Stellar companions to exoplanet host stars: Lucky Imaging of transiting planet hosts

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ABSTRACT

Observed properties of stars and planets in binary/multiple star systems provide clues to planet formation and evolution. We extended our survey for visual stellar companions to the hosts of transiting exoplanets by 21 stars, using the Lucky Imaging technique with the two AstraLux instruments: AstraLux Norte at the Calar Alto 2.2-m telescope, and AstraLux Sur at the ESO 3.5-m New Technology Telescope at La Silla. Typically a sensitivity to companions of magnitude difference $\Delta z' \approx 4$ is achieved at angular separation $\rho = 0.5''$ and $\Delta z' \gtrsim 6$ for $\rho = 1''$.

We present observations of two previously unknown binary candidate companions, to the transiting planet host stars HAT-P-8 and WASP-12, and derive photometric and astrometric properties of the companion candidates. The common proper motions of the previously discovered companion candidates with the exoplanet host stars TrES-4 and WASP-2 are confirmed from follow-up observations. A Bayesian statistical analysis of 31 transiting exoplanet host stars observed with AstraLux suggests that the companion star fraction of planet hosts is not significantly different from that of solar-type field stars, but that the binary separation is on average larger for planet host stars.

Key words: Techniques: high angular resolution - Binaries: visual - Planetary systems

1 INTRODUCTION

About half of solar-type stars in our neighbourhood are part of a binary or multiple system (Duquennoy & Mayor 1991; Raghavan et al. 2010). Understanding how a secondary star affects the formation and evolution of planets in the system is therefore of high importance for an estimate of the overall occurrence of planets in our Galaxy.

A close stellar companion is expected to affect planet formation in several ways, e.g., by heating and truncating the circumstellar protoplanetary disc (Artymowicz & Lubow 1994; Armitage, Clarke, & Tout 1994; Nelson 2001), or by increasing the relative velocities of the planetesimals (Heppenheimer 1974, 1978; Whitmire et al. 1998). A secondary star may either stimulate (Boss 2006) or hinder (Nelson 2000; Kley & Nelson 2002) planet formation. The occurrence and properties of planets formed in binary systems may also provide a way to discriminate between the two most widely supported planet formation models: core accretion (e.g., Pollack et al. 1996) and gravitational instability (e.g., Boss 1997; Mayer et al. 2002). For instance, formation by gravitational instability (GI) requires a massive disc for fragmentation to occur ($M > 0.1M_\odot$). Mayer et al. (2003) found that planet formation by GI in massive discs is not significantly different from formation around a single star if the binary separation is $> 120$ AU, while at close binary separations ($< 60$ AU) the high temperatures caused by shock heating effectively suppress fragmentation. Formation by core accretion, on the other hand, does not require a massive disc, and planets may form closer to their parent star without being much affected by a close binary companion. Therefore, a trend
of giant planet frequency with binary star separation, i.e., fewer giant planets in binary systems closer than 100 AU than in wider binaries or single systems, might point to GI as a main formation mechanism (Mawer et al. 2003).

Observations show that the frequency by which giant planets are formed in close binary stellar systems appears to be slightly lower than around single stars. Egenberger et al. (2008, 2011) found that giant planets are more common in single-star systems than in binaries separated by 35-100 AU. Nevertheless, surveys of multiplicity among planet host stars show that many exoplanet host stars are part of a binary or multiple system. We now know of ~50 binary or multiple systems where the planet(s) belong to one of the stars (S-type orbit), and Kepler observations recently revealed the first known planets that transit both stars in a close binary system, i.e., in a P-type orbit (Doyon et al. 2011, Welsh et al. 2012). System characteristics such as binary separation together with properties of the planets (orbital period, mass, eccentricity, etc.) and any differences compared to the properties of the single-star planetary systems provide important constraints on planet formation and dynamical system evolution. Among suggested correlations between stellar and planetary binaries, two appear significant: The most massive planets in short-period orbits belong to stars in binary systems, and so do the planets with the highest eccentricities (Desidera & Barbieri 2007; Sozzetti & Desidera 2011; Tamuz et al. 2008).

A significant fraction of exoplanets to date have been discovered using radial velocity measurements, and such systems have also been the subject of several multiplicity surveys (e.g., Patience et al. 2002; Chaumian et al. 2006; Egenberger et al. 2007; Mugrauer et al. 2007; Roberts et al. 2011; Mason et al. 2011; Ginski et al. 2012).

However, the discovery rate of transiting exoplanets (TEPs) has increased tremendously over the last couple of years, mainly due to the success of ground-based transit searches such as SuperWASP (Pollacco et al. 2006) and HATNet (Bakos et al. 2004), as well as space-based programs such as CoRoT (Baglin et al. 2006) and Kepler (Borucki et al. 2010). Transiting exoplanets are unique in the way that properties such as mass and radius can be measured, and a variety of additional physical parameters such as true mass, mean density and surface gravity can thus be derived, potentially providing information on planet formation (see, e.g., Mazeh, Zucker, & Pont 2003; Torres, Winn, & Holman 2008; Southworth 2004, 2010).

An unresolved faint secondary star within the photometric aperture, whether it is a bound companion or chance alignment, contributes a constant flux offset to the transit light curve and affects the accuracy with which stellar and planetary parameters can be derived. High resolution imaging of TEP hosts have shown that the presence of a (projected) nearby star may require a correction of derived stellar and planetary parameters between a few to several tens percent (Daemgen et al. 2009; Buchhave et al. 2011).

Another important aspect of transiting planets is that they allow for a measurement of the projected alignment between the orbital plane of the planet and the rotational plane of the star through the Rossiter-McLaughlin effect (e.g., Queloz et al. 2000). Studies using this effect have shown that many transiting hot Jupiters are significantly misaligned with respect to the stellar spin (e.g., Winn et al. 2010), which implies that three-body mechanisms such as Kozai migration (e.g., Fabrycky & Tremaine 2007) may be responsible for the formation of those systems, rather than classical orbital migration (e.g., Lin et al. 1996). Since the Kozai mechanism requires the presence of a wide stellar companion, it follows that searching for binarity among TEP hosts could provide important clues for the formation of hot Jupiter systems.

In this paper we present high resolution Lucky Imaging observations of 21 TEP host stars using the two AstraLux instruments at the 2.2 m telescope at Calar Alto and at NTT at La Silla. The observations complement the sample of TEP hosts presented by Daemgen et al. (2009), and are described in Sect. 2 together with the methods used for obtaining relative astrometry and photometry. All the transiting exoplanets in our survey transit only one star, in a short-period orbit. In Section 3 we derive magnitudes, $(i-z)$ colours, and photometric spectral types and distances to the companion candidates from the photometric observations in SDSS $i'$- and $z'$-band and known spectral types of the planet host stars. Evidence of physical companionship of the planet host stars and the companion candidates is investigated, and the results for each individual target are compared with previously published astrometric and photometric data if available. We estimate the probability of chance alignment and perform a Bayesian analysis of our complete observed sample of TEP hosts with AstraLux. The results are summarized and discussed in Sect. 4.
observed each night for calibration of the detector rotation and pixel scale. Field rotation and plate scale were derived using custom IDL routines to compute separation and position angle of the astrometric reference stars pairwise in several frames and compare to values derived from e.g. HST/WFPC2 archive images. The plate scale for the observations with AstraLux Norte was \(23.43 \pm 0.06\) mas/px with the detector rotated \(0.06 \pm 0.02^\circ\) east of north in October-November 2009 and plate scale \(23.74 \pm 0.05\) mas/px in November 2011 with a detector rotation of \(1.6 \pm 0.2^\circ\) to the east. For the AstraLux Sur instrument we derived a plate scale of \(15.373 \pm 0.002\) mas/px and detector rotation \(1.7 \pm 0.3^\circ\) to the west of north in November 2008 (see Bergfors et al. 2010), and \(15.245 \pm 0.006\) mas/px, \(1.4 \pm 0.2^\circ\) to the west in April 2009.

### 2.2 Photometry and astrometry

In the sample of 21 TEPs, we found candidate companion stars from visual inspection of the reduced Lucky Imaging frames to 7 stars: the previously known companion candidates to WASP-2 (Collier Cameron et al. 2007), TrES-2 and TrES-4 (Daemgen et al. 2009), HAT-P-7 (Narita et al. 2010), and new companion candidates to HAT-P-8, WASP-12 and XO-3. Stars for which no companions were detected within the FoV of AstraLux in these observation runs are listed in Table 1. The stars for which we observed a candidate companion are listed in Table 2.

Most of the companion candidates reside close to the primary stars, within the PSF-wings (HAT-P-7 and XO-3 being the exceptions). For these stars we performed relative photometry and astrometry of the companion candidates using mainly the IRAF allistar (Tody 1986, 1993) task for PSF-fitting. The PSF was built from the primary star in an image where the secondary star had been removed (see Daemgen et al. 2008, for more details on the procedure). Aperture photometry with IRAF apphot was used to determine the properties of the wide companion candidates to XO-3 and HAT-P-7. The astrometric and photometric properties in Tables 3A and 3B are averaged measurements of the final images using the Lucky Imaging combination of the best 5% and 10% of the individual integrations. For follow-up astrometry in November 2011, only \(\delta\)-band measurements were used. The separation and position angle error bars are propagated from 1σ uncertainties in the positional measurements, and take into account systematic errors (i.e., plate scale and detector orientation, see Sect. 2.1). The uncertainty in detector rotation is usually the dominant error source in the relative astrometry. The error bars in magnitude differences are propagated from the photometric errors estimated with IRAF.

Figure 1 shows the typical 5σ detection limit for the observations with AstraLux Norte in October-November 2009. At separation \(\rho = 0.5''\) we can typically detect a companion 4 magnitudes fainter than the primary in \(\Delta \rho\), and 6 magnitudes fainter at \(\rho = 1''. A similar plot representing observations with AstraLux Sur can be found in Bergfors et al. (2010). The \(\Delta \text{mag}\) as a function of angular separation was estimated by pairwise subtraction of a set of images of single stars with similar peak flux and FWHM from each other and measuring the noise level in concentric circles at increasing separations from the centre.

### 3 RESULTS

#### 3.1 Properties of the stellar companion candidates

The spectral types of the companion candidates are derived using primary star spectral types from literature and assuming that the additional flux from the much fainter secondary stars do not affect these spectral types. We use stellar SEDs by Kraus & Hillenbrand (2007) for the known TEP host spectral type in combination with 2MASS photometry in the JHK bands (Cutri et al. 2003) to find the average distance modulus and SDSS \(i\) - and \(z\)-band magnitudes. The measured magnitude difference between the primary and secondary stars in \(i\)’ and \(z\)’ then provides apparent magnitudes and \((i - z)\) colour for the companion candidate. While we do not explicitly correct for the transformation

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Table 1. Transiting exoplanet host stars with no observed companions.

| Planet Host | Instrument       | FoV ["] | Obs. Date (UT) |
|-------------|------------------|----------|----------------|
| HAT-P-2     | AstraLux Norte   | 12.00 x 12.00 | 1 Nov 2009    |
| HAT-P-11    | AstraLux Norte   | 12.00 x 12.00 | 29 Oct 2009   |
| HAT-P-13    | AstraLux Norte   | 12.00 x 12.00 | 2 Nov 2009    |
| HD 149026   | AstraLux Norte   | 12.00 x 12.00 | 1 Nov 2009    |
| HD 209458   | AstraLux Sur     | 7.87 x 7.87  | 12 Nov 2008   |
| HD 80606    | AstraLux Norte   | 12.00 x 12.00 | 30 Oct 2009   |
| WASP-3      | AstraLux Norte   | 12.00 x 12.00 | 30 Oct 2009   |
| WASP-4      | AstraLux Sur     | 15.74 x 15.74 | 10 Nov 2008   |
| WASP-5      | AstraLux Sur     | 15.74 x 15.74 | 10 Nov 2008   |
| WASP-7      | AstraLux Sur     | 7.87 x 7.87  | 10 Nov 2008   |
| WASP-13     | AstraLux Norte   | 12.00 x 12.00 | 30 Oct 2009   |
| WASP-15     | AstraLux Sur     | 7.83 x 7.83  | 12 Apr 2009   |
| XO-4        | AstraLux Norte   | 12.00 x 12.00 | 1 Nov 2009    |
| XO-5        | AstraLux Norte   | 12.00 x 12.00 | 31 Oct 2009   |

[1] Visual binary star (e.g., Naef et al. 2001), outside of AstraLux field of view.

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![Figure 1. Average sensitivity of the AstraLux Norte observations in October-November 2009. The squares mark the companion candidates (see Table 2). The dashed line represents the typical 5σ detection limit.](image-url)
Figure 2. AstraLux Norte $z'$-band observations of the candidate binaries (a) HAT-P-8 and (b) WASP-12 in October 2009. The images are shown in a square root scale with north up and east to the left.

Table 2. Relative photometry and astrometry for the companion candidates.

| ID         | Date of obs. | Instrument         | FoV      | Separation ["] | Position Angle [°] | $\Delta z'$ [mag] | $\Delta i'$ [mag] |
|------------|--------------|---------------------|----------|----------------|------------------|----------------|-----------------|
| HAT-P-7    | 30 Oct 2009  | AstraLux Norte      | 12.00×12.00 | 3.82±0.01 | 90.4±0.1         | 6.89±0.07 | 7.94±0.21 |
|            | 9 Nov 2011   | AstraLux Norte      | 12.00×12.00 | 3.86±0.07 | 89.9±0.8         | 6.87±0.07 | 7.58±0.07 |
| HAT-P-8    | 29 Oct 2009  | AstraLux Norte      | 12.00×12.00 | 1.027±0.011 | 137.3±0.4 | 6.87±0.07 | 7.34±0.10 |
| TrES-2     | 29 Oct 2009  | AstraLux Norte      | 12.00×12.00 | 1.085±0.006 | 136.1±0.2 | 3.48±0.06 | 3.73±0.03 |
| TrES-4     | 30 Oct 2009  | AstraLux Norte      | 12.00×12.00 | 1.550±0.007 | 359.9±0.2 | 4.19±0.05 | 4.57±0.05 |
| WASP-2     | 13 Apr 2009  | AstraLux Sur        | 15.66×15.66 | 0.761±0.009 | 103.5±0.2 | 3.62±0.05 | 4.17±0.03 |
|            | 9 Nov 2011   | AstraLux Norte      | 12.00×12.00 | 0.739±0.024 | 104.0±1.3 | 3.64±0.04 | 4.17±0.03 |
| WASP-12    | 30 Oct 2009  | AstraLux Norte      | 12.00×12.00 | 1.047±0.021 | 249.7±0.8 | 3.79±0.10 | 4.03±0.07 |
|            | 8.9 Nov 2011 | AstraLux Norte      | 12.00×12.00 | 1.043±0.014 | 249.9±0.5 | 3.79±0.10 | 4.03±0.07 |
| XO-3       | 30 Oct 2009  | AstraLux Norte      | 12.00×12.01 | 6.059±0.047 | 296.7±0.3 | 8.22±0.23 | 8.57±0.24 |

[1] The October 2009 observations were first published in Narita et al. (2010)

[2] Companion was discovered by Daemgen et al. (2009)

[3] Companion was discovered by Collier Cameron et al. (2007) and has also been observed by Daemgen et al. (2009)

between SDSS $i'$, $z'$ to $i$, $z$, the difference, when calculated from the photometric transformation equations (SDSS webpage), is small. The magnitude difference between the two photometric systems is less than $(i - i') = 0.05$ mag for stars bluer than $(r - i) \approx 1.5$, and even less in $(z - z')$. According to the SEDs of Kraus & Hillenbrand (2007), this $(r - i)$ colour corresponds to spectral types M4 or earlier. None of our derived spectral types are later than M4, and we conservatively assume error bars of ±0.1 for the derived $i$, $z$ magnitudes of the primary and secondary stars so as to include the transformation between photometric systems as well as uncertainty in the photometric measurements (±0.2 for the very faint companion candidate to XO-3). The secondary star spectral types and primary and secondary photometric distances were estimated from the derived $(i - z)$ colour and the SEDs of Kraus & Hillenbrand (2007). Interstellar extinction and stellar metallicity were not considered in these estimates but may affect the photometric distances, as well as the colours and spectral types. The photometric distance estimates are therefore only indicative and not hard limits. The components' spectral types, apparent magnitudes, photometric distances and the secondary stars’ $(i - z)$ colours are listed in Table 3.

3.2 Notes on individual systems

Companion candidates to 7 transiting exoplanet hosts were found from these observations. Of these, the three TEP hosts WASP-2, TrES-2 and TrES-4 and their candidate companions had been observed with AstraLux previously (Daemgen et al. 2009), and the candidate companion to HAT-P-7 is discussed in Narita et al. (2010). The widely
The transiting exoplanet HAT-P-8 b was discovered by Latham et al. (2009). It is a slightly inflated planet with mass $M_p = 1.52_{-0.10}^{+0.15} M_J$ and radius $R_p = 1.50_{-0.06}^{+0.08} R_J$ (Latham et al. 2009). The host star spectral type is only given as F in the discovery paper, but is referred to as F8V by Jones & Sleap (2011). We find from the 2MASS JHK photometry and colours that a spectral type of F5V also fits the SEDs of Kraus & Hillenbrand (2007), and list both alternatives in Table 3 until a more precise spectral classification can be made. Although the assumed primary spectral type affects the derived primary $i’, z’$ magnitudes and thereby the colour and spectral type of the companion candidate (see Sect. 3.1.), we find for both alternatives of primary spectral type that the stellar candidate companion is likely be of spectral type M2 to M4 from the $(i – z)$-colours.

3.2.2 TrES-2

The companion candidate was first discovered by Daemgen et al. (2007) from AstraLux Norte observations in May 2007. The observations presented here took place in October 2009. We measure a separation of $\Delta RA = 0.752’’ \pm 0.007”$, $\Delta Dec = 0.782’’ \pm 0.007”$, which is consistent with the astrometry of Daemgen et al. (2009) who found $\Delta RA = 0.763’’ \pm 0.007”$, $\Delta Dec = 0.777’’ \pm 0.007$. The proper motion of TrES-2 is only $\mu_\alpha \cos \delta = 2.34 \pm 1.7$ mas/yr, $\mu_\delta = -1.55 \pm 1.7$ mas/yr (PPMX Catalog. Röser et al. 2008), which is within our positional error bars over the time interval of $\sim 2.4$ years between observations. We have to await future observations to tell whether the pair is physically bound or not.

3.2.3 TrES-4

The candidate companion star was discovered in AstraLux Norte observations from June 2008 by Daemgen et al. (2009). Our measurement of $\Delta RA = 0.003’’ \pm 0.006”$, $\Delta Dec = 1.550’’ \pm 0.007”$ in October 2009 is consistent with the separation $\Delta RA = 0.005’’ \pm 0.003”$, $\Delta Dec = 1.555’’ \pm 0.005”$ measured by Daemgen et al. (2009). With a proper motion of $\mu_\alpha \cos \delta = -9.94 \pm 2.5$ mas/yr, $\mu_\delta = -27.80 \pm 2.5$ mas/yr (Röser et al. 2008), the observations over a time baseline of 16 months differ by $\approx 1.4r$ in RA and $\approx 4.3r$ in Dec from what would be expected if the companion candidate was a physically unrelated stationary background star, where $r$ is the quadratic sum of the observed and proper motion
errors. We thus conclude that this is a common proper motion binary.

### 3.2.4 WASP-2

WASP-2 b was discovered by Collier Cameron et al. (2007), who also reported the stellar companion candidate to the east of the TEP host star at an angular separation of \( \rho = 0.7'' \). The first AstraLux observation of this target was obtained in November 2007 (Daemgen et al. 2009). Although the primary star is a K1 V star, we list in Table 3 the derived magnitudes, colours and photometric distances assuming primary spectral type K0 and K2, since colours for K1 are not provided by Kraus & Hillenbrand (2007). Depending on primary spectral type (see Sect. 3.1), we find that the companion candidate is of spectral type M1/M2 … M4. Daemgen et al. (2009) observed the companion candidate at separation \( \Delta RA = 0.732'' \pm 0.004'', \Delta Dec = 0.192'' \pm 0.004'' \) in November 2007. In November 2011 we observed the separation \( \Delta RA = 0.720'' \pm 0.015'', \Delta Dec = 0.188'' \pm 0.012'' \). The proper motion of the planet host star is \( \mu_x \cos \delta = 3.38 \pm 2.9 \text{ mas/yr}, \mu_\delta = -52.31 \pm 2.9 \text{ mas/yr} \). The observations over a time baseline of 4 years are marginally inconsistent with the hypothesis of a stationary background object in RA (\( \approx 1.3\sigma \)) but by more than 11\( \sigma \) in Dec. We therefore conclude that this is a common proper motion system.

### 3.2.5 WASP-12

The very bloated planet WASP-12 b was discovered by Hebb et al. (2009). It is a highly irradiated planet, and one of the hottest with an equilibrium temperature \( T_{\text{eq}} = 2516 \pm 36 \text{ K} \) (Hebb et al. 2009).

The stellar companion candidate is not previously known. We derive a spectral type K2 ... M0 V from the measured \( (i-z) \) colour and the SEDs of Kraus & Hillenbrand (2007). The proper motion of WASP-12 is \( \mu_x \cos \delta = -0.36 \pm 1.7 \text{ mas/yr}, \mu_\delta = -6.38 \pm 1.7 \text{ mas/yr} \) (Ro\ss er et al. 2008), and future observations will be necessary to determine whether or not the stars are physical companions. The companion candidate has an elongated shape (Fig. 2) on both dates of observation, which suggests that the companion candidate may be an unresolved binary.

### 3.2.6 XO-3

A very faint companion candidate (\( \Delta z \approx 8.2 \)) was found at large angular separation (\( \rho \approx 6'' \)) from the TEP host star XO-3. The \( (i-z) \)-colour places the companion candidate at a distance of \( \geq 860 \text{ pc} \) if a main sequence star, and it is hence likely to be a non-related background object. Another possibility is that the companion candidate is a white dwarf at the approximately same distance as the TEP host. The colours and brightness are consistent with a white dwarf with \( T_{\text{eff}} \approx 4000 \text{ K} \), corresponding to a very hydrogen deficient white dwarf with cooling age 4 Gyr according to cooling curves by Chen & Hansen (2011). The age of XO-3 has been estimated to \( 2.8^{+0.58}_{-0.82} \) Gyr (Winn et al. 2008), and is thus compatible with a 4.6 Gyr white dwarf at 3\( \sigma \). While the candidate is unlikely to be a coeval comoving white dwarf companion, we can not exclude the possibility until future proper motion observations can be performed.

### 3.3 Probability of chance alignment

The probability of chance alignment is estimated using the statistical approach of Daemgen et al. (2009). The density of detectable background giants \( \rho(m_K) \), is calculated by selecting all stars included in the 2MASS PSC (Cutri et al. 2003) within 30' of each of the observed targets (Tables 1-2) that are brighter than the estimated limiting magnitude of AstraLux, \( m_K \approx 14 \), and redder than \( (J-K) \geq 0.5 \). The probability of detecting a background giant is

\[
P(\Theta, m_K) = 1 - e^{-\pi \rho(m_K) \delta^2},
\]

where \( \Theta \) is the maximum angular separation (Brandner et al. 2009). Using the aforementioned cuts in \( m_K \), \( (J-K) \) for \( \Theta = 2'' \) (see Daemgen et al. 2009) the average probability of finding a non-related background star within 2'' to the target star is \( P = 0.08 \%). We would then expect to detect unrelated background sources to \( E = 21 \times P = 0.016 \) of our observed targets. This expectation value of chance alignment increases to 0.14 at the separation of 6'' at which we find the probable background object in the observations of XO-3 (see Sect. 3.2.6).

We also consider a possible contamination by M dwarfs by selecting stars in the 2MASS PSC with \( m_K \leq 14.0 \text{ mag} \), and NIR colours \( J-H \geq 0.55 \text{ mag} \) and \( H-K \geq 0.0 \text{ mag} \). We get a typical surface density of \( 6 \times 10^{-5} \) M dwarfs per square arcsec, which corresponds to a probability of \( 7.5 \times 10^{-4} \) to find an unrelated M dwarf within 2'' of one of our target stars. We conclude that the probability of contamination by an unrelated M dwarf is of the same order as contamination by a background giant. The close candidate companions in our sample are thus likely to be true companions, although future observations are still necessary for confirmation of common proper motions for HAT-P-8, TrES-2, HAT-P-7 and WASP-12.

### 3.4 Bayesian statistical analysis

We adapt the Bayesian statistical analysis method established in Allen (2007) and utilized as well in Kraus et al. (2011) to our survey for binarity of exoplanet host stars. We model the distributions of stellar binary mass ratios and projected separations as a power law in mass ratio \( q = M_{\text{sec}}/M_{\text{prim}} \), and a Gaussian in projected separation. Thus, we are left with 4 parameters to our models:

- \( F \) – the companion star fraction (number of companions per primary star)
- \( \gamma \) – the power law index for the mass ratio \( (q) \) power law
- \( r_0 \) – the average radius, i.e. the center of the Gaussian of projected separations
- \( \sigma \) – the width of the Gaussian of projected separations

The full combined form of our model is

\[
R(q, r|F, \gamma, r_0, \sigma) \propto F q^\gamma \exp\left(-\frac{(r - r_0)^2}{2\sigma^2}\right)
\]

\[\square\]
This equation gives us the probability of detecting a binary companion to a given star in a given projected separation, mass ratio range given a particular set of values for $F$, $\gamma$, $r_o$ and $\sigma$.

To calculate the likelihood, we must compare this model value with the actual data in each part of parameter space. To do so, we must calculate how many binary companions we expect to detect with this model in each projected separation, mass ratio bin and then compare with the actual number detected in each bin (generally 0). For a given mass ratio, projected separation bin and set of model parameters, the number of companions predicted will be:

$$N_{\text{pred}}(q, r) = N_{\text{obs}}R(q, r|F, \gamma, r_o, \sigma)$$

where $N_{\text{obs}}$ is the number of times this projected separation, mass ratio bin was observed in our survey (derived from the contrast curves and stellar properties of each survey star). To compare data and model, we need to adopt a likelihood estimator. Since we expect to detect only small numbers of binary companions, our survey can be treated as a counting experiment. Thus, we adopt Poisson statistics here to calculate the likelihood:

$$\text{likelihood} = \text{prob}(N_{\text{det}}|F, \gamma, r_o, \sigma) = \frac{N_{\text{pred}}^{N_{\text{det}}}}{N_{\text{det}}!} \exp(-N_{\text{det}})$$

To derive the posterior probability distribution function (PDF) for this bin, we must multiply the likelihood by any prior probability distribution for our parameters. Certain priors can be adopted according to the functional form of the model parameters. We adopt the simplest uniform priors for $\gamma$ and $r_o$:

$$\text{prob}(\gamma|I) = \text{prob}(r_o|I) = 1$$

However, $F$ and $\sigma$ are scale parameters (i.e. invariant to changes in scale), allowing us to adopt a slightly more complex prior:

$$\text{prob}(F|I) = \frac{1}{F}$$

$$\text{prob}(\sigma|I) = \frac{1}{\sigma}$$

Thus our full prior is:

$$\text{prior} = \text{prob}(F, \gamma, r_o, \sigma|I) = \frac{1}{F\gamma\sigma}$$

For a justification of this choice, please see pages 109-110 in Sivia & Skilling (2006). Multiplying the likelihood and prior then yields the posterior PDF for this projected separation, mass ratio bin. This can be generalized across all projected separation, mass ratio bins for the survey fairly easily. We generalize $N_{\text{obs}}$ and $N_{\text{det}}$ into 2d arrays for each separation, mass ratio bin observed, which we will henceforth call the window function and detection array.

To build the window array, we use the contrast curve for each survey star to define the ranges in angular separation and contrasts where binary companions can be detected and the ranges where the contrast is insufficient to do so. Bins where a companion can be detected are assigned a value of 1; bins where no companion can be detected are assigned a value of 0. The window function for each star is then converted to projected separation vs. minimum detectable mass ratio using the models of Baraffe et al. (1998) and the distance to each survey star. $z'$-band contrasts and magnitudes were converted to H and K band for comparison with the Baraffe et al. (1999) models by interpolating the stellar SEDs from Table 5 from Kraus & Hillenbrand (2007). All the single star window functions are added together to form the survey window function. The detection array is set up in a similar manner — first as a simple array with the number of objects detected in each separation and mass bin, and then deprojected into projected separation, mass ratio space.

Then, for each set of model parameter, we calculate for each bin the posterior PDF. We multiply the posterior PDFs from each bin of observable space together to get the full posterior PDF across observable space for this set of model parameters. This process is repeated for all sets of model parameters of interest to derive the full posterior PDF as a function of the four model parameters. We calculated the posterior PDF for a grid in projected separation and mass ratio, running from 10 AU to 2000 AU in steps of 10 AU for projected separation and from 0.01 to 1.0 in $q_o$ in steps of 0.005. We allowed $\gamma$ to run from -3.9 to 3.7, in steps of 0.4 and $F$ to run from 0.05 to 9.72 in steps of 0.33. The average radius, $r_o$, ran from 10 AU to 2137 AU in steps of 73.33 AU and $\sigma$ ran from 1 to 2901 AU in steps of 100 AU.

At the 67% (90%) confidence level, we constrain $r_o$ to lie between 10 AU and 890 AU (10 – 1476 AU), $\sigma$ to lie between 300 and 1800 AU (300 – 2901 AU), $\gamma$ to lie between -1.1 and 0.5 (-1.5 – 0.9) and $F$ to lie between 0.38 and 2.05 (0.38 – 4.72).
4 DISCUSSION

The presence of a close binary companion is thought to affect processes of formation and subsequent dynamical evolution of the planets in such a system. We performed high angular resolution Lucky Imaging of 21 host stars to transiting exoplanets in search of faint, close stellar companions. Two previously unknown companion candidates were discovered, to the TEP hosts HAT-P-8 and WASP-12. Future follow-up observations are necessary to confirm common proper motion and hence physical companionship. Of the three candidate binary TEP hosts observed previously with AstraLux (Daemgen et al. 2009), TrES-4 and WASP-2 were confirmed as common proper motion couples from follow-up observations presented in this paper. Observations over a longer time baseline are still necessary to confirm the TrES-2 system as a physical binary, although we find that the probability of non-related background objects is very low (see Sect. 3.3). A wide companion candidate to XO-3 is likely to be a background object, although we cannot rule out the possibility of a comoving white dwarf companion from these observations.

We performed a Bayesian analysis of the full sample of 31 TEP hosts observed with AstraLux, including the sample presented in Daemgen et al. (2009). The companion star fraction of the TEP host stars is not significantly different from that of solar type field stars (Duquennoy & Mayor 1991; Raghavan et al. 2010). This is in accordance with what was found in previous compilations of multiplicity among RV planet hosts (Raghavan et al. 2006; Desidera & Barbieri 2007; Bonavita & Desidera 2007). At the 67% confidence level we find a companion star fraction lower limit of \( F \geq 0.38 \) which is slightly higher than the lower limits found by Raghavan et al. (2006) of \( \approx 26\% \) and Mugrauer & Neuhauser (2009), \( \approx 20\% \). However, those multiplicity fractions are based on samples of RV planet hosts and do not account for the common RV target selection bias of excluding known binaries from exoplanet surveys. No such pre-selection of single targets is made in transit surveys, and may explain the higher fraction derived in this survey.

The slope of the mass-ratio distribution is likely to be uniform or slightly negative with a maximum posterior PDF value of \( \gamma = -0.7 \) (67% confidence), indicating a preference for low mass ratio and hence large magnitude difference between companion stars. While this result is again in agreement with the field population of solar-type stars (Duquennoy & Mayor 1991; Raghavan et al. 2010), the blending by a nearby, bright star may cause rejection in transit candidate follow ups, and thus the sample of TEP hosts may be biased towards faint, low mass-ratio companions.

The main difference in multiplicity properties between field stars and planet host stars from this survey appears to be the average binary separation, which is about a factor of ten larger for the TEP hosts. With AstraLux we are typically sensitive to companions 2 magnitudes fainter than the planet host at angular separation of \( \rho = 0.2\arcsec \), corresponding to 40 AU at the average TEP host distance of 200 pc in our target sample. All our discovered candidate companions are found at projected separations \( \geq 100 \) AU. While our sample is still small, the lack of close, faint companions may be a real property of exoplanet hosts.

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