Improved measurement of parton distribution functions and $\alpha_s(M_Z)$ with the LHeC

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The potential of the LHeC, a future electron-proton collider, for precision Deep Inelastic Scattering measurements is reviewed with particular emphasis on the reduction of uncertainties on the parton distribution functions (PDFs) of the proton and on the measurement of $\alpha_s(M_Z)$. The interpretation of possible Beyond Standard Model (BSM) signals at the LHC is crucially dependent on precise knowledge of the predictions of the Standard Model (SM) and the uncertainties on PDFs and $\alpha_s(M_Z)$ are a limiting factor. The LHeC project, running in parallel with later stages of LHC running, would provide much improved precision on the PDFs as compared to the precision expected from LHC data alone.
The LHeC project proposes a Large Hadron-Electron Collider using a Linac-Ring configuration with electrons of 50-100 GeV colliding with 7 TeV protons in the LHC tunnel, designed such that e-p collisions can operate synchronously with p-p. The details of the accelerator and the detector are covered in other contributions to this conference. This talk focuses on Deep Inelastic Scattering and low-x physics. Higgs, BSM physics and e-A collisions are covered in other talks. Further details may be found in the Conceptual Design Report (CDR) [1].

The LHeC represents an increase in the kinematic reach of Deep Inelastic Scattering and an increase in the luminosity. This allows a potential increase in the precision of parton distributions in the kinematic region of interest for the detailed understanding of BSM physics at the LHC. It also allows the exploration of a kinematic region at low-x where we learn more about QCD - is there a need for resummations beyond DGLAP, or even for non-linear evolution and gluon saturation?

If a 100TeV Future Circular Collider (FCC) is built for hadron-hadron collisions, FCChh, this will extend the kinematic region for BSM physics further and it is worth contemplating an electron-hadron collider, FCCeh, which would provide a much more precise knowledge of parton distributions in this new kinematic region as well as exploration of QCD at even lower x.

Deep Inelastic Scattering is the best process to probe proton structure. The Neutral Current Cross Sections measure the sea quarks and access the gluon via the scaling violations and the longitudinal structure function. The Charged Current processes give information on flavour separated valence quarks and the difference between the Neutral Current $e^+$ and $e^-$ distributions probes the valence quarks via the $\gamma-Z$ interference term.

To study the potential of the LHeC a scenario with 50 GeV electrons on 7 TeV protons with $50 \text{ fb}^{-1}$ luminosity is simulated. The kinematic region accessed is $0.000002 < x < 0.8$ and $2 < Q^2 < 100,000 \text{GeV}^2$. Uncorrelated and correlated systematic errors are simulated using our knowledge of dominant sources such as the electron and hadron energy scales, angular resolution and photoproduction background, based on experience with the H1 detector, see the LHeC CDR [1] for details.

In Fig. 1 the current level of our knowledge of valence distributions is shown, comparing various modern PDF sets in ratio to NNPDF3.0. In Fig. 2 the potential improvement in uncertainty from LHeC data is shown by comparing the uncertainties on the valence PDFs from a fit to just HERA-I combined data [2] to a fit to these data plus LHeC pseudo-data. Fits to HERA plus BCDMS fixed target data and HERA plus LHC W-asymmetry data are also illustrated but...
these do not bring such a dramatic reduction in uncertainty, even when current LHC data have their uncertainties reduced to reflect our best estimate of the ultimate achievable accuracy.

In Fig. 3 the current level of our knowledge of the gluon distribution is shown, comparing various modern PDF sets in ratio to NNPDF3.0. Log and linear axes illustrate the current level of uncertainty at low and high-\(x\), respectively. Fig. 4 shows the expected level of improvement from LHeC data.

As an example of the importance of such precision at high \(x\), Fig. 5 left-hand side, shows a plot of the PDF uncertainty on the gluino pair production cross section as a function of energy, from current PDFs and from the projected post-LHeC PDF. Such gain in PDF precision will be necessary to exploit the gain in experimental precision of future searches for gluinos when the LHC luminosity is increased from 0.3ab\(^{-1}\) to 3ab\(^{-1}\).

The uncertainty on \(\alpha_s(M_Z)\) is also important for many BSM cross sections. The LHeC can
Figure 4: The PDF uncertainty on the gluon distribution from a fit to just HERA-I data, HERA-I+BCDMS data, HERA-I+LHC W-asymmetry data and HERA-I+LHeC pseudo-data.

Figure 5: Left-hand side: Gluino pair production cross-section for various PDFs in ratio to MSTW2008, as calculated in NLO SUSY QCD assuming squark mass degeneracy and equality of squark and gluino masses. Right-hand side: PDF uncertainty on the $d/u$ ratio, relaxing the assumption $\bar{d} = \bar{u}$ at low $x$, for current data and after LHeC pseudo-data is used from both $ep$ and $eD$ runs.

deliver per-mille accuracy on $\alpha_s(M_Z)$ and this will be a strong constraint on Grand Unified Theories which predict where the couplings unify [3]. This is illustrated in Fig. 6.

Turning now to the low-$x$ region. Fig. 3 shows that HERA sensitivity stops at $x > 5 \times 10^{-4}$ whereas the LHeC can probe down to $x \sim 10^{-6}$, see Fig. 4. Thus one can better explore the low-$x$ region where DGLAP evolution may need to be supplemented by $ln(1/x)$ resummation (BFKL resummation) and one may enter into a kinematic regime where non-linear evolution is required, possibly leading to gluon saturation. In DGLAP based QCD fits we get the gluon from the scaling violations at low-$x$, $dF_2/dln(Q^2) \sim P_{qg} xg(x, Q^2)$. The shape of the gluon extracted may be incorrect if the splitting function $P_{qg}$ needs modification. To check this one can measure other gluon related quantities like the longitudinal structure function $F_L$, which is gluon dominated at low $x$, $F_L(x, Q^2) \sim xg(2.5x, Q^2)$ at LO. Unfortunately the final $F_L$ measurements from HERA do not have sufficient kinematic range or sufficient accuracy to challenge DGLAP. However, Fig. 7 compares current measurements with the projected LHeC measurements of $F_L$, which should be discriminating.
Figure 6: Extrapolation of the coupling constants ($1/\alpha$) to the GUT scale in MSSM as predicted by SOFT-SUSY. The width of the red line shows the uncertainty on the current world average of $\alpha_s(M_Z)$ and width of the black-line shows the projected accuracy of an LHeC measurement.

Figure 7: The current measurements of $F_L$ from HERA data (in blue) compared to projected measurements of $F_L$ at the LHeC (in red).
Figure 8: Current measurements of $F_2^{c\bar{c}}$ (left) and $F_2^{b\bar{b}}$ (right) from HERA (in red) compared to projected measurements at the LHeC (in black).

Further low-x studies include relaxing the conventional assumption, used in many PDFs, that $\bar{u} = \bar{d}$ at low-$x$. The right-hand side of Fig. 3 shows PDF uncertainties on the $d/u$ ratio with this constraint relaxed, and compares current levels of uncertainty with the projections from LHeC pseudo-data. Further improvement could be achieved with LHeC eD data.

LHeC data will also allow us to increase our knowledge of the heavy flavour partons because of the higher cross sections, higher luminosity and new generation of Silicon detectors. Fig. 8 shows projected measurements of $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$ compared to present measurements. Measurements of the strange PDF could also be performed through charm tagging in CC events. If an FCCeh option is explored then it should also be possible to measure top PDFs produced through the $Wb \rightarrow t$ process.

In summary the LHeC would allow improvement in the precision of PDF determinations both at low $x$ and at high $x$. Improvement at high $x$, together with improved precision in the determination of $\alpha_s(M_Z)$ which is also expected at the LHeC, would allow us to predict BSM cross sections with sufficient accuracy to distinguish between different explanations of new physics phenomena. At low $x$ it has long been expected that extension of the conventional QCD DGLAP resummation is necessary to explain the data, but distinguishing between different possible scenarios such as BFKL resummation, non-linear evolution or the onset of gluon saturation, has not been possible. The improvement in accuracy at low $x$ at the LHeC would allow such discrimination.

References

[1] LHeC Study group, CERN-OPEN-2012-015
[2] F. D. Aaron et al. [H1 and ZEUS Collaboration], JHEP 1001 (2010) 109 [arXiv:0911.0884 [hep-ex]].
[3] LHeC Study group, LHeC-Note-2012-005 GEN