Detection of crack in structure using dynamic analysis and artificial neural network

Manisha Maurya*, Jatin Sadarang* and Isham Panigrahi*

*School of Mechanical Engineering, KIIT deemed to be UNIVERSITY, Bhubaneswar, India

ABSTRACT

Cracks are one of the main causes of structural failure and they develop in the structures due to various reasons such as fatigue, temperature variation, excessive load, cyclic load, environmental effects, impact loading etc. Thus, structural health monitoring is necessary to avoid risks, damages and failures. So, in order to avoid an extensive failure or accident, the early prognosis of crack in structures is necessary. Visual inspection and some non-destructive testing (NDT) methods for detection of crack are difficult as it requires time, expenses and are quite inefficient. So the alternative methods are motivated to be developed. In this study, vibration analysis, finite element analysis (FEA) and an alternative way which is artificial neural network (ANN) is used to predict, detect and identify the damages in structures. It is found that the theoretical, experimental, finite element analysis and artificial neural network have good accuracy in predicting the crack characteristics.

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1. Introduction

Crack is a discontinuity in a body and is one of the main causes of structural failure and there are many research studies for crack and defect detection or characterizing the mechanical property and cracking behavior, remaining life, final load bearing capacity of cracked components and engineering materials (Scholey et al., 2009; Taheri-Bebrooz et al., 2018; Wang et al., 2016,2017; Rossi & Le Maou, 1989; Aliha & Gharehbaghi, 2017; Scholey et al., 2009; Abd-Elhady, 2013; Mahdavi et al., 2015; Fayed, 2018; Akbarodoost, 2014; Akbarodoost et al., 2014; Mirdsayar et al., 2017, 2018; Mirdsayar & Zollinger, 2017; Carpinteri & Ingraffea, 2012; Frommherz et al., 2016; Aliha et al., 2012, 2017a,b, 2016; Ayatollahi & Aliha 2011; Abd-Elhady, 2013; Mahdavi et al., 2015). Cracks are developed in the structures and machines due to various reasons such as fatigue, temperature variation, excessive load, cyclic load, environmental effects, impact loading, shear failure, resonance, wear corrosion, residual stress and etc. The presence of crack not only affects the stiffness of the structure but also affect the mechanical response of the whole structure to a larger extent (Prabhakar, 2009). Due to these changes, there is a reduction in modal frequencies and mode shapes. Therefore, it is feasible to anticipate the crack characteristics by determining changes in the vibration parameters (Vakil-Baghmisheh et al., 2008). Its development in a beam leads to sudden failure of a system and machines without any prior indication or warning (Satpute et al., 2017).
Visual inspection of cracks and damages is unsuitable and not worth considering in most of the cases, thus non-destructive testing (NDT) methods like thermography, ultrasonic testing, X-ray diffraction etc. are used to predict damage in the structures. But these methods require time and expenses and are quite inefficient. So the other possible methods are motivated to be developed (Sutar et al. 2015). In this analogy the use of mathematical methods, vibration-based methods, and soft-computing techniques such as artificial neural network (a subfield of artificial intelligence) is promising and favorable.

Artificial neural networks (ANN) are mathematical model of human nerve system. Its structure is exactly identical to the biological form of the cells in human brain. It consists of a number of layers like input, hidden and output layers. The various neurons are present in each layer. The neurons in input layer represent the raw data which are fed to the system. The hidden layer is connected to the input and output layer through some weights. The neurons available in output layer represents the result of the data provided which can be represented as,

\[ Y = f \left( \sum_{i=1}^{n} a_i w_i + b \right) \]

where, \( b \) = bias, \( w_i \) = weight associated with the \( i^{th} \) input, \( a_i \) = input value and \( Y \) = output of the neuron. The competence of artificial neural networks was studied by Dimarogonas (1996) for prediction of damages in structural members and rotating machinery elements. Nasiri et al. (2017) presented a review paper on the utilization of Artificial Intelligence (AI) methods for mechanical fault detection and discussed the applications of Bayesian networks, GA (genetic algorithms), fuzzy logics, case-based reasoning and ANN i.e. artificial neural networks. The behavior of the undamaged and cracked beam is compared according to the FEA results and it was found that natural frequency of transverse vibrations can be used to detect a crack in cantilever beam by Satpute et al. (2017). Sutar et al. (2015) investigated transverse crack in cantilever beam by proposing a neural network based controller. Crack stiffness to beam elemental stiffness matrix was used to obtain a homogenous linear elastic beam finite element by Teidj et al. (2016) and used the measurement of the changes in the beam frequencies and observed their variations to detect the crack defect characteristics. Thatoi et al. (2014) described the Cascade Forward Back Propagation (CFBP) network to detect cracks in structural beams with the idea of changes in the natural frequencies and their measurements. Pan et al. (2010) developed a two-stage approach combining of artificial neural network (ANN) and genetic algorithm (GA) to identify crack characteristics. The use of power series technique (PST) and ANN was analyzed by Rosales et al. (2009) for crack detection in structural beam who concluded that by the use of PST algorithm, the crack can be detected with very less errors and low cost but limits its use to simple problems like economical detection while on the other hand by the use of the ANN model, cracks with large errors can be detected and can be used for complex problems like large deformations or nonlinearities. A continuous approach for prediction of damages in beams through time-modal characteristics and artificial neural networks was presented by Park et al. (2009). Firstly, an acceleration-based neural networks (ABNN) algorithm is modeled to examine the development of crack. Secondly, a modal feature-based neural networks (MBNN) algorithm is made to detect the crack characteristics. Li et al. (2005) used a collaboration of changes in natural frequencies and strain mode shapes as input parameters in neural network for prediction of crack depth and its location in structural beams. A cantilever beam having transverse crack was used by Suresh et al. (2004) and computed the modal frequencies analytically for various crack depth and locations. These frequencies were taken as inputs to train a neural network using a modular approach with two type of architecture, specifically the multi-layer perceptron (MLP) network and radial basis function (RBF) network. Sahin & Shenoi (2003) presented an algorithm for damage detection using a collaboration of changes in natural frequencies as input parameter to the network. To check the robustness of the input data, they numerically generated a simulated arbitrary noise and added to the noise free data during training of the network. Tan et al. (2017) used the technique based on vibration, where only the first vibration mode was used to predict crack characteristics in steel beams. The modal strain energy based damage index \( \beta \) was used which is competent to detect, locate and quantify the damage. The Two-
Parameter Model (TPM) was used by Ince (2004) to model fracture in cementitious material with back propagation ANN. He summarized the use of ANN in concrete fracture problems and observed that there is no use to make material parameters assumptions as ANN directly uses the experimental values for training and testing.

2. Theoretical analysis

The Euler’s Bernoulli beam equations are used to determine the first three natural frequency of the undamaged specimen.

For mode 1:

\[ \omega_{nf1} = 1.875^{\frac{Eh^2}{12\rho L^4}} \]  

(2)

For mode 2:

\[ \omega_{nf2} = 4.694^{\frac{Eh^2}{12\rho L^4}} \]  

(3)

For mode 3:

\[ \omega_{nf3} = 7.855^{\frac{Eh^2}{12\rho L^4}} \]  

(4)

where Eq. (2) to Eq. (3) are the corresponding modes of natural frequency (rad/sec) for mode 1, mode 2 and mode 3, respectively. Also, \( E \) = Young's Modulus of elasticity, \( h \) = Thickness of specimen, \( \rho \) = Density of the specimen \( L \) = Length of the specimen, \( \omega_{nf1} = 1/2\pi \) \( f_n1 \).

From the Euler formula, the natural frequency is given in radian per second to obtain it in Hz, it divided by 2\( \pi \). The modulus of the steel beam specimen is 167.439 x 10^9 Pa and density is 8169.69 kg/m^3. The thickness of steel beam is 5mm, total length is 330 mm and gage length is 300 mm. 30mm of the beam was fixed at one end of the specimen such that it behaves like a cantilever beam. From the Euler’s equation the first modal natural frequency of beam specimen is 40.624 Hz, second modal natural frequency is 254.606 Hz and third modal natural frequency is 712.975 Hz.

3. Experimental analysis through tap test

In this paper, a single cracked cantilever beam specimen as shown in Fig. 1 has been taken of following dimensions and material: Total length of beam, \( L = 330 \) mm, gage length, \( l = 300 \) mm, breadth, \( W = 25 \) mm, thickness, \( t = 5 \) mm and material is the mild steel.

![Fig. 1. Single cracked cantilever beam specimen.](image)

Tap test was performed to obtain first three modal natural frequencies. Six single cracked cantilever beam specimen are taken and tap test was performed using these beams. In the experiment several crack locations from the fixed end were given in the beam. Tap test is a method used to determine the natural frequency of the beam structures. This setup as shown in Fig. 2 involved the use of a clamp (to fix the mild steel beam as a cantilever), accelerometer (PCB 353B33), connecting cables, FFT analyzer (OROS OR34- 4 channels compact analyzer) and a laptop (with FFT analyzer software NV GATE).
The one end of the specimen was fixed as a cantilever beam on to the clamp, keeping a length of 300 mm of the beam to hang freely and 30 mm of the part was clamped. An accelerometer was mounted at the fixed end to obtain natural frequencies. The accelerometer data reader collects vibration acceleration data and shows it in the software. In this test, the cantilever beam was given a downward displacement of 20 mm and then released such that it vibrates freely and gets damped to its own. The corresponding vibration data was taken from the NV Gate software installed in the laptop. Readings were taken out for both damaged and undamaged beam specimens. The line diagram of the setup is also shown in Fig. 3. Here, six cracked beam as shown in Fig. 4 is taken with crack depth of 1 mm, 2 mm, 3 mm and 4 mm at various crack locations from the fixed end.
The experimental data i.e. first three natural frequencies of undamaged and damaged beam at depth of 1mm, 2mm, 3mm and 4 mm at different locations obtained through tap test are given in Table 1. The frequencies of undamaged beam are as follows \( F_1 = 41\) Hz, \( F_2 = 256.64\) Hz and \( F_3 = 717.62\) Hz.

**Table 1. Experimental results of cracked beam**

| Serial No. | \( F_1\) (Hz) | \( F_2\) (Hz) | \( F_3\) (Hz) | cd (a/t) | cl (from fixed end) (b/l) |
|------------|----------------|----------------|----------------|----------|--------------------------|
| 1          | 40.234         | 249.219        | 695.313        | 1        | 1                        |
| 2          | 38.281         | 242.969        | 683.594        | 2        | 1                        |
| 3          | 36.718         | 245.703        | 687.69         | 3        | 1                        |
| 4          | 33.943         | 224.219        | 633.359        | 4        | 1                        |
| 5          | 35.937         | 238.672        | 693.45         | 3        | 45                       |
| 6          | 37.5           | 220.313        | 674.609        | 3        | 150                      |
| 7          | 41.012         | 254.297        | 664.063        | 3        | 225                      |

The frequency versus acceleration graph of crack depth of 1 mm, 2 mm, 3 mm and 4 mm at fixed end and 3mm at mid, quarter and fixed quarter is shown in Fig. 5 (a,b,c,d).

**Fig. 5(a).** Frequency Vs acceleration graph of crack depth 1mm & 2mm at fixed end

**Fig. 5(b).** Frequency Vs acceleration graph of crack depth 3mm & 4mm at fixed end
4. Finite element analysis

ANSYS is used to determine the first three modal natural frequencies of undamaged and cracked beam specimen. In model module, the material property of the specimen is given and the geometry is created of dimension of 300 mm length, 30 mm width and 5 mm thickness for undamaged specimen. The geometry of cracked specimen is same as the undamaged specimen having a crack of given depth at required locations. The thickness of crack is 0.5 mm for all cracks of depth 1 mm, 2 mm, 3 mm and 4 mm. The brick elements are used to mesh the beam. Fine mesh is used in which total numbers of elements is 1800 and numbers of node is 10777. One end face of the beam specimen is fixed so that the beam behaves like a cantilever beam. Then three model natural frequencies is obtained. The first modal natural frequency of the undamaged beam specimen is 41 Hz, second model natural frequency is 255.45 Hz and third model natural frequency is 714.11 Hz.
The following Table 2 gives the FEA results i.e. first three natural frequencies and Fig. 6 shows the first three mode shapes of undamaged beam and Fig. 7(a, b, c, d) shows the mode shapes of cracked beam.

**Table 2. FEA results of cracked beam**

| Serial No. | F₁ (Hz) | F₂ (Hz) | F₃ (Hz) | cd | cl (from fixed end) |
|------------|---------|---------|---------|----|--------------------|
| 1.         | 40.32   | 252.46  | 706.21  | 1  | 1                  |
| 2.         | 39.015  | 245.14  | 687.54  | 2  | 1                  |
| 3.         | 37.199  | 236.22  | 667.42  | 3  | 1                  |
| 4.         | 33.01   | 219.87  | 637.72  | 4  | 1                  |
| 5.         | 37.627  | 253.16  | 714.75  | 3  | 45                 |
| 6.         | 40.032  | 235.30  | 715.70  | 3  | 150                |
| 7.         | 40.937  | 254.64  | 696.60  | 3  | 225                |

![Fig. 6. Mode shapes of undamaged beam](image1)

![Fig. 7(a). Mode shapes of cracked beam](image2)
Fig. 7(b). Mode shapes of cracked beam

Fig. 7(c). Mode shapes of cracked beam

Fig. 7(d). Mode shapes of cracked beam
4.1 Comparison between experimental and FEA results

The first three modal natural frequencies of beam with crack of depth of 1 mm, 2 mm, 3 mm and 4 mm at different locations are obtained from both the experimental and finite element method. The natural frequencies obtained from both the experimental and FEA methods are compared as given in Table 3.

| Serial No. | F1 (EXPT) | F1 (FEA) | Error % w.r.t Expt. | F2 (EXPT) | F2 (FEA) | Error % w.r.t Expt. | F3 (EXPT) | F3 (FEA) | Error % w.r.t Expt. |
|------------|-----------|----------|----------------------|-----------|----------|----------------------|-----------|----------|----------------------|
| 1.         | 40.234    | 40.32    | **0.213**            | 249.219   | 252.46   | **1.3**              | 695.313   | 706.21   | **1.567**            |
| 2.         | 38.281    | 39.015   | **1.917**            | 242.969   | 245.14   | **0.893**            | 683.594   | 687.54   | **0.577**            |
| 3.         | 36.718    | 37.199   | **1.309**            | 245.703   | 236.22   | **3.859**            | 687.69    | 667.42   | **2.947**            |
| 4.         | 33.943    | 33.01    | **2.748**            | 224.219   | 219.87   | **1.939**            | 633.359   | 637.72   | **0.688**            |
| 5.         | 35.937    | 37.627   | **4.702**            | 238.672   | 253.16   | **6.07**             | 693.45    | 714.75   | **3.071**            |
| 6.         | 37.5      | 40.032   | **6.752**            | 220.313   | 235.3    | **6.802**            | 674.609   | 715.7    | **6.091**            |
| 7.         | 41.012    | 40.937   | **0.182**            | 254.297   | 254.64   | **0.134**            | 664.063   | 696.6    | **4.899**            |

From the above Table 3, it is found that the maximum error percentage between the experimental and finite element analysis results is less than 7% and average error percentage for first, second and third natural frequencies are 2.54, 2.99 and 2.83 respectively. Thus, it can be seen that the experimental data are very close to the finite element analysis values hence for further prediction of crack in neural network; we can obtain the analytical values of natural frequencies at various depth and location and use it for training in neural network. This involves simplicity and less time for evaluation of natural frequencies as compared to experimental method.

4.2 Other FEA data

In ANSYS, natural frequencies of beam with crack depth of 1mm, 2mm, 3mm and 4mm at every 25mm from fixed location for each depth has been obtained using modal analysis. The input and output variables have to be normalized such that it should lie in the same range group of 0 to 1. Therefore the relative values are obtained according to the equations given below:

- Relative frequency (f1, f2, f3) = frequency of cracked beam / frequency of undamaged beam
- Relative crack depth, cd = a / t = depth of crack / thickness of the beam
- Relative crack location, cl = b / l = location of crack from fixed end / length of the beam

The Table 4 gives the relative natural frequencies at desired relative depth and location. These data are used in neural networking for prediction of crack.

5. Neural network modeling

Artificial neural networking (ANN) in MATLAB is used to analyze and predict the depth and position of crack in the beam and data obtained by training is validated by the analytical results. The data given in Table 3.9 are used for training in neural network except data number 3, 8, 13, 19, 25, 31, 37, 43, 49 and 52 which are used for testing the network as 80% of the data are for training ad 20% are for testing the networks. In MATLAB, the desired inputs and outputs or targets are imported in the workspace and using “nntool” network is created using inputs and targets. Here, a typical three-layered Cascade-Forward Back Propagation (CFBP) neural network is considered consisting of three neurons in input layer, nine neurons in hidden layer and two neurons in output layer as shown in Fig. 8 and architecture is shown in Fig. 9.
Table 4. Relative natural frequencies at given depth and location

| Serial No. | f₁ | f₂ | f₃ | cd  | cl  |
|------------|----|----|----|-----|-----|
| 1.         | 0.983561 | 0.9837126 | 0.9841002 | 0.2 | 0.0033 |
| 2.         | 0.9877561 | 0.9936097 | 0.9969482 | 0.2 | 0.0833 |
| 3.         | 0.9986342 | 0.9970776 | 0.9966695 | 0.2 | 0.1666 |
| 4.         | 0.9919268 | 0.99774 | 0.9929628 | 0.2 | 0.25 |
| 5.         | 0.9939024 | 0.9955969 | 0.9917784 | 0.2 | 0.3333 |
| 6.         | 0.9956342 | 0.9934149 | 0.9952761 | 0.2 | 0.4166 |
| 7.         | 0.9963171 | 0.9902977 | 0.9969761 | 0.2 | 0.5 |
| 8.         | 0.9971951 | 0.9913887 | 0.9943842 | 0.2 | 0.5833 |
| 9.         | 0.9978537 | 0.9929084 | 0.9904546 | 0.2 | 0.6666 |
| 10.        | 0.9980976 | 0.9950514 | 0.9898136 | 0.2 | 0.75 |
| 11.        | 0.9982195 | 0.9967269 | 0.9933112 | 0.2 | 0.8333 |
| 12.        | 0.9983659 | 0.9973893 | 0.9960564 | 0.2 | 0.9166 |
| 13.        | 0.9986342 | 0.9983635 | 0.9974499 | 0.2 | 0.9966 |
| 14.        | 0.9515854 | 0.9551901 | 0.9580837 | 0.4 | 0.0033 |
| 15.        | 0.9502927 | 0.9757637 | 0.988852 | 0.4 | 0.0833 |
| 16.        | 0.9685366 | 0.9952073 | 0.9956244 | 0.4 | 0.1666 |
| 17.        | 0.9748049 | 0.9974283 | 0.9810763 | 0.4 | 0.25 |
| 18.        | 0.9829268 | 0.9896743 | 0.9786935 | 0.4 | 0.3333 |
| 19.        | 0.9868049 | 0.9744392 | 0.9888938 | 0.4 | 0.4166 |
| 20.        | 0.9911463 | 0.9692716 | 0.9977704 | 0.4 | 0.5 |
| 21.        | 0.9945122 | 0.969841 | 0.9860372 | 0.4 | 0.5833 |
| 22.        | 0.9971463 | 0.9820371 | 0.9747499 | 0.4 | 0.6666 |
| 23.        | 0.9982927 | 0.9883494 | 0.9703604 | 0.4 | 0.75 |
| 24.        | 0.9988537 | 0.9961425 | 0.986843 | 0.4 | 0.8333 |
| 25.        | 0.9990732 | 0.9982466 | 0.9964048 | 0.4 | 0.9166 |
| 26.        | 0.9985854 | 0.9981686 | 0.9958892 | 0.4 | 0.9966 |
| 27.        | 0.9072927 | 0.9204333 | 0.9300465 | 0.6 | 0.0033 |
| 28.        | 0.884 | 0.9495402 | 0.9803099 | 0.6 | 0.0833 |
| 29.        | 0.8984634 | 0.9897132 | 0.9909283 | 0.6 | 0.1666 |
| 30.        | 0.9368829 | 0.9959476 | 0.955868 | 0.6 | 0.25 |
| 31.        | 0.9462683 | 0.96988 | 0.9384911 | 0.6 | 0.3333 |
| 32.        | 0.965561 | 0.9421758 | 0.975363 | 0.6 | 0.4166 |
| 33.        | 0.9756829 | 0.9134975 | 0.9976868 | 0.6 | 0.5 |
| 34.        | 0.9874878 | 0.9215243 | 0.9677267 | 0.6 | 0.5833 |
| 35.        | 0.9929024 | 0.9315383 | 0.9162927 | 0.6 | 0.6666 |
| 36.        | 0.9972683 | 0.9679707 | 0.9190937 | 0.6 | 0.75 |
| 37.        | 0.9990732 | 0.9907263 | 0.9582091 | 0.6 | 0.8333 |
| 38.        | 0.9996098 | 0.9982855 | 0.9941195 | 0.6 | 0.9166 |
| 39.        | 1.0002439 | 1.0009352 | 0.9994983 | 0.6 | 0.9966 |
| 40.        | 0.805122 | 0.8567254 | 0.8858727 | 0.8 | 0.0033 |
| 41.        | 0.669561 | 0.8892612 | 0.9618182 | 0.8 | 0.0833 |
| 42.        | 0.7276098 | 0.979855 | 0.9801984 | 0.8 | 0.1666 |
| 43.        | 0.8285854 | 0.9922459 | 0.8904016 | 0.8 | 0.25 |
| 44.        | 0.8213659 | 0.9134585 | 0.8500181 | 0.8 | 0.3333 |
| 45.        | 0.8743415 | 0.826956 | 0.934882 | 0.8 | 0.4166 |
| 46.        | 0.9208537 | 0.7783276 | 0.9976868 | 0.8 | 0.5 |
| 47.        | 0.9527317 | 0.78012 | 0.9201249 | 0.8 | 0.5833 |
| 48.        | 0.9804146 | 0.8184227 | 0.827764 | 0.8 | 0.6666 |
| 49.        | 0.9927805 | 0.8896898 | 0.7862518 | 0.8 | 0.75 |
| 50.        | 0.9988781 | 0.9760365 | 0.8948887 | 0.8 | 0.8333 |
| 51.        | 1.0000244 | 0.9954021 | 0.9743458 | 0.8 | 0.9166 |
| 52.        | 1.0009024 | 1.0015976 | 1.0001533 | 0.8 | 0.9966 |

The first three relative natural frequencies (f₁, f₂, and f₃) are taken as input parameter; relative length (l) and relative depth (d) are taken as output parameters. The various functions used are: Levenberg Marquardt (trainlm) is taken as Training function, LEARNINGDM is taken as adaption learning function, Mean square error (MSE) taken as performance function and Sigmoid function (tansig) as transfer function. The input parameters required for the training of data are provided as shown in Table 5.
Table 5. Input parameters for training

| Serial No. | Input Parameters for Training       | Values |
|------------|------------------------------------|--------|
| 1.         | Goal                               | 1e-06  |
| 2.         | Learning rate                      | 0.1    |
| 3.         | Momentum parameter                 | 0.9    |
| 4.         | Number of epochs                   | 1000   |
| 5.         | Number of nodes in input layer     | 3      |
| 6.         | Number of neuron in hidden layer   | 9      |
| 7.         | Number of nodes in output layer    | 2      |

6. Validation of ANN results with FEA results

The data from the Table 4 are trained in the neural network and the outputs are predicted.
The outputs of both the analytical and predicted testing data as given above (through ANN) are compared as shown in Table 6.

| Data No. | cd (FEA) | cd (ANN) | Error % w.r.t FEA | cl (FEA) | cl (ANN) | Error % w.r.t FEA |
|----------|----------|----------|-------------------|----------|----------|-------------------|
| 3.       | 0.2      | 0.2047   | 2.375             | 0.1666   | 0.1593   | 4.396             |
| 8.       | 0.2      | 0.2119   | 5.99              | 0.5833   | 0.6376   | 0.9794            |
| 13.      | 0.2      | 0.2039   | 1.95              | 0.9966   | 0.9763   | 2.0414            |
| 19.      | 0.4      | 0.4034   | 0.867             | 0.4166   | 0.4050   | 2.7976            |
| 25.      | 0.4      | 0.4194   | 4.87              | 0.9166   | 0.9003   | 1.783             |
| 31.      | 0.6      | 0.6054   | 0.9083            | 0.3333   | 0.3337   | 0.11              |
| 37.      | 0.6      | 0.6167   | 2.7983            | 0.8333   | 0.7852   | 5.7711            |
| 43.      | 0.8      | 0.8146   | 1.825             | 0.25     | 0.2470   | 1.172             |
| 49.      | 0.8      | 0.8007   | 0.0912            | 0.75     | 0.7511   | 0.152             |
| 52.      | 0.8      | 0.8405   | 5.0737            | 0.9966   | 0.9942   | 0.2474            |

7. Results and discussion

In order to avoid an extensive failure or accident, the early prognosis of crack in structures is necessary. With the use of Euler’s equation, the natural frequency of the undamaged beam is obtained and it is found that it is close to the experimental and numerical results. The experimental natural frequencies and mode shapes of six cracked beam specimens at seven different crack locations of crack depth 1mm, 2mm, 3mm and 4mm are obtained. For the same depth and location, finite element analysis results are obtained and are compared with experimental values as shown in Table 3. It is found that the error percentage between them is less than 7% which indicates that the FEA results are closer to the experimental results. Therefore, to reduce time, money and material, the finite element method is used to determine the first three modal frequencies of cracked beam for different depth and locations which are further used as inputs to the neural network for prognosis of crack.

The frequencies of cracked beam obtained from finite element analysis are trained in the Cascade Forward Back Propagation (CFBP) Neural Network. Table 6 shows us the comparison between numerical and ANN outputs. The results obtained are as follows:

- It is been seen from Table 6 that the maximum error percentage between the actual (FEA) and the predicted (ANN) outputs is less than 6% which shows that ANN is well built to estimate the crack characteristics of cantilever cracked beam.
- The average error percentage between the FEA and ANN outputs is 2.67 for depth and 2.49 for location.

The regression analysis of training, validation and test data is shown in Fig. 10 which shows that predicted data are well fitted to the actual outputs.

![Fig. 10. Regression analysis](image-url)
A comparison graph between FEA and ANN outputs for crack depth and crack location has been shown in Fig. 11(a) & 11(b) respectively.

![Fig. 11(a). Comparison graph for crack depth.](image1)

![Fig. 11(b). Comparison graph for location.](image2)

8. Conclusions

Crack development in a beam leads to sudden failure of a system without any prior indication or warning. Thus, structural health monitoring is necessary to avoid risks, damages and breakdown. So, in order to avoid an extensive failure or accident, the early prognosis of crack in structures is necessary. Therefore, in this study various techniques like vibration analysis, finite element analysis (FEA) and soft computing method i.e. artificial neural network (ANN) have been used for diagnosis and identification of crack in structures. Based on this study, the following points are concluded as:

- Due to the presence of crack in structure, the natural frequency decreases and hence the stiffness of the structure also decreases.
- The maximum error percentage between the experimental and FEA results are less than 7% which indicates that both the results are in good agreement to each other. So the natural frequencies obtained by FEA can be used for training in neural network for prediction of crack which involves simplicity and less time for evaluation of natural frequencies as compared to experimental method.
- Thus, the maximum error % between the actual (FEA) and the predicted (ANN) outputs is less than 6 % which shows that ANN is well built to estimate the crack depth and location of cantilever cracked beam.
- ANN can be used to predict damages in metallic and composite structures and classify faults in rolling bearing elements with good accuracy.
• A neural controller can be programmed, trained and installed in a structure and this ANN controller will provide us the damage information accurately.

9. Future scope

A neural controller can be made and installed in structures using the ANN algorithm and can be programmed according to it, which can predict the damages and can provide prior warning and indication.

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