epsilon^{\mu \nu \alpha \beta} \epsilon^\alpha_{Z_2} p_2 \epsilon_{Z_2} (p_4) \times \epsilon_{B'}(p_1) \epsilon_{Z_2} (p_4) \epsilon_{Z_2} (p_4).
\]

Again, the isospin coefficients \(T_{5}(Q^{11},Q^{21}), U_{4}(Q^{11},Q^{21})\) and \(U_{5}(Q^{11},Q^{21})\) are defined in Table I.

The scattering amplitudes associated with the inverse processes \(\pi Z_b^{(i)+} \rightarrow \bar{B} B, B' B, B'' B'\) and \(\pi Z_b^{(i)+} \rightarrow B' B, B'' B\) can be determined as above, by using the correspondence \(p_1 \leftrightarrow p_3\) and \(p_2 \leftrightarrow p_4\). At this point we are able to determine the isospin-spin-averaged cross section for the processes \(\bar{B} B, \bar{B} B', \bar{B} B'' \rightarrow \pi Z_b^{(i)+}\), which in the center of mass (CM) frame is defined as
\[
\sigma_r(s) = \frac{1}{64\pi^2 s} \frac{|\vec{p}_f|}{|\vec{p}_i|} \int dQ \sum_{S,I} |M_r(s, \theta)|^2,
\]
where \(r = 1, 2, 3\) label processes associated with \(Z_b^+\) production, and \(r = 4, 5\) to \(Z_b^+\) production, as in the notation introduced above; \(\sqrt{s}\) is the CM energy; \(|\vec{p}_i|\) and \(|\vec{p}_f|\) denote the tri-momenta of initial and final particles in the CM frame, respectively; \(\sum_{S,I}\) represents the sum over the spins and isospins of the particles in the initial and final state, weighted by the isospin and spin degeneracy factors of the two particles forming the initial state for the reaction \(r\), i.e. [27]
\[
\sum_{S,I} |M_r|^2 = \frac{1}{(2S_{1r} + 1)(2S_{2r} + 1)} \sum_{S,I} |M_r|^2,
\]
where
\[
\sum_{S,I} |M_r|^2 = \sum_{Q_1, Q_2} \sum_S |M(Q_1, Q_2)|^2.
\]
Notice that the charges of the two particles forming the initial state for the processes in Figs. 1 and 3 can be combined, giving a total charge \(Q_r = Q_{11} + Q_{21} = 0, +1\). We
have then three possibilities: (0, 0), (−, +) and (0, +), yielding
\[ \sum_{s,t} |M_{s,t}|^2 = \sum_s \left( |M_{s}^{(0,0)}|^2 + |M_{s}^{(0,+)}|^2 + |M_{s}^{(0,-)}|^2 \right). \]

(13)

Each amplitude \( M_{s}^{(Q_1,Q_2)} \) in Eq. (12) can be written, in general, as
\[ M_{s}^{(Q_1,Q_2)} = T_{s}^{(Q_1,Q_2)} + U_{s}^{(Q_1,Q_2)}, \]
where \( T_{s}^{(Q_1,Q_2)} \) and \( U_{s}^{(Q_1,Q_2)} \) are the t- and u-channel amplitudes given in Eqs. (9-10).

III. RESULTS

In this Section we analyze the \( Z_{b}^{(t^+)} \)-production cross sections as a function of CM energy \( \sqrt{s} \). The values of physical quantities and coupling constants used here are \( \bar{B} \): \( m_{\bar{B}} = 137.3 \) MeV; \( m_{B} = 5279.4 \) MeV; \( m_{B^*} = 5324.8 \) MeV; \( m_{Z} = 10607.2 \) MeV; \( m_{Z^*} = 10652.2 \) MeV; \( m_{\pi} \equiv m_{\rho} = 775 \) MeV; and \( f_{\pi} = 93 \) MeV. As for the \( g_{ZBB^*} \) and \( g_{Z^{*}B^{*}B} \) coupling constants introduced in Eq. (5), the values considered here are those obtained in Ref. [21] (in accordance with the ones used in Ref. [20]):
\[ g_{ZBB^*} = 13.10^{\pm0.83} \text{ GeV}, \]
\[ g_{Z^{*}B^*B} = 1.04^{+0.1}_{-0.1}. \]

To take into account the uncertainties of these couplings, the results discussed below will be represented by shaded regions in the plots.

In Fig. 6 the \( Z_{b}^{t^+} \)-production cross sections are plotted as a function of the CM energy \( \sqrt{s} \). We see that the cross sections are \( \sim 3 \times 10^{-3} - 5 \times 10^{-2} \) mb for \( 10.80 \leq \sqrt{s} \leq 11.05 \) GeV. From the figure we can see that the biggest contribution to the \( Z_{b}^{t^+} \)-production comes from the reaction with \( \bar{B}B \) in the initial state. The \( \bar{B}B \rightarrow \pi Z_{b} \) cross section is bigger than the others by a factor about 2-3.

The \( Z_{b}^{t^+} \)-production cross sections are plotted in Fig. 7 as a function of the CM energy \( \sqrt{s} \). Remembering that in this case there is no reaction with initial \( \bar{B}B \) state at leading order, the two relevant processes have cross sections found to be \( \sim 6 \times 10^{-4} - 2 \times 10^{-2} \) mb for \( 10.82 \leq \sqrt{s} \leq 11.05 \) GeV, but with the reaction with initial \( B^{*}B^{*} \) state having the largest cross section by a factor about 2-3.

For completeness, the cross sections related to the inverse processes can be also analyzed. In Fig. 8 the \( Z_{b}^{t^+} \) absorption cross sections are plotted as a function of the CM energy \( \sqrt{s} \). They are found to be \( \sim 8 \times 10^{-2} - 6 \times 10^{-1} \) mb for \( 10.80 \leq \sqrt{s} \leq 11.05 \) GeV. As can be seen, the reaction with the final \( B^{*}B^{*} \) state has cross section larger by a factor about 3-4 with respect to other reactions.

Also, another relevant point is the comparison among the \( Z_{b}^{t^+} \)-production and absorption cross sections reported in Figs. 6 and 8 respectively: the \( Z_{b} \)-production cross sections are smaller than the absorption ones by a factor about 2-10, depending on the specific channel. The essence of the difference between production and absorption cross sections is due to kinematic effects.

In Fig. 9 the \( Z_{b}^{t^+} \) absorption cross sections are plotted as a function of the CM energy \( \sqrt{s} \). The order of the cross sections is found to be \( 4 \times 10^{-2} - 3 \times 10^{-1} \) mb.
FIG. 8: Cross sections for the processes $\pi Z_b \to B B$ (dark shaded region), $\pi Z_b \to \bar{B}^* B$ (medium shaded region) and $\pi Z_b \to \bar{B}^* B^*$ (light shaded region), as function of CM energy $\sqrt{s}$.

for $10.82 \leq \sqrt{s} \leq 11.05$ GeV. The reaction with final $B^* B^*$ state has the largest cross section by a factor about 2-3 with respect to reaction with final $B^* B$ state. In addition, it can be noticed that the $Z_b^\prime$ absorption cross sections in Fig. 7 are greater than the $Z_b$ production cross sections in Fig. 9 by a factor about 8-10, depending on the specific channel. This behavior is qualitatively similar to the case involving the $Z_b$ state.

The findings reported above can be compared to previous works. In particular, in Ref. 34 the $Z_b^{(l)}$ production cross sections are analyzed making use of Heavy-Meson Effective Theory (HMET), taking as guiding principles chiral $SU(3)_L \times SU(3)_R$ and heavy quark symmetries. Considering the relevant scales for HMET, in this approach $p_\pi$ (the tri-momentum of the pion) is requested to be much less than $\Lambda_\chi = 4\pi f_\pi \sim 1$ GeV. This fact engenders a range of validity for the collision energy of each process. Thus, restricting the comparison to the energy ranges in which the results reported in Ref. 34 are valid, it can be noticed that $Z_b^{(l)}$ production cross sections in the present work are smaller by a factor about 10. We believe that this discrepancy is mainly due to the difference between the magnitude of the couplings, since in Ref. 34 the $g_{ZBB^*}$ and $g_{Z^\prime B^*B^*}$ coupling constants employed are larger (by a factor of $\sqrt{8}$) as compared to the ones used here.

FIG. 9: Cross sections for the processes $\pi Z_b^\prime \to \bar{B}^* B$ (dark shaded region) and $\pi Z_b^\prime \to \bar{B}^* B^*$ (light shaded region), as function of CM energy $\sqrt{s}$.

A. Inclusion of Form Factors

We can also include form factors in the vertices when evaluating the cross sections for the processes discussed above. Following [27, 31], we introduce a form factor of the type

$$ F(\vec{q}) = \frac{\Lambda^2}{\Lambda^2 + \vec{q}^2} \quad (16) $$

in the calculation of the cross sections for each of the vertices: $\Lambda$ is the cutoff and $\vec{q}$ the momentum transfer in the CM frame [that is, $\vec{q} = (\vec{p}_{1CM} - \vec{p}_{3CM})$ for the $t$-channel, and $\vec{q} = (\vec{p}_{1CM} - \vec{p}_{4CM})$ for the $u$-channel].

In Figs. 10-13 we show the cross sections for the different reactions studied here when we include form factors.
IV. CONCLUSIONS

We have studied the interactions between the $Z_b^+(10610)$ (and also $Z_b^+(10650)$) state and pions, in the processes $\bar{B}B \rightarrow \pi Z_b$, $\bar{B}^*B \rightarrow \pi Z_b^{(*)}$ and their inverse reactions. We have obtained the amplitudes and cross sections related to these processes at leading order within the framework of $SU(4)$ effective Lagrangians.

We have found that the $Z_b^{(*)+}$ production cross sections for the different final $\bar{B}B$, $\bar{B}^*B$, $\bar{B}^*B^*$ states are of the same order of magnitude. The same happens for the $Z_b^{(*)+}$ absorption cross sections.

But one of the main points here is that for reactions involving both $Z_b$ and $Z_b'$ states, the absorption cross sections are greater than the production cross sections, but still comparable with them. This fact may give a chance of significant survival probability of $Z_b^{(*)}$ in heavy ion collisions.

A similar result was found for the $X(3872)$ [27]. However, whereas the $X$ absorption cross sections are, on average, about two orders of magnitude larger than the production ones, the $Z$'s absorption cross sections are only a factor about ten larger than the production ones. These significant differences of the cross sections imply that the $X$ and the $Z$’s are much more easily destroyed than produced in a hot hadronic medium, but the $Z$’s have slightly better survival chances.

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