Search for $B \to \tau \nu$ and $B \to K \nu \bar{\nu}$ Decays with a Fully
Reconstructed $B$ at Belle

K. Abe,9 K. Abe,47 I. Adachi,9 H. Aihara,49 K. Aoki,23 K. Arinstein,2 Y. Asano,54
T. Aso,53 V. Aulchenko,2 T. Aushev,13 T. Aziz,45 S. Bahinipati,5 A. M. Bakich,44
V. Balagura,13 Y. Ban,36 S. Banerjee,45 E. Barberio,22 M. Barbero,8 A. Bay,19 I. Bedny,2
U. Bitenc,14 I. Bizjak,14 S. Blyth,25 A. Bondar,2 A. Bozek,29 M. Bračko,9,21,14
J. Brodzicka,29 T. E. Browder,8 M.-C. Chang,48 P. Chang,28 Y. Chao,28 A. Chen,25
K.-F. Chen,28 W. T. Chen,25 B. G. Cheon,4 C.-C. Chiang,28 R. Chistov,13 S.-K. Choi,7
Y. Choi,43 Y. K. Choi,43 A. Chuvikov,37 S. Cole,44 J. Dalseno,22 M. Danilov,13 M. Dash,56
L. Y. Dong,11 R. Dowd,22 J. Dragic,9 A. Drutskoy,5 S. Eidelman,2 Y. Enari,23 D. Epifanov,2
F. Fang,8 S. Fratina,14 H. Fujii,9 N. Gabyshev,2 A. Garmash,37 T. Gershon,9 A. Go,25
G. Gokhroo,45 P. Goldenzweig,5 B. Golob,29,14 A. Gorišek,14 M. Grosse Perdekamp,38
H. Guler,8 R. Guo,26 J. Haba,9 K. Harai,9 T. Hara,34 Y. Hasegawa,42 N. C. Hastings,49
K. Hasuko,48 K. Hayasaka,23 H. Hayashii,24 M. Hazumi,9 T. Higuchi,9 L. Hinz,19 T. Hojo,34
T. Hokuue,23 Y. Hoshi,47 K. Hoshina,52 S. Hou,25 W.-S. Hou,28 Y. B. Hsiung,28
Y. Igarashi,9 T. Iijima,23 K. Ikado,23 A. Imoto,24 K. Inami,23 A. Ishikawa,9 H. Ishino,50
K. Itoh,49 R. Itoh,9 M. Iwasaki,49 Y. Iwasaki,9 C. Jacoby,19 C.-M. Jen,28 R. Kagan,13
H. Kakuno,49 J. H. Kang,57 J. S. Kang,16 P. Kapusta,29 S. U. Kataoka,24 N. Katayama,9
H. Kawai,3 N. Kawamura,1 T. Kawasaki,31 S. Kazi,5 N. Kent,8 H. R. Khan,50
A. Kibayashi,50 H. Kichimi,9 H. J. Kim,18 H. O. Kim,43 J. H. Kim,43 S. K. Kim,41
S. M. Kim,43 T. H. Kim,57 K. Kinoshita,5 N. Kishimoto,23 S. Korpar,21,14 Y. Kozakai,23
P. Križan,20,14 P. Krovokny,9 T. Kubota,23 R. Kulasirii,5 C. C. Kuo,25 H. Kurashiro,50
E. Kurihara,3 A. Kusaka,49 A. Kuzmin,2 Y.-J. Kwon,57 J. S. Lange,6 G. Leder,12
S. E. Lee,41 Y.-J. Lee,28 T. Lesiak,29 J. Li,40 A. Limosani,9 S.-W. Lin,28 D. Liventsev,13
J. MacNaughton,12 G. Majumder,45 F. Mandl,12 D. Marlow,37 H. Matsumoto,31
T. Matsumoto,51 A. Matyja,29 Y. Mikami,48 W. Mitasoff,12 K. Miyabayashi,24 H. Miyake,34
H. Miyata,31 Y. Miyazaki,23 R. Mizuk,13 D. Mohapatra,56 G. R. Moloney,22 T. Mori,50
A. Murakami,39 T. Nagamine,48 Y. Nagasaka,10 T. Nakagawa,51 I. Nakamura,9
E. Nakano,33 M. Nakao,9 H. Nakazawa,9 Z. Natkaniec,29 K. Neichi,47 S. Nishida,9
O. Nitoh,52 S. Noguchi,24 T. Nozaki,9 A. Ogawa,38 S. Ogawa,46 T. Ohshima,23 T. Okabe,23
S. Okuno,15 S. L. Olsen,8 Y. Onuki,31 W. Ostrowicz,29 H. Ozaki,9 P. Pakhlov,13 H. Palka,29
C. W. Park,43 H. Park,18 K. S. Park,43 N. Parslow,44 L. S. Peak,44 M. Pernicka,12
R. Pestotnik,14 M. Peters,8 L. E. Piilonen,56 A. Poluektov,2 F. J. Ronga,9 N. Root,2
M. Rozanska,29 H. Sahoo,8 M. Saigo,48 S. Saitoh,9 Y. Sakai,9 H. Sakamoto,17
H. Sakaue,33 T. R. Sarangi,9 M. Satapathy,55 N. Sato,23 N. Satoyama,42 T. Schietinger,19
O. Schneider,19 P. Schönmeier,48 J. Schümann,28 C. Schwanda,12 A. J. Schwartz,5
T. Seki,51 K. Senyo,23 R. Seuster,8 M. E. Sevior,22 T. Shibata,31 H. Shibuya,46
J.-G. Shiu,28 B. Shwartz,2 V. Sidorov,2 J. B. Singh,35 A. Somov,5 N. Soni,35 R. Stamen,9
S. Stanic,32 M. Staric,14 A. Sugiyama,39 K. Sumisawa,9 T. Sumiyoshi,51 S. Suzuki,39
S. Y. Suzuki,9 O. Tajima,9 N. Takada,42 F. Takasaka,9 K. Tamai,9 N. Tamura,31
K. Tanabe,49 M. Tanaka,9 G. N. Taylor,22 Y. Teramoto,33 X. C. Tian,36 K. Trabelsi,8
Y. F. Tse, T. Tsuboyama, T. Tsukamoto, K. Uchida, Y. Uchida, S. Uehara, T. Uglov, K. Ueno, Y. Unno, S. Uno, P. Urquijo, Y. Ushiroda, G. Varner, K. E. Varvell, S. Villa, C. C. Wang, C. H. Wang, M.-Z. Wang, M. Watanabe, Y. Watanabe, L. Widhalm, C.-H. Wu, Q. L. Xie, B. D. Yabsley, A. Yamaguchi, H. Yamamoto, S. Yamamoto, Y. Yamashita, M. Yamauchi, Heyoung Yang, J. Ying, S. Yoshino, Y. Yuan, Y. Yusa, H. Yuta, S. L. Zang, C. C. Zhang, J. Zhang, L. M. Zhang, Z. P. Zhang, V. Zhilich, T. Ziegler, and D. Zürcher (The Belle Collaboration)

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Abstract

We present a search for the decays $B^- \rightarrow \tau^- \bar{\nu}$ and $B^- \rightarrow K^- \nu \bar{\nu}$ in a 253 $fb^{-1}$ data sample collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric energy $B$ factory. Combinatorial and continuum backgrounds are suppressed by selecting a sample of events with one fully reconstructed $B$. The decay products of the $B$ on the other side of the event are analyzed to search for $B^- \rightarrow \tau^- \bar{\nu}$ and $B^- \rightarrow K^- \nu \bar{\nu}$ decays. We find no significant evidence for a signal and set 90% confidence level upper limits of $\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}) < 1.8 \times 10^{-4}$ and $\mathcal{B}(B^- \rightarrow K^- \nu \bar{\nu}) < 3.6 \times 10^{-5}$. All results are preliminary.

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The purely leptonic decay $B^- \rightarrow \ell^- \nu$ (charge conjugate states are implied throughout the paper) is of particular interest since it provides direct measurement of the product of the Cabibbo-Kobayashi-Maskawa (CKM) matrix element $V_{ub}$ and the $B$ meson decay constant $f_B$. In the Standard Model (SM), the branching fraction of the decay $B^- \rightarrow \ell^- \nu$ is given as

$$B(B^- \rightarrow \ell^- \nu) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

(1)

where $G_F$ is the Fermi coupling constant, $m_\ell$ and $m_B$ are the charged lepton and $B$ meson masses, $\tau_B$ is the $B^- \rightarrow \ell^- \nu$ lifetime. The dependence on the lepton mass arises from helicity conservation, which suppresses the muon and electron channels. The CKMFitter predicts the $B^- \rightarrow \tau^- \nu$ branching fraction to be $(9.3^{+3.4}_{-2.7}) \times 10^{-5}$ \cite{1}. No evidence for an enhancement relative to the SM prediction was observed in previous experimental studies. The most stringent upper limit has been achieved by the BABAR Collaboration: $B(B^- \rightarrow \tau^- \nu) < 4.2 \times 10^{-4}$ at 90% confidence level (C.L.) \cite{2}.

Flavor-changing neutral-current transition such as $b \rightarrow s\nu\bar{\nu}$ occurs in the SM via one-loop box or electroweak penguin diagrams with heavy particles in the loops. Because heavy non-SM particles could contribute additional loop diagrams, various new physics scenarios can lead to significant enhancements in the observed rates \cite{3,4}. The SM $B^- \rightarrow K^-\nu\bar{\nu}$ branching fraction has been estimated to be $(3.8^{+1.2}_{-1.0}) \times 10^{-6}$ \cite{5,6}, while the most stringent published experimental limit is $B(B^- \rightarrow K^-\nu\bar{\nu}) < 5.2 \times 10^{-5}$ at 90% C.L. \cite{7}.

We use a 253 fb$^{-1}$ data sample containing $275 \times 10^6$ $B$ meson pairs collected with the Belle detector at the KEKB asymmetric energy $e^+e^-$ (3.5 on 8 GeV) collider \cite{8} operating at the $\Upsilon(4S)$ resonance ($\sqrt{s} = 10.58$ GeV). The Belle detector is a large-solid-angle magnetic spectrometer consisting of a three-layer silicon vertex detector, a 50-layer central drift chamber (CDC), a system of aerogel threshold Čerenkov counters (ACC), time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to identify $K_S^0$ and muons. The detector is described in detail elsewhere \cite{9}.

The strategy adopted for this analysis is to reconstruct exclusively the decay of one of the $B$ mesons in the event and compare properties of the remaining particle(s) in the event (referred to as the signal side) to those expected for signal and background. All the tracks and photon candidates in the event not used to reconstruct the $B$ are studied to search for $B^- \rightarrow \tau^-\nu$ and $B^- \rightarrow K^-\nu\nu$. The advantage of having a sample of fully reconstructed $B$ meson is to provide a strong suppression of the combinatorial and continuum background events. The disadvantage is the low efficiency of full $B$ meson reconstruction (approximately 0.3%).

Fully reconstructed $B$ mesons, $B_{unc}$, are observed in the following decay modes: $B^+ \rightarrow D^{(*)+}\pi^+$, $\bar{D}^{(*)0}\rho^+$, $\bar{D}^{(*)0}a_1^+$ and $D^{(*)0}D_s^{(*)+}$ where $\rho^+$ is reconstructed in $\pi^+\pi^0$ mode ($|M_{\pi^+\pi^0} - M_{\rho^+}| < 0.3$ GeV/$c^2$) and $a_1^+$ is reconstructed as $a_1^+ \rightarrow \rho^0\pi^+$ ($|M_{\rho^0\pi^+} - M_{a_1^+}| < 0.25$ GeV/$c^2$). $\bar{D}^{(*)0}$ candidates are reconstructed as $\bar{D}^{(*)0} \rightarrow K^+\pi^-$, $K^+\pi^-\pi^0$, $K^+\pi^-\pi^+\pi^-$, $K_S^0\pi^0$, $K_S^0\pi^-\pi^+$, $K_S^0\pi^-\pi^+\pi^0$ and $K^-K^+$. $D^{(*)0}$ mesons are reconstructed by combining the $\bar{D}^{(*)0}$ candidates with a pion or a photon. The invariant mass of $\bar{D}^{(*)0}$ candidates is required to be within a $\pm 3$ MeV/$c^2$ (for $\bar{D}^{(*)0}\pi^0$) and $\pm 10$ MeV/$c^2$ (for $\bar{D}^{(*)0}\gamma$) intervals around the nominal $\bar{D}^{(*)0}$ mass. $D_s^{(*)}$ candidates are reconstructed in the decay modes $D_s^{(*)} \rightarrow K_s^0K^+$ and $K^+K^-$ $\pi^+$. The invariant mass of the $D_s^{(*)}$ candidates is required to be within $\pm 15$ MeV/$c^2$ interval.
around the nominal $D_s^+$ mass. $D_s^{*+}$ candidates are defined as $D_s^+\gamma$ combinations where the $D_s^+\gamma$ invariant mass lies in the interval $\pm 15$ MeV/c\(^2\) around the nominal $D_s^{*+}$ mass. Charged $B$ pair events are produced from $\Upsilon(4S)$ resonance ($\sqrt{s} \sim 10.58$ GeV), where the $B^+$ or $B^−$ is produced with specific momentum and energy. Selection of the fully reconstructed $B$ candidates is made according to the values of two variables: the beam-constrained mass $M_{bc} \equiv \sqrt{E_{\text{beam}}^2 - p_B^2}$ and the energy difference $\Delta E \equiv E_B - E_{\text{beam}}$. Here, $E_B$ and $p_B$ are the reconstructed energy and momentum of the fully reconstructed $B$ candidate in the center-of-mass (CM) system, and $E_{\text{beam}}$ is the beam energy in the CM frame. The signal region for tagging $B$ candidates is defined as $M_{bc} > 5.27$ GeV/c\(^2\) and $-80$ MeV $< \Delta E < 60$ MeV.

The $M_{bc}$ distribution of reconstructed $B$ candidates is fit with the sum of an Argus function [10] and a Crystal Ball function [11]. The Argus function models the continuum and combinatorial background whereas the Crystal Ball function models the signal component, which peaks at the $B$ mass. The purity is defined as $S/(S+B)$, where $S$ ($B$) is the number of signal (background) events for $M_{bc} > 5.27$ GeV/c\(^2\), as determined from a fit. Fig. 1 shows the $M_{bc}$ distribution for all $B_{\text{rec}}$ candidates in our data set in the signal $\Delta E$ region. In this sample, there are cross-feed effects between charged and neutral $B$. From the Monte Carlo simulation, we estimate the fraction of $B^0$ ($B^+$) events in the reconstruction of $B^+$ ($B^0$) to be 0.095 (0.090). Then, we obtain $N_{B^+B^-} = (4.00 \pm 0.24) \times 10^5$ and the purity of 0.55, where the uncertainty on $N_{B^+B^-}$ is dominated by systematic errors.

In the events where a $B_{\text{rec}}$ is reconstructed, we search for decays into a $\tau$ plus a neutrino and a $K$ plus two neutrinos. Candidate events are required to have one or three signal-side charged track(s) with the total charge being opposite to that of the reconstructed $B$. The $\tau$ lepton is identified in the following decay channels: $\tau^- \rightarrow \mu^- \nu \bar{\nu}$, $\tau^- \rightarrow e^- \nu \bar{\nu}$, $\tau^- \rightarrow \pi^- \nu$, $\tau^- \rightarrow \pi^− \pi^0 \nu$, and $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu$.

We require the charged particles to be identified as leptons, pions or kaons. The event is required to have zero net charge and $E_{\text{ECL}}$ less than 0.3 GeV where $E_{\text{ECL}}$ is the remaining energy calculated by adding the energy of the photons that are not associated with either the $B_{\text{rec}}$ or the $\pi^0$ candidate from $\tau^- \rightarrow \pi^- \pi^0 \nu$ decay. For all modes except $\tau^- \rightarrow \pi^- \pi^0 \nu$
We place the following requirements on the momentum of the track(s) in the CM, $p_{\pi^-} > 0.8 \text{ GeV}/c$ for $\tau^- \rightarrow \pi^- \nu$, $p_{\pi^-\pi^0} > 1.2 \text{ GeV}/c$ for $\tau^- \rightarrow \pi^-\pi^0\nu$, $p_{\pi^-\pi^+\pi^-} > 1.4 \text{ GeV}/c$ for $\tau^- \rightarrow \pi^-\pi^+\pi^-\pi^-$, and $p_K^- > 1.2 \text{ GeV}/c$ for $B^- \rightarrow K^-\nu\bar{\nu}$. The event is required to have the total missing momentum of the event to be greater than $0.2 \text{ GeV}/c$ for all modes except lepton-decay modes and the direction of missing momentum to be $-0.86 < \cos \theta^*_{\text{miss}} < 0.95$ in the CM frame. Further requirements are made on the invariant mass of two or three pions $|M_{\pi\pi} - M_\rho| < 0.15 \text{ GeV}/c^2$ and $|M_{\pi\pi\pi} - M_\omega| < 0.2 \text{ GeV}/c^2$. The selection efficiencies for each decay mode we consider in this analysis are determined from a large sample of GEANT-based Monte Carlo simulations \[12\] for $B^- \rightarrow \tau^-\nu\bar{\nu}$ and $B^- \rightarrow K^-\nu\bar{\nu}$ events generated by EvtGen decay package \[13\]. We compute the efficiency as the ratio of the number of events surviving each of our selections over the number of fully reconstructed $B^\pm$.

The most powerful variable for separating signal and background is the remaining energy $E_{ECL}$. We use different energy cuts for neutral clusters contributing to the $E_{ECL}$ for barrel part and end-cap parts since the effect of beam background is severe in the end-caps. For signal events the neutral clusters contributing to the $E_{ECL}$ can only come from beam background, therefore the signal events peaks at low $E_{ECL}$ and the background events, which contain additional sources of neutral clusters, are distributed toward higher $E_{ECL}$ values.

The $E_{ECL} < 0.3 \text{ GeV}$ region is defined as the signal region and the $0.45 < E_{ECL} < 1.5 \text{ GeV}$ region is defined as the sideband region. The $E_{ECL}$ shape in the MC distribution is used to extrapolate the sideband data to the signal region. The number of MC events in signal region and sideband are counted and their ratio ($r_{MC}$) is obtained. Using the number of data in the sideband and the ratio $r_{MC}$, the number of expected background events in the signal region is estimated. The background estimation for the different subdecay modes from the $E_{ECL}$ sideband extrapolation is shown in Table I. The numbers of events in sideband region agrees well between MC and data. To obtain the background expected from the MC simulation, $B\bar{B}$ and $e^+e^- \rightarrow u\bar{u}$, $d\bar{d}$, $s\bar{s}$, $c\bar{c}$ events are scaled to equivalent luminosity in data.

The double tag events, for which one of the $B$ mesons is fully reconstructed and the other $B$ meson is reconstructed in the set of decay modes $B^- \rightarrow D^0\ell^-\nu$, where $\ell$ is a muon or an electron and the $D^0$ is reconstructed in two modes: $D^0 \rightarrow K^+\pi^-$ & $K^+\pi^0\pi^+\pi^-$, are used as a control sample to validate the $E_{ECL}$ simulation. The sources affecting the $E_{ECL}$ in double-tagged events are similar to those affecting the $E_{ECL}$ distribution in the signal MC.

| Decay Mode | $r_{MC}$ | Sideband Data | Sideband MC | MC signal region | Expected BG |
|------------|---------|---------------|-------------|-----------------|-------------|
| $B^- \rightarrow \tau^-\nu\bar{\nu}$ | 0.17 | 70 | 63.9 ± 7.2 | 10.7 ± 2.8 | 11.8 ± 3.6 |
| $\tau^- \rightarrow e^-\nu\bar{\nu}$ | 0.14 | 67 | 62.3 ± 8.1 | 8.9 ± 2.6 | 9.5 ± 3.2 |
| $\tau^- \rightarrow \pi^-\nu$ | 0.07 | 47 | 48.4 ± 7.7 | 3.6 ± 1.6 | 3.5 ± 1.7 |
| $\tau^- \rightarrow \pi^-\pi^0\nu$ | 0.23 | 13 | 19.2 ± 4.0 | 4.4 ± 2.1 | 3.0 ± 1.8 |
| $\tau^- \rightarrow \pi^-\pi^+\pi^-$ | 0.23 | 16 | 23.0 ± 7.2 | 5.2 ± 2.5 | 3.6 ± 2.2 |
| $B^- \rightarrow K^-\nu\bar{\nu}$ | 0.15 | 17 | 18.9 ± 4.7 | 2.9 ± 1.4 | 2.6 ± 1.6 |

Table I: Expected background in the signal region for the different selection modes.
simulation. The agreement of the $E_{ECL}$ distribution between data and MC simulation for the double-tagged sample, in Fig. 2, is used as a validation of the $E_{ECL}$ simulation in the signal MC.

The main sources of uncertainty we consider in the determination of the $B(B^- \rightarrow \tau^- \nu)$ and $B(B^- \rightarrow K^-\nu\bar{\nu})$ are the number of $B^+B^-$ events with one reconstructed $B$, the determination of the signal efficiency and the determination of the number of expected background events. The number of $B^+B^-$ events is determined as the area of the Crystal Ball function fitted to the $M_{bc}$ distribution. Using a Gaussian function as an alternative fitting function, we obtain a relative change in the number of events and this difference is assigned as the systematic uncertainty on the number of $B^+B^-$ events. The main contribution to the systematic uncertainties in the determination of the efficiencies comes from uncertainty on tracking efficiency, Monte Carlo statistics and particle identification. The uncertainty in the expected background comes from Monte Carlo statistics and statistics of sideband data events. Estimates of systematic uncertainties are summarized in Table II.

After finalizing the signal selection criteria, the signal region ($E_{ECL} < 0.3$ GeV) in the on-resonance data is examined. Table III lists the number of observed events in data in the signal region, together with the expected number of signal and background events in the signal region. Fig. III shows the $E_{ECL}$ distributions in the data after all selection requirements except the one on $E_{ECL}$ have been applied compared with the expected background. Each distribution refers to a different mode.

Since we do not observe significant excess over the expected background, we set upper limits. To extract the upper limits on the branching fraction for $B(B^- \rightarrow \tau^- \nu)$ and $B(B^- \rightarrow K^-\nu\bar{\nu})$, we fit the observed $E_{ECL}$ distributions to the expected background and signal, using
| Source | Relative uncertainty (%) |
|--------|--------------------------|
| Number of $B^+B^-$ | 6.0 |
| tracking | 2.0 2.0 2.0 6.0 2.0 |
| $\tau$ decay BR | 0.3 0.3 1.0 0.6 1.1 |
| MC statistics | 0.6 0.6 0.7 1.0 2.0 4.1 |
| Lepton identification | 2.2 2.2 |
| $\pi^0$ identification | 2.6 |
| $\pi^{\pm}$ identification | 1.7 1.7 5.1 |
| Total Efficiency Uncertainty | 2.9 2.9 3.0 4.0 8.8 5.0 |
| MC statistics | 28.2 31.8 47.5 52.0 57.1 55.8 |
| Data in sideband | 12.0 12.2 14.6 27.2 25.0 24.3 |
| Total Background Uncertainty | 30.6 34.1 49.7 58.7 62.3 60.9 |

TABLE II: Systematic uncertainties for the number of $B^+B^-$ events with one reconstructed $B^-$, the determination of the efficiency and the determination of the number of expected background events for the different decay channels.

| Decay Mode | Signal Efficiency(%) | Signal Expected | Background Expected | Observed Events |
|------------|----------------------|-----------------|---------------------|-----------------|
| $B^{-} \rightarrow \tau^{-}\bar{\nu}$ | 9.8 ± 0.1 | 3.9 ± 0.1 | 11.8 ± 3.6 | 8 |
| $\tau^{-} \rightarrow \mu^{-}\nu\bar{\nu}$ | 9.4 ± 0.1 | 3.8 ± 0.1 | 9.5 ± 3.2 | 10 |
| $\tau^{-} \rightarrow e^{-}\nu\bar{\nu}$ | 8.4 ± 0.1 | 3.4 ± 0.1 | 3.5 ± 1.7 | 11 |
| $\tau^{-} \rightarrow \pi^{-}\nu$ | 3.5 ± 0.1 | 1.4 ± 0.1 | 3.0 ± 1.8 | 4 |
| $\tau^{-} \rightarrow \pi^{-}\pi^{0}\nu$ | 2.6 ± 0.1 | 1.0 ± 0.1 | 3.6 ± 2.2 | 6 |
| Total | 33.7 ± 1.4 | 13.5 ± 0.2 | 31.4 ± 5.9 | 39 |

TABLE III: Number of observed data events in the signal region, together with number of expected signal and background events. Errors in the background expectation is both statistical and systematic errors. The numbers of expected signal are obtained by assuming that $B(B^{-} \rightarrow \tau^{-}\bar{\nu}) = 10^{-4}$ and $B(B^{-} \rightarrow K^{-}\nu\bar{\nu}) = 4 \times 10^{-6}$. 
FIG. 3: \( E_{\text{ECL}} \) distributions in the data after all selection requirements except the one on \( E_{\text{ECL}} \) have been applied. The red histograms represent the distributions for Monte Carlo simulated signal events scaled to \( B(B^- \rightarrow \tau^- \nu) = 10^{-4} \) and \( B(B^- \rightarrow K^- \nu) = 4 \times 10^{-6} \).

maximum likelihood method. The likelihood function \( \mathcal{L} \) is defined as

\[
\mathcal{L} = \frac{1}{\sqrt{2\pi \sigma_b}} e^{-(n_b-N_b)^2/2\sigma_b} \cdot \frac{e^{-(n_s+n_b)}(n_s+n_b)^N}{N!} \prod_{i=1}^{N} \frac{n_s f_s(i) + n_b f_b(i)}{n_s + n_b}
\]

where \( n_b \) and \( n_s \) represent the number of background and signal events, respectively, \( N \) is the number of observed events, \( N_b \) is the calculated number of background events, and \( \sigma_b \) is the calculated background uncertainty. The variable \( f_s \) is the normalized signal \( E_{\text{ECL}} \) distribution and \( f_b \) is the normalized background \( E_{\text{ECL}} \) distribution. The negative log likelihood function is minimized using MINUIT [14] with respect to \( n_b \) for each \( n_s = \varepsilon_i \cdot N_{B^+B^-} \cdot B \). The 90% C. L. upper limit on the branching fraction \( B \) is calculated by

\[
0.9 = \frac{\int_0^{B_{90}} \mathcal{L}(B) dB}{\int_0^{\infty} \mathcal{L}(B) dB}
\]  

For \( B^- \rightarrow \tau^- \nu \), we calculate the likelihood function for each different decay mode (\( \mathcal{L}_i(B) \)). Total likelihood function is defined by

\[
\mathcal{L}(B) = \prod_{i=1}^{n_{\text{ch}}} \mathcal{L}_i(B)
\]

where \( n_{\text{ch}} \) is the number of decay modes for \( B^- \rightarrow \tau^- \nu \). The full systematic uncertainty must be incorporated into the likelihood function. We convolve the systematic uncertainty into the likelihood function, \( \mathcal{L}(B) \), by replacing each point of \( \mathcal{L}(B) \) by a Gaussian distribution
FIG. 4: Likelihood functions for the fit to data after smearing.

centered at that point with width $\Delta B$ which is determined from systematic uncertainty study. To get the value of a particular point of the smeared likelihood function, we integrate all the contributions from the Gaussian replaced points of the unsmeared likelihood function.

To combine likelihood functions of 5 decay modes for $B^- \to \tau^- \nu$, we simply multiply the likelihood functions to produce the combined likelihood. The only complication arises in that there are common sources of systematic uncertainty and therefore correlated uncertainties between the samples. We throw different normal Gaussian random number for correlated and uncorrelated systematics for each systematics sources. In this way, we can smear the correlated systematics in the same direction. We obtain the final smeared likelihood function by multiplying smeared likelihood functions for $B^- \to \tau^- \nu$. For $B^- \to K^- \nu \bar{\nu}$ decay, we smear the likelihood function by the total systematic uncertainty. Fig. 4 shows the likelihood functions for the fit to data after smearing for $B^- \to \tau^- \nu$ (left) and $B^- \to K^- \nu \bar{\nu}$ (right). We obtain upper limits on the branching fraction at the 90% (C.L.) of

$$B(B^- \to \tau^- \nu) < 1.8 \times 10^{-4}$$

$$B(B^- \to K^- \nu \bar{\nu}) < 3.6 \times 10^{-5}.$$  

In the extension of the Standard Model, one expects significant modification to the $B^- \to \tau^- \nu$ decay branching fraction. In the two-Higgs doublet model, the decay can occur via a charged Higgs particle. The $B^- \to \tau^- \nu$ branching fraction is given as

$$B(B^- \to \tau^- \nu) = B(B^- \to \tau^- \nu)_{SM} \times r_H,$$

where $r_H$ is defined as

$$r_H = \left(1 - \frac{\tan^2 \beta}{m_H^2} m_B^2\right)^2,$$

$m_H$ is the charged Higgs mass and $\tan \beta$ is the ratio of vacuum expectation values of two Higgs doublets [15]. $B(B^- \to \tau^- \nu)_{SM}$ represents SM contribution given by Eq. (1). Once
we get an upper limit on $\mathcal{B}(B^- \to \tau^- \nu)$, we can give a constraint on $\tan \beta$ and $m_{H^+}$. Fig. 5 shows the 90% C.L. exclusion boundaries in the $[m_{H^+}, \tan \beta]$ plane obtained with $m_B = 5279$ MeV/$c^2$ and $\mathcal{B}(B^- \to \tau^- \nu)_{\text{SM}} = 0.93 \times 10^{-4}$ from the CKMfitter prediction compared with other experimental searches at LEP\cite{16}, at the Tevatron\cite{17}, and at BABAR.

In conclusion, we have performed a search for the $B^- \to \tau^- \nu$ and $B^- \to K^- \nu \bar{\nu}$ decays in a fully reconstructed $B$ sample. Upper limits have been set:

$$\mathcal{B}(B^- \to \tau^- \nu) < 1.8 \times 10^{-4} \; (90\% \text{ C.L.}) \quad (8)$$

$$\mathcal{B}(B^- \to K^- \nu \bar{\nu}) < 3.6 \times 10^{-5} \; (90\% \text{ C.L.}) \quad (9)$$

which are the most stringent upper limits on these processes to date.

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