A new model to predict the influence of surface temperature on contact angle

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The measurement of the equilibrium contact angle (ECA) of a weakly evaporating sessile drop becomes very challenging when the temperatures are higher than ambient temperature. Since the ECA is a critical input parameter for numerical simulations of diabatic processes, it is relevant to know the variation of the ECA with the fluid and wall temperatures. Several research groups have studied the effect of temperature on ECA either experimentally, with direct measures, or numerically, using molecular dynamic simulations. However, there is some disagreement between the authors. In this paper two possible theoretical models are presented, describing how the ECA varies with the surface temperature. These two models (called Decreasing Trend Model and Unsymmetrical Trend Model, respectively) are compared with experimental measurements. Within the experimental errors, the equilibrium contact angle shows a decrease with increasing surface temperatures on the hydrophilic surface. Conversely the ECA appears approximately constant on hydrophobic surfaces for increasing wall temperatures. The two conclusions for practical applications for weakly evaporating conditions are that (i) the higher the ECA, the smaller is the effect of the surface temperature, (ii) a good evaluation of the decrease of the ECA with the surface temperature can be obtained by the proposed DTM approach.

The cohesive forces between molecules of the same phase (liquid, solid and gas/vapor) are responsible for the interphase tension of the liquid. The equilibrium balance of the forces acting on the liquid–vapor interface in contact with a solid surface determines the so-called “equilibrium contact angle” (ECA). At equilibrium, the ECA does not vary any more with time. The corresponding equation describing the balance of these forces is the well-known Young’s equation and it has been proved recently to be valid down to the nanometer scale1,2. The sum of forces parallel to the solid surface, per unit length of contact line, is perpendicular to the line and defines the local spreading coefficient \(\gamma_{SV} - \gamma_{SL} - \gamma \cos \theta = \gamma \cos \theta_Y - \gamma \cos \theta\), where \(\theta\) is the measured local contact angle and \(\theta_Y\) is the Young angle implied by the equation. Therefore, for a static condition, ideally the equilibrium contact angle \(\theta_Y\) is equal to the measured \(\theta\). The local contact angle \(\theta\) is a macroscopic quantity, with slight variation on the macroscopic scale, when the fluid surface is smooth. The value of this contact angle \(\theta\) (CA) is affected by many parameters at very different length scales, for example the chemical properties of the surface, the surface roughness3 and the temperature of the liquid/vapour/solid system.

The correct value of this parameter at high temperature is critical in modelling and simulation of droplet evaporation4,5 and pool boiling6,7. In the numerical simulations, the wettability effect is normally introduced as a boundary condition at the wall in terms of ECA or the dynamic contact angle DCA8,9. The DCA depends on the contact line velocity and can strongly diverge with respect to the ECA10,11. The effect of surface wettability on bubble growth is normally incorporated in a Volume of Fluid (VOF) numerical model by imposing a prescribed ECA between the vapour/liquid interface and the heated solid surface10.

Several groups have studied the effect of surface temperature on the equilibrium contact angles either experimentally12–16, or even using molecular dynamic simulations17–20. However, there is still some disagreement between the authors about the dependency of the equilibrium contact angle on the system temperature for a given system pressure.

For Hydrophilic surfaces (HPIS in this work is defined as a surface with an equilibrium contact angle lower than 90°) the experiments show typically a reduction of the equilibrium contact angle with the increase of the surface temperature. In Aydar et al.13 contact angles of oils on polytetrafluoroethylene (PTFE) with different

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surface temperature (from 23 °C up to the oil smoke point at 200 °C) are measured and compared to values predicted by the Girifalco-Good-Fowkes-Young (GGFY) equation. This equation, in combination with the Eötvös rule (that assumes an interface tension linear with the temperature), predicts a reduction of contact angle with increase of the surface temperature. Petke et al. measured the temperature dependence of contact angles of liquids on Hydrophilic and Hydrophobic (HPOS is a surface with an ECA greater than 90°) plastic surfaces, stating that the ECA decreases with the surface temperature in both cases. Not all the literature results agree with the reduction of the equilibrium contact angles with the surface temperature. Kenneth et al. examined surface temperature-dependence of the contact angle of water on graphite, silicon, and gold. The contact angle of water on various substrates did not monotonically decrease in every experiment, but also other behaviours have been observed. Kandlikar et al. measured the CA during rapid evaporation of liquid on a heated Hydrophobic surface and the values of the CA for high surface temperatures (100 °C < Tw < 250 °C) are remarkably constant. They showed that the liquid temperature has a much larger effect on the value of contact angles for polar liquids (water) than for apolar liquid (Diiodomethane), and for water they observed an increase of the CA with temperature, and a constancy of CA for diiodomethane. Another technique to study the effect of temperature on equilibrium contact angle is molecular dynamic (MD) simulation. What has been observed using MD is for Hydrophillic case a decrease of the ECA with temperature, and for Hydrophobic surface the contact angle increases with temperature. In Bruin et al. and also Blake et al. simulate a liquid-vapor interface which is confined by two parallel walls to study the contact angle versus the solid-fluid interaction strength. They found that the cosθ increases monotonically from −1 to 1 as solid-fluid interaction strength factor grows from 0.2 to 0.7. Outside this range the system gets unstable.

In the present work, two theoretical models (DTm and UTm) to predict the trend of the equilibrium contact angle (ECA) with temperatures are proposed. Equilibrium contact angle (called ECA) is defined in this paper as the time-average of the contact angle (called CA) in a given range (see eq. 3.31). Contact angle (CA) is the angle, conventionally measured through the liquid, where a liquid–vapor interface meets a solid surface, to a certain instant t. The experimental measurements of ECA of a sessile drop on heated surfaces are compared with these two theoretical models. The ECA is evaluated for sessile droplets at ambient pressure (1 bar) on surfaces with different wettabilities.

Theoretical Models

Two theoretical models are proposed in order to estimate the ECA at different averaged temperatures:

- Decreasing trend model (DTm): this model provides a decreasing of the ECA with temperature for all type of surfaces (Hydrophobic and Hydrophilic).
- Unsymmetrical trend model (UTm): this model provides a decreasing of the ECA with temperature if the surface is Hydrophilic, and an increasing of ECA with temperature if the surface is Hydrophobic.

Moreover, in paragraph 2.4, a second law thermodynamic approach is used in order to bound the ECA behaviour for small temperature variations around the equilibrium condition of the three phases.

Decreasing trend model – apolar liquid. The equilibrium contact angle reflects the balance between the relative strength of the liquid, solid, and vapor molecular interaction. The shape of a liquid–vapor interface is determined by the Young–Laplace equation, describing the equilibrium between solid–vapor interfacial energy (γsv) the solid–liquid interfacial energy (γsl) and the liquid–vapor interfacial energy (the surface tension γlv). Fowkes has suggested a simple equation to describe γlv as function of γsv and γlv (the expression is only valid for substances interacting with additive dispersive forces and without hydrogen bonds, called apolar liquid):

\[ γ_{lv} = γ_{sv} + γ_{lv} - 2\sqrt{γ_{sv}γ_{lv}} \]  \hspace{1cm} (2.1)

Using the expression in eq. 2.1, it is possible to eliminate γlv and write the into Young–Laplace equation without the solid–liquid interfacial energy γlv we get:

\[ \cos(θ) = \frac{γ_{tv} - γ_{lv}}{γ_{lv}} = \frac{γ_{tv} - γ_{lv} - γ_{lv} + 2\sqrt{γ_{tv}γ_{lv}}}{γ_{lv}} \]  \hspace{1cm} (2.2)

Finally, the basic equation of DTm model is:

\[ \cos(θ) = -1 + 2\sqrt{γ_{tv}} \sqrt{γ_{tv}} \]  \hspace{1cm} (2.3)

It is possible to note from eq. 2.3 that DTm requires two parameters to estimate the equilibrium contact angle: γtv, γlv. The γlv value at different temperatures can be found in. Experimentally the surface tension decreases with temperature in the temperature range interesting for this work (20 °C < T < 150 °C) the function is generally considered linear with temperature for most of the fluids, and it assumes the form:

\[ γ_{lv} = γ_{lv,i}(1 - aT) \]  \hspace{1cm} (2.4)

where γtv is the surface tension of the liquid [Nm] at a reference temperature T0 (normally T0 = 20 °C) and a is the temperature coefficient [Nm/T]. The second value γlv is the surface tension of the solid. The parameter a is positive for one phase substance. If we suppose that the variation of the γlv in the tested temperature range (20 °C < T < 150 °C) is negligible compared to the variation of γlv in the same range.
The experimental value of the equilibrium contact angle at ambient temperature (T = 20 °C) is used to extrapolate \( \gamma_{sv} \) for the tested surfaces, applying the following equation:

\[
\gamma_{sv} = \cos\left(\theta_0/2\right) \left(\gamma_{LV,0}(1 - a T_0)\right)
\] (2.6)

**Decreasing trend model – polar liquid.**  The decreasing trend model can be extended for liquids with a-scalar forces (the combined polar interactions: dipole, induction, and hydrogen bonding) such as water. In this case it is necessary to use a different equation to describe \( \gamma_{sl} \) as function of \( \gamma_{sv} \) and \( \gamma_{lv} \). Owens and Wendt\(^{30}\) extended the formulation of Fowkes\(^{25,26}\) introducing the dispersion forces (van der Waals interaction) and a-scalar forces for the combined polar forces (e.g. dipole-dipole interactions and hydrogen bonding):

\[
\gamma_{sl} = \gamma_{sv} + \gamma_{lv} - 2\sqrt{\frac{\gamma_{w}^D \gamma_{lv}^D}{\gamma_{lv}} - 2\sqrt{\gamma_{w}^P \gamma_{lv}^P}} \tag{2.7}
\]

The total free energy at the surface is the sum of all the contributions, the dispersion and the polar intermolecular forces at the surface\(^{26}\):

\[
\gamma = \gamma_{lv}^D + \gamma_{lv}^P \tag{2.8}
\]

\( D \) refer to the dispersion forces (van der Waals interaction) and \( A \) refer to the combined polar forces (e.g. dipole-dipole interactions and hydrogen bonding). Using eq. 2.7, it is possible to rewrite the Young–Laplace equation:

\[
\cos(\theta) = \frac{\gamma_{w} - \gamma_{sl}}{\gamma_{w}} = \frac{\gamma_{w} - \gamma_{w} - \gamma_{lv} + 2\sqrt{\gamma_{w}^D \gamma_{lv}^D} + 2\sqrt{\gamma_{w}^P \gamma_{lv}^P}}{\gamma_{lv}} \tag{2.9}
\]

As already done in the apolar case, it is supposed that the variation of \( \gamma_{sv} \) in the tested temperature range (20 °C < T < 90 °C) is negligible compared to the variation of \( \gamma_{lv} \) in the same range\(^{29}\):

\[
\frac{\partial(\gamma_{lv})}{\partial T} \bigg|_{20^\circ C < T < 90^\circ C} \gg \frac{\partial(\gamma_{lv}^P + \gamma_{sv}^D)}{\partial T} \bigg|_{20^\circ C < T < 90^\circ C} \approx 0
\] (2.11)

\( \gamma_{lv} \) is a linear function in T. It is supposed that both components are linear function of fluid temperature and by definition:

\[
\gamma_{lv,0}(1 - a T) = \gamma_{lv,0}^D (1 - a^D T) + \gamma_{lv,0}^P (1 - a^P T) \quad \forall T \tag{2.12}
\]

The temperature coefficients \( a^D \) and \( a^P \) are positive for one component liquid. It is possible to write the following inequality:

\[
|a^P| \leq |a^D| \leq a \tag{2.13}
\]

Therefore the ratio in eq. 2.10 can be considered constant in the range 20 °C < T < 90 °C and a polar liquid. The variation of the ratio in the temperature range is less than 1%:

\[
\frac{\partial\gamma_{w}}{\partial T} \bigg|_{20^\circ C < T < 90^\circ C} \leq \frac{\partial\gamma_{lv}}{\partial T} \bigg|_{20^\circ C < T < 90^\circ C} \pm 1\% \quad \text{for water if } 0 \leq |a^P| \leq |a^D| \leq a
\] (2.14)

Therefore the term \( c = \gamma_{lv}^D \gamma_{lv}^P \) can be considered constant (with temperature) for water in the range 20 °C < T < 90 °C:

\[
\cos(\theta) = -1 + \frac{2}{\sqrt{\gamma_{lv}}} \sqrt{\gamma_{lv}^D \gamma_{lv}^P} \tag{2.15}
\]

The experimental value of the equilibrium contact angle at ambient temperature (T = 20 °C) is used to extrapolate the constant parameter \( c \):
\[ c = \left( \cos(\theta_0) + \frac{1}{2} \sqrt{\gamma_{LV,0}(1 - a T_0)} \right)^2 \]  

(2.16)

**Unsymmetrical Trend Model.** In the Unsymmetrical Trend Model it is assumed that the difference of the interphase energy solid-vapor and solid-liquid \((\gamma_{SV} - \gamma_{SL})\) is a weak function of the liquid temperature compared to \(\gamma_{LV}\):

\[ \cos(\theta) = \frac{\gamma_{SV} - \gamma_{SL}}{\gamma_{LV}} = \text{const} \]  

(2.17)

This assumption means that \(\partial(\gamma_{SV} - \gamma_{SL})/\partial T = 0\), in other words:

\[ \frac{\partial(\gamma_{SV})}{\partial T} \approx \frac{\partial(\gamma_{SL})}{\partial T} \]  

(2.18)

The value of the equilibrium contact angle at ambient temperature \((T = 20^\circ C)\) is again used to extrapolate the value of \((\gamma_{SV} - \gamma_{SL})\) for the tested surfaces, applying the following equation:

\[ (\gamma_{SV} - \gamma_{SL}) = \cos(\theta_0)(\gamma_{LV,0}(1 - a T_0)) \]  

(2.19)

The value \((\gamma_{SV} - \gamma_{SL})\) will be clearly positive for Hydrophilic surfaces \(\theta < 90^\circ\) and negative for Hydrophobic surfaces \(\theta > 90^\circ\) at fixed temperature \(T_0\).

**Thermodynamic approach.** The influence of the temperature on equilibrium contact angle can be complemented using thermodynamics variables. In this approach, the Helmholtz free energy can be used to rewrite the surface tension:

\[ \gamma_{SV} - \gamma_{SL} = \Delta E - T \Delta S \]  

(2.20)

the Young–Laplace equation can thus be re-written as follow:

\[ \cos(\theta) = \frac{\gamma_{SV} - \gamma_{SL}}{\gamma_{LV}} = \frac{\Delta E - T \Delta S}{\gamma_{LV,0}(1 - a T)} \]  

(2.21)

Referring to a reference value of the temperature \(T_0\) which is connected to an equilibrium contact angle \(\theta_0\), the variation of the \(\cos(\theta)\) with respect to the reference value \(\cos(\theta_0)\) is:

\[ \cos(\theta) - \cos(\theta_0) = \frac{\Delta E - T \Delta S}{\gamma_{LV,0}(1 - a T)} - \frac{\Delta E_0 - T_0 \Delta S_0}{\gamma_{LV,0}} \]  

(2.22)

\[ \cos(\theta) - \cos(\theta_0) = \frac{\Delta E_0 - T_0 \Delta S_0}{\gamma_{LV,0}} \left[ \frac{\Delta E - T \Delta S}{\Delta E_0 - T_0 \Delta S_0} - 1 \right] \]  

(2.23)

\[ \cos(\theta) - \cos(\theta_0) = \cos(\theta_0) \left[ \frac{\Delta E - T \Delta S}{\Delta E_0 - T_0 \Delta S_0} - 1 \right] \]  

(2.24)

For a Hydrophobic surface \((\theta_0 \geq 90^\circ)\) \(\cos(\theta_0) \leq 0\). Suppose, according to the unsymmetrical trend model, that \(0 > \theta_0\) due to the temperature increases \((T > T_0)\):

\[ \cos(\theta) - \cos(\theta_0) < 0 \]  

(2.25)

Hence:

\[ \frac{\Delta E - T \Delta S}{\Delta E_0 - T_0 \Delta S_0} > 1 \]  

(2.26)

Considering \(\Delta S \approx \Delta S_0\)

\[ (T - T_0) \Delta S_0 - (\Delta E - \Delta E_0) < a T (\Delta E_0 - T_0 \Delta S_0) \]  

(2.27)

The internal energy \(E\) is a monotonic function of the temperature. This relation shows a potential violation of the II principle if we assume an increase of the contact angle with temperature. Indeed Eq. 2.27 can be written as:

\[ (T - T_0 + a T T_0) \Delta S_0 < k (T - T_0 + a T T_0) \]  

(2.28)
where $k = \Delta E/T$. Eq. 2.28 is valid only if $\Delta S_0 < k$ ($\Delta S_0$ and $k$ are positive). But for a free energy:

$$\Delta E_0 - T_0 \Delta S_0 = T_0 (k - \Delta S_0) > 0$$

which is violating the second principle. The thermodynamic approach shows that, if the temperature of all the three phases (solid, liquid and vapour) is the same, an increase of this common temperature state cannot induce an increase of the equilibrium contact angle. In many experiments, the three phases are not at the same temperature, for example the wall surface is kept at a higher temperature with respect to the liquid or vapour phase. In this sense the Unsymmetrical Trend Model can be still considered valid for a comparison with experimental results.

**Methods**

The apparatus used in this work to measure the equilibrium contact angle is schematically described in Fig. 1. A drop shape analyser (DSA100-Kruss®) is used to measure the contact angle of a sessile drop on the selected surface. The sample and the syringe are connected to a thermal bath (Julabo® EC-5) in order to change the temperature of the system. An InfraRed-camera (SC5000 Flir®) is placed on the other side of the chamber to measure the average temperature of the droplet for some preliminary tests.

Table 1 reports the equilibrium contact angle (measured at ambient temperature $20 \, ^\circ C$, and $P = 1 \, \text{atm}$) for the tested surfaces. Water and Diiodomethane are the liquids used in these experiments. Both liquid have a surface tension greater than $50 \, \text{mN/m}$, which affords high value even at high temperature. In the measurement of the ECA, the experiment is conducted in an environment with 3 species (solid, liquid and air-vapor) at ambient condition ($P_{\text{atm}} = 1 \, \text{atm}$ and $T_{\text{atm}} = 20 \, ^\circ C$). The presence of air and the no saturation condition of the gas phase (vapor and air) can induce inaccuracy on the equilibrium contact angle measurement, as reported by Weisensee et al.31.

A specific procedure to evaluate the ECA at medium high temperature is proposed in this paper. Four surfaces are tested: (a) poltetrafluoroetilene (PTFE) and (b) polished aluminium samples, (c) SHS is a glass sample covered by a uniform and thin coating to generate super-Hydrophobicity, it is using a commercial product (Glaco Mirror

| Surface | Liquid  | ECA [°] | Ra [μm] |
|---------|---------|---------|---------|
| Aluminium | water   | 68.6 ± 5.0 | 0.135   |
| PTFE    | water   | 110.6 ± 2.2 | 0.188   |
| SHS     | water   | 148.6 ± 3.6 | 0.045   |
| NP      | diiodomethane | 152.6 ± 3.4 | 0.07    |

Table 1. ECA of the surfaces, at temperature $T_0 = 20 \, ^\circ C$, measured with sessile drop method. The mean surface roughness ($R_a$) is also reported.
Coat Zero©), (d) NP is a glass sample covered by a film of nanoparticles (silicon dioxide with polydimethylsiloxyn group). Table 2 shows the physical properties for the two tested liquids (water and diiodomethane).

The evaluation of the ECA is performed in a range time called “Plateau” stage. The experimental measurement of the ECA on heated surface can be divided into 3 stages (as shown in Fig. 2b). The “Plateau” stage starts when the influence of convective motion on the value of contact angle is negligible (after the “transition” stage). The “Plateau” stage is over when the evaporation begins to change substantially the shape of the droplet (“evaporation” stage) and consequently the contact angle could be considerably influenced by evaporation32. The period covered by “Plateau” stage decreases with the increase of the temperature. The convective motion, as far as the evaporation rate, increases with surface temperature. Based on this assumption, the definition of the time constraints, called $t_1$ and $t_2$, for the “Plateau” stage can be addressed by the experiment shows in Fig. 2a. A IR-camera image of a sessile water drop deposited on a hot aluminium surface is shown. The surface temperature for this test ($T_{\text{wall}} = 100 ^\circ \text{C}$) is higher than the temperature tested for the validation of the water drop ECA ($T_{\text{wall}} = 20 ^\circ \text{C}$).

**Table 2.** Physical properties of the liquids. $T_{\text{sat}}$ is the boiling temperature (at 1 atm). Surface tension, density and dynamic viscosity are evaluated at $T_{\text{amb}} = 20 ^\circ \text{C}$.

|                | Water  | Diiodomethane |
|----------------|--------|---------------|
| $T_{\text{sat}}$ [°C] | 100    | 181           |
| Density [kg/m³]   | 973    | 3300          |
| Dynamic viscosity [mPa s] | 0.283  | 2.76          |
| Total free energy of the liquid ($\gamma_{LV}$) [mN/m] | 72.10  | 50.88         |
| Temperature coefficient $a$ [mN/m K] | $-0.1514$ | $-0.1376$ |
| Dispersion free energy contribution ($\gamma_{D}^0$) [mN/m] | 19.9   | 47.4          |
| Polar free energy contribution ($\gamma_{P}^0$) [mN/m] | 52.2   | 2.6           |

**Figure 2.** IR-camera images of a sessile water drop deposed on a hot aluminium surface. $T_{\text{wall}} = 100 ^\circ \text{C}$. The contour plots values are set for the droplet object. The IR-camera is calibrated with emissivity of water, therefore only the temperature values of the liquid droplet are real in the images.
the system, the drop starts to evaporate in a more vigorous mode (“Evaporation” stage in Fig. 2b). It is known that an evaporative droplet has a time-dependent contact angle. The CA decreases with time due to the simultaneous reduction of the droplet volume and the initial pinning of the contact line (as described by Stauber et al.32). The pinning of a contact line can be described by the Furmidge’s equation:

\[ F = \gamma \left( \cos(\theta_A) - \cos(\theta_R) \right). \]  

where \( \theta_A \) and \( \theta_R \) are the receding and advancing contact angle. The contact line can move if the force acting on the contact line is larger than \( F \), otherwise the pinning line doesn’t change. We define conventionally that, for our experimental conditions, the values \( t_1 = 2 \) s and \( t_2 = 6 \) s are the best to evaluate ECA in all the tested cases.

Furthermore Fig. 3 shows the evolution of the CL (the footprint of the projected drop profile on the solid surface) and the dimensionless drop volume \( V^* = V(t)/V(0) \) (\( V(0) \) is the volume of initial drop) up to \( t = 7 \) s. The CL (the footprint of the projected drop profile on the solid surface) does not show a significate change in the “Plateau” stage. For the case of water droplet on aluminium surface at \( T_w = 70^\circ \)C (that is the tested case with the highest evaporation rate) the dimensionless drop volume decreases less than 6%. Indeed on the aluminium surface (Fig. 3a) with \( T_w = 50^\circ \) and \( T_w = 70^\circ \)C, the CA changes up to 3°, while on the PTFE (Fig. 3c) the variation of the CA is negligible. This confirms the negligible effect of the evaporation rate in the range \( 2 < t < 6 \) s for on evaluation of ECA for our tests. During the “evaporation” stage, the evaporation is influenced by the DCA5,32,33.

We define here the “equilibrium contact angle” \( \theta_{ECA} \) as the average of the contact angles \( \theta_{CA} \) during the “Plateau” stage, between two times \( t_1 \) and \( t_2 \):

![Figure 3. Evolution of the CA of a water droplet contact line (CL) and the non-dimensional volume (V*) of water drop on aluminium surface (on the left) and water drop on PTFE surface (on the right). Two tested surface temperatures are plotted (50 °C and 70 °C). The ECA is evaluated between t1 = 2 s and t2 = 6 s.](image-url)
Experimental Results

In Fig. 4 experimental results of ECA are presented for a water droplet on aluminium, PTFE and SHS. A clear decrease appears for the Hydrophilic aluminium sample (from 70.3° to 58.5°). The standard deviation in this measurement is between 5° and 7°. Also on the Hydrophobic PTFE sample a slight decrease appears (from 109.5° to 101.0°). However, the uncertainty on the calculation of equilibrium contact angles (a standard deviation of 7° is reached at higher temperatures) does not allow to conclude that the ECA varies with temperature in this case.

On SHS the equilibrium contact angle is almost constant (from 148.6° to 151.6°). The trends of the ECA for these three cases are compared with the estimates from the two model DTmP and UTm. The DTmP and UTm show a good agreement with the experimental results for aluminium and PTFE. However, for the SHS case, with high equilibrium contact angle, the UTm predicts an increase of the equilibrium contact angle, in contradiction with the experimental data and against DTmP prediction.

Another surface (called NP) which shows a high ECA for diiodomethane is used as a further check. Figure 5 shows the comparison between the experimental measurement of ECA for diiodomethane and the two models. The prediction of DTm seems in better agreement with experimental data than UTm. The experimental data shows a decrease of the ECA (from 152.5° to 137.8°). The UTm diverges and is not able to capture the ECA value for Tw > 60°C.

\[
\theta_{ECA} = \frac{\int_{r_1}^{r_2} \theta_{CA}(t) \, dr}{r_2 - r_1}
\]  

(3.31)
Conclusions

The effect of surface temperature on equilibrium contact angle for a weakly evaporating sessile droplet sitting on a surface with different wettabilities is investigated. The “equilibrium contact angle” at a temperature higher than the standard ambient temperature is an important physical property, and an essential boundary condition in numerical simulations of phase-change phenomena and diabatic interface dynamics. However, there is some discrepancies in the literature about the value of the equilibrium contact angle with varying system temperature. Two theoretical models to predict the trend of the equilibrium contact angle (ECA) with temperatures are here proposed. The Decreasing Trend Model, with two formulations for apolar (DTm) and polar (DTmP) liquids, predicts a decrease of the ECA with temperature for both Hydrophilic and Hydrophobic surfaces. Instead the Unsymmetrical Trend Model (UTm) predicts a decrease of the ECA with temperature for Hydrophilic and an increase of ECA with temperature for Hydrophobic surfaces. The UTm is in contradiction with a thermodynamic approach base on the second law principle, which shows that for a homothermous system in equilibrium, an increase of the temperature cannot induce an increase of the ECA. However, since in many experiments the three phases are not really at the same temperature, the Unsymmetrical Trend Model can be still considered for the comparison with experiments.

Testing liquid droplets at different solid characteristics, a method to evaluate the ECA in function of the wall temperature is presented considering the average of the measured contact angle in a suitable time interval related to the evaporation stages and called “Plateau stage”. The ECA is here recorded for sessile droplets at ambient pressure (1 bar) on aluminum and PTFE surfaces with different wettabilities. Two fluids are used here: water and diiodomethane. For a water sessile drop, it is observed that a clear decrease of the ECA occurs for the Hydrophilic aluminum sample (from 70.3° to 58.3°). Also on the Hydrophobic PTFE sample a slight decrease appears (from 109.5° to 101.0°). However, the uncertainty on the estimate of ECA (a standard deviation) does not allow to precisely conclude that the ECA varies with the surface temperature in this case. Instead on the SHS it is quite clear that the ECA is almost constant (from 148.6° to 151.6°). In conclusion, the DTm and UTm show a good agreement with the experimental results in the cases of aluminium/water and PTFE/water. The trends of the ECA for these two cases are compared with the estimates from the two model DTm and UTm. However, in the last two cases, SHS/water and NP/diiodomethane, UTm model predicts an increasing of the ECA in contrast with the experimental results which show a constant trend of ECA with temperature. This trend is better captured by DTm model, for both tested liquid (water and diiodomethane). In conclusion DTm approach is in better agreement with all the experimental data presented in this work.

References

1. Fernandez-Toledano, J.-C., Blake, T. D., Lambert, P. & De Coninck, J. On the cohesion of fluids and their adhesion to solids: Young’s equation at the atomic scale. Adv. Colloid Interface Sci. https://doi.org/10.1016/j.cis.2017.03.006 (2017).
2. De Coninck, J., Dunlop, F. & Huillet, T. Contact angles of a drop pinned on an incline. Phys. Rev. E 95, 52805 (2017).
3. Al-Yaseri, A. Z., Lebedev, M., Barifcani, A. & Iglauer, S. Receding and advancing (CO₂–water and diiodomethane). In conclusion DTM approach is in better agreement with all the exper-
4. Al-Yaseri, A. Z., Lebedev, M., Barifcani, A. & Iglauer, S. Receding and advancing water and diiodomethane. In conclusion DTM approach is in better agreement with all the exper-
5. Erbli, H. Y., McHale, G. & Newton, M. I. Drop Evaporation on Solid Surfaces: Constant Contact Angle Mode. Langmuir 18, 2636–2641 (2002).
6. Diao, Y. H., Li, C. Z., Zhao, Y. H., Liu, Y. & Wang, S. Experimental investigation on the pool boiling characteristics and critical heat flux of Cu-R141b nanorefrigerant under atmospheric pressure. Int. J. Heat Mass Transf. 89, 110–115 (2015).
7. Kandlikar, S. G. A Theoretical Model to Predict Pool Boiling CHF Incorporating Effects of Contact Angle and Orientation. J. Heat Transfer 123, 1071 (2001).
8. Hirt, C. W. & Nichols, B. D. Volume of fluid (VOF) method for the dynamics of free boundaries. J. Comput. Phys. 39, 201–225 (1981).
9. Malgarinos, I., Nikolopoulos, N., Marengo, M., Antonini, C. & Gavaises, M. VOF simulations of the contact angle dynamics during the drop spreading: Standard models and a new wetting force model. Adv. Colloid Interface Sci. 212, 1–20 (2014).
10. Sikalo, S., Wilhelm, H.-D., Rosiman, I. V., Jakirlić, S. & Tropea, C. Dynamic contact angle of spreading droplets: Experiments and simulations. Phys. Fluids 17, 62103 (2005).
11. Antonini, C., Villa, F., Bernagazzi, I., Amirfazli, A. & Marengo, M. Drop rebound after impact: The role of the receding contact angle. Langmuir 29, 16045–16050 (2013).
12. Deendadianto et al. Effect of static contact angle on the droplet dynamics during the evaporation of a water droplet on the hot walls. Int. J. Heat Mass Transf. 71, 691–705 (2014).
13. Aydar, A. Y., Rodriguez-Martinez, V. & Farkas, B. E. Determination and modeling of contact angle of Canola oil and olive oil on a PTFE surface at elevated temperatures using air or steam as surrounding media. IWT - Food Sci. Technol. 65, 304–310 (2016).
14. Osborne, III & Kenneth, L. Temperature-Dependence of the Contact Angle of Water on Graphite, Silicon, and Gold. master, (Worcester Polytechnic Institute, 2009).
15. Terpiowski, K. Influence of the ambient temperature on water and diiodomethane contact angle with quartz surface. Ann. Chem. 70 (2015).
16. Sarmadivaleh, M., Al-Yaseri, A. Z. & Iglauer, S. Influence of temperature and pressure on quartz-water—CO₂ contact angle and CO₂—water interfacial tension. J. Colloid Interface Sci. 441, 59–64 (2015).
17. Sergi, D., Scorocchi, G. & Ortona, A. Molecular dynamics simulations of the contact angle between water droplets and graphite surfaces. Fluid Phase Equilib. 352, 173–177 (2012).
18. Leroy, F. & Müller-Plathe, F. Solid-liquid surface free energy of Lennard-Jones liquid on smooth and rough surfaces computed by molecular dynamics using the phantom-wall method. J. Chem. Phys. 133, 44110 (2010).
19. Nijmeijer, M. J. P., Bruin, C., Bakker, A. F. & Van Leeuwen, J. M. J. A visual measurement of contact angles in a molecular-dynamics simulation. Phys. A Stat. Mech. its Appl. 160, 166–180 (1989).
20. Stock, P., Utzig, T. & Valtiner, M. Direct and quantitative AFM measurements of the concentration and temperature dependence of the hydrophobic force law at nanoscopic contacts. J. Colloid Interface Sci. 244–251 (2015).
21. Good, R. J. & Girifalco, L. A. A theory for estimation of surface and interfacial energies. Ill. Estimation of surface energies of solids from contact angle data. J. Phys. Chem. 64, 561–565 (1960).
22. Petke, F. D. & Ray, B. R. Papers Presented at the 43rd National Colloid SymposiumTemperature dependence of contact angles of liquids on polymeric solids. J. Colloid Interface Sci. 31, 216–227 (1969).
23. Kandlikar, S. G. & Steinke, M. E. Contact angles and interface behavior during rapid evaporation of liquid on a heated surface. *Int. J. Heat Mass Transf.* **45**, 3771–3780 (2002).
24. Blake, T. D., Fernandez-Toledano, J.-C., Doyen, G. & De Coninck, J. Forced wetting and hydrodynamic assist. *Phys. Fluids* **27**, 112101 (2015).
25. Fowkes, F. M. Attractive forces at interfaces. *Ind. Eng. Chem.* **56**, 40–52 (1964).
26. Fowkes, F. M. Contact Angle, Wettability, and Adhesion. *Advances in Chemistry* **43** (American chemical society, 1964).
27. Vargaftik, N. B., Volkov, B. N. & Voljak, L. D. International Tables of the Surface Tension of Water. *J. Phys. Chem. Ref. Data* **12**, 817–820 (1983).
28. Spelt, J. K., Absolom, D. R. & Neumann, A. W. Solid surface tension: The interpretation of contact angles by the equation of state approach and the theory of surface tension components. *Langmuir* **2**, 620–625 (1986).
29. Frolov, T. & Mishin, Y. Temperature dependence of the surface free energy and surface stress: An atomistic calculation for Cu(110). *Phys. Rev. B* **79**, 45430 (2009).
30. Owens, D. K. & Wendt, R. C. Estimation of the surface free energy of polymers. *J. Appl. Polym. Sci.* **13**, 1741–1747 (1969).
31. Weisensee, P. B., Neelakantan, N. K., Suslick, K. S., Jacobi, A. M. & King, W. P. Impact of air and water vapor environments on the hydrophobicity of surfaces. *J. Colloid Interface Sci.* **453**, 177–185 (2015).
32. Stauber, J. M., Wilson, S. K., Duffy, B. R. & Selane, K. On the lifetimes of evaporating droplets with related initial and receding contact angles. *Phys. Fluids* **27**, 122101 (2015).
33. Kim, J. Y., Hwang, I. G. & Weon, B. M. Evaporation of inclined water droplets. *Sci. Rep.* **7**, 42848 (2017).
34. Surface tension values of some common test liquids for surface energy analysis. Available at: http://www.surface-tension.de/, (Accessed: 9th April 2017).

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**Author Contributions**
J.d.C. and M.M. devised the project, the main conceptual ideas and proof outline. F.V. worked out almost all of the technical details, and performed the experiment. F.V. prepared Figures 1–5. M.M. and F.V. proposed the theoretical models and drafted the manuscript. J.d.C. aided in interpreting the results and worked on the final manuscript. All authors (J.d.C., M.M., F.V.) discussed the results and commented on the manuscript. F.V. = Fabio Villa M.M. = Marco Marengo J.d.C. = Joël De Coninck.

**Additional Information**
Competing Interests: The authors declare no competing interests.

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