Using photoemission spectroscopy to probe a strongly interacting Fermi gas

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Ultracold atom gases provide model systems in which many-body quantum physics phenomena can be studied. Recent experiments on Fermi gases have realized a phase transition to a Fermi superfluid state with strong interparticle interactions \cite{1, 2, 3, 4, 5, 6, 7}. This system is a realization of the BCS-BEC crossover connecting the physics of BCS superconductivity and that of Bose-Einstein condensation (BEC) \cite{8, 9, 10}. While many aspects of this system have been investigated, it has not yet been possible to measure the single-particle excitation spectrum, which is a fundamental property directly predicted by many-body theories. Here we show that the single-particle spectral function of the strongly interacting Fermi gas at $T \approx T_c$ is dramatically altered in a way that is consistent with a large pairing gap. We use photoemission spectroscopy to directly probe the elementary excitations and energy dispersion in the Fermi gas of atoms. In these photoemission experiments, an rf photon ejects an atom from our strongly interacting system via a spin-flip transition to a weakly interacting state. We measure the occupied single-particle density of states \cite{11}. This new measurement technique for ultracold Fermi gas of $^{40}$K atoms at the cusp of the BCS-BEC crossover and on the BEC side of the crossover, and compare these results to that for a nearly ideal Fermi gas. Our results probe the many-body physics in a way that could be compared to data for high-$T_c$ superconductors \cite{12}. This new measurement technique for ultracold atom gases, like photoemission spectroscopy for electronic materials, directly probes low energy excitations and thus can reveal excitation gaps and/or pseudogaps. Furthermore, this technique can provide an analog to angle-resolved photoemission spectroscopy (ARPES) for probing anisotropic systems, such as atoms in optical lattice potentials.

As interacting quantum systems with highly tunable parameters and well understood two-body interactions, ultracold atom gases provide model systems in which to test condensed matter theories. A challenge for experimenters is to find ways to probe these atom gases that relate directly to condensed matter ideas and enable sensitive searches for new phenomena that can advance our understanding of strongly correlated systems. At a very basic level, the effect of interactions is a modification of the single-particle states. As interactions are increased, the single-particle eigenstates of the non-interacting case become quasi-particles and phase transitions manifest themselves as qualitative changes to the excitation spectrum \cite{13}, such as the appearance of energy gaps. The single-particle excitation spectrum can be predicted by many-body theory and is a fundamental property of any interacting system.

For electronic systems, photoemission spectroscopy (PES) provides a powerful technique to probe the occupied single-particle states \cite{13}. In a typical PES experiment, electrons are ejected from a substance through the photoelectric effect, see Fig. 4a. The photoelectrons are collected, energy and momentum resolved, and counted to give a spectrum of intensity as a function of the measured kinetic energy, $\epsilon_k = \hbar^2 k^2/2m$. Here, $\hbar = h/2\pi$, where $h$ is Planck’s constant, and $m$ is the particle mass. By conservation of energy, one can determine the energy of the original single-particle state, $E_s$, using

\begin{equation}
E_s = \epsilon_k + \phi - \hbar \nu.
\end{equation}

Here, $\hbar \nu$ is the photon energy, $\phi$ is the work function of the surface, and $E_F - E_s$ is often referred to as the binding energy \cite{13}.
For ultracold atom gases, radio-frequency (rf) spectroscopy has been used to probe a strongly interacting Fermi gas \[1, 2, 3, 4, 5, 6, 7\]. In a typical experiment, a pulse of rf drives atoms into an unoccupied Zeeman spin state, where they are counted to yield a spectrum of counts versus rf frequency. To date, the rf out-coupled atoms have not been energy or momentum resolved. However, analogous to electron PES, the momentum of the rf photon is negligible compared to the typical momentum of the atoms and therefore the momenta of the out-coupled atoms are characteristic of the original atom states. Eqn. (1) applies to photoemission spectroscopy of atom gases, by means of momentum-resolved rf spectroscopy, if one simply replaces the work function \(\phi\) with the Zeeman energy splitting, see Fig. 1a. The extension of photoemission spectroscopy from condensed matter to cold Fermi gases was discussed by Dao et al. \[19\].

In this paper, we use photoemission spectroscopy, by means of momentum-resolved rf spectroscopy, to probe an ultracold gas of fermionic \(^{40}\)K atoms. Similar to PES in solids, this measurement probes the single-particle spectral function, which is directly related to the single-particle Green’s function predicted by many-body theories \[13\]. We use this new technique to probe the Fermi gas near a magnetic-field Fano-Feshbach resonance where one can tune strong atom-atom interactions to realize a Fermi superfluid in the region of the BCS-BEC crossover \[1, 2, 3, 4, 5, 6, 7\].

Our Fermi gas consists of \(3 \times 10^5\) \(^{40}\)K atoms in a mixture of two spin-states. The gas is confined in an optical dipole trap and evaporatively cooled to \(T/T_F = 0.18\), where \(T\) is the temperature, \(T_F\) is the Fermi temperature as defined by \(T_F = E_F/k_B\), and \(k_B\) is Boltzmann’s constant. The Fermi energy, \(E_F = \hbar \cdot (9.4 \pm 0.5\,\text{kHz})\), is determined from a measurement of the peak density of the trapped gas. For the photoemission spectroscopy, we apply an rf pulse that couples atoms in one of the two spin states to an unoccupied third spin state. There are two essential requirements for determining the excitation spectrum. The first is that the interaction energy is sufficiently small that \(\epsilon_k = \hbar^2 k^2 / 2m\) holds and the data are not subject to complicated final-state effects \[20, 21, 22, 23, 24, 25, 26\]. The second requirement is that collisions do not scramble the energy and momentum information carried by the out-coupled atoms. In previous rf spectroscopy measurements both of these requirements were not satisfied \[3, 15, 16, 17, 18\]. In our \(^{40}\)K gas, however, the interaction energy for the out-coupled atoms is approximately 640 Hz, which is much smaller than \(E_F\). Furthermore, the mean-free path for the out-coupled atoms is much larger than the size of the gas: \(1/\sigma n \approx 6 R_F\), where \(\sigma\) is collision cross section, \(n\) is the average density, and \(R_F\) is the Fermi radius of the non-interacting gas.

To resolve the kinetic energy, \(\epsilon_k\), of the rf out-coupled atoms we apply an rf pulse that is short compared to the trap period. We then immediately turn off the trap, let the gas ballistically expand, and measure the velocity distribution using state-selective time-of-flight absorption imaging, see Fig. 2. Assuming a symmetric momentum distribution, we extract the 3D momentum distribution of the out-coupled atoms from the 2D image by performing an inverse Abel transform.

We first consider the case of an ideal Fermi gas. To create a very weakly interacting gas we adiabatically ramp the magnetic field to the zero crossing of the Feshbach resonance. In Fig. 3a, we plot the intensity, which is proportional to the number of atoms transferred into the third spin state, as a function of the original single-particle energy \(E_s\) and wave vector \(k\). The data are obtained by varying the rf frequency and counting the out-coupled atoms as a function of their momenta. We define zero energy to be the energy of a non-interacting atom at rest in the initial spin state. The intensity map for a non-interacting Fermi gas is expected to show delta function peaks at \(E_s = \epsilon_k\). The white asterisks mark the centers of the intensity at each value of \(k\) as determined from Gaussian fits; these show good agreement with the expected dispersion (black line). The rms width in \(E_s\) of the measured spectrum in Fig. 3a is 2.1 kHz and is due to an energy resolution that comes from the rf pulse duration.

To create a strongly interacting Fermi gas we adiabatically ramp the magnetic field to the peak of the Feshbach resonance where the s-wave scattering length \(a\) diverges and the dimensionless interaction parameter \(1/k_F^0 a = 0\). Here \(k_F^0\) is the Fermi wave vector that corresponds to the peak density of the original weakly interacting gas. Previous measurements have shown that after the ramp to \(1/k_F^0 a = 0\), our Fermi gas will be at \((0.9 \pm 0.1) \cdot T_c\) for the superfluid state \[2\]. With photoemission spec-
measured two-body binding energy is $h \Delta$. The second feature is very broad in energy, is shifted to high energy, and is qualitatively very similar to that in Fig. 3b. The energy width is broadened well beyond our energy resolution. There is now a wide consensus that interpretation of previous rf spectroscopy measurements \[2, 16, 17\] in terms of a pairing gap is a difficult problem that is still unsolved theoretically \[27\]. The photoemission spectroscopy technique presented here directly measures the occupied single-particle density of states and is therefore well-suited for measuring pairing gaps. In BCS theory the gap vanishes at $T_c$; however, in the BCS-BEC crossover a pseudogap due to preformed pairs is predicted to exist above $T_c$ \[11, 28\]. Perali et al. calculated the spectral function for a homogeneous Fermi gas near $T_c$ and found that the peaks of the spectral function fit almost exactly to a “BCS-like” dispersion curve where the BCS gap was replaced by the pseudogap \[11\]. As a first step to analyzing our data, we fit the centers of the intensity at each value of $k$ to this BCS-like dispersion curve \[11\], $E_s = \mu' - \sqrt{(\epsilon_k - \mu')^2 + \Delta^2}$. Here, the fitting parameters are the renormalized chemical potential $\mu'$ and the pseudogap $\Delta$. The best fit, shown as the white line in Fig. 3b, gives $\mu' = h \cdot (12.6 \pm 0.7 \text{ kHz})$ and $\Delta = h \cdot (9.5 \pm 0.6 \text{ kHz})$. In Fig. 14 of Ref. 11, Perali et al. also plot an example of predicted spectral functions for a few values of wave vector $k$. To facilitate comparison with theory, in Fig. 4 we show measured energy distribution curves (EDCs) for select values of $k$. It should be noted that in all trapped gas experiments, the density is inhomogeneous and the pairing gap will depend on the local Fermi energy. Therefore, our data should eventually be compared with a theory that includes the effect of the trapping potential through, for example, a local density approximation. Finally, we note that we have performed photoemission spectroscopy for a gas cooled below $T_c$ (initial $T/T_F = 0.10$) and found that the data is qualitatively very similar to that in Fig. 3b.

Far on the BEC side of the resonance, for $1/k_F^0 a \gg 1$, the pairing gap eventually becomes a two-body binding rather than a many-body effect that depends on the local Fermi energy. We measure the excitation spectrum for the Fermi gas at $1/k_F^0 a \approx 1$ where the molecule binding energy measured for a low density gas is $h \cdot (25 \pm 2 \text{ kHz})$. We observe two prominent features, see Fig. 4. The first feature is narrow in energy, starts at zero energy, and follows the quadratic dispersion expected for free atoms (black line). We attribute this feature to unpaired atoms, which may be out of chemical equilibrium with the pairs. The second feature is very broad in energy, is shifted to
lower energy, and trends towards lower energy for increasing \( k \). This feature we attribute to atoms in the paired state. An excitation gap separating the two features is evident in the data. We fit the centers of the molecule feature to a quadratic dispersion (white line) with the free parameters being the energy offset and an effective mass \( m^* \). In the BEC limit, where one has tightly bound molecules, we would expect the energy offset to be the molecule binding energy, which equals \( 2\Delta \), and the effective mass to be \(-m\). This negative effective mass reflects the fact that out coupling an atom at high \( k \) leaves behind an excitation in the form of an unpaired atom. The best fit to the data gives an energy offset of 28 kHz and \( m^* = -1.25m \).

The large energy width seen in Fig. 3: is likely due to center-of-mass motion of the pairs. For comparison with the data, we have performed a simple Monte Carlo simulation assuming a thermal distribution for the center-of-mass motion and using the predicted distribution of relative kinetic energy for rf dissociation of weakly bound molecules [20]. We assume the pairs are in thermal equilibrium with the unpaired atoms and use the measured temperature of the rf out-coupled atoms corresponding to the upper feature in Fig. 3. Assuming a molecule binding energy of \( h \cdot (25 \text{ kHz}) \), the calculation gives the intensity map shown in Fig. 5a.

The occupied density of states is obtained by summing the data in Fig. 3 over all \( k \), see Fig. 5b-d. For the nearly ideal Fermi gas data, Fig. 5, we find good agreement with the expected density of states for a Fermi gas at \( T = 0.18T_F \) in a harmonic trap (red curve). For the strongly interacting gas, Fig. 5, the occupied density of states becomes wider in energy and the peak shifts towards lower energies by an amount comparable to \( E_F \). From previous measurements of the in-trap size of the cloud [29] we estimate the Fermi energy of the strongly interacting gas to be \( h \cdot (12.4 \pm 0.7 \text{ kHz}) \) (dashed line). For the BEC side of the resonance, Fig. 5d, a pairing gap between bound pairs and free atoms is readily apparent. The red curve is the expected density of states determined from the simulation of a thermal distribution of weakly bound molecules (Fig. 5b). The only free parameter in the simulation is an overall scaling factor.

In this work, we have used photoemission spectroscopy, accomplished by momentum resolving the out-coupled atoms in rf spectroscopy, to probe the occupied single-particle density of states and energy dispersion through the BCS-BEC crossover. In the future, it may be possible to use spatially resolved photoemission spectroscopy to probe the local pairing gap. Another extension of this work will be to study the BCS-BEC crossover as a function of temperature and/or unbalanced spin population. Photoemission spectroscopy for ultracold atoms is a powerful and conceptually simple probe of strongly correlated atom gases that could be applied to many other atom gas systems. In the studies presented here, the atoms are interacting via isotropic s-wave interactions and therefore considering different directions of the out-coupled atoms' momenta was not necessary. However, like angle-resolved photoemission spectroscopy (ARPES) for solids, this technique could also be applied to non-isotropic systems such as atoms in an optical lattice, low dimensional systems, or higher partial wave pairing of atoms [30].

**Methods**

We evaporatively cool an equal mixture of \(^{40}\text{K} \) atoms in the \( |f, m_f\rangle = |9/2, -7/2\rangle \) and \( |f, m_f\rangle = |9/2, -9/2\rangle \) states, where \( f \) and \( m_f \) give the hyperfine level in the ground-state manifold. We cool the gas to in an optical dipole trap as described previously [29]. The frequencies for the cylindrically symmetric trap are \( f_r = 233 \text{ Hz} \) and \( f_z = 19 \text{ Hz} \). The time-of-flight imaging uses a beam that propagates along the \( \hat{z} \) direction. At the end of
the evaporation, we adiabatically increase the interaction strength by lowering the magnetic field, at a rate of 0.1 G/ms, to a value near the Feshbach resonance located at 202.10 ± 0.07 G [2]. The magnetic field values for the data in Fig. 5b-c are 208.43, 202.10, and 201.51 G, respectively.

For photoemission spectroscopy, we apply an rf pulse with a Gaussian amplitude envelope with a 1/\(e^2\) width of 240 \(\mu\)s, to transfer atoms from the \(|9/2, -7/2\rangle\) state to the \(|9/2, -5/2\rangle\) state. The rf frequency is approximately 47 MHz. Atoms in the \(|9/2, -5/2\rangle\) state have a two-body s-wave scattering length that is 130 Bohr radii with the \(|9/2, -7/2\rangle\) state and 250 Bohr radii with the \(|9/2, -9/2\rangle\) state. Immediately after the rf pulse we turn off the optical trap and let the atoms expand for 3 to 6.5 ms before taking a resonant absorption image of the \(|9/2, -5/2\rangle\) atoms. Typically four images are averaged for each rf frequency. For the weakly-interacting Fermi gas, the rf power was chosen to achieve maximum transfer. For data on resonance and on the BEC-side of resonance, no more power was chosen to achieve maximum transfer. For data on the imaging system.

In Eqn. [1] we take \(\phi\) to be the rf resonance energy measured for a weakly interacting gas. There is an uncertainty of \(\pm 1\) kHz in \(\phi\) and therefore also in the zero of \(E_s\). The measured wave vector \(k\) has an uncertainty of approximately 5% from uncertainty in the magnification of the imaging system.

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