First-principles study of electronic, mechanical and optical properties of mixed valence SmB₆

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Abstract. The mechanical and optical properties, electronic structure, and theoretical hardness of mixed valence SmB₆ are calculated from first principles using density functional theory. The calculated results are in excellent agreement with previously reported experiments and theory. The band structures of SmB₆ reveal that this material has the qualities of a semiconductor with a minimum gap. The elastic constants, bulk modulus, shear modulus and Young’s moduli of SmB₆ are obtained. The calculated results indicate that SmB₆ is a brittle material. The calculated theoretical hardness is 24.00 GPa. The optical properties of SmB₆ are discussed in detail. It is shown that SmB₆ absorbs in the near infrared and visible light range. Therefore, SmB₆ has the potential to be used as a heat-absorbing coating in order to shield objects from solar heat radiation.

1. Introduction

Rare earth hexaborides (RB₆) have been widely studied because of their low densities, low thermal expansion coefficients, high melting points, high harnesses, high chemical stabilities, superconductivity capabilities,¹⁻⁴ magnetic properties,⁵⁻⁶ high efficiency thermionic emission abilities⁷⁻¹⁰ narrow band gap semiconductivities,¹¹ and others.¹²⁻¹³ Recently, these materials have been used in transparent heat-insulating windows¹⁴⁻¹⁷ by taking advantage of their strong near-infrared radiation absorption and their high visible light transmittance that arise from the free electron plasmatic behaviors. The unusual properties of rare earth hexaborides are ascribed to the interaction of the 5d and 4f electrons of R with the 2p conduction electrons of B. These interactions seem to play an important role in determining the electrical, optical and mechanical properties of these materials.

The mixed valence compound SmB₆ belongs to a family of extremely hard and stable metal hexaborides. SmB₆ has been well studied because of its topological Kondo insulator properties which have intrigued physicists for many years. There have been significant theoretical and experimental efforts to understand the physical properties of SmB₆. Recent theoretical predictions have suggested that the mixed valence compound SmB₆ exhibits a topological Kondo insulator phase.¹⁸⁻²¹
Researchers have experimentally probed the topological Kondo insulator properties of SmB\textsubscript{6} by performing transport measurements,\textsuperscript{[22-25]} torque magnetometer measurements,\textsuperscript{[26]} neutron measurements,\textsuperscript{[27,28]} various angle-resolved photoemission spectroscopy,\textsuperscript{[29-35]} and scanning tunneling microscopy measurements.\textsuperscript{[36-38]} The mechanical and optical properties of SmB\textsubscript{6} are very important owing to its applications as photoelectric functional material. At present, only a few reports have performed to investigate the mechanical and optical properties for SmB\textsubscript{6} and the results also provided some useful information.\textsuperscript{[16, 17, 39-42]} However, the systematical information of mechanical and optical properties is still lack, which hinders the better understandings and applications of SmB\textsubscript{6}. A systematic compilation of these properties is crucial for further material design and better understanding how to utilize SmB\textsubscript{6}. Therefore, a systematic study of the electronic, mechanical and optical properties of SmB\textsubscript{6} must be performed to provide supplements to these shortages using the present first principles calculations.

In the present work, we investigated the electronic, mechanical and optical properties of SmB\textsubscript{6} using the first-principles calculations. This paper is organized as follows. First, the computational details based on first-principles calculations are depicted. Then, the structural properties, electronic structures, elastic constants, mechanical and optical properties for SmB\textsubscript{6} are presented. Finally, the conclusions of the present work are given.

2. Computational details

SmB\textsubscript{6} is ferromagnetic at low temperatures. Therefore, the spin polarized calculations, including spin-orbit coupling, were performed using density-functional theory (DFT)\textsuperscript{[43]} as implemented in the Cambridge sequential total energy package (CASTEP) code.\textsuperscript{[44]} The Vanderbilt-type ultra-soft pseudopotential was used to describe the interactions between ions and electrons. The exchange-correlation energy was described by a generalized gradient approximation (GGA) of the Pardew-Burke-ERNZERHOF (PBE)\textsuperscript{[45]} parameterization. The ultra-soft pseudo-potentials in this work were performed with 4f\textsuperscript{6}p\textsuperscript{6}s\textsuperscript{2} and 2s\textsuperscript{2}p\textsuperscript{1} valence-electron configurations for Sm and B atoms, respectively. The change of total energy during the optimization was converged to 1\times 10^{-6} \text{ eV} and the forces per atom were reduced to 0.02 \text{ eV/Å}. The Brayden-Fletcher-Goldfarb-Shannon (BFGS) algorithm was applied to relax the crystal structure to reach the ground state where both the cell parameters and the fractional coordinates of the atoms were simultaneously optimized. Brillouin zone (BZ) integrations were performed using Monk horst-Pack\textsuperscript{[46]} k-point meshed. The k point separation in the Brillouin zone of the reciprocal space was 10\times 10\times 10 for SmB\textsubscript{6}. The cut-off energy for plane wave expansions was determined to be 400 \text{ eV}. The separation of the reciprocal space was around 0.01 \text{ Å}^{-1} and the self-consistent field (SCF) tolerance was set to 5.0\times 10^{-7} \text{ eV/atom}. The tolerance for elastic constants was set to within 1.0\times 10^{-6} \text{ eV/atom}, a maximum force within 0.002 \text{ eV/Å}, and a maximum strain amplitude within 0.003 \text{ GPa}.

3. Results and discussion

3.1. Structural properties and elastic constants

At ambient pressure, SmB\textsubscript{6} crystallizes in the cubic CsCl lattice structure and with a P\textsubscript{m}m\textsubscript{3}m space group in which the hexaboride cluster (B\textsubscript{6}) form a three-dimensional network with the octahedral structure. The Sm atom and B\textsubscript{6} octahedron occupy the site of cesium and chlorine, respectively. The crystal structure is shown in Fig. 1. Sm is located at the Wyckoff position 1\textsubscript{a} (0, 0, 0) and the B atoms at the 6f (1/2, 1/2, z) site (Fig. 1a). The boron-framework consists of octahedral B\textsubscript{6} groups joined together as shown in Fig. 1b. The framework has two kinds of boron-boron bonds where B-B\textsubscript{in} is on the edge of the octahedron and B-B\textsubscript{out} is between the octahedral. The B-B\textsubscript{in} distance is larger than the B-B\textsubscript{out} distance in SmB\textsubscript{6}, which shows that the large octahedron keeps a large distance between neighboring Sm atoms.
The crystal structure of SmB₆. (a) Primitive cell and (b) Occupied sites of Sm atoms’–Bin and B–Bout are the inter-octahedral and intra-octahedral boron bond lengths, respectively.

The calculated lattice parameter ($a_0$) and internal parameter ($z$) of SmB₆ are listed in Table 1 along with available experimental and theoretical values. The calculated parameters are slightly larger than the experimental ones due to the inherent nature of the GGA approximation. The results of our calculations are in good agreement with previous experimental and theoretical data.

Table 1. Calculated and experimental structural parameters and the plasma energy ($\omega_p$) of SmB₆

|          | $a_0$(Å) | z     | B-Bin(Å) | B-Bout(Å) | M-B(Å) | $\omega_p$(eV) |
|----------|----------|-------|----------|-----------|--------|---------------|
| Calc.    | 4.1704   | 0.2018| 1.7588   | 1.6831    |        | 1.34          |
|          | 4.133[42]|       |          |           |        |               |
| Expt.    | 4.1346[47]| 0.2018| 1.7438[47]| 1.6688[47]| 3.0381[47]|               |
|          | 4.131[39]|       |          |           |        |               |
|          | 4.133[48]|       |          |           |        |               |

This work.

In order to study the mechanical properties of SmB₆, its Elastic constant $C_{ij}$, bulk modulus $B$, shear modulus $G$, Young’s modulus $E$ and Poisson’s ratio $\sigma$ were calculated. The experimental data from the literature are shown in Table 2. For the cubic crystal, the mechanical stability leads to restrictions on the elastic constants as follows: $C_{44} > 0$, $C_{11} > C_{12}$, $C_{11} + 2C_{12} > 0$. The elastic constant $C_{11}$ represents the elasticity in length while $C_{12}$ and $C_{44}$ are related to the elasticity in shape. Table 2 shows that the elastic constants of SmB₆ satisfy all of these criteria. It is important to note that the calculated elastic properties of SmB₆ agree well with the available experimental data. Unfortunately, to our knowledge, there are no theoretical data in which to compare our elastic constants of SmB₆. Therefore, our results were compared to the experimental and theoretical elastic constants of other hexaborides, such as RB₆ (R=Y, La, Eu and Gd)[49] and MB₆ (M=Ca, Sr and Ba).[50] When comparing to these data, our calculated results are reasonable. From the ratio of $B/G$ and Poisson’s ratio $\sigma$, one can judge whether a material is ductile or brittle. The threshold of $B/G$ and Poisson’s ratio $\sigma$ was found to be around 1.75 and 0.26, respectively. When $B/G > 1.75$ and $\sigma > 0.26$, the material behaves in a ductile manner, whereas it behaves in a brittle manner with values lower than 1.75 and 0.26, respectively. It is obvious from Table 2 that SmB₆ is brittle in nature.
Table 2. Elastic constants $C_{ij}$ (GPa), bulk modulus $B$ (GPa), shear modulus $G$ (GPa), Young’s modulus $E$ (GPa), $B/G$, and Poisson’s ratio $\sigma$ of SmB$_6$

|     | $C_{11}$  | $C_{12}$ | $C_{44}$ | $B$   | $G_V$  | $G_R$  | $G$   | $B/G$ | $E$   | $\sigma$ |
|-----|-----------|----------|----------|-------|--------|--------|-------|-------|-------|----------|
| Calc. | 415.89    | 9.88     | 75.69    | 145.22| 126.61 | 101.03 | 113.82| 1.28  | 415.43| 0.023    |
| Expt. | 465$^{[40]}$ | 29$^{[40]}$ | 56$^{[40]}$ | 174.1$^{[40]}$ |        |        |       |       |       |          |

3.2. Electronic structure, magnetic properties and theoretical hardness

The energy band of the mixed valence compound SmB$_6$ was investigated to compare the exchange interaction. The energy band corresponding to the spin-up and spin-down split apart is due to the exchange coupling between the electrons. The spin energy band structures of SmB$_6$ are show in Fig. 2. The low energy band structures of SmB$_6$ have characteristics of semiconductors in that they have with a minimum gap of about 130 meV along the X-R direction in the majority spins (spin up) states and about 200 meV in the minority spins (spin down) states. The Sm-$4f$ orbitals form narrow bands under the Fermi level in the majority spins (spin up) states. Our calculated energy band structures are in good agreement with results produced by the LDA + Gutzwiller method of Lu et al$^{[51]}$ and with the experimental results from transport and optical measurements which revealed the formation of a small gap only at temperatures under 50 K.$^{[52-54]}$

![Figure 2. The spin energy band structure of SmB$_6$](image)

The origin of the magnetic behaviors of SmB$_6$ was studied by calculating and analyzing the spin-projected total and partial density of states (DOS) for magnetic spin-states (Fig. 3). The spin-projected density of states of SmB$_6$ consists of four parts. The first part of bands consists of Sm $5p$ and B $2s2p$ states (-20 to -12 eV). The second part of bands (-10 to -1 eV) is characterized by B $2p$ states and some amount of Sm $5s5p$ states in order to make the distribution of spin-projected total density of states overall symmetric. It is interesting to note that $4f$ states cross the Fermi energy $E_F$, and hybridize with $5d$ states near the $E_F$, which is consistent with various experimental results.$^{[55-57]}$ The last group of bands (above $E_F$) is mainly made up of Sm $5d4f$ states. The Sm $5d$ band has a higher energy than La $5d$ in the lanthanum hexaboride due to the mixed valence character of SmB$_6$. The bottom of the conduction band and the top of the valence band are mainly formed from hybridized Sm $4f$ states and from B $2p$ states; there is also some amount of Sm $5d$ states and B $2p$ states. Figure 3 shows that orbital polarization is negligible for SmB$_6$. 


Figure 3. Spin-projected densities of states of SmB6

The Mullikan charge and overlap population are useful in evaluating the covalent, ionic, or metallic nature of bonds in a compound. Therefore, the Mullikan charge population for SmB6 was calculated in order to better understand bonding in this compound. The Mullikan population results are given in Table 3. The calculated charge transfer from Sm to B is about 2.29 e. This value indicated that the bonding behaviour in SmB6 is a combination of covalent and ionic. The Mullikan charge populations for SmB6 were also calculated in order to obtain the intrinsic hardness of SmB6 on the basis of Gao’s model.\cite{54} The intrinsic hardness of each chemical bond was calculated using the data in Table 4. Previous work has suggested that the hardness of complex compounds can be expressed as a geometric average of the hardness of all binary systems in the solid. This rule of considering the joint contributions of different bindings was applied to our calculations.\cite{50} The calculated hardness values listed in Table 4 generally agree with previous experimental results.\cite{39}

Table 3. Mullikan charge population of SmB6

| Species | s  | p  | d  | f  | Total Charge (e) |
|---------|----|----|----|----|------------------|
| B       | 0.85 | 2.53 | 0.00 | 0.00 | -0.38            |
| Sm      | 1.81 | 5.17 | 0.81 | 5.92 | 13.71 2.29       |

Table 4. Calculated Mullikan population analysis and hardness (GPa) of SmB6.

| Atom Charge (e) | Bond Population Length (Å) N\(^{\rho}\) Vcell (Å\(^{3}\)) v\(^{\nu}\) H\(^{\mu}\) H | H\(_{\text{Exp.}}\) \(^{[39]}\) |
|-----------------|---------------------------------|-----------------|-----------------|-----------------|----------------|-----------------|-----------------|
| SmB\(_{6}\) Sm\(_{\text{in}}\) | 2.29 | 0.58 | 1.6831 | 3 | 72.53 | 4.49 | 35.12 | 24.00 | 17.8±0.065 |
| B\(_{\text{out}}\) | -0.38 | 0.45 | 1.7587 | 12 | 5.13 | 21.82 |

3.3. Optical properties

The optical properties of a solid material are determined by the frequency-dependent dielectric function \(\varepsilon (\omega) = \varepsilon_1 (\omega) + \varepsilon_2 (\omega)\), which characterizes the linear response of the material to an electromagnetic radiation (e.g., governs the propagation behavior of radiation in a medium). The imaginary part of the dielectric function \(\varepsilon_2 (\omega)\) is calculated from the momentum matrix elements between the occupied and unoccupied electronic states. The real part \(\varepsilon_1 (\omega)\) is derived from the imaginary part \(\varepsilon_2 (\omega)\) by the Kramers-Kronig transformation. All other optical constants, such as
reflectivity, the absorption value, and the electron energy-loss function value are derived from $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$.[58]

The complex dielectric function, reflectivity, the absorption spectrum, and the electron energy-loss function as a function of photon energy are presented in Fig. 4-7. The calculated static dielectric constant $\varepsilon_1(\omega)$ was found to be 36.67. The peaks of the imaginary part of the dielectric function $\varepsilon_2(\omega)$ are related to the electron excitation. These peaks which have a relatively strong intensity are located at 0.47 eV (A), 4.09 eV (B), and 6.98 eV (C). Peak A is ascribed to the transition of the inner electron excitation of Sm 4$f$ states. Peak B and peak Care ascribed to the transition between B 2$p$ states in the valence bands and Sm 5$d$ states in the conduction bands.

![Figure 4. (Color online) Dielectric function of SmB6.](image)

The reflectivity spectra were derived from the calculated dielectric functions for SmB6 and are shown in Fig. 5. The calculated reflectivity was compared to the experimental data from Kimura et al.[59] Evidently, The experimental value shows a large value of reflectivity in the low energy range. Our calculated reflectivity also shows similar characteristics. In addition, the calculated result shows a dip below 1.78 eV in the visible light range. This is in good agreement with the experimental data from Kimura et al. (1.8 eV).[60]

![Figure 5. Reflectivity of SmB6. The dotted line stands for experimental data of SmB6.](image)

By analyzing the transmittance profiles of nanoparticle dispersions of rare-earth hexaborides, Takeda et al. concluded that hexaboride nanoparticles have potential uses as coatings for solar control windows to shield against solar heating. These results inspired us to study the absorption spectrum of SmB6. Fig. 6 shows the calculated absorption spectrum of SmB6. The strong absorption coefficient above $10^4$ cm$^{-1}$ occurs in the near infrared and visible light range because it is a metallic compound. The absorption spectrum has a sharp increase of about 3 eV in the high-energy region. Most significantly, there are no significant absorption peaks in the near infrared and visible light ranges. Therefore, we conclude that SmB6 is a candidate for use in heat-absorbing coatings to shield solar heating.
Figure 6. Absorption spectrum of SmB6.

The electron energy-loss function describes the energy loss of electrons that quickly traverse materials. The peak in the low-loss region characterizes the plasma resonance and the peak position corresponds to the relevant plasma frequency $\omega_p$. Fig. 7 shows the calculated electron energy-loss spectrum. According to Kimura et al., [59] the peak at 1.34 eV is derived from the excitation of the plasmon of the conduction electron. Additionally, the peak at 17.4 eV can be attributed to the excitation of the plasmon of the valence band which consists of the boron 2s and 2p bonding states and the 4f5/2 state of Sm atom. The peak at 28.0 eV shows the transition or excitation from 5p states. By comparing this information with other literature, [16] we conclude that the very weak peak at 1.34 eV, which is the plasma energy $\hbar \omega_p$ of SmB6, shows a plasma resonance in the low-energy scale. This corresponds to an abrupt descent in reflectivity.

Figure 7. Energy-loss spectrum of SmB6.

4. Conclusion
In summary, first-principles calculations were used to investigate the structural parameters, mechanical properties, electronic structure, theoretical hardness and optical properties of SmB6. The band structures of SmB6 showed that this material has properties of a semiconductor (i.e. a minimum gap). The elastic constants, bulk modulus, shear modulus and Young’s moduli of SmB6 were calculated. These results showed that SmB6 is brittle in nature. A theoretical hardness of 24.00 GPa was calculated. Finally, the dielectric function, reflectivity, absorption spectrum and electron energy-loss spectrum were obtained and discussed in detail. Our calculated reflectivity spectrum is in good agreement with the experimental literature. The absorption spectrum of SmB6 shows that it has the potential for use as a heat-absorbing coating in order to shield solar radiation. We hope that our calculated results provide the theoretical data that are necessary for further material design and development of applications of the topological Kondo insulator SmB6.
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