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Study of KIC 8561221 observed by Kepler: an early red giant showing depressed dipolar modes*

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ABSTRACT

Context. The continuous high-precision photometric observations provided by the CoRoT and Kepler space missions have allowed us to understand the structure and dynamics of red giants better using asteroseismic techniques. A small fraction of these stars show dipole modes with unexpectedly low amplitudes. The reduction in amplitude is more pronounced for stars with a higher frequency of maximum power, νmax.

Aims. In this work we want to characterise KIC 8561221 in order to confirm that it is currently the least evolved star among this peculiar subset and to discuss several hypotheses that could help explain the reduction of the dipole mode amplitudes.

Methods. We used Kepler short- and long-cadence data combined with spectroscopic observations to infer the stellar structure and dynamics of KIC 8561221. We then discussed different scenarios that could contribute to reducing the dipole amplitudes, such as a fast-rotating interior or the effect of a magnetic field on the properties of the modes. We also performed a detailed study of the inertia and damping of the modes.

Results. We have been able to characterise 36 oscillations modes, in particular, a few dipole modes above νmax that exhibit nearly normal amplitudes. The frequencies of all the measured modes were used to determine the overall properties and the internal structure of the star. We have inferred a surface rotation period of ~91 days and uncovered a variation in the surface magnetic activity during the last 4 years. The analysis of the convective background did not reveal any difference compared to “normal” red giants. As expected, the internal regions of the star probed by the ℓ = 2 and 3 modes spin 4 to 8 times faster than the surface.

Conclusions. With our grid of standard models we are able to properly fit the observed frequencies. Our model calculation of mode inertia and damping give no explanation for the depressed dipole modes. A fast-rotating core is also ruled out as a possible explanation. Finally, we do not have any observational evidence of a strong deep magnetic field inside the star.

Key words. stars: evolution – stars: oscillations – stars: individual: KIC 8561221

1. Introduction

Turbulent motions in the outer convective envelope of solar-like pulsating stars excite oscillation modes that propagate inside the stars probing their interiors (e.g. Goldreich & Keeley 1977; Goldreich & Kumar 1988; Samadi & Goupil 2001). The first indications of solar-like oscillations in red giants were obtained from ground-based observations in the K-giant Arcturus (Merline 1999) and in the G7-giant star ξ Hya (e.g. Frandsen et al. 2002). With the development of high-precision space photometry, the field moved rapidly from the study of a few red giants (e.g. Buzasi et al. 2000; Barban et al. 2007) to multi-month continuous observations – provided by CoRoT (Baglin et al. 2006) and Kepler (Borucki et al. 2010) – of many field red

* Table 3 and Appendix A are available in electronic form at http://www.aanda.org
mosser et al. (2012a) on 800 red giants observed by Kepler (KASC-4) meeting, garcía et al. showed two red-giant stars observed by Kepler in which the amplitudes of the dipole modes were unexpectedly small. The following ensemble analysis by Mosser et al. (2012b) and Deheuvels et al. (2012) will help for understanding the properties of their cores on few hundred stars belonging to clusters (e.g. Stello et al. 2010; Basu et al. 2011). These data provide strong constraints on these stars. In particular, the detection of mixed modes (Beck et al. 2011) will help for understanding the properties of their cores (Bedding et al. 2011; Mosser et al. 2011), including their dynamics (Mosser et al. 2012b; Deheuvels et al. 2012; Beck et al. 2012).

In 2011, at the 4th Kepler Asteroseismic Science Consortium (KASC-4) meeting, garcía et al. showed two red-giant stars observed by Kepler in which the amplitudes of the dipole modes were unexpectedly small. The following ensemble analysis by Mosser et al. (2012a) on 800 red giants observed by Kepler (e.g. Huber et al. 2010; Hekker et al. 2011) shows that in about 5% of these stars the dipole modes had lower visibilities than expected from theory (see Fig. 11 of Mosser et al. 2012a). Moreover, these stars followed a relation with v_max where higher v_max stars showed lower dipole mode visibility. No clear correlation appeared with other variables such as the effective temperature or the mass, although a lower limit of the mass seems to be established at around 1.4 M⊙.

To better understand the possible physical mechanisms responsible for such a decrease in the dipole amplitudes, we study KIC 8561221, an early red giant near the base of the red giant branch (RGB) (see Fig. 3 of Mosser et al. 2012c). This is the least evolved, known depressed dipole-mode star (see Fig. 1) and, as a consequence, is the star with the strongest mode depression/suppression. It also shows a clear transition/gradient in the level of depression/suppression from very strong below v_max to near normal at high frequencies. This could therefore represent the Rosetta stone for our studies of the depressed/suppressed dipole-mode phenomenon since it marks the transition where the reduction in the dipole amplitudes kicks in.

KIC 8561221 was observed by the NARVAL spectrograph mounted on the 2-m Bernard-Lyot telescope at the Pic du Midi Observatory in France. Two groups analysed the spectra using different methods. Bruntt et al. (2012) used the semi-automatic software VWA (Bruntt et al. 2010) to retrieve T_eff and [Fe/H] after adopting the asteroseismic log g. Molenda-Zakowicz et al. (2013) used two other codes (ROTFIT and ARES+MOOG) to analyse the same spectra and re-estimated T_eff and [Fe/H]. The values obtained by these different methods agree within the uncertainties and are summarised in Table 1. For the rest of our paper we use the parameters obtained by Bruntt et al. (2012) because they took the seismic log g into account.

We start in Sect. 2 by presenting the Kepler observations used in this paper, as well as the determination of the dynamic (convection, rotation and magnetic activity) and seismic properties of the star. With this set of observables and the spectroscopic constraints from the VWA method, we compute several stellar models in Sect. 3 using different methodologies. Finally, in Sect. 4, we discuss different physical mechanisms that could potentially contribute to reducing the dipole-mode amplitudes

### Table 1. Spectroscopic parameters of KIC 8561221 obtained by Bruntt et al. (2012) using the VWA method and by Molenda-Zakowicz et al. (2013) using ROTFIT and ARES+MOOG.

| KIC     | log g     | T_eff (K)   | [Fe/H]  |
|---------|-----------|-------------|---------|
| VWA     | 3.61 ± 0.03 | 5245 ± 60   | −0.05 ± 0.06 |
| ROTFIT  | 3.76 ± 0.13 | 5290 ± 89   | −0.04 ± 0.10 |
| ARES+MOOG | 3.80 ± 0.11 | 5352 ± 68   | −0.04 ± 0.06 |

Fig. 1. Zoom of the power density spectrum around ν_max. Vertical lines indicate the central frequencies obtained in the analysis described in Sect. 2.3 and Table 3 for modes ℓ = 0, 1, 2, and 3, black dot, blue dashed, red dot dashed, and pink triple-dot dashed lines, respectively.
quarters Q5 to Q13 – starting on March 20, 2010 and ending on October 3, 2012 – have been used to study the oscillation properties of KIC 8561221.

We used simple aperture photometry (SAP) time series (e.g. Thompson et al. 2013) that were corrected for different instrumental perturbations – outliers, jumps, and drifts – using the procedures described in García et al. (2011) and high-pass filtered by a two-day triangular smoothing function.

To complement the seismic studies, we measured the surface rotation rate from the modulations in the light curve following previous analyses of space-borne photometry (e.g. García et al. 2009; Campante et al. 2011; Mathur et al. 2011a). To do so, we used SAP LC photometry for almost the full Kepler mission from Q2 to Q16, i.e. from June 20, 2009 to April 08, 2013 corrected following García et al. (2011). The data corresponding to Q0 and Q1 were rejected because of instrumental instabilities. We filtered the data using a double triangular smoothing function with a 200-day width. The LC flux is shown in the top panel of Fig. 2. The blue shaded regions during Q5 and Q13 mark two regions that were rejected in the analysis because they seemed to be affected by instrumental instabilities. Unfortunately, in the case of KIC 8561221, the data corrected...
using Pre Data Conditioning multi-scale Maximum A Posteriori methods (PDC-msMAP, e.g. Thompson et al. 2013) are not reliable because they are high-pass filtered with a limit at around 21 days.

2.1. Surface rotation period and magnetic activity

To determine the average rotation rate of the stellar surface we look for any modulation in the light curve induced by the dimming produced by spots crossing the visible stellar disk. As can be seen in the top left-hand panel of Fig. 2, there is a regular long-period modulation clearly visible in the light curve. This modulation seems to be due to variations in the brightness of KIC 8561221 because the contamination of the field is very small, 0.000264, and visual inspection of the UKIRT high-resolution images does not show any other star that could pollute the photometric signal. Finally, the modulation can be seen at the same level for all pixels within the photometric mask.

To study the rotation period we use two complementary techniques that are described in García et al. (2013a): the study of the global power spectrum (GPS, e.g. Mathur et al. 2010a) and the autocorrelation of the temporal signal (e.g. McQuillan et al. 2013). Unfortunately, as said in the previous section, we were not able to use PDC-msMAP corrected data and we have only used the data corrected following García et al. (2011).

The GPS represented in the middle right-hand panel of Fig. 2 is a periodogram computed by projecting the wavelet power spectrum shown in the middle left-hand panel into the time domain. We use the Morlet wavelet, i.e. a Gaussian envelope with a varying width (Torrence & Compo 1998), which we prefer to the analysis of the low-frequency end of the standard periodogram (shown in the top right-hand panel in Fig. 2) because it allows us to verify that the dominant features at low frequency are the consequence of isolated events (related to instrumental perturbations), or if they are present during all the observations (see middle left-hand panel of Fig. 2). Although there is an increase in the photometric modulation after Q9, a periodic signal is visible in the whole light curve. Fitting three Gaussian functions to the GPS provides a rotation period, $P_{\text{rot}} = 91.1 \pm 12.5$ days, with a secondary period at 46.0 \pm 3 days and a third at 73.6 \pm 2.5 days (here we quote the half width at half maximum, of the fitted functions as the uncertainty). The period of 46 days corresponds to the second harmonic of the rotation period. Indeed the time frequency diagram shows that the -91 day period is seen at several moments during the observations (Q6 and Q7, Q10 to Q12, and during Q14 to Q16). However, there is considerable dispersion in the exact period which is reflected in the large uncertainty we obtain. This could be the signature of surface differential rotation.

The analysis of the autocorrelation function of the light curve – shown in Fig. 3 – confirms the value of the rotation period obtained by the GPS. The maximum peak of the autocorrelation is at 90.9 \pm 11.7 days (uncertainty computed as the half width at half maximum of the peak).

The observed $P_{\text{rot}}$ is suspiciously close to the length of a Kepler quarter. To decide whether this measurement has a stellar origin, we need to check if it is in phase with the quarters. If we take a closer look at the light curve, for example, between Q6 and Q8 (see top left-hand panel in Figs. 2 and 4), the maxima of the modulation are not aligned with the quarters and the ends of each quarter are stitched together well without any significant jumps between them (see Fig. 4). The ACF of just these quarters provides $P_{\text{rot}} \sim 93$ days although the average length of the quarters is \sim 82 days. Similar results are obtained when other sections of the light curve are analyzed separately. We therefore conclude that the retrieved $P_{\text{rot}}$ is probably of stellar origin.

To theoretically estimate the surface rotation, we adopted a 1.5 solar mass reference model at [Fe/H] = 0 and evolved it to log $g = 3.62$ using the input physics and angular momentum evolution model described in van Saders & Pinsonneault (2013). We assumed rigid rotation and a range of initial conditions chosen to bracket the observed distribution of rotation rates in intermediate-aged open cluster stars of this mass range. Angular momentum loss was included but does not have a significant effect on the main sequence; however, these models do experience significant post-main sequence angular momentum loss that was included in the calculations. With these models we predict a surface rotation rate in the range 35 to 43 days. This range reflects the range of main sequence rotation rates for normal stars and assumes rigid rotation at all times. If the progenitor had a lower mass, the expected rotation periods would increase. For example, the surface rotation increases to the range 58 to 63 days.

\footnote{\url{http://keplerscience.arc.nasa.gov/ToolsUKIRT.shtml}}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig3.png}
\caption{Autocorrelation function (ACF) of the light curve shown in the top left-hand panel of Fig. 2. The maximum of the ACF caused by rotation is marked by a vertical red dashed line (90.9 \pm 11.7 days).}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig4.png}
\caption{Zoom of the light curve of KIC 8561221 (top) and ACF of this part of the light curve. The position of maximum of the ACF, 93.0 days, is marked by a vertical red dashed line in the bottom panel. The red-dashed lines in the light curve (top panel) are the corresponding period intervals, which match the repeating flux modulations. The ends of each quarter are indicated by the blue dotted lines.}
\end{figure}
by decreasing the mass to 1.4 $M_\odot$. Core-envelope decoupling in the post-main sequence would decrease the predicted surface rotation, although van Saders & Pinsonneault (2013) found that this had only a modest impact on model predictions. If the main sequence precursors had rapidly rotating embedded cores the surface rotation would be above the predicted range.

A lower rotation rate could also be obtained if the precursor was a chemically peculiar star or if we consider any extra magnetic braking at the surface of the star. As we see later, KIC 8561221 seems to still have a magnetic field in action at the surface with a possible observational signature of a dynamo at this stage of evolution.

The presence of spots on the surface of the star demonstrated by the low-frequency modulation of the photometric signal shows that the star is active. We can define a photometric activity index, $S_{ph}$, directly from the light curve in order to quantify the activity and to be able to compare it with other Kepler targets and the Sun (e.g. Mathur et al. 2014). To do so, we divide the light curve into subseries of $5 \times P_{rot}$ (to have enough realisations of the rotation per subseries) and compute the standard deviation of each segment. We have verified that the results do not change when we use subseries of $3 \times P_{rot}$. The activity index, $S_{ph}$, will be the average of the individual standard deviations of each subseries. We prefer to use the average instead of the median because, if there is an on-going magnetic activity cycle, the median underestimates the final results and because we only have three independent realisations of $5 \times P_{rot}$. Finally, we subtract the photon noise ($19.9$ ppm) computed following the procedure described in Jenkins et al. (2010). For KIC 8561221 we obtain $S_{ph} = 637.0 \pm 5.1$ ppm with a minimum activity of $473 \pm 3.5$ ppm and a maximum of $965 \pm 7.2$ ppm. As a comparison, we can compute the same activity index for the Sun, $S_{ph,\odot}$ using the sum of the red and green channels of the Sun SpectroPhotoMeters (SPM) of the VIRGO instrument (Fröhlich et al. 1995) aboard the Solar and Heliospheric Observatory (SoHO; Domingo et al. 1995). Indeed – as recently demonstrated by Basri et al. (2013) – the use of these two colours of VIRGO/SPM constitutes a good approximation to the Kepler photometric bandpass. In the solar case – using 16 years of quasi-continuous measurements – we found that $S_{ph,\odot} = 166.1 \pm 2.6$ ppm with a variation between the minimum and the maximum of $89.0 \pm 1.5$ and $258.5 \pm 3.5$ ppm respectively. Therefore the changes in the photometric activity of KIC 8561221 are around $3.5$ times higher than the one exhibited by the Sun, although it is a more evolved star (see Sect. 3).

To uncover the possible existence of a magnetic activity cycle in KIC 8561221, we compute the scale-averaged time series, i.e., the projection into the time domain of the wavelet power spectrum around the time scales of the rotation period (an application of this methodology to the Sun can be seen in García et al. 2013b). This is done to ensure that the temporal variations we are computing are only related to the stellar spots and not to any other instrumental or stellar feature on different time scales (see bottom panel in Fig. 2). However, we have followed a conservative approach by using a wide range of periods (between 15 and 150 days). It is also important to notice that we have removed additional data in the vicinity of the rejected observations at Q5 and Q13 because we need to take border effects on the reconstruction of the signal into account.

There is a clear increase in the magnetic activity at the end of Q9 with a maximum around Q14 and Q15, followed by a slow decline. We can therefore argue that despite its late stage of evolution (see Sect. 3) it is very likely that a magnetic activity cycle (probably a dynamo) is in action in KIC 8561221.

Fig. 5. Power density spectrum of KIC 8561221 short-cadence data at full resolution (grey curve) and after rebinning by a factor of 100 (black curve). The green line shows the spectrum smoothed by a box car with a width equal to the mean large separation $\Delta \nu$. The fitted background is the solid red line, and its three components (W, Bg, Ba) are plotted as red dotted lines. P-mode power excess, fitted as a Gaussian profile, is also represented with a red dashed line.

2.2. Background parameters

The convective background of KIC 8561221 has been studied by fitting a simple three-component model, $B(\nu)$ to the power spectrum. The first component is the photon noise, $W$, which dominates the frequency-independent noise at high frequency. The second component is a Harvey-like profile (Harvey 1985) to model the granulation contribution:

$$B_g(\nu) = \frac{4 \tau_g a_g^2}{1 + (2\pi \tau_g \nu)^{\alpha_g}},$$

in which $\tau_g$ is the characteristic time scale of the granulation, $a_g$ is its amplitude, and $\alpha_g$ is an exponent characterising its temporal coherence.

The third background component models the low-frequency part of the power spectrum dominated by activity. For this we use a power law $B_s(\nu) = P_s \nu^{-\gamma_s}$. To obtain the best fit we have followed the same procedure as in Ballot et al. (2011b). The results of the fit are $\tau_g = 1112 \pm 21$, $a_g = 102.2 \pm 0.5$ ppm, and $\alpha_g = 2.41 \pm 0.02$.

In addition, we have computed the effective granulation timescale as defined in Mathur et al. (2011b). We obtained a value of $\tau_{eff} = 1415 \pm 19$ s, which is in perfect agreement with the expected value from the relation inferred for red-giant stars by Mathur et al. (2011b). Therefore, it seems that there are no differences in the convection timescales between this star and those having dipole modes with normal amplitudes.

2.3. Seismic characterisation

We determined the global parameters of the acoustic modes of the star using the A2Z pipeline (Mathur et al. 2010b), one of the extensively tested tools to reliably extract those parameters (see e.g. Hekker et al. 2011). The mean large separation was obtained by computing the power spectrum of the power spectrum. This led to $(\Delta \nu) = 29.88 \pm 0.80 \mu Hz$. We fitted the p-mode bump with a Gaussian function to measure the frequency at maximum power and the maximum amplitude: $\nu_{max} = 490 \pm 24 \mu Hz$ and $A_{max} = 6.8 \pm 0.24$ ppm.
A Bayesian approach using a Markov chain Monte Carlo (MCMC) algorithm (Benomar et al. 2009) was used to globally extract the characteristics of the individual p modes in KIC 8561221. The priors are similar to the ones defined by Benomar et al. (2013). However, we directly fit each dipole mixed mode instead of using the coupled oscillator model. The results were compared and validated using standard maximum likelihood estimator (MLE) fits.

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Table 2. Fitting scenarios studied to check the robustness of the result.

| Case | $\delta \nu (\ell = 1)$ | $N_{\text{ndata}}(\ell = 2)$ | $\delta \nu (\ell = 2, 3)$ | $\Gamma (\ell = 0)$ | $\Gamma (\ell = 1)$ | $\Gamma (\ell = 2, 3)$ |
|------|-----------------|------------------|-----------------|-----------------|-----------------|-----------------|
| 1    | independent     | All               | $\delta \nu (\ell = 2) \neq \delta \nu (\ell = 3)$ | independent     | independent     | interpolated from $\Gamma (\ell = 0)$ |
| 2    | =               | =                | =               | =               | =               | =               |
| 3    | =               | =                | =               | $\Gamma (\ell = 1) \leq \Gamma (\ell = 0)$ | =               | =               |
| 4    | =               | $4$ highest S/N  | =               | =               | independent     | =               |
| 5    | =               | =                | =               | $\Gamma (\ell = 1) \leq \Gamma (\ell = 0)$ | =               | =               |

Notes. When the value is not changed compared to the preceding case it has been indicated by “=“.

Figure 6b shows the mode width as a function of frequency. High-frequency dipole modes have widths similar to modes of different degree but similar frequency. However, at lower frequency, widths apparently increase, which must be significant because the prior in the Case-3 fit (shown in Fig. 6b) penalises the width of the dipole modes to be significantly greater than for the radial modes. A closer analysis of the power spectrum indicates that modes around 504 $\mu$Hz and 535 $\mu$Hz are indeed broad and correctly fitted. The amplitude of the dipole modes, determined by the relation $A = \sqrt{\pi \hat{H}}$, remains lower overall than the $\ell = 0$ amplitudes (Fig. 6c).

The different scenarios all yield inferred inclination angles that are consistent within 1$\sigma$, spreading from 13$^\circ$ to 29$^\circ$. This suggests that the star is seen from a low angle close to the pole (see Appendix A for a detailed discussion). However, with such a low inclination angle, measurements of the rotational splitting become less precise, especially for the dipole modes (e.g. Gizon & Solanki 2003; Ballot et al. 2006). This was verified by looking at the probability distributions of the $\delta \nu (\ell = 1)$ that are highly multimodal. The splittings of the $\ell = 1$ modes have median values of several $\mu$Hz and have a standard deviation of the same order of magnitude. A computation of the average splitting does not improve the estimates. The $\ell = 2$- and $\ell = 3$-mode rotational splittings are much better constrained, although they depend on the hypothesis we included in the fitting model. Thus, in the first case, $\delta \nu (\ell = 2) = 0.69 \pm 0.10 \mu$Hz and $\delta \nu (\ell = 3) = 0.16 \pm 0.08 \mu$Hz are inconsistent and non Gaussian. Such a solution would have implied that the kernels
of $\ell = 2$ and $\ell = 3$ modes are very different and that the radial differential rotation is very steep. However, when we assume $\delta \nu_\ell(\ell = 2) = \delta \nu_\ell(\ell = 3)$ (Cases 2 to 5), the rotational splitting becomes consistent within 1σ. The median values we obtain range between 0.3 and 0.6 µHz. The lower limit is close to twice the inferred surface rotation rate of about 91 days, and it would imply an increase in the internal rotation rate as has already been observed in other evolved stars (Beck et al. 2012; Deheuvels et al. 2012).

Figure 7 shows the correlation maps between the rotational splitting of $\ell > 1$ modes and the inclination axis (case-3 fit). The splitting shows a multi-modal distribution, and in contrast, the maximum probability for the inclination axis is very well defined. This figure also shows the probability density function (PDF) of the seismic $v \sin i$, calculated using the rotational splitting, and the effective temperature and the radius obtained by the RADIUS pipeline (assuming Gaussian uncertainties, see Table 4 and Sect. 3).

Concerning the extracted heights and widths, the values obtained for $\ell = 0$, 2, and 3 modes are very stable and are consistent among all the different scenarios. However, owing to the low signal-to-noise ratio of the dipole modes, their heights and widths are barely measurable, and the uncertainties increase dramatically towards low frequencies.

3. Stellar modelling

Using the asteroseismic and spectroscopic constraints described in the previous sections, we modelled KIC 8561221 using different methods to gain some knowledge of the internal structure of the star. An initial set of stellar parameters was determined using a grid-based method. This technique relies on a pre-constructed grid of stellar tracks or isochrones where the global seismic quantities ($\Delta \nu$ and $\nu_{\text{max}}$) and atmospheric parameters are used as input to determine a best-fitting model. This model and the uncertainties on its fundamental parameters such as mass, radius, and age are usually obtained using a maximum likelihood approach coupled with Monte Carlo simulations, as described in Basu et al. (2010) and Silva Aguirre et al. (2012).

We obtained two sets of grid-based modelling results using the BaSTI isochrones (Pietrinferni et al. 2004) especially computed for asteroseismic analysis, as described in Silva Aguirre et al. (2013). One set considered the canonical BaSTI isochrones, while the other used a grid of non-canonical isochrones including the effect of overshooting in the main-sequence phase when a convective core is present. A third set of grid-modelling results was obtained using the RADIUS pipeline described in Stello et al. (2009), where the stellar properties are estimated from the best fitting model (the one with the
The individual oscillation frequencies of the models were calculated using the Aarhus adiabatic pulsation package (ADIPLS, Christensen-Dalsgaard 2008a). The empirical near-surface correction suggested by Kjeldsen et al. (2008) was applied to the model frequencies, although additional care was given to the mixed modes following Doğan et al. (2013). Since most of the non-radial modes of this star are mixed modes with high mode inertias relative to those of the radial modes, the magnitude of the correction was divided by the ratio between the mode inertia and the inertia of a radial mode at the same frequency (Aerts et al. 2010). The model presented here (see Fig. 9) was selected based on a \( \chi^2 \) minimisation between the individual observed frequencies and the model frequencies. In Fig. 10 we have shown the Brunt-Väisälä and the Lamb frequencies for the dipole and quadrupole modes, as well as the range in which the modes were observed.

The results from the different methods are given in Table 4. They are in remarkably good agreement (within 1\( \sigma \)).

### 4. Discussion

The observed Fourier spectrum of the \( \ell = 1 \) modes in KIC 8561221 shows modes with normal amplitudes at high frequencies, while at lower frequencies their amplitudes drop at a level close to the noise (see Figs. 1 and 6c). The threshold frequency is not exactly \( \nu_{\text{max}} \) but close to it. We do not have a clear explanation of the reason for this behaviour, but we can perform computations in order to reject some possible hypothesis.

The threshold frequency around \( \nu_{\text{max}} \) is not present for most of the other stars with depressed dipolar modes (Mosser et al. 2012a). Therefore, this circumstance can be a coincidence, and the threshold frequency could be related to a perturbation induced by other phenomena such as a fast rotation or a magnetic field that modifies the oscillation properties.

#### 4.1. Influence of a fast internal rotation

The first two stars shown to have depressed dipole modes also display a modulation in the light curve that was interpreted as

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**Table 4.** Frequencies, amplitudes, linewidths, and their associated uncertainties for the models described in the text.

| Method            | \( M (M_\odot) \) | \( R (R_\odot) \) | \( t (\text{Gyr}) \) | \( \log g \) |
|-------------------|------------------|------------------|----------------|-------------|
| BaSTI Canonical   | 1.51\( ^{+0.12}_{-0.17} \) | 3.14\( ^{+0.09}_{-0.06} \) | 2.16\( ^{+0.13}_{-0.06} \) | 3.62\( ^{+0.01}_{-0.02} \) |
| BaSTI Overshooting| 1.47\( ^{+0.09}_{-0.12} \) | 3.12\( ^{+0.06}_{-0.09} \) | 2.50\( ^{+0.10}_{-0.25} \) | 3.62\( ^{+0.01}_{-0.01} \) |
| RADIUS            | 1.56 \( \pm 0.06 \) | 3.16 \( \pm 0.05 \) | 1.98 \( \pm 0.34 \) | 3.63 \( \pm 0.01 \) |
| ASTEC             | 1.55 \( \pm 0.13 \) | 3.18 \( \pm 0.18 \) | 1.87 \( \pm 0.51 \) | 3.62 \( \pm 0.03 \) |
due to star spots (García et al. 2011, KASC-4 meeting). For both stars, a fast surface rotation rate was inferred. An initial link between the reduction in the amplitude of the dipole modes and a fast surface rotation was proposed. Unfortunately, this idea was very rapidly abandoned. Indeed, from the ensemble analysis performed by Mosser et al. (2012a), the reduction in amplitude of the dipole modes is more pronounced for stars with higher $\nu_{\text{max}}$. If the physical mechanism depended on stellar rotation, we would have expected to find some scatter in the visibilities because the rotation rate of the star is not a direct function of $\nu_{\text{max}}$ in the subgiant or giant evolutionary stage.

Concerning KIC 8561221, our analysis provides us with two indicators of rotation. First, the analysis of the rotational modulation of the light curve allows us to retrieve the surface rotation frequency of around 0.13 $\mu$Hz. Moreover, the seismic characterisation provides us with the mean rotational splitting for $\ell = 2$ and $\ell = 3$ modes, that is around 0.29 and 0.65 $\mu$Hz (see Fig. 7). Computing the rotational kernels with a stellar model as described in the previous section, we found that to explain this difference, the radiative region should – on average – rotate four to eight times faster than the convective zone (assumed to spin at the surface value). This is in good agreement with the previously analysed red giant stars that are in a similar evolutionary stage. Indeed, for the three, more evolved, red giants analysed by Beck et al. (2012), it has been found that their cores rotate ten times faster than the envelope, while for another early red giant star, KIC 7341231, Deheuvels et al. (2012) have inferred a core-to-surface rotation ratio of five. As such, KIC 8561221, rotates slowly enough that a first-order perturbative analysis is sufficient to model the effects of rotation (Goupil et al. 2013; Ouazzani et al. 2013). Nonetheless, in what follows, we consider higher order effects to see whether they can provide insight into the present observations.

At higher rotation rates, one should observe uneven frequency multiplets. This is caused by higher order effects of rotation and, in the case of red giants, by different p-g mode trapping of individual members of a given frequency multiplet, thereby leading to different mode inertias (Ouazzani et al. 2013). If one focusses on $m = 0$ modes, centrifugal deformation affects the frequencies of quadrupole modes before those dipole modes (this can be seen, for instance, in the frequency spectra of Reese et al. 2013). In order to modify the frequencies of axisymmetric dipole modes alone, one could thus imagine that only the...
innermost parts of the star is rotating very rapidly. In this case, only the mixed dipole modes would be affected since they are the only ones that reach this region while retaining a significant amplitude at the stellar surface. Indeed, the coupling of the \( \ell = 2 \) modes would be small in stars close to the base of the red-giant branch as KIC 8561221. However, the ensemble analysis done by Mosser et al. (2012b) showed that the frequencies of the dipole modes are located where they are expected from theory. Likewise, the dipole modes measured in KIC 8561221 at high frequency are at the expected frequencies, and the only issue is a smaller-than-expected amplitude.

One can then turn to mode visibilities. Recently, Reese et al. (2013) carried out visibility calculations in rapidly rotating 2 \( M_\odot \) ZAMS models. Their Fig. 7 indicates an increase in the visibilities of dipole modes at 10% and 20% of the critical rotation rate. However, the mode normalisation applied in that work is inappropriate for solar-like oscillators. If we renormalise these modes so that their kinetic energy is constant, then at low inclination angles, dipole modes are more visible than other modes in the non-rotating case, but then their amplitudes decrease relative to the other modes so as to reach a similar level as the \( \ell = 0 \) modes at 30% of the critical rotation rate. Although this effect goes in the right direction for the present study, it is much too subtle given that the surface rotation rate of KIC 8561221 is below 1% of the critical rotation rate, and that the observed amplitudes of the \( \ell = 1 \) modes are significantly below that of the \( \ell = 0 \) modes. Rapid rotation therefore remains an unlikely explanation for the lower amplitudes of the dipole modes.

Up to now there has been no simple explanation that could link the reduction of \( \ell = 1 \) mode amplitudes to a rapid internal rotation. To go further, one should study the impact of rotation on the excitation and damping of modes, and that requires a non-adiabatic treatment accounting for rotation.

### 4.2. Mode inertia

Since KIC 8561221 is the least evolved red giant star with depressed dipolar modes we may even ask ourselves whether it belongs to this sequence of stars (Mosser et al. 2012a). It is the first star in which we observe both normal and depressed dipolar modes. In fact, KIC 8561221 has evolved to a point where \( \ell = 1 \) and 2 modes are mixed, although the amplitudes of the g-dominated \( \ell = 2 \) modes are very low. In particular, between two consecutive radial modes there may not be any \( \ell = 1 \) modes with a clear p-mode character. This gives rise to the question of whether the depressed dipolar modes in this star are due to a fortuitous circumstance where all the \( \ell = 1 \) modes in the lower part of the observed frequency range behave like g-dominated mixed modes with low amplitudes, while regular p modes would be present at higher frequencies. Figure 11 shows schematic frequency spectra for the observations (top row) and some models with similar global seismic properties. The models were computed with the CESAM code (Morel 1997), while frequencies were computed in the adiabatic approximation with the ADIPLS code (Christensen-Dalsgaard 2008a). Because of the surface effects, the theoretical mode frequencies would have appeared shifted if they were directly compared with the observed values. To simplify the comparison, the theoretical frequencies have been decreased by a dimensionless factor to improve visual comparison. Although the true correction should be lower for core-trapped modes, as indicated in the Sect. 3, in Fig. 11 we have kept the actual theoretical spectrum patterns.

The ratio between the surface rms amplitude and the energy of the mode is proportional to \( 1/\nu E \) where \( E \) is the dimensionless mode inertia. For low-degree modes that are excited stochastically in the upper layers of the convection zone, one expects that their energy and damping would be mainly a function of frequency and that the observed \( m \)-averaged amplitude would have the form \( f(\omega)/\sqrt{\nu E} \). Hence, in a given frequency range, the ratio between the mean amplitude of the dipolar and the radial modes would be proportional to \( (\sqrt{\nu E_d})/(\sqrt{\nu E}) \). In the absence of mixed modes, this ratio is roughly constant. The same behaviour can be expected for evolved red giants where p-dominated mixed \( \ell = 1 \) modes contribute the most to \( (\sqrt{\nu E}) \). In fact, from an observational point of view, Mosser et al. (2012a) computed the integrated power spectrum over frequency bands centred on the expected central frequencies for different degrees and find that the power ratios, both between the \( \ell = 1 \) and \( \ell = 0 \) modes and the \( \ell = 2 \) and \( \ell = 0 \) modes, were approximately constant for all the “normal” stars or at most that the ratios change gradually with \( \nu_{\max} \). The set included RGB stars with \( \nu_{\max} \lesssim 200 \) \( \mu \)Hz, which all have large numbers of mixed \( \ell = 1 \) modes clustered around each \( p \) mode.

As mentioned above, KIC 8561221 is in an evolutionary stage in which such arguments could be invalid. A priori, significant changes in the ratio \( (\sqrt{\nu E_d})/(\sqrt{\nu E}) \) cannot be rejected. This could explain the observed power spectrum while keeping the theoretical energy ratios. According to the observed amplitudes in KIC 8561221, the transition between the normal and the depressed dipole modes is around \( \nu_{\max} \). Therefore, we have verified that for some specific models the power above and below \( \nu_{\max} \) is very different in comparison to the normal case. To be more specific, we estimate \( \nu_{\max} \) from the \( T_{\text{eff}} \) and \( \log g \) computed from the models, and then we search for the radial mode closest to that frequency, \( \nu(\ell = 0, n \approx n_{\max}) \). Finally, we compute the ratios

\[
r_{\ell}=\frac{E(n=n_{\max}\pm\Delta n/2;\ell=0)}{\left(\sum_{n}1/E(\ell=1)\right)^{-1}(\Delta n+1/2)} \sim \frac{\langle \Lambda^2 \rangle_{\ell=1}}{\langle \Lambda^2 \rangle_{\ell=0}} \quad (2)
\]

where the sum over \( i \) is for all the \( \ell = 1 \) modes in the frequency range \( [\nu(\ell = 0, n \approx n_{\max} - \Delta n), \nu(\ell = 0, n \approx n_{\max})] \) for the “+” solution and in the frequency range \( [\nu(\ell = 0, n \approx n_{\max}), \nu(\ell = 0, n \approx n_{\max} + \Delta n)] \) for the “−” solution. These ratios are shown in Fig. 12 where a value of \( \Delta n = 3 \) has been chosen as a representative example. In this figure, every pair of red and blue points corresponds to a given model from a 1.5 \( M_\odot \) evolution sequence with the large separation indicated on the ordinate. As explained above, the observations suggest that this ratio can be interpreted as a power amplitude ratio, \( \langle \Lambda^2 \rangle_{\ell=1}/\langle \Lambda^2 \rangle_{\ell=0} \), except for a constant visibility factor.

As seen in Fig. 12 the power of the \( \ell = 1 \) modes on the left of \( \nu_{\max} \) is not very different to that on the right, despite the number and nature of the \( \ell = 1 \) involved. In fact, for the models with the highest \( \Delta \nu \), most of the \( \ell = 1 \) are p modes whereas for the models with the lowest \( \Delta \nu \), mixed modes are predominant. Although for stars with \( \nu_{\max} \approx 30-40 \) \( \mu \)Hz there is a little higher scatter, only a change of 10%–20% in the relative amplitudes could be explained by the fluctuations in the mean mode inertia, far from the observed situation for KIC 8561221. We checked this result against other evolutionary sequences as well as for models with different stellar parameters. The result is always comparable to the one showed in Fig. 12. Hence, we do not have any reason to think that the nature of the mixed modes in the relatively unevolved red giant KIC 8561221 can make this star different compared to more evolved ones with depressed dipolar modes.
Fig. 11. Top: frequency spectrum corresponding to the observed modes (dashed lines). All other spectra (solid lines) are based on theoretical models along a 1.5 $M_\odot$ evolution sequence with large separations $\Delta \nu$ around the observed value. Theoretical frequencies have been decreased by a constant factor to improve visual comparison. Different colours correspond to different degrees as in Fig. 6: $\ell = 0$ (black), $\ell = 1$ (blue), $\ell = 2$ (red), and $\ell = 3$ (pink). The amplitudes of the theoretical modes have been scaled to $1/\sqrt{E}$ relative to the radial modes except for the $\ell = 3$ modes, which in addition contain a 0.3 factor (to improve the visibility). The numbers on the left are the values of the large separation $\Delta \nu$ in $\mu$Hz. Grey shaded regions are done to guide the eye.

Fig. 12. Energy ratios $r_+$ (red plusses) and $r_-$ (blue diamonds) versus $\Delta \nu$ computed for a 1.5 $M_\odot$ evolution sequence. See text for details.

4.3. Damping

For common red giants observed by Kepler, the power of the $g$-dominated mixed modes have smaller width than the regular $p$ modes. This result can be expected because most of the damping is produced in the envelope layers, while for $g$-dominated mixed modes this region contributes relatively less to the total work than for $p$-dominated ones. However, as shown in Fig. 6, the width of the dipole modes below $\nu_{\text{max}}$ is greater than for the rest of the modes. A strong damping in the core could explain the lower power observed for these dipole modes.

It is interesting to notice that the damping in the core is very important for highly evolved – very luminous – red giants (e.g. Dziembowski 1977, 2012). In fact, for these stars the damping is expected to make $g$-dominated mixed modes hardly observable. However, $\ell = 1$ $p$-dominated modes are very effectively trapped in the envelope, so at least one of such modes should have high amplitudes between every radial mode. Dupret et al. (2009) computed theoretical amplitudes for selected red giants and showed how the damping changes with evolution and luminosity through the red giant branch. For low-luminosity stars, the core damping becomes lower than the one in the envelope and the $g$-dominated mixed modes are then expected to be observed, as is the case for the large majority of red giants studied with CoRoT and Kepler.

Here we consider models that match – to a high accuracy – the fundamental parameters (and oscillation frequencies) of KIC 8561221 derived in the previous section, namely the model in Fig. 11 with $\Delta \nu = 29.85$ $\mu$Hz. This model has a mass of $M = 1.5 M_\odot$, a luminosity of $L = 7.23 L_\odot$, and an effective temperature of $T_{\text{eff}} = 5281$ K.

First we estimated pulsation linewidths for radial modes that include a full nonadiabatic treatment and convection dynamics in the stability computations. Both the convective heat and momentum (turbulent pressure) fluxes were treated consistently in both the equilibrium and pulsation computations, using the nonlocal generalisation of the Gough (1977a,b) time-dependent convection model. The computations were carried out as described by Houdek et al. (1999) and Houdek & Gough (2002). For the nonlocal convection parameters we adopted the
envelope damping through all the observed frequency range. As
cencies (the scale is logarithmic), it is negligible compared to the
(g-mode cavity) damping rate increases rapidly at low frequen-
crates computed using only the eigenfunctions in the
dial mode with the same frequency. We also represent damping
ing the whole star, and modes with p-dominated character, that
for the indicated model, the damping rate computed by consider-
the imaginary part of the frequency, \(2\eta\) (see Fig. 10) would not make any
difference.

4.4. Influence of a deep magnetic field

The presence of a deep (fossil) magnetic field in the stably strat-
ified inner core of the star could be evoked as a possible reason for
the reduction of the amplitude of the dipole \(l = 1\) modes. Here again, one can expect that the mixed dipole modes would
be most sensitive to such a magnetic field as they are the only
observed modes that can have high amplitudes in the core.

Magnetic fields could contribute to reducing the amplitude of the dipole modes through the following effects:

1. If a strong (axisymmetric) magnetic field exists, that is not
aligned with the rotation axis, the effects of the magnetic
field and rotation lift the degeneracy of dipole modes (with
a given radial order) with respect to the azimuthal order, \(m\),
which produces three eigenmodes (for \(m = 0, \pm1\) with dif-
frent frequencies in the rotating frame. If we observe these
modes in the inertial (observer’s) frame, each of them has
three frequency components owing to the advection effects
(e.g. Goode & Thompson 1992; Shibahashi & Takata 1993).
Therefore, it is possible to observe nine frequency compo-
nents in total that come from dipole modes with a given
radial order. Provided that the kinetic energy of each eigen-
mode is not changed by the magnetic field, the increase in the
number of the frequency components results in the reduction
of their amplitudes.

2. More energy is needed to displace each mass element to a
fixed amplitude against the Lorentz force in the presence of
the magnetic field. This means that the amplitude is lower, if
the mode energy is the same.

3. The magnetic field generally modifies the eigenfunction of
the dipole modes to have components with higher spherical
degrees, which suffer stronger geometrical cancellation
when observed. Since part of the mode energy goes to those
additional components with lower visibility, the total ampli-
tude of the distorted dipole mode in the power spectrum gets
smaller.
It is beyond the scope of the present work to quantify the magnitude and geometrical topology of the magnetic field to reproduce the observed effect on the \( \ell = 1 \) modes, while keeping at the same time a negligible influence of this magnetic field on higher degree modes. However, there is no evidence of magnetic splitting or shift in other modes. The standard models fit the frequencies of the \( \ell = 0, 2, \) and 3 modes with a similar accuracy to those of normal red giants. Therefore, there is no observational support in favour of a strong (fossil) magnetic field in the core of this star.

5. Conclusions

In this paper we have studied KIC 8561221, which is the least evolved observed star with depressed dipole modes, in order to better understand the possible physical mechanisms responsible for the reduction of the amplitude of these modes. KIC 8561221 background parameters were found to be normal and they follow the relation described in Mathur et al. (2011b). The detailed analysis of the light curve showed a modulation in the brightness of the star that we assumed to be due to spots crossing the stellar disk. Our analysis of the surface rotation suggests a rotation period of 91 days. It is slower than expected following standard calculations for stars in the range 1.4 to 1.5 \( M_\odot \). A lower rotation rate is possible if the precursor was a chemically peculiar star or if the star slowed down owing to a strong magnetic braking. Indeed, the variation in the scale-averaged time series around the rotation period indicates that the star still has a surface dynamo magnetic field. We have also unveiled changes in the photometry suggesting an on-going magnetic activity cycle.

The detailed seismic analysis concluded that KIC 8561221 is an early red giant located at the base of the RGB. Modes with \( \ell = 0, 1, 2, \) and 3 were observed and seismically characterised. Frequencies of all the detected modes were found at the expected locations, ruling out a very fast spinning interior. Moreover, the splitting of the modes with \( \ell = 2, 3 \) indicate that the interior is rotating four to eight times faster than the surface, a similar rate to other RGB stars.

However, the dipole amplitudes were found to be much lower than expected, in particular below \( v_{\text{max}} \), while their widths were higher than expected. The amplitudes of the \( \ell = 2 \) modes were also found to be lower than expected, although to a lesser extent. While the latter could be explained by an energy leakage towards the \( g \)-dominated \( \ell = 2 \) mixed modes, current models of mode damping are unable to explain the observed reduction in the amplitudes of the dipole modes. Unlike more evolved stars in the sequence, in KIC 8561221 only one or two dipole modes are expected between two consecutive radial modes. This means that for some radial orders there is not a single clear \( p \)-dominated \( \ell = 1 \) mode. However, our analysis of the mode inertia shows that even when this happens it cannot explain the observed amplitude of the dipole modes. As a result, we expect that KIC 8561221 has the same unknown physical mechanism operating as in the other stars showing low-amplitude dipole modes. As shown in this paper, there is evidence for a strong dynamo magnetic field on the surface of KIC 8561221. It is very tentative to link this surface magnetic activity with the amplitude reduction of the dipolar modes. However, it seems that only a fossil magnetic field in the core could differentiate between the \( \ell = 1 \) modes and other non-rotational influences. The lack of any observational evidence of magnetically split components or frequency shift makes the hypothesis of a strong core magnetic field unlikely.

The next step will be to do an ensemble study of all the Kepler red giants showing depressed dipole modes, not only in the set of stars analysed by Mosser et al. (2012a) but also in the 13,000 red-giant stars studied by Stello et al. (2013). Complementary ground-based observations of some of these stars could also be necessary to solve this puzzle.

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References

Aerts, C., Christensen-Dalsgaard, J., & Kurtz, D. W. 2010, Asteroseismology (Springer Science+Business Media B.V.)
Angulo, C., Arnold, M., Ruyet, M., et al. 1999, Nucl. Phys. A, 656, 3
Baglin, A., Auvergne, M., Boissard, L., et al. 2006, in COSPAR, Plenary Meeting, 36th COSPAR Scientific Assembly, 36, 3749
Ballot, J., García, R. A., & Lambert, P. 2006, MNras, 369, 1281
Ballot, J., Barban, C., & van’t Veer-Memmeret, C. 2011a, A&A, 531, A124
Ballot, J., Gizon, L., Samadi, R., et al. 2011, A&A, 530, A97
Barban, C., Matthews, J. M., De Ridder, J., et al. 2007, A&A, 468, 1033
Basri, G., Walkowicz, L. M., & Reiners, A. 2013, ApJ, 769, 37
Basu, S., Chaplin, W. J., & Elsworth, Y. 2010, ApJ, 710, 1596
Basu, S., Grundahl, F., Stello, D., et al. 2011, ApJ, 729, L10
Beck, P. G., Bedding, T. R., Mosser, B., et al. 2011, ApJ, 732, 205
Beck, P. G., Montalban, J., Kallinger, T., et al. 2012, Nature, 481, 55
Bedding, T. R., Huber, D., Stello, D., et al. 2010, ApJ, 713, L176
Bedding, T. R., Mosser, B., et al. 2011, Nature, 471, 608
Benomar, O., Appourchaux, T., & Baudin, F. 2009, A&A, 506, 15
Benomar, O., Bedding, T. R., Mosser, B., et al. 2013, ApJ, 767, 158
Böhm-Vitense, E. 1958, ZAp, 46, 108
Borucki, W. J., Koch, D., Basri, G., et al. 2010, Science, 327, 977
Bruntt, H., Bedding, T. R., Quirion, P.-O., et al. 2010, MNras, 405, 1907
Bruntt, H., Basu, S., Smalley, B., et al. 2012, MNras, 423, 122
Bozasi, D., Czaban, J., Laher, R., et al. 2000, ApJ, 532, L133
Campante, T. L., Handberg, R., Mathur, S., et al. 2011, A&A, 534, A6
Christensen-Dalsgaard, J. 2008a, Ap&SS, 316, 113
Christensen-Dalsgaard, J. 2008b, Ap&SS, 316, 13
Cunha, M. S. 2005, J. Astrophys. Astron., 26, 213
De Ridder, J., Barban, C., Baudin, F., et al. 2009, Nature, 459, 398
Deheuvels, S., García, R. A., Chaplin, W. J., et al. 2012, ApJ, 756, 19
Domingo, V., Fleck, B., & Poland, A. I. 1995, Sol. Phys., 162, 1
Dogan, G., Metcalfe, T. S., & Scotland, D. 2013, ApJ, 763, 49
Dupret, M., Belkacem, K., Samadi, R., et al. 2009, A&A, 506, 57
Dziembowski, W. A. 2012, A&A, 539, A84
Dziembowski, W. A. 2012, A&A, 539, A83
Ferguson, J. W., Alexander, D. R., Allard, F., et al. 2005, ApJ, 623, 585
Fiery Frailion, D., Gelly, B., Schmidt, F. M., et al. 1998, A&A, 333, 362
Frandsen, S., Carrier, F., Aerts, C., et al. 2002, A&A, 394, L5
Frohlich, C., Romero, J., Roth, H., et al. 1995, Sol. Phys., 162, 101
García, R. A., Régnier, C., Samadi, R., et al. 2009, A&A, 506, 41
García, R. A., Hekker, S., Stello, D., et al. 2011, MNras, 414, L6
Table 3. Frequencies, amplitudes, and linewidths for all the modes computed with the MCMC for case 3.

| l | Frequency (µHz) | σ    | Linewidth (µHz) | +σ   | −σ   | Power (ppm²/µHz) | +σ   | −σ   |
|---|----------------|------|-----------------|------|------|-----------------|------|------|
| 0 | 370.33         | 0.06 | 0.36            | 0.11 | 0.23 | 10.37           | 2.26 | 2.73 |
| 0 | 399.34         | 0.02 | 0.24            | 0.04 | 0.05 | 70.03           | 12.57| 18.21|
| 0 | 428.91         | 0.02 | 0.44            | 0.07 | 0.09 | 46.48           | 9.78 | 11.39|
| 0 | 458.64         | 0.01 | 0.37            | 0.04 | 0.05 | 113.92          | 17.26| 20.66|
| 0 | 488.34         | 0.00 | 0.40            | 0.03 | 0.03 | 152.80          | 17.46| 18.89|
| 0 | 518.12         | 0.03 | 0.51            | 0.06 | 0.07 | 88.67           | 12.32| 18.29|
| 0 | 548.03         | 0.05 | 0.76            | 0.09 | 0.11 | 32.36           | 4.34 | 5.07 |
| 0 | 578.37         | 0.09 | 1.01            | 0.17 | 0.18 | 12.55           | 2.25 | 2.78 |
| 0 | 608.72         | 0.11 | 1.33            | 0.21 | 0.23 | 7.39            | 1.13 | 1.43 |
| 0 | 638.67         | 0.42 | 1.70            | 0.55 | 0.71 | 1.47            | 0.39 | 0.44 |
| 1 | 503.83         | 0.17 | 1.99            | 0.85 | 0.57 | 5.49            | 1.26 | 2.40 |
| 1 | 535.21         | 0.10 | 0.99            | 0.18 | 0.27 | 11.49           | 2.64 | 3.00 |
| 1 | 567.26         | 0.12 | 0.75            | 0.21 | 0.32 | 5.58            | 1.66 | 1.40 |
| 1 | 591.27         | 0.15 | 0.96            | 0.30 | 0.38 | 6.63            | 1.77 | 2.23 |
| 1 | 625.23         | 0.25 | 1.64            | 0.47 | 0.52 | 2.54            | 0.64 | 1.07 |
| 1 | 660.36         | 0.29 | 1.32            | 0.38 | 0.47 | 1.58            | 0.52 | 0.59 |
| 2 | 367.72         | 0.37 | 0.36            | 0.11 | 0.23 | 3.92            | 0.80 | 1.03 |
| 2 | 396.38         | 0.03 | 0.24            | 0.04 | 0.05 | 26.62           | 4.92 | 7.42 |
| 2 | 426.25         | 0.17 | 0.44            | 0.07 | 0.09 | 17.54           | 3.79 | 4.70 |
| 2 | 455.86         | 0.07 | 0.37            | 0.04 | 0.05 | 43.22           | 6.67 | 8.57 |
| 2 | 485.51         | 0.06 | 0.40            | 0.03 | 0.03 | 57.83           | 6.89 | 8.56 |
| 2 | 515.43         | 0.06 | 0.51            | 0.06 | 0.07 | 33.63           | 4.72 | 6.48 |
| 2 | 545.53         | 0.08 | 0.76            | 0.09 | 0.11 | 12.29           | 1.76 | 2.08 |
| 2 | 575.47         | 0.17 | 1.01            | 0.17 | 0.18 | 4.75            | 0.87 | 1.11 |
| 2 | 605.11         | 0.37 | 1.33            | 0.21 | 0.23 | 2.80            | 0.45 | 0.57 |
| 2 | 636.60         | 0.70 | 1.70            | 0.55 | 0.71 | 0.56            | 0.15 | 0.18 |
| 3 | 379.13         | 0.82 | 0.36            | 0.11 | 0.23 | 0.85            | 0.21 | 0.26 |
| 3 | 408.13         | 0.62 | 0.24            | 0.04 | 0.05 | 5.80            | 1.18 | 1.59 |
| 3 | 436.93         | 0.19 | 0.44            | 0.07 | 0.09 | 3.78            | 0.84 | 1.13 |
| 3 | 467.03         | 0.15 | 0.37            | 0.04 | 0.05 | 9.25            | 1.39 | 1.94 |
| 3 | 496.95         | 0.10 | 0.40            | 0.03 | 0.03 | 12.49           | 1.69 | 2.06 |
| 3 | 526.69         | 0.16 | 0.51            | 0.06 | 0.07 | 7.30            | 1.08 | 1.33 |
| 3 | 556.69         | 0.26 | 0.76            | 0.09 | 0.11 | 2.66            | 0.45 | 0.49 |
| 3 | 587.09         | 0.40 | 1.01            | 0.17 | 0.18 | 1.03            | 0.23 | 0.29 |
| 3 | 618.62         | 0.62 | 1.33            | 0.21 | 0.23 | 0.61            | 0.11 | 0.13 |
| 3 | 650.38         | 0.61 | 1.70            | 0.55 | 0.71 | 0.12            | 0.03 | 0.04 |
Appendix A: Evaluating the reliability of the fitted results

In order to verify the reliability of the results, we tested the robustness of our measurements of the frequencies, widths, heights, and rotational splittings using simulated spectra that reproduce the general properties of KIC 8561221. The present appendix summarises the results from these tests.

Usually, reliability is assessed using artificial spectra that mimic the known properties of the stellar oscillations and of the noise by the means of a limit spectrum and of an excitation function. However, this assumes that the physics and the noise properties are perfectly known. This is not the case since stars often behave differently than predicted by theory (e.g. the case of the so-called surface effects or, in the present case, puzzling depressed dipole modes). Therefore, rather than using an artificial spectra, we used a modified spectrum of a reference star (KIC 9574283) with very similar global properties (cf. Table A.1), but with clear split $\ell = 1$ modes.

The physics of stochastically driven modes tells us that a real star power spectrum $S_R^* (\nu)$ can be written as

$$S_R^* (\nu) = M_R^* (\nu) F(\nu),$$  \hspace{1cm} (A.1)

where $M_R^*$ is the limit spectrum and $F(\nu)$ a random noise function (see more details in Fierry Fraillon et al. 1998). The limit spectrum $M_R^*(\nu)$ is unknown by definition but can be written as a function of an approximate model $M_R(\nu)$ and of an error function $\epsilon_R^*(\nu)$. Therefore, $M_R^*(\nu) = M_R(\nu) + \epsilon_R^*(\nu)$, and we can define a new noise function $F^*(\nu)$

$$F^*(\nu) = S_R^* (\nu) / M_R^* (\nu) = F(\nu) \left( 1 + \epsilon_R^*(\nu) / M_R(\nu) \right).$$  \hspace{1cm} (A.2)

In such case, $F^*(\nu)$ contains information on the excitation function, the instrumental noise, and the model inaccuracies. Using $F^*(\nu)$ we can now build a simulated spectrum $S_A$, where:

$$S_A(\nu) = M_A(\nu) F^*(\nu) \left( 1 + \epsilon_R(\nu) / M_R(\nu) \right).$$  \hspace{1cm} (A.3)

Here, $M_A(\nu)$ is the desired limit spectrum and corresponds to an altered version of the model $M_R(\nu)$ such that $M_A(\nu) = \alpha(\nu) M_R(\nu)$. In this expression, $\alpha(\nu)$ acts as a filter.

In our application, $M_A(\nu)$ is determined by the best fit of the reference power spectrum of the reference star. We modified $\alpha(\nu)$ to reduce the height of the $\ell = 1$ modes to a similar signal-to-noise as in KIC 8561221 ($S/N \approx 2$) when their frequency is greater than $\nu_{\text{max}}$, and by removing the $\ell = 1$ modes when their frequencies are lower than $\nu_{\text{max}}$. All the other mode parameters were unchanged. An example of the results can be seen in Fig. A.1.

This method ensures that the simulated spectra contains the unknown physics from the reference star as well as any unknown source of noise, which makes it very realistic. In addition, the alteration factor $\alpha(\nu)$ is a known deterministic modification that only controls the limit spectrum properties. Therefore, by modifying $\alpha(\nu)$, we are sure that we only evaluate its effect and not, for example, an effect of the random noise. In our case, we can therefore evaluate the effect of low signal-to-noise, $\ell = 1$ modes on parameters of the reference star KIC 9574283, by comparing the results of the original spectrum of this star with the modified spectrum. This method has also been applied to a second star, KIC 8751420, with a higher inclination angle (64.4 $\pm$ 1.5) and a higher $\ell = 0$ signal-to-noise ($\approx 55$). The conclusion being the same, we only describe the results on KIC 9574283.

We compared the measured mode parameters (frequencies, width, height, splitting) before and after modifying of the reference spectrum. Although the altered spectrum provides larger uncertainties, results remain compatible at the 1$\sigma$ level. However, we notice that the uncertainty in the inclination angle is increased by the lack of information from the dipole modes, although the median remains quite robust (see Figs. A.2 and A.3). We also notice that the dipole splittings measured on

| Table A.1. Global properties of the modes for KIC 8561221, compared to KIC 9574283 (reference star), using a MCMC mode-fitting algorithm. |
|-----------------|-----------------|-----------------|
| Parameter       | KIC 8561221     | KIC 9574283     |
| $\Delta \nu$ (\mu Hz) | 29.79 $\pm$ 0.14 | 29.8 $\pm$ 0.21 |
| $\nu_{\text{max}}$ (\mu Hz) | 491 $\pm$ 5 | 450 |
| $\Delta P_1$ (s) | Unknown | 117 |
| Maximum $S/N$ (\ell = 0) | $\leq$30 | $\leq$35 |
| Inclination (deg) | Unknown | 44.8 $\pm$ 1.4 |
| $\delta \nu_0$ (\ell = 1) | 0.15 $\pm$ 0.008 |
| $\delta \nu_0$ (\ell = 3) | [0.3, 0.6] | 0.097 $\pm$ 0.015 |

Fig. A.1. Simulated spectra generated by modifying the signal-to-noise of dipole modes of the reference star KIC 9574283. Bottom: the original reference spectrum. Top: the modified spectrum with a $S/N$ of the dipole modes $\approx$2, such as in KIC 8561221.
the altered spectrum can be measured at best with a precision of $\sigma = 0.05\ \mu Hz$ (mode of S/N around 3) and at worst with a precision of $\sigma = 0.6\ \mu Hz$ (mode of S/N around 1). Although the lower precision is typical of what we measured for $\ell = 1$ in KIC 8561221, the best precision is much better than what is achievable in this star. Also $\ell = 2$ and $\ell = 3$ splittings of the reference star are changed because of the increase in the uncertainty of the inclination angle, even if we did not modify these mode properties. In the reference spectrum, the inclination angle $i \approx 45^\circ$ means that $\ell = 1$ are triplets of the same amplitude. This eases the measure of the splitting and explains the precision of $\sigma = 0.05$ achieved in the best case.

Our tests therefore suggest that in the case of KIC 8561221, the inclination angle of $\sim 20^\circ$ is probably correct. Indeed, if the inclination were higher (say $i > 40$), the splitting of the dipole modes would have been well constrained, as well as the inclination. This is not what we obtained in the analysis of KIC 8561221, which indicates a low-inclination angle.