Development of an Empirical Model for the Wear Rate of Contact Bearing Materials Using a Standard Pin-On-Disc Test

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ABSTRACT
The wear rate for contact bearing materials is studied as a function of a number of potentially influential factors, including applied load, rotational speed, sliding distance, and material type. A standard pin-on-disc test is used to conduct this study. Two levels of applied load (20 and 10 N), rotational speed (100 and 200 rpm), sliding distance (150 and 450 m), and material type (AISI 440C and AISI 420 martensitic stainless steel) were tested. Tests are run according to the design of experiments (DOE) methodology. Experimental results are analyzed based on the analysis of variance (ANOVA) approach in order to determine the factors that have a significant impact on the wear rate. An empirical model is developed to fit the true relationship between wear rate and the significant factors in the case AISI 440C and AISI 420 materials. Finally, the morphology of the worn surface is studied using SEM and EDX images.

Key words: Wear Rate, Standard pin-on-disc test, contact bearing materials, applied load, rotational speed, sliding distance, material type

INTRODUCTION
Wear can generally lead to severe economic and technological problems as it is the effect on resource utilization, machine performance, national economy and conservation of fuel. Therefore, the control of wear becomes a very strong need to eliminate and reduce its effects by studying the factors influences in the wear (Andersson et al., 2011; Andersson, 2012).

Wear is a surface phenomenon that depends on material properties such as hardness (Berglund and Shi, 2017), microstructure (Blau, 2015) and surface finish, and working conditions such as load, speed, lubrication, and temperature. Different conditions can cause
wear by different mechanisms. Generally, small changes in speed, load or environmental conditions can typically lead to considerable changes in the material wear rate of two or one surfaces in contact (Boher, 2009; Cavalieri et al., 2016).

A common way, which is used in order to measure wear rate is a pin-on-disc test based on the ASTM G99 standard. The test material is usually made in the form of a pin (Chongyi et al., 2013). This pin is setup to apply a certain force against a rotating disc at a constant rotational speed (w). Mass loss due to wear is then measured after some period of time. The wear rate (mm3/N.m) is then calculated according to the equation (Wang et al., 1996)

\[
\text{Wear Rate} = \frac{M}{\rho FL}
\]

Where that M represents the mass loss (g), F refers to the applied load against the pin (N), the alloy density of the test specimens (g/mm3) represented by \( \rho \), as well as L represents the length of distance of the sliding (m).

The previous equation can be useful for comparing between materials in terms of their wear resistance. However, this comparison may be accurate or reliable when the wear rate is measured at the same conditions of applied load, rotational speed, run length and surface finish. But when such conditions are different, the above equation is known to give different results. Thus, it will be very advantageous for practical reasons to have an empirical model for wear rate that is less sensitive to the various levels of process conditions.

**AIMS AND OBJECTIVES**

This paper aims to develop an Empirical Model for the Wear Rate of Contact Bearing Materials Using a Standard Pin-On-Disc Test, three main objectives are set to reach paper aim:

- Determine the sensitivity of the wear rate against the relevant process conditions for two commonly used contact bearing materials: AISI 440C and AISI 420 martensitic stainless steel.
- Develop an empirical relationship between wear rate and all the significant factors.
- Determine the morphology of the worn surface of the studied materials

**METHODOLOGY**

This part includes a description of AISI 440C and AISI 420 Martensitic stainless steel, the generation the DOE design, material preparation, the dry sliding wear tests and examination of surface morphology. Figure 1 shows a flow chart of the paper procedures and tests.
RESULTS AND DISCUSSION

Table 1 shows experimental results of the dry sliding wear that are obtained through pin-on-disc tests. This table shows two levels for each factor with center points. The data are listed based on their random run order, which are produced through using Minitab software. Further, the process parameters impact on the wear weight loss has been investigated through (ANOVA) test.

Table 1: Experimental results of the dry sliding wear experiments

| Run Order | Load (N) | Speed (rpm) | Distance (m) | Material Type | Mass Loss | Run Order | Load (N) | Speed (rpm) | Material Type | Distance (m) | Mass Loss |
|-----------|----------|-------------|--------------|---------------|-----------|-----------|----------|-------------|---------------|--------------|-----------|
| 1         | 20       | 100         | 200          | AISI 440C     | 0.0109    | 21        | 20       | 100         | AISI 440C     | 200          | 0.0105    |
| 2         | 10       | 200         | 600          | AISI 420HC    | 0.0138    | 22        | 20       | 200         | AISI 440C     | 600          | 0.0151    |
| 3         | 20       | 100         | 200          | AISI 420HC    | 0.0075    | 23        | 15       | 150         | AISI 440C     | 400          | 0.0148    |
| 4         | 10       | 100         | 200          | AISI 440C     | 0.0061    | 24        | 10       | 200         | AISI 420HC    | 200          | 0.0043    |
| 5         | 10       | 200         | 600          | AISI 420HC    | 0.0140    | 25        | 20       | 100         | AISI 420HC    | 200          | 0.0073    |
| 6         | 10       | 100         | 600          | AISI 420HC    | 0.0246    | 26        | 15       | 150         | AISI 420HC    | 400          | 0.0149    |
| 7         | 20       | 100         | 600          | AISI 440C     | 0.0274    | 27        | 10       | 200         | AISI 420HC    | 200          | 0.0054    |
| 8         | 10       | 200         | 600          | AISI 440C     | 0.0160    | 28        | 15       | 150         | AISI 440C     | 400          | 0.0094    |
| 9         | 10       | 100         | 200          | AISI 420HC    | 0.0054    | 29        | 20       | 100         | AISI 420HC    | 600          | 0.0231    |
| 10        | 20       | 200         | 200          | AISI 420HC    | 0.0051    | 30        | 10       | 100         | AISI 440C     | 600          | 0.0226    |
| 11        | 20       | 200         | 600          | AISI 420HC    | 0.0120    | 31        | 10       | 200         | AISI 440C     | 600          | 0.0140    |
| 12        | 20       | 100         | 200          | AISI 440C     | 0.0071    | 32        | 20       | 200         | AISI 440C     | 600          | 0.0129    |
| 13        | 10       | 100         | 600          | AISI 440C     | 0.0217    | 33        | 15       | 150         | AISI 440C     | 400          | 0.0104    |
| 14        | 15       | 150         | 400          | AISI 420HC    | 0.0124    | 34        | 10       | 200         | AISI 440C     | 200          | 0.0048    |
| 15        | 20       | 200         | 200          | AISI 440C     | 0.0077    | 35        | 15       | 150         | AISI 420HC    | 400          | 0.0108    |
| 16        | 10       | 100         | 600          | AISI 420HC    | 0.0238    | 36        | 10       | 100         | AISI 420HC    | 200          | 0.0042    |
| 17        | 15       | 150         | 400          | AISI 440C     | 0.0127    | 37        | 20       | 200         | AISI 420HC    | 200          | 0.0057    |
| 18        | 20       | 200         | 600          | AISI 420HC    | 0.0154    | 38        | 10       | 100         | AISI 440C     | 200          | 0.0050    |
| 19        | 20       | 100         | 600          | AISI 420HC    | 0.0223    | 39        | 15       | 150         | AISI 420HC    | 400          | 0.0115    |
| 20        | 20       | 200         | 200          | AISI 440C     | 0.0057    | 40        | 20       | 100         | AISI 440C     | 600          | 0.0213    |

Analysis of Variance (ANOVA)

The ANOVA is applied on the model by using 95% a confidence level. The obtained results of ANOVA analyses for weight loss are shown in Table 2. It can be noted from the table that the P-value for the sliding speed, length of sliding distance and their interaction is lower than 0.05 which imply that both factors and their interaction have a significant effect on the weight loss at the confidence level 95%. On the other hand, the P-value of the applied load and materials factors is more than 0.05, which mean that these factors are not significant and they are not influenced on the weight loss. Moreover, the result in Table 1 shows that the length of sliding distance factor is the most significant and its contribution is 72.28% followed by sliding speed and the length-speed interaction that having 13.32% and 7.25% contribution respectively.
Table 2: ANOVA for the dry sliding wear rate

| Source                        | DF | Seq SS   | Contribution | Adj SS   | Adj MS   | F-Value | P-Value |
|-------------------------------|----|----------|--------------|----------|----------|---------|---------|
| Model                         | 16 | 0.001616 | 95.99%       | 0.001616 | 0.000101 | 34.41   | 0.000   |
| Linear                        | 4  | 0.001454 | 86.37%       | 0.001454 | 0.000363 | 123.84  | 0.000   |
| Load                          | 1  | 0.000009 | 0.54%        | 0.000009 | 0.000009 | 3.11    | 0.091   |
| Speed                         | 1  | 0.000224 | 13.32%       | 0.000224 | 0.000224 | 76.39   | 0.000   |
| Length                        | 1  | 0.001216 | 72.28%       | 0.001216 | 0.001216 | 414.49  | 0.000   |
| Material                      | 1  | 0.000004 | 0.24%        | 0.000004 | 0.000004 | 1.35    | 0.257   |
| 2-Way Interactions            | 6  | 0.000150 | 8.91%        | 0.000150 | 0.000025 | 8.51    | 0.000   |
| Load*Speed                    | 1  | 0.000009 | 0.52%        | 0.000009 | 0.000009 | 2.97    | 0.098   |
| Load*Length                   | 1  | 0.000111 | 0.68%        | 0.000111 | 0.000111 | 3.88    | 0.061   |
| Load*Material                 | 1  | 0.000004 | 0.24%        | 0.000004 | 0.000004 | 1.36    | 0.256   |
| Speed*Length                  | 1  | 0.001222 | 7.25%        | 0.001222 | 0.001222 | 41.59   | 0.000   |
| Speed*Material                | 1  | 0.000000 | 0.00%        | 0.000000 | 0.000000 | 0.00    | 0.976   |
| Length*Material               | 1  | 0.000004 | 0.22%        | 0.000004 | 0.000004 | 1.27    | 0.272   |
| 3-Way Interactions            | 4  | 0.000100 | 0.59%        | 0.000100 | 0.000002 | 0.85    | 0.510   |
| Load*Speed*Length             | 1  | 0.000003 | 0.15%        | 0.000003 | 0.000003 | 0.88    | 0.357   |
| Load*Speed*Material           | 1  | 0.000006 | 0.35%        | 0.000006 | 0.000006 | 2.00    | 0.171   |
| Load*Length*Material          | 1  | 0.000000 | 0.00%        | 0.000000 | 0.000000 | 0.00    | 0.976   |
| Speed*Length*Material         | 1  | 0.000001 | 0.09%        | 0.000001 | 0.000001 | 0.51    | 0.484   |
| 4-Way Interactions            | 1  | 0.000001 | 0.03%        | 0.000001 | 0.000001 | 0.20    | 0.661   |
| Load*Speed*Length*Material    | 1  | 0.000001 | 0.03%        | 0.000001 | 0.000001 | 0.20    | 0.661   |
| Curvature                     | 1  | 0.000001 | 0.08%        | 0.000001 | 0.000001 | 0.49    | 0.493   |
| Error                         | 23 | 0.00068  | 4.01%        | 0.00068  | 0.000003 |          |         |
| Lack-of-Fit                   | 1  | 0.000004 | 0.22%        | 0.000004 | 0.000004 | 1.25    | 0.276   |
| Pure Error                    | 22 | 0.000064 | 3.79%        | 0.000064 | 0.000003 |          |         |
| Total                         | 39 | 0.001683 | 100.00%      |          |          |         |         |

The normal plot of the standardized effects in Figure 2 shows that the length (represented by C symbol) is significant and had a positive effect on the weight loss. Sliding speed and length/speed interaction (represented by B and BC symbols) are significant and have a negative effect in the mass loss.

![Figure 2: Normal curve for the standardized effect of the weight loss](image-url)
Figure 3 shows the Pareto chart of the standardized effect. The chart shows the importance and the magnitude of the effects. The bars cross the red line (length, speed, and their interaction bars) at 2.07 are significant.

![Pareto Chart of the Standardized Effects](image)

Figure 3: Pareto chart of the weight loss factors

The significance of the weight loss factors can be checked also by analyzing their main-effect-plots as illustrated in Figure 4. So, it can be noticed from the plot that both normal load and material had a very small effect on the weight loss, but the length and sliding speed had a high effect on the weight loss. Furthermore, the increase in length leads to increase the mass loss, but the increase in sliding speed leads to reduce the mass loss.

![Main Effects Plot for Weight loss](image)

Figure 4: Effect of weight loss

Figure 5 shows the interaction plot for the weight loss. It can be noticed from the plots that the mass loss at the high speed and low length had a significant effect.
The significance of the mass loss factors can be checked also by analyzing their main-effect-plots as illustrated in the following paragraphs:

Effect of Load on the Weight Loss

Figure 6 shows that the normal load factor has a negligible impact on the weight loss. As the applied load increases, the temperature of rubbing surface increases due to the frictional force. As the temperature increases, carbon atoms of Martensite steel diffuses out and formed carbides which leads to increase the material hardness. Therefore, the material resistance of weight loss increases due to the increment of material hardness which justify the small effect of load in the weight loss.
The hardness of the worn surfaces of AISI 440C and AISI 420 stainless steel subjected to 10N and 20N loads, 600 m sliding distance and 100 rpm sliding speed are included in Table 3.

Table 3: Material hardness at different loads

| Material | Load (N) | Hardness (HRC) |
|----------|----------|----------------|
| AISI 440C | 10       | 29             |
| AISI 440C | 20       | 53             |
| AISI 420  | 10       | 35             |

**Sliding Speed Effect on the Weight Loss**

The main effect of the speed plot is shown in Figure 7. It can be noted that the plot line is not horizontal which means the speed factor has effect in the weight loss. It can be noted also that the sliding speed has a negative effect on the weight loss.

![Figure 7: Main effect plot of the speed factor](image)

**Effect of Sliding Distance on the Weight Loss**

The main effect plot of the length, shown in Figure 8, indicate that the length factor is significant because the line slope is not horizontal. It can be noticed from the plot that the length factor has a positive effect on the weight loss.

![Figure 8: Main effect plot of the length factor](image)
Effect of material on the weight loss

The main effect plot of the material, shown in Figure 9, indicate that the length factor is significant because the line slope is not horizontal. It can be noticed from the plot that the length factor has a positive effect on the weight loss.

![Main effects plot of the material factor](image)

Figure 9: Main effect plot of the material factor

Model Adequacy Checking

The data of weight loss are examined by the residual plots as shown in Figures 10, 11, and 12. The normal probability plots in Figure 10 made a straight line referring to the normal distribution of the errors.

![Normal probability plot](image)

Figure 10: Standardized residual plot of the weight loss data
The plot of versus order in Figure 11 shows that the data are independent and they have not constant variability.

![Figure 11: observation order of the standardized residual](image)

The fitted value plot in Figure 12 show that the value of the response is randomly distributed.

![Figure 12: standardized residual of fitted value](image)

**Wear Rate Formula**

The wear rate formula could include only the significant wear factors. The result of this paper shows that the sliding speed and the sliding distance are significant factors, but the normal load is not significant. Therefore, the formula 1 could be adjusted by removing the insignificant factor (normal load) and adding the significant factor (sliding speed).
To determine the relation between the sliding speed and the mass loss, several experiments are conducted by using a pin-on-disc machine at different sliding speeds with fixing the values of the normal load and sliding distance. By analyzing the experimental data, the obtained results demonstrate that the relation between the sliding speeds in addition to the mass loss can be represented by Michaelis–Menten equation as the following:

\[ M = \frac{\theta_1 \cdot S}{\theta_2 + S} \]

Where the mass loss (g) expressed by M, S: is the sliding speed (rpm), and \( \theta_1 \) and \( \theta_2 \): material dependent parameters.

Then, the wear rate formula can be adjusted and expressed by the following equation:

\[ W = \frac{M}{\rho L \cdot \frac{\theta_1 \cdot S}{\theta_2 + S}} \]

Where the wear rate (\( \text{mm}^3/\text{m} \)) is represented by W, and the mass loss (g) is represented by M, \( \rho \): is the material density (g/mm3), L represents the length of the sliding distance (m), the sliding speed (rpm) expressed by S, as well as \( \theta_1 \) and \( \theta_2 \) are material dependent parameters.

The estimation \( \theta_1 \) and \( \theta_2 \) parameters for AISI 440C are determined by Minitab. Table 4 includes the parameter estimation and the estimated standard error of the regression.

\[ \text{Mass Loss } 440 = 0.0265154 \times \text{‘Speed(rpm)’} / (136.371 + \text{‘Speed(rpm)’}) \]

Figure 13: Fitted line of mass loss versus speed of AISI 440C steel

| Parameter | Estimate | SE Estimate |
|-----------|----------|-------------|
| Theta1    | 0.027    | 0.0054      |
| Theta2    | 136.371  | 56.3862     |

The relation between the mass loss and the speed of AISI 440C are represented by the following equation:

\[ \text{Mass Loss } 440 = 0.0265154 \times \text{‘Speed (rpm)’} / (136.371 + \text{‘Speed (rpm)’}) \]
Table 5: Lack of Fit

| Source       | DF | SS           | MS           | F     | P    |
|--------------|----|--------------|--------------|-------|------|
| Error        | 6  | 0.00000098   | 0.0000016    |       |      |
| Lack of Fit  | 5  | 0.00000098   | 0.0000020    | 393.28| 0.038|
| Pure Error   | 1  | 0.00000000   | 0.00000000   |       |      |

S shows the average distance, which the observed values fall from the regression line. Thus, it is referring to how wrong the regression model is on average using the units of the response variable. Smaller values are better because it indicates that the observations are closer to the fitted line.

Examination of the Worn Surface Morphology

The morphology of the worn surface is examined for each material by using SEM images to investigate the wear mechanism. Figures 14, 15, and 16 show the worn surface of AISI 420 stainless steel sample after dry sliding wear test at 20 N normal load, 600 m sliding distance and 200 rpm sliding speed. The figures show that there are mixed wear mechanisms. For example, Figure 14 includes a delamination and abrasive wear mechanism, Figure 15 shows adhesion wear and Figure 16 shows an image includes the three types.

Figure 14: A delamination and abrasive wear mechanism

Figure 15: adhesion wear
Figures 17 and 18 show the worn surface of AISI 440C stainless steel sample after dry sliding wear test at 20 N normal load, 600 m sliding distance and 200 rpm sliding speed. Figure 17 includes an abrasive wear mechanism, and Figure 18 shows an image of abrasive, adhesion and delamination wear mechanisms.

Figures 19 and 20 show the worn surface of AISI 440C stainless steel sample after dry sliding wear test at 10 N normal load, 600 m sliding distance and 200 rpm sliding speed. Figure 19 shows an image abrasive, adhesion and delamination wear mechanisms, and Figure 20 includes an abrasive wear mechanism.
Figure 19: abrasive, adhesion and delamination wear mechanisms

Figure 20: an abrasive wear mechanism

Figure 21: EDX image of AISI 440C stainless steel at 10N load, 100 rpm sliding speed and 600m sliding distance

Figures 21 and 22 include the EDX images of the worn surfaces at different loads. It can be observed from the EDX that the content of carbides in the worn surface at 20N load is higher than the carbides content at 10N load.
CONCLUSION

The present research is accomplished to develop an empirical model to fit the true relationship between wear rate and the significant factors in the case of AISI 440C and AISI 420 materials. Four factors are studied in this research namely the applied load, the sliding distance, the sliding speed and the material using two replicate full factorial design. Throughout this research, an attempt was made to determine the most significant parameters that influence the wear performance. The results showed that the sliding distance is the most significant factor influencing the mass loss with 72.28% contribution followed by sliding speed (13.32% contribution). Further, the applied load and material have a negligible effect on the mass loss. A relation between sliding speed and the mass loss was determined. Moreover, a relation between the wear rate and the significant factors are developed. The list of the following points includes the conclusions drawn from this research:

- The applied load and material have a negligible effect on the mass loss.
- The sliding speed and the sliding distance have a significant effect on the mass loss.
- Increasing the sliding distance leads to increase of the mass loss and the increasing of the sliding speed leads to reduce the mass loss.

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