A Hidden Population of Massive Black Holes in Simulated Dwarf Galaxies

Ray S. Sharma1, Alyson M. Brooks1,2, Michael Tremmel3, Jillian Bellovary4,5,6, Angelo Ricarte7,8, and Thomas R. Quinn9

1 Department of Physics and Astronomy, Rutgers, The State University of New Jersey, 136 Frelinghuysen Road, Piscataway, NJ 08854, USA; raysharma@physics.rutgers.edu
2 Center for Computational Astrophysics, Flatiron Institute, 162 Fifth Avenue, New York, NY 10010, USA
3 Department of Astronomy, Yale University, 52 Hillhouse Ave., New Haven, CT 06511, USA
4 Department of Physics, Queensborough Community College, City University of New York, 222-05 56th Avenue, Bayside, NY 11364, USA
5 Department of Astrophysics, American Museum of Natural History, Central Park West at 79th Street, New York, NY 10024, USA
6 The Graduate Center, City University of New York, 365 5th Avenue, New York, NY 10016, USA
7 Center for Astrophysics | Harvard & Smithsonian, 60 Garden Street, Cambridge, MA 02138, USA
8 Department of Astronomy, University of Washington, PO Box 351580, Seattle, WA 98195, USA
9 Department of Astrophysics, American Museum of Natural History, Central Park West at 79th Street, New York, NY 10024, USA

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Abstract

We explore the characteristics of actively accreting massive black holes (MBHs) within dwarf galaxies in the ROMULUS25 cosmological hydrodynamic simulation. We examine the MBH occupation fraction, X-ray active fractions, and active galactic nucleus (AGN) scaling relations within dwarf galaxies of stellar mass $10^8 M_\odot < M_{\star} < 10^{10} M_\odot$ out to redshift $z = 2$. In the local universe, the MBH occupation fraction is consistent with observed constraints, dropping below unity at $M_{\star} > 3 \times 10^9 M_\odot$. Local dwarf AGN in ROMULUS25 follow observed scaling relations between AGN X-ray luminosity, stellar mass, and star formation rate, though they exhibit slightly higher active fractions and number densities than comparable X-ray observations. Since $z = 2$, the MBH occupation fraction has decreased, the population of dwarf AGN has become overall less luminous, and as a result the overall number density of dwarf AGN has diminished. We predict the existence of a large population of MBHs in the local universe with low X-ray luminosities and high contamination from X-ray binaries and the hot interstellar medium that are undetectable by current X-ray surveys. These hidden MBHs make up $76\%$ of all MBHs in local dwarf galaxies and include many MBHs that are undermassive relative to their host galaxy’s stellar mass. Their detection relies on not only greater instrument sensitivity but also better modeling of X-ray contaminants or multiwavelength surveys. Our results indicate that dwarf AGN were substantially more active in the past, despite having low luminosity today, and that future deep X-ray surveys may uncover many hidden MBHs in dwarf galaxies out to at least $z = 2$.

Unified Astronomy Thesaurus concepts: Dwarf galaxies (416); Active galaxies (17); Hydrodynamical simulations (767); Supermassive black holes (1663)

1. Introduction

Observations over the past two decades have begun to explore the prevalence of massive black holes (MBHs) in dwarf galaxies (Shields et al. 2008; Reines et al. 2013; Moran et al. 2014; Miller et al. 2015; Trump et al. 2015; Nguyen et al. 2018; Kaviraj et al. 2019; Baldassare et al. 2020). There are now many observations out to $z \sim 2$ that indicate that dwarf galaxies are capable of hosting actively accreting MBHs (Reines et al. 2013; Lemons et al. 2015; Reines & Volonteri 2015; Pardo et al. 2016; Baldassare et al. 2017; Ahn & Seth et al. 2018; Baldassare et al. 2018; Martín-Navarro & Mezcua 2018; Mezcua et al. 2018; Birchall et al. 2020; Molina et al. 2021b), albeit at lower luminosities than in massive galaxies (Kormendy & Ho 2013). Recent studies have leveraged the observed active galactic nucleus (AGN) fraction into constraints on the occupation fraction of MBHs in dwarf galaxies (Miller et al. 2015; Trump et al. 2015; Mezcua et al. 2018; Baldassare et al. 2020; Birchall et al. 2020).

Dwarf galaxies in the local universe provide a laboratory for studying how MBHs may have formed and grown in the early universe. Theoretical work suggests that MBHs in local dwarf galaxies have grown little relative to those found in massive galaxies (Volonteri et al. 2008; Bellovary et al. 2019). Hence, MBHs in dwarf galaxies may provide insight into the early conditions of MBH seeding and growth, potentially explaining the origin of supermassive BHs found in the early universe (e.g., Vestergaard & Osmer 2009; Willott et al. 2010; Mortlock et al. 2011; Venemans et al. 2013; Wu et al. 2015). Several mechanisms have been proposed that form either light seeds ($M_{\text{seed}} \sim 10^9 M_\odot$; Devecchi & Volonteri 2009; Davies et al. 2011; Whalen & Fryer 2012; Madau et al. 2014; Taylor & Kobayashi 2014; Katz et al. 2015; Yajima & Khochfar 2016) or heavy seeds ($M_{\text{seed}} \geq 10^4 M_\odot$; Begelman et al. 2006; Johnson et al. 2013; Ferrara et al. 2014). Each formation mechanism requires different density and metallicity characteristics of the local environment and may ultimately imprint themselves on the MBH occupation fraction or mass function (Lodato & Natarajan 2006; Volonteri & Natarajan 2009; Ricarte & Natarajan 2018). See Volonteri (2010, 2012), Latif & Ferrara (2016), and Greene et al. (2020) for in-depth reviews of MBH seeding mechanisms.
MBHs within dwarf galaxies are difficult to detect outside the local universe because of their small sphere of influence (of order 0.1 pc for an MBH of mass $M_{\text{BH}} = 10^7 M_\odot$). A small sphere of influence will (1) necessitate high resolving power in order to make dynamical MBH detections and (2) restrict accretion rates, leading to less AGN activity and hence lower likelihood of detection (Baldassare et al. 2016). Recent searches for MBHs in dwarf galaxies have thus relied on searching for AGN via optical emission-line diagnostics (Barth et al. 2004; Greene & Ho 2004; Peterson et al. 2005; Greene & Ho 2007; Reines et al. 2013; La Franca et al. 2015; Sartori et al. 2015; Bentz et al. 2016a, 2016b; Marleau et al. 2017; Onori et al. 2017; Chilingarian et al. 2018), IR color selection (Satyapal et al. 2014), IR/optical coronal line emission (Satyapal et al. 2007, 2008, 2009; Cann et al. 2018, 2020; Molina et al. 2021a; Bohn et al. 2021; Cann et al. 2021; Satyapal et al. 2021), nuclear X-ray emission (Mezcua et al. 2018; Birchall et al. 2020), and optical variability (Heinis et al. 2016; Baldassare et al. 2020). See Mezcua (2017) for an overview of the various techniques for observing dwarf AGN.

Observations indicate that AGN may play a role in dwarf galaxy evolution by impacting cold star-forming gas, reminiscent of the feedback found in massive galaxies (Fabian 2012; Kormendy & Ho 2013; Somerville & Dave 2015). Bradford et al. (2018) connect AGN-like line ratios to H I gas depletion and quiescence in $M_{\text{star}} = 10^9 - 10^{10} M_\odot$ galaxies in the ALFALFA 70% survey (Haynes et al. 2011). Penny et al. (2018) identify ionized gas kinematically offset from stars in five Sloan Digital Sky Survey IV AGN with stellar masses $M_{\text{star}} < 10^{9.5} M_\odot$. Manzano-King et al. (2019) find 13 dwarf AGN with high-velocity ionized gas outflows, 6 of which have outflows with AGN-like line ratios. Dickey et al. (2019) detect AGN-like hard-ionizing radiation in 16 of 20 low-mass, isolated, quiescent galaxies with stellar masses $M_{\text{star}} = 10^{9.0} - 10^{9.5} M_\odot$. Liu et al. (2020) identify high-velocity, AGN-driven outflows in eight dwarf galaxies, where a small portion of outflowing material appears to escape into the circumgalactic medium.

On the theory side, the question of AGN impact on dwarf galaxy evolution has yielded mixed results. Cosmological simulations have historically ignored AGN in dwarf galaxies owing to resolution limitations, or assumptions on the inefficiency of AGN feedback in low-mass galaxies (e.g., Sijacki et al. 2015). Only in recent years has it become more common to allow MBHs to form in galaxies below $M_{\text{star}} < 10^{10} M_\odot$ within cosmological simulations (e.g., Habouzit et al. 2017). Analytical models have found that dwarf AGN can eject gas with higher efficiencies than supernovae (SNe; Mashyan et al. 2018). Such a mechanism may help resolve certain anomalies in concordance LCDM cosmology (Silk 2017). Kouzmann et al. (2019) explore the impact of AGN feedback by applying various AGN activity models to a high-resolution isolated dwarf galaxy simulation. They find that dwarf AGN do not directly impact star formation but do drive hotter, faster outflows that may inhibit gas inflows. Using cosmological hydrodynamic simulations, Barai & de Gouveia Dal Pino (2019) detect early $z > 4$ star formation suppression via AGN feedback. Sharma et al. (2020) find that ROMULUS25 dwarf galaxies that form relatively overmassive MBHs exhibit both suppressed star formation and depleted H I gas. Kouzmann et al. (2021) use the FABLE cosmological simulation to study population statistics of AGN in dwarf galaxies. They find that AGN can drive the kinematic misalignment between ionized gas and stars observed by Penny et al. (2018).

On the other hand, many cosmological hydrodynamic simulations indicate that strong SN feedback will disperse gas in the central regions of dwarf galaxies and preemptively halt accretion onto the MBH (Dubois et al. 2015; Anglés-Alcázar et al. 2017; Bower et al. 2017; Habouzit et al. 2017; Trebitsch et al. 2018; Barausse et al. 2020). The MBH can only begin growing again once the halo grows large enough to confine gas inflows. In particular, Habouzit et al. (2017) find that early, strong SN feedback is an important ingredient to suppress MBH growth and match the observed $M_{\text{BH}} - M_{\text{star}}$ relation in dwarf galaxies. Their SN feedback model drives winds that sweep away star-forming gas, thereby cutting off early MBH accretion. They find that a weaker thermal SN feedback model allows the MBHs to constantly grow, likely growing too large at low redshift. Barausse et al. (2020) find that MBH growth regulated by SN feedback is important for matching the bolometric luminosity function at high redshift. SN feedback suppresses MBH growth and reduces the number of low-luminosity AGN, particularly in simulations with light seedling mechanisms.

Recent analyses have shed light on the ability of cosmological simulations to model the low-mass MBHs found in low-mass galaxies. Haidar et al. (2022) perform a comparison of six large-scale ($> 100$ cMpc$^3$) cosmological simulations, finding that simulations tend to produce MBHs overmassive relative to their host galaxies. Their results indicate that simulations typically power too many AGN relative to observations, which may result from generating overmassive MBHs that consistently overaccrete, or may indicate that MBHs in dwarf galaxies are more obscured than previously thought. They suggest that tighter constraints on the AGN fraction from future X-ray facilities may better illuminate the true prevalence of MBHs among low-mass galaxies. However, contamination from X-ray binaries (XRBs) and the hot interstellar medium (ISM) will likely impact the detection of AGN with total X-ray luminosities fainter than $L_X^{\text{AGN}} < 10^{38}$ erg s$^{-1}$. Similarly, Schirra et al. (2021) analyze the properties of faint AGN among four large-scale cosmological simulations, finding that the properties of low-luminosity AGN hosts differ strongly between simulations. Their results show that the populations of low-luminosity AGN in some simulations are powered by MBHs in massive galaxies ($M_{\text{star}} > 10^{10} M_\odot$), while in other simulations they are powered by lower-mass MBHs in low-mass galaxies ($M_{\text{star}} < 10^{10} M_\odot$). These differences may be attributable to differing efficiencies of AGN feedback within each simulation. Regardless, nearly all simulations overestimate the total X-ray luminosity (AGN + non-AGN emission) in star-forming galaxies relative to observations.

In this work, we explore the properties of actively growing MBHs in dwarf galaxies out to $z = 2$ in the ROMULUS25 cosmological simulation. We select dwarf galaxies between $10^8 M_\odot < M_{\text{star}} < 10^{10} M_\odot$, straddling the mass threshold below which the effects of SN feedback are often thought to dominate over AGN feedback, $M_{\text{star}} \sim 10^9 M_\odot$ (e.g., Habouzit et al. 2017). ROMULUS25 is one of the rare examples of large, high-resolution, cosmological hydrodynamic simulations capable of resolving the evolution of dwarf galaxies as small as $M_{\text{star}} \gtrsim 10^7 M_\odot$, while also modeling MBH growth and dynamics within these galaxies. The TNG-50 (Nelson et al. 2019; Pillepich et al. 2019) and FABLE (Henden et al. 2018)
simulations reach comparable resolution but have a simplistic MBH seeding mechanism that will only track MBHs in more massive dwarfs at late times. These simulations also do not realistically follow the dynamical evolution of MBHs. The NEWHORIZON simulation (Volonteri et al. 2020; Dubois et al. 2021), which resimulates a (16 Mpc)$^3$ region of HORIZON-AGN (Dubois et al. 2014) at higher resolution, is most comparable to ROMULUS25, as it allows MBHs to exist widely within well-resolved, low-mass galaxies while also implementing a prescription for gasdynamical friction (though see Pfister et al. 2019 for a discussion on the effectiveness of gasdynamical friction relative to that of stars and dark matter). Our analysis provides insight into the prevalence of MBHs and their emitting characteristics across time. With this information, we may further learn more about the impact AGN may have on the evolution of dwarf galaxies.

In Section 2 we describe the physics of the ROMULUS25 cosmological simulation, including the resultant MBH occupation fraction. In Section 3.1 we consider local scaling relations between $L_X^A$, $M_{\text{star}}$, and SFR. In Section 3.2 we explore the evolution of active fractions across time. In Section 3.3, we predict a population of MBHs with low X-ray luminosities and high contamination by XRBs and the hot ISM. In Section 3.4 we report on the number densities of MBHs, both hidden and visible, as well as AGN out to $z=2$. We summarize our findings in Section 5.

2. Simulation

We now summarize the relevant aspects of the ROMULUS25 cosmological hydrodynamic simulation. See Tremmel et al. (2017) for a full description of the physical prescriptions.

The ROMULUS suite of cosmological hydrodynamic simulations, including ROMULUS25 (Tremmel et al. 2017) and ROMULUSC (Tremmel et al. 2019), were run with the N-body + smoothed particle hydrodynamics (SPH) code CHANGA (Menon et al. 2015; Wadsley et al. 2017). In this work, we focus on the ROMULUS25 (25 Mpc)$^3$ uniform-resolution volume. In ROMULUS25, dark matter particles have a mass of $3.39 \times 10^5 M_\odot$, gas particles have a mass of $2.12 \times 10^6 M_\odot$, and particles have a Plummer-equivalent force softening of 250 pc. ROMULUS25 contains 3.375 $\times$ more dark matter particles than gas particles to better resolve MBH dynamics (Tremmel et al. 2015). The simulations were run with a Planck 2014 ΛCDM cosmology, with $\Omega_m = 0.3086$, $\Omega_{\Lambda} = 0.6914$, $h = 0.6777$, and $\sigma_8 = 0.8288$ (Planck Collaboration et al. 2014).

Throughout our analysis, we adjust simulated stellar masses with corrections from Munshi et al. (2013) that account for the impact of aperture photometry on observed stellar masses, such that $M_{\text{star,obs}} = 0.6 M_{\text{star,sim}}$. These corrections allow us to perform a more direct comparison between simulated and observed stellar masses. ROMULUS25 resolves galaxies down to corrected stellar masses $M_{\text{star}} \gtrsim 10^7 M_\odot$.

2.1. Star Formation

Stars in ROMULUS25 form according to a star formation efficiency when cold gas has a density that exceeds a threshold for star formation:

1. star formation efficiency $e_s = 0.15$;
2. gas density threshold $n_g \geq 0.2 m_p$ cm$^{-3}$;
3. gas temperature $T < 10^4$ K.

Additionally, $0.75 \times 10^{51}$ erg of thermal energy is deposited in the ISM by Type II SNe following the “blast wave” mechanism (Stinson et al. 2006). Cooling is shut off in the gas particles that receive Type II SN energy for a time period representing the adiabatic expansion phase of a blast wave SN remnant.

These star formation parameters were tuned using a set of 80 zoom-in simulations of four halos with halo masses $M_{200} = 10^{10.5}$ - $10^{12} M_\odot$. A set of parameters were chosen by their ability to reproduce $z=0$ scaling relationships between stellar mass, halo mass, H I gas mass, and angular momentum (Cannon et al. 2011; Haynes et al. 2011; Moster et al. 2013; Obreschkow & Glazebrook 2014).

Prescriptions for metal diffusion (Shen et al. 2010), thermal diffusion (Wadsley et al. 2017), and low-temperature radiative cooling (Guedes et al. 2011) are also included in ROMULUS25, with a Kroupa (2001) initial mass function for stars. ROMULUS25 does not include high-temperature metal cooling, which should not have an effect in low-mass halos with typically low-metallicity gas (see Tremmel et al. 2019 for a more detailed discussion).

2.2. Black Hole Physics

MBHs in ROMULUS25 are seeded according to local, precollapse gas properties with thresholds and seed mass similar to a direct-collapse model (Wiklind et al. 2013; Greene et al. 2020). A star-forming gas particle is instead marked to form an MBH if it meets the following criteria:

1. low metallicity, $Z < 3 \times 10^{-4}$;
2. gas density threshold, $n_g, BH > 3 m_p$ cm$^{-3}$;
3. temperature, $T = 9500 - 10^4$ K,

effectively restricting BH creation to high-density regions in the early universe. If these criteria are met, the gas particle forms an MBH with mass $M_{BH} = 10^6 M_\odot$, accreting mass from nearby gas particles. This seed mass is somewhat higher than theoretical estimates (e.g., Volonteri 2012). The high seed mass for MBHs allows us to well resolve their dynamics over cosmic time (Tremmel et al. 2015; see below). Additionally, the early growth onto MBH progenitors may exceed 0.1 $M_\odot$ yr$^{-1}$ and is governed by processes below the resolution limits of the simulation (Hosokawa et al. 2013; Schleicher et al. 2013). In ROMULUS25, 95% of MBHs form within the first Gyr of the simulation (Tremmel et al. 2017).

ROMULUS25 employs prescriptions for MBH dynamical friction that produce realistic MBH sinking timescales (Tremmel et al. 2015). This subgrid model allows MBHs in large halos to stay centered (Kazantzidis et al. 2005; Pfister et al. 2017) but also allows some MBHs to “wander” within sufficiently shallow potentials, as has been discovered in recent observations (Reines et al. 2020) and simulations (e.g., Tremmel et al. 2018; Bellovary et al. 2019; Ricarte et al. 2021a, 2021b; Bellovary et al. 2021). The dynamical friction prescriptions, along with the “oversampling” of dark matter particles, the high seed mass, and high resolution of ROMULUS25, together help avoid unrealistic numerical heating of MBHs and help ensure accurate MBH dynamics.

MBH feedback takes the form of thermal energy injection into the surrounding environment. Thermal energy from the MBH, $E_{BH}$, is isotropically injected into the 32 nearest gas particles in some time, $dt$, following

$$E_{BH} = \epsilon_r \epsilon_f M c^2 dt,$$

(1)
where $\epsilon_r = 0.1$ is the radiative efficiency, $\epsilon_f = 0.02$ is the energy injection efficiency, and $M$ is the MBH accretion rate.

Accretion itself follows a modified Bondi–Hoyle prescription to incorporate angular momentum on unresolved spatial scales. The “instantaneous” accretion is averaged over the smallest simulation time element, typically $10^6$–$10^7$ yr, and remains Eddington limited at all times. We can write the accretion rate depending on whether the dominant gas motion is rotational, $v_{\text{rot}}$, or bulk flow, $v_{\text{bulk}}$:

$$M = \alpha \begin{cases} \frac{\pi G^2 M_{\text{BH}}^2 \rho}{(v_{\text{bulk}} + c_s^2)^{3/2}} & \text{if } v_{\text{bulk}} > v_{\text{rot}} \\ \frac{\pi G^2 M_{\text{BH}}^2 c_s}{(v_{\text{rot}} + c_s^2)^2} & \text{if } v_{\text{bulk}} < v_{\text{rot}}, \end{cases}$$

where

$$\alpha = \begin{cases} \left( \frac{n_{\text{gas}}}{n_*} \right)^3 & \text{if } n_{\text{gas}} > n_* \\ 1 & \text{if } n_{\text{gas}} \leq n_* \end{cases}$$

is the density-dependent boost factor that corrects for underestimated accretion rates due to resolution limitations (Booth & Schaye 2009), $\beta = 2$ is the corresponding boost coefficient, $n_{\text{gas}}$ is the number density of the surrounding gas, $n_*$ is the star formation density threshold, $\rho$ is the mass density of the surrounding gas, $c_s$ is the local sound speed, $v_{\text{rot}}$ is the rotational velocity of the surrounding gas at the smallest resolved scales, and $v_{\text{bulk}}$ is the bulk velocity of the surrounding gas. This calculation is performed over the 32 nearest particles. Free parameters related to accretion and feedback were optimized to reproduce various empirical scaling relations for low-mass halos ($M_{\text{th}} < 10^{12} M_\odot$) at $z = 0$ (Tremmel et al. 2017), including the observed relationship between MBH mass and stellar mass (Schramm & Silverman 2013).

Figure 1 illustrates the evolution of the MBH occupation fraction in ROMULUS25, where the occupation fraction is defined as the fraction of halos of a given stellar/halo mass containing at least one MBH within the inner 10 kpc. We do not include MBHs within the substructure of the primary halo. The high-redshift MBH occupation fraction is determined by the seeding mechanism, while the time evolution is primarily driven by structure growth. We show the occupation fraction as a function of both stellar mass and halo mass. At $z = 0.05$, the MBH occupation fraction drops below unity at $M_{\text{star}} = 3 \times 10^{10} M_\odot$, $M_{200} = 3 \times 10^{11} M_\odot$.

The local $z = 0.05$ occupation fraction is consistent with constraints from observations and empirical modeling. Dynamical MBH mass estimates (Nguyen et al. 2019) place the occupation fraction between 50% and 80% for dwarf galaxies between $10^9 < M_{\odot} < 10^{10} M_{\odot}$. X-ray-selected AGN (Miller et al. 2015) provide lower limits on the occupation fraction as a function of stellar mass. Greene (2012) estimates the occupation fraction using X-ray observations of eight optically selected AGN with $M_{\text{BH}} > 3 \times 10^5 M_\odot$, as estimated from the $M_{\text{BH}}-\sigma$ relation (Desroches et al. 2009). Baldassare et al. (2020; not shown) use variability of optical light curves from the NASA-Sloan Atlas with Palomar Transient Factory coverage to identify local, low-mass AGN. They find that AGN variability fractions are approximately constant down to stellar masses $M_{\text{star}} = 10^9 M_\odot$, suggesting that the MBH occupation fraction does not change much between $M_{\text{star}} > 10^9$ and $10^{10} M_\odot$, consistent with our estimates. The local occupation fraction also agrees with occupation fractions from Buchner et al. (2019; closeup $\rho = 0.3$, $\log M_* = 10$), who use empirical models to explore valid regions of the parameter space of critical halo mass versus MBH seed probability.
2.3. Halo and Galaxy Extraction

We use the Amiga Halo Finder (AHF; Knollmann & Knebe 2009) to extract gravitationally bound dark matter halos, as well as subhalos, and the baryonic content associated with these structures. AHF utilizes a spherical top-hat collapse technique to define the virial radius ($R_{\text{vir}}$) and mass ($M_{\text{vir}}$) of each halo and subhalo. AHF uses a spherical top-hat collapse technique to define the virial radius and total mass of each halo. The center of each halo/galaxy is calculated using a shrinking spheres approach (Power et al. 2003).

3. Results

In this work, we are primarily interested in dwarf galaxies between corrected stellar masses $10^8 M_\odot < M_{\text{star}} < 10^{10} M_\odot$ at redshifts $z = 0.05–2$. Aside from encompassing the regime where feedback is thought to change from AGN dominated to SN dominated (Habouzit et al. 2017), these limits are also similar to the ranges for dwarf AGN observed to date (e.g., Mezcua et al. 2018; Birchall et al. 2020, 2022).

Galaxies in ROMULUS25 frequently host multiple MBHs, and some galaxies have been found to host “wandering” MBHs at large radii from the center (Tremmel et al. 2018; Ricarte et al. 2021a, 2021b). We restrict our sample to MBHs within 10 kpc of the halo center, similar to the optical counterpart search radius from Birchall et al. (2020). In cases where there are multiple MBHs within the central region, we choose the most luminous. This choice is nearly always (>95% of the time) the same as choosing the most massive or most central MBH.

At low stellar masses in ROMULUS25, MBH seed masses often make up the majority of the total MBH mass. Further, the simulation does not impose restrictions on seeding multiple MBHs within close proximity, sometimes allowing multiple seeds to rapidly merge at high redshift (Ricarte et al. 2019). When observing on MBH masses, we subtract off the seed masses of all progenitor MBHs from the final mass such that

$$M_{\text{BH}} = M_{\text{BH}} - M_{\text{seeds}}.$$  (3)

Subtracting off all progenitor seed masses maintains the accreted mass from MBHs merging onto the main progenitor but removes the contribution from seeding. Ricarte et al. (2019) find that MBHs in ROMULUS25 with total masses $>10^7 M_\odot$ are dominated by accretion and that the accreted MBH mass follows the observed $M_{\text{BH}} - M_{\text{star}}$ relation down to dwarf galaxy scales. This result suggests that the accreted MBH mass may be a more realistic proxy for the true MBH mass within dwarf galaxies in ROMULUS25 (although see Bellvary et al. 2019 for a discussion on MBH accretion properties in high-resolution dwarf galaxy simulations). It is important to note that without these adjustments the total MBH masses in low-mass ROMULUS25 galaxies are overmassive compared to observed scaling relations (Sharma et al. 2020), which indicates that the seed masses are unrealistically large. It is possible that the fiducial Bondi accretion model within ROMULUS25 is unsuitable for modeling accretion in dwarf galaxies—an alternate accretion model that allows for the same growth with lower seed masses may be more realistic.

In order to calculate bolometric luminosities for MBHs, we follow the Churazov et al. (2005) two-mode accretion model that distinguishes between radiatively efficient and inefficient AGN. Many simulations, including ROMULUS25, use a single, radiatively efficient accretion model for internally calculating feedback (Hirschmann et al. 2014). Using a two-mode accretion model in post-processing reduces the number of low-luminosity AGN, though it misses the feedback effects of radiatively inefficient AGN. We convert the instantaneous accretion rate, $\dot{M}_{\text{BH}}$, such that

$$L_{\text{bol}} = \left\{ \begin{array}{ll}
\epsilon_0 \dot{M}_{\text{BH}} c^2, & f_{\text{edd}} \geq 0.1 \\
10 f_{\text{edd}} \epsilon_0 \dot{M}_{\text{BH}} c^2, & f_{\text{edd}} < 0.1,
\end{array} \right.$$  (4)

with radiative efficiency $\epsilon_0 = 0.1$ and Eddington fraction $f_{\text{edd}} = \dot{M}_{\text{BH}} / \dot{M}_{\text{edd}}$. Note that we calculate the Eddington fraction using the accreted MBH mass, $\dot{M}_{\text{acc}}^c$, and hence $f_{\text{edd}}$ is higher than when calculated using the total MBH mass. In the two-mode accretion model, higher $f_{\text{edd}}$ leads to higher luminosities (and hence higher, more conservative estimates of the active fractions in Section 3.2) among radiatively inefficient AGN. To estimate X-ray luminosities, $L_\text{AGN}$, between 0.5 and 10 keV, we apply Shen et al. (2020) bolometric corrections in the soft (0.5–2 keV) and hard (2–10 keV) X-ray bands.

As done in Koudman et al. (2021) and Haidar et al. (2022), we calculate mock X-ray luminosities for dwarf galaxies by modeling the contributions from XRBs and emission from the hot ISM. We model high-and low-mass XRB contributions using the Lehmer et al. (2016) relation:

$$L_\text{X}^{\text{XRB}} = \alpha_0 (1 + z)^{\gamma} M_{\text{star}} + \beta_0 (1 + z)^{\delta} \text{SFR},$$  (5)

where $(\log \alpha_0, \gamma, \log \beta_0, \delta) = (29.04, 3.78, 39.38, 0.99)$ for soft X-rays and $(29.37, 2.03, 39.28, 1.31)$ for hard X-rays. Emission from hot gas follows the Mineo et al. (2012) relation, which establishes a relationship between (0.5 and 2 keV) X-ray luminosity of the diffuse ISM and the star formation rate (SFR):

$$L_\text{X, soft} = \alpha_1 \times 10^{38} \times \left( \frac{\text{SFR}}{M_\odot \text{yr}^{-1}} \right).$$  (6)

We calculate the hot gas contribution in the hard X-ray band by assuming a photon index $\Gamma = 3$. Hence, we can write the total (0.5–10 keV) X-ray luminosity for a galaxy:

$$L_\text{X} = L_\text{X}^{\text{AGN}} + L_\text{X}^{\text{XRB}} + L_\text{X}^{\text{Gas}}.$$  (7)

In order to more closely compare with observations from Mezcua et al. (2018) and Birchall et al. (2020), we classify AGN in ROMULUS25 such that their X-ray luminosity is significantly greater than the contribution from non-AGN sources, $L_\text{X} > 2L_\text{X}^{\text{XRB}+\text{Gas}}$. We do not model emission from background quasars, which have been found to contaminate observations (e.g., Reines et al. 2020).

Recent work by Kristensen et al. (2021) indicates that among low-mass ($10^9 M_\odot < M_{\text{star}} < 3 \times 10^9 M_\odot$) galaxies in three large-scale cosmological simulations, non-AGN are more likely than AGN to be found in a denser environment with closer galactic neighbors. Their results also indicate that galaxies that maintain close proximity to other galaxies are less likely to exhibit star formation or AGN activity. While we do not show results from subhalos of the target halo in this work, we do not make further selections based on galaxy environment. Although we lose the ability to identify the impact of galaxy environment, we are able to make more direct
comparisons with Mezcua et al. (2018) and Birchall et al. (2020), who similarly do not make selections on galaxy environment.

3.1. Dwarfs in the Local Universe

Dwarf galaxies have been found to exhibit relationships between MBH X-ray luminosity, stellar mass, and SFR similar to those found in massive galaxies (e.g., Aird et al. 2017, 2018). These relationships may illuminate any connection between MBH activity and star formation, as well as provide insight into how readily dwarf AGN at each mass scale may be observed.

Figure 2 shows the relationships between $L_{\text{X}}^{\text{AGN}}, M_{\text{star}},$ and SFR for dwarf galaxies at $z = 0.05$ that host an MBH in the central 10 kpc. Each point that satisfies the contamination threshold $L_{\text{X}}^{\text{AGN}} > 2L_{\text{X}}^{\text{XRB+Gas}}$ is colored according to the instantaneous Eddington fraction. Dwarfs that fail the contamination threshold are marked in gray. Arrows mark dwarfs with extremely low luminosities or zero star formation, with SFRs averaged over the past 100 Myr.

We compare our results with X-ray-selected dwarf AGN from Mezcua et al. (2018), who identify 40 dwarf AGN between $10^7 M_\odot < M_{\text{star}} < 3 \times 10^9 M_\odot$ from the Chandra-COSMOS-Legacy survey out to $z < 2.4$, in the full 0.5–10 keV band. We only show their sample up to $z < 0.25$ for better comparison with our local dwarfs. We also include results from Birchall et al. (2020), who provide 61 X-ray-selected dwarf AGN that fall within both the optical MPA-JHU footprint and X-ray 3XMM footprint. Birchall et al. (2020) identify dwarfs with $M_{\text{star}} < 3 \times 10^9 M_\odot$ out to $z < 0.25$ in the harder 2–12 keV band. Both observational sets calculate the AGN X-ray luminosity by subtracting off contributions to the total X-ray luminosity from XRBs and the hot ISM.

Overall, the scaling relationships between our uncontaminated luminous dwarfs are consistent with observed relations of local dwarf AGN. Simulated dwarfs tend not to reach the highest luminosities found in the observations, $L_{\text{X}}^{\text{AGN}} > 10^{42} \text{ erg s}^{-1}$, though these observed luminous dwarfs are typically at slightly higher redshifts, $z \gtrsim 0.1$. Our dwarfs strike a middle ground between the higher luminosities found in Mezcua et al. (2018) and the lower luminosities found in Birchall et al. (2020), which are at least partially due to the harder X-ray band in which Birchall et al. (2020) observe.

There exists a large population of dwarfs at low luminosities and high contamination ($L_{\text{X}}^{\text{AGN}} < 2L_{\text{X}}^{\text{XRB+Gas}}$) that are not found in observations. These contaminated dwarfs make up 70% of dwarfs with MBHs at $z = 0.05$. This hidden population that is missed by observations suggests that typical relationships between $L_{\text{X}}^{\text{AGN}}$ and both $M_{\text{star}}$ and SFR are dramatically impacted by a survey’s ability to detect low luminosities and distinguish contaminated AGN. Indeed, the largest scatters in these relationships are found at dwarf galaxy masses, suggesting that the relationships found in massive galaxies may break down for dwarf galaxies. We further explore the role of detection threshold and X-ray contaminants in Section 3.3.

Many simulated dwarfs also exhibit quenched star formation. Since MBH accretion is, on average, correlated with SFR among star-forming main-sequence galaxies in ROMULUS25 (Ricarte et al. 2019), it is unsurprising that many low-luminosity MBHs are found in galaxies with little star formation. However, a surprising number of quenched dwarfs exhibit an actively accreting MBH, in line with X-ray observations from Aird et al. (2019) and Carraro et al. (2020), which both find elevated AGN activity among quiescent galaxies relative to star-forming galaxies at the same SFR. This phenomenon suggests that the mechanism that fuels star formation is, at least in some dwarfs, separate from that which fuels MBH activity. It may also indicate a connection between active accretion and the suppression of star formation in some dwarfs.

It is worth noting that 20% of quenched (zero SFR) dwarf galaxies in ROMULUS25 are isolated, meaning that they are (i) outside the virial radius of a larger halo and (ii) farther than $>1.5$ Mpc from any neighboring galaxy with $M_{\text{star}} > 2.5 \times 10^9 M_\odot$ (Geha et al. 2012). The high number of quenched, isolated dwarf galaxies in ROMULUS25 is in tension with observations of local...
Figure 3. Fraction of all galaxies containing an active MBH vs. stellar mass, in bins of redshift. Activity is defined by three X-ray luminosity thresholds, $L_{\rm X}^{\rm AGN} > [39, 40.5, 41.5]$. The MBH occupation fraction (black dashed) sets upper limits on the active fraction. Error bars mark 95% binomial constraints from X-ray observations. The MBH occupation fraction sets upper limits on the active fraction. Error bars mark 95% binomial constraints from X-ray observations.

Next, we examine the evolution of AGN prevalence across cosmic time. The active fraction is defined here as the fraction of all galaxies emitting above a given $0.5$–$10$ keV X-ray luminosity threshold. Figure 3 shows the active fraction for all galaxies in ROMULUS25 above $M_{\star} > 10^9 M_\odot$ as a function of stellar mass, in bins of redshift. We define activity using three X-ray luminosity thresholds and include observational constraints from X-ray observations. We calculate the active fraction in lower-luminosity AGN but does not change fractions among the two highest AGN luminosities shown here.

In addition to expressing a lower occupation fraction than massive galaxies, low-mass galaxies are overall less luminous and hence exhibit a lower active fraction. While the most massive galaxies consistently emit well above $L_{\rm X}^{\rm AGN} > 10^{41.5}$ erg s$^{-1}$, only the higher-mass dwarf galaxies between $10^8 M_\odot < M_{\star} < 10^9 M_\odot$ reach such high luminosities, and most prominently around $z = 2$. Dwarf galaxies peak in activity around $z = 2$ and drop off in luminosity with time, steeply dropping around $z = 0.05$. By $z = 0.05$, approximately 2% of galaxies between $10^8 M_\odot < M_{\star} < 10^9 M_\odot$ and 8% of galaxies between $10^9 M_\odot < M_{\star} < 10^{10} M_\odot$ host an X-ray-detectable MBH brighter than $L_{\rm X}^{\rm AGN} > 10^{40.5}$ erg s$^{-1}$. For reference, this luminosity threshold is similar to the detection threshold for the $4.6$ Ms Chandra-COSMOS-Legacy observations at $z = 0.05$ in the full X-ray band (Suh et al. 2017). Despite the steep drops in luminosity, dwarf galaxies at $z = 0.05$ in ROMULUS25 exhibit a factor of a few higher active fractions than found in X-ray observations.

There may be a few reasons why our dwarf active fractions are higher than the observed ones: (1) The high seed mass in ROMULUS25 may ultimately drive unrealistically high accretion rates onto dwarf AGN at the wrong times. Although our dwarf AGN follow observed local scaling relations, including the $M_{\rm BH} = M_{\star}$ relation for more massive galaxies, dwarfs in reality may follow a different $M_{\rm BH} = M_{\star}$ relation from massive galaxies (Reines & Volonteri 2015). Further, it is possible to correctly predict the empirical relationships while still overpredicting the AGN fraction if the timing of the simulated MBH accretion history is wrong. Indeed, Ricarte et al. (2019) find that the luminosity density of AGN in ROMULUS25 is high relative to observations at $z = 0$. (2) MBHs in ROMULUS25 accrete on timescales greater than $\sim 10^7$ yr. A duty cycle of order $10^4$ yr may account for factor $\sim 10$ differences in observed fraction. (3) Although our occupation fractions are consistent with observations, changing the MBH seeding model to be more restrictive may alleviate the AGN fraction discrepancy while maintaining agreement with observational constraints on the occupation fraction. This change is largely equivalent to changing the seeding model of the simulation. (4) As with other cosmological simulations, we do not directly measure AGN luminosities but instead assume a radiative efficiency to convert MBH accretion rates. We convert accretion rates using a two-mode accretion model where radiative efficiency depends on Eddington fraction (Churazov et al. 2005). However, there is no consensus on the Eddington fraction distributions that underlie accretion models for low-luminosity AGN, and hence the precise dependence on Eddington fraction is unclear (Trump et al. 2011; Weigel et al. 2017; Pesce et al. 2021). Further, we do not take into account AGN obscuration. Although the obscuration fraction among AGN is still uncertain, population synthesis models from Tasnim Ananna et al. (2019) indicate that 50% of AGN within $z < 0.1$ may be Compton-thick. (5) Similarly, we rely on existing bolometric corrections from Shen et al. (2020) to calculate X-ray luminosities, but these corrections are calibrated for more massive galaxies. As with radiative efficiency, there is evidence that X-ray bolometric corrections depend on Eddington fraction (Lusso et al. 2012). Radiative efficiency and bolometric corrections are closely linked quantities and together form a free parameter that is not well constrained within dwarf galaxies (Baldassare et al. 2017). Indeed, Latimer et al. (2021) find evidence that IR-selected dwarf AGN are comparatively underluminous in the X-ray regime, suggesting a breakdown in typical luminosity scaling relations at dwarf masses, as we have found. Moreover, Molina et al. (2021b) identify 81 AGN candidates using coronal line emission in the optical regime and find that 49% cannot be correctly identified using other AGN-detection techniques, including X-ray detection.

Figure 4 illustrates how the active fraction differs when switching from a two-mode accretion model to a single-mode model in which $L_{\rm bol} = \epsilon R M_{\rm BH} c^2$. We calculate the active
fraction for the two-mode model using a flat bolometric correction, \( k_{\text{bol, X}} = L_{\text{bol}} / L_{X, \text{AGN}} = 25 \). We also explore the luminosity-dependent bolometric corrections obtained from X-ray-selected AGN by Lusso et al. (2012), applying them to the two-mode accretion model. For the low luminosities found among ROMULUS25 dwarfs, the extrapolated luminosity-dependent corrections are approximately \( k_{\text{bol, X}} \sim 10 \). Lusso et al. (2012) provide Eddington fraction bolometric corrections for hard X-rays, but we do not use those corrections since their AGN do not extend down to the Eddington fractions found in ROMULUS25.

Single-mode accretion, wherein even MBHs with low Eddington fractions radiate equally efficiently, produces luminosities that are significantly higher than in two-mode accretion. Active fractions for single-mode accretion at a given stellar mass are approximately 1 dex higher than observations from Birchall et al. (2020). On the other hand, applying a flat bolometric correction of \( k_{\text{bol, X}} = 25 \) (~5× larger than corrections from Shen et al. 2020) to the two-mode model yields even closer consensus with observations. The luminosity-dependent corrections derived from X-ray AGN yield even lower active fractions, despite having \( k_{\text{bol, X}} \sim 10 \) (only ~2× larger than corrections from Shen et al. 2020). It is worth noting that among massive galaxies, high bolometric corrections of order \( k_{\text{bol}} \sim 100 \) are typically only found in Compton-thick AGN and/or AGN with particularly high Eddington fraction (Vasudevan & Fabian 2007; Lusso et al. 2012; Brightman et al. 2017), while the dwarfs in ROMULUS25 typically exhibit Eddington fractions \( f_{\text{Edd}} < 10^{-2} \).

### 3.3. Population of Hidden MBHs

Next, we illuminate a population of MBHs within ROMULUS25 that may be hidden from current X-ray surveys. We explore the impact of current X-ray detection limits, contamination of low-luminosity AGN by XRBs and the hot ISM, and off-center (outside 2 kpc of the galaxy center) versus central (within 2 kpc of the galaxy center) MBHs within dwarf galaxies on the detected population of dwarf AGN.

Using semianalytic models of MBH growth in low-mass galaxies, Pacucci et al. (2018) find that the tight scaling relationship between MBH mass and bulge stellar velocity dispersion, \( \sigma_* \), found in high-mass galaxies tends to overpredict \( M_{\text{BH}} \) in low-mass galaxies.

Observations indicate that the tight scaling relationships between \( M_{\text{BH}} \) and \( M_{\text{star}} \) (or velocity dispersion, \( \sigma_* \)) found among massive galaxies tend to overpredict \( M_{\text{BH}} \) in low-mass galaxies (Reines & Volonteri 2015). Using semianalytic models, Pacucci et al. (2018) find that MBHs that are undermassive relative to the expected \( M_{\text{BH}} - \sigma_* \) or \( M_{\text{BH}} - M_{\text{star}} \) relations tend to have grown from weakly accreting low-mass seeds, which may fall below typical survey detection thresholds. This trend suggests that the observed \( M_{\text{BH}} - \sigma_* \) (and similarly the \( M_{\text{BH}} - M_{\text{star}} \)) relation in massive galaxies only appears to extend to low-mass galaxies because those MBHs are detectable, when there may in fact be many undetected, low-luminosity MBHs that fall below the relation (Baldassare et al. 2020).

Figure 5 illustrates how varying the X-ray detection limit alters the detected distribution of \( M_{\text{BH}} / M_{\text{star}} \) for dwarf galaxies at \( z = 0.05 \). As a baseline, we show the underlying distribution of \( M_{\text{BH}} / M_{\text{star}} \) without cuts on X-ray luminosity for dwarfs in each stellar mass bin. In each stellar mass bin, setting luminosity thresholds as low as \( L_{X, \text{AGN}} > 10^{39} \) erg s\(^{-1}\) removes the majority of MBHs from detection, including many of the most undermassive MBHs. Setting a threshold at \( L_{X, \text{AGN}} > 10^{39} \) erg s\(^{-1}\) misses 78% of MBHs in dwarfs between \( 10^8 M_\odot < M_{\text{star}} < 10^{10} M_\odot \) and 38% of MBHs in dwarfs between \( 10^9 M_\odot < M_{\text{star}} < 10^{10} M_\odot \). Increasing the threshold to \( L_{X, \text{AGN}} > 10^{41.5} \) erg s\(^{-1}\) samples a strongly biased sample of MBHs, keeping only those few with \( \log (M_{\text{BH}} / M_{\text{star}}) \sim -3 \). However, the median of the distribution changes little regardless of detection threshold, different from what is found by Pacucci et al. (2018).

Figure 6 further shows how varying the acceptable contamination from XRBs and hot gas impacts the detected distribution of \( M_{\text{BH}} / M_{\text{star}} \), where we define \( f_{\text{cont}} = L_{X, \text{AGN}} / L_{X, \text{XRB + Gas}} \). Throughout this work we have adopted \( f_{\text{cont}} = 2 \) as the standard contamination threshold. Setting a contamination threshold as low as \( f_{\text{cont}} = 1 \) similarly misses the most undermassive MBHs. A threshold set at \( f_{\text{cont}} = 1 \) misses 77% of MBHs in dwarfs between \( 10^8 M_\odot < M_{\text{star}} < 10^{10} M_\odot \) and 60% of MBHs in dwarfs between \( 10^9 M_\odot < M_{\text{star}} < 10^{10} M_\odot \). As with setting luminosity thresholds, the median of the distribution changes little when setting contamination thresholds.

Another complicating factor in MBH detection is distance from the galaxy center. Both simulations (Bellovary et al. 2019, 2021) and observations (Mezcua & Domínguez Sánchez 2020; Reines et al. 2020; Greene et al. 2021) have
found MBHs at large radii from the centers of dwarf galaxies. Galaxies in ROMULUS25 have also been found to frequently host off-center MBHs at radii >2kpc from the halo center (Ricarte et al. 2021a, 2021b). Off-center MBHs frequently exhibit low luminosities (Mezcua & Domínguez Sánchez 2020) and low accretion efficiencies (Ricarte et al. 2021b), implying that the detection of off-center MBHs is intrinsically tied to luminosity thresholds and contamination. When selecting our initial sample of MBH hosts, we search for the brightest MBH within 10 kpc of the halo center, which includes the majority of off-center MBHs. At $z = 2$, 20% of dwarfs with MBHs have their brightest MBH outside of 2 kpc. Over time, bright off-center MBHs become even less common, as the percentage drops to 11% by $z = 0.05$. Regardless of redshift, approximately 98% of MBHs in dwarf galaxies are found within 10 kpc of the halo center.

To further quantify the combined impact of off-center MBHs, X-ray luminosity limits, and contamination on the detection of MBHs, Figure 7 shows the $M_{\text{BH}}^{\text{acc}} - M_{\text{star}}$ relation up to $M_{\text{star}} < 10^{11} M_\odot$ with the same set of X-ray luminosity thresholds and acceptable contamination fractions. We distinguish between galaxies with central (within 2 kpc of the galaxy center) and off-center (outside 2 kpc of the galaxy center) MBHs. In cases where there are multiple central or multiple off-center MBHs, we choose the brightest one. For reference, we overplot observed relations for massive galaxies from Schramm & Silverman (2013) and Kormendy & Ho (2013). There exists a “hidden” population of MBHs at both low luminosities ($L_X^{\text{AGN}} < 10^{39}$ erg s$^{-1}$) and high contamination ($L_X^{\text{AGN}} < L_X^{\text{XRB+Gas}}$) that are undetectable by current instruments. Approximately 74% of central MBHs in dwarf galaxies are hidden by these criteria. While the majority of hidden central MBHs lie directly along the observed relation, a significant number are found well below the relation. On the other hand, 88% of off-center MBHs in dwarf galaxies are further hidden by low luminosities and/or contamination, and the majority are significantly undermassive. These results indicate that increasing the detection sensitivity alone would not allow hidden MBHs to be reliably detected since they are often heavily contaminated and sometimes exist at large distances from the galaxy center. Detecting these hidden MBHs with X-rays, especially MBHs that are far off-center, would require higher instrument sensitivity in addition to (i) a better understanding of XRBs + hot ISM emission in dwarf galaxies (e.g., in the low-metallicity, low-SFR regimes as discussed in Lehmer et al. 2021) and/or (ii) multiwavelength imaging of the AGN.

Although we predict that sensitivity limits will cause surveys to miss many undermassive MBHs, common detection limits only slightly impact the fit relation. Fits to the total (central + off-center) $M_{\text{BH}}^{\text{acc}} - M_{\text{star}}$ relation below $M_{\text{star}} < 10^{10} M_\odot$ at $z = 0.05$ reveal that setting a $L_X^{\text{AGN}} > 10^{39}$ erg s$^{-1}$ detection limit simply shifts the relation up by 0.1 dex while keeping the slope intact. The small change in predicted $M_{\text{BH}}$ is not large enough to explain the 1 dex difference found in Pacucci et al. (2018). Their abundant undermassive MBHs are likely the result of their mixed seeding mechanism that generates both high-mass ($M_{\text{seed}} > 10^2 M_\odot$) and weakly accreting low-mass ($M_{\text{seed}} < 10^2 M_\odot$) seeds.
3.4. Number Density of Detectable MBHs

Finally, we report on the spatial number density of hidden MBHs and AGN relative to the total number density of MBHs in ROMULUS25. The initial number of MBHs within ROMULUS25 is set by the seeding prescription, while the evolution with time is determined by the merger rates. In particular, the seeding prescription determines where and with what frequency MBHs can form. Since the majority of MBHs in ROMULUS25 form prior to $z = 5$ (Tremmel et al. 2017), the evolution of the number density from $z = 2$ to $z = 0.05$ is driven by MBH mergers. Although we do not directly report on MBH merger rates, it is worth noting that Volonteri et al. (2020) find that MBH merger rates tend to increase among low-mass galaxies when moving to higher-resolution simulations. Lower-resolution simulations tend to miss mergers of low-mass galaxies and hence underpredict the MBH merger fraction. It is likely that moving to higher resolutions than ROMULUS25 would lead to differing results for the evolution of the MBH number density.

Figure 8 tracks the comoving number density of MBHs as a function of redshift. We include lines for all MBHs in well-resolved halos, “detectable” MBHs in dwarf galaxies ($L_{X}^{\mathrm{AGN}} > 10^{39}$ erg s$^{-1}$ and $L_{X}^{\mathrm{AGN}} > 2 L_{X}^{\mathrm{XRB} + \mathrm{Gas}}$), and hidden MBHs in dwarf galaxies ($L_{X}^{\mathrm{AGN}} < 10^{39}$ erg s$^{-1}$ and/or $L_{X}^{\mathrm{AGN}} < 2 L_{X}^{\mathrm{XRB} + \mathrm{Gas}}$). We also show the evolution of the AGN number density from ROMULUS25 alongside X-ray observations (Ueda et al. 2014; Aird et al. 2015; Buchner et al. 2015) and EAGLE (Rosas-Guevara et al. 2016) in the hard X-ray band with $L_{X}^{\mathrm{hard}} > 10^{42}$ erg s$^{-1}$.

The total number density of MBHs decreases over time, from $n_{\mathrm{BH}} = 8 \times 10^{-2} \, \text{cMpc}^{-3}$ at $z = 2$ down to $n_{\mathrm{BH}} = 5 \times 10^{-2} \, \text{cMpc}^{-3}$ at $z = 0.05$. These number densities are within a factor of a few of estimates from Volonteri (2010), who estimate $n_{\mathrm{BH}} = 0.02 - 0.1 \, \text{cMpc}^{-3}$ at $z = 0$; slightly lower than those from Buchner et al. (2019), who find $n_{\mathrm{BH}} > 0.01 \, \text{cMpc}^{-3}$ at $z = 0$ for their seed-independent empirical model; and in line with those from EAGLE (Rosas-Guevara et al. 2016), which finds $n_{\mathrm{BH}} = 7.2 \times 10^{-2} \, \text{cMpc}^{-3}$ at $z = 0.1$ with MBH seed mass $M_{\mathrm{seed}} = 1.48 \times 10^{7} \, \text{M}_{\odot}$. Among dwarf galaxies, visible and hidden MBHs are found in equal amounts at $z = 2$, approximately with densities $2 \times 10^{-2} \, \text{cMpc}^{-3}$, but at $z = 0.05$ hidden dwarfs are more common by a factor of 3, around $2 \times 10^{-2} \, \text{cMpc}^{-3}$.

AGN follow a slightly different shape and evolution than the full population of MBHs. The number densities of AGN are instead determined by the accretion history of the underlying...
population of MBHs. As explored in Section 3.2, AGN have decreased in both luminosity and prevalence since \( z = 2 \) within the simulation. The number of AGN above \( L_{X,\text{hard}} > 10^{42} \) erg s\(^{-1}\) peaks at \( z = 2 \) around \( n_{\text{AGN}} = 1.2 \times 10^{-7} \) cMpc\(^{-3}\). AGN are most rare at \( z = 0.05 \), at \( n_{\text{AGN}} = 4.2 \times 10^{-4} \). These estimates are slightly higher than those from EAGLE and results in the same band (Ueda et al. 2014; Aird et al. 2015; Buchner et al. 2015; Rosas-Guevara et al. 2016) at \( z \sim 0 \). This difference is likely tied to our overprediction of the AGN fraction.

4. Caveats

As discussed in Sharma et al. (2020), the primary caveat of our analysis is the relatively large mass of MBHs in ROMULUS25. Accretion rates in the lowest-mass MBHs are inflated by the relatively large MBH seed mass. A lighter MBH seed mass might instead drive a different accretion history owing to the lower average accretion rates. It is worth noting that our local dwarfs exhibit X-ray luminosities consistent with AGN observations down to \( M_{\text{BH}} > 10^8 \) M\(_{\odot}\) (see Section 3.1) and follow the observed \( M_{\text{BH}} - M_{\text{stellar}} \) relation at low redshift (Sharma et al. 2020). It is not clear whether a lighter MBH seed would push luminosities below what is observed or alter their agreement with local scaling relations. On the other hand, less accretion may mitigate the higher AGN fractions found in ROMULUS25 (see Section 3.2).

A lighter MBH seed mass may also lead to more frequent seeding of MBHs, though constraints from simulations indicate that a lighter seed formation channel may ultimately lead to similar present-day MBH number densities (Greene et al. 2020). Occupation fractions are often thought to differ between seed formation channels, though Ricarte & Natarajan (2018) find that light seeds may produce a large range of occupation fractions, with overlap with heavy seed mechanisms. Given these results, it is not obvious how MBH occupation would be impacted if ROMULUS25 had a lighter seed mass.

There are a number of uncertainties that we do not fully address when presenting results for the detected fraction of MBHs in dwarf galaxies. For one, we do not take into account uncertainties on the contaminant relations themselves. The observed relations that govern how we calculate \( L_{X,\text{XRB}} \) and \( L_{X,\text{MBH}} \) may differ from real dwarfs. Indeed, results derived from six large-scale cosmological simulations by Haidar et al. (2022) indicate that it is possible to qualitatively reproduce the observed \( M_{\text{BH}} - M_{\text{stellar}} \) and SFR – \( M_{\text{stellar}} \) relations but still yield different estimates of the detected fraction. A closer examination of the quiescent fractions in ROMULUS25 may help validate the MBH detected fractions shown here.

As found in Section 3.2, comparisons with observations are sensitive to the choice of accretion model, bolometric corrections, and AGN obscuration. Active fractions are much closer to what is observed when we calculate luminosities with two-mode accretion, but ROMULUS25 internally uses a single-mode model when implementing feedback. It is only our post-processing results that suggest that the single-mode thermal feedback in ROMULUS25 does not properly emulate what happens in reality. A feedback model that depends on accretion rate, as found in some other cosmological simulations (Sijacki et al. 2015; Dubois et al. 2016; Weinberger et al. 2017; Davé et al. 2019), may better match reality. If it is true that the radiative efficiency decreases for low \( f_{\text{Edd}} \), it is still unclear what form the feedback (and hence the radiative efficiency) should take at low \( f_{\text{Edd}} \). A closer examination of the Eddington fraction distributions, full spectral energy distributions, and obscuration fraction among dwarf AGN will be required to constrain dwarf activity in the future.
5. Conclusions

In this work we explore the characteristics of activity in MBHs within the high-resolution cosmological hydrodynamic simulation ROMULUS25. We study the population statistics of MBHs in galaxies above $M_{\text{star}} > 10^8 \, M_\odot$, including the occupation and number densities of MBHs in galaxies out to $z = 2$. We focus on investigating the properties of MBH activity in dwarf galaxies between $10^7 \, M_\odot < M_{\text{star}} < 10^{10} \, M_\odot$.

In summary, we find the following:

1. Figure 1 shows that the MBH occupation fraction at $z = 0.05$ drops below unity for galaxies below $M_{\text{star}} < 2 \times 10^{10}$, in broad agreement with observed constraints from X-ray-selected AGN (Miller et al. 2015), X-ray observations of late-type spiral galaxies (Desroches et al. 2009; Greene 2012), dynamical MBH estimates (Nguyen et al. 2019), and variability-selected dwarf AGN (Baldassare et al. 2020).

2. MBHs in dwarf galaxies around $z = 0.05$ follow established scaling relations between $L_X^{\text{AGN}}$, $M_{\text{star}}$, and SFR that have been observed in dwarf AGN (Mezcua et al. 2018; Birchall et al. 2020). Figure 2 shows that these relations hold for AGN relatively uncontaminated by XRBs and hot gas emission but break down at low stellar masses for weakly accreting and/or strongly contaminated sources.

3. Dwarf AGN are rare in ROMULUS25, but not as rare as expected from X-ray observations. The dwarf active fractions in Figure 3 evolve strongly with time, peaking at $z = 2$ and dropping steeply toward the present day. Despite the steep evolution, the active fractions at $z = 0.05$ are slightly higher than observations of local dwarf AGN (Mezcua et al. 2018; Birchall et al. 2020).

4. Changes in radiative efficiency and bolometric corrections can dramatically affect activity among MBHs in simulated dwarf galaxies, as illustrated in Figure 4. Constraining these quantities will require observations of Eddington fraction distributions and spectral energy distributions among dwarf AGN.

5. We predict a considerable population of both central and off-center MBHs at $z = 0.05$ that are undetectable by current X-ray facilities. These MBHs often exhibit luminosities lower than current X-ray detection limits ($L_X^{\text{AGN}} < 10^{33} \, \text{erg s}^{-1}$) in addition to high X-ray contamination ($L_X^{\text{AGN}} < L_X^{\text{XRB+Gal}}$). Figures 5 and 6 indicate that this population of hidden MBHs does not significantly change the observed $M_{\text{BH}}$-$M_{\text{star}}$ relation for central MBHs, though off-center MBHs are nearly all undermassive. Figure 7 shows that 74% of central MBHs in dwarf galaxies and 88% of off-center MBHs in dwarf galaxies are hidden by low luminosities and/or high contamination.

6. Figure 8 shows that the number densities of MBHs in ROMULUS25 are consistent with direct-collapse seeding estimates from empirical models (Buchner et al. 2019), analytic models (Volonteri 2010), and the EAGLE cosmological simulation (Rosas-Guevara et al. 2016). As expected from elevated active fractions, AGN are somewhat more common than in X-ray observations (Ueda et al. 2014; Aird et al. 2015; Buchner et al. 2019).

Detecting MBHs in dwarf galaxies with X-ray observatories has been a challenging endeavor, due to the combination of low intrinsic luminosities, the possibility of being off-center, and high chances of contamination from XRBs, background quasars, and low surface brightness hot gas. Our work here highlights how a nonnegligible fraction of MBHs are “hidden” to most observations owing to a combination of low accretion luminosities and blending in with background sources. To maximize detection, one requires an X-ray observatory with both high sensitivity (to find faint sources) and high angular resolution (to disentangle a potential AGN from other X-ray sources). At present, the Chandra X-ray Observatory is the only instrument with subarcsecond spatial resolution. The purported angular resolution of the planned Athena telescope is $5''$, which is not sufficient to localize an AGN candidate and separate it from other sources. Only a probe-class X-ray mission, such as that recommended by the Astro2020 Decadal Survey (National Academies of Sciences, Engineering, & Medicine 2021) and based on the design of the Lynx Observatory, or as planned for the AXIS observatory, can meet the needs for discovering these elusive objects.

In future work, we will further explore the potential connection between AGN activity and the star formation quiescence we find in dwarf galaxies.

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**ORCID iDs**

Ray S. Sharma [https://orcid.org/0000-0001-8350-4535](https://orcid.org/0000-0001-8350-4535)
Alyson M. Brooks [https://orcid.org/0000-0002-0372-3736](https://orcid.org/0000-0002-0372-3736)
Michael Tremmel [https://orcid.org/0000-0002-4353-0306](https://orcid.org/0000-0002-4353-0306)
Jillian Bellovary [https://orcid.org/0000-0001-7596-8372](https://orcid.org/0000-0001-7596-8372)
Angelo Ricarte [https://orcid.org/0000-0001-5287-0452](https://orcid.org/0000-0001-5287-0452)

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