Group quenching and galactic conformity at low redshift

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ABSTRACT

We quantify the quenching impact of the group environment using the spectroscopic survey Galaxy and Mass Assembly to $z \sim 0.2$. The fraction of red (quiescent) galaxies, whether in groups or isolated, increases with both stellar mass and large-scale (5 Mpc) density. At fixed stellar mass, the red fraction is on average higher for satellites of red centrals than of blue (star-forming) centrals, a galactic conformity effect that increases with density. Most of the signal originates from groups that have the highest stellar mass, reside in the densest environments, and have massive, red only centrals. Assuming a colour-dependent halo-to-stellar-mass ratio, whereby red central galaxies inhabit significantly more massive haloes than blue ones of the same stellar mass, two regimes emerge more distinctly: at $\log (M_{\text{halo}}/M_\odot) \lesssim 13$, central quenching is still ongoing, conformity is no longer existent, and satellites and group centrals exhibit the same quenching excess over field galaxies at all mass and density, in agreement with the concept of ‘group quenching’; at $\log (M_{\text{halo}}/M_\odot) \gtrsim 13$, a cut-off that sets apart massive ($\log (M_*/M_\odot) > 11$), fully quenched group centrals, conformity is meaningless, and satellites undergo significantly more quenching than their counterparts in smaller haloes. The latter effect strongly increases with density, giving rise to the density-dependent conformity signal when both regimes are mixed. The star formation of blue satellites in massive haloes is also suppressed compared to blue field galaxies, while blue group centrals and the majority of blue satellites, which reside in low-mass haloes, show no deviation from the colour–stellar mass relation of blue field galaxies.

Key words: surveys – galaxies: evolution – galaxies: groups: general – galaxies: star formation – galaxies: statistics.

1 INTRODUCTION

Most galaxies are either discy and actively forming stars, or spheroidal, with little or no ongoing star formation (e.g. Strateva et al. 2001; Baldry et al. 2004). This bimodality has been shown to exist up to redshift $z \sim 1$ (e.g. Bell et al. 2004; Tanaka et al. 2005; Willmer et al. 2006), and possibly to $z \sim 2$ and beyond (e.g. Kriek et al. 2008; Brammer et al. 2009). In between these so-called blue and red populations lies the little populated ‘green valley’ (Wyder et al. 2007), in which galaxies are thought to transit from star forming to ‘red and dead’ (Krause et al. 2013). The star formation rate (SFR), which correlates with the density of gas in galaxy discs 

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(Schmidt 1959; Kennicutt 1998), drops when the gas goes missing, a phenomenon known as quenching. Stellar mass and environment on various scales both seem to play a role in quenching galaxies (e.g. Peng et al. 2010), but the physical processes most responsible for it remain elusive.

The specific star formation rate (sSFR, the SFR per unit stellar mass) of blue galaxies is shown to decrease with increasing mass (e.g. Elbaz et al. 2007; Noeske et al. 2007; Salim et al. 2007), the most massive galaxies being almost completely quenched. Several ‘mass quenching’ mechanisms limited to massive haloes have been proposed. Supplemented by virial shock heating of infalling cold gas (Birnboim & Dekel 2003; Keres et al. 2005; Dekel & Birnboim 2006), and gravitational heating due to clumpy accretion (Birnboim, Dekel & Neistein 2007; Dekel & Birnboim 2008; Dekel, Sari & Ceverino 2009), feedback from active galactic nuclei (AGNs) has been found to be the most efficient mechanism to self-regulate the mass content of simulated massive galaxies (e.g. Croton et al. 2006; Hopkins et al. 2006; Sijacki et al. 2007) and the key ingredient to produce realistic mock massive galaxies in state-of-the-art hydrodynamical cosmological simulations (Dubois et al. 2014, 2016; Vogelsberger et al. 2014; Schaye et al. 2015). The stabilization of gas discs (‘morphological quenching’; Martig et al. 2009) can explain quenching in less massive haloes.

The properties of galaxies with respect to their local environment – on the scale of dark matter (DM) haloes, i.e. groups and clusters – have long been investigated, e.g. their colour (e.g. Butcher & Oemler 1984; Balogh et al. 2004b), morphology (e.g. Dressler 1980; Dressler et al. 1997) or SFR (e.g. Gómez et al. 2003; Balogh et al. 2004a; Wijesinghe et al. 2012; Brough et al. 2013; Robotham et al. 2013; Davies et al. 2015); galaxies are known to be more often red and elliptical in clusters (e.g. Oemler 1974; Davis & Geller 1976; Balogh et al. 1997, 1999).

Various local environmental quenching processes have been proposed. These include cluster-specific processes, such as galaxy harassment (Moore et al. 1996), ram pressure stripping of gas (Gunn & Gott 1972) or interactions with the tidal field of clusters (Byrd & Valtonen 1990), and group-specific processes, such as galaxy mergers (e.g. Toomre & Toomre 1972) and strangulation (Larson, Tinsley & Caldwell 1980; Balogh, Navarro & Morris 2000). Prescott et al. (2011) found that the effect of environment on satellite galaxies was primarily a function of their host’s stellar mass rather than their own stellar mass, and that strangulation was likely to be the main gas removal process that quenches them. Groote et al. (2017) argued on the contrary that it was the ongoing substantial accretion of gas in groups that led to the build-up of spheroidal components in satellite disc galaxies, and eventually to their ‘death by gluttony’ rather than starvation.

It is also debated whether it is the central-satellite dichotomy (e.g. Peng et al. 2012; Kovač et al. 2014) or simply being a member of a group that is crucial for the quenching of star formation, i.e. are we mostly seeing satellite quenching (e.g. van den Bosch et al. 2008; Hartley et al. 2015; Carollo et al. 2016) or group quenching (Knobel et al. 2015)?

In addition to local (halo scale) effects, the formation epoch and subsequent accretion history of a halo depend on its locus in the large-scale environment, a phenomenon referred to as ‘assembly bias’ (e.g. Sheth & Tormen 2004a; Gao, Springel & White 2005; Wechsler et al. 2006; Musso et al. 2018). An observation, first made and coined ‘galactic conformity’ by Weimann et al. (2006), who analysed galaxy groups in the Sloan Digital Sky Survey (SDSS; York et al. 2000), has been suggested as evidence of this past large-scale environmental effect: the fraction of quenched satellites around a quenched central is found to be significantly higher than around a star-forming central,\(^1\) at fixed halo mass. An interpretation might be that galaxy properties depend not only on the mass of their DM haloes but also on their assembly history (e.g. Hearin, Watson & van den Bosch 2015). Galactic conformity has since been confirmed by other analysis of the SDSS and observed at redshift \(z \geq 2\) (Hartley et al. 2015; Kawinwanichakij et al. 2016). It was also claimed to persist out to scales far larger than the virial radius of haloes (Kaufmann et al. 2013; Hearin et al. 2015), but this puzzling result, named ‘two-halo conformity’, and which several studies have accounted for by advocating the mutual evolution of haloes in the same large-scale tidal field (Hearin et al. 2015; Hearin, Behroozi & van den Bosch 2016; Zu & Mandelbaum 2018; Rafieferantsoa & Dave 2018), was recently questioned and found attributable to methodological biases (Sin, Lilly & Henriques 2017).

Quenching in groups has been studied (e.g. van den Bosch et al. 2008; Prescott et al. 2011; Peng et al. 2012; Wetzel et al. 2013; Knobel et al. 2015; Kawinwanichakij et al. 2016) by means of red fractions (fractions of quiescent galaxies) and quenching efficiencies (QEs, excess quenching with respect to some control sample) as a function of various environmental parameters, such as halo mass, halo-centric distance, local galaxy density, or mass of the central galaxy. While there is general agreement on the dependence of satellite quenching on these parameters, a physical interpretation is not straightforward, mainly because the parameters are correlated and difficult to disentangle, even through multidimensional analysis (Knobel et al. 2015).

The aim of this paper is to revisit the quenching impact of group environment, and to probe ‘one-halo’ galactic conformity in particular, using the spectroscopic survey Galaxy and Mass Assembly (GAMA; Driver et al. 2009, 2011; Liske et al. 2015). Thanks to its depth and spectroscopic completeness, GAMA allows us to expand the SDSS investigations to \(z \sim 0.2\) in a significant volume of the Universe. From a group catalogue, we constructed using an anisotropic Friends-of-Friends (FoF) algorithm taking into account the effects of redshift-space distortion, we study the red fraction, QE, and star formation activity of galaxies in groups as a function of central galaxy colour, group stellar mass, large-scale density, and finally halo mass. This group catalogue, corrected for the finger-of-god effects, is used in a companion paper (Kraljic et al. 2018) to improve the reconstruction of the cosmic web and to explore the impact of its anisotropic features (nodes, filaments, walls, and voids) on galaxy properties.

The outline of the paper is as follows: in Section 2, we describe the GAMA data, the derivation of the physical properties of the galaxies and our criterion for classifying them into star forming and quiescent. We present the group catalogue in Section 3. The stellar mass and environmental dependencies of quenching and conformity are analysed in Sections 4 and 5, respectively. Star formation in groups is explored in Section 6. We discuss the uncertainties of our analysis in Section 7 and conclude in Section 8. The paper also contains appendices dedicated to the detailed description of our group finder (adopted algorithm, mock catalogues used for its

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1 Holmberg (1958) first observed colour conformity in galaxy pairs and concluded that it could not be accounted for by the known correlation with morphological type. For 20 yr, the Holmberg effect received attention from neither observers nor theoreticians, but it was later confirmed by several groups as evidence of coupled evolution (http://ned.ipac.caltech.edu/level5/Sept02/Kee/Keel5_4.html).
calibration, optimization strategy, and tests of group reconstruction quality.

Throughout our analysis, we adopt a flat cold dark matter cosmology with \( H_0 = 67.3 \, \text{km} \, \text{s}^{-1} \, \text{Mpc}^{-1} \), \( \Omega_m = 0.3 \), and \( \Omega_\Lambda = 0.7 \) (Planck Collaboration XIII 2016). All magnitudes are quoted in the AB system and the physical parameters are derived assuming a Chabrier initial mass function (IMF, Chabrier 2003).

2 DATA

The GAMA\(^3\) survey (Driver et al. 2009, 2011; Liske et al. 2015) is a joint European-Australian spectroscopic survey combining multiband photometric data from several ground- and space-based programs. The photometric coverage includes data from the Galaxy Evolution Explorer (GALEX) in the far- and near-ultraviolet (FUV and NUV), the SDSS at optical wavelengths (\( u, g, r, i \), and \( z \) passbands), the VISTA Kilo-degree Infrared Galaxy (VIKING) Survey in the \( ZYJHK \) bands, and the Wide-Field Infrared Survey Explorer (WISE) in four mid-infrared bands from 7 to 22 \( \mu \)m. Far-infrared (FIR) data from Herschel ATLAS (H-ATLAS) and radio data from the Giant Meterwave Radio Telescope have also been acquired. GAMA was intended to link wide and shallow surveys such as the SDSS Main Galaxy Sample (Strauss et al. 2002) to narrow and deep surveys such as DEEP2 (Davis et al. 2003).

The photometric data used in this work are the LAMBDA\(^3\) panchromatic photometric catalogue LambdaCatv01 (Wright et al. 2016), consisting of three equatorial fields (G09, G12, and G15) covering a total of 180 deg\(^2\) (3 times 12 \times 5 deg\(^2\)). The spectroscopy was carried out using the 2dF/AOOmega multi-object spectrograph on the Anglo-Australian Telescope, building on previous spectroscopic surveys such as SDSS, the 2dF Galaxy Redshift Survey and the Millennium Galaxy Catalogue (MGC). It is nearly complete (98 per cent) to \( r = 19.8 \) (Liske et al. 2015), each region of the sky being observed multiple times (the target density being much higher than the available fibre density), with at least one member of any given close-packed group receiving a fibre whenever that region was visited (Robotham et al. 2010). This makes GAMA a more suitable data set to study galaxies in groups and close pairs than other spectroscopic surveys (e.g. SDSS) that miss a fraction of close targets, especially in high-density regions [see Liske et al. (2015) for the GAMA completeness on small scales].

2.1 Physical parameters

The physical quantities used in this work were derived from the spectral energy distribution (SED) fitting code LEPHARE\(^4\) using the FUV to NIR photometry (11 bands). We used a set of model spectra from Bruzual & Charlot (2003), assuming a range of exponentially declining star formation histories and a Chabrier IMF (Chabrier 2003), as well as three dust obscuration laws: the commonly used starburst law of Calzetti et al. (2000), an exponential law with exponent 0.9 and the Small Magellanic Cloud law of Prevot et al. (1984). The physical quantities of interest in this paper are the stellar mass (defined as the median of the probability distributions), the dust-corrected absolute magnitudes, the sSFR, and the maximum volume \( V_{\text{max}} \) in which a galaxy would remain observable above the survey flux limit given its luminosity and spectral type.

2.2 Star-forming (blue) versus quiescent (red) classification

While the bimodality in galaxy properties has been observed as far back as Hubble (1926), with late type, star-forming, spiral or irregular, blue galaxies on the one hand and early type, elliptical, ‘red and dead’ galaxies on the other, defining a transition between the two populations is not straightforward as the distributions overlap (Taylor et al. 2015). Colour–magnitude or colour–mass diagrams are most often used to draw the line, or a smooth transition zone, e.g. Taylor et al. (2015) introduced a statistical approach allowing for the natural overlap of the two populations in the \( (g-i) \) versus stellar mass diagram using GAMA at \( z < 0.12 \). However, shorter wavelengths prove most discriminating (e.g. UV–optical colours; Wyder et al. 2007), even though dust causes confusion since dusty star-forming galaxies look red and may be mistaken for quiescent galaxies. This mixing can be efficiently sorted out by using colour–colour diagrams, such as \( (NUV-r) \) versus \( (r-k) \) which was shown to be a powerful diagnostic to separate dusty star-forming galaxies from intrinsically red, quiescent ones (Arnouts et al. 2013).

Fig. 1 shows the distribution of galaxies in the \( (NUV-r) \) versus \( (r-k) \) diagram for the \( \sim 85 \) per cent that are UV detected (left-hand panel), and the dust corrected \( (u-r) \) versus \( r \) and versus stellar mass diagrams (middle and right-hand panels respectively), where \( NUV, u, r, \) and \( k \) refer to the rest-frame magnitudes. The colour code reflects the average sSFR per pixel. The dust-corrected colour and sSFR are correlated through the modelling of the attenuation, but the two populations are separated equally well around the same sSFR values in the uncorrected \( (NUV-r) \) versus \( (r-k) \) diagram. The consistency between the dust-uncorrected bi-colour diagram and the dust-corrected colour gives us confidence in the dust recipes used in our SED fitting. We find that a straight colour cut at \( (u-r)_{\text{cut}} = 1.8 \) is consistent with a cut in sSFR at \( \sim 10^{-10.5} \, \text{yr}^{-1} \). The solid and dashed lines show the median relations for the quiescent and star-forming populations defined in terms of these \( (u-r) \) and sSFR boundaries, respectively. They form the well-known red and blue sequences.

In the range of stellar masses that we use in this work (\( \log (M_*/M_\odot) \gtrsim 10.25 \), see the next section), the above separation criteria yield undistinguishable results. Thus, we simply define the blue and red populations in terms of dust corrected \( (u-r) \) colour with a dividing line at \( (u-r)_{\text{cut}} = 1.8 \), and we will use the terms red (blue) and quiescent (star-forming) galaxies interchangeably. The term \( (u-r) \), or U–R in figure labels, will always refer to the dust-corrected colour.

2.3 Stellar mass completeness

In order to compute redshift and mass unbiased red fractions, we must restrict our sample to group members more massive than the completeness limit at the maximum redshift considered. Fig. 2 shows the mass completeness limits as a function of redshift for the blue and red galaxies as blue and red dashed lines, respectively. These limits are defined as the mass above which 90 per cent of the galaxies reside at a given redshift \( z \geq 0.004 \). The redshift/mass compromise used in the rest of this paper is \( z < 0.21 \) and \( \log (M_*/M_\odot) > 10.25 \) (the red mass limit in this redshift range).

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\(^2\) http://www.gama-survey.org/

\(^3\) Lambda Adaptive Multi-Band Debending Algorhythm in R.

\(^4\) http://cesam.lam.fr/lephare/lephare.html
Figure 1. Rest frame \((\text{NUV} \, - \, r)\) versus \((r \, - \, k)\) colours (left-hand panel), and dust-corrected \((u \, - \, r)\) colour versus \(r\) magnitude (middle panel) and versus stellar mass (right-hand panel) at \(0.02 < z < 0.24\). Stellar masses are in units of \(\log (M_\star / M_\odot)\). The contours are unweighted number density contours. The colour code reflects the average sSFR per pixel. The straight colour cut at \((u \, - \, r)_{\text{corr}} = 1.8\) (dotted line) is statistically consistent with a cut in sSFR at \(\sim 10^{-10.5} \, \text{yr}^{-1}\) except for low-mass red galaxies. The solid and dashed lines show the median relations for the quiescent and star-forming populations defined in terms of these \((u \, - \, r)_{\text{corr}}\) and sSFR cuts. In the rest of this paper, the blue and red populations are defined in terms of dust corrected \((u \, - \, r)\) with a dividing line at \((u \, - \, r)_{\text{corr}} = 1.8\).

Figure 2. The stellar mass in units of \(\log (M_\star / M_\odot)\) versus redshift distribution, with number density contours for the red population. The blue and red dashed lines represent the mass completeness limits for the blue and red galaxies, respectively, as a function of \(z\). The vertical lines and the red horizontal lines are the redshift and mass limits used in our analysis: \(0.02 < z < 0.21\) and \(\log (M_\star / M_\odot) > 10.25\).

3 GROUP CATALOGUE

3.1 Group catalogue construction

Although a GAMA group catalogue already exists (Robotham et al. 2011), we developed our own tool for the purpose of an ongoing cosmic web study in this and other data sets (e.g. Malavasi et al. 2017; Kraljic et al. 2018). A detailed description of the FoF algorithm we adopted to detect the groups is presented in the appendices. A schematic illustration of the method is depicted in Fig. 3. In order to deal with the effects of redshift-space distortions, the distance between two galaxies \(i\) and \(j\) is measured in two coordinates: the parallel \(d_{\parallel, ij}\) (equation B3) and perpendicular \(d_{\perp, ij}\) (equation B4) projected comoving separations to the mean line of sight (LoS) \(l\) (equation B1). We next introduce two linking lengths \(b_\perp\) and \(b_\parallel\), the projected and LoS linking lengths in units of the mean intergalactic separation \(r_{ij}\) (equation B7), respectively, related through the radial expansion factor \(R = b_\parallel / b_\perp\) accounting for the peculiar motions of galaxies within groups. Two galaxies are assumed to be linked to each other if their projected perpendicular and parallel separations are smaller than the corresponding linking lengths (equations B5 and B6).

The linking length \(b_\perp\) and the radial expansion factor \(R\) (or equivalently, the perpendicular and LoS linking lengths) are the two free parameters to be optimized. Their values will affect the quality of the resulting group catalogue: too small values will tend to breakup single groups into several groups, while too large values will merge multiple groups into single ones.

These free parameters can be determined from the optimization of some group cost function, depending on the scientific purpose of the group catalogue, when tested on mock catalogues. Our objective is to obtain a catalogue with a high group detection rate and a low contamination by galaxies coming from different groups. We followed the definition of the group cost function of Robotham et al. (2011), \(S_{\text{tot}}\), with slightly different notations and minor modifications. This cost function is meant to fulfill the requirement that the reconstructed and underlying real group catalogues are mutually accurate representations of each other. By definition, \(S_{\text{tot}}\) takes values...
between 0 and 1 and must be maximized. The method is described in Appendix C.

Results of the optimization computation are shown in Fig. 4. As can be seen, there is a degeneracy between the parameters $b_\perp$ and $R$: for values of $b_\perp$ equal to 0.06 and 0.07, $S_{\text{tot}}$ does not evolve significantly between $R \gtrsim 16$ and $R \approx 30$, and between $R \gtrsim 14$ and $R \approx 25$, respectively. This means that the global statistical properties of group catalogues constructed using a combination of $b_\perp$ and $R$ in these ranges will be similar.

Given this degeneracy, we include an additional criterion of symmetry between the recovered and real groups: we request that the individual contribution of the mock and FoF components to the overall cost function be similar (the more similar these contributions, the more similar the reconstructed groups of the mock and FoF catalogues). With this additional constraint, our final choice for the FoF parameters are $b_\perp = 0.06$ and $R = 19.0$. This combination of parameters is optimal when considering statistical measures of the group reconstruction quality independent of those used in the optimization, as shown in Appendix F. Our linking lengths are in good agreement with the combination found to be optimal for studies of environmental effects by Duarte & Mamon (2014), who tested the parameters according to the scientific goal of the group catalogue. We did not apply any completeness correction to the linking parameters since the GAMA survey is spectroscopically extremely complete ($\approx 98\%$ per cent within the r-band limit, Driver et al. 2011) and the mean modifications would be less than 1 per cent (Robotham et al. 2011).

### 3.2 Central versus satellite classification

Central galaxies are often assumed to be the most massive galaxies in a halo lying at the minimum of its gravitational potential well, while satellites are all remaining group members orbiting the centrals within the group potential. This central-satellite dichotomy is easily applied in simulations but represents a non-trivial challenge in real data. Groups may be fragmented, overmerged, they can contain interlopers or miss actual members, and spurious groups may be generated.

To minimize the impact of group membership misidentification, in addition to a given physical property of galaxies (stellar mass and/or luminosity), some information about their spatial (e.g. Robotham et al. 2011; Knobel et al. 2012, 2015) and velocity (Carollo et al. 2013) distribution within the group may be included. Following Robotham et al. (2011) (see also Eke et al. 2004, for a different implementation), we tested an iterative approach. The first step of this method is to compute the centre of mass (CoM) of the group, then to proceed iteratively by computing the projected distance (as in equation B4) from the CoM for each group member and by rejecting the most distant galaxy. This process stops when only two galaxies remain: the most massive of the two is identified as the central galaxy of the group and all other group members are classified as satellites. As this iterative centre coincides with the most massive galaxy in 98 per cent of the groups, we chose the most massive galaxies as centrals. Thus, all groups keep their central when applying a mass cut-off, or else disappear completely.

For each group in the redshift range $0.02 < z < 0.21$ with $N_{\text{FoF}}$ members, we defined $N_{\text{FoF}}^{\text{red}}$ as the number of group members with mass $\log(M_*/M_\odot) > 10.25$ (see Section 2.3). In the following sections, ‘group galaxies’ refer to all galaxies in groups with $N_{\text{FoF}}^{\text{red}} \geq 2$. ‘Isolated’, ‘lone’ or ‘field’ galaxies refer to galaxies for which $N_{\text{FoF}} = 1$ instead of $N_{\text{FoF}}^{\text{red}} = 1$ to exclude known group centrals, satellites detected below the mass limit, although this makes negligible difference in our results. Of course group centrals with faint satellites undetected in the survey will still be present in the lone category, especially at the lower mass limit and upper redshift limit of the sample. The total numbers of blue and red isolated centrals, group centrals, and satellites are reported in Table 1. Fig. 5 shows the group richness distribution (left-hand panel) and the mean group richness as a function of the central’s stellar mass (right-hand panel) for groups with blue and red centrals.

For comparison, we also show these distributions for the group catalogue of Robotham et al. (2011). Our algorithm leaves more galaxies alone (61.5 per cent versus 51.8 per cent), yields more small groups and less satellites (24.6 per cent versus 34.5 per cent) than Robotham et al. (2011), who generate larger groups. 20 per cent of their satellites are field galaxies and 6 per cent group centrals in our own catalogue. However but we find that these differences in the rates of fragmentation/merging is not significant enough to alter our statistical results (see also Section 7). In both cases, 76 per cent of group centrals are red and these red centrals tend to have more satellites than blue ones of the same stellar mass, in agreement with Wang & White (2012). Red centrals collectively own over 80 per cent of the satellites above the chosen mass limit.

### 4 QUENCHING AND CONFORMITY

As mentioned in the Introduction, Weinmann et al. (2006) first coined the concept of ‘galactic conformity’, referring to the observation derived from a SDSS DR2 galaxy group catalogue, that the fraction of quiescent satellites around a quiescent central was significantly higher than around a star-forming central. They observed this phenomenon at all satellite luminosities and at all halo masses, computed via abundance matching from the total luminosity of the groups. We explore this effect in the GAMA group catalogue described in the previous section, as a function of stellar mass, of various local and large-scale environmental parameters, and finally of halo mass.
Table 1. Group catalogue. Number of objects with \( \log (\frac{M_*}{M_\odot}) > 10.25 \) at 0.02 < \( z < 0.21 \)

|            | Red   | Blue  | Group centrals | Red   | Blue  | Satellites |
|------------|-------|-------|----------------|-------|-------|------------|
| Isolated   | 9659  | 8392  | 3092           | 975   | 4850  | 2378       |
|            | 32.9 per cent | 28.6 per cent | 10.5 per cent | 3.3 per cent | 16.5 per cent | 8.1 per cent |

Figure 5. Left: the richness distribution of the groups derived in this work (Section 3) and by Robotham et al. (2011). Right: the mean group richness as a function of the central’s stellar mass for groups with at least two members above the stellar mass limit. 76 per cent of group centrals are red in both group catalogues and collectively own \( \sim 82 \) per cent [85 per cent for Robotham et al. (2011)] of the satellites above the mass limit.

4.1 Mass quenching

We estimate the fraction of quiescent galaxies (red fraction) in a given sample as:

\[
f_q = \frac{\sum q_i w_i}{\sum w_i},
\]

where \( q_i \) is unity if the \( i \)th galaxy in the sample is quenched and zero otherwise. The parameter \( w_i \) is the \( 1/V_{\text{max}} \) weight of the \( i \)th galaxy (note that no weighting yields undistinguishable results above the chosen completeness limit).

Fig. 6 shows the red fraction of galaxies as a function of stellar mass in different environments as follows: (i) isolated galaxies (grey solid line for the data and dotted line for its polynomial fit), (ii) centrals of groups (dashed green line), (iii) satellites of blue central galaxies (blue line), (iv) satellites of red central galaxies (red line), and (v) satellites of any central (dotted line with grey shaded errors). The fractions are estimated globally in each mass bin, not averaged over the red fractions of individual groups. In all environments, the red fraction increases strongly with increasing stellar mass. In the mass range that we are able to probe, a 10-fold increase in stellar mass roughly doubles the red fraction. We will refer to this trend as ‘mass quenching’ (e.g. Peng et al. 2012), as opposed to the ‘environmental quenching’ observed in the vertical direction at a given stellar mass.

4.2 Conformity

Fig. 6 shows that the red fraction of satellite galaxies, which is dominated by satellites of red centrals, is significantly higher at all masses than that of lone centrals. The difference is largest at low masses and getting smaller towards the highest masses, in general agreement with van den Bosch et al. (2008), although the trend they observe is more dramatic (but see Section 5.3).

The red fraction of satellites around blue centrals is about 10 per cent higher than the red fraction of isolated galaxies, except perhaps in the two highest mass bins (\( \log (\frac{M_*}{M_\odot}) \gtrsim 10.8 \)) where uncertainties are large. At \( \log (\frac{M_*}{M_\odot}) \gtrsim 11 \), blue centrals become rare (<20 per cent) and we find no massive satellites around them. There are mixed results in the literature about whether or not satellites around star-forming central galaxies are quenched in excess of field galaxies. By examining the star formation properties of bright satellites around isolated Milky Way-like hosts in the local Universe, Phillips et al. (2014) found...
that quenching occurs only for satellites of quenched hosts while star formation is unaffected in the satellites of star-forming hosts. Hartley et al. (2015) also reported that the satellite population of star-forming centrals was similar to the field population of equal stellar mass at intermediate to high redshift. Conversely, Kavirwanichakij et al. (2016) found a higher QE of satellites around star-forming centrals compared to the background galaxies at $0.3 < z < 1.6$, in agreement with the study of Phillips et al. (2015) in the local Universe considering Milky Way-like systems hosting two satellites. Our analysis is more consistent with the latter studies, at least for low-mass satellites.

Satellites of red centrals exhibit the highest level of quenching. Their red fraction is systematically about 10 per cent higher than that of satellites around star-forming centrals at all masses $\log (M_\ast/M_\odot) \lesssim 11$. This difference between the blue and the red lines is a significant galactic conformity signal, an environmental effect that adds to mass quenching: satellites around blue centrals have to be $\sim 2$ times more massive than those around red centrals to exhibit the same level of quenching. In the high-mass regime, $\log (M_\ast/M_\odot) \gtrsim 11$, where conformity disappears for lack of massive blue centrals hosting massive satellites, the red fraction becomes closer to that of field galaxies.

4.3 Group quenching

Lastly, group centrals appear to follow the minimum quenching behaviour of the satellite population as a function of mass: at $\log (M_\ast/M_\odot) \lesssim 11$, they quench like satellites of blue centrals, while at higher mass, they converge with satellites of red centrals, in such a way that their red fraction runs $\sim 10$ per cent above that of isolated galaxies at all masses, reaching 100 per cent at $\log (M_\ast/M_\odot) \gtrsim 11.4$. This excess quenching of group centrals over isolated centrals, despite the fact that the latter are likely to be contaminated by group members, supports the idea that quenching in groups is not reduced to ‘satellite quenching’, as advocated by Knobel et al. (2015). We refer to this mass-independent excess as ‘group quenching’, which, at this point, does not necessarily mean that satellites and group centrals respond equivalently to the group environment (Knobel et al. 2015). We return to this point later.

Fig. 7 shows another view of these results, called QE ($\epsilon_\mathrm{q}$), following the formalism of Knobel et al. (2015) (see also van den Bosch et al. 2008). This formalism which separates out the dependence on stellar mass, helps to highlight the dependence on other parameters. The QE represents the excess red fraction of a given population with respect to the red fraction of a reference sample, $f_{q,\text{ref}}$, normalized by the star-forming fraction of that reference sample:

$$
\epsilon_q(M_\ast) = \frac{f_q(M_\ast) - f_{q,\text{ref}}(M_\ast)}{1 - f_{q,\text{ref}}(M_\ast)}.
$$

We choose the lone central population as our reference sample, and fit its red fraction curve, $f_{q,\text{ref}}(M_\ast)$ (solid grey line in the left-hand panel of Fig. 6), with a polynomial function of order 2, $f_{q,\text{ref}}^{\text{lin}}(M_\ast)$ (the overlapping dotted line):  

$$
 f_{q,\text{ref}}^{\text{lin}}(M_\ast) = 6.580 - 1.535 \log \left( \frac{M_\ast}{M_\odot} \right) + 0.091 \log^2 \left( \frac{M_\ast}{M_\odot} \right).
$$

This allows us to define the QE of any individual galaxy $i$ of mass $M_\ast$ as:

$$
\epsilon_{q,i}(M_\ast) = \frac{q_i - f_{q,\text{ref}}^{\text{lin}}(M_\ast)}{1 - f_{q,\text{ref}}^{\text{lin}}(M_\ast)}.
$$

The meaning of these individual $\epsilon_{q,i}$ is limited [$\epsilon_{q,i}(M_\ast) = 1$ for red galaxies ($q_i = 1$) and negative for blue galaxies ($q_i = 0$)], but allows the QE of any set of galaxies to be computed as a function of any parameter of interest by simply averaging them over the sample (Knobel et al. 2015).

Fig. 7 shows that this QE as a function of stellar mass, is, by definition, null for lone centrals. Up to the transition mass $\log (M_\ast/M_\odot) \approx 11$, all the QE curves are nearly independent of mass, with satellites of blue centrals and centrals of groups at the level of what we called group quenching ($\epsilon_q \approx 0.15$). Galactic conformity manifests in the difference between the blue and the red curves, the QE of satellites around red centrals being about twice the group quenching value. In the higher mass regime where satellites of blue centrals no longer exist, the QEs of satellites of red centrals and of centrals of groups fast increase towards complete quenching (which can be inferred from the parallel behaviour of their red fraction curves with respect to isolated galaxies in the left-hand panel).

5 ENVIRONMENTAL EFFECTS

5.1 Environmental parameters

We now address the dependence of the satellite red fractions and QEs on three environmental parameters:

(i) the dust-corrected ($u - r$) colour of central galaxies,
(ii) the group stellar mass $M_g$, defined as the total stellar mass from group members with $\log (M_\ast/M_\odot) > 10.25$,
(iii) the density contrast ($1 + \delta$) at the centrals’ location, defined as the density of central galaxies = satellites are excluded = smoothed by a 3D Gaussian kernel of $\sigma = 5$ Mpc and normalized by the redshift-dependent mean density of the survey.
Figure 8. Correlations between the three environmental parameters: dust-corrected $(u - r)$ colour of the central galaxies, group stellar mass, and large-scale density contrast at the central’s location (see the text for details). The solid blue and red lines show the mean values for blue and red group central galaxies, respectively. The dashed blue and red lines are the mean values for satellites of blue and red centrals, respectively (i.e. the same distributions weighted with the number of satellites in each bin). The green line shows the mean colour/density relation of group centrals when blue and red ones are mixed.

These parameters are labelled ‘U-R OF CENTRAL’, ‘GROUP MASS’, and ‘DENSITY CONTRAST’ for visual clarity in all figures. The group mass and the density contrast are always expressed logarithmically as $\log (M_\text{gr}/M_\odot)$ and $\log (1 + \delta)$, respectively.

The density estimator used in satellite quenching studies is generally based on the ‘fifth nearest neighbour’ (e.g. Knobel et al. 2015). A major disadvantage of this approach is that it does not probe the same environment for small and large groups (Peng et al. 2012; Carollo et al. 2013); for small groups ($N_{\text{FoF}} \lesssim 5$), the density is estimated on a scale much larger than the size of their DM halo, whereas for rich groups, it is measured well within their virial radius. Our choice of density estimator intentionally probes scales beyond the virial radius of all groups.

Fig. 8 shows how these environmental parameters may be correlated. The solid blue and red lines show the median values for blue and red centrals of groups, respectively. The dashed blue and red lines are the median values for satellites of blue and red centrals, respectively (i.e. the same distributions weighted with the number of satellites in each bin). A weak correlation is seen between group mass and colour, expected since the group mass is dominated by the central’s mass, which correlates with colour (Fig. 1). None is found between density and colour. A colour–density relation appears only when star-forming and quenched centrals are mixed (green line), reflecting their evolving ratio with density (see Section 5.3). Density does correlate with group mass for groups with red centrals. The correlation is all the more apparent when the medians are weighted by the number of satellites in each group (solid versus dashed lines): rich, massive groups with red centrals are clearly more common in high-density environments. The satellite weighting effect needs to be kept in mind when considering environmental correlations in general. Artificially boosted trends may be induced by a few very rich groups, as emphasized by Sin et al. (2017) in case of two-halo conformity signals.

5.2 Satellite quenching

Fig. 9 shows the red fraction of satellite galaxies as a function of the above three environmental parameters in four bins of stellar mass, which displays mass quenching in the vertical direction. The left-hand panel shows the red fraction of satellites as a function of their central’s colour, with the vertical dotted line indicating our boundary between blue and red centrals. This expands the blue/red central dichotomy in Fig. 6 to a continuum in central colour, similar to the trend in sSFR reported by Knobel et al. (2015). The fraction of red satellites increases in all mass bins, most noticeably in the lowest, as their centrals redden, in such a way that the red fraction of low-mass satellites around very red centrals exceeds that of satellites several times more massive around very blue centrals.

More significant trends are found with the groups’ stellar mass (middle panel), in agreement with earlier studies showing that satellite quenching is more efficient in more massive systems (using the mass or the magnitude of the central galaxy or some proxy for the halo mass; Weinmann et al. 2006; Ann, Park & Choi 2008; Prescott et al. 2011; Knobel et al. 2015). In addition, two distinct sequences for satellites of blue and red centrals appear (dashed and dot-dashed lines, respectively): satellites of similar stellar mass, in groups of similar group mass above $\sim 10^{11} M_\odot$, are more likely to be red if their central is red than if it is blue, as also found by Knobel et al. (2015) using the central’s mass and halo mass. The upward trends with group mass are essentially driven by satellites of red centrals, which vastly dominate the satellite population. The curves for satellites of blue centrals, which span a narrower range of group masses and have poorer statistics, are consistent with being flat.

Lastly, significant correlations are observed between the red fractions in all mass bins and the density contrast (right-hand panel). Again two sequences are seen that exhibit conformity at fixed density contrast, at least for $\log (1 + \delta) > 0$. For satellites of red centrals, quenching increases significantly with $\log (1 + \delta)$, while the statistics are inconclusive for satellites of blue centrals. These trends may simply duplicate the middle panel: satellite quenching is enhanced in massive groups whose central is red and these are found preferentially in high-density regions (cf. Fig. 8). We will attempt to disentangle these effects in the next section.

Since satellites behave similarly in the four mass bins we probed, we may increase our statistics, especially for satellites of blue centrals, by using mass-matched samples instead of bins, i.e. samples of satellites of blue and red centrals having similar stellar mass distributions. We also make use of the QE formalism described in the previous section, to detach mass quenching from the environmental quenching we are trying to highlight. Fig. 10 recasts Fig. 9 using this new methodology. The adopted common mass distribution is the intersection of the two samples, i.e. the mass distribution of satellites of blue centrals. The unnormalized blue and red distributions are shown in the leftmost inset, with the intersection shaded in yellow. The orange histogram is the total mass distribution of the satellites of red centrals. As it is significantly larger than the blue histogram, we make several draws in it in order to pick every galaxy
Figure 9. The red fraction of satellites in four bins of stellar mass as a function of their central’s \((u-r)\) colour (left), their group’s stellar mass in units of \(\log (M_*/M_\odot)\) (middle), and the large-scale density contrast in units of \(\log (1+\delta)\) (right). Mass quenching shows in the vertical direction at fixed environmental parameter. The upward trends with increasing central colour, group mass, and density, at fixed stellar mass, are essentially driven by satellites of red centrals (dot–dashed lines). The red fractions for satellites of blue centrals (dashed lines) are lower and consistent with being independent of all three environmental parameters.

Figure 10. QEs with respect to lone centrals at fixed mass (equation 4) as a function of central colour (left), group stellar mass (middle), and density contrast (right). The blue and red curves are the QE of satellites of blue and red centrals, respectively, in mass-matched samples. The adopted shape for the mass distribution is shown in the inset of the left-hand panel (shaded histogram), with the matched distributions for the blue and red central samples (unnormalized). The orange histogram is the parent stellar mass distribution of the satellites of red centrals. This QE formalism reinforces the conclusions of Fig. 9 with better statistics. The QE of lone centrals (grey curve in the right-hand panel), which is calibrated over their own red fraction as a function of mass but independently of density, is also a strongly increasing function of density.

at least once, and compute the final QE curve as the average of the QE curves computed for each individual draw.

The three panels of Fig. 10 reinforce the findings of Fig. 9: the QE of satellites is a smoothly rising function of central colour from blue to red; the QE of satellites around red centrals increases with their group stellar mass, while it is independent of it for satellites of blue centrals, but also consistently positive (i.e. they quench more efficiently than field galaxies); the QE of both populations strongly increases with large-scale density. This figure also emphasizes that much of the excess quenching in satellites of red centrals originates from the most massive groups that have no counterpart with blue centrals. The QE of lone centrals – which is calibrated over their own red fraction as a function of mass but independently of density – is also a strongly increasing function of density contrast, negative below the peak density, positive above. This point is addressed in the next section. We note too that there exists circumstances in which conformity disappears, i.e. the blue and red curves converge: first for centrals in the ‘green valley’, the QE being a monotonically increasing function of central colour from the bluest to the reddest; secondly in low-mass groups \((M_g < 10^{11} M_\odot)\); and thirdly at the lowest density contrasts \((\log (1+\delta) < 0)\) where the QE of both populations reaches zero or negative values. The last two circumstances are clearly correlated (Fig. 8). We will now attempt to disentangle them.

5.3 Density quenching

Fig. 11 reproduces the left-hand panel of Fig. 6 in three bins of density contrast. The middle bin spans the peak of the density distribution of the full sample. The dotted orange baseline in the three panels is a fit to the lone central curve in the lowest bin to guide the eye: the uplift as density increases is clear for all galaxies, indicating that quenching, is affected by the environment far beyond the virial radius of DM haloes.\(^6\)

For central galaxies, this effect is interpreted as reflecting the earlier collapse of proto-haloes in large-scale overdense regions. At a given halo mass, the haloes populating denser environments are older on average, with different accretion histories (delayed or quenched mass inflow), a phenomenon referred to as assembly bias (Sheth & Tormen 2004b; Croton, Gao & White 2007). The age of a halo is usually defined as the epoch at which the halo has assembled one half of its current mass, however Tinker et al. (2017) showed that the amplitude of assembly bias was significantly reduced if age was defined using halo mass at its peak rather than current value (removing the effect of ‘splashback’ haloes), and in better agreement with their analysis of SDSS data. They find a \(\sim 5\) per cent increase in halo mass.

\(^6\) Qualitatively similar results are also found using densities computed on a scale of 8 Mpc instead of 5.
from low to high large-scale \((10 \, h^{-1}\, \text{Mpc})\) density in the red fraction of central galaxies with \(\log (M_*/M_\odot) \gtrsim 10.3\). The increase between the orange and grey dotted line in the right-hand panel of Fig. 11 is \(\sim 10\) per cent, a reasonable agreement given the many differences in the two analyses. For comparison, a factor of 2 in stellar mass at fixed density roughly induces the same increase in red fraction.

Also notable in this figure is the increasing vertical gradient between the satellites of red centrals and the other curves, in particular that of satellites of blue centrals, at \(\log(M_*/M_\odot) \lesssim 11\) as density increases: conformity is hardly detectable in the lowest density bin, emergent in the middle bin, and very significant in the highest bin, where it is also mass dependent. The difference between satellites of red and lone centrals in this bin is significantly larger at lower masses than in the average density case (Fig. 6), in better agreement with van den Bosch et al. (2008, their fig. 8, top right panel, for all satellites combined).

In all three panels, the red fraction curve of group centrals runs roughly 10 per cent higher than that of lone centrals at all masses, as in the global case of Fig. 6. Thus group quenching, which we defined in Section 4.3 as the difference between the dashed green and the grey curves, adds a somewhat constant boost to density quenching. At low and medium density, where conformity is marginal, group centrals do not distinguish themselves from satellites, supporting the idea of group quenching by Knobel et al. (2015). Conformity is most significant in the highest density bin.

In Fig. 11 using the new \(f_{q_{\text{ref}}}^\text{fit}(M_*)\), multiplied by a fudge factor of 0.8:

\[
g(\delta) = 0.8 \times (-0.07 + 0.23\Delta + 0.25\Delta^2 - 0.02\Delta^3) \tag{7}\]

This empirical recipe provides a good fit to the red fraction of lone galaxies as a function of both mass and density. It allows us to redefine the QE \(\epsilon_{q,i}(M_*, \delta)\) of an individual galaxy \(i\) of mass \(M_*\), living in a region of density contrast \(\delta\), as:

\[
\epsilon_{q,i}(M_*, \delta) = \frac{q_i - f_{q_{\text{ref}}}^\text{fit}(M_*, \delta)}{1 - f_{q_{\text{ref}}}^\text{fit}(M_*, \delta)}. \tag{8}\]

and the QE of a galaxy sample as the average of these individual \(\epsilon_{q,i}\).

The solid lines in Fig. 12 represent this new QE for satellites of blue and red centrals as a function of the three environmental parameters in stellar mass-matched samples as in Fig. 10. The grey curve in the right-hand panel represents the QE of lone centrals, designed to be null with respect to both stellar mass and density. The dependence on density completely disappears for satellites of blue centrals, whereas is remains significant for satellites of red centrals.

As was already visible in Fig. 10, much of the excess quenching in the satellites of red central population originates from the most massive groups that have no blue central counterpart. The dashed lines in Fig. 12 show that if we match the group stellar mass distributions of satellites around blue and red centrals, which excludes these massive groups and which also results in nearly perfectly matching the stellar mass and density distributions of both populations (distributions shown in the insets), the dependence with density and colour are strongly reduced for the remaining satellites of red centrals. Some amount of conformity persists as a function of group mass, which affects the QE of satellites of red centrals only, but this figure allows us to conclude that most of the conformity signal arises from the most massive groups with the reddest centrals that not only have no counterpart with blue centrals in terms of group mass, but in which satellite quenching is more dependent on density than in other groups, including low-mass groups with red centrals.

In Fig. 13, we show the red fraction of all galaxies as a function of group mass. For field galaxies, the group stellar mass equals their stellar mass by definition. We find that the quenching gap between group and lone centrals at fixed stellar mass is filled at fixed group mass, as if groups centrals ‘carried’ the weight of their satellites (an extra \(\sim 0.25\) dex in stellar mass on average). Satellites,
mass as previously claimed (Weinmann et al. 2006; Hartley et al. 2005; Croton et al. 2007), which refers to the dependence of halo clustering on properties other than mass. One such property is age: older haloes (those that assembled earlier) presumably are more concentrated than less concentrated ones. Another property, which correlates with halo age, is concentration: more concentrated haloes are typically more clustered than less concentrated ones.

If there exists a sufficiently tight relation between one of these halo properties and galaxy colour or star formation history, galaxy conformity is expected to arise. A relation between galaxy colour and halo age was indeed found in the cosmological hydrodynamical simulation Illustris (Bray et al. 2016), where the reddest galaxies preferentially reside in the oldest haloes. Similarly, Paranjape et al. (2015) and Pahwa & Paranjape (2017) found conformity in models correlating galaxy colour with halo concentration.

However inferring halo masses in real data is an uncertain task and those derived from total group luminosities or masses, as used in establishing galactic conformity, are not flawless. In fact it was observed that red galaxies reside in more massive haloes than average galaxies of similar luminosity or mass (Zehavi et al. 2011; Wang & White 2012; Krause et al. 2013). More recently, Zu & Mandelbaum (2016) claimed to have discovered, from weak-lensing measurements of local bright galaxies in the SDSS that there exists a strong bimodality in the average host halo mass of blue versus red galaxies: at fixed stellar mass, red centrals preferentially reside in haloes that are a factor of 2–10 more massive than haloes hosting blue galaxies. They found that a model in which ‘halo quenching’—referring to all the physical processes tied to halo mass (virial shocks, accretion shocks, AGN feedback, and gas stripping)—is the main driver of galaxy quenching, best fits the available data and explains galactic conformity without assembly bias (Wang & White 2012; Phillips et al. 2014, 2015; Zu & Mandelbaum 2018).

To test this scenario, we derive halo masses for all groups using the double, blue/red, average halo-to-stellar-mass ratio (HSMR) of Zu & Mandelbaum (2015, their fig. 16), applied to the central galaxies. Fig. 14 shows the QE of satellites as a function of this halo mass estimate: conformity at fixed halo mass has disappeared. This model splits the halo mass into two distinct regimes that were blurred with the group stellar mass: a high halo mass regime, \( \log (M_\text{h}/M_\odot) \geq 13 \) (29 per cent of the groups, 46 per cent of the satellites, 5 per cent of the field galaxies), in which centrals are fully quenched and conformity has no meaning, and a low halo mass regime, \( \log (M_\text{h}/M_\odot) \leq 13 \) (71 per cent of the groups, 54 per cent of the satellites, and 95 per cent of the field galaxies), in which centrals still experience quenching, i.e. can be either red or blue at a given halo mass, but with no significant impact on the quenching of their satellites. The
Figure 14. The QE of satellites around blue and red centrals (blue and red curves, respectively), as a function of halo mass in units of log (Mh/M⊙) estimated from the blue/red HSMRs of Zu & Mandelbaum (2015, see the text for details). The inset shows the normalized halo mass distributions for satellites of blue and red centrals. This model highlights two regimes: at log (Mh/M⊙) ≳ 13, centrals are fully quenched and conformity has no meaning, while at log (Mh/M⊙) ≲ 13, central quenching is still ongoing and conformity is insignificant.

Figure 15 revisits Fig. 11, in the two regimes of halo mass. We note that haloes of both types exist in all tree density bins although they are not equally represented (~24, 25, 22 per cent of groups in the low-mass regime are in the low-, medium-, and high-density bins, respectively, versus ~13, 28, 31 per cent for groups in the high halo mass regime). In the low halo mass regime, conformity is insignificant indeed. Satellites and group centrals also exhibit the same quenching excess (~10 per cent) over field galaxies at all mass and density, in agreement with the group quenching definition of Knobel et al. (2015). In the high halo mass regime, in which the centrals are all massive (log (M∗/M⊙) > 11), fully quenched galaxies, satellites undergo significantly more quenching than their counterparts in smaller haloes. This effect increases with density, giving rise to the increasing conformity signal observed in Fig. 11 from low to high density when the two regimes are mixed. The dependence on stellar mass also appears to be less significant than satellite QE in this regime as well.

Figure 16. The red fraction of centrals and satellites as a function of halo mass. The red triangles are the predictions based on the stellar mass and density dependence of the satellite red fraction in the two regimes of halo mass (see the text for details).

Fig. 16 shows the red fractions of both satellites and centrals as a function of halo mass. The red fraction of group and lone centrals (matched in stellar mass distribution) is a much steeper function of this halo mass than of the stellar group mass (Fig. 13), reaching unity at ~10¹³ M⊙, while all satellites follow the same gentler path regardless of central type. Since the red fraction of satellites and group centrals depends on their own stellar mass equivalently in low-mass haloes, and halo mass is strongly correlated to the stellar mass of the central only, it is not surprising that central quenching depends strongly on halo mass while satellite quenching does not, at least in the low halo mass regime. The slope might simply be explained by the increasing mean stellar mass and surrounding density of the satellites as halo mass increases. At log (Mh/M⊙) ~ 12 and 12.7,
the mean stellar masses of the satellites are $< \log (M_*/M_\odot) > = 10.41$ and 10.54, respectively, and their mean surrounding densities are 0.24 and 0.30. Using equation (5), which models the red fraction of the field population as a function of mass and density, to which we add 0.1 to account for the group quenching excess, we compute the mean red fractions expected from these two combinations of stellar mass and density. The resulting values are shown as orange, upward pointing triangles. The reasonable agreement indicates that satellite quenching depends on halo mass inasmuch as more massive haloes contains more massive satellites on average (the difference in mean density makes negligible difference). At $\log (M_*/M_\odot) \sim 13$ and 13.8, in the high halo mass regime, the mean stellar masses of the satellites are $< \log (M_*/M_\odot) > = 10.61$ and 10.65, while their mean surrounding densities are 0.37 and 0.6, respectively. The saturation in mean stellar mass is expected from the increasingly small contribution of high-mass satellites to the overall mass distribution. Here, we simply compute the mean red fractions of satellites in small bins around these two combinations, with the condition that their central is red and massive. The resulting values are shown as orange downward triangles. The agreement shows that the dependence on halo mass in this regime is equivalent to a dependence on density. Fig. 17 shows how the two properties are strongly correlated, as in the case of the group stellar mass shown in Fig. 8 for groups with red centrals.

We conclude that halo mass, as defined in this section, is the ‘hidden’ parameter (Knobel et al. 2015) behind galactic conformity, due to comparing satellites in two distinct ranges of halo mass. The Zu & Mandelbaum (2015) HSMRs separate groups with massive ($\log (M_*/M_\odot) > 11$), red centrals from all the others, and offers a halo mass interpretation to our finding that satellite quenching appears to proceed differently in these two types of groups. The change of regimes marks a change in the stellar mass and density dependence of satellite quenching, from mostly stellar mass dependent to mostly density dependent. We find that the concept of group quenching advocated by Knobel et al. (2015), whereby satellites and group centrals quench similarly at a given stellar mass and density (‘feel environment in the same way’), holds in the low halo mass regime ($\sim 70$ per cent of the groups): the red fraction of all galaxies in these groups is determined by the same combination of their own stellar mass and large-scale density, with a constant $\sim 10$ per cent boost with respect to their field counterpart. In more massive haloes whose centrals are massive, fully quenched galaxies ($\sim 30$ per cent of the groups), satellite quenching also depends on stellar mass and surrounding density, but less on the former and more on the latter, which strongly correlates with halo mass. This may point to different, satellite-specific quenching processes in these massive haloes, or simply to the increasing importance of group pre-processing, i.e. satellites first quenching in lower mass groups prior to infalling into more massive ones, as halo mass increases (Wetzel et al. 2013).

6 STAR FORMATION IN GROUPS

We now examine the level of star-forming activity of blue satellites compared to their field counterparts. Grootes et al. (2017) found that the median sSFR—stellar mass relation of a morphologically selected sample of disc-dominated satellites in the GAMA survey was mildly suppressed compared to isolated spiral galaxies. They also find that this mild suppression originates from a minority population ($\leq 30$ per cent) with strongly suppressed sSFR with respect to isolated spirals, whereas the majority of spiral satellites show no sign of being affected by their group environment. Nor do spiral group centrals. These results led them to conclude that the gas cycle of spiral galaxies is largely independent of environment, the intra-halo medium of the host group being the most likely reservoir of cold gas fuelling star formation in satellite galaxies.

Our sample of star-forming galaxies is unlikely to be purely disc-dominated, even if most of the star formation in the local Universe is shown to occur in disc regions (e.g. James et al. 2008). To exclude the less discy galaxies, we apply an upper limit of 2 to the $r$-band Galfit Sérsic index of our blue population, which excludes 33 per cent of the star-forming sample. Transposing the methodology of Grootes et al. (2017) to $(u-r)_{\text{corr}}$ colours, we consider the offset of a galaxy’s colour from the median value measured for isolated blue (disc) galaxies of the same mass:

$$\Delta(u-r) = (u-r)_{\text{corr}} - (u-r)_{\text{field}}(M_*) ,$$

where $(u-r)_{\text{field}}(M_*)$ is a linear fit to the median colour–mass relation (Fig. 1) of blue field galaxies in our mass and redshift ranges. We do not find that this relation varies with large-scale density, nor does the mean colour of blue group centrals (Fig. 8).

Fig. 18 shows the $\Delta(u-r)$ distributions of blue field galaxies, blue satellites in the two regimes of halo mass ($\log (M_*/M_\odot) < 12.9$), and blue group centrals (in small haloes by design), with their corresponding median values. Two-sample Kolmogorov–Smirnov tests show that: (i) blue group centrals are very similar to blue field galaxies in colour–mass relation (two-tailed p-value $p = 0.2$); (ii) blue satellites in small haloes (69.4 per cent) are also compatible with being drawn from the same distribution ($p = 0.04$), and (iii) blue satellites in massive haloes (30.6 per cent) differ significantly from blue field galaxies ($p \sim 10^{-8}$), with a red offset $\Delta(u-r) = 0.087 \pm 0.015$ mag. The cut in Sérsic index sharpens the distinction between the populations but not applying one does not alter these conclusions.

We propose that the blue satellites of massive red centrals (in the massive halo regime) correspond to the population of disc satellite galaxies in which Grootes et al. (2017) found evidence of suppressed star formation with respect to field galaxies. Gas fuelling must be hindered in these massive haloes, in which the fraction of red satellites is also significantly enhanced. However, most haloes appear not to have a significant impact on the star formation activity of their
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Figure 18. The $\Delta(u - r)$ distributions (equation 9) of blue field galaxies and blue satellites in low- and high-mass haloes ($\log(M_\star/M_\odot) < 12.9$) respectively, with corresponding median values (vertical lines). The star-forming activity of blue satellites in low-mass haloes ($\sim70\%$) is similar to that of blue isolated galaxies, while it is mildly suppressed for blue satellites in massive haloes ($\sim30\%$).

blue satellites, in agreement with Grootes et al. (2017) who argue for a change in morphological mix rather than a change in the gas fuelling process in groups to explain the well-known colour-(local) density relation (e.g. Zehavi et al. 2011, and references therein), stating that galaxies are redder in denser environments. We postpone a morphological investigation of group galaxies to a future study.

7 CAVEATS

Our analysis is based on an FoF algorithm that was optimized on mock catalogues (Robotham et al. 2011) to yield a high group detection rate and a low rate of contamination by interlopers (the best balance between completeness and purity). The linking lengths we selected are in good agreement with the combination found to be optimal for studies of environmental effects by Duarte & Mamon (2014). However no group finder is perfect, and it is impossible to recover all the groups exactly as they are known to be in the mocks: some groups will be fragmented and/or merged, contain galaxies unrelated to them, and miss members that will be misplaced in neighbouring groups or left alone in the field. Misidentifications of satellites and centrals will follow, and group masses will be wrongly attributed, adding to the uncertainty inherent to any method of assigning a central and a halo mass to each group.

As mentioned in Section 3.1 and detailed in Appendix E, there is a degeneracy between the two free parameters $b_1$, and $R$ used to optimize the cost function, which is why we considered additional statistical quantities, as described in Appendix F. Our choice of parameters, $(b_1, R) = (0.06, 19)$, corresponds to the highest purity. However while purity may be most important when comparing satellites to centrals, prioritizing completeness may be preferred to study conformity. To try and evaluate the impact of our choice, we tested a combination of parameters $(0.07, 19.0)$ that maximizes the completeness instead of purity and found no substantial changes in any of our results (conformity, group quenching, and star formation in groups). Additionally, instead of using an optimization based on the global grouping efficiency and global grouping purity, we considered the combination of parameters that maximizes the global purity alone $(0.07, 23.5)$, and the one that maximizes the completeness alone $(0.06, 25.5)$. Again, we found all the results to be qualitatively similar, albeit noisier.

These different combinations may be considered similar by design as they belong to the zone of degeneracy of the same algorithm and the changes in purity and completeness are relatively small. However, our red fractions of centrals and satellites (Fig. 6) are also in qualitative agreement with previous studies using the official SDSS group catalogue, and can also be reproduced using the GAMA group catalogue of Robotham et al. (2011), despite significant differences in their rates of fragmentation and/or merging (Section 3.1).

Campbell et al. (2015) showed that accounting for the systematic errors associated with a particular group finder is best achieved by running the group finder over mock catalogues that include realistic galaxy colours and proposed a new statistic (called HTP for halo transition probability) to weigh the combined impact of the above errors. While such forward modelling is beyond the scope of this paper, their general conclusions shed light on the uncertainties that may plague our results (and others that also do not account for these errors (e.g. Weinmann et al. 2006; Yang, Mo & van den Bosch 2008, 2009; Peng et al. 2012; Wetzel, Tinker & Conroy 2012; Knobel et al. 2015)).

Campbell et al. (2015) created a mock by populating the DM haloes of a large N-body simulation with galaxies of different luminosities and colours ($g - r$), using both subhalo abundance matching and age matching (Hearin & Watson 2013), which reproduces both one- and two-halo conformities (Hearin et al. 2014). Three different types of group finder were tested on this mock to assess their ability to recover colour-dependent halo occupation statistics, including satellite fractions, red fractions, and conformity. The resulting group catalogues were found to be remarkably similar (which is reassuring and in agreement with our tests), and to recover most colour-dependent statistics reasonably well. In particular, the difference between the red fractions of centrals and satellites at fixed r-band luminosity (not shown as a function of stellar mass) is qualitatively reproduced.

The three group finders tested by Campbell et al. (2015) also recover galactic conformity at fixed halo mass, defined using abundance matching on total group luminosity, but also tend to create weak conformity when this property is removed from the mock. They also found that the strength of the recovered or induced conformity signal at fixed halo mass may be reduced or enhanced, depending on whether luminosity or stellar mass is the primary galaxy property driving halo occupation in the mock data, and in the recovered groups. In other words, the definition of the ‘true’ and inferred halo masses (which can be both based on luminosity, or on stellar mass, or on one property for the mock and the other for the FoF), have a substantial impact on the systematic uncertainties that are assessed through forward modelling.

Nevertheless, we understand from Campbell et al. (2015) that whatever the choice of primary galaxy property, or properties, none of the three FoF algorithms can completely abolish conformity at fixed halo mass when it exists in the mock, nor induce a significant conformity signal when it does not. Running our FoF algorithm on real data, we find that conformity does indeed depend on the definition of halo mass that it is weak if we use the total group stellar mass, and non-existent in a scenario that assigns larger halo masses to red centrals than to blue ones. We conclude from the work of Campbell et al. (2015) that our particular choice of FoF algorithm and parameters is unlikely to be solely responsible for these results.
8 SUMMARY AND CONCLUSIONS

We investigated the properties of central and satellite galaxies in groups at redshift $z \lesssim 0.2$ and with stellar mass log ($M/M_\odot$) $> 10.25$ using the spectroscopic survey GAMA. The group catalogue was constructed using an anisotropic FoF algorithm taking into account the effects of redshift-space distortion. Red (quiescent) and blue (star-forming) galaxies were classified according to their dust-corrected $(u - r)$ colour, shown to be a good bimodal measure of star-forming activity. We explored the fraction of quiescent galaxies (red fraction) in different environments. Our density contrast is defined as the density of central galaxies (satellites were excluded), smoothed by a 3D Gaussian kernel of $\sigma = 5$ Mpc and normalized by the redshift-dependent mean density of the survey (using an 8 Mpc scale yields similar results). This estimator probes beyond the virial radius of all groups and is therefore quite different from the ‘fifth nearest neighbour’ generally used in satellite quenching studies, and which is sensitive to the varying size of DM haloes. Our results can be summarized as follows:

(i) **Mass and density quenching:** the red fraction of all galaxies, whether isolated or in groups, is a strongly increasing function of stellar mass, a phenomenon referred to as mass quenching. At fixed stellar mass, the red fraction of all galaxies, including isolated galaxies, increases with the large-scale density contrast. We account for both these effects by defining a QE that separates out both mass and density quenching, designed to be null for field (isolated) galaxies.

(ii) **Galactic conformity:** the average red fraction of satellites around quenched centrals is significantly higher than that of satellites of the same stellar mass around star-forming centrals. Their QE increases with their central’s colour, group stellar mass, and large-scale density, while that of satellites of blue centrals appears to be independent of all three parameters. This creates a conformity signal that increases with density and group stellar mass. Most of the signal originates from the most massive groups in the densest environments around quenched centrals, in a group stellar mass regime devoid of blue centrals. Some amount of conformity remains at fixed group stellar mass and density.

(iii) **Halo quenching:** assuming group mass traces halo mass, galactic conformity is indeed observed at fixed halo mass as originally claimed. However, if red centrals inhabit more massive haloes than blue ones of the same stellar mass, as several studies suggested, and we assume a colour-dependent HSMR, we find that conformity disappears entirely at fixed halo mass. Two quenching regimes emerge: at log ($M_h/M_\odot$) $\lesssim 13$, centrals still undergo quenching but conformity is insignificant at any given stellar mass and density; at log ($M_h/M_\odot$) $\gtrsim 13$, a cut-off that sets apart massive (log ($M_h/M_\odot$) $> 11$) red only centrals, conformity is meaningless, and the satellites undergo significantly more quenching than their counterparts in smaller haloes, all the more so as density increases. This accounts for the conformity signal that increases with density when both regimes are mixed.

(iv) **Group quenching:** in the low halo mass regime, satellites and group centrals exhibit the same quenching excess, ~10 per cent in red fraction, over field galaxies at fixed stellar mass and density, in agreement with the notion of group quenching advocated by Knobel et al. (2015), who argued against the importance of satellite-specific processes. However in the high halo mass regime where satellites still undergo quenching, while their centrals are fully quenched, the central/satellite dichotomy cannot be ruled out. In this regime, satellite quenching strongly depends on large-scale density, which correlates with halo mass.

(v) **Star formation activity in groups:** star-forming group centrals and the majority of star-forming satellites, which reside in low-mass haloes, show no deviation from the colour—stellar mass relation of blue field galaxies. However star-forming satellites in high-mass haloes (~30 per cent) significantly deviate from the colour distribution of blue field galaxies, with a mean $(u - r)$ reddening of ~0.09 mag.

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APPENDIX A: GROUP RECONSTRUCTION METHODS

It is known that the identification of the groups in redshift space is hampered by several difficulties. Of particular concern are redshift-space distortions such as the elongation of groups along the LoS due to the peculiar velocities of the group galaxies (the ‘fingers-of-God’ effect), and the less significant distortions caused by the coherent infall of galaxies towards the centre of assembling structures (the ‘Kaiser effect’). Both of these effects cause confusion when determining group membership, resulting in excessive merging of galaxies into large structures or, contrarily, the fragmentation of large groups into smaller structures, depending on the adopted strategy for finding the groups. Without the measure of an absolute distance, it is impossible to separate the peculiar velocities from the Hubble flow and these complications cannot be fully avoided.
To surmount these difficulties, different algorithms have been developed, most notably the FoF algorithm (Huchra & Geller 1982) recursively creating links between galaxies within a specified volume around each galaxy. An alternative and more complicated approach to group identification is the Voronoi–Delaunay method developed by Marinoni et al. (2002) which makes use of the Voronoi–Delaunay tessellation to locally measure clustering parameters on a cluster-to-cluster basis (rather than on a galaxy-to-galaxy basis as in the FoF algorithm). This method was introduced to overcome some of the difficulties inherent to the standard FoF algorithm, but modified FoF implementations have proved competitive [e.g. Robotham et al. 2011 found that while the Voronoi-Delaunay method (VDM) variant of Gerke et al. (2005) worked reasonably well for larger groups and clusters, their FoF implementation performed better in the low halo mass regime; see also Knobel et al. 2009 for an extensive performance comparison of both algorithms]. In this paper, we adopted an FoF algorithm, as described below.

APPENDIX B: FRIENDS-OF-FRIENDS

To deal with the effects of redshift distortions, the distance between two galaxies \(i\) and \(j\) is measured with two coordinates, the parallel \(d_{\parallel,j}\) and perpendicular \(d_{\perp,j}\) projected comoving separations to the mean LoS. Let \(r_i\) and \(r_j\) denote the redshift positions of a pair of objects \(i\) and \(j\), we define the mean LoS as:

\[
I \equiv \frac{1}{2} \left( r_i + r_j \right) \tag{B1}
\]

and the redshift space separation is given by:

\[
s \equiv r_i - r_j. \tag{B2}
\]

The projected parallel and perpendicular LoS separations between \(i\) and \(j\), \(d_{\parallel,j}\) and \(d_{\perp,j}\) respectively, are then given by:

\[
d_{\parallel,j} = s \cdot \frac{l}{\parallel l \parallel} \tag{B3}
\]

and

\[
d_{\perp,j} = \sqrt{s \cdot s - d_{\parallel,j}^2}. \tag{B4}
\]

The two galaxies are linked to each other if:

\[
d_{\parallel,j} < b_{\parallel} \bar{r}_{ij} \tag{B5}
\]

and

\[
d_{\perp,j} < b_{\perp} \bar{r}_{ij}. \tag{B6}
\]

Here, \(b_{\parallel}\) and \(b_{\perp}\) are the projected and LoS linking lengths in units of the mean intergalactic separation given by:

\[
\bar{r}_{ij} = \frac{1}{2} \left( n_i^{-1/3} + n_j^{-1/3} \right), \tag{B7}
\]

with \(n_i\) and \(n_j\) being the galaxy number densities at the redshifts of galaxies \(i\) and \(j\). The parameter \(b_{\parallel}\) is related to \(b_{\perp}\) through the radial expansion factor \(R = b_{\parallel}/b_{\perp}\) accounting for the peculiar motions of galaxies within groups.

APPENDIX C: PARAMETERS OPTIMIZATION STRATEGY

The FoF algorithm described above has two free parameters, the linking length \(b_{\parallel}\) and the radial expansion factor \(R\) (or equivalently the perpendicular and LoS linking lengths). Their values will affect the quality of the resulting group catalogue: too small values will tend to breakup single groups into several groups, while too large values will merge multiple groups into single ones.

These free parameters can be determined by optimizing a group cost function (a measure of the grouping quality) when tested on the mock catalogues. No combination of linking lengths will create a group catalogue recovering simultaneously all aspects of the underlying halo distribution, no matter how large the systems are (see e.g. Berlind et al. 2006). The optimization strategy depends on the scientific purpose of the group catalogue. Our objective is to obtain a catalogue with a high group detection rate and a low contamination by galaxies coming from different groups. We followed the definition of the group cost function of Robotham et al. (2011), with slightly different notations and minor modifications.

We need to define the way reconstructed groups (the FoF groups) are associated with the underlying real groups in the mock catalogues (the mock groups). Ideally, the associations between the real and reconstructed groups should be bijective, meaning that the joint galaxy population of the FoF and mock groups includes more than 50 per cent of their respective members. Such an association is unambiguous, as each group can bijectively match one group at most, and the reconstructed and the corresponding real group catalogues are mutually an accurate representation of each other.

To cast such a two-way grouping quality into a statistical measure, let \(N_{\text{FoF}}, N_{\text{FoF}}^\ast\), and \(N_{\text{mock}}\) denote the number of bijective, FoF, and mock groups, respectively. Following Robotham et al. (2011), we define:

\[
E_{\text{FoF}} = \frac{N_{\text{FoF}}}{N_{\text{FoF}}^\ast}, \tag{C1}
\]

\[
E_{\text{mock}} = \frac{N_{\text{mock}}}{N_{\text{mock}}^\ast}, \tag{C2}
\]

and

\[
E_{\text{tot}} = E_{\text{FoF}}E_{\text{mock}}. \tag{C3}
\]

By definition, these measures take values in the range 0–1. \(E_{\text{tot}}\) can be seen as the global halo finding efficiency, telling us how well the groups are recovered. It will be 1 if all groups are bijective, and 0 if there is no group with a bijective match.

Another measure of the grouping quality is how well galaxies within the groups are recovered. Let \(P_{\text{FoF},ij}\) and \(P_{\text{mock},ij}\) denote the purity products defined as follows:

\[
P_{\text{FoF},ij} = \frac{N_{\text{FoF},i\cap\text{FoF},j}}{N_{\text{FoF},i}N_{\text{FoF},j}}, \tag{C4}
\]

where \(N_{\text{FoF},i\cap\text{FoF},j}\) is number of galaxies the \(i\)th FoF group shares with the \(j\)th mock group, and

\[
P_{\text{mock},ij} = \frac{N_{\text{mock},i\cap\text{mock},j}}{N_{\text{mock},i}N_{\text{mock},j}}, \tag{C5}
\]

where \(N_{\text{mock},i\cap\text{mock},j}\) is the number of galaxies that the \(i\)th mock group shares with the \(j\)th FoF group. We will call the best match the association between the \(i\)th mock (FoF) group and the \(j\)th FoF (mock) group for which \(P_{\text{mock},ij}(P_{\text{FoF},ij})\) is highest.

We then define the following measures:

\[
Q_{\text{FoF}} = \sum_{i=1}^{N_{\text{FoF}}} \frac{N_{\text{mock},i\cap\text{mock},ij}}{N_{\text{mock},i}N_{\text{FoF},j}}Q_{\text{FoF},ij}, \tag{C6}
\]

where

\[
Q_{\text{FoF},i} = \frac{N_{\text{mock},i\cap\text{mock},ij}}{N_{\text{mock},i}}. \tag{C7}
\]
where
\[ Q_{\text{mock},i} = \frac{N_{\text{mock},i}}{N_{\text{mock}}}. \]

Finally, the global grouping purity is defined as:
\[ Q_{\text{tot}} = Q_{\text{FoF}} Q_{\text{mock}}. \]

The final quantity defining our group cost function is:
\[ S_{\text{tot}} = E_{\text{tot}} Q_{\text{tot}}, \]
which takes values between 0 and 1 and should be maximized.

In order to find the right combination of linking lengths, we use the publicly available GAMA mock catalogues\(^7\) described below, on which we run our FoF group-finder algorithm for a grid of \( b_\perp \) and \( R \) values, and compute \( S_{\text{tot}} \).

**APPENDIX D: MOCK CATALOGUES**

The GAMA mock galaxy catalogues [see Robotham et al. (2011) for a detailed description] were constructed from the Millennium DM N-body simulation (Springel et al. 2005) run with the following cosmological parameters: \( \Omega_m = 0.25, \Omega_\Lambda = 0.75, \Omega_b = 0.045, h = 0.73, n = 1, \) and \( \sigma_8 = 0.9. \) The DM haloes were then populated with galaxies using the Bower et al. (2006) variant of the GALFORM semi-analytic model of galaxy formation.

There are nine mock catalogues, each of which covers a complete analogue of the full GAMA I survey, i.e. three regions of 12 \( \times \) 4 deg\(^2\) out to redshift 0.5, preserving the true angular separation between them. The public mocks are limited to the apparent magnitude \( \text{M}_{\text{mag}} = 15.0 \). The public mocks are limited to the apparent magnitude \( \text{M}_{\text{mag}} = 15.0 \).

**APPENDIX E: RESULTS OF THE OPTIMIZATION**

As we already mentioned, the optimization of the group-finding parameters should be carried out in a way that the resulting group catalogue best fulfills the desired scientific goals. For our optimization, we use only groups with five or more members which can match groups with two or more members. This choice is motivated by the desire to estimate the global group properties of the resulting group catalogue.

The results of the optimization computation are shown in Fig. 4. The global maximum of \( S_{\text{tot}} \) is obtained for the combination of two parameters \((b_\perp, R) = (0.06, 27.5)\). We note however, that between \( R \gtrsim 16 \) and \( R = 30, S_{\text{tot}} \) does not evolve significantly. This remains true for \( b_\perp = 0.07 \) as well. In addition, the values of \( S_{\text{tot}} \) for these two linking lengths, and in the \( R \) range 16–30 are very similar within the error bars. This means that increasing the value of \( R \) in a given range leads to very similar global statistical properties of the reconstructed catalogues. We will thus include an additional criterion by considering the contribution from the mock and FoF components to the overall cost function. This contribution should be as symmetric as possible, indicating that the FoF algorithm recovers on average similar groups, in terms of number and quality of reconstruction, that actually exist in the mock catalogue. Table E1 shows the FoF parameters corresponding to the maximum global cost function \( S_{\text{tot}} \), and the most symmetric contribution to \( S_{\text{tot}} \) from the mock and FoF components (\( S_{\text{mock}} = E_{\text{mock}} Q_{\text{mock}} \) and \( S_{\text{FoF}} = E_{\text{FoF}} Q_{\text{FoF}} \), respectively). For the global maximum of the cost function, corresponding to \((b_\perp, R) = (0.06, 27.5)\), the cost from mock groups to \( S_{\text{tot}} \) is lower than the one from FoF groups indicating that the group-finding algorithm globally recovers less groups than actually exist in the mock catalogue. Similar asymmetry is found for the combination \((b_\perp, R) = (0.07, 19.0)\), corresponding to the maximum of \( S_{\text{tot}} \) for \( b_\perp = 0.07 \), and \((b_\perp, R) = (0.07, 15.0)\), which is the most symmetric solution for \( b_\perp = 0.07 \). The most equilibrated contribution is obtained for \((b_\perp, R) = (0.06, 19.0)\), which is our preferred choice for the FoF parameters.

**APPENDIX F: QUALITY OF GROUP RECONSTRUCTION**

The statistical measures used to define our cost function introduced in the previous section already allow us to assess the performance of our group-finding algorithm. We will however introduce additional statistical quantities, different from those used in the optimization, in order to test the quality of the reconstructed catalogue independently. Following Knobel et al. (2009)\(^8\), we define two classes of statistical quantities. One on a group-to-group basis, including the completeness, purity, overmerging, and fragmentation, and the second one on a galaxy-to-group basis, with the galaxy success rate

\(^7\) http://www.gama-survey.org

\(^8\) The statistical quantities defined in this section follow with some modifications those introduced in Knobel et al. (2009). Some of these measures can be found in their original form in Gerke et al. (2005).
and the interloper fraction. We will define each of these quantities for the best and bijective matches as introduced in Appendix C.

Let \( N^{\text{best}}_{\text{FoF}} (\geq N) \) and \( N^{\text{bij}}_{\text{FoF}} (\geq N) \) be the number of mock groups with \( N \) or more members for the best and bijective matches, respectively.

We define the completeness \( c^{\text{best}}(N) \) and \( c^{\text{bij}}(N) \) as the fraction of real groups with \( N \) or more members that are successfully recovered in the reconstructed group catalogue corresponding to the best and bijective matches, respectively:

\[
c^{\text{best}}(N) = \frac{N^{\text{best}}_{\text{FoF}} (\geq N)}{N^{\text{real}}_{\text{FoF}} (\geq N)}, \tag{F1}
\]

\[
c^{\text{bij}}(N) = \frac{N^{\text{bij}}_{\text{FoF}} (\geq N)}{N^{\text{real}}_{\text{FoF}} (\geq N)}. \tag{F2}
\]

Similarly, if \( N^{\text{best}}_{\text{FoF}} (\geq N) \) and \( N^{\text{bij}}_{\text{FoF}} (\geq N) \) denote the number of FoF groups with \( N \) or more members in the best and bijective matches, respectively, the purity \( p^{\text{best}}(N) \) and \( p^{\text{bij}}(N) \) are defined as the fractions of reconstructed groups with \( N \) or more members belonging to real groups:

\[
p^{\text{best}}(N) = \frac{N^{\text{best}}_{\text{FoF}} (\geq N)}{N^{\text{real}}_{\text{FoF}} (\geq N)}, \tag{F3}
\]

\[
p^{\text{bij}}(N) = \frac{N^{\text{bij}}_{\text{FoF}} (\geq N)}{N^{\text{real}}_{\text{FoF}} (\geq N)}. \tag{F4}
\]

By definition, the quantities \( c^{\text{best}}, c^{\text{bij}}, p^{\text{best}}, \) and \( p^{\text{bij}} \) take values between 0 and 1. The completeness is one if all real groups are reconstructed, while it is 0 if no real group is detected. Similarly, the purity is 1 if all reconstructed groups are matched with real groups, 0 if all reconstructed group are spurious (none is associated with any real group).

For each mock catalogue, we define fragmentation as the inverse of the number of FoF groups it is matched with. For each FoF group overmerging is given as the inverse of the number of mock groups it is matched with. These quantities are well defined only for groups that have been actually matched (bijective or best match). Fragmentation (overmerging) is equal to one if each matched mock (FoF) group is associated with only one FoF (mock) group and the smaller the values are, the more FoF (mock) groups are associated with a given mock (FoF) group.

The galaxy success rate \( S_{\text{gal}}(N) \) is defined as the fraction of galaxies in real groups with \( N \) or more members that are found to belong to any reconstructed group with two or more members. For best and bijective matches, these definitions become:

\[
s^{\text{best}}_{\text{gal}} = \frac{N^{\text{best}}_{\text{FoF}} (\geq N)}{N^{\text{real}}_{\text{FoF}} (\geq N)}, \tag{F5}
\]

\[
s^{\text{bij}}_{\text{gal}} = \frac{N^{\text{bij}}_{\text{FoF}} (\geq N)}{N^{\text{real}}_{\text{FoF}} (\geq N)}, \tag{F6}
\]

respectively.

We define the interloper fraction \( f_{i}(N) \) as the fraction of galaxies in reconstructed groups having \( N \) or more members that do not belong to any matched real group of richness \( \geq 2 \). We again distinguish best and bijective matches:

\[
f_{i}^{\text{best}} = \frac{N^{\text{best}}_{\text{FoF}} (\geq N) - N^{\text{best}}_{\text{mock}} (\geq N)}{N^{\text{mock}} (\geq N)}, \tag{F7}
\]

\[
f_{i}^{\text{bij}} = \frac{N^{\text{bij}}_{\text{FoF}} (\geq N) - N^{\text{bij}}_{\text{mock}} (\geq N)}{N^{\text{mock}} (\geq N)}. \tag{F8}
\]

In the above definitions, an interloper is defined as any galaxy in a reconstructed group not belonging to its matched real group. We also define interlopers as field galaxies that end up in reconstructed groups. The corresponding interloper fraction \( f_{i,\text{field}}(N) \) is the fraction of galaxies belonging to reconstructed groups with \( N \) or more galaxies that are field galaxies. \( S_{\text{gal}}, f_{i}, \) and \( f_{i,\text{field}} \) take values in the range 0–1. By definition, \( f_{i,\text{field}} \) is lower or equal to \( f_{i} \) (equal if all interlopers are field galaxies).

All of the above-defined quantities can be combined into three statistical measures of quality of our group reconstruction as follows:

\[
g_{1} = \sqrt{(1 - c^{\text{best}})^2 + (1 - p^{\text{best}})^2} , \tag{F9}
\]

\[
g_{2} = \text{overmerging}^{\text{best}} \times \text{fragmentation}^{\text{best}} \tag{F10}
\]

and

\[
g_{3} = \sqrt{(1 - S_{\text{gal}}^{\text{best}})^2 + (f_{i}^{\text{best}})^2} . \tag{F11}
\]

For a perfectly reconstructed group catalogue \( c^{\text{best}}, p^{\text{best}}, \) overmerging, fragmentation, and \( S_{\text{gal}} \) are equal to one, and \( f_{i} = 0 \). As the reconstruction of such a perfect catalogue is not possible, the best we can do is to try and find a balance between different quantities that often tend to be exclusive. This is the case of completeness and purity, the balance of which is measured by \( g_{1} \). Increasing the completeness of a group catalogue often results in decreasing its purity (less undetected groups, more spurious ones). Similarly, \( g_{3} \) is a measures of balance between spurious groups and interlopers. \( g_{1} \) and \( g_{3} \) should thus be minimized. A good group catalogue should also avoid overmerging and fragmentation, so \( g_{2} \) should be maximized.

We recall that the purpose of the above-defined measures is not the optimization of the group-finder parameters, but rather an attempt to break the degeneracy between several combinations of potentially optimal parameters. A summary of the statistics computed for \( N \geq 5 \) for such combinations is shown in Table F1. We notice that there is no couple of linking lengths for which all three goodness parameters are optimized at the same time. Based on the argument of symmetry between real and reconstructed group catalogues, we selected in Appendix C the combination of linking lengths (\( b_{\perp}, R \)) = (0.06, 19.0) as being optimal. This set of parameters leads to the highest balance between completeness and purity (lowest \( g_{1} \)), and lowest interloper fraction among all four considered combinations.

The FoF parameters (\( b_{\perp}, R \)) = (0.07, 19.0) result in a catalogue

| \( b_{\perp} \) | \( R \) | \( g_{1} \) | \( g_{2} \) | \( g_{3} \) | \( S_{\text{gal}} \) | \( f_{i} \) |
|---|---|---|---|---|---|---|
| A | 0.06 | 27.5 | 0.016 | 0.724 | 0.308 | 0.772 | 0.208 |
| B | 0.07 | 19.0 | 0.024 | 0.739 | 0.306 | 0.808 | 0.238 |
| C | 0.06 | 19.0 | 0.013 | 0.723 | 0.329 | 0.729 | 0.188 |
| D | 0.07 | 15.0 | 0.021 | 0.733 | 0.318 | 0.776 | 0.226 |

In all the following definitions in this section, if not stated differently, the richness \( N \) refers to the richness of groups that are being matched (mock groups in this case). In the matching procedure, the minimum richness of groups in the reference sample (FoF groups in this case) is two.
with the lowest overmerging and fragmentation (highest $g_2$), and lowest number of spurious groups (highest $S_{\text{gal}}$), again among the four selected combinations. However, they also produce the highest asymmetry between the mock and FoF counterparts. Thus, it seems reasonable to keep $(b_{\perp}, R) = (0.06, 19.0)$ as our best choice of optimal FoF parameters for the construction of our group catalogue.

The following figures illustrate the quality level of this particular reconstructed catalogue. Fig. F1 shows the completeness and purity for the best and bijective matches as a function of richness $N$. The completeness for the best match $c_{\text{best}}$ is about 0.99, showing no dependence on the richness $N$, while the completeness for the bijective match $c_{\text{bij}}$ $\simeq$ 0.84 only shows a weak dependence on $N$. The purity parameters, $p_{\text{best}}^{\text{bij}} \simeq 0.94$ and $p_{\text{bij}}^{\text{bij}} \simeq 0.76$, are also almost independent on richness for $N \geq 3$. For $N = 2$ both purities drop significantly (to $\simeq 0.7$ for $p_{\text{best}}$ and $\simeq 0.56$ for $p_{\text{bij}}$).

Fragmentation and overmerging are shown in Fig. F2. Bijectively matched groups are neither overmerged nor fragmented no matter their richness. For groups matched according to our best criterion, fragmentation is more severe than overmerging. The overall average fragmentation is $\simeq 7.4$, while this value drops to $\simeq 0.65$ for groups with $N \geq 5$. Overmerging decreases with $N$, however only mildly with an average value of $\simeq 0.91$.

The galaxy success rate and interloper fraction, two statistical quantities on a galaxy-to-group basis, are shown in Fig. F3. For both best and bijective matches, these measures show similar dependencies on $N$. The galaxy success rates $S_{\text{gal}}^{\text{best}} \simeq 0.73$ and $S_{\text{gal}}^{\text{bij}} \simeq 0.65$, both decline until $N \simeq 5$, after which the dependence on $N$ weakens. The interloper fraction is overall very low ($f_{\text{I}}^{\text{best}} \simeq 0.17$ and $f_{\text{I}}^{\text{bij}} \simeq 0.09$) with almost no dependence on $N$, except for $N = 2$, where it reaches its minimum value.

Finally, Fig. F4 shows the statistics as a function of redshift for different bins of richness $N$. All quantities are consistent with no or very weak evolution with redshift. Only in the highest redshift bin do we note an increase in purity for groups with $N \leq 4$, and a decrease in completeness and interloper fraction for bijective matches among groups of richness $\geq 10$. 

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**Figure F1.** Completeness (upper panel) and purity (lower panel) as a function of richness $N$ for the best (blue) and bijective (red) matches. The points represent the mean values among the nine mock catalogues and the error bars show their scatter.

**Figure F2.** Fragmentation (upper panel) and overmerging (lower panel) as a function of richness $N$ for the best (blue) and bijective (red) matches.
Figure F3. Galaxy success rate (upper panel) and interloper fraction (lower panel) as a function of richness $N$ for the best (blue) and bijective (red) matches. In the lower panel, the solid line corresponds to the interloper fraction as defined by equations (F7) and (F8), and the dashed line refers to the definition of interlopers as field galaxies ($f_{I,\text{field}}$). For the sake of clarity in the lower panel, error bars are shown only for $f_I$.

Figure F4. Completeness (blue), purity (red), galaxy success rate (green), and interloper fraction (black) as a function of redshift for different bins of $N$. The solid and dotted lines correspond to the best and bijective matches, respectively. For the sake of clarity, error bars and bijective matches are shown only for completeness and purity.

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