SPECTRA AND LIGHT CURVES OF FAILED SUPERNOVAE

Chris L. Fryer1,2, Peter J. Brown3, Filomena Bufano4, Jon A. Dahl1, Christopher J. Fontes1, Lucille H. Frey1, Stephen T. Holland5, Aimee L. Hungerford1, Stefan Immler5, Paolo Mazzali6,7,8, Peter A. Milne9, Evan Scannapieco10, Nevin Weinberg11, and Patrick A. Young10
1 Los Alamos National Laboratory, Los Alamos, NM 87545, USA; fryer@lanl.gov, dahl@lanl.gov, cjf@lanl.gov, aimee@lanl.gov
2 Physics Department, University of Arizona, Tucson, AZ 85721, USA
3 Department of Astronomy & Astrophysics, Pennsylvania State University, University Park, PA 16802, USA; grbpeter@yahoo.com
4 Dipartimento di Astronomia, Univ. Padova, INAF-Osservatorio Astronomico di Padova, Italy; filomena.bufano@oapd.inaf.it
5 Astrophysics Science Division, NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA; sholland@milkyway.gsfc.nasa.gov, stefan.m.immler@nasa.gov
6 Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, 85748 Garching, Germany; mazzali@MPA-Garching.MPG.DE
7 Padova: INAF-Osservatorio Astronomico di Padova, Padova, Italy
8 Scuola Normale Superiore, Piazza dei Cavalieri, 7, 56126 Pisa, Italy
9 Steward Observatory, 933 North Cherry Avenue, RM N204, Tucson, AZ 85721, USA; pmilne511@cox.net
10 SESE, Arizona State University, Tempe, AZ 85287, USA; evan.scannapieco@asu.edu, patrick.young.1@asu.edu
11 Astronomy Department and Theoretical Astrophysics Center, University of California, Berkeley, 601 Campbell Hall, Berkeley, CA 94720, USA; nweinberg@astro.berkeley.edu

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ABSTRACT

Astronomers have proposed a number of mechanisms to produce supernova explosions. Although many of these mechanisms are now not considered primary engines behind supernovae (SNe), they do produce transients that will be observed by upcoming ground-based surveys and NASA satellites. Here, we present the first radiation-hydrodynamics calculations of the spectra and light curves from three of these “failed” SNe: SNe with considerable fallback, accretion-induced collapse of white dwarfs, and energetic helium flashes (also known as type Ia SNe).

Key words: gravitational waves – neutrinos – supernovae: general – white dwarfs

Online-only material: color figures

1. INTRODUCTION

Supernovae (SNe) and gamma-ray bursts (GRBs) are among the brightest transients in the universe. As such, they have been well studied, both observationally and theoretically. Although many theoretical models have been proposed to explain the engines behind these explosions, astronomers have focused on a few, best-fitting “standard” models. The rest of the models were, for the most part, discarded because either the engine, when studied in more detail, could not explain the observed supernova (SN)/GRB characteristics (e.g., the explosion was weaker than that needed to explain most SNe or GRBs) and/or the rate of explosions was below the observed SN or GRB rate.

These “failed” SNe have been neglected: very few studies have focused on their explosions and virtually no studies have calculated the emission from the explosions. With their typically dimmer outbursts and often lower rates, these objects were unlikely to have a large presence in past SN surveys. But current (Palomar Transient Factory, PanSTARRS) and upcoming (SkyMapper, VLT Survey Telescope, One Degree Imager, Large Synoptic Survey Telescope) transient surveys are beginning to observe these neglected transients. In this paper, we present some of the first spectra and light curves from radiation-hydrodynamics models of a few of these transients to both help guide searches and use the observations of the transients to constrain our understanding of the explosions.

The emission from explosions is powered by two primary sources: the decay of radioactive elements produced in the explosion and shock heating as the ejecta blows through the medium surrounding it. These two energy sources play varying roles in SNe and GRBs. We believe that shock heating (albeit through shock acceleration mechanisms) powers the emission in GRBs (e.g., Meszaros & Rees 1992). Fryer et al. (2006b) found that even the GRB-associated SN could well be dominated by shock heating. For SNe, the dominant energy source depends on the class or type of SNe: the decay of radioactive 56Ni and its daughter products dominate the type Ia emission but for many type Ib/c and II SNe, shock heating can dominate the emission at peak (e.g., L. H. Frey et al. 2009, in preparation). The radiation-hydrodynamics calculations in this paper allow us to include both power sources and determine the crucial conditions behind the observed emission of these explosions.

Many transients also are sources of gravitational wave (GW) and neutrino emission. The possible GW and neutrino signals from standard SN and GRB engines have been studied in detail and the broad set of studies for these outbursts exhibit some of the features from failed SNe. But failed SN will have slightly different GW and neutrino features from normal SNe and these differences can be used to help us understand both explosion mechanisms better. Neutrino and GW observations of failed SNe provide complementary (and, in some cases, stronger) probes of nuclear physics and general relativity.

In this paper, we study three “failed” SN models: accretion-induced collapse (AIC) of a white dwarf (WD; Section 3), dim SNe produced by fallback (Section 4), and type Ia SNe (Section 5). We review the engine and its environment, estimate the occurrence rate, show spectral and light curve results from radiation-hydrodynamics calculations (using the Radiation Adaptive Grid Eulerian (RAGE) SN emission code—see Section 2) of these explosions. In Section 6, we discuss the neutrino and GW emission for each of these explosions. We conclude with a comparison to specific potential “failed” SNe currently in the literature.

12 Explosions that do not produce the standard models for SNe.
2. CODE DESCRIPTION

To include shock heating in our light curve calculations, we must couple our radiation transport calculation with a hydrodynamics package. For our radiation–hydrodynamics calculations, we use the multidimensional radiation–hydrodynamics code RAGE, which was designed to model a variety of multimaterial flows (Baltrusaitis et al. 1996). The conservation equations for mass, momentum, and total energy are solved through a second-order, direct-Eulerian Godunov method on a finite-volume mesh (Gittings et al. 2008). It includes a flux-limited diffusion scheme to model the transport of thermal photons using the Levermore–Pomraning flux limiter (Levermore & Pomraning 1981). RAGE has been extensively tested on a range of verification problems (Holmes et al. 1999; Hueckstaedt et al. 2005) and applied to (and tested on) a range of astrophysics problems (Herwig et al. 2006; Coker et al. 2007; Fryer et al. 2007a, 2007b), including the strong velocity gradients that exist in SN explosions (Lowrie & Rauenzahn 2006).

The RAGE code can be used in one, two, and three dimensions with spherical, cylindrical, and planar geometries in one-dimension, cylindrical and planar geometries in two-dimensions, and planar geometries in three-dimensions. For this paper, we limit our analysis to one-dimensional spherical calculations. RAGE uses an adaptive mesh refinement technique, allowing us to focus the resolution on the shock and follow the shock as it progresses through the star. Even so, we were forced to regrid in the calculations to ensure that the shock was resolved (typically with coarse-grid cell sizes set to a few percent of the shock position and fine grid cell sizes set to a fraction of a percent) at early times but still allow us to model the shock progression out to 40–100 days (the shock moves from 10⁹ cm out to 10¹⁶ cm in the course of a simulation).

For most of our calculations, the energy released from the decay of ⁵⁶Ni and ⁵⁶Co is deposited directly at the location of the ⁵⁶Ni using the following formula:

\[
dE/dt = E_{Ni}/\tau_{Ni}e^{-t/\tau_{Ni}} + E_{Co}/(\tau_{Co} - \tau_{Ni})[e^{-t/\tau_{Co}} - e^{-t/\tau_{Ni}}],
\]

where \(E_{Ni} = 1.7\) MeV and \(E_{Co} = 2.9\) MeV are the mean energies released per atom for the decay of ⁵⁶Ni and ⁵⁶Co, respectively, and \(\tau_{Ni} = 7.6 \times 10^5\) s, \(\tau_{Co} = 9.6 \times 10^6\) s. Especially at late times, this energy is not deposited into the matter surrounding it, but rather escapes the star.

In order to test the accuracy of the assumption of in situ energy deposition, we have run a single simulation including the transport of the gamma rays emitted during the decay of ⁵⁶Ni and its daughter product ⁵⁶Co. These results are compared with our local deposition models. To solve the transport equation in this calculation, we use the discrete ordinates “S_0” method (Wick 1943; Chandrasekhar 1950; Carlson 1955). In the spherical, one-dimensional calculations used here, we discretize the angular variables as

\[
\frac{1}{c}\frac{\partial I_{n}(r, v)}{\partial t} + \frac{\mu_{n}}{r}\frac{\partial r^{2}I_{n}(r, v)}{\partial r} + \frac{2}{rw_{n}}[\alpha_{n+1/2}I_{n+1/2}(r, v) - \alpha_{n-1/2}I_{n-1/2}(r, v)] + \sigma_{tot}(r, v)I_{n}(r, v) = \int_{0}^{\infty}d\nu L_{o}(\nu, v)\sum_{l=0}^{L}(2l + 1)\sigma_{\text{scat}, l}(r, \nu)P_{l}([\mu_{n}])
\]

\[\times \sum_{m}P_{l}([\mu_{m}])I_{m}(r, v)w_{m} + Q_{n}(r, v),
\]

where \(c\) is the speed of light, \(I_{n}(r, v)\) is the angular intensity as a function of space coordinate \(r\) and photon energy \(v\), \(\mu_{n} = \cos \theta_{n}\) is the discretized \(\mu\) and is taken from the abscissas of the standard one-dimensional Gauss Legendre quadrature with \(w_{n}\) the weights of this quadrature, \(\alpha_{n+1/2} = \alpha_{n-1/2} = \mu_{n}w_{n}\) is the angular differencing coefficient (with \(\alpha_{1/2} = 0\), \(\sigma_{tot}(r, v)\) is the macroscopic total cross section, \(\sigma_{\text{scat}, l}(r, \nu)\) is the \(l\)th Legendre moment of the differential scattering cross section, \(P_{l}([\mu_{n}])\) is the Legendre polynomial of \(l\)th order and \(Q_{n}(r, v)\) is our discretized source arising from the radioactive decay. The energy-dependent variable is discretized using standard multi-group theory (we use 12 groups). Spatial and angular cell edges are related to their respective cell centers by the standard diamond difference approach and time integration is done using Crank–Nicholson. The transport operator is inverted using a space-angle sweep, one energy group at a time. The multi-group cross section data come from the Los Alamos MENDF6 library (Little 1996).

For the comparison of our in situ gamma-ray deposition to that of transport, we model a Wolf–Rayet star. The spectra for our in situ gamma-ray deposition and transported gamma-ray calculations are shown in Figure 1. At these early times, the two calculations are identical. The mean free path of gamma rays remains small for this model, and most of the models studied in this paper, for roughly 60 days (longer for some), so the fact that in situ deposition is a good approximation is not surprising. The one exception is our low density IA model. In this IA model, the gamma rays emitted by the decay ⁵⁶Ni are not trapped after ~15 days. We discuss these results further in Section 5.

For opacities, our radiation–hydrodynamics calculations consider a single group using the Rosseland mean opacity for the diffusion coefficient and the Planck mean opacity for the emission/absorption terms in the transport equation.¹³ These gray opacities are obtained from the LANL OPLIB database (Magee et al. 1995; http://www.t4.lanl.gov/cgi-bin/opacity/tops.pl) and have been extensively used in astrophysics modeling, including many problems in SNe (e.g., Fryer et al. 1999b; Deng et al. 2005; Mazzali et al. 2006). This opacity database is continually updated and we use the most recently produced opacity data in all of our calculations. The opacities made available in this database are computed under the assumption that the atomic populations are in local thermodynamic equilibrium at the material temperature. Thus, the opacity can be determined assuming a single temperature in each cell.

As an illustration of the opacities used in our calculations, we have plotted the opacity values from the LANL OPLIB database for a variety of pure elements at three different density/temperature pairs (Figure 2). At low densities, we note that hydrogen in local thermodynamic equilibrium will be completely ionized, even at temperatures as low as 1 eV, because the effect of three-body recombination is suppressed relative to that of photoionization. Thus, bound–bound features associated with the hydrogen atom, such as the Hα line, are not expected to be present under these conditions. The pure elemental opacities are subsequently combined in the appropriate ratios for each cell that is considered in the calculation. Figure 3 shows three different density/temperature pairings for the composition of the surrounding wind medium used in our fallback model.

With our radiation–hydrodynamics calculations, we calculate the temperature structure of the matter in the exploding star as a function of time. Unlike post-process calculations based on

¹³ We have run one calculation in our fallback runs using five groups (see Section 4). Although the basic fluxes remain the same, the spectral line strengths will vary.
purely hydrodynamic models, we can use this matter temperature profile in a post-process approach to determine the full time-dependent spectra from this SN explosion. To calculate the spectrum, we first assume that each radial zone emits radiation isotropically based on its temperature and absorption coefficient:

\[ L_\nu = m_{\text{zone}} \frac{2h\sigma_{\text{abs}}v^3}{c^2} \frac{1}{e^{\nu/T_{\text{mat}}} - 1} d\nu \sqrt{1 - (v/c)^2}, \]  

where \( m_{\text{zone}} \) is the mass of the zone, \( h = 6.626 \times 10^{-27} \text{erg} \) is Planck’s constant, \( c \) is the speed of light, \( v \) is the velocity of that zone, \( (1 - v/c)^2/\sqrt{1 - (v/c)^2} \) is the time dilation effect on the luminosity, \( \sigma_{\text{abs}} \) is the absorption cross section (which depends on composition, temperature, and density), \( \nu \) is the frequency (\( d\nu \) is the size of the frequency bin), and \( T_{\text{mat}} \) is the matter temperature (note that in the exponential, \( \nu \) and \( T_{\text{mat}} \) must have the same units—e.g., \( h\nu/k_{\text{Bolzmann}}T_{\text{mat}} \)).

This equation gives us the emission in each zone, but what we really want is the emission directed toward an observer in a single direction. In order to calculate both accurate mean
free paths through the spherically symmetric zones (to get limb effects) and the correct Doppler shifts, we have discretized each zone into angular bins (Figure 4). For our calculations, we use 40 angle bins. The observed spectrum is then

$$L_{\text{tot}}^{\nu} = \sum_{\text{zone}} \sum_{\text{angle}} L_{\nu}^{\text{angle,zone}} e^{-\tau_{\text{angle,zone}}},$$

where $\tau_{\text{angle,zone}}$ includes both Doppler effects (everything is calculated in the rest frame of the observer) and geometric or limb effects. $L_{\nu}^{\text{angle,zone}}$ is now the emission based on the mass in our angular bin ($m_{\text{zone}}^{\text{angle}}$) pointed in the observer's direction:

$$L_{\nu} = \frac{m_{\text{angle,zone}}}{n_{\text{angular bins}}} \frac{2h\sigma_{\text{abs}}v^3}{c^2} \frac{1}{(e^{v/T_{\text{mat}}}-1)} \frac{dv}{\sqrt{1-(v/c)^2}} (1-v/c)^2,$$

where $n_{\text{angular bins}} = 40$ in our case. As long as our assumption holds concerning the accuracy of the matter temperature obtained from our radiation–hydrodynamics calculation, this semianalytic post-process gives us an accurate calculation of
the emission. We then can calculate the emission over our entire energy grid consisting of 14,900 groups from roughly $10^{-3}$ eV–$10^4$ eV (the grid depends upon the temperature and density of the matter). For typical SN temperatures and densities, we generally have $\sim$13,000 groups lying between 1000 and 10000 Å.

To obtain optical and UV light curves over the wavelength range 1600–6000 Å, we need to integrate our spectrum over a band filter. In our case, we use the *Swift* band filters for $U$, $B$, and $V$ (Gehrels et al. 2004; Roming et al. 2005; Poole et al. 2008): swuuu_20041120v104.arf, swubb_20041120v104.arf, and swuvv_20041120v104.arf to be specific. We also include the data for the swuw1_20041120v104.arf, swuw2_20041120v104.arf, and swum2_20041120v104.arf UV bands.

### 3. ACCRETION-INDUCED COLLAPSE

When accretion onto a WD pushes its mass above the Chandrasekhar limit, the star begins to compress. This compression can lead to one of two fates. In one scenario, nuclear burning releases enough energy to completely unbind the star in a thermonuclear explosion, producing the well-known type Ia SN used to probe the early universe. In the other, the WD collapses down to a neutron star (AIC). The gravitational potential energy released in this collapse also produces an explosion. It is this latter, lesser-known, AIC that we study here. An AIC can only form if nuclear burning during the collapse does not inject enough energy to unbind the star. If the core of the WD

![Figure 3](image-url). Opacities for our wind mixture used in our fallback calculations at three different density/temperature pairs relevant to our supernova explosion. Note that the placement of the lines can move dramatically based on the temperature profile. We have also included one plot showing the opacity for a mixture where the hydrogen has been replaced by helium.
is cool enough such that nuclear burning does not occur (or is weak) until after the core has imploded (and lost energy through neutrino emission), nuclear burning will be unable to unbind the star.

Nomoto & Kondo (1991) summarized the fate of an accreting WD based on its composition (carbon–oxygen versus oxygen–magnesium–neon WD), initial mass, and accretion rate. They argued that WDs with initial masses above $1.2 M_\odot$ are likely to form AICs. Unless the accretion rate is quite low ($<10^{-6} M_\odot$ yr$^{-1}$), the mass of these WDs will exceed the Chandrasekhar mass well before accretion energy can heat the core. The fact that many of these massive WDs are OMeNe WDs whose cores are cooled by Urca processes (the emission of a neutrino and anti-neutrino pair within a nucleus) does not help. They also argued that AICs are formed when the accretion rate is high, again causing the WD mass to exceed the Chandrasekhar limit before the core is heated by this accretion. With these two constraints, we can study the rates of AICs.

Note that an AIC has many properties similar to that of electron capture SNe. An electron capture SN is produced in an asymptotic giant branch (AGB) star with a mass placing its evolution at the boundary between mass ejection (forming a WD) and further core nuclear burning producing an iron core and, ultimately, a iron core-collapse SNe (see Wheeler et al. 1998; Wannajo et al. 2003; Poelarends et al. 2008). An electron capture SN is produced in the collapse of the OMeNe core at the center of this AGB star. The details of the explosion for an electron capture SNe are very similar to those of an AIC. The primary difference between these objects is the surrounding environment and, as we shall see, this environment plays a strong role in determining the observations of these objects. In this paper, we focus only on the surrounding environments of AICs.

Metzger et al. (2009) have outlined many of the important features of the observable signatures of AICs. They estimated the differences between “naked” AICs in low-density environments and “enshrouded” AICs from WD–WD mergers. They found that the peak flux for both was roughly constant, but the enshrouded outburst occurred later and was longer in duration.

3.1. Accretion-induced Collapse Rates

A number of methods have been used to constrain AIC rates. Thus far, we have no indisputable observation of the AIC of a WD (although see our summary discussion). The Katzman Automatic Imaging Telescope (KAIT) now has a complete SN sample out to 60 Mpc and down to absolute $R$ magnitudes of $-16$ (A. V. Filippenko 2009, private communication). Could an AIC be hidden in their type Ia sample? We expect the outburst to be dim because shock heating is negligible and the predicted $^{56}$Ni yields are all low, i.e., $<0.05 M_\odot$ (Fryer et al. 1999a; Kitaura et al. 2006; Dessart et al. 2007), but the KAIT sample includes some dim type Ia SNe. If none of these SNe are AICs, the AIC rate is limited to a few percent the type Ia rate. Detailed comparisons to these KAIT results could well place firm limits on the AIC rate.

Theoretical estimates of the rate of AICs are also quite uncertain. A number of progenitor scenarios have been proposed, mostly in the search for the elusive progenitor to type Ia SNe (see Livio 2001 for a review). Although single degenerate models exist, the dominant progenitor of AICs, if we accept the conclusions of Nomoto & Kondo (1991), comes from double degenerate mergers with a rate of $\sim 10^{-3}$ yr$^{-1}$ in a Milky Way sized galaxy. This result depends upon a number of assumptions about the accretion evolution in these binary systems and the true rate of AICs could be many orders of magnitude lower than this value. Studies of binary mass transfer (Yoon et al. 2007; Livio 2001, and references therein) and WD accretion (Fisker et al. 2006) are both becoming more accurate. As they are coupled with stellar evolution models of these systems, this rate estimate for AICs should become more accurate.

Alternatively, one can use observed features of AIC explosions to constrain the AIC rate. By comparing observations of nucleosynthetic yields to explosion models, Fryer et al. (1999a) argued that the neutron rich ejecta from an AIC limits their rate to $\sim 10^{-4}$ yr$^{-1}$. More recent results, which eject a smaller fraction of neutron-rich material, may loosen this constraint by 1 order of magnitude (Kitaura et al. 2006; Dessart et al. 2007), allowing rates as high as $\sim 10^{-3}$ yr$^{-1}$.

3.2. AIC Light Curves and Spectra

Recall that light curves and spectra are powered by both shock heating as the ejecta hits its surrounding medium and through the decay of radioactive elements. The standard explosion model of Fryer et al. (1999a) predicted $<0.05 M_\odot$ of $^{56}$Ni ejecta. Other explosion models predict even less mass in $^{56}$Ni. In this case, shock heating will play an equal, if not dominant, role in the light curve.

For our calculations, we use an explosion from Fryer et al. (1999a). The total explosion energy for our canonical AIC is $2 \times 10^{51}$ erg. With the low ejecta mass ($0.2 M_\odot$), this energy corresponds to a high average initial velocity of the ejecta ($3 \times 10^8$ cm s$^{-1}$). The composition is also based on the explosion models of Fryer et al. (1999a), with roughly $20\%$ of the ejecta in the form of $^{56}$Ni ($0.04 M_\odot$). We construct a second explosion with $1/10$th the amount of mass (hence $1/10$th the explosion energy and $1/10$th the $^{56}$Ni yield) to compare to the lower ejecta models predicted by more recent calculations (Dessart et al. 2007). A summary of the explosion energy, ejecta mass, and $^{56}$Ni mass is shown in Table 1. On top of these explosions, we construct a surrounding environment with a density structure (Figure 5) based on preliminary binary merger calculations by P. M. Motl et al. (2010, in preparation).

Due to the low envelope mass, the ejecta begin to emit within the first day of the explosion (Figure 6). At this time, the ejecta is still hot, ionizing the material above it, leading to very few lines. Even when we place a CO atmosphere on top of the WD,
Density distribution (density vs. radius) for our AIC calculations.

Table 1

| Name  | Total Energy $(10^{51} \text{ erg})$ | Nickel Yield $(M_{\odot})$ | Total Mass $(M_{\odot})$ | Peak V (mag) |
|-------|-------------------------------------|---------------------------|--------------------------|-------------|
| AIC   | 2.0 (0.2$^a$)                      | 0.041 (0.0041)            | 0.1925 (0.01925)         | $-18.5 (-16)$ |
| Type Ia | 0.7 (0.07$^b$)                    | 0.014                     | 0.10                     | $-16$ to $-19$ |
| Fallback | 1.7                               | $10^{-13}$                | 3.0                      | $-13$ to $-15$ |

Notes.

$^a$ For our AIC models, we have high and low ejecta models.

$^b$ For our Ia models, we have run 1 low energy model.

at early times there are very few lines due to the high peak temperature. As the ejecta expands, it cools and line features appear. But there are no strong identifying (specific to AICs) features in the spectra.

The light curves in $V$ and $B$ bands peak at roughly 15 days with peak absolute magnitudes of $-18.5$ to $-19$ mag (close to that of SNe) for our standard model (Figure 7). The drop is fairly rapid, and by 30 days, the absolute magnitude for both these models is $-15$.

(A color version of this figure is available in the online journal.)
bands is below $-$17. The peak in the $U$ and Swift UV bands is bright (as we might expect from the high effective temperatures of the spectra).

For our lower yield model, the combined lower energy and lower mass of $^{56}$Ni ejected lowers the AIC emission. The peak absolute $V$ and $B$ magnitudes of our low-density run do not exceed $-$16 and by 40 d are below $-$14. At early times, there are a number of lines in the UV, but by 20 days, the low density and high temperature of this model ionizes most of the material and the spectra are fairly featureless.

4. FALLOUT SUPERNOVAE

Standard core-collapse SNe are the explosions produced when the iron cores of stars more massive than 8–10 $M_\odot$ collapse to form neutron stars. The potential energy released in this collapse drives an explosion. But not all stellar collapses form strong SN explosions. The explosion launched in the stellar core moves out through the star and decelerates as it pushes out the rest of the star. For some of the initial exploding material, this deceleration drops the explosion energy below the escape energy from the core. This material ultimately falls back onto the neutron star.

Fryer (1999) argued that although this “fallback” is only a few tenths of a solar mass for 15 $M_\odot$ stars, it might be several solar masses for 25 $M_\odot$ stars. Based on their understanding of fallback, Fryer & Kalogera (2001) argued for a range of neutron star and black hole masses. The success of the current SN mechanism is its prediction of fallback and a broad range of remnant masses. Fryer & Kalogera (2001) found that, within the uncertainties, the formation rate of black holes in SN explosions was somewhere between 10% and 40% that of the total supernova rate. The largest uncertainty in this estimate is the initial mass function. Winds can allow the formation of neutron stars by more massive, solar metallicity stars (above $\sim 60$ $M_\odot$), but this does not affect the rate significantly.

4.1. Fallback Rates

In current simulations, the energy produced in the convective engine decreases for stars more massive than 20 $M_\odot$, while the binding energy of the star increases dramatically at roughly this same mass point. Including large errors in the explosion energies, Fryer & Kalogera (2001) were able to pinpoint the transition mass from neutron star and black hole formation to stars with initial masses within the 18–23 $M_\odot$ range. Fryer & Kalogera (2001) found that, within the uncertainties, the formation rate of black holes in SN explosions was somewhere between 10% and 40% that of the total supernova rate. The largest uncertainty in this estimate is the initial mass function. Winds can allow the formation of neutron stars by more massive, solar metallicity stars (above $\sim 60$ $M_\odot$), but this does not affect the rate significantly.

4.2. Fallback Spectra and Light Curves

For our calculations, we use a 40 $M_\odot$ binary progenitor for Cas A (Fragos et al. 2009). In this star, we drive a $2 \times 10^{51}$ erg explosion. The binding energy of this star is much greater than $2 \times 10^{51}$ erg and the final remnant mass after fallback is 4.5 $M_\odot$. With this much fallback, very little $^{56}$Ni is ejected: <2 $\times 10^{-13}$ $M_\odot$. A summary of the explosion energy, ejecta mass, and $^{56}$Ni mass is shown in Table 1. On top of this explosion, we construct two surrounding environments with density structures (Figure 8): one based on binary mass ejection (100 km s$^{-1}$ velocity, $M = 1 M_\odot$ yr$^{-1}$) and one with a
small atmosphere <$0.00054 M_\odot$) topped by a wind profile (1000 km s$^{-1}$ velocity, $M = 10^{-5} M_\odot$ yr$^{-1}$).

The large mass in the binary mass ejection case, coupled to the weak explosion energy, delays shock breakout until after the ejecta loses much of its energy (Figures 9 and 10). In this simulation, the explosion has yet to peak, even 100 days after the explosion. But it will peak at very low $V, B$ magnitudes (below absolute magnitudes of $-13$). This is an extreme case, where the environment is very dense out to $10^{16}$ cm due to a binary mass ejection just prior to collapse.

More likely, the mass ejection phase is followed by a Wolf–Rayet wind phase. Even with this lower-density surrounding medium, the low ejecta velocity coupled to its low $^{56}$Ni ejecta produces a very weak explosion with peak $V, B$ absolute magnitudes of $-15$ (Figures 9 and 10). The lower density means the peak emission occurs quickly ($\sim 10$ days) and the $V$-band absolute magnitude drops below $-12$ at about 45 days.

To test our single group approximation, we modeled a five-group transport calculation for our diffuse case (Figure 9). Although many of the lines are similar, the spectral fluxes can be very different. Although the peak in the light curve does not change dramatically in the $V$-band, the $UV$ light curve is very different. Ultimately, many group calculations will be required to model detailed spectral light curves.

To test our resolution, we completed 1 run with twice the coarse-bin resolution and 10 times the effective (adaptive mesh refinement, AMR) spatial resolution (Figure 9). The spectra from this simulation are nearly identical to our standard runs. Detailed spectra might also help to give us a better understanding of the surrounding medium. Figure 11 shows the optical/IR spectra for our two fallback models for the same snapshots in time of Figure 9. Note that we assume our atomic levels are in local thermodynamic equilibrium with the radiation front. Especially, for material ahead of our shock front (which is not in thermodynamic equilibrium), we overestimate the level of ionization, producing fewer lines than what may be observed. Within the shocked material, local thermodynamic equilibrium is a better assumption, and our broad lines representing this shocked ejecta are fairly accurate and provide an ideal probe of the explosion itself.

5. IA SUPERNOVAE

Bildsten et al. (2007) have argued that faint SN-like outbursts can occur in helium flashes of accreting material in AM Canum Venaticorum (AM CVn) binaries. In these binary systems, a C/O WD is accreting from its smaller He WD companion, slowly whittling away the mass of the He WD. At high accretion rates, the helium accretes onto the C/O WD and burns stably. Such systems can produce short-period supersoft x-ray sources (Shen & Bildsten 2007). The system evolves, widening the orbit, and causing the accretion rate to decrease. At sufficiently low accretion rates ($M < 2 \times 10^{-6} M_\odot$ yr$^{-1}$), the burning can be unstable. The accreting WD can go through a series of flashes, each increasing the entropy of the system, leading to larger ignition masses. Typically, the last “flash” will result in the largest explosion and it is this explosion that Bildsten et al. (2007) focus on as a potential transient observation.

5.1. Ia Supernova Rates

Using the local Galactic density of AM CVn’s and assuming every AM CVn gives one explosive last flash, Bildsten et al. (2007) argued that the Ia SNe should occur at a rate of $6.67 \times 10^{-3} - 0.0002$ per year in an E/SO galaxy.

5.2. Ia Supernova Spectra and Light Curves

For our calculations, we use a FLASH (Fryxell et al. 2000) simulation of a Type Ia outburst. This model produced a $7 \times 10^{50}$ erg explosion with $0.1 M_\odot$ of ejecta. This is our fastest explosion, with mean velocities around 25,000 km s$^{-1}$. The total amount of $^{56}$Ni ejected is $0.014 M_\odot$. This fast ejecta velocity is due, in part, to a mismatch in the binding energy, still a large effect at the end of our FLASH calculations. We simulate an additional run reducing this energy by a factor of 10 ($7 \times 10^{49}$ erg, 8000 km s$^{-1}$) to determine its effect on our light curve calculations.

On top of this explosion, we construct two surrounding environments with density structures (Figure 12) based on binary accretion simulations (P. M. Molt et al. 2010, in preparation): one using the density profile along the binary orbital plane (higher density) and one using the profile along the orbital axis (lower density).

The emission from a Ia SN is strongly dependent on the density profile. First, there is very little radioactive ejecta, so it does not contribute strongly to the light curve. But with the fast ejecta velocities and low masses, the gamma rays from radioactive decay begin to stream out early, also limiting how much the gamma rays can contribute to the light curve. Recall that we deposit our energy in situ and hence we are overestimating the emission from this low-density case. The presence of fast moving ejecta means that shocks are important for the light curve (Figure 13). For our dense environment, the $V$ and $B$ bands peak between absolute magnitudes of $-18$ to $-19$ (near to normal SN brightnesses). The light curve will remain bright for nearly 100 days. The high shock velocities and low densities lead to high temperatures and spectra peaked in the $UV$ and X-ray at early times (Figure 14). In the dense model, there is a decided drop in the $UV$ band emission after 20 days. This occurs when the radiation leading the shock emerges from...
Figure 9. Spectra from our extremely dense and dense surrounding medium models of supernova fallback. In the more dense case, the outburst is still peaking 100 days after the launch of the explosion and strong emission/absorption lines are evident. The lines, dominated by material ahead of the ejecta, are narrow. In the lower density case, the peak occurs much sooner and lines are part of the ejected material and hence are broader. The bottom, left plot shows the lower density case using five groups for the radiation transport. The additional groups lead to a slightly different temperature profile that can change the spectra dramatically. But the peak fluxes are not altered significantly. The bottom right plot shows the results using twice the coarse-bin resolution and 10 times the fine (AMR) resolution. The spectra are nearly identical to their comparable low resolution spectra (dense surrounding medium).

(A color version of this figure is available in the online journal.)

ejecta and the radiation front leading the ejected shock cools. From this point on, the photosphere of the explosion resides near the density peak in the ejecta. Shock emergence is discussed in more detail by L. H. Frey et al. (2009, in preparation).

But if the surrounding environment is diffuse, there is too little material to create strong emission, and the peak emission is limited to that of the initial explosion, peaking with absolute magnitudes around $-16$ and dropping below $-14$ before 20 days (below $-12$ by 30 days).

The high temperatures and low densities limit the number of lines in the emitting regions and the regions just above these emitting regions. Aside from absorption lines caused by the surrounding medium, we expect very few line features in their spectra.

6. NEUTRINOS AND GRAVITATIONAL WAVES FROM “FAILED SUPERNOVAE”

AICs. The collapse and bounce of an AIC is very similar to that of a normal SN (see Fryer & New 2003 for a review). As such, both the neutrinos and GW emission should be similar to that of core collapse. The primary difference is that the explosion is likely to happen quickly and there is unlikely to be much, if any, material falling back onto the newly formed neutron star. For
neutrinos, this means that the explosion is clean, allowing a clear view of a cooling neutron star. For gravitational waves, there will be no strong signal from convective instabilities above the proto-neutron star. But there is a possibility that AICs will have high angular momenta at collapse. As such, the AIC scenario is a leading candidate among stellar collapse to form bar-mode (and related) instabilities.

**Fallback.** The collapse and bounce phases of stellar collapse with considerable fallback are weaker explosions. In general, these explosions have longer delays between bounce and explosion. As such, the convective timescale is longer, producing a longer boiling phase prior to explosion. After the explosion, fallback accretion adds mass to the proto-neutron star, possibly causing it to collapse to form a black hole. These engines produce neutrino light curves that are much broader than normal SNe. The total emission will be more than a factor of 2 higher than normal SNe, primarily in an extended convective phase.
(during the first second) and a higher neutrino flux in the first 10 s from fallback (Fryer 2009). Observations of this extended emission will constrain our understanding of the SN explosion mechanism and the nature of fallback.

The extended convective phase may also develop low-mode instabilities, leading to stronger GW emission, especially through asymmetric neutrino emission (Kotake et al. 2009). If the proto-neutron star collapses to form a black hole, black hole ringing, and related instabilities may occur, producing another source of GWs (see Fryer & New 2003).

**Type Ia.** Ia SNe will not be strong sources of neutrinos or GWs.

### 7. SUMMARY

In this paper, we reviewed three separate explosions, providing the first radiation-hydrodynamics calculations of their emission (both spectra and light curves). Each of these explosion scenarios will ultimately require detailed, individual studies as upcoming surveys begin to make first observations. Here, we have described many of the basic features one should expect in these explosions, focusing on the physics that alters the emission. In all cases, the surrounding environment affected both the duration and peak of the emission.

For SNe, the emission is powered by a combination of the energy from the decay of radioactive elements (primarily $^{56}$Ni and its daughter products) and shock heating as the ejecta moves through its surroundings. For all of these “failed SNe,” the low $^{56}$Ni yield coupled to the high explosion velocities lead to peak emission dominated by the shock heating. The energy from shock heating depends both on the velocity of the ejecta and the density structure of the surrounding medium. For a given explosion, its surrounding medium (strength of the stellar wind, ejecta from a binary mass transfer phase, etc.) determines the peak luminosity and also shapes the spectra. The strong dependence of the surroundings makes it difficult to differentiate the explosion mechanism based on light-curve observations alone. Unfortunately, neither the wind mass-loss nor the ejecta from binary mass transfer are well known theoretically. Observations of these transients will first and foremost help us in constraining the nature of these mass ejection mechanisms.

Depending upon the environment, the AIC outburst could reach peak magnitudes that are nearly as bright as normal SNe, if only for a brief time (absolute magnitude in the $V$ band of $-18.5$, but dropping to below $-17$ by 30 days). If the total mass ejecta is at the lower limit predicted by simulations, the peak brightness will be several magnitudes dimmer than typical SNe ($V$-band absolute magnitude of $-16$). The rate of AICs could well be as high as the type Ia SN rate, but it could be several orders of magnitude lower. If the rate is high, we should have (and as we discuss below, may have) observed some of these outbursts in existing samples. The progenitors of AICs are intimately linked to the progenitors of type Ia SNe, and understanding the AIC progenitor will teach us about this SN progenitor. A nearby detection of an AIC will also provide insight into neutron star formation. Without the convective engine and possibility of fallback, the neutrino signal from AICs is a pristine measurement of stellar collapse and bounce. We can use the neutrino signal to study nuclear physics and the formation of the neutron star. In addition, because of the potential for rapid spinning prior to collapse, AICs are the most promising candidates for bar mode, and related, instabilities in the proto-neutron star, a strong source of GW emission. The observation, or lack thereof, of a GW signal can be used both to understand the WD accretion process and the nature of these proto-neutron star instabilities.

Type Ia SNe eject even less $^{56}$Ni (and less total mass) than our AIC model. Shock heating will dominate this explosion’s emission, and hence the emission from these explosions depends even more strongly on the surrounding medium. The peak $V$-band absolute magnitudes ranged from $-18.5$ (holding above $-18$ for nearly 100 days for dense surroundings) to $-14$ (dropping below $-12$ in 25 days). Clearly, if the former were true, these should have been observed in our current transient surveys and it is likely that the answer lies somewhere in between these two extremes. Observations of type Ia SNe will place constraints on binary mass transfer processes, ultimately improving our understanding of this process. This, in turn, will teach us about the progenitor scenarios for type Ia SN.

Fallback in SNe, preferentially occurring in weaker explosions, can drastically decrease the $^{56}$Ni yield. We have studied an extreme case where fallback ultimately causes the core to collapse to form a black hole. With its low $^{56}$Ni yield and low ejecta velocities, it is the dimmest of all our models. For the object studied in this paper that produced a $4.5 M_\odot$ black hole, the brightest explosion (with a Wolf–Rayet wind medium) peaks at $V$-band absolute magnitudes of $-15$, dropping below $-12$ after 40 days. Such systems would be very difficult to observe, but they are likely to be the most common in the formation of stellar-massed black holes. Their neutrino signals would have delayed emission arising from a long convective stage and fallback as material accretes onto the proto-black hole. These systems would also exhibit oscillations in the general relativity metric and are prime sites to observe GWs from black hole ringing.

We now have observations of several potential “failed” SN outbursts. The strong dependence on the surroundings (and relatively poorly understood explosion mechanism) makes it difficult to rule out any particular engine. Nevertheless, we can already use our models to infer “likely” engines for these observations. We review a few cases here.
SN 1987A is an example of a fallback SN, but whether the compact remnant is a neutron star or black hole remains a matter of debate. Scientists expect that accretion onto either a neutron or black hole compact remnant should produce some emission arising from this compact remnant. Deep images of the SN now place strong upper limits on this emission, forcing Graves et al. (2005) to conclude that either this remnant is heavily obscured by dust or that an early photon-driven wind off of a neutron star remnant has blown off any late-time accreting material (Fryer et al. 1999b). If the fallback was sufficiently high to produce a black hole, the relatively high $^{56}$Ni yield of this SN requires large asymmetries to mix this $^{56}$Ni out from the core into material that is ejected in the explosion (Hungerford et al. 2005). As we discussed in Section 4, fallback SN can produce a range of emission. SN 1987A is clearly closer to a normal SN than it is to the extreme low-$^{56}$Ni yield outbursts studied here.

SN 2008ha is an example of a possible “failed” SN (Perets et al. 2009, Valenti et al. 2009, Kawabata et al. 2009). Its low peak absolute magnitude and low nickel are indicative of many of our transients. Perets et al. (2009) placed this SN in a class
Figure 14. Spectra from our Ia models. This fast shock in this models ionizes most of the material, producing line-free spectra. This strong shock also produces spectra that peak in the X-ray.

Valenti et al. (2009) and Kawabata et al. (2009) argue instead that 2008ha is an example of a SN with considerable fallback. Because SN 2008ha is a well-studied SN, we can use our models to help settle this debate. Foley et al. (2009) present data over a wide range of wavelengths, from infrared to ultraviolet. One of the primary constraints on our AIC models is that the ultraviolet emission tends to be higher (lower absolute magnitudes) than the V and B bands. The Swift observations of this outburst had swuw1, swuw2, and swum2 filter bands dimmer than the V and B bands. These observations argue against SN2008ha being an AIC. To a lesser extent, our type Ia models also argue for brighter emission in the UV (especially at early times) than in the V and B bands. Of our simulations, only the fallback model fits this observed trend in the ultraviolet emission. Based on this constraint, our data suggest that a fallback model best-fits 2008ha. Valenti et al. (2009) and Kawabata et al. (2009) also argue for a fallback model, requiring a slightly lower-mass progenitor with more ejecta (and extensive mixing) to eject $^{56}\text{Ni}$ than our fallback simulation used here.

One possible AIC observation is SN 2005cz, a “core-collapse” SN in an elliptical galaxy. Based on the decline rate...
at intermediate and late phases of the outburst, Kawabata et al. (2009) argued that the ejected mass was below 1 $M_\odot$ for explosions below $10^{51}$ erg. They also found the nickel yield to be less than 0.02 $M_\odot$. These constraints led them to conclude that this SN arose from the collapse of a $\sim 10 M_\odot$ star.

Given that SN 2005cz occurred in an elliptical galaxy, it is extremely unlikely that such an explosion was produced by a SN with strong fallback. However, with a peak $R$-band magnitude around $-15$ and its low nickel yield, it is possible such systems are fitted by AICs or type Ia SNe. The $R$-band light curve (Figure 15) is roughly fitted by our low-ejecta AIC progenitor or could be fitted by a type Ia SN if we tune the surrounding material. Many of the line features of at 25 days in 2005cz are present in our spectra (Figure 11), but accurate yields of AIC are necessary to compare these spectra in detail.

Another example of a possible AIC/type Ia is SN 2005E. This supernova occurred 11.3 kpc above the disk of S0/Sa galaxy, leading Perets et al. (2009) to argue that it arose from an old stellar population. If true, both an AIC or type Ia outbursts are likely progenitors for this explosion. Like 2005cz, we can tune the surrounding environment from the binary system to match the existing light curves.

Perets et al. (2009) provide a growing list of Ca-rich SNe in relatively old stellar populations that are potential type Ia or AIC SNe. Given the uncertainties in the surroundings of these objects and the details of their yields, we can probably fit many of these objects with our transients. As with SN 2008ha, we can use ultraviolet observations to constrain these observations. The difficulty will be distinguishing these SNe from explosions of 8–12 $M_\odot$ stars (which should be more common than either AICs or type Ia SNe). One ultimately definitive constraint will be placed on the age of the star formation for these systems: an 8 $M_\odot$ star has a $\sim 50$ Myr lifetime; AICs and type Ia SNe can arise from much older systems.

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REFERENCES

Baltrusaitis, R., Gittings, M., Weaver, R., Benjamin, R., & Budzinski, J. 1996, Phys. Fluids, 8, 2471
Bildsten, L., Shen, K. J., Weinberg, N. N., & Nilemans, G. 2007, ApJ, 662, L95
Carlson, R. G. 1955, Solutions of the Transport Equation by S_5 Approximations, LA-1891 (Los Alamos, NM: Los Alamos National Laboratory)
Chandrasekhar, S. 1950, Radiative Transfer (Oxford: Clarendon)
Coker, R. F., et al. 2007, Ap&SS, 307, 57
Deng, J., Tominaga, N., Mazzali, P. A., & Maeda, K. 2005, ApJ, 624, 898
Desart, L., Burrows, A., Livne, E., & Ott, C. D. 2007, ApJ, 669, 585
Fisker, J. L., Balsara, D. S., & Burger, T. 2006, New Astron. Rev., 50, 509
Foley, R. J., et al. 2009, AJ, 138, 376
Fragos, T., Willems, B., Kalogera, V., Ivanova, N., Rockefeller, G., Fryer, C. L., & Young, P. A. 2009, ApJ, 697, 1057
Fryer, C. L. 1999, ApJ, 522, 413
Fryer, C. L. 2009, ApJ, 699, 409
Fryer, C. L., Benz, W., Herant, M., & Colgate, S. A. 1999a, ApJ, 516, 892
Fryer, C. L., Colgate, S. A., & Pinto, P. 1999b, ApJ, 511, 885
Fryer, C. L., Hungerford, A. L., & Rockefeller, G. 2007a, Int. J. Mod. Phys. D, 16, 941
Fryer, C. L., Hungerford, A. L., & Young, P. A. 2007b, ApJ, 662, L55
Fryer, C. L., & Kalogera, V. 2001, ApJ, 554, 548
Fryer, C. L., & New, K. C. B. 2003, Living Rev. Rel., 6, 2
Fryer, C. L., Rockefeller, G., & Young, P. A. 2006a, ApJ, 647, 1269
Fryer, C. L., Young, P. A., & Hungerford, A. L. 2006b, ApJ, 650, 1028
Fryxell, B., et al. 2000, ApJS, 131, 273
Gehrels, N., et al. 2004, ApJ, 611, 1005
Gittings, M., et al. 2008, Comput. Sci. Discovery, 1, 015005
Graves, G. J. M., et al. 2005, ApJ, 629, 944
Herwig, F., Freytag, B., Hückstaedt, R. M., & Timmes, F. X. 2006, ApJ, 642, 1057
Holmes, R., et al. 1999, J. Fluid Mech., 389, 255
Hückstaedt, R., et al. 2005, Ap&SS, 298, 255
Hungerford, A. L., Fryer, C. L., & Rockefeller, G. 2005, ApJ, 635, 487
Kawabata, K. S., Maeda, K., Nomoto, K., Taubenberger, S., Tanaka, M., Hattori, T., & Itagaki, K. 2009, Nature, submitted (arXiv:0906.2811)
Kitaura, F. S., Janka, H.-Th., & Hillebrandt, W. 2006, A&A, 450, 345
Kotake, K., Ikawami, W., Ohnishi, N., & Yamada, S. 2009, ApJ, 697, L133
Levermore, C. D., & Pomraning, G. C. 1981, ApJ, 248, 321
Little, R. C. 1996, MENDF6: A 30-Group Neutron Cross-Section Library Based on ENDF/B-VI (Los Alamos National Laboratory memorandum XTM:96-82, 1996 February 28; Los Alamos, NM: Los Alamos National Laboratory)
Livio, M. 2001, in Space Telescope Science Institute Symp Series, Vol. 13, Supernovae and Gamma-ray Bursts: The Greatest Explosions Since the Big Bang, ed. M. Livio, N. Panagia, & K. Sahu (Cambridge: Cambridge Univ. Press), 334
Lowrie, R. B., & Rauenzahn, R. M. 2006, LANL Technical Report, LA-UR-06-3853 (Los Alamos, NM: Los Alamos National Laboratory)
Magee, N. H., et al. 1995, in ASP Conf. Proc. 78, Astrophysical Applications of Powerful New Databases, ed. S. J. Adelman & W. L. Wiese (New York: ASP), 51
Mazzali, P. A., et al. 2006, ApJ, 645, 1323
Meszaros, P., & Rees, M. J. 1992, MNRAS, 258, 41
Metzger, B. D., Piro, A. L., & Thompson, T. A. 2009, arXiv:0907.1127
Nomoto, K., & Kondo, Y. 1991, ApJ, 367, L19
Perets, H. B., et al. 2009, arXiv:0906.2003
Poelarends, A. J. T., Herwig, F., Langer, N., & Heger, A. 2008, ApJ, 675, 614
Poole, T. S., et al. 2008, MNRAS, 383, 627
Roming, et al. 2005, Space Sci. Rev., 120, 95
Shen, K., & Bildsten, L. 2007, ApJ, 699, 1365
Valenti, S., et al. 2009, Nature, 459, 674
Wanajo, S., Tamamura, M., Itoh, N., Nomoto, K., Ishimaru, Y., Beers, T. C., & Nozawa, S. 2003, ApJ, 593, 968
Wheeler, J. C., Cowan, J. J., & Hillebrandt, W. 1998, ApJ, 493, L101
Wick, G. C. 1943, Z. Phys., 121, 702
Yoon, S.-C., Podsiadlowski, P., & Rosswog, S. 2007, MNRAS, 380, 933

Figure 15. $R$-band absolute magnitudes for many of our models. Within a given model, we can produce a wide range of peak brightnesses and duration in the $R$-band magnitudes. $R$ band alone is not enough to constrain the models. (A color version of this figure is available in the online journal.)