Dark Matter in the Alternative Left Right Model

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Abstract: The Alternative Left-Right Model is an attractive variation of the usual Left-Right Symmetric Model because it avoids flavour-changing neutral currents, thus allowing the additional Higgs bosons in the model to be light. We show here that the model predicts several dark matter candidates naturally, through introduction of an $R$-parity similar to the one in supersymmetry, under which some of the new particles are odd, while all the SM particles are even. Dark matter candidates can be fermionic or bosonic. We present a comprehensive investigation of all possibilities. We analyze and restrict the parameter space where relic density, direct and indirect detection bounds are satisfied, and investigate the possibility of observing fermionic and bosonic dark matter signals at the LHC. Both the bosonic and fermionic candidates provide promising signals, the first in LHC at 300 fb\textsuperscript{-1}, the second at higher luminosity, 3000 fb\textsuperscript{-1}. Signals from bosonic candidates are indicative of the presence of exotic $d'$ quarks, while fermionic candidates imply the existence of charged Higgs bosons, all with masses in the TeV region.

Keywords: ALRM, scotino and scalar dark matter, collider signatures.
1 Introduction

While the discovery, 10 years ago, of the Higgs boson has provided the Standard Model (SM) with the needed missing piece, questions remain as to how complete a description of nature it offers. Thus far, its agreement with experiment is remarkable, but still outstanding questions remain, both from the theoretical foundation and the missing experimental pieces. It is hoped that looking for explanations will lead to a more complete scenario, which is the goal of Beyond The Standard Model (BSM) explorations.

Although there are many phenomena unexplained in the SM, perhaps none is more mysterious than dark matter. Found to comprise about 27% of the universe, dark matter interacts gravitationally, and perhaps weakly, with the SM particles. The primary (particle physics) candidate is a weakly interacting massive particle (WIMP), which has not been observed, but whose indirect indications come from gravitational lensing [1], the cosmic microwave radiation background [2, 3], and other astrophysical observations. There are few models which include a natural candidate for WIMP, most notable among them is the supersymmetric extension of the SM. In supersymmetry, $R$-parity is a symmetry that distinguishes between ordinary versus supersymmetric particles. In that case, $R$-parity is a $Z_2$ symmetry defined as

$$ R = (-1)^{3B + L + 2s} $$

with $B$ the baryon number, $L$ the lepton number and $s$ the spin. Forbidding $R$-parity violation yields a stable lightest supersymmetric particle (LSP), which is a natural dark matter candidate. Other BSM scenarios deal with the existence of dark matter by introducing an ad-hoc particle, chosen as scalar, fermion, or vector. By requiring the interactions of such particle with the SM matter to obey constraints from relic abundance of dark matter [4], direct [5, 6] and indirect [7–9] detection experiments, as well as collider searches, one can
determine its properties (usually mass and couplings) and restrict the parameter space of the models.

In this work we shall analyze a non-supersymmetric model where one can define a symmetry analogous to the $R$-parity in supersymmetry, yielding a natural dark matter particle. This is the Alternative Left-Right Model (ALRM). Based on the gauge group $SU(3)_C \otimes SU(2)_L \otimes SU(2)_R' \otimes U(1)_{B-L}$, the model emerges from the breaking of the exceptional group, $E_6$ [10–12], and it differs from the usual Left-Right Symmetric Model (LRSM) [13–16] in its assignment of right-handed fermion doublets. The ALRM avoids the unwanted tree-level flavour-changing interactions which conflict with the observed properties of the $K$ and $B$-meson systems, which are forcing the right-handed sector of the LRSM into a high TeV range. This is avoided by the ALRM, while at the same time maintaining some of the attractive properties of the LRSM, such as providing an understanding of parity violation and a mechanism to give neutrino masses.

The dark matter in the left-right symmetric model was analyzed most recently in [17]. The ALRM model has been studied before [18–21], including tests of a fermionic candidate for dark matter. However, while the notion of an extended $R$-parity was known, it was not properly explored in the context of an analysis of the dark matter sector. We remedy this here. We show that the particles in the model can divided naturally into $R$-parity odd and $R$-parity even sectors, which do not mix with each other. The lightest $R$-parity odd particle can be a scalar, a fermion or both. We analyze here all possibilities. We impose the constraints from relic density, direct and indirect detection experiments (to restrict the parameter space), before assessing the signatures at colliders for the different options.

Our work is organized as follows. In Sec. 2 we present a brief discussion of the model, with emphasis on the particle structure, symmetry breaking and fermion masses. We then proceed to analyze the possibilities for dark matter candidates and their properties in Sec. 3. We look at the consequences of scalar dark matter candidates in Sec. 3.1, fermionic dark matter in Sec. 3.2, and degenerate fermion-scalar dark matter in Sec. 3.3. We investigate the possibilities of observing and of discriminating among the scenarios at the LHC in Sec. 4. Finally we summarize our findings and conclude in Sec. 5.

2 The Model

The particle content of the ALRM, together with their quantum number assignments under the gauge group $SU(3)_C \otimes SU(2)_L \otimes SU(2)_R' \otimes U(1)_{B-L}$ is listed in Table 1 [20].

As they emerge from different choices of breaking $E_6$, the quark and lepton assignments in multiplets differ from those in the LRSM. Here the left-handed (LH) fermions form $SU(2)_L$ doublets, while the right-handed (RH) up-type quarks form doublets with exotic down-type quarks $d'_R$. Similarly, while the LH leptonic doublets are the same as in the SM, the RH charged leptons partner with exotic RH neutral fermions ($n_R$) to form $SU(2)_R'$ doublets. In addition, there are the left-handed partners of exotic quarks ($d'_L$), right-handed partners of the usual quarks ($d_R$), and two neutral fermions, $n_L$ and $\nu_R$, which are singlets under both $SU(2)_L$ and $SU(2)_R'$ [20, 22, 23]. The electroweak symmetry breaking occurs as follows. First, the gauge and global symmetry $SU(2)_R' \times U(1)_{B-L} \times U(1)_S$ is
Table 1. Particle content of ALRM together with their quantum numbers under SU(3)_C ⊗ SU(2)_L ⊗ SU(2)_R′ ⊗ U(1)_B−L ⊗ U(1)_S considered in this study. While several U(1)_S assignments exist in the literature, we follow [20], and define the generalized lepton number as \( L = S + T_{3R′} \).

\[
\begin{array}{|c|c|c|c|c|c|}
\hline
\text{Particles} & \text{SU(3)}_C & \text{SU(2)}_L & \text{SU(2)}_R' & \text{U(1)}_{B-L} & \text{U(1)}_S \\
\hline
\text{Quarks} & & & & & \\
Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} & 3 & 2 & 1 & \frac{1}{6} & 0 \\
Q_R = \begin{pmatrix} u_R \\ d_R' \end{pmatrix} & 3 & 1 & 2 & \frac{1}{6} & -\frac{1}{2} \\
d'_L & 3 & 1 & 1 & -\frac{1}{3} & -1 \\
d_R & 3 & 1 & 1 & -\frac{1}{3} & 0 \\
\hline
\text{Leptons} & & & & & \\
L_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} & 1 & 2 & 1 & -\frac{1}{2} & 1 \\
L_R = \begin{pmatrix} n_R \\ e_R \end{pmatrix} & 1 & 1 & 2 & -\frac{1}{2} & +\frac{3}{2} \\
n_L & 1 & 1 & 1 & 0 & 2 \\
\nu_R & 1 & 1 & 1 & 0 & 1 \\
\hline
\text{Scalars} & & & & & \\
\Phi = \begin{pmatrix} \phi_1^1 \\ \phi_2^1 \\ \phi_2^0 \\ \phi_2^0 \end{pmatrix} & 1 & 2 & 2^* & 0 & -\frac{1}{2} \\
\chi_L = \begin{pmatrix} \chi_L^+ \\ \chi_L^0 \end{pmatrix} & 1 & 2 & 1 & \frac{1}{2} & 0 \\
\chi_R = \begin{pmatrix} \chi_R^+ \\ \chi_R^0 \end{pmatrix} & 1 & 1 & 2 & \frac{1}{2} & \frac{1}{2} \\
\hline
\text{Gauge Bosons} & & & & & \\
B^\mu & 1 & 1 & 1 & 0 & 0 \\
W_L^\mu & 1 & 3 & 1 & 0 & 0 \\
W_R^\mu & 1 & 1 & 3 & 0 & 0 \\
\hline
\end{array}
\]

broken to the hypercharge \( U(1)_Y \) while preserving the generalized lepton number defined as \( L = S + T_{3R′} \). This is achieved through the vacuum expectation value (VEV) of the \( SU(2)_R′ \) doublet scalar \( \chi_R \), which is charged under \( U(1)_S \). The electroweak symmetry is then broken down to electromagnetism by means of the VEV of the bidoublet Higgs field \( \Phi \), charged under both \( SU(2)_L \) and \( SU(2)_R′ \), but with no \( U(1)_{B-L} \) quantum numbers, as well as by the VEV of \( \chi_L \) [20, 24–27].

The model Lagrangian includes standard gauge-invariant kinetic terms for all fields, a Yukawa interaction Lagrangian \( \mathcal{L}_Y \), and the scalar potential \( V_{\Phi\chi} \). The most general Yukawa Lagrangian respecting gauge and global \( U(1)_S \) symmetries is

\[
\mathcal{L}_Y = \bar{Q}_L \hat{Y}^u \hat{\Phi} Q_R - \bar{Q}_L \hat{Y}^d \phi_R - \bar{Q}_L \hat{Y}^d \phi_R - \bar{L}_L \hat{Y}^e \Phi L_R + \bar{L}_L \hat{Y}^e \chi_R + \bar{\nu}_R \hat{\chi}_R \nu_L + h.c.,
\]
with flavour indices omitted for clarity, where the Yukawa couplings $\hat{Y}$ are $3 \times 3$ matrices in the flavour space. The hatted quantities refer to the duals of the scalar fields $\hat{\Phi} = \sigma_2 \sigma_2$ and $\hat{\chi}_{L,R} = i \sigma_2 \chi_{L,R}$. Unlike conventional LRSM, in this framework right-handed neutrinos are gauge singlets which allows us to introduce a bare Majorana mass term,

$$\mathcal{L}_M = m_M \bar{\nu}_R^c \nu_R.$$

The most general Higgs potential $V_{\Phi_X}$ preserving left-right symmetry is [28]

$$V_{\Phi_X} = -\mu_1^2 \text{Tr} (\Phi^\dagger \Phi) - \mu_2^2 (\chi^\dagger_L \chi_L + \chi^\dagger_R \chi_R) + \lambda_1 (\text{Tr} (\Phi^\dagger \Phi))^2 + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(\Phi^\dagger \Phi)$$

$$+ \lambda_3 \left( (\chi^\dagger_L \chi_L)^2 + (\chi^\dagger_R \chi_R)^2 \right) + 2 \lambda_4 (\chi^\dagger_L \chi_L) (\chi^\dagger_R \chi_R) + 2 \alpha_1 \text{Tr}[\Phi^\dagger \Phi] [\chi^\dagger_L \chi_L + \chi^\dagger_R \chi_R]$$

$$+ 2 \alpha_2 \left[ (\chi^\dagger_L \Phi^\dagger \Phi) (\chi^\dagger_R \chi_R) + (\chi^\dagger_R \Phi^\dagger \Phi) (\chi^\dagger_L \chi_L) \right] + 2 \alpha_3 \left[ (\chi^\dagger_L \Phi^\dagger) (\Phi^\dagger \chi_R) + (\chi^\dagger_R \Phi^\dagger) (\Phi^\dagger \chi_L) \right]$$

$$+ \mu_3 [\chi^\dagger_L \Phi \chi_R + \chi^\dagger_R \Phi^\dagger \chi_L],$$

(2.3)

The properties of this potential and implications for the vacuum stability of the model have been analyzed in [21]. After the breaking of the left-right symmetry down to $U(1)_{em}$, the neutral components of the scalar fields acquire non-vanishing VEVs,

$$\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ v_2 \end{pmatrix}, \quad \langle \chi_L \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_L \end{pmatrix}, \quad \langle \chi_R \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_R \end{pmatrix},$$

(2.4)

with the exception of $\phi^0_1$, which is protected by the conservation of the generalized lepton number, which also forbids mixing between the SM $d$ and exotic $d'$ quarks.

Left-right symmetry breaking generates masses for the model gauge bosons, and Higgs-boson kinetic terms are responsible for their mixing. Because $\langle \phi^0_1 \rangle = 0$, the charged $W = W_L$ and $W' = W_R$ bosons do not mix, and their masses are given by

$$M_{W_L} = \frac{1}{2} g_L \sqrt{v_L^2 + v^2_2} \equiv \frac{1}{2} g_L v \quad \text{and} \quad M_{W_R} = \frac{1}{2} g_R \sqrt{v^2_2 + v^2_R} \equiv \frac{1}{2} g_R v',$$

(2.5)

with $g_L$ and $g_R$ the coupling constants for $SU(2)_L$ and $SU(2)_R$. This releases the $W_R$ boson from contributing to low energy physics, in particular to flavor violation in $K^0 - \bar{K}^0$ and $B^0 - \bar{B}^0$ (as $W_R$ always couples to $ud'$) and lifts all constrains on its mass. However, the $W_R$ is related to $Z_R$ mass. In the neutral sector, the gauge boson squared mass matrix is written, in the $(B_\mu, W_{3L}^\dagger, W_{3R}^\dagger)$ basis, as

$$(M_V^0)^2 = \frac{1}{4} \begin{pmatrix} g_{B-L}^2 (v_L^2 + v_R^2) & -g_{B-L} g_L v_L v_R^2 & -g_{B-L} g_R v_R^2 \\ -g_{B-L} g_L v_R v_L^2 & g_L^2 v_2^2 & -g_L g_R v_2^2 \\ -g_{B-L} g_R v_L v_R^2 & -g_R g_L v_R v_2^2 & g_R^2 v_2^2 \end{pmatrix},$$

(2.6)

with $g_{B-L}$ the coupling constant for $U(1)_{B-L}$. The matrix can be diagonalised through three rotations that mix the $B$, $W_{3L}$ and $W_{3R}$ bosons into the massless photon $A$ and massive $Z$ and $Z'$ states. Neglecting the $Z/Z'$ mixing, the $Z$ and $Z'$ boson masses are given by

$$M_Z = \frac{g_L}{2 \cos \theta_W} v \quad \text{and} \quad M_{Z'} = \frac{1}{2} \sqrt{g_{B-L}^2 v_L^2 (v_L^2 + v_R^2) + g_L^2 (v_2^2 + v_R^2) + 2g_{B-L} g_R v_R^2 v_R^2},$$

(2.7)
where $\theta_W$-rotation denotes the usual electroweak mixing with the definition $\sin\theta_W = \frac{g_Y}{\sqrt{g^2_B + g^2_Y}}$, where $e$ and $g_Y$ denote electromagnetic coupling constant and hypercharge respectively [20]. The relationship between $M_{WR}$ and $M_{Z'}$ is not as transparent as in LRSM. However, unlike $W_R$, $Z'$ couples to ordinary quarks and leptons, and its mass is restricted by measurements at ATLAS [29], requiring $v_R$ to be large. In the limits $v_R \gg v_2, v_L$

$$\frac{M_{Z'}}{M_{WR}} \sim \sqrt{\frac{g^2_B - L + g^2_Y}{g_R}},$$

(2.8)

forcing $W_R$ to be heavy$^1$.

Fermion masses are generated from the Yukawa Lagrangian (2.1), after the breaking of the $SU(2)_L \times SU(2)_R' \times U(1)_{B-L}$ symmetry down to $U(1)_{em}$. The resulting fermion masses are

$$m_u = \frac{1}{\sqrt{2}} Y_u v_2 \sin \beta, \quad m_d = \frac{1}{\sqrt{2}} Y_d v_2 \cos \beta, \quad m_d' = \frac{1}{\sqrt{2}} Y_{d'} v_R, \quad m_e = \frac{1}{\sqrt{2}} Y_e v_2 \sin \beta,$$

(2.9)

with $\tan \beta = v_2/v_L$. Allowing for soft-breaking of the lepton number, $L$, $\nu_R$ can acquire a Majorana mass as given in Eq. 2.2, and the consequent lepton asymmetry could lead to leptogenesis [30]. The Dirac mass for the left-handed, Majorana mass for the right-handed neutrinos and Dirac mass for scotinos are, respectively

$$M_\nu = \frac{1}{\sqrt{2}} Y^\nu_L v_L, \quad M_N = m_M, \quad M_n = \frac{1}{\sqrt{2}} Y^n_R v_R,$$

(2.10)

We assume neutrinos to be Majorana particles. Defining

$$\nu = \frac{\nu_L + \nu^c_R}{\sqrt{2}}, \quad N = \frac{\nu_R + \nu^c_L}{\sqrt{2}},$$

(2.11)

light left-handed neutrino masses are generated through the see-saw mechanism

$$\left(\begin{array}{c} \bar{\nu}_L \\ \nu^c_R \end{array} \right) \left(\begin{array}{cc} 0 & M_\nu \\ M^T_{\nu} & M_N \end{array} \right) \left(\begin{array}{c} \nu^c_L \\ \nu_R \end{array} \right).$$

(2.12)

Here $\nu$ and $N$ are approximate eigenstates with masses

$$m_N \simeq M_N \quad \text{and} \quad m_\nu = M_\nu M_N^{-1} M^T_\nu,$$

(2.13)

with $M_N$ assumed to be diagonal, and $m_\nu$ is diagonalized in flavor eigenstates as

$$m^\text{diag}_\nu = V_L^{-1} m_{\nu} V_L.$$

(2.14)

Other details of the model, including a complete description of the gauge sector, can be found in Refs. [22, 23, 27, 28, 30].

$^1$In fact the ratio $\frac{M_{Z'}}{M_{WR}}$ is lower in ALRM than in the LRSM, meaning that the spectrum is more compressed in the latter [20].
3 Dark Matter

The ALRM augmented by the extra $U(1)_S$ symmetry allows the introduction of the generalised lepton number $L = S + T_{3R}$. Similarly, one can introduce a generalized R-parity, similar to the one existing in supersymmetry, defined here in a similar way as $(-1)^{3B + L + 2s}$ [24]. Under this R-parity, all SM quarks, leptons and SM gauge bosons are even. The odd R-parity particles are as follows: in the scalar sector, $\chi^\pm_{LR, R}, \phi_i^\pm$, $\Re(\phi_i^0)$ and $\Im(\phi_i^0)$, in the fermion sector, the scotinos $n_L, n_R$, and the exotic quarks $d'_L, d'_R$, and in the gauge sector, $W_R$. All the rest of the particles in the spectrum are R-parity even. The existence of a dark matter sector arising from R-parity odd particles is another attractive feature of this model, and an advantage over the more common LRSM. Of the R-parity odd particles, only the neutral Higgs, the pseudoscalar Higgs or the scotino can be DM candidates, as the rest of the particles are electromagnetically charged, and in addition, $d'$ quarks have strong interactions. Thus, in what follows we shall investigate the possibility that the DM is either the R-parity odd Higgs boson (scalar or pseudoscalar), or the scotino(s), or both.\footnote{The possibility that the scotino is a dark matter candidate, without the association to R-parity, was examined in [19, 20, 24–27].}

We proceed to analyze these in turn, looking for ways to observe and distinguish them.

3.1 Scalar Dark Matter

The scalar sector of the model consists of one bidoublet $\Phi$ Higgs field, with the $SU(2)_L$ symmetry acting along the columns and the $SU(2)_R$ along the rows, as in Table 1. In addition to the bidoublet Higgs boson $\Phi$ there are two doublet Higgs fields transforming under $SU(2)_L$ and $SU(2)_R$, denoted by $\chi_L$ and $\chi_R$, respectively. $SU(2)_R \otimes U(1)_{B-L}$ to $U(1)_Y$ breaking is induced by the VEV of $\chi_R$, while the electroweak symmetry breaking is driven by the VEVs of $\Phi$ and $\chi_L$. The global $U(1)_S$ symmetry insures that the quark doublets can interact with $\Phi$ and lepton doublets with $\Phi$ only. This symmetry also restricts $\phi_i^0$ from acquiring a VEV, forbidding the $W_L - W_R$ gauge boson mixing, as well as the $d - d'$ and $n - \nu$ mixing in the model. The conservation of R-parity as defined above is reflected in the Higgs boson mixing matrices, which are consistent with the absence of the mixing between the R-parity even and R-parity odd scalars. In the charged scalar sector, the squared mass matrix is block diagonal. The $\phi_1^\pm$ and $\chi_1^\pm$ (R-parity even) fields mix independently of the $\phi_2^\pm$ and $\chi_2^\pm$ (R-parity odd) fields. The $2 \times 2$ block mass matrices $(M^+_L)^2$ and $(M^+_R)^2$ are, in the $(\phi_1^\pm, \chi_1^\pm)$ and $(\phi_2^\pm, \chi_2^\pm)$ bases, respectively, as

$$
(M^+_L)^2 = \begin{pmatrix}
-\left(\alpha_2 - \alpha_3\right)v^2 v_{L,R} - \frac{\mu_3 v_{L,R}}{\sqrt{2} v_2} & \left(\alpha_2 - \alpha_3\right)v_2 v_{L,R} + \frac{\mu_3 v_{L,R}}{\sqrt{2} v_2} \\
\left(\alpha_2 - \alpha_3\right)v_2 + \frac{\mu_3 v_{L,R}}{\sqrt{2} v_2} & -\left(\alpha_2 - \alpha_3\right)v_2^2 - \frac{\mu_3 v_{L,R}}{\sqrt{2} v_{L,R}}
\end{pmatrix},
$$

(3.1)

The masses of the charged Higgs bosons are obtained by diagonalizing the $2 \times 2$ matrices:

$$
m^2_{H^+_L} = -\left[v_2 v_L \left(\alpha_2 - \alpha_3\right) + \frac{\mu_3 v_R}{\sqrt{2}}\right] \frac{v^2}{v_2 v_L} \quad (3.2)
$$

$$
m^2_{H^+_R} = -\left[v_2 v_R \left(\alpha_2 - \alpha_3\right) + \frac{\mu_3 v_L}{\sqrt{2}}\right] \frac{v^2}{v_2 v_R} \quad (3.3)
$$
with \( v^2 = v_L^2 + v_R^2 \) and \( v'^2 = v_L'^2 + v_R'^2 \). Here \( H_2^\pm \) is \( R \)-parity odd and \( H_1^\pm \) is \( R \)-parity even. The other two eigenstates of these matrices correspond to the Goldstone bosons \( G_2^\pm \) (\( R \)-parity even) responsible for giving mass to the \( W_L^\pm \) boson, and the Goldstone \( G_1^\mp \) (\( R \)-parity odd) giving mass to \( W_R^\pm \), also odd under \( R \)-parity.

In the neutral scalar sector, components of the \( \phi^0_1 \) field (\( \Re(\phi^0_1) \) and \( \Im(\phi^0_1) \)) do not mix with other states, as they are both \( R \)-parity odd. They yield the physical \( H_1^0 \) and \( A_1 \) eigenstates, which are degenerate in mass. Calling these masses \( M_{H_1^0} \) and \( M_{A_1} \), we obtain

\[
M_{H_1^0} = M_{A_1}^2 = 2v_L^2\lambda_2 - (\alpha_2 - \alpha_3) (v_L^2 + v_R^2) - \frac{\mu_3 v_L v_R}{\sqrt{2}v_2}. \tag{3.4}
\]

Thus, if these are the lightest \( R \)-parity odd particles, \( H_1^0 \) and \( A_1 \) would form the two components of the dark matter.

For the three remaining scalar and pseudoscalar fields (all of which are \( R \)-parity even), the mass-squared matrices \((M_{R}^{0})^2\) and \((M_{A}^{0})^2\) of in the \((\Re(\phi^0_2), \Re(\phi^0_3), \Re(\chi^0_1), \Re(\chi^0_2), \Im(\phi^0_2), \Im(\phi^0_3), \Im(\chi^0_1), \Im(\chi^0_2))\) bases, are given, respectively, by

\[
(M_{R}^{0})^2 = \begin{pmatrix}
2v_L\lambda_1 - \frac{\mu_1 v_L v_R}{\sqrt{2}v_2} & 2\alpha_2 v_L v_R + \frac{\mu_1 v_R}{\sqrt{2}} & 2\alpha_2 v_L v_R + \frac{\mu_1 v_R}{\sqrt{2}} \\
2\alpha_2 v_L v_R + \frac{\mu_1 v_R}{\sqrt{2}} & 2\lambda_3 v_L^2 - \frac{\mu_3 v_R^2}{\sqrt{2}v_2} & 2\lambda_3 v_L v_R - \frac{\mu_3 v_R^2}{\sqrt{2}} \\
2\alpha_2 v_L v_R + \frac{\mu_1 v_R}{\sqrt{2}} & 2\lambda_3 v_L v_R - \frac{\mu_3 v_R^2}{\sqrt{2}} & 2\lambda_3 v_L^2 - \frac{\mu_3 v_R^2}{\sqrt{2}v_2}
\end{pmatrix}, \tag{3.5}
\]

\[
(M_{A}^{0})^2 = \frac{\mu_3}{\sqrt{2}} \begin{pmatrix}
-\frac{v_L v_R}{v_2} & v_R & -v_L \\
v_R & -\frac{v_L v_R}{v_2} & v_2 \\
-v_L & v_2 & -\frac{v_L v_R}{v_2}
\end{pmatrix}, \tag{3.6}
\]

where \( \alpha_2 = \alpha_1 + \alpha_2 \). The mass of the pseudoscalar boson \( A_2 \) is

\[
M_{A_2}^2 = -\frac{\mu_3 v_L v_R}{\sqrt{2}v_2} \left[ 1 + v_R^2 \left( \frac{1}{v_L^2} + \frac{1}{v_R^2} \right) \right]. \tag{3.7}
\]

The other two CP-odd states in \((M_{A}^{0})^2\) are Goldstone bosons \( G_1^0 \) and \( G_2^0 \) corresponding to the gauge bosons \( Z_L \) and \( Z_R \), respectively. Both the Goldstone bosons \( Z_L \) and \( Z_R \) are \( R \)-parity even, thus conserving \( R \)-parity. Furthermore, unlike in the case of the charged gauge bosons, \( Z_L \) and \( Z_R \) can mix, to give the mass eigenstates \( Z \) and \( Z' \) [22, 23]. Thus, in fact, while LHC constraints \( Z' \) mass, the \( W_R \) mass cannot be constrained directly as it decays into exotic quarks. However, the mass relations between \( Z' \) and \( W_R \) indirectly restricts the latter through the direct constraints on the former.

In the CP-even, \( R \)-parity even scalar sector, we denote the mass eigenstates (the eigenstates of \( M_{R}^{0} \) in Eq. 3.5) as \( H_{0,1,2,3} \), and further identify the lightest state \( H_0^0 \) as the SM-like Higgs boson, \( h \). It is then conventional to fix the quartic coupling, \( \lambda_1 \) in terms of the mass of the lightest Higgs state, \( M_h = 125 \text{ GeV} \), giving

\[
\lambda_1 = \frac{1}{2v^2} \frac{\sqrt{2}v_2v_Lv_RM_h^6 + 4(4)M_h^4 - 2n(2)M_h^2 - 4\alpha_2^2\mu_3v_2^4(v_L^2 - v_R^2)^2}{\sqrt{2}v_Lv_RM_h^6 + (\mu_3v_2 - 2\sqrt{2}\lambda_3v_Lv_R)(v_L^2 + v_R^2)M_h^2 - 2\mu_3v_2\lambda_3(v_L^2 - v_R^2)^2}. \tag{3.8}
\]
With this masses of the other two CP-even (R-parity-even) neutral Higgs boson states are given by

\[ M_{H^0_{2,3}}^2 = \frac{1}{2} \left[ a - M_h^2 + \sqrt{(a - M_h^2)^2 + 4 \left( b + M_h^2 (a - M_h^2) \right)} \right], \quad (3.9) \]

where

\[
\begin{align*}
a &= 2v^2_2 \lambda_1 + 2 (v^2_L + v^2_R) \lambda_3 - \frac{(v^2_L v^2_R + v^2_L + v^2_R)}{\sqrt{2}v_2 v_L v_R} \mu_3, \\
b &= \frac{(v^2_L + v^2_R)}{v_2 v_L v_R} \left\{ 4v^3_2 v_L v_R \left[ (\alpha_1 + \alpha_2)^2 - \lambda_1 \lambda_3 \right] + \sqrt{2}v^3_2 \lambda_1 \mu_3 + \sqrt{2}v^3_2 v_R \lambda_3 \mu_3 \right\} \\
&\quad + \frac{\sqrt{2}v_2 \mu_3}{v_L v_R} \left[ 4v^2_2 v_R (\alpha_1 + \alpha_2) + (v^2_L - v^2_R)^2 \lambda_3 \right].
\end{align*}
\]

We now proceed to investigate the consequences of having $H^0_1$ and $A_1$ as degenerate scalar dark matter candidates. First, we must ensure that the chosen particles satisfy experiments searching for dark matter, and their interactions with ordinary matter. Searches for dark matter fall into three categories: (ii) direct detection, where dark matter is observed through possible scattering events with baryonic matter such as protons and neutrons making up atomic nuclei in the detectors; (ii) indirect detection, where dark matter particles annihilate into SM particles such as photons, positrons, antiprotons etc; and (iii) production at colliders, where dark matter particles are created from colliding of SM particles. (See the review [31]).

In direct detection, experiments aim to detect nuclear recoils emerging from collisions between dark matter particles and a detector target, such as Xenon. Discriminating the signal emerging from dark matter particles from the background requires concentrating on characteristic signatures of dark matter, such as the energy dependence or the annual modulation of the signal [32]. From the non-observation of the signal, stringent bounds were imposed on the nucleon scattering cross section of the DM particle in both spin-independent (SI) and spin-dependent (SD) cross sections. Only the former is applicable here, as scalars are spinless. Several experiments such as XENON [5], LUX [6], PANDA [7], and PICO [8, 9] have set stringent limits on dark matter particle masses based on non-observation of signals.

Complementary to direct detection, indirect detection of dark matter relies on detection of photons and/or electrons or positrons as products of annihilating dark matter particles. Ideal targets are those where the dark matter density is high and the background from astrophysical processes is small or well known, such as galaxy clusters, making the Galactic Centre of the Milky Way a fertile ground for H.E.S.S [33] and Fermi-LAT [34] experiments.

Collider experiments focus on production of dark matter particles in colliders like the LHC in association with other SM particles. In such case, the DM would not be detected and become part of the missing information. This is much like the information that would lost in events with neutrinos in the final state. From the measurement of missing transverse momentum and energy, one can infer the presence of these missing particles. We shall discuss possible LHC signatures in the scenario discussed here in Sec. 4.
To explore the viability of $H_0^1$ and $A_1$ as dark matter candidates, we first investigate the amount of thermal relic abundance of dark matter, aiming to restrict the parameter space based on agreement with the measured cosmological dark matter density. For this, we use the implementation of the ALRM into FeynRules [20, 35], which encodes the information on the particle content of the model and then link this to MicrOmegas package [36], which calculates relic abundance, and direct and indirect cross sections relevant to dark matter. In the early universe $H_0^1$ and $A_1$ would have been produced in abundance, and they were in thermal equilibrium. However, as the Universe cooled down and the temperature came down to near the mass of the dark matter, the annihilation process became more relevant and the reactions fell out of equilibrium, resulting in a fall of the number density of the dark matter. This continued until the reaction rate is larger than the Hubble expansion parameter. Beyond this temperature, the number density of the dark matter remains the same. This freeze-out and the remaining relic abundance of the dark matter thus depends crucially on the annihilation reactions and their cross sections. The total dark matter relic density obtained from the anisotropy in the cosmic microwave background radiation (CMBR) measured by the Planck experiment is, $\Omega_{DM}^{obs} h^2 = 0.120 \pm 0.001$ [4], where $h$ is the dimensionless Hubble constant. An immediate goal of the present study is to find the parameters of the model that give the right annihilation cross section so as to obtain the required relic density. The annihilation channels available depend on the mass of the dark matter candidates ($H_0^1$ and $A_1$). Only channels where sum of the masses of the final states is smaller than $2M_{H_0^1}$ will contribute. Table 2 lists all the annihilation channels for different ranges of $M_{H_0^1} = M_{A_1}$. We restrict our study to $M_{H_0^1}$ up to 2 TeV, which is much lighter than the $Z'$, and therefore channels with $Z'$ in the final state are irrelevant here.

| $M_{H_0^1}$ (GeV) | Annihilation Channels |
|-------------------|-----------------------|
| $M_{H_0^1} < M_h$ | $H_0^1 H_0^1 \rightarrow WW, ZZ, GG, \gamma\gamma, bb$ |
| $M_h < M_{H_0^1} < m_t$ | $H_0^1 H_0^1 \rightarrow WW, ZZ, GG, \gamma\gamma, bb, hh$ |
| $m_t < M_{H_0^1} < M_{H_1^\pm}$ | $H_0^1 H_0^1 \rightarrow WW, ZZ, GG, \gamma\gamma, bb, hh, t\bar{t}$ |
| $(M_{H_1^\pm} + M_W) < 2M_{H_0^1}$ | $H_0^1 H_0^1 \rightarrow WW, ZZ, GG, \gamma\gamma, bb, hh, t\bar{t}, W^\pm H_1^\mp$ |

**Table 2.** Annihilation channels for $H_0^1$ for different scalar dark matter masses.

We consider the following independent parameters: $\alpha_1$, $\alpha_2 = \alpha_3$, $\lambda_2$, $\tan \beta$ and masses of all exotic particles. Other parameters and the VEV’s are fixed in terms of these parameters. For our numerical study, we fix $\tan \beta = 2.0$, $\lambda_2 = -0.1$, $\alpha_1 = 0.1$, $\alpha_2 = \alpha_3 = 0.1$ and perform a scan over range of masses as given in Table 3. We import this scan into MicrOmegas to obtain the relic density and cross sections relevant to direct and indirect detection experiments. In a broader parameter range scan, the results of which are not discussed here, we found that only cases with $H_1^0$ and scotino being closely degenerate lead to the required relic abundance. This is due to the role played by the co-annihilation channels in the freeze-out mechanism. Furthermore, we take $n_\tau$ as the lightest scotino, as
### Table 3

| Parameter               | Range                     |
|-------------------------|---------------------------|
| $M_{H_1^0} = M_{A_1}$   | (100 – 2000) GeV          |
| $M_{H_2^0} - M_{H_1^0}$ | (10 – 60) GeV             |
| $m_{d'} - M_{H_1^0}$    | (200 – 500) GeV           |
| $m_{n_r} - M_{H_1^0}$   | (0.001 – 1) GeV           |
| $\lambda_3$            | (1.0 – 2.0)               |
| $v'$                    | (1.9 – 35) TeV            |
| $|\mu_3|$                | (100 – 2000) GeV          |

| $m_{n_e}$ and $m_{n_\mu}$ |
|---------------------------|
| Case (i) (degenerate)     | $m_{n_e} = m_{n_\mu} = m_{n_r}$ |
| Case (ii) (small splitting)| $(m_{n_e} = m_{n_\mu}) - m_{n_r} =$ Range (10 keV - 20 MeV) |
| Case (iii) (large splitting)| $(m_{n_e} = m_{n_\mu}) - m_{n_r} =$ Range (100 MeV - 10 GeV) |

Three different cases of neutrino mass hierarchy are considered. Choosing $n_r$ as the lightest scotino enhances signals in the collider studies, as discussed in Sec. 4.

in the collider study $\tau$ channel has the advantage of having larger Yukawa coupling. We consider three different mass hierarchies between the scotinos; i.e. (i) $m_{n_e} = m_{n_\mu} = m_{n_r}$, (ii) $(m_{n_\mu}, m_{n_e}) - m_{n_r} \sim 10$ keV - 20 MeV, and (iii) $(m_{n_\mu}, m_{n_e}) - m_{n_r} \sim 100$ MeV - 10 GeV, separately. These three cases are identified, respectively, by greenish yellow, green and magenta dots in Fig. 1 and 2.

In Fig. 1 we show the relic density and cross sections for direct detection (in a log plot) against $M_{H_1^0}$. On the left-hand side, the plot gives the relic density, with horizontal lines representing the Planck constraints within 1$\sigma$. The middle plot shows the direct detection results, compared to the results from the XENON [5] and PICO [8, 9], while in the right-handed plot we keep only the points that satisfy both direct detection and relic density constraints. The figure indicates that points corresponding to all Cases in Table 3 satisfy both constraints, with the region of light and heavy $H_1^0$ being favoured by either degenerate, or small splitting among scotinos, while the region of intermediate $M_{H_1^0}$ is preferred by larger mass splittings among scotinos. In all cases, we choose the scotino masses to be almost degenerate with scalar masses to enhance annihilations and yield correct relic density. For this analysis, we found the relic abundance to be sensitive to variations in $\tan \beta = \frac{v}{v_L}$, while much less so to $\lambda_1, \lambda_2, \alpha_1, \alpha_2$ and $\alpha_3$. For our analysis, we optimized the choice of $\tan \beta = 2$ as it allows for lighter DM masses to satisfy the relic conditions.

In Fig. 2 we plot the results of our analysis on indirect scalar dark matter detection, with the photon flux versus dark matter mass. All the points in the plots obey indirect detection bounds from Fermi-LAT [34], while the black points satisfy relic, direct and
indirect detection bounds together. This figure shows that, for all scotino mass splittings considered here, (i)–(iii), photon flux bounds from indirect detection are consistent with a large region of the parameter space, indicating that a significant range of masses for both the $H^0/A_1$ dark matter candidates and the scotino splittings satisfy all experimental constraints.

**Figure 1.** (Left): Relic density vs. $M_{H^0}$ with horizontal black lines showing $1\sigma$ range $\Omega_{\text{obs}}^{\text{DM}} h^2$. (Middle): Direct detection cross section plotted against $M_{H^0}$, along with bounds from XENON1T (in black solid) and PICO experiments (in black dashed). As the direct detection cross sections are independent of scotino masses, all the three cases overlap. (Right): Direct detection cross section plotted against $M_{H^0}$, with points satisfied by $\Omega_{\text{obs}}^{\text{DM}}$ within $1\sigma$. Different colours correspond to different scotino mass hierarchy with Case (i) (greenish yellow), Case (ii) (green) and Case (iii) (magenta) given in Table 3.

**Figure 2.** Indirect detection restrictions case with the photon flux versus dark matter mass for Case (i) - degenerate scotino mass scenario (Left), Case (ii) - small mass splitting (Middle), and Case (iii) - large mass splitting (Right). All points satisfy constraints from Fermi-LAT [34], while the black dots are also consistent with relic density + DD restrictions imposed by PICO-60 as well as XENON1T experiments (Fig. 1).

We now turn to analyzing the parameter space available for the fermionic candidates for dark matter, restricted by relic abundance, direct detection cross section, and indirect detection experiments.

### 3.2 Scotino Dark Matter

An alternative to the above scalar dark matter scenario is to assume that one of the scotinos is the lightest $R$-parity odd particle. We shall chose $n_\tau$ scotino as the dark matter candidate. This is because it is more promising for collider studies (see Sec. 4). The other two, $n_e$ and
$n_\mu$ can be (i) degenerate with $n_\tau$, or have hierarchical mass. In the non-degenerate case, we shall consider two different cases i.e. (ii) small mass splittings with $(m_{n_\mu}, m_{n_\tau}) - m_{n_\tau} \sim 10 \text{ keV} - 20 \text{ MeV}$, or (iii) large mass splitting with $(m_{n_\mu}, m_{n_\tau}) - m_{n_\tau} \sim 100 \text{ MeV} - 10 \text{ GeV}$. These three scenarios are indicated by the same colour-coded dots as in the scalar DM case reported in the previous subsection (Sec. 3.1). In this section, $R$-parity odd scalars, $H^0_1$ and $A_1^0$ are taken to be heavier with a mass splitting of around 100 GeV with $n_\tau$. Smaller mass splittings are found to not yield the required relic density. The relevant annihilation channels are listed in Table 4.

Table 4. Annihilation channels for $n_\tau$. A specific channel will be available as long as the total mass of the final state is smaller than $2m_{n_\tau}$.

We perform a scan over the parameter region with the couplings, which do not affect the DM annihilation, fixed, and varying the masses of particles involved. The values of the parameters used and the range of masses considered are given in Table 5.

Table 5. Range of masses considered for the scan in the scotino dark matter case, with $q' = d', s', b'$. Three different cases of neutrino mass hierarchy are considered. $n_\tau$ is taken as the lightest, which would be important for the collider studies as discussed in Sec. 4.

In Fig. 3 we plot the relic density and the direct detection cross section, as a function of the scotino dark matter masses. On the plot at the left, we show the relic density, required to be within the horizontal lines representing $1\sigma$ consistency with the measurements at the Planck experiment [4]. The middle plot shows the parameter space restricted by the
XENON [5] and PICO [8, 9] experiments, while on the right, we indicate regions of the parameter space satisfying both direct detection and relic density constraints. As in the case of scalar dark matter, points with degenerate masses, small or larger mass splittings among the scotinos satisfy both constraints, but the masses are required to be $m_{n_\tau} > 500$ GeV for PICO alone, while $m_{n_\tau} > 1250$ GeV for the combined requirements of XENON1T and PICO.

The relic is sensitive to $v' = \sqrt{v_2^2 + v_R^2}$, as $Y_{n_\tau} = m_{n_\tau} / v_R \sim m_{n_\tau} \sqrt{v_R^2 - v_2^2}$, so we have varied both $v' \in [1.9, 35]$ TeV and $m_{n_\tau}$. This dependence can be understood as follows: for a fixed scotino DM mass, if the $v'$ increases within the above-mentioned range, the Yukawa couplings decrease; thus the cross-section mediated by corresponding Higgs bosons would decrease and relic density increases. Moreover, for fixed $v'$, if we increase scotino DM mass, the relic density for these associated channels decreases. But unlike the case of scalar dark matter, the relic is insensitive to variations in $\tan \beta$ or to the scalar couplings. To check compatibility with indirect detection experiments, we plot the photon flux as a function of the scotino mass in Fig. 4. Here again, the greenish yellow points (for degenerate scotino masses), green points (for small mass splittings among scotinos) and magenta points (for large scotino mass splittings) represent regions of parameter space that satisfy indirect detection bounds, while the black asterisks are a subset of these points, which are consistent with relic density bounds and direct detection constraints.

### 3.3 Degenerate Scalar-Scotino Dark Matter

The case where the scalar and scotino masses are the same represents the mixed/degenerate dark matter scenario. We have analyzed this case in detail and found it to be indistinguishable from the scalar dark matter scenario. The reason is that, for the case of scalar dark matter, the scotino masses had to be chosen to be almost degenerate with the DM scalar masses to yield the correct relic density. Thus the degenerate case introduces no new phenomenological features and we shall not investigate it further.
Figure 4. Indirect detection restrictions for scotino dark matter. The photon flux versus dark matter mass with Case (i) - degenerate scotino mass scenario (Left), Case (ii) - small mass splitting (Middle), and Case (iii) - large mass splitting (Right). All points satisfy constraints from Fermi-LAT [34], while the black asterisks are also consistent with relic density + direct detection restrictions from PICO-60 and XENON1T experiments.

4 Discriminating amongst the different scenarios at the LHC

We shall now analyze the signatures of the model at the LHC, through the direct production of the additional particles present beyond the SM within the two distinct dark matter scenarios presented above. The spectrum beyond the SM has two heavy charged scalars, two neutral pseudoscalars, and three neutral scalar particles plus the right-handed charged and neutral gauge bosons, $W_R$ and $Z'$, as well as the exotic fermions, $d', n$ and $\nu_R$.

Exotic quark masses are constrained by experimental bounds. Searches for additional quarks have concentrated on vector-like states, as additional hierarchical quark states conflict with the Higgs gluon fusion data. We briefly review the searches here. Vector-like quarks were searched for at ATLAS [37–41] and CMS [42–46], focusing mainly on the pair-production mode. Mass limits were also obtained from differential cross sections measurements at the LHC [37]. The most stringent limits at 95% confidence level (CL) on masses depend on the assumed branching ratio (BR) configuration: for 100% BR for the decay $b' \to Wt$ masses up to 1.35 TeV are excluded, while for 100% BR for $b' \to Zb$ and $b' \to Hb$, $b'$ masses up to 1.39 TeV and 1.5 TeV, respectively, are excluded [42]. The most recent study at ATLAS [47] looks at pair production of $b'$ quarks in events with at least two electrons or muons, where at least two same-flavour leptons with opposite-sign charges originate from the decay of the $Z$ boson, and where various branching ratios for the decay into a $Z, W$ or $H$ boson and a third-generation quark are considered. Mass limits of $m_{b'} > 1.42$ TeV for singlets, and $m_{b'} > 1.20$ TeV for doublets are obtained.

While these searches do not apply exactly to the exotic quarks in ALRM (which are part of doublets, but with exotic quantum numbers), for our benchmarks we set conservative mass limits on the exotic fermions, $m_{q'} > 1.45$ TeV, $q' = d', s', b'$. The masses of scalar particles are given in Sec. 3.1. The masses of fermions can be set independently from the other sectors. In principle, all these particles can be produced at the LHC in pairs, in association with each other, or with other SM particles, as long as $R$-parity is conserved.

As the model depends on several parameters, we choose two benchmarks corresponding to the scalar dark matter case, BP1 and BP2, and two for the scotino dark matter, BP3.
and BP4, to showcase our results. These benchmarks are parameter points which satisfy dark matter constraints, are consistent with the analysis in the previous subsections 3.1 and 3.2, and show some promise toward being observed at the LHC. For this, the masses of the new particles are set such that the DM candidates (the lightest scalar and/or pseudo-scalar and the scotinos) are in the $\mathcal{O} \sim$ 1 TeV range. Note that, while the Higgs masses could be in the sub-TeV range, correct relic density is obtained only for the case where they are almost degenerate in mass with the scotinos. As dark matter constraints require the scotino masses to be $m_{n_{\tau}} > 1250$ GeV, this pushes the Higgs masses in the TeV region as well. Similarly, the lightest charged Higgs bosons and the exotic down-type quarks are also chosen to have masses in the $\mathcal{O} \sim$ 1 TeV range. This enhances their production, followed then by the cascade decay down to the DM plus other SM particles. Note that for the scotino cases, we take the tau scotino as the LSP to enhance production rates due to the larger Higgs-$\tau$ Yukawa coupling. (Note that in BP1 and BP2 the scotino and scalar masses are almost degenerate, to enhance co-annihilation as discussed in Sec. 3.1.)

The presence of charged Higgs bosons and exotic quarks in the low-TeV range of mass presents the possibility that their presence can be explored at the LHC. On the other hand, the new gauge bosons $W_R$ are expected to be a few TeV in mass so as to respect the existing LHC limits on $Z'$ dilepton decays [29]. This bound is satisfied by all the points we have considered in the DM analysis. The values for the model parameters corresponding to benchmark points BP1, BP2, BP3 and BP4, satisfying all the DM constraints from the study in Sec. 3.2 are given in Table 6. With these choices for the parameters, the

| BP’s | tan $\beta$ | $v_R$ (TeV) | $\lambda_2$ | $\lambda_3$ | $\alpha_1$ | $\alpha_2 = \alpha_3$ | $\mu_3$ |
|------|-------------|-------------|-------------|-------------|-------------|----------------|---------|
| BP1  | 2           | 12.9        | -0.1        | 1.2         | 0.1         | 0.1            | -100    |
| BP2  | 3           | 14.4        | -0.1        | 1.4         | 0.01        | 0.1            | -340    |
| BP3  | 2           | 14          | -0.001      | 1.6         | 0.1         | 0.1            | -320    |
| BP4  | 10          | 13          | -0.01       | 1.6         | 0.1         | 0.1            | -2800   |

| BP’s | $M_{H^0} = M_{A^0}$ | $m_{n_{\tau}}$ | $m_{n_{\mu}}$ | $m_{n_e}$ | $m_{d'}$ | $m_{s'}$ | $m_{b'}$ |
|------|---------------------|----------------|----------------|-----------|---------|---------|---------|
| BP1  | 1230                | 1230.004       | 1230.085       | 1230.453  | 1465    | 1704    | 1712    |
| BP2  | 1428                | 1428.039       | 1428.481       | 1428.868  | 1764    | 1877    | 1902    |
| BP3  | 1258.51             | 1210           | 1215           | 1220      | 1600    | 1700    | 1800    |
| BP4  | 1603.97             | 1395           | 1399           | 1402      | 1600    | 1700    | 1800    |

Table 6. Benchmark points compatible with the scalar (BP1 and BP2) and scotino (BP3 and BP4) DM constraints, selected for the study of collider effects.

masses of right-handed gauge bosons and the other heavy scalars corresponding to the above BP’s are listed in Table 7. The choice for the masses of new particles such that the DM candidates (the lightest scalar and/or pseudo-scalar and the scotinos) in the low
Table 7. Masses of the gauge bosons and heavy scalars corresponding to the four Benchmark Points considered in this study.

| BP’s | $M_{H^\pm}$ | $M_{H^0}$ | $M_{A^0}$ | $M_{H^0}$ | $M_{H^0}$ | $M_{W_R^+}$ | $M_{Z'}$ | $\Omega h^2$ |
|------|-------------|-----------|-----------|-----------|-----------|-------------|---------|-----------|
| BP1  | 1515.839    | 1277      | 1515.882  | 20137.437 | 4212      | 5054.39     | 0.119   |
| BP2  | 1520.740    | 1471      | 1520.912  | 21750.899 | 4687.23   | 5624.63     | 0.121   |
| BP3  | 2814.18     | 1258.67   | 2814.24   | 2814.72   | 4571.56   | 5485.88     | 0.120   |
| BP4  | 16123.30    | 1604.60   | 16123.30  | 23255.30  | 4245.22   | 5094.27     | 0.119   |

Table 7. Masses of the gauge bosons and heavy scalars corresponding to the four Benchmark Points considered in this study.

In the TeV range, the lightest charged Higgs also arranged to also have masses in the same range, facilitates the production of these latter degrees of freedom, which then decay into the DM and other SM particles.

For production mechanisms, the only available processes are the pair productions of $q'q'$ (with $q' = d', s', b'$), $H^+_2H^-_2$ and $W^+_RW^-_R$ at the LHC with centre of mass energy 14 TeV and high luminosity, as these particles have negative $R$-parity, necessary for decay into the lightest $R$-parity negative particle. The corresponding cross sections are listed in Table 8. For the scalar DM, the dominant cross section comes from $pp \rightarrow q'q'$, while for the scotino DM case, the only viable process is the charged Higgs pair production, since the gauge bosons $W_R$ are heavy$^3$. In Table 8, the dash means that the cross section is not important for the BP under consideration. The relevant decay branching fractions of $q'$ and $H^+_2$ are given in Table 9.

For the case of scalar DM we consider benchmarks BP1 and BP2 and study $pp \rightarrow q'q'$, with $q' \rightarrow bH^0_1/A_1$. The light quark decay channels are negligible compared to the $b$ decay channel. The final state is thus $b\bar{b}$ DM DM, with $DM = (H^0_1/A_1)$ not detected, and $H^+_2$.

$^3$The same is true for the production cross section $pp \rightarrow W^+_RH^+_2$ which is much smaller than that of $pp \rightarrow H^+_2\ H^+_2$. Further, we do not include processes like $pp \rightarrow q'q'$ with $q' \rightarrow H^+_2\ u \rightarrow \tau\nu, \nu$, considering its large jet multiplicity.
we consider the SM background $pp \to b \bar{b} \nu \bar{\nu}$, where we sum over the neutrino flavours ($\nu = \nu_e + \nu_\mu + \nu_\tau$) and assume $b$-tagging. The differences in cross sections between BP1 and BP2 are due to the differences in the masses of the exotic quarks, assumed heavier in BP2 than in BP1.

For the case of scotino dark matter, we consider the production chain $pp \to H_2^+ H_2^-$, followed by the decay $H_2^\pm \to n_\tau \tau^\pm$ (with the $\tau$ scotino as the lightest to enhance production rates due to the larger Higgs-$\tau$ Yukawa coupling), leading to the final state process $pp \to H_2^+ H_2^- \to n_\tau n_\tau \tau^+ \tau^-$. The decay rates for $H_2^\pm \to n_\tau \tau^\pm$ for BP3 and BP4 are included in Table 9. We limit our feasibility study to the parton level, and consider the SM background $pp \to \nu \bar{\nu} \tau^+ \tau^-$. The corresponding cross sections for the signal and background for BP1, BP2, BP3 and BP4 are listed in Table 10.

For the collider analysis, we used MadGraph5 [48] and MadAnalysis5 [49] to generate events with the input parameters corresponding to the BP’s considered. We use the parameters as defined in the software, before imposing our cuts to enhance the signal over the background.

First we analyze the scalar dark matter case. Considering a cut and count method to improve the signal significance, in Table 11 and 12 we give the number of signal and background events and the corresponding significance at each stage of selection, for an
integrated luminosity of 300 fb$^{-1}$. The significance is defined as

$$S = \frac{N_{\text{signal}}}{\sqrt{N_{\text{signal}} + N_{\text{background}}}},$$

(4.1)

and it yields a sufficiently large significance even at the early stages of HL-HLC. However, this analysis does not include any detector effects, and possible additions to background from processes like $pp \rightarrow bb$, $bbjj$, $jj$, $jjjj$, which can mimic the final state of $bb + \not{E}_T$ when parton showering, jet formation and detector efficiencies are considered. We do not attempt a full analysis including these effects here. These effects could reduce the significance quoted in Table 11 and 12. For example, an assumed total event reconstruction efficiency of 30% and an increase in the background events by about 50% would change the final significance from 13.8 to 3.4 at the integrated luminosity of 300 fb$^{-1}$, in the case of BP1. In Fig. 5

| Selection criteria | Fiducial Cross section (fb) | Significance $S$ @ 300 fb$^{-1}$ |
|--------------------|-----------------------------|---------------------------------|
| Initial (no cut)   | 20.3                        | 2046.6                          | 7.7                             |
| reject : $E_T < 200$ GeV | 19.6                        | 1175.6                          | 9.8                             |
| reject : $E_T(b) < 100$ GeV | 18.1                        | 777.5                           | 11.1                            |
| reject : $\not{E}_T < 100$ GeV | 16.2                        | 464.6                           | 12.8                            |
| reject : $-1.5 < y(b) < 1.5$ | 15.1                        | 341.4                           | 13.8                            |

Table 11. Fiducial cross section of the signal ($pp \rightarrow d'd' \rightarrow bb H^0 H^0_1/A_1 A_1$) and the SM background ($pp \rightarrow bb\nu\nu$) corresponding to BP1 at 14 TeV LHC, with and without the selection criteria considered, and the signal significance at the HL-LHC.

we show the relevant kinematic distributions for BP1. The first column refers to the case before the selection criteria are applied, while second column corresponds to the signal and background events, after the listed selection cuts are applied. We repeat the same analysis for BP2. The cuts implemented are given in Table 12 and the plots corresponding to signal and background events before and after cuts are shown in Fig. 6.

The above analysis illustrates that HL-LHC can potentially discover the presence of exotic quarks that appear in the ALRM version considered in this study, even at 300 fb$^{-1}$.

Turning to the scotino DM case, we analyze the signal and background. Defining the signal significance as in Eq. 4.1, the fiducial cross sections and the signal significance corresponding to the integrated luminosities of 300 fb$^{-1}$ and 3000 fb$^{-1}$ are given in Table 13.

In Fig. 7 (left column) we show some of the kinematic distributions normalized to an integrated luminosity of 3000 fb$^{-1}$ for the benchmark BP3. We plot, in the left column (top to bottom): the total transverse energy $E_T = \sum_{\text{visible particles}} |p_T|$, the rapidity $y$, the total transverse energy of the $\tau$ lepton, $E_T(\tau)$, and the missing transverse energy $\not{E}_T = |\sum_{\text{visible particles}} p_T|$. We noticed that the signal events are mostly concentrated in a larger
Figure 5. Parton level event distributions for $pp \to q'q' \to \bar{b}bH_0^1H_0^1/A_0^1A_0^1$ for BP1 normalized to an integrated luminosity of 300 fb$^{-1}$ along with the SM background (in red), here $q'$ represents all the exotic quarks i.e., $d', s', b'$. (Left column, top to bottom): the total transverse energy $E_T$, the rapidity $y$, the total transverse energy of the $b$ quark, $E_T(b)$, and the missing transverse energy $E_T$, before cuts. (Right column, top to bottom): the same distributions after implementing the cuts in Table 11, which reduce the background.
Table 12. Fiducial cross section of the signal ($pp \rightarrow d'd' \rightarrow bbH_0^1H_0^1/A_1A_1$) and the SM background ($pp \rightarrow bb\nu\nu$) corresponding to BP2 at 14 TeV LHC, with and without the selection criteria considered, and the signal significance at the HL-LHC.

| Selection criteria (BP1) | Fiducial Cross section (fb) | Significance $S$ @ 300 fb$^{-1}$ |
|-------------------------|-----------------------------|----------------------------------|
| Initial (no cut)        | 3.7                         | 2046.6                           | 1.4                              |
| reject : $E_T < 200$ GeV| 3.3                         | 79.4                             | 6.3                              |
| reject : $E_T(b) < 200$ GeV| 2.8                     | 29.5                             | 8.4                              |

Table 13. Fiducial cross section of the signal ($pp \rightarrow H_0^+H_0^- \rightarrow \nu\tau^{+}\tau^{-}$) and the SM background ($pp \rightarrow \nu\nu\tau^{+}\tau^{-}$) corresponding to BP3 at 14 TeV LHC, with and without the selection criteria considered, and the signal significance (Eq. 4.1) at the HL-LHC.

| Selection criteria (BP3) | Fiducial Cross section (fb) | Significance, $S$ at integrated luminosity |
|-------------------------|-----------------------------|---------------------------------------------|
| Initial (no cut)        | 5.52                        | 506.11                                      | 300 fb$^{-1}$                     |
| reject : $|y(\tau)| < 2.5$ | 0.096                       | 0                                           | 5.39 16.98                        |

rapidity region, while the background is more or less evenly distributed in the central region, within $|y| < 2.5$, so we impose the cuts as in Table 13. We chose to highlight features of the $\tau^+$ lepton, but similar results are obtained for the other $\tau$ lepton, $\tau^-$. Exploiting this, we employ a rejection criteria of $|y| < 2.5$, to eliminate the background, while still keeping about 288 events at 3000 fb$^{-1}$ luminosity. Distributions after this event selection are given in Fig. 7 (right column).

The case of BP4 is similar, with the cuts given in Table 14 and the event distributions given in Fig. 8. With the same selection criteria used in the case of BP3 (rejecting events in the central rapidity region with $|y| < 2.5$) completely eliminates the background, but yields a cross section of only 0.01 fb and only 30 events at the highest luminosity 3000 fb$^{-1}$, with detector efficiencies estimated to be 20%.

Selecting an alternative cut, $E_T > 400$ GeV, the cross section is reduced to 0.2 fb cross section for the signal after cuts, corresponding to 595 events at 3000 b$^{-1}$. While these cuts do not eliminate the background, they reduce it to 2 fb corresponding to 5834 events. The significance is however larger than the case of rapidity cut eliminating the whole of background, 2.3 at 300 fb$^{-1}$ and 7.4 at 3000 fb$^{-1}$. We show the results for both cuts in Table 14, and give the plots for both the rapidity and for the transverse energy cuts in Fig. 8.

Note, however that observability of BP3 is more likely than of BP4 due to the larger
Figure 6. Parton level event distributions for $pp \rightarrow q'q' \rightarrow \bar{b}bH_0^1/\bar{A}_0^1/A_0^1$ for BP2 normalized to an integrated luminosity of 300 fb$^{-1}$ along with the SM background (in red), here $q'$ represents all the exotic quarks i.e., $d', s', b'$. (Left column, top to bottom): the total transverse energy $E_T$, the rapidity $y$, the total transverse energy of the $b$ quark, $E_T(b)$, and the missing transverse energy $\slashed{E}_T$, before cuts. (Right column, top to bottom): the same distributions after implementing the cuts in Table 12, which reduce the background.
Figure 7. Parton level event distributions for $pp \rightarrow H_2^+ H_2^- \rightarrow n_\tau n_\tau \tau \tau$ for BP3 normalized to an integrated luminosity of 3000 fb$^{-1}$ along with the SM background (in red). (Left column, top to bottom): the total transverse energy $E_T$, the rapidity $y$, the total transverse energy of the $\tau^+$ lepton, $E_T(\tau^+)$, and the missing transverse energy $\hat{E}_T$, before cuts. (Right column, top to bottom): the same distributions after the selection criteria of $|y| > 2.5$, which eliminates the background.

corresponding cross section for $pp \rightarrow H_2^+ H_2^-$. This yields an increase of the number of events of BP3 compared to BP4, and has a measurable impact on the signal significance.
Table 14. Fiducial cross section of the signal \((pp \rightarrow H^+_2 H^-_2 \rightarrow \nu \nu \tau^+ \tau^-)\) and the SM background \((pp \rightarrow \nu \nu \tau^+ \tau^-)\) corresponding to BP4 at 14 TeV LHC, with and without two selection criteria considered, and the signal significance (Eq. 4.1) at the HL-LHC.

| Selection criteria (BP4) | Fiducial Cross section (fb) | Significance, \(S\) at integrated luminosity 300 fb\(^{-1}\) | Significance, \(S\) at integrated luminosity 3000 fb\(^{-1}\) |
|-------------------------|----------------------------|-----------------------------------------------------|-----------------------------------------------------|
| Initial (no cut)        | 0.58                       | 506.11                                              |                                                     |
| reject : \(|y(\tau)| < 2.5\) | 0.009                      | 0                                                   | 1.73                                                |
| reject : \(E_T < 400\) GeV | 0.198                      | 1.945                                               | 2.3                                                 |

Figure 8. Parton level event distributions for \(pp \rightarrow H^+_2 H^-_2 \rightarrow \nu \nu \tau^+ \tau^-\) for BP4 normalized to an integrated luminosity of 3000 fb\(^{-1}\) along with the SM background (in red). (Left column, top to bottom): the total transverse energy \(E_T\). The rapidity \(y\), the total transverse energy of the \(\tau^+\) lepton, \(E_T(\tau^+)\), and the missing transverse energy \(\cancel{E}_T\) before cuts. (Middle column, top to bottom): the same distributions after the selection criteria of \(|y| > 2.5\), which eliminates the background. (Right column, top to bottom): the same distribution, after imposing the cut \(E_T > 400\) GeV.
This feasibility study demonstrates that, under favourable conditions, the HL-LHC may be able probe the presence of $H_2^+$ around 1 TeV mass in this model within a few years of its run, while heavier ones need to wait for much larger integrated luminosity.

5 Conclusion

We examined the dark matter candidates in ALRM and the opportunity to observe signals compatible with these choices at the LHC. Introducing an additional $U(1)_S$ symmetry allows to define a generalized lepton number, while protecting the model against low energy flavor violation, and allows the additional Higgs bosons to be relatively light. In this scenario an $R$-parity arises naturally, as in supersymmetry, enabling us to distinguish among $R$-parity positive particles (which include all the SM particles) and $R$-parity negative particles, the lightest of which is stable and thus a candidate for dark matter. Depending on the mass hierarchy, the model allows either a scalar dark matter (neutral $R$-parity negative Higgs boson and pseudoscalar) or a fermion (scotino) dark matter.

We study the parameter space compatible with the dark matter relic density, and the direct and indirect dark matter experiments for these two possibilities separately to find compatible regions. While the scalar dark matter case accommodates lighter masses, the scotino case restricts the dark matter mass to be above a TeV. We note that while mixed scalar-fermion dark matter could exist, to yield the correct relic density, the scalar dark matter scenario requires the scotinos to be almost degenerate in mass with the DM candidate, and thus the mixed case resembles closely the scalar case. This approximate degeneracy means that constraints from dark matter experiments require both scalar and fermionic candidates to have masses in the TeV region. We find that in all scenarios, degenerate, or small and larger mass splittings among the scotinos can be accommodated, and we indicate the parameters sensitive to the experimental constraints and restrict the parameter space accordingly.

We follow the dark matter analysis by an exploration of the collider signature of the model. We devise four benchmarks, two for the scalar dark matter case, and two for the scotinos. The scalar dark matter could be probed by the production through two exotic quarks $pp \rightarrow d'\bar{d}'$, followed by the branching ratios into $bH_1^0/A_1$ (where $H_1^0/A_1$ is the DM candidate). This production-decay mode yields a relatively large number of signals, and even though the QCD background is much larger, cuts on the rapidity and transverse energy give a promising signal over background ratio for two representative sets of model parameter values presented in BP1 and BP2. Even considering that the background can be much larger, and with conservative detector efficiencies, this signal can be probed at LHC with 300 fb$^{-1}$, and would be indicative of exotic $d'$ quarks with masses in the TeV range.

The scotino benchmarks BP3 and BP4 also prove to be promising. Produced through $pp \rightarrow H_2^+H_2^- \rightarrow n\tau n\tau^+\tau^-$ (with $n\tau$ the dark matter candidate), the process also yields events that are much smaller than the corresponding background. However, a cut on the rapidity in the central region renders the signal above the background, with a significance of between 1.7 to 17 at the LHC operating at 14 TeV, with luminosity of 300-3000 fb$^{-1}$. For the second benchmark BP4, a cut on the transverse energy, while not eliminating the
background, yields a better signal significance. In particular, observing BP3 is promising at 300 fb$^{-1}$, while BP4 would be observable only at 3000 fb$^{-1}$. This signal would be indicative of the presence of charged Higgs bosons with masses in the TeV region. While a more detailed collider study including realistic detector effects is beyond the scope of our work, our parton level simulations indicate the model shows some promise in finding signals for the lightest charged Higgs with mass in the TeV range with reasonable integrated luminosity, even accounting for detector efficiencies of 20-30%.

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