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Electronic structure theory of the hidden-order material URu$_2$Si$_2$

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We report a comprehensive electronic structure investigation of the paramagnetic (PM), the large moment antiferromagnetic (LMAF), and the hidden order (HO) phases of URu$_2$Si$_2$. We have performed relativistic full-potential calculations on the basis of the density-functional theory, employing different exchange-correlation functionals to treat electron correlations within the open 5f shell of uranium. Specifically, we investigate—a comparison between calculated and low-temperature experimental properties—whether the 5f electrons are localized or delocalized in URu$_2$Si$_2$. The local spin-density approximation (LSDA) and generalized gradient approximation (GGA) are adopted to explore itinerant 5f behavior, the GGA plus additional strong Coulomb interaction (GGA+U approach) is used to approximate moderately localized 5f states, and the 5f-core approximation is applied to test potential properties of completely localized uranium 5f states. We also performed local-density approximation plus dynamical mean-field theory calculations (DMFT) to investigate the temperature evolution of the quasiparticle states at 100 K and above, unveiling a progressive opening of a quasiparticle gap at the chemical potential when temperature is reduced. A detailed comparison of calculated properties with known experimental data demonstrates that the LSDA and GGA approaches, in which the uranium 5f electrons are treated as itinerant, provide an excellent explanation of the available low-temperature experimental data of the PM and LMAF phases. We show furthermore that due to a material-specific Fermi-surface instability a large, but partial, Fermi-surface gapping of up to 750 K occurs upon antiferromagnetic symmetry breaking. The occurrence of the HO phase is explained through dynamical symmetry breaking induced by a mode of long-lived antiferromagnetic spin fluctuations. This dynamical symmetry breaking model explains why the Fermi-surface gapping in the HO phase is similar but smaller than that in the LMAF phase and it also explains why the HO and LMAF phases have the same Fermi surfaces yet different order parameters. A suitable order parameter for the HO is proposed to be the Fermi-surface gap, and the dynamic spin-spin correlation function is further suggested as a secondary order parameter.

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I. INTRODUCTION

Over the past 15 years the concept of “hidden order” (HO) has evolved to describe the emergent behavior of various quantum or strongly correlated materials where the order parameter (OP) of a clear phase transition along with its elementary excitations remain unknown. Often modern microscopic measurement techniques of diffraction (neutrons or photons), nuclear magnetic resonance (NMR), or muon spin rotation (μSR), etc., are unable to detect and characterize the new ordered phase. Yet the thermodynamic and transport properties unambiguously discern a novel state of matter appearing at a sharp transition temperature. Within this state additional unconventional phases may form depending on varying parameters such as pressure, magnetic (electric) fields, and doping. Although there is at present no comprehensive review of the generic HO problem and its relation to quantum criticality, the HO concept is beginning to make headway into the recent literature.

A prototype system for this behavior is the intermetallic compound URu$_2$Si$_2$, discovered 25 years ago. This material displays strong electron correlations such that the U 5f magnetic moments are dissolved into hybridized bands near the Fermi surface (FS) and a moderately heavy Fermi liquid forms at temperatures below approximately 70 K. Then at 17.5 K the HO state appears via a dramatic (second-order) phase transition. The above-mentioned techniques fail to discern the order parameter and cannot characterize its elementary excitations. Great attention has been devoted to studying this system with the aim of uncovering its hidden nature. A vast collection of experimental data has been gained and excellent single crystals are now available for definitive investigations thereby eliminating extrinsic effects of impurities and stress (see, e.g., Ref. 12). In addition there are numerous theoretical proposals and exotic models spanning many years that have, however, not come to full grips with many aspects of the experimental behavior.

Recent investigations on good single crystals have mapped out the phase diagram of URu$_2$Si$_2$. Apart from the paramagnetic (PM) phase and the HO phase below 17.5 K at ambient pressure, there is also the large moment antiferromagnetic (LMAF) phase, which appears with modest pressure of about 0.5 GPa and is characterized by uranium moments of 0.4 μ$_B$ in a type-I AF arrangement. Surprisingly, the bulk properties of the HO and LMAF phases are very much alike. Very similar, continuous changes in the thermodynamic and transport quantities have been reported for both phases. A comparable Fermi-surface gapping occurs for the transitions from the PM phase to the HO and LMAF phases, respectively. This similarity—which has been called adiabatic continuity—extends to the Fermi surfaces of the HO and LMAF phases. De Haas–van Alphen (dHvA)
experiments detect no significant differences between the Fermi surfaces of the HO and LMAF phases\(^\text{17}\) and, consistently, neutron-scattering experiments find the same nesting vectors.\(^\text{38}\) Nonetheless, the HO and LMAF unmistakably have different order parameters; simple magnetic order in the LMAF phase but an unknown order parameter in the HO phase. Neutron and x-ray scattering experiments\(^\text{39-43}\) detected a small magnetic moment ~0.03 \(\mu_B\) in the HO phase but this small moment is currently considered as a parasitic moment that is not intrinsic to the HO phase.\(^\text{12,33,44}\) Other differences between the HO and LMAF phases is that below 1.2 K and only out of the HO an unconventional\(^\text{15}\) superconducting (SC) state appears, which is the subject of recent interest.\(^\text{46-48}\) A further salient difference between the HO and LMAF phases is that inelastic neutron detectors detected a mode of AF spin fluctuations in the HO phase which freezes to the static antiferromagnetic Bragg peak in the LMAF phase.\(^\text{35,38,42}\)

As a starting point toward a full theoretical understanding of the intriguing electronic structure of URu\(_2\)Si\(_2\), state-of-the-art band-structure calculations are required. We present here detailed investigations of the electronic structures of the PM and LMAF phases, using various computational methods. On the basis of the obtained electronic structures, we analyze in how far the known physical properties of URu\(_2\)Si\(_2\) can be explained from these underlying electronic structures, and draw conclusions on what the valid electronic structure of URu\(_2\)Si\(_2\) is, emerging from the electronic structure calculations. Subsequently, we focus on the implications for a prospective explanation of the HO. Also, we expand on the “dynamical symmetry-breaking” model for the HO, which we have recently proposed.\(^\text{54}\) Details of this model are given and we relate the model to a larger collection of experimental properties. We also compare the derived electronic structure and the HO model to other recent proposals. In the following we first consider an issue that is central to the current discussion of model explanations of the HO phase.

II. ITINERANT OR LOCALIZED 5f BEHAVIOR?

One of the most intriguing questions regarding the electronic structure of URu\(_2\)Si\(_2\), and consequently the explanation of the HO, is whether the uranium 5f electrons are localized or delocalized. Single-ion theories of the HO, such as, e.g., quadrupolar or octupolar ordering, are based on the assumption of localized 5f electrons.\(^\text{14,16,19,21,23,26,28,49-52}\) This important issue of the degree of 5f localization has been controversially discussed recently. Several theories adopt the picture of localized 5f states from the outset, however, an examination of the grounds for this is needed. A thorough examination seems to unveil that there is little compelling experimental evidence for localized 5f’s. Smoking-gun evidence for localized f states would be the classical observation of crystal electrical field (CEF) f excitations in neutron experiments but only itinerant spin excitations have been detected and CEF excitations have never been observed for URu\(_2\)Si\(_2\) (see, e.g., Ref. \text{53}). Another indication of a CEF excitation could, e.g., come from measured specific-heat curves in which humps or peaks could signal the occurrence of CEF excitations. The measured \(C/T\) curve of URu\(_2\)Si\(_2\) shows a maximum at 70 K,\(^\text{8}\) which has sometimes been interpreted as evidence for a CEF transition. However, later measurements\(^\text{54}\) of the \(C/T\) of ThRu\(_2\)Si\(_2\), which has no occupied 5f’s and hence no CEFs, revealed a very similar maximum at the very same temperature. This suggests that the peak at 70 K is more likely related to the same underlying lattice structure and not to a CEF transition of 5f states. The shape of the measured magnetic entropy \(S_m(T)\) in the PM state does not correspond to Schottky-type anomaly expected for CEF levels.\(^\text{54,55}\) Also, very recent scanning tunneling spectroscopy (STS) measurements could not detect any CEF splitting of the 5f’s.\(^\text{56}\) Consistently, the susceptibility of URu\(_2\)Si\(_2\) does not show Curie-Weiss behavior near the HO temperature that might indicate localized f states, rather Curie-Weiss behavior commences only above 150 K.\(^\text{7,57}\)

One particular piece of experimental evidence in favor of localized 5f’s has come from inelastic neutron-scattering experiments\(^\text{58}\) in which a small inelastic peak was observed at 363 meV. This peak has been interpreted as a signature of an intermultiplet transition.\(^\text{58}\) A similar peak has been observed for UO\(_2\), which is indeed known to have a localized 5f\(^2\) configuration. However, for UO\(_2\), CEF excitations, too, were definitely observed with inelastic neutron scattering (see, e.g., Ref. \text{59}). The inelastic neutron experiments\(^\text{58}\) also detected a small peak at 363 meV for ThRu\(_2\)Si\(_2\), which indicates that the peak might in fact not be due to an intermultiplet transition. In addition, a similar peak has been observed\(^\text{60}\) for URhAl, which is however known to be an itinerant 5f material.\(^\text{61}\) The origin of the neutron peak at 380 meV in URhAl has consequently been debated;\(^\text{62}\) the issue is not completely solved but it could be an artifact related to the measurement apparatus.

Several other experimental data rather advocate the existence of delocalized 5f electrons in URu\(_2\)Si\(_2\). High-resolution photoemission spectroscopy (PES) using He I and He II radiation gave evidence for a typical delocalized 5f response in the He II-He I difference spectrum.\(^\text{63}\) A similar difference spectrum has been observed for itinerant U metal and UGa\(_3\).\(^\text{64}\) In addition, angular-resolved PES (ARPES) revealed dispersive bands in URu\(_2\)Si\(_2\),\(^\text{65,66}\) yet it still needs to be clarified what the dominant character of the observed bands is (f related or not). On the other hand, very recent He I ARPES measurements provided a picture of an almost flat band which sinks through \(E_F\) at the HO transition.\(^\text{67}\) The picture of a narrow band very close to \(E_F\) may however arise from the special data treatment, i.e., division by the Fermi function and double-differentiation technique, which always tends to give an impression of a flat state near \(E_F\).

A recent electron energy-loss spectroscopy (EELS) study\(^\text{68}\) deduces for the 5f states in URu\(_2\)Si\(_2\) the intermediate coupling mechanism to be valid, which might imply a tendency to f localization, or perhaps a dual, i.e., both itinerant and localized (see, e.g., Ref. \text{69}), nature of the f electrons. However, an unambiguous connection between the atomic coupling scheme and degree of f localization has not yet been established.

The AF phase of URu\(_2\)Si\(_2\) is commonly referred to as the large moment antiferromagnetic phase. This name suggests that the 5f’s in the LMAF phase might be partially localized.
However, in spite of its name, the uranium moment in the LMAF phase is actually relatively small and not the typical moment of a localized $5f$ material. For example, the $5f$ states of the cubic uranium salt USe are known to be closer to $5f$ localization, but still exhibit some $f-d$ hybridization, which leads typically to spin, orbital, and total moments of $-1.1$ $\mu_B$, $3.1$ $\mu_B$, and $2.0$ $\mu_B$, respectively, for USe. The total moment on U in AF URu$_2$Si$_2$ is with 0.4 $\mu_B$ quite far from such value. Instead, the U moment is much closer to values of 0.6 $\mu_B$ measured for an itinerant $5f$ material such as UGa$_5$.

It also deserves to be mentioned that the results of recent positron annihilation experiments on URu$_2$Si$_2$ proved to be incompatible with localized $f$'s but are on the contrary in good agreement with delocalized $f$'s. Also, recent neutron-scattering experiments detected itinerant $5f$ spin excitations.

Altogether, there does not appear to be clear, compelling evidence for localization of $5f$ electrons in URu$_2$Si$_2$. On the other hand, there exists a body of evidence in favor of delocalized $5f$'s. Nonetheless, the decision on localized-itinerant behavior should be concluded from an extensive comparison of calculated and experimental properties, which will be presented below.

In the following section we first outline the here-to-be-applied first-principles based techniques to study the electronic structure of URu$_2$Si$_2$. With these different approaches we can treat the full range of $5f$ behavior, from delocalized to localized. In view of the above considerations regarding the itinerant or localized $5f$ behavior, our main focus will be on the $5f$ band description. The applied density-functional theory (DFT)-local spin-density approximation (LSDA) and LSDA+$U$ approaches can provide only ground-state $T$ =0 K properties. The temperature dependence of quasiparticle spectra will be treated through dynamical mean-field theory (DMFT) calculations.

### III. COMPUTATIONAL METHODOLOGY

Our calculations are based on the DFT as well as on the DMFT. Specifically, for the treatment of the DFT static exchange-correlation potential we have employed the LSDA, the generalized gradient approximation (GGA), and also orbital-dependent extensions (LSDA+$U$ and GGA+$U$) to include the influence of strong on-site Coulomb correlations.

In our calculations we have used three accurate full-potential, relativistic electronic structure codes. These are the full-potential local orbitals (FPLO) method and the full-potential linearized augmented plane-wave (FLAPW) method; the latter we employed both in the WIEN2K (Ref. 77) and KANSAI implementations. We have verified that the three codes give, on the self-consistent local-density approximation (LDA) level, identical results for the electronic structure of nonmagnetic URu$_2$Si$_2$. WIEN2K and FPLO have been verified to provide identical results for the LMAF phase.

In the FLAPW calculations the relativistic valence states are computed within the full, nonspherical potential. The relativistic spin-orbit interaction was included self-consistently, and, in the WIEN2K calculations, we used the relativistic local orbitals extension of the scalar-relativistic FLAPW basis to treat accurately the $2p_{1/2}$ semicore states. The product of $R_{\text{nl}}$ and maximum reciprocal space vector ($K_{\text{max}}$), i.e., the basis size determining parameter ($R K_{\text{max}}$) was set to 7.5 and the largest reciprocal vector $G$ in the charge Fourier expansion, $G_{\text{max}}$, was equal to 12. We used about 5000 $k$ points for self-consistent convergence.

With the WIEN2K calculations we have employed the orbital-dependent GGA+$U$ method with around mean-field double-counting correction, in which an additional on-site Coulomb interaction, expressed by the Hubbard $U$ and exchange $J$ parameters, is introduced for the $5f$ states manifold.

In the relativistic full-potential FPLO calculations the four-component Kohn-Sham-Dirac equation, which implicitly contains spin-orbit coupling up to all orders, is solved self-consistently. We note that the relativistic Kohn-Sham-Dirac approach does not assume any atomic type of angular momentum coupling mechanism, rather the coupling follows from the self-consistent calculation. With the relativistic FPLO and FPLAPW implementations we are normally in the intermediate coupling regime for uranium intermetallics. In the FPLO calculations we used the following sets of basis orbitals: $5f$; 6$s$6$p$6$d$; 7$s$7$p$ for U, 4$s$4$p$4$d$; 5$s$5$p$, and 3$s$3$p$3$d$ for Ru and Si, respectively. The high-lying $6s$ and $6p$ U semicore states, which might hybridize with other valence states are thus included in the basis. The site-centered potentials and densities were expanded in spherical harmonic contributions up to $l_{\text{max}}$ = 12. Brillouin zone (BZ) sampling was performed with maximally $20 \times 20 \times 20$ $k$ points.

For the DMFT calculations we have used a recently developed full-potential, relativistic LDA+DMFT method. For a detailed review of the DMFT method we refer to Ref. 81. In our DMFT calculations we use the spin-polarized $T$-matrix fluctuation-exchange (FLEX) impurity solver for generating the self-energy. This impurity solver is expected to be applicable to moderately correlated materials, as, e.g., uranium intermetallic compounds. The local Green’s function is computed employing Kohn-Sham states which are obtained from a relativistic LDA calculation. The Coulomb $U$ and exchange $J$ quantities of the DMFT part are connected to the two-electron integrals of the Coulomb interaction of the $f$ electrons through the effective Slater integrals $F_{ij}(0 \leq \kappa \leq 3)$, where $F_{ij} = F^\text{U} + F^\text{GGA}$; $F^\text{U} = 41/297$ and $F^\text{GGA} = 175/11583$. In the DMFT calculation we used 8192 Matsubara frequency points to compute the temperature-dependent quasiparticle spectrum, which was obtained using a Padé approximation to the frequency-dependent lattice Green’s function $G(k,i\omega)$. Within the present DMFT FLEX implementation temperatures down to about 100 K can only be reached.

In our investigations we employ the ThCr$_2$Si$_2$-type body-centered tetragonal (bct) structure with space group No. 139 for paramagnetic URu$_2$Si$_2$ and the simple tetragonal (ST) structure with space group No. 123 for AF URu$_2$Si$_2$. The ST unit cell volume of AF URu$_2$Si$_2$ is twice the bct unit-cell volume of PM URu$_2$Si$_2$. The space group of the HO phase has not yet been definitely established because the symmetry breaking in the HO phase is as yet to be unveiled. In Fig. 1

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the Brillouin zones of the bct and ST structures are shown with high-symmetry points indicated. The ST BZ corresponds to a main folding of the bct BZ at ± 3Z and smaller folding along the X-X axes. In the bct BZ we have additionally labeled several nonhigh-symmetry points (Σ, F, Y, and Λ) for later discussion.

IV. RESULTS
A. DFT delocalized 5f electron calculations
1. Structural optimization

To start with, we consider the structural properties of URu2Si2, that is, the equilibrium lattice coordinates, bulk modulus, and equation of state. Several experimental investigations of the structural properties of URu2Si2 have been reported. For comparison to the available data, we have performed ab initio optimizations of the equilibrium volume, the c/a ratio, and the internal Si coordinate, zSi. These optimizations have been performed on the LSDA level, both for the PM and LMAF phases. In Fig. 2 we show the computed total energy versus unit-cell volume. Both PM and LMAF total energies are given for the ST cell, to convene comparing the two phases. The theoretically predicted equilibrium unit-cell volume is about 1.7% smaller than the experimental volumes, which are 162.9 Å³ (Refs. 7 and 85) and 162.6 Å³ (Ref. 87), respectively. Hence, the theoretical value is in very good agreement with experiment. As Fig. 2 illustrates the total energies of the PM and LMAF phases are very near one another. The total energy of the LMAF phase is computed to be only 7 K/f.u. deeper than that of the PM phase. This is in itself a remarkable finding, which appears to be a specific feature of URu2Si2. The inset of Fig. 2 presents the computed volume versus pressure dependence of URu2Si2. With pressure the antiferromagnetic state becomes slightly more stable. The inset includes recent experimental data points of Ref. 87. A fit of the computed volume versus pressure curves gives a bulk modulus B₀ of 204 GPa (208 GPa) for the LMAF (PM) phase. The recent pressure experiment obtained a value of 190 GPa; an older experiment reported a value of 230 GPa.

The optimized theoretical c/a ratio is shown in Fig. 3. The obtained theoretical c/a ratio almost coincides with the experimental value (2.32). The optimized c/a ratio of the LMAF phase is found to be just a small fraction larger than that of the PM phase. We note that x-ray diffraction experiments have been unable to detect any difference in the lattice constants of the PM, LMAF, and HO phases. Only dilatation experiments could so far detect tiny differences in both the a and c lattice constants of the three phases; the c axis lattice constant of the LMAF and HO phases are elongated with a few parts in 10⁻⁵, as compared to the PM phase (at higher temperature). The a axis of the HO and LMAF phases is contracted by a few parts in 10⁻⁵. As a result, the c/a ratio increases with about 10⁻⁴ from the PM above 17.5 K down to the LMAF phase at 10 K. The optimized c/a ratio of the LMAF phase is consistently computed here to be about 10⁻⁴ larger than that of the PM phase, in agreement with experiment. We refrain however from a more detailed comparison because we cannot make a meaningful quantitative statement for such tiny numbers.

Using the optimized c axis lattice constant and volume, the theoretical a axis lattice constant is about 0.6% smaller than the experimental value. As the LSDA approach is known to produce a small overbinding, the correspondence with the experimental lattice constant can be regarded as very good.
The bct structure of URu$_2$Si$_2$ has one internal coordinate, the Si $z$ position. Results for the total-energy optimization of the $z_{\text{Si}}$ coordinate are given in Fig. 4. The theoretical LSDA value is found to be 3% smaller than the experimental value of 0.371 (Ref. 85). A more recent experiment obtained a somewhat smaller $z_{\text{Si}}$ value, 0.3609, which would agree quite well with our theoretical result. As will be shown in more detail below, the essential physical properties of URu$_2$Si$_2$ are stable with respect to moderate variations in the unit-cell dimensions and the internal $z_{\text{Si}}$ coordinate.

Altogether, the ab initio structural optimization shows that the crystallographic properties of URu$_2$Si$_2$ are well described by the LSDA approach, which intrinsically is based on the assumption of itinerant 5$f$ electrons. It is known from computational investigations for other actinide materials that, when these have 5$f$ states that are localized, the LSDA approach usually does not provide a good description of the lattice properties (see, e.g., Ref. 90). Such deviant behavior is not found here for URu$_2$Si$_2$.

2. Energy band dispersions

We first consider the outcome of LSDA 5$f$-itinerant calculations for the electronic structure of URu$_2$Si$_2$. In Fig. 5 we show the computed LSDA energy dispersions in the PM and LMAF phases for the experimental lattice parameters. To draw a comparison, both sets of dispersions are given for the double unit cell (space group No. 123). As has been noted recently by us, the energy dispersions of these two phases are very similar. The dispersions of the AF phase are almost on top of those of the PM phase, except for some influence of the exchange splitting of 5$f$-related bands. This finding corroborates fully with the compute tiny total-energy difference between these two phases. A degeneracy of crossing bands occurs near the Fermi level, as can be recognized along the $\Gamma$-M and X-$\Gamma$ symmetry directions. The degenerate band crossing, existing in the PM phase along the $\Gamma$-M direction just below $E_F$, is lifted in the LMAF phase, due to a rehybridization, and thereby a small gap opens. A similar degenerate crossing point along the X-$\Gamma$ direction is however not removed in the LMAF phase. Through a larger part of the BZ degenerate crossings of the two bands exist, yet the opening of a gap in the AF phase does not happen uniformly over the FS. This gapping is related to a FS instability of URu$_2$Si$_2$ in the PM phase, where degenerate band crossing (Dirac points) occur off the high-symmetry directions, between the $\Gamma$-M and $\Gamma$-X directions. These degenerate points, which are closely related to the Fermi-surface hot spots discussed below, are removed in a transition to the LMAF phase, leading to a $k$-dependent FS gapping that is largest in the $z=0$ plane.

An enlarged view of the PM and LMAF energy bands along the $\Gamma$-M direction is shown in Fig. 6. In addition we have highlighted the orbital character of the bands through the colors and the amount of orbital character through the thickness of the bands. Ru 4$d$ character is shown by the light grey shading (green color in online version); the bands that consist primarily of Ru 4$d$ character appear about 0.20 eV below $E_F$. The bands closer to the Fermi energy contain dominantly U 5$f$ character, as is shown by the medium grey shading (online: blue color) in the PM phase and the dark red shade in LMAF phase.
grey shading (online: red color) in the LMAF phase. A small admixture of Ru 4d character is nevertheless present. The lifting of the degenerate band crossing is clearly borne out uranium 5f dominated states. The bands with mainly Ru 4d character are unaffected. The gap opening due to the rehybridization of states in the LMAF phase is about 60 meV wide and located in a narrow reciprocal space region at a distance of about 0.25a*–0.3a* from the Γ point. These values agree well with those observed in recent STS measurements.91

URu2Si2 is known to be a compensated metal (see, e.g., Refs. 46 and 92). The LSDA-computed energy bands of URu2Si2 (Fig. 5) are fully consistent with the property, as has been pointed out recently.24 Both the opening of the gap in the symmetry-broken phase and the compensated metal character are closely connected to the uranium 5f occupancy. Our LSDA calculations predict a 5f occupancy of 2.7,93 a value which is consistent with recent EELS measurements.68

The lifting of a FS instability in the LMAF phase is a significant feature of URu2Si2 obtained from ab initio calculations. The gap appearing around the Fermi level is narrow and might therefore sensitively depend on the lattice constants. In Fig. 7 we show the influence of the volume on this feature. For a range of volumes about the experimental volume the gapping property is found to be stable. We have similarly investigated the influence of the zSi coordinate on the FS gapping (not shown). Also for the zSi coordinate we find that the gapping property is stable for a range of values around the experimental one.

To end this LSDA/GGA band-structure section we briefly mention that several LSDA electronic structure calculations have been reported for URu2Si2.92,94–96 Rozing et al.,95 and Ohkuni et al.92 reported LDA calculations for PM URu2Si2, Yamagami and Hamada96 reported LSDA calculations of antiferromagnetic URu2Si2. The nonfull-potential calculations92,95 for the PM phase are in reasonable agreement with our full-potential results. Our energy bands and FS of AF URu2Si2 are however distinctly different from earlier published results.96 A reason for this difference is not known. As mentioned before, we have verified that independent state-of-the-art electronic structure codes give nearly identi-
moment of 0.39 $\mu_B$, in good agreement. We note first, with regard to the value of the moment, that we observed in the calculations a sensitivity of the moment to the $a$ and $c$ lattice constants. For an elongated unit cell with the same volume as the equilibrium volume, but a smaller $a$ and larger $c$ lattice parameter, the moment increases significantly. Conversely, for a compressed equal-volume unit cell with larger $a$ and smaller $c$ the computed moment is slightly reduced. Such behavior has been clearly observed in uniaxial pressure experiments.\(^{37}\) Second, the computed equilibrium spin and orbital moments are $M_S=0.36 \mu_B$ and $M_L=-0.75 \mu_B$, respectively, i.e., the orbital moment is antiparallel to the spin moment and twice as large. Detailed measurements of the separate spin and orbital moments have not been reported. Nonetheless, it can be inferred that the computed spin and orbital moments separately are in good agreement with experiment. Recent neutron form factor measurements\(^{98}\) indicated a value for $C_2=M_L/(M_L+M_S)$ of about 1.8 $\pm$ 0.2. From the theoretical values of $M_L$ and $M_S$ we obtain $C_2=1.9$, implying that the predicted values for the spin and orbital moments are indeed consistent with experiment (which, recalculating from $C_2$ and the total moment, gives $M_S=0.32 \pm 0.04 \mu_B$ and $M_L=-0.72 \pm 0.08 \mu_B$).

5. Transport properties

The thermal and charge transport properties of URu$_2$Si$_2$ are experimentally well documented.\(^{7,9,10,30,31,34,46,99–104}\) The normal\(^{7,9,34,103}\) and Hall\(^{10,46,99,106}\) resistivities as well as the thermal conductivity and Nernst effect\(^{46,101,102}\) display a clear behavior has been clearly observed in uniaxial pressure.\(^{205103,7}\) The thermal and charge transport properties of URu$_2$Si$_2$ are accessible from the electronic structures. To compute the electrical conductivities in these two phases, we have used the Kubo linear-response formulation in constant relaxation time approximation. Apart from the Fermi velocity which enters as a constant prefactor. The electronic structure theory of the hidden–...
Re doping were performed by Thieme et al. Infrared optical measurements of the gap in the HO phase were made by Degiorgi et al. and Bonn et al. The gapping occurring in the upward by 3 \begin{equation}
\frac{1}{c} = 0 \text{ K},
\end{equation}
where the Fermi energy. The optical conductivities, being maximal for the LMAF phase, are given for different uranium total magnetic moments, with \begin{equation}
\frac{1}{c}, \text{ where is the electric field vector of the light.}
\end{equation}
Using linear-response theory we have computed the optical conductivity of URu2Si2 for the two possible geometries, \begin{equation}
E_{\parallel \alpha} \text{ and } E_{\parallel \epsilon},
\end{equation}
where \begin{equation}
E = \text{the electric field vector of the light.}
\end{equation}
In Fig. 9 we show the calculated conductivity spectra, \begin{equation}
\text{Re}[\sigma_{\text{m}}(\omega)] \text{ and } \text{Re}[\sigma_{\epsilon c}(\omega)].
\end{equation}
The optical conductivity spectra for URu2Si2 have been measured in several investigations.109–111 The gap occurring in the HO phase was observed originally by Bonn et al.109 The optical spectra of URu2Si2 have been measured in the HO phase for photon energies below 30 meV. The Sommerfeld coefficient is comparable to that of, e.g., UG_3,114 which is an itinerant antiferromagnet.115,116 The unrenormalized specific-heat coefficient calculated with the LSDA approach is about 9 mJ/mol K^2, i.e., there is an expected mass renormalization of six, a value not unusual for actinides. As a consequence, the computed LSDA bands will become renormalized, but not strongly. Our LDA+DMFT calculations (to be presented below) indicate a further influence of the dynamic part of the electronic self-energy \begin{equation}
\Sigma(\omega),
\end{equation}
through which a renormalization of the bare LSDA band masses would occur. However, as we can currently not compute \begin{equation}
\text{Re}[\Sigma(\omega)/\omega]
\end{equation}
down to low enough temperatures, we refrain from giving values for the estimated mass renormalization. Also, low-energy spin fluctuations, which are not accounted for in the bare specific-heat coefficient, can be expected to give a considerable enhancement.55

The entropy of URu2Si2 has drawn attention from the beginning.8,9,113 The phase transition to the HO state was originally discovered from a \begin{equation}
\lambda \text{-type anomaly in the specific heat; 7–9 the related magnetic entropy change in the } \lambda \text{ anomaly is, with about 0.16R ln 2, relatively large.8,9,113}
\end{equation}
Such entropy removal can, in particular, not be explained by assuming a phase transition to a SMAF state that at first was thought to be connected to the HO transition.39–42

The total magnetic entropy \begin{equation}
S_m, \text{ has been determined by van Dijk et al. and Janik,4 through subtracting the measured specific heat of ThRu2Si2, which has no } 5f \text{ electrons, from that of URu2Si2. From the specific-heat difference a total electronic entropy }
\end{equation}
\begin{equation}
\int_{T_1}^{T_2} (\Delta C/T) dT,
\end{equation}
approaching \begin{equation}
R \ln 4 \text{ (mJ/mol K) was obtained.4 This value is not inconsistent with our LSDA calculations, predicting a low-temperature } 5f \text{ count of 2.7. Assuming at higher temperatures an occupancy of three } 5f \text{ electrons, a spin entropy of } R \ln 4 \text{ [i.e., } R \ln(2S+1), \text{ with } S = 3 \times 1/2 \text{ follows.}
\end{equation}
For the HO phase, the total electronic entropy at $T_0$ amounts to about $0.25R \ln 2$ (Ref. 113). As was pointed out several times, assuming the opening of a gap $\Delta$ in the electronic spectrum, the electronic specific heat would scale as $C_{\text{e}}(T) \approx \exp(-\Delta/k_B T)$, which fits the measured specific heat in the HO phase extremely well. In fact, the opening of gap in the magnetic excitation spectrum can wholly explain the entropy removed at the HO transition. The magnitude of the gap was estimated to be about 11 meV from specific-heat measurements, or smaller from inelastic neutron measurements. Our energy band calculations also show that the HO gapping removes a considerable amount of accessible states at $E_F$. The band-structure gap computed here is in fact larger, maximally 60 meV (for the LMAF phase) but it is strongly $k$ dependent. The $k$-averaged gap would thus be considerably smaller and be consistent with the entropy loss associated with the HO transition.

### B. LSDA+$U$ and 5f-core calculations

Actinide materials with enhanced Coulomb correlations between the 5f electrons can be computationally treated with LSDA+$U$ or GGA+$U$ calculations (see, e.g., Refs. 118–120), which are expected to give a good description for materials with a moderate degree of 5f localization. Actinide or lanthanide materials with localized f electrons are conversely well described by open f-core calculations in which the f’s are treated as unhybridized core electrons (see, e.g., Ref. 121).

The energy bands of AF URu$_2$Si$_2$ computed with the “around-mean-field” GGA+$U$ approach are shown in Fig. 10. For the Coulomb $U$ and exchange $J$ parameters we have chosen the values $U=1.4$ eV and $J=0.68$ eV. The $U$ value can be considered as relatively small and has been chosen such in order not to depart much from the LSDA solution. Nonetheless, the computed bands in Fig. 10 reveal that the bands near the Fermi level are modified to a considerable extent so that also the FS becomes quite different. The bands near the M point are pushed down, whereby new FS sheets appear. Bands near the X and $\Gamma$ points are pushed upward, whereby also a new FS sheet appears around X. Furthermore, two new electron pockets appear around A. The gap features along the $\Gamma$-M and $\Gamma$-X directions are strongly affected; the gapping occurring along $\Gamma$-M has practically vanished. As we shall see below, experiments support in fact the Fermi surface predicted by LSDA calculations. This illustrates that the Fermi surface and its gapping is rather sensitive to the Coulomb $U$ in GGA+$U$ calculations. This is understandable, as the FS gap is quite small (several tens of millielectron volt) and the opening of the FS gap is due to a subtle hybridization change in 5f bands just above and below the Fermi level. The Coulomb $U$ acting on the 5f states changes the 5f band dispersions substantially.

As mentioned before, a large number of theories for the HO of URu$_2$Si$_2$ are based on the assumption of completely or nearly localized 5f electrons. Particularly, an underlying localized 5f$^2$ configuration has been discussed recently. In itself, a localized 5f$^2$ configuration possesses very interesting properties, as is can sustain both a nonmagnetic spin-singlet and a magnetic triplet configuration, something which might be related to the occurrence of two different phases.

In Fig. 11 we show the energy dispersion computed for paramagnetic URu$_2$Si$_2$ with the open-core approach for a localized 5f$^2$ configuration. As expected, the f-core energy bands are very different from the bands obtained for PM URu$_2$Si$_2$ assuming itinerant 5f$^2$ valence states. Such band structure of URu$_2$Si$_2$, computed with WIEN2K in the PM phase was reported already in Ref. 72 and is therefore not repeated here. The f core energy dispersions are indeed so different from the 5f$^2$ delocalized ones that it makes no sense to compare them. As mentioned before, the 5f occupancy obtained from LSDA itinerant 5f calculations is about 2.7. Even with a dependence on the used muffin-tin sphere radius, this occupation number is not two. Hence, it is understandable that very distinct energy dispersions emerge. The concomitant FS’s are consequently also very different, as will be exemplified below when we discuss the FS of URu$_2$Si$_2$ in detail.

LSDA-5f$^2$ core calculations were recently also performed by Haule and Kotliar, who only show a small reciprocal
space section of the bands in a narrow energy interval near the Fermi level and around the $\Gamma$ point, yet their results agree with our full-potential results. In particular, there is one band at the $\Gamma$ point near $E_F$ that has an inverted parabolic shape, and there are two bands with a steep dispersion crossing the Fermi level between $\Gamma$ and $\Sigma$.

Whether or not a localized 5$f^2$ picture is more appropriate for URu$_2$Si$_2$ has to be considered in the light of all available experimental data. The delocalized 5$f$ picture provides a quite accurate description of the known experimental data; this cannot be said of the localized 5$f^2$ configuration. In first instance one might think that the LMAF phase might be related to a magnetic, localized 5$f$ configuration, but the delocalized 5$f$ approach is thus far the only one that has provided an accurate explanation of the LMAF phase, which is a conventional antiferromagnetically ordered state without mysterious properties.

C. DMFT calculations

In our LDA+DMFT calculations we used a large number of Matsubara frequency points (8192) when taking the sum over the frequencies on the temperature axis, nonetheless, we can only compute a finite number of frequency points and therefore the calculations are valid for moderately high temperatures in practice (100 K and above). This implies that we can investigate the influence of dynamical electron configuration fluctuations in the paramagnetic phase. At high temperatures the uranium 5$f$ moments are expected to behave as incoherent, local moments. Note that the single-ion Kondo temperature is estimated to be 370 K in URu$_2$Si$_2$.\cite{10} With reducing temperature, lattice coherence between the $f$ moments develops below 100 K, leading to a coherence temperature $T^*$ of about 70 K, which is witnessed by a maximum in the normal and Hall resistivities.\cite{7,10} Below the coherence temperature $T^*$ the 5$f$ local magnetic moments are incorporated into the conduction electron sea, which greatly enhances the electron effective masses and, for conventional Kondo lattice materials, is expected to enlarge the Fermi surface, too.

In the LDA+DMFT calculations we started from computed LDA Kohn-Sham states that are subsequently used in the DMFT self-consistency loop. In the DMFT part we assumed effective $U$ values of 0.4 and 0.6 eV (in both cases, $J$ was set to 0.0 eV). These $U$ values are chosen to approximate the more localized behavior of the 5$f$’s that is anticipated at higher temperatures.

In Fig. 12 we show the computed quasiparticle density of states of URu$_2$Si$_2$ for several temperatures. Pronounced changes in the quasiparticle DOS occur around the chemical potential (at 0 eV). Lowering of the temperature and increase in electron coherence leads to the typical opening of a quasiparticle coherence gap (also called hybridization gap) of about 100 meV. Concomitant with the opening of the quasiparticle gap, there is a buildup of spectral weight on both sides of the gap. The development of coherence gaps has been observed with infrared optical spectroscopy for several $f$-electron materials\cite{12} but for URu$_2$Si$_2$ this property has not yet been reported.

In Fig. 13 we show the calculated quasiparticle bands of URu$_2$Si$_2$ at $T=100$ K. The bright colors depict a high intensity of the spectral function. For comparison, the nonmagnetic LDA bands are shown by the black lines. Note that the $Z'$ point on the reciprocal space abscissa is positioned in the neighboring BZ. We observe that the LDA+DMFT quasiparticle bands are relatively close to the LDA bands. Their similarity is even more so for energy bands below $-1$ eV (not shown here) because these bands possess less uranium $f$ character. Some differences between the LDA and quasiparticle bands can nonetheless be seen from Fig. 13. In the N-P-X panel the quasiparticle band just above $E_F$ moves distinctly closer to $E_F$ and becomes flatter. Near the $X$ point the quasiparticle band below the Fermi level moves slightly upward and disperses stronger downward toward the $\Gamma$ point. The $k$-dependent quasiparticle DOS gives the impression of a band dispersing downward from above the $X$ point toward the $\Gamma$ point and crossing $E_F$ between the two points.

Another DMFT calculation for URu$_2$Si$_2$ has been reported recently by Haule and Kotliar.\cite{26} We note that our DMFT results are distinctly different from those of Ref. 26. We have performed DMFT calculations using the spin-polarized FLEX impurity solver, starting from LDA results, which should be valid for the weakly correlated uranium $f$ electrons at higher temperatures. The DMFT calculations of Ref. 26, on the other hand, used the one-crossing approximation solver together with a nearly localized uranium 5$f^2$ configuration. The difference can be understood to arise from the 5$f$ configuration used in the LDA or LDA+U band-structure.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig12}
\caption{(Color online) The $k$-integrated quasiparticle DOS calculated with the LDA+DMFT approach for URu$_2$Si$_2$ in the high-temperature, nonmagnetic phase.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig13}
\caption{(Color online) The LDA+DMFT quasiparticle bands of URu$_2$Si$_2$ at $T=100$ K (for details, see text). Bright colors indicate a high intensity of the $k$-dependent spectral function, $-\frac{1}{\pi} \text{Im} \, G(k, E)$. Black lines show the LDA energy bands for comparison. Note that $Z'$ denotes the Z point in the neighboring bct Brillouin zone.}
\end{figure}
part of the LDA+DMFT calculation, which obviously determines largely the gross electronic structure, whereas the DMFT part involving dynamical self-energy fluctuations induces mainly modifications of energy dispersions in the vicinity of the chemical potential.

DMFT $k$-dependent spectral functions can be compared to ARPES data. Several ARPES measurements on URu$_2$Si$_2$ have been reported. Ito et al. and Santander-Syro et al. both used a He I light source, whereas Denlinger et al. used tunable synchrotron radiation. Only the recent experiment of Santander-Syro et al. measured quasiparticle bands below $T_D$. These latest measurements indicate the existence of a narrow band just below $E_F$ in the HO phase, as well as of an inverted parabolic band at $k_z=0$ below $E_F$; the latter band was attributed to a surface state. In our 5$f$-itinerant LSDA calculation there is no such inverted parabolic band at $k_z$=0, but LDA localized 5$f$-itinerant responses at ura-

D. Fermi surface of URu$_2$Si$_2$

1. Nesting vectors

An appropriate description of the Fermi-surface topology of URu$_2$Si$_2$ is an indispensable ingredient for unraveling the nature of the HO phase as well as the unconventional SC. Experimental information regarding he FS of URu$_2$Si$_2$ has been gained from nesting vectors, identified through inelastic neutron experiments, and through extremal FS orbits, obtained from quantum-oscillation experiments.

To start our discussion, we show a side view of the FS of PM URu$_2$Si$_2$, computed with the LSDA approach, in Fig. 15. The two FS sheets reveal the existence of a nesting vector with length $c^*=2\pi/c$ (i.e., half the distance from one $\Gamma$ point to the next-nearest $\Gamma$ point). These two FS sheets have a similar round curvature, favorable for nesting, with the exception that close to $Z/2$ the $\Gamma$-centered sheet has a more pointed part, with only a small area that would not be favorable for nesting. This FS part corresponds to a small part at the $Z$ point in the simple tetragonal cell, which we believe to be insignificant. The identified nesting vector fits accurately to the antiferromagnetic wave vector $Q_{AF}=(0,0,1)$ of longitudinal spin fluctuations observed in the HO phase with inelastic neutron-scattering experiments, and it is the AF ordering vector of the LMAF phase. This nesting vector is important for understanding the low-temperature behavior of URu$_2$Si$_2$. When a coherent state emerges at temperatures sufficiently below the coherence temperature $T^*$, the system develops a FS sustaining this nesting vector, which is favorable for AF spin fluctuations in the HO phase and formation of long-range AF order in the LMAF phase. Inelastic neutron experiments showed that the inelastic response at $Q_{AF}$ in the HO phase becomes the static AF Bragg peak of the LMAF phase. The thereby induced symmetry breaking implies a folding of the BZ at $Z/2$, i.e., folding $Z$ to $\Gamma$.

A second, incommensurate nesting vector of URu$_2$Si$_2$ has been detected at $Q_1=(1 \pm 0.4,0,0)$. This nesting vector has been observed in both the HO and LMAF phases. In Fig. 16 we show a cross section of the LMAF and PM Fermi surfaces in the $z=0$ plane. To draw comparison, both FS cross sections are plotted in the simple tetragonal unit cell of the LMAF phase.
implying a nesting vector that matches precisely the measured incommensurate vector \( \mathbf{Q}_1 = (1 \pm 0.4, 0, 0) \). Figure 16 illustrates that \( \mathbf{Q}_1 \) is a suitable nesting vector for the LMAF phase, but less so for the PM phase (shown by blue circles), because in the latter phase the FS curvature does not support nesting as much. Hence, the incommensurate nesting vector is characteristic for the LMAF phase but not for the PM phase. \textit{A priori} we do not know how the FS in the HO phase looks like, because this would require knowing the order parameter of the HO, but it is known that de Haas–van Alphen experiments could not detect any notable difference between the FSs of the HO and LMAF phases.\textsuperscript{57} Likewise, inelastic neutron-scattering experiments\textsuperscript{38} give the same incommensurate wave vector in the HO and LMAF phases. From these facts we infer that the FS of URu\textsubscript{2}Si\textsubscript{2} in the HO phase should be quite close to the one we have computed for the LMAF phase.

Figure 16 in addition illustrates the positions of the FS hot spots in the \( z=0 \) plane. The degenerate crossing of two bands occurs right at \( E_F \) at eight places, indicated by the thin dashed arrow. At these hot spots there exists an instability of the FS as a small perturbation may already cause a lifting of the degeneracy and hence cause a topological FS reconstruction (Lifshitz transition).

The gap symmetry in the superconducting phase has been discussed recently\textsuperscript{36–48} but the symmetry of the partial gap in the HO phase has not yet been studied. The calculations in Fig. 16 illustrate that the HO gap has in the \( z=0 \) plane a fourfold symmetry, in which there exist nodal lines with \( d_{x^2-y^2} \) symmetry in the ST structure, which is equivalent to nodal \( d_{xy} \) symmetry in the bct structure. A possible additional phase factor in the gap structure might exist but cannot be deduced from the current calculations.

2. Quantum oscillations

Details of the FS of URu\textsubscript{2}Si\textsubscript{2} has been investigated, too, through studies of quantum oscillations in dHvA and Shubnikov-de Haas (SdH) measurements.\textsuperscript{36,92,105,124–126} In earlier experiments,\textsuperscript{124–126} only a few extremal orbits could be detected. The more recent dHvA and SdH measurements\textsuperscript{36,92,105} on purer crystals have provided a consistent set of data for the quantum oscillations in URu\textsubscript{2}Si\textsubscript{2}. These experimental data are listed together with the calculated extremal FS cross-sectional areas in Table I. The dHvA experiments of Ohkuni \textit{et al.}\textsuperscript{92} as well as the SdH experiments of Jo \textit{et al.}\textsuperscript{92} revealed three FS orbits, which these authors labeled \( \alpha \), \( \beta \), and \( \gamma \). However, it was already noted\textsuperscript{92} that one or more orbits were missing because the cyclotron mass of the small FS orbits would not be able to account for the full, enhanced mass that was deduced from the specific heat. Quite recently, it was shown with SdH experiments on ultraclean crystals\textsuperscript{105} that there is indeed a further branch, which was named the \( \varepsilon \) branch. The calculated FS of URu\textsubscript{2}Si\textsubscript{2} is shown in Fig. 17, where we have also indicated the theoretical extremal orbits \( \varepsilon \), \( \alpha \), \( \beta \), and \( \gamma \) for magnetic field along the \( z \) axis. Note that there is a small \( \Gamma \)-centered ellipsoid (\( \gamma' \)) which is not visible in Fig. 17 because it is masked by the large \( \Gamma \)-centered ellipsoid. Table I illustrates that the calculated extremal orbits of the four branches are in quite good agreement with the available experiments. The computed orbits pertain to the LMAF phase, however, consistent with the observations made above, we assume the same FS for the HO and LMAF phases. The newly discovered\textsuperscript{105} \( \varepsilon \) branch corresponds to the large \( \Gamma \)-centered rugby ball, stemming from band 107 in our calculations. The earlier reported extremal orbits correspond to the \( \Gamma \)-centered ellipsoids (branches \( \alpha \) and \( \gamma \), band nos. 109 and 111), the rounded half sphere (\( \beta \), band no. 109), and the small, \( \Gamma \)-centered sphere (\( \gamma' \), band no. 107). The computed frequencies of these extremal orbits agree well with dHvA and SdH measurements: the extremal areas of the \( \varepsilon \) and \( \beta \) orbits are well reproduced. The \( \alpha \) orbit is somewhat smaller than the experimental value and the \( \gamma \) orbit is somewhat larger. The calculations predict, in fact, a \( \gamma \) and a \( \gamma' \) orbit, which have nearly the same frequency. Also, as discussed below, the angular dependence of their cross-sectional area is very similar. This similarity appears to be coincidental. Experimentally, it would thus be difficult to distinguish between the \( \gamma \) and \( \gamma' \) branches. One other difference between the experiments and the calculations is that the calculations predict an additional, small FS part around the \( Z \) point (see Fig. 17). Its

![FIG. 16. (Color online) Cross sections of the PM (circles) and LMAF (squares) Fermi surface in the \( z=0 \) plane of the simple tetragonal BZ. The Fermi-surface portions along the \( \Gamma-M \) directions are gapped in the PM to LMAF transition. Note that other Fermi-surface parts are completely unaffected; the LMAF Fermi-surface cross sections are on top of the PM ones. The thick dashed arrow indicates the nesting vector \( 0.4a^* \), the thin dashed arrow indicates the position of one of the eight degenerate band crossings precisely at the Fermi energy \( E_F \).](image-url)
extremal area is very small (about 0.07 kT) and, as mentioned previously, its occurrence is related to an insignificant, small FS area at the Z point which occurs through band folding. The origin of this small FS sheet is the pointed part of one FS sheet near \( \pm Z/2 \) in the PM phase (Fig. 15), which causes an imperfect nesting of the two FS sheets and hence an incomplete FS gapping near the ST Z point when being folded to the LMAF phase.

We briefly mention that earlier studies of quantum oscillations in URu$_2$Si$_2$ were reported by Bergemann et al., Ohkuni et al., and Keller et al.. Although the measurements were performed on less well-defined samples, there are some consistencies with the newer data. Bergemann et al. report the observation of two orbits, which cross-sectional areas of 1.09 and 0.41 kT for magnetic field along the c axis. Keller et al. reported magnetoresistive measurements from which they obtained several SDH frequencies of about 1.0 and 0.2 kT.

The crystallographic anisotropy of the extremal FS areas has been investigated by angular-dependent dHvA and SDH experiments. The computed angular dependence of the FS areas is shown in Fig. 18, for field directions in the bct cell.

A comparison of the computed angular dependence with experimental data reveals a good overall correspondence. Ohkuni et al. report that the \( \alpha, \beta, \) and \( \gamma \) branches are quite flat, i.e., corresponding to nearly spherical FS sheets. Shishido et al. also report that the \( \alpha \) and \( \beta \) branches are flat and due to spherical FSs. As Fig. 18 shows, the theoretical FS sheets are predicted to be relatively spherical, and hence, a very similar angular behavior is furnished by the calculations. Moreover, a more detailed comparison reveals that the angular anisotropy of the e, \( \alpha, \) and \( \beta \) branches is also in good agreement with experiment. The extremal frequency of the \( \alpha \) orbit is predicted to increase from the [001] to [100] direction, which was also found experimentally. The frequency of one part of the \( \beta \) orbit decreases slightly, in accordance with experiment. The four half spheres in the z=0 plane are anisotropic with respect to the field direction, therefore the single \( \beta \) orbit for field \( H_{\text{b}} c \) splits in two orbits for fields along [100] but no splitting occurs along [110]. Such a splitting of the \( \beta \) branch has been detected recently in SDH experiments. The \( \epsilon \) orbit increases in the [100] direction, which was also observed in recent SDH measurements. However, the SDH experiment finds a larger increase than the theory predicts.

The crystallographic anisotropy calculated for the \( \gamma \) orbit is not in accordance with experiment; the calculation predicts a slight increase in the frequency for magnetic fields toward [100] but the dHvA experiment observed a slight decrease. Ohkuni et al. mention, however, that the signal of this orbit is very weak and therefore it was difficult to follow the orbit under angular field variation. The recent SDH experiments could not determine the angular dependence of the \( \gamma \) orbit for the same reason. We also note, lastly, that the difference between the \( \gamma \) and \( \gamma' \) extremal orbits is predicted to be larger for fields along the [110] direction.

As a nearly localized uranium 5\( f^2 \) configuration has been suggested to be applicable to URu$_2$Si$_2$, we briefly consider the FS that would correspond to such configuration. In Fig. 19 we show the FS computed for URu$_2$Si$_2$ in the LMAF phase obtained for a localized 5\( f^2 \) configuration. Obviously, this FS is much larger than that computed assuming delocal-
ized 5f’s. In addition, there are quite a number of extremal orbits (more than ten for \( H \parallel z \)). Both these aspects of the 5f\(^2\) localized FS are not in correspondence with experiments. We have in addition computed the FS corresponding to a 5f\(^3\) localized configuration; the resulting FS is shown in Fig. 20. For the localized 5f\(^3\) uranium configuration the FS exists of several open FS sheets, leading to many extremal orbits. Also, several FS sheets have a cylindrical shape, in contrast to the small, closed FS pockets detected in experiments. Hence, we observe neither for the local 5f\(^2\) FS nor for the local 5f\(^3\) FS a correspondence with experiment. Conversely, the overall agreement between the experimental and theoretical FSs computed with delocalized 5f’s can be regarded as quite good, a result which definitely supports that the theoretically predicted LSDA/GGA FS is in close agreement with the experimental Fermi surface.

E. Longitudinal spin fluctuations and dynamical symmetry breaking

1. Potential relevance of AF spin fluctuations

A significant difference between the HO and LMAF phase is the existence of an intense mode of long-lived longitudinal AF fluctuations at the wave vector \( Q_{\text{AF}} \) in the HO phase, which has been identified as a fingerprint of the HO.\(^{35,38}\) This AF mode was studied in inelastic neutron experiments by Broholm et al.,\(^{39,42}\) Wiebe et al.,\(^{53}\) and Villaume et al.,\(^{38}\) and in x-ray scattering experiments by Bernhoeft et al.\(^{129,130}\) The longitudinal fluctuation was estimated\(^{39,43}\) to amount to \( \Delta M_z \approx 1.2 \ \mu_B \), its characteristic time scale is on the order of picoseconds or slower.\(^{35}\) The potential importance of the longitudinal AF mode for the HO phase was recently emphasized by Elgazzar et al.\(^{24}\)

Although the existence of the intense AF mode in the HO phase is evident, its connection to the HO phase is not yet fully understood. A major question in the discussion is whether a mode of long-lived AF fluctuations can induce any FS gapping. In ordinary materials, a mode of (normally transversal) spin excitations would be a very weak perturba-

![FIG. 19. (Color online) The Fermi surface of URu_{2}Si_{2} in the LMAF phase computed with a 5f\(^2\) local uranium configuration.](image1)

![FIG. 20. (Color online) The Fermi surface of URu_{2}Si_{2} in the LMAF phase computed with a 5f\(^3\) local uranium configuration.](image2)
small AF moments only at the FS hot spots but for increasing moments the gap widens until the hole FS part centered along the Γ–M direction has been gapped (cf. Fig. 16). The magnitude of the computed gap develops, to a reasonable approximation, as a linear function of $M_z$. Figure 21 additionally shows that the maximal FS gapping shifts from being at the hot spots for moderate $M_z$ amplitudes to being along the Γ–M axis for the largest amplitude. For the time dependence of the gap caused by moderately slow spin fluctuations it is essential to note that the gap $\Delta$ is an even function of $M_z$. Using that the magnitude of the calculated gap is a linear function of the moment $M_z$, we can write $\Delta(t) = \alpha |M_z(t)|$, with $\alpha$ a positive constant. The time dependence of the moment gives the time dependence of the gap, $\Delta(t) = \Delta_0 |\cos(\omega t)|$, with $\Delta_0 = \Delta_{\text{LMAF}}$, the maximal gap occurring for the LMAF phase. The time-averaged, macroscopic gap $\Delta_{\text{HO}}$ follows from

$$\Delta_{\text{HO}} = \frac{1}{\tau} \int_0^\tau \Delta(t) dt = \frac{\Delta_0}{\tau} \int |\cos(\omega t)| dt = \frac{2}{\pi} \Delta_{\text{LMAF}}. \quad (1)$$

Hence, with these approximations we estimate that the time-averaged HO gap is 64% of the gap of the LMAF phase. This value is in reasonable agreement with experimental data obtained from resistivity measurements that find that the HO gap is 70–80% of that of the LMAF phase.

Consequently, in the special case of URu$_2$Si$_2$ a long-lived AF mode can indeed induce a substantial FS gapping. Moreover, the similarity detected experimentally in the FS gapping of the HO and LMAF phases can be explained by the presence of the AF mode in the HO phase and AF order in the LMAF phase. Nonetheless, in spite of the similar gapping, thermodynamic and transport properties, we emphasize that the HO and LMAF are distinct phases. In the LMAF phase the sublattice U moment $M_0$ is nonzero and thus is the standard OP for an ordered AF material. In the HO phase, conversely, $M_z = 0$ and can obviously not be a suitable order parameter for the HO. We note that in the here-developed theory it is the amplitude $M_0(T)$ of the longitudinal AF mode that determines the magnitude of the time-varying gap (cf. Fig. 21). An appropriate, observable OP for the HO that follows from our model could be derived from the macroscopic average of an even function of $M_z(t)$. As mentioned above, the FS gap is such an even function, $\Delta(t) = [M_z(t)]$. Assuming for the temperature dependence of the mode $M_z(t) = M_0(T) \cdot \cos(\omega t)$, this gives for the temperature dependence of the averaged, macroscopic gap $\Delta_{\text{HO}}(T) \approx M_0(T)$. Consequently, if the amplitude of the mode $M_0(T)$ behaves as an OP, the macroscopic, time-averaged gap $\Delta_{\text{HO}}$ should be expected to behave as an observable OP. Two experimental techniques, point contact and far-infrared optical spectroscopy revealed that the HO gap does indeed approximately behave as a typical BCS-type order parameter with temperature. Very recent STS measurements have unambiguously demonstrated this feature. We remark that in contrast to standard BCS theory the here-obtained FS gap is not symmetric around $E_F$, see Fig. 5.

A second possibility for an even function of $M_z(t)$ would be the dynamical susceptibility, expressed by the (longitudinal) dynamical spin-spin correlation function,

$$S(q, \omega') \approx \sum_{i,j} e^{i(q \cdot R_i - R_j)} \int e^{-i\omega' (S_{z,i}(t)S_{z,j}(0))} dt, \quad (2)$$

where $S_{z,i}$ is the $z$ component of the spin operator at the U position $R_i$. For relativistic materials such as actinides, it is more appropriate to use the total angular momentum, i.e., $\langle J_{z,i}(t)J_{z,j}(0) \rangle$. Approximating $\langle J_{z,i}(t)J_{z,j}(0) \rangle$ as $\langle J_{i}(t) \rangle \langle J_{j}(0) \rangle$, i.e., as $M_z(t)M_z(0)$, and using for $q$ the AF wave vector $Q_{\text{AF}}$, the dynamical spin-spin correlation function $S(q, \omega')$ would show a resonance peak at $\omega' = \omega$ that would be detectable in inelastic neutron experiments. Computing the frequency-integrated area of the peak, $A = \int S(Q_{\text{AF}}, \omega') d\omega'$, it follows that $A(T) \approx M_z^2(T) \approx \Delta_{\text{HO}}^2$. Hence, the area of the inelastic neutron peak at the AF wave vector was predicted to behave as a secondary OP; on account of its form with a temperature-behavior different from $\Delta_{\text{HO}}$. A very recent study of the inelastic AF resonance confirms that the area of the inelastic peak indeed displays OP behavior. Further investigations of its temperature behavior are warranted to determine its precise contour. In the LMAF phase the AF mode seizes to exist and hence the inelastic peak area vanishes. Adopting the spin-spin correlation function expressed through the inelastic peak area $A$ as a derived OP for the HO phase, one obtains the situation where the staggered AF moment $M_z = 0$ and $A = 0$ in the LMAF phase while conversely $M_z = 0$ and $A \neq 0$ in the HO phase, i.e., the phases have distinct OP’s (cf. the discussion regarding this in Refs. 1, 33, 86, and 133–135).

Interestingly, so far only the gap $\Delta_{\text{HO}}$ and the inelastic neutron peak intensity $A$ were proven to display typical OP behavior. Both quantities are evidently related to the intense AF mode in the HO phase, emphasizing that the AF mode is essential for the HO. Earlier $^{29}$Si NMR experiments on an oriented powder sample indicated that the NMR line width displayed $S = 1/2$ mean-field OP behavior in the HO phase. Later $^{199}$Ru NMR measurements also...
suggested an increase in the linewidth below $T_0$. Another NMR experiment, however, observed an inhomogeneous development of AF order below $T_0$,\textsuperscript{138} and a further NMR experiment did indeed detect an increase in the linewidth below $T_0$ but this effect disappeared at lower temperatures and more strain-free crystals.\textsuperscript{44} Hence, it cannot be excluded that in the early NMR measurements some inhomogeneity causing small AF patches could have influenced the result.

Second order phase transitions are characterized by a divergence of a (generalized) susceptibility at the critical temperature. We note that the critical behavior of the dynamical susceptibility $\chi(q, \omega)$ at the HO transition is consistent with the proposed importance of spin fluctuations. Its imaginary part $\chi''$ is proportional to the spin-spin correlation function, $S(q, \omega)$. Its real part $\chi'(q, \omega)$, however, was found—from inelastic neutron experiments—to exhibit a sharp cusp at $q = Q_{\text{AF}}$ and $\omega \approx 0$ when entering the HO.\textsuperscript{139} This signals a divergence of $\chi'(Q_{\text{AF}}, \omega \approx 0)$ at $T_0$, which has been broadened only by experimental resolution.

The magnetic fluctuations could also bear relevance\textsuperscript{24} to the occurrence of unconventional\textsuperscript{45–47} SC out of the HO,\textsuperscript{140} reveals a small energy shift in the HO phase. This finding might indicate the presence of time-invariance breaking in the HO phase. Also, the temperature-dependent static magnetic susceptibility of URu$_2$Si$_2$ displays a clear kink at $T_0$.\textsuperscript{11,142,143} Such feature is not uncommon at an AF ordering transition in actinide compounds, and it indicates the influence of a magnetic field on the HO. This in turn could suggest that a purely electric OP such as an electric quadrupole or hexadecapole is unlikely. Electric hexadecapolar order has been proposed for PrRu$_4$P$_{12}$ precisely because of the observed insensitivity of an ordering transition to a magnetic field.\textsuperscript{144}

Altogether, clear experimental evidence for either breaking of the time-reversal or the translational symmetry in the HO phase is so far lacking. A possible verification of the symmetry breaking due to the AF mode would require a sufficiently fast experimental technique, such as x-ray scattering or photoemission. The here-proposed breaking of the body centering could be probed in ARPES experiments, where the corresponding doubling of the unit cell would appear as a sudden folding of bands at $T_0$, together with a change in the $c^*$ axis periodicity. A further argument in favor of time-reversal and translational symmetry breaking in the HO might come from dHvA and SdH experiments. The theoretical FS (Fig. 17) computed for the symmetry-broken phase agrees well with the inferred experimental FS. This correspondence suggests that the body-centered translation vector is broken in the HO phase and most likely the time-reversal symmetry as well. Conversely, using the FS computed for the bc lattice, it is not possible to explain the observed dHvA and SdH quantum oscillations.\textsuperscript{36,92,105} Although this is consistent with the dynamical symmetry-breaking model, it cannot be excluded that other mechanisms for the HO lead to the same symmetry reduction.

V. DISCUSSION

It is elucidative to consider if hidden order phases have been discovered in other 5f materials. Apart from URu$_2$Si$_2$, the actinide dioxide NpO$_2$ has drawn considerable attention\textsuperscript{145–147} because a sharp phase transition to an unusual phase occurs below 30 K as is witnessed by specific-heat measurements.\textsuperscript{148} Intensive research during the last two decades revealed that, in the absence of any magnetic dipole moment, long-range multipolar ordering of a higher order magnetic multipole (octupole or higher) on the Np ions is likely to occur in the unusual phase below 30 K.\textsuperscript{145} These higher multipoles cannot be observed experimentally but electric quadrupolar order appearing as a secondary OP has been observed through resonant x-ray scattering (RXS) (Ref. 145) and $^{17}$O NMR.\textsuperscript{149} Theories based on 5f$^3$ localized states on the Np$^{4+}$ ion have further provided insight in the multipolar order.\textsuperscript{5,150}

Also for URu$_2$Si$_2$ a number of theories for the low-temperature order have been developed on the basis of localized or nearly localized 5f$^2$ configurations. Specifically, for URu$_2$Si$_2$ the following multipolar OPs have been proposed: electric quadrupole,\textsuperscript{14,28,50} magnetic octupole,\textsuperscript{19,21,23,51} elec-
Electric hexadecapole, and magnetic triakontadipole. Other theories on the basis of CEF considerations for a $U^{4+} 5f^2$ ionic state have also been developed.\textsuperscript{16,49} Electric quadrupolar ordering should be detectable with RXS,\textsuperscript{145} yet experimental studies gave a null result.\textsuperscript{151,152} Quadrupolar order requires an $E_1^* E_2$ scattering channel to be detected, whereas higher order multipole require at least an $E_2$ optical transition. Since the scattering cross section for $E_2$ transitions is extremely small, a detection of higher order multipoles is currently unlikely. Furthermore, most of these theories are based on a localized $U 5f^2$ configuration, but in spite of a similarity in the thermodynamic properties of $\text{URu}_2\text{Si}_2$ and NpO$_2$, treating the $5f$’s as localized in NpO$_2$ is a good approximation,\textsuperscript{53} but it is questionable if this approximation is valid for $\text{URu}_2\text{Si}_2$, too.

Triakontadipolar order in the HO phase of $\text{URu}_2\text{Si}_2$ was recently proposed\textsuperscript{27} on the basis of LSDA+$U$ calculations with a Coulomb $U$ of about 1 eV. In contrast to localized $5f^2$ theories, the $f$ electrons are relatively delocalized in this description. These LSDA+$U$ calculations predict an unusual long-range ordered AF state for $\text{URu}_2\text{Si}_2$ with parallel spin and orbital magnetic moments.\textsuperscript{154} $\text{URu}_2\text{Si}_2$ is an unconventional material and it might indeed be that such an unusual magnetic state is realized. It should be noted however that thus far not a single ordered $U$ compound has been discovered having this property. This can be understood from the strong spin-orbit interaction in actinides, which enforces always antiparallel spin and orbital moments in the early actinides. Also, conventional LSDA calculations predict antiparallel spin and orbital moments,\textsuperscript{24} and, as mentioned above, antiparallel spin and orbital moments are in fact consistent with neutron form factor measurements.\textsuperscript{98} Moreover, the experimental values deduced for the separate spin and orbital moments are in close agreement with values predicted by LSDA calculations. The Fermi surface predicted by LSDA+$U$ calculations deviates already substantial from the LSDA FS. In particular, new band crossings appear and the FS gapping feature is lost (cf. Fig. 10); thus, the LSDA+$U$ approach with a $U$ of more than 1 eV cannot explain the FS gapping appearing in the LMAF phase. The recent LSDA+$U$ calculations\textsuperscript{27} predict that, with expansion of the lattice parameter $a$, a phase transition would occur in $\text{URu}_2\text{Si}_2$ from the AF ordered phase to the same AF ordered phase but with both spin and orbital moments being opposite to the original ones. The triakontadipolar moment is predicted\textsuperscript{27} to be present in both AF phases, but it could become the main OP precisely at the transition point between these two AF phases, where the dipolar moment would vanish. It should be noted, however, that such a phase transition from one AF to another AF phase, being identical by symmetry has not been observed in $\text{URu}_2\text{Si}_2$. Also the predicted\textsuperscript{27,154} parallel spin and orbital moments are not supported by experimental observations.

Electric hexadecapolar order in $\text{URu}_2\text{Si}_2$ has been considered on the basis of a CEF Hamiltonian\textsuperscript{14} and more recently on the basis of DMFT calculations.\textsuperscript{26} Santini and Amoretti\textsuperscript{14} showed that for a $5f^2$ level scheme consisting of three singlets magnetic dipolar and electric hexadecapolar order parameters would be possible but could not reproduce the experimental features for the chosen parameter values. The recent DMFT calculations\textsuperscript{26} suggest a nearly localized $5f^2$ configuration on the uranium ion, consisting of two singlet ground levels, separated by 35 K. The HO phase with hexadecapolar OP emerges from an excitonic mixing of the CEF ground and the first excited state singlet. The two singlet levels are the same as those considered by Santini and Amoretti\textsuperscript{14} but notably with the order of ground state and first excited state reversed. The same CEF level scheme as that used in Ref.\textsuperscript{14} had been proposed earlier\textsuperscript{155} to explain the Ising-type anisotropy and maximum of the magnetic susceptibility. Although such CEF model can indeed explain certain properties of $\text{URu}_2\text{Si}_2$, it is one of the observations of the present study that on the whole the CEF model does not corroborate with many other experimental data.

The here-reported computed results suggest altogether that an applicable explanation of the properties of $\text{URu}_2\text{Si}_2$ ought to arise from an itinerant $5f$ electronic structure. A number of earlier HO theories\textsuperscript{13,17,18,20,22,156} have been based on the itinerant $5f$ picture, and more recently, two theories have emphasized the importance of dynamic spin fluctuations for the HO.\textsuperscript{24,25} The earlier theories\textsuperscript{13,17,18,20,22} could offer an explanation for some aspects of the HO but none of the models could be unambiguously confirmed experimentally (see, e.g., Refs.\textsuperscript{38, 72, and 157} for a discussion). The two HO theories that highlight the role of dynamical spin excitations have either focused on spin fluctuations at the AF wave vector\textsuperscript{24} or at the incommensurate wave vector.\textsuperscript{25} Obviously, spin fluctuations at the incommensurate wave vector as proposed in the recent theory by Balatsky \textit{et al.}\textsuperscript{25} are expected to have an influence, therefore further investigations of the incommensurate mode are needed to establish the relative importance of the two modes.

In the present work we have studied particularly the effect of the AF mode and find that its presence in the HO phase can explain the FS gapping, the broken-symmetry FS, the relation $\Delta_{\text{HO}} = (0.7–0.8)\Delta_{\text{LMAF}}$, as well as the mean-field OP behavior of $\Delta_{\text{HO}}$ and the secondary OP behavior of the inelastic neutron peak. The dynamical symmetry-breaking model nonetheless builds on the surprising and exceptional explanation of the HO phase being driven by the dynamic AF mode. Spin excitations are usually only weak perturbations of the ground state, that in conventional materials, cannot modify the ground state nor its properties. In $\text{URu}_2\text{Si}_2$, however, the exceptional situation appears to be realized that the low-lying spin excitations actually dictate the thermodynamic properties of the HO phase. Thus far a similar situation was apparently realized only in one other material, $\text{PrAu}_2\text{Si}_2$,\textsuperscript{156} which has the same crystal structure as $\text{URu}_2\text{Si}_2$. Why the low-lying AF spin excitations are so effective in $\text{URu}_2\text{Si}_2$ is related to materials’ specific aspects. The calculated energy scale of AF excitations is only on the order of 7 K, but they couple to an unexpectedly large FS reconstruction, with gaps of about 700 K. Thereby these low-lying modes can essentially modify the thermodynamic and transport properties and are indeed inherent to the HO phase.

Our calculations lastly emphasize that in $\text{URu}_2\text{Si}_2$ several remarkable, materials’ specific features are combined. First, the LMAF phase with its relatively modest total moment has a total energy that is very close to that of the PM phase. Second, the low-temperature FS of $\text{URu}_2\text{Si}_2$ supports a nest-
ing vector \( \mathbf{Q}_{\text{AF}} \) that promotes long-range AF ordering or longitudinal AF spin fluctuations. Third, the energy bands in the ST BZ exhibit accidental degenerate crossing points at \( E_F \) as well as close to \( E_F \). Fourth, a breaking of the body-centered translational symmetry together with time-reversal symmetry breaking in the LMAF phase or through longitudinal spin fluctuations causes a lifting of the degeneracy at the Dirac points and thus to the opening of a partial gap. These observations underline that to a large extent the HO is not a generic property but rather, it is borne out of the materials’ specific electronic structure.

VI. CONCLUSIONS

For a quarter century the mysterious hidden order phase in URu\(_2\)Si\(_2\) has been in the focus of many investigations. A detailed understanding of the underlying electronic structure of URu\(_2\)Si\(_2\) in both the PM and LMAF phases is required before a full explanation of the HO can be formulated. Neither the PM nor the LMAF phase appear to be exceptional, therefore first-principles electronic structure calculations should be capable of explaining the known solid-state properties of these two phases. Using \textit{ab initio} electronic structure calculations on the basis of the DFT-LSDA/GGA, the GGA+\( U \), and LDA+DMFT methodologies, we have performed an extensive study of the electronic structure of URu\(_2\)Si\(_2\). A major question has for a long time been what the applicable electronic structure of the PM and LMAF phases is, whether it has itinerant or localized uranium \( 5f \) electrons or perhaps \( 5f \) electrons with dual, i.e., both itinerant and localized characteristics (cf. Ref. 69). Our conclusion regarding this issue is that we obtain an electronic structure picture consistent with available experimental data only when we adopt delocalized \( 5f \) states.

Specifically, we find that materials’ specific DFT-LSDA/GGA electronic structure calculations on the basis of delocalized \( 5f \)'s explains the following low-temperature properties of URu\(_2\)Si\(_2\): (1) the equilibrium volume, (2) the internal \( z_\parallel \) coordinate and \( c/a \) ratio, (3) the bulk modulus and equation of state, (4) the spin and orbital magnetic moment of the LMAF phase, (5) the closeness in total energy of the PM and LMAF phases, with the LMAF phase becoming more stable under pressure, (6) the Fermi-surface gapping and instability, (7) the compensated metal character, (8) the number of holes, (9) the \( 5f \) occupation number, (10) the resistivity jump at the PM to LMAF transition, (11) crystallographic anisotropy of the resistivity, (12) the gapping in the infrared optical spectra, (13) the antiferromagnetic and incommensurate FS nesting vectors, and (14) the dHvA and SdH frequencies, as well as their angular dependence. In contrast, assuming a localized uranium \( 5f^2 \) configuration we cannot obtain a satisfactory explanation of the experimental low-temperature data.

The recent ARPES data\(^{67} \) form a notable exception to the set of low-temperature properties that are explained by \( 5f \) itinerant electronic structure calculations. A (nearly) localized \( 5f^2 \) uranium configuration appears to tally better with the observed spectral features.\(^{26} \) As the Fermi surface detected through ARPES evidently has to match that obtained with quantum oscillation techniques, more experimental investigations appear to be needed to resolve this issue.

We have additionally studied URu\(_2\)Si\(_2\) in the high-temperature PM phase, using LDA+DMFT calculations. Our DMFT calculations predict the progressive opening of a quasiparticle coherence gap at the chemical potential when temperature is reduced toward the coherence temperature.

An explanation of the hidden order requires still taking a step beyond conventional electronic structure calculations, however, the electronic structure picture underlying any explanation of the HO phase must be consistent with those underlying the PM and LMAF phases. The current investigations strongly emphasize that a well-grounded explanation of the HO has to emerge from an itinerant \( f \)-electron picture. From the presented calculations we conclude that the presence of the intense AF mode in the HO phase could explain (i) the FS gapping occurring in the HO phase, (ii) its broken-symmetry FS extremal orbits and incommensurate nesting vector, (iii) the experimentally found relation between the gaps in the HO and LMAF phases, \( \Delta_{\text{HO}} = (0.7–0.8)\Delta_{\text{LMAF}} \), and (iv) the OP behavior of the gap \( \Delta_{\text{HO}} \) and the secondary OP behavior of the inelastic dynamical susceptibility. The dynamical symmetry-breaking model appears so far to be the only theory that explains and even predicted\(^{24} \) these four properties. The importance of this mode for bringing about the HO transition is further exemplified by its occurrence and gapping in its magnon dispersion, its assistance in the entropy removal, as well as the divergent behavior of the staggered susceptibility \( \chi' \) at \( T_0 \). The presence of the inelastic AF mode at low temperatures, down into the SC phase,\(^{140} \) could provide a clue as to why an unconventional form of superconductivity develops.

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Note that we have included the additional points F, Σ, and Y that strictly do not belong to the standard bct high-symmetry points.
ELECTRONIC STRUCTURE THEORY OF THE HIDDEN...