Metal-insulator transition and magnetism in correlated band insulator: FeSi and Fe$_{1-x}$Co$_x$Si

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Abstract: The LDA+DMFT (local density approximation combined with dynamical mean-field theory) computation scheme has been used to study spectral and magnetic properties of FeSi and Fe$_{1-x}$Co$_x$Si. Having compared different models we conclude that a correlated band insulator scenario in contrast to Kondo insulator model agrees with FeSi band structure as well as experimental data. Coulomb correlation effects lead to band narrowing of the states near the Fermi level with mass renormalization parameter $m^* \approx 2$ in agreement with the results of angle-resolved photoemission spectroscopy (ARPES). Temperature dependence of spectral functions and magnetic susceptibility calculated in DMFT reproduces transition from nonmagnetic semiconductor to metal with local magnetic moments observed experimentally. Cobalt doping leads to ferromagnetism that has itinerant nature and can be successfully described by LDA+DMFT method.

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I. INTRODUCTION

The narrow-gap semiconductor FeSi demonstrates an interesting interplay between magnetic and electronic properties. Magnetic susceptibility temperature dependence shows maximum at 500 K and Curie-Weiss behavior at higher temperatures. While intrinsic magnetic susceptibility vanishes below 50 K, FeSi does not show any sign of spin ordering down to the lowest temperatures. Photoemission and optical experiments show an energy gap of about 60 meV at low temperatures that is gradually filled with temperature increase. A resistivity temperature dependence shows transition from a narrow gap semiconductor to a bad metal. Cobalt doping results in ferromagnetic metal state for Fe$_{1-x}$Co$_x$Si.

Several models have been suggested to explain the unusual temperature dependence of the FeSi physical properties ranging from spin fluctuations to phenomenological models assuming two narrow $d$-bands in the vicinity of the band gap. Such density of states (DOS) models are similar to a Kondo insulator description, and due to the striking similarities in the physical properties of these Kondo insulators it was claimed that FeSi is the first Kondo insulator containing no $f$-electrons.

Historically, the first FeSi model was proposed by Jaccarino et al. To describe the unusual magnetic susceptibility and specific heat a model DOS was proposed with extreme narrow band peaks around a small energy gap. Despite the fact that the model fitting results were in good agreement with experimental data for the susceptibility this picture contradicts a band structure calculation where no unphysical narrow bands were obtained.

The next model proposed to describe electronic and magnetic properties of FeSi was the Kondo insulator model. The motivation of applying the Kondo model to explain physical properties of FeSi was that the spin-fluctuation spectra of CeNiSn and FeSi are similar. According to this model, a set of localized atomic-like electron levels interact with a wide itinerant band. The insulating state scaled by a Kondo temperature $T_K$ is the result of a weak hybridization between the localized and itinerant bands. The implementation of the Kondo insulator model to FeSi compound is however questionable since the band structure of FeSi shows a strong hybridization between the Fe-3$d$ and Si-3$p$ states. Also the magnetic interactions in FeSi are essentially ferromagnetic and not antiferromagnetic, as it would be expected from an RKKY-picture. For all these reasons it is desirable to have a microscopic model based on the realistic band structure which can reproduce experimental data.

First-principle band structure calculations of Mattheis and Hammann have shown that energy gap value of 0.1 eV is essentially smaller than the width of the band above the Fermi level ($\sim 0.5$ eV). Band structures analysis led the authors to conclusion that hybridization between Fe-3$d$ and Si-3$p$ states is very strong. These results do not support the Jaccarino’s model as well as the Kondo scenario.

Recently, another model of a correlated band insulator (CBIM) was proposed by Kunes and Anisimov. Using the Dynamical Mean-Field Theory the authors have taken into account local dynamical correlations for a gapped LDA spectral function of FeSb$_2$ that experimentally demonstrates transition with temperature increase from nonmagnetic semiconductor to metal with local moments similar to FeSi. It was found that the DMFT energy gap is reduced due to correlation effects by a factor...
of two from its LDA value. Within the CBIM picture bands above and below the energy gap are formed by nonlocal bonding and antibonding orbital combinations. The on-site Coulomb interaction leads to a competition between localization and formation of nonlocal bonds. The DMFT calculations allowed to reproduce successfully temperature dependence of magnetic susceptibility, resistivity and optical conductivity experimentally observed in FeSb$_2$.

Recent angle-resolved photoemission experiments have proved validity of the correlated band insulator scenario for FeSi. The authors have found an effective band-mass renormalization $m^*/m \approx 2$. As a consequence the LDA band gap of 100 meV is renormalized by a factor of 0.5 to about 60 meV in agreement with other experimental data.

We summarized the parameter values of the models used to describe FeSi in Table I. The basic difference between Kondo insulator and correlated band insulator (CBIM) models is a ratio between energy gap value $E_{gap}$ and a width $W$ of the bands around the gap. While Kondo insulator model requires $W/E_{gap} << 1$ to give good results, CBIM uses $W/E_{gap} >> 1$ in agreement with FeSi realistic band structure.

**TABLE I: Classification of FeSi models.**

| Model                  | $W/E_{gap}$       | $E_{gap}$ (K) |
|------------------------|-------------------|---------------|
| Jaccarino’s model      | $W << E_{gap}$    | 1520          |
| Kondo insulator model  | $W = E_{gap}/2$   | 500           |
| CBIM (this work)       | $W >> E_{gap}$    | 5000          |

This paper is aimed to provide microscopic analysis of hybridization and correlation processes in FeSi. First we propose a simple band insulator model that captures the essential hybridization effects between Fe-3$d$ and Si-3$p$ states in FeSi (Section II A). This model demonstrates an energy gap that is five times narrower than the width of bands. In order to investigate correlation effects we define a density of states model based on LDA calculations for FeSi and solve it using the Dynamical Mean-Field Theory (Section II B). A strong renormalization of DOS near the Fermi level was found in the DMFT calculations that is in good agreement with a band narrowing observed in the recent ARPES experiments. Temperature increase in DMFT calculations results in transition from nonmagnetic insulator to a bad metal with local moments in agreement with experimental data. Having encouraged by these results we have investigated a doped FeSi model to study the magnetic properties of Fe$_{1-x}$Co$_x$Si alloys (Section III). We have demonstrated that a good agreement between calculated and experimental values for magnetization $M$ as a function of doping $x$ can be achieved using the LDA+DMFT method.

![FIG. 1: TB-LMTO energy band of FeSi obtained with different sets of atomic position parameters u(Fe) and u(Si).](image)

(a) Structure with u(Fe)=0.25 and u(Si)=0.75 corresponds to nonprimitive rocksalt structure that contains four FeSi formula units. Figures (b) and (c) are energy band results for two transitional structures with u(Fe)=0.23,u(Si)=0.76 and u(Fe)=0.19,u(Si)=0.79, respectively. Figure (d) corresponds to the real FeSi structure. Symmetry lines are chosen according to Ref. [12].

As first step we have studied effects of atomic positions shift on the band picture of FeSi. For that purpose we have carried out calculations using the Tight Binding Linear-Muffin-Tin-Orbital Atomic Sphere Approximation (TB-LMTO-ASA) method with conven-
tional local-density approximation (LDA)\textsuperscript{[14]} for real (simple cubic) structure (atomic positions u(Fe)=0.1358 and u(Si)=0.844), rocksalt (face-centered-cubic) phase (u(Fe)=0.25 and u(Si)=0.75) and for two model structures with atomic positions intermediate between those values (Fig. 1). The obtained bands agree with LAPW results for real and rocksalt phases\textsuperscript{[12]}. The fcc band structure contains several electrons and holes pockets near G and X points in the Brillouin zone that corresponds to a pseudogap in the energy spectrum in contrast to the real gap in the simple cubic structure. For intermediate structure with atomic position parameters u(Fe)=0.19 and u(Si)=0.79, the energy gap is open along all symmetry lines of the Brillouin zone with the exception of GM. One can see that there is a complete energy gap in the real FeSi structure. This result agrees with a conclusion of Mattheiss and Hamann\textsuperscript{[12]} that the energy gap state of FeSi results from the distortion of the pseudogapped rocksalt structure.

It is naturally to expect that the features of the FeSi electronic spectrum (such as the narrow gap and the peak above the Fermi level) are provided by Fe-3d and Si-3s, 3p states.\textsuperscript{[12,14]} To investigate the origin of the pseudogap state in the fcc phase we artificially scaled the hybridization strength between Si-3s, 3p and Fe-3d states. To do so off-diagonal Hamiltonian elements which describe the hybridization between Fe and Si atoms were multiplied by a coefficient $0 \leq \alpha \leq 1$. These results are presented in Fig. 2.

To simplify our analysis of the band structures one can consider dispersion curves along LG symmetry line where complete energy gap opens due to hybridization between Fe-3d and Si-3s, 3p states. Without hybridization ($\alpha = 0$) the wide silicon band crosses three narrow 3d-bands of iron for $k$-vectors along LG direction. At increasing hybridization strength (Fig. 2b and 2c) two of the iron bands strongly interact with silicon states while one of them remains practically unaffected by $d-p$ hybridization. The resulting dispersion curves of the fully hybridized system are presented in Fig. 2(d). It is clear that the pseudogapped state (Fig. 2d) originates from a strong hybridization of the wide silicon band ($\approx 10$ eV) with the relatively narrow iron band ($\approx 1$ eV). The narrow gap opens between antibonding hybridized band above and unhybridized band below the Fermi level.

While qualitatively this situation resembles the Kondo insulator picture with weakly hybridized wide and narrow bands, there are two essential quantitative differences. First of all the “narrow” band having width of an order of magnitude smaller than the “wide” band is still too wide in absolute value of about 1 eV. At second $d-p$ hybridization is so strong that “pure hybridization” gap in Fig. 2d is larger than 2 eV. The small value of the gap is not due to $d-p$ hybridization weakness but happens between hybridized and unhybridized bands.

Another argument against the Kondo scenario can be found from analysis of the two bands (Fig. 2d) forming a well-separated narrow peak above the Fermi level (Fig. 3). In Kondo system these bands should be associated with strongly localized atomic orbitals of an iron atom. To check this we have calculated Wannier functions for two bands above the Fermi level using a projection procedure.\textsuperscript{[12]} A spatial distribution for one of the calculated Wannier functions is shown in Fig. 3. The resulting Wannier functions correspond to a complex combination of 3d-states of iron and 3s-, 3p-states of silicon and are spread over whole unit cell of FeSi containing eight atoms. This picture is very far from localized atomic orbital needed for the Kondo scenario and supports the band insulator model.

We built an effective microscopic model (Fig. 4) for LG direction, that contains a minimal set of orbitals and reproduces the gapped state. The model silicon and model iron are described with one and two orbitals, respectively. The model Hamiltonian is given by

$$
H = \begin{pmatrix}
2t_3 \cos(k) & 2t_4 \cos(k) & 2t_1 \cos(k/2) \\
2t_4 \cos(k) & 2t_3 \cos(k) & 2t_2 \cos(k/2) \\
2t_1 \cos(k/2) & 2t_2 \cos(k/2) & 2t_3 \cos(k)
\end{pmatrix},
$$

where $t_1$, $t_2$, $t_3$ and $t_4$ are hoppings between model iron and silicon orbitals presented in Fig 4. We have estimated the hopping parameters of the LG model using...
FIG. 3: (Color online) Wannier function corresponding to a narrow band above the Fermi level (see Fig. 1d). The Wannier function is centered at a 3d orbital of iron atom (red spheres). We found about 40% of the electron density at the central atom and its iron neighbours. Green spheres correspond to silicon atoms.

The real band structure of the full Hamiltonian presented in Fig. 2. The obtained hopping integrals are $t_1=2.0$ eV, $t_2=3.0$ eV, $t_3=-1.2$ eV, $t_4=-0.25$ eV. These values are much larger than those calculated for localized systems$^{15}$ and are far outside of the values range needed for the Kondo insulator scenario.

The calculated model band structures with ($\alpha=1$) and without ($\alpha=0$) hybridization are presented in Fig. 5. One can see that our model results are in good agreement with those obtained from calculations with full Hamiltonian (Fig. 2). The substantial Fe-Si hybridization leads to splitting into a lower bonding and an upper antibonding bands with a non-bonding band in between. We have obtained a small gap semiconducting ground state with the energy gap value of 0.8 eV that is much smaller than the narrowest band width of 4.8 eV near the Fermi level. One should note that the small value of the energy gap is not a consequence of a weak Fe-Si hybridization and the minimal realistic band structure model of FeSi differs qualitatively from the Kondo insulator regime.

The proposed band model can be used to study Coulomb correlation problem within statical or dynamical mean-field approaches. However, as we will show below, it is possible to define an effective density of states model derived from the full DOS obtained in LDA calculation for the real crystal structure. Solution of this model by DMFT allows us to describe anomalous physical properties of FeSi.

B. Correlation effects

In this section we study the effects of the Coulomb correlation on the electronic structure and physical properties of FeSi using the Dynamical Mean-Field Theory. As an input DMFT requires a non-interacted Hamiltonian or a density of states (DOS).$^{20}$ The essential features of FeSi density of states obtained in LDA calculations (Fig. 6) are small energy gap $\approx 100$ meV and narrow ($\approx 0.5$ eV) peak above the Fermi level containing 0.5 electrons per spin per Fe atom. We have defined the model density of states (see filled area in Fig. 6) by cutting from the entire DOS area around Fermi energy with an integral equal to 1 electron per spin per Fe atom. The model density of states contains the main features of the FeSi spectrum, namely the energy gap (0.1 eV) and the narrow peak above the Fermi level (0.5 eV).

As impurity solvers of the DMFT problem we have used a Quantum Monte-Carlo method with Hirsch-Fye algorithm$^{20}$ (QMC-HF), a Continuous-time Quantum Monte-Carlo method with interaction expansion$^{21}$ (CT-QMC) and an exact diagonalization temperature dependent Lanczos$^{22}$ approach.

The value of the on-site Coulomb interaction parameter $U$ was chosen to be 1 eV that is close to the value...
used in Ref. 14. This rather small value can be justified by an effective screening of $d-d$ Coulomb interaction due to strong Fe-ligand hybridization as it was demonstrated in constrain DFT calculation of the Coulomb interaction parameter $U$ for LaOFeAs.

The resulting paramagnetic densities of states at $T = 232$ K calculated in DMFT using various impurity solvers are presented in Fig. 7. One can see that all methods result in a pseudogapped state with strongly renormalized density of states near the Fermi level. There are satellites at $\pm U/2$ which correspond to the lower and upper Hubbard bands.

The energy area around the Fermi level corresponds to quasiparticle states that are usually described as non-interacting bands renormalized by Coulomb correlations. The renormalization process can be understood by a low-frequency analysis of the dynamical mean-field equations. The lattice Green function is given by

$$G(k,\omega) = \sum_{\omega} (\omega - \Sigma(\omega) - \epsilon(k))^{-1},$$

where $\Sigma$ is a self-energy and $\epsilon(k)$ is a LDA spectrum. We expand the real part of the self-energy in the vicinity of the Fermi energy leaving only linear term:

$$\text{Re}\Sigma(\omega) \approx \text{Re}\Sigma(0) + \omega \frac{d\text{Re}\Sigma(\omega)}{d\omega} |_{\omega=0}.$$  \hfill (2)

Then Green function for specific wave vector $k$ is

$$G_k(\omega) \approx (\omega m^* - \epsilon(k))^{-1},$$

where $m^*$ is the effective band mass renormalization parameter

$$m^* \equiv 1 - \frac{d\text{Re}\Sigma(\omega)}{d\omega} |_{\omega=0}.$$ \hfill (4)

Equation (3) can be rewritten as

$$G_k(\omega) \approx \frac{Z}{\omega - \tilde{\epsilon}(k)},$$

where $Z \equiv 1/m^*$ is a quasiparticle weight and $\tilde{\epsilon}(k) \equiv \epsilon(k)/m^*$ is a new band dispersion. Therefore, the Coulomb correlation renormalization for quasiparticle states near the Fermi level results in a band structure narrowing by a factor of $m^*$ and a reduction of the corresponding spectral weight by a factor of $Z$ with the rest of the spectral weight transferred to upper and lower Hubbard bands at $\pm U/2$.

In our DMFT calculations the effective band mass renormalization parameter $m^* \approx 2$ was found in good agreement with the results of angle-resolved photoemission spectroscopy (ARPES)\cite{15} showing band narrowing by a factor of two in comparison with bands calculated in LDA.

Experimentally FeSi demonstrates transition with temperature increase from narrow gap semiconductor to bad metal.\cite{5} We have performed DMFT calculations at different temperatures and such an experimentally observed transition was successfully reproduced theoretically. The DMFT spectral functions calculated for different temperatures are presented in Fig. 8. The energy gap

FIG. 8: (Color online) Density of states obtained from QMC calculations at $T = 386$ K (black line) and $96$ K (orange line).
of about 50 meV found at \( T = 96 \) K agrees with experimental results of resistivity measurements which indicate a charge gap of about 60 meV. At \( T = 386 \) K the gap area is nearly completely filled by spectral weight transfer from sharp peaks near the gap resulting in the spectral function corresponding to a bad metal. The energy gap value obtained in the DMFT calculation is two times smaller than corresponding value from LDA band structure calculations (0.1 eV). That agrees very well with the effective band mass renormalization parameter \( m^* \approx 2 \) obtained in our DMFT calculations.

Optical spectroscopy experiments show gradual filling of the low-temperature energy gap with temperature increase till complete gap disappearance above room temperature. We have estimated the optical conductivity by a spectral function convolution using the following expression

\[
\sigma(\omega, T) = \frac{1}{\omega} \int d\epsilon N(\epsilon)N(\epsilon + \omega)[1 - f(\epsilon + \omega, T)],
\]

where \( N(\epsilon) \) is a spectral function obtained from DMFT calculations (Fig. 7) and \( f(\epsilon, T) \) is the Fermi distribution function. The calculated convolution together with experimental data for temperature dependent optical conductivity\(^6\) are presented in Fig. 9.

At low temperatures a well pronounced energy gap of about 0.05 eV can be observed in both experimental and theoretical curves. With temperature increase optical conductivity increases at the energies below 0.05 eV and finally at \( T = 386 \) K there is no any trace of the gap in the theoretical curve in good agreement with experimental data.

FeSi displays an unusual crossover in the vicinity of the room temperature from a singlet semiconducting ground state with a narrow band gap to a metal with an enhanced spin susceptibility and Curie-Weiss temperature dependence. All previous attempts to explain this behavior were based on the models assuming extremely narrow (< 1000K) peaks at the energy gap edges in DOS, while LDA calculations gave band width nearly an order of magnitude larger than that value. Our DMFT calculations demonstrate that the correlated band insulator model with realistic DOS can reproduce anomalous temperature dependence of the magnetic susceptibility for FeSi. We have computed \( \chi(T) \) as a ratio

\[
\chi(T) = \frac{M}{h},
\]

where \( h \) is a small uniform external magnetic field and \( M \) is an induced magnetization of the system. The comparison of the experimental and calculated magnetic susceptibilities is presented in Fig. 10. The calculated spin sus-

FIG. 9: (Color online) The convolution for FeSi model at 386 K (black line), 232 K (red line), 116 K (brown line) and 96 K (orange line). Inset: The experimentally observed optical conductivity taken from Ref. 4.

FIG. 10: (Color online) Spin susceptibility \( \chi(T) \) (in \( \mu_B^2/\text{eV} \)) from LDA+DMFT calculations (orange solid line) and from experiment\(^4\) (blue dashed line).

III. \( \text{Fe}_{1-x}\text{Co}_x\text{Si} \)

The correct theoretical description of magnetic properties for transition metal monosilicides such as for example MnSi and \( \text{Fe}_{1-x}\text{Co}_x\text{Si} \) alloys presents a longstanding problem. There has been a considerable amount of experimental and theoretical work on MnSi and \( \text{Fe}_{1-x}\text{Co}_x\text{Si} \), regarding their structural, magnetic and electronic properties. However, at the moment there is no satisfactory first-principles description of monosilicides magnetic
properties. For instance, in case of MnSi it was found that the experimental value of the magnetic moment is about $0.4 \mu_B$. Different first-principles calculations based on the density functional theory give much larger magnetic moment value of $1 \mu_B$\textsuperscript{26,27}.

Fe$_{1-x}$Co$_2$Si alloys are magnetic for almost all of the intermediate concentration regimes\textsuperscript{6,28,29} while the end compounds FeSi and CoSi are nonmagnetic, the latter being a diamagnetic semimetal. Fe$_{1-x}$Co$_2$Si system is also interesting for scientists due to the promising properties for spintronic device applications. For instance, in \textit{paper p}\textsuperscript{30} the authors have reported the discovery of a large anomalous Hall effect for Fe$_{1-x}$Co$_2$Si. They have demonstrated that the large effect is most likely intrinsic – derived from the band-structure effects rather than due to impurity scattering. They have proposed to consider the transition metal monosilicides as potential alternatives to the (GaMn)As and (GaMn)N which are the most popular materials for spintronics.

From theoretical side no calculation reported so far seems to reproduce correctly both magnetic moment value and Curie temperature of Fe$_{1-x}$Co$_2$Si system. To model Fe$_{1-x}$Co$_2$Si alloys the authors of \textit{paper p}\textsuperscript{31} have used the full potential linearized augmented plane-wave method in combination with a virtual crystal approximation (VCA) as well as with a supercell approach. The resulting magnetic moments agree with experimental values only for $x < 0.25$. Having supposed an important role of ordering and segregation they have simulated several alloy configurations for concentrations $x \leq 0.5$. The weighted average magnetic moment which was calculated through Boltzmann distribution is in reasonable agreement with experimental values. However, there are no experimental results which support the segregation and ordering phenomena. Moreover, the results of neutron measurement\textsuperscript{32} have demonstrated a random distribution of transition metals in Fe$_{0.5}$Co$_{0.5}$Si.

To simulate randomly distributed Fe$_{1-x}$Co$_2$Si alloys the authors of Ref. \textsuperscript{33} have used the combination of an exact muffin-tin orbitals method and a coherent potential approximation. They have found an extreme sensitivity of magnetic properties to the internal structure parameters and lattice constant. However, the calculated magnetic moments at concentrations $x > 0.3$ still disagreed with those experimentally observed.

In this paper we have investigated electronic structure and magnetic properties of Fe$_{1-x}$Co$_2$Si alloys using statical (LSDA) and dynamical (DMFT) mean-field approaches. The virtual crystal approximation gives us opportunity to investigate the electronic structure of Fe$_{1-x}$Co$_2$Si system in whole range of concentrations. We have found that LSDA results strongly overestimate magnetic moment values and extend magnetic phase diagram to much large values of Co concentration $x$ comparing with experiment. An account of correlation effects within DMFT results in good agreement with experiment for magnetic moment values as well as the position of the magnetization $M(x)$ maximum. We came to conclusion that Fe$_{1-x}$Co$_2$Si is an itinerant electrons system which magnetic properties can be correctly described by LDA+DMFT method.

\section{A. Statical mean-field results}

The electronic structure of Fe$_{1-x}$Co$_2$Si was calculated using the Tight Binding Linear-Muffin-Tin-Orbital Atomic Sphere Approximation (TB-LMTO-ASA) method with conventional local-density approximation (LDA)\textsuperscript{34} The Fe and Co atoms in Fe$_{1-x}$Co$_2$Si alloy were treated by virtual atoms with the atomic number value averaged by the concentration $x$. The experimentally observed lattice constants\textsuperscript{35} were used in the present band structure calculations. The calculated magnetic moment as a function of cobalt concentration is presented in Fig. \textit{11} and densities of states for $x$=0.2, 0.5 and 0.8 are presented in Fig. \textit{12} One can see that the calculated results start strongly deviate from experimental values of magnetic moments for Co concentration $x > 0.3$ with magnetization $M(x)$ maximum at 0.5 $\mu_B$ instead of experimental value of about 0.2 $\mu_B$ and giving stable magnetism for larger $x$ values than it is observed experimentally. Our results agree well with those presented in Ref\textsuperscript{31,33}.

A small magnetic moment value calls the question of the nature of magnetism in Fe$_{1-x}$Co$_2$Si: do we see itinerant electrons magnetism of the Stoner type or moments are local but their average value is suppressed due to quantum fluctuations and disorder effects? In order to investigate the localization degree of the magnetic moment in Fe$_{1-x}$Co$_2$Si system we have performed the supercell calculation to simulate a Co impurity in FeSi. The supercell was constructed in the FeSi lattice with all basis lattice vectors doubled and containing a total of 64 atoms of transition metal. The impurity Co atom was

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{graph11}
\caption{(Color online) Concentration dependences of the magnetization (in $\mu_B$) obtained from neutron scattering experiment\textsuperscript{6} (blue dashed line), LDA+DMFT (orange bold line) and virtual crystal approximation (black thin line).}
\end{figure}
assumed to substitute one of Fe atom. The obtained magnetization spatial distribution in Fe$_{63}$Co$_{64}$Si is presented in Fig. 13. One can see that magnetic moment is not localized on the Co impurity. There is a magnetic cluster containing one cobalt atom and six nearest iron atoms. This is a result of a strong hybridization of 3$d$-states cobalt and iron through 3$s$- and 3$p$-states of silicon. Such a magnetic cluster can be considered as a model for magnetic alloy Fe$_{1-x}$Co$_x$Si for which the experimentally observed magnetic moment is about 0.13 $\mu_B$ per transition metal atom. The averaged value of the magnetic moment in the cluster of 0.13 $\mu_B$ is in excellent agreement with the experimental value.

The fact that the magnetic moment induced in FeSi by Co alloying is delocalized supports the itinerant magnetism picture. In this case the Stoner approach is expected to give a realistic description of Fe$_{1-x}$Co$_x$Si magnetic properties. However, the results of this section and previous works show that direct Stoner theory application leads to the overestimation of the magnetic moment value at intermediate concentrations (Fig. 11). This is a result of ignoring dynamical correlation effects that, as we will show below, result in a strong renormalization of states near the Fermi level and subsequent reduction of the magnetic moment value.

### B. Dynamical mean-field results

In this section we investigate the influence of dynamical correlation effects on the magnetic properties of Fe$_{1-x}$Co$_x$Si. In our calculations we assume that Coulomb correlations treated by DMFT renormalize a paramagnetic density of states and then this new DOS is used as an input for Stoner theory calculations.

Let us first qualitatively discuss the origin of magnetism of the investigated alloys using the Stoner criterion

$$I_d N(E_F) > 1.$$  \hspace{1cm} (8)

Assuming the Stoner parameter $I_d$ value is equal to 1 eV the magnetic ground state is stable if the density of states at the Fermi level $N(E_F)$ is larger than 1 states/eV. With Co substituting Fe in FeSi number of electrons per formula unit increases and the Fermi level runs through the peak above the energy gap. Hence for Fe$_{1-x}$Co$_x$Si the value of $N(E_F)$ is determined by the height of this peak. In DMFT the spectral function depends on the temperature. Fig. 14 gives DMFT densities of states obtained by using the exact diagonalization technique. One can
see that the density of states value at the peak maximum is larger than 1 states/eV at $T = 58$ K but becomes smaller than 1 at $T = 232$ K. Then the Stoner criterion for magnetism Eq. (8) is satisfied for $T = 58$ K but not for $T = 232$ K. This result agrees with experimental values of the Curie temperature ($T_c = 50$ K).

![Density of states](image1)

**FIG. 14:** (Color online) Density of states for FeSi obtained by using exact diagonalization DMFT method at $T=232$ K (red dashed line) and $T=58$ K (brown solid line).

We are now in a position to perform the quantitative analysis of the magnetism. The DMFT calculations for Fe$_{1-x}$Co$_x$Si were performed for various concentrations $x$ values. The results for $x=0.36$ and $x=0.66$ are presented in Fig. 15. One can see that for $x=0.36$ the density of states at the Fermi level $N(E_F) > 1$ and for $x=0.66$ $N(E_F) < 1$. According to the Stoner criterion Eq. (8) that gives magnetic and nonmagnetic ground states for $x=0.36$ and $x=0.66$ correspondingly in good agreement with experimental data (see Fig. 11).

We have used the obtained paramagnetic DMFT densities of states for different concentrations (Fig. 15) to solve the Stoner model. Self-consistent values for spin-up $n_\uparrow$ and spin-down $n_\downarrow$ numbers of electrons are given by equations for the total magnetic moment

$$M = \int_{-\infty}^{+\infty} (N(\epsilon + I_d n_\uparrow) - N(\epsilon + I_d n_\downarrow)) f(\epsilon, T) d\epsilon,$$

and the total number of electrons

$$N = \int_{-\infty}^{+\infty} (N(\epsilon + I_d n_\uparrow) + N(\epsilon + I_d n_\downarrow)) f(\epsilon, T) d\epsilon,$$

that are recalculated iteratively. Here $N(\epsilon)$ is a density of states obtained in DMFT calculations and $f(\epsilon, T)$ is the Fermi distribution function. The Stoner parameter $I_d$ was chosen to be 1 eV close to that used in previous theoretical estimations.

The calculated concentration dependence of magnetization $M(x)$ is presented in Fig. 11. There is good agreement between experimental and theoretical values. The main effect of using $\rho(\epsilon)$ obtained in DMFT is a strong reduction of the resulting magnetic moment values compared to calculations using unrenormalized LDA DOS. This reduction is due to the quasiparticle weight factor $Z \equiv 1/m^*$ appearing in the numerator for Green function expression Eq. (9). Then the integral over quasiparticle band states near the Fermi level is decreased by a factor of $Z$ comparing with unrenormalized LDA values. As $Z \approx 0.5$ in our DMFT calculations that results in corresponding decrease of $M(x)$ values by this factor.

**IV. DISCUSSION**

In this paper we have investigated electronic structure and magnetic properties of FeSi and Fe$_{1-x}$Co$_x$Si systems using statical and dynamical mean-field approaches. Our band structure analysis supports the correlated band insulator model for this materials in contrast to the Kondo insulator model. The results of DMFT calculations have shown a strong renormalization of states near the Fermi level. The estimated band-mass renormalization $m^* \approx 2$ agrees with that obtained in the recent ARPES experiments. Analyzing paramagnetic DMFT densities of states calculated at different temperatures and at different Co concentrations we have shown that itinerant magnetism picture is valid for Fe$_{1-x}$Co$_x$Si alloys.

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The calculations were performed on the computer cluster of “University Center of Parallel Computing” of USTU-UPI.

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