

TOWARDS TRUSTWORTHY MULTI-LABEL SEWER DEFECT CLASSIFICATION VIA EVIDENTIAL DEEP LEARNING

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ABSTRACT

An automatic vision-based sewer inspection plays a key role of sewage system in a modern city. Recent advances focus on utilizing deep learning model to realize the sewer inspection system, benefiting from the capability of data-driven feature representation. However, the inherent uncertainty of sewer defects is ignored, resulting in the missed detection of serious unknown sewer defect categories. In this paper, we propose a trustworthy multi-label sewer defect classification (TMSDC) method, which can quantify the uncertainty of sewer defect prediction via evidential deep learning. Meanwhile, a novel expert base rate assignment (EBRA) is proposed to introduce the expert knowledge for describing reliable evidences in practical situations. Experimental results demonstrate the effectiveness of TMSDC and the superior capability of uncertainty estimation is achieved on the latest public benchmark.

Index Terms— Trustworthy visual inspection, evidential deep Learning, multi-label sewer defect classification, sewer pipelines

1. INTRODUCTION

Underground sewage system is one of the most vital lifelines in a modern city [1], which can guarantee the community health, safety, and manufacture. Vision-based inspection method is widely applied to maintain the underground sewage system [2]. The internal situations across the sewer pipes can be captured via a remote mobile vehicle, while the sewer inspectors diagnose the defects with a long time of looking at a screen. Such manual inspection is not only laborious and time-consuming, but also may cause ophthalmic diseases during the high-frequency illumination of the screen. Consequently, how to construct an automatic sewer inspection method has long been a research topic attracting constant attention in the field of sewer inspection [3].

Recently, deep learning model has received substantial interest in industrial applications [4, 5, 6]. In the vision-based sewer inspection community, deep learning also attracts increasing attention from both academia and industry [7, 8, 9]. Here, we focus on the sewer defect classification in the setting of multi-label, in which multiply defect classes in an image are recognized simultaneously. Although these deep learning-based methods have achieved acceptable performances in sewer defect classification, the inherent uncertainty of sewer defects might not be considered sufficiently in real-world applications [10]. For instance, some categories of sewer defects might not appear in historical data, in sense that, the trained sewer defect classification model has not seen these unknown defects which are the samples out of knowledge. Existing deep learning-based methods [7, 8, 11, 12] for sewer defect classification could not describe the magnitude of epistemic uncertainty across known and unknown sewer defect categories. The model would be over-confident to “trust” the prediction, resulting in the missed detection of serious unknown sewer defect categories.

In this paper, we propose a trustworthy multi-label sewer defect classification (TMSDC) method for unknown sewer samples setting. To enable the multi-label sewer defect classification model to “know unknown”, we cast the task as an uncertainty estimation problem via evidential deep learning (EDL) [13]. EDL describes the uncertainty via a Dirichlet distribution of class probability, which can be seen as an evidence collection process via a deep neural network. The collected evidence is leveraged to quantify the uncertainty of sewer defect prediction, for instance, unknown sewer defects would present a high uncertainty explicitly. Moreover, we introduce the expert knowledge to model the uncertainty and propose an expert base rate assignment (EBRA), in which the realistic base rate can provide reliable diagnosis of sewer defects in practical situations [14]. It is noteworthy that TMSDC can quantify the uncertainty effectively of model whose capability of distinguishing the known categories would only be weakened slightly. The main contributions are summarized as follows:

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A novel expert base rate assignment (EBRA) is proposed to model reliable evidences in practical situations via expert knowledge.

The effectiveness of TMSDC is demonstrated with diverse metrics on Sewer-ML [9] which is a large-scale public benchmark in the field of sewer inspection.

2. METHODOLOGY

TMSDC aims to quantify the uncertainty of sewer defect predictions via EDL in a deep learning-based paradigm, ensuring the reliable performance of multi-label sewer defect classification. The overall framework of our proposed method consists of deep feature extraction and deep evidence-based uncertainty estimation, as illustrated in Fig. 1. Specifically, given a sewer pipe image x whose feature map \( f \in \mathbb{R}^{C \times H \times W} \) is first obtained via a deep learning-based feature extractor \( F \) as follows:

\[
\mathbf{f} = F(\mathbf{x}|\theta_F),
\]

where \( \theta_F \) denotes the learnable parameters of feature extractor, \( C \) is the number of channels and \( H \times W \) is the resolution. Then, an evidential generation module is modeled to collect the deep evidence of sewer defect classes, in which the sewer defect probability is assumed to follow a Dirichlet distribution.

Formally, the evidence \( \mathbf{p}_k \) and uncertainty \( \mathbf{u}_k \) of \( K \) sewer defect classes can be formulated via the evidential generation module (EGM) \( G \) as follows:

\[
\{ \mathbf{e}_K, \mathbf{u}_K \} = G(\mathbf{f}|\theta_G, \text{Dir}(\mathbf{p}_K|\mathbf{\alpha}_K), \hat{\omega}),
\]

where \( \theta_G \) presents the learnable parameters of the EGM. \( \text{Dir}(\mathbf{p}_K|\mathbf{\alpha}_K) \) is a Dirichlet distribution, \( \mathbf{p}_K \) and \( \mathbf{\alpha}_K \) are the predicted probability and the Dirichlet parameter, respectively. \( \hat{\omega} \) denotes a subjective opinion adjusted via EBRA.

2.1. Deep evidence-based uncertainty

**Evidential Deep Learning.** Recent EDL [13] is widely utilized to estimate the uncertainty of classification results [15, 16], introducing the evidence framework of Subjective Logic (SL) [14]. SL defines a subjective opinion by explicitly considering the dimension of uncertainty derived from evidence vacuity. Here, we first describe the original EDL for classification with \( K \) categories. A subjective opinion for a sample with \( K \)-dimensional class domain can be first formulated as a triplet \( \omega = (\mathbf{b}, \mathbf{u}, \mathbf{a}) \) consisting of the belief mass \( \mathbf{b} = \{b_1, b_2, \ldots, b_K\} \), the uncertainty \( \mathbf{u} \), and the base rate distribution \( \mathbf{a} = \{a_1, a_2, \ldots, a_K\} \). For the \( k \)-th dimensional class, the probability mass \( p_k \) of the subjective opinion \( \omega \) is defined as:

\[
p_k = b_k + a_k u.
\]

Since \( p_k \) should be treated as a probability, the entities of \( \omega \) are constrained by \( u + \sum_{k=1}^{K} b_k = 1 \) and \( \sum_{k=1}^{K} a_k = 1 \). Formally, the probability mass \( \mathbf{p} \) of \( \omega \) follows a Dirichlet distribution with parameter \( \mathbf{\alpha} = \{a_1, a_2, \ldots, a_K\} \):

\[
\text{Dir}(\mathbf{p}|\mathbf{\alpha}) = \frac{1}{B(\mathbf{\alpha})} \prod_{k=1}^{K} p_k^{\alpha_k-1} \quad \text{for} \; \mathbf{p} \in S_K,
\]

where \( B \) is the Beta function, and \( S_K = \{\mathbf{p}|\sum_{k=1}^{K} p_k = 1 \text{ and } p_k \in [0,1], \forall k\} \) is the \( K \)-dimensional unit simplex. Then, the evidence \( e = \{e_1, e_2, \ldots, e_K\} \) of \( \omega \) is linked with Dirichlet parameter \( \mathbf{\alpha} \) based on DST as follows:

\[
\alpha_k = e_k + a_k W;
\]

where \( e_k \in [0, +\infty) \) obtained directly from the last layer of neural network with a non-negative activation function, such as Rectified Linear Units (ReLU). \( W \) is the weight of uncertain evidence set as \( K \) empirically. Following the Dirichlet assumption, the expectation of \( \mathbf{p} \) is given by:

\[
E(\mathbf{p}_k) = \frac{\alpha_k}{\sum_{k=1}^{K} \alpha_k} = \frac{e_k + a_k W}{W + \sum_{k=1}^{K} e_k}.
\]

When \( a_k \) is set \( 1/K \), the Dirichlet parameter \( \alpha_k \) can be formulated as \( \alpha_k = e_k + 1 \), in which \( u \) and \( b_k \) can be determined by the parameter as \( u = K/\sum_{k=1}^{K} \alpha_k \) and \( b_k = (\alpha_k - 1)/\sum_{k=1}^{K} \alpha_k \). Thus, the probability of sample with evidence \( e_k \) for \( k \)-th class can be predicted by Eq. 3 (or Eq. 6) simultaneously.

**EDL for multi-label sewer defect classification.** Since the \( K \)-dimensional predicted probability \( \mathbf{p} \) of the popular multi-label classifier may not belong to \( S_K \), we cast the \( K \)-dimensional multi-label classification as \( K \) binary classifications. The predicted probability of each binary classification follows corresponding Dirichlet distribution. Here, the Dirichlet distribution reduces to a Beta distribution. For generality, we still describe EDL for multi-label sewer defect classification via Dirichlet distribution.
Evidential generation module (EGM) is conducted to generate the defective (+) and non-defective (−) evidences \( e_K = \{(e^+_k, e^-_k), \ldots, (e^+_K, e^-_K)\} \) of \( K \) binary sewer defect classifications as follows:

\[
e_K = \phi(w^T f^* + b), \tag{7}
\]

where \( w \in \mathbb{R}^{C \times 2K} \) and \( b \in \mathbb{R}^{2K} \) refer to the weight vector and bias, respectively. \( \phi \) denotes a non-negative activation function which is ReLU empirically. \( f^* \in \mathbb{R}^{C \times 1} \) is the feature vector of deep feature f pooled via global average operation. Intuitively, we can exploit Eq. 3 (or Eq. 6) to derive the defect probability \( \hat{p}_K \) based on the set of \( K \) Dirichlet distributions \( \{Dir((p_k, \alpha_k))\}_{k=1}^K \), in which the Dirichlet parameter \( \alpha_k = (\alpha^+_k, \alpha^-_k) \) is given by:

\[
\alpha^+_k = e^+_k + a^+_k W, \tag{8}
\]

where \( i \in \{+, -\} \) from a set including defective and non-defective indicators. \( a^+_k, \alpha^-_k \) and \( W \) are set 1/2, 1/2 and 2, respectively.

### 2.2. Expert base rate assignment

Intuitively, the importance of defect classes is different in the practice, we introduce the expert knowledge to reassign the base rates of each defect class via expert base rate assignment (EBRA). The realistic base rates based on expert knowledge would enhance the reliability of determination intuitively [14]. Here, we utilize class-importance weights (CIW) as the expert knowledge, which is normalized by [9]. The procedure of EBRA for the \( k \)-th binary classification can be formulated as follows:

\[
\hat{\alpha}_k = \alpha^+_k + (-1)^{[i \neq +]}(\sigma(CIW_k) - 1/2), \tag{9}
\]

where \( [\cdot] \) is the indicator function which takes 1 when the argument is true and 0 otherwise. \( \sigma \) denotes a sigmoid function, and CIW is the class-importance weight of the \( k \)-th defect class. Subsequently, the probability mass, uncertainty, belief mass, and Dirichlet parameter of \( K \) binary classifications can be derived by formulations in Section 2.1 based on \( \hat{\alpha}_K = \{(\hat{\alpha}^+_k, \hat{\alpha}^-_k)\}_{k=1}^K \), termed as \( p_K = \{(\hat{p}^+_k, \hat{p}^-_k)\}_{k=1}^K \), \( u_K = \{\hat{u}_k\}_{k=1}^K \), \( b_K = \{\hat{b}^+_k, \hat{b}^-_k\}_{k=1}^K \) and \( \hat{\alpha}_K = \{(\hat{\alpha}^+_k, \hat{\alpha}^-_k)\}_{k=1}^K \), respectively.

### 2.3. Training and inference

The training procedure of EDL is conducted based on the Type II Maximum Likelihood (Empirical Bayes) [17]. We first obtain the evidences \( e_K \) from EGM, and then, convert multi-class label \( y \in \mathbb{H}^{K \times 1} \) as \( K \) binary class labels \( y_K = \{(y^+_k, y^-_k), \ldots, (y^+_K, y^-_K)\} \), where \( \mathbb{H} \) denotes Hamming space. The loss function of \( k \)-th binary classification can be formulated as a minimization of negative log-likelihood:

\[
\mathcal{L}_k = -\log \left( \prod_{i \in \{+, -\}} \frac{1}{B(\alpha_i)} \prod_{i \in \{+, -\}} \hat{p}^i_k \right) = \sum_{i \in \{+, -\}} y^i_k \left( \log(\hat{S}_k) - \log(\hat{\alpha}^i_k) \right) = \sum_{i \in \{+, -\}} y^i_k \left( \log(\hat{S}_k) - \log(e^i_k + \hat{\alpha}^i_k W) \right), \tag{10}
\]

where \( \hat{S}_k = \sum_{i \in \{+, -\}} \hat{\alpha}^i_k \). Eventually, TMSDC for \( K \) binary sewer defect classifications can be optimized as follows:

\[
\arg \min_{\theta_F, \theta_G} \sum_{k=1}^K \mathcal{L}_k.
\]

In the inference, we utilize maximum operation to obtain the uncertainty estimation \( \hat{u} \) of sewer pipe image \( x \) as follows:

\[
\hat{u} = \max_k \hat{u}_k \tag{11}
\]

### 3. EXPERIMENTS

#### 3.1. Experimental setup

**Dataset.** Sewer-ML [9] is a large-scale benchmark dataset, which focuses on the multi-label sewer defect classification task. 1.3 million sewer pipe images are collected over a nine year period, annotated with 17 defect classes and divided into 3 subsets in terms of training, validation, and testing. The numbers of samples for 3 subsets are 1,040,129, 130,046, and 130,026, respectively. Since the annotations of testing set are not public, we conduct the experiments focused on the training and validation sets.

**Evaluation tasks and metrics.** To evaluate the performance of TMSDC on both known and unknown settings, we conduct the evaluation tasks as follows: multi-label sewer defect classification \( T_{MSDC} \) and out-of-distribution (OOD) detection \( T_{OOD} \), separately. Specifically, \( T_{MSDC} \) is utilized to demonstrate TMSDC capability of classifying the known sewer defect categories, in which \( F_1 \) and \( F_2 \) are introduced as evaluation metrics following [9]. In \( T_{OOD} \), we select the partial categories as the unknown defect categories, and the sewer samples with unknown defect labels are regarded as unknown samples. It means that the samples with unknown defect labels would not be “seen” in the training phase. The uncertainty estimation \( \hat{u} \) of TMSDC is leveraged to distinguish the unknown and known samples. The evaluation metrics for the OOD detection task are AUROC, AUPR, and FPR95, where the unknown samples are defined as the positive cases.

**Implementation details.** The experiments are carried out on a work station with NVIDIA Tesla A100 GPUs. The proposed method is implemented based on PyTorch deep learning framework. The backbone of feature extractor \( F \) is TResNet-L [18]. In the training phase of \( T_{MSDC} \), the learnable parameters of TMSDC are trained from scratch via stochastic gradient descent (SGD) with a weight decay of 1e-4. The
Table 1. Comparison of our method with the state-of-the-art methods of $\mathcal{T}_{\text{ODD}}$ on Sewer-ML. † represents the two-stage-based method.

| Method   | Validation F2CIW(%)↑ | Validation F1Normal(%)↑ |
|----------|----------------------|-------------------------|
| Xie†[8]  | 48.57                | 91.08                   |
| Chen†[7] | 48.67                | 91.06                   |
| ResNet-101 [19] | 53.26              | 79.55                   |
| KSSNet [20] | 54.42              | 80.60                   |
| TResNet-L [18] | 54.63             | 81.22                   |
| TMSDC (Ours) | 54.54             | 81.15                   |

Table 2. Comparison of our method with the competitive methods of $\mathcal{T}_{\text{OOD}}$ on Sewer-ML.

| Method      | Arch       | AUROC↑ | Validation AUROC↑ | Validation AUPR↑ | Validation FPR95 ↓ |
|-------------|------------|--------|-------------------|------------------|-------------------|
| MaxLogit [21] | $F_S \circ M$ | 65.19   | 77.40             | 83.03            |
| JointEnergy [22] | $F_S \circ M$ | 81.15   | 90.33             | 81.35            |
| SLCS [23]   | $F_S \circ M$ | 81.97   | 91.11             | 77.14            |
| TMSDC (Ours) | $F_S \circ G$ | 85.56   | 92.23             | 55.83            |

Total training epochs are 90 and the initial learning rate is 1e-1, while the learning rate is reduced with the decay ratio of 0.1 after every 30 epochs. The batch size of training is 256. The input images are scaled as $224 \times 224$, while random flip, jitter of pixel values (such as brightness, contrast, saturation, and hue) are used as data argumentation. In $\mathcal{T}_{\text{OOD}}$, RB, OB, FS and OS are selected as unknown defect categories based on higher CIW, since it is more valuable to verify the model performance of uncertainty estimation for serious unknown sewer defect samples. For a fair comparison, we utilize a shared weight feature extractor for TMSDC and other OOD methods. We first train TResNet-L $F_S$ with a fully connected layer-based multi-label classifier $M$ via hyper-parameters in $\mathcal{T}_{\text{MSDC}}$. Then, $M$ is replaced by EGM $G$, and the trained parameters of $F_S$ are fixed. $G$ is fine-tuned for 20 epochs with 1e-3 learning rate. To simplify the description, the architectures of TMSDC and other OOD methods are denoted as $F_S \circ G$ and $F_S \circ M$, respectively.

3.2. Comparisons with the state-of-the-art

Multi-label sewer defect classification $\mathcal{T}_{\text{MSDC}}$. We compare our method with 5 state-of-the-art methods recently reported on Sewer-ML, which can be categorized into two-stage and end-to-end methods. As shown in Tab. 1, we observe that TMSDC achieves competitive performances of 17 defect classes ($K = 17$) in terms of $F2_{\text{CIW}}$ and $F1_{\text{Normal}}$. It validates the acceptable performance of TMSDC for classifying known multi-label sewer defect samples.

OOD detection $\mathcal{T}_{\text{ODD}}$. We compare our method against competitive OOD detection methods of multi-label classification, in which TMSDC demonstrates state-of-the-art performance, as reported in Tab. 2. Here, the performances of $F_S \circ M$ for 13 defect classes ($K = 13$) are close to $F_S \circ G$. $F2_{\text{CIW}}$ of two architectures are 54.67% and 54.61%, while $F1_{\text{Normal}}$ of them are 84.34% and 84.27%. These facts verify that TMSDC achieves the reliable results on unknown uncertainty estimation with a tolerable decrease of classification performance.

3.3. Ablation studies

Effectiveness of expert base rate assignment. To clarify the effectiveness of EBRA, we train TMSDC with a average base rate whose performance is reported in Tab. 3. It can be seen that EBRA improves the capability of distinguishing unknown defect categories for TMSDC obviously, validating the effectiveness of EBRA.

Impact of different aggregation methods in Eq. 11. To explore the impact of different aggregation method, we utilize three aggregation methods for uncertainty estimation alternately including summation (Sum), top-5 (Top-5) and maximum (Max) operations. Top-5 means that the summation of the highest five uncertainty scores in $\hat{u}_k$. As listed in Tab. 3, the summation operation might worsen the discriminability of uncertainty estimation, resulting in the lower performance. The top-5 operation outperforms the maximum operation in terms of AUROC and AUPR, in which the maximum operation achieves the lowest false positive rate of unknown samples where the true positive rate of known samples is at 95%.

4. CONCLUSION

In this paper, we propose a trustworthy multi-label sewer defect classification (TMSDC) method, which can quantify the uncertainty of sewer defect prediction via evidential deep learning. Meanwhile, a novel expert base rate assignment (EBRA) is proposed to introduce the expert knowledge for describing reliable evidences in practical situations. Experimental results demonstrate that TMSDC is effective and achieves the superior capability of uncertainty estimation on the latest benchmark.

5. REFERENCES

[1] Nikola Stanić, Jeroen G. Langeveld, and François H.L.R. Clemens, “Hazard and operabil-
ity (hazop) analysis for identification of information requirements for sewer asset management.” *Struct. Infrastructure Eng.*, vol. 10, no. 11, pp. 1345–1356, 2014.

[2] Zheng Liu and Yehuda Kleiner, “State of the art review of inspection technologies for condition assessment of water pipes,” *Meas.*, vol. 46, no. 1, pp. 1–15, 2013.

[3] Rakibah Rayhana, Yutong Jiao, Amirhossein Zaji, and Zheng Liu, “Automated vision systems for condition assessment of sewer and water pipelines,” *IEEE Trans. Autom. Sci. Eng.*, vol. 18, no. 4, pp. 1861–1878, 2021.

[4] Chuanfei Hu and Yongxiong Wang, “An efficient convolutional neural network model based on object-level attention mechanism for casting defect detection on radiography images,” *IEEE Trans. Ind. Electron.*, vol. 67, no. 12, pp. 10922–10930, 2020.

[5] Jin Deng, Wenjuan Jiang, Ye Zhang, Gong Wang, Sheng Li, and Hairui Fang, “Hs-kdnet: A lightweight network based on hierarchical-split block and knowledge distillation for fault diagnosis with extremely imbalanced data,” *IEEE Trans. Instrum. Meas.*, vol. 70, pp. 1–9, 2021.

[6] HaiRui Fang, Jin Deng, DongSheng Chen, WenJuan Jiang, SiYu Shao, MingCong Tang, and JingJing Liu, “You can get smaller: A lightweight self-activation convolution unit modified by transformer for fault diagnosis,” *Adv. Eng. Inf.*, vol. 55, pp. 101890, 2023.

[7] Kefan Chen, Hong Hu, Chaozhan Chen, Long Chen, and Caiying He, “An intelligent sewer defect detection method based on convolutional neural network,” in *2018 IEEE ICIA*, 2018, pp. 1301–1306.

[8] Qian Xie, Dawei Li, Jinxuan Xu, Zhenghao Yu, and Jun Wang, “Automatic detection and classification of sewer defects via hierarchical deep learning,” *IEEE Trans. Autom. Sci. Eng.*, vol. 16, no. 4, pp. 1836–1847, 2019.

[9] Joakim Brulsund Haorum and Thomas B. Moeslund, “Sewer-ml: A multi-label sewer defect classification dataset and benchmark,” in *2021 IEEE/CVF CVPR*, 2021, pp. 13451–13462.

[10] Bardia Roghani, Frédéric Cherqui, Mehdi Ahmadi, Pascal Le Gauffre, and Massoud Tabesh, “Dealing with uncertainty in sewer condition assessment: Impact on inspection programs,” *Autom. in Constr.*, vol. 103, pp. 117–126, 2019.

[11] L. Minh Dang, Hanxiang Wang, Yanfen Li, Tan N. Nguyen, and Hyeonjoon Moon, “Defecttr: End-to-end defect detection for sewage networks using a transformer,” * Constr. Build. Mater.*, vol. 325, pp. 126584, 2022.

[12] Chuanfei Hu, Bo Dong, Hang Shao, Jiapeng Zhang, and Yongxiong Wang, “Toward purifying defect feature for multilabel sewer defect classification,” *IEEE Trans. Instrum. Meas.*, vol. 72, pp. 1–11, 2023.

[13] Murat Sensoy, Lance Kaplan, and Melih Kandemir, “Evidential deep learning to quantify classification uncertainty,” *Advances in NIPS*, vol. 31, 2018.

[14] Audun Jøsang, *Subjective logic*, vol. 3, Springer, 2016.

[15] Zongbo Han, Changqing Zhang, Huazhu Fu, and Joey Tianyi Zhou, “Trusted multi-view classification with dynamic evidential fusion,” *IEEE Trans. Pattern. Anal. Mach. Intell.*, vol. 45, no. 2, pp. 2551–2566, 2023.

[16] Xujiang Zhao, Xuchao Zhang, Wei Cheng, Wenchao Yu, Yuncong Chen, Haifeng Chen, and Feng Chen, “Seed: Sound event early detection via evidential uncertainty,” in *2022-2022 IEEE ICASSP*. IEEE, 2022, pp. 3618–3622.

[17] Tahira Jamil and Cajo J.F. ter Braak, “Selection properties of type ii maximum likelihood (empirical bayes) in linear models with individual variance components for predictors,” *Pattern Recognition Letters*, vol. 33, no. 9, pp. 1205–1212, 2012.

[18] Tal Ridnik, Hussam Lawen, Asaf Noy, Emanuel Ben, Baruch Gilad Sharir, and Itamar Friedman, “Tresnet: High performance gpu-dedicated architecture,” in *2021 IEEE WACV*. IEEE, 2021, pp. 1399–1408.

[19] K. He, X. Zhang, S. Ren, and J. Sun, “Deep residual learning for image recognition,” in *2016 IEEE CVPR*, June 2016, pp. 770–778.

[20] Ya Wang, Dongliang He, Fu Li, Xiang Long, Zhichao Zhou, Jinwen Ma, and Shilei Wen, “Multi-label classification with label graph superimposing,” *Proceedings of the AAAI*, vol. 34, no. 07, pp. 12265–12272, Apr. 2020.

[21] Dan Hendrycks, Steven Basart, Mantas Mazeika, Mohammadreza Mostajabi, Jacob Steinhardt, and Dawn Song, “Scaling out-of-distribution detection for real-world settings,” *arXiv preprint arXiv:1911.11132*, 2019.

[22] Haoran Wang, Weitang Liu, Alex Bocchieri, and Yixuan Li, “Can multi-label classification networks know what they don’t know?,” in *Advances in NIPS*. 2021, vol. 34, pp. 29074–29087, Curran Associates, Inc.

[23] Lei Wang, Sheng Huang, Luwen Huangfu, Bo Liu, and Xiaohong Zhang, “Multi-label out-of-distribution detection via exploiting sparsity and co-occurrence of labels,” *Image Vision Comput.*, vol. 126, pp. 104548, 2022.