Dual parameterization of generalized parton distributions and
description of DVCS data

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Abstract

We discuss a new leading-order parameterization of generalized parton distributions of the proton, which is based on the idea of duality. In its minimal version, the parameterization is defined by the usual quark singlet parton distributions and the form factors of the energy-momentum tensor. We demonstrate that our parameterization describes very well the absolute value, the $Q^2$-dependence and the $W$-dependence of the HERA data on the total DVCS cross section and contains no free parameters in that kinematics. The parameterization suits especially well the low-$x_{Bj}$ region, which allows us to advocate it as a better alternative to the frequently used double distribution parameterization of the GPDs.

PACS numbers: 13.60.-r,12.38.Lg
I. INTRODUCTION

Generalized parton distributions (GPDs) have become a standard QCD tool for analyzing and parameterizing the non-perturbative parton structure of hadronic targets, for reviews see \cite{1, 2, 3, 4, 5, 6}. In general, GPDs are more general and complex objects than structure functions and form factors. In addition, experimentally measured observables do not access the GPDs themselves but only their convolution with the hard scattering coefficients. Therefore, the experimental determination of the GPDs is an extremely difficult task. Hence, when dealing with the GPDs, one invariably uses models, the known limiting behavior and general properties of the GPDs and the physical intuition.

The GPDs have been modeled using virtually all known models of the nucleon structure: bag models \cite{7}, the chiral quark-soliton model \cite{8}, light-front models \cite{9, 10}, constituent quark models \cite{11}, Bethe-Salpeter approach \cite{12}, a NJL model \cite{13}. In addition, a double distribution model of the GPDs \cite{14, 15} and modeling by perturbative diagrams \cite{16} were suggested.

The factorization theorem for deeply virtual Compton scattering (DVCS) \cite{17} gives a practical possibility to measure the GPDs by studying various processes involving the GPDs: DVCS, exclusive electroproduction of vector mesons, wide angle Compton scattering \cite{18, 19}, exclusive \( p\bar{p} \rightarrow \gamma \gamma \) annihilation \cite{20}, the \( p\bar{p} \rightarrow \gamma \pi^0 \) process \cite{21}, \( \gamma^* \gamma \rightarrow \pi \pi \) near threshold \cite{22}. However, in order to accommodate such a potentially large number of data, parameterizations of the GPDs should be sufficiently flexible and versatile. In particular, they should allow for the connection of the DVCS with the \( p\bar{p} \rightarrow \gamma \gamma \) process.

The commonly used double distribution parameterization of the GPDs \cite{14, 15} is one example of the model of the GPDs which could be used to connect different physical channels \cite{23}. However, the parameterization of the GPDs based on the double distribution has a number of problems from the phenomenological point of view. First, in order to have the full form of polynomiality, the so-called \( D \)-term \cite{24} has to added by hand. Second, the model dramatically overestimates the low-\( x \) HERA data on the total DVCS cross section because it involves proton parton distributions at extremely small and unmeasured values of Bjorken \( x \) \cite{25}. Third, the model does not allow for an intuitive physical motivation and interpretation, see \cite{26} for a discussion of the physics of GPDs.

In this paper, we offer a new model for the GPDs, which was in a general form intro-
duced in \[27\]. Unlike the models of the GPDs mentioned above, the present model has a simple physical interpretation and direct correspondence to the mechanical properties of the target \[28\]. The suggested parameterization of the GPDs can be analytically continued in \(t\) to the physical region of the \(p\bar{p} \rightarrow \gamma \gamma\) reaction and also allows for flexible modeling of the \(t\)-dependence of the GPDs.

The considered parameterization of the GPDs is called dual because the GPDs are presented as an infinite series of \(t\)-channel exchanges, which reminds of the ideas of duality in hadron-hadron scattering.

In this work, we formulate the minimal version of the dual parameterization and determine the free parameters of the model. Using the resulting dual parameterization of the GPDs, we successfully describe the HERA data on the DVCS cross section \[29, 30, 31\]. We explain that our parameterization suits the low-\(x_{Bj}\) kinematics especially well because the quark singlet parton distributions are never probed at the unmeasurably low values of Bjorken \(x\) and because the final expression for the DVCS amplitude is numerically stable. Thus, the dual parameterization of the GPDs gives an opportunity to have a physically intuitive model of the GPDs, which agrees with the DVCS experiments and which can serve as an alternative to the popular double distribution model.

II. THE DUAL PARAMETERIZATION OF GPDs

The dual representation of the GPDs was first introduced for the pion GPDs in \[32\]. The essence of that derivation is presented below. The starting point was the decomposition of the two-pion distribution amplitude (2πDA) in terms of the eigenfunctions of the ERBL evolution equation (Gegenbauer polynomials \(C_n^{3/2}\)), the partial waves of produced pions (Legendre polynomials \(P_l\)) and generalized form factors \(B_{nl}\). The moments of the 2πDA, being the matrix elements of certain local operators, could be related by crossing to the moments of the pion GPDs. Then, the pion GPDs could be formally reconstructed using the explicit form of their moments.

Based on the result of \[32\], the dual representation for the proton GPDs was suggested in \[27\]. In this paper, we will consider only the singlet (\(C\)-even) combination of the GPDs \(H\), which give the dominant contribution to the total DVCS cross section at high energies and small \(t\). We will work in the leading order approximation and, hence, we will consider
only quark GPDs.

The dual representation of the singlet GPD $H^i$ of the quark flavor $i$ is

$$H^i(x, \xi, t, \mu^2) = \sum_{n=1, \text{odd}}^{\infty} \sum_{l=0, \text{even}}^{n+1} B^i_{nl}(t, \mu^2) \theta \left(1 - \frac{x^2}{\xi^2}\right) \left(1 - \frac{x^2}{\xi^2}\right) C^{3/2}_n \left(\frac{x}{\xi}\right) P_1 \left(\frac{1}{\xi}\right), \quad (1)$$

where $x$, $\xi$ and $t$ are the usual GPD variables. The series (1) is divergent at fixed $x$ and $\xi$, and, hence, it should be understood as a formal series. In particular, it is incorrect to evaluate the series term by term. As a result, the GPD $H^i$ of Eq. (1) has a support over the entire $-1 \leq x \leq 1$ region, regardless that each term of the series is non-vanishing only for $-\xi \leq x \leq \xi$. The formal representation (1) can be equivalently rewritten as a converging series using the technique developed in [27].

The derivation of Eq. (1) used the idea of duality of hadronic physics, when the scattering amplitude in the $s$-channel is represented as an infinite series of the $t$-channel exchanges. This explains the name “the dual representation” for the representation of Eq. (1).

As a double series, Eq. (1) is inconvenient for phenomenological applications. For the evaluation of the LO DVCS amplitude, it is useful to introduce the functions $Q_k(x, t)$ whose Mellin moments generate the $B^i_{nl}$ form factors [27]

$$B^i_{n+1-k}(t, \mu^2) = \int_0^1 dx x^n Q_k^i(x, t, \mu^2), \quad (2)$$

where $k$ is even. A remarkable property of the dual representation is that the $\mu^2$-evolution of the functions $Q_k^i$ is given by the usual leading order (LO) DGLAP evolution.

Since the $B^i_{nl}$ form factors are related to the moments of $H^i$, the $Q_k$ functions are also constrained by these moments. In particular, from

$$\int_{-1}^{1} dx x H^i(x, \xi, t) = M^i_2(t) + \frac{4}{5} \xi^2 d^i(t) = \frac{6}{5} \left[ B_{12}(t) - \frac{1}{3} (B_{12}(t) - 2B_{10}(t)) \xi^2 \right], \quad (3)$$

it follows that

$$\int_0^1 dx x Q^i_0(x, t, \mu^2) = \frac{5}{6} M^i_2(t, \mu^2),$$

$$\int_0^1 dx x Q^i_2(x, t, \mu^2) = \frac{5}{12} M^i_2(t, \mu^2) + d^i(t, \mu^2), \quad (4)$$

where $M^i_2$ at $t = 0$ is the proton light-cone momentum fraction carried by the quarks; $d^i(t)$ is the first moment of the quark $D$-term.
In addition, the $B_{nm+1}$ form factors at the zero momentum transfer are fixed by the Mellin moments of the quark singlet parton distribution functions (PDFs). In particular,

$$\frac{3}{4} \int_0^1 dx \left( q^i(x, \mu^2) + \bar{q}^i(x, \mu^2) \right) = B_{10}(0) = \int_0^1 dx \ Q^i_0(x, 0, \mu^2). \quad (5)$$

The $Q^i_0$ functions at $t = 0$ are completely fixed in terms of the forward proton PDFs 

$$Q^i_0(x, 0, \mu^2) = q^i(x, \mu^2) + \bar{q}^i(x, \mu^2) - \frac{x}{2} \int_x^1 \frac{dz}{z^2} \left( q^i(z, \mu^2) + \bar{q}^i(z, \mu^2) \right). \quad (6)$$

As suggested in [27], keeping only the functions $Q^i_0$ and $Q^i_2$ constitutes the minimal version of the dual parameterization of the GPDs. The functions $Q^i_0$ and $Q^i_2$ are defined by Eqs. (6) and (4), where $M^i_2(t)$ and $d^i(t)$ have a clear physical interpretation since they are the form factors of the energy-momentum tensor evaluated between the states representing the given target. At $t = 0$, $M^i_2(0)$ is the fraction of the plus-momentum of the nucleon carried by the quarks of flavor $i$; $d^i(0)$ characterizes the shear forces experienced by the quarks in the target.

Next we discuss the minimal version of the dual representation in detail. While $Q^i_0$ at $t = 0$ is defined by Eq. (6), only the first $x$-moment of $Q^i_2$ is constrained. We simply assume that $Q^i_2 \propto Q^i_0$ and take

$$Q^i_2(x, 0, \mu^2) = \beta^i Q^i_0(x, 0, \mu^2), \quad (7)$$

where $\beta^i$ are constants. From Eq. (4), we obtain

$$\beta^i = \frac{6}{5} \frac{d^i(0)}{M^i_2(0)} + \frac{1}{2}, \quad (8)$$

which gives

$$\beta^u = -4.4, \quad \beta^d = -8.9, \quad \beta^s = 0.5. \quad (9)$$

In this numerical estimate, we assume that $d^u = d^d \approx -2$ and $d^s \approx 0$, which agrees with the SU(3)-symmetric chiral quark soliton model calculation of the nucleon D-term [33]: $\sum_i d^i(0) \approx -4$, and takes into account the SU(3) symmetry breaking in the nucleon PDFs (the suppression of the strange quark PDF at the low resolution scale). The momentum fractions $M^i_2$ were evaluated at $\mu_0 = 0.6$ GeV using the LO GRV parton PDFs [34].

In general, $\beta^i$ also depend on $\mu^2$. However, as will be seen from the general expression for the DVCS amplitude, at small values of $\xi$ typical for the HERA data on the total DVCS cross section, the contribution of the $Q^i_2$ function is kinematically suppressed. Therefore,
the goodness of the description of the data is not affected by the exact values of $\beta_i$, and we simply used Eq. (9) at all $\mu^2$.

Until recently, the $t$-dependence of the DVCS cross section was not measured. One would simply assume that the DVCS cross section exponentially depends on $t$,

$$
\frac{d\sigma_{\text{DVCS}}(x_{Bj}, Q^2, t)}{dt} = \exp (-B |t|) \left( \frac{d\sigma_{\text{DVCS}}(x_{Bj}, Q^2, t)}{dt} \right)_{t=0},
$$

such that the total DVCS cross section is

$$
\sigma_{\text{DVCS}}(x_{Bj}, Q^2) = \frac{1}{B} \left( \frac{d\sigma_{\text{DVCS}}(x_{Bj}, Q^2, t)}{dt} \right)_{t=0}.
$$

The value of the slope parameter $B$ was rather uncertain, $5 \leq B \leq 9$ GeV$^{-2}$. The range of the values covers the experimentally measured range of the $t$-slope of electroproduction of light vector mesons at HERA. However, very recently the $t$-dependence of the total DVCS cross section for $0.1 \leq |t| \leq 0.8$ GeV and at $Q^2 = 8$ GeV$^2$ was measured by the H1 collaboration at HERA and was fitted by the exponential form of Eq. (10) with the result $B = 6.02 \pm 0.35 \pm 0.39$ GeV$^{-2}$ [31].

In our numerical estimates of the DVCS cross section, we calculate the DVCS amplitude at $t = 0$ and then use Eq. (11) in order to find the $t$-integrated DVCS cross section. In general, the slope $B$ should decrease with increasing $Q^2$. A particular model for the $Q^2$-dependent slope was suggested in [36]: $B(Q^2) = 8 \left( 1 - 0.15 \ln(Q^2/2) \right)$ GeV$^{-2}$. In our analysis, we use the same $Q^2$-dependence,

$$
B(Q^2) = 7.6 \left( 1 - 0.15 \ln(Q^2/2) \right) \text{ GeV}^{-2},
$$

but with a slightly smaller constant 7.6 GeV$^{-2}$, which is chosen such that Eq. (12) reproduces the H1 value of the slope at $Q^2 = 8$ GeV$^2$.

In summary, our parameterization of the GPDs $H^i$ is defined by Eqs. (4), (6) and (7). The $t$-dependence of the DVCS cross section is given by Eqs. (10) and (12). This is the minimal version of the dual representation of the GPDs, which can be readily extended by considering more $Q^i_k$ functions, a more elaborate $t$-dependence and by taking into account the other GPDs of the proton. The main practical advantage of our representation is that the $\mu^2$-evolution of $Q^i_{0,2}$ is given by the usual DGLAP evolution of the singlet PDFs, see Eq. (5).
III. DESCRIPTION OF LOW-\(x\) HERA DATA ON DVCS CROSS SECTION

In this section, we evaluate the total DVCS cross section using the minimal model of the
dual representation of the GPDs and compare the results to the HERA data \[30, 31\].

The total unpolarized DVCS cross section on the photon level reads, see e.g. \[35\],
\[
\sigma_{DVCS}(x_{Bj}, Q^2) = \frac{\alpha_{e.m.}^2 x_{Bj}^2 \pi (1 - \xi^2)}{Q^4 \sqrt{1 + 4x_{Bj}^2 m_N^2 / Q^2}} \int_{t_{\text{max}}}^{t_{\text{min}}} dt |\tilde{A}_{DVCS}(\xi, t, Q^2)|^2, \tag{13}
\]
where \(\alpha_{e.m.}\) the fine-structure constant; \(\xi = 1/2x_{Bj}/(1-x_{Bj}/2)\) in the Bjorken limit; \(t_{\text{max}} \approx 0\) and \(t_{\text{min}} \approx -1\ \text{GeV}^2\); \(|\tilde{A}_{DVCS}|^2\) is the squared and spin-averaged DVCS amplitude.

To the leading order in \(\alpha_s\), the DVCS amplitude is expressed in terms of the singlet
combination of the GPDs \(H^i\),
\[
A_{DVCS}(\xi, t, Q^2) = \sum_i e_i^2 \int_0^1 dx H^i(x, \xi, t, Q^2) \left( \frac{1}{x - \xi + i0} + \frac{1}{x + \xi - i0} \right). \tag{14}
\]

Using our model for the GPDs and the results of \[27\], the DVCS amplitude can be presented
in a compact form in terms of the \(Q_0^i\) and \(Q_2^i\) functions
\[
A_{DVCS}(\xi, t, Q^2) = -\sum_i e_i^2 \int_0^1 \frac{dx}{x} \sum_{k=0}^2 x^k Q_k^i(x, t, Q^2) \left( \frac{1}{\sqrt{1 - \frac{2x}{\xi} + x^2}} + \frac{1}{\sqrt{1 + \frac{2x}{\xi} + x^2}} - 2\delta_{k0} \right). \tag{15}
\]

Using the exponential ansatz for the \(t\)-dependence of the DVCS cross section, the total
DVCS cross section is expressed in terms of the DVCS amplitude at \(t = 0\) [see Eq. (11)]
\[
\sigma_{DVCS}(x_{Bj}, Q^2) = \frac{\alpha_{e.m.}^2 x_{Bj}^2 \pi (1 - \xi^2)}{Q^4 \sqrt{1 + 4x_{Bj}^2 m_N^2 / Q^2}} \frac{1}{B(Q^2)} |\tilde{A}_{DVCS}(\xi, t = 0, Q^2)|^2, \tag{16}
\]
where \(A_{DVCS}(\xi, t = 0, Q^2)\) is given by Eq. (15) evaluated with \(Q_{0,2}^i(x, 0, Q^2)\).

Our predictions for the \(Q^2\) and \(W\)-dependence of the total DVCS cross section are pre-
sented in Figs. \[\text{1}\] and \[\text{2}\] respectively. For comparison, we also present the H1 \[31\] and
ZEUS \[30\] data.

Note that the ZEUS data points, which were taken at \(W = 89\ \text{GeV}\) and at \(Q^2 = 9.6\ \text{GeV}^2\),
have been rescaled to the H1 values of \(W = 82\ \text{GeV}\) and \(Q^2 = 8\ \text{GeV}^2\) using the fitted \(W\)
and \(Q^2\)-dependence of the DVCS cross section: \(\sigma_{DVCS} \propto W^{0.75}\) and \(\sigma_{DVCS} \propto 1/(Q^2)^{1.54}\) \[30\].

For the proton forward PDFs, which are required to evaluate \(Q_0^i\), we used the LO CTEQ5L
parameterization \[37\].
FIG. 1: The total DVCS cross section at $W = 82$ GeV as a function of $Q^2$. The predictions of the dual parameterization of the GPDs (solid curve) is compared to the H1 [31] and ZEUS [30]. The error bars represent the statistical and systematic uncertainties added in quadrature.

One can see from Fig. 1 that the absolute value and the $Q^2$-dependence of the total DVCS cross section is described very well. The agreement with the data at the highest values of $Q^2$ would have been worse, if we had used the $Q^2$-independent slope $B$.

From Fig. 2 one can see that the absolute value and the $W$-dependence of the DVCS cross section is also reproduced rather well. However, one should note a slight discrepancy between the ZEUS and H1 data points at lower values of $W$ and large experimental errors at the high end of $W$.

It is important to emphasize that our predictions for the total DVCS cross section were made using the parameterization of the GPD, which contains no free parameters (the role of $Q_2^i$ and $\beta$, see Eq. (7), is negligible in the H1 and ZEUS kinematics). It is very remarkable
FIG. 2: The total DVCS cross section at $Q^2 = 8$ GeV as a function of $W$. The predictions of the dual parameterization of the GPDs (solid curve) is compared to the H1 [31] and ZEUS [30]. The error bars represent the statistical and systematic uncertainties added in quadrature.

that the agreement with the data is so good.

In order to understand, at least partially, the success of the dual parameterization of GPDs in the description of the low-$x$ HERA data, it is instructive to analyze the DVCS amplitude $A_{DVCS}$ of Eq. 15 in some detail. Evaluating the imaginary and real parts of Eq. 15, one obtains

$$\text{Im} A(\xi, Q^2) = - \sum_i e_i^2 \int_a^1 \frac{dx}{x} \frac{1}{\sqrt{2x/\xi - x^2} - 1} \sum_{k=0}^2 x^k Q_k(x, 0, Q^2),$$

$$\text{Re} A(\xi, t) = - \sum_i e_i^2 \int_a^1 \frac{dx}{x} \sum_{k=0}^2 x^k Q_k(x, 0, Q^2) \left( \frac{1}{\sqrt{1 + 2x/\xi + x^2} - 2\delta_{k0}} \right)$$
\[-\sum_i e_i^2 \int_0^a \frac{dx}{x} \sum_{k=0}^2 x^k Q_k(x, 0, Q^2) \left( \frac{1}{\sqrt{1 - 2x/\xi + x^2}} + \frac{1}{\sqrt{1 + 2x/\xi + x^2}} - 2\delta_{k0} \right), \]

where \(a = (1 - \sqrt{1 - \xi^2})/\xi\).

At low \(x_{Bj}\), \(\xi \approx x_{Bj}/2\) and the integration limit is \(a \approx \xi/2 = x_{Bj}/4\). Thus, the functions \(Q_0^i\) and \(Q_2^i\) are never sampled at \(x < x_{Bj}/4\). This is clearly an advantage over the double distribution parameterization of GPDs, where the forward parton distributions are sampled all the way down to \(x = 0\), which results in the acute sensitivity to the unmeasured, very low-\(x\) behavior of the proton PDFs and leads to a gross overestimate of the data [25].

In addition, Eqs. (17) are convenient for the numerical implementation since the integrands do not contain large end-point contributions, as can be explicitly seen by changing the integration variables.

IV. DISCUSSION AND CONCLUSIONS

We presented and discussed a new leading order parameterization of GPDs introduced in [27]. In its minimal form, the parameterization is defined by the forward singlet quark PDFs and the form factors of the energy-momentum tensor, see Eqs. (4) and (6). The \(t\)-dependence of the DVCS cross section was assumed in a simple factorized form with the \(Q^2\)-dependent slope, see Eqs. (10) and (12).

We showed that our parameterization of the GPDs describes very well the absolute value, the \(Q^2\)-dependence and \(W\)-dependence of the HERA data on the total DVCS cross section. Moreover, since the data is at low \(x_{Bj}\), our parameterization can be simplified by omitting the contribution of the \(Q_2^i\) function. This means that we achieved a remarkably good description of a large set of the data on DVCS using a parameterization of the GPDs which contains no free parameters!

We discuss that our parameterization suits the low-\(x_{Bj}\) kinematics especially well because the quark singlet PDFs are never probed at the unmeasurably low values of Bjorken \(x\), as is the case for the popular double distribution model [25], and because the expression for the DVCS amplitude is numerically stable. This allows us to advertise our model as a better alternative to the popular double distribution parameterization of the GPDs, at least in the low-\(\xi\) region.

The parameterization presented in this work can be readily generalized by including more
\( Q_k^i \) functions, considering the GPDs \( E, \tilde{H} \) and \( \tilde{E} \) and by using more elaborate models of the \( t \)-dependence. This was not necessary in the H1 \cite{H1} and ZEUS \cite{ZEUS} kinematics, but might be required for the HERMES and CLAS kinematics.

Also, the role of next-to-leading order (NLO) corrections and higher twist effects should be investigated. In particular, it is important to compare the size of the NLO corrections using the dual parameterization with the results of the analysis using the double distribution parameterization, where the NLO corrections were found to be large \cite{DLP}.

**Acknowledgements**

We would like to thank M. Strikman and P. Pobylitsa for valuable discussions and comments. It is a pleasure to thank A. Freund for carefully reading the initial draft of the manuscript and making valuable suggestions. This work is supported by the Sofia Kovalevskaya Program of the Alexander von Humboldt Foundation.

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