SUPPRESSION OF FIBER MODAL NOISE INDUCED RADIAL VELOCITY ERRORS FOR BRIGHT EMISSION-LINE CALIBRATION SOURCES

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ABSTRACT

Modal noise in optical fibers imposes limits on the signal-to-noise ratio (S/N) and velocity precision achievable with the next generation of astronomical spectrographs. This is an increasingly pressing problem for precision radial velocity spectrographs in the near-infrared (NIR) and optical that require both high stability of the observed line profiles and high S/N. Many of these spectrographs plan to use highly coherent emission-line calibration sources like laser frequency combs and Fabry–Perot etalons to achieve precision sufficient to detect terrestrial-mass planets. These high-precision calibration sources often use single-mode fibers or highly coherent sources. Coupling light from single-mode fibers to multi-mode fibers leads to only a very low number of modes being excited, thereby exacerbating the modal noise measured by the spectrograph. We present a commercial off-the-shelf solution that significantly mitigates modal noise at all optical and NIR wavelengths, and which can be applied to spectrograph calibration systems. Our solution uses an integrating sphere in conjunction with a diffuser that is moved rapidly using electrostrictive polymers, and is generally superior to most tested forms of mechanical fiber agitation. We demonstrate a high level of modal noise reduction with a narrow bandwidth 1550 nm laser. Our relatively inexpensive solution immediately enables spectrographs to take advantage of the innate precision of bright state-of-the-art calibration sources by removing a major source of systematic noise.

Key words: instrumentation: spectrographs -- methods: observational -- techniques: radial velocities -- techniques: spectroscopic

Online-only material: color figures

1. INTRODUCTION

High-resolution fiber-fed spectrographs are being used for demanding astrophysical applications, including the detection of low-mass planets (e.g., Dumusque et al. 2012) using precise radial velocity (RV) measurements. The promise of detecting rocky planets around M dwarfs has led to the development of stabilized high-resolution near-infrared (NIR) spectrographs such as the Habitable Zone Planet Finder (HPF; Mahadevan et al. 2012) and CARMENES (Quirrenbach et al. 2012), while ambitious instruments like ESPRESSO (Mégevand et al. 2012) seek to achieve 10cm s⁻¹ RV precision to find true Earth analogs around G and K stars. These instruments require extremely stable and accurate calibration sources like laser frequency combs and stabilized Fabry–Perot etalons that are now being developed and tested.

The finite number of electromagnetic modes in an optical fiber leads to a form of noise that, if left unmitigated, limits the achievable signal-to-noise ratio (S/N) and adds a source of RV noise. This modal noise is worst with narrow emission-line sources and at longer wavelengths, and can significantly hinder the ability to achieve the high S/N needed to search for biomarkers in the atmosphere of transiting planets (Snellen et al. 2013) in the NIR.

In this paper we experimentally demonstrate a commercially available and easy to implement solution to modal noise that is applicable to calibration sources. This solution is immediately useful to multiple groups attempting to push forward the limits of precision spectroscopy in the optical and NIR. The development of such techniques is closely related to the growing field of astrophotonics (Bland-Hawthorn & Kern 2009).

2. FIBER MODAL NOISE AND ITS IMPACT ON HIGH PRECISION SPECTROSCOPY

The term modal noise refers to a noise source caused by the changing spatial distribution of light at the output end of a fiber. The conditions under which modal noise manifests itself (Rawson et al. 1980) are as follows.

1. A narrow source or observed spectrum.
2. Spatial filtering of the light from the output face of the fiber.
3. Movement, stress, or temperature changes in the fiber, wavelength change in the source, or changes in input illumination that change the distribution of propagating modes.

All three conditions are present in modern fiber-fed astronomical spectrographs to some degree, and lead to a manifestation of modal noise in the recorded spectra (Baudrand & Walker 2001; Grupp 2003). Calibration light input to the spectrograph can be highly coherent and have narrow linewidth (e.g., laser frequency combs). Some spatial filtering is always present in any spectrograph, typically caused either by a slit, spatially dependent grating efficiency, vignetting, variable path length through prisms, or other similar sources. Optical fibers have to connect the spectrograph to the telescope focal plane and will inevitably move and bend as the telescope slews. Temperature changes and stress in the fibers will also cause the output speckle pattern to change, all resulting in effectively limiting the achievable S/N of the observed spectrum.

While the term modal noise traditionally refers to fluctuations in the recorded intensity, the presence of a finite number of speckles is also a source of noise in determining the centroid
Figure 1. (a) Number of modes propagating at each wavelength in step index cylindrical optical fibers of diameter 50 μm, 100 μm, and 300 μm for unpolarized light. For simplicity, we have assumed an input focal ratio of \( f/3.65 \) (NA = 0.1357) in all cases. (b) The maximum achievable S/N with a narrow linewidth source for 100(μm and 300(μm fibers at wavelengths of 400 nm and 1550 nm, chosen to roughly correspond to the limits of wavelengths covered by precision RV spectrographs. \( \rho^2 \) is the fraction of light from the illuminated fiber end incident on the detector.

(A color version of this figure is available in the online journal.)

of an observed emission and absorption line, even with no spatial filtering. Fiber-fed astronomical spectrographs dedicated to high precision RV surveys are affected by the limitation in both the S/N and the RV noise.

We distinguish modal noise from “fiber scrambling” as the term is commonly used in astronomical spectroscopy. The former arises from the result of the finite number of electromagnetic modes excited in optical fibers, and the conditions described above, while the latter refers to the dampening of correlated spatial variations in fiber output when the input illumination varies. Optical double scramblers (Hunter & Ramsey 1992) that interchange the near-field and far-field images between two fibers to provide both radial and azimuthal scrambling are now routinely used for the highest precision spectrographs. Coupling these with non-circular fibers (e.g., octagonal fibers) provides additional radial and azimuthal scrambling, leading to output illumination that is largely decoupled from the input variations, enabling high velocity precision (Bouchy et al. 2013). These techniques do not mitigate modal noise since such scrambling is static and merely redistributes the modes. McCoy et al. (2012) have shown that the use of octagonal fibers does not provide any better modal noise suppression than the use of circular fibers.

Following Goodman & Rawson (1981) and Lemke et al. (2011), the modal noise limited S/N from a fiber is

\[
S/N = \frac{\rho^2}{\nu} \sqrt{\frac{M + 1}{1 - \rho^2}},
\]

where \( \rho^2 \) is the fraction of light from the illuminated fiber end incident on the detector, \( M \) is the number of excited modes in the fiber, and \( \nu \) the visibility of the speckle contrast at the fiber output. For highly coherent narrow linewidth calibration sources it is appropriate to set \( \nu \sim 1 \). For illumination of high-resolution spectrographs by less coherent sources (i.e., starlight), the expected speckle contrast (or visibility) is lower, leading to modal noise being less of a problem, though not negligible. For such sources, Lemke et al. (2011) experimentally derive a visibility \( \nu \) ranging from 0.01 to 0.05. The S/N approaches infinity as \( \rho^2 \) approaches 1, implying that the intensity modal noise is no longer the limiting factor compared to other noise sources like the intrinsic photon noise. In reality \( \rho^2 \) is never unity for any astronomical spectrograph.

The maximum number of modes (for unpolarized light) at a wavelength \( \lambda \) supported by a cylindrical step index fiber of diameter \( d \), and input numerical aperture NA is given by

\[
M = 0.5 \left( \frac{\pi d NA}{\lambda} \right)^2.
\]

Figure 1 shows the number of modes propagating at each wavelength in a 300 μm (HPF), 100 μm (CARMENES), and 50 μm fiber at an input focal ratio of \( f/3.65 \). Most high-resolution instruments operate at input focal ratios between \( f/3.5 \) and \( f/5 \) to avoid significant amounts of focal ratio degradation. Also shown is the corresponding S/N for coherent input illumination (such as that provided by a laser frequency comb), as a function of \( \rho^2 \) for wavelengths of 400 nm and 1550 nm.
As expected, the modal noise is significantly higher for the NIR wavelengths due to the much smaller number of available modes (M) in the fiber. Using a slit or an image slicer leads to a lower ρ^2, thereby increasing modal noise on the recorded spectra. Noise increases even in the case of an ideal (zero-loss) image slicer with an ideal spectrograph. The speckle distribution on the fiber output is constrained by the need to preserve the total intensity (Goodman & Rawson 1981), but no such constraint applies to any of the individual fiber slices.

3. WAVELENGTH CALIBRATION SOURCES

Challenging astrophysical goals push high-resolution spectrographs to use the most precise wavelength calibration sources available. For fiber-fed spectrographs the calibration source sets the wavelength scale and helps continuously monitor the instrument drift. Commonly used atomic emission-line lamps like thorium–argon and uranium–neon (Redman et al. 2011) provide a large number of stable emission lines across the UV–NIR range.

Laser frequency combs offer significant calibration advantages in astronomical spectroscopy (Murphy et al. 2007; Braje et al. 2008). Such combs are now being built and tested both with optical (Lo Curto et al. 2012) and NIR (Osterman et al. 2012) spectrographs, and can lead to significant improvements in RV precision. The intrinsic linewidths of each of these laser comb lines is typically ~300–800 kHz (Quinlan et al. 2010; Ycas et al. 2012a) making them extremely coherent narrow-band sources, and therefore subject to significant modal noise. An added complication with these devices is that the light is output in a single-mode fiber (SMF hereafter). Coupling of the SMF to a multi-mode fiber excites only a small number of modes in the multi-mode fiber, further exacerbating the impact of modal noise. The problem can be mitigated by agitating the optical fiber (Baudrand & Walker 2001). While this has been done at the shorter optical wavelengths, with good results, systematic noise and velocity error has been reported at longer wavelengths (Phillips et al. 2012a, 2012b). Tests with the Pathfinder spectrograph and a laser comb in the NIR H band (1.5–1.7 μm) were limited by modal noise even with the use of an integrating sphere and a high frequency fiber agitator (Ycas et al. 2012b; Redman et al. 2012).

Many groups are also pursuing the development of calibration sources based on Fabry–Perot etalons (Wildi et al. 2012; Halverson et al. 2014). While lacking the level of stability and frequency traceability of a comb, these sources can be stabilized at a high level, at least in the short term, enabling the spectrograph drift to be monitored at high precision. The linewidths from these devices range from 0.1–1 GHz, still less than the resolution element of the spectrographs. The speckle visibility ν is still very high, and modal noise remains a significant problem.

4. DYNAMIC MODAL NOISE MITIGATION

McCoy et al. (2012) have discussed the mitigation of modal noise by fiber agitation. In the NIR, bulk agitation of fibers is necessary, even with the use of an integrating sphere, and a specific form of high amplitude low frequency hand agitation performs better than currently tested forms of mechanical agitation. While more sophisticated mechanical agitators will eventually solve this problem, these devices are harsh on the optical fibers and may reduce their lifetime. In addition a source of high level of vibrations near, or coupled to, a stabilized spectrograph is undesirable. This lead us to explore dynamic diffusers that rapidly change the input modal pattern, thereby effectively randomizing the output mode pattern.

Our experiments achieve a high level of modal noise mitigation with a commercially available dynamical diffuser, which is an Optotune”4 Laser Speckle Reducer (Blum et al. 2012). These devices consist of a diffusive surface attached to electroactive polymers that are used as actuators to rapidly move the diffuser. Voltage applied across the actuators leads to a squeezing of the elastic polymer film, causing them to expand laterally and move the attached diffuser. This can be done very rapidly (180–300 Hz), causing rapid changes in the output speckle pattern. Commercially available diffusers have a surface relief structure that is tuned to the required performance, such as angle of diffusion, shape of the diffused beam, etc. In general a larger diffusion angle requires smaller diffuser structures. The changes in the output pattern can further be randomized by the use of an integrating sphere. The key concept here is that while an integrating sphere alone randomizes the output modal distribution, that randomization is static, leaving one still susceptible to modal noise in the fibers. A combination of a dynamic diffuser and integrating sphere yields dramatic reductions in modal noise.

We purchased an Optotune Laser Speckle Reducer with a specified diffusion angle of 20° and a 10 mm clear aperture. For our experiment we used a 1550 nm laser with a specified linewidth of <10 MHz, which is expected to lead to a high speckle contrast (ν = 1). Working at 1550 nm also ensures we are probing modal noise at long wavelength, where it is expected to be worse. We use a single-mode fiber (SMF28) to couple the laser light through the diffuser and into a 4 inch diameter integrating sphere, and use a Polymicro 200 μm core fiber on the output fiber port of the integrating sphere. The integrating sphere was purchased from SphereOptics,5 and is the same sphere used in on-sky demonstrations of a laser frequency comb described in Ycas et al. (2012b). The sphere is manufactured using a proprietary form of Teflon that approaches ideal Lambertian behavior and provides a diffuse reflectance value of 98% across the visible and infrared. The output of the fiber is re-imaged onto a Xenics InGaAs NIR camera that records the speckle pattern. The choice of the 200 μm fiber was driven by availability as well as the fact that the number of modes propagating in this fiber, when fed at its maximum numerical aperture (NA = 0.22) by the integrating sphere, is quite similar to that propagating in a 300 μm fiber-fed at f/3.65 (which is the planned fiber for the HPF spectrograph).

Figure 2 shows a sketch of the experimental setup as well as an inset image of the diffuser. The experimental setup allows use of the diffuser with and without the dynamical motion, removal of the diffuser, and the integration of a mechanical agitator that is an improved version of one we described in McCoy et al. (2012).

As part of our experiment we obtained short integration time (3 s) images of the modal pattern from the output fiber for the following five different tests.

1. Direct injection of the light from the SMF fiber to the multi-mode fiber.
2. SMF coupled directly to the integrating sphere, and mechanical agitation of the multi-mode fiber.

4 http://www.optotune.com/
5 http://www.sphereoptics.de
3. SMF coupled to integrating sphere through the diffuser, but no diffuser motion (static diffuser).
4. SMF coupled directly to the integrating sphere, and hand agitation of the multi-mode fiber.
5. SMF coupled to integrating sphere through the diffuser, with diffuser actuated motion (dynamic diffuser).

These images are shown in Figure 3. As can be seen visually, the dynamic diffuser or manual hand agitation leads to a significant reduction in speckle contrast compared to other cases. Figure 4 plots the azimuthally averaged power spectrum of the images, showing the significant reduction in the intensity at intermediate and high spatial frequencies. Figures 3 and 4 both show the impact of fringing in the experimental setup, likely from the detector window, which does not impact the results. The theoretical floor is set by a smooth fit to the power spectrum of the synthetic image (Figure 3(f)). The dynamic diffuser performs extremely well approaching this floor. A specific form of hand agitation at $\sim$1–2 Hz with a $\sim$10 cm fiber bend is also able to approach these levels, but is not highly repeatable and not a practical alternative for a long-term RV survey. Based on these results, we are confident that the use of dynamic diffusers effectively removes any systematic-based S/N limitation on high-resolution spectroscopy even with highly coherent narrow line sources in the NIR $H$ band, corresponding to a worst case manifestation of modal noise. It follows that the problem is also effectively solved for any shorter wavelengths and for less coherent calibration sources.

The solution can be applied to any calibration source, but with a significant light loss penalty. While the diffuser transmits 60%–70% of the light, the integrating sphere is typically very lossy. In our experiments the total efficiency of the system is $\sim$10$^{-6}$, driven largely by the integrating sphere. This is not necessarily a problem. Laser combs and Fabry–Perot cavities fed by supercontinuum sources are often very bright, enabling sufficient photons to be recorded by the spectrograph even with the losses from the integrating sphere.

Typical NIR laser frequency combs now under development can conservatively output $\sim$1–10 nW per individual comb mode. Factoring in losses from the integrating sphere, this roughly corresponds to 5000–50,000 photons s$^{-1}$ at 1 $\mu$m entering the spectrograph calibration fiber. As typical astronomical exposures are on the order of minutes, we expect the comb will have no difficulty achieving adequate S/N in our modal noise mitigation system during typical science exposures. Previous on-sky uses of an NIR “astro-comb” required a series of neutral density filters to prevent saturation during short exposures, even when coupling though the very same integrating sphere into a lossy testbed spectrograph (Ycas et al. 2012b).

Exceptions, perhaps, are the U–Ne or Th–Ar lamps. If efficiency is indeed an issue then the diffuser can be used alone, with a converging lens focusing on the multi-mode fiber. This configuration is significantly less lossy than using an integrating sphere (we achieve a total efficiency of $2 \times 10^{-3}$) with modal noise mitigation exceeding the mechanical agitation case, but inferior to using both the dynamic diffuser and integrating sphere, though it may be sufficient for many applications.

5. RADIAL VELOCITIES AND MODAL NOISE

Modal noise severely limited our RV precision during tests with a NIR laser comb calibrator (Ycas et al. 2012b;
Redman et al. 2012), and we must eliminate this noise source as we develop the new generation of stabilized NIR spectrographs. The changing speckle pattern on the fiber output manifests itself as a change in the centroid position (an RV change) of the line since each speckle maps to a slightly different wavelength position in the dispersion direction.

While we have shown that the dynamical diffuser significantly reduces the higher spatial frequencies in an image of the fiber output, it is instructive to perform an experiment to explicitly map the modal noise to achievable velocity precision.

We simulate the RV impact by acquiring a number of 3 s exposures using the 1550 nm laser, the Optotune diffuser, integrating sphere, and an unagitated 200 μm fiber coupled to the integrating sphere. Image sets were acquired with the diffuser in the static and dynamic mode. Between each set of exposures the fiber bend radius and positions were changed using our mechanical scrambler, and the resulting mode pattern was allowed to settle. No mechanical agitation was present during the exposures themselves.

We use these images to simulate the case of the HPF spectrograph baseline (Mahadevan et al. 2012), a 300 μm
fiber-fed at $f/3.65$ with a 100 $\mu$m slit at spectrograph input. The 200 $\mu$m fiber-fed at NA = 0.22 has roughly the same number of modes as a 300 $\mu$m fiber-fed at $f/3.65$. We impose a scaled digital slit on each of the recorded images and calculate the change in the centroid position in the dispersion direction. We use the expected resolution of the HPF spectrograph ($R \sim 50,000$) to translate this centroid shift into a velocity shift. Figure 5 shows the digital slit used for these calculations, as well as the resulting RV scatter for the case of the static and dynamic diffuser. The results corroborate our experience (Ycas et al. 2012b; Redman et al. 2012) and show that modal noise is indeed a serious problem, leading to an RV scatter of
20 m s$^{-1}$ even with the use of an integrating sphere and the static diffuser. The dynamic diffuser significantly reduces this, yielding an RV scatter of only 1.3 m s$^{-1}$. To probe the measurement precision of our setup in the absence of modal noise we replace the input SMF with a multi-mode fiber illuminated by a continuum source. Figure 5 (bottom) shows that our experimental precision is 0.3 m s$^{-1}$. The 1.3 m s$^{-1}$ measurement is likely subject to other systematics (detector inhomogeneities, pixel quantum efficiency variability, flat fielding, etc.) as well as the stability of the experimental setup and not necessarily the performance floor for the diffuser. This measurement also corresponds to the centroid precision of only one line on the spectrograph focal plane. Assuming 30–50 such emission lines across a typical echelle order yields a modal noise limited wave-length solution error of less than 15–20 cm s$^{-1}$. The use of the dynamical diffuser will therefore enable high precision RVs to be acquired even with narrow emission-line sources.

6. DISCUSSION

We have demonstrated a commercial off-the-shelf solution to the fiber modal noise problem that has previously limited the use of narrow emission-line calibration sources with high-resolution astronomical spectrographs. Our solution uses a dynamic diffuser (Blum et al. 2012) and integrating sphere to randomize the modes. The dynamical diffuser changes the mode distribution at a timescale much shorter than the typical spectrograph exposure, and the integrating sphere further randomizes this distribution. Our solution is also quite general in that any combination of a dynamic mode re-distributor and a mode mixer will help mitigate modal noise, though not necessarily as well as the setup we present. For example a Galvano scanner may be used as a replacement to the dynamic diffuser in conjunction with an integrating sphere. Experiments coupling light from the diffuser directly to a multi-mode fiber achieve a total light throughput of $\sim$0.2%, with modal noise mitigation exceeding the mechanical agitation case. Such solutions are useful with calibration sources like Th–Ar and U–Ne where minimizing light loss becomes important.

The commercial Optotune diffuser is made of polycarbonate and has shallow absorption bands at certain wavelengths ($\sim$1180 nm and 1400 nm). It is possible to create custom-engineered diffusers made of glass or fused silica (Sales et al. 2006) that do not exhibit such absorption. Lightweight diffusers can be agitated with the electroactive polymers, while heavier diffusers can utilize a rotating mount, albeit at lower frequencies.

While light loss with the use of an integrating sphere makes it impractical to use with starlight, modal noise is less problematic in this case due to lower visibility ($\nu$). Some modal mixing may be accomplished with custom diffusers between two fibers, but requires very small diffusion angles to minimize light loss and focal ratio degradation. While exploration of such techniques may be fruitful, our opinion is that the star fiber modal noise is likely best addressed with a small amount of gentle agitation (Baudrand & Walker 2001; Plavchan et al. 2013), while a solution to the calibration fiber modal noise problem is presented in this paper for all optical and NIR wavelengths.

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6 Optotune Data Sheet: http://www.optotune.com/images/products/Optotune%20LSR-3000%20Series.pdf