The effect of electrode heating on the discharge parameters in complex plasma experiments

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Received 1 September 2010, in final form 19 November 2010
Published 25 January 2011
Online at stacks.iop.org/PSST/20/015026

Abstract
Thermophoresis is a tool often applied in complex plasma experiments. One of the usual stated benefits over other experimental tools is that electrode temperature changes required to induce thermophoresis do not directly influence the plasma parameters. From electronic data, plasma emission profiles in the sheath, and Langmuir probe data in the plasma bulk, we conclude that this assumption does not hold. An important effect on the levitation of dust particles in argon plasma is observed as well. The reason behind the changes in plasma parameters seems to be the change in neutral atom density accompanying the increased gas temperature while running at constant pressure.

1. Thermophoresis in complex plasma

Partially ionized gases containing small solid particles, called complex plasmas, are a widespread phenomenon in space, found for instance in molecular clouds, planetary atmospheres, planetary rings and comets [1, 2]. In the laboratory, complex plasma has become a promising tool to study the physics of solid state systems, fluid dynamics and turbulence, even biophysics, on a level accessible with ordinary optical techniques [3–5].

Unless experiments are performed during parabolic flights, or under micro-gravity conditions on the International Space Station [6], gravity dominates the force equilibrium in complex plasma, resulting in the formation of two-dimensional crystal structures in places where the electrostatic force acting on the particles balances gravity. An alternative is to extend the confinement of the particles vertically by adding a dielectric (glass) box in the discharge [7]. In these experiments, thermophoresis played an important role in reducing the effect of gravity, and three-dimensional crystals were produced.

The thermophoretic force depends on the establishment of a temperature gradient in the background gas, resulting in a net imbalance of the momentum imparted by neutral atoms colliding with a particle in the gas. Therefore, it has to date been regarded as a tool independent of the plasma parameters, which in complex plasma experiments are hard to measure, since they can become strongly coupled to the presence of particles in the plasma [8]. As a consequence, changes in discharge characteristics (like the dc bias, or absorbed power) accompanying temperature changes are usually considered insignificant and are not specified in complex plasma experiments involving thermophoresis, see for instance [9].

This paper reports on complex plasma experiments involving thermophoresis performed in a modified Gaseous Electronic Conference (GEC) reference cell [10] at the Center for Astrophysics, Space Physics, and Engineering Research (CASPER). Two direct observations connected with thermophoresis are a change in the dc bias on the powered electrode with increasing electrode temperature, which was briefly mentioned before [11], accompanied by a change in levitation height of the particles. From electronic data, optical emission data and Langmuir probe data, we show that the plasma properties indeed change. Using a self-consistent fluid model [12], we show that the volume-averaged gas temperature...
increases with electrode temperature, resulting in a decrease in the neutral atom density.

2. The complex plasma experiment at CASPER

The experiments discussed here were performed using argon gas at low pressures (a few tens of pascals). The upper electrode in the cell, as well as the walls surrounding the chamber, is grounded, while a 13.56 MHz radio-frequency (RF) potential is applied to the lower electrode with an amplitude of a few tens of volts.

Once plasma is formed, spherical micrometer-sized melamine-formaldehyde (MF) particles are introduced from shakers situated at the top of the chamber. The particles fall through the grounded electrode, which consists of a hollow cylinder, rather than a solid electrode. At equilibrium, the particles are vertically suspended in the sheath above the bottom electrode while horizontally confined by a cutout plate placed on top of the bottom electrode, which contains a cylindrical depression creating a radial electric field.

Two diode lasers are used to illuminate the particles. The lasers are equipped with cylindrical lenses, so that thin (±100 μm), but wide (fan angle >5°) laser sheets are created. A vertical laser sheet in combination with a side-view camera allows side-view pictures of the suspended particles, whereas a horizontal laser sheet together with a top-view camera focused through the hollow upper cylinder allows for top-view images. A schematic drawing of the experimental setup is shown in figure 1.

The lower electrode temperature is regulated by coolant liquid running through tubes which are placed inside bores in the electrode. The temperature of the liquid is maintained by a heater/chiller with a thermostat, and is adjusted from 0 to +70 °C in steps of 10 °C. The lower electrode temperature is measured with a thermistor attached to the bottom of the electrode and logged with a digital datalogger.

Electronic data, including the driving potential, the electrode current and the signals from two derivative probes, measuring the derivatives of the potential and electrode current, are collected on two oscilloscopes. The latter signals are used to determine the phase angle between the potential and the current. From this angle and the first two signals, the power input into the plasma is calculated. From the electronic data, the floating dc bias on the lower electrode is obtained too, as the shift in the mean value of the driving potential data.

3. Data obtained during thermophoresis complex plasma experiments

This section presents the data obtained during experiments at a pressure of 200 mTorr (26 Pa). In these experiments, 8.89 μm diameter MF particles were used. Initially, the dc bias was allowed to float and clear changes in the dc bias were observed with the increase in lower electrode temperature. Theoretically, the effect of thermophoresis is expected to be independent of plasma parameters and the effect of electrode heating on the plasma parameters is considered to be unimportant. Hence, the dc bias is expected to be constant with changing electrode temperature. We therefore repeated the experiment while keeping the dc bias fixed with an external power supply to represent the case that is theoretically expected. The results from this set of experiments are then compared with the results from the experiments with floating dc bias, which leads to changes in the dc bias with changes in the electrode temperature.

We first present the measured dc bias and the levitation height of the particles above the lower electrode, obtained with the side-view camera, for the two sets of experiments. We then present the additional data obtained from the data-loggers, oscilloscopes and Langmuir probe, as well as optical emission profiles in the sheath.

3.1. Dc bias and dust levitation

The measured dc bias on the lower electrode is shown for both sets of data in figure 2. When the dc bias is allowed to float, it becomes less negative with increasing lower electrode temperature. Because our discharge chamber is fairly symmetric, the induced dc bias is small; even so, the change in dc bias with the change in lower electrode temperature is significant. Even when the power supply was used, the dc bias had to be manually adjusted for each electrode temperature setting, showing that it still changed despite the connection to the power supply. This indicates that changes in the dc bias are a diagnostic for changes in the plasma occurring due to electrode heating. A slight variation of the dc bias is observable despite the power supply, although the variation was much smaller than in the experiments with floating dc bias.

For each temperature setting in each experiment, the dc bias was logged for 150 s. The error bars in figure 2 indicate the range over which the dc bias varied during these 150 s, whereas the symbol shows the mean. As can be seen, the dc bias varies over a rather large range. This is better illustrated in figure 3, where 50 consecutive data points are shown during the 150 s of measurement. The upper panel shows the registered lower electrode temperature with the thermostat set at 70 °C, while the lower panel shows the dc bias on the lower electrode. In this case, the dc bias was floating with values fluctuating around −5.45 V. Clearly, the dc bias directly follows the temperature on the powered electrode. The variations in temperature shown are due to hysteresis in the heater/thermostat system. As can be seen, there is an offset between the temperature setting on the thermostat and the mean temperature measured with the thermistor (about 4 °C at 70 °C), as well as the tendency to overshoot the set temperature (plus offset).
The levitation height of the particles in both sets of experiments is not the same. In figure 4(a) the overlaid side-view images for both experiments at an electrode temperature of 40 °C are shown. The white dots represent the particles in the experiment with fixed dc bias, the black dots the particles in the experiment with floating dc bias. There is a clear difference in levitation height of about 15 pixels. The side-view camera resolution is roughly 25 μm per pixel, so this difference in levitation height corresponds to 350 μm. The difference in levitation height for all electrode temperatures is shown in figure 4(b).

It is not the aim of this paper to completely analyze the levitation of the dust particles, but rather to show the difference as an indication of changing plasma parameters. Nonetheless, the difference in levitation is caused by a change in the forces acting on the dust particles. For experiments such as these, the two main forces determining the levitation height are the downward force of gravity and the upward force due to the electric field in the sheath. The change in levitation height is therefore an indication of a change in the electric field structure in the sheath, or a change in the dust particle charge, or both. Even though a change in the dust charging cannot be excluded, there are clear indications of changes in the sheath electric field structure as the lower electrode temperature is changed, as discussed below.

3.2. Electronic data from oscilloscopes

To investigate whether the changes shown are related to changes in the plasma parameters, we logged the root-mean-square driving potential ($V_{\text{RMS}}$) and current ($I_{\text{RMS}}$), as well as signals from two derivative probes. The raw signals are shown in figure 5. Each RF cycle is sampled by 37 points, giving a resolution of roughly 2 ns. The top panel shows $V_{\text{RMS}}$ and $300 \times I_{\text{RMS}}$ (which is typically on the order of 10 to 100 mA). The bottom panel shows the normalized derivative probe signals, which are used to determine the phase angle $\Phi$ between $V_{\text{RMS}}$ and $I_{\text{RMS}}$.

Using these data, we can calculate the total power absorbed in the plasma, as $P_{\text{RMS}} = V_{\text{RMS}}I_{\text{RMS}} \cos(\Phi)$. The amplitude of the RMS voltage and current, the phase angle $\Phi$ and the RMS plasma power derived for both sets of experiments.
that the electron density appears to decrease with increasing electrode temperature. The electron temperature does seem to be high, since in typical plasma discharges in the GEC cell at similar discharge settings, the electron temperature is normally on the order of 1 eV [15], while numerical simulations of the discharge result in electron temperatures around 5 eV [12], consistent with previously conducted numerical simulations of the GEC cell [16]. This means that the measured electron temperature is on average overestimated by a factor of 3.

3.4. Sheath emission profiles

Optical emission profiles in the sheath were obtained with the side-view camera. To ensure that particles did not influence the profiles, they were taken in the absence of dust. Figure 8 shows the side-view obtained in an experiment with fixed dc bias at 0 °C subtracted from the side-view obtained at 70 °C, on the left. The image shows the plasma glow fairly close to the lower electrode surface. The contrast has been enhanced in the image to increase visibility of the intensity differences.

The dark region indicates that higher up in the sheath, the intensity is less at higher electrode temperature, while the thin bright structures show that at higher electrode temperature the local emission is increased in front of the electrode. These thin emission structures have recently been associated with the presence of fast neutral particles [17] or energetic ions [18].

Figure 8 shows vertical emission profiles collected at 10, 40 and 60 °C divided by the one obtained at 70 °C, on the right. The images are taken slightly higher up in the sheath than in the figure on the left. The recorded height corresponds to 12 mm, roughly the width of the sheath in front of the lower electrode. The profiles in both sets of experiments look similar, having a peak toward the bottom of the picture, corresponding to the highest horizontal band of figure 8. For all temperatures the intensity becomes the same at the top of the image, which corresponds to the start of the plasma bulk, indicating that the bulk plasma emission is the same for all temperatures. For increasing electrode temperature, the observed intensity throughout a large part of the sheath decreases, however, indicating a change in the properties of the sheath.

4. Discussion of results

4.1. Emission profiles

Most of the visible line radiation in argon plasma at the powers and pressures discussed is due to the de-excitation of neutral atoms in excited states rather than due to excited ionic states [19], since the energy required for the direct excitation of ions is high (35 eV) and we do not expect a significant electron population with sufficient electron energy. The most likely excitation process is due to direct electron-impact excitation by energetic electrons (with $E > 11.7$ eV), whereas the most likely de-excitation process is spontaneous de-excitation with the emission of a photon. There are three possible explanations for the observed reduction in emission: a reduction in the creation of excited atoms, a different de-excitation process.
(which does not involve the emission of photons in the visible spectrum) becoming dominant, or an increase in transport of the excited species away from their origin.

Due to the long lifetime of meta-stable states, transport of such excited atoms away from their origin is possible. Since the GEC cell is constructed to minimize gas flow, and since the temperature gradients induced by thermophoresis are too small to cause thermal convection [20], the excited neutral species will move through random Brownian motion. Thus, an increase in transport is possible with an increase in the neutral gas temperature. Since most energetic electrons are found in the sheath, the main source of excited atoms is the sheath region. Increased transport of these excited species might diffuse the emission coming from the sheath region, explaining in part the reduced observed emission.

Different de-population mechanisms from excited states could include the excitation from such a state to a higher-energy state, which in turn spontaneously de-excites emitting a photon with a wavelength outside the visual spectrum, or increased electron-impact ionization from the excited state. For the de-population to become important, a significant increase in electron density in the sheath would be required, since these processes require a second electron to collide with the excited atom within its lifetime. Langmuir probe data in the sheath are not available, while details about the population of energy levels would require techniques such as line-ratio spectroscopy. We can therefore at this moment not exclude this possibility.

Finally, the easiest explanation would simply be a decrease in electron density and/or neutral gas density, since electron-impact excitation rates are proportional to the product of both densities. This possibility seems more likely, as is discussed below. A significant cooling of the electron population as a whole would also explain a reduction in the excitation processes, since an electron energy of at least 11.7 eV is
4.2. Langmuir probe data

The Langmuir probe data presented above show no clear trend with temperature. According to numerical simulations, the local floating potential (which basically shows how negatively charged an object immersed in the local plasma would become) should be directly proportional to the electron temperature; $(V_{fl} - V_p) = -KT_e$ where $K$ is a constant that depends on the gas. At room temperature in argon it was shown that $K = 2.989$ [21]. A plot of the ratio obtained from our data is shown in figure 9, showing results consistent with theory. It also demonstrates a lack of a clear trend with electrode temperature. We therefore conclude that the bulk plasma parameters do not show a clear change with lower electrode temperature, which is consistent with the emission profiles.

The floating potential is determined by the probe as the potential where the total probe current vanishes, $V_{fl} : I(V) = 0$, which is a rather precise measurement. The plasma potential is determined as the potential at which the second derivative of the probe current vanishes, $V_p : I''(V) = 0$, which is a much less precise measurement, due to the fluctuation of the probe current caused by the RF field, despite the fact that the SmartProbe is an RF-compensated probe. The electron temperature is determined with the help of the plasma potential, $T_e = \int V_{fl} I(V) dV/I(V_p)$, so it has a similar uncertainty to the plasma potential. This could explain why the ratio of the potential to the electron temperature gives results in agreement with theory, as shown in figure 9.
Nonetheless, estimating the floating potential by the dc bias on the lower electrode, $-10 \leq V_0 \leq -5 \text{ V}$, and a plasma potential on the order of the RMS driving potential $30 \leq V_p \leq 28 \text{ V}$, we obtain $-40 \leq (V_0 - V_p) \leq -33 \text{ V}$, which is consistent with most of the data. This could indicate that the obtained electrode temperature of roughly $12 \text{ eV}$ could be consistent with the potential measurements. Possibly, this high electron temperature is due to the changes made to the experiment to allow complex plasma experiments, including the upper electrode geometry and the cutout plate on top of the lower electrode. These changes add additional edges to the discharge, which might lead to additional electric fields in which electrons can gain energy. These effects are expected to be small, however, and the high electron temperature as indicated by the Langmuir probe data is not reproduced by the numerical simulations. It seems therefore more likely that there is a systematic error introduced by the probe measurements, which leads the probe software to systematically overestimate the plasma potential.

4.3. Electronic data

In a low pressure RF discharge the sheaths act mostly capacitively, whereas the main power dissipation is due to the resistive bulk. In this case, the impedance of the plasma can be represented by two sheath reactances, $X_s$, in series with the bulk reactance $R_b$ [22]. Since the dissipative character of the sheaths is much smaller than the bulk, they are considered to be completely capacitive, and hence their impedance is purely imaginary. The discharge then has a complex impedance $Z$ given by $Z = R_b + i(X_{sg} + X_{sp})$ where it is assumed that the grounded sheath and the powered sheath are not identical.

The absolute value of the impedance is given by $|Z| = V/I$, the ratio of the discharge voltage and current. The phase angle between the voltage and current, $\Phi$, is related to the resistance and reactance through $\tan(\Phi) = (X_{sg} + X_{sp})/R_b$, so that $R_b = |Z|/\sqrt{1 + \tan^2(\Phi)}$. From our electronic data, we can thus calculate the RMS impedance, resistance and reactance. The results are shown in figure 10.

In a capacitively coupled RF discharge in argon at the pressures and powers considered, the bulk resistance can be approximated by $R_b = v_c/\alpha e_0$, with $v_c = n_{\text{gas}} \int \sigma v_c f_e \, dv_e$ the electron–neutral collision frequency, $\sigma$ the cross section for elastic electron–neutral collisions [22], which is approximately $3 \times 10^{-19} \text{ m}^2$ for the electron energies in the discharge [23], and $\omega_p = \sqrt{n_e e^2/m_e e_0}$ the electron plasma oscillation frequency. Hence, $R_b \approx 3 \times 10^{-10} m_e n_{\text{gas}} \sqrt{8 k_B T_e / \pi m_e n_e e^2} \approx 10^{-7} (n_{\text{gas}}/n_e) \sqrt{T_e} \Omega$, where we have assumed a Maxwellian distribution for the electrons. For a pressure of 200 mTorr, an electron density of about $5 \times 10^{14} \text{ m}^{-3}$, and an electron temperature of $7 \text{ eV}$, we obtain $R_b \approx 370 \Omega$, which is very close to the determined values.

The sheath reactance can be approximated by $X_s = d_s/\sqrt{\omega_{\text{RF}} e_0 A} \approx 1321 d_s / A \Omega$, where $d_s$ is the sheath width and $A$ is the electrode surface area [22]. The sheath width can be approximated by the Child–Langmuir law, as $d_s \approx 10^{-4} (\Delta V)^{3/2} J_{s}^{-1/2}$, with $\Delta V$ the voltage drop across the sheath and $J_s$ the ion current density across the sheath [24]. Assuming that the ion current density can be approximated by the Bohm flux ($J_s = e n_{\text{gas}} \sqrt{k_B T_e / m_e}$), and using the surface area of the lower electrode ($A = \pi (0.05)^2$), the sheath reactance becomes $X_s \approx 10^{10} (\Delta V)^{3/2} n_{\text{gas}}^{-1/2} T_e^{-1/4} \Omega$. For a potential jump across the sheath of 30 V, an ion density of $5 \times 10^{14} \text{ m}^{-3}$ (assuming quasi-neutrality at the sheath edge), and an electron temperature of $7 \text{ eV}$, we find $X_s \approx 340 \Omega$, which is in good agreement with the determined values.

From the above, we see that a slight increase in resistance can result from an increase in gas density, a decrease in electron density, an increase in electron temperature, or a combination of these. On the other hand, the much stronger decrease in sheath reactance must result from a shrinking of the sheaths, which can result from an increase in plasma density, or electron temperature, or a smaller potential jump across the sheath. The observed change in plasma emission in the sheath might be an indication of these changes in the sheath width. Since the same decrease in reactance is also seen in the experiments with fixed dc bias, it is more likely that a change in the plasma parameters is responsible.
4.4. Neutral atom density

Most complex plasma experiments, like the ones reported here, are performed at constant pressure. Heating or cooling the lower electrode causes heating or cooling of the gas inside the chamber, however. Even though one might suspect this to be a small effect, the change in temperature can be significant. Self-consistent fluid model calculations were done for our experimental setup for different electrode temperature settings, using a self-consistent model for complex plasma simulations [12]. The model solves the complete set of plasma parameters, including the electron and ion densities and electron temperature. Dust can be included in the model and the transport of the dust is then computed using the plasma parameters as input to calculate the forces acting on the dust.

The gas temperature profile can also be calculated throughout the discharge chamber, which is done by solving the energy balance. The input consists mainly of the dissipation of energy by ions, which are heated in the time-averaged electric field, even though the heating by dust particles can be included. For our experiments this plays no role of importance, due to the small amount of dust. The loss of heat is due to conduction by the gas, while the wall temperatures are set as boundary conditions. A more detailed description can be found in [25].

The volume-averaged gas temperature computed for the experiments is shown in figure 11. Assuming the ideal gas law, \( P_{\text{gas}} = n_{\text{gas}} k_B T_{\text{gas}} \), we see that the density for 200 mTorr can vary from \( 6.6 \times 10^{21} \text{ m}^{-3} \) at 0°C to \( 6.0 \times 10^{21} \text{ m}^{-3} \) at 70°C, a difference of 10%. Such a change in neutral atom density will have a definite effect on both the global particle and power balance in the discharge, in turn affecting the electron temperature and the electron density.

4.5. Additional control experiments

Since the coverplate on top of the lower stainless steel electrode is made of aluminum, it is possible that a contact potential might be responsible for the change in dc bias. We therefore conducted a control experiment without the coverplate and found the same result. This also eliminated secondary electron emission as a cause, since aluminum has 2–4 times the secondary electron emission coefficient of steel [26], which means that any significant change in the dc bias behavior would have been observable. Another control experiment was conducted without the presence of particles, again showing the same results, indicating that the particles were not creating the observed change in dc bias.

One possibility we cannot exclude is a change in surface-recombination chemistry, due to the increased electrode temperature [27]. It is not unlikely that the surface accommodation might change with increased temperature, and this change might in part be responsible both for a change in the sheath behavior, as well as a change in the plasma parameters. At this time, no observational techniques are available in the CASPER laboratory to study this further. However, even if this were the responsible mechanism, it would still show that electrode heating to induce thermophoresis in complex

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**Figure 10.** The magnitude of the RMS impedance \( Z \), the resistance \( R \) and the reactance \( X \) of the plasma discharge against lower electrode temperature. The ◦ correspond to experiments with floating dc bias, the ● to experiments with fixed dc bias. The dashed and dotted lines are linear fits to the data, which are indicated in the figure. For both sets of data, the linear fits are very similar.

**Figure 11.** The volume-averaged gas temperature in the discharge for various electrode temperatures, calculated using a self-consistent complex plasma fluid model. All other surfaces were kept at room temperature (293 K, 20°C). The temperature response can be well represented by a linear function, indicated by the dashed line.
plasma changes the plasma parameters, indirectly coupling the thermophoretic effect to changes in the plasma parameters.

5. Conclusion

Using images of levitated dust particles, as well as of the plasma emission in the sheath, as well as electronic and Langmuir probe data, we have shown that electrode heating to induce thermophoresis has an effect on the discharge parameters in a capacitively coupled argon RF discharge. An almost constant bulk resistance together with a more strongly reduced sheath reactance can be deduced from the electronic data. Optical emission data seem to be consistent with this, in the sense that a clear change in the emission detected from the sheath region close to the electrode surface is observed, whereas the emission toward the plasma bulk does not change much with temperature. Langmuir probe data in the bulk are less conclusive, but seem to indicate a change in electron density, whereas the floating potential and electron temperature do not show a clear trend with changes in the electrode temperature, even though it seems likely that the plasma potential is overestimated by the probe measurements.

Numerical modeling indicates that experiments running at constant pressure have a varying neutral atom density when thermophoresis is applied, due to an increase in the volume-averaged gas temperature. This is expected to have a noticeable effect on the plasma parameters, consistent with our observations. Therefore, reports on thermophoresis experiments should clearly indicate if the dc bias was allowed to float, or was fixed, since the bias has an important effect on the dust levitation height and both types of experiments give different results for the equilibrium levitation height.

In the past, such information was considered unimportant. Our data seem to suggest that possibly some aspects of experiments in complex plasma involving thermophoresis might have been overlooked. In some recent experiments, thermophoresis played an important role, but the effects discussed in this report were not explicitly considered. Discussions in these works involved, for instance, the correct formulation of the thermophoretic force using dust particle levitation [9], the exact shape of the external confinement of particles levitated in a glass box with the help of thermophoresis [28], as well as observations of oscillations in a single layer of dust particles at an unusually thin edge (due to additional thermophoresis) of a void, even though in that particular case the temperature gradient arose naturally [29]. Even though the relative changes in plasma parameters due to thermophoresis depend on the exact discharge settings, our results indicate that any explanation that assumes constant plasma parameters at different electrode temperatures used to induce thermophoresis is automatically invalid and cannot describe the external confinement of dust particles in the discharge correctly for all temperatures.

This is something that experimentalists in the field should be aware of.

Acknowledgments

This work was supported by NSF under Grant PHY-0648869 and CAREER Grant PHY-0847127. The authors appreciate the discussion with many CASPER members. First author is especially grateful to Professor Overzet at UT Dallas for the discussions.

References

[1] Mendis D A and Rosenberg M 1994 Annu. Rev. Astron. Astrophys. 32 419–63
[2] Meirino R L and Goree J A 2004 Phys. Today 57 32–9
[3] Melzer A, Homann A and Piel A 1996 Phys. Rev. E 53 2757–66
[4] Morrill G E et al 2004 Phys. Rev. Lett. 92 175004
[5] Tsytovich V N, Morrill G E, Fortov V E, Gusein-Zade N G, Klumov B A and Vladimirov S V 2007 New J. Phys. 9 263
[6] Morrill G E, Thomas H M, Konopka U, Rothermel H, Zuzic M, Ilev A and Goree J 1999 Phys. Rev. Lett. 83 1598–601
[7] Arp O, Block D, Piel A and Melzer A 2004 Phys. Rev. Lett. 93 165004
[8] Stefanović I, Kovačević E, Berndt J and Winter J 2003 New. J. Phys. 5 39
[9] Rothermel H, Hagl T, Morrill G E, Thoma M H and Thomas H M 2002 Phys. Rev. Lett. 89 175001
[10] Hargis P J et al 1994 Rev. Sci. Instrum. 65 140–54
[11] Land V, Smith B, Matthews L and Hyde T W 2010 IEEE Trans. Plasma Sci. 38 768–73
[12] Land V, Shen E, Smith B, Matthews L and Hyde T 2009 New J. Phys. 11 063024
[13] Braithwaite N St J 1997 Plasma Sources Sci. Technol. 6 133–9
[14] http://www.scisys.com/langmuir.cfm
[15] Anderson H M and Radovanov S B 1995 J. Res. Natl Inst. Stand. Technol. 100 449
[16] Boeuf J P and Pitchford L C 1995 Phys. Rev. E 51 1376
[17] Donko Z, Hartmann P and Kutasi K 2007 J. Phys.: Conf. Ser. 71 012008
[18] Nemschokmichal S, Dittman K and Meichsner J 2008 IEEE Trans. Plasma Sci. 36 1360–1
[19] Palmero A, van Hattum E D, Rudolph H and Habraken F H P M 2007 J. Appl. Phys. 101 053306
[20] Goedheer W J, Land V and Venema J 2009 Contrib. Plasma Phys. 49 199–214
[21] Goree J 1994 Plasma Sources Sci. Technol. 3 400–6
[22] Beneking C 1990 J. Appl. Phys. 68 4461
[23] Raju G G 2004 IEEE Trans. Dielectric Electric Insul. 11 649
[24] Godyak V A, Piejak R J and Sternberg N 1993 IEEE Trans. Plasma Sci. 21 378
[25] Land V, Bolser D, Matthews L S and Hyde T W 2010 Phys. Rev. E 81 056402
[26] Böhm C and Perrin J 1993 Rev. Sci. Instrum. 64 31
[27] Rebrow A K, Morozov A A, Plotnikov M Yu, Timoshenko N I and Maltsev V A 2003 Rev. Sci. Instrum. 74 1103
[28] Arp O, Block D, Klinendworth M and Piel A 2005 Phys. Plasmas 12 122102
[29] Bin Liu et al 2009 Phys. Plasmas 16 083703