Light Gluino Constituents of Hadrons
and a Global Analysis of Hadron Scattering Data

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Abstract

Light strongly interacting supersymmetric particles may be treated as partonic constituents of nucleons in high energy scattering processes. We construct parton distribution functions for protons in which a light gluino is included along with standard model quark, antiquark, and gluon constituents. A global analysis is performed of a large set of data from deep-inelastic lepton scattering, massive lepton pair and vector boson production, and hadron jet production at large values of transverse momentum. Constraints are obtained on the allowed range of gluino mass as a function of the value of the strong coupling strength \( \alpha_s(M_Z) \) determined at the scale of the \( Z \) boson mass. We find that gluino masses as small as 10 GeV are admissible provided that \( \alpha_s(M_Z) \geq 0.12 \). Current hadron scattering data are insensitive to the presence of gluinos heavier than \( \sim 100 - 150 \) GeV.

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I. INTRODUCTION

Relatively light strongly-interacting fundamental particles may be considered as constituents of nucleons. The nature of these constituents and their experimental effects become evident when the parent hadrons are probed at sufficiently short distances or, equivalently, sufficiently large four-momentum transfer $Q$. The charm quark $q = c$ and the bottom quark $b$ are treated appropriately as constituents of hadrons in situations in which $Q > m_q$, where $m_q$ is the mass of the heavy quark. Other strongly interacting fundamental particles may exist, as yet undiscovered experimentally, with masses lying somewhere between the bottom- and top-quark masses. One example is a relatively light gluino: a color-octet fermion and the supersymmetric partner of the massless spin-1 gluon. For our purposes, we define a “light” particle to have a mass less than 100 GeV. In this paper, we explore the effects that a color-octet fermion would have on the parton distribution functions of nucleons, with a view toward establishing whether the set of hard-scattering data used in global analysis may already place significant constraints on the existence and allowed masses of such states.

In our investigation, we use a light gluino from supersymmetry (SUSY) \cite{1,2} as a concrete example, but our analysis and conclusions should apply as well to the case of a color-octet fermion of whatever origin. As constituents of hadrons, these color-octet fermions share the momentum of the parent hadron with their standard model quark, antiquark, and gluon partners. The distribution of light-cone momentum fraction $x$ carried by constituents is specified by parton distribution functions (PDFs) as functions of both $x$ and the scale $Q$ of the short-distance hard scattering. The process-independent PDFs are essential ingredients for obtaining normalized predictions of rates for hard-scattering reactions at high energies. A simultaneous analysis of a large body of scattering data (global analysis) provides strong constraints on the magnitude and $x$ dependence of the PDFs.

In perturbative quantum chromodynamics (QCD), the existence of a color-octet fermion and its couplings to the standard model constituents alter the coupled set of evolution equations that governs the functional change of the parton distributions as momentum is varied. Gluinos have different renormalization group properties from those of the quark and gluon constituents, and the contributions of fermions in the color-octet representation are enhanced strongly. Within the context of broken supersymmetry, squarks (scalar partners of quarks) may also be relatively light, particularly those of the third generation, the bottom-
and top-squarks \[3, 4, 5, 6\]. In the study reported here, we include a gluino in our PDF analysis, but we neglect possible contributions from other hypothesized supersymmetric states with masses above a few GeV, such as bottom squarks. As explained in Sec. II, the effects of squark contributions on the current data are much less important than those of gluinos. The approximation of retaining only the light gluino contribution simplifies the calculations while retaining most of the relevant physics.

In a global analysis of hadronic data, a large sample of data is studied (about 2000 points) from a variety of experiments at different momentum scales. The data set included in our study is the same as in the recent CTEQ6 study done within the context of the standard model. The data come from deep-inelastic lepton scattering, massive lepton pair and gauge boson production, and hadron jet production at large values of transverse momentum. We apply the methodology of the next-to-leading order (NLO) CTEQ6 analysis to explore the compatibility of a light gluino with the large set of hadronic data. Methods developed recently for the analysis of uncertainties of PDFs \[8, 9, 10, 11, 12, 13, 14, 15\] allow us to obtain quantitative bounds on the existence and masses of gluinos from a global analysis. In early PDF analyses within the context of light gluinos \[16, 17, 18\], a gluino with a mass 5 GeV or less was found to be consistent with the data available at that time. A more recent study \[19\] disfavors a gluino with a mass 1.6 GeV or less. The much larger sample of the data in the modern fit and improved understanding of PDF uncertainties make it possible to derive more precise bounds.

Light superpartners influence the evolution with scale \(Q\) of the strong coupling strength \(\alpha_s(Q)\). The constraints we obtain on the gluino mass from a global analysis depend significantly on the value of the strong coupling strength \(\alpha_s(M_Z)\) that is an ingredient in the global analysis. In Sec. II, we begin with a brief review of the dominant experimental constraints on \(\alpha_s\) and consider the changes that may arise if supersymmetric particles and processes are present. Further discussion of experimental constraints on \(\alpha_s(M_Z)\) may be found in the Appendix. We describe in Sec. II.B how we implement the NLO evolution of the PDFs, while including the gluino degree of freedom at leading order (LO). Once supersymmetric particles are admitted, they contribute to hard scattering processes either as incident partons and/or as produced particles. We therefore specify the hard scattering matrix elements that describe supersymmetric contributions to the rate for jet production at large transverse momentum. In Sec. III, we present and discuss the results of our global fits. The discrimi-
nating power of our analysis depends crucially on the inclusion of the Tevatron jet data in the fit. The inclusion of a light gluino in the PDFs removes momentum from the gluon PDF at large $x$, tending to depress the contribution from SM processes to the jet rate at large $E_T$. However, the effect is compensated partially by a larger value of $\alpha_s(M_Z)$, slower evolution of $\alpha_s$ that makes $\alpha_s(E_T > M_Z)$ larger than in the standard model, and by contributions to the jet rate from production of SUSY particles in the final state.

Our conclusions are summarized in Sec. IV. We find that the hadron scattering data provide significant constraints on the existence of gluinos whose mass is less than the weak scale $\sim 100$ GeV. A large region of gluino parameter space is excluded by the global analysis independently of direct searches or other indirect methods. The quantitative lower bounds we obtain on the gluino mass must be stated in terms of the assumed value of the the strong coupling strength $\alpha_s(M_Z)$. For the standard model world-average value $\alpha_s(M_Z) = 0.118$, gluinos lighter than 12 GeV are disfavored. However, the lower bound on $m_{\tilde{g}}$ is relaxed to less than 10 GeV if $\alpha_s(M_Z)$ is increased above 0.120.

II. $\alpha_s$, PARTON DENSITIES, AND HARD-SCATTERING SUBPROCESSES

The presence of a light gluino $\tilde{g}$ and/or a light squark $\tilde{q}$ modifies the PDF global analysis in three ways. First, the gluino and squark change the evolution of the strong coupling strength $\alpha_s(Q)$ as the scale $Q$ is varied. Second, the gluino and squark provide additional partonic degrees of freedom that share in the nucleon’s momentum and affect the PDFs of the standard model partons, e.g., via the channels $g \rightarrow \tilde{g}\tilde{g}$ and $q \rightarrow \tilde{q}\tilde{g}$. Third, gluino and squark contributions play a role in the hard-scattering matrix elements for the physical processes for which data are analyzed and fitted. We discuss each of these modifications in the following three subsections.

A. Modified evolution and values of $\alpha_s(Q)$

The expansion of the evolution equation for $\alpha_s(Q)$ as a power series in $\alpha_s(Q)$ is

$$Q \frac{\partial}{\partial Q} \alpha_s(Q) = -\frac{\alpha_s^2}{2\pi} \sum_{n=0}^{\infty} \beta_n \left( \frac{\alpha_s}{4\pi} \right)^n$$

$$= - \left[ \beta_0 \frac{\alpha_s^2}{2\pi} + \beta_1 \frac{\alpha_s^3}{2^3\pi^2} + \ldots \right]. \quad (1)$$
When supersymmetric particles are included, the first two coefficients in Eq. (1) are (see, e.g., Ref. [20])

$$\beta_0 = 11 - \frac{2}{3} n_f - 2 n_{\tilde{g}} - \frac{1}{6} n_{\tilde{f}},$$

(2)

and

$$\beta_1 = 102 - \frac{38}{3} n_f - 48 n_{\tilde{g}} - \frac{11}{3} n_f + \frac{13}{3} n_{\tilde{g}} n_{\tilde{f}},$$

(3)

where $n_f$ is the number of quark flavors, $n_{\tilde{g}}$ is the number of gluinos, and $n_{\tilde{f}}$ is the number of squark flavors. Equation (2) shows that, to the leading order, one generation of gluinos $\tilde{g}$ contributes the equivalent of 3 quark flavors to the QCD $\beta$-function. The effect of one squark flavor is equivalent to one-fourth of the contribution of a quark flavor. In our work, we henceforth neglect the possibility of a light squark contribution to the $\beta$-function and limit ourselves to the effects of a light gluino. Inclusion of a light bottom squark changes the running of $\alpha_s$ slightly, compatible with current data [21, 22]. The modified coefficients $\beta_0$ and $\beta_1$ for $n_{\tilde{g}} = 1$ and $n_{\tilde{f}} = 0$ are implemented in our numerical calculation to full NLO accuracy.

In our global fit of hadron scattering data, the allowed range of the gluino mass $m_{\tilde{g}}$ depends strongly on the assumed value of the strong coupling $\alpha_s(M_Z)$. Therefore, it is important to understand the current experimental constraints on $\alpha_s(M_Z)$ from sources other than hadron scattering data. A combined analysis of all $Z$-pole data within the context of the standard model, carried out by a working group of members of the four CERN Large Electron-Positron Collider (LEP) experiments and the SLAC SLD experiment [23], obtains the value $\alpha_s(M_Z) = 0.1187 \pm 0.0027^1$. This value is but a shade greater than the often-quoted standard model world-average value $\alpha_s(M_Z) = 0.1183 \pm 0.0027$ [24] obtained from a variety of determinations of $\alpha_s(Q)$ at different momentum scales $Q$. On the other hand, the value of $\alpha_s(Q)$ extracted from data in the context of supersymmetric contributions can be different from the value obtained in standard model fits. Some of the assumptions made in a standard model analysis are modified by the presence of the supersymmetric contributions [6, 25, 26, 27], and the value of $\alpha_s(Q)$ at $Q = M_Z$ obtained in standard model analyses may have to be be revised. A recent estimate [27] of SUSY effects on directly

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1 See Table 16.2 of Ref. [23].
measured $\alpha_s(M_Z)$ finds values in the interval $(0.118 - 0.126) \pm 0.005$, where the variation in the central value arises from uncertainty in the magnitude of SUSY-QCD corrections to the $Z$-boson decay width from processes such as $Z \to \bar{b}b\tilde{g}$ and $Z \to \bar{\tilde{b}}b\tilde{g}$. Further discussion of the evolution of $\alpha_s(Q)$ in the presence of light supersymmetric states may be found in the Appendix.

In a general purpose CTEQ fit, $\alpha_s(M_Z)$ is fixed to be equal to its world-average value, determined from a combination of the $\tau$-lepton decay rate, LEP $Z$ pole observables, and other measurements. As discussed above, this value may change in the presence of light superpartners. To explore fully the range of strong coupling strengths compatible with the global fit, we perform a series of fits in which $\alpha_s(M_Z)$ is varied over a wide range $0.110 \leq \alpha_s(M_Z) \leq 0.150$. We then determine the values of $m_{\tilde{g}}$ and $\alpha_s(M_Z)$ preferred by the global fits.

**B. Implementation of a gluino in the NLO evolution of parton distributions**

In the construction of parton distributions, we include a light gluino and omit squark contributions. A squark enters parton splitting functions only in combination with another rare particle, and these splittings are characterized by smaller color factors than in the gluino case. We incorporate the gluino sector into the PDF evolution package used to build the CTEQ6 unpolarized parton distributions [7].

The standard procedure for extracting parton distribution functions from global QCD analysis is to parametrize the distributions at a fixed small momentum scale $Q_0$. The distributions at all higher $Q$ are determined from these by the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution equations [28, 29, 30]. The agreement with experiment is measured by an effective $\chi^2$, which can be defined by $\chi^2 = \sum_{\text{expts}} \chi^2_n$, or by generalizations of that formula to include published systematic error correlations. The PDF shape parameters at $Q_0$ are chosen to minimize $\chi^2$ and obtain the “best fit” PDFs.

We choose the starting value $Q_0$ for the QCD evolution equal to the smaller of the gluino mass $m_{\tilde{g}}$ or charm quark mass $m_c$. At the scale $Q = Q_0$, the only non-perturbative input distributions are those of the gluons $g$ and light ($u$, $d$, $s$) quarks. Non-zero PDFs of the gluinos and heavy quarks ($c$, $b$) are generated radiatively above their corresponding mass thresholds. In the CTEQ6 analysis, $Q_0$ coincides with the charm quark mass: $Q_0 = m_c = 1.3$
GeV. Therefore, for $m_{\tilde{g}} \geq m_c$ the input scale $Q_0 = 1.3$ GeV is the same as in the CTEQ6 study. We use the CTEQ6 functional forms for the input PDFs of the standard model partons at $Q = Q_0$, but the starting values of the parameters are varied in order to obtain acceptable fits to the full set of scattering data.

The prescription for $Q_0$ allows us to investigate the possibility of gluinos lighter than charm quarks ($m_{\tilde{g}} < m_c$). We include fits for gluino masses $0.7 \leq m_{\tilde{g}} \leq 1.3$ GeV by choosing $Q_0 = m_{\tilde{g}}$. Such super-light gluinos may be generated both via perturbative and nonperturbative mechanisms, and, in principle, an independent phenomenological parametrization must be introduced for the gluino PDF to describe nonperturbative contributions. Our prescription for the region $m_{\tilde{g}} < m_c$ provides a particular model for such an input gluino parametrization, similar in its spirit to the dynamical parton distributions of the GRV group [31], as well as the procedure used in earlier light gluino analyses [18] and [19].\footnote{In Ref. [19], the PDFs are obtained from the procedure described here, but at LO and without inclusion of the jet production data, for $m_{\tilde{g}} = 0.5$ and 1.6 GeV.}

In the presence of a light gluino, the DGLAP equations must be extended to account for the new processes. The coupled evolution equations take the form

$$Q^2 \frac{d}{dQ^2} \begin{pmatrix} \Sigma(x, Q^2) \\ g(x, Q^2) \\ \tilde{g}(x, Q^2) \end{pmatrix} = \frac{\alpha_s(Q^2)}{2\pi} \times$$

$$\times \int_x^1 \frac{dy}{y} \begin{pmatrix} P_{\Sigma\Sigma}(x/y) & P_{\Sigma\tilde{g}}(x/y) & P_{\Sigma\tilde{g}}(x/y) \\ P_{g\Sigma}(x/y) & P_{gg}(x/y) & P_{g\tilde{g}}(x/y) \\ P_{\tilde{g}\Sigma}(x/y) & P_{\tilde{g}g}(x/y) & P_{\tilde{g}\tilde{g}}(x/y) \end{pmatrix} \begin{pmatrix} \Sigma(y, Q^2) \\ g(y, Q^2) \\ \tilde{g}(y, Q^2) \end{pmatrix} ; \quad (4)$$

$$\Sigma(x, Q^2) = \sum_{i=u, d, s,...} (q_i(x, Q^2) + \bar{q}_i(x, Q^2)). \quad (5)$$

Here $\Sigma(x, Q^2)$, $g(x, Q^2)$, and $\tilde{g}(x, Q^2)$ are the singlet quark, gluon, and gluino distributions, respectively; $q_i(x, Q^2)$ and $\bar{q}_i(x, Q^2)$ are the quark and antiquark distributions for flavor $i$. The splitting functions $P_{ij}(x)$ may be found in the literature [32].

The inclusion of a gluino in the evolution equations complicates the calculation substantially. To achieve acceptable accuracy, evolution of the quarks and gluons must certainly be done at next-to-leading order accuracy. However, without a substantial loss in accuracy, we
can simplify the overall calculation by evaluating the gluino contributions to leading order accuracy only. We use the following prescription:

1. Evolve the ordinary quarks and gluons at NLO (so that the splitting functions $P_{\Sigma\Sigma}$, $P_{\Sigma g}$, $P_{g\Sigma}$, and $P_{gg}$ are evaluated to order $O(\alpha_s^2)$).

2. Evolve the gluinos at LO (so that the splitting functions $P_{g\tilde{g}}$, $P_{\Sigma\tilde{g}}$, $P_{\tilde{g}g}$, $P_{\tilde{g}\Sigma}$, and $P_{\tilde{g}\tilde{g}}$ are evaluated to $O(\alpha_s)$). In particular, at LO (and in the absence of the squarks), $P_{\tilde{g}\Sigma} = P_{\Sigma\tilde{g}} = 0$.

3. For the evolution of $\alpha_s$, use the full NLO ($O(\alpha_s^2)$) expression, including the effect of the gluino.

In this prescription, the evolution is fully accurate to NLO except for the gluino splitting kernels. Were we interested in a process dominated by gluino contributions, we might need a NLO representation of the gluino PDF, $\tilde{g}(x, Q^2)$. However, the impact of the gluino PDF is minimal for the inclusive data in the global analysis, since $\tilde{g}(x, Q^2)$ is much smaller than the quark and gluon PDFs (cf. Figs. 1 and 2). As a result, the gluino plays only an indirect role. Its presence modifies the fit in two ways:

1. The gluino alters $\alpha_s(Q)$, thereby modifying the evolution of ordinary quark and gluon PDFs.

2. The gluino carries a finite fraction of the hadron’s momentum, thereby decreasing the momentum fraction available to the gluons and standard model quarks.

Regarding item (1), we compute the effects of the gluino correctly by using the exact NLO beta function that includes SUSY effects. Therefore, the only shortcoming of our prescription is with respect to item (2). We describe correctly the NLO mixing between the quarks and the gluons, but the less consequential mixing of the standard model partons and the gluino is correct only to leading order. In the energy range of our interest, the gluinos carry a small fraction ($\lesssim 5\%$) of the proton’s momentum. The neglected NLO corrections to this small quantity are further suppressed by a factor of $\alpha_s/\pi$. They are comparable in magnitude to the NNLO corrections for the standard model splittings, which are suppressed by $\alpha_s^2/\pi^2$. The uncertainty introduced by the omission of the NLO gluino splittings is
comparable to that due to the NNLO corrections for other particles, and it may be ignored in the present NLO analysis.

Figures 1 and 2 illustrate and support our assumptions. They show the momentum distributions for the gluons, singlet quarks, and gluinos, respectively. In these figures, the strong coupling strength $\alpha_s(M_Z)$ is equal to 0.118 (the value of $\alpha_s(M_Z)$ assumed in the CTEQ6 analysis). The momentum scale $Q$ is 10 GeV in Fig. 1 and 100 GeV in Fig. 2. The abscissa (x-axis) is scaled as $x^{1/3}$ in these plots of the dependence on the momentum fraction $x$. The distributions are obtained from the light gluino (LG) fits for $m_{\tilde{g}} = 10$ GeV, with or without the inclusion of the Tevatron jet data. For $xg(x, Q^2)$ and $x\Sigma(x, Q^2)$, we also show the corresponding distributions from the best-fit set CTEQ6M of the CTEQ6 analysis.

With $Q = m_{\tilde{g}} = 10$ GeV, the gluino density $x\tilde{g}(x, Q^2) = 0$. Nevertheless, the effects of gluino contributions on the fit at $Q > 10$ GeV force a change in the gluon and quark distribution functions from their standard model values at $Q = m_{\tilde{g}} = 10$ GeV, as shown in Fig. 1. Once $Q$ is evolved to 100 GeV, Fig. 2 shows a nonzero momentum distribution for the gluinos and a persistent change of the gluon and quark densities from their CTEQ6M standard model values.

The figures demonstrate two important features. First, the magnitude of the gluino distribution is much smaller than the gluon and quark distributions. This large difference justifies the assumptions that contributions are small from scattering subprocesses with initial-state gluinos, and that NLO gluino contributions may be omitted in our analysis.

Second, the presence of the gluino depletes the gluon distribution at $x \gtrsim 0.05$. The effect on the singlet distribution is less pronounced. The gluinos take their momentum (3.7% of the proton’s momentum at $Q = 100$ GeV for $m_{\tilde{g}} = 10$ GeV) from the gluons (3.0%) principally, less from quarks (0.7%), independently of whether the Tevatron jet data are included in the fit. Since the jet data at large transverse energy $E_T$ are known to probe the behavior of $g(x, Q^2)$ at large $x$, i.e., in the region where the depletion of the gluon’s momentum is the strongest, we judge that inclusion of the jet data in the fit strengthens the constraining power of the fit.
FIG. 1: The gluon and singlet momentum distributions $xg(x,Q^2)$ and $x\Sigma(x,Q^2)$ are displayed as functions of $x$ at $Q = 10$ GeV with $\alpha_s(M_Z) = 0.118$ and $m_{\tilde{g}} = 10$ GeV. The curves show the conventional CTEQ6M fit (solid) and the LG solutions with (short-dashed) and without (long-dashed) the Tevatron jet data included in the data set.

C. Gluino contributions to hard scattering

Once light superpartners are introduced as degrees of freedom, we must consider their impact on all hard scattering processes. Their effects can be felt both at tree level and in virtual-loop diagrams. At leading order in perturbation theory, we may consider hard subprocesses initiated by light gluinos or light bottom squarks that are constituents of the initial hadrons, as well as subprocesses in which gluinos or bottom squarks are emitted in the final state. We evaluate SUSY contributions to the hard matrix elements at leading order only for the same reasons that justify the omission of NLO SUSY contributions to the splitting kernels in Sec. II B.

The CTEQ6 fit is performed to data from lepton-nucleon deep-inelastic scattering (DIS), vector boson production (VBP), and hadronic jet production at the Tevatron. In DIS and VBP, the lowest-order contribution from gluinos is $\gamma^* + g \rightarrow \tilde{q} + \tilde{g}$ at order $\mathcal{O}(\alpha_s)$. This subprocess proceeds via squark exchange, and its contribution can be neglected as being much smaller than the Born-level QCD subprocesses (which contribute at order $\mathcal{O}(\alpha_s^0)$). The
FIG. 2: The gluon, singlet, and gluino momentum distributions $xg(x, Q^2)$, $x\Sigma(x, Q^2)$, and $x\tilde{g}(x, Q^2)$ are displayed as functions of $x$ at $Q = 100$ GeV with $\alpha_s(M_Z) = 0.118$ and $m_{\tilde{g}} = 10$ GeV. The curves show the conventional CTEQ6M fit (solid) and the LG solutions with (short-dashed) and without (long-dashed) the Tevatron jet data included in the data set.

bottom squarks can contribute at $\mathcal{O}(\alpha_s^0)$ through the subprocesses $\tilde{b} + \gamma^* \rightarrow \tilde{b}$ in DIS and $\tilde{b} + \tilde{b}^* \rightarrow \gamma^*$ in the Drell-Yan process. However, these contributions appear in a combination with a small bottom squark PDF $\tilde{b}(x, Q^2)$ and, therefore, are also negligible. We conclude that Born-level SUSY contributions appear only in the Tevatron jet production data, while, to the assumed level of accuracy, the hard matrix elements in DIS and VBP remain the same as in the SM case.

We now consider the influence that gluino subprocesses may have on the rate for jet production at large values of transverse energy $E_T$. Gluinos are color-octet fermions and, produced in the the final state, they materialize as jets. Since the gluino parton density is relatively large only at small values of fractional momentum $x$ and, as illustrated in Figs. [1]
and 2 is small even there when compared with the gluon and light-quark densities, we are justified in neglecting the contributions to the large $E_T$ jet rate from subprocesses initiated by two gluinos. An example is $\tilde{g} + \tilde{g} \rightarrow g + g$. However, in the interest of completeness, we include two subprocesses initiated by one gluino: $g + \tilde{g} \rightarrow g + \tilde{g}$, and $q + \tilde{g} \rightarrow q + \tilde{g}$. Subprocesses initiated by gluons and/or light quarks can be important. We include $g + g \rightarrow \tilde{g} + \tilde{g}$ via either a direct channel gluon or a cross channel gluino, and $q + \bar{q} \rightarrow \tilde{g} + \tilde{g}$ via a direct channel gluon. We can ignore the $t$-channel exchange diagrams that contribute to $q + \bar{q} \rightarrow \tilde{g} + \tilde{g}$. With the possible exception of the bottom squark, the masses of most squarks are so large that the relevant $t$-channel amplitudes are negligible. In the case of bottom squark exchange, the two initial-state partons would be bottom quarks, with small parton densities. For similar reasons, we may also ignore subprocesses such as $q + g \rightarrow \tilde{g} + \tilde{q}$.

At the Tevatron $p\bar{p}$ collider, the $q\bar{q}$ partonic luminosity is relatively large in the region of large $E_T$, and one might expect naively that the subprocess $q + \bar{q} \rightarrow \tilde{g} + \tilde{g}$ would increase the jet rate significantly. However, just as for the direct channel gluon subprocess $q + \bar{q} \rightarrow q' + \bar{q}'$ in standard QCD, the squared matrix element for $q + \bar{q} \rightarrow \tilde{g} + \tilde{g}$ is relatively small.

In our treatment of jet production, we compute the matrix elements for the SUSY-QCD subprocesses at leading order. Working at large $E_T \gg m_{\tilde{g}}$, we neglect the gluino mass in the calculation. We include these matrix elements as additional contributions to the jet rate in the fitting program, adding them to those of the NLO standard model QCD processes [$O(\alpha_s^3)$] to obtain constraints from the inclusive jet data.

As indicated in the previous subsection, inclusion of a light gluino in the PDF set removes momentum from the gluon PDF at large $x$, tending to depress the contribution from SM processes to the jet rate at large $E_T$. However, as we show, the effect is compensated partially by a larger value of $\alpha_s(M_Z)$, by slower evolution of $\alpha_s$ that makes $\alpha_s(E_T > M_Z)$ larger than in the standard model, and by contributions to the jet rate from production of SUSY particles in the final state.

III. PRESENTATION OF THE GLOBAL FITS

Our global fits are made to the complete set of data used in the CTEQ6 analysis, for several fixed values of the gluino mass. At this stage of the analysis, we do not impose a value of $\alpha_s(M_Z)$, preferring to determine a range of values directly from the global analysis.
of hadronic scattering data. We perform fits to the hadronic data with $\alpha_s(M_Z)$ set equal to one of several selected values in the range $0.110 \leq \alpha_s(M_Z) \leq 0.150$. As discussed in Sec. II C, jet production at the Tevatron is the only process among those we include that acquires Born-level contributions from the light gluinos. Most of the figures presented are for fits to the full set of data. To gauge the effect of the jet data, we also show results of additional fits that do not include these data. The numbers of experimental points in the fits with (without) the Tevatron jet data are 1811 (1688).

**A. Contour plots of $\Delta \chi^2$ vs $\alpha_s$ and $m_{\tilde{g}}$**

The principal result of our analysis is shown in Fig. 3. It maps the region of acceptable values of $\chi^2$ in the plane of $\alpha_s(M_Z)$ and $m_{\tilde{g}}$. The contour plot shows the difference $\Delta \chi^2 \equiv \chi^2(\alpha_s, m_{\tilde{g}}) - \chi^2|_{\text{CTEQ6M}}$, between the value of $\chi^2$ obtained in our LG fit and the standard model result equivalent to the CTEQ6M fit. The point in the plane corresponding to the CTEQ6M fit ($\alpha_s(M_Z) = 0.118$ and $m_{\tilde{g}} \to \infty$) is marked by the arrow. 3 The variation of $\chi^2$ in the neighborhood of the minimum is used to estimate limits of uncertainty.

An overall tolerance parameter $T$ and a condition $\Delta \chi^2 < T^2$ are used in the CTEQ6 analysis to characterize the acceptable neighborhood around the global minimum of $\chi^2$ in the parton parameter space. The quantitative estimate $T = 10$ is obtained from a combination of the constraints placed on acceptable fits by each individual experiment included in the fit. 4

According to the tolerance on $\Delta \chi^2$ of the CTEQ6 analysis, a fit is strongly disfavored if $\Delta \chi^2 > 100$. The isoline corresponding to $\Delta \chi^2 = 100$ is shown in Fig. 3 by the solid line. The acceptable fits lie inside a trough that extends from large gluino masses and $\alpha_s(M_Z) = 0.118$ down to $m_{\tilde{g}} \approx 0.8$ GeV and right to $\alpha_s(M_Z) = 0.145$. An even narrower area corresponds to fits with $\chi^2$ close to those in the CTEQ6M fit. We note that $\chi^2$ is better than in the

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3 The best-fit value $\alpha_s(M_Z) = 0.117$ in the CTEQ6 fit is slightly below the world-average value $\alpha_s(M_Z) = 0.118$ assumed in the CTEQ6M PDF set.

4 The tolerance $T = 10$ is estimated from the degree of consistency between the various data sets in the global fit. It includes effects due to experimental uncertainty and uncertainties that are of theoretical or phenomenological origin. It is an oversimplification to represent all uncertainties of PDFs and their physical predictions by a single number $T$. However, given the complexity of the problem, it is unrealistic to be more precise at this stage. The criterion $T = 10$ must be used with awareness of its limitations.
CTEQ6M fit in a small area in which $m_{\tilde{g}} \lesssim 20$ GeV and $\alpha_s(M_Z) > 0.125$, with the minimum $\Delta\chi^2 \approx -25$ at $m_{\tilde{g}} = 8$ GeV and $\alpha_s(M_Z) = 0.130$. This negative excursion in $\Delta\chi^2$ is smaller than the tolerance $T^2$ and should therefore not be interpreted as evidence for a light gluino.

A substantial region of $\alpha_s(M_Z)$ and $m_{\tilde{g}}$ is excluded by the criterion $\Delta\chi^2 < 100$. For $\alpha_s(M_Z) = 0.118$, gluinos lighter than 12 GeV are disfavored. However, the lower bound on $m_{\tilde{g}}$ is relaxed to less than 10 GeV if $\alpha_s(M_Z)$ is increased above 0.120.

In Fig. 3, the positions are marked of the points \{\alpha_s(M_Z), m_{\tilde{g}}\} of the best fits in earlier PDF analyses with a light gluino [16, 17, 18, 19]. Most of these earlier solutions are excluded by the present data set, with the exception of the fits corresponding to $m_{\tilde{g}} = 5$ GeV and large $\alpha_s(M_Z) = 0.124, 0.129$, and 0.134 [16, 17].

Another perspective is provided by a plot of $\chi^2$ vs. $m_{\tilde{g}}$ for several fixed values of $\alpha_s(M_Z)$, shown in Fig. 4. The dependence on $m_{\tilde{g}}$ is observed to be quasi-parabolic, with a shift of the minimum of $\chi^2$ to lower $m_{\tilde{g}}$ as $\alpha_s(M_Z)$ increases. When $\alpha_s(M_Z)$ is close to the current world-average value of 0.118, the fit prefers a heavy gluino, or no gluino at all. Very light gluinos are strongly disfavored, and the bound $m_{\tilde{g}} > 12$ GeV is obtained for $\Delta\chi^2 < 100$. For $\alpha_s = 0.122$ and 0.124, the corresponding bounds are $m_{\tilde{g}} > 5$ GeV and $m_{\tilde{g}} > 3$ GeV, respectively.

Conversely, for a very large $\alpha_s(M_Z)$ (> 0.127), the pattern is reversed, and lighter gluinos ($m_{\tilde{g}} < 50$ GeV) are preferred. In the transition region of $\alpha_s(M_Z)$ about 0.127, both very light and very heavy gluinos are disfavored, and a gluino mass in the range 10 to 20 GeV yields a slightly better $\chi^2$ than in the CTEQ6M fit. For a very small gluino mass of 1.3 to 5 GeV, the minimum in $\chi^2$ is achieved for $\alpha_s(M_Z)$ about 0.135, while even larger values of $\alpha_s(M_Z)$ are disfavored as well (c.f. the curves for $\alpha_s = 0.140$ and 0.145).

The behavior of $\chi^2$ in Figs. 3 and 4 exhibits irregular structure when the gluino mass lies in the range 50 to $\sim 200$ GeV. These gluino masses lie beyond the range of sensitivity of the data sets in the fit, with the exception of the Tevatron jet data at jet transverse energies $E_T > 2m_{\tilde{g}}$. Variations in $\chi^2$ at high gluino masses are caused by an interplay between the gluino mass and individual CDF and DØ jet data points. Contributions from gluinos with masses of 100 – 140 GeV improve the description of very high-$E_T$ jet events, leading to a

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5 The points corresponding to fits with gluino mass $m_{\tilde{g}} < 0.7$ GeV in Refs. [17, 18, 19] are off scale and are not shown.

6 The irregularities of the contours are smoothed in Fig. 3.
FIG. 3: A contour plot of \( \Delta \chi^2 = \chi^2(\alpha_s(M_Z), m_{\tilde{g}}) - \chi^2|_{\text{CTEQ6M}} \) as a function of the strong coupling \( \alpha_s(M_Z) \) and gluino mass \( m_{\tilde{g}} \). The values of \( \Delta \chi^2 \) are shown by labels on the corresponding isolines. The shaded region is excluded by the CTEQ6 tolerance criterion. The points corresponding to the earlier PDF fits with a LG \([16, 17, 18, 19]\) are denoted by the symbols described in the legend. The solid line marks the \( \Delta \chi^2 = 100 \) isoline. The dashed completion of this line at the bottom of the contour plot corresponds to fits done with \( m_{\tilde{g}} = Q_0 \leq m_c = 1.3 \text{ GeV} \).

In summary, as \( \alpha_s(M_Z) \) increases, the window of allowed gluino masses shifts from high to low values. Very large values of \( \alpha_s(M_Z)(\gtrsim 0.148) \) can be ruled out for any gluino mass. Gluino masses between 10 and 20 GeV are allowed, as long as \( \alpha_s(M_Z) \) is not smaller than \( \sim 0.118 \).
FIG. 4: Dependence of $\chi^2$ on $m_{\tilde{g}}$ for several fixed values of $\alpha_s(M_Z)$ (denoted by labels on each corresponding line).

B. Exploration of the light gluino fits

The contour plot in Fig. 3 indicates that excellent fits to the global data can be obtained with a gluino mass below the weak scale, $m_{\tilde{g}} \lesssim 100$ GeV, provided that $\alpha_s(M_Z)$ is allowed to increase above the nominal value $\alpha_s(M_Z) = 0.118$. It is instructive to examine the compensating effects of $\alpha_s(M_Z) > 0.118$ and finite gluino mass on the parton distribution functions themselves.

In Fig. 3, the ratio shown as a dashed line provides a comparison of the gluon distribution $g(x, Q^2)$ at $Q = 15$ GeV and gluino mass $m_{\tilde{g}} = 15$ GeV with $g(x, Q^2)$ in the CTEQ6M fit (without gluinos). The strong coupling $\alpha_s$ at the scale $M_Z$ is chosen to be the same as in the CTEQ6M fit, $\alpha_s(M_Z) = 0.118$. The ratio shows that, as the gluino mass is decreased below the weak scale, $g(x, Q^2)$ is depleted at large $x$ and increased at small $x$. This softening of the gluon distribution follows from the slower evolution of $\alpha_s(Q)$, as well as from the presence of the additional coupling $g \rightarrow \tilde{g}\tilde{g}$.
FIG. 5: Illustration of the compensation in the gluon density that arises between an increase in \( \alpha_s(M_Z) \) and a finite gluino mass. Shown are the ratios of the gluon density in the LG solution divided by the CTEQ standard model best fit \((m_{\tilde{g}} = \infty \) and \( \alpha_s(M_Z) = 0.118 \)) at \( Q = 15 \) GeV. The gluino mass is \( m_{\tilde{g}} = 15 \) GeV or \( m_{\tilde{g}} = \infty \), as specified in the figure. The CTEQ6 uncertainty band is shown by the dotted lines.

For the same \( \alpha_s(M_Z) \), the magnitude of \( \alpha_s(Q) \) at scales \( Q < M_Z \) is smaller in the LG case than in the SM case (cf. Fig. 12b). Correspondingly, PDF evolution is slower in the LG case. To some degree, the effects of the slower backward evolution can be compensated by selection of a larger value of \( \alpha_s(M_Z) \). In some range of \( m_{\tilde{g}} \) and \( \alpha_s(M_Z) \), the effects of a smaller light gluino mass can be offset by a larger value of \( \alpha_s(M_Z) \). This statement is illustrated by the dot-dashed curve in Fig. 5. The dot-dashed curve shows the ratio of the gluon density for \( m_{\tilde{g}} = \infty \) and \( \alpha_s(M_Z) \) increased arbitrarily to 0.127, divided by the SM CTEQ6M result \((m_{\tilde{g}} = \infty \) and \( \alpha_s(M_Z) = 0.118 \)). The comparison shows that, when \( \alpha_s(M_Z) \) is increased, \( g(x, Q^2) \) is enhanced at large \( x \) and depleted at small \( x \). The solid line in Fig. 5 shows that, by lowering \( m_{\tilde{g}} \) below 100 GeV for a fixed \( \alpha_s(M_Z) \), we can approximately cancel the effect of increasing \( \alpha_s(M_Z) \) at a fixed \( m_{\tilde{g}} \). The solid line lies within the band of uncertainty of the
CTEQ6 gluon density, indicative of a fit of good quality. The cancellation breaks down at very large $\alpha_s(M_Z)$.

A similar cancellation between the effect of a small $m_{\tilde{g}}$ and increased $\alpha_s(M_Z)$ is apparent in the singlet quark PDF. Consequently, a region exists at small $m_{\tilde{g}}$ and large $\alpha_s(M_Z)$ where the resulting PDFs remain close to those in the CTEQ6M fit. If $\alpha_s(M_Z)$ is allowed to float freely in the fit, one can obtain PDFs similar to the CTEQ6M PDFs for all values of $m_{\tilde{g}}$ above 0.8 GeV. For $m_{\tilde{g}} \gtrsim 150$ GeV, the PDFs are practically the same as in the CTEQ6M fit, indicating that the current inclusive hadronic data are not sensitive to such heavy particles.

C. Impact of various data sets

To appreciate which data are the most restrictive in our fits, we examine the roles played in the fit by the hadronic jet data and other experiments.

1. Tevatron jet data

The Tevatron jet data places important constraints on $m_{\tilde{g}}$. In the absence of the jet data, the lower limit on $m_{\tilde{g}}$ is weaker, with $m_{\tilde{g}} \gtrsim 5$ GeV at $\alpha_s(M_Z) = 0.118$ if the jet data are omitted, but $m_{\tilde{g}} \gtrsim 12$ GeV if the jet data are included.

Comparisons between theory and the inclusive jet data from the CDF Collaboration [33] and the DØ Collaboration [34, 35] are shown in Fig. 6 and Figs. 7-9. The results are from a series of fits for fixed $\alpha_s(M_Z) = 0.118, 0.122, \text{and } 0.124$. These three values of $\alpha_s(M_Z)$ represent roughly the world-average central value and the values that are approximately one and two standard deviations larger. The CDF data are rescaled by 1.06, to account for differences in the measured luminosity used by the CDF and DØ Collaborations for the run-I data sample. The SM CTEQ6M fit with $\alpha_s(M_Z) = 0.118$ provides a good description of the data. For $\alpha_s(M_Z) = 0.118$ and $m_{\tilde{g}} = 15 - 25$ GeV, the theoretical cross sections are below the data due to the depletion of the gluon PDF at large momentum fractions $x$ (Fig. 5). The gluon depletion can be counterbalanced in a wide range of $m_{\tilde{g}}$ by a larger value of $\alpha_s(M_Z)$. The best fits correspond to combinations of $\alpha_s$ and $m_{\tilde{g}}$ near the bottom of the trough in $\Delta \chi^2$ in Fig. 3. For gluinos in the range 10-25 GeV, an acceptable fit is possible if $\alpha_s(M_Z)$ is increased to about 0.124.
FIG. 6: Comparison of theoretical predictions with the CDF inclusive jet data. The data points show the ratio \((\text{Data}-\text{CTEQ6M})/\text{CTEQ6M}\), where Data denotes the CDF measurements, and CTEQ6M is the SM prediction based on the CTEQ6M PDFs. The curves show the ratio \((\text{Theory}-\text{CTEQ6M})/\text{CTEQ6M}\), where the Theory curves are the calculations based on the LG PDFs, for \(\alpha_s(M_Z) = 0.118, 0.122, \) and \(0.124\), and gluino masses \(m_{\tilde{g}} = \{15, 25, 100\} \) GeV. The solid curves correspond to the SM fits (effectively \(m_{\tilde{g}} = \infty\)) for the indicated choices of \(\alpha_s(M_Z)\). The horizontal scale shows the transverse energy \(E_T\) of the jet in GeV units.

Contributions from gluinos increase the jet cross sections at \(E_T > 2m_{\tilde{g}}\). A new channel for hard scattering is opened, and the evolution of \(\alpha_s(Q)\) is slower. For \(\alpha_s(M_Z) = 0.118\), a heavy gluino in the range \(100 - 140\) GeV improves agreement of theory with the Tevatron jet data in the high-\(E_T\) tail by augmenting the rate of the tightly constrained standard model contributions. Better agreement for \(m_{\tilde{g}} = 100\) GeV (dashed line) is visible in the high-\(E_T\) region in Figs. 6(a) and 7. Below the gluino threshold, the theory prediction (derived from the fit to the data insensitive to gluino contributions) is identical to the CTEQ6M fit. While \(\chi^2\) for the DØ data set is visibly improved (cf. Fig. 10), the reduction of the overall \(\chi^2\) by 20 units is not statistically significant. It will be interesting to see whether the trend in favor
of contributions from gluinos (or other new color-charged fermions) with masses around 100 GeV is preserved in the jet data from run-II at the Tevatron.
FIG. 8: Same as in Fig. 7 for $\alpha_s(M_Z) = 0.122$. The solid curves correspond to the SM fit for $\alpha_s(M_Z) = 0.122$.

2. Plots of the data sets vs $\chi^2$

To investigate further the influence of various sets of data, we display the ratios $\chi^2/\chi^2_{CTEQ6M}$ for individual experiments. Results for $\alpha_s(M_Z) = 0.118$ are shown in Fig. 10 and those for $\alpha_s(M_Z) = 0.135$ in Fig. 11. The choice of the extreme value $\alpha_s(M_Z) = 0.135$ is made to accentuate the effects we want to demonstrate. In Fig. 10, we observe that, in addition to the jet data (sets (n) and (o)), the DIS data from the H1 Collaboration (sets
FIG. 9: Same as in Fig. 7 for $\alpha_s(M_Z) = 0.124$. The solid curves correspond to the SM fit with $\alpha_s(M_Z) = 0.124$.

(c) and (d)) and the CCFR $F_2$ measurement (set (i)) tend to drive the gluino mass to large values when $\alpha_s(M_Z) = 0.118$. On the other hand, in Fig. 11 we see that several sets of data are accommodated better with a light gluino if $\alpha_s(M_Z)$ is large.

If $\alpha_s(M_Z)$ is chosen between 0.118 and 0.135, the behaviors of the values of $\chi^2$ for individual experiments follow a mixture of the patterns shown in Figs. 10 and 11. Several data sets disallow very small and very heavy gluino masses, while gluinos in the intermediate mass range are accommodated well by the fit.
D. Section summary and momentum fractions

If $\alpha_s(M_Z)$ is allowed to vary freely, reasonable fits to the global data set are possible for essentially any gluino mass above $\sim 1$ GeV. However, if $\alpha_s(M_Z)$ is constrained from other sources, say, $\tau$ decay or direct measurements at $M_Z$, then a global fit to scattering data imposes good constraints on $m_{\tilde{g}}$. This situation is reminiscent of the strong correlation between the gluon PDF and $\alpha_s$ observed in previous analyses of parton densities \[48, 49\]. Similarly, it is not surprising that constraints on the gluino mass are coupled to our knowledge of the
The principal uncertainties on our quoted bounds on the gluino mass arise from neglect of NLO supersymmetric contributions to the PDF evolution (affecting the PDFs at a percent level), neglect of NLO SUSY-QCD corrections to jet production, and the limited precision of the criterion $\Delta \chi^2 < 100$ for the selection of acceptable fits. The lower limit on the gluino mass can be relaxed if the NLO virtual-loop SUSY-QCD corrections enhance the rate of the standard model subprocesses in the Tevatron jet production. These uncertainties can be reduced in future analyses.

We conclude this section with Table I, in which we show the fraction of the proton’s momentum carried by its constituents, in both the standard model CTEQ6M fit and in the LG fit with $m_{\tilde g} = 15$ GeV and $\alpha_s(M_Z) = 0.122$. 

FIG. 11: Same as in Fig. 10 for $\alpha_s(M_Z) = 0.135$. 

gluon PDF (constrained by the hadronic jet data) and $\alpha_s(M_Z)$. 

TABLE I: Fractions of the proton’s momentum carried by different parton species at $Q = 100$ GeV in the CTEQ6M fit ($m_{\tilde{g}} \to \infty$ and $\alpha_s(M_Z) = 0.118$) and in the LG fit with mass $m_{\tilde{g}} = 15$ GeV and $\alpha_s(M_Z) = 0.122$.

| Parton type | CTEQ6M | $m_{\tilde{g}} = 15$ GeV, $\alpha_s(M_Z) = 0.122$ |
|-------------|---------|--------------------------------------------------|
| $u + \bar{u}$ | 25.2    | 25.4                                             |
| $d + \bar{d}$ | 15.4    | 15.5                                             |
| $s + \bar{s}$ | 5.3     | 5.1                                              |
| $c + \bar{c}$ | 3.9     | 3.6                                              |
| $b + \bar{b}$ | 2.5     | 2.3                                              |
| $\Sigma$    | 52.3    | 51.9                                             |
| $g$         | 47.5    | 44.7                                             |
| $\tilde{g}$ | 0       | 3.2                                              |
| Total:      | 100     | 100                                              |

**IV. SUMMARY**

Our new analysis of the compatibility of a light gluino with inclusive scattering data goes beyond earlier studies [16, 17, 18, 19] in a number of aspects. First, the current data are strikingly more extensive than available ten years ago. They cover both small-$x$ and large-$Q$ regions, come from a variety of experiments, and are characterized by high precision. The primary effects of a gluino in the global analysis are changes in the evolution of the strong coupling strength and changes in the evolution of the parton distributions. It is easier to observe these changes in a data sample with large lever arms in $Q$ and $x$.

Second, in contrast to previous studies, our fit includes the complete set of data from the CTEQ global analysis, including the Tevatron jet production data. The major role of the jet data is to constrain the gluon density at large values of fractional momentum $x$. The behavior of the gluon density at large $x$ is affected strongly by the presence of the gluinos in the mix. Because they are sensitive to gluons at large $x$, the jet data enhance the discriminating power of the global fit. When the gluino mass changes, large variations in $\chi^2$ are observed, an influence that can be used to constrain the gluino parameter space. In
view of the strong correlations between the gluino mass, $\alpha_s(M_Z)$, and the gluon distribution, the constraints can be determined only after a consistent implementation of SUSY effects throughout all stages of the analysis.

The third new component in our study is a method for quantitative interpretation of uncertainties in parton distributions. With the help of this method, constraints on the acceptable gluino mass can be imposed on the basis of the values of $\chi^2$ obtained in the fits. The main result of the paper is presented in Fig. 3. It shows the region of the gluino masses $m_{\tilde{g}}$ and QCD coupling strengths $\alpha_s(M_Z)$ allowed by the present data. The standard model fit prefers $\alpha_s(M_Z) \approx 0.118$. Gluinos with mass of a few GeV can be accommodated only if $\alpha_s(M_Z)$ is increased. For example, gluinos with mass below 1 GeV are admissible only if $\alpha_s(M_Z)$ is about 0.130 or larger. If one takes into account the effects of a light gluino on the measurement and running of $\alpha_s$, it is hard (if at all possible) to reconcile such a large value of $\alpha_s(M_Z)$ with both low- and high-energy electroweak data.

On the other hand, a possibility remains open for the existence of gluinos with mass between 10 to 20 GeV, with a moderately increased $\alpha_s$ ($\alpha_s(M_Z) > 0.119$). This possibility is even slightly favored by the $\chi^2$ of the global fit. A model with light gluinos and bottom squarks is not incompatible with the results of our PDF analysis. Tighter constraints can be obtained in the near future, when new data from HERA and the Tevatron become available. In particular, it will be intriguing to see whether higher statistics jet data at larger values of $E_T$ show indications of physics beyond the standard model. The constraints we obtain depend on the value of $\alpha_s(M_Z)$. Uncertainties in the value of $\alpha_s(M_Z)$ could be reduced through a consistent determination of $\alpha_s(M_Z)$ from the CERN LEP data in a SUSY-QCD analysis, in which the effects of superpartners are included in the data analyses and Monte-Carlo simulations.

Implementation of the gluino in our study relies only on the knowledge of its strong interactions, which are determined uniquely by supersymmetry. We consider only theoretically clean one-scale inclusive observables. In this sense, our constraint $m_{\tilde{g}} > 12$ GeV for $\alpha_s(M_Z) = 0.118$ should be compared to the constraint $m_{\tilde{g}} > 6.3$ GeV for the same value of $\alpha_s$ from the $Z$-boson width measurement. Tighter constraints on $m_{\tilde{g}}$ were quoted by the searches for traces of gluino hadronization and a study of jet shapes. Although important, these constraints are less general, since they involve assumptions about the gluino lifetime or deal with several momentum scales in the jet shape observables. Our
TABLE II: $\alpha_s(M_Z)$ derived by evolution from $\alpha_s(m_\tau) = 0.323 \pm 0.030$ \cite{24} for several gluino masses and in the standard model.

| $m_{\tilde{g}}$, GeV | $\alpha_s(M_Z)$       |
|----------------------|-----------------------|
| 10                   | 0.132 $\pm$ 0.004    |
| 25                   | 0.125 $\pm$ 0.004    |
| 50                   | 0.121 $\pm$ 0.004    |
| 90                   | 0.118 $\pm$ 0.003    |
| SM                   | 0.118 $\pm$ 0.003    |

study demonstrates the potential of global analysis to independently constrain new physics from hadron collider data.

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APPENDIX: STRONG COUPLING STRENGTH

In this appendix we discuss the quantitative changes that occur in the evolution of the strong coupling strength $\alpha_s(Q)$ in the presence of a light gluino in the spectrum. We consider compatibility of $\tau$ decay and LEP $Z$-pole measurements of $\alpha_s$, which constrain $\alpha_s(Q)$ at low and large momentum scales, respectively.

The measurement of $\alpha_s$ at LEP provides a constraint at scales of order of the $Z$-boson
FIG. 12: Dependence of $\alpha_s(Q)$ on the renormalization scale $Q$. The three data points shown are $\alpha_s(m_\tau) = 0.35 \pm 0.03$ \cite{54}, $\alpha_s(m_\tau) = 0.323 \pm 0.030$ \cite{24}, and $\alpha_s(M_Z) = (0.118 - 0.126) \pm 0.005$ \cite{27}.

In Fig. 12a, the average $\alpha_s(m_\tau) = 0.337$ of two experimental values at $Q = m_\tau$ is evolved to higher energies. In Fig. 12b, the central value $\alpha_s(M_Z) = 0.122$ of the interval at $Q = M_Z$ is evolved to lower energies. The thick solid line represents the Standard Model (SM) evolution in the absence of SUSY effects. The dashed series of curves are generated for gluino masses $m_{\tilde{g}} = 5, 10, \text{ and } 25$ GeV (shown by the labels on the corresponding curves).

mass $M_Z$, and the measurement of $\alpha_s$ in $\tau$-lepton decay provides a constraint at scales of order of the $\tau$-lepton mass $m_\tau$. If the gluino is substantially heavier than the $\tau$-lepton, its presence in the spectrum cannot affect the measurement of $\alpha_s$ in $\tau$ decay. Therefore, $\alpha_s(Q)$ measured at the scale $Q = m_\tau$ is the same as in the standard model. Its recently quoted values are $\alpha_s(m_\tau) = 0.35 \pm 0.03$ \cite{54} and $\alpha_s(m_\tau) = 0.323 \pm 0.030$ \cite{24}. On the other hand, the measurement of $\alpha_s(Q)$ at $Q = M_Z$ can be affected by light superpartners in the spectrum. The values obtained in standard model analyses may have to be revised. A recent estimate \cite{27} of SUSY effects on direct measurements of $\alpha_s(M_Z)$ finds values in the interval $(0.118 - 0.126) \pm 0.005$, where the variation in the central value arises from the uncertainty in the magnitude of SUSY-QCD corrections to the $Z$-boson decay width from processes such as $Z \rightarrow b\bar{b}g$ and $Z \rightarrow b\bar{b}\tilde{g}$.

The $\tau$-decay and LEP values of $\alpha_s(Q)$ must be related by the renormalization group equation. Figure 12a shows the evolution of $\alpha_s(Q)$ measured in $\tau$ decay to the energy of order $M_Z$ for different choices of the gluino mass. According to Eqs. (2) and (3), $\alpha_s(Q)$ evolves
more slowly in the presence of light gluinos. Forward evolution of $\alpha_s(m_\tau)$ in the LG case leads to a higher value at $Q = M_Z$ than in the standard model. Evolution of $\alpha_s(m_\tau) = 0.35 \pm 0.03$ results in $\alpha_s(M_Z) = 0.120 \pm 0.003$ in the standard model and $0.135 \pm 0.004$ for a gluino mass of 10 GeV. Table lists the values of $\alpha_s(M_Z)$ obtained by evolution from the $\tau$ decay value $\alpha_s(m_\tau) = 0.323 \pm 0.030$.

Alternatively, we may evolve $\alpha_s$ measured in Z-boson decay backward to energies of order $m_\tau$ (Fig. 12b). The resulting $\alpha_s(m_\tau)$ in the LG case is lower than in the standard model. If we use the central value $\alpha_s(M_Z) = 0.122$ from the interval $0.118 - 0.126$ of Ref. 27 as our starting point, we obtain $\alpha_s(m_\tau) = 0.367$ in the standard model and 0.266 for $m_{\tilde{g}} = 10$ GeV.

For the quoted experimental and theoretical uncertainties, the measurements of $\alpha_s$ at $m_\tau$ and $M_Z$ are incompatible at the one-standard deviation (1 $\sigma$) level if the gluino mass is less than about 5.8 GeV. For such gluino masses, the 1 $\sigma$ interval of $\alpha_s(M_Z)$ obtained by evolution from $\alpha_s(m_\tau)$ is above the 1 $\sigma$ interval for the LEP measurement. On the other hand, the $\tau$ decay and LEP data do agree at the 1 $\sigma$ level for a gluino heavier than 5.8 GeV, if $\alpha_s(M_Z)$ is at the upper end of the theoretical uncertainty range (i.e., $\alpha_s(M_Z) \sim 0.126 + 0.005$). Lower values of $\alpha_s(M_Z)$ increase the lower bound on $m_{\tilde{g}}$, but gluino masses in the range $10 - 25$ GeV are possible within the uncertainties, as long as the central value of $\alpha_s(M_Z)$ from LEP is not less than about 0.119.

Bounds on the gluino mass obtained from the global PDF fit depend on the value of $\alpha_s(M_Z)$ assumed in the fit. Gluino masses lighter than 6 GeV cannot agree simultaneously with the results of the global fit, $\tau$ decay, and LEP $Z$ pole measurements. Gluino masses as small as 10 GeV are consistent with values of $\alpha_s(Q)$ obtained from both $\tau$ decay and LEP data, if $\alpha_s(M_Z)$ is increased moderately compared to its SM world-average value of 0.118 $\pm$ 0.002.

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