finite blocklength communications in smart grids for dynamic spectrum access and locally licensed scenarios
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abstract—this work focuses on the performance analysis of short blocklength communication with application in smart grids. we use stochastic geometry to compute in closed form the success probability of a typical message transmission as a function of its size (i.e. blocklength), the number of information bits and the probability of a typical message transmission as a function of its size. two different scenarios are investigated: (i) dynamic spectrum access where the licensed and unlicensed users, share the uplink channel frequency band and (ii) local licensing approach using the so called micro operator, which holds an exclusive license of its own. approximated outage probability expression is derived for the dynamic spectrum access scenario, while a closed-form solution is attained for the micro-operator. the analysis also incorporates the use of retransmissions when messages are detected in error. our numerical results show how reliability and delay are related in either scenarios.

index terms—machine-to-machine, micro-operator, short message, dynamic spectrum access, local licensing, ultra-reliability, poisson point process

i. introduction

wireless networks have become an indispensable part of our daily life through a wide range of applications. for instance, we may now remotely monitor and control different processes within our homes, workplaces or even at industrial environments. in the upcoming years the advances in wireless communications shall be even more seamless and will provide connectivity through the so called internet of things (iot) [1]. it is envisioned that by the year 2020, billions of devices (including sensors and actuators) will be connected to the internet, gathering all kinds of data and generating a huge economic impact [2]. [3].

one of the key enablers of this future is the so-called machine-type communication (mtc) where a large number of devices will perform sensing, monitoring, actuation and control tasks with minimal or even no human intervention [1]. in other words, mtc – also known as machine-to-machine (m2m) communication – incorporates sensors, appliances and vehicles and this is expected to lead to a decrease of human-centric connections [4]. mtc is also one of the cornerstones of the upcoming 5g communication technologies. as discussed before, it contemplates a massive deployment of devices communicating with diverse range of requirements in terms of reliability, latency and data rates [5]–[8]. for example, [9], table. 2 lists the main requirements and features for different use cases of mtc over cellular networks.

intelligent transportation systems, industrial automation and smart grids have already been deployed using the iot concept, which is also one of the main driving technologies of 5g [10], [11]. it should be noted that the mentioned applications have different reliability requirements. for instance, some smart grid applications requires a reliability as low as 10^-6, which in their turn is less strict if compared to some industrial automation applications [10].

a. dynamic spectrum access and locally licensed in 5g

one of the main features of 5g will be its capability of connecting very large number of devices in different locations, while being able to serve case specific needs of different applications. indoor networks are responsible for the larger part of the mobile traffic, hence, it is essential to build new, more efficient indoor small cell networks. this will require more spectrum, which makes its availability a big challenge to tackle. there are generally two ways to access the available spectrum in a network which are [12]: (i) individual authorization (licensed), and (ii) general authorization (unlicensed). there are five different allocations scenarios associated with the previously mentioned access schemes, namely dedicated licensed spectrum, limited spectrum pool, mutual renting, vertical sharing and unlicensed horizontal sharing.

cognitive radio has gained a high popularity during the past few years since it makes a more efficient use of the frequency spectrum possible [13], [14]. dynamic spectrum access is one of the many interesting aspects of cognitive radios [15] where the unlicensed-users can use the same frequency band as the licensed-users while not affecting their transmission. for that sake, the unlicensed-users evaluate the spectrum usage and then transmit if the channel is free, otherwise, they postpone their transmission or use other frequency bands [16], [14]. dynamic spectrum access can also be implemented in smart grid communication networks. in [17], [18], the use of dynamic spectrum access in smart grid communication networks is evaluated and its suitability is positively assessed.

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Another interesting approach towards reaching spectral efficiency is using the non-orthogonal cognitive radio techniques. Despite being relatively new, many valuable research works have been done in this field. In [19], authors develop a cognitive radio scheme for multicarrier wireless sensor networks by studying a dense wireless sensor network model where the sensors can opportunistically use the primary users’ spectrum for their transmissions. Unlike the previous case, this model does not require the sensor nodes to sense the channel before transmission which is useful in terms of maintaining the limited resources of the sensors. Authors in [20] propose a number of new interference control and power allocation methods for cognitive radios which sheds light on the primary and secondary users’ power allocation requirements. An interesting work has been done in [21] where a new spectrum sharing model is proposed for multicarrier cognitive radio systems in which the secondary users can simultaneously use the primary users’ frequency band for their transmission while actually improving the primary users’ transmission by the mean of convolutive superposition.

Moreover, in [22] and [23], two different spectrum access protocols are proposed for the secondary networks via controlled amplify-and-forward relaying and cooperative decode-and-forward relaying. These protocols are proven to not have a negative impact on the rate and outage probability of the primary network. Another interesting work while using amplify-and-forward scheme has also been done in [24] where the proposed model makes it possible for secondary users to use the primary users’ frequency channel for their transmissions even when the primary network is active. By using this model, it is possible to improve the secondary user’s packet delay and primary users’ achievable rate. A useful model for improving the secondary network’s achievable rate is also introduced in [25] where the authors achieve this goal by applying superposition coding to a collaborative spectrum sharing scenario.

While all the aforementioned spectrum sharing and dynamic spectrum access models shall be a part of the future wireless communications, having exclusively licensed spectrum (locally licensed) is crucial for 5G to be able to meet some Quality of Service (QoS) requirements [12]. For instance, the micro-operator (µO) concept has been introduced as a mean for local service delivery in 5G which will benefit from having exclusively licensed spectrum. µOs make the previously mentioned case-specific services in the future indoor small cell networks possible [26]. [12]. Micro-operators have their own specific infrastructure which enables them to handle different kinds of Mobile Network Operator (MNO) users while also collaborating with the network infrastructure vendors, facility users/owners, utility service companies and regulators.

µOs shall help the MNOs specially in the areas that the traffic demand is high by offering them indoor capacity. It should be noted that the functionality of a µO depends on the available spectrum resources, which are limited. As mentioned earlier, having exclusive licensed spectrum is very important for the success of 5G so the µOs are the entities in a network that can benefit from it since regulators are able to issue local spectrum licenses for their own usage within a specific location [12], [26]. While we acknowledge all the valuable works mentioned earlier that have been done in the area of spectrum sharing which are also relevant for smart grid applications, it is important to mention that, in this study, our focus is to analyze the performance of the two dynamic spectrum access and locally licensed models. To do so, next we review the reliability requirements for smart grid applications and recent works in the MTC area.

B. Reliability in Smart Grids and the Role of MTC

Communication systems have been traditionally studied using the notion of channel capacity that assumes very large (infinite) blocklength [27]–[29], this is a reasonable benchmark for practical systems with blocklength in the order of thousands of bits. MTC, however, often uses short messages which is not currently supported by the wireless networks and periodic data traffic, coming from a massive number of devices. The same assumptions in terms of channel capacity cannot be directly applied to short blocklength messages as pointed out in [27], [30]. This imposes the need for a new paradigm on the network design and analysis architecture to support such amount of connected devices with their heterogeneous requirements [3].

New information theoretic results have been presented to evaluate the performance of short blocklength systems, from point-to-point additive white Gaussian noise (AWGN) links up to Multiple-Input Multiple-Output (MIMO) fading channels [30]. In [31], [32], the authors investigate retransmission methods and interference networks in this context. Nevertheless, network level analysis is still missing in the literature, except for [33], where the authors utilize Poisson Point Process (PPP) to characterize the network deployment and interference, considering finite block codes in a cellular network context.

Smart grids characterize the modernization process that the power grids undergo and is one important case for MTC [34], [35]. Communication systems are one the most important parts of the smart grids and different communication technologies are currently being used in smart grids most of which use the existing communication technologies such as PLC, fiber optical communications and LTE [36]. However, considering the rapid advancements of the communication systems towards 5G, smart grid communication systems should also be designed in a way that would be compatible with the newest telecommunication technology requirements which would not be really possible by using the traditional communication systems anymore. Therefore, smart grids are an interesting topic to be studied under the umbrella of 5G, especially considering that the requirements imposed by smart grids have hitherto overlooked specially with respect to massive connectivity and ultra reliable low latency communication [11]. Hence, motivated by smart grids stringent requirements [11], [37], here we focus on two different scenarios looking at the ultra-reliability using finite blocklength (short messages) in order to reduce latency and capture practical aspects regarding the message size, which is one of the novel aspects of 5G.

The reliability requirement of a smart grid network varies from one application to another [37]. For instance, applications such as remote meter reading have less strict reliability require-
C. Related Work

Ultra reliable communications and finite blocklength have become popular topics and many studies have been done in this field, however, there are still many issues that need to be addressed. For instance, [27], [40], [41], being amongst the first fundamental works in the finite blocklength area, where they set the foundation of the finite blocklength communications for cases such as block fading, MIMO and AWGN, also open up a variety of topics that need to be tackled. In [30], the necessity of studying and employing short packet communications is explained and is foreseen as one of the main enablers of the future telecommunication technologies. The authors bring into light the recent achievements in the field of short message transmission while also emphasizing the need for more research to be done on several open challenges. Valuable works have been done in [31], [32] where authors use the finite blocklength notion to analyze the throughput of different wireless networks. In [33], a model similar to ours is investigated where they also use PPP to characterize the cellular networks and evaluate the outage and throughput of the network in which a base station is connected to its nearest neighbor. However, this is not the case in our model. In the models studied in this paper, we use PPP where users are at a fixed distance, we use a different characterization of the signal-to-interference-plus-noise ratio (SINR) distribution and constraints which have led to totally different analysis and results. Our focus is not on a single link communication, hence, the SINR in this case captures interference, and to some extend, the network dynamics as well. We provide a general approximation for the outage probability which does not rely on any specific distribution of the SINR. Here, we focus on massive connectivity constrained by reliability which are imposed on the network from the application at hand (smart grids). We show that it is possible to achieve reliable and ultra reliable communication using finite blocklength which is also a characteristic of smart metering transmissions. It is shown how important it is to know how reliability and latency are affected by the increasing number of interferers. We also propose two different schemes in order to overcome this problem, namely dynamic spectrum access and local licensing scenarios, that can be used based on the restrictions imposed by the application.

D. Contributions

The followings are the main contributions of this paper.

- The general expression of the outage probability as a function of the number of information bits, blocklength and density of interferers in closed-form in the finite blocklength regime.
- Closed-form approximations of the outage probability are derived for both the dynamic spectrum access and locally licensed scenarios, under different conditions in the finite blocklength regime.
- Two different schemes are evaluated to be used in different smart grid applications based on network density and reliability requirements, considering the finite blocklength regime. We show that these schemes can not be used in every network model, since they have different requirements, while we also show when it is most suitable to use which.
- A general expression for the delay is proposed where the effect of retransmissions is investigated.

Table I summarizes the functions and symbols that are used in this paper. The rest of the paper is divided as follows. Section II introduces the network model with how the communication model using the short blocklength is modeled, while Section III details the outage analysis for both of the proposed scenarios. Section IV presents the numerical results and how the two scenarios can reach the reliability requirements of smart grids, and how retransmissions affect the reliability and latency. Section V concludes this paper.

**Notation:** The probability density function (PDF) and the cumulative distribution function (CDF) of a random vari-
able (RV) \( T \) are denoted as \( f_T(t) \) and \( F_T(t) \), respectively, while its expectation is \( E_T \). The gamma function is defined as \( \Gamma(t) \) \cite{ref:8} Ch 6, §6.1.1, and the regularized upper incomplete gamma function is denoted as \( \Gamma(s,t) \) \cite{ref:8} Ch 6, §6.5.3. \( Q(\cdot) \) denotes the Gaussian Q-function \( Q(t) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{t^2}{2}\right) \) \cite{ref:8} §26.2.3.

II. NETWORK MODEL

The conventional methods for evaluating communication networks are not usually a suitable choice when studying large wireless networks due to several reasons such as focusing on signal to noise ratio (SNR) rather than signal to interference plus noise ratio (SINR) or the fact that the interference in these kinds of networks depends on the path loss, meaning that it also depends on the network geometry. However, using stochastic geometry and Poisson point process to model large wireless networks have proven to be a useful tool in solving the challenges faced by the classical methods \cite{ref:7}. Hence, in wireless networks due to several reasons such as focusing on networks are not usually a suitable choice when studying large networks, we are dealing with a Poisson field of interferers \cite{ref:8}.

\textbf{Formally, we are dealing with a Poisson field of interferers} \cite{ref:8}.

The challenges faced by the classical methods \cite{ref:7}. Hence, in wireless networks have proven to be a useful tool in solving stochastic geometry and Poisson point process to model large wireless networks due to several reasons such as focusing on networks are not usually a suitable choice when studying large networks.

\[ X \lambda \]

\(|6, \S 6.5.3\).

The estimations of the position of the surrounding elements possible and is used as a fixed point of reference which makes the set of interferers’ locations and \( H \) represents the set of quasi-static channel fading coefficients in relation to the reference receiver located arbitrarily at the origin \cite{ref:2, ref:3}.

Notice that from Slivnyak theorem \cite{ref:3} an arbitrarily-located receiver is placed at the center of the Euclidean space and is used as a fixed point of reference which makes the estimation of the position of the surrounding elements possible \cite{ref:3}.

Note that \( x_i \in X \) denotes a position in the 2-dimensional plane and \( i \in \mathbb{N}^+ \). Besides, \( h_i \in H \) is assumed to be constant during the transmission of one block, which takes \( n \) channel uses, and during a spatial realization of the point process. We assume the fading coefficients follow a Rayleigh distribution, so that \( h_i^2 \) is exponentially distributed \( h_i^2 \sim \text{Exp}(1) \). The fading coefficient \( h_i \) is associated with the reference link, composed by a transmitter located at distance \( d \) from its associated receiver. It should be noted that since here we are using unbounded path loss model, \( \alpha > 2 \) \cite{ref:4} Ch. 5.

A. Communication Model

Signal propagation is modeled using large-scale distance-based path-loss and Rayleigh fading. The received power at the reference receiver from the interferer \( i \) is given by

\[ I_i = W_p h_i^2 |x_i|^{-\alpha}, \]

where \( W_p \) is the transmit power, \( \alpha > 2 \) is the path-loss exponent and \( |x_i| \) is the distance between the node \( x_i \) and the reference receiver. It is important to note that \( W_p \) is related to the interferers’ transmit power; the same equation is valid for the reference link 0, which may have a different transmit power denoted by \( W_s \). Then: \( I_0 = W_s h_0^2 d^{-\alpha} \).

The SINR \cite{ref:5} is defined as the random variable \( Z = \frac{W_p h^2}{\sum_{i \neq 0} W_i h_i^2 d^{-\alpha}} \), and \( I = \sum_{i \in \mathbb{N}^+} I_i \) and \( n > 0 \) is the AWGN power.

Under these conditions the SINR cumulative distribution function (CDF) \cite{ref:6} is given as \cite{ref:5} Corollary 1

\[ F_Z(z|\alpha,\lambda,\zeta,\xi) = 1 - \Pr[Z > z] = 1 -\exp(-(\zeta \lambda z^{2} - \xi) z). \]

while \( \zeta = \kappa \pi d^2 (W_p/W_s)^{\frac{\beta}{2}}, \quad \xi = \frac{w_2}{W_s}, \quad \text{and} \quad \kappa = \Gamma(1 + \frac{\beta}{2}) \Gamma(1 - \frac{\beta}{2}). \)

The probability density function (PDF) is then

\[ f_Z(z|\alpha,\lambda,\zeta,\xi) = \frac{2 \lambda \zeta z^{\frac{\beta}{2} - 1} + \xi}{\alpha} \exp(-(\zeta \lambda z^{2} - \xi) z). \]

B. Short Blocklength Messages

Following \cite{ref:10}, \cite{ref:11}, we define the encoding/decoding procedures as follows. First, the encoder maps \( k \) information bits \( B = \{B_1, ..., B_k\} \) into a codeword with \( n \) symbols \( S = \{S_1, ..., S_n\} \), satisfying the power constraint \( \frac{1}{n} \sum_{n=1}^{n} |S_m|^2 \leq W_s \). Then, \( S \) is transmitted through the wireless channel generating \( T = \{T_1, ..., T_n\} \) as the output. Finally, the decoder makes an estimate about the information bits based on \( T \), namely \( B \), satisfying a maximum error probability constraint \( \epsilon \). Then, we denote \( R^*(n, \epsilon) \) in bits per channel use (bpcu) as the maximal coding rate at finite blocklength (FB) which renders the largest rate \( \frac{k}{n} \) where \( k \) is the number of information bits and \( n \) denotes the blocklength, whose error probability does not exceed \( \epsilon \) \cite{ref:12}. Then, under quasi-static conditions \( R^*(n, \epsilon) \) can be tightly approximated by \cite{ref:11}

\[ R^*(n, \epsilon) \approx \sup \{R: \Pr[\log_2 (1 + Z) \leq R] < \epsilon\}. \]

For codes of \( R = \frac{1}{n} \) bpcu, the outage probability in quasi-static fading is approximated as \cite{ref:11}

\[ \epsilon = \mathbb{E}_{Z} \left[ Q\left(\sqrt{n} \log_2 (1 + Z) - R \right) / \sqrt{V(Z)} \right], \]

where \( V(Z) = (1 - (1 + Z)^{-2}) \left(\log_2 e\right)^2 \) is the channel dispersion and measures the stochastic variability of the channel relative to a deterministic one with the same capacity \cite{ref:13}.

The above outage function can also be expressed as \( \Pr[SINR < \gamma_{th}] \), where \( \gamma_{th} \) is the SINR threshold of the receiver which is determined by the channel capacity and is the minimum SINR which is needed in order to have a successful link connection, then the reliability can be defined as \( 1 - \Pr[SINR < \gamma_{th}] \). In other words, an outage event occurs when a transmitted message is not successfully decoded by the receiver.

III. OUTAGE ANALYSIS

In this section we focus on the outage probability of the network described in Section II. The analysis is done for two different scenarios, which are special cases of the general outage expression to be presented first. The outage probability in \cite{ref:5} is intricate to be evaluated in closed-form, especially when considering a general SINR distribution as in \cite{ref:4}.

Therefore, we resort to a tight approximation of \cite{ref:5}.

\[ \text{Notice that we denote} \ F_Z(z) = F_Z(z|x,\alpha,\lambda,\zeta,\xi) \quad \text{and} \quad f_Z(z) = f_Z(z|x,\alpha,\lambda,\zeta,\xi), \quad \text{except when the parameters are being manipulated, then we explicitly indicate them.} \]
an interference limited scenario where $\xi \approx 0$, the outage probability is

$$
\epsilon_{SS} = \frac{\beta(\vartheta - \varrho)}{\sqrt{2\pi}} + \frac{\alpha \beta}{\sqrt{2\pi}(\zeta \lambda \vartheta^2)} - \Gamma\left(\frac{\alpha}{2}, \zeta \lambda \vartheta^2\right) - \Gamma\left(\frac{\alpha}{2}, \zeta \lambda \vartheta^2\right).
$$

(7)

Proof. See Appendix B}

\[ \square \]

**Corollary 1.** For the special case of interference-limited dense urban scenarios, where $\alpha = 4$ is a good approximation for the path loss exponent, the outage probability in (7) reduces to

$$
\epsilon_{SS,\alpha=4} = \frac{\beta(\vartheta - \varrho)}{\sqrt{2\pi}} + \frac{2\beta}{\sqrt{2\pi}(\zeta \lambda \vartheta^2)}
$$

\[ \times \left[ e^{-\zeta \lambda \vartheta^2} \left( \frac{\zeta \lambda \vartheta^2}{\vartheta} + 1 \right) - e^{-\zeta \lambda \vartheta^2} \left( \frac{\zeta \lambda \vartheta^2}{\vartheta} + 1 \right) \right]. \tag{8} \]

The effect of different transmit powers $W_s$ on the outage probability as a function of the network density is shown in Fig. 2. We can see that, as the transmit power increases, the link can reach a higher reliability level in denser networks even with a high rate. It should be noted that this model is suitable for applications that do not require so strict reliability levels, such as smart meter reading.

As the noise level is negligible compared with the interference, the density of interfering nodes shall be high. The mobile users – the source of interference in this case – transmit with a higher power compared with the smart meters.

**B. Locally Licensed Scenario**

In this case, we analyze a locally licensed scenario, using the $\mu O$ concept, where the previous unlicensed link is now also a licensed user in the system in a specific geographical region. Although this concept guarantees the exclusive usage of the frequency band, the environment is still unfriendly: there are different entities that may cause interference such as base stations, smart meters and mobile users. Therefore, instead of assuming no interference, we consider a point process with low density $\lambda$, leading to low interference levels. However, unlike the previous case, the noise level is not negligible in this case anymore and it will affect the reliability of the system. The outage probability is given next.

**Proposition 3.** For the network model described in Section II and the characteristics of the $\mu O$ scenario described in Section II B, the outage probability is given in (9) on top of page 8 where $\alpha = 4$, hence, (2) is denoted by $F_{Z}(\vartheta|\xi)$.

Proof. See Appendix C

\[ \square \]

The $\mu O$ scenario cannot be assumed interference-limited; on the contrary, the noise power here is the major factor in the SINR. To compute the numerical results, we assume here $W_p = W_s = 1$ and $\xi = 0.001$. Recall that in the interference limited scenario, when the interference is low, we can achieve a low outage probability even with a high network density for a given coding rate. Increasing the smart meters transmit power results in having a higher success probability. As the

before evaluating it in closed-form for the scenarios under investigation in this work.

**Proposition 1.** Given the network described in Section II, the outage probability of the reference link (the link between the reference receiver and its respective transmitter [47]) is well approximated as

$$
\epsilon_{ap} = \frac{F_Z(\vartheta) + F_Z(\varrho)}{2} + \frac{\beta \theta (F_Z(\vartheta) - F_Z(\varrho))}{\sqrt{2\pi}} - \int_{\theta}^{\vartheta} \frac{\vartheta}{\sqrt{2\pi}} f_Z(z) dz,
$$

(6)

where $\beta = \sqrt{\frac{\rho^2}{2\beta} - 1}^{-1}$, $\theta = 2\vartheta - 1$, $\vartheta = \theta + \sqrt{\frac{\rho}{2\beta}}$ and $\vartheta = \theta - \sqrt{\frac{\rho}{2\beta}}$.

Proof. See Appendix A

\[ \square \]

Note that [6] covers a wide range of scenarios with path-loss exponent $\alpha > 2$. It is worth mentioning that only one integral remains in (6), and the overall expression is composed of well known functions, which facilitates its integration by numerical methods compared with the original expression in [5].

**A. Dynamic Spectrum Access Interference-Limited Scenario**

We consider a dynamic spectrum access model, shown in Fig. 1 where licensed and unlicensed users share the frequency bands allocated to the uplink channel [48]. We assume an interference-limited scenario where the licensed and unlicensed transmission powers are respectively $W_p$ and $W_s$. In this case, the noise power is negligible with respect to the aggregated interference [14]. The licensed users are mobile users communicating with a cellular base-station while the unlicensed users are the smart-meters that send data to their corresponding aggregator. The interference in this model is generated by mobile users with respect to the aggregator (reference receiver), as discussed in [14].

**Proposition 2.** Assuming the network deployment described in Section II and the reference scenario in section II A, in
interference power increases, a lower coding rate is needed to have the same outage probability with the same density.

In terms of outage, the $\mu O$ scenario, in its turn, behaves similarly, meaning that with increasing the network density, the outage probability increases, however, the outage probability is generally lower in this model as the interference level is negligible and noise is what is going to harm the performance of the network. The operating regions for the dynamic spectrum access and the $\mu O$ scenarios are shown in Figs. 4 and 5, respectively. The presented outage levels are chosen based on the fact that the dynamic spectrum access model is suitable for the non-critical applications, which we illustrate by reliabilities between 98% to 99%, which is relatively high for some applications (for smart grid application, refer to [37], Table.3), and will be further discussed in the next section.

On the other hand, when we assess the $\mu O$, one can see a very high reliability with error probability as low as 0.1% (i.e., reliability $\geq 99.9%$). In other words, $\mu O$ is suitable for critical applications with high reliability requirements. Thus, the operating region for this model is presented as the area where $\tau_{uo} \leq 10^{-3}$.

### C. On the Accuracy of (6) - (9)

As it was mentioned earlier in this section, we use an approximation of (5) for calculating the outage probability in (6) which is then used to derive the closed form equations of the outage probability for different scenarios presented in (7)-(9). In this section, the approximation is compared to the exact equation for both the interference and noise limited scenarios, as shown in Figs. 6 and 7 respectively. We can see that the results from the approximated and closed form equations are almost always equal to the exact equation (5). Considering the error metric below

![Fig. 2. Dynamic spectrum access scenario outage probability $\epsilon$ as a function of the network density $\lambda$ and coding rate $R$, where $d = 1$ and $\eta = 1$.](image)

![Fig. 3. An illustration of the locally licensed scenario, where the micro operator holds an exclusive license for its own usage in a specific geographical region (isolated area). There is interference caused by the entities outside of this area such as mobile phones and Wi-Fi. However, since the level of interference in this area is very low, noise is what is going to harm the operating of the network. The operating regions for the dynamic spectrum access model is $\eta = 1$ and $\Lambda = 1$.](image)

![Fig. 4. Dynamic spectrum access scenario outage probability $\epsilon$ with different transmit power as a function of the network density $\lambda$, considering $d = 1$, $\eta = 1$, and $R = 0.1$.](image)
we can see that $\Delta$ is almost always either zero or very close to zero. It is only for the case of the locally licensed scenario that we can see, for a very low values of $\lambda$, a difference of at most $4\%$ between (5) and the approximation which is still a very low difference. A more elaborated analysis of the error metric can be found in [49].

IV. MEETING THE SMART GRID REQUIREMENTS

This section focuses on the specific requirements for different smart grid applications. Specifically, we analyze the impact of blocklength, retransmission attempts, and network density on the outage probability of the two proposed scenarios.

1) Dynamic Spectrum Access Scenario: This scenario is suitable for applications like smart meters periodic transmissions [37]. The frequency of the transmissions might be relatively high over one day [48]; the smart meters transmit data every 15 minutes during a period of 24 hours which means smart meters need to transmit data 96 times per day.

The properties explained above can be seen in Fig. 8-a where the behavior of $\lambda(\epsilon_{avg})(\alpha = 4)$ is shown. With increasing $\lambda$, the outage probability also increases due to the higher interference level. Nevertheless, we can still achieve our desired outage probability, even in denser networks. We can confirm that as the unlicensed users transmit power increases, we can achieve better reliability in denser networks.

It was mentioned earlier that with finite blocklength, we cannot achieve the ultra-reliable (UR) region with the dynamic spectrum access model. Consequently, this approach shall be used in applications with looser requirements (98%-99%). In Fig. 8-a, we investigate the effect of the finite blocklength ($n$) on the outage probability for different information bit sizes ($k$). where we can see that, for $100 \leq n \leq 1000$, $\epsilon \leq 10^{-3}$ cannot be achieved. For reaching the UR region, the blocklength would have to be increased to very large numbers.

2) Locally Licensed Scenario: $\muO$ can achieve higher levels of reliability, meeting the requirements of more critical applications like fault detection. For more examples about the reliability and data size requirements for different smart grid applications, refer to [37 Table.3]. The $\muO$ approach is subjected to a lower interferers’ density when compared to the dynamic spectrum access, as shown in Fig. 8-b. When the noise level is low, the outage probability is also low. It is illustrated in this figure that for $\lambda \leq 10^{-2}$, this model can operate in the UR region where reliability level is at least 99.9%.

Fig. 8-b shows that ultra-reliability can be achieved with short blocklength in the $\muO$ scenario. By increasing $k$, the required blocklength for keeping the link in the UR region also increases; in any case, $\epsilon \leq 10^{-3}$ is still achievable for relatively high $k$ when $100 \leq n \leq 1000$.

A. Retransmission Attempts

Two basic strategies are normally employed to cope with transmission errors in communication systems, namely automatic repeat request (ARQ) and forward error correction (FEC) [50]. In this paper, we only consider ARQ.

ARQ consists of an acknowledgment (ACK) or negative acknowledgment (NACK) messages to be sent by the receiver to inform whether the intended message has been successfully decoded. If the transmission was not successful, a retransmission is requested and the retransmission continues until the codeword is decoded successfully or the allowed maximum number of retransmission is reached [51]. This strategy has some drawbacks such as loss of throughput, which are studied in [51], [52] (without considering the high reliability or low latency, though). Following [53], we study the effect of the number of transmission attempts for a given message on the outage probability $\epsilon$, including at most $m$ transmission attempts assuming Type-I HARQ is [54]:

$$\bar{\epsilon} = \epsilon(n, \lambda)^m,$$

where $\epsilon$ is the outage probability in (5).

The effect of increasing the number of transmission attempts on both scenarios is shown in Fig. 10. It can be seen that as $m$ increases, the reliability is enhanced. Comparing the outage probabilities of when only one or up to two transmission attempts are allowed, we can see that for the same $\lambda$, a much lower outage probability can be achieved.

Considering the outage curve for dynamic spectrum access and $\muO$, at some point at very low interferers’ densities, the two curves cross each other. This is due to the fact that the network density becomes very low from that point onward. Therefore, the interference power becomes lower and the dynamic spectrum access model starts to have a lower outage than the $\muO$ scenario. However, it is important to remember that the dynamic spectrum access model is designed to be used in denser networks; so the fact that its outage probability becomes less than the $\muO$ scenario for networks with very low densities shall be neglected since it contradicts the basic assumption of an interference-limited network.

While retransmissions increase the reliability of the network, it also increases the latency, which is in fact another important aspect of MTC. As 5G and MTC have strict
The average delay expression is then

$$\bar{\tau} = \frac{1}{m} \sum_{j=1}^{m} \epsilon(n, \lambda).$$

(13)

The number of channel uses and symbol time are the determining factors when dealing with delay. The symbol time ($T_s$) of LTE (long term evolution) is $T_s \approx 66.7\mu s$ and the current latency requirements of different smart grid applications are described in [37, Table.3]. However, 5G is going to benefit from ultra low latency compared to LTE. Hence, the smart grids are also going to have ultra low latency which is expected to be 3ms to 5ms [55]. Considering that the symbol time is going to be $T_s = \frac{1}{600} \approx 8.3\mu s$, for $n = 200$ and $m = 1$, $\delta = 1.66ms + \nu$. As the number of allowed transmission attempts increases, the delay also increases. If $m = 2$, then $\delta = 3.32ms + \nu$. We can see that increasing $m$ results in increasing the delay and this increase will not be linear since at each transmission there is also a feedback message sent every time. Thus, it is very important to limit the number of transmission attempts to avoid increasing the latency of the system.

V. DISCUSSION AND FINAL REMARKS

This paper evaluates the possibility of meeting the reliability requirements of different smart grid applications by using FB in two different system models, (i) dynamic spectrum access scenario suitable for applications with loose reliability requirements (98% - 99%), and (ii) μO scenario suitable for applications with strict reliability requirements (more than 99%).

Our results show that it is possible to meet the expected reliability levels and even reach the UR region for smart grids while having FB. It is shown that several factors such as network density, coding rate and interference and noise level affect the outage probability of the system, hence, they should be taken into consideration when choosing a suitable model considering the required reliability level of a specific application. Studying the ultra reliability and delay opens up a wide range of research opportunities in the smart grid communication systems.

APPENDIX A

PROOF OF PROPOSITION 11

As pointed out in [31], the function $Q(g(t))$ can be tightly approximated by a linear function for the whole S(1)NR range. Notice that the argument inside the $Q$-function in (5) is given as $g(t) = \sqrt{n} (1 - (1 + t)^{-2})^{-\frac{3}{2}} \log(1 + t)$, and that $g(t)$ is

$$\tau_{so} = \left[1 - F_Z(\vartheta|\xi]\right] - \frac{1}{2} - \beta\theta \sqrt{\frac{\lambda}{\vartheta^2}} + \left[1 - F_Z(\vartheta|\xi]\right] - \frac{1}{2} + \beta\theta \sqrt{\frac{\lambda}{\vartheta^2}} - \frac{[1 - F_Z(\vartheta|\xi]\left[1 - F_Z(\vartheta|\xi]\right] - \frac{1}{2}}{2\sqrt{2\pi} \theta^2}$$

$$\times \left[2\beta\sqrt{\xi}((F_Z^{-1}(\xi|\vartheta]\xi|\vartheta) = (F_Z^{-1}(\xi|\vartheta) + \exp(\xi(\vartheta + \vartheta) + \xi(\vartheta + \vartheta) + \xi(\vartheta + \vartheta)) + \frac{\xi\lambda^2}{4\xi}\sqrt{\pi}\beta\lambda$$

$$\times \left[\text{erf}\left(\frac{\xi\lambda}{2\sqrt{\xi}} + \sqrt{\vartheta^2}\right) - \text{erf}\left(\frac{\xi(\vartheta + \vartheta)}{2\sqrt{\xi}}\right)\right].$$

(9)

Fig. 6. Comparison of the accuracy of the approximation used in (6) and (7) compared to (5) for the Dynamic spectrum access scenario outage probability $\epsilon$ as a function of the density $\lambda$, considering $d = 1$, $\eta = 1$, $n = 500$, and $R = 0.1$.

Fig. 7. Comparison of the accuracy of the approximation used in (6) and (9) compared to (5) for the locally licensed scenario outage probability $\epsilon$ as a function of the density $\lambda$, considering $d = 1$, $n = 500$, and $R = 0.1$.

requirements in terms of latency, we should also consider this metric in our analysis by limiting the maximum number of transmission attempts. In this case, the total delay is calculated as

$$\bar{\tau} = n + \nu + \sum_{j=1}^{m} (n_j + \nu_j),$$

(12)

where $\nu$ denotes the number of channel uses for ACK/NACK messages that have been sent and $n$ is the number of channel uses. The average delay expression is then

$$\bar{\tau} = \frac{1}{m} \sum_{j=1}^{m} \epsilon(n, \lambda).$$

(13)
Fig. 8. Network density $\lambda$ as a function of the outage probability $\epsilon$ in (a) dynamic spectrum access scenario where $d = 1$, $\eta = 1$, $n = 200$, and $R = 0.1$ and (b) locally licensed scenario, considering $d = 1$, $n = 200$, $R = 0.1$ and $W_p = W_s$.

Fig. 9. Blocklength $n$ as a function of the outage probability $\epsilon$ in (a) dynamic spectrum access scenario, considering $d = 1$, $\eta = 1$, $n = 200$, $R = 0.1$, $\lambda = 10^{-2}$ and $W_p = W_s = 1.4$ and (b) locally licensed scenario, considering $d = 1$, $n = 200$, $R = 0.1$, $\xi = 0.001$ Watts, $\lambda = 10^{-4}$ and $W_p = W_s = 1$.

Fig. 10. Effect of increasing the number of retransmissions on (a) dynamic spectrum access scenario and (b) locally licensed scenario outage probability $\epsilon$ as a function of the network density $\lambda$, considering $d = 1$, $W_p = W_s = 1.4$ and $\xi = 0.001$. 
an increasing function of $t$, but not strictly positive $\forall t \in \mathbb{R}$, which restricts the use of other well known approximations for the Q-function [57]. Then, let $Q(g(t)) \approx W(t)$ be denoted as

$$W(t) = \begin{cases} 
1 & t \leq \varrho \\
\frac{1}{2} - \frac{\beta}{\sqrt{2\pi}} (t - \varrho) & \varrho < t < \varrho \\
0 & t \geq \varrho 
\end{cases}$$

(14)

where $\theta = 2^{R} - 1$ is the solution of $g(t) = 0$, while $\beta = \frac{\sqrt{2\pi}(2^{R} - 1)^{\frac{1}{2}}}{\varrho}$ is the solution for $\frac{\varrho Q(g(t))}{e^{\varrho t}}|_{t=\varrho} = 0$. Then, the outage probability becomes,

$$\epsilon = \mathbb{E}_Z[\epsilon] = \int_{0}^{\infty} W(z)f_Z(z)dz$$

$$= \int_{0}^{\varrho} (f_Z(\varrho))dz + \int_{\varrho}^{\infty} \left(\frac{1}{2} - \frac{\beta}{\sqrt{2\pi}} (z - \varrho)\right)f_Z(z)dz$$

$$= F_Z(\varrho)\left[\left(\frac{1}{2} - \frac{\beta}{\sqrt{2\pi}} (\varrho - \varrho)\right)\right]f_Z(\varrho)dz$$

$$= F_Z(\varrho) + \frac{1}{2} F'_Z(\varrho)\left[\frac{\varrho}{\beta} F_Z(\varrho) - \int_{\varrho}^{\infty} \frac{\beta z}{\sqrt{2\pi}} f_Z(z)dz\right],$$

(15)

which after few algebraic manipulations is written as in [6].

**APPENDIX B**

**PROOF OF PROPOSITION 3**

By setting $\xi = 0$ and replacing it into (2) and (3), while considering $F_Z(\varrho) = F_Z(\varrho|\alpha = 4, \xi = 0)$ and $f_Z(z|\alpha = 4, \xi = 0)$, the integral in [6] assumes the form of the upper incomplete gamma function [42], §6.5.3.

$$I = \frac{\beta}{\sqrt{2\pi}} \int_{0}^{\varrho} z f_Z(z)dz$$

$$= \frac{\beta}{\sqrt{2\pi}} \int_{0}^{\varrho} \frac{2\lambda \zeta}{\alpha} z^{\frac{\alpha}{2} - 1} \exp\left(-\lambda z \frac{\zeta}{\alpha}\right)dz$$

$$= \frac{2\lambda \zeta}{\sqrt{2\pi} \alpha} \int_{0}^{\varrho} z^{\frac{\alpha}{2} - 1} \exp\left(-\lambda z \frac{\zeta}{\alpha}\right)dz$$

$$= \frac{2\lambda \zeta}{\sqrt{2\pi} \alpha} \int_{0}^{\varrho} z^{\frac{\alpha}{2}} \exp\left(-\frac{\lambda z \zeta}{\alpha}\right)dz,$$

(16)

where the integral can be solved using integration by parts [58], §2.02-5]. Hence, we attain (7) by replacing (15) into (6) after few algebraic manipulations and using [58] §2.321-1 and [58] §2.33-10).

**APPENDIX C**

**PROOF OF PROPOSITION 3**

Considering $F_Z(z) = F_Z(z|\alpha = 4, \xi)$ and $f_Z(z) = f_Z(z|\alpha = 4, \xi)$, the integral in [6] has a closed-form solution when $\alpha = 4$ as follows

$$I = \frac{\beta}{\sqrt{2\pi}} \int_{0}^{\varrho} z f_Z(z)dz$$

$$= \left[1 - F_Z(\varrho)\right]\left[1 - F_Z(\varrho)\right]$$

$$\times \left[\frac{2\beta}{\sqrt{2\pi}} \left(1 - F_Z(\varrho)\right)^{-1} (1 + \xi \varrho) - \left((1 - F_Z(\varrho))^{-1} (1 + \xi \varrho)\right)\right]$$

$$\times \left[\exp\left(\lambda\sqrt{\varrho} + \sqrt{\varrho}^2 + \xi (\varrho + \varrho) + \frac{\varrho^2 \xi^2}{4\xi}\right)\sqrt{\frac{\pi}{2\xi}} \beta \zeta\right]$$

$$\left[\text{erf}\left(\frac{\lambda \sqrt{\varrho}}{2\sqrt{\xi}} + \sqrt{\varrho}^2\right) - \text{erf}\left(\frac{\lambda \sqrt{\varrho}}{2\sqrt{\xi}} + \sqrt{\varrho}^2\right)\right].$$

(17)

where the integral can be solved though integration by parts and with the help of [58], §2.33-10) and [58], §2.33-16). Then, substituting $\alpha = 4$ and (17) into (6), yields (9).

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