Assessment of friction from compression ring conjunction of a high-performance internal combustion engine: A combined numerical and experimental study

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Abstract
The paper presents direct measurement of in-cylinder friction from a single cylinder motocross race engine under motored conditions and compares the same with a new analytical predictive method. These conditions are encountered in piston–cylinder system with the application of cylinder deactivation (CDA) technology, which is a growing trend. The analytical method takes into account the various regions within instantaneous contact of compression ring–cylinder liner, including lubricant film rupture, cavitation zone and the subsequent lubricant film reformation. The analysis also includes the effect of boundary friction and lubricant rheology. The predictions and direct measurements of cyclic friction show good agreement and indicate dominance of viscous friction under the investigated engine running conditions. In particular, it is shown that the compression ring contribution to in-cycle friction is most pronounced in the region of high cylinder pressures because of combined Poiseuille friction and some boundary solid interactions. The combined experimental-analytical approach has not hitherto been reported in literature.

Keywords
In-cycle friction, floating liner, compression ring, viscous friction, boundary friction, cylinder deactivation

Introduction
The engine friction consumes around 7–8% of generated combustion energy in an internal combustion (IC) engine. Nearly half of these frictional losses are due to the piston system.¹,² The frictional losses from the compression ring conjunction alone can amount for 3% of the total engine losses, which is quite significant for such a small component of the engine system.³,⁴ With the combination of pervading global competition in the automotive sector, the rising fuel costs and ever stringent emission regulations, it is clear that these levels of parasitic losses are unsustainable. Therefore, a combination of verifiable methods of prediction and direct measurement of friction has to be sought so that the effect of any subsequent palliative measures may be accurately ascertained. The palliative approaches usually include the use of hard wear-resistant smooth coatings, cross-hatch honed cylinder liners and/or introduction of lubricant retaining textures in regions with poor lubricant entrainment such as at the piston dead centre reversals.⁵–⁸

Indirect measurement of friction is routinely performed through use of net indicated mean effective pressure (NIMEP).²,³ However, the method is prone to inaccuracies. Therefore, floating liners have been developed to directly measure friction from engine test rigs. The principle of a floating liner was used by Furuhama and Sasaki,⁹ based on a cylinder liner whose only connections to the bore were restricted through a set of intervening piezoelectric transducers. The inertial motion of the piston drags the liner, with the reaction measured by the transducers. The total reaction is equivalent to the net applied force on the liner due to gas pressure loading and the opposing friction. The principle of the operation and the system dynamics is fully explained by Gore et al.¹⁰,¹¹ A brief explanation of this is provided in the next section.

The compression ring–liner conjunction is a multi-parameter variate problem where a plethora of parameters affect the regime of lubrication, thus the...
generated numerical analyses with varying degrees of complexity. The basic approach assumes good circumferential ring-bore conformance. This enables the solution of Reynolds equation (as the hydrodynamic governing equation) in one dimension with an analytical approach. Haddad and Tjan\textsuperscript{12} show that such a simplification can be assumed with good ring-bore peripheral conformance and crucially the fitted ring’s perimeter-to-face width ratio being greater than 30 (assumed long line sliding contact). With this method other salient features such as the effect of surface topography can also be included within an analytical solution,\textsuperscript{13} thus not resulting in long computation times. For example, Sawicki and Yu\textsuperscript{14} provide such a solution, incorporating the effect of lubricant cavitation which affects both the load-carrying capacity and generated friction.

Morris et al.\textsuperscript{15} provide an alternative analytical solution which makes use of average flow model representation of Reynolds equation, including the effect of surface topography in the prediction of viscous friction with the addition of boundary contribution, based on the approach of Greenwood and Tripp.\textsuperscript{16} Morris et al.\textsuperscript{17} and Shahmohamadi et al.\textsuperscript{18} also included a control volume thermal mixing model to take into account the effect of lubricant shear heating as well as surface temperature of the contiguous solids (liner and the ring); the latter using a computational fluid dynamics approach. This predicts more realistic lubricant viscosity, thus generated friction. Another tribodynamic analysis including the effect of generated temperature for the high-pressure region around the top dead centre (TDC) reversal from compression to power stroke was recently provided by Mishra.\textsuperscript{19} A combined solution of Reynolds and energy equations was made.

The engine used in the current investigation is a high-performance spark ignition single-cylinder motocross motorbike engine, which uses a single compression ring of 1.15 mm face width. The floating liner has a bore of 96 mm; thus a fully fitted ring has a perimeter of 301.1 mm, with a fitted end gap of 0.4 mm. The perimeter-to-face width ratio is in excess of 262, justifying the use of one-dimensional sliding analysis. In practice, however, the bore is out-of-round\textsuperscript{20} although every effort is made for the current floating liner to closely approximate an idealised right circular cylindrical shape. Furthermore, the ring is subjected to variable chamber pressure loading,\textsuperscript{21} thus in reality ring dynamic occurs,\textsuperscript{22–24} which would ideally require a lengthy two-dimensional solution such as those developed in Ma et al.\textsuperscript{25} Bolander et al.\textsuperscript{26} and Mishra et al.\textsuperscript{27,28} Nevertheless, for the conditions described in this paper a one-dimensional analytical solution is quite adequate and shows good conformance to the measurements. In fact, such a combined analytical-experimental approach has not hitherto been reported in literature.

It should be noted that the results in this study are for motored running conditions. For the engine used the results are applicable to fired conditions with up to 30% throttle for cold running conditions. The engine testing time for in situ measurement is also kept short, typically 15 min in order to guard against any significant rise in the liner temperature, thus enabling a reasonable comparison between the predictions based upon an isothermal analytical method and the measured results. It is also applicable to deactivated cylinders in the growing trend in the use of partially deactivated engines in urban driving conditions.

**The engine test-bed**

A Honda CRF 450R motocross motorcycle 4-stroke engine with the maximum speed of 11,000 r/min was chosen because of its high power and torque characteristics (41 kW, 50 Nm). The load-speed combination envelopes a wide range of engine technology. In fact, it is representative of the highest performing naturally aspirated single cylinder engine technology (i.e. over 90 kW/L and 110 Nm/L). The engine’s original engine manufacturer (OEM) barrel was replaced by a wet barrel, containing the floating liner. Due to the differential operating temperature, there is a need to control the clearance between the cylinder liner and the housing, thus minimising the induced stresses in the OEM aluminium structure. The choice of housing material was restricted to materials with a coefficient of thermal expansion between 16 and 18 ppm/K, and yield strength significantly higher than the original OEM engine barrel. Thus, austenitic stainless steel grade 304 was used for the floating liner (Figure 1). The working surface of the liner is coated with a 60 µm thick Ni–SiC layer. As shown, the floating liner is suspended in such a way that any point of contact between the liner and any rigidly mounted components are intervened by a number of piezoelectric load cells.\textsuperscript{10,11} The load cells are preloaded whilst in situ and at rest, including the weight of the liner itself. The preload value is obtained and recorded prior to any testing. Thereupon, the readings of all the load cells are set to zero prior to any testing. This means that the values obtained during any testing represent the dynamic changes only. The infinitesimal movement of the liner is such that the load cells remain perpetually in compression. The total load cell readings equate the inertial force of the liner, dragged by the motion of the piston. The net applied force is due to gas pressure loading on the upper rim of the liner, which is sealed by a labyrinth seal and liner–piston friction. Thus, depending on the sense of liner motion the friction is measured directly as

\[
\pm f = M \Delta \omega - P, \quad (1)
\]

The engine was mounted onto an Oswald 250 kW transient dynamometer. All standard engine testing...
parameters (chamber pressure, air fuel ratio, test cell humidity, test cell temperature, input temperature of fuel and coolant, etc.) were logged as well as friction to ensure reliability and consistency of all measurements. The basic setup is shown in Figure 2. Further details are given by Gore et al.\textsuperscript{10,11}

### Analytical predictive method

With the aforementioned assumptions of good ring–liner conformability and large ring perimeter-to-face width ratio, Reynolds equation in one-dimensional flow along the ring face width becomes

\[
\frac{\partial}{\partial x} \left( \frac{\rho h^3}{6 \eta} \frac{\partial p}{\partial x} - \rho U h \right) = \frac{\partial (2 \rho h)}{\partial t}
\]

where \(U\) denotes the piston sliding velocity.

This form of Reynolds equation assumes no side leakage of the lubricant in the lateral (circumferential) direction to that of lubricant entrainment. This assumption is justified as the ring–liner conjunction enjoys a thin lubricant film.

Therefore, the lubricant entrainment occurs along the ring face width, \(x\) in a domain characterised by

\[
x \in [a, b] \quad \text{where,} \quad a \leq c < r \leq b
\]  

(3)

The parameters \(a, c, r\) and \(b\) represent the contact inlet, lubricant film rupture point (onset of cavitation region), lubricant reformation boundary and the outlet edge of the ring face width, respectively (see Figure 3). These positions demarcate regions of

**Figure 1.** The floating liner (after Gore et al.\textsuperscript{11}).

**Figure 2.** The engine test-bed.
assumed full film, cavitation and lubricant film reformation.

Reynolds equation has to be solved simultaneously with the film shape function in a transient manner

\[ h(x, t) = h_{\text{min}}(t) + h_s(x) \]  

where \( h_s(x) = x^2 / 2R \) is the parabolic shape of the ring face width profile.

The appropriate boundary conditions for solution of Reynolds equation are

\[
\begin{align*}
    p|_{x=a} &= P_a \quad (I) \\
    p|_{x=c} &= P_c \quad (II) \\
    \frac{\partial p}{\partial x}|_{x=c} &= 0 \quad (III) \\
    p|_{x=r} &= P_r = P_c \quad (IV) \\
    p|_{x=b} &= P_b \quad (V)
\end{align*}
\]  

The inlet pressure \( P_a \) varies according to the sense of motion of the piston (Condition (I)). In the upstroke, it is the combustion chamber pressure, whilst in the downstroke it is the inter-ring pressure, which is considered to be the atmospheric pressure in the current study. The lubricant film ruptures at a position \( x = c \), where the lubricant pressure falls below its cavitation vaporisation pressure \( P_c \) (Condition (II)). At this location, the third boundary condition in equation (5) is also taken into account which ensures flow continuity (Condition (III)). The second and third boundary conditions, taken together, are known as the Swift–Stieber boundary conditions. The pressure remains the same in the cavitation region, and gradually rises to that prevailing at the lubricant exit boundary edge of the ring (Conditions (IV) and (V)). These induce lubricant film reformation.

The solution of Reynolds equation has to take into account three different regions in the contact domain as shown in Figure 3 as further explained below.

**Region of full film (a \leq x \leq c)**

Two successive integrations of Reynolds equation with respect to \( x \) yields

\[
p = 6U \int_a^c \frac{\eta}{h^2} \, ds + 12 \int_a^c \left( \frac{\eta}{\rho h^3} \int_a^x \frac{\partial (\rho h)}{\partial t} \, ds \right) \, ds + 6C_1 \int_a^c \frac{\eta}{\rho h^3} \, ds + C_2
\]  

Now using the boundary conditions (I) and (III) yields the integration constants

\[
C_1 = \frac{6U \int_a^c \frac{\eta}{\rho h} \, dx + 12 \int_a^c \left( \frac{\eta}{\rho h^3} \int_a^x \frac{\partial (\rho h)}{\partial t} \, ds \right) \, ds}{6 \int_a^c \frac{2}{\rho h^3} \, dx}
\]

and \( C_2 = P_a \)

Therefore, the pressure distribution in the full film region of the contact is determined by replacing for constants of integration \( C_1 \) and \( C_2 \) from equation (7) into equation (6) in terms of the film rupture position \( x = c \), which is unknown. This position can be determined at any given time (crank angle position), using the boundary condition (III) in equation (5)

\[
6U + \frac{12}{\rho h c} \int_a^c \frac{\partial (\rho h)}{\partial t} \, ds
\]

\[
(P_e - P_a) = \left[ \frac{6U \int_a^c \frac{\eta}{\rho h} \, dx}{6 \int_a^c \frac{2}{\rho h^3} \, dx} \right] + 12 \int_a^c \left( \frac{\eta}{\rho h^3} \int_a^x \frac{\partial (\rho h)}{\partial t} \, ds \right) \, ds = 0
\]
Equation (8) is solved by Newton–Raphson iterations to determine the position \( x = c \). Note that both \( P_c \) and \( U \) are functions of the crank angle location in an engine cycle. \( P_c \) is a function of chamber pressure or is simply atmospheric in the downstroke sense of the piston and the sliding speed \( U \) is given as\(^{29}\)

\[
U(\varphi) = r_c \omega \left( \sin \varphi + \frac{r_c}{2t} \sin 2\varphi + \ldots \right) \quad (9)
\]

**The film reformation region \( r \ll x \ll b \)**

Reynolds equation (2) is doubly integrated again between the limits \( r \) and \( b \)

\[
p = 6U \int_r^b \frac{\eta}{h^2} \frac{dx}{ds} 12 \int_r^b \left( \frac{\eta}{\rho h^3} \int_r^x \frac{\partial (\rho h)}{\partial t} ds' \right) ds + 6C_3 \int_r^b \frac{\eta}{\rho h^3} ds + C_4
\]

Applying the boundary conditions (IV) and (V) yields the integration constants

\[
C_3 = \frac{(P_b - P_r) - \left[ 6U \int_r^b \frac{\eta}{h^2} \frac{dx}{ds} + 12 \int_r^b \left( \frac{\eta}{\rho h^3} \int_r^x \frac{\partial (\rho h)}{\partial t} ds' \right) ds \right]}{6 \int_r^b \frac{\eta}{\rho h^3} dx}
\]

and \( C_4 = P_r \) \( \quad (11) \)

The conjunctural outlet pressure \( P_b \) depends on the sense of piston motion, in the same manner as the inlet pressure \( P_r \). However, constant \( C_3 \) can only be calculated if the film reformation position, \( r \) can be determined. For this purpose, the conditions in the cavitation region should be considered.

**The cavitation region \( c \ll x \ll r \)**

In the cavitation region the pressure is assumed to be constant at the lubricant vapourisation pressure, \( P_c \)\(^{14}\) with the density of lubricant being a function of pressure and its bulk modulus as\(^{30}\)

\[
\beta = \rho \frac{\partial \rho}{\partial \rho} \quad (12)
\]

The ratio of density in the cavitated region to that in the full film region of the contact is defined as the film ratio, \( \theta = \rho_c/\rho_r \), where lubricant density and viscosity vary with pressure and temperature (see the next section).

As the result of constant pressures in the cavitation region, striated flow only proceeds in moderate to highly loaded contacts, mainly due to viscous shear (Couette flow).\(^{31}\) This means that the Poiseuille (pressure-induced) flow in Reynolds equation may be neglected in this region. Therefore, Reynolds equation can be altered to the form, initially proposed by Elrod\(^ {31}\) in terms of \( \theta \) as

\[
\frac{\partial}{\partial x} \left( \frac{\rho_c h^3}{6\eta} g \frac{\partial \theta}{\partial x} - U \rho_c \theta \right) = 2 \frac{\partial (\rho_c \theta h)}{\partial t} \quad (13)
\]

where pressure is replaced by the film ratio as

\[
p = g \theta \ln \theta + P_c
\]

And \( g \) is defined as switching term

\[
g = \begin{cases} 1 & \text{in the full film region} \\ 0 & \text{in the cavitated region} \end{cases}
\]

In the cavitation region with viscous shear flow only, the equation above reduces to

\[
\frac{U \frac{\partial (\theta h)}{\partial x}}{\partial t} + 2 \frac{\partial (\theta h)}{\partial t} = 0
\]

De la Cruz et al.\(^ {32}\) observed that the value of \( \theta \) alters in the cavitation region according to the approach or separation of surfaces, as indicated by the second term in equation (16), where a negative value indicates approach of the surfaces. Equation (16) is essentially a first-order partial differential equation which can be solved using the method of characteristics. Sawicki and Yu\(^ {14}\) show that

\[
(\theta h)_{x=r,t_c} = (\theta h)_{x=r,t_r}
\]

where, \( t_c \) and \( t_r \) are the times at which film rupture and reformation occur.

At the film rupture point: \( \theta_{x=r} = \theta_1 = 1 \), which using equation (17) leads to

\[
\theta_{x=r} = \theta_r = \frac{h_{x=r}}{h_{r,t_r}}
\]

This, together with equation (14) fully describes the cavitation region of the flow. The only remaining unknown is the constant of integration \( C_3 \) in equation (11), which depends on the position at the onset of film reformation. Using the boundary conditions of equation (5) in the Elrod’s equation (13), it follows that

\[
\begin{align*}
\left. \begin{array}{l}
p_{x=r} = P_r = P_c \\
\frac{\partial p}{\partial x} \bigg|_{x=r} = 12 \eta_c \left( \frac{U}{h_r^2} \frac{dr}{dt} \right) (1 - \theta_r) \end{array} \right\} \text{where } \theta_r = \frac{\rho_r}{\rho_c}
\end{align*}
\]

\((19)\)

At the start of reformation region, \( r \), this also must equate to the pressure gradient for the
reformation region in the previous sub-section, obtained as
\[
\frac{\partial p}{\partial x} = \frac{6\eta}{\rho h^2} \left( \rho U h + \int_r^x \frac{\partial (\rho h)}{\partial t} \, dx + C_3 \right)
\] (20)

Equating (19) and (20) and replacing for \( \theta_r \) from equation (18) and after some basic manipulations
\[
C_3 = \rho h_r \left[ \left( \frac{\partial U}{\partial t} - 2 \frac{d\rho}{dt} \right) \left( 1 - \frac{h_{r,t}}{h_{r,t,r}} \right) - U \right]
\]
(21)

Replacing for \( C_3 \) in equation (11) enables the evaluation of the rupture point \( r \) from the equation below using Newton–Raphson iterations
\[
\left( \frac{\partial U}{\partial t} - 2 \frac{d\rho}{dt} \right) \left( 1 - \frac{h_{r,t}}{h_{r,t,r}} \right)
= \left( P_h - P_r \right) - \left[ 6U \int_r^\theta \frac{\eta}{h} \, dx + 12 \int_r^\theta \frac{\eta}{h^3} \int_r^x \frac{\partial (\rho h)}{\partial t} \, dx \right] \frac{d\rho}{dx}
\]
\[
= U + \frac{6\rho_h h_r \int_r^\theta \frac{\eta}{h^3} \, dx}{6\rho_h h_r \int_r^\theta \frac{\eta}{h^3} \, dx}
\]
(22)

**Lubricant rheology**

Lubricant density and viscosity alter with pressure and temperature. The density variation with pressure and temperature in the full film region is given by Dowson and Higginson\(^{33} \) and Yang et al.\(^{34} \)
\[
\rho = \rho_0 (1 - \gamma \Delta T) \left[ 1 + \frac{6 \times 10^{-10}(p - P_{aim})}{1 + 1.7 \times 10^{-9}(p - P_{aim})} \right]
\]
(23)

where \( \gamma \) is the thermal expansion coefficient for the lubricant. It is usually considered to be around \( 6.4 \times 10^{-3} \text{K}^{-1} \); Morris et al.\(^{17} \) showed that the rise in lubricant temperature occurs at the inlet to the contact by the contiguous surfaces conveving heat into the entrant bulk lubricant. Therefore, \( \Delta T \) can be taken as the difference between the liner temperature and the bulk oil temperature, measured from the engine sump (i.e. \( \Delta T = T - T_0 \)). The liner temperature and that of the ring are assumed to be the same, although in practice the moving surface has a slightly higher temperature.\(^{17} \) In the cavitation region, the density is obtained from equation (23) and the film ratio \( \theta \).

Lubricant viscosity alters with temperature more significantly than its density in moderately loaded contacts such as the ring–bore conjunction. According to Houpert\(^{35} \)
\[
\eta = \eta_0 \exp \left[ \ln(\eta_0) - \ln(\eta_{\infty}) \right] \times \left[ \left( \frac{T - 138}{T_0 - 138} \right)^{S_0} \left( 1 + (p - P_{aim})/C_p \right)^{Z - 1} \right]
\]
(24)

where \( Z \) and \( S_0 \) are constants, independent of temperature and pressure
\[
Z = \frac{\alpha_0}{[\ln(\eta_0) - \ln(\eta_{\infty})] / C_p} \quad \text{and} \quad S_0 = \frac{\rho_0(T_0 - 138)}{\ln(\eta_0) - \ln(\eta_{\infty})}
\]
(25)

and, \( C_p = 1.98 \times 10^8 \text{ Pa} \) and \( \eta_{\infty} = 6.31 \times 10^{-5} \text{ Pa.s.} \)

**Contact load and friction**

Disregarding any ring elastodynamic behaviour described by Baker et al.,\(^{24} \) the instantaneous contact load is a quasi-static balance between the applied load to the ring and the contact reaction. The applied forces include the ring tension force, \( F_T \), which strives to return the ring to its unfitted state, as the result adhering it to the liner surface (Figure 3). Additionally, the chamber pressure acts behind the inner rim of the compression ring and acts outwards as the gas force, \( F_G \), also orthogonal to the contact surface. The summation of these forces constitutes the instantaneous applied contact load as
\[
F = F_T + F_G
\]
(26)

It is assumed that 100% of the chamber pressure acts behind the compression ring, which fully conforms circumferentially to the liner surface with the footprint contact area of \( A = 2\pi r_0 (b - a) \), \( r_0 \) being the radius of an idealised liner of right circular cylindrical shape, and \( P_G \) is the chamber pressure. Therefore
\[
F_G = P_G A
\]
(27)

The ring tension force is
\[
F_T = P_e A
\]
(28)

where the uniform elastic pressure \( P_e \) is\(^{36} \)
\[
P_e = \frac{GEI}{3\pi(b - a)r_0^2}
\]
(29)

where \( G \) is the end-gap of the incomplete circular compression ring in its free state.

The net applied force on the ring towards the liner surface is balanced by the contact reaction, comprising the hydrodynamic load-carrying capacity as the result of generated lubricant pressures and any
direct contact of surface asperities. The hydrodynamic reaction is

\[ W_h = 2\pi r_0 \int_{x=a}^{b} pdx \]  

(30)

Note that the low pressures in the cavitation and lubricant film reformation regions do not appreciably contribute to lubricant hydrodynamic reaction.

A small area of asperity contact can occur in the compression ring–liner contact, particularly at piston dead centre reversals with low values of \( U \), thus low entrainment flow of lubricant into the conjunction.\(^\text{13}\) The area of asperity contact is a tiny fraction of the apparent contact area \( A \), described above. If a Gaussian distribution of asperities is assumed, then the proportion of contact load carried by them may be obtained, using Greenwood and Tripp\(^\text{16}\) approach, where the asperity contact area and their share of carried load respectively become

\[ A_a = \pi^2 (\kappa \sigma)^2 A F_2(\lambda) \]  

(31)

\[ W_a = \frac{16\sqrt{2}}{15} \pi (\kappa \sigma)^2 \frac{\sigma}{k} E A F_{5/2}(\lambda) \]  

(32)

The statistical functions \( F_2(\lambda) \) and \( F_{5/2}(\lambda) \) relate to the Gaussian distribution of asperities and are functions of the Striebeck oil film parameter defined as \( \lambda = \lambda_{\text{min}}(t)/\sigma \), where \( \sigma \) is the standard deviation of composite surface roughness of the counterface surfaces. These functions can be represented by the fitted polynomial functions of \( \lambda \) and diminish as \( \lambda \to 3 \) (purely hydrodynamic condition)\(^\text{37}\)

\[ F_2(\lambda) = -0.0018\lambda^5 + 0.0281\lambda^4 - 0.1728\lambda^3 \]  

\[ + 0.5258\lambda^2 - 0.8043\lambda + 0.5003 \]  

(33)

\[ F_{5/2}(\lambda) = -0.0046\lambda^5 + 0.0574\lambda^4 - 0.2958\lambda^3 \]  

\[ + 0.7844\lambda^2 - 1.0776\lambda + 0.616 \]  

(34)

It is noteworthy that the usual cylinder liner configuration is cross-hatch honed. In such cases, the surface topography does not follow a Gaussian distribution of asperities as it forms a plateau. This makes a comparison between analytical predictions and measured results quite complicated. Therefore, for the case of the floating liner in this study a super-finished liner surface is made. For the usual cross-hatched liners the height of the plateau \( \sigma = R_k \) is used, whereas in the current study \( \sigma = R_q \) is appropriate and a Gaussian distribution of asperities is assumed. The surface topography is measured, using an infinite focus white light interferometer with a nominal measurement resolution of 1 nm. The procedure followed is described in detail in Styles et al.\(^\text{38}\)

The total contact reaction is, therefore

\[ W = W_h + W_a \]  

(35)

As already mentioned, there are two contributing sources to conjunctural friction: Firstly, the reported literature shows that for most of the engine cycle, the dominant mechanism of friction is viscous shear of the lubricant. Secondly, in the regions of piston motion with low sliding velocity (at or in the vicinity of motion reversals) there is lack of sufficient lubricant entrainment into the contact conjunction (low value of \( U \)). In these locations two other sources of friction play an important role. One is due to the direct contact of counterface surface asperities (boundary lubrication). The other mechanism is pressure-induced viscous shear (Poiseuille shear), which occurs with a rise in pressure gradient across the conjunction (\( dp/dx \)). This can occur at piston reversals, particularly at the top dead centre and in transition from the compression stroke to the power stroke. All these sources of friction should be taken into account. For lubricant contributions

\[ f_v = \tau_v (A - A_a) \]  

(36)

where

\[ \tau_v = \pm \left( \frac{\Delta p}{2} + \frac{\eta U}{h} \right) \]  

(37)

The contribution due to asperity interactions occurs over the area of asperity peaks \( A_a \). There are two contributions in this case: One is due to adhesive friction of cold welded asperities under localised pressure which is shown by the second term on the right-hand side of equation (38). Here, the coefficient of asperity shear strength, \( \zeta \) is analogous to the coefficient of friction at the asperity-level contact and is usually measured through use of atomic force microscopy (AFM) in contact mode.\(^\text{38,39}\) The second contribution is the first term in equation (38), which is based on the assumption that an ultra-thin film of lubricant is adsorbed to the asperity tips and undergoes non-Newtonian shear at its limiting Eyring shear stress, \( \tau_0 \)\(^\text{40}\).

\[ f_h = \tau_0 A_a + \zeta W_a \]  

(38)

The asperity contacts can also cause elasto-plastic deformation, which affect boundary friction. These are not taken into account, but are indirectly accounted for by the direct measurement of \( \zeta \). The value of \( \zeta \) corresponds to the coating of the cylinder liner which is Ni–SiC. This is obtained through use of an AFM, operating in lateral force mode as fully described by Styles et al.\(^\text{38,39}\) More comprehensive
models for asperity level friction have recently been developed.\textsuperscript{41,42} Finally, the total friction is

\[ f = f_v + f_b \] (39)

Therefore, the predicted and measured frictions from equations (1) and (39) can be compared.

**Solution method**

The following solution procedure is followed:

**Step 1**: At the initial crank angle (time), an initial value for the hydrodynamic pressure distribution enables calculation of the corresponding rheological parameters from ‘Lubricant rheology’ section. In addition, an initial value for the minimum film thickness, \( h_{\text{min}} \), and squeeze film velocity \( \frac{dh}{dt} \), is assumed. These values are subsequently altered during the iteration process.

**Step 2**: The pressure distribution is calculated (‘Analytical predictive method’ section).

**Step 3**: The rheological properties of lubricant are updated based on the pressure distribution from Step 2. This step is repeated until the following convergence criterion is met

\[ \sum_{i=0}^{N} \frac{|p_i^{\text{new}} - p_i^{\text{old}}|}{\sum_{i=0}^{N} p_i^{\text{new}}} < 10^{-4} \] (40)

**Step 4**: The final hydrodynamic pressure distribution is integrated over the entire contact area (equation (30)). The asperity load support is also calculated from equation (32).

**Step 5**: The instantaneous applied contact load is obtained from equations (26) to (29).

**Step 6**: Instantaneous quasi-static equilibrium at a given crank angle demands that the following convergence criterion is satisfied

\[ \frac{|W - F|}{F} < 10^{-3} \] (41)

Otherwise, a new minimum film thickness value is calculated from

\[ h_{\text{min}}^{\text{new}} = h_{\text{min}}^{\text{old}} \left[ 1 + \chi \left( \frac{W - F}{F} \right) \right] \] (42)

where the numerical damping factor was considered to be \( \chi = 0.075 \) for optimum trade-off between solution stability and computation time.

Then, Steps 2 to 6 are repeated until the condition (41) above is satisfied.

The calculation process continues until a periodic minimum film thickness variation is achieved for the whole engine cycle.

**Results and discussion**

In practice, it is difficult to isolate the frictional losses from a particular conjunction (such as that of the compression ring–liner contact) in an IC engine.

Firstly, unlike multi-cylinder configuration, in single cylinders the contribution to frictional losses is quite significant in the case of engine bearings.\textsuperscript{43} Consequently, the single cylinder engine used in this investigation uses rolling element bearings as its big-end bearing, which significantly reduces the...
Table 1. List of engine specifications and employed data.

| Parameter                          | Value | Unit |
|-----------------------------------|-------|------|
| Engine speed                      | 3000  | r/min|
| Connection rod length             | 107   | mm   |
| Engine stroke                     | 62.1  | mm   |
| Liner base material               | Steel | –    |
| Liner coating material            | Ni–SiC| –    |
| Bore nominal radius               | 48    | mm   |
| Top ring material                 | Steel | –    |
| Liner elasticity modulus          | 203   | GPa  |
| Liner Poisson's ratio             | 0.3   | –    |
| Ring elasticity modulus           | 203   | GPa  |
| Ring Poisson's ratio              | 0.3   | –    |
| Ring end gap                      | 10.5  | mm   |
| Ring face width                   | 1.15  | mm   |
| Coefficient of asperity shear     | 0.22  | –    |
| Ra for liner surface              | 0.515 | µm   |
| Ra for ring surface               | 0.201 | µm   |
| Combined roughness parameter (r/ñ) | 0.0771 | – |
| Combined roughness parameter (ñ/β) | 0.211  | –    |
| Operating temperature             | 25    | °C   |
| Oil density at 15 °C              | 833.8 | kg/m³|
| Oil viscosity at 40 °C            | 50    | mPa.s|
| Thermal expansion coefficient     | 6.4 × 10⁻⁴ | K⁻¹ |
| Pressure–viscosity coefficient, α₀| 1 × 10⁻⁸ | Pa⁻¹ |
| Temperature–viscosity coefficient, β₀| 0.04 | K⁻¹ |

generated friction when compared with the usual elliptic bore journal bearing. This is another reason for the choice of Honda CRF 450R engine for this study.

Secondly, direct measurement of in situ friction requires a floating liner, described in The Engine Test-bed Section. A somewhat over-sized piston, providing a nominal clearance of 50 µm was specifically produced in order to be able to remove the top compression ring and measure friction of the piston skirt and oil control ring assembly alone under motored conditions. Such a test is not possible under fired conditions. The difference between the friction of full piston assembly (with the compression ring included) and that without it, is assumed to yield the frictional contribution of the compression ring. Fortunately, with the Honda CRF 450R, the chamber pressure reaches a maximum value of 20 bar at the top dead centre without cylinder firing (Figure 4). This is quite representative of chamber pressure for fired condition at 30% throttle at the same engine speed of 3000 r/min. This has the added advantage of eliminating other phenomena under fired conditions, such as piston and liner thermo-elastic distortion. Therefore, the motorised testing in line with the above stated conditions reported here can also provide representative conditions for fired engine conditions at cold start-up.

Table 1 lists the engine specifications and all the data used as the input to the analysis. Note that the maximum cylinder pressure occurs at the top dead centre under motored condition and is slightly lower without the presence of the top compression ring because the cylinder chamber is not completely sealed, even with a slightly over-sized piston.

Figure 5(a) shows the measured friction using the floating liner’s piezo-electric transducers, chamber pressure curves in Figure 4 and equation (1). The changes of sign in friction represent piston reversals. The gap between the two traces can be attributed to the frictional contribution of the compression ring. The results show that the main contribution to friction in the case of this engine set up and running conditions is due to the piston skirt and oil ring. For the test conditions reported here (Table 1), the compression ring friction contribution is approximately 10–15% of the total (Figure 5). Since the conditions with or without the compression ring in place are not identical (e.g. different in-cylinder pressures) and there is a certain amount of noise resident on the friction traces, the signals cannot reliably be subtracted.

Figure 5(b) shows the predicted friction during an engine cycle under the same conditions as those in Figure 5(a). The variations in the sliding velocity are also shown in the figure. The first thing to note is that friction variation is directly proportional to the sliding velocity (i.e. \( f \propto U \)), indicating that Couette shear of the lubricant film is the dominant responsible mechanism for friction (see second term on the right-hand side of equation (37)). This proportionality is lost in the region of rising chamber pressures prior to the TDC and proceeds further into the last stages of expansion stroke (corresponding to the power stroke in a fired engine). However, this rise in friction cannot entirely be attributed to the boundary friction effect as examining the variations of the minimum film thickness shown in Figure 6 indicates that the minimum film thickness barely falls below the mixed regime of lubrication (the demarcation boundary: \( \lambda = 3 \) line in Figure 6). In fact only in a very small part of the aforementioned compression-to-intake region someasperity interactions occur. This highlights the contribution from the pressure-induced shear (Poiseuille shear) as shown by the first term on the right hand side of equation (37). Therefore, in the case of a motored engine, where a sufficient supply of lubricant is available on the liner at the TDC reversal, the shear induced by pressure gradient at the end of the compression stroke and start of the expansion stroke can be quite significant.

Figure 5(c) and (d) shows the compression ring–liner friction contributions in two regions.
One region is in the compression part of the cycle, prior to the TDC reversal at the crank angle of 0° and the other is in the early stages of the expansion stroke, past the same TDC reversal. An average value for each region is calculated from measurements and predictions. These are shown in Figure 5(c) and (d).

Reasonably good agreement is demonstrated. However, there are some residual differences which can be attributed to many causes. These may include some of the assumptions of the analytical method used, such as ring–liner circumferential conformity, ignoring the piston (and ring) dynamics, assumed isothermal conditions and/or a fully flooded conjunctional inlet. Although the engine is motored and the test duration does not exceed 15 min, the viscous shear of the lubricant can promote a rise in its temperature and that of the adjacent solid boundaries. Therefore, the isothermal analysis here can lead to a certain degree of error. Furthermore, in practice a fully flooded inlet in the upstroke sense of the engine is not likely, and such an assumption can be regarded as idealised. On the experimental side the presented results are average of many cycles, where there are small variations (1–2%) in chamber pressure. In addition, the position of TDC reversals can alter from cycle to cycle, this being a characteristic of inherently unbalanced...
single cylinder engines. Nevertheless, there is generally good overall agreement between measurements and predictions.

Conclusions

The paper presents direct in situ measurement of incylinder friction using a devised floating liner system. With a slightly over-sized piston, it was possible to remove the compression ring in the single cylinder motocross motor-cycle engine. The difference in the cyclic frictional traces with and without the presence of the compression ring provided an assessment of incylinder friction contributed by the compression ring. An analytical predictive method, based on Elrod's modification to Reynolds equation, taking into account the effect of film reformation is also presented. The predicted viscous friction using this approach, supplemented by boundary friction as the result of any asperity interactions has shown reasonable agreement with the measurements. Both predictions and measurements show that the contribution of compression ring is most significant in the high pressure part of the engine cycle and at top centre reversal between compression and expansion strokes. This indicates that the compression ring complies with its primary sealing function. Viscous friction of the lubricant dominates under the tested and simulated isothermal motored conditions. This in fact is representative of idle to low-speed cycling in creeping traffic with a cold engine (conditions which typically form a part of the high performance engines using CDA). The next stage of this research is to include the thermal effects in the analysis and undertake measurement and simulation for steady-state hot engine cycle at simulated low crawling speeds (another part of the NEDC). It is anticipated that boundary friction would play a more significant role under such conditions.

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### Appendix

#### Notation

- $a, b$: front and rear coordinates of piston ring/cylinder liner contact
- $a_t$: acceleration of floating liner
- $A$: piston ring/cylinder liner contact area
- $A_a$: total contact area at the tip of asperities of two opposing surfaces
- $c$: cavitation (film rupture) point
- $C_1$ to $C_4$: integration constants
- $E$: composite elasticity modulus
- $EI$: piston ring flexural rigidity
- $f$: total friction
- $f_b$: boundary friction
- $f_v$: viscous friction
- $F$: total force applied on the ring liner contact
- $F_2, F_{5/2}$: statistical functions
- $F_G$: gas force on the back of the ring
- $F_T$: ring elastic tension force
- $g$: switching parameter
- $G$: ring end gap at free state
- $h$: film thickness
- $h_{\text{min}}$: minimum film thickness
- $h_s$: ring face profile
- $\ell$: connecting rod length
- $M$: floating liner mass
- $N$: total number of computational segments
- $p$: pressure
- $p_e$: elastic pressure
- $P_{\text{atm}}$: atmospheric pressure
- $P_G$: in-cylinder gas pressure
- $P_s$: gas force at the upper rim of the floating liner
- $r$: film reformation point
- $r_0$: bore radius
- $r_{cr}$: crank pin radius
- $R$: radius of curvature for ring face
- $s_s, s'$: intermediate integration variables
- $S_0, Z$: viscosity constants
- $t$: time
- $T$: temperature
- $T_0$: ambient temperature
- $U$: piston velocity
- $W$: total load supported by contact
- $W_a$: load supported by asperities
- $W_h$: hydrodynamic load
- $x$: Cartesian coordinate
- $a_0$: atmospheric viscosity-pressure coefficient
- $\beta_0$: atmospheric viscosity-temperature coefficient
- $\beta$: bulk modulus of elasticity
- $\chi$: numerical damping factor
- $\eta$: dynamic viscosity
- $\eta_0$: dynamic viscosity at atmospheric pressure
- $\gamma$: thermal expansion coefficient
- $\kappa$: average radius of curvature of asperity tips
- $\lambda$: Stribeck oil film parameter
- $\omega$: engine speed
- $\phi$: crank angle
- $\rho$: density
- $\rho_0$: density at atmospheric conditions
- $\sigma$: standard deviation of composite surface roughness of the counterface surfaces
- $\xi$: coefficient of asperity shear strength
- $\tau_v$: viscous shear stress
- $\tau_0$: Eyring shear stress
- $\theta$: film ratio
- $\xi$: number of asperity peaks per unit area

#### Subscripts

- $a, b$: at the ring edges
- $c$: at the cavitation (lubricant film rupture) point
- $r$: at the film reformation point
- $i$: rid index