Stereodynamic control of overlapping resonances in cold molecular collisions

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Stereodynamic control of resonant molecular collisions has emerged as a new frontier in cold molecule research. Recent experimental studies have focused on weakly interacting molecular systems such as HD collisions with H_2, D_2, and He. We report here the possibility of such control in strongly interacting systems taking rotational relaxation in cold collisions of HCl and H_2. Using explicit quantum scattering calculations in full six dimensions it is shown that robust control of the collision dynamics is possible even when multiple (overlapping) shape resonances coexist in a narrow energy range, indicating that cold stereochemistry offers great promise for many molecules beyond simple systems. We demonstrate a striking case where two prominent peaks in overlapping resonances are switched off simultaneously by suitable alignment of the HCl molecule.

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Recent progress in cooling and trapping molecules below 1 K has led to new insights into chemical dynamics, quantum information processing, quantum simulation, and the test of fundamental physics beyond the standard model [1–10]. In particular, the ability to prepare molecules in selected motional, internal, and orientational quantum states has allowed interrogation of molecular events with unprecedented precision. The suppression of higher-order angular momentum partial waves in cold collisions provides an ideal platform to explore state-to-state chemistry with partial wave resolution.

A series of papers by Perreault et al. [11–13] laid the groundwork for cold stereodynamics [14–17] by combining cold molecular beam technology and coherent optical control of molecular states. They demonstrated stereodynamic control of rotational quenching of vibrationally excited HD (ν = 1, j = 2) in cold collisions with H_2, D_2, and He [11–13] in a single molecular beam. The initial molecular state of HD, including the bond axis alignment, was prepared by Stark-induced adiabatic Raman passage (SARP) [18,19]. The quenching rate and angular distribution were found to vary significantly depending on whether the HD bond axis is preferentially aligned horizontal (H-SARP) or vertical (V-SARP) to the initial relative velocity vector between the collision partners, providing conclusive evidence of strong stereodynamic effect in HD+H_2/D_2 collisions near 1 K.

While the collision energies involved in the experiment are narrow (<5 K) and only a limited number of partial waves (~l < 5) is involved, the experiments do not provide energy or partial wave resolution directly. In a subsequent theoretical study Croft et al. [20] attributed the key feature of the angular distribution of the rotationally deexcited HD to an incoming d-wave (l = 2) shape resonance centered at about 1 K. The role of isolated (shape) resonances in controlling quenching rate and overall angular distribution of the products was further explored in theoretical studies of HD+H_2 [21,22] and in recent experiments on HD+He [13].

In addition to H-SARP and V-SARP, Perreault et al. [13] illustrated an X-SARP orientation in which the HD bond axis is prepared in a superposition state with axis orientation of 45° with respect to the collision velocity. Indeed, an explicit stereodynamic control was demonstrated in their experiments as the bond-axis orientation was varied discretely from 0° to 45° to 90° with respect to the collision velocity. This was generalized to an arbitrary orientation of the HD bond axis by Croft and Balakrishnan [21] and Jambriña et al. [22] for HD+H_2, achieving further control of the stereodynamics by preparing appropriate superposition states of the HD rotational state. We note that the SARP technology has the capability to achieve such flexible control of molecular states and it is applicable to a broad class of molecules including those with no permanent electric dipole moment [18,23].

These advances now allow controlled studies of molecular collisions and chemical reactions using fully tailored molecular initial rovibrational states (ν, j, m) and their coherent superpositions, where m is the projection of j onto a quantization axis. Such investigations of systems beyond HD+H_2, HD+D_2, and HD+He are crucial to unveil whether the stereodynamic control is possible for broader classes of molecules with stronger intermolecular interactions. In particular, the existence and possible control of any stereodynamic effect in the presence of multiple (overlapping) resonances in cold collisions remain to be addressed.

In this Rapid Communication, we examine this question by tackling rotational quenching of HCl by collisions with H_2 in the subkelvin regime based on full-dimensional quantum scattering calculations on a recently reported ab initio
potential energy surface (PES) [24]. This system is of current experimental interest in Zare’s group (private communication). In comparison with HD, the HCl molecule is strongly dipolar (dipole moment \( \sim 1.08 \) D) and is amenable to high optical controllability of its internal states. The HCl+H2 interaction potential is deeper and more anisotropic [24] leading to strong coupling between the different rovibrational channels at short range. The small rotational constant of HCl (a factor of 5 smaller than HD) also contributes to the increased density of states and more complex collision dynamics for the HCl+H2 system.

Details of the ab initio PES for HCl+H2 and its analytical representation have been reported previously [24]. Briefly, the PES consists of a short-range part fit to high-level ab initio data and a long-range part giving an accurate description of the electrostatic and dispersion interactions. The depth of the interaction potential well is \( \sim 216 \) cm\(^{-1}\), significantly deeper than that between two H2 molecules (\( \sim 35 \) cm\(^{-1}\)). The time-independent Schrödinger equation for the molecular scattering is numerically solved using the close-coupling method as implemented in the TwoBC code [25,26]. More details of the computational approach can be found in previous publications [20,21,24] and we limit our discussions to key notations and essential formulas.

The state-to-state differential cross section (DCS) for isotropic collisions (no polarization) in the helicity representation is given by [27]

\[
\frac{d\sigma_{\alpha \rightarrow \alpha'}}{d\Omega} = \frac{1}{2(j_1 + 1)(2j_2 + 1)} \sum_{k_1,k_2,k_1',k_2'} |q_{\alpha,k_1,k_2 \rightarrow \alpha',k_1',k_2'}|^2,
\]

where \( \alpha \equiv v_1 j_1 v_2 j_2 \) and \( \alpha' \equiv v'_1 j'_1 v'_2 j'_2 \) refer to the initial and final combined molecular rovibrational states, respectively, \( d\Omega \) is the infinitesimal solid angle, and the subscript 1 refers to HCl and 2 to H2. The quantum number \( k/k' \) is the projection of the initial/final molecular rotational angular momentum \( j/j' \) onto the body-fixed (BF) \( z \) axis. The \( \theta \) dependence in the scattering amplitude is given as [20,21,27]

\[
q_{\alpha,k_1,k_2 \rightarrow \alpha',k_1',k_2'} = \frac{1}{2k_0} \sum (2J + 1) \sum_{j_{12},j_{12}',k_{12}} i^{j_{12}+1} T_{\alpha,j_{12},\alpha',j_{12}'}(E) d_{k_{12},k_1,k_2}^{j_{12}}(\theta)
\times \langle j'_1 j'_2 k'_1 j'_2 k'_1 k'_2 | j_{12} k_{12} j_{12} k_{12} | 00 \rangle
\times \langle j_{12} k_{12} j_{12} k_{12} | j_{12} k_{12} j_{12} k_{12} \rangle,
\]

where \( k_0 \) is the wave number for the incident channel, and \( J \) is the quantum number of the total angular momentum of the collision complex defined as \( J = j_{12} + \frac{I}{2} \) with the combined rotational angular momentum \( j_{12} \) of the two molecules given by \( j_{12} = j_1 + j_2 \) and the relative orbital angular momentum \( I \) between the collision partners. The \( T \) matrix is given in terms of the \( S \) matrix as \( T = 1 - S \). \( E \) is the total energy, and \( d_{k_{12},k_1,k_2}^{j_{12}}(\theta) \) is the Wigner’s reduced rotation matrix, and the bracket \( \langle | \rangle \) denotes a Clebsch-Gordan coefficient. We note that \( k_{12} \) and \( k_{12}' \) in Eq. (2) mean \( k_1 + k_2 \) and \( k_1' + k_2' \), respectively.

By taking the integral of the DCS in Eq. (1) over \( \theta \) and \( \phi \) one obtains the state-to-state integral cross section (ICS) as [24,26,27]

\[
\sigma_{\alpha \rightarrow \alpha'}(E) = \frac{\pi}{(2j_1 + 1)(2j_2 + 1)k_0^2} \times \sum_{j_{12},j_{12}',l} (2J + 1) \delta_{\alpha,j_{12},\alpha',j_{12}'} - S_{\alpha,j_{12},\alpha',j_{12}'}(E)|^2.
\]

Equations (1) and (3) include averaging over all possible initial orientations of the molecular rotational states specified by the projections \( k_1 \) and \( k_2 \). Our primary goal is to explore the effect of aligning the HCl bond axis relative to the initial relative velocity vector for the collision (BF \( z \) axis), as explored in previous studies of HD [11,12,21,22]. In this scheme the initial rotational state of HCl is prepared as \( |j_1, m_1 = 0 \rangle \) by the laboratory fixed SARP laser where \( m_1 \) is the projection of \( j_1 \) onto the linear polarization direction of the SARP laser. The prepared state \( |j_1, m_1 = 0 \rangle \) can be expressed as a coherent superposition of a set of states \(|j_1, k_1 \rangle \) specified by the projection \( j_1 \) onto the BF \( z \) axis as [21]

\[
|j_1, m_1 = 0 \rangle = \sum_{k_1 = -j_1}^{j_1} d_{\alpha,0,0}^{j_1}(\beta)|j_1, k_1 \rangle,
\]

where \( \beta \) is the angle between the aligned HCl bond axis and the initial relative velocity vector for the collision.

For rotational quenching of aligned HCl by cold collision with para-H2 \((v_2 = 0, j_2 = 0, k_2 = 0)\), the state-to-state DCS with respect to the scattering angle \( \theta \) is given by [21]

\[
\left( \frac{d\sigma}{d\theta} \right)_\beta = 2\pi \sin \theta \sum_{k_1 = -j_1}^{j_1} \left| d_{\alpha,0,0}^{j_1}(\beta) \right|^2 |q_{\alpha,k_1,0 \rightarrow \alpha',k_1',0}|^2,
\]

where it is assumed that, like in previous experiments [11–13], the rotationally deexcited HCl molecules in a specific rotational state \( (j'_1) \) are detected with no resolution of their \( k_1' \) or azimuthal angle \( \phi \). The overall effect of the alignment of the HCl molecules is captured in the weight factor \( |d_{\alpha,0,0}^{j_1}(\beta)|^2 \) for each \( |q| \) term associated with an initial \( k_1 \). The behavior of \( |d_{\alpha,0,0}^{j_1}(\beta)|^2 \) as a function of \( \beta \) for \( j_1 = 2 \) is displayed in Ref. [21] (see also Fig. S1 in the Supplemental Material [28]).

First we discuss rotational quenching of HCl \((v_1 = 1, j_1 = 2) \rightarrow (v_1' = 1, j_1' = 0)\) by collisions with para-H2 \((v_2 = 0, j_2 = 0, k_2 = 0)\), namely, \( \Delta j = -2 \). The ICS for isotropic collisions is shown by the dashed curve in Fig. 1. Contributions from different incoming partial waves \( l = 0 \) to \( l = 3 \) are also shown. It is seen that a pronounced peak at about a collision energy of \( E_C = 0.3 \) cm\(^{-1}\) has the main contribution (77%) from an incoming \( p \)-wave \((l = 1) \) and a smaller contribution from an incoming \( f \)-wave \((l = 3) \). The quasibound states due to closed channels are inaccessible at these collision energies (see Fig. S2 in the Supplemental Material [28]), thus the observed resonance is a \( p \)-wave shape resonance.

We note that a \( p \)-wave shape resonance was not observed for HD+para-H2 collisions [20–22], indicating that cold HCl+H2 collisions exhibit markedly different features compared to HD+H2. Indeed, the adiabatic potential energy curves for HCl+H2 are much more complicated [28] than those of HD+H2 [20].
We now discuss how to control this resonance by the preparation of initial alignment of the HCl bond axis. The ICS in the resonance region with and without initial alignment of HCl is shown in Fig. 2(a) using linear axis scale. The dashed curve (isotropic) is identical to the dashed curve (Total) in Fig. 1. Other solid curves correspond to different alignment angles of the HCl bond axis with respect to the initial relative velocity vector for the collision, obtained by integrating the corresponding DCS over $\theta$ from 0 to $\pi$ in Eq. (5). The cross section varies almost monotonically by a factor of 3 as $\beta$ increases from 0$^\circ$ to 90$^\circ$, indicating the feasibility of robust control of quenching rate by changing the angle of alignment.

As shown in Eq. (5), the DCS and the resultant ICS are given as the sum of terms specified by the different projection component $k_1$ of $j_1$. Therefore, the observed trend of the ICS in terms of $\beta$ can be effectively analyzed by examining the ICS with initially oriented HCl specified by a projection $k_1$ [Fig. 2(b)]. Note that the result for $k_1 = 0$ is the same as $\beta = 0$ in Fig. 2(a). The cross sections for other values of $k_1$ are relatively suppressed in the resonance region. In particular, a shallow dip is observed for $|k_1| = 2$.

The above findings indicate that the sensitive dependence of the dynamics in the resonance region to the initial orientation (specified by $k_1$) of HCl can cause dramatic change in collision outcome. Compared to $|k_1| = 2$, the ICS for $k_1 = 0$ is about 12-fold larger at the peak of the resonance ($E_C = 0.3$ cm$^{-1}$). Since the projections of the final rotational states are $k'_1 = 0$ and $k'_2 = k_2 = 0$ due to $j'_2 = 0$ and $j_2 = j_2 = 0$, collisions with $k_1 = 0$ conserve helicity as $k_1 + k_2 = k'_1 + k'_2 = 0$ and the resonance enhancement can be attributed to a helicity conserving transition. It is worth pointing out that results in Fig. 2(a) do not reflect the full potential of stereodynamic control. If it is possible to specifically prepare an initial HCl rotational state with $k_1 = 2$ or $k_1 = -2$, or their linear combination, the resonance can be completely switched off. Recent advances in SARP techniques have made progress in this direction [13,19]. Indeed, preparation of a phase-locked superposition of $k_1 = \pm 1$ states, $\sqrt{1/2}(|j_1 = 2, k_1 = 1\rangle + |j_1 = 2, k_1 = -1\rangle)$, termed X-SARP, was demonstrated for HD [13], expanding the range of control achievable using SARP techniques. The range of control expands into the nonresonant region for the DCS as shown in the Supplemental Material [28].

Next we examine $\Delta j_1 = -1$ transition in HCl, i.e., $(v_1 = 1, j_1 = 2) \rightarrow (v'_1 = 1, j'_1 = 1)$. Figure 3 presents the total and partial wave resolved ICSs for this process for the isotropic case. The crucial difference here in comparison with Fig. 1 is the enhanced incoming $f$-wave contribution at around 0.4 cm$^{-1}$ in addition to a strong $p$-wave resonance at about 0.15 cm$^{-1}$ leading to two prominent peaks. While the two resonances appear as distinct peaks in close proximity we note that the $p$-wave peak has a small contribution from the $f$-wave resonance illustrating the complex nature of the dynamics and partial overlap of these resonances. This brings up an important question that has not been addressed before: Can
stereodynamic control be effective for such overlapping resonances associated with multiple partial waves? In previous studies of HD+$\text{H}_2$, HD+$\text{D}_2$, and HD+$\text{He}$, the stereodynamic effect was attributed to the characteristics of a specific isolated shape resonance. However, such simplicity is not necessarily expected for the vast majority of systems due to the higher density of states caused by the stronger interaction and/or heavier mass.

As shown in Fig. 4(a) the angle ($\beta$) between the aligned HCl bond axis and the initial relative velocity vector for the collision has a strong effect on the magnitude of both resonances. However, some notable differences are also visible compared to the $\Delta j_1 = -2$ transition [Fig. 2(a)]. In Fig. 4(a), the $f$-wave shape resonance peak increases in intensity with increasing $\beta$ from $0^\circ$ to $90^\circ$, just the opposite of the trend observed for the peak in the $\Delta j_1 = -2$ transition. The $p$-wave peak at lower energy increases in intensity with increasing $\beta$ but it saturates at around $50^\circ$ before eventually decreasing with increasing $\beta$ (from $70^\circ$ to $90^\circ$). Nevertheless, both resonances exhibit a considerable range of control by the alignment preparation. In particular, with a small value of $\beta$ ($< 10^\circ$), both peaks are essentially switched off.

To gain more insights into the two resonances Fig. 4(b) presents the ICS with different initial HCl orientations. The cross section for $k_1 = 0$ is the smallest near the resonance peaks and exhibits a small bump near $0.3$ cm$^{-1}$, the region in between the two resonances. On the other hand, we observe two intense peaks with $|k_1| = 1$ and $2$, revealing the origin of the overlapping resonances. Unlike the $\Delta j_1 = -2$ results shown in Fig. 2(b), $|k_1| = 2$ gives the largest cross sections while it does not conserve the helicity ($k_1 + k_2 \neq k'_1 + k'_2$). It means that the resonances for $\Delta j_1 = -2$ and $\Delta j_2 = -1$ transitions do not share the same mechanism. While the interaction potential does not directly contribute to a change in the helicity $k_1 + k_2$, the centrifugal term can induce it (Coriolis coupling), and the combined effect of these terms determines the resulting resonance profile. Recent studies of molecular reaction and spin-relaxation in the cold energy regime have also pointed out that approximate calculations assuming the conservation of helicity tend to fail in resonance regions [29,30].

In summary, we have demonstrated flexible and robust control of resonant rotational quenching of HCl in cold collisions with H$_2$ at the level of integral cross sections and rates by preparing HCl in an aligned or oriented state in the $v = 1$ vibrational level. The most striking result of our study is that even multiple peaks due to resonances associated with disparate partial waves can be controlled, indicating that stereodynamic control is not limited to simple systems with isolated resonances. Our results also reveal the importance of helicity-nonconserving transitions in stereodynamic control of resonant molecular collisions. The analysis based on the initial orientations of the HCl rotational state demonstrates the enormous potential controllability in cold molecular collisions, which is tractable with current experimental techniques.

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