Intrinsic alignments in redMaPPer clusters – I. Central galaxy alignments and angular segregation of satellites

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ABSTRACT

The shapes of cluster central galaxies are not randomly oriented, but rather exhibit coherent alignments with the shapes of their parent clusters as well as with the surrounding large-scale structures. In this work, we aim to identify the galaxy and cluster quantities that most strongly predict the central galaxy alignment phenomenon among a large parameter space with a sample of 8237 clusters and 94817 members within 0.1 < z < 0.35, based on the redMaPPer cluster catalog constructed from the Sloan Digital Sky Survey. We first quantify the alignment between the projected central galaxy shapes and the distribution of member satellites, to understand what central galaxy and cluster properties most strongly correlate with these alignments. Next, we investigate the angular segregation of satellites with respect to their central galaxy major axis directions, to identify the satellite properties that most strongly predict their angular segregation. We find that central galaxies are more aligned with their member galaxy distributions in clusters that are more elongated and have higher richness, and for central galaxies with larger physical size, higher luminosity and centering probability, and redder color. Satellites with redder color, higher luminosity, located closer to the central galaxy, and with smaller ellipticity show a stronger angular segregation toward their central galaxy major axes. Finally, we provide physical explanations for some of the identified correlations, and discuss the connection to theories of central galaxy alignments, the impact of primordial alignments with tidal fields, and the importance of anisotropic accretion.

Key words: galaxies: clusters: general – large-scale structure of universe

1 INTRODUCTION

In the framework of the standard cold dark matter (CDM)-dominated Universe, cosmic structures grow hierarchically. Small galaxies form first, then merge and group together through channels of the filamentary network to form clusters of galaxies (White & Rees 1978; Blumenthal et al. 1984). During the process of structure formation, the distribution and orientation of galaxies may be set by the surrounding gravitational tidal fields, or be disturbed by activities such as mergers or feedback processes due to supernova or active galactic nuclei. In this work, we refer to any net preferred orientation toward some reference direction or any existing galaxy shape correlations caused by these physically-induced events as intrinsic alignments (in contrast with the coherent alignments induced by gravitational lensing). For recent reviews, see Joachimi et al. (2015), Kiessling et al. (2015) and Kirk et al. (2015).

Intrinsic alignments occur on a variety of scales. On large scales, several Mpc and above, galaxies show a net tendency to align radially towards overdensities (e.g., Mandelbaum et al. 2006; Hirata et al. 2007; Okumura et al. 2009; Joachimi et al. 2011), and more detailed analysis of the cos-

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mic web indicates coherent alignments along the stretching direction of filaments (Tempel et al. 2015; Chen et al. 2015c; Rong et al. 2016). One of the leading theoretical models for intrinsic alignments at large scales ($\gtrsim 6\,\text{Mpc}$) is the linear alignment model, which relates the alignment strength linearly to the smoothed tidal field at the time of galaxy formation (Catelan et al. 2001; Hirata & Seljak 2004), or variations of that model that include nonlinear evolution of the density field (Bridle & King 2007; Blazeck et al. 2015). Based on a sample of luminous red galaxies (LRGs), Singh et al. (2015) adopted the above alignment models to quantify the large-scale alignment amplitude as a function of several LRG properties. They found that the alignment amplitude becomes stronger toward more luminous LRGs residing in higher mass halos (see also Hirata et al. 2007; Joachimi et al. 2011).

On small scales, within galaxy clusters, there are two types of alignments. The first type is the alignment of satellite major axes toward the center of their host dark matter (DM) halo, for which the observational proxy usually is the brightest cluster galaxy (BCG). This is often called satellite (or radial) alignment. Satellite alignment is believed to originate from the tidal torque induced primarily from the gravitational field of the DM halo (Ciotti & Dutta 1994; Kuhlen et al. 2007; Pereira et al. 2008; Faltenbacher et al. 2008; Tenneti et al. 2015a). Observationally, the existence of satellite alignment is still controversial, with Pereira & Kuhn (2005); Agustsson & Brainerd (2006); Faltenbacher et al. (2007); Singh et al. (2015) reporting detections of the signal, while Hung & Ebeling (2012); Schneider et al. (2013); Chisari et al. (2014); Sifón et al. (2015) found no significant detection. Some of this tension may arise from selection effects, as discussed by Singh et al. (2015). In addition, Hao et al. (2011) cautioned about the possibility of spurious satellite alignment signals due to systematic errors (the contamination from the diffuse light from BCGs). We will report our measurement of satellite alignment in red-sequence Matched-filter Probabilistic Percolation (redMaPPer) clusters and present detailed systemic analysis in the upcoming Paper II. In the current paper, we focus on the second type of alignment, called central galaxy alignment.

Central galaxy alignment refers to the tendency of the major axis of the central galaxy to align with that of its host DM halo, for which the observational signature is that satellites (which we use as a tracer of the DM halo shape) preferentially reside along the central’s major axis direction. This type of alignment is also termed “BCG alignment” in the literature, as it is often assumed that the brightest galaxy within each cluster is the central galaxy (the central galaxy paradigm, see van den Bosch et al. 2005). However, Skibba et al. (2011) showed that 40%, and Hoshino et al. (2015) that 20-30%, of BCGs are not the galaxies that are located closest to the center of the cluster potential well. The fact that the redMaPPer algorithm identifies centrals not only based on their luminosity but also on their color and local galaxy density enables us to select a more robust set of central galaxies for our intrinsic alignment study. Therefore, through out this work, we will use the term “central galaxy alignment” for our result, and keep the term “BCG alignment” when referring to previous works that utilize the BCG as a proxy for the central galaxy.

Unlike satellite alignment, the observational evidence for central galaxy alignment is strong and uncontroversial (e.g., Sastry 1968; Binggeli 1982; Niederste-Ostholt et al. 2010), and it can be explained by two possible physical mechanisms. The first is the filamentary nature of matter accretion (Dubinski 1998), and the second is primordial alignment with the tidal field set by both the host dark matter halo and large-scale structure (Faltenbacher et al. 2008). Since central galaxy alignment is robustly detected with existing large datasets, many studies have investigated its dependence on physical predictors such as central galaxy luminosity, color, host halo mass, redshift, and so on, in order to better understand the physical origin of the effect (Brainerd 2005; Yang et al. 2006; Azzaro et al. 2007; Faltenbacher et al. 2007; Wang et al. 2008; Siverd et al. 2009; Agustsson & Brainerd 2010; Niederste-Ostholt et al. 2010; Hao et al. 2011). There is general agreement that the central galaxy alignment signal is stronger for red and luminous centrals, and shows higher significance when using red satellites as tracers. However, some controversies still remain about the importance of other predictors besides luminosity or color. Furthermore, some of the previous studies started with the assumption that only a few predictors could be important in determining the central galaxy alignments, and therefore performed an analysis based only on those predictors without considering others, ignoring potential degeneracies among predictors when splitting and comparing subsamples.

In Paper I, our goal is to present a comprehensive analysis of the predictors of central galaxy alignments. We include as many physical properties as possible, and properly account for potential correlations among them with the help of a linear regression analysis. We also discuss potential systematic effects based on signals obtained from various shape measurement methods. The two main questions we aim to address are 1) what central and cluster properties are the strongest predictors of the strength of central galaxy alignments? 2) What kinds of satellites are more likely to lie along the major axis direction of their host centrals? We build corresponding linear regression models, use variable selection techniques to select important predictors, and further quantify their significance. Finally, we discuss possible physical origins for these selected predictors and compare our result with the literature.

The paper is organized as follows. In Sec. 2, we describe our data and definitions of the physical quantities used in the linear regression analysis. Details of the linear regression process are described in Sec. 3. Sec. 4 presents our measurement of central galaxy alignment and results of the variable selection process. Sec. 5 discusses the detected central galaxy alignment signal for three different shape measurement methods, and the interpretation of those findings. The physical origins of our identified featured predictors for central galaxy alignments with the cluster shape and angular segregation of satellites with respect to the central galaxy major axis are discussed in detail in Secs. 6 and 7, respectively. We conclude and summarize our key findings in Sec. 8.

Throughout this paper, we adopt the standard flat ΛCDM cosmology with $\Omega_m = 0.3$ and $\Omega_{\Lambda} = 0.7$. All the length and magnitude units are presented as if the Hubble constant were 100 km s$^{-1}$ Mpc$^{-1}$. In addition, we use log as shorthand for the 10-based logarithm, and ln for the natural logarithm.
2 DATA AND MEASUREMENTS

In this section, we introduce the data that we analyze in this work, including the definitions of the galaxy cluster and galaxy properties that we use. All data used in this paper came from the Sloan Digital Sky Survey (SDSS) I/II surveys. The SDSS I (York et al. 2000) and II surveys imaged roughly \( \pi \) steradians of the sky, and followed up approximately one million of the detected objects spectroscopically (Eisenstein et al. 2001; Richards et al. 2002; Strauss et al. 2002). The imaging was carried out by drift-scanning in the photoometric conditions (Hogg et al. 2001; Ivezić et al. 2004), in five bands (ugriz) (Fukugita et al. 1996; Smith et al. 2002) using a specially-designed wide-field camera (Gunn et al. 1998). These imaging data were used to create the catalogs that we use in this paper. All of the data were processed by completely automated pipelines that detect and measure photometric properties of objects, and astrometrically calibrate the data (Lupton et al. 2001; Pier et al. 2003; Tucker et al. 2006). The SDSS-I/II imaging surveys were completed with a seventh data release (Abazajian et al. 2009), but we use the processed data from an improved data reduction pipeline that was part of the eighth data release, from SDSS-III (Aihara et al. 2011); and an improved photometric calibration (ubercalibration; Padmanabhan et al. 2008).

2.1 Galaxy cluster catalog

We use member galaxies in the redMaPPer v5.10 cluster catalog\(^1\) to study galaxy alignments in galaxy clusters. The redMaPPer cluster catalog is constructed based on photometric galaxy samples with a magnitude cut \( m_i < 21.0 \) from the SDSS data release eight (DR8; Aihara et al. 2011) over a total area of \( \sim 10,000 \) deg\(^2\). Details of the redMaPPer cluster finding algorithm and properties of the SDSS redMaPPer catalogs can be found in Rykoff et al. (2014); Rozo & Rykoff (2014); Rozo et al. (2015a,b). Briefly, the redMaPPer algorithm has two stages: the red-sequence calibration, and the cluster-finding stage. With a set of red spectroscopic galaxies as training sample, redMaPPer first constructs a redshift-dependent evolutionary red-sequence model, including zero-point, tilt, and scatter. The calibrated red-sequence model is then used to group red galaxies at similar redshifts into clusters, assuming certain radial and luminosity filters.

One of the features of the redMaPPer algorithm is that it is probabilistic, which enables users to select suitable samples to do statistics. For each cluster, it provides the central galaxy probability, \( P_{\text{cen}} \), for the top five potential BCGs, and all potential member galaxies are assigned with a membership probability, \( p_{\text{mem}} \), according to their color, magnitude, and position information. The photometric redshift \( z \) for each cluster is estimated from high-probability members; and the cluster richness, \( \lambda \), is defined by summing the membership probabilities over all cluster members.

In this work, we restrict our analysis to clusters with richness \( \lambda \geq 20 \), corresponding to a halo mass threshold of \( M_{200m} \geq 10^{14} \) h\(^{-1}\)M\(_{\odot}\) (Rykoff et al. 2012), and photometric redshift in the range \( 0.1 \leq z \leq 0.35 \). The lower redshift limit is selected so as to minimize edge effects from the training sample when doing calibration, while the upper redshift cutoff is set such that the sample of clusters is volume-limited (Rykoff et al. 2014). All in all, there are 10702 clusters within this redshift and richness range. To perform higher quality statistics, we only explore satellite galaxies with membership probability \( p_{\text{mem}} \geq 0.8 \) when doing linear regression analysis, and restrict to satellites with \( p_{\text{mem}} \geq 0.2 \) when defining cluster shape (while weighting those satellites appropriately by their values of \( p_{\text{mem}} \)).

2.2 Definitions and measurements of physical parameters

In this subsection, we describe many of the physical parameters that we will use to study central galaxy alignments.

2.2.1 Galaxy ellipticity

The galaxy ellipticity used for the majority of this work is corrected for the effect of the PSF using the red-Gaussianization shape measurement method (see Sec. 2.3 for detail). We use the components of the distortion \( e_1 \) and \( e_2 \) (Bernstein & Jarvis 2002) provided from the Reyes et al. (2012) (or R12) and Mandelbaum et al. (2005) (or M05) catalogs by fitting the 'atlas images' (Stoughton et al. 2002) in both \( r \) and \( i \) bands. The distortion can be related to the axis ratio \( b/a \) as

\[
(e_1, e_2) = \frac{1 - (b/a)^2}{1 + (b/a)^2} (\cos 2\alpha, \sin 2\alpha),
\]

where \( \alpha \) is the position angle of the major axis. The total galaxy distortion \( e \) is calculated as

\[
e = \sqrt{e_1^2 + e_2^2}
\]

2.2.2 Galaxy alignment angles

Once the galaxy position angle is known, we can assign each satellite its central galaxy alignment angle, \( \theta_{\text{cen}} \), and satellite alignment angle, \( \phi_{\text{sat}} \).

The central galaxy alignment angle \( \theta_{\text{cen}} \) is defined as the angle between the major axis of the central galaxy and the line connecting the central to the satellite galaxy; as illustrated in the left panel of Fig. 1. Calculating \( \theta_{\text{cen}} \) requires a viable shape measurement for the central galaxy (but not the satellites). Within the redshift range \( 0.1 \leq z \leq 0.35 \), there are 8237 centrals with shape measurements in the R12 catalog, resulting in 94817 central-satellite pairs with satellites that have \( p_{\text{mem}} \geq 0.8 \).

The satellite alignment angle \( \phi_{\text{sat}} \) is defined as the angle between the major axis of the satellite galaxy and the line connecting its center to the central, as shown in the right panel of Fig. 1. Calculating \( \phi_{\text{sat}} \) requires a shape measurement for the satellite galaxy. In this paper, we only consider \( \phi_{\text{sat}} \) as a potential predictor of central galaxy alignments; future work will include a detailed analysis of satellite alignments.

We restrict both \( \theta_{\text{cen}} \) and \( \phi_{\text{sat}} \) to the range \( [0^\circ, 90^\circ] \) due to symmetry. By definition, \( \theta_{\text{cen}} = 0^\circ/90^\circ \) indicates a satellite located along the major/minor axis of the central. A satellite is radially/tangentially aligned with the central if \( \phi_{\text{sat}} = 0^\circ/90^\circ \).

\(^1\) http://risa.stanford.edu/redmapper/
2.2.3 Cluster position angle and ellipticity

We follow the method used in Niederste-Ostholt et al. (2010) to define the orientation and ellipticity of the redMaPPer clusters from their satellite distributions. In order to have enough member galaxies to trace the shape of each cluster, we use all member galaxies with membership probability $p_{\text{mem}} \geq 0.2$. We calculate the reduced second moments from the positions of member galaxies, weighted by $p_{\text{mem}}$:

$$M_{\text{xx}} \equiv \left\langle x^2 \right\rangle = \frac{\sum p_{\text{mem,}i} x_i^2}{\sum p_{\text{mem,}i}},$$

and likewise for $M_{\text{yy}}$ and $M_{\text{xy}}$; by definition, $M_{\text{xx}} + M_{\text{yy}} = 1$. Here $x_i$ is the distance of member galaxy $i$ from the cluster center. We can then define the cluster ellipticity as

$$(Q, U) = \frac{1 - b/a}{1 + b/a} (\cos 2\beta, \sin 2\beta) = (M_{\text{xx}} - M_{\text{yy}}, 2M_{\text{xy}}),$$

where $b/a$ is the cluster projected minor-to-major axis ratio and $\beta$ is the cluster position angle (P.A.). The cluster ellipticity can then be calculated via

$$\epsilon = \sqrt{Q^2 + U^2}.$$  

2.2.4 Central galaxy dominance

The central galaxy dominance parameter is defined as the difference in the r-band absolute magnitude of the central galaxy and the mean magnitude of the first and second brightest satellites:

$$\text{Central dominance} \equiv \text{Central}^{0.1} M_r - \frac{0.1 M_{\text{r,1st}} + 0.1 M_{\text{r,2nd}}}{2}.$$  

We calculate the central galaxy dominance parameter using only $p_{\text{mem}} \geq 0.8$ members. For the very few clusters (134 out of 8237) that have only one member satisfying the $p_{\text{mem}} \geq 0.8$ criterion, we simply use the difference between the absolute magnitudes of central and that member galaxy to define the central galaxy dominance. Smaller central dominance values correspond to more dominant central galaxies.

2.2.5 Central galaxy probability

For each cluster, the redMaPPer catalog contains the five most likely central galaxy candidates, each with centering probability $P_{\text{cen}}$. In this paper, we use the most probable central as our central galaxy, and measure the central galaxy and satellite alignment angles of the associated central-satellite pairs. Over 80% of our centrals have $P_{\text{cen}} \geq 0.7$.

2.2.6 Galaxy absolute magnitude

We calculate the absolute magnitude for each galaxy using the luminous red galaxy (LRG) templates in the kcorrect package (v4.2) distributed by Blanton & Roweis (2007). The kcorrect software determines the best composite fit to the observed galaxy spectral energy distribution (SED) with the Chabrier (2003) initial mass function (IMF) and a variety of Bruzual & Charlot (2003) stellar population synthesis models differing in star formation histories and metallicities. We use extinction-corrected SDSS model magnitudes and the photometric redshift $z$ provided in redMaPPer as input, and k-correct the magnitudes of all galaxies in our sample to $z = 0.1$.

2.2.7 Galaxy effective radius

The effective radius we report in this paper is the circularly-averaged half-light radius, defined as

$$R_{\text{eff}} \equiv \sqrt{\frac{b}{a}} R_{\text{deV}}.$$  

where $b/a$ is the semi-minor to semi-major axis ratio taken from the SDSS parameter $\text{deVAB}_r$, and $R_{\text{deV}}$ is the semi-major half-light radius, $\text{devRad}_r$. Both parameters are estimated as part of the SDSS DR8 pipeline by fitting de Vaucouleurs light profiles to galaxy r-band images. Here we convert the value of $R_{\text{deV}}$ from the provided angular units to physical units ($h^{-1}\text{kpc}$), using the redshift $z$ of the host cluster.
2.2.8 Member distance from the cluster center

For each satellite galaxy, we compute its projected distance, \( r \), to the central galaxy, to check for radial dependence in the central galaxy alignment signal. To fairly compare among satellite galaxies in clusters with different halo masses, we further normalize \( r \) by the estimated halo radius, \( R_{200m} \), corresponding to the radius within which the average density of the enclosed mass is \( 200 \) times the mean density, \( \rho \). We first use the mass-richness relation provided in Eq. B4 of Rykoff et al. (2012),

\[
\ln \left( \frac{M_{200m}}{\, h_{70}^{-1} \, 10^{14} \, \text{M}_\odot} \right) = 1.72 + 1.08 \ln \left( \frac{\lambda}{0.08} \right),
\]

to estimate \( M_{200m} \). Then we compute \( R_{200m} \) via the definition \( M_{200m} = (4\pi/3) \, 200 \rho \, R_{200m}^3 \). Our conclusions would not change even if applying different mass-richness relations recently calibrated via weak lensing (Simet et al. 2016) or via clustering of clusters (Baxter et al. 2016).

2.2.9 Cluster member concentration \( \Delta_R \)

Recently, Miyatake et al. (2016) found that the average projected distance of member galaxies from the cluster center, defined as

\[
R_{\text{mem}} = \frac{\sum_i p_{\text{mem},i} R_i}{\sum_i p_{\text{mem},i}},
\]

not only describes the concentration of the member galaxy distribution in the cluster, but also plays a role in determining the large-scale clustering of redMaPPer clusters at fixed mass. Here \( p_{\text{mem},i} \) is the membership probability of the \( i \)-th member galaxy, and \( R_i \) is the physical separation between that galaxy and its corresponding cluster central galaxy.

To properly model the richness and redshift dependence in \( R_{\text{mem}} \), we use another parameter, \( \Delta_R \), defined in Eq. 22 of Baxter et al. (2016) as an indicator of cluster member concentration at fixed \( \lambda \) and \( z \):

\[
\Delta_R = \frac{\langle R_{\text{mem}} \rangle_{\lambda,z}}{\langle R_{\text{mem}} \rangle_{\lambda}}.
\]

Here \( \langle R_{\text{mem}} \rangle_{\lambda} \) is the mean \( R_{\text{mem}} \) value at a particular \( \lambda \) bin estimated by fitting a spline to the average value of \( R_{\text{mem}} \) in ten bins of \( \lambda \) and five bins of \( z \). By construction, negative \( \Delta_R \) value means the cluster has a more compact member galaxy distribution than the average cluster at that richness and redshift.

2.3 Galaxy shape data

In this work, we use 3 different galaxy shape measurement methods from 4 catalogs to determine the galaxy position angle and ellipticity, to investigate systematics in the measured central galaxy alignment signal. This section includes a description of all of these methods.

2.3.1 Re-Gaussianization shape measurement

The first shape measurement method is based on the re-Gaussianization technique (Hirata & Seljak 2003), which not only corrects the effects of the point spread function (PSF) on the observed galaxy shapes with a standard elliptical Gaussian profile, but also corrects for low-order deviations from Gaussianity in both the galaxy and PSF profiles.

Two shape catalogs generated using the re-Gaussianization technique are used in this work; the primary one is based on the SDSS DR8 photometric pipeline, and was presented in R12; however, for systematics tests we also use the catalog from M05, which was based on the DR4 photometric pipeline. The R12 catalog covers an area of 9432 deg\(^2\), with an average of \( 1.2 \) galaxies arcmin\(^{-2}\) with shape measurements; the M05 catalog covers an area of 7002 deg\(^2\). Both shape catalogs select galaxies down to the extinction-corrected r-band model magnitude \( m_r < 21.8 \), and require galaxies to be well resolved compared to the PSF size in both \( r \) and \( i \) bands. While there are minor differences in galaxy selection criteria in the catalogs, the main difference is the version of the SDSS photometric pipeline (photo) that they used. The M05 catalog relies on photo v5.4 (Adelman-McCarthy et al. 2006) while the R12 is based on photo v5.6 (Aihara et al. 2011). The new version of photo has a more sophisticated sky-subtraction algorithm that improves the photometry of large galaxies and fainter ones near them. By comparing the central galaxy alignment measured using these catalogs, we will estimate the impact of the sky-subtraction quality on the final results.

2.3.2 Isophotal shape measurement

Many previous central galaxy alignment studies used the SDSS isophotal position angle to define the orientation of the BCG (Brainerd 2005; Yang et al. 2006; Faltenbacher et al. 2007; Azzaro et al. 2007; Wang et al. 2008; Siverd et al. 2009; Agnostsson & Brainerd 2010; Hao et al. 2011). To compare with these studies, we also measure the central galaxy alignment using the isophotal shape measurement. The SDSS pipeline measures the isophotal position angle of galaxies at the isophote corresponding to 25 mag arcsec\(^{-2}\), which is fairly low surface brightness and generally encompasses a much larger part of the galaxy light profile than the centrally-weighted re-Gaussianization shapes.

Isophotal shapes were not released in DR8, so we take the isophotal position angle in \( r \) band from DR7 (using the previous version of photo) to compute central galaxy alignments.

2.3.3 De Vaucouleurs shape measurement

Some galaxy alignment studies use the shape measurement from the de Vaucouleurs model fit (Niederste-Ostholt et al. 2010; Siverd et al. 2009; Hao et al. 2011), which is a good description of the surface brightness profile for a typical elliptical galaxy, including most galaxies in redMaPPer clusters. Here we use the de Vaucouleurs fit position angle provided in the SDSS DR7, which fits galaxies through a two-dimensional fit to a PSF-convolved de Vaucouleurs profile. For more detail about these SDSS shape measurements, we refer readers to Stoughton et al. (2002).

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2.4 The central-satellite pair sample

We define three samples of central-satellite pairs for our analysis:

(i) After applying the redshift cut and requiring that central galaxies have shape measurements in the R12 catalog, we have 8237 centrals with DR8 re-Gaussianization shape measurement, and 94817 satellites with $r_{	ext{mem}} \geq 0.8$ in our parent sample. This parent sample is used for the majority of our analysis, while the other subsamples are used primarily for systematics tests.

(ii) To investigate the effect of the sky-subtraction technique on the measured central galaxy alignment signal, we match our parent centrals with the M05 catalog, and construct another sub-sample of centrals that have re-Gaussianization shape measurement based on both DR4 and DR8 photometry. This subsample has 4316 centrals and 46370 central-satellite pairs within the DR4 footprint.

(iii) To compare the degree of central galaxy alignment signal using different shape measurement methods, another subsample of central-satellite pairs is constructed. If we require centrals to have a DR8 re-Gaussianization shape, along with both isophotal and de Vaucouleurs shape measurements from DR7, we have 7488 centrals with 86350 satellites within the DR7 footprint.

Fig. 2 shows the distributions of the $r$-band absolute magnitude, $0.1 M_r$, of the centrals (left panel) and satellites (right panel) in these three sets of central-satellite pairs. Both the central and satellite $0.1 M_r$ distributions for the subsample in the DR7 footprint (iii) are almost the same as for the parent DR8 sample (i), while there are slight shifts for the subsamples in DR4 footprint (ii).

When measuring the central alignment angle, we only require satellite positions and central shape measurements. However, in the linear regression analysis, we require all galaxies to have well-defined physical parameters such as ellipticity, color, effective radius. . . ; these requirements eliminate some satellites, mainly due to the requirement of an ellipticity measurement. Table 1 summarizes the three sets of central-satellite pairs defined in this section, and also records the actual number of central-satellite pairs used when doing linear regression analysis.

In Fig. 3, we compare the absolute magnitude distributions of the satellite subsamples actually used in the linear regression analysis to that of the original set of satellites from which they were drawn. The selected satellites used in linear regression are biased to brighter magnitudes, since we rely on good quality photometry (higher $S/N$ and/or more resolved light profile) to measure shapes. For the reason, the derived significance levels for potential predictors that could possibly affect the degree of central galaxy alignment in this work are lower limits, especially for predictors that strongly correlate with satellite brightness. If the effect of a predictor on central galaxy alignment is strong enough, then even...
Table 1. Numbers of clusters and central-satellite pairs used in this work. The first three rows are the three subsamples we used for the overall measurement of the central galaxy alignment angle defined in Sec. 2.4. The last row is the subsamples used when doing linear regression analysis.

| Sample                  | N\textsubscript{cluster} | N\textsubscript{pair} |
|-------------------------|---------------------------|-----------------------|
| DR8 Footprint Sample    | 8237                      | 94817                 |
| DR4 Footprint Sample    | 4316                      | 46370                 |
| DR7 Footprint Sample    | 7488                      | 86350                 |
| Linear Regression Sample| 8233                      | 73146                 |

if some faint satellites are excluded when doing linear regression, we could still select the predictor out as a featured predictor.

3 LINEAR REGRESSION ANALYSIS

Regression is one of the most commonly used methods to study dependence. It is used to find optimal values of the free parameters in a specified function \( Y = f(X) + \epsilon \). Here \( Y \) is the response variable, which quantifies the physical effect one wants to study, \( X = (X_1, ... X_n) \) is a set of potential predictors that may affect the behavior of \( Y \), and \( \epsilon \) represents random observational error, usually assumed to be drawn from a normal distribution. For the central galaxy alignment effect, as there is no a priori-known functional form relating \( X \) to \( Y \), we apply \textit{multiple linear regression}, which allows one to at least determine if the central galaxy alignment depends on \( X \) to first order.

The multiple linear regression model we apply is

\[
Y = f(X) = \beta_0 + \beta_1 X_1 + \ldots + \beta_i X_i + \ldots + \beta_N X_N, \quad (11)
\]

where the intercept \( \beta_0 \) and the slopes \( \beta_i \) are the unknown regression coefficients to be estimated via least squares. For each regression coefficient \( \beta_i \), we perform the two-sided \( t \)-value and \( p \)-value tests for the dependence of \( Y \) on the \( X_i \). These are tests of the hypothesis that \( \beta_i = 0 \) against the alternative hypothesis that \( \beta_i \neq 0 \). The \( t \)-value is the ratio of \( \beta_i \) to its standard error, which can be positive or negative depending on the sign of \( \beta_i \). A larger \( |t| \) indicates a more significant statement that \( \beta_i \neq 0 \), which means it is more likely that there is a relationship between \( Y \) and \( X_i \). Statistically, the \( t \)-value and \( p \)-value are inextricably linked. Under the assumption of normally distributed errors, a \( p \)-value of 0.05 corresponds to a 95% confidence that \( \beta_i \) is not equal to zero. Thus we select out a regressor \( X_i \) as a featured predictor if its \( p \)-value < 0.05 (e.g., Weisberg 2013).

There are reasons not to use our predictors \( P_i \) defined in Sec. 2.2 (cluster ellipticity, central galaxy dominance, etc.) directly as regressors \( X_i \). Since there is a large variation in the range of each predictor, if we simply regress by \( Y = \beta_0 + \sum_i \beta_i' P_i \), the fitted magnitude of \( \beta_i' \) would depend on that range, i.e., for a given level of correlation between the parameters, \( \beta_i' \) would be small if its \( P_i \) tends to be large. To make our results more directly illustrate how the relative change of a physical parameter affects the value of \( Y \), throughout we normalize our predictors \( P_i \) to obtain regressors as follows:

\[
X_i = \frac{P_i - \langle P \rangle}{\sigma_{P_i}}. \quad (12)
\]

Here \( \sigma_{P_i} \) is the sample standard deviation of the predictor \( P_i \), reflecting the width of the intrinsic distribution and measurement error. We will use the term “predictor” to correspond to the original variables, and “regressor” to refer to variables that are transformed as in Eq. (12). We note, however, that using the normalized predictors as our regressors does not affect the result of hypothesis tests to select featured predictors.

In this work, we will build two multiple linear regression models with two different response variables, and use a total of 16 potential predictors to analyze the central galaxy alignment and the angular segregation of satellites. Details on the definitions and measurements of these physical parameters were presented in Sec. 2.2.

3.1 Response variables

The two response variables used to quantify the level of central alignment are: 1) the position angle difference between the central galaxy and its host cluster

\[
\Delta \eta = |P.A.\text{cen} - P.A.\text{cluster}|, \quad (13)
\]

and 2) the central galaxy alignment angle for each central-satellite pair, \( \theta_{\text{cen}} \). We use these in different ways as described below.

\( \Delta \eta \) lies in the range \([0^\circ, 90^\circ]\), where \( 0^\circ \) indicates that the central galaxy is perfectly aligned with the shape of the projected member galaxy distribution of the cluster. That distribution is believed to trace the underlying DM halo shape with some scatter (Evans & Bridle 2009; Oguri et al. 2010). The quantity \( \Delta \eta \) is thus an observable proxy for the level of central galaxy alignment with its DM halo. We will regress it onto central galaxy- and cluster-related predictors to identify what central galaxy properties and/or cluster properties most strongly predict the alignments of central galaxies with their satellite galaxy distributions.

The definition of \( \theta_{\text{cen}} \) is illustrated in the left panel of Fig. 1. It is a direct observable reflecting a satellite’s angular position with respect to the major axis direction of its central galaxy. With each satellite galaxy having its corresponding \( \theta_{\text{cen}} \) as the response variable, we will regress it onto individual satellite quantities to understand what kind of satellites are more preferentially located along the major axis of the central galaxy.

3.2 Potential predictors

We classify the 16 predictors into three categories: central-related, cluster-related and satellite-related quantities. Table 2 lists these predictors under each category.

**Central Galaxy Quantities:** We use six central galaxy related physical parameters: central galaxy dominance, \(0.1 M_e\), \(0.1 M^*\), \(0.1 M_e\), color, ellipticity, effective radius, and central probability. Since there is a tight correlation between the size and luminosity of galaxies (e.g., Bernardi et al. 2014), in order to investigate the effect of galaxy size on central galaxy alignments, we use the offsets in galaxy size from the fitted size-magnitude relation, \( \Delta \log(\text{central } R_e) \equiv \)
measured log(central $R_{\text{eff}}$) – predicted log(central $R_{\text{eff}}$), as our predictor when doing linear regression. The top panel of Fig. 4 shows the log(central $R_{\text{eff}}$)–central $0.1M_r$ correlations for the DR8 central galaxies. In the bottom panel, we present the log(central $R_{\text{eff}}$) residuals from the fitted log(central $R_{\text{eff}}$)–central $0.1M_r$ relation, as a function of central $0.1M_r$.

**Cluster Quantities:** We have four cluster-related physical parameters: log(richness), redshift, cluster ellipticity and cluster member concentration $\Delta B$.

**Satellite Quantities:** The six satellite-related quantities are the cluster-centric distance of each satellite normalized by its host $R_{200\text{m}}$, $0.1M_r$, $0.1M_o$,$0.1M_c$ color, ellipticity, effective radius, and the satellite alignment angle $\phi_{\text{sat}}$. As for the central galaxies, we use the residual effective radius, $\Delta \log(R_{\text{eff}})$, for satellites as our physical parameter instead of the directly measured $R_{\text{eff}}$, in attempt to eliminate the contribution of luminosity on size. We fit the log($R_{\text{eff}}$)$0.1M_r$ correlations for the the 73146 satellites as shown in the top panel of Fig. 5 first, and then use $\Delta \log(R_{\text{eff}}) \equiv$ measured log($R_{\text{eff}}$) – predicted log($R_{\text{eff}}$) as our new size predictor. The bottom panel of Fig. 5 shows the $\Delta \log(R_{\text{eff}})$ as function of $0.1M_r$.

![Figure 4](image.png)

Figure 4. The top panel shows the contour plot of log(central $R_{\text{eff}}$) versus central $0.1M_r$. The red dash line shows the least-squares fitting of a linear relationship between log(central $R_{\text{eff}}$) and central $0.1M_r$, with the equation of the best fitted line shown on the plot. The bottom panel plots the residuals versus central $0.1M_r$.

![Figure 5](image.png)

Figure 5. Similar to Fig. 4 but for cluster member galaxies instead of centrals.

### 3.3 Variable selection

The goal of variable selection (e.g., Burnham & Anderson 2003; James et al. 2013) is to identify the subset of predictors that are important within a large pool of potential predictors. There are many statistical methods for subset selection; we adopt the “Forward-Stepwise Selection” approach (See e.g., Sec. 3.3 of Friedman et al. 2001). Beginning with a model containing no predictor, forward-stepwise selection involves fitting $N$ models for the $N$ predictors separately: $Y = \beta_0 + \beta_1X_1$, and selects the regressor $X_p$ with the most significant hypothesis test on $\beta_p \neq 0$, i.e., greatest absolute t-value or smallest p-value. In the second cycle, $N-1$ models for the remaining $N-1$ predictors are fit via $Y = \beta_0 + \beta_pX_p + \beta_1X_1$, where $i \neq p$, and again we select the most significant regressor $X_p$. At each stage, one predictor is selected to add to the model until the remaining regressors have p-value > 0.05, which is a common stopping choice in many statistical packages. The forward stepwise algorithm therefore considers at most $N+(N-1)+\ldots+1 = N(N+1)/2$ models in the extreme case when all $N$ regressors have p-value < 0.05. We then fit a model using least squares on the reduced set of variables, and determine the final t- and p-values of the selected featured predictors.

To ensure the robustness of our variable selection scheme, we compare our variable selection result with another variable selection method – “Best-Subset Selection” – which considers all $2^N$ possible combinations of models from the $N$ predictors, and selects the best one based on a model-selection criterion, such as Mallow’s $C_p$ (Mallows 1973), Akaike information criterion (AIC, Akaike 1998), etc.
Table 2. The 16 potential predictors used to study the central galaxy alignment effect in this work.

| Central Galaxy Quantities | Cluster Quantities | Satellite Quantities |
|---------------------------|--------------------|---------------------|
| central galaxy dominance  | log(richness)      | log(r/R200a)        |
| central $0.1 M_\odot$    | redshift           | satellite $0.1 M_\odot$ |
| central $0.1 M_\odot - 0.1 M_\odot$ color | cluster ellipticity | satellite ellipticity |
| central ellipticity      | cluster member concentration $\Delta_R$ | $\Delta \log$ (satellite $R_{\text{eff}}$) |
| $\Delta \log(central\, R_{\text{eff}})$ | $P_{\text{cen}}$ | $\phi_{\text{sat}}$ |

Bayesian information criterion (BIC, Schwarz et al. 1978), or adjusted $R^2$. (By contrast, forward-stepwise selection is a so-called greedy algorithm – at each step, it selects only that one regressor that best improves the overall fit – and thus it can fail to uncover the optimal model. However, it does have the virtue of computational efficiency.) Different section criterion places different penalty on the complexity of the model. BIC penalizes heavier on models with more variables and hence tends to select smaller number of predictors, while adjusted $R^2$ puts less penalty thus results in selecting more predictors. In this work we use p-value < 0.05 as the criteria to pin down the total number of predictors in the forward-stepwise selection process, and this result agrees with that from best-subset selection under Mallow’s $C_p$, and AIC, validating our use of forward-stepwise selection with our dataset.

Throughout this work, we use the statistical package StatsModels in Python to do forward stepwise selection, and use the leaps package in R to perform best-subset selection.

In this work, we attempt to address two main questions: 1) What central galaxy and cluster properties are the strongest predictors of the strength of central galaxy alignments? 2) What kinds of satellites are more likely to lie along strongest predictors of the strength of central galaxy alignments: 1) What central galaxy and cluster properties are the strongest predictors of the strength of central galaxy alignments? 2) What kinds of satellites are more likely to lie along strongest predictors of the strength of central galaxy alignments:

$$\Delta \eta$$

To compare the effect of sky-subtraction algorithm on the signal, we use the sample of 4316 centrals in the DR4 footprint with re-Gaussianization shape measurements using both DR8 and DR4 photometry. The middle panel of Fig. 6 shows the $\Delta \eta$ distributions of this sample, with the light (dark) green dots indicating measurements based on the DR4 (DR8) photometry. Within the error bars, the two $\Delta \eta$ distributions and their mean ($\langle \Delta \eta \rangle$) values are consistent with each other. We therefore conclude that for the re-Gaussianization shapes, the effect of sky-subtraction does not substantially influence the overall distribution of $\Delta \eta$. However, this conclusion may not be applicable for other shape measurement methods that trace different regions on the surface brightness profile of galaxies. Re-Gaussianization shapes are weighted more toward the inner part of the light profile, which is less sensitive to sky subtraction errors, while isophotal shapes are more sensitive to the outer part and could have more systematics due to sky subtraction. However, due to the lack of isophotal shapes in DR8, we cannot test this effect by comparing different data reductions.

To investigate the effect of shape measurement methods on the detection of central galaxy alignments, we use the sample of 7488 BCGs that have re-Gaussianization, de Vaucouleurs, and isophotal shape measurements in DR7 footprint. The right panel of Fig. 6 shows the $\Delta \eta$ distributions of these samples, with the red, orange, and yellow dots representing shape measurements based on the re-Gaussianization method, de Vaucouleurs fit, and isophotal fit, respectively. Within the error bars, the second and third distributions agree, while the $\Delta \eta$ distribution measured using the re-Gaussianization method differs systematically. The value of $\langle \Delta \eta \rangle$ using the re-Gaussianization method ($35.07^\circ \pm 0.28^\circ$) is significantly larger than that calculated by de Vaucouleurs ($33.34^\circ \pm 0.29^\circ$) and isophotal shapes, then centrals also tend to align with their underlying halos.

The left panel of Fig. 6 is the $\Delta \eta$ distribution of the 8237 centrals measured by the re-Gaussianization method in DR8. The average $\langle \Delta \eta \rangle$ for parent dataset is $\langle \Delta \eta \rangle = 35.07^\circ \pm 0.28^\circ$; this represents our primary result in this section, with the remaining results serving as systematics tests.

| Variable | Description |
|----------|-------------|
| $\Delta \log(central\, R_{\text{eff}})$ | $P_{\text{cen}}$ |

4 RESULTS

In this section, we report the results of an analysis of central galaxy alignments, including our linear regression analysis.

4.1 Overall signal

4.1.1 Distribution of $\Delta \eta$

We begin with a basic analysis of the properties of central galaxy alignments. Fig. 6 shows the distributions of the position angle difference between the central galaxy and cluster shapes, $\Delta \eta$, for our three cluster samples tabulated in Table 1, defined for the purpose of investigating systemics in various shape measurement techniques. The distributions show a highly significant degree of central galaxy alignment with cluster orientations. The bottom left corner of each panel shows the average $\Delta \eta$ value, $\langle \Delta \eta \rangle$, for each sample; they are all $\langle \Delta \eta \rangle < 45^\circ$ at high significance. Hence, if indeed the satellite galaxy distributions trace the dark matter halo shapes, then centrals also tend to align with their underlying halos.

The left panel of Fig. 6 is the $\Delta \eta$ distribution of the 8237 centrals measured by the re-Gaussianization method in DR8. The average $\langle \Delta \eta \rangle$ for parent dataset is $\langle \Delta \eta \rangle = 35.07^\circ \pm 0.28^\circ$; this represents our primary result in this section, with the remaining results serving as systematics tests.

To compare the effect of sky-subtraction algorithm on the signal, we use the sample of 4316 centrals in the DR4 footprint with re-Gaussianization shape measurements using both DR8 and DR4 photometry. The middle panel of Fig. 6 shows the $\Delta \eta$ distributions of this sample, with the light (dark) green dots indicating measurements based on the DR4 (DR8) photometry. Within the error bars, the two $\Delta \eta$ distributions and their mean ($\langle \Delta \eta \rangle$) values are consistent with each other. We therefore conclude that for the re-Gaussianization shapes, the effect of sky-subtraction does not substantially influence the overall distribution of $\Delta \eta$. However, this conclusion may not be applicable for other shape measurement methods that trace different regions on the surface brightness profile of galaxies. Re-Gaussianization shapes are weighted more toward the inner part of the light profile, which is less sensitive to sky subtraction errors, while isophotal shapes are more sensitive to the outer part and could have more systematics due to sky subtraction. However, due to the lack of isophotal shapes in DR8, we cannot test this effect by comparing different data reductions.

To investigate the effect of shape measurement methods on the detection of central galaxy alignments, we use the sample of 7488 BCGs that have re-Gaussianization, de Vaucouleurs, and isophotal shape measurements in DR7 footprint. The right panel of Fig. 6 shows the $\Delta \eta$ distributions of these samples, with the red, orange, and yellow dots representing shape measurements based on the re-Gaussianization method, de Vaucouleurs fit, and isophotal fit, respectively. Within the error bars, the second and third distributions agree, while the $\Delta \eta$ distribution measured using the re-Gaussianization method differs systematically. The value of $\langle \Delta \eta \rangle$ using the re-Gaussianization method ($35.10^\circ \pm 0.30^\circ$) is significantly larger than that calculated by de Vaucouleurs ($33.34^\circ \pm 0.29^\circ$) and isophotal shapes, then centrals also tend to align with their underlying halos.
Figure 6. Distributions of the position angle difference between central galaxy and cluster, $\Delta \theta = |P.A._{cen} - P.A._{cluster}|$. The left panel shows the $\Delta \theta$ distribution of the parent 8237 centrals measured by the re-Gaussianization method in DR8. The middle panel plots the $\Delta \theta$ distributions of the 4316 centrals which are both measured by the re-Gaussianization method in the DR4 footprint, with the light (dark) green dots representing measurements based on the DR4 (DR8) photometry. The right panel shows the $\Delta \eta$ distributions of the 7488 centrals in DR7 footprint measured by re-Gaussianization (red dots), de Vaucouleurs (orange dots), and isophote (yellow dots) methods respectively. Points are slightly shifted horizontally for clarity. Error bars indicate the standard error of the mean. The horizontal black dashed line indicates the case where the position angle of the central is the same as that of its cluster. The blue dot-dashed lines delineate a region where the $\Delta \theta$ values are consistent with the random orientation of the cluster.

Figure 7. Comparison between the position angles of cluster and central galaxy. The blue dashed line indicates the case where the position angle of the central is the same as that of its cluster. The two blue dot-dashed lines delineate a region where the P.A. differences between the cluster and central galaxy are less than 45°. The overall distribution peaking around the symmetric axis of the figure, we observe the preference for centrals pointing toward the orientation directions of clusters.

4.1.2 Distribution of $\theta_{cen}$

Fig. 8 shows the distributions of the central galaxy alignment angle, $\theta_{cen}$, for our three sets of central-satellite pairs. The preferential alignment of satellites along the central galaxy major axis is quantified in the average central galaxy alignment angle, $\langle \theta_{cen} \rangle$, in the bottom left corner of each panel. The alignment signal looks less dramatic as revealed in $\langle \theta_{cen} \rangle$ value compared with $\langle \Delta \eta \rangle$ shown in Fig. 6. This is because $\theta_{cen}$ records the individual location of each satellite with respect to its central galaxy major axis; these tend to be more randomized than simply considering the overall satellite distribution as a whole.

The left panel of Fig. 8 shows the $\theta_{cen}$ distribution of the 94817 central-satellite pairs measured by the re-Gaussianization method in DR8. The average central galaxy alignment angle for this dataset is $\langle \theta_{cen} \rangle = 41.42^\circ \pm 0.08^\circ$.

The middle panel shows the $\theta_{cen}$ distributions for the 46370 central-satellite pairs in the DR4 footprint, using DR8 (dark green) and DR4 (light green) photometry, constructed to compare the effect of sky-subtraction technique on the measurement of $\theta_{cen}$. Within the error bars, the two $\theta_{cen}$ distributions and the derived $\langle \theta_{cen} \rangle$ values are consistent with each other. As for $\Delta \eta$, we conclude that for the re-Gaussianization shapes, use of different SDSS photometry pipelines does not influence the results, but caution that this argument may not hold for other shape measurement methods.

To fairly compare our $\theta_{cen}$ measurement with studies based on different shape measurement methods, the right

$P.A. \ [\text{degree}]$

$\Delta \eta \ [\text{degrees}]$

$\langle \Delta \eta \rangle = 35.07 \pm 0.28$

$\langle \Delta \eta \rangle = 35.87 \pm 0.39$

$\langle \Delta \eta \rangle = 35.85 \pm 0.39$

$\langle \Delta \eta \rangle = 35.07 \pm 0.28$

$\langle \Delta \eta \rangle = 35.87 \pm 0.39$

$\langle \Delta \eta \rangle = 35.85 \pm 0.39$

$\langle \Delta \eta \rangle = 35.07 \pm 0.28$

$\langle \Delta \eta \rangle = 35.87 \pm 0.39$

$\langle \Delta \eta \rangle = 35.85 \pm 0.39$
Figure 8. Distributions of the central galaxy alignment angle. The left panel shows the $\theta_{\text{cen}}$ distribution of the 94817 central-satellite pairs measured by the re-Gaussianization method in DR8. The middle panel shows the $\theta_{\text{cen}}$ distributions of the 46370 central-satellite pairs measured by re-Gaussianization in both DR8 photometry (dark green) and DR4 photometry (light green), within the DR4 footprint. The right panel shows the $\theta_{\text{cen}}$ distributions of the 86350 central-satellite pairs in DR7 that are measured by re-Gaussianization (red dots), de Vaucouleurs (orange dots), and isophote (yellow dots) methods respectively. Points are slightly shifted horizontally for clarity. Error bars are represented by the standard error of the mean. The horizontal black dash line indicates the case if satellites were isotropically distributed around centrals. The mean central galaxy alignment angle, $\langle \theta_{\text{cen}} \rangle$, is shown at the bottom left corner of each panel.

The panel of Fig. 8 shows $\theta_{\text{cen}}$ measured via re-Gaussianization (red dots), de Vaucouleurs (orange dots), and isophotal shapes of the 86350 central-satellite pairs in the DR7 footprint. Within the error bars, the histograms of $\theta_{\text{cen}}$ using de Vaucouleurs and isophotal shapes are consistent with each other, but that for re-Gaussianization method is systematically different, resulting in a systematically higher $\langle \theta_{\text{cen}} \rangle$ (41.40° ± 0.09°). We will discuss the measurement difference in Sec. 5.

4.2 Linear regression: central galaxy alignments with satellite distributions

To investigate the alignment of the central galaxy with its dark matter Halo, we use our observational proxy (the difference in central and cluster position angles, $\Delta \eta$) as the response variable, and apply forward-stepwise selection described in Sec. 3.3 to select featured predictors among the central- and cluster-related quantities. The list of predictors is defined in Sec. 3.2, with the observational method for determining them in Sec. 2.2.

Fig. 9 displays the scatterplot matrix between $\Delta \eta$ and all of the central- and cluster-related predictors based on the re-Gaussianization shape measurement. The diagonal panels are histograms of physical parameters, and the other panels are scatterplots between pairs of parameters, with the corresponding correlation coefficient noted on each plot.

Several important results are evident in this scatterplot matrix. First, the top row summarizes how $\Delta \eta$ is related to all ten predictors. The sign of the correlation coefficient reveals the direction of the relationship between $\Delta \eta$ and the regressor, while the magnitude of the correlation coefficient indicates the strength of this dependence. The overall impression is that $\Delta \eta$ is weakly related to most of the predictors, with a maximum correlation coefficient of $\sim -0.2$ with cluster ellipticity. Though the correlations are weak, we can still judge whether these dependences are statistically significant given our large sample size. Second, some of the predictors are highly correlated with each other, such as central galaxy $0.1 M_\odot$, central galaxy dominance and $P_{\text{cen}}$. The forward-stepwise selection procedure will help determine whether we should keep them all as featured predictors; if any are jointly responsible for the same variation in $\Delta \eta$, then we will select just the most representative one among them.

After performing forward-stepwise selection, we find that cluster ellipticity is the most dominant predictor for the central galaxy alignment effect, and almost all of the central-related quantities are selected as feature predictors except for cluster ellipticity. The relationship between central galaxy ellipticity and the central galaxy alignment signal is more complicated. We will provide further investigation in Sec. 6.5.

Table 3. Selected featured predictors for the central galaxy-cluster alignment effect based on the 8233 DR8 clusters. The first column is the name of the selected predictor. The second column gives the regression coefficient $\beta$. Columns 3 and 4 provide the $t$- and $p$-values from the significance tests on the deviation of $\beta$ from zero. Higher $|t|$ or smaller $p$ indicates a higher significance for $\beta \neq 0$. Columns 5 and 6 are the mean and standard deviation of the corresponding predictor for the 8233 clusters, necessary in Eq. (12) to normalize our predictor $P_i$ to regressor $X_i$.

| Predictor   | $\beta$ | t-value | p-value | mean  | $\sigma$ |
|-------------|---------|---------|---------|-------|---------|
| cluster $e$ | -4.91   | -17.8   | 8.0 $\times 10^{-70}$ | 0.21  | 0.11    |
| $\Delta \log(\text{cen. R}_{\text{off}})$ | -2.67   | -9.7    | 6.0 $\times 10^{-22}$ | 0.00  | 0.15    |
| cen. $0.1 M_\odot$ | 2.42   | -7.8    | 9.0 $\times 10^{-15}$ | -22.30 | 0.47    |
| cen. color | -1.29   | -4.6    | 4.0 $\times 10^{-5}$  | 0.97  | 0.08    |
| $P_{\text{cen}}$ | -1.21   | -4.0    | 6.0 $\times 10^{-5}$  | 0.87  | 0.17    |
| cen. $e^1$ | -1.03   | -3.7    | 0.00002 | 0.26  | 0.16    |
| log(richness) | -0.65   | -2.2    | 0.03     | 1.48  | 0.15    |

The relationship between central galaxy ellipticity and the central galaxy alignment signal is more complicated. We will provide further investigation in Sec. 6.5.

MNRAS 000, 1–26 (2016)
Figure 9. Scatterplot matrix of the position angle difference between central and cluster shapes, $\Delta \eta$, with the ten central- and cluster-related predictors. The correlation coefficient between each pair of parameters is noted on the plot. We highlight scatterplots with correlations that are significant at $>10\sigma$ in yellow. The gray contour levels indicate 20%, 40%, 70%, and 95% number of clusters of our data.

for central galaxy dominance. The linear regression results, including the statistical significance of each selected predictor, are in Table 3, and the estimated best-fitting equation is:

$$
\Delta \eta = 35.07 - 4.91 \frac{\text{cluster } e}{0.11} - 2.67 \frac{\Delta \log(\text{cen. } R_{200}) - 0.00}{0.15} + 2.42 \frac{\text{cen. } 0.1 M_r + 22.30}{0.47} - 1.29 \frac{\text{cen. color} - 0.97}{0.08} - 1.21 \frac{P_{\text{cen}} - 0.87}{0.17} - 1.03 \frac{\text{cen. } e - 0.26}{0.16} - 0.65 \frac{\log(\text{richness}) - 1.48}{0.15}
$$

MNRAS 000, 1–26 (2016)
Here we note that since the relation between $\Delta \eta$ and these selected predictors is not truly linear and has substantial stochasticity, we cannot rely on the resulting regression equation to predict the value of $\Delta \eta$ for any given cluster. We can only use Eq. (14) to understand the sign and approximate strength of the variation of $\Delta \eta$ with those predictors to first order. Therefore, based on the trend of Eq. (14), we find that central galaxy alignment effects are strongest for clusters that are more elongated and higher richness, or clusters that have centrals with larger physical size, brighter absolute magnitude, redder color, larger ellipticity\(^2\), and a higher centering probability.

### 4.3 Linear regression: angular segregation of satellite galaxies

In Sec. 4.2, we used the positions of satellite galaxies weighted by their membership probabilities to trace the cluster and underlying halo shape, without any consideration of individual satellite properties. However, satellite galaxies with different properties are known to be distributed in different ways within clusters, a phenomenon known as segregation (e.g., van den Bosch et al. 2016). Segregation is often discussed in terms of the radial direction to the cluster center. Here we investigate angular segregation with respect to the central galaxy major axis, to understand what satellite properties most strongly predict the satellite tendency to lie along the central galaxy major axis.

Fig. 10 shows the scatterplot matrix of $\theta_{\text{cen}}$ versus the six satellite-related quantities for the 73146 DR8 central-satellite pairs. The top row displays scatterplots between $\theta_{\text{cen}}$ and all other satellite quantities. Compared with Fig. 9, the absolute magnitudes of the correlation coefficients of $\theta_{\text{cen}}$ with these satellite quantities are generally smaller than the correlation between $\Delta \eta$ and central and cluster quantities. Although the correlations are weak, the large number of pairs means there is still enough statistical power to measure these correlations robustly. In general, the relationships between all pairs of predictors appear to be weak, except for $0.1^0 M_\odot$ and ellipticity, with a correlation coefficient of $0.236$. The lower right corner shows the distribution of $\phi_{\text{sat}}$, which is very close to flat, indicating that satellite radial alignment is a far weaker phenomenon compared to central galaxy alignments; we explore this phenomenon in more detail in future work.

Given that we already identified the important central galaxy- and cluster-related predictors that affect the central galaxy alignment signal, it is reasonable to include these predictors in our linear regression analysis in order to compensate for their influence on the angular segregation of satellites. Table 4 shows the results of linear regression, with the new selected satellite quantities on top and the already-known central galaxy and cluster quantities on the bottom. Almost all previously-selected quantities have an associated $p$-value below 0.05 when using $\theta_{\text{cen}}$ as the response variable, except for cluster richness $\lambda$. This may be due to the fact that higher richness clusters tend to be rounder (as revealed in the last row of Fig. 9), and thus have their member galaxies less segregated toward any specific direction. Also, although the regression slope for log(richness) is positive, we cannot infer that satellites in lower richness clusters tend to be more segregated (i.e. having smaller $\theta_{\text{cen}}$). The level of angular segregation against richness is not significant enough for us to make such a conclusion. The best-fitted linear regression equation with these predictors is

$$
\theta_{\text{cen}} = 41.60 - 0.66 \frac{\text{sat. color} - 0.91}{0.09} + 0.54 \frac{\text{sat. } 0.1^0 M_\odot + 20.46}{0.76} + 0.21 \frac{\log(r/R_{\text{200m}}) + 0.87}{0.32} + 0.20 \frac{\text{sat. } e - 0.43}{0.26}
- 2.52 \frac{\text{cluster } e - 0.21}{0.11} - 0.64 \frac{\Delta \log(\text{cen. } R_{\text{eff}}) - 0.02}{0.15} + 0.58 \frac{\text{cen } 0.1^0 M_\odot + 22.35}{0.49} - 0.28 \frac{\text{cen color} - 0.98}{0.07} - 0.46 \frac{\text{cen } e - 0.25}{0.16} + 0.09 \frac{\log(\text{richness}) - 1.58}{0.21}
$$

The tendency of satellites to reside along the central galaxy major axis is strongest for satellites that are redder, brighter, rounder, and located closer to the central.

### 5 THE EFFECT OF SHAPE MEASUREMENT METHOD ON THE CENTRAL GALAXY ALIGNMENT SIGNAL

In the rightmost panels of Figs. 6 and 8, we compared the distributions of our response variables, $\Delta \eta$ and $\theta_{\text{BCG}}$, using three different shape measurements methods. In both cases, the level of central galaxy alignment measured via de Vaucouleurs and isophotal shapes agree with each other within the error bar, while the re-Gaussianization measurement gives us a less strong central galaxy alignment effect.

---

\(^2\) As we will demonstrate later in Sec. 6.5, the dependence on central galaxy ellipticity is actually more complicated than this simple linear regression result indicates.
In this section, we discuss the interpretation of this result in terms of systematic and physical effects in these shape measurements. Our discussion also relies on results of Singh & Mandelbaum (2015), who analyzed the effect of these three shape measurement methods on the inferred galaxy alignments of luminous red galaxies (LRGs).

5.1 Systematic error

Different shape measurements deal with the effects of the PSF on galaxy images differently. The re-Gaussianization technique was designed for weak lensing studies requiring the most complete removal of the PSF effect on galaxy shapes. The de Vaucouleurs shape measurement only partially corrects for the PSF by using a double-Gaussian fit instead of the full PSF model, while the isophotal shape measurement does not correct for the effect of the PSF explicitly.
Another relevant aspect of systematics has to do with what part of the light profile is used for the measurement. The re-Gaussianization method has an elliptical Gaussian weight function, emphasizing the central regions of the profile. The de Vaucouleurs profile includes both the central region and the large-scale wings of the light profile, while the isophotal shape measurement only uses the 25 mag/arcsec² isophote which is quite far out in the wings. These choices could make the latter two methods more sensitive to sky subtraction systematics than the re-Gaussianization method (for more discussion in the context of the isophotal method, see Hao et al. 2011).

One could infer that isophotal shapes would contain severe systematics due to the PSF. However, the results of Singh & Mandelbaum (2015) suggest that the impact of the PSF on the shape measured at very low surface brightness is quite small. Instead, the de Vaucouleurs shapes exhibited the most significant systematic errors of the three methods. Therefore, we may treat the detected differences in the central galaxy alignment strength between the re-Gaussianization and isophotal shapes as reflecting a true physical effect that we will discuss below. However, we should keep in mind that the systematic tests in Singh & Mandelbaum (2015) were based on a specific sample of galaxies, while our central galaxy sample (which is preferentially located in regions of high galaxy density) may still suffer from some contamination in the isophotal shapes, as suggested by Hao et al. (2011).

5.2 Physical effect

The higher apparent degree of central galaxy alignment using isophotal shapes compared to that using re-Gaussianization shapes may be primarily due to a mechanism called “isophote twisting” (di Tullio 1978, 1979; Korremedy 1982; Romanowsky & Kochanek 1998; Lauer et al. 2005). The physical origin of this effect is that the outer part of the galaxy light profile may respond more strongly to tidal fields than the inner part of the galaxy. Thus, by tracing the outermost isophote of the galaxy, the isophotal shape records the highest level of alignment with the tidal field.

6 THE ORIGIN OF CENTRAL GALAXY ALIGNMENT

In Sec. 4.2 we applied linear regression analysis to the nine central galaxy and cluster quantities, and picked the predictors that significantly influence the alignment between central galaxy and its host cluster. We now address the origin of this alignment phenomenon and compare our results with previous studies.

6.1 Dependence on cluster ellipticity

Simulations have revealed that clusters are triaxial rather than spherical (Jing & Suto 2002; Hopkins et al. 2005; Kanon & Evrard 2005; Allgood et al. 2006; Hayashi et al. 2007), so they look elongated when projected on the sky. The last panel in the second last row of Fig. 9 shows the distribution of projected redMaPPer cluster ellipticities traced by the weighted member galaxy distribution (see Sec. 2.2.3 for definition of cluster ellipticity), with a mean cluster ellipticity of ~0.20 and a mean projected semi-minor to semi-major axis ratio of ⟨b/a⟩ ~ 0.67, which agrees with the N-body simulation of Hopkins et al. (2005) (⟨b/a⟩ ~ 0.67, at redshift zero), but is rounder than that directly measured through gravitational lensing (⟨b/a⟩ ~ 0.48 ± 0.09 in Evans & Bridle 2009, and ⟨b/a⟩ ~ 0.46 ± 0.04 in Oguri et al. 2010).

As shown in Table 3, we find that cluster ellipticity has the most significant influence on the central galaxy alignment signal, with centrals in more elongated clusters having a stronger alignment with the orientation of their host clusters (see also the second-to-last panel in the first row of Fig. 9, which directly displays the correlation between cluster ellipticity and central galaxy alignment). Since the position angle for round clusters is not very meaningful, particularly given observational noise, we have examined the correlation trend for clusters with ellipticity > 0.2, and found the trend that more elongated clusters show stronger alignment still holds.

The influence of cluster ellipticity on central galaxy alignment can be further visualized in the left panel of Fig. 11, where we plot the distribution of the ⟨p_mem⟩-weighted averaged central galaxy alignment angle for all p_mem > 0.2 central-satellite pairs in each cluster, ⟨θ_cl⟩ = Σ_i p_mem,i p_i, against the cluster ellipticity. The sharp boundary on each side is due to the way we define cluster ellipticity. Since we calculate cluster ellipticity via the satellite galaxy distribution, round clusters (with satellites distributed in an almost circularly symmetric way) thus have ⟨θ_cl⟩ ≈ 45°. More elongated clusters have more potential for going to lower or higher ⟨θ_cl⟩ values. At fixed cluster ellipticity, the distribution of ⟨θ_cl⟩ tends to cluster towards the edges of the minimum and maximum available values. As a demonstration, the right panel of Fig 11 shows the results of simulating two fake clusters with fake member galaxies distributed with elliptical symmetry such that the two clusters would have measured cluster ellipticity of 0.5 (green) and 0.3 (red). We then randomized the P.A. of the simulated central galaxies, and calculated the corresponding ⟨θ_cl⟩ value. From the scatter plot and histograms of P.A. central vs. ⟨θ_cl⟩, it is clear that the relationship between central galaxy P.A. and ⟨θ_cl⟩ is non-linear, and that this non-linearity is responsible for the shape of the left panel of Fig. 11. However, with more clusters distributed on the ⟨θ_cl⟩ < 45° side across the full cluster ellipticity range shown in the left panel of Fig 11, centrals do prefer to align with their overall satellite distributions.

There are two mechanisms that may be responsible for the strong dependence of central galaxy alignment on cluster ellipticity: 1) the imprint of infall of matter and galaxies into the cluster preferentially along filaments, and 2) the large-scale tidal gravitational field (either primordial, at the time of central galaxy formation, or tidal torquing over time). First, centrals and their parent clusters are both formed via accreting galaxies along filaments, which imprint preferred directions. As a result of these inflows, we expect central galaxies to be aligned with their clusters, especially for relatively young and small clusters with only one dominant filament, leaving an elongated distribution of galaxies (Knebe et al. 2004; Libeskind et al. 2005, 2015). More mas-
sive clusters may have experienced several merger events along filaments in various directions during their assembly history. This more complicated history makes the distribution of galaxies in these clusters more disturbed and randomized, resulting in a rounder shape. Indeed, as shown in the second-to-last row of Fig. 9, there is a weak anti-correlation between cluster ellipticity and richness in our data, with richer clusters having a smaller ellipticity. The subsequent violent merger activities may wash out the memory of the primordial filamentary structure, causing a reduction in the alignment signal (Ragone-Figueroa & Plionis 2007).

However, over the process of virialization, the distribution of galaxies in clusters would again gradually be stretched out along the direction with the surrounding large-scale tidal field, reaching new equilibrium states with a triaxial morphology. At the same time, central galaxies would also gradually be tidally torqued along the new established direction of tidal field. A more anisotropic distribution of satellites could indicate a more intense tidal fields to torque the centrals. It is unclear how important this instantaneous torquing is; Camellio & Lombardi (2015) demonstrated that at galaxy scales, it is too weak to account for the observed intrinsic alignments, but it is unclear whether it is definitely subdominant for cluster mass scales.

We emphasize that the above two scenarios (anisotropic infall and tidal torquing) are not mutually exclusive and do not necessarily have some sequence in time. They could both operate at various stages of the cluster and central galaxy evolutionary process. Also, according to the linear alignment model (e.g., Catelan et al. 2001; Hirata & Seljak 2004), the intrinsic alignment is already set by tidal fields at the time of galaxy formation, and it is not clear how relevant these additional processes that operate later may be.

6.2 Dependence on central galaxy effective radius

As we have shown, the central galaxy effective radius at fixed intrinsic luminosity is also a very significant predictor of the central galaxy alignment effect, with larger-sized centrals at a given luminosity exhibiting a stronger degree of central galaxy alignment than smaller-sized centrals.

Observations and semi-analytic models have revealed that most massive galaxies grow inside-out, with their extended stellar halos dominated by accreted stars. The supply of accretion stars may originate from the stellar streams (Belokurov et al. 2006) or the diffuse intracluster light (ICL) which is composed of tidally-stripped stars that are gravitationally bound to the cluster potential (Oemler 1976; Lin & Mohr 2004). These massive accretion-dominated galaxies thus tend to have more extended light profiles compared to galaxies with a stellar component that primarily underwent "in situ" star formation (van Dokkum et al. 2010; Cooper et al. 2013).

There are two scenarios that can explain the dependence of central galaxy alignment on central galaxy size. First, centrals with more extended morphology may respond
more strongly to tidal forces (either the primordial or instantaneous tidal field). Defined as the difference between the gravitational forces at two different positions on an object, the strength of the tidal force would be stronger for objects that have a larger spatial extent. The alternative explanation stems from the closely linked formation and evolution histories of centrals with their host clusters and the surrounding large-scale structures (Conroy et al. 2007). As reported in Zhao et al. (2015), centrals with extended cD envelopes tend to have larger $R_c$ and are believed to be dominated by baryons from accretion. If there is an abundant supply of accretion stars in some direction aligning with the overall distribution of member galaxies, the central galaxy shape would naturally extend towards the preferred direction of accretion, and thus align with the angle of the member galaxy distribution. We are unable to distinguish between these two scenarios.

6.3 Dependences on central galaxy luminosity, dominance and centering probability

According to Fig. 9, central galaxy luminosity, dominance and centering probability are mutually highly correlated with each other, and thus are likely caused by similar physical origins. Here we discuss the dependences of central galaxy alignment on these three predictors.

As revealed in Table 3, we found that $\Delta \eta$ depends significantly on central galaxy $M^0.1 \cdot M_r$ and $P_{cen}$, with centrals that are more luminous and have a higher centering probability tending to be more aligned with the cluster position angle. Central galaxy dominance, however, was not selected as a featured predictor. This does not mean that central galaxy dominance is not important, but rather that its effect on central galaxy alignment may have been soaked up by the effects of central $M^0.1 \cdot M_r$ and $P_{cen}$, so that knowing the central galaxy dominance provides no further help when predicting $\Delta \eta$ if the other two predictors are also known.

Our result is consistent with that of Hao et al. (2011), who also detected a strong dependence of BCG alignment on BCG luminosity based on a sample of richness $\geq 15$ clusters taken from GMBCG, a cluster catalog constructed based on the red-sequence method (Hao et al. 2010). Also, due to the tight correlation between central galaxy $M^0.1 \cdot M_r$ and dominance, with more luminous centrals showing higher degree of central galaxy dominance, our result implies that clusters with more dominant centrals should have stronger central galaxy alignment. This agrees with the result of Niederste-Ostholt et al. (2010). They found that BCG-dominant clusters exhibit stronger BCG alignments than less BCG-dominant clusters do, with a difference significant at the 4.4$\sigma$ level, based on both the maxBCG cluster catalog (Koester et al. 2007) and a matched filter cluster catalog of Dong et al. (2008).

The dependences of the central galaxy alignment signal on central $M^0.1 \cdot M_r$, dominance and $P_{cen}$ have their common origin in the following aspects. 1) It may originate from the purity of measurement. Luminous and dominant centrals have a higher probability of sitting closer to the true center of their dark matter potential wells (Wen & Han 2013). This kind of system suffers less contamination from wrong detections, and could therefore end up showing a higher central galaxy alignment signal. 2) Clusters with luminous and dominant centrals are typically more relaxed. More relaxed systems have experienced the uninterrupted (by mergers) influence of surrounding large-scale tidal fields for a longer period of time, and thus it may be more likely for their centrals to align.

Given that central $M^0.1 \cdot M_r$ and dominance are highly correlated at $\sim 0.6$, it is natural to ask what causes us to select central $M^0.1 \cdot M_r$ rather than dominance as a featured predictor? To address this question, in Fig. 12, we show some example clusters with luminous but less dominant centrals. As shown, these clusters typically have several bright galaxies, and may still be undergoing significant merging and disruptive interactions. Figs. 12a and c show examples of clusters with their dominantly bright members still some distance away from the centrals. These systems may be not relaxed, but if the centrals’ high luminosities and the distributions of their members stem from the same primary avenue of accretion, high alignment signals can still shown even if the centrals are not dominant. This explains why the importance of central $M^0.1 \cdot M_r$ stands out from central galaxy dominance.

Fig. 12b shows the case where the bright members already sank into the potential well of the cluster and are closely interacting with the central galaxy. In this case, the orientation of the central galaxy may be affected temporarily by these closely interacting galaxies, rather than reflecting the tidal field originating from the large-scale environment. The upper right corner of each panel in Fig. 12 shows some physical properties of the central galaxy. In the case of Fig. 12b, with several bright galaxies crowded in the central region of the cluster, the central $P_{cen}$ tends to be low. This demonstrates that $P_{cen}$ can still be selected as a featured predictor even after selecting central $M^0.1 \cdot M_r$, because it indicates whether there are other bright galaxies near the central that may reduce the central galaxy alignment with the large-scale tidal field through dynamical processes. While examining images of individual clusters does not give the full picture, it is a way of supplementing the statistical measure of central galaxy alignment from the linear regression analysis.

6.4 Dependence on central galaxy color

We observed that redMaPPer centrals with redder color show stronger central galaxy alignments. The enhancement of the central galaxy alignment signal among red hosts has also been observed in systems across a wide range in halo masses. Based on a sample of isolated host galaxies with typically 1–2 c-satellites, Azzaro et al. (2007) and Agustsson & Brainerd (2010) found an excess of satellites along the major axis of their centrals only in red-colored hosts, while satellite distributions are consistent with isotropic around blue hosts. Based on group catalogs spanning from isolated host to cluster scale halos, Yang et al. (2006), Wang et al. (2008), and Siverd et al. (2009) all found that the alignment signal is only detected in groups with red centrals, and is strongest when considering red centrals and red satellites.

Unlike those previous works, our sample is selected based on the red-sequence method, so the centrals all belong to the red galaxy population. Within the red population, we nonetheless found that the central galaxy alignment depends on the $M^0.1 \cdot M_r$–$M^0.1 \cdot M_g$ color of central galaxy in cluster scale. Galaxy color indicates the age of the stellar populations. Re-
cent star formation activities induced by the supply of gas from surrounding materials or merger events would cause the central galaxy color to become less red. Our result thus suggests that central galaxy alignment signal preferentially exists in centrals with relatively old stellar population. For clusters with bluer central galaxies, the alignment of centrals may be disturbed by the recent merger events that also triggered star formation and contributed to the bluer color.

6.5 Dependence on central galaxy ellipticity
Our linear regression shows that central galaxy ellipticity (as defined in Eq. 2) is negatively correlated with $\Delta \eta$, which means that centrals with larger ellipticity exhibit stronger central galaxy alignment. However, the complication in detecting this trend is that it is more difficult to accurately determine the position angles for round centrals. Statistical scatter in measuring the position angles of more round centrals could in principle drive the effect we have observed, rather than it being a true physical effect. Many studies have required the central galaxy ellipticity to exceed some value in order to avoid this effect, at the expense of introducing some systematic selection effect.

To address this issue, in Fig. 13 we show what happens to the correlation between central galaxy ellipticity and central galaxy alignment angle when we divide the original full sample (left panel) into two ellipticity bins at a value of 0.2, with 3554 centrals in the < 0.2 bin, and 4679 centrals in the other. This division reveals that the detected negative correlation of -0.047 in the full cluster sample is dominated by centrals with ellipticity below 0.2 (middle panel), in which a correlation coefficient of -0.12 is measured. These centrals are particularly sensitive to measurement error in the position angle, so the observed negative correlation may arise at least in part from measurement error. It may be also possible that this negative correlation originates from real physical mechanisms. The morphology of centrals reflect their formation history. More elliptical centrals may have experienced more anisotropic accretion that contributes to a stronger alignment effect. Distinguishing between measurement error and this real physical effect is difficult.

If focusing on systems with ellipticities above 0.2 (right panel), the central galaxy alignment angle becomes positively correlated at $0.044 \pm 0.015$, meaning that more elongated centrals have smaller alignment signals. We also find that the observed positive correlation is largely driven by the 8% highest ellipticity centrals, with ellipticity $\geq 0.5$. Our result agrees with that of Yang et al. (2006) (see their

Figure 12. Examples of clusters with central galaxies that are luminous but not dominant. The widths of panels (a), (b), (c) are set to be $\frac{1}{4}$, $\frac{1}{5}$, and $\frac{1}{2} R_{200m}$ (respectively) of their host clusters.
Fig. 2), who found the same tendency using groups with central galaxy ellipticity $^3 \geq 0.2$.

What causes high-ellipticity centrals to be less aligned? To partially address this question, we visually inspected the images of centrals with very high ellipticities ($\geq 0.6$) and presented some examples in Fig. 14. Surprisingly, besides the expected cases of high-ellipticity centrals that are more blue and exhibit disky structures (Fig. 14a) or those with anisotropic ICL (Fig. 14b), we found that in many instances, high-ellipticity centrals are systems with a single extended envelope (Fig. 14c, 14d). These multiple-core centrals are currently undergoing mergers. During the violent coalescence processes, the position angles of centrals change rapidly and no longer reflect the large-scale matter distribution, resulting in a wide spread in $\Delta \eta$.

We conclude that we should ignore central galaxy ellipticity as a predictor, although it is significantly identified through our variable selection process. The observed negative correlation is mostly driven by rounder centrals whose P.A. determination is more likely affected by systematics. For more elongated centrals, positive correlation with $\Delta \eta$ is found, and this correlation is possibly driven by centrals at higher ellipticity end. So far we cannot draw a clear conclusion about the impact of central ellipticity on central galaxy alignments. Larger sample size and improved shape measurement method in the future would help us to analyze the non-linear relation between $\Delta \eta$ and central galaxy ellipticity.

6.6 Dependence on richness

Richness was selected as a statistically significant predictor when using $\Delta \eta$ as the response variable, but not for the response variable $\theta_{cen}$. This result suggests that the impact of richness on the central galaxy alignment signal is marginal. We refer the reader back to the ending of Sec. 4.3 for related discussion. At similar cluster mass scales, Niederste-Ostholt et al. (2010) also found a slight indication that richer clusters show stronger alignment signals, at 2.3σ significance, while Hao et al. (2011) detected no dependence of BCG alignment on richness.

Observationally, richness is a good estimator for the underlying cluster dark matter halo mass (Rykoff et al. 2012). The weak dependence on richness may be due to the limited range of halo masses covered by the redMaPPer cluster sample. In what follows, we compare papers in which the mean central galaxy alignment angles, $\langle \theta_{cen} \rangle$, are provided, and summarize the comparison results in Table 5. Since almost all of the previous works used the isophotal shape measurements, we also turn to our isophotal measurements to fairly compare the $\theta_{cen}$ values. At the mass scale corresponding to galaxy groups, many studies have observed that there is a stronger alignment tendency in richer groups (Yang et al. 2006; Wang et al. 2008; Siverd et al. 2009). As shown in Table 5, the $\theta_{cen}$ value in the highest mass bin of Yang et al. (2006) is consistent with our isophotal $\langle \theta_{cen} \rangle$. Going down to even smaller systems, Brainerd (2005) and Agustsson & Brainerd (2010) have measured the $\theta_{cen}$ using a sample of isolated host centrals. The values of $\theta_{cen}$ are generally larger than that measured in cluster scales. Therefore, we suggest that there truly is some effect of host halo mass on alignments, despite our marginal findings using richness as a mass tracer on cluster mass scales.

Another possible reason that richness may be a less significant predictor is due to the cluster assembly process. Perhaps originally more massive and richer clusters had a stronger primordial alignment with the tidal field, but the subsequent mergers and other major events washed them out, making central galaxy alignments depend only weakly on richness.

$^3$ The definition of galaxy ellipticity adopted in Yang et al. (2006) is $1-b/a$, based on SDSS isophotal measurement.
Figure 14. Examples of centrals with measured ellipticity $\geq 0.5$. The central galaxy ellipticity and position angle difference between the central galaxy and cluster member galaxy distribution ($\Delta \eta$) is shown in the upper right corner of each panel. All panels are 150 kpc on each side. (a) Disky structure central with blueish color. (b) Central galaxy with elongated ICL. (c)&(d) Centrals with double or more bright cores within common extended envelopes.
Table 5. Summary of central galaxy alignment measurements. Here we provide a detailed comparison of the observed average central galaxy alignment angle, $\langle \theta_{\text{cen}} \rangle$, from previous work using a variety of datasets in order to test for the potential evolution of $\langle \theta_{\text{cen}} \rangle$ with halo mass. Relevant properties of the sample used in these studies are also listed.

| paper | $\langle \theta_{\text{cen}} \rangle$ | redshift | shape measurement method | SDSS pipeline | Npair | cluster catalog properties |
|-------|-----------------|---------|----------------------|-------------|-------|---------------------------|
| This work DR8 re-Gaussianization | 41.42±0.08 |  | re-Gaussianization | DR8 | 94187 | • redMaPPer |
| DR7 de Vaucouleurs | 40.74±0.09 | 0.1-0.35 | de Vaucouleurs | DR7 | 86350 | • halo mass $\geq 10^{14} \, h^{-1} M_\odot$ |
| DR7 isophotal | 40.60±0.09 |  | isophotal | DR7 | 86350 | • richness $\geq 20$ |
| Yang et al. (2006) | 43.1±0.4 |  | isophotal | DR2 | 24728 | • Weinmann et al. (2006) group catalog based on the group finder of Yang et al. (2005) |
| $\log [M_{\text{halo}}/(h^{-1} M_\odot)]:12-13$ | 42.6±0.3 | 0.01-0.2 | isophotal | DR2 | 24728 | • 9220 binary, 3073 triplet, 3270 member $> 3$ groups |
| $\log [M_{\text{halo}}/(h^{-1} M_\odot)]:13-14$ | 40.7±0.5 |  | isophotal | DR4 | 62212 | • restricted to groups with BCG ellipticity $> 0.2$ |
| $\log [M_{\text{halo}}/(h^{-1} M_\odot)]:14-15$ | 43.38±0.15 |  | isophotal | DR4 | 62212 | • Yang et al. (2007) group catalog |
| Wang et al. (2008) | 42.1±0.5 | 0.01-0.2 | isophotal | DR3 | 3292 | • isolated host galaxy |
| $\log [M_{\text{halo}}/(h^{-1} M_\odot)]:12-13$ | 42.1±0.5 | 0.01-0.2 | isophotal | DR3 | 3292 | • dominated by systems containing 1-2 satellites |
| $\log [M_{\text{halo}}/(h^{-1} M_\odot)]:13-14$ | 42.1±0.5 | 0.01-0.2 | isophotal | DR3 | 3292 | • isolated host galaxy |
| $\log [M_{\text{halo}}/(h^{-1} M_\odot)]:14-15$ | 42.1±0.5 | 0.01-0.2 | isophotal | DR3 | 3292 | • same selection criteria as Sample1 of Brainerd (2005) |
| Brainerd (2005) Sample1 | 42.9±0.5 | 0.01-0.15 | isophotal | DR7 | 7399 | • isolated host galaxy |
| Agustsson & Brainerd (2010) | 42.9±0.5 | 0.01-0.15 | isophotal | DR7 | 7399 | • isolated host galaxy |

*Note: $z_{\text{median}}$ denotes the median redshift of the sample.*
6.7 Dependence on redshift

We did not find any significant redshift dependence of central galaxy alignment within the limited redshift range of 0.1–0.35. In agreement with our observation, Kang et al. (2007) studied the alignment strength from redshift 2 to 0 and found no redshift evolution based on N-body simulations with a semi-analytical model for galaxy formation. Based on hydrodynamic simulations, Tenneti et al. (2015b) showed a weak redshift dependence on the intrinsic alignment amplitude at galaxy mass scales, with the alignment signal decreasing at lower redshift. However, based on samples at cluster scale, both Niederste-Ostholt et al. (2010) and Hao et al. (2011) have found that the BCG alignment signal is stronger as redshift decreases within the redshift ranges of 0.08 < z < 0.44 and z < 0.4, respectively. The discrepancies between their results and ours may arise from the following: 1) The two previous studies have considered slightly wider redshift ranges than us such that the redshift-dependent trends become detectable. 2) The observed redshift evolution may be just a reflection of possible combined evolutions with other physical predictors, since those two studies did not consider as many parameters as we do. 3) For studies that based on isophotal shape, there may be more contamination from systematic errors at lower redshift, since for an apparently brighter BCG (at fixed luminosity), its 25 mag/arcsec² isophote traces a larger radius where the light of BCG is more easily confused with that from other neighboring satellites. For our redMaPPer sample, when using isophotal shape measurements, we find that the correlation coefficient between $\Delta \eta$ and $z$ is ∼1.5 times higher than that based on re-Gaussianization shape. As discussed in Sec. 5, this could be partly due to a systematic and partly driven by a real physical effect.

Studying the redshift evolution of the overall central galaxy alignment signal is important for understanding the physical mechanism that is responsible for it. If the central galaxy alignment largely stems from the primordial tidal field at the time of cluster formation (Catelan et al. 2001; Hirata & Seljak 2004), later merging or virialization processes may weaken the primordial signal (Hopkins et al. 2005). However, if the central galaxy alignment is dominated by signals established from underlying tidal fields acting during the entire lifetime of clusters, or as suggested by Niederste-Ostholt et al. (2010), the primordial alignment signals could be enhanced by the secondary infall episodes, we may expect stronger alignment toward lower redshifts. Currently we lack data to make a convincing conclusion about redshift evolution of central galaxy alignment; further simulations or deeper observational data pushing to higher redshift are needed to further investigate this problem.

6.8 Dependence on cluster concentration $\Delta R$ 

Miyatake et al. (2016) observed that separating redMaPPer clusters with similar richness and redshift distributions into large-$R_{\text{mem}}$ and small-$R_{\text{mem}}$ populations (see Eq. 9 for definition of $R_{\text{mem}}$) yields two cluster subsamples with similar halo masses, but different large-scale biases. Based on the N-body simulation in the work of More et al. (2016), $R_{\text{mem}}$ is found to be a good indicator for cluster mass accretion rate. Miyatake et al. (2016) thus interpreted the detected difference in large-scale bias as evidence for halo assembly bias, wherein the clustering of halos depends not only on their mass, but also on other properties related to their assembly histories, such as halo formation time, mass accretion rate, concentration, and spin (see, e.g., Gao et al. 2005; Wechsler et al. 2006; Gao & White 2007; Dalal et al. 2008; Lin et al. 2016). Regardless of whether this result indicates assembly bias or some other physical effect can explain the differences in large-scale bias, $R_{\text{mem}}$ does correlate with the concentration of the cluster member galaxy distribution, and it is nonetheless interesting to test whether $R_{\text{mem}}$ influences central galaxy alignments. Here we use the parameter $\Delta R$, which removes the richness and redshift dependence of the observed concentration of the member galaxy distribution (Eq. (10)).

We found that $\Delta R$ has no effect on the central galaxy alignment. In fact, the correlation coefficient between $\Delta \eta$ and $\Delta R$ is the smallest (0.016) among our predictors, as shown in the upper right corner of Fig. 9. Moreover, the last row of Fig. 9 shows that $\Delta R$ does not have any > 10σ correlations with other parameters, and is therefore relatively independent from the rest of the parameter space considered in this work.

7 THE ORIGIN OF ANGULAR SEGREGATION OF SATELLITES

We find that the angular segregation of satellites with respect to their central galaxy major axis direction depends strongly on satellite color and $0.1 M_r$, and weakly but still significantly on $\log(r/R_{200m})$ and satellite ellipticity, as shown in Table 4 in Sec. 4.3. In the following we discuss the possible origins of these dependencies, and compare our results with previous work. We remind the reader that instead of considering all satellite galaxies, our analysis is only based on red-sequence satellites with membership probability above 0.8 according to the redMaPPer algorithm.

7.1 Dependence on satellite color

The color of the red-sequence satellites is the strongest predictor of their angular segregation, with redder satellites tending to preferentially lie along the major axis direction of centrals. This result agrees with previous work that considered satellites in a wider color range and revealed that the distribution of redder satellites shows more anisotropy than that of bluer ones (Yang et al. 2006; Azzaro et al. 2007; Faltenbacher et al. 2007; Wang et al. 2008; Agustsson & Brainerd 2010).

Part of the dependence on satellite color may originate from galaxy properties in filaments connected to clusters. Clusters assembled mainly by accreting satellites from surrounding filaments (e.g., Omor attached to Thomas 2000; Lee & Evrard 2007). As a result, galaxy properties in filaments may leave some imprint on structures within clusters. Using a filament catalog (Chen et al. 2015a) constructed from SDSS, Chen et al. (2015b) found that red galaxies are on average closer to filaments than blue galaxies. Hence, the observed angular segregation of redder satellites may be due to their being preferentially accreted along filaments, which
likely have more tendency to align with the major axes of centrals (see also Kang et al. 2007).

Another possible explanation for the angular segregation by color is related to environmental quenching. Galaxies in denser environments are redder than galaxies of similar mass in less dense environments (Peng et al. 2010, 2012). Thus, satellites falling along denser filamentary channels would tend to be redder than those falling into the cluster from the field (Martínez et al. 2016). Those falling into the cluster along filaments already pre-quenched. Also, satellites orbiting closer to the major axis direction of centrals should experience higher environmental quenching efficiency due to the higher matter density there.

7.2 Dependence on satellite luminosity

More luminous satellites are more likely to lie along the major axis directions of centrals. For isolated host-satellite systems, Agustsson & Brainerd (2010) have also found a consistent trend.

The satellite luminosity dependence may also have its origin from galaxy properties in filaments. By analyzing galaxies in filaments, Chen et al. (2015b) found that more massive galaxies tend to be closer to filaments than lower mass galaxies. Li et al. (2013) observed that there is a significant alignment between the orientations of brightest satellite galaxies with the major axes of their groups, suggesting that brightest satellite galaxies entered their host groups more recently than other satellites. Using N-body simulations, van den Bosch et al. (2016) have also shown that subhalos with a larger mass at the time of accretion (a quantity used to link with galaxy stellar mass through abundance matching) tend to be accreted at a later time (see their Fig. 5) with smaller orbital energy (i.e., on more bound orbits, see their Fig. 9). Combining these previous findings, the physical picture is that more luminous satellites are more likely in-falling from filaments connected to clusters. Since they are accreted by the cluster at a later time, they have not yet orbited enough to lose the imprint of their original large-scale structure. Furthermore, with smaller orbital energy at infall, their dynamics would be more easily influenced by the overall mass distribution in the cluster, and thus as they settle into orbit in the cluster potential well they are more likely to remain along the major axis direction of the central galaxy.

7.3 Dependence on satellite-central distance

We found that the satellite-central distance is a statistically significant predictor of the angular segregation of satellites, with those closer to centrals being more likely to be located along the major axis directions of central galaxies. This may seem puzzling given that the second panel in the first row of Fig. 10 shows that the correlation coefficient between log(r/R_{200m}) and θ_{cen} is consistent with zero within the error bar. Apparently, log(r/R_{200m}) is selected as a feature predictor due to some interplay with another predictor. To identify which other predictor is responsible, we removed one predictor at a time in Eq. (15) to find which one, when removed, caused log(r/R_{200m}) to no longer be selected as a feature predictor.

The result of this process was that satellite-central distance was selected due to the presence of cluster ellipticity in the model. The reason why adding cluster ellipticity results in the selection of log(r/R_{200m}) is illustrated in Fig. 15. For satellites with projected distances r < b (the semi-minor axis of the cluster), the possible values of θ_{cen} can vary between 0° and 90°, while for those with r > b, their θ_{cen} values are confined within 0° and θ_{cen} < 90° due to the boundary of the region contained by the circularized halo radius. Thus, if satellites were randomly distributed within the elliptical footprint of a cluster, we would expect that more elliptical clusters exhibit a stronger anti-correlation between log(r/R_{200m}) and θ_{cen}, with larger log(r/R_{200m}) showing smaller θ_{cen}. The fact that that anti-correlation is not observed suggests that galaxies are not randomly distributed within the elliptical footprint of a cluster, but rather are preferentially located on the major axis to a degree that is more significant at smaller values of log(r/R_{200m}). Or viewing in the other way, central galaxies tend to point toward nearby satellites, whose distribution reflects local, smaller-scale tidal field.

Several previous studies have also investigated the dependence of projected distance on θ_{cen}. For isolated host scale, Brainerd (2005) found that strength of anisotropy increases with decreasing projected distance, while Azzaro et al. (2007) claimed that the degree of anisotropy is independent of the projected distance and Agustsson & Brainerd (2010) also reported no distance dependence for red host galaxies. For galaxy group scale, both Yang et al. (2006) and Siverd et al. (2009) detected stronger central galaxy alignment effects at smaller projected distance. Also, in Fig. 2 of Faltenbacher et al. (2007), θ_{cen} is smaller in the inner part of halos than in the outer part for red satellites.

The general physical picture regarding angular segregation of satellites is that it is due to large-scale tidal fields, which leads to preferential infall of satellites along the connected filaments. This picture is also reflected in the identification of cluster ellipticity as a predictor described in Sec. 6.1. If a cluster’s small-scale tidal field always followed it’s large-scale tidal field, then with the presence of predictor cluster ellipticity (reflecting the direction large-scale tidal field), log(r/R_{200m}) (reflecting small-scale tidal field) would not be selected out, as all of its effect would be absorbed in cluster ellipticity. During the chaotic assembly process, a cluster’s inner tidal field may differ from it’s large-scale tidal field. The positive correlation between θ_{cen} and log(r/R_{200m}) found here implies that smaller-scale local tidal field, either newly established or following along the large-scale tidal field, does play some role in torquing the central galaxies to align with satellites located relatively nearby as well.
7.4 Dependence on satellite ellipticity

We observed a (marginally) statistically significant dependence of the angular segregation of satellites along the central galaxy major axis on satellite ellipticity, with rounder satellites exhibiting a stronger tendency to lie along the central galaxy major axis direction.

An intuitive way of interpreting the effect of satellite ellipticity is to link it with related galaxy properties. Rounder galaxies have less disk component and an older stellar population, and thus look redder in color. Also, luminous galaxies tend to be rounder in morphology. Given the relation between satellite ellipticity, color, and luminosity, they may share similar origins, as we have discussed in Secs. 7.1 and 7.2. However, notice in Fig. 10 that the correlation coefficients for satellite ellipticity with \(0.1 M_\odot\) and color are \(\sim 0.2\) and \(\sim 0.1\) respectively, meaning that there exists other physical origins different from the effects of \(0.1 M_\odot\) or color. We must seek other physical mechanisms that are more tightly linked to the satellite ellipticity itself.

One possible mechanism for the preference of rounder satellites to lie along the major axis directions of centrals may be their frequent interaction with nearby galaxies. According to Kuehn & Ryden (2005), harassment processes due to close encounters with neighboring galaxies make galaxies rounder. Also, Rodríguez et al. (2016) found that elliptical galaxies in groups, where more disturbing events are likely to happen, are more spherical than field elliptical galaxies with similar intrinsic properties. Therefore, satellites residing near the major axis directions of centrals are more likely to be harassed due to the higher number density there. Besides the effect of shaping galaxies, higher frequency interactions with other members let satellites experience through more phase mixing and relation processes, thus speeding up their sinking onto the plane of central galaxy, as the gravitational potential is deeper there.

8 SUMMARY AND CONCLUSION

In this work, we investigate the central galaxy alignment effect using the redMaPPer cluster catalog. We use three kinds of measurements of the central galaxy position angle from the SDSS derived from previous work: re-Gaussianization, de Vaucouleurs, and isophotal shapes, compare the derived central galaxy alignment strength among them, and discuss possible systematic effects. To identify the dominant predictors of the central galaxy alignment signal, we include as many potential physical parameters as possible, and apply forward-stepwise linear regression to quantify the statistical significance of these parameters as predictors, as well as to properly account for correlations between them.

Our analysis has two steps. In step one, we regress the position angle difference between the central galaxy and cluster shape (as traced by the member galaxy distribution, a proxy for the dark matter halo shape), \(\Delta\eta\), against central galaxy and cluster related quantities. The goal of this step is to identify the central galaxy and cluster properties that most significantly affect their alignment. In step two, we regress the angular location \(\theta_{\text{cen}}\) of each member galaxy with reference to its central galaxy major axis direction against several satellite-related quantities, in order to identify important predictors for the angular location of the satellite with respect to the central galaxy major axis. Our key results are as follows.

(i) The detected central galaxy alignment signal is strongest based on isophotal shape, followed by de Vaucouleurs and re-Gaussianization shape (see the right panels in Figs. 6 and 8). This may be caused by the fact that the isophotal shape traces a galaxy’s outermost regions, which are more susceptible to the external tidal fields.

(ii) The central galaxy-cluster alignment is strongest for clusters that are more elongated and higher richness, or that have centrals with larger physical size, higher luminosity, redder color, and higher centering probability.

(iii) The tendency of satellites to reside along the central galaxy major axis direction is strongest for satellites with redder color, higher luminosity, located closer to its central galaxy and with smaller ellipticity.

As shown, we have selected many predictors that have a statistically significant influence on the central galaxy alignment effect. This implies that central galaxy alignment is a complicated phenomenon potentially involved multiple relevant physical processes during galaxy and cluster formation and evolution, such that it cannot be straightforwardly explained by just few dominant factors. We have discussed in great detail the potential physical origins of these selected predictors in Secs. 6 and 7. The most relevant factors seem to be that central galaxy alignment may originate from the filamentary accretion processes, but also possibly affected by the tidal field (either the large-scale primordial tidal field, or the newly-established small-scale tidal field after the redistribution of satellites). Also, merger events tend to destroy alignment. From this work, we cannot fully disentangle the relative contributions from the above three effects, or rule out contributions from other possible mechanisms that can increase or reduce central galaxy alignment. We expect future investigations either based on observations or simulations to put tighter constraints on possible central galaxy alignment scenarios.

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REFERENCES

Abazajian K. N., et al., 2009, ApJS, 182, 543

4 Although central galaxy ellipticity is found to be a significant predictor as listed in Table 3, we discussed in Sec. 6.5 that the correlation between central galaxy ellipticity and \(\Delta\eta\) is more complicated than a simple linear relation, which requires further investigation in future work.
