The Influence of Depth of Cut, Feed Rate, and Step-over on Dimensional Accuracy in Subtractive Rapid Prototyping of Polycarbonate Material

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Abstract. Subtractive rapid prototyping is fast and automatic three dimensions physical modelling that uses computer aided design model as the input. The dimensional accuracy of the result of the subtractive rapid prototyping is influenced by its process parameters. The aim of this research is to study and then develop a model that shows the influence of depth of cut, feed rate, and step-over on the vertical length error, horizontal length error, and depth error in subtractive rapid prototyping of polycarbonate material. This research implements response surface methodology to develop the model and then followed by the residual tests to evaluate the developed model. The result shows that the increase of the feed rate and the step-over will increase the horizontal dimension error. The most influenced factor on the horizontal dimension error is the step-over. Meanwhile, the vertical dimension error will be affected mostly by the step-over. Last, the depth error is influenced by the feed rate, the step-over, and the depth of cut. The depth of cut is the most critical factor that increases the depth error. The developed models give an insight on how several process parameters of rapid prototyping will influence the dimensional accuracy of a polycarbonate material. Based on the model, efficient resources utilization can be achieved.

1. Introduction
Polycarbonate material is a strong, tough, and transparent thermoplastic material that is used in various applications including in tooling. As an example, a polycarbonate can be implemented as a complex shape chocolate mould. In order to produce a complex shape mould, a subtractive rapid prototyping is implemented as it is typically suitable for polycarbonate material to produce parts that require specific finishes.

Subtractive rapid prototyping is fast and automatic three dimensions physical modelling that uses Computer Aided Design model as the input. The physical modelling process is performed by implementing milling process to cut the raw material with tool that rotates in very high speed. According to Toh, C.K., the milling process with 10 mm tool diameter that is rotated in 10,000 rpm is called high speed milling [1]. Therefore, the subtractive rapid prototyping can be categorised as a high speed milling.

One of the important considerations in manufacturing a mold by using subtractive rapid prototyping is the dimensional accuracy of the mold. However, no research found in the literature that investigates the influence of high speed milling process parameters on the dimensional accuracy of the polycarbonate material. Most of the previous studies found in the literature investigate the dimensional
accuracy of part produced by additive rapid prototyping [2-6]. According to Ippolito, R., et. al., one of the additive rapid prototyping processes which is Stereolithography process can achieve the average dimensional accuracy until 0.08 mm [3]. This research also describes that the highest dimensional accuracy for additive rapid prototyping process is achieved by using Fused Deposition Modelling. The achieved dimensional accuracy of this process is 0.03 mm. However, this process will generate higher surface roughness compared to other processes.

Nieminem, I., et. al., investigate the possibility to use high speed milling to fabricate a thin fin of polycarbonate material by changing the depth of cut and step-over [7]. However, Nieminem, I., et. al. did not investigate the influence of these parameters on the dimensional accuracy of the polycarbonate material.

Based on the studies conducted by Oktem, H., et al., The, J.S., et. al., the dimensional accuracy of a milling process are affected by interpolation type, tool holder type, controller of the machine, computer aided manufacturing software, physical and mechanical characteristics of the material, physical and mechanical characteristics of the tool, vibration, depth of cut, step-over, feed rate, cutting speed, and cut type. [8-12].

The aim of this research is to study and develop a model that shows the influence of depth of cut, feed rate, and step-over on the dimensional accuracy of polycarbonate material in subtractive rapid prototyping. These three process parameters are selected because these parameters are the dominant factors that influence the material rate removal and the dimensional accuracy simultaneously.

2. Research methodology
This research implements Response Surface Methodology to develop the dimensional accuracy model. To validate the developed model, three residual tests, which are independence test, constant variance test, and normality test are conducted.

In this research, the subtractive rapid prototyping process is implemented on the polycarbonate material to achieve the shape shown in figure 1. The subtractive rapid prototyping machine used in this research is Roland MDX 40. The machine is assisted by CAM Modela Player 4.0 software to generate the tool path. The required input to generate the tool path is a three dimension model in STL format. The software uses zigzag cut type to move the cutting tool. The cutting tool used in this research is carbide solid square end mill with 5 mm diameter.

![Figure 1. The designed shape.](image)

Roughing and finishing processes are applied in order to create the shape above. Each process requires different parameter values. Table 1 shows the parameter value of the subtractive rapid prototyping for the roughing process. For finishing process, three levels of value for depth of cut, feed rate, and step-over are determined. The value of each level for each parameter is determined based on the machine specification, literature study, and the preliminary experiment as shown in table 2. Meanwhile, the spindle and the entry speed for finishing process are 10000 rpm and 4 mm/s consecutively. In this research, no coolant is used in performing the subtractive rapid prototyping.
Table 1. Parameter value for roughing.

| Parameter       | Value     |
|-----------------|-----------|
| Feed Rate       | 12 mm/s   |
| Entry Speed     | 4 mm/s    |
| Spindle Speed   | 8500 rpm  |
| Depth of Cut    | 0.37 mm   |
| Step-over       | 1 mm      |

Table 2. Parameter value for finishing.

| Parameter          | Low  | Middle | High |
|--------------------|------|--------|------|
| Depth of Cut (mm)  | 0.1  | 0.235  | 0.37 |
| Feed Rate (mm/s)   | 12   | 14.5   | 17   |
| Step-over (mm)     | 0.3  | 0.65   | 1    |

This research takes several assumptions, which are the polycarbonate material is always homogeneous, the cutting temperature is always constant, and the tool wear occurs after performing three roughing and finishing processes.

The response investigate in this research is the dimensional accuracy. The measurement of the dimensional accuracy is conducted at Industrial Metrology Laboratory of University of Surabaya. The dimensional accuracy is determined based on the difference between the actual and the designed length of horizontal edge (parallel to the feed direction), the difference between the actual and the designed length of vertical edge (parallel to the step over direction), and the difference between the actual and the designed depth of the hole. The actual length and the depth are measured by using a caliper with 0.01 µm of accuracy. After the measurement process, the measured data is analyzed by using MINITAB release 14 software.

3. Result and discussion

The first step in implementing the response surface methodology is designing and conducting the first order experiment. The experimental design and the result of the first order experiment are shown in Table 3. Based on the experiment results, the first order models of horizontal length error, vertical length error, and depth error are developed.

Table 3. Experiment results.

| Std Order | Run Order | Feed Rate (mm/s) | Step-over (mm) | Depth of Cut (mm) | Hor. Length Error (mm) | Ver. Length Error (mm) | Depth Error (mm) |
|-----------|-----------|------------------|----------------|-------------------|------------------------|------------------------|-----------------|
| 11        | 1         | 14.50            | 0.65           | 0.235             | 0.05                   | 0.57                   | 0.00            |
| 13        | 2         | 14.50            | 0.65           | 0.235             | 0.05                   | 0.61                   | -0.01           |
| 2         | 3         | 17.00            | 0.30           | 0.100             | 0.04                   | 0.28                   | -0.01           |
| 12        | 4         | 14.50            | 0.65           | 0.235             | 0.03                   | 0.67                   | -0.04           |
| 7         | 5         | 12.00            | 1.00           | 0.370             | 0.06                   | 1.00                   | 0.02            |
| 9         | 6         | 14.50            | 0.65           | 0.235             | 0.04                   | 0.72                   | 0.01            |
| 3         | 7         | 12.00            | 1.00           | 0.100             | 0.09                   | 1.03                   | 0.00            |
| 5         | 8         | 12.00            | 0.30           | 0.370             | 0.05                   | 0.36                   | 0.01            |
| 10        | 9         | 14.50            | 0.65           | 0.235             | 0.05                   | 0.73                   | 0.00            |
| 6         | 10        | 17.00            | 0.30           | 0.370             | 0.03                   | 0.29                   | 0.03            |
| 1         | 11        | 12.00            | 0.30           | 0.100             | 0.04                   | 0.40                   | 0.01            |
| 4         | 12        | 17.00            | 1.00           | 0.100             | 0.09                   | 1.07                   | 0.03            |
| 8         | 13        | 17.00            | 1.00           | 0.370             | 0.09                   | 1.02                   | 0.02            |
The mathematical model to predict the horizontal length error values is shown in equation (1). Figure 2 and 3 shows that the residual of the horizontal length error model is to be normally and independently distributed. Furthermore, based on the regression equation analysis, the residual of the horizontal length error model is identical. The residual tests show that the first order model of horizontal length error is satisfied all the assumptions and can be used as the best prediction of horizontal length error model and no second order experiment is required to be conducted. This model shows that the increase of the feed rate and the step over will increase the horizontal length error value. In the opposite, the increase of the depth of cut will decrease the horizontal length error value. According to the model, the horizontal length error is mostly affected by the step-over.

\[
E_{hor} = 0.0144289 + 0.0005 x F + 0.0607143 x S - 0.0277778
\]

(1)

where:
- \(E_{hor}\) is horizontal length error (mm)
- \(F\) is feed rate (mm/s)
- \(S\) is step-over (mm)
- \(D\) is depth of cut (mm).

Figure 2. Normal Probability plot of the residuals for horizontal length error.

Furthermore, the mathematical model to predict the vertical length error values is shown in equation (2). Figure 4 and 5 shows that the residual of the vertical length error model is to be normally and independently distributed. Furthermore, the residual of the vertical length error model is identical based on the regression equation analysis.

\[
E_{ver} = 0.143584 - 0.0065 x F + 0.996429 x S - 0.1018528 x D
\]

(2)

where:
- \(E_{ver}\) is vertical length error (mm)
- \(F\) is feed rate (mm/s)
- \(S\) is step-over (mm)
- \(D\) is depth of cut (mm).

This model shows that the increase of the step-over will increase the vertical length error value. Meanwhile, the increase of the depth of cut will decrease the vertical length error value. Based on the residual tests, the first order model of vertical length error is satisfied all the assumptions and can be used as the best prediction model for vertical length error.

Last, the mathematical model to predict the depth error is developed as shown in equation (3).

\[
E_{depth} = - 0.0342093 + 0.0015 x F + 0.0107143 x S + 0.0462963
\]

(3)

where:
- \(E_{depth}\) is depth error (mm)
- \(F\) is feed rate (mm/s)
- \(S\) is step-over (mm)
D is depth of cut (mm).

![Figure 4](image1.png) ![Figure 5](image2.png)

**Figure 4.** Normal Probability plot of the residuals for vertical length error.

**Figure 5.** Autocorrelation plot of the residuals for vertical length error.

Figure 6 and 7 shows that the residual of the depth error model is to be normally and independently distributed. Furthermore, based on the regression equation analysis, the residual of the depth error model is identical. The mathematical model shows that the depth error will increase following the increase of the feed rate, the step over, and the depth of cut. The model also shows that the most influenced factor is the depth of cut. The residual tests shows that the first order model of depth error is satisfy all the assumptions and can be used as the best prediction model for depth error.

![Figure 6](image3.png) ![Figure 7](image4.png)

**Figure 6.** Normal Probability plot of the residuals for depth error.

**Figure 7.** Autocorrelation plot of the residuals for depth error.

4. Conclusions

This result of this research shows that the increase of the step-over will increase the vertical and horizontal length errors. In addition, the increase of the feed rate will increase the vertical length error. Meanwhile, the increase of the depth of cut will decrease the vertical and horizontal length error value. Additionally, the depth error will increase following the increase of all process parameters. This most affected factor of the length error and the depth error are the step-over and the depth of cut consecutively.

The developed error models give an insight on how several process parameters of rapid prototyping will influence the dimensional accuracy of a polycarbonate material. Based on the model, efficient resources utilization can be achieved. This research also provides a preliminary study to optimize the material removal rate and the accuracy in rapid prototyping of the polycarbonate material. For the future work, the optimization of various parameters in rapid prototyping of the polycarbonate material to achieve the highest accuracy, the highest material removal rate, and the minimum surface roughness...
need to be done. In addition, based on the experiment results, there is a possibility that the length error is affected by the length of the designed shape. In the future, it is also important to investigate this possibility further.

5. References
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