Shear shuffling governs plastic flow in nanocrystalline metals: An analysis of thermal activation parameters

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From strain rate- and temperature-dependent deformation studies on nanocrystalline PdAu alloys with grain sizes \(\lesssim 10 \text{ nm}\), the shear activation volume \((6b^3)\), strain rate sensitivity \((0.03)\) as well as the Helmholtz \((0.9 \text{ eV})\) and Gibbs free energy of activation \((\Delta G = 0.2 \text{ eV})\) have been extracted. The close similarity to values found for metallic glasses indicates that grain boundary mediated shear shuffling dominates plasticity at the low end of the nanoscale. More fundamentally, we find that the energy barrier height exhibits universal scaling behavior \(\Delta G \propto \tau^{3/2}\), where \(\Delta \tau\) is a residual load, giving rise to a generalization of the Johnson-Samwer \(T^{2/3}\) scaling law of yielding in metallic glasses.

INTRODUCTION

The good tensile ductility of conventional fcc polycrystalline metals relies on two essentials: presence and stress-induced multiplication of dislocations, which act as flow defect and propagate strain, in conjunction with the capability of strain or work hardening, which is basically due to intraplane dislocation interactions and self-organized dislocation-cell-structure formation \([1]\). By contrast, in metallic glasses, dislocations are configurationally unstable and are consequently not available as carriers of strain. The missing long-range atomic order in metallic glasses favors the emergence of incipiently localized shear transformations (STs) upon loading \([2]\). The concomitant shuffling or flipping of groups of atoms manifests as a flow defect, thus playing the same role as dislocations do in crystalline environments. With increasing applied load, STs typically self-organize in the form of shear bands, regions of high strain localization, which upon further increasing stress propagate through the material to eventually lead to catastrophic failure \([3]\).

With regard to nanocrystalline (NC) metals \([4]\), it is obvious that none of these limiting cases applies. Clearly, the plasticity of NC metals involves a much higher degree of complexity for the following reasons: Since the volume fraction of grain boundaries (GBs) scales with the reciprocal grain size, the abundance of GBs at the nanometer scale supplies barriers for intergranular slip transfer, and the nanometer-sized grains entail a reduced capacity of dislocation generation and intraplane dislocation interaction even at the upper limit of the nanometer scale of \(\approx 100 \text{ nm}\). As a consequence, higher strength, lower activation volume, and higher strain-rate sensitivity have been observed \([5, 6]\). Upon decreasing the grain size to the lower end of the nanoscale \(\lesssim 10 \text{ nm}\), it is expected that intragranular crystal plasticity is largely replaced by intergranular plasticity, deformation processes that essentially emerge in the core regions of GBs \([7, 8]\). Computational simulations and experiments unraveled a variety of modes of plastic deformation related to GBs. So far the following processes have been identified: GB slip and sliding \([9–11]\), stress-driven GB migration coupled to shear deformation and grain rotation \([12–14]\), as well as shear shuffling (ST) mediated plasticity \([15, 16]\), here operating in the confined space set up by the core region of GBs. Moreover, GB-ledges and triple junction lines, locations where typically three GBs meet, act as stress concentrators \([17, 18]\), thereby effectively reducing the barrier for partial dislocation nucleation and emission. One of the intriguing aspects here is that in NC metals plastic deformation requires that those mechanisms operate together in the sense that deformation but also accommodation processes must at least partly coexist in order to make deformation happen in a compatible manner, thus avoiding brittle fracture and enabling substantial deformability.

Therefore, one of the central remaining issues is to identify the relative importance of the variety of possible inter- and intragrain deformation modes and assign and quantify in which manner the relevant modes contribute with rising stress to overall strain. It is the aim of this work to deduce principal activation parameters for plasticity from experiment and to analyze these parameters to enable discriminating between the dominating mechanism(s) and the just possible mechanisms, here for NC Pd90Au10 in the limiting case of \(D \lesssim 10 \text{ nm}\).

The activation parameters \([1]\) that are most informative for probing the mechanism(s) of thermally activated plasticity include: first of all, the Gibbs free energy of activation \(\Delta G^\ast\), which at low temperature \(T\), where entropic effects play a minor role, can be approximated by the enthalpy of activation \(\Delta H^\ast\). In transition state theory \([19]\), the free-energy difference between the initial state \((i)\) and the saddle point configuration \((s)\) is usually denoted by \(Q\) having the connotation of an activation free energy and thus \(\Delta G^\ast \approx Q\). Secondly, there is the shear activation volume \(\Delta v^\ast_P\) as well as the phenomenological strain rate sensitivity \(m\), and thirdly, the activation dilatation \(\Delta v^\ast_P\), which is particularly sensitive to the dependence of yield stress on hydrostatic pressure. The full set of activation parameters allows one to iden-
tify, discriminate, and/or obtain information about the relative importance of thermally activated deformation mechanisms. We concentrate in this study on the shear relative importance of thermally activated deformation processes. We first analyze how the measured or effective shear activation volume $\Delta v^*_{\text{eff}}$, strain rate sensitivity $m$, and the Gibbs free energy of activation $\Delta G^*$ are extracted for NC Pd$_{90}$Au$_{10}$ in the limiting case of $D \lesssim 10\text{ nm}$; results on the activation dilatation $\Delta v^*_p$ will be communicated in a forthcoming report.

**SPECIMEN PREPARATION AND MECHANICAL TESTING**

NC Pd$_{90}$Au$_{10}$ specimens with average grain sizes $D \lesssim 10\text{ nm}$ were prepared by inert gas condensation and subsequent consolidation [4]. The microstructure of these as-prepared specimens is characterized by a lognormal grain size distribution [21], a random texture [22] and a GB misorientation distribution that resembles the random MacKenzie distribution [23]. It is dominated by high-angle GBs, which is also reflected by the area-weighted average GB energy of NC Pd $\gamma_A \approx 0.8\text{ J/m}^2$ obtained from calorimetry [24]. For mechanical testing, miniaturized shear-compression specimens (SCSs) [25] were cut from as-prepared disk-shaped samples. Tests were carried out at room temperature and at 77 K. Regarding sample preparation, mechanical testing, and data reduction, all relevant details and graphs can be found in [19, 26]. To get rid of corrections for machine stiffness etc., we meanwhile improved the accuracy of the displacement measurement by utilizing a high resolution optical set-up consisting of a Zeiss SteReo Discovery V12 optical microscope (ca. 100× magnification) and a High-SpeedStar 3G CMOS camera capable of recording up to 1000 images per second at 1 MP resolution. The recorded images were processed by digital image correlation using the software package Lavision DaVis 7.2 to deduce sample displacement. Von Mises equivalent stress and strain values are computed by the finite element method (FEM) using Abaqus [26]. In Fig. 1(a) we display the so-obtained stress-strain curves reflecting a slope of 105 GPa in the elastic region that is in good agreement with the high frequency Young’s modulus of 110 GPa deduced from ultrasound measurements [27].

**SHEAR ACTIVATION VOLUME: CONCEPT AND DETERMINATION**

We first analyze how the measured or effective shear activation volume $\Delta v^*_{\text{eff}}$ is related to experimentally accessible quantities (applied stress and strain rate). We start with the definition of the shear activation volume $\Delta v^*_{\alpha}$ that is assumed to be associated with a unique deformation mechanism [1] and given as

$$\Delta v^*_{\alpha} = -\left. \frac{\partial \Delta G^* (\tau_{\alpha}, \dot{\gamma})}{\partial \tau_{\alpha}} \right|_{T,P},$$

where $\Delta G^*$ must be supplied by thermal fluctuations at constant applied stress $\tau_{\alpha}$, pressure $P$, and temperature $T$ to reach a saddle point configuration of the shear barrier and thus cause an activated process to take place. The shear resistance $\tau$ is a material property and is defined as $\tau = V^{-1} \partial F/\partial \gamma$, where $\gamma$ denotes the shear strain, $V$ is the volume of the system, and $F$ is the Helmholtz potential. In particular, $\dot{\gamma}$ is the...
an effective quantity. The following identity holds for the Helmholtz free energy of activation: $\Delta F^* = \Delta G^* + \Delta W^*$, where $\Delta W^* = V\tau_a \Delta \gamma_c$ denotes the external mechanical work supplied during activation, and $\Delta \gamma_c$ is the activation strain related to localized inelastic shear events with $\Delta \gamma_c = \gamma_s - \gamma_i$. We note that $\Delta \gamma_c^*\gamma$ is an apparent activation volume that is given to first order by $\Delta \gamma_c^*\gamma = \Omega \Delta \gamma_c$, where $\Omega$ is the true volume of a cluster of atoms that has been involved in a local shear event. For applied stresses close to $\tau$, where the reverse rate of deformation can be neglected, the inelastic net strain rate $\dot{\gamma}_p$ is given by

$$\dot{\gamma}_p = \dot{\gamma}_0 \exp\left[-\Delta G^*(\tau_a, \dot{\tau})/kT\right],$$

(2)

and the preexponential factor $\dot{\gamma}_0$ represents a reference strain rate. It essentially depends on the volume fraction of fertile sites that trigger configurational transformations, the unconstrained transformation shear strain, and a normal mode frequency of atom clusters of size $\Omega$ taking part in configurational changes along the activation path. Usually, $\dot{\gamma}_0$ is considered constant, an assumption we also made for the sake of feasibility when deriving Eq. 3 in the next paragraph. This assumption may fail, however, when the preexponential term becomes stress-dependent. In such a scenario, we expect (a) stress-dependent correction term(s) to $\dot{\gamma}_0$ that sensitively depend(s) on the deformation mechanism(s) and atomistic and microstructural details of the material. As a consequence, $\Delta \gamma_c^*\gamma$ will also change its behavior.

With the continuum theory of plasticity, we find the kinetic shear rate $\dot{\gamma}_p$ related to the tensile strain rate $\dot{\varepsilon}_p$ by $\dot{\gamma}_p = \sqrt{3} \dot{\varepsilon}_p$, and the analog regarding shear and tensile stress reads $\tau_a = \sigma_a/\sqrt{3}$ [1]. Solving Eq. 2 for $\Delta G^*$ and substituting $\dot{\gamma}_p$ by $\dot{\varepsilon}_p$, we derive from Eq. 1

$$\Delta \gamma_c^*\gamma = \sqrt{3} kT \left(\frac{\partial \ln \dot{\varepsilon}_p}{\partial \sigma_a}\right)_{T, P, \dot{\varepsilon}_p},$$

(3)

where $\dot{\varepsilon}_p$ is related to the prescribed strain rate $\dot{\varepsilon}_a$ by $\dot{\varepsilon}_p/\dot{\varepsilon}_a = (1 - \Theta/C)$ where $\Theta$ is the tangent modulus, and $C$ denotes the effective Youngs modulus given by the slope of the linear part of the applied stress-strain curve [19] [28]. Clearly, the applied stress $\sigma_a$ is a function of the applied strain and strain rate $\sigma_a = \sigma_a(\varepsilon_a, \dot{\varepsilon}_a)$, and since the concept of the applied activation volume is related to inelastic deformation, it follows that $\Delta \gamma_c^*\gamma$ has to be determined at a given plastic strain $\dot{\varepsilon}_p$. We would like to point out here that values of $\Delta \gamma_c^*\gamma$ derived according to Eq. 3 from experimental data have to be interpreted as effective shear activation volume $\Delta \gamma_c^*\gamma_{\text{eff}}$, since it is a priori not known which mechanisms contribute in which manner to overall deformation. In the following we use the short notation $\Delta \gamma_c^*\gamma_{\text{eff}} \equiv \Delta \gamma_c^*\gamma_{\text{eff}}$. The phenomenological strain rate sensitivity $m$ is defined as $m = (\partial \ln \sigma_a/\partial \ln \dot{\varepsilon}_a)_{T, P, \dot{\varepsilon}_a}$ and also has the character of an effective quantity.

**SHEAR ACTIVATION VOLUME: RESULTS AND DISCUSSION**

The evolution of $\Delta \gamma_c^*\gamma_{\text{eff}}$ as a function of plastic strain is displayed in Fig. 1(b) we note that values for $\Delta \gamma_c^*\gamma_{\text{eff}}$ are by a factor of $\sqrt{3}$ larger than the ones given in [19], where tensile stress has been used in the definition rather than shear stress. The evolution of the strain-rate sensitivity $m$ is also shown in Fig. 1(b) we take $m$ at fixed values $\varepsilon_p$ to allow direct comparison with $\Delta \gamma_c^*\gamma_{\text{eff}}$.

Fundamentally, the activation volume for crystalline metals is bounded by $\approx 10^3 \text{b}^3 \approx 2 \cdot 10^4 \text{nm}^3$ when forest dislocation cutting dominates plasticity [29], and the lower end by $\approx 0.02 - 0.1 \text{b}^3 \approx 2 \cdot 10^{-3} - 4 \cdot 10^{-4} \text{nm}^3$ which is indicative of creep processes [30]. They are based on point defect migration and essentially constitute deformation modes such as Nabarro-Herring [31] and Coble diffusion creep, usually manifesting the concomitant phenomenon of GB sliding [32]. Based on the magnitude of $\Delta \gamma_c^*\gamma_{\text{eff}} \approx 6 \text{b}^3$ extracted for NC Pd$_{90}$Au$_{10}$ it can be concluded that intragranular lattice dislocation activity and creep processes can be ruled out as contributing in an appreciable manner to strain propagation by virtue of a discrepancy in magnitude of their respective $\Delta \gamma_c^*\gamma$ values. This view is also supported by the values found for $m$ which are more than a magnitude smaller than typical values for Coble creep ($m \approx 1.0$) [32] and GB sliding ($m \lesssim 0.3$) [33] [34].

There is a misuse of nomenclature in the pertinent literature dealing with nanoplasticity through associating GB-mediated deformation with GB sliding. Originally, the term GB sliding was introduced to denote the rigid body translation of abutting crystallites along a shared interface that produces offsets in marker lines at the GBs. There are two different modes of GB sliding: Rachinger sliding [35], which must be accommodated by intragranular dislocation glide and climb, and Lifshitz sliding [36], which is based on stress-directed diffusion of vacancies and is self-accommodating. Since both types of GB sliding occur under creep conditions, they are observed at elevated temperatures, and not until a crossover temperature of $\approx 0.5 T_m$ has been reached [12]. Moreover, as it is nearly impossible to experimentally identify and quantify GB sliding in nanoscale microstructures or discriminate the so-called GB sliding from the evolution of shear transformations (STs) and successive avalanches of STs [37] [40], we decided to refer in the following to the more general concept of ST-mediated plasticity [41], which bears a resemblance to events of self-organized criticality [42], but may also lead to marker line shifts at GBs without requiring creep conditions.

Quite generally, we may argue that the high stress levels present in our experiment at room temperature suggest that shear mechanisms should almost instantly overtake processes of diffusional matter transport. As a result, likely mechanisms that may be incorporated in $\Delta \gamma_c^*\gamma_{\text{eff}}$
are related to partial dislocation activity (PDA) involving nucleation and glide, shear-stress driven GB migration (SDGBM) including grain rotation and generation of shear strain, as well as ST-mediated plasticity. In the following paragraph, we discuss how $\dot{\gamma}_{\text{eff}}$ can be decomposed into contributions related to the above-mentioned mechanisms.

Assuming additivity of strains resulting from the PDA, SDGBM, and ST mechanisms, we can write for the effective plastic strain rate, $\dot{\gamma}_{\text{eff}}$,

$$\dot{\gamma}_{\text{eff}} = \dot{\gamma}_{\text{PDA}} + \dot{\gamma}_{\text{SDGBM}} + \dot{\gamma}_{\text{ST}}. \quad (4)$$

Rewriting Eq. 3 as $\Delta v_{\text{eff}} = kT(\partial \ln \dot{\gamma}_{\text{eff}}/\partial \tau_0)$, substituting $\dot{\gamma}_{\text{eff}}$ by Eq. 4 and using Eq. 2 it is straightforward to derive

$$\Delta v_{\text{eff}} = \sum_i \left( \frac{\dot{\gamma}_i}{\dot{\gamma}_{\text{eff}}} \right) \Delta v_i^*, \quad (5)$$

where the summation runs over $i =$ PDA, SDGBM, and ST. The expression in the round bracket obeying $\sum_i (\dot{\gamma}_i/\dot{\gamma}_{\text{eff}}) = 1$ emerges as the shares of the different mechanisms to overall deformation. In what follows, we argue that the share of SDGBM to overall strain plays a minor role, and as a result Eq. 5 can be simplified.

To identify and characterize SDGBM that may occur during deformation, we applied focused ion beam (FIB) to prepare thin lamellae from the undeformed part of the specimen and the gauge section having experienced 30% plastic strain. We then took transmission electron microscopy (TEM) dark field images that have been analyzed in terms of size histograms, which are shown in Fig. 2. The shift of the median $D_0$ from 10.5 nm to 15.5 nm clearly indicates that SDGBM took place during deformation. Referring to a simple model shown in Fig. 2(c), we estimate the share of SDGBM to overall strain.

The shear strain $\gamma_{\text{SDGBM}}$ induced through the migration of GBs in response to the applied shear stress $\tau$ is given by $\gamma_{\text{SDGBM}} = \Delta x/3D$. Using an average coupling factor of $\langle \beta \rangle \approx 0.3$ [43] to describe the ratio of migration of both boundaries parallel ($v_{||}$) and perpendicular ($v_{\perp}$) to the applied stress, we find $\gamma_{\text{SDGBM}} = \beta \Delta D/3D \approx 0.05$, where $\Delta D$ is set equivalent to the increase of the median $\Delta D_0 = 5$ nm. With $\varepsilon = \gamma/\sqrt{3}$, SDGBM contributes 2.8% plastic strain or roughly 1/10th to the overall deformation at 30% plastic strain. For the sake of simplicity, we neglect the SDGBM-contribution in Eq. 5. With the value $\Delta v_{\text{eff}} \approx 6b^3$ determined for NC Pd$_{90}$Au$_{10}$, the theoretical value for $\Delta v_{\text{SDGBM}}^{10b} \approx 10b^3$ [17], and $\Delta v_{\text{ST}}^{5b} \approx 5b^3$ derived from experiment [44, 45], we find $\langle \frac{\Delta v_{\text{SDGBM}}}{\Delta v_{\text{eff}}} \rangle \approx 4\langle \frac{\Delta v_{\text{PDA}}}{\Delta v_{\text{eff}}} \rangle$ so suggesting that ST-mediated plasticity dominantly contributes to overall strain. At first sight, this result seems to be in contradiction to the usual assumption that PDA-based deformation controls the overall deformation behavior of NC metals even below 20 nm grain size. This conflict can be reconciled by noting a recent work on texture formation that is capable of accumulating and storing information of subtle changes in microstructure due to dislocation-based plasticity. Studying texture formation in NC Pd$_{90}$Au$_{10}$ induced by high-pressure torsion, Skrotzki et. al. [46] find that for grain sizes below 20 nm and applied strains up to $\gamma \approx 1$ any texture formation is missing. Moreover, they observed that twinning and stacking fault formation is basically absent, and it is argued that due to the extremely low remnant dislocation density in individual nanograins cross-slip and recovery by edge dislocation climb is unlikely. At strains $\gamma > 1$ texture formation starts evolving and originates mainly from slip of 1/6(112) partial dislocations that are un-

![Graph showing grain size distribution](image)

FIG. 2. (a) Grain size distribution of undeformed NC Pd$_{90}$Au$_{10}$ derived from TEM dark field images. The solid line is a lognormal fit to the histogram with width $\sigma$, median $D_0$ and $N$ denotes the number of counted grains. (b) Grain size distribution after deformation to 30% plastic strain. (c) Sketch of a three grain column where the middle grain exhibits stress driven GB migration in response to $\tau$. For more details, see the text.
cleared from GBs and glide on \{111\} planes. Since our experiments entail strains $\gamma \leq 0.4$, it appears safe to follow our assertion of negligible strain contribution of dislocation activity to overall strain. In the following we are going to scrutinize our conjecture of dominating ST-mediated plasticity by determining activation energies, $\Delta G_{\text{eff}}$ and $\Delta F_{\text{eff}}$, and comparing them with available data for metallic glasses.

**ACTIVATION ENERGY: CONCEPT AND DETERMINATION**

Before discussing experimental details, we first look into how $\Delta G_{\text{eff}}$ relates to the activation energies of the involved mechanisms. Since the form of Eq. 2 applies to the effective activation energy $\Delta G_{\text{eff}}$ as well as to the specific activation energies $\Delta G_i^*$ of possible mechanisms, it follows from combining Eqs. 2 and 4

$$\Delta G_{\text{eff}} = -kT \ln \left( \sum_i \left( \frac{\hat{G}_{0i}}{\gamma_{0i,\text{eff}}} \exp \left( -\frac{\Delta G_i^*}{kT} \right) \right) \right). \quad (6)$$

In contrast to $\Delta v_{\text{eff}}$, which entails a weighted linear superposition of the possible mechanisms (Eq. 5), the effective activation energy $\Delta G_{\text{eff}}$ is given as the logarithm of the sum of exponential terms. Even for small differences in the $\Delta G_i^*$-terms of conceivable mechanisms, it is evident that at room temperature the smallest value of $\Delta G_i^* \approx \Delta G_{\text{eff}}$. We anticipate that the value $\Delta G_{\text{eff}}$ derived from experiment should agree with some characteristic value $\Delta G_i^*$ obtained for ST-based plasticity in metallic glasses.

A supposition made here is that ST-mediated plasticity can take place in an unconstrained manner so that coupling to e.g. accommodation modes having significantly higher $\Delta G_i^*$ values is missing. In fact, the argument that the minimal $\Delta G_i^*$ approximates the measured $\Delta G_{\text{eff}}$ presumes undisturbed superposition of deformation modes making up for the overall strain. From a mechanistic point of view, it is implied that the contiguous network of GBs, the core regions of which are characterized by atomic mismatch associated with excess volume \[37, 38\], offers a plethora of fertile sites, particularly at the low end of the nanoscale. They are predestined to trigger local shear events, most notably since the shear stiffness in those core regions is reduced by about 30% compared to the abutting crystal lattices \[27\], and so the overall deformation may evolve without requiring any significant deformation share originating from generation of intracrystalline strain increments.

For determination of $\Delta G_{\text{eff}}$, we refer to Eq. 2 to find $\Delta G_{\text{eff}}(\hat{\tau}, \tau_a) = kT \ln(\hat{\varepsilon}_{0,\text{eff}}/\hat{\varepsilon}_{\text{eff}})$. Experimentally, we have direct access to $\sigma a = \sigma a(T, \hat{\varepsilon}_{\text{mech}} = \hat{\varepsilon}_{\text{eff}})$ and using continuum plasticity also to $\tau a = \tau a(T, \gamma_{\text{eff}})$. Extracting values for $\Delta G_{\text{eff}}$ therefore requires to express how $\Delta G_{\text{eff}}$ depends explicitly on $\hat{\tau}, \tau_a$.
fixed exponent \( n = 3/2 \) we find for the free parameters \( \Delta F_0 = 1.04 \) eV and \( \tilde{\sigma} = 2.1 \) GPa. The fit based on these values is shown as a full line in Fig. 3. Treating \( \Delta F_0 \), \( \tilde{\sigma} \) as well as \( n \) as free parameters, we find that the exponent \( n \) depends sensitively on small variations \( \delta \tilde{\sigma} \) of the order of 0.05 GPa. However, we can independently estimate \( \tilde{\sigma} \) by arguing that the strain-rate dependent onset stress of inelastic deformation should approximate \( \tilde{\sigma} \) when \( 1/\dot{\varepsilon}_a \to 0 \). Thus using the experimentally extracted value \( \dot{\varepsilon}_{a,\text{eff}} = 10^8 \) s\(^{-1} \) at the onset of inelastic deformation as an upper bound for \( \dot{\varepsilon}_a \), we find \( \tilde{\sigma} = 2.05 \) GPa by linear extrapolation. A least-squares fit to the data points in Fig. 3 based on Eq. 7 now with \( \Delta F_0 \) and \( n \) as free parameters and fixed \( \tilde{\sigma} = 2.05 \) GPa yields \( \Delta F_0 = 1.0 \) eV and \( n = 1.4 \). The good agreement between both approaches makes us feel confident that the extracted parameter values are meaningful. We come back to a physical interpretation of the \( n = 3/2 \) power-law behavior (Eq. 7) in a later paragraph but now concentrate on activation energies.

Since \( \Delta G_{\text{eff}} \) depends on \( \dot{\varepsilon}_{\text{eff}} \) and \( \sigma_{\text{a}} \) is related to \( \varepsilon_{p,\text{eff}} \equiv \varepsilon_p \) via the stress-strain curve, we display how \( \Delta G_{\text{eff}} \) varies with \( \varepsilon_p \) and \( \dot{\varepsilon}_{\text{eff}} \) in Fig. 4. To compare with literature data, we also compute \( \Delta F_{\text{eff}} = \Delta G_{\text{eff}} + \Delta W_{\text{eff}} \), where the mechanical work done by the external agency is defined as \( \Delta W = V\tau_a \Delta \gamma \). It is plausible to substitute \( V\Delta \gamma \) by the local quantities of the flow defect \( \Omega \Delta \gamma_c = \Delta \nu_{\text{eff}} \), thus obtaining \( \Delta F_{\text{eff}} = \Delta G_{\text{eff}} + (\sigma_a/\sqrt{3}) \Delta \nu_{\text{eff}}(\varepsilon_p) \), which is, together with \( \Delta W_{\text{eff}} \), also shown in Fig. 4. In the regime of microplasticity, it is clearly reflected how increasing mechanical work reduces \( \Delta G_{\text{eff}} \) to then reach a nearly plateau behavior for macroscopic plastic flow, which is characterized by \( \Delta G_{\text{eff}} \approx 0.15 \) eV and \( \Delta F_{\text{eff}} \approx 0.9 \) eV. It emerges that \( \Delta F_{\text{eff},\varepsilon_p=0} = 0.78 \) eV is smaller than \( \Delta F_0 \), extracted from the fit in Fig. 3, indicating the expected Helmholtz potential difference between the initial stress-free state and the still stable but stressed state at \( \varepsilon_p = 0 \). We now compare this data set with data obtained for inelastic deformation of metallic glasses.

Studying yielding and plastic flow of a Zr-based metallic glass \([34]\), it has been argued that the activation of STs is the rate limiting step of thermally activated shear-band propagation at a macroscopic scale. Hence temperature-dependent shear displacement jump velocity measurements have been performed to deduce an activation energy of \( \Delta G^* = 0.32 \) eV.

The investigation of room-temperature anelastic relaxation behavior has been exploited to characterize the properties of STs in Al-rich metallic glasses \([35]\). An activation energy distribution of \( 0.85 < \Delta F_m^* < 1.26 \) eV has been extracted, where the index \( m \) relates to the number of atoms involved in a cluster undergoing a ST. It has been estimated that the size of these ST-events, \( \Omega \), entails between 15-20 atoms. This result is based on the reasonable assumption \( \Delta \gamma_c^* \approx 0.2 \) \([31,35]\). Dividing our experimentally determined \( \Delta \nu_{\text{eff}} \) by 0.2, we find a remarkably similar \( \Omega \approx 32 \) atoms in NC Pd\(_{90}\)Au\(_{10}\).

Atomic scale simulations have been used to study the plastic event distributions in the plastic flow state of a Lennard-Jones CuZr metallic glass \([35]\). By exploring the potential energy landscape the activation energy spectrum has been derived from unloading at different shear stress levels. In the limit of high stresses the most probable activated states are characterized by an activation energy (not further specified) of 0.35 eV, and the spectrum of energies between 0.05 eV and 0.35 eV is populated with a frequency which is reduced by a third compared to the most probable state.

Molecular-dynamics (MD) simulations based on a highly realistic embedded atom method (EAM) potential for a CuTi model glass were carried out to study the highly localized as well as spatial and temporal heterogeneous flow occurring in STs to find a minimal activation energy of \( \Delta G^* \approx 0.35 \) eV for viscous flow of successive shear events involving \( \approx 140 \) atoms \([36]\).

Overall, there is a reasonable agreement between activation energies reported in the pertinent literature and the values found in this study, particularly for the onset of macroyielding which occurs at \( \varepsilon_p \approx 3\% \). For the Al-rich glass, there is even a surprisingly good accordance between both the activated cluster size and the Helmholtz activation energy. The overall slightly smaller values of activation energies of NC Pd\(_{90}\)Au\(_{10}\) may reflect the fact that transient dilatancy going along with STs is easier to accomplish in GBs due to preexisting enhanced free volume stored in the GB core regions (GB excess volume) \([37,38]\).

On the basis of this evidence, it is suggested that ST-mediated deformation dominates the plastic flow of NC Pd\(_{90}\)Au\(_{10}\) with an average grain size of \( \approx 10 \) nm. We note that the shear modulus of GBs in NC metals is reduced by about 30% compared to the respective bulk value \([27]\).
and therefore local shear shuffling is predestined to take place in the contiguous network of GBs. Since we have estimated the size of an ST to $\Omega = 32$ atoms in Pd$_{90}$Au$_{10}$, it is implied, based on the structural (or polyhedral) unit model of GBs \[\text{[57]},\] that two or three structural units are involved in the rearrangements of a ST. Those structural units carry different amounts of excess volume depending on the degree of local misfit and therefore may act as fertile sites that trigger the ST. Moreover, the various structural units formed in relaxed GBs resemble the polyhedral building blocks of the liquid structure \[\text{[58–60]}\].

In contrast to metallic glasses, the topology and connectivity of the areal defects (GBs) in NC metals seems to avoid macroscopic shear band formation, which would give rise to stick-slip dynamics, which is clearly not observed. Mechanistically, the self-organized arrangement of STs to form a shear band seems to be effectively impeded in NC metals through possible local bifurcation instabilities at triple junctions, which in turn inhibit strain localization and catastrophic failure.

**UNIVERSAL SCALING**

Finally we come back to the experimentally extracted stress exponent $n = 3/2$ of the stress dependence of activation energy. It is given by the power law $\Delta G_{\text{eff}} = F_0 [1 - (\dot{\tau}_a/\dot{\tau})^{3/2}]$ (Eq. 7). This barrier height scaling has been shown to be universal for many driven systems, including flowing liquids, mechanically deformed glasses, and stretched proteins \[\text{[40]}\]. Inserting Eq. 7 into Eq. 2 and setting $T_0 = \Delta F_0/k_B$, we find

$$\tau_a/\dot{\tau} = 1 - \left[\ln(\dot{\gamma}_0/\dot{\gamma}_p)\right]^{2/3} [T/T_0]^{2/3},$$

(8)

a temperature dependence of stress that agrees with the universal $T^{2/3}$ temperature dependence of plastic yielding in metallic glasses proposed by Johnson and Samwer \[\text{[61–62]}\]. Verification of this temperature dependence for NC Pd$_{90}$Au$_{10}$ is subject-matter of ongoing work. Nevertheless, it becomes evident that the $[\ln(\dot{\gamma}_0/\dot{\gamma}_p)]^{2/3}$-term is not a negligibly small correction term as estimated for metallic glasses at $T < T_g$ where $T_g$ is the glass transition temperature \[\text{[61]}\]. Assuming fixed temperature (RT) and inverting the power law (Eq. 8), it is predicted that $(1 - \sigma_a/\sigma)^{3/2}$ scales as $\ln \dot{\varepsilon}_p$. In Fig. 5 we display that our experimental data obey the predicted scaling behavior even in the entire microplastic regime. Assuming that each ST is governed by the crossing of a saddle-node bifurcation where the energy barrier assumes the universal scaling form, $\Delta G \propto (1 - \tau_a/\dot{\tau})^{3/2}$, Chattoraj et al. \[\text{[63]}\] found similar results in 2D Lenard-Jones glasses. Overall, it seems self-evident to presume that our finding manifests a generalization of the Johnson-Samwer expression $\tau_g/G = a - b(T/T_g)^{2/3}$ where $a, b$ are constants \[\text{[61]}\]. Finally we remark that the observed scaling behavior, covering the entire microplastic regime, suggests that the material response is characteristic of nonlinear viscous behavior, also seen in metallic glasses at temperatures $T > 0.6 T_g$ \[\text{[64–65]}\]. The connotation of strain or work hardening taking place in NC metals in the microplastic regime seems to be misleading then.

**CONCLUSION**

In summary, we conclude that shear transformations \[\text{[2]}\] dominate the plastic deformation of NC Pd$_{90}$Au$_{10}$ at the low end of the nanoscale ($\leq 10\text{ nm}$). Intragranular plasticity based on dislocation glide seems to play a minor role. Likewise, stress-driven grain boundary migration contributes a share of approximately 10% shear strain to overall strain. Since shear transformations are considered to be the generic flow defect in metallic glasses, it seems reasonable to suppose that the atomic site mismatch (disorder) and the concomitant excess volume in the core regions of grain boundaries provoke the occurrence of shear transformations. We do not stipulate that grain boundaries are structurally – in terms of atomic short- and mid-range order – equivalent to metallic glasses. Our conclusion is based on a detailed analysis of thermal activation parameters (activation volume, strain-rate sensitivity, and activation energy) suggesting that grain boundaries can mimic shear deformation behavior as observed in metallic glasses without exhibiting stick-slip behavior and catastrophic failure through running away shear bands. By analyzing the stress dependence of activation energy, we find that the energy barrier scales as stress to the power 3/2. It is straightforward to show that this scaling behavior translates into the universal $T^{2/3}$ temperature dependence of plastic yielding in metallic glasses proposed by Johnson and Samwer \[\text{[61]}\], and it has been verified for a whole variety of different metallic glasses. Moreover, our analysis reveals that plastic yielding in NC...
metals with grain sizes of $\approx 10$ nm or smaller depends markedly on the imposed strain rate $\dot{\varepsilon}$ where stresses $\sigma$ in the entire microplastic regime scale as $\sigma \sim (\ln \dot{\varepsilon})^{2/3}$. From this scaling behavior, we infer that the customary assumption that work or strain hardening takes place in the microplastic regime is not likely to be true. The observed scaling behavior suggests that nonlinear viscous behavior underlies the pronounced increase of stress beyond the regime of linear elasticity up to the yield stress. A similar behavior is observed for metallic glasses when the testing temperature approaches the glass transition temperature from below.

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