MC²: Subaru and Hubble Space Telescope Weak-lensing Analysis of the Double Radio Relic Galaxy Cluster PLCK G287.0+32.9

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Abstract

The second most significant detection of the Planck Sunyaev–Zel’dovich survey, PLCK G287.0+32.9 (z=0.385), boasts two similarly bright radio relics and a radio halo. One radio relic is located ∼400 kpc NW of the X-ray peak and the other ∼2.8 Mpc to the SE. This large difference suggests that a complex merging scenario is required. A key missing puzzle for the merging scenario reconstruction is the underlying dark matter distribution in high resolution. We present a joint Subaru Telescope and Hubble Space Telescope weak-lensing analysis of the cluster. Our analysis shows that the mass distribution features four significant substructures. Of the substructures, a primary cluster of mass $M_{200c} = 1.59^{+0.25}_{-0.22} \times 10^{15} h_{70}^{-1} M_{\odot}$ dominates the weak-lensing signal. This cluster is likely to be undergoing a merger with one (or more) subcluster whose mass is approximately a factor of 10 lower. One candidate is the subcluster of mass $M_{200c} = 1.16^{+0.15}_{-0.13} \times 10^{14} h_{70}^{-1} M_{\odot}$ located ∼400 kpc to the SE. The location of this subcluster suggests that its interaction with the primary cluster could be the source of the NW radio relic. Another subcluster is detected ∼2 Mpc to the SE of the X-ray peak with mass $M_{200c} = 1.68^{+0.22}_{-0.20} \times 10^{14} h_{70}^{-1} M_{\odot}$. This SE subcluster is in the vicinity of the SE radio relic and may have created the SE radio relic during a past merger with the primary cluster. The fourth subcluster, $M_{200c} = 1.87^{+0.24}_{-0.22} \times 10^{14} h_{70}^{-1} M_{\odot}$, is NW of the X-ray peak and beyond the NW radio relic.

Key words: cosmology: observations – dark matter – galaxies: clusters: individual (PLCK G287.0+32.9) – gravitational lensing: weak – X-rays: galaxies: clusters

1. Introduction

Among the largest of the gravitationally bound structures, galaxy clusters are composed of about 90% dark matter, 9% plasma intracluster medium (ICM), and 1% stars. Galaxy clusters grow by the accretion of gas, galaxies, and other clusters. The most energetic of these events is a collision of two massive galaxy clusters, releasing $\sim 10^{64}$ erg of energy (Sarazin 2002).

During a cluster merger, galaxies and dark matter interact predominantly through the gravitational force and for the most part can be considered collisionless. In contrast, the gas particles of the ICM are collisional and can suffer an abrupt dissipation of energy from ram pressure. The difference in the two interaction mechanisms has been observed as a lag of the dissipation of energy from ram pressure. The difference in the particles of the ICM are collisional and can suffer an abrupt part can be considered collisionless. In contrast, the gas clusters grow by the accretion of gas, galaxies, and other clusters. The most energetic of these events is a collision of two massive galaxy clusters, releasing $\sim 10^{64}$ erg of energy (Sarazin 2002).

Within the ICM of highly energetic galaxy cluster mergers, shock waves have been observed. As the two clusters collide, the supersonic velocity ($\sim 2000–3000$ km s$^{-1}$) of the collision causes a rapid compression of gas at the intersection of the cores, producing a shock. Shocks observed in X-ray emissions appear in low-surface-brightness regions of the ICM with a surface brightness profile showing a discontinuous jump perpendicular to the shock front. Numerical simulations have reproduced shocks ranging from a few hundred kiloparsecs to a few megaparsecs in size (Ryu & Kang 2003). Even though the shocks are large, their detection by X-ray emission is difficult because of low surface brightness.

In the low-density outskirts of merging galaxy clusters, diffuse radio emissions from the ICM, known as radio relics, are believed to trace shocks. To date, approximately 50 clusters have been detected with radio relics. For a recent review of diffuse radio emissions from galaxy clusters see Feretti et al. (2012). Among the clusters exhibiting radio relics, 18 have double radio relics. The systems hosting radio relics are believed to arise in clusters that have a merging axis near the plane of the sky (Golovich et al. 2017). Diffuse radio emissions have also been observed in the centers of about 40 galaxy clusters (Feretti et al. 2012). In this region, the radio emission is called a radio halo, and it is believed to be synchrotron emission from the turbulent ICM caused by a major merger.

The Merging Cluster Collaboration (MC²) has selected a sample of 29 merging clusters with elongated radio relics in an effort to improve our understanding of galaxy cluster physics and to constrain dark matter properties. This sample contains three galaxy clusters with a visible radio halo and double radio relics confirmed: RXC J1314.4−2515, CIZA J2242.8+5301,
and PLCK G287.0+32.9. Of these, PLCK G287.0+32.9 is the most massive and highest redshift and is the focus of this paper. PLCK G287.0+32.9 was first detected by the Planck telescope through the Sunyaev–Zel’dovich (SZ) effect. It was reported as the second most significant detection in the Planck Collaboration all-sky early SZ cluster sample (Planck Collaboration et al. 2011a). Warranted by its high SZ signal-to-noise ratio (S/N), PLCK G287.0+32.9 was included in XMM-Newton follow-up observations of significant SZ detections (Planck Collaboration et al. 2011b). XMM-Newton measurements found the temperature of the ICM to be 12.86 ± 0.42 keV. The mass of the cluster within R500c was inferred to be M500c = 15.72 ± 0.27 × 10^{14} h_{70}^{-1} M_{\odot} (only statistical error considered) from the mass–Compton Y parameter relation. The X-ray emissions were further analyzed by Bagchi et al. (2011) and found to have a disturbed morphology that is compressed in the north.

In addition to the X-ray analysis, Bagchi et al. (2011) performed the first radio investigation of the cluster. Equipped with 150 MHz Giant Meterwave Radio Telescope (GMRT) and 1.4 GHz Very Large Array (VLA) radio data, the discovery of two megaparsec-sized radio relics was made, one north and the other south of the cluster. Bagchi et al. (2011) estimated the projected separation of the relics to be ∼4.4 Mpc. A third diffuse radio feature closer to the X-ray peak (named Y) was discussed, but given the poor resolution imaging, it was unclear whether this feature was a relic on the periphery of the cluster or central and part of a radio halo. In conjunction with the X-ray observations, the radio features distinguished PLCK G287.0+32.9 as a merging galaxy cluster.

A clearer picture of the radio emissions from PLCK G287.0+32.9 was provided by Bonafede et al. (2014) with more sensitive (5–7 times) and higher-resolution (4–8 times) GMRT and VLA radio observations. They determined that the previously named northern radio relic is in fact emission from a radio galaxy and that the poorly resolved emissions near the cluster center are indeed a radio relic. This realization decreases the projected separation of the radio relics to ∼3.2 Mpc, with the northern relic ∼0.4 Mpc and the southern relic ∼2.8 Mpc from the X-ray peak. Since the newly coined relic is much closer to the X-ray peak, the asymmetric distances require a complex merging scenario. Bonafede et al. (2014) also confirmed the existence of a radio halo approximately 1.3 Mpc in diameter. The spectral index of the southern relic decreases with distance from the cluster as expected in diffuse synchrotron aging. However, interestingly, the spectral index of the northern relic decreases initially and then increases sharply with distance from the cluster. This reverse trend is hard to reconcile with the conventional understanding of the diffusive shock acceleration (DSA) spectral aging mechanism (Bonafede et al. 2014).

With a complex merging scenario unfolding from the X-ray and radio observations, a considerable improvement in our understanding of the merger history is possible if we know the underlying dark matter distribution. Mass estimations that rely on equilibrium conditions are inadequate approximations for merging galaxy clusters. The first mass estimation without a hydrostatic equilibrium assumption for PLCK G287.0+32.9 was included in a weak-lensing analysis of SZ-selected clusters (Gruen et al. 2014) with MPG/ESO telescope/Wide Field Imager (WFI) observations. Based on a single Navarro–Frenk–White (NFW) halo fit, centered at the brightest cluster galaxy (BCG), the mass was found to be M_{200m} = 3.77^{+0.95}_{−1.06} × 10^{15} h_{70}^{-1} M_{\odot}. Additional support for this extremely large mass is provided in a recent strong-lensing analysis by Zitrin et al. (2017), where they identified 20 sets of multiply imaged galaxies in Hubble Space Telescope (HST) data and determined the cluster to have an effective Einstein radius of θ_E ≈ 42″ (when they assumed z_s ≈ 2).

In this study, we present the first constraints on the mass distribution of PLCK G287.0+32.9 from a weak-lensing analysis of Subaru and HST observations. Our analysis with this new data set provides substantial improvements over the previous weak-lensing study of Gruen et al. (2014). In terms of the source density, our deeper Subaru imaging data alone yield more than four times the background galaxies usable for lensing analysis. This enhancement enables us to achieve much tighter constraints on the cluster mass and to resolve merging substructures. In addition, the high-resolution HST coverage in the central 3′ × 3′ region allows us to obtain more than 100 galaxies arcmin^{-2}, which is essential to reveal substructures in the densest region.

Our paper is organized in the following manner. In Section 2, we describe our data reduction techniques for Subaru and HST photometric data and Keck spectroscopic data. Modeling of the point-spread function (PSF) is explained in Section 3, followed by a brief overview of weak-lensing theory in Section 4. We describe our shape measurement in Section 5 and the resulting source catalog creation in Section 6. Section 7 briefly explains the redshift estimation for the source catalogs. In Section 8 we present our results. We then discuss the results in Section 9 and conclude in Section 10.

Throughout this work, we assume a flat ΛCDM cosmology with H_0 = 70 km s^{-1} Mpc^{-1}, Ω_m = 0.3, and Ω_Λ = 0.7. At the redshift of PLCK G287.0+32.9 (z = 0.385), 1″ corresponds to 5.25 kpc. We use the notation of R_Δ and R_Δm to indicate the radius of a sphere inside which the mean matter density is Δ times the critical matter density (c) or the mean matter density (m) of the universe at the cluster redshift. The analogous notation is used to present mass enclosed at the defined radii. The factor h_{70}^{-1} = H_0/(100 km s^{-1} Mpc^{-1}) is included in masses derived in this work. All magnitudes are defined in the AB magnitude system.

2. Observations

2.1. Subaru/SuprimeCam Data Reduction

Observations of the galaxy cluster PLCK G287.0+32.9 were carried out with the 8.2 m Subaru Telescope on Maunakea, on the night of 2014 February 26 (PI: D. Wittman). We obtained seven pointings of the g-band filter with total integration time of 753 s and 10 pointings of the r-band filter with total integration time of 2913 s. The median seeing for g and r was 1″17 and 1″13, respectively. In our analysis, we use the r-band image to measure the shapes of galaxies (Section 5) and use g − r color to select galaxies (Section 6).

Weak-lensing analyses can be hampered by spurious features such as bad columns, cosmic rays, bleeding trails, and diffraction spikes. A rotation of 30° for g and 15° for r was introduced between pointings to minimize the effect of these features. This method has been shown to increase the number of usable galaxies available for weak-lensing studies (Jee et al. 2015, 2016), minimizing the number of galaxies contaminated
by the bleeding trails of saturated stars. The SuprimeCam’s 34′ × 27′ field of view allowed each pointing to amply cover the galaxy cluster region (∼11 Mpc × 8.5 Mpc at z = 0.385).

Special care is required during data reduction to produce a weak-lensing quality image. The Subaru supplied SDFRED2 package\(^\text{10}\) is used for the basic steps: overscan subtraction, bias correction, and flat-fielding. SDFRED2 is also used to correct for the geometric distortion due to the telescope optics and distortion due to the differential atmospheric dispersion. Each frame is then passed through SExtractor (Bertin & Arnouts 1996) to prepare a catalog of objects to be used in SCAMP (Bertin 2006). SCAMP is applied to correct for residual distortions and to refine the World Coordinate System (WCS) for each frame. SCAMP uses a reference catalog to compute astrometry. A quality reference catalog is required to achieve the precision needed for weak-lensing analysis. We use the Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006) catalog as reference because it has been shown (Heymans et al. 2012; Jee et al. 2015, 2016) that it provides the most accurate astrometric solution (measured rms ∼ 0.02 pixels) in our field. Photometric solutions are obtained by comparing common astronomical objects.

The final step in creating a weak-lensing quality image is to precisely co-add the frames into a mosaic image. A mean stack yields the highest-S/N results. However, the frames are prone to cosmic rays and saturation trails. For this reason, the frames are co-added in two steps. First, the software SWarp (Bertin et al. 2002) is applied to the frames to create a median-stacked mosaic image. As part of the SWarp process, frames are translated, rotated, and distortion-corrected in preparation for co-addition. These individual RESAMP frames are useful for our analysis, and we store them for later use. After resampling, the frames are carefully aligned using the WCS solution from SCAMP and co-added by SWarp into a median-stacked mosaic image. The median-stacking process outputs a weight file for each component frame that contains the Gaussian variance of each pixel. The median-stacked mosaic image is then compared to the stored RESAMP frames, and pixels from the RESAMP frames that deviate more than 3σ from the median-stacked image are set to zero in the corresponding weight file. Finally, the frames are co-added in SWarp by weight-averaging the input frames, and a mean-stacked mosaic image is created.

2.2. Hubble Space Telescope/Advanced Camera for Surveys

Data Reduction

HST observations of PLCK G287.0+32.9 were made under program 14165 on 2016 August 3 (PI: S. Seitz) and program 14096 on 2017 February 21 (PI: D. Coe). Program 14165 observed the cluster using the Advanced Camera for Surveys (ACS) filters F475W, F606W, and F814W with exposure times of 2160 s (one orbit), 2320 s (one orbit), and 4680 s (two orbits), respectively. In addition, four orbits were used to image the central region of the cluster. For each orbit, four exposures were taken with a half-pixel dithering pattern administered. Program 14096 carried out observations with the ACS filter F435W (2125 s of integration) and the ACS filters F105W (1362 s), F120W (711 s), F140W (712 s), and F160W (1962 s). The ACS observations are limited to the inner ∼2′ around the BCG and have a larger PSF than the ACS observations. The ACS filters are carefully aligned using the WCS solution from SCAMP and co-added by SWarp into a median-stacked mosaic image. The median-stacking process outputs a weight file for each component frame that contains the Gaussian variance of each pixel. The median-stacked mosaic image is then compared to the stored RESAMP frames, and pixels from the RESAMP frames that deviate more than 3σ from the median-stacked image are set to zero in the corresponding weight file. Finally, the frames are co-added in SWarp by weight-averaging the input frames, and a mean-stacked mosaic image is created.

2.3. Keck/DEIMOS Data Reduction

Spectroscopic observations (PI: W. Dawson) were done with the DEep Imaging Multi-Object Spectrograph (DEIMOS) mounted on the Keck II Telescope. Here we will highlight the spectroscopic procedure and refer the reader to Dawson et al. (2015) and N. Golovich et al. (2017, in preparation) for a thorough description. The data were collected with three slit masks on 2015 February 16 using the Subaru SuprimeCam photometric images for target selection. A 1200 line mm\(^{-1}\) grating was used with 1″ wide slits, which resulted in a pixel scale of 0.33 Å pixel\(^{-1}\) and a resolution of ∼1 Å. From this, we obtained secure spectroscopic redshifts for 211 cluster member galaxies in a redshift range of 0.36 < z < 0.41.
Figure 1 is the redshift distribution of the cluster members. The mean redshift of the cluster member galaxies is \( z = 0.385 \) with a velocity dispersion of \( \sigma_v = 1697 \pm 87 \) km s\(^{-1}\). A Kolmogorov–Smirnov (K-S) test compares the cumulative distribution of the galaxy redshifts with that of a Gaussian function, and the result, \( p = 0.82 \), suggests that the distribution is consistent with a Gaussian. This may suggest that the substructures of the cluster possess negligible line-of-sight velocity differences. We found no additional clustering in the range \( 0.15 < z < 0.90 \).

2.4. Object Detection and Photometry

The main noise contribution to weak-lensing analyses is the large intrinsic ellipticity dispersion of galaxies. Therefore, one would like to have as many galaxies in the shape catalog as possible, including faint and small galaxies, as long as we can control systematic errors (e.g., noise bias). To achieve this, we do photometry with SExtractor in dual-image mode. The merit of dual-image mode is that it uses one image for detection and a second for photometry, allowing photometry to be performed consistently with the same isophotal aperture for each object across different filters. For the Subaru data, we utilize the deeper, \( r \)-band mosaic as the detection image and perform photometry on both the \( g \) and \( r \)-band mosaics. For \( HST \) data, a detection image is created by combining the F435W, F475W, F606W, and F814W mosaic images, and photometry is done on F606W and F814W. A band-specific weight image created by SExtractor during photometric data reduction is provided for detection, and an rms image is provided for each photometry run. The rms image is created by multiplying the band-specific weight image by the background rms of its mosaic image and masking spurious pixels. For object detection, we require objects to have a pixel value greater than two times the sky rms and to have at least five connected pixels. The settings for deblending are optimized to detect weakly lensed galaxies. DEBLEND\_NTHRESH is set to 32 and DEBLEND\_MINCOUNT to \( 10^{-4} \) to maximize detection of overlapping objects.

The Subaru photometric zero-point is calibrated by matching detected objects to an external star catalog. As our Suprime-Cam photometric data are observed through the \( g \) and \( r \)-band filters, which have similar throughputs to those of the Sloan Digital Sky Survey (SDSS) filters, it would be ideal to directly use SDSS data to calibrate SExtractor magnitudes. However, PLCK G287.0+32.9 is outside the SDSS sky coverage. Thus, we use both an SDSS catalog and a USNO-B1 catalog. First, we choose a field that has overlapping regions in the SDSS and USNO-B1 surveys. We then match stars in the field and plot a color–color diagram (Figure 2) to find a relation between the \( g_{\text{sdss}} \) and \( r_{\text{sdss}} \) filters and the \( B2_{\text{usno}} \) and \( R2_{\text{usno}} \) filters. The transformations are

\[
\begin{align*}
r_{\text{sdss}} &= -0.006(B2_{\text{usno}} - R2_{\text{usno}}) + 0.133 + R2_{\text{usno}}, \\
r_{\text{sdss}} &= -0.014(B2_{\text{usno}} - R2_{\text{usno}}) - 0.132 + B2_{\text{usno}}.
\end{align*}
\]

These transformations allow us to find the SDSS-equivalent magnitudes of the stars in the USNO catalog, which are then used to calibrate the Suprime-Cam instrumental magnitudes. We also correct for Milky Way dust extinction with estimates provided by Schlafly & Finkbeiner (2011).

The \( HST \) zero-point calibration is more straightforward. We determine the AB zero-point using the header values for

3. PSF Modeling

A critical step to recovering the weak-lensing signal is to model and remove the effect of the PSF. In this analysis, we utilize the principal component analysis (PCA) method to model the PSF. As Jee et al. (2007) showed, the PCA approach accounts for small- and large-scale structures of the PSF better than the wavelet and shapelet methods. Additional merits are that PCA derives the basis functions from the data set itself and requires fewer components than the other two methods to model the PSF. Here we describe the Subaru \( r \)-band PSF modeling method in detail and follow it with a few comments on the alterations used for the \( HST \) F814W PSF modeling.

The Subaru PSF varies from frame to frame, as well as within each frame, and the variation of the PSF is inherited by the co-added mosaic image from each of its component frames. Therefore, the PSF must be modeled for each frame individually and accumulated to a final PSF to be used for galaxies in the mosaic image.

The first step in our PSF modeling is to select a robust sample of stars to measure the PSF from. Stars are identified in the RESAMP frames that are created during the SWarp step of our data reduction. The star sample is constrained by half-light radius, magnitude, maximum flux, and ellipticity \( (e = (a - b)/(a + b)) \), where \( a \) and \( b \) are the semimajor and semiminor axes, respectively. Figure 3 shows the magnitude as a function of flux radius for objects in one of the RESAMP frames. In this particular frame, the stellar locus resides around 3.4 pixels and trails off where the CCD becomes nonlinear with saturation. This should not be confused with
the brighter-fatter effect (for recent work see Lage et al. 2017), which is seen in the figure as a gradual increase in the flux radius of stars with decreasing magnitude. The stars used to model the PSF are marked with red stars. Typically, each frame provides approximately 100 “good” stars. It is assumed that the stars are point sources (i.e., delta function) and any shape is due to convolution with the PSF. To observe the shape of stars, postage stamp images ($21 \times 21$ pixels) of each star are cut from the mosaic and fit with a Gaussian weighted quadrupole. The direction and magnitude of the ellipticity of the stars are shown in the left panel of Figure 4. These ellipticities describe the variation of the PSF across the mosaic image.

3.1. Principal Component Analysis

With the robust sample of stars determined, we can now model stellar PSFs and use them to construct galaxy PSFs. We characterize the PSF using PCA on the stars in each of the RESAMP frames. PCA is an orthogonal linear transformation of a data set to a new basis of vectors (principal components), ordered by their decreasing degree of variance. One method to implement an orthogonal linear transformation is PCA with a covariance matrix. Briefly, the steps of PCA applied to a single RESAMP frame are as follows:

1. Determine the mean stellar PSF and residual PSF.
2. Calculate the covariance matrix of the residual.
3. Compute eigenvectors and eigenvalues of the covariance matrix.
4. Select the eigenvectors that describe the majority of the PSF variation.
5. Project the stellar images onto the new orthogonal basis (principal components).

The first step is to determine the mean stellar PSF and compute the residual PSF (star – mean) for each star. Stellar postage stamp images ($21 \times 21$ pixels) are cut from the RESAMP image. RESAMP images are ideal for measuring the PSF because they have been rotated, shifted, and distortion-corrected as needed for the co-added mosaic. Next, the stellar postage stamps are stacked into a data cube of $N$ (stars) $\times$ $21$ (pixels) $\times$ $21$ (pixels). When creating the data cube, subpixel shifts are applied to each postage stamp to ensure that the peak of the stellar intensity is located at the center pixel. As explained in Jee et al. (2007), the variance of the PSF would be dominated by the scattered peak positions if centering was not applied. Bicubic interpolation is used to achieve the subpixel shifts because it creates fewer interpolation artifacts than higher-order windowed sinc interpolation schemes (Jee et al. 2007). Once centered, the flux of each star is normalized. At this point, we remove a dimension from the data cube by flattening each stellar image into a 441-component one-dimensional array of pixels, $M$. This results in a matrix that is $M$ columns (pixels) $\times$ $N$ rows (stars). We calculate the mean PSF by averaging along each column and then subtract the mean from each row to get the residuals, $R$. These residuals represent the deviation of each stellar PSF from the mean PSF for a single RESAMP frame.

Next, the covariance matrix for $R$, the residuals, is calculated, and the eigenvalues and their corresponding eigenvectors are determined from the covariance matrix. The eigenvalues are the variance of the residual, and the eigenvectors are the principal components. As shown in Jee et al. (2007), the majority of the variance exists in the 21 components with the highest eigenvalues. This allows us to describe the residual in 21 components without sacrificing precision. The last step of the PCA is to project the residuals $R$ onto the orthogonal basis formed by the 21 principal components.

3.2. Modeling the PSF

The objective of modeling the PSF is to create images that represent the PSF of galaxies in the stacked mosaic image, where the weak-lensing signal is measured. Therefore, the variation of the PSF as measured from stars needs to be applicable to galaxies. We achieve this by fitting the spatial variation of each of the 21 components of the projected $R$ with a third-order polynomial and storing the 10 coefficients, $d_m$. The coefficients represent the variation of the PSF from the mean PSF across an individual RESAMP frame. The PCA and polynomial fitting process is repeated for each RESAMP frame that was co-added to create the mosaic. The PSF at any location $(x, y)$ of the mosaic is constructed for each RESAMP frame and then stacked to a final PSF. The reconstruction of the $k$th object PSF, before stacking, has pixel values:

$$C_x(i, j) = \sum_{n=0}^{20} a_{kn} P_n(i, j) + T(i, j),$$

where $a_{kn}$ are the coefficients of the $k$th object derived from the $d_m$ coefficients as

$$a_{kn} = \sum_{l,m=0}^{l+m\leq3} d_{lm} x^l y^m,$$

with $x$ and $y$ the mosaic image coordinates of the object. The polynomial fit is found by projecting the coefficients onto the principal component basis, $P_k(i, j)$, and the model PSF is constructed by adding the mean PSF, $T(i, j)$. The $k$th object PSF from each model is saved to a fits file to be used in shape fitting. The right panel of Figure 4 shows the quadrupole measured ellipticity of the modeled stellar PSFs. Comparing...
the panels of the figure, the ellipticity of modeled stellar PSFs is in good agreement with the observed ellipticity.

Modeling of the PSF for the HST frames is also done using a PCA approach. However, unlike the Subaru observations, the HST frames do not have the necessary number of high-S/N stars to extract the PSF information from the science frames. Thus, we match PSFs for each frame from a PSF library created using external stellar field images (Jee et al. 2007). As Jee et al. (2007) showed, this is possible because the variation in the HST PSFs is primarily caused by the focus of the telescope. The PSF variation pattern becomes nearly identical when two observations are taken under the same focus offset.

4. Weak Gravitational Lensing Theory

Since the first detection by Tyson et al. (1990), weak gravitational lensing has become a powerful tool to investigate the mass of galaxy clusters. Immense progress has been made in understanding the systematic uncertainties that are introduced by the telescope and atmosphere. Along with these advances, the nature of weak lensing has cemented it as a distinct tool in galaxy cluster mass determination. In this section, we will give an overview of weak-lensing theory. For a more detailed description of weak-lensing theory we refer the reader to reviews by Bartelmann & Schneider (2001) and Hoekstra (2013).

Weak lensing by a galaxy cluster occurs when light from galaxies beyond the cluster (source galaxies) is deflected as it passes through the cluster gravitational potential. The simplest way to model gravitational lensing is to consider the galaxy cluster as a thin lens. This approximation holds because the size of a galaxy cluster is small compared to the distance from observer to cluster. In the thin-lens approximation, the gravitational potential is analogous to the index of refraction for media. As light passes through the galaxy cluster, it follows Fermat’s principle, following the path of extrema in travel time. This introduces a shift in the apparent location of the source galaxy on the sky. Considering the geometry of the system, we can formulate the relation between the true source position, $\beta$, and the observed position, $x$, as

$$\beta = x - \alpha(x).$$

The scaled deflection angle,

$$\alpha(x) = \frac{1}{\pi} \int \kappa(x') \frac{x - x'}{|x - x'|^2} d^2x,$$

is the gradient of the deflection potential, $\alpha = \nabla \psi$, where

$$\psi(x) = \frac{1}{\pi} \int \kappa(x') \ln|x - x'|d^2x',$$

and the convergence $\kappa$ (defined below) is the dimensionless surface mass density. Through a Green’s function, it can be shown that the deflection potential satisfies the Poisson equation $\nabla^2 \psi(x) = 2\kappa(x)$.

The convergence ($\kappa$) is one of two lens properties used to quantify the gravitational lensing effect. It causes an isotropic focusing of the light rays, which magnifies the image. It is defined as the projected surface mass density ($\Sigma$) of the cluster normalized by the critical surface mass density ($\Sigma_c$) at the cluster redshift:

$$\kappa = \frac{\Sigma(x)}{\Sigma_c}, \quad \Sigma_c = \frac{c^2D_s}{4\pi GD_lD_{ls}},$$

where $G$ is the gravitational constant, $D_l$ is the angular diameter distance to the lens, $D_s$ is the angular diameter distance to the source, $D_{ls}$ is the angular diameter distance from lens to source, and $c$ is the speed of light. The second lens property is shear ($\gamma$)
and is caused by the tidal gravitational field. The shear anisotropically distorts the shape of galaxy images. In the weak-lensing regime ($\kappa \ll 1$, $\gamma \ll 1$), gravitational lensing results in small distortions and single galaxy images.

For source galaxies of angular size much smaller than the variation of lens properties the coordinate transformation by weak gravitational lensing may be expressed by the Jacobian matrix $A$:

$$A = (1 - \kappa) \begin{bmatrix} 1 - g_1 & -g_2 \\ -g_2 & 1 + g_1 \end{bmatrix},$$

where

$$g = \frac{\gamma}{1 - \kappa}$$

is the reduced shear. Joining the two components of the reduced shear gives a complex representation of the shear, $g = g_1 + ig_2$. Positive and negative values of $g_1$ distort the shape of the galaxy along the $x$-axis and $y$-axis directions, respectively, whereas positive and negative values of $g_2$ distort the shape along the $y = x$ and $y = -x$ directions, respectively.

The effect of the transformations changes a circle into an ellipse. As shown in Kaiser & Squires (1993), the shear and convergence are related by the following convergences:

$$\kappa(x) = \frac{1}{\pi} \int D(x - x') \gamma(x') d^2x',$$

$$\gamma(x) = \frac{1}{\pi} \int D(x - x') \kappa(x') d^2x',$$

where $D(x) = -1/(x_1 - ix_2)^2$ is the convolution kernel. In the weak-lensing regime ($\kappa \ll 1$), the reduced shear is approximately equal to the shear, allowing a reconstruction of the surface mass density through measurement of the reduced shear. To measure the reduced shear, we do a statistical analysis of the observed shape of galaxies beyond the cluster. The ellipticity of a galaxy image is

$$\epsilon \approx \epsilon_{\text{intrinsic}} + g,$$

where $\epsilon_{\text{intrinsic}}$ is the source galaxy intrinsic ellipticity. Assuming that the source galaxies are randomly oriented, their complex ellipticity should sum to zero over a large statistical sample. It is then given that the averaged ellipticity of images is the reduced shear:

$$\langle \epsilon \rangle \approx g.$$  

In the following section, we will discuss the steps required to get the reduced shear by measurement of galaxy shapes.

5. Shape Measurement with PSF Correction

In weak lensing, it is critical to accurately measure the shapes of the source galaxies so that the weak-lensing distortion can be quantified with minimal systematic errors. A popular method to measure shapes was proposed by Kaiser, Squires, & Broadhurst (1995, hereafter KSB). The KSB method and its many variations use the quadrupole moments of galaxies and PSFs to estimate the shapes of galaxies. The limitations of this method, such as the uncertainty arising from photon noise and dense fields, have been outlined in Kaiser (2000).

Another method to measure galaxy shapes is to fit their light profile with an analytic model. As highlighted in the GREAT3 challenge (Mandelbaum et al. 2015), fitting a galaxy light profile with an inexact model introduces “model bias” into the measured shear. We choose to model galaxy shapes by fitting the light distribution with an elliptical Gaussian function. To account for model bias, as well as noise bias, we apply a multiplicative correction factor of 1.15 to calibrate our ellipticities. The correction factor is derived from simulations using real galaxy images as described in Jee et al. (2013). The elliptical Gaussian function is

$$G(x, y) = A_0 + A_1 \exp \left[ -\frac{(\Delta x \cos \theta - \Delta y \sin \theta)^2}{2\sigma_x^2} - \frac{(\Delta x \sin \theta + \Delta y \cos \theta)^2}{2\sigma_y^2} \right].$$

where $\Delta x$ and $\Delta y$ are $x - x_0$ and $y - y_0$, respectively. The parameters of the Gaussian function are background flux ($A_0$), peak flux ($A_1$), centroid ($x_0, y_0$), variance ($\sigma_x^2, \sigma_y^2$), and orientation angle ($\theta$). It is well known that the elliptical Gaussian function is a rough approximation of the galaxy light profile. However, weak lensing is a statistical study of minute galaxy shape distortions, and the most effective means to achieving high $S/N$ is to include as many galaxies as possible. For this reason, we choose to fit galaxies with a model that requires few free parameters. Jee et al. (2013) explain that a Sérsic profile (a better model for galaxy light distribution) increases the uncertainty of the measurement by including more pixels with low signal and by having more free parameters to fit. Therefore, although using the Sérsic profile decreases model bias, the larger uncertainty due to additional parameters, in turn, increases noise bias.

Each object in the mosaic image is fit with its own elliptical Gaussian function. To do so, a square postage stamp image of each object is created from the mosaic. The dimensions of the postage stamp are chosen to be $4_0 \times 4_0$ Image per side, where $A_{\text{IMAGE}}$ is the semimajor axis determined by SExtractor. This provides enough room to fit the galaxy profile while at the same time limiting contamination from other sources.

Before fitting the model to each galaxy, it is critical to consider the PSF. We use forward modelling to account for the PSF. This is done by convolving the model Gaussian function (Equation (14)) with the model PSF prior to fitting the object. The convolved model is

$$M(x, y) = G(x, y) \otimes C(x, y),$$

where $G$ is the Gaussian model and $C$ is the PSF model. An iterative minimization method is applied to find the best-fit elliptical Gaussian model for the target object in each postage stamp. For this step, we use MPFIT (Markwardt 2009), which performs least-squares minimization using a Levenberg–Marquardt method. MPFIT accepts initial conditions and allows constraints for all parameters of the function being fit. We fix the background and centroid to the SExtractor measured values in order to minimize the free parameters, and we do not impose any additional constraints on the fit. The algorithm minimizes the difference between the PSF-convolved
model $M_i(x, y)$ and the observed image $O_i(x, y)$:

$$\chi^2 = \sum_{i=1}^{n} \frac{(O_i(x, y) - M_i(x, y))^2}{\sigma_i^2}. \quad (16)$$

For the variance of the $\chi^2$, we provide an rms postage image. Segmentation and rms postage images are cut from the rms and segmentation mosaics output from SExtractor. These images provide a means to disregard pixels from the postage image that do not belong to the current target object, as defined by SExtractor. This is accomplished by setting the rms value of pixels selected from the segmentation map that do not belong to the current target object to an arbitrarily large number ($10^5$). This effectively hides their flux from the fitting algorithm.

The outputs from the $\chi^2$ fit are the seven elliptical Gaussian parameters, status of fit, reduced $\chi^2$, and the $\chi^2$ error. The status is a notification of the success of fit, and the $\chi^2$ error is the $1\sigma$ error for each parameter with an assumed Gaussian prior. From the outputs, we determine the semimajor axis ($a$), semiminor axis ($b$), and orientation angle ($\theta$, measured counterclockwise from the $x$-axis to the semimajor axis) for each object. The complex ellipticity can then be defined as $e = e_1 + ie_2$, with

$$e_1 = \frac{a - b}{a + b} \cos(2\theta),$$
$$e_2 = \frac{a - b}{a + b} \sin(2\theta). \quad (17)$$

The ellipticity error is found by propagating the errors that are output for each of the parameters. Finally, a catalog of the ellipticities for all objects detected from the mosaic image is accumulated. Residual multiplicative biases in shears derived from these shape estimates could be present because the simulations we used for calibration are not perfect representations of our data. Nevertheless, such biases are likely small (at the level of a few percent) and thus subdominant to the statistical uncertainty of this study.

6. Source Selection

The geometry of gravitational lensing requires that the source galaxies be located at a greater distance than the cluster in order for their light to be distorted by the galaxy cluster potential. It is thus expected that these galaxies, on average, appear fainter than the cluster member galaxies. Also, due to the hierarchical formation of the universe, we expect the average cluster galaxies to be more evolved and thus redder. These two characteristics are the basis of a color–magnitude diagram and provide the primary selection criteria for our background source catalog.

Figure 5 is the color–magnitude diagram for Subaru observations of PLCK G287.0+32.9. The horizontal axis is the $r$-band MAG_AUTO, and the vertical axis is $g - r$ MAG_ISO color. The red markers indicate cluster members confirmed by DEIMOS spectroscopy. Near $g - r \sim 1.5$ the confirmed cluster members form a red sequence. Combining the color–magnitude relation and the spectroscopically confirmed cluster members, we create a Subaru cluster member catalog. The catalog contains sources whose $g - r$ color is between 1.2 and 1.7 and $r$ magnitude is between 19 and 23. From this catalog, we remove spectroscopically confirmed noncluster members. This cluster member catalog is used to create cluster luminosity and number density maps.

Next, we select our source galaxies by applying the following constraints:

1. $22 < r < 27$;
2. $-1 < g - r < 1$;
3. semiminor axis, $b > 0.2$ pixels;
4. ellipticity, $e < 0.9$;
5. ellipticity error $<0.3$.

The source galaxies selected in this way are fainter and bluer than the red sequence. To separate stars from background galaxies, the semiminor axis after deconvolution is required to be larger than 0.2 pixels. This excludes objects that have been improperly fit with an extremely elongated ellipse or whose signal covers too few pixels to be from a sheared galaxy. Further star–galaxy separation is achieved by requiring the preseeing ellipticity to be less than 0.9 and the ellipticity error to be less than 0.3. The source galaxies are plotted with blue markers in the color–magnitude diagram. The total number of source galaxies is 27,089 galaxies ($\sim27$ galaxies arcmin$^{-2}$).

An HST source catalog is created using the same constraints as the Subaru catalog with the following adjustments to the magnitude and color cuts:

1. $22 < F814W < 28$;
2. $-0.5 < F606W - F814W < 0.8$.

The mean number density of sources in the HST source catalog is $\sim110$ arcmin$^{-2}$. An HST cluster member catalog is created by selecting galaxies with magnitude ranging from 16 to 23 and $F606W-F814W$ color between 0.8 and 1.3. These constraints encapsulate the spectroscopically confirmed cluster members.

Obviously, our source selection above does not remove blue cluster members. If significant, the contamination will dilute.
our lensing signal and thus lead to underestimation of the cluster mass. This issue has been discussed by a number of authors (Broadhurst et al. 2005; Okabe et al. 2010; Applegate et al. 2014; Medezinski et al. 2017; Melchior et al. 2017). However, based on the number density excess test with respect to control fields, our previous analyses have shown that the dilution, if any, is much below the statistical errors. For example, Figure 4 of Jee et al. (2014b) demonstrates that the source number density distribution in the “El Gordo” cluster at z = 0.87, obtained by removing only the red cluster members, is in good agreement with the statistics in GOODS-N and GOODS-S fields, which implies that the blue member contamination is negligible. More recently, a similar conclusion is made by Jee et al. (2017) for two clusters at even higher redshift (z ≥ 1.5). Because PLCK G287.0+32.9 is at much lower redshift (z = 0.385) than these clusters, it is unlikely that the contamination becomes a critical issue in the current study.

7. Redshift Estimation

As shown in Equation (7), the convergence depends on source redshift (more exactly, sensitive to the ratio of Dls/Ds). We cannot determine photometric redshifts for source galaxies for PLCK G287.0+32.9 based on two filters. Therefore, we estimate the redshift distribution of the source galaxies by modeling an external photometric redshift catalog to match our source catalog. We use the Great Observatories Origins Deep Survey (GOODS) South photo-z catalog compiled by Dahlen et al. (2010). The GOODS-S catalog makes use of 12 photometric bands to determine redshifts and has a total sky coverage of ~153 arcmin².

The red bars in the top panel of Figure 6 show the magnitude distribution of galaxies in the GOODS-S catalog after applying the filter-corrected constraints (Section 6) that were used to form the Subaru source catalog. The magnitude distribution of our Subaru source catalog galaxies (blue bars) shows a large departure from that of the constrained GOODS-S catalog at faint magnitudes because the GOODS-S imaging is much deeper than our Subaru imaging. We weight the GOODS-S catalog magnitude distribution to match our source catalog magnitude distribution. The weighted distribution is shifted to lower redshift, as the blue bars in the bottom panel show. However, foreground galaxies, which are not lensed, do not contribute to the lensing signal. To account for dilution of the lensing signal (Equation (7)) by foreground galaxies, we enforce the following on the GOODS-S catalog:

$$\beta = \max \left[ \frac{D_{ls}}{D_s}, 0 \right].$$

(18)

Using this definition of lensing efficiency gives an effective redshift. The effective redshift of the weighted GOODS-S sample that has been modeled to represent our Subaru source catalog is $z_{\text{eff}} = 0.935$ and $\langle \beta \rangle = 0.523$. Representation of the redshift distribution of galaxies by a single number leads to an overestimation of the shear (e.g., Hoekstra et al. 2000). The first-order correction applied to the reduced shear to take the width of the redshift distribution into consideration when fitting a shear model is (Seitz & Schneider 1997)

$$g' = \left[ 1 + \left( \frac{\langle \beta^2 \rangle}{\langle \beta \rangle^2} - 1 \right) \kappa \right] g,$$

(19)

Figure 6. Estimation of the effective redshift for Subaru source catalog galaxies using the GOODS-S photometric redshift catalog of Dahlen et al. (2010). The GOODS-S catalog is modeled to represent the redshift distribution of our Subaru source catalog. Top: number density of objects in the color- and magnitude-constrained GOODS-S catalog (red bars) and the Subaru source catalog (blue bars) highlights the difference in depth between the two catalogs. Bottom: redshift distribution of the GOODS-S catalog before (red) and after (blue) correcting for depth and applying Equation (18).

where the variance of the distribution for the Subaru source catalog is $\langle \beta^2 \rangle = 0.33$ and $\kappa$ is the modeled (iterated) convergence.

We also use the GOODS-S catalog to estimate the redshift of the HST source catalog. After applying Equation (18) and correcting for depth, our HST source catalog is estimated to have $\langle \beta \rangle = 0.545$ with an effective redshift of $z_{\text{eff}} = 0.996$. The width of the distribution is found to be $\langle \beta^2 \rangle = 0.35$. We note that these estimates of $\langle \beta \rangle$ have an uncertainty, in particular due to the small area of the GOODS-S data. Comparison with detailed studies of these effects (e.g., Gruen & Brimioulle 2017; Jee et al. 2017) indicates that this is below a relative uncertainty of 5% and thus subdominant compared to the statistical uncertainty of our mass estimates.

8. Results

8.1. Surface Mass Density

Merging galaxy clusters, such as the Bullet Cluster, have been shown to have multimodal mass distributions. This is not surprising, as the merging timescale is of the order of gigayears. PLCK G287.0+32.9 shows telltale signs of a merger, as it hosts two radio relics and a radio halo. Therefore, it may be expected to contain a multimodal mass distribution. To investigate the mass distribution, we create mass maps in the following manner.

First, a shear map is created by spatially averaging the galaxy ellipticities from the source catalog. The left panel of
Figure 7. Left: whisker plot of the Subaru reduced shear determined by averaging the galaxy ellipticities within an \( r = 80'' \) top-hat kernel. The direction and length of the whiskers represent the direction and magnitude of the reduced shear. The shear tends to be tangential to the cluster center and increase in magnitude toward the cluster center (around \( 1^h 50^m 45^s, -28^\circ 05' \)). Right: Subaru convergence reconstructed by the inversion (Equation (10)) of the shear map. The mass reconstruction shows a clear peak. Low convergence detections are seen to the NW and SE.

Figure 7 is a low-resolution visualization of the Subaru reduced shear created by averaging the source galaxy ellipticities within an \( r = 80'' \) top-hat kernel. Each whisker represents the local magnitude and direction of the averaged ellipticity or, approximately, the reduced shear. This figure shows that the shear is predominantly oriented tangential to the cluster center (around \( 1^h 50^m 45^s, -28^\circ 05' \)), with the magnitude of the shear tending to decrease with distance from the center. A convergence map, as shown in the right panel of Figure 7, is reconstructed by convolving the shear map with the transformation kernel (Equation (10)). As portrayed in Equation (7), the convergence is the normalized projected surface mass density, which is dominated by dark matter. With this in mind, we will use the terms convergence, mass, dark matter, and projected surface mass density interchangeably.

The resolution of the mass map is sensitive to the size of the kernel used to average the source ellipticities. The primary concern when selecting a kernel size is to ensure that the number of galaxies averaged over is sufficient enough that the relation \( \langle e \rangle \approx g \) holds. At the same time, we wish to probe the details of the mass distribution to a precision that may allow the detection of substructure. With this in mind, we create two versions of convergence maps.

8.1.1. Subaru Telescope Convergence Map

As mentioned above, the Subaru convergence map is created with an \( 80'' \) radius top-hat kernel. For each spatial bin, \( \sim 150 \) source galaxies, on average, are used to find the reduced shear. The right panel of Figure 7 is the Subaru convergence reconstruction. It is important to note that the convergence values are subject to mass-sheet degeneracy (see, e.g., Falco et al. 1985; Schneider & Seitz 1994); thus, they should not be taken at face value but are useful to distinguish the distribution of mass. The Subaru convergence reconstruction shows a remarkably strong signal that dwarfs any nearby detections. This primary mass clump has a distinct global maximum (mapped in red color and labeled NWc). Around the peak, the convergence has a somewhat triangular shape with vertices pointing west, SE, and NE (mapped in green color). A lesser detection \( \sim 2 \) Mpc to the NW of the global maximum is a local maximum (labeled NW) that is found to have a statistical significance of \( \sim 3 \sigma \) (see below for bootstrap analysis). A second local maximum (\( \sim 3 \sigma \)), at approximately \( 1^h 50^m 55^s, -28^\circ 10' \) (labeled SE), is found in the elongation to the SE. Based on the convergence map, it can be inferred that NWc is the primary cluster and that the SE and NW convergence detections could be subclusters.

In the left panel of Figure 8, the mass distribution is overlaid onto a Subaru color-composite image with color-enhanced GMRT radio (green) and XMM X-ray (red) emissions. It is evident that NWc is within the X-ray-emitting ICM. The NW mass clump is found to be farther NW than the NW radio relic. The SE convergence peak is matched well with the NWc convergence map peak. This convergence peak is dominated by the flux of the BCG. Trailing off to the SE, a second luminosity peak (SEc) is found, but with no clear convergence peak associated with it. This bimodality of the central galaxy distribution was mentioned in Bonafede et al. (2014). In their analysis, it was suggested that NWc and SEc could be two subclusters undergoing a major merger. Since our central galaxy peaks are consistent with theirs, we have adopted their nomenclature. In addition, Bonafede et al. (2014) found a galaxy overdensity in the SE, coinciding with the SE radio relic. Our SE convergence peak is roughly in the same location as the galaxy overdensity (coined SEext) from
Bonafede et al. (2014) and is statistically (see the bootstrap analysis below) consistent with our SE luminosity peak. In Section 9.2, we discuss the statistical significance of any offset between the mass and galaxies. The NW convergence peak has a weak counterpart in galaxy luminosity.

One way to test the significance of each structure that is detected in the convergence map is bootstrapping. We perform bootstrapping by resampling the source catalog with replacement 1000 times. The bootstrapped catalogs are then processed through the same method to produce 1000 convergence maps. From the sample of 1000 bootstraps, we calculate the rms noise of the data and divide the original convergence map by the noise map to find the S/N. The S/N in Figure 9 is a measure of the statistical significance of the structures observed in the surface mass density map. The NWc peak of the mass distribution is detected at the $\sim 9\sigma$ level. The SE and NW structures are less significant, with a $\sim 3\sigma$ detection each. Bootstrapping only predicts the statistical significance of the weak-lensing signal. Additional uncertainty from systematics could be present.

8.1.2. Hubble Space Telescope Convergence Map

To probe the cluster at a higher resolution, we make use of deep HST imaging. The observation footprint of the HST imaging (blue box in Figure 8) is much smaller than the Subaru observations, covering the central $3' \times 3'$ ($\sim 1$ Mpc $\times$ 1 Mpc) field of the cluster. The average distortion within this subfield is high because the region is within a strong-lensing regime. This high distortion accompanied by the high source density ($\sim 100$ arcmin$^{-2}$) allows us to use a smaller kernel to average the ellipticities for mass reconstruction. We choose a 20$''$ radius top-hat kernel to average ellipticities for the HST source catalog. The expected S/N within this 20$''$ kernel is comparable to the one for the 80$''$ kernel applied to the Subaru catalog.

The left panel of Figure 10 shows the HST convergence map overlaid on an HST color composite. It is remarkable that the primary convergence peak that was detected in the Subaru reconstruction as a single peak is now resolved into three peaks in the HST reconstruction. This weak-lensing mapping of the convergence has a striking resemblance to the strong-lensing map of Zitrin et al. (2017). The primary peak (NWc) is consistent with the BCG, a secondary peak (SEc) is observed $\sim 400$ kpc to the SE, and a substructure is found to the west (Wc).

Figure 8. Left: color-composite Subaru image with enhanced radio (green) and X-ray (red) emissions. Radio emissions are from GRMT observations (Bonafede et al. 2014), and X-ray emissions are from XMM-Newton. The overlaid convergence contours (white) peak in the X-ray-emitting ICM, with the highest contour enveloping the BCG. The mass is distributed along a direction similar to the axis connecting the radio relics. The HST F814W pointing is outlined in light blue. Right: mass distribution overlaid on the Subaru cluster member catalog luminosity density. The luminosity density has a bimodal distribution in the cluster center, with the NWc luminosity peak consistent with the mass peak. The SEc luminosity peak has no clear mass counterpart in the Subaru mass reconstruction.

Figure 9. Subaru S/N map obtained by 1000 bootstraps of the Subaru source catalog. The signal is the original convergence map, and the noise is determined from the standard deviation of the bootstrapped convergence maps. The peak of the mass distribution is detected at $9\sigma$ significance, and the substructures to the NW and SE are detected at $3\sigma$ significance.
We test the significance of the substructures by bootstrapping. The resulting *HST* S/N map is shown in the right panel of Figure 10. The color map is the smoothed luminosity distribution of cluster member galaxies. The primary peak, NWc, is detected at the 6σ level and lies on top of the luminosity peak. A 3σ detection of the SEc mass structure is made. An offset (∼12″) from the luminosity peak is observed and is further analyzed in Section 9.2. Wc is detected with a statistical significance of 3σ.

In summary, our Subaru and *HST* mass reconstructions of PLCK G287.0+32.9 find five structures that are detected at ≥3σ statistical significance. The NWc peak (1) is the dominant feature in both the Subaru and *HST* convergence maps. An analysis of *HST* imaging shows that the cluster has two additional substructures detected in close proximity to the NWc peak. The SEc peak (2) is a substructure ∼1″ SE of NWc and has an optical counterpart. The other structure lies to the west, thus named the Wc peak (3), and has a weak optical detection of galaxy light. Looking at the large-scale mass distribution provided by the Subaru convergence map, an NW peak (4) is to the NW beyond the NW radio relic, and an SE peak (5) is located in the SE toward the SE radio relic. In the following sections, the mass of each substructure will be estimated and their relation to the cluster galaxies and ICM will be analyzed.

### 8.2. Substructure Analysis

The detection of multiple peaks in the mass maps reveals that PLCK G287.0+32.9 is a complex system. However, mass reconstruction is a noisy inversion procedure. It is possible that spurious substructures arise because of chance alignments of background galaxies. Here, we quantify the significance of the substructures and their centroids.

We use the galaxy distribution as a supplement to the convergence map to identify substructures. By looking at spatial correlations between the galaxy distribution and convergence peaks, we test the five substructures. For each substructure, we calculate the luminosity centroid by its luminosity-weighted moment within a top-hat prior. The galaxy number centroid is estimated in a similar fashion, except that each galaxy is treated equally. The top-hat prior is centered on the brightest confirmed cluster member nearest the convergence peak, and the radius of the top-hat function depends on the distance to the nearest substructure. Table 1 shows the positions and radii of the top-hat windows. The resulting positions of the luminosity and number density centroids are labeled in Figure 11 with yellow plus signs and green circles, respectively.

We utilize the 1000 bootstrap results of the Subaru and *HST* convergence maps to investigate the statistical significance of the galaxy and convergence alignment. The Subaru data are used to find the peak distribution of the NW and SE substructures. We choose not to analyze the NWc peak in the Subaru bootstraps because it is too close to the SEc and Wc peaks that are not resolved in the Subaru convergence. The NWc and SEc peak distributions are determined from the *HST* bootstraps. The 1000 peak centroids are smoothed by a Gaussian kernel density estimator in order to create the probability density map. Figure 11 shows the 1σ, 2σ, and 3σ contours of each convergence peak distribution. One caveat is that the priors used to find the *HST* convergence peak distributions are very restricted, due to the close proximity of

![Figure 10](image_url)
the NWc and SEc peaks. Therefore, it is possible that the significance contours are artificially tightened by this restrictive prior. We find that the NWc, Wc, NW, and SE substructures have convergence peak distributions that are within 2σ of the galaxy centroids. The fifth, SEc, is outside 2σ, but we warrant its inclusion in our mass analysis because of the nearby luminosity peak, the limited size of the window due to the close proximity of NWc, and the detection of this structure in the strong-lensing analysis of Zitrin et al. (2017). We defer the detailed discussion of the relation of the galaxy distribution and convergence map to Section 9.2.

8.3. Mass Estimation

A traditional approach in quantifying a cluster mass is to approximate the entire mass distribution with a single profile based on a tangential shear profile. However, this approximation becomes inadequate and leads to bias for merging galaxy clusters, which possess multiple halos. Nevertheless, as we have shown in Section 8.1, PLCK G287.0+32.9 is dominated by the primary mass peak coincident with the cluster BCG. Therefore, in this study we choose to use this traditional method to estimate the total cluster mass and also present a comprehensive mass analysis accounting for the substructures. Careful estimation of the substructure masses is critical in our reconstruction of the cluster merger scenario and also provides valuable inputs to our future numerical simulations.

For our tangential shear calculations, we choose to use the BCG as the origin because both the Subaru and HST mass reconstructions show that the BCG and the primary convergence peak are highly consistent. The reduced tangential shear and cross-shear are calculated as

\[
g_T = -g_1 \cos 2\phi - g_2 \sin 2\phi, \\
g_\pi = g_1 \sin 2\phi - g_2 \cos 2\phi,
\]

where \(g\) is the ellipticity of source galaxies (as explained in Section 4). The angle \(\phi\) is measured from the horizontal axis that intersects the defined cluster center to each galaxy position. The cross-shear (or B-mode) is a \(\pi/4\) rotation of the galaxy ellipticities and should be devoid of signal. Significant deviations of the cross-shear from zero are often attributed to residual systematic errors. We measure the tangential shear in annular bins of \(\delta r = 100''\). Weak-lensing approximations become invalid in the central region. Thus, galaxies within \(R_{\text{min}} = 100''\) of the center are omitted from the tangential shear fitting. This minimum radius is approximately twice the estimated Einstein radius (\(\theta_E \approx 42''\); Zitrin et al. 2017).

Figure 12 shows the reduced tangential shear (blue circles) and cross-shear (black crosses) measured from the Subaru shape catalog. The cross-shear is consistent with zero, suggesting minimal systematic errors. The tangential shear is highest near the cluster center, reaching \(g_T = 0.1\), and decreases with radius. The tangential shear is measured out to 1000'' (~5 Mpc), beyond which an annulus does not complete a circle.

The mass of the cluster is estimated by fitting a density profile to the reduced tangential shear. We note that, in this fit, we assume only shape noise in our covariance, i.e., the scatter due to the intrinsic shapes of background galaxies. At the data quality of Subaru and HST data, this is an important but not the only relevant source of mass uncertainty. Uncorrelated large-scale structure along the line of sight to the cluster (e.g., Hoekstra 2003) and variations of cluster mass profiles at fixed mass (e.g., Becker & Kravtsov 2011) cause an uncertainty floor of \(\approx 20\%\) (e.g., Gruen et al. 2015) for massive clusters. The uncertainty on mass due to shape noise (\(\approx 10\%)\) that we quote is thus not the full error on mass. Likewise, we do not expect the residuals of the fit, weighted by the inverse shape noise covariance, to follow a \(\chi^2\) distribution, but rather to be somewhat larger.
uncertainties on the...s 1385 ± 48 km s^{-1}.

\[ M_{200c} = 2.04^{+0.21}_{-0.22} \times 10^{15} h_{70}^{-1} M_{\odot} \]

\[ \chi_{\nu}^{2} = 1.83 \]

where \( \gamma = \frac{\sigma_t}{\sqrt{1 - \kappa}} \) and the Einstein radius is

\[ \theta_E = 4\pi \left( \frac{\sigma_\varepsilon^2}{c} \right) \frac{D_h}{D_s}. \]

where \( \sigma_v \) is the velocity dispersion and \( c \) is the speed of light. In the top panel of Figure 12, the red curve shows the SIS model fit to the reduced tangential shear by least-squares minimization. The model returns the velocity dispersion \( \sigma_v = 1385 \pm 48 \) km s\(^{-1}\). This velocity dispersion is much lower than \( \sigma_v = 1697 \pm 87 \) km s\(^{-1}\) derived from the redshift distribution in Section 2.3. The difference reinforces the importance of an equilibrium-independent mass estimation when considering a merging galaxy cluster. The radius where the SIS model density is 200 times the mean critical density of the universe is \( r_{200c} = 2.29 \pm 0.08 \) Mpc (at \( z = 0.385 \)). The mass within \( r_{200c} \) is \( M_{200c} = 2.04^{+0.21}_{-0.22} \times 10^{15} h_{70}^{-1} M_{\odot} \).

A better description of a dark matter halo is the NFW profile. The density profile of an NFW halo is described by two parameters: the scale radius \( r_s \) and the dimensionless concentration \( c \). Compared to the SIS model, the NFW profile is steeper at large radii and shallower at small radii. We use the mathematical formulation as described in Wright & Brainerd (2000) to model the NFW reduced tangential shear. In general, because of the degeneracy between \( r_s \) and \( c \), a mass–concentration relation is assumed when fitting an NFW profile. However, the extreme mass of the cluster and the high S/N of the lensing signal over a large range permit fitting an NFW profile without relying on a mass–concentration relation. Therefore, our main mass estimate is obtained without any mass–concentration assumption (hereafter 2PNFW). To compare with previous studies, we also provide masses estimated using the mass–concentration relation of Duffy et al. (2008) (hereafter 1PNFW).

The 2PNFW approach gives \( M_{200c} = 2.04^{+0.21}_{-0.22} \times 10^{15} h_{70}^{-1} M_{\odot} \) and \( r_{200c} = 2.29 \) Mpc (435\(^\circ\)). The best-fit parameters are centered at \( (c_{200c}, r_s) = (3.92, 1119) \). As mentioned above, these two parameters are highly degenerate. The uncertainty of the 2PNFW mass is estimated by an MCMC of the parameter space. Figure 13 gives the 1σ (green) and 2σ (blue) filled contours for the uncertainty of the mass–concentration relation. The contours highlight the degeneracy of \( r_s \) and \( c \), but a tight relation is seen along the mass axis.

The middle panel of Figure 12 shows that the 1PNFW profile fits the reduced tangential shear well. The estimated mass of the cluster is \( M_{200c} = 2.22^{+0.27}_{-0.24} \times 10^{15} h_{70}^{-1} M_{\odot} \), with \( c_{200c} = 2.80^{+0.03}_{-0.02} \) and \( r_{200c} = 2.35 \pm 0.09 \) Mpc. The mass–concentration relation is determined from simulations using WMAP5 cosmology, and the scatter in the relation introduces additional uncertainty when used to derive mass.

8.4. Multiple Halo Fit

Radio relics, a radio halo, and a disturbed X-ray morphology suggest that PLCK G287.0+32.9 is a merging galaxy cluster. Adding to this evidence, we detect a complex mass distribution and define five structures. Therefore, modeling the cluster as a single halo may bias the mass estimation. A more proper method is to use a superposition of multiple halos to model the lensing signal.
For our multiple-halo fitting a combined Subaru and HST source catalog is created by joining the catalogs, with the HST shapes taking precedence for all spatially matched sources. Multiple-halo fitting is done by minimizing the difference between the measured ellipticity and a modeled ellipticity for each source galaxy. We assume that each substructure follows an NFW halo with the same mass–concentration relation as above and model the expected ellipticity (shear) at each source galaxy position. The 2PNFW model is not used because the added freedom leads to divergence when fitting. Model ellipticities for each galaxy are constructed while considering multiple halos simultaneously. Each halo is given an initial concentration and is fitted to its convergence peak. Then, the shear at each galaxy position is modeled by considering the contribution from all halos. Halos are fixed at $z = 0.385$ with $\beta = 0.523$ and width of the redshift distribution $(\beta^2)/\langle \beta^2 \rangle^2 = 1 = 0.218$ for galaxies from the Subaru source catalog and $\beta = 0.545$ and $(\beta^2)/\langle \beta^2 \rangle^2 = 1 = 0.163$ for the HST galaxies. The contribution of each galaxy to the complete model is weighted by the uncertainty of its ellipticity as
\[
\sigma_i = \frac{1}{\sqrt{\delta \epsilon_i^2 + \sigma_{SN}^2}},
\]
where $\delta \epsilon_i$ is the ellipticity uncertainty of the $i$th galaxy and $\sigma_{SN}$ is the shape noise ($\sim 0.25$).

We fit a single halo to compare this method with the tangential shear fit (Section 8.3). We fix the halo at the BCG, the same center used in tangential shear fitting, and allow the concentration to vary. Consistent with the tangential shear method, galaxies within 100′ of the peak are excluded from the fitting algorithm. The result is summarized in Table 2. The fitted concentration is $c_{200c} = 2.79 \pm 0.02$, the mass of the halo is $M_{200c} = 2.31^{+0.17}_{-0.17} \times 10^{15} h^{-1}_{70} M_{\odot}$, and $r_{200c} = 2.38 \pm 0.06$ Mpc. As expected, fitting an NFW halo by modeling the contribution of each galaxy is consistent with that of tangential shear fitting. Table 2 also contains the masses derived based on the X-ray and SZ peaks, which are consistent with the mass estimated using the BCG as the center.

A five-halo model is fit to the five structures that were defined from the convergence maps. Halo models are built simultaneously with each centroid fixed to its convergence peak. The masses derived from fitting five halos are summarized in Table 3. Multiple-halo fitting shows that NWc is the primary mass of the system. SEc, NW, and SE are approximately 1/10 of the mass of NWc based on the five-halo fitting. The WC structure is low mass and is insignificant compared to the others. Note that multiple-halo fitting should be more robust than the 1D tangential shear fitting for estimating the mass of a merging galaxy cluster, but the accuracy of this method is still limited by the imposed model.

### 9. Discussion

#### 9.1. Comparison with Other Mass Estimates

As the second most significant detection from the Planck SZ survey, PLCK G287.0+32.9 is expected to be extremely massive. This extreme mass is supported by the high X-ray luminosity ($L_X = 17.20 \pm 0.11 \times 10^{44}$ erg s$^{-1}$) measured by XMM-Newton. Also, the recent strong-lensing analysis by Zitrin et al. (2017) has classified PLCK G287.0+32.9 among the largest Einstein radius ($\theta_E \approx 42''$ for source at $z \approx 2$) clusters detected.

The mass of the cluster was first estimated by the $M_{500c} - Y_{X,500c}$ relation to be $M_{500c} = (15.72 \pm 0.27) \times 10^{14} M_{\odot}$ (Planck Collaboration et al. 2011b). This method uses an equilibrium assumption where $Y_{X,500c}$ is the product of the gas mass inside $R_{500c}$ and the gas temperature measured by XMM-Newton observations. However, mass estimates of merging galaxy clusters that rely on the hydrostatic equilibrium assumption are prone to large systematic errors, due to the severe departure from the hypothesized equilibrium of the merging system.

The first weak-lensing mass estimate was provided by Gruen et al. (2014) with MPG/ESO telescope/WFI observations.
measured the mass by fitting a single NFW halo to the shear centered at the BCG. Using the mass-concentration relation of Duffy et al. (2008), they estimated the mass to be $M_{200c} = 3.77^{+0.95}_{-0.76} \times 10^{15} h_{70}^{-1} M_\odot$. ($M_{200c} = 2.40^{+0.59}_{-0.48} \times 10^{15} h_{70}^{-1} M_\odot$).

In Section 8.3, we fit an NFW halo model to the reduced tangential shear without a mass-concentration relation. Our single-halo mass measurement based on reduced tangential shear for PLCK G287.0+32.9 is $M_{200c} = 2.04^{+0.21}_{-0.22} \times 10^{15} h_{70}^{-1} M_\odot$. Confining the mass-concentration relation to that of Duffy et al. (2008), we find the mass to be $M_{200c} = 2.22^{+0.27}_{-0.24} \times 10^{15} h_{70}^{-1} M_\odot$. This result is consistent with the result of Gruen et al. (2014). The tighter uncertainty ($\sim50\%$ smaller) of our fit is a result of the improved statistics that arises from using deeper imaging. Fitting a single profile to a merging system has been shown to give a biased mass (e.g., Jee et al. 2015). A more careful method to measure the mass, presented in Section 8.4, gives $M_{200c} = 2.31^{+0.17}_{-0.17} \times 10^{15} h_{70}^{-1} M_\odot$.

9.2. Comparing the Galaxy and Convergence Distributions

Galaxy cluster merger scenarios can be tightly constrained by understanding the exact physical interaction among different cluster components: the dark matter mass distribution as reconstructed from weak lensing, the galaxy distribution observed in the optical, and the ICM distribution observed by X-ray and radio emissions. In general, merging galaxy clusters have been shown to have coincident dark matter and galaxies while showing large offsets from the gas distribution. Conversely, some studies have shown dark matter coincident with gas and offset from the galaxy distribution (e.g., Mahdavi et al. 2007; Jee et al. 2014a). Here we discuss the peak distributions for PLCK G287.0+32.9 and its implications for the merging scenario.

The mass peaks of each distribution are summarized in Table 3, and the distribution of mass peaks measured from bootstrap realizations of the mass map is plotted in Figure 11. Figure 14 shows the relation between the mass peak distribution of each halo and the corresponding galaxy number density and luminosity peaks. The most massive clump, NWc (top left), shows a tight distribution of peaks and $1\sigma$ consistency with the galaxy peaks. On the other hand, the SEc (top right) mass distribution is offset from the galaxy peaks by $\sim12''$ ($\sim60$ kpc). This offset is also present in the convergence map presented in Figure 10. Measurement of the peaks in close proximity to the primary NWc cluster is a difficult task that requires a top-hat prior. Also, our weak-lensing assumption relating shears to ellipticity becomes invalid in the strong-lensing regime. The constraint of the top-hat prior may be constricting the distribution, though it did include the galaxy peaks. The NW and SE mass peak distributions are much broader, as expected from their low-S/N detections (Figure 9). Both the NW and SE mass peaks are $2\sigma$ consistent with the galaxy peaks. Looking at the large-scale distribution of the peaks, they are aligned with the axis connecting the radio relics, which is consistent with merger expectations.

9.3. Mass Implications for the Merging Scenario

An integral part of studying galaxy clusters is to provide mass constraints to be used in simulations. Galaxy clusters with ideal merger features, such as the Bullet Cluster (Clowe et al. 2006) and Sausage Cluster (Jee et al. 2015), have been exhaustively analyzed from both observational and theoretical stances. PLCK G287.0+32.9 is by no means as clear as these clusters appear to be, which makes it a good candidate for testing merger theories in a complex environment. For this reason, we provide results that may be used as constraints in future simulations of PLCK G287.0+32.9.

The geometry of the system is consistent throughout the data. Roughly, a merger axis can be defined by connecting the two radio relics through the cluster. Subaru optical observations show that the galaxy distribution is elongated in the SE to NW direction along the merger axis. The evidence presented by our weak-lensing analysis shows that the mass distribution on large scales also follows the same merger axis (Figure 8). The higher-resolution HST mass map shows that two mass peaks (NWc and SEc) exist within the central mass clump and that these two mass peaks also lie along the merger axis.

One of the features that makes PLCK G287.0+32.9 so unique is its asymmetric radio relics. The SE relic is located $\sim2.8$ Mpc from the X-ray peak, whereas the NW relic is only $\sim0.4$ Mpc. Bonafede et al. (2014) proposed two merging scenarios that may result in the asymmetry of the relics. In one scenario, a low-mass group may have accreted from the NW direction and created the two relics during two passages through the primary cluster. Bonafede et al. (2014) mention that the remnant of this subgroup may be detected in the NW. Our mass reconstruction provides locations of substructures that are helpful in constraining the merger scenario. The SEc and SE convergence substructures are consistent with the formation of the SE relic. In one scenario the relic is formed by a merger between the SE mass clump and the primary cluster. In order to explain the NW relic using this scenario, a second subcluster must have been involved. A second scenario could be the formation of both relics by two passes of the SEc substructure. In this scenario, the SE relic is created during first passage and the NW relic upon second passage. The Subaru mass map in Figure 8 shows a substructure in the NW that lies along the merging axis. However, current theories predict that shocks (radio relics) suffer little deceleration while subclusters do (Springel & Farrar 2007). Because the NW substructure is beyond the radio relic, it is not likely the cause of the relic.

10. Conclusions

A weak gravitational lensing analysis of PLCK G287.0+32.9, the second most significant merging galaxy cluster of the Planck SZ survey, has been presented. The large mass of the cluster, coupled with deep HST and Subaru imaging, allowed us to fit an NFW model to the reduced tangential shear, without the restriction of a mass-concentration relation. Our fit confirms that the cluster is extremely massive, with a mass of $M_{200c} = 2.04^{+0.20}_{-0.21} \times 10^{15} M_\odot$. An eye-catching feature of this cluster is its numerous radio emissions. Hosting two radio relics and a radio halo categorizes this cluster as merging. In this work, making use of new imaging, we were able to probe the mass distribution of the cluster and make the first discovery of five substructures. The mass is dominated by the primary cluster, with three of the substructures being $\sim10\%$ of the mass of the primary cluster. The fifth substructure is low mass, $\sim10^{13}$, and cannot be considered a galaxy cluster. Based on the spatial distribution of the substructures, we found that two of
them are consistent with merger scenarios that may have created the radio relics. We believe that there are two ways to proceed in the future. One is to improve the imaging of the cluster by fully covering it with deep HST imaging. The sensitivity of the HST would allow a more thorough look into the substructures that lie in the outskirts of the cluster. The other is to model the merger with simulations using the masses that have been estimated in our work. The asymmetry of the radio relics is rare and would be a good test for our understanding of galaxy cluster mergers.

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