CH in stellar atmospheres: an extensive linelist

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ABSTRACT

The advent of high-resolution spectrographs and detailed stellar atmosphere modelling has strengthened the need for accurate molecular data. Carbon-enhanced metal-poor (CEMP) stars spectra are interesting objects with which to study transitions from the CH molecule. We combine programs for spectral analysis of molecules and stellar-radiative transfer codes to build an extensive CH linelist, including predissociation broadening as well as newly identified levels. We show examples of strong predissociation CH lines in CEMP stars, and we stress the important role played by the CH features in the Bond-Neff feature depressing the spectra of barium stars by as much as 0.2 magnitudes in the λ =3000 – 5500 Å range. Because of the extreme thermodynamic conditions prevailing in stellar atmospheres (compared to the laboratory), molecular transitions with high energy levels can be observed. Stellar spectra can thus be used to constrain and improve molecular data.

Key words. Stars : carbon, molecular data, line: identification, techniques: spectroscopic

1. Introduction

The computation of stellar atmosphere models requires, among various other ingredients, the knowledge of radiative transition rates for a large number of atomic and molecular species (Gustafsson et al. 2008). Extensive linelists, as complete as possible, with accurate oscillator strength values are needed for the calculation of opacities that affect the thermal structure of the atmosphere. The computation of detailed emergent spectra also requires accurate line positions (Plez 2008). The advent of high-resolution spectrographs on 8m-class telescopes (e.g. VLT/UVES, Keck/HIRES, VLT/CRiRES, SUBARU/HRS) allows a very detailed study of spectra of many astronomical objects. The discussion of possible abundance pattern differences between stars with and without planets lies now at a level of the order of 0.01 dex (Gustafsson et al 2010 Asplund 2005). The conclusions therefore heavily depend on the quality of the whole chain of data acquisition and analysis, not the least of which are the physical data. This kind of study requires a line position accuracy of the order of a few hundredths of Å or cm⁻¹ in the optical domain, and oscillator strengths with an accuracy better than 5%.

Great efforts have been devoted to improving atomic and molecular line data, e.g. VALD (Kupka et al. 1999) and DREAM (Biémont et al. 1999) for atoms, and Bernath (2009) and EXOMOL (Tennyson & Yurchenko 2012) for molecules. In particular, many transitions have been analysed in the laboratory, leading to a large number of accurate line positions, and molecular constants. However, line strength information is often missing, and lines involving highly excited states, not visible in the laboratory but important in warm astrophysical environments like stellar atmospheres, are lacking. We are therefore aiming at constructing molecular linelists for astrophysical use. The present paper targets CH.

The CH molecule is one of the most studied free radicals because it forms in various physical and astrophysical environments. This molecule was first detected by Heurlinger & Hulthen (1913) and then studied by many scientists (see references in Kalemos et al. 1999). This molecule has many valence and Rydberg states as reviewed by Vázquez et al. (2007), but only the lower energy states are of interest for stellar astrophysics. Our aim in this paper is to improve the situation for the ro-vibrational X²Σ⁺–X²Σ⁻ and the A²Δ–X²Π, B²Σ⁺–X²Π, and C²Σ⁺–X²Π electronic transitions of CH (for both 12C and 13CH isotopologues). Bound-bound transitions for CH appear in the near UV spectra of almost all F, G, K stars, whatever their carbon enrichment is. The G band at 4300 Å is particularly prominent, and is used, for example as a criterion for stellar classification (CH stars), and as a proxy for magnetic flux concentrations in the solar photosphere (Shelyag et al. 2004). As another example the 12C/13C isotopic ratio can be derived from the CH molecular lines in the near UV, and are often the only available carbon abundance indicator in very metal-poor stars. In addition, a good knowledge of the CH lines in the blue-UV part of the spectrum is also a prerequisite for determining the abundance of heavier metals (e.g. Bi, Pb, and U) in stellar environments, as these lines often blend those of the atomic species. To date, three linelists...
exist for CH. The first two have been available for a long time: one from R. Kurucz, for which there is little information on how the linelist was computed, and the SCAN-CH of Jørgensen et al. (1996), which also contains the ro-vibrational X-X transition. More recently, we compiled a third linelist, published as a poster at the “14th Cool Stars, Stellar Systems, and the Sun” conference in Pasadena, in 2006, and distributed since then by Plez. This list was assembled after our discovery that unidentified strong and broad lines in the near-UV spectrum of carbon-enhanced metal-poor (CEMP) stars were due to predissociation lines of CH (see the Appendix). The line positions and gf values come from the LIFBASE program (Luque & Crosley 1999); excitation energies from the SCAN linelist, and isotopic shifts were recomputed by our team.

It is this last linelist that is presented and discussed here, but we have largely updated it by (i) the computation of a uniform set of molecular constants from laboratory data supplemented by our measurement of high excitation lines in stellar spectra, (ii) the inclusion of both the observed and calculated line positions, (iii) the inclusion of radiative damping parameters accounting for predissociation, and (iv) the inclusion of the ro-vibrational X-X transition. The paper is structured as follows: first, we explain the method used to derive the linelist (Sect. 2), then we describe the data we have used for $^{12}$CH and $^{13}$CH (Sect. 3), and finally we summarize the content of the list (Sect. 4); we illustrate its improvements for stellar spectra in the Appendix.

2. Method

At least two parameters are required to assemble a molecular linelist: line positions and absolute line intensities. Other parameters may be added, e.g. collisional broadening parameters or Landé factors. Ab initio calculations can be attempted, but the use of observed line positions and intensities is more reliable. We therefore collected extensive laboratory data for $^{12}$CH and $^{13}$CH, which we supplemented with line positions extracted from stellar spectra.

We followed the method outlined in Li et al. (2012). First, we used the PGopher software to determine molecular constants from line positions. For the specific case of CH, these molecular constants include vibrational, rotational, and spin-rotational constants for all electronic states as well as spin-orbit and Λ-doubling constants for the X, Σ, Π and Υ states. The line positions used as input to PGopher were weighted according to the quoted accuracy of the various sources.

The version of PGopher we use is able to generate linelists and also provides Hön-London factors for doublet states. The computation of Einstein coefficients requires, however, the knowledge of transition moments. Hence, in a second step, from the vibration-dependent constants provided by PGopher, we derived the Dunham constants and used them in the RK1 code to calculate the potential $V_J(r)$. These potentials were injected into the LEVEL program to compute the transition moment matrix elements, $|\langle v', J'|Re(r)|v'', J'' \rangle|$, where $Re(r)$ is the transition moment as a function of the internuclear distance $r$, and $|v', J'|$ and $|v'', J'' \rangle$ are, respectively, the upper and the lower state vibrational wavefunctions. The matrix elements of the R(0) levels were then used as input to PGopher. However, in contrast to Li et al. (2012), we attempt to consider the rotational dependence of the transition moment matrix elements because we observed transitions involving highly excited rotation levels in order to consider the rotational effect on oscillator strengths. For example, the Einstein coefficient is decreased by $\sim 40\%$ between the lowest and the highest observed rotational A-X transition. We simultaneously attempt to correct for the Herman-Wallis effect. In order to approximate the rotational dependence of the transition moment and the Herman-Wallis correction, we approximated the moment matrix elements provided by LEVEL by fitting a polynomial function such that

$$|\langle v', J'|Re(r)|v'', J'' \rangle| = \sum_{i=1}^{n} a_i(v', v'', J', J''),$$

where the polynomial order $n$ is determined by requiring the rms of the fit to be less than 1%. Because the Einstein coefficient is proportional to the square of the transition matrix elements, we then correct the Einstein coefficients provided by the PGopher program by the square of the polynomial value for each transition. We note that it is not obvious that this polynomial fit of singlet-singlet transitions as delivered by LEVEL can be applied to doublet transitions. To test our approach, we therefore synthesized the solar spectrum with and without the polynomial correction. As demonstrated by Fig. 1, the synthetic spectrum of the Sun is improved greatly on the line intensity when corrections are applied.

In a third step, once a first CH linelist had been generated with PGopher, we generated a number of synthetic stellar spectra using Turbospectrum and appropriate MARCS stellar model atmospheres (Gustafsson et al. 2008). In addition to CH, we included other atomic lines from VALD (Kupka et al. 1999; Hill et al. 2002; Masseron 2006), as well as molecular linelists of CN and C$_2$ (Plez, private communication) and MgH from the Kurucz linelists. These spectra were compared with carefully selected observed stellar spectra (see Section 3.3) in an attempt to identify CH lines as yet unobserved in the laboratory. Thanks to the specific thermodynamic conditions present in cool carbon-star atmospheres, new transitions could indeed be observed and assigned. Although the resolution of spectrographs mounted at telescopes (typically $\Delta \lambda \approx 60\,000$, or $\approx 0.4\,\text{cm}^{-1}$ in our spectral range) does not reach that of laboratory spectrometers ($\approx 10^{-2}\,\text{cm}^{-1}$), the inclusion of some high rotational transitions only observed in stellar spectra allows us to improve the determination of the molecular constants in PGopher, with the appropriate weight for each line set by the measurement accuracy. We iterated the process of identification in stellar Atmospheres, and the Sun” conference in Pasadena, in 2006, and distributed since then by Plez.
spectra, and recalculated the list until no new lines could be identified.

Finally, we computed the radiative lifetime of each level $(\tau_{\ell^\prime J'})$ according to the formula

$$\tau_{\ell^\prime J'} = (\sum_{\ell J' \rightarrow \ell J} A_{\ell^\prime J' \ell J} \tau_{\ell J})^{-1},$$

where $A_{\ell^\prime J' \ell J}$ is the Einstein coefficient of one transition. As CH is a molecule known to show predissociation (Herzberg & Johns 1969), we also included the predissociation lifetimes, in order to allow for a better estimate of the line broadening parameter $\Gamma_{\text{rad}} = 1/\tau_{\ell^\prime J'} + 1/\tau_{\text{predissoc}}$.

3. Observed transitions

3.1. $^{12}$CH laboratory data

Laboratory data was collected from the literature. For the $^3\Pi$ fundamental state, we used the observations of Colin & Bernath (2010) of the ro-vibrational transitions in the ACE (Atmospheric Chemical Experiment; Bernath et al. 2005) solar spectrum. The quality and resolution of this spectrum is close to laboratory standard (0.02 cm$^{-1}$ in line position accuracy) and the 777 observed transitions allowed an accurate determination of the $^3\Pi$ state constants up to $v = 5$. For the $^3\Delta - ^3\Pi$ transition, we merged the laboratory measurements of Bernath et al. (1991) and Zachwieja (1995), with an average accuracy of 0.005 cm$^{-1}$ over 665 and 432 observed transitions, respectively. The experimental data for the $^3\Sigma^- - ^3\Pi$ transition was taken from Kepa (1996), Kumar et al. (1998), and Bernath et al. (1991), with respective accuracies (and number of lines) of 0.015 cm$^{-1}$ (169), 0.01 cm$^{-1}$ (73), and 0.005 cm$^{-1}$ (126). When the same line was present in different studies, we favoured the value from the most accurate measurement. For the $^3\Sigma^- - ^1\Phi$ transition, we used the experimental data from Bembenek et al. (1997) (56 lines), Ubachs et al. (1990) (35 lines), and Heider (1932) (159 lines) for the 0-0 transition with respective accuracies of 0.02 cm$^{-1}$, 0.003 cm$^{-1}$, 0.2 cm$^{-1}$, and Li et al. (1999) (124 lines) for the 1-1 transition with an accuracy of 0.05 cm$^{-1}$, and Herzberg & Johns (1969) (42 lines) for the 2-2 transition, with an accuracy of 0.2 cm$^{-1}$. Some line assignments from these papers did not correspond to the identification we could make with PGopher. They were changed to the closest matching wavenumber when using the published constant of each author (see Table 1).

3.2. $^{13}$CH

We could not find any observations of the $^{13}$CH ro-vibrational bands in the literature. For the $^3\Delta - ^3\Pi$, $^3\Sigma^- - ^3\Pi$, and $^3\Phi - ^3\Pi$ transitions, we use the observations of Zachwieja (1997) (601 lines), Para (1996) (177 lines), and Bembenek et al. (1997) (52 lines), with the respective quoted accuracies of 0.005 cm$^{-1}$, 0.015 cm$^{-1}$, 0.02 cm$^{-1}$. We reassigned some lines for $^{12}$CH in order to match the PGopher identifications (see Table 2).

3.3. Stellar observations and modelling

One may wonder why predissociation lines of CH, a molecule observed in basically all cool stars, were never detected before. They are definitely present (see Fig. 3), although never recognized, in stars as accurately known as the Sun, but such shallow flux depressions, in the middle of a forest of other atomic and molecular lines, were never previously identified as distinct spectral features.

Metal-poor stars, on the contrary, display much weaker atomic and molecular features, allowing a better estimate of the continuum level, and of possible deviations from it. It is therefore in the spectra of metal-poor stars, especially those with carbon-enrichment, that the weak and wide lines caused by CH predissociation are best seen.

Therefore, we use four stellar spectra: CS 22942-019 and HD 224959 both from VLT/UVES ranging from 3300 Å to 5500 Å, HD 196944 also from VLT/UVES with a spectral coverage of 3050-3850 Å better suited for the analysis of the C-X band, and a Keck/HIRES spectrum of HE 2201-0345 from 3650 Å to 4950 Å. The resolving power of these instruments, $R = \lambda/\Delta\lambda \approx 60,000$, combined with the turbulent and thermal Doppler broadening of the lines, leads to an accuracy of typically 0.1 Å in line positions, or about 0.5 cm$^{-1}$ in these spectral ranges. The positions of the predissociation lines of the B-X system are difficult to measure accurately as they are very broad and sometimes even diffuse. We estimate a 10 cm$^{-1}$ uncertainty for them (see Sect. 3.3). The lines were weighted accordingly in PGopher fits. The four stars are cool metal-poor C-rich giants, with $T_{\text{eff}} \sim 5000$ K. Their spectra show strong CH features, but they are only weakly blended by atomic lines. While CS 22942-019 and HE 2201-0345 have $^{12}$C/$^{13}$C ratios around 10, HD 196944 and HD 224959 have a carbon isotopic ratio of 4 to 5, allowing an easier identification of $^{13}$CH lines. The blending of CH features by other atomic and molecular features may lead to confusion. Therefore we strive to also reproduce the line intensities in order to resolve ambiguities (see Fig. 2). Our MARCS (Gustafsson et al. 2008) model atmospheres were specifically tailored to take into account the specific chemical composition (notably C and O), because this affects the thermodynamical structure (see the discussion in Masseron 2009). The elemental abundances are from Masseron et al. (2010) (except for HE 2201-0345, Masseron et al., in prep.). They are listed in Table 3. We note that $^{13}$CH lines are always weaker than the corresponding $^{12}$CH lines, because $^{13}$C is always less abundant than $^{12}$C. Line identifications could only be made for the strongest $^{13}$CH lines, limiting the number of molecular constants we could derive.

The positions of newly identified lines of the $^{12}$CH A-X, B-X, and C-X transitions in our stellar spectra are reported in Tables A.2, A.3 and A.4, while those for $^{13}$CH are reported in Tables A.5, A.6 and A.7 (available online).

For the A-X transition, we observed levels up to $J'' = 36.5$ for $v' = 0$, $J'' = 32.5$ for $v' = 1$, $J'' = 31.5$ for $v' = 2$, and $J'' = 27.5$ for $v' = 3$, very close to the dissociation limit, while only levels up to $J'' = 27.5$ for $v' = 0$, $J'' = 19.5$ for $v' = 1$, $J'' = 12.5$ for $v' = 2$, and $J'' = 10.5$ for $v' = 3$ were measured by Zachwieja (1995). We were able to determine for the first time the constants for the $^3\Delta - ^3\Pi$ v = 4 and v = 5 states. For the B-X transition (Table A.3), we observed transitions from higher $J''$ levels than Kepa (1996) and Bernath et al. (1991) (J'' < 15.5), and than Kumar et al. (1998) (J'' < 21.5). For the C-X transition, we also observe lines to higher rotational levels in our CEMP star spectrum than in laboratory spectra. There is an excellent agreement
Table 1. Modified line assignments for the $^{12}$CH transitions. NA stands for lines used in previous studies that we no longer consider in the constant determination process.

| Colin & Bernath (2010) X-X | Bernath et al. (1991) B-X | Kepa (1996) B-X |
|-----------------------------|--------------------------|-----------------|
| previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ | previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ | previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ |
| 1-0 P2ee(1.5)               | 1-0 P2ee(1.5)            | 1-1 Q12ee(0.5)  | 1-1 Q12ee(0.5)  | 1-0 Q12ee(0.5)  | 1-0 Q12ee(0.5)  |
| 1-0 P2ff(1.5)               | 1-0 P2ff(1.5)            | 1-1 Q2ee(0.5)   | 1-1 Q2ee(0.5)   | 0-1 Q2ee(0.5)   | 0-1 Q2ee(0.5)   |
| 1-1 P2ee(1.5)               | 1-0 P2ee(1.5)            | 1-1 R1ee(0.5)   | 1-1 R1ee(0.5)   | 1-1 P2ee(0.5)   | 1-1 Q1fe(0.5)   |
| 1-1 P2ff(1.5)               | 1-0 P2ff(1.5)            |                 |                 | 1-1 Q1fe(0.5)   |                 |
| 2-1 Q2ee(1.5)               | 1-0 Q1fe(0.5)            |                 |                 | 2-1 Q2ff(0.5)   | 2-1 Q2ff(0.5)   |
| 2-1 Q2ff(1.5)               | 1-0 Q1fe(0.5)            |                 |                 | 0-0 R1ee(0.5)   | 0-0 R1ee(0.5)   |
| 2-1 R2ee(0.5)               | 1-0 R2ee(0.5)            |                 |                 | 0-1 R2ff(0.5)   | 0-1 R2ff(0.5)   |
| 2-1 R2ff(0.5)               | 1-0 R2ff(0.5)            |                 |                 | 1-1 R2ee(0.5)   | 1-1 R2ee(0.5)   |
| 4-3 P2ee(1.5)               | 1-0 P2ee(1.5)            |                 |                 | 0-0 Q12ff(0.5)  | 0-0 Q12ff(0.5)  |
| 4-3 R2ff(0.5)               | 1-0 R2ff(0.5)            |                 |                 | 0-0 R12ff(0.5)  | NA              |

Table 2. Modified line assignments for the $^{13}$CH transitions.

| Zachwieja (1995) A-X | Ubachs et al. (1986) C-X | Bembenek et al. (1997) C-X |
|----------------------|--------------------------|---------------------------|
| previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ | previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ | previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ | previous $v'$-$v'' F(J'_p)$ | new $v'$-$v'' F(J''_p)$ |
| 1-1 R2ff(0.5)        | 1-1 R2ff(0.5)            | 0-0 Q12ee(0.5)            | 0-0 Q12ee(0.5)  | 0-0 R2ff(0.5)   | NA              |
| 1-1 R2ee(0.5)        | 1-1 R2ee(0.5)            | 0-0 Q12ee(0.5)            | 0-0 Q12ee(0.5)  | 1-1 R1ee(0.5)   | 1-1 R1ee(0.5)   |
| 2-2 R2ff(0.5)        | 2-2 R2ff(0.5)            | 0-0 R1ee(0.5)             | 0-0 R1ee(0.5)   | 1-1 Q2ff(0.5)   | 1-1 Q2ff(0.5)   |
| 3-3 R2ff(0.5)        | 3-3 R2ff(0.5)            | 3-3 R2ff(0.5)             | 3-3 R2ff(0.5)   | 1-1 Q2ff(0.5)   | 1-1 Q2ff(0.5)   |
| 0-1 R2ff(0.5)        | 0-1 R2ff(0.5)            | 1-2 R2ee(0.5)             | 1-2 R2ee(0.5)   | 0-0 R12ff(0.5)  | 0-0 R12ff(0.5)  |
| 1-2 R2ee(0.5)        | 1-2 R2ee(0.5)            | 0-1 Q1fe(0.5)             | 0-1 Q1fe(0.5)   | 1-1 R2ff(0.5)   | 1-1 R2ff(0.5)   |
| 2-3 R2ff(0.5)        | 2-3 R2ff(0.5)            | 1-1 R2ff(0.5)             | 1-1 R2ff(0.5)   | 1-1 R2ff(0.5)   | 1-1 R2ff(0.5)   |
| 4-3 R2ff(0.5)        | 4-3 R2ff(0.5)            | 2-3 R2ff(0.5)             | 2-3 R2ff(0.5)   | 2-3 R2ff(0.5)   | 2-3 R2ff(0.5)   |

Table 3. Adopted stellar parameters and abundances for the sample stars.

|          | HD 196944 | HD 224959 | CS 22942-019 | HE 2201-0345 |
|----------|-----------|-----------|--------------|--------------|
| $T_{\text{eff}}$ | 5250      | 4900      | 5100         | 4800         |
| log $g$   | 1.7       | 2.0       | 2.5          | 1.9          |
| [Fe/H]    | -2.25     | -2.10     | -2.50        | -2.10        |
| [$\alpha$/Fe] | +0.40     | +0.40     | +0.40        | +0.40        |
| log A(C)  | 7.35      | 8.15      | 8.10         | 7.95         |
| $^{12}$C/$^{13}$C | 5        | 4         | 12           | 10           |
| log A(N)  | 7.05      | 7.60      | 6.40         | 6.70         |
| log A(O)  | 6.8       | 7.7       | 6.7          | 7.5          |
| [Sr, Y, Zr, Ba, La, Pb]/Fe | 1.5 | 2.0 | 1.5 | 1.3 |

with the predicted line positions derived from the laboratory experiments.

4. Results

4.1. Revised molecular constants for $^{12}$CH

After merging all data of all transitions (i.e. ro-vibrational, A-X, B-X, and C-X) from laboratory and from stellar spec-
tra observations into PGopher, weighted according to their respective accuracy, we were able to derive a single set of new molecular constants for the four lowest doublet electronic states of CH. The constants we provide in this section are consistent with the definition of the Hamiltonian of Brown et al. (1979): \( B \) is the rotational constant; \( D_v \), \( H_v \), \( L_v \), and \( M_v \) are the centrifugal distortion constants. \( \Lambda \) is the spin-orbit constant; \( \gamma_\tau \) and \( \gamma_\nu \) are the spin-rotation constant and its centrifugal distortion; and \( p_\nu \) and \( q_\nu \) are the \( \Lambda \)-doubling constants. For the computation of Einstein coefficients and level radiative lifetime, we used the electronic-transition moments of van Dishoeck (1987). For the ro-vibrational transitions, we used the dipole moment function calculated by Hettema & Yarkony (1994). We scaled the electronic-transition moments to match the experimental lifetime measurements: \( \tau_{\text{obs}} = 535 \text{ ns} \) for the \( \Lambda^2\Delta \nu = 0 \) level (Luque & Crosley 1996a), \( \tau_{\text{obs}} = 325 \text{ ns} \) for the \( B^2\Sigma^- \nu = 0 \) level (Luque & Crosley 1996b), and \( \tau_{\text{obs}} = 110 \text{ ns} \) for the \( C^2\Sigma^+ \nu = 0 \) level (Brzozowski et al. 1974).

4.1.1. The \( \text{X}^2\Pi \) fundamental state

Thanks to the supplementary data offered by our spectra in the optical region, we could improve the ground state constants. The constants we obtained are presented in Table 4. They are consistent with the work of Colin & Bernath (1996). We included their data in our fit. Moreover, thanks to our observations of high J A-X transitions (see Fig. 2), we could improve the accuracy of the high-order constants, notably of \( L_v \).

4.1.2. The \( \text{A}^2\Delta \) state

Table 5 contains the constants we derive for the \( \Lambda^2\Delta \) state. We were able to determine for the first time the constants for the \( \Lambda^2\Delta \nu = 4 \) and 5 levels (Fig. 2). For the lower vibrational levels, our constants agree well with the ones of Zachwieja (1995) because we used of their laboratory measurements. The small differences come from the fact that we obtained different constants for the ground state. However, in contrast to Zachwieja (1995), we could not recover the \( \Lambda \)-doubling constants \( p_\nu \) and \( q_\nu \) similar to Bernath et al. (1991). The resulting \( \text{rms} \) difference of the observed minus calculated line positions is \( 1.46 \times 10^{-2} \text{ cm}^{-1} \), which is very satisfactory for studies of stellar spectra. Because some of the A levels are expected to predissociate (see Sect. 2), their lifetime should be shorter than their radiative lifetime (Brzozowski et al. 1974). However, we did not observe any increased broadening for the A-X lines in our stellar spectra. The predissociation broadening is dominated by thermal and turbulence broadening in our target stars. Nevertheless, the predissociation lifetimes are included in our linelist.

4.1.3. The \( \text{B}^2\Sigma^- \) state

Table 6 presents the constants we have derived for the \( \text{B}^2\Sigma^- \) state. The constants are in good agreement with Kemp (1996).

There are a number of high J B-X predissociation lines that can be seen even in the solar spectrum (Fig. 5). However, as already noted by Kumar et al. (1998), their positions are not well defined. These lines do not help to improve the accuracy of the B state constants, but nevertheless we include them in our final linelist. Predissociative lifetimes of the corresponding levels are listed in Table 7. They are in good agreement with the laboratory observations of Kumar et al. (1998), and Luque & Crosley (1996b). Because of the increasing broadening of the lines with rotational quantum number, the identification of the lines becomes more and more uncertain as \( J \) increases. Consequently, the identification of some levels is ambiguous and the exact dissociation energy of the B state is very difficult to determine. We set the height of the predissociation barrier according to our new line identifications, that include the observed \( 0 \rightarrow 0 \) R(1) (21.5) line, with an upper energy level of \( 31474 \text{ cm}^{-1} \). The height of the barrier is thus at least \( 31474 - 29374 = 2100 \text{ cm}^{-1} \), with \( D_v = 29374 \pm 10 \text{ cm}^{-1} \) (Kumar et al. 1998), almost twice as high as the value of \( 1550 \text{ cm}^{-1} \) predicted by van Dishoeck (1987).

Assuming this barrier height, \( \text{B}^2\Sigma^- \nu = 1 \) levels have been included up to \( J^\prime = 20.5 \) in our list, although we were able to identify B-X transitions only up to \( J^\prime = 16.5 \) because the combination of low \( g_f \) values and large predissociation broadening limits the identification. However, we stress that these very broad lines act as a pseudo-continuum and must be taken into account in spectrum synthesis (see Fig. 4).

An atlas of predissociation lines for some typical spectra (the Sun, Arcturus, and several carbon-enhanced metal-poor stars) is presented in the Appendix.

Table 7. Radiative lifetimes from this work and experimental lifetimes from Luque & Crosley (1996b) of the \( \text{B}^2\Sigma^- \) levels in ns. a extraplated value from astrophysical observations. Predissociation onset is the limit of the lowest level with evidence for predissociation and predissociation barrier indicates the limit of the uppest level with evidence for predissociation.

| \( J \) | \( \tau_{\text{rad}} \) | \( \tau_{\exp} \) | \( \tau_{\text{rad}} \) | \( \tau_{\exp} \) |
|---|---|---|---|---|
| 0.5 | 3.28 | 4.72 | 4.72 | 4.72 |
| 1.5 | 3.29 | 4.74 | 4.74 | 4.74 |
| 2.5 | 3.30 | 4.76 | 4.76 | 4.76 |
| 3.5 | 3.32 | 4.80 | 3.96 | 3.96 |
| 4.5 | 3.35 | 4.86 | 4.10 | 4.10 |
| 5.5 | 3.38 | 4.93 | 4.05 | 4.05 |
| 6.5 | 3.43 | 5.02 | 3.00 | 3.00 |
| 7.5 | 3.48 | 5.12 | 5.0 | 5.0 |
| 8.5 | 3.54 | 5.26 | 0.350 | 0.350 |
| 9.5 | 3.61 | 5.43 | 0.075 | 0.075 |
| 10.5 | 3.70 | 5.63 | 0.015 | 0.015 |
| 11.5 | 3.80 | 5.89 | 0.005 | 0.005 |
| 12.5 | 3.92 | 6.20 | 0.0013 | 0.0013 |
| 13.5 | 4.06 | 3.95 | 0.0004 | 0.0004 |
| 14.5 | 4.23 | 4.35 | 0.0002* | 0.0002* |
| 15.5 | 4.43 | 1.40 | 0.00001* | 0.00001* |
| 16.5 | 4.68 | 7.0 | 0 | 0 |
| 17.5 | 4.98 | 0.6 | 1.0E-6* | 1.0E-6* |
| 18.5 | 5.35 | 0.045 | 3.0E-7* | 3.0E-7* |
| 19.5 | 5.82 | 0.010 | 1.0E-7 | 1.0E-7 |
| 20.5 | 6.42 | 0.003 | 3.0E-8* | 3.0E-8* |
| 21.5 | 7.23 | 0.0004 | 3.0E-8* | 3.0E-8* |

a predissociation barrier –
Because the abundance of Para (1996), and Bembenek et al. (1997) (see Sect. 3.2).

4.2. Revised molecular constants for Brzozowski et al. (1976) and Ubachs et al. (1986). The corresponding predissociation lifetime measurements of (Brzozowski et al. 1976). We could not detect any increase predissociation lifetimes are larger than for the B state linelist (see Fig. 4).

Jorgensen et al. (1996), we were able to improve the C-X lienlist (see Fig. 4). Li et al. (1999) and Bembenek et al. (1997) compared to thanks to the inclusion of more recent laboratory data from did not attempt to use these lines in our global fit. However, as our identifications of their measured positions with the predicted values de-

so far. As shown in Table 8, there is an excellent agreement Tables 9, 10, 11, and 12 present the molecular constants we a\( ^2\Sigma^+ \) state

We were able to identify C-X lines in our CEMP star spectrum at higher J than in any published laboratory works so far. As shown in Table 8 there is an excellent agreement of their measured positions with the predicted values derived from the laboratory constants. As our identifications carry a lower accuracy than laboratory measurements, we did not attempt to use these lines in our global fit. However, thanks to the inclusion of more recent laboratory data from Li et al. (1999) and Bembenek et al. (1997) compared to Jorgensen et al. (1996), we were able to improve the C-X linelst (see Fig. 4).

The C state is also known to predissociate, but the predissociation lifetimes are larger than for the B state (Brzozowski et al. 1976). We could not detect any increase in the line broadening in our stellar spectra, but we nevertheless include the broadening lifetime in our list using the corresponding predissociation lifetime measurements of Brzozowski et al. (1976) and Ubachs et al. (1986).

4.2. Revised molecular constants for \(^{13}\)CH

Tables 9, 10, 11, and 12 present the molecular constants we derive for the four lowest doublet electronic states of \(^{13}\)CH. The experimental data were taken from Zachwieja (1997), Para (1996), and Bembenek et al. (1997) (see Sect. 3.2). Because the abundance of \(^{13}\)C is lower than \(^{12}\)C in stellar atmospheres, we were not able to observe transitions to much higher J values than in the laboratory, as we did for \(^{12}\)CH. Although the lines observed in stellar spectra contribute to improve the accuracy of high-order \(J\) constants, the major improvements in the constants come from our global fit of all the laboratory data for the three electronic transitions (A-X, B-X, and C-X), which had never been done previously; for example we were able to recover experimentally for the first time the spin-orbit constant (\(A_v\)) of the fundamental level (Table 9).

We were also able detect for the first time predissociation lines for the B state of \(^{13}\)CH. Because the potential and the energy levels are not strictly identical to the \(^{12}\)CH case, predissociation may occur for other levels and with different lifetimes. The quality of our spectra, the presence of blends with other lines, and the diffuse character of the predissociation lines did not allow us to measure any significant difference in the widths of the predissociated lines of \(^{13}\)CH and \(^{12}\)CH. Therefore, the same predissociation lifetimes as for \(^{12}\)CH were adopted. For the C state, only the constants for the \(v = 0\) level could be determined as we could not assign any lines linking to other vibrational levels. Improvements of the \(^{13}\)CH constants could certainly be obtained with the identification of the infrared ro-vibra-tional X-X transition.

4.3. Equilibrium constants and partition function

4.3.1. Equilibrium constants

In Table 13 we present equilibrium molecular constants (in cm\(^{-1}\)) for the four lowest doublet electronic states of \(^{12}\)CH, including the \(a^4\Sigma^-\) state for which the constants

| Constant | \(v = 0\) | \(v = 1\) | \(v = 2\) | \(v = 3\) | \(v = 4\) | \(v = 5\) |
|----------|----------|----------|----------|----------|----------|----------|
| \(T_e\)   | 0.0      | 2732.97906(130) | 5339.9051(20) | 7822.2222(28) | 10181.0060(41) | 12416.755(24) |
| \(B_e\)   | 0.0      | 2732.97813(94) | 5339.9036(15) | 7822.2184(18) | 10180.9996(22) | 12416.786(10) |
| \(A_v\)   | 14.192249(57) | 13.661720(50) | 13.135783(58) | 12.613439(67) | 12.092993(100) | 11.57877(52) |
| \(\gamma_{v=2}^2\) | 14.192393(61) | 13.661786(53) | 13.135809(50) | 12.613441(50) | 12.092993(54) | 11.57800(23) |
| \(p_v^2\) | 28.14756(8) | 28.33833(5) | 28.5312(78) | 28.652(14) | 28.909(30) | 28.64(40) |
| \(q_v^2\) | 28.14756(8) | 28.33833(5) | 28.5312(78) | 28.652(14) | 28.909(30) | 28.64(40) |

Notes. a fixed to Jackson et al. (2008) b kept fixed
Table 5. Constants (in cm\(^{-1}\)) for the A\(^2\Delta\) state. Uncertainties in parentheses are one standard deviation in units of the last quoted digit.

| Constant | \(v = 0\) | \(v = 1\) | \(v = 2\) | \(v = 3\) | \(v = 4\) | \(v = 5\) |
|----------|-----------|-----------|-----------|-----------|-----------|-----------|
| \(T_e\)  | 25173.4558(110) | 25913.7404(21) | 28460.7221(32) | 30794.1049(45) | 32885.355(84) | 34695.691(73) |
| \(B_e\)  | 14.57906(58) | 13.911205(75) | 13.18806(11) | 12.37277(17) | 11.4667(21) | 10.33371(21) |
| \(D_e\times10^3\) | 1.56601(34) | 1.60903(46) | 1.6909(11) | 1.8257(21) | 2.171(15) | 2.455(19) |
| \(H_e\times10^8\) | 9.962(61) | 8.94(11) | 8.60(27) | 6.30(62) | 32.5(38) | -39.9(53) |
| \(L_e\times10^{14}\) | -2.817(33) | -5.274(69) | -11.88(17) | -20.634(50) | -93.2(32) | -127.2(30) |
| \(A_e\)  | -1.10150(140) | -1.0721(20) | -1.0402(26) | -0.9934(38) | -0.95(9) | -0.9(9) |
| \(\gamma_e\times10^2\) | 4.171(37) | 3.979(49) | 3.821(53) | 3.370(75) | 3.21(27) | 3.0(9) |
| \(\gamma D_e\times10^5\) | -0.730(150) | -0.700(270) | -0.871(92) | -1.0697(13) | -0.925(65) | -1.0392(27) |
| \(p_e\times10^7\) | 6.6(14) | 13.0(74) | 28.1(11) | 58.88(8) |
| \(q_e\times10^8\) | 4.53(88) | 14.1(53) | -2.89(36) | -17.5(24) |

Notes.  a Constants by Zachwieja (1993).  b kept fixed

Table 6. Constants (in cm\(^{-1}\)) for the B\(^2\Sigma^-\) state. Uncertainties in parentheses are one standard deviation in units of the last quoted digit.

| Constant | \(v = 0\) | \(v = 1\) | \(v = 2\) | \(v = 3\) | \(v = 4\) | \(v = 5\) |
|----------|-----------|-----------|-----------|-----------|-----------|-----------|
| \(T_e\)  | 25712.50(12) | 27507.5216(24) | 28460.7212(32) | 30794.1049(45) | 32885.355(84) | 34695.691(73) |
| \(B_e\)  | 12.6400(15) | 11.15815(48) | 11.15788(14) | 11.15788(14) | 11.15788(14) | 11.15788(14) |
| \(D_e\times10^3\) | 2.13110(560) | 3.1680(260) | 3.1260(60) | 3.09(77) | 3.09(77) | 3.09(77) |
| \(H_e\times10^8\) | -4.930(540) | -14.90(500) | -30.22(74) | -30.22(74) | -30.22(74) | -30.22(74) |
| \(L_e\times10^{10}\) | 9.7(21) | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| \(M_e\times10^{12}\) | -2.70(27) | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| \(\gamma_e\times10^2\) | -2.938(47) | -2.1(46) | -2.10(16) | -2.10(16) | -2.10(16) | -2.10(16) |
| \(\gamma D_e\times10^5\) | 2.08(39) | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

Notes.  a Constants derived by Kopáč (1996).

4.3.2. Partition function

Using our calculated levels up to the dissociation energy limit, we compute the partition function \(Q\) following Tatum (1966),

\[
Q(T) = \sum_{i=0}^{E_i \leq D_e} g_i e^{-\frac{E_i}{kT}},
\]

where \(T\) is the temperature, \(g_i = 2J + 1\) is the multiplicity of a single \(\Lambda\)-doubling rotational level of energy \(E_i\), and \(k\) is the Boltzmann constant. For the \(X^2\Pi, A^2\Delta, B^2\Sigma^-,\) and \(C^2\Sigma^+\) states we used the constants derived in this work. We also included the low-lying \(a^4\Sigma^-\) state with constants from Lie et al. (1973) and Kalemos et al. (1999), important for the accuracy of the partition function. Following the formula \(\ln(Q) = \sum_{i} a_i \ln(T)^i\), the derived coefficients for our new partition function are \(a_0 = 11.00608809, a_1 = -2.68892131\) and \(a_2 = 0.27091654\). This updated partition function differs from that of Sauval & Tatum (1984) by 6 % at \(T = 4000\) K, and 2 % at 6000 K (see Fig. 5).
Table 8. Constants (in cm\(^{-1}\)) for the \(C^2\Sigma^+\) state. Uncertainties in parentheses are one standard deviation in units of the last quoted digit.

| Constant | \(v=0\) | \(v=1\) | \(v=2\) |
|----------|----------|----------|----------|
| \(T_c\)  | 31791.6479(16) | 34403.310(21) | 36772.842(54) |
| \(B_c\)  | 14.255724(90) | 13.50577(43) | 12.6046(29) |
| \(D_c\times10^3\) | 1.59375(97) | 1.6363(21) | 1.918(37) |
| \(H_c\times10^6\) | 7.45(29) | 14.7(27) | -73.10(10) |
| \(L_c\times10^{11}\) | -3.75(26) | 0.0 | 0.0 |
| \(\gamma_v\times10^2\) | 4.120(58) | 3.320(120) | 3.80(10) |
| \(\gamma_D\times10^5\) | -1.66(62) | 0.0 | 0.0 |
| \(\gamma_H\times10^8\) | 0.0 | 0.0 | 0.0 |

Notes. * Values from Li et al. (1999).

Table 9. Constants (in cm\(^{-1}\)) for the \(X^2\Pi\) state of \(^{13}\)CH. Uncertainties in parentheses are one standard deviation in units of the last quoted digit.

| Constant | \(v=0\) | \(v=1\) | \(v=2\) |
|----------|----------|----------|----------|
| \(T_c\)  | 28.1426(81) | 28.3355(87) | 28.508(21) |
| \(B_c\)  | 3.823672 | 3.243(59) | 2.969(51) |
| \(D_c\times10^3\) | -2.514(59) | -2.308(53) | -2.146(66) |
| \(H_c\times10^6\) | -1.36(14) | 0.0 | 0.0 |
| \(p_{\nu}\times10^6\) | 1.426(52) | 1.386(7) | 1.397(10) |
| \(q_{\nu}\times10^5\) | -8.51(56) | -12.6(36) | 0.0 |
| \(r_{\nu}\times10^5\) | -8.91(40) | -7.92(15) | -6.93(7) |
| \(\gamma_{\nu}\times10^3\) | 1.44440(29) | 1.42186(32) | 1.40001(43) |
| \(\beta_{\nu}\times10^3\) | 1.1380(180) | 1.0240(190) | 1.08(11) |

Notes. * Constants derived by Zachwieja (1997). * kept fixed. ° taken from Steinle et al. (1983).

4.4. linelist format

Our linelist includes the A-X, B-X, and C-X electronic transitions up to the last observed vibrational levels (i.e., \(v<5\) for the A and X states, \(v<1\) for the B state, and \(v<2\) for the C state), with rotational levels up to the dissociation energy as listed in Table 13. Concerning the \(^{13}\)CH linelists, for the vibrational levels that could not be observed but that exist for \(^{12}\)CH (i.e., \(X^2\Delta \; v=4\) and 5, \(A^2\Delta \; v=4\) and 5, and \(C^2\Sigma^+ \; v=1\) and 2), the Born-Oppenheimer approximation from \(^{12}\)CH has been used to determine the transitions applying the Jorgensen (1994) formulas (3), (4), and (5). The X-X ro-vibrational transitions up to dissociation are also included for both isotopologues. The linelist is available on http://www.astro.ub.ac.be/~spectrotools/, and will be made available through the VALD database (Kupka et al. 1999). An example of the default output format is presented in Table 13. The database offers various output
### Table 10. Constants (in cm\(^{-1}\)) for the A\(^2\Delta\) state of \(^{13}\)CH. Uncertainties in parentheses are one standard deviation in units of the last quoted digit.

| Constant | \(v = 0\) | \(v = 1\) | \(v = 2\) | \(v = 3\) |
|----------|-----------|-----------|-----------|-----------|
| \(T_c\)  | 23173.84500(200) | 25996.4648(33) | 28447.0901(50) | 30775.3828(78) |
|          | 23173.84460(69)\(^a\) | 25996.4596(15)\(^a\) | 28446.9953(30)\(^a\) | 30775.3748(59)\(^a\) |
| \(B_c\)  | 14.492570(100) | 13.492009(73) | 12.31697(34) | 11.20720(50) |
| \(A_v\)  | -1.09930(270) | -1.0741(33) | -1.0312(38) | -0.9981(68) |
| \(\gamma_v\times10^2\) | 4.211(66) | 4.056(77) | 3.717(78) | 3.530(160) |
| \(D_v\times10^3\) | 1.54753(74) | 1.58069(82) | 1.64999(87) | 1.7963(34) |
| \(H_v\times10^8\) | 9.610(18) | 5.05(18) | 0.0 | 0.0 |
| \(L_v\times10^{11}\) | -2.61(14) | 0.0 | 0.0 | 0.0 |
| \(\gamma_{Dv}\times10^5\) | -1.140(220) | -1.610(270) | 0.0 | 0.0 |
| \(p_v\times10^7\) | 0.0 | 0.0 | 0.0 | 0.0 |
| \(q_v\times10^8\) | 5.7(18)\(^a\) | 10.4(24)\(^a\) | 20.5\(^a\) | 27.5\(^a\) |

**Notes.** \(^a\) Constants derived by \cite{Zachwieja1997}. \(^b\) kept fixed in \cite{Zachwieja1997}.

### Table 11. Constants (in cm\(^{-1}\)) for the B\(^2\Sigma^-\) state of \(^{13}\)CH. Uncertainties in parentheses are one standard deviation in units of the last quoted digit.

| Constant | \(v = 0\) | \(v = 1\) |
|----------|-----------|-----------|
| \(T_c\)  | 25713.4438(29) | 27504.4876(40) |
|          | 25713.4456(13)\(^a\) | 27504.4859(21)\(^a\) |
| \(B_c\)  | 12.56638(22) | 11.09913(67) |
|          | 12.56652(11)\(^a\) | 11.09553(20)\(^a\) |
| \(\gamma_v\times10^2\) | -2.700(74) | -2.206(80) |
|          | -2.680(110)\(^a\) | -2.260(110)\(^a\) |
| \(D_v\times10^3\) | 2.10830(400) | 3.0660(290) |
|          | 2.10289(89)\(^a\) | 3.0621(35)\(^a\) |
| \(H_v\times10^7\) | -3.340(270) | -28.9(35) |
|          | -3.945(30)\(^a\) | -29.57\(^a\) |
| \(L_v\times10^{10}\) | -1.31(60) | 0.0 |
| \(\gamma_{Dv}\times10^5\) | 1.19(41) | 0.0 |

**Notes.** \(^a\) Constants derived by \cite{Para1996}.

### Table 12. Constants (in cm\(^{-1}\)) for the C\(^2\Sigma^+\) state of \(^{13}\)CH. Uncertainties in parentheses are one standard deviation in units of the last quoted digit. \(^a\) Values from \cite{Li1999}.

| Constant | \(v = 0\) |
|----------|-----------|
| \(T_c\)  | 31791.8419(33) |
|          | 31791.8329(31)\(^a\) |
| \(B_c\)  | 14.17084(20) |
|          | 14.17132(35)\(^a\) |
| \(\gamma_v\times10^2\) | 4.001(80) | 4.030(250)\(^a\) |
| \(D_v\times10^3\) | 1.5666(20) | 1.5728(27)\(^a\) |
| \(H_v\times10^8\) | 4.49(53) | 5.15(51)\(^a\) |
| \(\gamma_{Dv}\times10^5\) | 0.0 | 2.03\(^a\) |

**Notes.** \(^a\) Constants kept fixed in \cite{Bembenek1997}.
Table 13. Equilibrium constants for $^{12}$CH

| Constant | $X^2\Pi$ | $a^3\Sigma^-$ | $A^2\Delta$ | $B^3\Sigma^-$ | $C^2\Sigma^+$ |
|----------|----------|--------------|-------------|--------------|--------------|
| $D_0$(cm$^{-1}$) | 29374.0 | 23349.6 | 16210.26 | 4731.57 | 7549.36 |
| $D_0^0$(cm$^{-1}$) | 27959.64 | | | | |
| $r_e$(Å) | 1.11981 | 1.0892 | 1.10366 | 1.16370 | 1.12777 |
| $T_e$ | 0.0 | 6024.40 | 23148.73 | 24642.42 | 31809.64 |
| $\omega_e x_e$ | 2860.92 | 3090.98 | 2923.37 | 2255.07 | 2853.1724 |
| $\omega_e y_e$ | 64.5818 | 102.17 | 90.2 | 223.2 | 120.8564 |
| $\omega_e z_e$ | 0.407275 | -0.1917 | -0.3892 | | |
| $B_e$ | 14.45924 | 15.3643 | 14.88536 | 13.3818 | 14.56066 |
| $\alpha_e$ | 0.53502 | 0.553 | -0.591798 | 1.4828 | 0.56653 |
| $\gamma_e$ | 0.001993 | -0.047110 | -0.08659 | | |
| $\epsilon_e$ | 0.000214 | 0.00782 | | | |

Notes. * Constants taken from Kalemos et al. (1999). * Constants taken from Lie et al. (1973). * Value fixed according to Lie et al. (1973).

Formats and unit conversions. The gf value is defined as in Larsson (1983),

$$gf = (2J'' + 1) \times f_{J', J''} = \frac{m_e e_0 c}{2\pi e_0 v^2 (2J' + 1)A_{J', J''}}, \quad (4)$$

$f_{J', J''}$ being the absorption oscillator strength and $\nu$ the line position in cm$^{-1}$.

Additionally, in our final linelist, we have included radiative and predissociation broadening ($\Gamma_{rad}$), using the formula

$$\Gamma_{rad} = 1/\tau_{J', J''}^{\text{rad}} + 1/\tau_{J', J''}^{\text{predissoc}}, \quad (5)$$

where $\tau_{J', J''}^{\text{rad}}$ is the radiative lifetime and $\tau_{J', J''}^{\text{predissoc}}$ is the predissociation lifetime of the level in seconds. This broadening includes both the radiative lifetime and the predissociation lifetime as measured by Luque & Crosley (1996a), Luque & Crosley (1996b) and Brzozowski et al. (1976) for, respectively, the A, B, and C state.
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Fig. 3. Top panel: example of a synthesis of the solar photospheric spectrum (dotted black) including (red) and omitting (blue) predissociation lines of the B-X system. Bottom panel: Same for the CEMP star CS 22942-019. Predissociation lines, as well as many other CH lines, are present and contribute to the flux depression. In the case of the CEMP star, the presence of several extremely broad CH predissociation lines is so important that it acts as a pseudo-continuum.

Fig. 4. Observed solar photospheric spectrum (black dots) and synthetic spectra using the former CX linelist (blue dotted line) from Jorgensen et al. (1996) and our C-X linelist (red solid line).

Fig. 5. Our new partition function compared to the work of Sauval & Tatum (1984). The discrepancy is on average 3%.
Fig. 1. Synthetic spectrum of the Sun near the 1-0 ro-vibrational band of CH compared to the observed solar spectrum (ACE; Bernath et al. 2005) (dotted line). The red line includes the J-dependence correction (see text) while the blue does not. The first 3 panels from left to right show from the R branch, for which intensity increases with increasing J. The increasing relative strength between the synthesis with and without the J-dependence correction demonstrates the rotational dependence of the transition moment for CH. The two right panels show lines from the P branch. The fact that the J-dependence correction is not the same as for R branches is due to the Herman-Wallis effect.
Fig. 2. Example of stellar spectrum syntheses in the CH A-X transition region. The stellar spectrum is plotted with black points, the red continuous line is the synthesis including both atomic and molecular lines, and the green dashed line is the synthesis with only CH A-X 5-5 transitions in HE 2201-0345 (upper panel) and CH A-X 4-4 transitions in CS 22942-019 (lower panel) identified for the first time in a spectrum. We note that some of the mismatches between the synthesis and the observation (e.g. 4505.7 Å, 4412 Å) can be attributed to inaccuracies of other atomic or molecular linelists.
### Table 14. Sample of the linelist 
(the complete list as well as the other electronic and ro-vibrational transitions are available electronically).

| λ (Å) | gf (10^{-1}) | E | J | Nl | sl | E (10^{-1}) | vu | Ju | Nu | su | Γrad | mol | trans | br | o-c (10^{-1}) |
|-------|---------------|---|---|----|----|-----------|----|----|----|----|-----|------|-----|-------|---|----------|
| 4300.3005 | 0.1170117E-01 | 14.27597 | 0 | 0.5 | 0 | e | 23261.91647 | 0 | 1.5 | 0 | e | 0.328588E+07 | 0.00000 | CH A X R -0.05040 |
| 3847.4470  | 0.1054307E-04 | 14.27597 | 0 | 0.5 | 0 | e | 25998.16801 | 1 | 1.5 | 0 | e | 0.311591E+07 | 0.00000 | CH A X R 0.00000 |
| 3504.5093  | 0.6155907E-05 | 14.27597 | 0 | 0.5 | 0 | e | 28540.78108 | 2 | 1.5 | 0 | e | 0.609882E+07 | 0.00000 | CH A X R 0.00000 |
| 3240.0300  | 0.1287390E-06 | 14.27597 | 0 | 0.5 | 0 | e | 30869.28429 | 3 | 1.5 | 0 | e | 0.142829E+07 | 0.00000 | CH A X R 0.00000 |
| 3034.9224  | 0.6833893E-08 | 14.27597 | 0 | 0.5 | 0 | e | 32954.46056 | 4 | 1.5 | 0 | e | 0.116662E+07 | 0.00000 | CH A X R 0.00000 |
| 2877.3544  | 0.1802274E-07 | 14.27597 | 0 | 0.5 | 0 | e | 34758.23015 | 5 | 1.5 | 0 | e | 0.898224E+06 | 0.00000 | CH A X R 0.00000 |
| 4872.9244  | 0.3025494E-03 | 2746.09918 | 1 | 0.5 | 1 | e | 23261.91647 | 0 | 1.5 | 1 | e | 0.328588E+07 | 0.01051 | CH A X R 0.01051 |
| 4299.4823  | 0.1028162E-01 | 2746.09918 | 1 | 0.5 | 1 | e | 25998.16801 | 1 | 1.5 | 1 | e | 0.311591E+07 | 0.00000 | CH A X R -0.03690 |
5. Conclusion

We have compiled the most up-to-date and extensive list of the main CH transitions observed in stellar spectra (rovibrational, A-X, B-X, and C-X). This list includes line positions as well as oscillator strengths and line broadening (radiative + predissociation). The combination of laboratory measurements and astronomical observations also allows the molecular data to be improved for this molecule. We have demonstrated that carefully selected stellar spectra can significantly improve molecular data despite their relatively poor quality compared to laboratory experiments or the solar spectrum. Although we were able to identify many new levels and we were able to assemble a large quantity of laboratory data, all levels of the CH molecules have not been identified. Therefore, the linelist we provide here is not complete, but is the most accurate existing for stellar spectroscopists. Other electronic transitions have been observed in some astrophysical contexts in the far UV (D-X, E-X, and F-X; Watson 2001, Sheffer & Federman 2007). Laboratory data for these transitions can be found concerning the line positions and constants in Li & Lec (1999) and Herzberg & Johns (1969) for the D state, Watson (2001) and Sheffer & Federman (2007) for E and F, while Kalamos et al. (1999) provide theoretical values for all of them. The corresponding transition moments have also been calculated in van Dishoeck (1987). The D and F states are also known to be highly predissociative (Herzberg & Johns 1969). Predissociation lifetimes for these states can be found in Metropolis & Mavrildis (2000). However, we did not include these transitions in our linelists because they are expected to be of minor importance for stellar spectra. We also highlight the fact that predissociation is not only known to exist in CH, but also in other molecules of astrophysical interest (NH, H₂O, etc...). (see Kato & Baba 1993.

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Appendix A: Atlas of predissociation lines

A.1. Predissociation lines in astronomical spectra

In the course of a study of carbon-enhanced metal-poor (CEMP) stars (Christlieb et al. 2002, Masseron 2006, Masseron et al. 2006, 2010, 2012), we came across wide and shallow lines spread in the wavelength ranges λ3660 – 3770 Å and λ3920 – 4130 Å (Fig. 3). Realising that these ranges matched those of the B-X system of the CH molecule, it soon became clear that these wide and shallow lines are in fact predissociation lines. It prompted the present work on the CH molecular linelist.

In molecules, different types of transitions may occur. If the energy provided to the molecule is higher than that needed to separate the atomic components, then dissociation occurs and no lines are formed. If both the upper and lower states of the transition are below the dissociation limit, the classical quantized transition occurs and a line forms. However, if a bound transition involves a level having a nearby unbound level, an internal conversion may occur, leaving the transition in the so-called predissociation state. Because the unbound level has a finite lifetime associated with the molecular dissociation, the lines associated with such transitions appear broadened beyond the natural broadening (Herzberg 1950) once the predissociation lifetime becomes shorter than the radiative lifetime. There are various situations leading to predissociation. The unbound level can be of the same or a different electronic state, but certain selection rules must be fulfilled (see Herzberg 1950). Furthermore, the predissociation may be internal to a molecule but can also be induced by external factors (e.g. magnetic fields).

For the CH molecule, predissociation is expected for the A, B, C, and D states. Predissociation was first observed in the laboratory by Shidle (1936) and confirmed by Herzberg & Johns (1969), and Ubachs et al. (1986) and studied theoretically in more detail by Elander & Smith (1973), Brooks & Smith (1974), Elander et al. (1976), and van Dishoeck (1987). For the A state, Brzozowski et al. (1976) noticed that the line structure disappears for energies below the dissociation limit, but reappears again at higher energies. They attribute this predissociation to perturbation of the X^2Σ ground state and from the B^2Σ^− state. Brzozowski et al. (1976) and Elander et al. (1979) show that the B-state has a potential barrier above the dissociation limit (see Fig. A1), so that its predissociation occurs by tunneling through the barrier by quasi-bound levels. Although a similar bump in the potential curve of the C state is observed, Brzozowski et al. (1976) and Elander & Smith (1973) first suspected the a^2Σ to be responsible for the perturbation of the C state leading to its predissociation. Nevertheless, more recent calculations of the C state by van Dishoeck (1987) and observations by Ubachs et al. (1986) show that the predissociation of the C state is instead due to interaction with the B state. Finally, van Dishoeck (1987) also predicted the D state to be entirely predissociated.

Although the predissociation phenomenon has been extensively observed in the laboratory, predissociation lines have rarely been identified in astronomical objects: NH₃ and NH₂ predissociation lines have been observed in Halley’s comet (Fink et al. 1992). Predissociation lines are often discussed in relation with diffuse interstellar bands (DIBs; see Herbig 1973, 1993; Fulara & Krelowski 2000). Hubble Space Telescope observations of Watson (2001) assign the ~ 1370 Å DIBs to the CH molecule. Later on, Sheffer & Federman (2007) confirmed this finding and extended it to the 1271, 1549, and 1694 Å DIBs. Carbon-rich stars present a large number of molecular features, and notably of CH, including predissociation lines. Because broadening in stellar spectra is large compared to laboratory spectra, only B-X predissociation lines are detectable. However, the thermodynamical conditions in their atmospheres allow us to observe a large number of those lines that we list in the following atlas.

A.2. Atlas

We present here an atlas of predissociation lines in carbon-rich stars (see Table A.1 for the stellar sample), the Sun, and Arcturus. The catalog (Figs. A.3 – A.10) clearly re-
veals the peculiar shapes that may be encountered in spectra, especially in carbon-rich stars where they are the most conspicuous, but also in normal stars like the Sun.

A.3. The Bond-Neff depression

In this section we evaluate the impact of the CH bands on low-resolution spectra and photometry, especially in the context of the Bond-Neff depression (Bond & Neff 1969) observed in barium stars (Bideman & Keenan 1951), which are G-K giants enriched in carbon and heavy elements predominantly produced in the s-process nucleosynthesis (see Käppeler et al. 2011 for a recent review).

Although the Bond-Neff depression was first assigned to CN and CH molecules, the depression was not satisfactorily accounted for with the old linelists. McWilliam & Smith (1984) therefore suggested a contribution from blanketing by heavy elements. By computing synthetic spectra for two among the barium stars originally considered by Bond & Neff (1969), we show in Fig. A.2 that there is now a very good agreement between predicted and observed colours, thanks to our complete molecular and atomic linelists. As demonstrated by this figure, both heavy-element and CH blanketing (including CH-predissociation lines) are necessary to reproduce the Bond-Neff depression.

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Table A.1. Stellar parameters of the stars presented in the Atlas.

| Star     | T$_{\text{eff}}$ | log(g) | [Fe/H] | [C/Fe] | reference          |
|----------|------------------|--------|--------|--------|--------------------|
| HD 187861| 4600             | 1.7    | -2.4   | 2.1    | Masseron et al. (2010) |
| CS 22942-019| 5100            | 2.5    | -2.5   | 2.2    | Masseron et al. (2010) |
| HE 1419-1324| 5600            | 3.2    | -2.1   | 1.2    | Masseron et al. (2010) |
| Arcturus  | 4300             | 1.5    | -0.5   | 0.0    | Decin et al. (2003)  |
| Sun       | 5777             | 4.44   | 0.0    | 0.0    |                    |

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Fig. A.3. Atlas of predissociation lines for a sample of stars. The black line shows the observations while the red line shows the synthetic fit with all atomic and molecular lines included, the blue line shows the synthetic fit without CH predissociation lines and the green line shows the contribution of the CH predissociation lines alone. We note that the continuum has been arbitrarily placed at 1.5 for the synthetic fit. See Table A.1 for a list of the basic properties of the displayed stars.
Fig. A.4. Atlas of predissociation lines (continued).
Fig. A.5. Atlas of predissociation lines (continued).
Fig. A.6. Atlas of predissociation lines (continued).
Fig. A.7. Atlas of predissociation lines (continued).
Fig. A.8. Atlas of predissociation lines (continued).
Fig. A.9. Atlas of predissociation lines (continued).
Fig. A.10. Atlas of predissociation lines (continued).
Table A.2. Vacuum wavenumbers (cm$^{-1}$) of clean CH A-X transitions in CS2942-019 used for the calculation of the constants. The numbers in parentheses are the observed - calculated value.

| J    | R11ff | R11ee | Q11ef | Q11fe | P11ee | P11ff |
|------|-------|-------|-------|-------|-------|-------|
| 0 - 0 |       |       |       |       |       |       |
| 27.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 28.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 29.5 | 24138.80(12) | ...   | ...   | ...   | ...   | ...   |
| 30.5 | 24159.33(22)  | 24134.84(41) | 23431.16(13) | ...   | ...   | ...   |
| 31.5 | 24151.75(54)  | 23437.20(23) | ...   | ...   | ...   | ...   |
| 32.5 | 24192.13(27)  | 24165.46(39) | ...   | ...   | ...   | ...   |
| 33.5 | 24203.43(-4)  | 24176.22(55) | ...   | ...   | ...   | ...   |
| 34.5 | 24210.99(-39) | 24180.89(-169)| ... | ... | ... | ... |
| 35.5 | ...   | ...   | 23438.52(-91) | ...   | ...   | ...   |
| 36.5 | ...   | ...   | ...   | ...   | 22625.61(-61) | ...   |
| 1 - 1 |       |       |       |       |       |       |
| 19.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 20.5 | 23785.15(-8) | 23772.25(-7) | ...   | ...   | 22740.01(-4) | 22752.95(-2) |
| 21.5 | 23807.80(-20) | 23793.92(-11) | ...   | ...   | 22723.58(95) | 22736.65(4)
| 22.5 | 23829.09(-6)  | 23813.93(-16) | ...   | ...   | 22705.20(4) | 22720.01(-22) |
| 23.5 | 23848.18(-23) | ...   | ...   | ...   | 22687.43(-9) | 22703.50(-17) |
| 24.5 | ...   | ...   | 23848.18(-13) | ...   | ...   | ...   |
| 25.5 | ...   | ...   | ...   | ...   | 22686.60(-16) | ...   |
| 26.5 | 23892.07(-9)  | 23872.79(0)   | ...   | ...   | 22631.70(0) | 22650.93(-17) |
| 27.5 | 23901.15(20)  | ...   | ...   | ...   | 22611.43(4) | 22631.70(-16) |
| 28.5 | 23906.07(-11) | 23884.99(31)  | ...   | ...   | 22611.43(14) | ...   |
| 29.5 | 23907.61(26)  | 23884.99(17)  | ...   | ...   | ...   | ...   |
| 30.5 | 23903.32(-62) | ...   | ...   | ...   | ...   | ...   |
| 31.5 | 23895.21(-14) | 23870.68(-14) | ...   | ...   | ...   | ...   |
| 32.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 2 - 2 |       |       |       |       |       |       |
| 11.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 12.5 | ...   | ...   | 23447.70(19) | ...   | ...   | ...   |
| 13.5 | 23475.29(69)  | 23468.95(19)  | ...   | 23118.09(25) | 22789.98(32) | 22795.65(14) |
| 14.5 | 23495.76(22)  | 23489.02(17)  | ...   | 23115.90(12) | ...   | ...   |
| 15.5 | 23515.43(22)  | 23507.69(5)   | ...   | 23113.07(5)  | ...   | ...   |
| J  | R22ff          | R22ee          | Q22ef          | Q22fe          | P22ff          | P22ee          |
|----|----------------|----------------|----------------|----------------|----------------|----------------|
| 10.5| 2353.36(40)   | ...            | 23118.09(20)  | 23109.49(6)   | 22714.95(14)  | 22723.58(28)  |
| 11.5| 23550.11(8)   | ...            | 23114.57(27)  | 23104.74(-12) | 22689.33(0)   | 22699.07(30)  |
| 12.5| 23554.16(-17) | ...            | 23109.49(-5)  | 23098.97(-16) | 22663.25(-14) | 22673.89(8)   |
| 13.5| 23577.21(-11) | ...            | 23103.51(5)   | ...            | 22636.67(-18) | 22648.31(5)   |
| 14.5| 23587.28(-20) | ...            | 23095.66(-15) | 23083.13(-26) | ...            | 22621.92(-4)  |
| 15.5| 23588.38(-28) | ...            | 23074.50(-21) | ...            | 22551.50(-17) | ...            |
| 16.5| 23588.38(-6)  | ...            | 23060.18(-41) | 23044.82(-23) | 22520.41(-20) | ...            |
| 17.5| 23550.11(28)  | ...            | 23042.04(-9)  | ...            | 22487.54(-16) | 22503.99(-29) |
| 18.5| 23554.16(-17) | ...            | 23013.51(-27) | 23005.42(-7)  | ...            | 22469.89(-26) |
| 19.5| 23577.21(-11) | ...            | 23003.13(-26) | ...            | 22393.07(-22) | ...            |
| 20.5| 23587.28(-20) | ...            | 22987.70(-2)  | ...            | 22329.17(55)  | 22350.97(13)  |
| 21.5| ...            | ...            | ...            | ...            | 22279.51(42)  | 22300.93(15)  |
| 22.5| ...            | ...            | ...            | ...            | ...            | 22246.69(-12) |
| 23.5| ...            | ...            | ...            | ...            | 22162.46(-36) | 22185.77(-66) |
| 24.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 25.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 26.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 27.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 28.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 29.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 30.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 31.5| ...            | ...            | ...            | ...            | ...            | ...            |

| J  | R11ff          | R11ee          | Q11ef          | Q11fe          | P11ee          | P11ff          |
|----|----------------|----------------|----------------|----------------|----------------|----------------|
| 11.5| 23430.28(-19) | ...            | ...            | ...            | ...            | ...            |
| 12.5| 23447.70(-20) | ...            | ...            | ...            | ...            | ...            |
| 13.5| 23468.95(-3)  | ...            | 23118.09(-2)   | 23118.09(-16) | 22714.95(24)  | ...            |
| 14.5| 23489.02(10)  | ...            | 23115.90(0)   | ...            | 22699.07(1)   | 22689.33(21)  |
| 15.5| 23507.69(10)  | ...            | 23113.07(6)   | ...            | 22648.31(-9)  | 22636.52(8)   |
| 16.5| 23533.64(-10) | ...            | 23109.49(20)  | 23118.09(-16) | 22733.58(-10)| 22714.95(24)  |
| 17.5| 23550.11(-14) | ...            | 23104.74(13)  | 23114.57(2)   | 22699.07(1)   | 22689.33(21)  |
| 18.5| 23553.94(-1)  | ...            | 23098.97(19)  | 23109.49(-23) | 22673.53(-49) | 22663.25(17)  |
| 19.5| 23574.43(-8)  | ...            | 23082.71(-16) | 23095.66(-20) | 22621.92(-11)| 22609.03(0)   |
| 20.5| 23580.82(1)   | ...            | 23072.16(-13) | 23074.62(-12) | 22519.70(-12)| ...            |
| 21.5| 23583.61(-38) | ...            | 23059.28(-28) | 23074.50(-17) | 22550.79(-24)| ...            |
| 22.5| 23583.61(1)   | ...            | 23060.18(-32) | ...            | 22519.70(-20)| ...            |
| 23.5| ...            | ...            | ...            | ...            | 22503.99(-18) | 22486.62(-31) |
| 24.5| ...            | ...            | ...            | ...            | 22469.89(-13) | ...            |
| 25.5| ...            | ...            | ...            | ...            | 22327.83(10)  | ...            |
| 26.5| ...            | ...            | ...            | ...            | 22246.69(6)   | ...            |
| 27.5| ...            | ...            | ...            | ...            | 22185.77(-50) | 22161.57(-31) |
| 28.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 29.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 30.5| ...            | ...            | ...            | ...            | ...            | ...            |
| 31.5| ...            | ...            | ...            | ...            | ...            | ...            |

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| J   | R111f | R11ee | Q11f | Q11e | P11ee | P11ff |
|-----|-------|-------|------|------|-------|-------|
| 2.5 | 22766.84(5) | 22766.84(18) | ... | ... | ... | ... |
| 3.5 | ... | 22694.84(-16) | 22694.84(15) | ... | ... | ... |
| 4.5 | ... | ... | ... | ... | ... | ... |
| 5.5 | ... | 22684.18(5) | 22569.68(8) | ... | ... | ... |
| 6.5 | ... | ... | ... | ... | ... | ... |
| 7.5 | ... | 22666.75(-13) | 22665.00(-21) | ... | ... | ... |
| 8.5 | ... | 22655.60(-5) | 22653.55(6) | ... | ... | ... |
| 9.5 | ... | 22860.44(-16) | 22642.52(2) | 22639.65(-15) | ... | ... |
| 10.5 | ... | 22627.20(-7) | 22623.97(0) | ... | ... | ... |
| 11.5 | ... | ... | 22605.91(10) | ... | ... | ... |
| 12.5 | ... | ... | 22584.83(31) | ... | ... | ... |
| 13.5 | ... | ... | 22561.78(15) | ... | ... | ... |
| 14.5 | ... | ... | 22535.23(19) | ... | ... | ... |
| 15.5 | ... | 22512.25(28) | 22504.95(-6) | 22197.44(39) | ... | ... |
| 16.5 | ... | 22817.87(-15) | 22471.01(-9) | 22139.68(1) | ... | ... |
| 17.5 | ... | ... | 22432.69(-11) | ... | 22094.67(12) | ... |
| 18.5 | ... | 22399.01(-3) | 22389.38(-9) | 22027.97(-22) | 22037.83(6) | ... |
| 19.5 | ... | 22350.69(-17) | 22339.95(-42) | ... | ... | ... |
| 20.5 | ... | 22295.81(-16) | 22284.43(-13) | ... | ... | ... |
| 21.5 | ... | 22233.08(-13) | 22220.88(1) | ... | ... | ... |
| 22.5 | ... | 22161.33(13) | ... | ... | ... | ... |
| 23.5 | ... | 22078.47(29) | ... | ... | ... | ... |

| J   | R22ff | R22ee | Q22f | Q22e | P22ff | P22ee |
|-----|-------|-------|------|------|-------|-------|
| 2.5 | ... | ... | ... | ... | ... | ... |
| 3.5 | ... | ... | 22693.20(21) | 22693.66(-2) | ... | ... |
| 4.5 | ... | ... | 22685.83(9) | ... | ... | ... |
| 5.5 | ... | ... | 22678.37(-11) | ... | ... | ... |
| 6.5 | ... | ... | 22666.75(-3) | 22668.65(-1) | ... | ... |
| 7.5 | ... | ... | 22654.78(4) | ... | 22043.80(5) | ... |
| 8.5 | ... | ... | ... | ... | ... | ... |
| 9.5 | ... | ... | 22624.58(-14) | 22628.27(-5) | ... | ... |
| 10.5 | ... | ... | 22606.01(-37) | ... | ... | ... |
| 11.5 | ... | ... | 22585.43(-8) | ... | ... | ... |
| 12.5 | ... | ... | 22561.78(-8) | ... | ... | ... |
| 13.5 | ... | ... | 22535.23(10) | ... | ... | ... |
| 14.5 | ... | ... | 22504.95(-2) | 22512.25(-10) | ... | 22190.20(9) |
| 15.5 | ... | 22817.87(5) | 22471.01(7) | 22479.09(-9) | ... | 22139.68(12) |
| 16.5 | ... | ... | 22432.69(16) | ... | 22094.67(-12) | ... |
| 17.5 | ... | ... | 22389.38(-3) | 22399.01(-14) | 22037.83(-9) | 22027.97(11) |
| 18.5 | ... | ... | 22339.95(-42) | ... | ... | ... |
| 19.5 | ... | ... | 22295.81(-13) | ... | ... | ... |
| 20.5 | ... | ... | 22233.08(-13) | ... | ... | ... |
| 21.5 | ... | ... | 22161.33(30) | ... | ... | ... |
| 22.5 | ... | ... | 22078.47(51) | ... | ... | ... |
| 23.5 | ... | ... | ... | ... | ... | ... |

| J   | R11ff | R11ee | Q11f | Q11e | P11ee | P11ff |
|-----|-------|-------|------|------|-------|-------|
| 2.5 | 22830.87(-17) | 22330.87(-4) | ... | ... | ... | ... |
| 3.5 | 22344.29(-20) | 22344.29(10) | 22261.95(-38) | 22261.95(-8) | ... | ... |
| 4.5 | 22354.89(0) | 22354.24(-11) | 22252.58(-9) | 22252.58(45) | ... | ... |

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5 - 5
\begin{table}[h]
\centering
\begin{tabular}{cccccc}
\hline
\textbf{J} & \textbf{R11ff} & \textbf{R11ee} & \textbf{Q11ef} & \textbf{Q11fe} & \textbf{P11ee} & \textbf{P11ff} \\
\hline
0.5 & ... & ... & ... & ... & ... & ... \\
1.5 & ... & ... & ... & ... & ... & ... \\
2.5 & ... & ... & ... & ... & ... & ... \\
3.5 & ... & ... & ... & ... & ... & ... \\
4.5 & ... & ... & ... & ... & ... & ... \\
5.5 & ... & ... & ... & ... & ... & ... \\
6.5 & ... & ... & ... & ... & ... & ... \\
7.5 & ... & ... & ... & ... & ... & ... \\
8.5 & 25818.70 (-2) & ... & ... & ... & ... & ... \\
9.5 & 25811.97 (5) & ... & ... & ... & ... & ... \\
10.5 & 25800.62 (0) & ... & ... & ... & ... & ... \\
11.5 & 25784.50 (-3) & ... & ... & ... & ... & ... \\
12.5 & 25763.17 (-16) & ... & ... & 25448.78 (-9) & ... & ... \\
13.5 & 25736.64 (4) & ... & ... & 25401.09 (0) & ... & ... \\
14.5 & 25703.89 (2) & ... & ... & 25348.17 (0) & ... & ... \\
15.5 & 25664.56 (3) & ... & ... & ... & ... & ... \\
16.5 & 25617.93 (11) & ... & ... & 25225.06 (8) & ... & ... \\
17.5 & 25562.84 (9) & ... & ... & 25153.60 (19) & ... & ... \\
18.5 & ... & ... & ... & 25074.30 (32) & ... & ... \\
19.5 & 25422.37 (58) & ... & ... & 24985.75 (36) & ... & ... \\
20.5 & 25331.48 (-27) & ... & ... & 24886.24 (33) & ... & ... \\
21.5 & 25226.27 (161) & ... & ... & 24773.20 (2) & ... & ... \\
22.5 & ... & ... & ... & ... & 24222.96 (14) & ... \\
\hline
\end{tabular}
\caption{Vacuum wavenumbers (cm\textsuperscript{-1}) of clean CH B-X transitions in CS 22942-019 used for the calculation of the constants. The numbers in parentheses are the observed minus calculated value. The numbers in italics are predissociation lines where the accuracy of the position is low.}
\end{table}
| J  | R11ff | R11ee | Q11ef | Q11fe | P11ee | P11ff |
|----|-------|-------|-------|-------|-------|-------|
| 0  |       |       |       |       |       |       |
| 1  |       |       |       |       |       |       |

| J  | R22ff | R22ee | Q22ef | Q22fe | P22ff | P22ee |
|----|-------|-------|-------|-------|-------|-------|
| 0  |       |       |       |       |       |       |
| 1  |       |       |       |       |       |       |

| J  | R11ff | R11ee | Q11ef | Q11fe | P11ee | P11ff |
|----|-------|-------|-------|-------|-------|-------|
| 1  |       |       |       |       |       |       |
| 2  |       |       |       |       |       |       |
Table A.4. Vacuum wavenumbers (cm$^{-1}$) of clean CH C-X transitions in our stellar spectra used for the calculation of the constants. The numbers in parentheses are the observed minus calculated value.

| J   | R11ff | R11ee | Q11ef | Q11fe | P11ee   | P11ff   |
|-----|-------|-------|-------|-------|---------|---------|
| 7.5 | ...   | ...   | ...   | ...   | ...     | ...     |
| 9.5 | ...   | ...   | 31381.79(24) | ...   | ...     | 31192.72(21) |
| 10.5| ...   | ...   | 31369.38(56) | ...   | 31121.54(30) |
| 11.5| ...   | ...   | ...     | ...   | 31083.62(21) |
| 12.5| ...   | ...   | ...     | ...   | 31043.85(1) |
| 13.5| ...   | 31317.60(20) | ...   | ...     | 31002.36(2) |
| 14.5| ...   | ...   | 31294.66(-11) | ...   | ...     |
| 15.5| 31628.30(-11) | ...   | ...   | ...     |
| 16.5| ...   | 31614.50(-26) | ...   | ...     |

| J   | R22ff | R22ee | Q22ef | Q22fe | P22ff   | P22ee   |
|-----|-------|-------|-------|-------|---------|---------|
| 7.5 | ...   | ...   | ...   | ...   | ...     | ...     |
| 8.5 | ...   | ...   | 31382.58(10) | ...   | ...     | 31193.40(-3) |
| 9.5 | ...   | ...   | 31369.38(-19) | ...   | 31121.54(-17) |
| 10.5| ...   | ...   | ...     | ...   | 31083.62(-7) |
| 11.5| ...   | ...   | ...     | ...   | 31043.85(-11) |
| 12.5| ...   | 31317.60(-13) | ...   | ...     | 31002.36(6) |
| 13.5| ...   | 31294.66(-33) | ...   | ...     |
| 14.5| 31628.30(27) | ...   | ...   | ...     |
| 15.5| 31614.50(24) | ...   | ...   | ...     |
| 16.5| ...   | ...   | ...     | ...   |

| J   | R11ff | R11ee | Q11ef | Q11fe | P11ee   | P11ff   |
|-----|-------|-------|-------|-------|---------|---------|
| 7.5 | ...   | ...   | ...   | ...   | ...     | ...     |
| 8.5 | 24775.47(2) | ...   | ...   | ...     | ...     |
| 9.5 | ...   | ...   | 24531.08(6) | ...   | 24413.37(3) |
| 10.5| 24700.85(14) | ...   | ...   | 24471.76(-3) | ...   | 24266.94(-1) |
| 11.5| 24648.17(-1) | ...   | ...   | 24403.60(-7) | ...   | 24182.83(-12) |
| 12.5| 24585.56(240) | ...   | ...   | 24325.46(17) | ...   | 24090.70(22) |
| 13.5| ...   | ...   | ...     | ...   | 24237.35(261) |
| 14.5| ...   | ...   | ...     | ...   |

| J   | R22ff | R22ee | Q22ef | Q22fe | P22ff   | P22ee   |
|-----|-------|-------|-------|-------|---------|---------|
| 7.5 | ...   | ...   | ...   | ...   | ...     | ...     |
| 8.5 | ...   | ...   | 24532.29(1) | ...   | 24415.04(1) |
| 9.5 | ...   | ...   | 24472.84(4) | ...   | 24268.36(1) |
| 10.5| 24648.17(-135) | ...   | ...   | 24404.61(-2) |
| 11.5| 24585.56(114) | ...   | ...   | 24325.46(-68) |
| 12.5| ...   | ...   | 24237.35(186) |
| 13.5| ...   | ...   | ...     | ...   |

| J   | R11ff | R11ee | Q11ef | Q11fe | P11ee   | P11ff   |
|-----|-------|-------|-------|-------|---------|---------|
| 7.5 | ...   | ...   | ...   | ...   | ...     | ...     |
| 8.5 | ...   | ...   | ...   | ...   | ...     | ...     |
| 9.5 | ...   | ...   | 24472.84(4) | ...   | ...     |
| 10.5| ...   | 24404.61(-2) | ...   | ...     |
| 11.5| 24325.46(-68) | ...   | ...   | ...     |
| 12.5| ...   | 24237.35(186) |
| 13.5| ...   | ...   | ...     | ...   | 26495.18(-282) |

Table B.1. Vacuum wavenumbers (cm$^{-1}$) of clean CH C-X transitions in our stellar spectra used for the calculation of the constants. The numbers in parentheses are the observed minus calculated value.
Table A.5. Vacuum wavenumbers (cm$^{-1}$) of clean CH A-X transitions of $^{13}$CH in our stellar spectra used for the calculation of the constants. The numbers in parentheses are the observed minus calculated value.

| J   | R11ff | R11ee | Q11ef | Q11fe | P11ee | P11ff |
|-----|-------|-------|-------|-------|-------|-------|
| 18.5| ...   | ...   | ...   | ...   | ...   | ...   |
| 19.5| 23758.86(-3) | ... | ... | ... | ... | ... |
| 20.5| 23783.00(-11) | ... | ... | ... | ... | ... |
| 21.5| 23805.71(-21)| ... | ... | ... | ... | ... |
| 22.5| 23826.87(-28)| ... | ... | ... | ... | ... |
| 23.5| 23846.14(-42)| ... | ... | ... | ... | ... |
| 24.5| 23863.38(-51)| ... | ... | ... | ... | ... |
| 25.5| ... | ... | ... | ... | ... | ... |
| 26.5| 23890.58(-65)| ... | ... | ... | ... | ... |

Table A.6. Vacuum wavenumbers (cm$^{-1}$) of clean CH B-X transitions of $^{13}$CH in our stellar spectra used for the calculation of the constants. The numbers in parentheses are the observed minus calculated value. The numbers in italic are predissociation lines where the accuracy of the position is low.

| J   | R11ff | R11ee | Q11ef | Q11fe | P11ee | P11ff |
|-----|-------|-------|-------|-------|-------|-------|
| 16.5| ...   | ...   | ...   | ...   | ...   | ...   |
| 17.5| ...   | ...   | ...   | ...   | ...   | ...   |
| 18.5| 25498.69(-384) | ... | ... | ... | ... | ... |
| 19.5| ... | ... | ... | ... | ... | 24593.72(-26) |
| 20.5| ... | ... | ... | ... | ... | ... |
| 15.5| ... | ... | ... | ... | ... | 24485.60(19) |
| 16.5| ... | ... | ... | ... | ... | ... |
| 17.5| ... | ... | ... | ... | ... | ... |
| 18.5| ... | ... | 24992.81(1) | ... | ... | 24594.69(-20) |
| 19.5| ... | ... | ... | ... | ... | ... |
| 20.5| ... | ... | ... | ... | ... | ... |

| J   | R11ff | R11ee | Q11ef | Q11fe | P11ee | P11ff |
|-----|-------|-------|-------|-------|-------|-------|
| 6.5 | 27525.72(12) | ... | ... | ... | ... | ... |
| 7.5 | 27501.19(12) | ... | ... | ... | ... | ... |
| 8.5 | ... | ... | ... | 27276.39(23) | ... | ... |
| 9.5 | ... | ... | ... | 27216.02(31) | ... | ... |
| 10.5| ... | ... | ... | ... | ... | ... |
| 11.5| ... | ... | ... | 27067.69(23) | ... | ... |
| 12.5| ... | ... | ... | 26975.59(-203) | ... | ... |
| 6.5 | ... | ... | ... | ... | ... | ... |
| 7.5 | ... | ... | ... | ... | ... | ... |
| 8.5 | ... | ... | ... | ... | ... | ... |
| 9.5 | ... | ... | ... | ... | ... | ... |
| 10.5| ... | ... | ... | 27067.69(-76) | ... | ... |
| 11.5| ... | ... | ... | 26975.59(-290) | ... | ... |
Table A.7. Vacuum wavenumbers (cm$^{-1}$) of clean CH C-X transitions of $^{13}$CH in our stellar spectra used for the calculation of the constants. The numbers in parentheses are the observed minus calculated value.

| J  | R11ff | R11ee | 0 - 0 | Q11ef | Q11fe | P11ee | P11ff |
|----|-------|-------|-------|-------|-------|-------|-------|
| 15.5 | ...   | 32223.03(9) | ...   | ...   | ...   | ...   | ...   |
| 16.5 | ...   | ...   | ...   | 31365.64(-25) | ...   | ...   | ...   |
| 17.5 | ...   | 3266.81(-2) | ...   | 31341.06(-23) | ...   | ...   | ...   |
| 18.5 | ...   | ...   | ...   | ...   | ...   | ...   | ...   |
| 19.5 | ...   | ...   | ...   | ...   | ...   | ...   | ...   |
| 20.5 | ...   | ...   | ...   | 31266.86(-95) | ...   | ...   | ...   |

| J  | R21ff | R21ee | Q21ef | Q21fe | P21ee | P21ff |
|----|-------|-------|-------|-------|-------|-------|
| 14.5 | 32223.03(49) | ...   | ...   | ...   | ...   | ...   |
| 15.5 | ...   | ...   | ...   | 31365.64(20) | ...   | ...   | ...   |
| 16.5 | 3266.81(64) | ...   | ...   | 31341.06(34) | ...   | ...   | ...   |
| 17.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 18.5 | ...   | ...   | ...   | ...   | ...   | ...   |
| 19.5 | ...   | ...   | ...   | ...   | 31266.86(-4) | ...   | ...   |
| 20.5 | ...   | ...   | ...   | ...   | ...   | ...   |