Speed limits for radiation driven SMBH winds

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ABSTRACT

Context. Ultra Fast Outflows (UFOs) have become an established feature in X-ray spectra of Active Galactic Nuclei (AGN). According to the standard picture, they are launched at accretion disc scales with relativistic velocities, up to 0.3-0.4 times the speed of light. Their high kinetic power is enough to induce an efficient feedback on galaxy-scale, possibly contributing to the co-evolution between the central supermassive black hole (SMBH) and the host galaxy. It is therefore of paramount importance to fully understand the UFO mechanisms, and in particular the processes driving their acceleration and the relation with the accretion flow from which they originate.

Aims. In this paper, we investigate the impact of special relativity effects on the radiative pressure exerted onto the outflow. The radiation received by the wind decreases for increasing outflow velocity v, implying that the standard Eddington limit argument has to be corrected according to v. Due to the limited ability of the radiation to counteract the black hole gravitational attraction, we expect to find lower typical velocities with respect to the non-relativistic scenario.

Methods. We integrate the relativistic-corrected outflow equation of motion for a realistic set of starting conditions. We concentrate on a range of ionisation columns, density and launching radii consistent with those typically estimated for UFOs. We explore a one-dimensional, spherical geometry and a three-dimensional setting with a rotating thin accretion disc.

Results. We find that the inclusion of special relativity effects leads to sizeable differences in the wind dynamics and that v is reduced up to 50 % with respect to the non-relativistic treatment. We compare our results with a sample of UFO from the literature, and we find that the relativistic-corrected velocities are systematically lower than the reported ones, indicating the need for an additional mechanism, such as magnetic driving, to explain the highest velocity components. We note that these conclusions, derived for AGN winds, have a general applicability.

Key words. accretion, accretion disks - black hole physics - quasars: supermassive black holes - quasars: absorption lines - opacity - relativistic processes

1. Introduction

Fast outflows, and in particular Ultra Fast Outflows (UFOs), are routinely observed in Active Galactic Nuclei (AGN) as blueshifted absorption and emission features imprinted on the X-ray spectrum, with velocities ranging from ~0.03 to 0.4 ~ 0.5 times the speed of light c (Tombesi et al. 2011, 2015; Nardini et al. 2015; Fiore et al. 2017; Parker et al. 2017). They are launched at accretion disc scales from the central supermassive black hole (SMBH) and may display a kinetic power as high as 20-40 % of the bolometric luminosity of the AGN (Feruglio et al. 2015; Nardini et al. 2015; Nardini & Zubovas 2018; Laurenti et al. 2020), which is more than enough to trigger a massive feedback in the host galaxy, according to theoretical models (Di Matteo et al. 2005; Hopkins & Elvis 2010; Gaspari et al. 2011).

Despite their crucial importance in the framework of the co-evolution between the host galaxy and the SMBH (Kormendy & Ho 2013), the physics of these outflows, and particularly their acceleration mechanism, still remains mostly unknown. According to one of the most accepted scenarios, the gas is accelerated through the pressure of the radiation emitted in the vicinity of the central black hole, even though it is not yet fully clear up to which velocities this mechanism can be effective (Proga & Kallman 2004; Higginbottom et al. 2014; Hagino et al. 2015; King & Pounds 2015).

Similarly, broad absorption lines (BALs) in the UV regime are observed in ~10 ~ 20% of optically selected quasars. Their velocities can be up to 0.3c and are located at parsec-scales from the SMBH (Hamann et al. 2018; Bruni et al. 2019), thus representing another potential energy input for a galactic-scale feedback. As for the X-rays winds, radiative driving has been suggested as their main driver (Elvis 2000; Matthews et al. 2020).

In a recent paper, Luminari et al. (2020) discussed the importance of special relativity effects when the wind outflow velocity becomes mildly relativistic, v ~ 0.05c. In fact, due to the space-time transformation, the amount of radiative power received by the fast wind decreases with increasing v: with respect to a layer of gas at rest, the amount of radiation impinging on the wind is reduced of ~ 30% for v = 0.1 c; of ~ 90% for v = 0.5 c. This implies that the classical derivation of the radiative pressure for a static gas is no longer valid for high velocity winds; accordingly, the radiative driving scenario has to be revised to incorporate these effects.

In this Paper, we integrate the equation of motion for a wind launched at accretion disc scales in order to assess the impact...
of special relativity effects on radiative acceleration. We will mainly focus on X-ray winds; however, our results applies also for BAL winds. In Sect. 2 we present a simple, one-dimensional model of a wind illuminated by a luminosity corresponding to the Eddington value and we demonstrate that, owing to these effects, radiation alone is not able to counteract the gravitational attraction of the SMBH. In Sect. 3 we present a three-dimensional scenario in which the gas is lifted from a geometrically thin accretion disk and it is radiatively accelerated. We refine this model in Sects. 4 and 5 with a more detailed treatment of the wind opacity. We present the results in Sect. 6 and we discuss them in Sect. 7. Finally, we summarise our results in Sect. 8.

2. One-dimensional, spherically symmetric wind model

In order to have a glimpse on the importance of special relativity effects, we start from a simple toy model as follows. We assume that all the luminosity comes from a central point source and the gas has an initial velocity $v_0$ at a distance $r_0$ from the centre. We solve the equation of motion along the radial coordinate $r$. According to the Euler momentum equation, the force exerted by the radiation pressure gradient $\nabla p$ on an infinitesimal wind element with density $\rho$ is:

$$\frac{dv}{dt} = \nabla p - \frac{G M \rho}{r^2}$$

(1)

where $\frac{dv}{dt}$ is the wind acceleration and $G, M$ are the gravitational constant and the SMBH mass, respectively. For the sake of simplicity, we assume for the moment that i) the wind is optically thin and ii) its opacity is dominated by the Thomson cross-section. We will relax these assumptions in the following. This way, we obtain an equation of motion for the wind:

$$\frac{dv}{dt} = \frac{L'}{4 \pi r^2 c} - \frac{G M}{r^2}$$

(2)

Where $L'$ is the central luminosity in the wind reference frame $K'$ and $k$ is the opacity of the wind, which we approximate as $k = \frac{\sigma_T c}{2}, $ where $\sigma_T, m_p$ are the Thomson cross-section and the proton mass, respectively (Rybicki & Lightman 1986). In the definition of $L'$ we include special relativity effects as described in (Lumiani et al. 2020), so that $L' = L \cdot \Psi$, where $L$ is the luminosity in the source frame $K$ and $\Psi \equiv \psi^4 = \frac{1}{\gamma(1 + \beta \cos \theta)}$, where $\gamma$ is the Lorentz factor, $\beta = \frac{v}{c}$ and $\theta$ is the angle between the velocity of the gas and the incident luminosity $L$.

For a wind that is moving radially outward, $\theta = 0$ deg, the luminosity can be written as $L' = L(\frac{1 - \beta^2}{1 + \beta^2})$. We can rewrite Eq. (2) as:

$$\frac{dv}{dt} = \frac{L}{4 \pi r^2 c} \left(1 - \frac{\beta^2}{1 + \beta^2}\right) \frac{\sigma_T}{4 \pi r^2 c m_p} - \frac{G M}{r^2}$$

(3)

Where $r$ and $\beta$ are functions of $v$ itself. The complete set of equations, including initial conditions, can be written as:

$$\frac{dv}{dt} = \frac{L}{4 \pi r^2 c} \left(1 - \frac{\beta^2}{1 + \beta^2}\right) \frac{\sigma_T}{4 \pi r^2 c m_p} - \frac{G M}{r^2}$$

(4a)

$$r(t) = r_0 + \int_{t_0}^{t} v \, dt$$

(4b)

$$r_0 = r(t = t_0)$$

(4c)

$$v_0 = v(t = t_0)$$

(4d)

Where $t_0, t_1$ are the starting and ending time of the numerical integration, respectively. Moreover, we assume that the launching velocity of the wind $v_0$ corresponds to the rotational velocity of an accretion disc, orbiting around the black hole with a Keplerian profile, at $r = r_0$, so that $v_0 = \sqrt{\frac{G M}{r_0}}$. Albeit this choice of $v_0$ may seem arbitrary at this point, it will be useful to compare the results with those of the following Sections. We also note that the escape velocity at $r = r_0$ is equal to $\sqrt{\frac{2 G M}{r_0}}$ . We can rewrite Eqs. (4) as:

$$\frac{dv}{dt} = \left(\frac{1}{1 + \beta^2}\right) \frac{1}{r^2}$$

(5a)

$$r(t) = r_0 + \int_{t_0}^{t} v \, dt$$

(5b)

$$r_0 = r(t = t_0)$$

(5c)

$$v_0 = \sqrt{\frac{2 G M}{r_0}}$$

(5d)

where $\lambda_{Edd} \equiv L / L_{Edd}$ is the luminosity in units of the Eddington luminosity $L_{Edd} = \frac{3 \times 10^{38} M_{sun}}{r}$, $t$, $r$ are in units of the gravitational radius and time, $r_G \equiv \frac{G M}{c^2}, t_G = \frac{r}{c}$ respectively, and $v$ is in units of $c$. We span the interval between $5$ and $500$ $r_G$ for $r_0$, to encompass the typical launching radius of UFOs, which usually lies between $\sim 50$ and some hundreds $r_G$ (Tombesi et al. 2012, 2013; Nardini et al. 2013; Tombesi et al. 2015; Laurenti et al. 2020). We divide this interval in five logarithmically-spaced steps: $r_0 \in \{5.0, 15.8, 50.0, 158.1, 500.0\} r_G$. As we will discuss in detail in Sect. 5 we note that the assumption of a point source may be less accurate for launching radii smaller than 50.0$G$. Nonetheless, it is instructive to study the solutions down to the smallest radii to identify possible trends. We integrate the equation for $10^9 t_G$, after which the dynamics of the wind reaches a steady state and the velocity appears to be almost constant in all the cases. We note that $10^9 t_G$ corresponds to $\sim 1(100) \text{yrs}$ for $M = 10^7 (10^9) M_{sun}$, while present-day X-ray observations have observation times smaller than a month. This will allow us to follow the wind dynamics for a sufficient time scale to compare with the observations for any value of $M$ inside the typical AGN range. We find that the wind evolution is best sampled by a logarithmic time grid, rather than by linear steps. We fix the number of time elements to $5 \cdot 10^6$ to obtain an optimal numerical accuracy. Using a higher resolution does not produce noticeable improvements in the solutions.

We show in Figure 1 the numerical result of Eqs. 5 for $\lambda_{Edd} = 1$. For comparison, we also show the classic analogue of Eq. 5, i.e., without the luminosity reduction factor $\Psi$ due to relativistic effects. Hereafter, we will indicate with solid(dashed) lines the values relative to the relativistic(classic) treatment, if not stated otherwise. Since we input a luminosity corresponding to the Eddington limit, $\lambda_{Edd} = 1$, in the classic case the radiative pressure is able to counteract (by definition) the gravitational pull from the black hole. As a result, the acceleration of the gas is null and we obtain constant velocity solutions. Once the wind is launched with a given $v_0$, it escapes from the system with constant $v = v_0$, as can be seen in the right panel of Fig. 1.

As expected, relativistic effects reduce radiation pressure, resulting in a deceleration of the wind under the gravitational pull of the SMBH. Indeed, it can be seen that the wind trajectories, especially the ones at smaller radii (i.e., closer to the black hole) undergo a significant velocity reduction. In the extreme case of $r_0 = 5 r_G$, the velocity drops to 0. When $v = 0$, relativistic ef-
factors vanish and radiation pressure is able, as in the classic case, to sustain the wind against the gravitational force, leading to a "stalling wind". The highest final velocity is given by the case with $r_0 = 50.0 R_\odot$ and it is $\approx 0.1 c$, consistent with the typical observed UFO velocities (e.g., Tombesi et al. 2011, Gofford et al. 2015).

3. Axisymmetric wind launched from an accretion disk

Let us now rewrite Eq. [5] in the case of a wind launched from an accretion disc. We assume axisymmetry and a geometrically thin disc, such as in Shakura & Sunyaev (1973), orbiting with a Keplerian profile. We adopt a cylindrical coordinate system $(R, \phi, z)$. The set of equations is then:

$$\frac{dR}{dt} = \left( \frac{\Lambda_{Edd}}{\gamma^2 R^2 (1 + \beta \cos \theta)^2} - 1 \right) \frac{R}{R^3} + \frac{\beta^2}{R^3}$$

$$\frac{dz}{dt} = \left( \frac{\Lambda_{Edd}}{\gamma^2 R^2 (1 + \beta \cos \theta)^2} - 1 \right) \frac{z}{R^3}$$

$$R = R_0 + \int_{t_0}^{t} v_R \, dt$$

$$z = \int_{t_0}^{t} v_z \, dt$$

$$r = \sqrt{R^2 + z^2}$$

$$v_0 = v(t = t_0) = (0, v_{rot}, v_z)$$

$$r_0 = r(t = t_0) = (R_0, 0, 0)$$

where, as in Eqs. [5] $r, t$ are in units of $R_\odot, t_\odot$, $\theta$ is the angle between the incident luminosity and the direction of motion of the gas and we assume that the luminosity source is point-like. Hereafter, we indicate in bold the vectorial quantities. In the first two equations, the second term in the right-hand bracket corresponds to the gravitational attraction. $l$ is the specific angular momentum (angular momentum per unit mass), which is a conserved quantity during the motion. $r_0, v_0$ are the starting radius and velocity, respectively. We assume that, initially, the gas lies on the disk plane and the starting velocity lifts the gas above the disk, along the z coordinate, with a velocity proportional to the disc rotational velocity $v_{rot} = \sqrt{\beta^2 R^2 + \beta^2 z^2}$. The velocity along the $\phi$ coordinate is updated at each step to ensure the conservation of $l$. These initial conditions are rather general, and represents a good approximation of the radiatively-driven wind scenario (Proga et al. 2000, Proga & Kallman 2004), as well as the magneto-hydrodynamic (MHD) scenario, in which the gas is lifted through magnetic field lines co-rotating with the disk (Blandford & Payne 1982, Contopoulos & Lovelace 1994, Fukumura et al. 2010, 2014, Cui & Yuan 2020).

Fig. 2 shows the solutions of Eqs. [6] for $R_0 = [5.0, 15.8, 30.0, 158.1, 500.0] R_\odot$, an integration time of $10^6 t_\odot$, a logarithmic temporal resolution of $5 \cdot 10^6$ steps, as in Sect. 2, $\Lambda_{Edd} = 1$ and $v_{rot} = v_{out}$. For comparison, we also show the corresponding classic solutions. As expected, the highest differences are observed at smaller radii, where the velocity is higher and the relativistic effects are stronger. We present in Fig. A.1 in the Appendix a detailed plot of the wind dynamics.

Hereafter, we concentrate on the outflow velocity, defined as $v_{out} = \sqrt{v_R^2 + v_z^2}$, rather than on the total wind velocity $v = \sqrt{v_R^2 + v_\phi^2 + v_z^2}$, to better compare our results with observations. The velocity of the observed UFOs is primarily derived through spectroscopy, thanks to the Doppler shift of the wind absorption lines. These lines are usually described with Gaussian or Voigt profiles, i.e. they have an average energy and some degree of broadening. The observed wind outflow velocity $v_{obs}$ is usually derived from the average velocity, while the broadening is phenomenologically ascribed to turbulence or rotational motion within the wind.

In our model, $v_{obs}$ is given by the projection of $v_R + v_\phi$ along the line of sight (LOS), while the rotational velocity $v_\phi$ only contributes to the broadening of the line, thanks to the axisymmetry of the system. The highest $v_{obs}$ is given by $v_{out}$, and corresponds to the case in which the LOS is parallel to $v_R + v_\phi$. We refer to Fukumura & Tombesi (2019) for a detailed discussion on this point. Interestingly, the authors discuss the possibility that a rotational motion of the wind around the X-ray corona is responsible for the broadening of the absorption lines, in a similar fashion to the discussion here.
4. Force multipliers

In the accretion disc wind literature, the wind opacity is usually calculated analytically over a broad range of absorption lines in the UV and X-ray energy range (see e.g. Proga & Kallman 2004; Risaliti & Elvis 2008; Sim et al. 2010; Dyda & Proga 2018; Quera-Bofarull et al. 2020), obtaining the so-called "force multipliers". Here, we use the radiative transfer code XSTAR (Kallman & Bautista 2001; Saez & Chartas 2011; Chartas et al. 2009) to perform calculations in a similar fashion using Cloudy photoionisation code (Ferland et al. 2017), albeit with a different formalism.

XSTAR accurately computes the transmitted spectrum $S_T$ through a gas layer, as a function of the following input quantities:

- $S_I$, the incident spectrum, and its integrated ionising luminosity $L_I^\text{int}$ in the 1-1000 Ry interval (1 Ry = 13.6 eV);
- $r_0$, the distance of the gas from the central luminosity source;
- $n_0$, the gas number density at $r_0$;
- $N_H$, its column density;
- $\alpha$, the coefficient regulating the radial dependence of $n$: $n = n_0 \left(\frac{r}{r_0}\right)^{\alpha}$;
- $\sigma_{v\text{ broad}}$, the gas velocity dispersion regulating the broadening of the absorption features.

The difference $L_I - L_T$ (where $L_I, L_T$ are the integrated luminosity of $S_I, S_T$) corresponds to the amount of radiation absorbed by the wind thanks to its opacity. This difference corresponds to a momentum $\Delta p$ deposited on the wind, which can be written as $\Delta p = \int_L^{E_f} \sigma_T N_H \, dv$, where we introduce the new variable $L_{\text{rad}} = \int_L^{E_f} \sigma_T$. Specifically, for a given set of initial parameters $\{S_I, r_0, n_0, N_H, \alpha, \sigma_{v\text{ broad}}\}$ we run an XSTAR simulation and we calculate $L_{\text{rad}}$ as:

$$L_{\text{rad}} = \int_{E_0}^{E_1} \frac{x'}{x'} - \frac{x}{x} \, dv$$

(7)

where $E_0, E_1$ correspond to the lower and upper energy bound and $x', x$ are the incident and transmitted photons, respectively, as functions of the frequency $x$, so that $\int x' \, dv = S_I$ and $\int x \, dv = S_T$. From a mathematical point of view, $L_{\text{rad}}$ corresponds to a weighted average of the wind opacity. In all the cases of interest, absorption features are comprised in the energy interval between 0.1 eV and 100keV, that we choose as $E_0, E_1$, respectively.

It is important to note that XSTAR, as well as other photoionisation codes such as Cloudy, does not allow the inclusion of a net velocity of the gas and the related relativistic effects. In order to take them into account, it is convenient to transform the spectra from the rest frame $K$ to the wind reference frame $K'$, and to manipulate $S_I$ and $S_T$, namely to shift their frequencies by a factor $\psi$ and multiply their fluxes by $\psi^2$ (we refer to Luminari et al. 2020 for a detailed explanation). However, since $L_{\text{rad}}$ is calculated as a ratio between $S_T$ and $S_I$, the transformations cancel out so that $L_{\text{rad}}$ can be directly calculated in $K$ without the need of any relativistic transformation.

We integrate the equation of motion, Eq. [2] for a radial interval $\Delta r$, in which a wind column density $N_H$ is enclosed, and we include the momentum $\Delta p$. The resulting equation is:

$$\frac{dv}{dt} = \frac{\Delta p}{4 \pi r^2 m_p N_H} + \frac{L_{\text{bol}}' \sigma_T}{4 \pi r^2 m_p} - \frac{GM}{r^2}$$

$$= \frac{1}{4 \pi r^2 m_p} \left(\frac{L_{\text{bol}}' f_{\text{rad}}}{N_H} + L_{\text{bol}}' \sigma_T\right) - \frac{GM}{r^2}$$

(8)

where we also include Thompson scattering and $L_{\text{bol}}' f_{\text{rad}}, L_{\text{bol}}' \sigma_T$ correspond to the bolometric luminosity and the incident luminosity between $E_0$ and $E_1$, respectively. The $'$ symbol indicates that the luminosities are in the $K'$ frame, i.e. $E_{\text{bol}}' = L_{\text{bol}}'(E_{\text{bol}}') = L_{\text{bol}}(E_{\text{bol}}) \cdot \frac{1}{\Delta t(\text{emission})}$. It must be noted that, for this equation to hold, $\Delta r$ must be small enough so that $r$ can be approximated as constant (i.e., $\Delta r \ll r$).

We put ourselves in the same framework of Sect. 3 (axisymmetry, thin accretion disk and conservation of $I$). The complete set of equations is then:

$$\frac{dv}{dt} = \left(\frac{\lambda_{\text{bol}}' f_{\text{rad}}}{\sigma_T N_H} + \lambda_{\text{bol}}' \sigma_T - 1\right) \frac{r}{f_3} + \frac{\beta^2}{(GM/c^2) \cdot r^3}$$

(9a)

$$\frac{dv}{dt} = \left(\frac{\lambda_{\text{bol}}' f_{\text{rad}}}{\sigma_T N_H} + \lambda_{\text{bol}}' \sigma_T - 1\right) \frac{z}{f_3}$$

(9b)

$$R = R_0 + \int_{\theta_0}^{\theta_1} v_\theta \, dt$$

(9c)

$$z = \int_{\theta_0}^{\theta_1} v_z \, dt$$

(9d)

$$r = \sqrt{R^2 + z^2}$$

(9e)

$$v_0 = (0, v_\theta, v_z)$$

(9f)

$$R_0 = (R_0, 0, 0)$$

(9g)

where, as in Sect. 3, $r, t$, are in units of $r_G, t_G$ and $\lambda_{\text{bol}}' \equiv L_{\text{bol}}'(L_{\text{bol}}' / \sigma_T)$.

5. Initial parameters and force multipliers calculation

Since we are primarily interested in winds from AGN accretion discs, we focus on "typical" values of $\lambda_{\text{bol}}' = 0.1$ and 2.0 and a black hole mass $M = 10^8 M_\odot$. However, as we show later in this section, the properties of the wind, and then the values of $f_{\text{rad}}$, mainly depend on $\lambda_{\text{bol}}'$, rather than on $M$ or $L_{\text{bol}}'$ alone, so our results are applicable regardless of the black hole mass.

We use the bolometric corrections of Lusso et al. (2012) to obtain the 2-10 keV luminosities. We assume a simple powerlaw incident spectrum with photon index $\Gamma = 2$, consistent with the typical values observed in AGNs (Piconcelli et al. 2005; Tombesi et al. 2011), to extrapolate $L_{\text{bol}}$ and $L_{\text{UX}}$.

Regarding the properties of the wind, we concentrate on a set of initial number density $n_0 (\text{cm}^{-3}) \in [10^2, 10^4]$, $r_0 (\text{cm}) \in [5 \cdot 10^1, 5 \cdot 10^2, 10^{24}] \text{cm}^{-2}$. As starting radii we use the same set of values of Sect. 2 and $r_0 \in [5.0, 15.8, 50.0, 158.1, 500.0] r_G$. In our picture, we assume that all the luminosity comes from a point source located at the coordinate origin ($R = 0, z = 0$). However, we note that observationally the X-ray flux is usually ascribed to a hot "corona", comprised within $\sim 10 r_G$ from the SMBH (Chartas et al. 2012; Reis & Miller 2013; Reis et al. 2014; Kara et al. 2016; Caballero-Garcia et al. 2020; Szaniecki et al. 2020), while the UV radiation is due to the disc emissivity which, for a thin disc, has a peak at $\sim 20 r_G$ (Quera-Bofarull et al. 2020). As a result, we expect that in order to code the radiative contribution may not be fully modelled for $R_0 < 50 r_G$; however, we include the cases for $R_0 = 5.0, 15.8 r_G$, since the fate of the wind is governed primarily by $v_0$, rather than by the radiation pressure, as we will show later.

We fix $\alpha$, the exponent regulating the radial dependence of $n$ to 2, so that $n = n_0 (\frac{r}{r_0})^2$, as expected by mass conservation for...
a medium expanding in a spherical geometry. Since we expect a high degree of velocity shear within the wind due to its acceleration, we use a high turbulent velocity $v_{\text{turb}} = 3000 \text{ km s}^{-1}$ to prevent line saturation. This value is consistent with those typically observed in UFOs (see e.g. [Fukumura & Tombesi 2019] and references therein).

We briefly summarise here the range of input quantities of our simulations, from which we calculate a grid of $f_{\text{rad}}$ values:

- $\lambda_{\text{Edd}}$: we divide the interval of interest in four values, logarithmically spaced: $\lambda_{\text{Edd}} = [0.1, 0.5, 1, 2]$.
- $n_0$: we divide the range in logarithmic steps: $\log(n_0/\text{cm}^3) \in [10, 11, 12, 13]$.
- $r_0 \in [5.0, 15.8, 50.0, 158.1, 500.0] r_G$.
- $N_H$: we span the range $[5 \cdot 10^{22}, 10^{24}] \text{ cm}^{-2}$ with steps of $5 \cdot 10^{22} \text{ cm}^{-2}$.

We compute the geometrical thickness of the wind to check whether the $\Delta \theta \ll r$ condition in Eq. [3] is met. The results plotted in Fig. [B.1] (first three panels) in Appendix show that $\Delta \theta / R_0 < 1$ in all the cases. The only exception is for $R_0 = 5 \text{ r}_G$, $\log(n_0/\text{cm}^3) = 10$ when the column density is very high ($N_H > 10^{23} \text{ cm}^{-2}$). However, as we will discuss later, the properties of the wind are quite independent from $N_H$ and we will focus on the typical UFO value of $N_H = 10^{22} \text{ cm}^{-2}$ (Tombesi et al. 2011) in most of the cases. In the last panel of Fig. [B.1] we show the ionisation parameter $\xi(r)$, defined as $\xi = n_0 / n_0^*, \text{ for } \lambda_{\text{Edd}} = 1.0, 0.1$.

This parameter is of great importance since the absorption structure of the wind, and then the values of $f_{\text{rad}}$, mainly depends on it. Our range of $\xi$, from $10^0$ to $10^6$, agrees well with the broad population of UFOs and Warm Absorbers (see e.g. Laha et al. 2014; Serafinelli et al. 2019); this, in turn, justifies our range of $\log(n_0)$. Moreover, our values for $\log(n_0)$ are in agreement with those commonly estimated for the Broad Line Region (BLR) and for UV and X-ray outflows (see e.g. Elvis 2000; Schurch & Done 2007; Saez & Chartas 2011; Netzer 2013). Finally, in Fig. [B.2] we show the values of $f_{\text{rad}}$ as a function of the wind parameters.

5.1 Impact of the initial parameters on the wind dynamics.

We solve the system of Eqs. [2] for the whole grid of initial parameters for an integration time of $10^7 \text{ t}_H$, the same temporal resolution of Sect. [2] and using a set of $v_{0,\text{rot}} \in [1.0, 10^{-1}, 10^{-2}, 10^{-3}] v_{\text{turb}}$. For a complete discussion of the results, we first analyse the impact of the different parameters. To characterise the wind dynamics, we define a wind successfully launched if it has a positive (outbound) velocity at the end of the integration time $t = t_1$, and we compute its terminal velocity as $v_t = v_{\text{out}}(t_1) = \sqrt{v_g(t_1)^2 + v_r(t_1)^2}$.

$\lambda_{\text{Edd}}$ and $v_{0,\text{rot}}$ are the dominant parameters, since they regulate the amount of radiation pressure and the initial velocity of the wind. When $v_{0,\text{rot}} > v_{\text{turb}}$, the high initial velocity allows the wind to be successfully launched for any value of $\lambda_{\text{Edd}}$ (albeit reaching different $v_t$). For $v_{0,\text{rot}} = 10^{-3}, 10^{-2}, 10^{-3} v_{\text{turb}}$, instead, the impact of the initial velocity itself to the wind evolution is almost negligible, and the different solutions are indistinguishable between them. However, $v_{0,\text{rot}}$ lifts the gas above the disk, displacing it from its equilibrium radius and exposing it to the radiation pressure. The fate of the wind will then depend on $\lambda_{\text{Edd}}$ and, secondarily, on $R_0$, but it is unaffected by the exact value of $v_{0,\text{rot}}$. We plot in Fig. [3] the failed wind region (i.e., the radius up to which the wind cannot be successfully launched) as a function of $\lambda_{\text{Edd}}$, for different $v_{0,\text{rot}}$. For $v_{0,\text{rot}} = v_{\text{rot}}$, the wind is always successful, then the failed region increases for decreasing $v_{0,\text{rot}}$ and becomes quite constant for $v_{0,\text{rot}} \leq 10^{-3} v_{\text{turb}}$. Please note that in this Figure we do not take into account wind opacity (i.e., we use the same treatment of Sect. [3] due to the long computational times required. However, the overall behaviour of $v_{0,\text{rot}}$ is similar. For simplicity, from now on we will concentrate only on $v_{0,\text{rot}} = [10^{-2}, 1.0] v_{\text{rot}}$. We note that $v_{0,\text{rot}} = v_{\text{rot}}$ represents a remarkably high starting velocity, which could be justified only under certain particular physical conditions (see discussion in Sect. [7] and is significantly higher from the velocities commonly assumed in the literature, which are closer to the $v_{0,\text{rot}} = 10^{-2} v_{\text{rot}}$ case (see e.g. Proga et al. 2000; Nomura et al. 2016; 2020). As we will detail in the following, we run the simulations using this starting value as a case study, in order to set an upper bound for the wind velocities that can be reached through radiative pressure, once corrected for relativistic effects.

For what concerns $n_0$, it can give rise to differences in $v_t$ of up to 0.05c, but it generally does not affect the overall behaviour of the wind. Since $f_{\text{rad}}$ is always roughly directly proportional to the column density, the wind solutions are also quite independent from $N_H$, because these two terms balance each other in the first term on the right-hand side of Eqs. [3]. We note that this trend holds also for optically-thick winds. In fact, for column densities $\sigma \leq 1.7 \cdot 10^{24} \text{ cm}^{-2}$, line opacity grows equally or less than linearly with $N_H$ (Tombesi et al. 2011), and so the $f_{\text{rad}}/N_H$ term in Eqs. [3] will not contribute more than for the optically-thin wind. We refer to Sect. [C] in the Appendix for further discussions on $n_0, N_H$. From now on we will focus on $\log(n_0/\text{cm}^3) = 11$, $N_H = 10^{23} \text{ cm}^{-2}$, if not stated otherwise.

6. Results

To examine the wind behaviour, we plot in Fig. [4] the trajectories in the $R - z$ plane for $\lambda_{\text{Edd}} = 0.1, 1.0$ (left and right panels, respectively). Hereafter, we convert the distance from the black hole (x-axis) from $r_0$ to $p_0$ assuming $M = 10^8 \text{ M}_\odot$. As discussed in Sect. [5.1] the dominant parameter in the wind motion is $v_{0,\text{rot}}$: for $v_{0,\text{rot}} = v_{\text{rot}}$ (solid lines) the wind is always successful,
while when \( v_{z,0} = 10^{-2}v_{\text{rot}} \) (dashed lines) it can be launched only for \( \lambda_{\text{Edd}} = 1.0 \) and \( R_0 > 5r_G \). In Fig. 4 and in the followings, a truncated trajectory corresponds to a failed wind, since we interrupt the numerical integration when the gas falls back to the disk plane. Classic and relativistic trajectories (represented with bold and thin lines, respectively) are almost indistinguishable; however, as we will see in the following, their velocities are rather different.

In Fig. 5 we show a comparison between the velocities in the relativistic and in the classic treatments (bold and thin lines, respectively) as a function of \( t \), for \( \lambda_{\text{Edd}} = 0.1, 1.0 \) (left and right panel, respectively). Purple, light blue and green lines correspond to \( R_0 = 5.0, 50.0, 500.0r_G \), respectively. Solid(dashed) lines correspond to \( v_0 = 1.0(=10^{-2}v_{\text{rot}}) \). The impact of relativistic effects is remarkable, especially in the highest velocity cases. The maximum \( v_t \) drops from \( \approx 0.6 \) to less than \( 0.3\ c \) when taking into account the reduction of radiative pressure due to special relativity effects. We also note that, in most of the cases, the wind attains its terminal velocity within \( 10^4 t_G \) (corresponding to \( 0.1 \) yr, i.e. roughly a month, for \( M = 10^8 M_{\odot} \)). For \( R_0 = 5r_G \), this time is reduced to \( 10^3 t_G \) (\( 10^{-2} \) yr, i.e. a few days). For comparison, we indicate the times corresponding to one day and one month with vertical dotted lines.

In Fig. 6 we show the velocity of the wind as a function of the distance from the black hole. Line styles are as in Fig. 5. To give an idea of the dimensions of the accretion disc - torus system, we also indicate the typical distance at which BLR are observed and the dust sublimation radius, as a proxy of the inner boundary of the torus. We choose \( 0.01 \ pc \) as the BLR inner radius and \( 0.5 \ pc \) as the dust sublimation radius, which marks the boundary between the BLR and the torus (Coffey et al. 2014, Rożańska et al. 2014, Adhikari et al. 2016, Sturm et al. 2018, Czerny 2019). For a detailed analysis of the wind dynamics, we show in Fig. D.1 in Appendix the case for \( \lambda_{\text{Edd}} = 1, v_{z,0} = v_{\text{rot}} \).

7. Discussion

To have an idea of the overall behaviour of the wind, we plot (Fig. 7) \( v_t \) as a function of \( R_0 \) for \( v_{z,0} = 10^{-2}, 1.0 \ v_{\text{rot}} \) (left and right panel). We also plot with dashed lines \( v_t \) obtained in the classic case. The null values indicate an unsuccessful wind. In order for the wind to attain the typical velocities of UFOs, i.e. \( \geq 0.1c \) (see e.g. Fiore et al. 2017 for a collection of values from the literature), either the luminosity must be very high (\( \lambda_{\text{Edd}} \geq 1.0 \)) or the initial velocity \( v_{z,0} \), must be comparable to the rotational velocity \( v_{\text{rot}} \).

In Fig. 8 we plot \( v_t \), as a function of \( \xi_0 \) (which is a monotonically increasing function of \( R_0 \)) in the densest and in the lightest cases, i.e. \( \log(n_0/cm^3) = 10 \) and \( = 13 \) for \( \lambda_{\text{Edd}} = 0.1 \) and \( = 1.0 \) (left and right panels, respectively). Generally, \( v_t \) is found to be a monotonically increasing function of \( \xi \) (see e.g. Tombesi et al. 2013). Interestingly, this behaviour can be reproduced only with \( v_{z,0} = v_{\text{rot}} \).

We now compare our results with UFOs from the literature. Our goal is to establish whether the observed UFOs velocities can be reproduced within our radiative driving framework. To do so, we consider two different limiting velocities emerging from our results. The first one is the terminal velocity, \( v_t \), which is almost reached by the wind after a very short time, and thus is the most likely to be observed. The second one is the maximum velocity reached by the wind, \( v_{\text{max}} \), which is associated with the short-living, initial phases of the wind motion (see Figs. 5, 6), and hence represents an upper limit of the observable velocity. Since we are interested in the highest possible velocities, we focus on the \( v_{z,0} = v_{\text{rot}} \) cases.
We compute the highest values of $v_r, v_{\text{max}}$ as a function of $\lambda_{\text{Edd}}$ for $R_0 \geq 50.0R_G$, that represents a lower bound for the launching radius of the observed UMOFs (see discussion in Sect. 2). We plot the results in Fig. 9 denoting with dark orange and blue the regions below the curves of $v_r, v_{\text{max}}$, respectively. These regions correspond to the allowed velocity ranges.

We show with different symbols (see legend) the location of several UMOFs reported in the literature (see Sect. 3 in Appendix for references on the single sources). Interestingly, many points lie above the $v_r$ (orange) allowed region, and many also above the $v_{\text{max}}$ (blue) region. Such high velocities, which can be hardly explained within our radiative driving model, may lend support to other launching mechanisms. As discussed in Sect. 5.1, $v_{r,0} = v_{\text{rot}}$ represents an upper bound of the expected launching velocities for a radiatively-driven wind. Lower, physically-motivated $v_{r,0}$ would result in even lower limiting velocities than those reported in Fig. 8. This, in turn, is due to the sub-dominant contribution of the force multipliers (and then of the line driving) with respect to Thompson scattering, as outlined also in Dannen et al. (2019).

Secondly, failed winds (FW) are a natural outcome in any radiative driven scenario, and we expect their presence to be ubiquitous, if the radiation is the main driver. In fact, in our analysis we show that successful winds can be launched only through very high launching velocities ($v_{r,0} \ll v_{\text{rot}}$) or extreme luminosities $\lambda_{\text{Edd}} \gtrsim 1$. However, many AGNs hosting UMOFs have $\lambda_{\text{Edd}} \sim 0.1$ (see Fig. 9), and such high $v_{r,0}$ are very difficult to justify in the framework of a steady-state accretion disc, unless postulating a “kick velocity” through hydrodynamic instabilities (see e.g. Janiuk & Czerny 2011 and references therein), disc magnetic reconnection (Di Matteo 1998; Ergun et al. 2020; Ripperda et al. 2020) or, again, resorting to a large scale MHD-driven outflow (see Yuan et al. 2015 for numerical simulations). Within the dynamics of the accretion-ejection system, we expect the FW to act as a shield for the gas launched at higher $R_0$, possibly regulating its ionisation status and observational properties (Gustin & Proga 2019, 2020). However, we note that the effectiveness of FW in favouring the launching of more distant layers of gas has not been proven yet (Higgsbottom et al. 2014) see discussion in Zappacosta et al. (2020) and references therein). FW are confined into a narrow equatorial region (i.e., their $z$ height is $\ll$ than the radial coordinate $r$, see Fig. 4), since the gravitational attraction prevents them from reaching high altitudes before bouncing back to the accretion disc, making them particularly difficult to observe. A careful modelisation of the wind duty cycle and of the disc region is needed in order to further shed light on this topic.

Finally, we note that our results are robust also in case of X-ray luminosity variability, as observed in several sources (see Fig. 9). Times are converted from $t_G$ to yr assuming $M = 10^8 M_{\odot}$.
Fig. 6: Velocity vs. distance from the black hole for $\lambda_{\text{Edd}} = 0.1, 1.0$ (left and right panel, respectively). Line styles as in Fig. 4. Distances are converted from $r_G$ to pc assuming $M = 10^8 M_{\odot}$.

Fig. 7: Terminal velocities $v_t$ as functions of $R_0$ for different values of $\lambda_{\text{Edd}}$ (colour coding). Solid lines refer to the relativistic treatment, dashed to the classic (non-relativistic) one. In the left panel $v_{z,0} = 10^{-2} v_{\text{rot}}$, in the right panel $v_{z,0} = v_{\text{rot}}$.

e.g. [Nardini et al. 2015; Parker et al. 2017]. As discussed above, for the typical UFO ionisation degrees most of the radiative pressure is channelled through Thompson scattering, rather than line pressure. Thus, the driving luminosity is $L_{\text{bol}}$ (expressed here as $\lambda_{\text{Edd}}$), that significantly varies in AGNs only on timescales larger than tens of years, rather than the X-ray luminosity (expressed through $\lambda_{\text{UX}}$).
8. Conclusion

Special relativity effects strongly reduce the radiative pressure exerted on fast moving clumps of gas, as in the case of UFOs from accretion discs, as well as BAL winds, as discussed in the Introduction. In our work, we carried out an extensive analysis of the radiative driving for a disc wind accounting for these effects. Our main findings can be summarised as follows:

– The dynamics of the wind is primarily governed by the AGN luminosity and the launching velocity $v_{c,0}$. For high luminosity, $\lambda_{Edd} = 1.0$, the wind is successfully launched independently from $v_{c,0}$, while for $\lambda_{Edd} = 0.1$ a higher $v_{c,0}$ of the order of the disc rotational velocity, is required in order to overcome the gravitational attraction from the central black hole (see Fig. 3).

– Shortly after the launch of the wind (between one day and one month, depending on $R_0$), the wind attains a roughly constant velocity $v_t$, which is conserved until the end of the integration time ($10^3 t_G$, i.e. 10yr for a black hole mass of $10^8 M_{\odot}$). After ~1 month, the wind reaches BLR-like distances, possibly suggesting an interaction with the gas in the BLR orbiting above the accretion disc.

– The inclusion of special relativity effects reduces the radiative pressure exerted on the wind. This, in turn, leads to remarkably lower $v_t$ with respect to the classical treatment, up to 50 % less for winds launched at the smallest $R_0$. Within the relativistic treatment, we find an upper limit of $v_t = 0.15 c$ for the highest luminosity case ($\lambda_{Edd} = 1.0$) and a launching radius $\geq 50 r_G$ in agreement with the observed UFO locations.

– Interestingly, we find that most of the UFO velocities from the literature cannot be reproduced within our radiative driving scenario. For the majority of the sources, which have $\lambda_{Edd}$ between 0.03 and 1, the luminosity is too low to reproduce the observed $v_{out}$. This evidence suggests that other acceleration mechanisms are at play. In particular, we suggest the possibility of magnetic driving, which could easily account for the observed $v_{out}$.

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Fig. 9: Comparison between UFO velocities from the literature (dots and squares) and the results of the present work as a function of $\lambda_{Edd}$. Theoretical limit according to the terminal velocity $v_t$ for $R_0 \geq 50 r_G$ corresponds to the orange shaded area. Limit according to the maximum (but short-lived) velocity $v_{\text{max}}$ corresponds to the light blue area. See Sect. 4 in Appendix for a description of the sample and the related references.

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Appendix A: Three-dimensional wind

We show in Fig. A.1 a detailed analysis of the wind trajectories for the preliminary three-dimensional model presented in Sect. 3.

Appendix B: Geometrical and physical properties of the wind

We show in Fig. B.1 (first three panels) the geometrical thickness of the wind. With our density profile $n(r) = n_0 \left(\frac{r}{r_0}\right)^2$ (see Sect. 5), the upper limit for the column density corresponds to $N_{H,\text{max}} = n_0 r_0$. For all the values of $n_0, r_0$ in this paper, $N_{H,\text{max}} > 10^{24} \text{ cm}^{-2}$. The only exception is for $n_0 = 10^{10} \text{ cm}^{-3}, r_0 = 5 r_G$ (first panel, blue line), for which $N_{H,\text{max}} = 7.4 \cdot 10^{23} \text{ cm}^{-2}$. In the last panel of Fig. B.1 we plot $\xi(r)$ for $\lambda_{Edd} = 0.1, 1.0$.

Fig. B.2 shows $f_{\text{rad}}$ as a function of $N_H$, for different $R_0$ (colour coding) and $\log(n_0/\text{cm}^3) = 10, 11, 12, 13$ (from left to right). From top to bottom, $\lambda_{Edd} = 0.1, 0.5, 1.0, 2.0$.

Appendix C: Dependence of the wind dynamics on $n_0, N_H$

To give an idea of the impact of $n_0$ on the wind dynamics, we show in Fig. C.1 the terminal velocity $v_t$ as a function of $R_0$ for different $n_0$ (colour coding). From left to right, $\lambda_{Edd} = 0.1, 0.5, 1.0, 2.0$. Top (bottom) row refers to $v_{z,0} = v_{\text{rot}}(v_{z,0} = 10^{-2} v_{\text{rot}})$. $v_t$ is similar for any value of $n_0$, except for $v_{z,0} = 0.01 v_{\text{rot}}$ and $\lambda_{Edd} = 0.5, 1.0$, where the initial velocity is low enough (and the luminosity is not too low nor too high) so that different $f_{\text{rad}}$ values can give rise to different wind behaviours.

Similarly, in Fig. C.2 we plot $v_t$ for $\log(n_0/\text{cm}^3) = 10, 13$ for the lower and upper values of $N_H$ ($5 \cdot 10^{22}$ and $10^{24} \text{ cm}^{-2}$). It can be seen that the overall dynamics of the wind is weakly sensitive to $N_H$.

Appendix D: Results

We present in Fig. D.1 a detailed analysis of the wind dynamics for $\lambda_{Edd} = 1, v_{z,0} = v_{\text{rot}}$, $\log(n_0/\text{cm}^3) = 11, N_H = 10^{23} \text{ cm}^{-2}$ and taking into account the wind opacity (Sect. 4).

Appendix E: Notes on UFOs sources from literature

We show in Table E.1 the properties of the sources plotted in Fig. 9. The sample is composed of three main groups. The first one is taken from the Tombesi et al. (2011) sample, with the updated $L_{\text{bol}}$ from Fiore et al. (2017), while the second one is from Golfford et al. (2015). The third one comprises the sources reported in Fiore et al. (2017) and not previously reported in Tombesi et al. (2011), together with other individually-reported UFOs published from 2017 on for which robust estimates of both $\lambda_{Edd}$ and $v_{\text{out}}$ are available. Where possible, the black hole mass $M$ and the AGN bolometric luminosity $L_{\text{bol}}$ have been updated with recent works, listed in the last column.
Fig. A.1: Wind trajectories for $v_{z,0} = v_{rot}$ and $\lambda_{Edd} = 1$. From top to bottom and left to right: distance $r$ from the BH (where $r = \sqrt{R^2 + z^2}$) as a function of $t$; outflow velocity $v_{\text{out}}$ as a function of $r$ ($v_{\text{out}} = \sqrt{v_R^2 + v_z^2}$); $v_{\text{out}}$ as a function of $t$; trajectories of the wind in the $z-R$ plane; $v_R$ (radial velocity) as a function of $t$; $v_z$ (vertical velocity) as a function of $t$. Solid(dashed) lines refer to the relativistic(classic) treatment.

Fig. B.1: First three panels: geometrical thickness of the wind as a function of $N_H$ for $\log(n_0) = 10, 11, 12, 13$ (in units of $cm^{-3}$, colour coding) and increasing $R_0$ (from left to right). Last panel: ionisation parameter as a function of $R_0$ for different $\log(n_0)$ (colour coding) and $\lambda_{Edd} = 0.1, 1.0$ (dashed and solid lines, respectively).
Fig. B.2: Values of $f_{\text{rad}}$ as functions of $N_H$ for $\log(n_0) = 10, 11, 12, 13$ (in units of cm$^{-3}$, from left to right) and $\lambda_{\text{Edd}} = 0.1, 0.5, 1.0, 2.0$ (from top to bottom).

Fig. C.1: Terminal velocity of the wind for $\log(n_0) = 10, 11, 12, 13$ (in units of cm$^{-3}$, colour coding) and for different luminosities (from left to right $\lambda_{\text{Edd}} = 0.1, 0.5, 1.0, 2.0$). In the top(bottom) panel $v_{z,0} = v_{\text{rot}}/v_{z,0} = 10^{-2}v_{\text{rot}}$. For simplicity, we fix $N_H = 10^{23}\text{cm}^{-2}$.
Fig. C.2: Terminal velocity of the wind for $\log(n_0) = 10, 13$ (in units of $cm^{-3}$, purple and green lines) and $N_H = 5 \cdot 10^{22}$ and $= 10^{24}$ (in units of $cm^{-2}$, solid and dashed lines). In the top(bottom) panel $v_{z,0} = 5 \cdot 10^{-2}$ and $v_{rot}$. 

Fig. D.1: Wind solutions in the relativistic and classic cases (solid and dashed lines, respectively) for $\lambda_{Edd} = 1$, $v_{z,0} = v_{rot}$ and taking into account the wind opacity. Meaning of the panels as in Fig. A.1.
Table E.1: Sources plotted in Fig. 9. From left to right, columns indicate the number of the group, the source name, $\lambda_{\text{Edd}}$, the UFO velocity $v_{\text{out}}$ (in units of $c$) and the additional references for each source. Group 1: UFO $v_{\text{out}}$ and black hole mass $M$ from Tombesi et al. (2012), $L_{\text{bol}}$ from Fiore et al. (2017). Group 2: values from Gofford et al. (2015). For both groups, $M, L_{\text{bol}}$ have been updated (where possible) with recent values from the literature, see reference column. Group 3: individual sources, see reference column. References: A Peterson et al. (2004), B Ricci et al. (2017), C Bentz & Manne-Nicholas (2018), D Vestergaard & Peterson (2006), E Tilton & Shull (2013), F Kelly & Bechtold (2007), G Caglar et al. (2020), H Chatterjee et al. (2011), I Ricci et al. (2017), L Nardini & Zubovas (2018), M Feruglio et al. (2015), N Nardini et al. (2015), O Tombesi et al. (2015), P Reeves & Braito (2019), Q Smith et al. (2019), R Onori et al. (2017), S Laurenti et al. (2020), T Chartas et al. (2009), U Saturni et al. (2018), V Braito et al. (2018).

| Group | Name               | $\lambda_{\text{Edd}}$ | $v_{\text{out}} (c)$ | Refs. |
|-------|--------------------|-------------------------|----------------------|-------|
| 1     | NGC4151            | 0.05 ± 0.01             | 0.106 ± 0.007        | A     |
|       | IC4329A            | 0.08 ± 0.03             | 0.098 ± 0.004        |       |
|       | Mrk509             | 0.09 ± 0.01             | 0.173 ± 0.004        | A     |
|       | Mrk509             | 0.14 ± 0.01             | 0.138 ± 0.004        | A     |
|       | ARK120             | 0.17 ± 0.02             | 0.29 ± 0.02          | A     |
|       | Mrk79              | 0.08 ± 0.01             | 0.092 ± 0.004        | B     |
|       | NGC4051            | 0.07 ± 0.01             | 0.04 ± 0.02          | B     |
|       | Mrk766             | 0.19 ± 0.02             | 0.082 ± 0.006        | C     |
| 2     | Mrk766             | 0.30 ± 0.03             | 0.088 ± 0.002        | C     |
|       | Mrk841             | 0.02 ± 0.00             | 0.06 ± 0.02          | D     |
|       | 1H0419-577         | 0.24 ± 0.04             | 0.079 ± 0.007        | E     |
|       | Mrk290             | 0.19 ± 0.02             | 0.16 ± 0.02          |       |
|       | Mrk205             | 0.16 ± 0.10             | 0.100 ± 0.004        | F     |
|       | PG1211+143         | 0.17 ± 0.03             | 0.151 ± 0.003        | D     |
|       | MCG-5-23-16        | 0.09 ± 0.02             | 0.116 ± 0.004        | G     |
|       | MCG5407            | 0.79 ± 0.54             | 0.20 ± 0.02          |       |
| 3     | 3C111              | 0.02 ± 0.01             | 0.07 ± 0.04          | H     |
|       | 3C3903             | 0.09 ± 0.02             | 0.145 ± 0.007        | A     |
|       | 4C+74.26           | 0.04 ± 0.00             | 0.18 ± 0.03          |       |
| 2     | ESO103-G035        | 0.13 ± 0.03             | 0.06 ± 0.03          |       |
|       | MR2251-178         | 0.16 ± 0.03             | 0.137 ± 0.008        |       |
|       | Mrk279             | 0.03 ± 0.00             | 0.220 ± 0.006        | B     |
|       | NGC5506            | 0.28 ± 0.05             | 0.246 ± 0.006        | I     |
|       | SQJ2127            | 0.16 ± 0.00             | 0.231 ± 0.006        |       |
| 3     | Mrk231             | 0.17 ± 0.03             | 0.067 ± 0.008        | L,M   |
|       | PDS456             | 0.46 ± 0.15             | 0.25 ± 0.01          | N     |
|       | Iras 11119         | 0.65 ± 0.19             | 0.26 ± 0.01          | L,O   |
| 3     | I Zwicky 1         | 0.85 ± 0.17             | 0.27 ± 0.01          | P     |
|       | Iras 05189         | 1.30 ± 0.27             | 0.110 ± 0.010        | Q,R   |
|       | PG1448             | 0.76 ± 0.077            | 0.150 ± 0.008        | S     |
|       | APM08279           | 0.40 ± 0.30             | 0.36 ± 0.02          | T,U   |
|       | MCG-03-58-007      | 0.20 ± 0.07             | 0.20 ± 0.01          | V     |