Search for Eccentric Binary Neutron Star Mergers in the First and Second Observing Runs of Advanced LIGO

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Abstract

We present a search for gravitational waves from merging binary neutron stars (BNSs) which have non-negligible eccentricity as they enter the Laser Interferometer Gravitational Wave Observatory (LIGO) observing band. We use the public Advanced LIGO data which covers the period from 2015 through 2017 and contains ~164 days of LIGO–Hanford and LIGO–Livingston coincident observing time. The search was conducted using matched-filtering using the PyCBC toolkit. We find no significant BNS candidates beyond GW170817, which has previously been reported by searches for binaries in circular orbits. We place a 90% upper limit of ~1700 mergers Gpc–3 yr–1 for eccentricities \( \lesssim 0.43 \) at a dominant-mode gravitational-wave frequency of 10 Hz. The absence of a detection with these data is consistent with theoretical predictions of eccentric BNS merger rates. Using our measured rate we estimate the sensitive volume of future gravitational-wave detectors and compare this to theoretical rate predictions. We find that, in the absence of a prior detection, the rate limits set by six months of Cosmic Explorer observations would constrain all current plausible models of eccentric BNS formation.

Unified Astronomy Thesaurus concepts: Elliptical orbits (457); Gravitational waves (678); Compact objects (288); Neutron stars (1108)

1. Introduction

With the detections made by the Advanced LIGO (Laser Interferometer Gravitational Wave Observatory; Aasi et al. 2015) and Virgo observatories (Acernese et al. 2015), we have entered the age of gravitational-wave astronomy. During their first (O1) and second (O2) observing runs, the LIGO and Virgo collaborations detected ten binary black hole (BBH) mergers and one binary neutron star (BNS) merger (Abbott et al. 2019a). Independent groups have since verified these events and detected several additional BBH mergers (Nitz et al. 2019b, 2019c; Venemadhav et al. 2019a, 2019b). One possible channel for the formation of merging binaries is through dynamical interaction in dense stellar environments such as globular clusters (Sigurdsson & Hernquist 1993; Portegies Zwart & McMillan 2000; Grindlay et al. 2006) or galactic nuclei (O’Leary et al. 2009; Antonini & Perets 2012). Unlike binaries formed in the field which can radiate away their eccentricity (Peters 1964; Hinder et al. 2008), dynamically formed binaries may still have significant residual eccentricity when their gravitational waves enter the LIGO–Virgo band. The observation of a binary with measurable eccentricity would confirm the existence of a dynamical formation channel. The existing LIGO–Virgo BBH candidates are consistent with non-eccentric binary mergers (Romero-Shaw et al. 2019). The third LIGO–Virgo observing run is currently underway5 and is expected to produce dozens more events (Abbott et al. 2016a). A search for eccentric BBH mergers in O1 and O2 data, using methods that do not use models of the gravitational waveform (Klimenko et al. 2008, 2016; Tiwari et al. 2016), reported no eccentric merger candidates (Abbott et al. 2019b). The sensitivity of gravitational-wave searches can be improved by the use of matched-filtering, if a model of the target waveform is available. Existing matched-filter searches were designed for the detection of circular binaries (Usman et al. 2016; Dal Canton & Harry 2017; Venemadhav et al. 2019a). It is possible that compact binaries with measurable eccentricity may have been missed by these initial searches (Brown & Zimmerman 2010; Huerta & Brown 2013). For BBH mergers, highly accurate models with the full inspiral-merger-ringdown, along with support for both a large range of eccentricity and spin do not yet exist, though development is rapidly progressing and there are models that satisfy some of these constraints (Cao & Han 2017; Hinderer & Babak 2017; Hinder et al. 2018; Huerta et al. 2018; Ireland et al. 2019).

In this paper, we search for eccentric BNS mergers. There are several models of the gravitational waveform suitable for this task which include EccentricFD (Huerta et al. 2014) and TaylorF2e (Moore et al. 2018; Moore & Yunes 2019a). These waveform models do not currently support compact-object spin. However, neutron star binaries formed by dynamical capture in globular clusters may have non-negligible spin if they follow the observed distribution of millisecond pulsars (MSPs). Even if large spins are supported, we may expect the effective spin \( \chi_{\text{eff}} = (\chi_{\text{eff1}} m_1 + \chi_{\text{eff2}} m_2)/(m_1 + m_2) \) to peak around zero if the individual neutron star orientations are isotropic. Searches that do not account for spin still have significant sensitivity to sources with low effective spin \( \chi_{\text{eff}} < 0.1 \), though there will be significantly reduced sensitivity in the case where both component neutron stars are consistent

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5 https://gracedb.ligo.org/superevents/public/O3
Figure 1. EccentricFD gravitational waveforms generated at a dominant-mode reference frequency of 10 Hz with component masses of 1.3 $M_\odot$ for a non-eccentric, $e = 0.0$ (blue), and eccentric, $e = 0.4$ (orange) merging BNS up to the time of merger. Though the waveforms look similar they overlap by $\sim$16%. The inset plot shows a zoomed-in depiction of the phase difference in the non-eccentric (blue) and eccentric (orange) waveforms from $-9.0$ to $-8.7$ s.

with the fastest observed MSP (Hessels et al. 2006) and their respective spins are aligned with the orbital angular momentum (Brown et al. 2012).

Using these waveforms, we perform a matched-filtering based analysis by extending the methods used by Nitz et al. (2019) to include eccentric binaries. We find that our search is effective at detecting eccentric BNS mergers up to an eccentricity $e \sim 0.43$ at a dominant-mode gravitational-wave frequency of 10 Hz. Using a representative sample of the O1 and O2 data set, we find that a non-eccentric search starts losing significant sensitivity relative to the eccentric search starting at $e \sim 0.07$, in agreement with the results of Huerta & Brown (2013) and Moore & Yunes (2019).

We find no individually significant eccentric BNS merger candidates using the public O1 and O2 data sets (Vallisneri et al. 2015). The only significant event is the previously reported merger GW170817 (Abbott et al. 2017) since our search is also sensitive to circular binaries. In the absence of a new detection, we place a 90% upper limit on the merger rate of $\sim1700$ Gpc$^{-3}$ yr$^{-1}$ for binaries whose eccentricity is $e \lesssim 0.43$ at the 10 Hz reference frequency. While we do not detect any individually significant mergers, it is possible that follow-up could uncover sub-threshold sources, and so we make available our full population of sub-threshold candidates (Nitz et al. 2019).

We can compare our measured rate to predictions for the proposed channels for eccentric BNS formation. Lee et al. (2010) predict a BNS merger rate of 30 Gpc$^{-3}$ yr$^{-1}$ at $z = 0$ from binaries formed by the tidal capture and collision of neutron stars in globular clusters. Ye et al. (2020) predict a merger rate of $\sim 0.02$ Gpc$^{-3}$ yr$^{-1}$ from binaries formed by dynamical interactions in globular clusters. Given these predicted rates, it is unsurprising that our search did not observe a signal. Future detectors like A+ (Abbott et al. 2016a) and Cosmic Explorer (Reitze et al. 2019), will observe a large volume of the universe and have a higher probability of observing eccentric BNS mergers. Using our measured rate and the expected sensitivity of A+ and Cosmic Explorer, we estimate the time it would take for observed rates to impinge on the predicted rates. Using the A+ expected sensitivity distance of 330 Mpc (Abbott et al. 2016a), we find the most optimistic predictions (Lee et al. 2010) require half a year of data for the measurement to be comparable to the predictions. The most pessimistic predictions (Ye et al. 2020) require $\sim 775$ yr of data before the measured rate limits are comparable with the prediction. However, the proposed third-generation detector Cosmic Explorer would need at most half a year of data to achieve a rate limit comparable to the most pessimistic models, although a serendipitous detection is always a possibility with current detectors.

2. Search Methodology

We use a matched-filtering search for compact-object binaries using the PyCBC toolkit (Nitz et al. 2019d). We use gravitational waveforms that model mergers with elliptical orbits, but otherwise employ the same configuration as used by Nitz et al. (2019) for their search for gravitational waves from compact binary mergers.

Of the available waveform models, we employ two waveform models that contain eccentricity, EccentricFD, and TaylorF2e. EccentricFD (Huerta et al. 2014) extends the post-circular (PC) analysis of Yunes et al. (2009) to obtain a 3.5PN Fourier-domain enhanced PC gravitational-wave model that produces an eccentric, compact binary inspiral waveform in the small eccentricity approximation. In the zero eccentricity limit this model reproduces the non-eccentric model, TaylorF2, and in the small eccentricity limit this model will reproduce the PC model to leading order. Figure 1 shows two waveforms generated using EccentricFD with a non-eccentric waveform shown in blue and an eccentric waveform shown in orange. TaylorF2e is a 3PN Fourier-domain, eccentric waveform model, valid for larger initial eccentricities, defined by the stationary phase approximation of a harmonically decomposed time-domain signal. While both models expand the amplitude coefficients in small eccentricity, the TaylorF2e model does not invert the dependence of orbital frequency on eccentricity and
numerically solves the stationary phase condition (Moore et al. 2018; Moore & Yunes 2019a, 2019b).

We find that a template bank generated by straightforward stochastic placement of EccentricFD waveforms starting at a gravitational-wave frequency of 30 Hz is sufficient to recover BNS signals with eccentricity as modeled by either EccentricFD or TaylorF2e. In addition to the component masses of the BNS, our bank adds a parameter for the eccentricity, $e_{30}$, along with an additional binary orientation parameter. Our template bank is designed to detect BNS mergers where the component masses range from 1.1 to 1.6 $M_{\odot}$ (Özel & Freire 2016) and eccentricities up to 0.2 at a reference frequency of 30 Hz. This corresponds to $\sim 0.43$ at a reference frequency of 10 Hz. Figure 2 shows the distribution of templates in both chirp mass and eccentricity. The density of templates increases rapidly with eccentricity. Adding the additional degrees of freedom increases the size of the template bank by a factor of 160 relative to a non-eccentric, non-spinning bank that would cover the same region. Due to the inherent degeneracy between the component masses, the template bank will have significant sensitivity outside this parameter space in regions where the chirp mass $\mathcal{M} = (m_1 m_2)^{3/5}/(m_1 + m_2)^{1/5}$ is otherwise consistent i.e., a $1.2\text{–}2.0 M_{\odot}$ merger.

Matched-filtering is used to calculate the signal-to-noise ratio (S/N) time series using our bank of template waveforms independently for each observatory (Allen et al. 2012). Peaks in the S/N time series are followed up by a series of signal consistency tests (Allen 2005; Nitz 2018) and combined into multi-detector candidates (Usman et al. 2016; Nitz et al. 2017). We assign each candidate a ranking statistic, $\hat{\rho}_i$, using the same methods employed in the 1-OGC catalog (Nitz et al. 2019b). The ranking statistic, $\hat{\rho}_i$, accounts for the S/N of each candidate, the consistency of its morphology and signal properties with an astrophysical source, and the rate of background for candidates arising from similar templates.

3. Observational Results

We search the public LIGO O1 and O2 data set which contains $\sim 164$ days of coincident LIGO–Hanford and LIGO–Livingston data after removal of data that has been flagged as potentially containing instrumental artefacts (Vallisneri et al. 2015; Abbott et al. 2016b, 2018). Data when only a single observatory was operating was not considered, nor was data from the Virgo observatory which operated only in the last month of O2. In this search, we neglect data from the Virgo detector as it only provides a marginal sensitivity improvement (Nitz et al. 2019c). Future analyses will incorporate data from the full network.

The most significant candidates are listed in Table 1. As our search is also sensitive to circular binaries, it is not surprising that GW170817—first detected by the LIGO–Virgo search for circular binaries—was observed as a high-signal event. The remaining candidates are consistent with the rate of false alarms expected for the amount of data analyzed. However, we cannot rule out a sub-threshold population, which may be uncovered by correlation with non-GW data sets (GRBs, Kilonovae, etc.) such as performed in Nitz et al. (2019e).

4. Upper Limits

As our search did detect any significant individual eccentric BNS merger candidates, we place an upper limit on the rate of eccentric mergers as a function of their eccentricity. We determined a 90% confidence upper limit on the rate of mergers using the method introduced in Brady et al. (2004). The upper limit on the merger rate $R_{90}$ is

$$R_{90} = 2.303 [T V (\mathcal{F}^{*})]^{-1},$$

where $T$ is the total observation time, and $V(\mathcal{F}^{*})$ is the average volume the search is sensitive to at the false alarm rate of the loudest observed candidate. Under the assumption that GW170817 is a non-eccentric merger, we exclude it from our analysis. The sensitivity is measured using a simulated population of sources distributed uniformly in volume and isotropic in orientation. We have primarily used the EccentricFD model for our simulated population, however, we have confirmed our results are consistent with a smaller sample using the TaylorF2e model. Figure 3 shows the upper limit on the merger rate as a function of the binary eccentricity as well as the average sensitive distance of the search over the observation period. We find that up to an eccentricity of $\sim 0.43$ at a reference frequency of 10 Hz, we can place a 90% upper limit at $\sim 1700$ mergers per cubic Gpc per year.

Under the assumption that eccentric signals will not have been detected, we can determine the observation time required by future detectors to constrain the BNS merger rates predicted by Lee et al. (2010) and Ye et al. (2020) by scaling the upper limit from our search. We find that the Advanced LIGO observatories had an average range, $D_{O1+O2}$, of 90 Mpc during O1 and O2 for a fiducial 1.4–1.4 $M_{\odot}$ merger by taking the weighted-average of their noise curves. Similarly, using their respective noise curves, we find an average range, $D_{A+}$, of 330 Mpc for A+ (Abbott et al. 2016a) and $D_{CE}$ of 7130 Mpc for Cosmic Explorer. The observation time required, $T_{CE,A+}$, to match the predicted rates, $R_{Ye,ce}$, is given as

$$T_{CE,A+|Ye,lee} = T_{O1+O2} \frac{D_{O1+O2}}{D_{CE,A+}} \left( \frac{R_{O1+O2}}{R_{Ye,lee}} \right)^3,$$

where $T_{O1+O2}$ is the total observation time of O1 and O2, and $R_{O1+O2}$ is the upper limit achieved by our current search. We find that with the increased sensitivity of A+ the most

https://cosmicexplorer.org/researchers.html
To aid in further analysis of our results, we make available our full sub-threshold catalog of eccentric BNS candidates. For each candidate we provide the false alarm rate, parameters of the associated template waveform, and signal parameters such as the S/N and results of our signal consistency tests. This is available at doi:10.5281/zenodo.3585523 (Nitz et al. 2019a).

While the detection of a single BNS or BBH eccentric merger would immediately demonstrate the existence of dynamical formation, current estimates of the rate of BNS mergers imply that a single observation would be rare for the current generation of ground based observatories. Future observatories such as Cosmic Explorer will be able to probe current models.

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### Table 1

| Date Designation | GPS Time | FAR^{-1} (y) | $\bar{\eta}$ | $\rho_{1}$ | $\rho_{2}$ | $m_{1}$ | $m_{2}$ | $c_{50}$ |
|------------------|----------|--------------|---------------|-------------|-------------|---------|---------|---------|
| 170817+12:41:04UTC | 118700882.45 | >10000 | 27.86 | 18.41 | 23.60 | 1.48 | 1.28 | 0.02 |
| 151127+02:24:56UTC | 1132626313.67 | 0.57 | 8.60 | 7.28 | 5.73 | 1.23 | 1.55 | 0.16 |
| 151310+22:40:53UTC | 1132958470.76 | 0.54 | 8.60 | 6.76 | 5.89 | 1.29 | 1.22 | 0.19 |
| 170705+12:52:05UTC | 1183291388.00 | 0.31 | 8.54 | 7.29 | 5.56 | 1.48 | 1.57 | 0.16 |
| 151227+13:12:35UTC | 1135257172.28 | 0.14 | 8.42 | 6.33 | 6.21 | 1.42 | 1.37 | 0.10 |
| 170618+15:53:01UTC | 1181833519.00 | 0.08 | 8.40 | 7.30 | 5.35 | 1.22 | 1.19 | 0.15 |
| 170812+20:07:43UTC | 1186603681.67 | 0.07 | 8.35 | 6.92 | 5.47 | 1.21 | 1.13 | 0.17 |
| 170302+22:45:10UTC | 1172529928.62 | 0.07 | 8.42 | 6.93 | 5.46 | 1.23 | 1.17 | 0.12 |
| 161222+07:49:11UTC | 1166428168.98 | 0.06 | 8.39 | 6.33 | 6.14 | 1.50 | 1.12 | 0.18 |
| 170328+07:26:40UTC | 1174721218.74 | 0.05 | 8.38 | 5.11 | 7.26 | 1.11 | 1.22 | 0.12 |

**Note.** The mass and eccentricity parameters of the template associated with each candidate are listed. Note the eccentricity is given at the 30 Hz gravitational-wave frequency reference used to generate the template bank. The values associated with a candidate can be considered point estimates and may differ significantly from the results of full Bayesian parameter estimation. Masses are quoted in the detector frame.
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