Muon transfer from deuterium to helium

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We report on an experiment at the Paul Scherrer Institute, Villigen, Switzerland measuring x rays from muon transfer from deuterium to helium. Both the ground state transfer via the exotic (dp34He)* molecules and the excited state transfer from (µd)* were measured. The use of CCD detectors allowed x rays from 1.5 keV to 11 keV to be detected with sufficient energy resolution to separate the transitions to different final states in both deuterium and helium. The x-ray peaks of the (dp34He)* and (dp3He)* molecules were measured with good statistics. For the D2 + 4He mixture, the peak has its maximum at Eµd34He = 6768±12 eV with FWHM Γµd34He = 863±10 eV. Furthermore the radiative branching ratio was found to be κµd34He = 0.301 ± 0.061. For the D2 + 4He mixture, the maximum of the peak lies at Eµd34He = 6831±8 eV and the FWHM is Γµd34He = 856±10 eV. The radiative branching ratio is κµd34He = 0.636 ± 0.097. The excited state transfer is limited by the probability to reach the deuterium ground state, q1s. This coefficient was determined for both mixtures: q1s3He = 68.9 ± 2.7% and q1s4He = 90.1 ± 1.5%.

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I. INTRODUCTION

Muon transfer from hydrogen to helium is a loss channel in muon catalyzed fusion (µCF), the muon induced fusion of hydrogen isotope nuclei). In the µCF cycle, where in favorable cases a negative muon can catalyze up to 200 fusions, muon transfer to helium limits the fusion yield. Muon transfer from hydrogen to helium can happen during the cascade in muonic hydrogen (excited state transfer) or from the muonic hydrogen 1s ground state through the formation of an excited, metastable hydrogen–helium molecule (µHe)* (h = proton p, deuteron d, or triton t, and He = 3He or 4He), a reaction first proposed by Aristov 2. These molecules decay from the excited state to the unbound ground state mostly by x-ray emission (Eγ ∼ 6.8 keV). Auger electron emission and µHe breakup are also possible. The scheme of the principal transfer and decay processes is presented in Fig. 1. The muon entering a deuterium–helium mixture may be captured either by deuterium (with probability Wd) or by helium (with probability Whel) via direct capture. The two vertical arrows indicate the cascade of the muon to the 1s ground state. The e1He represents the probability for the µd* to reach the ground state in the presence of helium. Excited state transfer is shown by the upper horizontal arrow. Ground state transfer is shown with a rate λµHe via the (dpHe)* molecule. The (dpHe)* molecule decay channels are shown with rates λe for the Auger decay, λγ for the x-ray channel, and λp for the break up channel, respectively.

FIG. 1: Scheme of the main processes induced by a µ− in a binary-gas mixture of deuterium and helium. The fusion reactions are not drawn. The symbols are defined in the text.
The energies and widths of the molecular states have been characterized by measuring the x-ray energy spectra. The most precise experiment on \((p\mu\text{He})^+\), with its intrinsically low x-ray yield, was carried out by our collaboration \([3]\). The \((d\mu\text{He})^+\) molecules were also studied by our collaboration \([1]\) and recently an experiment was performed on \((t\mu\text{He})^+\) \([2]\). In those publications, earlier less precise experiments were referenced and discussed in detail. Our precision of \(\sim 0.2\%\) for the energies and \(\sim 1.2\%\) for the widths of the \((d\mu\text{He})^+\) molecular deexcitations make detailed comparisons with calculations possible. Precise results on the excited state transfer probabilities were also obtained. The combined use of results obtained with standard detectors and CCD techniques allowed us to determine the radiative branching ratio of the \((d\mu\text{He})^+\) molecules, a value which has been of considerable theoretical interest in recent years due to its direct and unique connection to the wave function overlap in the muonic molecule \([3]\). The experimental challenges in obtaining the results were overcome thanks to months of beam time, and the use of large area Charge Coupled Device (CCD) x-ray detectors, as well as germanium detectors \([3]\). A more detailed description of the present work can be found in Augsburger's thesis \([7]\).

### II. EXPERIMENT

The experiment was performed at the \(\mu\text{E4}\) channel at the Paul Scherrer Institute (PSI), Villigen, Switzerland. Setup, Ge and Si(Li) detector, gas handling and target conditions can be taken from Tresch \([3]\) and Gartner \([4]\). Figure 2 shows the target setup with the detectors. Detailed information about the large area CCD x-ray detectors is found in Tresch \([3]\).

![Fig. 2: Schematic target setup as viewed by the entering muons. The thin lines represent target and detector windows. The drawing is not to scale.](image)

| Target | \(T\) | \(p\) | \(\phi\) | \(c_{\text{He}}\) (atomic) |
|--------|------|------|------|-----------------|
| \(D_2 + ^3\text{He}\) | 30.5 \(\pm\) 0.2 | 5.58 \(\pm\) 0.01 | 69.7 \(\pm\) 0.7 | 9.13 \(\pm\) 0.27 |
| \(D_2 + ^4\text{He}\) | 31.5 \(\pm\) 0.2 | 5.51 \(\pm\) 0.01 | 79.2 \(\pm\) 0.8 | 3.25 \(\pm\) 0.05 |

### A. Experimental conditions

The experimental setup consisted of a gas target, Ge and Si(Li) detectors, scintillators, and CCD detectors, as shown in Fig. 2. Both Tresch \([3]\) and Gartner \([4]\) measured the molecular formation rates \(\lambda_{\mu\text{He}}\) in protium and deuterium. The CCDs were used by Tresch \([3]\) for the protium measurement. The present work shows our results for the deuterium measurement using CCDs.

The deuterium and related measurements, as well as the gas handling and mixture analysis are described in great detail in Gartner \([4]\). From this reference, we summarized in Table I the gas mixtures used for our analysis. The choice of helium concentration was dictated by the goal of Gartner \([4]\) measurement, namely the molecular formation rates. Due to the different theoretical values for the rates in \(D_2 + ^3\text{He}\) and \(D_2 + ^4\text{He}\), the relative concentrations of \(^3\text{He}\) and \(^4\text{He}\) are very different.

### B. CCDs as low energy x-ray detectors

CCDs are excellent x-ray detectors in the energy range from 1 keV to 15 keV (details can be found in \([3]\)). In most cases, an x ray produces charge in only a single pixel, whereas charged particles produce cluster events or tracks with more than one adjacent pixel hit. The usual way to distinguish x ray event pixels from charged particle, neutron, and higher energy gamma-ray background is to require that none of the eight surrounding pixels have a charge that is considerably above the noise level. The CCD type used for this experiment was a silicon based MOS type, model CCD–05–20 by E2V. Each CCD chip has a size of 4.5 cm\(^2\) \((770 \times 1152\) pixels of area 22.5 \(\times\) 22.5 \(\mu\text{m}^2\)) and a depletion depth of \(\sim 30 \mu\text{m}\). In this experiment the energy resolution of the muonic deuterium \(\mu\text{D}(2\rightarrow 1)\) line was 130 eV FWHM and the muonic helium \(\mu\text{He}(2\rightarrow 1)\) transition had a resolution of 215 eV FWHM.

1 E2V, Technologies Inc, Waterhouse Lane, Chelmsford, Essex, CM1 2QU, England (previously EEV and Marconi).
FIG. 3: Muonic deuterium x–ray energy spectrum. Diamonds are the experimental points, whereas the solid line represents the fit to the data.

Unfortunately, our CCDs cannot be triggered so there is no timing information. The CCD data were read out approximately every 3 minutes by a data-acquisition system which operated independently from the data acquisition of the other detectors. Therefore, we cannot normalize the collected data to the incoming muon rate. The results of CCD’s measurements can only be analyzed using absolute numbers.

III. ANALYSIS AND RESULTS

A. Analysis of the x–ray energy spectra

We present in this section the different spectra obtained and explain the fitting procedures. Two CCDs were used. Since each CCD half was read out separately, we have 4 sets of measurements. At first, the data from each half CCD were analysed separately in order to detect any possible malfunction and to perform the energy calibration and background reduction by single-pixel analysis. After checking that the separate treatment of each half CCD gave consistent results, the calibrated energy spectra were added and the fits performed on the summed spectra.

1. Pure element spectra

The x–ray spectra from single element targets were studied in detail to find as much information as possible about the detector response function and target related backgrounds. The final results required that the entire energy range be fit at once and this was accomplished in several steps.

The final result for the muonic deuterium x–ray spectrum is presented in Figs. 3 and 4, namely the $\mu d$ x–ray transition to the 1s ground state and a series of contaminant peaks essentially at higher energies. Also visible are the electronic Kα and Kβ transitions of Si (CCD), Cr, Mn, Fe, Ni, and Cu (target), although only the positions of the Kα peaks are indicated in Fig. 4 (except for Fe, where both lines are clearly visible). In addition, muonic aluminium at 10.66 keV from the $\mu Al(5−4)$ transition is clearly visible. Other muonic aluminium transitions, $\mu Al(6−5)$ at 5.79 keV and $\mu Al(7−6)$ at 3.49 keV, are

FIG. 4: Energy spectrum from the pure deuterium measurement (same as Fig. 3) showing the contamination in the higher energy region. It is used to estimate the importance of the different contaminants shown (electronic Si, Cr, Mn, Fe, Ni, and Cu lines and muonic Al).

FIG. 5: Muonic $^4$He x–ray energy spectrum. The muonic helium Lyman series are located between 8 and 11 keV. The same contaminants as in the muonic deuterium spectrum can be seen. The shape of the $\mu ^4He(2−1)$ peak is used to obtain the standard line shape which is given in Fig. 6.
also present but much weaker than the $\mu Al(5-4)$ line.

The first fits were made using Gaussian peak shapes and a standard CCD background with the goal of locating all lines and characterizing the continuous background. The CCD background in a high-noise environment was studied in detail in Ref. [7]. The large hill starting at 7 keV seen in Fig. 4 is due essentially to energy deposited by electrons crossing the CCD. The relative importance of each contaminant was estimated with the Kβ/Kα intensity ratio held fixed according to values given in Ref. [9]. Once the relative intensities of the contaminant peaks were known, the first fits to the full spectra were carried out. The variation of the contaminant intensities for the different spectra were found to be small, and hence could be well parametrized.

Figure 4 presents the spectrum for pure $^4$He. The Lyman series between 8 and 11 keV and the Balmer series around 2 keV are clearly seen and the contaminant peaks are the same as in the muonic deuterium spectrum.

To further refine the fit, the muonic helium $\mu$He($2-1$) transition was examined in detail to fully understand the true CCD response function for the line shape. This peak was chosen, even though it contained a small copper contamination (less than 1%), since it has high statistics and is well separated from the other peaks. The small copper contribution was subtracted. Since we could not use an analytical function for fitting the remaining asymmetric peaks, we interpolated the asymmetric peak shape of the $\mu$He($2-1$) line, shown in Fig. 6 to fit the data correctly. As one can see, it looks like a Gaussian with an asymmetry on the left side. This same peak shape was then used to represent all other lines, replacing the Gaussian shape, and the spectra refit. In particular, the FWHM of each peak was obtained by using a scaling factor from the FWHM given in Fig. 6. In addition, all peak positions were defined by the center of gravity (not by the maximum). The values for the resolution of the $\mu$He($2-1$) transition as well as the electronic lines are shown in Fig. 7. The fitting procedure was repeated for both the muonic deuterium and muonic helium spectra until a minimum $\chi^2$ was obtained. Replacing the Gaussian line shape with the final fit function including background parametrization and asymmetric line shapes reduced the $\chi^2_{dof}$ from 5 to about 1.4 for both spectra.

2. Spectra of the $D_2 + ^4$He and $D_2 + ^3$He mixtures

Figure 8 presents the energy spectrum of the $D_2 + ^4$He mixture. In addition to the peaks from muonic deu-
FIG. 9: Resulting peak shape (dotted line) of the (dµ⁴He)⁺ molecular x-ray after fitting contaminants and background (solid line).

FIG. 10: X-ray energy spectrum of the D₂⁺³He mixture. The wide peak represents the decay of the (dµ³He)⁺ molecule via an x ray of about 6.8 keV.

terium, muonic helium, and the contaminants, a large x-ray peak from the decay of the (dµ³He)⁺ molecule appears around 6.8 keV. Again, the fitting procedure outlined above was used for all peaks except the molecular peak, for which theoretical curve has been calculated and is given in Ref. 11. The difference in shape corresponding to decays of the J = 0 and J = 1 state, respectively, is negligible in our case. Hence, the calculated shape of Ref. 11 was taken for the shape of this molecular peak. The positions of the maximum is a free parameter. We used two scaling factors to determine the amplitude and FWHM relative to the theoretical shape. Figure 9 shows the fit of the D₂⁺⁴He mixture in the region of the molecular peak (the fit was carried out over the whole energy region, 1.6 to 11.25 keV). The results are given in Table II.

Figure 10 presents the spectrum of the D₂⁺³He mixture and Fig. 11 shows the same spectrum in the region of the molecular peak. The analysis of that spectrum was identical to the D₂⁺⁴He analysis with results also given in Table II.

B. Relative intensities of the K series transitions in muonic ⁴He

The relative intensities of the K series transitions in pure muonic ⁴He are given in Table III. The errors include a statistical part (fit) and a systematic part (CCD detection efficiency). The main error comes from the CCD efficiency which is not surprising since the fit parameters for “CCD depletion depth” and “CCD window thickness” converge in a range of (28 ± 2) µm and (35 ± 1) µm respectively. The results are compared to 3 where no isotopic effect (³He or ⁴He) was seen (last column of Table III). The agreement is excellent for the Kα transition, and the significant discrepancies of the other values are understood, since the measurement of Tresch 3 was carried out at a lower density, which ex-

| Value   | Unit  | (dµ³He) | (dµ⁴He) |
|---------|-------|---------|---------|
| E_{dµHe} | [eV]  | 6768 ± 12 | 6831 ± 8 |
| Γ_m     | [eV]  | 914 ± 9  | 907 ± 8  |
| Γ_{dµHe} | [eV]  | 863 ± 10 | 856 ± 10 |
| N_{dµHe} |       | (411 ± 23) × 10⁵ | (196 ± 11) × 10⁵ |
where we added the errors quadratically. Taking this sum from Table IV, one gets a measurement of the detection efficiency. The errors include both statistical and CCD efficiency errors. The last column shows the results from Tresch [3].

| Transition   | $K_i/K_{\text{total}}$ | $K_i/K_{\text{total}}$ |
|--------------|------------------------|------------------------|
| $\mu\text{He}(2 - 1)$ | 46.9 ± 4.5             | 47.0 ± 0.2             |
| $\mu\text{He}(3 - 1)$ | 27.9 ± 2.8             | 20.3 ± 0.1             |
| $\mu\text{He}(4 - 1)$ | 16.3 ± 1.7             | 19.8 ± 0.1             |
| $\mu\text{He}(5 - 1)$ | 6.2 ± 0.7              | 8.8 ± 0.1              |
| $\mu\text{He}(6 - 1)$ | 2.5 ± 0.4              |                       |
| $\mu\text{He}(7 - 1)$ | 0.1 ± 0.3              |                       |
| $\mu\text{He}(\infty - 1)$ | 0.1 ± 0.1             | 4.1 ± 1.6             |

The numbers of $K\alpha$ and $K\beta$ events occurring with the direct capture, $N_{\text{dc}}$, and $N_{\text{dc}}$, were obtained using the intensity ratios $K_i/K_{\text{total}}$ determined in the pure $\mu^4\text{He}$ spectrum and $N_{\text{dc}}$. The total number of $\mu^4\text{He} K\alpha$ and $K\beta$ events in the mixture is given in Table IV. The differences are due to excited state transfer from $\mu d^\ast$. The number of $K\alpha$ and $K\beta$ events coming from excited state transfer, $N_{\text{exc}}$, and $N_{\text{exc}}$, are the difference between the first two lines of Table IV and the previously determined $N_{\text{dc}}$ and $N_{\text{dc}}$. Therefore the sum of events from excited state transfer is $N_{\text{exc}} = (398 \pm 47) \times 10^3$. Now $q_{1s}^4\text{He}$ can be determined by

$$q_{1s}^4\text{He} = \frac{N_{\mu d}^4\text{He}(1s)}{N_{\mu d}^4\text{He}(1s) + N_{\text{exc}}^4\text{He}} = 90.1 \pm 1.5 \% $$

where $N_{\mu d}^4\text{He}(1s)$ is the total number of $\mu d$ Lyman x rays in the $D_2 + ^3\text{He}$ mixture (see Table IV). The analysis carried out in the case of the $D_2 + ^3\text{He}$ mixture was the same as in the $D_2 + ^4\text{He}$ mixture with the additional hypothesis that the muonic cascade was the same in both $^3\text{He}$ and $^4\text{He}$. Pure $^3\text{He}$ was not measured (only $^4\text{He}$) for this work. However, Tresch [3] has shown no isotopic effects between the two gases. Therefore, the $q_{1s}^3\text{He}$ is determined as

$$q_{1s}^3\text{He} = \frac{N_{\mu d}^3\text{He}(1s)}{N_{\mu d}^3\text{He}(1s) + N_{\text{exc}}^3\text{He}} = 68.9 \pm 2.7 \% $$

where $N_{\mu d}^3\text{He}(1s)$ is the total number of $\mu d$ Lyman x rays in the $D_2 + ^3\text{He}$ mixture (Table IV).

### C. Excited state transfer and the $q_{1s}^4\text{He}$ probability

The $q_{1s}$ value represents the probability for a newly formed light muonic atom to fully deexcite to the $1s$ state when the muon also has the possibility of transferring directly from an excited state to a heavier nucleus (cf. Fig. II). In binary mixtures, the notation often includes the identity of the heavier nucleus, $q_{1s}^3\text{He}$ for example.

We begin our analysis with the $D_2 + ^4\text{He}$ mixture. The number of events in the K series transitions is $\mu^4\text{He}$ and $\mu^4\text{He}$ in the gaseous mixture of $D_2 + ^4\text{He}$ is given in Table IV. The sum of $\mu d$ events represents the total number of $\mu d$ which reach the ground state and is called $N_{\mu d}^4\text{He}(1s)$.

Part of the $^4\text{He}$ events come from the direct capture of the muon by helium, the other part by excited state transfer from muonic deuterium. It was shown in $\S$ that in gaseous $H_2 + ^4\text{He}$ mixtures, excited-state transfer proceeds only to the levels $n = 3$ and $n = 2$ of $^4\text{He}$. A detailed comparison of Figs. $\S$ and $\S$ also shows that in the $D_2 + ^4\text{He}$ mixture there is a large enhancement of the $K\alpha$ and $K\beta$ He lines over the higher transitions. In addition, some L lines can also be seen in Fig. $\S$. The fact that the $L\gamma$ transition (in Fig. $\S$) contains approximately 200 000 (efficiency corrected) events versus only 2000 for the $L\delta$ line further confirms the above hypothesis. Therefore the sum of the events from the $\mu\text{He}(4 - 1)$, $\mu\text{He}(5 - 1)$, and $\mu\text{He}(6 - 1)$ transitions in $^4\text{He}$ is due to direct capture. Taking this sum from Table IV one gets a measured number of direct capture, $N_{\text{dc}} = (65.5 \pm 6.2) \times 10^3$, where we added the errors quadratically.

In the spectrum from pure $^4\text{He}$ (see results in Table IV) the percentage sum of the $K_i/K_{\text{total}}$ fractions for $i \geq 4$ is 25.20 ± 1.81%. The $N_{\text{dc}}^4\text{He}$ therefore corresponds to 25.20% of the total number of K-series x rays in $^4\text{He}$. (N$_{\text{dc}}$). Thus, we deduced the total number of direct capture events $N_{\text{dc}}^4\text{He} = (260 \pm 43) \times 10^3$. This number will allow us to differentiate between direct capture and excited state transfer events in the $K\alpha$ and $K\beta$ intensities, measured in the mixture of deuterium and $^4\text{He}$.

The radiative branching ratio $\kappa_{d^4\text{He}}$ of the $(d\mu^4\text{He})^*$ molecule

The radiative branching ratio $\kappa_{d^4\text{He}}$ for the $(d\mu^4\text{He})^*$ molecular decay can be determined the same way as in $\S$ for the $(p\mu^4\text{He})^*$ molecule. $\kappa_{d^4\text{He}}$ is given by

$$\kappa_{d^4\text{He}} \cdot W = \frac{N_{d^4\text{He}}}{N_{\mu d}^4\text{He}(1s)} ,$$

where $N_{d^4\text{He}}$ is the number of events in the molecular peak (see Table IV) and $N_{\mu d}^4\text{He}(1s)$ the total number of the $\mu d$ Lyman series x rays in the mixture. $W$ is the probability of a $\mu d_{1s}$ forming a $(d\mu^4\text{He})^*$ molecule and is given by the equation:

$$W = \frac{\phi^\text{He} \cdot \lambda_{d^4\text{He}}}{\Lambda_{\mu d_{1s}}} ,$$
TABLE IV: Number of events in the K series transitions of $\mu d$ and $\mu$He in a gaseous mixture of deuterium and $^4$He as well as in a gaseous mixture of deuterium and $^3$He. All values are corrected for CCD detection efficiency.

| Transition | $\mu d \times 10^5$ | $\mu^4$He $\times 10^3$ | $\mu d \times 10^5$ | $\mu^3$He $\times 10^3$ |
|------------|---------------------|--------------------------|---------------------|--------------------------|
| (2 − 1)    | 2915 ± 173          | 438 ± 26                 | 1445 ± 86           | 805 ± 48                 |
| (3 − 1)    | 603 ± 21            | 154 ± 10                 | 385 ± 14            | 287 ± 19                 |
| (4 − 1)    | 85.8 ± 3.4          | 38.6 ± 2.9               | 55.4 ± 2.8          | 61.9 ± 4.2               |
| (5 − 1)    | 2.3 ± 2.8           | 15.9 ± 3.8               | 1.4 ± 2.3           | 15.4 ± 1.9               |
| (≥ 6 − 1)  | 1.2 ± 1.8           | 10.9 ± 3.9               | 1.0 ± 1.5           | 4.0 ± 3.4                |
| total      | $N^\mu_{\mu d}(1s) = 3608 ± 174$ | 657 ± 29                 | $N^\mu_{\mu d}(1s) = 1889 ± 87$ | 1174 ± 52               |

where $\phi$ is the atomic density of the mixture, normalized to LHD, $c_{\text{He}}$ is the helium atom proportion, $\lambda_{\mu d}\text{He}$ the ground state transfer rate from $\mu d$ to He, and $\Lambda_{\mu d 1s}$ the disappearance rate of muons from the $(\mu d)_{1s}$ level.

TABLE V: Radiative branching ratio $\kappa_{\mu d}\text{He}$ of the $(d\mu^3\text{He})^*$ and $(d\mu^4\text{He})^*$ molecules. The errors are commented in the text.

| $(d\mu^3\text{He})^*$ | $(d\mu^4\text{He})^*$ |
|----------------------|----------------------|
| $\lambda_{d\mu^3\text{He}} (10^8 s^{-1})$ | 1.856 ± 0.077 | 10.50 ± 0.21 |
| $\lambda_{d\mu^4\text{He}} (10^8 s^{-1})$ | 1.637 ± 0.032 | 3.159 ± 0.018 |
| $W$ | 0.721 ± 0.073 | 0.856 ± 0.044 |
| $\kappa_{d\mu^3\text{He}}$ | 0.301 ± 0.061 | 0.636 ± 0.097 |

The so determined values for $\kappa_{d\mu^3\text{He}}$ and $W$ are given in Table V for both helium isotopes. The values for $\lambda_{d\mu^3\text{He}}$ and $\Lambda_{\mu d 1s}$ (in Table V) were taken from Gartner [4]. While the errors for $N_{d\mu^3\text{He}}$ and $N_{d\mu}(1s)$ include both the statistical and systematic uncertainties, the errors in $\phi$ and $c_{\text{He}}$ given in Table II are purely systematic. The errors on $W$ and $\kappa_{d\mu^3\text{He}}$ were calculated by normal error propagation without specifying the type of error.

IV. DISCUSSIONS

A. General features of the x–ray energy spectra

The spectra presented in Figs. 3, 4, 5 and 10 deserve three general comments. First, the relative intensities of the muonic deuterium $K\alpha$ and $K\beta$ transitions are density dependent [11]. Since the density changed between mixtures (see Table II), the muonic deuterium $K\alpha$ peak is slightly enhanced over $K\beta$ in the $D_2 + ^4$He mixture.

Second, the x–ray count rate for the $(d\mu^3\text{He})^*$ molecule is smaller than for the $(d\mu^4\text{He})^*$ molecule since in the $(d\mu^3\text{He})^*$ case the two–particle breakup channel is more prominent. Third, the relative helium/deuterium line intensities depend on the helium concentration (see Table D).

B. $(d\mu^3\text{He})^*$ and $(d\mu^4\text{He})^*$ molecules

In Table VI our CCD results for the position of the maximum of the two molecular peaks are compared to theoretical predictions [10,12] and to results [1] obtained with Ge and Si(Li) detectors. The Ge and Si(Li) detector results seem to favor the $J=1$ state but the CCD results imply a preference for transitions from $J = 0$. Even if the CCD results are more precise and the CCD statistics are significantly higher, it is difficult to decide for $J = 0$ or $J = 1$ since the results of both detector types are effectively compatible considering the errors. What can be said unambiguously is that the CCD results are in excellent agreement with both theoretical predictions for decay from the $J = 0$ state. It should be stressed that both the Ge and Si(Li) and the CCD data were taken simultaneously during the experiment.

In Table VII the CCD experimental FWHM widths for the molecular peaks are again compared with the theoretical predictions [10,12] and with the Ge and Si(Li) data [4]. The CCD results are in very good agreement with theoretical predictions for both $J = 0$ and $J = 1$ states, but distinguishing between the two states is not possible due to the almost identical theoretical values. On the other hand, the results with the “classic” (Ge or Si(Li)) x–ray detectors are between 1.5 to 2.5 $\sigma$ away

TABLE VI: Theoretical and experimental energies of the maximum of the molecular peaks, in eV. For the experimental values, we also list the detector type. Our values are taken from Table II.

| Theory | $(d\mu^3\text{He})$ | $(d\mu^4\text{He})$ |
|--------|-------------------|-------------------|
| $J = 0$ | 6766 | 6808 | 6836 | 6878 |
| $J = 1$ | 6760 | 6782 | 6836 | 6857 |

| Experiment | $(d\mu^3\text{He})$ | $(d\mu^4\text{He})$ |
|------------|-------------------|-------------------|
| Ge + Si(Li) | $(6.80 \pm 0.03) \times 10^3$ | $(6.88 \pm 0.03) \times 10^3$ |
| this work  | 6768 ± 12 | 6831 ± 8 |
TABLE VII: Theoretical and experimental widths (FWHM) of the molecular peaks in eV. For the experimental values, we also list the detector type. Our values are taken from Table II.

| Mixture | Experimental (dμ3He) | Experimental (dμ4He) | Theoretical (dμ3He) | Theoretical (dμ4He) |
|---------|----------------------|----------------------|---------------------|---------------------|
| H2 + 3He | 863 ± 10             | 856 ± 10             |                     |                     |
| H2 + 4He | 910 ± 20             |                     |                     |                     |
| D2 + 3He |                     | 863 ± 10             | 856 ± 10            |                     |
| D2 + 4He |                     | 910 ± 20             |                     |                     |

TABLE VIII: Comparison of the theoretical and experimental radiative branching ratios κ of the (dμHe)+ molecules. Only Kravtsov includes all three disintegration channels (the others neglect the Auger channel, given in Fig. 1).

| Mixture | κ_{dμ3He} | κ_{dμ4He} | κ_{dμ3He} | κ_{dμ4He} |
|---------|-----------|-----------|-----------|-----------|
| Kino    | 0.234     | 0.503     | 0.465     |           |
| Gershtein | 0.185    | 0.41      | 0.44      |           |
| Kravtsov | 0.31      | 0.45      | 0.69      |           |
| Belyaev | 0.33      | 0.40      | 0.67      |           |
| this work | 0.309    | 0.568     | 0.54      |           |

D. Ground state formation probabilities q_{1s}^He

The meaning of q_{1s}^He has been described in Section III C. Our results for the deuterium–helium mixtures, Eqs. (1) and (2), are listed together with those for the hydrogen–helium mixtures in Table IX. It is interesting to note that in both cases (hydrogen or deuterium) q_{1s}^He is smaller for 3He, and therefore, the excited state transfer is more probable for the lighter of the two helium isotopes. In the case of hydrogen–deuterium mixtures, q_{1s}^He has been shown to depend on the concentration of the components of the mixture. The large difference seen in our case between D2 + 3He and D2 + 4He is therefore partially due to the differing helium concentrations (see Table IX). The second observation is that q_{1s} is significantly larger for deuterium, a result of consequence in the case of muon catalyzed fusion in deuterium–helium mixtures.

V. CONCLUSIONS

The use of CCDs for low energy x–ray detection allowed for a complete energy measurement of muonic deuterium, helium, and molecular (dμHe) x rays with excellent energy resolution and low background. The large CCD surface resulted in an increased solid angle and therefore in better statistics when compared to traditional Ge or Si(Li) detectors. Of course, results like transfer rates still need the usual x–ray detectors since the CCDs give no timing information. The simultaneous use of CCDs and other x–ray detectors allows for systematic error checks of the experiment since the CCD electronics is completely independent. In conclusion, the addition of CCDs permitted a characterization of all transfer parameters and some high precision results. Only the use of CCD detectors allowed the determination of the radiative branching ratio, a result which was long awaited by theorists.

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