Antiferromagnetic resonance excited by oscillating electric currents

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In antiferromagnetic materials the order parameter exhibits resonant modes at frequencies that can be in the terahertz range, making them interesting components for spintronic devices. Here, it is shown that antiferromagnetic resonance can be excited using the inverse spin-Hall effect in a system consisting of an antiferromagnetic insulator coupled to a normal-metal waveguide. The time-dependent interplay between spin-torque, ac spin-accumulation and magnetic degrees of freedom is studied. It is found that the dynamics of the antiferromagnet affects the frequency-dependent conductivity of the normal metal. Further, it is shown that in antiferromagnetic insulators, the resonant excitation by ac spin-currents can be orders of magnitude more efficient than excitation by the current-induced Oersted field.

Spin-transfer torque (STT) and giant magnetoresistance [1–6] form the foundation of spintronics, together with more recent additions such as spin-orbit torques, whose prominent manifestations are the spin-Hall and inverse spin-Hall effects (SHE/ISHE) [7–9]. The latter, besides their usefulness for device applications, have also developed into standard experimental methods of spin current generation and detection. The interplay of spin-currents and ferromagnetic materials continue to be at the core of developments towards magnetic random access memory (STT-MRAM), sensors, and radio-frequency components.

Parallel to these efforts, antiferromagnetic materials have recently been considered as active components in spintronic applications. So far, most theoretical studies show that, similarly to ferromagnets, the order parameter of an antiferromagnet can be manipulated by spin-transfer torque [10–14] or by optical and magnetic pulses [15–17], and other excitation mechanisms have been proposed [18]. Insulating antiferromagnets are also intensively studied in conjunction with spin transport [19–22].

In the context of practical applications, antiferromagnets exhibit a number of advantages compared to ferromagnets [23]. First, their compensated magnetic moments lack any stray fields, which have been identified as potentially limiting the performance of ferromagnet-based STT-MRAM. In addition, antiferromagnet dynamics can be significantly faster than in ferromagnets — their response can be at THz frequencies. Besides the conventional generation of STT through perpendicular-to-plane injection of polarized dc or — in the case of STT ferromagnetic resonance [24] — ac charge currents, the SHE can be employed for the same purpose. In latter case, a nonmagnetic metal (NM) with pronounced spin-orbit coupling is placed adjacent to the magnetically ordered layer. A charge current parallel to the plane of the NM layer will result in spin-current, whose spatial direction is set by the vector product of the charge current and the spin-polarization direction [9]. Studies exploiting the SHE in this particular geometry have so far mostly been performed on ferromagnetic and ferrimagnetic materials [25–30], and few on antiferromagnetic layers [31].

In this work, an experiment is proposed that takes advantage of the SHE in order to study antiferromagnets in a sample geometry similar to that used to do ferromagnetic resonance spectroscopy, where the role of the Oersted field is replaced by an oscillating spin-current.
Resonant excitation of antiferromagnetic insulators by spin-orbit torques can be of significantly higher efficiency compared to that by Oersted fields. In deriving the frequency-dependent waveguide conductivity it will be shown that the resonant precession of the antiferromagnetic order parameter affects the ac electrical transmission properties of the waveguide. The proposed method can be used to investigate in principle any antiferromagnetic insulator thin film, including MnF$_2$, and NiO.

The considered system consists of an antiferromagnetic insulator (AFM) with two symmetric sublattice magnetizations which is assumed to exhibit a uniaxial anisotropy. The AFM is coupled to a normal metal (NM) thin film with strong spin-orbit interaction that serves as a waveguide for an oscillating ac charge current.

The coordinate system is depicted in Fig. 1. The $x$-axis is the direction of current propagation and coincides with the direction of uniaxial anisotropy in the AFM. The $z$-axis is the direction perpendicular to the NM/AFM interface, which is assumed to lie in the $x$-$y$ plane ($z = 0$). Denoting the thicknesses of NM and AFM films by $d_N$ and $d_A$, respectively, the NM film occupies the space $[0, d_N]$ and the AFM is located in $[-d_A, 0]$. An externally imposed oscillating charge current density of frequency $\omega = 2\pi f$, $j^{\text{ext}}(t) = \hat{e}_x \delta(t) \cos(\omega t)$, flows along the $x$-direction, where $\hat{e}_i$, $i \in \{x, y, z\}$ denotes the unit vector along the $i$th direction. That current arises from a time-dependent electric field $E^{\text{ext}}(t) = E(t) \hat{e}_z$, so that $j^{\text{ext}}(t) = \sigma(\omega)E^{\text{ext}}(t)$, where $\sigma(\omega)$ is the frequency-dependent conductivity of the NM.

As the goal is to investigate processes in the scale of hundreds of GHz and higher, the frequency dependence of the conductivity will be included in the calculation. In the frequency domain, and to first order in the excitation, the spin-polarization vector in the normal metal, with $\sigma_{dr}(\omega) := i/(\omega + i\tau_{rd})$, and $D(\omega) := \frac{1}{2} \sigma_{dr}(\omega) v_F^2$, where $\sigma_{tr}(\omega) := i/(\omega + i\tau_{rt})$, $D(0)$ coinciding with the diffusion constant in the stationary spin-diffusion equation. $\tau_{rd}$ and $\tau_{rt}$ denote the transport and spin-flip relaxation times, respectively, and $v_F$ is the Fermi velocity. With $\nu(\omega) = [\sigma_{sf}(\omega) D(\omega)]^{-1} \tau$, the general solution of Eq. 11 is

$$\mu_s(z, \omega) = \sigma_{sf}(\omega) D(\omega) \frac{\partial^2}{\partial z^2} \mu_s(z, \omega) \tag{1}$$

for the spin-polarization vector $\mu_s$ in the normal metal, with $\sigma_{sf}(\omega) := i/(\omega + i\tau_{sf})$, and $D(\omega) := \frac{1}{2} \sigma_{sf}(\omega) v_F^2$, where $\sigma_{tr}(\omega) := i/(\omega + i\tau_{rt})$, $D(0)$ coinciding with the diffusion constant in the stationary spin-diffusion equation. $\tau_{sf}$ and $\tau_{rt}$ denote the transport and spin-flip relaxation times, respectively, and $v_F$ is the Fermi velocity. With $\nu(\omega) = [\sigma_{sf}(\omega) D(\omega)]^{-1} \tau$, the general solution of Eq. 11 is

$$\mu_s(z, \omega) = A(\omega) \exp[-\nu(\omega)z] + B(\omega) \exp[\nu(\omega)z]. \tag{2}$$

The frequency-dependent spin current along the $z$-direction, caused by the gradients in the spin-polarization and the external electric field via the ISHE is then

$$J_{s,z}(z, \omega) = -\sigma(\omega) \theta_{\text{SH}} E(\omega) \hat{e}_y - \frac{\sigma(\omega)}{2e} \frac{\partial \mu_s(z, \omega)}{\partial z}, \tag{3}$$

where $e > 0$ is the elementary charge and $\theta_{\text{SH}}$ denotes the Spin-Hall angle. The requirement that the above spin current vanishes at the lower boundary of the normal metal, $J_{s,z}( -d_N, \omega) = 0$, allows to express spin-polarization with $A(\omega) + B(\omega) = \mu_s(0, \omega)$ as the single parameter:

$$\cosh[\nu(\omega)d_N]\mu_s(z, \omega) = \cosh[\nu(\omega)(d_N - z)]\mu_s(0, \omega) - 2e\nu^{-1}(\omega) \sinh[\nu(\omega)z] \hat{e}_y \theta_{\text{SH}} E(\omega), \tag{4}$$

Accordingly, the spin current at the NM/AFM interface is

$$J_{s,z}(0, \omega) = \frac{[\sigma(\omega)/(2e)\nu(\omega) \tan\nu(\omega)d_N)]\mu_s(0, \omega)}{[\cosh[\nu(\omega)d_N]]} \hat{e}_y \theta_{\text{SH}} E(\omega). \tag{5}$$

We now consider the spin currents in the AFM. There are two contributions [10, 28, 38], one related to the spin-transfer torque,

$$J_{s,z}^{\text{STT}}(t) = G_{z} \sum_i m_i(t) \times [m_i(t) \times \mu_s(0, t)], \tag{6}$$

and the one arising from spin pumping

$$J_{s,z}^{\text{SP}}(t) = \frac{\hbar G_{r}}{2e} \sum_i m_i(t) \times \frac{d}{dt} m_i(t). \tag{7}$$

In Eqs. (6) and (7), $m_i \ (i \in \{1, 2\})$ denote the two sublattice magnetization unit vectors, and for simplicity it is assumed that the spin-mixing conductance $G_{r}$ is real. This assumption can be made, since its imaginary part usually orders of magnitude smaller than its real part.
The goal is to solve the continuity condition at the NM/AFM interface,

$$J_{s,z}(0, t) = J_{s,z}^{\text{SFT}}(t) + J_{s,z}^{\text{SP}}(t)$$

(8)

for $\mu_s(0, t)$, while considering that the magnetization dynamics of the sublattices is governed by two coupled Landau-Lifshitz-Gilbert equations \[10, 28\],

$$\frac{\text{d}m_i}{\text{d}t} = -\gamma m_i \times H_i + \alpha m_i \times \frac{\text{d}m_i}{\text{d}t} + \gamma Gm_i \times [m_i \times \mu_s(0, t)].$$

(9)

The exchange coupling between the lattice magnetizations is mediated by the effective fields $\mu_0 M_s H_i = -\nabla m_i \cdot \mathcal{E}$, derived from the energy density $\mathcal{E}$ with $(\mu_0 M_s)^{-1} \mathcal{E} = -\lambda m_1 \cdot m_2 - h_{\text{ext}} \cdot \sum m_i - \frac{1}{2} h_k \sum (\varepsilon_x \cdot m_i)^2 + \frac{1}{2} h_p \sum (\varepsilon_z \cdot m_i)^2$. Here, $M_s$ is the saturation magnetization of each sublattice. Furthermore, $\gamma$ is the gyromagnetic ratio, while $h_k$ and $h_p$ denote the strength of two uniaxial anisotropies to include biaxial cases such as NiO. The axes of $h_k$ and $h_p$ are oriented along the $x$- and $z$-direction, respectively. $\lambda$ determines the strength of the exchange interactions between the sublattice magnetic moments, and $G = hG_r/(4e^2 \mu_0 M_s d_A)$ is the scaled (real) spin-mixing conductance. The external magnetic field is assumed to consist only of the time dependent Oersted field $h_{\text{Oe}}$ generated by the oscillating charge current, $h_{\text{ext}} = h_{\text{Oe}} e_y$. Finally, the effective damping $\alpha$ is the sum of the Gilbert damping $\alpha_0$ and a contribution $\gamma hG_r$ accounting for spin-pumping.

The AFM resonance frequency can be as high as 0.1 THz, i.e., it is comparable to $\tau_{sp}^{-1}$ and $\tau_{TR}^{-1}$. Thus, the spin-accumulation in the NM and the magnetization dynamics in the AFM take on the same time scale, which requires a self-consistent solution of Eq. \[8\]. This is in contrast to previous work considering similar sample geometries \[28-29\], where the dynamical time scales of the magnetic system and the conductor could be separated, and the time dependence only entered through the boundary conditions. To this end, it is helpful to note that the interest is in small angle precession of the magnetizations. It is therefore sufficient to expand to first order in the deviations of the sublattice magnetizations from the ground state, where the lattice magnetizations are largely oriented along the anisotropy axis, i.e., $m_i \approx (-1)^{i-1} \varepsilon_x + \delta m_{1y} e_y + \delta m_{2z} e_z$. The dynamic parts of the lattice magnetizations, the spin-accumulation and the Oersted field can be considered as small and of first order in $E^{\text{ext}}$. Then, the linearized equation of motion for the magnetizations reads

$$\frac{\text{d}}{\text{d}t} \delta m(t) = \mathcal{A} \delta m(t) + \mathcal{N} h_{\text{Oe}}(t) + \mathcal{A} \mathcal{F}(t),$$

(10)

with $\delta m(t) := [\delta m_{1y}(t), \delta m_{1z}(t), \delta m_{2y}(t), \delta m_{2z}(t)]^T$ and $\mathcal{F}(t) = [0, \mu_{sy}(0, t), \mu_{sz}(0, t)]^T$. Furthermore, in Eq. \[10\],

$$- (1 + \alpha^2) \gamma^{-1} \mathcal{A} := \begin{pmatrix}
\alpha(h_k - \lambda) & h_k - h_p - \lambda & -\alpha \lambda & -\lambda \\
-h_k + \lambda & \alpha(h_k - h_p - \lambda) & \lambda & -\alpha \lambda \\
-\alpha \lambda & -\lambda & \alpha(h_k - \lambda) & -h_k + h_p + \lambda \\
-\lambda & -\alpha \lambda & h_k - \lambda & \alpha(h_k - h_p - \lambda)
\end{pmatrix},$$

and $\mathcal{N} := -\gamma \mathcal{A}^{-1} \mathcal{N} = (-\alpha, 1, -\alpha, -1)^T$. Then, to first order, the expressions \[9\] and \[7\] can be written as

$$J_{s,z}^{\text{SFT}}(\omega) = \frac{G_r}{\gamma} p(\omega),$$

(11)

and

$$\frac{e}{hG_r} J_{s,z}^{\text{SP}}(\omega) = \mathcal{Z} \left[ -i\omega - \mathcal{A} \right]^{-1} [\mathcal{N} h_{\text{Oe}}(\omega) + \mathcal{A} \mathcal{F}(\omega)],$$

(12)

where

$$\mathcal{Z} := \frac{1}{2} \gamma e \gamma_{\text{sp}}^{-1} \times \begin{pmatrix}
0 & 0 & 0 & 0 \\
0 & h_k - 2\lambda & -\alpha(h_k - h_p) & h_k - 2\lambda & \alpha(h_k - h_p) \\
0 & h_k - h_p - 2\lambda & -\alpha h_k & h_k - h_p - 2\lambda & -\alpha h_k
\end{pmatrix}.$$

With Eqs. \[11\] and \[12\], Eq. \[8\] can be solved for $\mu_s(0, \omega)$. In the symmetric sample orientation considered here, only the $y$-component of the spin-accumulation is non-vanishing:

$$\frac{\mu_{sy}(0, \omega)}{e \theta_{\text{SH}} E(\omega)} = \left[ \frac{\cosh(d_N \kappa / 2)}{2 \sinh^2(d_N \kappa / 2)} + \coth \left( \frac{d_N \kappa}{2} \right) \frac{\kappa}{2} \right]^{-1}$$

(13)

with the effective conductance

$$\mathcal{F}(\omega) = G_r \frac{\gamma^2(h_k - 2\lambda)(h_k - h_p + iG_h\omega) + \alpha \gamma \omega[G_h\omega - i(2h_k - h_p - 2\lambda)] - (1 + \alpha^2) \omega^2}{\gamma^2(h_k - h_p)(h_k - 2\lambda) - i\alpha \gamma (2h_k - h_p - 2\lambda) \omega - (1 + \alpha^2) \omega^2}$$

(14)
The quantity $G(\omega)$ contains all the properties of the AFM and establishes the link between the two subsystems of wave-guide and magnet. An example for $G(\omega)$, computed for MnF$_2$, is shown in Fig. 2. The line-shaped feature reflects the increased spin pumping activity when the AFM is driven near resonance. With $G(\omega)$, it is possible to compute the self-consistent spin-accumulation resulting from the interplay with the AFM. Examples are shown in Fig. 3.

The influence of the Oersted field generated by the oscillating current is much smaller than that of the SHE, and therefore its contribution to the result (13), has been omitted. In Fig. 4 the two excitation mechanisms are compared as a function of waveguide thickness under the experimentally relevant condition of constant power injection. Starting at low $d_N$, the AFM precession amplitude first increases, as the spin-accumulation builds up on the length scale of the spin diffusion length $\lambda_N$. As $d_N$ is increased further, the current density and thus the influence of the spin-transfer torque decrease, until the Oersted field starts to dominate at $d_N \approx 0.5 \mu m$. At this length scale, however, the skin depth is expected to limit further increase of the Oersted field’s influence.

The spin-accumulation imbalance induced by the AFM dynamics influences the charge transport through the NM layer via the SHE. The waveguide thickness-averaged charge current density and the electric field are related by the effective electric conductivity $\tilde{\sigma}$ with

$$\frac{\tilde{\sigma}}{\sigma} - 1 = 4\theta_{SH}^2 \frac{\sinh(\kappa d_N) [\kappa \sigma \sinh(\kappa d_N) + G \cosh(\kappa d_N)]}{d_N [\kappa \sigma \sinh(\kappa d_N) + 2G \cosh(\kappa d_N)]},$$

(15)

The above change in the conductivity is shown in Fig. 3(c). The resonant dynamics of the AFM is transferred via the ISHE to the charge flow through the spin-Hall metal, resulting in an effective conductivity that exhibits a peak at the resonance frequency of the AFM. The effect is caused by the magnetization dynamics; it takes place on top of the spin-accumulation background set by the so-called Spin-Hall magnetoresistance [42, 43].

![Figure 3](image-url)
The size of the feature is small due to the averaging over the waveguide and the fact that it is of second order in $\theta_{SH}$. However, transport effects of comparable size have been measured at GHz frequencies [44], and modules extending network analyzer operation to the THz range are available.

In summary, the analysis here considers the time-dependent interplay between the AFM spin dynamics and the spin-transport in the waveguide on an equal, self-consistent footing. The proposed method provides an efficient mechanism to excite and study spin-waves in normal metal / antiferromagnet thin film systems. From a practical point of view, ac-spin currents generated by spin-orbit torques provide a new way to study antiferromagnetic resonance in insulators and thus characterize their magnetic interactions, including their magnetic anisotropy, exchange and damping.

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[1] M. N. Baibich, J. M. Broto, A. Fert, F. Nguyen Van Dau, F. Petroff, P. Etienne, G. Creuzet, A. Friederich, and J. Chazelas, Phys. Rev. Lett. 61, 2472 (1988).
[2] J. Barnas, A. Fuss, R. E. Camley, P. Grünberg, W. Zinn, Phys. Rev. B 42, 8110 (1990).
[3] J. Slonczewski, J. Magn. Magn. Mater. 159, L1 (1996).
[4] L. Berger, Phys. Rev. B 54, 9353 (1996).
[5] E. B. Myers, D. C. Ralph, J. A. Katine, R. N. Louie and R. A. Buhrman, Science 285, 867 (1999).
[6] J. A. Katine, F. J. Albert, R. A. Buhrman, E. B. Myers and D. C. Ralph, Phys. Rev. Lett. 84, 3149 (2000).
[7] M. I. Dyakonov and V. I. Perel, JETP Lett. 13, 467 (1971).
[8] S. O. Valenzuela and M. Tinkham, Nature 442, 176 (2006).
[9] S. Takahashi and S. Maekawa, Sci. Technol. Adv. Mater. 9, 014105 (2008).
[10] H. V. Gomonay, and V. M. Loktev, Phys. Rev. B 81, 144427 (2010).
[11] H. V. Gomonay, R. V. Kunitsyn, and V. M. Loktev, Phys. Rev. B 85, 134446 (2012).
[12] R. Cheng, J. Xiao, Q. Niu, and A. Brataas, Phys. Rev. Lett. 113, 057601 (2014).
[13] R. Cheng, M. W. Daniels, J. G. Zhu, and D. Xiao, Phys. Rev. B 91, 064423 (2015).
[14] M. W. Daniels, W. Guo, G. Malcolm Stocks, D. Xiao and J. Xiao, New J. Phys. 17, 103039 (2015).
[15] S. Wienholdt, D. Hinckle, and U. Nowak, Phys. Rev. Lett. 108, 247207 (2012).
[16] O. Gomonay, M. Kläui, and J. Sinova, Appl. Phys. Lett. 109, 142404 (2016).
[17] T. Higuchi and M. Kuwata-Gonokami, Nat. Commun. 7, 10720 (2016).
[18] A. Sekine and T. Chiba, Phys. Rev. B 93, 220403(R) (2016).
[19] C. Hahn, G. de Loubens, V. V. Nalotov, J. B. Youssef, O. Klein, and M. Viret, Europhys. Lett. 108, 57005 (2014).
[20] H. Wang, C. Du, P. C. Hammel, and F. Yang, Phys. Rev. Lett. 113, 097202 (2014).
[21] T. Moriyama, S. Takei, M. Nagata, Y. Yoshimura, N. Matsuzaki, T. Terashima, Y. Tserkovnyak, and T. Ono, Appl. Phys. Lett. 106, 162406 (2015).
[22] Y. M. Hung, C. Hahn, H. Chang, M. Wu, H. Ohldag, and A. D. Kent, AIP Adv. 7, 055903 (2017).
[23] V. Baltz, A. Manchon, M. Tsol, T. Moriyama, T. Ono, and Y. Tserkovnyak, arXiv:1606.01281v2 (2017).
[24] J. C. Sankey, Y.-T. Cui, J. Z. Sun, J. C. Slonczewski, R. A. Buhrman, and D. C. Ralph, Nat. Phys. 4, 67 (2008).
[25] L. Liu, T. Moriyama, D. C. Ralph, and R. A. Buhrman, Phys. Rev. Lett. 106, 036601 (2011).
[26] Y. Zhou, H. Jiao, Y. -t. Chen, G E. W. Bauer, and J. Xiao, Phys. Rev. B 88, 184403 (2013).
[27] H. -J. Jiao and G. E. W. Bauer, Phys. Rev. Lett. 110, 217602 (2013).
[28] T. Chiba, G. E. W. Bauer, and S. Takahashi, Phys. Rev. Applied 2, 034003 (2014).
[29] R. Cheng, J. -G. Zhu, and D. Xiao, Phys. Rev. Lett. 117, 097202 (2016).
[30] M. Schreier, Y.-T. Cui, A. Schreier, J. Chiba, A. Niedermayr, J. Lotze, H. Huebl, S. Geprägs, S. Takahashi, G. E. W. Bauer, R. Gross, and S. T. B. Goennenwein, Phys. Rev. B 92, 144411 (2015).
[31] A. Manchon, Physica Status Solidi RRL 11, 1600409 (2017).
[32] I. S. Jacobs, J. Appl. Phys. 32, S61 (1961).
[33] M. Hagiwara, K. Katsumata, H. Yamaguchi, M. Tokunaga, I. Yamada, M. Gross, and P. Goy, Int. J. Infrared Milli. 20, 617 (1999).
[34] M. P. Ross, Diploma thesis (2013).
[35] M. T. Hutchings and E. J. Samuelsen, Phys. Rev. B 6, 3447 (1972).
[36] L. A. Machado, P. R. T. Ribeiro, J. Holanda, R. L.
Rodríguez-Suárez, A. Azevedo, and S. M. Rezende, Phys. Rev. B 95, 104418 (2017).

[37] D. Hou, Z. Qiu, J. Barker, K. Sato, K. Yamamoto, S. Vélez, J. M. Gomez-Perez, L. E. Hueso, F. Casanova, and E. Saitoh, Phys. Rev. Lett. 118, 147202 (2017).

[38] A. Brataas, Y. Tserkovnyak, G. E. W. Bauer, and P. J. Kelly, arXiv:1108.0385v3 (2012).

[39] T. Satoh, S. -J. Cho, R. Iida, T. Shimura, K. Kuroda, H. Ueda, Y. Ueda, B. A. Ivanov, F. Nori, and M. Fiebig, Phys. Rev. Lett. 105 077402 (2010).

[40] M. Weiler, M. Althammer, M. Schreier, J. Lotze, M. Pernpeintner, S. Meyer, H. Huebl, R. Gross, A. Kamra, J. Xiao, Y.-T. Chen, H. J. Jiao, G. E.W. Bauer, and S. T. B. Goennenwein, Phys. Rev. Lett. 111, 176601 (2013).

[41] M. Obstbaum, M. Härtinger, H. G. Bauer, T. Meier, F. Swientek, C. H. Back, and G. Woltersdorf, Phys. Rev. B 89, 060407 (2014).

[42] H. Nakayama, M. Althammer, Y. -T. Chen, K. Uchida, Y. Kajiwara, D. Kikuchi, T. Ohtani, S. Geprägs, M. Opel, S. Takahashi, R. Gross, G. E. W. Bauer, S. T. B. Goennenwein, and E. Saitoh, Phys. Rev. Lett. 110, 206601 (2013).

[43] Y. -T. Chen, S. Takahashi, H. Nakayama, M. Althammer, S. T. B. Goennenwein, E. Saitoh, and G. E. W. Bauer, Phys. Rev. B 87, 144411 (2013).

[44] J. Lotze, H. Huebl, R. Gross, and S. T. B. Goennenwein, Phys. Rev. B 90, 174419 (2014).