Finite Element Analysis on Lining Structure of Diversion Tunnel in a Hydropower Station

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Abstract. Aiming at the high internal and external water pressure tunnels built in unfavorable geological bodies, this study proposes a novel type of composite support structure in which steel plates are poured inside concrete linings. Compared with traditional structures, it has the advantages of higher tensile strength, better crack resistance, and impermeability. Taking the diversion tunnel of a hydropower station as an example, based on linear and non-linear finite element simulations, mechanical properties of the steel-concrete composite lining structure for a hydraulic tunnel in soft surrounding rocks are analyzed. On this basis, the concrete crack control under this supporting condition is verified. Research results can provide a reference for the selection of reasonable steel plate thicknesses and reinforcement types in design.

1 Introduction

Hydraulic tunnels generally adopt a composite lining structure, with rock bolts and sprayed concrete as the initial flexible support, and reinforced concrete as the secondary rigid lining [1]. The traditional reinforced concrete lining has the defects of large thickness, complicated process, and poor crack resistance, so it is prone to cracking, water leakage, and other diseases in long-term operation. Composite structures of steel plate and concrete is a new type of tunnel lining structure, which has the characteristics of excellent tensile performance of steel plates, and high compressive strength of concrete [2]. In its construction, the technology of prefabricating steel plates in factories, assembling and pouring concrete on site is adopted. The lining has the advantages of small thickness, high strength, easy operation, and maintenance [3-5].

A hydropower station locates on the mainstream of the Nan'er River in central Laos, which is the third stage of cascade development from downstream to upwards. The control drainage area above the dam site is 3913km², the annual runoff is 3.47 billion m³, and the annual average flow is 110m³/s. The project layout form is CFRD + left bank spillway + right bank diversion system (including about 11km long diversion tunnels, upstream surge tanks, ground powerhouses, etc.). Among them, the pressure diversion tunnel has a flow rate of 178.92m³/s, which connects to the upstream surge tank through a turn on the plane. The tunnel traverses the 3# ravine with a buried depth of 120~160m and a circular section diameter of 9.3m. The upstream side of the 3# ravine is a granite section, and the downstream side is a limestone section. The granite in lithological contact zones is strongly weathered, with a full-strength weathering depth of up to 160m; limestone karst is developed, and the surface densely covers with sinkholes. The groundwater in excavated granite walls is dripping and flowing. The limestone section is rich in groundwater and has good connectivity with surface water. Therefore, water inrush occurred in several places during the construction process (see Fig. 1 for the geological profile). Due to the extremely poor geological conditions of the tunnel and high-water pressures, considering the safety and cost of the project, the tunnel adopts a new type of lining with steel plates placed in the middle of reinforced concrete linings.

Fig. 1. Geological profile of the tunnel traverses 3# ravine

Using linear and non-linear finite element simulation methods, this study takes the diversion tunnel as an example, the mechanical properties of steel-concrete composite lining structures under the conditions of high internal-external water pressures in soft rocks are comparatively analysed. Meanwhile, concrete crack control under this support scheme is verified.
Furthermore, a reasonable plate thickness and reinforcement type for design selection are put forward.

2 Methodology

2.1. Reinforcement calculation

Reinforcement calculation of concrete linings adopts a linear elastic finite element method based on the ANSYS platform, and the tensile bearing capacity of the lining section is shown in Fig. 2. The axial tensile force \( N \) acts on the small eccentric tension member between resultant points \( A_i \) and \( A'_i \) of the steel, the tensile bearing capacity at the normal section is,

\[
Ne \leq \frac{1}{\gamma_d} f_s A'_i (h - a'_i) \quad (1)
\]

\[
Ne' \leq \frac{1}{\gamma_d} f_s A_i (h'_i - a_i) \quad (2)
\]

where, \( A_i \) and \( A'_i \) are the cross-sectional areas of the longitudinal steel bars arranged on the side close to and away from the axial tension; \( e \) and \( e' \) are the distances from the axial tension to the resultant points \( A_i \) and \( A'_i \) of reinforcement.

![Fig. 2. Calculation of tensile bearing capacity at normal section of small eccentric tension member](image)

According to the regulations on crack control check for non-member system structure: the circular reinforced concrete lining is calculated by nonlinear finite element, and the crack width is controlled according to the stress of steel bars. The maximum allowable crack width in limit state design of hydraulic tunnels is: long-term combination 0.25mm (when the thickness of protective layers is 50mm, the corresponding steel stress is 147.5MPa), short-term combination 0.30mm (when the thickness of protective layers is 50mm, the corresponding steel stress is 160MPa).

The width of surface cracks can be controlled by limiting the element stress of the first layer of tension steel. Under the action of standard combination, element stress \( \sigma_{ds} \) of the first layer of tensile steel on the surface should meet the following requirements:

\[
\sigma_{ds} \leq \sigma_{sp}
\]

where, \( \sigma_{ds} \) is the element stress of tensile steels in the first layer calculated by finite elements of reinforced concrete under the standard combination action; \( \sigma_{sp} \) is the stress limit of tensile steel elements with surface cracks on non-member structures. \( \sigma_{sp} \) should be selected according to the crack width and the thickness of protective layers: when the crack width is controlled at 0.1mm~0.3mm and the thickness of protective layers is 50mm, \( \sigma_{sp} \) should not exceed 110N/mm²~160N/mm²; when the thickness of protective layers is 100mm, it should not exceed 80N/mm²~140N/mm².

3 Modelling scheme and parameter selection

The reservoir water level during normal operation is 723m, the pressure head of internal and external water in modeling is 200m and 110m respectively. Internal and external pressures are considered based on surface forces when calculating lining structures; the internal pressure includes hydrostatic pressures and water hammer pressures.

The steel plate-concrete composite lining structure is shown in Fig. 3. To compare the mechanical properties of the structure when a steel plate is located at different positions in concrete, the following four modeling schemes are selected in this study:

- **Scheme 1**: The steel plate is not considered, and the thickness of lining concrete is 110cm;
- **Scheme 2**: The steel plate locates in the middle of lining concrete (the inner and outer concrete thicknesses are 50cm and 60cm respectively), considering the action of steel plate and inner concrete;
- **Scheme 3**: The steel plate locates in the middle of lining concrete (the inner and outer concrete thicknesses are 50cm and 60cm respectively), considering the action of the steel plate and outer concrete;
- **Option 4**: The steel plate is located in the middle of the lining concrete (the inner and outer concrete thicknesses are 40cm and 70cm respectively), considering the action of the steel plate and outer concrete.
Fig. 1 reveals that the tunnel passes through the 3# ravine with stake numbers T6+680~T6+710 to expose the most unfavorable geological conditions. Based on this section as a standard, the physical and mechanical parameters of surrounding rocks and supporting structure in numerical modeling are selected as shown in Tables 1-4.

Table 1. Physical and mechanical parameters of rocks.

| Stake number /m | T6+680~T6+710 |
|-----------------|----------------|
| Rock category   | V              |
| Saturation density /g/cm³ | 2.18 |
| Uniaxial compressive strength /MPa | 10 |
| Deformation modulus /MPa | 350 |
| Unit elastic resistance coefficient /MPa/cm | 2.5 |
| Poisson's ratio  | 0.45           |
| Cohesion /MPa    | 0.05           |
| Friction coefficient | 0.36 |

Table 2. Physical and mechanical parameters of concrete.

| Strength grade | C25 |
|----------------|-----|
| Bulk density /kN/m³ | 24 |
| Design value of axial compressive strength /MPa | 11.9 |
| Design value of axial tensile strength /MPa | 1.27 |
| Elastic modulus /MPa | 28000 |
| Poisson's ratio  | 0.167 |

Table 3. Reinforcement strength and elastic modulus.

| Type of reinforcement | HRB400 |
|-----------------------|--------|
| Strength standard value /MPa | 400 |
| Strength design value /MPa | 360 |
| Elastic modulus /MPa   | 2.0×10⁵ |

Note: Tensile design value of steel bar for axial tension and small eccentric tension members is 300MPa.

Table 4. Design value of steel plate strength.

| Steel grade (standard) | Q345R (GB 713) |
|------------------------|-----------------|
| Thickness /mm          | 14              |
| Bulk density /kN/m³    | 78.5            |
| Yield strength /MPa    | 345             |
| Tensile strength/MPa   | 510             |
| Tensile/Compression/Bending | 310 |

4 Result analysis

Fig. 4 shows the circumferential stress cloud diagram of the lining under normal operation conditions and different steel plate layouts. Without considering the concrete reinforcement and steel plate (Scheme 1), the maximum hoop stress of the tunnel lining is 4.86 MPa (Fig. 4a), which is much greater than the concrete axial tensile strength. Considering the combined bearing of steel plate and lining (Scheme 2), the hoop stress of concrete is reduced compared with that without considering combined bearing (Fig. 4b). Since concrete is regarded as a linear elastic material in the calculation of reinforcement, the coordinated deformation of concrete and steel plates makes the concrete stress exceed its limit tensile strength. However, the Mises stress of the steel plate is not large, and the maximum value is 27.9MPa. If the model considers the effects of steel plate and outer concrete, as shown in Scheme 3 (the combined bearing of outer concrete and steel plate, without considering the effect of inner concrete), the hoop stress of concrete (8.01 MPa) increases significantly compared to when the inner concrete is considered. Meanwhile, the Mises stress of the steel plate also increases obviously, with a maximum value of 60.73MPa (Fig. 5), and the radial deformation does not exceed 1.86mm.

In Scheme 4, the steel plate divides the lining concrete into 40cm and 70cm thickness of inner and outer concrete. The interaction between the steel plate and the outer concrete is considered in the model.
Compared with Scheme 3, due to the increase in the thickness of the outer concrete, the hoop stress of the lining and the Mises stress of the steel plate is significantly reduced to 6.89 MPa and 53.89 MPa (Fig. 5), respectively. The radial deformation does not exceed 1.81 mm.

![Fig. 5. Mises stress cloud diagram of steel plate in each scheme (MPa)](image)

A steel plate is arranged in the middle of lining concrete as an anti-seepage structure. In the most unfavorable case, that is, when inner concrete cracks (internal water seepage at this time), the cracks develop in outer concrete are checked. Simulation selects the thickness of 40cm inner concrete and 70cm outer concrete (Scheme 4), so that internal water pressures are borne by steel plates, outer concrete, and surrounding rocks. Because it is difficult to set four layers of steel bars in the outer 70cm thick concrete, the reinforcement with two layers of the inner side and one layer of the outer side is considered in calculation, see Table 5. In this condition, the maximum tensile stress of the steel bar is 134 MPa (Fig. 6), which is less than the maximum allowable stress of a steel bar demonstrated in section 2.2. Therefore, the design solution meets the requirements for crack control.

### Table 5. Reinforcement scheme and stress (protective layer thickness 50mm).

| Reinforcement recommend | Maximum stress of steel bar /MPa | Limit strength of steel bar /MPa |
|-------------------------|---------------------------------|---------------------------------|
| Two layers of \(22\)@150 at inner side, one layer of \(22\)@150 at outer side | 134 | 147.5 |

Note: Spacing of 150mm means that 7 steel bars are arranged at 1m. Net spacing of each layer of steel bars is 100mm.

### 5 Conclusion

Considering the requirements of anti-seepage and anti-cracking properties for hydraulic tunnels, a novel form of steel-concrete composite support is proposed. The result of finite element simulations based on a diversion tunnel of a hydropower station shows that, the installation of steel plates in concrete linings can not only achieve the effect of anti-seepage, but also share the tensile stress generated by high internal water pressures on lining structure to a certain extent. In addition, to ensure that the overall thickness of a lining remains unchanged, the increase of outer concrete thickness can significantly reduce the tensile stress in the lining. For this tunnel, steel-concrete support with inner and outer concrete thicknesses of 40cm and 70cm is selected. Considering the most unfavorable conditions for inner concrete cracking, the outer concrete can meet crack control requirements when two layers of \(22\)@150 on the inner side and one layer of \(22\)@150 on the outer side are set for the reinforcement.

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