Aberration-corrected quantum temporal imaging system

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We describe the design of a temporal imaging system that simultaneously reshapes the temporal profile and converts the frequency of a photonic wavepacket, while preserving its quantum state. A field lens, which imparts a temporal quadratic phase modulation, is used to correct for the residual phase caused by field curvature in the image, thus enabling temporal imaging for phase-sensitive quantum applications. We show how this system can be used for temporal imaging of time-bin entangled photonic wavepackets and compare the field lens correction technique to systems based on a temporal telescope and far-field imaging. The field-lens approach removes the residual phase using four dispersive elements. The group delay dispersion (GDD) $D$ is constrained by the available bandwidth $\Delta \nu$ by $D > t/\Delta \nu$, where $t$ is the temporal width of the waveform associated with the dispersion $D$. This is compared to the much larger dispersion $D \gg \pi t^2/8$ required to satisfy the Fraunhofer condition in the far field approach.

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I. INTRODUCTION

Quantum communication systems rely on transforming and transmitting information using quantum systems, such as atoms, trapped ions and photons [1–5]. It is widely believed that future quantum information system will consist of more than one type of physics system [2–5], such hybrid quantum connections have been demonstrated between ion and photon [6] and proposed for atoms and quantum dots [7]. In hybrid systems, photons are often used as propagating quantum information carrier, or flying qubits, to connect different quantum systems [5–9]. In long-distance quantum communication between hybrid quantum platforms, the wavelength, temporal scale and spectral profile of the photonic wavepacket for the source and target quantum memories and transmission channel are very different [5]. We need an efficient interface to convert the wavelengths and temporal scales of the photonic wave packet to match quantum memories, while preserving the quantum state. Here, we propose a quantum interface for flying qubits (photons) using temporal imaging integrated with nonlinear optical wavelength conversion.

The bridge between different wavelengths has been intensely investigated in the quantum optics field. Quantum connections are generated either via broadband entangled photon pair sources [10], or via nonlinear frequency conversion of the photonic wavepacket [11–22]. Preserving the quantum state is achieved using nonlinear frequency conversion processes that do not amplify the input state (which adds noise), such as three-wave mixing (3WM) [11–19] and Bragg-scattering-type four-wave mixing [19–23]. In these schemes, the quantum state of the signal beam is transferred to the idler beam at full conversion without excess noise [21]. Additionally, the phase of the pump beam is impressed onto the generated idler waveform [22], enabling engineered phase modulation of the wavepacket.

At the same time, researchers have been investigating temporal reshaping of photonic wavepacket, while preserving its quantum states [24–27]. Kielpinski et al. propose to use a well designed frequency-dependent dispersion function and temporal phase modulation to reconstruct the pulse shape [24]. McKinstrie et al. suggest reshaping the signal pulse profile using pump pulse that has slight mismatch in group velocity [28]. Both proposed schemes requires tailored dispersion functions that are highly depended on the details of original pulse shape.

Temporal imaging techniques have been developed by the ultrafast optics laser community for temporal rescaling of optical pulses [29–32]. They are the temporal analog of spatial imaging systems. As shown in Fig. 1, in a single-lens spatial imaging system, spatial Fourier components of light waves scattered from the object diffract into different angular directions. A lens encodes a quadratically-varying phase to each of these components according to the direction. The resulting Fourier components then diffract and recombine to form an image at the image plane. In a temporal imaging system, temporal Fourier components of light waves are dispersed into different temporal locations upon propagating in a medium characterized by a non-zero group velocity dispersion. The dispersed (or chirped) light wave is modulated by a temporally-varying quadratic phase, known as a “time lens.” Similarly, a temporal “image” is formed after a second dispersive medium recombines (or dechirps) the Fourier components in time.
II. QUANTUM THEORY FOR TEMPORAL IMAGING SYSTEMS

A. System design overview

The flying qubit interface consists of a single-lens imaging system and a field lens placed in the image plane, as shown in Fig. 2. An input wavepacket (denoted by the annihilation operator \( \hat{a}_0 \)) first propagates through a dispersive medium \( D_1 \). The dispersed wavepacket \( \hat{a}_1 \) then enters the time lens, which is constructed using a 3WM process in a crystal with a second-order nonlinear optical susceptibility \( \chi_2 \). The beam that pumps the 3WM process (field \( E_p' \)) has a quadratic phase \( \phi_p' \) obtained upon propagating through another dispersive material \( D_f \), which is encoded on the generated waveform \( \hat{a}_2 \) in the 3WM frequency down-conversion process. The phase-modulated wavepacket \( \hat{a}_2 \) then propagates through dispersive medium \( D_2 \) to dechirp (into \( \hat{a}_3 \)). Finally, a field lens (with quadratic phase \( \phi_p' \) on the pump filed \( E_p' \) obtained from dispersion \( D_f \)) frequency up-converts the wavepacket and removes the residual phase \( \theta_r \). We obtain a chirp free temporal image wavepacket \( \hat{a}_4 \). Here all \( D \)'s are the group delay dispersion \( D = \beta_2 L \), where \( \beta_2 \) and \( L \) are the group velocity dispersion (GVD) parameter and length of the dispersive material, respectively.

B. Quantum description of light propagating in a dispersive material

To explore the evolution of the annihilation operator \( \hat{a} \) for a photonic wavepacket propagating along the +z direction in a dispersive material, we expand the operator in the temporal \( t \) and frequency \( \omega \) domains as \[ \hat{a} = \int dt \hat{a}(t) = \int d\omega \hat{a}(\omega), \] (1)

where \( \hat{a}(t) \) and \( \hat{a}(\omega) \) are Fourier transform pairs and are the temporal and spectral profile annihilation operators of the mode, respectively. Dispersive propagation is best described in the frequency domain and is governed by \[ \frac{\partial \hat{a}(z,\omega)}{\partial z} = i \frac{\omega n(\omega)}{c} \hat{a}(z,\omega), \] (2)

where \( c \) is the speed of light in vacuum, and \( n \) is the refractive index of the material. For the case of small dispersion, \( \omega n(\omega)/c \) is expanded around the carrier frequency \( \omega_0 \) as

\[
\frac{\omega n(\omega)}{c} \approx \beta_0 + \beta_1 (\omega - \omega_0) + \frac{\beta_2}{2} (\omega - \omega_0)^2 + \ldots,
\] (3)

where \( \beta_i = \partial^i (\omega n(\omega)/c)/\partial \omega^n |_{\omega=\omega_0} \).

To second-order in the dispersion and ignoring absorption, the solution to the evolution equation Eq. (2) is...
FIG. 2. Abberation-corrected flying qubit interface consists of a single-lens imaging system and a field lens

given by
\[ \hat{a}(z, \omega) = \hat{a}(0, \omega)e^{i(1/2)\beta_2(\omega-\omega_0)^2z}, \]  
when moving in a reference frame traveling at speed \(1/\beta_1\).

We therefore obtain the results that
\[ \hat{a}_1(\omega) = \hat{a}_0(\omega)e^{iD_1(\omega-\omega_0)^2}, \]  
and
\[ \hat{a}_3(\omega) = \hat{a}_2(\omega)e^{iD_2(\omega-\omega_0)^2}. \]

C. Quantum theory of the time lens using the 3WM process

The time lens is constructed using a 3WM process in a \(\chi^2\) crystal. When pumped by a strong (classical) beam \(E_p(t) = A_p(t)e^{i\phi_p(t)}\) \((A_p\) and \(\phi_p\) being the amplitude and phase of the pump beam, respectively), the mode occurrence probability oscillates back and forth between the two co-propagating signal \(\hat{a}_s\) and idler \(\hat{a}_i\) beams as a result of sum-frequency and difference-frequency generation (SFG and DFG). When the phase matching conditions of frequency \(\omega\) and wavevector \(k\)

\[ \omega_i = \omega_s + \omega_p \]
\[ k_i = k_s + k_p \]

are fulfilled, the Hamiltonian for the process is expressed as

\[ H = \int dt \gamma E_p(t)a_s^\dagger(t)\hat{a}_i(t) + c.c., \]  
where the nonlinear coefficient \(\gamma\) is proportional to \(\chi^2\.

Note the pump is assumed to not be depleted and thus \(E_p\) remains unchanged throughout the process.

Solving the evolution equations of the wavepacket operators, namely
\[ \partial \hat{a}_s / \partial z = i[\hat{a}_s, H], \]
\[ \partial \hat{a}_i / \partial z = i[\hat{a}_i, H], \]
we find that the mode occurrence probabilities oscillate with the pump amplitude. Particularly, when the \(A_p\) reaches the critical value so that \(\gamma A_p L_c = \pi/2\), where \(L_c\) is the length of the crystal, the conversion efficiency becomes 100% and the optical field switches between two frequency modes, as expressed by
\[ \hat{a}_i(z, t) = i\hat{a}_s(0, t)e^{i\phi_p(t)} \]
\[ \hat{a}_s(z, t) = i\hat{a}_i(0, t)e^{-i\phi_p(t)} \]

By using such a non-amplifying process, the quantum state of the input signal waveform is transformed to the idler beam (or vice versa) and the phase (or conjugated phase) from the pump pulse is imposed onto the output beam as well [20, 21].

The result is applied to the time lens sections in the imaging systems. For the down-conversion time lens
\[ \hat{a}_2(t) = te^{-i\phi_p(t)}\hat{a}_1(0, t), \]
and for the up-conversion field lens
\[ \hat{a}_4(t) = te^{i\phi_p'(t)}\hat{a}_3(0, t). \]

D. A single-lens temporal imaging system with residual phase

We now consider the single-lens temporal imaging system with two dispersive elements \((D_1, D_2)\) and a time lens (characterized by \(D_f\)). The pump pulse \(E_p(t) = A(t)e^{i\phi_p(t)}\) has a quadratic phase \(\phi_p(t) = t^2/2D_f\), generated via propagating a short pulse through a dispersive element with total dispersion \(D_f\) [34].
Combining Eq. (5) and Eq. (9), the output wavepacket \( \hat{a}_3(\omega) \) at the image plane is expressed in terms of input wavepacket \( \hat{a}_0(\omega) \) by

\[
\hat{a}_3(\omega) = e^{i[D_2(\omega-\omega_0)^2/2]} \int dt e^{-i\omega t} e^{-it^2/2D_f} \\
\int d\omega' e^{i\omega' t} \hat{a}_0(\omega') e^{i[D_1(\omega'-\omega_0)^2/2]},
\]

(11)

Carrying out the integration over \( t \), we obtain

\[
\hat{a}_3(\omega) = e^{i[D_2(\omega-\omega_0)^2/2]} \\
\int d\omega' e^{i[-D_1(\omega-\omega')^2/2+D_1\omega'^2/2]i\theta_0(\omega')}.
\]

(12)

When the imaging conditions

\[
1/D_1 + 1/D_2 = 1/D_f \\
-D_2/D_1 = M
\]

(13)

are fulfilled, taking a Fourier transform of \( \hat{a}_3(\omega) \) and carrying out the integration over \( \omega \), result in the simplified expression

\[
\hat{a}_3(t) = -i\sqrt{M} \hat{a}_0(0, t/M) e^{i\theta_0(t)},
\]

(14)

where the output temporal profile is magnified by a factor \( M \) and a quadratic phase \( \theta_0 = t^2/(2MD_f) \) is left in the waveform.

III. RESIDUAL PHASE CORRECTION SCHEMES AND COMPARISON

The quadratic residual phase \( \theta_0 \) results from the temporally curved wave front at the image plane, analogous to the spatial image aberration known as Petzval field curvature (shown in Fig. 3(a)). Petzval field curvature cannot be corrected in a single-lens imaging system, while other types of aberration such as spherical aberration can be corrected by a well-designed lens [35]. Similarly, we have quadratic residual phase in a single-lens temporal imaging system. (Note that astigmatism and coma do not appear in a temporal imaging system due to its 1-D nature.) Since phase does not affect the intensity profile, it is not often considered in classical applications. Residual-phase free temporal imaging is discussed by using a telescope in Ref. [31]. In quantum information processing, it is important to faithfully preserve the phase profile of photonic wavepacket.

A. Three configurations to solve the residual phase problem

One method is to reduce the residual phase using larger dispersions, equivalent to “far-field imaging” in spatial imaging systems. In far-field imaging, the variation of \( \theta_0 \) is reduced across the output waveform duration time as a result of the reduced curvature of the wavefront at the image plane, shown for the analogous spatial imaging system in Fig. 3(b).

A possible method to fully correct for the residual phase is to include a second lens, known as a field lens, in the image plane as shown in Fig. 2 and Fig. 3(c). Note that we can set the field lens at the temporal image plane while still spatially separating the imaged waveform from the lens via non-dispersive propagation. If the pump pulse of the field-lens is dispersed by an amount of \( D_f = MD_f \), a phase modulation \( \phi_p(t) = -\theta_0(t) \) will be generated and imposed on the wavepacket. The resulting output image wavepacket is given by Eq. (14) and Eq. (10) as

\[
\hat{a}_4(t) = e^{i\phi_p(t)} \hat{a}_3(t) = \frac{1}{\sqrt{M}} \hat{a}_0(0, t/M),
\]

(15)

where a constant \( \pi \) phase is ignored. We see that the residual phase is eliminated, the quantum state of the input field is transferred to the output field and the temporal profile is extended by the factor \( M \). The wavelength of the single photon will be properly converted by choosing the appropriate crystal and pump-beam carrier wavelength.

A third approach is to use the temporal telescope system [31], as shown in Fig. 3(d). This configuration consists of two time lenses (with focal dispersions \( D_{f1} \) and...
$D_1$, $D_2$, and $D_3$). With similar derivation, we find that an image with magnification $M$ is formed when

$$D_1 = -D_1,$$

$$D_3 = -D_{f_2} = -MD_1,$$

$$D_2 = D_1 + D_3. \tag{16}$$

The output wavepacket is given by

$$\hat{a}_4(t) = \frac{1}{\sqrt{M}} \hat{a}_0(0, \frac{t}{M}), \tag{17}$$

where the residual phase is eliminated.

B. Comparison of three configurations with a single Gaussian pulse

We now analyze the imaging of a single Gaussian pulse using the three configurations and compare numerically the required dispersion and bandwidth. Consider an input single-photon wavepacket with a Gaussian profile

$$\hat{a}_0(t) = \hat{a}(t)e^{-2\ln 2(t/t_0)^2}, \tag{18}$$

where $\hat{a}(t)$ is the annihilation operator of the quantum mode, $t_0$ is the full width at half maximum (FWHM) of the input temporal profile. In the single-lens imaging system, according to Eq. (14), the output photonic wavepacket is

$$\hat{a}_3(t) = \hat{a}(t)e^{-2\ln 2[(t/(Mt))]/2}e^{it^2/(2MD_f)}. \tag{19}$$

The width of the pulse is expanded to $t_o = Mt_i$. The residual phase $\Delta \phi = t^2/(2MD_f)$ varies by an amount of

$$\Delta \phi = Mt_i^2/(8D_f), \tag{20}$$

over the temporal duration of the output waveform $t_o$. The quadratic phase can be neglected when \[ |\Delta \phi| \ll \pi. \tag{21} \]

Achieving this far-field criterion or Fraunhofer condition requires that $|D_f| \gg \pi Mt_i^2/8$. According to Eq. (13), we require that $|D_1| \gg \pi(M + 1)t_i^2/8$ and $|D_2| \gg \pi t_i^2/8$. These dispersion values quickly become large with increasing output temporal width $t_o$. For example, if a 100-ps pulse is desired at the output, we require $|D_2| \gg 3,900$ ps$^2$. Note that 3,900 ps$^2$ corresponds approximately to the total dispersion of a 200-km SMF-28 optical fiber at 1550 nm. The required dispersion needs to be much larger, which is difficult to realize despite various efforts to make large-dispersion devices for narrow band optical pulses. Popular approaches include virtually imaged phased arrays (VIPA) [37], multimode dispersive fibers [38], chirped volume holographic gratings [39] and chirped fiber grating [40]. Nevertheless, it is challenging to obtaining a total dispersion exceeding 1,000 ps$^2$, which is often accompanied by non-ideal characteristics, such as high loss, higher-order dispersion and group-delay ripple \[20 \tag{21}]\tag{41}. For example, a 200-km SMF-28 fiber at 1550 nm has a transmission of only 10$^{-4}$. Such huge loss will have serious consequences for successful quantum state transfer. These challenges limit this aberration correction method to applications requiring pulse in the ps range or shorter.

On the other hand, according to Eq. (15) and Eq. (17), the output wavepacket $\hat{a}_4$ in both the field lens and the telescope configurations are given by

$$\hat{a}_4(t) = \hat{a}(t)e^{-2\ln 2(t/(Mt))}/2). \tag{22}$$

eliminating the residual phase independent of the scale of the dispersions.

As a result, arbitrarily small dispersions can be used until bandwidth broadening induced by strong (heavily chirped) time lenses hits the bandwidth limit. In spatial imaging systems, we can move all components closer (less diffraction) and maintain good imaging with shorter focal-length lenses. Similarly, systems built with smaller dispersions require larger quadratic phase modulation. However, strong phase modulation will expand the spectral bandwidth of the optical pulses, which may eventually exceed the available bandwidth of the pump source and/or bandwidth of the 3WM process. The practical bandwidth $\Delta \nu$, therefore, determines the limit of the dispersions in these two temporal imaging configurations, which is much reduced compared to the far-field approach. The spectral bandwidth of the chirped pump pulse is estimated by taking the Fourier transform of the pump waveform. Assuming a Gaussian pump pulse with temporal width $t_i$ and a quadratic phase $\phi_p(t)$ described by

$$E_p(t) = e^{-2\ln 2(t^2)/2}e^{it^2/2D_f}, \tag{23}$$

the spectral bandwidth (FWHM) of this pulse is $\Delta \nu = t_i/D_f$. (Small dispersion $|D_1| \ll t_0^2$ is assumed, so that the input signal pulse $\hat{a}_1$ is not significantly broadened and maintains the temporal width $t_i$.) The lower limit of dispersion is set by the available bandwidth $|D_f| > t_i/\Delta \nu$. Limits for the other dispersions are obtained via Eq. (13) and summarized in Table 1.

As an example, consider magnifying a 5-ps input waveform at 710 nm to 100 ps. Pump pulses of bandwidth $\Delta \nu = 1 \times 10^{12}$ rad/s (roughly twice the spectral width of the input pulse) at 1550 nm are used as temporal lenses. The input signal is first converted to 1310 nm, and after $D_2$, converted back to 710 nm via the field lens. In this configuration, the required dispersions are

- $D_1@710$ nm: 5.25 ps$^2$,
- $D_3@710$ nm: 105 ps$^2$,
- $D_2@1550$ nm: 5 ps$^2$,
- $D_3@1550$ nm: -100 ps$^2$.
The largest dispersion is 105 ps$^2$, well within reach for typical dispersion devices. These parameters can be obtained using the following off-the-shelf fiber-based dispersive components:

- $D_1$, 73 m of SM600 fiber,
- $D_2$, 6.2 km of LEAF fiber,
- $D_f$, 0.13 km of VascadeS1000 fiber,
- $D_r$, 5.5 km of SMF28 fiber.

A input wavepacket will go through dispersion material $D_1$ (loss=0.7 dB) and $D_2$ (loss=2.1 dB), with total loss of 2.8 dB. We see that the system now has much less loss, which can be further reduced using special low-loss dispersion compensation fiber for 1310 nm and 710 nm.

A similar procedure is used to analyze the telescope configuration. The results of the dispersion and bandwidth bounds are listed in Table 1. We find that the telescope configuration uses similar dispersions as the field lens configuration. In both cases, the largest dispersion is $|D_2| > (M + 1)t_i/\Delta\nu$, substantially lower compared to the far-field criterion ($|D_2| \gg \pi t_i^2/8$). The telescope system requires one additional large dispersion element $D_3$ compared to the field lens approach which achieves complete residual phase correction with fewer components and less loss.

**IV. APPLICATION: QUANTUM TEMPORAL IMAGING OF A TIME-BIN ENTANGLED STATE**

As an example application of a quantum temporal imaging system, we consider a time-bin entangled coherent photon wavepacket, prepared by splitting a coherent faint laser pulse using a Franson interferometer (shown in Fig. 4). The input wavepacket is a coherent state with a double-Gaussian profile given by

$$\hat{a}_0(t) = \frac{1}{2} A_+ (t/M) \hat{\alpha}(t) + \frac{1}{2} e^{i\psi} A_-(t/M) \hat{\alpha}(t)$$  \hspace{1cm} (24)

where

$$A_{\pm} (t) = e^{-2n_2 (t/\tau \pm \delta)^2},$$  \hspace{1cm} (25)

$$\hat{\alpha}(t) = \exp(\hat{a}^\dagger - \hat{a}),$$

is the coherent state operator, $\tau$ is the width of the Gaussian profile (FWHM), $\Delta t = 2d\tau$ is the propagation delay in the interferometer, and $\psi$ is the phase difference between the entangled time bins. The total temporal width of the pattern can be defined as $t_i = \Delta t + \tau$.

The image waveform of the time-bin entangled photonic wavepacket is given by Eq. (15)

$$\hat{a}_4 = \frac{1}{2\sqrt{M}} A_+ (t/M) \hat{\alpha}(t) + \frac{1}{2\sqrt{M}} e^{i\psi} A_- (t/M) \hat{\alpha}(t)$$  \hspace{1cm} (26)

As shown in Fig. 4 we split and recombine the output image wavepacket through another unbalanced interferometer, where the time difference and phase between the two paths are adjusted to $M\Delta t$ and $\psi'$. The output temporal waveform is expected to be a three-peak profile with interference in the central peak. Constructive interference happens when $|\psi - \psi'| = 0$, while destructive interference happens when $|\psi - \psi'| = \pi$. Since interference pattern crucially depends on the phase, a complete true imaging of the phase information encoded in the original time-bin qubit requires that the residual phase is small throughout the image temporal profile.

We numerically simulate the evolution of the waveform using Eq. (15). In the simulation, we set $\tau = 5$ ps, $t_i = 20$ ps, pump pulse initial width $\tau_p = 0.5\tau$ (pump
FIG. 5. Interference pattern of a temporal imaged time-bin entangled photon wavepacket. (a) Input waveform and perfect image waveform. (b)-(d) Interference pattern after the second interferometer, simulated for the single-lens imaging system (b), telescope system (c) and field lens system (d). Blue solid line shows the constructive interference pattern when $|\psi - \psi'| = 0$, red dashed line shows the destructive interference pattern when $|\psi - \psi'| = \pi$. The visibility $v$ is calculated for the central peak. We obtain $v = 0.984$ for field lens and $v = 0.986$ for the telescope system, while in the single lens system, fast varying residual phase washes out the visibility.

FIG. 6. Intensity profile aberrations. (a) Simulated image waveforms using the single-lens imaging system (blue dot-dash), telescope system (green dot) and field lens system (red dash), which are almost identical to each other and closely match the expected perfect output waveform (black solid). (b) Output waveforms in two severe-distorted situations, insufficient bandwidth $\tau_p = \tau$ (red dash) and large third-order dispersion $\beta_3/\beta_2 = 1$ ps$^{-1}$ (blue dot-dash), compared to the expected perfect output waveform (black solid).

V. CONCLUSION

We demonstrate a quantum temporal imaging system that allows us to simultaneously match the wavelengths of two quantum memories and match their characteristic time scales, enabling exchange of quantum information between different quantum platforms such as quantum dots and ions. A field lens in the image plane eliminates the residual phase in the temporal imaging system. When applied to a time-bin entangled photonic wavepacket, the image waveform has good interference visibility, which demonstrates that the field lens configuration is a good candidate for phase-sensitive quantum
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