Interplay between multiple charge-density waves and the relationship with superconductivity in Pd$_x$HoTe$_3$

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HoTe$_3$, a member of the rare-earth tritelluride (RTe$_3$) family, and its Pd-intercalated compounds, Pd$_x$HoTe$_3$, where superconductivity (SC) sets in as the charge-density wave (CDW) transition is suppressed by the intercalation of a small amount of Pd, are investigated using angle-resolved photoemission spectroscopy (ARPES) and electrical resistivity. Two incommensurate CDWs with perpendicular nesting vectors are observed in HoTe$_3$ at low temperatures. With a slight Pd intercalation ($x = 0.01$), the large CDW gap decreases and the small one increases. The momentum dependence of the gaps along the inner Fermi surface (FS) evolves from orthorhombicity to near tetragonality, manifesting the competition between two CDW orders. At $x = 0.02$, both CDW gaps decrease with the emergence of SC. Further increasing the content of Pd for $x = 0.04$ will completely suppress the CDW instabilities and give rise to the maximal SC order. The evolution of the electronic structures and electron-phonon couplings (EPCs) of the multiple CDWs upon Pd intercalation are carefully scrutinized. We discuss the interplay between multiple CDW orders, and the competition between CDW and SC in detail.

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The recent observation of charge ordering in cuprate high-temperature superconductors has reignited interests in CDW and its interplay with SC. A new charge ordering is always introduced by different types of instabilities, such as lattice distortion or FS nesting. However, the driving force behind the CDW phase is still under debate. From a Peierls perspective, in an ideal one-dimensional (1D) system, the electronic susceptibility would develop a logarithmic divergence singularity at some sheets of the FSs spanning by nesting vectors via EPCs, and hence results in a phase transition to a collective order. Incommensurate periodic lattice distortions and the opening of energy gaps at $E_F$ provide an unprecedented opportunity to systematically investigate the CDW formation and its relationship with FS nesting under pretty accurate theoretical models. An incommensurate CDW modulation characterized by a wave vector $q_1 \approx 2/7c^*$ was commonly observed. Recently, a second CDW transition occurs at lower temperatures with $q_2 \approx 1/3a^*$ perpendicular to the first was discovered in heavier members of RTe$_3$. Additionally, by the Pd intercalation, the suppression of CDWs and even the emergence of SC were observed. Thus, this system offers the valuable possibility to explore the interplay between multiple CDW instabilities, and also between the CDW and SC orders. However, to date, little is known about the relationship of these orders belong to different collective phases. In order to obtain a much more comprehensive insight into the multiple CDWs formation and the interplay between various correlated electronic states, we performed high-resolution ARPES experiments on series of Pd$_x$HoTe$_3$ single crystals with the help of electrical transport measurements, focusing on the evolution of electronic structures and EPCs upon Pd intercalation. We provide the first systematic electronic structure study on the interplay between multiple CDWs, and their relationship with SC in RTe$_3$ family as a function of chemical intercalation.

Pd$_x$HoTe$_3$ single crystals with various nominal intercalated compositions ($x = 0, 0.01, 0.02, \text{and} 0.04$) are used in our study. In this paper, two incommensurate CDWs are identified. We observe the coexistence of two CDW gaps created by perpendicular nesting vectors in HoTe$_3$ at low temperature. The momentum dependence of the gaps along the inner FS reveals orthorhombicity. A slight
Pd intercalation ($x = 0.01$) leads to remarkably different trends of these gaps, the gap symmetry turns out to be near tetragonality, proving the competition between the CDW orders. Both CDWs are further suppressed in $x = 0.02$, leading to the appearance of SC, and they vanish in $x = 0.04$, where the SC order reaches the maximum, showing the competition between CDW and SC. By quantitatively inspecting the evolution of electronic structures and EPCs, we demonstrate the nesting nature of multiple CDWs, suggest the significant increment of the second CDW gap from $x = 0$ to 0.01 determined by the EPC strength. The competition between these two CDWs, and their relationship with SC is very likely to be a FS competition scenario.

High-quality single crystals of Pd$_x$HoTe$_3$ were synthesized by the flux method. ARPES measurements were performed at Renmin University of China and Institute of Physics, Chinese Academy of Sciences, with a He-discharge lamp, at the 1-cubed ARPES end station at BESSY and PGM beam line of the Synchrotron Radiation Center (Stoughton, WI). Spectra were recorded with 55 eV photons, taken at $T = 30$ K, with a pressure better than $4 \times 10^{-11}$ Torr. Electrical transport measurements were performed in a PPMS-14 (Quantum Design).

As presented in Fig. 1(a), the monotonic increase of lattice constant $b$ along with the increasing Pd content demonstrates the successful intercalation of Pd into the weakly bonded double Te layers. Figs. 1(b)-1(e) show the temperature dependence of electrical resistivity for Pd$_x$HoTe$_3$. Consistent with previous work, two bumps can be seen at $\sim 290$ and $\sim 100$ K in HoTe$_3$, suggesting two well-separated CDW transitions. The second CDW transition at $\sim 100$ K is barely visible in the resistivity, this was interpreted as a renormalization of the electron dispersion in the ungapped FS parts, which may partially compensate the opening of the CDW gap on some FS sheets. With the increasing amounts of Pd ($x$...
FIG. 3. (Color online) (a)-(c) FSs for \( x = 0.01, 0.02, \) and 0.04, respectively, obtained by integrating the spectra within \( \pm 15 \) meV with respect to \( E_F \). The superimposed TB bands are calculated with the hopping parameters equally to that of HoTe\(_3\) and fine adjustment of \( E_F \) values. (d),(e) ARPES intensity plots of \( x = 0.01 \) along cuts \#a and \#b, respectively, indicated by green arrows in (a). Red dashes are guides to the eye for the shadow bands. (f),(g) EDCs measured at various \( k_F \) points of the inner FS along \#1−\#2−\#3, where \#1, \#2, and \#3 are indicated by red circles in (a),(b), respectively. The spectra at these three \( k_F \) points are highlighted by black curves. Black dashes are extracted peak positions, serving as guides to the eye. (h),(i) Momentum distribution curve (MDC) plots of \( x = 0.04 \) along cuts \#c and \#d, respectively, indicated by green lines in (c).

For \( x = 0.01 \), these two CDWs exhibit opposite trends, two bumps merge at \( \sim 220 \) K. More clearly observed in the insets of Figs. 1(d) and 1(e), the SC emerges in \( x = 0.02 \) around 2.0 K with further suppressed CDW orders, and reaches the maximum (\( \sim 2.8 \) K) in \( x = 0.04 \) accompanied by the vanished CDW instabilities, respectively.

We present in Fig. 2 the electronic structure of HoTe\(_3\). The FS in Fig. 2(a) is well described by a 2D tight-binding (TB) model including only the in-plane \( p_x \) and \( p_z \) orbitals of a Te plane, except at the crossings between them, owing to their interactions are neglected in our calculation. The dispersions for \( p_x \) and \( p_z \) can be readily derived as,

\[
E_{p_x}(k) = -2t_{\parallel} \cos \left( \frac{k_x + k_z}{2} \right) + 2t_{\perp} \cos \left( k_x - k_z \right) \frac{a}{2} - E_F,
\]

\[
E_{p_z}(k) = 2t_{\perp} \cos \left( k_x + k_z \frac{a}{2} \right) - 2t_{\parallel} \cos \left( k_x - k_z \right) \frac{a}{2} - E_F.
\]

Details of the TB model are described elsewhere. The residual spectral distribution along the inner pocket, which is similar to that in ErTe\(_3\), indicates the existence of multiple CDWs characterized by different nesting vectors.

We choose two sets of cuts (\#a,\#b and \#c,\#d) to elucidate the different appearance of multiple CDW gaps, and present the corresponding energy distribution curves (EDCs) in Figs. 2(c)−2(f). Both cuts \#a and \#b show a back-bending band feature, this is reminiscent of the dispersion of Bogoliubov quasiparticles, suggesting the opening of a CDW gap. Instead, cuts \#c and \#d reveal both two quasiparticle branches, demonstrating the center of the CDW gap is pushed below \( E_F \) due to the longer than perfect nesting vector observed. As illustrated in Figs. 2(f) and 2(g) for Pd\(_x\)HoTe\(_3\), the definition of CDW gap is dependent on both the nesting conditions and EPC strength. For an ideal nesting, the CDW gap center locates at \( E_F \), thus only the lower branches are visible; for an imperfect nesting with \( q_n > q_{CDW} \), the gap center is pushed below \( E_F \), moreover, if the coupling parameter \( V \) between these two nested states including EPCs is
smaller than the binding energy of gap center, both two quasiparticle branches can be observed.8,18,28 Reasonably, the CDW gap definitions can be classified as, the gap between the lower branch and $E_F$ is used for the situations with only lower branches visible, and the gap between these two branches is for the latter case, yielding $2\Delta$. More details are discussed quantitatively below.

This apparent distinction indicates a second CDW gap different from that in cuts #a and #b. Detailed inspection on the binding energies of the branches at $k_F$ reveals the decreasing trend from #a ($\sim$0.275 eV) to #b ($\sim$0.255 eV), and the same trend holds from #c ($\sim$0.121 eV) to #d ($\sim$0.103 eV), manifesting the shortened nesting vectors. To precisely determine the gap size and their momentum dependence, the EDCs at various momenta are precisely measured. To precisely determine the gap size and their momentum dependence, the EDCs at various $E_F$ ($\sim$0.103 eV) to #d ($\sim$0.103 eV), manifesting the shortened nesting vectors. To precisely determine the gap size and their momentum dependence, the EDCs at various momenta are precisely measured. To precisely determine the gap size and their momentum dependence, the EDCs at various momenta are precisely measured. To precisely determine the gap size and their momentum dependence, the EDCs at various momenta are precisely measured.

To illustrate the characteristic of multiple CDWs and fully understand the interplay between them, we elaborate on the electronic structure evolution upon Pd intercalation. Figs. 4(a)-4(c) show the FS mapping data at $x = 0.01, 0.02, 0.04$, respectively. One can see the nearly fourfold symmetric intensity variation in the FSs of $x = 0.01$ and 0.02 rather than the apparent twofold symmetry in HoTe$_3$, manifesting the symmetry of gap-opening connected to a CDW picture. The shadow bands sketched by red dashes in Figs. 4(d) and 4(e), indicated via cuts #a and #b in Fig. 4(a), respectively, also confirm the validity of FS nesting in determining the CDW instabilities in this system.

The detailed gap anisotropy study of $x = 0.01$ and 0.02, like that of HoTe$_3$ in Fig. 2(b), are displayed in Figs. 4(f) and 4(g), respectively, revealing slightly orthorhombic, or nearly tetragonal symmetry, in stark contrast to the orthorhombicity in HoTe$_3$. In the nesting-driven CDW picture, the origin of the intensity variation along the FS can be reasonably interpreted by the momentum dependence of these CDW gaps. We summarize the gap size along the inner FS of $x = 0.01, 0.02$, and 0.04 as a function of the FS angle ($\theta$) in Figs. 4(a), respectively, clearly confirming the anisotropy. It is noted that, as indicated by blue filled pentacles in Fig. 4(a), the definition of the second CDW gap in HoTe$_3$ is different from others’ ascribed to the observation of both upper and lower quasiparticle branches. According to the different gap definitions discussed above, instead of the gap between the lower branch and $E_F$ for others, we use the one between these two branches, characterized by $2\Delta$.8,18,23

We now discuss the nesting properties associated with the multiple gaps and spectral distribution along the FS. By comparing the nesting vectors determined by ARPES and TB model calculations with the x-ray diffraction results, we can reasonably interpret the momentum dependence of the multiple CDW gaps and the gap center of the second CDW in HoTe$_3$ underlying $E_F$. For HoTe$_3$, the two nesting vectors reveal $\mathbf{q}_{a1} = c^* - q_{CDW1} \approx 0.71(3) c^*$ and $\mathbf{q}_{a2} = a^* - q_{CDW2} \approx 0.69(5) a^*$, where the former is in complete agreement with the perfect nesting vector along $c$ axis and the latter is longer than that along $a$ axis, respectively. Thus, the center of the second CDW gap is pushed below $E_F$ even at the corner (#2) of the inner FS, and gradually moves to lower binding energy with the shortened nesting vector. For $x = 0.01$ and 0.02, the ones parallel to $c$ axis are 0.68(8) and 0.67(1) $c^*$, and to $a$ axis are 0.68(4) and 0.67(3) $a^*$, respectively, elucidating the FS topology becomes more isotropic upon Pd intercalation.

The evolution of the maximal gap size of the two CDW orders upon Pd intercalation are summarized in...
FIG. 5. (Color online) (a) FS for $x = 0.01$ around the second 3D (reduced) BZ center obtained by integrating the spectra within $\pm 15$ meV with respect to $E_F$. The calculated TB bands with orbital projection and shadow $p_z$ band are indicated to enable a study of the coupling strength between the states linked by a nesting vector, $\alpha^* - q_{\text{CDW}2}$, shown as magenta arrow. (b) ARPES intensity plot measured at the crossing between $p_z$ and shadow $p_z$ bands along cut #a, indicated by green arrow in (a), and (c) corresponding EDC plot. The definition of $2V$ is emphasized by black curve. Black dashes are extracted peak positions, serving as guides to the eye.

Combining the multiple nesting properties discussed above, it is conspicuous that upon Pd intercalation, the interplay between these two collective phases yields competition, similar to the optical spectroscopy results upon chemical pressure$^{30}$ and to the transport measurements under pressure$^{31,32}$. These can to some extent be explicated by our multiple nesting properties, but not adequate yet. Along with the increasing Pd content, the first CDW gap gradually decreases ascribed to the shortened nesting vector. Simultaneously, the second CDW gap substantially increases for $x = 0.01$, and then decreases monotonically. The appreciable transform of the second CDW gap magnitude from $x = 0$ to 0.01 strongly suggests that, upon Pd intercalation, not only the FS evolution pointing to the nesting picture, but also the variation of EPC strength is needed to be fully included for investigating the interplay between multiple CDW orders quantitatively.

According to the above discussions, one can obtain the coupling strength $(V)$ between the states linked by $\alpha^* - q_{\text{CDW}2}$ in HoTe$_3$ from Fig. 5(b), where $2V = 0.142$ eV. However, as only the lower quasiparticle branch being observed in $x = 0.01$, one cannot determine the $V$ unambiguously. Thus, we perform the measurements extended to the second three-dimensional (3D) BZ on $x = 0.01$, and illustrate the FS in Fig. 5(a). The dispersion presented in Fig. 5(b), indicated via cut #a in Fig. 5(a), is measured at the crossing between $p_x$ and shadow $p_z$ bands, of which the intensity is too weak to be clearly visible in the plot. It is distinct that a gap completely opens below $E_F$. Since these two states are coupled by a nesting vector, guided by magenta arrow in Fig. 5(a), the interaction between them would also yield the $V$. We now can precisely measure $2V$ using the corresponding EDC plot in Fig. 5(c), showing $2V = 0.484$ eV. Based on this, it is further confirmed that the EPC strength undergoes a significant variation from $x = 0$ to 0.01.

The detailed studies on the evolution of electronic structures and EPCs give us a high chance to extract the nature of the interplay between multiple CDWs, as well as their relationship with the SC in Pd$_x$HoTe$_3$. According to the temperature versus pressure phase diagram proposed in Refs. 31 and 32, the role of Pd intercalation on the evolution of two CDWs and SC is similar to that of pressure performed on $RTe_3$ compounds. As already pointed out, the first CDW is suppressed monotonically because of the imperfect nesting. Simultaneously, the EPC strength of the second CDW has a remarkable transform from $x = 0$ to 0.01. This may be driven by the possible lattice distortion towards the tetragonal structure upon Pd intercalation, resulting from the competition between CDW orders for the low-energy spectral weight available for nesting.$^{30}$ Nevertheless, due to the longer than perfect nesting vector along a axis, the center of the second CDW gap still slightly locates below $E_F$ in $x = 0.01$. Thus, the gap further decreases even with an ideal nesting vector in $x = 0.02$. The competition and suppression of these two CDW instabilities give rise to the emergence of SC in $x = 0.02$, then the SC order reaches the maximum with the vanished CDWs in $x = 0.04$. Extensive work has been carried on the interplay between CDW and SC, principally in cuprate high-temperature superconductors$^{31,32}$ yet the underlying mechanism for the competition is still controversial.

Our ARPES results for the relationship between these collective states may shed light on it, even the high-temperature SC. As shown in the phase diagram of polycrystalline Pd$_x$HoTe$_3$ in Ref. 25, the weak Pd-intercalation dependence of $T_c$ indicates the SC possibly not determined by quantum critical fluctuations, the competition for FS with CDWs based on the Bilbro-McMillan partial gaping scenario may be the dominant nature instead.$^{30,33}$

To conclude, we have performed ARPES and electrical transport experiments on Pd$_x$HoTe$_3$ single crystals to study the interplay between multiple CDWs and their relationship with SC. We report the systematic evolution of the electronic structures and EPCs upon Pd intercalation, determine the nesting-driven nature of the CDWs formation, and find the competition between these CDW
orders is for the low-energy spectral weight. The compelling evidences for the dramatic transform of EPC strength along a axis from $x = 0$ to 0.01 leave the effect of Pd intercalation further complicated, requiring future studies to clarify. The competition between SC and CDWs for the FS may provide insight into the microscopic origin of high-temperature SC, paving the way to identify more high-temperature superconductors.

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