The demographic transition and economic growth: implications for development policy

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ABSTRACT  An important transition in the economic history of countries occurs when they move from a regime of low prosperity, high child mortality and high fertility to a state of high prosperity, low child mortality and low fertility. Researchers have proposed various theories to explain this demographic transition and its relation to economic growth. In this article, we test the validity of some of these theories by fitting a non-linear dynamic model for the available cross-country data. Our approach fills the gap between the micro-level models that discuss causative mechanisms but do not consider if alternative models may fit the data well, and models from growth econometrics that show the impact of different factors on economic growth but do not include non-linearities and complex interactions. In our model, mortality and fertility decline and economic growth are endogenized by considering a simultaneous system of equations in the change variables. The model shows that the transition is best described in terms of a development cycle involving child mortality, fertility and GDP per capita. Fertility rate decreases when child mortality is low, and is weakly dependent on GDP. As fertility rates fall, GDP increases, and as GDP increases, child mortality falls. We further test the hypothesis that female education drives down fertility rates rather than child mortality, but find only weak evidence for it. The Bayesian methodology we use ensures robust models and we identify non-linear interactions between indicators to capture real-world non-linearities. Hence, our models can be used in policymaking to predict short-term evolutions in the indicator variables. We also discuss how our approach can be used to evaluate policy initiatives such as the Millennium Development Goals or the Sustainable Development Goals and set more accurate, country-specific development targets.
Introduction

The Industrial Revolution that brought unprecedented economic growth to Western Europe and North America also coincided with a new epoch in population dynamics (Galar, 2005). Countries moved from a regime of high mortality and high fertility to a regime of low mortality and low fertility, a process that researchers call the demographic transition (Kalemli-Ozcan, 2002). A key question for economists is whether economic growth causes the demographic transition or vice versa. In this article, we address this question by looking at the relationship between child mortality, fertility and economic growth.

One part of the relationship between economic growth and demography is clear. There is evidence of the impact of economic growth on child mortality: looking across all countries, there is a strong negative correlation between a country’s income per capita and child mortality (Cutler et al., 2006). So while inequalities and corruption may cause distortions due to inefficiencies and wastage of resources (Filmer and Pritchett, 1999; Rajkumar and Swaroop, 2008), the general pattern is that more money tends to produce better health-care systems. It is plausible that child mortality also impacts economic growth. For example, Heckman and Walker (1990) showed that the return to human capital is highest before the age of 5 years.

The relationship between the other socio-economic indicators is more complicated. Exogenous child mortality decline should lead to a fertility decline as women have fewer children if they know the chance of their survival is high (Kalemli-Ozcan, 2002). But there are many caveats due to specific factors (Ben-Porath, 1976; Barro, 1991; Haines, 1998). For instance, if the loss of a child affects the mother’s health, there may be a subsequent fertility decline following from a child mortality increase (Rutstein and Medica, 1978). Moreover, families make sequential fertility choice decisions, accounting for the gender and health of surviving children, before choosing to have more children (Sah, 1991; Wolpin, 1997).

Economic growth might also directly influence fertility decisions. In the classic Barro–Becker model (Becker, 1981; Barro and Becker, 1989), fertility choice is due to opportunity costs as increased wages for women result in less time spent on child bearing and child rearing. The Barro–Becker model has been highly influential and extended by others (Tamura, 1996; Strulik, 2004). Empirically its predictions are confirmed for Swedish fertility data (Eckstein et al., 1999), which show that two-thirds of fertility decline can be explained by child mortality decline and the remaining one-third can be explained by increase in wages. More broadly, using a quality–quantity trade-off model, Kögel and Prskawetz (2001) and Tamura (2002) show that an endogenous switch from an agricultural to a manufacturing economy has implications for fertility, which explains the coincidence of industrialization with fertility and mortality declines in countries.

The impact of fertility choice decisions at the individual level on country-level economic growth have proved difficult to quantify. Cigno (1998) proposed that at low development “death-reducing public expenditures are most effective”, but at high development these “crowd out parental expenditures and result in fertility decline”. However, Kalemli-Ozcan (2002, 2003) shows that the importance of fertility choice under uncertainty of child survival could explain empirical observations of the demographic transition of a wide range of countries. Moreover, Strulik (2004) suggests that child quality expenditures can initiate economic take-offs and result in perpetual growth, while its absence may cause economic stagnation with high fertility. Similarly, Galor (2005) and co-workers (Galor and Weil, 1996, 1999; Galor and Moav, 2002) suggest that the quality–quantity trade-off is endogenously triggered by technological progress, which leads to an increase in returns to education.
and others that the MDGs were unfair to Sub-Saharan Africa. We show that this is due to the differences in development trajectories in these countries caused by the inherent non-linearity in child mortality decline with respect to GDP. We suggest that, instead of setting arbitrary development targets, our non-linear dynamic model can be used to set country-specific development targets in the future, providing more feasible and fairer goals, especially for the upcoming Sustainable Development Goals initiative.

**Methods**

**Data.** The data are from the World Bank “World Development Indicators” dataset (WDI, 2013). This contains data for over 200 countries for a period of more than 50 years. For the economic indicator, we use the GDP per capita (in constant 2005 dollars). We use the log GDP value and call the variable G in the analysis.

We use child mortality as the mortality indicator (denoted by C). Child mortality refers to the number of children not surviving to age 5 per 1,000 live births and is a strong indicator of child health. The total fertility rate is the fertility measure (denoted by A) and is defined as the average number of children a woman has in the course of her reproductive lifetime.

We define the educational indicator E to be the average years of schooling for the female population as collected in the Barro–Lee dataset (Barro and Lee, 2010). Since the data are available only on a 5-yearly basis in that dataset, we use linear interpolation to obtain yearly data points.

The entire dataset is also available in the Palgrave Communications’ Dataverse repository (Ranganathan et al., 2015a).

**Model.** The changes in the variables are modelled endogenously so that the model specifies how changes in each of the state variables takes place as a function of the current state of the system. For the demographic transition, the state of the system is defined by the values of C, G and A and we model the time evolution of these variables. We estimate the model from cross-country data and write the estimating equations in terms of the variable values for a given country at a given time instant as:

\[ \Delta C(t, i) = f_C(C(t, i), G(t, i), A(t, i)) + \epsilon_C(t, i) \]

\[ \Delta G(t, i) = f_G(C(t, i), G(t, i), A(t, i)) + \epsilon_G(t, i) \]

\[ \Delta A(t, i) = f_A(C(t, i), G(t, i), A(t, i)) + \epsilon_A(t, i) \]

where we assume \( \epsilon_C(t, i), \epsilon_G(t, i) \) and \( \epsilon_A(t, i) \) are i.i.d normally distributed and independent for different countries \( i \) and at different time instants \( t \). The functions \( f_C(\cdot), f_G(\cdot), f_A(\cdot) \) are modelled using polynomial basis functions in the state variables \( C, G, A \). We include first-order and quadratic terms in the variables and their inverses along with all possible two-variable and three-variable interaction terms in the variables and their inverses. For example, the full specification of \( f_C \) is:

\[
 f_C(C, G, A) = a_0 + a_1 C + a_2 G + a_3 A + \frac{a_4}{C} + \frac{a_5}{G} + \frac{a_6}{A} + a_7 C^2 + a_8 G^2 + a_9 A^2 + \frac{a_{10}}{C^2} + \frac{a_{11}}{G^2} + \frac{a_{12}}{A^2} + a_{13} CG + a_{14} GA + a_{15} AC + \frac{a_{16}}{C G} + \frac{a_{17}}{G A} + \frac{a_{18}}{A C} + a_{19} CG^2 + \frac{a_{20}}{C^2 G} + \frac{a_{21}}{G^2 A} + \frac{a_{22}}{A^2 C} + a_{23} CGA + \frac{a_{24}}{C G A} + \frac{a_{25}}{G A C} + \frac{a_{26}}{A C G} + a_{27} CGA^2 + \frac{a_{28}}{C G A^2} + \frac{a_{29}}{G A C^2} + \frac{a_{30}}{A C G^2} + a_{31} CGA^3 .
\]

Thus, there are 33 terms in the full model specification, and the objective of the model selection algorithm we now present is to find the most efficient submodel that fits the data well. We do this in two stages. First, we rank all models with a given number of terms based on their log-likelihood score so that \( M_1, M_2, M_3, ... \) are the best possible models that include only 1, 2, 3, ... polynomial terms, respectively. The log-likelihood scores for these models are an increasing function of the number of terms in the model.

In the second stage, we select the best model among these preselected models using the Bayesian marginal likelihood score, similar to the Bayes factor. For this, we assume a uniform, non-informative prior on the parameter space, so that every possible model coefficient is weighted equally (conditioned on the corresponding term being included in the submodel). This penalizes more complex models with larger number of terms as the dimension of the parameter space increases with increasing number of terms (see Ranganathan et al., 2014 for a fuller description of the approach).

We perform an additional test to find the best explanatory variable for each model. For instance, for the \( \Delta C \) model, we test among all submodels that contain only \( C \) and one of the other two variables to test if two variables are sufficient to explain the \( \Delta C \) data instead of all three. If we find that the \( \Delta C \) data is explained well with only \( C \) and \( G \) variables and their interaction terms, we say that \( G \) explains changes in \( C \) adequately and is the variable with the most explanatory power for the \( \Delta C \) model.

**Robustness tests.** We assumed the errors are independent for different countries and different time instants. However, performing independent estimations for the three variables is suboptimal if the error terms across the variables are correlated for the same countries at the same time instants (as may happen if there are systematic reasons for changes in the variable due to omitted variables, for example). We use a generalized least squares approach called the seemingly unrelated regressions (Amemiya, 1985) to handle this case. This involves an iterative procedure where Ordinary Least Squares (OLS) estimates of the model coefficients are first computed and the error covariance matrix is estimated based on this first model estimate. This error covariance matrix is then used to recompute the model coefficients and this two-step procedure is iterated until convergence.

Another issue related to model robustness is to test how the model performs on different subsamples of the data. We have fitted the data for all countries to obtain our models. Researchers have shown that development patterns may differ vastly in countries with different socio-economic conditions (for example, Masanjala and Papageorgiou, 2008; Crespo Cuemas, 2011). So we expect that applying our method to specific groups of countries, such as only low-income countries or those in Sub-Saharan Africa, should give significantly different models from the overall model estimated at the same time instants. But using non-random subsamples to test for robustness restricts our modelling to only a particular region of the phase space, which is not consistent with our goal of identifying the overall trend in the data.

We instead test for robustness using random subsamples with different fractions of the data used for training the model (50%, 60%, 70%, 80% and 95% of the full sample) and with 100 different iterations for each case. Estimates of model fit for each of these models are obtained on the remaining out-of-sample test data. If our models are robust, they will be chosen as the best in most of the iterations for different subsamples. As more of the data are used for training, the probability of the training subsample being representative of the full data increases and the probability of the test-out-of-sample data being representative of the full data simultaneously decreases. As we use the out-of-sample data for evaluating model fitting error, other models are selected more often than for smaller training fractions due to unrepresentative test sets. However robust models should still be chosen more frequently than these other models. Hence, we report two numbers for each given size of training dataset—the absolute frequency with which our model is chosen as the best model for the different subsamples, and the relative position of our model in the list of models selected for different subsamples.

Multicollinearity is an issue when using a large number of regressors that are related to each other. It is possible that some terms are correlated with each other and this results in less efficient models being accepted. In evaluating models based on the Bayes factor, there is an implicit penalty to increasing the number of terms indefinitely but it is useful to perform direct tests to detect multicollinearity. Durlauf et al. (2008) suggest methods from within the Bayesian framework but we use a standard diagnostic test—the condition numbers or condition indices defined as the ratios of the individual singular values to the largest singular value in the singular value decomposition of \( X'X \), where \( X \) is the design matrix (Belsley et al., 1980). Condition numbers of over 50 (or 30 for conservative estimates) are considered to indicate presence of significant multicollinearity that may affect the OLS estimates.

**Adding other explanatory variables.** Our methodology expresses changes in the three variables only as a function of these three variables. However, it is well known that other variables, while not being part of the system in terms of the demographic transition, are important predictors of changes in these variables. For instance, education affects GDP growth, and has been postulated to cause fertility decline (Barro, 1991) and child mortality decline (Galor, 2005). Omitting these variables limits the explanatory power of our models.

However, these additional variables can be added in a straightforward manner to the model specification. If we wish to include the education variable into the full model for fertility decline, we can modify equation (3) so that we have:

\[ \Delta A(t, i) = f_A(C(t, i), G(t, i), A(t, i), E(t, i)) + \epsilon_A(t, i) \]

Similarly, if we wish to add more explanatory variables \( V_1, V_2, ... \) that are known to be good predictors of \( \Delta A \), but we are interested only in the linear effect of \( V_1 \) on \( \Delta A \), we modify the equation as:

\[ \Delta A(t, i) = f_A(C(t, i), G(t, i), A(t, i)) + \sum a_j V_j(t, i) + \epsilon_A(t, i) \]

where \( a_j \) are the regression coefficients. This straightforward extension allows us to refine our models easily to get better fits by the addition of more explanatory variables.

**Lagged effects.** In socio-economic systems, indicator variables may have lagged effects on one another. To model these effects from within our framework, we find the Bayes factor of the best models with a lagged variable instead of the actual
variable. For example, to investigate the possible lag effect for $G$ in the $\Delta C$ model, we consider the modified estimating equation

$$\Delta C(i, t) = f(C(i, t), G(i, t - 1), A(i, t)) + \epsilon_C(i, t)$$

for different values of the lag parameter $t$ and find the model that best fits the data using the methodology described above, while also evaluating the best lag parameter value.

For practical purposes, in this article, we modify this proposed approach slightly so that we first evaluate the best model using the methodology described above for the unlagged variables. For this best model, we investigate lag effects by evaluating the models for different values of the lag parameters. The first approach is more consistent with the Bayesian framework we have described earlier, but datasets with lagged variables are more sparse and the models that we obtain using the first approach may not be robust enough for lag analysis. Hence, we use the second approach to analyse lagged effects.

**Results**

We apply the methods to the dataset with child mortality, log GDP per capita and fertility rate and find that the best dynamic model for the three key indicator variables ($C$, $G$ and $A$) is given by

$$\Delta C = -0.0028 C(1.6G - 0.02C)$$

(4)

$$\Delta G = \frac{0.043}{A} \left( 16 - \frac{51}{G} \right)$$

(5)

$$\Delta A = -0.0007 A \left( 100 - 0.11C - 9A - \frac{130}{A} \right)$$

(6)

On the basis of Bayes factor values, we find that fertility rate is less important than changes in GDP as a predictor of changes in child mortality. Similarly, to explain changes in fertility rate, the Bayes factor for models with only two variables $C$ and $A$ is relatively close to that of the models where all three variables are used. In the case of GDP, the two variable $A$ and $G$ model has a higher Bayes factor than the three variable model, which includes $C$. But alternative models for GDP also have similar Bayes factor values and hence it is not clear that this is the best possible $\Delta G$ model based on the data.

The interaction effects between the variables can be represented as shown in Fig. 1. The overall cycle illustrated here is that child mortality decreases faster with higher GDP, fertility rate decreases faster when child mortality is low and decreases in fertility rate are faster at higher levels of GDP. In going through the cycle, we can see that there is a tendency of countries to go from the regime of high mortality, high fertility and low economic growth regime to the demographic transition literature. Thus, the two steady states correspond to the two opposite ends of the spectrum described in the demographic transition literature.

In the $\Delta G$ model, a high fertility rate slows economic growth. Solving $\Delta G = 0$ gives two equilibrium points, $G^* = 4.4$ and $G^* = 11.6$, suggesting that there is a slowdown in growth at both low and high GDP. We interpret the steady-state value of $G^* = 10$ as evidence of a transitional "poverty trap" (Ranganathan et al., 2015b), where countries are forced by certain self-reinforcing mechanisms to be trapped in a state of poverty without escape except through external means (Bowles et al., 2006). The other steady state $G^* = 11.6$ indicates a slowing of economic growth in rich countries.

**Robustness tests.** To evaluate the validity of the OLS estimates, we first test if the different error terms for different variables in the model are uncorrelated. We find there is only limited correlation (the maximum off-diagonal term in the scaled covariance matrix is 12% of the diagonal term). Hence, we are justified in assuming that the errors across variables are almost uncorrelated and we use the models obtained using this assumption. Performing generalized least squares using the seemingly unrelated regressions approach does not significantly alter the coefficients of the different terms and the iterative procedure converges quickly.

When we perform random subsample robustness tests on the models with 100 different subsamples, we find that the models specified by equations (4)–(6), are chosen a significant proportion of the time (69%, 45%, 96%, respectively, for the $\Delta C$, $\Delta G$, $\Delta A$ models) when 50% of the data are used for training. These numbers are necessarily lower (28%, 12% and 17%, respectively) when 95% of the data are used for training, as each test set is now...
we noted earlier, a number of alternative models in terms of relative frequency. The $\Delta G$ and $\Delta A$ models in equations (5) and (6) are chosen more often than any other model for any fraction of training data used, while the $\Delta C$ model in equation (4) is chosen as the best model most often for all fractions of training data except for 95%, when it is chosen second most often. These results cumulatively support the conclusion that the models selected using our methodology are robust.

Next, we test if multicollinearity is a significant issue affecting the OLS estimates. Using the condition number test, we find that the $\Delta C$ model predictors $CG$ and $C^2$ are not significantly correlated (condition numbers $= [1, 4.76]$). For the $\Delta A$ model, we find slight evidence of multicollinearity (condition numbers $= [1, 3.3, 7.5, 35.67]$) slightly above the conservative threshold of 30 but still below 50. For the $\Delta G$ model there is significant multicollinearity (condition numbers $= [1, 10.45, 246.8]$). But as we noted earlier, a number of alternative models fit the $\Delta G$ data closely. In fact, while the other two models have $R^2$ values of 0.29 and 0.26, the $\Delta G$ model has a very low $R^2$ value of less than 0.01 suggesting a very weak relationship.

Additional variables: the effect of education on fertility. There are a number of important covariates to be considered when looking at changes in fertility rates (Barro, 1991). Many policymakers work with female education as an important tool to reduce fertility rate and increase economic growth (Cochrane, 1979; UN, 2002). International organizations such as the United Nations Population Fund and the World Bank advocate better schooling for girls as a means of achieving lower child mortality and fertility rate. However, the evidence is not conclusive as significant fertility declines have occurred without noticeable changes in female education (Cleland, 2000; Basu, 2002). To test the hypothesis on whether female education is significant for fertility decline, we construct a model relating it to total fertility rate. However, the evidence is not conclusive as significant fertility declines have occurred without noticeable changes in female education (Cleland, 2000; Basu, 2002). To test the hypothesis on whether female education is significant for fertility decline, we construct a model relating it to total fertility rate and test it against a model that relates child mortality to fertility.

We test the $\Delta A$ models containing only the two variables $A$ and $C$ in equation (6) against $\Delta A$ models containing only $A$ and $E$. If $C$ is a more significant predictor than $E$ of $\Delta A$, then those models will have higher Bayes factors. Figure 2 shows that education is the best single explanatory variable when only first-order effects are considered. For models that contain 2, 3 and 4 polynomial terms, with $C$ being better than models with $E$ as the explanatory variable. If we go on to compute Bayes factor values for $\Delta A$ models with all these three variables ($A$, $E$ and $C$)

we find that the best 2, 3 and 4 term models involve only $A$ and $C$. We conclude based on this that while higher female educational attainment does predict first-order decreases in fertility rate well, child mortality is the more effective predictor overall.

This explains empirical findings (Cleland, 2000; Basu, 2002)—while investments in female education are valuable, improvement in child health and investments in health-care systems in general might be more important.

Lagged effects. We find the lagged effect of $G$ on $\Delta C$ by evaluating the set of models

$$\Delta C = -0.0028C(1.6G(t - \tau) - 0.02C)$$

for values of $\tau$ ranging between −15 and 15 years and find that the rate of decrease in child mortality depends on the level of GDP in the preceding 5 years. There is no lagged effect of $C$ on changes in $C$.

We repeat the same procedure for the $\Delta A$ model

$$\Delta A = -0.0007A \left(100 - 0.11C(t - \tau) - 9A - \frac{130}{A}\right)$$

now with $C(t - \tau)$ as the lagged variable. The results suggest that the longer lead we use on child mortality the better prediction we get on fertility rate decrease. This suggests that women use their future prediction of the probability of their child surviving when making fertility choice decisions. The greater the probability of future survival, the lower the fertility rate (this is again in agreement with the mechanism in the Kalemi-Ozcak, 2002 model). Finally, the $\Delta G$ model does not show significant improvement when using a lagged variable.

Some caution is required in the interpretation of these results. The dataset for lagged variables is necessarily shorter than that used in the original non-lagged fitting. Given the significant amount of missing data for poorer countries, the long lags might be a selection effect for richer countries where this data are available. As lagged datasets become available for developing countries, these results should become clearer (Fig. 3).

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**Figure 2** | The log-Bayes factor plots for $A$-$C$ models (solid circles) and $A$-$E$ models (hollow circles), showing that child mortality is more important than average years of schooling as an explanatory variable for fertility rate. But for the simplest one-term models, the education indicator seems more crucial.

**Figure 3** | The log-Bayes factor plots for the $\Delta C$ and $\Delta A$ models as a function of the lag in $G$ and $C$, respectively. The (Bayes factor values are reported in the log scale). The $\Delta C$ model suggests that a lag time of around 5 years in $G$ is the best parameter for the $\Delta C$ models. A long lead time is suggested for $C$ in the $\Delta A$ model.
Discussion

We have constructed a model of the demographic transition and its relationship to economic growth using the key indicator variables log GDP per capita, child mortality and total fertility rate. Our important substantive findings relate to the sequence of events in the demographic transition and may be seen as a test of the theory proposed by Kalemi-Ozcan (2002, 2003). Child mortality is reduced as a result of economic growth with a possible lagged effect. The reduction in child mortality, or possibly anticipation of this change, then drives fertility rates down. Although a predictor of fertility, female education plays a less important role than child mortality. Finally, economic growth is mostly independent of the other indicators, but is weakly driven by lowered fertility. The link back to child mortality completes the development cycle.

The innovation of the approach we have presented here lies in identifying the dynamic interactions that best explain the demographic transition and its effects on economic growth. Our approach provides (1) an emphasis on yearly changes instead of long-run equilibria that may not be attained; (2) the modelling of non-linearities and interaction effects, which is the norm in most realistic complex systems; and (3) a robust model that best explains empirical evidence on the demographic transition. An important question is how we interpret our results in terms of causal mechanisms. Can we use the equations we have derived to understand the actions of people living in the countries from which data were collected? To address this question we now give an interpretation of the models we have obtained in the context of earlier theoretical literature.

Various causative mechanisms are proposed for the onset of the demographic transition. For instance, Becker (1981) and a large body of literature following his work explains the demographic transition as a consequence of increased investments in human capital due to economic growth or technological progress. Increased returns on education are also thought to initiate the demographic transition and therefore a decline in fertility (Galor and Weil, 1999).

Our analysis and the cycle presented in Fig. 1 supports the models developed by Kalemi-Ozcan (2002, 2003) and emphasizes endogenously lowered child mortality over increased economic opportunities as the more immediate cause of drops in fertility rates. From an individual mother’s point of view, if the probability of children surviving is lower, then having more children increases biological fitness. While GDP has some effect on changes in fertility rate, the best single predictor of decreases in fertility rate is child mortality. Economic growth, however, comes into the picture indirectly as high GDP increases the survival probability, probably as a result of improvements in economic and social conditions.

Similarly, we find that while female education does predict decreases in fertility, child mortality remains a better predictor of these decreases. The decision whether or not to have a child may well involve a trade-off against other economic and education opportunities (Becker et al., 1990), but it is changes in the overall costs (and not just economic cost) of child bearing and child rearing that have the greatest role in decreasing fertility.

Although the emphasis on child mortality in the development cycle in Fig. 1 is different from that emphasized in some of the earlier work, the change in focus is relatively small. Importantly, none of our findings shift us a long way from those hypotheses previously proposed about human development. Instead, our analysis sharpens the picture by finding those models that are closest to all the available aggregate data. By fitting rate of change of indicators to their current state we have looked explicitly at how the state of the world in one year leads to the state of the world the following year.

This allows us to make robust short-term predictions on the evolution of the state of the system as defined by the three variables. There has been strong criticism of the MDGs (Easterly, 2009; Vandemoortele, 2009) for setting arbitrary development targets. As our methodology models changes in the child mortality, we can integrate it forward simultaneously with the other variables to make quantitative predictions on future values of child mortality for each specific country (as we have done in Ranganathan et al., 2015b). With this expected future value as a baseline value and a desired policy improvement based quantitatively on deviations from the business-as-usual scenario (say one standard deviation better than business-as-usual value), a feasible but fair development target can be set for each country.

From an econometric standpoint, in modelling the demographic transition, we have omitted many covariates specific to each indicator variable and hence do not explain the processes fully. For instance, adult mortality is an important variable and Kalemi-Ozcan (2002) and Soares (2005) include it in their models of fertility choice. The long lead time in our lagged effects analysis of the fertility rate model (equation (7)) suggests the importance of considering adult mortality. Child mortality levels are correlated with adult mortality levels and the inclusion of future child mortality levels in our model could be a proxy for women using future adult mortality levels in making decisions based on whether their children will survive into adulthood. Similarly, the growth econometrics literature has discussed in detail the important covariates of economic growth and these need to be included in our models to explain changes in log GDP (Barro, 1991; Durlauf et al., 2008; Ley and Steel, 2009).

However, our approach captures the interactions between the key variables and can be extended in a straightforward manner (as discussed in the Methods section) to include other variables of interest. We can add these additional variables either as control variables with only linear effects on the change variable or into the full framework of our methodology with non-linear and interaction effects. This will directly contribute to improving model fit and our understanding of the particular processes. Endogeneity is an important consideration when adding more explanatory variables. We show that our models are reasonably robust to the data but the addition of new variables may make the statistical estimates inefficient and this needs to be considered carefully.

From the statistical methods standpoint, we use non-informative priors on the parameter and the model space because we use an exploratory approach to obtain the model that best explains the data. To define “best fit”, we assumed that any submodel (equivalent to specifying the set of non-zero coefficients in the full model) is equally likely and that any model coefficient has an equal prior probability of being present. This is equivalent to assuming a discrete uniform prior on the model space (George, 2010). Chipman (1996) suggests the use of heredity priors to ensure that interaction terms are likely to be present only in models where the main effects are present. When we test our models with the strong heredity priors suggested by Chipman (1996), we find models with different terms. However, we prefer the uniform prior on the model space because some mechanisms can be better represented by using higher-order interaction terms without main effects. For instance, the ΔC model in equation (4) includes interaction and non-linear effects and no main effects, and hence would not be selected if a strong heredity prior were used. But the model we find suggests a mechanism whereby proportional changes (ΔC/C) as opposed to absolute changes (ΔC) are linearly related to the main effects C and G.

Finally, from the mechanistic standpoint, the approach we have taken in this article can be contrasted with one that starts from
the point of view of underlying micro-level interactions of economic agents. There are a number of limitations to the micro-level modelling approach, with respect to providing succinct and empirically accurate models of data. First, although based on observations, such models do not necessarily provide the best fit to the existing data as they do not test alternative models. Instead, correlational evidence is provided for particular assumptions or predictions. The advantage of the Bayes factor-based analyses we have performed here is that they provide a likelihood measure over a number of plausible models. A second limitation of micro-level economic models is that they usually involve specific mathematical forms that limit the range of models, which can be studied formally using the available tools. While these restrictions help mathematical analysis, they are not necessarily feasible in terms of mechanisms and restrict the degree to which non-linearities in the data can be captured by the model. A third limitation is that, despite their mathematical tractability, the statement of such models is often not amenable to direct policy applications in comparison with a set of equations such as equation (4)–(5), which can be used to predict short-term evolutions in the state variables robustly.

At the same time, while the approach we have outlined in this article avoids these limitations, we use no underlying assumptions and thus provide no a priori causal basis for our models. This criticism must be taken seriously because, without identifying underlying mechanisms, there are always a multitude of possible models. But letting the data reveal the patterns helps us discuss, in a post-analysis stage as we have done above, how the derived models relate to the micro-level motives of economic actors.

References

Amemiya T (1985) Advanced Econometrics. Blackwell: Oxford.
Barro RJ (1991) Economic growth in a cross-section of countries. The Quarterly Journal of Economics; 106 (2): 407–443.
Barro RJ and Becker GS (1988) Fertility choice in a model of economic growth. Economica; 57 (2): 481–501.
Barro RJ and Lee J-W (2010) A new data set of educational attainment in the world, 1950–2010. Working Paper 15902, National Bureau of Economic Research, http://www.nber.org/papers/w15902.
Basu AM (2002) Why does education lead to lower fertility? A critical review of observations, such models do not necessarily provide the best fit to the existing data as they do not test alternative models. Instead, correlational evidence is provided for particular assumptions or predictions. The advantage of the Bayes factor-based analyses we have performed here is that they provide a likelihood measure over a number of plausible models. A second limitation of micro-level economic models is that they usually involve specific mathematical forms that limit the range of models, which can be studied formally using the available tools. While these restrictions help mathematical analysis, they are not necessarily feasible in terms of mechanisms and restrict the degree to which non-linearities in the data can be captured by the model. A third limitation is that, despite their mathematical tractability, the statement of such models is often not amenable to direct policy applications in comparison with a set of equations such as equation (4)–(5), which can be used to predict short-term evolutions in the state variables robustly.

At the same time, while the approach we have outlined in this article avoids these limitations, we use no underlying assumptions and thus provide no a priori causal basis for our models. This criticism must be taken seriously because, without identifying underlying mechanisms, there are always a multitude of possible models. But letting the data reveal the patterns helps us discuss, in a post-analysis stage as we have done above, how the derived models relate to the micro-level motives of economic actors.
Data Availability
The datasets analysed are available in Palgrave Communications’ Dataverse repository (Ranganathan et al., 2015a): http://dx.doi.org/10.7910/DVN/IZU6JI. These datasets are from the World Bank World Development Indicators dataset and the Barro-Lee dataset.

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