GOSH: Task Scheduling Using Deep Surrogate Models in Fog Computing Environments

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Abstract—Recently, intelligent scheduling approaches using surrogate models have been proposed to efficiently allocate volatile tasks in heterogeneous fog environments. Advances like deterministic surrogate models, deep neural networks (DNN) and gradient-based optimization allow low energy consumption and response times to be reached. However, deterministic surrogate models, which estimate objective values for optimization, do not consider the uncertainties in the distribution of the Quality of Service (QoS) objective function that can lead to high Service Level Agreement (SLA) violation rates. Moreover, the brittle nature of DNN training and the limited exploration with low agility in gradient-based optimization prevent such models from reaching minimal energy or response times. To overcome these difficulties, we present a novel scheduler that we call GOSH for Gradient Based Optimization using Second Order derivatives and Heteroscedastic Deep Surrogate Models. GOSH uses a second-order gradient based optimization approach to obtain better QoS and reduce the number of iterations to converge to a scheduling decision, subsequently lowering the scheduling time. Instead of a vanilla DNN, GOSH uses a Natural Parameter Network (NPN) to approximate objective scores. Further, a Lower Confidence Bound (LCB) optimization approach allows GOSH to find an optimal trade-off between greedy minimization of the mean latency and uncertainty reduction by employing error-based exploration. Thus, GOSH and its co-simulation based extension GOSH*, can adapt quickly and reach better objective scores than baseline methods. We show that GOSH* reaches better objective scores than GOSH, but it is suitable only for high resource availability settings, whereas GOSH is apt for limited resource settings. Real system experiments for both GOSH and GOSH* show significant improvements against the state-of-the-art in terms of energy consumption, response time and SLA violations by up to 18, 27 and 82 percent, respectively.

Index Terms—DL for PDC, Fog Computing, Scheduling, Heteroscedastic Models, Lower Confidence Bound, QoS Optimization, Second-Order Optimization.

1 INTRODUCTION

MAINSTREAM parallel and distributed computing (PDC) technologies like Edge and Cloud Computing have recently been combined together into a hybrid paradigm commonly termed Fog Computing. Fog computing architectures are currently one of the most successful technologies to seamlessly harvest both remote computational cloud resources, as well as compute capabilities close to the edge of the network [1]. Such environments use containers for lightweight, flexible and fine-grained resource sharing among the myriad of fog devices [2]. However, scheduling tasks in heterogeneous fog environments with volatile workloads is challenging [3]. Moreover, modern day users demand ultra-low response times and energy consumption, thanks to the shift to AI/ML/DL based workloads [4], [5]. Finally, resource heterogeneity further complicates task placement in such fog environments due to non-uniform task affinity for optimal cost-performance trade-off [6].

Existing Solutions. To deal with the challenges of scheduling volatile tasks in heterogeneous fog environments, recent work uses dynamic scheduling strategies which adapt to changing infrastructure conditions in realtime [7]. Many schedulers use techniques like reinforcement learning and update their estimate of the “expected outcome of interest, like QoS score, cannot be easily directly measured. Examples include neural approximators and stochastic processes [8]. In this work, we only refer to DNN-based surrogate models; hence, the term deep surrogate models.

1. A deep surrogate model is defined as a method used when an outcome of interest, like QoS score, cannot be easily directly measured. Examples include neural approximators and stochastic processes [8]. In this work, we only refer to DNN-based surrogate models; hence, the term deep surrogate models.
ing model approximations, measurement imprecision and fluctuations of parameters over time [23]. Specifically, having a deterministic model does not always give a complete picture of the distribution, due to the unknown nature or inherent stochasticity of some parameters like network latency, temperature and hardware faults [23]. Thus, in this work, we use heteroscedastic surrogate models, specifically the Natural Parameter Network (NPN) that uses twice the parameters of a traditional DNN to output both mean and variance estimates. Further, it is crucial to model the curvature of the QoS hyper-surface to converge quickly to an optimal [24] § 6.1. This entails using higher-order derivatives of the surrogate output while running decision optimization. Further, when modeling uncertainty, we may leverage this to trade-off between the exploration and exploitation to converge to the optimal scheduling decision [25]. However, even after feeding more data, the performance of deep neural networks tends to saturate and we use recently proposed co-simulation based bootstrapping schemes to circumvent this [3]. A co-simulator is a discrete-event simulator that can provide schedulers with future QoS score estimates for more robust scheduling [3].

**Contributions.** Drawing these insights together, we present GOSH: Gradient Based Optimization using Second Order derivatives and Heteroscedastic Surrogate Model. We perform extensive empirical experiments on a real-life fog computing testbed to compare and analyze GOSH against state-of-the-art methods. Our experiments show that GOSH performs best in terms of QoS metrics, reducing the energy consumption, response time and Service Level Agreement (SLA) violations by up to 18, 27 and 82 percent, respectively. It achieves this by being one of the first methods to mitigate volatility by fully taking into account the uncertainty in DNN model predictions. Specifically, the technical contributions of this work include the use of a heteroscedastic neural network based surrogate model of the QoS objective score, uncertainty-based exploration and an adapted version of higher-order optimization. An extension of GOSH, namely GOSH*, further improves model predictions by running a discrete-event co-simulator to generate QoS estimates, but at the cost of increasing the scheduling time.

The rest of the paper is organized as follows. Section 2 overviews related work. Section 3 provides the system model assumptions, the working of the heteroscedastic models, uncertainty based exploration and higher-order optimization methods. Section 4 presents the GOSH and GOSH* schedulers. A performance evaluation of the proposed methods on physical and simulated fog environments is shown in Section 5. Finally, Section 6 concludes and presents future directions.

### 2 RELATED WORK

We list in Table 1 the prior work, dividing such methods into four classes: Reinforcement learning (rows 1 and 2 of Table 1), MaxWeight (row 3), stochastic modelling (rows 4 and 5) and gradient-based methods (row 6).

**Reinforcement Learning models:** Many recent scheduling approaches use various forms of reinforcement learning to adapt in hybrid edge-cloud environments. Predominantly, these approaches use policy-gradient methods, which use a neural network to model a policy and output a decision for each state (assuming Markovian dynamics). In a dynamic scheduling setup, at each scheduling interval, a reward signal that quantifies the QoS of that interval is used to update the parameters of the model. Examples include asynchronous-actor-critic (A3C) policy gradient approach [9]. Such methods are shown to be robust and able to adapt in diverse scenarios [8], [9], [10]. However, such methods can be slow to adapt and fail to model volatile scenarios/workloads to be able to efficiently schedule in complex environments [3]. Furthermore, they are known to perform poorly in heterogeneous setups or when the QoS is adaptive [26].

**MaxWeight based schedulers:** Many prior scheduling approaches use the popular MaxWeight based techniques with robust theoretical guarantees. Such strategies aim to maximize the “weight” of job schedules where this weight is calculated using expected QoS metrics [11], [16], [17]. To compare with our method, we use the POND approach as a baseline due to its high performance compared to other methods in this class [11]. POND uses a pessimistic-optimistic Upper Confidence Bound (UCB) based optimization in maximization setup. UCB optimization of the weight of virtual queues for constrained online dispatch minimizes the violations and maximizes the expected average reward. However, such techniques are unable to leverage the edge-cloud diversity in energy consumption and latency to improve SLA [12].

**Stochastic Modelling:** Prior work also uses stochastic surrogate models such as Heteroscedastic Gaussian Processes to optimize metrics like QoS by appropriate task scheduling [12], [19], [20], [21]. Other works use mean and variance estimates based on historical data to perform safe optimization [12], [18]. These methods typically utilize the uncertainty information for robust or safe optimization [27] or use error-based exploration [20]. Typically, due to poor modeling accuracy of Gaussian Processes, they are unable to perform well in complex environments like heterogeneous fog environments and hence more sophisticated models like NPNs are used in this work [28].

| Work | Edge Cloud | Heterogeneous Environment | Coupled Simulation | Stochastic Workload | Adaptive QoS | Second-Order Optimization | Stochastic Modelling | Method | Optimization Parameters |
|------|-------------|--------------------------|--------------------|--------------------|-------------|---------------------------|---------------------|--------|------------------------|
| 20| ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| 31 | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| 32 | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| 33 | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| 34 | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| 35 | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| This work | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |

**TABLE 1**

Comparison of related works with different parameters (✓ means that the corresponding feature is present).
Gradient-based Optimization: A recently proposed class of methods (GOBI/GOBI*) use a deep neural network based surrogate model to approximate the QoS parameters like energy and response time [3]. An extension of the GOBI scheduler for long-term QoS estimation is the MCDS approach [29] that utilizes Monte-Carlo simulations to estimate the reward at a future system state. Their predictions are aided by a co-simulated digital-twin of the target hosts which receive the tasks. These algorithms use gradient-based optimization approaches like AdamW [30] with cosine annealing and restarts [31], [32] to converge to an appropriate scheduling decision. Leveraging gradient-based directed search on neural approximator with coupled-simulation, GOBI* is able to adapt to non-stationary workloads. The neural approximator used in these methods is a Fully Connected Network (FCN) with input including the host and task utilization metrics of Instructions per second (IPS), RAM, Disk and Bandwidth with the scheduling decisions for each active task. GOBI’s neural approximator also includes the objective score after the single-step execution of GOBI’s scheduling decision on a simulated platform. The output of these neural approximators is an objective score that is minimized.

Although GOBI* provides distinct advantages compared to the state-of-the-art, it also faces drawbacks. First, the model requires a neural approximator to be pre-trained on several hours of workload traces generated using a random allocation based scheduler. This might be infeasible for application scenarios where swift deployment is required. Second, the deployment environment might be very different from the setup used to generate the training data for the model. Even though the model is able to adapt to completely different setups, experiments show that GOBI* lacks the agility required for QoS efficient scheduling (Section 5.6). Finally, even with techniques like momentum, our experiments show that the gradient-based optimization can take a large number of iterations to converge due to many saddle points in the QoS hyper-surface. Considering these shortcomings, there is a need for a model that is able to leverage state-space exploration to quickly adapt to setups different from the one used for training. To this end, we present the GOSH approach as part of this work.

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3 Modelling and Exploration
To model the variance of the QoS objective score in our system, we characterize its uncertainties into two classes defined below.

Definition 3.1 (Aleatoric Uncertainty). The aleatory uncertainty of a collection of datapoints refers to an inherent variation in the physical system to be modeled, also known as irreducible uncertainty [33].

Definition 3.2 (Epistemic Uncertainty). The epistemic uncertainty of a collection of datapoints refers to the deficiencies caused by a lack of knowledge or information, also known as reducible uncertainty [33].

Both uncertainties are used in GOSH as discussed in Section 5. We now describe the system, workload and the QoS objective models that are used in this work.
a normal distribution, NPNs use twice the parameters of exponential distribution, the output can be characterized with a. Compared to standard BNNs, this allows NPNs to avoid an adapted version of the backpropagation approach [36]. Such networks are trained using parameters as exponential-family distributions, giving a stochastic output of each layer. Such networks are trained using an adapted version of the backpropagation approach [36].

3.2 NPN as Heteroscedastic Surrogate Model

Motivation. Predicting just the mean response time using a deterministic surrogate model and ignoring the uncertainty in the distribution is insufficient for an accurate forecast of Service Level Agreement (SLA) violations [12]. Moreover, our tests show that in many cases (more than 70%), taking a scheduling decision according to the minimum mean latency (but high uncertainty) gives a higher SLA violation rate than a decision with higher mean latency (but lower uncertainty). Consider the real-world experiments we have carried out in Figure 2, where response time (seconds) is plotted against the CPU utilization of a host in a fog environment. Here, based on a dataset (red points), we train a heteroscedastic Gaussian process surrogate model (mean in black and confidence interval shaded). Considering the mean prediction model, there are two minima of the curve, 0.3 (local minimum) and 0.55 (global minimum) CPU utilization of a host. However, the probability of exceeding the SLA deadline (20 seconds) is higher for 0.55 than 0.3. Thus, both mean and statistical uncertainty need to be modeled to minimize the best objective value that can be guaranteed with some given probability viz the value at risk (VaR) [24]

Natural Parameter Networks. To model uncertainty, recent works have used models like Gaussian Processes (GP) or Bayesian Neural Networks (BNN) [19], [20]. However, prior work has shown Natural Parameter Networks (NPNs) to be more accurate in modeling heteroscedastic uncertainty, also corroborated by our experiments (Section 5.6). NPNs form a class of probabilistic-neural networks that provide a lightweight Bayesian treatment of traditional neural models [36]. To do this, NPNs express neural network parameters as exponential-family distributions, giving a stochastic output of each layer. Such networks are trained using an adapted version of the backpropagation approach [36]. Compared to standard BNNs, this allows NPNs to avoid executing time consuming sampling. Typically for an exponential distribution, the output can be characterized with a set of natural parameters (for instance, mean and variance in a normal distribution). Exploiting this, say for mapping a normal distribution, NPNs use twice the parameters of a traditional neural network to output both mean and variance estimates. In contrast to a traditional NN, an input goes through multiple layers of stochastic transformation, producing an output distribution that is matched with a target distribution. A major advantage of NPNs is that they model aleatoric uncertainty more accurately than the more popular Bayesian Neural Networks (BNNs) [36]. However, inference using an NPN scales linearly with the dimension of the output [36]. Considering a uni-variate objective function, NPNs become a natural choice for stochastic modeling for our problem when compared to BNNs.

Heteroscedastic Modelling. An NPN model cannot be used directly in our setting. This is because, unlike standard NPNs, we do not have the uncertainty information for each input state and scheduling decision. Instead, we have a single datapoint corresponding to each input of the network.

To resolve this, we consider the underlying datapoint that corresponds to a probabilistic distribution instead of being static. Specifically, we consider a NPN neural approximator \( f(x_t; \theta) \) of the objective score \( O \), with \( \theta \) as the network parameters and \( x_t \) as the state of the fog environment and scheduling decision \( [S_t, \phi(D_t)] \). The output of the NPN is a pair \( (\mu_t, \sigma_t) = f(x_t, \theta) \). The parameters \( \theta \) are learnt using a dataset \( \Lambda = \{ [S_t, \phi(D_t)], O_t \}_{t=0} \), and the aleatoric loss \( L \) defined as:

\[
L(f, \Lambda) = \frac{1}{T} \sum_{(x_t, y_t) \in \Lambda} \frac{(\mu_t - y_t)^2}{2\sigma_t^2} + \frac{1}{2} \ln \sigma_t^2, \tag{1}
\]

where \((\mu_t, \sigma_t) = f(x_t; \theta)\). This is the same as Kullback–Leibler divergence loss between \( N(\mu, \sigma) \) and \( N(\mu_t, 1) \) of the ground-truth datapoint. Using this loss function, we train our NPN model to predict an estimate \( \mu \) and aleatoric uncertainty \( \sigma \).

Now, we calculate the value at risk using the prediction of the NPN model. The value at risk (VaR) is defined as the best objective value that can be achieved with \( \alpha \) probability, which is equivalent to the \( \alpha \) quantile of the distribution. Considering a Gaussian distribution and 95% confidence bound as per [24], [36], [37], the parameterized VaR for interval \( I_t \) is given by

\[
VaR_{I_t} = \mu + 1.65\sigma. \tag{2}
\]

Optimizing this metric in GOSH allows it to minimize the mean latency (\( \mu \)) as well as reduce uncertainty (\( \sigma \)) in response time, leading to a lower probability of overshooting deadline and hence lower SLA violation rates.

3.3 LCB Exploration

Motivation. Prior work shows that exploration of the state space based on the uncertainty estimates of heteroscedastic models can provide a performance boost in dynamic scenarios [20]. In particular, methods like \( \epsilon \)-greedy, softmax and Lower-confidence bound (LCB) have been popular [20], [38]. However, due to the adaptability of LCB exploration, we use LCB to trade off between greedy minimization of the mean latency and error reduction by employing uncertainty-based exploration [24 § 17.3.4]. However, it is known that uncertainty modeling in such NPNs only includes the aleatoric uncertainty [39]. Thus, in this work, we use the LCB metric with episodic uncertainty.
Teacher-Student Network. To implement the LCB exploration strategy, we need estimates of the epistemic uncertainty for each input \([S_t, φ(Δ_t)]\). Prior work leverages models like BNNs or Monte-Carlo Dropout to achieve this by sampling the output multiple times and quantifying the variance in the output to determine the epistemic uncertainty \([40]\). However, the measure of epistemic uncertainty obtained from this method is not in closed form and hence cannot be differentiated. Having closed-form solutions is better for second-order optimization as finite difference methods tend to be slow and imprecise \([24 § 2.3.2]\), having a negative effect on the scheduling time.

To solve this problem, we employ a teacher-student learning model, similar to the one in \([41]\), with an overview given in Figure 3. Compared to other methods like approximated variance propagation or sampling based propagation \([40]\), a teacher-student model is able to adapt quickly to changing scenarios. The teacher network, denoted as \(g(x_t; θ')\), is a FCN model that takes \([S_t, φ(Δ_t)]\) as an input and outputs an estimate of \(O_t\). However, in this model, we use Monte-Carlo Dropout (MCD) for Bayesian inference at test time \([42]\). Unlike conventional dropout, MCD enables dropout at inference time as well. This allows us to run inference multiple times (say \(M\)) and obtain a stochastic output. We can then calculate the standard-deviation of the resultant output samples. This deviation quantifies the epistemic uncertainty (denoted as \(ξ\) of the model as described in \([43]\). In contrast, the student network, denoted as \(h(x_t; θ'')\), is another identical FCN model without the MC Dropout. It takes \([S_t, φ(Δ_t)]\) as an input and directly outputs an estimate of the epistemic uncertainty \(ξ\) (denoted as \(ξ\)). Unlike the teacher, the output epistemic uncertainty of the student is differentiable, allowing quick and precise second-order optimization. Both teacher \((g)\) and student \((h)\) networks are trained using the Mean Square Error (MSE) loss such that for a dataset \(Λ\) as described previously,

\[
\mathcal{L}(g, Λ) = \frac{1}{T} \sum_{(x_t, y_t) \in Λ} (g(x_t; θ') - y_t)^2 \\
\mathcal{L}(h, Λ) = \frac{1}{T} \sum_{(x_t, y_t) \in Λ} (h(x_t; θ'') - ξ_t)^2.
\]

Assuming we use affine activations, the student-network is a differentiable closed-form function; its output \(ξ\) is differentiable with respect to the input.

Now that we have the VaR from the NPN model and an estimate of the epistemic uncertainty, we use the LCB optimization where the final objective function to minimize becomes

\[
LCB_t = VaR_t - k \cdot ξ_t, \tag{5}
\]

where \(k\) is the exploration factor.

Minimizing the first term aims to reduce the chance of an SLA violation (considering response time as part of \(O_t\)) and can be termed the exploitation part of the algorithm. Minimizing the second term, i.e., maximizing the epistemic uncertainty helps the model explore in cases with limited data or knowledge. This interactive dynamic between the exploration and exploitation allows the GOSH scheduler to quickly adapt while maintaining low SLA violation rates.

3.4 Second-Order Optimization

We now describe how we optimize the scheduling decision. To reduce the number of iterations, avoid saddle points and shorten the scheduling time, we employ a second-order stochastic optimization approach which dynamically incorporates the curvature of the surrogate function \([44]\). Exploiting the improved convergence properties of the second order algorithms over first order ones, our approach gives low scheduling times and improved QoS objective scores.

For a trained neural approximator \(f\), at the start of each interval \(I_t\), a typical second-order approach (Newton methods) optimizes the decision matrix \(φ(Δ)\) by the following rule (\(γ\) is the learning rate)

\[
φ(Δ_{n+1}) ← φ(Δ_n) - γ \cdot [∇^2 φ(Δ_n) f]^{-1} \cdot ∇ φ(Δ_n) f,
\]

where \(f\) is a shorthand for \(f([S_t, φ(Δ_t)]; θ)\). This operation is iteratively performed until the absolute value of the gradient is more than the convergence threshold \(ε\).

Computing the second-order derivative, or Hessian in a multivariate case, allows us to make a quadratic approximation of the objective function and estimate an appropriate step size to reach a local minimum \([24 § 6]\). For instance, it is known that if \(f\) is quadratic and its Hessian is positive definite, one can reach its global minimum in a single step using the Newton method. Moreover, second-order methods provide resilience against ill-conditioned objective function landscapes and guarantee convergence to second-order critical points \([44]\).

However, computing the inverse of the Hessian is known to be computationally expensive (cubic time-complexity with matrix size). In this endeavor, prior work proposed Hessian free approaches like secant or Quasi-Newton methods \([24 § 6.3]\). Moreover, it has been shown that the exact computation of Hessian is not required and an approximate of the diagonal of the Hessian is sufficient for low-cost iterations \([45]\). One such method for computing this Hessian diagonal for neural networks is the Hutchinson’s method with a linear computational complexity \([46]\). However, even an approximate Hessian can give local curvature information, which is misleading. This is alleviated by adapting the Hutchinson’s method and using the moving average of the approximate Hessian diagonal to speed up convergence. Thus, for Hutchinson’s estimate of the Hessian
diagonal of $f([S_t, \phi(D_n)]; \theta)$ at $I_t$, denoted as $H_t(f)$, we compute the moving average $\hat{H}_t(f)$ as
\[
\hat{H}_t(f) \leftarrow \omega \cdot H_t(f) + (1 - \omega) \cdot H_t(f),
\]
where $\omega$ is the momentum parameter. Hence, the update equation becomes
\[
\phi(D_{n+1}) \leftarrow \phi(D_n) - \gamma \cdot \hat{H}_t^{-1}(f) \cdot \nabla_{\phi(D_n)} f. \tag{6}
\]

Unlike prior efforts that utilize Hutchinson’s method for lightweight second-order optimization like [44, 47], we perform iteration based moving averages and not spatial averaging. This allows our model to be robust to sudden variations in reward metrics in volatile workload settings. The main overhead of this approach is the computation of the approximate of the Hessian diagonal using Hutchinson’s method. Also, it is possible to improve the estimate of the Hessian diagonal by increasing the iteration count of Hutchinson’s method. However, one-step iteration performs as well in practice, giving low per-iteration computational overhead compared to the GOBI approach [44]. Comparisons of the scheduling overheads are shown later in Section 5.6.

4 The GOSH and GOSH* Schedulers

In the GOSH approach, we combine the LCB metric given by (3) and second-order optimization in [6]. Thus, our update equation becomes
\[
\phi(D_{n+1}) \leftarrow \phi(D_n) - \gamma \cdot \hat{H}_t^{-1}(LCB_t) \cdot \nabla_{\phi(D_n)} LCB_t, \tag{7}
\]
where $\hat{H}_t(LCB_t)$ denotes the moving average of the Hessian diagonal estimate of LCB_t. As we utilize the output of the student network for the epistemic uncertainty, we can generate a closed-form second-order Hessian estimate (see Figure 3).

To optimize the QoS parameters, we consider a standard objective function that focuses on energy consumption and response time as is done in prior work [3]. For interval $I_t$,
\[
O_t = \alpha \cdot AEC_t + \beta \cdot ART_t, \tag{8}
\]
where $AEC_t$ and $ART_t$ are the average energy consumption of the fog environment in $I_t$ and average response time of tasks leaving at the end of $I_t$. Here, $\alpha$ and $\beta$ (such that $\alpha + \beta = 1$) are hyper-parameters that can be set by users in line with the application requirements. Typically, in real-life settings, these values are around 0.5 [3]. For an energy-constrained setting, a higher $\alpha$ value is used, whereas for latency-critical tasks, a higher $\beta$ value is used.

We also extend GOSH to benefit from co-simulated results. GOSH* uses a simulator to execute the scheduling decision predicted by GOSH and the utilization metrics of the next state using an LSTM (Section 3). This allows GOSH* to make more informed decisions and hence reach better objective scores than GOSH, spending additional computational overhead in return for increased accuracy. We will show that GOSH* is more suitable for environments with resource-constrained fog brokers, whereas GOSH* reaches a better objective score but requires heavier computational resources.

Algorithm 1 The GOSH scheduler

Require:
Pre-trained stochastic function approximator $f(x; \theta)$
Pre-trained Teacher-Student models $g(x; \theta')$, $h(x; \theta'')$
Dataset used for training $\Lambda$; Convergence threshold $\epsilon$
Iteration limit $L$; Learning rate $\gamma$; LCB parameter $k$
Value at Risk parameter $\alpha$

1: procedure MINIMIZE($D_t$, $f$, $g$, $h$, $z$)
2: Initialize decision matrix $\phi(D)$; $i = 0$
3: do
4: $x \leftarrow [z, \phi(D)]$ \Comment*[r]{Concatenation}
5: $\mu, \sigma \leftarrow f(x; \theta)$ \Comment*[r]{Stochastic Prediction}
6: $\xi \leftarrow h(x; \theta'')$ \Comment*[r]{Uncertainty Prediction}
7: $LCB \leftarrow VaR(\mu, \sigma, \alpha) - k \cdot \xi$ \Comment*[r]{LCB metric}
8: $\phi(D) \leftarrow \phi(D) - \gamma \cdot \hat{H}_i^{-1}(LCB) \cdot \nabla_{\phi(D)} LCB$
9: $i \leftarrow i + 1$
10: while $|\hat{H}_i^{-1}(LCB) \cdot \nabla_{\phi(D)} LCB| > \epsilon$ and $i \leq L$
11: Convert matrix $\phi(D)$ to scheduling decision $D^*$
12: return $D^*$
13: end procedure
14: procedure INITIALIZE(scheduling interval $I_t$)
15: if ($t == 0$)
16: \Comment*[r]{Output for the previous interval}
17: return random decision $D$
18: end procedure
19: procedure TUNE(scheduling interval $I_t$)
20: $x_t \leftarrow [S_t, \phi(D_t)]$
21: $\xi_t \leftarrow Sample(g(x_t; \theta'))$
22: $k, \xi_M \leftarrow Update(\xi, \psi)$
23: $\Lambda_{t-1} \leftarrow \{(x_{t-1}, \Omega_{t-1})\}$
24: Fine-tune $\theta, \theta'$ with $\Lambda_{t-1}$ and loss as in 1, 3
25: Fine-tune $\theta''$ with $\xi_t$ and loss as in 4
26: end procedure
27: procedure GOSH(scheduling interval $I_t$)
28: $D \leftarrow INITIALIZE(I_t)$
29: Get $S_t$
30: $D_t \leftarrow MINIMIZE(D, f, g, h, S_t)$
31: TUNE($I_t$)
32: return $D_t$
33: end procedure

4.1 Model Training

As described previously in Section 3.2, the models $f$, $g$ and $h$ are trained using a dataset $\Lambda = \{(S_t, \phi(D_t)), O_t\}_{t=0}^{T}$ as discussed in Section 3. The model $f$ is trained using the aleatoric loss (1), whereas $g, h$ are trained using MSE loss given in (3) and (4). We train using the AdamW optimizer [48]. Using these models, we obtain the LCB metric [5].

For GOSH*, we train models $f^*$, $g^*$ and $h^*$ which take input $[S_t, \Omega_t, \phi(D)]$, where $\Omega_t$ is a simulated estimate of $O_t$. We also train a next-state predictor using a LSTM network (Section 5). This model uses the state history to predict the next state, where the predicted state is denoted as
\[
\hat{S}_t \leftarrow LSTM([S_{t'}, \forall t' < t]).
\]
This LSTM model is also trained using the $\Lambda$ dataset.
Algorithm 2 The GOSH* scheduler

Require:
- Pre-trained stochastic function approximator \( f^*(x; \theta) \)
- Pre-trained Teacher-Student models \( g^*(x; \theta'), h^*(x; \theta'') \)
- Pre-trained LSTM model \( LSTM(\{S_t|0 < t < T\}) \)

1: \textbf{procedure} GOSH* (scheduling interval \( I_t \))
2: \( \mathcal{D} \leftarrow \text{INITIALIZE}(I_t) \)
3: \( S_t \leftarrow \text{LSTM}(\{S_t|0 < t < T\}) \)
4: \( \bar{S}_t \leftarrow \text{LSTM}(\{S_t|0 < t < T\}) \) \quad \text{\(\triangleright Simulation\)}
5: \( D_t \leftarrow \text{GOSH}(I_t) \)
6: \( \bar{O}_t \leftarrow \text{S}(\mathcal{D}(A_t), \bar{S}_t) \)
7: \( \mathcal{D}_t \leftarrow \text{MINIMIZE}(\mathcal{D}, f^*, g^*, h^*, [S_t, \bar{O}_t]) \)
8: \( \text{TUNE}(I_t) \)
9: \( \text{return } \mathcal{D}_t \)
10: \textbf{end procedure}

4.2 Dynamic Exploration Weight

As we show in Section 5.6, keeping a static value of the exploration weight \( k \) is not ideal as the objective scores are very sensitive to its value. Hence, GOSH and GOSH* use a dynamic exploration weight \( k \), which is updated based on the epistemic uncertainty value in each scheduling interval. Thus, we update the \( k \) parameter such that it increases when the epistemic uncertainty increases, indicating more exploration required and decreases otherwise, while at the same time remaining fairly insensitive to the step-size parameter.

We use a feedback based weight control scheme similar to the one in \[49\]. At run-time, we maintain an exponential moving average of the epistemic uncertainty metric \( \xi \) (denoted as \( \xi_{MA} \)). Thus, at each interval \( I_t \), \( \xi_{MA} \leftarrow \psi \cdot \xi_{MA} + (1 - \psi) \cdot \xi_t \), where \( \psi \) is the exploration momentum parameter. Now, the value of \( k \) is updated as per the rule

\[
    k = \begin{cases} 
    (1 + \delta) \cdot k, & \text{if } \xi > (1 + \delta) \cdot \xi_{MA} \\
    (1 - \delta) \cdot k, & \text{if } \xi < (1 - \delta) \cdot \xi_{MA} \\
    k, & \text{otherwise,}
    \end{cases}
\]

where \( \delta \) is the step-size.

4.3 Scheduling

An overview of the GOSH scheduler is given in Algorithm 1. After training models \( f, g \) and \( h \) and obtaining LCB metric, we optimize \( \phi(D_t) \) as per the rule (7) until the step-size \( H^{-1}_t(LCB_t) \cdot \nabla \phi(D_t) LCB_t \) is greater than the convergence threshold \( \epsilon \) (line 10). We also use Implicit Gradient Regularization in the \( \phi(D_t) \) optimization steps for numerical stability in high aleatoric uncertainty cases \[50\]. This adds a loss term that imposes structural constraints to the gradient values making them more robust to noisy parameter perturbations \[50\].

For interval \( I_{D_t} \), we initialize a random decision and for \( I_{t}, t > 0 \) we initialize the decision to be the same as \( D_{t-1} \) (lines 16-17). We obtain the current state of the system which includes the IPS, RAM, Disk and Bandwidth utilizations of the hosts and tasks as \( S_t \) (line 29). We utilize the MINIMIZE function, given in Algorithm 1, to find the decision at each interval \( I_t \) (line 30). We then fine-tune the models \( f, g \) using the latest datapoint \( (x_{t-1}, O_{t-1}) \) (line 24). Finally, we sample and obtain the epistemic uncertainty from \( g \) as \( \xi_{t} \) and fine-tune \( h \) using MSE loss (line 25). This continuous fine-tuning allows the models to adapt in dynamic scenarios.

An overview of the working GOSH* scheduler is given in Algorithm 2. Here, we employ GOSH, next-state predictor (LSTM model) and a simulator (denoted as \( S \)). Using the predicted next-state \( \bar{S}_t \) and an action of interest \( D_t = \text{GOSH}(I_t) \), we use the simulator to predict the objective score at the end of the current interval \( O_t \leftarrow S(D(A_t), \bar{S}_t) \) (line 6).

5 PERFORMANCE EVALUATION

5.1 Evaluation Setup

To show the performance of the GOSH and GOSH* models against baselines methods, we use two test-beds, physical and simulated platforms. The former for precise comparison and the latter for large-scale experiments. For our experiments, we keep \( \alpha = \beta = 0.5 \) in \[5\] and \( \delta = 0.1 \) in \[9\] since the same values are used in the baselines we compare with \[3\], \[9\], \[49\]. These values have been shown to represent a characteristic set of deployments closely resembling the ones in practical settings \[51\], \[52\]. We get similar trends for other values.

Physical Setup: Motivated from prior work \[3\], \[9\], we use Microsoft Azure VMs to create a heterogeneous fog test-bed. The configuration consists of 10 VMs and is as follows:

- 4 Azure B2s (dual core) VMs in London, UK.
- 2 Azure B4ms (quad core) VMs in London, UK.
- 2 Azure B4ms (quad core) VMs in Virginia, USA.
- 2 Azure B8ms (octa core) VMs in Virginia, USA.

The fog broker node was a system situated in London, UK and with configuration: Intel i7-10700K CPU, 64GB RAM and Windows 10 Pro OS. All neural network models are trained in the broker node.

Simulated Setup: We consider 50 host machines as a scaled up version of the physical setup. Here, each category has five times the instance count to test models in a large-scale fog environment as considered in prior art \[8\], \[53\].

We run all experiments for 100 scheduling intervals, with each interval being 300 seconds long, giving a total experiment time of 8 hours 20 minutes. We average over five runs and use diverse workload types to ensure statistical significance. We truncate the first 10% of the scheduling intervals to ensure that the system reaches a stable state and minimize noise in the results.

5.2 Workloads

We use popular and real-world workloads to test GOSH and GOSH* models. For our simulator, we use the Bitbrain\[2\] workload traces dataset \[54\]. These traces are generated by running computational analysis applications on 1750 VMs. The workloads consist of data intervals of 5 minutes, including the CPU, RAM, Disk and Bandwidth utilization of all tasks. We use both random and sequential computation traces, sampling them uniformly at random when generating workload containers.

For our physical setup, we use Defog benchmark applications \[55\]. We use the COSCO container orchestration
platform [3] to map these fog benchmark applications to containers run in our physical setup. These include the popular deep learning bag-of-task applications: Yolo, PocketSphinx and Aeneas. At the beginning of each scheduling interval we create Poisson(λ) tasks with λ = 1.2 tasks for physical and λ = 5 tasks for the simulated setup [9].

5.3 Model Training and Assumptions

For the GOSH and GOSH* algorithms, we use standard NPN models with the following characteristics adapted from [8]. We use the following non-affine activation functions for our neural approximators to be differentiable for all input values. Consider the number of hosts as N and the maximum number of tasks as M.

1) Input layer of size |S_i| + M × N for GOSH and |S_i| + M × N + 1 for GOSH*. The non-linearity used here is softplus as in [9]. Note, N may vary from 10 in tests in the physical environment to 50 in the simulator.
2) FC/NPN layer of size 128 with softplus activation.
3) FC/NPN layer of size 64 with tanhshrink activation.
4) FC/NPN layer of size 1 with sigmoid activation.

The f model has NPN layers with same sizes as above. The g and h models had FC layers with the g model using 50% dropout for Bayesian inference as in prior work [36].

We generate training data for GOSH by running a random placement scheduler for 2000 scheduling intervals to capture diverse state-space. For GOSH*, we create a separate dataset by running a random scheduler with pre-trained dataset of the GOSH scheduler to include the O_t in the data-points. To implement and test GOSH and GOSH* models, we use the COSCO framework implemented in Python [3].

The gradient calculation and optimization (Equation 7) are performed using the Autograd package [56]. At training time, we use 50% dropout in the teacher network and learning rate 10^{-5} in the AdamW optimizer. We perform five-fold cross-validation for statistical significance, where we randomly sample 80% of data to get the training set and the rest as the cross-validation set. All models are trained using the PyTorch 1.8 library. To prevent model overfitting, we use decoupled adaptive weight regularization from [48] using the weight decay parameter of 10^{-4}. The values of the learning rate and the regularization hyper-parameters are obtained via grid search using the Ray Tune API in PyTorch [57]. We also use the early stopping criterion to train the models [55]. The hyperparameter search is performed on the mean five-fold cross-validation accuracy.

5.4 Baselines and Evaluation Metrics

We evaluate the performance of the GOSH/GOSH* model against the state-of-the-art approaches discussed in Section 2 These include the pessimistic-optimistic UCB optimization approach POND [11], deterministic surrogate based methods GOBI and GOBI*, A3C [9] and the HGP model, where we use the LBFGS method with a HGP surrogate model for optimization as done in [20], [21].

We also compare the proposed methods with ablated models, where we replace either one of second-order optimization or heteroscedastic modeling components with simpler versions as described below.
- HGOBI/HGOBI*: GOSH with first-order optimization (as in GOBI) instead of second-order. Thus, LCB_t was optimized using first-order gradient descent. HGOBI* is the co-simulator aided extension of HGOBI.
- SGobi/SGobi*: GOSH with updating the output of an FCN neural model (as in GOBI). Thus, the optimization was done as per [6]. SGobi* is the co-simulator aided extension of SGobi.

Comparison with the ablated models allows us to study individual contributions of both components.

Evaluation Metrics: We use the following evaluation metrics in our experiments motivated from prior works [3], [59].

1) Energy: To measure the energy consumption, we use the power consumption models taken from the commonly-used SPEC benchmarks repository [60].
2) SLA Violations: A task’s SLA is violated if its response time is greater than the deadline. We consider the relative definition of SLA (as in [3]) where the deadline is the 95th percentile response time for the same application type on the state of the art baseline GOBI*. To ensure sufficient sample size, we run the GOBI* baseline for 1000 scheduling intervals and evaluate the 95th percentile response times for each application. We define the fraction of SLA violations for each application as the ratio of the application instances where SLA was violated to the total number of instances running in a trace of this type. Also, fraction of SLA violations for a scheduler is defined as the ratio of the application instances where SLA was violated to the total instances run in a trace across all application types.
3) Fairness: We use the Jain’s fairness index over the IPS of the running tasks in the system.
4) Average Migration Time which is the average time for task (container) migrations.

We also compare the Response Time, Scheduling Time and Average Wait Time of all executed tasks. For a bag-of-task workload model, each workload container is composed of multiple tasks (inference over different data inputs). Each task is independent of the other task within the same running application instance, allowing parallel execution. However, when an application instance, realized as a Docker container, is scheduled on a host with limited available resources, the tasks within the application may be run sequentially. We define the average response time of a scheduler as the mean response time of all completed tasks in an execution trace using the particular scheduler for task placement and migration. We define the average response time per application as the time it takes to execute all running tasks within the same application instance. This means the timestamp from the start of execution of the first task to the timestamp when the last task completes execution.

5.5 Results and Ablation Analysis

We now provide comparative results showing the performance of the GOSH and GOSH* schedulers against the
baselines and ablated models (described in Section 5.4). Figure 4 shows results for the physical setup with 10 Azure hosts and Table 2 for the simulation platform with 50 hosts.

Figure 4(a) shows the average energy consumption per task for the Azure hosts, with Figure 4(h) showing energy consumption with execution time. GOSH and GOSH* (150.9 – 157.6 KW-hr respectively) have lower energy consumption than the GOBI* approach by 17.91% – 21.40% where GOBI* has the least consumption among the baselines. This is because of the ability of the second-order optimization approach to reach better objective scores and hence reduce the $AEC_t$ metric, as the SGOBI/SGOBI* models also reach low energy consumption values. Further, the reduced average response time for GOSH and GOSH* models gives a higher number of completed tasks (Figure 4(i)) and hence lower average energy consumption. A similar trend is also seen for the simulation setup (Table 2) where GOBI* achieves the least energy consumption among the baselines (211.05 KW-hr) and GOSH/GOSH* improve upon this by 15.13% – 16.29%.

Figure 4(b) compares the average response time for each scheduler. Again, the GOBI* scheduler has the least average response time of 154 ± 29 seconds. Here, GOSH* has much lower response times (28.57% lower than GOBI*) and the GOSH scheduler has 28.29% lower than the GOBI model. Again, this is because of the second-order optimization, which gives low scheduling overhead and can reach better objective scores of $ART_t$. We see here that the ablated model HGObi* has higher response times than the GOBI* model. Specifically, HGObi* gives 16.88% higher response time than GOBI*. On the contrary, the HGObi* model has a significantly lower SLA violation rate compared to the best baseline GOBI* (relative improvement is 44.21%) as seen in Figure 4(d). This is because the HGObi* model aims to minimize the value-at-risk instead of the mean response time, reducing the chance of violating the SLA deadline. Among the baselines, the GOBI* model has the lowest SLA violation rate (5.82%) with the HGP model coming second
(8.21%). The GOSH and GOSH* models beat the GOBI* scheduler giving SLA violation rates of just 3.04% − 1.11%. Similar trends are seen in the case of 50 simulated hosts where the GOSH and GOSH* models give 14.25% − 19.16% lower average response time and 55.98% − 66.23% lower SLA violation rate.

For the three applications, the average response time and SLA violation for each scheduler are shown in Figures 4(g) and 4(h). The high response time of the POND baseline is mostly attributed to frequent migrations performed by this method (see Figure 4(e)). On the other hand, GOSH* is the most parsimonious strategy in task migrations, allowing lower response times than other approaches. The deviations from the 5% mark in Figure 4(h) is due to the stochasticity in the workloads, motivating us to fine-tune the model at each interval (line 8 in Alg. 2). Clearly, among the DeFog benchmark applications, Yolo takes the maximum time. As seen previously, Figure 4(h) shows the SLA violations rates for each application. The SLA violation rates of the SGOBI and SGOBI* methods are higher than the heteroscedastic models GOSH, GOSH*, HGOBI and HGOBI*. Even the HGP baseline has a lower SLA violation rate than the SGOBI model for the Yolo application. This shows the importance of having heteroscedastic modeling in estimating QoS scores. These improvements are at the cost of task execution fairness.

In terms of the scheduling time, as seen in Figures 4(i) and 4(j), the co-simulation variant of GOBI, HGOBI, SGOBI and GOSH have higher scheduling times. This is due to the additional step that calls the co-simulator to estimate the QoS scores of the next interval (see line 6 in Alg. 2). GOBI has the least scheduling time among baselines, showing the importance of gradient-based optimization. However, the second-order optimization further reduces the scheduling time of SGOBI and SGOBI* by 11.79% − 20.90% compared to GOBI and GOBI* respectively in the large-scale setting of 50 hosts (see Table 2). However, having a more sophisticated neural network (NPN) in HGOBI and HGPOBI increases the scheduling time compared to GOBI and GOBI* due to a slight increase in the time taken to fine-tune the model (line 31 in Alg. 1 and line 8 in Alg. 2). A more detailed comparison of the model overheads is given in Section 5.6. Figure 4(c) shows that the GOBI* baseline is the fairest among all models with a Jain’s fairness index of 0.75. GOSH* has the highest fairness of 0.57, higher than all baselines other than GOBI*. The average wait times for applications with execution is shown in Figure 4(k). A3C has high wait times due to the inability of the RL baseline to quickly adapt in cases of hosts running and capacity. Comparing other metrics like fairness, GOSH and GOSH* have lower Jain’s fairness index value than the GOBI and GOBI* models. Among all models, the GOBI* model has the highest fairness index, with GOSH and GOSH* having only 0.26 and 0.57 respectively. The scheduling time is lowest for the GOBI* ablated model of 2.33 seconds in the physical setup and 5.46 seconds in the simulated setup. Moreover, the scheduling overhead of GOSH compared to GOBI is 12.72% and that of GOSH* compared to GOBI* is 15.22%. Similar overheads are observed for the 50 simulated hosts case of 16.39% − 28.9%.

### Table 2

| Model   | Energy | Response Time | SLA violation | Scheduling Time | Fairness | Migration Time | Wait Time |
|---------|--------|---------------|---------------|----------------|----------|----------------|-----------|
| POND    | 326.21 | 2083.81 ± 176.25 | 2.93E-01 | 18.94 ± 0.01 | 0.56 ± 0.01 | 1.10 ± 0.07 | 114.28 ± 0.32 |
| A3C     | 270.28 | 2017.52 ± 164.76 | 3.29E-01 | 15.77 ± 0.03 | 0.71 ± 0.02 | 0.72 ± 0.06 | 206.34 ± 0.26 |
| HGP     | 364.20 | 2219.36 ± 202.75 | 1.32E-01 | 21.56 ± 0.00 | 0.60 ± 0.01 | 0.21 ± 0.01 | 60.64 ± 0.12 |
| GOBI    | 214.29 | 1767.29 ± 126.00 | 1.51E-01 | 6.19 ± 0.00 | 0.53 ± 0.01 | 0.84 ± 0.01 | 26.98 ± 0.07 |
| GOBI*   | 211.05 | 1487.06 ± 123.98 | 7.02E-02 | 13.73 ± 0.00 | 0.39 ± 0.01 | 0.31 ± 0.02 | 4.13 ± 0.04 |
| HGOBI   | 209.22 | 1557.84 ± 137.79 | 5.22E-02 | 11.22 ± 0.01 | 0.53 ± 0.01 | 0.38 ± 0.02 | 24.90 ± 0.11 |
| HGOBI*  | 215.29 | 1295.32 ± 157.90 | 3.22E-02 | 17.33 ± 0.01 | 0.59 ± 0.01 | 0.31 ± 0.02 | 20.81 ± 0.15 |
| SGOBI   | 182.21 | 1324.99 ± 84.07  | 6.40E-02 | 5.46 ± 0.00 | 0.48 ± 0.02 | 0.41 ± 0.03 | 14.41 ± 0.08 |
| SGOBI*  | 179.09 | 1291.31 ± 96.20  | 4.99E-02 | 10.86 ± 0.00 | 0.46 ± 0.01 | 0.35 ± 0.01 | 12.73 ± 0.05 |
| GOSH    | 179.10 | 1275.80 ± 89.89  | 3.09E-02 | 7.98 ± 0.01 | 0.42 ± 0.01 | 0.19 ± 0.01 | 8.31 ± 0.07 |
| GOSH*   | 176.66 | 1202.39 ± 77.55  | 2.37E-02 | 15.98 ± 0.01 | 0.51 ± 0.02 | 0.33 ± 0.02 | 12.23 ± 0.09 |

Fig. 5: Sensitivity Analysis for $k$ (0.1).
5.6 Additional Experiments

Modelling Accuracy: Experiments on the dataset collected using a random scheduler show that the NPN model is able to give lower KL divergence between the predicted output and the ground-truth compared to the baseline FCN model, even though the Mean-Square Error is slightly higher (0.5 – 8.9%, see Table 3). The NPN models perform even better than the HGP models used in prior work [20], [21], giving more accurate predictions and hence improving QoS.

Sensitivity Analysis: We now show the importance of dynamically updating the value of the $k$ parameter based on the epistemic uncertainty. We conduct our experiments on the simulated setup with the Bitbrain workload traces. We run the GOSH model for 200 intervals with static values of $k$ and one with $k = 5$ initialization being updated at each interval as per (9). We keep the workloads as Bitbrain random traces for the first 100 intervals and the sequential traces for the next 100 intervals. The “Changed Workload” vertical line in Figure 5 highlights the instant of this workload transition. We average our results over 20 runs for 5 cases of static $k$ with the dynamic $k$ setup.

As is apparent from Figure 5(a), the aleatoric uncertainty in the random traces is higher than the sequential traces. The sharp fall in the epistemic uncertainty (Figure 5(a)) is due to the fact that the model explores and quickly reaches a local region of “well known” state space. Figure 5(b) shows the average response time per interval of leaving tasks. The converged response time (before the 100th and after the 150th interval) is lower for low values of $k$ as a higher relative weight is given to the value-at-risk metric. However, as $k$ increases, the model takes more time to adapt to the new scenario, as shown by the slopes in Figure 5(d) indicating that higher $k$ enforces higher exploration and swift adaptability. Finally, Figure 5(e) shows that the average response time over the complete 200 interval duration is also minimum for the dynamic $k$ setup. This indicates that dynamically adapting the $k$ parameter is crucial for quick adaptability in volatile environments.

Agility Testing: Figure 6 compares how quickly GOSH is able to adapt to the new setting compared to baselines. As we see, GOSH, HGOBI and HGP are able to adapt quickly to new settings compared to GOBI or SGobi. Both SGobi and GOBI take twice the time (40 intervals) to converge to the new scenario compared to GOSH. Thus, heteroscedastic modeling aids quick adaptability in the proposed methods.

Performance with Uncertainty: Figure 7 compares the performance of the GOSH approach with the baseline models as the aleatoric uncertainty of the system increases. We exclude the co-simulated extensions to focus on the effects of second-order optimization and heteroscedastic modeling. To test this, we vary the ratio of the sequential and random traces of the Bitbrain dataset (with the former having lower uncertainty than the latter). We run them sequentially with the sequential only workloads first. The sequential only workload traces give the lower bound (0.72) and random only traces give the upper bound (0.81) of the uncertainty considered across the x axis in Figure 7. In terms of energy consumption, response time and SLA violation rate, GOSH not only has better metric scores, but also does not face excessive performance drop in highly uncertain cases, thanks to its gradient regularization.

Overhead Comparison: Figure 8 compares the cost per iteration (in milliseconds), average number of iterations and the overall scheduling time for GOSH and baseline models. The per-iteration cost of SGobi is higher due to the additional step of Hutchinson’s method and moving average computation. However, the improvement due to the reduction in the number of iterations is more than this excess cost, so much so that the overall scheduling time of SGobi is lower than GOBI. This allows the overall overhead of GOSH due to the heteroscedastic modeling to not be as high as GOBI (33.65%) compared to the HGOBI approach (40.12%).

6 Conclusions and Future Work

In this work, we have presented multiple contributions including heteroscedastic modeling for aleatoric uncertainty estimation and value-at-risk calculation, a teacher-student
model for epistemic uncertainty estimation, efficient second-order optimization and feedback based exploration control. All these contributions allow GOSH and GOSH* to outperform the baseline models in terms of QoS metrics such as energy, response time and SLA violation by up to 18%, 27% and 82% respectively in a heterogeneous fog environment with real-world workloads. As shown in Figure 4(b) between GOSH and GOSH*, the former is more suitable for environments with a resource-constrained fog broker, whereas the latter reaches a better objective score but requires heavier computational resources.

For the future, we propose the following extensions. The GOSH and GOSH schedulers could be adapted for serverless frameworks allowing us fine-grained orchestration with increased productivity and flexibility, reducing the container management overheads. Further, other stochastic surrogate models like distributed Bayesian Neural Networks may be explored for decentralized scheduling with higher modeling performance and lower resource consumption overheads per host.

SOFTWARE AVAILABILITY

The code is available at [https://github.com/imperial-qore/COSCO/tree/gosh](https://github.com/imperial-qore/COSCO/tree/gosh) The Docker images used in the experiments are available at [https://hub.docker.com/u/shreshhtuli](https://hub.docker.com/u/shreshhtuli) The training datasets are available at [https://doi.org/10.5281/zenodo.4897944](https://doi.org/10.5281/zenodo.4897944) released under the CC BY 4.0 license.

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