Compact high-redshift galaxies are the cores of the most massive present-day spheroids

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ABSTRACT

Observations suggest that the effective radii of high-redshift massive spheroids are as much as a factor of ∼6 smaller than low-redshift galaxies of comparable mass. Given the apparent absence of low-redshift counterparts, this has often been interpreted as indicating that the high-density, compact red galaxies must be ‘puffed up’ by some mechanism. We compare the ensemble of high-redshift observations with large samples of well-observed, low-redshift ellipticals. At the same physical radii, the stellar surface mass densities of low- and high-redshift systems are comparable. Moreover, the abundance of high surface density material at low redshift is comparable to or larger than that observed at z > 1–2, consistent with the continuous buildup of spheroids over this time. The entire population of compact, high-redshift red galaxies may be the progenitors of the high-density cores of present-day ellipticals, with no need for a decrease in stellar density from z = 2 to 0. The primary difference between low- and high-redshift systems is thus the observed low-density material at large radii in low-redshift spheroids (rather than the high-density material in high-redshift spheroids). Such low-density material may either (1) assemble at z < 2 or (2) be present, but not yet detected, at z > 2. Mock observations of low-redshift massive systems suggest that the amount of low-density material at high redshifts is indeed significantly less than that at z = 0. However, deeper observations will be important in constraining the exact amount (or lack thereof) and distribution of this material, and how it builds up with redshift. We show that, without deep observations, the full extent of such material even at low redshifts can be difficult to determine, in particular if the mass profile is not exactly a single Sersic profile. We discuss the implications of our results for physical models of galaxy evolution.

Key words: galaxies: active – galaxies: elliptical and lenticular, cD – galaxies: evolution – galaxies: formation – cosmology: theory.

1 INTRODUCTION

Recent observations suggest that high-redshift spheroids may have significantly smaller effective radii than low-redshift analogues of the same mass (e.g. Daddi et al. 2005; Trujillo et al. 2006a, 2007; Toft et al. 2007; van Dokkum et al. 2008; Franx et al. 2008; van der Wel et al. 2008; Cimatti et al. 2008; Buitrago et al. 2008). The apparent differences are dramatic: the inferred effective radii are as much as a factor of ∼6 smaller at fixed stellar mass in the most massive galaxies at z = 2. Whatever process explains this apparent evolution must be particular to this class of galaxies: disc galaxies are not similarly compact at high redshift (Ferguson et al. 2004; Ravindranath et al. 2004; Barden et al. 2005; Somerville et al. 2008). As such, these observations represent a strong constraint on models of galaxy and bulge formation.

Relative to the abundance of massive galaxies today, there are not a large number of compact systems at high redshift. However, even if just ∼10 per cent survived intact to z = 0, this would greatly exceed the observed number density of such systems in the local Universe (Trujillo et al. 2009). In fact, at a fixed stellar mass, ellipticals with older stellar populations appear to have the largest radii (Gallazzi et al. 2006; Bernardi et al. 2007; Graves, Faber & Schiavon 2009; van der Wel et al. 2009).

The challenge for both observations and models is therefore to understand how these high-redshift systems could evolve to become ‘typical’ spheroids today. Their masses, number densities and

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clustering dictate that they are the progenitors of the most massive ellipticals and brightest cluster galaxies (BCGs) today (Hopkins et al. 2007c; Quadri et al. 2007). These systems have much larger $R_e$ and thus have lower effective densities $\Sigma_{\text{eff}} = M(<R_e)/(\pi R_e^2)$. However, this does not necessarily mean that the physical densities are lower than those of the high-redshift systems. One way to increase $R_e$ would be to uniformly ‘puff up’ the profiles, lowering the physical density everywhere. This would imply that the central densities of massive high-redshift ellipticals would need to decrease by two orders of magnitude from $z = 2$ to 0. Alternatively, $R_e$ can change by just as much by adding a relatively small amount of mass at low surface densities and large radii, without affecting the central density at all. In other words, an evolving effective density does not necessarily imply an evolving physical density at all radii.

Buildup of an ‘envelope’ of low-density material is expected as massive early-forming galaxies undergo late-time (major and minor) gas-poor mergers with later-forming, less dense ellipticals, discs and dwarfs (Gallagher & Ostriker 1972; Ostriker & Tremaine 1975; Hausman & Ostriker 1978; Weil & Hernquist 1994; Weil & Hernquist 1996; Naab et al. 2007). This is a relatively efficient channel for size–mass evolution, yielding a factor of several size evolution with only a factor of 1.5–2 increase in stellar mass (Hopkins et al. 2009d). But this less dense material added at large radii does not significantly affect the high-density core,1 and so these models predict that the dense, high-redshift systems should survive to become the central regions of (some fraction of) today’s massive ellipticals.

If, on the other hand, high-redshift systems evolved primarily by equal-mass dry mergers between equivalently dense spheroids, then this will ‘inflate’ the profiles relatively uniformly. In this extreme case, effective radii and stellar mass both approximately double in the merger; high-redshift systems would be uniformly more dense than their low-redshift descendants (see e.g. Hernquist, Spergel & Heyl 1993; Boylan-Kolchin, Ma & Quataert 2006).

Distinguishing between these possibilities, as well as other dynamical, stellar evolution, or observational effects that could lead to apparent size–mass evolution, clearly depends on understanding in detail differences in the surface density profiles of spheroids as a function of radius, at low and high redshifts. In this paper, we quantitatively compare low- and high-redshift observations to constrain these scenarios and inform how systems are evolving from $z \gtrsim 2$ to ~0.

In Section 2, we directly compare the observed profiles of high- and low-redshift massive spheroids, and show that, at the same physical radii, their stellar surface mass densities are comparable. The massive, high-redshift systems appear no different than the ‘cores’ of today’s massive ellipticals. In Section 3, we determine the distribution of maximum/central densities, and show that this has not evolved significantly from $z = 0$ to $z > 2$. In Section 4, we calculate the mass function (and global mass density) of these high-density ‘cores’ at both low and high redshifts. This allows us to quantitatively compare the abundance of high-density material observed at both low and high redshifts. We show that there is as much or more high-density material in the cores of massive spheroids at $z = 0$ as is observed to be in place at $z = 1$–2. The difference between low- and high-redshift systems, we conclude, lies in the lack of observed low surface density envelopes around the high-redshift systems. In Section 5, we show that, although such envelopes are weaker at high redshifts, some caveats should be borne in mind with respect to the determination of the mass in low-density material in high-redshift spheroids. We summarize our results and discuss their consequences for physical models of spheroid evolution in Section 6.

Throughout, we assume a WMAP (Wilkinson Microwave Anisotropy Probe) cosmology ($\Omega_M = 0.27$, $\Omega_\Lambda = 0.73$, $h = 0.705$; Komatsu et al. 2009), but the exact choice makes no significant difference.

## 2 SURFACE DENSITY PROFILES OF ELLIPTICALS AT HIGH AND LOW REDSHIFTS

Fig. 1 shows a direct comparison of the observed surface stellar density profiles of high-redshift compact galaxies and low-redshift massive galaxies. At low redshift, we compile observed surface brightness profiles from Kormendy et al. (2008) and Lauer et al. (2007); this consists of a total of ~180 unique local ellipticals with nuclear Hubble Space Telescope (HST) observations and ground-based data at large radii (allowing accurate surface brightness profile measurements from ~10 pc to ~50 kpc).2 The isophotaly averaged major-axis profiles are measured in rest-frame optical; we convert to a stellar mass profile based on the measured total stellar masses and the assumption of a radius-independent stellar mass-to-light ratio. Conversion to stellar mass profiles using, for example, colour or stellar population gradients and comparison of profiles from different instruments and wavebands in these samples are discussed extensively in Hopkins et al. (2009a) and Hopkins, Cox & Hernquist (2008a); the differences are much smaller than the scatter between individual profiles, and do not affect our conclusions. In Fig. 1, we restrict our comparison to massive galaxies with $M_* > 10^{11} M_\odot$ because these systems are most likely to be descendants of massive high-redshift galaxies. The Kormendy et al. (2008) sample is a volume-limited survey of the Virgo spheroid population; as such it includes few very massive galaxies ($M_* > 3 \times 10^{11} M_\odot$). The Lauer et al. (2007) galaxies are chosen to be the representative of massive ellipticals in the local Universe, including more massive systems up to a couple $10^{12} M_\odot$. At the masses of interest, both are representative of the distribution of spheroid sizes in the local Sloan Digital Sky Survey (SDSS) galaxy sample (Shen et al. 2003).

Fig. 1 compares the low-redshift sample with the observed, point spread function (PSF) de-convolved profiles of nine high-redshift compact massive galaxies ($M_* \gtrsim 10^{10} M_\odot$, $R_e \sim 1$ kpc), specifically the $z \sim 2$–3 sample from van Dokkum et al. (2008). This is a well-studied sample that represents the extreme of implied size evolution: the inferred average $R_e$ is a factor of ~3 smaller than local spheroids of the same mass. Fig. 1 shows the best-fitting Sersic profile of each galaxy in the sample; stellar mass-to-light ratios are determined by assuming a radius-independent $M_*/L$ and normalizing the observed portion of the profile to the total stellar mass

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1 By ‘core’, we refer to the central regions of the galaxy, not to any specific class of central profile slopes. We use the phrases ‘cusp ellipticals’ or ‘core ellipticals’ to distinguish these.

2 Note that although the composite (HST+ground-based) profiles were used in Lauer et al. (2007) to estimate effective radii, they were not actually shown in the paper.

3 Stellar masses for all objects are determined from the combination of rest-frame optical and near-IR photometry, corrected to an assumed Chabrier (2003) IMF. We refer to Hopkins et al. (2009a) and Kriek et al. (2008b) for details of the low and high-redshift samples, respectively. Varying the specific bands used to determine stellar masses makes little difference, and changing the IMF will systematically change the stellar masses of all objects considered, but will not change our comparisons.
Figure 1. Direct comparison of the (major-axis) surface stellar mass density profiles of $z \gtrsim 2$ compact massive spheroids ($M_\star \sim 10^{11} M_\odot$, best-fitting $R_e \sim 1$ kpc; red dashed) and local, massive ellipticals ($M_\star \gtrsim 10^{11} M_\odot$, $R_e \gtrsim 4$–5 kpc; solid). Both $\Sigma$ and $R$ are in physical units. The high-$z$ profiles are the PSF de-convolved fit, plotted over the observed range in radius given the best-case limitations in seeing and surface brightness (from van Dokkum et al. 2008). The low-$z$ profiles combine space and ground-based photometry to obtain very large dynamic range: they are from the Kormendy et al. (2008) Virgo elliptical sample (left-hand panel) and the Lauer et al. (2007) local massive elliptical sample (right-hand panel). The former is a volume-limited sample, so it contains fewer, very massive galaxies with high central surface brightness. Although the high-$z$ systems have much smaller $R_e$, their densities at any physical radius are not unusual compared to the local objects: the central $\sim 1$–2 kpc of massive ellipticals today are just as dense. The difference in $R_e$ owes to the presence of the large wings/envelopes at low surface density in the low-redshift objects.

determined from photometry and spectroscopy in Kriek et al. (2006, 2008a,b) We plot the profile of each system over the maximum radial range observed: from the scale of a single pixel at the observed redshift to the limiting surface brightness depth of the best images. Both the low- and high-redshift systems are plotted in terms of major-axis radii (a non-negligible correction). At low redshift, the stellar mass-to-light ratios of ellipticals appear to be nearly independent of radius (reflected in, for example, their observed weak colour gradients), but the stellar mass-to-light ratio may depend significantly on radius in the high-redshift systems (Trager et al. 2000; Côté et al. 2006; Sánchez-Blázquez et al. 2007). However, based on the observed stellar population gradients in local ellipticals, the observed ages/colours of the high-redshift systems, or the outcomes of numerical simulations, the expected variation in $M_\star / L$ is such that a young, recently formed post-starburst stellar population at the centre of the high-redshift galaxy will have higher $L/M_\star$ than older stars at larger $R_e$ (see e.g. Hopkins et al. 2008b). This would make the high-redshift systems less dense than we assume here; we conservatively allow for the maximal stellar mass densities in those systems.

The comparison in Fig. 1 is quite striking: although the best-fitting effective radii and effective surface densities of the high-redshift systems are quite different from their low-redshift analogues, the actual stellar surface mass densities at any given observed radius do not appear significantly higher than a substantial fraction of the low-redshift population. In other words, inside the same observed radii $\sim 1$–5 kpc, many of today’s massive ellipticals are just as dense as the high-redshift systems. The difference in effective radius stems primarily from the fact that the low-redshift systems have substantial extended wings/envelopes of low surface brightness material ($\Sigma \ll 10^9 M_\odot$ kpc$^{-2}$); by contrast, the inference from fitting the high-redshift systems is that their profiles fall more rapidly at large radii (as we discuss further below).

For the sake of comparison with these and future high-redshift observations, it is useful to define the “upper envelope” of low-redshift galaxy density profiles. Formally, we can take e.g. the $+1\sigma$ $\approx 86$ per cent contour of the combined sample of density profiles shown in Fig. 1, but we find that this can be conveniently approximated with a simple Sersic function. This envelope is approximately given by

$$\Sigma_{1\sigma}(z = 0) = 4.5 \times 10^{12} M_\odot \text{kpc}^{-2} e^{-11.67 \left(\frac{R}{R_e}\right)^{1/6}}.$$  

(1)

This is a Sersic profile with $n_e = 6$, $R_e = 40$ kpc, and total stellar mass $M_\star = 1.7 \times 10^{12} M_\odot$. Note that most single galaxies do not remain along this envelope over its entire extent. Rather, at each radius, this represents the $+1\sigma$ upper extent of observed densities within the spheroid population (i.e. the most dense systems at each radius); most individual systems approach it over some more limited dynamic range. This is a useful comparison quantity in particular because, although the median profiles of $z = 0$ ellipticals are well-known, there has been relatively little parameterization of the scatter in profile shapes. Thus, even if high-redshift ellipticals are more dense than the median system today, if they do not exceed the relation given by (1), then their densities can be accommodated within some portion of the present-day spheroid population, so long as they do not represent a large fraction of the present-day abundance of spheroids. As expected, we find that at their centers, the $z = 2$ systems are at most comparable to this upper envelope, i.e. comparable to the most dense $z = 0$ spheroid cores, and at large radii, they fall well below the envelope.

3 CENTRAL STELLAR DENSITIES

Fig. 2 plots the peak surface stellar mass densities $\Sigma_{\text{peak}}$ obtained in both the low- and high-redshift galaxy populations. The ‘maximum’ or peak surface density must be defined within some radius, for galaxies whose surface density continues to rise to unresolved radii (e.g. cusp ellipticals; although most of the local massive galaxies are core ellipticals, with relatively flat maximum surface densities within $\sim 50$–500 pc). For example, the maximum stellar surface
Density can be defined as the average $\Sigma$ interior to some fixed small radius $\sim 50 – 100$ pc, or a fixed fraction of $R_e$ from $\sim 0.02$ to $0.04$, or by extrapolation to $R = 0$ of a best-fitting Sersic profile – we are simply interested in comparing the central densities at small radii in both low- and high-redshift systems. For each determination, we find qualitatively similar results albeit with some small normalization differences; Fig. 2 shows $\Sigma_{\text{peak}}$ determined from averaging within 50 pc and within 0.02 $R_e$. For the high-redshift systems, PSF and seeing effects smear out the maximum observed surface brightness/density inside $\sim 1$ kpc; we extrapolate the best-fitting Sersic profiles inwards to the same radii as the local systems. Making this same approximation in the low-redshift samples shows that it is reasonable, but tends to slightly overestimate the central surface density, especially in core ellipticals.

At both low and high redshifts, there is a characteristic maximum central surface stellar mass density $\sim 0.3 – 2 \times 10^{11} M_\odot$ kpc$^{-2}$, with significant, but still surprisingly little scatter given the known diversity in the profile shapes of ellipticals (e.g. variation in Sersic indices and cusp versus core populations). The maximum is similar whether we include ellipticals of all masses ($\sim 10^9 – 10^{12} M_\odot$), or restrict to cusp or core populations; although dry mergers are expected to transform cusp ellipticals into core ellipticals via ‘scouring’ (ejecuting mass from the central regions in a BH–BH merger), this primarily affects the mass profile on very small scales (comparable to or less than the scales here – well below what we generally refer to as the ‘central’ regions of ellipticals at $\sim$ kpc scales). The maximum surface density of the high-redshift systems is perhaps a factor of $\sim 2$ larger than that of low-redshift systems, but given that we are extrapolating Sersic profiles inwards for the high-redshift systems, this is probably an upper limit. Thus, while the observations imply up to a factor of $\sim 40$ evolution in effective surface brightness, there is nowhere near this much evolution in the true maximum stellar surface density, a much more physically relevant quantity.

Recently, Bezanson et al. (2009) reached to very similar conclusions from a similar comparison between high- and low-redshift profiles, using a different methodology and low-redshift sample. One subtle difference between our conclusions and theirs is that they claim the central densities of the high-redshift systems appear higher, on average, than those at low redshifts by a small factor ($\sim a$ couple). This owes largely to the fact that the authors extrapolate the best-fitting Sersic profiles inwards to small radii – as we show here, this does lead to slightly higher central densities. But, we caution that, doing the same in the low-redshift systems, we would obtain similar slightly higher densities: over the observed range (Fig. 1), there is no difference. Moreover, Bezanson et al. (2009) compare the high-redshift profiles only with the average profile of similar-mass galaxies at low redshift; in Fig. 1 and Section 4, we consider the full distribution of profile shapes at low redshift: even if the high-redshift systems have, on average, slightly higher central densities, they are still compatible with the central densities of a large fraction of the $z = 0$ massive elliptical population.

It is worth noting that the mass and redshift independence in $\Sigma_{\text{peak}}$ in Fig. 2 is somewhat surprising, given the diversity of formation histories and scatter in, for example, the mass present at larger radii (see e.g. Hopkins, Murray & Thompson 2009c). A more detailed discussion of this will be the subject of future work, but it may relate to the maximum surface density of gas that can turn into stars (see Section 6).

### 4 The Mass at High Stellar Densities

We now quantify the amount of mass at different stellar surface densities. In order to reduce the effects of noise and PSF effects (important in particular for the high-redshift systems), we define the surface density in this section as the average surface density within each radius, i.e. $\Sigma(R) = (\Sigma(<R)) = M_*(<R)/\pi R^2$. We obtain similar results using the local $\Sigma$, but with larger noise. For each observed system in our low-redshift sample, given the stellar mass profile (Fig. 1), we calculate the total fraction of the stellar mass that lies above a given threshold in surface density $\Sigma_{\text{min}}$. We evaluate this for each system separately, and in Fig. 3 we plot the average mass fraction at each $\Sigma$ for all observed systems in our sample, in several bins of total stellar mass. Although the mass fraction above

**Figure 2.** Distribution of peak (maximum) spheroid stellar mass surface densities. Left-hand panel: low-$z$ systems from Fig. 1. Most ellipticals, at any mass, have $\Sigma_{\text{peak}} \sim 0.3 – 1 \times 10^{11} M_\odot$ kpc$^{-2}$, Histograms show two different calculations of $\Sigma_{\text{peak}}$ (within 50 pc and $R_e/50$); dotted lines are the median from each. Right-hand panel: same, for the high-$z$ samples. Direct observations are PSF and seeing-limited, so we extrapolate the best-fitting Sersic profile inwards to obtain $\Sigma_{\text{peak}}$ (this is typically an upper limit in the low-$z$ samples). The results are striking: central densities are reasonably independent of redshift.
Figure 3. Average mass fraction above some threshold surface stellar mass density $\Sigma_{\text{min}}$, for the low-$z$ sample from Fig. 1. The values shown are the average fraction of all spheroid mass (in a narrow range around each $M_*$) above the given $\Sigma_{\text{min}}$. A significant fraction of the $z = 0$ spheroid mass ($\sim 25$ per cent) resides in matter at the inferred effective $\Sigma$ of the high-$z$ compact systems ($10^{10} M_\odot$ kpc$^{-2}$).

Figure 4. Spheroid stellar mass function (number density) for mass above a given surface stellar mass density threshold ($\Sigma_{\text{min}}$). We calculate the $z = 0$ mass function of spheroids including only stellar material in any galaxy above the given $\Sigma_{\text{min}}$, given the total stellar mass function and the observed distribution of profile shapes. The magenta dotted line shows the total spheroid mass function (Bell et al. 2003) – most of the mass is accounted for above $10^{10} M_\odot$ kpc$^{-2}$. The value of $\Sigma_{\text{min}} = 10^{10} M_\odot$ kpc$^{-2}$ corresponds to the effective surface density of the compact high-redshift spheroids; points show the results of the same calculation for the observed high-redshift systems and this value of $\Sigma_{\text{min}}$. We show this for the $z \sim 2.3$ data from van Dokkum et al. (2008, black circles) and $z \sim 1$ data from van der Wel et al. (2008, triangles).

Unsurprisingly, Fig. 4 shows that at lower $\Sigma$ thresholds the predicted mass function converges to the total stellar mass function of spheroids, i.e. most stellar mass is accounted for. Moreover, at high thresholds it drops rapidly, especially at high masses: $10^{11} M_\odot$ kpc$^{-2}$ is the peak surface density inside $< 1$ kpc at both low and high redshifts – no observed systems have significant amounts of mass $> 10^{12} M_\odot$ above this threshold.

In Fig. 4, we compare the $z = 0$ volume density of mass at $\Sigma > 10^{10} M_\odot$ kpc$^{-2}$ (solid lines) with observational inferences at $z = 1$ (diamonds) and $z = 2$ (circles). Specifically, given the total number density of $> 10^{10} M_\odot$ spheroids/compact red systems at these redshifts (Pérez-González et al. 2008b), convolved with the distribution of profile shapes from van Dokkum et al. (2008), we obtain the number density of objects with mass above the relevant $\Sigma$ threshold. In the error budget in Fig. 4, we include the difference in number densities estimated by Fontana et al. (2006), van Dokkum et al. (2006) and Marchesini et al. (2008), and variation in the distribution of profile shapes/sizes fitted in other works, including Trujillo et al. (2007), Toft et al. (2007), Buitrago et al. (2008), Cimatti et al. (2008). These yield similar conclusions to within a factor of 10.
factor of \(~2\sim3\). At the masses of interest, the observations should be reasonably complete to these high surface densities.

We can also integrate the mass functions in Fig. 4 to obtain the total volume density of stellar mass in spheroids above some threshold in surface density \(\Sigma_{\text{min}}\); this is shown in Fig. 5. Whereas mergers will not conserve number density, they should conserve total stellar mass in this calculation (to the extent that they do not change the \(\Sigma_{\text{min}}\) of the central regions of galaxies). Since the high-redshift systems are primarily massive, \(>10^{11} \, M_\odot\), and their descendants cannot presumably be of much lower mass, we restrict this calculation to only systems with a total stellar mass above this limit (although this only removes the very lowest mass contributions to the high-\(\Sigma\) population in Fig. 4, and does not substantially affect our comparison). We then calculate, in systems above this mass, the total stellar mass above each threshold \(\Sigma_{\text{min}}\).

Fig. 5 shows that there is \(\sim4 \times 10^9 \, M_\odot \, \text{Mpc}^{-3}\) of stellar mass in \(>10^{11} \, M_\odot\) ellipticals, above a surface density threshold of \(\Sigma > 10^{10} \, M_\odot \, \text{kpc}^{-2}\) in the local Universe. This is comparable to the total stellar mass density of high-redshift red spheroids (Labbé et al. 2005; van Dokkum et al. 2006; Abraham et al. 2007; Grazian et al. 2007). Convolving over the observed size distribution at \(z \sim 2\), the mass density above this threshold \(\Sigma\) is of course lower, \(\sim1\sim2 \times 10^9 \, M_\odot \, \text{Mpc}^{-3}\). We obtain a similar result comparing to the \(z = 1\) observations from van der Wel et al. (2008), with the relevant constraints being at lower surface density as there is less relative evolution.

Our comparisons indicate that the local Universe contains just as much, or more, stellar mass at high surface densities as implied by observations of high-redshift systems. It is thus possible that all of the high stellar mass density systems at high redshift can be incorporated into massive ellipticals today, without any conflict with their observed number densities or surface brightness profiles. In fact, a reasonable amount of high surface density material must continue to be added to the elliptical population, perhaps by gas-rich mergers, from high redshifts until \(z = 0\). It is the subject of another study whether gas-rich mergers produce an adequate amount of high-\(\Sigma\) stellar mass in current galaxy formation models to account for the observed growth of \(\rho_*\) in Fig. 5. None the less, the high-density material at high redshifts is not inconsistent with the \(z \sim 0\) data and therefore does not have to ‘go away’.

5 THE MASS AT LOW STELLAR DENSITIES

Our results demonstrate that the difference between low- and high-redshift spheroids does not arise in their central densities, but in the large envelopes of low surface brightness material observed in low-redshift systems. This is the origin of their larger effective radii.

There are two natural ways of reconciling the low- and high-redshift observations with the hypothesis that the high-redshift spheroids are the progenitors of today’s ellipticals. First, the high-redshift systems may not have much low-density material at large radii; low-density material would then have to be accreted at lower redshifts via late-time mergers (minor or major) with gas-poor discs and ellipticals (i.e. lower-density systems). Such a scenario is feasible, and indeed expected – if the initial spheroid-forming mergers are sufficiently gas-rich, there will be little low-density material from extended stellar discs to contribute to an extended envelope (Hopkins et al. 2009a). Moreover, comparison of clustering properties, merger rates and stellar populations all imply that these massive, high-redshift systems should grow by a factor of \(\sim1\sim2\) via these channels between \(z \sim 2\) and \(0\), more or less sufficient to account for the envelopes seen in Fig. 1 (see e.g. van Dokkum 2005; Bell et al. 2006; Zheng, Coil & Zehavi 2007; Lin et al. 2008; Consroy & Wechsler 2009).

The second way of reconciling the low- and high-redshift observations is that high-redshift systems do already have material at low surface densities, but it is not seen in present observations (in such a case, there would be much less than expected buildup of low-density material). In order to be as conservative as possible, in considering the possible degree of envelope buildup since high redshifts, we consider this possibility here.

Fig. 6 illustrates circumstances under which the high-redshift observations may not be sensitive to extended, low-\(\Sigma\) wings. We consider a few representative galaxy profiles from the local sample of Kormendy et al. (2008), ranging from low-mass cusp ellipticals with low Sersic indices at large radii (steep surface density falloff) to high-mass core ellipticals with high Sersic indices at large radii (extended envelopes).\(^5\) For each, we convolve the observed profile with a simple Gaussian PSF with typical best-case resolution for the high-redshift observations of interest (\(\sigma = 0.5 \, \text{kpc}\); full width at half-maximum (FWHM) 1.2 kpc). We then fit the (one-dimensional) profile to a single Sersic profile (fitting appropriately convolved model profiles). We do this as a function of image depth.

\(^5\)The specific five galaxies shown are (from top to bottom) NGC 4464, NGC 4515, NGC 4473, NGC 4365 and NGC 4552. The first three are classified as cusp ellipticals, and the latter two as core ellipticals. The observations are described in Kormendy et al. (2008), but typically include ~80–100 photometric points from a few pc to ~50 kpc in radii; photometric errors are \(\lesssim 0.04 \, \text{mag arcsec}^{-2}\) (not visible in Fig. 6). They have stellar masses of \(M_* = (0.17, 0.13, 1.2, 3.9, 2.0) \times 10^{10} \, M_\odot\), true effective radii \(R_e\) – fit from the data with proper multi-component profiles – of \(R_e = (0.60, 1.05, 3.19, 14.6, 10.6) \, \text{kpc}\) and central velocity dispersions of \(\sigma = (120, 90, 192, 271, 252) \, \text{km s}^{-1}\). Fitting their outer profile shapes to Sersic profiles (where they are uncontaminated by the central, high surface density components; see e.g. Hopkins et al. 2009a; Hopkins et al. 2009d) yields best-fitting outer Sersic indices of \(n_e = (2.1, 3.9, 4.6, 7.1, 9.2)\).
Figure 6. Best-fitting light profile parameters $R_e$ and $n_s$ versus image depth. Left-hand panel: observed (V-band) surface brightness profiles (black) for several typical local spheroids in the Kormendy et al. (2008) sample from low mass (low-$n_s$, i.e. steep light profile decay; top) to high mass (high-$n_s$, i.e. shallow decay/large envelope; bottom). These are compared to the profiles constructed from mock images of the same objects with best-case imaging available at $z \sim 0.5–2$ (cyan diamonds; seeing/PSF FWHM of 1.2 kpc, and depth/dynamic range of $\mu_{\text{max}} - \mu_{\text{min}} = 4.5$ mag; arrows in bottom-left panel). Dotted cyan line shows the best-fitting (convolved) Sersic profile fit to the mock high-$z$ imaging data, extrapolated to large radii. Centre: effective radii of the best-fitting Sersic profile, relative to the true $R_e$, as a function of image depth. We construct a series of mock profiles with similar PSF, seeing, noise and pixel size (as left-hand panel), but vary the image depth $\Delta \mu = \mu_{\text{max}} - \mu_{\text{min}}$. We fit the resulting mock profile (with each $\Delta \mu$) with either a free Sersic index $n_s$ (red diamonds) or fixed $n_s = 4$ (black circles). Dotted vertical line shows the $\Delta \mu$ of the mock profile at left. Right-hand panel: corresponding best-fitting $n_s$ (for free-$n_s$ fits). At low masses (little stellar envelope), there is little dependence on the image depth. At high masses (large-envelope systems), a strong trend appears, because the $z = 0$ profiles of massive galaxies are fundamentally not well-described over a large dynamic range by single Sersic laws. At small $R \lesssim 2–10$ kpc ($\Delta \mu \sim 2–4$), the radii that dominate the fit in all but the deepest local imaging data, the profiles show a steeper falloff (indicative of $n_s \lesssim 4$, weak-envelope profiles) and yield a smaller best-fitting $R_e$. Only at $R \gtrsim 20–50$ kpc ($\Delta \mu \sim 6–8$) do the low-density wings appear, leading to larger $n_s$ and $R_e$.

Specifically, we plot the results of the fits as a function of $\Delta \mu = \mu_{\text{max}} - \mu_{\text{min}}$, the surface brightness (mag arcsec$^{-2}$) of the deepest point included relative to the central/maximum surface brightness of the convolved image. In Fig. 6, we plot the resulting best-fitting effective radii, considering both fits with a free Sersic index $n_s$ and a fixed $n_s = 4$. For fits with a free $n_s$, we plot the corresponding best-fitting $n_s$.

For low- and intermediate-mass galaxies, which have low $n_s$ and therefore fall off steeply in $\Sigma$ at large $R$, the true profiles can be recovered with even relatively shallow observations. If anything, for the lowest mass galaxies, which have Sersic profile indices $n_s \sim 2–3$ (when fit in this manner to a single Sersic index; see e.g. Ferrarese et al. 2006; Balcells, Graham & Peletier 2007a,b), the effects of the PSF tend to slightly increase the inferred effective radius in shallow images. For systems very close to $n_s = 4$, characteristic of intermediate-mass galaxies, there is almost no depth-dependent bias to the inferred $R_e$ and $n_s$ (see NGC 4515 in Fig. 6). The same conclusions are reached in the analysis of mock-redshifted SDSS images of low-mass galaxies in van der Wel et al. (2008). In short, there is no strong low surface brightness envelope, whether or not the low surface brightness data are well-observed makes little difference to the fitted properties. Again, we emphasize, for normal $\sim L_*$ ellipticals, that there appears to be no bias, and the relevant parameters are recovered well via simple Sersic fits, even given a very limited dynamic range of fitting.

However, in the most extreme systems characteristic of the most massive galaxies – those with large outer Sersic indices indicative of extended envelopes that include significant low-density material out to $\sim 100$ kpc radii – the inferred $R_e$ and $n_s$ can be sensitive to whether or not this material is included in the fits. Considering
the entire sample, we find that the typical depth required to obtain a ‘converged’ $R_e$ and $n_s$ (to within ∼30–50 per cent of the value obtained with the deepest available data) is a strong function of stellar mass (really, the strength of the low-density envelope), rising from $\Delta \mu \sim 4$ mag in intermediate-mass systems to $\Delta \mu \sim 6$–8 in high-mass ($M_* > 10^{11} M_\odot$) systems. If we require that at least 50 per cent of local systems have converged $R_e$, we obtain the approximate mass-dependent criteria $\Delta \mu_{\text{cont.}} > 3.0 + 2.3 \log(M_*/10^{11} M_\odot)$; if we raise our desired threshold to ∼75–90 per cent, the minimum $\Delta \mu$ should be uniformly deeper by another 1.5 mag. In terms of physical radii, depth of $\Delta \mu \sim 4$ mag corresponds roughly to a maximum well-sampled, high signal-to-noise ratio (S/N) physical radius of ∼5 kpc; the depth required for obtaining converged $R_e$ in massive systems (6–8 mag) corresponds to physical radii of ∼20–50 kpc.

This bias arises because the systems with large envelopes are not perfect Sersic profiles; indeed, it is now well-established that no populations of spheroids are completely described by single Sersic profiles given sufficient dynamic range (see e.g. Kormendy 1999; Ferrarese et al. 2006; Côté et al. 2007; Lauer et al. 2007; Kormendy et al. 2008). As a consequence, although a single Sersic profile is often a formally good fit (in a $\chi^2$ sense) over limited dynamic range, the best-fitting $n_s$ can change systematically as that dynamic range changes. The effect is most pronounced in systems with the most dramatic envelopes; at small radii, $R < 2$–10 kpc, systems are either ‘concave down’ (which corresponds to a local Sersic index $n_s < 4$) or uncurved ($n_s \sim 4$). At larger radii, the profiles become more ‘concave up’ ($n_s > 4$). It is important to stress that, as such, the ‘correct’ Sersic index is fit for the dynamic range sampled in the simple examples shown. If, in fact, the high-mass systems shown in Fig. 6 were perfect Sersic profiles, there would be no significant effect. Ultimately, this reflects the obvious caveat to any limited dynamic range observation: a fit is being extrapolated to radii not directly observed, based on some assumed functional form.

We emphasize that Fig. 6 is intended to be purely illustrative; we are not attempting to construct a specific comparison with or calibration for any individual observed sample. The specific calibrations for these observations are different from sample to sample, and well outside the scope of this paper – we refer the readers to the relevant observational papers for more details. For example, the real fit results will also depend on the resolution, instrument PSF, sky subtraction and other details. Given the non-trivial dependence of profile shape curvature on radius in the most extreme systems, the results will depend just as much on the relative weighting (error bars as a function of radius) in the observed profile as on any choice of a ‘cut-off’ radius (recall that we simply truncate the profile at some limit – realistically, this will appear as some surface brightness dependent error bar). Moreover, in many works (e.g. Trujillo et al. 2007; Buitrago et al. 2008; van Dokkum et al. 2008), the best-fitting Sersic profile is determined directly from a fit to the two-dimensional image data, assuming an (radius-independent) ellipticity. In other works (e.g. Lauer et al. 2007; Kormendy et al. 2008), the image data are used to produce a major-axis or circularized profile (which allows for e.g. variations in ellipticity with radius or isophotal twists) and then fit to a Sersic profile. The attendant systematics, at this level of detail, are not identical; and re-fitting the objects shown in Fig. 6 in two-dimensional images tends to suppress the run of the Sersic index with fitted radius (owing to the difference in relative error weighting; C. Peng, private communication).

The consequences of those details can, in principle, affect the inferred sizes in either direction, and not just towards inferring smaller sizes in lower-depth observations.

That being said, we can consider these caveats in the context of the deepest available observations at $z \sim 1$–2, spanning $\Delta \mu \sim 3$–4 mag (S/N rapidly decreasing at $R > 5$ kpc; see Trujillo et al. 2004; Cimatti et al. 2008; Damjanov et al. 2009). At these depths, our comparisons suggest that – if the ‘true’ profiles were identical to those of today’s most extreme massive galaxies (again, systems with $\sim 100$ kpc envelopes and very large $n_s \sim 8$–10) the effective radii could be underestimated by factors of up to ∼2–3. It is not, in principle, hard to recover fitted $R_e \sim 2$–3 kpc for such systems in this simplified experiment, for individual objects given limited dynamic range. Note, however, that the details are sensitive to the above issues: there is less of a discrepancy (in at least this idealized case), for example, comparing the two-dimensional profiles. More importantly, even allowing for this level of an effect, it is very difficult to account for the entire evolution observed; in short, there is a real deficit of low-density material at large radii in the high-redshift systems. This is already apparent at the lowest $\Sigma$ sampled in, for example, Fig. 1, where the high-redshift profiles are falling more rapidly than those of low-redshift analogues.

Again, if there is no large envelope as in the extreme case considered here, then there will be no bias in $R_e$ in high-redshift observations. But, of course, this becomes circular – the point is simply that caution is warranted in extrapolating any profile (especially profile shapes calibrated to the observations of low-redshift galaxies) to radii not directly observed.

Other, simple tests can constrain these possibilities. For example, Zirm et al. (2007) stack ∼14 high-redshift ($z \gtrsim 2$) systems identified as compact (gaining roughly an additional $\Delta \mu \sim 1.5$), and see no significant change in the Sersic profile or size (relative to the luminosity-weighted average size of the individual fits). Likewise, stacking the $z = 1$ compact systems in van der Wel et al. (2008), the best-fitting Sersic index is $n_s \approx 4$, comparable to the individual fit results. These appear to support what can already be seen in Fig. 1 (and fig. 1 of Bezanson et al. 2009); at the maximum radii, ∼5 kpc, sampled in the high-redshift observations, the profiles do appear to be falling more rapidly with radius than profiles of similar-mass low-redshift galaxies.

It appears, therefore, that despite the above caveats, there is a real deficit of material at low surface densities at large radii around massive, high-redshift galaxies.

However, it is important to emphasize two simple points this highlights with respect to the interpretation of observed surface density profiles. First, some caution is always warranted when the dynamic range is limited. Additional checks, such as stacking the observed images, calibrating against low-redshift samples and testing for bias in surface brightness limits of the sample, are important (and indeed have been a critical component of many of the high-redshift studies considered here). Given the lack of strong constraints on the amount of material at very low surface densities at high redshifts, the effective radii of the most extreme systems could (again, depending on the circumstances as noted above) be biased at the factor of ∼2 level.

This is insufficient to explain the total observed evolution – there appears to clearly be some real evolution in the amount of low surface density material – but it points to the still relatively large uncertainties in just ‘how much’ low-density material is (or is not) already in place at $z = 2$. Constraints on this quantity, in particular as a function of redshift, will be of considerable interest for constraining models of how low-density envelopes build up from high redshifts to redshift zero.

Secondly, it should be borne in mind that real ellipticals are not always perfect Sersic profiles, and in some cases the best-fitting profile shape can change depending on the dynamic range sampled.
As such, direct comparison of profiles, such as that considered here or in, for example, Bezanson et al. (2009), is important (as opposed to just a comparison of fitted quantities such as the Sersic index and effective radius). Moreover, inferences made from extrapolation of Sersic fits should always be treated with some caution: the approach appears to work reasonably well with normal, ∼ L∗ galaxies, for inferring simple quantities such as the effective radius, but it ultimately depends on the assumption that the functional form of the Sersic profile is a good description of the ‘true’ profile at radii where the direct observational constraints are not as strong. For example, the approach of many works attempting to infer whether or not significant bias is present, by mock imaging systems modelled as single Sersic profiles (artiﬁcially redshifting and imaging them, then re-ﬁtting to a Sersic proﬁle), is a useful exercise, but does not necessarily capture all of the physical possibilities. Even at low redshifts, in fact, only a small fraction of massive ellipticals have effective radii that can be directly determined from the observations (i.e. converged R_e from the actual observed light proﬁle, independent of ﬁtting or extrapolation, that do not change as deeper radii are sampled; see e.g. the discussion in Kormendy et al. 2008). Extending these examples, in particular at low and intermediate redshifts, is important both for studying the light-density envelopes that build up at later times and for informing our interpretation of the high-redshift observations.

6 DISCUSSION

6.1 Can yesterday’s compact spheroids be the cores of today’s ellipticals?

We have compared the stellar mass proﬁles of high-redshift, ‘compact’ massive spheroids and well-studied local massive ellipticals. There has been considerable debate in the literature regarding the origin and fate of the compact high-redshift systems: they appear to be smaller (R_e ∼ 1 kpc at ∼ 10^{11} M⊙) than all but a tiny fraction of local, similarly massive galaxies which have R_e ∼ 4–5 kpc at z = 0. However, comparing the surface stellar mass density proﬁles directly, over the ranges that are actually well-sampled by observations, we show that the observed high-redshift systems have surface density proﬁles similar to the inner, dense regions of local massive ellipticals (Fig. 1).

In other words, although the effective stellar mass surface density within R_e, Σ_{eff} ≡ 1/2 M_*/(π R_e^2), is large in high-redshift systems, the physical stellar surface densities are comparable to the typical central surface densities observed at radii ∼ 0.5–5 kpc in many local ellipticals. The centres or cores of local spheroids are just as dense as those of high-redshift systems: the difference is in the effective radii and effective densities, owing to the large, extended wings/envelopes of low surface brightness material around local massive spheroids. This material leads to a larger R_e and lower effective surface density in the local systems.

We have further shown that the distributions of the maximum stellar surface densities are nearly the same at z ∼ 2 and z = 0 (Fig. 2) – at small radii today’s ellipticals have similar maximum nuclear stellar surface densities of ∼ 0.3–1 × 10^{11} M⊙ kpc^{-2} over a wide range in stellar mass from ∼ 10^9 to ∼ 10^{12} M⊙. The high-redshift systems have their central surface densities smeared out by PSF and seeing effects, and thus do not reach these densities at any observed point; but extrapolating their best-ﬁtting Sersic proﬁles inwards, they exhibit similar peak surface densities. Similar conclusions are reached by Bezanson et al. (2009) as well (note that the factor of ∼ a couple apparently higher densities those authors note in the central regions of high-redshift systems depends on extrapolating Sersic proﬁles to smaller radii than observed, as well as ignoring the scatter in the central densities of ellipticals today). High-redshift red galaxies are thus not uniformly more dense; indeed, the maximum/peak surface density of spheroids does not appear to evolve signiﬁcantly from z ≥ 2 to z ∼ 0.

Using a large sample of local, high-dynamic range observations, we have constructed a census of the local spheroid population and have quantitatively calculated the number of systems with central/core mass densities above a given surface mass density and stellar mass threshold (Figs 3–5). We have used this to construct the stellar mass function of spheroid ‘cores’ – i.e. the stellar mass function of the parts of today’s ellipticals that lie above a given surface stellar mass density threshold.

The regime of particular interest is Σ ∼ 10^{10} M⊙ kpc^{-2}, which corresponds to the effective surface brightness of the high-redshift compact systems (10^{11} M⊙ with R_e = 1 kpc). We ﬁnd that ∼ 25–35 per cent of the stellar mass density in z = 0 massive spheroids lies above this surface density. Typical ellipticals have cores containing ∼ 1–5 × 10^{10} M⊙ above this threshold. Comparing this to the observed properties of massive galaxies at z = 1 and 2, we ﬁnd that by both number and total stellar mass, all of the high-redshift, compact systems can be accounted for in the cores of today’s ellipticals. For example, even in the extreme case in which every z = 2, 10^{11} M⊙ or larger spheroid (space density ∼ 10^{-4} Mpc^{-3}) had R_e = 1 kpc, this would correspond to the same space density of systems with > 1/2 M_* = 5 × 10^{10} M⊙ above the effective surface density 10^{10} M⊙ kpc^{-2}. At z = 0, the space density of such massive, high surface density cores is a factor of ∼ 1.5–2 higher. Doing the calculation more properly (convolving over the mass function and distribution of proﬁle shapes), there is a factor of ∼ 2 more mass in local massive cores than is present at z > 2; the difference is qualitatively similar, but smaller, comparing to z = 1 populations. Not only can the high-redshift systems be accommodated (rather than being destroyed), but also high-density material in the centres of ellipticals may continue to build up even at relatively low redshifts.

6.2 How does this relate to physical models?

These conclusions are of considerable importance for physical models of spheroid formation and evolution, and in particular for the models that have been proposed to explain both the formation of high-redshift, apparently compact galaxies and their evolution into local z = 0 systems.

Models for spheroid formation naturally predict that ellipticals and bulges are fundamentally two-component objects, with a dense, central core built by dissipational processes – the loss of angular momentum in a progenitor gas disc, which then falls to the centre and turns into stars in a compact starburst – and an extended, lower-density envelope built by dissipationless processes – the violent relaxation of progenitor disc stars, observed to be at much lower phase-space densities than the compact cores of ellipticals (Mihos & Hernquist 1994; Hopkins et al. 2008a). Observations in the local Universe have conﬁrmed much of this picture and made it increas-ingly robust (Hibbard & Yun 1999; Kormendy 1999; Rothberg & Joseph 2004; Kormendy et al. 2008). Indeed, simulations by several independent groups consistently ﬁnd that it is not possible to make realistic ellipticals without the appropriate mix of these two components (Barnes & Hernquist 1996; Cox et al. 2006; Naab, Jesseit & Burkert 2006; O’Horo et al. 2006; Jesseit et al. 2007; Burkert et al. 2008). As such, the existence of dense cores in spheroids at
both low and high redshifts is a natural consequence of dissipational spheroid formation.

It is possible, if mergers are sufficiently gas-rich,\(^6\) to build just the high-density core, and to add the envelope in relatively gas-poor mergers at later times. Given the gas-richness of high-redshift galaxies, some size evolution is naturally predicted in models, with high-redshift systems being more dominated by the dense, dissipational remnant (Khochfar & Silk 2006; Hopkins et al. 2009c).

The high-redshift observations represent an ideal opportunity to catch such cores ‘in formation’ and strongly constrain their physical origin. Today, such cores are typically extremely old: \(\sim 10^{10}\) yr. At high redshifts, however, they have ages \(\lesssim 500\) Myr (Kriek et al. 2006). Understanding their stellar populations, metallicities, kinematics and densities is critical to inform models of how dissipation builds the central regions of galaxies. There appears to be a natural link between the observed compact red galaxies and bright submillimetre galaxies, which are intense starbursts with consistent number densities (accounting for their short duty cycles) and physical sizes (Tacconi et al. 2006; Younger et al. 2007, 2008; Cimatti et al. 2008). This class of sub-millimetre galaxies (SMGs) is widely believed to be the product of major mergers (Shapiro et al. 2008; Tacconi et al. 2008). Establishing further connections between these populations would not only enable new tests of the merger hypothesis, but would also rule out alternative models (e.g. monolithic collapse) for spheroid core formation.

The maximal mass densities of spheroids at both low and high redshifts \((\sim 10^{11} M_\odot \, \text{kpc}^{-2})\), for example, may inform models of star formation and feedback in extreme environments. This maximum surface density is intriguingly similar to previous suggestions of maximal (Eddington-limited) starbursts: if the observed mass surface density is initially pure gas, forming stars according to the Kennicutt (1998) relation \((\text{giving } \sim 2500 M_\odot \, \text{yr}^{-1} \, \text{kpc}^{-2})\), this implies a luminosity of \(1.5 \times 10^{13} L_\odot \, \text{kpc}^{-2}\). This is the Eddington limit for dusty systems (Thompson, Quataert & Murray 2005). Interestingly, it corresponds to the maximum star formation rate surface density in dense SMGs (Tacconi et al. 2006; Younger et al. 2008). The fact that so few ellipticals scatter above this peak surface density also suggests that their centres may have formed in a few dissipational events – if Eddington-limited arguments explain these peak densities, then there is no reason why they could not be exceeded if the gas ‘trickled in’ at a lower rate or in several smaller events. Clearly, it is of interest to investigate constraints on star formation and feedback models stemming from this.

Understanding the evolution in profile shapes, in particular how central versus outer densities evolve, is necessary to constrain how the potential and binding energy at the centres of spheroids evolve. This may be intimately related to the BH–host galaxy correlations in feedback-regulated models of BH growth (see e.g. Hopkins et al. 2007a,b, and references therein). There has been considerable debate regarding the state of the BH–host correlations at these redshifts: better understanding of spheroid cores that dictate the local potential depth is critical to informal theoretical models.

Current observations suggest that a large fraction of the high-density material in spheroids was assembled at early times. Although we have shown that it is possible to accommodate the mass in dense, high-redshift cores in the elliptical population today, the observations suggest that of the order of half of the massive cores of today’s massive ellipticals had to be in place by \(z > 2\). Compare this to just \(\sim 5\) per cent of the total spheroid mass density in place at these redshifts, and \(\sim 20\) per cent of the massive galaxy \((\sim 10^{11} M_\odot)\) density (Grazian et al. 2007; Pérez-González et al. 2008b; Marchesini et al. 2008). In other words, it appears that the massive cores of today’s ellipticals assembled preferentially early. This is qualitatively consistent with models of dissipational formation, but in semi-analytic models explaining early massive elliptical formation is quantitatively quite challenging (see e.g. Bower et al. 2006; Fontana et al. 2006). The observations thus constrain not just the total assembly, but also how this takes place – invoking early minor mergers or gas-poor processes, for example, might be able to account for the shape of the mass function, but would not explain the early formation of dense cores.

The observational comparison here favours models in which high-redshift compact galaxies are not destroyed (as has typically been concluded), but accrete or reveal previously ‘hidden’ extended envelopes of low surface brightness material. Their central densities remain, but with the appearance of low-density material, the effective radii, and profile shapes quickly become comparable to massive galaxies today. If the high-redshift systems genuinely do have such low-density envelopes, the required evolution is only a factor of \(\sim 1.5–2\) growth in stellar mass from high redshifts to redshift zero. Indeed, dry mergers on to such massive, early-forming systems are cosmologically inevitable, and the mass growth requirements found here are consistent with the current stellar mass function constraints (Brown et al. 2008; Pérez-González et al. 2008a). Moreover, most dry mergers in such massive systems will be with later-forming, less massive and less dense systems, that are not expected to disrupt the dense cores, but will instead build up an envelope of lower surface density material (see e.g. Naab, Johansson & Ostriker 2009).

In fact, the observations allow the possibility that the central regions of some massive ellipticals today have evolved with little or no strong perturbation, and corresponding change in densities, since high redshifts, while their envelopes assemble over this same period in time. This is important for the kinds of mergers that influence bulge formation: mergers with the kinds of low-density systems needed to build up an extended, low-density envelope (minor mergers, mergers with relatively gas-poor discs and mergers with later-forming, less dense ellipticals) will not significantly perturb the (much more dense) central regions of the galaxy. In detail, even equal-mass mergers with equal density systems do significantly less to lower than central densities than a simple energetic argument would imply: the central density profile remains relatively unperturbed while energy tends to be preferentially transferred to less bound outer material (see Hopkins et al. 2009d).

Such mergers may also transform an initial central ‘cuspy’ profile into a ‘cored’ profile, via the scavenging action of a binary BH–BH merger (if the initial high-redshift systems are ‘cuspy’, expected if they have just formed in gas-rich mergers, then they must become cored by low redshift to correspond to observed systems; see e.g. Faber et al. 1997; Graham et al. 2003; Côté et al. 2007; Kormendy et al. 2008). Both minor and major dry mergers are expected to be efficient mechanisms for scavenging, even where the secondary is of sufficiently low density so as not to perturb the density profile as discussed above (see e.g. Milošavlijević et al. 2002). But the cusp–core distinction (in all but the most extreme systems) affects the mass profile only on very small scales (well below the scales observed in all but the nearest systems) and involves only a very small fraction of the galaxy mass \((\sim M_{\text{BH}}, \text{or } \sim 10^{-5} M_\odot)\).

\(^6\) We exclude cases where the systems are gas-dominated from this discussion, as in these cases the relevant physics lead to qualitatively different behaviour in mergers, and will not necessarily make spheroids at all (Robertson et al. 2006; Hopkins et al. 2009b,f).
6.3 Observational tests and future prospects

Observed high-redshift systems require the growth of extended, low surface density envelopes to match the profiles of massive ellipticals today. It is quite possible that such envelopes are entirely absent at high redshifts. However, Fig. 6 highlights the fact that it remains difficult to say precisely how much of a ‘mass deficit’ at large radii must be accreted from $z = 2$ to 0. In short, the total mass at very low surface densities at high redshifts remains more uncertain than the mass budget at high surface densities. Even where observations detect light at relatively low surface brightness, the relevant S/N weighting means that the profile fits can be preferentially weighted towards the high-brightness central regions. As a result, there could remain some non-trivial differences in the best-fitting $R_e$ from high-redshift observations, compared to deep low-redshift observations of analogous systems.

At low and intermediate stellar masses, where Sersic indices tend to be low ($n_s \lesssim 4$), our simple experiments, as well as those in other works calibrated to the specific observation techniques used therein (see e.g. Trujillo et al. 2006b; Trujillo et al. 2007; Zirm et al. 2007; Alam et al. 2008; van der Wel et al. 2008), suggest that there is no strong dependence on the depth of the observations. In other words, when there is no significant envelope, the precise mass profile of the low-density material makes little difference. At the highest masses, however – i.e. local systems where the outer Sersic indices are very large ($n_s \gtrsim 6$) because of the presence of large stellar envelopes that can extend to $\gtrsim 100$ kpc scales – there can be a non-trivial mass at extremely low brightness, whose profile is difficult to recover in detail. If massive-envelope ellipticals such as NGC 4552 were present at $z > 0.5$, full recovery of their envelopes (in the sense of recovering high S/N profile information) would require observations $\sim 4–5$ mag deeper than typical of individual high-redshift objects (Fig. 6). Even at low redshifts, only a small fraction of objects at the highest masses have directly measured and converged effective radii (determined purely from the observed light profile); in other cases, the effective radius is usually estimated by the extrapolation of a best-fitting Sersic profile to low densities and large radii. It is possible, if envelopes are present, but do not follow a perfect Sersic profile (or if the Sersic profile shape of the galaxy profile changes from small to large radii), to underestimate the envelope mass, and correspondingly to underestimate the true effective radius by a factor of $\sim 2$.

This has important consequences even at low redshifts. Some recent studies have claimed that most of the apparent size–mass evolution in massive galaxies occurs at very low redshifts, a factor of $\sim 2$–3 change in sizes between $z = 0.1$ and 0.3, with the evolution from $z = 0.4$ to 2 restricted to a smaller factor of $\sim 1.5$–2 (Bernardi 2009; Ferreras et al. 2009). Such extreme apparent low-redshift evolution (as opposed to the more plausible high-redshift evolution) may be related to the observed dynamic range and fitting: it is almost impossible to explain such a large change in the true stellar half-mass radius in any model over a narrow low-redshift interval $z = 0.1$–0.3. Independent constraints have clearly established that in this redshift range, there is almost no evolution in the stellar mass function of massive spheroids, nor is there significant evolution in the (uniformly old) stellar populations, or any significant stellar mass loss or new star formation given the old stellar population ages (Nelan et al. 2005; Thomas et al. 2005; Gallazzi et al. 2006; Masjedi et al. 2006; Borch et al. 2006; Jones et al. 2006). Likewise, there is no change in their kinematics or the fundamental plane relation in clusters or the field (Treu et al. 2005; di Serego Alighieri et al. 2005; van der Wel et al. 2005; van Dokkum & van der Marel 2007).

Even the dark matter haloes grow by only a tiny fraction over the redshift range of $z = 0.1$ to 0.3 (<0.1 dex; almost all accreted at large radii). What do change over this redshift range, however, are the spatial resolution and effective surface brightness limits, and as a consequence the radial range of the profile sampled in observations. We find that the observations of rapid changes in the best-fitting $R_e$ at low redshifts can be accounted for by the biases summarized in Fig. 6. Indeed, other observations, using somewhat different fitting methodology and sample selection, have found no such significant evolution at low redshifts, while the high-redshift evolution appears more robust (see e.g. McIntosh et al. 2005; Trujillo et al. 2007; Franx et al. 2008).

Clearly, better constraints on just how much low-surface brightness material is present, as a function of redshift, will improve our understanding of elliptical galaxy formation. Whether there has been a great deal of evolution in the amount of low-density material or relatively little, either result is of considerable interest. If high-redshift systems have essentially no stellar mass at low densities ($\Sigma \lesssim 10^{−9} M_\odot$ kpc$^{-2}$), then mergers forming spheroids must initially be very gas-rich, and mergers with lower-mass galaxies or evolved discs at high redshift must be relatively rare. Moreover, this would determine how much material would have to be built up by subsequent mergers, putting requirements on models for tidal destruction and minor mergers as well as later dry major mergers. If some envelopes are present at high redshifts – perhaps not as much as at low redshifts. To the extent that envelopes exist that contain significant mass not previously detected, it would increase the stellar masses of these galaxies, perhaps yielding tension with constraints from e.g. the galaxy mass function, and certainly presenting a challenge for models, which have difficulty explaining very early mass assembly without much subsequent growth.

There are a number of observational means to study these possibilities. Most directly, observations can probe whether such material exists at high redshifts. In addition to profile fitting, which necessarily relies on the assumption that some functional form will represent a good approximation to light at radii where the profile shape cannot be strongly constrained directly, it should be possible to estimate that total light contribution from comparison of deep integrations of the total light/stellar mass in fixed physical annuli. Also, stacking the observed high-redshift systems, allowing for a gain of $\sim 1–1.5$ mag in surface brightness depth, seems to show a continued steep falloff in surface density ($n_s \lesssim 4$), indicating that there is not a large undetected mass in envelopes at high redshift (Zirm et al. 2007; van der Wel et al. 2008). This reinforces the conclusion that the envelopes must be predominantly built up at lower redshifts; unfortunately, it remains difficult to say precisely how much material is at low densities (other than to say that it is not a large fraction of the galaxy mass and cannot change $R_e$ at the level of evolution seen), or what the exact mass profile of the low-density material is (e.g. whether it corresponds to the inference from extrapolating the fitted Sersic profiles, cuts off more steeply or obeys a power-law-like distribution analogous to observed intracluster/halo light in low-redshift systems).

Observations of major and minor dry merger rates offer complimentary constraints on how much material is added to these systems between high redshifts and to redshift zero. In the local universe, studying the properties of these envelopes can inform models of their formation histories. For example, stellar population gradients and kinematics might reflect a more dramatic transition in properties if the envelopes form by late accretion on to earlier-forming cores. If the envelopes form early, they will be metal poor and have different $\alpha$-element abundances compared to late-accreting disc/outer...
Some efforts have been made along these lines (see e.g. Sánchez-Blázquez et al. 2007), and gradients in e.g. α-element abundances show significant diversity, suggesting that in some systems, envelopes formed quickly (perhaps in e.g. later-forming ellipticals, where a large envelope can be formed from relatively gas-poor discs), while in others, envelopes are contributed by systems with more extended star formation (e.g. late mergers with lower-mass or later-forming systems, as expected for systems described here). However, samples remain small, and the differences are subtle; larger samples are needed to correlate the behaviour of these properties with other aspects of galaxies (e.g. galaxy mass, kinematics, cusp/core status, environment) that might provide an indication of whether or not they are descendants of similar high-redshift systems. Moreover, typical observations of these quantities extend only to relatively small radii (∼R_e); it remains difficult to probe stellar populations in the low-density outer regions that constitute spheroid envelopes. Together, however, these observations offer promising avenues towards constraining these observationally challenging, low-surface brightness components.

Corroborating evidence for the picture presented here has recently been presented in Cenarro & Trujillo (2009). The authors measure the average velocity dispersions of compact spheroids at z = 0–2, and show that it evolves weakly relative to, for example, the naive expectation of models with uniform contraction/expansion (i.e. σ^2 ∝ M_e / R_e). Despite a factor of ~2 evolution in effective radii of massive galaxies over this interval, the median σ at fixed mass evolves by a factor of ≃1.3. Moreover, the high-redshift σ values are in fact consistent with the high end of the observed low-redshift scatter at this mass, or with the median σ of slightly more massive (a factor of ~2) low-redshift ellipticals. This is precisely the behaviour expected if the central, high-density regions (which determine the central potential depth and correspondingly σ) assemble preferentially early, and evolve relatively unperturbed to low redshift (for examples in simulations; see Hopkins et al. 2009c). Low-density material accreted later is clearly important for the effective radii, and changes, for example, the dark matter fraction within R_e as well as the profile shape, but has very little effect on the velocity dispersion. The observations represent a strong constraint on the physical densities at a fixed radius: if the central densities at high redshift were in fact substantially higher than those at low redshift, by even a factor of a few, it would significantly overpredict the observed evolution in velocity dispersions.

Throughout this paper, we have neglected several additional physical effects that might affect estimates of the stellar surface mass densities and effective radii of high-redshift ellipticals. For example, at low redshifts, stellar mass-to-light ratios are independent of radius to within ~20 per cent in optical bands in massive ellipticals, which tend to be uniformly old and have weak colour gradients (see e.g. Faber et al. 1989; Bender, Burstein & Faber 1993). However, given the observed stellar population gradients run backwards in time, or considering local recent merger remnants and/or simulations, the expectation is that this could be quite different at the high redshifts when the ellipticals formed (Schweizer 1996; Rothberg & Joseph 2004; Yamauchi & Goto 2005). The young, post-starburst population (ages ≲ 1–2 Gyr) in the core has higher optical L / M_e, which can lead to a rest-frame B-band best-fitting R_e that is a factor of ~1.5–2 smaller than the stellar-mass R_e (or the B-band R_e observed when the system has aged and this effect vanishes). Some reassurance, however, comes from the fact that the size–mass relation does not seem to depend strongly on the precise stellar population age/colours (specifically within the ‘quenched’ or ‘star-forming’ populations; see Toft et al. 2007; Pérez-González et al. 2008a) and the fact that the observed sizes of the galaxies of interest here are similar in rest-frame near-UV and optical (Trujillo et al. 2007). There may also be some bias in estimated stellar masses of systems at similar ages, owing to the uncertain contribution of AGB stars (Maraston 2005; Maraston et al. 2006). This is estimated to be a possible factor of ~1.2–1.4 overestimate of the high-redshift masses where high-quality optical photometry is available (Wuyts et al. 2007; Wuyts et al. 2009). We have conservatively ignored these effects, but if present they will strengthen most of our conclusions. To test for these effects, it is important to obtain deeper spectra and photometry to test for the presence of blue cores and constrain the contribution of stellar populations of different ages (and stellar population gradients) in systems at intermediate and high redshifts.

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