Abstract

Proton inelastic scattering experiments at energy $E_p = 200$ MeV and a spectrometer scattering angle of $0^\circ$ were performed on $^{144,146,148,150}$Nd and $^{152}$Sm exciting the IsoVector Giant Dipole Resonance (IVGDR). Comparison with results from photo-absorption experiments reveals a shift of resonance maxima towards higher energies for vibrational and transitional nuclei. The extracted photo-absorption cross sections in the most deformed nuclei, $^{150}$Nd and $^{152}$Sm, exhibit a pronounced asymmetry rather than a distinct double-hump structure expected as a signature of $K$-splitting. This behaviour may be related to the proximity of these nuclei to the critical point of the phase shape transition from vibrators to rotors with a soft quadrupole deformation potential. Self-consistent random-phase approximation (RPA) calculations using the SLy6 Skyrme force provide a relevant description of the IVGDR shapes deduced from the present data.

Keywords: $^{144,146,148,150}$Nd, $^{152}$Sm(p,p$'$), $E_p = 200$ MeV, $\theta_{lab} = 0^\circ$, relativistic Coulomb excitation of the IVGDR, comparison with photo-absorption results, transition from spherical to deformed nuclei

1. Introduction

Giant resonances represent a prime example of collective modes in the nucleus. A smooth mass-number dependence of the resonance parameters is characteristic of all nuclear giant resonances and, as such, a study of them yields information about the non-equilibrium dynamics and the bulk properties of the nucleus [1]. The oldest and best known giant resonance is the IVGDR owing to the high selectivity for isovector E1 excitation in photo-absorption experiments. The properties of the IVGDR have been studied extensively using $(\gamma,xn)$-type experiments, particularly in the Saclay [2] and Livermore [3] laboratories. These sets of experiments are a major source of information with respect to the $\gamma$-strength function [4] above the neutron threshold - an important quantity used in statistical reaction calculations relevant to applications like astrophysical large-scale reaction networks [5, 6], reactor design [7], and even nuclear waste transmutation [8].
Recently, a new experimental technique for the extraction of electric dipole-strength distributions in nuclei via relativistic Coulomb excitation has been developed [9, 10]. It utilises proton inelastic scattering with energies of a few hundred MeV at scattering angles close to 0°. Although many of these experiments focus on establishing the strength below and around neutron threshold and its contribution to the dipole polarisability [11–15], such data also provide information on the photo-absorption cross sections in the energy region of the IVGDR.

The chain of stable even-even neodymium isotopes is known to comprise a transition from spherical to deformed ground states for heavier isotopes and thus represents an excellent test case to study the influence of deformation on the properties of the IVGDR. A (γ,xn) experiment at Saclay [16] revealed that the width increases with deformation evolving into a pronounced double-hump structure in the most deformed nucleus 150Nd, considered to be a textbook example [17] of K-splitting owing to oscillations along the different axes of the quadrupole-deformed ground state. Here, we report new photo-absorption cross sections for 144,146,148,150Nd extracted from 200 MeV proton scattering experiments with results differing significantly from Ref. [16]. In particular, no double-hump structure is observed in the most deformed 150Nd nucleus. This finding is confirmed in a further measurement of the comparably deformed 152Sm nucleus, again in contrast to a (γ,xn) measurement at Saclay [18].

2. Experiment and analysis

The proton inelastic scattering experiments were performed at the iThemba Laboratory for Accelerator Based Sciences (iThemba LABS) in South Africa. The K600 magnetic spectrometer, positioned at 0° with the acceptance defined by a circular collimator having an opening angle θlab = ±1.91°, was used to analyse a scattered 200 MeV dispersion-matched proton beam delivered from the Separated Sector Cyclotron of iThemba LABS. The self-supporting 144,146,148,150Nd and 152Sm targets were all isotopically enriched to values >96% (except 148Nd enriched to 90%) with areal densities ranging from 1.8 to 2.6 mg/cm². The corresponding ground-state deformation parameters β2 are given in the second column of Table 1. The beam preparation and the detector setup are described in Ref. [10]. Details regarding the data extraction and analysis of the present measurements can be found in Ref. [21].

In the chosen kinematic conditions, relativistic Coulomb excitation of the target nuclei is the dominant reaction mechanism. The resulting double-differential cross sections (with a systematic uncertainty of ±7%) obtained following the procedures detailed in Ref. [21] are displayed in Fig. 1 for 20 keV energy bins. A typical energy resolution ΔE = 45 keV (FWHM) was achieved. The broad structure visible in all spectra between approximately E_x = 12 and 18 MeV corresponds to

![Figure 1: Experimental double-differential cross sections for the 144,146,148,150Nd(p,p') and 152Sm(p,p') reactions at E_p = 200 MeV and θ_lab = 0° ± 1.91°.](image-url)
the excitation of the IVGDR. Statistical errors in this region are of the order of 2-4%. From Fig. 1 it is immediately evident that the width of the IVGDR increases steadily from the nearly spherical $^{144}\text{Nd}$ nucleus through the transition region to the more deformed $^{150}\text{Nd}$ and $^{152}\text{Sm}$ nuclei.

In order to compare to the $(\gamma,xn)$ data of Carlos et al. [16, 18], the $(p,p')$ spectra had to be converted to equivalent photo-absorption cross sections. By way of example, Fig. 2 provides an overview of the conversion process for $^{150}\text{Nd}$. It can be divided into three distinct stages, namely, background subtraction in the region of the IVGDR, calculation of the virtual-photon spectrum and the division by this spectrum multiplied through by the virtual γ energy to obtain equivalent photo-absorption cross sections. This procedure has been tested for several cases ($^{48}\text{Ca}$, $^{120}\text{Sn}$, $^{208}\text{Pb}$) and fair agreement of the resulting shape and absolute values of the photo-absorption cross sections with experiments using real photons was obtained [11–15].

Figure 3: (Colour online). Example of DWBA calculations of the IVGDR (red), ISGMR (blue) and ISGQR (green) excitation cross sections in $(p,p')$ scattering at $E_0 = 200$ MeV off Nd and Sm isotopes. After averaging over the experimental angular acceptance, these calculations provide a relation between theoretical cross sections and transition strengths under the assumption of a dominant one-step reaction mechanism, which should be well fulfilled at an incident proton energy of 200 MeV. Utilising this proportionality, experimental ISGMR and ISGQR strength distributions can then be converted to $(p,p')$ cross sections in the present spectra. For comparison, the predicted IVGDR cross section is also shown and clearly dominates the spectra. However, the B(E1) transition strengths (and thus the photo-absorption cross sections) cannot be extracted with this method because the Coulomb-nuclear interference term breaks the proportionality.

Itoh et al. [24] reported isoscalar giant resonance strength distributions for the Sm isotope chain which could be directly applied to $^{152}\text{Sm}$. The results of Ref. [24] were also used for the corresponding Nd isotones, which show very similar deformation parameters, with a correction for the global

Background from nuclear processes studied in similar experiments at 300 MeV has been found to be small in heavy nuclei [11–13]. It was modelled in the present case by three components. The contributions of the IsoScalar Giant Monopole Res-
mass dependences of the ISGMR and the ISGQR \[1\]. The ISGQR contribution was independently estimated from a recent study of the ISGQR in the Nd isotope chain \[25\] with methods analogous to Refs. \[26–28\] in good correspondence with results from the above procedure.

A phenomenological background shown as blue line Fig. 2(a) describes the behaviour of the double-differential cross section at the high excitation energy part of the spectrum where the Coulomb excitation contribution is negligible. This component incorporates all unknown multipolarity contributions as well as quasi-free scattering and is approximated by finding the maximum of the cross section between \(E_x = 20\) MeV and \(23\) MeV and using a width that best describes the spectrum in this region. A similar description for the shape of this component was found in a study of \(^{208}\)Pb \[29\] where an experimental extraction of the angular distribution of the background was possible.

The virtual E1 photon spectrum \[30\] for each isotope was calculated using the eikonal approximation \[31\] and averaged over the angular acceptance of the detector. The equivalent photo-absorption spectrum (cf. Fig. 2(c)) was then obtained using the following equation

\[
\frac{d^2\sigma}{d\Omega dE_{\gamma}} = \frac{1}{E_{\gamma}} \frac{dN_{E1}}{d\Omega} \sigma^{\gamma\lambda}(E_{\gamma}).
\]  

Finally, Fig. 2(d) shows the equivalent photo-absorption spectrum rebinned to 200 keV for direct comparison with the \((\gamma,\text{xn})\) results. The present setup at \(\theta_{\text{lab}} = 0^\circ\) does not allow for the determination of accurate vertical scattering angles, thus limiting the angular resolution \[10\]. We therefore refrain from extracting absolute photo-absorption cross sections. The excitation energy dependence of the conversion, however, is not affected.

3. Comparison with \((\gamma,\text{xn})\) results

Through the simultaneous measurement of the partial photo-nuclear cross sections \(\sigma(\gamma, n) + \sigma(\gamma, p\text{n})\) and \(\sigma(\gamma, 2n)\) using a monochromatic photon beam, total photo-absorption cross sections can be determined in heavy nuclei. Data obtained with this method for the IVGDR in the stable even-even neodymium and samarium isotopic chains are given in Refs. \[16\] and \[18\], respectively. Figure 4 displays the rebinned spectra from the present work normalised to the maximum of the photo-absorption cross sections \[16\] \[18\] to facilitate a comparison of the evolution of the shape of the IVGDR with increasing deformation.

Carlos et al. \[16\] \[18\] (green histograms) observed a spreading of the IVGDR as the nuclei become softer followed by a splitting of the IVGDR into two distinct dipole modes for \(^{150}\)Nd and \(^{152}\)Sm, which were interpreted as \(K = 0\) and \(K = 1\) components. The equivalent photo-absorption cross sections from the present work (red histograms) display a similar trend, i.e., a general broadening of the IVGDR with increasing deformation. For the most deformed \(^{150}\)Nd and \(^{152}\)Sm, the resonance becomes skewed with increased strength on the low-energy
side, but no split into two distinct components is observed.

The obvious discrepancies (in both the $K = 0$ and $K = 1$ regions) between the photo-absorption results and the present data are reflected in a change of parameters when attempting to describe the observed resonances by Lorentzians. The present spectra were fitted with a modified Lorentzian of the form used in Refs. [16, 18]

\[ \sigma(E) \propto \frac{1}{1 + \left[ \frac{(E^2 - E_R^2)^2}{E^2 \Gamma^2} \right]}, \]  

(2)

where $E_R$ corresponds to the resonance centroid energy and $\Gamma_R$ to the resonance half-width. For the more deformed nuclei, a sum of two modified Lorentzians was used. The best fit to the experimental data was selected such that the value for the reduced $\chi^2$ was optimised. In the case of the $^{148}$Nd isotope, it was found that the reduced $\chi^2$ value was not improved through the use of a two Lorentzian fit as assumed in a reanalysis [32] of the data of Ref. [16]. The results are summarised in Table 1.

In order to further illustrate the systematic differences between the two results, we also provide the ratio $R$ of summed photoabsorption cross sections in the excitation energy regions $10 – 14$ and $14 – 18$ MeV, respectively.

For spherical and transitional nuclei, a shift of the centroid to higher energies is observed for the present data. The new parametrisations for the deformed nuclei do not yield a ratio of $\approx 0.5$ for $K = 0$ and $K = 1$ oscillator strengths, respectively, as expected for prolate deformed ground states [3]. One should remember, however, that $^{150}$Nd and $^{152}$Sm lie just above the shape phase transition from vibrators to axial rotors [19, 33]. Although they are already well deformed, their deformation potential is soft in the $\beta$ degree of freedom [20]. The corresponding shape fluctuations thus enhance the width of the resonance peaks which, in turn, may hinder a clear discrimination of the $K = 0$ and 1 branches.

The present results do not provide absolute photo-absorption cross sections and thus cannot distinguish whether the main discrepancies lie in the $K = 0$ or $K = 1$ region, but the agreement at high excitation energies in Fig. 4 and Table 1 suggest the former. In any case, they clearly indicate a different ratio of $K = 0$ and $K = 1$ components compared to Refs. [16, 18]. This finding is independent of the background in the spectra due to nuclear processes shown to be small in the energy region of the IVGDR, cf. Fig. 2(a). The largest component stems from the ISGMR, whose angular distribution peaks at 0°. Even at the maximum of the ISGMR peak, the cross section contribution does not exceed 10%.

New photo-absorption data are available from $(\gamma, n)$ experiments [33, 35] in the excitation-energy region between the neutron threshold and $E_n \approx 13$ MeV. A study of the Sm isotope chain finds systematically smaller cross sections than Ref. [18], corroborating the present results. A similar investigation of $^{143–148}$Nd finds again significantly lower cross sections than Ref. [18] for the lighter isotopes but fair agreement for $^{146, 148}$Nd. Photo-absorption cross sections of $^{154}$Sm [36] have been deduced in a study of the E1 strength with forward angle proton scattering analogous to the experiments described in Refs. [11–14]. The results do show a double-hump structure but with a clear reduction in the $K = 0$ region and a slight enhancement in the $K = 1$ region compared to the Saclay data [18], again leading to a reduced $K = 0/K = 1$ ratio as in the present case. These findings are qualitatively consistent with a global reanalysis of data taken with the Saclay method [37], which indicates that the $(\gamma, n)$ cross sections are systematically too large and the $(\gamma, 2n)$ cross sections too small.

One may speculate whether the observed differences are related to the reaction mechanism (real vs. virtual photoexcitation). However, photoabsorption cross sections deduced from similar $(p, p')$ experiments using the virtual photon method show good correspondence with $(\gamma, xn)$ data in other cases, cf. Refs. [11, 14].

4. Comparison with model calculations

In order to investigate the role of $K = 0$ and $K = 1$ components further, a comparison with RPA calculations particularly suited for modelling the IVGDR is presented. The calculations are performed within the Skyrme Separable Random Phase Approximation (SSRPA) approach [58]. The method is fully self-consistent since both the mean field and residual interaction are derived from the same Skyrme functional. The residual interaction includes all the functional contributions as well as the Coulomb direct and exchange terms. The self-consistent factorisation of the residual interaction crucially reduces the computational effort for deformed nuclei and maintains high accuracy of the calculations [38, 40].
We note that various methods can be applied to the description of IVGDR and other collective excitations in deformed nuclei, see e.g. approaches with finite-range Gogny forces [41, 42] and a relativistic mean field [13]. Some of these more elaborate approaches based on the generator coordinate method take into account nuclear triaxiality [42] or investigate the breaking of axial symmetry by using projection techniques [43]. However, either no theoretical predictions for the present problem are available [12, 43] or they show rather large deviations from experiments [41].

Here, the Skyrme parameterisation SLy6 [44] is used which was shown to provide a good description of the IVGDR in medium-heavy, deformed nuclei [10]. The code exploits the 2D grid in cylindrical coordinates. The axial quadrupole deformation characterised by the parameter $\beta_2$ is determined by minimisation of the total energy, and $\beta_2$ values obtained are typically close to data [10] when taking into account that data, deduced from B(E2) values, embrace ground state deformation plus some quantum fluctuations not included in mean field calculations. We thus adopt the experimental values (cf. Table 1) for the quadrupole deformation in $^{146,148,150}$Nd and $^{152}$Sm, respectively. For the nearly spherical $^{144}$Nd, a negligible deformation, $\beta_2 = 0.001$, is used. Nd and Sm isotopes in the transitional region, however, show very soft deformation energy surfaces, which gives a large uncertainty to the theoretical ground-state deformations. We have checked triaxiality with full 3D mean-field calculations and do not find any for the nuclei considered here, in agreement with a systematic study of nuclear shapes using the Skyrme functional SKM* [16].

Pairing is treated with delta forces at the BCS level [47]. A large two-quasiparticle basis up to $\sim 100$ MeV is taken into account. The Thomas-Reiche-Kuhn energy-weighted sum rule [18] for isovector E1 strength is exhausted by 98–100%. To facilitate a comparison between the experimental results and the model calculations, the SSRPA predictions were smoothed with a width $\Gamma = 2$ MeV, which provides a good description of the broad structure of experimental IVGDR strength distributions in many heavy deformed nuclei [10].

The resulting photo-absorption cross sections are shown in Fig. 4 as blue lines. They are normalised to the data at the high-energy flank of the IVGDR, where the results of Carlos et al. [16, 18] and the present work agree reasonably well. For the most deformed nuclei, $^{150}$Nd and $^{152}$Sm, the separation into $K = 0$ (dashed-dotted) and $K = 1$ (dashed) components is additionally shown. For the spherical and transitional nuclei, $^{144,146,148}$Nd, the calculations are in better agreement with the present results, i.e. favouring smaller cross sections on the low-energy flank. For $^{150}$Nd and $^{152}$Sm, the SSRPA results display a double-hump structure, but again with a lower $K = 0$ component than observed in the Saclay results and total cross sections closer to the present data. Since there is a certain degree of freedom in the normalisation one could bring the theoretical results in better agreement with the re-

Table 1: Comparison of Lorentzian parameterisations, Eq. (2), for the present photo-absorption cross sections with those from Ref. [16] for the neodymium isotopes and from Ref. [18] for $^{152}$Sm. The quantity $R$ denotes the ratio of photo-absorption cross sections summed in the excitation energy regions $10 − 14$ MeV and $14 − 18$ MeV, respectively.

| Isotope | $\beta_2$ | $E_1$ (MeV) $\pm$ $\epsilon$ | $\Gamma_1$ (MeV) | $E_2$ (MeV) $\pm$ $\epsilon$ | $\Gamma_2$ (MeV) | $R$ | Reference |
|---------|-----------|---------------------|-----------------|---------------------|-----------------|-----|-----------|
| $^{144}$Nd | 0.13      | 15.05 ± 0.10        | 5.30 ± 0.25     | 15.64 ± 0.01        | 4.93 ± 0.03     | 0.55 | [16]     |
|          |           |                     |                 |                     |                 | 0.42 | Present  |
| $^{146}$Nd | 0.15      | 14.80 ± 0.10        | 6.00 ± 0.30     | 15.69 ± 0.02        | 6.11 ± 0.07     | 0.66 | [16]     |
|          |           |                     |                 |                     |                 | 0.47 | Present  |
| $^{148}$Nd | 0.20      | 14.70 ± 0.15        | 7.20 ± 0.30     | 15.52 ± 0.01        | 5.84 ± 0.04     | 0.74 | [16]     |
|          |           |                     |                 |                     |                 | 0.53 | Present  |
| $^{150}$Nd | 0.28      | 12.30 ± 0.15        | 3.30 ± 0.10     | 16.00 ± 0.15        | 5.20 ± 0.15     | 0.77 | [16]     |
|          |           |                     |                 |                     |                 | 0.60 | Present  |
| $^{152}$Sm | 0.31      | 12.45 ± 0.10        | 3.20 ± 0.15     | 15.85 ± 0.10        | 5.10 ± 0.20     | 0.87 | [18]     |
|          |           |                     |                 |                     |                 | 0.62 | Present  |
sults of Carlos et al. at lower excitation energies, but at the price of overshooting all available data at higher $E_x$.

5. Conclusions

A measurement of the $(p,p')$ reaction at $E_p = 200$ MeV and $\theta_{lab} = 0^\circ$ favouring relativistic Coulomb excitation in the energy region of the IVGDR has been presented for the even-even $^{144-150}$Nd isotopic chain as well as for $^{152}$Sm. While the high energy-resolution data show considerable fine structure (even in the deformed isotopes), which carries information on the role of different decay mechanisms of the giant resonances [26–29] and level densities [29, 49], the present work focuses on a study of the evolution of the IVGDR as a function of deformation.

A general broadening of the IVGDR is observed with increasing deformation and the most deformed $^{150}$Nd and $^{152}$Sm nuclei exhibit a pronounced asymmetry rather than a double-hump structure owing to $K$-splitting, in contrast to previous photo-absorption data from Saclay [16, 18]. This is interpreted as a signature of the peculiar nature of these two nuclei which lie close to the critical point of a shape phase transition from vibrators to rotators characterised by a soft potential in the $\beta$ degree of freedom [20]. Self-consistent RPA model calculations with the Skyrme SLy6 force, particularly suited to describe the IVGDR, provide a fair description of the data consistent with a reduction of cross sections on the low-energy side of the resonance with respect to the Saclay data. In view of their general relevance, an independent test of these unexpected results would be highly valuable. It should be possible to realise such experiments in the near future at the low-energy tagger system NEPTUN at the S-DALINAC [50] and at ELI-NP [51].

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