AFTERGLOW OBSERVATIONS SHED NEW LIGHT ON THE NATURE OF X-RAY FLASHES

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ABSTRACT

X-ray flashes (XRFs) and X-ray–rich gamma-ray bursts (XRGRBs) share many observational characteristics with long-duration (≥2 s) GRBs, but the reason for which the spectral energy distribution of their prompt emission peaks at lower photon energies \( E_p \) is still a subject of debate. Although many different models have been invoked in order to explain the lower values of \( E_p \), their implications for the afterglow emission were not considered in most cases, mainly because observations of XRF afterglows have become available only recently. Here we examine the predictions of the various XRF models for the afterglow emission and test them against the observations of XRF 030723 and XRGRB 041006, the events with the best monitored afterglow light curves in their respective classes. We show that most existing XRF models are hard to reconcile with the observed afterglow light curves, which are very flat at early times. Such light curves are, however, naturally produced by a roughly uniform jet with relatively sharp edges that is viewed off-axis (i.e., outside of the jet aperture). This type of model self-consistently accommodates both the observed prompt emission and the afterglow light curves of XRGRB 041006 and XRF 030723, implying viewing angles \( \theta_{\text{obs}} \) from the jet axis of \( (\theta_{\text{obs}} - \theta_0) \sim 0.15 \theta_0 \) and \( (\theta_{\text{obs}} - \theta_0) \sim \theta_0 \), respectively, where \( \theta_0 \sim 3° \) is the half-opening angle of the jet. This suggests that GRBs, XRGRBs, and XRFs are intrinsically similar relativistic jets viewed from different angles. It is then natural to identify GRBs with \( \gamma (\theta_{\text{obs}} - \theta_0) \leq 1 \), XRGRBs with \( 1 \leq \gamma (\theta_{\text{obs}} - \theta_0) \leq 0 \), and XRFs with \( \gamma (\theta_{\text{obs}} - \theta_0) \geq 0 \), where \( \gamma \) is the Lorentz factor of the outflow near the edge of the jet, from which most of the observed prompt emission arises. Future observations with HETE-2 and Swift could help test this unification scheme in which GRBs, XRGRBs, and XRFs share the same basic physics and differ only by their orientation relative to our line of sight.

Subject headings: gamma rays: bursts — ISM: jets and outflows — polarization — radiation mechanisms: nonthermal

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1 INTRODUCTION

X-ray flashes (XRFs) are transient X-ray sources with durations ranging from several seconds to a few minutes, and their distribution on the sky is consistent with its being isotropic (Heise et al. 2001; Kippen et al. 2003), similar to what is observed in long-duration (≥2 s) gamma-ray bursts (GRBs). XRFs are also similarly variable. They were first detected by the Wide-FIELD Camera of BeppoSAX (Heise et al. 2001), and subsequently studied with HETE-2 (Barraud et al. 2003; Lamb et al. 2004; Sakamoto et al. 2004). In addition to XRFs, HETE-2 expanded the empirical classification of variable X-ray transients to include an intermediate class of events known as X-ray–rich GRBs (XRGRBs). The spectrum of XRGRBs and XRFs is similar to that of GRBs (Sakamoto et al. 2004), except for the lower values of the photon energy \( E_p \) at which their \( \nu F_\nu \) spectrum peaks and the lower energy output in gamma-rays and/or X-rays, \( E_{\gamma, \text{iso}} \), assuming isotropic emission. In all other respects XRFs, XRGRBs, and GRBs seem to form a continuum.

Many different models have been proposed for XRFs, most of which try to incorporate them into a unified scenario with GRBs. These models include high-redshift GRBs (Heise et al. 2001), dirty (low \( \gamma \)) fireballs (Dermer et al. 1999; Heise et al. 2001; Huang et al. 2002; Zhang et al. 2003, 2004b), regular GRBs viewed off-axis (Yamazaki et al. 2002, 2003, 2004a, 2004b; Dado et al. 2004; Kouveliotou et al. 2004; Zhang et al. 2004b), photosphere-dominated emission (Drenkhahn 2002; Ramirez-Ruiz & Lloyd-Ronning 2002; Mészáros et al. 2002), weak internal shocks (low variability, \( \Delta v \ll \gamma \); Zhang & Mészáros 2002a; Barraud et al. 2003; Mochkovitch et al. 2004), and large viewing angles in a structured (Lamb et al. 2005) or quasi (Zhang et al. 2004a) universal jet.

Most of these models mainly aim at explaining the low values of \( E_p \) in XRFs and do not address their expected afterglow properties. The afterglow evolution alone can, however, serve as a powerful test for XRF models, especially after the recent discovery of several afterglows of XRFs (020427, 020903, 030723, 040701, 040825B, 040912, 040916) and XRGRB 041006. Until a few years ago, XRFs were known predominantly as bursts of X-rays, largely devoid of any observable traces at any other wavelengths. However, a striking development in the last several years through the impetus of the HETE-2 satellite has been the measurement and localization of fading X-ray and optical signals from some XRFs. These afterglow observations resulted in three redshift determinations, for XRF 020903 (\( z = 0.251 \); Soderberg et al. 2004), XRF 040701 (\( z = 0.2146 \); Kelson et al. 2004), and XRGRB 041006 (\( z = 0.716 \); Fugazza et al. 2004; Price et al. 2004b). In two cases, XRF 030723 and XRGRB 041006, the afterglow light curves are reasonably well monitored from sufficiently early times so that they can be used to derive meaningful constraints on XRF models.

In this paper we critically examine the different XRF models and contrast them with the afterglow observations of XRF 030723 and XRGRB 041006, as well as other available observations such as the prompt emission characteristics and the
measured distances. The paper is organized as follows. Section 2 describes the current empirical classification and general properties of GRB, XRGB, and XRF sources. Various XRF models are considered in § 3, along with a brief discussion of the observations that support or undermine these schemes. All the models that are discussed in § 3 have at least one major flaw in common: they do not naturally produce the very flat afterglow light curve seen at early times in both XRF 030723 and XRGB 041006. In the remainder of the paper we thus concentrate only on the class of models that naturally produce such light curves, that is, a roughly uniform jet with sufficiently sharp edges viewed outside the jet core. This class of models is discussed qualitatively in § 4 and more quantitatively in § 5, where it is also directly compared to the prompt emission and afterglow observations of XRGB 041006 (§ 5.1) and XRF 030723 (§ 5.2). The role of our viewing angle as an essential parameter is given particular attention. In § 5.3 we briefly consider other XRFs and XRGBs and find that the data in these cases are too sparse and insufficient to derive meaningful constraints on the underlying model. Our conclusions are discussed in § 6.

2. EMPIRICAL CLASSIFICATION OF GAMMA-RAY BURSTS, X-RAY–RICH GAMMA-RAY BURSTS, AND X-RAY FLASHES

The operational definition of an XRF by the BeppoSAX team was that of a transient source with a duration of less than 10^5 s whose flux triggered the Wide-Field Camera but not the Gamma Ray Burst Monitor. Later, with HETE-2, the definition changed slightly and was based on the ratio of the fluence in the X-ray band to that in the gamma-ray band, f_X,γ = log_{10} (S_X(2–30 keV)/S_X(0.3–100 keV)). In addition to XRFs, the intermediate class of XRGBs was also introduced. According to this new operational scheme, GRBs, XRGBs, and XRFs correspond to f_X,γ < 0.5, 0.5 < f_X,γ < 0, and f_X,γ > 0, respectively. Although the observed peak energies, E_p^{obs} = (1+z)^{-1}E_p (the photon energy where νF_ν peaks), are on average about a factor of ~10 less than those of the “standard” GRBs (E_p^{GRB} ~ 25 keV while E_p^{XRF} ~ 250 keV), the spectra of XRFs are fitted by the same Band function that is commonly used to fit GRBs (Band et al. 1993), and they seem to obey the same correlation between E_p (which is required for cosmological redshift) and the isotropic energy output seen in gamma rays (or X-rays), E_{iso}. E_p ∝ E_{iso}^{-1/4} (Amati et al. 2002; Lloyd-Ronning & Ramirez-Ruiz 2002; Lamb et al. 2005). While GRBs and XRFs have a different operational definition, they appear to form a continuum of events rather than a bimodal distribution, with bursts varying uniformly from XRFs to XRGBs to GRBs.

3. THE VIABILITY OF VARIOUS X-RAY FLASH MODELS

In the next section we show that in order to reproduce the observed behavior seen in the afterglow light curves of both XRGB 041006 and XRF 030723, a roughly uniform jet with sufficiently sharp edges viewed off-axis is required. This is a direct consequence of the very flat evolution of the afterglow light curve that is seen at early times. Such a behavior does not occur for a spherically symmetric outflow or for a uniform jet that is viewed from within its aperture. The same also applies for a “structured” jet (Lipunov et al. 2001; Rossi et al. 2002; Zhang & Meszaros 2002b), where the energy per solid angle ϵ varies as the inverse square of the angle θ from the jet axis, outside of some small core angle θ_{core}, ϵ ∝ cosθ_{min}/(θ/θ_{core})^2. For most models that have been proposed in the literature to explain the phenomenology of XRFs, the afterglow light curve at early times is expected to be similar to that of a spherical flow [with ϵ = ϵ(θ_{obs}) if ϵ varies with θ] and thus behaves qualitatively similar to GRB afterglow light curves. Although this early afterglow behavior alone makes most XRF models inconsistent with observations, in what follows we give additional arguments that further undermine these various schemes.

A straightforward interpretation of the low E_p^{obs} seen in both XRFs and XRGBs is that they are in fact the high-redshift counterparts of long-duration GRBs. While XRFs have on average lower energies than GRBs, their durations are comparable to those of GRBs (Heise et al. 2001), which argues against a high-redshift origin. Moreover, the recent redshift determination of XRF 020903 (z = 0.251; Soderberg et al. 2004), XRF 040701 (z = 0.2146; Kelson et al. 2004), and XRGB 041006 (z = 0.716; Fugazza et al. 2004; Price et al. 2004b) directly rules out this interpretation. Although some GRBs at very high redshifts may resemble XRFs, it is now clear that they do not represent the bulk of the population. In fact, recent estimates suggest that this high-redshift population may only constitute a small fraction of the total number of bursts, provided that the redshift distribution of GRBs accurately tracks the cosmic star formation rate of massive stars (e.g., Blain & Natarajan 2000; Bromm & Loeb 2002; Lloyd-Ronning et al. 2002).

Dermer et al. (1999) have pointed out that “dirty fireballs,” i.e., relativistic outflows with a larger baryonic load and hence a lower initial Lorentz factor Γ_0 compared to classical GRBs, would have a smaller E_p, which could be in the X-rays. When XRFs were discovered it was natural to suggest this scenario as a possible way of achieving low values for E_p (Heise et al. 2001; Huang et al. 2002). We note here that while a lower Γ_0 implies a lower E_p (X(25 keV)/z^4) in the external shock model for the prompt emission, in the internal shocks model it would produce a higher E_p (X(25 keV)/z^4). For the external shock model, the lower the observed E_p = (1+z)E_p^{obs}, the lower the value of Γ_0 that is required to explain it. This implies that events with lower values of E_p should have longer durations, since the deceleration time scales as t_{dec} ∝ (1/(3–k))Γ_0^2(4–k)/(3–k), where k is the energy per solid angle and η_{peak} ∝ r^{-k}. This is inconsistent with observations, as no clear trend exists between the total duration of the event and its E_p (Sakamoto et al. 2004). What is more, as is the case in any external shock model, the afterglow should be a smooth continuation of the prompt emission, as both arise from the same external shock. The observations of XRF 030723 (Fynbo et al. 2004a) offer the best evidence so far against this.

The presence of a dominant baryonic or shock pair photosphere within the standard fireball model was invoked by Ramirez-Ruiz & Lloyd-Ronning (2002) and Meszaros et al. (2002) to explain the formation of XRFs. While this is a tenable scenario for producing XRGBs, the very low E_p < 5 keV observed for XRFs at z ~ 0.2 are hard to reconcile with a low-Γ_0, pair-dominated photospheric component (Meszaros et al. 2002).

Another way of obtaining low values of E_p is with a roughly constant Γ_0 between different events, but with a small contrast in the value of Γ_0 between different colliding shells in the internal shocks model, ΔΓ_0 ≪ Γ_0 (Zhang & Meszaros 2002a; Barraud et al. 2003; Mochkovitch et al. 2004). This model, however, should produce an afterglow with an intensity that is comparable to that seen in typical GRBs. Furthermore, the isotropic equivalent kinetic energy of the afterglow shock at early times (when only the local value of ϵ along the line of sight is sampled, similar to the prompt emission) should be much...
larger than $E_{\gamma,\text{iso}}$, because of the low radiative efficiency of the prompt emission in this scenario.

An alternative model for XRFs arises in the context of the so-called universal (structured) jet models. In this class of models it is assumed that all GRB jets have the same structure, where both $\epsilon$ and $\Gamma$ depend on the angle $\theta$ with respect to the jet axis (Lipunov et al. 2001; Rossi et al. 2002; Zhang & Meszaros 2002b). This model can reproduce the key features expected from the conventional on-axis uniform jet models, with the novelty being that the achromatic break time in the broadband afterglow light curves corresponds to the epoch during which the core of the jet becomes visible, rather than the edge of the jet as in the uniform jet model. For the internal shock model, which is thought to be the mechanism responsible for the prompt emission, $E_p \propto \Gamma_0^{-2} \Gamma_{18}^{-1}$ (e.g., Ramirez-Ruiz & Lloyd-Ronning 2002). As there is no observed correlation between the duration of an event and its $E_p$, this suggests that $E_p \propto \Gamma_{18}^{-1/2} \Gamma_0^{-2}$. This reproduces the observed narrow correlation $E_p \propto \Gamma_{18}^{1/2} \Gamma_0$ only if $\Gamma_0$ is both independent of $\theta$ and has a very small scatter between different events.

Lamb et al. (2005) have proposed a unified description of XRFs, XRGRBs, and GRBs in which either (1) the half-opening angle $\theta_0$ of a uniform jet varies over a wide range while its energy remains constant, or (2) our viewing angle $\theta_{\text{obs}}$ with respect to a universal structured jet varies over a wide range. For convenience, we shall refer to $\theta_0$ and $\theta_{\text{obs}}$ in these two options, respectively, simply as $\theta$. In this picture, small values of $\theta$, correspond to GRBs, while increasingly larger values of $\theta$, correspond to XRGRBs and then to XRFs. In this scenario $E_p \propto \theta^{-1}$, so that the large range of observed $E_p$ values, ranging from $E_p \approx 1$ MeV for bright GRBs to $E_p \approx 5$ keV for dim XRFs (i.e., a range of a factor of $\approx 200$), directly corresponds to a similar range in $\theta$. Both the inferred values of $\theta$, from the jet break times in the afterglow light curves and the log $N - \log S$ distribution of BATSE GRBs (Guetta et al. 2005) suggest, however, a smaller range for $\theta$, of about $\approx 10$ (0.05 $\leq \theta \leq 0.5$), rather than $\approx 200$.

4. OFF-AXIS JET MODELS OF GAMMA-RAY BURSTS AND X-RAY FLASHES

The possibility that GRB outflows are collimated into narrow jets, where in many cases our line of sight would be outside of the jet aperture, resulting in no detectable prompt emission and “orphan afterglows” at later times, was suggested by Rhoads (1997). This was shortly after the first detection of a GRB afterglow and before there was compelling observational evidence for jets in GRBs. As observational evidence in favor of GRB outflows being collimated into narrow jets gradually accumulated, studies of the observational signatures of off-axis GRB jets became more common (Perna & Loeb 1998; Woods & Loeb 1999; Moderski et al. 2000; Dalal et al. 2002; Granot et al. 2002; Levinson et al. 2002; Totani & Panaitescu 2002; Nakar et al. 2002; Granot & Loeb 2003; Eichler & Levinson 2004), again mostly devoted to orphan afterglows. The possibility that for viewing angles that are only slightly outside of the jet aperture the prompt emission might still be detectable, but would shift into the X-rays due to the reduced Doppler factor, has been pointed out by Woods & Loeb (1999). That was, however, before the discovery of XRFs. After XRFs were discovered, Yamazaki et al. (2002) suggested that GRB jets viewed slightly off-axis could naturally account for this newly discovered class of events. In later works they have significantly developed some aspects of this model (Yamazaki et al. 2003, 2004a, 2004b), in particular those regarding the prompt emission. In this section we discuss various aspects of this model in some detail, with both the prompt and afterglow signatures being at the forefront of our attention.

4.1. The Jet Structure

The usual assumption about the jet structure is that it is perfectly uniform within some finite initial half-opening angle, $\theta_0$, from the jet symmetry axis and abruptly truncates outside of $\theta_0$ (Woods & Loeb 1999; Yamazaki et al. 2002). Obviously, this is only an approximation, as physically one might expect that the jet would have a smoother outer edge, where the energy per solid angle, $\epsilon$, and the initial Lorentz factor, $\Gamma_0$, decrease smoothly with the angle from the jet symmetry axis over some finite range in $\theta$, $\Delta \theta \approx \Gamma_0^{-1}$. In fact, numerical simulations show that even if the jet initially has perfectly sharp edges (i.e., a “top hat” jet), the interaction with the ambient medium causes its edges to become smoother with time (Granot et al. 2001). This serves as a motivation for considering a roughly uniform jet with smooth edges as a more realistic version of the top hat jet. The most widely used version of such a jet is one with a Gaussian angular profile for $\epsilon$ (Zhang & Meszaros 2002b; Kumar & Granot 2003), $\epsilon = \epsilon_0 \exp (\theta^2/2\theta_0^2)$. There are also other similar jet profiles, where most of the energy resides within some finite half-opening angle $\theta_0$ and $\epsilon$ sharply drops outside of $\theta_0$. Numerical simulations of a jet boring its way through a massive star progenitor in the context of the collapsar model (Zhang et al. 2004b) predict a roughly uniform jet core with $\theta_0 \approx 3^\circ - 5^\circ$ and wings where $\epsilon \propto \theta^{-3}$ that extend to larger angles, i.e., $\epsilon \approx \epsilon_0 \min [1, \theta/(\theta_0)^3]$. We consider all such models to be variants of the same basic jet structure, and when viewed from outside the jet core ($\theta_{\text{obs}} > \theta_0$) they are considered as members of the same class of XRF models. The different aforementioned variants of this jet structure are considered in § 5.

4.2. The Afterglow Light Curves

The early afterglow light curves for off-axis viewing angles ($\theta_{\text{obs}} > \theta_0$) are generally flatter than those observed in typical on-axis ($\theta_{\text{obs}} < \theta_0$) GRB afterglows (see Granot et al. 2002 and references therein). For a jet structure for which $\epsilon$ and $\Gamma_0$ drop sharply with $\theta$ at $\theta > \theta_0$, we expect its early light curve to rise with time. In this case, the sharper the edge of the jet, the sharper the rise in the light curve (Granot et al. 2002). For jets with sharp enough edges, the emission from the core of the jet (i.e., from $\theta < \theta_0$) dominates even at off-axis viewing angles ($\theta_{\text{obs}} > \theta_0$), despite its being strongly beamed away from our line of sight (see Fig. 1). This is either because there is no emitting material along the line of sight or because even if present its emission is still weaker than that arising from the jet core. As the jet sweeps up an increasing amount of external medium, it slows down and thereafter the relativistic beaming of the emission from the jet core away from our line of sight decreases. When $\gamma$ drops to $\approx (\theta_{\text{obs}} - \theta_0)^{-1}$, our line of sight enters the beaming cone of the radiation from the jet core, causing the light curve to peak and subsequently decay, asymptotically approaching the light curve for an on-axis observer.

If the edge of the jet is not sufficiently sharp (i.e., if $\epsilon$ and $\Gamma_0$ do not drop sufficiently sharply with $\theta$ at $\theta > \theta_0$), then the emission from material along our line of sight may dominate over that from the core of the jet for viewing angles slightly outside the edge of the jet. In this case the light curve at early times would not rise with time, but would instead simply decay more slowly when compared to the light curve seen by on-axis observers ($\theta_{\text{obs}} < \theta_0$). Therefore, we conclude that the jet structure, and specifically the sharpness of its edges, can be
constrained by early afterglow observations. In the context of the model discussed in this section, increasingly larger viewing angles will correspond to XRGRBs and XRFs. Such a scheme is tested against observations of XRGRB 041006 and XRF 030723 in § 5.

4.3. The Prompt and Reverse Shock Emission

The prompt emission for off-axis viewing angles ($\theta_{\text{obs}} > \theta_0$) may also be dominated either by the emission from the jet core or by the emission from the material along the line of sight, depending on the viewing angle and on how sharp the edge of the jet is. If the edge of the jet is sufficiently sharp, the prompt emission is dominated by the core of the jet and both the fluence and the peak photon energy drop sharply when compared to their on-axis values, as $[\gamma(\theta_{\text{obs}} - \theta_0)]^{-6}$ and $[\gamma(\theta_{\text{obs}} - \theta_0)]^{-2}$, respectively (Granot et al. 2002; Ramirez-Ruiz et al. 2005). The prompt emission in this case arises from the same region as for on-axis viewing angles, which in this scenario correspond to GRBs. This suggests that the same physical mechanism is responsible for the prompt emission in GRBs and in XRFs (i.e., most likely internal shocks).

If, on the other hand, the edges of the jet are not sharp enough, then the prompt emission will be dominated by material along our line of sight. As it might be hard to produce strong variability in the Lorentz factor of the outflow outside the core of the jet (Ramirez-Ruiz et al. 2002; Zhang et al. 2004b), internal shocks may not be very efficient and the external shock due to the interaction with the external medium might dominate the prompt emission. In that case, a smooth prompt light curve consisting of a single wide peak might be expected.

The “optical flash” emission from the reverse shock is generally expected to be weaker for off-axis observers (Fan et al. 2004). If the reverse shock is Newtonian or only mildly relativistic, then the beaming of the prompt emission (which is attributed to internal shocks within the outflow, which in turn occur before the ejecta is decelerated by the external medium) and the reverse shock emission would not be very different. In this case the ratio of the off-axis to on-axis flux or fluence should be roughly similar for the optical flash and the prompt emission. If the reverse shock is relativistic then it would significantly decelerate the ejecta, and the emission from the reverse shock would be less strongly beamed than the prompt emission. In this case, if the emission is dominated by the jet core (i.e., for a sharp-edged jet), the optical flash emission at off-axis viewing angles could be less suppressed compared to the prompt X-ray or gamma-ray emission.

4.4. Linear Polarization

An interesting implication of the off-axis jet model for XRGRBs and XRFs is that it predicts a higher degree of linear polarization of the prompt emission, the emission from the reverse shock, and the afterglow emission, if the polarization is dominated by the jet geometry while the magnetic field is mostly tangled in the plane of the shock, as expected from the two-stream instability (Medvedev & Loeb 1999). For a shock-produced magnetic field that is tangled within the shock plane, the linear polarization peaks at a viewing angle that satisfies $\gamma(\theta_{\text{obs}} - \theta_0) \sim 1$ (Gruzinov 1999; Waxman 2003; Granot 2003; Nakar et al. 2003b), since at such a viewing angle most of the observed radiation is emitted roughly along the shock plane in the rest frame of the emitting plasma, due to aberration of light effects. The peak polarization can reach up to tens of percent. This is relevant to the prompt emission and may also be relevant for the optical flash emission. The peak of the polarization that occurs at $\gamma(\theta_{\text{obs}} - \theta_0) \sim 1$ can shift to a larger viewing angle $\theta_{\text{obs}}$ during the optical flash as the ejecta is decelerated by the reverse shock.

For jets with sufficiently sharp edges that are viewed off-axis, the afterglow light curve initially rises at early times and the polarization peaks around the time of the peak in the light curve, which occurs when $\gamma(\theta_{\text{obs}} - \theta_0)$ decreases to $\sim 1$, as our line of sight enters the beaming cone of the emitting material (Granot et al. 2002). Even if there is some lateral spreading of the jet and an initially off-axis viewing angle enters into the jet aperture as the latter grows with time, then the afterglow polarization would be relatively large, as the line of sight would still be relatively close to the edge of the jet (Sari 1999; Ghisellini & Lazzati 1999).

One should keep in mind, however, that ordered magnetic fields might potentially play an important role in the polarization of the prompt emission (Waxman 2003; Granot 2003; Nakar et al. 2003b; Lyutikov et al. 2003), as well as that of the reverse shock emission (the optical flash and radio flare) and the afterglow emission (Granot & K"onigl 2003). If the dominant cause of polarization is an ordered magnetic field component instead of the jet geometry together with a shock-produced magnetic field, then the viewing angle would have a smaller effect on the observed linear polarization.

A recent analysis of archival radio flare observations (Granot & Taylor 2005) has set strong upper limits on the linear and circular polarization of this radio emission and shown that these limits constrain the presence of an ordered magnetic field in the ejecta. The existing radio flare observations are for GRBs, which in the model considered here correspond to on-axis viewing angles ($\theta_{\text{obs}} < \theta_0$). For a uniform jet with an ordered toroidal magnetic field, the polarization vanishes at the jet symmetry axis (i.e., for $\theta_{\text{obs}} = 0$) and strongly increases toward the edge of the jet. Therefore, the observed upper limits on the linear polarization translate to an upper limit on $\theta_{\text{obs}}/\theta_0$. The best constraints so far are for GRB 991216: $P < 7\%$ and $\theta_{\text{obs}}/\theta_0 \leq 0.4 - 0.55$, respectively. There are weaker constraints for GRBs 990123 and...
from relativistic electrons that are accelerated behind the shock using the conventional assumptions of synchrotron emission. The light curves for observers located at different angles relatively little lateral expansion as long as the jet is relativistic. It has a redshift of z = 0.716 (Fugazza et al. 2004; Price et al. 2004a), which for a fluence of f = 1.2 × 10^{-3} erg cm^{-2} in the 2–400 keV range gives E_{\gamma,\text{iso}} \approx 1.6 \times 10^{52} erg. It had an observed peak photon energy of E_p^{\text{obs}} = 63 \pm 20 keV, corresponding to E_{\gamma} = 109^{+12}_{-9} keV. Figure 2 shows an off-axis model yielding an acceptable fit to the optical and X-ray afterglow observations of XRGRB 041006, which is also consistent with the upper limits at radio and submillimeter wavelengths (Barnard et al. 2004a, 2004b; Soderberg & Frail 2004). From this analysis one can conclude that a successful model for the afterglow of XRGRB 041006 is that of a collimated, misaligned jet interacting with a stellar wind external medium of mass density \rho_{\text{ext}} = Ar^{-2}, where r is the distance from the central source. The parameter values used in this fit are E = 1.0 \times 10^{51} erg, A_{\nu} = A (5 \times 10^{11} g cm^{-1}) = 0.03, \theta_{0} = 3^\circ, \theta_{\text{obs}} = 1.15\theta_{0}, p = 2.2, \epsilon_{e} = 0.1, and \epsilon_{B} = 0.001.

The optical light curve is very flat at early times (\alpha \approx 0 at t \leq 1 hr, where F_\nu \propto t^{\alpha - 3}) and becomes steeper after a few hours, \alpha \approx 1.2, which is a little steeper than the decay index in the X-ray at a similar time (\alpha \approx 1 at t \approx 1 day). Also, the ratio of the flux in the optical and X-ray at t \approx 1 day implies a spectral index of \beta \approx 0.7–0.75 assuming a single power law between them. This suggests that the cooling break frequency \nu_c is above the optical after 1 day. Since one requires very extreme parameters to get \nu_c to the X-ray range after 1 day (even getting \nu_c to be above the optical after a day requires relatively low values of \epsilon_{\text{B}} and of the external density), it is most likely range and 7 \times 10^{-6} ergs cm^{-2} in the 30–400 keV range, corresponding to f_{\lambda, 30} \approx 0.15, which classifies it as an XRGRB.
that \( \nu_c \) is between the optical and X-ray at 1 day, which can also explain the steeper temporal decay index in the optical (by \( \Delta \alpha = 0.25 \)) for a stellar wind environment (\( k = 2 \)). This favors a wind medium over a uniform density one, since otherwise the flux in the optical will decay more slowly than in the X-ray (also by \( \Delta \alpha = 0.25 \)), which is contrary to what is observed for XRGRB 041006. At \( t < 5 \) days there is a flattening in the optical light curve, which is probably due to an underlying supernova (SN) component (Garg et al. 2004). This explains why the observed flux is higher than that predicted by our narrow relativistic jet model.

The X-ray light curve consists of a single Chandra observation, between 16.8 and 42.6 hr after the burst (Butler et al. 2004). It showed a temporal decay index of \( \alpha = 1 \pm 0.1 \) and a spectral index of \( \beta = 0.9 \pm 0.2 \). Thus the X-ray light curve is not as densely sampled as the optical light curve and therefore provides fewer constraints on theoretical models on its own. However, when combined with the optical light curve it provides complementary information and gives a better handle on the broadband spectrum, thus significantly improving upon the constraints from the optical data alone. The stellar wind external density profile produces a very smooth and extended jet break in the light curve, resulting in a gradual increase of the temporal decay index \( \alpha \) in the X-rays.

The smooth and gradual steepening of the X-ray light curve at early times is due to our choice of a slightly off-axis viewing angle, which naturally gives rise to the observed temporal behavior as the off-axis afterglow light curve gradually joins that seen by an on-axis observer. In the optical, on the other hand, there are two break frequencies passing through the observed band, first \( \nu_c \) (which increases with time), and subsequently \( \nu_m \) (which decreases with time). At late times \( \nu_c \) passes through the X-ray band and the temporal evolution of the optical and X-ray light curves thereafter becomes similar.

The fit to the afterglow observations does not, however, uniquely determine the model parameters. Some physical parameters are nonetheless constrained better than others. The afterglow data for XRGRB 041006 require a stellar wind environment (\( k = 2 \)) with a low density \( (A, \sim 0.03) \) and a viewing angle that is only slightly outside the edge of the jet, \( (\theta_{\text{obs}} - \theta_0) \sim 0.15 \text{h}^{-1} \sim 10^{-2} \text{rad} \), in order to successfully explain both the spectrum+temporal decay rates in the optical and X-ray at \( t \approx 1 \) day and the very flat optical light curve seen at early times. A smaller viewing angle \( \theta_{\text{obs}} \) might still be possible. In fact, in § 6 we show that an on-axis viewing angle and a wide jet or even a spherical outflow could still provide an acceptable fit to the afterglow observations. The viewing angle, however, cannot be significantly larger than our best-fit value, as this would produce a rising light curve at early times, in contrast to the observed very flat behavior.

If GRB jets have well-defined edges, both the prompt gamma-ray fluence and the peak of the spectrum drop very sharply outside the opening of the jet, as \( \delta = 3 \) and \( \delta = 1 \), respectively.

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6 This is an approximate expression that is valid for a point source at the edge of the jet at the point closest to the line of sight and gives reasonable off-axis light curves (Granot et al. 2002). A more accurate calculation (e.g., Eichler & Levinson 2004) shows a more complex behavior. If one defines the local slope of the fluence, \( f \), as a function of \( \delta \), \( a = -d \log f / d \log \delta \), then \( a > 3 \) at very small off-axis angles \( 0 < (\theta_{\text{obs}} - \theta_0) \lesssim 1 \) hr, \( a \approx 2 \) at intermediate angles \( 1 < (\theta_{\text{obs}} - \theta_0) \lesssim 3 \), and \( a < 3 \) at \( (\theta_{\text{obs}} - \theta_0) > 3 \). This is somewhat different from our simple power-law approximation. However, since the exact shape of the edge, as well as other model uncertainties, could introduce effects of similar magnitude to the difference between our simple power-law approximation and the more accurate calculation, the former is sufficient for our purposes.

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7 This is the ratio of the Doppler factor for a viewing angle along the edge of the jet (i.e., at the point where most of the off-axis emission comes from) to the Lorentz factor \( \gamma \) is that of the emitting fluid at the edge of the jet, \( \gamma | \theta_{\text{obs}} - \theta_0 | \lesssim 1 \), and the Doppler factor for an off-axis viewing angle \( \theta_{\text{obs}} \) that satisfies \( \gamma | \theta_{\text{obs}} - \theta_0 | \gtrsim 1 \).
although a firm upper limit of $z < 2.3$ could be placed (Fynbo et al. 2004a). Chandra observations of the X-ray afterglow were reported by Butler et al. (2005). In the radio band, only an upper limit of 180 $\mu$Jy was reported at 8.46 GHz, 3.15 days after the event (Soderberg et al. 2003).

The optical transient was discovered by Fox et al. (2003), and extensive follow-up in the optical and near-infrared was reported by Fynbo et al. (2004a). The well-monitored $R$-band light curve is initially very flat, with $\alpha \approx 0$ (where $F_\nu \propto \nu^{-\alpha}$). After about 1 day it steepens to $\alpha \approx 2$. This behavior is unusual for standard GRB light curves and allows one to constrain models of XRFs. Fynbo et al. (2004a) already noted how the early-time flattening of the light curve might be an indication of an off-axis jet. Between 1 and 4 days the optical spectral slope $\beta_{op}$ was in the range $\sim 1.0 - 1.3$, which is not unusual for GRB afterglows.

After about $\sim 10$ days, a strong bump appeared in the optical light curve. This was assumed to be a SN component by Fynbo et al. (2004a), while Huang et al. (2004) interpreted it as an indication of a second jet, within the context of the two-component jet model (see Ramirez-Ruiz et al. 2002; Peng et al. 2005 and references therein). The bump had a sharp rise and red colors (Fynbo et al. 2004a). The sharp rise, with $\Delta t < t$, is hard to explain in both of these models, although Tominaga et al. (2004) were able to fit the sharp rise with models of SN light curves. The red colors arise naturally for a SN but are very hard to account for in a two-component jet model or for that matter also in other models of bumps in the afterglow light curve, such as a density bump in the external medium, angular inhomogeneities in the jet (“patchy shell”), or a refreshed shock (Rees & Mészáros 1998; Panaitescu et al. 1998; Ramirez-Ruiz et al. 2001a, 2001b; Wang & Loeb 2000; Lazzati et al. 2002; Heyl & Perna 2003; Nakar et al. 2003a; Mészáros et al. 1998; Kumar & Piran 2000). Therefore, the SN explanation for the bump in the optical light curve seems to be favored by the currently available data.

The X-ray light curve consists of two points, at 3.2 and 13.2 days. A joint fit for the spectral slope at these two epoch
gives $\beta_X = 0.9^{+0.3}_{-0.2}$, while the temporal index between these two points is $\alpha_X = 1.0 \pm 0.1$ (Butler et al. 2005). This is a significantly shallower decay compared to that in the optical prior to the bump ($\alpha_{op} \approx 2$) and is therefore not easy to account for. Since the optical bump is most likely due to a SN component, the same physical component is not expected to contribute significantly to the X-ray flux. The shallower decay in the X-rays might be due to the contribution of SSC, which can dominate the X-ray flux on timescales of days to weeks (Panaitescu & Kumar 2000; Sari & Esin 2001). This would generally also decrease the value of the spectral slope $\beta_X$, and therefore Butler et al. (2005) considered this option to be incompatible with the data.

We wish to stress that if the bump in the optical light curve is not because of the contribution from an underlying SN but is instead hydrodynamic in nature, such as a refreshed shock or an external density bump, then this would naturally explain the X-ray light curve without the need of advocating a SSC component (Butler et al. 2005). The main problem with such an explanation is that it fails to reproduce the spectral behavior seen in the optical during the bump, as stated by Fynbo et al. (2004a).

We performed a tentative fit to the data and demonstrate here that the observational constraints on the spectral slope can still be satisfied by this scenario (see Fig. 4). The physical parameters of this fit are $z = 0.8$, $E = 1.0 \times 10^{50}$ ergs, $n = 4.5$ cm$^{-3}$, $\beta = 2.36$, $\epsilon_R = 0.012$, $\epsilon_e = 0.13$, $\theta_0 = 2.9$, and $\theta_{obs} = 2.03 \theta_0$. We stress that the model parameters cannot be uniquely determined from the fit to the afterglow observations, and other sets of model parameters could provide an equally good fit to the data. Some features are, however, rather robust. Most noticeable is a viewing angle of $\theta_{obs} \sim 2\theta_0$, which is required in order to reproduce the initially very flat part of the optical light curve. A narrow jet with $\theta_0$ of no more than a few degrees is required in order for the jet break time $t_B$ to be less than about a day, which is in turn needed in order to reproduce the steep decay in the optical light curve that starts after $\sim 1$ day. The other model parameters are somewhat degenerate and their values cannot be very tightly constrained from the afterglow light curves. It is stated here that the flattening or mild bump seen in the X-ray light curve after a week or so is due to the contribution from the SSC component. This is indeed needed in order to account for the very slow temporal X-ray decay and requires $\epsilon_{\gamma}/\epsilon_R \sim 10$ in order for the SSC component to be sufficiently prominent.

A redshift of $z \lesssim 0.8$ is suggested by a fit of the late-time bump in the optical light curve to core-collapse SN light curves (Tomimaga et al. 2004). This in part motivated us to choose a redshift of $z = 0.8$ for the fit that we present here, but fits for other values of $z$ are also plausible. A higher $z$ would require a higher jet energy $E$, while a lower $z$ would require a smaller jet energy. For $z \approx 0.8$, $E_{\gamma,iso} \approx 9.3 \times 10^{50}$ ergs, which together with $E_{k,iso} \approx 7.8 \times 10^{52}$ ergs implies $\delta \sim 4.4$ and $\gamma \sim 40$. This would in turn imply a (cosmological) rest-frame $E_{p}$ of $\sim 66$ keV

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\[ \frac{d\beta}{d\log \nu} = \frac{\beta_{op} - \beta_X}{\log \frac{\nu_{op}}{\nu_X}} \]

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\[ \frac{d\beta}{d\log \nu} = \frac{\beta_{op} - \beta_X}{\log \frac{\nu_{op}}{\nu_X}} \]

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\[ \frac{d\beta}{d\log \nu} = \frac{\beta_{op} - \beta_X}{\log \frac{\nu_{op}}{\nu_X}} \]
if viewed on-axis, which is a factor of ~3 lower than the value required to fall exactly on the Amati relation (see Fig. 3). Given the large uncertainties associated with this relationship (Lloyd-Ronning & Ramirez-Ruiz 2002; Nakar & Piran 2005; Band & Preece 2005), we consider this to be in good agreement with observations of on-axis GRBs.

It is reasonable to expect a relatively low Lorentz factor ($\gamma \sim 40$) at the edge of the jet. Assuming $\gamma$ decreases from $\gamma_{\text{int}} \lesssim 100$ in the interior of the jet to much lower values at $\Delta \theta \approx 1/\gamma_{\text{int}}$ centered around $\theta_{\text{obs}}$, then for $\gamma \lesssim 40$ the optical depth to pair production would be large, while for larger values of $\gamma$ many fewer photons would reach an off-axis observer, so that it is reasonable that the off-axis prompt emission will be dominated by $\gamma$ for which $\tau_{\gamma\gamma}$ is just smaller than 1. A similar result was obtained in a fit to GRB 031203 (Ramirez-Ruiz et al. 2005).

In addition to a uniform jet with sharp edges, we also consider other jet structures: (1) a narrow core with power-law wings $\epsilon \approx \epsilon_0 \min \left[ 1, (\theta/\theta_0)^{-2} \right]$, $\Gamma_0 - 1 \approx 299 \min \left[ 1, (\theta/\theta_0)^{-2} \right]$, and (2) a Gaussian jet with $\epsilon \propto \exp \left( -\theta^2/\theta_0^2 \right)$ and either a constant $\Gamma_0 = 200$ or a Gaussian $\Gamma_0 = 1$ [i.e., $\Gamma_0 = 1 + 199 \exp \left( -\theta^2/\theta_0^2 \right)$]. The light curves for different viewing angles are shown in Figure 5. For a jet with power-law wings where $\epsilon \propto \theta^{-2}$, it is hard to reproduce the very flat light curve at early times that is observed in XRF 070323 (and in XRGRB 041006), even for the $\theta \approx 3$ that is expected for the collapsar model (Zhang et al. 2004b), and a steeper drop in $\epsilon$ (i.e., a larger value of $a$) is required. For a Gaussian jet, the light curves have a stronger dependence on the angular profile of the initial Lorentz factor, $\Gamma_0(\theta)$. If it is constant, then the deceleration time at large viewing angles is still very small, and the contribution to the observed flux from material along the line of sight dominates at early times out to reasonably large viewing angle $\theta_{\text{obs}}/\theta_0 \sim \sim 1$. If, on the other hand, it has a Gaussian profile, $\Gamma_0 - 1 \propto \exp \left( -\theta^2/\theta_0^2 \right)$, then the deceleration time at large angles becomes large and the observed flux is dominated by emission from the jet core even at early times. This causes a rise in the observed flux at early times for viewing angles outside the core of the jet, similarly to a uniform jet viewed off-axis (Kumar & Granot 2003) and in better agreement with the initially very flat light curves of XRF 070323 and XRGRB 041006. We consider a Gaussian profile for the kinetic energy per unit mass, $\Gamma_0 - 1$, to be more realistic than a constant $\Gamma_0$, since the latter requires a Gaussian profile for the rest mass per unit solid angle, $\mu$, that is entrained in the outflow [since $\epsilon = (\Gamma_0 - 1)/\mu c^2$], while the former implies a constant $\mu$. If anything, one might expect $\mu$ to increase with $\theta$ rather than decrease with $\theta$ (since a larger amount of mass in the ejecta might be expected near the walls of the funnel). Thus, from the models we considered, a reasonable fit to the light curve of XRF 030723 (and XRGRB 041006) can be obtained either for a uniform jet with sharp edges viewed off-axis or for a Gaussian jet with a Gaussian profile in both $\epsilon$ and $\Gamma_0 - 1$ viewed from outside its core.

The fact that the afterglow light curve of an XRF requires a viewing angle that is only slightly outside the edge of the jet, while the afterglow light curve of an XRF requires a larger viewing angle ($\theta_{\text{obs}} \sim 2\theta_0$), provides a consistent picture wherein a roughly uniform jet with relatively sharp edges is viewed as a

For XRGRB 041006 we obtain $(\theta_{\text{obs}} - \theta_0) \sim 0.15\theta_0 \sim 10^{-2}$ rad and $\gamma \sim 240$ at the edge of the jet. The larger value inferred for $\gamma$ might be explained by the smaller value of the off-axis viewing angle, $\theta_{\text{obs}} - \theta_0$, since such a line of sight that is significantly closer to the edge of the jet intersects the beaming cone of the emitting material near the edge of the jet up to a Lorentz factor of $\gamma \sim (\theta_{\text{obs}} - \theta_0)^{-1} \sim 10^2$.

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**Fig. 5.—**$R$-band light curve of XRF 030723 overlaid on theoretical light curves for three different jet structures and viewing angles $\theta_{\text{obs}}/\theta_0 = 0.5$, 1, 1.5, 2, 2.5, 3, 4, 5, 6. The physical parameters are the same as in Fig. 4, where the half-opening angle of the uniform jet, $\theta_0 = 2.9$, is identified with the core angle in the two other jet structures. [See the electronic edition of the Journal for a color version of this figure.]

GRB from within the jet aperture [i.e., $\gamma(\theta_{\text{obs}} - \theta_0) \leq 1$], as an XRGRB from slightly outside the edge of the jet [i.e., $1 \leq \gamma(\theta_{\text{obs}} - \theta_0) \leq \text{a few}$], and as an XRF from yet larger off-axis viewing angles [i.e., $\gamma(\theta_{\text{obs}} - \theta_0) \geq \text{a few}$].

### 5.3. Other Events with Sparse Data

Besides the two events discussed above (in §§ 5.1 and 5.2), there have been a few other XRFs with candidate afterglow detections. The data in these cases are, however, too sparse to allow any meaningful constraint on theoretical models.

XRF 020903, detected by HETE-2, had an exceptionally low peak energy of ~5 keV. Detection of the optical and radio afterglow was reported by Soderberg et al. (2004), together with the identification of the likely host galaxy at $z = 0.251$. Due to the large error box and the proximity to two other transient sources (which delayed prompt identification), the optical light curve at early times was not well sampled. The first detection is at $t = 0.9$ days after the burst, while later observations are dominated by the light from the host. In contrast to the sparse optical measurements, the radio light curve was extensively monitored with the Very Large Array over the period 25–370 days. The source, which was monitored at frequencies of 1.5, 4.9, 8.5, and 22.5 GHz, was found to have a temporal index $\alpha$ similar to that of “standard” GRBs (Fain et al. 2003).

XRF 020427 was detected by BeppoSAX, and no redshift measurement is available. There is a detection of X-ray emission at $t < 100$ s and a later detection at $t \sim 1$ day. If the last of
the early-time detections (at $t \sim 50$ s) is indeed marking the beginning of the afterglow (as suggested by Amati et al. 2004), then the inferred steep afterglow decline would be hard to reconcile with a sharp edge seen off-axis. However, given the lack of coverage, it is not clear whether the detection at $t \sim 50$ s is indeed part of the afterglow or, instead, still a component of the prompt emission. In the latter situation, with only one X-ray detection available, there is not much that can be said in terms of possible models.

Other cases with possible counterparts are XRF 040912, which has a candidate X-ray afterglow between 13.57 and 38.65 hr, and XRF 040916, which has an optical afterglow candidate but with no X-ray detection.

5.4. Supernova Signatures in XRFs

The combined results on SN 1998bw and SN 2003dh offer the most direct evidence yet that typical, long-duration, energetic GRBs result from the deaths of massive stars (e.g., Hjorth et al. 2003; Stanek et al. 2003). The lack of hydrogen lines in both spectra is consistent with model expectations that the star lost its hydrogen envelope to become a Wolf-Rayet star before exploding. The broad lines are also suggestive of an asymmetric explosion viewed along the axis of most rapid expansion (Mazzali et al. 2001; Zhang et al. 2002b). Despite the rather large uncertainty in the true event rate of GRBs, a comparison with the event rate of Type Ib/c SNe suggests that only a small fraction, $f_{\text{GRB}} \leq 10^{-3}$, of such SNe produce GRBs. While the great majority of Type Ic SNe appear to lack the engine-driven ejecta that characterize the SNe associated with GRBs (Berger et al. 2003), a comparison between the peak luminosity of the local Type Ib/c SNe and that of the combined sample of GRB/XRF-associated SNe shows that these are likely to be drawn from the same population (Soderberg et al. 2005b). The current sample is, however, too small to establish whether this holds true for the GRB-SN and the XRF-SN samples separately.

If the unification hypothesis discussed here is true (or in any model where GRBs and XRFs are intrinsically the same object), XRFs should indeed be accompanied by a SN (Zhang et al. 2004b) brightening in their afterglow light curves similarly to GRBs. As of the time of writing, however, only two XRFs (namely XRF 020903 and XRF 030723) have a candidate SN association. Optical observations with the *Hubble Space Telescope* (HST) by Soderberg et al. (2005a) have yielded strong spectroscopic evidence for a SN associated with XRF 020903. Given its redshift, $z = 0.251$, the luminosity of the candidate SN must be, however, up to ~1 mag fainter than SN 1998bw at maximum light. XRF 030723, on the other hand, has a well-sampled light curve but no measured redshift. There are, nevertheless, both upper and lower limits on its redshift. A lower limit of $z \geq 0.3$ has been derived from the nondetection of its host galaxy (Fynbo et al. 2004a), while an upper limit of $z < 2.3$ was derived from the lack of Ly$\alpha$ absorption. Fynbo et al. (2004a) obtained optical photometry and spectroscopy of XRF 030723 and found that the optical counterpart showed a “bump” in the light curve that may be the signature of a SN component. As discussed in § 5.2, the temporal and spectral energy distribution evolution are hard to reconcile with other interpretations such as a refreshed shock or a density variation in the external medium. For the redshift range $z \sim 0.3$–1, all possible SN models require a rather small mass of synthesized $^{56}$Ni (Tominaga et al. 2004). This is because the SN brightness at this distance is ~2 mag fainter than SN 1998bw. As the SN peak luminosity scales roughly linearly with its $^{56}$Ni yield, we would expect very little $^{56}$Ni production from a very faint SN.

The SN associated with XRF 030723 therefore appears to have properties similar to those associated with GRB 010921 and GRB 020410; i.e., it seems to lie at the low end of the hypernova luminosity function and is perhaps even closer in its properties to a normal Type Ic SN. This might potentially be caused by our off-axis viewing angle, which resulted not only in an XRF instead of a GRB but also in a dimmer SN, as opacity effects prevented us from seeing the brightest part of the SN ejecta, which lies along the rotational axis. Nomoto et al. (2005) find that for the SNe that are associated with GRBs (or hypernovae), a significant decrease in luminosity may occur only for viewing angles $\theta_{\text{obs}} \approx 30^\circ$. This is a direct consequence of the anisotropic distribution of the SN ejecta. We find, however, that for XRF 030723 $\theta_{\text{obs}} \sim 20^\circ$, which is well below 30$^\circ$. Thus, the SN associated with XRF 030723 is probably intrinsically dimmer than SN 1998bw, similarly to the one associated with XRF 020903.

While the Type Ic SNe that are firmly associated with GRBs are very bright Type Ic events with SN 1998bw being the brightest), the lack of a SN in GRBs 010921 (Price et al. 2003) and 020410 (Levan et al. 2005b) to a limit of ~1.5 and ~2 mag fainter than SN 1998bw, respectively, suggests that also for the Type Ic SNe that are associated with GRBs we may be seeing a broad luminosity function. A recent *HST* search for SNe accompanying XRFs by Soderberg et al. (2005a) has yielded upper limits to the presence of a SN 1998bw–like supernova in XRFs 040701, 040812, and 040916. In the case of XRF 040701, which has a known redshift ($z = 0.21$), the HST limit constrains the SN component to be ~6 mag fainter than SN 1998bw. Combining their results with the lack of detection in two other cases (XRFs 011030 and 020427; Levan et al. 2005a), Soderberg et al. (2005a) suggest that XRFs are associated with systematically fainter SNe. While clearly more data on the SN-GRB/XRF connection are necessary before we can understand the full extent of the relation between these phenomena, we note that selection effects may play more of a role against observations of SNe associated with XRFs than of those associated with GRBs. In particular, if as in our model GRBs are seen on-axis while XGRBs and XRFs are seen at increasingly large values of $\theta_{\text{obs}}$, dust obscuration can play a role in selectively obscuring the SNe associated with XRFs and XGRBs more than those associated with GRBs. In the off-axis jet model, indeed, prompt and intense X-ray/UV radiation from the reverse shock may efficiently destroy and clear the dust (Waxman & Draine 2000; Fruchter et al. 2001; Perna & Lazzati 2002) in the circumburst cloud within the solid angle corresponding to the initial jet aperture, i.e., at $\theta < \theta_0$. This implies relatively little extinction for on-axis viewing angles, $\theta_{\text{obs}} < \theta_0$ (practically no extinction of emission from $\theta < \theta_0$ and a gradual increase in the extinction as $\theta$ increases above $\theta_0$) but a relatively large extinction for off-axis viewing angles, $\theta_{\text{obs}} > \theta_0$, especially for emission arising from $\theta > \theta_0$. Interestingly enough, in this case there could be many more obscured XRF optical afterglows, compared to GRB optical afterglows.

6. CONCLUSIONS

The existing XRF models have been examined and their predictions tested against the afterglow observations of XRF 030723 and XGRB 041006, the events with the best monitored
afterglow light curves to date within their respective class. We find that most models failed to reproduce the very flat part observed in their early afterglow light curve. This behavior is, however, naturally produced by a uniform jet viewed off-axis (i.e., from $\theta_{\text{obs}} > \theta_0$). The edge of the jet must be sufficiently sharp, so that the emission at early times would be dominated by the core of the jet, rather than by material along the line of sight. Even for a jet with a narrow core and wings where the energy per solid angle drops as $\propto \theta^{-3}$, as expected in the collapsar model, the afterglow light curves at early times are not quite as flat as those observed in XRF 030723 and XRGRB 041006. A Gaussian jet can produce a sufficiently flat light curve at early times as long as both $\epsilon$ and $\Gamma_0 - 1$ have a Gaussian profile (but not for a constant initial Lorentz factor $\Gamma_0$; see Fig. 5).

The afterglow light curve of XRGRB 041006 requires $\gamma(\theta_{\text{obs}} - \theta_0) \sim 0.15\theta_0 \sim 0.8 \times 10^{-2}$ rad, while that of XRF 030723 requires $\gamma(\theta_{\text{obs}} - \theta_0) \sim \theta_0 \sim 3^\circ \sim 0.5$ rad. This supports a unified picture for GRBs, XRGRBs, and XRFs, wherein they all arise from the same narrow and roughly uniform relativistic jets with reasonably sharp edges and differ only by the viewing angle from which they are observed. Within this scheme, GRBs, XRGRBs, and XRFs correspond to $\gamma(\theta_{\text{obs}} - \theta_0) \leq 1$, $1 \leq \gamma(\theta_{\text{obs}} - \theta_0) \leq a$ few, and $\gamma(\theta_{\text{obs}} - \theta_0) \geq a$ few, respectively.

The empirical classification scheme by which an event is tagged as a GRB, XRGRB, or XRF (see § 2) is rather arbitrary. Therefore there could be some cases where a jet that is viewed on-axis ($\theta_{\text{obs}} < \theta_0$) will be classified as an XRGRB or XRF instead of as a GRB, or there could be the opposite case in which a jet viewed off-axis ($\theta_{\text{obs}} > \theta_0$) might be classified as a GRB instead of as an XRGRB or XRF. A more physically motivated classification would be according to the ratio of the viewing angle $\theta_{\text{obs}}$ and the jet half-opening angle $\theta_0$ [e.g., on-axis events vs. off-axis events, where off-axis events could further be classified according to the value of $\gamma(\theta_{\text{obs}} - \theta_0)$, instead of relying purely on spectral characteristics as in the present empirical scheme. Such a classification would, however, be much harder to implement, as it is not a trivial task to accurately determine the viewing angle.

Future observations with HETE-2 and the recently launched Swift satellite will allow us to further test this picture and might also provide us with the necessary information to test the structure of the jet. The strongest constraints could be obtained from afterglow light curves of XRFs and XRGRBs that are well monitored from early times and at various frequencies (ranging from radio to X-rays). A useful complementary method for constraining the jet structure is via the statistics of the observed jet break times $t_j$ in the afterglow light curves and the corresponding viewing angle $\theta_{\text{obs}}$ in the universal structured jet model or the jet half-opening angle $\theta_0$ in the uniform jet model (Perna et al. 2003; Nakar et al. 2004; Liang et al. 2004).

Similarly, the large statistical sample of GRBs and XRFs with redshift that will be available during the HETE-2/Swift era will allow a reconstruction of the intrinsic luminosity function of the prompt emission. If GRBs, XRGRBs, and XRFs are only a manifestation of the viewing angle for a structured, universal jet (whose wings are producing the XRFs), then no break would be expected in the luminosity function. On the other hand, if GRBs are the results of viewing angles that intersect the jet (whether structured or not), while XRFs and XRGRBs are off-axis events, then one would naturally expect a break in the luminosity function. Guetta et al. (2004) found that a luminosity function with a break is favored in order for the predicted rate of local bursts to be consistent with the observed rate. This also prevents the existence of an exceedingly large number of GRB remnants in the local universe (Loeb & Perna 1998; Perna et al. 2000).

The relative fraction of XRFs and XRGRBs to GRBs is also expected to be different in the various models (Lamb et al. 2005). If indeed an XRF corresponds to $\gamma(\theta_{\text{obs}} - \theta_0) \sim a$ few and $\gamma(\theta_{\text{obs}} - \theta_0) \lesssim \theta_0$, the solid angle from which an XRF is seen scales as $\theta_0/\gamma$ or as $\theta_0$ for a constant $\gamma$ (at a constant distance to the source), while the solid angle from which a GRB is seen scales as $\theta_0^2$. Therefore, the ratio of solid angles for GRBs and XRFs scales as $\theta_0$, and more GRBs compared to XRFs would be seen for larger $\theta_0$. As the distance to the source increases, XRFs could be detected only out to a smaller off-axis viewing angle, while most GRBs would still be bright enough to be detected out to reasonably large redshifts. Therefore, the ratio of GRBs to XRFs should increase with redshift. Finally, if the true energy $E_p$ in the jet is roughly constant, then the maximal redshift out to which a GRB could be detected would decrease with $\theta_0$ since $E_{\gamma, \text{iso}} \propto \theta_0^{-2}$. This would increase the statistical weight of narrow jets in an observed sample, as they could be seen out to a larger volume.

We now briefly mention a few possible implication of the off-axis model for XRFs and XRGRBs. For sufficiently large viewing angles outside the edge of the jet, one might expect some decrease in the variability of the prompt emission. This is since the width of an individual spike in the light curve scales as $\Delta t \propto \delta \sim (\gamma(\theta_{\text{obs}} - \theta_0))^2$ while the peak photon energy and fluence scale as $E_p \propto \delta^{-3}$ and $f \propto \delta^{-3}$, respectively. Since the interval between neighboring spikes in the light curve is typically comparable to the width of an individual spike, $\Delta t$, then if $\Delta t$ increases significantly for large viewing angles this would cause at least some overlap between different pulses, which would smear out some of the variability. Thus one might expect XRFs and XRGRBs to be somewhat less variable than GRBs, at least on average, where a lower variability might be expected for lower values of $E_p$. This may lead to a simple physical interpretation of the observed variability-luminosity relation in the prompt gamma-ray/X-ray emission (Fenimore & Ramirez-Ruiz 2000; Reichart et al. 2001).

In the internal shocks model, if all the different collisions between shells in the outflow within a given event are exact copies of each other and occur at exactly the same radius $R$, then the observed spacing in the onset of the resulting spikes in the light curve would be independent of the viewing angle $\theta_{\text{obs}}$. In practice, however, one might expect a spread $\Delta R \sim R$ in the radius of collision between different pairs of shells and a similar spread in radius for each collision, due to the finite time it takes the shocks to cross the shells. This would cause a random spread in the observed onset time of the different spikes in the light curve of about $\Delta t_{\text{onset}} \sim \Delta R(\theta_{\text{obs}} - \theta_0)^2/2c \sim (\theta_{\text{obs}} - \theta_0)^2/2c$ for off-axis observers. The on-axis duration of a single pulse is $\Delta t_0 \sim R/2c\gamma^2$ so that $\Delta t_{\text{onset}} \sim \delta\Delta t_0 \sim \Delta t$; i.e., the random spread in the onset of the different spikes is comparable to the observed duration of a single spike.

The total duration of the burst will therefore change significantly (i.e., become significantly longer) only for large off-axis viewing angles for which $\delta \gtrsim t_0/\Delta t_0 \sim 10-100$, where $t_0$ is the observed duration of the burst when viewed on-axis. For such large viewing angles most of the variability would be washed out, typically resulting in a light curve with a single peak. For more moderate off-axis viewing angles for which $\delta \sim (\gamma(\theta_{\text{obs}} - \theta_0))^2 < t_0/\Delta t_0 \sim 10-100$, the total duration of the burst does not change.

\footnote{One usually associates $\Delta t_0$ and $t_0$ with the variability and total activity timescales of the source, respectively.}
significantly while its variability decreases with increasing viewing angle \( \theta_{\text{obs}} \), due to the incrementing overlap between different pulses in the light curve of the prompt emission.

Another possible signature of the off-axis model for XRFs is in the reverse shock emission. If the reverse shock is at least mildly relativistic, then the optical flash emission would be less beamed than the prompt X-ray or gamma-ray emission, due to the deceleration of the ejecta by the passage of the reverse shock. This might cause the optical flash to be suppressed by a smaller factor relative to the gamma-ray emission, compared to the corresponding on-axis fluxes. Thus XRFs or XRGRBs might still show reasonably bright optical emission from the reverse shock, which might in some cases be almost as bright as for classical GRBs. Finally, XRFs and XRGRBs might also show a larger degree of polarization compared to GRBs (see § 4.4).

An important conclusion from this study is that jet models in which \( \epsilon \) and \( \Gamma_0 \) vary smoothly inside the jet, and where our lines of sight are within the jet, do not naturally reproduce the afterglow light curves of XRF 030723 and XRGRB 041006. The best example of such a model is the “universal structured jet” model (Lipunov et al. 2001; Rossi et al. 2002; Zhang & Mészáros 2002b), where both \( \epsilon \) and \( \Gamma_0 \) vary smoothly as a power law in \( \theta \) (the usual assumption being that \( \epsilon \propto \theta^{-2} \) outside of some core angle). This model fails to account for the very flat initial part of the afterglow light curves and its subsequent decay.

A possible way around this problem might be to identify the flat part of the light curve with the passage of the break frequency \( \nu_m \), through the optical band. This should be accompanied by a change in the optical spectral slope and should not be observed in other frequency ranges such as the radio or X-rays. For XRGRB 041006 this may actually provide a viable explanation for the data (see Fig. 6). For XRF 030723, however, a similar model fails because it does not reproduce both of the observed values of the temporal index \( \alpha_{\text{op}} \) (before or after the passage of \( \nu_m \)) or the observed spectral slope \( \beta_{\text{op}} \). One could in principle invoke both a jet break and the passage of a break frequency at roughly the same time, for a jet viewed on-axis. This would require that \( \nu_m \sim \nu_e \sim \nu_{\text{op}} \) at \( t \approx 0.1-1 \) days, which is a large coincidence and is therefore unlikely. Even if this were the case, this assumption would be hard to reconcile with the measured optical spectral slope of \( \beta_{\text{op}} = 0.96 \pm 0.04 \) at \( t = 1.13 \) days, as the spectral break frequencies would still be near the optical at that time, resulting in a smaller value of \( \beta_{\text{op}} \). The afterglow light curve of XRF 030723 therefore provides evidence against this class of models.

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13 Such constraints would not leave enough free model parameters to also account for the temporal decay index in the X-rays, \( \alpha_X \).

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