Heterogeneous neural coding of corrective movements in motor cortex

Adam S. Dickey¹, Yali Amit¹,² and Nicholas G. Hatsopoulos¹,³*

¹ Committee on Computational Neuroscience, University of Chicago, Chicago, IL, USA
² Department of Statistics, University of Chicago, Chicago, IL, USA
³ Department of Organismal Biology and Anatomy, University of Chicago, Chicago, IL, USA

INTRODUCTION

There is a long tradition of investigating motor control by using a double-step reaching paradigm, where a target jumps to a new location after a movement is initiated (Georgopoulos et al., 1983; Archambault et al., 2009, 2011). These studies found that in primary motor (MI) and dorsal premotor (PMd) cortices from rhesus macaques to directly compare double-step neural activity better than a standard linear encoding model, the original movement and the corrective movement. To allow a direct and fair comparison to the standard linear encoding model, decomposition into a linear combination of its two constituent parts: neurons first encode the kinematics of the original movement, and the instantaneous direction and speed (Georgopoulos et al., 1982; Schwartz et al., 1988; Moran and Schwartz, 1999; Wang et al., 2007). These models would not predict anything different during a double-step reach.

We use multi-electrode arrays to record neural data from MI, PMd, and ventral premotor (PMv) cortices from rhesus macaques performing reaches, and directly compare the default, linear encoding hypothesis to the replacement hypothesis previously proposed in cortical double-step studies. The replacement hypothesis (Archambault et al., 2009, 2011) was developed in the context of a standard center-out task, requiring reaches from a center target to one of eight peripheral targets arranged in a circle. The double-step involved jumping from the original target to a target located 180° opposite on the circle. Double-step activity was fit by starting with the original neural activity for movement from the center to the first target and replacing it with neural activity for movement from the center to the second target, which predicted the observed neural activity better than replacing it with neural activity associated with movement from the center to a randomly selected target (Archambault et al., 2009, 2011). Though these studies found that a linear encoding model generalized poorly from single-step to double-step trials (Archambault et al., 2009, 2011), the prediction of the “Replacement” hypothesis was not directly compared to the alternative of linear encoding of observed kinematics. This is because the “Replacement” prediction was derived from the directly observed, trial-averaged neural activity, instead of the prediction of a linear model fit using single-trials. Thus it is not clear that the replacement model predicts double-step neural activity better than a standard linear encoding model of observed kinematics.

Here, we use the concept of superposition to allow a direct comparison of the two hypotheses. It has been previously shown that the kinematics during a double-step can be expressed as the superposition (or vector sum) of the original, unperturbed movement and a corrective movement from the original target location to the new target location (Flash and Henis, 1991). We define the “Replaced” hypothesis to mean that, during a double-step trial, neurons first encode the kinematics of the original movement, and then switch to encode the kinematics of the corrective movement. To test this prediction, the observed movement first needs to be decomposed into a linear combination of its two constituent parts: the original movement and the corrective movement. To allow a direct and fair comparison to the standard linear encoding model,
we define an alternative “Summed” hypothesis which states that neurons encode the summed kinematics of the two constituent movements, which should closely match the observed movement.

The difference between the “Replaced” and “Summed” hypotheses can be best understood in the context of a double-step movement in one dimension, where the target is simply perturbed farther in the direction of the original movement (Figure 1). If the target jump happens soon after movement onset, the correction will be triggered before the original movement ends. This means that the velocity profile will be double-peaked, and it will not return to 0 between the peaks (Figure 1A, top). This double-peaked profile can be decomposed into the sum of two overlapping single-peaked speed profiles. If we assume that neurons linearly encode the velocity in the neuron’s preferred direction at a single leading time delay, then the firing rate profile should also be double-peaked (Figure 1A, middle). That is the “Summed” prediction. In contrast, in the “Replaced” prediction, the firing rate first follows the original, single-peaked profile and then switches to the second, corrective single-peaked profile at some time prior to the start of the second movement (Figure 1A, bottom). This switch produces a sharp drop in firing rate back to the baseline level, before rising again to match the corrective velocity profile.

If instead neuronal firing lags the velocity profile, the “Summed” prediction simply shifts to the right but is otherwise unchanged (Figure 1B, middle). However, if the switch time happens at the same time point, then the “Replaced” hypothesis predicts an extended silent period where the firing rate drops to the baseline level, before rising again to track the corrective movement (Figure 1B, bottom). The predictions of the “Summed” and “Replaced” hypotheses are quite different, so we should be able to resolve on a neuron by neuron basis which hypothesis better fits single-trial neural activity.

MATERIALS AND METHODS

NEURAL RECORDINGS

Three rhesus macaques (Macaca mulatta) were implanted with a total of five Utah 100-microelectrode arrays (Blackrock Microsystems, Salt Lake City, UT, USA) in MI, PMv, or PMd cortices in the right hemisphere (contralateral to the arm used for the task). Subject CO had arrays in MI, PMd, and PMv; subject MK had an array in MI, and subject BO had an array in PMd (Figure 2). The length of the electrodes on subject CO’s MI array was 1.5 mm, while the length on the other four arrays was 1 mm. All electrode tips were sputter-coated with platinum, except for subject MK’s MI electrode tips, which were coated with iridium oxide. The procedure for implanting the Utah array has been described elsewhere (Rousche and Normann, 1992; Maynard et al., 1999). During a recording session, signals from 96 electrodes were amplified (gain of 5,000), band-pass filtered between 0.3 Hz and 7.5 kHz, and recorded digitally (14-bit) at 30 kHz per channel using a Cerberus acquisition system (Blackrock Microsystems Inc., Salt Lake City, UT, USA). Only waveforms (duration, 1.6 ms; 48 sample time points per waveform) that crossed a voltage threshold were stored for off-line sorting. This voltage threshold was set just outside the noise band, so that all potential spike waveforms were recorded for later off-line spike sorting. Spike waveform data were sorted in Offline Sorter (Plexon, Dallas, TX, USA) using a user-defined unit template, which was a single waveform shape to which all potential spike waveforms were compared. All waveforms whose mean square error from this template fell below a...
user-defined threshold were classified as spikes belonging to that unit.

BEHAVIORAL TASK
Subjects were operantly conditioned to perform a behavioral task requiring planar reaching movements using a two-link robotic exoskeleton (KINARM, BKIN Technologies, Kingston, ON, Canada) that sampled X and Y positions of the hand at 500 Hz. However, for these experiments, the shoulder angle was locked, so only one-dimensional, elbow flexion and extension movements were possible. Control (single-step) trials of the behavioral task involved maneuvering a cursor controlled by the hand position to acquire a target within 1,500 ms of its appearance and then holding on it for a random hold period (uniformly distributed from 300 to 700 ms). There was no instructed delay, so subjects were free to move to the target as soon as it appeared. There were five discrete target locations (numbered 1–5), equally spaced at 1.35, 1.5, 1.65, 1.8, and 1.95 radians, respectively. Here, 0 radians indicates a fully extended elbow and an increasing angle indicates elbow flexion. The target width was 0.05 radians. Since the subjects' forearm lengths were approximately 20 cm, this corresponds to an approximately 1 cm wide target.

In addition to these single-step control trials, up to one-third of trials requiring movement between targets 2, 3, or 4 were perturbed to become double-step trials. The target shifted its position when the cursor moved more than 0.075 radians from the original target center.

In the three “Forward Jump” datasets, the target was perturbed in the same direction as the initial movement by 0.15 radians (for example, a movement starting at location 2 to a target at location 4 was perturbed by moving the target to location 5). In the four “Reverse Jump” datasets, the target was perturbed in the opposite direction of the initial movement by 0.15 radians. More details of the seven datasets analyzed are given below (Table 1). Of note, subject CO had all three arrays implanted simultaneously, and datasets #1 and #5 were recorded simultaneously. Each dataset represents all neurons recorded from one cortical area in a given day’s training session. All of the surgical and behavioral procedures were approved by the University of Chicago Institutional Animal Care and Use Committee and conform to the principles outlined in the Guide for the Care and Use of Laboratory Animals.

DATA PROCESSING
The raw angular position traces were first low-pass filtered forward and backward using a fourth order Butterworth filter and a 10-Hz cutoff frequency. These were then differentiated to obtain the angular velocity traces. For single-step trials, spike times were aligned on the first crossing of a 0.3-radians/s velocity threshold after target appearance. For double-step trials, spike times were aligned on the jump time (when the change in target location occurred). Mean trajectories and peri-event time histograms (PETHs) were computed by averaging kinematics and spike counts across all trials with the same starting and ending locations in a time window from —300 ms before the velocity threshold crossing (or jump time for the double-step trials) to 800 ms afterward.

ENCODING MODEL
Previous studies have reported that motor cortical firing is linearly related to both the Cartesian velocity and speed of the hand at a single time lag (Moran and Schwartz, 1999), but also that cortical

| # | Area | Jump Dir. | Single | Double | Neurons Analyzed |
|---|------|-----------|--------|--------|------------------|
| 1 | MI   | Forward   | 1,626  | 167    | 26               |
| 2 | MI   | Reverse   | 1,276  | 228    | 70               |
| 3 | MI   | Reverse   | 1,428  | 242    | 36               |
| 4 | PMd  | Reverse   | 1,645  | 260    | 115              |
| 5 | PMd  | Forward   | 1,626  | 167    | 88               |
| 6 | PMd  | Reverse   | 1,407  | 259    | 128              |
| 7 | PMv  | Forward   | 1,943  | 275    | 90               |

From left to right, the columns list the dataset number (#), the cortical area recorded from (Area), the subject ID (Subject), whether the dataset had a “Forward” or “Reverse” double-step jump, the number of single-step trials (Single), double-step trials (Double), sorted neurons (Neurons), and neurons analyzed in the Section “Results” (Analyzed).
Although in 1-D angular velocity and speed can differ only in sign, 
analyzed in each dataset is given in 
These are neurons for 
remaining neurons, we compared the prediction of the encoding 
anticipation of future velocity or response to past velocity. For the 
pairs of targets.

We first fit the control, single-step movements to a single 
minimum jerk trajectory. The minimum jerk velocity profile is 
expressed below (Eq. 2).

\[
V(t; t_0, a, d) = \begin{cases} 
30 \left( t^4 - 2t^3 + t \right), & \text{for } t_0 \leq t \leq t_0 + d \\
0, & \text{otherwise}
\end{cases}
\]

(2)

The angular velocity during a double-step trial \(V_{JUMP}(t)\) was 
fit as a sum of a primary \(V_1(t)\) and secondary \(V_2(t)\) minimum 
velocity profile (Eq. 3). Thus the double-step velocity can be 
described with six parameters.

\[
V_{JUMP}(t) = V_{JUMP}(t; t_1, a_1, d_1, t_2, a_2, d_2) = V_1(t; t_1, a_1, d_1) + V_2(t; t_2, a_2, d_2). 
\]

(3)

We found the optimal set of six parameters to fit a given 
double-step velocity profile \(V_{JUMP}(t)\) by minimizing the cost function 
expressed below (Eq. 4).

\[
C(t_1, a_1, d_1, t_2, a_2, d_2) = \frac{1}{\Theta(HEE)^2} \sum_{t} \left[ V_{JUMP}(t) - V_{JUMP}(t; t_1, a_1, d_1, t_2, a_2, d_2) \right]^2 
+ \sigma^2 \sum_{i=1}^{3} \left( a_i - \bar{a_i} \right)^2 + \frac{\sigma^2}{\Theta^2} \sum_{i=1}^{3} \left( d_i - \bar{d_i} \right)^2 
+ \sigma^2 \sum_{i=1}^{3} \left( \alpha_i - \bar{\alpha_i} \right)^2 
+ \sigma^2 \sum_{i=1}^{3} \left( \sigma_i - \bar{\sigma_i} \right)^2 
\]

(4)

We make the assumption that the parameters of two compo-
nents movements will be similar to the corresponding single-step 
motions. Thus, for a double-step which starts at location 2 where 
the target jumps from location 4 to 5, we assume the primary 
velocity \(V_1\) is similar to the single-step movement from 2 to 4, 
and the secondary motion \(V_2\) is similar to the single-step movement 
from 4 to 5. The values of the coefficients were constrained by 
including a squared error term relative to a reference value, multi-
plied by a scaling factor. The reference values and scaling factors were 
derived from single-step trials. We fit the velocity profiles from 
single-step trials to a minimum jerk velocity profile (Eq. 2) by 
minimizing the sum of squared errors. The reference ampli-
tudes \((a_1^*, a_2^*, \sigma_1^*, \sigma_2^*)\) and durations \((d_1^*, d_2^*)\) were set to the median 
of the amplitudes and durations fit to the corresponding single-
step trials, and so these values varied from dataset to dataset. The 
remaining parameters \((t_1^*, a_1^*, d_1^*, \sigma_1^*, a_2^*, d_2^*)\) were set constant for 
all datasets, and were derived from the “well-fit” single-step tri-
als from one dataset \((\Theta)\) whose correlation between actual and 
fit velocity was above 0.9 for 1,694 of 1,943 trials (87%). The 
start time of the first movement was unconstrained, but the ref-
ERENCE start time of the second movement (relative to the jump
time) was set as the mean of the reaction time of these well-fit single-step trials ($t^* = 220$ ms), with scaling factor given by their standard deviation ($\sigma_t = 50$ ms). Similarly, the scale factor for the amplitude and duration was again set to the pooled estimate of their standard deviations for the well-fit single-step trials ($\sigma_a = 0.3$ radians, $\sigma_d = 90$ ms). The sum squared error between the actual and fit velocity was normalized by the mean squared error of the well-fit single-step trials ($\sigma_{VEL} = 0.08$ radians/s). There was also an arbitrary weight constant ($\alpha = 0.95$) added to prevent the velocity error term from dominating the coefficient error terms.

**“SUMMED” vs. “REPLACED” HYPOTHESIS**

Under the default “Summed” hypothesis, the same encoding model (Eq. 1) that was fit to single-step trials was applied to double-step trials. However, rather than applying this encoding model to the observed velocity profile $V_{SUM}$, the firing rate was predicted using the fit velocity profile $V_{SUM}$:

$$FR_{SUM}(t - k) = b_0 + b_1 V_{SUM}(t) + b_2 |V_{SUM}(t)|. \quad (5)$$

The “Summed” prediction is based on the fit velocity $V_{SUM}$ to allow a direct comparison to the alternative “Replaced” hypothesis, where neurons instead encode the constituent movements $V_1$ and $V_2$, which comprise $V_{SUM}$. The “Replaced” hypothesis states that neurons will first encode the primary movement, and then switch to encoding the secondary movement at some time after the target jump (Eq. 6). We assume that this switch time is fixed to the start of the second movement $t^*_2$ minus some constant neural offset $\Delta t$. To prevent over-fitting, we fixed the neural offset to a constant for each cortical area before comparing the prediction to the “Summed” hypothesis.

$$FR_{REPL}(t) = \begin{cases} b_0 + b_1 V_1(t + k) + b_2 |V_1(t + k)| \text{ for } t < t^*_2 - \Delta t \\ b_0 + b_1 V_2(t + k) + b_2 |V_2(t + k)| \text{ for } t \geq t^*_2 - \Delta t \end{cases}. \quad (6)$$

We compared the “Summed” (Eq. 5) and the “Replaced” (Eq. 6) predictions in terms of their fit to observed neural activity during a double-step paradigm. We predicted the spike count in 10 ms bins for each trial, and assessed the goodness of fit of these predictions by computing the root-mean-square error (RMSE) between the prediction and the smoothed spike train (after convolution with a Gaussian kernel with a 30-ms standard deviation). The calculation of the RMSE metric was limited to a time interval from the jump time to 500 ms after the jump, as the predictions of the two hypotheses were very similar outside of this window. The RMSE metric includes data, from double-step trials from all the movement conditions. Predicted firing rates less than 1 spike/s were replaced with replaced with 1 spike/s. This thresholding was performed to prevent the linear model from predicting a negative or zero firing rate. A paired $t$-test was then used to determine if the mean RMSE was significantly different between the two predictions.

We also compared the predictions for the “Summed” and “Replaced” hypotheses using the logistic version of Eq. 1. For the logistic prediction of firing rate, $FR(t)$, we computed a log-likelihood of observed binary spike counts in 10 ms bins, given the “Summed” or “Replaced” predictions. We assume spike counts are conditionally independent Bernoulli random variables. If the binary spike count for a given neuron at time $t$ is denoted $x(t)$, then the log-likelihood of a spike train given the “Summed” hypothesis ($L_{SUM}$) is given in Eq. 7. A similar expression holds for log-likelihood of the “Replaced” hypothesis ($L_{REPL}$).

$$L_{SUM} = \sum \log \left(\frac{e^{FR_{SUM}(t)}}{1 + e^{FR_{SUM}(t)}}\right) + \left(1 - x(t)\right) \log \left(1 - e^{FR_{SUM}(t)}\right).$$

**RESULTS**

A decomposition algorithm was used (see Decomposing Double-step Kinematics) to fit the double-step velocity profiles to the sum of two minimum jerk velocity profiles (Figure 3). For a single trial (Figure 3A), the fit velocity profile does a good job matching the bulk of the observed double-peak profile, though it does not fit the reversal in velocity, which comes after the second movement. The fraction of variance ($R^2$) of the actual velocity explained by the fit velocity was 0.986. The decomposition performed similarly well for all 52 double-step trials for this movement condition from dataset 7 (Figure 3B), where the starting point was location 2, and the target jumped from location 4 to 5. The main difference is that the fit velocity is constant at 0 before and after the double-peak velocity profile. The median $R^2$ for these trials was also 0.986, and the mean was 0.983 (standard deviation 0.015). For the 1,658 successful double-step trials from all datasets, the median $R^2$ was 0.982, with a mean of 0.970 (standard deviation 0.0357).

We can use the parameters of the fit velocity profile as an estimate of the reaction time, either from the target appearance or the target jump (Table 2, left). The average reaction time of all single-step trials (with amplitude 0.15 radians) of a given dataset varied from 203 to 230 ms. However, when looking across the seven datasets, the mean of these single-step reaction times was not significantly different from the mean of the first or second double-step reaction times (paired $t$-test, $p > 0.05$). The average movement duration for single-step trials (with amplitude 0.15 radians) varied from 405 to 457 ms (Table 2, right). Similarly, when looking across the seven datasets, the mean of these single-step durations was not significantly different from the mean of the first or second double-step durations (paired $t$-test, $p > 0.05$).

Given the decomposition, we still need one extra parameter to predict the neural firing under the “Replaced” hypothesis: the neural offset $\Delta t$. This is a constant which represents how soon before the start of the secondary movement ($t^*_2$) the neurons show the replacement effect. We first assumed that the neural offset for each neuron was constant for all movement conditions, but different across neurons. We then tested a range of offsets for each neuron, from 0 to 250 ms in 10 ms increments, and picked the offset which minimized the RMSE of the data given the “Replaced” prediction. Within this range, we are trying to find a change in
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**FIGURE 3** Decomposition of actual kinematics observed during a double-step. (A) The actual kinematics of a double-step trail (black line) are well-approximated by the sum (gray line) of a primary (light gray) and secondary (dark gray) single-peaked profiles. (B) The single-trial velocity profiles are displayed as heat maps, with the vertical axis representing different trials, and the horizontal axis representing time elapsed within a given trial. The actual kinematics (top left) can be compared to the fit kinematics (top right), which is the sum of the single-trial primary (bottom left) and secondary (bottom right) motions.

**Table 2** The mean and standard deviation of the reaction times (RT) and movement durations of the single-step (SS), the first double-step (DS 1), and the second double-step (DS 2) movements for all seven datasets.

| # | SS RT (±SD) in ms | DS 1 RT (±SD) in ms | DS 2 RT (±SD) in ms | SS Duration (±SD) in ms | DS 1 Duration (±SD) in ms | DS 2 Duration (±SD) in ms |
|---|-------------------|---------------------|---------------------|------------------------|--------------------------|--------------------------|
| 1 | 228 (47)          | 207 (40)            | 222 (34)            | 418 (68)               | 418 (68)                 | 366 (51)                 |
| 2 | 203 (71)          | 202 (57)            | 201 (50)            | 405 (100)              | 405 (98)                 | 409 (109)               |
| 3 | 231 (53)          | 224 (42)            | 181 (48)            | 406 (105)              | 419 (84)                 | 409 (119)               |
| 4 | 221 (84)          | 253 (46)            | 248 (44)            | 416 (67)               | 413 (68)                 | 366 (51)                 |
| 5 | 228 (47)          | 207 (40)            | 222 (34)            | 413 (71)               | 396 (51)                 | 413 (77)                 |
| 6 | 230 (55)          | 221 (40)            | 174 (43)            | 430 (76)               | 420 (55)                 | 389 (84)                 |
| 7 | 223 (55)          | 208 (43)            | 217 (38)            |                        |                          |                          |

Data are reported for all single-step trials with an amplitude of 0.15 radians, and all double-step trials where each component has an amplitude of 0.15 radians. Outlying reaction times >400 ms (6% of original data) and durations >700 ms (7%) were removed before the mean and standard deviation were computed.
neural activity in the reaction time period, between the change in target position but before the onset of movement. We then compared the distributions of neural offsets across cortical regions, from neurons which were better fit by the “Replaced” prediction (lower mean RMSE, \( p < 0.05, t\)-test) and whose neural offset was greater than 0 ms and less than 250 ms. The distribution of neural offsets was markedly different between MI and premotor cortices, i.e., PMd and PMv cortices (Figure 4). The mean neural offset of the 26 eligible MI cortical neurons (53 ms) was significantly less (\( p < 0.01, t\)-test) than the mean of neural offset of the 91 eligible premotor neurons (84 ms).

This indicates that premotor cortex shows an earlier response to the double-step target jump than MI cortex, consistent with previous results (Archambault et al., 2011). There was no significant difference in mean neural offsets between neurons in PMd and PMv (\( p > 0.05, t\)-test). To compare the “Replaced” prediction to the “Summed” prediction, we did not want the neural offset to be a free parameter, because this could lead to over-fitting of the “Replaced” neural prediction and would represent an unfair comparison between the two hypotheses. Thus, we rounded the mean neural offsets up to the nearest 10 ms, so that all MI neurons had a neural offset of 60 ms, and all premotor neurons had a neural offset of 90 ms. Recall that the neural offset specifies when the neural replacement happens relative to start of movement. It is different that the encoding delay, which specifies whether neural firing lags or leads observed movement.

We observed that the response profiles of some neurons were consistent with the “Summed” hypothesis while others were more consistent with the “Replaced” hypothesis during the double-step trials, even among neurons that were recorded simultaneously. For an example PMv neuron (from dataset #7), the prediction of a linear encoding model (fit on all single-step trials) closely matched the PETH for single-step movements from location 2 to 4 (Figure 5A). The \( R^2 \) between the actual PETH (Figure 5A, solid black) and predicted PETH (Figure 5A, gray dot dash) was 0.96 for this movement condition. Fitting a linear encoding model to all single-step trials gave an optimal encoding delay \( \delta = 30 \) ms, meaning this neuron’s firing led the observed velocity.

The corresponding double-step condition also involved starting at location 2 and moving to location 4, but the visual target was switched to location 5 after the original movement was initiated. This resulted in a double-peaked velocity (see Figure 3) where the constituent velocity profiles overlapped. For a neuron which leads velocity, the “Summed” hypothesis predicts the firing rate should follow the shape of the double-peaked profile, while the “Replaced” hypothesis predicts a temporary reset to baseline after the target jump (see Figure 1A). For this neuron, the “Summed” prediction much better fit to the observed double-step PETH than did the “Replaced” prediction (Figure 5B).

This neuron’s spike times from individual trials of the single-step (Figure 5C) and double-step (Figure 5D) conditions show a similar smooth rise and fall in firing rate. The raw double-step rasters (Figure 5D) can be visually compared to the single-trial predictions of the “Summed” (Figure 5E) and “Replaced” (Figure 5F) predictions. These are displayed as heat maps, where black indicates a high firing rate and white indicates a low firing rate. There is a sharp drop in firing rate (seen as a black to white transition) in the “Replaced” prediction (Figure 5F) around 100 ms after the target jump. However, this predicted drop in firing rate is not seen in the raw double-step rasters (Figure 5D) or the observed PETH (Figure 5B). Instead, the neuron reaches a similar peak firing rate as the single-step condition (23 spikes/s) at the jump time (0 s), before gradually decreasing its firing rate over the next 500 ms. Note that the double-step rasters and predictions (Figures 5D–F) are sorted by the start of the second constituent motion (as defined by the decomposition algorithm). This is why the reset to baseline is predicted to occur later for trials near the bottom for the “Replaced” hypothesis (Figure 5F). The \( R^2 \) between the actual double-step PETH and the “Summed” prediction is 0.94, compared to 0.62 for the “Replaced” prediction. For this neuron, across all trials of all double-step conditions, the average RMSE for the “Summed” prediction (7.6 spikes/s) was significantly less (\( p = 0.001, paired-test \)) than the average RMSE of the “Replaced” prediction (8.2 spikes/s).

In contrast, the firing of a different but simultaneously recorded PMv neuron was clearly better fit by the “Replaced” hypothesis (Figure 6). The single-step PETH (Figure 6A, black) from target 2 to 4 showed a smooth increase and decrease in firing rate. The firing rate profile was wider than that predicted by the linear encoding model (gray dot dash), but the \( R^2 \) between the actual and fit PETH was still 0.80. This neuron’s optimal delay \( \delta = 70 \) ms, indicating that neural firing lagged hand velocity. During the corresponding double-step profile, the “Summed” hypothesis failed to predict the neuron’s response (Figure 6B, gray dotted). It predicted that the neural firing rate should reach a peak of 20 spikes/s 200 ms after the target jump. Instead,
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FIGURE 5 | A neuron from ventral premotor cortex is better fit by the "Summed" hypothesis. (A) During single-step (SS) trials, the observed peri-event time histogram (PETH, black) is well fit by a model assuming linear encoding of velocity and speed (gray dot dash). Zero time refers to the time of target appearance. (B) During double-step (DS) trials, the observed PETH (black) is well fit by the "Summed" prediction (gray dotted) but not the "Replaced" prediction (gray dashed). Zero time refers to the time of the target jump. (C) The single-trial spike time rasters for the SS trials. (D) The single-trial spike time rasters for the DS trials, arranged by the predicted replacement time (gray). (E) The DS single-trial prediction of the "Summed" hypothesis, displayed as a heat map. (F) The DS single-trial prediction of the "Replaced" hypothesis.

FIGURE 6 | A neuron from ventral premotor cortex is better fit by the "Replaced" hypothesis. Format follows Figure 5.

The actual neural firing dropped below 2 spikes/s from 150 to 250 ms after the target jump. Unlike the "Summed" prediction, the "Replaced" prediction (gray dashed) successfully predicted this transient drop in firing rate for the double-step condition. The $R^2$ between the actual and predicted double-step PETH was 0.80 for the "Replaced" hypothesis, but 0.05 for the "Summed" hypothesis.

While the single-trial spike times for the control, single-step trials (Figure 6C) showed a smooth increase and decrease in firing rate, each individual trial in the double-step condition showed an abrupt cessation of spiking activity (Figure 6D). This drop is not seen in the single-trial predictions of the "Summed" hypothesis (Figure 6E), but it is seen in the predictions of the "Replaced" hypothesis (Figure 6F). Across all trials of all
double-step conditions, the mean RMSE for the “Replaced” prediction (7.5 spikes/s) was significantly less ($p < 0.001$, paired-test) than the mean RMSE of the “Summed” prediction (8.8 spikes/s).

Similar examples of “Replaced” neurons can be found in MI (Figure 7) and PMd (Figure 8). The MI neuron (from dataset #2) had an optimal encoding delay $\delta$ of $-90$ ms, and the $R^2$ between the actual and predicted single-step PETH for movement from location 2 to 4 was 0.86 (Figure 7B). The $R^2$ between double-step PETH and the “Replaced” prediction was 0.68, and between the PETH and “Summed” prediction was 0.08. The RMSE was significantly less for the “Replaced” than the “Summed” prediction (14.2 vs. 15.7 spikes/s, $p < 0.001$, paired-test). In this dataset, the jump involved a reversal in the direction of movement (see Materials and Methods), but this neuron increased its firing rate for movements in both directions, so the “Replaced” prediction was similar to the previous example. The PMd neuron (from dataset #5) had an optimal encoding delay $h$ of $-100$ ms, and the $R^2$ between the actual
and predicted single-step PETH for movement from location 2 to 3 was 0.89 (Figure 8B). The R^2 between double-step PETH and the “Replaced” prediction was 0.81, and between the PETH and “Summed” prediction was 0.40 (Figure 8F). The RMSE was significantly less for the “Replaced” than the “Summed” prediction (3.3 vs. 6.2 spikes/s, p < 0.001, paired-test).

Across all neurons, two-thirds were better fit with the “Summed” prediction, and one-third were better fit with the “Replaced” prediction (Table 3). For the linear version of Eq. 1, we defined the better prediction as having a lower average RMSE, while for the logistic version, the better prediction had a higher log-likelihood (see Materials and Methods). The percentage of cells which were better fit with the “Replaced” prediction (using RMSE) did not differ significantly between MI cortex (29/73, 39%) and premotor cortex (82/207, 40%).

Interestingly, we found that “Replaced” neurons were more likely to lag movement velocity while “Summed” neurons tended to lead movement velocity. Specifically, the percentage of neurons with an encoding delay less than 0 was significantly different for “Summed” and “Replaced” neurons, as were the mean and median lags (Table 3). Recall that the encoding lag is fit only to single-step trials, while the determination of “Replaced” vs. “Summed” is made on the double-step trials. This difference in the distribution of encoding delays was most dramatic when we looked at the 128 neurons that exhibited a significant difference (R^2 < 0.01, t-test) in the mean RMSE between the “Summed” and “Replaced” predictions (Figure 9). Of these cells, 46 (56%) were better “Replaced” and 82 (64%) were better “Summed.” Again, the “Replaced” neuronal firing was significantly more likely (R^2 < 0.001, chi-square test) to lag observed velocity (39/46 or 76% with δ < 0) than was “Summed” neuronal firing (42/82 or 51% with δ < 0).

Table 3 | Neurons which were better “Replaced” were more likely to lag the kinematics (encoding delay < 0) than neurons better “Summed.”

|           | Replaced | Summed | p-Value |
|-----------|----------|--------|---------|
| Linear    |          |        |         |
| Percentage of cells | 39% (111) | 61% (171) |         |
| Percentage lagging | 58% (64)  | 30% (66)  | 0.01    |
| Mean delay | −49 ms  | 13 ms  | <0.001  |
| Median delay | −70 ms  | 30 ms  | <0.001  |
| Logistic   |          |        |         |
| Percentage of cells | 36% (108) | 64% (194) |         |
| Percentage lagging | 56% (81)  | 43% (83)  | 0.02    |
| Mean delay | −116 ms | −11 ms | 0.01    |
| Median delay | −140 ms | −10 ms | 0.03    |

The top rows list the percentage and number of cells better “Replaced” or better “Summed,” while the subsequent rows show the percentage of those cells with a lagging delay, the mean delay, and median delay. The percentages were compared using a chi-square test, the mean delays were compared with a t-test, and the median delays were compared with a Wilcoxon rank-sum test.

DISCUSSION

We found that for a third of the neurons analyzed from MI and premotor cortices, single-trial neural activity during a double-step was better explained with the “Replaced” rather than “Summed” encoding hypothesis. In some cases, the drop in firing rate predicted by the “Replaced” hypothesis was dramatic and readily visible in the single-trial raster plots (see Figure 6). Thus we were able to replicate the replacement phenomenon described previously (Georgopoulos et al., 1983; Archambault et al., 2009, 2011), though we saw it in only a minority of cells. The majority of neurons was consistent with the “Summed” hypothesis and conformed to the model of linear encoding of velocity (Schwartz et al., 1988; Moran and Schwartz, 1999).

Why did we only observe the “Replaced” phenomenon in a minority of cells? One potential difference from the studies by Archambault et al. (2009, 2011) is that we used a 1-D reaching paradigm rather than 3-D unconstrained reaching. We chose the 1-D paradigm to make the decomposition algorithm as simple as possible (see Decomposing Double-step Kinematics). However, we do not expect the change in the degrees of freedom to affect the results – the “Replaced” hypothesis was described for both 2-D planar reaching (Georgopoulos et al., 1985) and 3-D unconstrained reaching (Archambault et al., 2009, 2011). Likewise, linear encoding models have been used to describe motor cortical firing both for 2-D planar reaching (Moran and Schwartz, 1999) and 3-D unconstrained reaching (Wang et al., 2007).

We feel the difference from the Archambault et al.’s (2009, 2011) studies is simply one of methodology. The previous studies were documenting the existence of a phenomenon, so the “Replaced” hypothesis was compared to a null condition. This null condition replaced neural firing with a randomly selected firing pattern,
while the alternative condition replaced with a firing pattern corresponding to the direction of the correction. That is an appropriate technique, but it does not address the question of whether the “Replaced” hypothesis is better than the existing linear encoding models (the “Summed” hypothesis). We wanted to know the prevalence of “Replaced” phenomenon, not just whether it existed. That is a higher threshold of evidence to cross, and only one-third of neurons crossed it.

That said, we tested a fairly restrictive form of the “Replaced” hypothesis, where the prediction of neuronal firing at one time point was instantaneously replaced with another firing rate, usually leading to a sharp drop in predicted firing rate back to baseline. This was done deliberately, because it helped ensure that the neurons found to be better “Replaced” were not simply being over-fit. However, it did mean that other neurons might be well-described with the “Replaced” hypothesis using a more gentle transition. Thus the number of “Replaced” neurons might be underestimated.

We also found that the firing of neurons better fit by the “Replaced” hypothesis was more likely to lag velocity than lead it (see Figure 9). This suggests that this population is monitoring on-going movement as opposed to causally driving it. However, it is unclear why these lagging neurons would shut-off during the target jump. The simplest interpretation is that the firing of these lagging neurons is related to incoming sensory information, but that this neuronal firing is inhibited after the target jump. This might be analogous to saccadic suppression, where sensory responses are dampened in primary visual cortex during a saccade (Vallines and Greenlee, 2006) to avoid the trouble of processing a blurry image. Perturbation experiments during voluntary movement have suggested that the proprioceptive effects on MI neurons are highly attenuated during large ballistic movements as compared to finer movement adjustments (Everts and Fromm, 1977). Therefore, modulation in this “sensory” population of MI neurons might be expected to temporarily shut-off during the early ballistic portion of the corrective movement.

Another possibility is these “Replaced” neurons are participating in a larger cortical network which monitors the consequences of motor actions, particularly whether or not the action is successful. For example, the anterior cingulate cortex (ACC) is known to have projections to MI cortex (Dum and Strick, 1991), and the ACC has been implicated in the monitoring of the consequences of one’s actions. One proposal is that the ACC encodes the “surprise related to the non-occurrence of a predicted event” (Alexander and Brown, 2011). Neurons in the ACC have been found that show an error-related phasic increase in firing rate peaking around 200 ms after the initiation of an inappropriate saccade (Bo et al., 2003). If these neurons (or similar neurons) directly inhibited the pool of “Replaced” neurons described here, it would explain the sudden drop in firing rate following a target jump.

We focused on kinematics for this study, because our single-trial “Replaced” prediction relied on a kinematic decomposition assuming summation of the original movement and a second corrective movement. One drawback of this focus is that we did not record forces, torques, or muscle activity. The lack of force data means we were unable to investigate alternatives to kinematic summation, such as the proposal that a target jump elicits a stereotyped force pulse made in the direction of the new target (Massey et al., 1986).

Another limitation is that we excluded a fair number of neurons from analysis. We excluded 190 of 553 neurons (34%) for having a predictive encoding lag greater than +175 ms. This was done purposely to exclude neurons firing in relation to the previous target appearance (Reimer and Hatsopoulos, 2010), rather than anticipation of future velocity. We did not want to consider target encoding effects here. We also excluded an additional 81 of 553 neurons (15%) because they were not well fit by the linear encoding model. However, such neurons might still encode relevant information, particularly if they use a temporal rather than a rate code. By focusing on the two main classes of neurons, “Summed” and “Replaced,” we are underestimating the heterogeneity of neural coding.

We used the double-step reaching paradigm in these experiments to reliably induce corrections, so that we could average across trials with similar corrections. However, we view this as a model system for corrections and motor variability in general. Corrective submovements are often observed when reaches require accuracy (Grossman and Goodeve, 1983; Milner and Ijaz, 1990; Novak et al., 2000) or when infants are first learning to reach (Berthier, 1997). We predict that these “Replaced” neurons would also show a sharp change in firing rate for these naturally occurring corrections as well as those resulting from a target jump. Decomposing submovements in naturalistic movement is a difficult problem if the exact nature of the submovement is uncertain (Kraus et al., 1999). However, unpredictable gain or rotation perturbations could be applied on a single-trial basis to reliably induce corrections without the need for a sudden shift in visual target location.

The existence of a subpopulation of “Replaced” neurons is relevant for the design of brain machine interfaces. Standard techniques, such as the linear filter (Serruya et al., 2002) or the Kalman filter (Wu et al., 2002), tend to only look at the neuronal firing with leading encoding delays. This means such techniques may ignore the lagging “Replaced” neurons entirely. However, this subpopulation might be used to identify the presence of a correction, which would indicate the need for a dramatic adjustment to the estimate of hand position. Additionally, the “Replaced” subpopulation could be used to identify trials where a correction was necessary, which could be used as a teaching signal in an adaptive decoding algorithm. If the “Replacement” phenomenon is replicated in situations involving more natural corrections, then we should be able to leverage the information they contain to make brain machine interface algorithms more accurate and easier to control during real-time, closed loop control.

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