Formation of Polar Terrestrial Circumbinary Planets

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Abstract

All circumbinary planets (CBPs) currently detected are in orbits that are almost coplanar to the binary orbit. While misaligned CBPs are more difficult to detect, observations of polar-aligned circumbinary gas and debris disks around eccentric binaries suggest that polar planet formation may be possible. A polar-aligned planet has a stable orbit that is inclined by 90° to the orbital plane of the binary with an angular momentum vector that is aligned to the binary eccentricity vector. With $n$-body simulations we model polar terrestrial planet formation using hydrodynamic gas disk simulations to motivate the initial particle distribution. Terrestrial planet formation around an eccentric binary is more likely in a polar alignment than in a coplanar alignment. Similar planetary systems form in a polar alignment around an eccentric binary and a coplanar alignment around a circular binary. The polar planetary systems are stable even with the effects of general relativity. Planetary orbits around an eccentric binary exhibit tilt and eccentricity oscillations at all inclinations; however, the oscillations are larger in the coplanar case than the polar case. We suggest that polar-aligned terrestrial planets will be found in the future.

Unified Astronomy Thesaurus concepts: Binary stars (154); Solar system terrestrial planets (797); Extrasolar rocky planets (511); Exoplanet formation (492)

1. Introduction

Planetesimals, the building blocks for circumbinary planets (CBPs), form initially with the orbital properties of the circumbinary gas disk from which they form. There are two stable stationary inclinations for a circumbinary gas disk around an eccentric binary: coplanar to the binary orbit and polar aligned to the binary orbit. A low-mass circumbinary gas disk that is in a polar alignment is inclined by 90° with respect to the orbital plane of the binary with the angular momentum vector of the disk aligned to the binary eccentricity vector (see Figure 1 for an example). A disk that is misaligned evolves toward one of these states depending upon its initial inclination (Aly et al. 2015; Martin & Lubow 2017, 2018; Zanazzi & Lai 2018). Circumbinary disks may be misaligned through turbulence in the molecular cloud that leads to chaotic accretion (Bate et al. 2010) or the effect of a companion star in the form of a binary or a stellar flyby (Nealon et al. 2020). A polar circumbinary gas disk has been observed around HD 98800 B (Kennedy et al. 2019), and a polar circumbinary debris disk has been observed around 99 Herculis (Kennedy et al. 2012; Smallwood et al. 2020). While no planets have been observed around these systems, both of these disks exhibit features indicative of ongoing planet formation.

Successful planet-observing campaigns by the Kepler and TESS space telescopes have cumulatively revealed more than a dozen CBPs (e.g., Doyle et al. 2011; Orosz et al. 2012; Kostov et al. 2020), but no highly misaligned or polar CBPs have yet been observed. The coplanar alignment of observed CBPs is likely a consequence of observational bias and not representative of the underlying population (Czekala et al. 2019; Martin 2019). CBPs, especially polar CBPs, are difficult to observe due to the long orbital periods of the planets and complex spectra of the stars (Eggenberger & Udry 2007; Wright et al. 2012; Martin & Triaud 2014). Detection of polar CBPs may be possible with eclipse timing variations (Zhang & Fabrycky 2019; Martin & Fabrycky 2021). However, a coplanar CBP has been found around a highly eccentric binary. Kepler-34b orbits a binary with an eccentricity of $e_b = 0.5$ (Welsh et al. 2012).

Simulations of circumbinary terrestrial planet formation have previously considered only coplanar or slightly misaligned initial configurations (e.g., Quintana & Lissauer 2006; Childs & Martin 2021). In this Letter, for the first time, we study the late stages of CBP formation in a polar-aligned circumbinary disk around an eccentric binary. We aim to understand how the efficiency of terrestrial planet formation in a polar alignment compares with the coplanar case in order to make predictions about planet properties for the so far unobserved polar CBPs. We use hydrodynamic circumbinary gas disk simulations to motivate the initial distribution of particles for our $n$-body simulations of terrestrial planet formation. In Section 2 we discuss the setup of our smoothed particle hydrodynamic (SPH) and $n$-body simulations. In Section 3 we present our results, and in Section 4 we summarize our findings.

2. Simulations

The surface density profile for a circumbinary gas disk is highly dependent on the binary eccentricity (Artymowicz & Lubow 1994, 1996; Miranda & Lai 2015) and inclination (Lubow et al. 2015; Franchini et al. 2019). The gap-opening Lindblad resonances are weaker around a tilted circumbinary disk and so the disk can extend closer to the binary (Lubow & Martin 2018). We set up our $n$-body simulations with a surface density profile based on our SPH gas disk simulations. There exists a phase where the disk transitions from being gas dominated to the late stage of planet formation that is dominated by self-gravity of the solid bodies. If the planets grow quickly, while the gas disk is still present, the planet–disk interactions in the gas can alter the distribution of the solid bodies embedded in the gas disk. However, if stable gas is able to grow and harbor only relatively small solid bodies and then dissipate on a short timescale, the gas profile is a good proxy for the initial location of the particles in our $n$-body
simulations. In this section we describe our SPH and n-body setups and the methods used in our simulations.

2.1. Hydrodynamic Circumbinary Gas Disk Simulations

We consider three simulations of a circumbinary gas disk around an equal-mass binary \((M_1 = M_2 = 0.5M)\) where \(M\) is the total mass of the binary) and fix the binary separation at \(a_b = 0.5\) au. We already presented the coplanar cases in Childs & Martin (2021, hereafter CM21), but we show them again here for comparison with the polar case. We vary the binary eccentricity \(e_b\) and binary inclination \(i_b\) for each simulation as described in Table 1. We use the PHANTOM SPH code (Price & Federrath 2010; Price et al. 2018) that has been used extensively for circumbinary disks (e.g., Nixon 2012; Smallwood et al. 2019; Aly & Lodato 2020). The first SPH simulation is for a circular-coplanar binary (CC) with \(e_b = 0.0\), \(i_b = 0^{°}\). The second simulation is for an eccentric-coplanar binary (EC) with \(e_b = 0.8\), \(i_b = 0^{°}\), and the last simulation is for an eccentric-polar binary (EP) with \(e_b = 0.8\), \(i_b = 90^{°}\).

Since we are interested only in the surface density profile for the disk and the mass scaling is arbitrary, we do not add material to the disk over time. We take a small disk mass of \(M_d = 0.001\) \(M\) initially. In each case, the disk surface density is initially a power law with radius \((\Sigma \propto R^{-3/2})\) between inner radius \(R_{in} = 6\) \(a_b\) and outer radius \(R_{out} = 10\) \(a_b\). The Shakura & Sunyaev (1973) viscosity parameter is set to \(\alpha = 0.01\). The viscosity is implemented by adapting the SPH artificial viscosity according to Lodato & Price (2010). The disk is locally isothermal with sound speed \(c_s \propto R^{-3/4}\) and the disk aspect ratio varies weakly with radius as \(H/R \propto R^{-1/4}\). This is chosen so that \(\alpha\) and the smoothing length \(\langle h \rangle / H\) are constant with radius (Lodato & Pringle 2007). Each simulation contains 500,000 SPH particles initially. The stars are treated as sink particles with accretion radii of \(0.25 a_b\). The mass and angular momentum of any SPH particle that passes inside the accretion radius is added to the star. The rapid flow of material inside the binary cavity is not well resolved in our simulations. However, because of the low disk mass, the effect of accretion on the binary orbit is negligible during the simulation. Since we do not try to resolve the flow in this region, we use a sink particle size that is larger than the size of a star in order to speed up the computational time. We do not include the effects of self-gravity in our calculations.

The surface density profiles for the three SPH simulations are shown in the solid lines in Figure 2 at a time of \(1000\) \(P_{orb}\), where \(P_{orb}\) is the orbital period of the binary. In Figure 2 we also show a double Gaussian analytic fit to each profile in the dashed lines.

| Model | \(a_b/\text{au}\) | \(e_b\) | \(i_b^{°}\) | No. of Planets | \(M_p/M_\oplus\) | \(a_p/\text{au}\) | \(e\) | \(i^{°}\) | \(M_d/M_\oplus\) |
|-------|----------------|--------|-----------|-------------|-------------|-------------|-------|--------|-------------|
| EP    | 0.5            | 0.8    | 90.0      | 4.8 ± 0.8   | 0.95 ± 0.61 | 2.80 ± 0.96 | 0.05 ± 0.03 | 89.99 ± 1.02 | 4.62 ± 0.04  |
| EPGR  | 0.5            | 0.8    | 90.0      | 4.6 ± 0.8   | 0.98 ± 0.63 | 2.77 ± 0.96 | 0.05 ± 0.03 | 89.96 ± 0.93 | 4.62 ± 0.04  |
| CC    | 0.5            | 0.0    | 0.0       | 5.1 ± 1.28  | 0.89 ± 0.58 | 2.76 ± 0.88 | 0.04 ± 0.03 | 0.96 ± 0.66  | 4.71 ± 0.01  |
| EC    | 0.5            | 0.8    | 0.0       | 3.4 ± 1.03  | 1.22 ± 0.67 | 3.21 ± 0.79 | 0.06 ± 0.04 | 2.63 ± 2.27  | 4.19 ± 0.27  |

**Table 1**

**Final System Statistics**

Note. Average values and standard deviations for the terrestrial planet multiplicity and planet mass \((M_p)\), semimajor axis \((a_p)\), eccentricity \((e)\) and inclination \((i)\) after 7 Myr of integration time for all models except the EPGR model that shows the final systems of the EP model after being integrated an additional Myr with the effects of GR. These statistics only consider bodies with a mass larger or equal to 0.1 \(M_\oplus\). We also list the binary separation and inclination, and the average total disk material, \(M_d\) that remains at the end of the simulation for each model.
We expect the late stage of terrestrial planet formation to take place inside of the snow line radius, where water is in a gaseous form (e.g., Lecar et al. 2006; Martin & Livio 2012). For consistency with previous work on terrestrial planet formation, we set the outer edge of our disk fits to be $R = 4 \, a_p$ (Quintana & Lissauer 2014; Quintana et al. 2016; Childs et al. 2019). This is equivalent to $R = 8 \, a_p$ for a binary separation of 0.5 au. The outer truncation radius for the planetesimal disk restricts the radial range where terrestrial planets may form and prevents their formation around binaries with wider orbits (e.g., Clanton 2013).

2.2. n-body Simulations

Our $n$-body simulations model the late stages of planet formation after the gas disk has completely dissipated and Moon-sized planetesimals and Mars-sized embryos interact with one another through purely gravitational interactions (Kokubo & Ida 1996; Chambers 2001). We use the $n$-body code REBOUND (Rein & Liu 2012) with the symplectic integrator IAS15 (Rein & Spiegel 2015). IAS15 utilizes an adaptive time step, and we set an initial time step of about 2% of the binary. We assume perfectly inelastic collisions. We remove particles from the simulation at the time they exceed a distance of 100 au from the binary’s center of mass.

We consider the same binary parameters described in the previous section and listed in the first four columns of Table 1. The coplanar models were discussed in CM21, but we show them here for comparison to the polar case. For the EP models the binary is initialized with a 90° inclination, longitude of ascending node, and argument of pericenter so that the angular momentum of the disk is aligned to the binary eccentricity vector, as shown in Figure 1. For the coplanar models CC and EC, the binary orbital plane and gas and particle disks begin close to coplanar and we consider a circular ($e_b = 0.0$) and highly eccentric ($e_b = 0.8$) binary, respectively. Each star has a radius of 0.001 au.

The particle disk we use for our $n$-body studies is adopted from Quintana & Lissauer (2014), which is based on the disk used in Chambers (2001) to model the solar system. To generate the initial particle disk surface profile we use the double Gaussian analytic fits to the results from the SPH simulations described in Section 2.1 (see Figure 2). We then uniformly distribute 26 Mars-sized embryos ($m = 0.093 \, M_\oplus$) and 260 Moon-sized planetesimals ($m = 0.0093 \, M_\oplus$) along the fits between 1.5 $a_p$ and 4.0 au. The total mass of the planetesimals and embryos is 4.85 $M_\oplus$.

This bimodal mass distribution reproduces the correct number of terrestrial planets in solar system studies. The larger embryos experience dynamical damping by the smaller more numerous planetesimals that allows the bodies to grow more efficiently than in the case of a uniform mass distribution, and more extended mass distributions lead to an excess of terrestrial planets. Body eccentricities are uniformly distributed in the range (0.0,0.01). All bodies begin on nearly coplanar orbits with inclinations uniformly distributed between (0°, 1°). For the polar EP model, the binary is inclined by 90° meaning that the disk particles have an initial inclination between (89°, 90°) relative to the binary orbit.

The longitude of ascending node, argument of pericenter, and true anomaly are uniformly distributed between 0° and 360°. All bodies, excluding the stars, are given an initial density of 3 g cm$^{-3}$. All bodies are spherical, and we set the radii adopting a uniform density.

We perform 50 runs for each setup, and all runs begin with the same initial conditions for a given model; however, we change the random seed generator used for the orbital elements of the planetesimals and embryos in each run.

Because IAS15 is a high-accuracy integrator, in order to reduce computation time we apply an expansion factor to the particle radii of the planetesimals and embryos of $f = 25$ (see CM21 for convergence tests). Expansion factors do not have a significant effect on the evolution of planets other than reducing the timescale of planet formation Kokubo & Ida (1996, 2002). We run our simulations for a time of 7 Myr. Although terrestrial planet formation takes place over hundreds of millions of years, the effective timescale of planet formation, $t'$, scales with the simulation time by a factor of $f^{-2.5}$ in the absence of short range forces and when perfect merging is used (CM21). While a lower expansion factor produces more faithful simulations we maintain $f = 25$ in order to make direct comparisons to previous literature.

We analyze the orbits of the bodies in the frame of the binary orbit by following the methods of Chen et al. (2019). The binary reference frame is defined by the three axes, $e_p, b_p \times b_s$, and $b_s$, where $e_b$ is the instantaneous eccentricity vector of the binary, and $b_s$ is the instantaneous angular momentum vector of the binary. The inclination of a particle orbit relative to the binary angular momentum vector is

$$i = \cos^{-1}(\hat{b}_s \cdot \hat{b}_p),$$

(1)

where $\hat{b}_s$ is the instantaneous angular momentum vector of the particle and $\cdot$ denotes a unit vector.

General relativity (GR) causes the eccentric binary to precess on a timescale of about 2 Myr (Naoz et al. 2017; Zanardi et al. 2018). We integrate the final systems from the EP runs for an additional Myr using the “gr_full” module from REBOUNDx (Tamayo et al. 2020), which models the relativistic effects on all bodies, to test the effect of GR on the polar terrestrial systems. We refer to these extended runs as the EPGR model.

3. Results

In all systems, the stellar collision rate is relatively low compared to the ejection rate (in agreement with Smullen et al. 2016). Within the first 500 yr, 45 planetesimals collide with a star in the CC systems, and 44 planetesimals and 8 embryos collide with a star in the EC systems. Bodies never collide with

![Figure 2. Surface density scaled to the total disk mass of the SPH simulations for a circular-coplanar (CC), eccentric-coplanar (EC), and eccentric-polar (EP) binary. The SPH data are shown with a solid line, and the analytic fits are shown with a dashed line.](image-url)
stars in the polar alignment. A polar-inclined binary provides a near-axisymmetric potential in the plane of the circumbinary disk that leads to a weaker perpendicular torque experienced by the disk than in the coplanar case (for a fixed radius). A circular-coplanar binary exerts a weaker torque than an eccentric-coplanar binary. The larger the torque from the central binary, the more disk mass that is ejected. On average, a CC system ejects 2% of its particle disk mass, an EC system ejects 13% of its particle disk mass, and an EP system ejects 4% of its particle disk mass. Table 1 lists the average total disk material, $M_d$, that remains at the end of the simulation for each binary model. We observe the largest mass loss in the EC system and the EP and CC maintain similar amounts of material.

Table 1 lists the average values of the planet multiplicity, mass, semimajor axis, eccentricity, and inclination between all 50 runs at 8 Myr for the EPGR model and at 7 Myr for the rest of the models. In the table we only consider bodies with a mass greater than $0.1\ M_\oplus$. Smaller bodies may still be found in most systems at this time but including these would skew the planet statistics. Due to high ejection rates in the EC system, the EC system produces fewer planets and retains less disk mass than the CC and EP systems. The EC system does produce more massive planets on average, however.

Figure 3 shows the eccentricity (left) and inclination (right) versus the planet semimajor axis, $a_p$, normalized by the binary separation, $a_b$, for all the bodies that survived 7 Myr of integration time except the EPGR model, which shows the final bodies of the EP model after being integrated for an additional Myr with the effects of GR. The size and color of the points correspond to the body’s mass.

Figure 4 shows the maximum differences in eccentricity and inclination, $\Delta e$ and $\Delta i$, respectively, that a planet experiences over the final Myr of integration time. They are plotted as a function of the planet’s final semimajor axis with marker sizes proportional to the planet’s final mass. GR does not significantly affect the EP system dynamics. There is a general trend that the closer in a planet is to the binary, the more variation in eccentricity the planet experiences. The polar planets show smaller variations compared to coplanar planets around eccentric binaries, while planets around coplanar circular orbit binaries show the smallest variation.

All planets around eccentric binaries experience inclination oscillations that take place over tens of thousands of years as a result of the asymmetric potential of the binary (Verrier & Evans 2009; Farago & Laskar 2010). Previous test particle studies reveal complex dynamics due to a set of resonances with an interior perturber that induce large oscillations in...
particle eccentricity and inclination as well as librating orbits (orbits whose argument of periapsis oscillates about a fixed point) and orbit flipping (orbits that flip from prograde to retrograde) of the test particle (Naoz et al. 2017; Vinson & Chiang 2018; de Elía et al. 2019). Such resonances can lead to the chaotic and unstable evolution of a body and explain the semimajor axis dependence on eccentricity variation we observe in our simulations. The terrestrial systems we study are much closer in than the test particle in previous studies, and the stronger gravitational force of the central binary stabilizes the bodies. We note that the more dynamically changing planet orbits do not significantly affect the number of planets that are able to form in a polar system around an eccentric binary compared to a circular-coplanar system (see Table 1).

Previously we found in coplanar disks that wide and eccentric binaries and exterior giant planets inhibit terrestrial planet formation by promoting mass ejections from the systems. A tertiary stellar companion may have similar effects on terrestrial planet formation. A tertiary stellar companion may have similar effects as a faint companion on detectable signatures of giant planets with eclipse timing variations, but we leave the exploration of this subject to future studies.

4. Conclusions

With n-body simulations, we have modeled the late stages of terrestrial planet formation in a polar alignment around an eccentric binary. Hydrodynamic gas disk simulations determined the initial distribution of Moon- and Mars-sized bodies for our n-body simulations. We found that terrestrial CBP formation around an eccentric binary is more likely in a polar alignment than a coplanar alignment. The potential of a polar-aligned binary leads to reduced mass loss and fewer stellar collisions than in coplanar binaries. Terrestrial planetary systems formed in a polar alignment around an eccentric orbit binary are similar to those around a circular-coplanar binary. Planetary systems around eccentric binaries exhibit tilt and eccentricity oscillations that are smaller in the polar configuration and unaffected by GR. We suggest that polar terrestrial planets will be found in the future.

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Software: REBOUND (Rein et al. 2019).

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Figure 4. $\Delta E$ (top) and $\Delta i$ (bottom) vs. the particle semimajor axis, $a_p/a_{1b}$, for bodies with $M_p > 0.1\ M_{\oplus}$ at $t = 8\ Myr$ for the EPGR runs and $t = 7\ Myr$ for all other runs. The size of the point is proportional to the body’s mass.
